

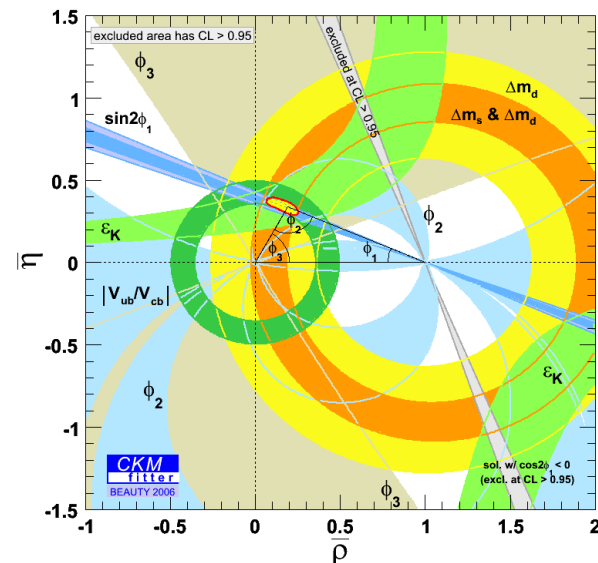
# CKM fitter

シーケーエムフィッター

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JOINT LAB  
JAPAN - FRANCE



FJPPL'08 – CNRS/IN2P3 Headquarter May 15-16 2008

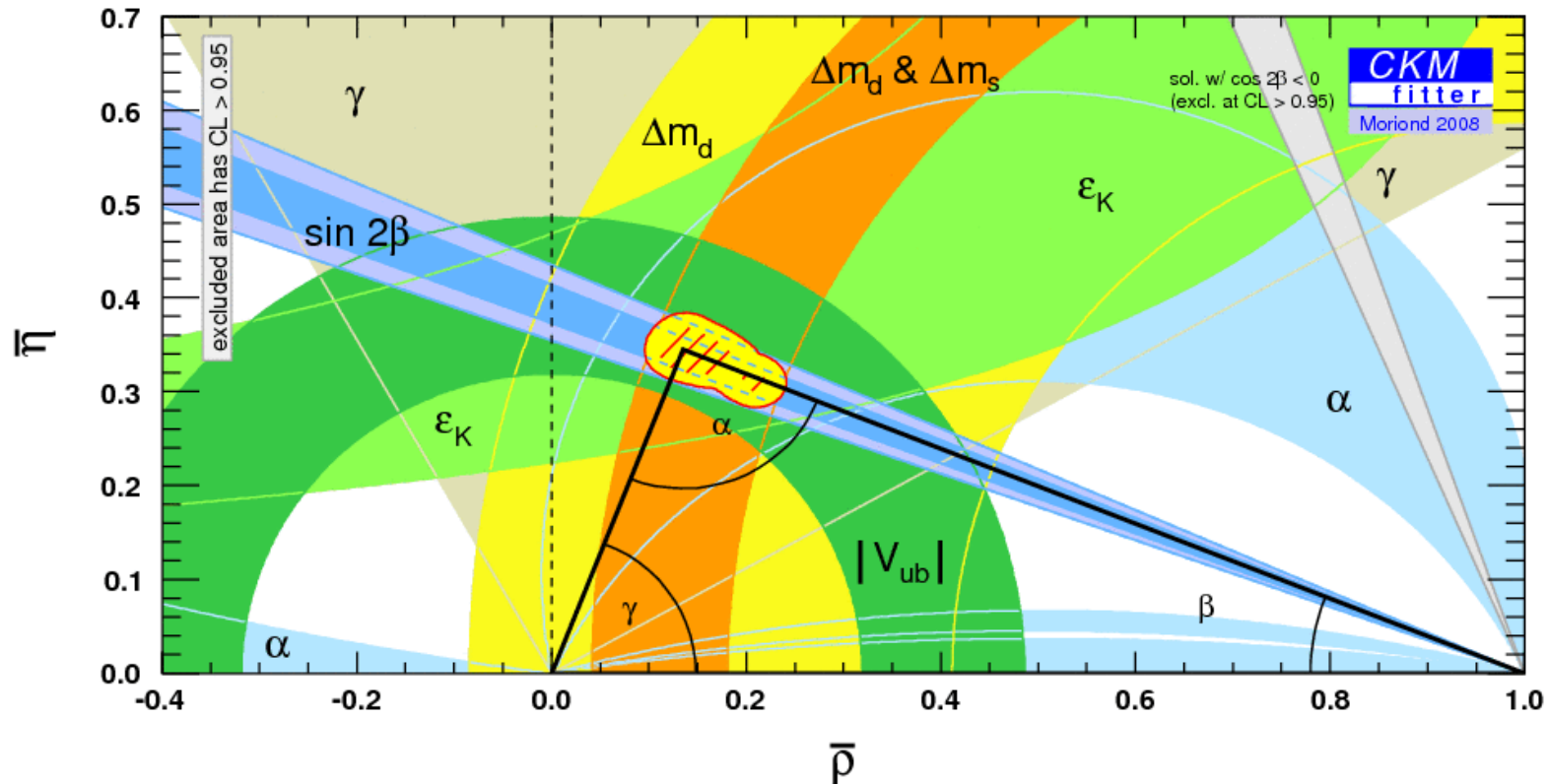


# Outline

## ☀ FJPPL '08:


- SuperBelle: Prospective with  $10 \text{ ab}^{-1}$
- $\Delta F=1$  FCNC transitions: NP in Wilson Coefficients
- Determination of the angle  $\gamma/\phi_3$ :
  - statistics: p-value and nuisance parameters

# Why believe the KM mechanism?



The **great success** of the B factories and Tevatron (and the Standard Model):  
the **KM mechanism is the dominant source of CPV** at the EW scale.

But the UT is not the whole story!

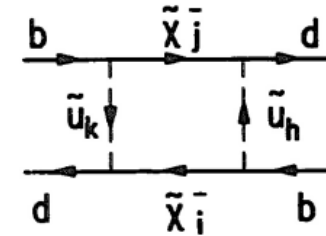
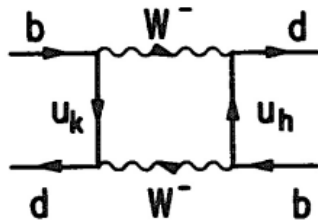
decreasing SM contrib. 			
	$b \rightarrow s \ (\sim \lambda^2)$	$b \rightarrow d \ (\sim \lambda^3)$	$s \rightarrow d \ (\sim \lambda^5)$
$\Delta F=2$ box	$\Delta M_{B_s}$ $A_{CP}(B_s \rightarrow \psi \phi)$	$\Delta M_{B_d}$ $A_{CP}(B_d \rightarrow \psi K)$	$\Delta M_K, \ \epsilon_K$
$\Delta F=1$ 4-quark box	$B_d \rightarrow \phi K, B_d \rightarrow K\pi, \dots$	$B_d \rightarrow \pi\pi, B_d \rightarrow \rho\pi, \dots$	$\epsilon'/\epsilon, K \rightarrow 3\pi, \dots$
