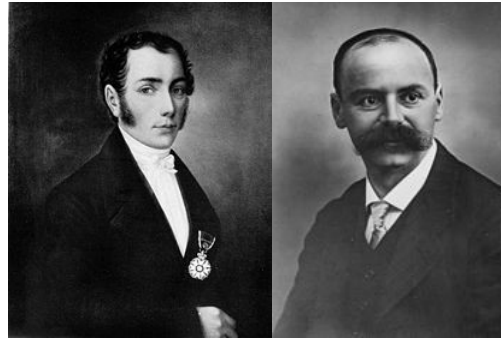




LUDWIG-
MAXIMILIANS-
UNIVERSITÄT
MÜNCHEN



How to ease the Hubble tension



MODIFIED RECOMBINATION IS WEIRD

Varying m_e (+ Ω_k)



(pass 3 of 3 tests)

EDE, NEDE, EMG
Majoron, WZDR



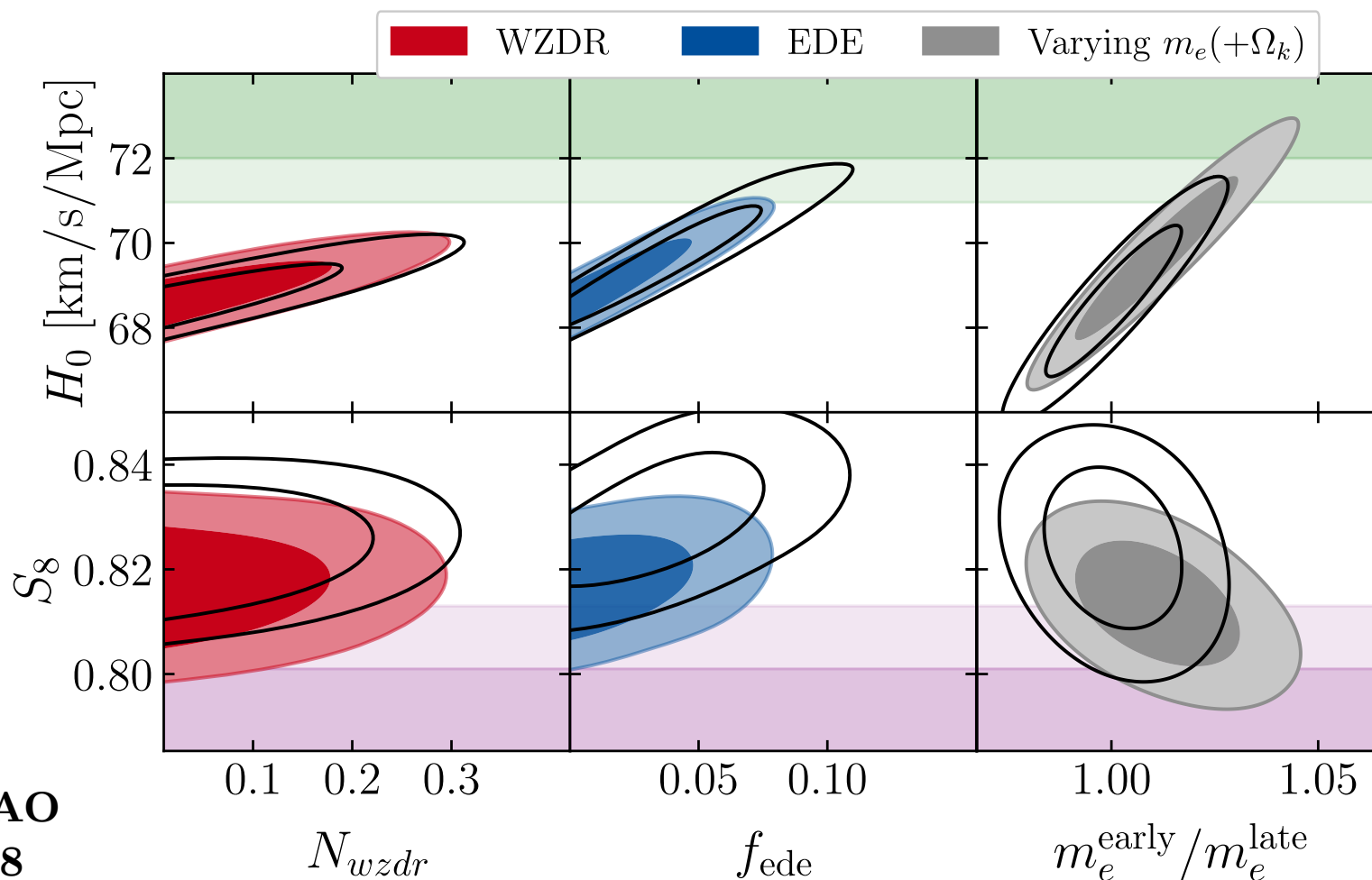
(pass 2 of 3 tests)

Primordial B
SIDR



(pass 1 of 3 tests)

MODIFIED RECOMBINATION IS WEIRD



CMB+BAO
+SN + S8

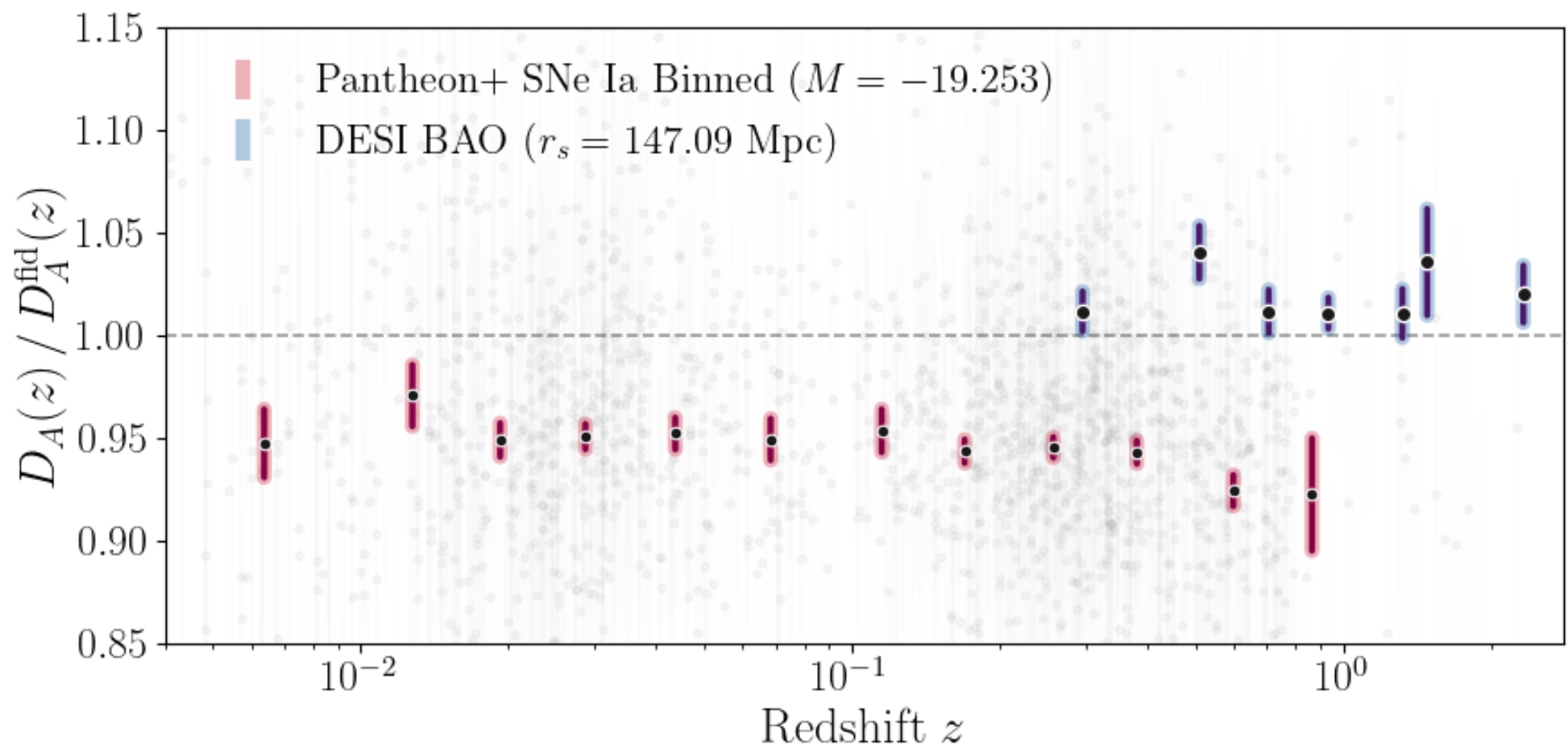


HOW DOES THIS MODEL WORK?

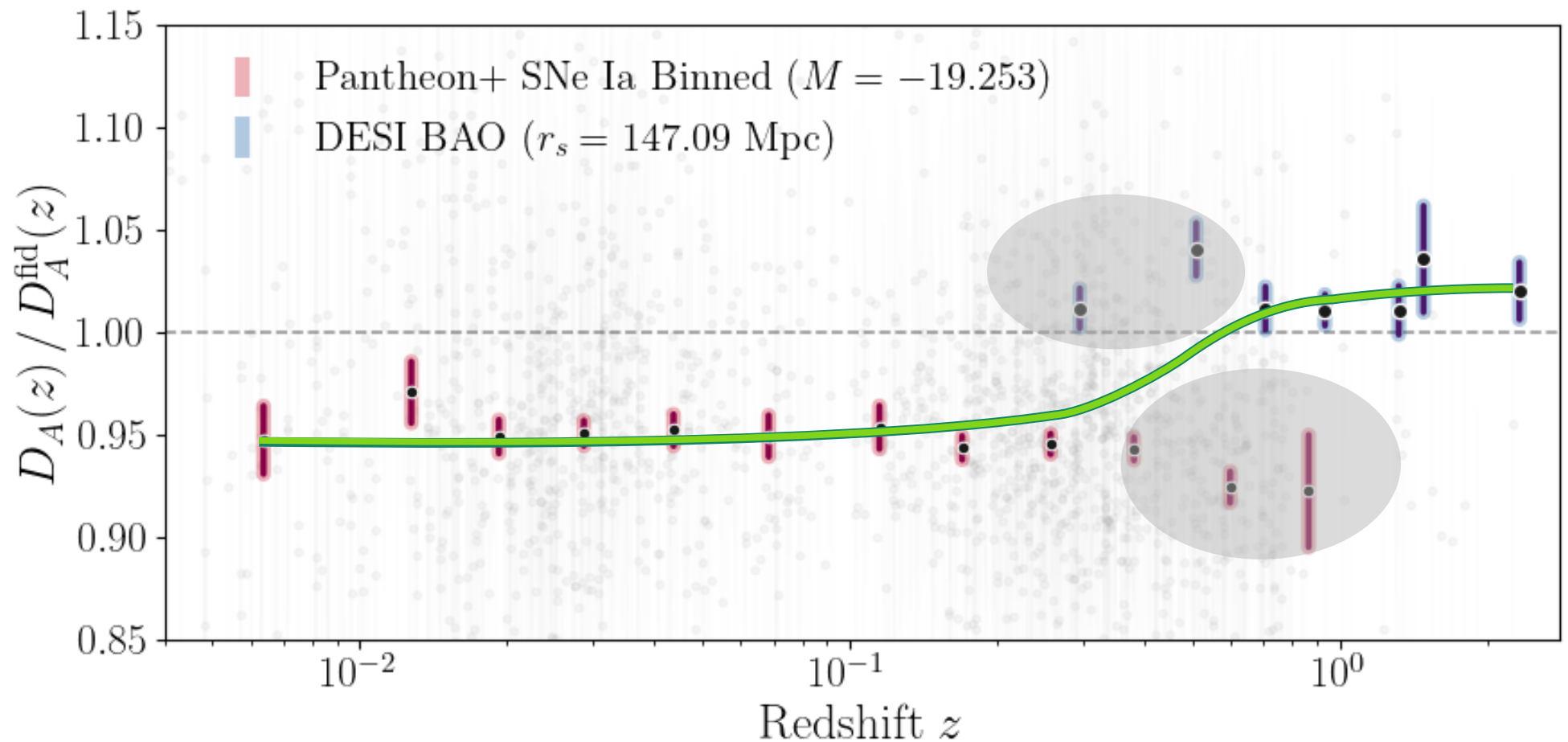
~~HOW DOES THIS MODEL WORK?~~

HOW DOES *ANY* MODEL WORK?

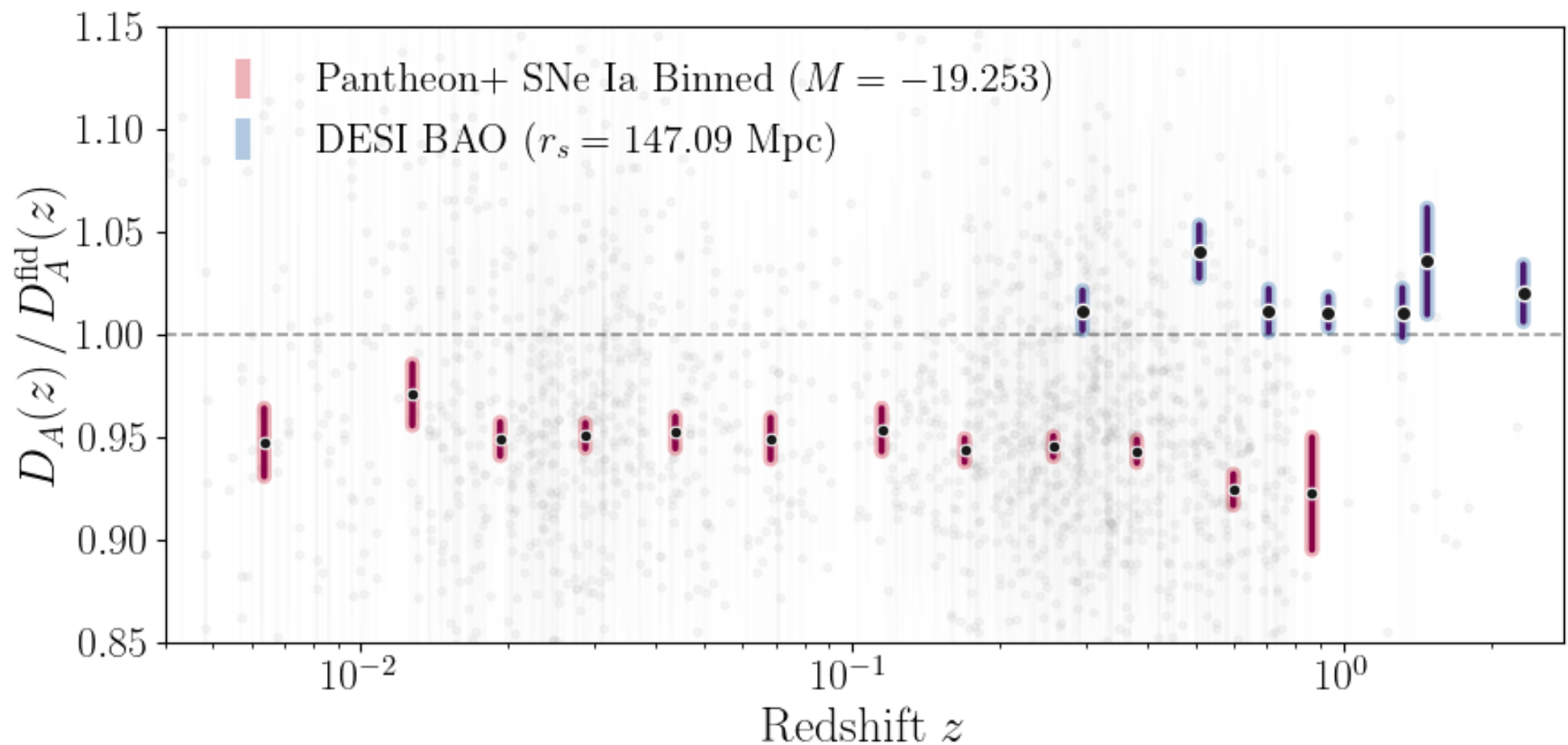
COSMIC CALIBRATOR TENSION



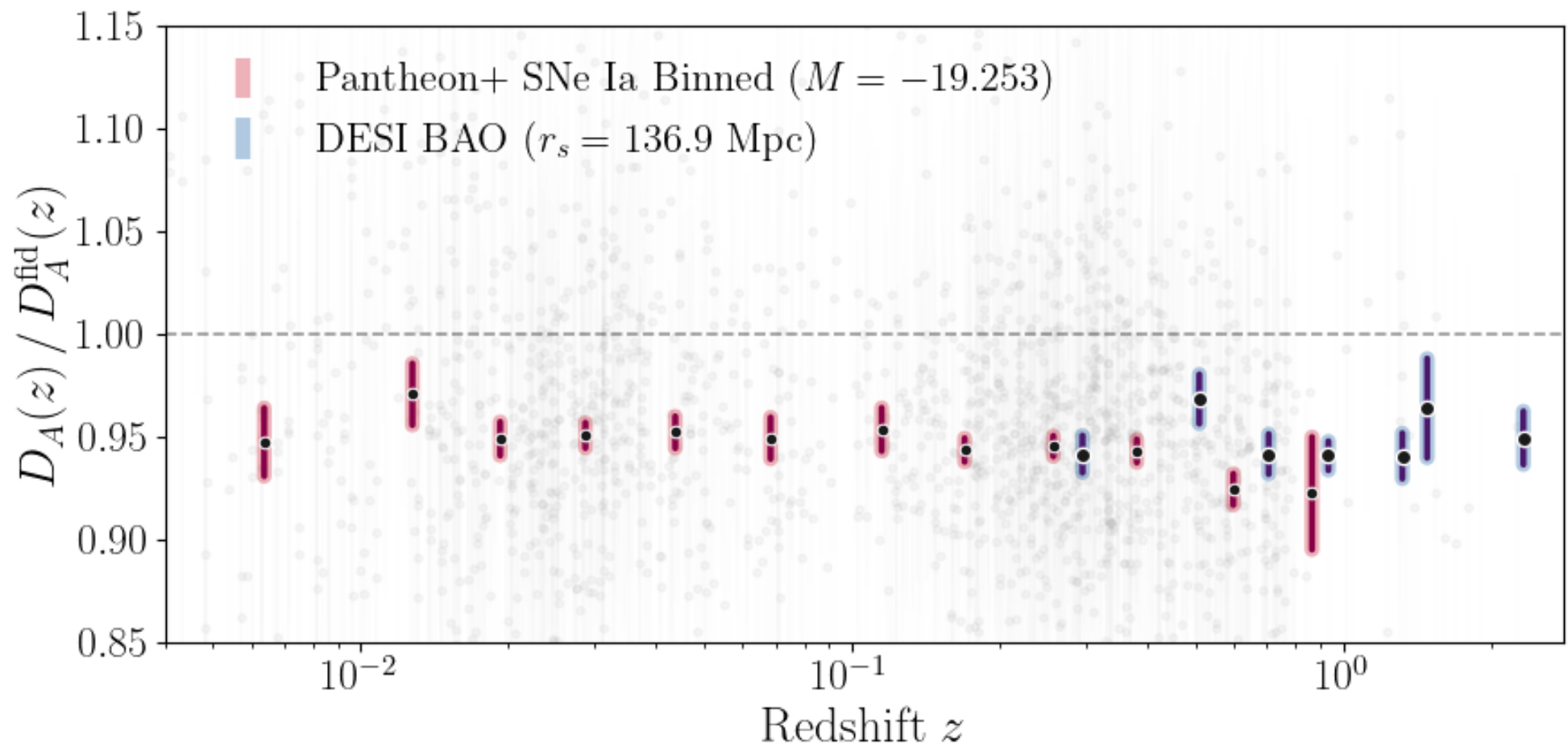
COSMIC CALIBRATOR TENSION



COSMIC CALIBRATOR TENSION

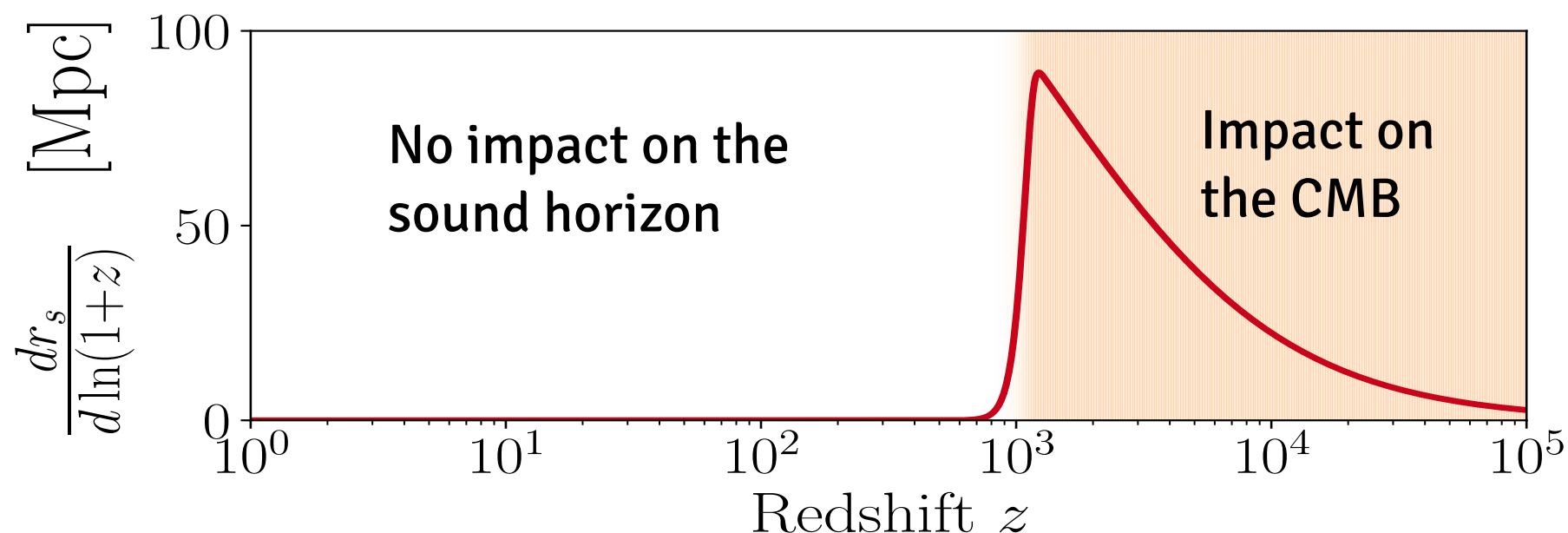


COSMIC CALIBRATOR TENSION



COSMIC CALIBRATOR TENSION

$$r_s = \int_{z_*}^{\infty} \frac{c_s(z) dz}{H(z)}$$

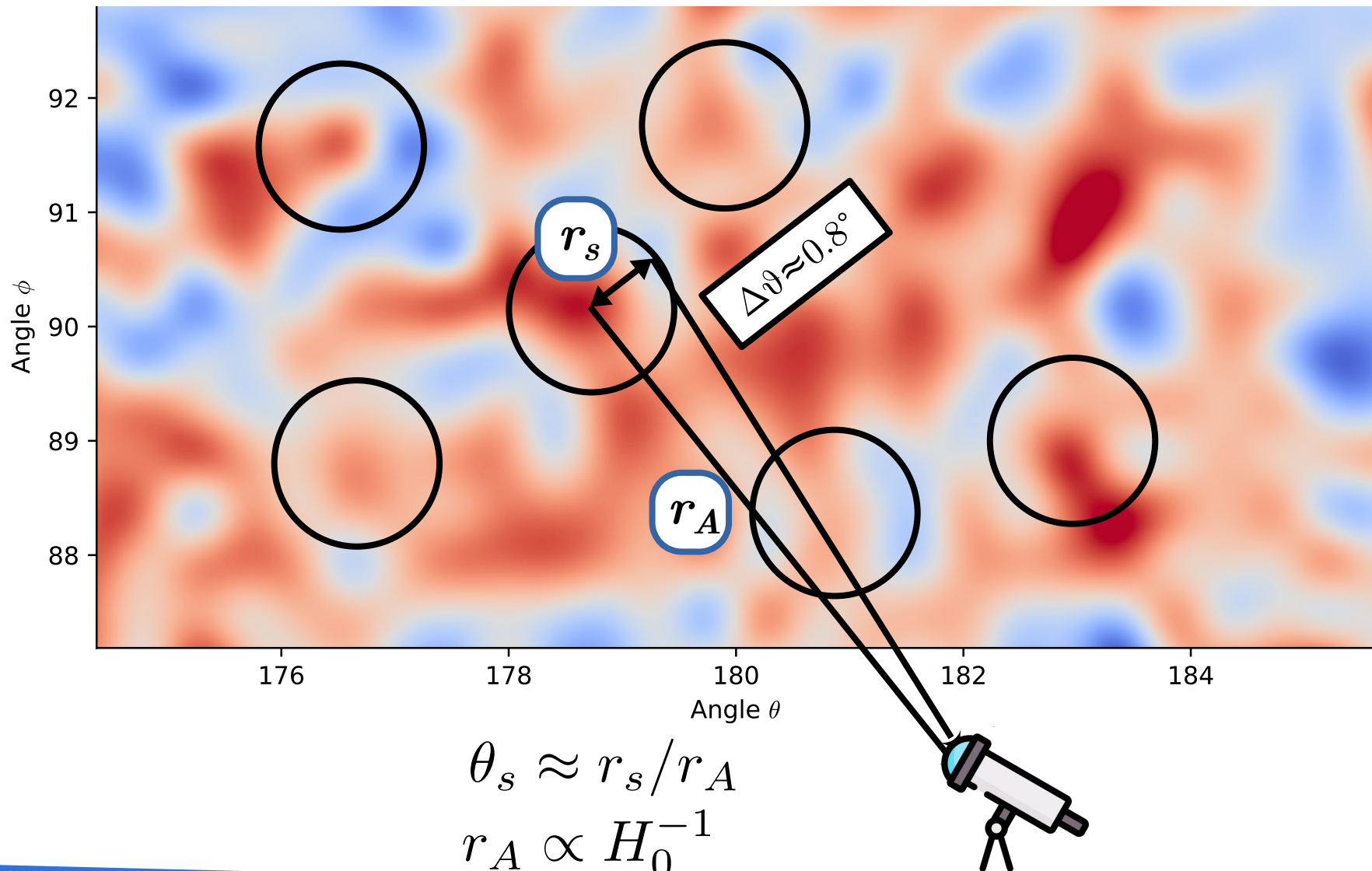


COSMIC CALIBRATOR TENSION

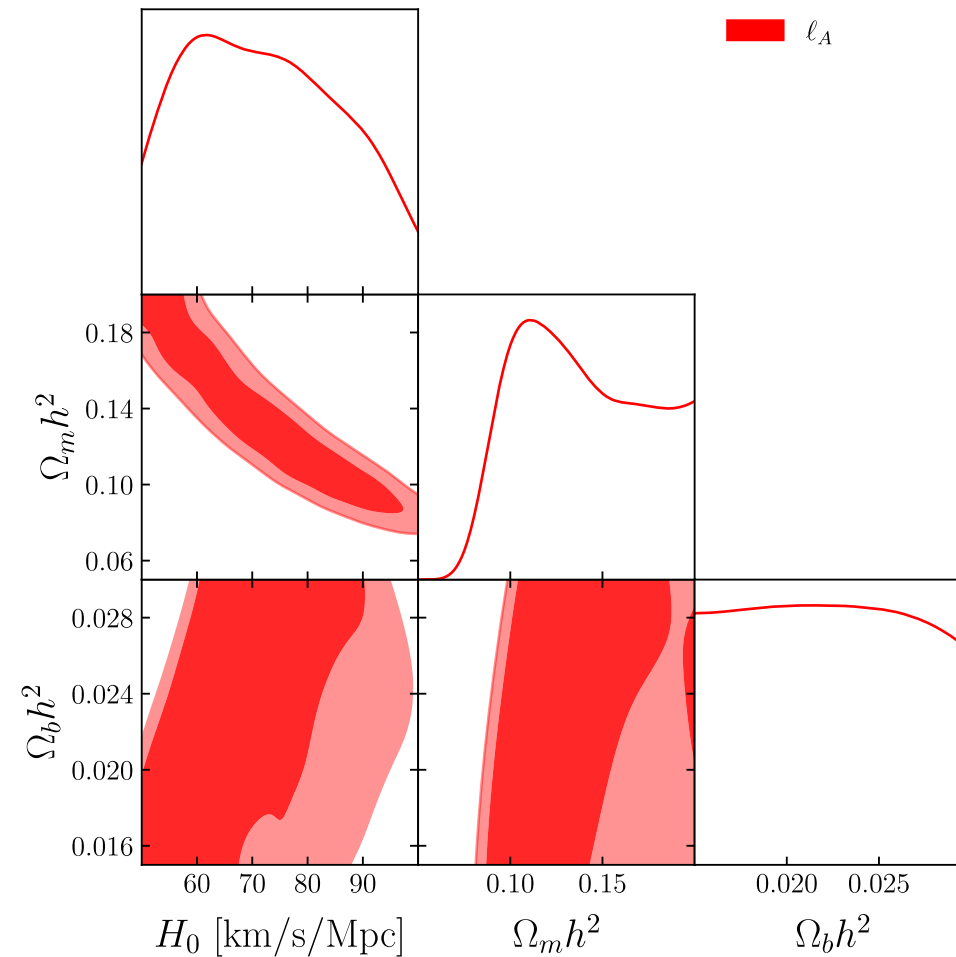
$$r_s = \int_{z_*}^{\infty} \frac{c_s(z) dz}{H(z)}$$

Group M Groups R+E

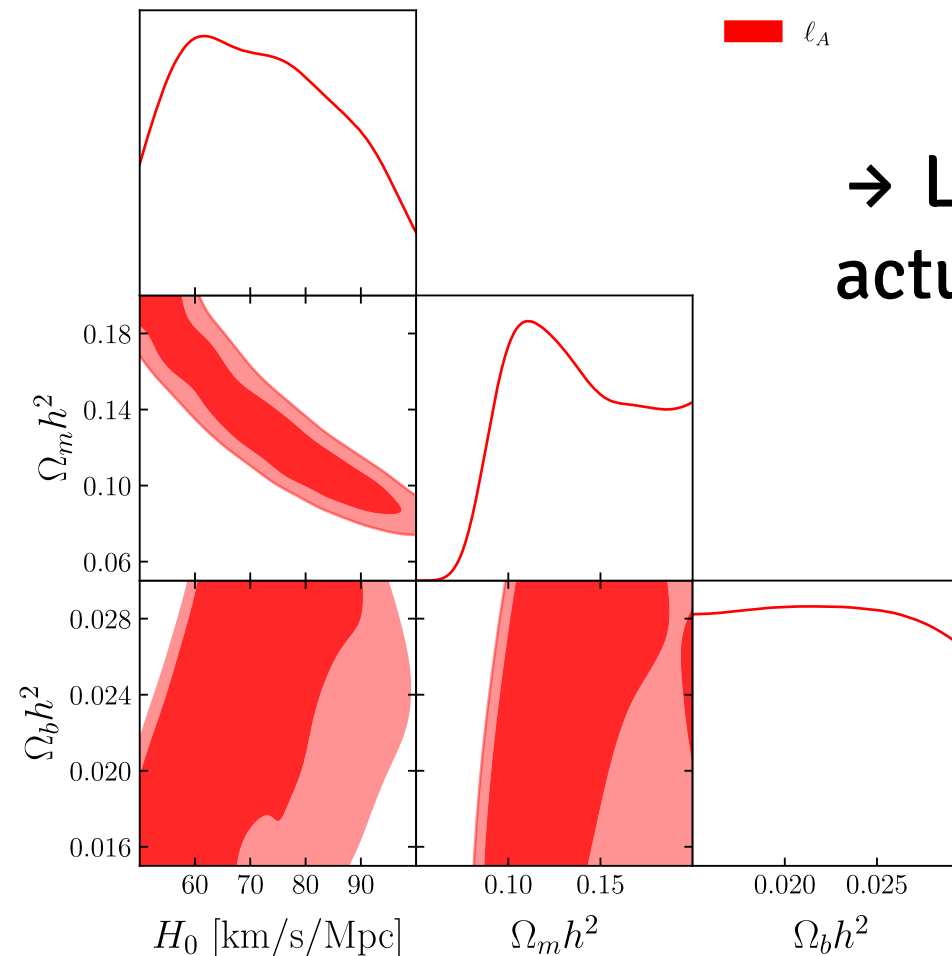
THE CMB ANISOTROPIES



IF YOU ONLY HAD THAT SCALE...

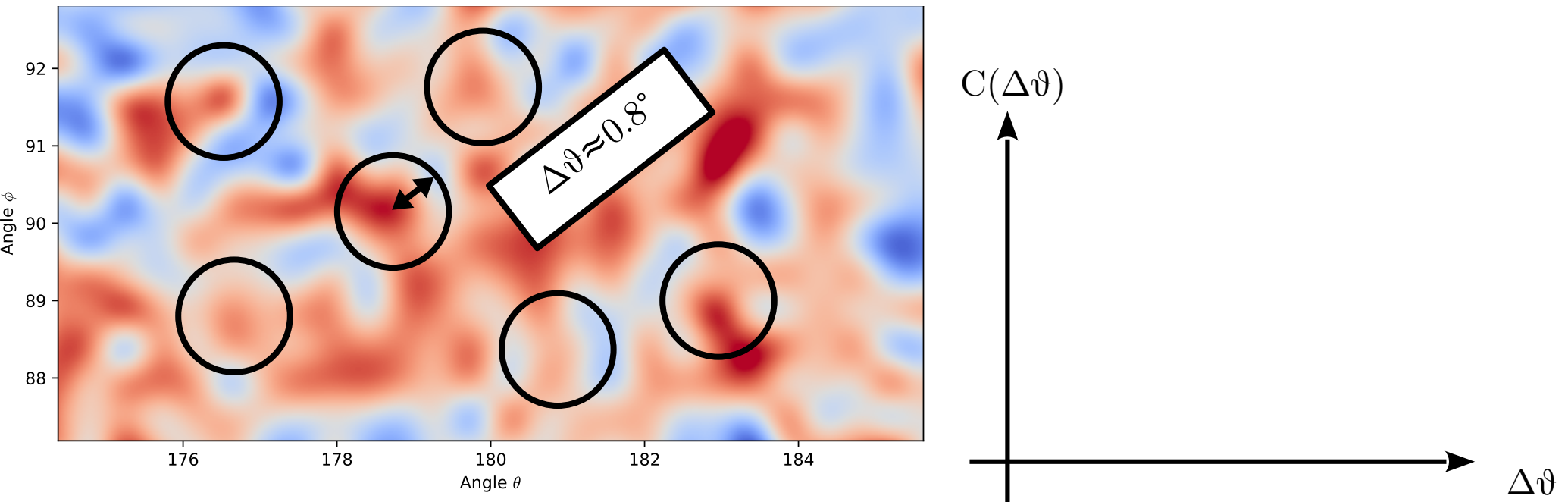


IF YOU ONLY HAD THAT SCALE...

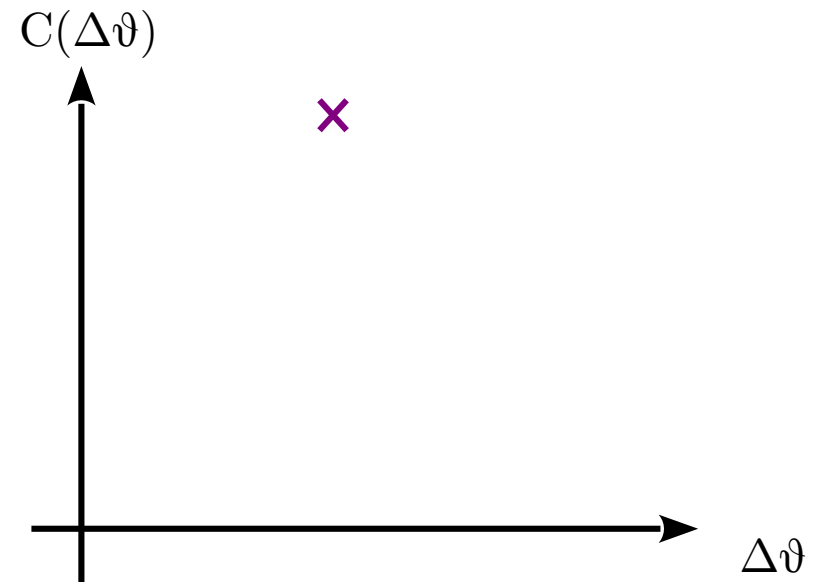
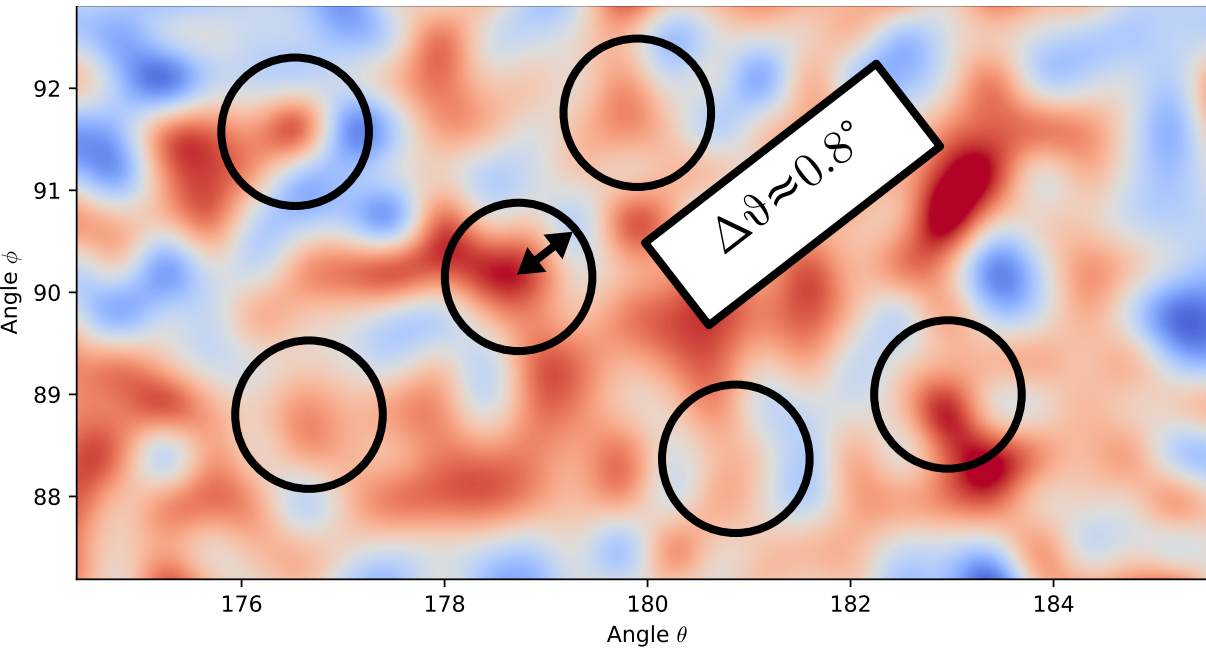


→ Let's see how it's actually done!

