Accelerator based neutrino projects in Japan

Takuya Hasegawa (KEK)

First generation

K2K: First Long-Baseline(250km) Neutrino Experiment in the World



• Definitely Measure the Finite Mass Difference of v's with Pure v_{μ} Beam with Well Defined Energy $\langle E_{\nu} \rangle \sim 1.3$ GeV with Fixed Long-Baseline L = 250km

(Motivated by the Claim on the Evidence of Neutrino Oscillation by Kamiokande and Super-Kamiokande)

• First Challenge of This Type of Experiment

Something Unexpected ?? / Something Surprise ??

Final results of K2K

- Obs'ed: 112 evts
- Exp'ed: 158.1 ^{+9.2}_{-8.6} evts
- Combined **4.3**σ effect
 - Null osc. Prob. = 0.0015%

12-GeV PS 2008 Review Report

February 22, 2008

First and foremost, the outstanding K2K long baseline neutrino experiment (E362) -- the first to demonstrate flavor changing oscillations with neutrinos produced by an accelerator -- has been the world leader in substantiating that the observed atmospheric disappearance signal is due to neutrino oscillations. This experiment has now moved to its second stage in the form of the T2K experiment at J-PARC which is being constructed by a very large international collaboration. The rare kaon decay ex-



Definitely confirmed SK atm. v results
The crucial principles of accelerator based long baseline neutrino experiment

have been proven to work

Second generation

J-PARC MW-class accelerator based neutrino beam

TH

inac

RCS (Rapid: Cycling Synchrotron)

Neutrino Beam

Muon Monitor for Neutrino Beam Target Station for Neutrino Beam

Fast Extraction Devices for Acutrine Beam Facility

(Main Ring Synchrotron) 30GeV Improvement from 0.75MW to1.66MW KEK Roadmap

Bird's eye photo in July. 2009

Overview of MR



Three dispersion free straight sections of 116-m long:

- Injection and collimator systems
- Fast extraction (beam is extracted inside/outside of the ring) and RF cavities inside: Neutrino Beamline (intense v beam to the west) outside: Beam abort line
- Slow extraction
 - to Slow extraction Experimental Facility
 - (K Rare decay, Muon Lepton Flavor Violation, hyper nucleus, etc.)

J-PARC MW-class accelerator based neutrino beam



Concept of J-PARC neutrino beam facility

- Preparation section: matching beam optics to arc section
- Arc section: bending the beam $\sim 90^{\circ}$ to SK with superconducting combined function magnet
- Final focus section: matching beam optics to target (position and profile, level of mm control is necessary which correspond to 1mrad v direction, also not to destroy target)
- Graphite Target and Horn Magnet: produce intense secondary π and focus them to SK (3horn system with 320kA pulse operation)
- Muon Monitor: monitor μ direction (=v direction) pulse to pulse with measuring center of muon profile
- On Axis Neutrino Monitor(INGRID): monitor v direction and intensity

*Designed to be up to \sim 2MW beam power is tolerable

Limited by temperature rise and thermal shock

(Al Horn, Graphite Target, Ti Vacuum Window)

*Everywhere high radiation

Careful treatment of radioactive water and air (~ 10 GBq/3week)is necessary Maintenance scenario of radio active beam facility components is necessary



Pointer 36° 23'41 59

T2K has started January 2010



T2K status as of summer 2010



Third generation

For discovery experiment in neutrino physics beyond T2K/NOvA era

- T2K is being conducted to explore $v_{\mu} \rightarrow v_{e}$
- Eager to prove that $\theta_{13} \neq 0$ & measure δ_{CP} :
 - If $\nu_{\mu} \rightarrow \nu_{e}$ signal is found in T2K,
 - Accelerator and Far Detector must be upgraded to measure δ_{CP}
 - If $\nu_{\mu} \rightarrow \nu_{e}$ signal is not found,

Accelerator and Far Detector must be upgraded to continue quest with improved sensitivity by ×10

• In Japan, there is a MW-class proton synchrotron within 10 years

Giant Liquid Argon TPC and/or **Giant Water Cherenkov Detector** as **new Far Detector** in **Japan**

