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## New directions in Kaon Physics

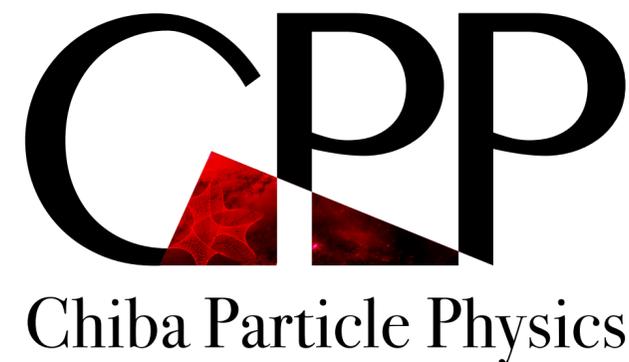
– Interference in  $K^0 \rightarrow \mu^+ \mu^-$  as a new golden mode –

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Teppei Kitahara (Chiba Univ., CPP)



The 60th Rencontres de Moriond EW 2026  
La Thuile, Italy  
March 17, 2026



Based on Marchevski, Martinez Santos + D'Ambrosio, Dery, Grossman, TK, Schacht, JHEP (2025)

$|V_{us}|$  vs unitarity (CAA)

$K \rightarrow \pi \ell \bar{\nu}$  tree-level CPC  
 $K^- \rightarrow \mu \bar{\nu}$

$\epsilon_K$  and  $\epsilon'$

$K_L \rightarrow \pi\pi$

FCNC and CPV

$K \rightarrow \pi \nu \bar{\nu}$

$K^0 \rightarrow \mu^+ \mu^-$

loop-level CPC  
Long-distance dominant  
just ultra-rare kaon decay...

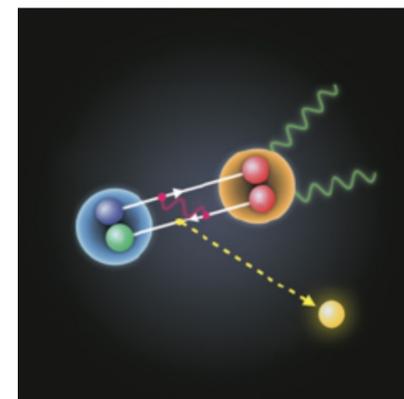
Correlation



B anomalies



$K \rightarrow \pi X?$





**New theoretical ideas**

$|V_{us}|$  vs unitarity (CAA)

$K \rightarrow \pi \ell \bar{\nu}$  tree-level CPC  
 $K^- \rightarrow \mu \bar{\nu}$

$\epsilon_K$  and  $\epsilon'$

$K_L \rightarrow \pi\pi$

FCNC and CPV

$K^0 \rightarrow \mu^+ \mu^-$

$K \rightarrow \pi \nu \bar{\nu}$



Sensitive to CPV when  $K_L^0 - K_S^0$  interference considered!



New idea in 2017

[D'Ambrosio, TK, PRL, [1707.06999](#)]

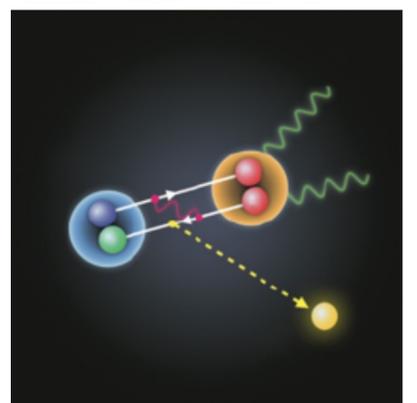


kaon unitarity triangle

[Dery, [2504.12386](#)]



$K \rightarrow \pi X?$

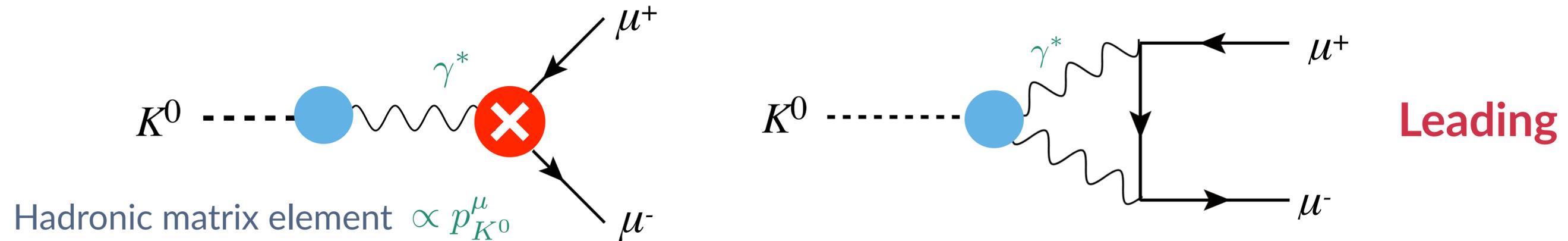


B anomalies

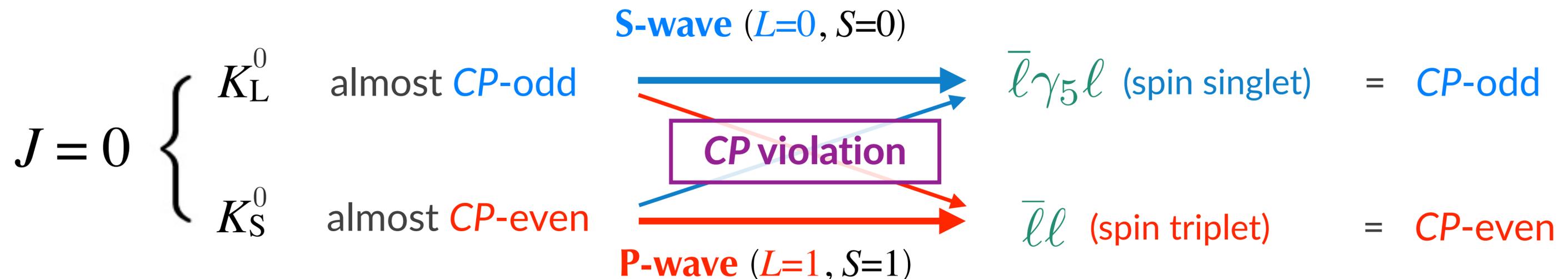


# Introduction to $K_{L/S}^0 \rightarrow \mu^+ \mu^-$

- Double-photon exchange is the leading contribution in  $K^0 \rightarrow \mu^+ \mu^-$

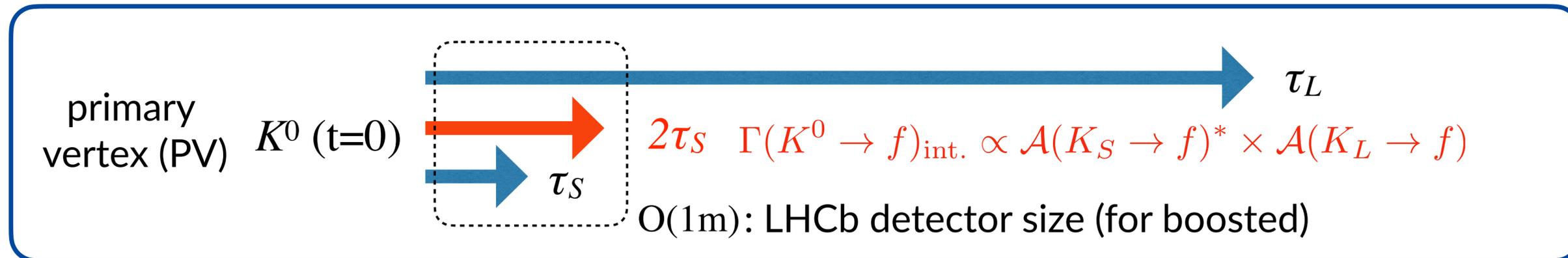


- Both CP-conserving and CP-violating contributions exist



# Interference between $K_L^0$ and $K_S^0$

- When the same final states exist in both  $K_L^0$  and  $K_S^0$  decays, the interference provides nonzero contributions:

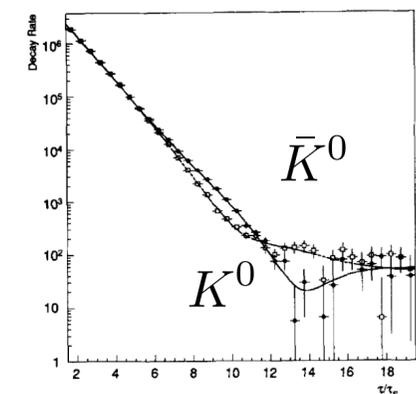
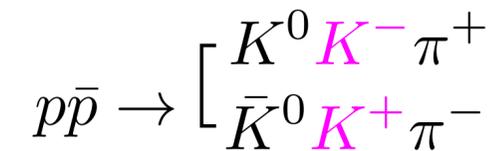