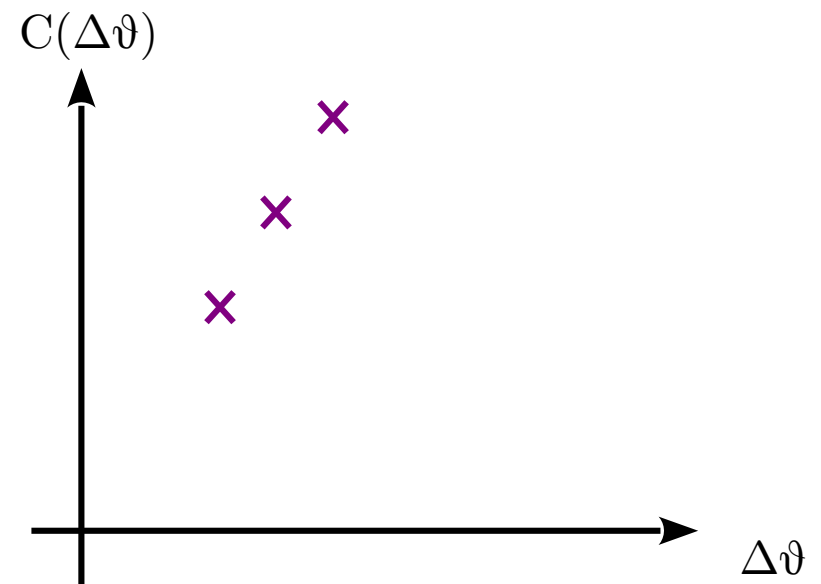
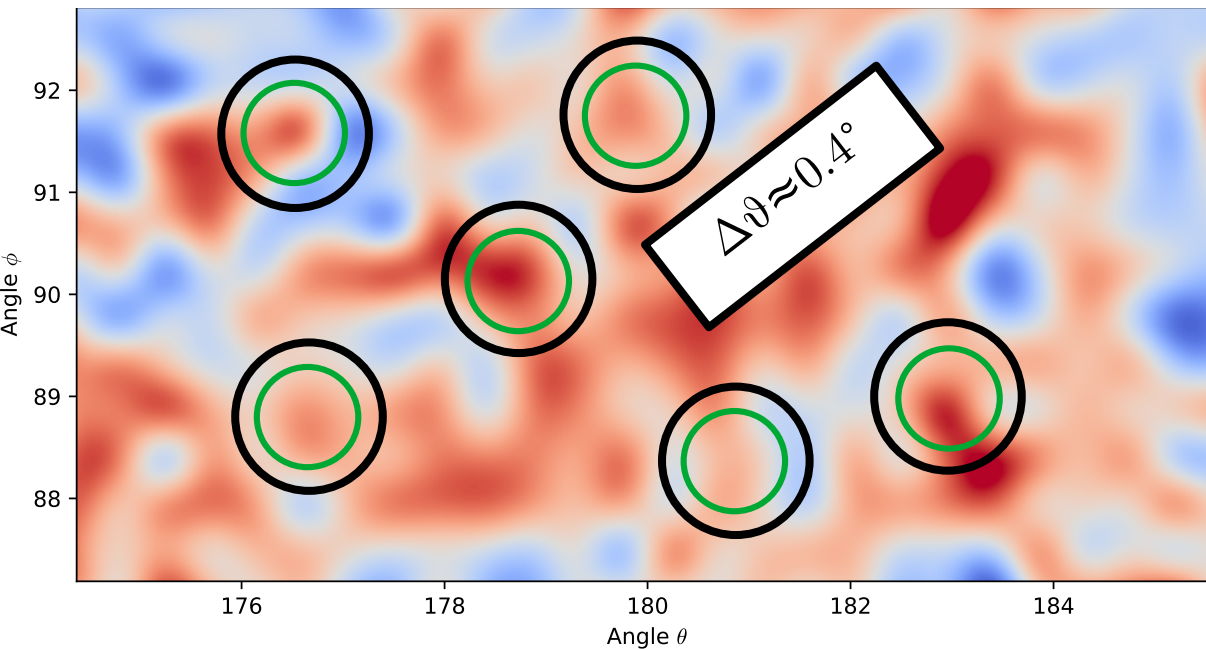
THE CMB ANISOTROPIES



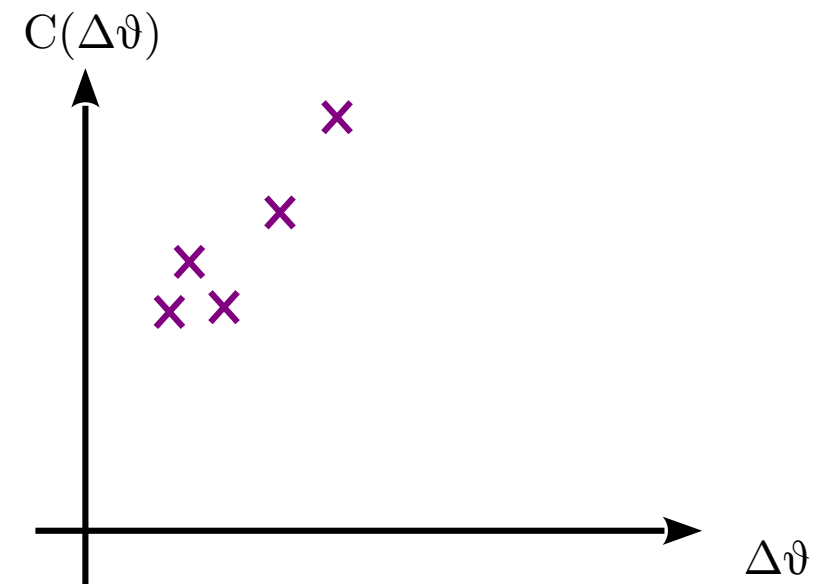
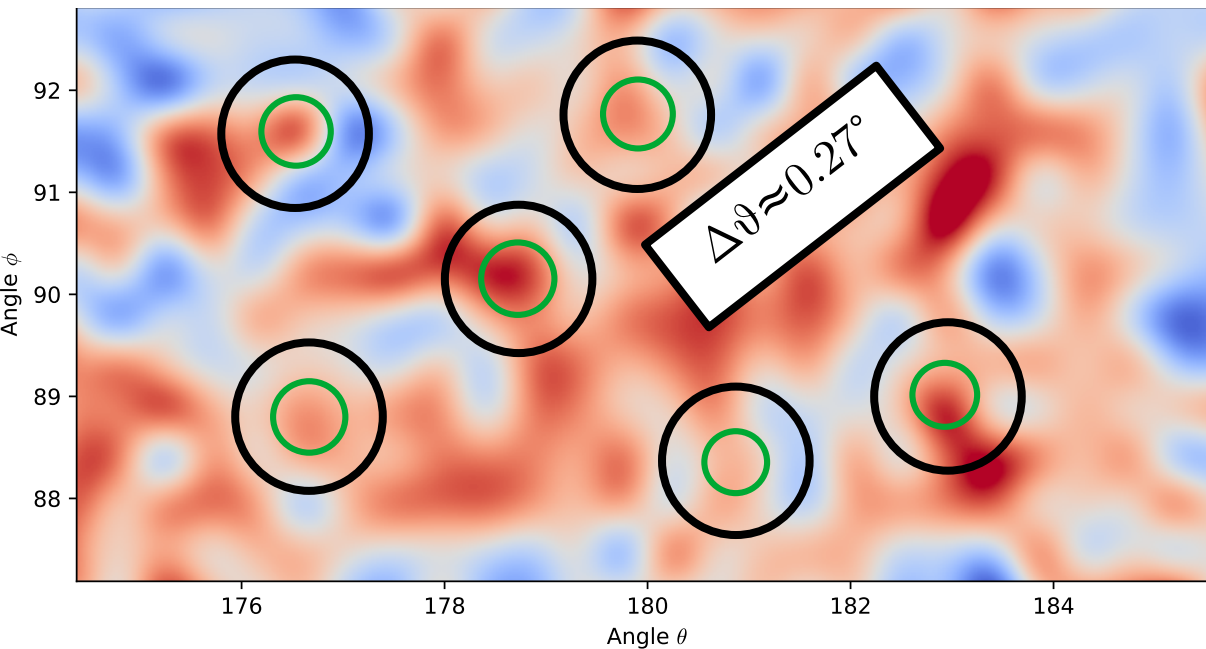
THE CMB ANISOTROPIES



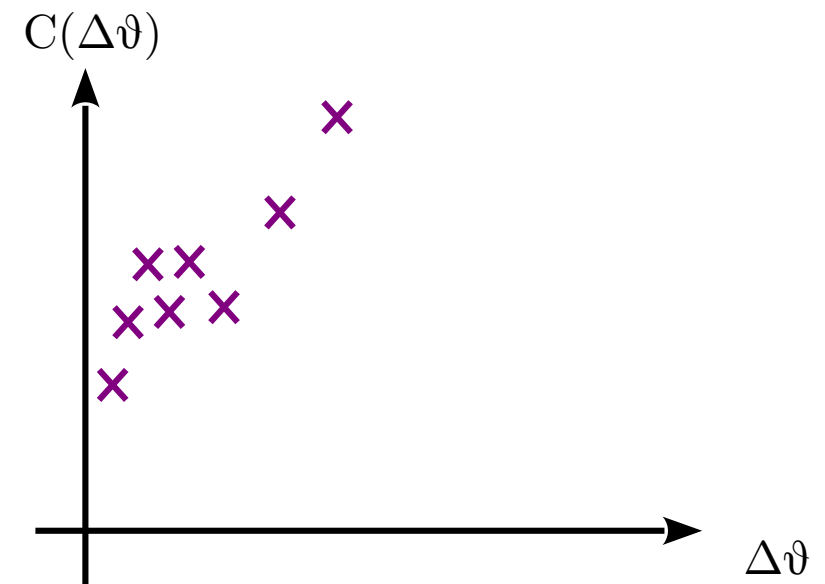
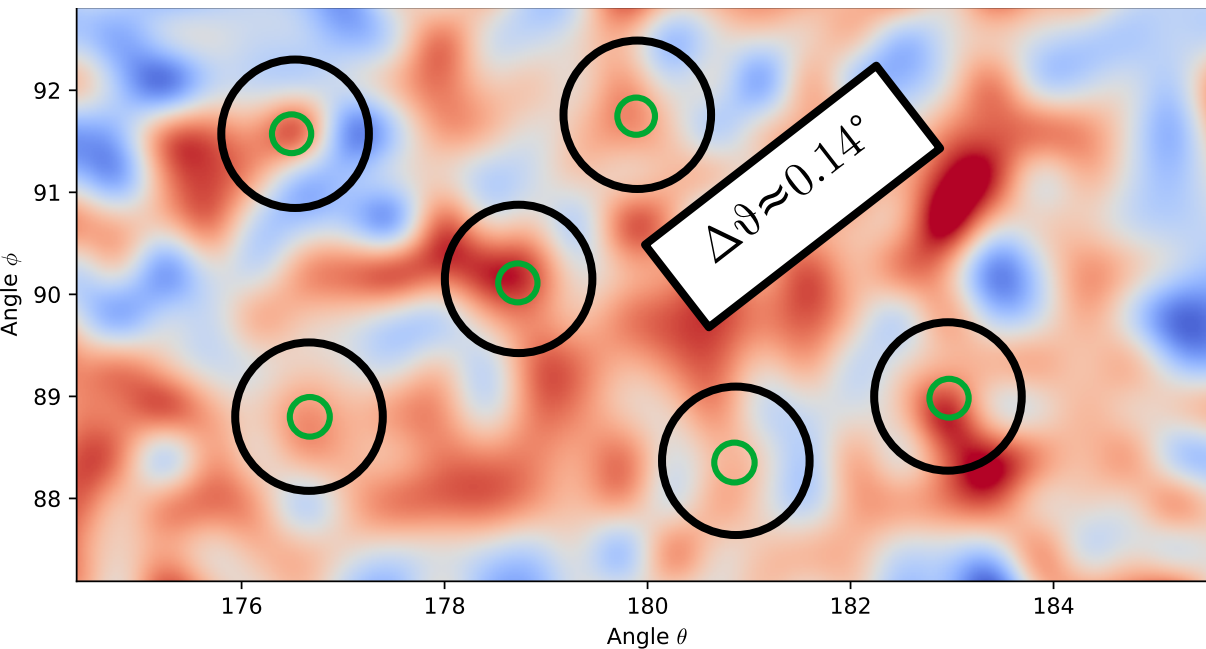
THE CMB ANISOTROPIES



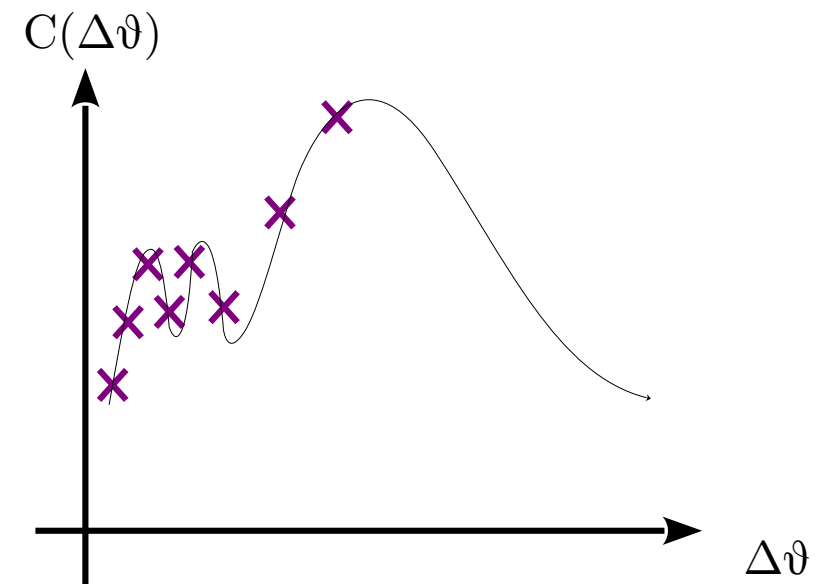
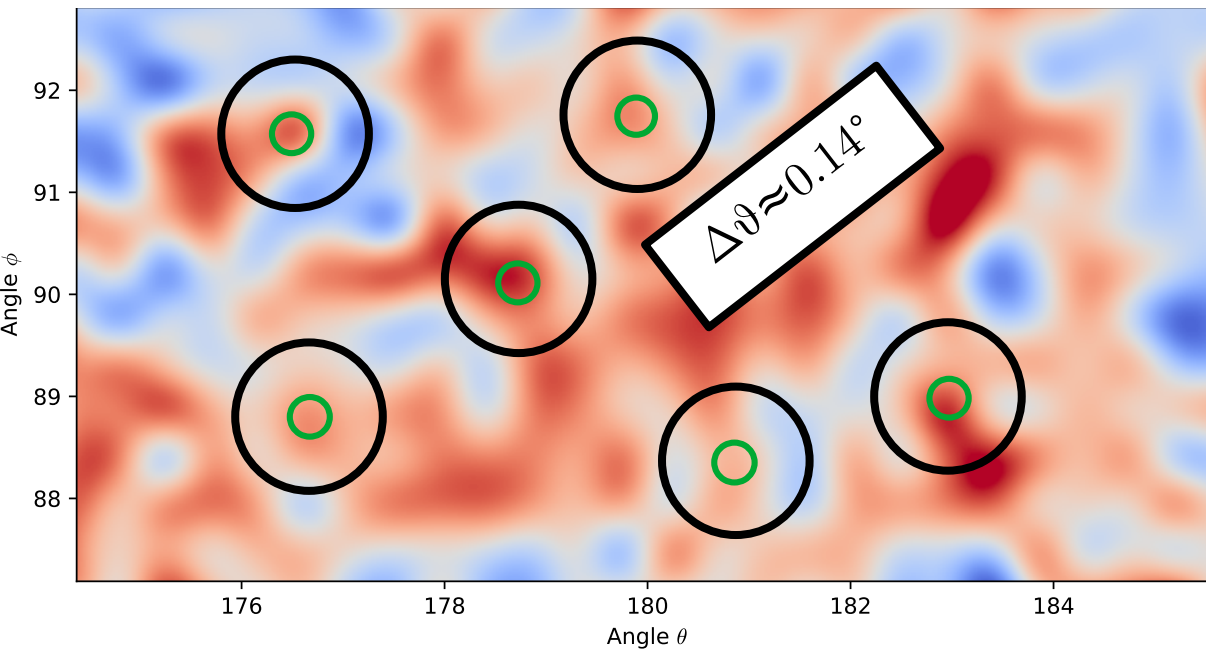
THE CMB ANISOTROPIES



