

Boosted Massive Jets @ the LHC

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L. Almeida, SL, G. Perez, G. Sterman, I. Sung, & J. Virzi

PRD 79, 074017 (2009);

L. Almeida, SL, G. Perez, I. Sung, & J. Virzi

PRD 79, 074012 (2009);

L. Almeida, SL, G. Perez, G. Sterman, & I. Sung

PRD 82, 054034 (2010)

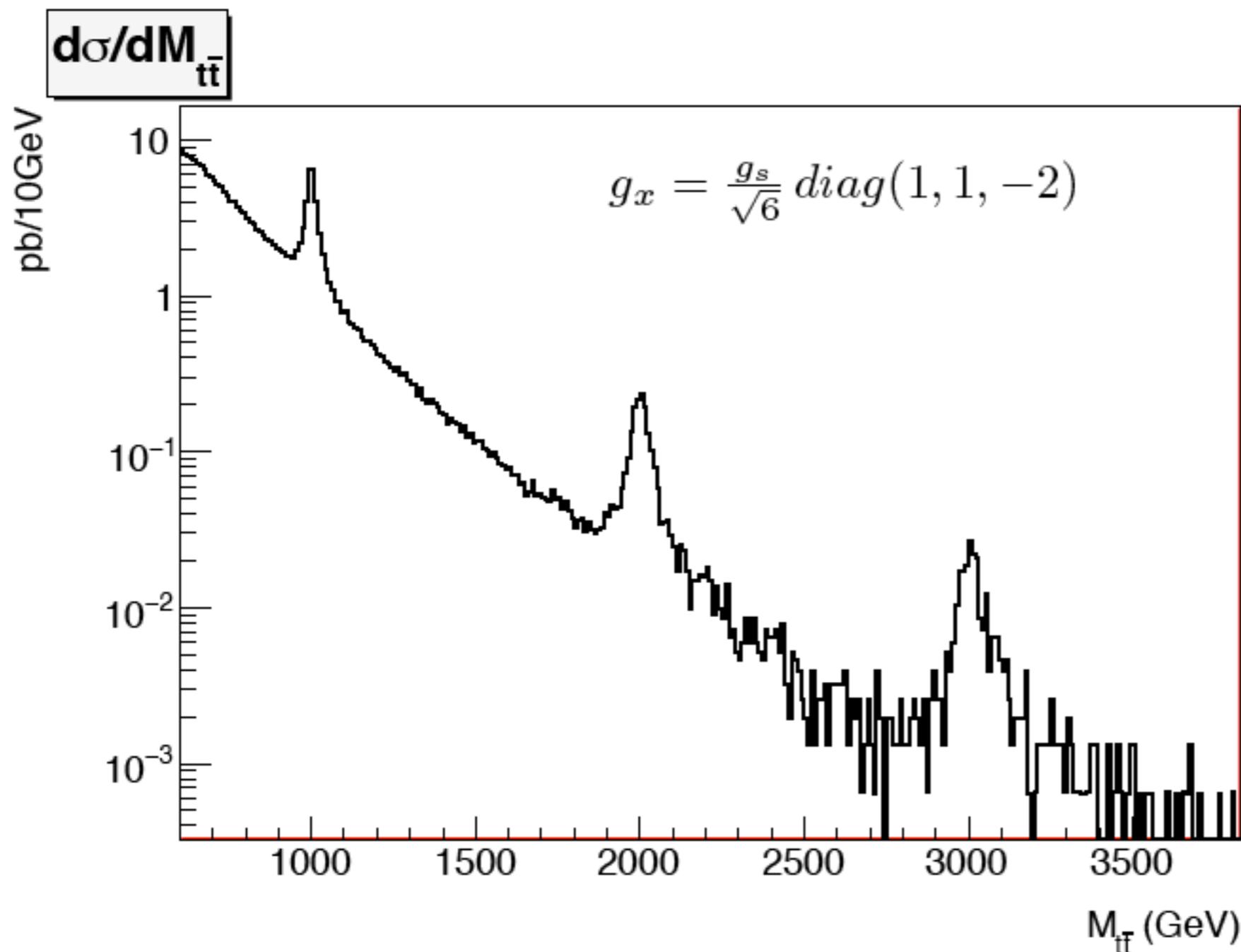
IPNL, Lyon, December 15, 2010

Outline

- ◆ Intro: emergence of massive jets @ LHC & the nature of the problem (finite resolution)
- ◆ Theory of massive jets:
 - jet mass
 - substructure: angularities, planar flow
- ◆ Template Overlap Method
- ◆ Summary

High P_T tops (or massive jets), might be crucial signal for various NP models

Z' : Butterworth, Cox & Forshaw; KK gluon: Agashe, Belyaev, Krupovnickas, GP & Virzi (06); Lillie, Randall & Wang (07); KK graviton: Fitzpatrick, Kaplan, Randall & Wang (07); Agashe, Davoudiasl, GP & Soni (07).



C. Csaki, SL, G. Perez, & A. Weiler (Flavor gauge bosons: to appear)

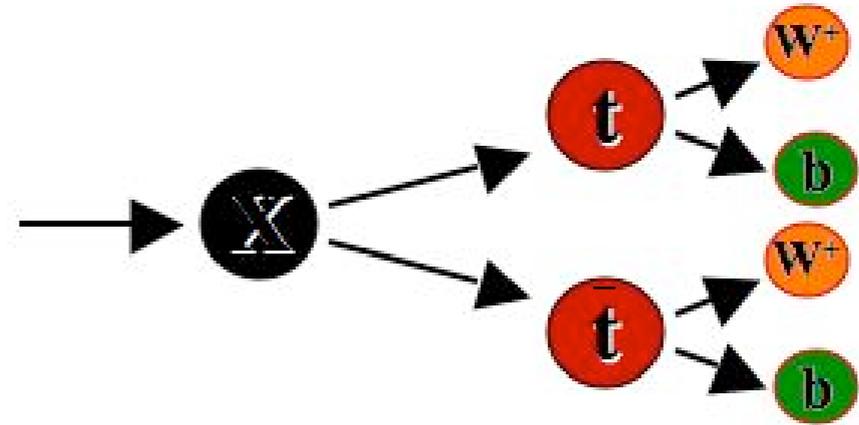
C. Delaunay, SL, & G. Perez (Extraordinary Phenomenology from Flavor Triviality: to appear)

The challenge of highly boosted Massive Jets

◆ High PT massive jets such as tops, might be crucial signal for various NP models ($X \rightarrow t\bar{t} + Y$):

e.g. KK states decaying into top pair

$$m_{KK} \gtrsim 1 \text{ TeV}$$

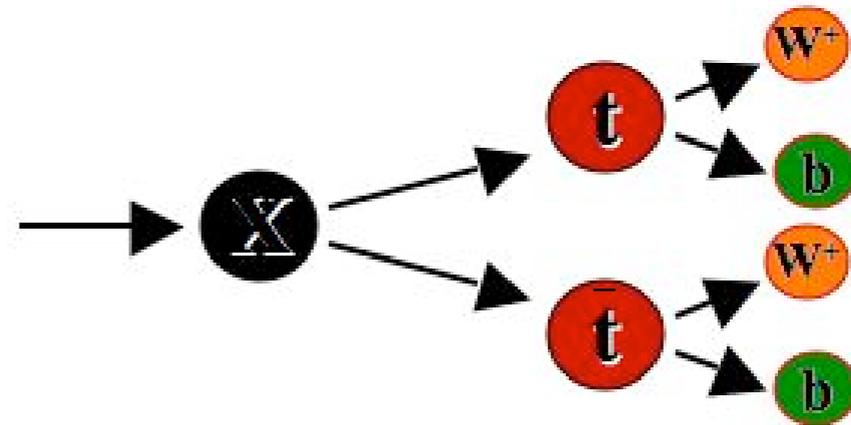


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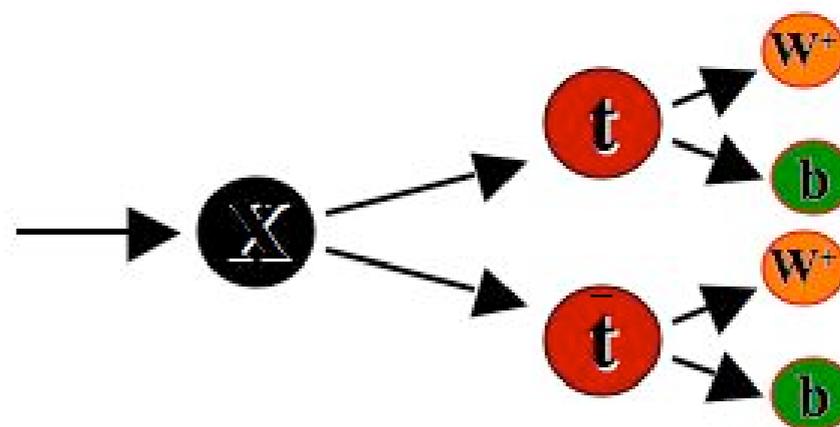
◆ Since $m_t \ll m_{KK}$ the outgoing tops are ultra-relativistic, their products collimate => **top jets**

The challenge of highly boosted Massive Jets

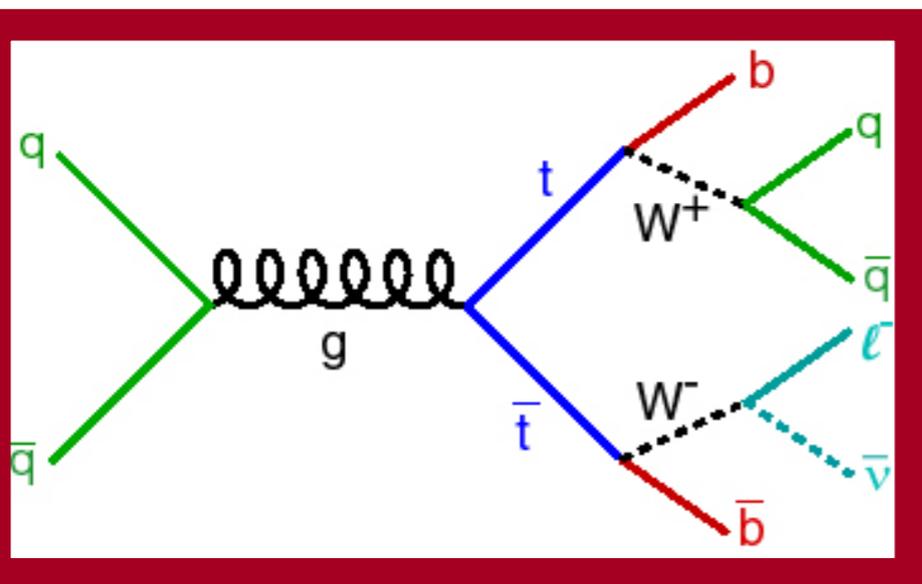
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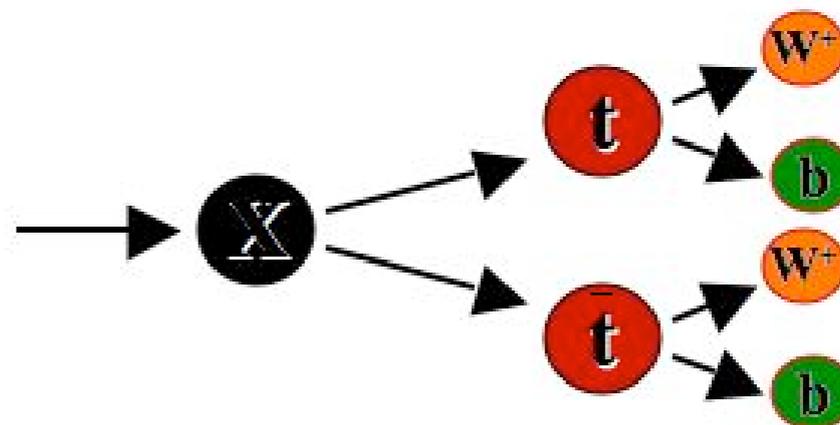


The challenge of highly boosted Massive Jets

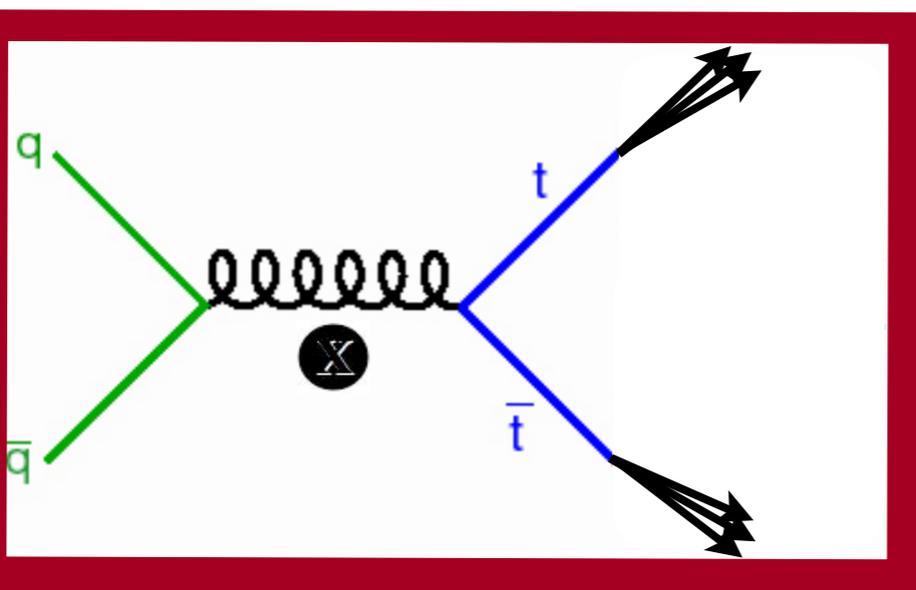
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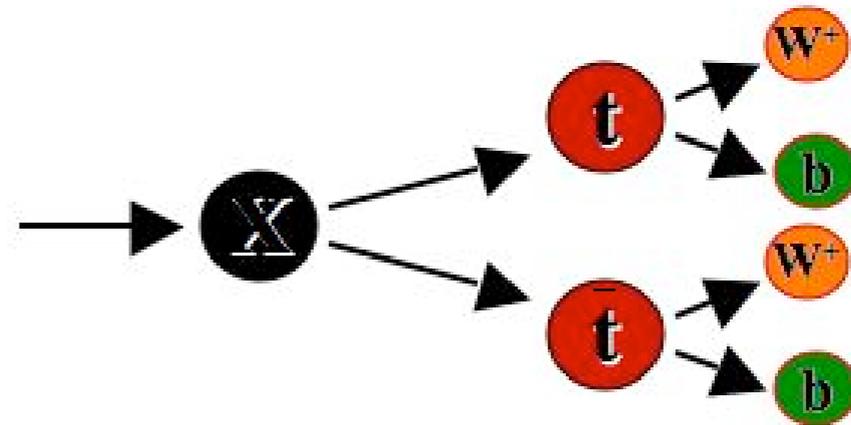


The challenge of highly boosted Massive Jets

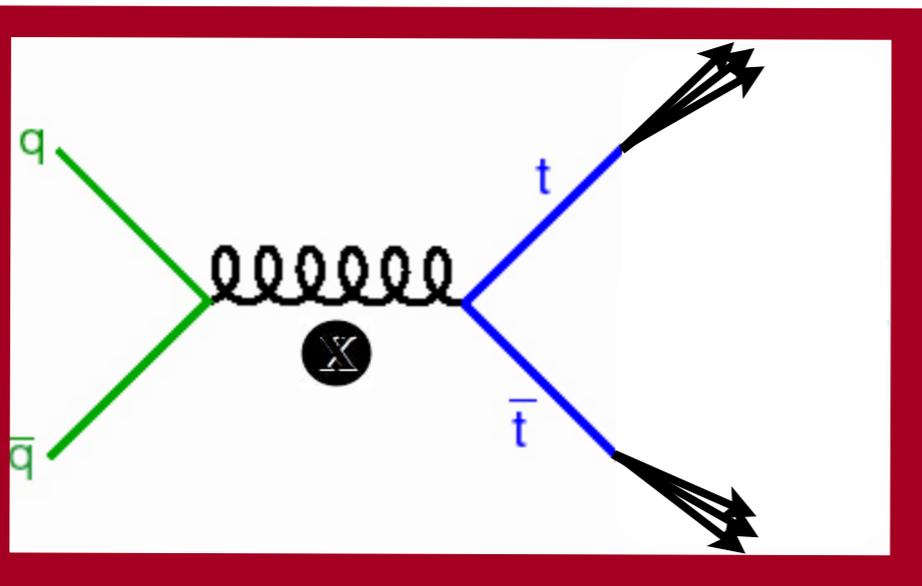
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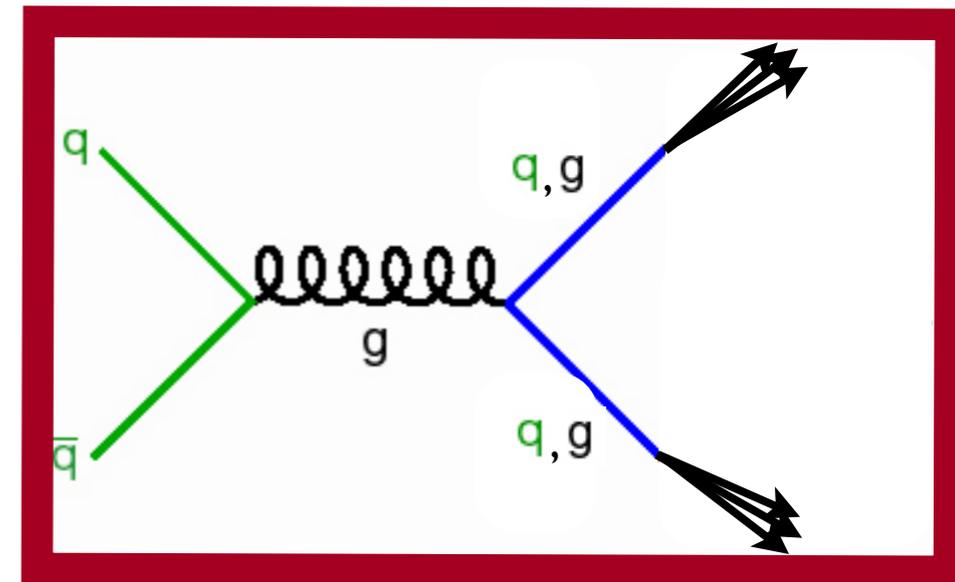
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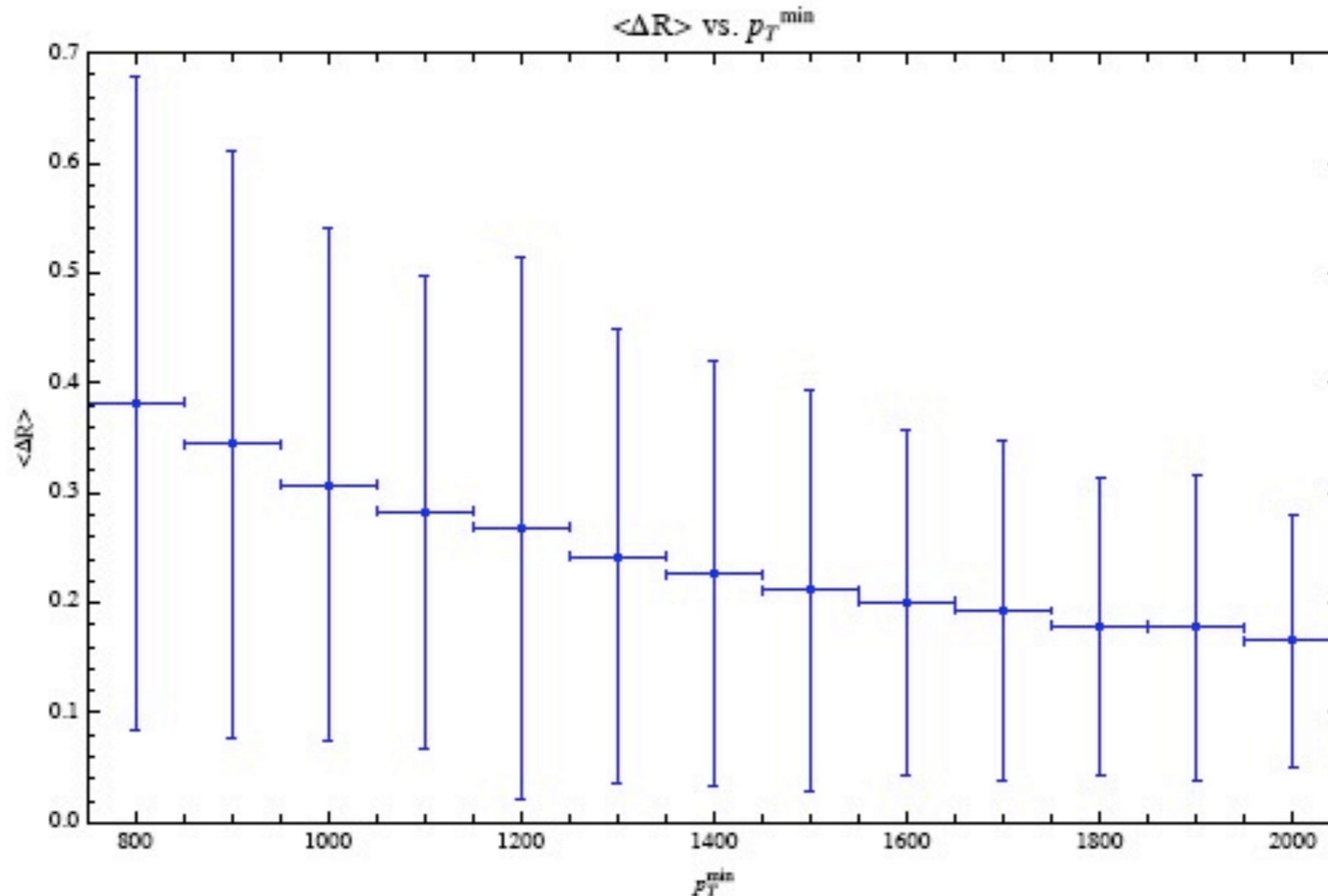
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Similar to ordinary
2-jet QCD
process impossible
to observe ??



Boosted top (w/z/h) jets & collimation



Partonic
Level

Highly Boosted Tops:
High Collimations!

ΔR vs. P_T

$$\Delta R = \sqrt{\Delta\eta^2 + \Delta\phi^2}$$

Why not use scaled-down conventional methods?

- ◆ IRC (IR & collinear) safety require inclusive observables (e.g. cone or kt jets).
- ◆ Hadronic calorimeter tower has an hard angular size $R \sim 0.1$
- ◆ Radial shower of energetic hadrons are very large (require 1 full cell of H-cal to capture single $P_T = 100$ GeV pion)
- ◆ $R = 0.4$ smallest cone used so far. A careful th'+exp' effort required to go beyond that.

Top jet & di-jet @ the LHC

Almeida, SL, Perez, Sung, & Virzi.

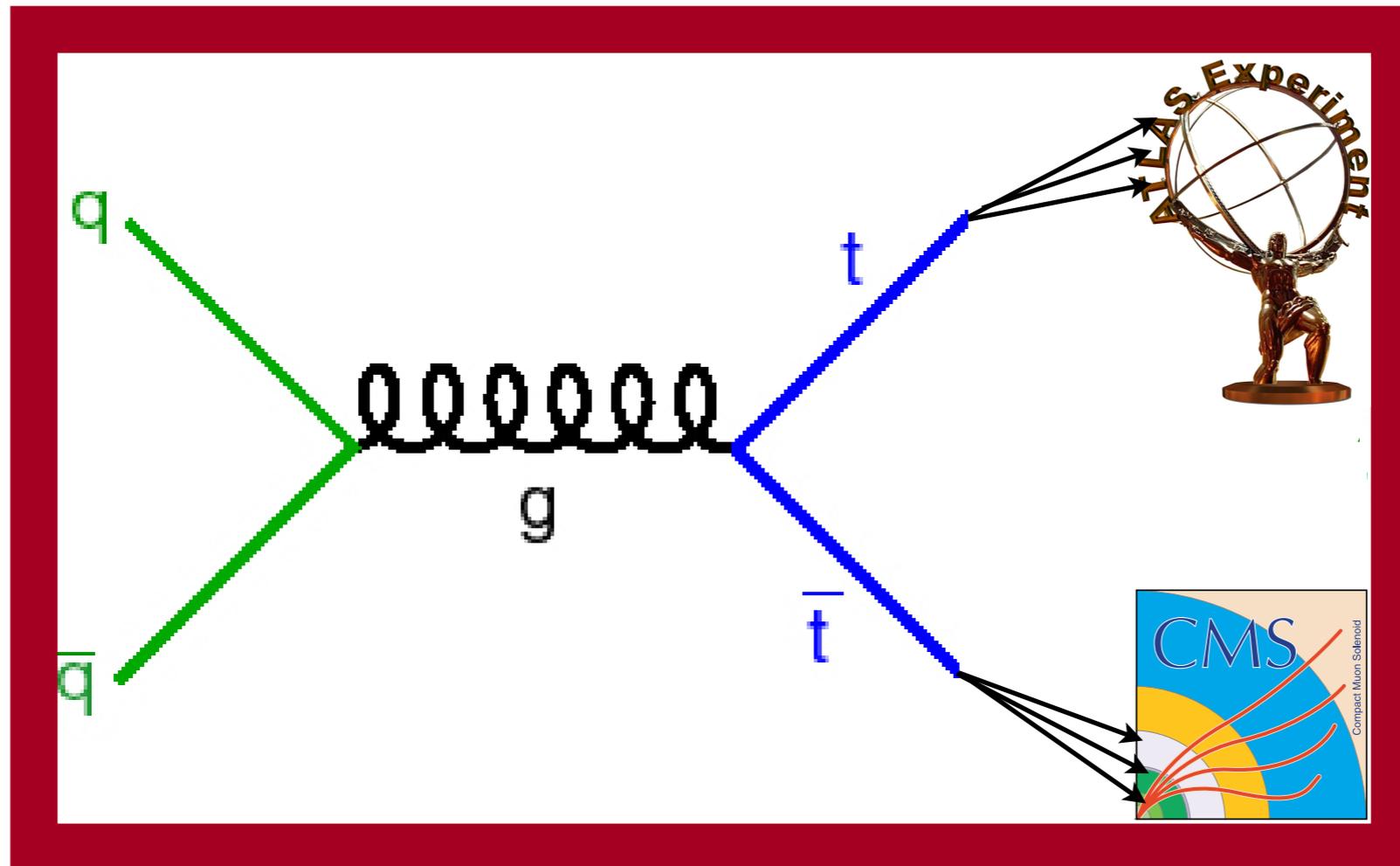
◆ $S/B < 10^{-2}$, for $p_t(j) > 1000 \text{ GeV}$, $R=0.4$
 (10 pb for $jj+X$, 100 fb for $t\bar{t}+X$)

Process	Generator	PDF	Matching	Cross Section
$pp \rightarrow t\bar{t}(j)$	SHERPA 1.0.9	CTEQ6M	CKKW	135 fb
$pp \rightarrow t\bar{t}(j)$	SHERPA 1.1.2	CTEQ6M	CKKW	149 fb
$pp \rightarrow t\bar{t}(j)$	MG/ME 4	CTEQ6M	MLM	68 fb
$pp \rightarrow t\bar{t}(j)$	MG/ME 4	CTEQ6L	MLM	56 fb
$pp \rightarrow t\bar{t}$	Pythia 6.4	CTEQ6L	-	157 fb
$pp \rightarrow t\bar{t}$	Pythia 8.1	CTEQ6M	-	174 fb
$pp \rightarrow jj(j)$	SHERPA 1.1.0	CTEQ6M	CKKW	10.2 pb
$pp \rightarrow jj(j)$	MG/ME 4	CTEQ6L	MLM	8.54 pb
$pp \rightarrow jj(j)$	MG/ME 4	CTEQ6M	MLM	9.93 pb
$pp \rightarrow jj$	Pythia 6.4	CTEQ6L	-	13.7 pb
$pp \rightarrow jj$	Pythia 8.1	CTEQ6M	-	13.3 pb

“Theory” of massive jets @ the LHC

Other works:

Butterworth, Cox, Forshaw;
Thaler & Wang; Conway; Vos; Brooijmans
Kaplan, Rehermann, Schwartz & Tweedie. ...
Butterworth, Davison, Rubin, Salam,...



(I) Jet mass.

(II) Jet substructure:

(i) angularity (ii) Planar flow (iii) Template Overlap

Jet Mass-Overview

- ◆ **Jet mass**-sum of “massless” momenta in h-cal inside the cone: $m_J^2 = \left(\sum_{i \in R} P_i \right)^2, P_i^2 = 0$
- ◆ Jet mass is non-trivial both for S & B
(naively: QCD jets are massless while top jets $\sim m_t$)

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- ◆ Jet mass is non-trivial both for S & B
- ◆ Simple mass tagging tricky (counting in mass window)
- ◆ S&B distributions via 1st principles & compare to Monte-Carlo.
- ◆ Allow to improve S/B & yield insights!

Non trivial top-jet mass distribution

- ◆ Naively the signal is $J \propto \delta(m_J - m_t)$
- ◆ In practice: $m_J^t \sim m_t + \delta m_{QCD} + \delta m_{EW}$

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+ detector smearing.

