

Identification of Dark Matter using Directional Detection

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(soon on the arXiv)

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GDR Terascale 2010 - Bruxelles

Outline

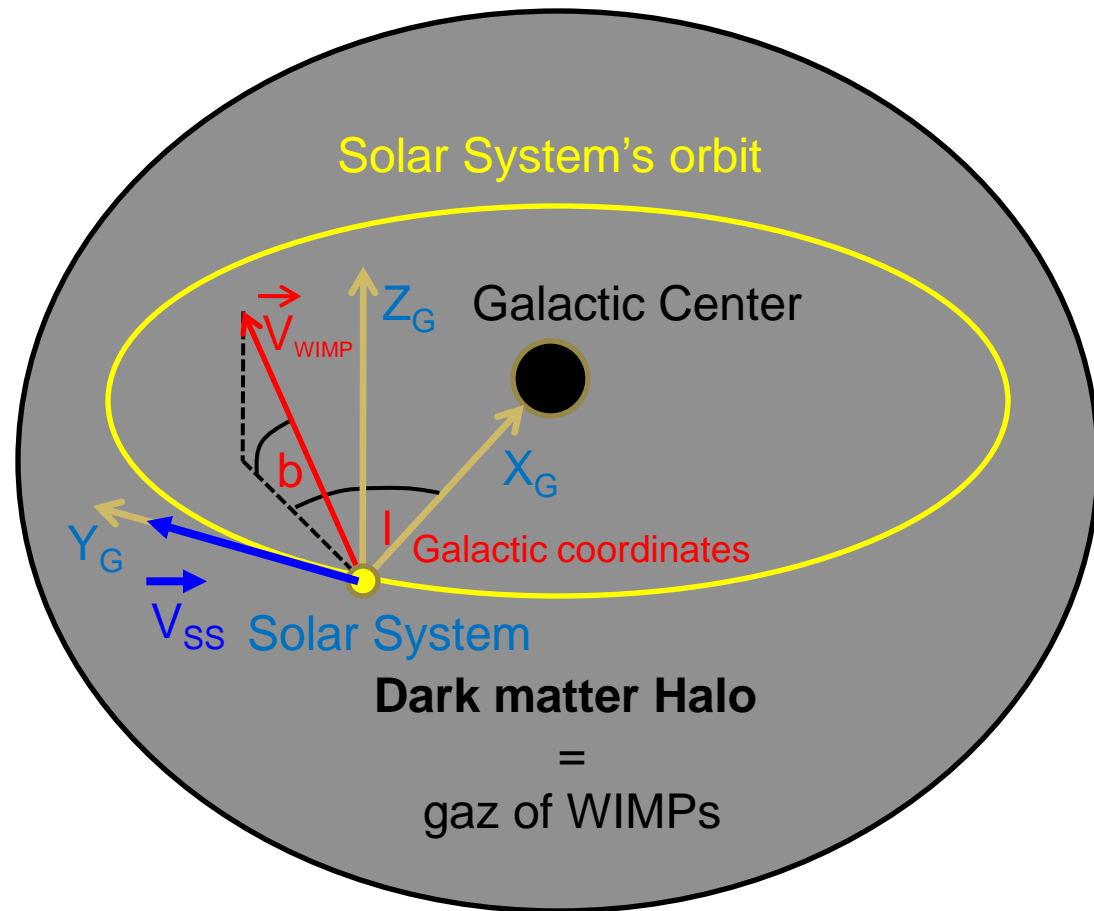
1. Directional detection & MIMAC prospects
2. Theoretical framework & a new MCMC analysis
3. Results from a simulated directional detection experiment
4. Effect of input parameters

Conclusions & discussion

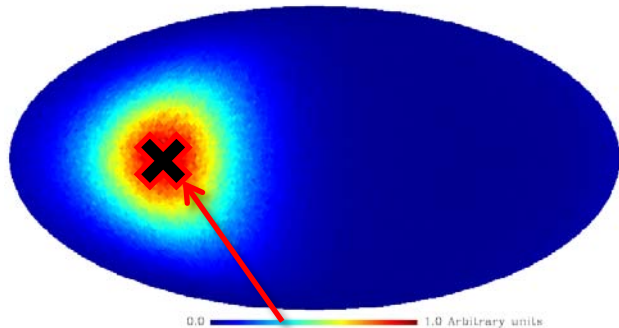
Directional detection & MIMAC prospects

I.a WIMP signal

Considering the standard halo model, isothermal sphere:



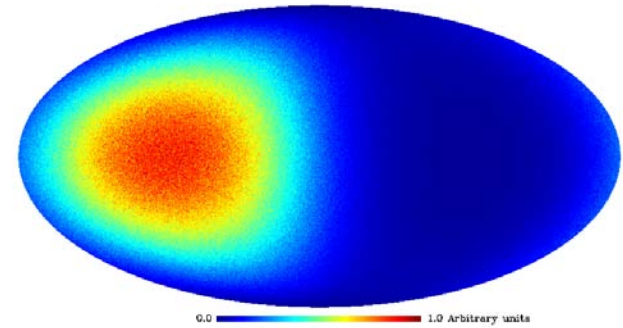
WIMP flux entering a terrestrial detector represented in Galactic coordinates



Cygnus Constellation ($l = 90^\circ, b = 0^\circ$) J. Billard - GDR Terascale 2010

WIMP induced recoil distribution

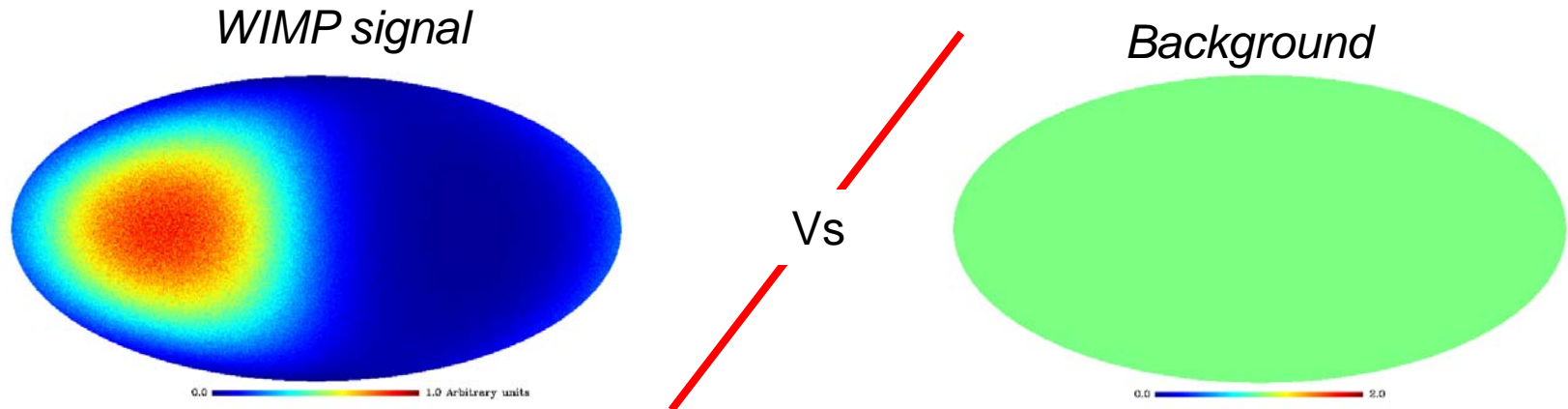
After scattering



Expected WIMP signal

I.b Interest of the directional detection

Background is supposed to be **isotropic**



Clear and unambiguous difference between WIMP signal and background

Directional detector :

- **Need to measure** : Recoil direction & Recoil energy
- **Technology** : Gaseous detector and TPC with low threshold
- **Projects** : **MIMAC**, DRIFT, DM-TPC, NEWAGE and Nuclear Emulsion