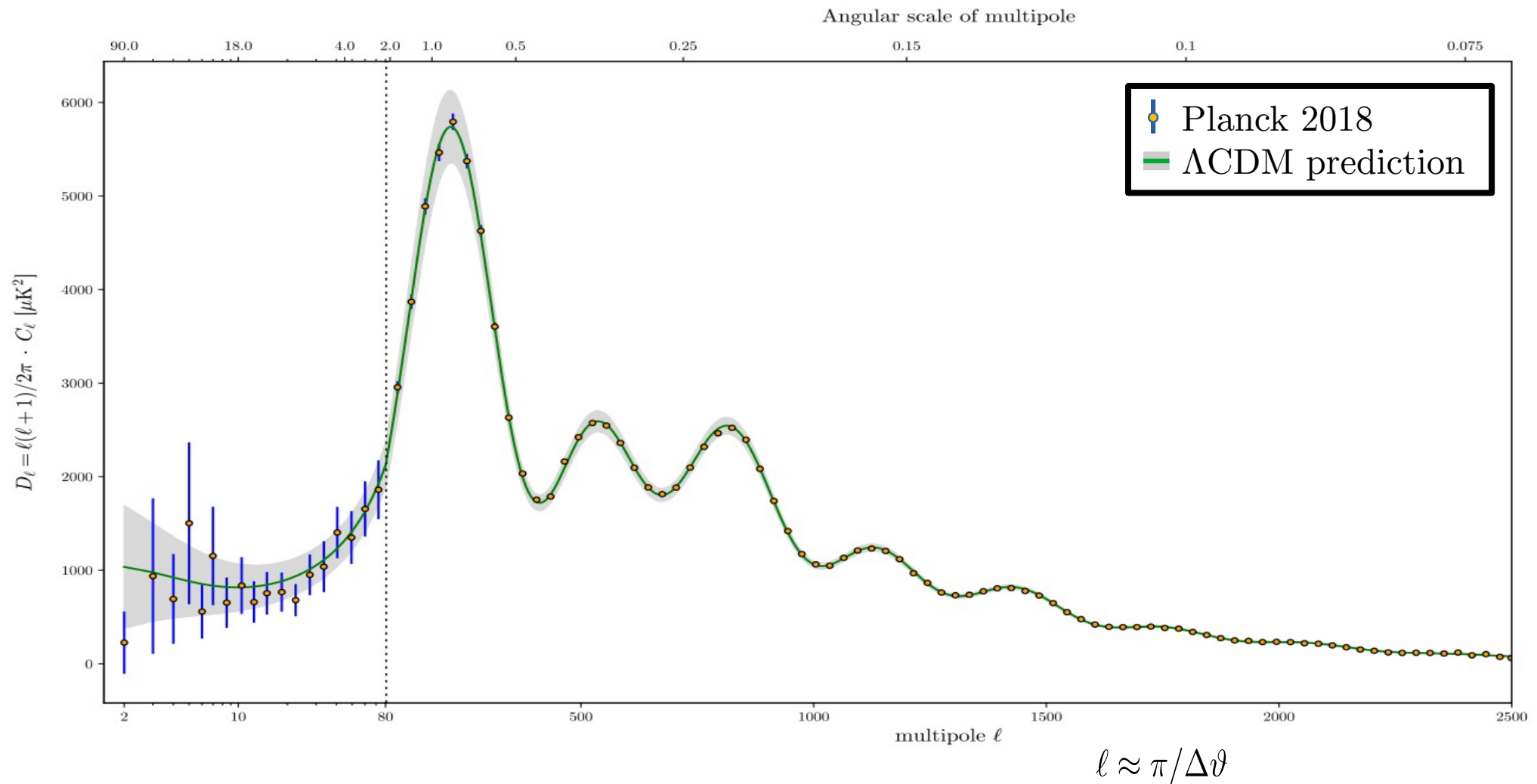
THE CMB ANISOTROPIES



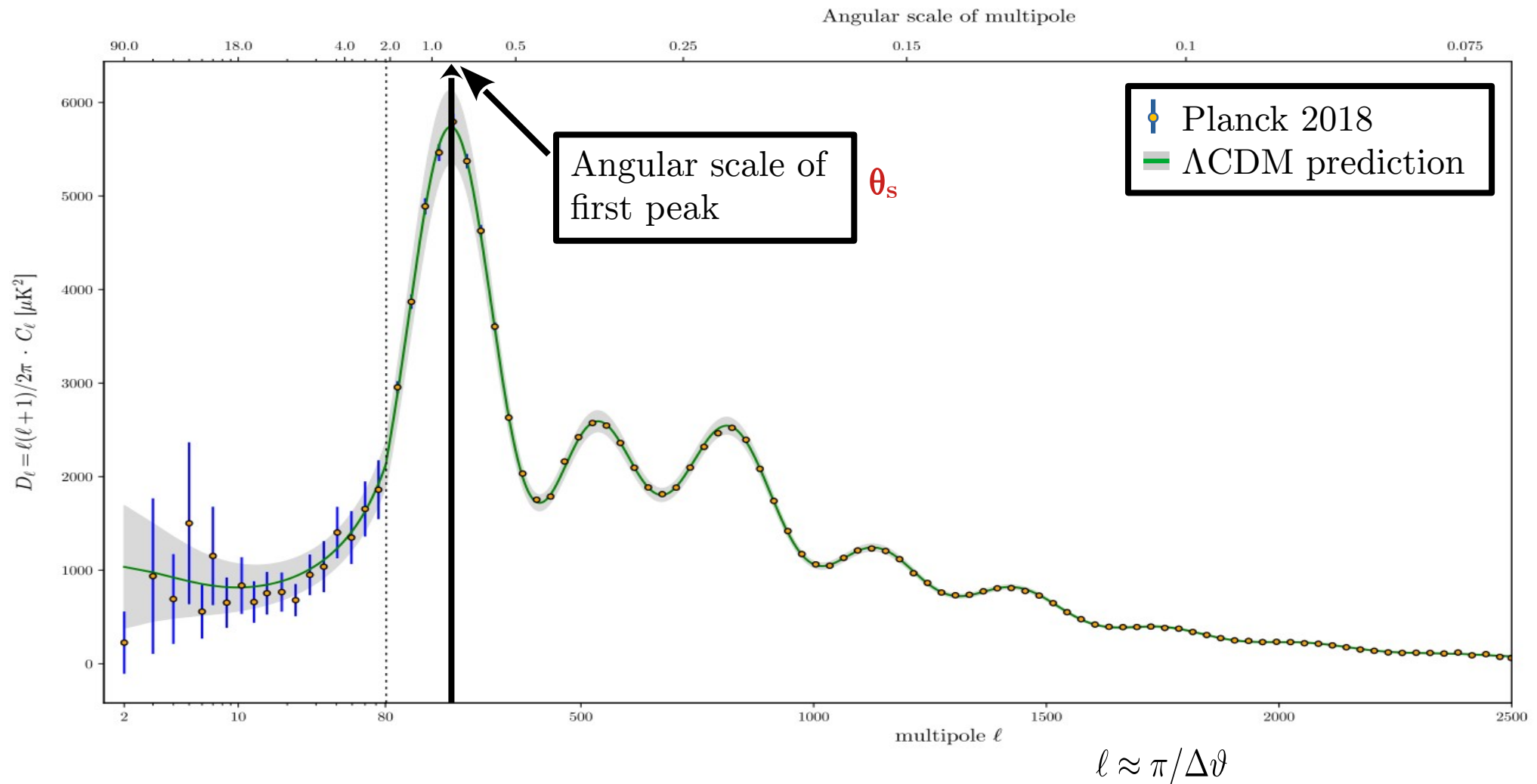
THE CMB ANISOTROPIES



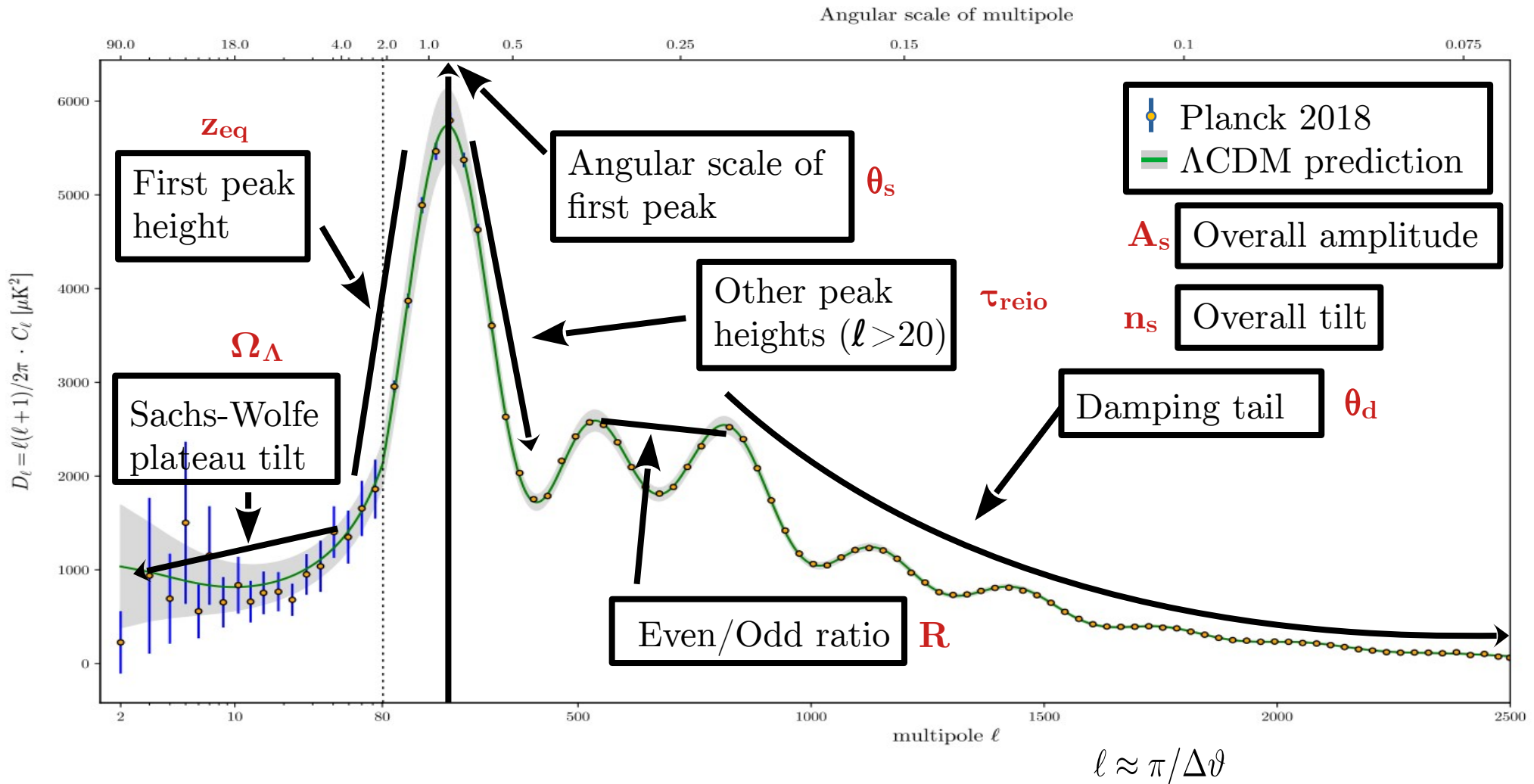
THE CMB



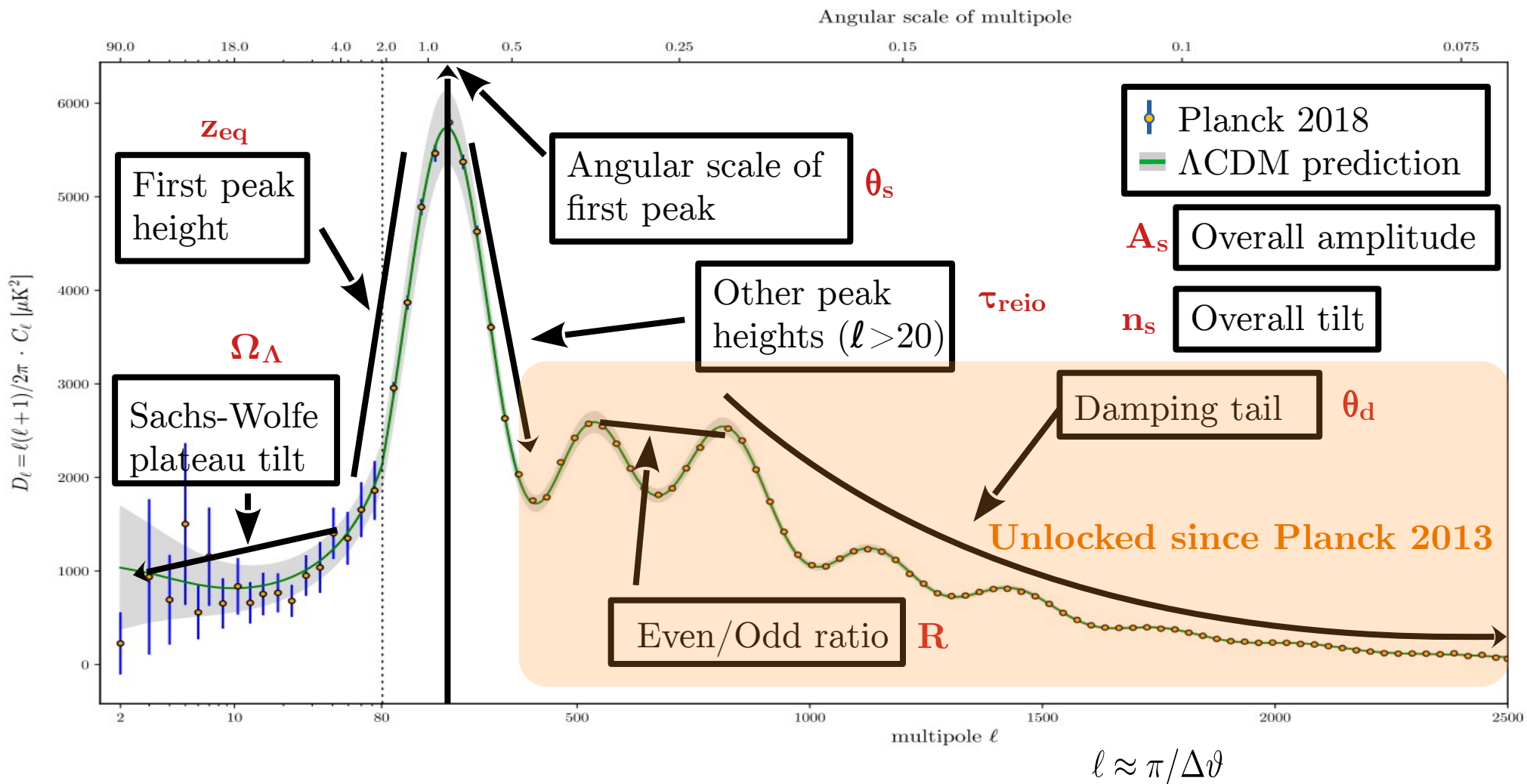
THE CMB



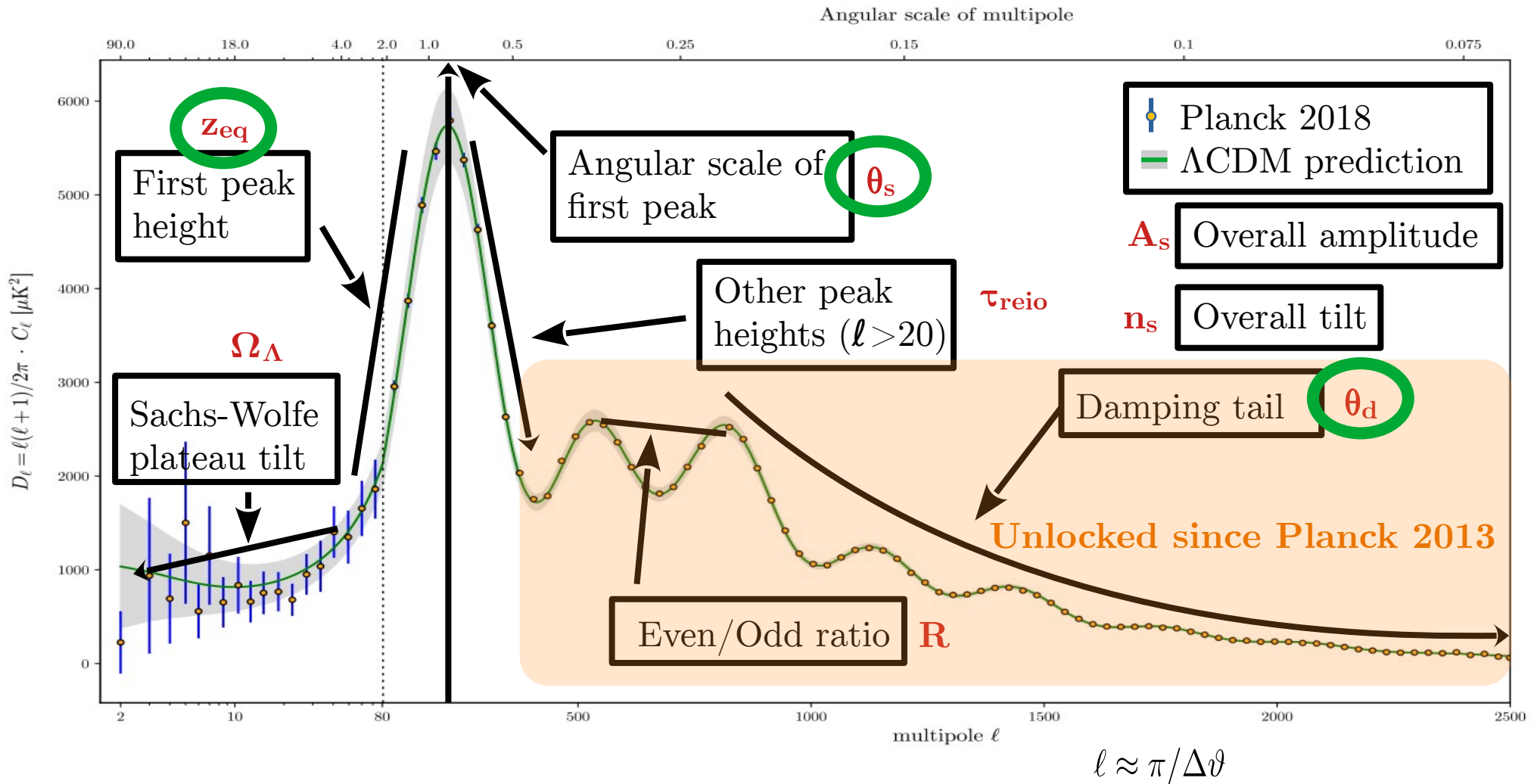
THE CMB



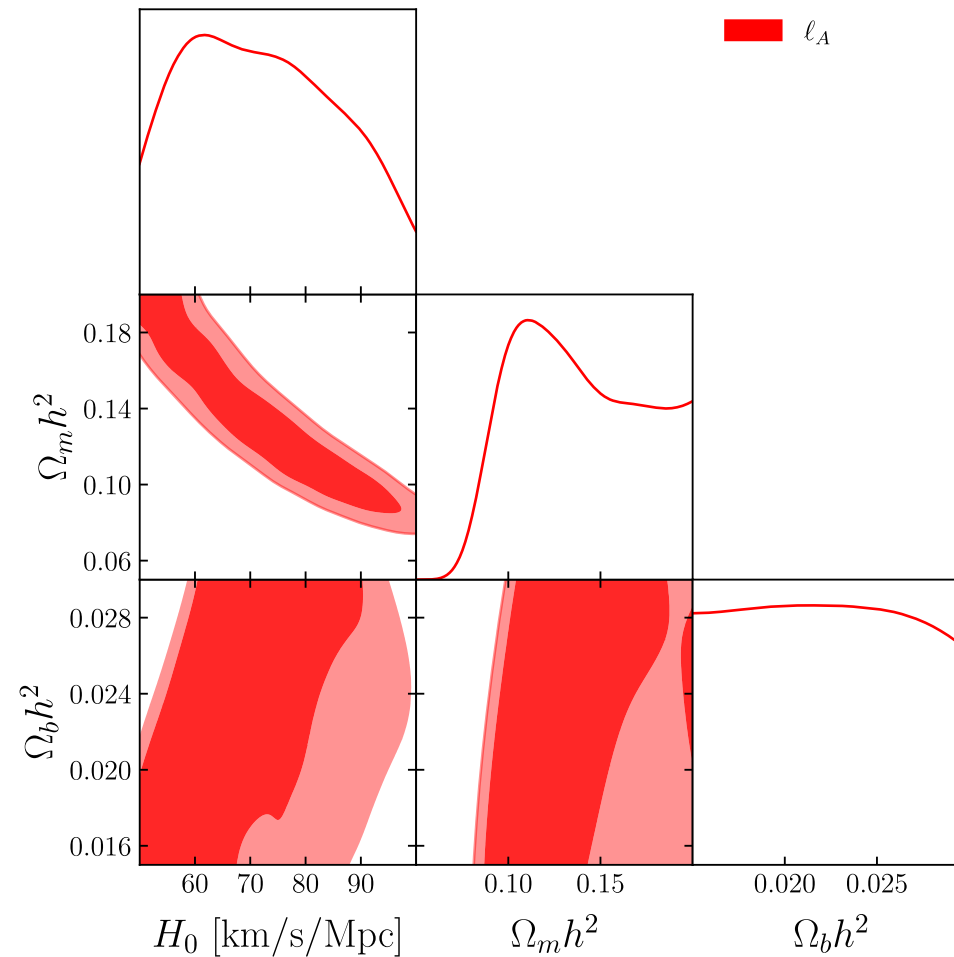
THE CMB



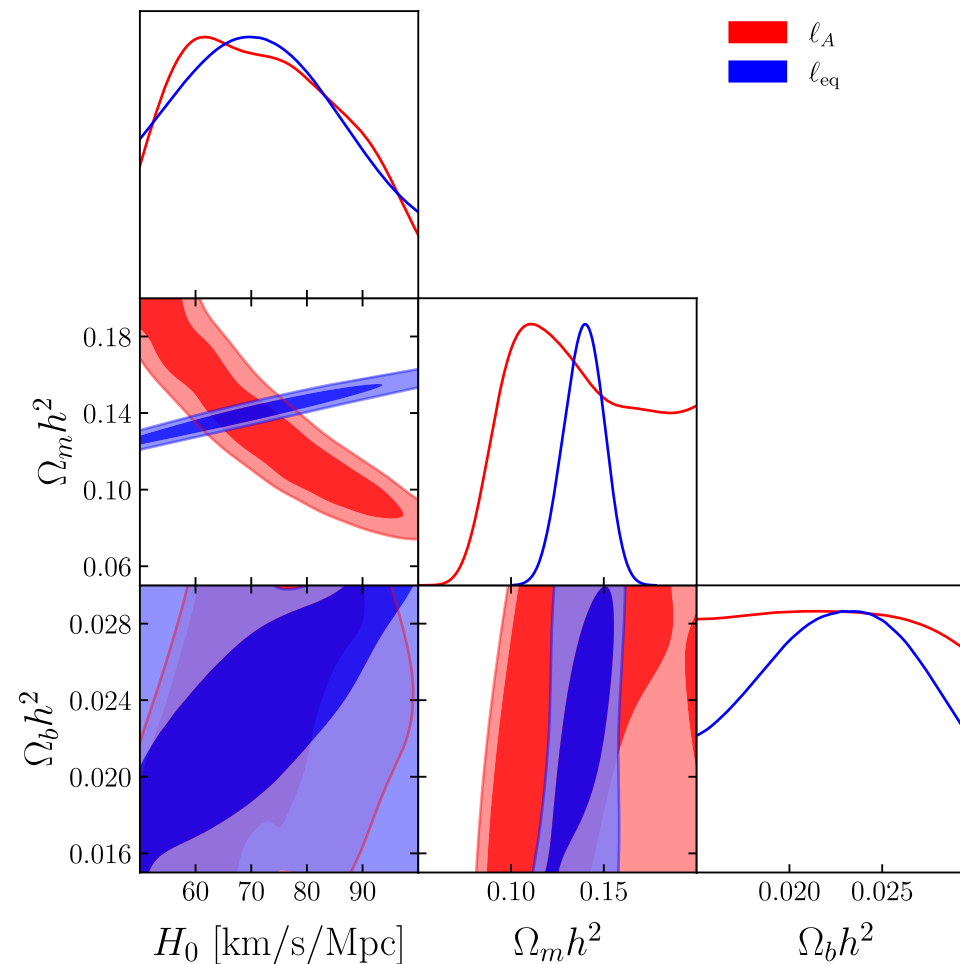
THE CMB



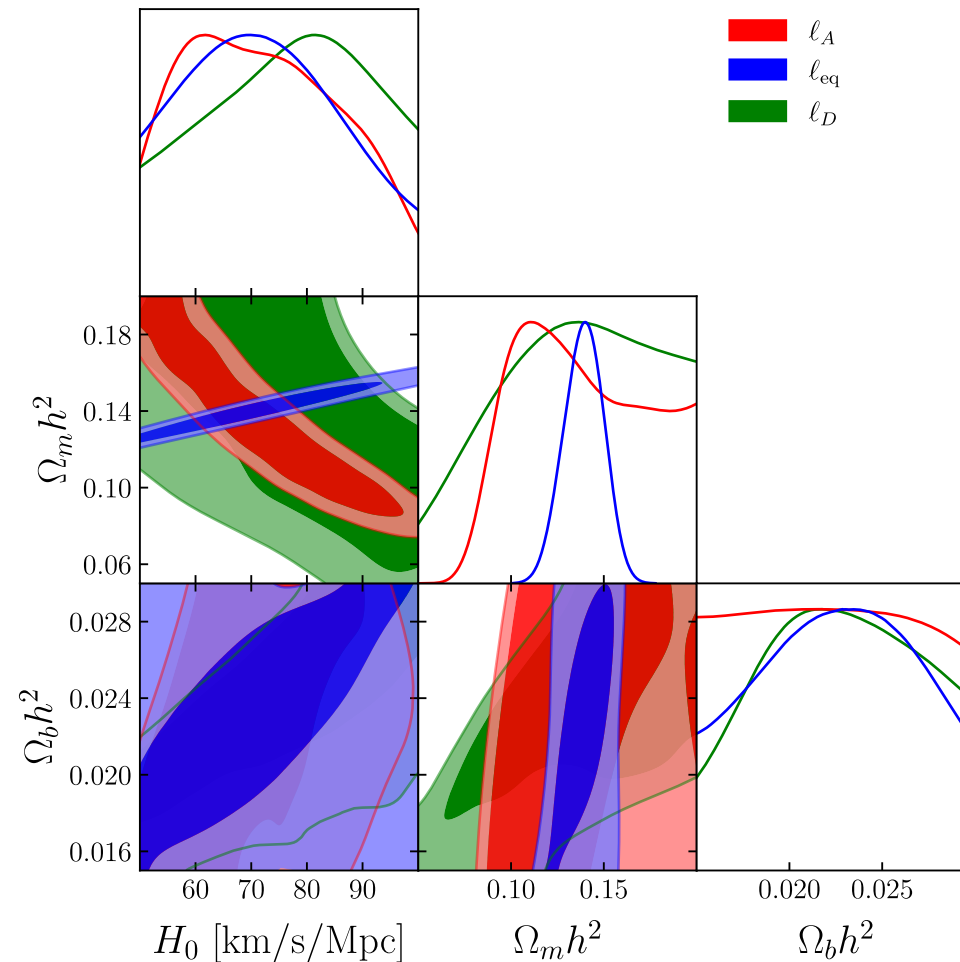
IF YOU ONLY HAD THOSE SCALES...



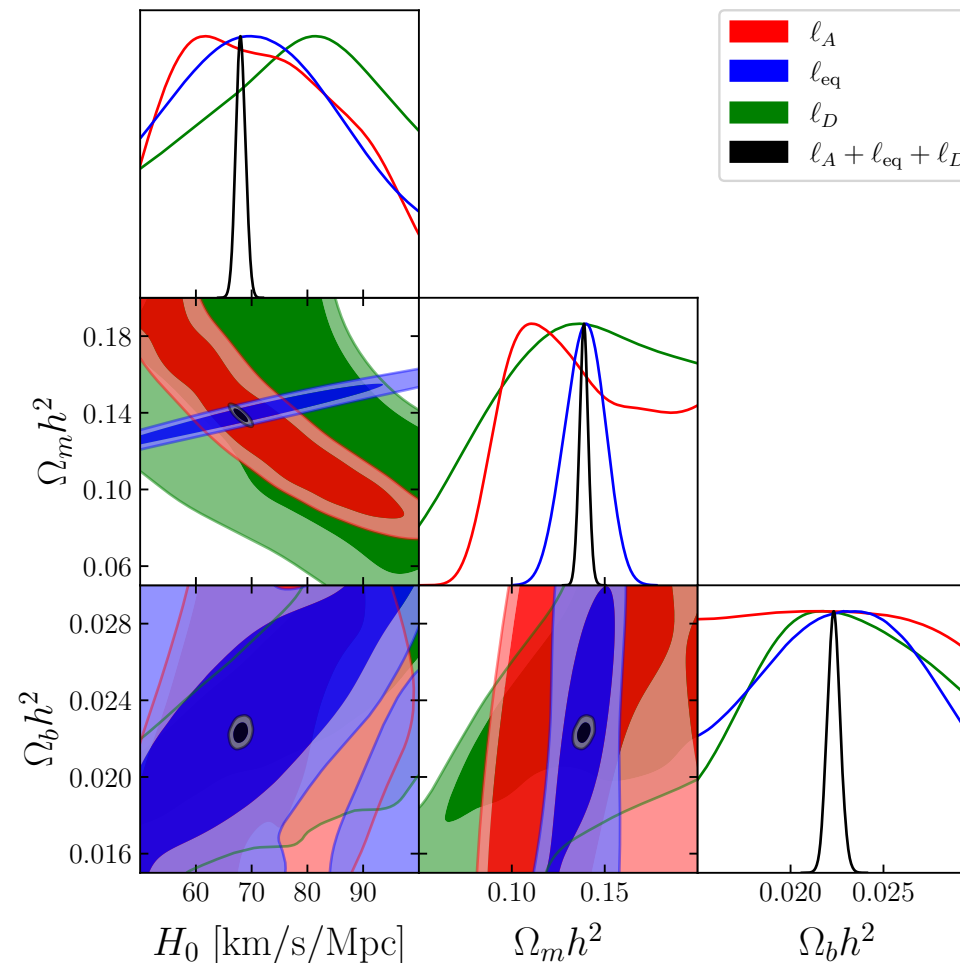
IF YOU ONLY HAD THOSE SCALES...



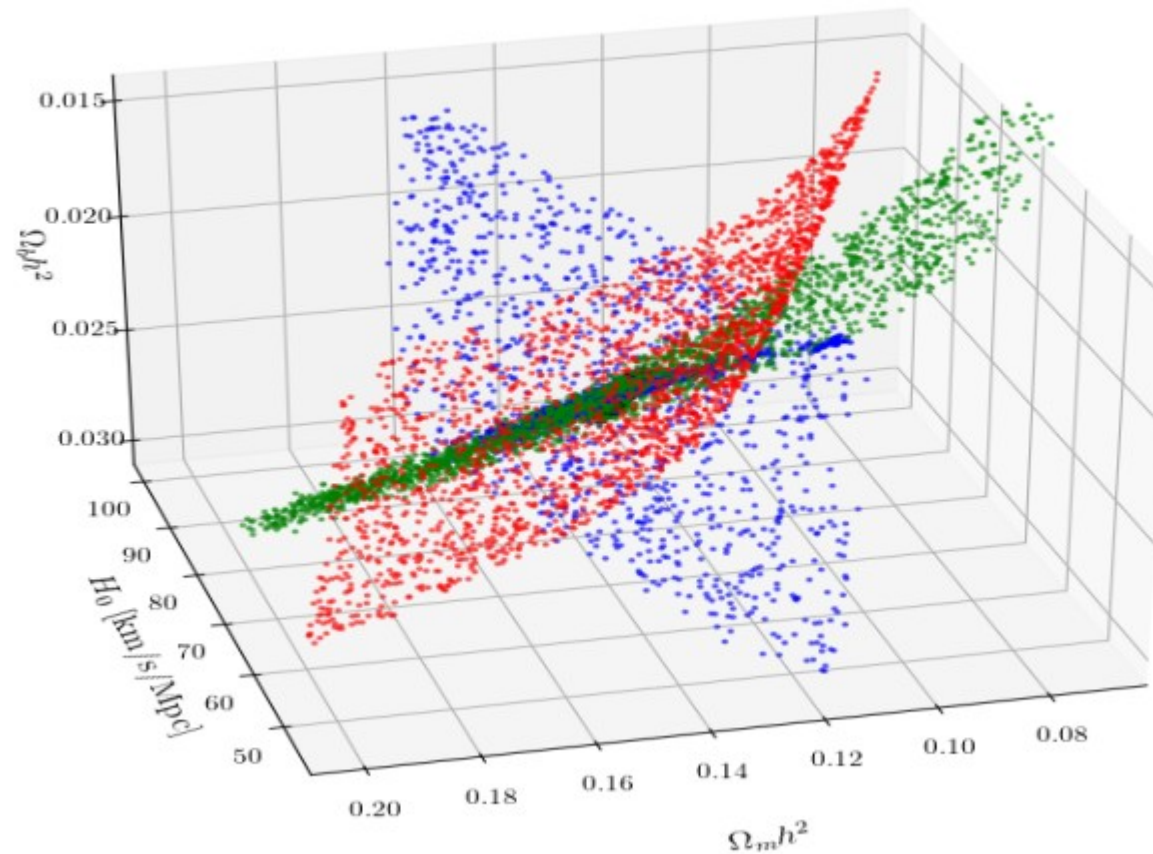
IF YOU ONLY HAD THOSE SCALES...



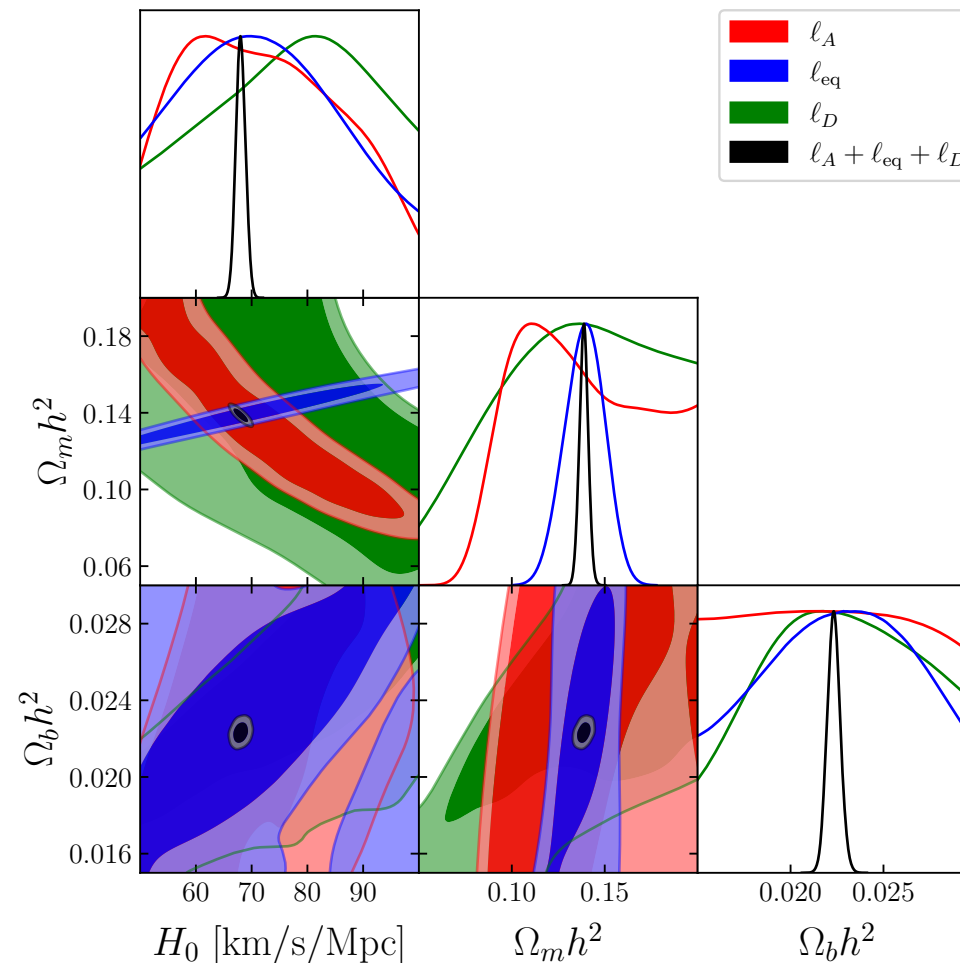
IF YOU ONLY HAD THOSE SCALES...



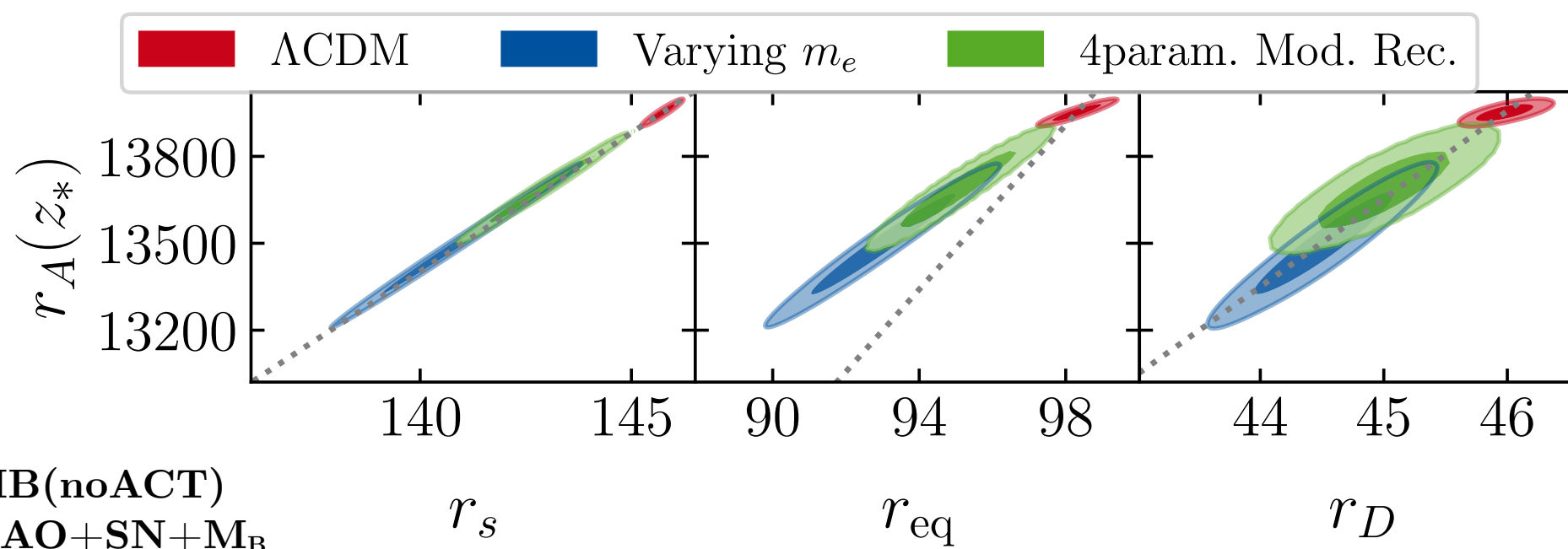
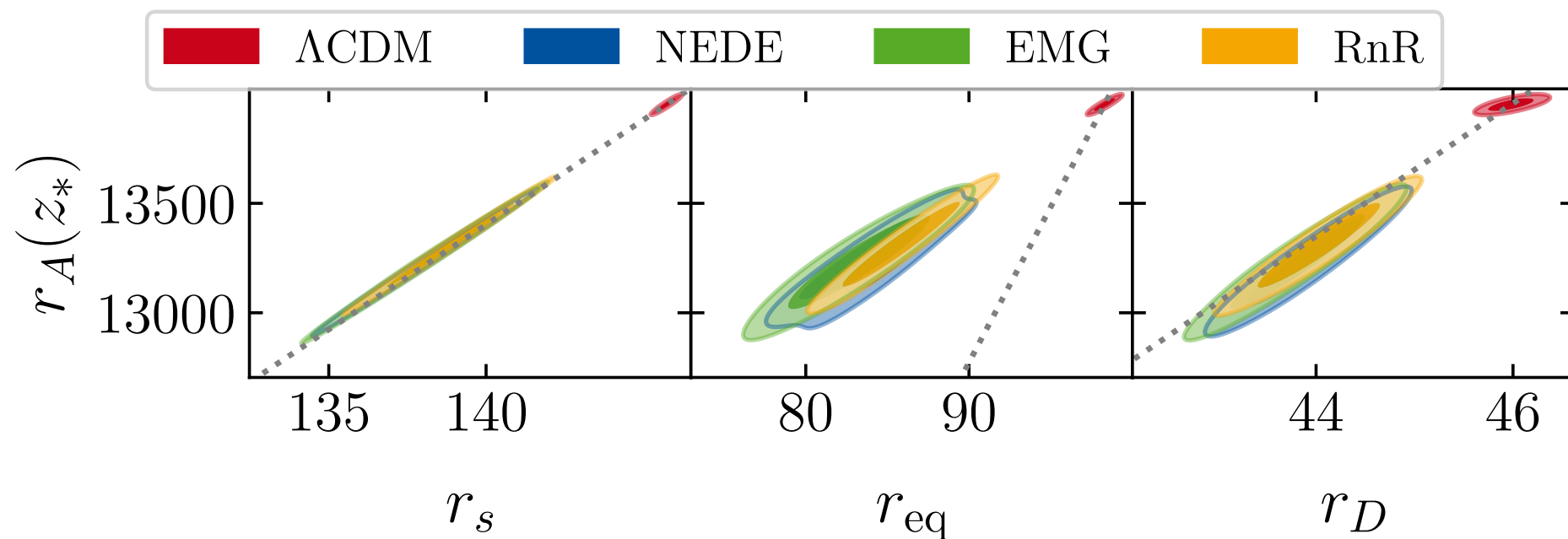
IF YOU ONLY HAD THOSE SCALES...

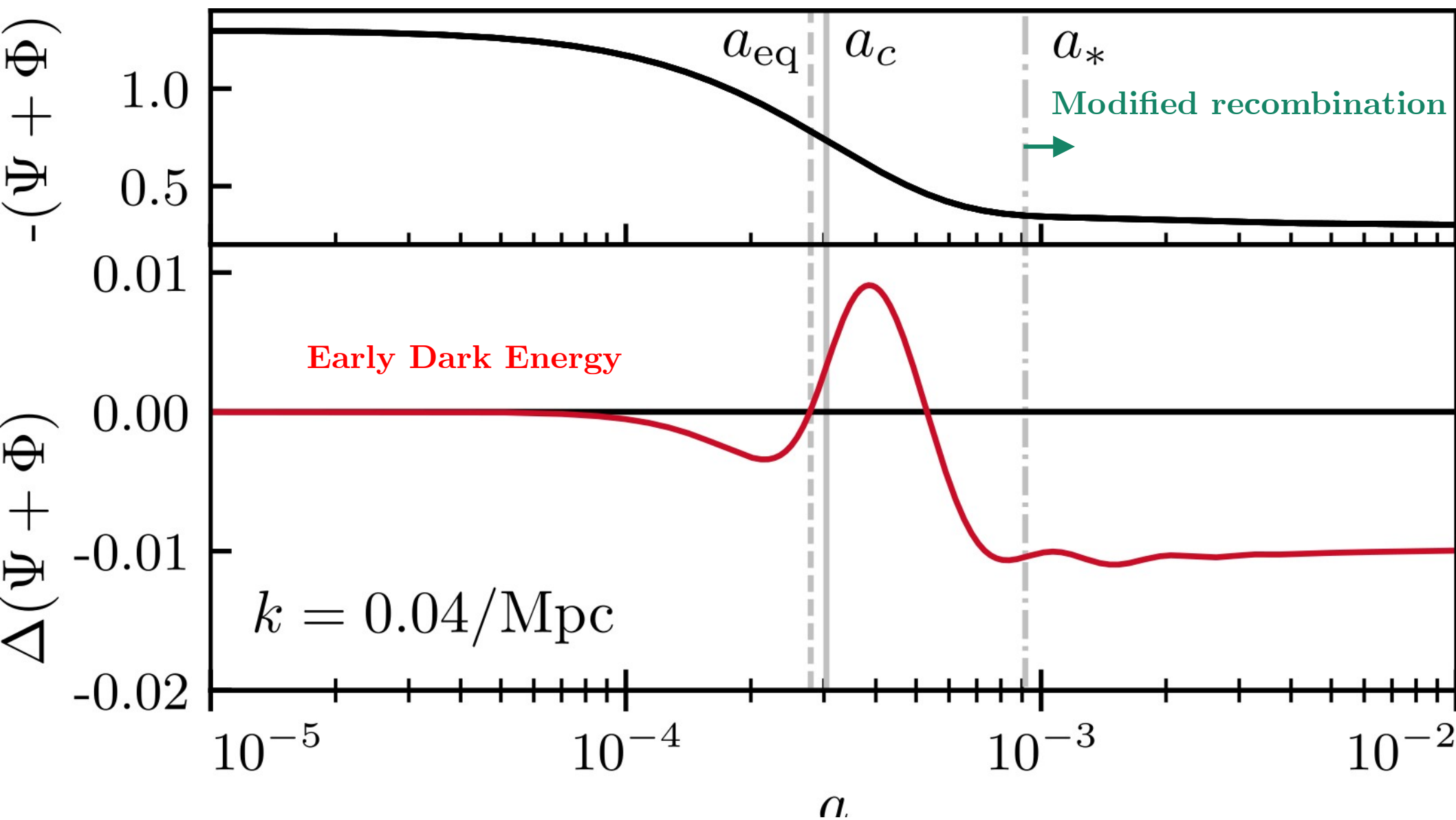


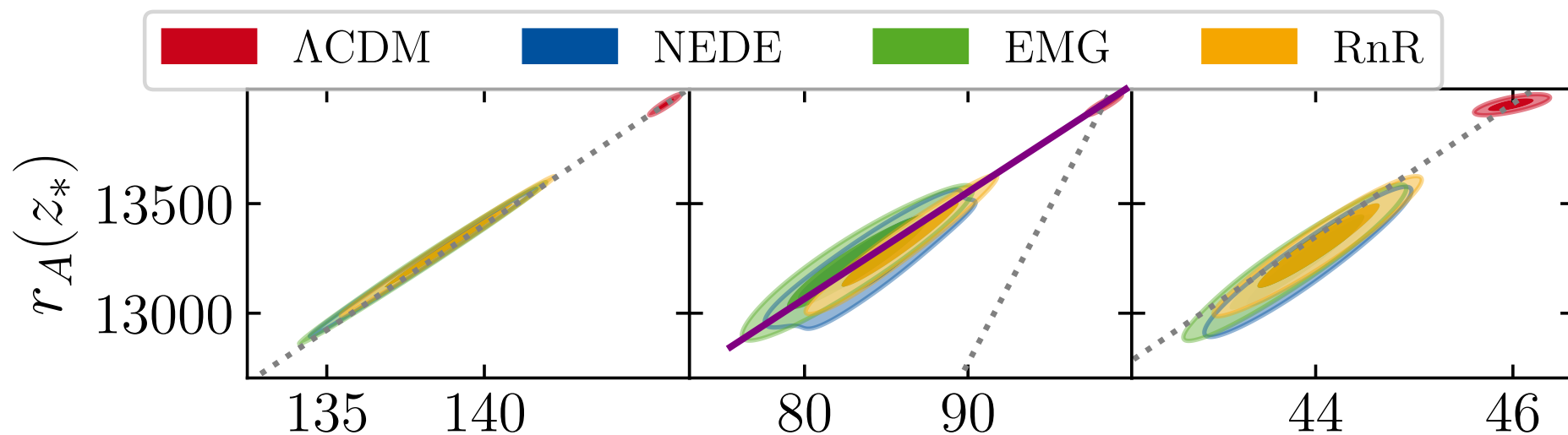
IF YOU ONLY HAD THOSE SCALES...



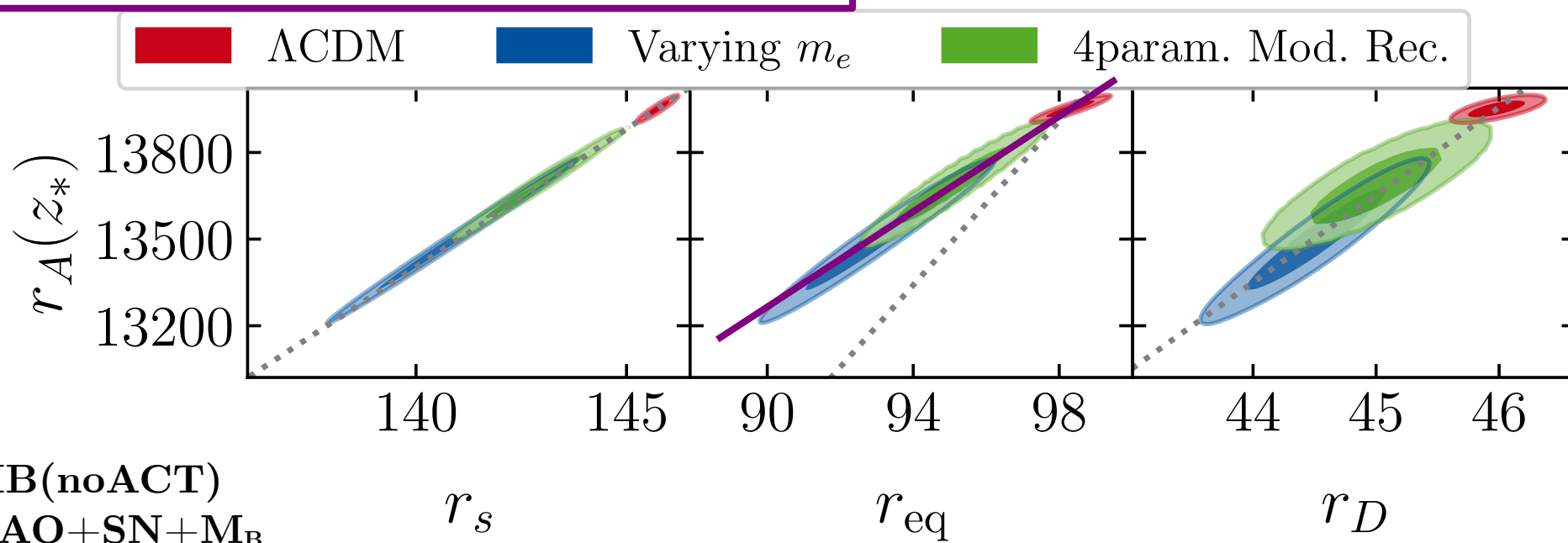








Still works, but with adjusted ℓ_{eq}



CMB(noACT)
+BAO+SN+M_B

PLAN

- I. Discuss picture with ℓ_{eq} fixed
- II. Adjust ℓ_{eq}
- III. Explain peculiar features

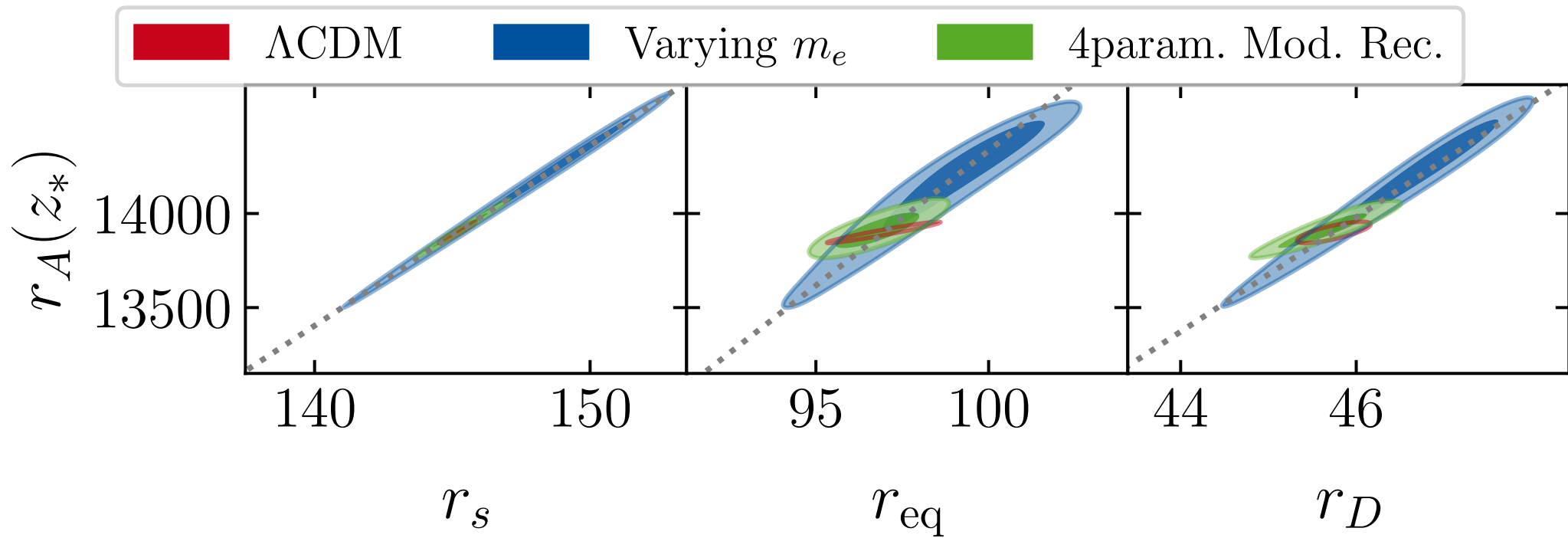
PLAN

Only for recombination models
(otherwise we'll be here all day)

I. Discuss picture with ℓ_{eq} fixed

II. Adjust ℓ_{eq}

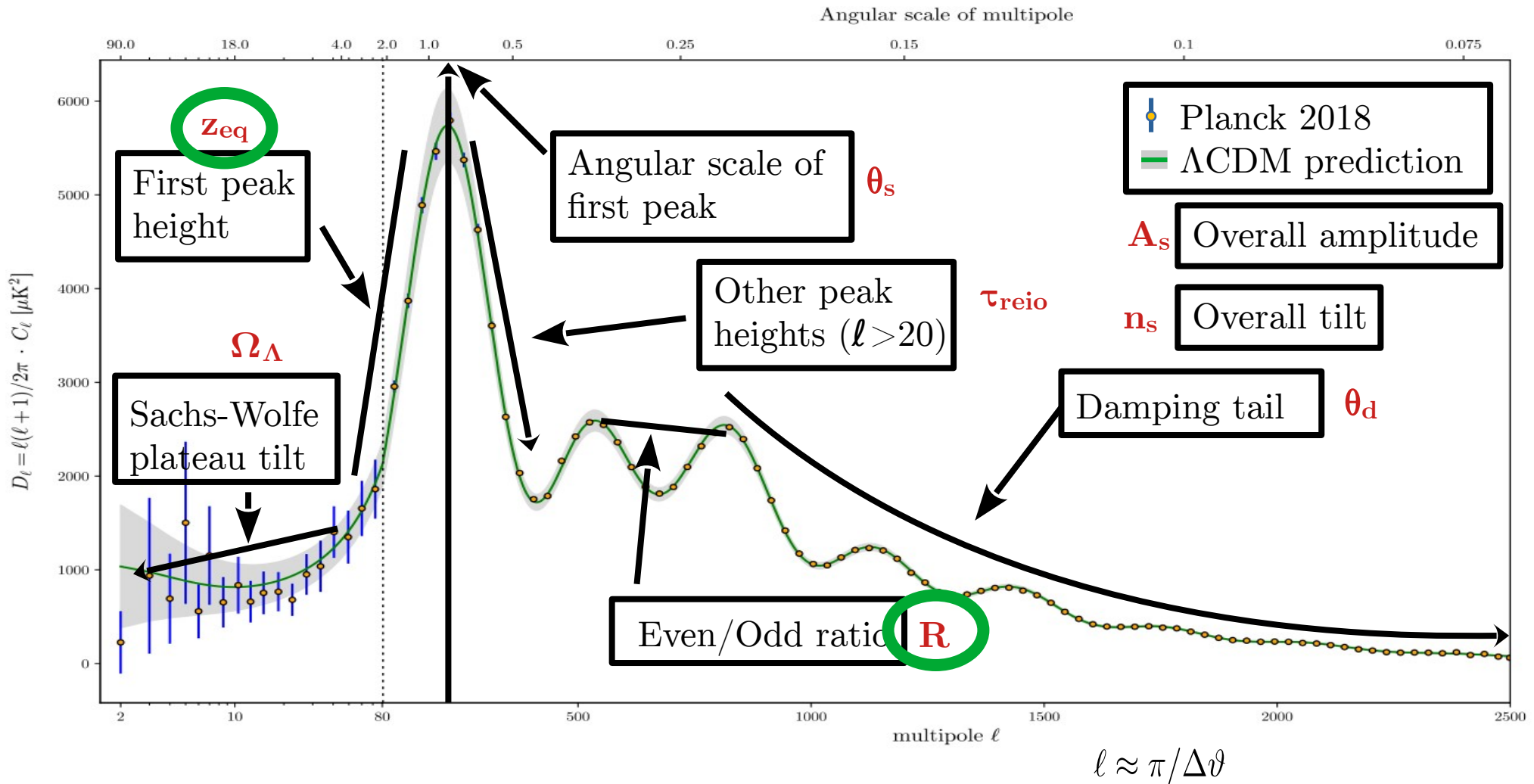
III. Explain peculiar features



Fixed equality is “natural” direction without BAO+SN

Shifting ℓ_{eq} requires “extra effort”