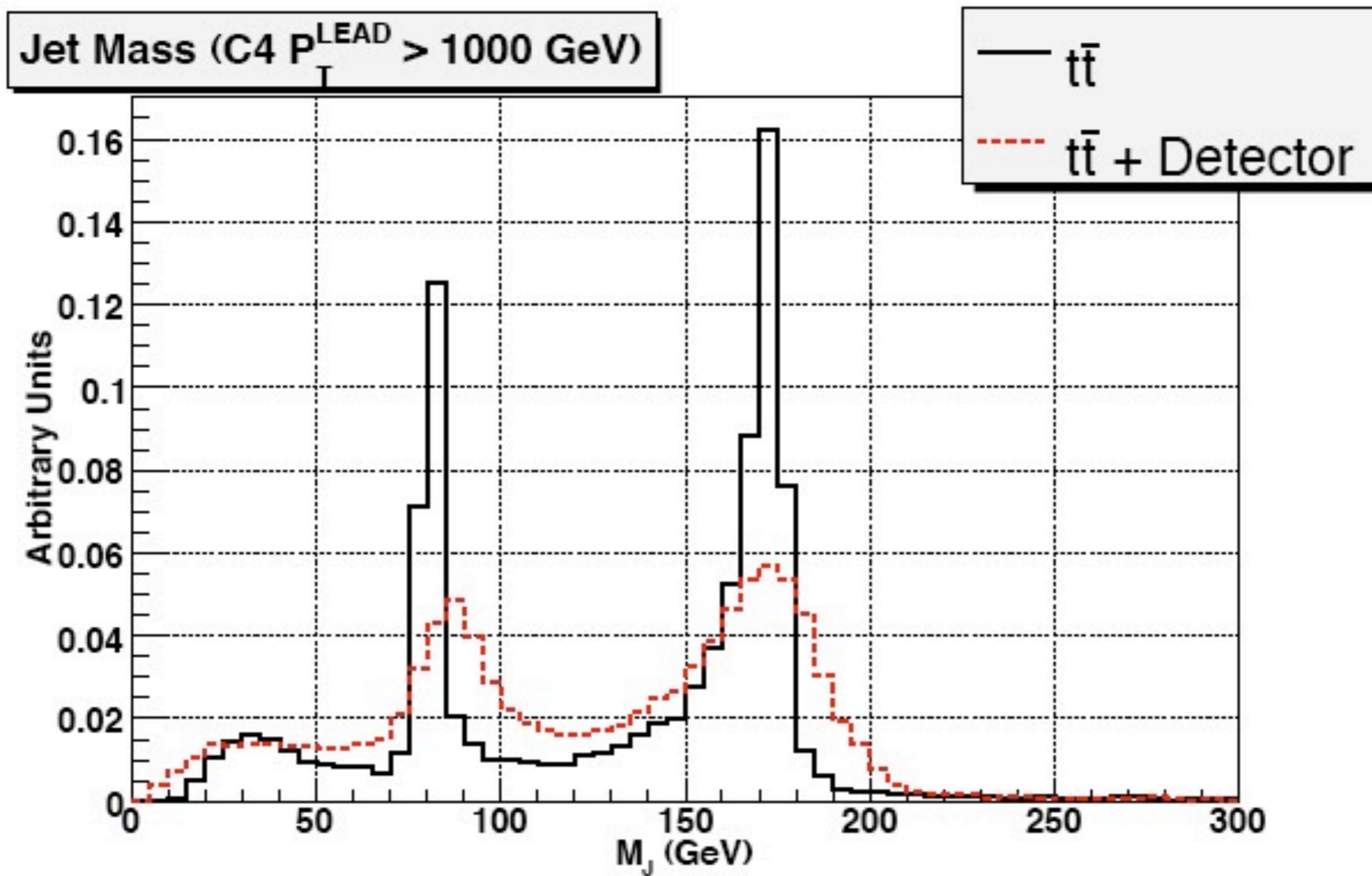
Can understood
perturbatively
fast & small ~10GeV

Pure kinematical bW(qq)
dist'
in/out cone
~0.2 GeV

Non trivial top-jet mass distribution

- ◆ $|J^t(m_J, R, p_T) \sim \int d(\delta m_{EW}) dm_{QCD} \delta(m_J - m_{QCD} - \delta m_{EW})$
 $\times J_{QCD}^t(m_{QCD}, R, p_T) \mathcal{F}_{EW}(\delta m_{EW}, m_{QCD}/(p_T R))$
 - ◆ In practice: $m_J^t \sim m_t + \delta m_{QCD} + \delta m_{EW}$
+ detector smearing.
- Can understood perturbatively fast & small $\sim 10\text{GeV}$
- Pure kinematical bW(qq) dist' in/out cone $\sim 0.2\text{ GeV}$

Sherpa => Transfer functions, JES
(CKKW)



QCD jet mass distribution

◆ Boosted QCD Jet via factorization:

$$\frac{d\sigma^i}{dm_J} = J^i(m_J, p_T^{\min}, R^2) \sigma^i(p_T^{\min})$$

$$\int dm_J J^i = 1 \quad i = Q, G$$

- can interpret the jet function as a probability density functions for a jet with a given pT to acquire a mass between mJ and mJ + δmJ

Full expression:

$$\frac{d\sigma_{H_A H_B \rightarrow J_1 J_2}}{dm_{J_1}^2 dm_{J_2}^2 d\eta} = \sum_{abcd} \int dx_a dx_b \phi_a(x_a, p_T) \phi_b(x_b, p_T) \frac{d\hat{\sigma}_{ab \rightarrow cd}}{dp_T d\eta}(x_a, x_b, \eta, p_T)$$

$$S(m_{J_1}^2, m_{J_2}^2, \eta, p_T, R^2) J_1^{(c)}(m_{J_1}^2, \eta, p_T, R^2) J_2^{(d)}(m_{J_2}^2, \eta, p_T, R^2)$$

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$i = Q, G$

For large jet mass & small R,
no big logs =>
can be calculated via
perturbative QCD!

- can interpret the jet function
mass between m_J and $m_J +$

quire a

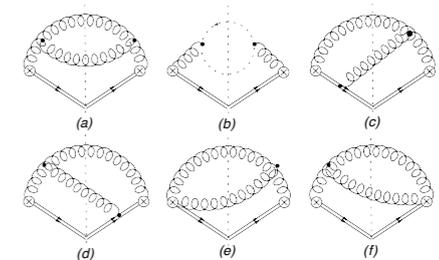
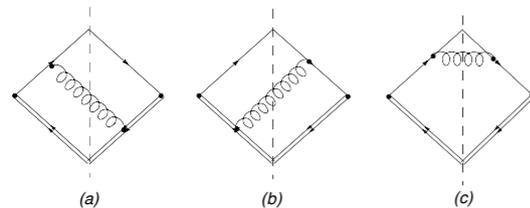
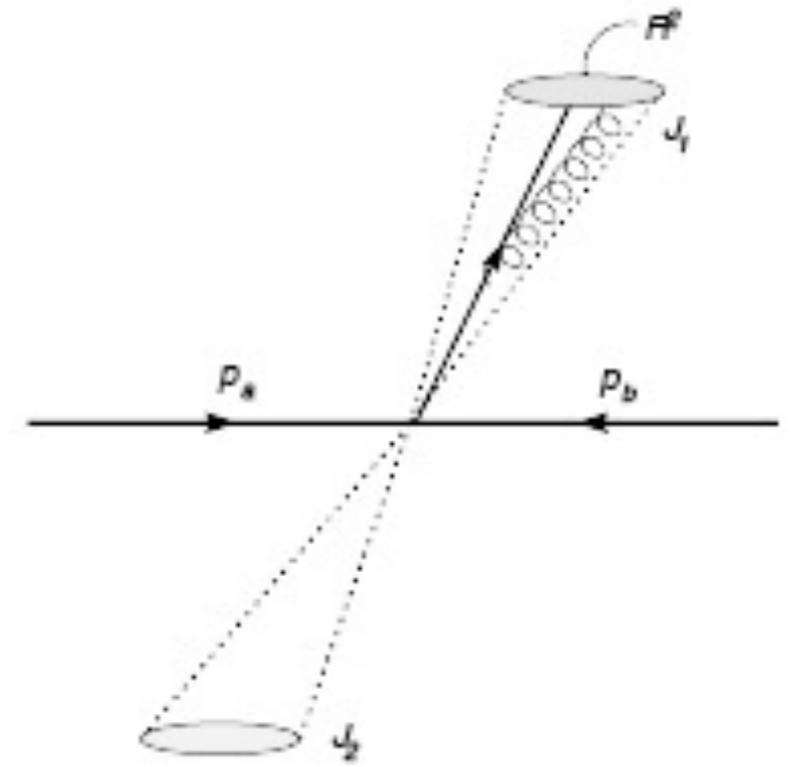
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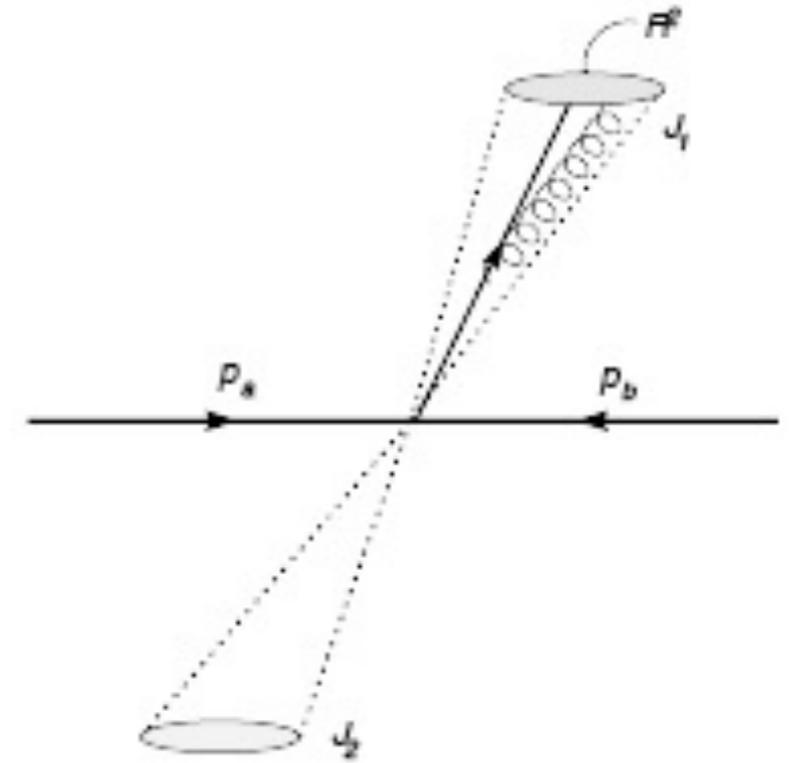
QCD jet mass distribution, Q+G

Main idea: calculating mass due to two-body QCD bremsstrahlung:



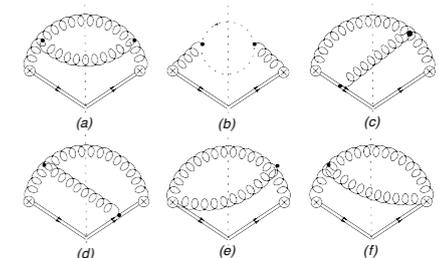
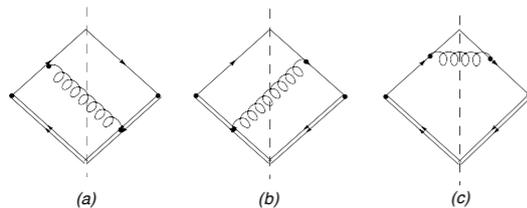
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Main idea: calculating mass due to two-body QCD bremsstrahlung:



$$J^{(eik),c}(m_J, p_T, R) \simeq \alpha_S(p_T) \frac{4C_c}{\pi m_J} \log \left(\frac{R p_T}{m_J} \right)$$

$C_F = 4/3$ for quarks, $C_A = 3$ for gluons.



QCD jet mass distribution, Q+G

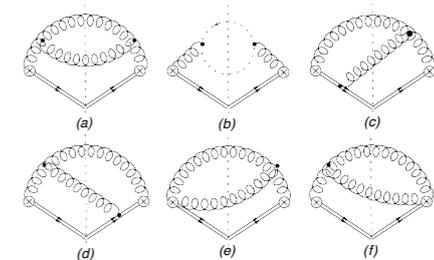
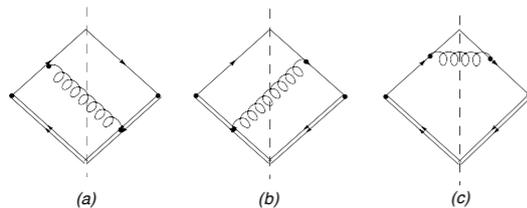
$$J_i^{q(1)}(m_J^2, p_{0,J_i}, R) = \frac{C_F \beta_i}{4m_{J_i}^2} \int_{\cos(R)}^{\beta_i} \frac{d \cos \theta_S}{\pi} \frac{\alpha_S(k_0) z^4}{(2(1 - \beta_i \cos \theta_S) - z^2)(1 - \beta_i \cos \theta_S)} \times$$

$$\left\{ z^2 \frac{(1 + \cos \theta_S)^2}{(1 - \beta_i \cos \theta_S)(2(1 + \beta_i)(1 - \beta_i \cos \theta_S) - z^2(1 + \cos \theta_S))} + \frac{3(1 + \beta_i)}{z^2} + \frac{1}{z^4} \frac{(2(1 + \beta_i)(1 - \beta_i \cos \theta_S) - z^2(1 + \cos \theta_S))^2}{(1 + \cos \theta_S)(1 - \beta_i \cos \theta_S)} \right\},$$

$$\beta_i = \sqrt{1 - m_{J_i}^2/p_{0,J_i}^2} \quad z = \frac{m_{J_i}}{p_{0,J_i}}, \quad p_{0,J_i} = \sqrt{m_{J_i}^2 + p_T^2}, \quad \text{and } k_0 = \frac{p_{0,J_i}}{2} \frac{z^2}{1 - \beta_i \cos \theta_S}.$$

$$J_i^{g(1)}(m_J^2, p_{0,J_i}, R) = \frac{C_A \beta_i}{16m_{J_i}^2} \int_{\cos(R)}^{\beta_i} \frac{d \cos \theta_S}{\pi} \frac{\alpha_S(k_0)}{(1 - \beta \cos \theta_S)^2 (1 - \cos^2 \theta_S) (2(1 + \beta) - z^2)}$$

$$\times (z^4(1 + \cos \theta_S)^2 + z^2(1 - \cos^2 \theta_S)(2(1 + \beta_i) - z^2) + (1 - \cos \theta_S)^2(2(1 + \beta_i) - z^2)^2)$$



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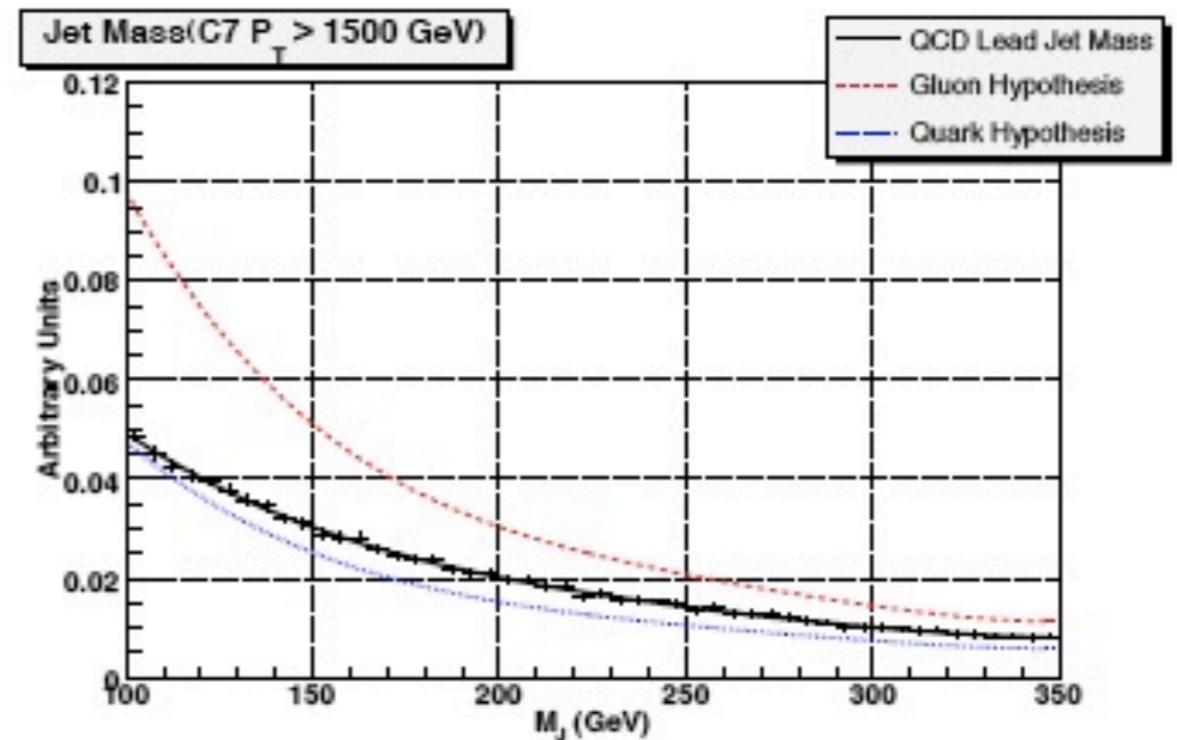
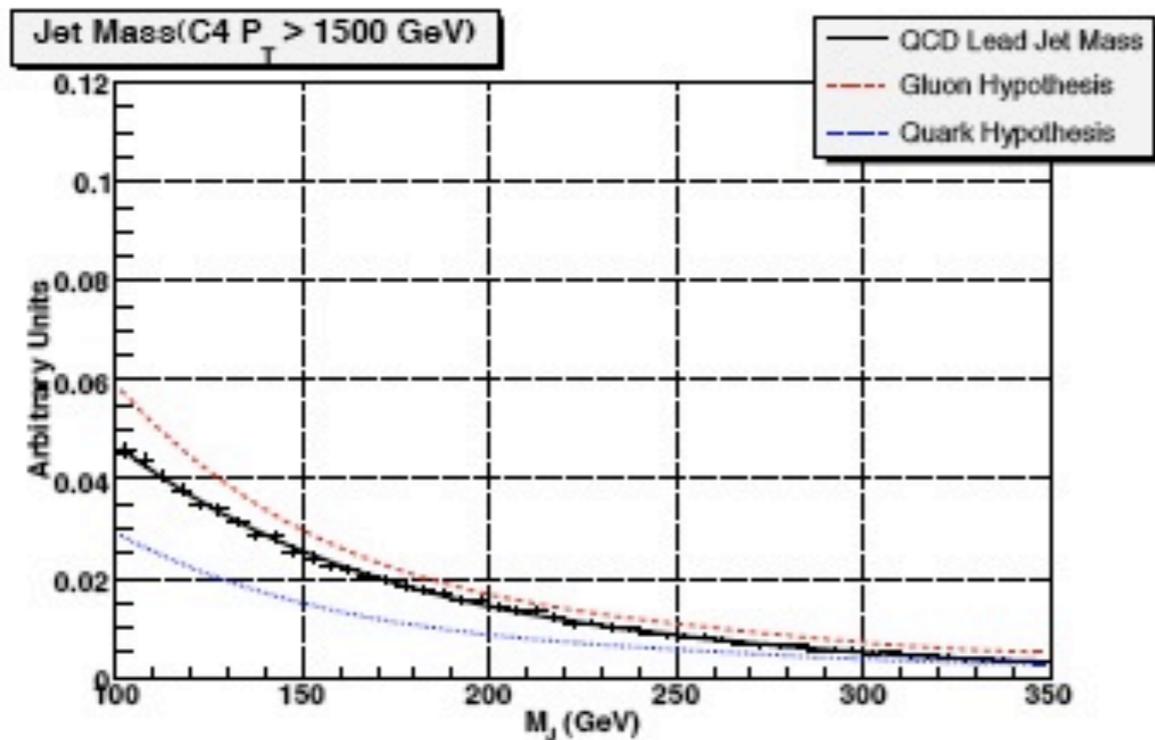
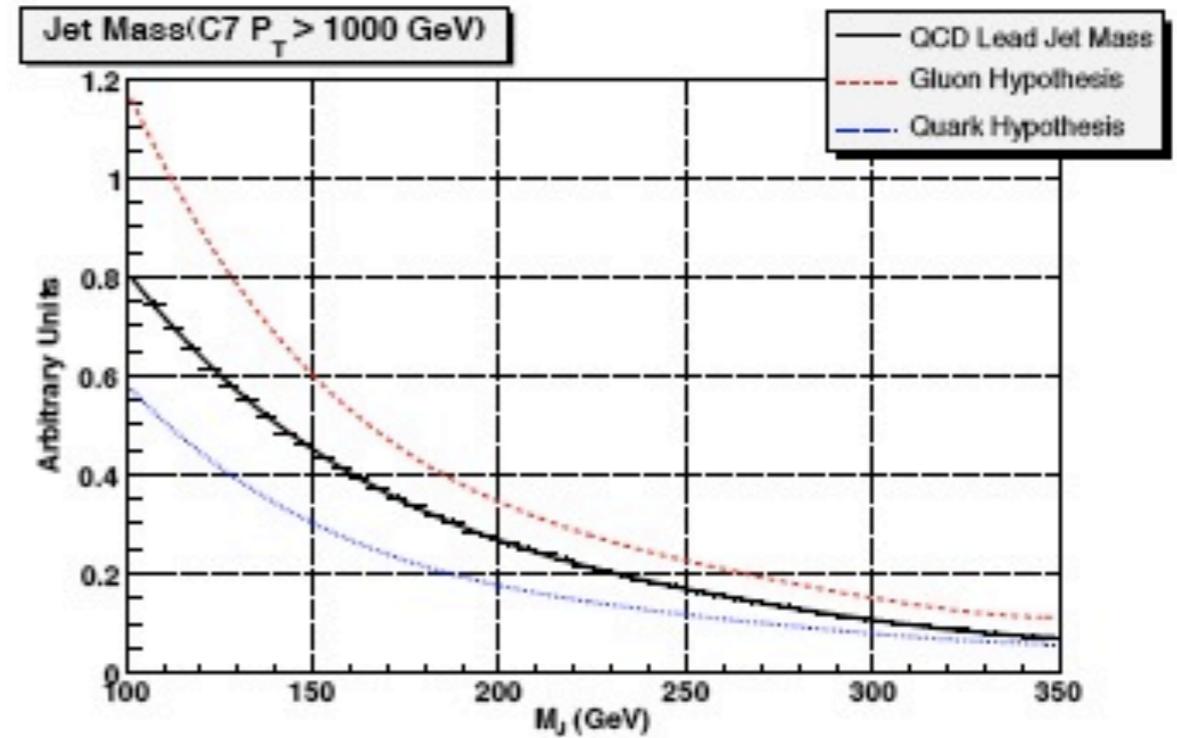
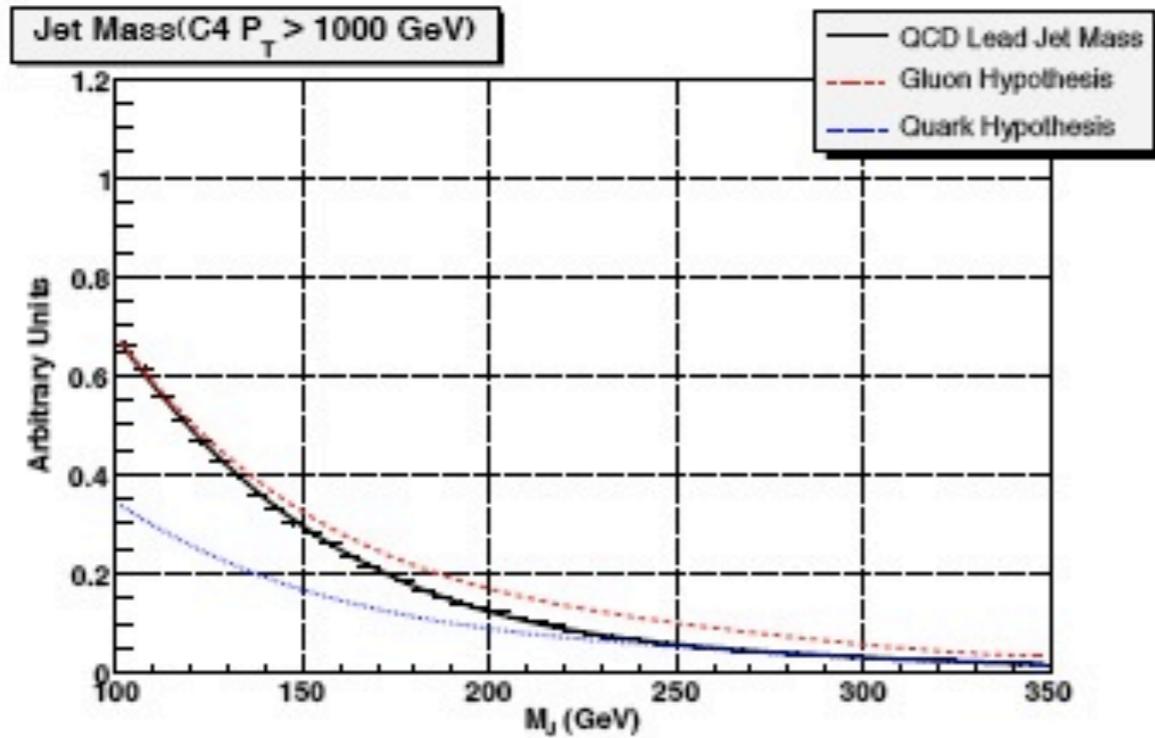
$C_F = 4/3$ for quarks, $C_A = 3$ for gluons.

Data is admixture of the two, should be bounded by them:

$$\frac{d\sigma_{pred}(R)}{dp_T dm_J} \text{ upper bound} = J^g(m_J, p_T, R) \sum_c \left(\frac{d\sigma^c(R)}{dp_T} \right)_{MC},$$
$$\frac{d\sigma_{pred}(R)}{dp_T dm_J} \text{ lower bound} = J^q(m_J, p_T, R) \sum_c \left(\frac{d\sigma^c(R)}{dp_T} \right)_{MC},$$

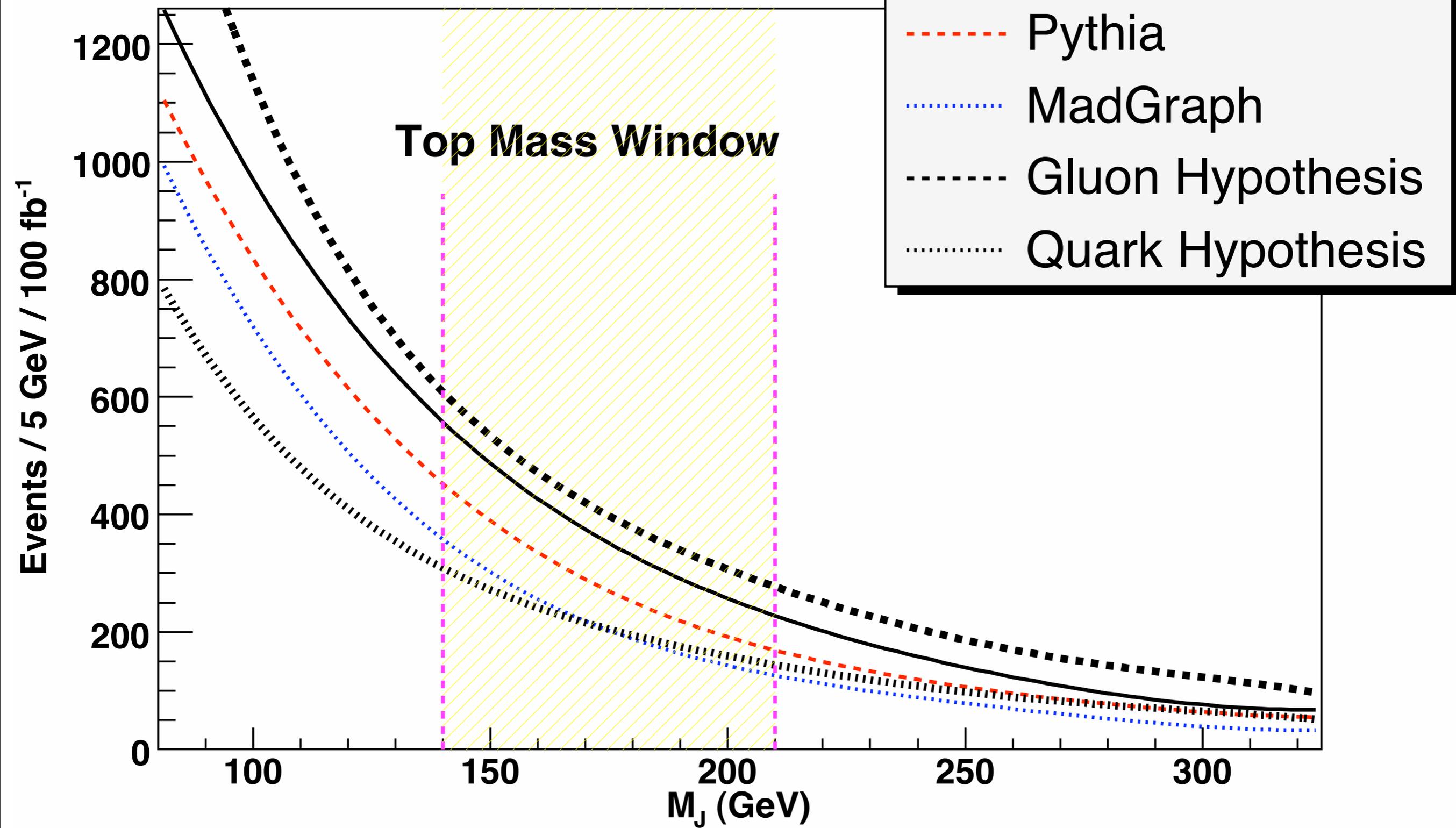
Jet mass distribution theory vs. MC

Sherpa, jet function convolved above p_T^{\min}



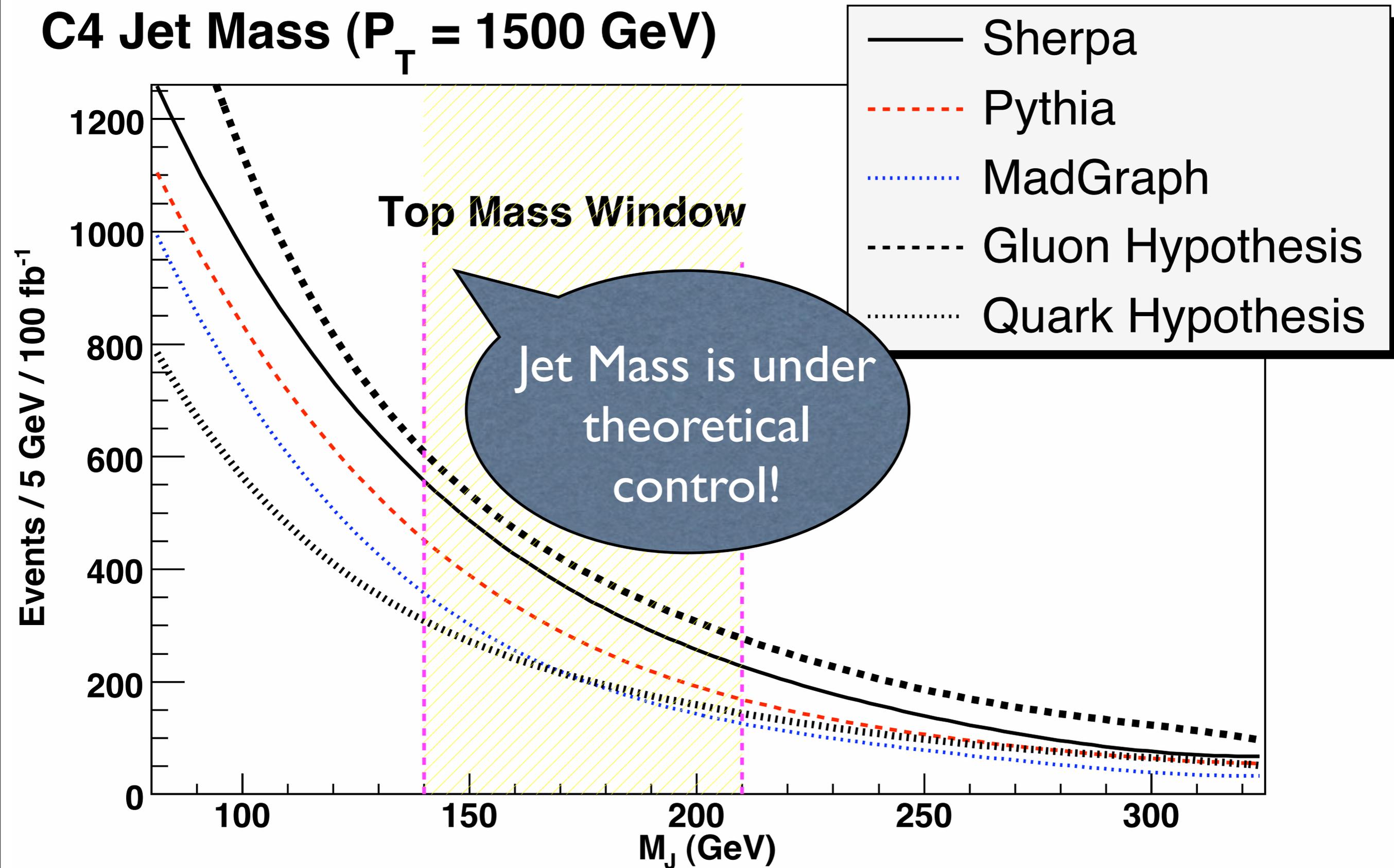
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C4 Jet Mass ($P_T = 1500$ GeV)



