



Universität Hamburg  
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CLUSTER OF EXCELLENCE  
QUANTUM UNIVERSE



# The Higgs boson through the lens of precision $e^+e^-$ data



Roman Kogler

60<sup>th</sup> Rencontres de Moriond

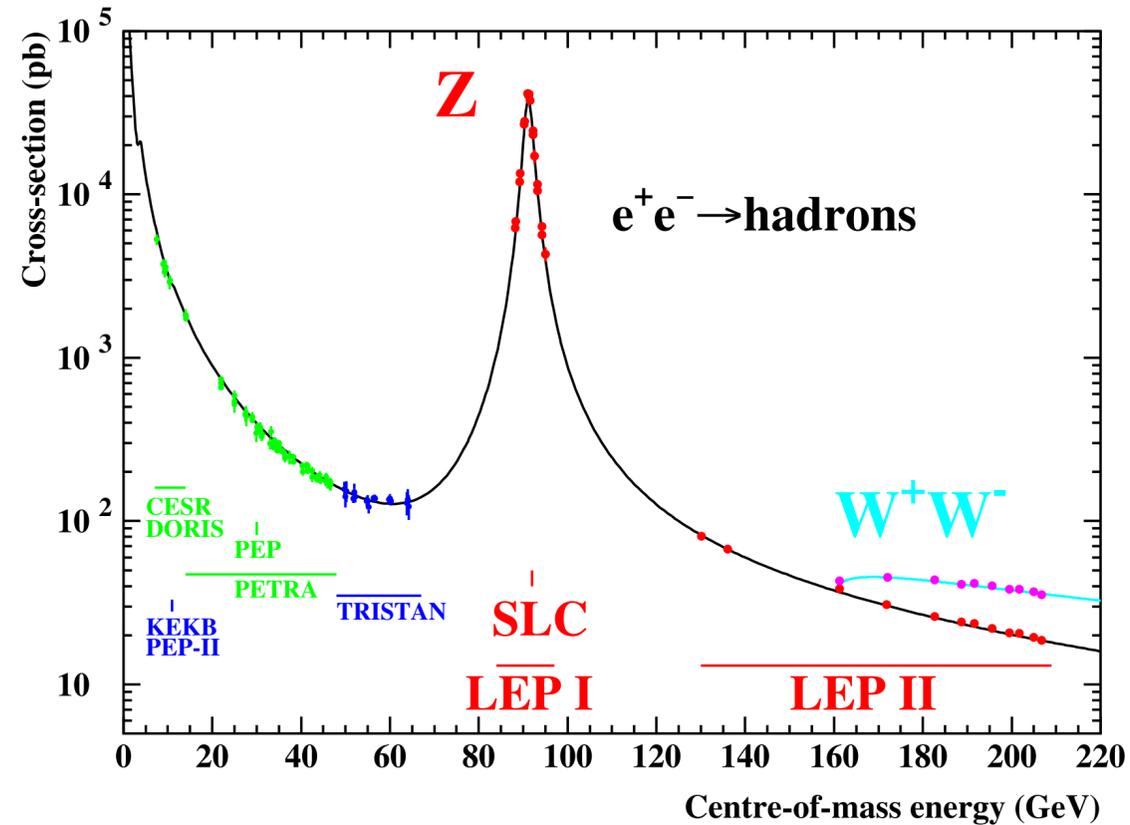
21 March, 2026

***The Gfitter group:***

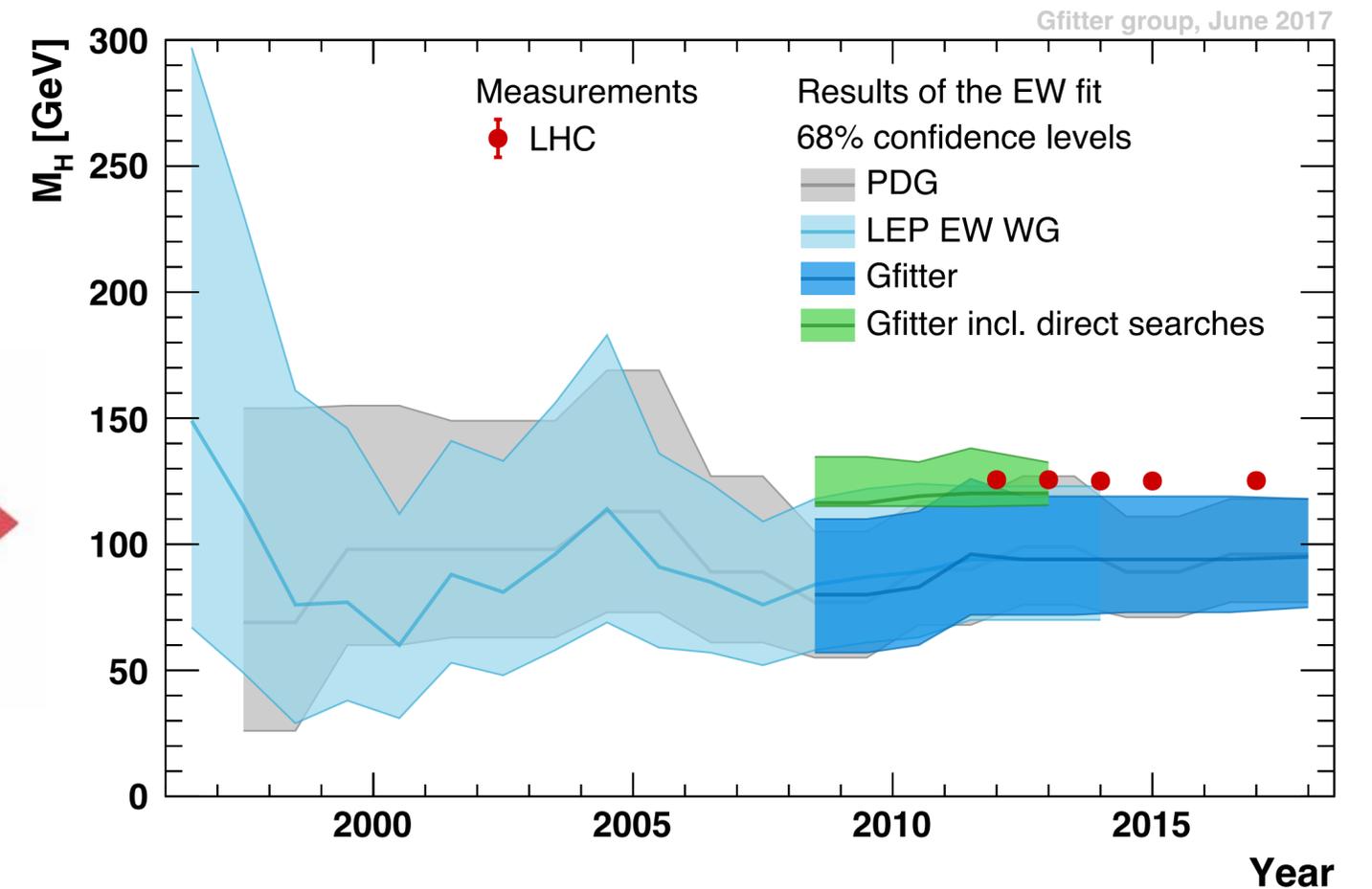
**Y. Fischer (Univ. Hamburg), J. Haller (Univ. Hamburg), A. Hoecker (CERN), RK (DESY),  
F. Labe (DESY), K. Mönig (DESY), D. Schwarz (DESY), J. Stelzer (Univ. Pittsburgh)**

# The Global EW Fit

## Precision data (EWPO)



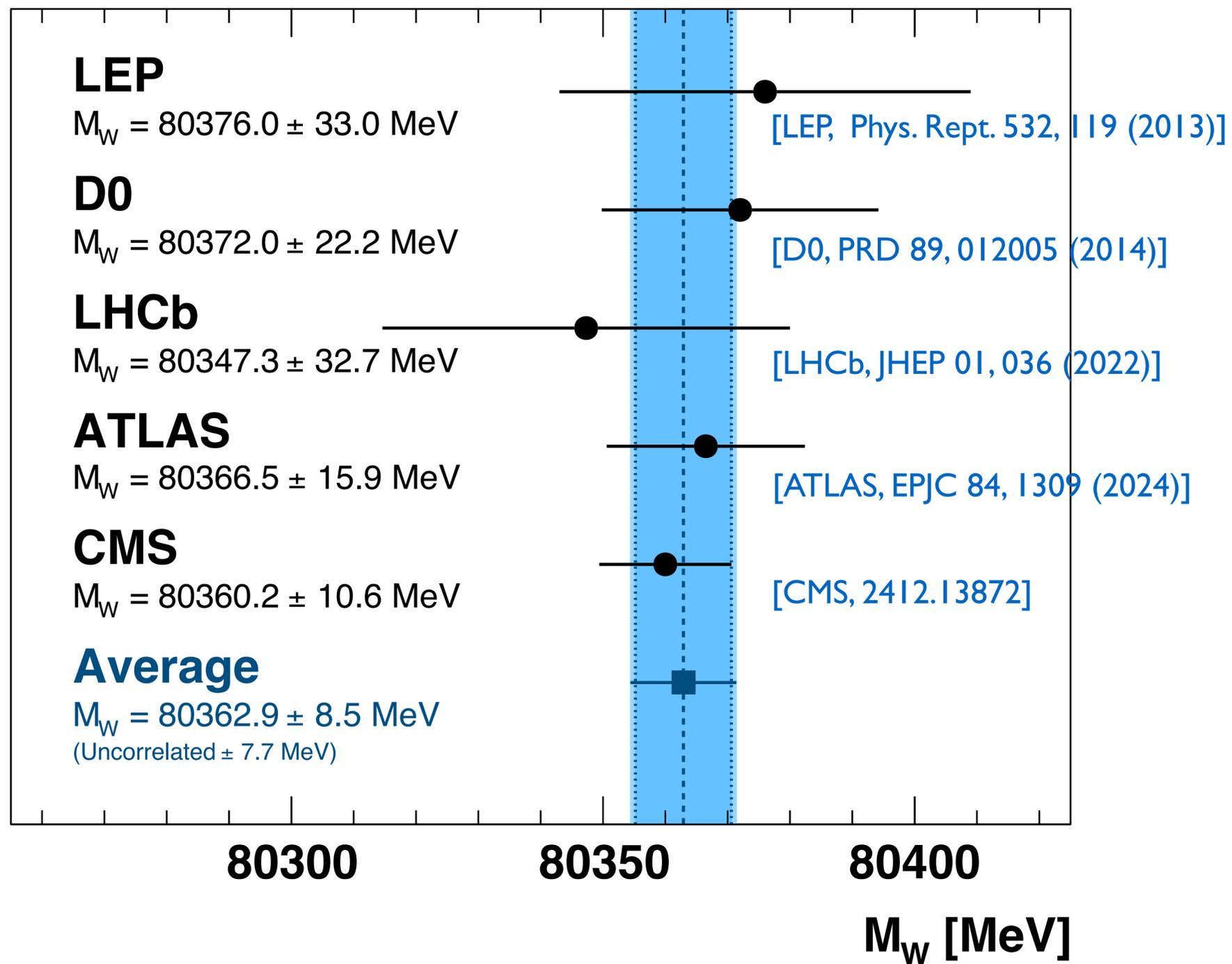
## Predictions and SM consistency tests



## Precision calculations (NNLO and higher)

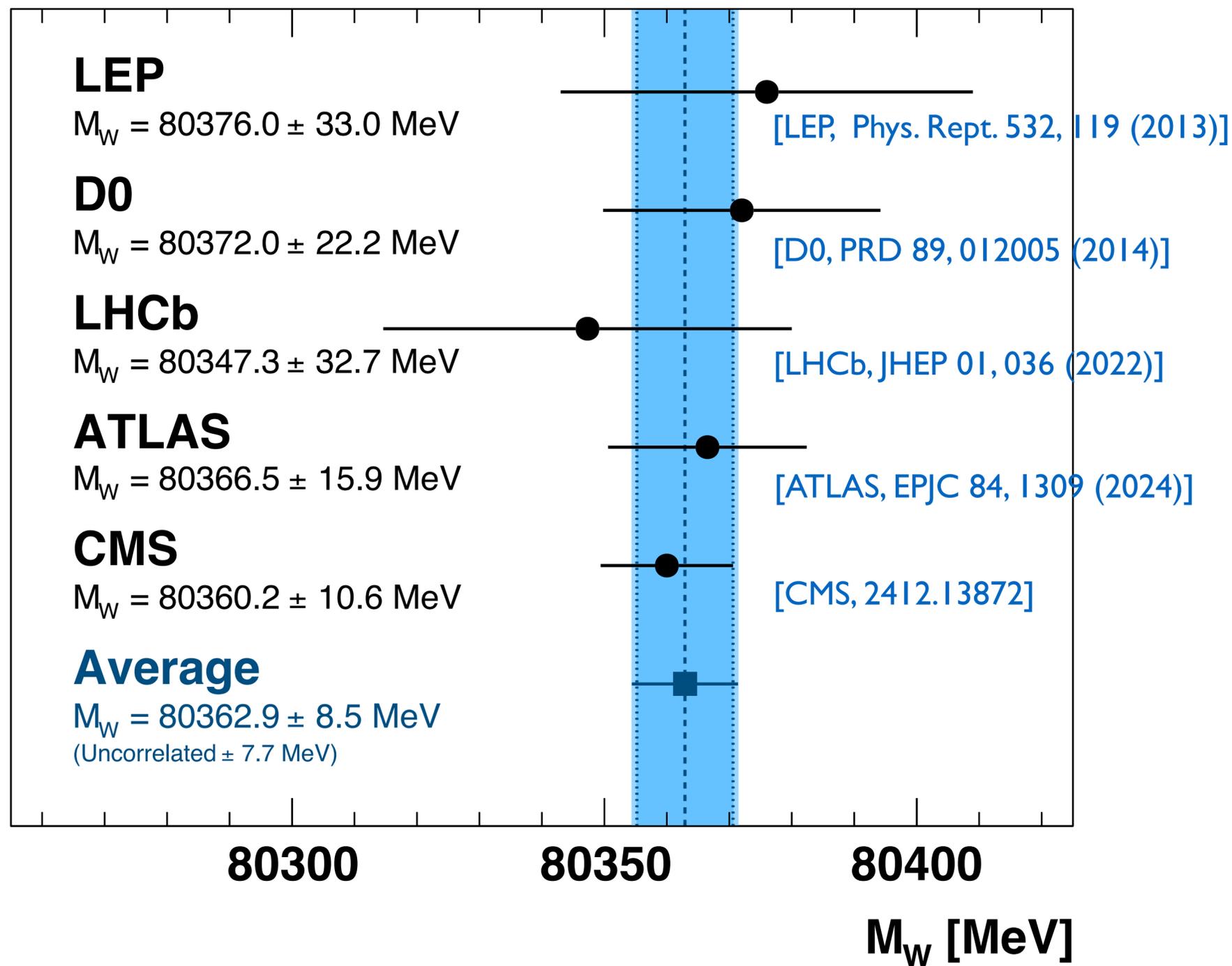
$$\text{Diagram} \propto \ln \frac{M_H^2}{M_W^2}$$

# W Mass



- ▶ Combination following LHC-TeV MW Working Group [MW WG, EPJC 84, 451 (2024)]
- ▶ Values adjusted to CT18
- ▶ Correlations accounted for
- ▶  $\chi^2/\text{ndf} = 0.7 / 5$

# W Mass

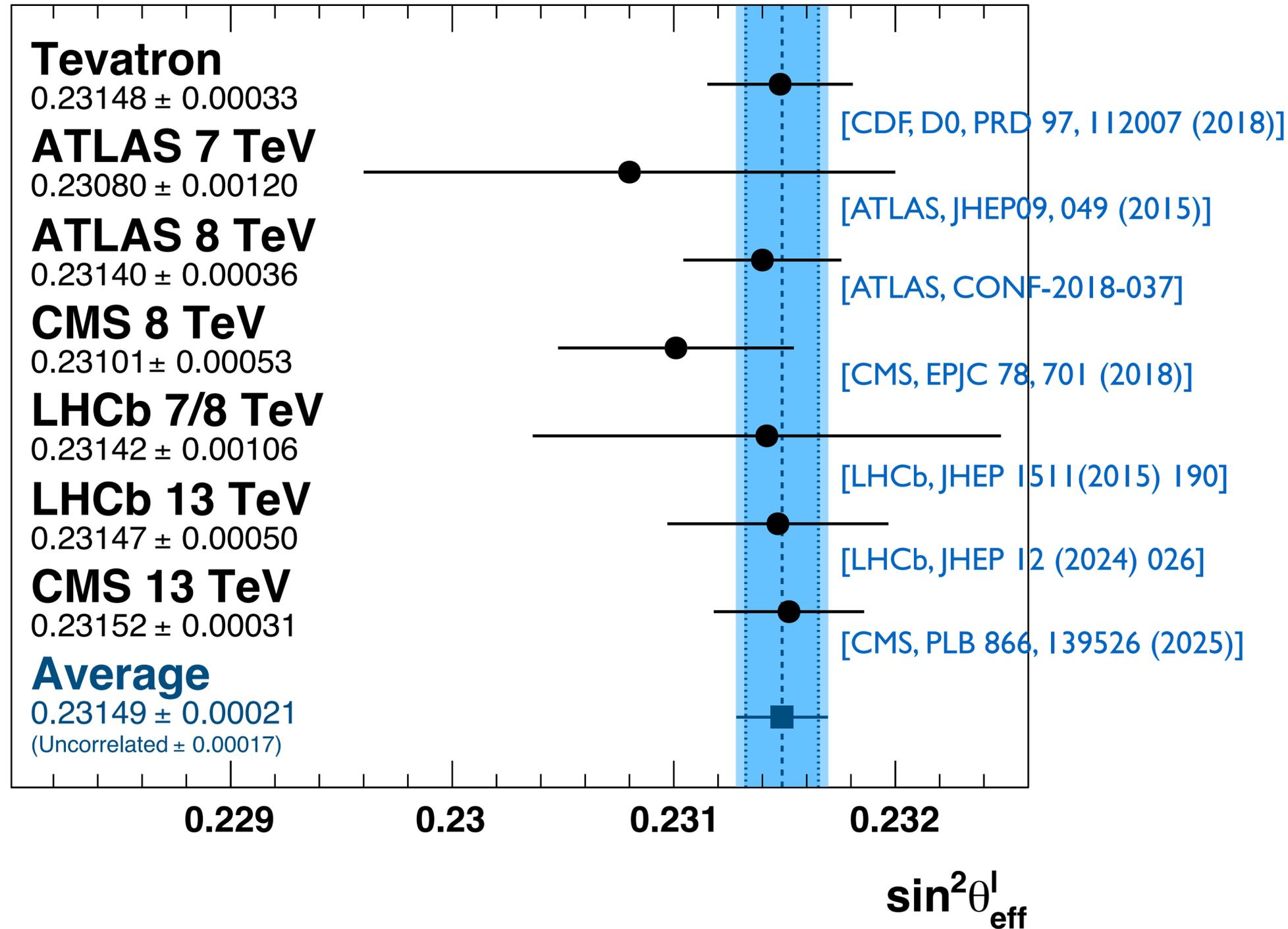


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**Precision on  $m_W$ :**  
**15 MeV (2015)**  
**8.5 MeV (today)**

