

New advances in the Trojan Horse Method as an indirect approach to Nuclear Astrophysics









The Trojan Horse Method

Indirect technique to measure charged particle two body cross sections at astrophysical energies

Astrophysical energies are determined by the Gamow peak: the most effective energy region for thermonuclear reactions



The Gamow energy $E_0 = f(Z_1, Z_2, T)$ varies depending on the <u>reaction</u> and/or the <u>temperature</u>, usually from tens to hundreds of keV.

Why we need indirect techniques?

Charged particle cross section measurements at astrophysical energies

 σ ~picobarn \Rightarrow Low signal-to-noise ratio due to the Coulomb barrier between the interacting nuclei

Extrapolation from the higher energies by using the

ASTROPHYSICAL FACTOR

S(E) = σ (E) E exp(2πη)

S(E) is a smoothly varying function of the energy than the cross section $\sigma(E)$

but large uncertainties in the extrapolation

→ EXPERIMENTAL IMPROVEMENTS/SOLUTIONS



- > to increase the number of detected particles
- > to reduce the background





In astrophysical plasma:

- the screening, due to free electrons in plasma, can be different \rightarrow we need S(E)_b to evaluate reaction rates



A theorical approach to extract the electron screening potential U_e in the laboratory is needed

Experimental studies of reactions involving light nuclides have shown that the observed exponential enhancement of the cross section at low energies were in all cases significantly larger

(about a factor of 2)

than it could be accounted for from available atomic-physics model, i.e. the adiabatic limit $(U_e)_{ad}$

Although we try to improve experimental techniques to measure at very low energy \rightarrow \rightarrow

5,(E)-factor extracted from <u>extrapolation</u> of higher energy data

... new methods are necessary

- to measure cross sections at never reached energies
- to get independent information on ${\rm U}_{\rm e}$



Asymptotic Normalization Coefficients (ANC)

Coulomb dissociation

Trojan Horse Method (THM)

...to extract direct capture cross sections using peripheral transfer reactions

...to study radiative capture reactions

...to extract charged particle reaction cross sections using the quasi-free mechanism...



Basic principle: astrophysically relevant two-body σ from quasi- free contribution of an appropriate three-body reaction

 $A + a \rightarrow c + C + s \rightarrow \rightarrow \rightarrow A + x \rightarrow c + C$

a: $x \oplus s$ clusters





 $A + a \rightarrow c + C + s \rightarrow \rightarrow \rightarrow A + x \rightarrow c + C$

PWIA hypotheses:

-A does not interact simultaneously with x and s

- The presence of s does not influence the A-x interaction

$\frac{d^{\mathfrak{s}} \mathfrak{b}}{d \mathbf{G}_{\mathfrak{c}} d \mathbf{G}_{\mathfrak{c}} d \mathsf{E}_{\mathfrak{c}}} = \mathbf{C} \cdot \mathsf{KF} \cdot \left| (\mathfrak{S} \mathbf{p}_{\mathfrak{s}})^{\mathfrak{s}} \frac{d \mathfrak{B}}{d \mathbf{G}} \right|$

MPWBA formalism

(S. Typel and H. Wolter, Few-Body Syst. 29 (2000) 75)

- distortions introduced in the c+C channel, but plane waves for the three-body entrance/exit channel

- off-energy-shell effects corresponding to the suppression of the Coulomb barrier are included

but No absolute value of the cross section

KF kinematical factors

 $|\phi|^2$ momentum distribution of *s* inside *a*

 $d\sigma^N/d\Omega$ Nuclear cross section for the A+x→C+c reaction

A. Tumino et al., PRL 98, 252502 (2007)

Typical experimental set-up

Very simple, consisting of few telescopes



Chambers

E-detector: Position sensitive detector (500 to 1000 μ m thick)

Selection of quasi-free contribution

Angular correlation analysis

coincidence spectra projected onto an E axis for a fixed θ_1 and different θ_2

events corresponding to a quasi-free mechanism show an enhancement of the yield for p_3 approaching zero (QF angles).