Discovery of nucleon decay

Long baseline neutrino experiment requires highly massive main/far detector

As a consequences

Nucleon decay experiment Research on grand unification is also possible

Giant Liquid Argon TPC and/or **Giant Water Cherenkov Detector** for **Nucleon Decay Experiment** in **Japan**

Quest for the Origin of Matter Dominated Universe

- Lepton Sector CP Violation
 - Search for CP violation in Neutrino Oscillation Process
 - Also examine mass hierarchy of neutrinos
 - Also examine matter effect in neutrino oscillation process
- Proton Decay
 - $\begin{array}{ll} & p \rightarrow \nu \ K \\ & p \rightarrow e \ \pi^0 \end{array}$

*Non-equilibrium environment in the evolution of universe is assumed

Same scientific direction as LAGUNA

Three possible scenario studied at NP08 workshop

Артем



J-PARC Neutrino Beam Upgrade Plan

MR Power Improvement Scenario toward MW-class power frontier machine — KEK Roadmap —

	Day1 Achieved ! (up to Jul.2010)	Next Step	KEK Roadmap
Power(MW)	0.1	0.45	>1.66
Energy(GeV)	30	30	30
Rep Cycle(sec)	3.5	2.2	1.92~0.5
No. of Bunch	6	8	8
Particle/Bunch	1.2×10^{13}	2.5×10^{13}	$4.1 \sim 8.3 \times 10^{13}$
Particle/Ring	7.2×10^{13}	2.0×10^{14}	$3.3 \sim 6.7 \times 10^{14}$
LINAC(MeV)	181	181	400
RCS	h=2	h=2	h=2 or 1

Combination of High rep. cycle and High beam density

Items to be modified from DAY1 toward MW-class power frontier machine

- No. of Bunch in MR($6 \rightarrow 8$)
 - Fast Rise Time Extraction Kicker Magnet
 - \rightarrow Installation is on-going now
- Increase Repetition Rate $(3.5Sec \rightarrow 0.5Sec)$
 - RF and Magnet Power Supply Improvement
- RCS h=1 Operation (longer beam bunch to decrease space charge effect)
 - RF Improvement h=2: 2 bunches × 4cycle injection to MR
 h=1:Single bunch with doubled no. of proton × 8cycle injection
- LINAC 400MeV Operation (avoid severe space charge effect at RCS injection)
 → Construction of necessary component is approved and started

Far Detector Options

How to approach Lepton Sector CP Violation



- ν_e Appearance Energy Spectrum Shape
 *Peak position and height for 1st, 2nd maximum and minimum
 *Sensitive to all the non-vanishing δ including 180°
 *Could investigate CP phase with v run only
- Difference between v_e and $\overline{v_e}$ Behavior

*Need both v and \overline{v} experiments (different systematics, low \overline{v} event rate)

Angle and Baseline



Optimal configuration for the investigation of CP Phase δ_{CP} with Liquid Argon TPC

• Reason

- Excellent v energy resolution and reconstruction ability from sub GeV to a few GeV, from single prong to high multiplicity
 - \rightarrow Suitable for spectrum measurement with wide energy coverage
- Excellent π^0 /electron discrimination
 - \rightarrow Wide band On-Axis beam is tolerable
- Neutrino intensity is finite and Energy is set (1.66MW J-PARC MR, 30GeV)
- Results within reasonable time scale (\sim 5years)

Spectrum measurement (1st and 2nd Oscillation Max.) with On-Axis beam with 5years v beam run, then think next (\overline{v} ?)

• Condition

- Need long baseline(>600km) to see 2nd Osc. max, since fixed neutrino energy
- Need On-Axis beam for wide energy coverage
- Need gigantic detector, since finite beam flux and long baseline

100 kton Giant Liquid Argon TPC @ Long Baseline, On-Axis



 \rightarrow Extract δ_{CP} from fit of 1st & 2nd maximum



 \rightarrow Extract δ_{CP} from fit of 1st & 2nd maximum



P32: Proposal submitted to J-PARC PAC Recommended by J-PARC PAC January 2010

6. PROPOSAL EVALUATIONS

 P32: (Towards a Long Baseline Neutrino and Nucleon Decay Experiment with a next-generation 100 kton Liquid Argon TPC detector at Okinoshima and an intensity upgraded J-PARC Neutrino beam)

The proponents propose to develop a suitable scalable Liquid Argon TPC detector with gas amplification in Argon vapor as an R&D for a next-generation long baseline neutrino experiment.