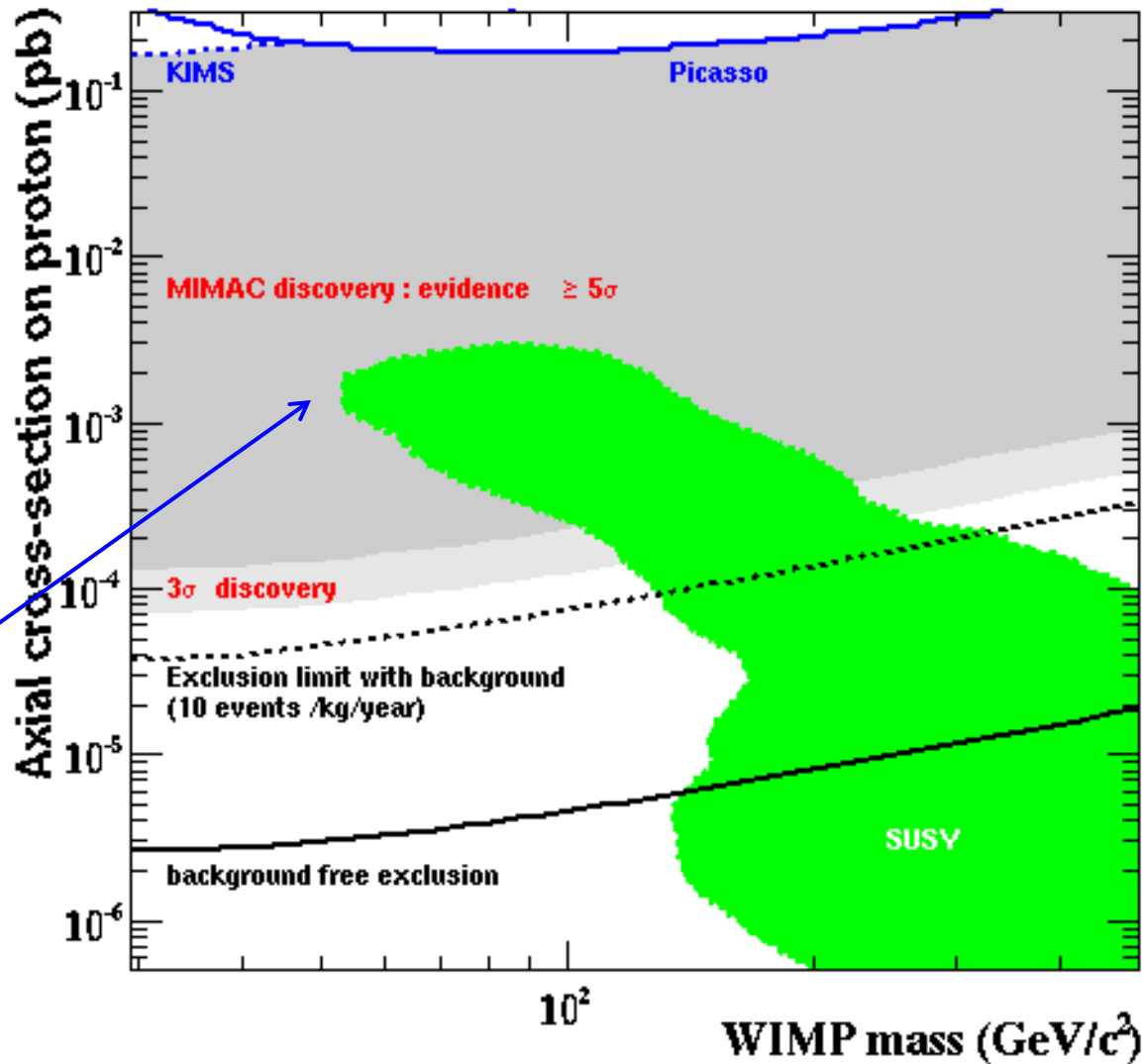
More details: S. Ahlen *et al.*, *International Journal of Modern Physics A25* (2010)

I.c MIMAC prospects

MIMAC characteristics

- 10 kg CF₄
- DAQ : 3 years
- Recoil energy [5, 50] keV
- Background rate:
10 evts/kg/year

J. Billard *et al.*:
Phys.Rev.D82:055011,2010 & Phys. Lett. B 691 (2010) 156-162



Down to 10⁻⁴ pb:

discovery

Down to 10⁻⁵ pb:

exclusion

Going further:

Characterization of
Dark Matter

Theoretical framework
&
a new MCMC analysis

II.a Directional event rate

$$\frac{d^2 R}{dE_R d\Omega} = \frac{\rho_0 \sigma_0}{4\pi m_\chi m_r^2} F^2(E_R) \hat{f}(v_{\min}, \hat{q})$$

↓
 Form factor

- Particle physics
- Nuclear physics
- Astrophysics

Radon transform: [P. Gondolo 2002]

$$\hat{f}(v_{\min}, \hat{q}) = \int d^3 v \delta(\vec{v} \cdot \hat{q} - v_{\min}) f(\vec{v})$$

Kinematic relationship

Which expression of $f(v)$?

II.b Velocity distribution

The multivariate gaussian velocity distribution function,

$$f(\vec{v}) = \frac{1}{(8\pi^3 \det \sigma_v^2)^{1/2}} \exp \left[-\frac{1}{2} (\vec{v} - \vec{v}_\odot)^T \sigma_v^{-2} (\vec{v} - \vec{v}_\odot) \right]$$

naturally arises from the fact that:

- It is the triaxial generalization of the standard isothermal sphere [Binney and Tremaine]
- It reproduces flat rotation curves ($\rho(r) = 1/r^2$) [N. W. Evans et al. 2000]
- It is quite consistent with recent numerical N-body simulations
[M. Vogler et al. 2009, M. Khullen et al. 2010, F. S. Ling et al. 2010]

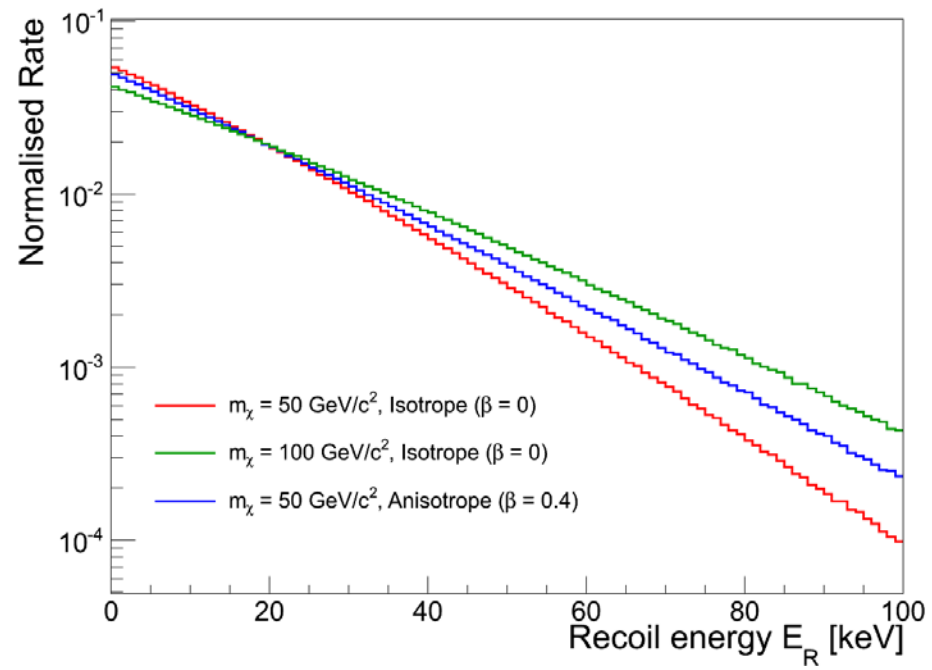
The velocity anisotropy parameter is defined as:

$$\beta(r) = 1 - \frac{\sigma_\theta^2 + \sigma_\phi^2}{2\sigma_r^2} \longrightarrow \begin{cases} \bullet \text{ if } \beta < 0: \text{ tangential anisotropy} \\ \bullet \text{ if } \beta > 0: \text{ radial anisotropy} \end{cases}$$

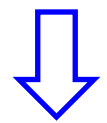
According to N-Body simulations, $0 < \beta < 0.4$

II.c Effect of input parameters

$$dR/dE_r$$

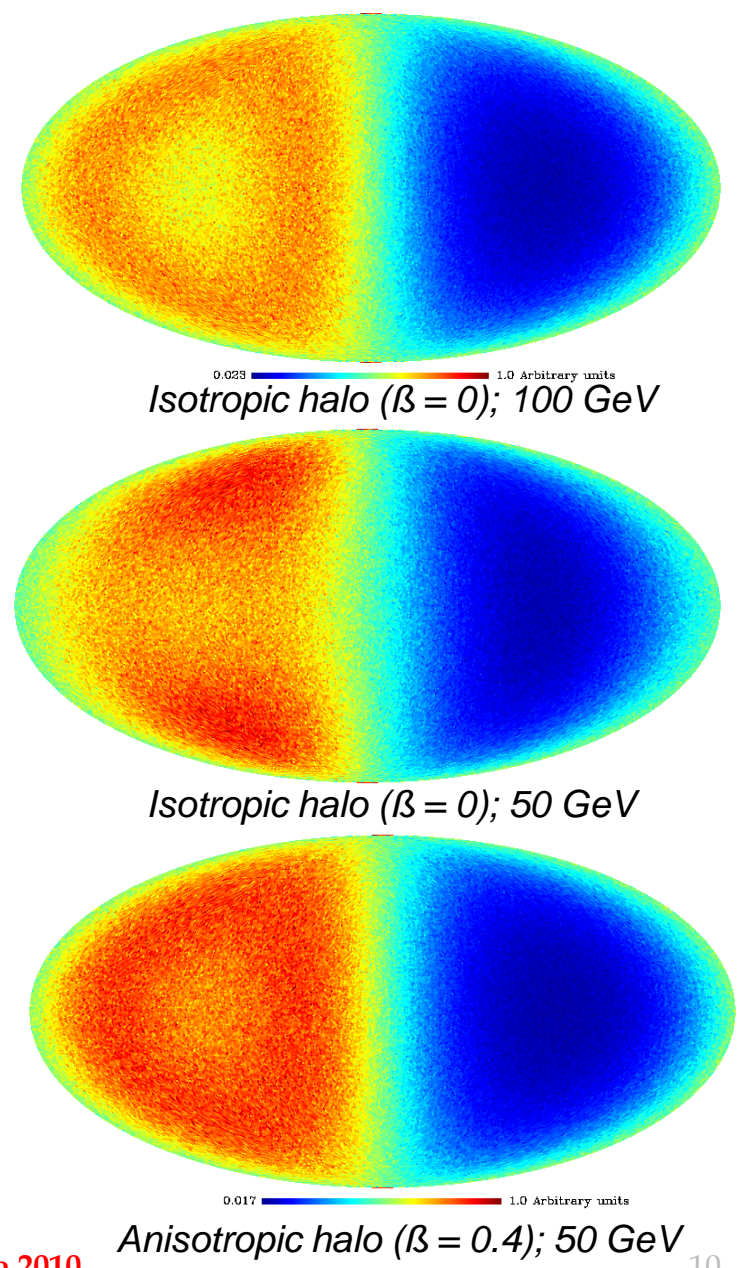


Directional detection: use of **angular** and **energy** information



Offers the possibility to identify Dark Matter
 J. Billard - GDR Terascale 2010

$$dR/d\Omega_r \text{ at } E_R = 5 \text{ keV}$$



II.d Free parameters

The 8 free parameters of the fitting model are:

