

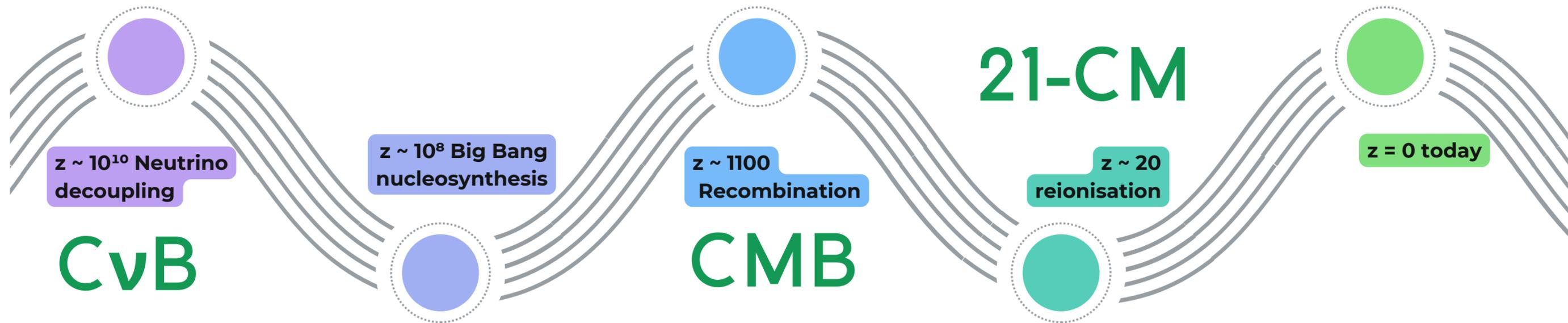
Primordial High Energy Neutrinos

Theoretical & observational constraints and sharp
spectral features

Nicolas Grimbaum Yamamoto

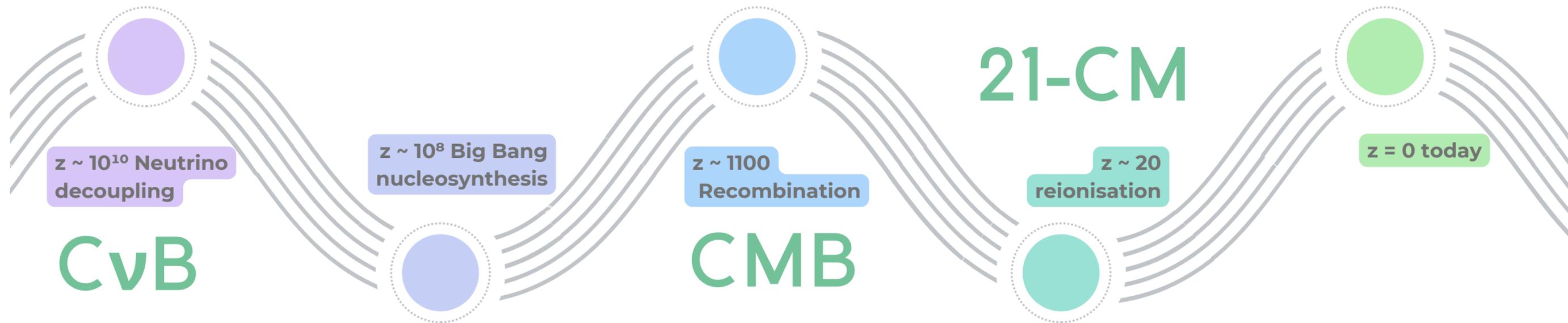
arXiv:[2507.02063](https://arxiv.org/abs/2507.02063) in collaboration with T.Hambye

Motivations.



→ **Primordial High
Energy Neutrinos
(PHENUs)**

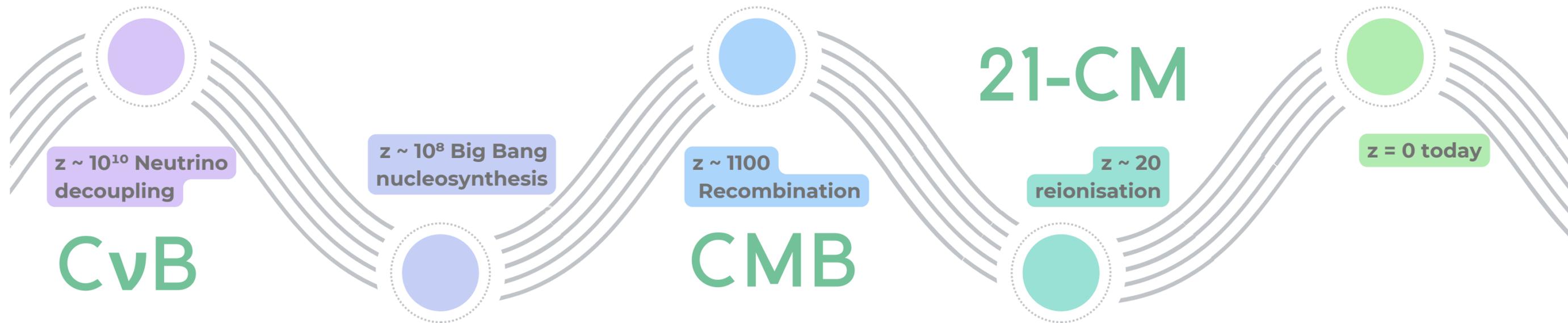
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→ Primordial High Energy Neutrinos (PHENUs)



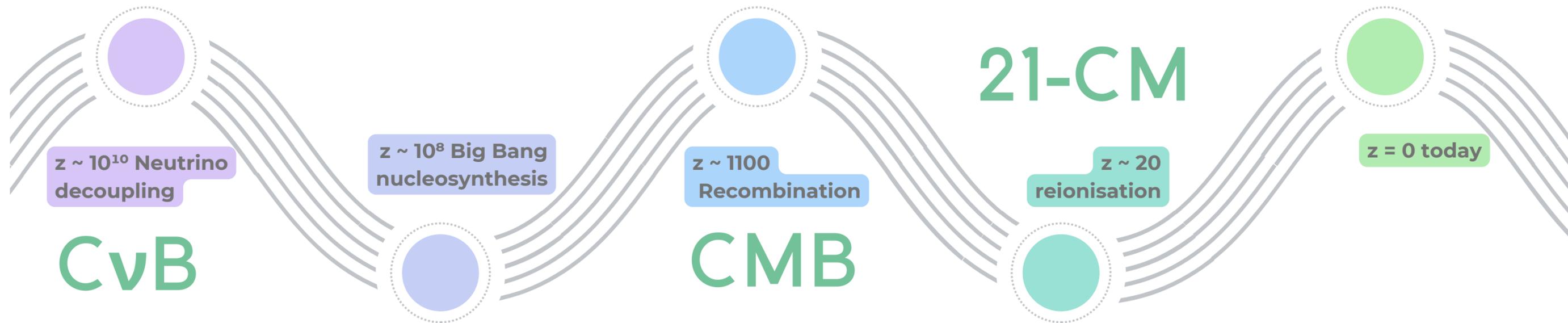
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→ Primordial High Energy Mewtrinos (PHEMEW) !



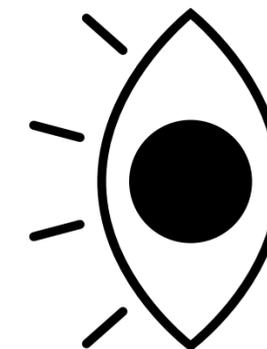
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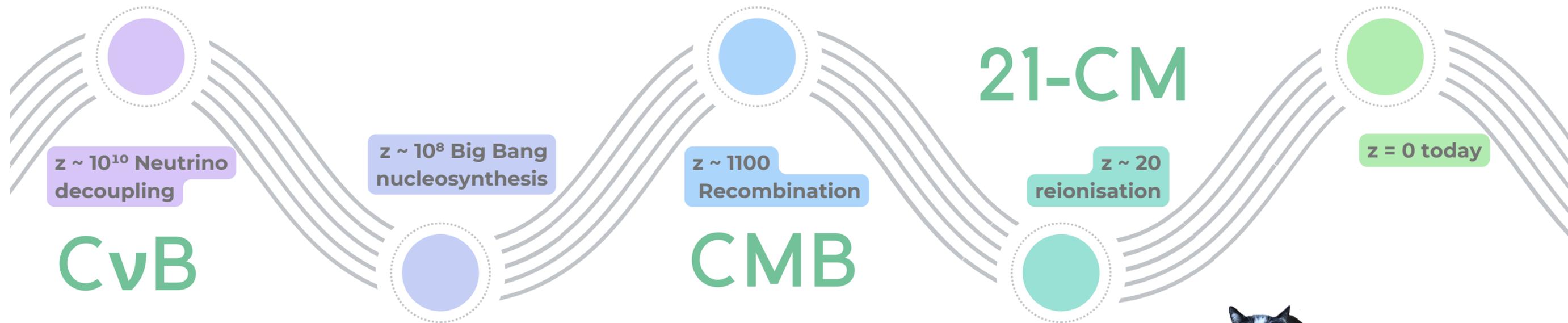
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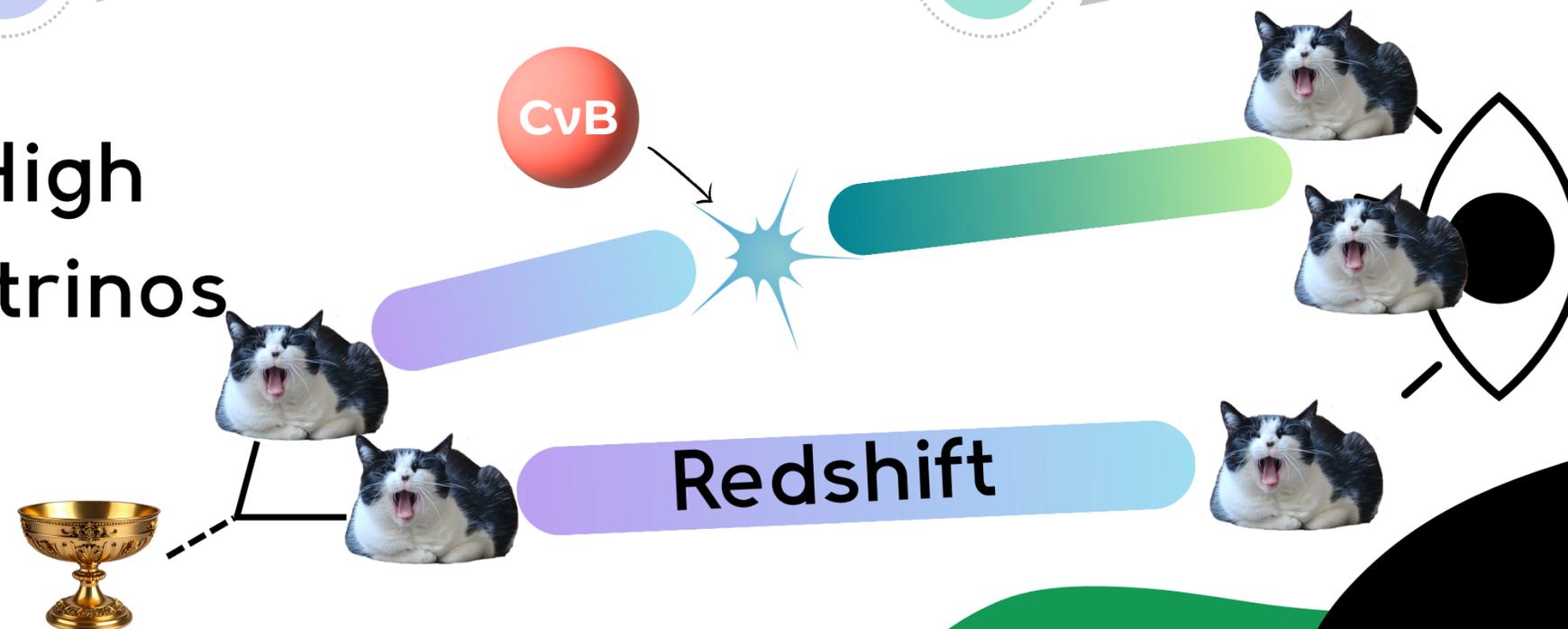
Redshift



