

# Lepton flavour and number violation with K decays at CERN

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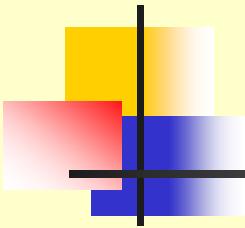
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## Outline:

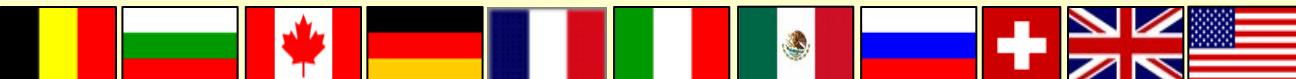
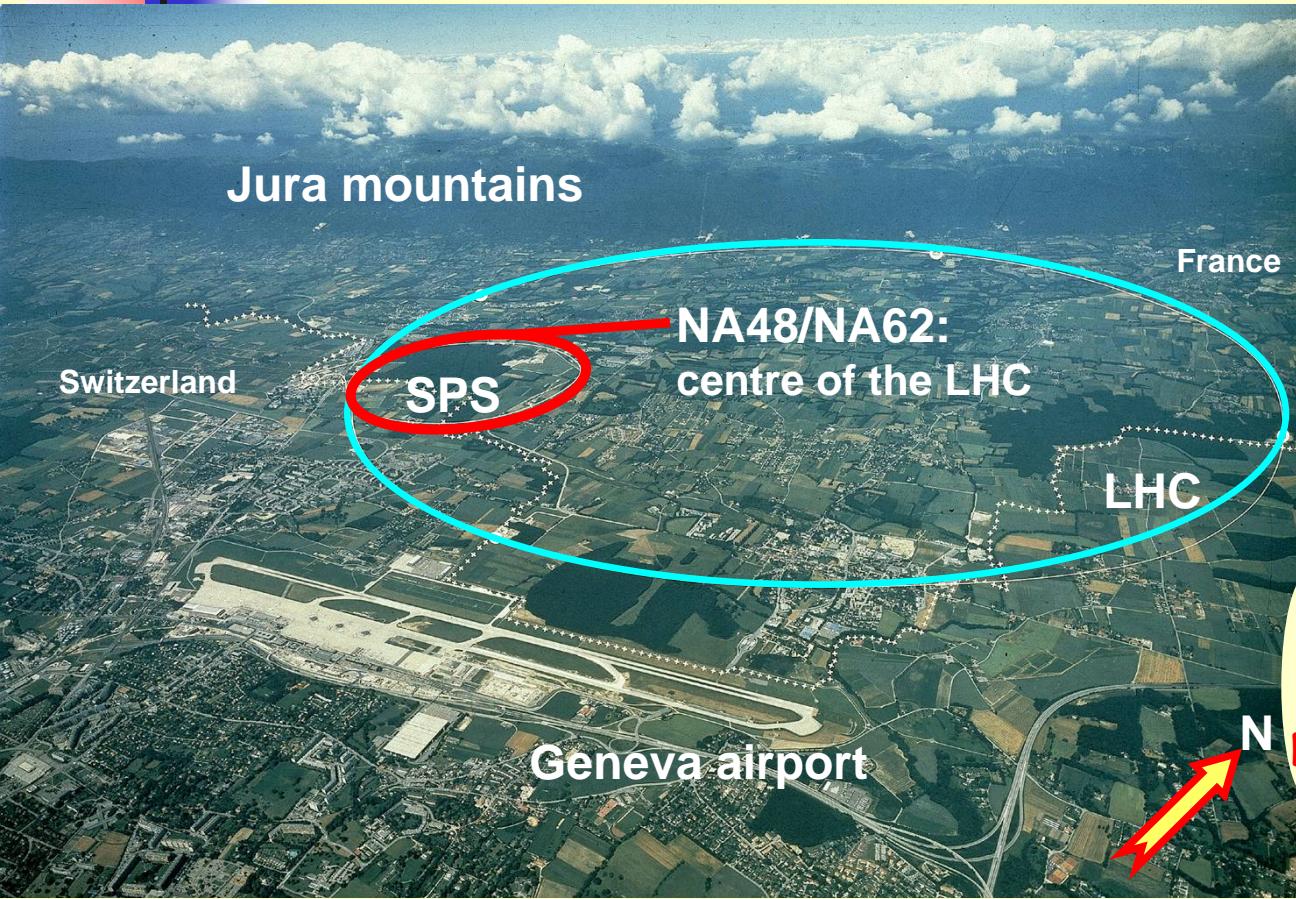
- 1) The NA48/NA62 experiments at CERN;
- 2) Lepton flavour universality test with  $K^+ \rightarrow e^+\nu / K^+ \rightarrow \mu^+\nu$  decays;
- 3) Search for the lepton number violating  $K^+ \rightarrow \pi^- \mu^+ \mu^+$  decay;
- 4) Conclusions.





# NA48/NA62 experiments at CERN

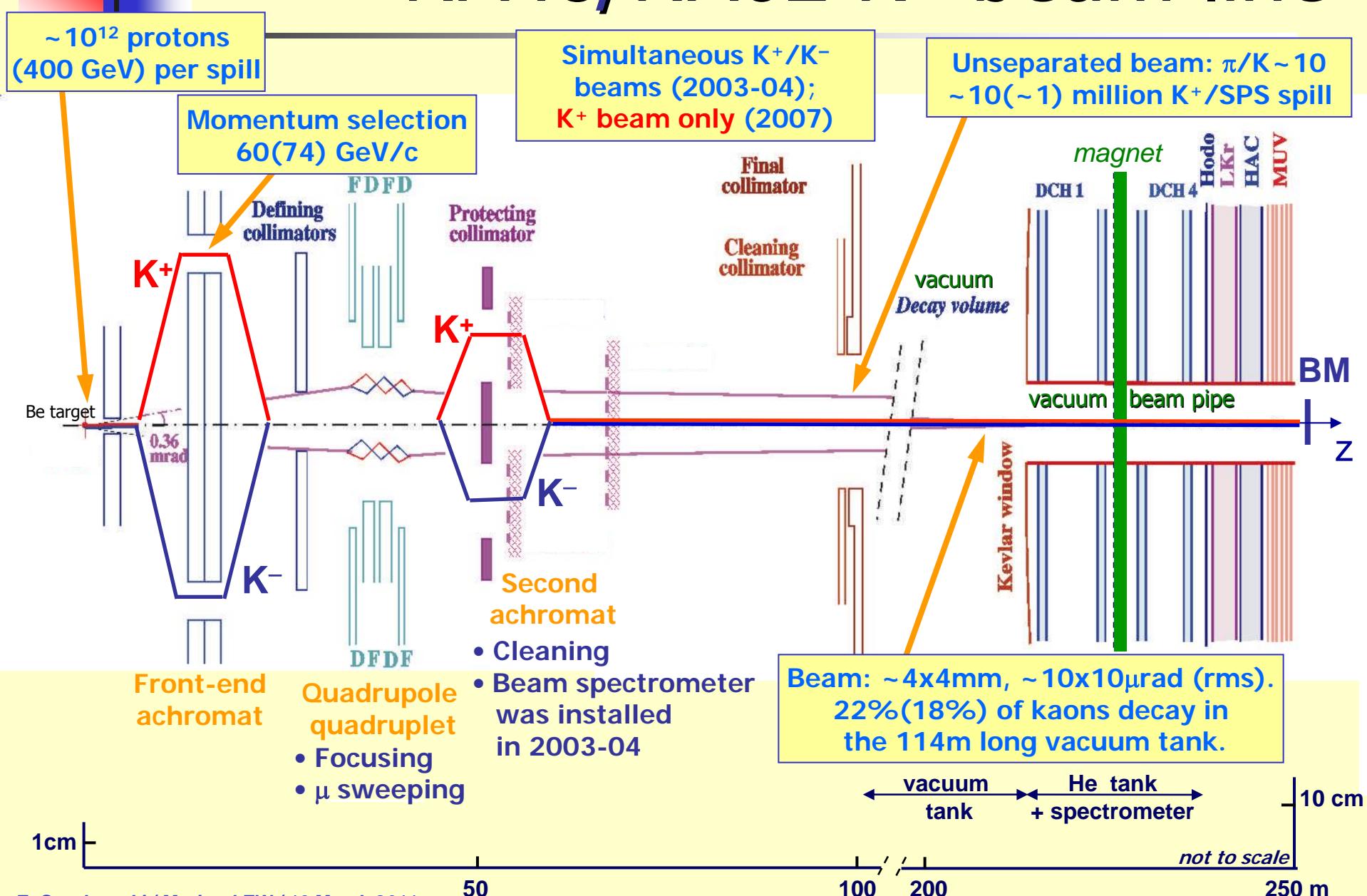
# CERN NA48/NA62 experiments



NA62: Birmingham, Bristol, CERN, Dubna, Fairfax, Ferrara, Florence, Frascati, Glasgow, IHEP Protvino, INR Moscow, Liverpool, Louvain-la-Neuve, Mainz, Merced, Naples, Perugia, Pisa, Rome I, Rome II, Saclay, San Luis Potosí, SLAC, Sofia, TRIUMF, Turin

Earlier: NA31	
1997: $\varepsilon'/\varepsilon: K_L + K_S$	
1998: $K_L + K_S$	
1999: $K_L + K_S$	$K_S$ HI
2000: $K_L$ only	$K_S$ HI
2001: $K_L + K_S$	$K_S$ HI
NA48	
discovery of direct CPV	
2002: $K_S$ /hyperons	
2003: $K^+ / K^-$	
2004: $K^+ / K^-$	
NA48/1	
NA48/2	
2007: $K^\pm_{e2} / K^\pm_{\mu 2}$	tests
2008: $K^\pm_{e2} / K^\pm_{\mu 2}$	tests
NA62 (phase I)	
NA62 (phase II)	
2007–2012:	design & construction
2013(?)–2016:	$K^+ \rightarrow \pi^+ v \bar{v}$ data taking