THE CMB



THE LITTLE SOLUTION THAT COULD

At CMB times, we need same **baryon-to-photon**
and **matter-to-radiation** ratios even-to-odd peak
gravitational boost of BAO

THE LITTLE SOLUTION THAT COULD

At CMB times, we need same **baryon-to-photon**
and **matter-to-radiation** ratios even-to-odd peak
gravitational boost of BAO

$$R = \frac{3}{4} \frac{\omega_b}{\omega_\gamma} \cdot a$$

THE LITTLE SOLUTION THAT COULD

At CMB times, we need same **baryon-to-photon**
and **matter-to-radiation** ratios even-to-odd peak
gravitational boost of BAO

$$R = \frac{3}{4} \frac{\omega_b}{\omega_\gamma} \cdot a \qquad R_* = \frac{3}{4} \frac{\omega_b}{\omega_\gamma} \cdot a_* \stackrel{!}{=} \text{constant}$$

THE LITTLE SOLUTION THAT COULD

At CMB times, we need same **baryon-to-photon**
and **matter-to-radiation** ratios even-to-odd peak

gravitational boost of BAO

$$R = \frac{3}{4} \frac{\omega_b}{\omega_\gamma} \cdot a \qquad R_* = \frac{3}{4} \frac{\omega_b}{\omega_\gamma} \cdot a_* \stackrel{!}{=} \text{constant}$$

$$\Rightarrow \omega_b \propto a_*^{-1}$$

THE LITTLE SOLUTION THAT COULD

At CMB times, we need same **baryon-to-photon**
and **matter-to-radiation** ratios even-to-odd peak
gravitational boost of BAO

$$R \rightarrow \omega_b \propto a_*^{-1}$$

THE LITTLE SOLUTION THAT COULD

At CMB times, we need same **baryon-to-photon**
and **matter-to-radiation** ratios even-to-odd peak
gravitational boost of BAO

$$\frac{\rho_m}{\rho_r} \approx \omega_m a / \omega_r$$

$$R \rightarrow \omega_b \propto a_*^{-1}$$

THE LITTLE SOLUTION THAT COULD

At CMB times, we need same **baryon-to-photon**
and **matter-to-radiation** ratios even-to-odd peak
gravitational boost of BAO

$$\frac{\rho_m}{\rho_r} \approx \omega_m a / \omega_r \quad \left. \frac{\rho_m}{\rho_r} \right|_{a=a_*} \approx \omega_m a_* / \omega_r \stackrel{!}{=} \text{constant}$$

$$R \rightarrow \omega_b \propto a_*^{-1}$$

THE LITTLE SOLUTION THAT COULD

At CMB times, we need same **baryon-to-photon**
and **matter-to-radiation** ratios even-to-odd peak
gravitational boost of BAO

$$\frac{\rho_m}{\rho_r} \approx \omega_m a / \omega_r \quad \left. \frac{\rho_m}{\rho_r} \right|_{a=a_*} \approx \omega_m a_* / \omega_r \stackrel{!}{=} \text{constant}$$

$$\Rightarrow \omega_m \propto a_*^{-1}$$

$$R \rightarrow \omega_b \propto a_*^{-1}$$

THE LITTLE SOLUTION THAT COULD

$$R \rightarrow \omega_b \propto a_*^{-1}$$

$$\rho_m / \rho_r \rightarrow \omega_m \propto a_*^{-1}$$

THE LITTLE SOLUTION THAT COULD

What about r_s ?

$$R \rightarrow \omega_b \propto a_*^{-1}$$

$$\rho_m / \rho_r \rightarrow \omega_m \propto a_*^{-1}$$

THE LITTLE SOLUTION THAT COULD

What about r_s ?

$$r_s = \int_0^{\eta_*} c_s d\eta$$

$$R \rightarrow \omega_b \propto a_*^{-1}$$

$$\rho_m / \rho_r \rightarrow \omega_m \propto a_*^{-1}$$

THE LITTLE SOLUTION THAT COULD

What about r_s ?

$$r_s = \int_0^{\eta_*} c_s d\eta = \int_{z_*}^{\infty} \frac{c_s dz}{H(z)}$$

$$R \rightarrow \omega_b \propto a_*^{-1}$$

$$\rho_m / \rho_r \rightarrow \omega_m \propto a_*^{-1}$$

THE LITTLE SOLUTION THAT COULD

What about r_s ?

$$r_s = \int_0^{\eta_*} c_s d\eta = \int_{z_*}^{\infty} \frac{c_s dz}{H(z)} \propto \int_{z_*}^{\infty} \frac{1}{\sqrt{3(1+R)}} \frac{1}{\sqrt{(\rho_m/\rho_r + 1) \cdot \rho_r}} dz$$

$$R \rightarrow \omega_b \propto a_*^{-1}$$

$$\rho_m/\rho_r \rightarrow \omega_m \propto a_*^{-1}$$

THE LITTLE SOLUTION THAT COULD

What about r_s ?

$$r_s = \int_0^{\eta_*} c_s d\eta = \int_{z_*}^{\infty} \frac{c_s dz}{H(z)} \propto \int_{z_*}^{\infty} \frac{1}{\sqrt{3(1+R)}} \frac{1}{\sqrt{(\rho_m/\rho_r + 1) \cdot \rho_r}} dz$$

$$R \rightarrow \omega_b \propto a_*^{-1}$$

$$\rho_m/\rho_r \rightarrow \omega_m \propto a_*^{-1}$$

THE LITTLE SOLUTION THAT COULD

What about r_s ?

$$r_s = \int_0^{\eta_*} c_s d\eta = \int_{z_*}^{\infty} \frac{c_s dz}{H(z)} \propto \int_{z_*}^{\infty} \frac{1}{\sqrt{3(1+R_s)}} \frac{1}{\sqrt{(\rho_m/\rho_r + 1) \cdot \rho_r}} dz$$

$$r_s \propto \int_{z_*}^{\infty} \frac{1}{\sqrt{\rho_r}} dz$$

$$R \rightarrow \omega_b \propto a_*^{-1}$$

$$\rho_m/\rho_r \rightarrow \omega_m \propto a_*^{-1}$$

THE LITTLE SOLUTION THAT COULD

What about r_s ?

$$r_s = \int_0^{\eta_*} c_s d\eta = \int_{z_*}^{\infty} \frac{c_s dz}{H(z)} \propto \int_{z_*}^{\infty} \frac{1}{\sqrt{3(1+R_s)}} \frac{1}{\sqrt{(\rho_m/\rho_r + 1) \cdot \rho_r}} dz$$

$$r_s \propto \int_{z_*}^{\infty} \frac{1}{\sqrt{\rho_r}} dz$$

$$\rho_r \propto a^{-4} \quad dz = -\frac{da}{a^2}$$

$$R \rightarrow \omega_b \propto a_*^{-1}$$

$$\rho_m/\rho_r \rightarrow \omega_m \propto a_*^{-1}$$

THE LITTLE SOLUTION THAT COULD

What about r_s ?

$$r_s = \int_0^{\eta_*} c_s d\eta = \int_{z_*}^{\infty} \frac{c_s dz}{H(z)} \propto \int_{z_*}^{\infty} \frac{1}{\sqrt{3(1+R_*)}} \frac{1}{\sqrt{(\rho_m/\rho_r + 1) \cdot \rho_r}} dz$$

$$r_s \propto \int_{z_*}^{\infty} \frac{1}{\sqrt{\rho_r}} dz \propto \int_0^{a_*} a^2 \cdot \frac{da}{a^2}$$

$$\rho_r \propto a^{-4} \quad dz = -\frac{da}{a^2}$$

$$R \rightarrow \omega_b \propto a_*^{-1}$$

$$\rho_m/\rho_r \rightarrow \omega_m \propto a_*^{-1}$$

THE LITTLE SOLUTION THAT COULD

What about r_s ?

$$r_s = \int_0^{\eta_*} c_s d\eta = \int_{z_*}^{\infty} \frac{c_s dz}{H(z)} \propto \int_{z_*}^{\infty} \frac{1}{\sqrt{3(1+R_*)}} \frac{1}{\sqrt{(\rho_m/\rho_r + 1) \cdot \rho_r}} dz$$

$$r_s \propto \int_{z_*}^{\infty} \frac{1}{\sqrt{\rho_r}} dz \propto \int_0^{a_*} a^2 \cdot \frac{da}{a^2}$$

$$\rho_r \propto a^{-4} \quad dz = -\frac{da}{a^2}$$

$$R \rightarrow \omega_b \propto a_*^{-1}$$

$$\rho_m/\rho_r \rightarrow \omega_m \propto a_*^{-1}$$

THE LITTLE SOLUTION THAT COULD

What about r_s ?

$$r_s = \int_0^{\eta_*} c_s d\eta = \int_{z_*}^{\infty} \frac{c_s dz}{H(z)} \propto \int_{z_*}^{\infty} \frac{1}{\sqrt{3(1+R_*)}} \frac{1}{\sqrt{(\rho_m/\rho_r + 1) \cdot \rho_r}} dz$$

$$r_s \propto \int_{z_*}^{\infty} \frac{1}{\sqrt{\rho_r}} dz \propto \int_0^{a_*} a^2 \cdot \frac{da}{a^2} = \int_0^{a_*} da = a_*$$

$$R \rightarrow \omega_b \propto a_*^{-1}$$

$$\rho_m/\rho_r \rightarrow \omega_m \propto a_*^{-1}$$

THE LITTLE SOLUTION THAT COULD

What about r_s ?

$$r_s = \int_0^{\eta_*} c_s d\eta = \int_{z_*}^{\infty} \frac{c_s dz}{H(z)} \propto \int_{z_*}^{\infty} \frac{1}{\sqrt{3(1+R)}} \frac{1}{\sqrt{(\rho_m/\rho_r + 1) \cdot \rho_r}} dz$$

$$r_s \propto \int_{z_*}^{\infty} \frac{1}{\sqrt{\rho_r}} dz \propto \int_0^{a_*} a^2 \cdot \frac{da}{a^2} = \int_0^{a_*} da = a_*$$

$$R \rightarrow \omega_b \propto a_*^{-1}$$

$$\rho_m/\rho_r \rightarrow \omega_m \propto a_*^{-1}$$

THE LITTLE SOLUTION THAT COULD

$$r_s \propto a_*$$

$$R \rightarrow \omega_b \propto a_*^{-1}$$

$$\rho_m / \rho_r \rightarrow \omega_m \propto a_*^{-1}$$

THE LITTLE SOLUTION THAT COULD

$$r_s \propto a_*$$

(this is the reason why it's a H_0 model)

$$R \rightarrow \omega_b \propto a_*^{-1}$$

$$\rho_m / \rho_r \rightarrow \omega_m \propto a_*^{-1}$$

THE LITTLE SOLUTION THAT COULD

What about r_{eq} ?

$$r_s \propto a_*$$

$$R \rightarrow \omega_b \propto a_*^{-1}$$

$$\rho_m / \rho_r \rightarrow \omega_m \propto a_*^{-1}$$

THE LITTLE SOLUTION THAT COULD

What about r_{eq} ?

$$r_{\text{eq}} \propto \frac{1}{k_{\text{eq}}}$$

$$r_s \propto a_*$$

$$R \rightarrow \omega_b \propto a_*^{-1}$$

$$\rho_m / \rho_r \rightarrow \omega_m \propto a_*^{-1}$$

THE LITTLE SOLUTION THAT COULD

What about r_{eq} ?

$$r_{\text{eq}} \propto \frac{1}{k_{\text{eq}}} \propto \frac{1}{a_{\text{eq}} H_{\text{eq}}}$$

$$r_s \propto a_*$$

$$R \rightarrow \omega_b \propto a_*^{-1}$$

$$\rho_m / \rho_r \rightarrow \omega_m \propto a_*^{-1}$$

THE LITTLE SOLUTION THAT COULD

What about r_{eq} ?

$$r_{\text{eq}} \propto \frac{1}{k_{\text{eq}}} \propto \frac{1}{a_{\text{eq}} H_{\text{eq}}} \propto \frac{1}{\sqrt{\omega_m a_{\text{eq}}^{-1} + \omega_r a_{\text{eq}}^{-2}}}$$

$$r_s \propto a_*$$

$$R \rightarrow \omega_b \propto a_*^{-1}$$

$$\rho_m / \rho_r \rightarrow \omega_m \propto a_*^{-1}$$

THE LITTLE SOLUTION THAT COULD

What about r_{eq} ?

$$r_{\text{eq}} \propto \frac{1}{k_{\text{eq}}} \propto \frac{1}{a_{\text{eq}} H_{\text{eq}}} \propto \frac{1}{\sqrt{\omega_m a_{\text{eq}}^{-1} + \omega_r a_{\text{eq}}^{-2}}} \propto \frac{1}{\sqrt{2\omega_r a_{\text{eq}}^{-2}}}$$

$$r_s \propto a_*$$

$$R \rightarrow \omega_b \propto a_*^{-1}$$

$$\rho_m / \rho_r \rightarrow \omega_m \propto a_*^{-1}$$

THE LITTLE SOLUTION THAT COULD

What about r_{eq} ?

$$r_{\text{eq}} \propto \frac{1}{k_{\text{eq}}} \propto \frac{1}{a_{\text{eq}} H_{\text{eq}}} \propto \frac{1}{\sqrt{\omega_m a_{\text{eq}}^{-1} + \omega_r a_{\text{eq}}^{-2}}} \propto \frac{1}{\sqrt{2\omega_r a_{\text{eq}}^{-2}}} \propto a_{\text{eq}}$$

$$r_s \propto a_*$$

$$R \rightarrow \omega_b \propto a_*^{-1}$$

$$\rho_m / \rho_r \rightarrow \omega_m \propto a_*^{-1}$$

THE LITTLE SOLUTION THAT COULD

What about r_{eq} ?

$$r_{\text{eq}} \propto \frac{1}{k_{\text{eq}}} \propto \frac{1}{a_{\text{eq}} H_{\text{eq}}} \propto \frac{1}{\sqrt{\omega_m a_{\text{eq}}^{-1} + \omega_r a_{\text{eq}}^{-2}}} \propto \frac{1}{\sqrt{2\omega_r a_{\text{eq}}^{-2}}} \propto a_{\text{eq}}$$

$$r_s \propto a_*$$

$$R \rightarrow \omega_b \propto a_*^{-1}$$

$$\rho_m / \rho_r \rightarrow \omega_m \propto a_*^{-1}$$



THE LITTLE SOLUTION THAT COULD

What about r_{eq} ?

$$\left. \frac{\omega_m a}{\omega_r} \right|_{a=a_{\text{eq}}} \stackrel{!}{=} 1$$

$$r_{\text{eq}} \propto \frac{1}{k_{\text{eq}}} \propto \frac{1}{a_{\text{eq}} H_{\text{eq}}} \propto \frac{1}{\sqrt{\omega_m a_{\text{eq}}^{-1} + \omega_r a_{\text{eq}}^{-2}}} \propto \frac{1}{\sqrt{2\omega_r a_{\text{eq}}^{-2}}} \propto a_{\text{eq}}$$

$$r_s \propto a_*$$

$$R \rightarrow \omega_b \propto a_*^{-1}$$

$$\rho_m / \rho_r \rightarrow \omega_m \propto a_*^{-1}$$

THE LITTLE SOLUTION THAT COULD

What about r_{eq} ?

$$\left. \frac{\omega_m a}{\omega_r} \right|_{a=a_{\text{eq}}} \stackrel{!}{=} 1 \quad a_{\text{eq}} = \omega_r / \omega_m$$

$$r_{\text{eq}} \propto \frac{1}{k_{\text{eq}}} \propto \frac{1}{a_{\text{eq}} H_{\text{eq}}} \propto \frac{1}{\sqrt{\omega_m a_{\text{eq}}^{-1} + \omega_r a_{\text{eq}}^{-2}}} \propto \frac{1}{\sqrt{2\omega_r a_{\text{eq}}^{-2}}} \propto a_{\text{eq}}$$

$$r_s \propto a_*$$

$$R \rightarrow \omega_b \propto a_*^{-1}$$

$$\rho_m / \rho_r \rightarrow \omega_m \propto a_*^{-1}$$

THE LITTLE SOLUTION THAT COULD

What about r_{eq} ?

$$\left. \frac{\omega_m a}{\omega_r} \right|_{a=a_{\text{eq}}} \stackrel{!}{=} 1 \quad a_{\text{eq}} = \omega_r / \omega_m \propto a_*$$

$$r_{\text{eq}} \propto \frac{1}{k_{\text{eq}}} \propto \frac{1}{a_{\text{eq}} H_{\text{eq}}} \propto \frac{1}{\sqrt{\omega_m a_{\text{eq}}^{-1} + \omega_r a_{\text{eq}}^{-2}}} \propto \frac{1}{\sqrt{2\omega_r a_{\text{eq}}^{-2}}} \propto a_{\text{eq}}$$

$$r_s \propto a_*$$

$$R \rightarrow \omega_b \propto a_*^{-1}$$

$$\rho_m / \rho_r \rightarrow \omega_m \propto a_*^{-1}$$

THE LITTLE SOLUTION THAT COULD

What about r_{eq} ?

$$\left. \frac{\omega_m a}{\omega_r} \right|_{a=a_{\text{eq}}} \stackrel{!}{=} 1 \quad a_{\text{eq}} = \omega_r / \omega_m \propto a_*$$

$$r_{\text{eq}} \propto \frac{1}{k_{\text{eq}}} \propto \frac{1}{a_{\text{eq}} H_{\text{eq}}} \propto \frac{1}{\sqrt{\omega_m a_{\text{eq}}^{-1} + \omega_r a_{\text{eq}}^{-2}}} \propto \frac{1}{\sqrt{2\omega_r a_{\text{eq}}^{-2}}} \propto a_{\text{eq}}$$

$$r_s \propto a_*$$

$$R \rightarrow \omega_b \propto a_*^{-1}$$

$$\rho_m / \rho_r \rightarrow \omega_m \propto a_*^{-1}$$

THE LITTLE SOLUTION THAT COULD

What about r_{eq} ?

$$\left. \frac{\omega_m a}{\omega_r} \right|_{a=a_{\text{eq}}} \stackrel{!}{=} 1 \quad a_{\text{eq}} = \omega_r / \omega_m \propto a_*$$

$$r_{\text{eq}} \propto \frac{1}{k_{\text{eq}}} \propto \frac{1}{a_{\text{eq}} H_{\text{eq}}} \propto \frac{1}{\sqrt{\omega_m a_{\text{eq}}^{-1} + \omega_r a_{\text{eq}}^{-2}}} \propto \frac{1}{\sqrt{2\omega_r a_{\text{eq}}^{-2}}} \propto a_{\text{eq}} \propto a_*$$

$$r_s \propto a_*$$

$$R \rightarrow \omega_b \propto a_*^{-1}$$

$$\rho_m / \rho_r \rightarrow \omega_m \propto a_*^{-1}$$

THE LITTLE SOLUTION THAT COULD

$$r_{\text{eq}} \propto a_*$$

$$r_s \propto a_*$$

$$R \rightarrow \omega_b \propto a_*^{-1}$$

$$\rho_m / \rho_r \rightarrow \omega_m \propto a_*^{-1}$$

THE LITTLE SOLUTION THAT COULD

What about r_D ?



$$r_{\text{eq}} \propto a_*$$

$$r_s \propto a_*$$

$$R \rightarrow \omega_b \propto a_*^{-1}$$

$$\rho_m / \rho_r \rightarrow \omega_m \propto a_*^{-1}$$

THE LITTLE SOLUTION THAT COULD

What about r_D ?

$$r_D \propto 1/k_D$$

$$r_{\text{eq}} \propto a_*$$

$$r_s \propto a_*$$

$$R \rightarrow \omega_b \propto a_*^{-1}$$

$$\rho_m/\rho_r \rightarrow \omega_m \propto a_*^{-1}$$

THE LITTLE SOLUTION THAT COULD

What about r_D ?

Sekiguchi & Takahashi (2007.03381)

$$r_D \propto 1/k_D \propto \dots$$

$$r_{\text{eq}} \propto a_*$$

$$r_s \propto a_*$$

$$R \rightarrow \omega_b \propto a_*^{-1}$$

$$\rho_m/\rho_r \rightarrow \omega_m \propto a_*^{-1}$$

THE LITTLE SOLUTION THAT COULD

What about r_D ?

$$r_D \propto 1/k_D \propto \dots \propto \frac{a_*^{3/2}}{\sqrt{\omega_b \sigma_T (1 - Y_{\text{He}})}}$$

$$r_{\text{eq}} \propto a_*$$

$$r_s \propto a_*$$

$$R \rightarrow \omega_b \propto a_*^{-1}$$

$$\rho_m / \rho_r \rightarrow \omega_m \propto a_*^{-1}$$

THE LITTLE SOLUTION THAT COULD

What about r_D ?

$$r_D \propto 1/k_D \propto \dots \propto \frac{a_*^{3/2}}{\sqrt{\omega_b \sigma_T (1 - Y_{\text{He}})}}$$

$$r_D \propto a_*^2 / \sqrt{\sigma_T}$$

$$r_{\text{eq}} \propto a_*$$

$$r_s \propto a_*$$

$$R \rightarrow \omega_b \propto a_*^{-1}$$

$$\rho_m / \rho_r \rightarrow \omega_m \propto a_*^{-1}$$

THE LITTLE SOLUTION THAT COULD

What about r_D ?

$$r_D \propto 1/k_D \propto \dots \propto \frac{a_*^{3/2}}{\sqrt{\omega_b \sigma_T (1 - Y_{\text{He}})}}$$

$$r_D \propto a_*^2 / \sqrt{\sigma_T}$$

$$r_{\text{eq}} \propto a_*$$

$$r_s \propto a_*$$

$$R \rightarrow \omega_b \propto a_*^{-1}$$

$$\rho_m / \rho_r \rightarrow \omega_m \propto a_*^{-1}$$

THE LITTLE SOLUTION THAT COULD

What about r_D ?

$$r_D \propto 1/k_D \propto \dots \propto \frac{a_*^{3/2}}{\sqrt{\omega_b \sigma_T (1 - Y_{\text{He}})}}$$

$$r_D \propto a_*^2 / \sqrt{\sigma_T} = a_* \cdot a_* / \sqrt{\sigma_T}$$

$$r_{\text{eq}} \propto a_*$$

$$r_s \propto a_*$$

$$R \rightarrow \omega_b \propto a_*^{-1}$$

$$\rho_m / \rho_r \rightarrow \omega_m \propto a_*^{-1}$$

THE LITTLE SOLUTION THAT COULD

$$r_{\text{eq}} \propto a_*$$

$$r_s \propto a_*$$

$$r_D \propto a_* \cdot (a_* / \sqrt{\sigma_T})$$

$$R \rightarrow \omega_b \propto a_*^{-1}$$

$$\rho_m / \rho_r \rightarrow \omega_m \propto a_*^{-1}$$

THE NATURAL DIRECTION

- Modified recombination scenarios “want” to follow these directions

$$r_{\text{eq}} \propto a_*$$

$$r_s \propto a_*$$

$$r_D \propto a_* \cdot (a_* / \sqrt{\sigma_T})$$

$$R \rightarrow \omega_b \propto a_*^{-1}$$

$$\rho_m / \rho_r \rightarrow \omega_m \propto a_*^{-1}$$

THE NATURAL DIRECTION

- Modified recombination scenarios “want” to follow these directions
 - This means we can explain what works and what doesn't !

$$r_{\text{eq}} \propto a_*$$

$$r_s \propto a_*$$

$$r_D \propto a_* \cdot (a_* / \sqrt{\sigma_T})$$

$$R \rightarrow \omega_b \propto a_*^{-1}$$

$$\rho_m / \rho_r \rightarrow \omega_m \propto a_*^{-1}$$

THE NATURAL DIRECTION

- Modified recombination scenarios “want” to follow these directions

→ This means we can explain what works and what doesn't !

→ Data can force us off preferred direction (increasing ℓ_{eq})

→ Importantly r_s , r_D scalings stay the same!

$$r_{\text{eq}} \propto a_*$$

$$r_s \propto a_*$$

$$r_D \propto a_* \cdot (a_* / \sqrt{\sigma_T})$$

$$R \rightarrow \omega_b \propto a_*^{-1}$$

$$\rho_m / \rho_r \rightarrow \omega_m \propto a_*^{-1}$$

EXPLAINING OUR FIRST MYSTERIES

EXPLAINING OUR FIRST MYSTERIES

For this, a bit of history :)



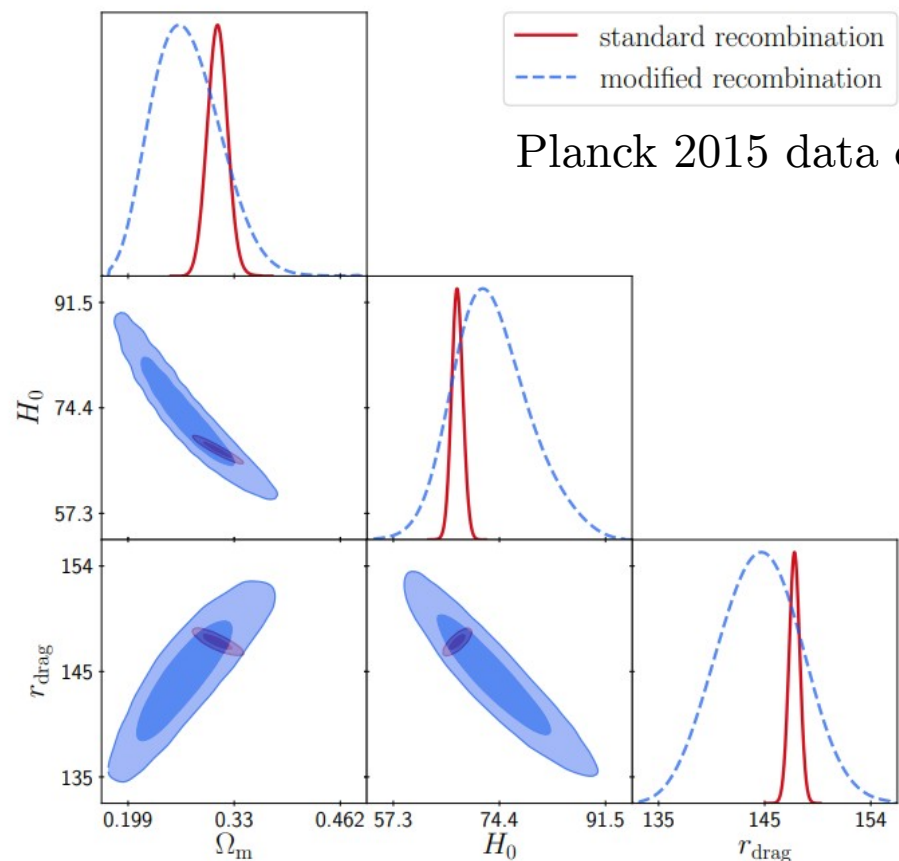
EXPLAINING OUR FIRST MYSTERIES

- Early exploratory work in [Chiang & Slosar \(1811.03624\)](#)



Full
cosmological
model

Phenomenological
model study



EXPLAINING OUR FIRST MYSTERIES

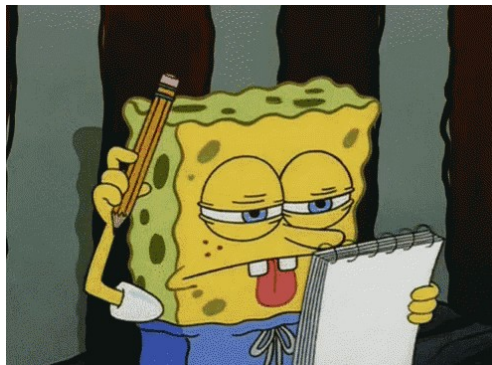
Liu+2020 (1912.00190)

Can Non-standard Recombination Resolve the Hubble Tension?

Miaoxin Liu, Zhiqi Huang,* Xiaolin Luo, Haitao Miao, Naveen K. Singh, and Lu Huang

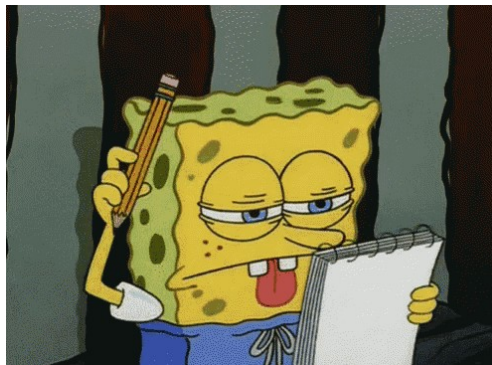
School of Physics and Astronomy, Sun Yat-sen University, 2 Daxue Road, Tangjia, Zhuhai, China

Thus, the Hubble tension is very robust against perturbations of recombination history, unless exotic physics modifies the atomic constants during the recombination epoch.



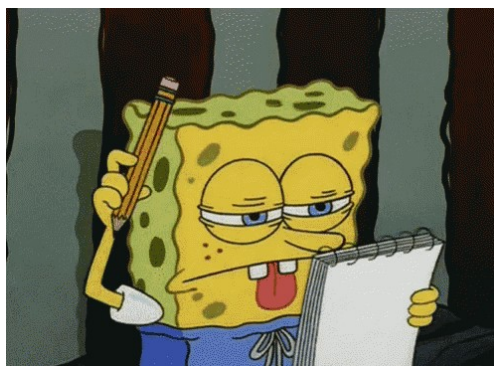
EXPLAINING OUR FIRST MYSTERIES

$$z_* \approx \underbrace{\frac{E_{\text{binding}}}{T_{\text{cmb}}}}_{\text{naive}} \cdot \underbrace{\frac{1}{40}}_{\text{Saha } (\eta_b)} \cdot \underbrace{0.75}_{\text{non-equilibrium}} \approx 1080$$



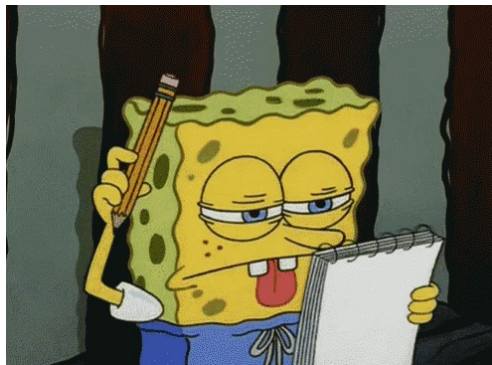
EXPLAINING OUR FIRST MYSTERIES

$$z_* \approx \underbrace{\frac{E_{\text{binding}}}{T_{\text{cmb}}}}_{\text{naive}} \cdot \underbrace{\frac{1}{40}}_{\text{Saha } (\eta_b)} \cdot \underbrace{0.75}_{\text{non-equilibrium}} \approx 1080$$



EXPLAINING OUR FIRST MYSTERIES

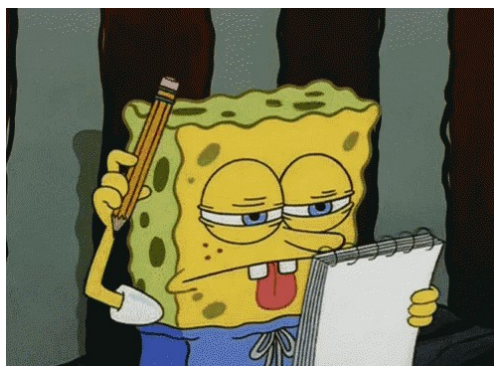
$$z_* \approx \underbrace{\frac{E_{\text{binding}}}{T_{\text{cmb}}}}_{\text{naive}} \cdot \underbrace{\frac{1}{40}}_{\text{Saha } (\eta_b)} \cdot \underbrace{0.75}_{\text{non-equilibrium}} \approx 1080$$



EXPLAINING OUR FIRST MYSTERIES

$$E_{\text{binding}} = \frac{1}{2} m_e \alpha^2 \approx 13.6 \text{eV}$$

$$z_* \approx \underbrace{\frac{E_{\text{binding}}}{T_{\text{cmb}}}}_{\text{naive}} \cdot \underbrace{\frac{1}{40}}_{\text{Saha } (\eta_b)} \cdot \underbrace{0.75}_{\text{non-equilibrium}} \approx 1080$$



