

# Brain dynamics and fractal behavior: about (fast) EEG microstates and (slow) fMRI resting-state networks

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joint work with Juliane Britz and Christoph Michel

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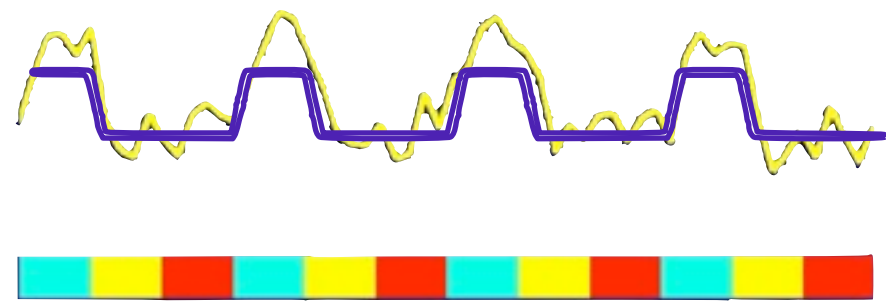
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<http://miplab.epfl.ch/>

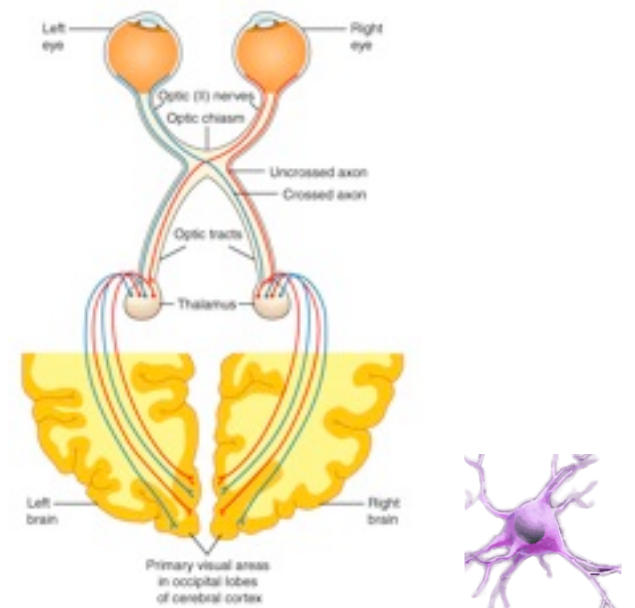
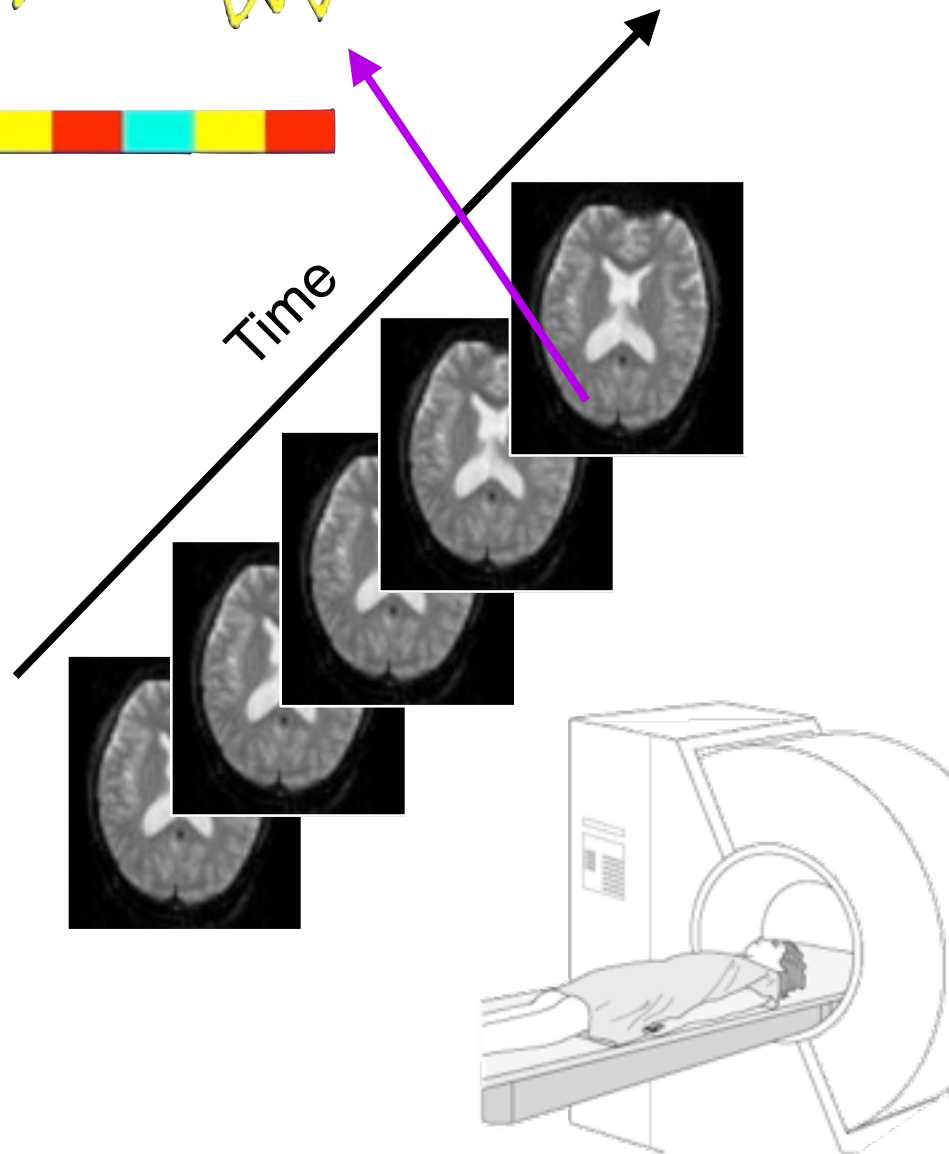
**Villars, September 6, 2011**

# FMRI in a nutshell

*Is there a face-selective brain region?*

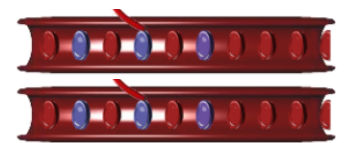


whole-brain scans  
2x2x2mm<sup>3</sup>  
20-30 slices  
every 2-4s



neurovascular coupling  
hemodynamics

T2\* effect  
BOLD response



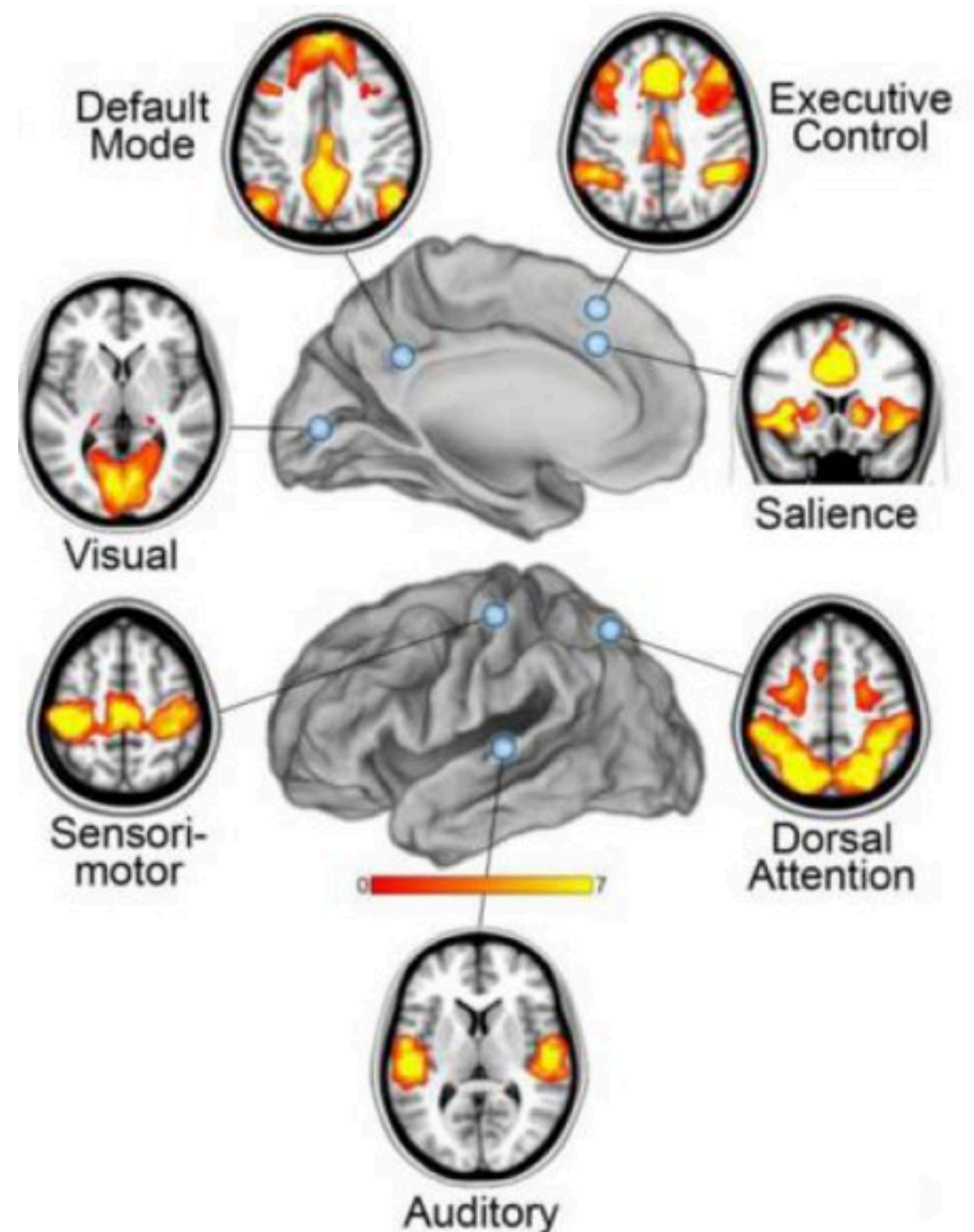
# Resting-state fMRI

- Evoked activity
  - Brain consumes 20% of energy budget
    - only 5% is needed for stimuli
    - 95% to maintain the machine
  - Consistent “deactivation” pattern in neuroimaging data such as PET and fMRI

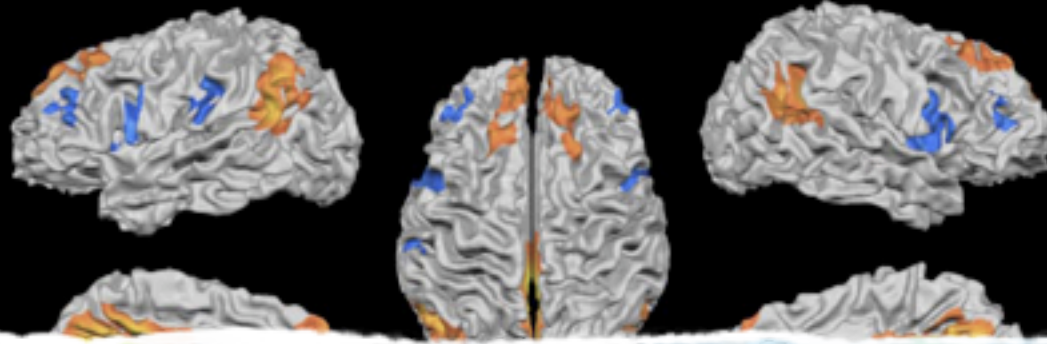


# Resting-state fMRI

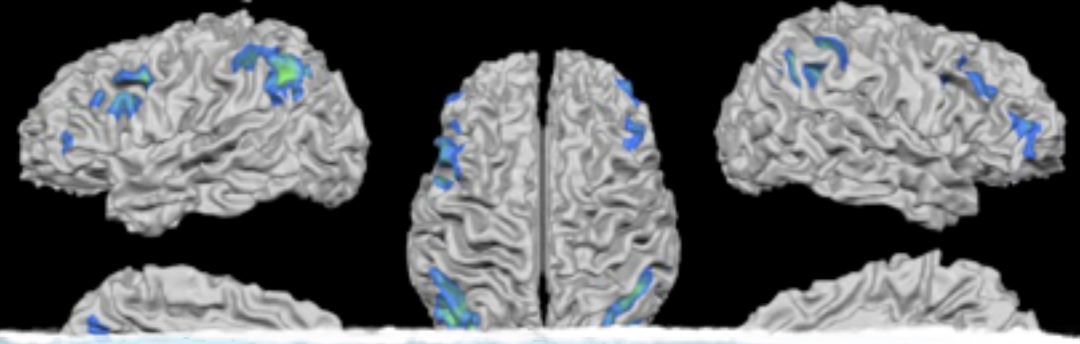
- Evoked activity
  - Brain consumes 20% of energy budget
    - only 5% is needed for stimuli
    - 95% to maintain the machine
  - “Deactivation” pattern in neuroimaging data such as PET and fMRI
- Intrinsic activity
  - *Seed voxel correlation*
  - Distinctive patterns of brain activity
  - Relevance for neurological disorder & disease