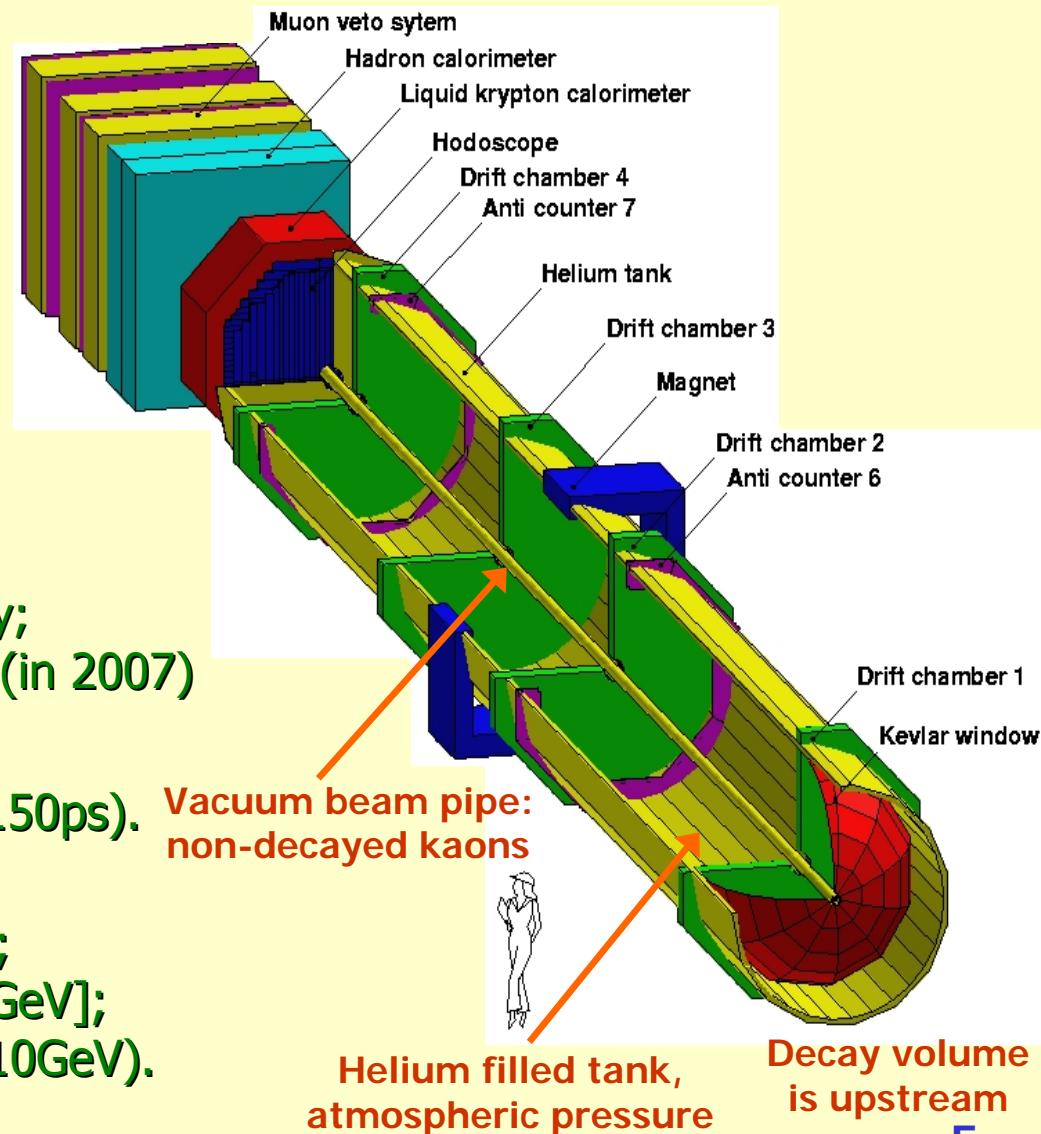
# NA48/NA62 K<sup>+</sup> beam line



# The detector

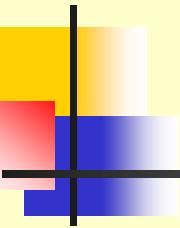
## Data taking

- NA48/2:  
~six months in 2003-04.
- NA62 (phase I):  
~four months in 2007.



## Principal subdetectors for $R_K$ :

- Magnetic spectrometer (4 DCHs):  
**4 views/DCH: redundancy  $\Rightarrow$  efficiency;**  
 $\Delta p/p = 0.47\% + 0.020\% \cdot p$  [GeV/c] (in 2007)
- Hodoscope  
**fast trigger, precise t measurement (150ps).**
- Liquid Krypton EM calorimeter (LKr)  
**High granularity, quasi-homogeneous;**  
 $\sigma_E/E = 3.2\%/E^{1/2} + 9\%/E + 0.42\%$  [GeV];  
 $\sigma_x = \sigma_y = 0.42/E^{1/2} + 0.6\text{mm}$  (1.5mm@10GeV).

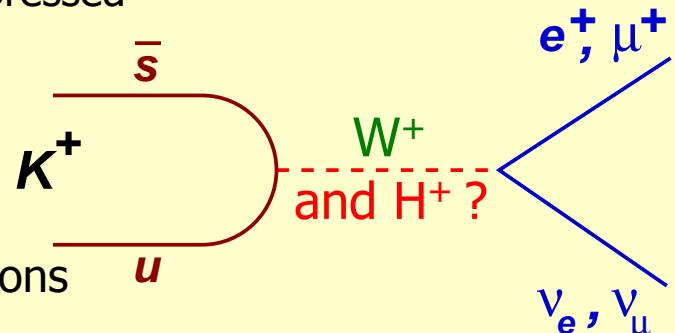


# Lepton flavour universality in $K^+ \rightarrow l^+ \nu$ decays

# Leptonic meson decays: $P^+ \rightarrow l^+ \nu$

Angular momentum conservation  $\rightarrow$  SM contribution is suppressed

$$\Gamma(P^+ \rightarrow l^+ \nu) = \frac{G_F^2 M_P M_l^2}{8\pi} \left(1 - \frac{M_l^2}{M_P^2}\right)^2 f_P^2 |V_{qq'}|^2$$



Models with 2 Higgs doublets (2HDM-II including SUSY):  
 sizeable tree level charged Higgs ( $H^\pm$ ) exchange contributions  
 PRD48 (1993) 2342; Prog.Theor.Phys. 111 (2004) 295

(numerical examples for  $M_H = 500 \text{ GeV}/c^2$ ,  $\tan\beta = 40$ )

$\pi^+ \rightarrow l\nu$ :	$\Delta\Gamma/\Gamma_{\text{SM}} \approx -2(m_\pi/m_H)^2 m_d/(m_u+m_d)$	$\tan^2\beta \approx -2 \times 10^{-4}$
$K^+ \rightarrow l\nu$ :	$\Delta\Gamma/\Gamma_{\text{SM}} \approx -2(m_K/m_H)^2 \tan^2\beta$	$\approx -0.3\%$
$D_s^+ \rightarrow l\nu$ :	$\Delta\Gamma/\Gamma_{\text{SM}} \approx -2(m_D/m_H)^2 (m_s/m_c) \tan^2\beta$	$\approx -0.4\%$
$B^+ \rightarrow l\nu$ :	$\Delta\Gamma/\Gamma_{\text{SM}} \approx -2(m_B/m_H)^2 \tan^2\beta$	$\approx -30\%$

$H^\pm$  exchange in  $B^+ \rightarrow \tau^+ \nu$  (R. Barlow, CKM 2010, arXiv:1102.1267)

BaBar+Belle:  $\text{Br}_{\text{exp}}(B \rightarrow \tau\nu) = (1.64 \pm 0.34) \times 10^{-4}$   
 (HFAG)

Standard Model:  $\text{Br}_{\text{SM}}(B \rightarrow \tau\nu) = (1.20 \pm 0.25) \times 10^{-4}$   
 ( $f_B$  from HPQCD,  $|V_{ub}|$  from HFAG)

$\sim 3\sigma$  discrepancy  
 between  $B_{\tau\nu}$  measurement  
 and expectation from  
 a global CKM fit  
 [UTfit, CKMfitter, ICHEP2010]

# $K_{\mu 2}$ : sensitivity to new physics

Comparison of  $|V_{us}|$  determined from helicity-suppressed  $K_{\mu 2}$  decays vs helicity-allowed  $K_{l3}$  decays

To reduce uncertainties of hadronic and EM corrections to  $K_{\mu 2}$ :

average from nuclear  $\beta$  decays,  
PRC79 (2009) 055502

$$R_{\mu 23} = \left( \frac{f_K/f_\pi}{f_+(0)} \right)^{-1} \left( \left| \frac{V_{us}}{V_{ud}} \right| \frac{f_K}{f_\pi} \right)_{\mu 2} \frac{\left| V_{ud} \right|_{0+ \rightarrow 0+}}{\left[ |V_{us}| f_+(0) \right]_{\ell 3}}$$

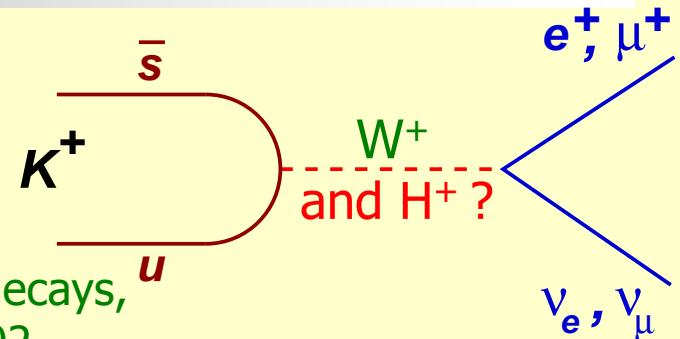
Lattice QCD input
Measured with  $K_{\mu 2}/\pi_{\mu 2}$ 
Measured with  $K \rightarrow \pi \mu \nu$

SM expectation:  $R_{\mu 23} = 1$ .