Example for the ³He + ⁶Li $\rightarrow \alpha$ + p + α : ⁴He-d relative motion within ⁶Li in s-wave

Large background contribution: sequential decay through the ⁸Be first excited state (already seen in a previous experiment (Zadro et al. (1987))



Selection of quasi-free contribution **Momentum Distribution**

An observable which turns out to be very sensitive to the reaction mechanism is the shape of the experimental momentum distribution



extracted experimental momentum distribution is compared with the theoretical one. For p-n system it is given by the Hulthén wave function in momentum space:

$$G^2(\mathbf{p}_s)=N\left[\frac{1}{a^2+\mathbf{p}_s^2}-\frac{1}{b^2+\mathbf{p}_s^2}\right]^2$$

N: normalization parameter

 $a= 0.2317 \text{ fm}^{-1}$

b= 1.202 fm⁻¹

Extraction of the 2-body cross section

Monte Carlo simulation of the threebody cross section under the assumptions:

- PWIA/DWBA approach
- Quasi-free contribution is the only reaction mechanism
- a p_s window of 20 MeV/c is considered

 $\sigma_{bare}(E) = \frac{Coincidence yield}{KF |\phi(p_s)|^2 P_0^{-1}}$



Spitaleri et al, PRC 69, 55806 (2004)

The indirect THM cross section $\sigma_{\text{bare}}(E)$ is normalized to the direct data at high energies, where the electron screening is negligible

		Indirect	E_{inc}	Q_2	THM-Nucl.
	Reaction	reaction	(MeV)	(MeV)	Cluster-x
1	⁷ Li(p, α) ⁴ He	² H(⁷ Li, $\alpha \alpha$)n	19-22	15.122	² H (p)
2	⁷ Li(p, α) ⁴ He	⁷ Li(³ He, $\alpha \alpha$) ² H	33	11.853	³ He (p)
3	⁶ Li(p, α) ³ He	² H(⁶ Li, <i>a</i> ³ He) <i>n</i>	14,25	1.795	² H (p)
4	$^6\mathrm{Li}(d,lpha)^4\mathrm{He}$	⁶ Li(³ He, $lpha lpha$) ¹ H	17.5	16.879	³ He (d)
5	6 Li(d , $lpha$) 4 He	⁶ Li(⁶ Li, $lpha$ $lpha$) ⁴ He	5	22.372	⁶ Li (d)
6	${}^{9}\text{Be}(p, \alpha){}^{6}\text{Li}$	² H(¹⁰ Be, α ⁶ Li) <i>n</i>	22.35	-0.099	²Н (р)
7	$^{10}\mathrm{B}(p, \alpha)^{7}\mathrm{Be}$	2 H(10 B, α 7 Be) <i>n</i>	24.4	-1.079	² H (p)
7	¹¹ B(p, α) ⁸ Be	2 H(11 B, $\alpha {}^{8}$ Be)n	27	6.36	² H (p)
8	15 N(<i>p</i> , α) 12 C	2 H(15 N, α 12 C)n	60	2.74	² H (p)
9	$^{17}{\rm O}(p, \alpha)^{14}{\rm N}$	2 H(17 O, α 14 N) <i>n</i>	45	-1.032	² H (p)
10	$^{18}\mathrm{O}(p,lpha)^{15}\mathrm{N}$	2 H(18 O, $lpha$ 15 N) n	54	1.76	² H (p)
11	³ He(<i>d</i> , <i>p</i>) ⁴ He	⁶ Li(³ He, <i>p</i> ⁴ He) ⁴ He	5,6	16.879	⁶ Li (d)
12	² H(<i>d,p</i>) ³ H	² H(⁶ Li, <i>p</i> ³ He) ⁴ He	14	2.59	⁶ Li (d)
13	² H(<i>d,p</i>) ³ H	² He(<i>d,p</i> ³ H) ¹ H	18	-1.46	³ He(d)
14	² H(<i>d,n</i>) ³ He	² H(<i>d,n</i> ³ He) ¹ H	18	-2.224	³ He(d)
15	$^{12}\mathrm{C}(\alpha,\alpha)^{12}\mathrm{C}$	⁶ Li(¹² C,α ¹² C) ² H	20,16	0	⁶ Li (α)
16	⁶ Li(<i>n, t</i>) ⁴ He	2 H(6 Li, $t lpha$) 1 H	14	2.224	² H (n)
17	¹ H(<i>p</i> , <i>p</i>) ¹ H	² H(<i>p, p p</i>) <i>n</i>	5,6	2.224	² H(p)
18	19 F(<i>p</i> , α) 16 O	19 F(p, $\alpha {}^{16}$ O)n	50	8.11	² H (p)