- Such an interference has been observed/utilized in many processes: e.g.,



cf. CPLEAR experiment@CERN)  $\{K_S, K_L\} \rightarrow \pi^+ \pi^-$

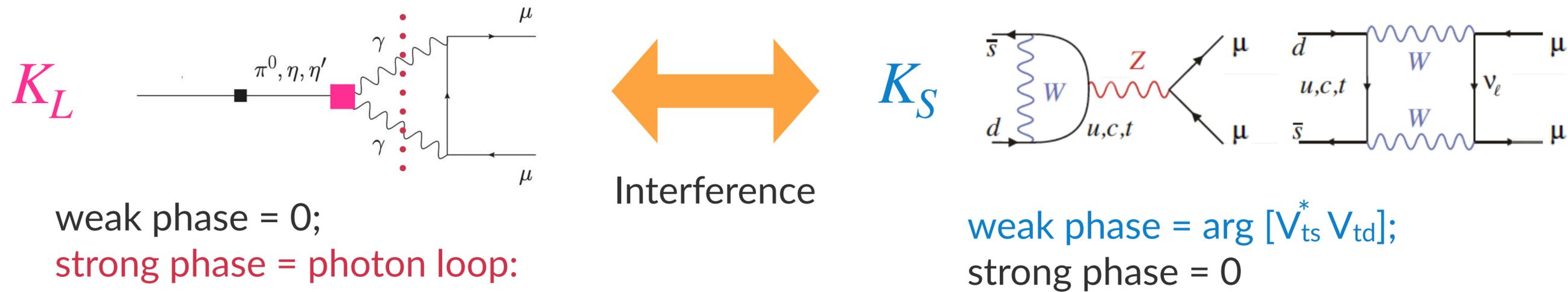
[CPLEAR collaboration '95] measured the interference between  $K_L$  and  $K_S$



# Direct CP violation in $K_{L/S}^0 \rightarrow \mu^+ \mu^-$

- Important idea: interference corresponds to **genuine direct CP violation**

[D'Ambrosio, TK, [1707.06999](#); Dery, Ghosh, Grossman, Schacht, [2104.06427](#)]



weak phase = 0;  
strong phase = photon loop:

$$K_L \rightarrow \gamma\gamma | \gamma\gamma \rightarrow \mu\mu$$

weak phase =  $\arg [V_{ts}^* V_{td}]$ ;  
strong phase = 0

Both weak and strong phase differences exist

Two advantages:

- Numerically enhanced by the anomaly-driven  $(\blacksquare) K_L^0 \rightarrow \gamma\gamma, \mathcal{O}(1/f_\pi)$
- Theoretically clean due to the optical theorem in  $K_L^0$  amplitude

# Four-fold ambiguity

- There are **four-fold ambiguity** of the **strong phase** in light of the experimental determination [Dery, Ghosh, Grossman, TK, Schacht, [2211.03804](#)]

Optical theorem

$$\cos^2 \varphi_0 \stackrel{\downarrow}{=} \frac{\alpha_{em}^2 m_\mu^2}{2\beta_\mu m_K^2} \log^2 \left( \frac{1 - \beta_\mu}{1 + \beta_\mu} \right) \times \frac{\mathcal{B}(K_L^0 \rightarrow \gamma\gamma)}{\mathcal{B}(K_L^0 \rightarrow \mu^+\mu^-)}$$

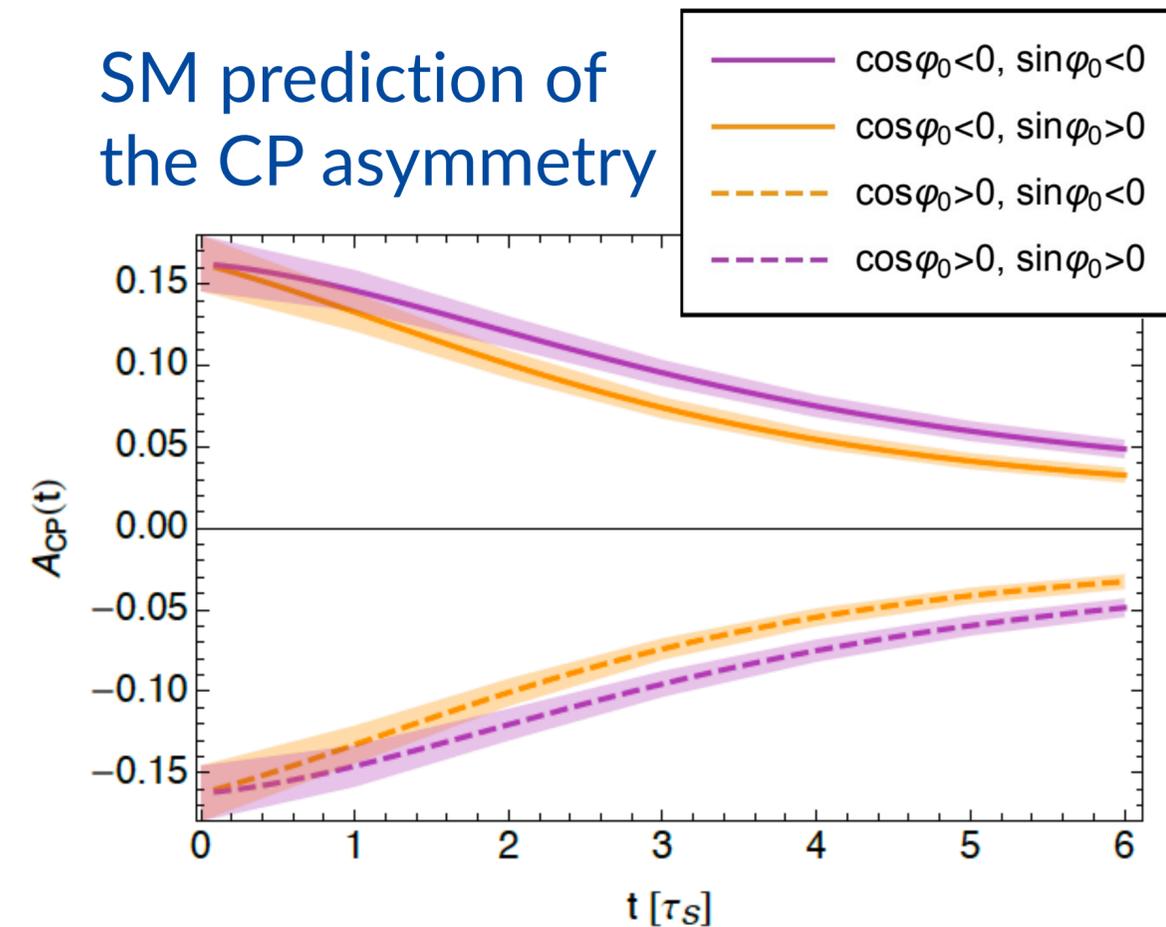
$$= 0.96 \pm 0.02_{\text{exp}} \pm 0.02_{\text{th}} \quad \varphi_0 \simeq 12^\circ, 168^\circ, 192^\circ, 348^\circ$$

- This provides two SM predictions in  $K_L^0 \rightarrow \mu^+\mu^-$

$$\mathcal{B}(K_L^0 \rightarrow \mu^+\mu^-)_{\text{SM}} = \begin{cases} 7.44_{-0.34}^{+0.41} \times 10^{-9} & \text{for } \tilde{A}_{\text{CP}} > 0 \quad (\cos \varphi_0 < 0) \\ 6.83_{-0.17}^{+0.24} \times 10^{-9} & \text{for } \tilde{A}_{\text{CP}} < 0 \quad (\cos \varphi_0 > 0) \end{cases}$$

[Hoferichter, Hoid, de Elvira, [2310.17689](#)]

SM prediction of the CP asymmetry



[D'Ambrosio, Dery, Grossman, TK, Marchevski, Martinez Santos, Schacht, [2507.13445](#)]