Motivations.

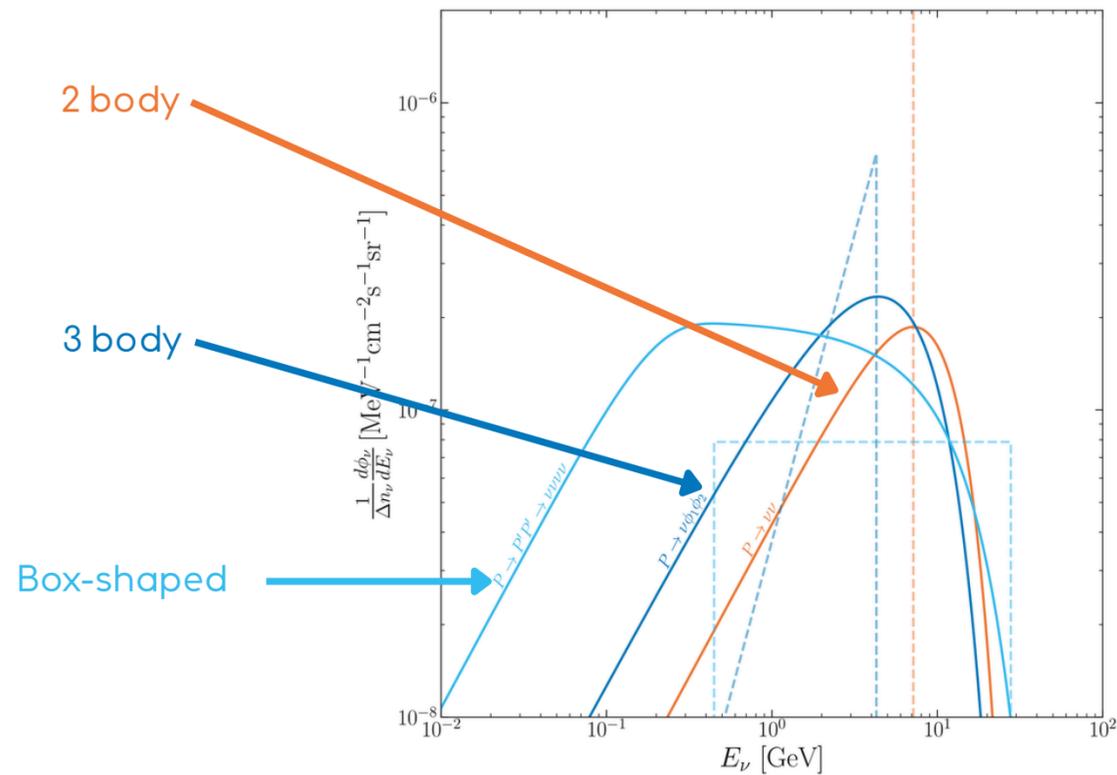


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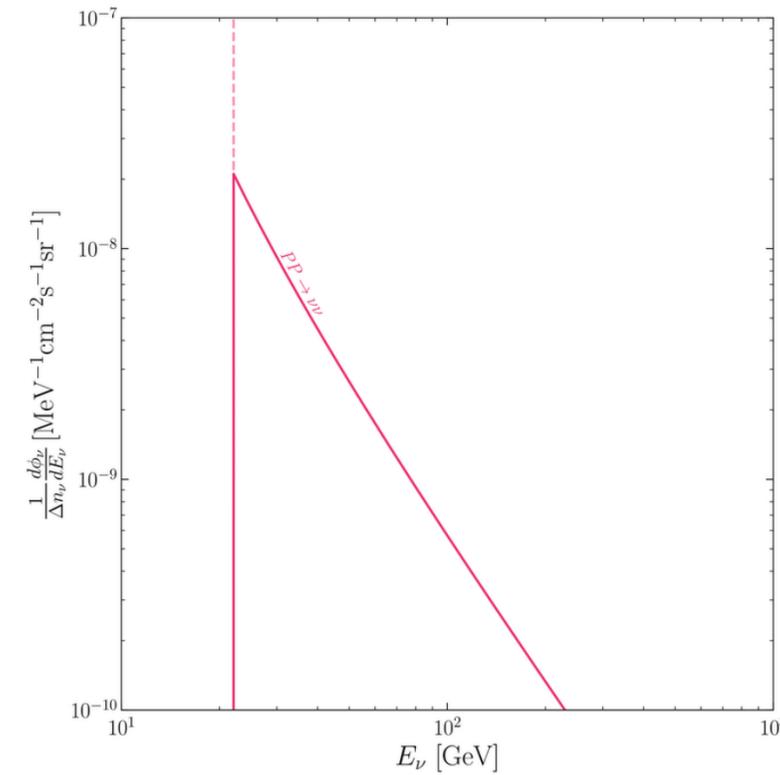
Sharp Spectral Features.

Decays



$$\frac{d\phi_\nu}{dE_\nu} = \frac{\Delta n_\nu \Omega_P^0 \rho_{crit}^0}{4\pi m_P \tau_P} \int_0^\infty dz_{inj} \frac{e^{-t_{inj}/\tau_P}}{H_{inj}} \left. \frac{df_\nu}{dE_{inj}} \right|_{E_{inj}=E_\nu(1+z_{inj})}$$

Out of equilibrium annihilation

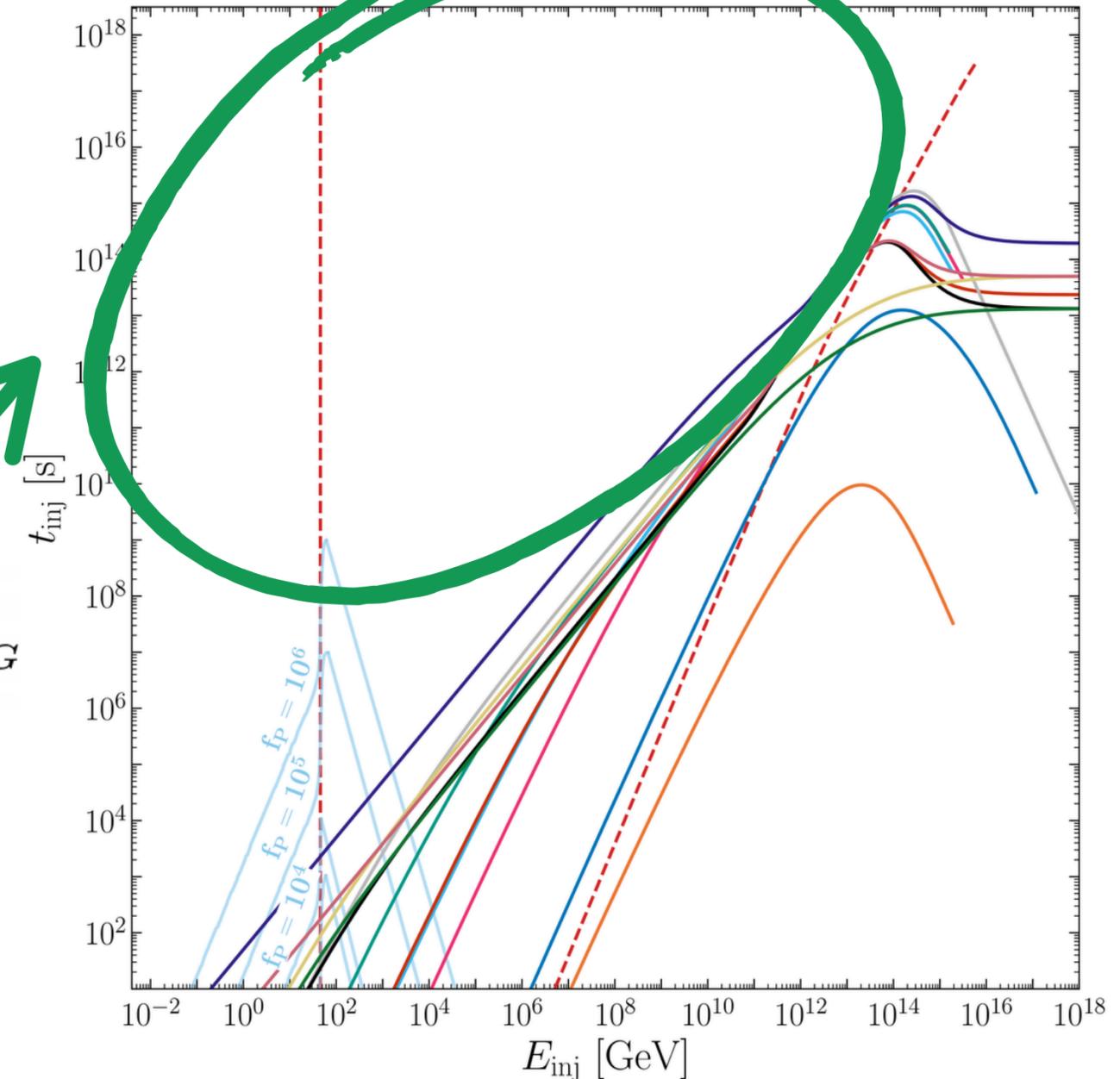


$$\frac{d\phi_\nu}{dE_\nu} = \frac{\Delta n_\nu}{16\pi} \frac{(\Omega_P^0 \rho_{crit}^0)^2 m_P \langle \sigma v \rangle}{E_\nu^4 H_{inj}} \frac{1}{\left(1 + \Omega_P^0 \rho_{crit}^0 \frac{\langle \sigma v \rangle}{2H_{inj}} \frac{m_P^2}{E_\nu^3} \left(\frac{E_\nu}{m_{Pa^*}} - 1\right)\right)^2}$$

