

# ELECTROWEAK BREAKING IN EXTRA DIMENSIONS

MINI REVIEW

Gero von Gersdorff (École Polytechnique)  
Moriond Electroweak Session, La Thuile, March 2011

# OUTLINE

- How can **Extra Dimensions** explain the electroweak scale?
- What are the **key signatures** of such models?
- How well do they comply with **Electroweak Precision data**?

# RS MODELS

Randall & Sundrum '99

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$$ds^2 = e^{-2ky} dx^\mu dx^\nu \eta_{\mu\nu} + dy^2$$

Warp factor



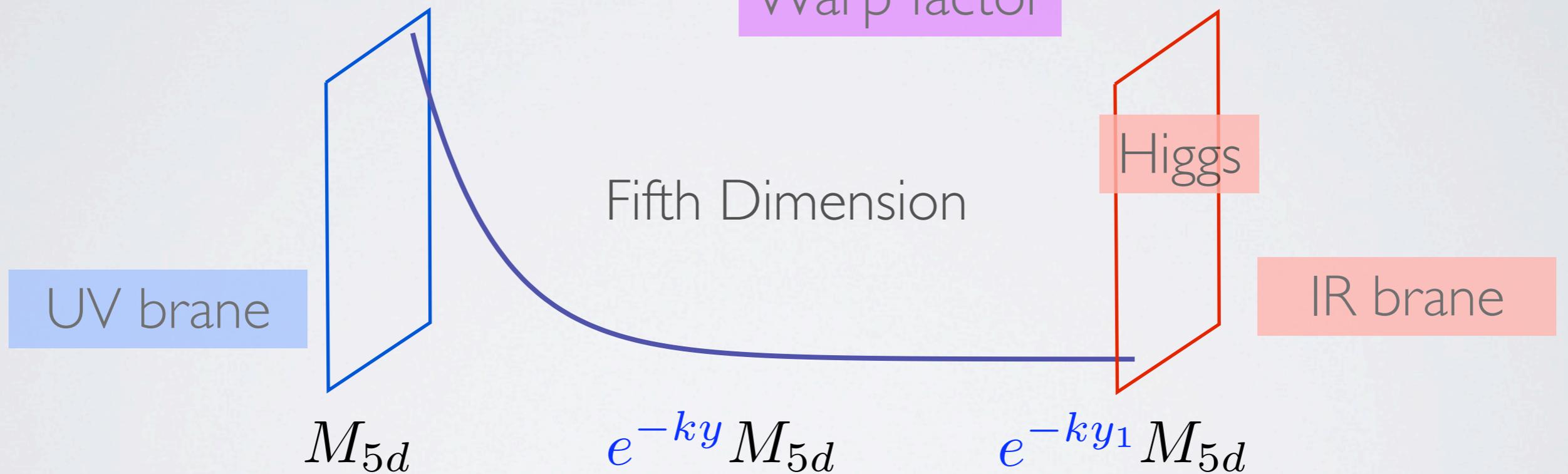


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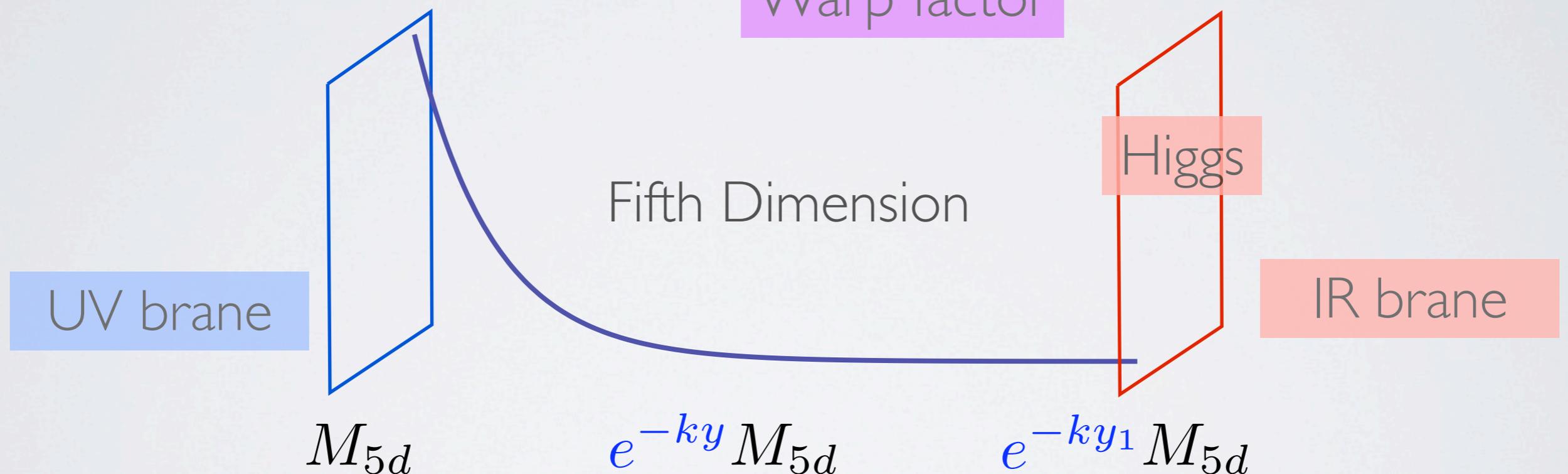


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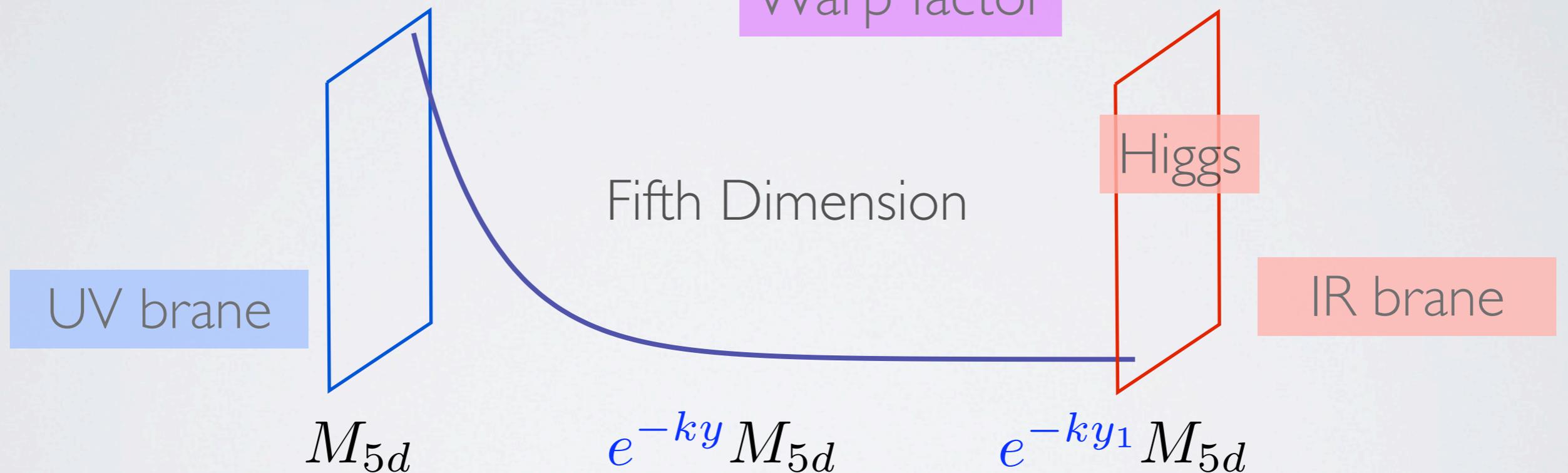
$$\mathcal{L} = \sqrt{g} (g^{\mu\nu} D_\mu H^\dagger D_\nu H - M_{5d}^2 |H^2|)$$

