

The see-saw and leptogenesis

- ★ There is now compelling evidence that **neutrinos have (tiny) masses and (large) mixings**. However, the underlying theoretical model is still unknown.
- ★ One very well-motivated possibility is the **see-saw mechanism**. In the original form, using **very heavy singlet neutrinos**, N_i , with a mass of, say, $M \sim 10^{10}$ GeV, naturally small (**Majorana**) neutrino masses are generated.
- ★ There is also compelling evidence that a **baryon asymmetry** must have been produced primordially in order to get [WMAP, 06]

$$\eta_B = n_B/n_\gamma = (6.1 \pm 0.2) \times 10^{-10}$$

- ★ **Baryogenesis via leptogenesis** [Fukugita, Yanagida, 86] is the generation of a lepton asymmetry by the **out-of-equilibrium** and **CP-violating** decay $\Gamma(N_i \rightarrow \ell_i \Phi^\dagger)$ of the heavy neutrinos, and the subsequent conversion into a **baryon asymmetry** by the anomalous sphaleron processes.

Unflavored leptogenesis

- ★ The flavor composition of the leptons is **NOT** taken into account:

$$\Gamma(N_i \rightarrow \ell_i \Phi^\dagger) \equiv \sum_\alpha \Gamma(N_i \rightarrow \ell_\alpha \Phi^\dagger)$$

- ★ After solving the relevant Boltzmann equations, **in the limit of hierarchical heavy neutrinos**, $M_1 \ll M_2 \ll M_3$, implying typically a N_1 -dominated scenario, bounds for successful leptogenesis are obtained.
- ★ From the bound on the CP asymmetry, one obtains the lower bounds [Davidson, Ibarra, 02; Buchmüller, Di Bari, Plümacher, 02]

$$M_1(T_{\text{reh}}) \gtrsim 3(1.5) \times 10^9 \text{ GeV}$$

- ★ There is a suppression of the efficiency for growing absolute neutrino mass scale which leads to the **upper bound** [Buchmüller, Di Bari, Plümacher, 02]:

$$m_1 \lesssim 0.1 \text{ eV}$$

- ★ The final asymmetry is insensitive to the measurable CP -violating phases (Dirac or Majorana).

Flavored leptogenesis

- ★ It turns out that the τ charged-lepton Yukawa interactions, $f_{\tau\tau}\bar{\ell}_\tau\Phi e_\tau$ become important when $T \lesssim 10^{12}\text{GeV}$. The medium distinguishes then **two flavors**: τ and not τ , i.e. $e+\mu$.
- ★ Flavor effects are important in that:
 - They change the *washout* (typically by a factor 2-3, but can be more)
 - They introduce a *new source of CP violation* (flavor composition of leptons \neq flavor composition of antileptons).
- ★ The lower bound on M_1 do not change [SB, Di Bari, 06] . Concerning the upper bound on m_1 , it is not clear whether it is still there or not.
- ★ It is interesting to notice that the Dirac phase, which one hopes to measure in future neutrino oscillation experiments, may provide a sufficient source of *CP* violation to explain the BAU [SB, Di Bari, 06] .

Conclusion

- ★ Baryogenesis via leptogenesis is an attractive mechanism to explain the origin of the BAU.
- ★ Two descriptions coexist: i) when $M_1 \gtrsim 10^{12} \text{GeV}$ the **unflavored picture** should be correct. ii) when $M_1 \lesssim 10^{12} \text{GeV}$ a **flavored treatment** is necessary.
- ★ For $M_1 \ll M_2 \ll M_3$, the lower bounds $M_1(T_{\text{reh}}) \gtrsim 3(1.5) \times 10^9 \text{GeV}$ hold **even accounting for flavor effects**. The question about the presence of an upper bound on m_1 is still open.
- ★ Within the flavored regime, the low-energy measurable phases (both Dirac and Majorana) can play an important role.



Back-up

The puzzle of neutrino masses

- ★ The Standard Model of particle physics predicts massless neutrinos.
- ★ Today, after 10 years of great successes in neutrino oscillation experiments, the evidence is overwhelming that **neutrinos have masses and mix**. One has measured quite precisely two mass-squared differences :

$$\begin{array}{l} \text{Sol.+ Reac. } \sqrt{\Delta m_{\text{sol}}^2} \simeq 0.009 \text{ eV} \\ \text{Atm.+ Acc. } \sqrt{\Delta m_{\text{atm}}^2} \simeq 0.05 \text{ eV} \end{array}$$

- ★ From the the measurement of the Z width at LEP, there should be **3 neutrino flavors**, and thus **3 neutrino masses**.
- ★ Neutrino oscillation experiments provide **no information on the absolute neutrino mass scale!** Fortunately, there are other probes possible...