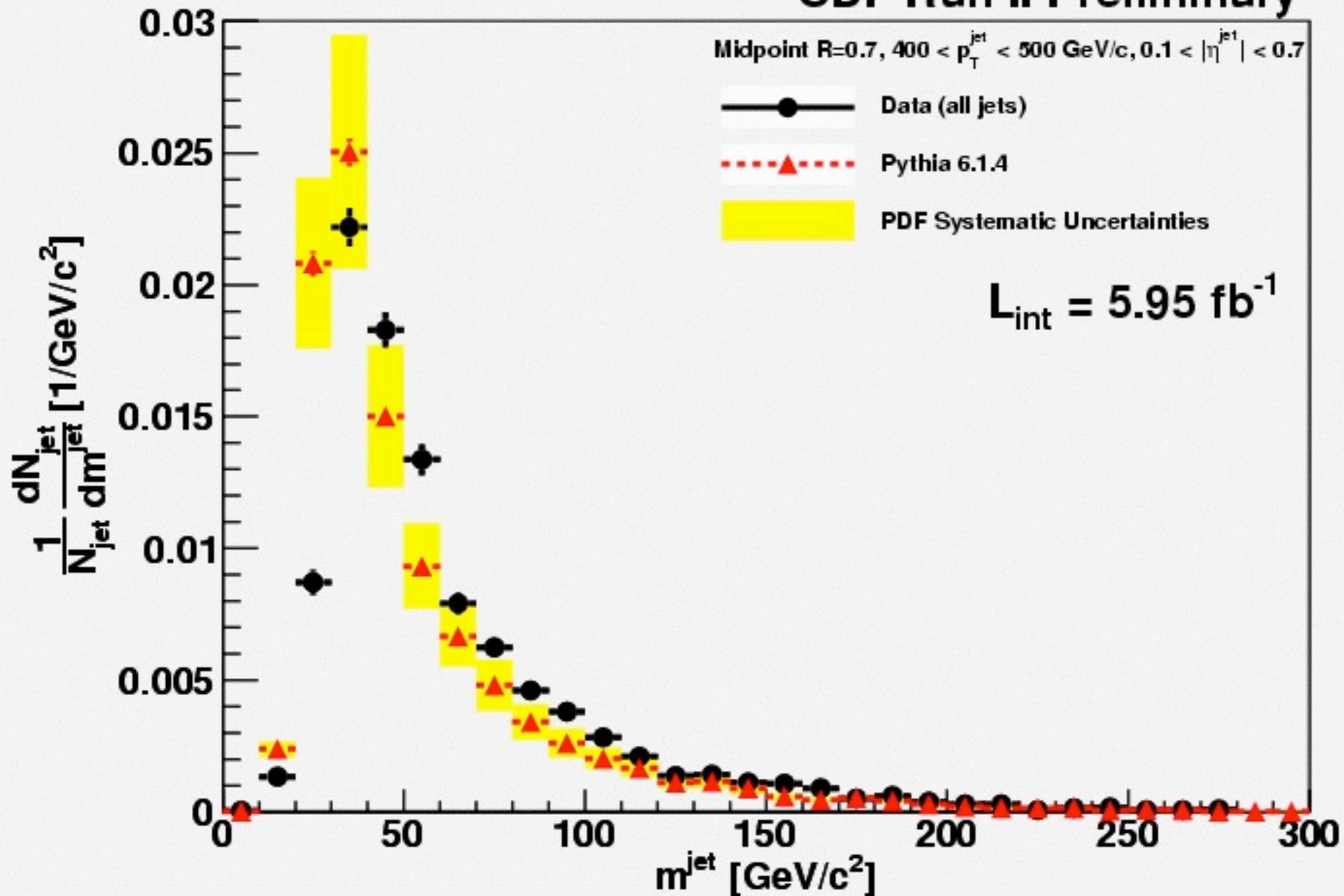
Jet mass distribution theory vs. MC

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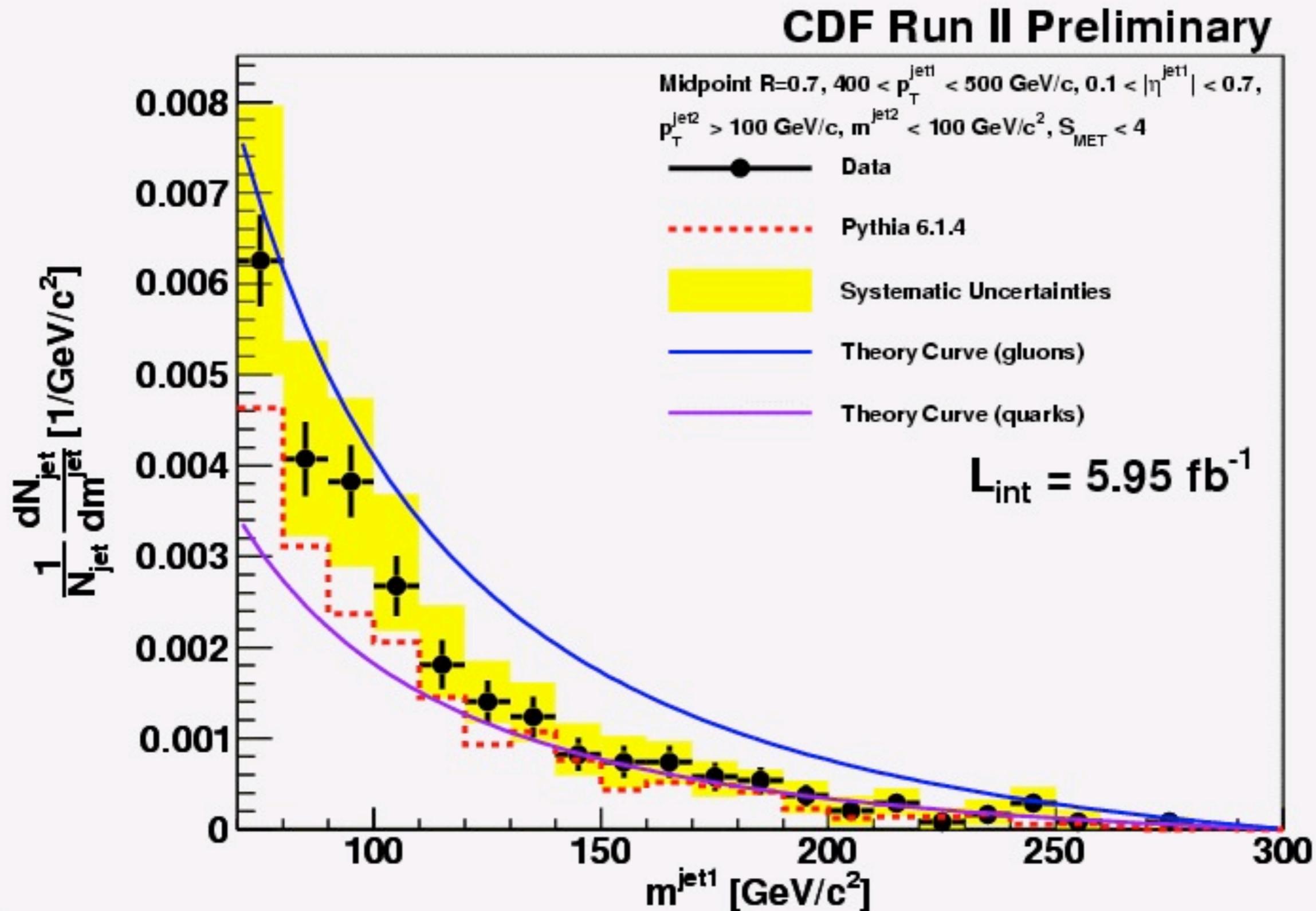
Jet mass distribution

CDF Run II Preliminary

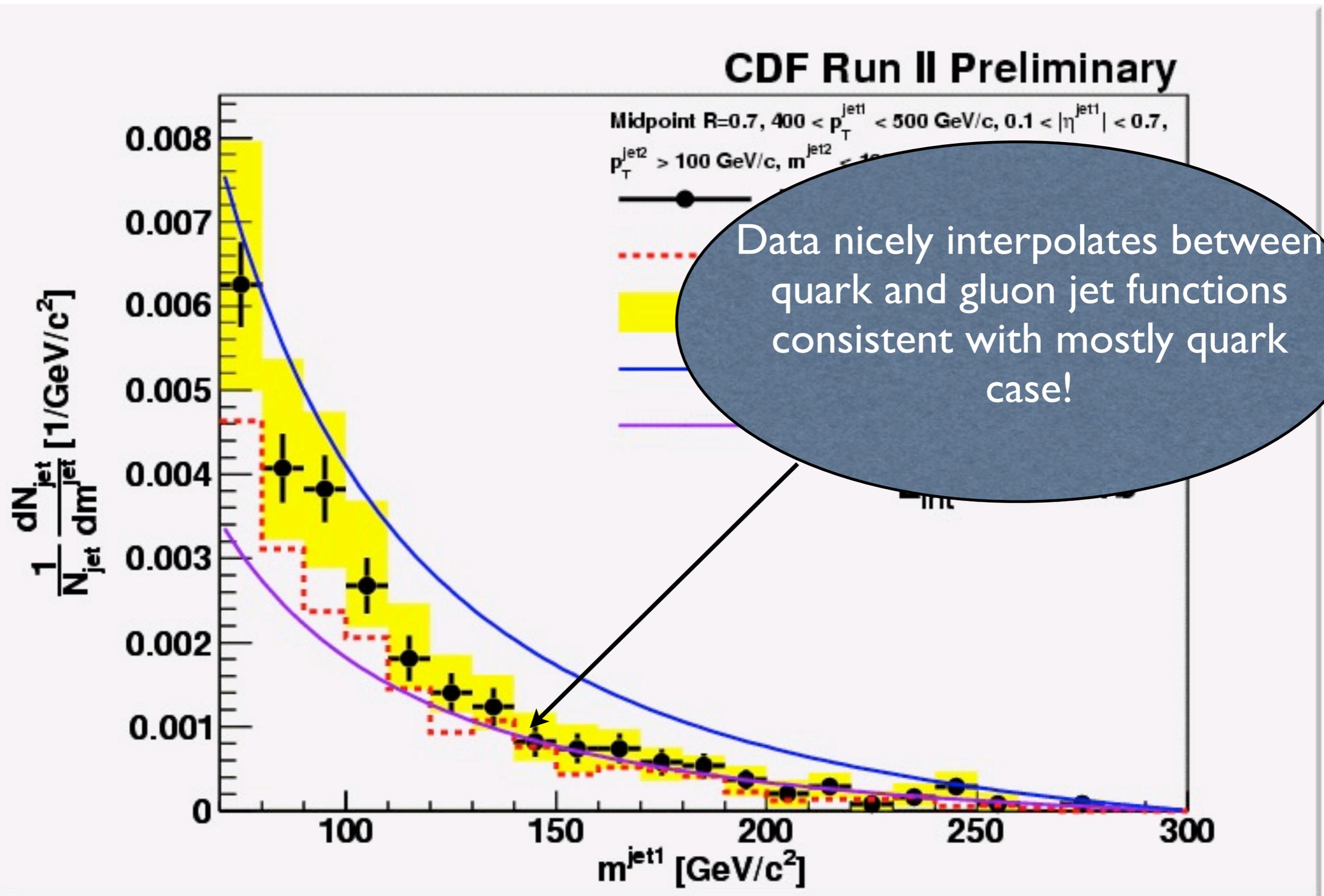


Distribution of jet mass after MI correction for jets with $400 < p_T < 500$ GeV/c, cone $R=0.7$, data and QCD MC

Jet mass distribution, high mass region



Jet mass distribution, high mass region



SM $t\bar{t}$ vs dijet: jet mass tagging

Resolve signal from dijet background:

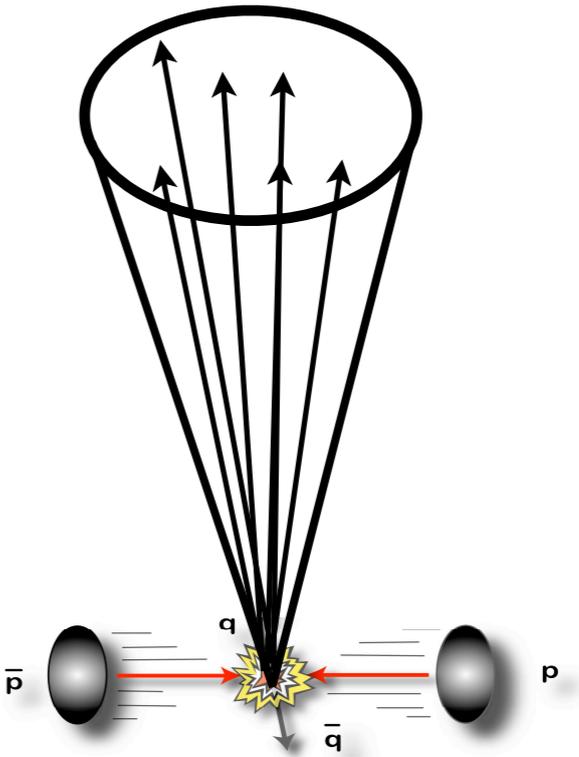
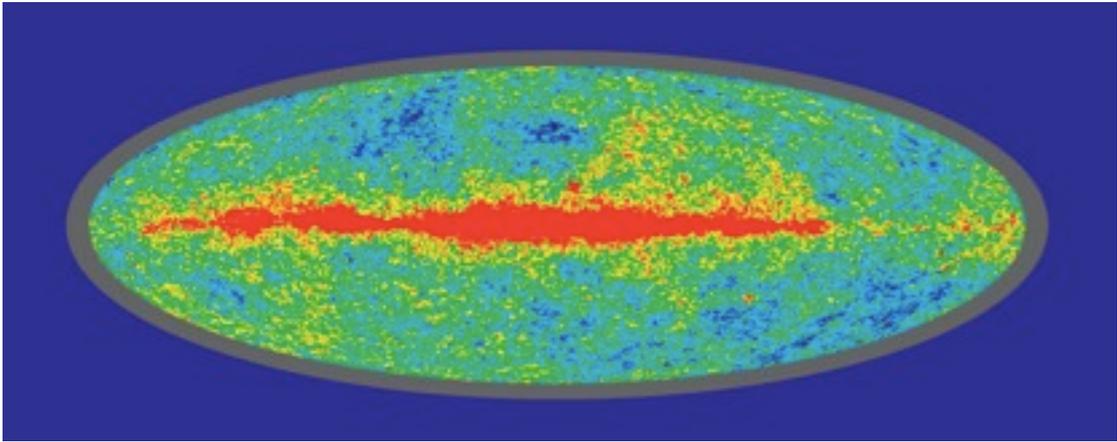
$$p_T^{\min} \sim 1 \text{ TeV and } 25 \text{ fb}^{-1}$$

$$p_T^{\min} \sim 1.5 \text{ TeV with } 100 \text{ fb}^{-1}$$

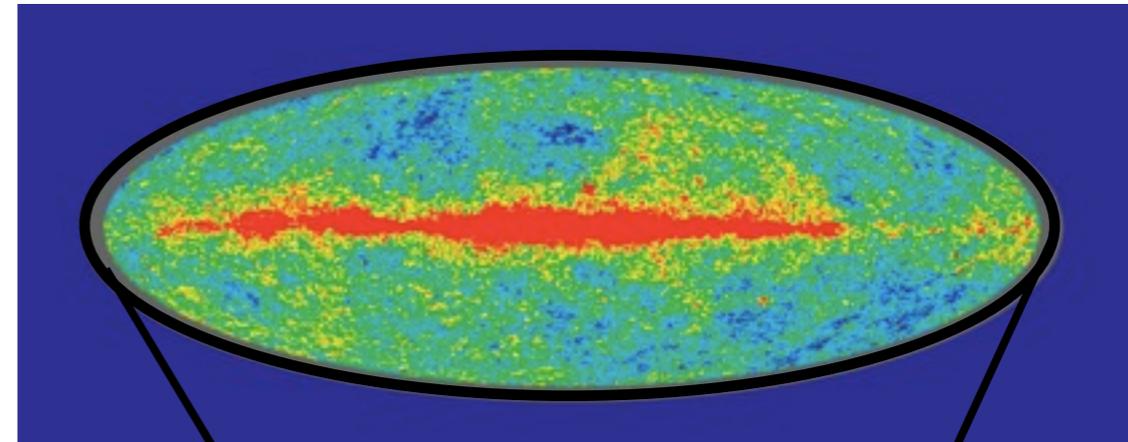
without jet substructure or b-tagging

Note that if S/B is enhanced,
as in RS or other NP models reach is better.

Need to distinguish between top & ordinary QCD jet



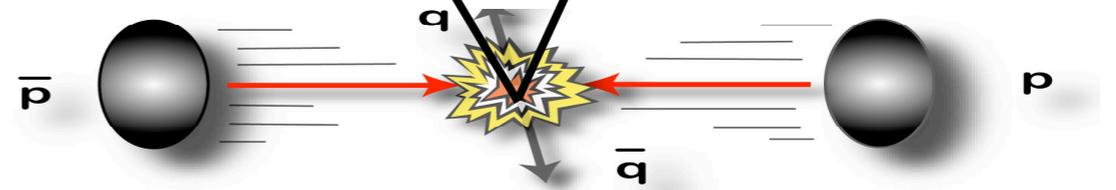
Need to understand the energy flow inside jet jet shapes or jet substructure



Theory of ultra massive boosted jets Part II:

(ii) Angularity & Planar flow.

(iii) Template Overlap Method



Why jets? What else?

- ◆ QCD amplitudes have soft-collinear singularity
- ◆ Observable: IR safe, smooth function of E flow
Sterman & Weinberg, PRL (77)
- ◆ Jet is a very inclusive object, defined via direction + p_T (+ mass)
- ◆ Even $R=0.4$ contains $O(50)$ had-cells \Rightarrow huge amount of info' is lost

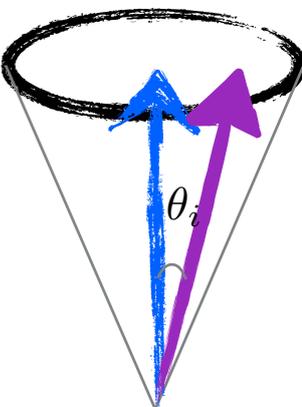
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Ellis & Weinberg, PRL (77)
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jet shape = inclusive observables
dependent on energy flow
within individual jets

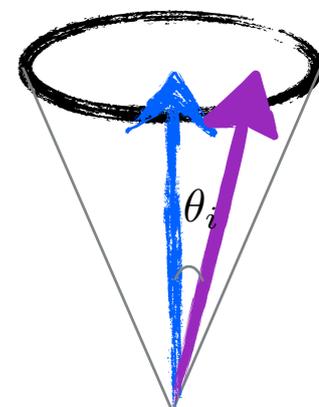
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- ◆ Once jet mass is fixed at a high scale
 - ➔ Large class of jet-shapes become perturbatively calculable

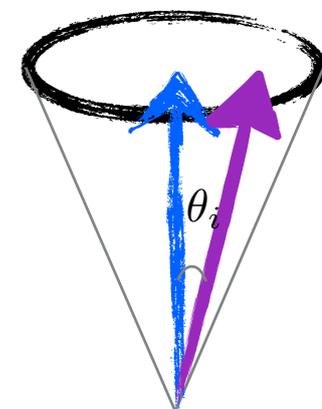


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- ◆ As a warm-up consider angularity (2-body final state):

Berger, Kucs and Sterman (03)

Angularities on a cone:



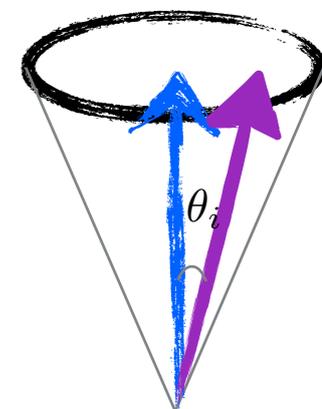
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Berger, Kucs and Sterman (03)

Angularities on a cone:

$$\tilde{\tau}_a(R, m_J) = \frac{1}{m_J} \sum_{i \in \text{jet}} \omega_i \sin^a\left(\frac{\pi\theta_i}{2R}\right) \left[1 - \cos\left(\frac{\pi\theta_i}{2R}\right)\right]^{1-a} \sim \frac{1}{m_J} \frac{1}{2^{1-a}} \sum_{i \in \text{jet}} \omega_i \left(\frac{\pi\theta_i}{2R}\right)^{2-a}$$



Almeida, SL Perez, Sterman, Sung, & Virzi.

2-body jet's kinematics, $Z/W/h$

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$a \leq 2$ for IR safety

◆ Angularities distinguish between Higgs and QCD jets:

$$\frac{dJ^h}{d\tilde{\tau}_a} \propto \frac{1}{|a| (\tilde{\tau}_a)^{1-\frac{2}{a}}}$$

v.s.

$$\frac{dJ^{\text{QCD}}}{d\tilde{\tau}_a} \propto \frac{1}{|a| \tilde{\tau}_a}$$

2-body jet's kinematics, $Z/W/h$

$$P^x(\theta_s) = (dJ^x/d\theta_s)/J^x \Rightarrow P^x(\tilde{\tau}_a); \quad R(\tilde{\tau}_a) = \frac{P^{\text{sig}}(\tilde{\tau}_a)}{P^{\text{QCD}}(\tilde{\tau}_a)}$$

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$R^{\tau_{-2}}$ vs. τ_{-2} for $z=0.05$

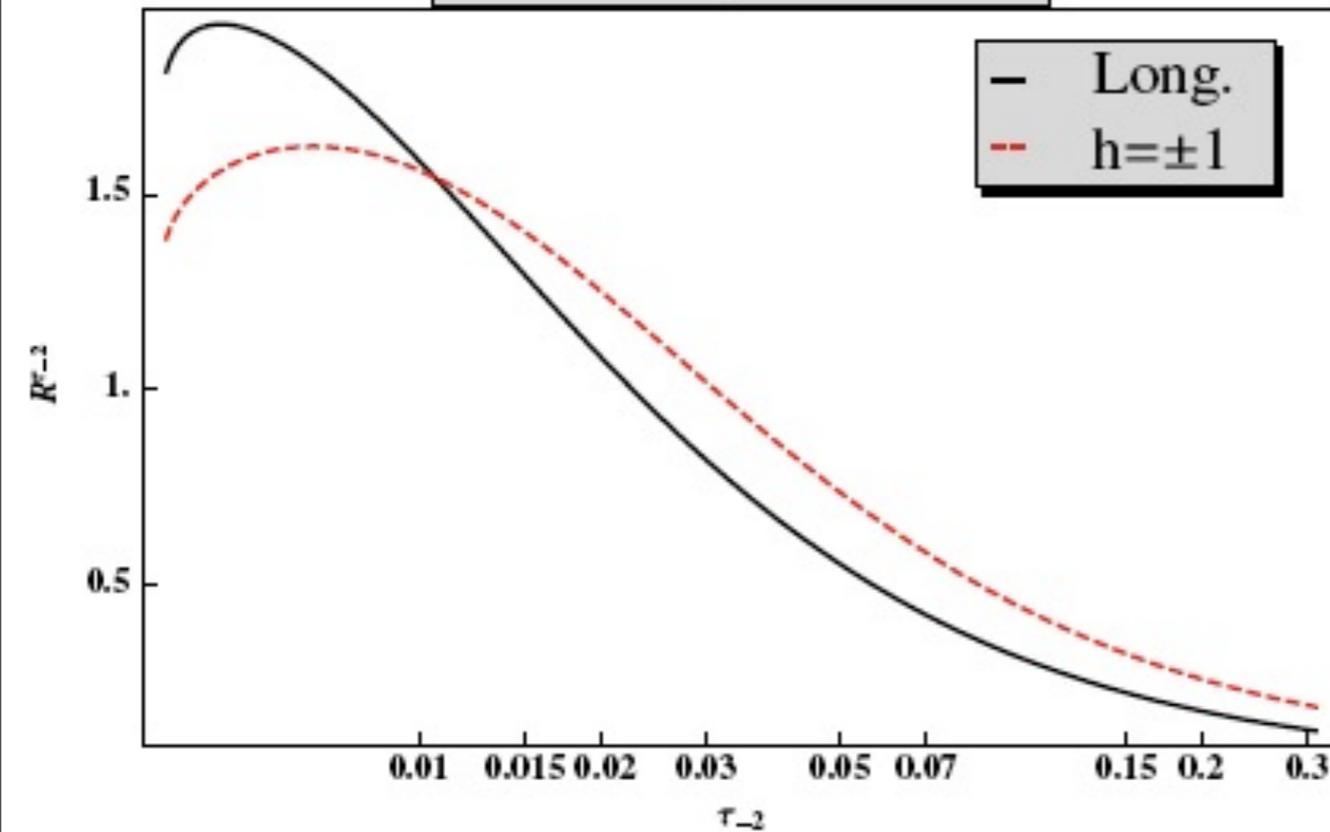


FIG. 3 (color online). The ratio between the signal and background probabilities to have jet angularity $\tilde{\tau}_{-2}$, $R^{\tilde{\tau}_{-2}}$.

$$(z = m_J/p_T)$$

Angularity, τ_a ($a = -2$, $z = 0.05$, $R = 0.4$)

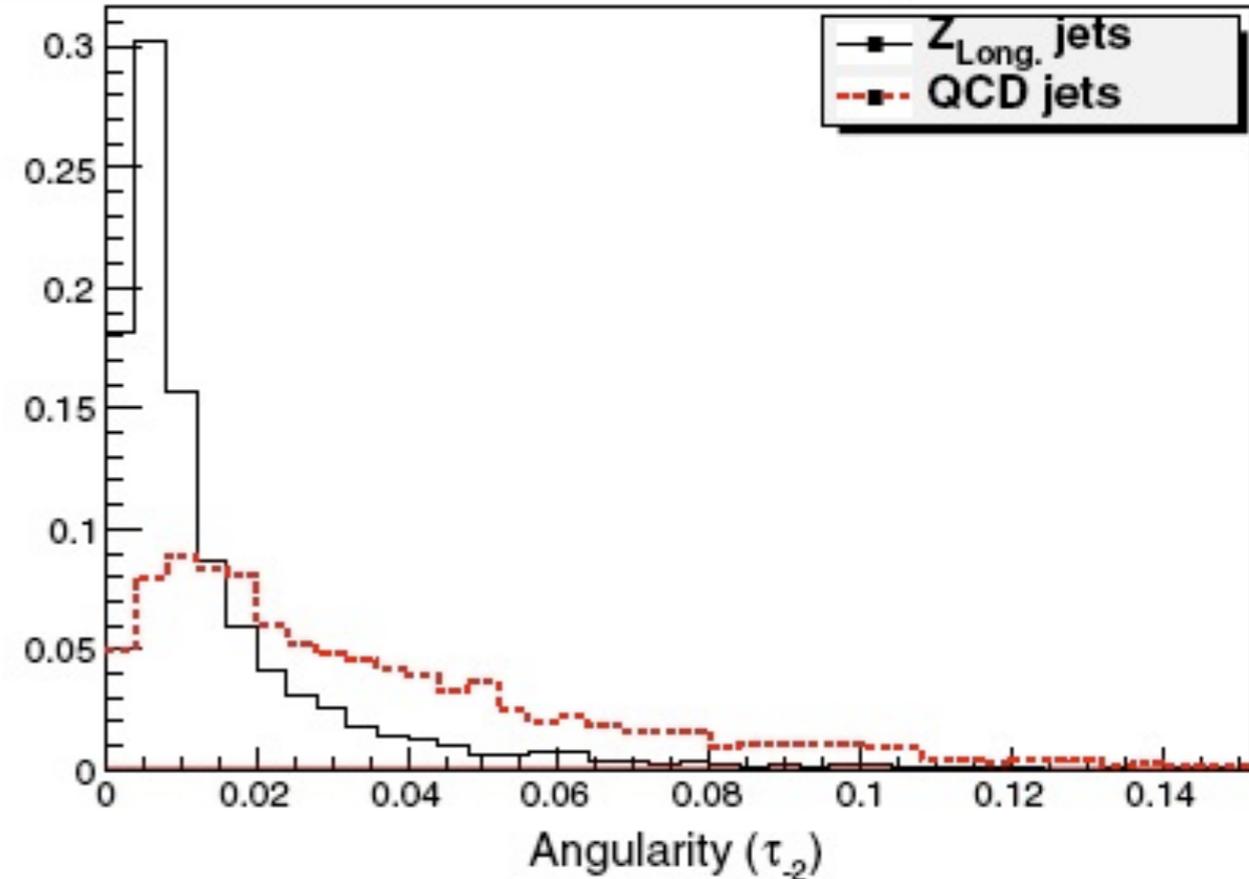


FIG. 4 (color online). The angularity distribution for QCD (red-dashed curve) and longitudinal Z (black-solid curve) jets obtained from MADGRAPH. Both distributions are normalized to the same area.