- The WIMP mass m_χ
- The WIMP-nucleon cross-section σ_n
- The main incoming direction of the signal (l_0, b_0)
- The 3 velocity dispersions σ_x, σ_y et σ_z
- The background rate R_b

What are the posterior PDF of each parameter according to a single experiment?

$$\mathcal{L}(\vec{\theta}) = \frac{(\mu_s + \mu_b)^{N_{\text{event}}}}{N_{\text{event}}!} \times \prod_{n=1}^{N_{\text{event}}} \left[\frac{\mu_s}{\mu_s + \mu_b} S(\vec{R}_n) + \frac{\mu_b}{\mu_s + \mu_b} B(\vec{R}_n) \right]$$

Where:

- N_{event} is the total number of recorded events
- μ_s and μ_b are the expected number of WIMP and background events
- S and B are the normalised directional rate for WIMP and background events

II.e The MCMC analysis

Interest of the Markov Chain Monte Carlo sampling:

- Size of the parameter space
- Reduced computational time compared to a grid calculation
- Precision on the estimation of the PDFs

Metropolis-Hastings algorithm with 2 different proposal functions:

- Multivariate gaussian
- Multivariate gaussian using the covariance matrix V

MCMC characteristics:

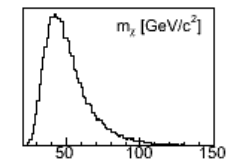
- 10-100 chains randomly started in the parameter space.
- Sub-sampling: « burn-in » and correlation lengths => **independent samples**
- Chain convergence checked

Results from a simulated directional detection experiment

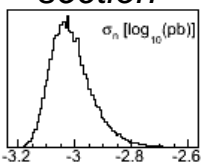
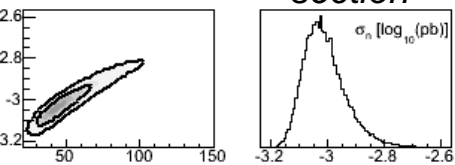
MIMAC characteristics

- 10 kg $\text{CF}_4 \Rightarrow 50 \text{ m}^3 @ 50 \text{ mbar}$
- DAQ : 3 years
- Recoil energy [5, 50] keV

Mass

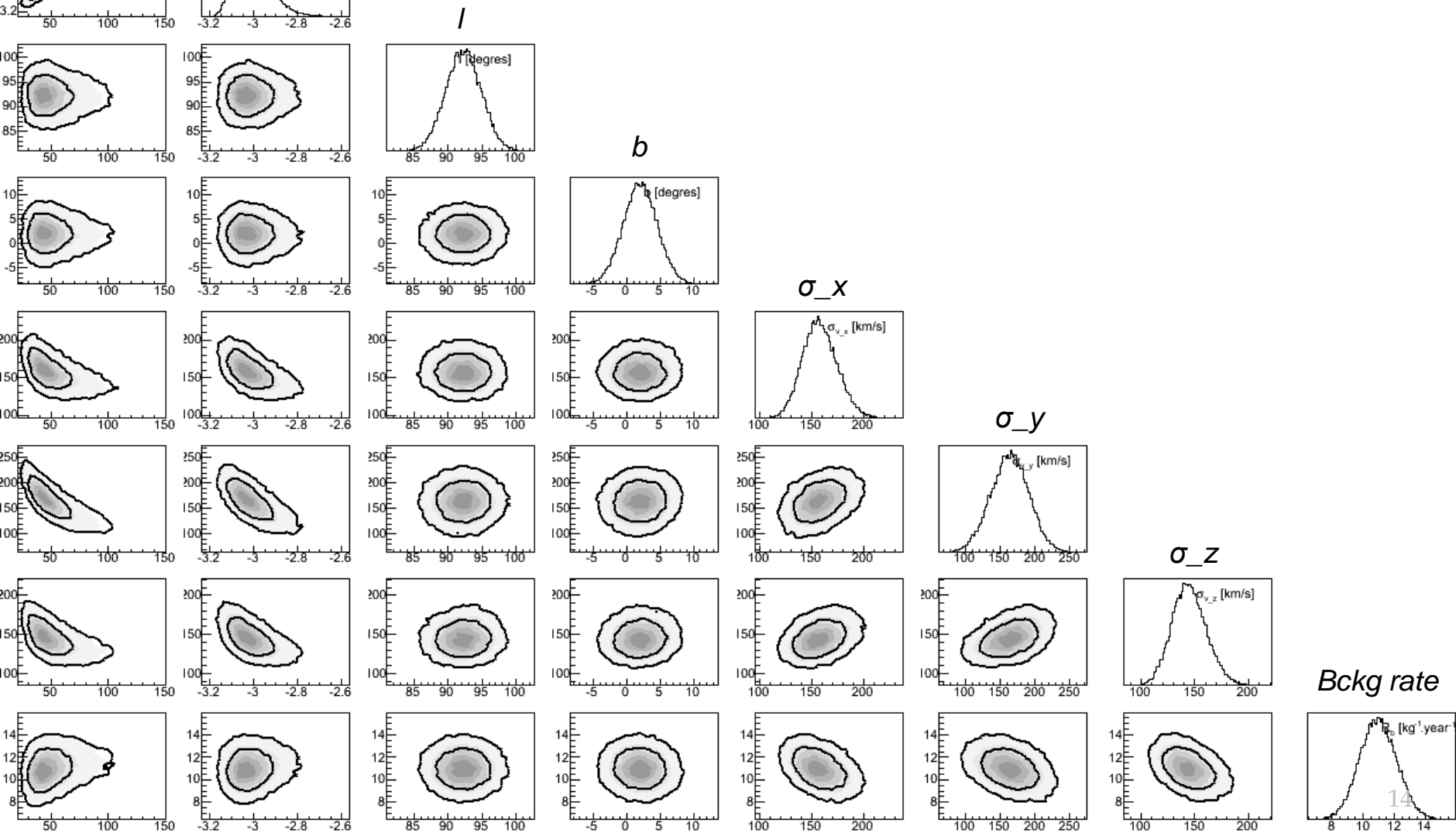


Cross-section

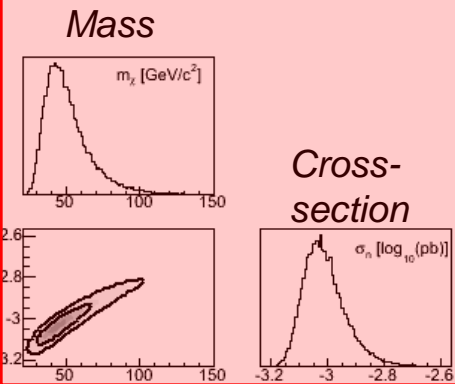


Input:

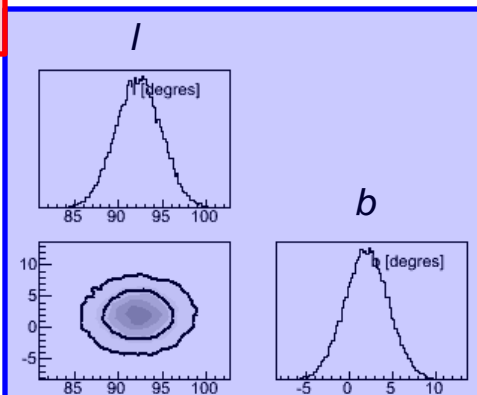
- isotropic halo: $\sigma_i = 155$ km/s
- mass: 50 GeV
- cross-section: 10^{-3} pb
- Bckg rate: 10 evts/kg/year (35%)