(about 10 years ago:  
 envisioned 8 MeV for LHC Run 3)

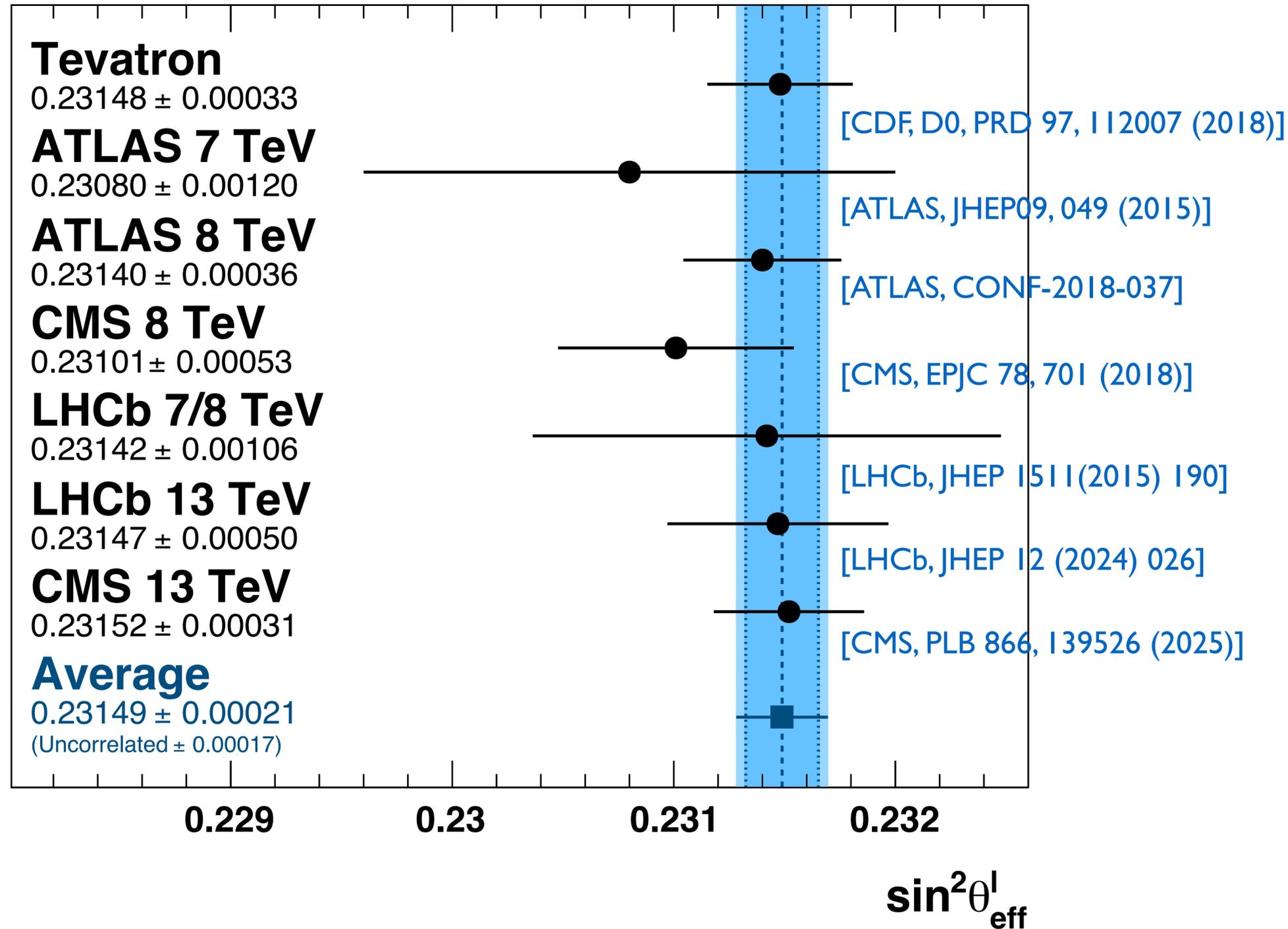
# Effective weak mixing angle $\sin^2(\theta_{\text{eff}}^l)$



Combination performed using assumptions and variations of PDF and model uncertainties

$$\chi^2/\text{ndf} = 1.3 / 6$$

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**LHC measurements now competitive with Tevatron**

Comparison:  
LEP/SLD:  $0.23153 \pm 0.00016$   
(included in fit through asymmetries)

[LEP, SLD, Phys. Rep. 427, 257 (2006)]

# SM Fit Results

## Recent updates

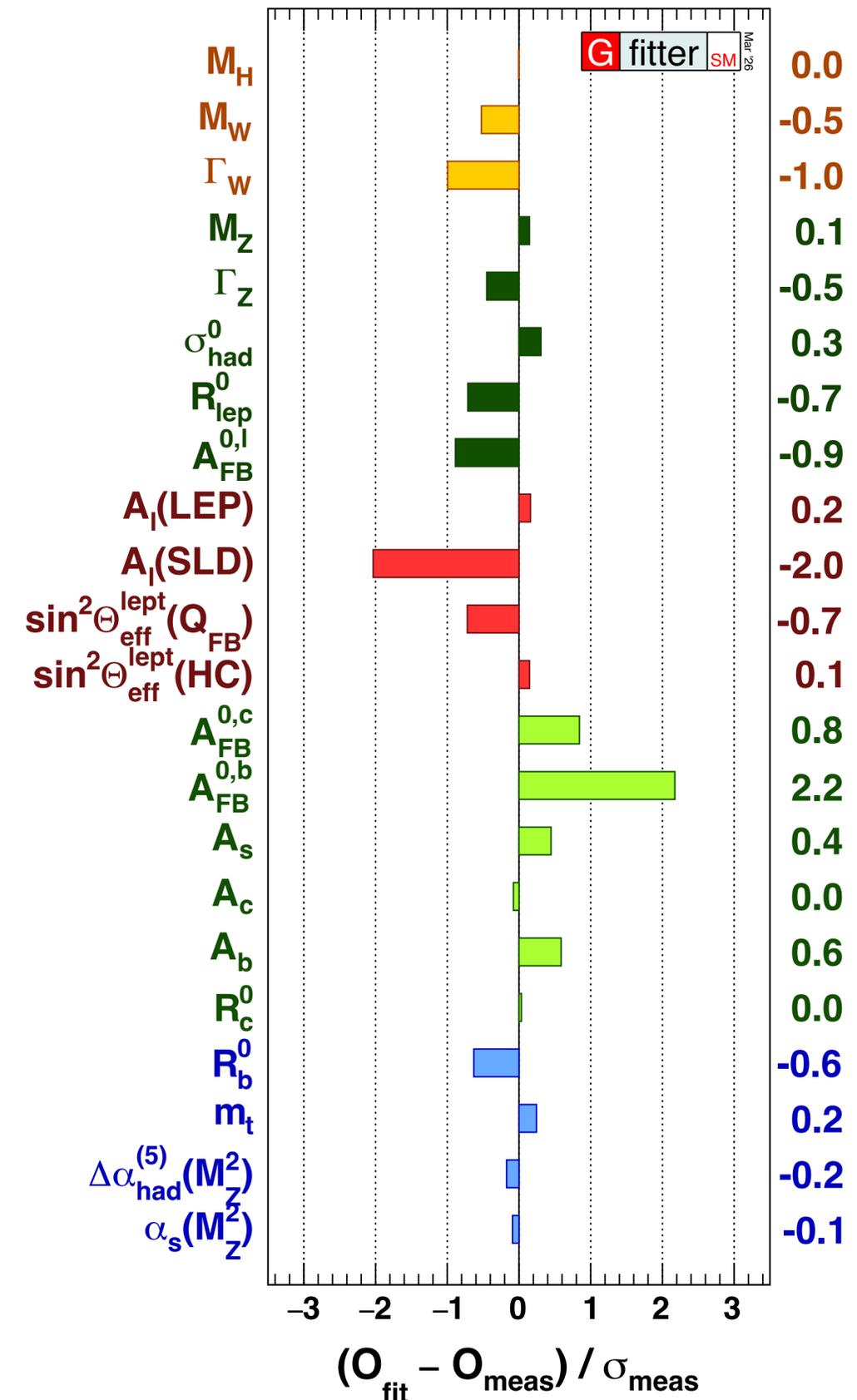
- ▶ Updated calculations of beam-beam effects on the LEP luminosity [Voutsinas et al, PLB 800, 135068 (2020)]
- ▶ Updated Bhabha cross section [Janot, Jadach, PLB 803, 135319 (2020)]

## Good fit quality

- ▶  $\chi^2 / \text{ndf} = 13.6 / 16$ , p-value = 0.63
  - $\chi^2 (2018) = 18.6$
  - $\chi^2 (2012) = 21.8$

## Indirect predictions:

- ▶  $m_H = 110^{+20}_{-17} \text{ GeV}$
- ▶  $m_W = 80.356 \pm 0.006 \text{ GeV}$
- ▶  $m_t = 173.7 \pm 1.6 \text{ GeV}$
- ▶  $\alpha_s(M_Z) = 0.1200 \pm 0.0028$



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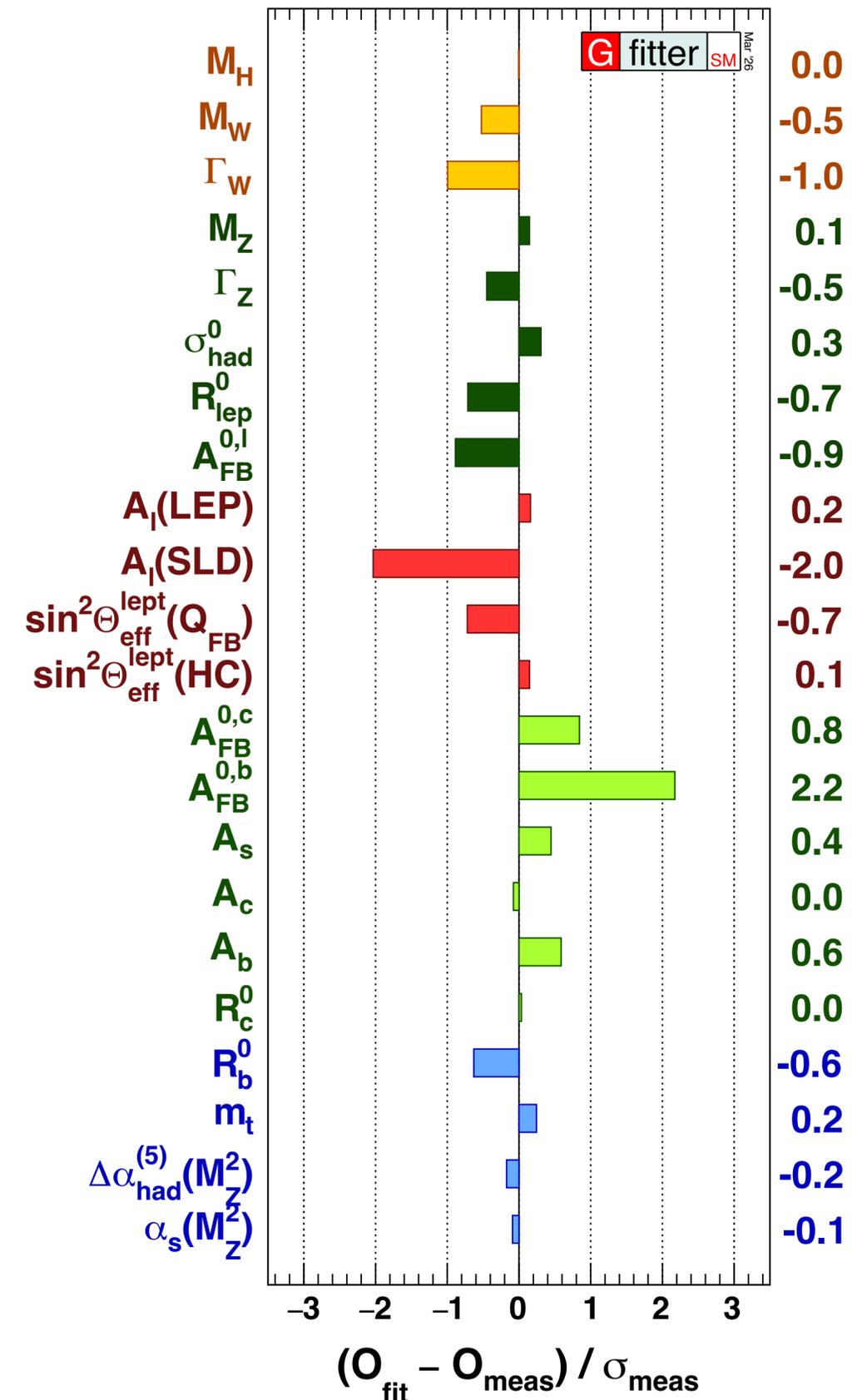
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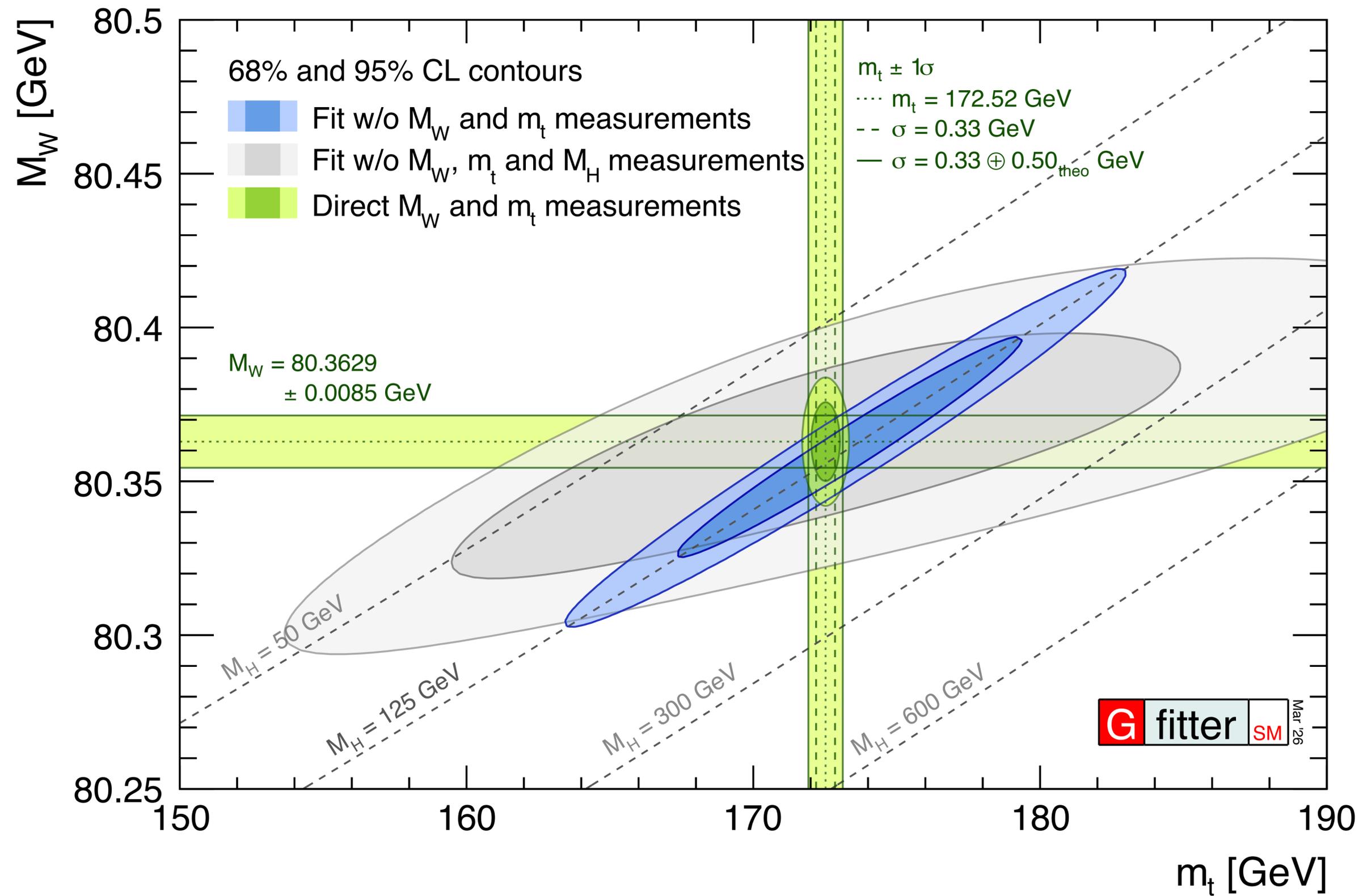
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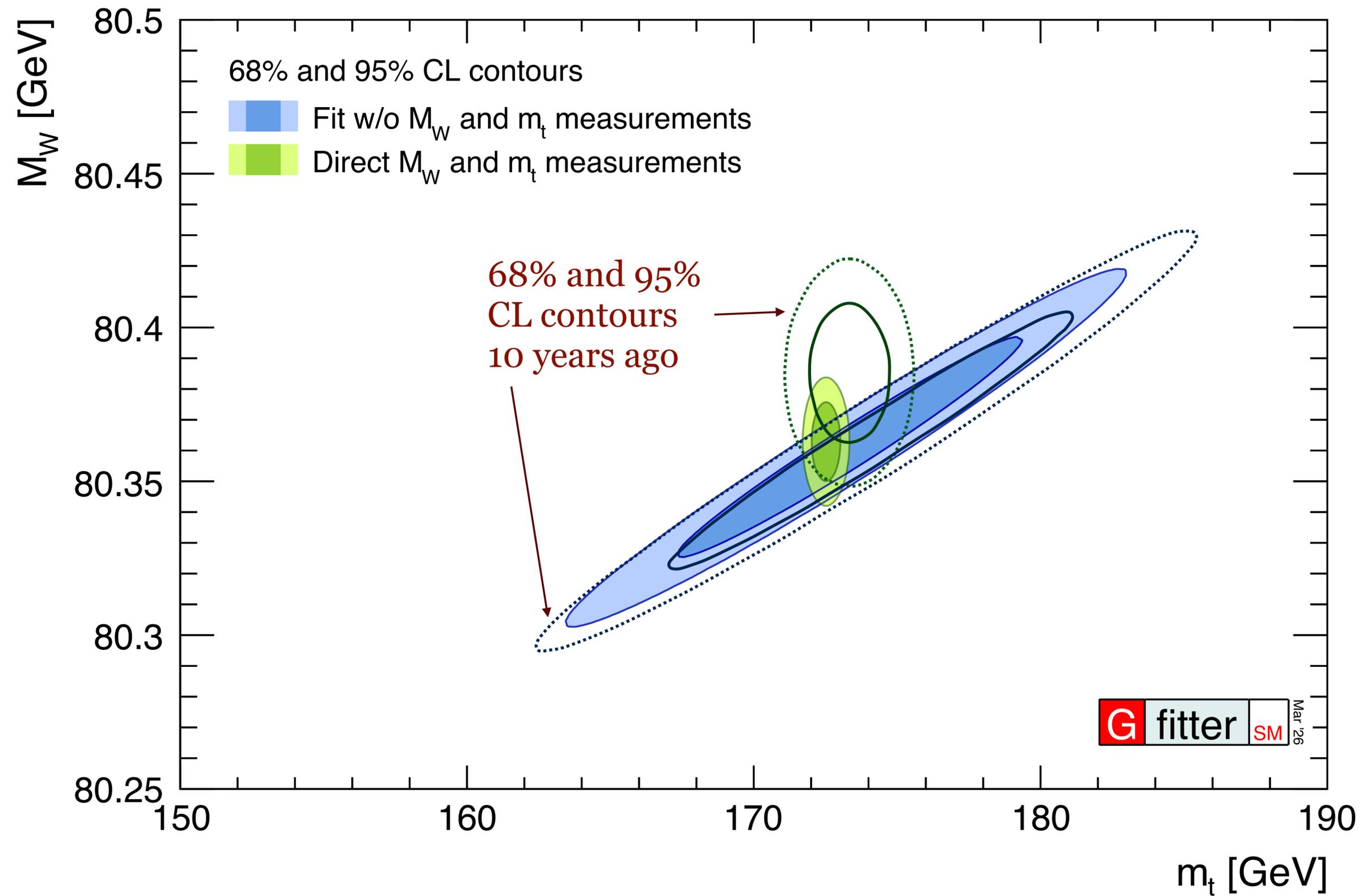
SM gets healthier with age