Resolution of the two puzzles



The see-saw mechanism



```
graph TD; A[The see-saw mechanism] --> B[Small neutrino masses]; A --> C[Matter-antimatter problem]; D[Baryogenesis through leptogenesis] --> A_C; style A stroke:#0000FF,stroke-width:2px; style B stroke:#8B0000,stroke-width:2px; style C stroke:#8B0000,stroke-width:2px; style D stroke:#8B0000,stroke-width:2px;
```

Small neutrino masses

**Baryogenesis
through
leptogenesis**

Matter-antimatter problem

The see-saw mechanism

- ★ The see-saw mechanism originates from the following extension of the SM Lagrangian:

$$\delta L = \bar{N}_i i \partial_\mu \gamma^\mu N_i - \underbrace{h_{i\alpha} \bar{N}_i \Phi L_\alpha}_{\text{Yukawa coupling}} - \underbrace{\frac{1}{2} M_i \bar{N}_i N_i^c}_{\text{Majorana mass term}} + h.c.$$

Yukawa coupling Majorana mass term

where $\Phi = (\phi^0, \phi^+)$ and $L_\alpha = (\nu_{L\alpha}, \alpha_L^-)$, $\alpha = e, \mu, \tau$ are the Higgs and left-handed lepton doublets, respectively, and N_i , $i = 1, 2, 3$ are RH neutrinos.

- ★ This extension is clearly acceptable on grounds of **gauge invariance** and **renormalizability**, and is **minimal** in its particle content (here: 3 new particles).

The see-saw mechanism

- ★ The masses of the singlet neutrinos are essentially free parameters, and thus can be taken to be very large ($\gg 100$ GeV).

→ See-saw mechanism! [Minkowski, 77]

- ★ After spontaneous symmetry breaking, the vev $\langle \Phi \rangle$ of the Higgs leads to a Dirac mass term $m_D = h\langle \Phi \rangle$. The see-saw assumes $M \gg m_D$ so that the neutrino mass term can be block-diagonalized as:

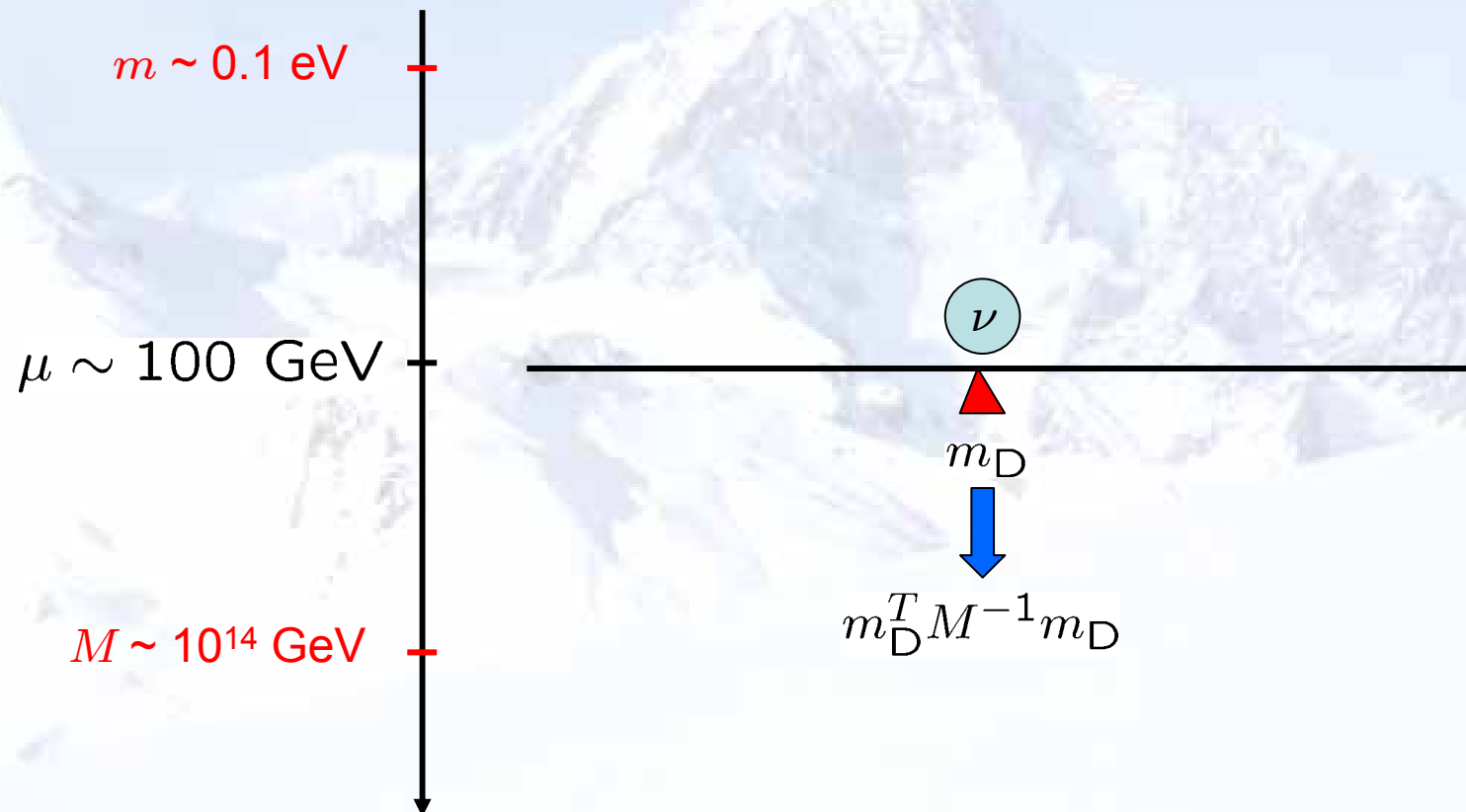
$$\begin{pmatrix} 0 & m_D^T \\ m_D & M \end{pmatrix} \xrightarrow{\text{1st order}} \begin{pmatrix} m_D^T M^{-1} m_D & 0 \\ 0 & M \end{pmatrix}$$