RSN 1



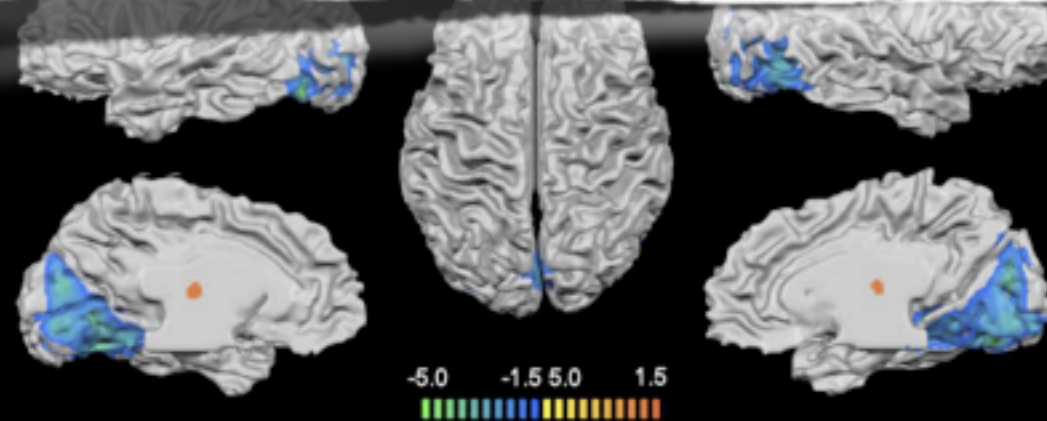
RSN 2



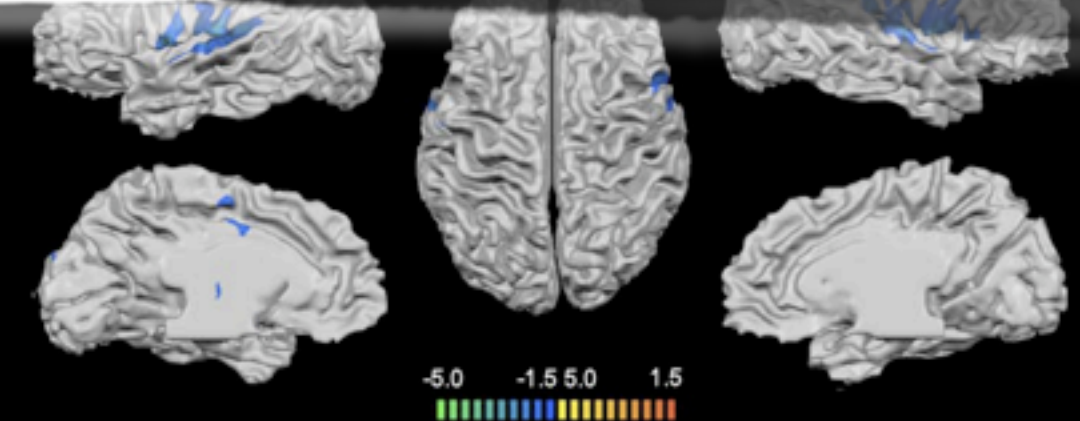
“Resting states reflect the intrinsic activity of anatomically connected networks [...] rather than spontaneous behavior or conscious mentation”

[Fox & Raichle, Nature Review Neuroscience, 2007]

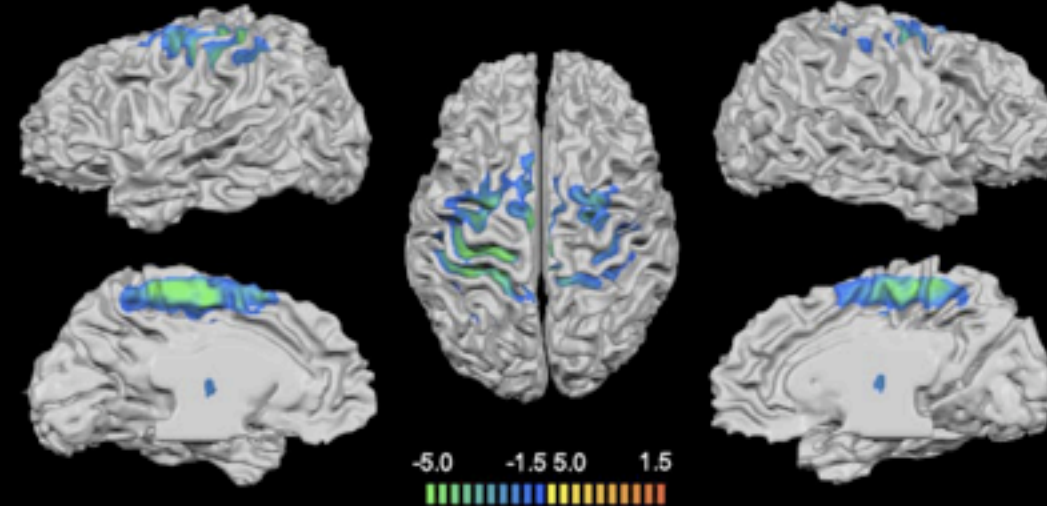
RSN 3



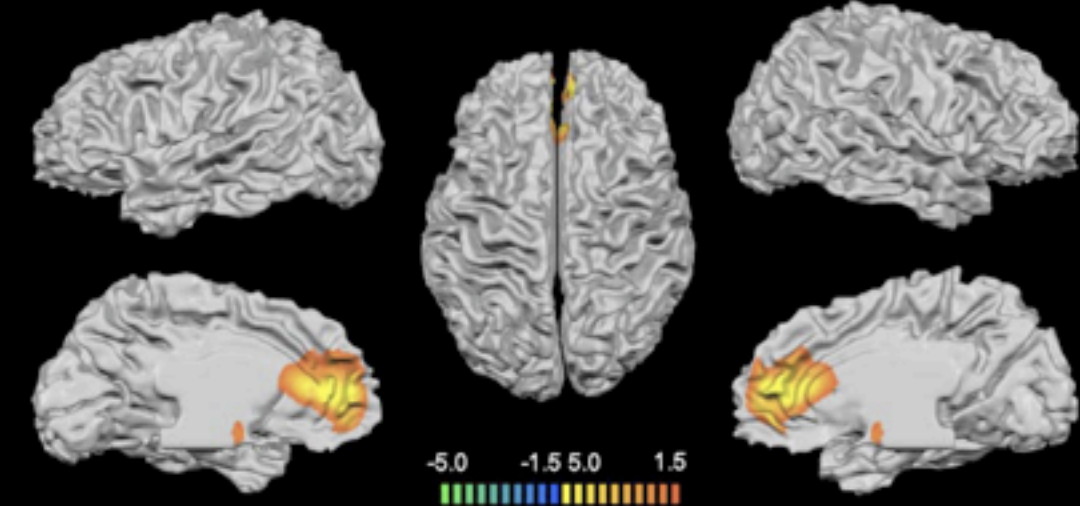
RSN 4



RSN 5



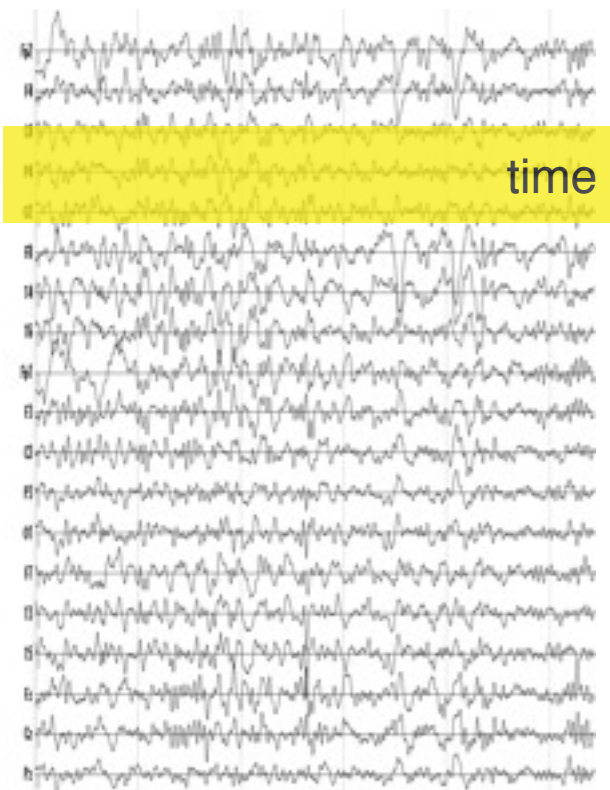
RSN 6



[Mantini et al., PNAS, 2007]