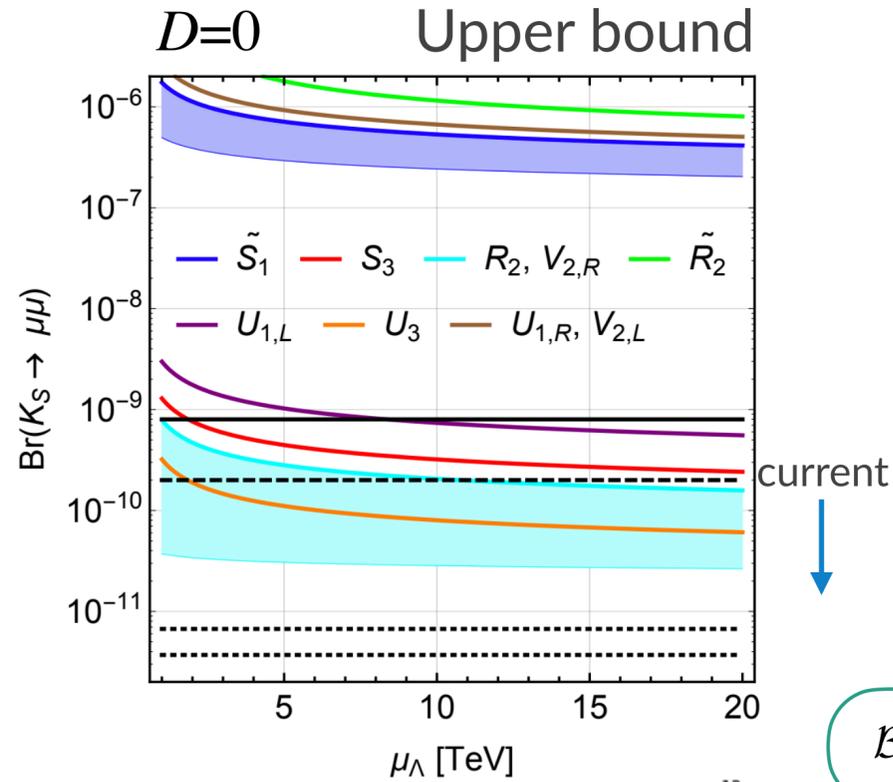
# New physics for $K_S^0 \rightarrow \mu^+ \mu^-$ including interference

Leptoquark

can be  $\mathcal{O}(10^{-10})$

$R_2$ , or  $U_{1,L}$   
(the others are excluded by  $K^+ \rightarrow \pi^+ \nu \bar{\nu}$ )

[Bobeth, Buras '18]



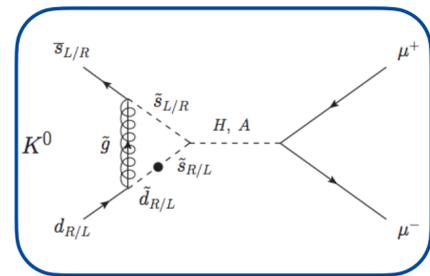
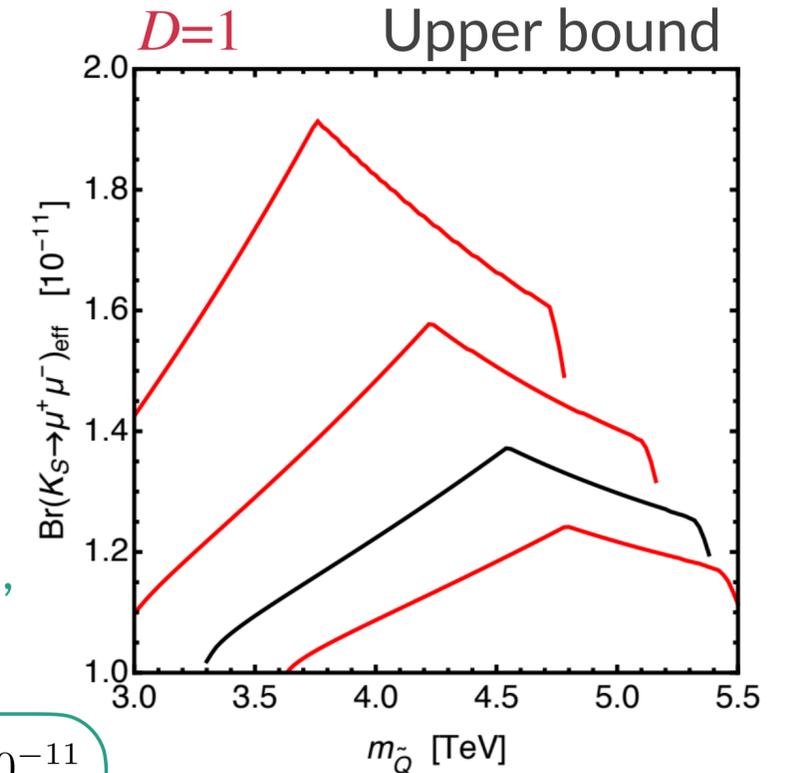
MSSM with large  $A_{LR}$

$\lesssim 2 \times 10^{-11}$

Only large  $|D|$

[Endo, Goto, TK, Mishima, Ueda, Yamamoto '18]

$\mathcal{B}(K_S \rightarrow \mu^+ \mu^-)|_{\text{MSSM}} \sim \mathcal{O}(1) \times 10^{-11}$

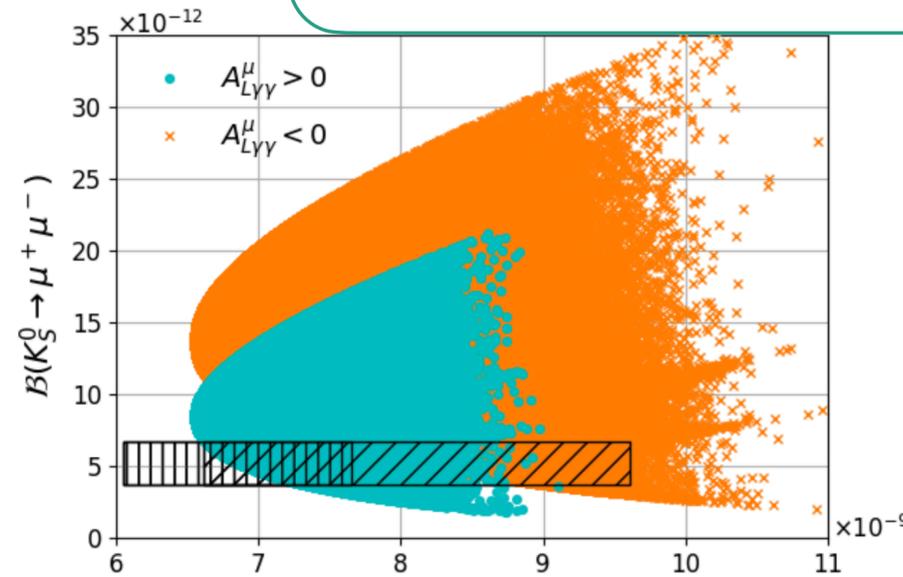


MSSM with large  $\tan \beta$

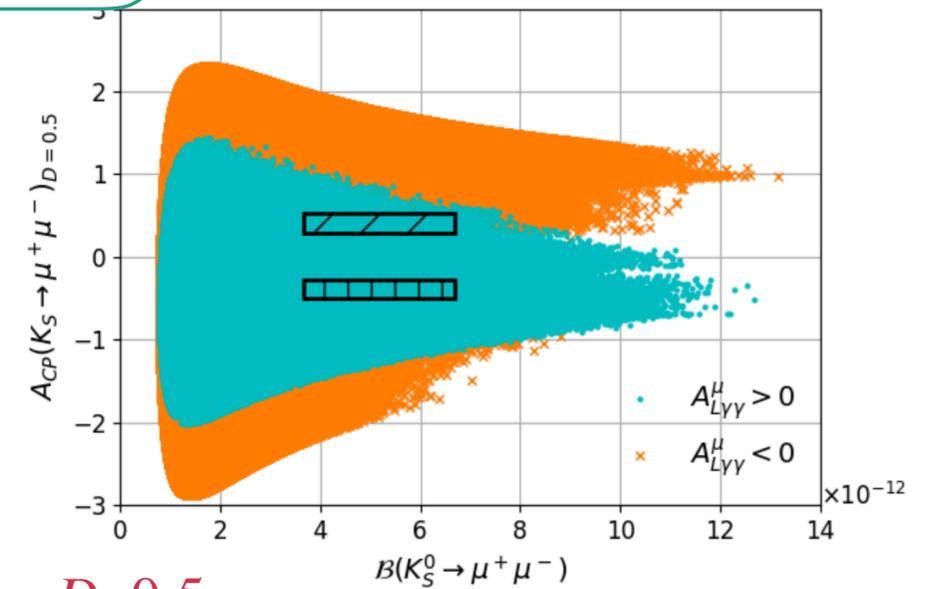
$\lesssim 3 \times 10^{-11}$

Even  $D=0$

[Chobanova, D'Ambrosio, TK, Martinez, Santos, Fernandez, Yamamoto '18]