The PAC acknowledges the high scientific merit of a neutrino oscillation experiment with a baseline longer than T2K. The measurements of the mixing angle θ_{13} and a possible CP violation in the lepton sector are of highest significance.

Before large detectors can be considered, it has to be shown that such a technique is adequate for the purpose and superior to alternative schemes. In particular, the readout scheme and the scalability are open questions. Based on a small-scale R&D, a roadmap has to be put forward.

The specific P32 proposal is to set up and test a 250 Liter LAr prototype TPC in a low-energy charged particle beam at J-PARC, preferentially with kaons from the K1.1BR beamline. The PAC encourages the team to proceed with this development work and recommends the allocation of beam time of a low intensity charged particle beam at J-PARC for this test.

250L Liq. Ar TPC

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250L Liq. Ar TPC

Optimal configuration for the investigation of CP Phase δ_{CP} with Water Cherenkov detector (same concept as T2K)

- Reason
 - Excellent v detector for sub GeV(Quasi elastic dominant, low multiplicity)
 - Neutrino intensity is finite and Energy is set (1.66MW J-PARC MR, 30GeV)
 - \rightarrow Oscillation maximum at sub GeV
 - \rightarrow Baseline to be ~300km
 - Enhancement of the beam intensity at the oscillation maximum
 - Beam configuration to avoid π^0 originated background is helpfull
 - \rightarrow Narrow band Off-Axis beam is only choice

Comparison between v and \overline{v} behavior at the oscillation maximum with Off-axis beam

• Condition

- Off-Axis beam (2.5⁰) for appropriate beam energy and suppress π^0 originated background
- Baseline to be 275km
- Need gigantic detector and relatively short baseline, since finite beam flux

> 270 kton × 2 Water Cherenkov Det. @ Kamioka, 2.5deg Off-Axis

Scenario 3 *J-PARC to Kamioka and Korea* •Cover 2nd Maximum @ Korea

Sin²(2 $\theta_{_{13}}$)=0.04, neutrino, normal hierarchy, Scenario B F.Dufour@NP08

(study is initiated by M.Ishitsuka et. al. hep-ph/0504026)

Comparison of Each Scenario

	Scenario 1 Okinoshima	Scenario 2 Kamioka	Scenario 3 Kamioka Korea
Baseline(km)	660	295	295 & 1000
Off-Axis Angle($^{\circ}$)	0.8(almost on-axis)	2.5	2.5 1
Method	v _e Spectrum Shape	Ratio between $v_e \overline{v}_e$	Ratio between $1^{st} 2^{nd}Max$ Ratio between $v_e \overline{v}_e$
Beam	5Years $v_{\mu,}$ then Decide Next	2.2 Years $v_{\mu,}$ 7.8 Years $\overline{v}_{\mu,}$	5 Years $v_{\mu,}$ 5 Years $\overline{v}_{\mu,}$
Detector Tech.	Liq. Ar TPC	Water Cherenkov	Water Cherenkov
Detector Mass (kt)	100	2×270	270+270

Study is continuing to seek for optimum choice

Third generation projects

□ Strong physics case for

New long baseline experiment with expected J-PARC beam and to

Search for nucleon decay

with

Giant Liquid Argon TPC and/or Water Cherenkov Detector in Japan

□ What's important to realize the project

- ➢ J-PARC MR towards MW-Class power frontier machine
- Successful R&D and performance evaluation with clear objective towards realization of Giant Detector
- > Decision should be based on T2K results on $v_{\mu} \rightarrow v_{e}$

Third generation projects

□ Strong physics case for

New long baseline experiment with expected J-PARC beam and to

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Giant Liquid Argon TPC and/or Water Cherenkov Detector in Japan

Same scientific direction as LAGUNA

•International collaborative effort is mandatory necessary for this scale of projects