After diagonalization: 3 light **Majorana** neutrinos, mass $m_1 \leq m_2 \leq m_3$

3 heavy **Majorana** neutrinos, mass $M_1 \leq M_2 \leq M_3$

The see-saw mechanism

★ Conventional picture

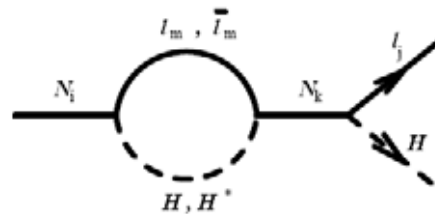
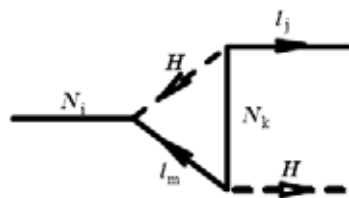


Baryogenesis through leptogenesis

★ Baryogenesis through leptogenesis [Fukugita, Yanagida, 86] is the generation of a lepton asymmetry by the decay of heavy right-handed neutrinos, and the subsequent conversion into a baryon asymmetry by the anomalous sphaleron processes.

★ The three Sakharov conditions are fulfilled :

- Baryon number is violated in anomalous processes
- *CP* is violated in the decay of the heavy neutrinos: interference between tree level and 1-loop diagrams



$$\epsilon_i = \frac{\Gamma(N_i \rightarrow L_i \Phi^\dagger) - \Gamma(N_i \rightarrow \bar{L}_i \Phi)}{\Gamma(N_i \rightarrow L_i \Phi^\dagger) + \Gamma(N_i \rightarrow \bar{L}_i \Phi)}$$

CP asymmetry parameter

- Decays are out of equilibrium at some point, parametrized by

$$K_i \equiv \frac{\Gamma(N_i \rightarrow L_i \Phi^\dagger)|_{T \rightarrow 0}}{H(T = M_i)}$$

“decay parameter”