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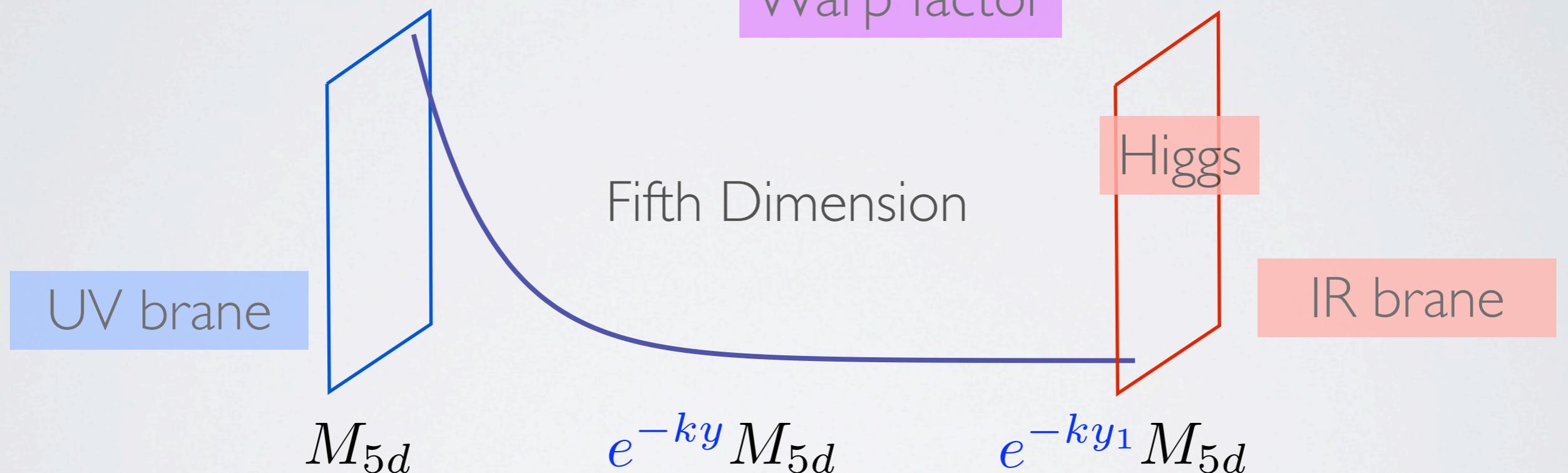
$$\mathcal{L} = e^{-4ky_1} \left( e^{2ky_1} \eta^{\mu\nu} D_\mu H^\dagger D_\nu H - M_{5d}^2 |H^2| \right)$$