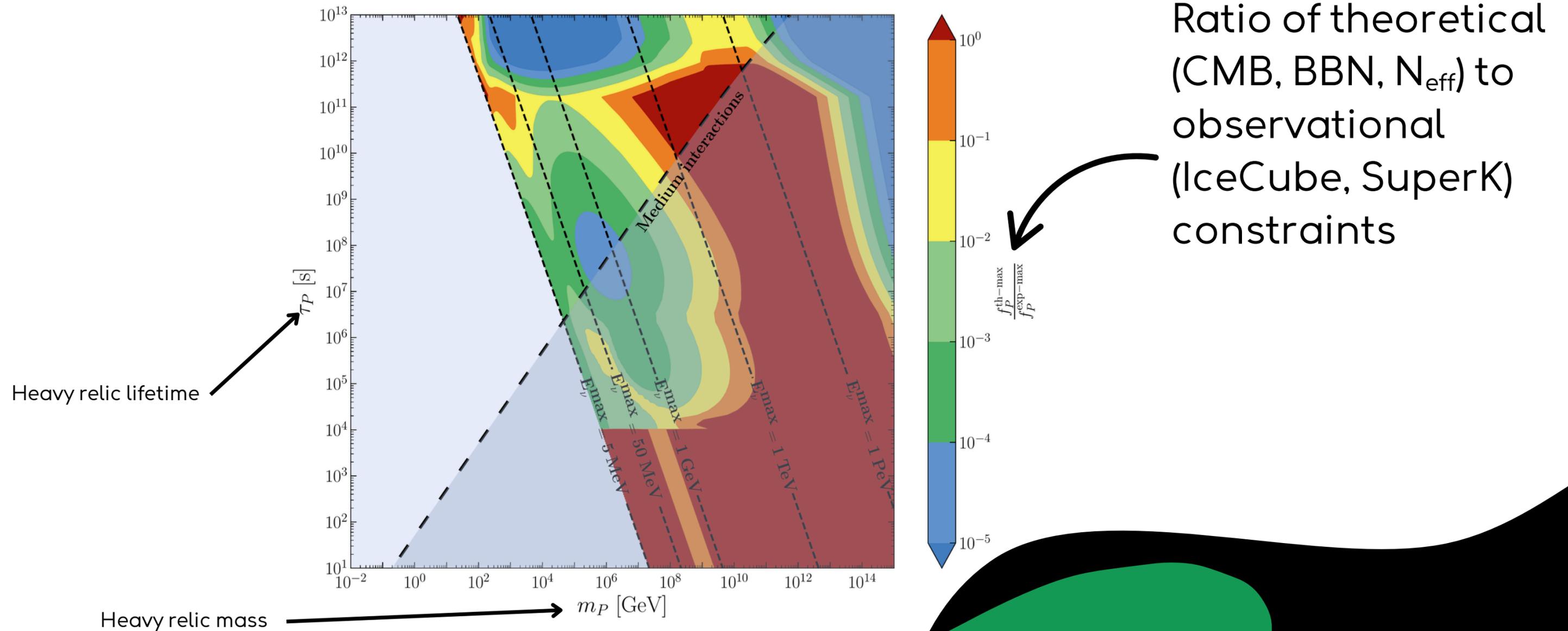
Medium interactions.

Sharp spectral features
mostly unaffected

$$S_\nu(z_e, E_0) = \int_0^{z_e} \frac{dz}{(1+z)H(z)} \langle \sigma v \rangle n_{\nu_{BG}}$$



Results.



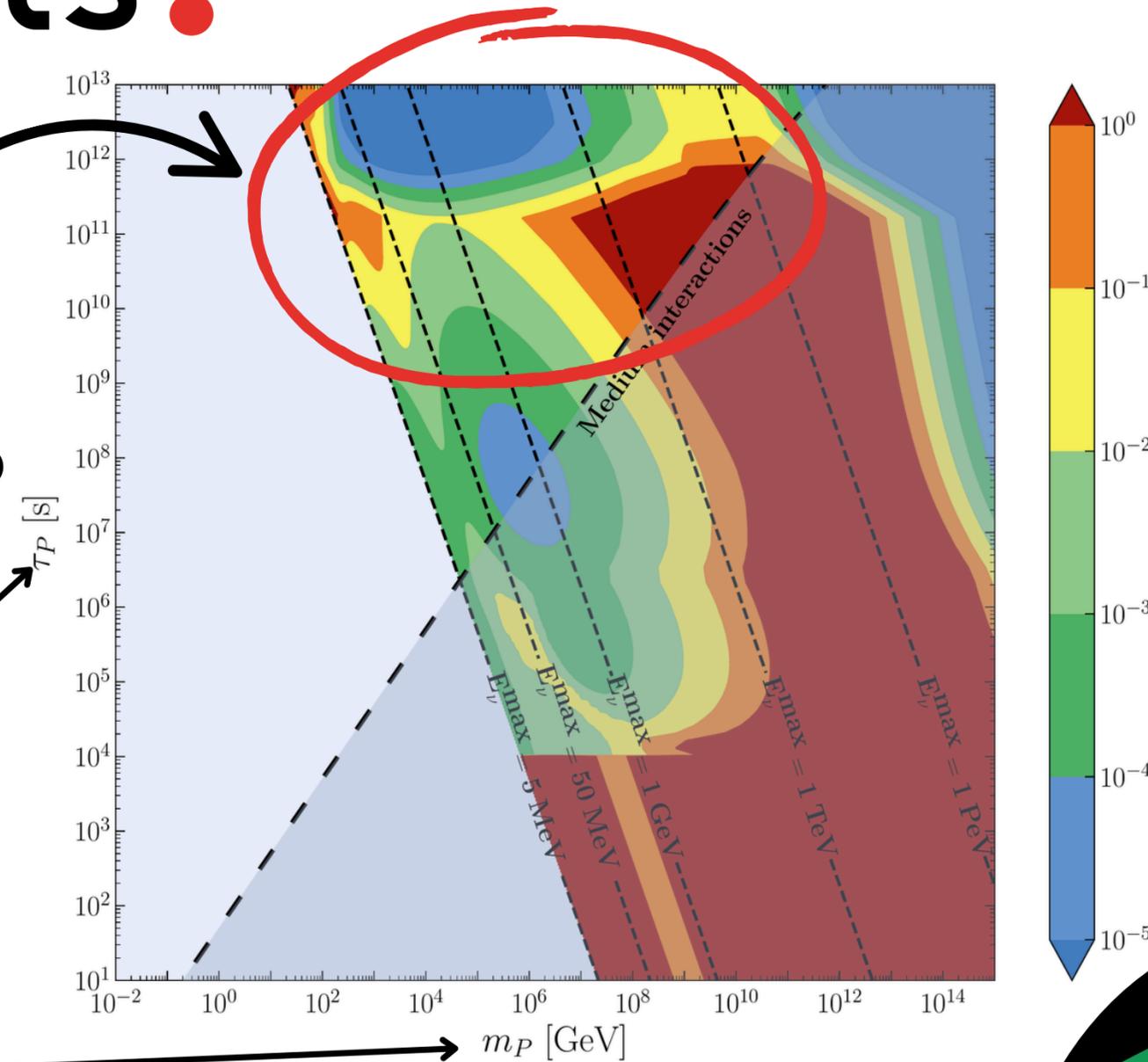
Results.

Potentially observable in existing and future neutrino telescopes

Heavy relic lifetime
 $10^9 \text{ s} \lesssim \tau_P \lesssim 10^{12.5} \text{ s}$

Heavy relic abundance
 $10^{-8} \lesssim f_P \lesssim 10^{-2}$

Heavy relic mass
 $10 \text{ TeV} \lesssim m_P \lesssim 10^{11} \text{ GeV}$



Ratio of theoretical (CMB, BBN, N_{eff}) to observational (IceCube, SuperK) constraints