$D=0$



$D=0.5$

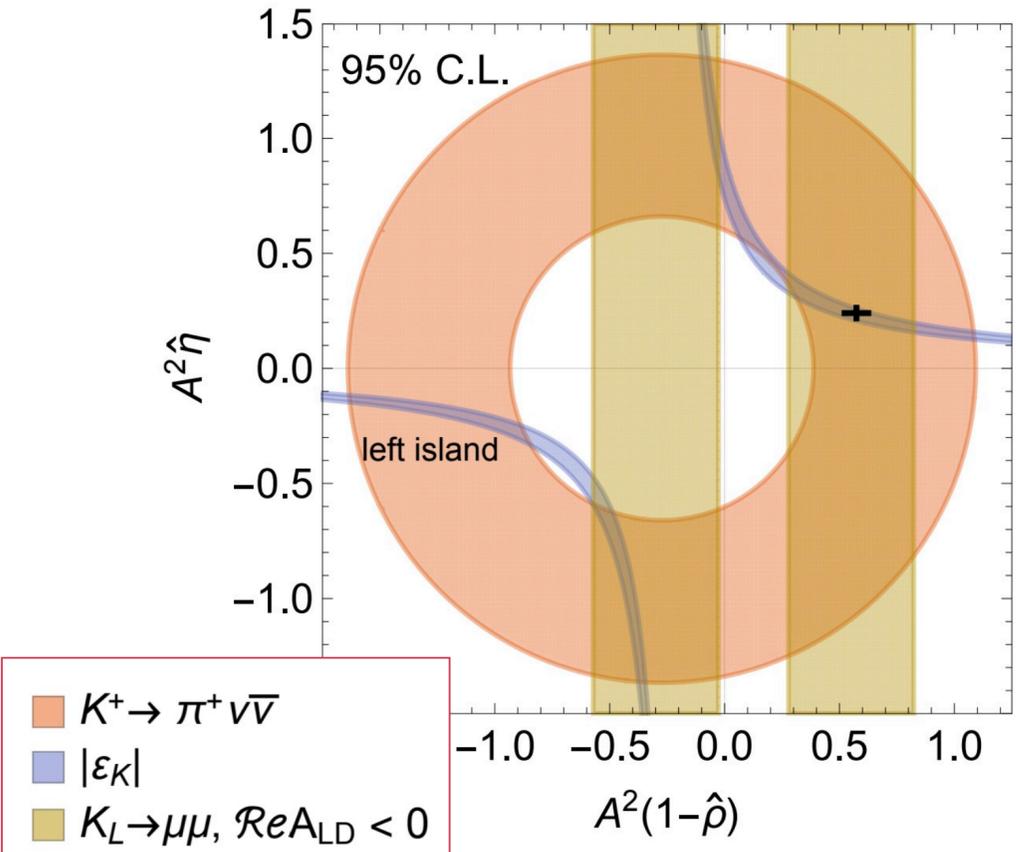
# Kaon unitarity triangle

[Buras, Venturini, [2109.11032](#);  
 Lunghi, Soni, [2408.11190](#);  
 Dery, [2504.12386](#)]

- New idea: large uncertainty from  $|V_{cb}|$  can be dropped, when one considers the unitarity triangle in not  $(\bar{\rho}, \bar{\eta})$ , but in  $(A^2(1 - \hat{\rho}), A^2\hat{\eta})$  plane

with  $A^2 \lambda^4 (1 - \hat{\rho} + i\hat{\eta}) \equiv -\frac{V_{td}V_{ts}^*}{V_{cd}V_{cs}^*}$

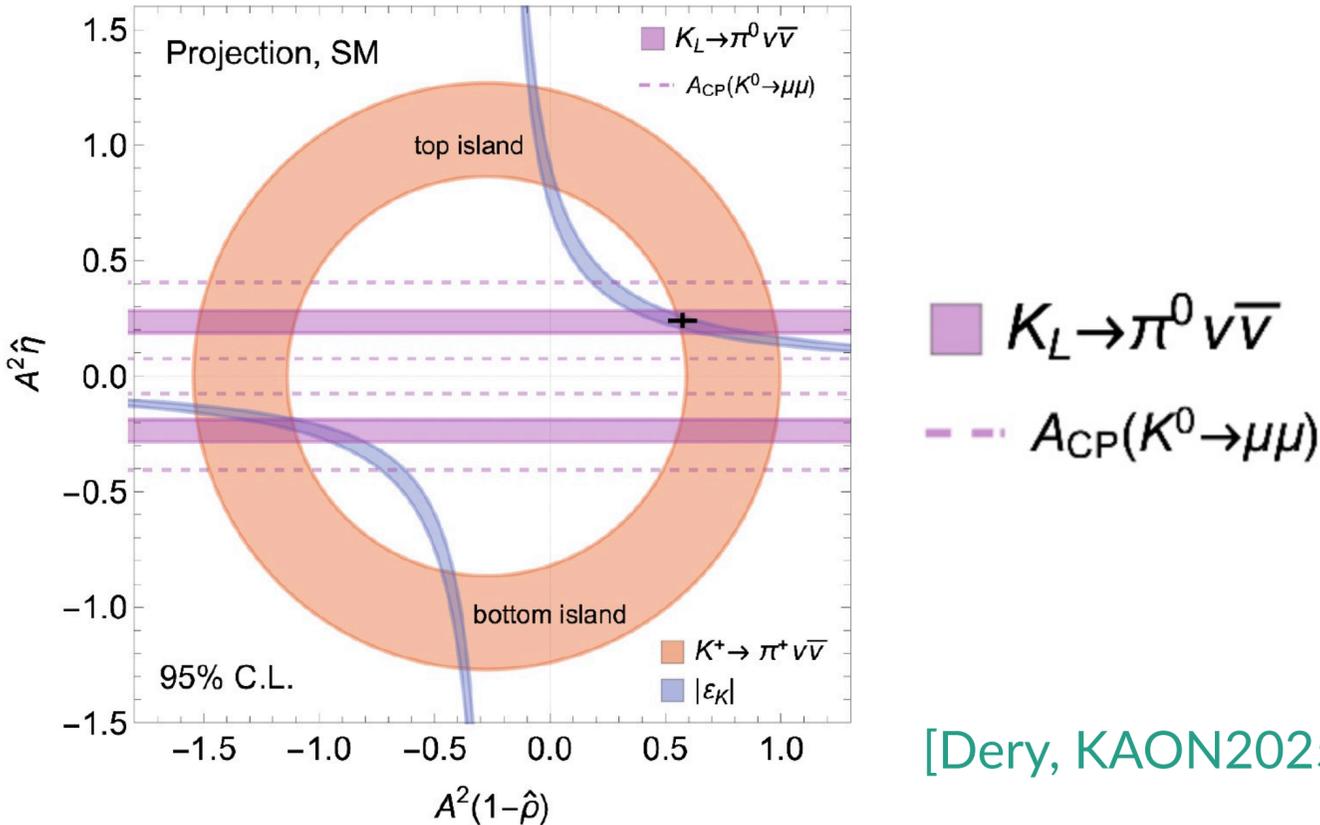
[Dery, [2504.12386](#)]



current best-fit point



near future  
 $\approx 2040$



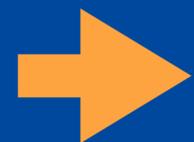
[Dery, KAON2025]

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# Beautiful in theory side – but can LHCb really do it?

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$K^0$  and  $\bar{K}^0$  yields are almost the same in the LHC (momentum-dependent asymmetry is about a few-percent)