EXPLAINING OUR FIRST MYSTERIES

$$E_{\text{binding}} = \frac{1}{2} m_e \alpha^2 \approx 13.6 \text{eV}$$

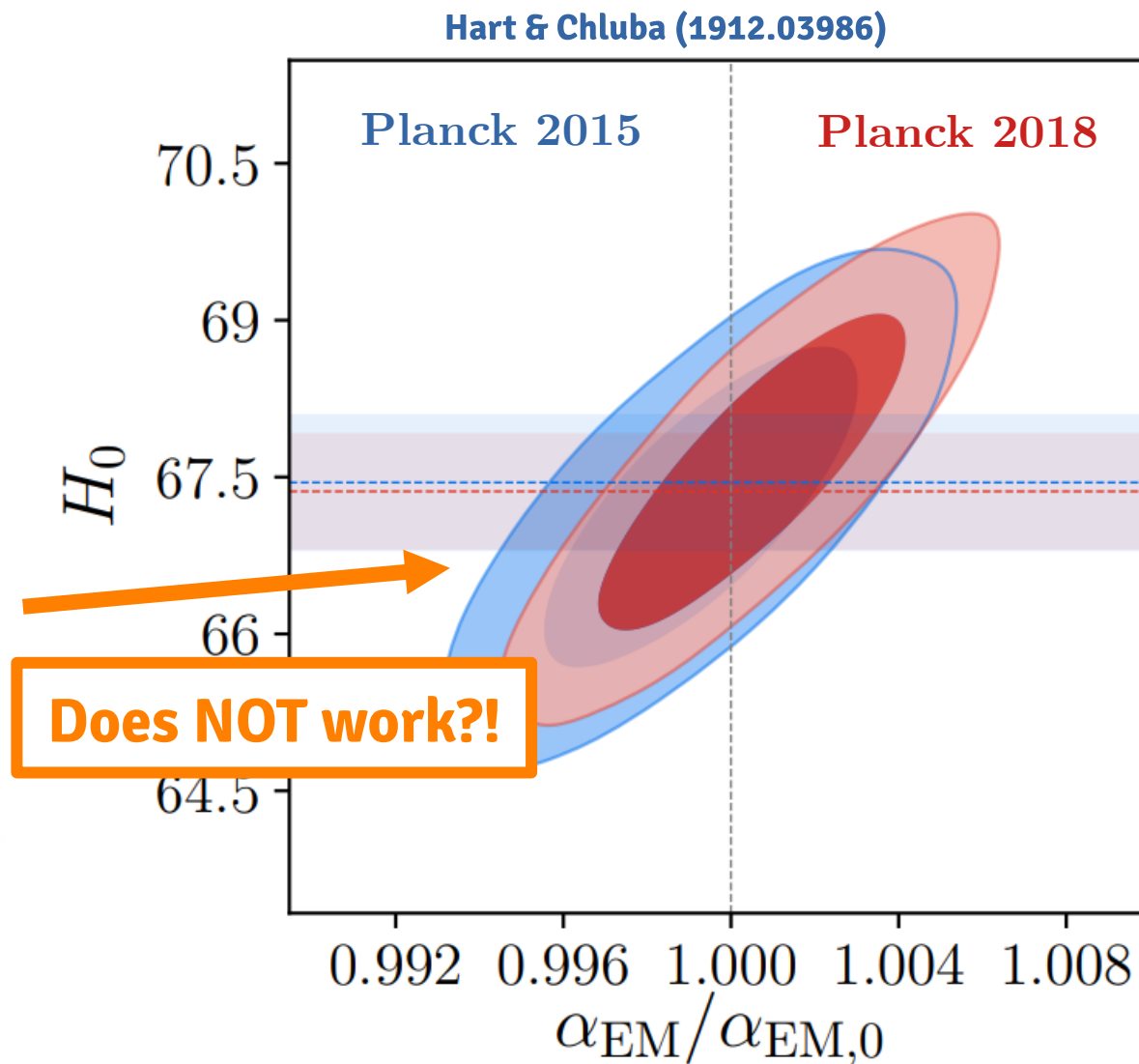
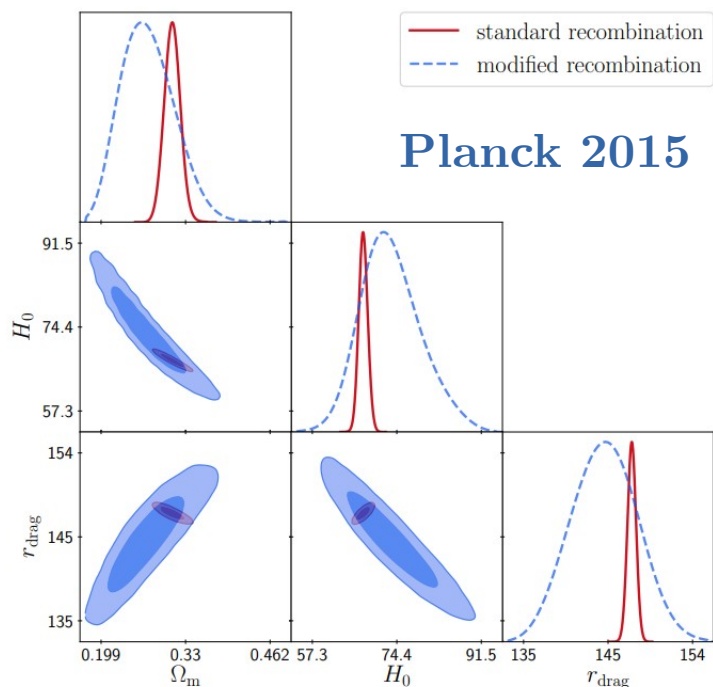
EXPLAINING OUR FIRST MYSTERIES

$$E_{\text{binding}} = \frac{1}{2} m_e \alpha^2 \approx 13.6 \text{eV}$$

$$\mathcal{L} = \dots + -\frac{1}{4} B_F(\phi) F_{\mu\nu} F^{\mu\nu}$$

$$\Rightarrow \frac{\Delta\alpha}{\alpha_0} = (B_F(\phi))^{-1} - 1$$

EXPLAINING OUR FIRST MYSTERIES



THE NATURAL DIRECTION

$$r_{\text{eq}} \propto a_*$$

$$r_s \propto a_*$$

$$r_D \propto a_* \cdot (a_* / \sqrt{\sigma_T})$$

$$R \rightarrow \omega_b \propto a_*^{-1}$$

$$\rho_m / \rho_r \rightarrow \omega_m \propto a_*^{-1}$$

THE NATURAL DIRECTION

$$(a_*)^{-1} \propto z_* \propto E_{\text{binding}} \propto m_e \alpha^2$$

$$a_* \propto \alpha^{-2}$$

$$a_* \propto m_e^{-1}$$

$$r_{\text{eq}} \propto a_*$$

$$r_s \propto a_*$$

$$r_D \propto a_* \cdot (a_* / \sqrt{\sigma_T})$$

$$R \rightarrow \omega_b \propto a_*^{-1}$$

$$\rho_m / \rho_r \rightarrow \omega_m \propto a_*^{-1}$$

THE NATURAL DIRECTION

$$(a_*)^{-1} \propto z_* \propto E_{\text{binding}} \propto m_e \alpha^2$$

$$a_* \propto \alpha^{-2}$$

$$a_* \propto m_e^{-1}$$

$$\sigma_T \propto \frac{\alpha^2}{m_e^2}$$

$$r_{\text{eq}} \propto a_*$$

$$r_s \propto a_*$$

$$r_D \propto a_* \cdot (a_* / \sqrt{\sigma_T})$$

$$R \rightarrow \omega_b \propto a_*^{-1}$$

$$\rho_m / \rho_r \rightarrow \omega_m \propto a_*^{-1}$$

THE NATURAL DIRECTION

$$(a_*)^{-1} \propto z_* \propto E_{\text{binding}} \propto m_e \alpha^2$$

$$a_* \propto \alpha^{-2}$$

$$a_* \propto m_e^{-1}$$

$$\sigma_T \propto \frac{\alpha^2}{m_e^2}$$

$$a_* / \sqrt{\sigma_T} \propto \alpha^{-3}$$

$$\frac{a_*}{\sqrt{\sigma_T}} \propto \frac{m_e^{-1}}{\sqrt{m_e^{-2}}} \propto \text{const}$$

$$r_{\text{eq}} \propto a_*$$

$$r_s \propto a_*$$

$$r_D \propto a_* \cdot (a_* / \sqrt{\sigma_T})$$

$$R \rightarrow \omega_b \propto a_*^{-1}$$

$$\rho_m / \rho_r \rightarrow \omega_m \propto a_*^{-1}$$

THE NATURAL DIRECTION

$$a_*/\sqrt{\sigma_T} \propto \alpha^{-3} \longrightarrow \text{Bad for CMB damping !}$$

$$a_*/\sqrt{\sigma_T} \propto \text{const} \longrightarrow \text{Perfect for CMB damping !}$$

$$r_{\text{eq}} \propto a_*$$

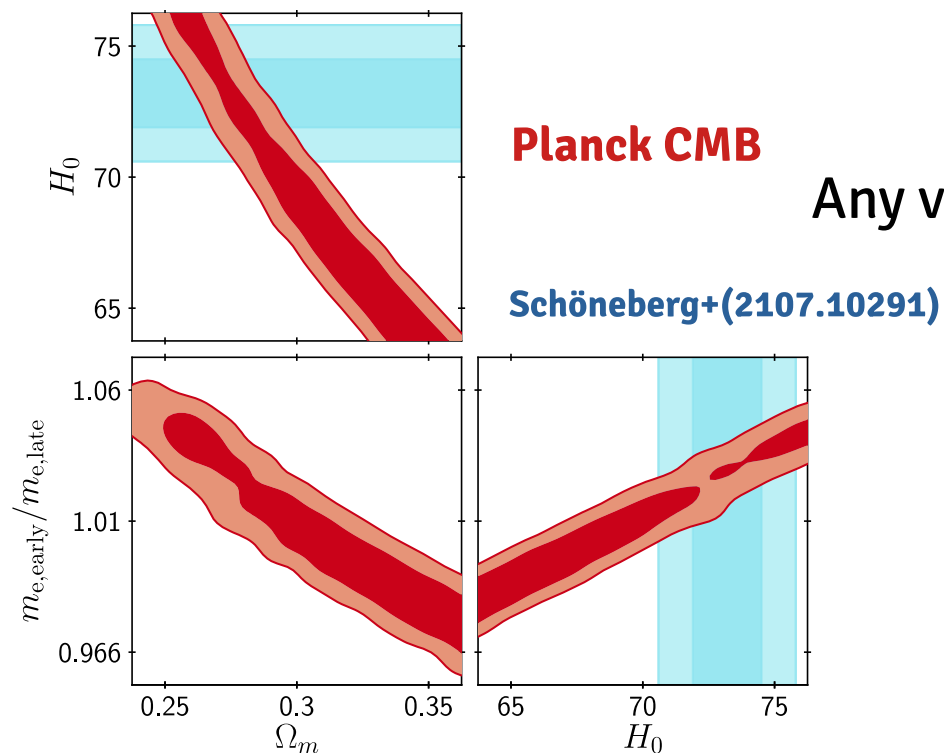
$$r_s \propto a_*$$

$$r_D \propto a_* \cdot (a_*/\sqrt{\sigma_T})$$

$$R \rightarrow \omega_b \propto a_*^{-1}$$

$$\rho_m/\rho_r \rightarrow \omega_m \propto a_*^{-1}$$

THE NATURAL DIRECTION



Planck CMB

Any value of H_0 is allowed!

Schöneberg+(2107.10291)

$$r_{eq} \propto a_*$$

$$r_s \propto a_*$$

$$r_D \propto a_* \cdot (a_*/\sqrt{\sigma_T})$$

$$R \rightarrow \omega_b \propto a_*^{-1}$$

$$\rho_m/\rho_r \rightarrow \omega_m \propto a_*^{-1}$$

SOLVING MYSTERIES

Mysteries solved:

- Why does α fail where m_e succeeds? $\rightarrow \sigma_T$ scaling

$$r_{\text{eq}} \propto a_*$$

$$r_s \propto a_*$$

$$r_D \propto a_* \cdot (a_* / \sqrt{\sigma_T})$$

$$R \rightarrow \omega_b \propto a_*^{-1}$$

$$\rho_m / \rho_r \rightarrow \omega_m \propto a_*^{-1}$$

SOLVING MYSTERIES

Can other models also shift σ_T ?

Yes, but...

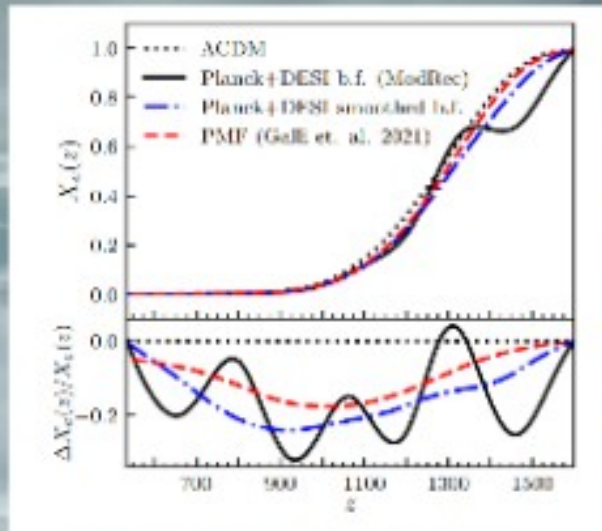
$$r_{\text{eq}} \propto a_*$$

$$r_s \propto a_*$$

$$r_D \propto a_* \cdot (a_* / \sqrt{\sigma_T})$$

$$R \rightarrow \omega_b \propto a_*^{-1}$$

$$\rho_m / \rho_r \rightarrow \omega_m \propto a_*^{-1}$$



SOLVING MYSTERIES

Can other models also shift σ_T ?

Yes, but it's not trivial/by default

$$r_{\text{eq}} \propto a_*$$

$$r_s \propto a_*$$

$$r_D \propto a_* \cdot (a_* / \sqrt{\sigma_T})$$

$$R \rightarrow \omega_b \propto a_*^{-1}$$

$$\rho_m / \rho_r \rightarrow \omega_m \propto a_*^{-1}$$

SOLVING MYSTERIES

Can other models also shift σ_T ?

Yes, but it's not trivial/by default



Frequentist vs Bayesian!

$$r_{\text{eq}} \propto a_*$$

$$r_s \propto a_*$$

$$r_D \propto a_* \cdot (a_* / \sqrt{\sigma_T})$$

$$R \rightarrow \omega_b \propto a_*^{-1}$$

$$\rho_m / \rho_r \rightarrow \omega_m \propto a_*^{-1}$$

SOLVING MYSTERIES

Mysteries solved:

- Why does α fail where m_e succeeds? $\rightarrow \sigma_T$ scaling
- Why did 4-param mod. rec. fail? $\rightarrow \sigma_T$ scaling + simple

$$r_{\text{eq}} \propto a_*$$

$$r_s \propto a_*$$

$$r_D \propto a_* \cdot (a_* / \sqrt{\sigma_T})$$

$$R \rightarrow \omega_b \propto a_*^{-1}$$

$$\rho_m / \rho_r \rightarrow \omega_m \propto a_*^{-1}$$

SOLVING MYSTERIES

Mysteries solved:

- Why does α fail where m_e succeeds? $\rightarrow \sigma_T$ scaling
- Why did 4-param mod. rec. fail? $\rightarrow \sigma_T$ scaling + simple
- Why does DESI love it?

$$r_{\text{eq}} \propto a_*$$

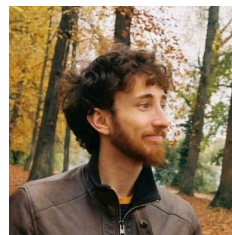
$$r_s \propto a_*$$

$$r_D \propto a_* \cdot (a_* / \sqrt{\sigma_T})$$

$$R \rightarrow \omega_b \propto a_*^{-1}$$

$$\rho_m / \rho_r \rightarrow \omega_m \propto a_*^{-1}$$

SOLVING MYSTERIES



Schöneberg & Vacher (2407.16845)

$\Delta m_e/m_{e,0}$	P18+DESI	1.21 ± 0.63	70.03 ± 1.06	2.0	this work
$\Delta m_e/m_{e,0} + \Omega_k$	P18+DESI	2.52 ± 1.85	70.94 ± 1.23	1.3	this work, see also [16]
$\Delta m_e/m_{e,0} + \Omega_k$	P18+DESI+PanPLUS	1.88 ± 0.52	71.61 ± 1.00	1.0	this work
$\Delta m_e/m_{e,0} + w_0/w_a$	P18+DESI	1.53 ± 0.63	70.30 ± 1.34	1.6	this work
$\Delta m_e/m_{e,0} + w_0/w_a$	P18+DESI+PanPLUS	0.72 ± 0.84	69.38 ± 2.17	1.5	this work

?!?!? **3 σ preference**

Without SH0ES we get a $<2\sigma$ Hubble tension?!

$$r_{\text{eq}} \propto a_*$$

$$r_s \propto a_*$$

$$r_D \propto a_* \cdot (a_*/\sqrt{\sigma_T})$$

$$R \rightarrow \omega_b \propto a_*^{-1}$$

$$\rho_m/\rho_r \rightarrow \omega_m \propto a_*^{-1}$$

SOLVING MYSTERIES

To answer this mystery:

→ Parameter changes!

$$r_{\text{eq}} \propto a_*$$

$$r_s \propto a_*$$

$$r_D \propto a_* \cdot (a_* / \sqrt{\sigma_T})$$

$$R \rightarrow \omega_b \propto a_*^{-1}$$

$$\rho_m / \rho_r \rightarrow \omega_m \propto a_*^{-1}$$

SOLVING MYSTERIES

To answer this mystery:

→ Parameter changes!

$$\theta_s = \frac{r_s}{r_A(z_*)} \quad \text{measured at 0.03\% uncertainty}$$

$$r_{\text{eq}} \propto a_*$$

$$r_s \propto a_*$$

$$r_D \propto a_* \cdot (a_* / \sqrt{\sigma_T})$$

$$R \rightarrow \omega_b \propto a_*^{-1}$$

$$\rho_m / \rho_r \rightarrow \omega_m \propto a_*^{-1}$$

THE NATURAL DIRECTION

Parameter changes:



$$r_A \propto \int_{a_*}^1 \frac{1}{\sqrt{\omega_m a^{-3} + h^2}}$$

Assumption:
 Λ CDM-like expansion
 history at low- z

$$r_A \stackrel{!}{\propto} a_*$$

$$r_{\text{eq}} \propto a_*$$

$$r_s \propto a_*$$

$$r_D \propto a_*$$

$$R \rightarrow \omega_b \propto a_*^{-1}$$

$$\rho_m / \rho_r \rightarrow \omega_m \propto a_*^{-1}$$

THE NATURAL DIRECTION

Parameter changes:



$$r_A \propto \int_{a_*}^1 \frac{1}{\sqrt{\omega_m a^{-3} + h^2}}$$

Assumption:
 Λ CDM-like expansion
 history at low- z

$$r_A \stackrel{!}{\propto} a_* \quad \Rightarrow \quad h \stackrel{!}{\propto} a_*^{-3.23}$$

$$r_{\text{eq}} \propto a_*$$

$$r_s \propto a_*$$

$$r_D \propto a_*$$

$$R \rightarrow \omega_b \propto a_*^{-1}$$

$$\rho_m / \rho_r \rightarrow \omega_m \propto a_*^{-1}$$

THE NATURAL DIRECTION



Assumption:
 Λ CDM-like expansion
history at low- z

$$r_{\text{eq}} \propto a_*$$

$$r_s \propto a_*$$

$$r_D \propto a_*$$

$$h \overset{!}{\propto} a_*^{-3.23}$$

$$R \rightarrow \omega_b \propto a_*^{-1}$$

$$\rho_m / \rho_r \rightarrow \omega_m \propto a_*^{-1}$$

THE NATURAL DIRECTION

$$a_* \propto m_e^{-1}$$

$$a_* \propto z_*^{-1} \propto E_{\text{bin}}^{-1} \propto m_e^{-1}$$



Assumption:
 Λ CDM-like expansion
 history at low- z

$$r_{\text{eq}} \propto a_*$$

$$r_s \propto a_*$$

$$r_D \propto a_*$$

$$h \overset{!}{\propto} a_*^{-3.23}$$

$$R \rightarrow \omega_b \propto a_*^{-1}$$

$$\rho_m / \rho_r \rightarrow \omega_m \propto a_*^{-1}$$

THE NATURAL DIRECTION

$$\Omega_m h^2 \propto a_*^{-1}$$



Assumption:
 Λ CDM-like expansion
 history at low- z

$$r_{\text{eq}} \propto a_*$$

$$r_s \propto a_*$$

$$r_D \propto a_*$$

$$h \stackrel{!}{\propto} a_*^{-3.23}$$

$$R \rightarrow \omega_b \propto a_*^{-1}$$

$$\rho_m / \rho_r \rightarrow \omega_m \propto a_*^{-1}$$

THE NATURAL DIRECTION

$$\Omega_m h^2 \propto a_*^{-1}$$

$$h \propto a_*^{-3.23}$$



Assumption:
 Λ CDM-like expansion
 history at low- z

$$r_{\text{eq}} \propto a_*$$

$$r_s \propto a_*$$

$$r_D \propto a_*$$

$$h \overset{!}{\propto} a_*^{-3.23}$$

$$R \rightarrow \omega_b \propto a_*^{-1}$$

$$\rho_m / \rho_r \rightarrow \omega_m \propto a_*^{-1}$$

THE NATURAL DIRECTION

$$\Omega_m h^2 \propto a_*^{-1} \quad \Omega_m \propto a_*^{5.26} \propto h^{-1.7}$$

$$h \propto a_*^{-3.23}$$



Assumption:
 Λ CDM-like expansion
 history at low- z

$$r_{\text{eq}} \propto a_*$$

$$r_s \propto a_*$$

$$r_D \propto a_*$$

$$h \overset{!}{\propto} a_*^{-3.23}$$

$$R \rightarrow \omega_b \propto a_*^{-1}$$

$$\rho_m / \rho_r \rightarrow \omega_m \propto a_*^{-1}$$

THE NATURAL DIRECTION

$$\Omega_m h^2 \propto a_*^{-1}$$

$$h \propto a_*^{-3.23}$$

$$\Omega_m \propto h^{-1.7}$$

We haven't used a
 m_e -specific law!



Assumption:
 Λ CDM-like expansion
history at low- z

$$r_{\text{eq}} \propto a_*$$

$$r_s \propto a_*$$

$$r_D \propto a_*$$

$$h \overset{!}{\propto} a_*^{-3.23}$$

$$R \rightarrow \omega_b \propto a_*^{-1}$$

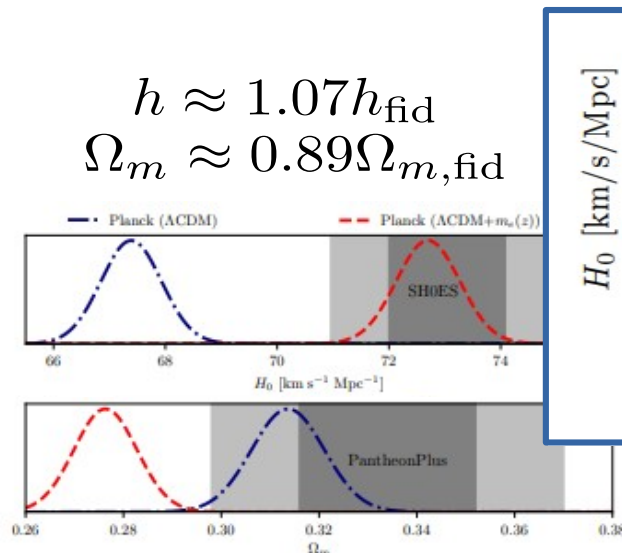
$$\rho_m / \rho_r \rightarrow \omega_m \propto a_*^{-1}$$

THE NATURAL DIRECTION

$$\Omega_m h^2 \propto a_*^{-1}$$

$$h \propto a_*^{-3.23}$$

$$\Omega_m \propto h^{-1.7}$$



Lee+2212.04494

Free-form reconstruction of m_e

$$r_{\text{eq}} \propto a_*$$

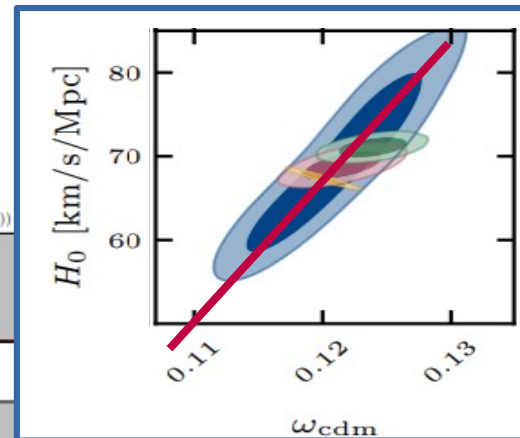
$$r_s \propto a_*$$

$$r_D \propto a_*$$

$$h \overset{!}{\propto} a_*^{-3.23}$$

$$R \rightarrow \omega_b \propto a_*^{-1}$$

$$\rho_m / \rho_r \rightarrow \omega_m \propto a_*^{-1}$$



Lynch+2404.05715

Free-form
reconstruction
of ionization x_e



Assumption:

Λ CDM-like expansion
history at low- z

THE NATURAL DIRECTION

$$\Omega_m h^2 \propto a_*^{-1}$$

$$h \propto a_*^{-3.23}$$

$$\Omega_m \propto h^{-1.7}$$



Assumption:
 Λ CDM-like expansion
 history at low- z

$$r_{\text{eq}} \propto a_*$$

$$r_s \propto a_*$$

$$r_D \propto a_*$$

$$h \overset{!}{\propto} a_*^{-3.23}$$

$$R \rightarrow \omega_b \propto a_*^{-1}$$

$$\rho_m / \rho_r \rightarrow \omega_m \propto a_*^{-1}$$

THE NATURAL DIRECTION

$$\Omega_m h^2 \propto a_*^{-1}$$

$$h \propto a_*^{-3.23}$$

$$\Omega_m \propto h^{-1.7}$$

$$r_s \cdot h \propto a_*^{-2.23}$$



Assumption:
 Λ CDM-like expansion
 history at low- z

$$r_{\text{eq}} \propto a_*$$

$$r_s \propto a_*$$

$$r_D \propto a_*$$

$$h \overset{!}{\propto} a_*^{-3.23}$$

$$R \rightarrow \omega_b \propto a_*^{-1}$$

$$\rho_m / \rho_r \rightarrow \omega_m \propto a_*^{-1}$$

THE NATURAL DIRECTION

$$\Omega_m h^2 \propto a_*^{-1}$$

$$h \propto a_*^{-3.23}$$

$$\Omega_m \propto h^{-1.7}$$

$$r_s \cdot h \propto a_*^{-2.23} \propto h^{0.7}$$



Assumption:
 Λ CDM-like expansion
 history at low- z

$$r_{\text{eq}} \propto a_*$$

$$r_s \propto a_*$$

$$r_D \propto a_*$$

$$h \overset{!}{\propto} a_*^{-3.23}$$

$$R \rightarrow \omega_b \propto a_*^{-1}$$

$$\rho_m / \rho_r \rightarrow \omega_m \propto a_*^{-1}$$

THE NATURAL DIRECTION

$$\Omega_m h^2 \propto a_*^{-1}$$

$$h \propto a_*^{-3.23}$$

$$\Omega_m \propto h^{-1.7}$$

$$r_s \cdot h \propto h^{0.7}$$



Assumption:
 Λ CDM-like expansion
 history at low- z

$$r_{\text{eq}} \propto a_*$$

$$r_s \propto a_*$$

$$r_D \propto a_*$$

$$h \overset{!}{\propto} a_*^{-3.23}$$

$$R \rightarrow \omega_b \propto a_*^{-1}$$

$$\rho_m / \rho_r \rightarrow \omega_m \propto a_*^{-1}$$

THE NATURAL DIRECTION

$$\Omega_m h^2 \propto a_*^{-1}$$

$$h \propto a_*^{-3.23}$$

$$\Omega_m \propto h^{-1.7}$$

$$r_s \cdot h \propto h^{0.7}$$



Assumption:
 Λ CDM-like expansion
 history at low- z

$$r_{\text{eq}} \propto a_*$$

$$r_s \propto a_*$$

$$r_D \propto a_*$$

$$h \overset{!}{\propto} a_*^{-3.23}$$

$$R \rightarrow \omega_b \propto a_*^{-1}$$

$$\rho_m / \rho_r \rightarrow \omega_m \propto a_*^{-1}$$

THE NATURAL DIRECTION

$$\Omega_m h^2 \propto a_*^{-1}$$

$$h \propto a_*^{-3.23}$$

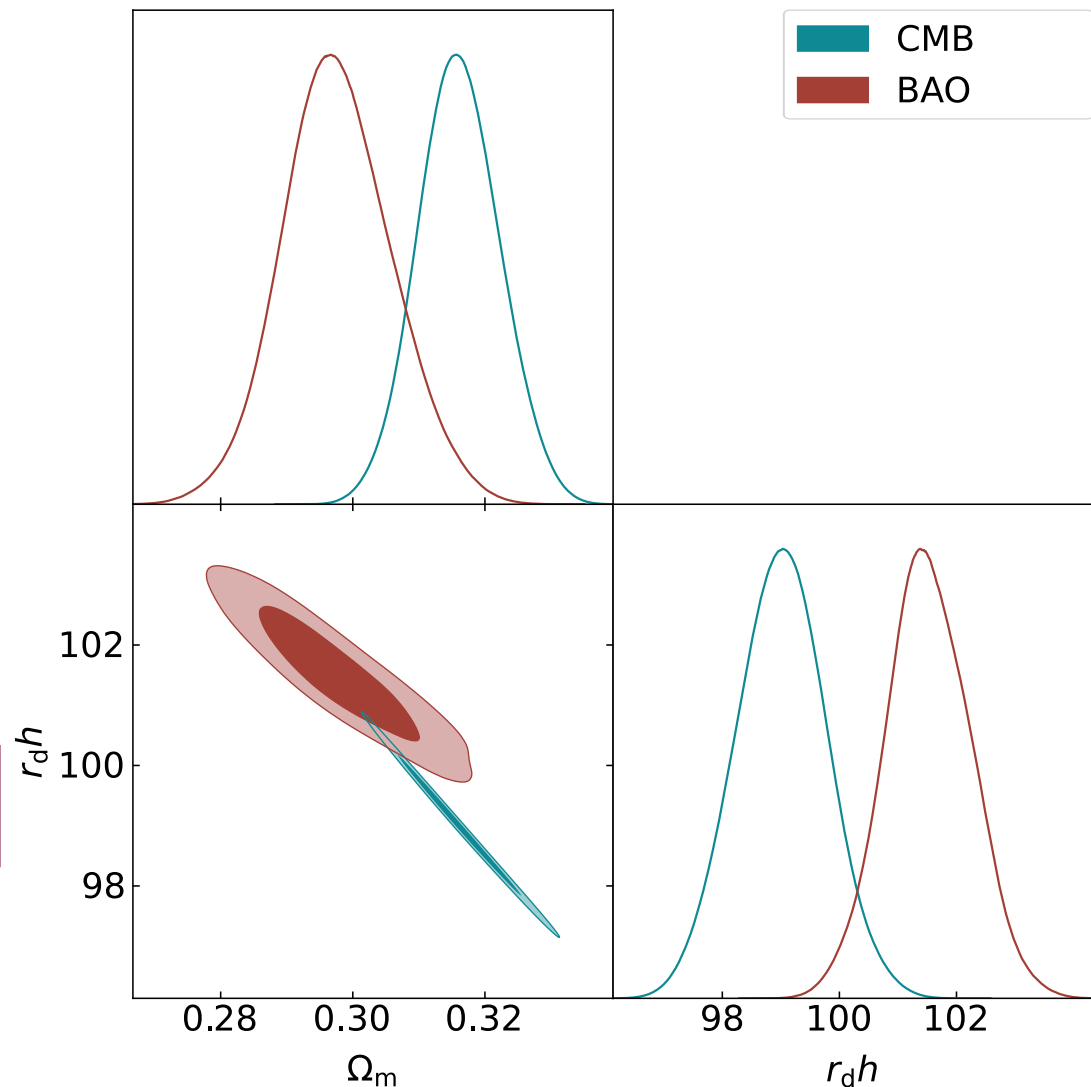
$$\Omega_m \propto h^{-1.7}$$

$$r_s \cdot h \propto h^{0.7}$$

$$r_{\text{eq}} \propto a_*$$

$$r_s \propto$$

$$R \rightarrow \omega_b \propto a_*^{-1}$$



THE NATURAL DIRECTION

$$\Omega_m h^2 \propto a_*^{-1}$$

$$h \propto a_*^{-3.23}$$

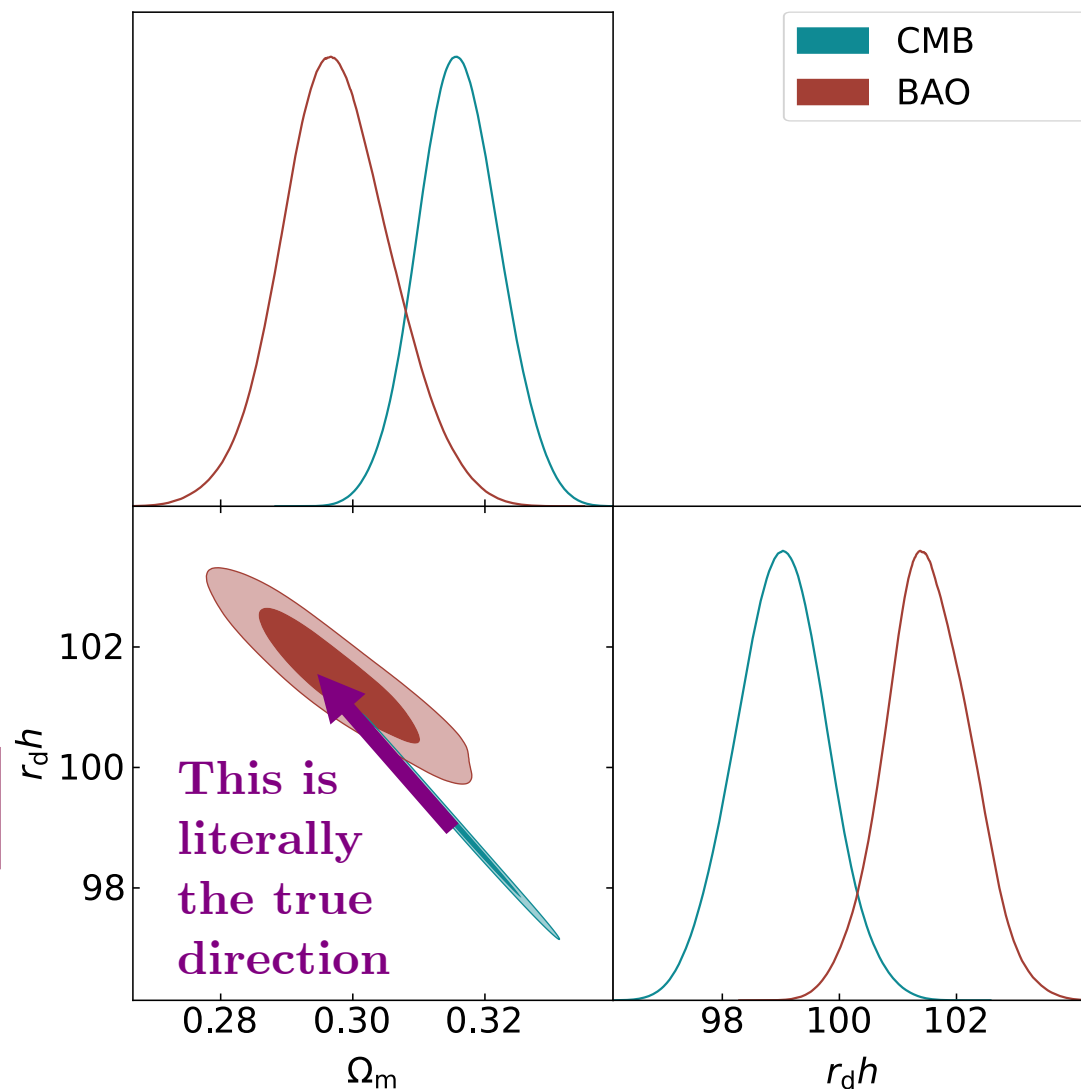
$$\Omega_m \propto h^{-1.7}$$

$$r_s \cdot h \propto h^{0.7}$$

$$r_{\text{eq}} \propto a_*$$

$$r_s \propto$$

$$R \rightarrow \omega_b \propto a_*^{-1}$$



SOLVING MYSTERIES

Mysteries solved:

- Why does α fail where m_e succeeds? $\rightarrow \sigma_T$ scaling
- Why did 4-param mod. rec. fail? $\rightarrow \sigma_T$ scaling + simple
- Why does DESI love it? $\rightarrow$ Reduces Ω_m , increases $h r_s$

$$r_{\text{eq}} \propto a_*$$

$$r_s \propto a_*$$

$$r_D \propto a_* \cdot (a_* / \sqrt{\sigma_T})$$

$$R \rightarrow \omega_b \propto a_*^{-1}$$

$$\rho_m / \rho_r \rightarrow \omega_m \propto a_*^{-1}$$





THE NATURAL DIRECTION

Claim: Model does not affect σ_8 much
(only BAO, baryon suppression)

$$\Omega_m h^2 \propto a_*^{-1}$$

$$h \propto a_*^{-3.23}$$

$$\Omega_m \propto h^{-1.7}$$

$$r_s \cdot h \propto h^{0.7}$$



Assumption:
 Λ CDM-like expansion
history at low- z

$$r_{\text{eq}} \propto a_*$$

$$r_s \propto a_*$$

$$r_D \propto a_*$$

$$h \overset{!}{\propto} a_*^{-3.23}$$

$$R \rightarrow \omega_b \propto a_*^{-1}$$

$$\rho_m / \rho_r \rightarrow \omega_m \propto a_*^{-1}$$

THE NATURAL DIRECTION

Claim: Model does not affect σ_8 much
(only BAO, baryon suppression)

$$S_8 \propto h^{-0.86}$$

$$\Omega_m \propto h^{-1.7}$$

$$r_s \cdot h \propto h^{0.7}$$



Assumption:
 Λ CDM-like expansion
history at low- z

$$r_{\text{eq}} \propto a_*$$

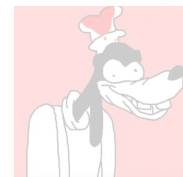
$$r_s \propto a_*$$

$$r_D \propto a_*$$

$$h \stackrel{!}{\propto} a_*^{-3.23}$$

$$R \rightarrow \omega_b \propto a_*^{-1}$$

$$\rho_m / \rho_r \rightarrow \omega_m \propto a_*^{-1}$$



THE NATURAL DIRECTION

S_8 from 0.83 $\rightarrow$ 0.81

$$S_8 \equiv \sigma_8 (\Omega_m/0.3)^{0.5} = 0.789^{+0.012}_{-0.012}$$

DES Y6 3x2pt

$$S_8 \equiv \sigma_8 \sqrt{\Omega_m/0.3} = 0.815^{+0.016}_{-0.021}$$

KiDS legacy

$$S_8 \propto h^{-0.86}$$

$$\Omega_m \propto h^{-1.7}$$

$$r_s \cdot h \propto h^{0.7}$$



Assumption:
 Λ CDM-like expansion
 history at low- z

$$r_{\text{eq}} \propto a_*$$

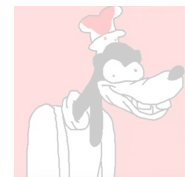
$$r_s \propto a_*$$

$$r_D \propto a_*$$

$$h \stackrel{!}{\propto} a_*^{-3.23}$$

$$R \rightarrow \omega_b \propto a_*^{-1}$$

$$\rho_m/\rho_r \rightarrow \omega_m \propto a_*^{-1}$$



SOLVING MYSTERIES

Mysteries solved:

- Why does α fail where m_e succeeds? $\rightarrow \sigma_T$ scaling
- Why did 4-param mod. rec. fail? $\rightarrow \sigma_T$ scaling + simple
- Why does DESI love it? $\rightarrow$ Reduces Ω_m , increases h r_s
- Why does S_8 data love it? $\rightarrow$ Reduces S_8