$$\frac{f_P^{\text{th-max}}}{f_P^{\text{exp-max}}}$$

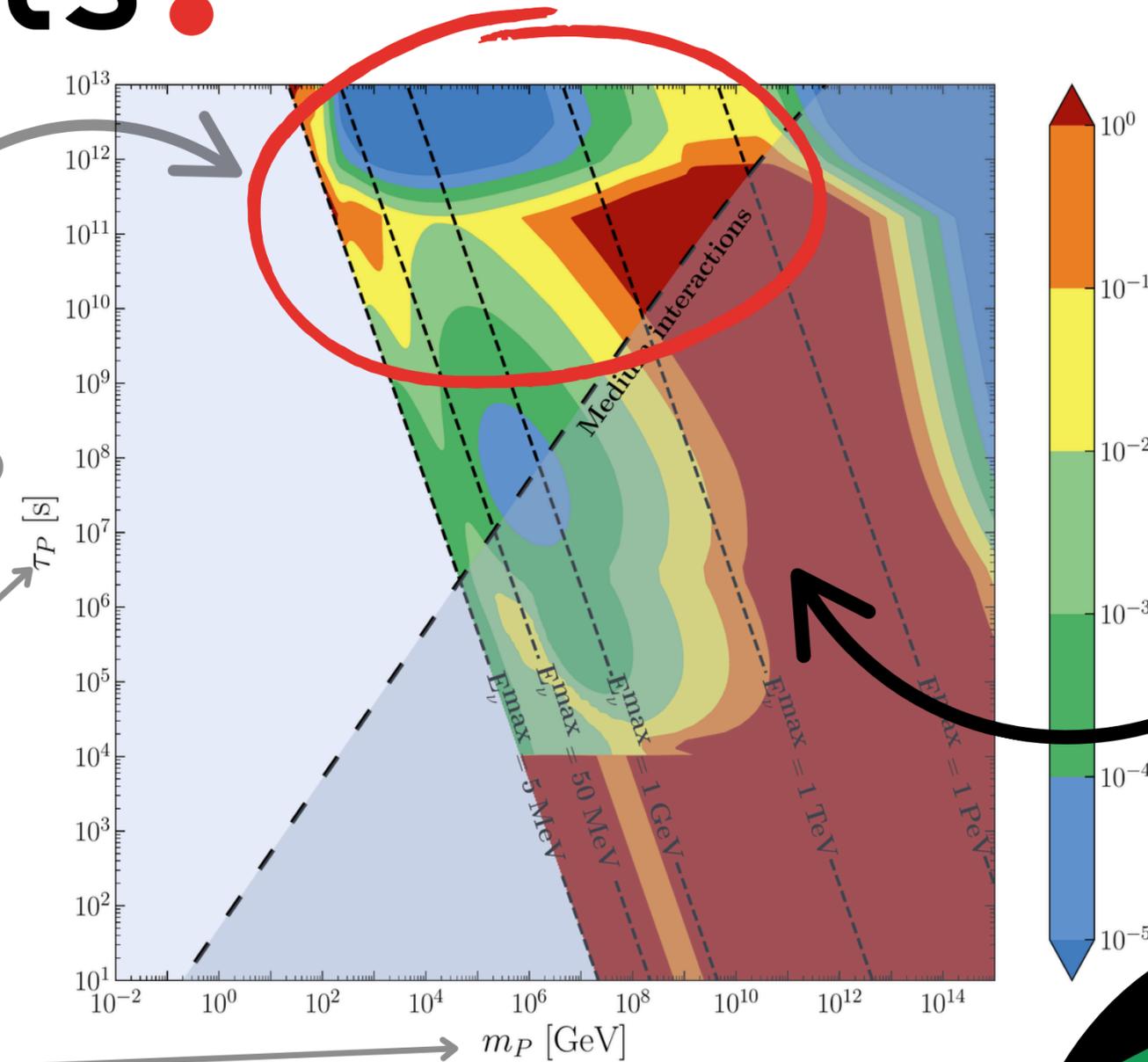
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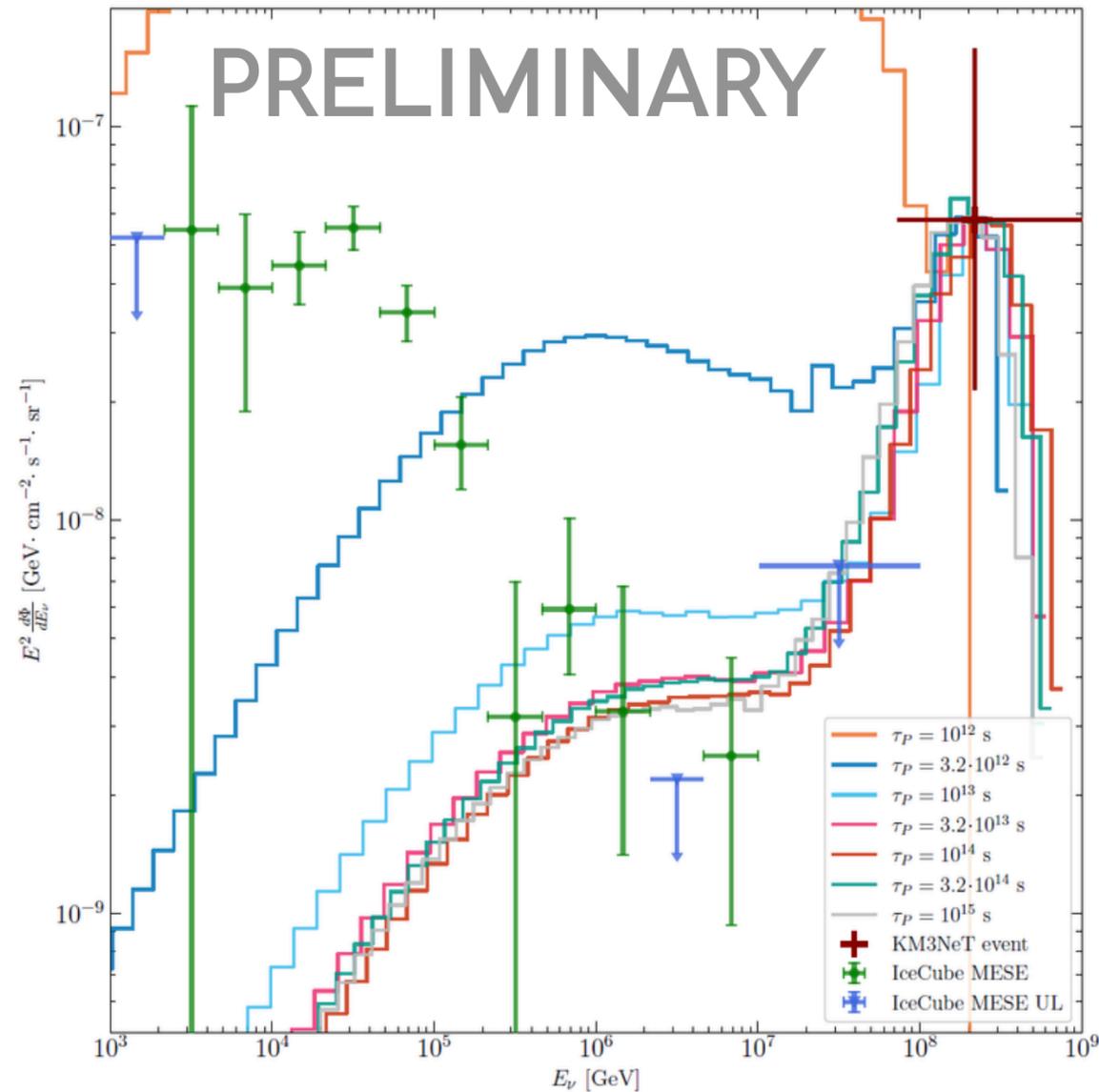
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Ongoing work: distortion of the spectrum using Monte Carlo techniques

Results.



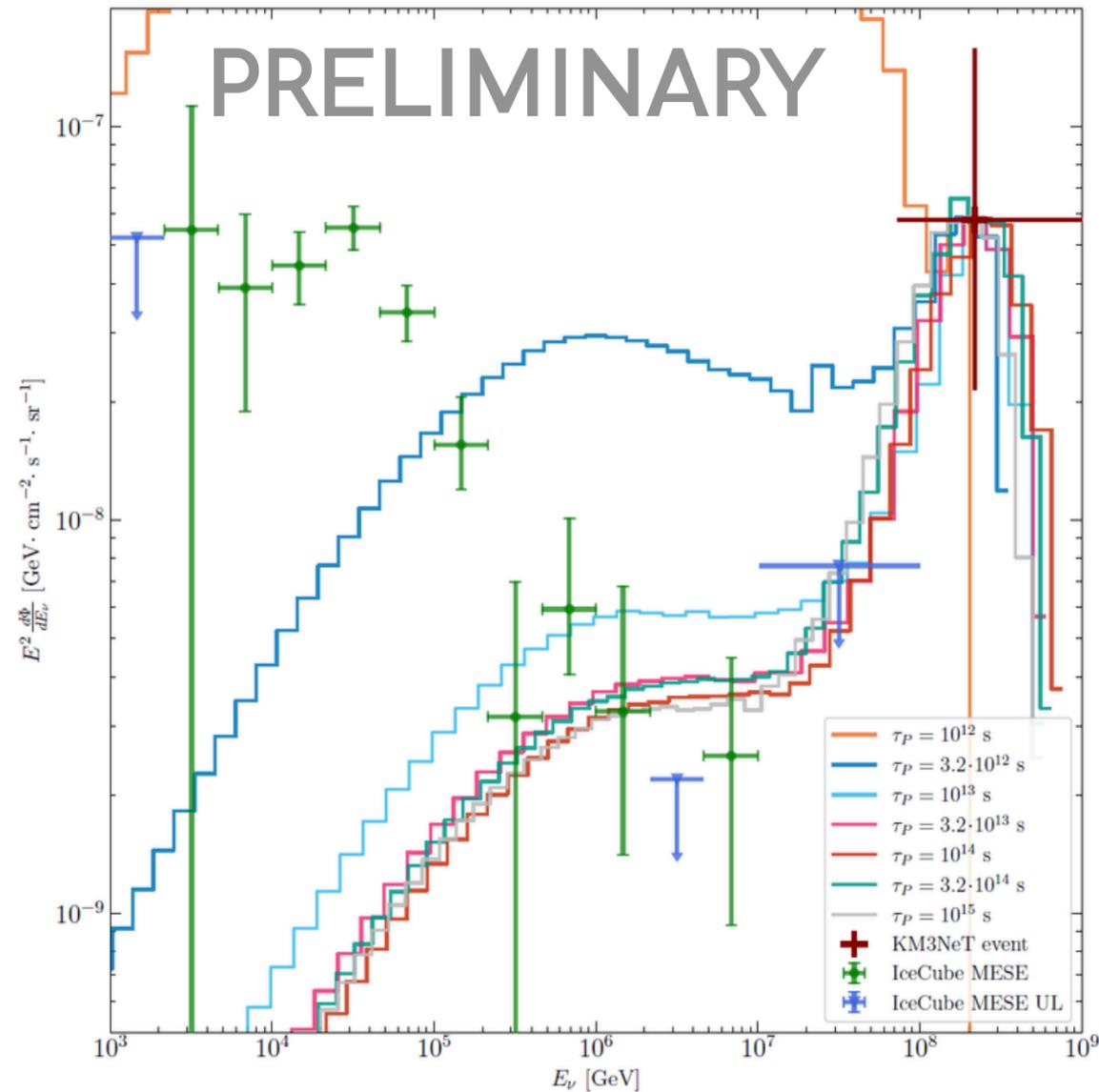
Monte carlo integration over adaptative redshift steps:

- Fully probabilistic approach
- Scatterings over CNB
- Final state radiation

Next step: joint likelihood analysis of IceCube 7.5 years HESE sample and the 2023 KM3Net event

τ_P [s]	m_P [GeV]	f_P
1.0×10^{12}	8.0×10^{11}	2.7×10^{-4}
3.2×10^{12}	5.3×10^{11}	2.0×10^{-6}
1.0×10^{13}	4.0×10^{11}	1.2×10^{-7}
3.2×10^{13}	2.3×10^{11}	3.9×10^{-8}
1.0×10^{14}	1.3×10^{11}	1.6×10^{-8}
3.2×10^{14}	5.0×10^{10}	8.4×10^{-9}
1.0×10^{15}	2.0×10^{10}	3.6×10^{-9}

Results.



