

# Dynamical SUSY breaking without scales

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DESY

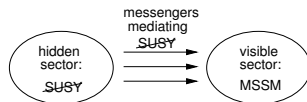


Based on arXiv:0705.2153, arXiv:1011.2659

# Gauge-mediated supersymmetry breaking

Build a model of SUSY breaking which is **as UV-independent as possible**

- no higher-dimensional operators
- SUSY broken in **hidden sector**
- massive **messenger fields** with SM charges couple to hidden sector
- SUSY communicated to SM through **messenger loops**



- e.g. gluino masses:



- Solves SUSY flavour problem

**This talk will mainly concern the hidden sector.**

# The hidden sector: Dynamical SUSY breaking

**Q: Why is  $M_{\text{EWSB}} \ll M_{\text{Planck}}$ ?**

A: SUSY protects Higgs potential from quadratic divergences  
EWSB scale set by soft SUSY breaking terms,  $M_{\text{EWSB}} \sim M_{\text{soft}}$   
In gauge-mediated SUSY:

$$M_{\text{soft}} \sim \frac{1}{16\pi^2} \frac{M_{\text{SUSY}}^2}{M_{\text{mess}}}$$

**Q: Why is  $M_{\text{SUSY}} \ll M_{\text{Planck}}$ ?**

A: **Dynamical SUSY breaking.**

$M_{\text{SUSY}}$  generated by strong gauge dynamics / dimensional transmutation  
(just like  $\Lambda_{\text{QCD}}$  in Standard Model) → Witten '81, Affleck/Dine/Seiberg '80s

**Q: How could this look like?**

→ this talk (and other models...)

# Review: $F$ -term SUSY breaking

## General Wess-Zumino model:

$$W = f_i \Phi_i + \mu_{ij} \Phi_i \Phi_j + \lambda_{ijk} \Phi_i \Phi_j \Phi_k$$

- $W$  = **superpotential**,  $\Phi_i$  = **chiral superfields**
- SUSY iff  $\langle \frac{\partial W}{\partial \Phi_i} \rangle \neq 0$  for some  $i$
- SUSY scale set by  $M_{\text{SUSY}}^2 \sim \left| \langle \frac{\partial W}{\partial \Phi_i} \rangle \right|$

## Example 1: Polonyi model

$$W = f \phi$$

- $\langle \frac{\partial W}{\partial \Phi} \rangle = f = \text{const.} \neq 0$   
 $M_{\text{SUSY}}^2 \sim$  **coefficient of linear term in  $W$**
- scalar potential exactly flat  $\Rightarrow$  not so interesting

# Review: $F$ -term SUSY breaking

## Example 2: O'Raifeartaigh model

$$W = \lambda \Phi_1 (\mu^2 - \Sigma^2) + m \Phi_2 \Sigma$$

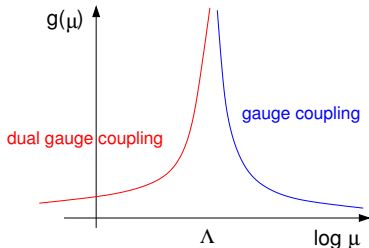
- For  $|m|^2 > |\lambda\mu^2|$  vacuum is at  $\Phi_1 = \Phi_2 = \Sigma = 0$
- $M_{\text{SUSY}}^2 = \left| \left\langle \frac{\partial W}{\partial \Phi_1} \right\rangle \right| = |\lambda\mu^2| =$  **coefficient of linear term in  $W$**
- No flat directions in (loop-corrected) scalar potential  $\Rightarrow$  more interesting
- Origin of small scale  $\sqrt{|\lambda||\mu|}$  unclear. **Not a dynamical model.**

# Review: $F$ -term SUSY breaking

## Example 3: ISS model

SQCD =  $SU(N)$  SUSY gauge theory, “quark” and “antiquark” superfields  $Q, \tilde{Q}$   
For suitable numbers of flavours and colours:

- asymptotically free
- strongly coupled at IR scale  $\Lambda$
- at energies below  $\Lambda$ , described by IR-free **Seiberg dual** “magnetic” theory
- magnetic theory contains composite **meson** superfield  $\Phi \sim Q\tilde{Q}/\Lambda$  and “dual quarks” and antiquarks  $\chi, \tilde{\chi}$



Add quark mass term  $W = m Q\tilde{Q} \Rightarrow W_{\text{IR}} = \chi\Phi\tilde{\chi} + m\Lambda \text{tr} \Phi$

**Linear term** leads to SUSY with  $M_{\text{SUSY}}^2 \sim m\Lambda \rightarrow$  Intriligator/Seiberg/Shih '06  
(only metastable, but with long-lived vacuum if  $m \ll \Lambda$ )

**Looks better:**  $M_{\text{SUSY}}$  depends on **dynamical scale  $\Lambda$**   
but  $m \ll \Lambda$  still put in by hand...

