

**A possible connection between neutrino mass generation and the lightness of a
NMSSM pseudoscalar**

Debottam Das

Laboratoire de Physique Theorique d'Orsay

Talk presented at : Rencontre de Physique des Particules 2011

Ref: arXiv:1011.5037

(Asmaa Abada, Gautam Bhattacharyya, Cédric Weiland)

Outline

- NMSSM can offer a very light pseudo-scalar Higgs boson A_1
⇒ interesting phenomenology related to
 - Higgs physics
 - dark matter annihilations
- Strong constraints coming from **Upsilon decays**, **B physics** and **accelerator bounds**
- Proposing a definite model for neutrino mass generation in NMSSM, we reanalyze the status of all those **experimental constraints**

More specifically :

Can we evade the experimental constraints which are otherwise very stringent ?

MSSM : μ problem

● Superpotential:

$$W_{\text{MSSM}} = \bar{u} \mathbf{y}_u Q H_u - \bar{d} \mathbf{y}_d Q H_d - \bar{e} \mathbf{y}_e L H_d + \mu H_u H_d$$

$H_u, H_d, Q, L, \bar{u}, \bar{d}, \bar{e} \Rightarrow$ chiral superfields

\Rightarrow Provides all Yukawa interactions in SM

$\Rightarrow \mathbf{y}_u, \mathbf{y}_d, \mathbf{y}_e$ are the dimensionless Yukawa couplings $\Rightarrow 3 \times 3$ matrices in family space

● Proper SUSY phenomenology requires

● $\mu \ll M_{\text{P}}$ (Plank scale), M_{G} (Gut scale)

● And, $\mu > 100 \text{ GeV}$ (From LEP limit on chargino mass)

$\Rightarrow \mu \sim M_{\text{SUSY}} \sim \text{TeV}$ is required

The so-called μ problem in MSSM

NMSSM

- Embedding MSSM in a *Supergravity* framework, $\mu \sim M_{\text{SUSY}}$ can be generated via a particular Higgs dependent (*ad-hoc*) term in the Kähler potential
 \Rightarrow Giudice-Masiero mechanism

This is true only for **Supergravity inspired SUSY breaking models**

- An elegant way to solve this problem is by introducing an additional singlet superfield \underline{S} with a coupling $\lambda \underline{S} H_u H_d$ in the superpotential \Rightarrow

$$W_{\text{NMSSM}} = \lambda \underline{S} H_u H_d + \frac{k}{3} \underline{S}^3 + \dots \quad (\mathbb{Z}_3 \text{ invariant superpotential})$$

The VEV v_S of the real scalar component of \underline{S} generates

$$\Rightarrow \mu_{\text{eff}} = \lambda v_S \Rightarrow \mu_{\text{eff}} \sim M_{\text{SUSY}}$$

This is known as **Next-to-Minimal Supersymmetric Standard Model (NMSSM)**

Simplest SUSY standard model with M_{SUSY} as the only scale in the Lagrangian

NMSSM : Spectrum

- The SM singlet scalar $S \Rightarrow$ can leave the footprints only in the Higgs sector and in the neutralino sector \Rightarrow
 - 3 CP-even neutral Higgs bosons H_i (H_1, H_2, H_3)
 H_1 is the lightest CP-even Higgs boson
 - 2 CP-odd neutral Higgs bosons A_1 and A_2 ($A_2 \simeq A_{MSSM}$)
 - One charged Higgs boson H^\pm
 - Five neutralinos χ_i^0 , $i = 1 \dots 5$, which are mixtures of the Bino, the neutral Wino, the neutral Higgsinos and the Singlino

Our focus will be on the lightest pseudoscalar A_1

Light pseudoscalar in the NMSSM

- In the MSSM, $\Rightarrow m_A > 93.4 \text{ GeV}$ (From LEP : $e^+ e^- \rightarrow A h$)
- In the NMSSM, the lightest pseudoscalar (A_1) can be very light