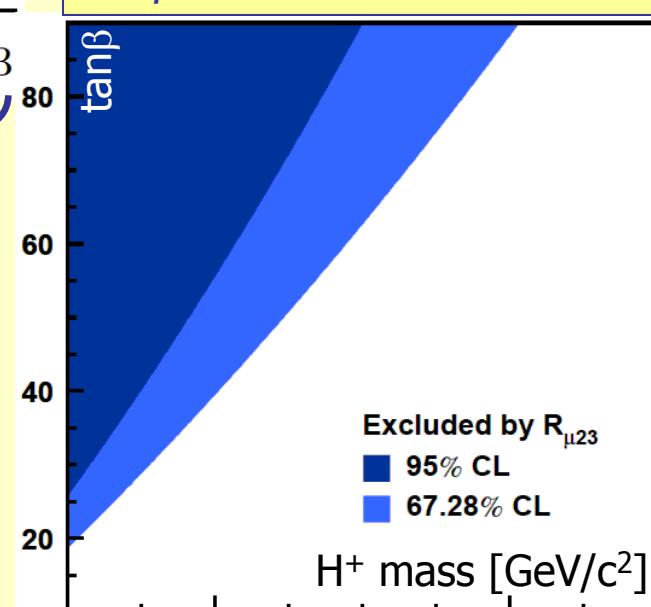
Charged Higgs mediated currents lead to

$$R_{\mu 23} \approx \left| 1 - \frac{m_{K^+}^2}{m_{H^+}^2} \frac{\tan^2 \beta}{1 + \epsilon_0 \tan \beta} \right|$$

Experiment:  $R_{\mu 23} = 0.999(7)$ , limited by lattice QCD input.



$\tan \beta$  vs  $H^+$  mass exclusion



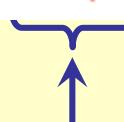
[Flavianet Kaon WG, EPJC69 (2010) 399]

# $R_K = K_{e2}/K_{\mu 2}$ in the SM

Observable sensitive to Lepton Flavour Violation:

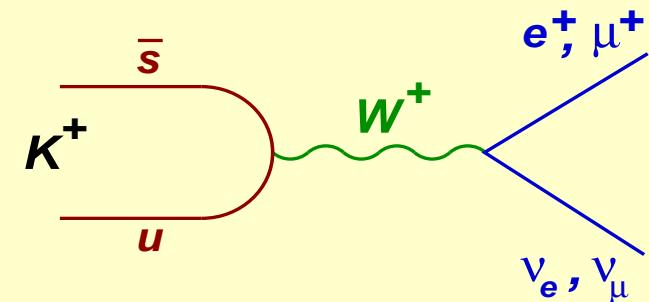
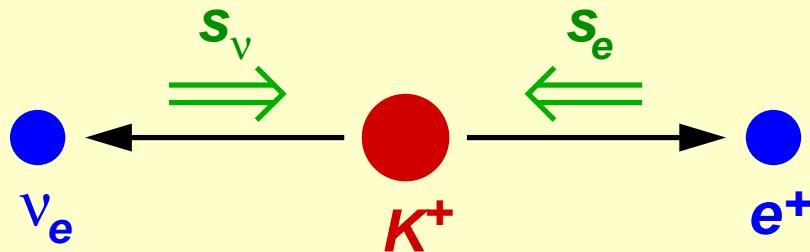
$$R_K = \frac{\Gamma(K^\pm \rightarrow e^\pm \nu)}{\Gamma(K^\pm \rightarrow \mu^\pm \nu)} = \frac{m_e^2}{m_\mu^2} \cdot \left( \frac{m_K^2 - m_e^2}{m_K^2 - m_\mu^2} \right)^2 \cdot (1 + \delta R_K^{\text{rad.corr.}})$$

(similarly,  $R_\pi$  in the pion sector)



Helicity suppression:  $f \sim 10^{-5}$

Radiative correction (few %)  
due to  $K^+ \rightarrow e^+ \nu \gamma$  (IB) process,  
by definition included into  $R_K$



- SM prediction: excellent sub-permille accuracy:  
not obstructed by hadronic uncertainties.
- Measurements of  $R_K$  and  $R_\pi$  have long been considered as tests of lepton universality.
- Understood recently: helicity suppression of  $R_K$  might enhance sensitivity to non-SM effects to an experimentally accessible level.

$$R_K^{\text{SM}} = (2.477 \pm 0.001) \times 10^{-5}$$

$$R_\pi^{\text{SM}} = (12.352 \pm 0.001) \times 10^{-5}$$

Phys. Lett. 99 (2007) 231801

# $R_K = K_{e2}/K_{\mu 2}$ beyond the SM

## 2HDM – tree level

(including SUSY)

$K_{l2}$  can proceed via exchange of charged Higgs  $H^\pm$  instead of  $W^\pm$   
 $\rightarrow$  Does not affect the ratio  $R_K$

## 2HDM – one-loop level

Dominant contribution to  $R_K$ :  $H^\pm$  mediated LFV (rather than LFC) with emission of  $v_\tau$   
 $\rightarrow R_K$  enhancement can be experimentally accessible

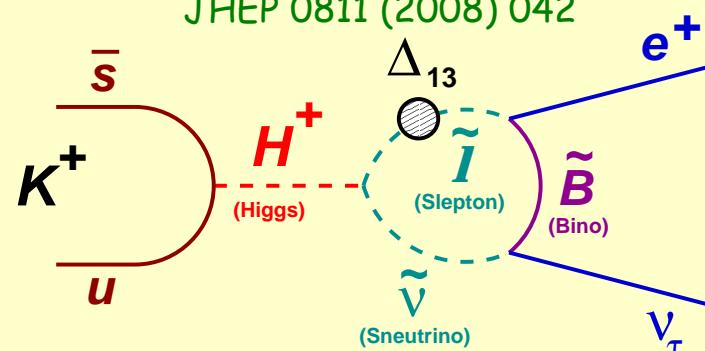
$$R_K^{\text{LFV}} \approx R_K^{\text{SM}} \left[ 1 + \left( \frac{m_K^4}{M_{H^\pm}^4} \right) \left( \frac{m_\tau^2}{M_e^2} \right) |\Delta_{13}|^2 \tan^6 \beta \right]$$

Up to  $\sim 1\%$  effect in large (but not extreme)  $\tan\beta$  regime with a massive  $H^\pm$

### Example:

$(\Delta_{13}=5\times 10^{-4}, \tan\beta=40, M_H=500 \text{ GeV}/c^2)$   
lead to  $R_K^{\text{MSSM}} = R_K^{\text{SM}}(1+0.013)$ .

PRD 74 (2006) 011701,  
JHEP 0811 (2008) 042



Analogous SUSY effect  
in pion decay is suppressed  
by a factor  $(M_\pi/M_K)^4 \approx 6 \times 10^{-3}$

Large effects in B decays  
due to  $(M_B/M_K)^4 \sim 10^4$ :

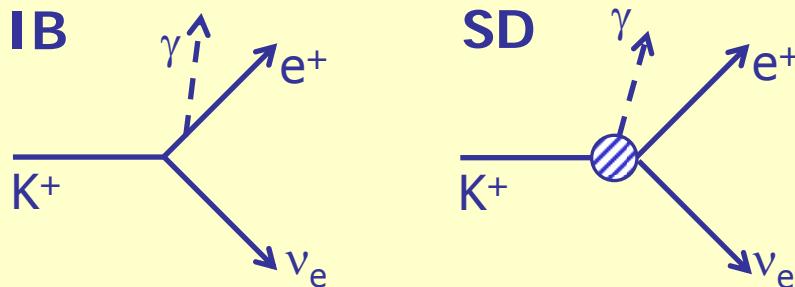
$B_{\mu\nu}/B_{\tau\nu} \rightarrow \sim 50\%$  enhancement;

$B_{ev}/B_{\tau\nu} \rightarrow$  enhanced by  
 $\sim$ one order of magnitude.

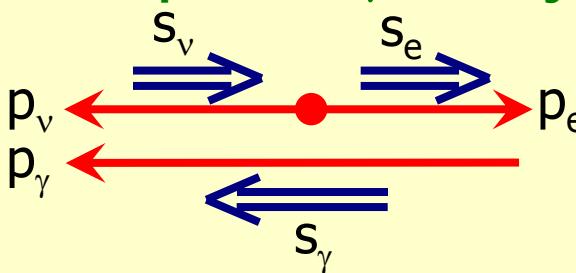
Out of reach:  $\text{Br}^{\text{SM}}(B_{ev}) \approx 10^{-11}$

# Radiative $K^+ \rightarrow e^+ \nu \gamma$ process

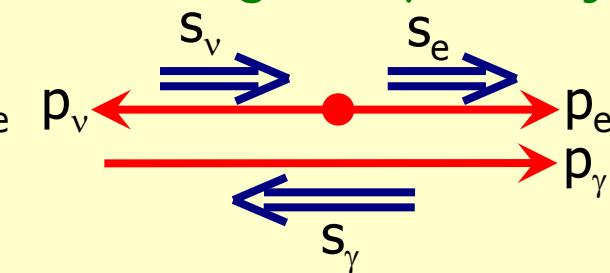
$R_K$  is inclusive of IB radiation by definition.  
SD radiation is a background. INT is negligible.