# Can we do better?

**Goal:** Build a model of (metastable) SUSY breaking which

- is renormalizable (minimize dependence on UV physics)
- generates **all** scales dynamically
- can serve as a realistic hidden sector for gauge-mediated SUSY
- is as simple as possible

**Idea 1:** Renormalizable + scale-free means cubic  $W$

ISS: Seiberg duality turns mass term  $mQ\tilde{Q}$

into linear term  $m\Lambda \text{tr} \Phi$  for composite  $\Phi \sim Q\tilde{Q}/\Lambda$

Now: **Use two dualities** to turn **cubic term** (for elementary fields)  
into **linear term** (for composites)

**Idea 2:** Take SQCD + SQCD' + singlet  $S$

$W = SQ'\tilde{Q}' + S^3$  gives  $\langle S \rangle = \Lambda'$  in SUSY vacuum

**Use  $\langle S \rangle$  as dynamically generated quark mass parameter for SQCD**

# 1. SUSY breaking from a sequence of dualities

**Roughly:**

$SU(N) \times SU(n)$ ; chiral superfields  $\tilde{Q}, \Sigma, \tilde{\Sigma}$ ; UV superpotential  $W = \lambda \Sigma \tilde{\Sigma} \tilde{Q}$

	$SU(N)$	$SU(n)$
$\Sigma$	$\square$	$\mathbf{1}$
$\tilde{\Sigma}$	$\overline{\square}$	$\square$
$\tilde{Q}$	$\mathbf{1}$	$\overline{\square}$

$SU(N)$  strongly coupled at scale  $\Lambda_N$ : meson  $Q \sim \Sigma \tilde{\Sigma} / \Lambda_N$

$W_{\text{eff}} = \underbrace{\lambda \Lambda_N}_{\equiv m} Q \tilde{Q}$ : **effective ISS model for  $SU(n)$**  if  $\lambda$  is small

$SU(n)$  strongly coupled at  $\Lambda_n \Rightarrow$  **linear term** for meson  $Q \tilde{Q}$  with coeff.  $\lambda \Lambda_N \Lambda_n$



# 1. SUSY breaking from a sequence of dualities

And in detail:

Gauge group  $SU(N) \times SU(n)$ , flavour group  $SU(N)_F \times SU(N-n)$

Choose  $n < N < \frac{3}{2}N$  (free magnetic range)

	$SU(n)$	$SU(N)$	$SU(N)_F$	$SU(N-n)$
$\tilde{\Sigma}$	$\square$	$\overline{\square}$	1	1
$\tilde{Q}$	$\overline{\square}$	1	$\square$	1
$\Sigma$	1	$\square$	$\overline{\square}$	1
$\tilde{P}$	1	$\overline{\square}$	1	$\square$
$S$	1	1	$\square$	$\overline{\square}$

Superpotential  $W = \lambda \Sigma \tilde{\Sigma} \tilde{Q} + \Sigma \tilde{P} S$

$SU(N)$  strongly coupled at scale  $\Lambda_N$ :  **$SU(N)$  SQCD with  $F = N$  flavours**

**Baryons**  $B, \tilde{B}$  and **mesons**  $Q \sim \Sigma \tilde{\Sigma} / \Lambda_N, \tilde{S} \sim \Sigma \tilde{P} / \Lambda_N$

$$W_{\text{eff}} = \lambda \Lambda_N Q \tilde{Q} + \Lambda_N S \tilde{S} + \underbrace{T \Lambda_N^2 \left( \frac{\det(\Sigma \oplus \tilde{S})}{(\Lambda_N)^N} - \frac{B \tilde{B}}{\Lambda_N^2} - 1 \right)}_{\text{deformed moduli space constraint}}$$

deformed moduli space constraint

# 1. SUSY breaking from a sequence of dualities

$$W_{\text{eff}} = \lambda \Lambda_N Q \tilde{Q} + \Lambda_N S \tilde{S} + \underbrace{T \Lambda_N^2 \left( \frac{\det(\Sigma \oplus \tilde{S})}{(\Lambda_N)^N} - \frac{B \tilde{B}}{\Lambda_N^2} - 1 \right)}_{\text{deformed moduli space constraint}}$$

$S$  and  $\tilde{S}$  decouple: constraint satisfied on baryonic branch  $B \tilde{B} = -\Lambda_N^2$

$$W_{\text{eff}} = \lambda \Lambda_N Q \tilde{Q}$$

For  $\lambda$  small,  $Q$  and  $\tilde{Q}$  can stay light to below  $SU(n)$  strong-coupling scale