gluon penguin	$B_d \rightarrow X_s \gamma, B_d \rightarrow \phi K,$ $B_d \rightarrow K\pi, \dots$	$B_d \rightarrow X_d \gamma, B_d \rightarrow \pi\pi, \dots$	$\epsilon'/\epsilon, K_L \rightarrow \pi^0 \ell^+ \ell^-, \dots$
$\gamma$ penguin	$B_d \rightarrow X_s \ell^+ \ell^-, B_d \rightarrow X_s \gamma$ $B_d \rightarrow \phi K, B_d \rightarrow K\pi, \dots$	$B_d \rightarrow X_d \ell^+ \ell^-, B_d \rightarrow X_d \gamma$ $B_d \rightarrow \pi\pi, \dots$	$\epsilon'/\epsilon, K_L \rightarrow \pi^0 \ell^+ \ell^-, \dots$
$Z^0$ penguin	$B_d \rightarrow X_s \ell^+ \ell^-, B_s \rightarrow \mu\mu$ $B_d \rightarrow \phi K, B_d \rightarrow K\pi, \dots$	$B_d \rightarrow X_d \ell^+ \ell^-, B_d \rightarrow \mu\mu$ $B_d \rightarrow \pi\pi, \dots$	$\epsilon'/\epsilon, K_L \rightarrow \pi^0 \ell^+ \ell^-,$ $K \rightarrow \pi \nu \nu, K \rightarrow \mu\mu, \dots$
$H^0$ penguin	$B_s \rightarrow \mu\mu$	$B_d \rightarrow \mu\mu$	$K_{L,S} \rightarrow \mu\mu$

decreasing  
SM  
contrib.

Theoretical errors  $\lesssim 10\%$

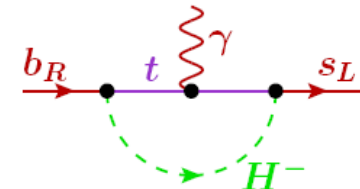
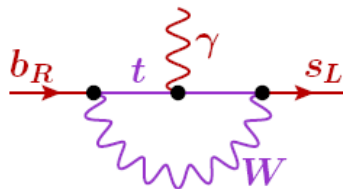
There is much more to learn than just the UT consistency check

## ● Mixing



Simple parameterization for each neutral meson:  $M_{12} = M_{12}^{\text{SM}} (1 + h e^{2i\sigma})$