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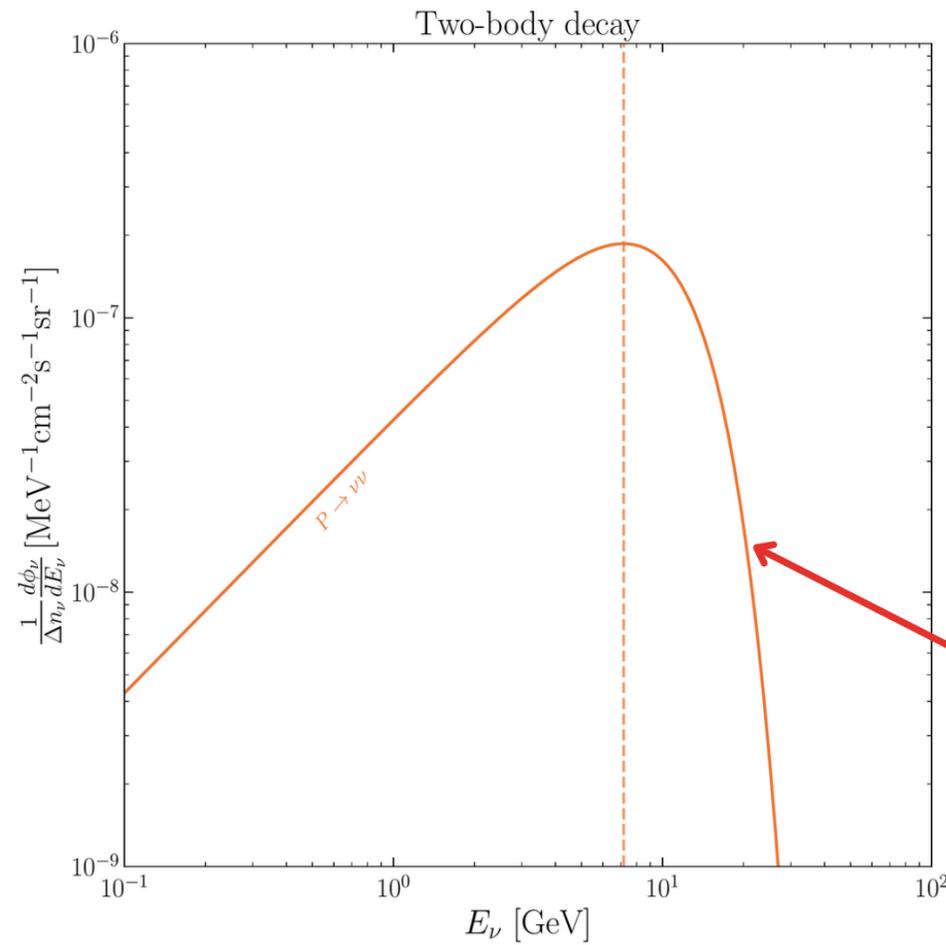
Stay tuned!

Thank you for your attention



[arXiv:2507.02063](https://arxiv.org/abs/2507.02063)
2604.xxxxxx

Sharp Spectral Features.



Gelmini, Gondolo, Sarkar 92'

$$\frac{d\phi_\nu}{dE_\nu} = \frac{n\Omega_P^0 \rho_{crit}^0}{4\pi m_P \tau_P} \int_0^\infty dz \frac{e^{-t(z)/\tau_P}}{H(z)} \left. \frac{dN}{dE} \right|_{E=E_\nu(1+z)}$$

Number of neutrinos per decay

Isotropy

Decaying particle density

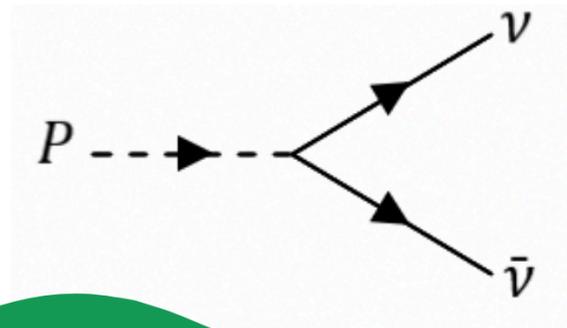
decay rate

Integration over the line of sight

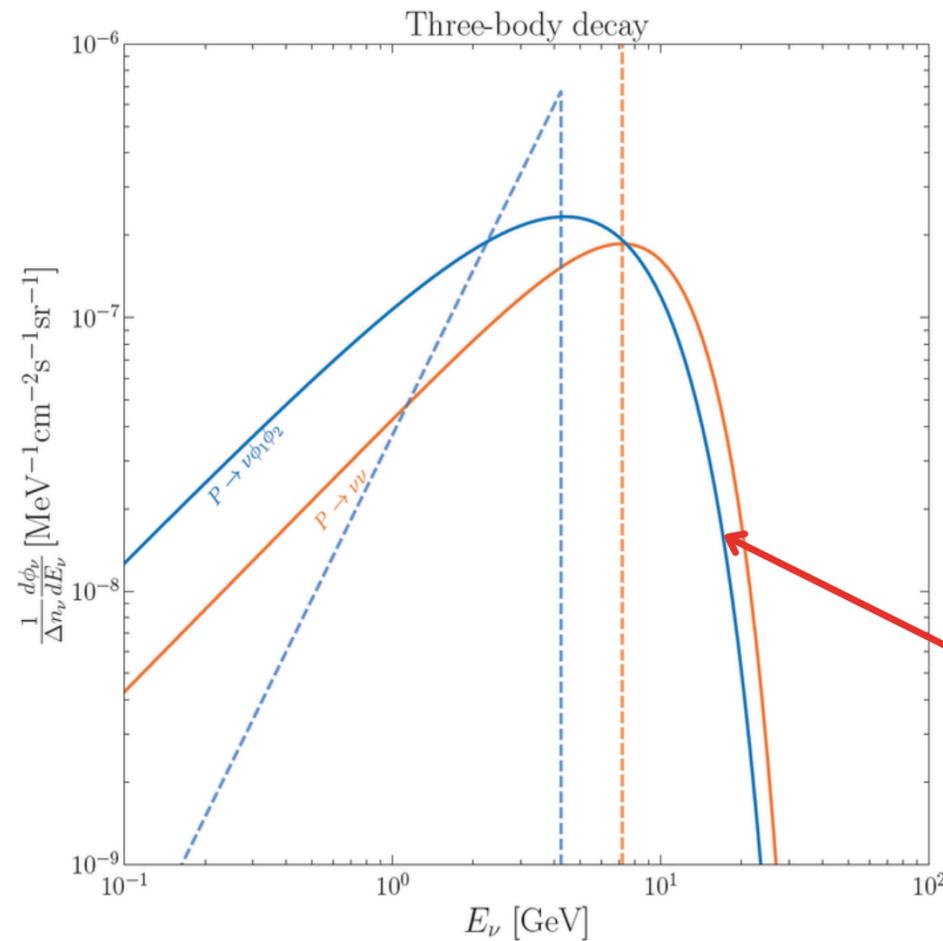
Exponential decay

Spectrum at production

2-body decay $P \rightarrow \nu \bar{\nu}$



Sharp Spectral Features.



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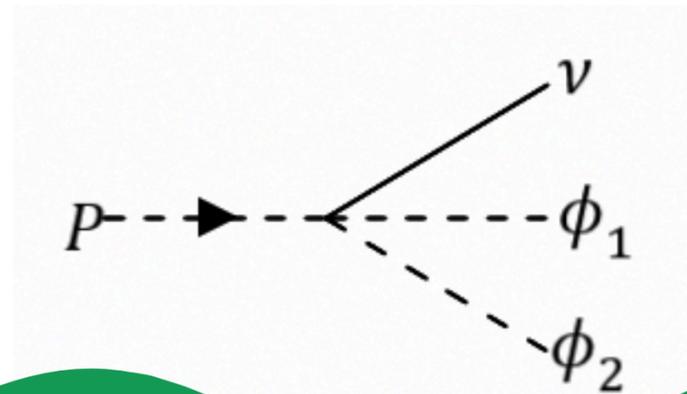
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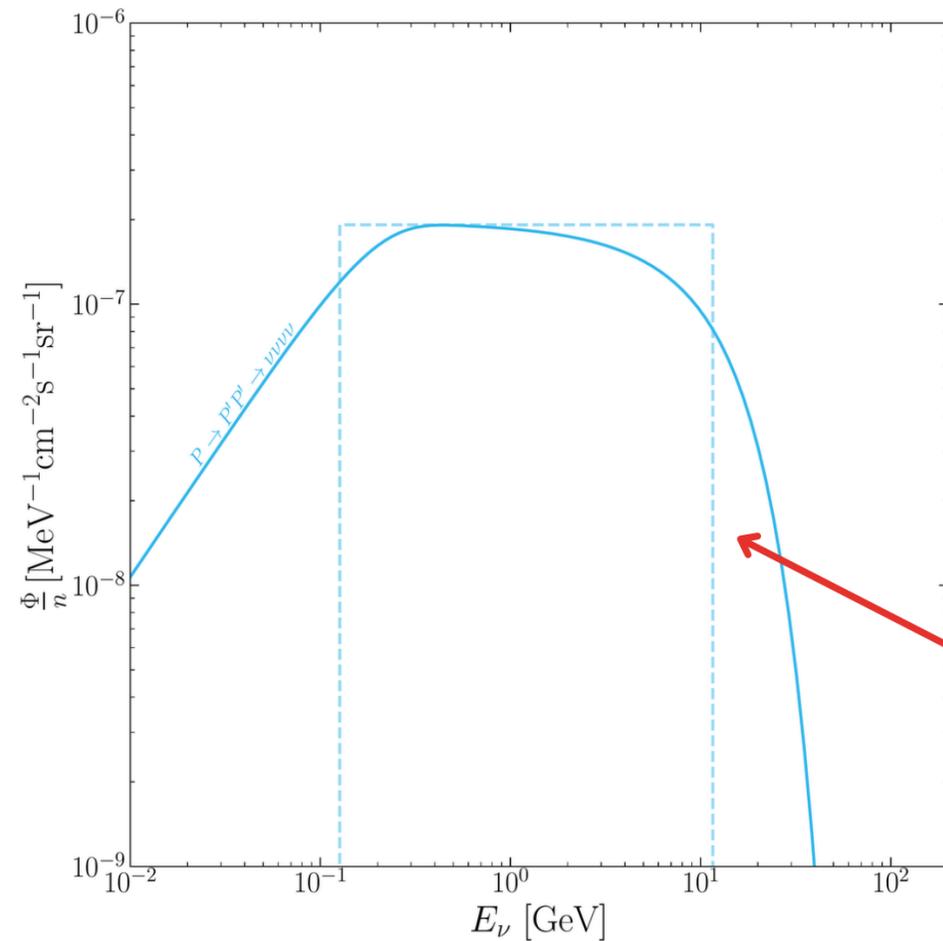
Exponential decay

Spectrum at production

3-body decay $P \rightarrow \nu\phi_1\phi_2$



Sharp Spectral Features.