•Fruitful collaboration on Liq. Ar TPC is already existing

objective towards realization of Giant Detector

► Decision should be based on T2K results on $v_{\mu} \rightarrow v_{e}$

Accelerator Based Neutrino Projects in Japan

	K2K	T2K	3 rd Generation Exp. (KEK Roadmap)
High Power Proton Synchrotron	KEK PS 12GeV 0.005MW Existing	J-PARC MR 30GeV 0.75MW Brand New	J-PARC MR 30GeV 1.66MW Technically Feasible Upgrade
Neutrino Beamline	K2K Neutrino Beamline Brand New	J-PARC Neutrino Beamline Brand New	J-PARC Neutrino Beamline Existing
Far Detector	Super Kamiokande Existing at KAMIOKA	Super Kamiokande Existing at KAMIOKA	Brand New -Detector Technology ? -Place ? (Angle and BaseLine)
1 st Priority Physics Case	Neutrino Oscillation v_{μ} Disappearance	Neutrino Oscillation $v_{\mu} \rightarrow v_{e}$	Lepton Sector CP Violation + Proton Decay Search

Able to concentrate on Far Detector issue toward the 3rd Generation Experiment after T2K startup

Summary Accelerator Based Neutrino Projects in Japan

* Long Baseline Neutrino Exp. is initiated with K2K Short Term

- Beam commissioning of J-PARC MR has started May-2008
- Commissioning of J-PARC Neutrino Beam Facility has started in April-2009
- T2K has started January-2010 to conclude "lepton flavor mixing structure"

Mid Term

- T2K data with 1-2MW × 10⁷sec integrated proton power on target will provide critical information on θ_{13} , which guides the future direction of the neutrino physics *In any case, complete T2K proposal of 3.75MW × 10⁷sec
- KEK Roadmap: MR toward MW-class power frontier machine
- Submit proposal

"J-PARC to Somewhere Long Baseline Neutrino Experiment and

Nucleon Decay Experiment with Giant Detector"

and construct Giant Detector

Long Term

• Discovery of CP violation in Lepton Sector (also Proton Decay)

P32 and Okinoshima site study

 A.Badertscher, A.Curioni, S.DiLuise, U.Degunda, L.Epprecht, L.Esposito, A.Gendotti, S.Horikawa, L.Knecht, C.Lazzaro, D.Lussi, A.Marchionni,
 A.Meregaglia, G.Natterer, F.Petrolo, F.Resnati, A.Rubbia, C.Strabel, T.Viant ETH Zurich, 101 Rämistrasse, CH-8092 Zurich, Switzerland

H.Naito, S.Narita Iwate University, Morioka, Iwate, 020-8551, Japan

O.Araoka, T.Hasegawa, K.Kasami, N.Kimura, T.Kobayashi, M.Maki, T.Maruyama, K.Nishikawa, M.Tanaka, M.Yoshioka KEK High Energy Accelerator Research Organization, 1-1, Oho, Tsukuba, Ibaraki, 305-0801, Japan

O.Hirabayashi, K.Kawakami, T.Kaneta, T.Oshimo, S.Taguchi PENTA-OCEAN construction co., Ltd., 2-2-8 Koraku, Bunkyo-ku, Tokyo, 112-8576, Japan

J.Naganoma, Y.Nagasaka, H.Okamoto, K.Yorita Waseda University 3-4-1 Okuba, Shinjuku-ku, Tokyo 169-8555, Japan

An example of performance evaluation with clear objective: 250L@KEK

Measurements with well defined charged particle test beam

- To benchmark performance of detector
- To develop realistic simulation/reconstruction software
- Cryogenic vessel with beam window (originally for MEG liquid Xe calorimeter test module)
- Ultra-Vacuum established
- Cryocooler and liquid Argon filling under investigation
- Liquid Argon purification system under procurement
- Exposure to low-momentum separated K beam @J-PARC $p \rightarrow v K(340 \text{MeV/c K}^+)$

rarameters for 250L@KEK	
Fiducial mass	170 kg
Total Liquid Argon mass	\sim 400 kg
Field cage dimensions	$42 \times 42 \times 78 \text{ cm}^3$
Fiducial volume	$40 \times 40 \times 76 \text{ cm}^3$
Drift field	1 kV/cm
Max. drift voltage	40 kV
Readout method	Double phase, Two view anode LEM-TPC
Readout segmentation	Two 40 \times 38 cm ² LEM-TPC
Readout pitch	3mm in x & y
Number of readout channels	288 per LEM-TPC 576 in total
LEM-TPC effective gain	~ 25