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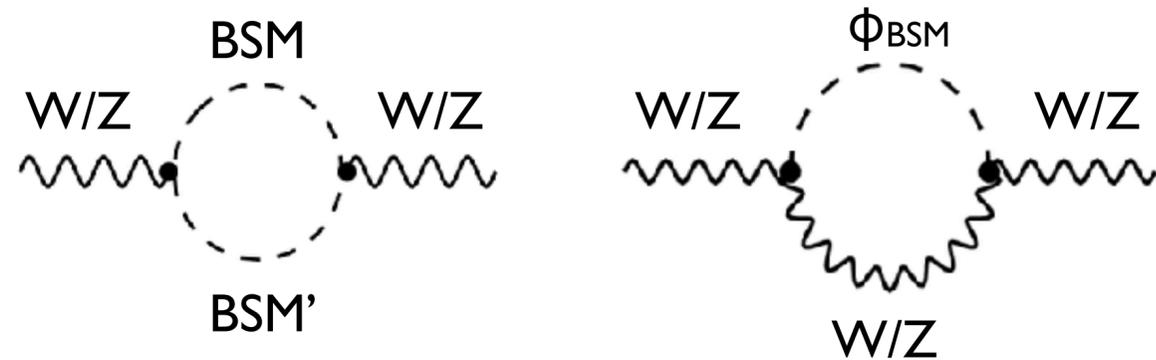




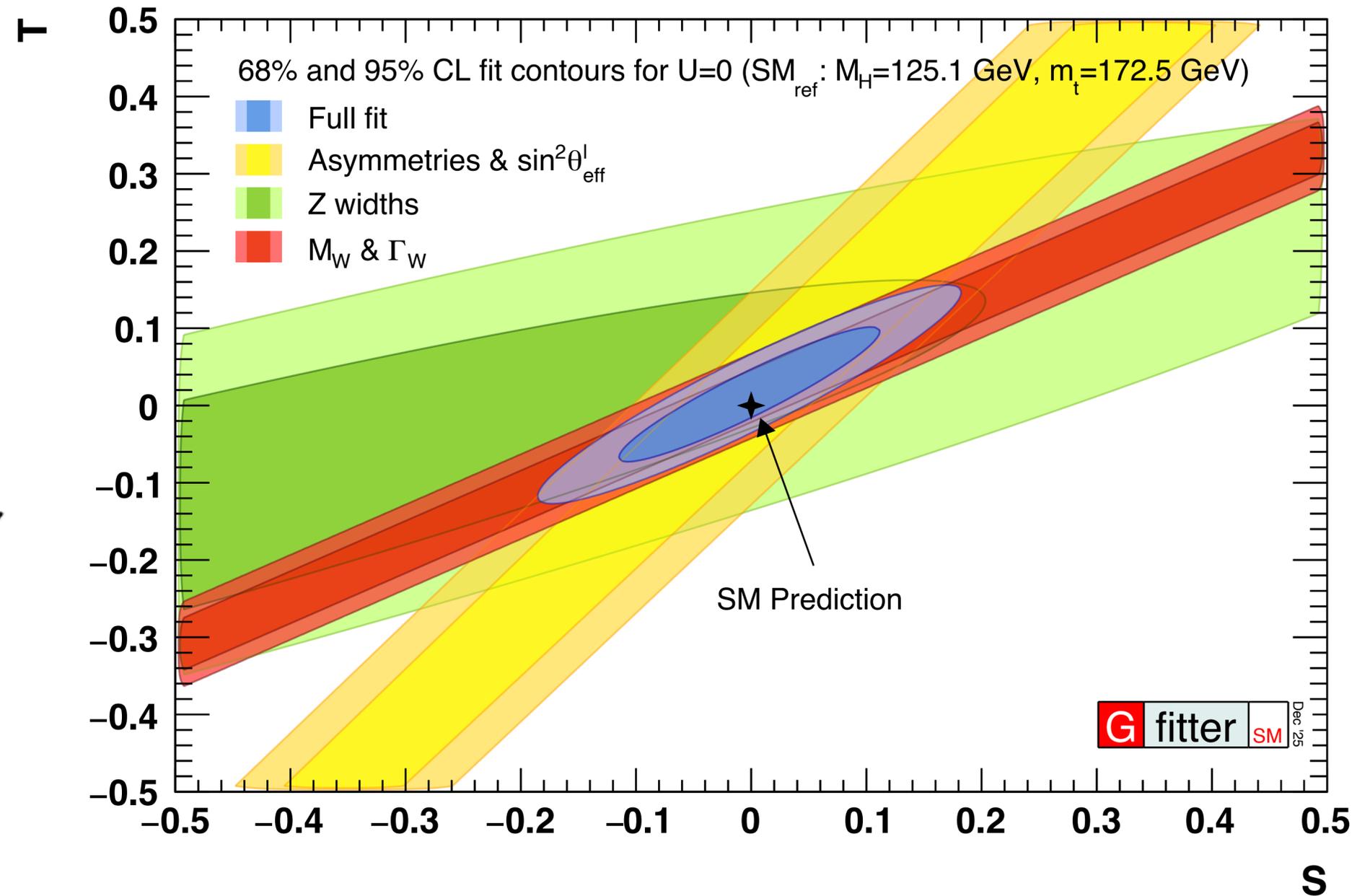
# BSM in the loops: Oblique Parameters

Constrain heavy BSM physics ( $M > M_Z$ ) through its effects on vacuum polarisation diagrams

- ▶ Universal modifications to light-particle scattering
- Oblique Parameters S, T, U



- ▶ Neutral current interactions: S, T
- ▶ Charged current: U



# The Higgs Boson Width

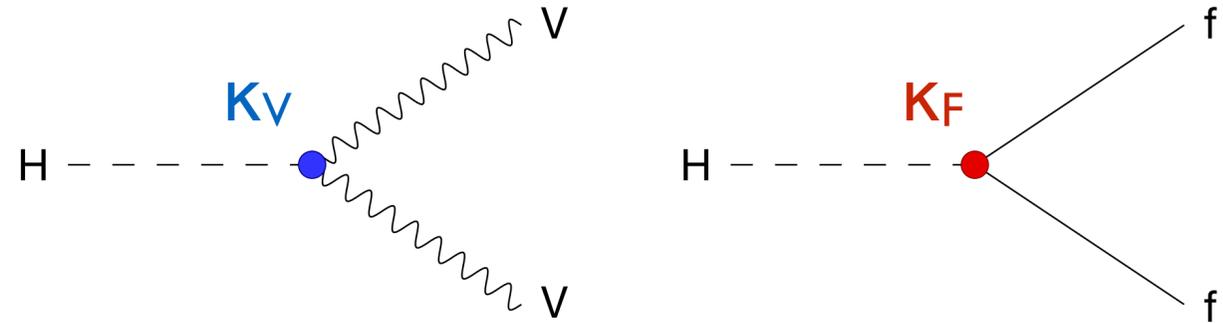
$$\text{(ATLAS)} \quad \Gamma_H = 4.3_{-1.9}^{+2.7} \quad [4.1_{-3.4}^{+3.5} \text{ (exp)}] \text{ MeV}$$

$$\text{(CMS)} \quad \Gamma_H = 3.0_{-1.5}^{+2.0} \quad [4.1 \pm 3.5 \text{ (exp)}] \text{ MeV} \quad [\text{PDG 2025}]$$

# The Higgs- $\kappa$ Framework

## Modification of SM Higgs couplings

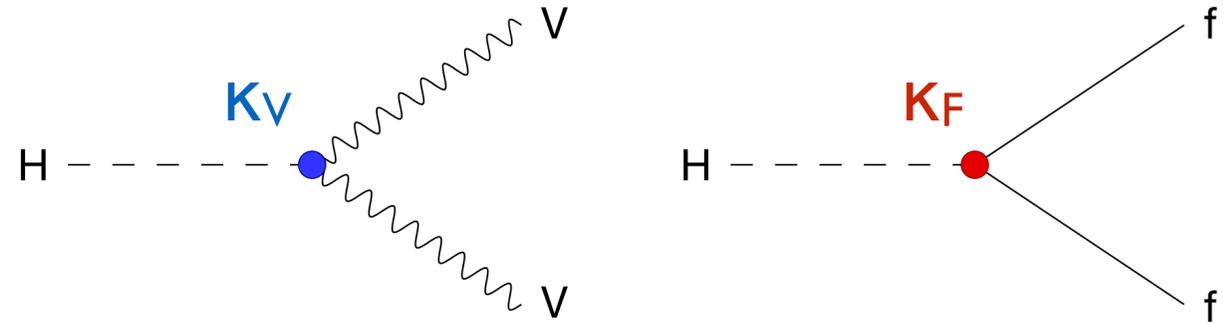
- ▶ Parameterised through  $\kappa_i$  modifiers
- ▶ Defined through partial widths  $\Gamma_i = \kappa_i^2 \Gamma_i^{\text{SM}}$



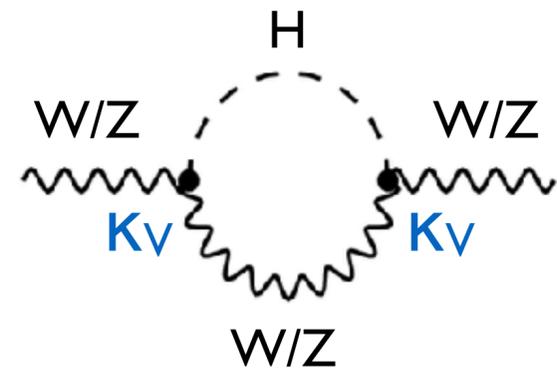
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- ▶ If couplings get modified, it's BSM physics and would show up in oblique corrections:



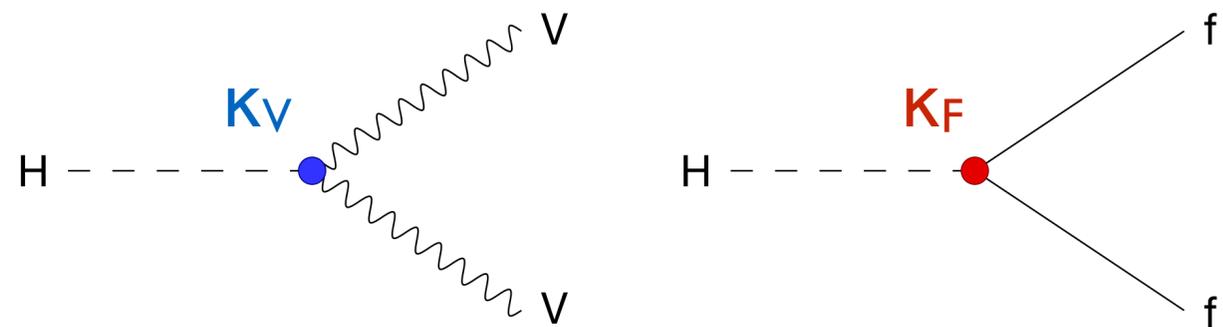
$$S = \frac{1}{12\pi} (1 - \kappa_V^2) \ln \left( \frac{\Lambda^2}{m_H^2} \right)$$

$$T = -\frac{3}{16\pi c_W^2} (1 - \kappa_V^2) \ln \left( \frac{\Lambda^2}{m_H^2} \right)$$

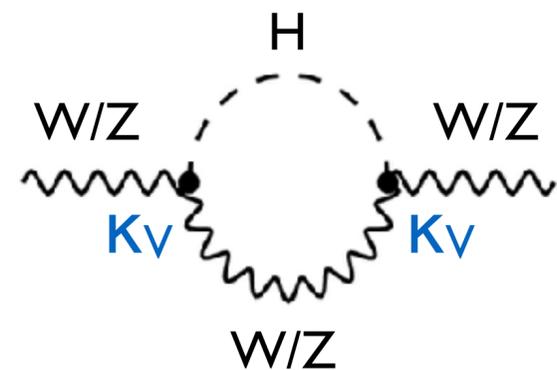
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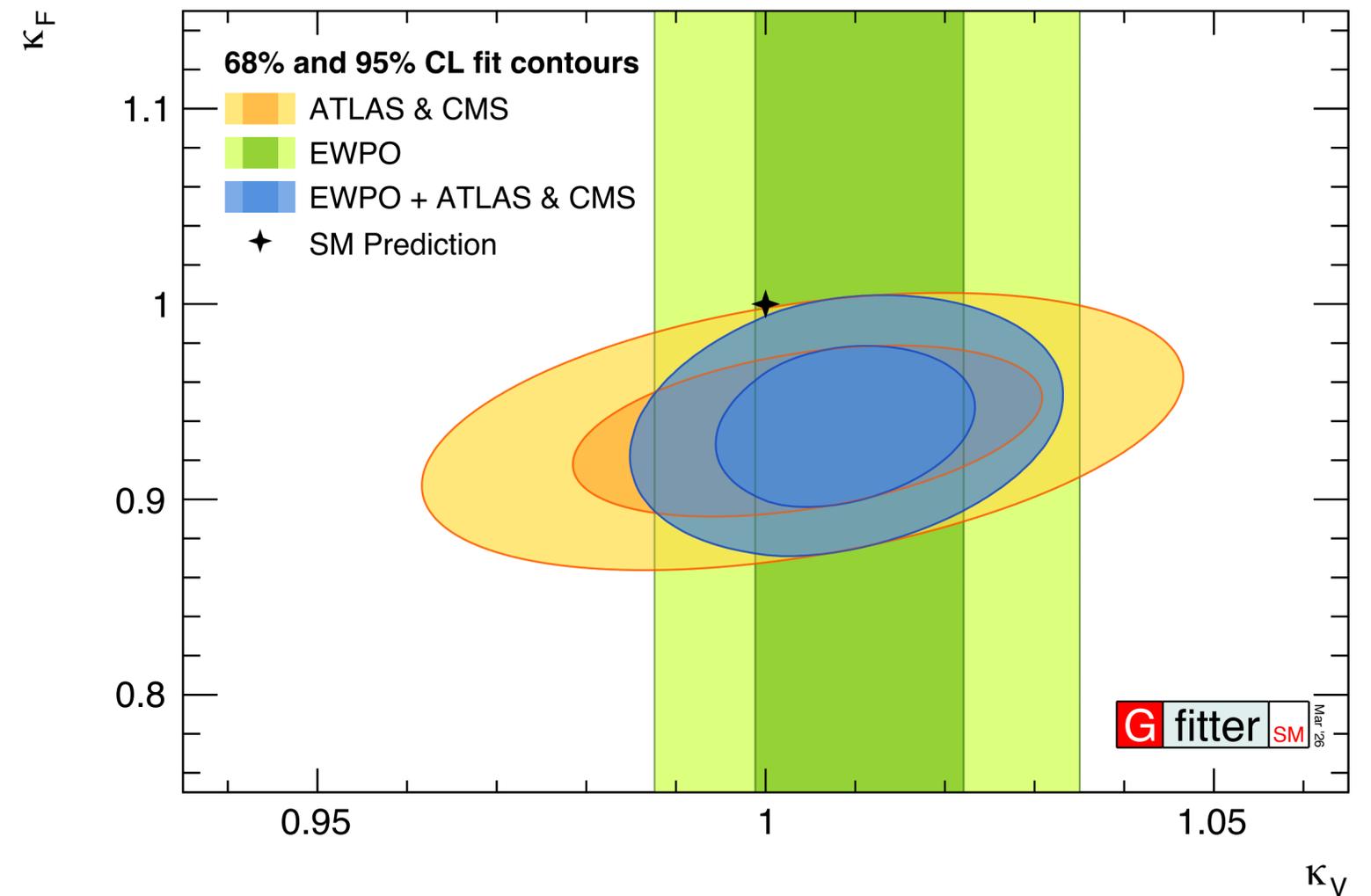