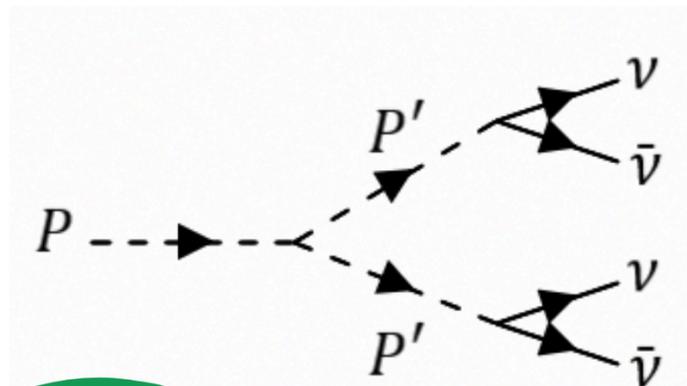


Ibarra, Lopez Gehler, Pato, Miguel, 12'

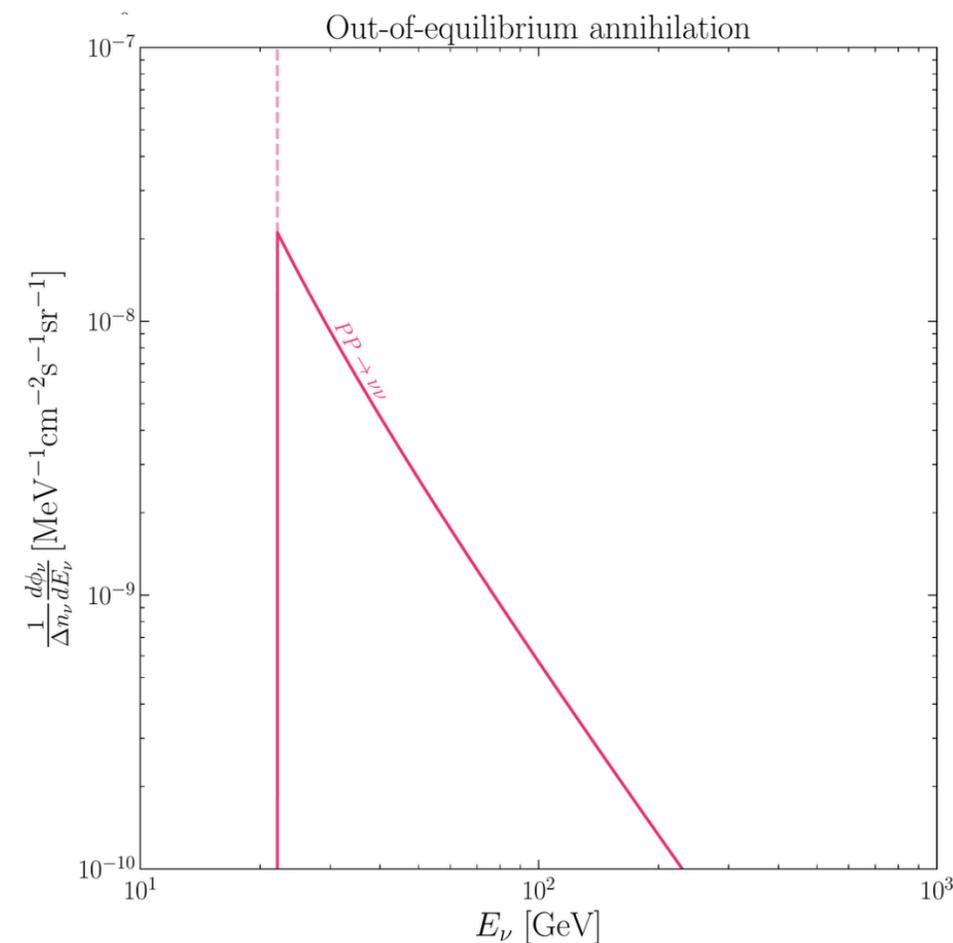
$$\frac{d\phi_\nu}{dE_\nu} = \frac{n\Omega_P^0 \rho_{crit}^0}{4\pi m_P \tau_P} \int_0^\infty dz \frac{e^{-t(z)/\tau_P}}{H(z)} \left. \frac{dN}{dE} \right|_{E=E_\nu(1+z)}$$

Number of neutrinos per decay (points to $n\Omega_P^0 \rho_{crit}^0$)
 Isotropy (points to 4π)
 Decaying particle density (points to m_P)
 decay rate (points to τ_P)
 Integration over the line of sight (points to $\int_0^\infty dz$)
 Exponential decay (points to $e^{-t(z)/\tau_P}$)
 Spectrum at production (points to $\left. \frac{dN}{dE} \right|_{E=E_\nu(1+z)}$)

Box shaped spectrum $P \rightarrow P' P' \rightarrow \nu \bar{\nu} \nu \bar{\nu}$



Sharp Spectral Features.

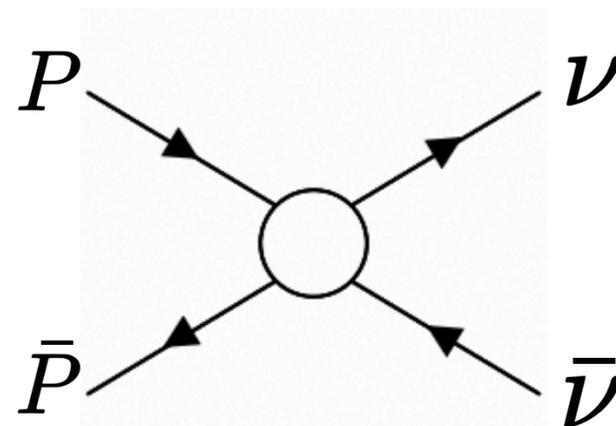


Out of equilibrium annihilation

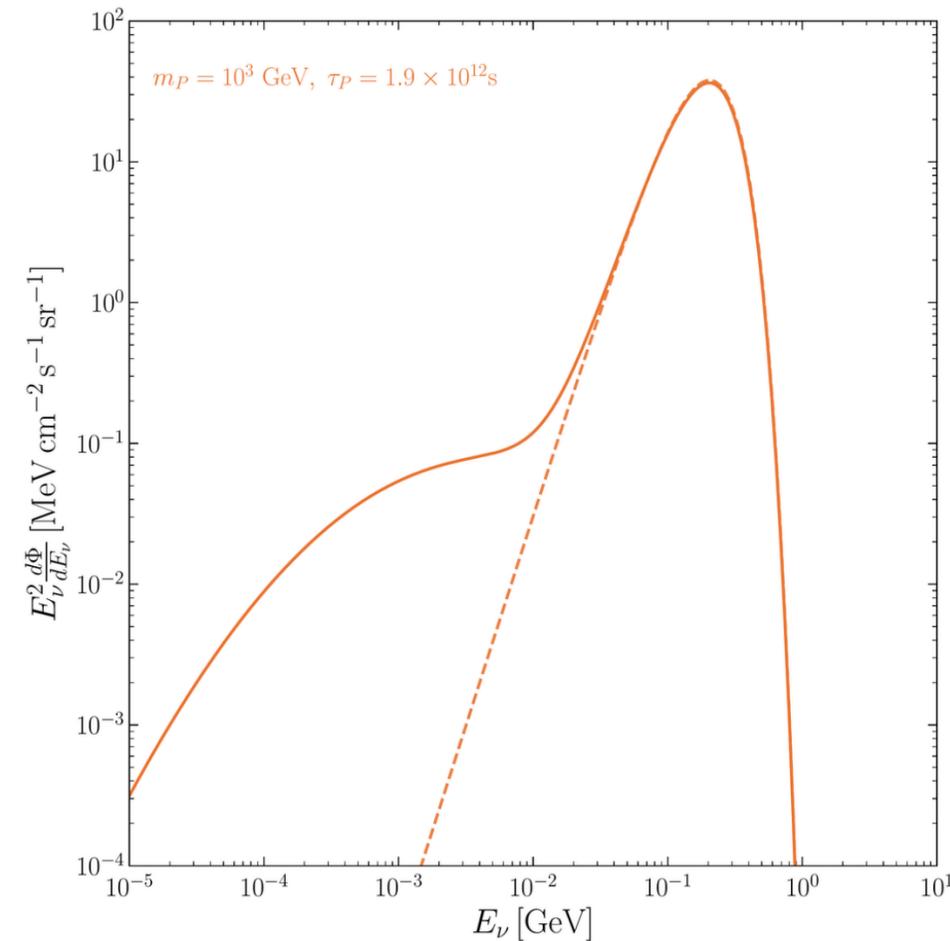
$$P\bar{P} \rightarrow \nu\bar{\nu}$$

New type of spectral feature

From, e.g., an asymmetric population of P oscillating into anti- P after a phase transition

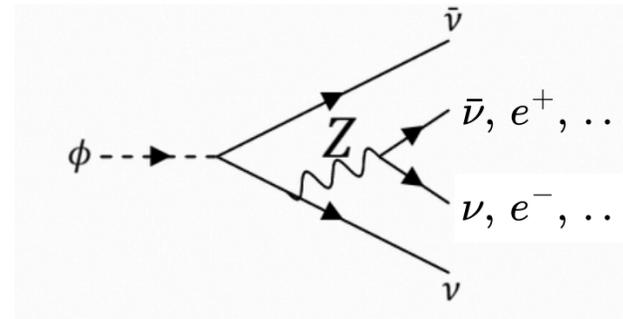


Sharp Spectral Features.