Recent analysis shows that $m_{A_1} > 210 \text{ MeV}$

Ref: S. Andreas, O. Lebedev, S. Ramos-Sanchez and A. Ringwald, JHEP 1008 (2010) 003

- Light A_1 boson leads to exciting phenomenology related to both Higgs hunting and dark matter annihilations

Light A_1 : What is so attractive

Higgs Physics:

- The interest of a light A_1 is that *it provides a new and dominant decay channel for the lightest Higgs boson h* \Rightarrow **LEP search strategy does not work !**

$h \rightarrow A_1 A_1 \rightarrow 4f$ final state !

where

$A_1 \rightarrow 2\mu, 2\tau, 2b$

- Particular interest is in the zone when $m_{A_1} < 10$ GeV
 - This allows to accommodate *lightest CP-even Higgs mass* $m_h \sim 95 - 105$ GeV
 - Such a light h boson does not require **large stop mass**
 - \Rightarrow This helps to ameliorate the **SUSY fine-tuning problem**
 - m_h (~ 98 GeV) could explain the slight excess of events as reported by the LEP2

Light A_1 : Blessings for light DM

- Lightest neutralino (LSP) \Rightarrow **neutral, massive** having only **weak interactions** \Rightarrow **ideal candidate for DM**
- DAMA.. CoGeNT.. \Rightarrow reported events in excess of the expected background \Rightarrow compatible with $m_{DM} \sim 5 - 12$ GeV

Light DM ~ 10 GeV is favoured !

- WMAP constraint is satisfied via CP-odd Higgs (A_1) exchange $\Rightarrow \tilde{\chi}_1^0 \tilde{\chi}_1^0 \rightarrow A_1^* \rightarrow f\bar{f}$

In **MSSM**, $m_{\tilde{\chi}_1^0} \lesssim 20$ GeV is practically ruled out *since A boson cannot be too light*

Ref: D. Feldman, Z. Liu and P. Nath, Phys. Rev. D 81 (2010) 117701

But NMSSM can ! thanks to lightness of A_1

A_1 : How it couples with matter

- In general

$$A_1 = \cos \theta_A A_{MSSM} + \sin \theta_A S_I$$

- A_{MSSM} is the doublet like CP-odd scalar in the MSSM sector of the NMSSM
- S_I represents the pseudoscalar component of the singlet scalar in the NMSSM

- Phenomenology related to A_1 is principally governed by its couplings to the SM fermions \Rightarrow includes the doublet component ($\cos \theta_A$) only



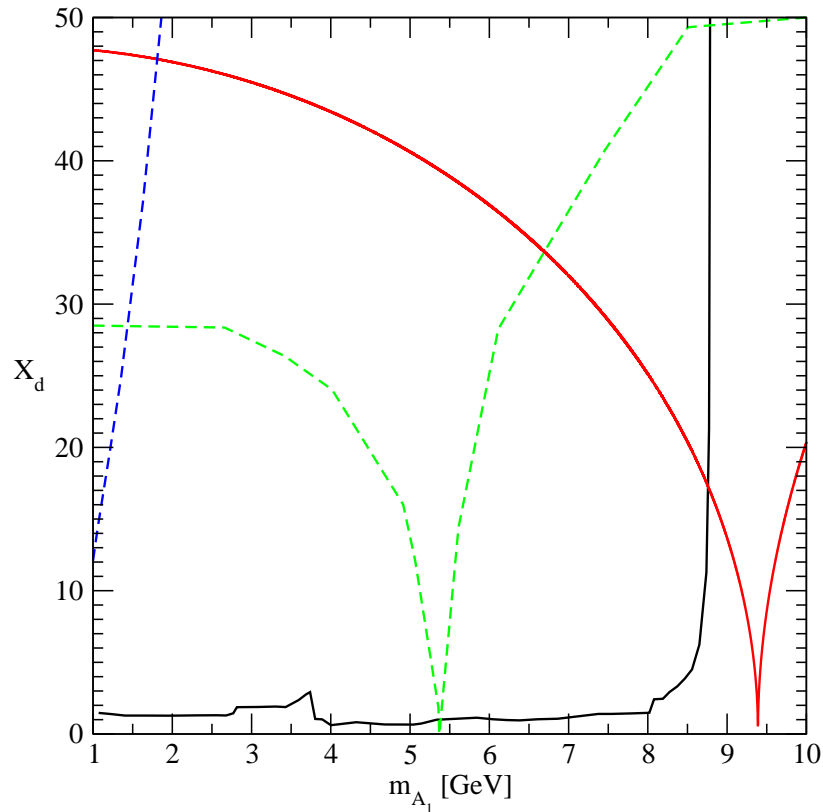
$$\mathcal{L}_{A f \bar{f}} \equiv C_{A f \bar{f}} \frac{ig_2 m_f}{2m_W} \bar{f} \gamma_5 f A,$$

