

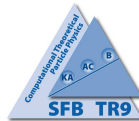
# Flavour physics, supersymmetry and GUTs

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Federal Ministry  
of Education  
and Research



FlaviA  
net

Rencontres de Moriond  
EW Interactions and Unified Theories

La Thuile, March 2011

May 14, 2010

Fermilab Wine&Cheese seminar, talk by Guennadi Borrisov:

*Evidence for an anomalous like-sign dimuon charge asymmetry*

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*Joe Lykken, a theorist at Fermilab, said, "So I would not say that this announcement is the equivalent of seeing the face of God, but it might turn out to be the toe of God."*

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The  $|V_{ub}|$  puzzle

Global analysis of  $B_s - \bar{B}_s$  mixing and  $B_d - \bar{B}_d$  mixing

Supersymmetry

GUTs

Conclusions

CKM matrix  $V$ 

$$V = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix}$$

fixed by measurements of

$$|V_{us}| = 0.2254 \pm 0.0013,$$

$$|V_{cb}| = (40.9 \pm 0.7) \cdot 10^{-3}$$

and a global fit to  $(\bar{\rho}, \bar{\eta})$

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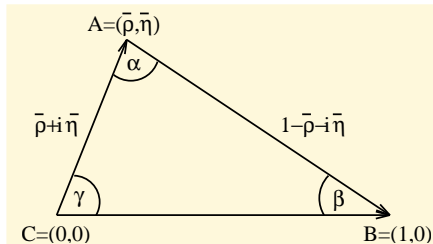
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Unitarity triangle:

$$\begin{aligned} \bar{\rho} + i\bar{\eta} &= -\frac{V_{ub}^* V_{ud}}{V_{cb}^* V_{cd}} \\ &= \left| \frac{V_{ub}^* V_{ud}}{V_{cb}^* V_{cd}} \right| e^{i\gamma} \end{aligned}$$



# The $|V_{ub}|$ puzzle

Three ways to measure  $|V_{ub}|$  :

- exclusive decay  $B \rightarrow \pi l \nu$ ,
- inclusive decay  $B \rightarrow X l \nu$  and
- leptonic decay  $B^+ \rightarrow \tau^+ \nu_\tau$ .



## The $|V_{ub}|$ puzzle

Three ways to measure  $|V_{ub}|$  :

- exclusive decay  $B \rightarrow \pi l \nu$ ,
- inclusive decay  $B \rightarrow X l \nu$  and
- leptonic decay  $B^+ \rightarrow \tau^+ \nu_\tau$ .

Average of several BaBar and Belle measurements:

$$B^{\text{exp}}(B^+ \rightarrow \tau^+ \nu_\tau) = (1.68 \pm 0.31) \cdot 10^{-4}$$

Standard Model:

$$B(B^+ \rightarrow \tau^+ \nu_\tau) = 1.13 \cdot 10^{-4} \cdot \left( \frac{|V_{ub}|}{4 \cdot 10^{-3}} \right)^2 \left( \frac{f_B}{200 \text{ MeV}} \right)^2$$

# The $|V_{ub}|$ puzzle

$$|V_{ub,\text{excl}}| = (3.51 \pm 0.47) \cdot 10^{-3}$$



$$|V_{ub,\text{incl}}| = (4.32 \pm 0.50) \cdot 10^{-3}$$



$$|V_{ub,B \rightarrow \tau \nu}| = (5.10 \pm 0.59) \cdot 10^{-3}$$



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Here  $f_B = (191 \pm 13)$  MeV is used:

$$\begin{aligned} |V_{ub,B \rightarrow \tau \nu}| &= \left[ 5.10 \pm 0.47|_{\text{exp}} \pm 0.35|_{f_B} \right] \cdot 10^{-3} \\ &= [5.10 \pm 0.59] \cdot 10^{-3} \end{aligned}$$

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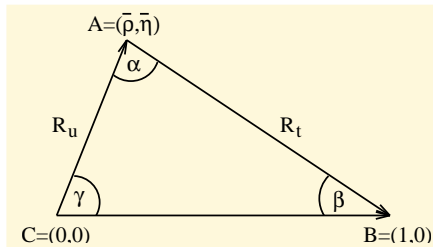
$\Rightarrow$  no puzzle with individual  $|V_{ub}|$  determinations