# EEG rhythms

- Temporal frequency bands

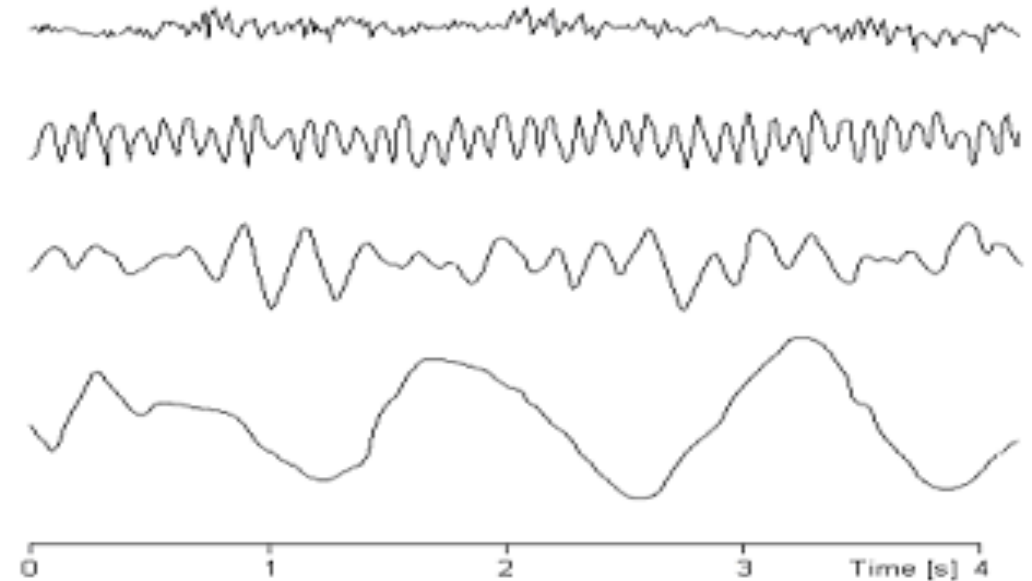


Beta 13-30 Hz

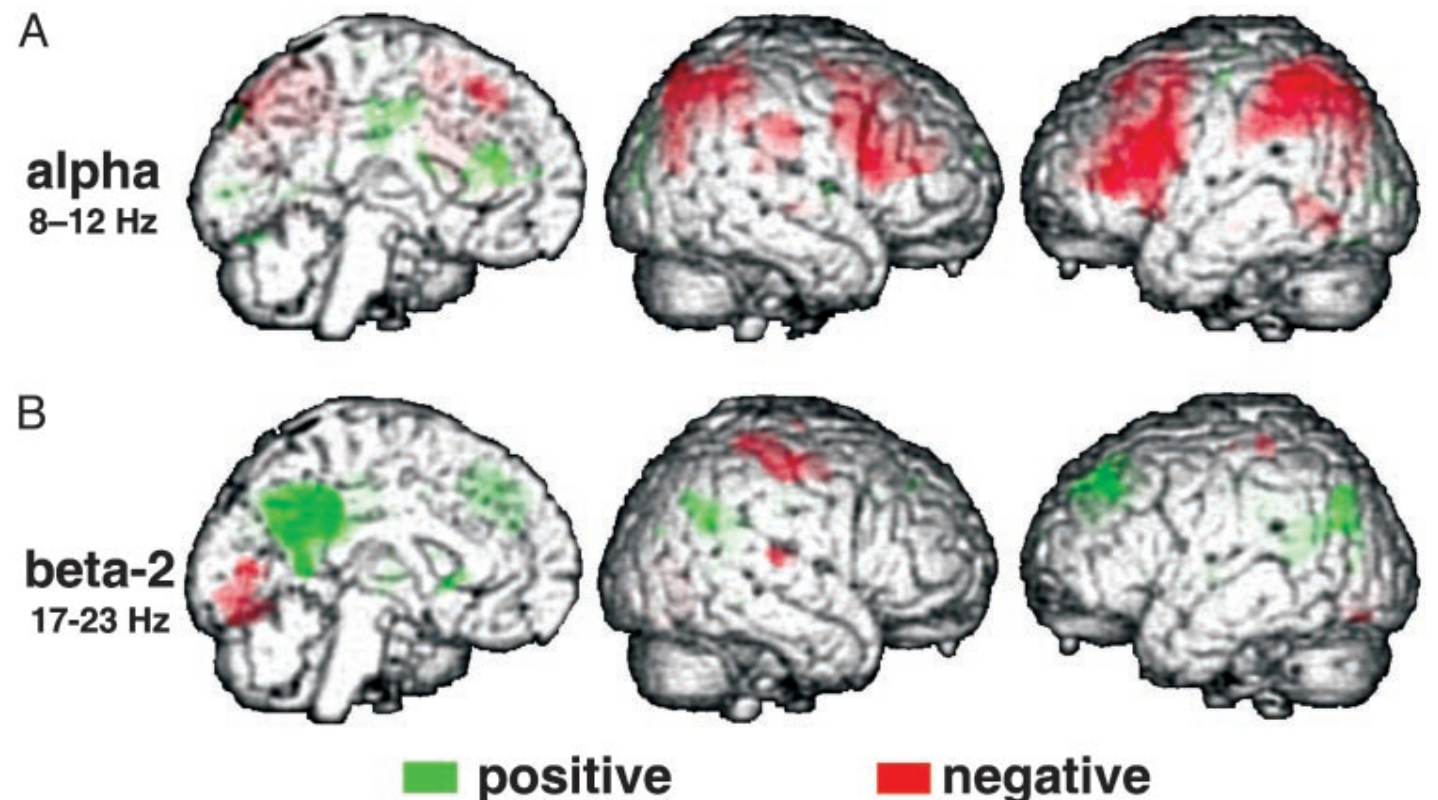
Alpha 8-13 Hz

Theta 4-8 Hz

Delta 0.5-4 Hz

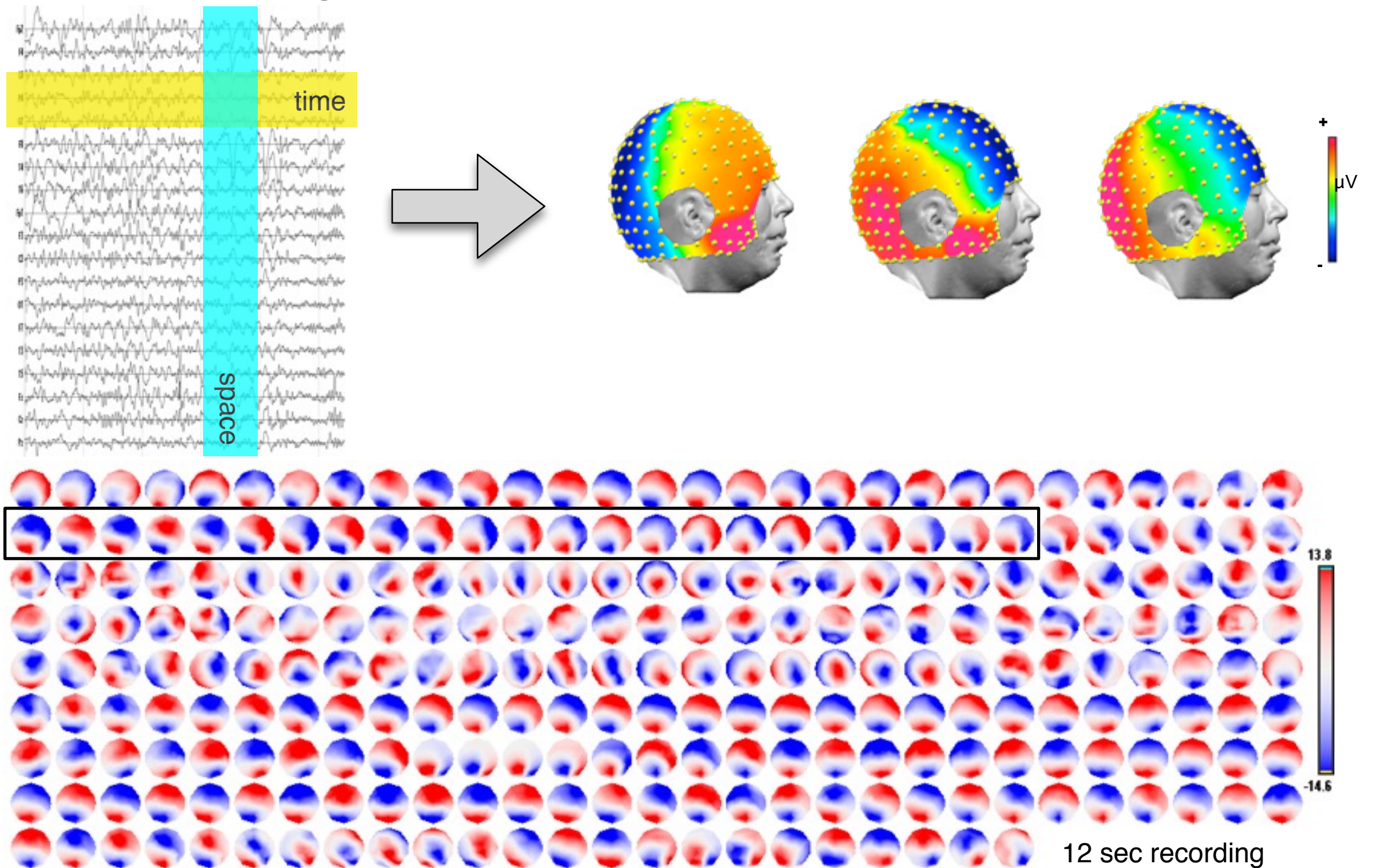


- Simultaneous EEG/fMRI can be acquired and cleaned
- Alpha-band energy correlates negatively with attention network



