

## New results on the search for spin-exotic mesons with COMPASS (diffractively produced on proton)



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## Outline:

- Introduction
  - Spin-exotic mesons & the COMPASS experiment
  - PWA method
- First results on diffractive  $3\pi$  production (2008 proton data)
  - >  $3\pi$  final states neutral vs. charged mode
  - PWA results on main & small waves
- Status on further relevant decay channels
  - $\succ \eta \, \pi, f_1 \pi$  decay channels
- Conclusions & outlook



**bmb+f** - Förderschwerpunkt

COMPASS

Großgeräte der physikalischen Grundlagenforschung





## **Constituent quark model**

- color neutral  $q\overline{q}$  systems
- Quantum numbers  $I^{G} J^{PC}$
- $P = (-1)^{L+1}$   $C = (-1)^{L+S}$   $G = (-1)^{l+L+1}$
- J<sup>PC</sup> multiplets: 0<sup>++</sup>, 0<sup>-+</sup>, 1<sup>--</sup>, 1<sup>+-</sup>, 1<sup>++</sup>, 2<sup>++</sup>, ...
- Forbidden: 0<sup>--</sup>, 0<sup>+-</sup>, 1<sup>-+</sup>, 2<sup>+-</sup>, 3<sup>-+</sup>, ...

Hybrid candidates  $(1.3 - 2.2 \text{ GeV/c}^2)$ : lightest hybrid predicted: exotic  $J^{PC} = 1^{-+}$ \*  $\pi_1(1400)$ : VES, E852, Crystal Barrel  $\rightarrow \eta\pi$ \*  $\pi_1(1600)$ : E852, VES  $\rightarrow p\pi, \eta^*\pi, f_1\pi, b_1\pi$ \*  $\pi_1(2000)$ : E852  $\rightarrow f_1(1285) \pi, b_1(1235) \pi$ .... still controversial  $\rightarrow COMPASS$ 

#### QCD: meson states beyond



#### Diffractive scattering

- study of J<sup>PC</sup> exotic mesons
- t-channel Reggeon exchange
- forward kinematics, target stays intact
- small momentum transfer







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- $\pi_1(1400)$ : VES, E852, Crystal Barrel ->  $\eta\pi$
- $\pi_1(1600)$ : E852, VES ->  $\rho\pi$ ,  $\eta^{`}\pi$ ,  $f_1\pi$ ,  $b_1\pi$
- $\pi_1(2000)$ : E852 ->  $f_1(1285) \pi$ ,  $b_1(1235) \pi$
- .... still controversial → COMPASS

#### QCD: meson states beyond

Glueballs: gg, ggg
Hybrids: qq

gg
Tetraquarks: (qq

)(qq

)

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#### COMPASS (2004 pilot run)

- 190 GeV  $\pi^-$  beam (Pb target)
- studied  $\rho\pi$  decay channel via

 $\pi^- \operatorname{Pb} \longrightarrow \pi^- \pi^+ \pi^- \operatorname{Pb}$ 

=> confirmation of a 1<sup>-+</sup> resonance at 1.66 GeV

#### [PRL 104 (2010) 241803]

#### QCD: meson states beyond



## **Diffractive pion dissociation**

- incoming  $\pi^-$ excited to resonance  $X^-$
- X<sup>-</sup> decays into final state, e.g.  $(3\pi)^-$ :







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### COMPASS (2008/09 data)

- 190 GeV  $\pi^-$  beam (proton target)
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  - a)  $\pi^- \mathbf{p} \longrightarrow \pi^- \pi^+ \pi^- \mathbf{p}$  (charged mode)
  - b)  $\pi^- p \longrightarrow \pi^- \pi^0 \pi^0 p$  (neutral mode)

### QCD: meson states beyond

Glueballs: gg, ggg
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qq
<ul

### **Diffractive pion dissociation**

- incoming  $\pi^-$ excited to resonance  $X^-$
- X<sup>-</sup> decays into final state, e.g.  $(3\pi)^{-}$ :