**SD<sup>+</sup>: positive  $\gamma$  helicity**



**SD<sup>-</sup>: negative  $\gamma$  helicity**

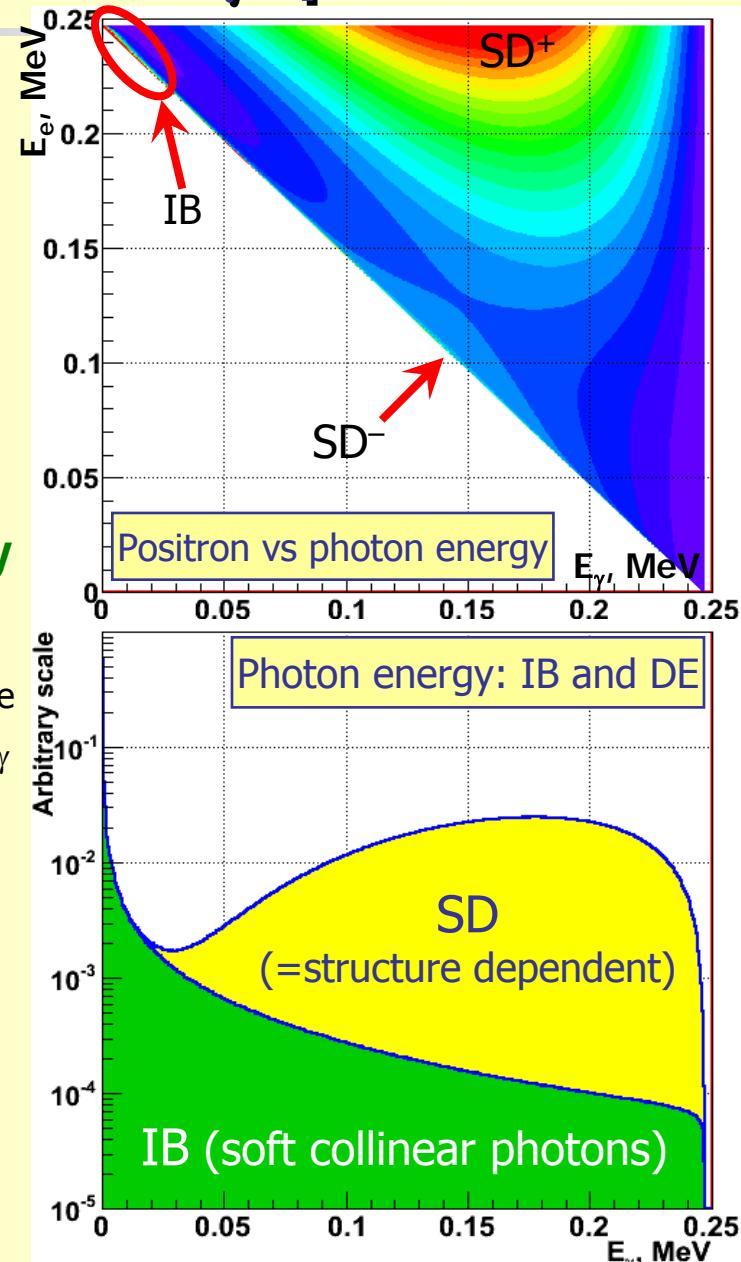


SD radiation is not helicity suppressed.

KLOE measurement of the form factor leads to  
 $BR(SD^+, \text{full phase space}) = (1.37 \pm 0.06) \times 10^{-5}$ .

(EPJC64 (2009) 627)

$B/(S+B) = (1.07 \pm 0.05)\%$



# K<sub>e2</sub> vs K<sub>μ2</sub> selection

## Large common part (topological similarity)

- one reconstructed track (lepton candidate);
- geometrical acceptance cuts;
- K decay vertex: closest approach of lepton track & nominal kaon axis;
- veto extra LKr energy deposition clusters;
- track momentum: 13GeV/c < p < 65GeV/c.

## Kinematic identification

missing mass

$$M_{miss}^2 = (P_K - P_l)^2$$

$P_K$  : average measured with K<sub>3π</sub> decays

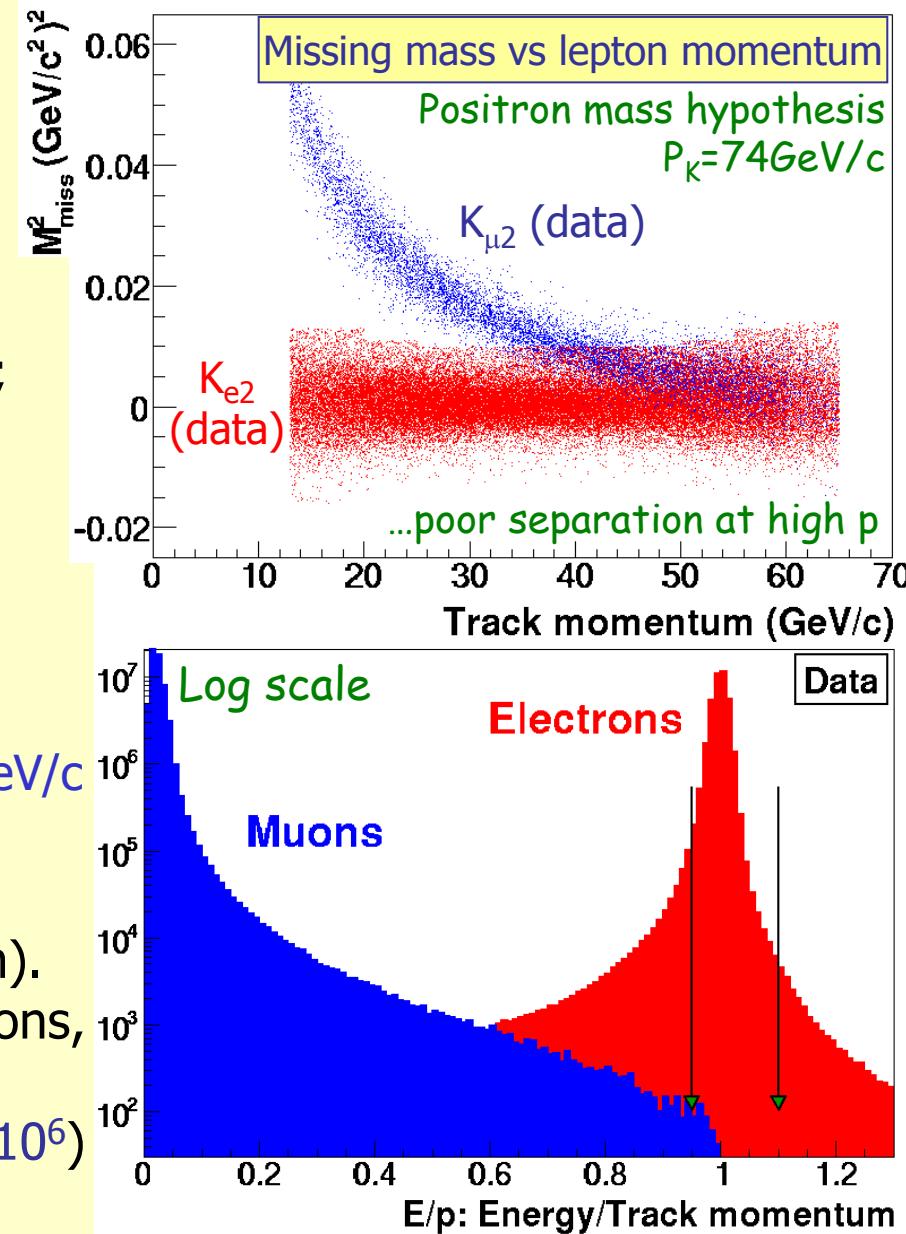
→ Sufficient K<sub>e2</sub>/K<sub>μ2</sub> separation at p<sub>track</sub> < 30GeV/c

## Lepton identification

E/p = (LKr energy deposit/track momentum).

(0.90 to 0.95) < E/p < 1.10 for electrons,  
E/p < 0.85 for muons.

→ Powerful μ<sup>±</sup> suppression in e<sup>±</sup> sample ( $\sim 10^6$ )

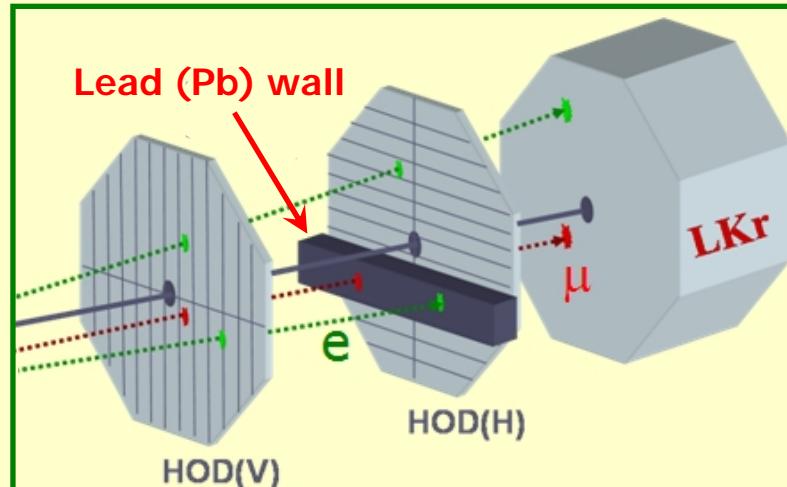


# $K_{\mu 2}$ background in $K_{e 2}$ sample

## Main background source

Muon 'catastrophic' energy loss in LKr by emission of energetic bremsstrahlung photons.  
 $P_{\mu e} \sim 3 \times 10^{-6}$  (and momentum-dependent).