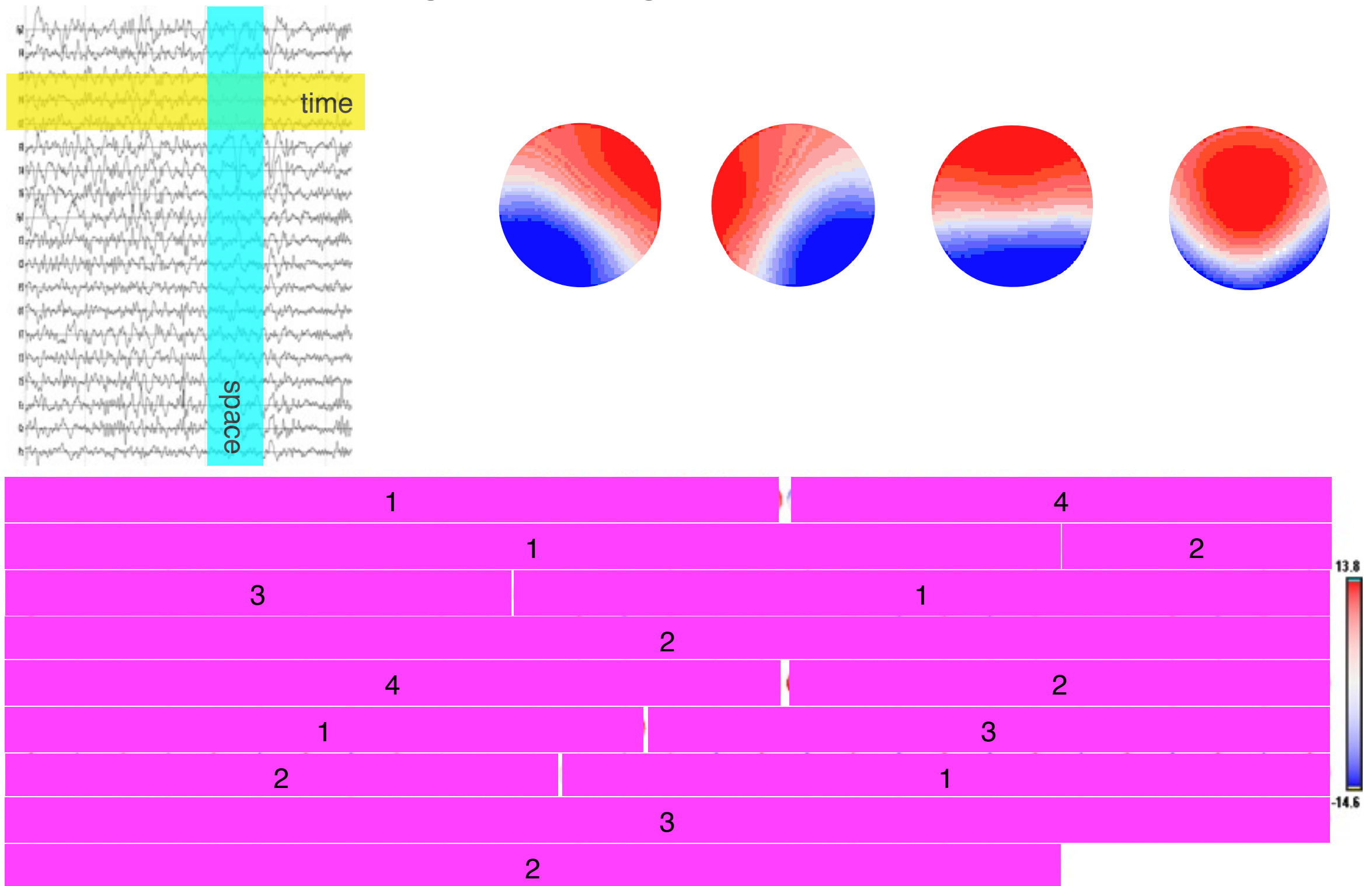
# EEG mapping

- Spatial topography is important too



# EEG microstates

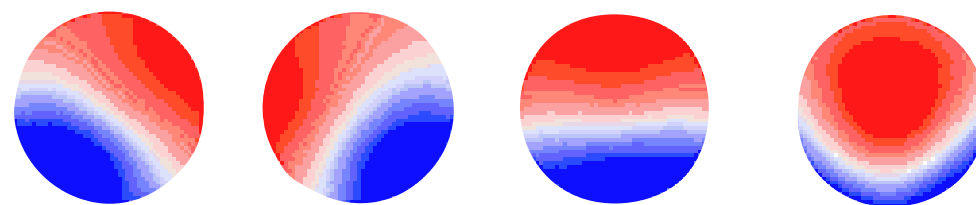
- Spatial clustering of topography maps





# EEG microstates

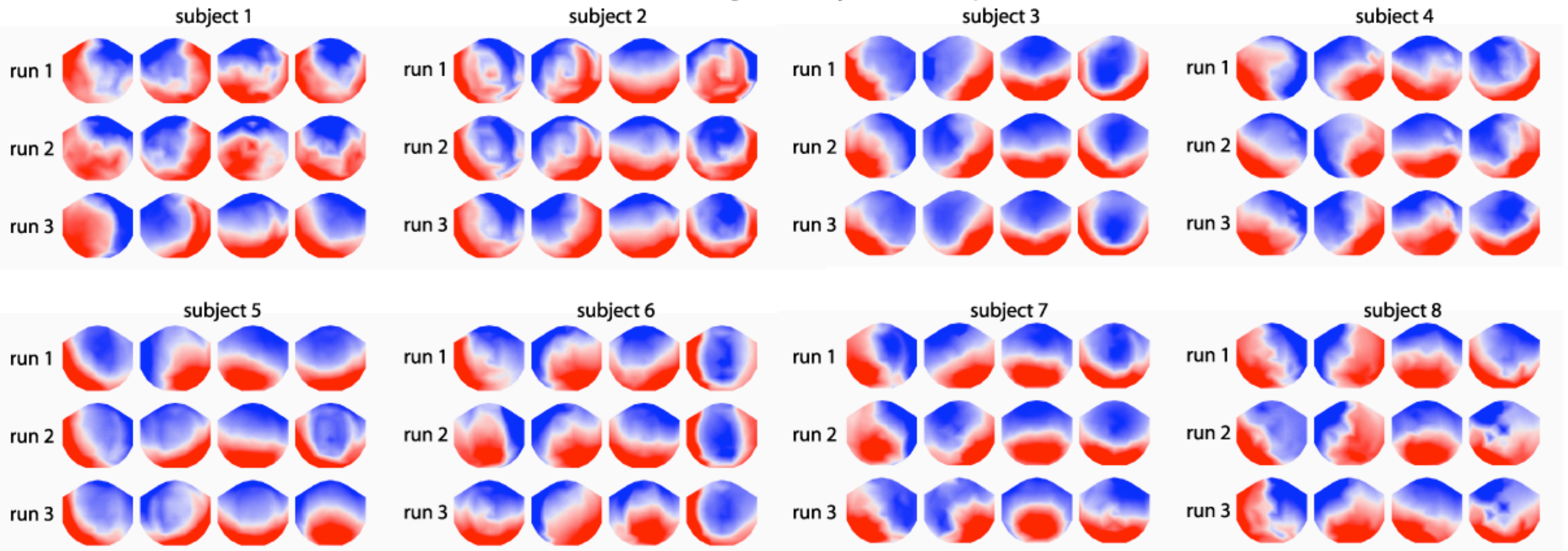
- Spatial clustering and cross-validation indicate
  - Four microstates explain spontaneous EEG (awake rest)
- Average duration of microstates is 100ms
  - Large cohorts (>500), age 6-67 [Koenig et al., 2002]
- Microstates are *functional*
  - Pre-stimulus microstate determines cognitive processing and perception [Mohr et al., 2009; Britz et al., 2009]
  - Modified in mental diseases
    - Duration is very sensitive parameter
    - Including schizophrenia, depression, Alzheimer