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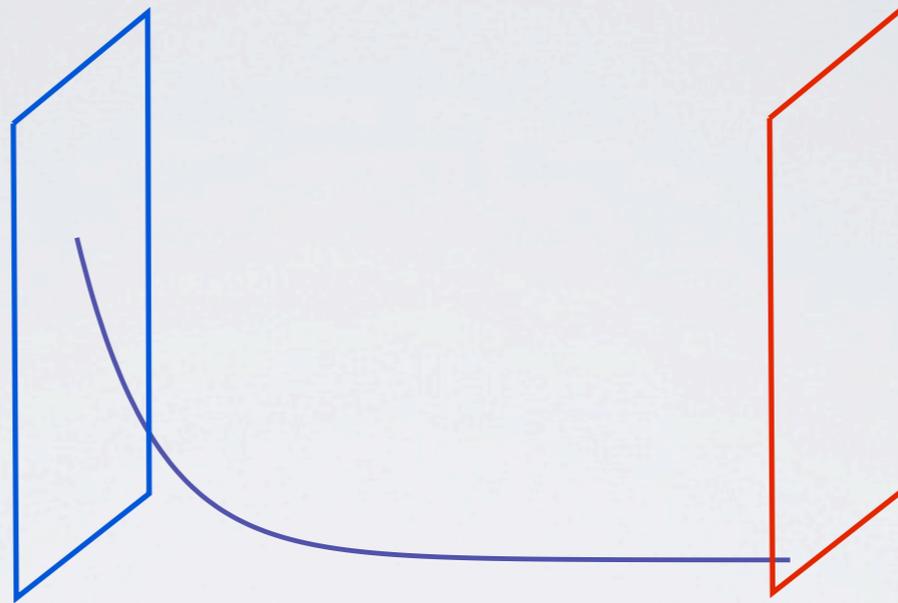
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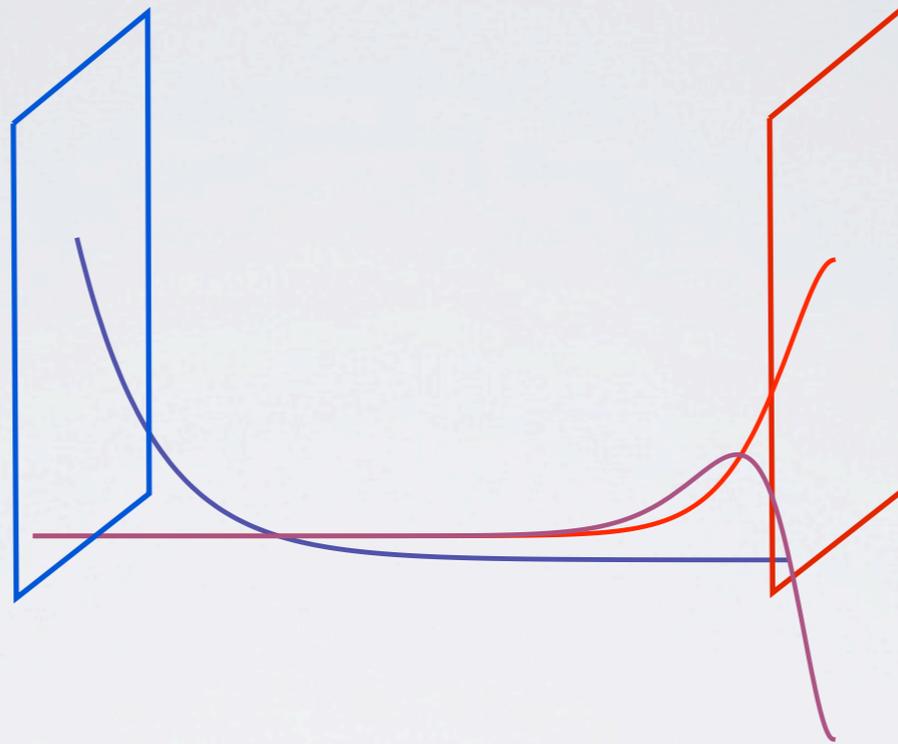
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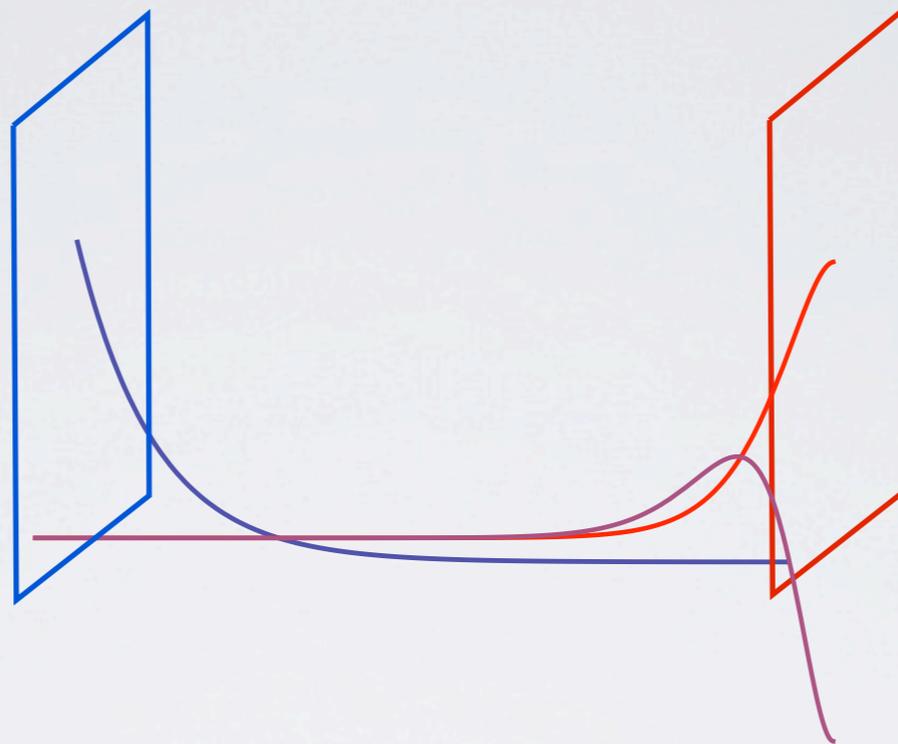
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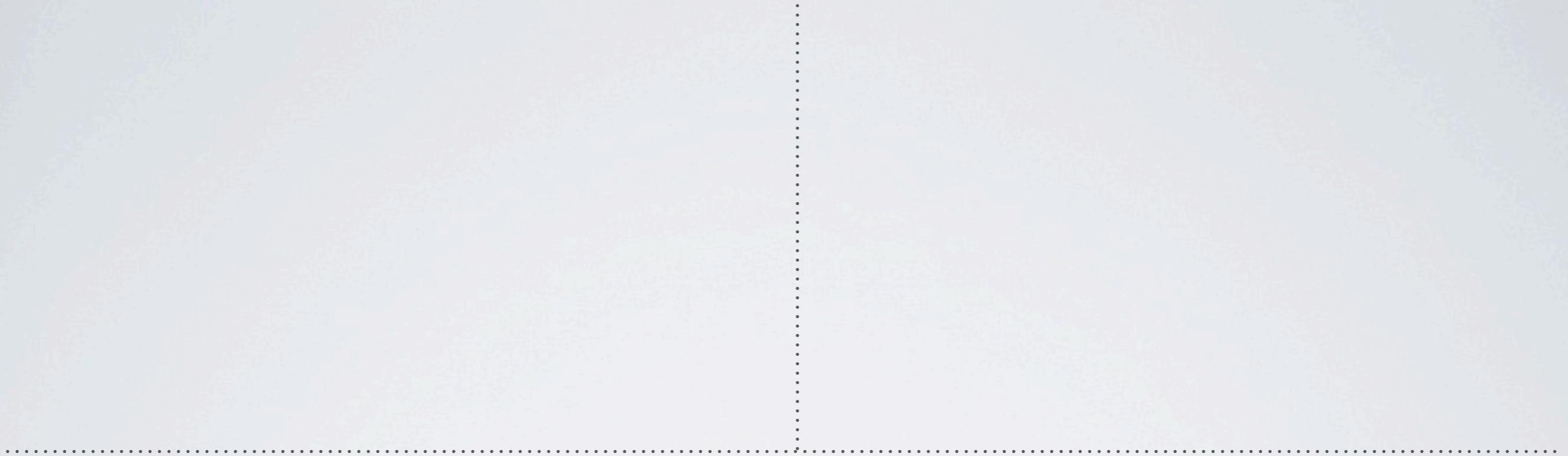
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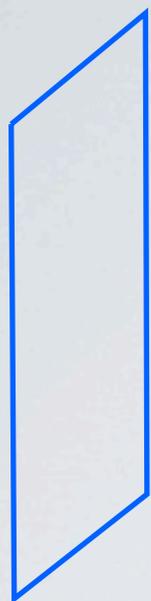
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RS predicts spin-2 resonances at LHC

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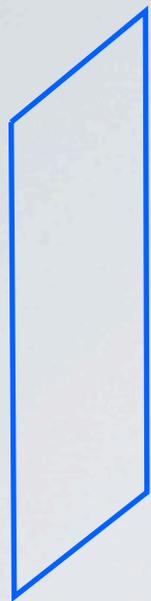
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Gauge  
Higgs  
Fermions