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Peak \Rightarrow special "democratic" configuration where the two particles have same energy & min' distance from

jet axis $\theta_m \approx z$.

$$(z = m_J/p_T)$$

Angularities, τ_a ($a = -2, z = 0.05, R = 0.4$)

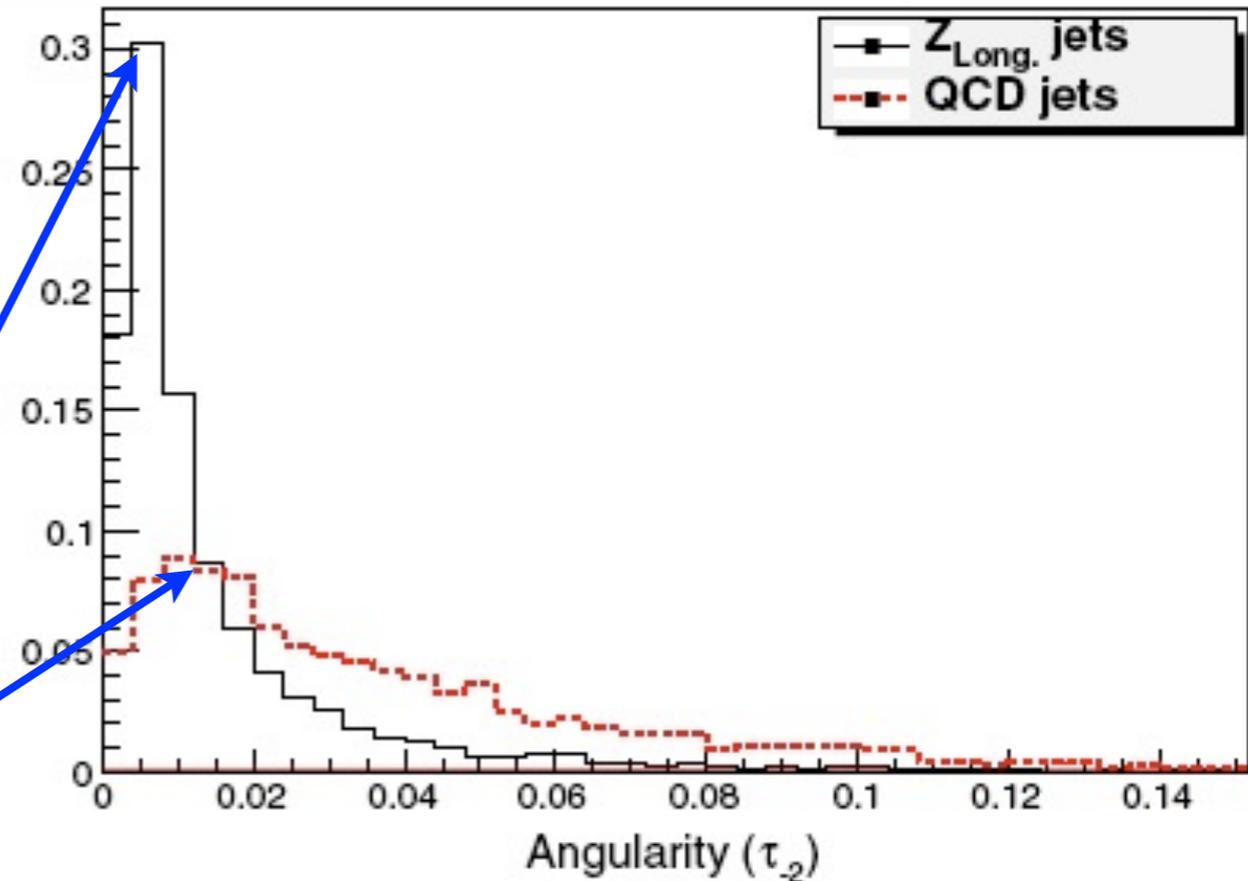


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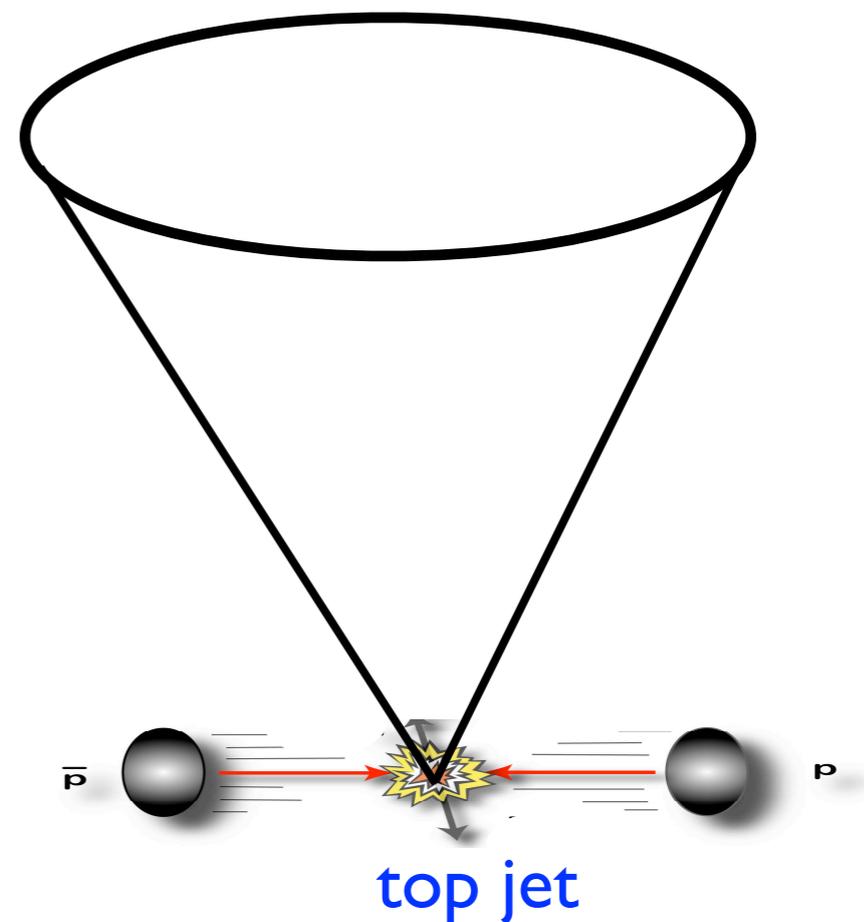
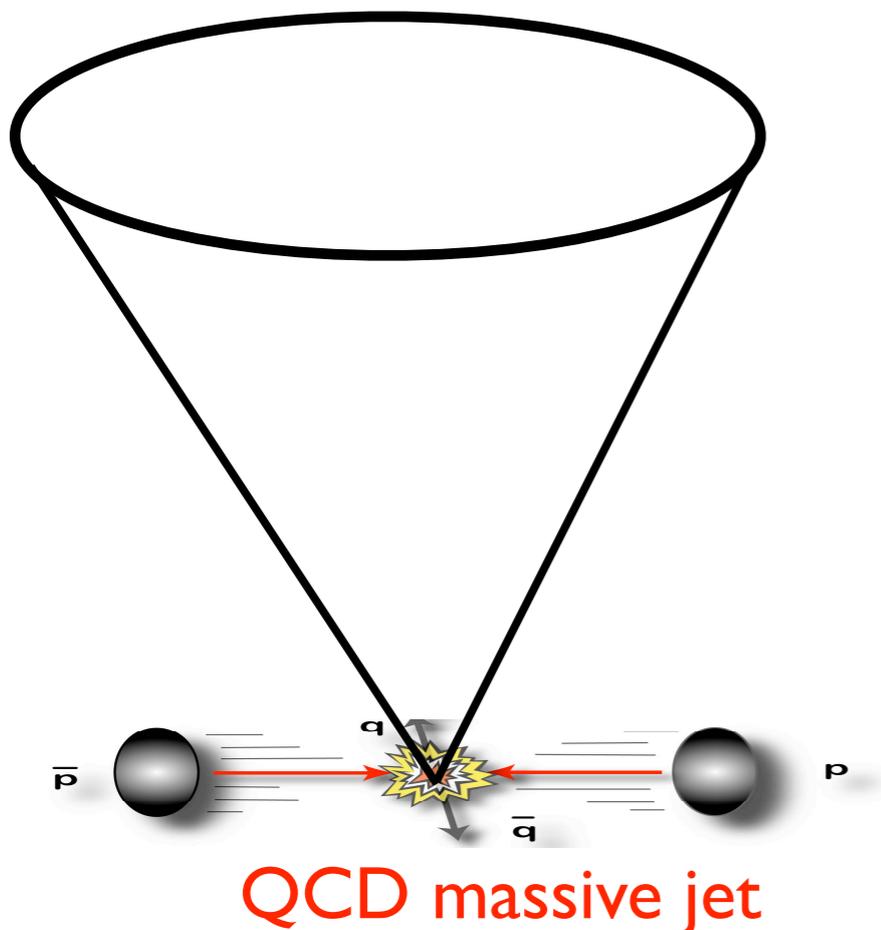
and back-

Planar flow

◆ Top-jet is 3 body vs. massive QCD jet \Leftrightarrow 2-body (our result)

Thaler & Wang, JHEP (08);

Almeida, Lee, GP, Sterman, Sung & Virzi, PRD (09).

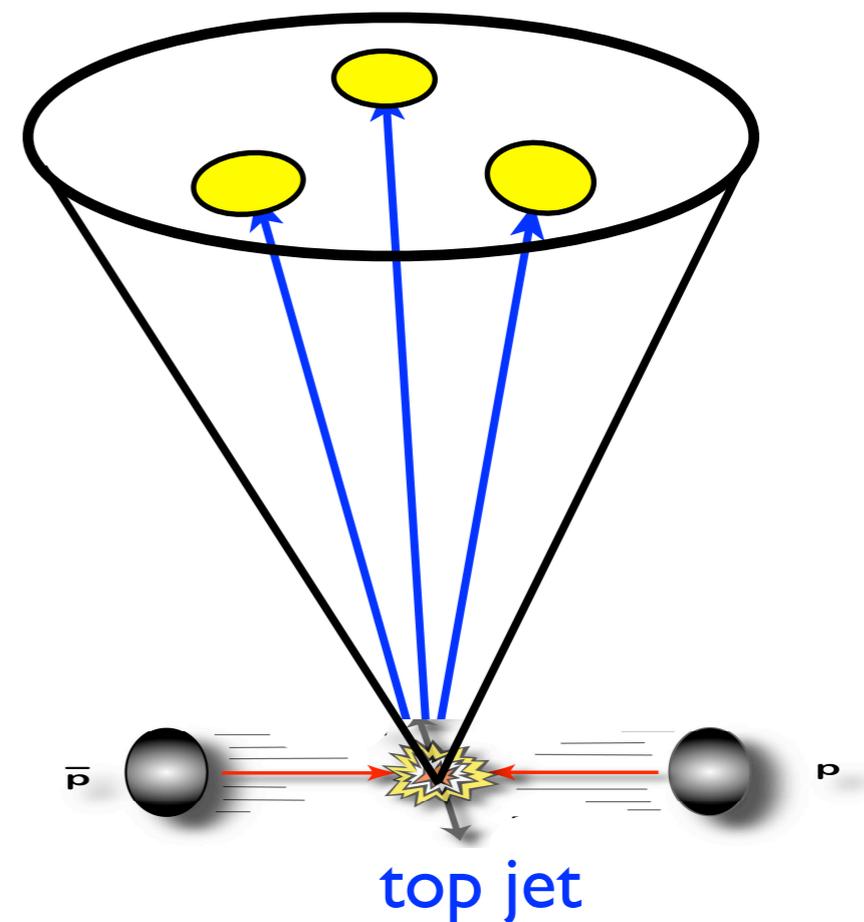
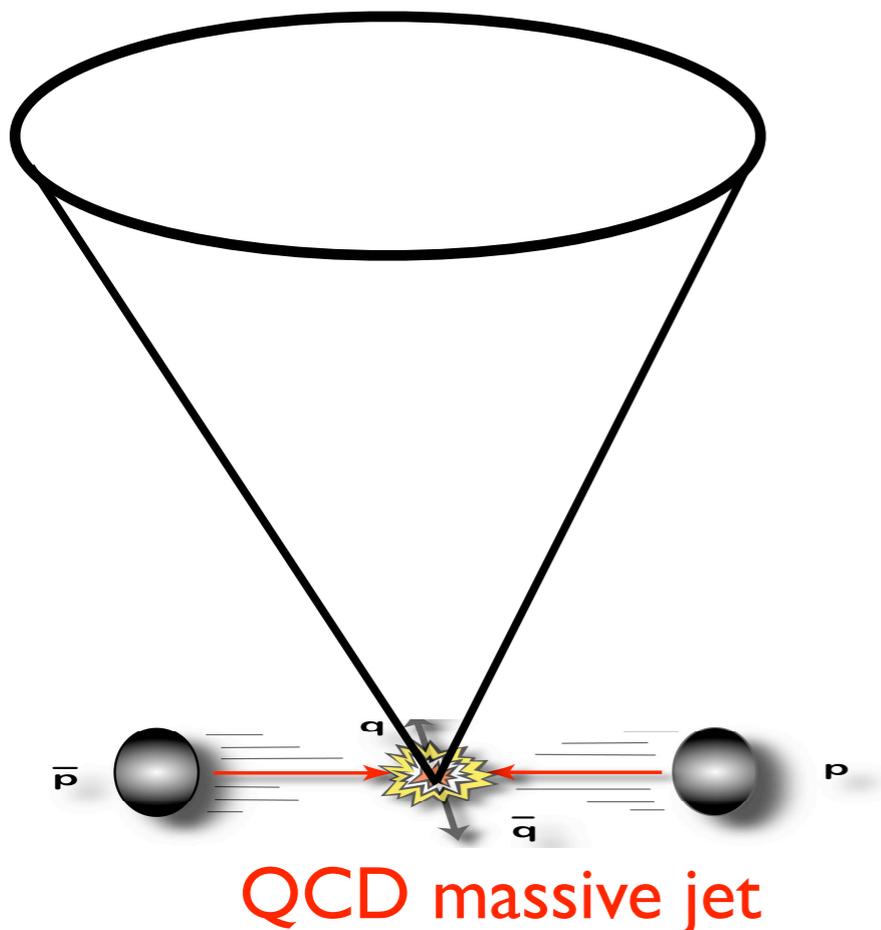


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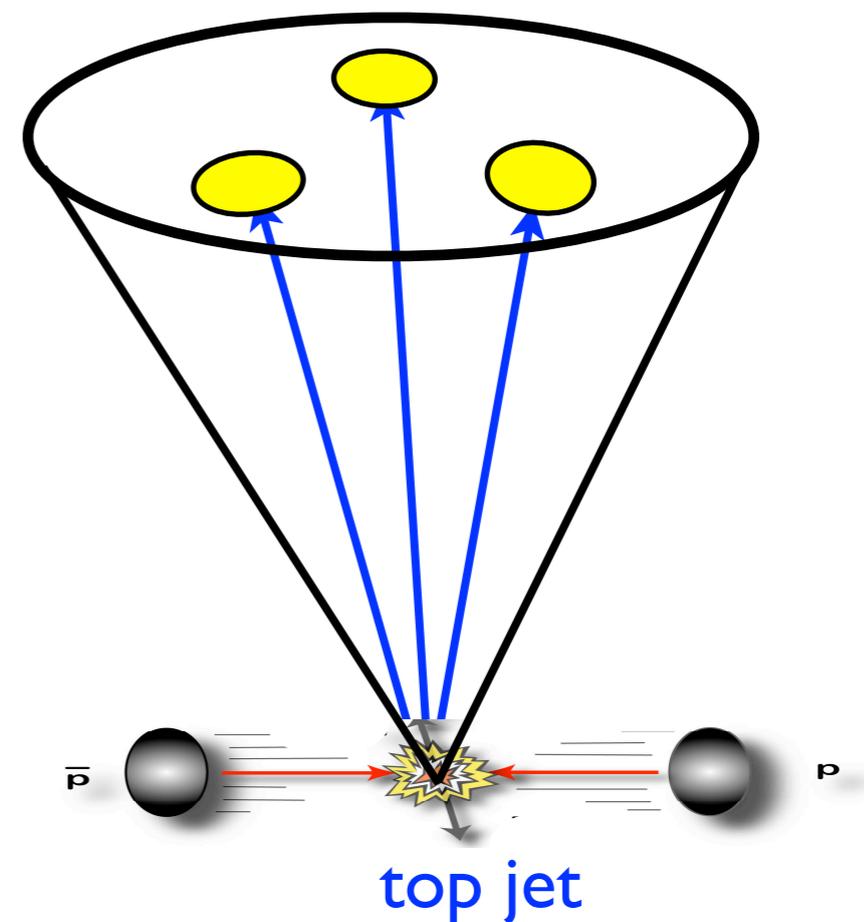
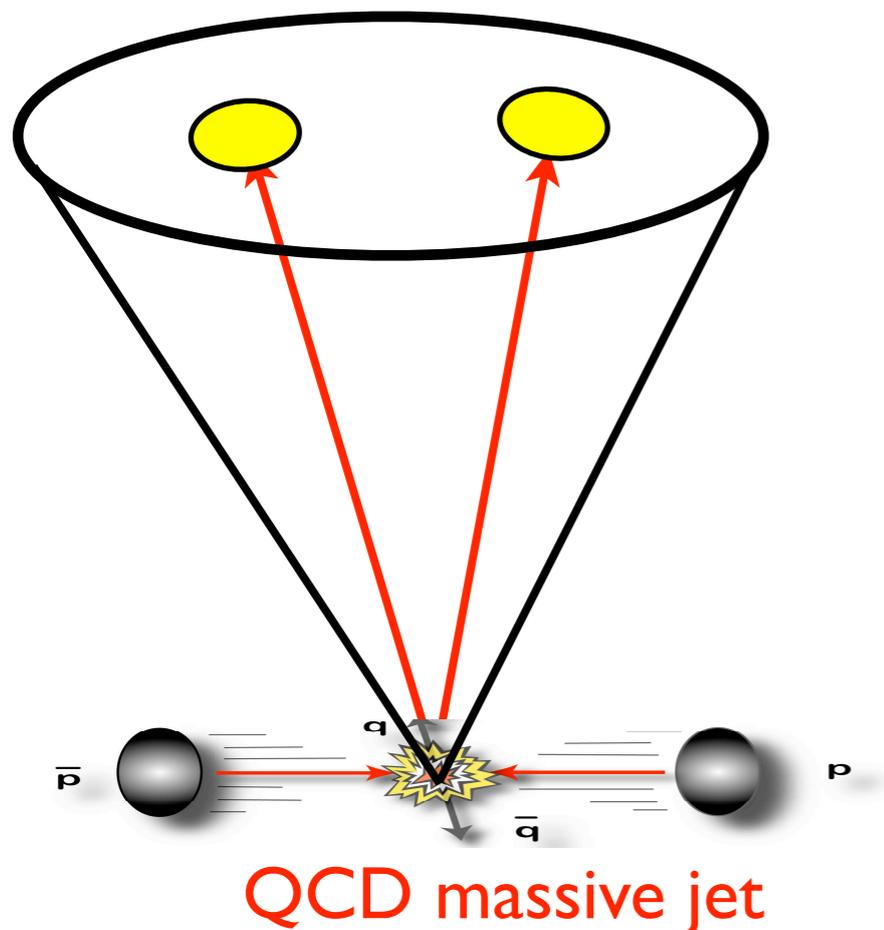


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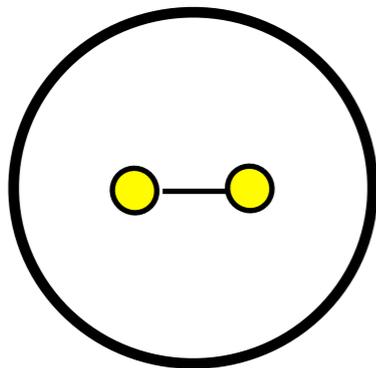
◆ Planar flow, Pf , measures the energy ratio between two primary axes of cone surface:

(i) “moment of inertia”:

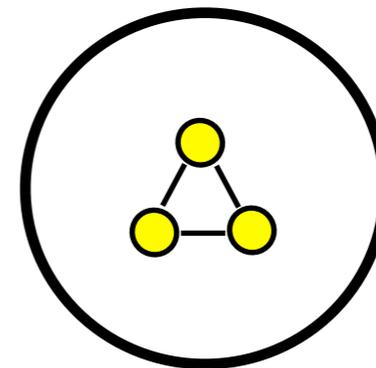
$$I_E^{kl} = \frac{1}{m_J} \sum_{i \in R} E_i \frac{p_{i,k}}{E_i} \frac{p_{i,l}}{E_i},$$

(ii) Planar flow:

$$Pf = 4 \frac{\det(\mathbf{I}_E)}{\text{tr}(\mathbf{I}_E)^2} = \frac{4\lambda_1\lambda_2}{(\lambda_1 + \lambda_2)^2}$$



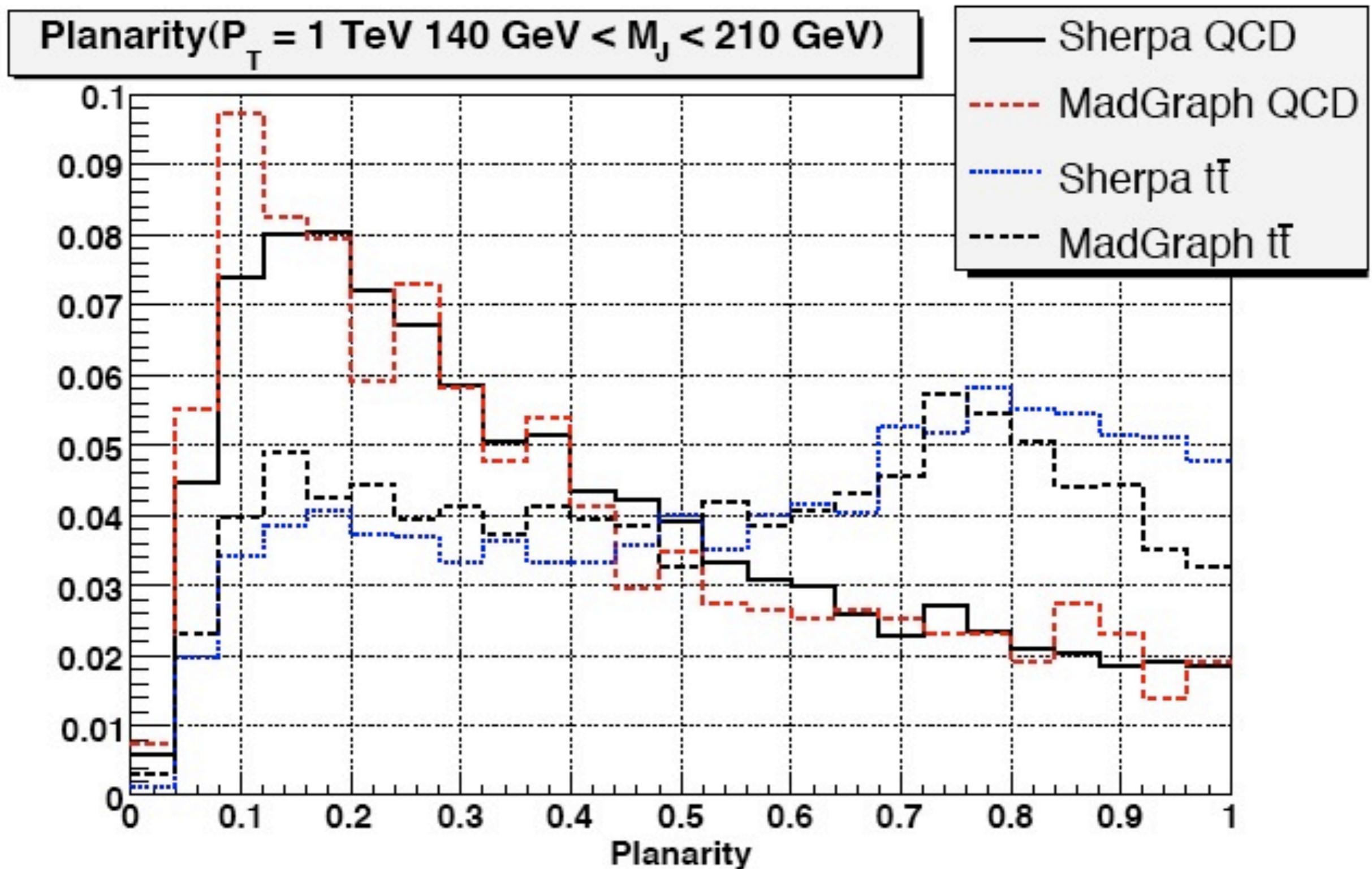
leading order QCD, $Pf=0$



top jet, $Pf=1$

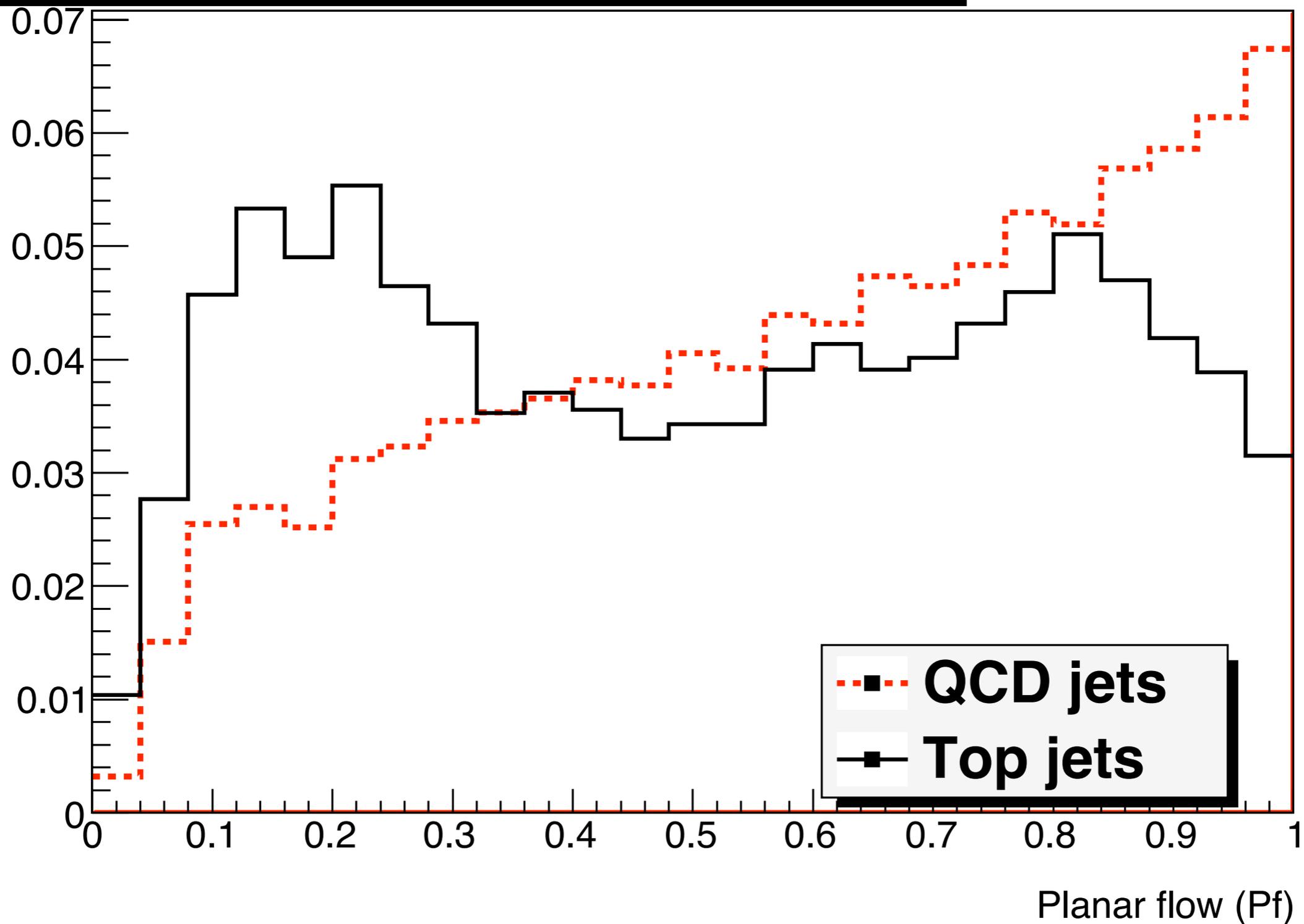
Planar flow, QCD vs top jets

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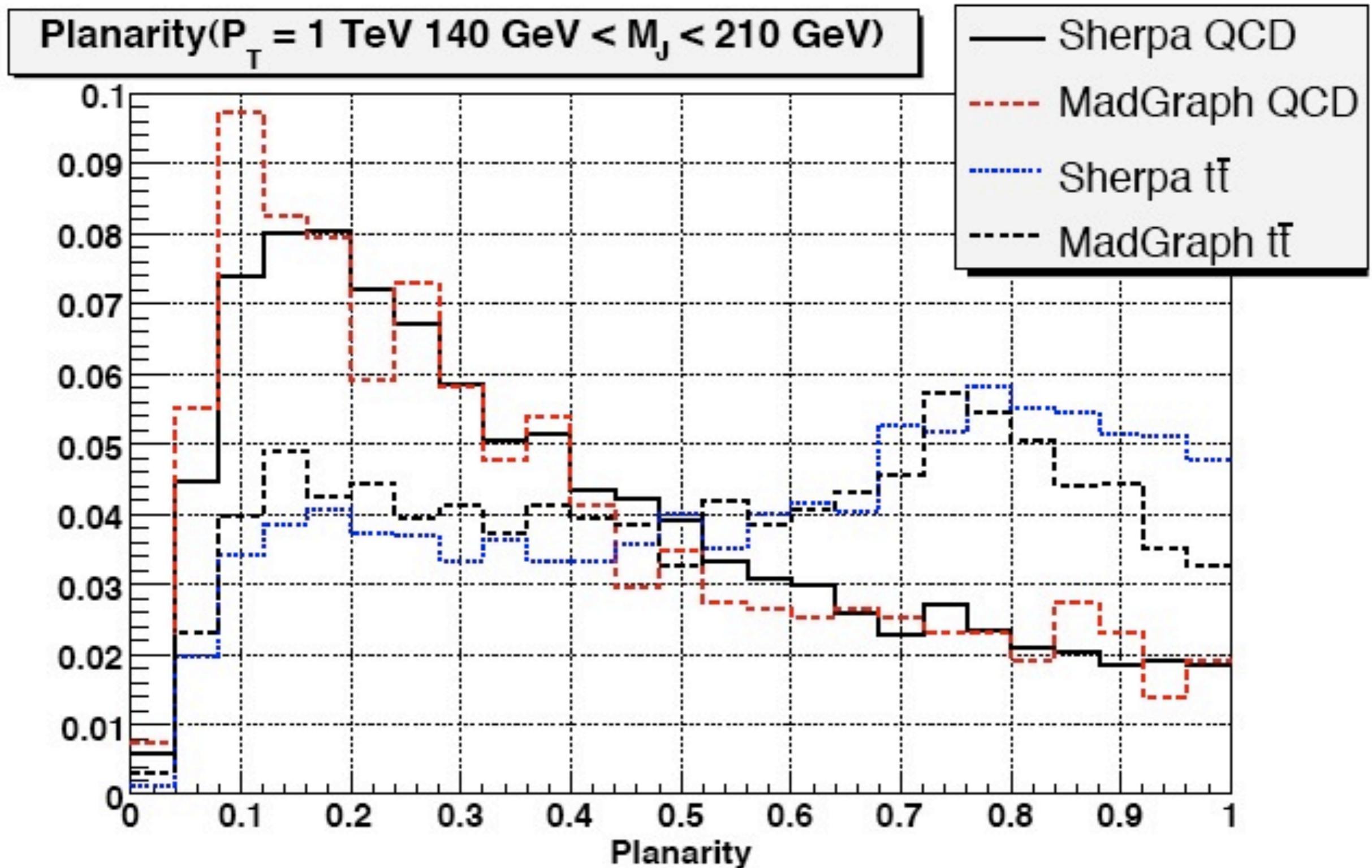


Planar flow, QCD vs top jets

Planar flow, Pf ($P_T = 1$ TeV, $R = 0.4$, "no mass cuts")