# The $|V_{ub}|$ puzzle

Indirect determination:

find  $|V_{ub}| \propto |V_{cb}| R_u$

from  $R_u = \frac{\sin \beta}{\sin \alpha}$



With  $\alpha = 89^{\circ} {}^{+4.4^{\circ}}_{-4.2^{\circ}}$  and  $\beta = 21.15^{\circ} \pm 0.89^{\circ}$  find

$$|V_{ub}|_{\text{ind}} = (3.41 \pm 0.15) \cdot 10^{-3}$$

Essential:  $\beta$  from  $A_{\text{CP}}^{\text{mix}}(B_d \rightarrow J/\psi K_S)$

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Alleviate the  $2.9\sigma$  tension between  $|V_{ub,\text{ind}}|$  and  $|V_{ub,B \rightarrow \tau \nu}|$  with new physics in

- $B^+ \rightarrow \tau^+ \nu_\tau$  or
- $A_{\text{CP}}^{\text{mix}}(B_d \rightarrow J/\psi K_S)$ . ← easier!

## $B - \bar{B}$ mixing in the Standard Model

$B_q - \bar{B}_q$  mixing with  $q = d$  or  $q = s$  involves the  $2 \times 2$  matrices  $M$  and  $\Gamma$ .

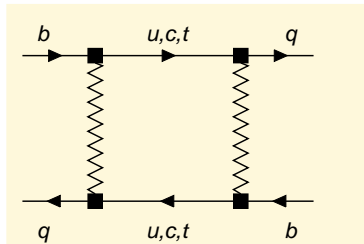


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The **mass matrix** element  $M_{12}^q$  stems from the **dispersive** (real) part of the box diagram, internal  $t$ .

The **decay matrix** element  $\Gamma_{12}^q$  stems from the **absorptive** (imaginary) part of the box diagram, internal  $c, u$ .

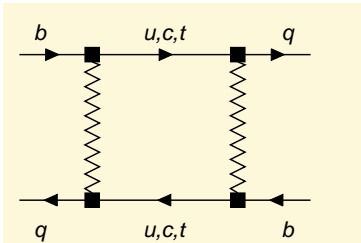


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3 physical quantities in  $B_q - \bar{B}_q$  mixing:

$$|M_{12}^q|, \quad |\Gamma_{12}^q|, \quad \phi_q \equiv \arg \left( -\frac{M_{12}^q}{\Gamma_{12}^q} \right)$$

The two eigenstates found by diagonalising  $M - i\Gamma/2$  differ in their masses and widths:

$$\begin{array}{ll} \text{mass difference} & \Delta m_q \simeq 2|M_{12}^q|, \\ \text{width difference} & \Delta\Gamma_q \simeq 2|\Gamma_{12}^q| \cos\phi_q \end{array}$$

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CP asymmetry in flavour-specific decays (semileptonic CP asymmetry):

$$a_{\text{fs}}^q = \frac{|\Gamma_{12}^q|}{|M_{12}^q|} \sin \phi_q$$

May 14, 2010: DØ presents

$$a_{fs} = (-9.57 \pm 2.51 \pm 1.46) \cdot 10^{-3}$$

for a mixture of  $B_d$  and  $B_s$  mesons with

$$a_{fs} = (0.506 \pm 0.043)a_{fs}^d + (0.494 \pm 0.043)a_{fs}^s$$

The result is  $3.2\sigma$  away from  $a_{fs}^{SM} = (-0.20 \pm 0.03) \cdot 10^{-3}$ .

A. Lenz, UN, 2006 and 2011

Averaging with an older CDF measurement yields

$$a_{fs} = (-8.5 \pm 2.8) \cdot 10^{-3},$$

which is  $2.9\sigma$  away from  $a_{fs}^{SM}$ .

## Generic new physics

Phases  $\phi_q = \arg(-M_{12}^q/\Gamma_{12}^q)$  in the Standard Model:

$$\phi_d^{\text{SM}} = -4.3^\circ \pm 1.4^\circ, \quad \phi_s^{\text{SM}} = 0.2^\circ.$$

Define the complex parameters  $\Delta_d$  and  $\Delta_s$  through

$$M_{12}^q \equiv M_{12}^{\text{SM},q} \cdot \Delta_q, \quad \Delta_q \equiv |\Delta_q| e^{i\phi_q^\Delta}.$$

In the Standard Model  $\Delta_q = 1$ . Use  $\phi_s = \phi_s^{\text{SM}} + \phi_s^\Delta \simeq \phi_s^\Delta$ .