- $C_{A_1 \mu^- \mu^+} = C_{A_1 \tau^- \tau^+} = C_{A_1 b \bar{b}} = X_d = \cos \theta_A \tan \beta$, ($\tan \beta = v_u / v_d$)
- $C_{A_1 t \bar{t}} = C_{A_1 c \bar{c}} = \cos \theta_A \cot \beta$

- However, light or ultra-light CP-odd scalars are highly constrained via Upsilon decays, B physics and collider searches

Most of these constraints *exploit* the $A_1 f \bar{f}$ coupling \Rightarrow thus couples via $\cos \theta_A$ only

Constraint on the A_1 mass : Upsilon decays



Ref: Florian Domingo, Ulrich Ellwanger, Esteban Fullana, Cyril Hugonie, Miguel-Angel Sanchis-Lozano : JHEP 0901:061,2009

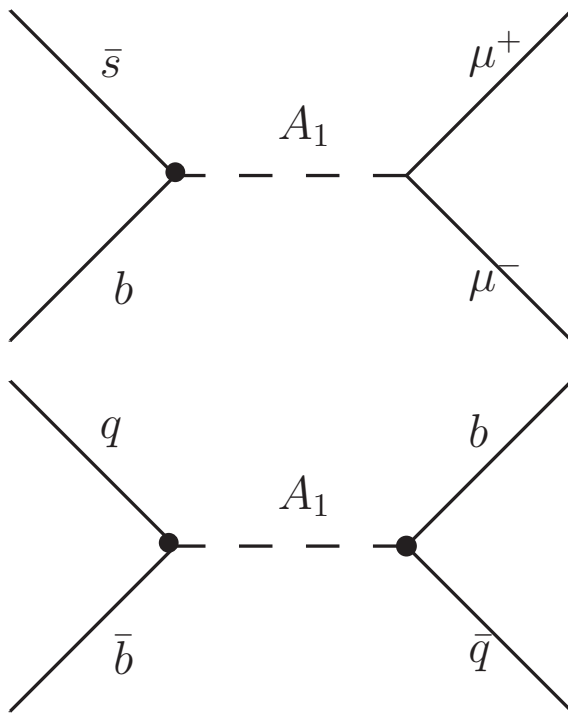
- Radiative Upsilon decays ($\Upsilon(ns) \equiv b\bar{b}$ vector-like bound state with $m_\Upsilon \geq 9.46$ GeV) i.e. $\Upsilon \rightarrow \gamma + X$ searched in B-factories like BaBar, CLEO..