# **COMPASS spectrometer: Hadron setup 2008/09**







# Diffractive dissociation into 3π final states (2008 data, LH<sub>2</sub> target)



search for  $\pi_1(1600)$ 



PWA: ~ 24M events (acceptance corrected)

PWA: ~ 1M events



# **PWA using isobar model**





#### Partial wave analysis:

- program: Illinois/Protvino/Munich (D.Ryabchikov) software (IHEP/VES, TUM/COMPASS)
- Isobars:  $(\pi\pi)_{S}$  [broad  $f_{0}(600)+f_{0}(1370)$ ],  $f_{0}(980)$ ,  $\rho(770)$ ,  $f_{2}(1270)$ ,  $\rho_{3}(1690)$
- Acceptance: corrections (2008: rather flat for charged, neutral not yet included )

## Step 1) Mass independent PWA: (40MeV/c<sup>2</sup> bins, 53 partial waves)

## **Step 2) Mass dependent** $\chi^2$ **fit:** (to mass independent result)

- Main partial waves chosen, parameterised by Breit-Wigner
- Coherent background for some waves



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= following results

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## Comparison: Neutral vs. charged mode simple isospin symmetry check







#### **Isospin symmetry:** neutral / charge mode

- $X^-$  decaying into  $f_2 \pi$ : 1/2 intensity expected
- X<sup>-</sup> decaying into  $\rho \pi$ : 1/1 intensity expected

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## Two sets of partial wave totals $3\pi$ diffractive -- Neutral vs. Charged mode: 53 waves





#### **Isospin symmetry:** neutral / charge mode

- X<sup>-</sup> decaying into  $f_2 \pi$ : 1/2 intensity expected
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#### Data follows isospin symmetry:

- throughout full wave-set
- main and small waves, next slides

2.2

2.4



# Selected partial waves isospin symmetry check ctd.













# **First glimpse on the exotic wave** $3\pi$ diffractive -- Charged mode: 53 waves



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- $\pi_1(1600)$ : E852, VES  $\rightarrow \rho \pi(\eta, f_1\pi) b_1 \pi$
- $\pi_1(2000)$ : E852  $\rightarrow$   $f_1(1285) \pi$ ,  $b_1(1235) \pi$ .... still controversial  $\rightarrow$  COMPASS

## COMPASS (2008 data)

- 190 GeV  $\pi^-$  beam (proton target)
- study of ρπ decay channel via:
  - a)  $\pi^- p \longrightarrow \pi^- \pi^+ \pi^- p$  (charged mode)
  - b)  $\pi^- p \longrightarrow \pi^- \pi^0 \pi^0 p$  (neutral mode)

### QCD: meson states beyond



## **Diffractive pion dissociation**

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- X<sup>-</sup> decays into final state, e.g.  $(3\pi)^{-}$ :





New results on the spin-exotics search with COMPASS

22/07/2011



# First studies of diffractive dissociation into $K\overline{K}\pi\pi$ final states



**Physics channel:**  $\pi^- p \rightarrow K\overline{K} \pi \pi^- p$  **Motivation:** Search for diffr. X<sup>-</sup> coupling to ss final states **First preliminary PWA started:**  $\overline{K^0}K^+ \pi^- \pi^-$ 

search for  $\pi_1(1600), \pi_1(2000)$ 



Statistics: 2008 data => ~ factor 10 w.r.t. BNL (~20 for 2008/09)



# **Summary & conclusions**



## • COMPASS: high potential for spin-exotic search

- ✓ 2008/09: Very high statistics taken (hadron beams, proton & nuclear targets)
- ✓ COMPASS measures **Neutral & Charged** channels
- => all relevant channels for spin-exotic search feasible

• New physics results presented (incl. exotic signals):

>  $(3\pi)^-$  system studied in both decay modes: charged & neutral (consistent results) => Independent confirmation of new states within same experiment!