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The measurements

$$\begin{aligned} \Delta m_s &= (17.77 \pm 0.10 \pm 0.07) \text{ ps}^{-1} && \text{CDF} \\ \Delta m_s &= (17.63 \pm 0.11 \pm 0.04) \text{ ps}^{-1} && \text{LHCb (prelim)} \end{aligned}$$

imply

$$|\Delta_s| = 1.03 \pm 0.14_{(\text{th})} \pm 0.01_{(\text{exp})}$$

## Confront the DØ/CDF average

$$\begin{aligned} a_{\text{fs}} &= (0.506 \pm 0.043) a_{\text{fs}}^d + (0.494 \pm 0.043) a_{\text{fs}}^s \\ &= (-8.5 \pm 2.8) \cdot 10^{-3} \end{aligned}$$

with (A. Lenz, UN, 2011)

$$a_{\text{fs}}^d = (5.4 \pm 1.0) \cdot 10^{-3} \cdot \frac{\sin \phi_d}{|\Delta_d|}, \quad a_{\text{fs}}^s = (5.1 \pm 1.0) \cdot 10^{-3} \cdot \frac{\sin \phi_s}{|\Delta_s|}.$$



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⇒ Need **both**  $\phi_s < 0$  and  $\phi_d < 0$ .

## Confront the $D\bar{0}/CDF$ average

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$\Rightarrow$  Need **both**  $\phi_s < 0$  and  $\phi_d < 0$ .

$$A_{CP}^{\text{mix}}(B_d \rightarrow J/\psi K_S) \propto \sin(2\beta + \phi_d^\Delta):$$

With  $\phi_d^\Delta < 0$  find  $\beta > \beta^{\text{SM}} = 21^\circ \Rightarrow |V_{ub}|$  puzzle solvable.

# Global analysis of $B_s - \bar{B}_s$ mixing and $B_d - \bar{B}_d$ mixing

Based on work with A. Lenz and the CKMfitter Group  
(J. Charles, S. Descotes-Genon, A. Jantsch, C. Kaufhold,  
H. Lacker, S. Monteil, V. Niess) arXiv:1008.1593

**Rfit method:** No statistical meaning is assigned to systematic errors and theoretical uncertainties.

We have performed a simultaneous fit to the Wolfenstein parameters and to the new physics parameters  $\Delta_s$  and  $\Delta_d$ :

$$\Delta_q \equiv \frac{M_{12}^q}{M_{12}^{q,SM}}, \quad \Delta_q \equiv |\Delta_q| e^{i\phi_q^\Delta}.$$

Three scenarios:

**Scenario I:** arbitrary complex parameters  $\Delta_s$  and  $\Delta_d$

**Scenario II:** new physics is minimally flavour violating (MFV) (meaning that all flavour violation stems from the Yukawa sector) and  $y_b$  is small:  
one real parameter  $\Delta = \Delta_s = \Delta_d$

**Scenario III:** MFV with a large  $y_b$ : one complex parameter  
 $\Delta = \Delta_s = \Delta_d$

Three scenarios:

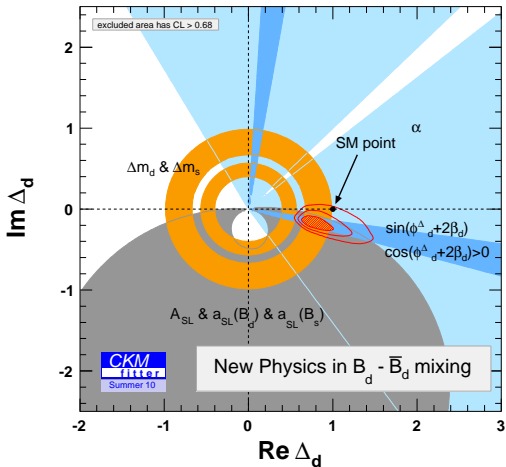
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**Examples:** Scenario I covers the **MSSM** with generic flavour structure of the soft terms and small  $\tan\beta$ .  
Scenario II covers the **MSSM** with **MFV** and small  $\tan\beta$ .  
Scenario III covers certain **two-Higgs-doublet models** (but **not** the **MFV-MSSM**, **CMSSM** and **mSUGRA**).

