

# Spatial Encoding in MRI with Nonlinear Fields

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Hans Weber, Anna Welz, Walter Witschey, Maxim Zaitsev

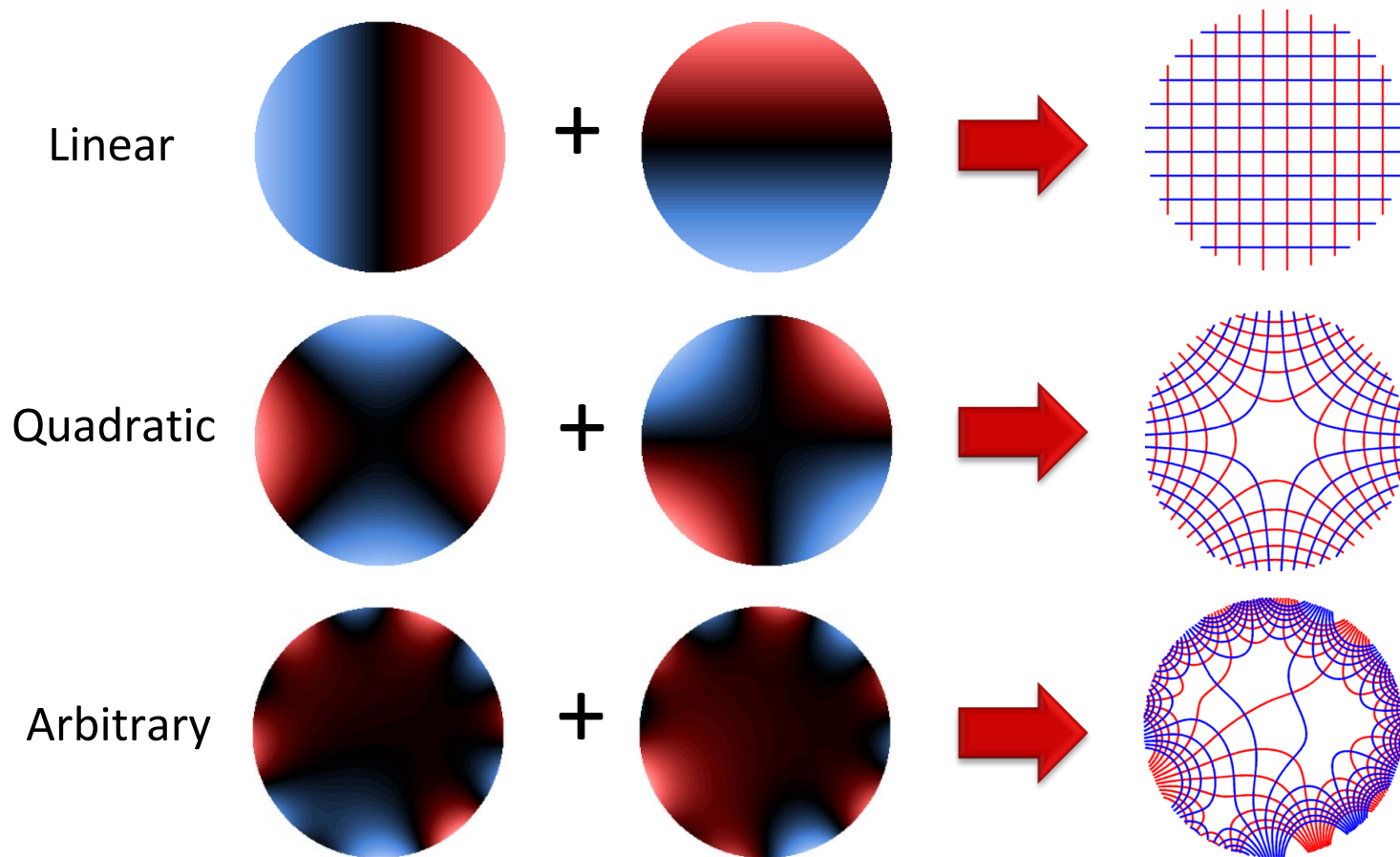
# Overview

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- Encoding with curved fields
  - What's different to normal?
  - Including first in vivo brain images
- Encoding with linear and curved fields simultaneously
  - How does the reconstruction work?
  - Experimental verification

# More general 2D encoding

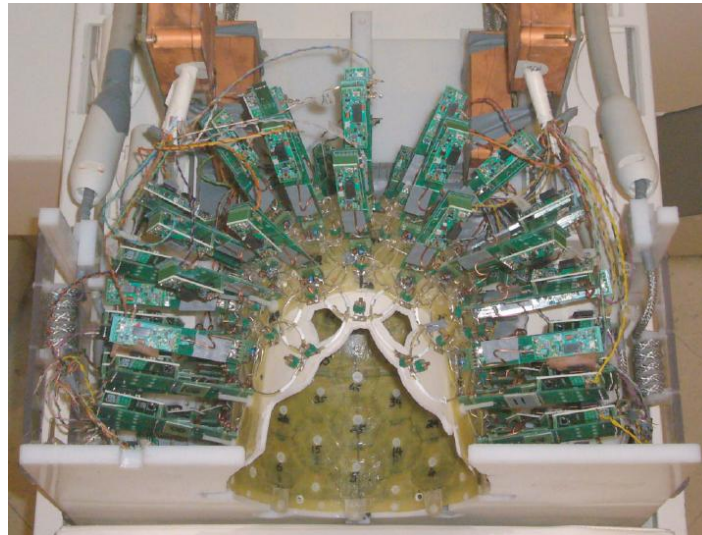
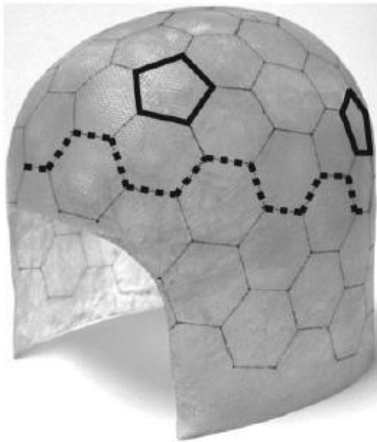
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# Why bother with curved fields?

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- Rectilinear fields are poorly suited to living organisms
  - RF coils are already matched to anatomy  
why not gradients?

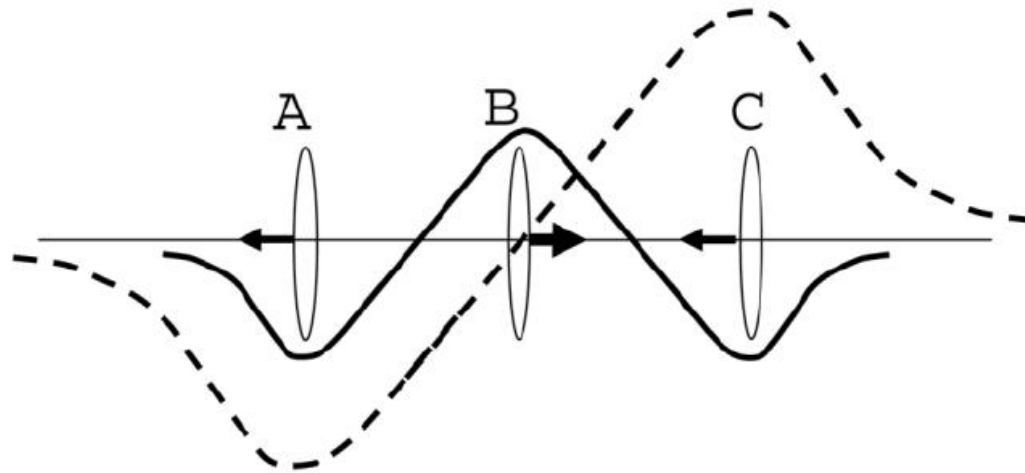


96-channel RF coil (Wiggins et al, MRM 2009)

# Why bother with curved fields?

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- Reduce nerve stimulation caused by gradient switching



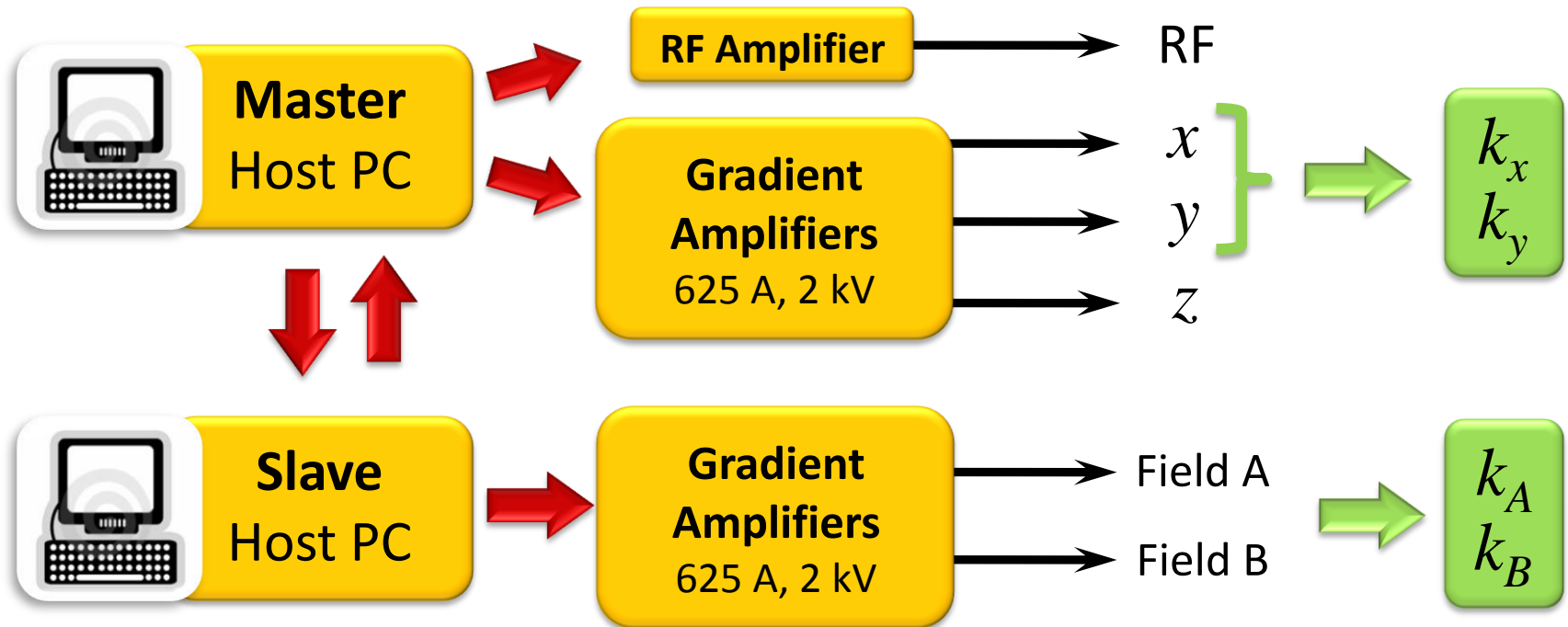
Multiple-region gradient encoding (Parker and Hadley, MRM 2006)

# Why bother with curved fields?

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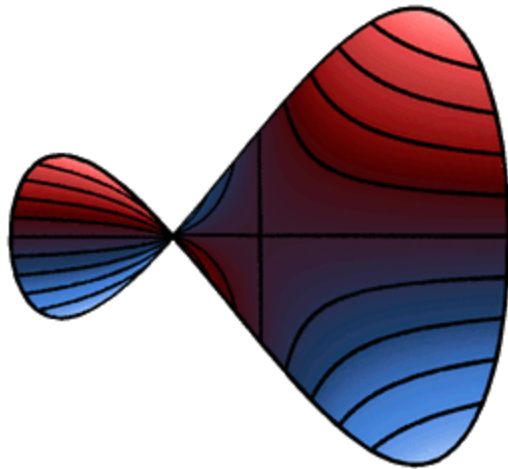
- Because we can!
- Potential applications include:
  - Allow imaging where linear fields are too difficult/expensive (portable MRI)
  - New kind of image acceleration (more later...)
  - Real-time shimming
  - Phase preparation
    - PIPS, M. Zaitsev, proc ISMRM 2009
    - GradLoc – W. Witschey, proc ISMRM 2011 and MRM (in press)
  - Combination with MREG/OVOC to provide fast spatial encoding

# Hardware: Modified Siemens 3T Trio

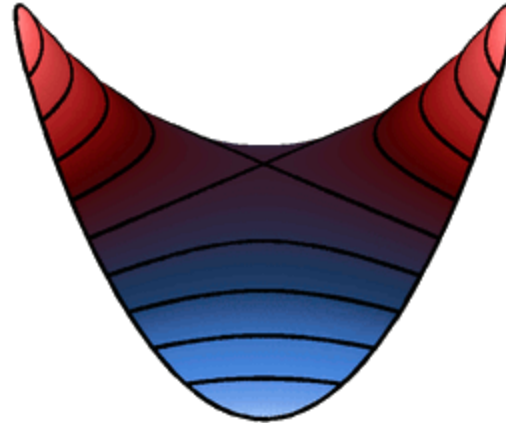


# The fields we decided to make

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**Field A**

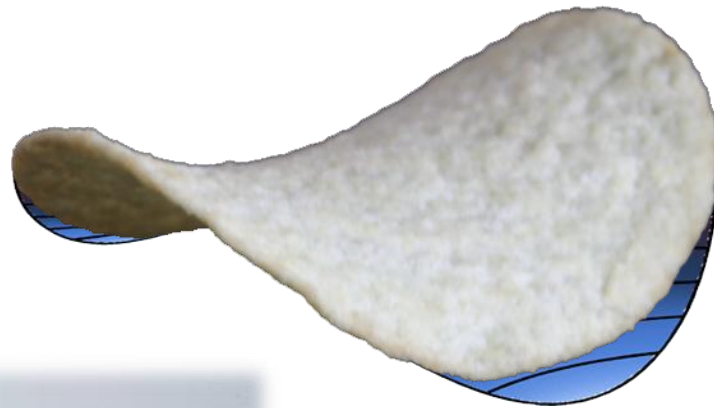


**Field B**



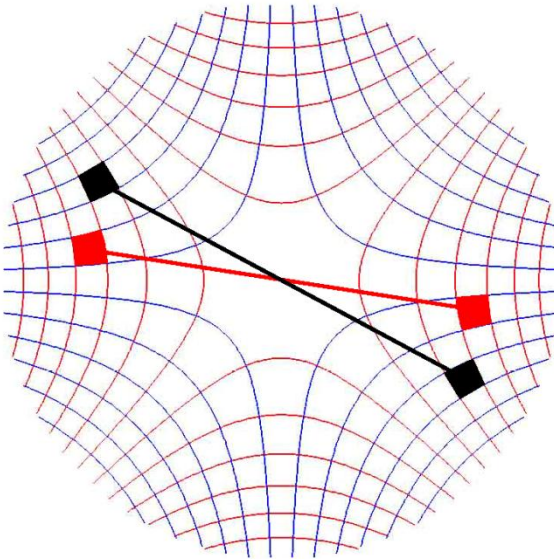
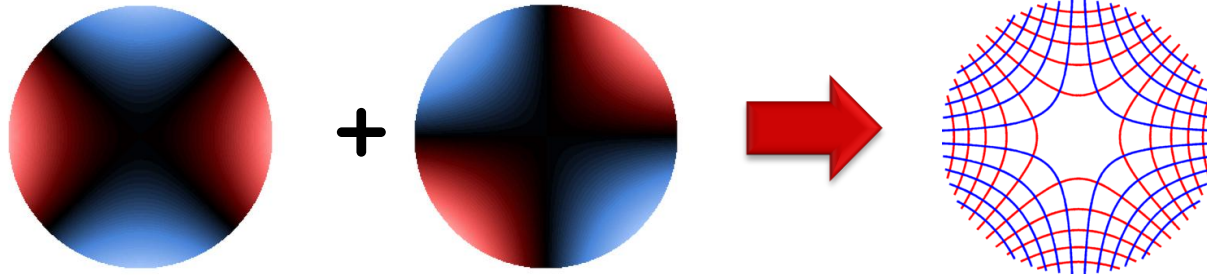
# The hyperbolic paraboloid