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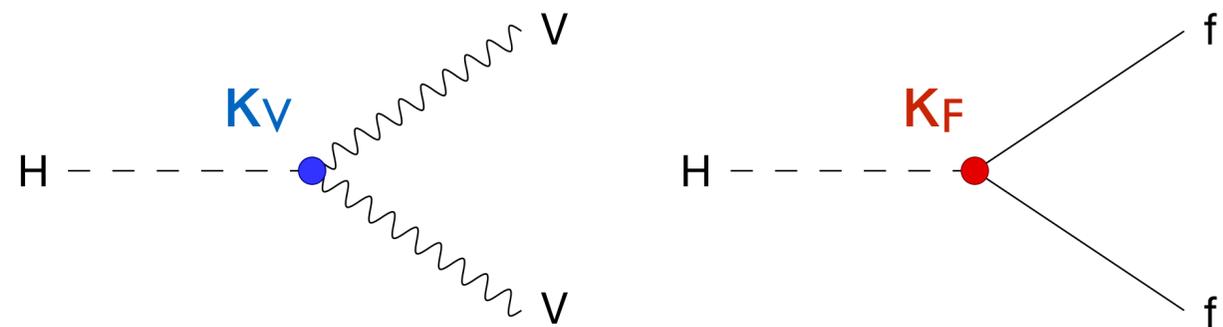


$\kappa_V = 1.010 \pm 0.012$  (EWPO only)

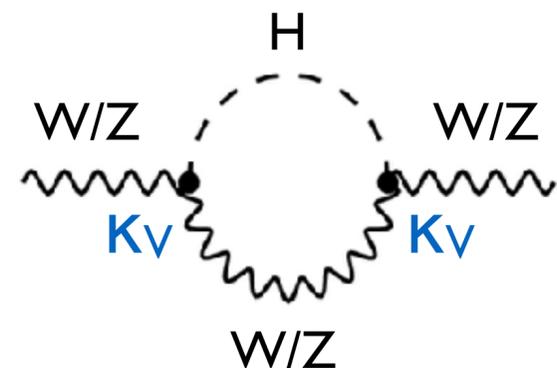
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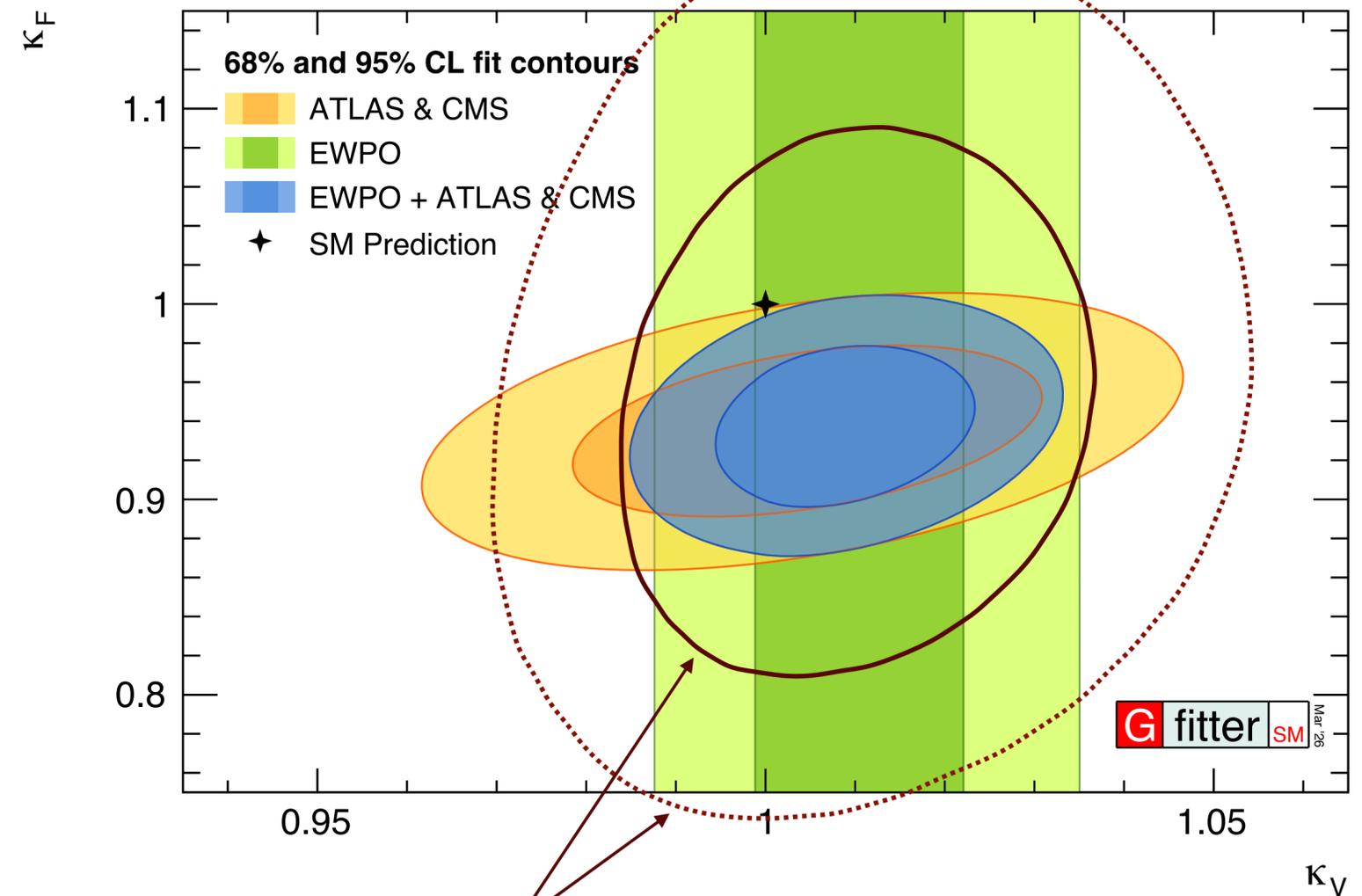


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68% and 96% CL contours  
10 years ago

# Higgs Signal Strengths

## General parameterisation:

$$(\sigma \cdot \text{BR})(i \rightarrow H \rightarrow f) = \frac{\sigma_i^{\text{SM}} \kappa_i^2 \cdot \Gamma_f^{\text{SM}} \kappa_f^2}{\Gamma_H^{\text{SM}} \kappa_H^2} \quad \text{with total width modifier } \kappa_H^2 = \frac{\Gamma_H}{\Gamma_{H,\text{SM}}}$$

$$\mu_i^f \equiv \frac{\sigma \cdot \text{BR}}{\sigma_{\text{SM}} \cdot \text{BR}_{\text{SM}}} = \frac{\kappa_i^2 \cdot \kappa_f^2}{\kappa_H^2}$$

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- ▶ With  $\kappa_Z = \kappa_W = \kappa_V$ , we can write

$$\mu_{\text{VBF}}^{WW} = \mu_{\text{VBF}}^{ZZ} = \mu_{\text{VH}}^{WW} = \mu_{\text{VH}}^{ZZ} = \frac{\kappa_V^4}{\kappa_H^2} \quad \leftarrow$$

Obtain the total H width through HVV coupling by combining EWPO and ATLAS & CMS Higgs data

- ▶ Adding more data, use  $\kappa_g$ ,  $\kappa_\gamma$ ,  $\kappa_\tau$ , and  $\kappa_V$

$$\mu_{\text{VBF}}^{VV} = \frac{\mu_{\text{ggF}}^{VV} \mu_{\text{VBF}}^{jj}}{\mu_{\text{ggF}}^{jj}}, \quad jj = \gamma\gamma, \tau\tau \quad \leftarrow$$

Effective couplings: Model-independent determination of H width including loop effects

(same for VH)

# Higgs Signal Strengths

Use latest ATLAS and CMS Run-2 Higgs combinations

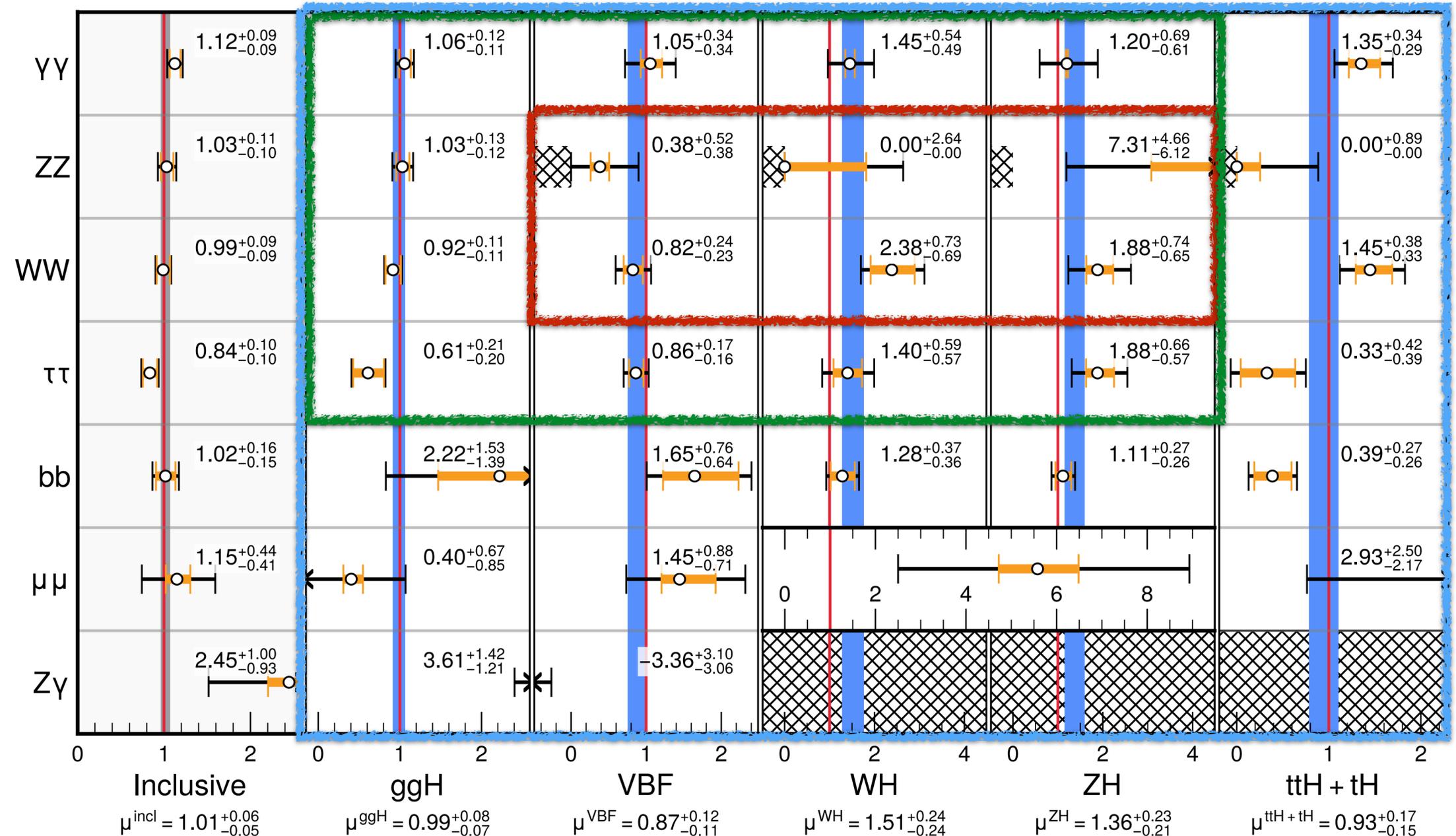
- ▶ [CMS, 2602.18611]
- ▶ [ATLAS, CONF-2025-006]
- ▶ Correlations between  $\mu_{ij}$  taken into account

Three sets of measurements, corresponding to the parameterisations:

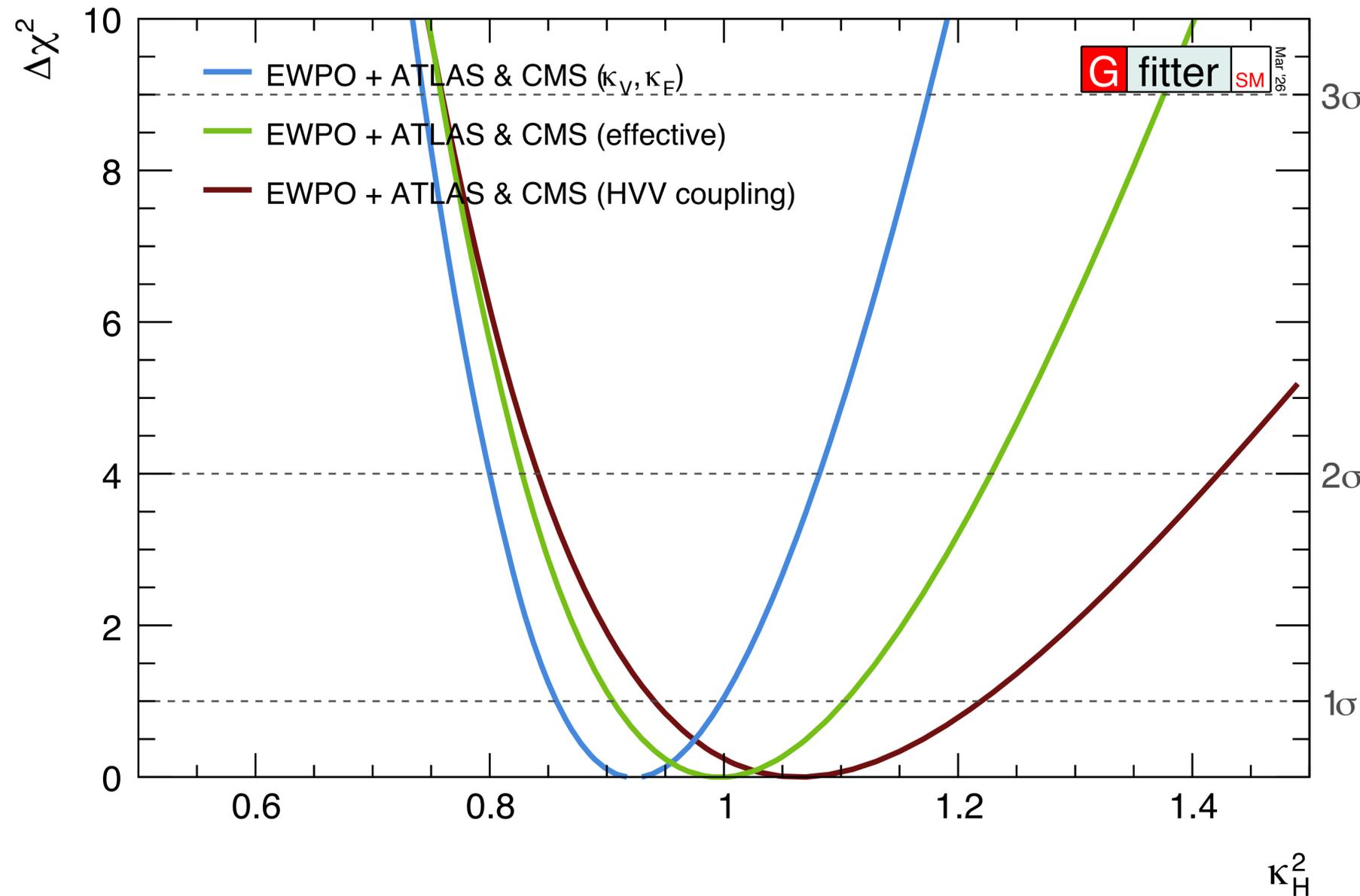
- ▶ HVV
- ▶ Effective (incl.  $\kappa_g, \kappa_\gamma$ )
- ▶ Resolved ( $\kappa_V, \kappa_F$ )

CMS (similar for ATLAS)

138 fb<sup>-1</sup> (13 TeV)



# Width of the Higgs Boson



## HVV coupling-only:

$$\Gamma_H = 4.36^{+0.64}_{-0.51} \text{ MeV}$$

$$\chi^2 / \text{ndf} = 28.8 / 28$$

## Effective parameterisation:

$$\Gamma_H = 4.09^{+0.44}_{-0.37} \text{ MeV} \quad (\delta\Gamma_H \approx 10\%)$$