Particle physics



DM signature



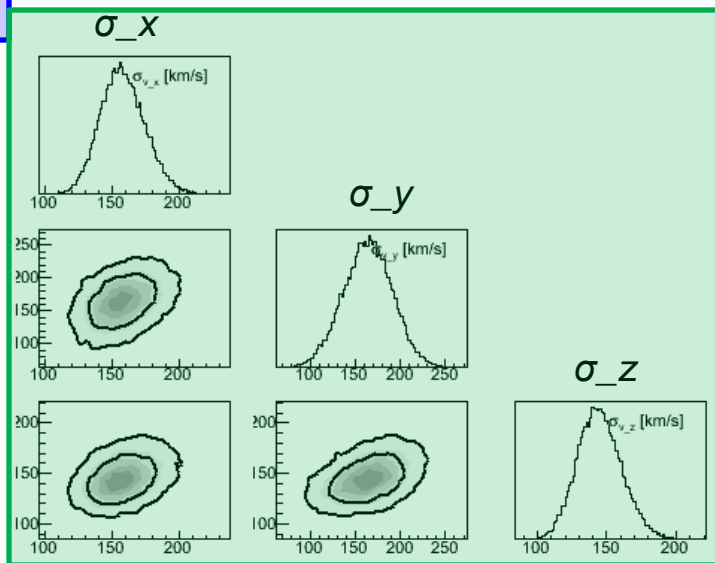
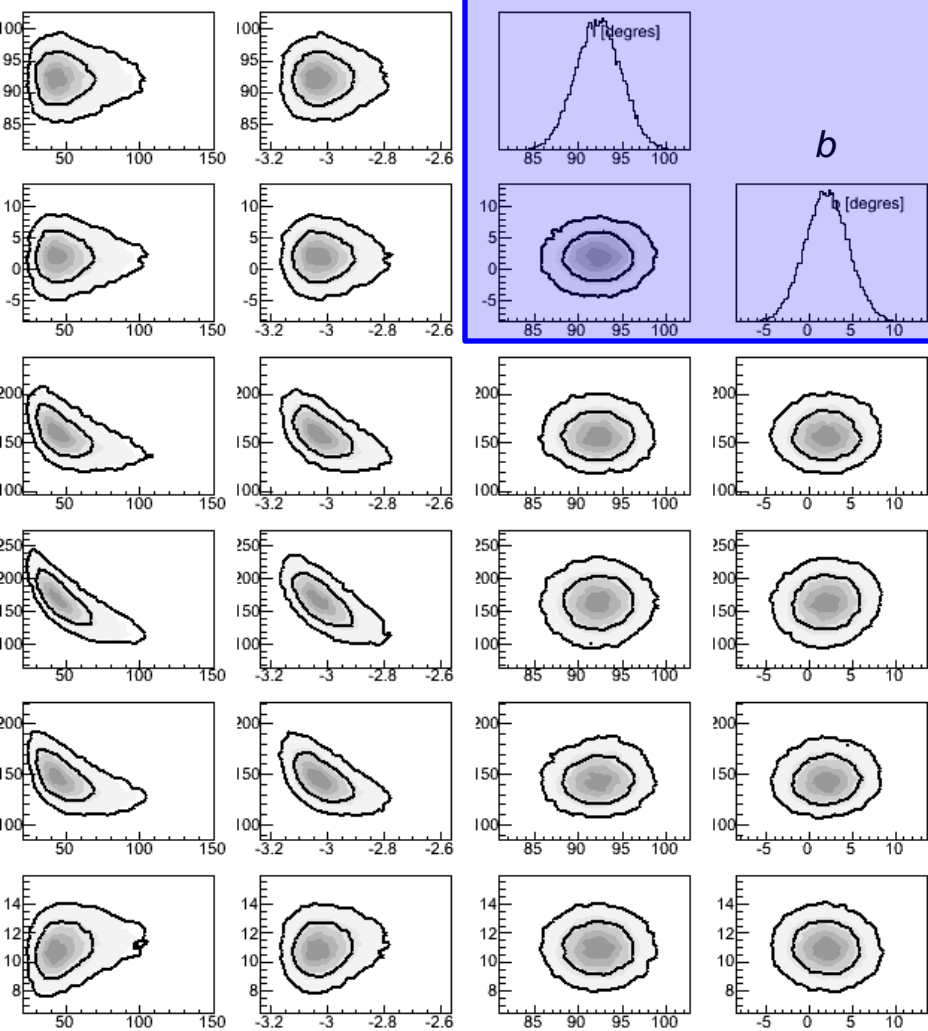
Input:

- isotropic halo: $\sigma_i = 155$ km/s
- mass: 50 GeV
- cross-section: 10^{-3} pb
- Bckg rate: 10 evts/kg/year (35%)

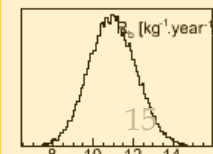
Conclusion:

The 8 parameters are strongly constrained from a single direction detection experiment

Dark Matter halo properties



Bckg rate



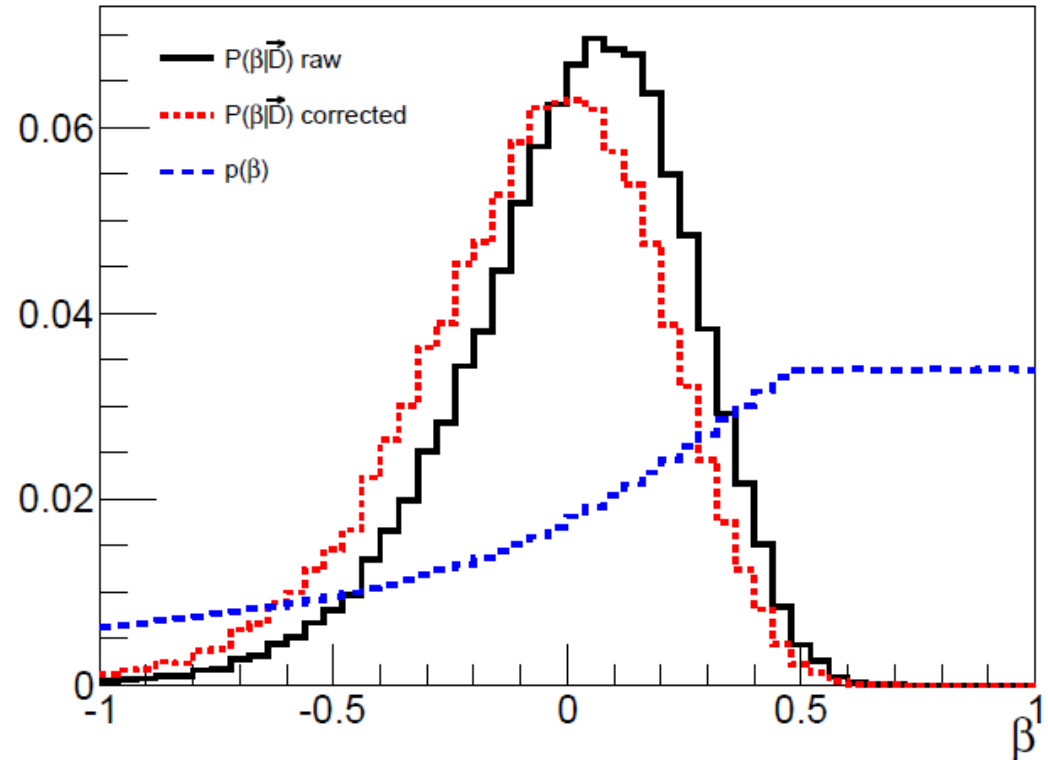
III.e Constraint on the velocity anisotropy

The PDF of the β parameter can be deduced from:
$$\beta(r) = 1 - \frac{\sigma_\theta^2 + \sigma_\phi^2}{2\sigma_r^2}$$

With a flat prior on the σ_i

Induced prior

With a flat prior on β



Excellent constraint on the β parameter from a single directional detection experiment:

$$\beta = -0.073^{+0.29}_{-0.18} \text{ (68\% CL)}$$

Effect of input parameters

MIMAC characteristics

- 10 kg CF_4 => 50 m³ @ 50 mbar
- DAQ : 3 years
- Recoil energy [5, 50] keV

III.e Input WIMP mass

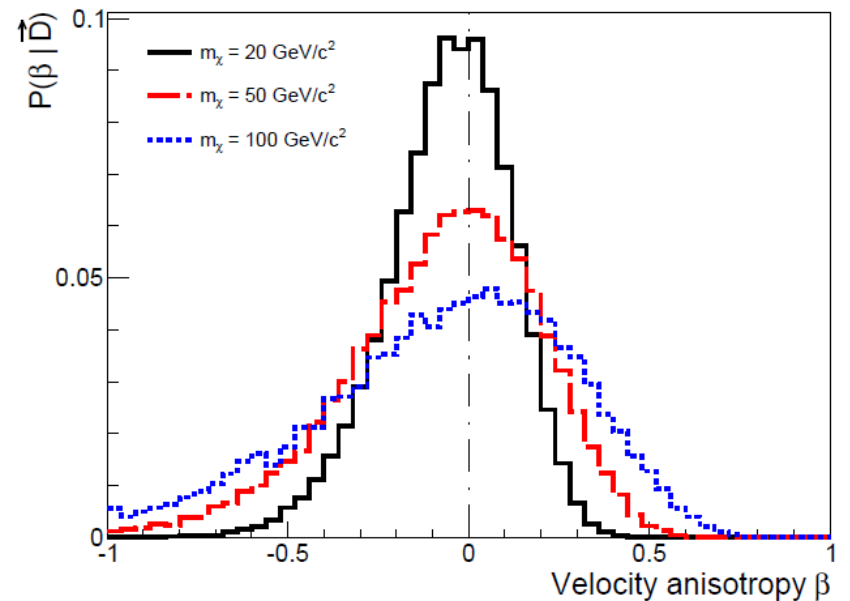
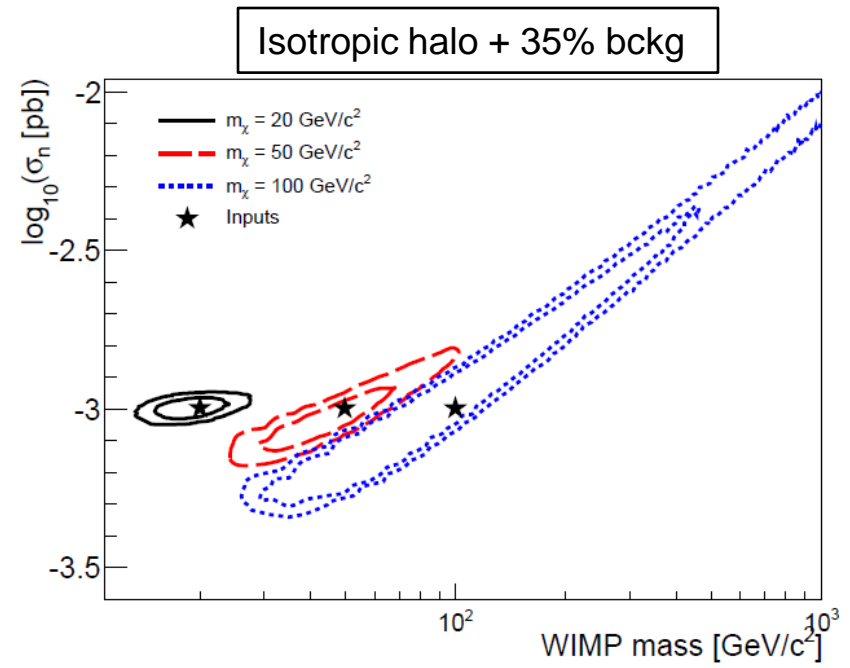
Isotropic halo ($\beta = 0$) with three different masses:

- 20 GeV
- 50 GeV
- 100 GeV

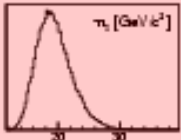
The β parameter is always constrained:

- 20 GeV $\longrightarrow \beta = -0.056^{+0.19}_{-0.12}$
- 50 GeV $\longrightarrow \beta = -0.073^{+0.29}_{-0.18}$
- 100 GeV $\longrightarrow \beta = -0.105^{+0.41}_{-0.24}$

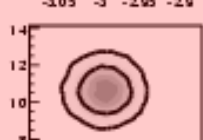
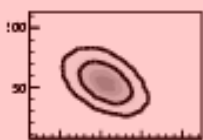
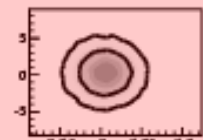
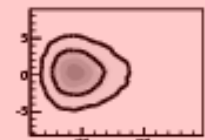
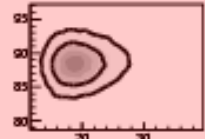
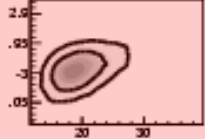
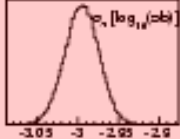
Heavy WIMP implies less stringent constraints



Mass



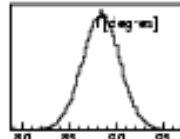
Cross-section



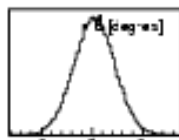
Input:

- isotropic halo: $\sigma_i = 155$ km/s
- cross-section: 10^{-3} pb
- Bckg rate: 10 evts/kg/year (35%)
- **mass: 20 GeV/c²**

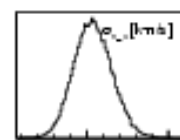
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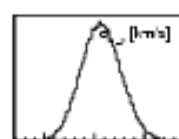
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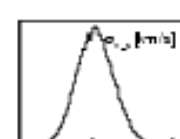
σ_x



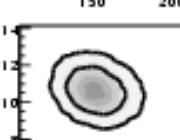
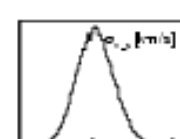
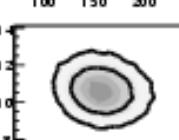
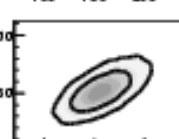
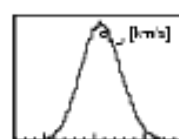
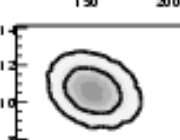
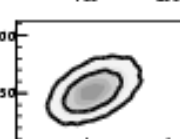
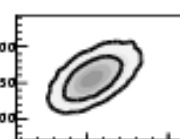
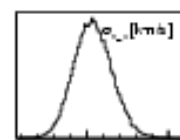
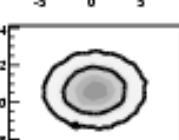
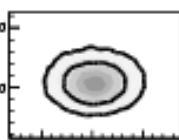
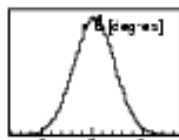
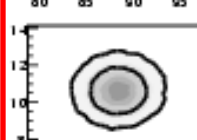
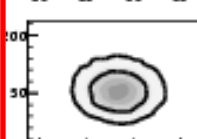
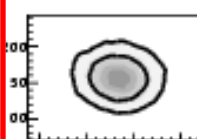
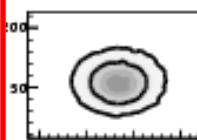
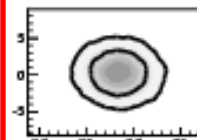
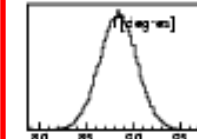
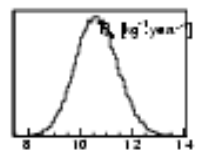
σ_y



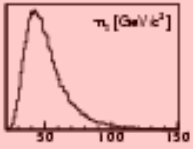
σ_z



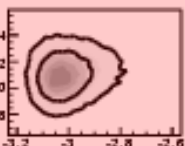
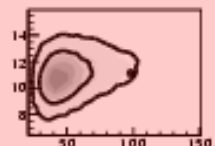
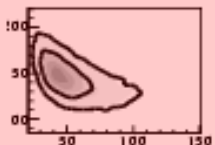
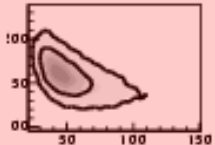
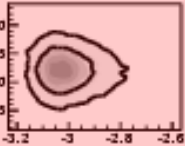
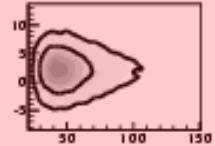
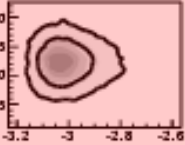
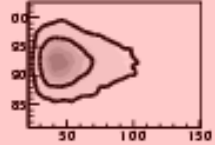
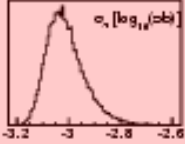
Bckg rate



Mass



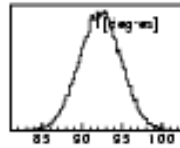
Cross-section



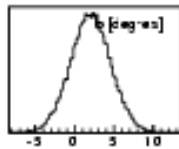
Input:

- isotropic halo: $\sigma_i = 155$ km/s
- cross-section: 10^{-3} pb
- Bckg rate: 10 evts/kg/year (35%)
- **mass: 50 GeV/c²**

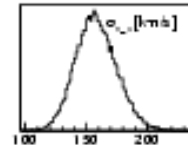
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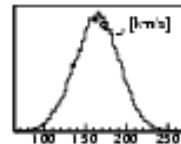
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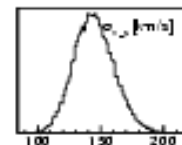
σ_x