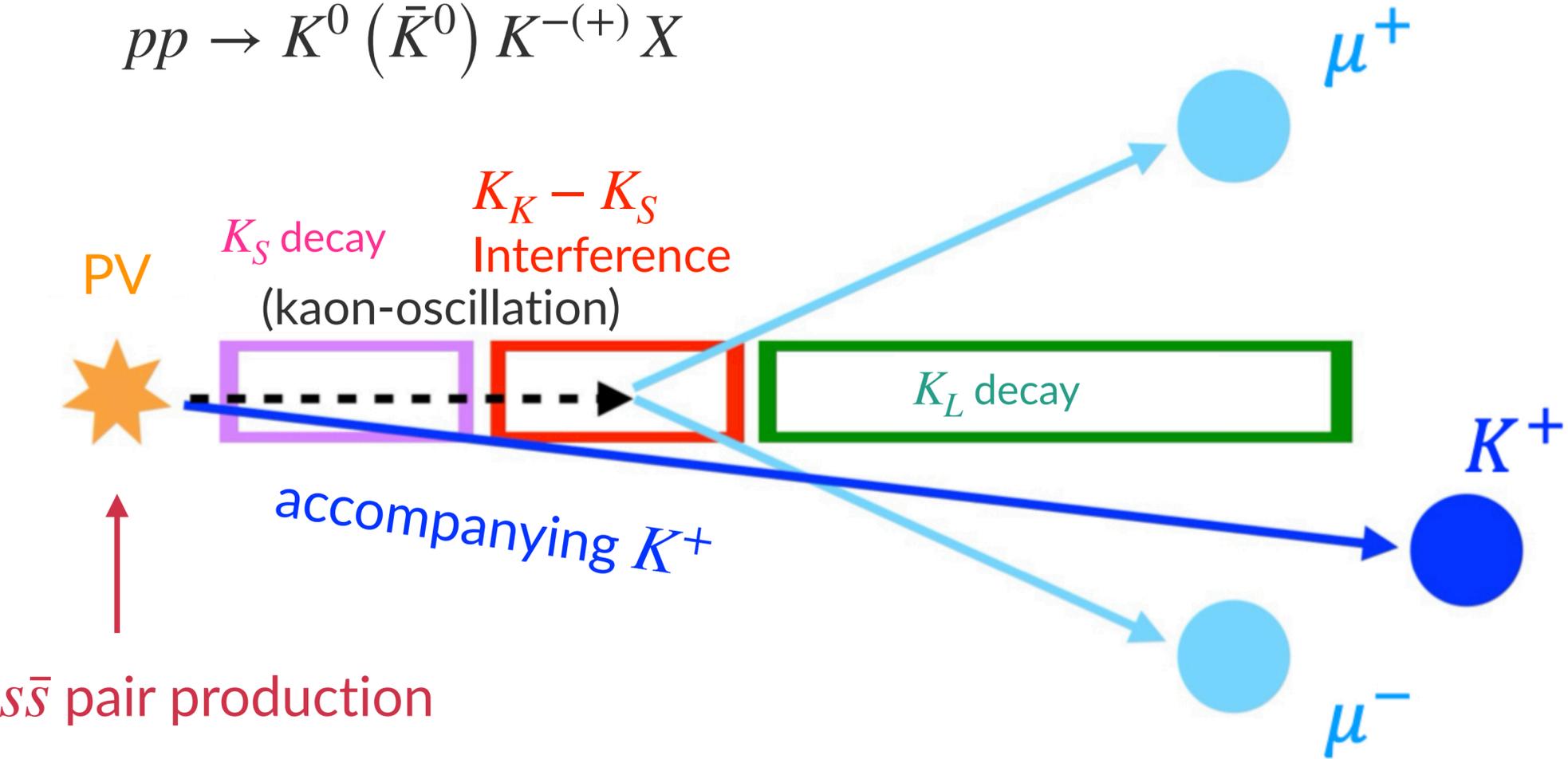
Additional flavor tag is needed

# Flavor tagging method

■ We simulate the following events within an LHCb-like setup:

[D'Ambrosio, TK, [1707.06999](#)]

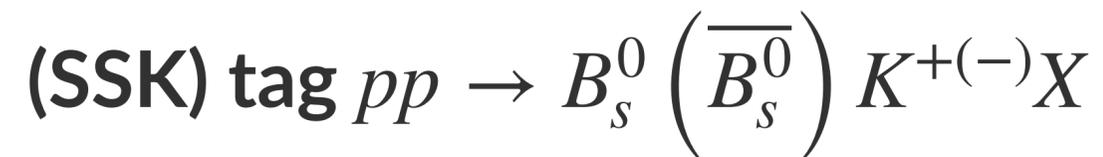
$$pp \rightarrow K^0 (\bar{K}^0) K^{-(+)} X$$



- Forward  $s\bar{s}$  productions
- Two opposite sign muon generated from the interference region
- Single accompanying charged kaon to distinguish  $K^0(t = 0)$  or  $\bar{K}^0(t = 0)$

# Comparison with $B_s^0$ tagging

- Similar tagging can be possible for  $B_s^0$  decays: **same-side-kaon**



[LHCb, [LHCb-CONF-2012-033](#)]

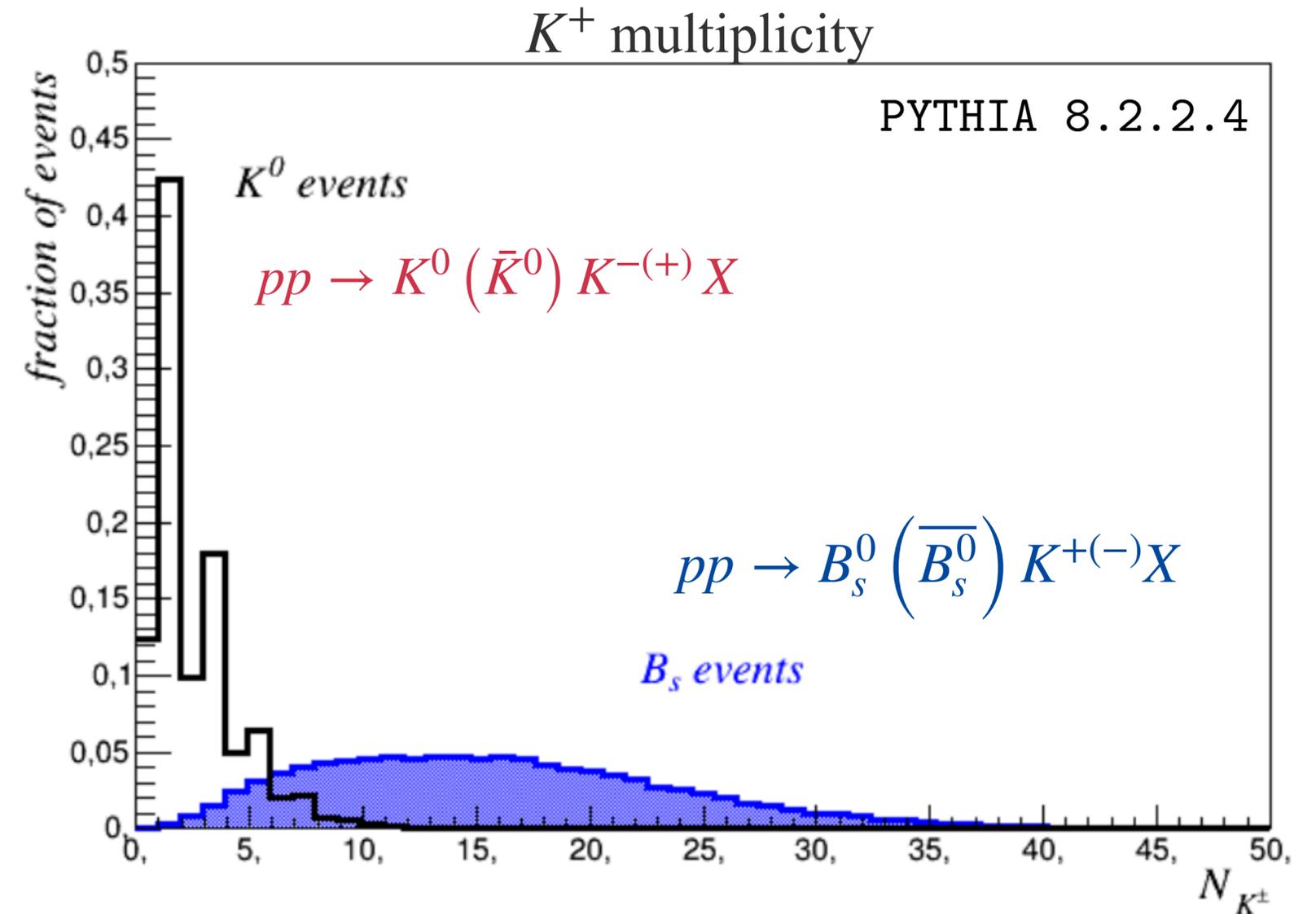
- Our fast simulation result:

Tagging power:  $T_P = \varepsilon_T D^2 \approx 22\%$

tagging efficiency of  $K^0$  Dilution factor

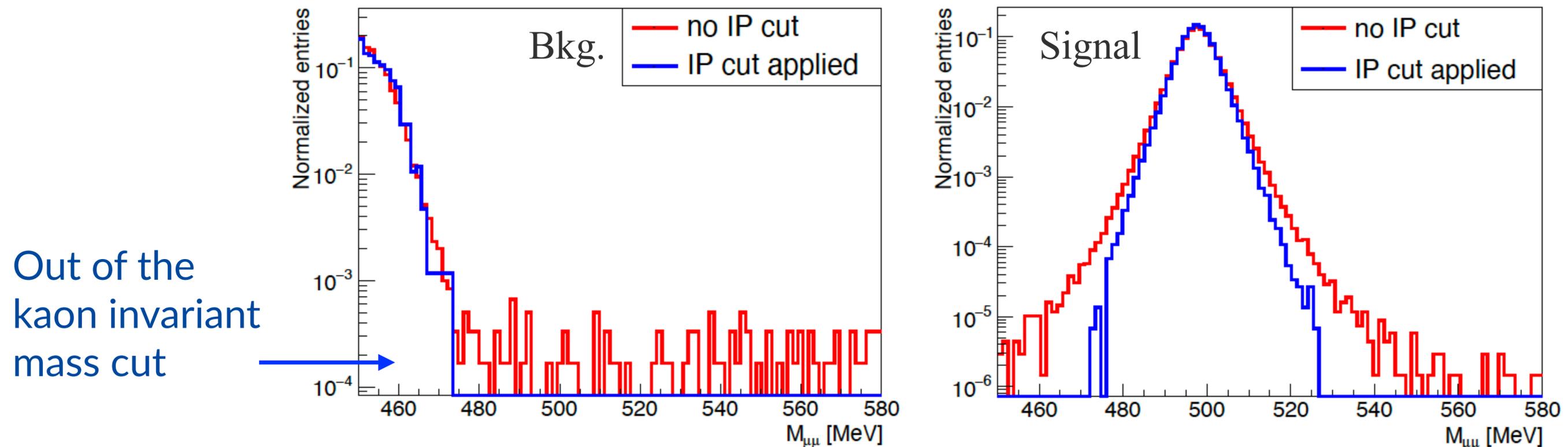
$$\varepsilon_T \approx 62\% \quad D \approx 60\%$$

cf.  $T_P(B_s^0) \approx 3\%$  much better than the  $B_s^0$  tagging power, thanks to the lower  $K^+$  multiplicity