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# Ambiguous encoding

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Voxels rotated  $180^\circ$  from each other receive identical encoding - they will overlap (alias) in the image

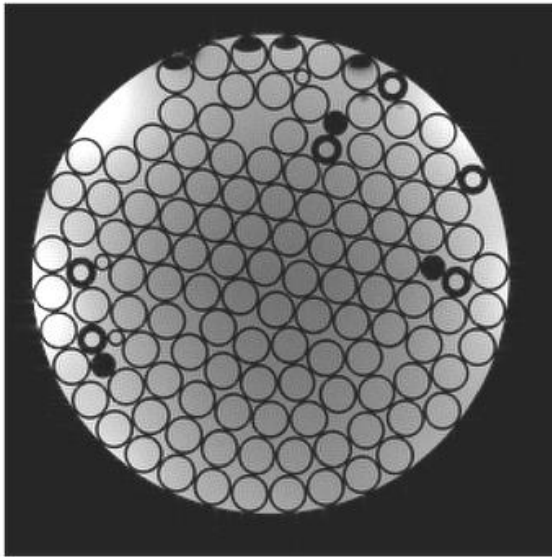
# But we already know how to deal with aliasing

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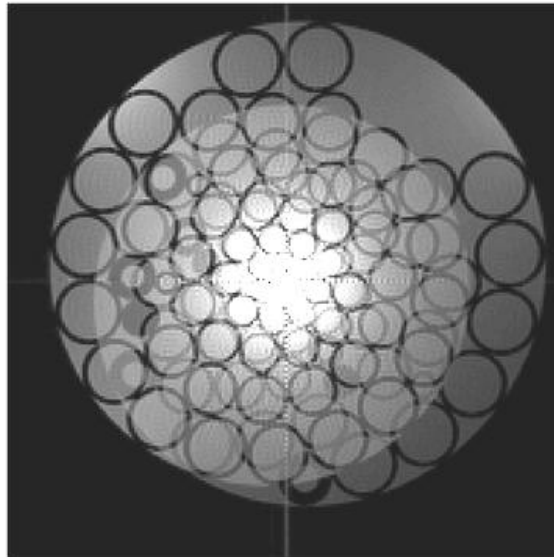
- Parallel Imaging (SENSE or GRAPPA) involves acquiring less data and therefore aliased images

# For our quadratic fields

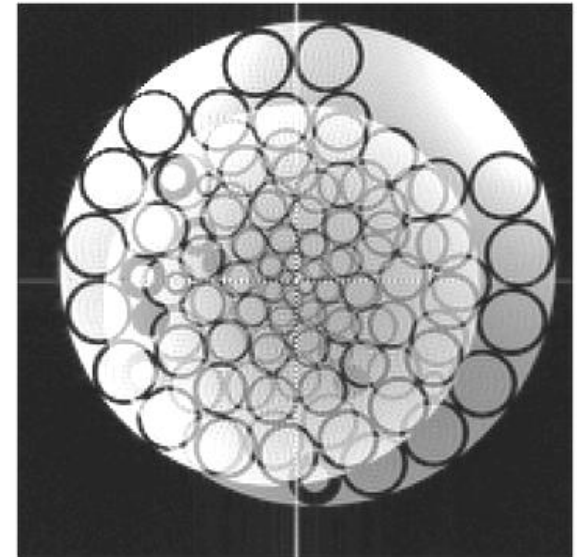
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Linear gradients



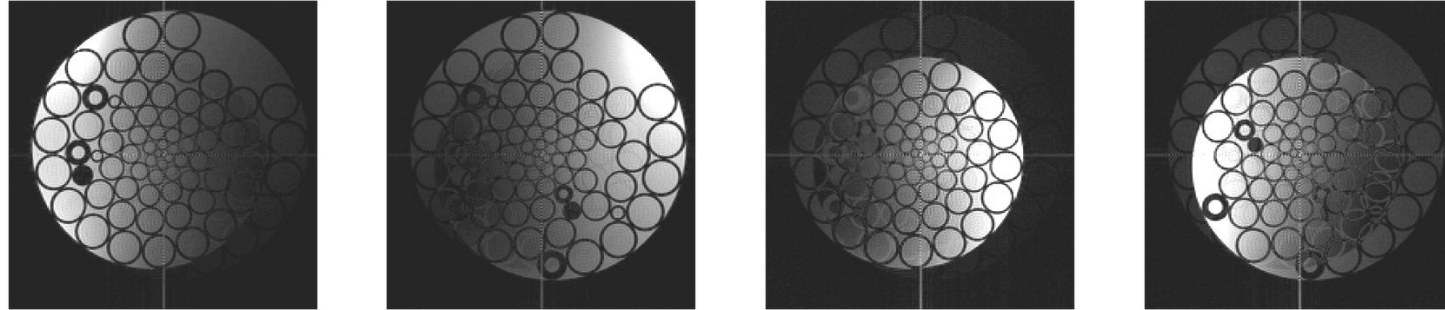
Quadratic gradients  
After FFT



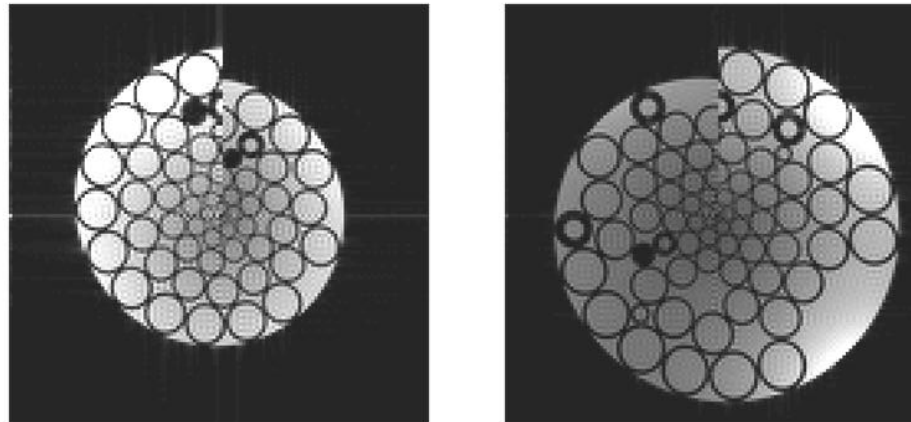
Quadratic gradients  
After FFT and  
intensity correction

# SENSE-like unaliasing

Separate coil images



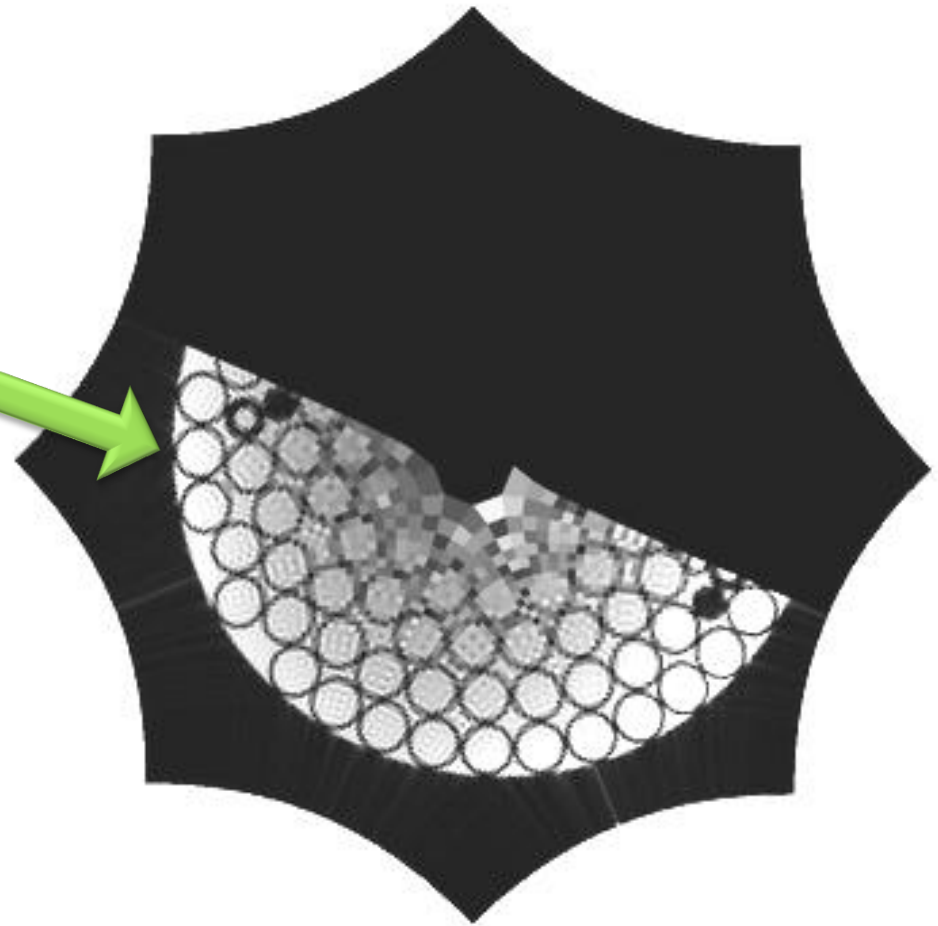
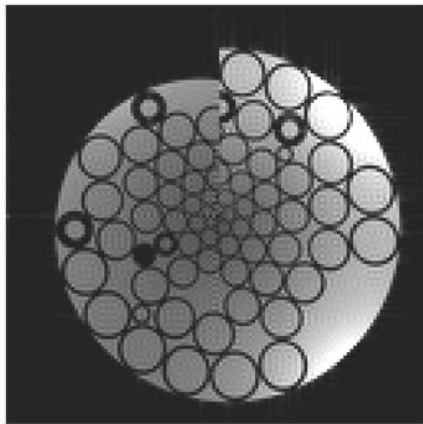
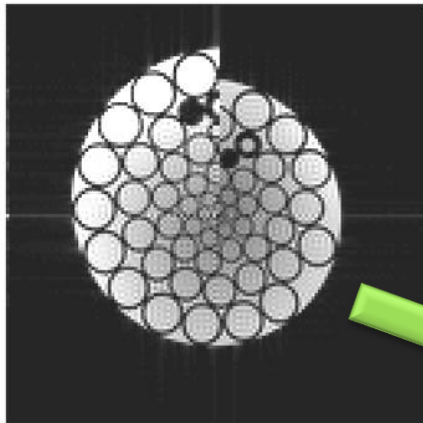
SENSE-like unaliasing



Unaliased images in encoding space

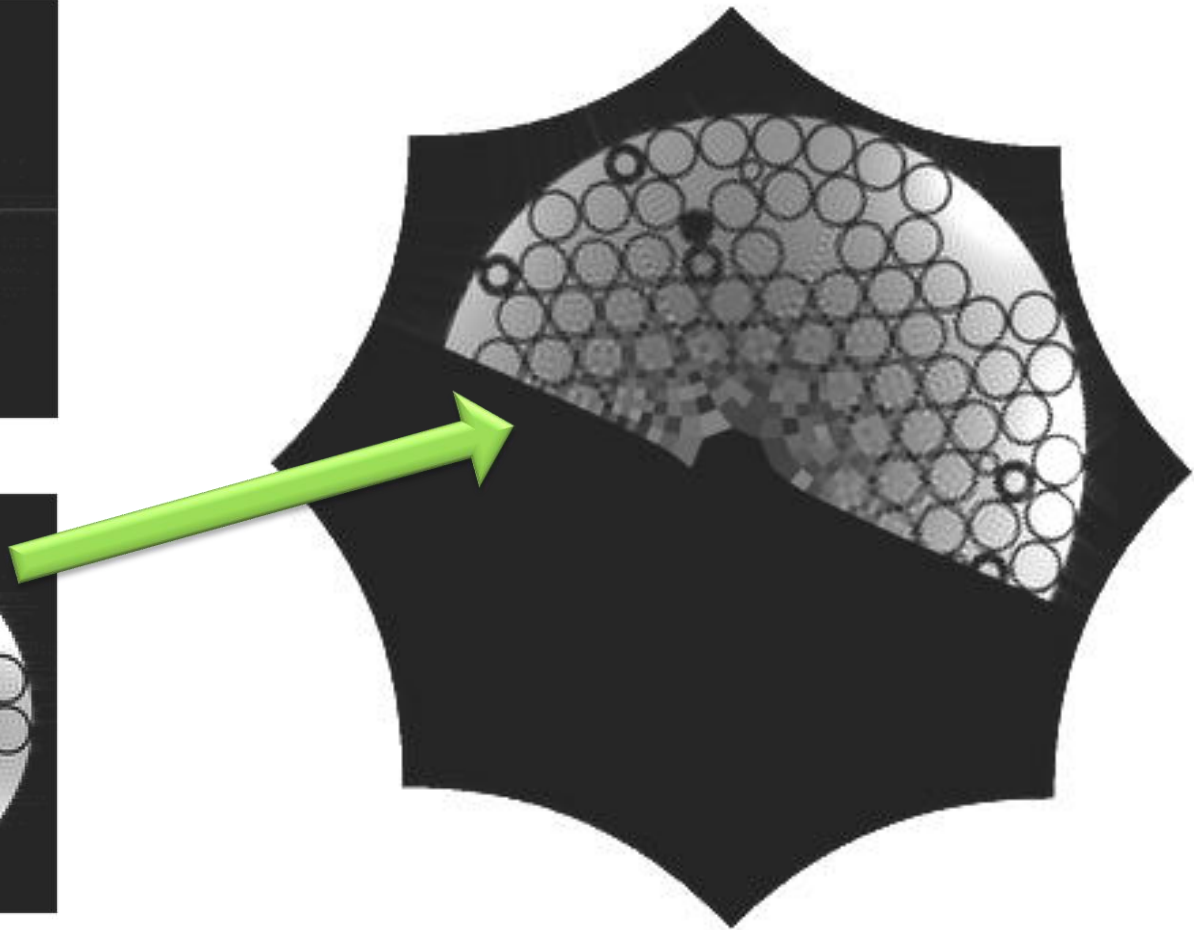
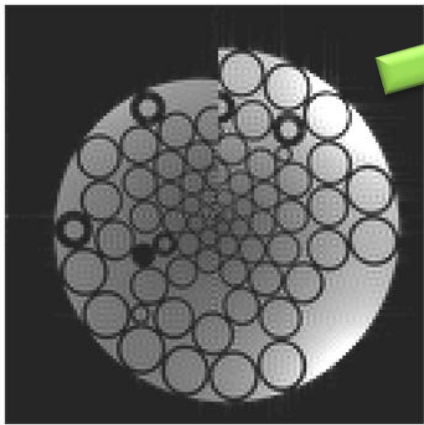
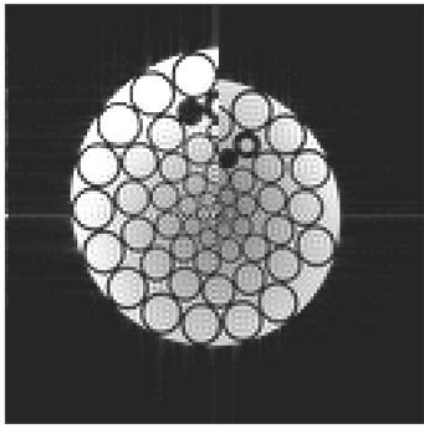
# Make 'human readable'