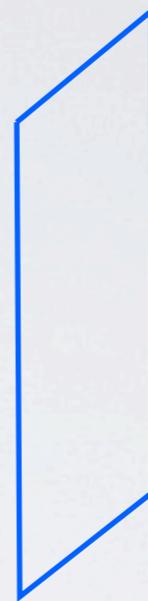
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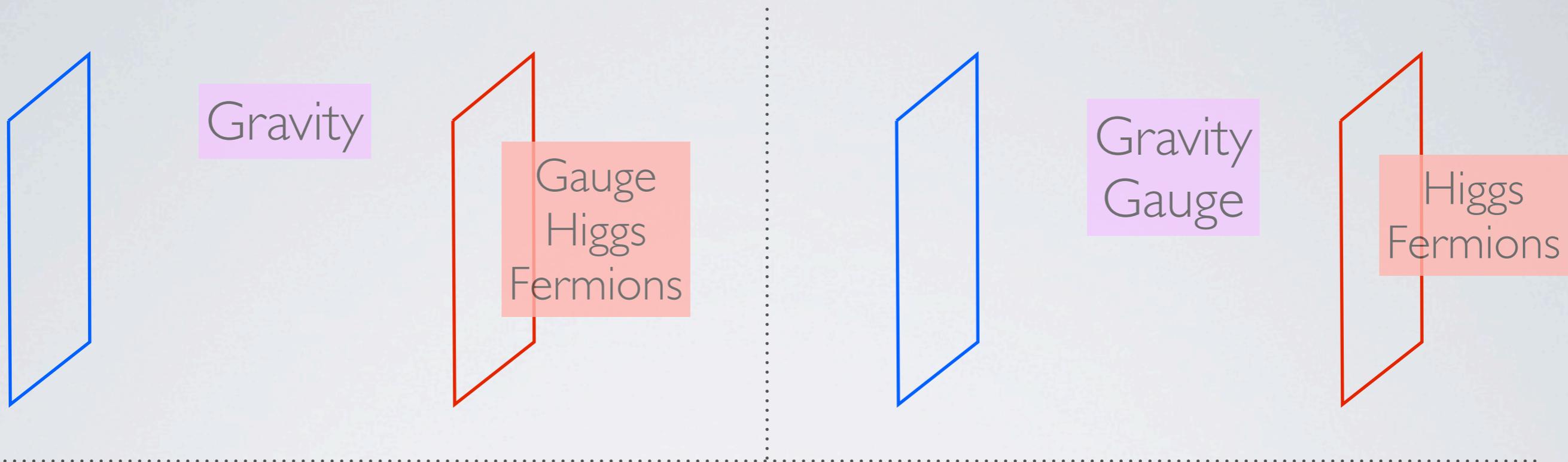


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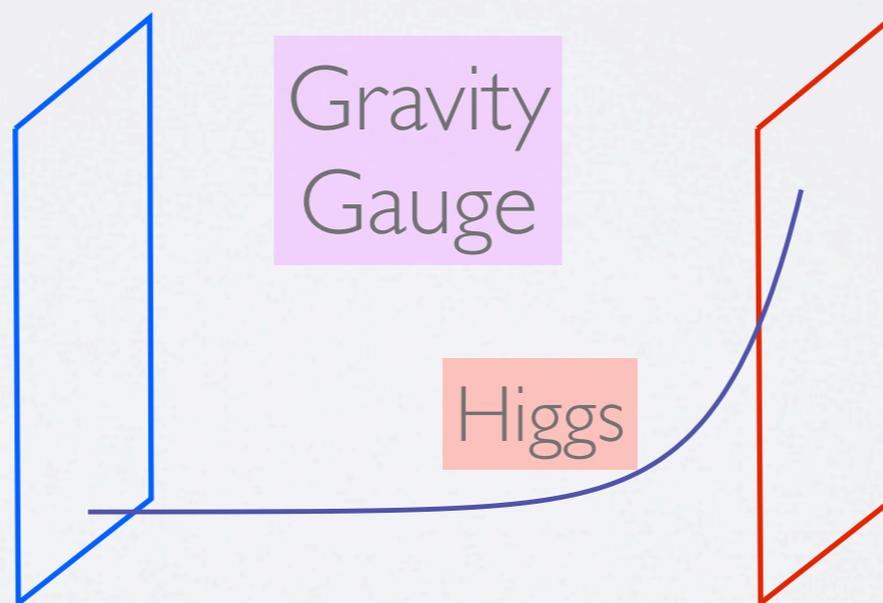