$$\chi^2 / \text{ndf} = 45.9 / 44$$

## All measurements (resolved parameterisation $\kappa_V, \kappa_F$ ):

$$\Gamma_H = 3.79^{+0.31}_{-0.27} \text{ MeV}$$

$$\chi^2 / \text{ndf} = 72.9 / 76$$

$$(\Gamma_H^{\text{SM}} = 4.1 \text{ MeV})$$

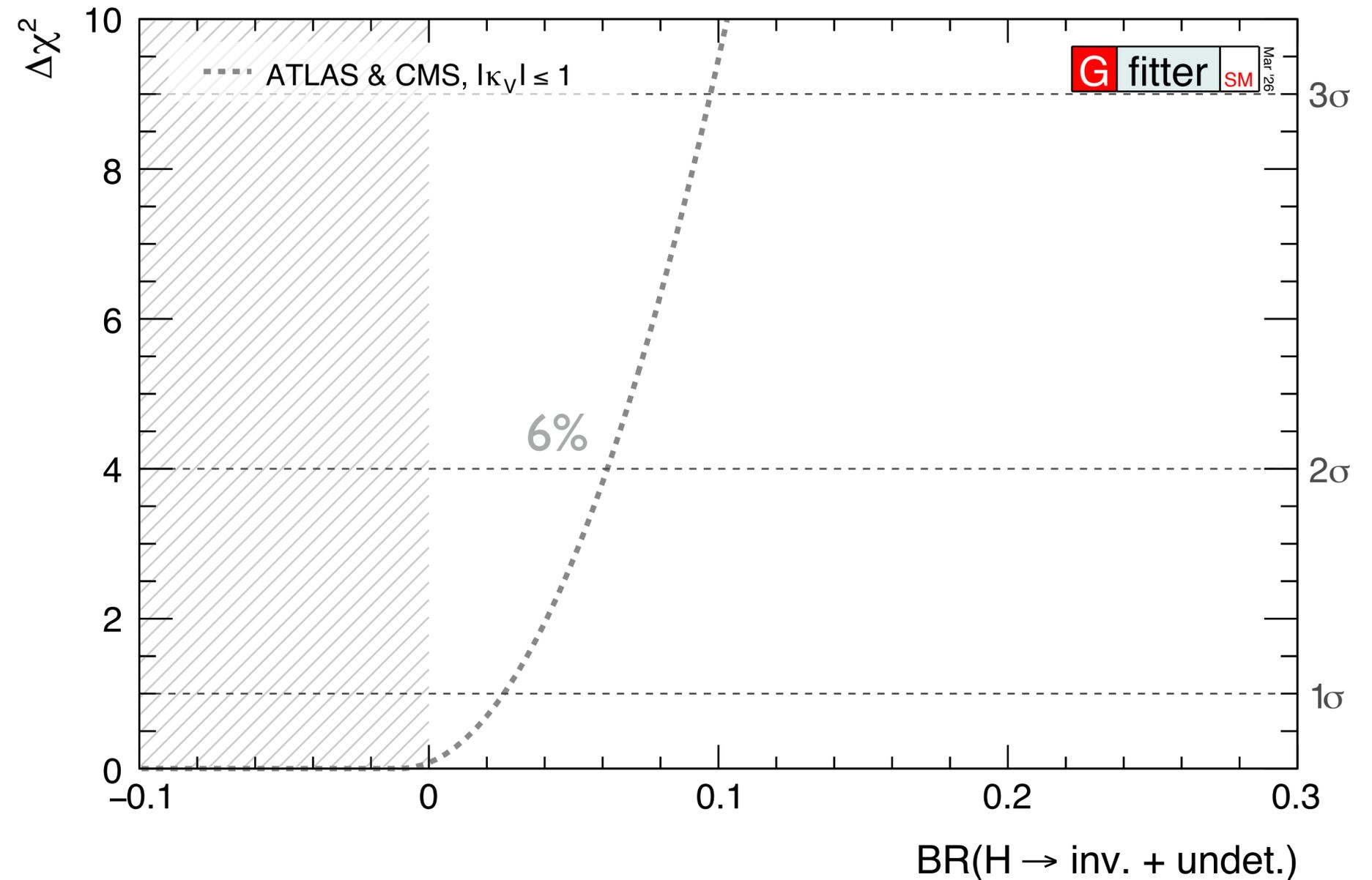
# The Invisible and Undetectable Higgs

Define  $BR(H \rightarrow BSM)$  through

$$BR(H \rightarrow BSM) = \frac{\Gamma_{BSM}}{\Gamma_H}$$

where  $\Gamma_H = \Gamma(\kappa) + \Gamma_{BSM}$

the visible widths are scaled with  $\kappa_i$



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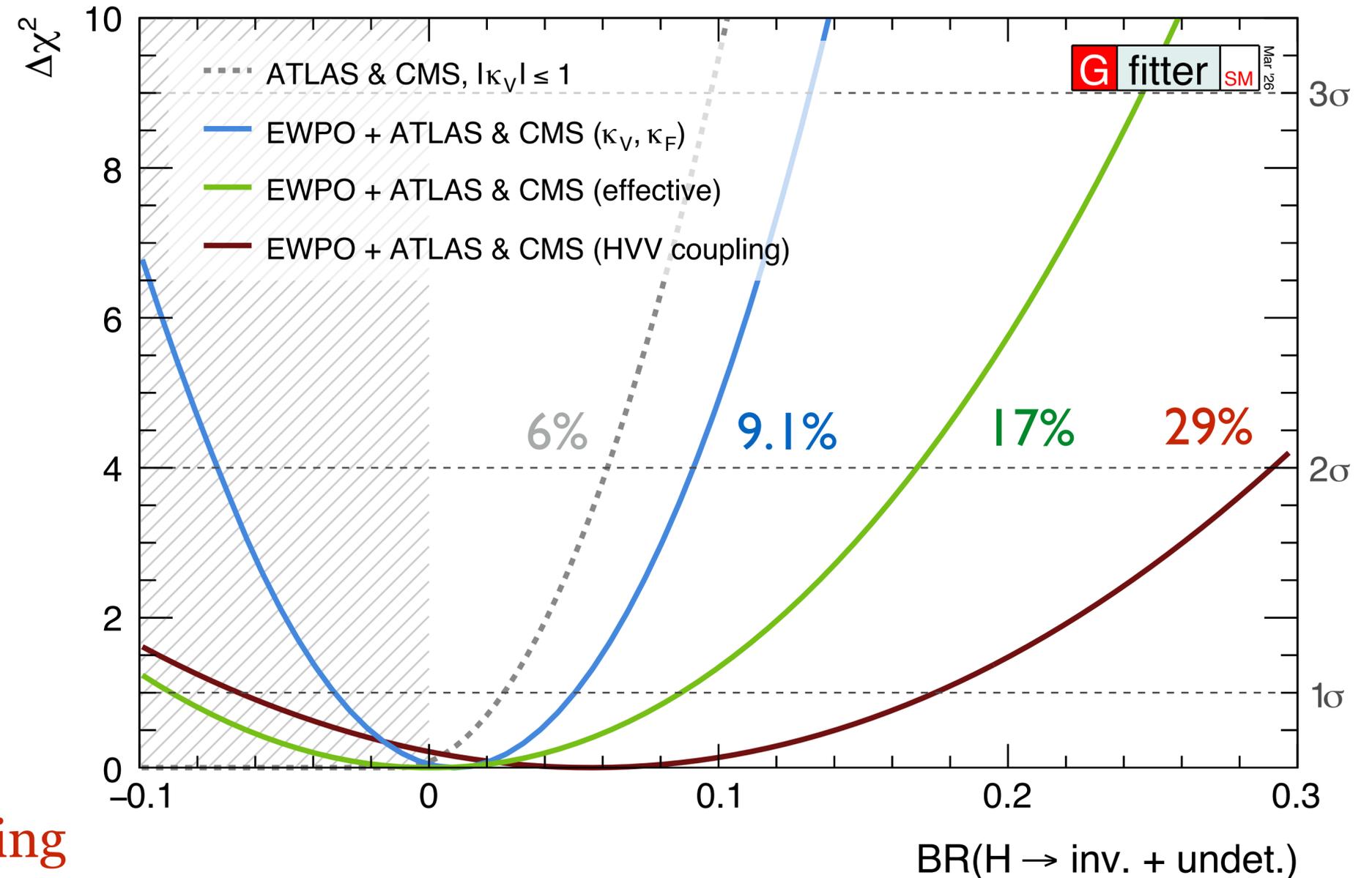
where  $\Gamma_H = \Gamma(\kappa) + \Gamma_{BSM}$

the visible widths are scaled with  $\kappa_i$

- ▶ Constraint on  $\kappa_V$  from EWPO
  - Less model-dependent than  $\kappa_V \leq 1$
  - Constrain  $\Gamma_{BSM}$  using  $\mu s$  only
- ▶ 95% CL limits:

$BR(H \rightarrow BSM) < 0.29$  for HVV coupling

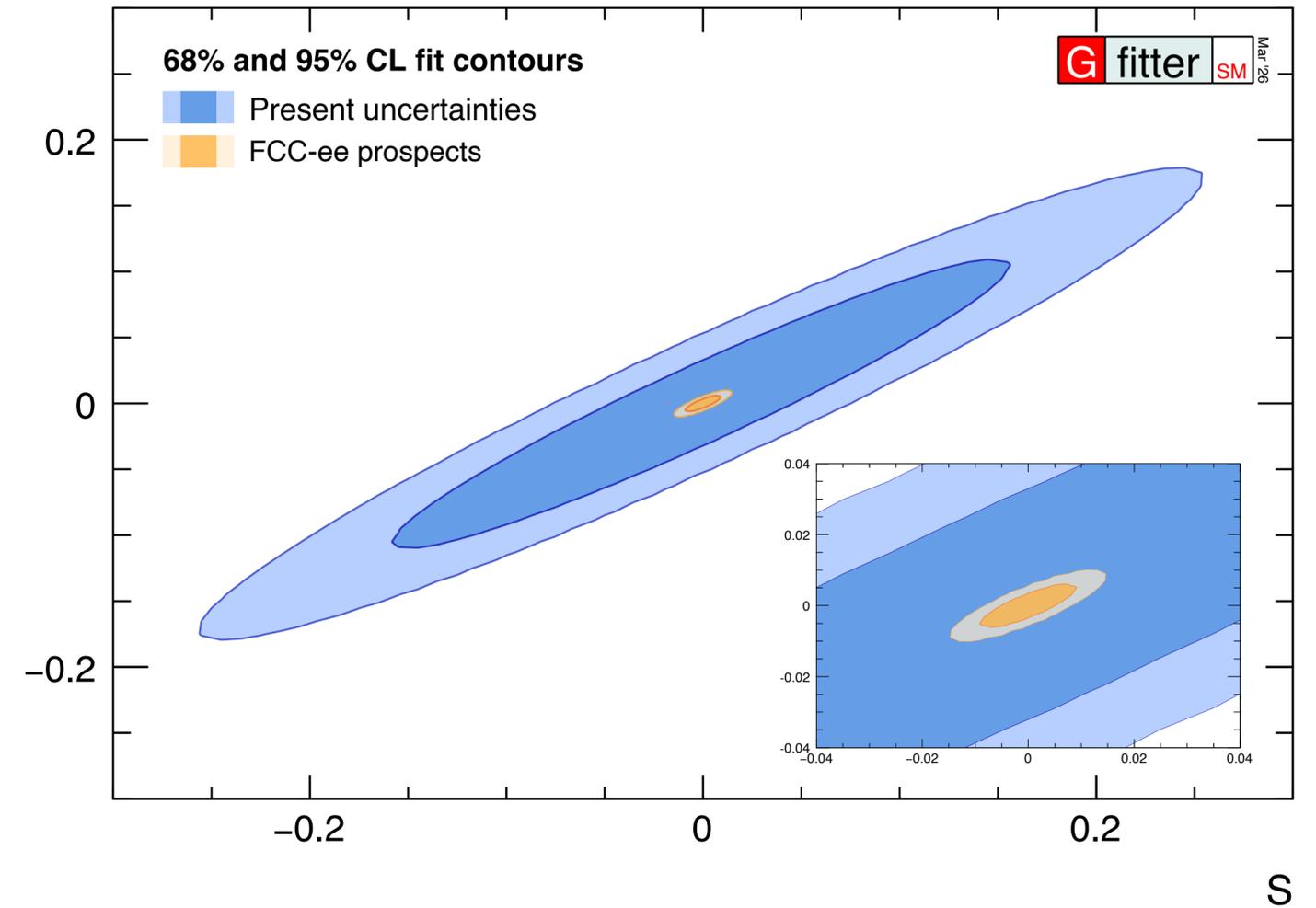
$BR(H \rightarrow BSM) < 0.17$  for effective coupling



# Future: FCC-ee

## Estimate precision of FCC-ee

- ▶ Uncertainties in EWPOs and Higgs boson measurements
  - Physics Briefing Book [ESPP, CERN YRM 8 (2025)]
  - Higgs at future colliders and updates [J de Blas et al., JHEP 01, 139 (2020)] [M Selvaggi et al., ESPP Input (2025)]
- ▶ Assume *conservative* theory uncertainties



Parameter	Present		FCC-ee	
	indirect	direct	indirect	direct
$\delta m_t$ [GeV]	$\pm 1.6$	$\pm 0.6$	$\pm 0.1$	$\pm 0.04$
$\delta M_H$ [GeV]	$^{+22}_{-19}$	$\pm 0.1$	$^{+2.4}_{-2.3}$	$\pm 0.004$
$\delta M_W$ [MeV]	$\pm 6$	$\pm 8.5$	$\pm 1.1$	$\pm 0.24$
$\delta \sin^2 \theta_{\text{eff}}^\ell (\times 10^{-5})$	$\pm 5$	$\pm 16$	$\pm 2$	$\pm 0.1$
$\delta \alpha_s(M_Z^2) (\times 10^{-2})$	$\pm 28$	$\pm 9$	$\pm 1.2$	
$\delta \Delta \alpha_{\text{had}}(M_Z^2) (\times 10^{-5})$	$\pm 33$	$\pm 10$	$\pm 3$	$\pm 3$

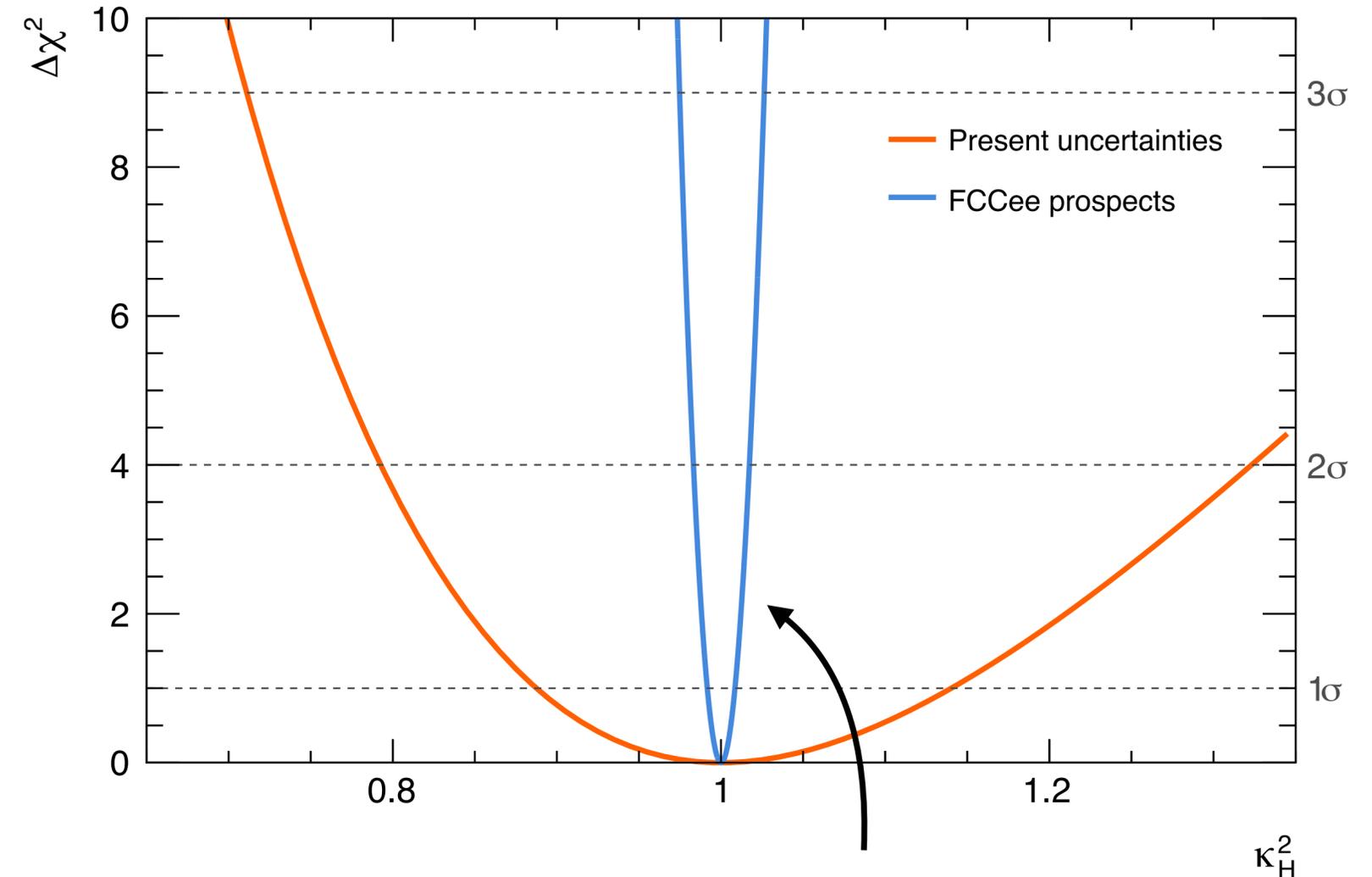
# $\Gamma_H$ at the FCC-ee

## HVV coupling from EWPO

- ▶  $\delta\kappa_V = 0.1\%$ 
  - $\mathcal{O}(10)$  improvement to present
- ▶ Combine  $\delta\kappa_V$  constraint with  $ZH(WW)$  and  $ZH(ZZ)$  measurements at FCC-ee

$\sqrt{s}$	240 GeV	
channel	ZH	WW $\rightarrow$ H
ZH $\rightarrow$ any	$\pm 0.31$	
$\gamma H \rightarrow$ any	$\pm 150$	
H $\rightarrow$ bb	$\pm 0.21$	$\pm 1.9$
H $\rightarrow$ cc	$\pm 1.6$	$\pm 19$
H $\rightarrow$ ss	$\pm 120$	$\pm 990$
H $\rightarrow$ gg	$\pm 0.80$	$\pm 5.5$
H $\rightarrow$ $\tau\tau$	$\pm 0.58$	
H $\rightarrow$ $\mu\mu$	$\pm 11$	
H $\rightarrow$ WW*	$\pm 0.80$	
H $\rightarrow$ ZZ*	$\pm 2.5$	
H $\rightarrow$ $\gamma\gamma$	$\pm 3.6$	
H $\rightarrow$ Z $\gamma$	$\pm 11.8$	

[M Selvaggi et al.,  
ESPP Input (2025)]



EWPO +  $H \rightarrow VV^*$ :  $\delta\kappa_H = 0.8\%$  at FCC-ee

Recoil-mass technique:  $\delta\Gamma_H \approx 1\%$

[A Blondel, P Janot, EPJ Plus 137, 92 (2022)]

# Summary

## SM is healthier than ever

- ▶ While we have the highest precision we have ever had
- ▶ SM predicts  $M_H = 110 \pm 18$  GeV