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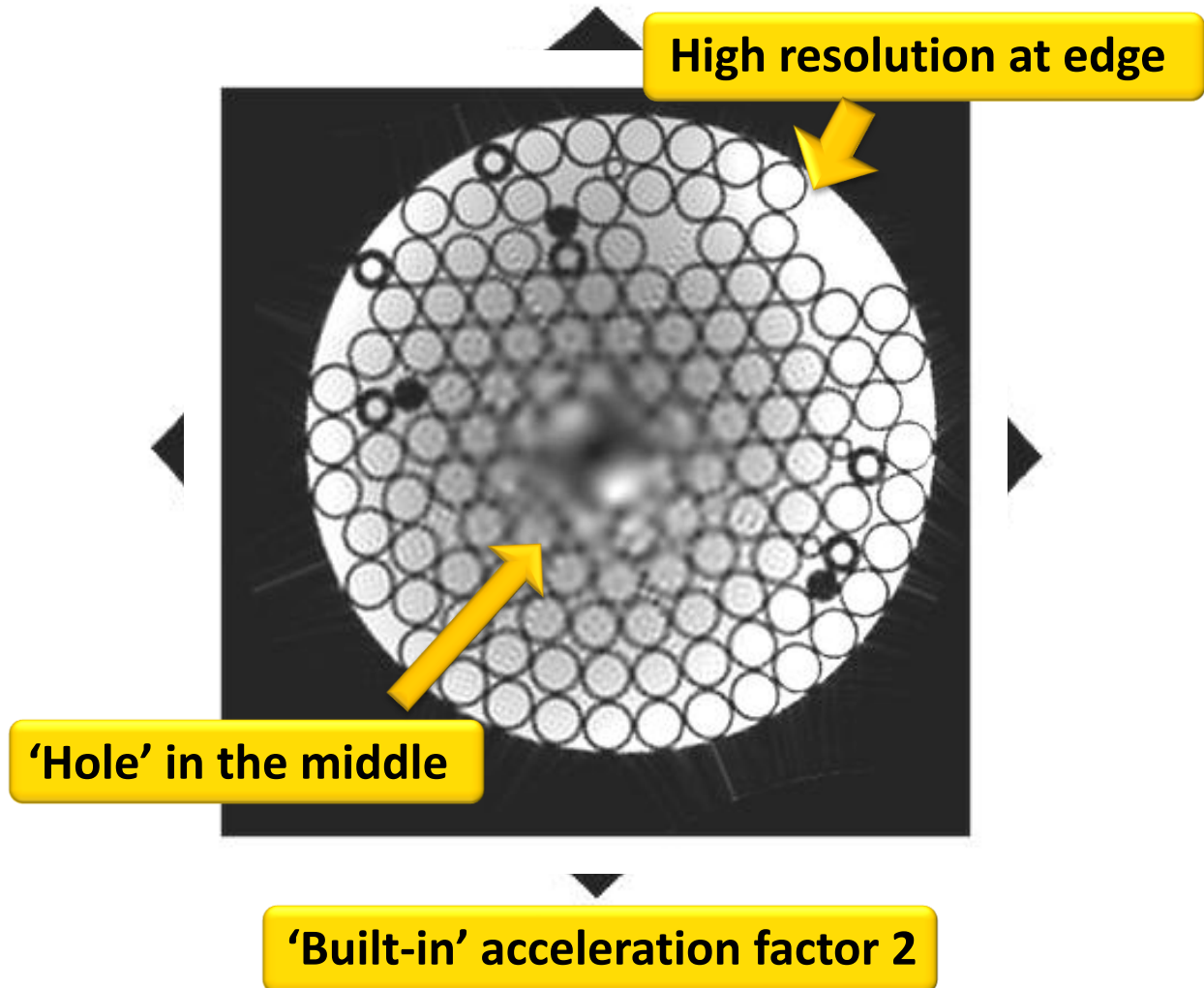
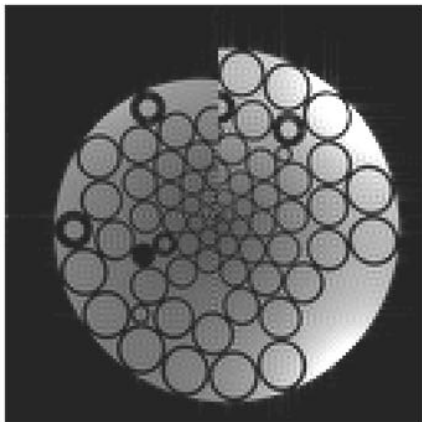
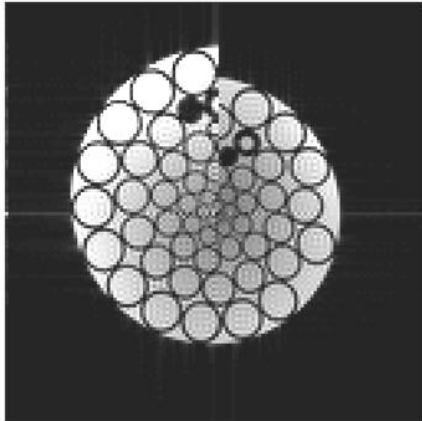
# Make 'human readable'

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# Make 'human readable'

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# PatLoc

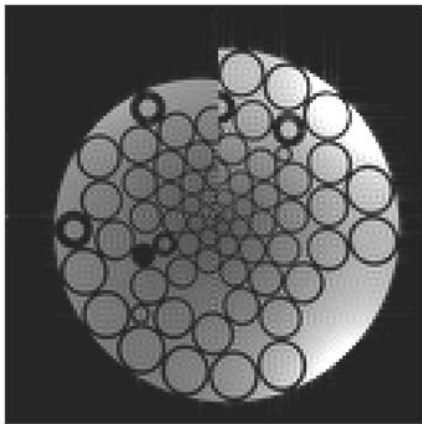
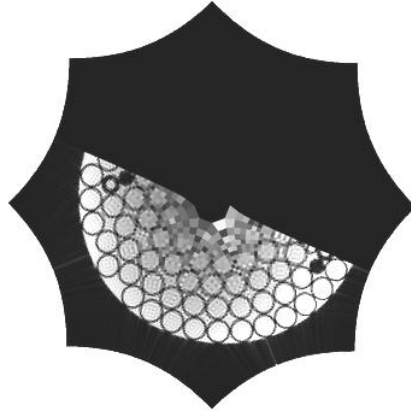
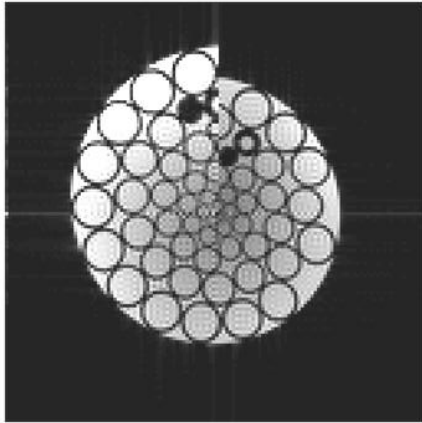
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Parallel imaging technique  
using localized gradients

Hennig *et al*, MAGMA 2008

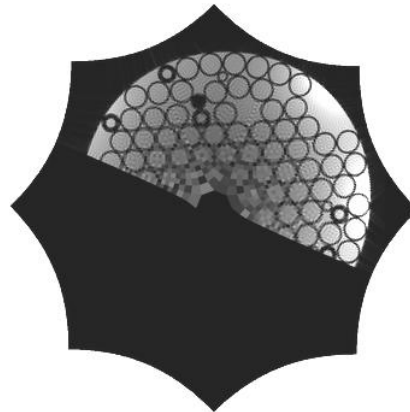
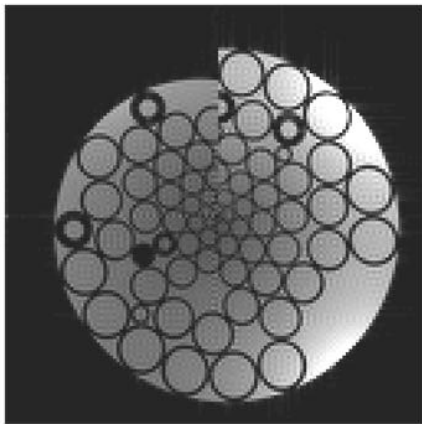
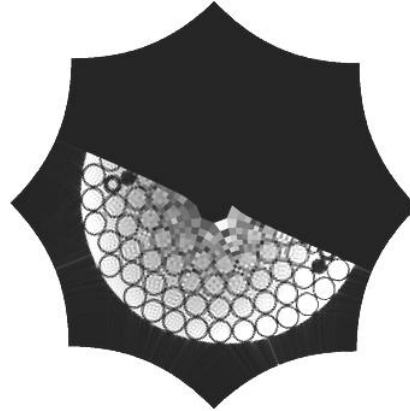
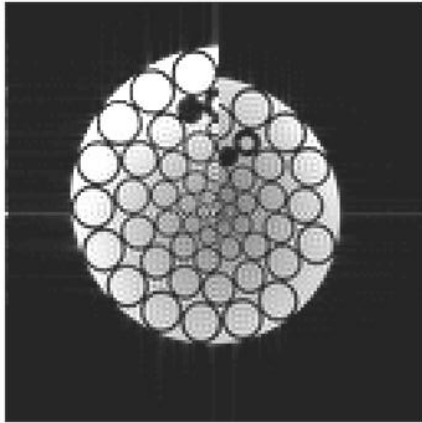
# Understanding the aliasing

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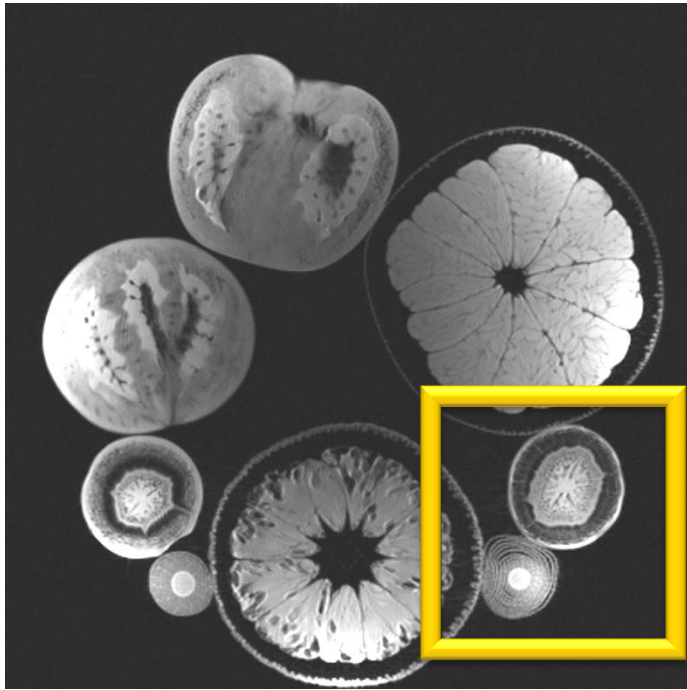
# Understanding the aliasing

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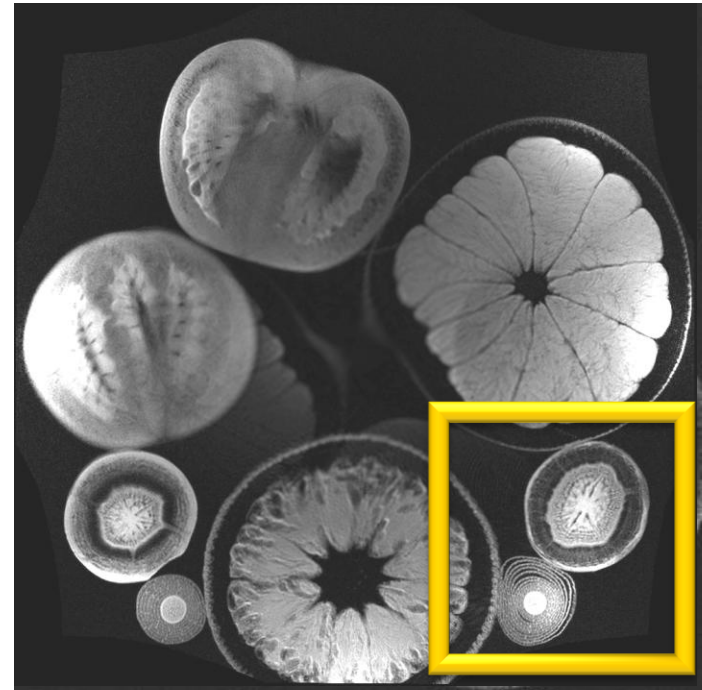


# Seeing the benefit

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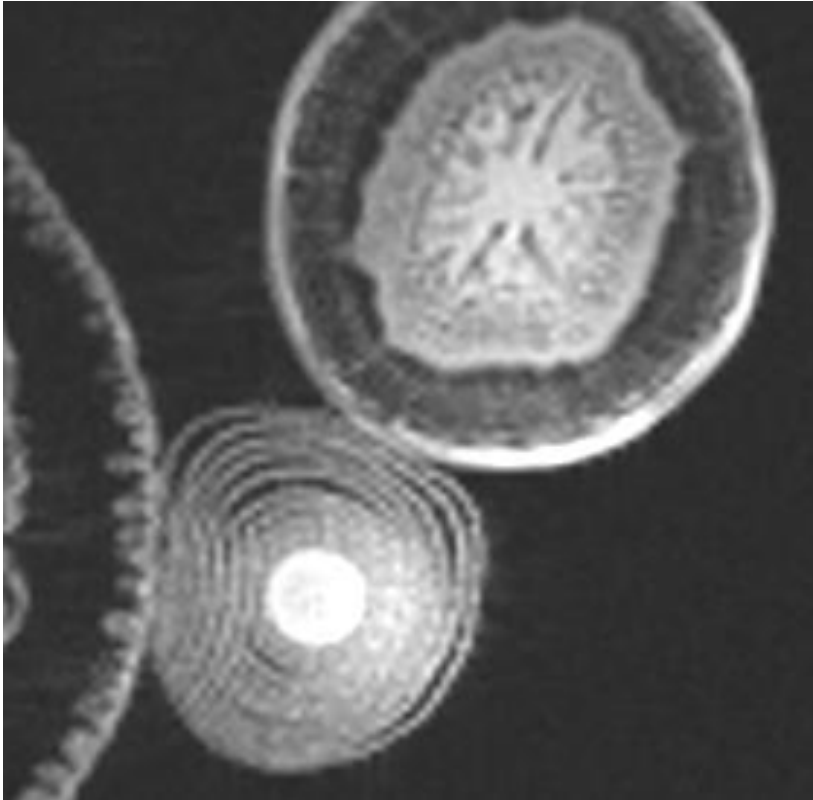
Linear gradients