 $\succ$  ( $\eta' \pi$ )<sup>-</sup> system shows large intensity in exotic wave (high mass range, to be understood)

>  $(K\overline{K}\pi\pi)^{-}$  system: feasibility shown for  $f_{1}\pi$  decay channel(s)!

→ exemplarily, further kaonic channels, also: <u>Kaon diffraction</u> (using Kaon beam)

#### Outlook:

• More systematic studies, PWA model, Mass-dependent PWA → more work ahead

Not discussed: Low t', Primakoff, Central production, Baryon spectroscopy, OZI violation → Quite rich physics programme: various further ongoing analsyes & results!



## **Summary & conclusions**









# **Additional material**



## Diffractive dissociation into 3π final states (2004 data, Pb target) [PRL 104 (2010) 241803]





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# Physics with the kaon beam: Kaon diffraction







## Further exemplary channels of interest – involving neutrals











# Decay modes of disputed $\pi_1$ (1600)





COMPASS has access to all of these decay modes









Not main goal, but also:

search for  $\pi_1(1600)$ 



No evidence for  $\pi_1(1600)$  Primakoff production, nor for  $\pi_1(1400)$ 

#### Preliminary confirmation of CLAS experiment:

 $\rightarrow$  no spin-exotic 1 <sup>-+</sup> signal in photoproduction

(structures at 1.1 GeV: non-resonating contribution (ChPT), at 1.9 GeV: some leakage)



# **Test of OZI violation**



- Comparison of differential cross sections in ω and φ production (with respect to x<sub>F</sub>, in pp reactions)
- value not yet released, in agreement with expectations
- good feedback received at conference



Top: Fit of  $\phi$  yield in different  $x_F$  bins. The data is not yet acceptance corrected. Bottom: Fit of  $\omega$  yield in the same  $x_F$  binning.

Blue: fit, red: background, green: peak

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## Primakoff production of charged 3pi at low masses



# PWA analysis with amplitude from ChPT calculations substituting isobaric waves at low masses:



First measurement of  $\gamma \pi^- \rightarrow \pi^- \pi^- \pi^+$  cross section in this range

## **Result in agreement with LO Ch.PT calculation**

More data avalable from 2009 running on lead

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## Acceptance for $\pi^-\pi^+\pi^-$ final states



















## **COMPASS:** $p_{\pi}$ =190 GeV/c

- · 4M events in 3 days (full t range)
- 450k events in 0.1<t'<1.0 GeV<sup>2</sup>/ $c^{2}$

**BNL852:** p<sub>π</sub>=18 GeV/c

• 250k events  $\Rightarrow \pi_1(1600)$ 





# **BNL controversial analyses**



E,g.: E852:  $\pi_1(1600) \longrightarrow [\rho^{\circ}\pi -] P$  $\rightarrow$  limited statistics E,g.: E852:  $\pi_1(1600) \longrightarrow [\rho^{\circ}\pi -] P$  $\rightarrow$  full statistics & extended waveset





# Fitted resonances (2004 data)





Resonance	Mass	Width	Intensity	Channel
	$(MeV/c^2)$	$(MeV/c^2)$	(%)	$J^{PC}M^{\epsilon}[isobar]L$
$a_1(1260)$	$1255 \pm 6^{+7}_{-17}$	$367 \pm 9^{+28}_{-25}$	$67 \pm 3^{+4}_{-20}$	$1^{++}0^+ \rho \pi S$
$a_2(1320)$	$1321 \pm 1^{+0}_{-7}$	$110 \pm 2^{+2}_{-15}$	$19.2 \pm 0.6^{+0.3}_{-2.2}$	$2^{++}1^+ \rho \pi D$
$\pi_1(1600)$	$1660 \pm 10^{+0}_{-64}$	$269 \pm 21^{+42}_{-64}$	$1.7 \pm 0.2^{+0.9}_{-0.1}$	$1^{-+}1^+ \rho \pi P$
$\pi_2(1670)$	$1658 \pm 3^{+24}_{-8}$	$271 \pm 9^{+22}_{-24}$	$10.0 \pm 0.4^{+0.7}_{-0.7}$	$2^{-+}0^+ f_2 \pi S$
$\pi(1800)$	$1785 \pm 9^{+12}_{-6}$	$208 \pm 22^{+21}_{-37}$	$0.8 \pm 0.1^{+0.3}_{-0.1}$	$0^{-+}0^{+} f_0 \pi S$
$a_4(2040)$	$1885 \pm 13^{+50}_{-2}$	$294 \pm 25^{+46}_{-19}$	$1.0 \pm 0.3^{+0.1}_{-0.1}$	$4^{++}1^+ \rho \pi G$