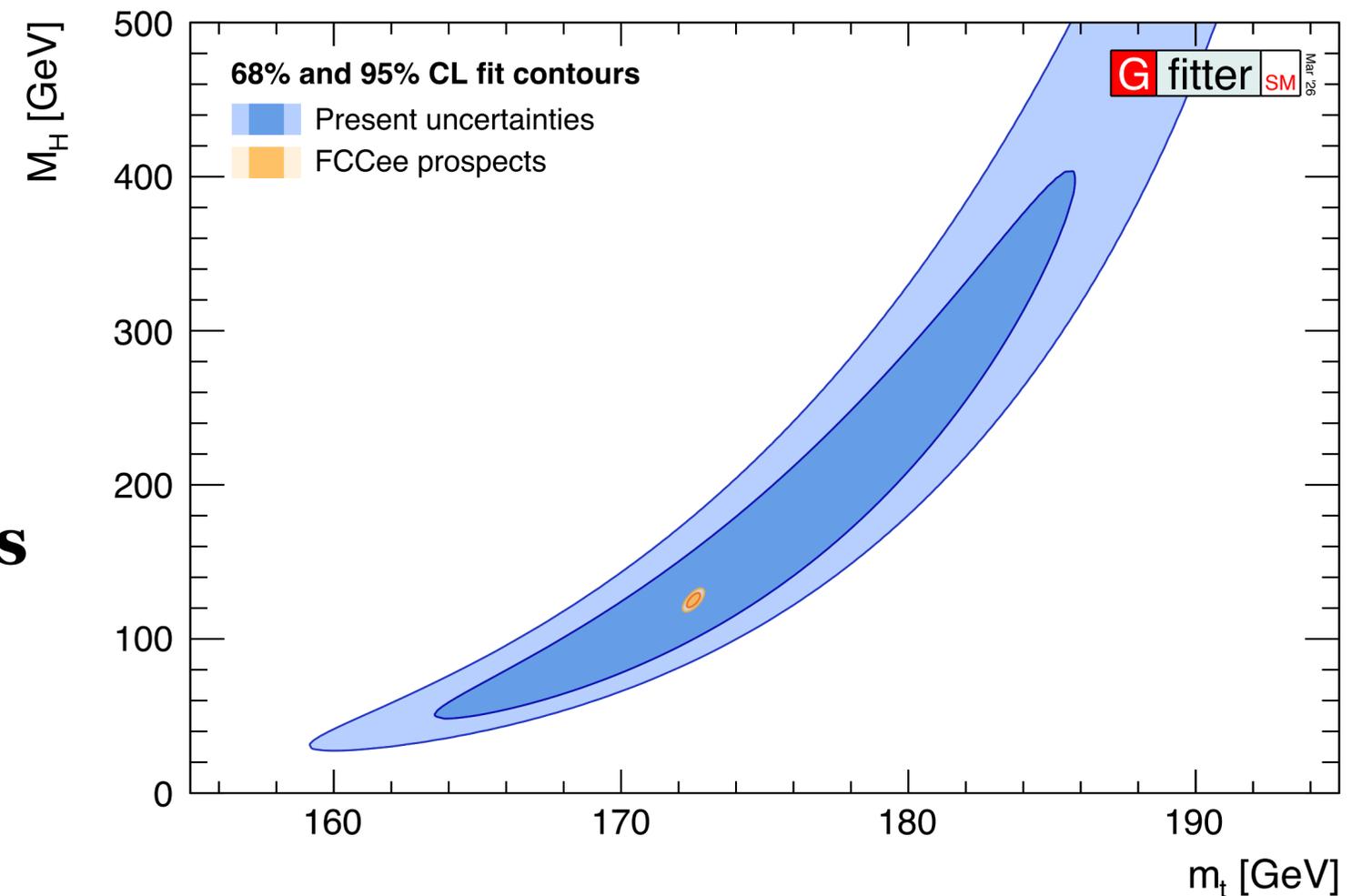
## EWPO and LHC Higgs measurements

- ▶ HVV coupling known to 1% precision
- ▶  $\delta\Gamma_H \approx 10\%$  with minimal assumptions!
- ▶  $\text{BR}(H \rightarrow \text{inv.} + \text{undet.}) < 17\%$  at 95% CL

## FCC-ee provides extraordinary capabilities

- ▶ HVV coupling with 0.1% from EWPO
- ▶ Indirect constraint on  $\Gamma_H$  about 1%

(conservative estimates)



# Additional Material

# Effective Weak Mixing Angle Combination

## Combination of $\sin^2(\theta_{\text{eff}}^l)$ measurements:

- + Tevatron combination [1801.06283]
- + ATLAS 7 TeV (1503.03709)
- + ATLAS 8 TeV (ATLAS-CONF-2018-037)
- + CMS 8 TeV [1806.00863]
- + LHCb 7+8 TeV [1509.07645]
- + *LHCb 13 TeV* [2410.02502]
- + *CMS 13 TeV* [2408.07622]

## Assumptions

Correlate PDF unc: 100% between ATLAS/CMS

50-75% for different  $\sqrt{s}$  at LHC

25% between Tev/ATLAS-CMS

0-25% between LHCb/ATLAS-CMS

0% between Tev/LHCb

$$\sin^2(\theta_{\text{eff}}^l) = \mathbf{0.23149} \pm \mathbf{0.00021} \quad (\chi^2/\text{ndf} = 1.3/6)$$

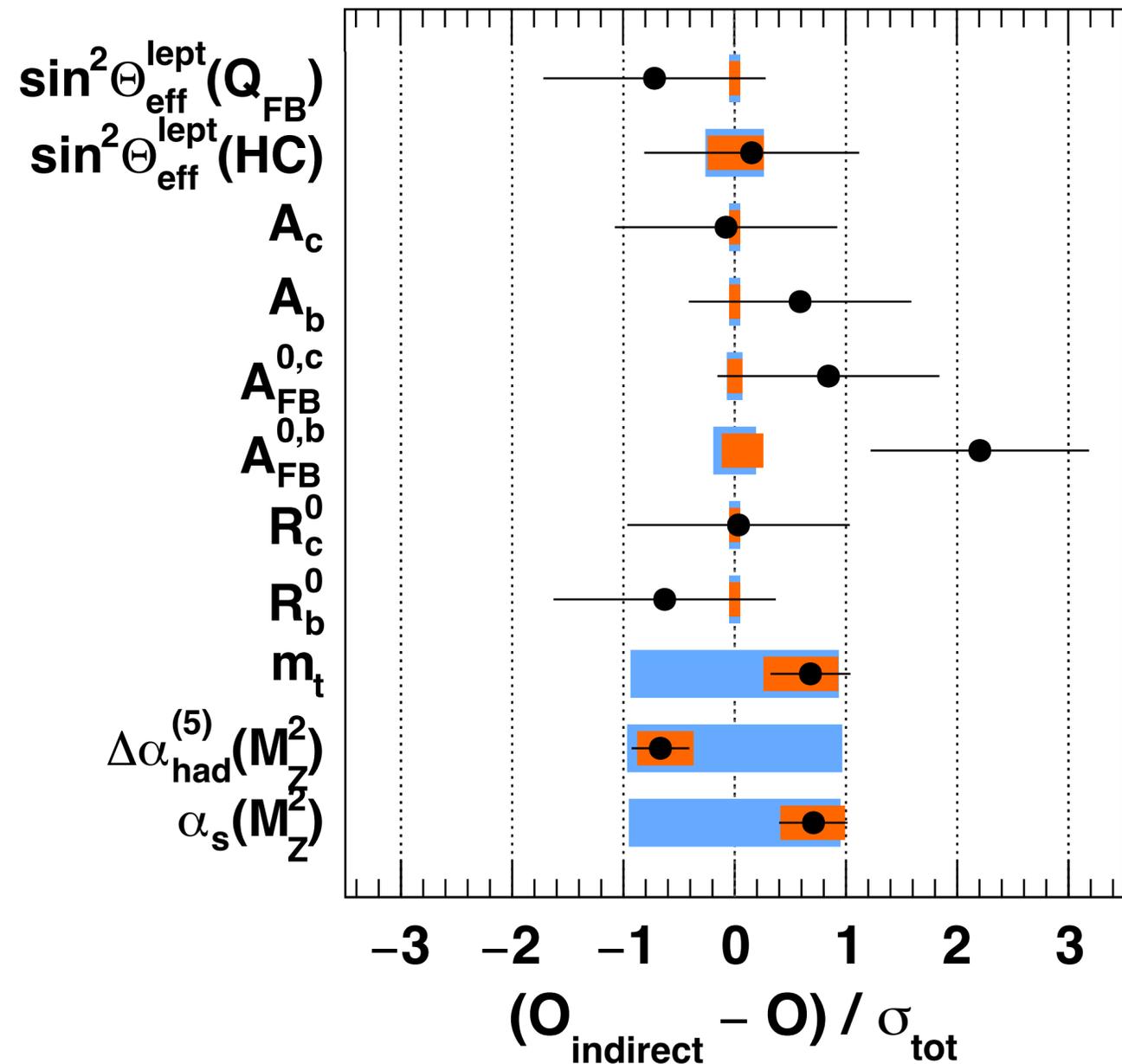
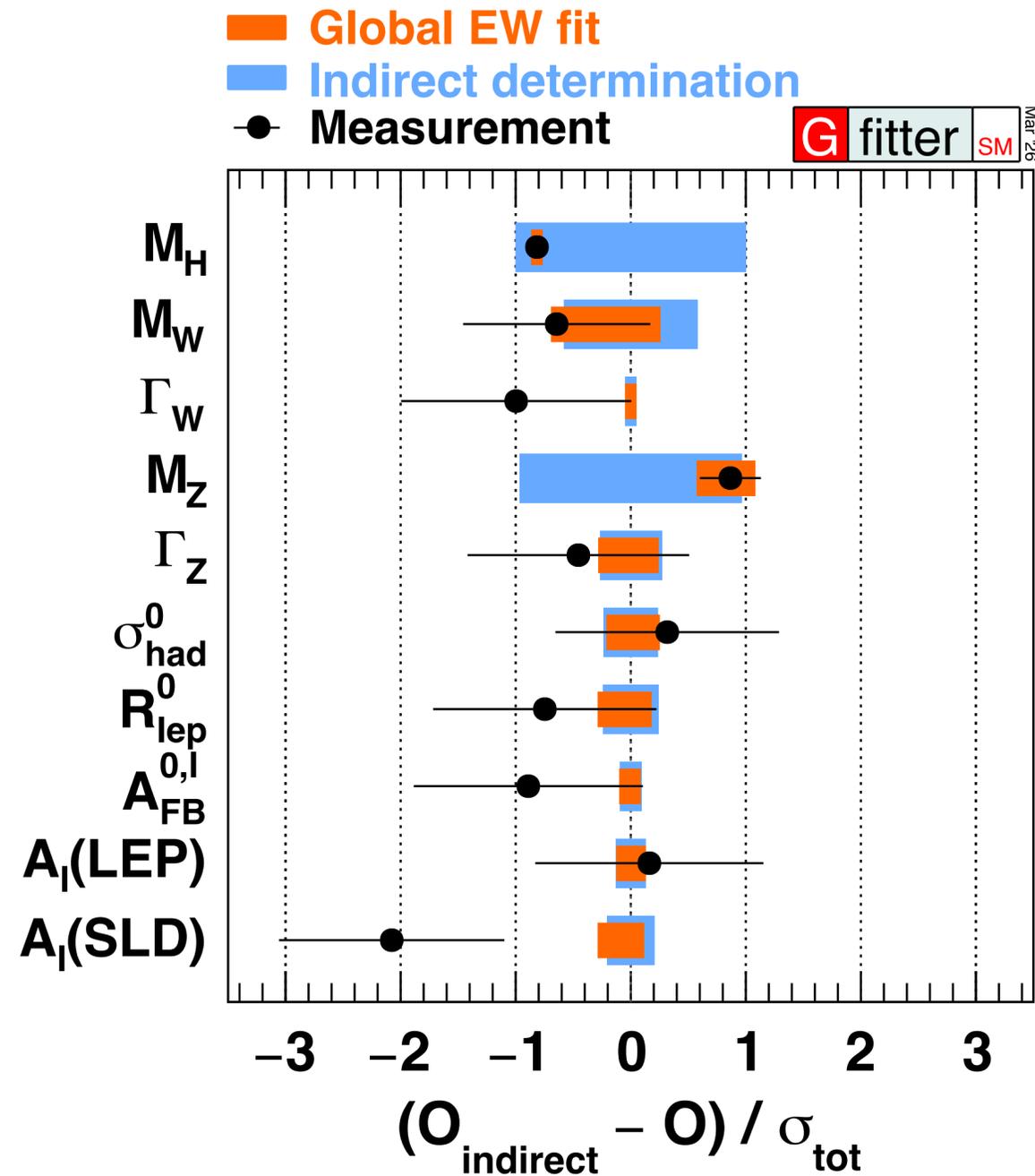
Uncertainty of 0.00017 for no correlation

# Complete SM Fit Results

Parameter	Input value	Free in fit	Fit Result	w/o exp. input in line	w/o exp. input in line, no theo. unc
$M_H$ [GeV]	$125.1 \pm 0.1$	yes	$125.1^{+0.1}_{-0.1}$	$110.1^{+19.5}_{-17.2}$	$110.3^{+17.2}_{-15.4}$
$M_W$ [GeV]	$80.363 \pm 0.009$	–	$80.358 \pm 0.005$	$80.356 \pm 0.006$	$80.356 \pm 0.004$
$\Gamma_W$ [GeV]	$2.140 \pm 0.050$	–	$2.090 \pm 0.001$	$2.090 \pm 0.001$	$2.090 \pm 0.000$
$M_Z$ [GeV]	$91.1880 \pm 0.0020$	yes	$91.1883 \pm 0.0019$	$91.1945 \pm 0.0073$	$91.1944 \pm 0.0064$
$\Gamma_Z$ [GeV]	$2.4955 \pm 0.0023$	–	$2.4945 \pm 0.0006$	$2.4944 \pm 0.0006$	$2.4944 \pm 0.0005$
$\sigma_{\text{had}}^0$ [nb]	$41.480 \pm 0.033$	–	$41.490 \pm 0.008$	$41.491 \pm 0.008$	$41.491 \pm 0.005$
$R_\ell^0$	$20.767 \pm 0.025$	–	$20.749 \pm 0.006$	$20.748 \pm 0.006$	$20.748 \pm 0.005$
$A_{\text{FB}}^{0,\ell}$	$0.0171 \pm 0.0010$	–	$0.01621 \pm 0.0001$	$0.01621 \pm 0.0001$	$0.01620 \pm 0.0001$
$A_\ell^{(*)}$	$0.1499 \pm 0.0018$	–	$0.1470 \pm 0.0004$	$0.1470 \pm 0.0004$	$0.1470 \pm 0.0003$
$\sin^2\theta_{\text{eff}}^\ell(Q_{\text{FB}})$	$0.2324 \pm 0.0012$	–	$0.23152 \pm 0.00005$	$0.23152 \pm 0.00005$	$0.23152 \pm 0.00003$
$\sin^2\theta_{\text{eff}}^\ell(\text{HC})$	$0.23149 \pm 0.00021$	–	$0.23152 \pm 0.00005$	$0.23152 \pm 0.00006$	$0.23153 \pm 0.00003$
$A_s$	$0.895 \pm 0.091$	–	$0.9357 \pm 0.00003$	$0.9357 \pm 0.00003$	$0.9357 \pm 0.00002$
$A_c$	$0.670 \pm 0.027$	–	$0.6679 \pm 0.00019$	$0.6679 \pm 0.00019$	$0.6679 \pm 0.00012$
$A_b$	$0.923 \pm 0.020$	–	$0.93475 \pm 0.00003$	$0.93475 \pm 0.00003$	$0.93475 \pm 0.00002$
$A_{\text{FB}}^{0,c}$	$0.0707 \pm 0.0035$	–	$0.0737 \pm 0.0002$	$0.0737 \pm 0.0002$	$0.0736 \pm 0.0001$
$A_{\text{FB}}^{0,b}$	$0.0996 \pm 0.0016$	–	$0.1031 \pm 0.0003$	$0.1032 \pm 0.0003$	$0.1031 \pm 0.0002$
$R_c^0$	$0.1721 \pm 0.0030$	–	$0.17220 \pm 0.00003$	$0.17220 \pm 0.00003$	$0.17220 \pm 0.00002$
$R_b^0$	$0.21629 \pm 0.00066$	–	$0.21587 \pm 0.00003$	$0.21587 \pm 0.00003$	$0.21588 \pm 0.00001$
$\bar{m}_c$ [GeV]	$1.273 \pm 0.003$	yes	$1.273 \pm 0.003$	–	–
$\bar{m}_b$ [GeV]	$4.183 \pm 0.004$	yes	$4.183 \pm 0.004$	–	–
$m_t$ [GeV] <sup>(∇)</sup>	$172.52 \pm 0.60$	yes	$172.67 \pm 0.56$	$173.66^{+1.55}_{-1.56}$	$173.67^{+1.43}_{-1.44}$
$\Delta\alpha_{\text{had}}^{(5)}(M_Z^2)$ <sup>(†Δ)</sup>	$2758 \pm 10$	yes	$2757 \pm 9$	$2735 \pm 34$	$2735 \pm 30$
$\alpha_s(M_Z^2)$	$0.1177 \pm 0.0009$	yes	$0.1179 \pm 0.0009$	$0.1200 \pm 0.0028$	$0.1198 \pm 0.0027$

(\*) Average of LEP ( $A_\ell = 0.1465 \pm 0.0033$ ) and SLD ( $A_\ell = 0.1513 \pm 0.0021$ ) measurements, used as two measurements in the fit. The fit w/o the LEP (SLD) measurement gives  $A_\ell = 0.1470 \pm 0.0004$  ( $A_\ell = 0.1468 \pm 0.0004$ ). <sup>(∇)</sup>Combination of experimental (0.331059 GeV) and theory uncertainty (0.5 GeV). <sup>(†)</sup>In units of  $10^{-5}$ . <sup>(Δ)</sup>Rescaled due to  $\alpha_s$  dependency.