$P_{\mu e} / R_K \sim 10\%$ :  
 $K_{\mu 2}$  decays represent a major background



<u>Thickness:</u>	$9.2X_0$ (Pb+Fe)
<u>Width:</u>	240cm (=HOD size)
<u>Height:</u>	18cm (=3 counters)
<u>Area:</u>	~20% of HOD area
<u>Duration:</u>	~50% of $R_K$ runs

## Direct measurement of $P_{\mu e}$

Pb wall ( $9.2X_0$ ) in front of LKr: suppression of  $\sim 10^{-4}$  positron contamination due to  $\mu \rightarrow e$  decay.

$K_{\mu 2}$  candidates, track traversing Pb,  $p > 30\text{GeV}/c$ ,  $E/p > 0.95$ : positron contamination  $< 10^{-8}$ .

$P_{\mu e}$  is modified by the Pb wall:

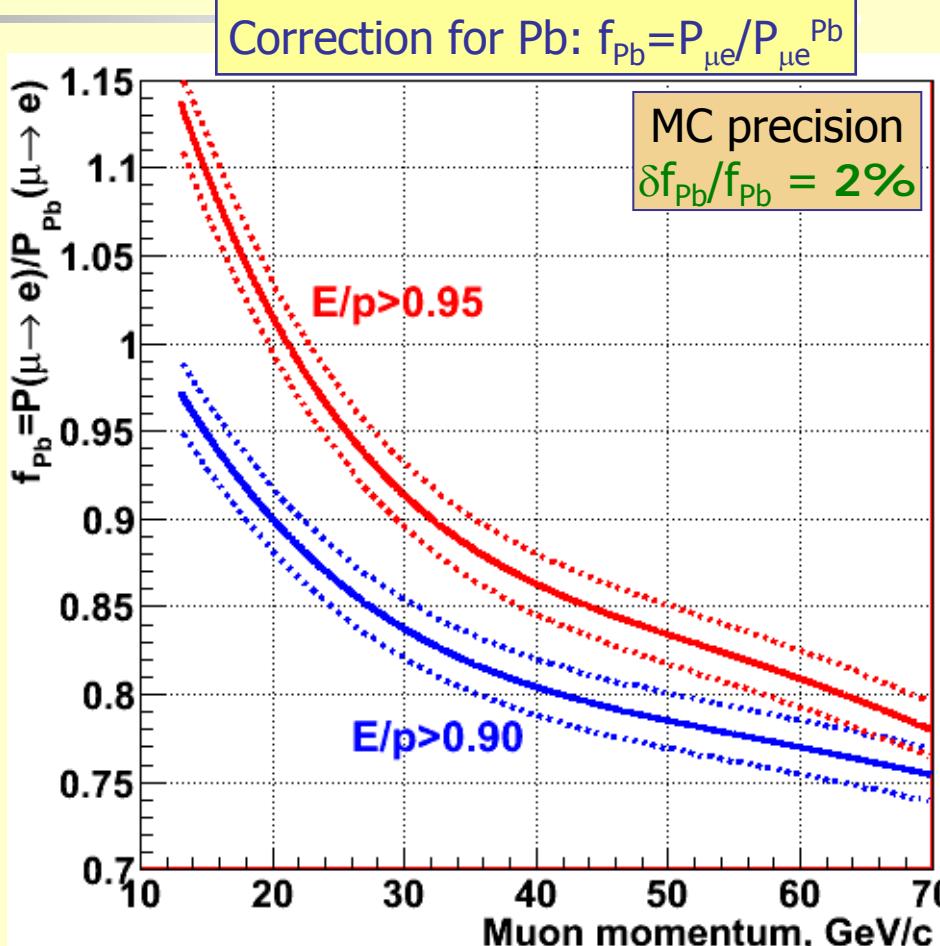
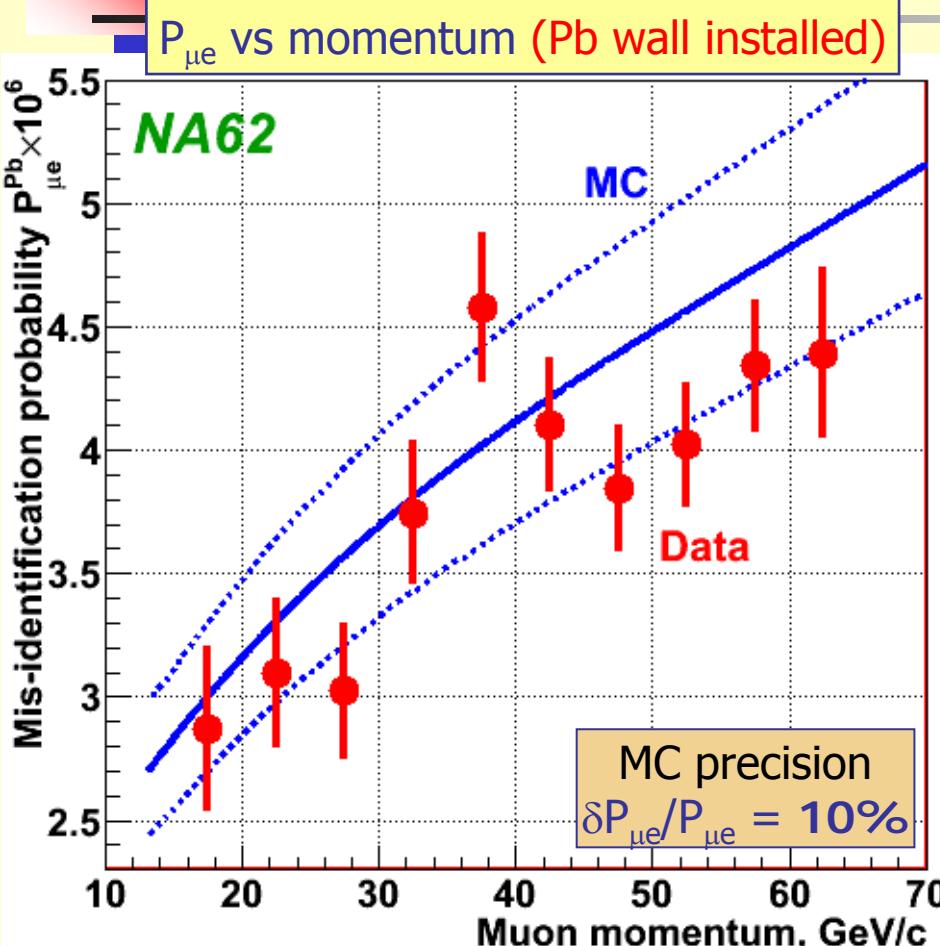
- ionization losses in Pb (low p);
- bremsstrahlung in Pb (high p).



The correction  $f_{\text{Pb}} = P_{\mu e} / P_{\mu e}^{\text{Pb}}$  is evaluated with a dedicated Geant4-based simulation

[Muon bremsstrahlung model:  
 Kelner et al., Phys. Atom. Nucl. 60(1997)576] 13

# Muon mis-identification



Result:  $B/(S+B) = (6.11 \pm 0.22)\%$

Uncertainty is  $\sim 3$  times smaller than the one obtained solely from simulation

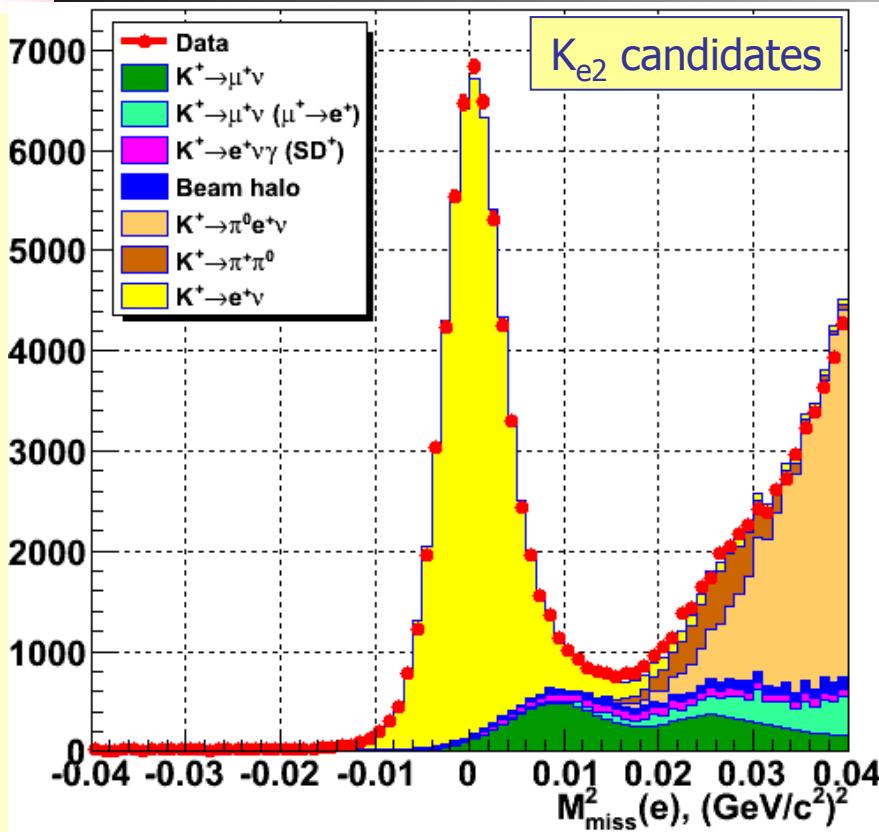
## Uncertainties:

limited control data sample (0.16%),  
 MC correction  $\delta f_{\text{Pb}}$  (0.12%),  
 $M_{\text{miss}}^2$  vs  $P_{\text{track}}$  correlation (0.08%).