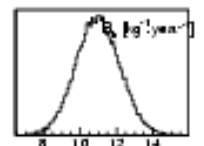
σ_y



σ_z

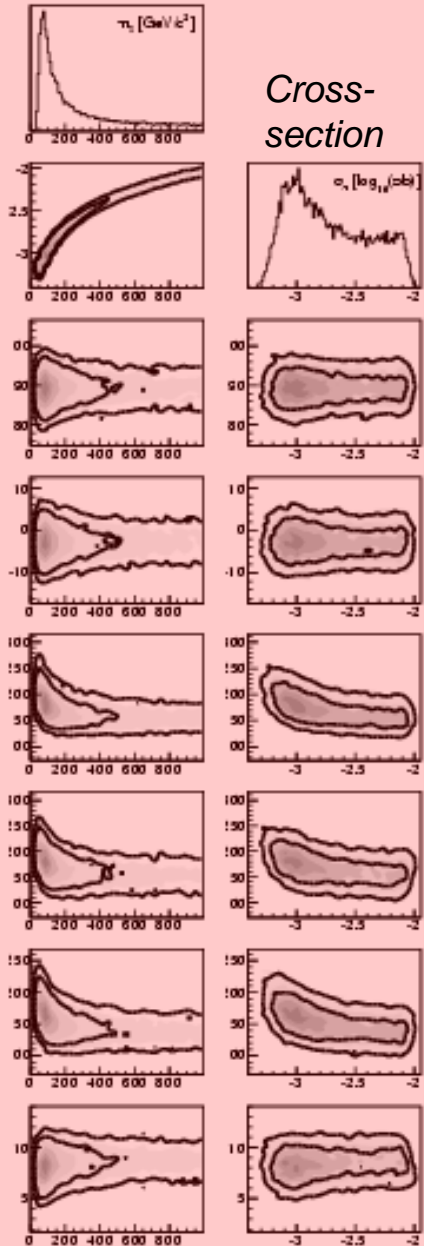


Bckg rate



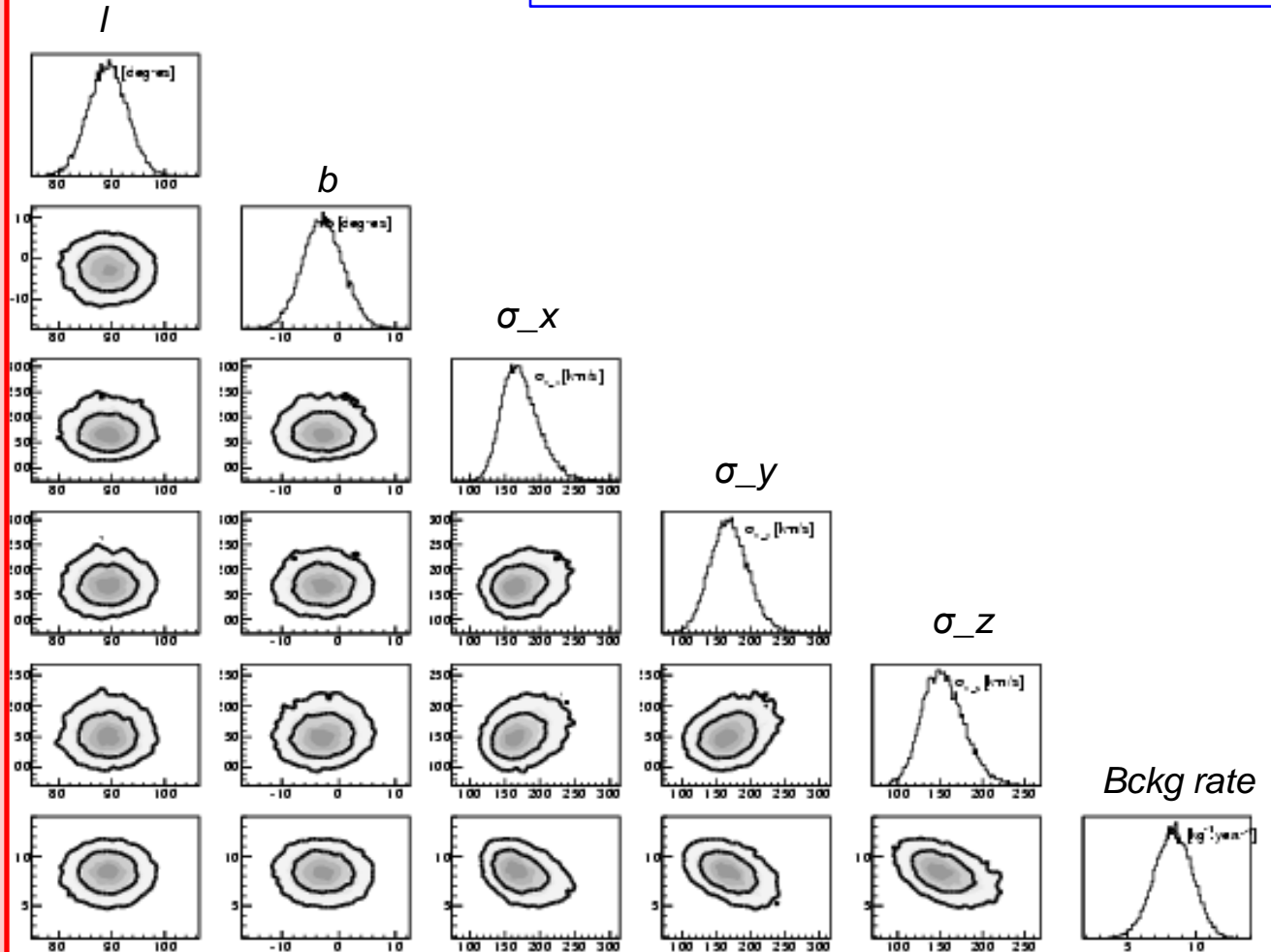
Mass

Cross-section



Input:

- isotropic halo: $\sigma_i = 155$ km/s
- cross-section: 10^{-3} pb
- Bckg rate: 10 evts/kg/year (35%)
- **mass: 100 GeV/c²**



III.e Input halo model

2 input halo models:

Isotropic ($\beta = 0$)

Anisotropic ($\beta = 0.4$)

Similar constraints on $(m_\chi, \log_{10}(\sigma_n))$

The β parameter is well constrained:

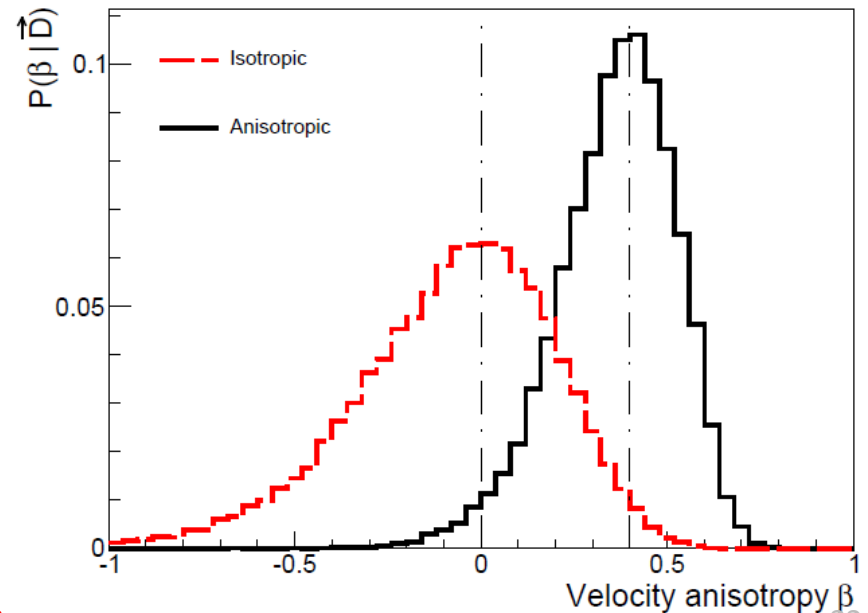
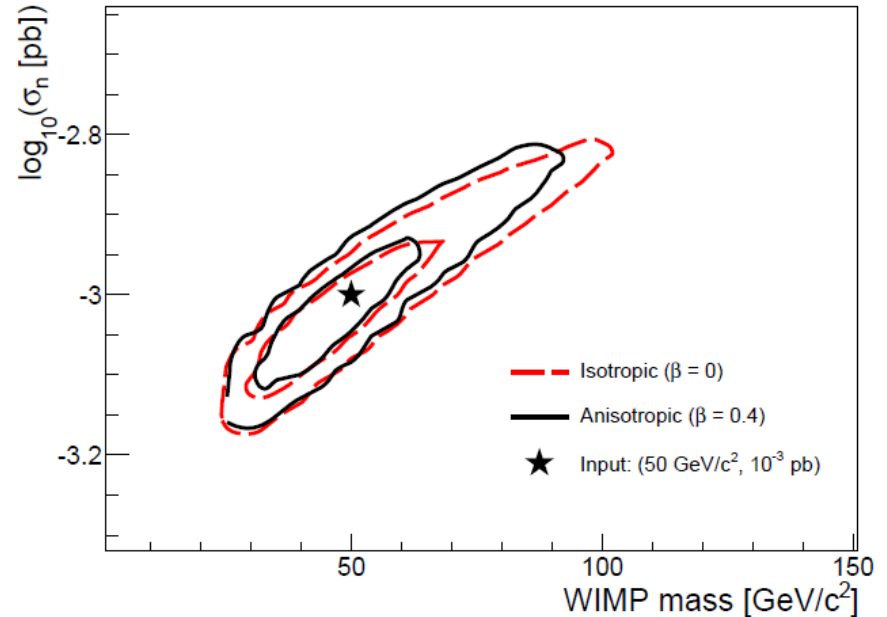
Isotropic $\longrightarrow \beta = -0.073^{+0.29}_{-0.18}$

Anisotropic $\longrightarrow \beta = 0.38^{+0.18}_{-0.10}$

This method allows to:

- *Constrain the Dark Matter halo properties*
- *Constrain the WIMP properties in a « quasi model-independent » analysis*

35% of bckg + 50 GeV/c²



III.e Input Background model

We used 3 input background models:

- No background (optimistic)
- Flat background
- Exponential background (pessimistic)
Similar to the expected WIMP spectrum

The β parameter is well constrained:

No background $\longrightarrow \beta = 0.049^{+0.26}_{-0.10}$

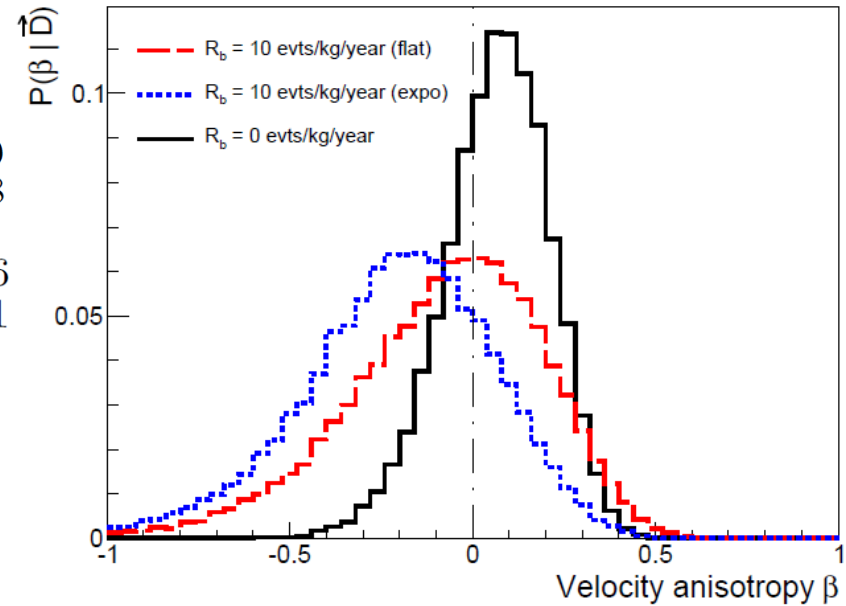
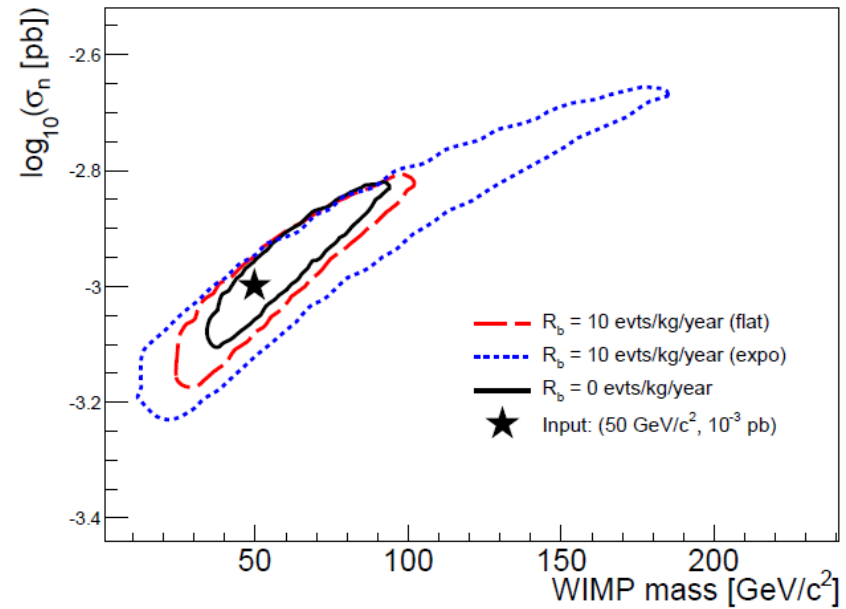
Flat $\longrightarrow \beta = -0.073^{+0.29}_{-0.18}$

Exponential $\longrightarrow \beta = -0.20^{+0.26}_{-0.21}$

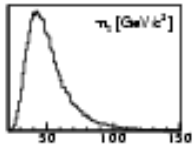
For each background model we have:

- Constraints on the Dark Matter halo
- Constraints on the WIMP properties

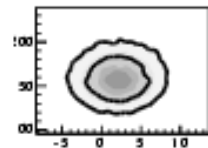
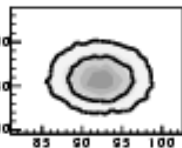
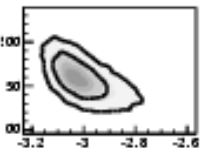
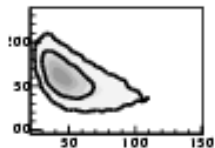
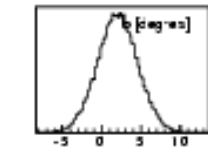
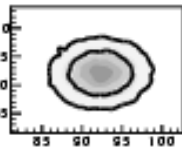
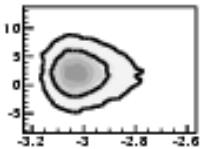
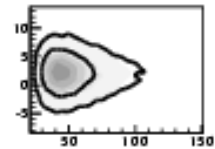
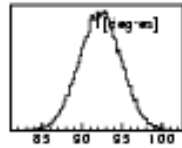
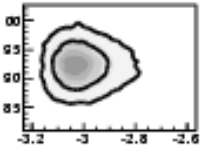
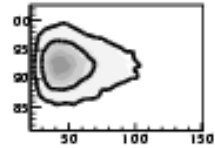
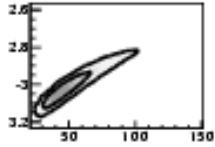
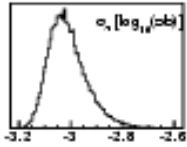
Isotropic halo + 50 GeV/c²



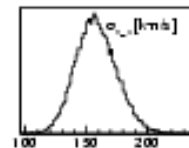
Mass



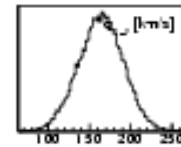
Cross-section



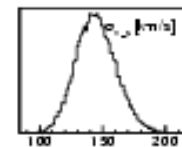
σ_x



σ_y



σ_z

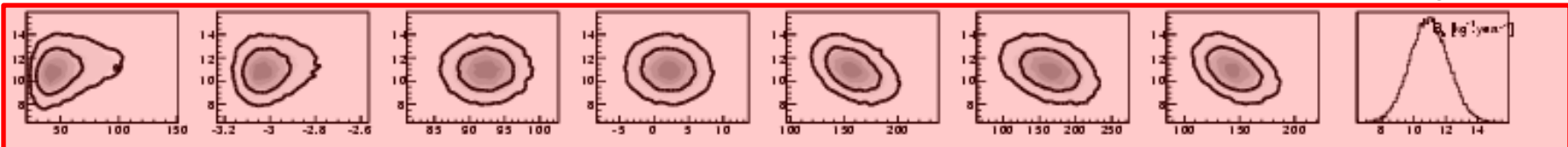


Bckg rate

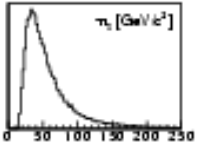


Input:

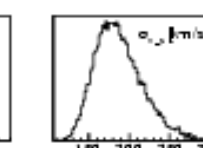
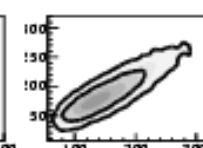
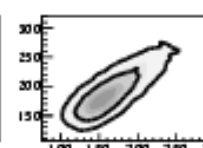
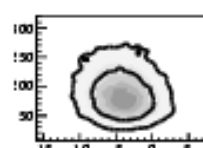
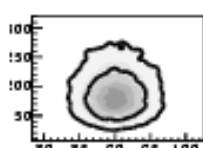
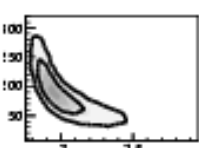
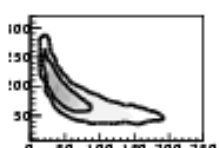
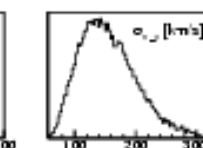
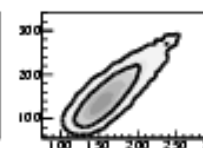
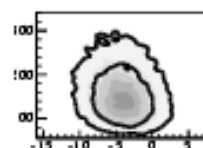
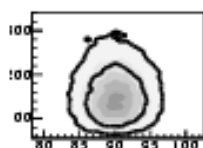
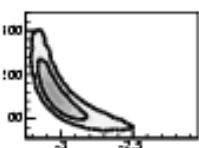
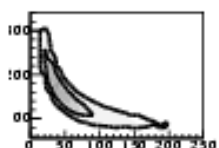
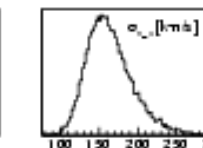
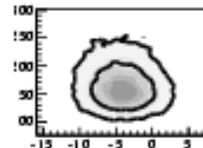
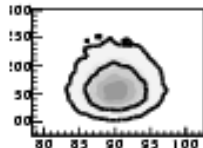
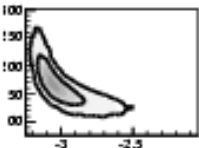
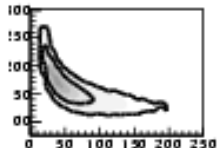
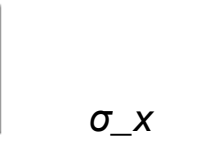
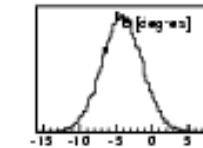
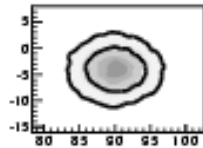
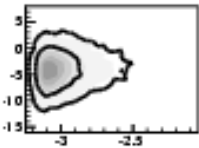
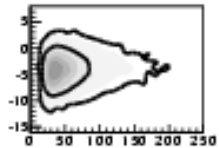
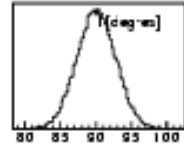
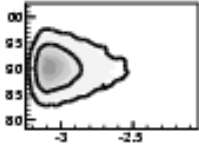
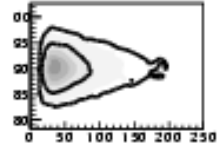
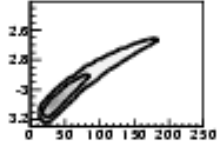
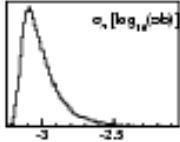
- isotropic halo: $\sigma_i = 155$ km/s
- mass: 50 GeV
- cross-section: 10^{-3} pb
- Bckg rate: 10 evts/kg/year (35%)
- **Bckg model: FLAT**