#### **Observed M-dependence:**

• production strength for M=1 vs. M=0 states depend on target material

- confirmed on 2009 data → real effect
- interesting to understand physics wise

# **COMPASS spectrometer: Hadron setup 2008/09**







# First comparison: Neutral vs. charged mode simple isospin symmetry check



#### **Isospin symmetry**: neutral / charged mode

- **X**<sup>-</sup> decaying into  $\rho \pi$ : 1/1 intensity expected
- $X^-$  decaying into  $f_2 \pi$ : 1/2 intensity expected

General: Branching not entirely determined by Clebsch-Gordon coeff.,

but also <u>Bose-Symmetrisation</u> with the bachelor  $\pi$ :

 $\Rightarrow$  <u>no effect</u> for resonances decaying into  $\rho\pi$  (same effect)

=> BR <u>might differ</u> for resonances going to  $f_{0,2}\pi$ 

#### Checked by calculation:

BR = N( $\pi^-\pi^0\pi^0$ )/N( $\pi^-\pi^-\pi^+$ ) – calculated from isobar model amplitudes BR( $0^{-+}f_0(980)\pi$  S) = 0.44 (at 1.8 GeV)

BR(  $1^{++}(\pi\pi)_s\pi P$ ) = 0.80 (at 1.3 GeV) BR(  $2^{-+}f_2(1270)\pi S$ ) = 0.50 (at 1.67 GeV)



# Selected partial waves isospin symmetry check ctd.





BR(  $1^{++}(\pi\pi)_s\pi P$ ) = 0.80 (at 1.3 GeV)

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## **Selected partial waves & phases** 3π diffractive -- Neutral vs. Charged mode: 53 waves





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## **Selected partial waves & phases** 3π diffractive -- Neutral vs. Charged mode: 53 waves







## **Decay angles in G.J. frame:** Full PhaseSpace Generated Prediction vs. fitted data





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# Decay angles in G.J. frame Full PhaseSpace Generated Prediction







# **PWA using isobar model**





#### Partial wave analysis:

- program: Illinois/Protvino/Munich (D.Ryabchikov) software (IHEP/VES, TUM/COMPASS)
- Isobars:  $(\pi\pi)_{S}$  [broad  $f_{0}(600)+f_{0}(1370)$ ],  $f_{0}(980)$ ,  $\rho(770)$ ,  $f_{2}(1270)$ ,  $\rho_{3}(1690)$
- Acceptance: corrections (2008: rather flat for charged, neutral not yet included )

## Step 1) Mass independent PWA: (40MeV/c<sup>2</sup> bins, 53 partial waves)

$$\sigma_{indep}(\tau, m, t') = \sum_{\epsilon = \pm 1} \sum_{r=1}^{N_r} \left| \sum_i T_{ir}^{\epsilon} f_i^{\epsilon}(t') \psi_i^{\epsilon}(\tau, m) / \sqrt{\int \left| \psi_i^{\epsilon}(\tau', m) \right|^2 d\tau'} \right|^2$$

- Production amplitudes  $\mathcal{T}^{\epsilon}_{ir} \rightarrow$  extended maximum likelihood fit
- Decay amplitudes  $\psi_i^{\epsilon}(\tau, m)$  (Zemach tensors, D functions)