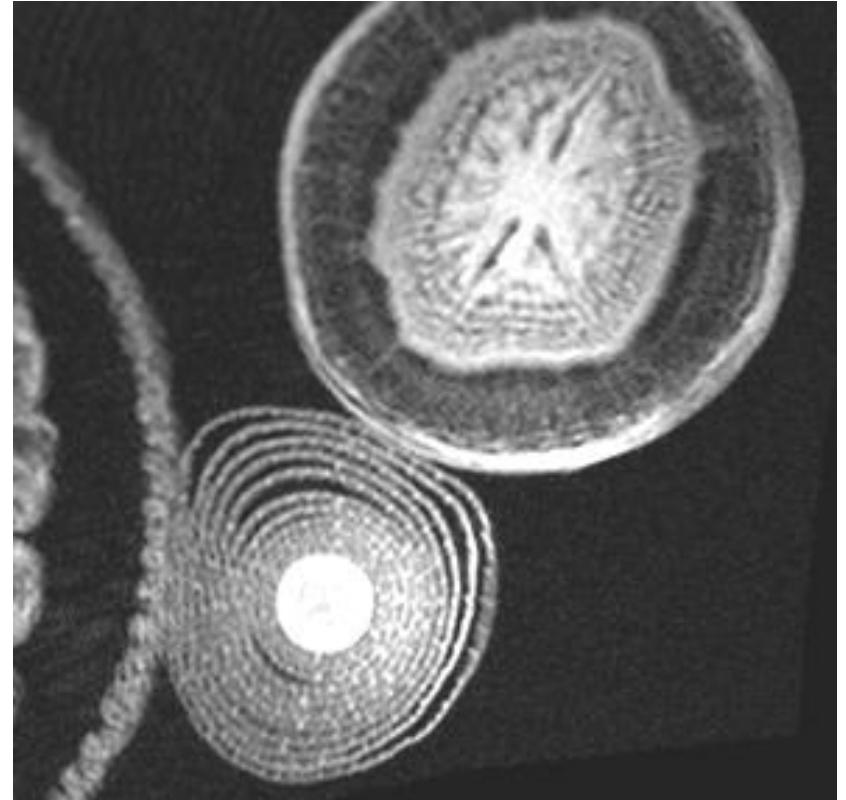
Quadratic gradients

# Seeing the benefit

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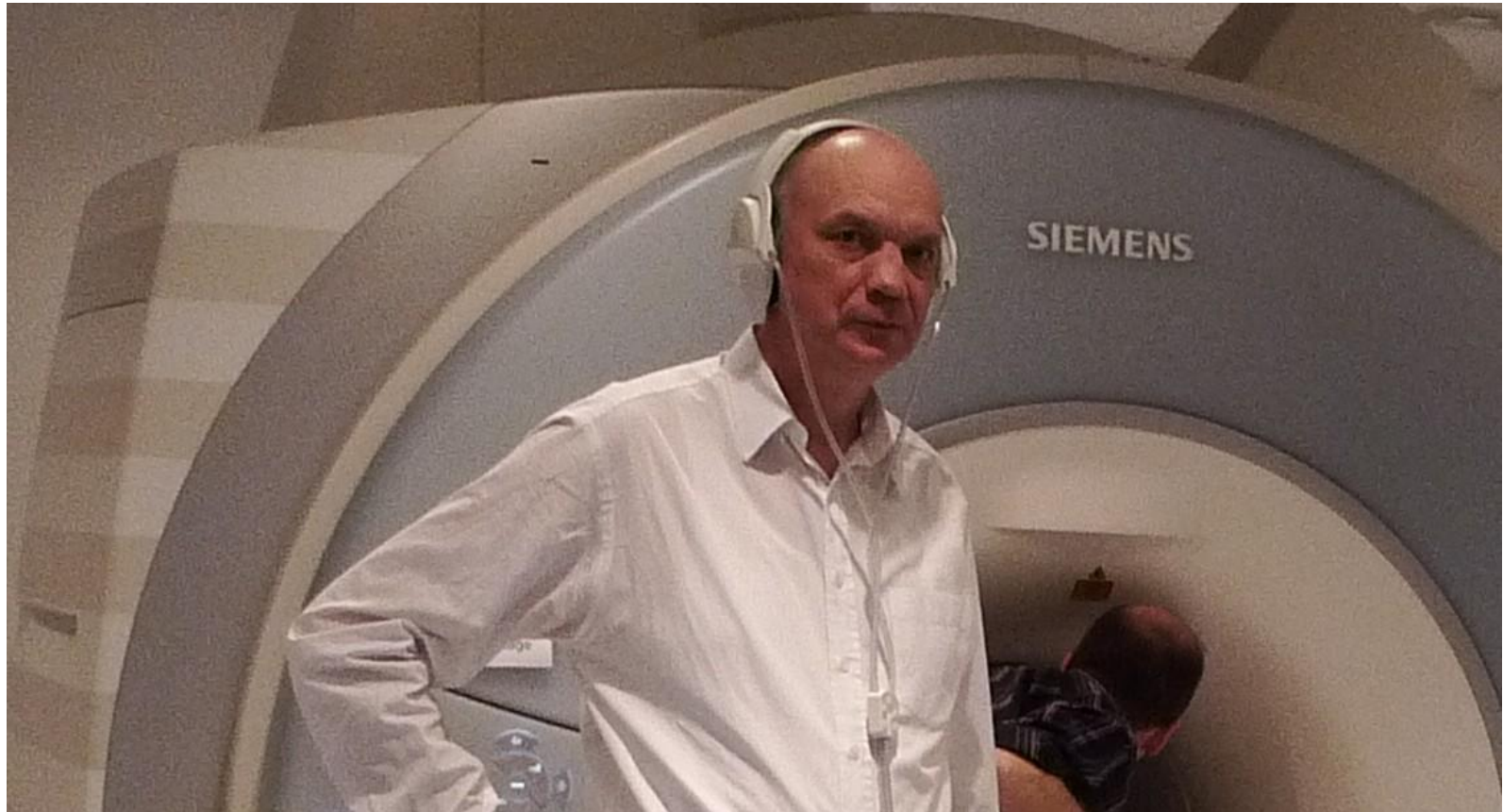
Linear gradients



Quadratic gradients

# And now... the first volunteer...

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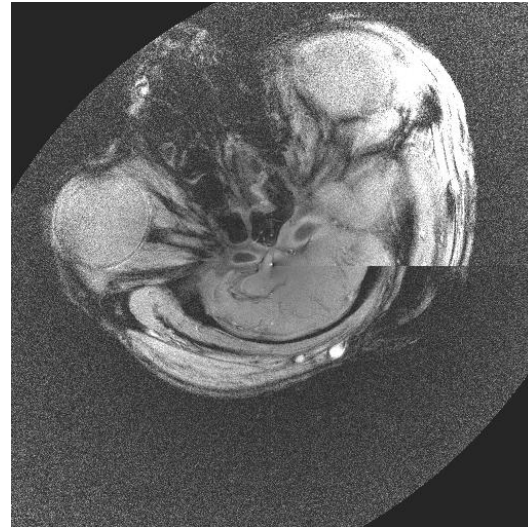
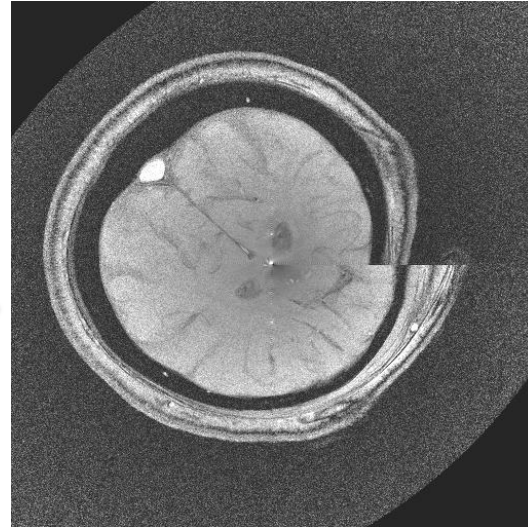
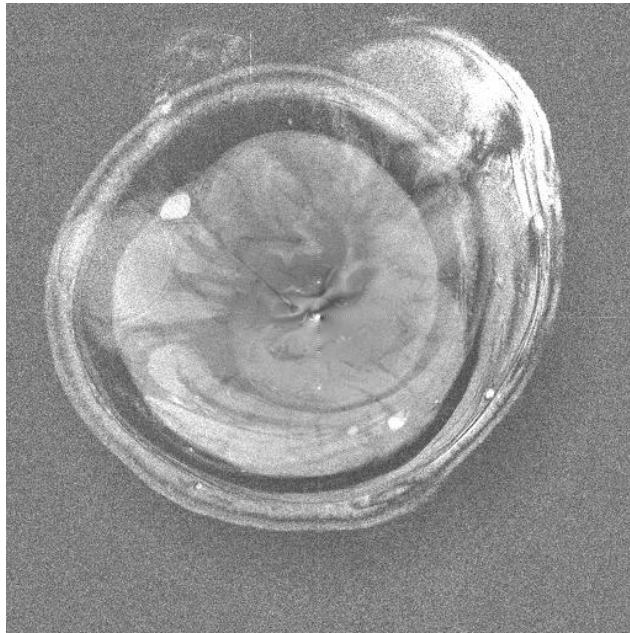
# And the first image...

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# And after some processing...

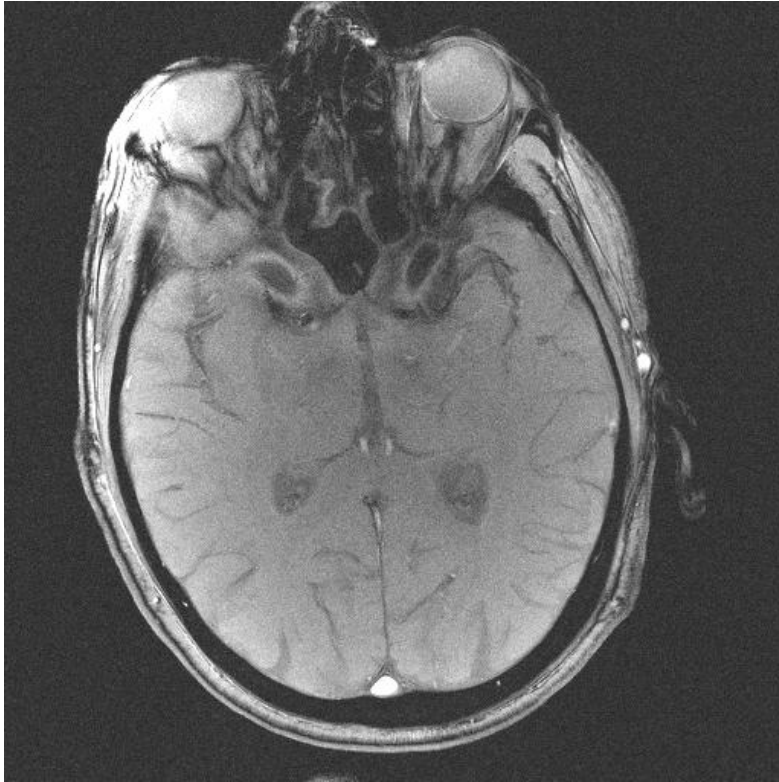
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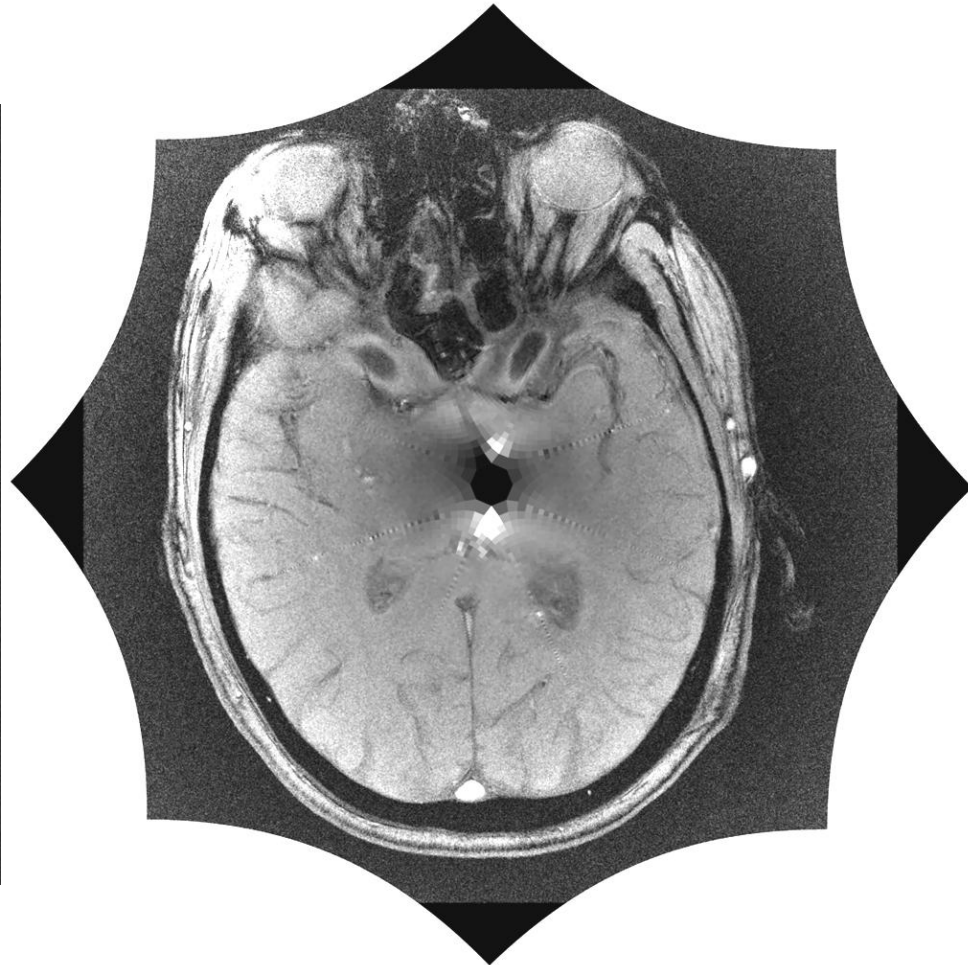


# And after some processing...

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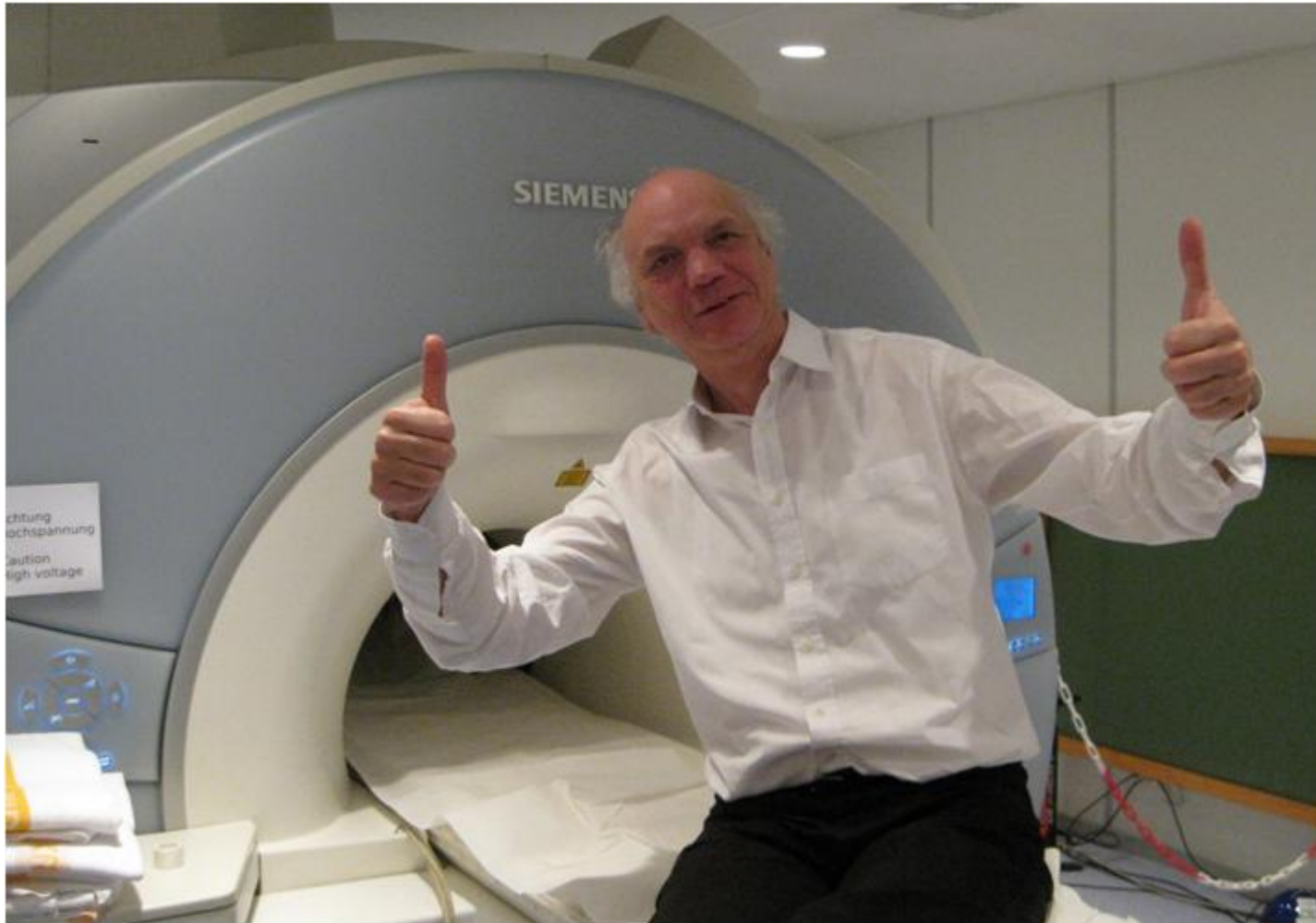
Linear encoding