## Stability checks:

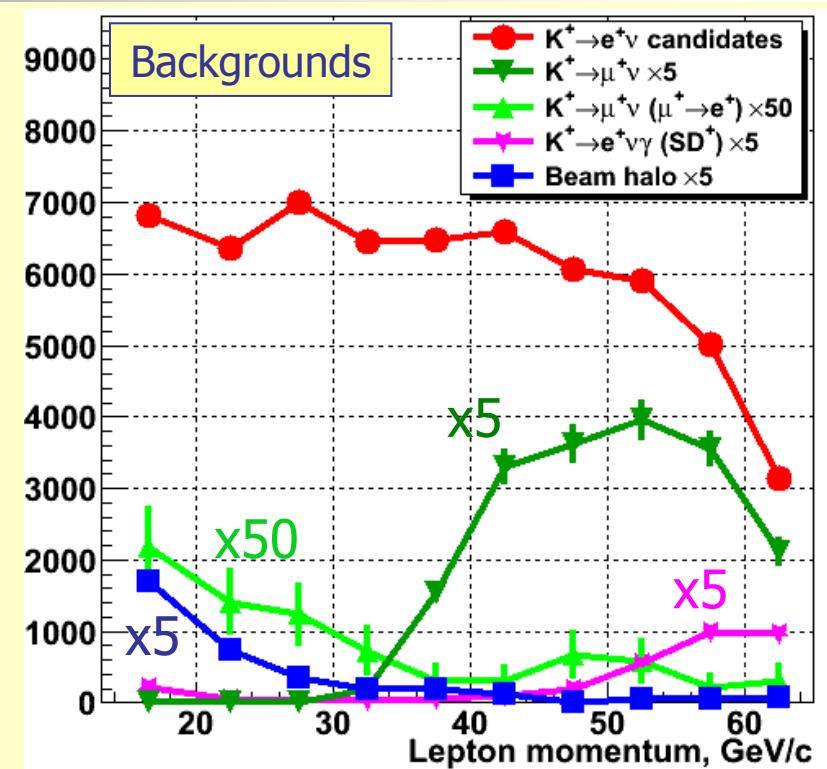
vs lower  $E/p$  cut, upper HOD energy deposit.

# K<sub>e2</sub>: partial (40%) data set



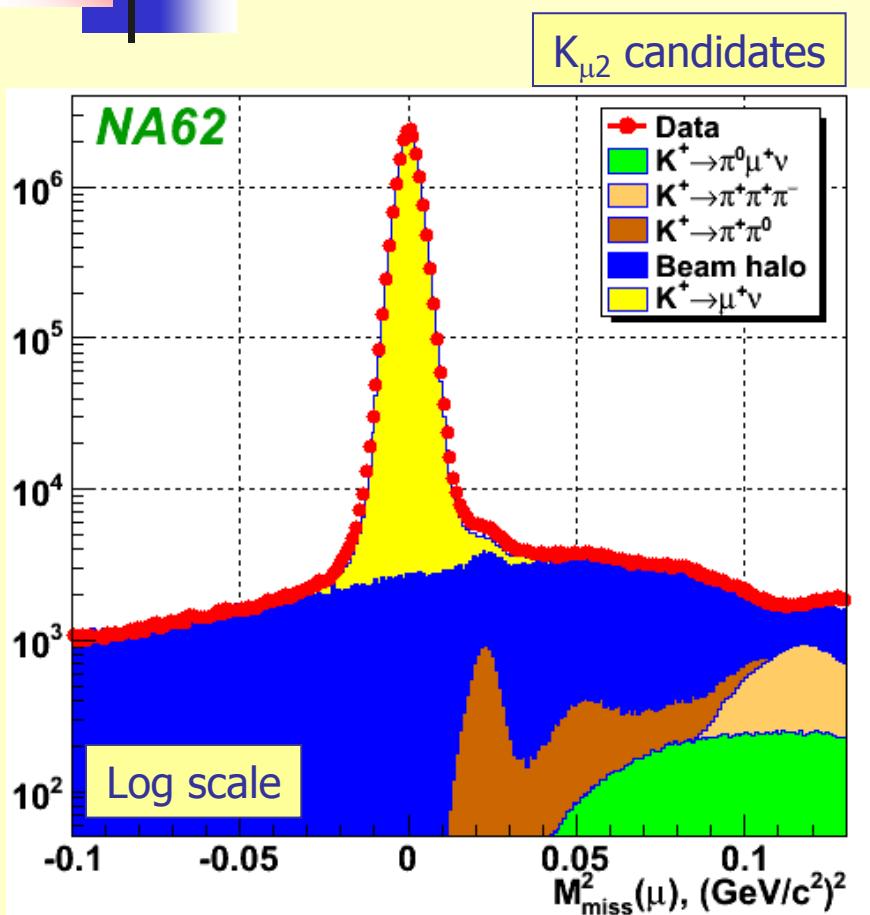
59,813  $K^+ \rightarrow e^+ \nu$  candidates.  
 Positron ID efficiency:  $(99.27 \pm 0.05)\%$ .  
 $B/(S+B) = (8.71 \pm 0.24)\%$ .

cf. KLOE: 13.8K candidates ( $K^+$  and  $K^-$ ),  
 ~90% electron ID efficiency, 16% background

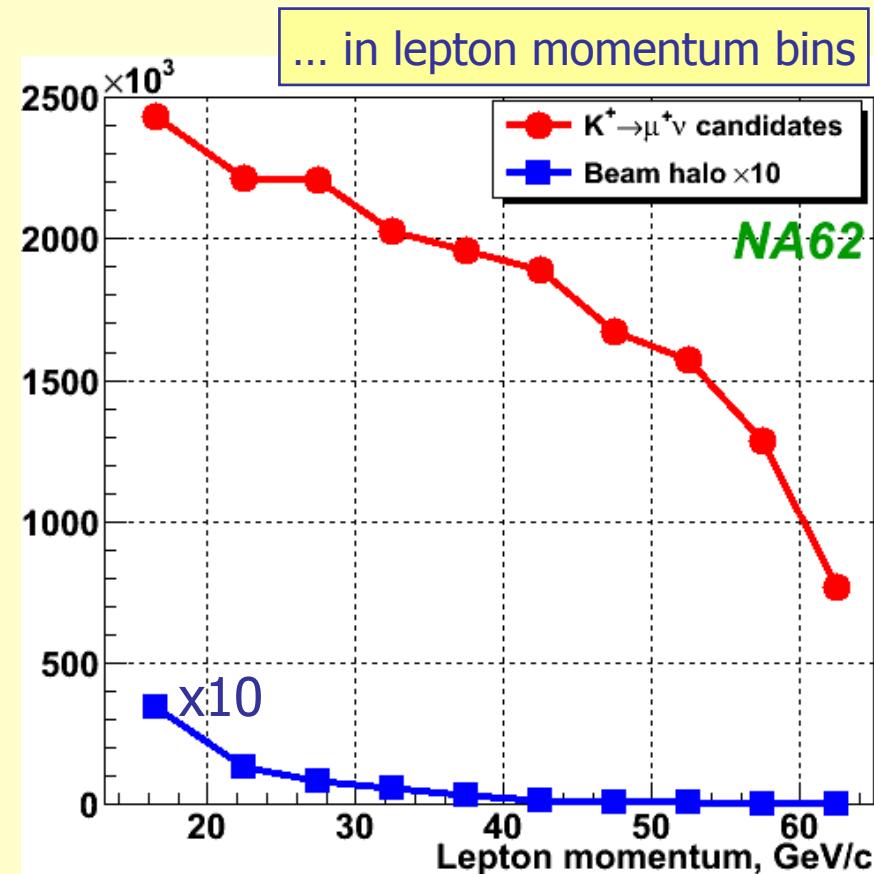


Source	$B/(S+B)$
$K_{\mu 2}$	$(6.11 \pm 0.22)\%$
$K_{\mu 2} (\mu \rightarrow e)$	$(0.27 \pm 0.04)\%$
$K_{e2\gamma} (SD^+)$	$(1.07 \pm 0.05)\%$
$K_{e3(D)}$	$(0.05 \pm 0.03)\%$
$K_{2\pi(D)}$	$(0.05 \pm 0.03)\%$
Beam halo	$(1.16 \pm 0.06)\%$
Total	$(8.71 \pm 0.24)\%$

# $K_{\mu 2}$ : partial (40%) data set



18.03M candidates (pre-scaled trigger).  
 $B/(S+B) = (0.38 \pm 0.01)\%$ ,  
background dominated by beam halo.