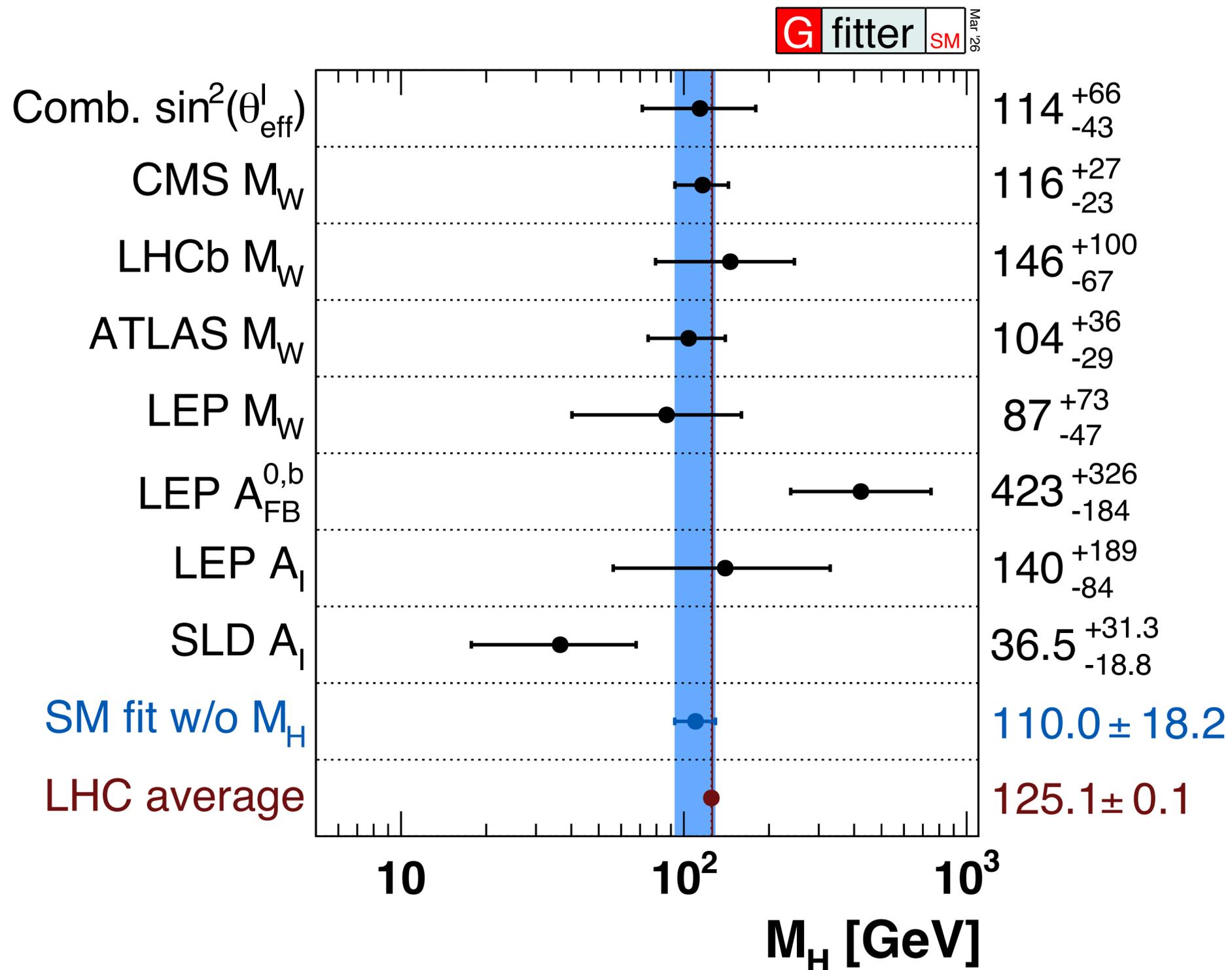
# Complete SM Fit Results



# Predicting $M_H$

## Prediction of $M_H$ with only a single observable

- ▶ weak mixing angle and  $M_W$  predict  $M_H$  to be closer to 125 GeV than before
- ▶ long-standing tension between  $A_{bFB}^0$  and  $A_\ell$ (SLD) visible



# $\alpha_s$ Consistency Improved

## Complete fit:

$$\alpha_s(M_Z^2) = 0.1200 \pm 0.0028$$

## Individual fits:

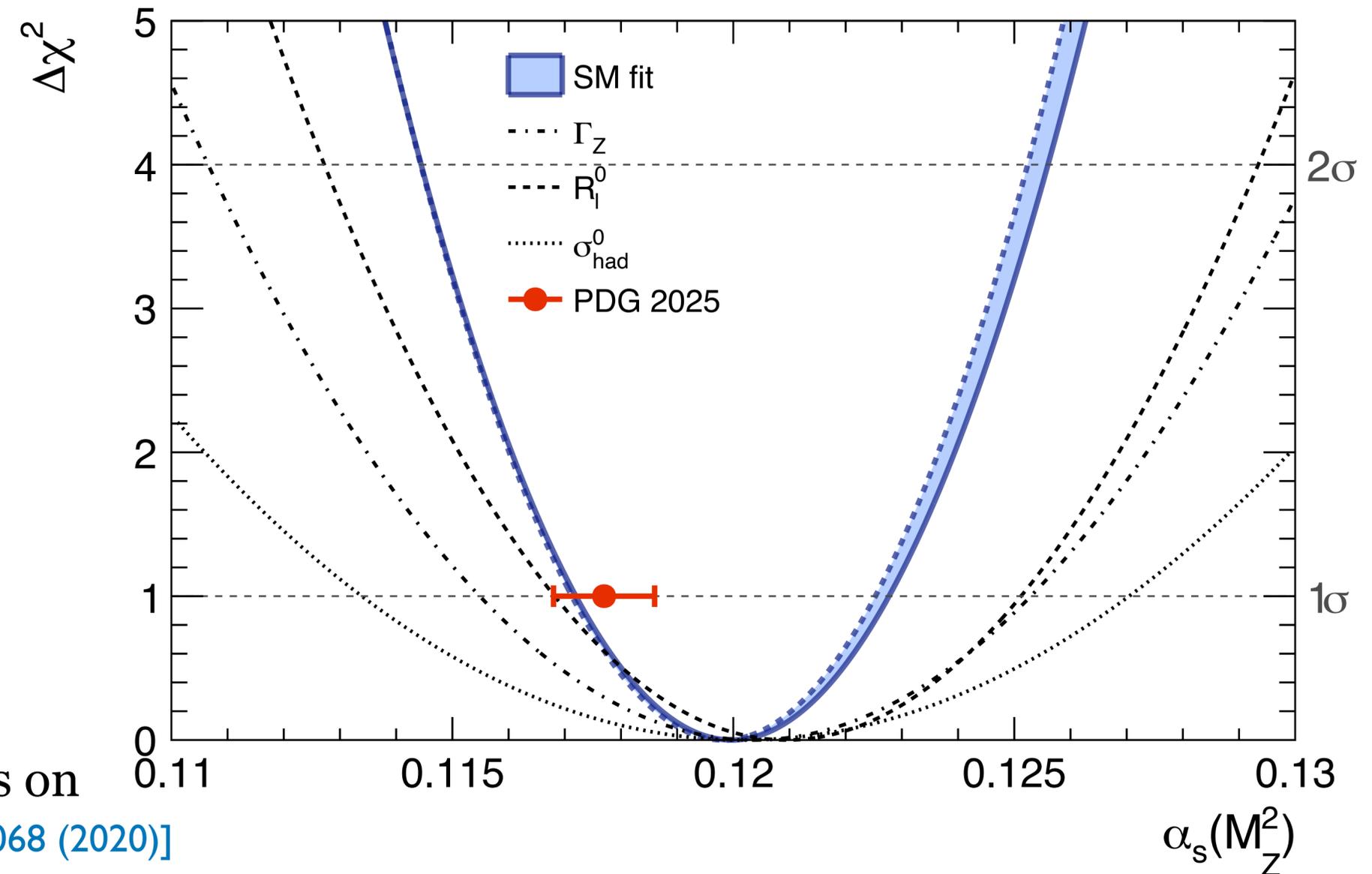
$$R_\ell : \alpha_s(M_Z^2) = 0.1211 \pm 0.0042,$$

$$\Gamma_Z : \alpha_s(M_Z^2) = 0.1214 \pm 0.0049,$$

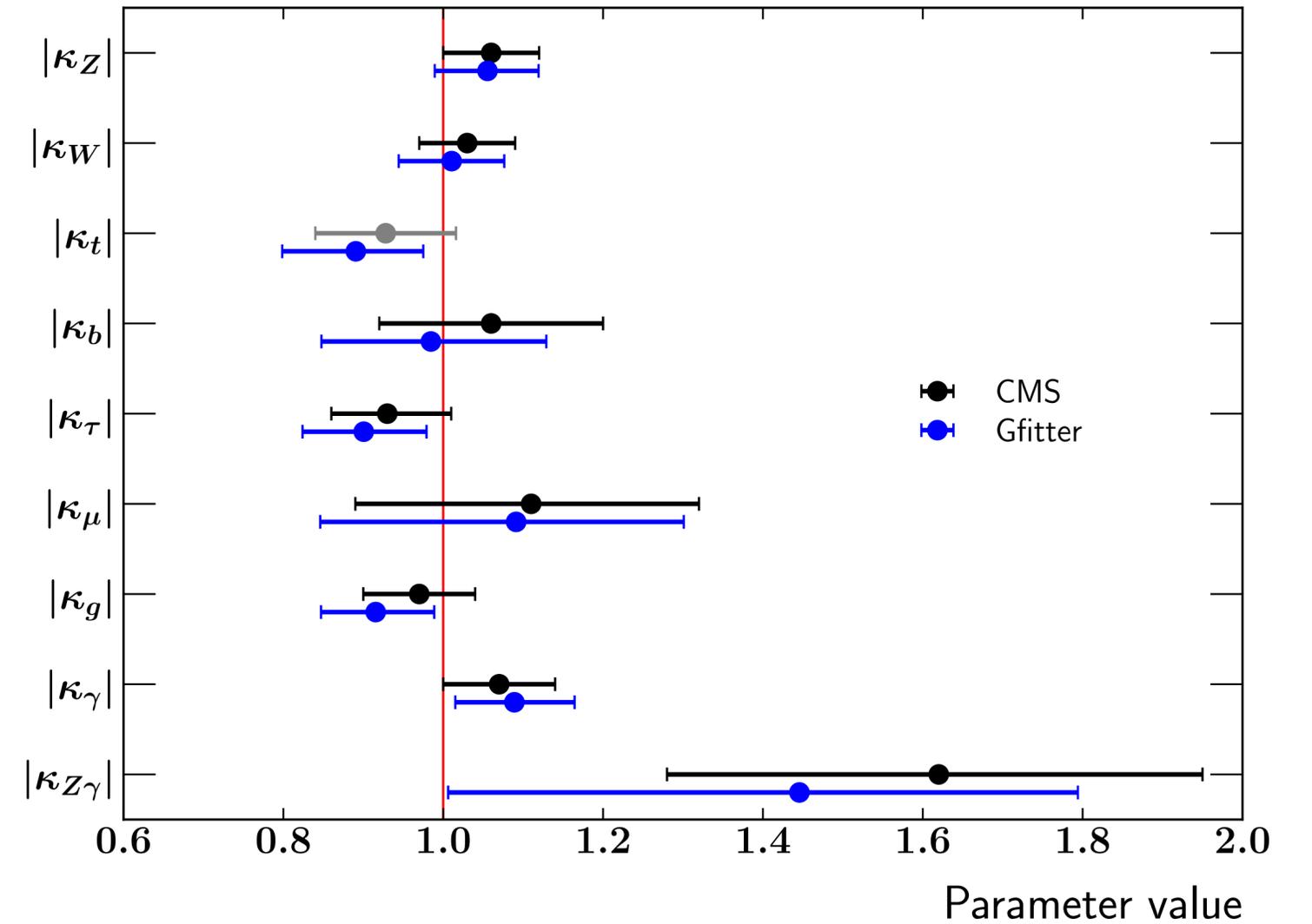
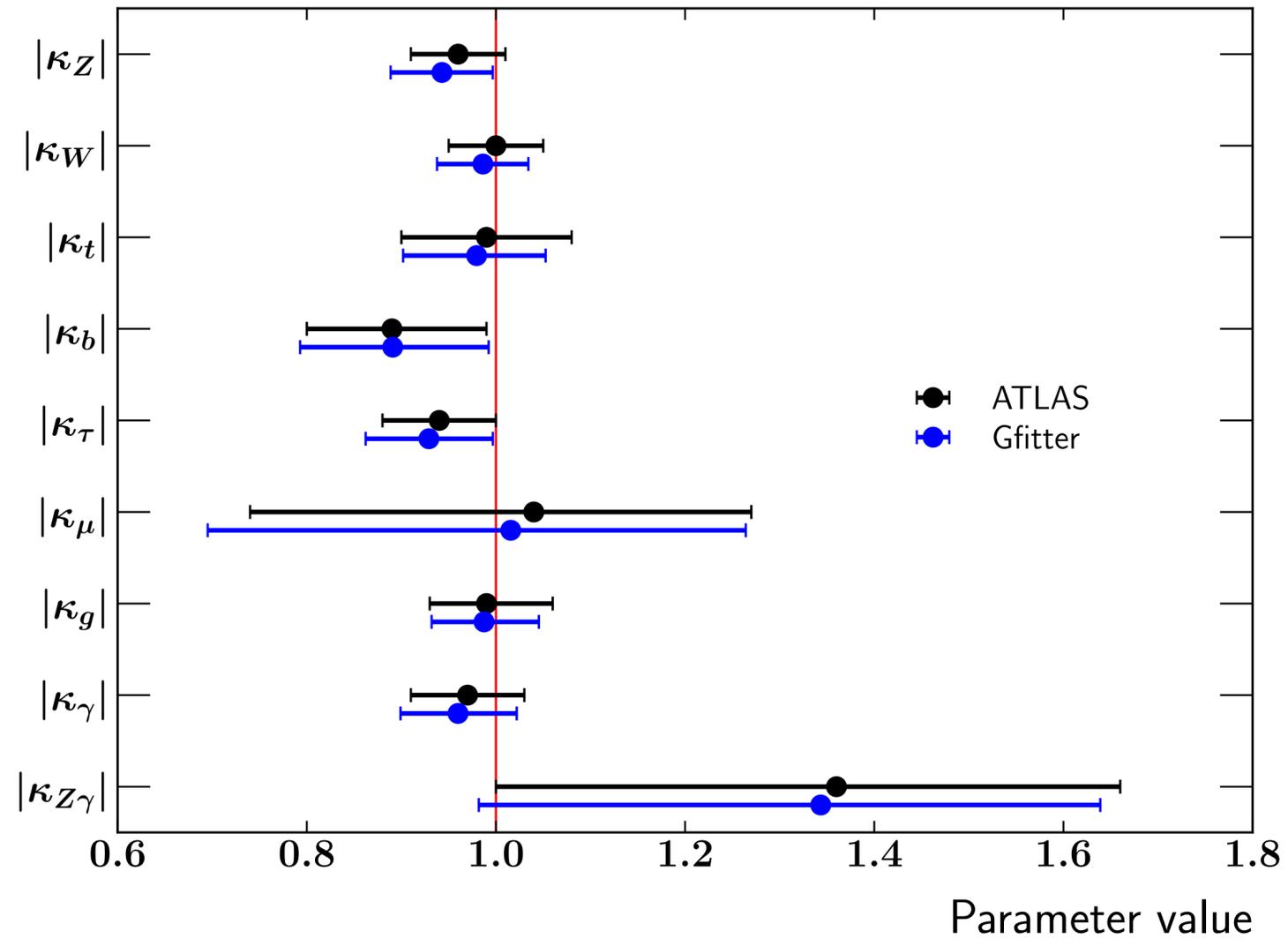
$$\sigma_{\text{had}} : \alpha_s(M_Z^2) = 0.1199 \pm 0.0068,$$

## Because of

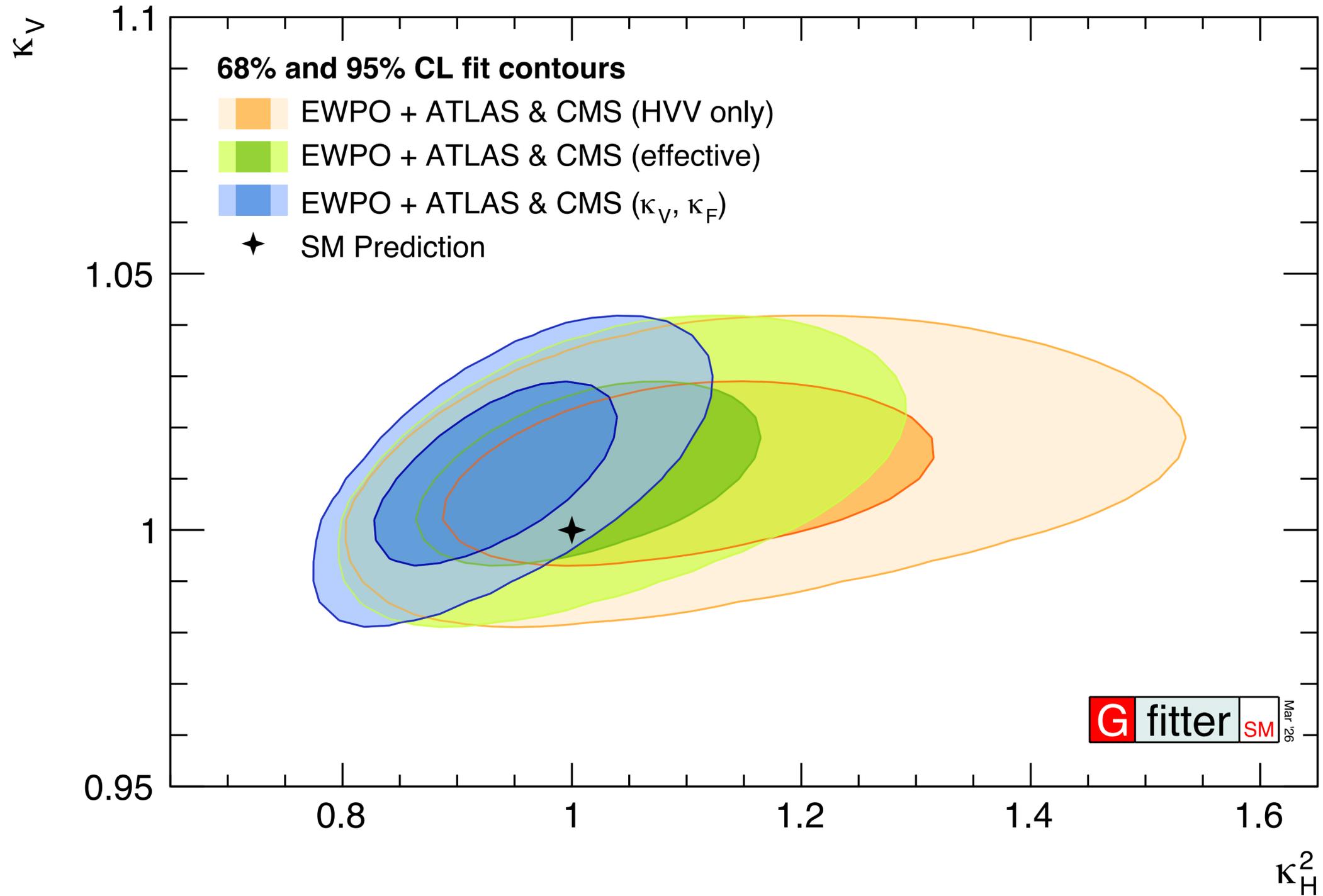
- ▶ Updated calculations of beam-beam effects on the LEP luminosity [Voutsinas et al, PLB 800, 135068 (2020)]
- ▶ Updated Bhabha cross section [Janot, Jadach, PLB 803 (2020) 135319]



# $\kappa$ Consistency Check



# The Higgs Boson Width



# FCCee Fit Setup

- ▶ Use EWPO uncertainty estimates from Physics Briefing Book [ESPP, CERN YRM 8 (2025)]
- ▶ Add projections for  $m_H$  and  $m_t$
- ▶ Adjust central values of EWPO for perfect fit with  $\chi^2 = 0$
- ▶ Conservative theory uncertainty estimates, about 1/4 of present uncertainties
- ▶ Estimate present uncertainties with same setup, but current uncertainties in EWPO