- $\Upsilon \rightarrow \gamma + A_1$ followed by $A_1 \rightarrow \tau^+\tau^-, \mu^+\mu^- \Rightarrow$ visible if A_1 is quite light ($A_1 \leq 10$ GeV) \Rightarrow put bounds on m_{A_1} and in particular on X_d

For $m_{A_1} > 10$ GeV \Rightarrow Strong bounds from B physics and accelerator results

Light A_1 : Constraints from B physics

- List of dominant constraints :
 - $\text{Br}(b \rightarrow s\gamma)$
 - $\Delta M_s, \Delta M_d$ ($\equiv m_{\bar{B}_{s,d}} - m_{B_{s,d}}$)
 - $\text{Br}(B_s \rightarrow \mu^+ \mu^-)$
 - $\text{Br}(B^+ \rightarrow \tau^+ \nu_\tau)$



- A_1 in s channel dominantly contributes to the process like $\Delta M_s, \Delta M_d$, and $\text{Br}(B_s \rightarrow \mu^+ \mu^-)$ via flavor changing vertices $b - s(d) - A_1$
 \Rightarrow via so-called penguin diagrams
- Other constraints are more dependent on m_{H^\pm}

Light A_1 : Constraints from collider physics

- ALEPH collaboration has reanalysed of LEP-2 data for $h \rightarrow A_1 A_1 \rightarrow 4\tau$ final states (relevant for $m_{A_1} < 2m_b$)

Consequently upper limits have been placed on :

$$\frac{\sigma(e^+e^- \rightarrow Zh)}{\sigma_{\text{SM}}(e^+e^- \rightarrow Zh)} \times \text{Br}(h \rightarrow A_1 A_1) \times \mathbf{Br}(A_1 \rightarrow \tau^+ \tau^-)^2$$

- D0 collaboration (Fermilab Tevatron) has analyzed $h \rightarrow A_1 A_1 \rightarrow 4\mu$ mode and placed an upper bound on (relevant for $m_{A_1} < 2m_\tau$):

$$\sigma(p\bar{p} \rightarrow hX) \times \text{Br}(h \rightarrow A_1 A_1) \times \mathbf{Br}(A_1 \rightarrow \mu^+ \mu^-)^2$$

- Similarly, other searches in this direction are :

- $h \rightarrow A_1 A_1 \rightarrow 4b$ for $m_h < 110$ GeV (LEP)
- $h \rightarrow A_1 A_1 \rightarrow gg, c\bar{c}, \tau^+ \tau^-$ for m_h 45 – 86 GeV (OPAL)
- $h \rightarrow A_1 A_1 \rightarrow \mu^+ \mu^- \tau^+ \tau^-$ (D0)

- All these observables constrain $\mathbf{Br}(A_1 \rightarrow f\bar{f})$ and $\mathbf{X_d}$

Outline :

Constraints	$m_{A_1} < 2 m_\tau$	$[2 m_\tau, 9.2 \text{ GeV}]$	$[9.2 \text{ GeV}, M_{\gamma(1S)}]$	$[M_{\gamma(1S)}, 2 m_B]$
$\Upsilon(nS) \rightarrow \gamma A_1 \rightarrow \gamma(\mu^+ \mu^-)$	✓	×	×	×
$\Upsilon(nS) \rightarrow \gamma A_1 \rightarrow \gamma \tau^+ \tau^-$	×	✓	×	×
$e^+ e^- \rightarrow Z + 4\tau$	×	✓	×	×
A_1 - η_b mixing	×	×	✓	✓
$e^+ e^- \rightarrow b \bar{b} \tau^+ \tau^-$	×	×	×	✓

We ask the following question: **Is it possible that a light A_1 can avoid elimination**

We remind that all constraints depend on : $A_1 \rightarrow f\bar{f} \Rightarrow \underline{m_{A_1} \text{ \& } X_d}$

We recall that **Neutrinos** are massless in the **NMSSM**

We propose an extension of the NMSSM with two additional gauge singlets carrying lepton numbers :