Table XI.1. Two-Body reactions studied via Trojan Horse Method.

Reactions recently studied

⁶Li + d $\rightarrow \alpha$ + α via ⁶Li+⁶Li $\rightarrow \alpha$ + α + α S₀= 16.9 MeV b

U_e ^(ad)	U_e (THM) ⁶ Li+d	U_e (Dir) ⁶ Li+d
186 eV	$\textbf{340} \pm \textbf{50} \text{ eV}$	$\textbf{330} \pm \textbf{120} ~ \textbf{eV}$

⁷ Li+p $\rightarrow \alpha + \alpha$ via ⁷ Li+d $\rightarrow \alpha + \alpha + n$ S ₀ = 55 ± 3 keV b									
U _e (ad)	U_e (THM) 7	′Li+p	U _e (Dir)	⁷ Li+p					
186 eV	330 ± 40) eV	300 ± 3	160 eV					
⁶ Li+p $\rightarrow \alpha$ + ³ He via ⁶ Li+d $\rightarrow \alpha$ + ³ He+n S ₀ = 3.± 0.9 MeV b									
U _e (ad)	U _e (THM) 6[_i+p	$U_{e}^{(Dir)}$	⁶ Li+p					
186 eV	435 ± 40 eV		440 ± 80 eV						
	(C. Spitaleri	i et al., PRC6	0 (1999)0558					
		C. Spitaleri	i et al., PRC6	3 (2001) 0058					

A. Tumino et al., PRC67 (2003) 065803



¹¹B(p, α_0)⁸Be: direct and indirect data

Astrophysical factor

Direct reaction at astrophysical energies proceeds through an intermediate state of ${}^{12}C$ at 16.1 MeV \rightarrow Very important result: resonance reproduced through the indirect approach!

 $S(0)_{b} = 2.2 \pm 0.3 \text{ MeV b}$



-2H+2H reactions in the primordial nucleosynthesis



-Other contexts of interest

- In the Pre Main Sequence phase (PMS) of the stellar

- In the future fusion power plants: nuclear energy production with inertial confinement

Range of interest : 0-30 keV

d+d->3He+n two-body cross section

Comparison between THM data (black dots) and direct data (colored symbols)

<u>Yellow line:</u> polynomial expansion reported in the NACRE compilation

<u>Blue line:</u> calculation from the Cyburt compilation

Green line: calculation by

P. Descouvemnont et al.

C. Angulo *et al.*, Nucl. Phys. A656, 3 (1999)
R.H. Cyburt, Phys. Rev. D70, 023505 (2004)
P. Descouvemont *et al.*, At. Data Nucl. Data Tables 88, 203 (2004)



A. Tumino et al., Few Body Syst. 50 (2011) 323 A.Tumino et al., Phys. Lett. B 700 (2011) 111

²H(³He,n ³He)p



²H(³He,p ³H)p

Symbols and lines with same meaning as in the previous figure

Screening potential estimate

 $f_{lab}(E) = exp(U_e/E)$ (Assenbaum, H.J. et al., 1987, Z. Phys. A, 327, 461)