# Background reduction

- Background is currently dominated by  $K_S^0 \rightarrow \pi^+(\rightarrow \mu^+\nu)\pi^-(\rightarrow \mu^-\bar{\nu})$   
muon from pion decays in flight
- This Bkg. can be separated by an impact parameter cut of  $K^0$  from the PV  
reconstructed invisible  $K^0$  line

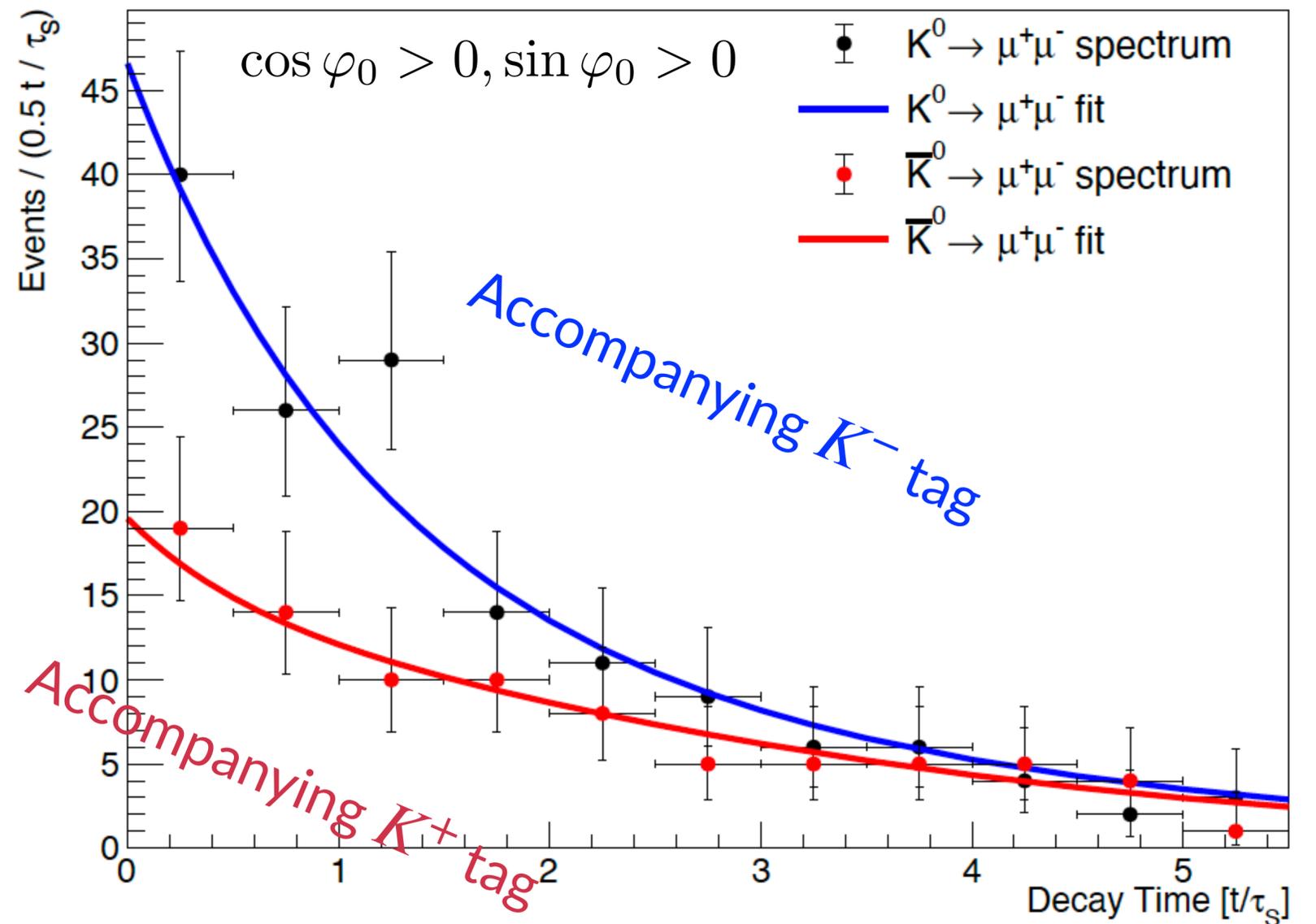


- The IP cut will improve the signal sensitivity by a factor of  $\approx 9$  for 300 fb<sup>-1</sup>

# Decay-time analysis

[D'Ambrosio, Dery, Grossman, TK, Marchevski, Martinez Santos, Schacht, [2507.13445](#)]

- We simulate the decay-time distribution for the **LHCb Upgrade II setup**
- It is clearly shown that the CP violation between  $K^0 \rightarrow \mu^+ \mu^-$  and  $\bar{K}^0 \rightarrow \mu^+ \mu^-$  can be measured for small decay time region

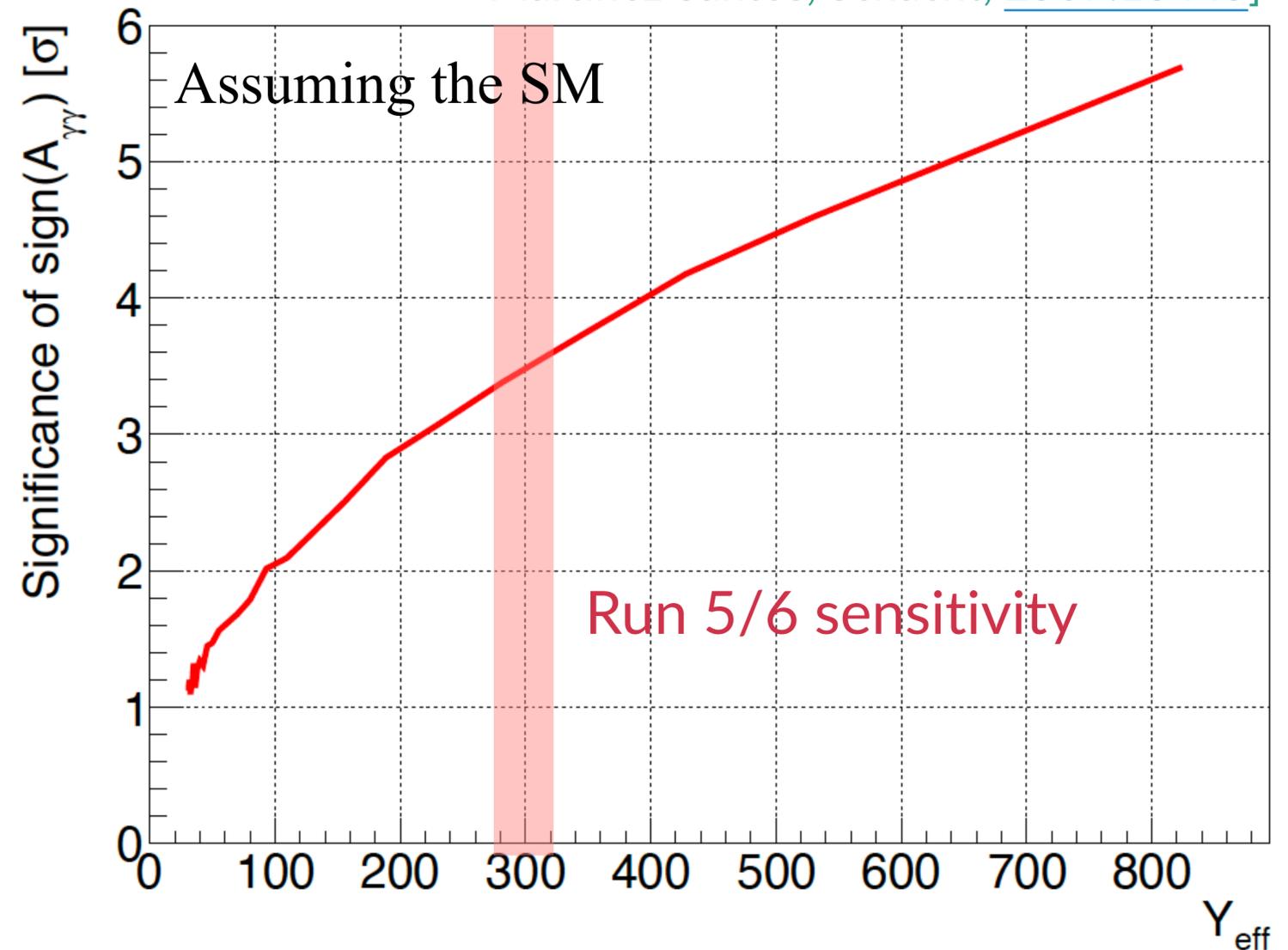


# Sensitivity to the sign of $A(K_L^0 \rightarrow \gamma\gamma)$

- A simultaneous fit to the  $K^0$  and  $\bar{K}^0 \rightarrow \mu^+\mu^-$  decay-time distributions can probe the unknown sign of  $A(K_L^0 \rightarrow \gamma\gamma)$
- LHCb Upgrade II can distinguish discrete ambiguity in the SM prediction of  $\mathcal{B}(K_L^0 \rightarrow \mu^+\mu^-)$