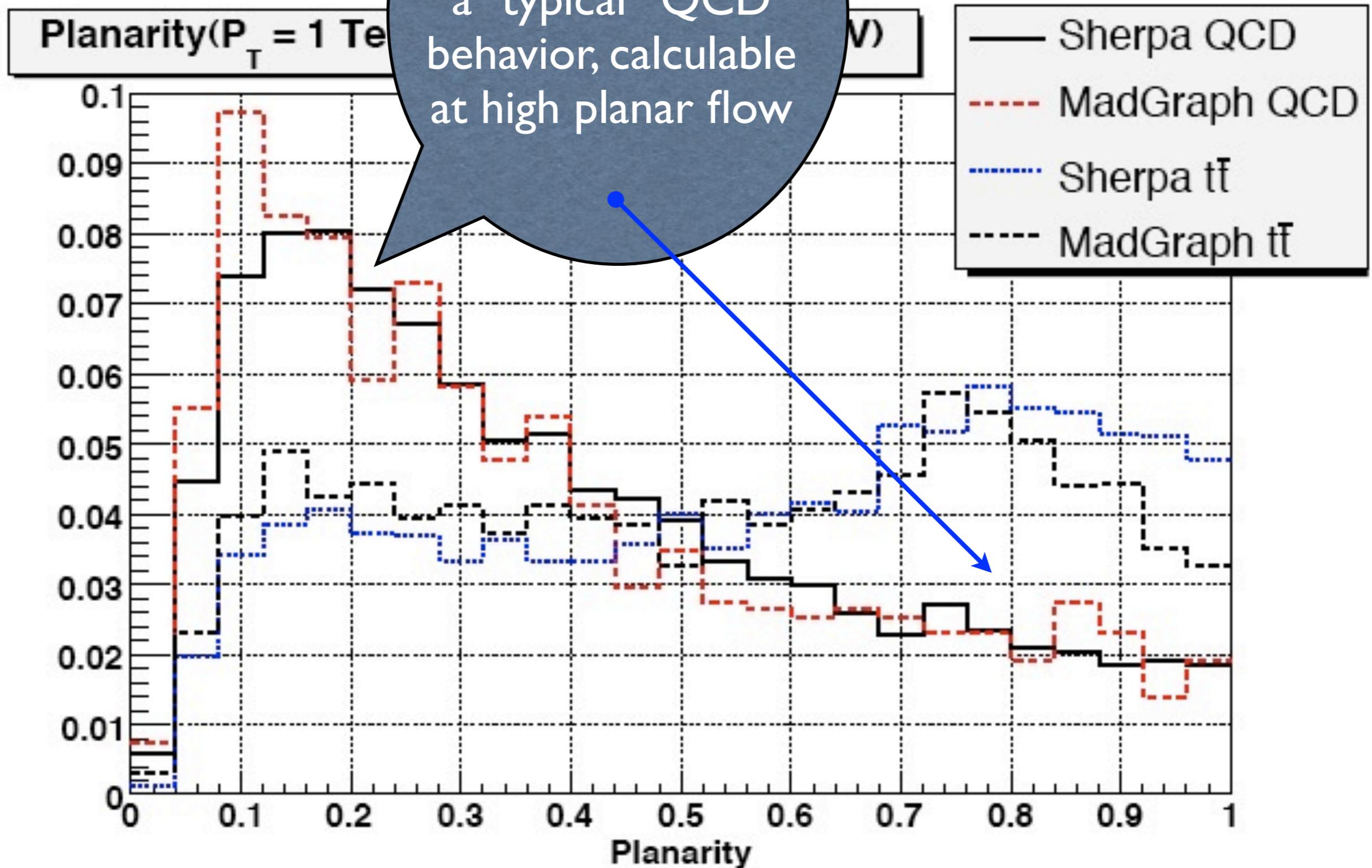


Planar flow, QCD vs top jets

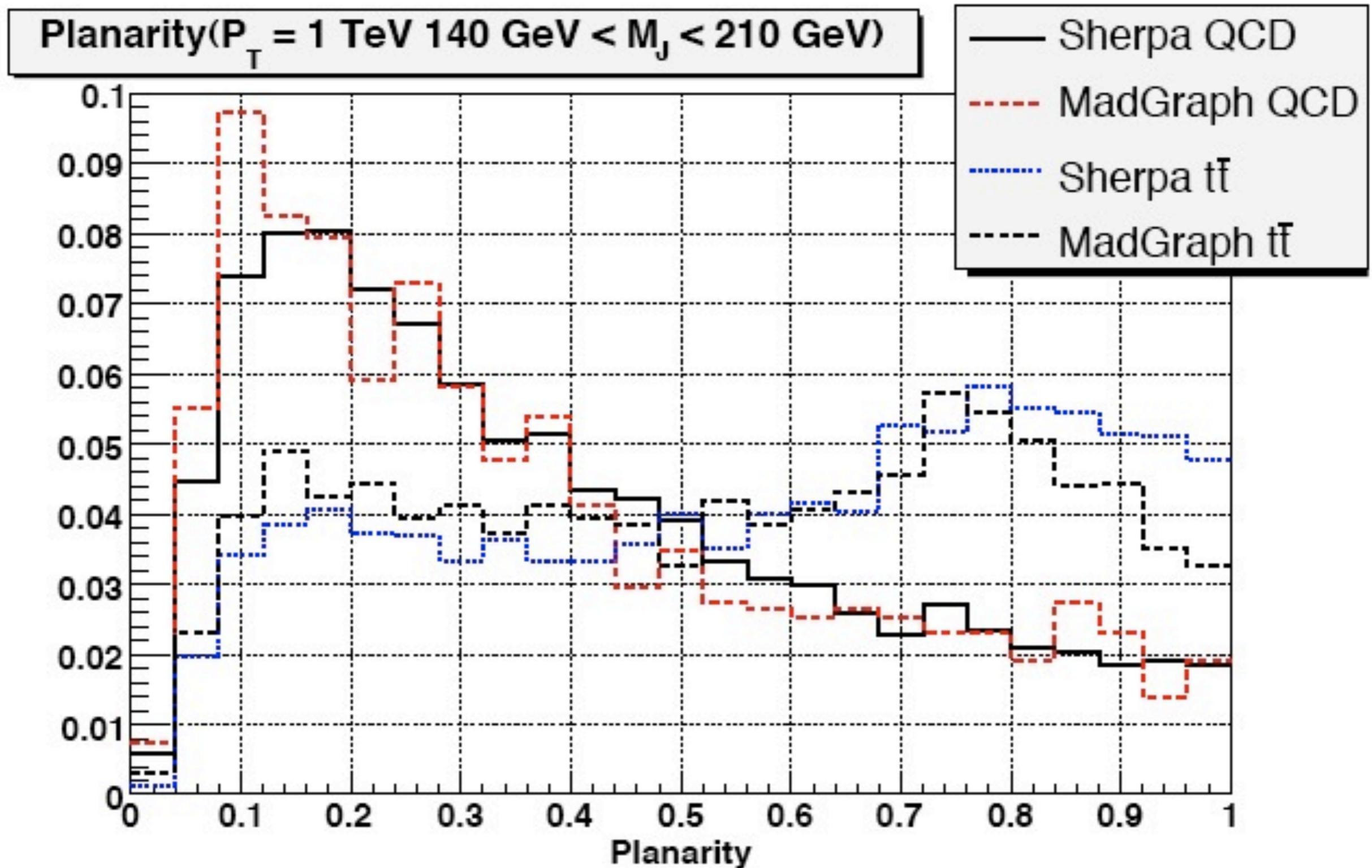


Planar flow in QCD vs top jets

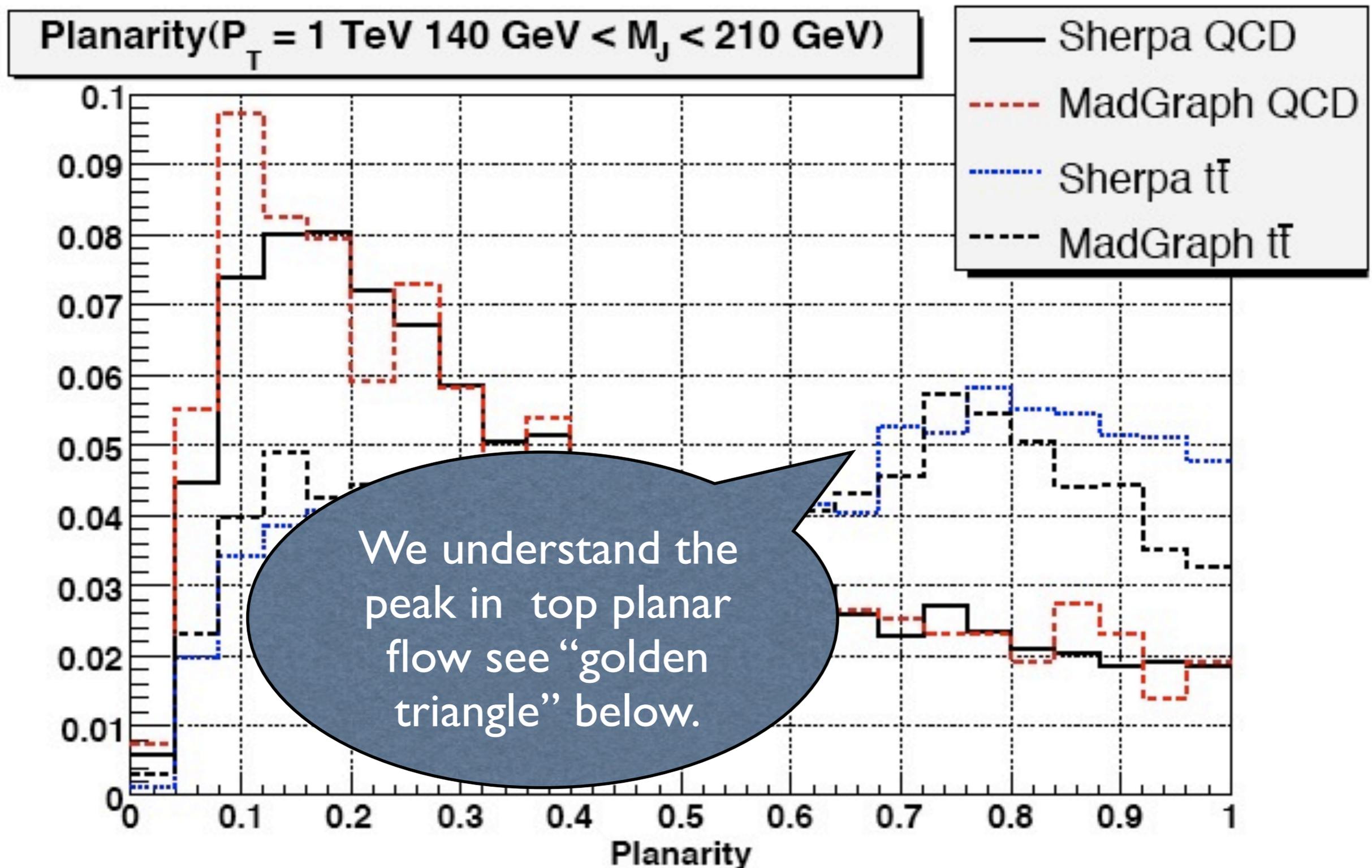
QCD
Planar flow shows
a “typical” QCD
behavior, calculable
at high planar flow



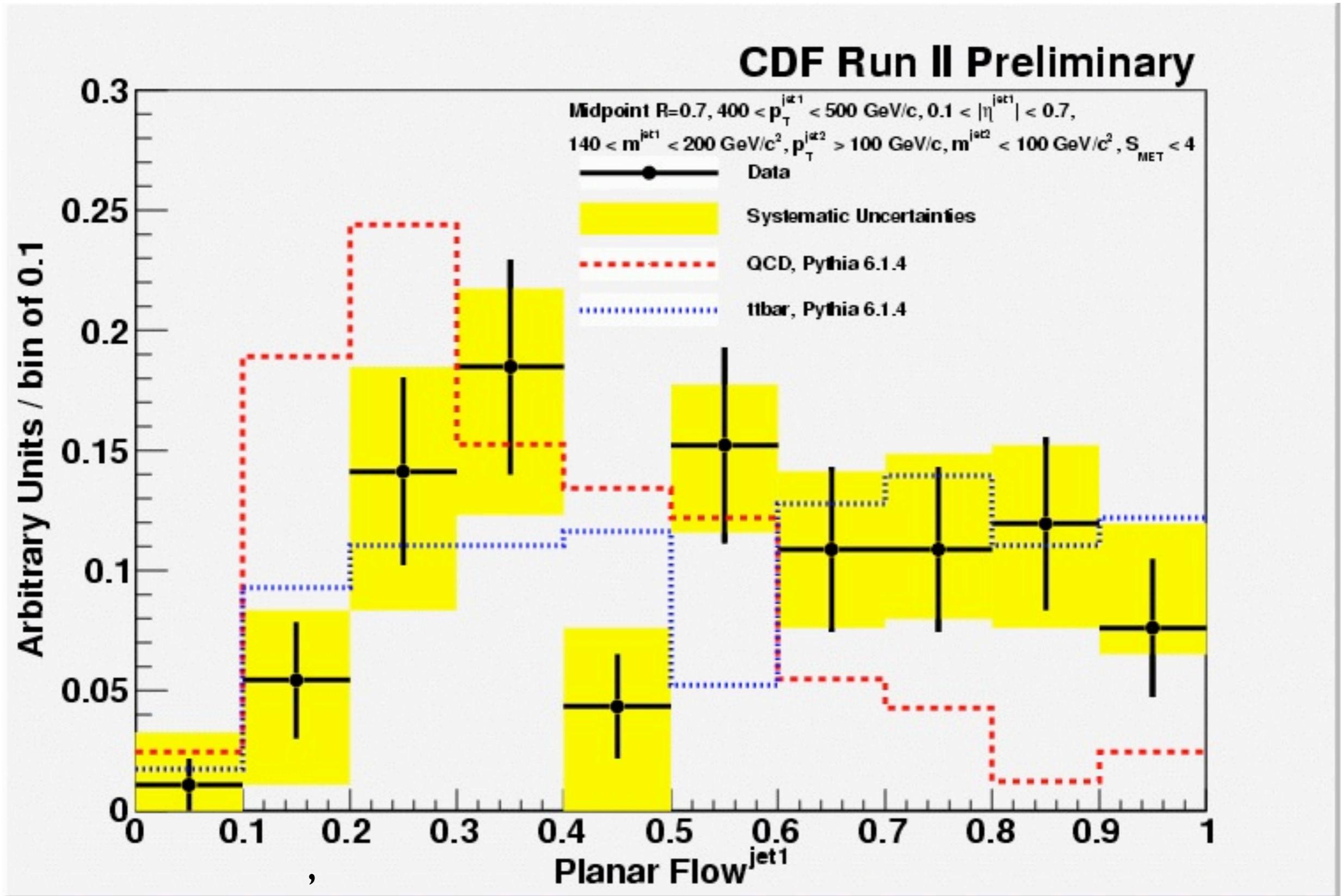
Planar flow, QCD vs top jets



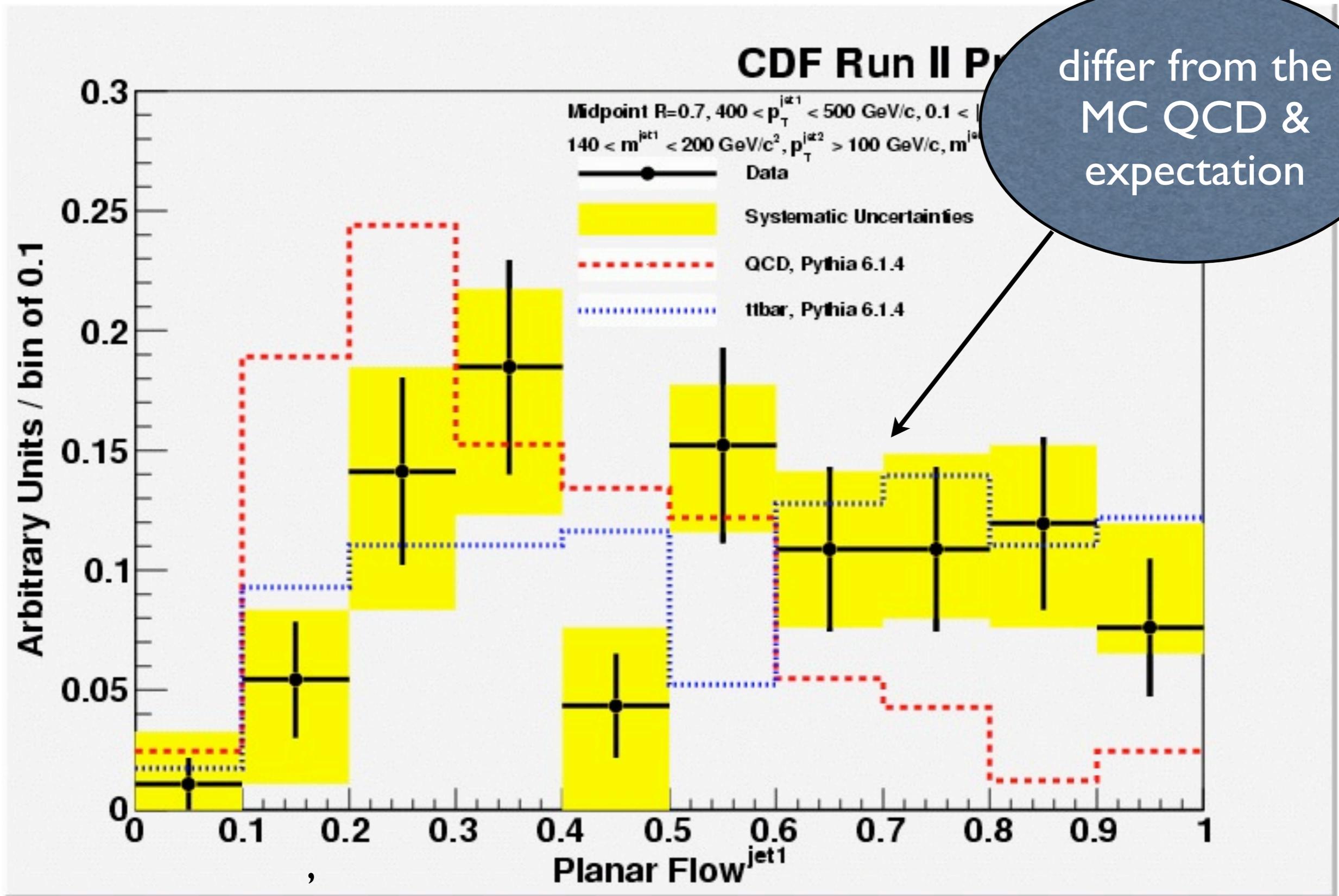
Planar flow, QCD vs top jets



Planar flow



Planar flow



Constraining New Physics

R, Alon, E. Duchovni, G. Perez & P. Sinervo, for the CDF, CDFANAL\TOP\PUBLIC
\10234.

Best known bound on energetic tops:

Boosted Top ($p_T > 400$ GeV/c) Cross Section
Upper Limit

– 54 fb @ 95% C.L. (c.f. SM prediction: 4.5 fb)

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Initial Result from CDF

R. Alon, E. Duchovni, G. Perez and P. Sinervo, for the CDF.

**Total Number of Observed Events in Signal
Region**

103

**Predicted Background from QCD Jets in Signal
Region**

$76 \pm 10(\text{stat})^{+26}_{-20}(\text{syst})$

**Expected Number of $t\bar{t}$ Events in Signal
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5.75 ± 0.72

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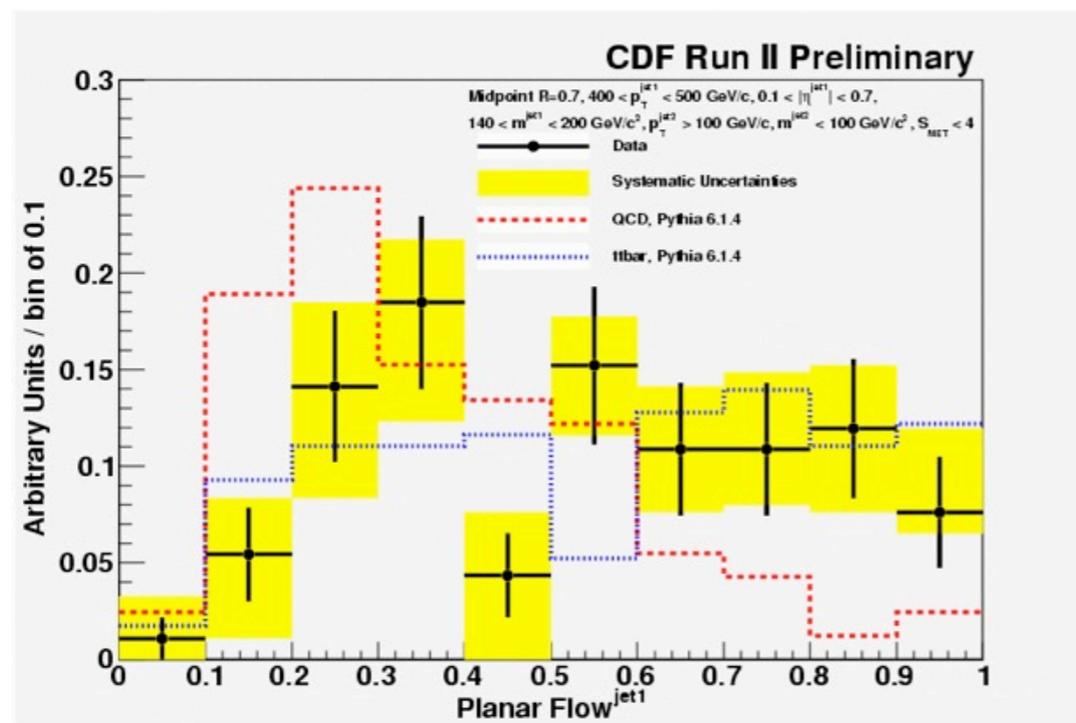
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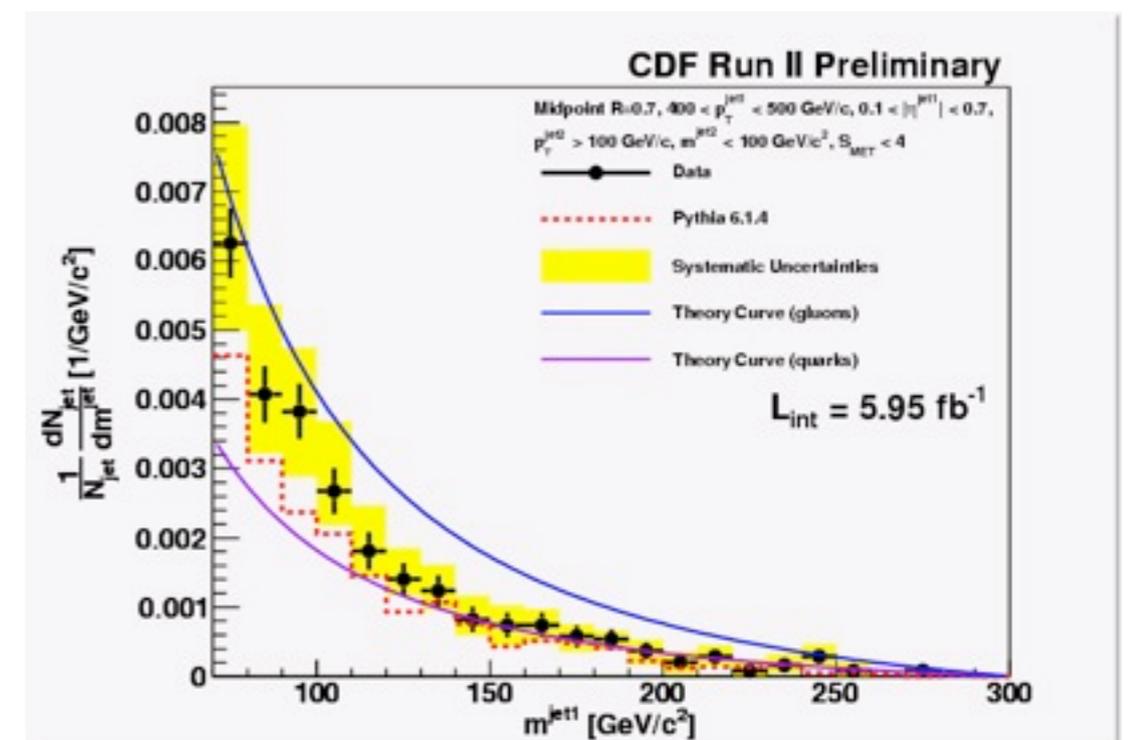
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Planar flow



Jet mass distribution



Initial Result from CDF

R. Alon, E. Duchovni, G. Perez and P. Sinervo, for the CDF.

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103

Predicted Background from QCD Jets in Signal Region

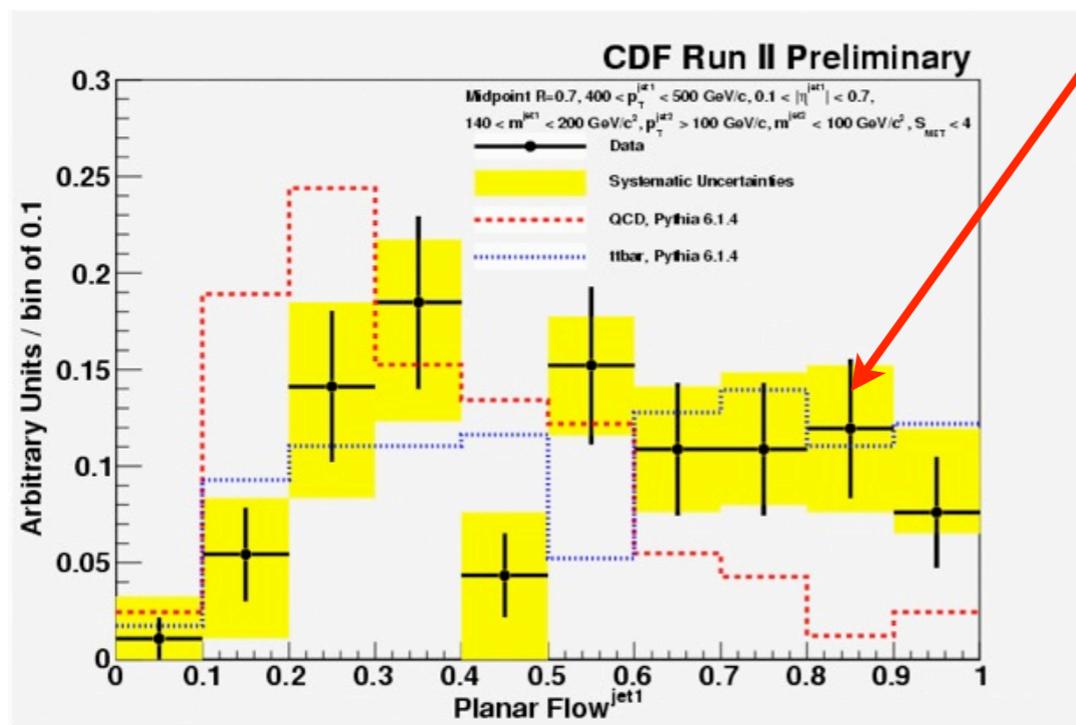
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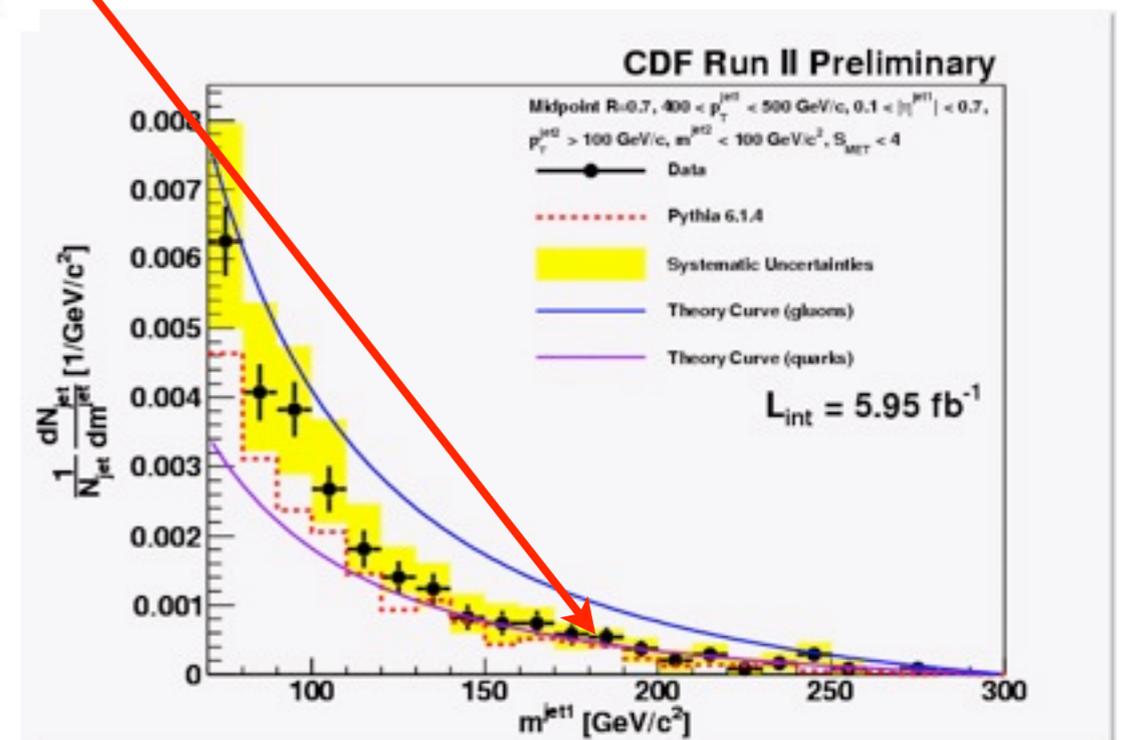
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Planar flow



Jet mass distribution



Initial Result from CDF

R. Alon, E. Duchovni, G. Perez and P. Sinervo, for the CDF.

Total Number of Signal

Predicted Signal

Expected Signal

see Cédric Delaunay's talk on Friday for a possible NP explanation

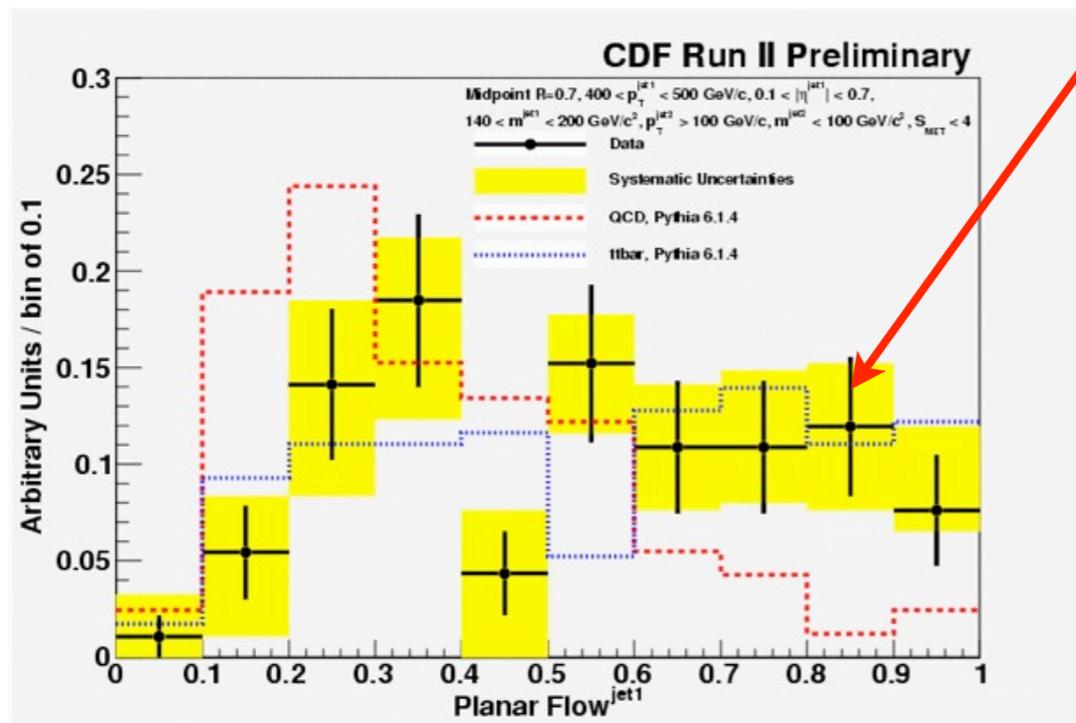
103

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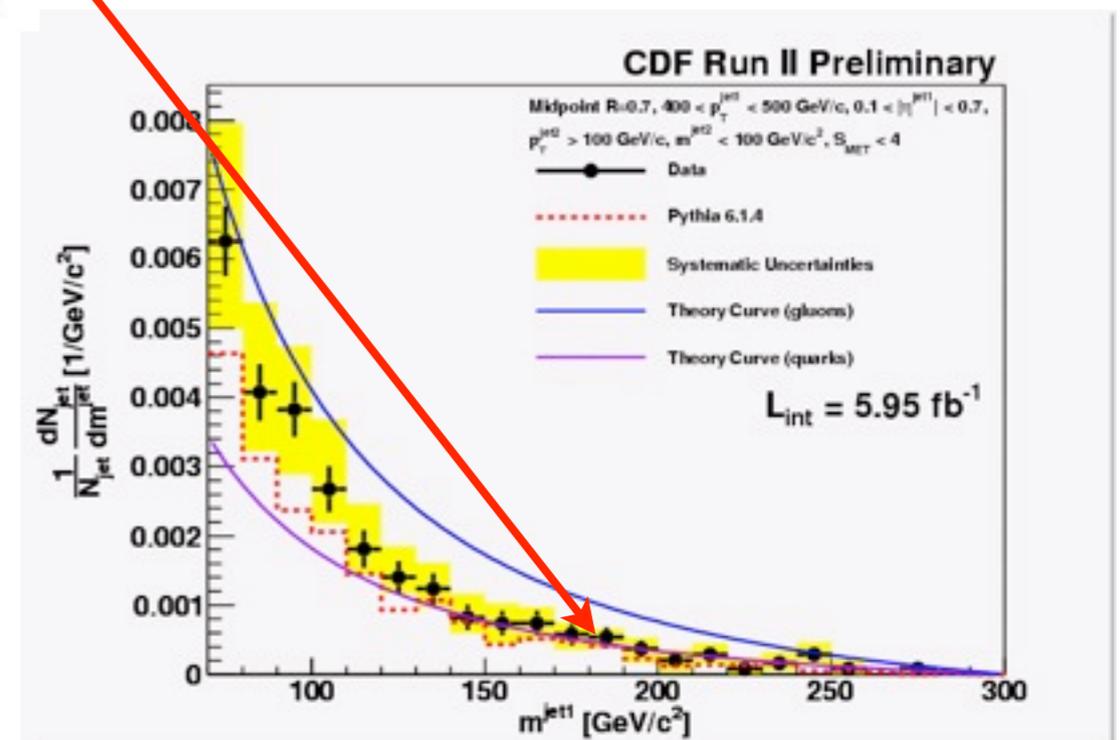
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Planar flow



Jet mass distribution



Template Overlap Method

- ◆ Planar flow is a single variable in a 4D 3-body kinematical-variable phase-space => info' is lost.