## Results in scenario I:



SM point  $\Delta_d = 1$   
disfavoured by  $2.7\sigma$ .

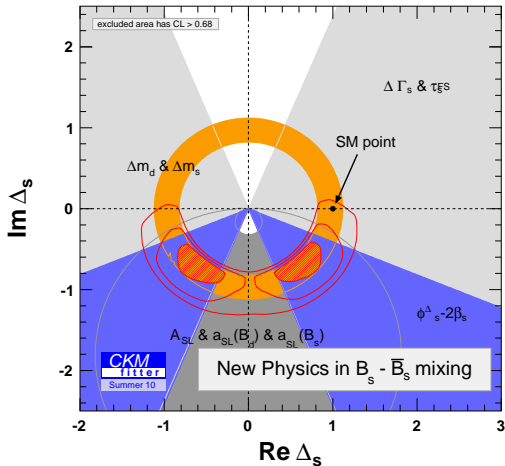
Main driver:  
 $B^+ \rightarrow \tau^+ \nu_\tau$

Global fit to UT hinting at  $\phi_d^\Delta < 0$ :

Other authors have seen a tension with the SM in the same direction stemming from  $\epsilon_K$ .

Lunghi, Soni; Buras, Guadagnoli

In our fit the tension with  $\epsilon_K$  is mild, because the Rfit method is more conservative. We use  $\hat{B}_K = 0.724 \pm 0.004 \pm 0.067$  corresponding to  $B_K(2 \text{ GeV}) = 0.527 \pm 0.0031 \pm 0.049$ , which is an average dominated by the result of Aubin, Laiho and van De Water, 2009.



SM point  $\Delta_s = 1$   
disfavoured by  $2.7\sigma$ .

without 2010 CDF/DØ data on  $B_s \rightarrow J/\psi\phi$



**p-values:**

Calculate  $\chi^2/N_{\text{dof}}$  with and without a hypothesis to find:

Hypothesis	p-value
$\Delta_d = 1$ (2D)	$2.7 \sigma$
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$\Delta_d = \Delta_s$ (2D)	$2.1 \sigma$
$\Delta_d = \Delta_s = 1$ (4D)	$3.6 \sigma$

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$\Delta_d = \Delta_s = 1$ (4D)	$3.6 \sigma$

Hypothesis	p-value
$\text{Im}(\Delta_d) = 0$ (1D)	$2.7 \sigma$
$\text{Im}(\Delta_s) = 0$ (1D)	$3.1 \sigma$
$\text{Im}(\Delta_d) = \text{Im}(\Delta_s) = 0$ (2D)	$3.8 \sigma$

Fit result at 95%CL :

$$\phi_S^\Delta = (-52_{-25}^{+32})^\circ \quad (\text{and } \phi_S^\Delta = (-130_{-28}^{+28})^\circ)$$

Compare with the 2010 CDF/DØ result from  $B_s \rightarrow J/\psi\phi$  :

CDF:  $\phi_S^\Delta = (-29_{-49}^{+44})^\circ$  at 95%CL

DØ:  $\phi_S^\Delta = (-44_{-51}^{+59})^\circ$  at 95%CL

Naive average:  $\phi_S^{\text{avg}} = (-36 \pm 35)^\circ$  at 95%CL

Is the result driven by the  $D\bar{D}$  dimuon asymmetry?

One can remove  $a_{fs}$  as an input and instead **predict** it from the global fit:

$$a_{fs} = \left( -4.2^{+2.9}_{-2.7} \right) \cdot 10^{-3} \quad \text{at } 2\sigma.$$

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This is just  $1.5\sigma$  away from the  $D\bar{D}/CDF$  average

$$a_{fs} = (-8.5 \pm 2.8) \cdot 10^{-3}.$$

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$\Rightarrow$  bad news for **CMSSM** and **mSUGRA**

Scenario III (complex  $\Delta_s = \Delta_d$ ) fits the data quite well irrespective of whether  $B(B^+ \rightarrow \tau^+ \nu_\tau)$  is included or not.