➔ reduce theoretical uncertainty

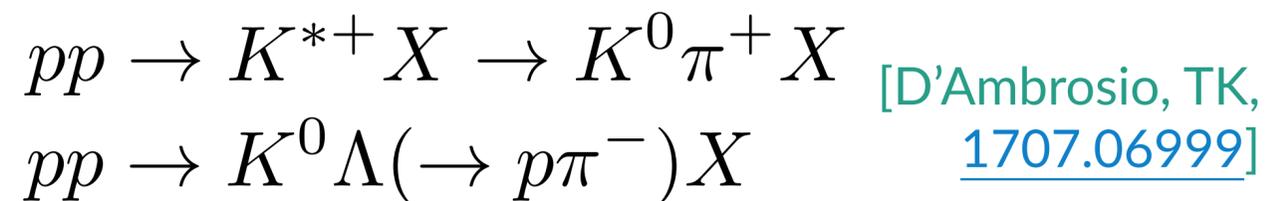
[D'Ambrosio, Dery, Grossman, TK, Marchevski, Martinez Santos, Schacht, [2507.13445](#)]



# Sensitivity to the CP-violating parameter

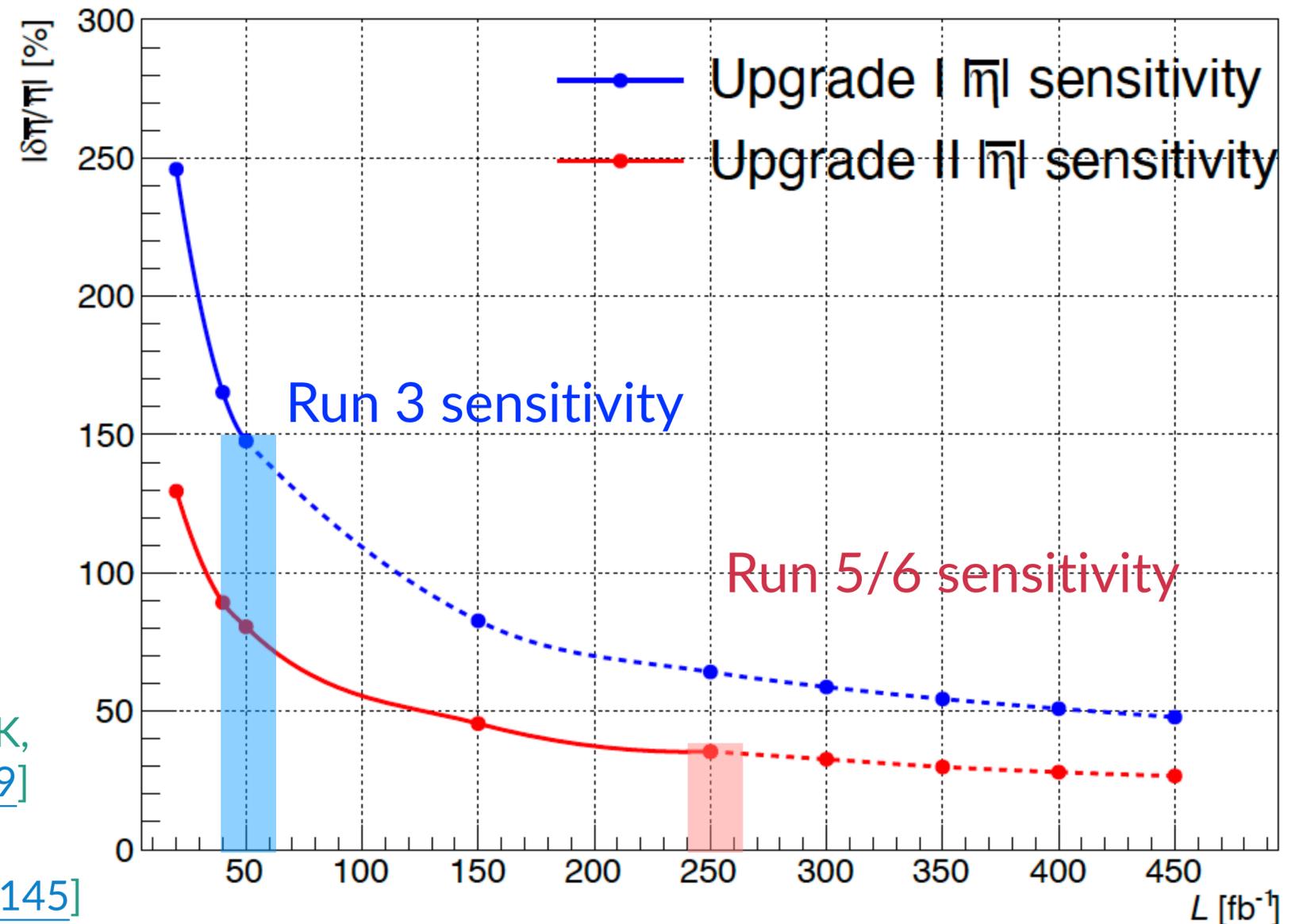
[D'Ambrosio, Dery, Grossman, TK, Marchevski, Martinez Santos, Schacht, [2507.13445](#)]

- In Upgrade II, a **factor 3 improvement** is expected using events by downstream track
- LHCb Upgrade I and II can measure  $A^2 \lambda^5 |\bar{\eta}|$  with **150%** and **35% accuracy**, respectively
- Further improvements for flavor tagging are possible via



[D'Ambrosio, TK, [1707.06999](#)]

deep-learning method [Prouve, et al, [2404.14145](#)]