 $\rightarrow U_e = 13.2 \pm 1.8 \text{ eV}$

In agreement with the adibatic limit



Recent results for resonant reactions

...reactions belonging to the ¹⁹F production/destruction path

¹²C(p,γ)¹³N(β⁺)¹³C [¹³C-pocket?] ¹³C(α,n)¹⁶O [s-process] ¹⁴N(n,p)¹⁴C ¹⁴C(α,γ)¹⁸O or ¹⁴N(α,γ)¹⁸F(β⁺)¹⁸O ¹⁸O(p,α)¹⁵N → ¹⁵N(p,α)¹²C ¹⁸O(α,γ)²²Ne ¹⁵N(α,γ)¹⁹F → ¹⁹F(α,p)²²Ne

¹⁹F depleting reactions

The importance of ¹⁹F in astrophysics:

 its abundance observed in red giants can constrain AGB star models

Open problem:

 fluorine abundance in red giants is enhanced by large factors with respect to the solar one



This would imply C/O values much larger than what experimental data suggest

The 180(p,a)15N Reaction: Current Status



~50 resonances in the 0-7 MeV region

The main contribution to the reaction rate is given by the resonances:

1- 20 keV $J^{\pi}=5/2^+$ 2- 144 keV $J^{\pi}=1/2^+$ (well established) 3- 656 keV $J^{\pi}=1/2^+$

The Trojan horse method for resonant reactions

In the THM the astrophysically relevant reaction, in particular $^{17,18}O(p,\alpha)^{14,15}N$, studied through an appropriate three-body process $^{2}H(^{17,18}O,\alpha^{14,15}N)n$:



The process is a transfer to the continuum where proton (p) is the transferred particle

Standard R-Matrix approach cannot be applied to extract the resonance parameters of the ¹⁸O(p, α)¹⁵N \rightarrow Modified R-Matrix is introduced instead

In the case of a resonant THM reaction the cross section takes the form

$$\frac{d^2\sigma}{dE_{Cc}\,d\Omega_s} \propto \frac{\Gamma_{(Cc)_i}(E)\,|M_i(E)|^2}{(E-E_{R_i})^2 + \Gamma_i^2(E)/4}$$

M_i(E) is the amplitude of the transfer reaction (upper vertex) that can be easily calculated → The resonance parameters can be extracted and in particular the strenght

How to extract the resonant strength?

When narrow resonances dominate the S-factor the reaction rate can be calculated by means of the resonance strength:

$$(\omega\gamma)_{i} = \frac{\hat{J}_{i}}{\hat{J}_{p}\hat{J}_{^{18}\mathrm{O}}} \frac{\Gamma_{(p^{18}\mathrm{O})_{i}}(E_{R_{i}}) \ \Gamma_{(\alpha^{15}\mathrm{N})_{i}}(E_{R_{i}})}{\Gamma_{i}(E_{R_{i}})}$$

(¹⁸O(p,α)¹⁵N case)

Where:

- Ĵ=2J+1
- $\Gamma_{(AB)}$ is the partial width for the A+B channel
- Γ_i is the total width of the i-th resonance
- E_{Ri} is the resonance energy

→Area of the Breit-Wigner describing the resonance

 \rightarrow no need to know the resonance shape

$$(\omega\gamma)_i = \frac{1}{2\pi} \omega_i N_i \frac{\Gamma_{(p^{18}\mathcal{O})_i}}{|M_i|^2}$$

Where: • $\omega_1 = \hat{J}_i / \hat{J}_p \hat{J}_{180}$ statistical factor

- N_i = THM resonance strength
- M_i = transfer amplitude

Advantages:

- possibility to measure down to zero energy
- No electron screening
- No spectroscopic factors in the $\Gamma_{(p180)}$ / $|M_i|^2$ ratio