# EEG microstates in the MR scanner

- Consistent topographies across subjects

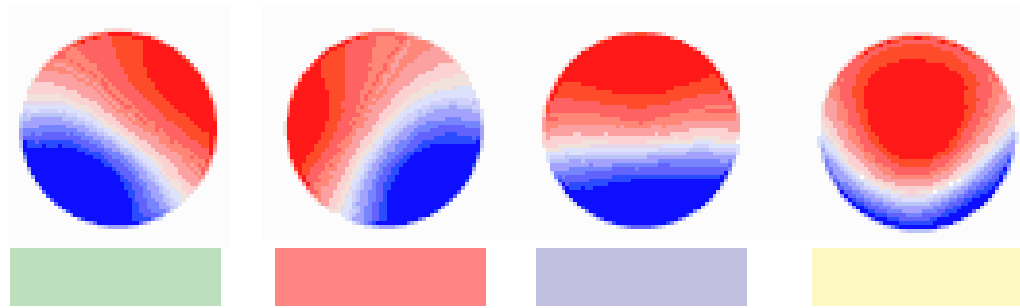
single subjects maps



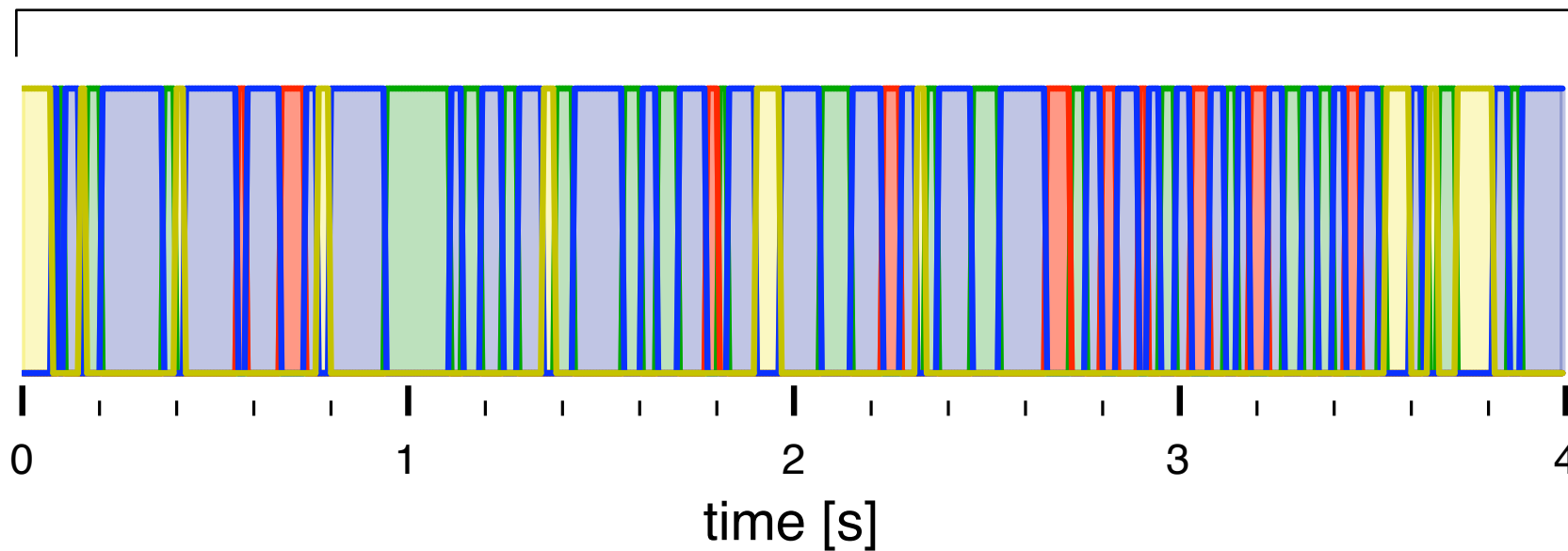
group level template maps



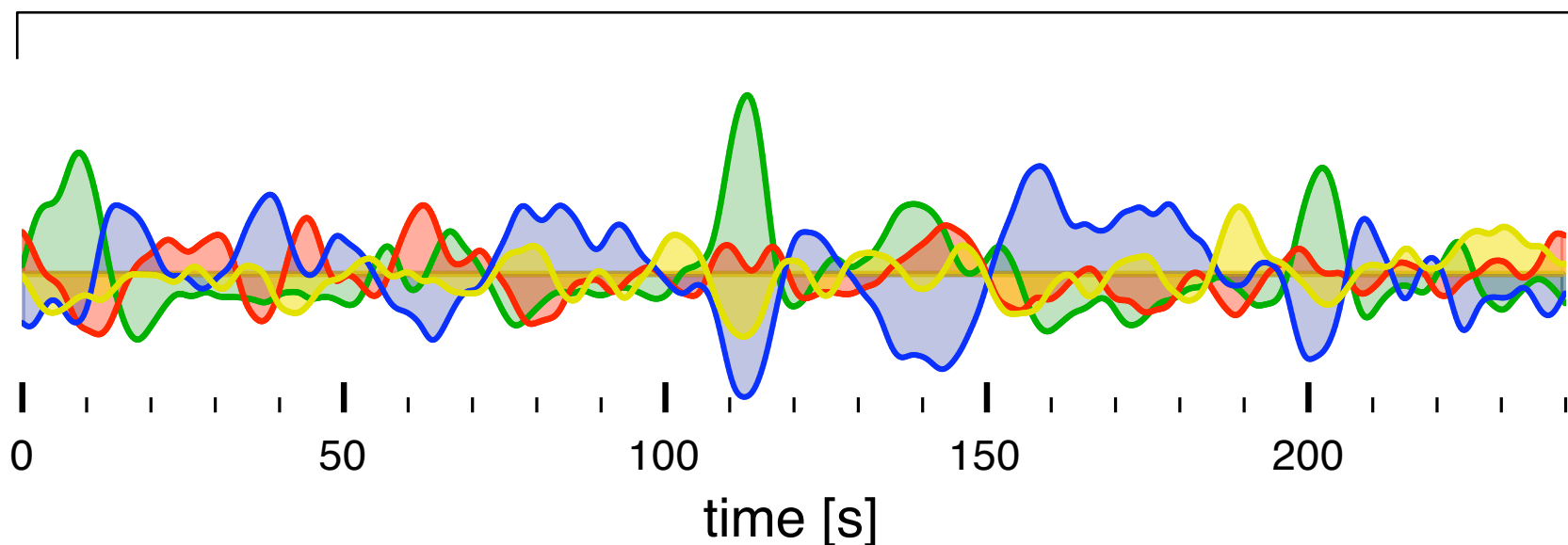
# Making the bridge from EEG to fMRI



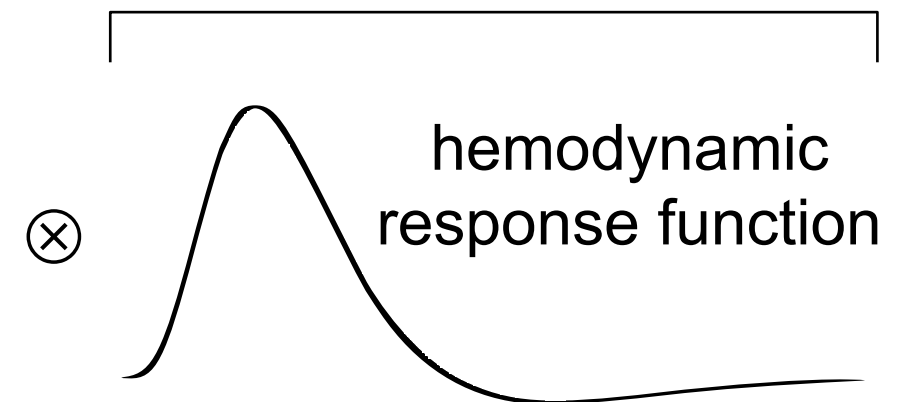
4 sec



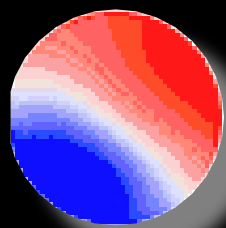
4 min



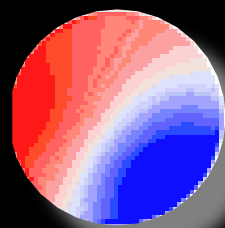
20 sec



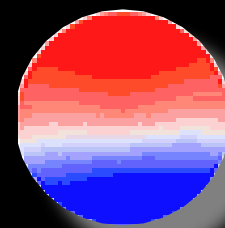
GLM analysis of fMRI data



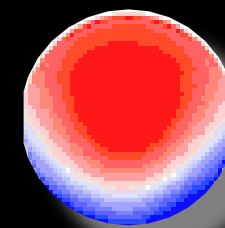
Auditory-phonological



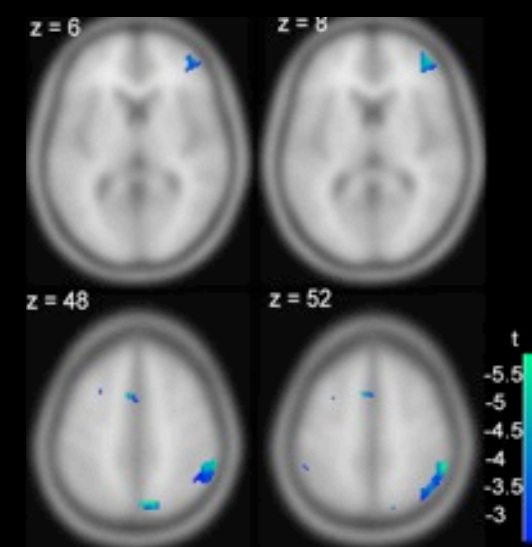
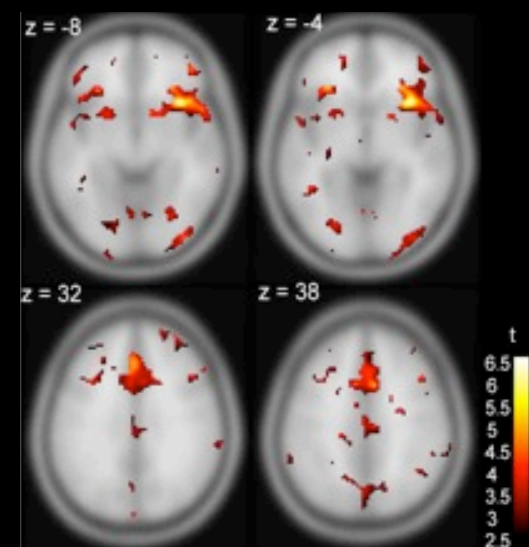
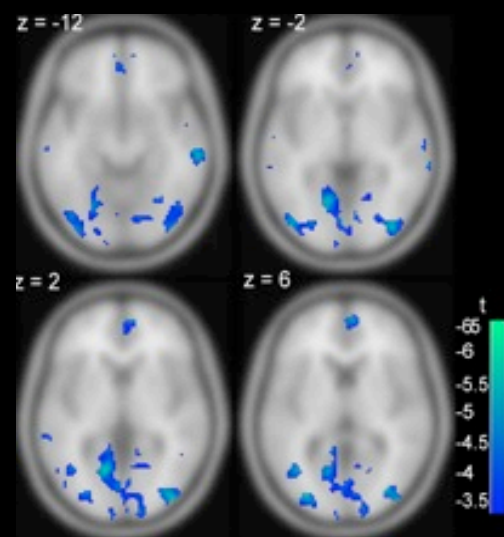
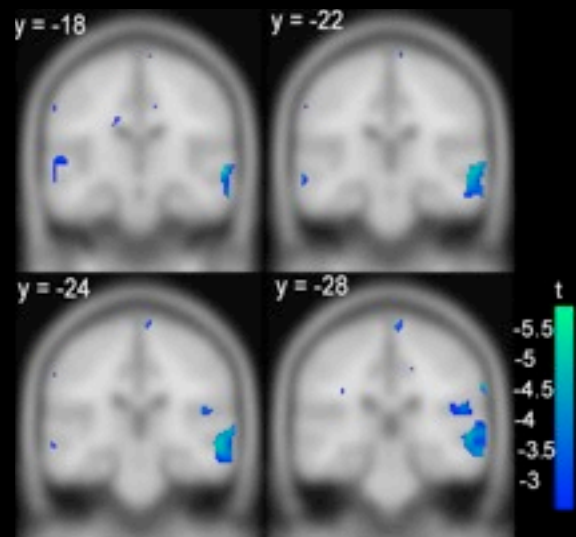
Visual



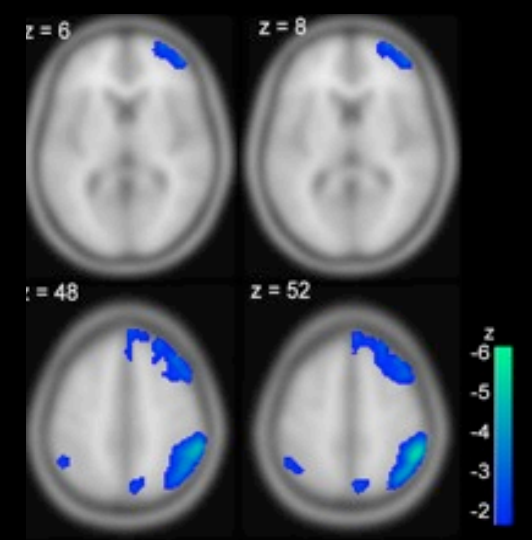
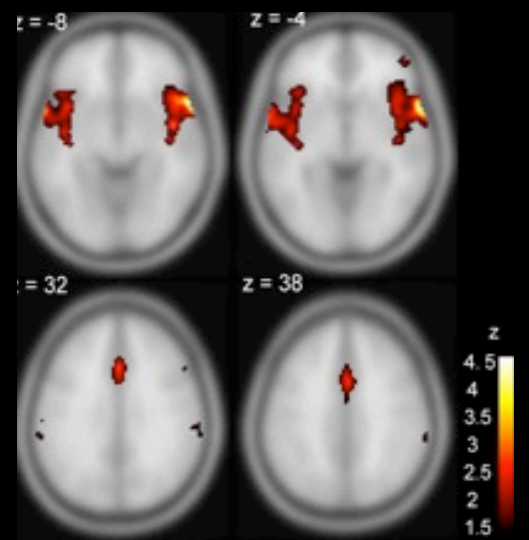
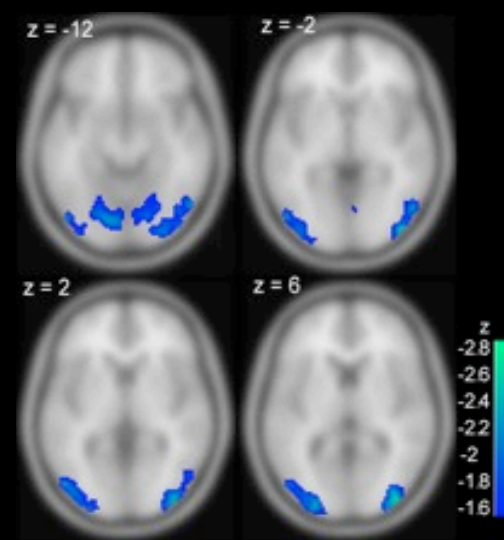
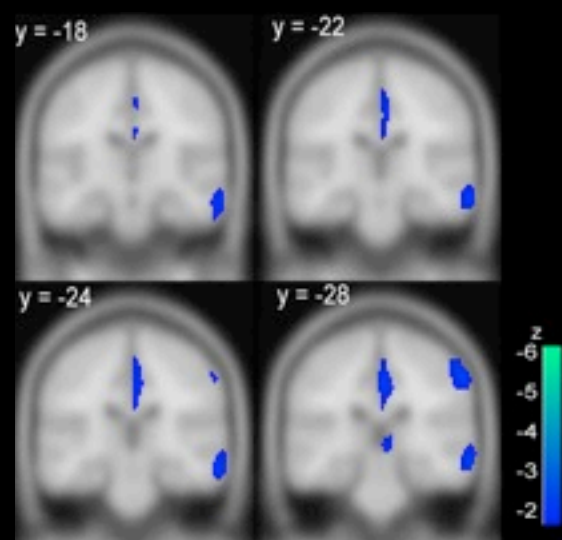
Self-referential



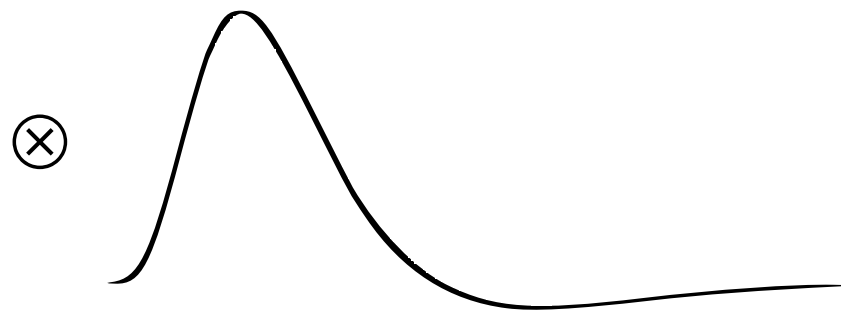
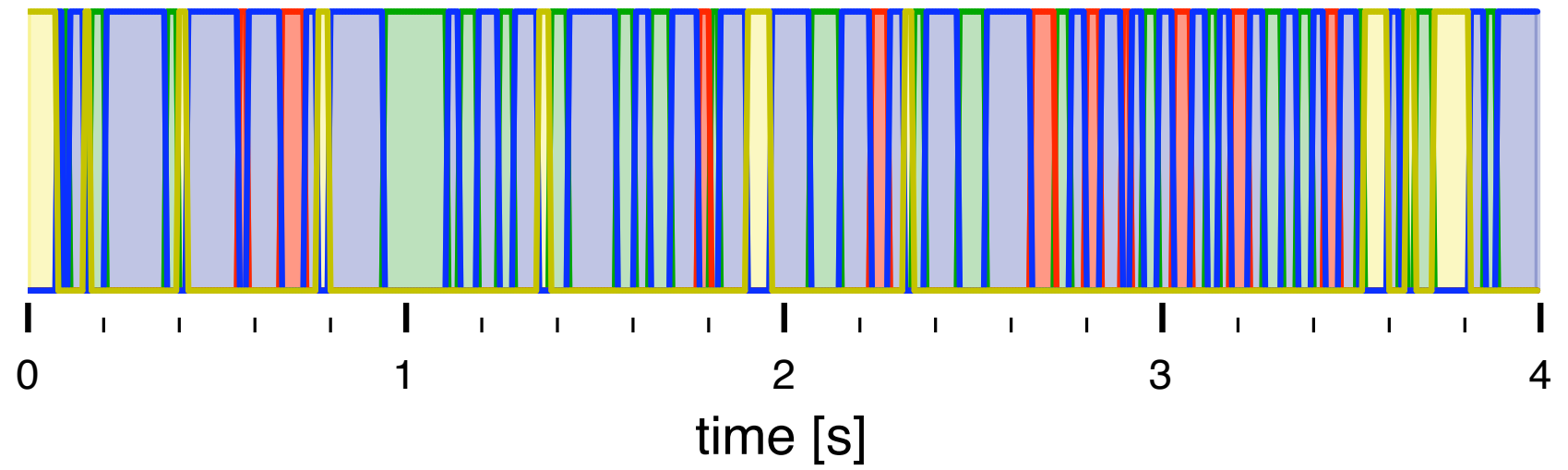
Dorsal attention



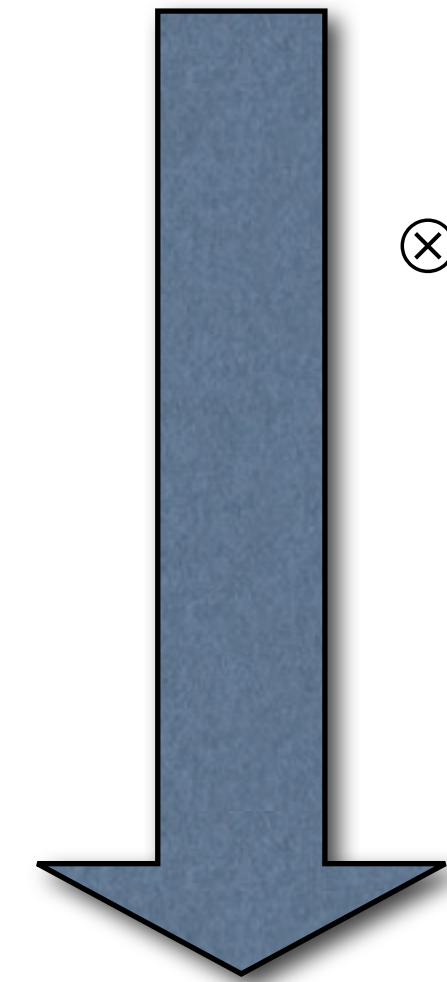
**Same networks are confirmed by fMRI group ICA analysis (out of 20 components)**