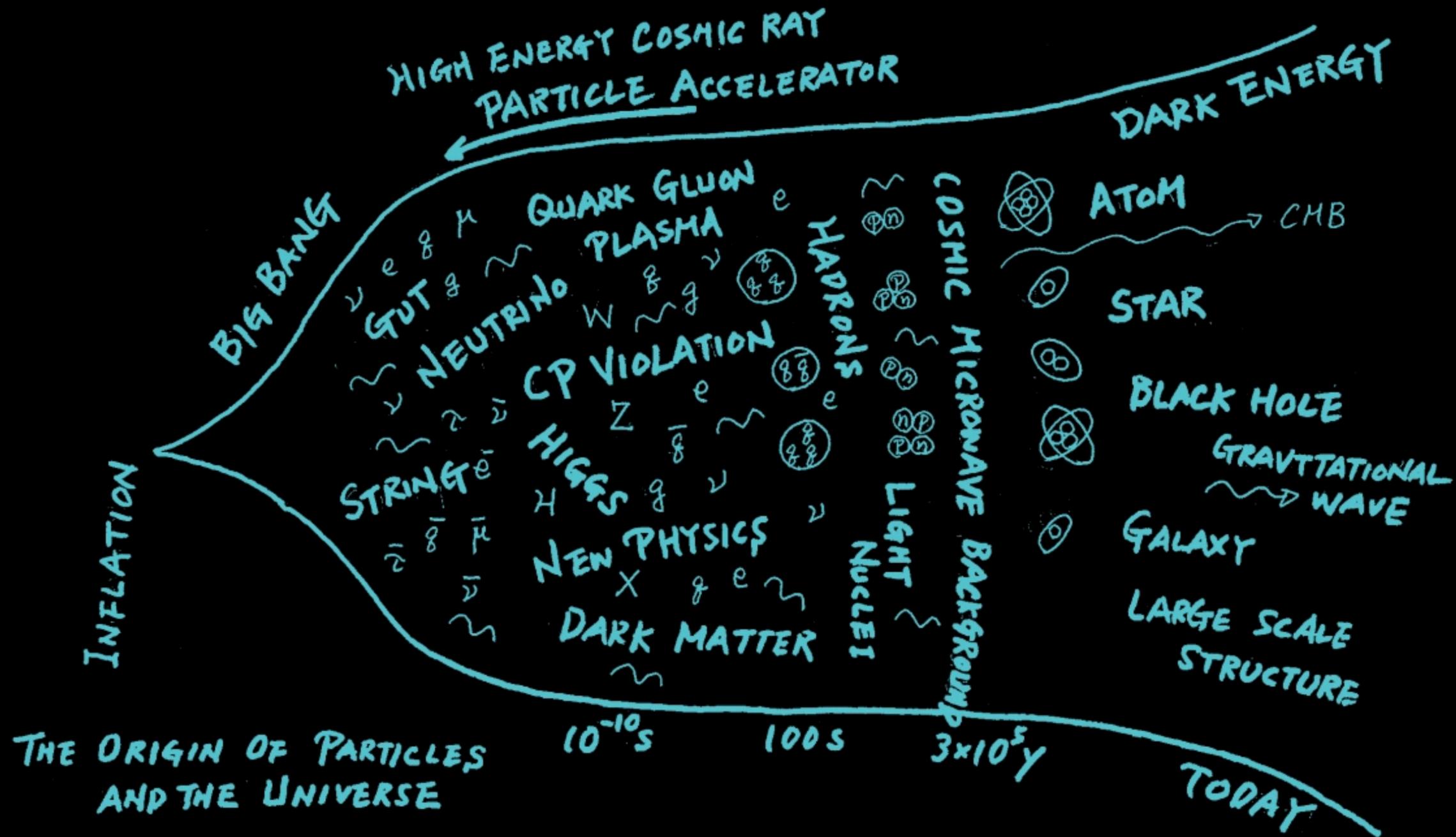
# Conclusions

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- **New direction**   $K_L^0 - K_S^0$  interference in  $K^0 \rightarrow \mu^+ \mu^-$  provides a powerful probe of **CP-violating short-distance physics**
- Excellent flavor tagging via  $pp \rightarrow K^0 (\bar{K}^0) K^{-(+) X}$  is essential, and simulation shows that it is **much better than** the SSK tag in  $B_s^0$  decays
- LHCb Upgrade II will offer a unique opportunity to directly measure the **CP-violating parameter**  $A^2 \lambda^5 |\bar{\eta}|$  **with 35% uncertainty via**  $K^0 \rightarrow \mu^+ \mu^-$
- Run 5 (after the Upgrade II) starts from 2036; **complementary to KOTO II** ( $K_L^0 \rightarrow \pi^0 \nu \bar{\nu}$ ) ?

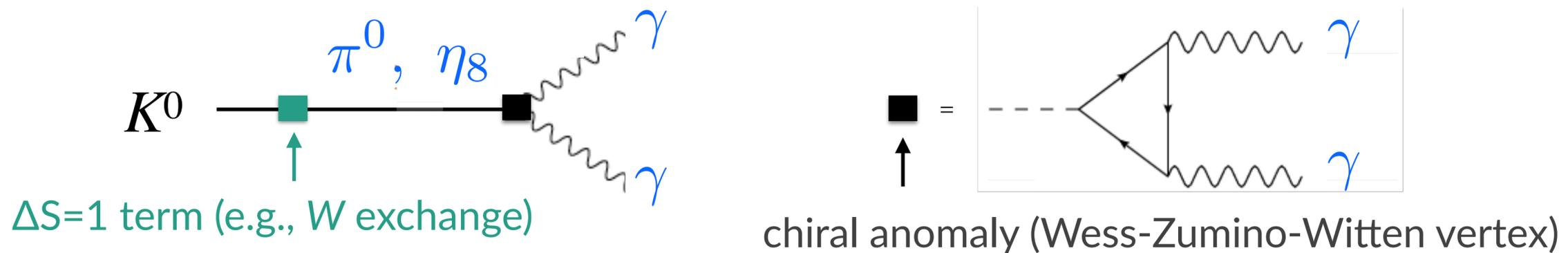
**Thank you!**

# Backup slides



# Interesting cancellation in $K^0 \rightarrow \gamma\gamma$

- ◆ Leading contribution in  $K^0 \rightarrow \gamma\gamma$  comes from the following diagram:



- ◆ The amplitude @ $O(p^4)$  [e.g., D'Ambrosio, Ecker, Isidori, Neufeld '94]

$$\text{Amp} \propto \frac{1}{m_K^2 - m_\pi^2} + \frac{1}{3} \frac{1}{m_K^2 - m_{\eta_8}^2} = \frac{4m_K^2 - 3m_{\eta_8}^2 - m_\pi^2}{3(m_K^2 - m_\pi^2)(m_K^2 - m_{\eta_8}^2)} = 0$$

- ◆ Gell-Mann–Okubo formula ( $SU(3)_F$  with massive strange) [Gell-Mann '61; Okubo '62]

$$4m_K^2 = 3m_{\eta_8}^2 + m_\pi^2$$

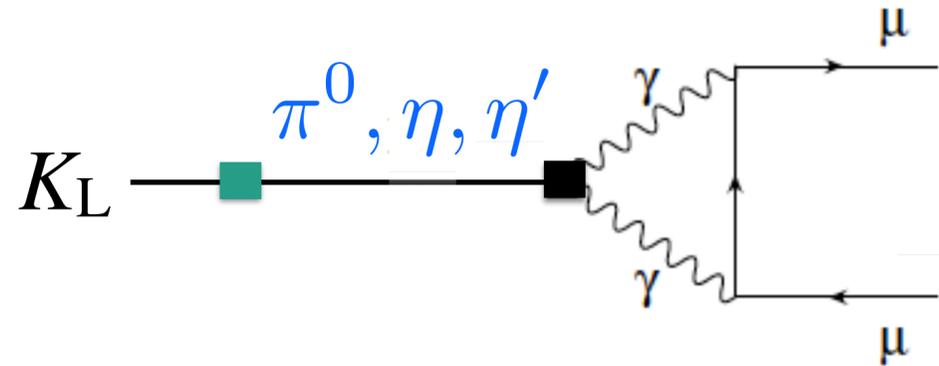
Leading pieces are canceled out

# Details of $K_L^0 \rightarrow \mu^+ \mu^-$

[D'Ambrosio, Ecker, Isidori, Neufeld '94;  
Gomez Dumm, Pich '98;  
Knecht, Peris, Perrottet, Rafael '99]

- ◆  $K_L \rightarrow \mu^+ \mu^- = |\text{S-wave}|^2$  ← P-wave is significantly suppressed in the SM

## Long distance CPC

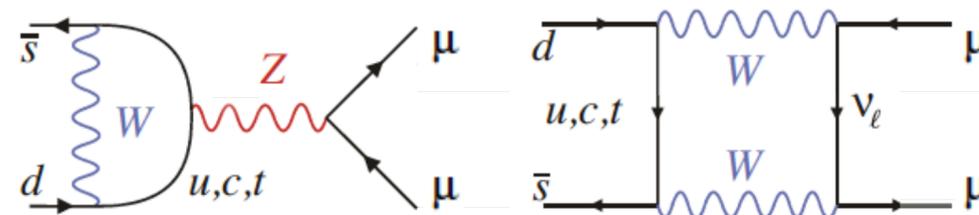


Interference

- ◆  $\pi^0$  and  $\eta$  contributions are cancelled out @ $\mathcal{O}(p^4)$  by the Gell-Mann–Okubo formula. The higher order corrections are unknown.
- ◆ Absolute value of the amplitude can be extracted from  $\text{BR}(K_L \rightarrow \gamma\gamma)_{\text{exp}}$

→ **sign ambiguity of**  
 $A(K_L \rightarrow \gamma\gamma)$

## Short distance CPC



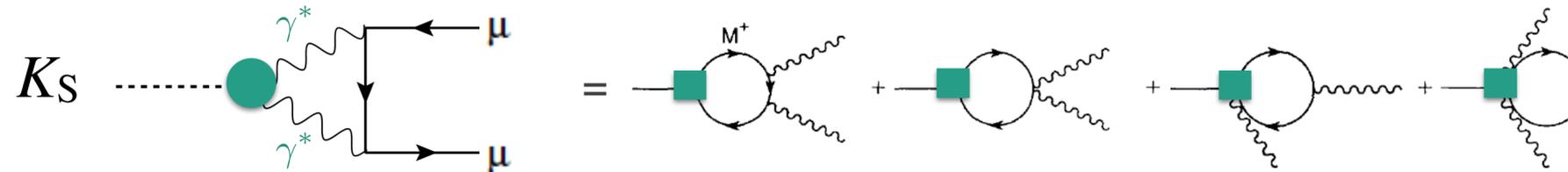
$$\propto \text{Re} [V_{ts}^* V_{td}] = \text{Re} [\lambda_t]$$

# Details of $K_S^0 \rightarrow \mu^+ \mu^-$

[Ecker, Pich '91;  
Colangelo, Stucki, Tunstall '16]

- ◆  $K_S \rightarrow \mu^+ \mu^- = |\text{P-wave}|^2 + |\text{S-wave}|^2 \quad \leftarrow \text{No interference when } \mu \text{ polarizations are not measured}$

## Long distance CPC



- ◆  $\text{BR}(K_S \rightarrow \gamma\gamma)_{\text{exp}}$  determines  $A(K_S \rightarrow \gamma\gamma)$ , which includes 17% (FSI) enhancement from pion loop
- ◆ Since two photons are off-shell states, the 17% enhancement is debatable and large uncertainty appears (reducible via  $K_S \rightarrow \gamma\mu\mu$ ,  $K_S \rightarrow \mu\mu\mu\mu$  and  $K_S \rightarrow \mu\mu ee$  by LHCb, KLOE-2)

## Short distance CPV