Mass



Cross-section

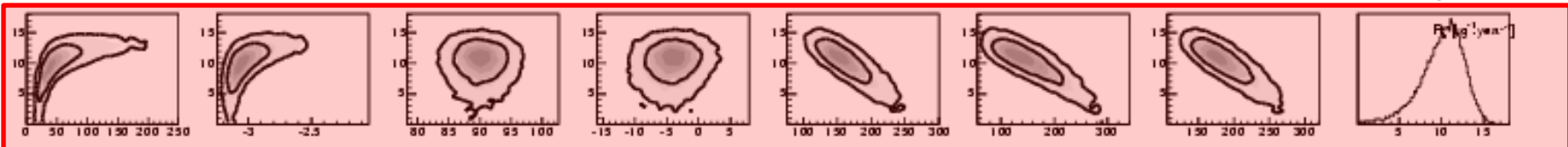


Background rate is less constrained

Bckg rate

Input:

- isotropic halo: $\sigma_i = 155$ km/s
- mass: 50 GeV
- cross-section: 10^{-3} pb
- Bckg rate: 10 evts/kg/year (35%)
- **Bckg model: EXPONENTIAL**



Conclusions & discussion

Development of a « quasi model-independent » MCMC analysis dedicated to directional detection (MIMAC)

The main assumption is: *WIMP velocities are Gaussian distributed*

Main results:

- Constraints on the WIMP velocity distribution
- Constraints on the WIMP properties
- Identification of a genuine WIMP positive detection

works for any input

Going further:

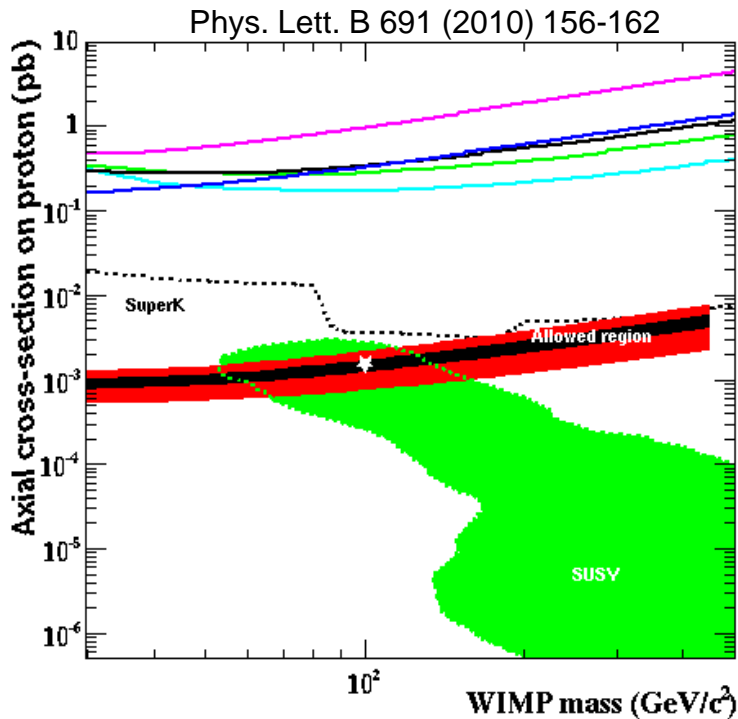
Use of N-Body generated Dark Matter haloes to evaluate effects of substructures: dark-disk, clumps, streams,...

I.c Directional analysis

Using a dedicated statistical methods applied to directional data

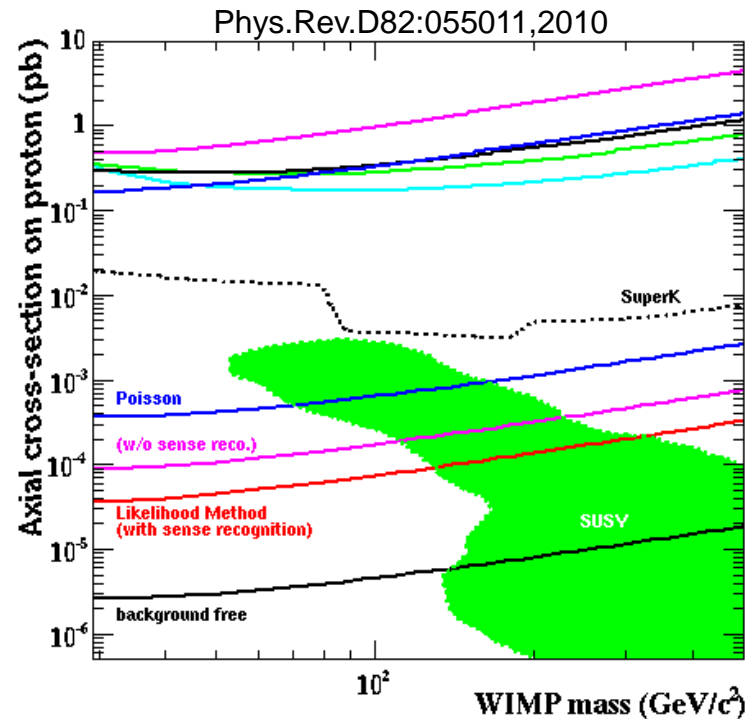
2 possible scenarios

Discovery of Dark Matter



High SD WIMP-proton cross-section
(down to $\sim 10^{-4}$ pb)
High significance discovery of DM

Exclusion of Dark Matter



Low SD WIMP-proton cross-section
(down to $\sim 10^{-4}$, 10^{-6} pb)
Competitive exclusion limits

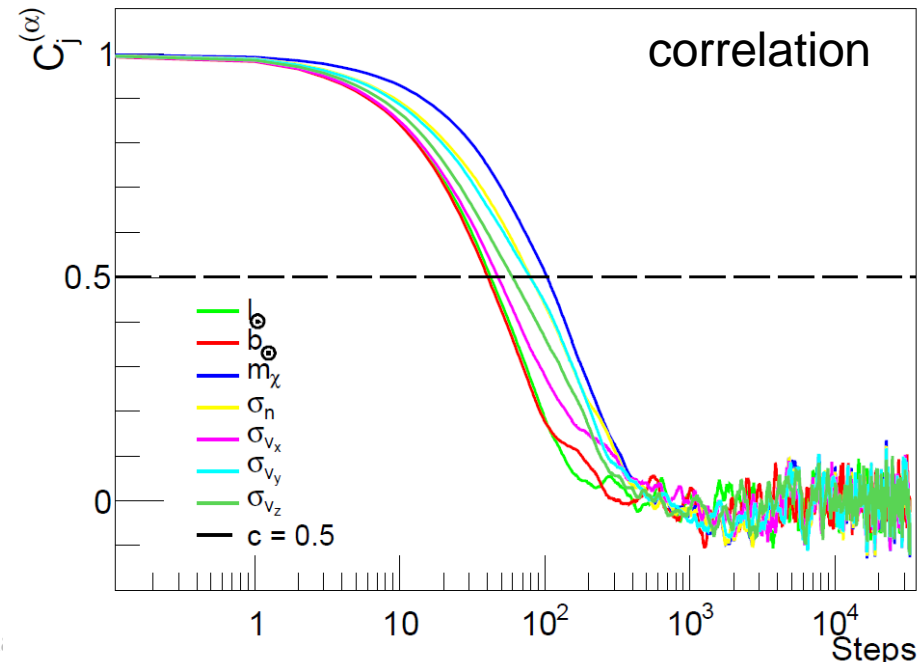
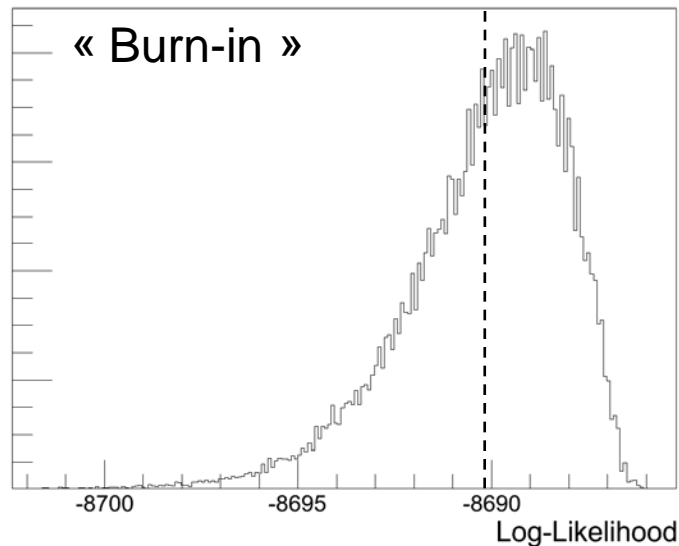
III.c Analyse d'une chaine de Markov

Il y a trois critères très important à prendre en compte:

1. La longueur de « Burn-in » b définie telle que: $p(\vec{\theta}_b) > E[p(\vec{\theta})]$
2. La longueur de corrélation l définie telle que: $l = \max[l^{(1)}, \dots, l^{(\alpha)}, \dots, l^{(m)}]$
Chaque $l^{(\alpha)}$ est défini comme étant égal au plus petit indice j tel que:

$$c_j^{(\alpha)} < 1/2$$

Avec $c_j^{(\alpha)}$ la fonction d'autocorrélation (FFT) du paramètre α



III.c Analyse d'une chaine de Markov

On effectue donc du *sub-sampling* pour ne récupérer que les échantillons indépendants tel que:

$$\vec{\theta}_{i=b+kl}$$

3. Critère de convergence: Il est défini par le ratio qui doit être inférieur à une limite r_c

$$r = \frac{\text{Var} \left[\text{E}(p(\vec{\theta})) \right]}{\text{E} \left[\text{Var}(p(\vec{\theta})) \right]}$$