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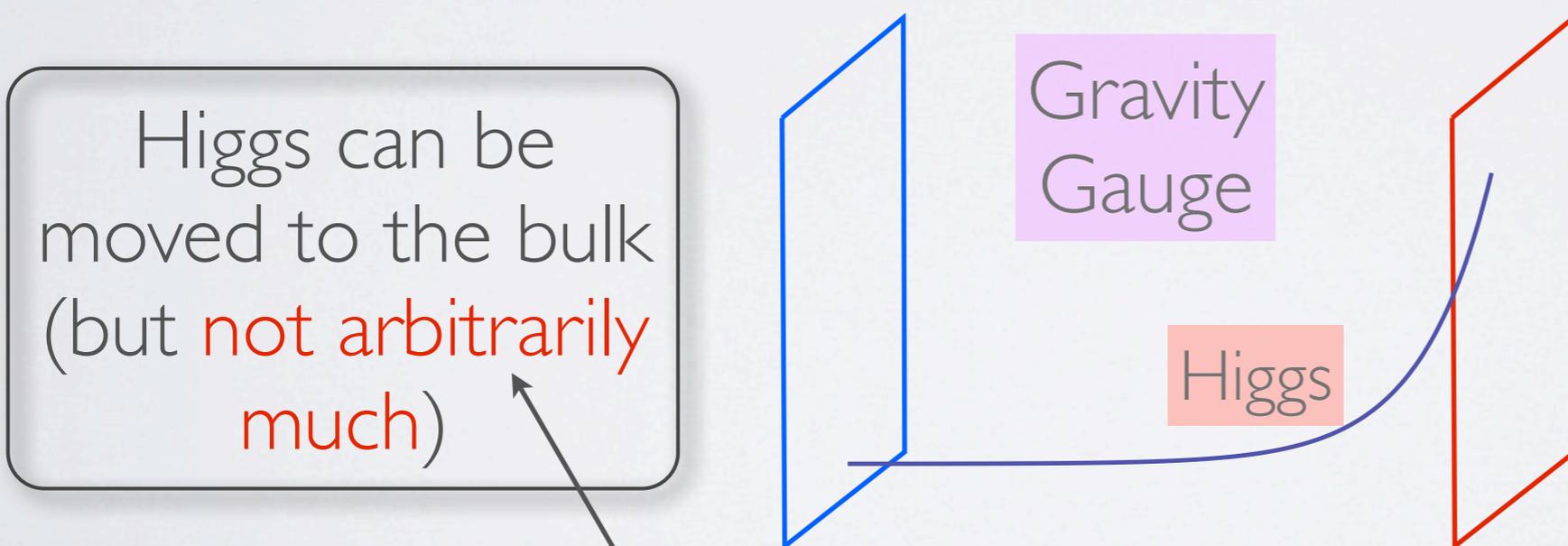
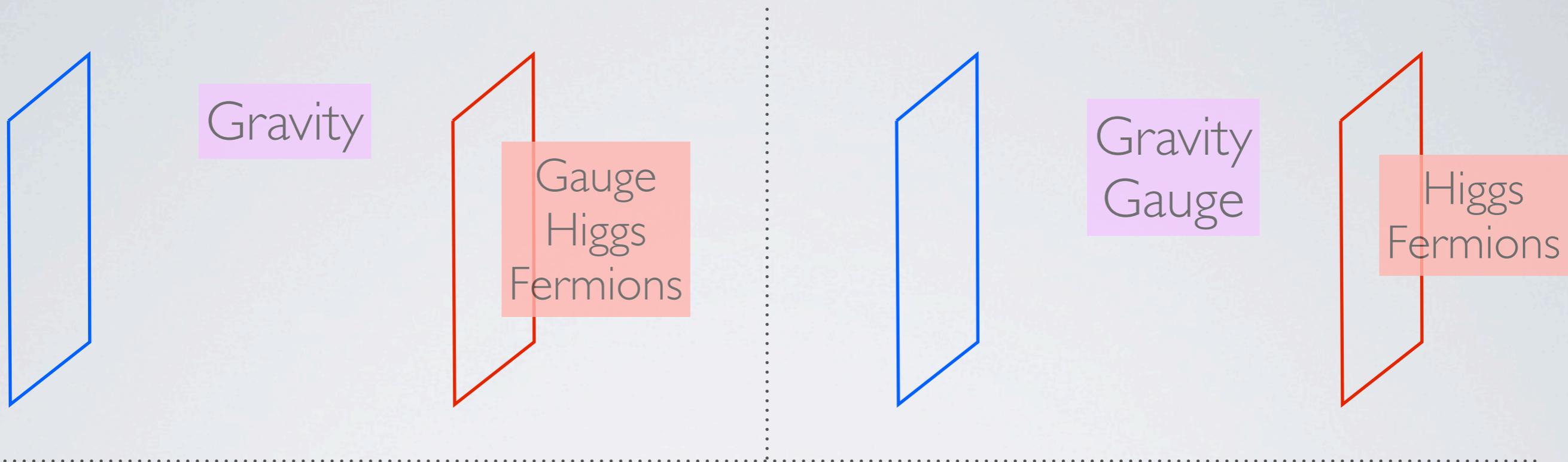
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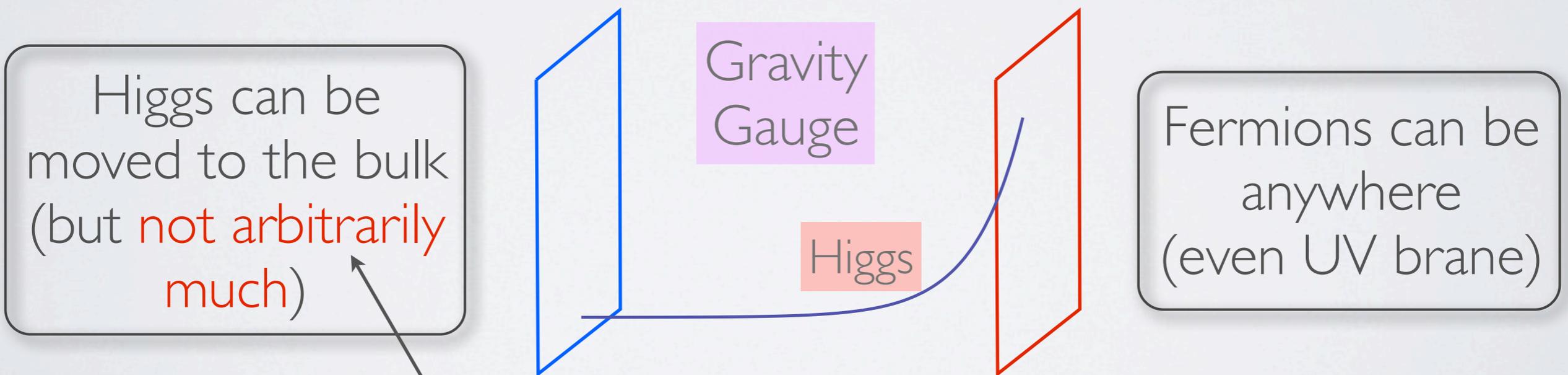
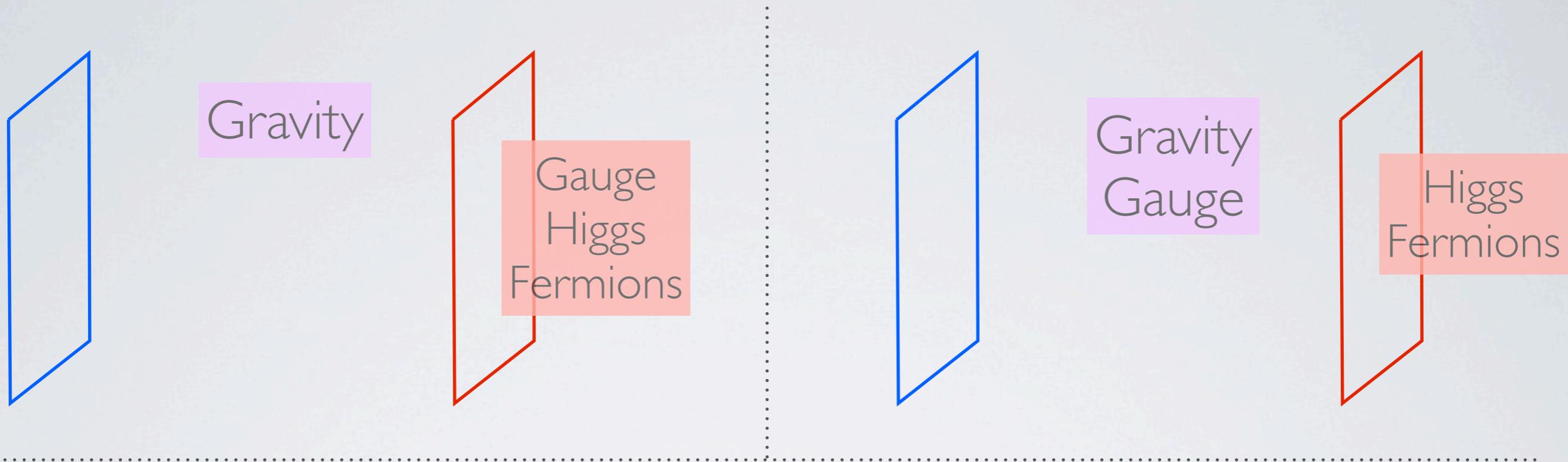
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# NEW PHYSICS STATES

RS models predict:

- ◇ KK gravitons at LHC
- ◇ Light scalar mode (Radion), fluctuations of volume
- ◇ KK modes of other fields, notably spin-1 (KK gluons)