## Waveset used for the PWA



	$J^{PC}M^{\epsilon}$	L	Isobar $\pi$	Treshold $(\text{GeV}/c^2)$					
-	$0^{-+}0^{+}$	S	$f_0(980)\pi$	1.25					
	$0^{-+}0^{+}$	S	$(\pi\pi)_s\pi$	-					
	$0^{-+}0^{+}$	P	$ ho\pi$	-					
-	$1^{-+}1^{+}$	P	$\rho\pi$	-					
-	$1^{++}0^{+}$	S	$\rho\pi$	-					
	$1^{++}0^{+}$	P	$f_2\pi$	1.20		2++1+	P	$f_2\pi$	1.20
	$1^{++}0^{+}$	P	$(\pi\pi)_s\pi$	0.94	$\rightarrow$	$2^{++}1^{+}$	D	$ ho\pi$	-
	$1^{++}0^{+}$	D	$\rho\pi$	1.30		3++0+	S	$ ho_3 \pi$	1.76
	$1^{++}1^{+}$	S	$\rho\pi$	-		$3^{++}0^{+}$	$\left  \begin{array}{c} P \\ D \end{array} \right $	$f_2\pi$	1.20
	$1^{++}1^{+}$	P	$f_2\pi$	1.40		$3^{++}1^{+}$	$\begin{bmatrix} D\\S \end{bmatrix}$	$\rho_3\pi$	$1.20 \\ 1.76$
	$1^{++}1^{+}$	P	$(\pi\pi)_s\pi$	1.20		$3^{++}1^{+}$	P	$f_2\pi$	1.20
	$1^{++}1^{+}$	D	$\rho\pi$	1.40		3++1+	D	$\rho\pi$	1.50
	$2^{-+}0^{+}$	S	$f_2\pi$	1.20		$4^{-+}0^{+}$	$\begin{bmatrix} F \\ F \end{bmatrix}$	$\rho\pi$	1.00
	$2^{-+}0^{+}$	P	$\rho\pi$	0.80		$\frac{4}{4^{++}1^{+}}$	$\frac{\Gamma}{F}$	$\frac{\rho_{\pi}}{f_{2}\pi}$	1.60
	$2^{-+}0^{+}$	D	$(\pi\pi)_s\pi$	0.80	-	$4^{++}1^{+}$	G	$\rho\pi$	1.40
	$2^{-+}0^{+}$	D	$f_2\pi$	1.50		1-+0-	P	$\rho\pi$	-
	$2^{-+}0^{+}$	F	$\rho\pi$	1.20		$1^{-+}1^{-}$	P	$ ho\pi$	-
	$2^{-+}1^{+}$	S	$f_2\pi$	1.20		$1^{++}1^{-}$ $9^{-+}1^{-}$	$\frac{S}{S}$	$ ho\pi$	- 1.20
	$2^{-+}1^{+}$	P	$\rho\pi$	0.80		$2^{++}0^{-}$	$\left  \begin{array}{c} D \\ P \end{array} \right $	$f_2\pi$	1.20 1.30
	$2^{-+}1^{+}$	D	$(\pi\pi)_{\circ}\pi$	1.20		$2^{++}0^{-}$	D	$\rho\pi$	-
	$2^{-+}1^{+}$	D	$f_{2}\pi$	1.50		2++1-	P	$f_2\pi$	1.30
	$2^{-+}1^{+}$	F	$\rho\pi$	1.20		FLAT			