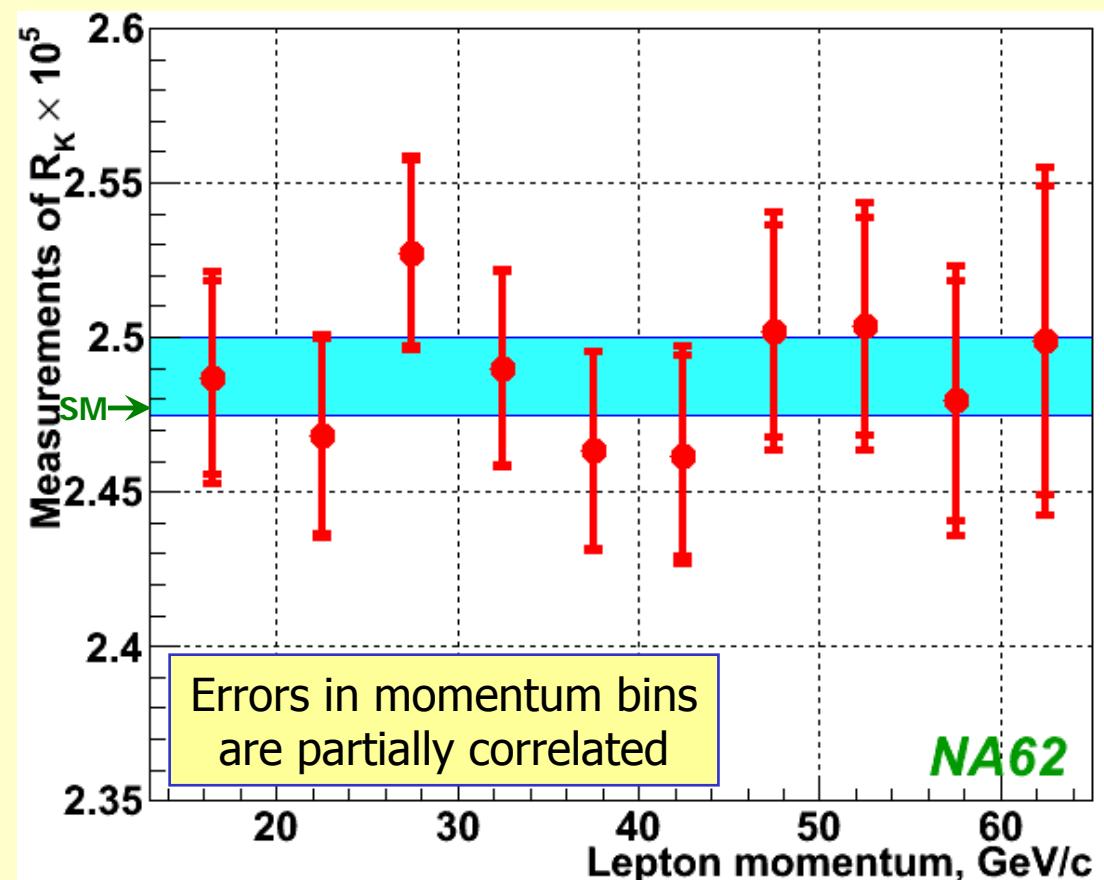
Sensitivity to heavy neutrinos ( $K^+ \rightarrow \mu^+ N$ ) is limited by beam halo and similar to that of  
Hayano et al., PLB49 (1982) 1305

# NA62 final result (40% data set)

$$R_K = (2.487 \pm 0.011_{\text{stat}} \pm 0.007_{\text{syst}}) \times 10^{-5}$$

$$= (2.487 \pm 0.013) \times 10^{-5}$$

CERN-PH-EP-2011-004,  
arXiv:1101.4805,  
accepted by PLB

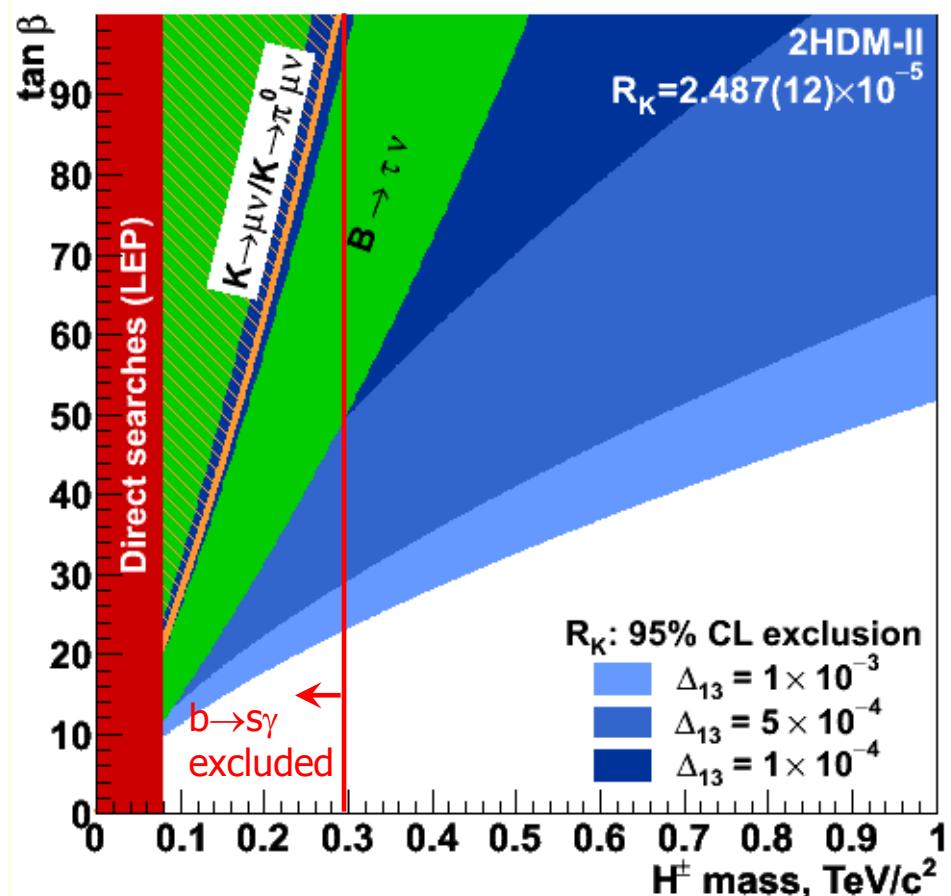
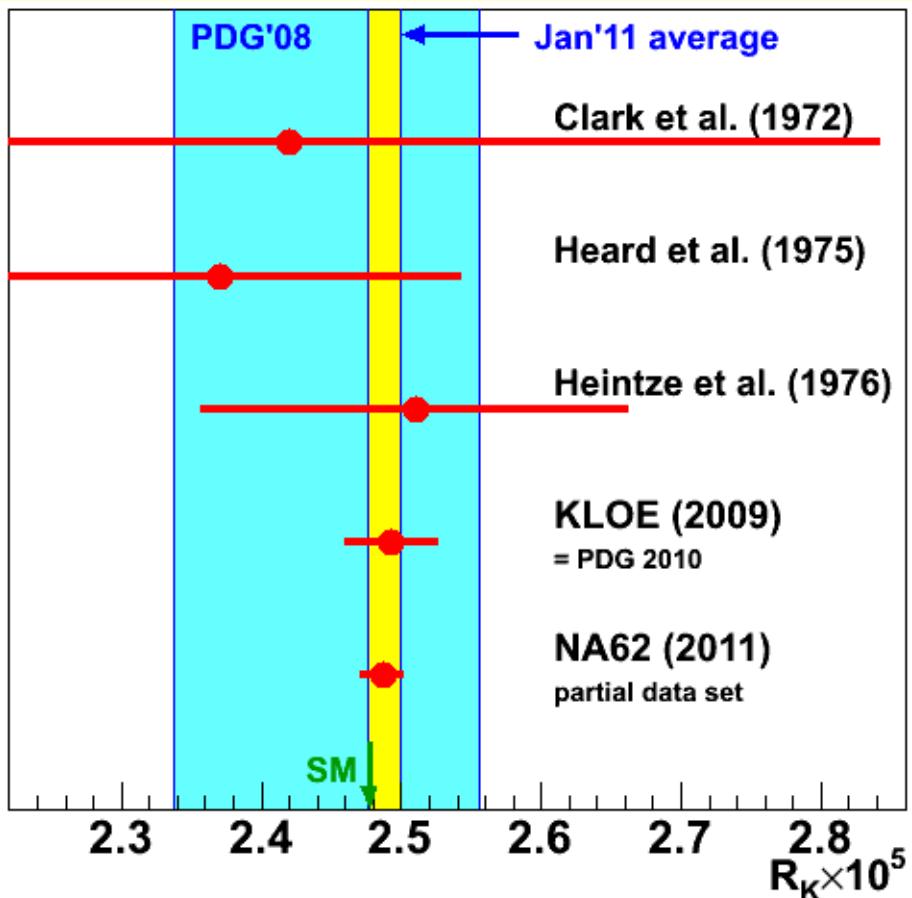


## Uncertainties

Source	$\delta R_K \times 10^5$
Statistical	0.011
$K_{\mu 2}$	0.005
$K \rightarrow e^+ \nu \gamma$ (SD <sup>+</sup> )	0.001
$K^+ \rightarrow \pi^0 e^+ \nu$ , $K^+ \rightarrow \pi^+ \pi^0$	0.001
Beam halo	0.001
Helium purity	0.003
Acceptance correction	0.002
Spectrometer alignment	0.001
Positron ID efficiency	0.001
1TRK trigger efficiency	0.002
LKr readout efficiency	0.001
Total	0.013

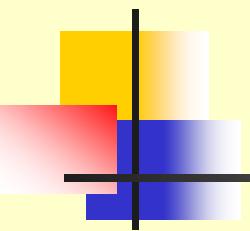
Full NA62 data set: precision will be improved from 0.5% to 0.4%.

# $R_K$ world average



World average	$\delta R_K \times 10^5$	Precision
PDG 2008	$2.447 \pm 0.109$	4.5%
Today	$2.487 \pm 0.012$	0.5%

Other limits on 2HDM-II:  
 PRD 82 (2010) 073012.  
 SM with 4 generations:  
 JHEP 1007 (2010) 006.