- **Provides a substantial invisible decay route for A_1 &**
- **Generates the right size of neutrino mass through lepton number violating interactions**

we examine the connection between neutrino masses and the pseudoscalar A_1

Light neutrino mass: Can it be a blessing for light A_1

- Previous studies are for neutrino masses in the **NMSSM**:
 - R-parity violating interactions in the **NMSSM** superpotential
⇒ **not compatible with DM motivation**
 - Adding gauge-singlet neutrino superfields N_i to the **NMSSM** field content
⇒ $M_{N_i} \sim O(\text{TeV})$ (via $SN_i N_i$) but Yukawa coupling $f^\nu \sim 10^{-6}$
- We implement the '**inverse seesaw**' mechanism for *generating neutrino masses*
 - Singlet neutrinos can be *very light (few GeV)*
 - The neutrino Yukawa couplings ($f^\nu \sim O(1)$)
 - Can enhance *lepton flavor violating processes*
- We will see *how this seesaw mechanism can influence the known existing decay pattern of the A_1 boson*

Inverse seesaw in the NMSSM

● Superpotential :

$$W = W_{\text{NMSSM}} + W'$$
$$W' = f_{ij}^{\nu} H_u L_i N_j + (\lambda_N)_i S N_i X_i + \frac{(\lambda_X)_i}{2} S X_i X_i$$

- N_i and X_i : Gauge singlets carrying the lepton numbers -1 and $+1$
- $(\lambda_N)_i S N_i X_i$ is lepton number conserving term
- $\frac{(\lambda_X)_i}{2} S X_i X_i$ provides lepton number violation

● Once the scalar component of S acquires a vev (v_S), we have

- Lepton number conserving mass terms

(i) $M_{N_i} \Psi_{N_i} \Psi_{X_i}$ with $M_{N_i} \equiv (\lambda_N)_i v_S$ and

(ii) $(m_D)_{ij} \Psi_{\nu_i} \Psi_{N_j}$ with $(m_D)_{ij} = f_{ij}^{\nu} v_u$

- Dynamically generated lepton number violating Majorana mass term $\mu_{X_i} \Psi_{X_i} \Psi_{X_i}$
with $(\mu_X)_i = (\lambda_X)_i v_S / 2$

Neutrino masses in the NMSSM

- Considering one generation, the (3×3) mass matrix in the $(\Psi_\nu, \Psi_N, \Psi_X)$ basis \Rightarrow

$$\mathcal{M} = \begin{pmatrix} 0 & m_D & 0 \\ m_D & 0 & M_N \\ 0 & M_N & \mu_X \end{pmatrix}$$

- The mass eigenvalues ($m_1 \ll m_2, m_3$)

$$m_1 = \frac{m_D^2 \mu_X}{m_D^2 + M_N^2}, \quad m_{2,3} = \mp \sqrt{M_N^2 + m_D^2} + \frac{M_N^2 \mu_X}{2(m_D^2 + M_N^2)}.$$

- m_1 is the lightest mass eigenvalue : Small values of μ_X provides $m_\nu \sim eV$ scale
- $\mu_X \sim O(eV)$ is natural as $\mu_X \rightarrow 0$ restores *lepton number symmetry*
- Thus M_N or m_D is unconstrained

$M_N \sim O(10) \text{ GeV}$ can influence substantially the decay pattern of A_1

Reanalyzing A_1 decay modes

- The lightest CP-odd scalar A_1 has additional interactions with the **sterile neutrinos**
 \Rightarrow **thus new decay final states**
 - $A_1 \rightarrow \Psi_\nu \Psi_N$: Depends on the $\cos \theta_A$ component of A_1
 - $A_1 \rightarrow \Psi_N \Psi_X$ and $\Psi_X \Psi_X$: Depend on the $\sin \theta_A$ component of A_1
- Consequently, the invisible branching ratios (normalized them with the visible modes)

$$\frac{\text{Br}(A_1 \rightarrow \Psi_\nu \Psi_N)}{\text{Br}(A_1 \rightarrow f\bar{f}) + \text{Br}(A_1 \rightarrow c\bar{c})} \simeq \frac{m_D^2}{m_f^2 \tan^4 \beta + m_c^2},$$