Hypothesis	p-value
$\Delta = 1$	$3.3 \sigma$



# Supersymmetry

The **MSSM** has many new sources of flavour violation, all in the **supersymmetry-breaking sector**.

No problem to get big effects in  **$B_s - \bar{B}_s$  mixing**, but rather to suppress the big effects elsewhere.

Are there natural ways to motivate sizable new flavour violation in  $B_s - \bar{B}_s$  mixing and  $B_d - \bar{B}_d$  mixing while simultaneously suppressing flavour violation elsewhere?

## Flavour and SUSY GUTs

Linking quarks to neutrinos: Flavour mixing:

quarks: Cabibbo-Kobayashi-Maskawa (CKM) matrix

leptons: Pontecorvo-Maki-Nakagawa-Sakata (PMNS) matrix

Consider SU(5) multiplets:

$$\bar{\mathbf{5}}_1 = \begin{pmatrix} d_R^c \\ d_R^c \\ d_R^c \\ e_L \\ -\nu_e \end{pmatrix}, \quad \bar{\mathbf{5}}_2 = \begin{pmatrix} s_R^c \\ s_R^c \\ s_R^c \\ \mu_L \\ -\nu_\mu \end{pmatrix}, \quad \bar{\mathbf{5}}_3 = \begin{pmatrix} b_R^c \\ b_R^c \\ b_R^c \\ \tau_L \\ -\nu_\tau \end{pmatrix}.$$

If the observed large atmospheric neutrino mixing angle stems from a rotation of  $\bar{\mathbf{5}}_2$  and  $\bar{\mathbf{5}}_3$ , it will induce a large  $\tilde{b}_R - \tilde{s}_R$ -mixing (Moroi; Chang, Masiero, Murayama).

⇒ new  $b_R - s_R$  transitions from gluino-squark loops possible.

Key ingredients: Some weak basis with

$$Y_d = V_{\text{CKM}}^* \begin{pmatrix} y_d & 0 & 0 \\ 0 & y_s & 0 \\ 0 & 0 & y_b \end{pmatrix} U_{\text{PMNS}}$$

and right-handed down squark mass matrix:

$$m_{\tilde{d}}^2(M_Z) = \text{diag} \left( m_{\tilde{d}}^2, m_{\tilde{d}}^2, m_{\tilde{d}}^2 - \Delta_{\tilde{d}} \right).$$

with a calculable real parameter  $\Delta_{\tilde{d}}$ , typically generated by top-Yukawa RG effects.

Rotating  $Y_d$  to diagonal form puts the large atmospheric neutrino mixing angle into  $m_{\tilde{d}}^2$ :

$$U_{\text{PMNS}}^\dagger m_{\tilde{d}}^2 U_{\text{PMNS}} = \begin{pmatrix} m_{\tilde{d}}^2 & 0 & 0 \\ 0 & m_{\tilde{d}}^2 - \frac{1}{2} \Delta_{\tilde{d}} & -\frac{1}{2} \Delta_{\tilde{d}} e^{i\xi} \\ 0 & -\frac{1}{2} \Delta_{\tilde{d}} e^{-i\xi} & m_{\tilde{d}}^2 - \frac{1}{2} \Delta_{\tilde{d}} \end{pmatrix}$$

The CP phase  $\xi$  affects  $B_s - \bar{B}_s$  mixing!

## Chang-Masiero-Murayama model

The Chang–Masiero–Murayama (CMM) model is based on the symmetry breaking chain

$$SO(10) \rightarrow SU(5) \rightarrow SU(3) \times SU(2)_L \times U(1)_Y.$$

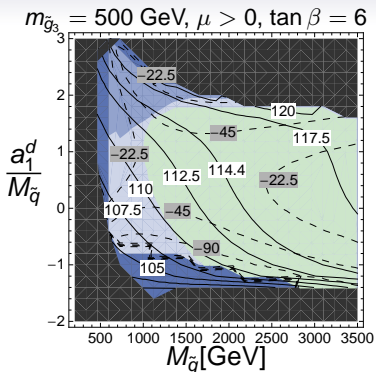
We have considered  $B_s - \bar{B}_s$  mixing,  $b \rightarrow s\gamma$ ,  $\tau \rightarrow \mu\gamma$ , vacuum stability bounds, lower bounds on sparticle masses and the mass of the lightest Higgs boson.