## ● Penguin decays

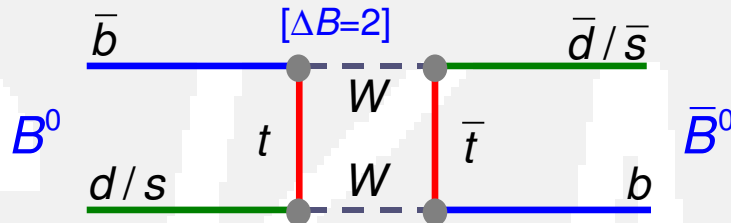


Many operators for  $b \rightarrow s$  transitions — no simple parameterization of NP

➔ NP in flavor physics: explore FCNC and precision measurements

# New Physics in $\Delta B=2$ transitions

$\Delta m_q$ :



Perturbative QCD

$$\Delta m_q = \frac{G_F^2}{6\pi^2} m_{B_q} m_W^2 \eta_B S(x_t) f_{B_q}^2 B_q |V_{tq} V_{tb}^*|^2 \quad (\text{for } q = d, s)$$

CKM Matrix Elements

Loop integral  
(top loop dominates)

Non-perturbative: Lattice  
(eff. 4 fermion operator)

CDF- hep-ex/0609040

HFAG PDG08

$\Delta m_s : 17.77 \pm 0.12 \text{ ps}^{-1}$

$\Delta m_d : 0.507 \pm 0.005 \text{ ps}^{-1}$

☀ Dominant theoretical uncertainties :  $\sigma_{\text{rel}} \left( f_{B_{d/s}} \sqrt{B_{d/s}} \right) ; 16\%$

• Improved error indirect via  $\Delta m_s$  :  $\sigma_{\text{rel}} \left( \xi = f_{B_s} \sqrt{B_s} / f_{B_d} \sqrt{B_d} \right) ; 5\%$   
[SU(3) breaking correction]

➔ Lattice QCD

## Itoh-san – BNM '08

- Experimental inputs: expected accuracies at SuperBelle with  $10 \text{ ab}^{-1}$ .



# Experimental inputs: from Belle to SuperBelle

Itoh-san – BNM '08

	Center	$\sigma(0.5/\text{ab})$	$\sigma(10/\text{ab})$	$\sigma(50/\text{ab})$
$V_{ub}$	$3.94 \times 10^{-3}$	6.3%	3%	2 %
$\Delta m_d$	0.507	0.8% (sys.limit)	0.8%	0.8%
$\sin 2\phi_1$	0.734	5.5%	2%	1.5%
$\phi_2$ (deg.)	94.6	$11^\circ$	$3^\circ$	$2^\circ$
$\phi_3$ (deg.)	61.6	$19^\circ$	$4^\circ$	$3^\circ$
$B(B \rightarrow \tau \nu)$	$1.13 \times 10^{-4}$	38%	8%	4%
$\frac{B(B \rightarrow \rho/\omega \gamma)^*}{B(B \rightarrow K^* \gamma)}$	0.032	25%	6%	3%
$\Delta m_s$	18.77	0.06%	0.06%	0.06%

\* Systematic errors are included in the quoted errors.

\*  $\Delta m_s$  : LHCb expectation



# Uncertainties in theory inputs

Itoh-san – BNM '08

梅 (ume) : uncertainties currently used in CKMfitter  
竹 (take) : uncertainties based on the predictions by S.Sharpe[1]  
松 (matsu) : uncertainties based on the predictions by V.Lubicz[2]

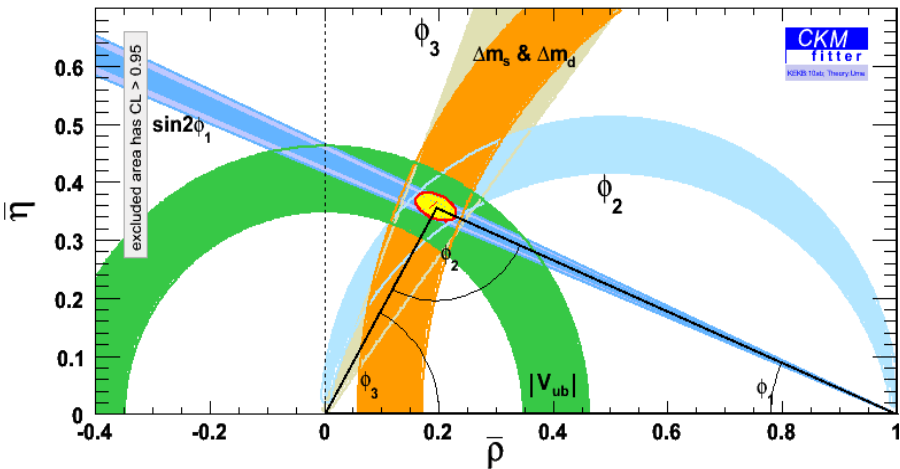
	central value	errors		
		梅 (ume)	竹 (take)	松 (matsu)
$f_{B_s}$	0.233	14%	4%	1%
$f_{B_s} \sqrt{B_s}$	0.277	13%	4%	1%
$\xi$	1.24	5%	2%	1%
$V_{ub}$ theory		7%	4%	2%
$B \rightarrow \rho \gamma$ theory		11%	8%	4%