¹⁸O + $p \rightarrow \alpha$ + ¹⁵N THM Results



¹⁷O + p $\rightarrow \alpha$ + ¹⁴N: recent experiment at LNS

Importance in novae nucleosynthesis and γ astronomy

It affects the production of 18F removing ¹⁷O from the production path

It influences the ¹⁷O/¹⁶O isotopic ratio, playing a crucial role to constrain extra mixing processes in AGB stars

$$(\omega \gamma)_1 = (3.66^{+0.76}_{-0.64}) \times 10^{-9} \text{ eV}$$



eV

THM reaction rate about 20% smaller than the most recent value reported in literature: screening effect?

$$f_{lab} = \frac{(\omega\gamma)_{Chafa}}{(\omega\gamma)_{THM}} = e^{\pi\eta(E_{R_i})\frac{U_e}{E_{R_i}}}$$

$$\rightarrow$$
 U_e = 1080 eV U_{AD} = 594

The ¹⁵N + p $\rightarrow \alpha$ + ¹²C: Astrophysical S-factor

- Results reported in terms of S(E) factors:
- THM data as red dots
- Direct data from NACRE as black + open dots

Standard R-Matrix approach cannot be applied to extract the resonance parameters of the ${}^{15}N(p,\alpha){}^{12}C \rightarrow$ Modified R-Matrix is introduced instead

R-matrix calculation assuming a little destructive interference between the 300 keV, 962 keV (12.44 and 13.09 MeV states of ¹⁶O) resonances and a subthreshold one (¹⁶O level at E_{exc} = 9.58 MeV), all of them with J^{π} = 1⁻

Data very well reproduced!



$S_{bare}(0)=62 \pm 10 \text{ MeVb}$

M. La Cognata et al. PRC 76, 065804 (2007)





Reaction rate: uncertainty of about 14 orders of magnitude

The ${}^{19}F(\alpha,p){}^{22}Ne$ reaction

¹⁹F(α ,p)²²Ne: main ¹⁹F destruction channel AGB stars with M>2 M_o and WR stars (~30 M_o)

T → 2 10⁸ K ⇒ Energies of interest 300-800 keV

Most recent measurement (2006) down to 800 keV \Rightarrow Extrapolation impossible because of the many

resonances

The rate is calculated by using simplified models





The ${}^{16}O + {}^{12}C$ experiment

Currently a great interest in the fusion channel in the low energy region because of its critical role in studying a wide range of stellar burning scenarios in carbon-rich environments \rightarrow constraints on the models

¹²C+ ¹²C $\rightarrow \alpha$ + ²⁰Ne ¹²C+ ¹²C \rightarrow p + ²³Na ¹²C+ ¹²C \rightarrow n + ²³Mg

Carbon burning temperature from 0.8 to 1.2 GK, corresponding to center-of-mass energies E_{cm} from 1 to 3 MeV

Measured down to $E_{cm} = 2.14$ MeV, still at the beginning of the region of astrophysical interest.

Extrapolation from current data to the ultra-low energies is complicated by the presence of resonant structures even in the low-energy part of the excitation function

Further measurements extending down to 1 MeV would be extremely important!

December 2011: ¹⁴N run at LNS



 $\left(rac{d\sigma}{d\Omega}
ight)_{p1p2-cm} rac{\sigma}{dE_{p1}d\Omega_{p1}d\Omega_{p2}}$ $\left|\phi(p_s)\right|^2 KF$

p+p elastic scattering via

 $p+d \rightarrow p+p+n$

THM p-p cross-section shows the 1/E behaviour also in the region of the expected Coulomb+nuclear interference:

Coulomb effects appear completely suppressed

NO MI

A. Tumino et al. PRL 98, 252502 (2007) A. Tumino et al. PRC 67, 065803 (2008)



Deuteron-Beam as a virtual Neutron-beam



New results from a recent experiment: magnifying glass effect in the resonant region...

A. Tumino et al., EPJ A (2005) 1 M. Gulino et al., JPG (2010) ⁶Li(n, α)³H via ⁶Li(d, α ³H)p reaction

E_{6Li} =14 MeV

The good agreement between THM and direct data suggests that no offenergy shell effects other than those deriving from the Coulomb barrier, when present, should be considered





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