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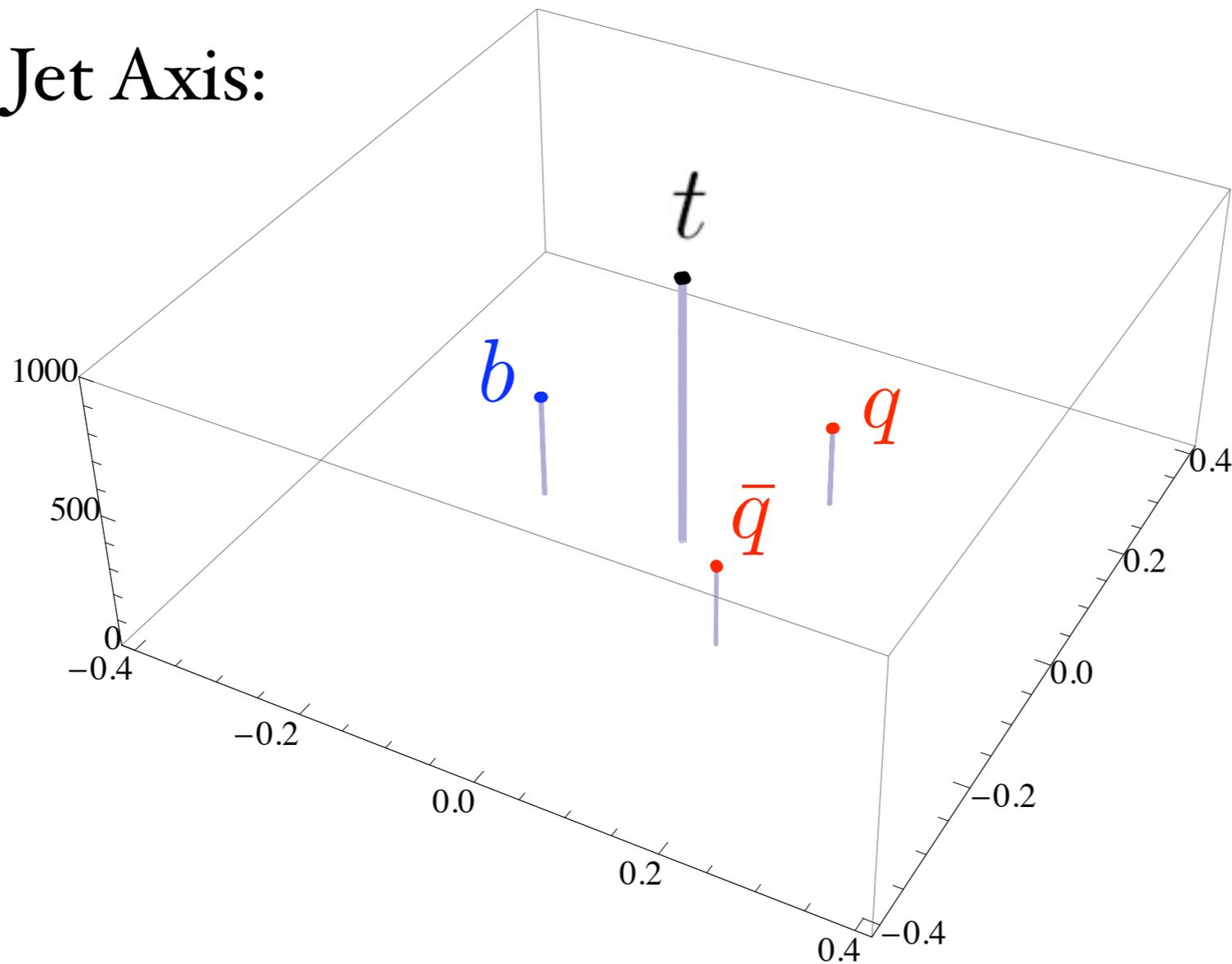
- ◆ Planar flow is a single variable in a 4D 3-body kinematical-variable phase-space => info' is lost.
- ◆ Can we be more systematic in our approach?
- ◆ Energy flow is a natural language for the description of jet structure:

Jet cross sections are naturally described in terms of correlation functions of energy flow

Example: The Golden Triangle

$$E(\hat{p}_x, \hat{p}_y)$$

Plane \perp to Jet Axis:



Template Overlap Method

◆ **Template overlaps**: functional measures that quantify how well the energy flow of a physical jet matches the flow of a boosted partonic decay

$|j\rangle$ = set of particles or calorimeter towers that make up a jet. e.g.
 $|j\rangle = |t\rangle, |g\rangle, \text{etc}$, where:

$|t\rangle =$ top distribution

$|g\rangle =$ massless QCD distribution

Lunch table
discussion with
Juan
Maldacena

We need a probe distribution, $|f\rangle$, such that

“template”

$$R = \left(\frac{\langle f|t\rangle}{\langle f|g\rangle} \right) \text{ is maximized.}$$

general overlap functional: $ov(j, f) = \langle j|f\rangle = \mathcal{F} \left[\frac{dE(j)}{d\Omega}, \frac{dE(f)}{d\Omega} \right]$

Template Overlap Method

◆ Any region of partonic phase space for the boosted decays, $\{f\}$, defines a template

◆ our ansatz: a good (if not the best) rejection power is obtained when we use the signal distribution itself to construct our templates

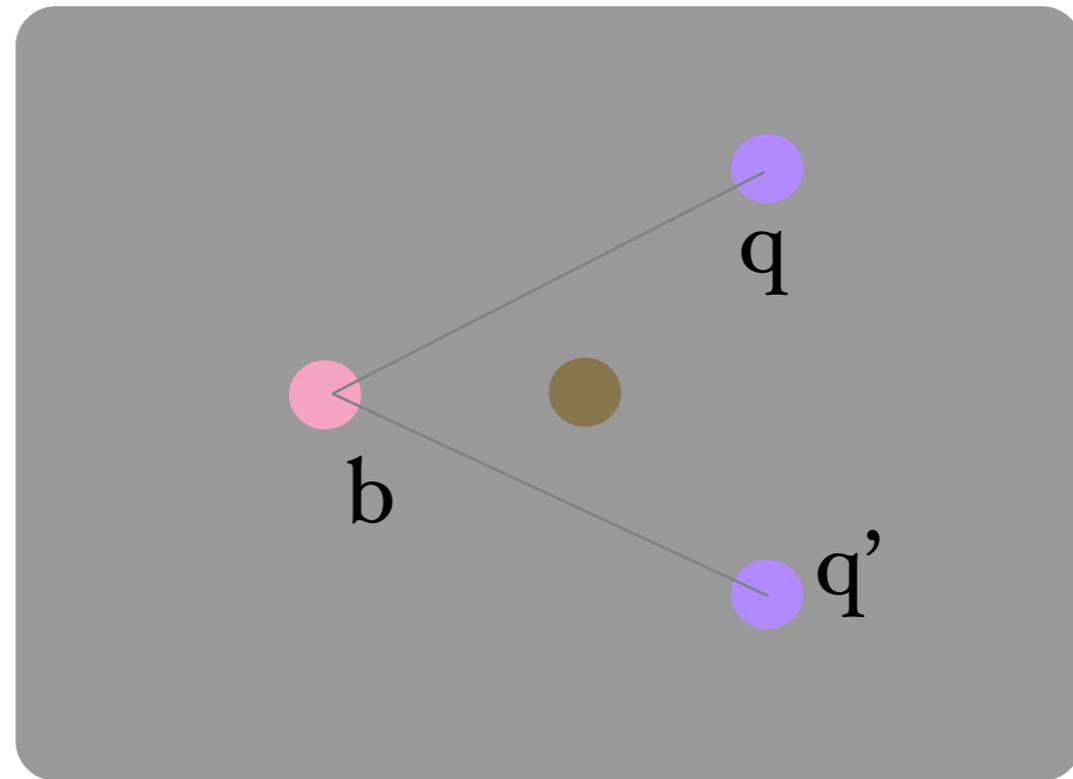
◆ Define “**template overlap**” as the **maximum** functional overlap of j to a state $f[j]$:

$$Ov(j, f) = \max_{\{f\}} \mathcal{F}(j, f)$$

◆ can match unequivocally arbitrary final states j to partonic partners $f[j]$ at any given order

Template Overlap Method

Example:
Template Config. for top



Our templates will be a set of partonic momenta $f = p_1 \dots p_n$, with

$$\sum_{i=1}^n p_i = P, \quad P^2 = M^2,$$

Probe template configuration in the entire phase space

By weighting energy distribution on detector (EG),
by how close it is to our **Template** configuration

Constructing a functional

- ◆ A natural measure: weighted difference of their energy flows integrated over a region (simple example: Gaussian)

$$Ov^{(F)}(j, f) = \max_{\tau_n^{(R)}} \exp \left[-\frac{1}{2\sigma_E^2} \left(\int d\Omega \left[\frac{dE(j)}{d\Omega} - \frac{dE(f)}{d\Omega} \right] F(\Omega, f) \right)^2 \right]$$

n-particle phase space:

$$\tau_n^{(R)} \equiv \int \prod_{i=1}^n \frac{d^3 \vec{p}_i}{(2\pi)^3 2\omega_i} \delta^4(P - \sum_{i=1}^n p_i) \Theta(\{p_i\}, R)$$

IR safety: F should be a sufficiently smooth function of the angles for any template state f :

-we may choose F to be a normalized step function around the directions of the template momenta p_i

For a given template, with direction of particle a , \hat{n}_a and its energy $E_a^{(f)}$:

$$Ov(j, p_1 \dots p_n) = \max_{\tau_n^{(R)}} \exp \left[-\sum_{a=1}^n \frac{1}{2\sigma_a^2} \left(\int d^2 \hat{n} \frac{dE(j)}{d^2 \hat{n}} \theta(\hat{n}, \hat{n}_a^{(f)}) - E_a^{(f)} \right)^2 \right]$$

for an n-particle final state

Three-particle Templates and Top Decay

◆ **Construct template:** three particle phase space for top decay

$$t \rightarrow b + W \rightarrow b + q + \bar{q}.$$

with $(p_q + p_{\bar{q}})^2 = M_W^2$

4 d.o.f.: most straightforward method by 4 angles:

- 1) polar and azimuthal angles that define b and W directions in the top rest frame relative to the direction of the boost
- 2) polar and azimuthal angles that define q and $q_{\bar{}}$ directions relative to the boost axis from the W rest frame

Three-particle Templates and Top Decay

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Lorentz transformations \Rightarrow 4 angles identified above determine the energies and directions of the three decay products of the top at LO

Three-particle Templates and Top Decay

◆ jet mass window $160 \text{ GeV} < m_j < 190 \text{ GeV}$, cone size $R = 0.5$ ($D = 0.5$ for anti-kT jet), jet energy $950 \text{ GeV} < E_j < 1050 \text{ GeV}$.

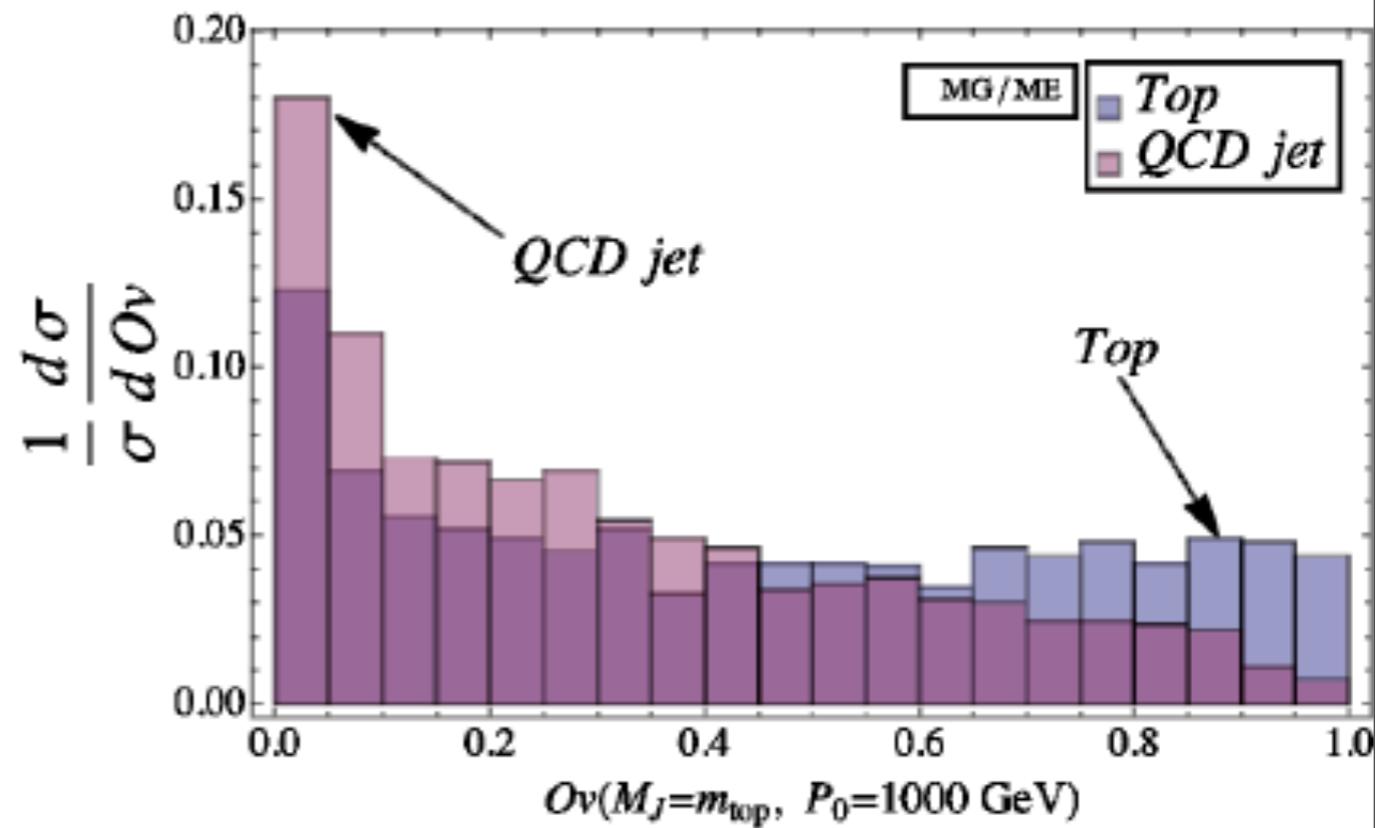
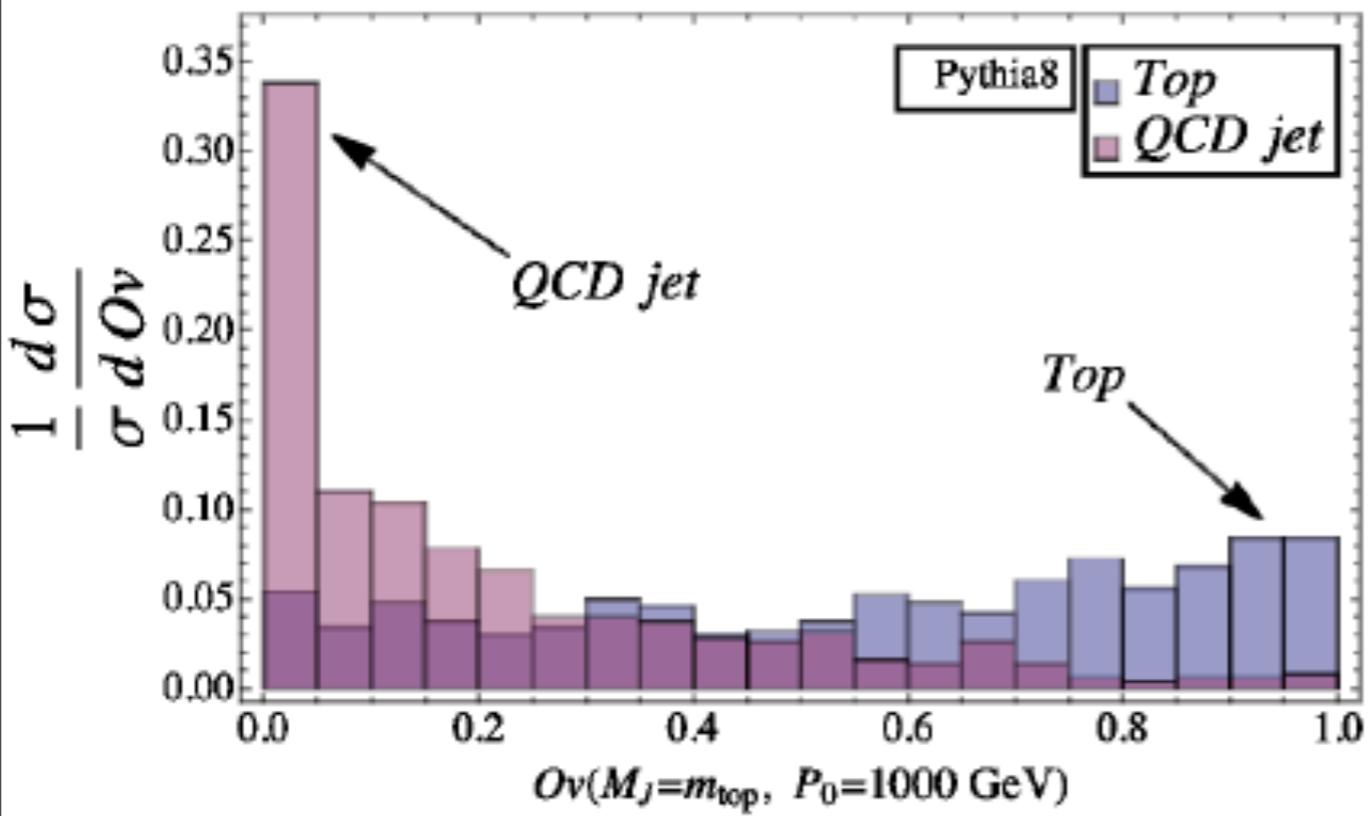
◆ Template Overlap with data discretization

$$Ov(j, f) = \max_{\tau_n^{(R)}} \exp \left[- \sum_{a=1}^3 \frac{1}{2\sigma_a^2} \left(\sum_{k=i_a-1}^{i_a+1} \sum_{l=j_a-1}^{j_a+1} E(k, l) - E(i_a, j_a)^{(f)} \right)^2 \right]$$

$$\sigma_a = E(i_a, j_a)^{(f)} / 2.$$

for data, we encode two physical angles in terms of row and column number

Three-particle Templates and Top Decay



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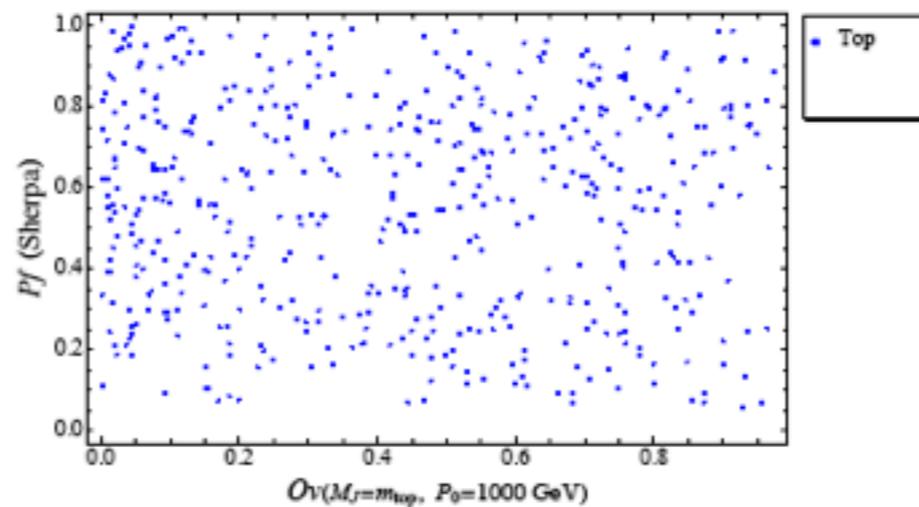
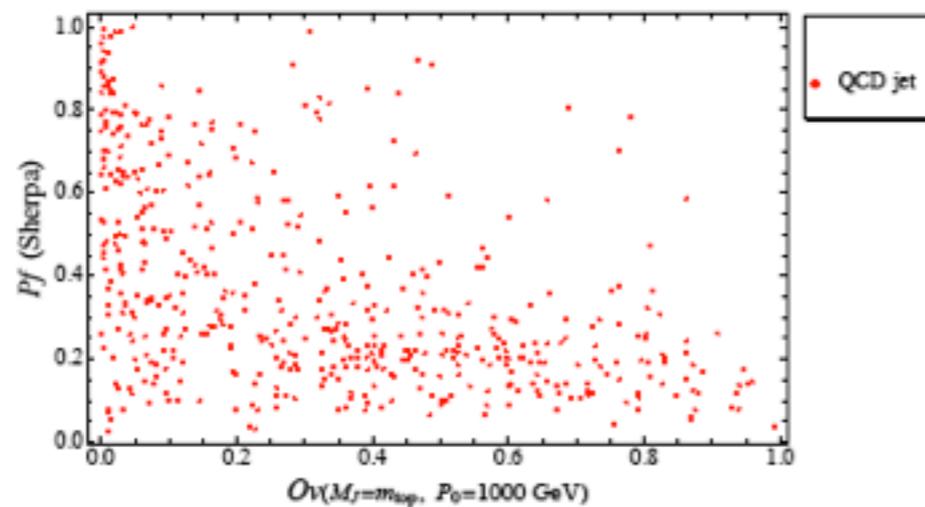
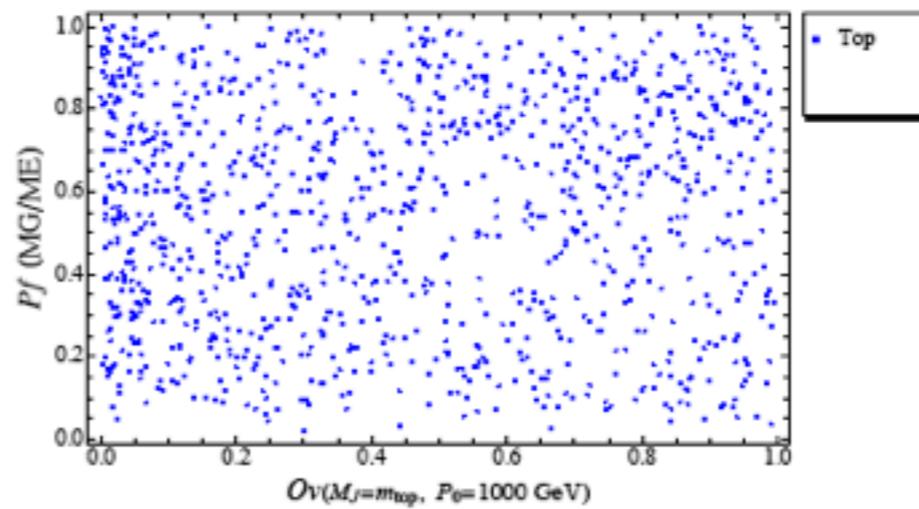
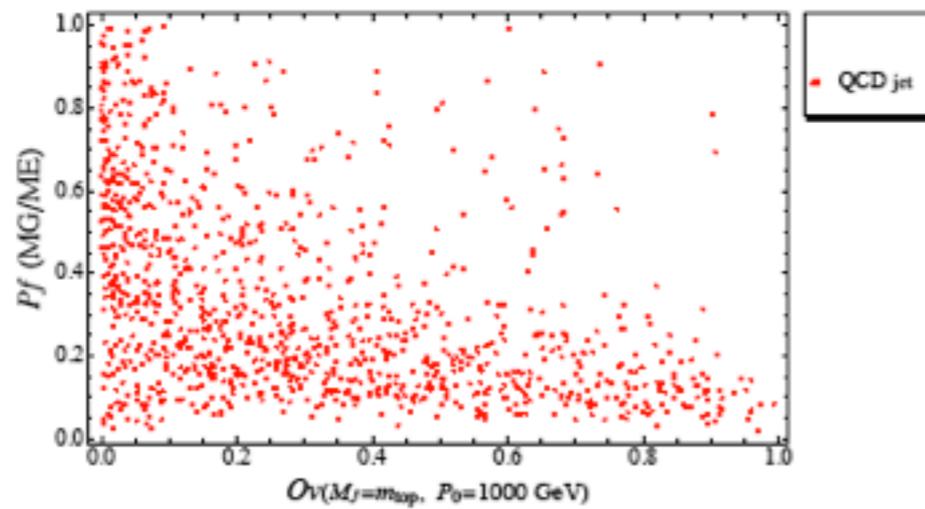
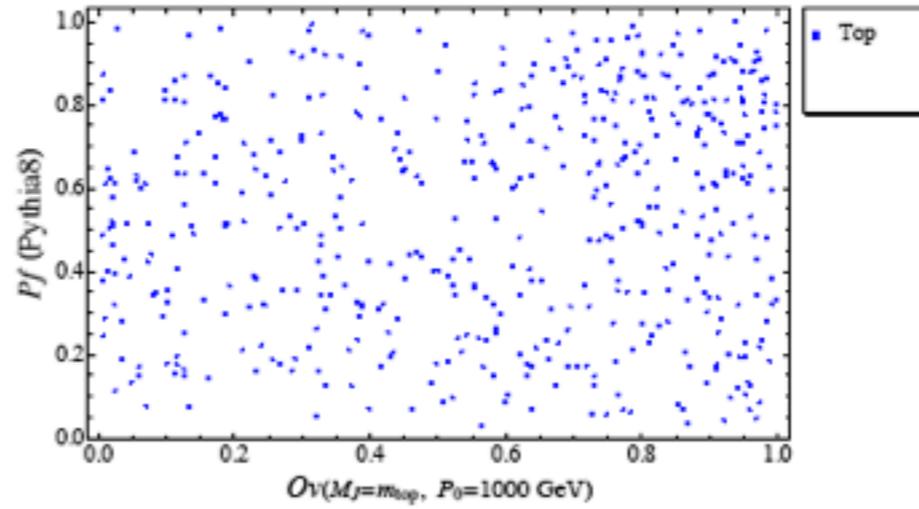
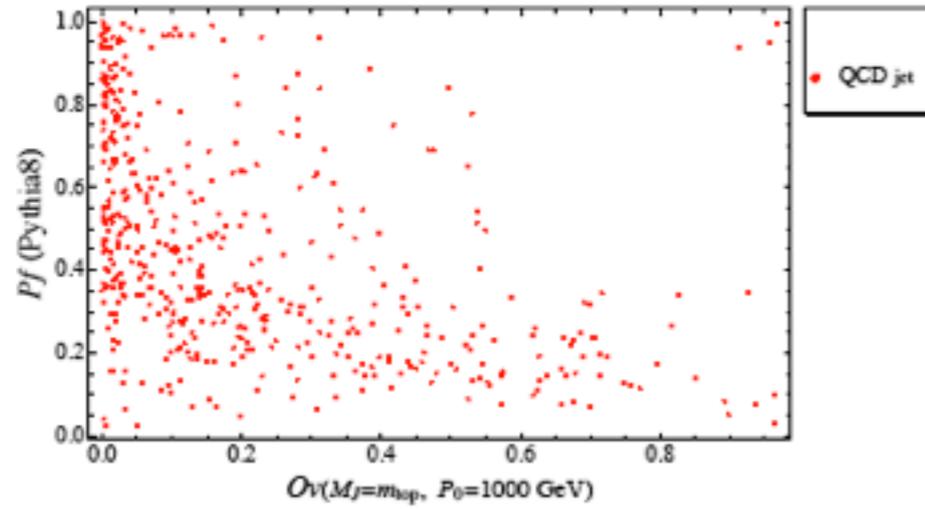
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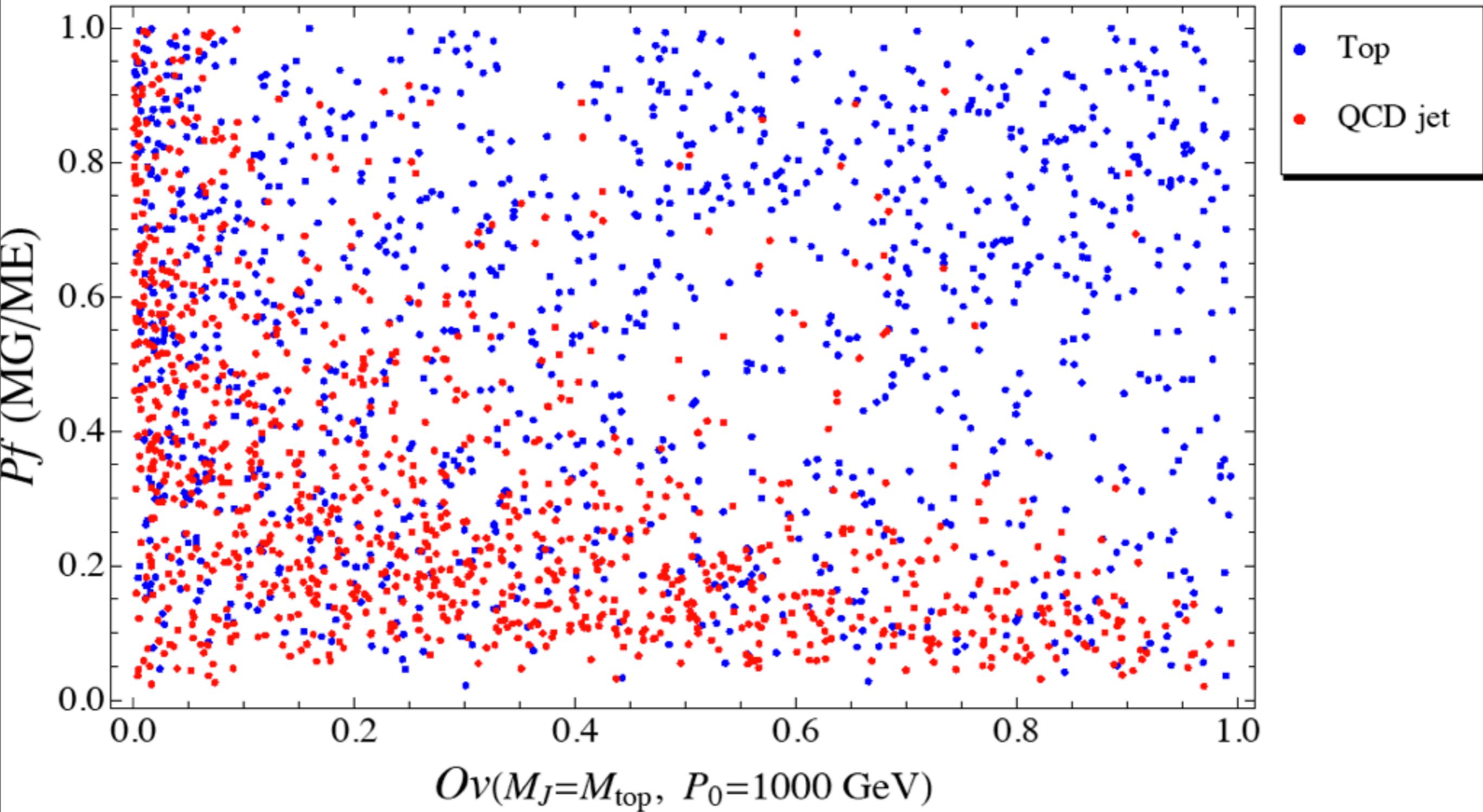
Three-particle Templates and Top Decay

- ◆ Combine with Planar flow-
distinguishes between many three-jet events with large template overlaps.
- ◆ In general, QCD events with large O_v will have significantly smaller planar flow than top decay events; for the QCD jets a large overlap would be a result of a kinematic “accident”.