[1] Lattice '04 ORSAY – 60TFlop year

[2] IV SuperB Workshop '06 – 10 PFlop year

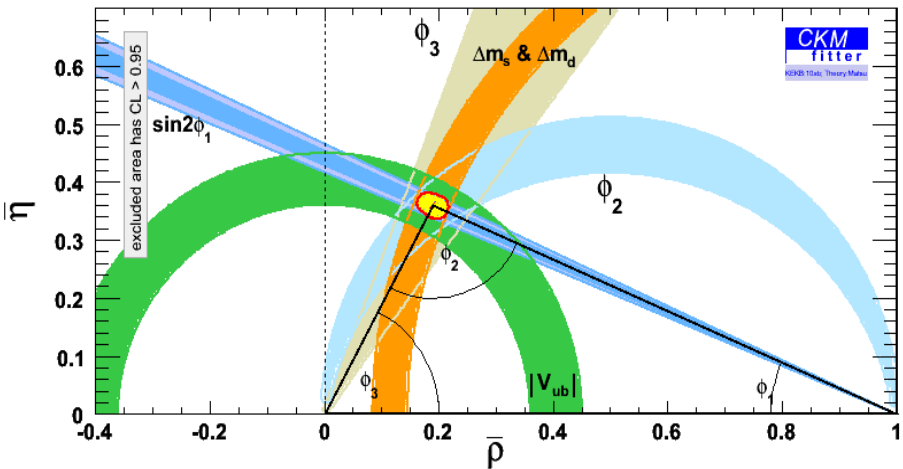
# Results of global CKM fit with 10 ab<sup>-1</sup> data sample

梅 (ume)



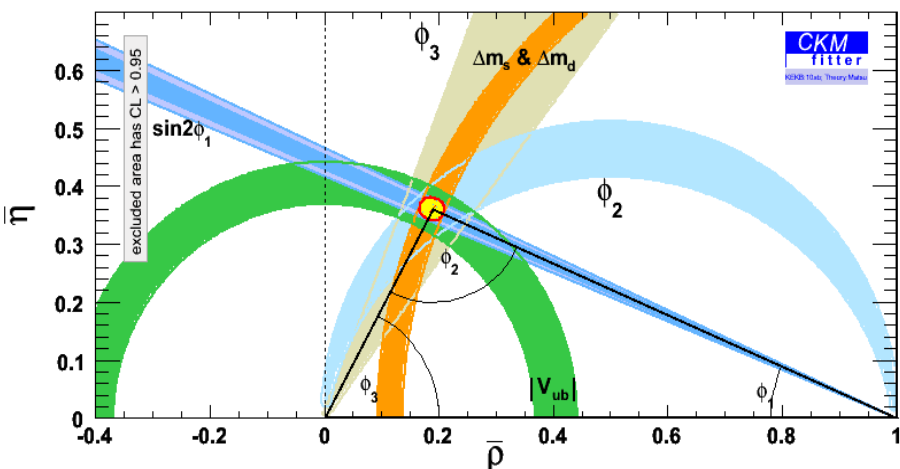
\*  $\phi_2$  is the main constraint to  $\bar{\rho}$

竹 (take)



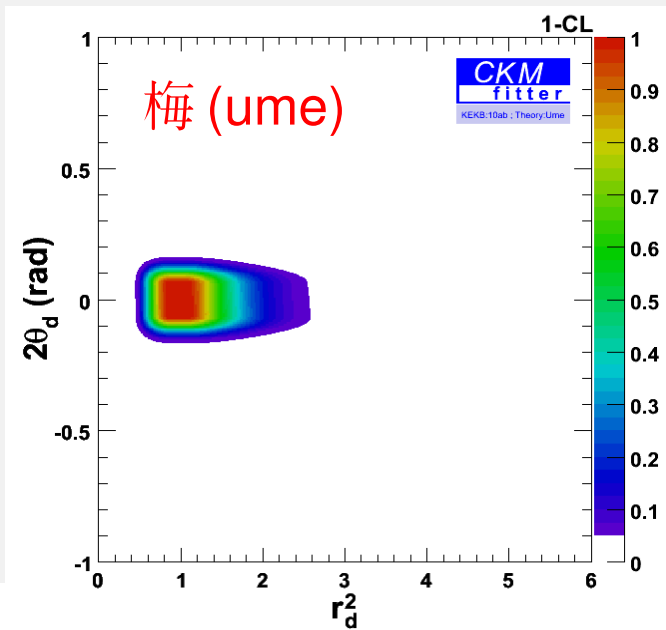
\*  $\Delta m_s$  becomes the main constraint to  $\bar{\rho}$