$$\frac{\text{Br}(A_1 \rightarrow \Psi_N \Psi_X)}{\text{Br}(A_1 \rightarrow f\bar{f}) + \text{Br}(A_1 \rightarrow c\bar{c})} \simeq \tan^2 \theta_A \frac{M_N^2}{m_f^2 \tan^2 \beta + m_c^2 \cot^2 \beta} \frac{v^2}{v_S^2}$$

$$\frac{\text{Br}(A_1 \rightarrow \Psi_X \Psi_X)}{\text{Br}(A_1 \rightarrow f\bar{f}) + \text{Br}(A_1 \rightarrow c\bar{c})} \simeq \tan^2 \theta_A \frac{\mu_X^2}{m_f^2 \tan^2 \beta + m_c^2 \cot^2 \beta} \frac{v^2}{v_S^2}$$

(neglecting phase-space effects)

Reanalyzing A_1 decay modes...contd

- Invisible decay prefers large $\tan^2 \theta_A$, thus large singlet component and moderate values for $\tan \beta$
- The branching ratio into $A_1 \rightarrow \Psi_N \Psi_X$ dominates over the other modes
- For numerical illustration: we choose
 $\tan \beta = 3, 20, \cos \theta_A = 0.1, M_N = 5, 30 \text{ GeV}$
 - $m_{A_1} > M_N$ to have the two-body decay modes available
 - Thus for the two study points, we consider $m_{A_1} < 10 \text{ GeV}$ and $m_{A_1} < 40 \text{ GeV}$
 - Our parameter choice reflects two regimes where
 - (i) **Upsilon constraints** and (ii) **B-physics or constraints from LEP** are strong

Results

	$\tan \beta = 20, \cos \theta_A = 0.1$		$\tan \beta = 3, \cos \theta_A = 0.1$	
M_N (GeV)	5	30	5	30
$\text{Br}(\mathcal{A}_1 \rightarrow \Psi_\nu \Psi_N)$	7×10^{-5}	3×10^{-6}	4×10^{-3}	1×10^{-4}
$\text{Br}(\mathcal{A}_1 \rightarrow \Psi_N \Psi_X)$	0.7	0.9	~ 1	~ 1
$\text{Br}(\mathcal{A}_1 \rightarrow \Psi_X \Psi_X)$	0	0	0	0

- With the above choices of $\cos \theta_A$ and $\tan \beta$, the resultant X_d is ruled out in **general NMSSM for $m_{\mathcal{A}_1} < 10$ GeV**
- Our results show that, in both cases, \mathcal{A}_1 has significant branching ratios into the invisible modes thus **relaxing the known constraints that would arise from its visible decays**
- Phase space suppression : $\left(\left\{ 1 - \left(\frac{2m_f}{m_{\mathcal{A}_1}} \right)^2 \right\} / \left\{ 1 - \left(\frac{2M_N}{m_{\mathcal{A}_1}} \right)^2 \right\} \right)^{1/2}$
 Our choice $m_{\mathcal{A}_1} > M_N$, m_f makes phase space contribution quite insignificant