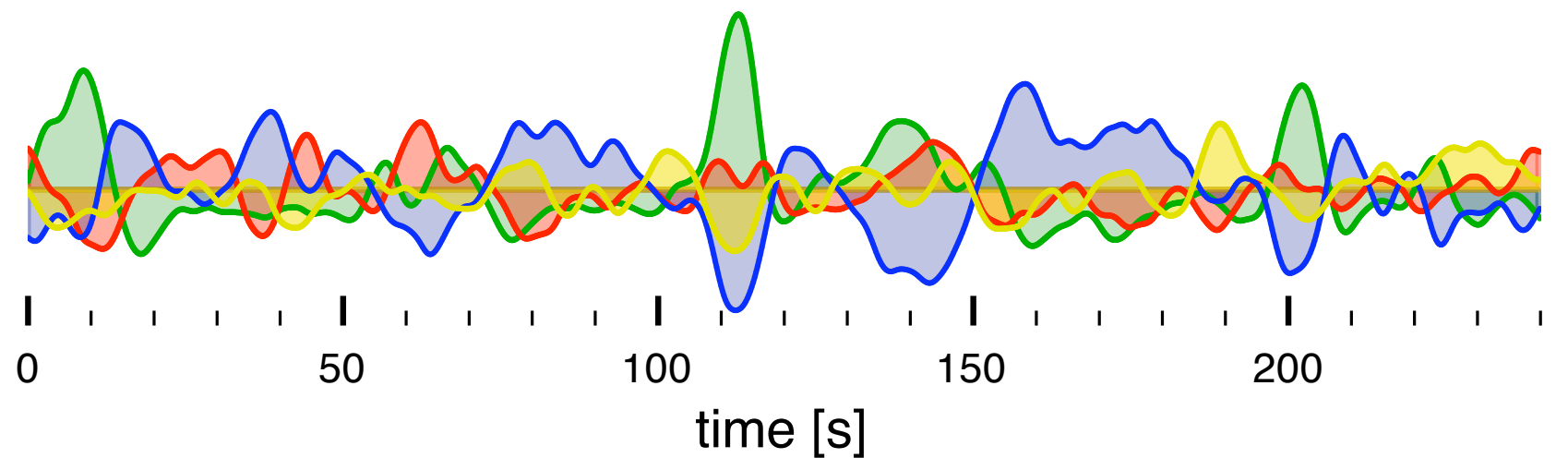
EEG  
100ms timescale



*How to explain that EEG  
dynamics remain  
meaningful after huge  
temporal smoothing?*



fMRI  
10sec timescale



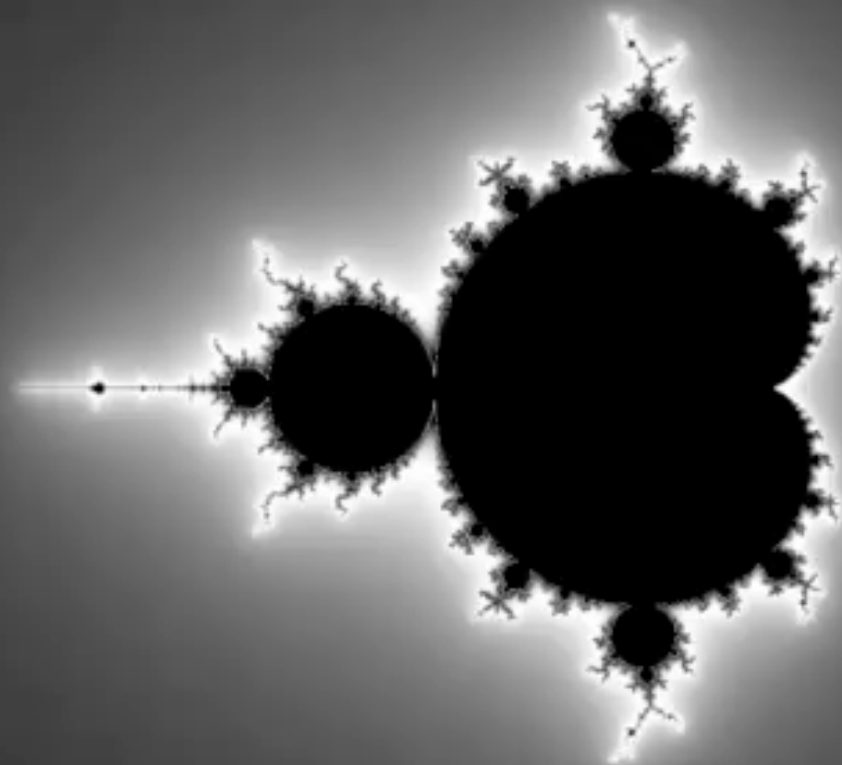
# Fractals everywhere...?

Benoît Mandelbrot



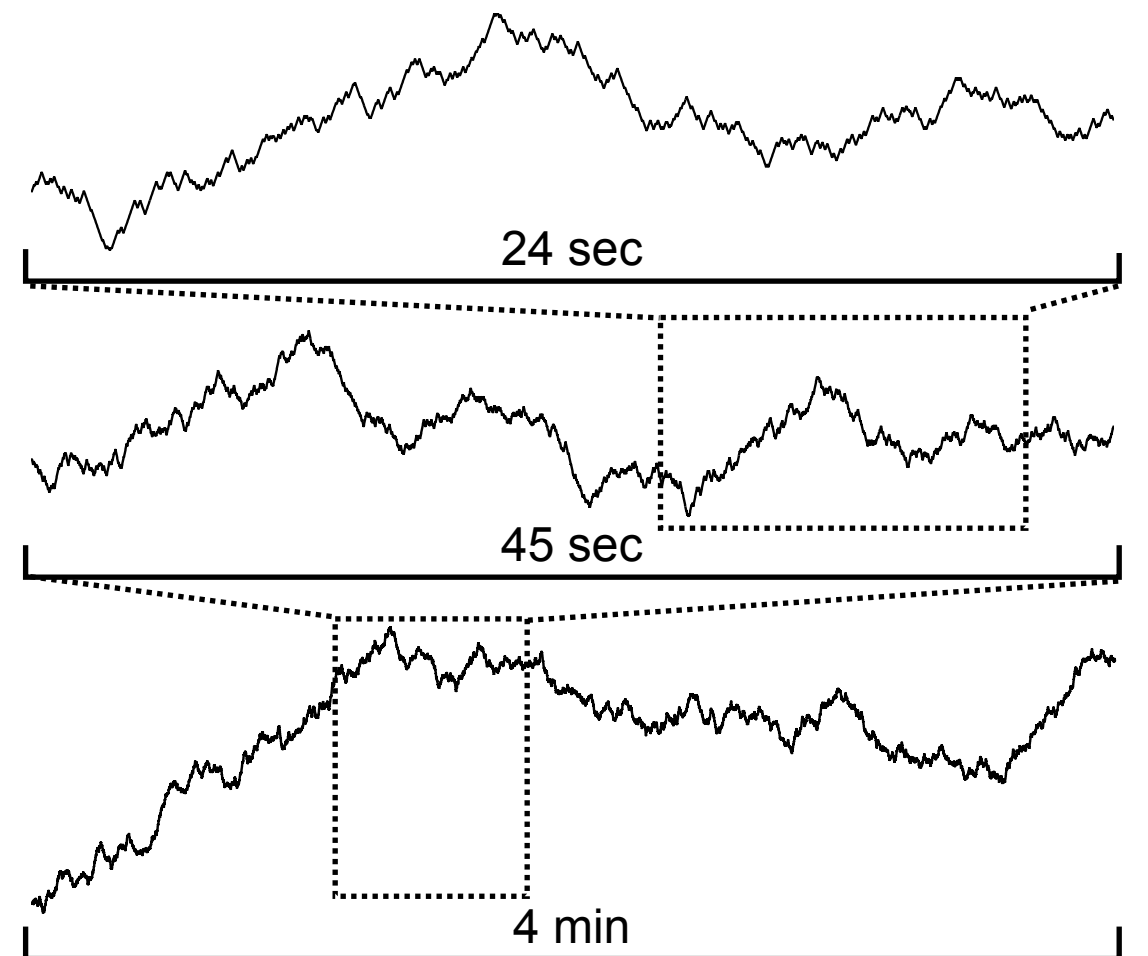
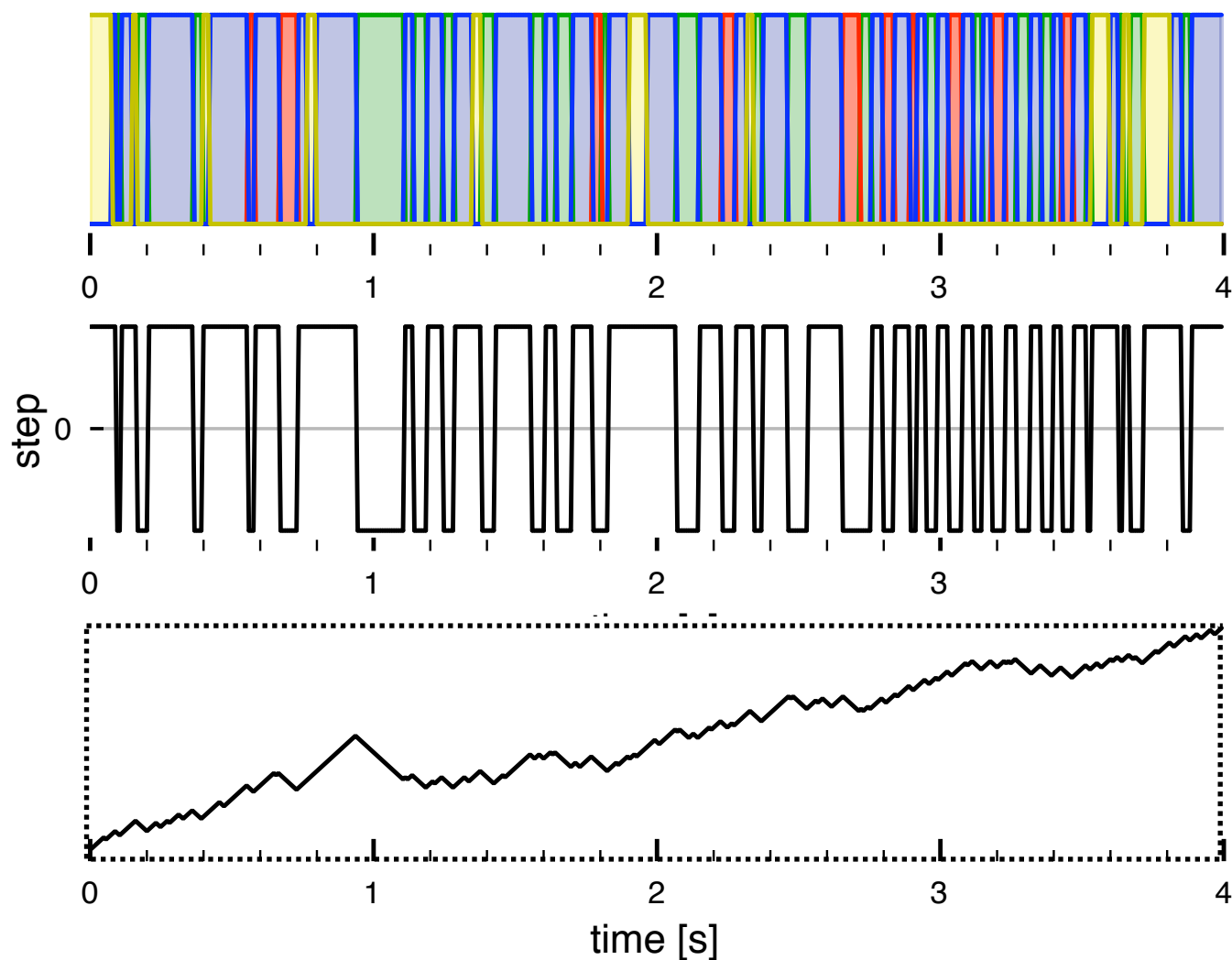
- Deterministic fractals
  - Completely predictable
  - Leads to exact or quasi self-similarity
  - E.g., Mandelbrot set
- Statistical fractals
  - Statistical measures are preserved across scales
  - E.g., stock market index, many physical and biological growth processes, hearth rhythm