Table 5: List of the 42 waves used for the mass independent PWA



## **Updated PWA model: 53waves**



					2++1+	P	$f_{\alpha}\pi$	1.20
$J^{PC}M^{\epsilon}$	L	Isobar $\pi$	Treshold $(\text{GeV}/c^2)$		$2^{++}1^{+}$	$\begin{bmatrix} I \\ D \end{bmatrix}$	$\rho\pi$	-
$0^{-+}0^{+}$	S	$f_0(980)\pi$	1.25		$3^{++}0^{+}$	S	$\rho_3 \pi$	1.76
$0^{-+}0^{+}$	S	$(\pi\pi)_{\circ}\pi$	-		$3^{++}0^{+}$	P	$f_2\pi$	1.20
0-+0+	$\tilde{P}$	$\alpha\pi$	_		$3^{++}0^{+}$	D	$ ho\pi$	1.20
1-+1+		$\rho\pi$			$3^{++}1^{+}$	S	$ ho_3\pi$	1.76
$\frac{1}{1++0+}$		$\rho_{\pi}$	-		$3^{++}1^{+}$	P	$f_2\pi$	1.20
1++0+	5	$\rho\pi$	-		$\frac{3^{++}1^{+}}{4^{-+}0^{+}}$	D	$ ho\pi$	1.50
1++0+	P	$f_2\pi$	1.20		$4^{-+}0^{+}$	$\begin{bmatrix} F \\ F \end{bmatrix}$	$\rho\pi$	1.00
$1^{++}0^{+}$	P	$(\pi\pi)_s\pi$	0.94		4 1		$\frac{\rho \pi}{f_{-} \pi}$	1.20
$1^{++}0^{+}$	D	$\rho\pi$	1.30		$4^{++1}$	$\Gamma$	$J_{2\pi}$	1.00
$1^{++}1^{+}$	S	$ ho\pi$	-		<u>+0-</u>		<i>Ρ</i> <sup>π</sup>	1.40
$1^{++}1^{+}$	P	$f_2\pi$	1.40		1-+1-	P	$\rho\pi$ $\rho\pi$	_
$1^{++}1^{+}$	P	$(\pi\pi)_s\pi$	1.20		$1^{++}1^{-}$	$\begin{bmatrix} 1\\ S \end{bmatrix}$	$\rho\pi$	_
$1^{++}1^{+}$	D	ρπ	1.40		$2^{-+}1^{}$	S	$f_2\pi$	1.20
$2^{-+}0^{+}$	S	$f_2\pi$	1.20		$2^{++}0^{-}$	P	$f_2\pi$	1.30
$2^{-+}0^{+}$	P	$\rho\pi$	0.80		$2^{++}0^{-}$	D	$ ho\pi$	-
$2^{-+}0^{+}$		$(\pi\pi)_{-}\pi$	0.80		$2^{++}1^{-}$	P	$f_2\pi$	1.30
$2^{-+0^+}$		$f_0\pi$	1.50		FLAT			
$2^{-+0+}$		$\int 2\pi$	1.30	Table 5: List of the	49 wovog 1	read f	for the mas	s independent PWA (T
2 0 0 -+1+		$f_{\pi}$	1.20	Table 5. List of the	42 waves t	iseu i	$1 \left( 0 \right)$	$\Delta = c \Delta (1 \Box \Delta \Delta)$
2 - 1 + 1 + 1 + 1 + 1 + 1 + 1 + 1 + 1 + 1		$J_{2\pi}$	1.20		1		1 - (0 - +)	0+ f0(1500) p1
$2^{-1}$		$\rho\pi$	0.80				1 - (2 + +)	2+ rho pi D
$2 \cdot 1$		$(\pi\pi)_s\pi$	1.20				1 - (2 - +)	2+ f2 pi S
2-+1+	D	$f_2\pi$	1.50				- ( <b>-</b> ) 1_(5++)	$0 \pm rho ni C$
$2^{-+}1^{+}$	F	$\rho\pi$	1.20				I = (0++)	
							I - (6 - +)	0+ rho pı H
							1 - (0 - +)	0+ f2 pi D
							1 - (1 - +)	1+ f2 ni D
A2	14/4	nvocot	extended h	waves	・  ノ		1 (0 .)	
76	WV (	78561	eviencea r	y II wuves	·   )		1 - (2 - +)	U+ rno3 p1 P
<u> </u>							1 - (3 + +)	0+ f0(1400) pi