Quadratic encoding

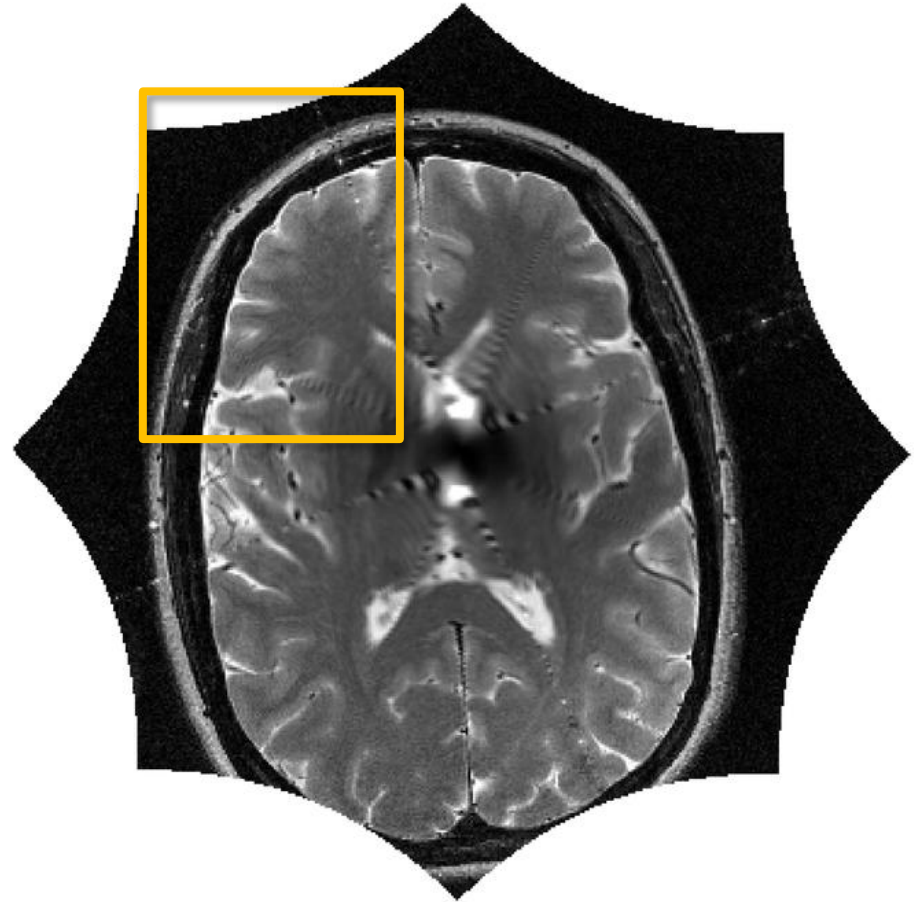
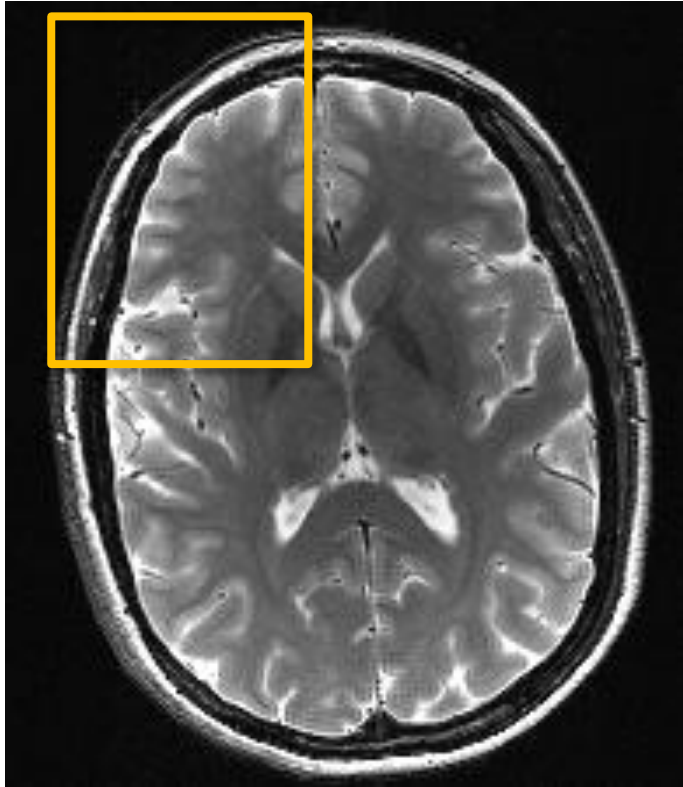
# Subject approval

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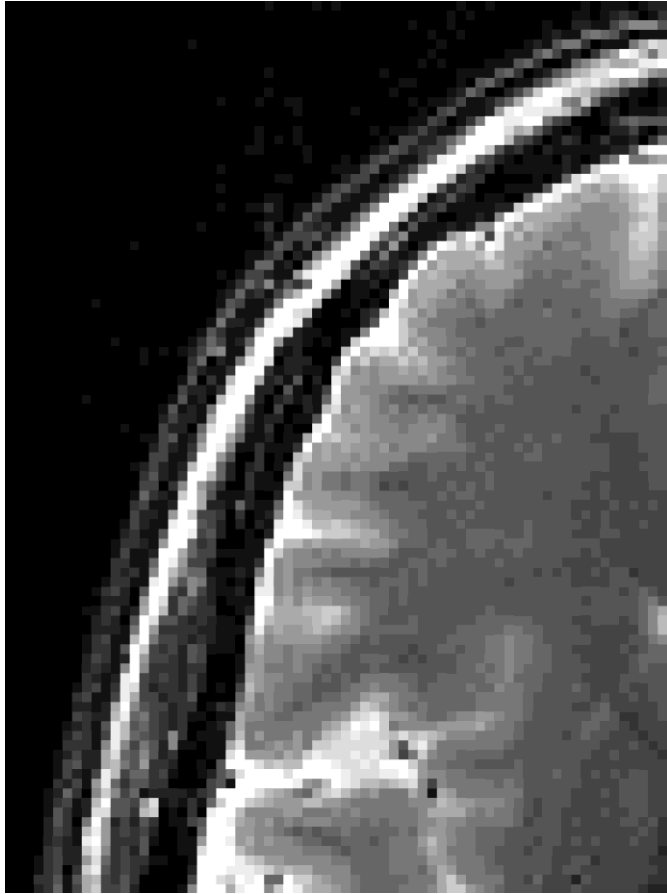
# And different contrast...

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# And different contrast...

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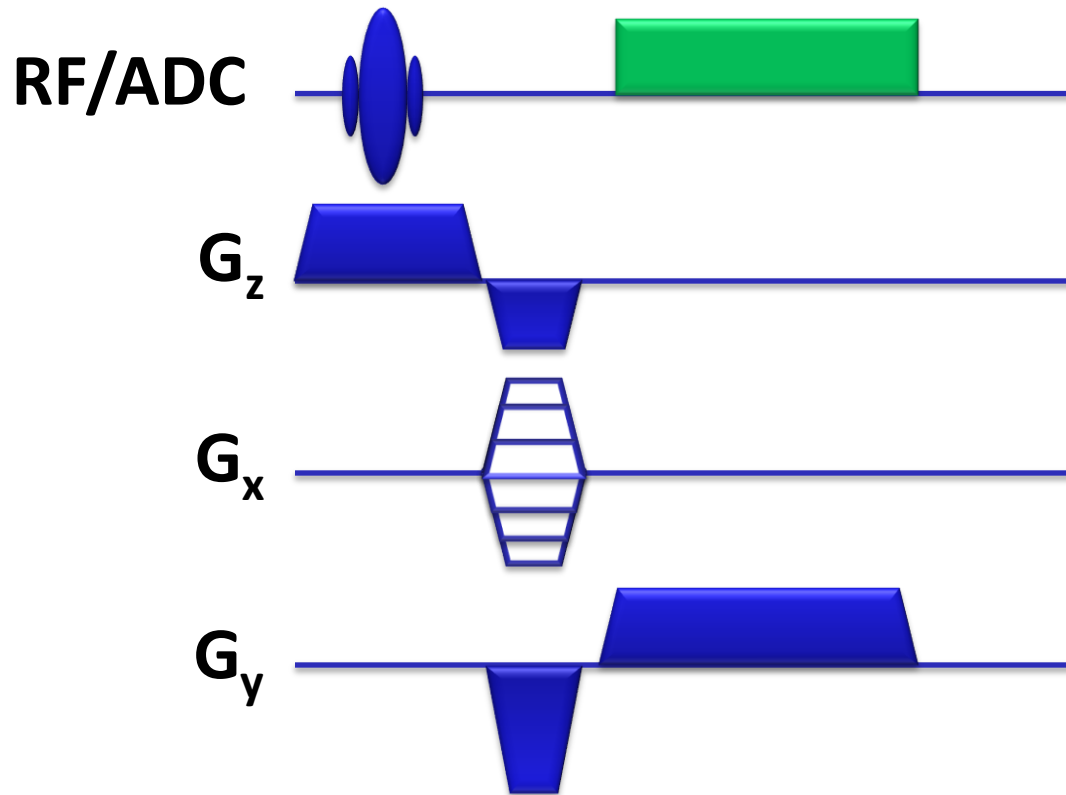
# Taking things further...

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Linear gradients and quadratic gradients, simultaneously