Zoom into Mandelbrot set



# Fractal analysis of microstates

- Bipartitioning and random-walk embedding
  - Four microstates (1, 2, 3, 4)...  
like the four bases of the DNA



$$\{X(t)\}_{t \in \mathbb{R}} = \{a^H X(t/a)\}_{t \in \mathbb{R}}, \quad a > 0$$

# Statistical fractals and wavelets

## ■ Self-similar processes

- Statistically undistinguishable under dilation and change of scale

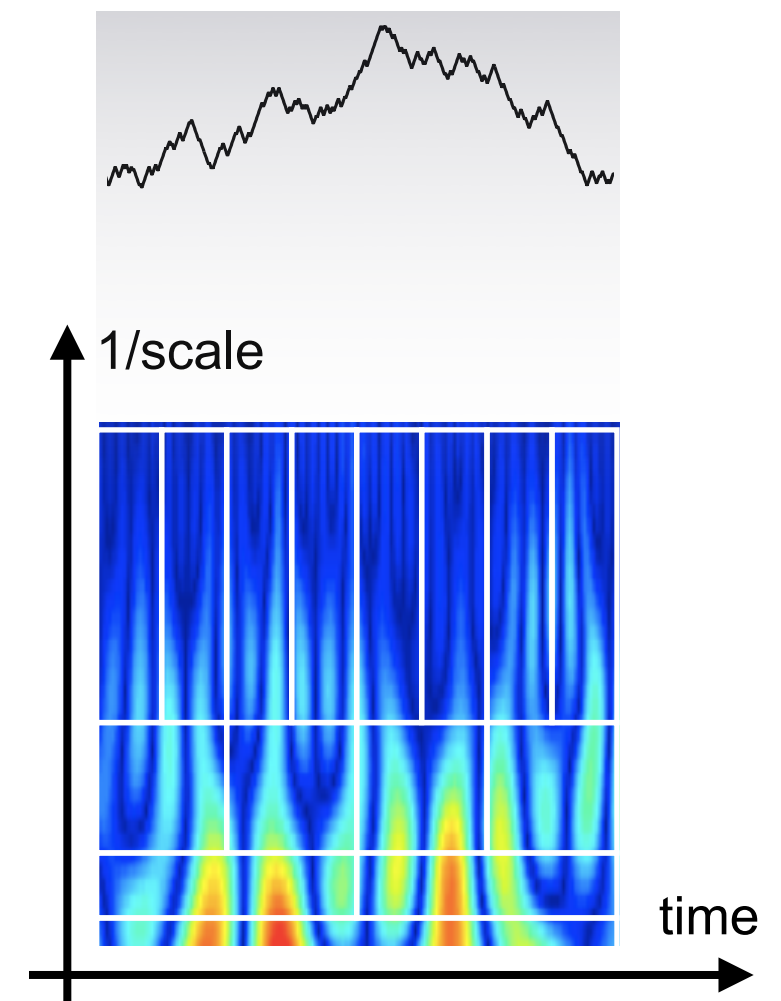
$$\{X(t)\}_{t \in \mathbb{R}} = \{a^H X(t/a)\}_{t \in \mathbb{R}}, \quad a > 0$$

- No characteristic scale of time, single Hurst exponent  $H$
- Non-stationary and long-range dependency
- Variogram:  $E[|X(t+a) - X(t)|^q] = C_q a^{qH}$

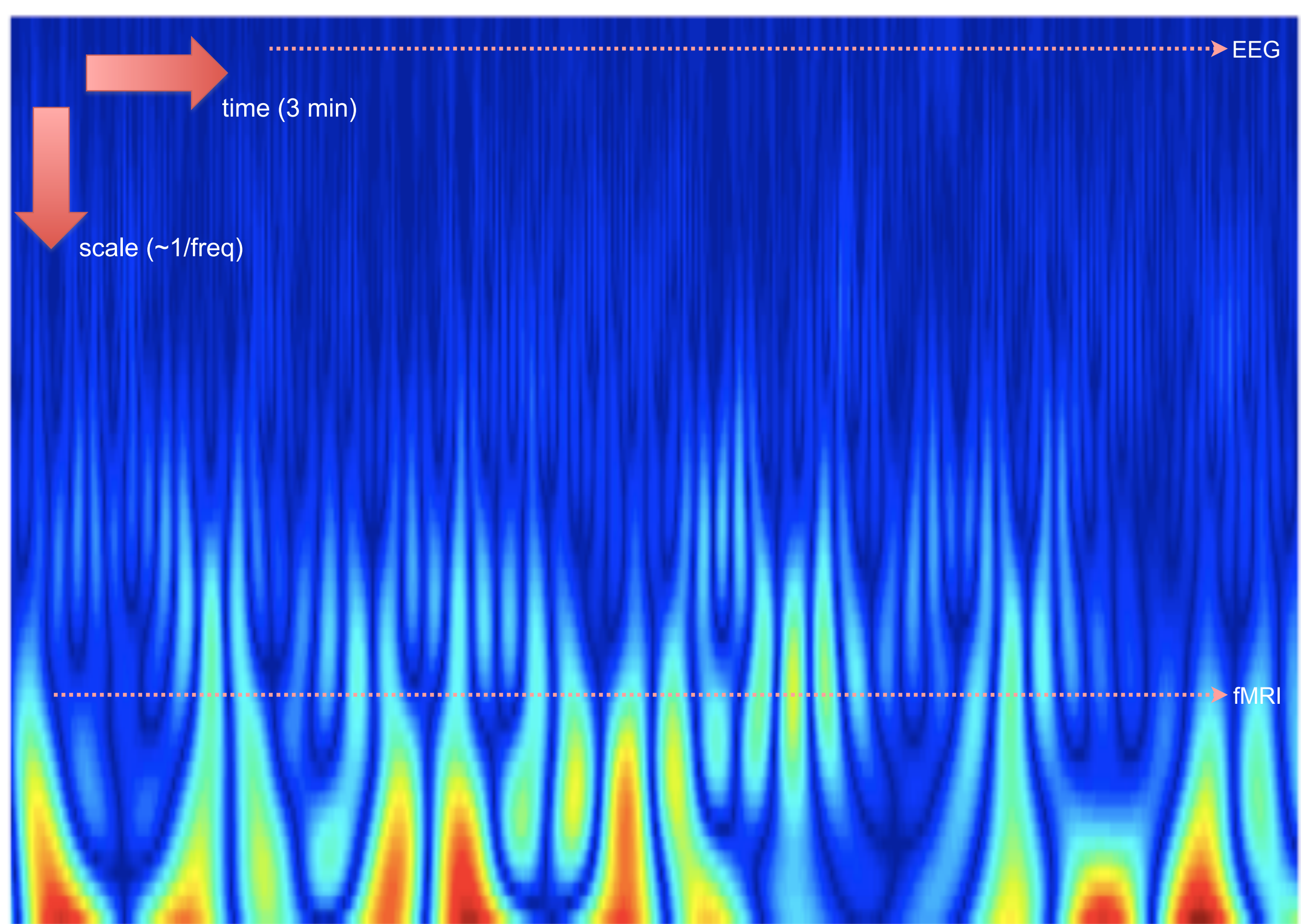
## ■ Wavelet fractal analysis

Coefficients  $d_X(a, k) = \frac{1}{a} \int X(t) \psi(t/a - k) dt$

- Stationary at each scale
- Self-similarity,  $\{d_X(0, k)\} = \{2^{-jH} d_X(2^j, k)\}$
- Short-range dependency



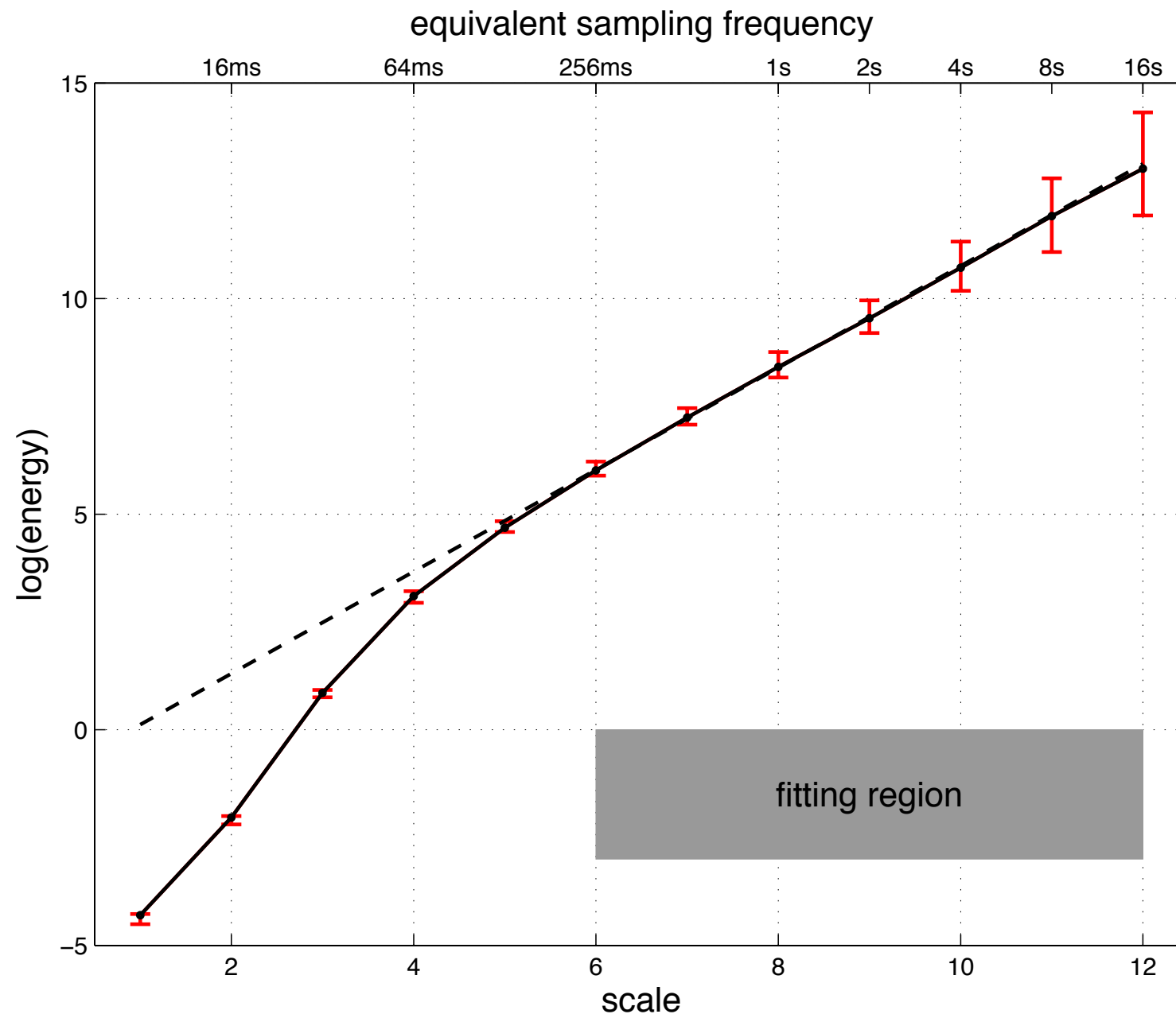




# Log-scaling diagram

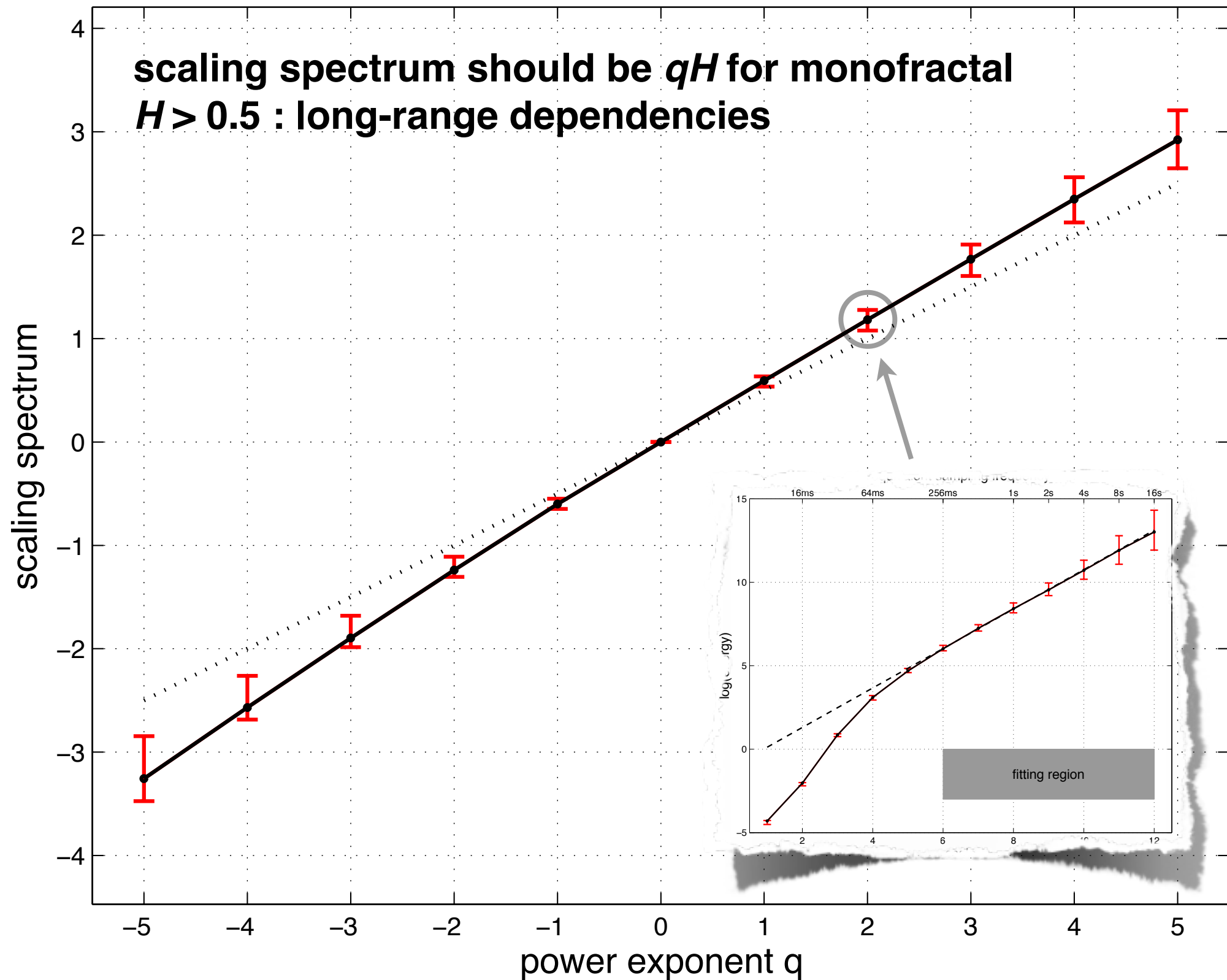
- Estimating  $E[|d_X(2^j, k)|^q]$  from the structure function