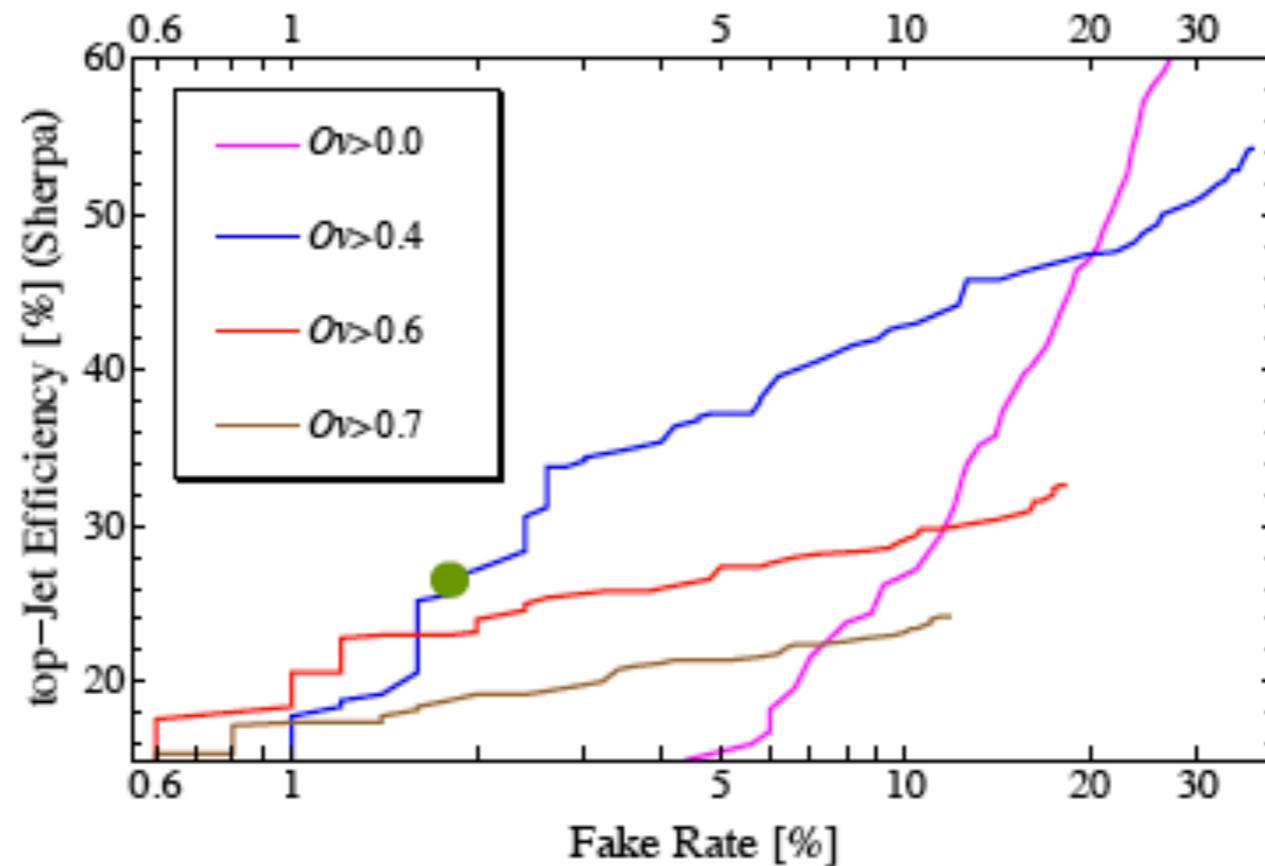
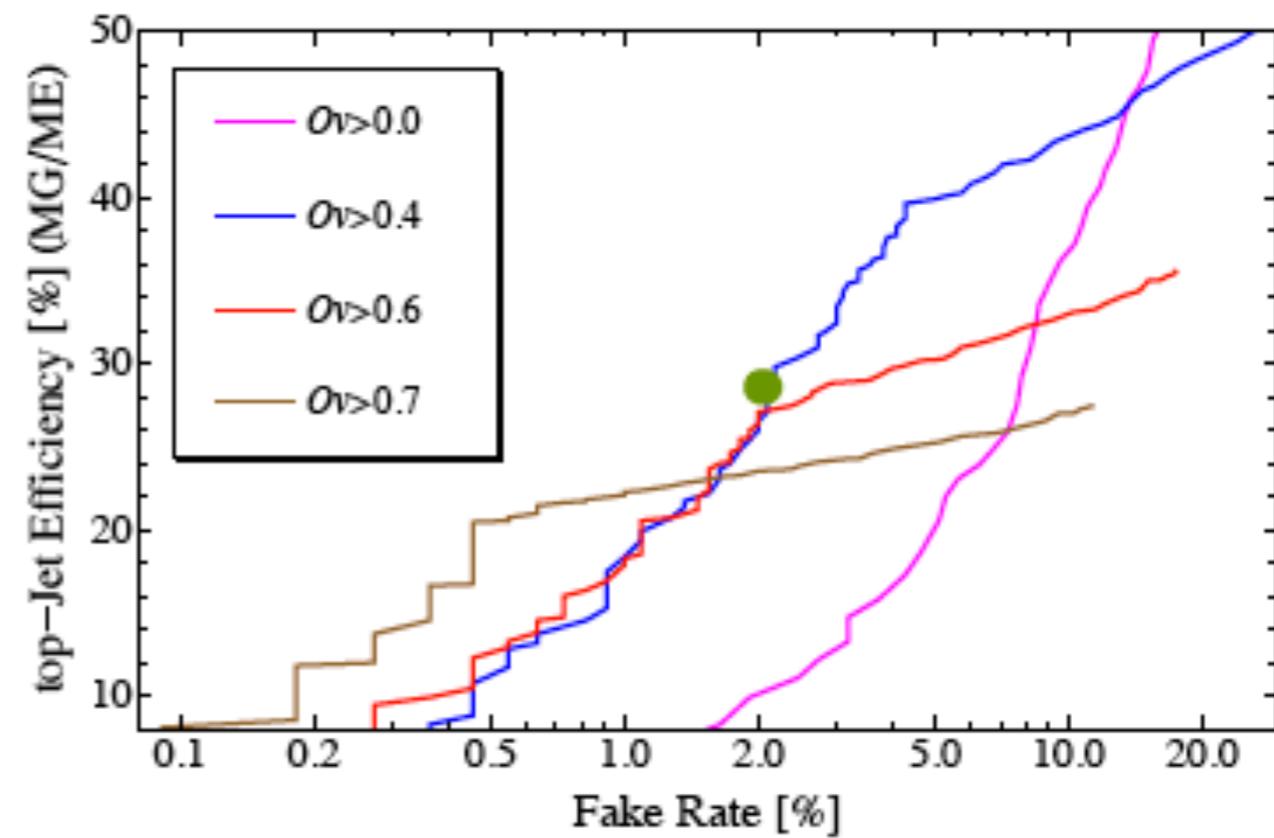
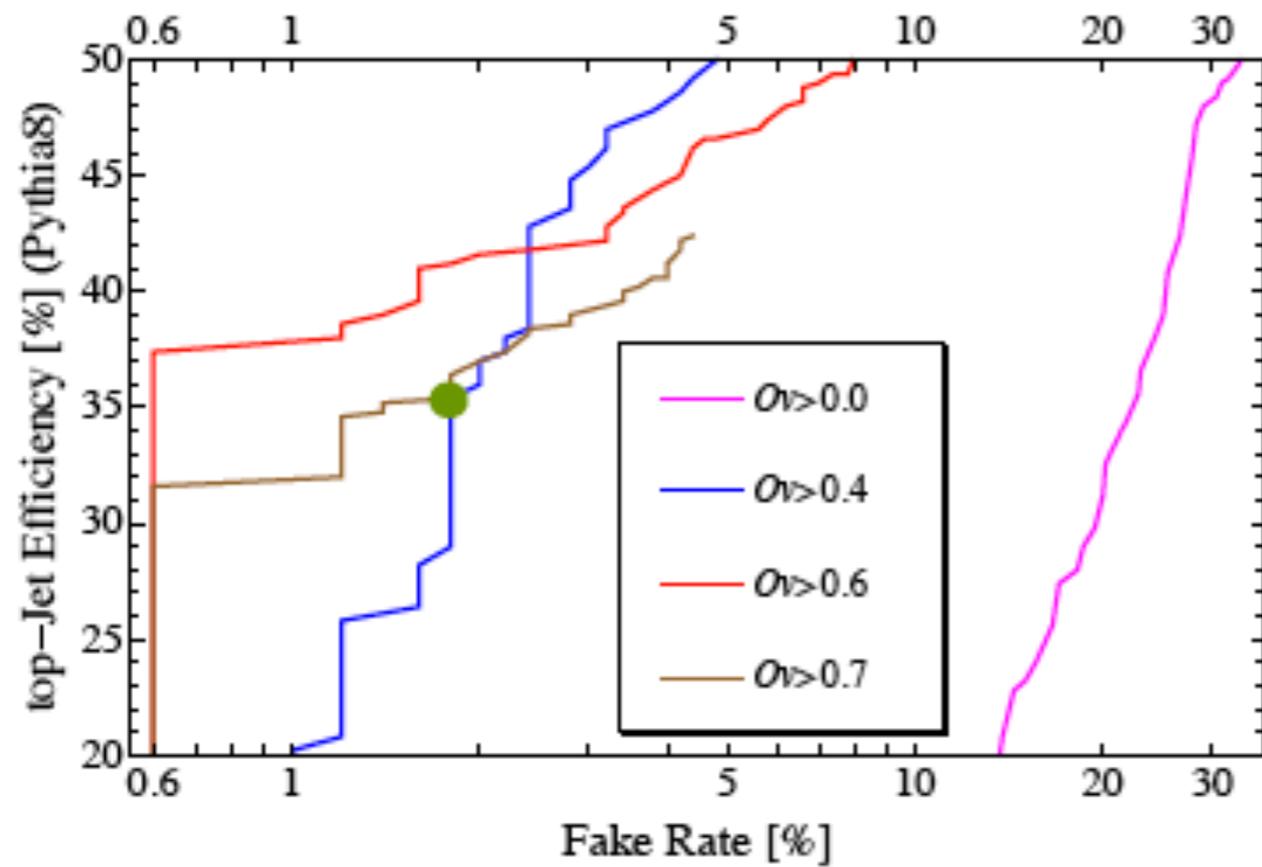
Three-particle Templates and Top Decay



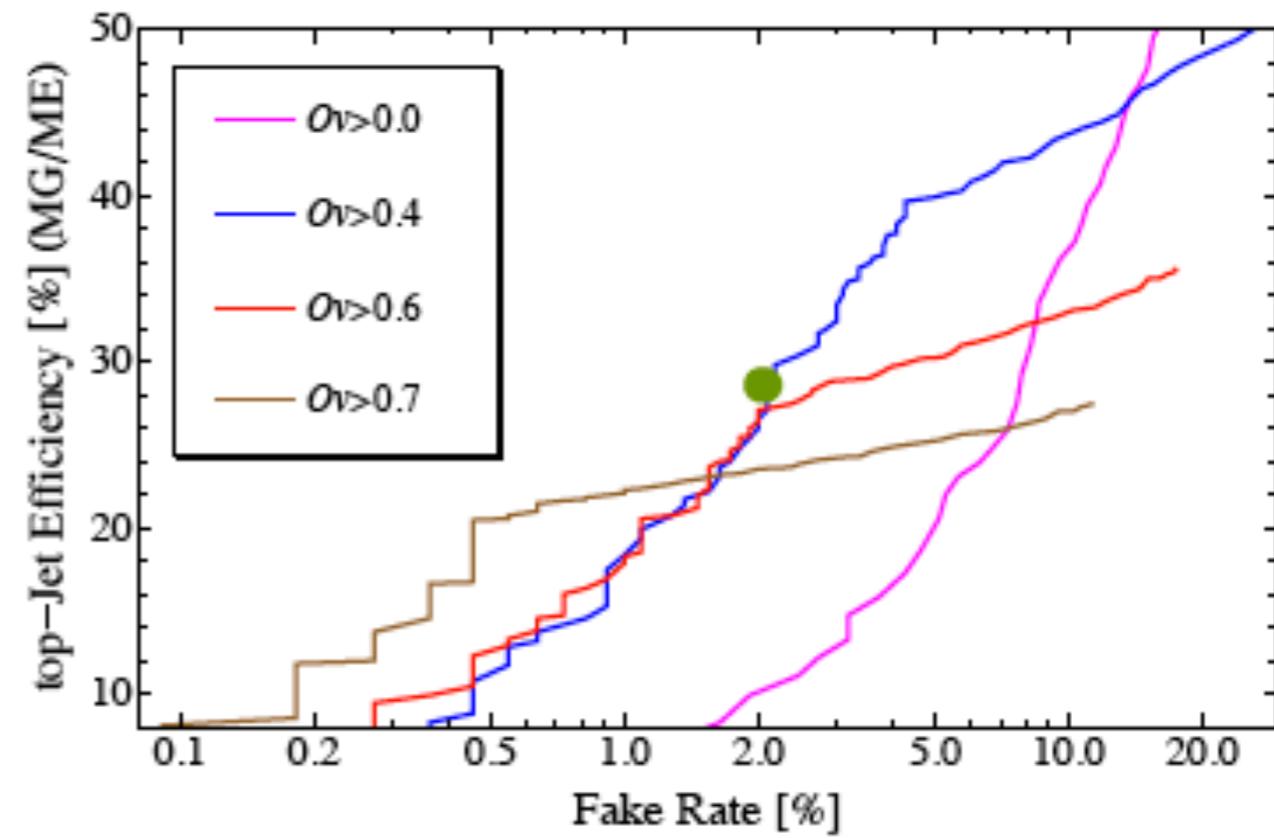
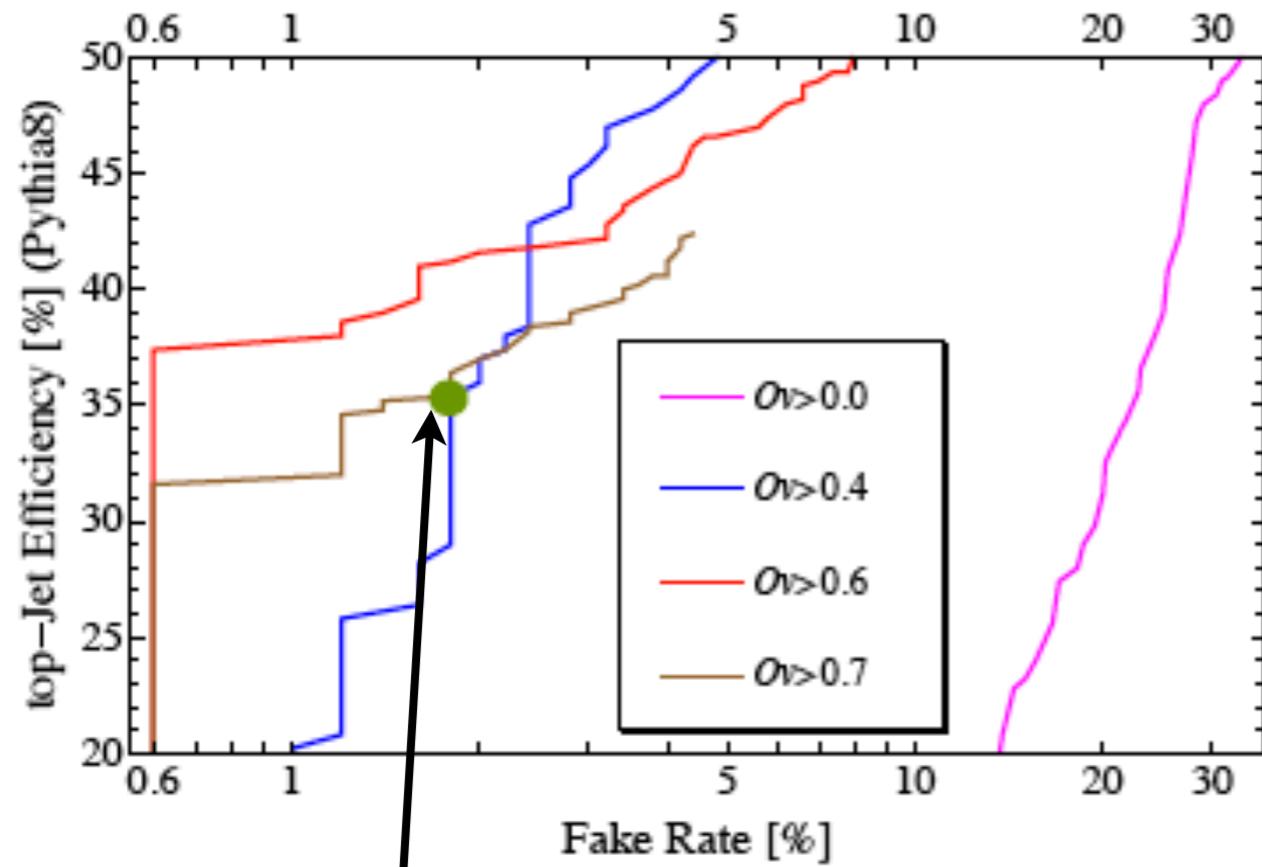
Three-particle Templates and Top Decay



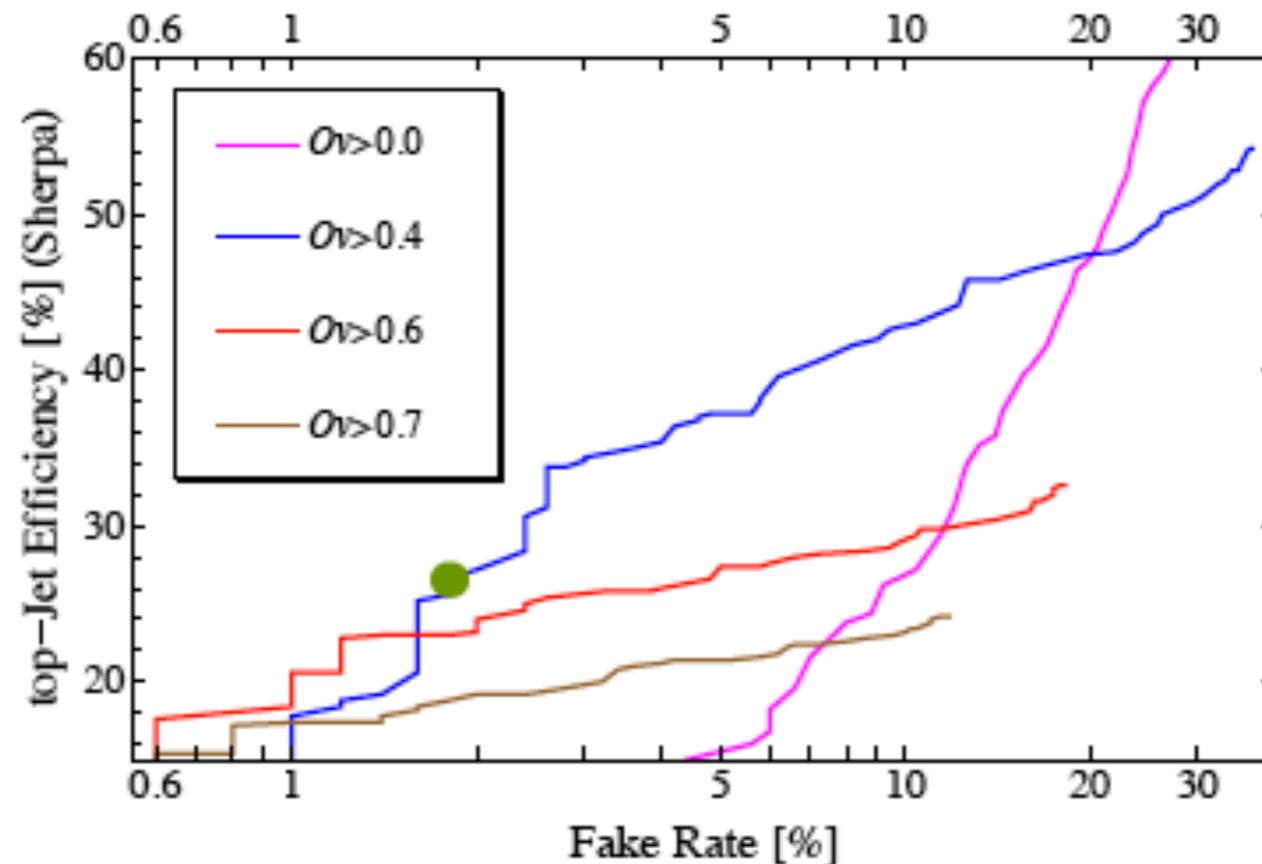
Three-particle Templates and Top Decay



Three-particle Templates and Top Decay



$Pf > 0.6$ and $Ov > 0.4$



Three-particle Templates and Top Decay

MC	Jet mass cut only		Mass cut + $ Ov + Pf$	
	Top-jet efficiency [%]	fake rate [%]	Top-jet efficiency [%]	fake rate [%]
Pythia8	58	3.6	21	0.022
MG/ME	52	3.7	11	0.017
Sherpa	34	3.2	7	0.032

Table 1: Efficiencies and fake rates for jets with $R = 0.5$ (using anti- k_T : $D = 0.5$), $95 \text{ GeV} \leq P_0 \leq 1050 \text{ GeV}$, $160 \text{ GeV} \leq m_J \leq 190 \text{ GeV}$ and $m_{top} = 174 \text{ GeV}$. The left pair of columns shows efficiencies and fake rates found by imposing the jet mass window only. The right pair takes into account the effects of cuts in Ov and Pf in addition to the mass window. For the different MC simulations, we have imposed various cuts on Ov and Pf variables: for Pythia8 $Ov \geq 0.6$ and $Pf \geq 0.4$, for MG/ME $Ov \geq 0.7$ and $Pf \geq 0.39$ and for Sherpa $Ov \geq 0.6$ and $Pf \geq 0.48$.

Three-particle Templates and Top Decay

MC	Jet mass cut only		Mass cut + Ov + Pf	
	Efficiency [%]	fake rate [%]	Efficiency [%]	fake rate [%]
Pythia8				0.022
MG/ME				0.017
Sherpa				0.02

Table 1: Efficiency of the top pair selection for $95 \leq P_0 \leq 105$ GeV. The first two columns show the efficiency of the right pair taking the top pair. For the different MCs, the efficiency is calculated for Pythia8 $Ov \geq 0.6$ and $Pf \geq 0.4$.

Rejection Power:
Pythia: 1 in 1000
MadGraph: 1 in 600
without optimization!

Fake Rate [%]

Three-particle Templates and Top Decay

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Three-particle Templates and Top Decay

- ◆ Template method provide a favorable rejection power compared to **other methods** (algorithm based jet-substructure)
- ◆ Template method is under theory control, while **other methods** depends on jet-reconstruction algorithm by removing soft jets (loosing theoretical handle)

Three-particle Templates and Top Decay

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Three-particle Templates and Top Decay

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◆ Can also optimize the cut for getting higher rejection power

Two-particle Templates and Higgs Decay

◆ Construct template: two particle phase space for Higgs decay

$$|f\rangle = |h\rangle^{(\text{LO})} = |p_1, p_2\rangle$$

◆ Higgs: at fixed $z = m_j/P_0 \ll 1$, θ_s distribution is peaked around θ_s in its minimum value
=> decays “democratic” (sharing energy evenly)

$$\frac{dJ^h}{d\theta_s} \propto \frac{1}{\theta_s^3}$$

◆ lowest-order QCD events is also peaked, but much less so

$$\frac{dJ^{\text{QCD}}}{d\theta_s} \propto \frac{1}{\theta_s}$$

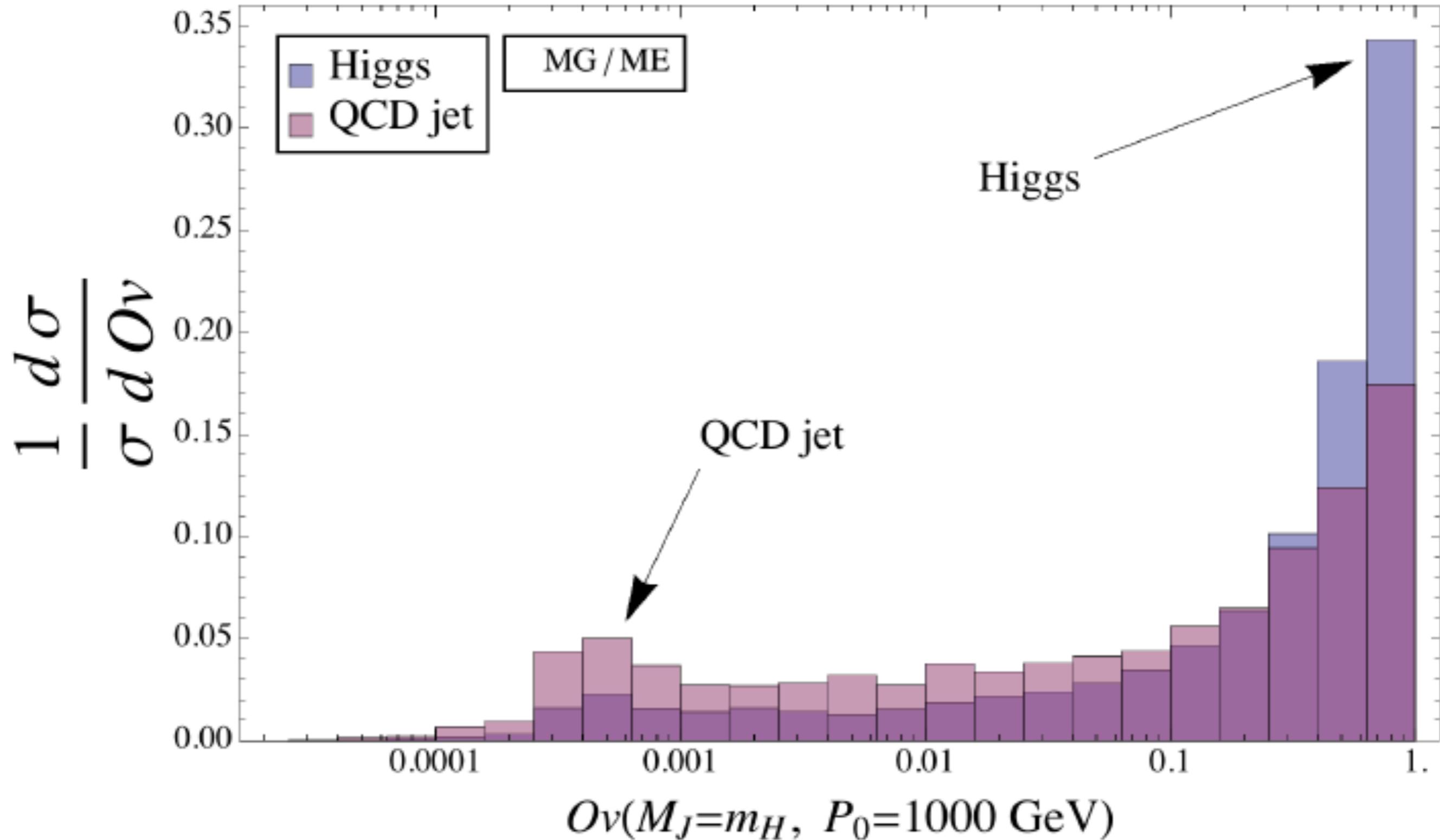
Two-particle Templates and Higgs Decay

◆ jet mass window $110 \text{ GeV} < m_j < 130 \text{ GeV}$, cone size $R = 0.4$ ($D = 0.4$ for anti-kT jet), jet energy $950 \text{ GeV} < E_j < 1050 \text{ GeV}$.