$SU(n)$  strongly coupled at  $\Lambda_n$

- $N$  flavours ( $Q = \text{composite}$ ,  $\tilde{Q} = \text{elementary}$ )
- in free magnetic range since  $n < N < \frac{3}{2}n$  by assumption
- if  $\lambda \Lambda_N < \Lambda_n \Rightarrow$  **effective ISS model** with  $M_{\text{SUSY}}^2 \sim |\lambda \Lambda_n \Lambda_N|$

Small marginal coupling  $\lambda$  required to satisfy  $\lambda \Lambda_N < \Lambda_n$

(since  $\Lambda_n < \Lambda_N$  by construction)

## 2. SUSY breaking with a singlet

### Idea:

$SU(n)$  SQCD with  $f < n$  flavours  $\Sigma, \tilde{\Sigma}$ : dynamical  $W$  admits **no stable vacuum**

But adding a singlet  $S$  and a tree-level superpotential

$$W_{\text{tree}} = S^3 + S \Sigma \tilde{\Sigma}$$

gives

$$W_{\text{exact}} = S^3 + S \Sigma \tilde{\Sigma} + \left( \frac{\Lambda^{3n-f}}{\det \Sigma \tilde{\Sigma}} \right)^{\frac{1}{n-f}}$$

**Stable SUSY vacuum** with  $\langle S \rangle \sim \Lambda$ .

**Use  $\langle S \rangle$  as dynamically generated ISS mass parameter**

Simplest version:  $n = 2$  and  $f = 1$ ,

$SU(2)$  gauge group with one flavour  $\Sigma, \tilde{\Sigma}$  and scale  $\Lambda_2$

## 2. SUSY breaking with a singlet

Take  $SU(N)$  with  $F$  flavours  $Q, \tilde{Q}$  in free magnetic range,  $N < F < \frac{3}{2}N$

Add auxiliary gauge group:  $SU(2)$  with  $\Sigma, \tilde{\Sigma}$ , and singlet  $S$

$$W_{\text{tree}} = S\Sigma\tilde{\Sigma} + \lambda SQ\tilde{Q} - \frac{1}{3}S^3$$

Strong-coupling scales: **Assume**  $\Lambda_2 > \Lambda_N$ .

Near  $\Lambda_2$ ,  $SU(2)$  generates dynamical superpotential:

$$\Delta W_{\text{ADS}} = \frac{(\Lambda_2)^5}{\Sigma\tilde{\Sigma}}$$

Use this to integrate out  $S$  and  $\Sigma\tilde{\Sigma}$ :  $\langle S \rangle \sim \Lambda_2$

$$W_{\text{eff}} = \lambda\Lambda_2 Q\tilde{Q}$$

If  $\lambda\Lambda_2 < \Lambda_N$  (requiring  $\lambda \ll 1$ ), again recover ISS superpotential:

**Effective ISS model** with  $M_{\text{SUSY}}^2 \sim |\lambda\Lambda_n\Lambda_N|$

# Messenger couplings

Straightforward to couple this model to **gauge mediation messengers**

$$W_{\text{tree}} = S\Sigma\tilde{\Sigma} + \lambda SQ\tilde{Q} - \frac{1}{3}S^3 + \kappa Sff$$

Gauge symmetries now

	SU(2)	SU(N)	SU(5)	$\supset$ SU(3) $\times$ SU(2) $\times$ U(1)
$\Sigma$	$\square$	1	1	
$\tilde{\Sigma}$	$\overline{\square}$	1	1	
$Q$	1	$\square$	1	
$\tilde{Q}$	1	$\overline{\square}$	1	
$f$	1	1	<b>R</b>	
$\tilde{f}$	1	1	<b><math>\overline{R}</math></b>	

Supersymmetric messenger mass  $\Lambda_2$  after setting  $\langle S \rangle \approx \Lambda_2$   
~~SUSY~~ mass splittings induced from effective  $Q\tilde{Q}ff$  couplings  
 (similar to  $\rightarrow$  [Murayama/Nomura '06](#))

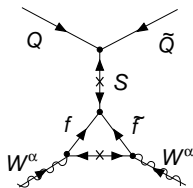
# Messenger couplings

$$W_{\text{tree}} = S\Sigma\tilde{\Sigma} + \lambda SQ\tilde{Q} - \frac{1}{3}S^3 + \kappa Sff$$

induces coupling

$$\mathcal{L} \supset \frac{g^2}{16\pi^2} \frac{\kappa\lambda C_R}{(\Lambda_2)^2} \int d^2\theta Q\tilde{Q} \text{tr} W^\alpha W_\alpha$$

to **MSSM gauge fields**  $W^\alpha$  by



With  $\Phi \sim Q\tilde{Q}/\Lambda_N$  and  $F_\Phi = N\lambda\Lambda_2\Lambda_N$ : **MSSM gaugino masses**

$$M_a \sim \frac{g_a^2}{16\pi^2} \frac{\kappa\lambda^2 C_R N \Lambda_N^2}{\Lambda_2}$$