$$S(d_X, j, q) = \frac{1}{n_j} \sum_{k=1}^{n_j} |d_X(2^j, k)|^q$$



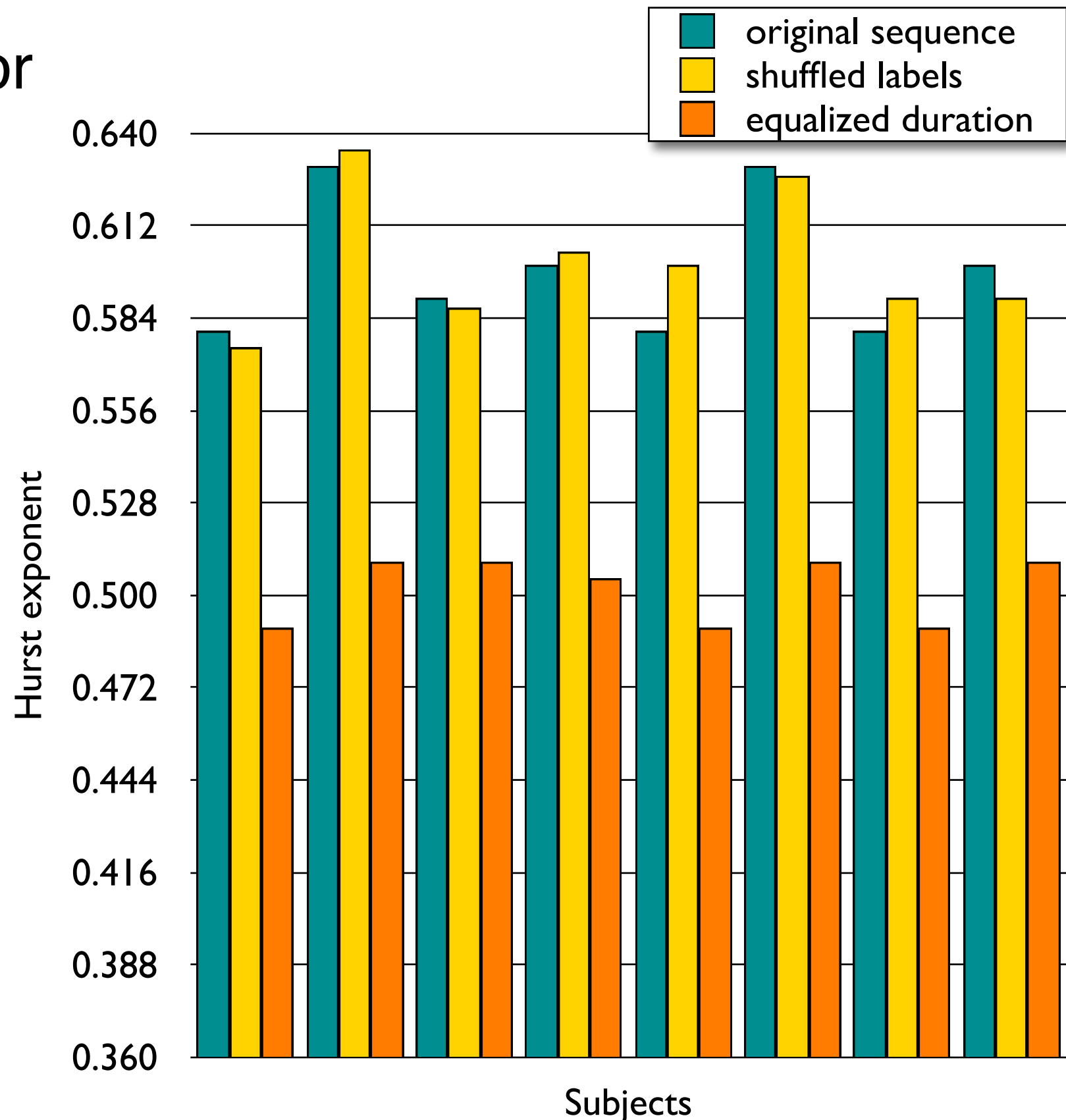
**confirms weak self-similarity,  
similar to PSD ( $q=2$ )**

# Scaling spectrum



# Fractal organization of microstates

- Monofractal behavior over two orders of magnitude (256ms-16s)
- Shuffled labels give same fractal signature!
- Equalized durations result into white noise dynamics ( $H=0.50$ ,  $p<0.05$ )



# Criticality of the brain

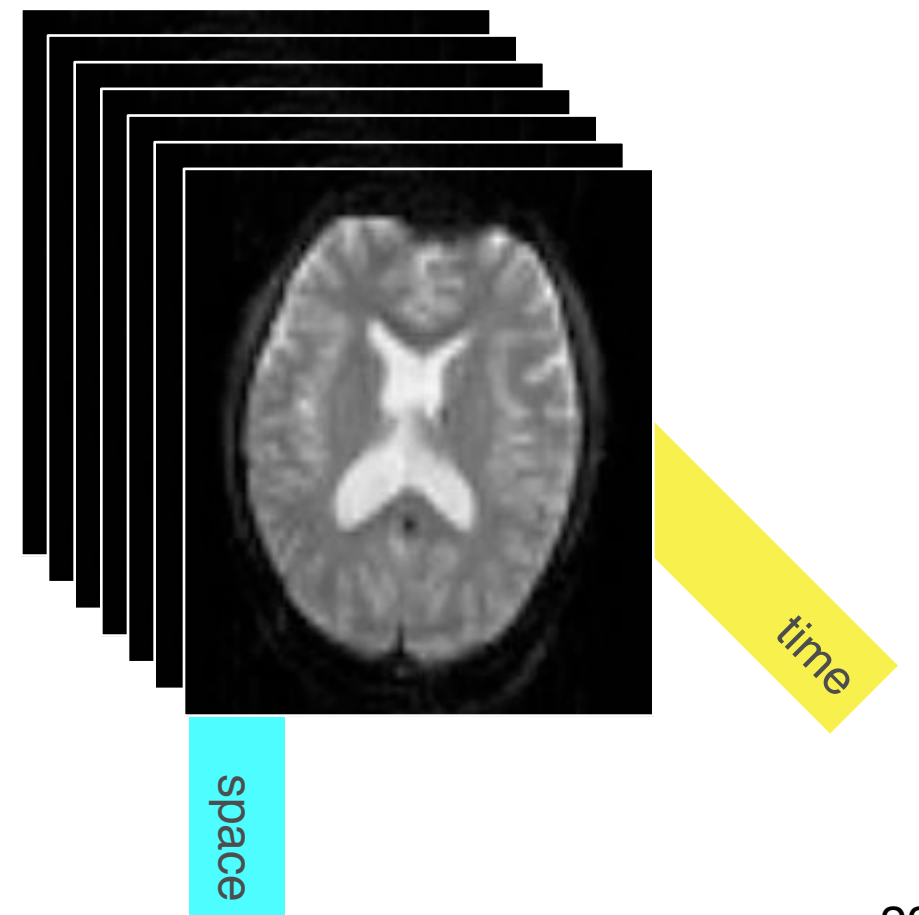
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- Our findings
  - Microstates are a *global* functional brain measure
  - Dynamics are strongly monofractality
  - Implies non-stationarity and long-range correlations
- Scale-free organization is reminiscent of system at critical state near phase transition
- Further evidence to seminal work of Chialvo, Bullmore, Bak, ...
  - Power-law behavior of various brain measures
    - Space: scale-free small-world networks
    - Time: EEG, MEG-fMRI synchronization, ...
  - Universal organizing principle, in order to reorganize and adapt rapidly  
~ self-organization of complex system

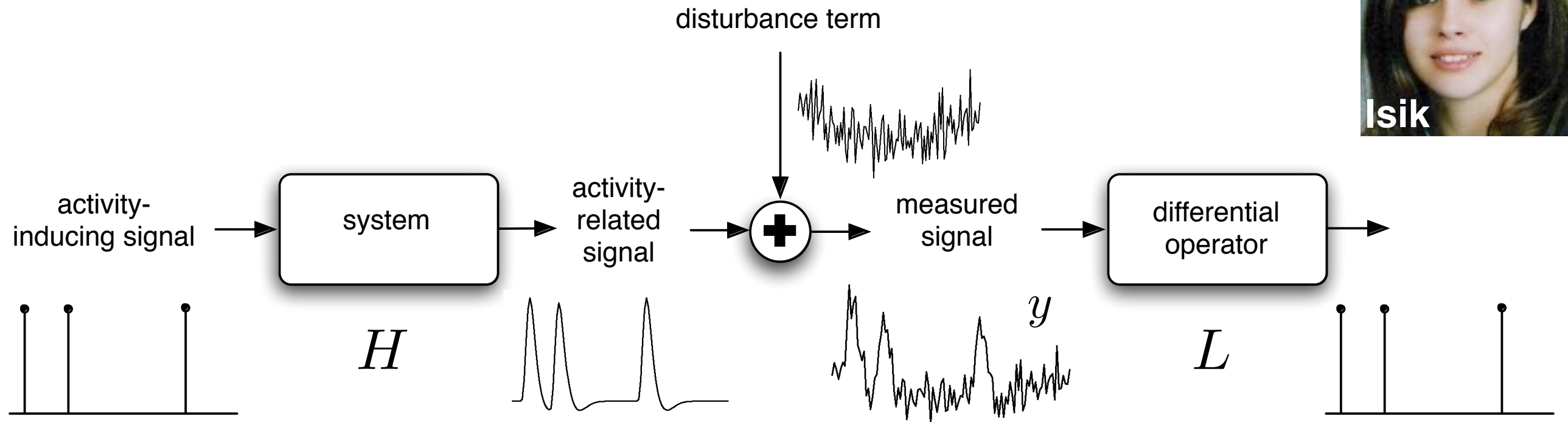
# Implications for fMRI...

- Scale-free dynamics at the EEG timescale
- At the fMRI timescale
  - Despite hemodynamic blur ( $\sim 10$  sec), meaningful process (with same characteristics) is observed
  - Scale-free organization is key to maintain information through timescales
- A lot of redundant information is acquired
  - Time:
    - Hemodynamic response is slow
  - Spatial:
    - Vascular nature of signal, spatial extent

fMRI



# ... and regularization for fMRI



- Identify differential operator  $L$  that “inverts” hemodynamic response
  - Linearization (first-order Volterra term)
- Analysis prior:  $\hat{s} = \arg \min_s ||y - s||_2^2 + \lambda ||L\{s}\|_1$ 
  - Novel analysis method of fMRI data (“paradigm free”)
  - Deploy for image reconstruction