Connection between light neutrino and light NMSSM pseudoscalar : Summary

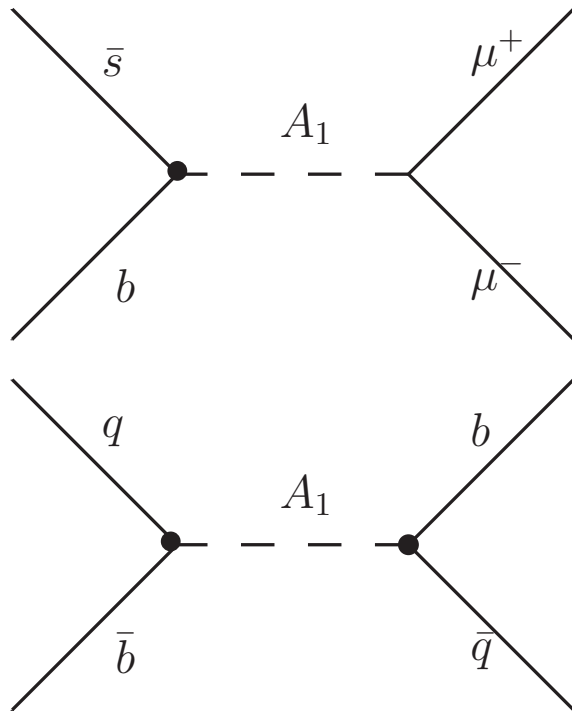
- Scenarios with very light pseudoscalars in NMSSM leads to attractive phenomenology related to both Higgs hunting and dark matter annihilations
- However, these scenarios are constrained due to experimental bounds associated with the decays of a light A_1 into a pairs of SM fermions
- Our primary goal was to rescue the scenarios with light A_1 bosons while at the same time providing an explanation for the smallness of neutrino masses
- We augment the NMSSM Superpotential with two additional singlet neutrinos (carrying opposite lepton number) to meet our twin purpose
- Our results show that the invisible channels of light A_1 can have substantial branching fractions, thus suppressing the visible modes to a large extent
- This in turn weakens the existing constraints on the A_1 mass and on its couplings namely X_d to a large extent

THANK YOU

Constraint on the Higgs masses : Light A_1

- Radiative Upsilon decays ($\Upsilon(nS) \equiv b\bar{b}$ vector like bound state with $m_\Upsilon \geq 9.46 \text{ GeV}$) $\rightarrow \gamma + X$ searched in B-factories like BaBar, CLEO..
- $\Upsilon \equiv \gamma + A_1$ followed by $A_1 \rightarrow \tau^+ \tau^- , \mu^+ \mu^- \Rightarrow$ visible if A_1 is quite light ($A_1 \leq 10$) GeV \Rightarrow put bounds on m_{A_1} and in particular on $\cos \theta_A$
- In this regime h decay leads $h \rightarrow A_1 A_1 \rightarrow 4\tau \Rightarrow$ constrained by the recent ALEPH results ($e^+ e^- \rightarrow Z + 4\tau$)
- bottom-eta η_b meson \equiv CP-odd scalar $b\bar{b}$ bound state with $m_{\eta_b} \sim 9.389 \text{ GeV}$ has recently been discovered
- The mass difference $\text{Upsilon}(1S) - \eta_b(1S) \Rightarrow$ hyperfine splitting ($E_{hfs}^{EXP}(1S)$)
- $E_{hfs}^{EXP}(1S) \sim 70 \text{ MeV} > E_{hfs}^{QCD}(1S) (42 \text{ MeV}) \Rightarrow$ could be explained by $\eta_b - A_1$ mixing
(M.Drees and K.i.Hikasa: Phys.Rev.D 41, 1547 (1990); F.Domingo, U.Ellwanger and M.A.Sanchis-Lozano, Phys.Rev.Lett. 103, 111802 (2009))
- m_{A_1} with mass very close to m_{η_b} is constrained \Rightarrow physical states after mixing should provide the correct mass $\sim 9.389 \text{ GeV}$

Br($B_s \rightarrow \mu^+ \mu^-$) and $\Delta M_{s,d}$: Role of A_1



- SUSY contributions arise from **box diagrams** at the **one-loop** level, but also from **penguin diagrams** involving flavour-changing vertices like $b-s(d)-A_1$
- $\text{Br}(B_s \rightarrow \mu^+ \mu^-) \propto m_{A_1}^{-4} \cos^4 \theta_A^4 \tan^6 \beta$
- Information on the mass differences $\Delta M_{s,d} \equiv m_{\bar{B}_{s,d}} - m_{B_{s,d}}$ originates from measurements of B meson oscillations
- Clearly, both contributions involve X_d as multiplicative factor \Rightarrow **provide constraints on m_{A_1} and X_d**

Small X_d : Constraints are much relaxed compared to the **MSSM A boson**