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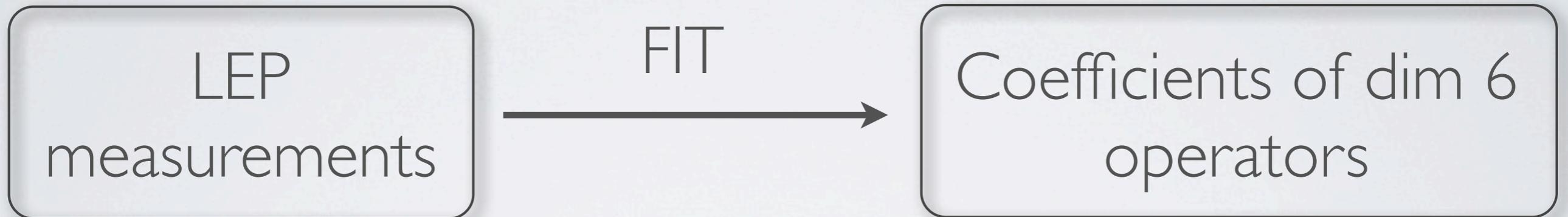
In particular **oblique** corrections

$$\mathcal{O}_S = H^\dagger W_{\mu\nu} H B^{\mu\nu}$$

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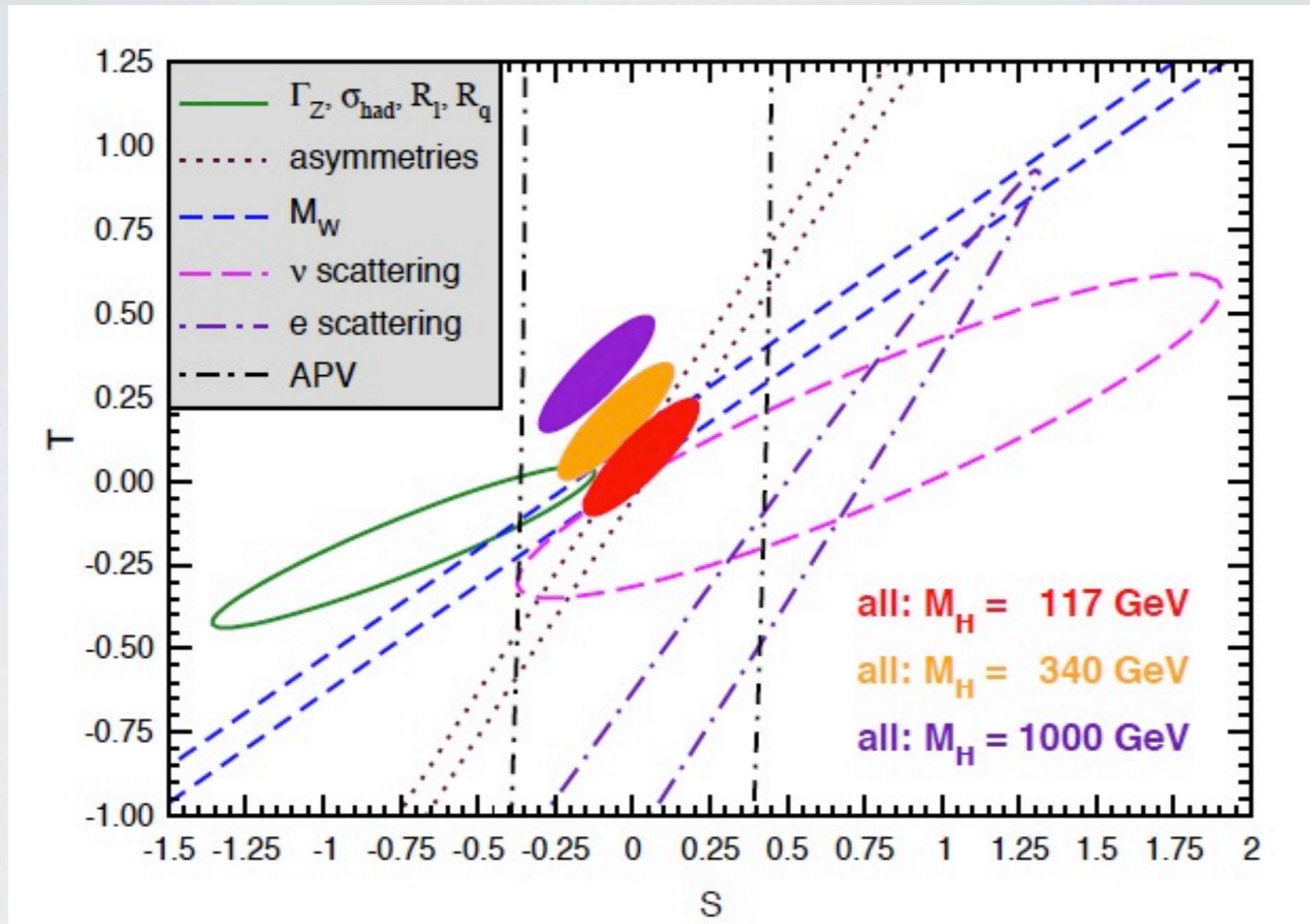
$$\mathcal{O}_S = H^\dagger W_{\mu\nu} H B^{\mu\nu}$$

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$$\mathcal{O}_Y = (\partial_\mu B_{\nu\sigma})^2$$

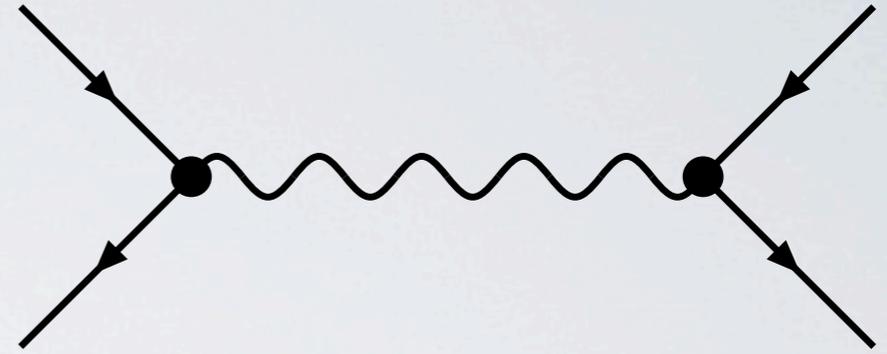
$$\mathcal{O}_W = (D_\mu W_{\nu\sigma})^2$$

# THE S - T ELLIPSE



# RS - EFFECTIVE THEORY

Integrating out KK modes creates these operators



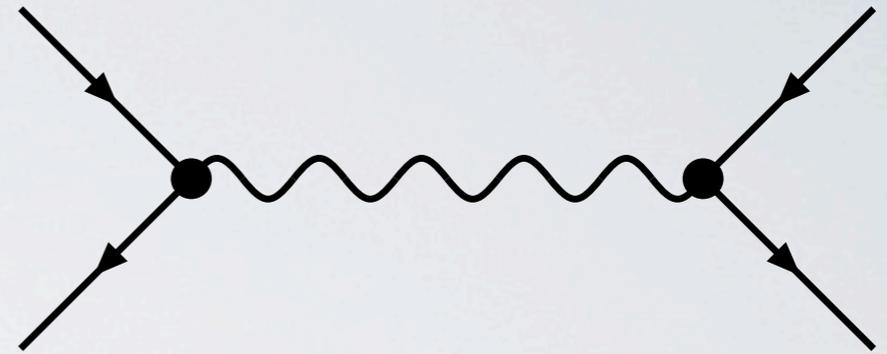
$$\alpha_S \sim \frac{m_W^2}{m_{KK}^2}$$