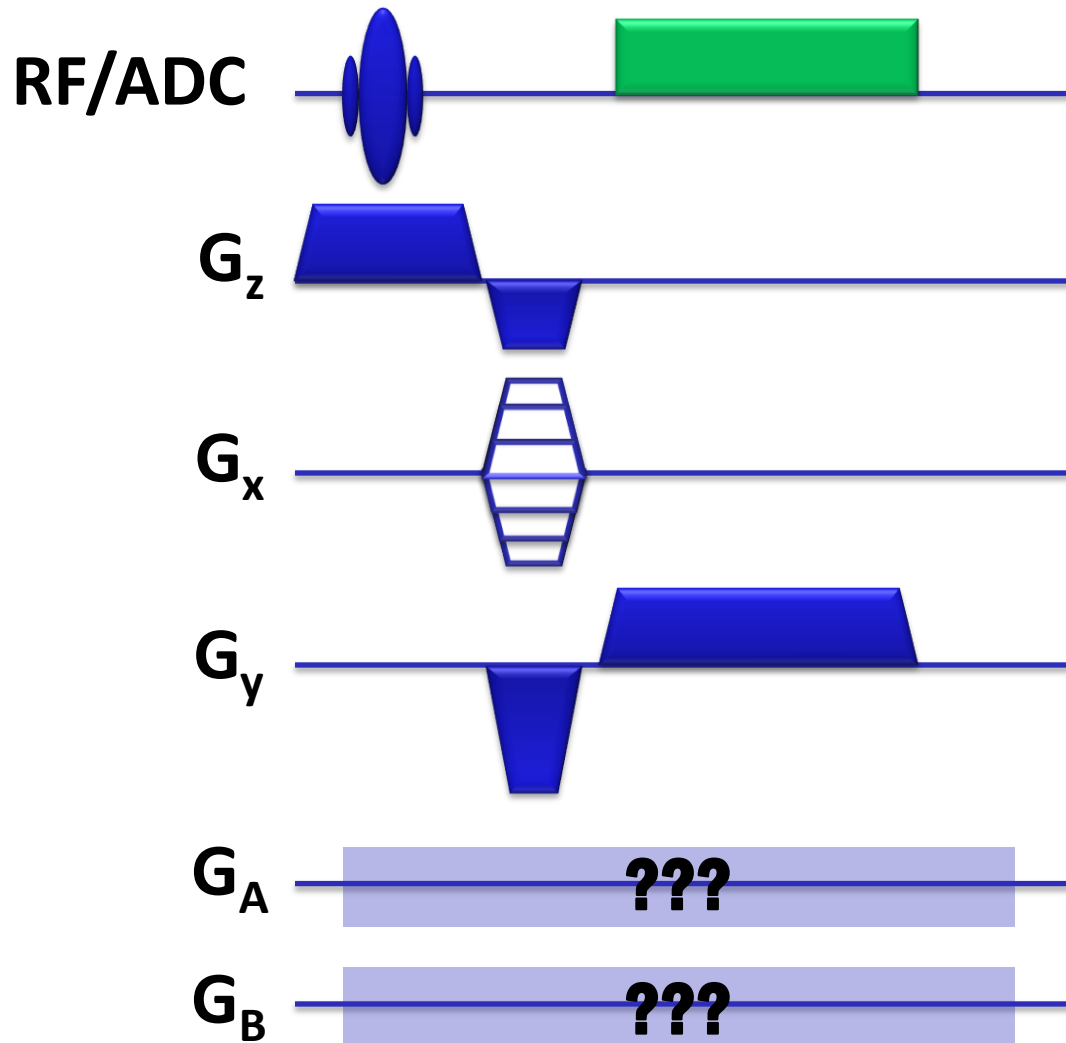
# A standard pulse sequence

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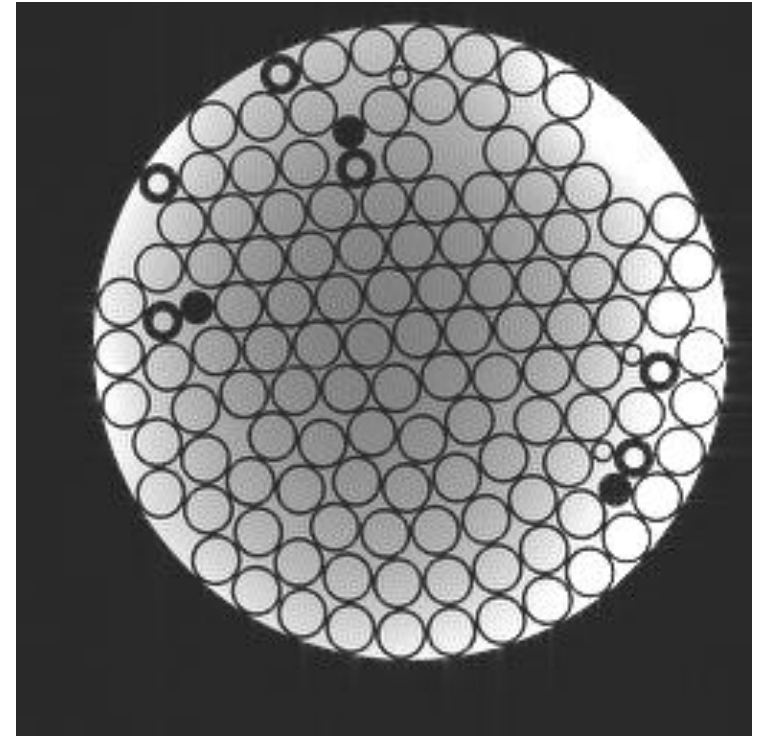
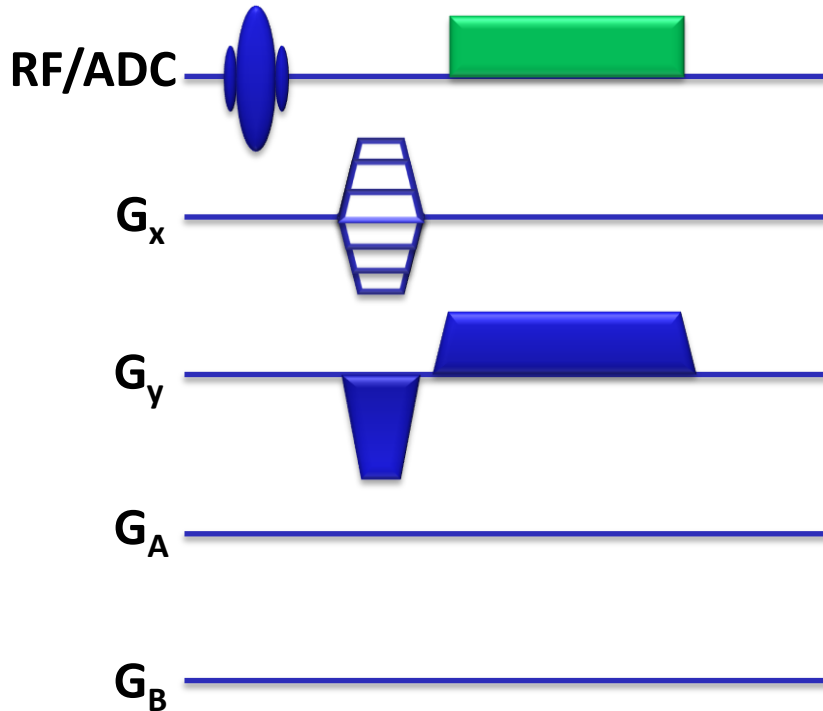
# 5 independent spatial encoding channels!

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# The familiar method of encoding

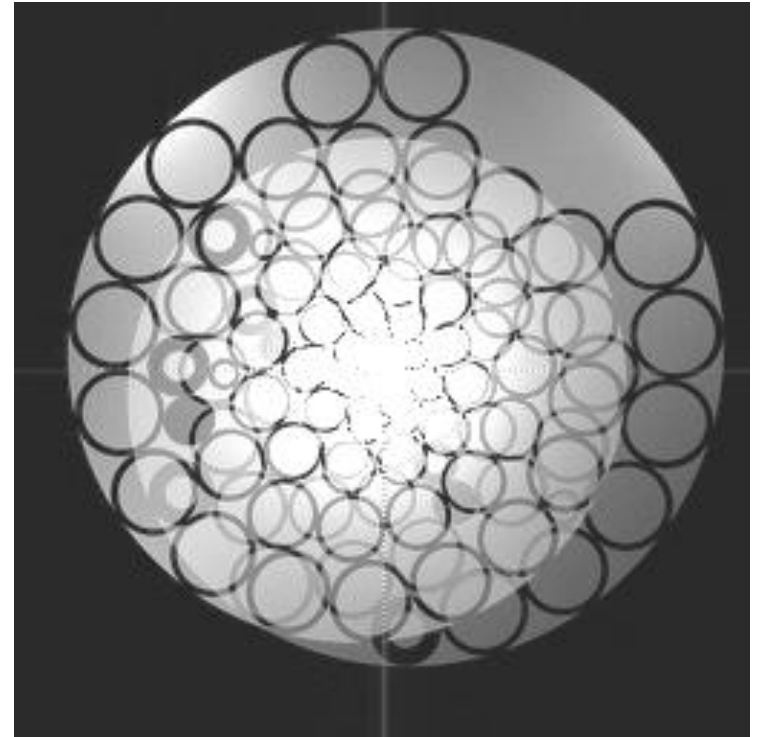
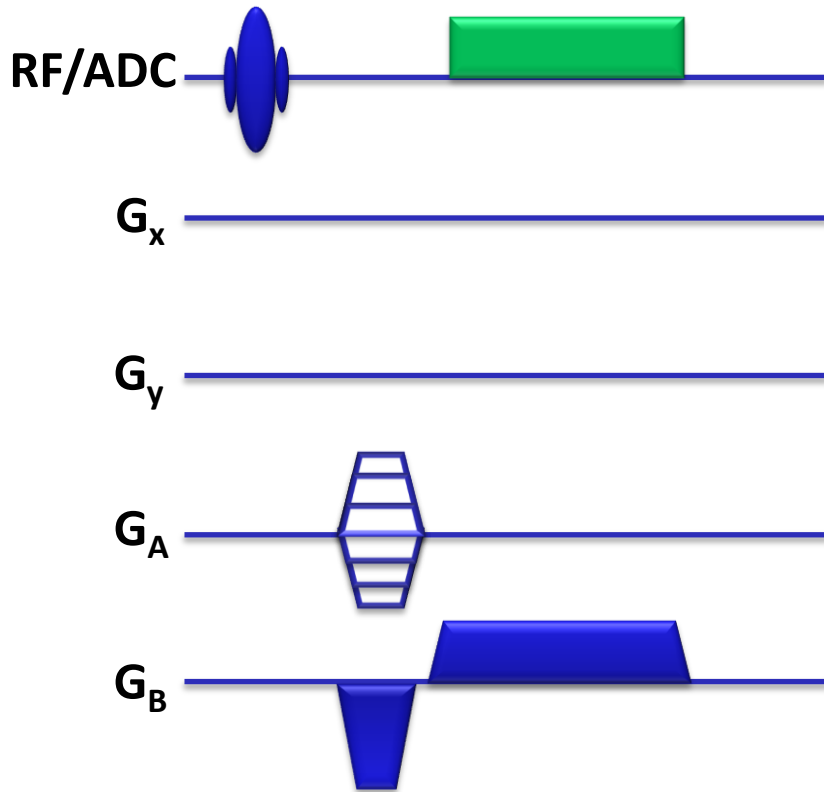
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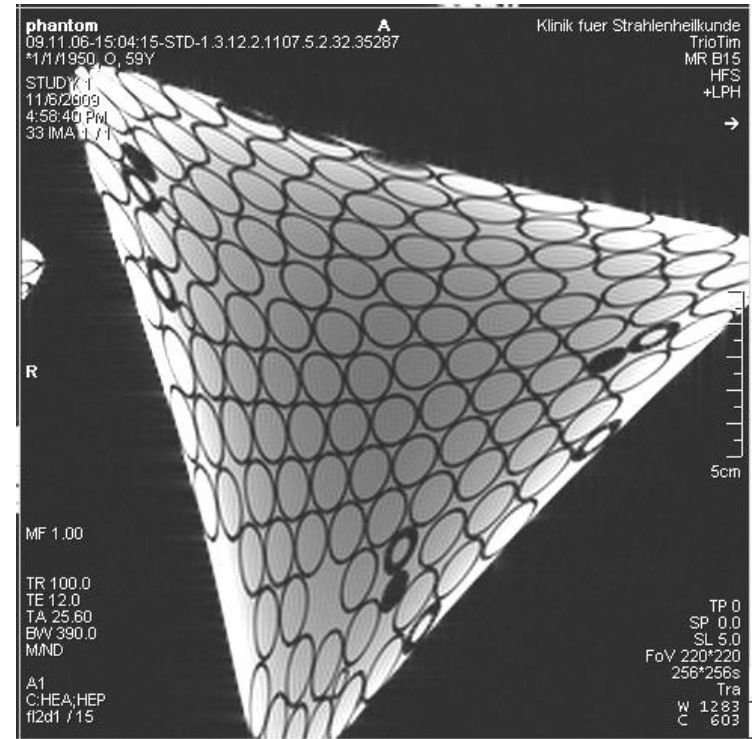
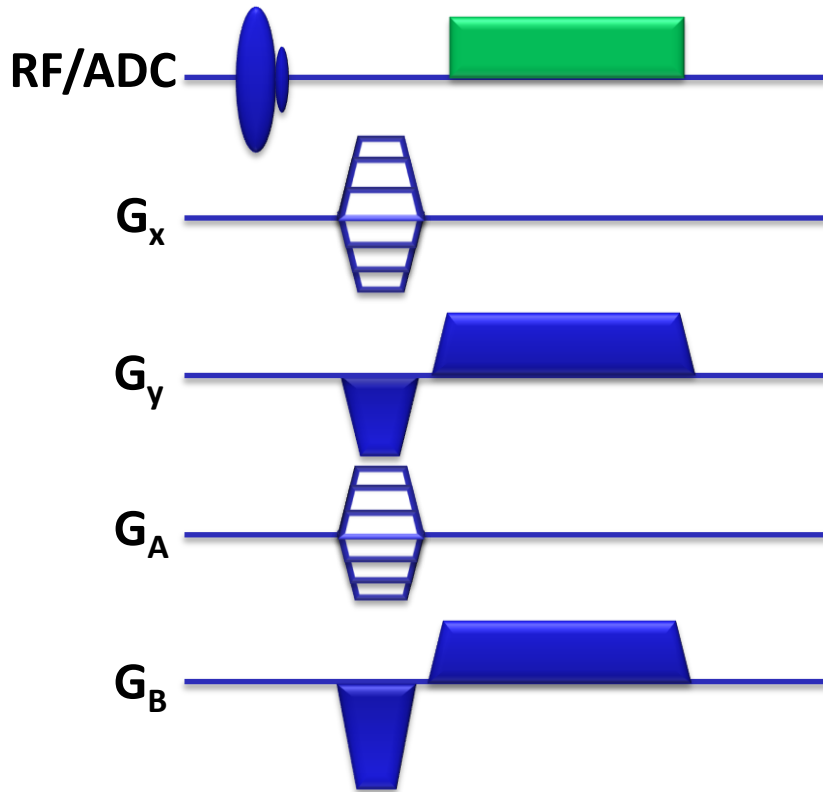


# The new-but-reasonably-understood way

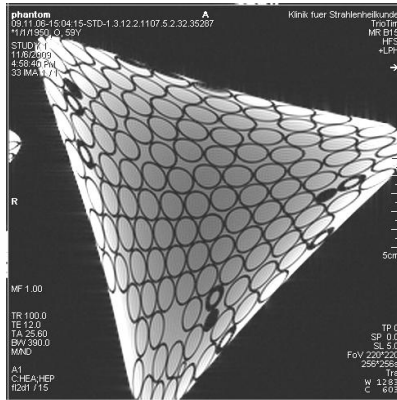
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# Uncharted territory...



# Uncharted territory...



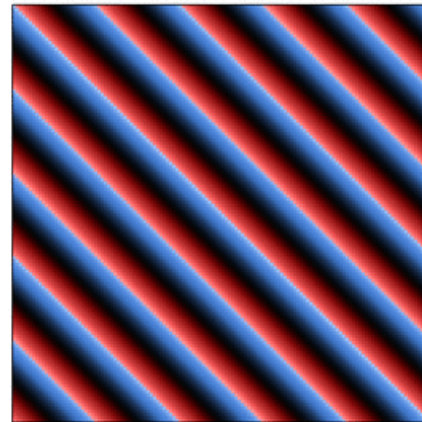
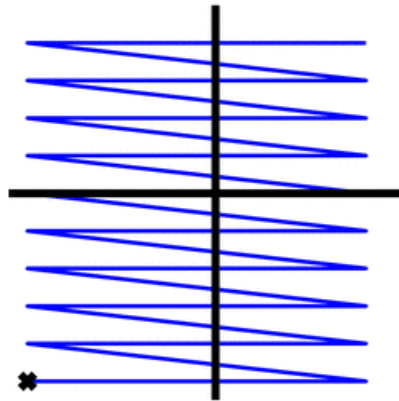
This is a weird image!

- How can we explain where this shape comes from?
- How can we predict things more generally?
- Can we use this to remove the PatLoc 'hole'?

# What patterns can we make?

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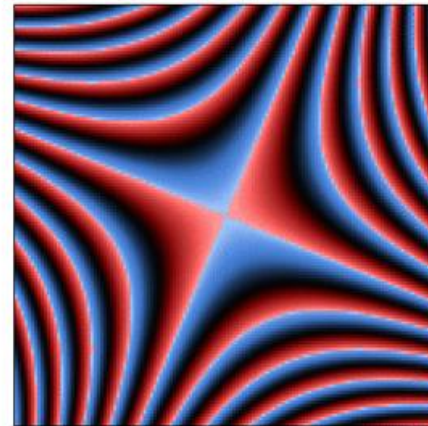
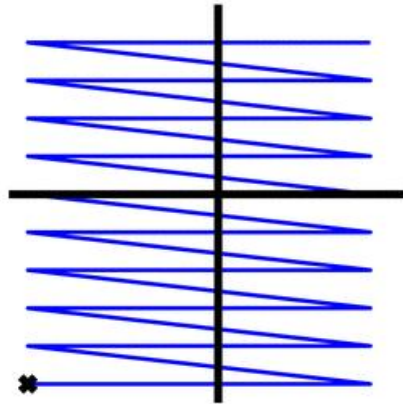
Just linear gradients



# What patterns can we make?

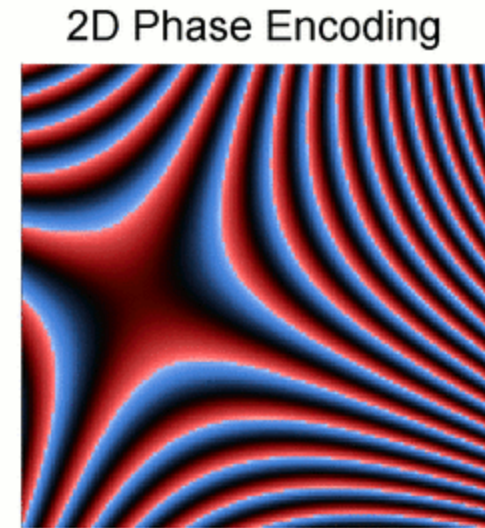
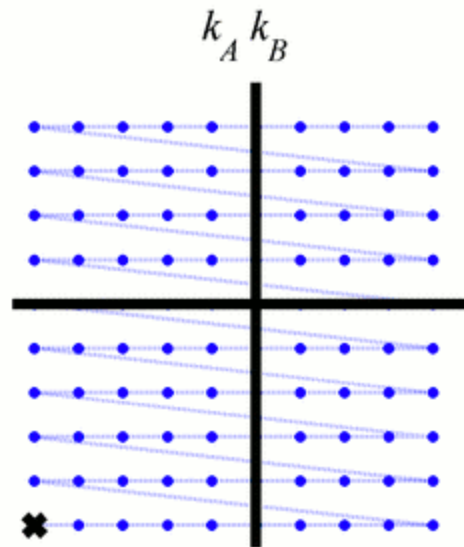
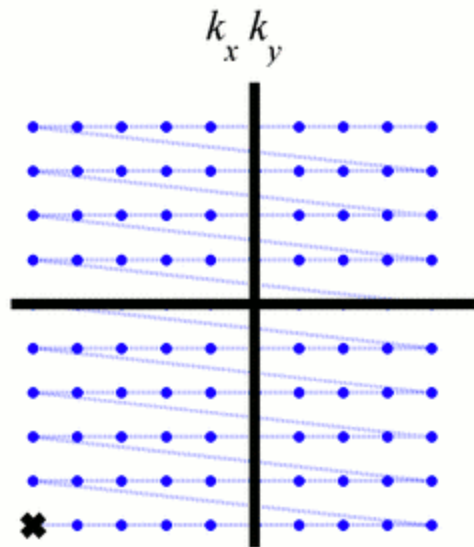
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Just quadratic gradients