340 MeV/c K⁺ ($p \rightarrow Kv$) in 250L@KEK

First beam exposure

in October 2010

Total energy deposit

200

- >90% of slow kaons stop in detector with range ≈ 10 cm (others decay in-flight)
- Many soft decay products are contained
- dE/dx analysis can be performed for particle ID

250L@KEK: Cryogenics

- GM Cryocooler

LN₂ Coil

- Heat input of 250L cryostat: ~ 30W
- GM Cryocooler (~150W)
 - For normal operation
- LN₂ heat exchange coil (~500W)
 - Additional cooling equipment for pre-cooling, filling, and recirculation for purification
- Successful filling of the vessel
 - ~ 3 hours for pre-cooling
 - 7 hours for 100L filling
 - ~ 50 L/hour (in case the vessel is cold enough)
- Stably kept ~1 week with cryocooler

250L@KEK: Purification

- Purification @ initial filling with purification filter (Activated Cu + Molecular sieve, possible to regenerate)
 - Initial purity after filling
 <ppb (>50 cm eq. of drift electron att. length)
 - ~3ppb/day purity degradation is observed (No degradation if cryocooler is OFF)
- Purity improvement with gas recirculation + high spec. purification filter is under development

Cosmic ray signal registered with temporary coarse anode

Okinoshima: Geology and Geography

ASAHI quarry

Islands were born by volcanic activity in 5~6M years ago.

BUT, bedrock is the oldest rock in Japan (2G years), which A single layer of thehassbeen left as →Oki-Gneiss TOKUHATA No.2 Suitable for Big Cavern Construction

> There are several quarries, Rhyolite good for direct observation

of geology. Plan E.I

The crackle of the Igneous rock PENTA-OCEAN construction ico

Dacite

OKI Gneiss

Andesite

Basalt

100 kton Giant Liquid Argon TPC Preliminary design (used for cost estimate)

Okinoshima: Infrastructure

SAIGOU Large electric power station enough for our facility

Okinoshima: Liquid Argon supply

Most efficient way is to use presently available ferry liner

Neutrino event rate and experimental sensitivity

Events in 100 kton, 658 km, 5 years @ 1.66 MW

	No Osc.	ν _μ CC	v_e CC	$\overline{\nu_{\mu}}$ CC	v _e CC]
	5 years	82000	750	1460	35	
δ	cp (deg)	0	90	180	2	270
sin ²	2θ ₁₃ =0.1	2867	2062	2659) 3	464
sin²2	θ ₁₃ =0.05	1489	1119	1342	2 1	908
sin²2	θ ₁₃ =0.03	942	506	829	1	266

- * $\times 10$ larger total events than T2K
- High detection efficiency, excellent background suppression, high precision electron neutrino energy spectrum measurement
- CP discovery exceeds 3σ for $\sin^2 2\theta_{13} > 0.02$
- measure θ_{13} with $\delta \sin^2 2\theta_{13} \approx \pm 0.01$ and test CP at better than 90%CL if $\sin^2 2\theta_{13} > 0.01$
- $sin^2 2\theta_{13} < 0.001$ @ 90%CL (if no signal is found) one order better than T2K

J-PARC to Okinoshima

CP Discovery potential

Mass hierarchy investigation

Fig. 7: Mass hierarchy investigation with neutrino run only. If fits with both hierarchy hypotheses provide neither 0 nor 180°, one can declare discovery of CP violation in the leptonic sector. If any of the fits results in a δ_{CP} of 0 or 180°, then an anti-neutrino run could be envisaged.

Mass Hierarchy Determination - 1.6MW - 100 kton

Fig. 10: Mass hierarchy discrimination at 90% C.L. and 3σ for 5+5 years neutrino-antineutrino runs.