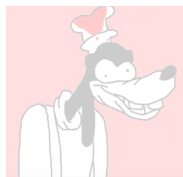
$$r_{\text{eq}} \propto a_*$$

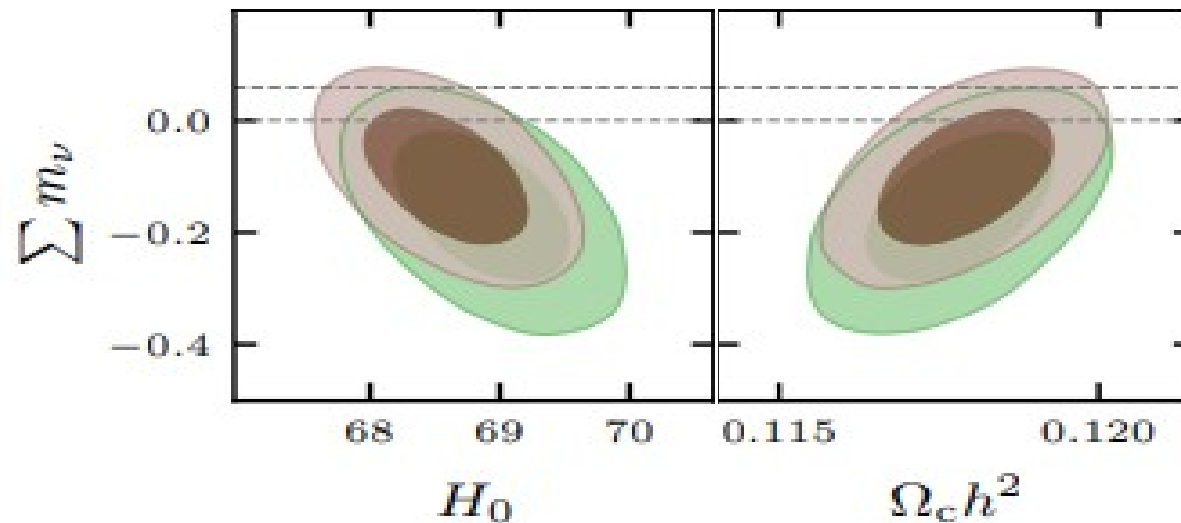
$$r_s \propto a_*$$

$$r_D \propto a_* \cdot (a_* / \sqrt{\sigma_T})$$

$$R \rightarrow \omega_b \propto a_*^{-1}$$

$$\rho_m / \rho_r \rightarrow \omega_m \propto a_*^{-1}$$

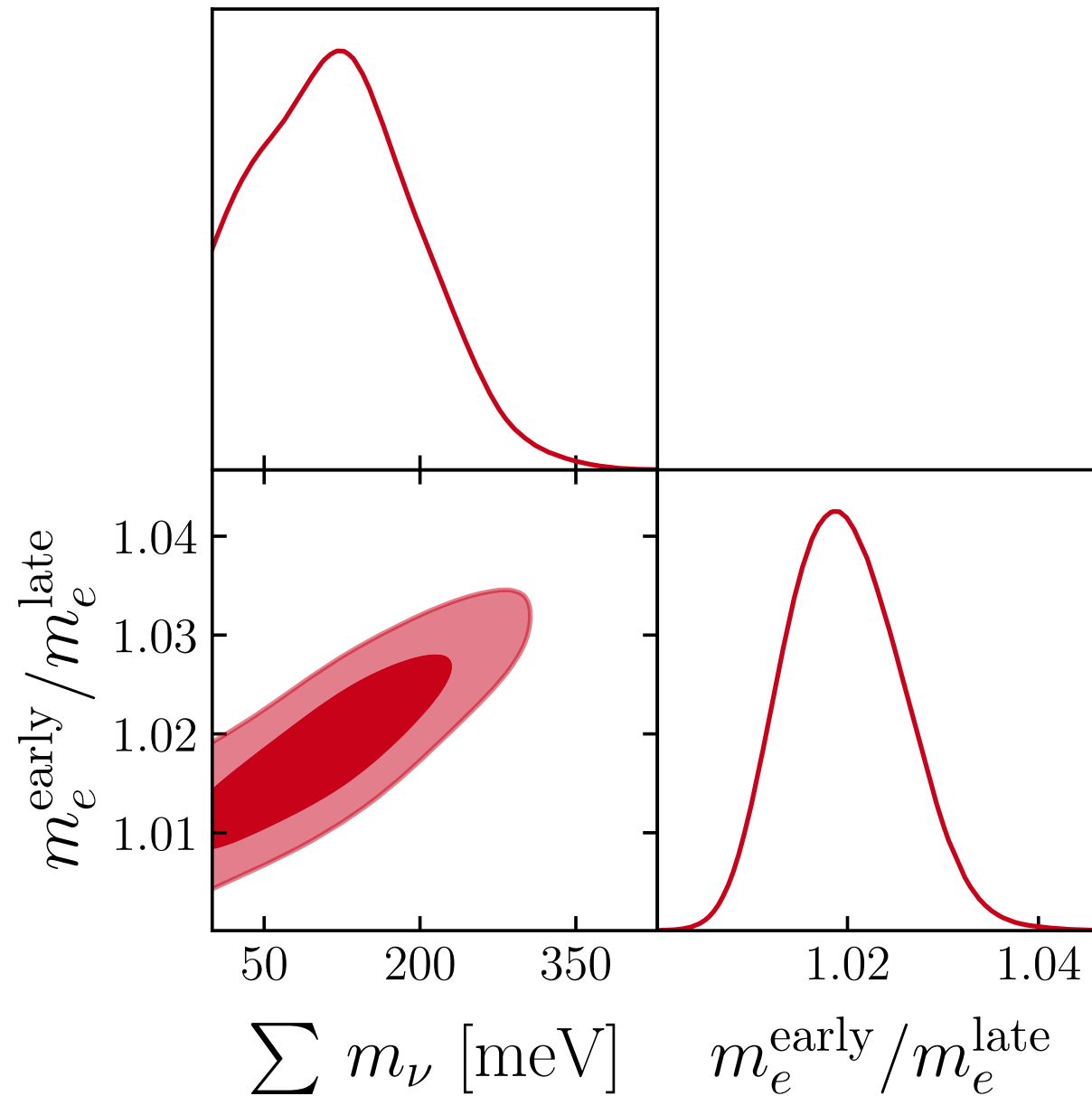




Neutrino mass is preferred negative
in order to get Ω_m smaller

More neutrinos $\rightarrow$ more
lensing $\rightarrow$ less Ω_m required

If only there was another way to get
to low Ω_m ...



SOLVING MYSTERIES

Mysteries solved:

- Why does α fail where m_e succeeds? $\rightarrow \sigma_T$ scaling
- Why did 4-param mod. rec. fail? $\rightarrow \sigma_T$ scaling + simple
- Why does DESI love it? $\rightarrow$ Reduces Ω_m , increases $h r_s$
- Why does S_8 data love it? $\rightarrow$ Reduces S_8
- Why do neutrinos love it? $\rightarrow$ Allows small Ω_m at $m_\nu > 0$

SOLVING MYSTERIES

Mysteries solved:

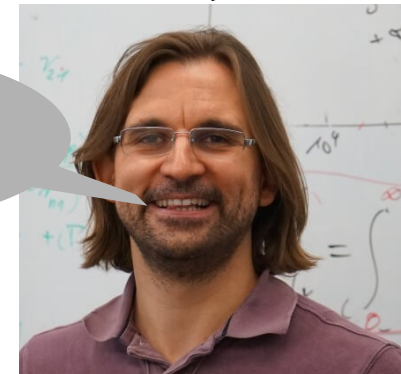
- Why does α fail where m_e succeeds? $\rightarrow \sigma_T$ scaling
- Why did 4-param mod. rec. fail? $\rightarrow \sigma_T$ scaling + simple
- Why does DESI love it? $\rightarrow$ Reduces Ω_m , increases h r_s
- Why does S_8 data love it? $\rightarrow$ Reduces S_8
- Why do neutrinos love it? $\rightarrow$ Allows small Ω_m at $m_\nu > 0$

=> Most of these not specific to m_e model !
(only σ_T scaling)

SOLVING MYSTERIES

- We need more investigations into modified recombination
- We need to solve σ_T scaling better than just complicated x_e history

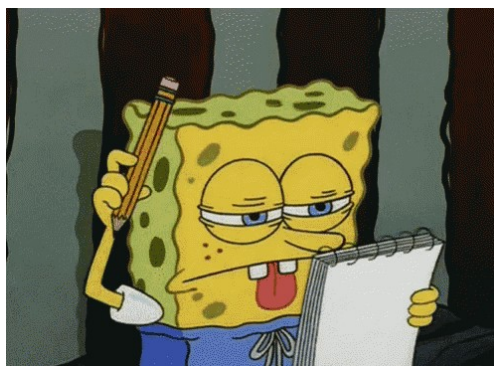
Already on it
with Ito



=> Most of these not specific to m_e model !
(only σ_T scaling)

EXPLAINING OUR FIRST MYSTERIES

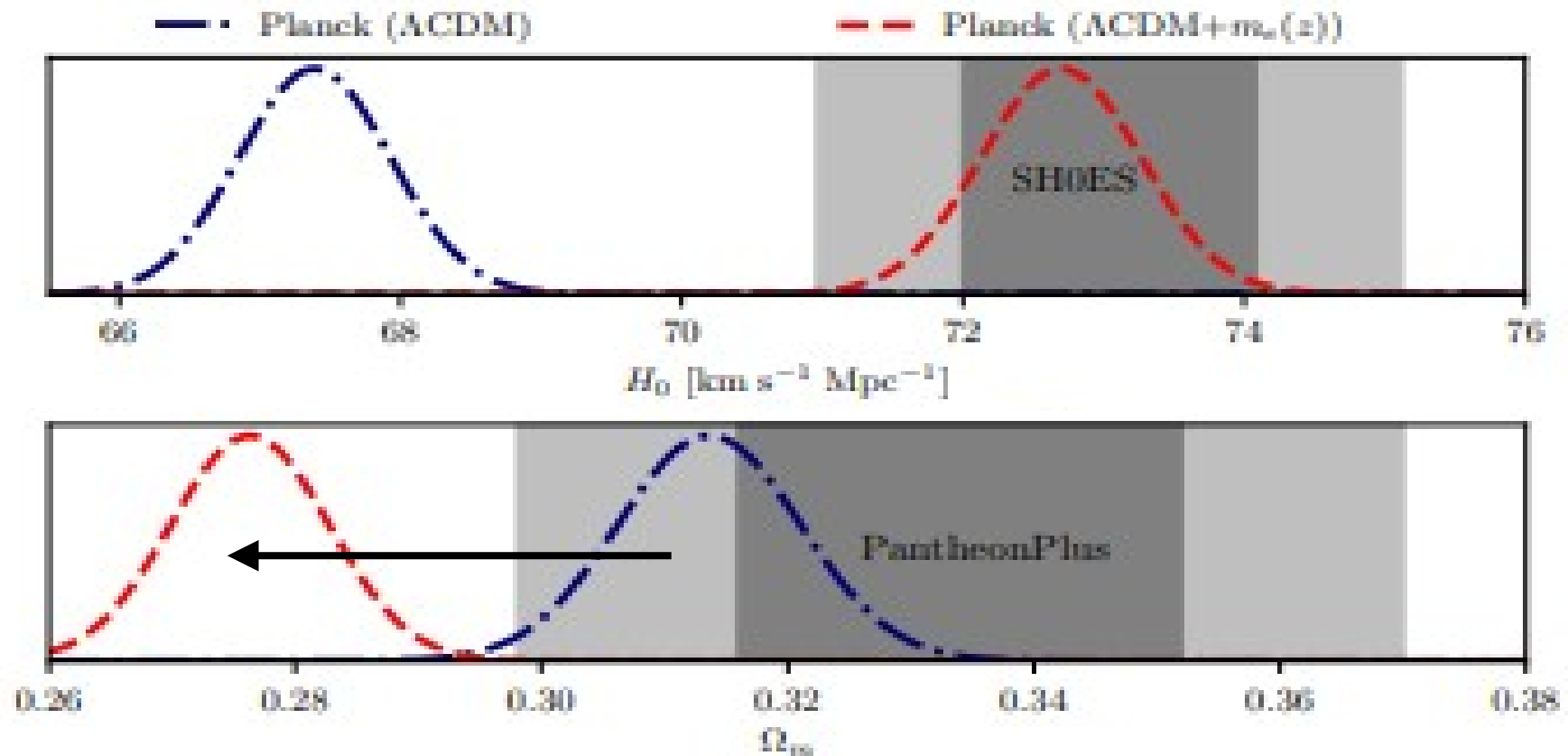
$$z_* \approx \underbrace{\frac{E_{\text{binding}}}{T_{\text{cmb}}}}_{\text{naive}} \cdot \underbrace{\frac{1}{40}}_{\text{Saha } (\eta_b)} \cdot \underbrace{0.75}_{\text{non-equilibrium}} \approx 1080$$











Lee+2212.04494

Supernova data does not like this type of models

By changing ℓ_{eq} we satisfy supernovae

→ Cost = play with other CMB parameters to balance first peaks (n_s , τ_{reio} , A_s , ...)

(not actually “liked”,
e.g. disappears if we get rid of SN or satisfy otherwise)



Supernova data does not like this type of models

Use curvature:

- Confuses supernovae data



Supernova data does not like this type of models

Use curvature:

- Confuses supernovae data
- Breaks angular diameter distance scaling



Supernova data does not like this type of models

THE NATURAL DIRECTION

Curvature allows
shallower slopes
between h and a_*

$$S_8 \propto h^{-0.86}$$

$$\Omega_m \propto h^{-1.7}$$

$$r_s \cdot h \propto h^{0.7}$$



Assumption:
 Λ CDM-like expansion
history at low- z

$$r_{\text{eq}} \propto a_*$$

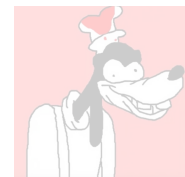
$$r_s \propto a_*$$

$$r_D \propto a_*$$

$$h \stackrel{!}{\propto} a_*^{-3.23}$$

$$R \rightarrow \omega_b \propto a_*^{-1}$$

$$\rho_m / \rho_r \rightarrow \omega_m \propto a_*^{-1}$$



Use curvature:

- Confuses supernovae data
- Breaks angular diameter distance scaling

→ Breaks $\Omega_m \propto h^{-1.7}$

Use curvature:

- Confuses supernovae data
 - Breaks angular diameter distance scaling
- Breaks $\Omega_m \propto h^{-1.7}$

Careful: Curvature well constrained by CMB + BAO + SN

Use curvature:

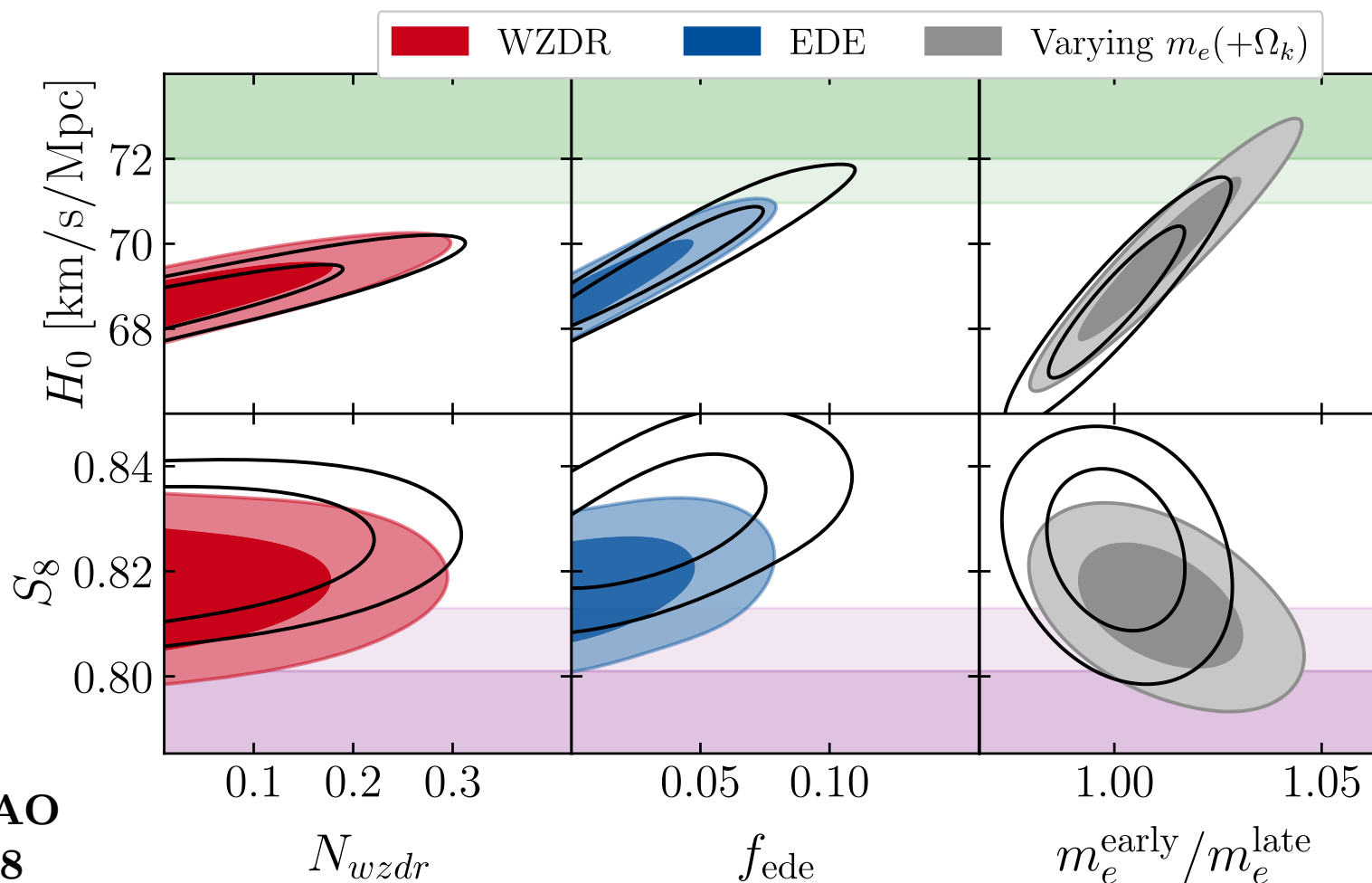
- Confuses supernovae data
- Breaks angular diameter distance scaling

→ Breaks $\Omega_m \propto h^{-1.7}$

Careful: Curvature well constrained by CMB + BAO + SN

Curvature is *not* the only extension doing this !

MODIFIED RECOMBINATION IS WEIRD



CMB+BAO
+SN + S8



IT'S NOT A VIABLE MODEL

IT'S NOT A VIABLE MODEL

- We are using it as:

m_e = modified recombination + σ_T scaling

- It's just the *simplest* implementation of this mechanism!

(That does not make it realistic, of course)

IT'S NOT A VIABLE MODEL

- Why not? $h \propto m_e^{3.23} \Rightarrow \Delta m_e / m_e \simeq 2\%$

IT'S NOT A VIABLE MODEL

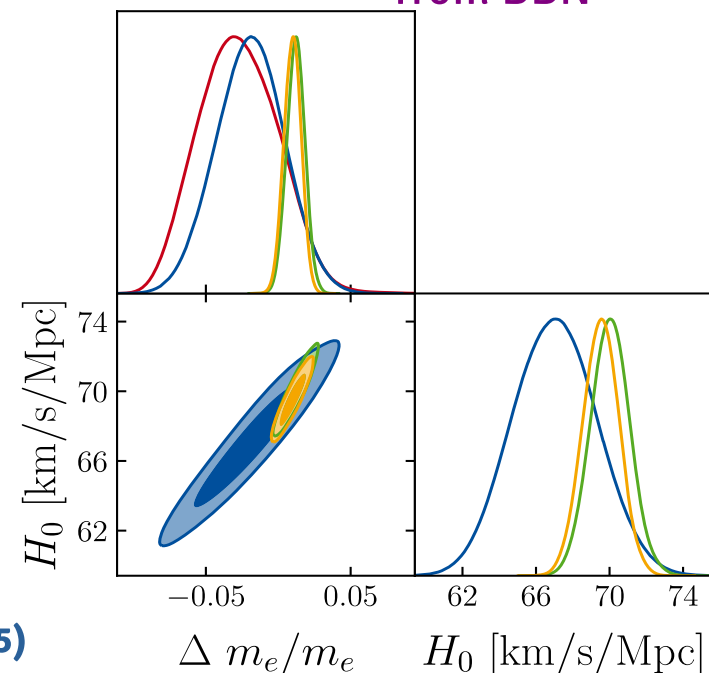
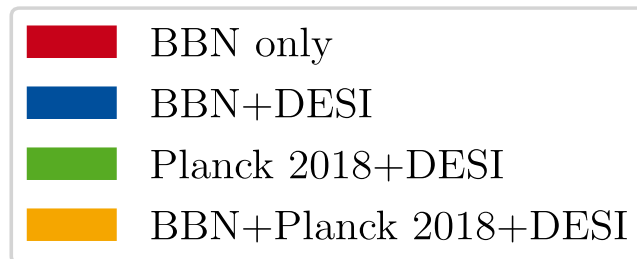
- Why not? $h \propto m_e^{3.23} \Rightarrow \Delta m_e / m_e \simeq 2\%$
 - BBN constraints (m_e influences weak rates, β decay)

IT'S NOT A VIABLE MODEL

- Why not? $h \propto m_e^{3.23} \Rightarrow \Delta m_e/m_e \simeq 2\%$
 - BBN constraints (m_e influences weak rates, β decay)

No big difference
from BBN

Constraint BBN
only is weak on m_e
~ 5%



BBN CONSTRAINTS

Garramone+(2602.05720)

$D + {}^4\text{He}$ (PDG)	NACRE II	0.982 ± 0.029
	PRIMAT	$1.015^{+0.023}_{-0.013}$
$D + {}^4\text{He}$ (LBT)	NACRE II	$0.986^{+0.013}_{-0.011}$
	PRIMAT	$0.994^{+0.017}_{-0.009}$

About **2% level** constraint on m_e , but value depends a bit on adopted He4 constraints
 → PDG would be fine with it

BBN CONSTRAINTS

Difference: also assumptions about G_F

→ V_{ud} Cabibbo angle and/or g_A nucleon axial coupling

→ Need a full UV-complete theory to compute QCD corrections to g_A from m_e variations

=> We cannot model-independently constrain m_e variations easily...

IT'S NOT A VIABLE MODEL

- **Why not?** $h \propto m_e^{3.23} \Rightarrow \Delta m_e / m_e \simeq 2\%$
 - BBN constraints (m_e influences weak rates, β decay)
 - Direct quasar constraints?
 - Not necessarily sensitive enough (too low z to catch it)
 - Requires a model of how m_e shifts back to standard value

$$\left(\frac{\Delta\mu}{\mu}\right)_{\text{Radio}} = -0.24 \pm 0.09 \text{ ppm}$$

Martins (1709.02923)

$$\left(\frac{\Delta\mu}{\mu}\right)_{\text{Optical}} = 2.9 \pm 1.9 \text{ ppm};$$

$$\mu \propto m_e^{-1}$$

$$m_e(z_q) = (1 + 0.24 \cdot 10^{-6}) m_e^{\text{late}}$$

IT'S NOT A VIABLE MODEL

- **Why not?** $h \propto m_e^{3.23} \Rightarrow \Delta m_e / m_e \simeq 2\%$
 - BBN constraints (m_e influences weak rates, β decay)
 - Direct quasar constraints?
 - Not necessarily sensitive enough (too low z to catch it)
 - Requires a model of how m_e shifts back to standard value
 - Might actually be beneficial...

IT'S NOT A VIABLE MODEL

- **Why not?** $h \propto m_e^{3.23} \Rightarrow \Delta m_e / m_e \simeq 2\%$
 - BBN constraints (m_e influences weak rates, β decay)
 - Direct quasar constraints? $\rightarrow$ Not really

IT'S NOT A VIABLE MODEL

- **Why not?** $h \propto m_e^{3.23} \Rightarrow \Delta m_e / m_e \simeq 2\%$
 - BBN constraints (m_e influences weak rates, β decay)
 - Direct quasar constraints? $\rightarrow$ Not really
 - Atomic clock constraints?
 - Again requires a model of how m_e settles back
 - Constraint strength **(2407.16845)**: $|(\Delta m_e / m_e)_{z_{\text{CMB}}}| \lesssim (2.3 \pm 1.6)\%$,
(Order of magnitude estimate!)
 - Weakened by even small curvature presence

IT'S NOT A VIABLE MODEL

- **Why not?** $h \propto m_e^{3.23} \Rightarrow \Delta m_e / m_e \simeq 2\%$
 - BBN constraints (m_e influences weak rates, β decay)
 - Direct quasar constraints? $\rightarrow$ Not really
 - Atomic clock constraints? $\rightarrow$ Very barely no

IT'S NOT A VIABLE MODEL

- **Why not?** $h \propto m_e^{3.23} \Rightarrow \Delta m_e / m_e \simeq 2\%$
 - BBN constraints (m_e influences weak rates, β decay)
 - Direct quasar constraints? $\rightarrow$ Not really
 - Atomic clock constraints? $\rightarrow$ Very barely no
 - Fifth force constraints?

IT'S NOT A VIABLE MODEL

- **Why not?** $h \propto m_e^{3.23} \Rightarrow \Delta m_e / m_e \simeq 2\%$
 - BBN constraints (m_e influences weak rates, β decay)
 - Direct quasar constraints? $\rightarrow$ Not really
 - Atomic clock constraints? $\rightarrow$ Very barely no
 - Fifth force constraints?
 - Weiner+ argues in [2502.04432](#) that no (quadratic coupling)
 - Others argue that still yes due to e.g. loop corrections
 - Above my pay grade to judge

IT'S NOT A VIABLE MODEL

- **Why not?** $h \propto m_e^{3.23} \Rightarrow \Delta m_e / m_e \simeq 2\%$
 - BBN constraints (m_e influences weak rates, β decay)
 - Direct quasar constraints? $\rightarrow$ Not really
 - Atomic clock constraints? $\rightarrow$ Very barely no
 - Fifth force constraints? $\rightarrow$ Maybe?

IT'S NOT A VIABLE MODEL

- **Why not?** $h \propto m_e^{3.23} \Rightarrow \Delta m_e / m_e \simeq 2\%$
 - BBN constraints (m_e influences weak rates, β decay)
 - Direct quasar constraints? $\rightarrow$ Not really
 - Atomic clock constraints? $\rightarrow$ Very barely no
 - Fifth force constraints? $\rightarrow$ Maybe?
 - Cannot be realized?
 - Appears possible, multiple options even
 - Yukawa (Randall-Sundrum), Higgs vacuum change
 - Maybe even GUT/extra dimensions, Symmetron (2201.03127)

IT'S NOT A VIABLE MODEL

- **Why not?** $h \propto m_e^{3.23} \Rightarrow \Delta m_e / m_e \simeq 2\%$
 - BBN constraints (m_e influences weak rates, β decay)
 - Direct quasar constraints? $\rightarrow$ Not really
 - Atomic clock constraints? $\rightarrow$ Very barely no
 - Fifth force constraints? $\rightarrow$ Maybe?
 - Cannot be realized? $\rightarrow$ Probably can be

IT'S NOT A VIABLE MODEL

- So far no definite conclusion reached on UV theory
- However, importantly, we are using it as:
 m_e = modified recombination + σ_T scaling
- It's just the *simplest* implementation of this mechanism!

HOW TO DIFFERENTIATE IT FROM EDE

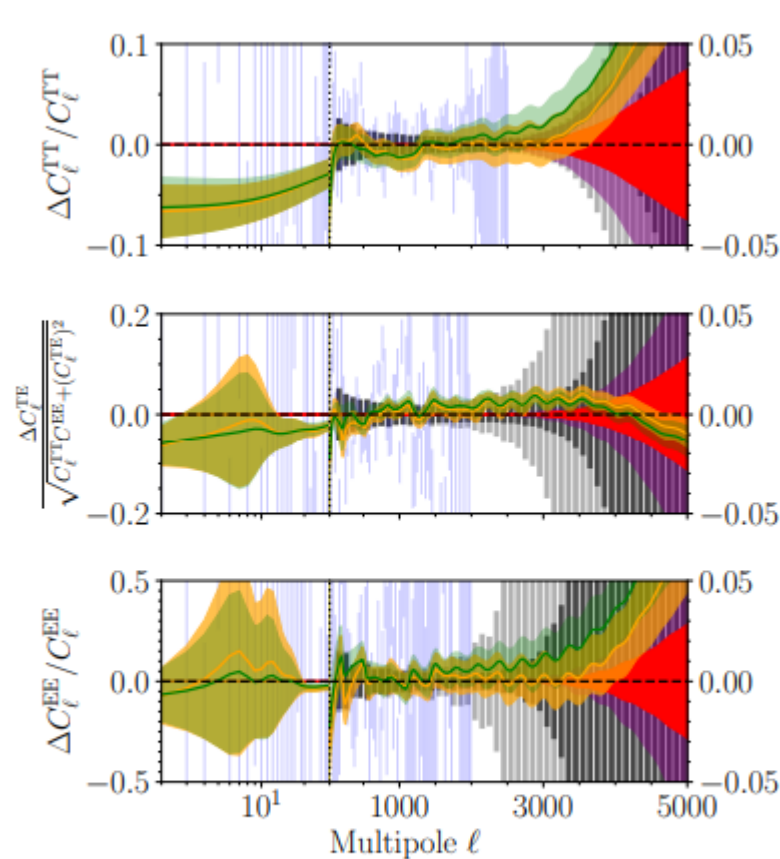


Figure 2. Same as figure 1 but for EDE (orange) fluid-like EDE model (green).

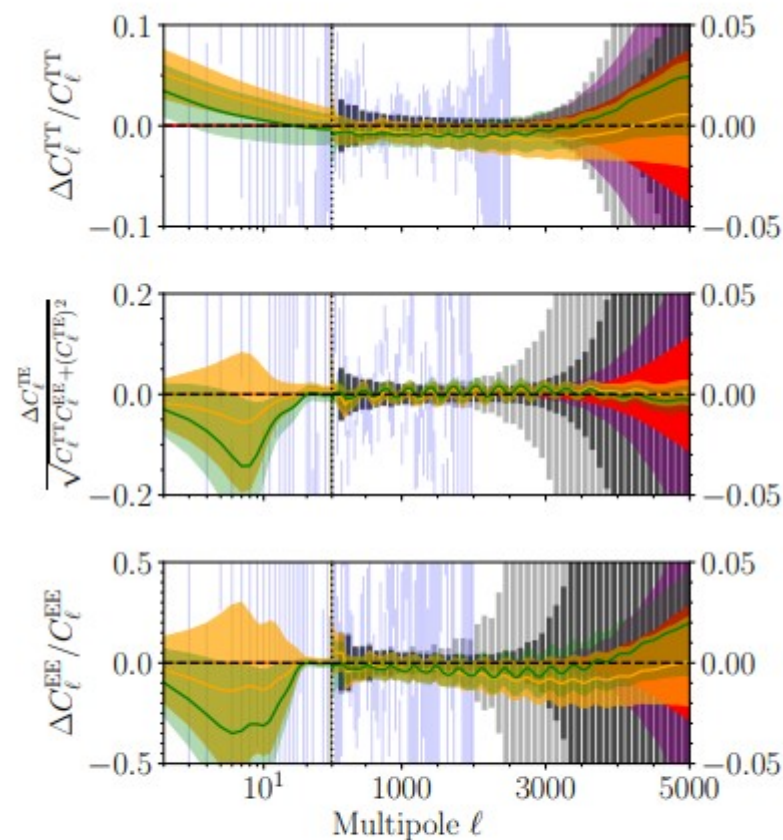
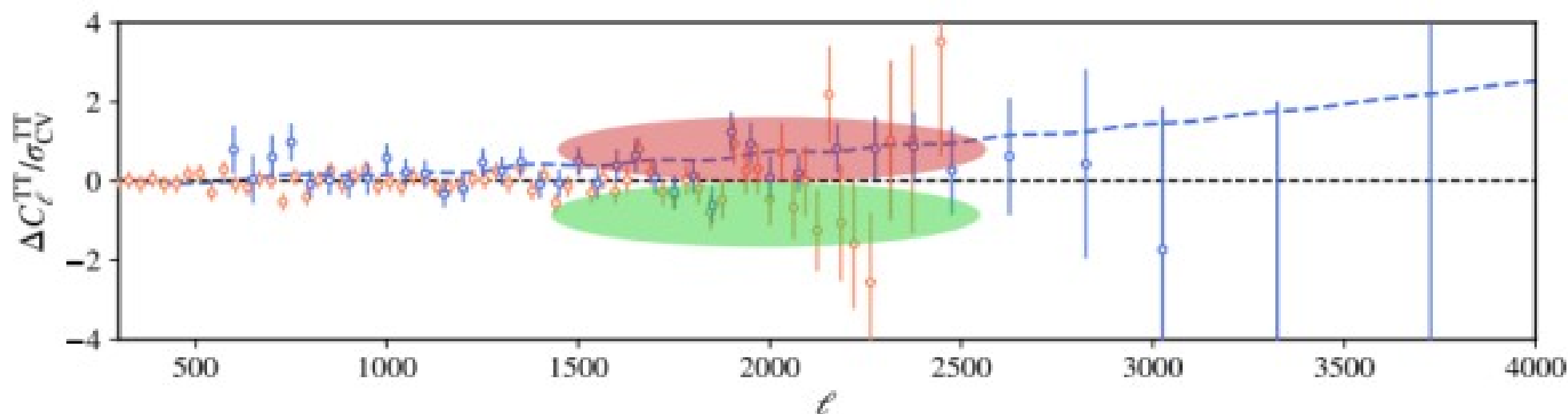


Figure 4. As in figure 1, but for a model with a time-variation of the electron mass. We show the predictions for the baseline model in orange and with additional curvature allowed in green.

HOW TO DIFFERENTIATE IT FROM EDE

See also Talk by Rodrigo Calderon



ACT data likes EDE-like upturn

→ ACT data does not like me

Further confirmation with SO

SUMMARY



SUMMARY

- It's weird but exciting (toy model!)
- Natural direction:
 - $\Omega_m \propto h^{-1.7}$ $r_s \cdot h \propto h^{0.7}$ $S_8 \propto h^{-0.86}$
 - Liked by BAO data, S_8 data, neutrinos
- SN data does not like direction
 - Increasing ℓ_{eq} helps (playing with other parameters)
 - Using curvature helps
- **ACT** data doesn't like it, **BBN** maybe bad, **quasar** no constraint, **atomic clock** no constraint, **fifth force** maybe
- Model motivation hard (but not impossible → Higgs, Yukawa)

BACKUP SLIDES

THE NAIL IN THE COFFIN

- Maybe the model can be ‘revived’ ?
- **Vacher & Schöneberg (2403.02256)** suggests: Most likely not

Generic bound $\Delta\alpha/\alpha$ at $5\cdot 10^{-4}$ **



** : Applying to non-fine-tuned single scalar fields

THE NAIL IN THE COFFIN

- → To be re-cycled for m_e constraints (!)