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- ◇ T is parametrically **enhanced** and provides dominant bounds on KK scale
- ◇ Best available bounds within RS

$$m_{KK} > 7 \text{ TeV}$$

Chang et al '99  
Davoudiasl et al '99  
Huber + Shafi '00

Cabrer, GG, Quiros '10

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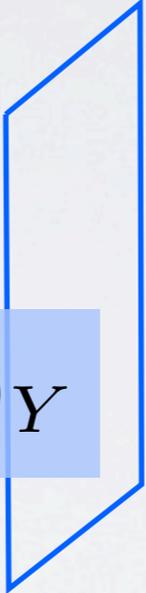
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$$SU(2)_L \times U(1)_Y$$


$$SU(2)_L \times SU(2)_R$$

- ◇ Zero modes: **only SM** gauge fields
- ◇ KK modes: **complete**  $SU(2)_L \times SU(2)_R$  multiplets
- ◇ Custodial Symmetry kills **T** at tree level
- ◇ Dominant bounds from **S**:  $m_{\text{KK}} > 2\text{-}3 \text{ TeV}$

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Brout-Englert-Higgs**less** models (breaking by boundary conditions)  
(based on  $SO(4)/SO(3)$ )  
(large  $N_C$  Technicolor-like)

Csaki et al 2003

# MODELS WITHOUT CS

## Large IR Brane Kinetic Terms

- Calculability an issue

Davoudiasl, Hewett, Rizzo 2002  
Carena et al 2002

## Little RS models

- Reduce volume such that  $T$  is reduced
- Only generates Hierarchy  $\sim 10^3 - 10^4$

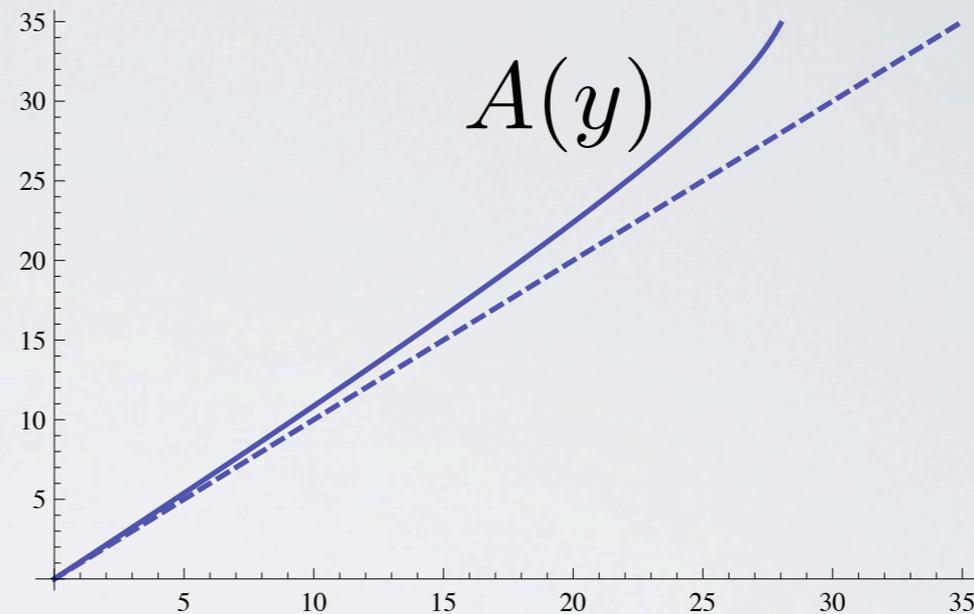
Davoudiasl, Perez, Soni 2008

## Metric Deformations...

Cabrer, GG, Quiros 2010

# METRIC DEFORMATIONS

Modified Warping  
creates large WFR  
for bulk Higgs



$$\mathcal{L}_{eff} = Z |D_\mu H|^2 - V(H) + S H^\dagger W_{\mu\nu} H B^{\mu\nu} + T |H^\dagger D_\mu H|^2$$