松 (matsu)

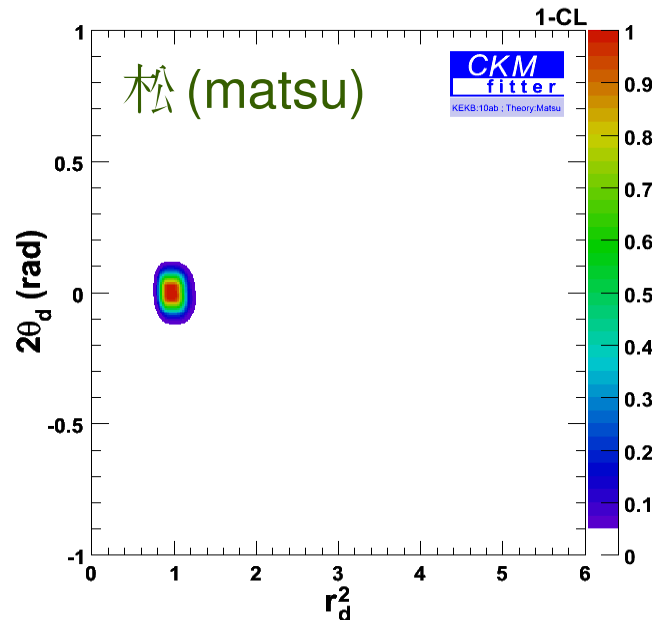
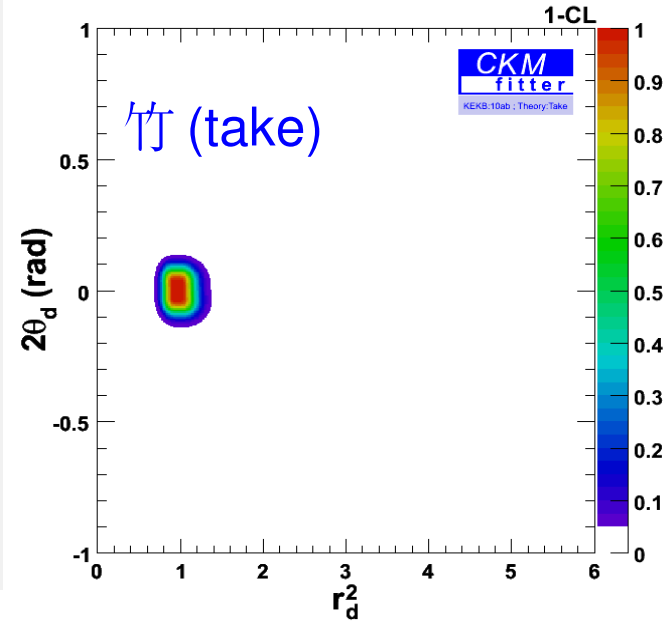


	$\sigma(\bar{\rho})$	$\sigma(\bar{\eta})$
梅 Ume	7.7%	3.1%
竹 Take	6.2%	2.8%
松 Matsu	4.6%	2.5%

# New Physics in Mixing [ $M = M_{SM} r_d^2 \exp(-i2\theta_d)$ ]

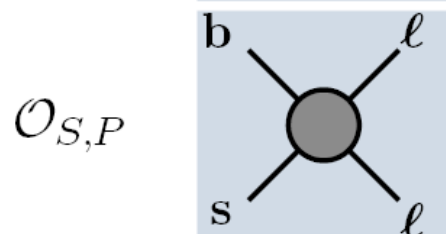
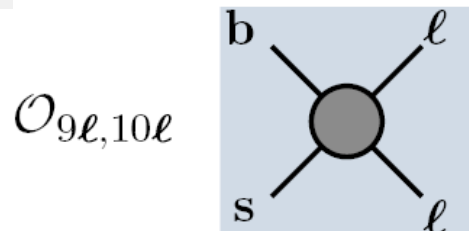
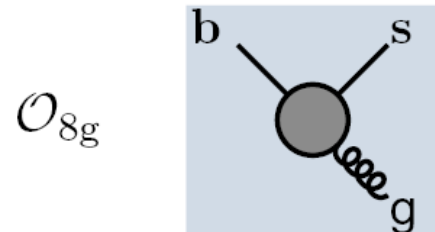
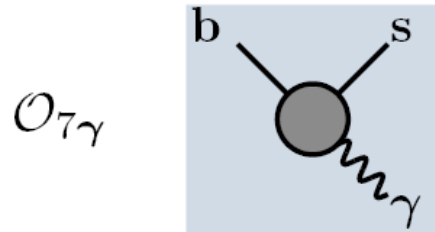


$10 \text{ ab}^{-1}$



	$\sigma(r_d^2)$	$\sigma(2\theta_d)$
梅 Ume	42%	$5.9^\circ$
竹 Take	17%	$4.3^\circ$
松 Matsu	13%	$3.3^\circ$

\*Improvement in  $f_B$  and  $B$  calculations is the key in the model independent NP search.