The analysis involves 7 parameters in addition to those of the Standard Model.

Generic results: Largest effect in  $B_s - \bar{B}_s$  mixing  
powerful constraint:  $M_h \geq 114 \text{ GeV}$

J. Gierbach, S. Jäger, M. Knopf, W. Martens, UN, C. Scherrer, S. Wiesenfeldt

1101.6047



Black: negative soft masses<sup>2</sup>

Gray blue: excluded by  $\tau \rightarrow \mu \gamma$

Medium blue: excluded by

$b \rightarrow s \gamma$

Dark blue: excluded by  $B_s - \bar{B}_s$

mixing

Green: allowed

$M_{\tilde{q}}$  : squark mass of first two generations

$a_1^d$  : trilinear term of first two generations

Dashed lines with gray labels:  $\phi_s$  in degrees

Solid lines with white labels:  $M_h$ .

## Conclusions

- The  $D\bar{0}$  result for the **dimuon asymmetry** in  $B_s$  decays supports the hints for  $\phi_s < 0$  seen in  $B_s \rightarrow J/\psi\phi$  data. The central value is easier to accommodate if both  $a_{fs}^s$  and  $a_{fs}^d$  receive negative contributions from new physics.



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- A global fit to the UT indeed shows a slight preference for a new CP phase  $\phi_d^\Delta < 0$ , driven by  $B(B^+ \rightarrow \tau^+\nu_\tau)$  (and possibly  $\epsilon_K$ ). In a simultaneously global fit to the UT and the  $B_s - \bar{B}_s$  **mixing** complex a plausible picture of new CP-violating physics emerges.

## Conclusions

- Large CP-violating contributions to  $B_s - \bar{B}_s$  mixing are possible in supersymmetry without violating constraints from other FCNC processes. If confirmed, the  $D\mathcal{O}/CDF$  results imply physics beyond the CMSSM and mSUGRA.

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- Models of GUT flavour physics with  $\tilde{b}_R - \tilde{s}_R$  mixing driven by the atmospheric neutrino mixing angle can explain the Tevatron data on  $B_s - \bar{B}_s$  mixing without conflicting with  $b \rightarrow s\gamma$  and  $\tau \rightarrow \mu\gamma$ .



A pinch of new physics in  
 $B-\bar{B}$  mixing?

# Backup slides

## Pull values

Quantity	Deviation			
	wrt SM fit	wrt Sc. I	wrt Sc. II	wrt Sc. III
$\widehat{B}_K$	0.0 $\sigma$	-	0.0 $\sigma$	-
$f_{B_s}$ [MeV]	0.0 $\sigma$	0.9 $\sigma$	0.8 $\sigma$	1.2 $\sigma$
$\widehat{B}_{B_s}$	1.2 $\sigma$	0.8 $\sigma$	0.9 $\sigma$	0.3 $\sigma$
$f_{B_s}/f_{B_d}$	0.0 $\sigma$	0.9 $\sigma$	0.0 $\sigma$	0.0 $\sigma$
$\mathcal{B}_{B_s}/\mathcal{B}_{B_d}$	1.0 $\sigma$	0.9 $\sigma$	1.0 $\sigma$	0.9 $\sigma$
$\widetilde{B}_{S,B_s}(m_b)$	1.0 $\sigma$	0.7 $\sigma$	1.1 $\sigma$	0.2 $\sigma$
$\alpha$	1.1 $\sigma$	0.2 $\sigma$	0.7 $\sigma$	1.0 $\sigma$
$\phi_d^\Delta + 2\beta$	2.8 $\sigma$	0.8 $\sigma$	2.6 $\sigma$	1.3 $\sigma$
$\gamma$	0.0 $\sigma$	0.0 $\sigma$	0.0 $\sigma$	0.0 $\sigma$
$\phi_s^\Delta - 2\beta_s$	2.3 $\sigma$	0.5 $\sigma$	2.4 $\sigma$	1.6 $\sigma$