Baryogenesis through leptogenesis

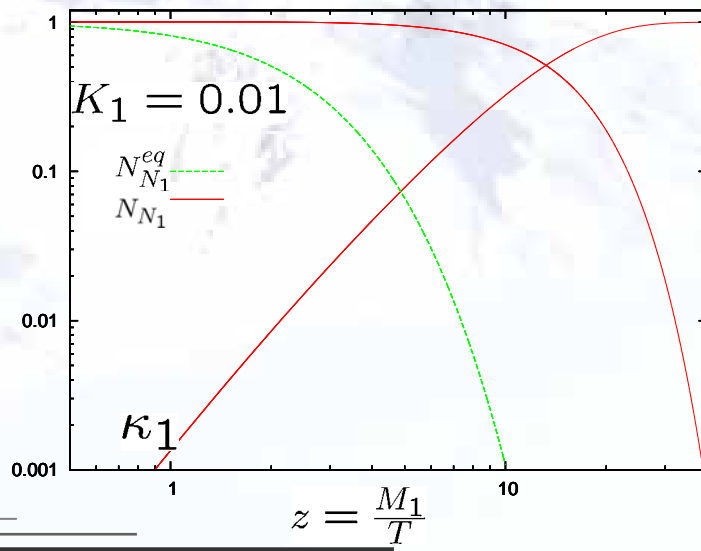
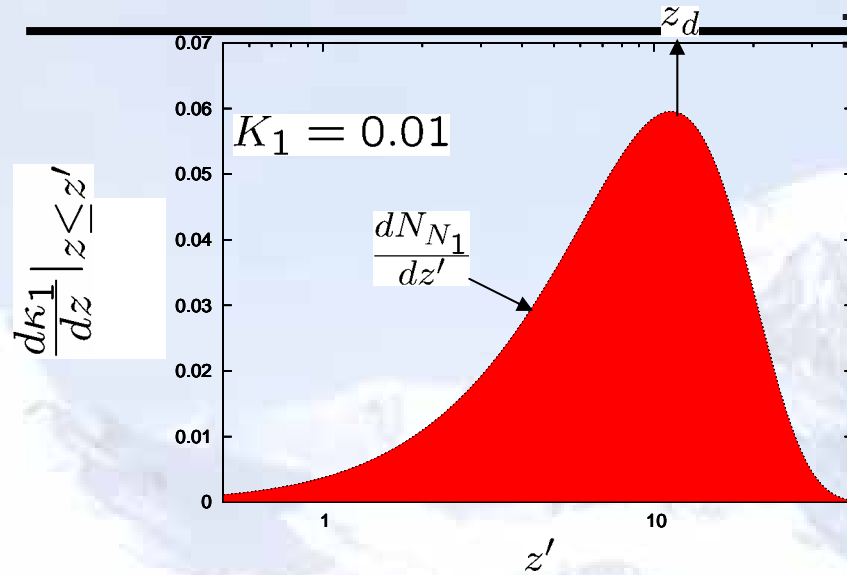
- ★ In practice, in order to estimate the baryon asymmetry produced in leptogenesis, one has to solve coupled Boltzmann equations.
- ★ In most cases where $M_1 \ll M_2 \ll M_3$, it is enough to consider the decay of the lightest RH neutrino:

$$\eta_B \propto \varepsilon_1 \kappa_1^{\text{fin}}$$

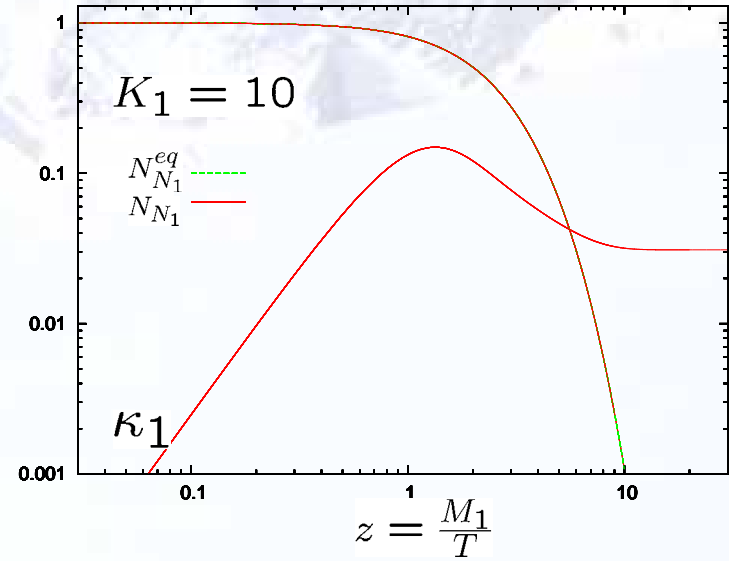
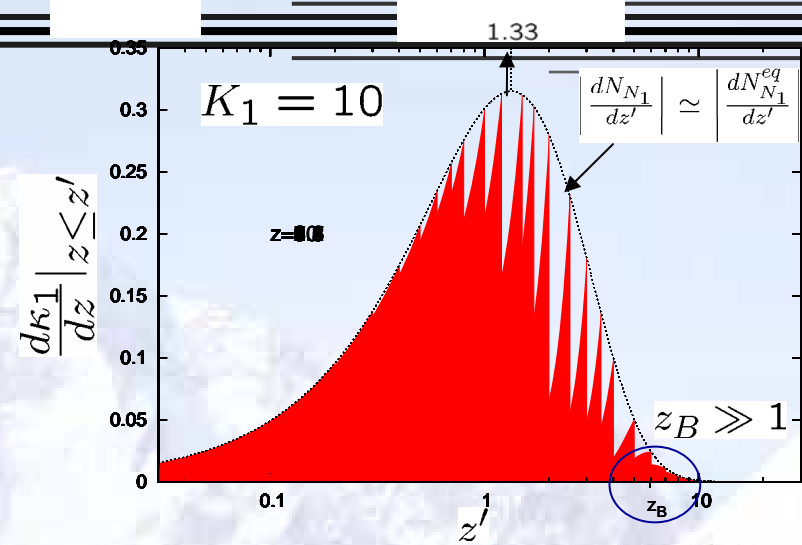
where κ_1^{fin} is the **final efficiency factor**, which depends mainly on K_1 .