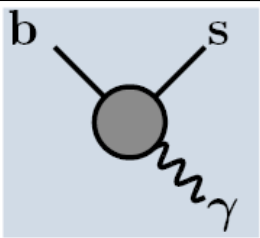
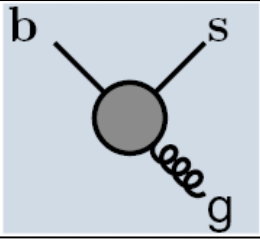
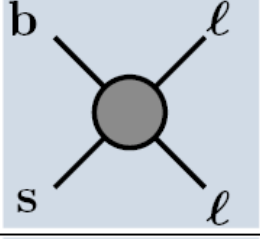
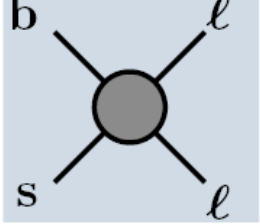
Describe  $b \rightarrow s$  transitions by an effective Hamiltonian

$$\mathcal{H}_{\text{eff}} = -\frac{4G_F}{\sqrt{2}} V_{ts}^* V_{tb} \sum_{i=1}^{10} C_i(\mu) \mathcal{O}_i(\mu)$$

- Long Distance:
  - Operators  $\mathcal{O}_i$
- Short Distance:
  - Wilson coef.  $C_i$

New physics shows up as modified  $C_i$ ,  
(or as new operators)

# Operators and Observables

		magnitude	phase	helicity flip $\mathcal{O}'_i$
$\mathcal{O}_{7\gamma}$		$b \rightarrow s\gamma$	$a_{CP}(b \rightarrow s\gamma)$	$\Lambda_b \rightarrow \Lambda\gamma$ $B \rightarrow (K^* \rightarrow K\pi)\ell^+\ell^-$ $B \rightarrow (K^{**} \rightarrow K\pi\pi)\gamma$
$\mathcal{O}_{8g}$		$b \rightarrow s\gamma$ $B \rightarrow X_c$	$a_{CP}(b \rightarrow s\gamma)$ $B \rightarrow K\phi$	$\Lambda_b \rightarrow \Lambda\phi$ $B \rightarrow K^*\phi$
$\mathcal{O}_{9\ell,10\ell}$		$b \rightarrow se^+e^-$	$A_{FB}(b \rightarrow s\ell^+\ell^-)$	$B \rightarrow (K^* \rightarrow K\pi)\ell^+\ell^-$
$\mathcal{O}_{S,P}$		$B_{d,s} \rightarrow \mu^+\mu^-$	$B_{d,s} \rightarrow \tau^+\tau^-$	$b \rightarrow s\tau^+\tau^-$

# Wilson Coefficient Fits

- In the framework of CKM fit, the NP effect is searched for in the  $B_{d,s} - B_{d,s}^*$  mixing diagram, i.e., comparison of  $\rho$ - $\eta$  constraints by  $(\beta/\phi_1, \alpha/\phi_2, \Delta m_{d,s})$  and by  $(\gamma/\phi_3, V_{ub})$
- A complementary NP search can be performed by studying the FCNC transitions like  $B \rightarrow X_s \gamma$  and  $B \rightarrow X_s l^+ l^-$  which are governed by Wilson Coefficients  $C_7$ ,  $C_9$  and  $C_{10}$ .
- The determination of Wilson Coefficients using various FCNC decays simultaneously in the similar manner as that in CKM fit (global fit) can be a sensitive probe to NP by comparing with the SM expectations.

# NP in Wilson Coefficients (cont'd)

- Belle measurement of  $A_{\text{FB}}$  in  $B \rightarrow K^* l l$  already gives good constraints to Wilson coefficients.
- The extension of this approach is considered to include other measurements together in the fit.
- **Inputs**
  - \*  $\text{Br}(B \rightarrow K^* \gamma)$
  - \*  $\text{Br}(B \rightarrow K^* l^+ l^-)$
  - \*  $A_{\text{FB}}(B \rightarrow K^* l^+ l^-)$  as a function of  $q^2$  (5 points)
- **Free parameters:** Wilson Coefficients  $C_7$ ,  $C_9$  and  $C_{10}$ .
  - \*  $|V_{tb} V_{ts}^*|$  is given through the standard CKMfitter interface.
- **Theoretical model:**
  - based on the paper by A. Ali, *et al.* PRD **61**, 0704024 (2000)
- Coded as an add-on theory model for CKMfitter.