THE NAIL IN THE COFFIN

- Idea: Use scalar field kinetics

$$\frac{d\dot{\phi}}{d \ln a} + 3\dot{\phi} = -\frac{1}{H} \frac{dV}{d\phi}$$

THE NAIL IN THE COFFIN

- Idea: Use scalar field kinetics

$$\frac{d\dot{\phi}}{d \ln a} + 3\dot{\phi} = -\frac{1}{H} \frac{dV}{d\phi}$$

$$\dot{\phi} = Ca^{-3} - a^{-3} \int \frac{a^3}{H} \frac{dV}{d\phi} d \ln a$$

THE NAIL IN THE COFFIN

- Idea: Use scalar field kinetics

$$\frac{d\dot{\phi}}{d \ln a} + 3\dot{\phi} = -\frac{1}{H} \frac{dV}{d\phi}$$

$$\dot{\phi} = \underbrace{Ca^{-3}}_{\text{Cannot slow down faster!}} - \underbrace{a^{-3} \int \frac{a^3}{H} \frac{dV}{d\phi} d \ln a}_{\text{Let's deal with this later!}}$$

THE NAIL IN THE COFFIN

- Idea: Taylor-expand the coupling $\Delta\alpha/\alpha = -\zeta\Delta\phi$

$$\Delta\alpha/\alpha = -\zeta\Delta\phi = -\zeta \int \frac{d\phi}{d \ln a} d \ln a$$

THE NAIL IN THE COFFIN

- Idea: Taylor-expand the coupling $\Delta\alpha/\alpha = -\zeta\Delta\phi$

$$\Delta\alpha/\alpha = -\zeta\Delta\phi = -\zeta \int \frac{d\phi}{d \ln a} d \ln a$$

$$\left. \frac{d \ln \alpha}{d \ln a} \right|_{z=0} = -\zeta \left. \frac{d\phi}{d \ln a} \right|_{z=0}$$

THE NAIL IN THE COFFIN

- Idea: Taylor-expand the coupling $\Delta\alpha/\alpha = -\zeta\Delta\phi$

$$\Delta\alpha/\alpha = -\zeta\Delta\phi = -\zeta \int \frac{d\phi}{d \ln a} d \ln a \sim 10^{-2}$$

$$\left. \frac{d \ln \alpha}{d \ln a} \right|_{z=0} = -\zeta \left. \frac{d\phi}{d \ln a} \right|_{z=0} \sim 10^{-8}$$

THE NAIL IN THE COFFIN

- Idea: Taylor-expand the coupling $\Delta\alpha/\alpha = -\zeta\Delta\phi$

$$\Delta\alpha/\alpha = -\zeta\Delta\phi = -\zeta \int \frac{d\phi}{d \ln a} d \ln a \sim 10^{-2}$$

$$\left. \frac{d \ln \alpha}{d \ln a} \right|_{z=0} = -\zeta \left. \frac{d\phi}{d \ln a} \right|_{z=0} \sim 10^{-8}$$

$$\frac{d\phi}{d \ln a} = \frac{\dot{\phi}}{H} \propto \frac{a^{-3}}{H}$$

THE NAIL IN THE COFFIN

- Idea: Taylor-expand the coupling $\Delta\alpha/\alpha = -\zeta\Delta\phi$

$$\Delta\alpha/\alpha = -\zeta\Delta\phi = -\zeta \int \frac{d\phi}{d \ln a} d \ln a \sim 10^{-2}$$

$$\left. \frac{d \ln \alpha}{d \ln a} \right|_{z=0} = -\zeta \left. \frac{d\phi}{d \ln a} \right|_{z=0} \sim 10^{-8}$$

$$\frac{d\phi}{d \ln a} = \frac{\dot{\phi}}{H} \propto \frac{a^{-3}}{H}$$

$$H \propto a^{-3/2} \Rightarrow \frac{d\phi}{d \ln a} \propto a^{-3/2}$$

THE NAIL IN THE COFFIN

- Idea: Taylor-expand the coupling $\Delta\alpha/\alpha = -\zeta\Delta\phi$

$$\Delta\alpha/\alpha = -\zeta\Delta\phi = -\zeta \int \frac{d\phi}{d \ln a} d \ln a \sim 10^{-2}$$

$$\left. \frac{d \ln \alpha}{d \ln a} \right|_{z=0} = -\zeta \left. \frac{d\phi}{d \ln a} \right|_{z=0} \sim 10^{-8}$$

$$\frac{d\phi}{d \ln a} = \frac{\dot{\phi}}{H} \propto \frac{a^{-3}}{H}$$

$$H \propto a^{-3/2} \Rightarrow \frac{d\phi}{d \ln a} \propto a^{-3/2}$$

3 decades of time
with a speed 3/2

→ $3 \cdot 3/2 = 4.5$ **decades** possible

Impossible to get 6 decades of deceleration

THE NAIL IN THE COFFIN

- Idea: Taylor-expand the coupling $\Delta\alpha/\alpha = -\zeta\Delta\phi$

$$\Delta\alpha/\alpha = -\zeta\Delta\phi = -\zeta \int \frac{d\phi}{d \ln a} d \ln a \sim 10^{-2}$$

$$\left. \frac{d \ln \alpha}{d \ln a} \right|_{z=0} = -\zeta \left. \frac{d\phi}{d \ln a} \right|_{z=0} \sim 10^{-8}$$

$$\frac{d\phi}{d \ln a} = \frac{\dot{\phi}}{H} \propto \frac{a^{-3}}{H}$$

$$\Delta\alpha/\alpha(z_*) < 5 \cdot 10^4 \cdot \left. \frac{d \ln \alpha}{d \ln a} \right|_{z=0}$$

$$= 10^{4.7} \text{ Primarily MD}$$

THE NAIL IN THE COFFIN

- Idea: Taylor-expand the coupling $\Delta\alpha/\alpha = -\zeta\Delta\phi$

$$\Delta\alpha/\alpha = -\zeta\Delta\phi = -\zeta \int \frac{d\phi}{d \ln a} d \ln a \sim 10^{-2}$$

$$\left. \frac{d \ln \alpha}{d \ln a} \right|_{z=0} = -\zeta \left. \frac{d\phi}{d \ln a} \right|_{z=0} \sim 10^{-8}$$

$$\frac{d\phi}{d \ln a} = \frac{\dot{\phi}}{H} \propto \frac{a^{-3}}{H}$$

$$\Delta\alpha/\alpha(z_*) < 5 \cdot 10^4 \cdot \left. \frac{d \ln \alpha}{d \ln a} \right|_{z=0}$$

THE NAIL IN THE COFFIN

- Idea: Taylor-expand the coupling $\Delta\alpha/\alpha = -\zeta\Delta\phi$

$$\Delta\alpha/\alpha = -\zeta\Delta\phi = -\zeta \int \frac{d\phi}{d \ln a} d \ln a \sim 10^{-2}$$

$$\left. \frac{d \ln \alpha}{d \ln a} \right|_{z=0} = -\zeta \left. \frac{d\phi}{d \ln a} \right|_{z=0} \sim 10^{-8}$$

$$\frac{d\phi}{d \ln a} = \frac{\dot{\phi}}{H} \propto \frac{a^{-3}}{H}$$

$$\Delta\alpha/\alpha(z_*) < 5 \cdot 10^{-4}$$

THE NAIL IN THE COFFIN

- Idea: Taylor-expand the coupling $\Delta\alpha/\alpha = -\zeta\Delta\phi$

$$\Delta\alpha/\alpha = -\zeta\Delta\phi = -\zeta \int \frac{d\phi}{d \ln a} d \ln a \sim 10^{-2}$$

$$\left. \frac{d \ln \alpha}{d \ln a} \right|_{z=0} = -\zeta \left. \frac{d\phi}{d \ln a} \right|_{z=0} \sim 10^{-8}$$

$$\frac{d\phi}{d \ln a} = \frac{\dot{\phi}}{H} \propto \frac{a^{-3}}{H}$$

$$\Delta\alpha/\alpha(z_*) < 5 \cdot 10^{-4} \quad \text{Stronger than CMB!}$$

THE NAIL IN THE COFFIN

- Idea: Use scalar field kinetics

$$\frac{d\dot{\phi}}{d \ln a} + 3\dot{\phi} = -\frac{1}{H} \frac{dV}{d\phi}$$

$$\dot{\phi} = \underbrace{Ca^{-3}}_{\text{Cannot slow down faster!}} - a^{-3} \int \frac{a^3}{H} \frac{dV}{d\phi} d \ln a$$

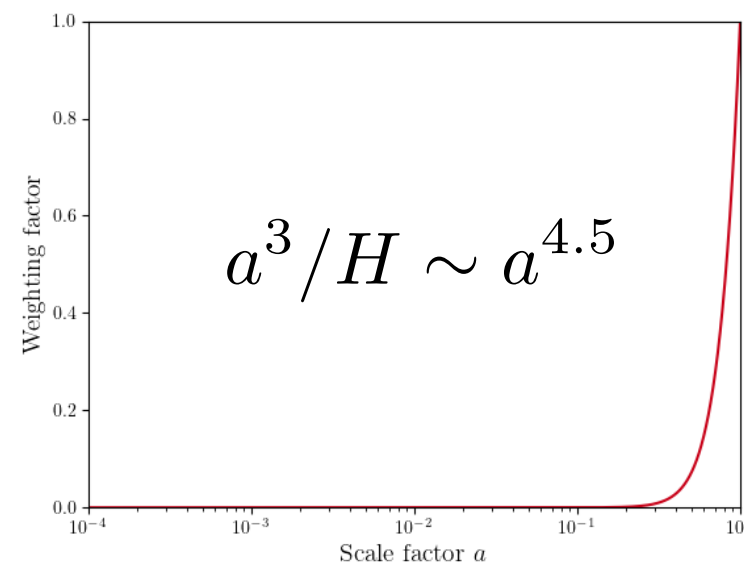
Cannot slow
down faster!

Let's deal with this
later!

THE NAIL IN THE COFFIN

- Idea: Use scalar field kinetics

$$\frac{d\dot{\phi}}{d \ln a} + 3\dot{\phi} = -\frac{1}{H} \frac{dV}{d\phi}$$



$$\dot{\phi} = \underbrace{Ca^{-3}}_{\text{Cannot slow down faster!}} - a^{-3} \int \frac{a^3}{H} \frac{dV}{d\phi} d \ln a$$

Cannot slow
down faster!

Let's deal with this
later!

THE NAIL IN THE COFFIN

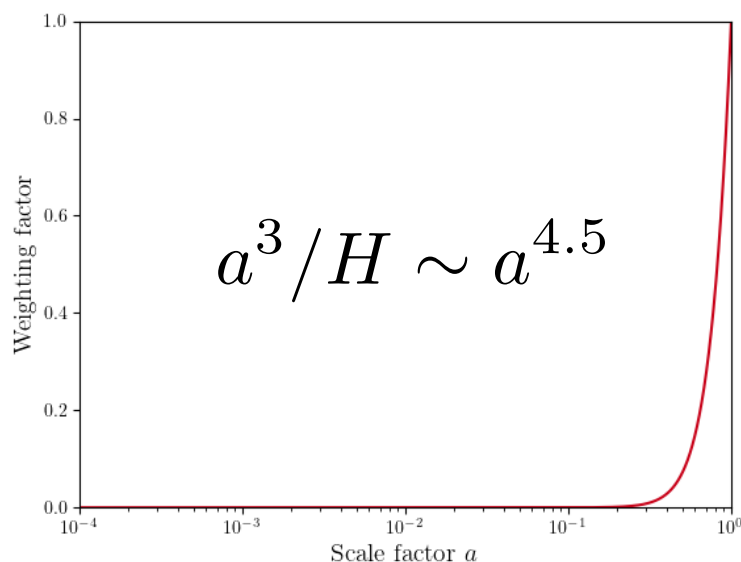
- Idea: Use scalar field kinetics

$$\frac{d\dot{\phi}}{d \ln a} + 3\dot{\phi} = -\frac{1}{H} \frac{dV}{d\phi}$$

$$\dot{\phi} = \underbrace{Ca^{-3}}_{\text{Cannot slow down faster!}} - a^{-3} \int \frac{a^3}{H} \frac{dV}{d\phi} d \ln a$$

Cannot slow
down faster!

Let's deal with this
later!



$$a \gtrsim 0.2$$

THE NAIL IN THE COFFIN

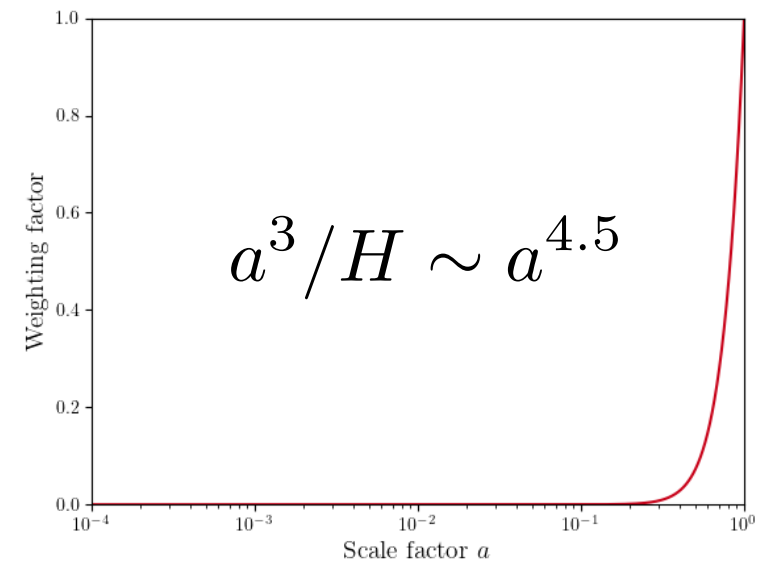
- Idea: Use scalar field kinetics

$$\frac{d\dot{\phi}}{d \ln a} + 3\dot{\phi} = -\frac{1}{H} \frac{dV}{d\phi}$$

$$\dot{\phi} = \underbrace{Ca^{-3}}_{\text{Cannot slow down faster!}} - a^{-3} \int \frac{a^3}{H} \frac{dV}{d\phi} d \ln a$$

Cannot slow
down faster!

Requires extreme finetuning!
(only relevant towards $a \rightarrow 1$)



$$a \gtrsim 0.2$$

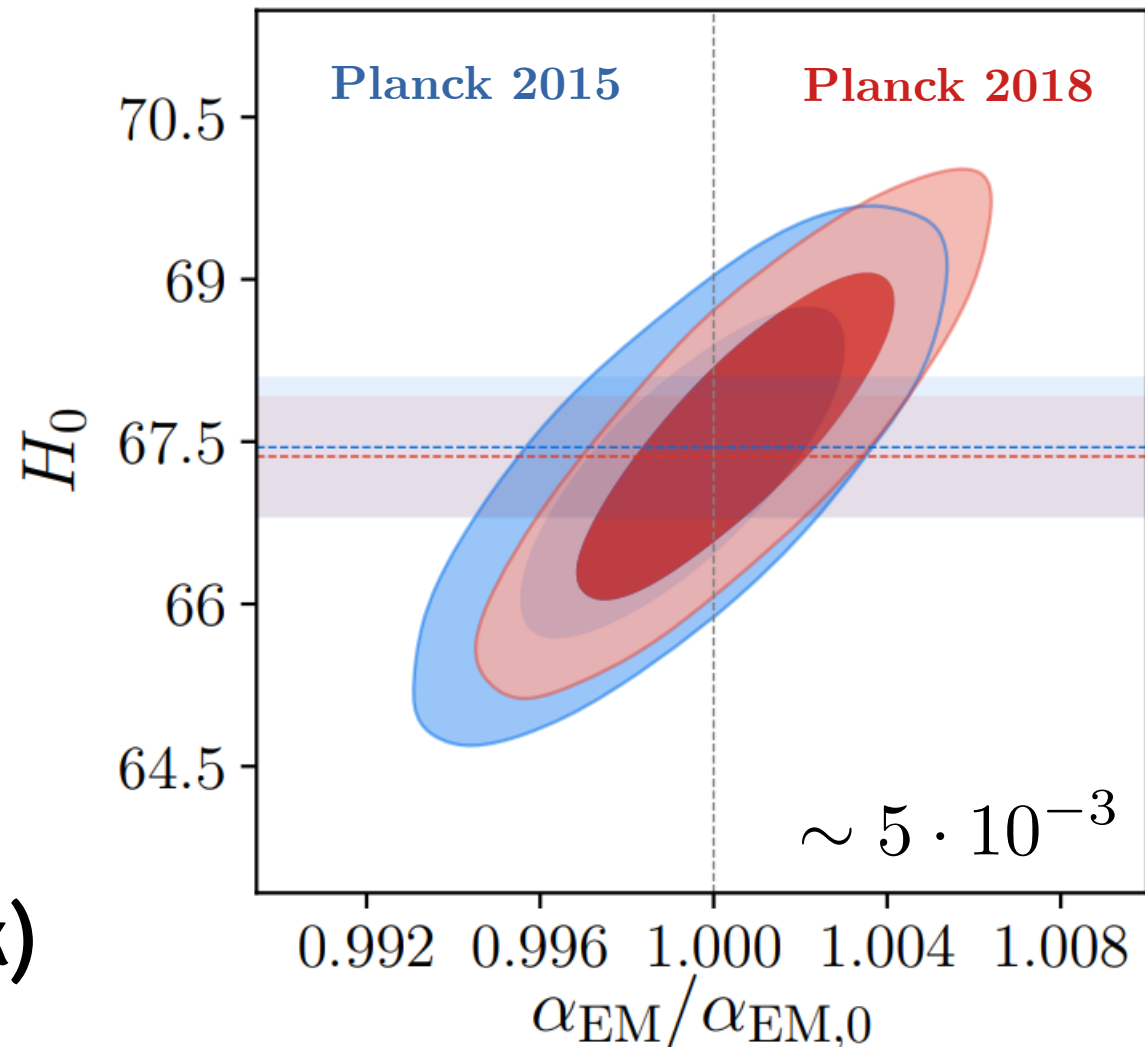
THE PROBLEM WITH ALPHA

Hart & Chluba (1912.03986)

- Not a good solution!



- Why?
 - Silk damping
(let's come back)



GETTING RID OF IT



- Single field kinetic constraint?

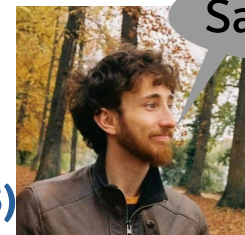
GETTING RID OF IT

- Single field kinetic constraint?



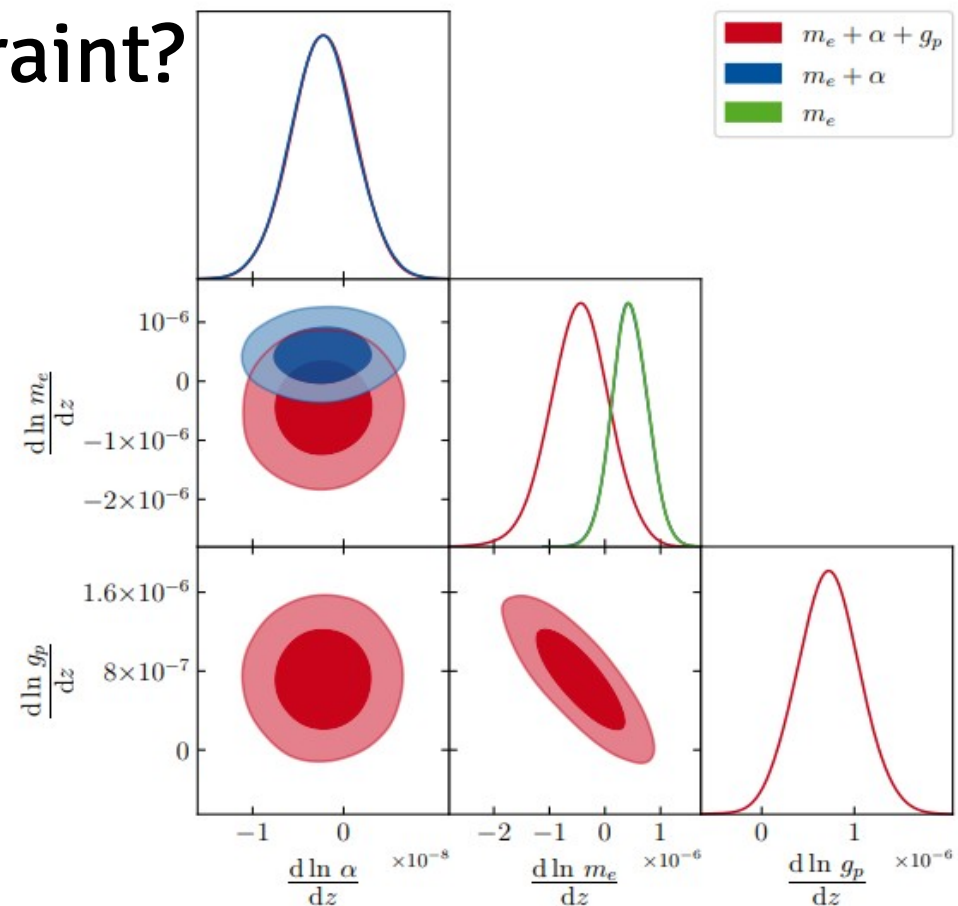
GETTING RID OF IT

Schöneberg & Vacher (2407.16845)



Sadly no

- Single field kinetic constraint?



GETTING RID OF IT

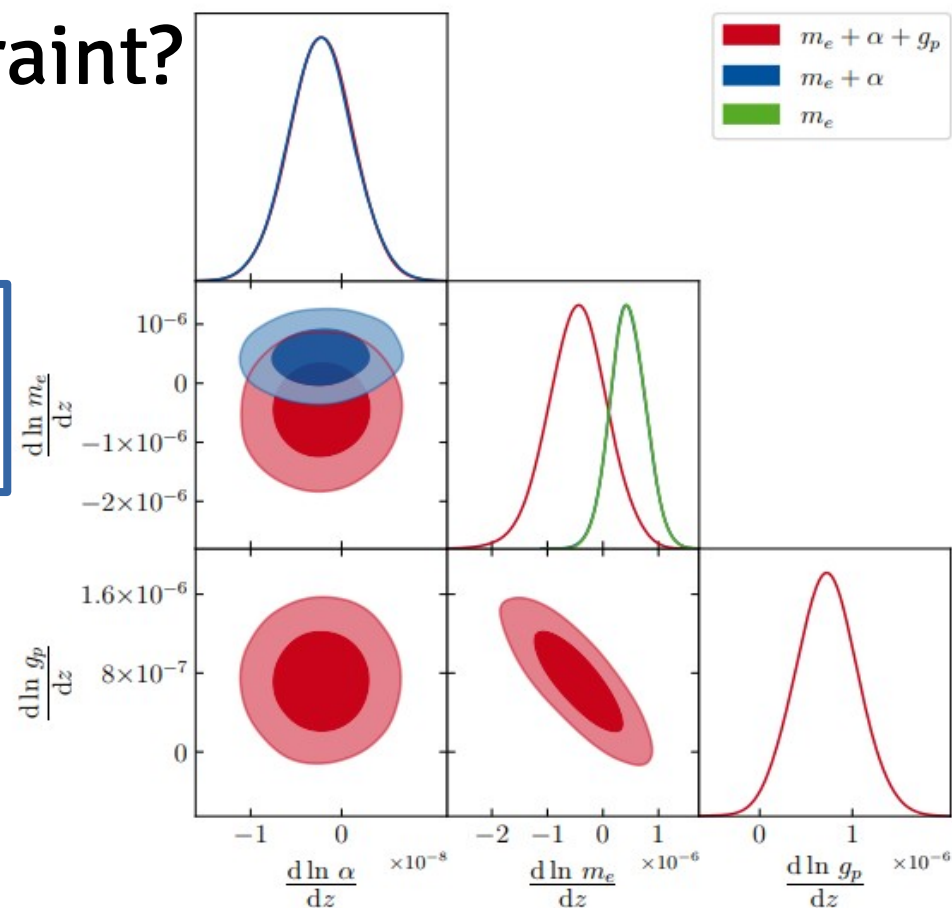
Schöneberg & Vacher (2407.16845)



Sadly no

- Single field kinetic constraint?
- Less sensitivity to m_e

$$\frac{d \ln \alpha}{dz} \sim 10^{-8} \quad \text{vs} \quad \frac{d \ln m_e}{dz} \sim 10^{-6}$$



GETTING RID OF IT

Schöneberg & Vacher (2407.16845)



Sadly no

- Single field kinetic constraint?
- Less sensitivity to m_e

$$\frac{d \ln \alpha}{dz} \sim 10^{-8} \quad \text{vs} \quad \frac{d \ln m_e}{dz} \sim 10^{-6}$$

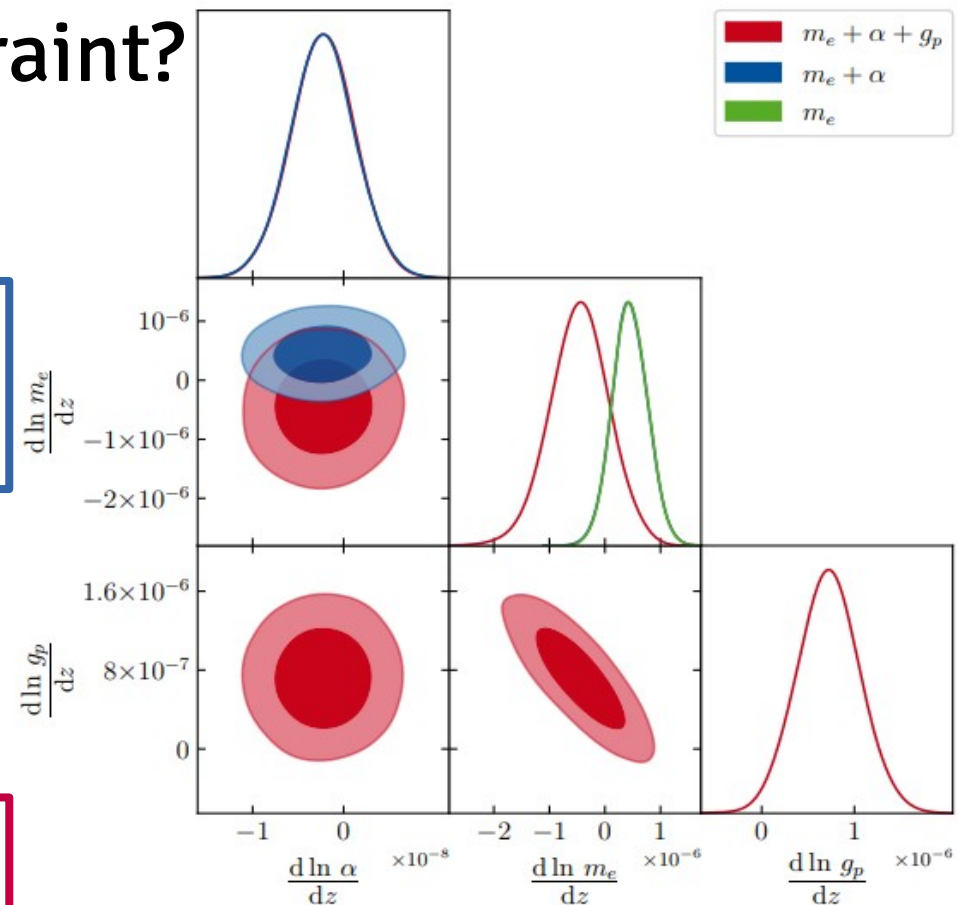
Two EM transitions $\rightarrow \alpha$

EM and hyperfine transitions $\rightarrow \alpha$ and μ
 $\mu = m_p/m_e$



$$5 \cdot 10^{-4} \quad \text{vs} \quad 5 \cdot 10^{-2}$$

$$\Delta\alpha/\alpha \quad \Delta m_e/m_e$$

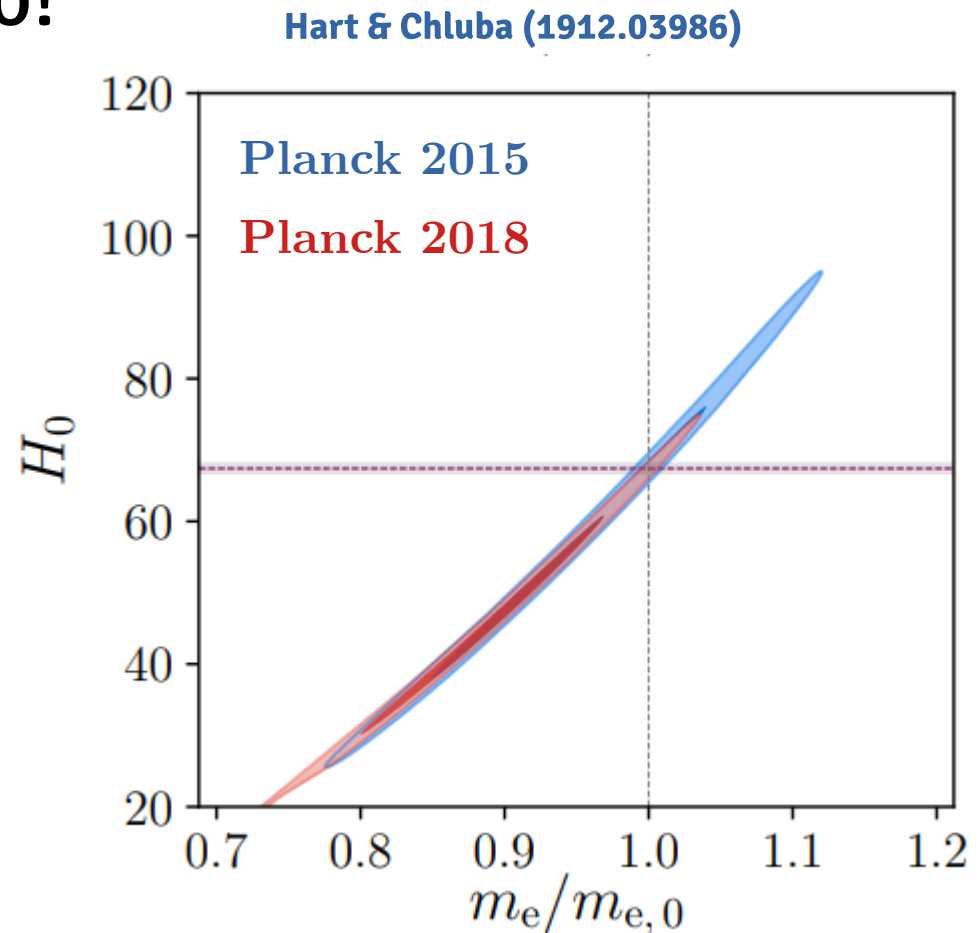


THE LITTLE SOLUTION THAT COULD

- Same problem for m_e ?

THE LITTLE SOLUTION THAT COULD

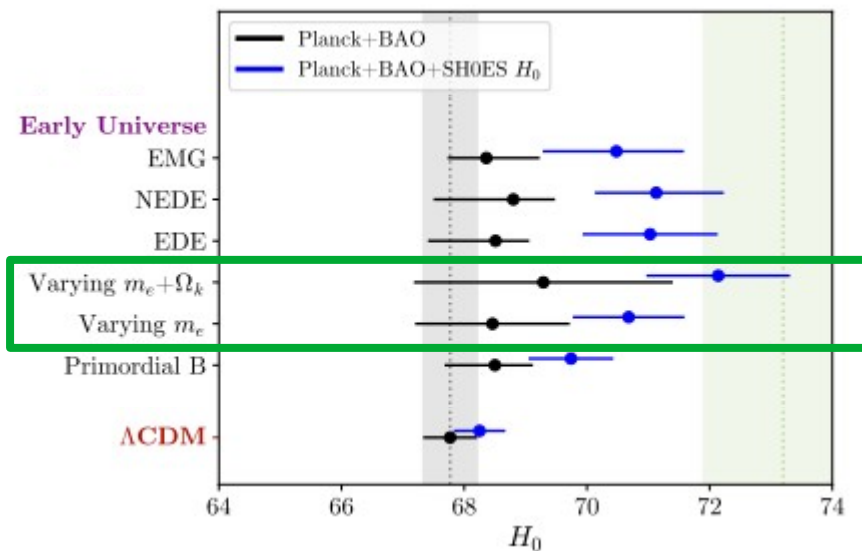
- Same problem for m_e ? No!



THE LITTLE SOLUTION THAT COULD

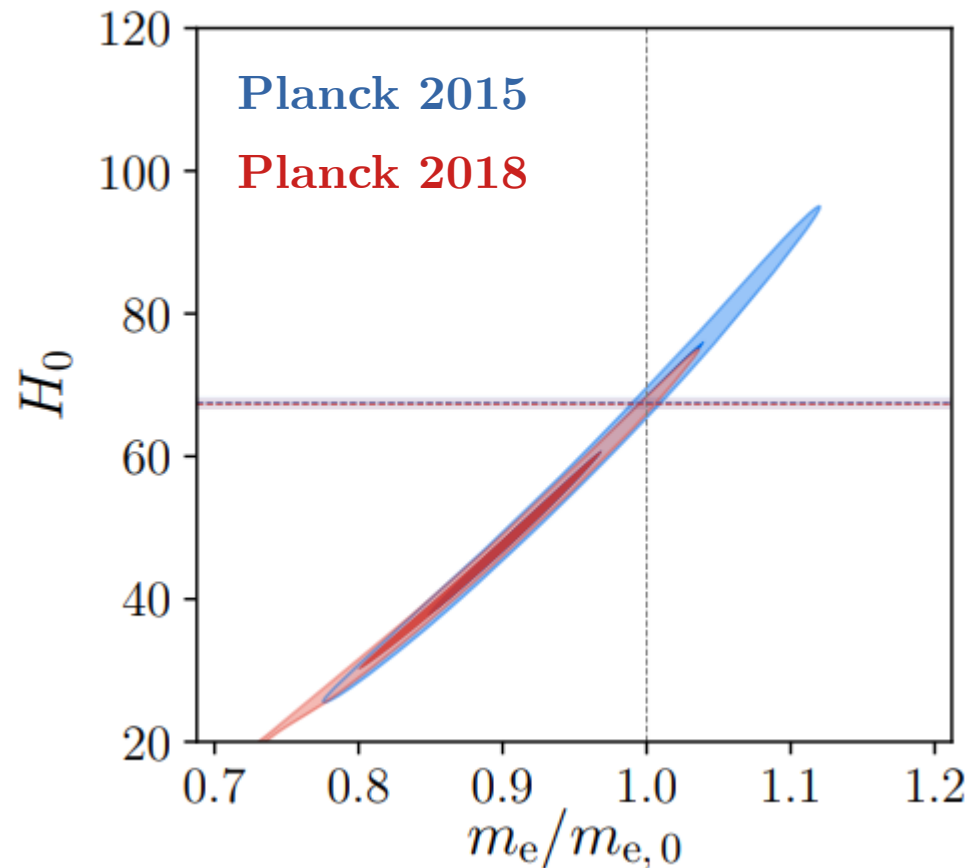
- Same problem for m_e ? No!

Schöneberg+ (2107.10291)



Gold medal in H_0 olympics?!