Observable	Current	FCC-ee
$\Delta m_Z$ (keV)	2000	4 (100)
$\Delta \Gamma_Z$ (keV)	2300	4 (12)
$\delta R_\mu (\times 10^{-6})$ $R_\mu \equiv \frac{\Gamma_{\text{had}}}{\Gamma_\mu}$	1600	2.4 (2.3)
$\delta R_b (\times 10^{-6})$ $R_b \equiv \frac{\Gamma_b}{\Gamma_{\text{had}}}$	3300	1.2 (1.6)
$\Delta \sin^2 \theta_W (\times 10^6)$	130	0.4 (0.5)
$\Delta \alpha(m_Z)^{-1} (\times 10^3)$	14	0.8, 3.8
$\Delta m_W$ (keV)	9900	180 (160)
$\Delta \Gamma_W$ (keV)	42000	270 (200)

# Radiative Corrections

## Modifications of Propagators and Vertices

### ▶ QED corrections

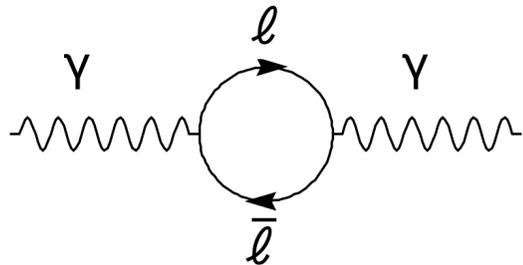
- leptonic loop insertions
  - calculable to high precision
- quark loop insertions (hadronic)
  - partially not calculable in pure pQCD

### ▶ Weak corrections

- Insertion of fermion loops
  - high sensitivity to  $m_f$  (if  $m_f \gg m_W$ )
- Insertion of boson loops
  - logarithmic sensitivity to  $M_H$

### ▶ QCD corrections

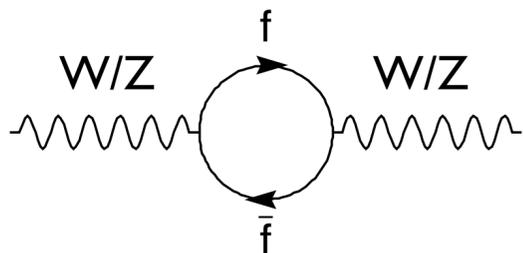
- Sensitivity to strong coupling
  - numerically small contribution ( $1 + \alpha_s/\pi$ )



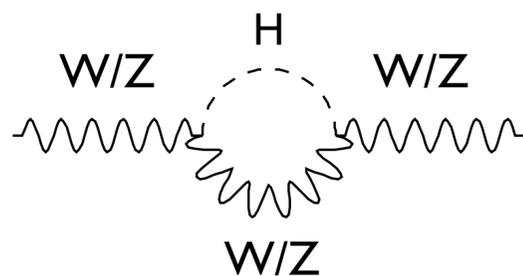
$$\propto \alpha \ln \frac{s}{m_\ell^2}$$



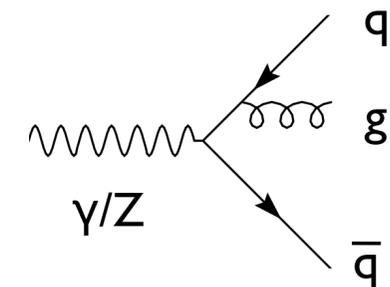
$$\propto \Delta\alpha_{\text{had}}(s)$$



$$\propto N_C m_f^2$$



$$\propto \ln \frac{M_H^2}{M_W^2}$$



$$\propto \alpha_s(s)$$

# Precision Calculations

## All observables calculated at 2-loop level

- ▶  $M_W$  : full EW one- and two-loop calculation of fermionic and bosonic contributions

[Awramik et al., PRD 69, 053006 (2004), PRL 89, 241801 (2002)]

+ 4-loop QCD correction [Chetyrkin et al., PRL 97, 102003 (2006)]

- ▶  $\sin^2\theta_{\text{eff}}^f$  : same order as  $M_W$ , calculations for leptons and all quark flavours

[Awramik et al, PRL 93, 201805 (2004), JHEP 11, 048 (2006), Nucl. Phys. B813, 174 (2009)]

- ▶ **Partial Z widths  $\Gamma_f$** : bosonic+fermionic corrections in two loops for

all flavours (includes predictions for  $\sigma^0_{\text{had}}$ ) [A. Freitas et al, PLB 730, 50 (2014), JHEP04, 070 (2014), PLB 783, 86 (2018), JHEP 1908, 113 (2019), JHEP 07, 210 (2020)]

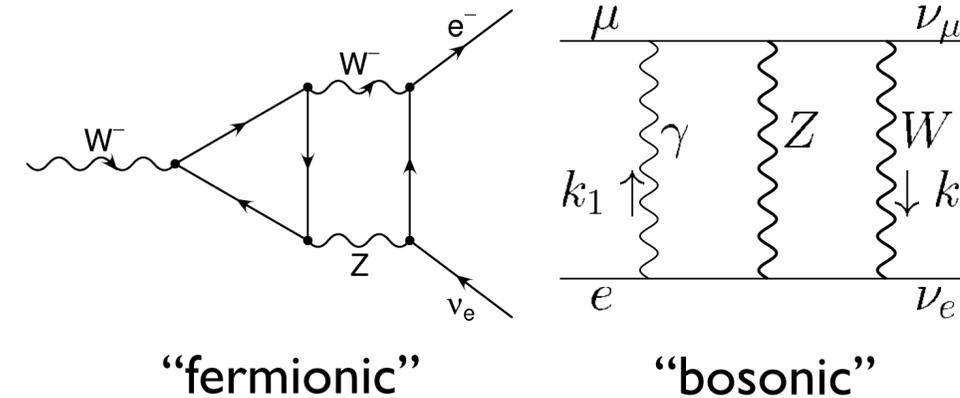
- ▶ **Radiator functions:** QCD corrections at N<sup>3</sup>LO

[Baikov et al., PRL 108, 222003 (2012)]

- ▶  $\Gamma_W$ : one-loop EW corrections available, negligible impact on fit

[Cho et al, JHEP 1111, 068 (2011)]

- ▶ **All calculations:** one- and two-loop QCD corrections and leading terms of higher order corrections



# Theoretical Uncertainties

▶ Estimated using **geometric series**

- $a_n = a r^n$ ,  
example: 
$$\mathcal{O}(\alpha^2 \alpha_s) = \frac{\mathcal{O}(\alpha^2)}{\mathcal{O}(\alpha)} \mathcal{O}(\alpha \alpha_s)$$

- similar results from scale variations
- **Reasonable estimates for all observables**

▶ **Exception:  $m_t$  !**

- MC parameter, translation to  $m_t^{\text{pole}}$  unknown

▶ **10 additional free parameters**

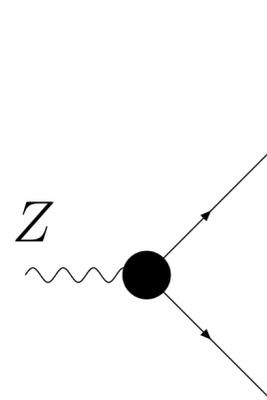
- Gaussian likelihood

▶ Important missing higher order terms:

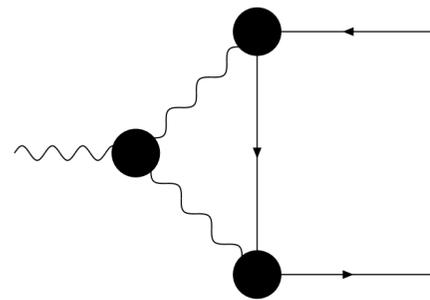
- $\mathcal{O}(\alpha^2 \alpha_s)$ ,  $\mathcal{O}(\alpha \alpha_s^2)$ ,  $\mathcal{O}(\alpha^3)$ ,  $\mathcal{O}(\alpha_s^5)$  (rad. functions)

Observable	Exp. error	<b>important</b> ↓ Theo. error
$M_W$	8.5 MeV	4 MeV
$\sin^2 \theta_{\text{eff}}^l$	$1.6 \cdot 10^{-4}$	$0.5 \cdot 10^{-4}$
$\Gamma_Z$	2.3 MeV	0.5 MeV
$\sigma_{\text{had}}^0$	37 pb	6 pb
$R_b^0$	$6.6 \cdot 10^{-4}$	$1.5 \cdot 10^{-4}$
$m_t$	0.33 GeV	0.5 GeV

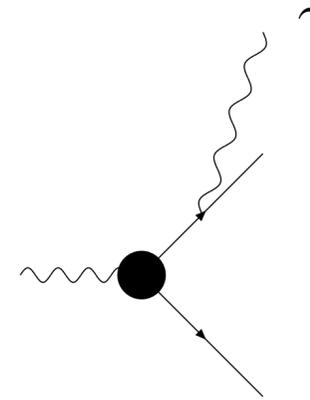
# SMEFT Contributions



LO



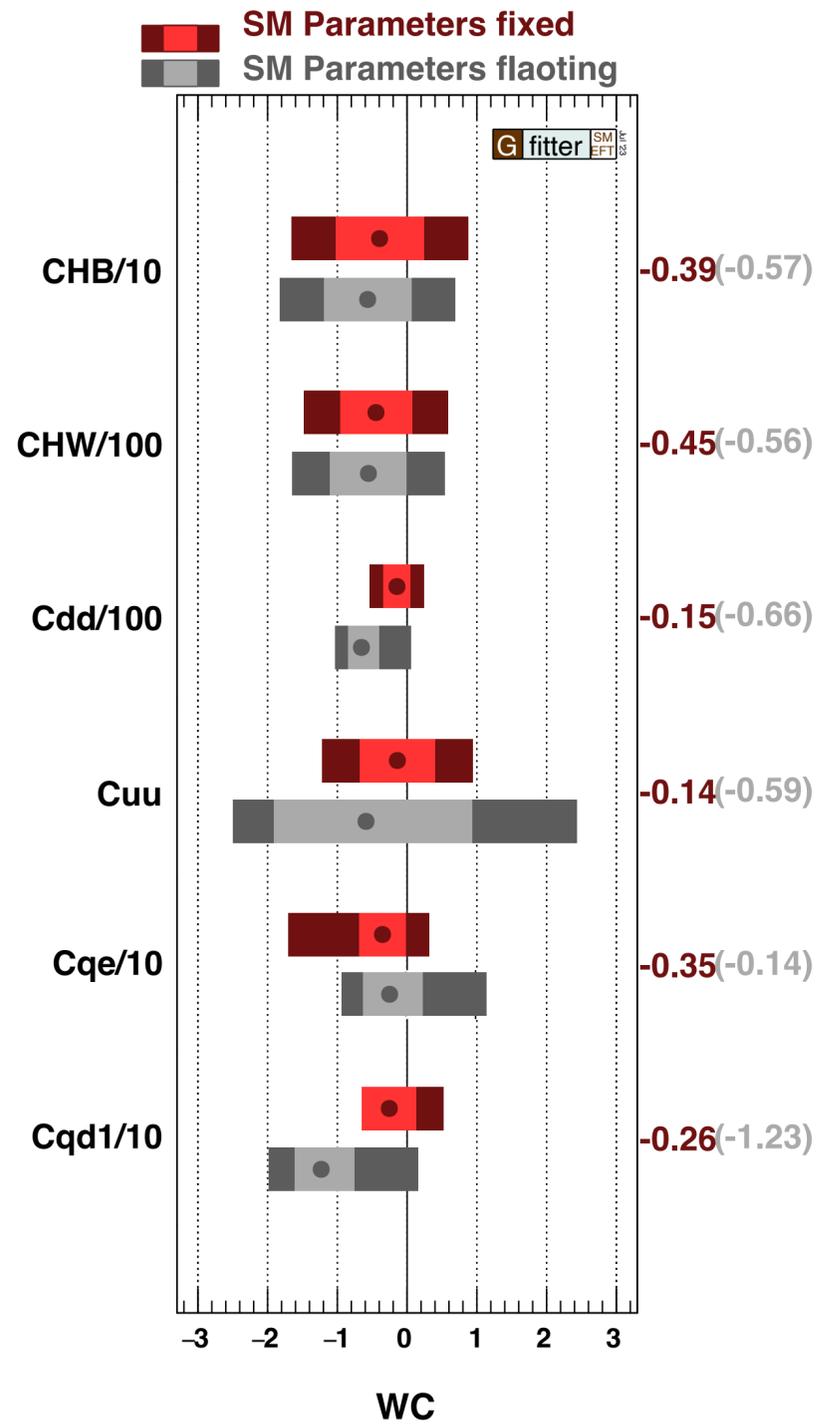
NLO virtual



NLO real

- Considering 32 flavour independent operators in Warsaw basis
  - 10 operators contributing at LO  $\mathcal{O}_{ll}, \mathcal{O}_{HWB}, \mathcal{O}_{HD}, \mathcal{O}_{He}, \mathcal{O}_{Hd}, \mathcal{O}_{Hu}, \mathcal{O}_{Hq}^{(3)}, \mathcal{O}_{Hq}^{(1)}, \mathcal{O}_{Hl}^{(3)}, \mathcal{O}_{Hl}^{(1)}$
  - 22 operators contributing at NLO:
    - 4 bosonic operators:  $\mathcal{O}_{\phi B}, \mathcal{O}_{\phi W}, \mathcal{O}_{\square}, \mathcal{O}_W$
    - 2 2-fermion operators:  $\mathcal{O}_{uB}[ij], \mathcal{O}_{uW}[ij]$
    - 16 4-fermion operators:  $\mathcal{O}_{ed}[ijkl], \mathcal{O}_{ee}[ijkl], \mathcal{O}_{eu}[ijkl], \mathcal{O}_{lu}[ijkl], \mathcal{O}_{ld}[ijkl], \mathcal{O}_{le}[ijkl], \mathcal{O}_{lq}^{(1)}[ijkl], \mathcal{O}_{lq}^{(3)}[ijkl]$   
 $\mathcal{O}_{qe}[ijkl], \mathcal{O}_{qd}^{(1)}[ijkl], \mathcal{O}_{qq}^{(3)}[ijkl], \mathcal{O}_{qq}^{(1)}[ijkl], \mathcal{O}_{qu}^{(1)}[ijkl], \mathcal{O}_{ud}^{(1)}[ijkl], \mathcal{O}_{uu}[ijkl], \mathcal{O}_{dd}[ijkl]$

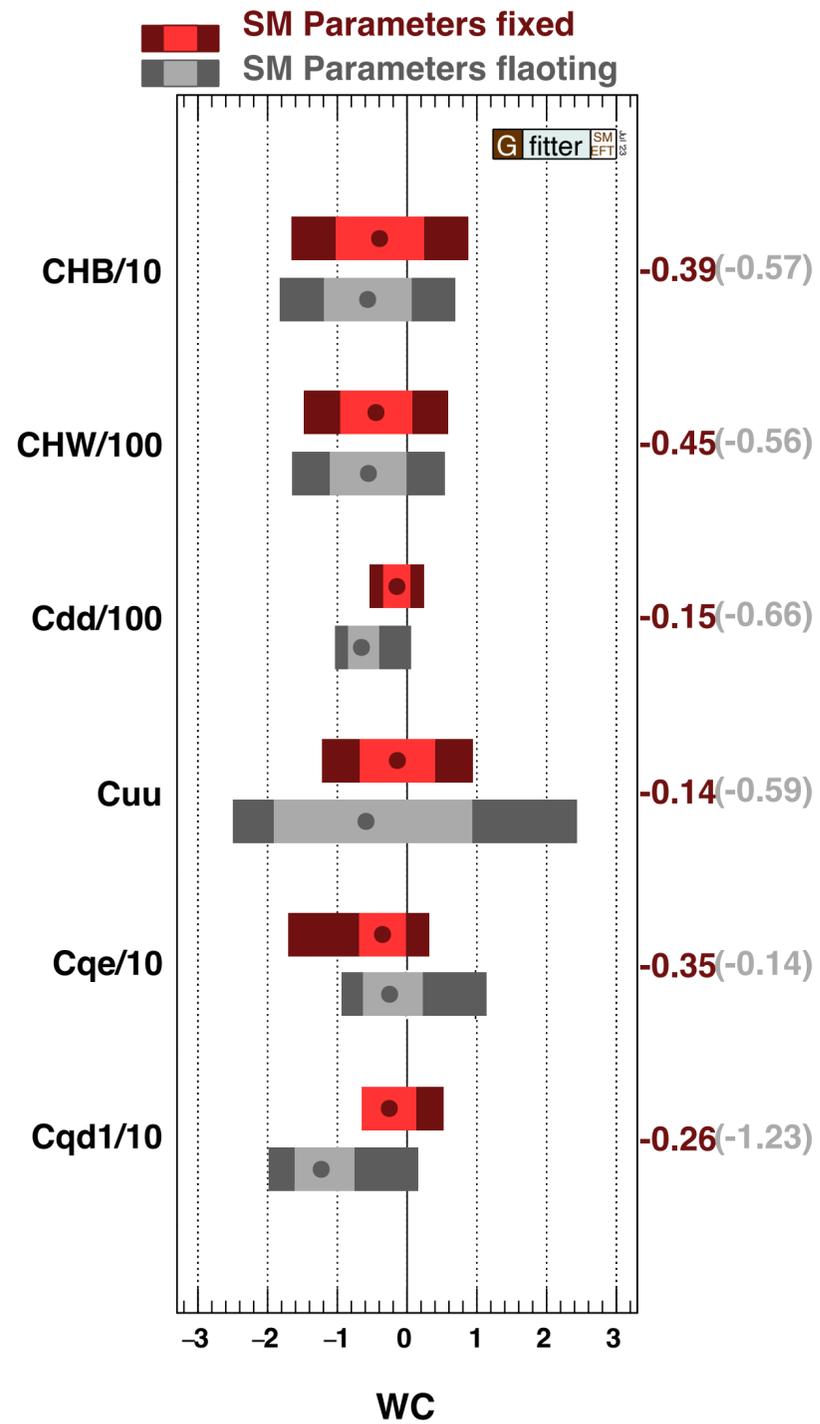
# SMEFT Fits



Effect of letting SM parameters floating in SMEFT fit



# SMEFT Fits



Effect of letting SM parameters floating in SMEFT fit

Simultaneous fit of down-quark couplings