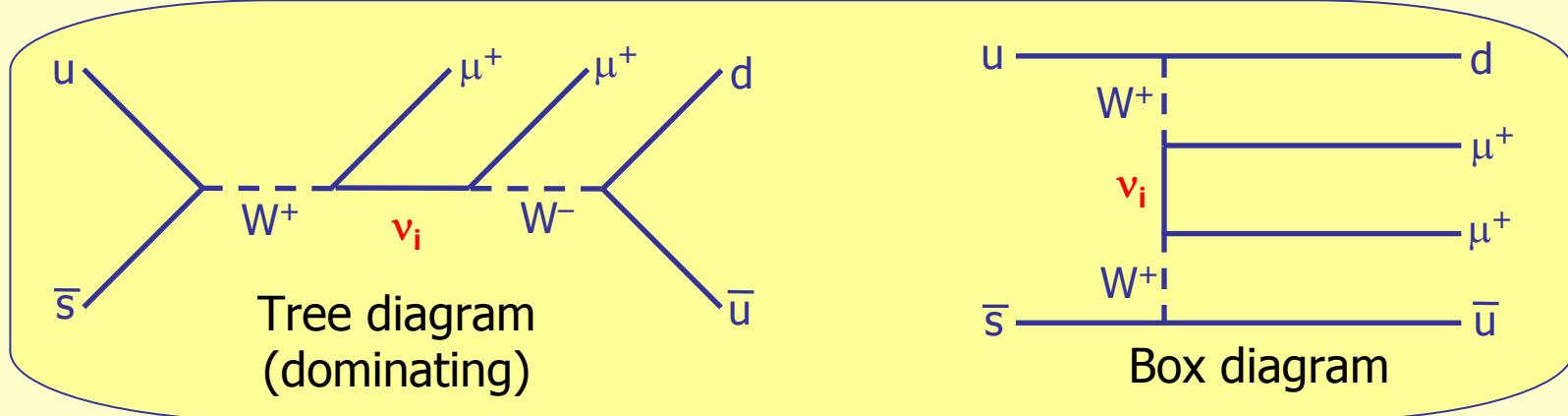


# Lepton number violation:

$$K^+ \rightarrow \pi^- \mu^+ \mu^+, \quad K^- \rightarrow \pi^+ \mu^- \mu^-$$

# Motivation

$K^+ \rightarrow \pi^- \mu^+ \mu^+$  proceeds if the neutrino is a Majorana particle:



$$BR \approx 10^{-8} \times (\langle m_{\mu\mu} \rangle / \text{TeV})^2$$

[K. Zuber, PLB 479 (2000) 33;  
L. Littenberg, R. Shrock,  
PRB491 (2000) 285]

Analogously, neutrinoless double beta decay rate is  $\sim \langle m_{ee} \rangle^2$ .

$\langle m_{ll} \rangle = |\sum m_i U_{li}^2|$  is the effective Majorana neutrino mass

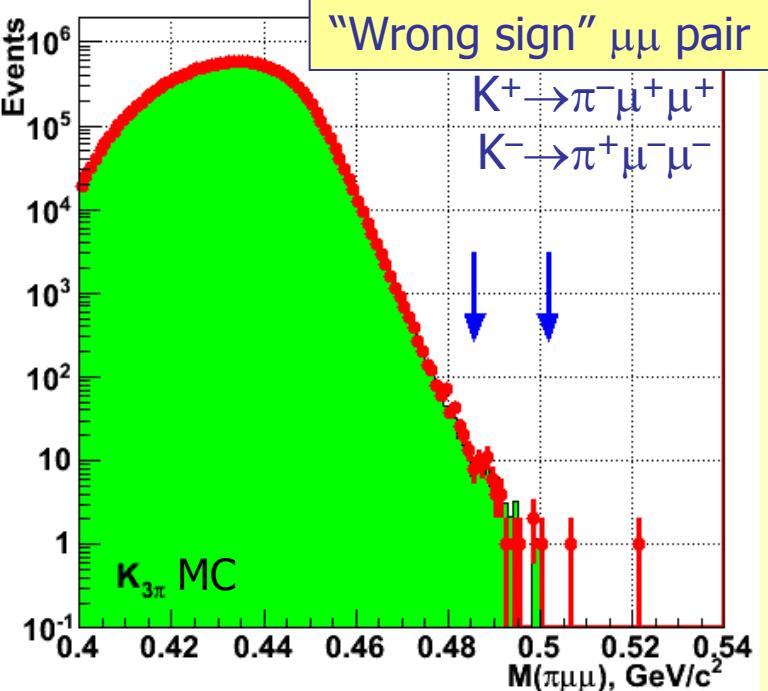
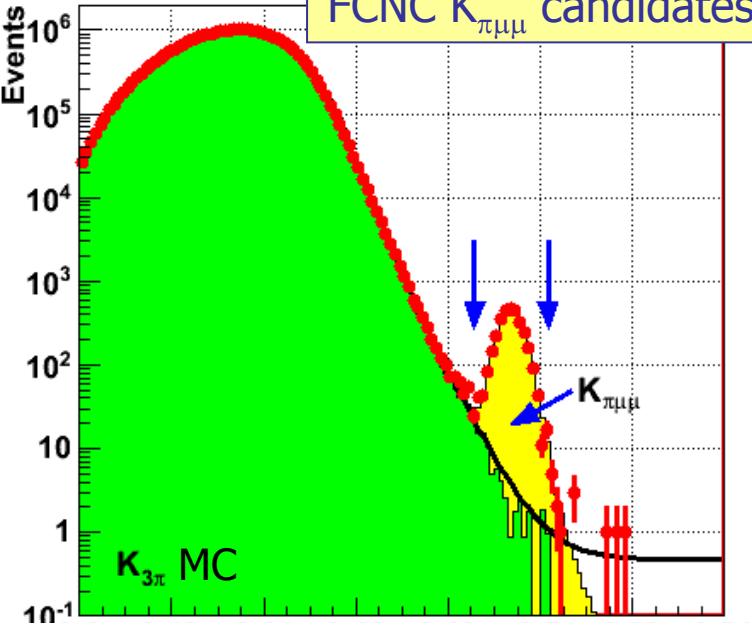
Best upper limits on LFV/LNV decays  $K_{\pi ee}$ ,  $K_{\pi \mu \mu}$ ,  $K_{\pi \mu e}$  come from BNL E865.

The E865  $K_{\pi \mu \mu}$  limit, based on a (short) special run, is the weakest:  $BR < 3 \times 10^{-9}$ .

→ NA48 is competitive for  $K_{\pi \mu \mu}$  mode:  
 $\sim 8$  times larger data sample ( $K^\pm$ ).

# NA48 results

PLB 697 (2011) 107



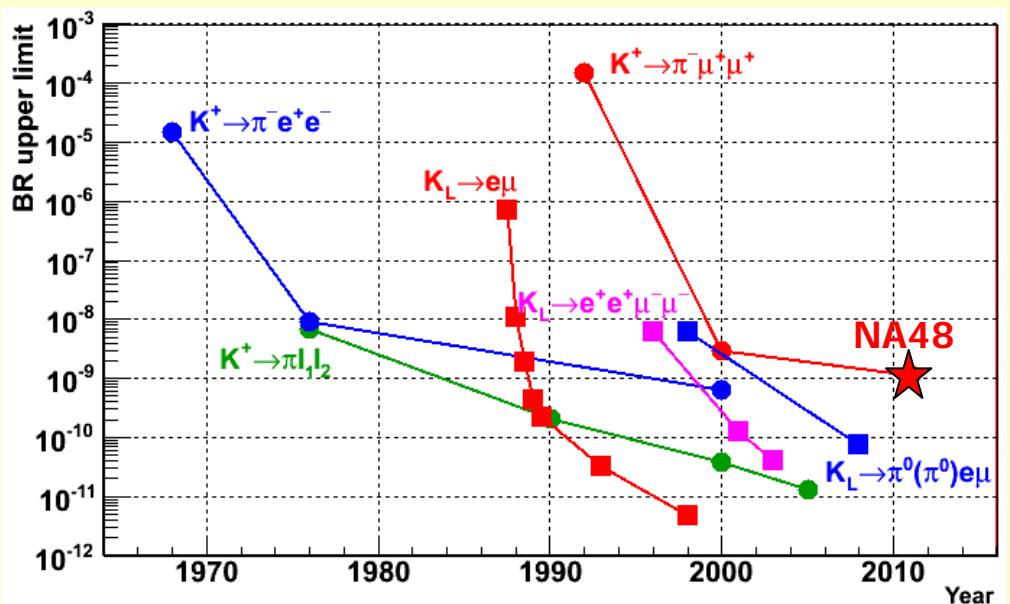
$K^\pm \rightarrow \pi^\pm \mu^+ \mu^-$  analysis: 3,120 candidates  
 (~4 times world sample),  
 $(3.3 \pm 0.7)\%$  background.  
 BR, CPV and FB asymmetries measured.

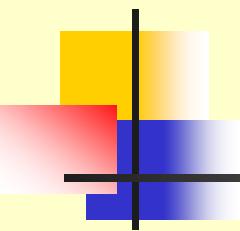
Lepton number violating decay:

$$N_{\text{data}} = 52 \quad \Rightarrow \quad \text{BR} < 1.1 \times 10^{-9} \text{ (90\% CL)}$$

$$N_{\text{bkg}} = 52.6 \pm 19.8_{\text{syst.}}$$

A factor of 3 improvement on the upper limit for  $\text{BR}(K^+ \rightarrow \pi^- \mu^+ \mu^+)$ .





# Summary

- Combined experimental precision on  $R_K = BR(K_{e2})/BR(K_{\mu 2})$  has improved by an order of magnitude over the last 3 years, but is still an order of magnitude behind that of the SM prediction.
- $R_K$  experiment and SM currently agree at  $0.8\sigma$  level.
- Short (**medium**) term plans at NA62: improvement of the experimental uncertainty on  $R_K$  to 0.4% (**0.2%**) exploiting the decay-in-flight technique.
- Upper limit on LNV  $BR(K^+ \rightarrow \pi^- \mu^+ \mu^+)$  improved by a factor of 3:  $BR < 1.1 \times 10^{-9} \rightarrow \langle m_{\mu\mu} \rangle < 300$  GeV at 90% CL.

Other recent CERN NA48/NA62 results:  
S.Balev @ La Thuile 2011; B.Bloch-Devaux @ Moriond QCD 2011