# Status: some work still needed

- Coding of theory model in Mathematica completed.
- Test of the coding is in progress:
  - \* Still have problems to reproduce  $A_{FB}(q^2)$  written in the paper by Ali, et al.
    - Careful check of both coding and theoretical expression
- More up-to-date **NNLO theoretical calculations** will be implemented after this trial is successful.
- Aiming at the completion by next annual CKMfitter meeting and hopefully the presentation at autumn JPS meeting.

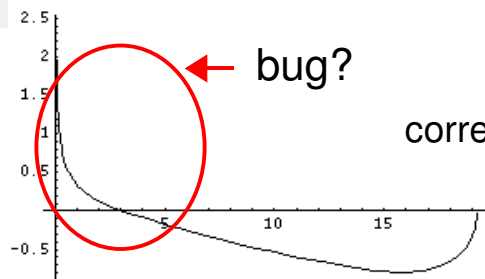
```
Plot[AFBnormsq[qsq], {qsq, 0.0, 20.0}];
```

```
Plot::plnr : AFBnormsq[qsq] is not a machine-size real number at qsq = 19.990385710617627. More...
```

```
Plot::plnr : AFBnormsq[qsq] is not a machine-size real number at qsq = 19.60554123951949. More...
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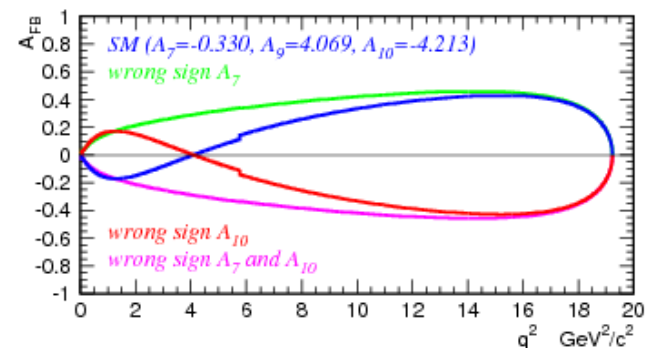
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Plot::plnr : AFBnormsq[qsq] is not a machine-size real number at qsq = 19.392358042486258. More...
```

```
General::stop : Further output of Plot::plnr will be suppressed during this calculation. More...
```



corresponding to red line in right fig.

Current trial implementation in CKMfitter



Ali's paper (drawn by Ishikawa)



# Complex extraction of $\gamma$

**GLW**

$$\begin{aligned} \mathbf{R}_{\text{CP}+-} &= 1 \pm 2 \mathbf{r}_B \cos(\delta_B) \cos(\phi_3) + \mathbf{r}_B^2 \\ \mathbf{A}_{\text{CP}+-} &= \pm 2 \mathbf{r}_B \sin(\delta_B) \sin(\phi_3) / \mathbf{R}_{\text{CP}+-} \end{aligned}$$

**ADS**

$$\mathbf{R}_{\text{ADS}} = \mathbf{r}_B^2 + \mathbf{r}_D^2 + 2 \mathbf{r}_B \mathbf{r}_D \cos(\delta_B + \delta_D) \cos \phi_3$$

**GGSZ**

$$(\mathbf{x}_{+-}, \mathbf{y}_{+-}) = (\mathbf{r}_B \cos(\delta_B \pm \phi_3), \mathbf{r}_B \sin(\delta_B \pm \phi_3))$$

$\mathbf{R}_{\text{CP}\pm}, \mathbf{A}_{\text{CP}\pm}$  for  $\text{DK}, \text{D}^* \text{K}, \text{DK}^*$

**32 observables**  $\mathbf{R}_{\text{ADS}}$  for  $\text{DK}, \text{D}^* \text{K}, \text{DK}^*$ , for  $\text{K}\pi, \text{K}\pi\pi^0$

$(\mathbf{x}_{\pm}, \mathbf{y}_{\pm})$  for  $\text{DK}, \text{D}^* \text{K}, \text{DK}^*$



$\mathbf{r}_B, \mathbf{r}_B^*, \mathbf{r}_B^{K^*}, \delta_B, \delta_B^*, \delta_B^{K^*}, \mathbf{r}_{D_{K\pi}}, \delta_{D_{K\pi}}, \mathbf{r}_{D_{K\pi\pi^0}}, \delta_{D_{K\pi\pi^0}}, \phi_3$

**11 parameters**

→ composite hypothesis (nuisance parameters): heavy statistical procedure

Assuming that the agreement between the data and the theory is OK ( $p\text{-value}(\chi^2_{\min})$ )

Perform metrology (estimation of theory parameters):

1) **Wilks (profile) likelihood-ratio test statistic** [ $W(a) \equiv \Delta\chi^2(a) = \chi^2(a, \hat{\mu}(a)) - \chi^2_{\min}$ ]

- $a$ =parameters of interest ( $\gamma$ ),  $\mu$ =nuisance parameters ( $r, \delta$ )
- profile: take MLE of  $\mu$  for each value of  $a$  [MINOS for CI in Minuit]

2) if the **sampling pdf** of  $W$  is a  $\chi^2$  law,  $p$ -value (CL) with Prob()

[the  $W$  test is pivotal [distribution under  $H_0$  independent of nuisance parameters]]

3) **if not**: it's where the situation starts becoming complicated  $\rightarrow$  **toy Monte Carlo**

But the sampling pdf depends, in general, on the nuisance parameters.