Quantity	Deviation			
	wrt SM fit	wrt Sc. I	wrt Sc. II	wrt Sc. III
$ \epsilon_K $	0.0 $\sigma$	-	0.0 $\sigma$	-
$\Delta m_d$	1.0 $\sigma$	0.9 $\sigma$	1.0 $\sigma$	0.8 $\sigma$
$\Delta m_s$	0.3 $\sigma$	0.7 $\sigma$	0.9 $\sigma$	1.2 $\sigma$
$A_{\text{SL}}$	2.9 $\sigma$	1.2 $\sigma$	2.9 $\sigma$	2.2 $\sigma$
$a_{\text{SL}}^d$	0.9 $\sigma$	0.2 $\sigma$	0.8 $\sigma$	0.3 $\sigma$
$a_{\text{SL}}^s$	0.2 $\sigma$	0.7 $\sigma$	0.2 $\sigma$	0.0 $\sigma$
$\Delta\Gamma_s$	1.0 $\sigma$	0.2 $\sigma$	1.1 $\sigma$	0.9 $\sigma$
$\mathcal{B}(B \rightarrow \tau\nu)$	2.9 $\sigma$	0.7 $\sigma$	2.6 $\sigma$	1.0 $\sigma$
$\mathcal{B}(B \rightarrow \tau\nu)$ and $A_{\text{SL}}$	3.7 $\sigma$	0.9 $\sigma$	3.5 $\sigma$	2.0 $\sigma$
$\phi_s^\Delta - 2\beta_s$ and $A_{\text{SL}}$	3.3 $\sigma$	0.8 $\sigma$	3.3 $\sigma$	2.3 $\sigma$
$\mathcal{B}(B \rightarrow \tau\nu)$ , $\phi_s^\Delta - 2\beta_s$ , $A_{\text{SL}}$	4.0 $\sigma$	0.6 $\sigma$	3.8 $\sigma$	2.1 $\sigma$

## Dimension-5 terms

Realistic GUTs involve further dimension-5 Yukawa terms to fix the Yukawa unification in the first two generations. One can use these terms to shuffle a part of the effect from  $b_R \rightarrow s_R$  into  $b_R \rightarrow d_R$  transitions. This “leakage” is strongly constrained by  $K - \bar{K}$  mixing.

Trine, Wiesenfeldt, Westhoff 2009



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Trine, Wiesenfeldt, Westhoff 2009

Similar constraints can be found from  $\mu \rightarrow e\gamma$ .

Ko, Park, Yamaguchi 2008; Borzumati, Yamashita 2009;

Girrbach, Mertens, UN, Wiesenfeldt 2009.

## SO(10) superpotential

$$\begin{aligned}
 W_Y = & \frac{1}{2} 16_i Y_u^{ij} 16_j 10_H + \frac{1}{2} 16_i Y_d^{ij} 16_j \frac{45_H 10'_H}{M_{\text{Pl}}} \\
 & + \frac{1}{2} 16_i Y_N^{ij} 16_j \frac{\overline{16}_H \overline{16}_H}{M_{\text{Pl}}}
 \end{aligned}$$

with the Planck mass  $M_{\text{Pl}}$  and

- $16_i$ : one **matter superfield** per generation,  $i = 1, 2, 3$ ,
- $10_H$ : Higgs superfield containing MSSM Higgs superfield  $H_u$ ,
- $10'_H$ : Higgs superfield containing MSSM superfield  $H_u$ ,
- $45_H$ : Higgs superfield in adjoint representation,
- $\overline{16}_H$ : Higgs superfield in spinor representation.

## Methodology of CMM analysis

### Input:

- squark masses  $M_{\tilde{u}}, M_{\tilde{d}}$  of right-handed **up** and **down squarks**,
- trilinear term  $a_1^d$  of first generation,
- gluino mass  $m_{\tilde{g}_3}$ ,
- **arg  $\mu$**  ,
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RG evolution from  $M_{\text{ew}}$  to  $M_{\text{Pl}}$ : find universal soft terms  $a_0$ ,  $m_0$ ,  $m_{\tilde{g}}$  and  $D$  .

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Repeat RG evolution  $M_{\text{ew}} \rightarrow M_{\text{Pl}} \rightarrow M_{\text{ew}}$ : find all **particle masses** and **MSSM couplings**

adjust CP phase  $\xi$  to approximate experimental  $\Delta_S$  best.