# What patterns can we make?

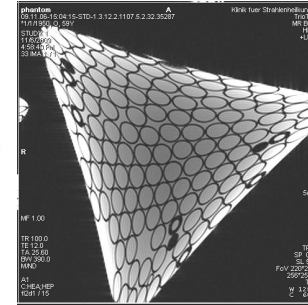
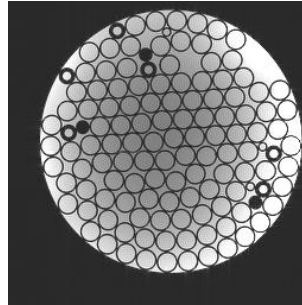
Linear gradients *and* PatLoc gradients



# But how does that explain the weird image?

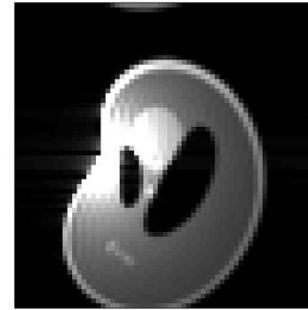
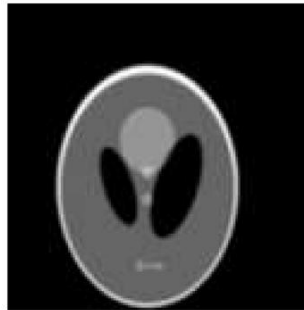
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Measured data:



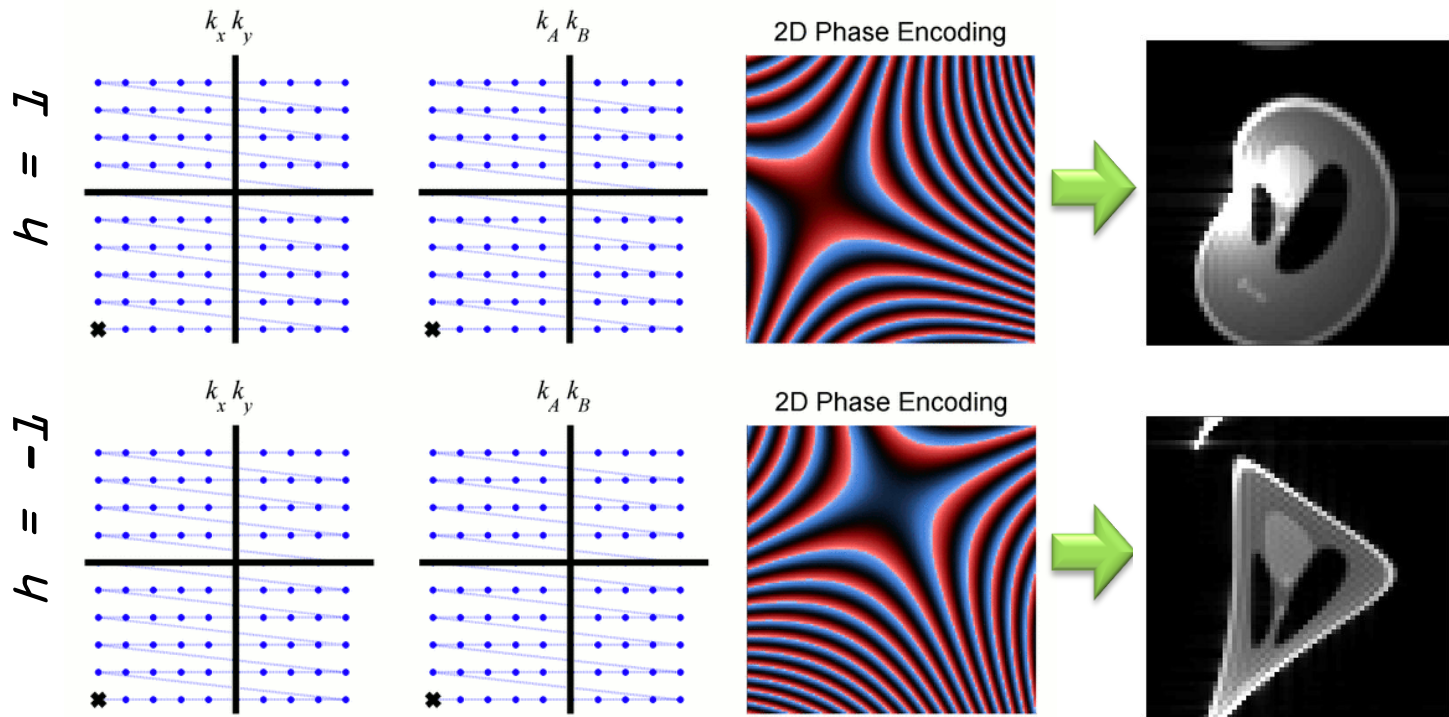
They don't match!

Simulation:



# But how does that explain the weird image?

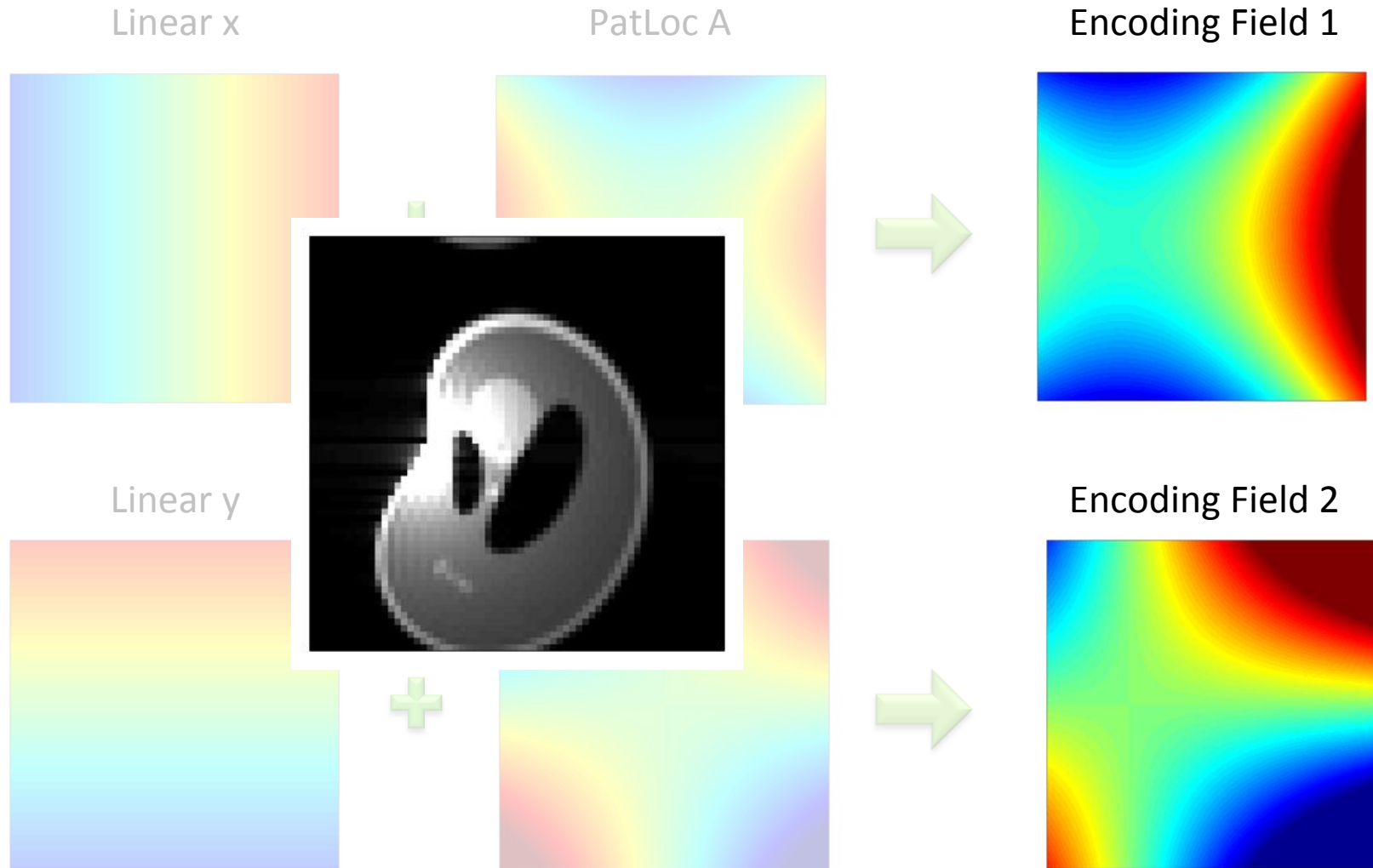
It turns out that 'handedness' of PatLoc fields is important:



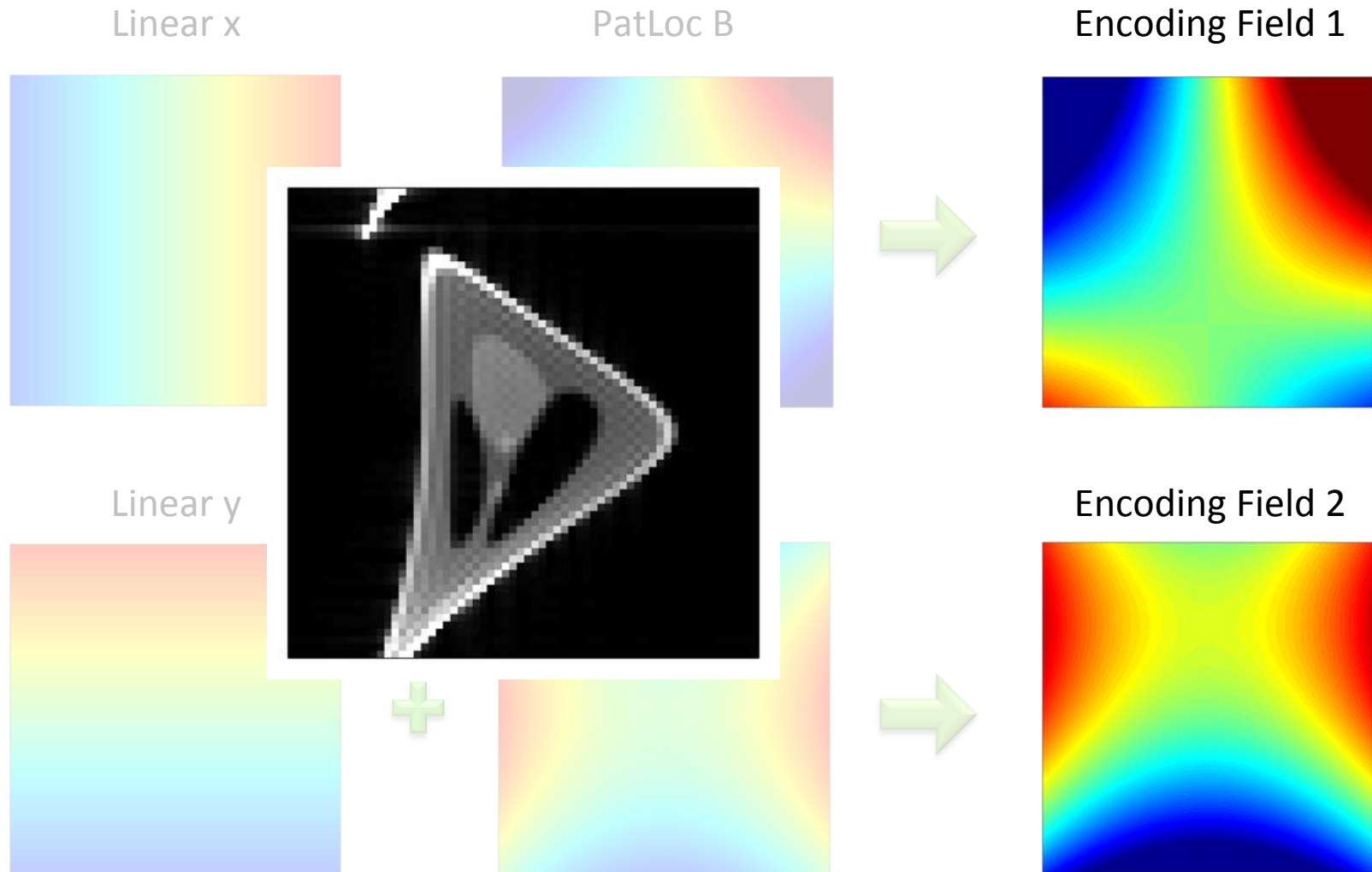
So clearly just looking at this 'dual  $k$ -space' is not enough to quickly tell the whole story



# But how does that explain the weird image?



# But how does that explain the weird image?



# But how does that explain the weird image?

---

Pure linear



Pure quadratic



$h = 1$



$h = -1$

# But how does that explain the weird image?

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Pure linear

Pure quadratic



$h = 1$



$h = -1$

# Getting rid of the hole...

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- New encoding fields need not remain proportional to the linear gradients
- Usually have two parameters  $(k_x, k_y)$  to encode 2D image
  - Now have four parameters  $(k_x, k_y, k_A, k_B)$  to encode 2D image
- Image reconstruction more complicated...