**What to do with the nuisance parameters?**

- plug-in principle (first order parametric bootstrap): take MLE for the nuisance parameters

- adjusted  $p$ -value (second order parametric bootstrap)
- supremum method: least favorable values for the nuisance parameters

L. Demortier's [talk@PHYSTAT2007](http://phystat-lhc.web.cern.ch/phystat-lhc/) [<http://phystat-lhc.web.cern.ch/phystat-lhc/>]

A.C. Davison and D.V. Hinkley, Bootstrap Methods and their Application (1997)

# Conclusion

Several on-going activities:

- prospective studies for SuperBelle
- New Physics search in Wilson coefficients.
- Longer term:  $\Delta F=1$  rare decays. [very complex NNLO formulas ... to be implemented and checked]
- Try to improve statistical treatment [beware of naïve average and/or naïve confidence interval from likelihood (check coverage probability if you want to have correct uncertainties)]



ありがとう



BACKUP SLIDES

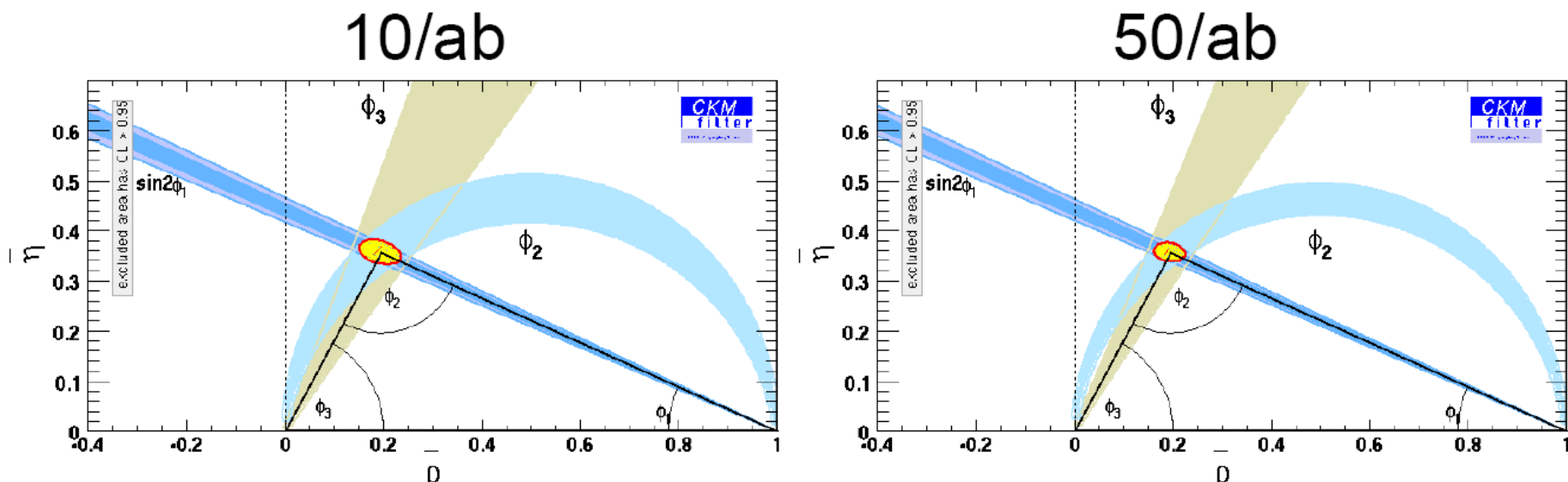
# Bayesian?

## Conclusions: Bayesian or frequentist?

F. James – Moriond QCD 07

1. The main problem in Bayesian methodology is the **prior**. Use Bayesian methods when you **know the prior** and have a good reason to use it. The only case I know where that is true is **maximum entropy image processing**.
2. Use Bayesian decision theory to make it clear what are the subjective criteria for your decision. [Example: where to look for new physics.]
3. For everything else, in particular objective data analysis, I don't see any reason to use Bayesian methods. We now know how to handle all the situations (nuisance parameters, systematic errors) that used to cause problems in the frequentist methodology.
4. Very few people would believe a result that can only be obtained by a Bayesian analysis with an arbitrary prior.

# Results of global CKM fit with angle measurements only



	$\sigma(\bar{\rho})$	$\sigma(\bar{\eta})$
10/ab	8.7%	2.8%
50/ab	6.7%	2.1%

\* Constraints by exp. measurements only in principle!