T2K θ_{13} sensitivity

1st Liq. Ar TPC Signal with Cosmic Ray in Japan

Trigger Counter set up

- HV setting
 - Cathode -2500 V
 - Grid -1000 V
 - Cathode-anode; 5cm
 - Oscilloscope waveform
 - Ch1 is the fastest signal
 - Drift time ~20 μs

Anode: $4ch \times 2.2cm \times 9cm$

The new LAr LEM-TPC

LAr LEM TPC = Double phase TPC with gain in GAr vapor

Motivated by the very long drift path needed in giant detectors hep-ph/0402110, arXiv:0811.3384, NIM A617(2010)188, and DM applications (keV detection) J.Phys.Conf.Ser.171:012020,2009, arXiv:1001.0076 segmented anode amplification stage Continuous waveform recording GAr electrons □ image Time Preamplifier Memory Shaping Amplifier FADC **AAA**.3 kV/cm Buffer ions 1 kV/cm ionization ... extraction Readout grids Cosmic tracks in 3 lt prototype (G \approx 6): LAr <u>\$</u>50 scintillation PMT cathode PMT signal dQ/dx distribution dE/dx-0.01 -0.012 strip number strip number time (ue) #Oldx (#C/c

LAR LEM-TPC 3L @CERN 100 x 100 mm² test setup

Produced by standard PCB technique

- Double-sided copper-clad (18 µm layer) FR4 plates, 1.6 mm thick
- Precision holes made by drilling
- Gold deposition on Cu (<~ 1 μm layer) to avoid oxidization
- HV decoupling (cryo-) capacitors & surge arrestors embedded

10cm

X-Y projective anode (NEW)

600 x 600 mm2 THGEM protoypes

Cosmic tracks in 3L@CERN with new two view anode Double phase (1.0 bar, 87K) **Two view anode** Single stage LEM amplification • Decouple the amplification and the readout stages Two view anode charge readout The charge is equally shared between X and Y (3mm pitch) strips O_2 contamination: $\sim 2ppb$ • Same signal shape of both coordinates Gain: ~ 25 xView signals (event 1898) xView signals (event 1765) yView signals (event 1898) yView signals (event 1765) 1400 1400 1000 1000 1200 1200 800 600 600 400 200 xView event display (event 1765) yView event display (event 1765) xView event display (event 1898) vView event display (event 1898) 4000 A000 200 200 amplitude (300 amplitude 150 150 150 200 200 100 100 100 100 100 25 30 25 25 30 25

strip number

strip number

strip number

6m3 @ CERN

A. Curioni et al., GLA2010 workshop

Partial pressure of impurity (mbar) in 1 bar ppb argon

- •R&D towards non evacuated vessels on large vessel
- •Purity measured with direct scintillation light measurement !
- •First test purging satisfactory!
- •Piston effect seen
- •Reached **3ppm** O₂ contamination via flushing
- •Gas recirculation under construction

Very high drift "high" voltage... S. Horikawa et al., GLA2010 workshop

ArDM-1t detector

Extrapolation to long drift

Extrapolation of the ArDM design

Changing Cs for fixed Cp = 2.35 pF and Vpp-in = 2E = 2.5 kV **ArDM**

Drift length	m	1.24	5	10		20
Total output voltage for I kV/cm	V	l 24k	500k	IM		2M
nput voltageVpp-in = 2E	۷	820	2.5k	2.5k	$\times \sqrt{2}$	3.5k
Shunt capacitance, Cp	F	2.35p	2.35p	2.35p	$\times 1/2$	І.1 8 р
Capacitor	F	328/164n	475n	Ι .90 μ	L L	Ι .90 μ
Number of stages, N	Ι	210	319	638		903
N per 10 cm	Ι	16.9	6.38	6.38		4.51
Total capacitance	F	l 25µ	303µ	2.43m		3.43m
Capacitance per 10 cm	F	Ι0.4μ	5.99µ	24.3µ		Ι 7.2 μ
Total stored energy	J	21.7	948	7.58k		21.5k

Actual ArDM parameters are given just for comparison.

For extrapolation, $2\gamma N = 1.42$ is always assumed.

LAr vaporization heat 160 kJ/kg

7.2µ 1.5k $V_{
m max} = rac{E}{\gamma}, \,\, \gamma pprox \sqrt{rac{C_{
m p}}{C_{
m r}}}$