Hart & Chluba (1912.03986)

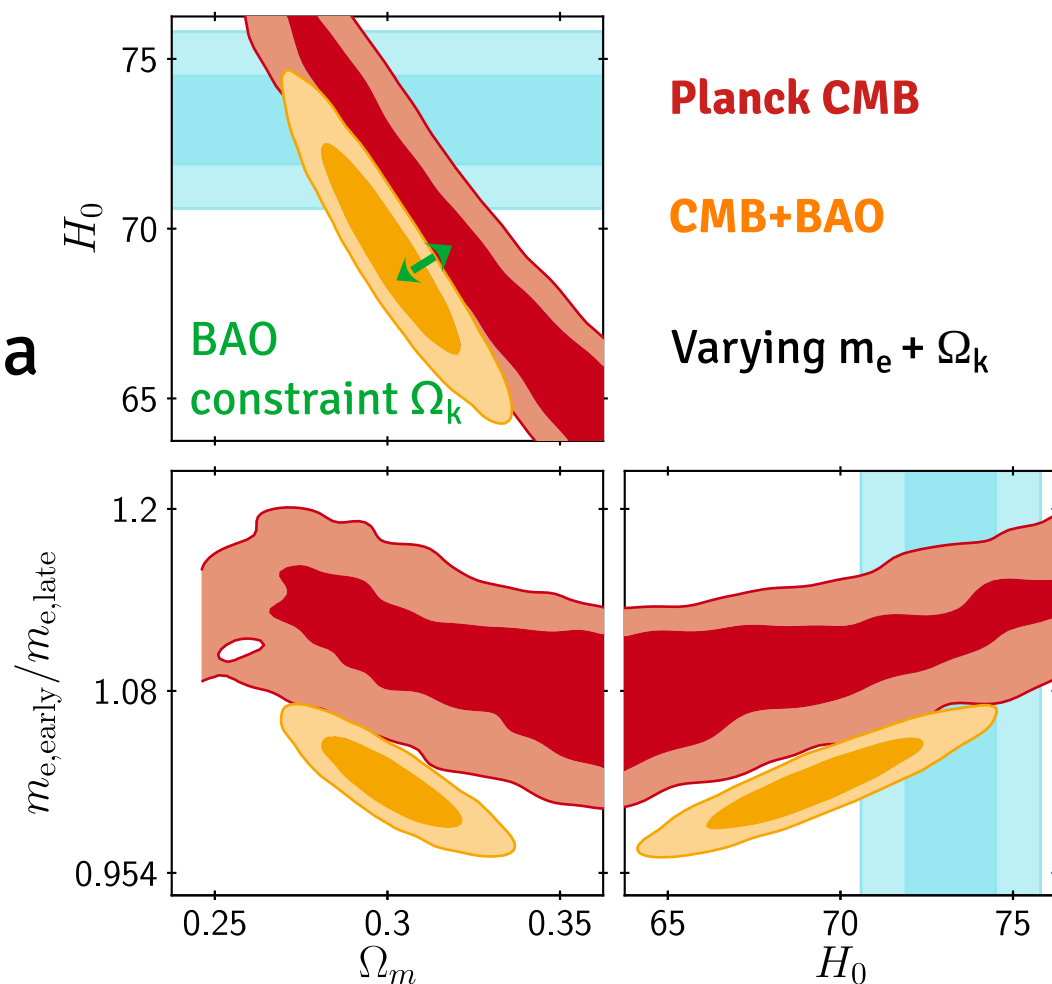


THE LITTLE SOLUTION THAT COULD

- Double trouble:

- Ω_k breaks $h \propto a_*^{-3.23}$
- Ω_k ‘confuses’ BAO/SN data

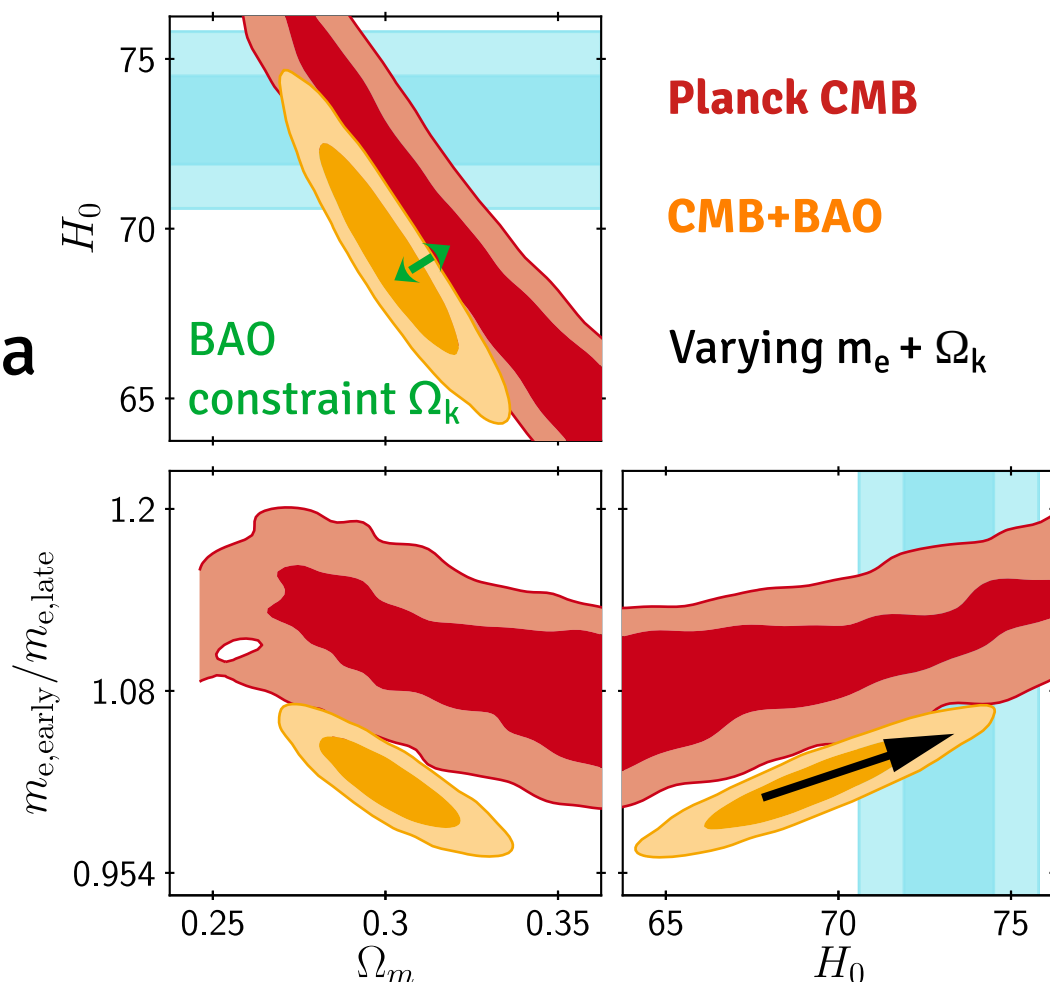
Schöneberg+ (2107.10291)



THE LITTLE SOLUTION THAT COULD

- Double trouble:
 - Ω_k breaks $h \propto a_*^{-3.23}$
 - Ω_k ‘confuses’ BAO/SN data
- → Works ‘well enough’ for current constraints

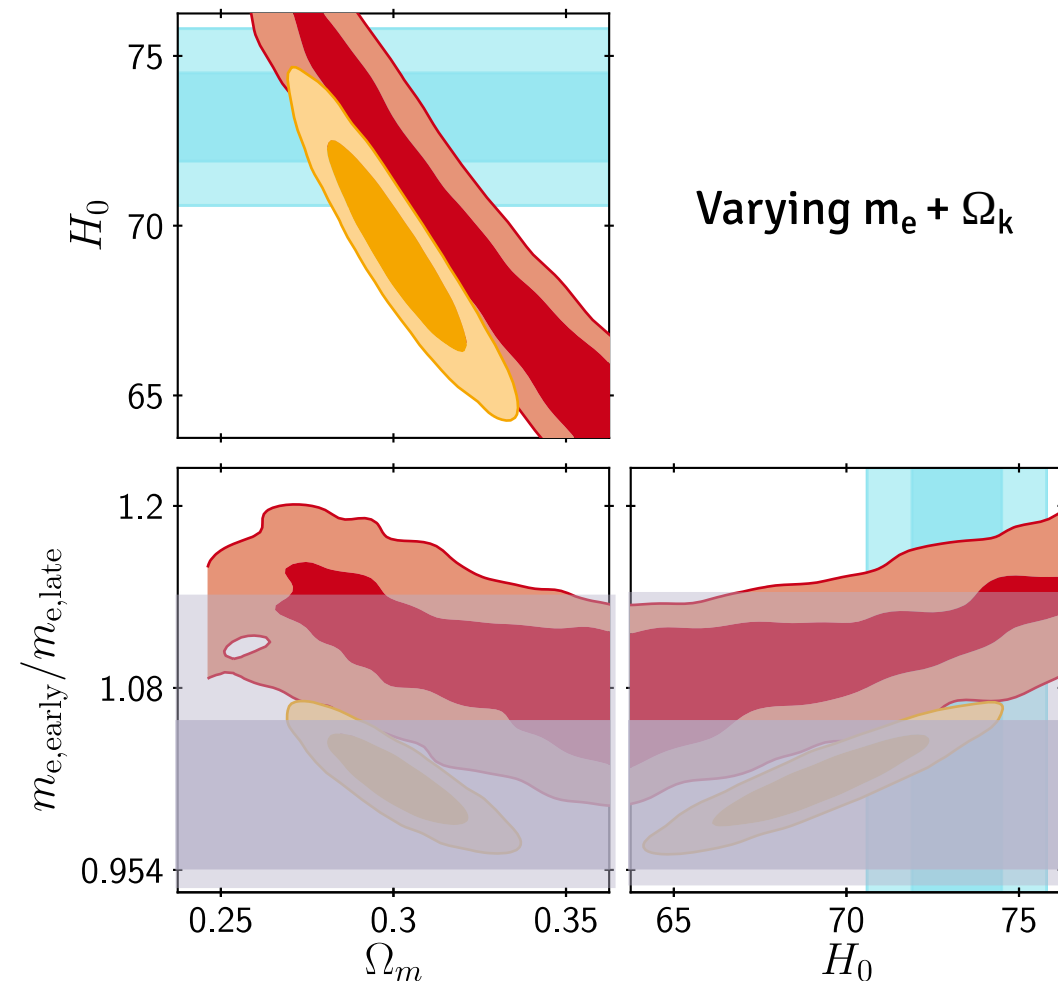
Schöneberg+ (2107.10291)



THE LITTLE SOLUTION THAT COULD

- $5 \cdot 10^{-2}$ is not good enough

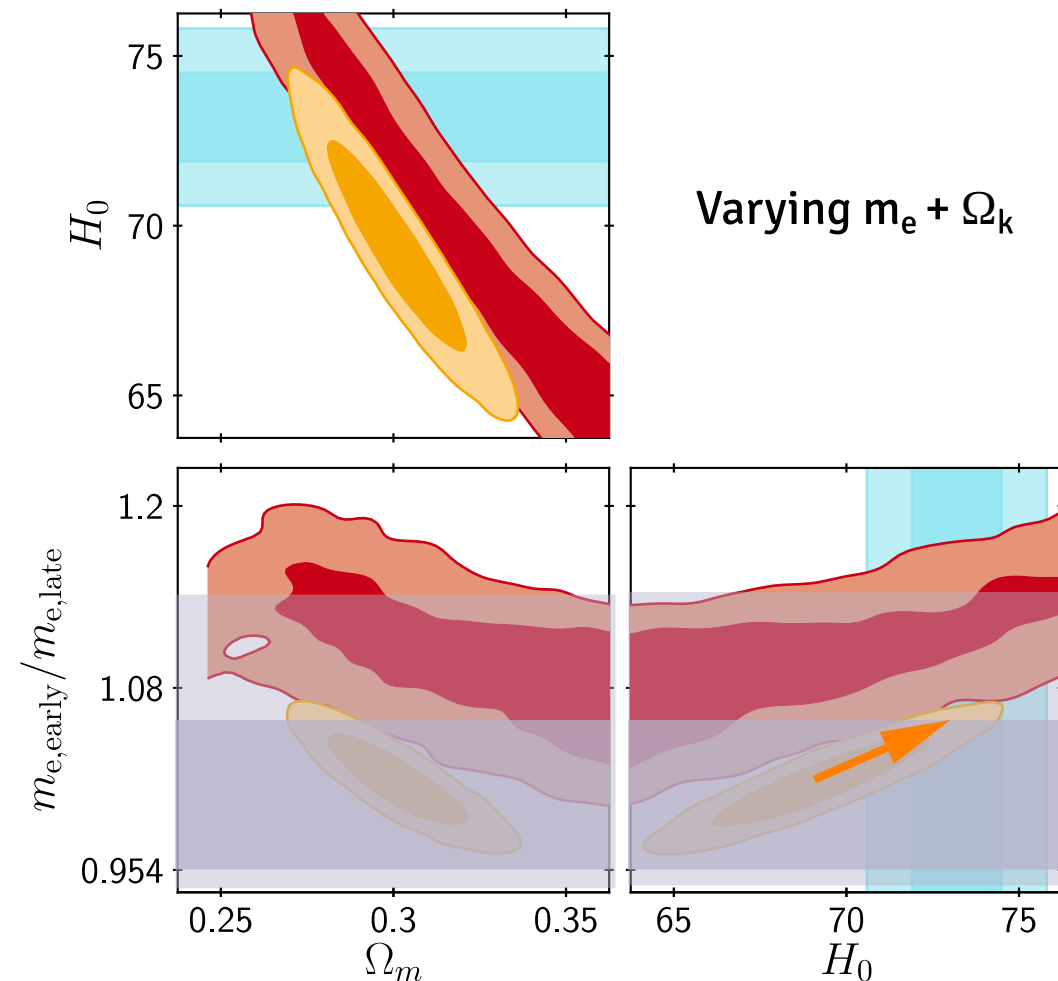
Schöneberg+ (2107.10291)



THE LITTLE SOLUTION THAT COULD

- $5 \cdot 10^{-2}$ is not good enough

Schöneberg+ (2107.10291)

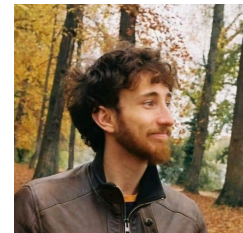


GETTING RID OF IT



- Single field kinetic constraint? → No

GETTING RID OF IT



- Single field kinetic constraint? → No
- New DESI data?

GETTING RID OF IT



- Single field kinetic constraint? → No
- New DESI data? → Even favored!

GETTING RID OF IT

- Single field kinetic constraint? → No
- New DESI data? → Even favored!
- BBN data?!



INTERLUDE

Gruber price cosmology 2025:

Ryan Cooke, Max Pettini → D/H measurement



$$E_{\text{bind}} = \frac{1}{2} m_e \alpha^2 \longrightarrow E_{\text{bind}} = \frac{1}{2} \mu_e \alpha^2 = \frac{1}{2} \frac{m_e m_{\text{nucleus}}}{m_e + m_{\text{nucleus}}} \alpha^2$$

$$\lambda_{\text{Deuterium}} \approx \lambda_H \cdot \left(\frac{1 + m_e/m_D}{1 + m_e/m_H} \right) \approx \lambda_H \cdot \left(1 - \frac{1}{2} \frac{m_e}{m_p} \right) \approx \lambda_H \cdot 99.97\%$$

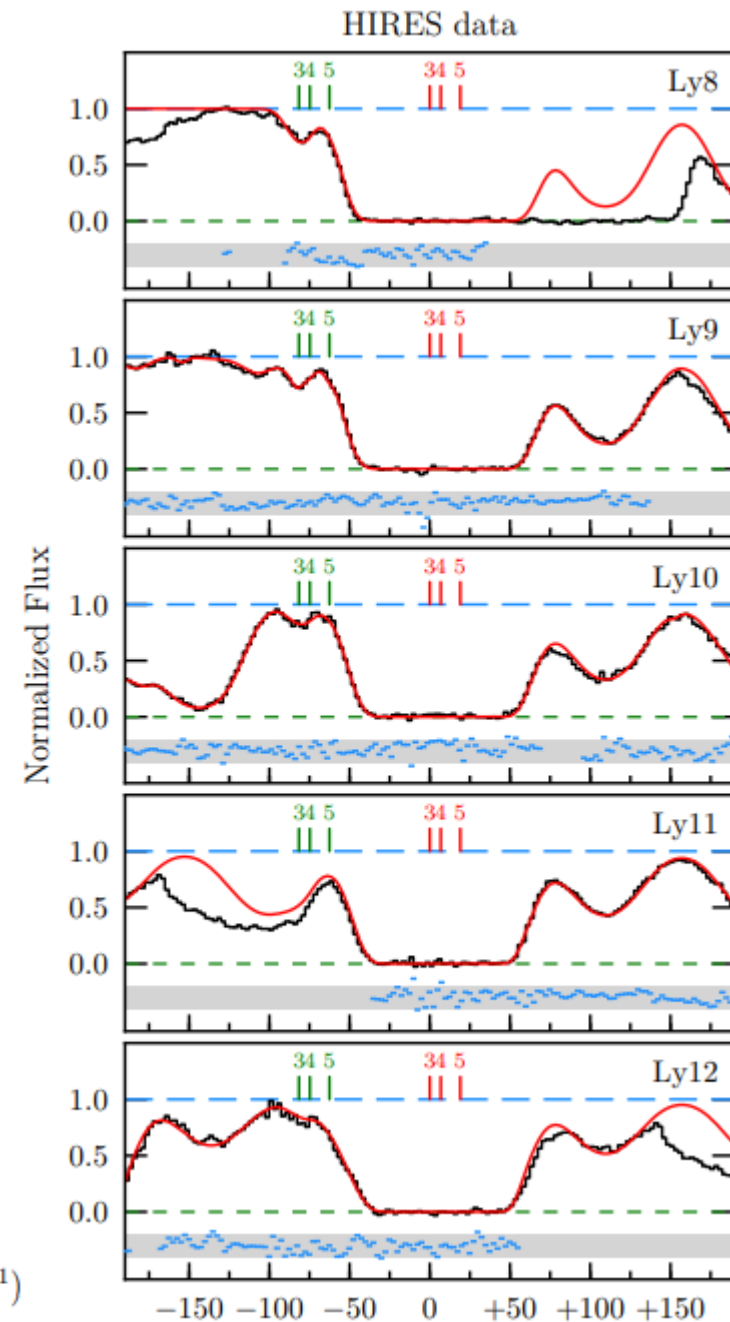
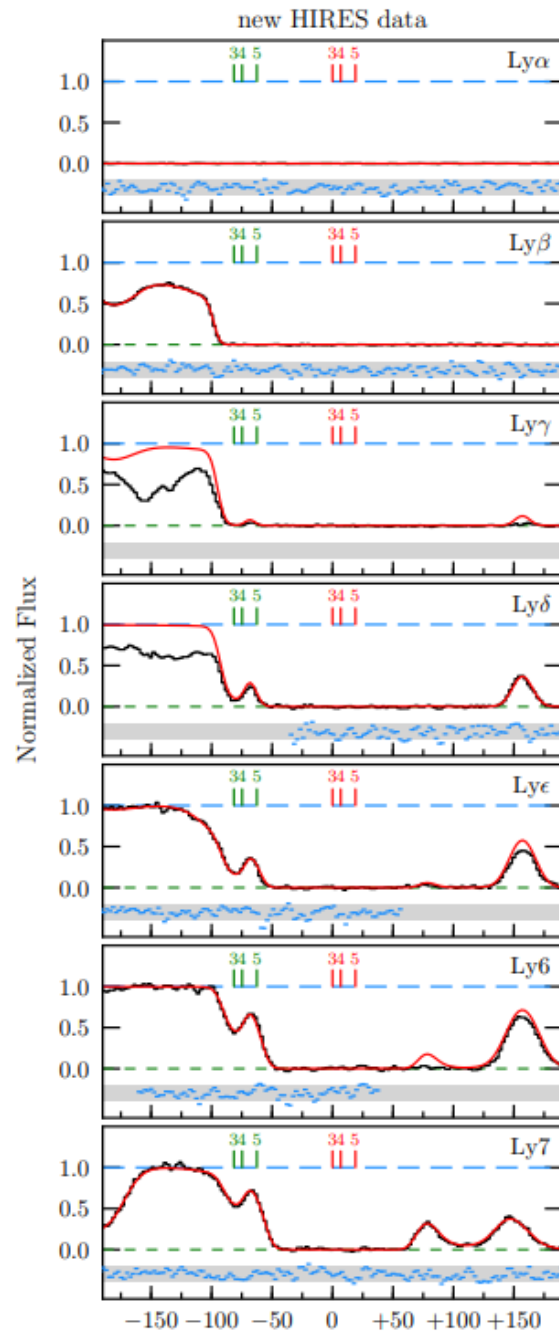
$$\delta\lambda/\lambda \sim 100\text{km/s}$$

INTERLUDE

Gruber prize cosmology 2025:
Ryan Cooke, Max Pettini →
D/H measurement

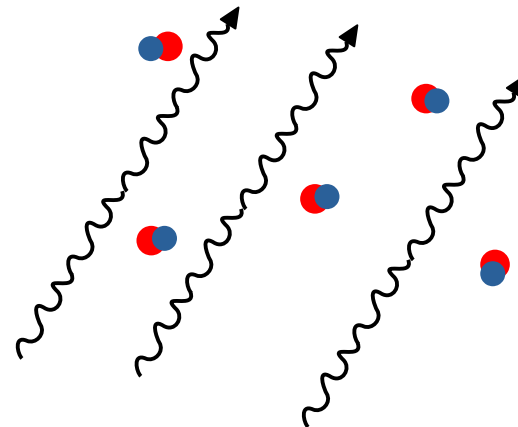
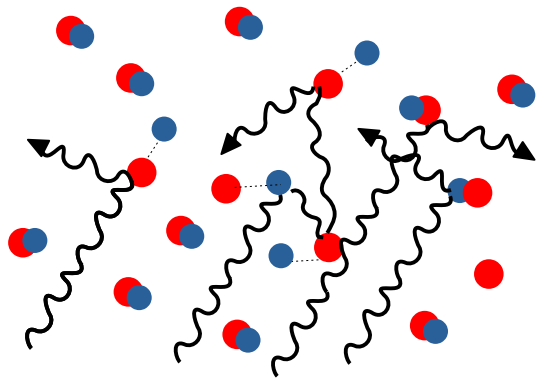


Velocity Relative to $z_{\text{abs}} = 2.525640$ (km s^{-1})



INTERLUDE

more baryons →
easier/earlier D burning →
hotter D burning →
more violent fusion →
less final D/H leftover



GETTING RID OF IT

- Single field kinetic constraint? → No
- New DESI data? → Even favored!
- BBN data?!

→ $\Omega_b h^2$ prior

GETTING RID OF IT

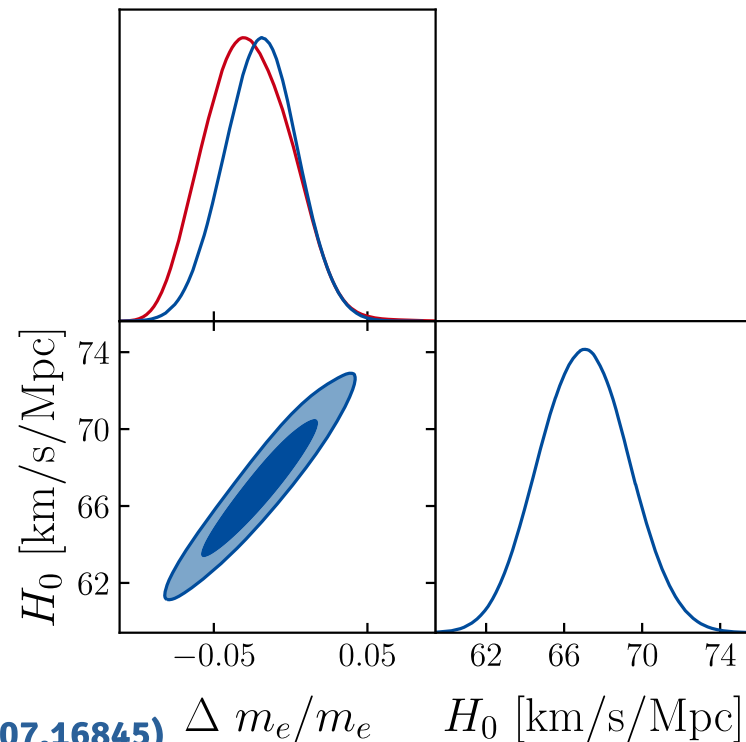
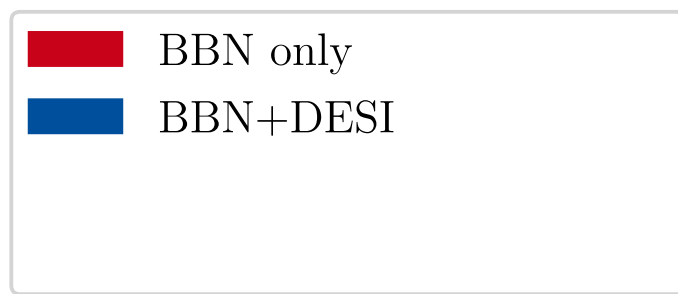
- Single field kinetic constraint? → No
- New DESI data? → Even favored!
- BBN data?!

~~→ $\Omega_b h^2$ prior~~



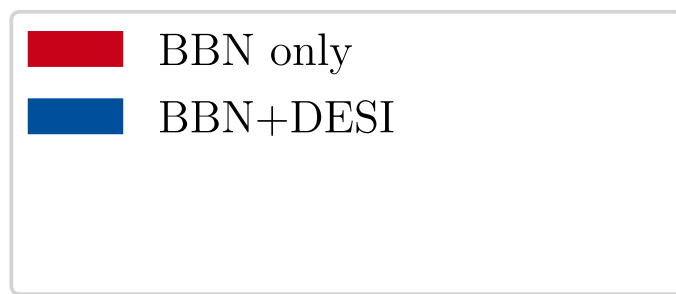
GETTING RID OF IT

- Single field kinetic constraint? → No
- New DESI data? → Even favored!
- BBN data?!

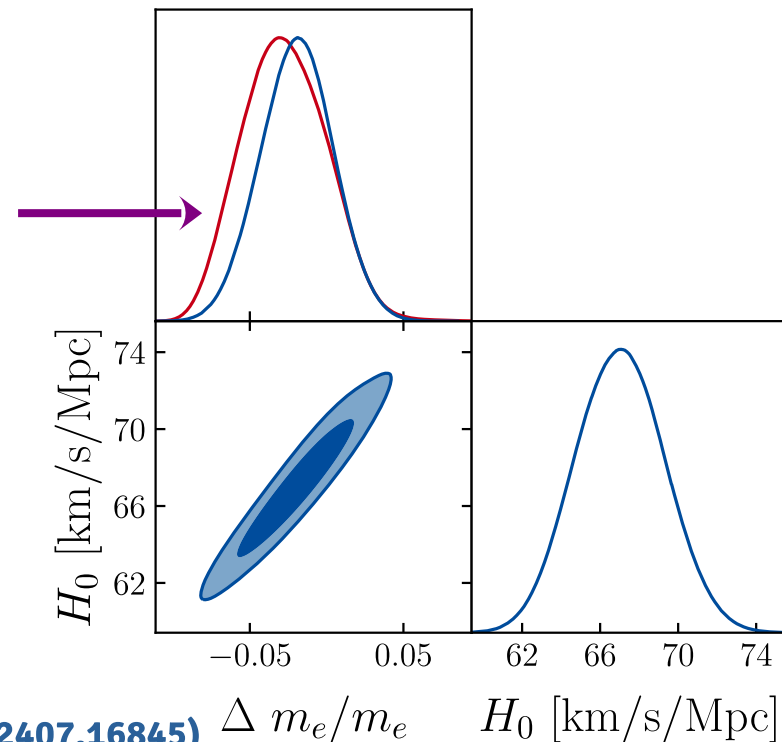


GETTING RID OF IT

- Single field kinetic constraint? → No
- New DESI data? → Even favored!
- BBN data?!

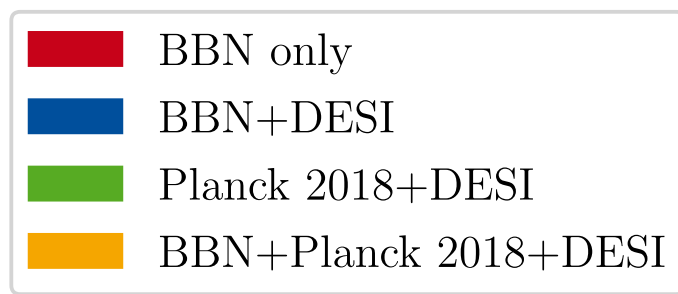


Constraint BBN
only is weak on m_e
~ 5%

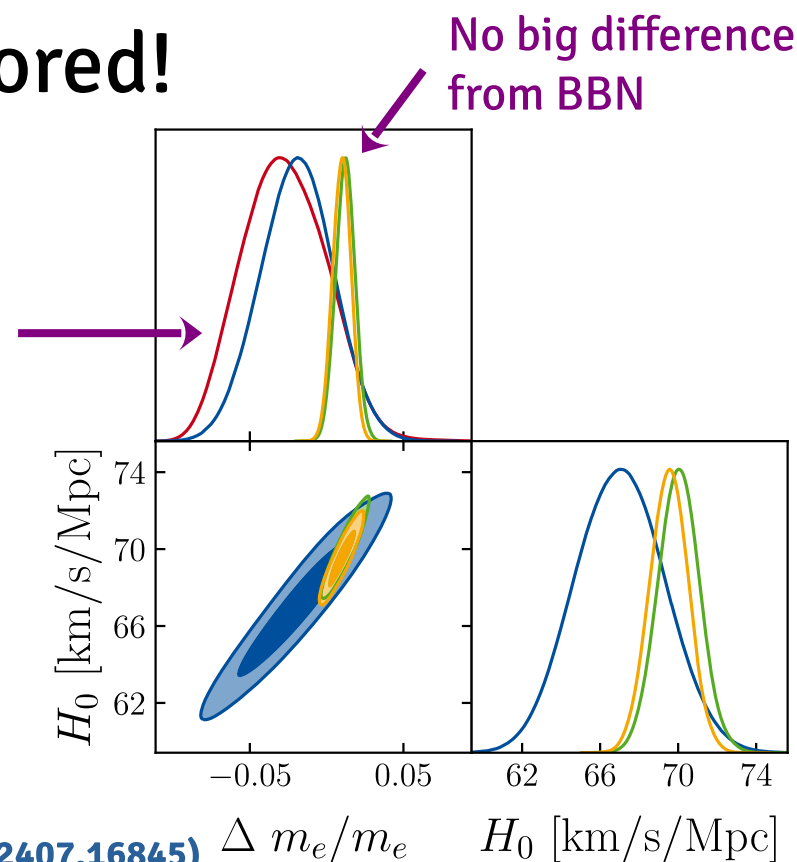


GETTING RID OF IT

- Single field kinetic constraint? → No
- New DESI data? → Even favored!
- BBN data?!



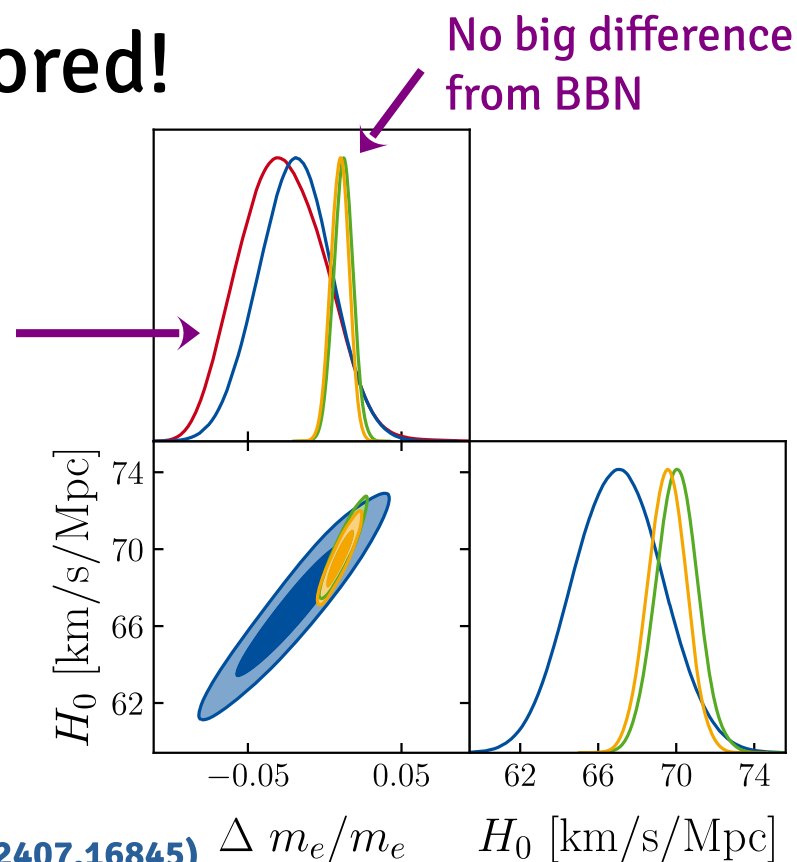
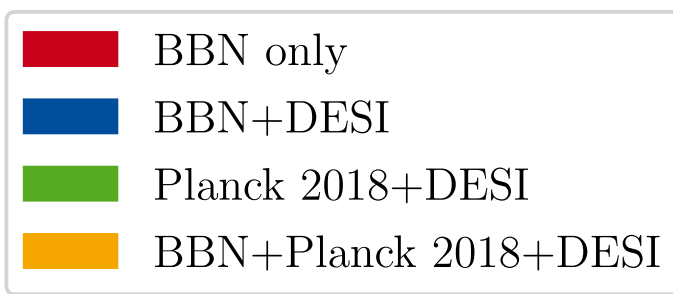
Constraint BBN
only is weak on m_e
~ 5%



GETTING RID OF IT

- Single field kinetic constraint? → No
- New DESI data? → Even favored!
- BBN data?! → Not even that

Constraint BBN
only is weak on m_e
~ 5%



GETTING RID OF IT

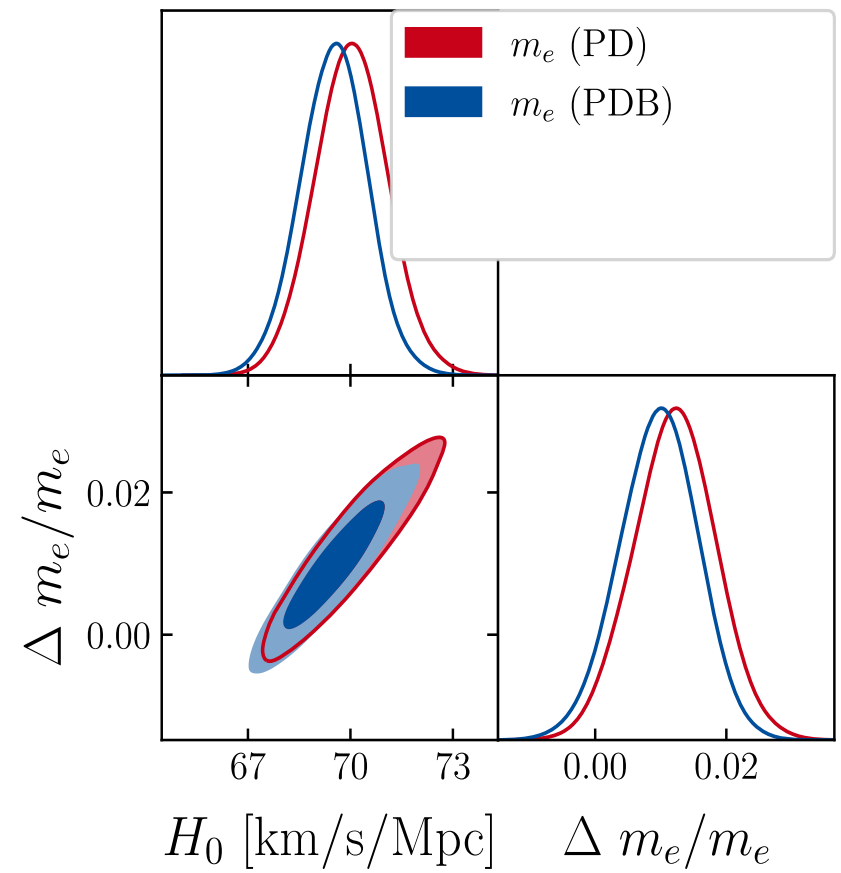
- Single field kinetic constraint? → No
- New DESI data? → Even favored!
- BBN data?! → Not even that

- Varying m_e is like a



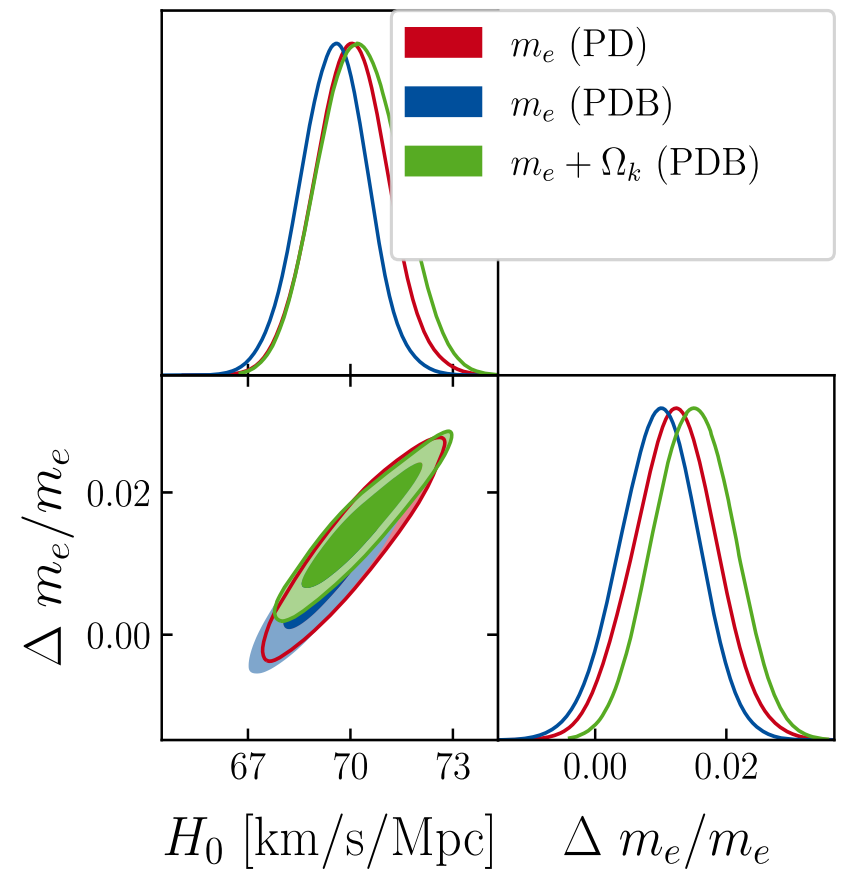
GETTING RID OF IT

- Even with extensions, doesn't look much worse



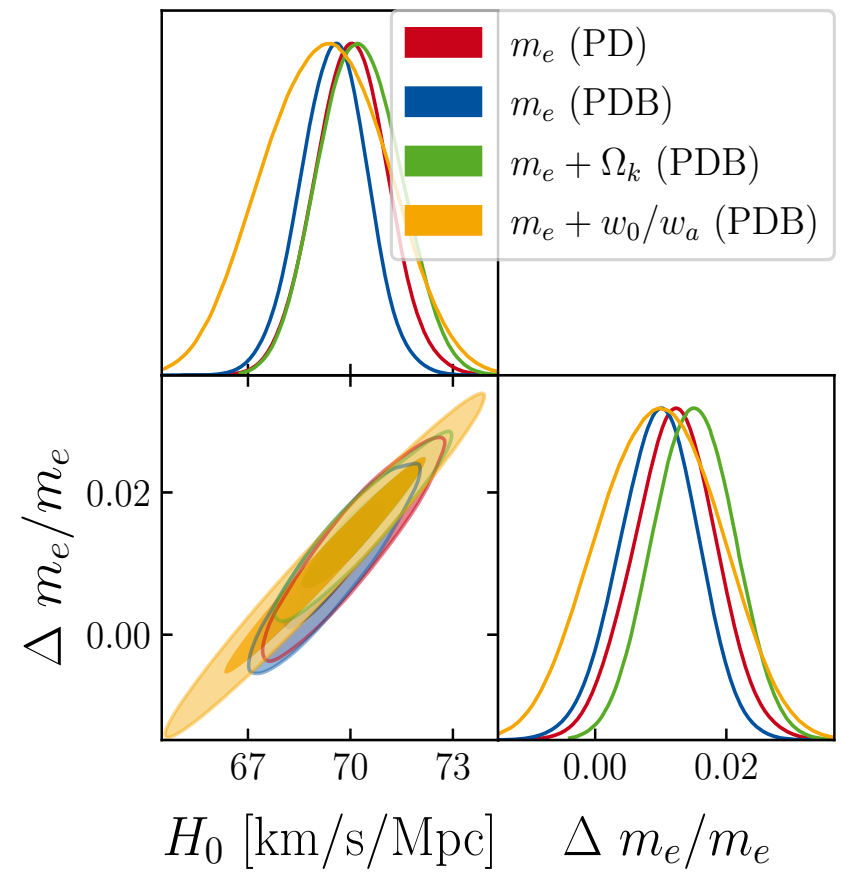
GETTING RID OF IT

- Even with extensions, doesn't look much worse



GETTING RID OF IT

- Even with extensions,
doesn't look much worse



HOW TO DIFFERENTIATE IT FROM EDE

- Different CMB
- Different cosmological parameters $\rightarrow$ structure growth $\rightarrow$ galaxy clustering + weak lensing