# Generalized Reconstruction

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$$\mathbf{s} = \mathbf{E}\mathbf{m}$$

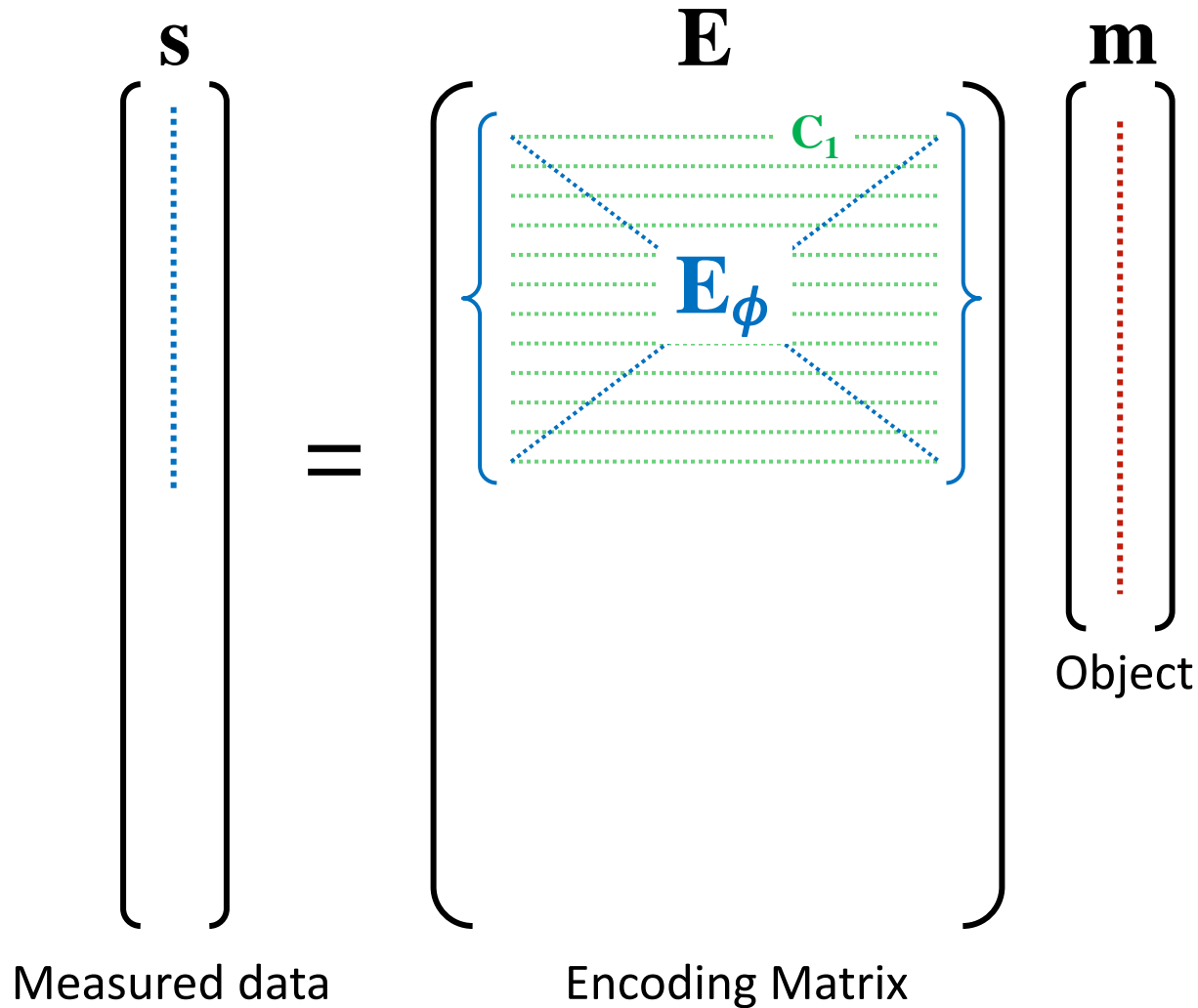
# Generalized Reconstruction

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$$\begin{array}{ccc} \mathbf{s} & & \mathbf{E} & & \mathbf{m} \\ \left[ \begin{array}{c} \phantom{s} \\ \phantom{s} \\ \phantom{s} \\ \phantom{s} \\ \phantom{s} \\ \phantom{s} \\ \phantom{s} \\ \phantom{s} \\ \phantom{s} \\ \phantom{s} \end{array} \right] & = & \left[ \begin{array}{c} \phantom{E} \\ \phantom{E} \\ \phantom{E} \\ \phantom{E} \\ \phantom{E} \\ \phantom{E} \\ \phantom{E} \\ \phantom{E} \\ \phantom{E} \\ \phantom{E} \end{array} \right] & \left[ \begin{array}{c} \phantom{m} \\ \phantom{m} \\ \phantom{m} \\ \phantom{m} \\ \phantom{m} \\ \phantom{m} \\ \phantom{m} \\ \phantom{m} \\ \phantom{m} \\ \phantom{m} \end{array} \right] \\ \text{Measured data} & & \text{Encoding Matrix} & & \text{Object} \end{array}$$

# Generalized Reconstruction

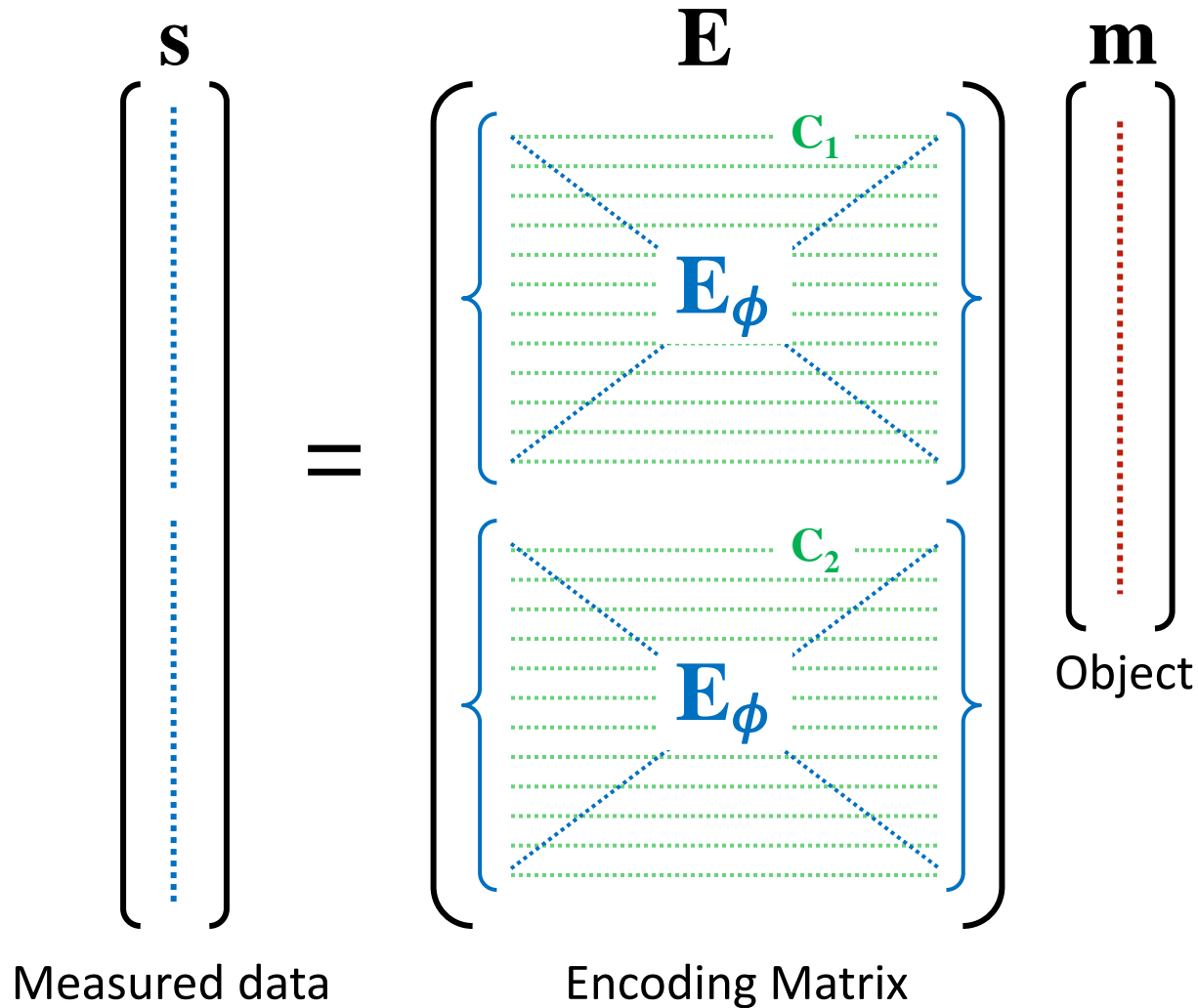
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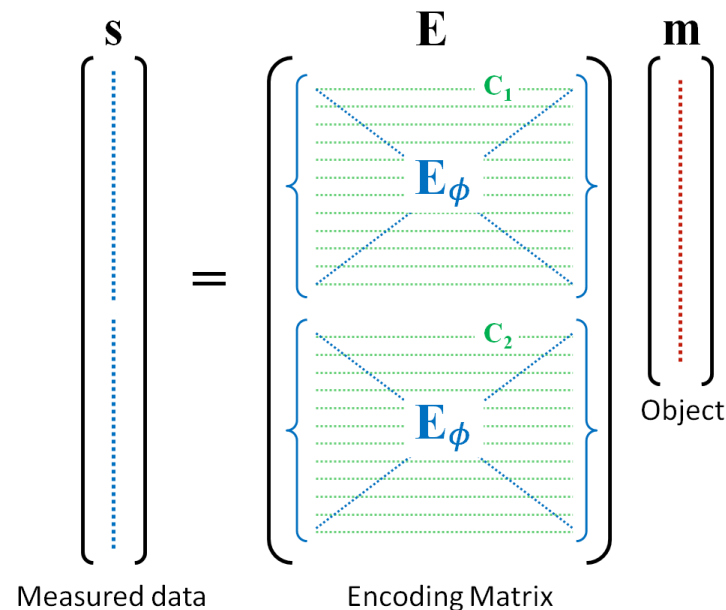
# Generalized Reconstruction

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# Generalized Reconstruction

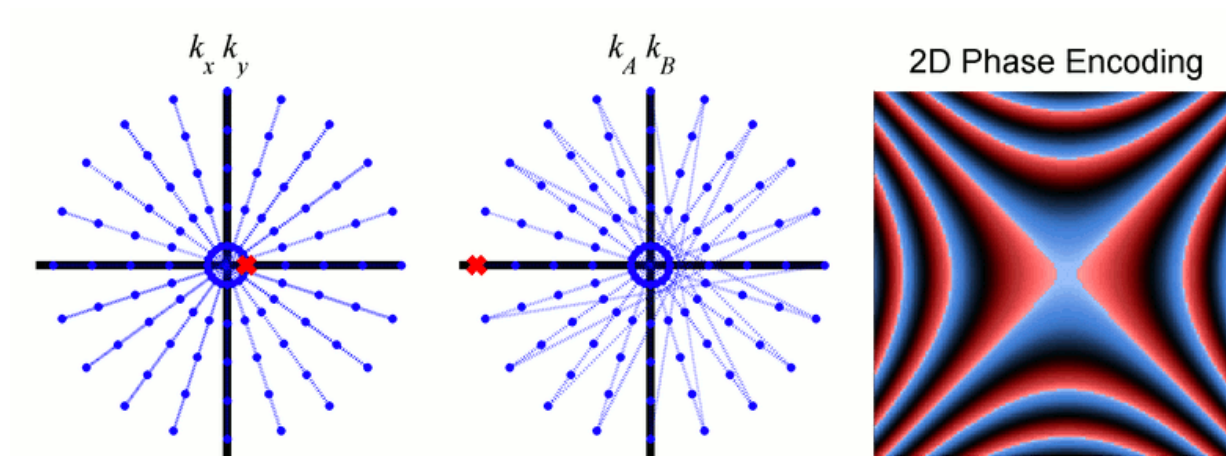
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- Reconstruction then performed with an iterative method, such as conjugate gradients

# 4D Radial-based trajectory (4D-RIO)

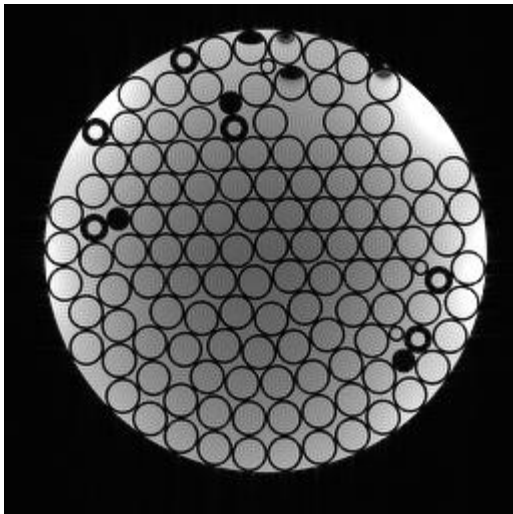
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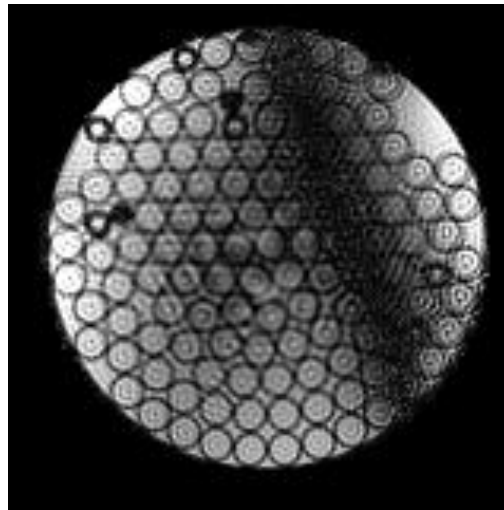
# Experimental verification

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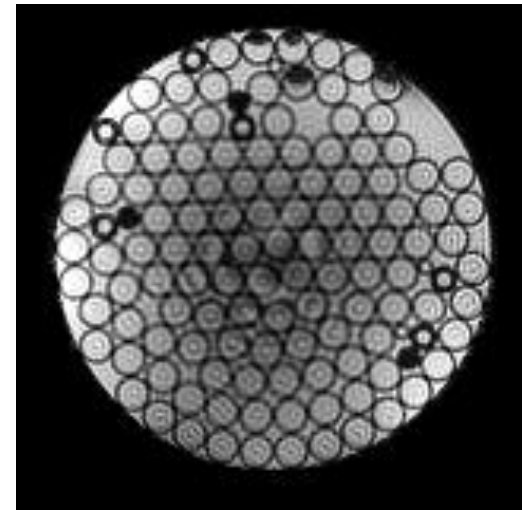
- 128 samples x 128 spokes, 8 RF coils
- Reconstructed to 160x160 Cartesian grid  
Encoding matrix 27 Gb, recon originally took ~10 hours on Desktop PC, now ~3 minutes in a more optimised parallel accelerated version



Phantom



4D-RIO



4D-RIO  
After calibration

# Experimental verification – in vivo

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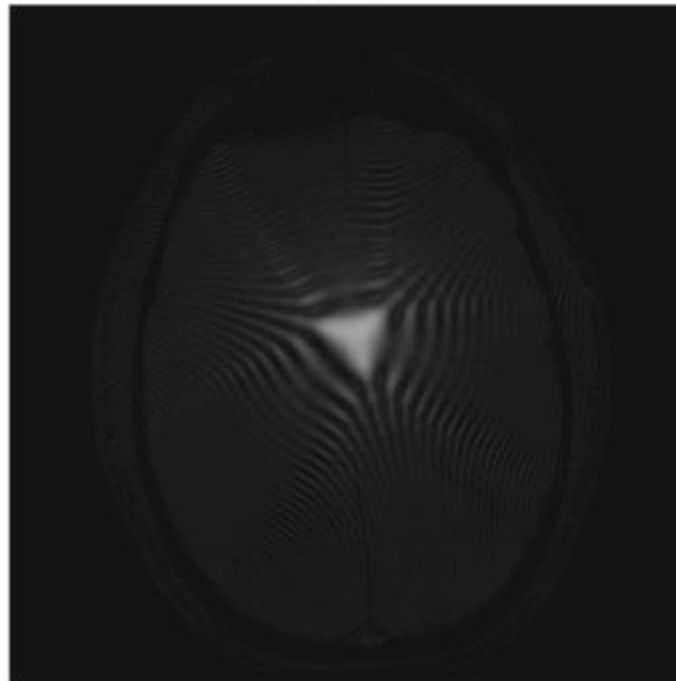
- 256 samples x 256 spokes, 8 RF coils
- Reconstructed to 320x320 Cartesian grid
  - Encoding matrix 430 Gb – ‘fast’ code takes ~30 mins per iteration
  - New Matlab-based GPU implementation ~ 10 sec per iteration

# Experimental verification – in vivo

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- 256 samples x 256 spokes, 8 RF coils
- Reconstructed to 320x320 Cartesian grid  
Encoding matrix 430 Gb – ‘fast’ code takes ~30 mins per iteration  
New Matlab-based GPU implementation ~ 10 sec per iteration

Iteration: 1



# Conclusions

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- PatLoc offers exciting new opportunities for spatial encoding in MRI
- Nonlinear encoding can still be performed in the ‘traditional’ way
  - Phase/Frequency encoding
  - SENSE-like reconstruction to resolve ambiguities
- More generally, encoding can be almost arbitrary – but reconstruction is slower
  - Is there an ‘optimal’ encoding pattern for a given scan time?

# The making of...





# Acknowledgements

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