# Messenger couplings

- Can induce  $\mu$  term at one-loop e.g. by taking  $f$  and  $\tilde{f}$  in  $\mathbf{10}$  and  $\overline{\mathbf{10}}$  of SU(5), from superpotential

$$W \supset y_u f f H_u + y_d \tilde{f} \tilde{f} H_d$$

leading to

$$\mu \sim \frac{y_u y_d}{16\pi^2} \frac{\kappa \lambda^2 C_{\mathbf{R}} N \Lambda_N^2}{\Lambda_2}$$

- Can forbid  $SH_u H_d$  coupling by symmetries (e.g. suitable  $R$ -Symmetry)
- sfermion masses<sup>2</sup>, trilinears and  $B\mu$ : difficult to extract (from operators non-holomorphic in hidden sector fields → [work in progress](#))

# Conclusions

- Modern models of SUSY breaking often rely on small scale put in by hand  
**Not fully dynamical**
- Can be cured in SQCD with **composite quark superfields**  
⇒ generate ~~SUSY~~ scale from a sequence of Seiberg dualities. . .
- . . . or by taking **two copies of SQCD** coupled by a singlet
- Obtain **simple, renormalizable**, fully **dynamical** models of ~~SUSY~~
- All scenarios require a small ( $\lesssim 10^{-3}$ ) marginal parameter  $\lambda$
- First scenario might be used for direct gauge mediation
- Second one can be elegantly coupled to gauge mediation messengers:
  - renormalizable
  - natural (except for tuning of  $\lambda$ )
  - potentially realistic (possible  $B\mu$  problem)



# Backup

# SUSY QCD

SQCD =  $SU(N)$  SUSY gauge theory,  $F$  copies of  $Q$  and  $\tilde{Q}$  chiral superfields

	$SU(N)$	$SU(F)_L$	$SU(F)_R$
$Q$	$\square$	$\square$	$1$
$\tilde{Q}$	$\bar{\square}$	$1$	$\square$

Take  $N < F < \frac{3}{2}N$ : “Free magnetic range”

- asymptotically free, strongly coupled at IR scale  $\Lambda$
- IR degrees of freedom constitute **Seiberg-dual gauge theory**  $\rightarrow$  Seiberg '93
  - $F$  copies of **dual quark** superfields  $\chi$  and **dual antiquarks**  $\tilde{\chi}$ ...
  - ... and composite **meson** superfield  $\Phi \sim Q\tilde{Q}/\Lambda$
  - dual gauge group:  **$SU(F - N)$** . IR free, strongly coupled at UV scale  $\approx \Lambda$

	$SU(F - N)$	$SU(F)_L$	$SU(F)_R$
$\Phi$	$1$	$\square$	$\bar{\square}$
$\chi$	$\square$	$\bar{\square}$	$1$
$\tilde{\chi}$	$\bar{\square}$	$1$	$\square$

- IR superpotential  $W_{IR} = \chi\Phi\tilde{\chi}$

# Review: $F$ -term SUSY breaking (continued)

## Example 3: ISS model

Deform SQCD in UV by superpotential  $W_{UV} = m Q \tilde{Q}$

Require  $m \ll \Lambda$  (otherwise  $Q$  and  $\tilde{Q}$  decouple in UV)

Effect on Seiberg dual IR theory:

$$W_{IR} = \chi \Phi \tilde{\chi} + m \Lambda \text{tr} \Phi + \dots$$

$$\frac{\partial W_{IR}}{\partial \Phi_j^i} = \underbrace{\chi_i^c \tilde{\chi}_c^j}_{\text{rank } F-N} + m \Lambda \underbrace{\delta_j^i}_{\text{rank } F}$$

$\partial W / \partial \Phi_j^i$  cannot all vanish  $\Rightarrow$  SUSY broken  $\rightarrow$  Intriligator/Seiberg/Shih '06

- Taking into account (IR-irrelevant) nonperturbative terms:  
SUSY breaking only metastable, but vacuum parametrically long-lived
- $M_{\text{SUSY}}^2 \sim \left| \left\langle \frac{\partial W}{\partial \Phi_j^i} \right\rangle \right| \sim |m \Lambda| \sim$  coefficient of linear term in  $W$
- Mechanism still not fully dynamical: small scale  $m$  put in by hand