- ★ When the decay parameter $K_1 \gtrsim 1$ one talks about the **strong wash-out**. Conversely, when $K_1 \lesssim 1$ one has a **weak wash-out**.
- ★ There are different reasons why the strong wash-out is favored, the most prominent one being that there the resulting is **independent of the initial conditions** in this case.

WEAK WASHOUT



STRONG WASHOUT



Implications of leptogenesis

- ★ There is an upper bound on the CP asymmetry [Asaka et al., 01; Davidson, Ibarra, 02]

$$\varepsilon_1 \leq \bar{\varepsilon}(M_1) \simeq 10^{-6} \left(\frac{M_1}{10^{10} \text{ GeV}} \right)$$

one obtains a **lower bound on M_1** and on the reheating temperature [Davidson, Ibarra, 02; Buchmüller, Di Bari, Plümacher, 02] :

$$M_1(T_{\text{reh}}) \gtrsim 3(1.5) \times 10^9 \text{ GeV}$$

- ★ There is a suppression of the efficiency for growing absolute neutrino mass scale leads to a **stringent upper bound** [Buchmüller, Di Bari, Plümacher, 02] :

$$m_1 \leq 0.1 \text{ eV}$$

Recent development: flavor effects

- ★ Recently, it was realized that the flavor structure of the leptons should be taken into account.
- ★ The reason is that when $T \lesssim 10^{12} \text{GeV}$, the τ -lepton Yukawa interaction $f_{\tau\tau} \bar{L}_\tau \Phi E_\tau$ is **in equilibrium**, i.e. $\Gamma_\tau \gtrsim H$.
- ★ These interactions are then fast enough to ‘measure’ if the flavor of the state produced in the decay of the heavy neutrino is τ or not; a **2-flavor basis** (‘ τ ’ and ‘ $e\mu$ ’) is defined. [Abada, Davidson, Josse-Michaux, Losada, Riotto, 06 ; Nardi, Nir, Racker, Roulet, 06]
- ★ These considerations can affect the resulting asymmetry by large factors in special cases. In particular, the upper bound on m_1 will be very affected, if not removed. Note that **the important lower bound on M_1 is not changed by flavor effects!!**
- ★ Interestingly, **flavor effects introduce a dependence of the final asymmetry on the lepton mixing matrix.**

Conclusions



- ★ The see-saw mechanism allows the resolution of two important puzzles of modern physics: the **smallness of neutrino masses** and the **origin of matter**.
- ★ **Baryogenesis through leptogenesis** is an elegant solution to the matter-antimatter problem and implies a link between neutrino masses and a cosmological parameter, the baryon-to-photon ratio.
- ★ In this scenario, one of the **largest energy scales in cosmology** is related to the **particles with the tiniest mass!**
- ★ Recent developments (**flavor effects**) have shown that the link with neutrino physics is tighter than previously thought.
- ★ In particular, the **Dirac phase** in the lepton mixing matrix, which one hopes to measure in future neutrino experiments, **could be the unique source of CP violation required to explain the origin of matter**.