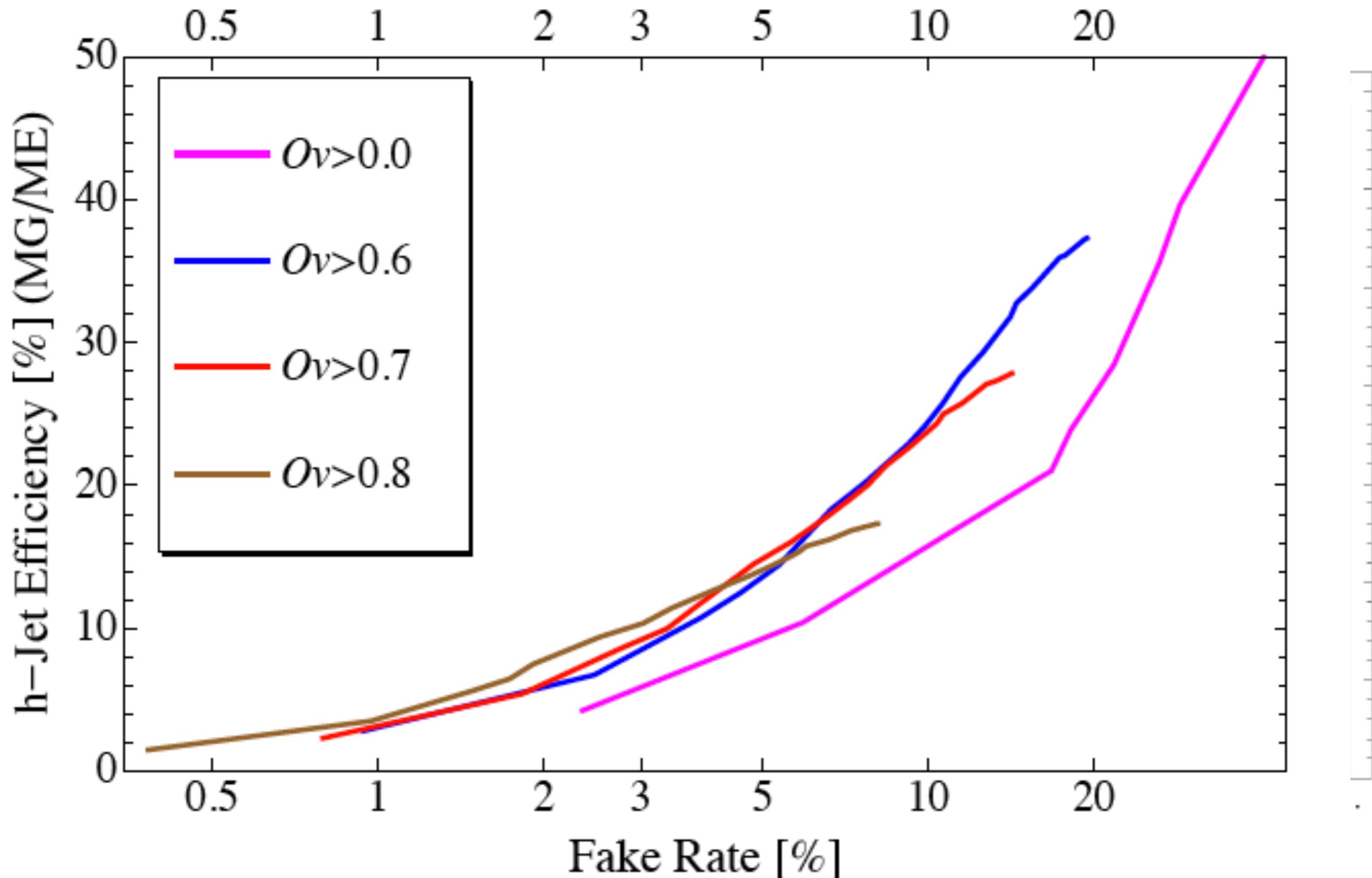
◆ Template Overlap with data discretization

$$Ov(j, f) = \max_{\tau_n^{(R)}} \exp \left[- \sum_{a=1}^2 \frac{1}{2\sigma_a^2} \left(\sum_{k=i_a-1}^{i_a+1} \sum_{l=j_a-1}^{j_a+1} E(k, l) - E(i_a, j_a)^{(f)} \right)^2 \right]$$

Two-particle Templates and Higgs Decay



Two-particle Templates and Higgs Decay



Two-particle Templates and Higgs Decay

- ◆ **The templates** can be systematically improved by including the effects of gluon emissions, which contain color flow information

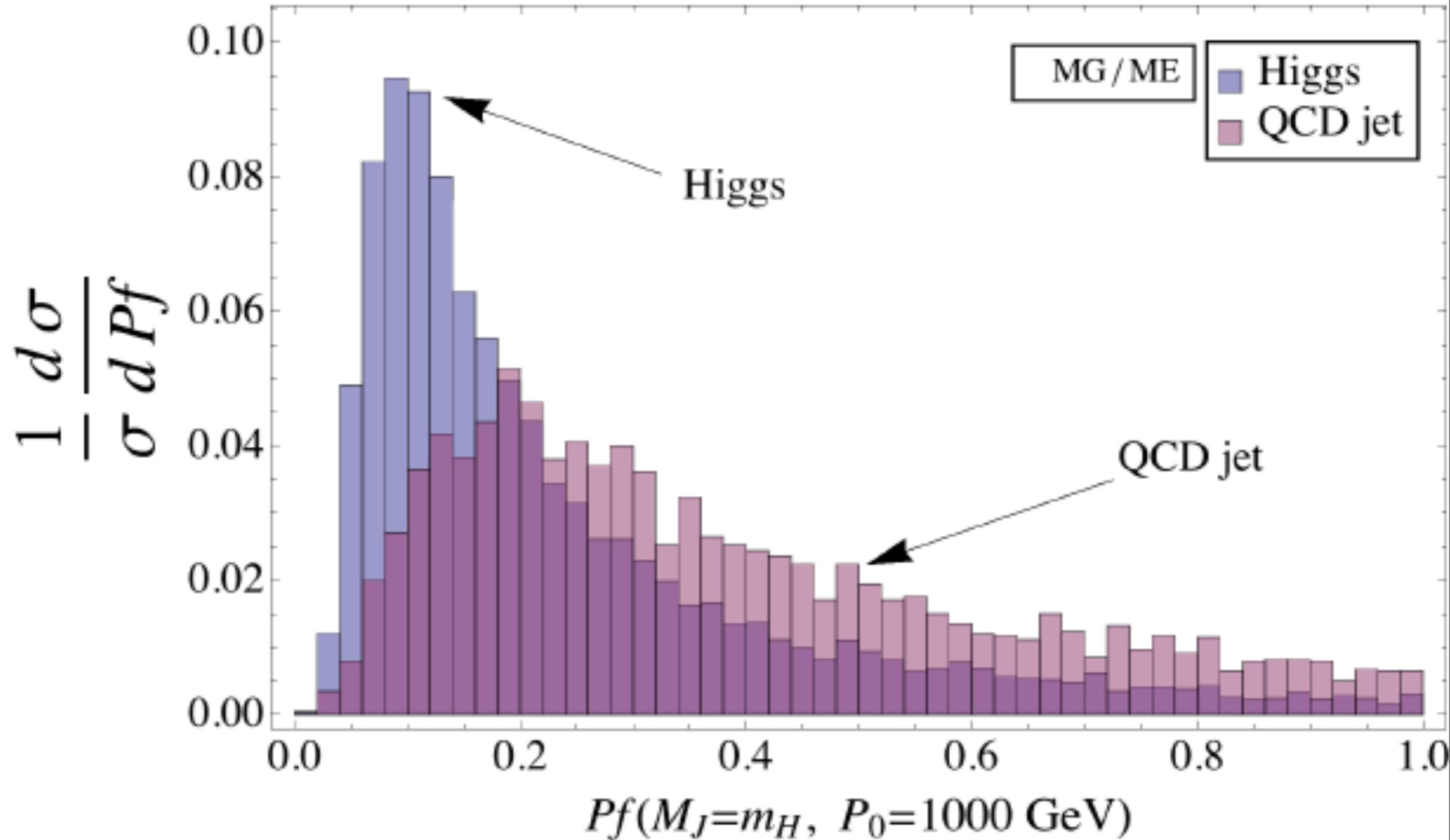
Two-particle Templates and Higgs Decay

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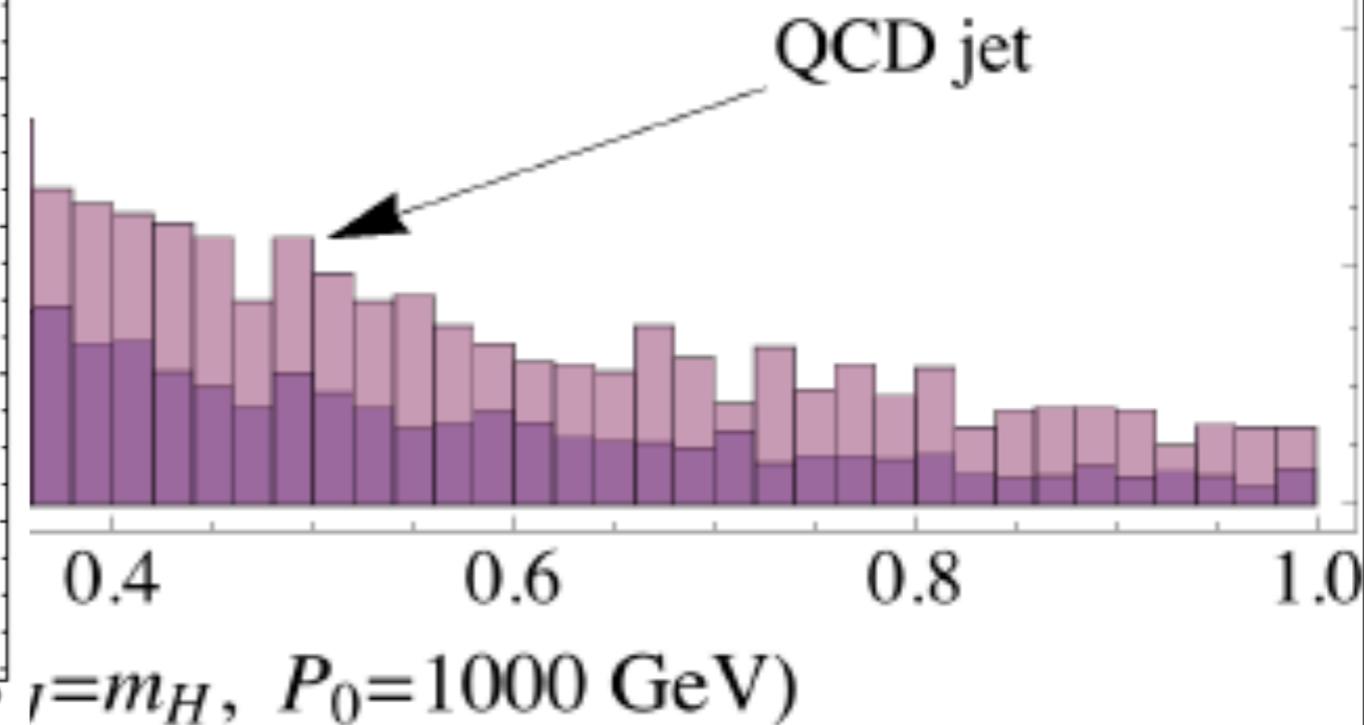
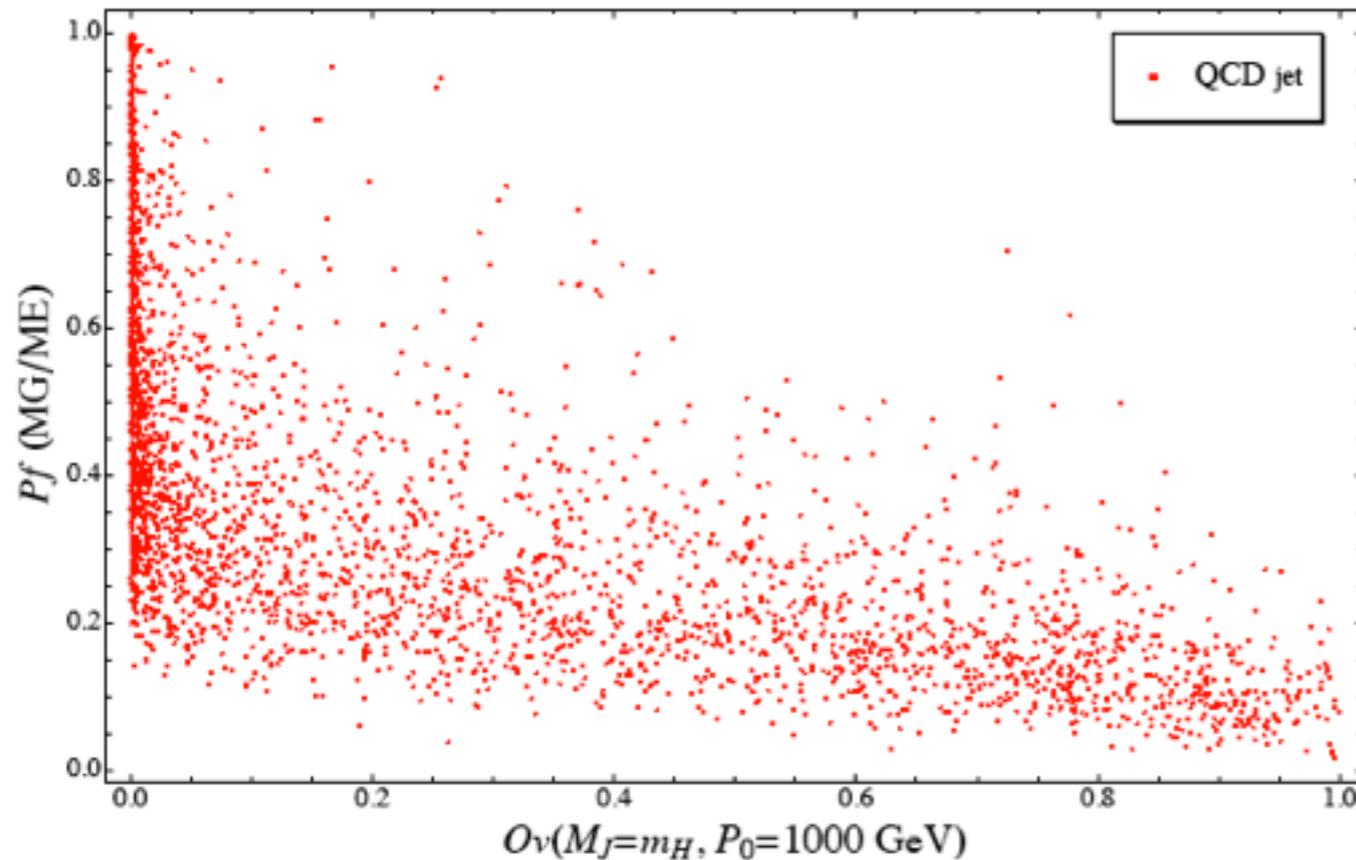
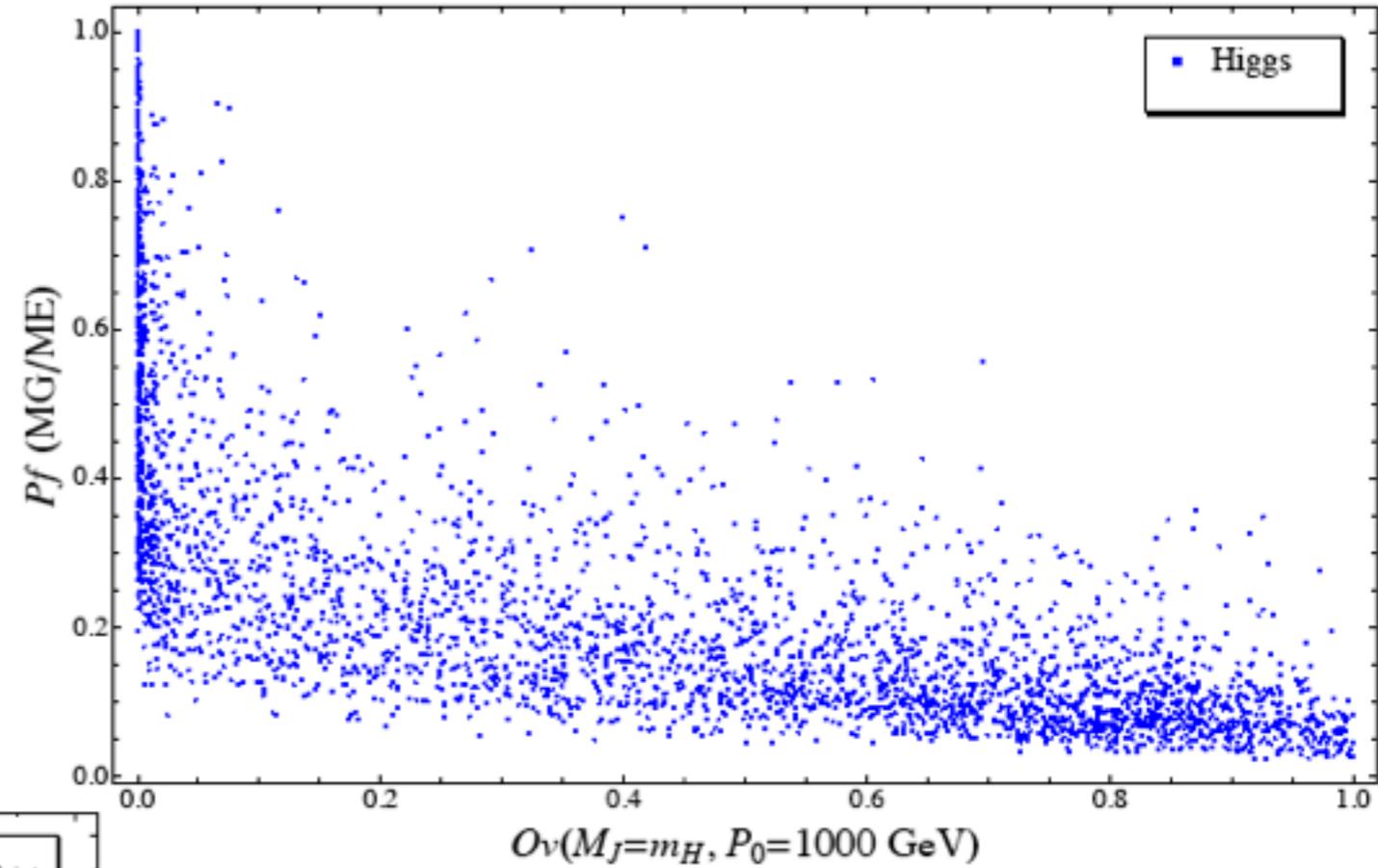
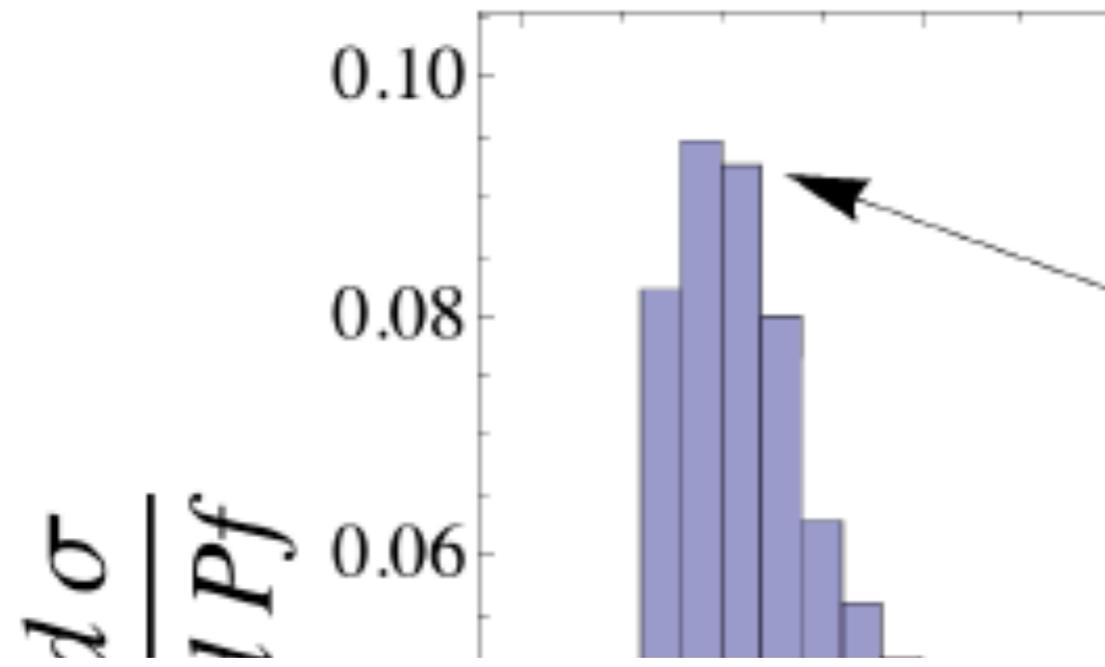
◆ The effects of higher-order effects can be partly captured by using **Planar flow**

(expect soft radiation from the boosted color singlet Higgs to be concentrated between the b and $b\bar{b}$ decay products, in contrast to QCD light jet)

Two-particle Templates and Higgs Decay



Two-particle Templates and Higgs Decay



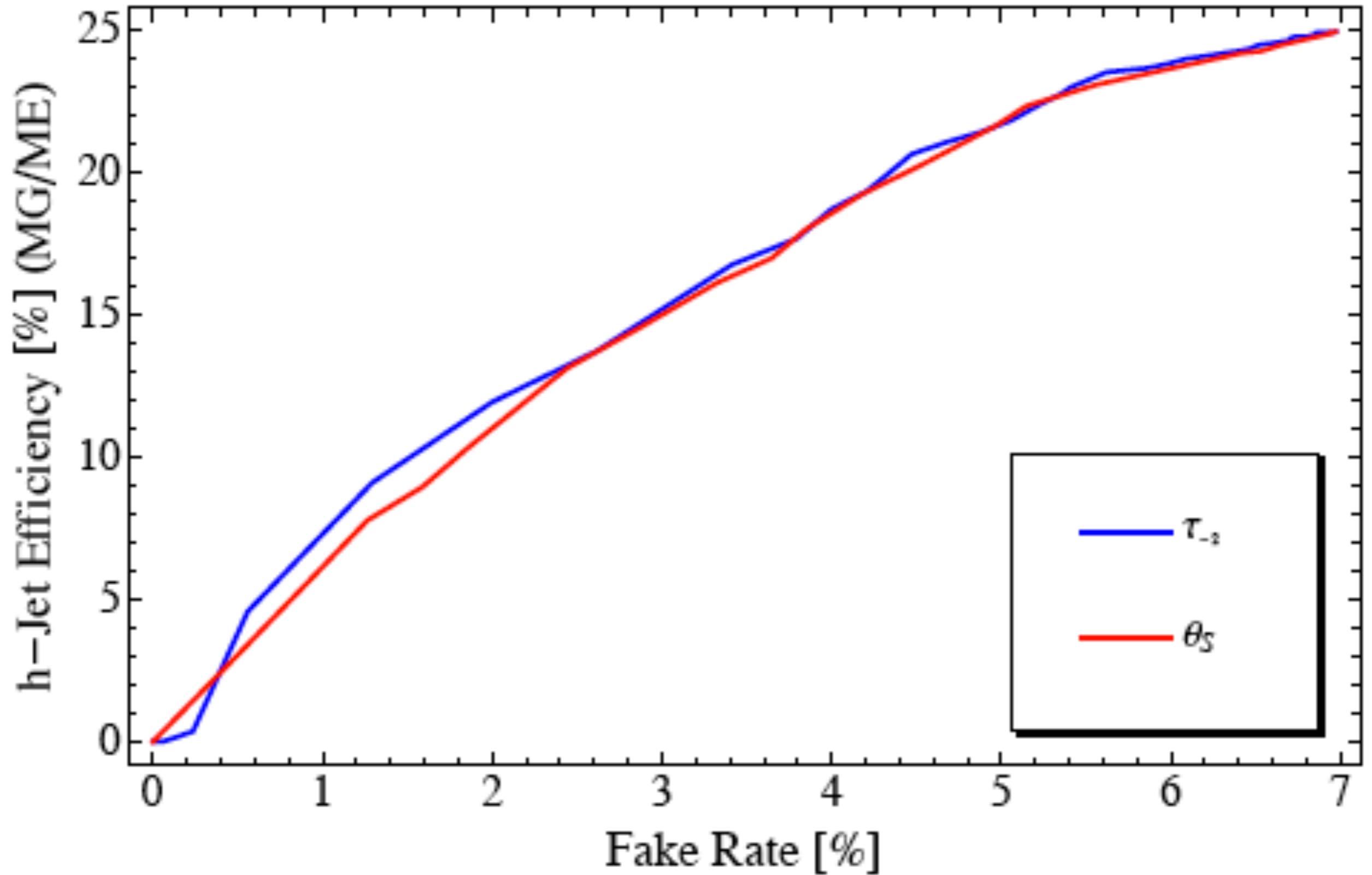
Two-particle Templates and Higgs Decay

- ◆ Combined with angularity or Θ_s : can improved rejection power (Θ_s and angularities are related)

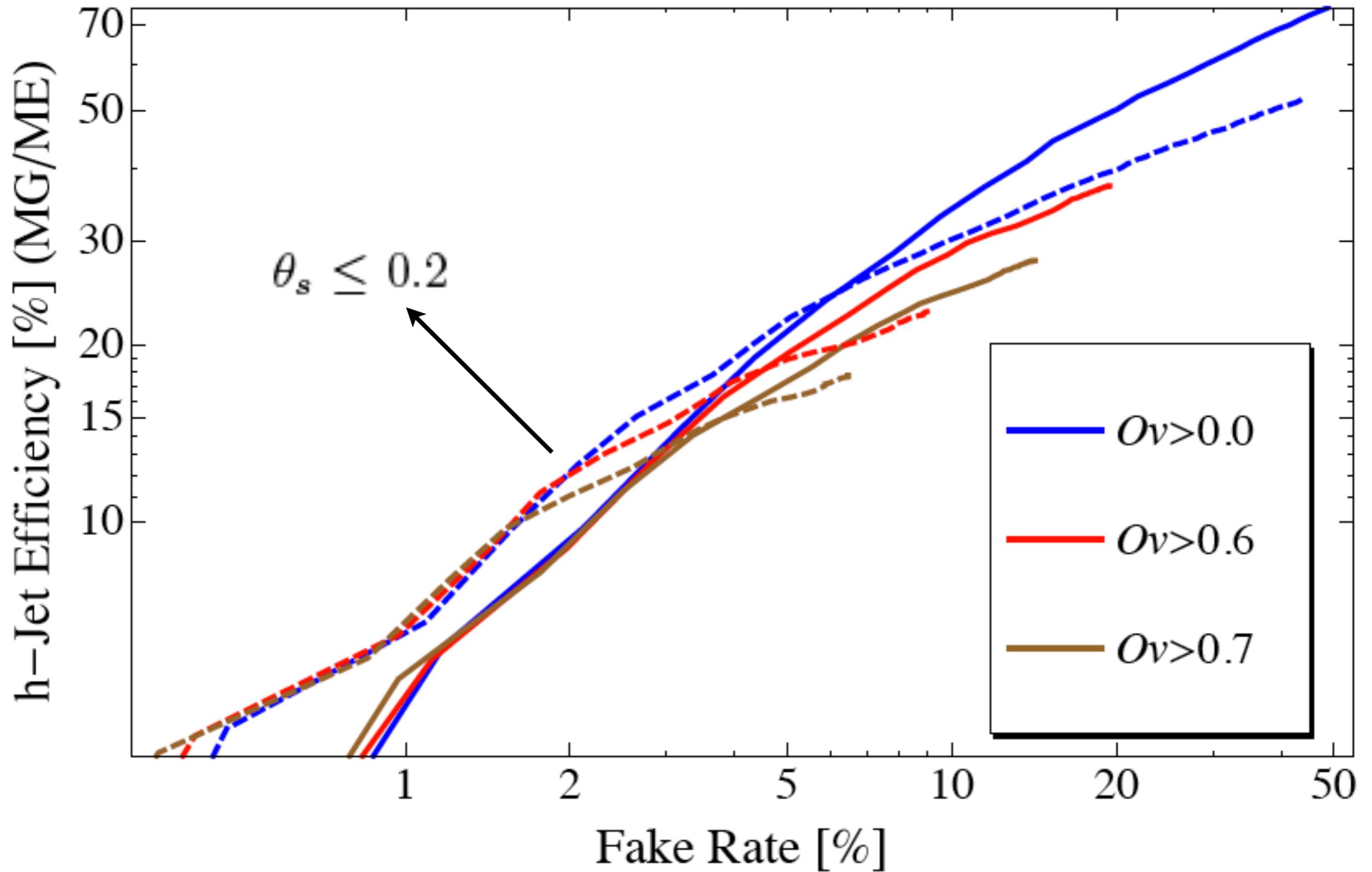
Two-particle Templates and Higgs Decay

- ◆ Combined with angularity or Θ_s : can improved rejection power (Θ_s and angularities are related)
- ◆ Compared to angularities, Θ_s is a parameter for two-body template states, which already provides useful information on physical states, as well as a clear picture of their energy flow.

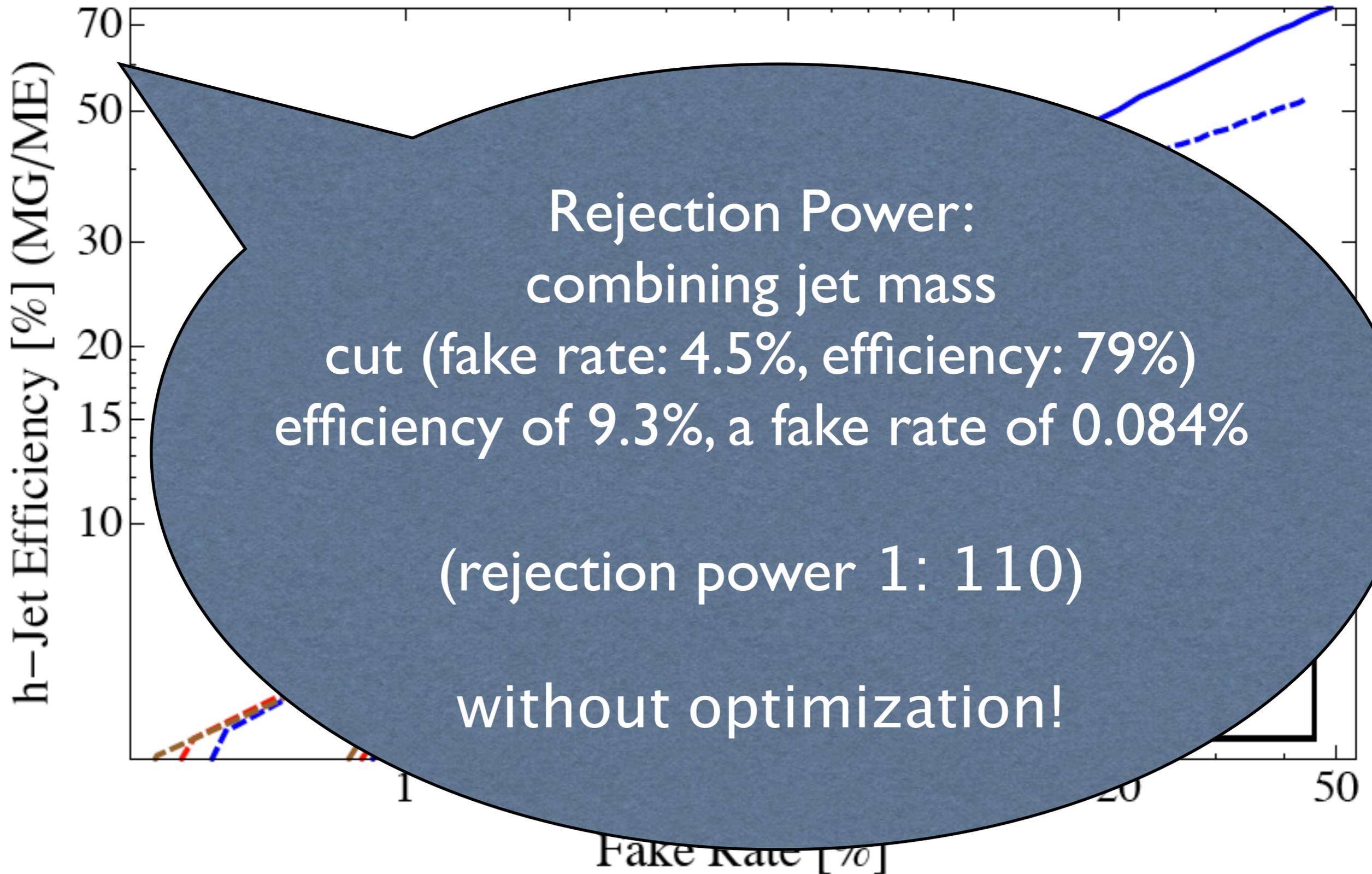
Two-particle Templates and Higgs Decay



Two-particle Templates and Higgs Decay



Two-particle Templates and Higgs Decay



Summary

- ◆ LHC => new era, boosted massive jets may be important for NP discovery
- ◆ Jet function provides a systematic approach to describe the jet mass background
- ◆ Substructures- jet shapes provide a global feature of the Jets (useful for highly collimated jets)
- ◆ Template Overlap method - provides a theoretical handle with good rejection power (systematically improvable): showed top and Higgs case, but can be more imaginative (can be used to NP particle decay)