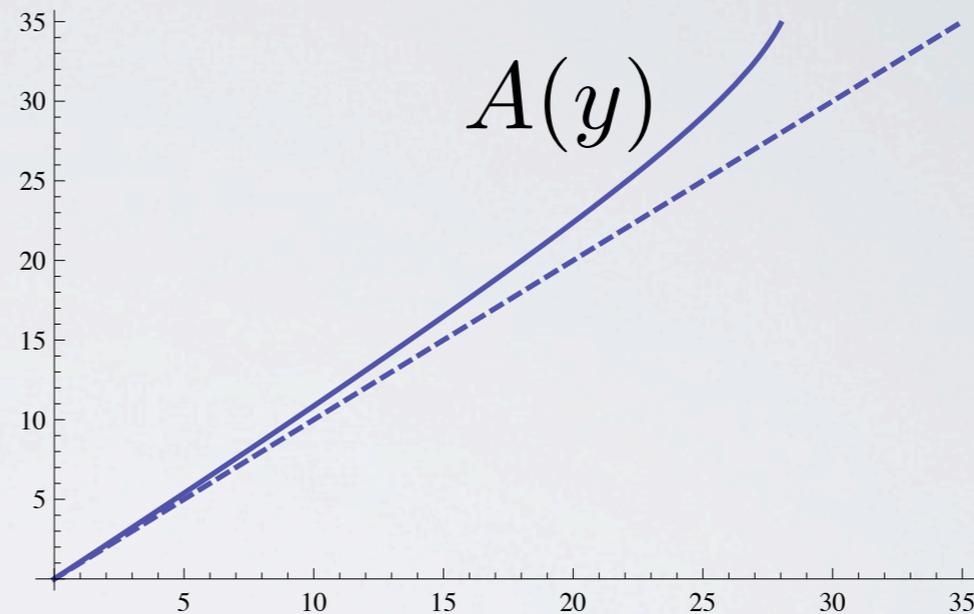
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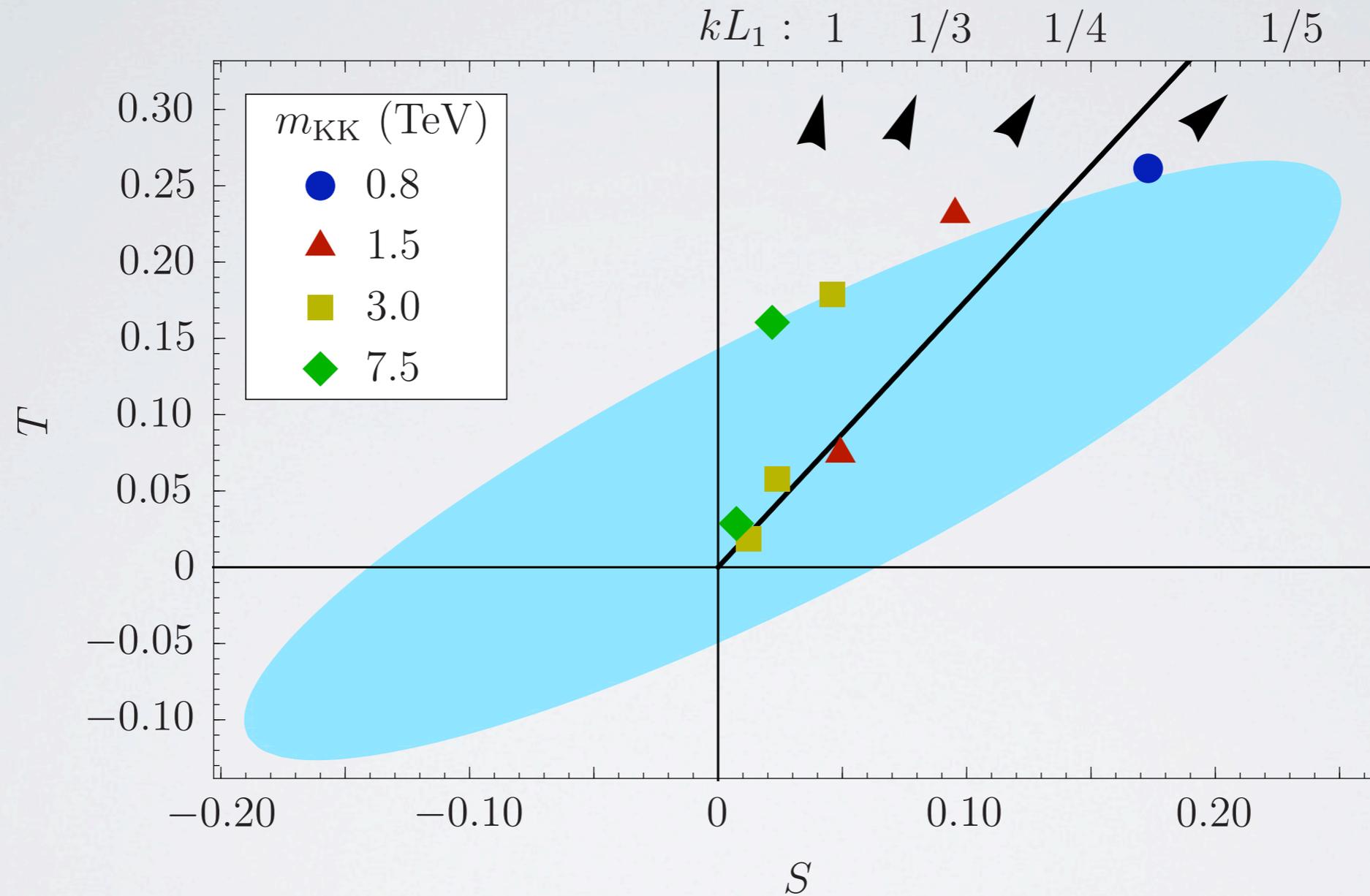
$$\mathcal{L}_{eff} = |D_\mu H|^2 - V\left(\frac{H}{Z^{\frac{1}{2}}}\right) + \frac{S}{Z} H^\dagger W_{\mu\nu} H B^{\mu\nu} + \frac{T}{Z^2} |H^\dagger D_\mu H|^2$$

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# METRIC DEFORMATIONS



# CONCLUSIONS

- A warped fifth Dimension can explain electroweak scale.
- Distinctive collider signature (KK-gravitons, KK gluons, Radion)
- Electroweak precision test require some protection mechanism (custodial symmetry, metric deformations, or rather large KK scale)

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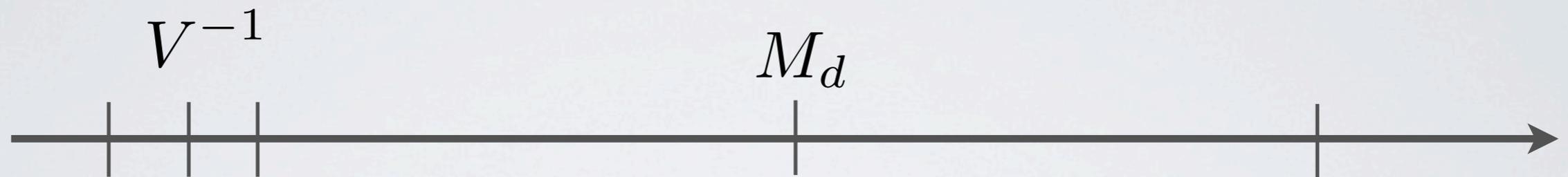


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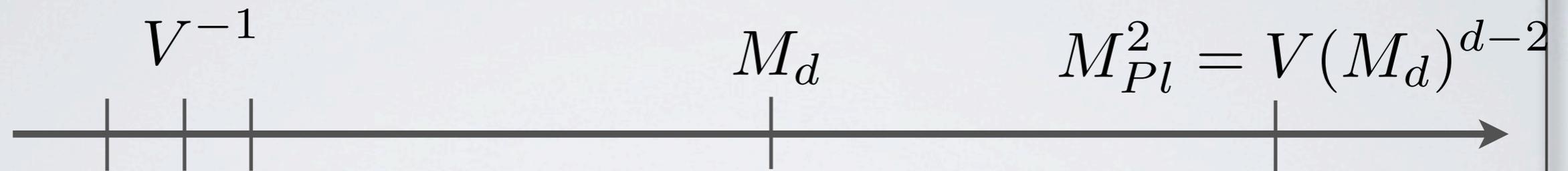


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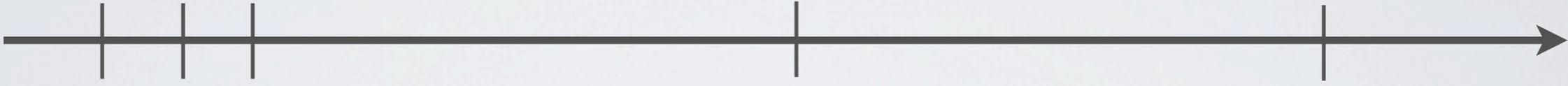
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$$M_d$$

$$M_{Pl}^2 = V (M_d)^{d-2}$$



A horizontal axis with an arrow pointing to the right. It has several tick marks. Above the axis, the labels  $V^{-1}$ ,  $M_d$ , and  $M_{Pl}^2 = V (M_d)^{d-2}$  are positioned above their respective tick marks. Below the axis, the labels  $m_{KK}^{gauge}$  and  $m_{KK}^{grav}$  are positioned above the first three tick marks. An arrow points from the text "Weakly coupled" to these two labels.

$m_{KK}^{gauge}, m_{KK}^{grav}$  ← Weakly coupled

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IR scale “put by hand” BUT can be made stable in the context of **gauge-Higgs unification**:

Manton '79, Hosotani '83,  
Antoniadis et al '01,.....

$$A_M \rightarrow A_\mu, A_i$$

- Embed Higgs in gauge bosons
- Gauge invariance forbids mass terms
- Finite radiative pot. controlled by volume!