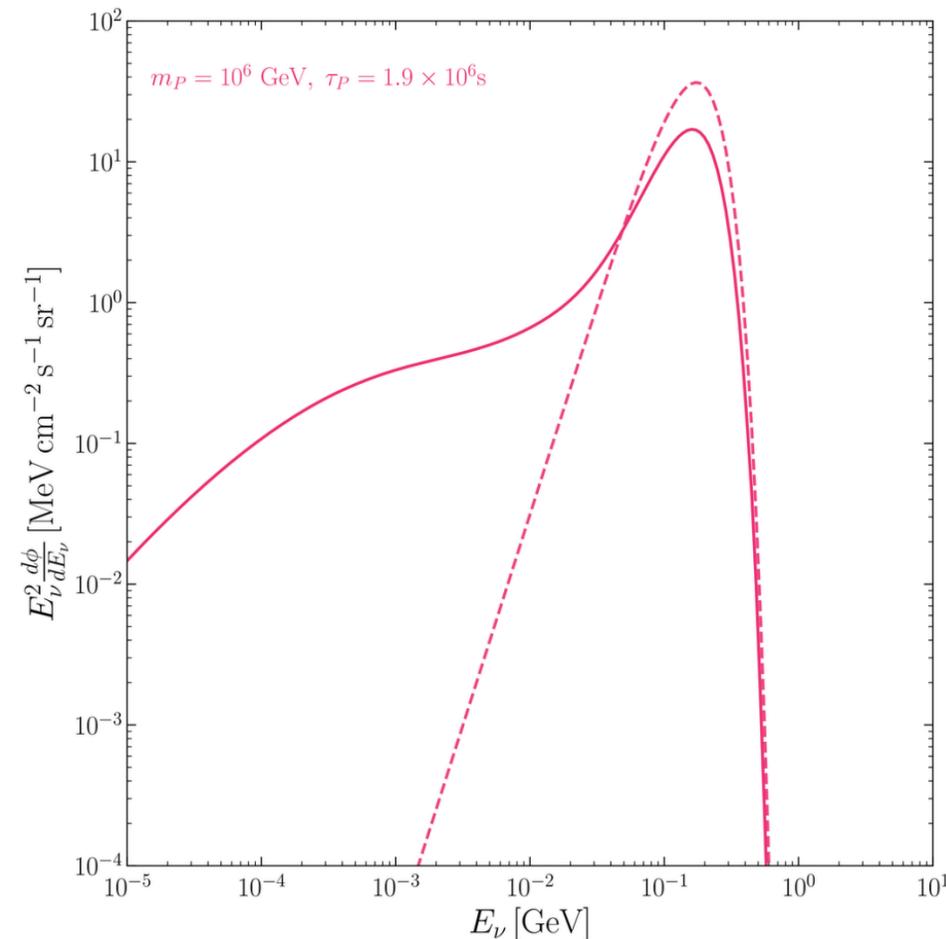


Final state radiation broadening

- If $E_\nu > M_{Z/W}$, gauge bosons can be radiated and generate a shower
- Production of (many) secondary neutrinos of lower energies
- Energy dependent process



Sharp Spectral Features.



Final state radiation broadening

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**Broadening of the peak
mostly due to redshift effect**

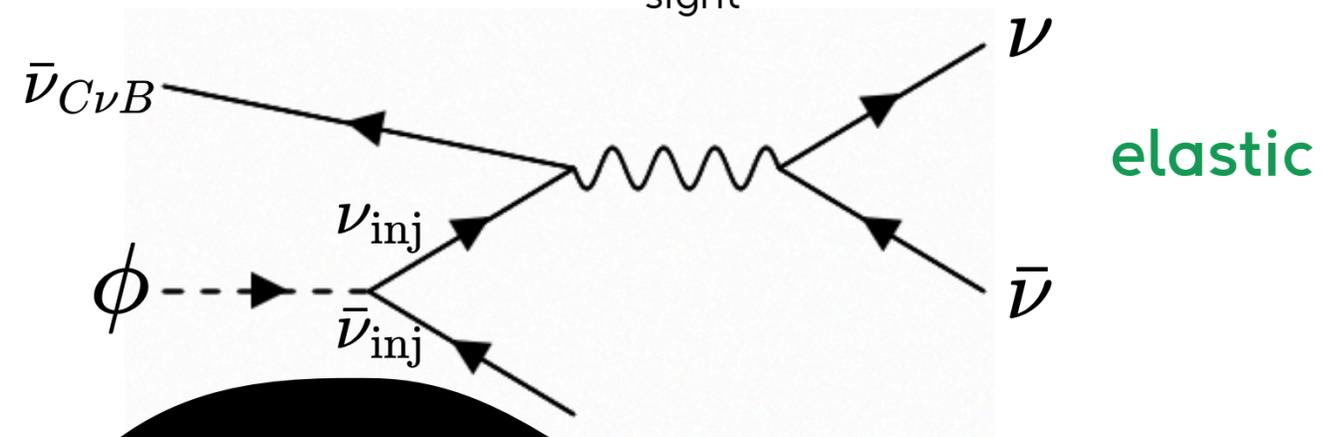
Medium interactions.

$$S_\nu(z_e, E_0) = \int_0^{z_e} \frac{dz}{(1+z)H(z)} \langle \sigma v \rangle n_{\nu BG}$$

Average number
of scattering

Integration
over the line of
sight

target neutrino
number
density



CνB:

- Decoupled at T~1 MeV from the thermal bath
- Has a present density of 336 cm^{-3}
- Non-relativistic today

$$T_{C\nu B}^0 = \left(\frac{4}{11} \right)^{1/3} T_{\text{CMB}}^0 \simeq 1.95\text{K}$$

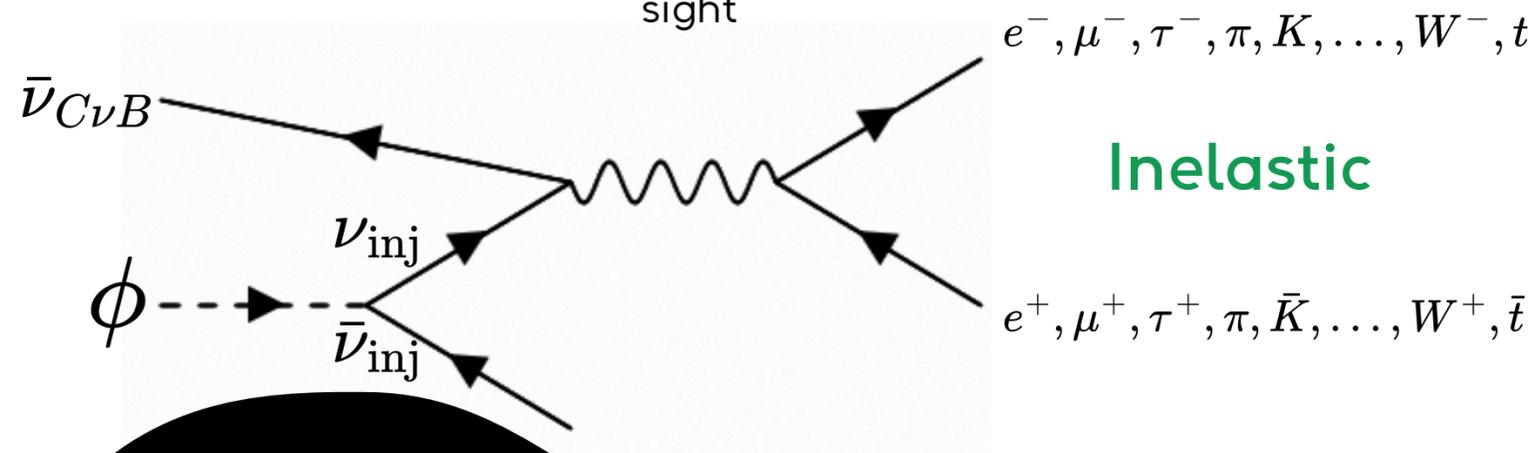
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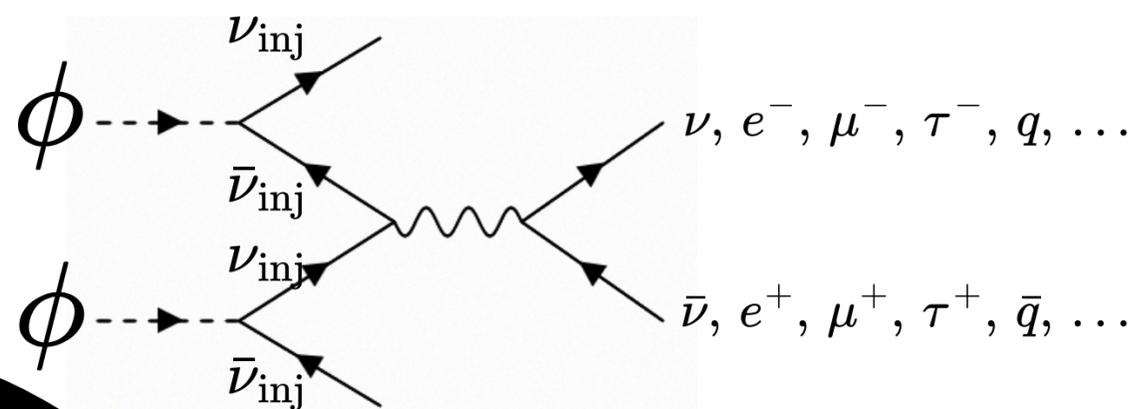
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Average number of scattering

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target neutrino number density



Self-scattering:

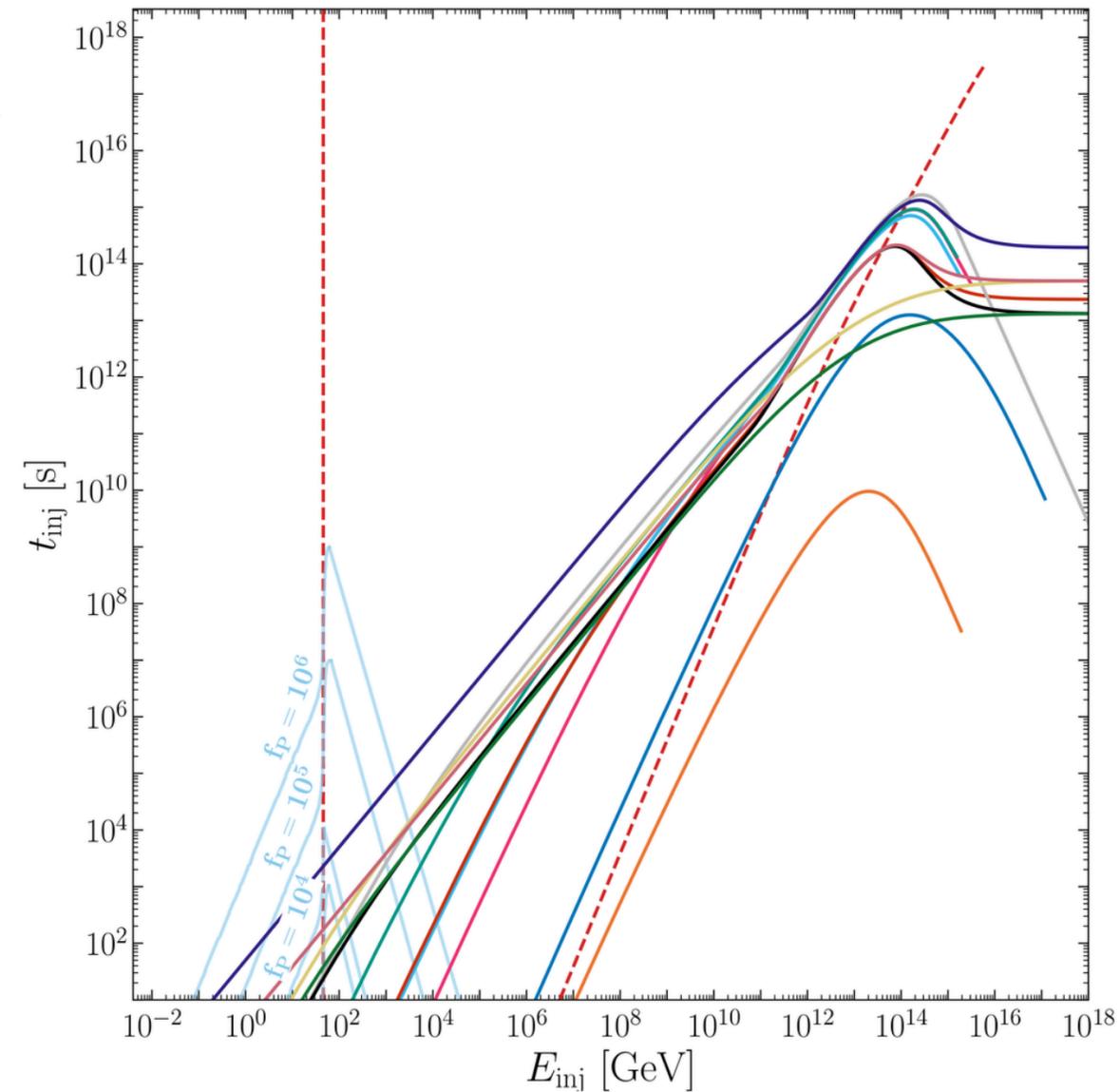
- Very low density, but high energies
- Numerically hard (triple integral)
- Assume instantaneous decay, i.e. all neutrinos produced at the same redshift with energy $m/2$

Medium interactions.

$$S_\nu(z_e, E_0) = \int_0^{z_e} \frac{dz}{(1+z)H(z)} \langle \sigma v \rangle n_{\nu BG}$$

Average number of scattering
 Integration over the line of sight
 cross section averaged over target distribution function
 target neutrino number density

$$f = \frac{\Omega_P^0}{\Omega_{DM}^0}$$

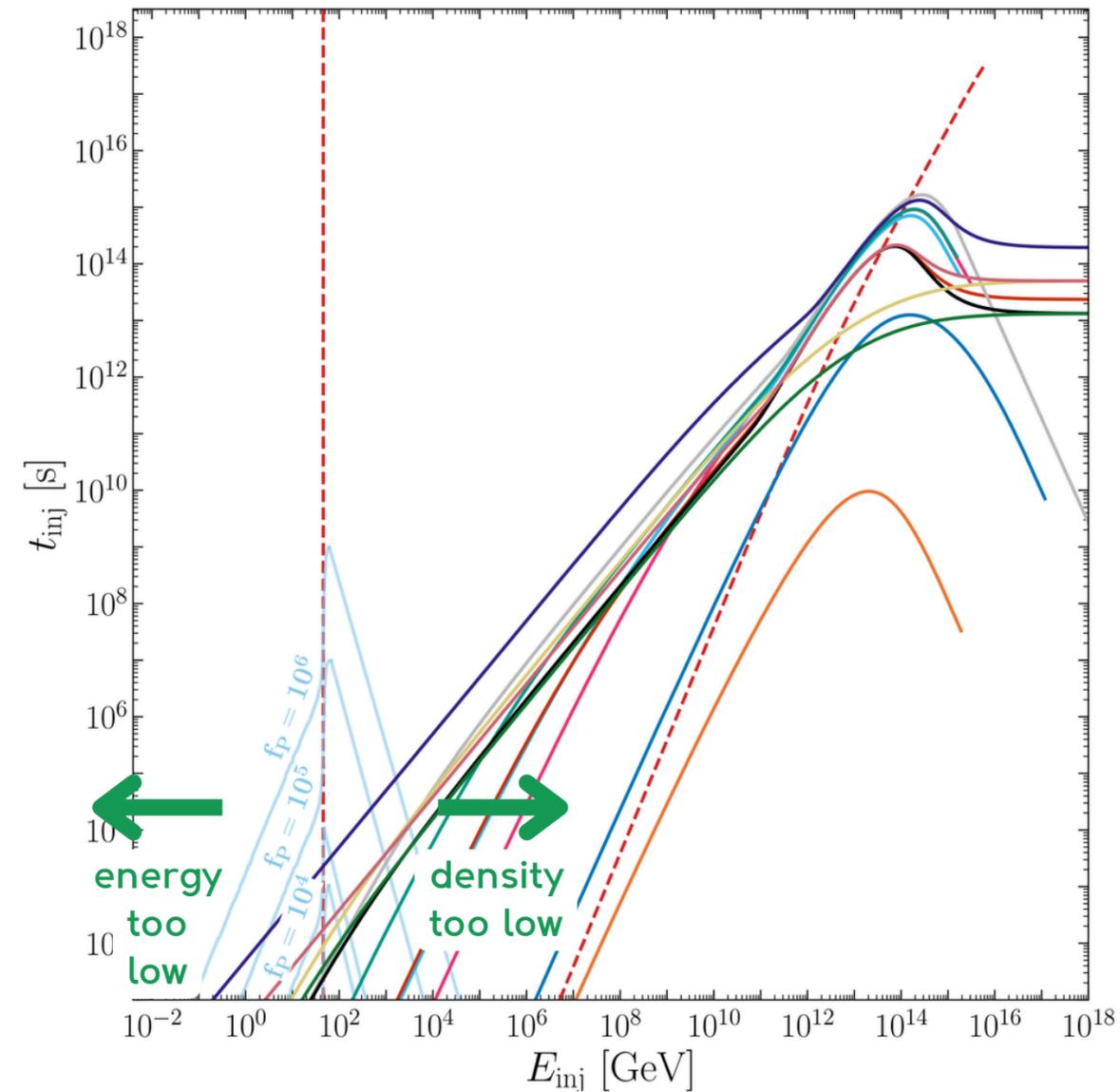


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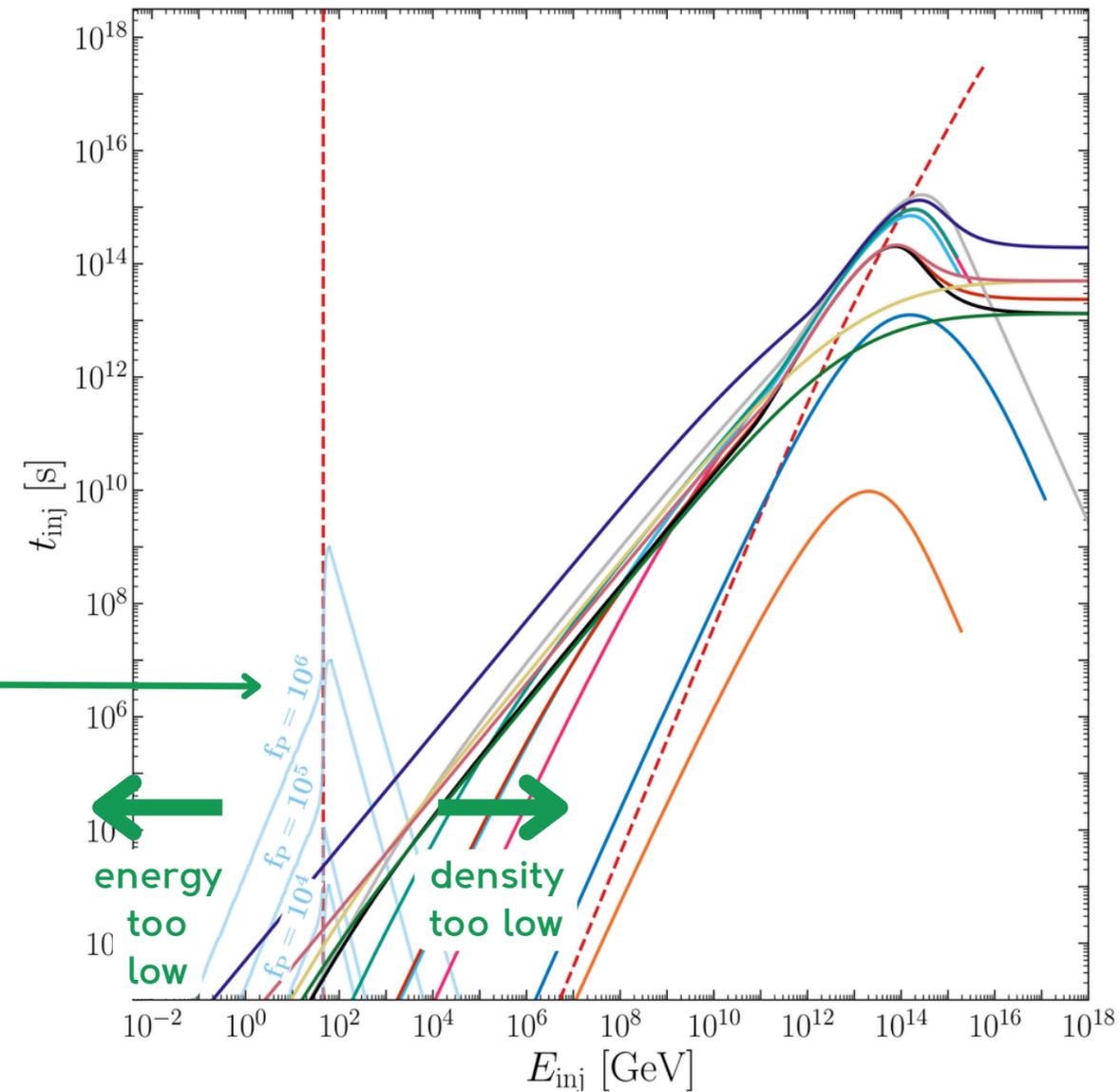
Integration over the line of sight

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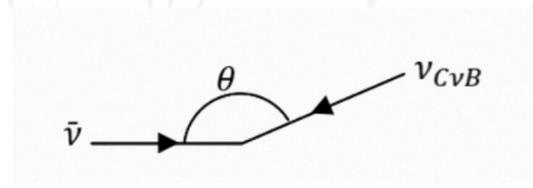
Self-scatterings are negligible except around the Z resonance

$$f = \frac{\Omega_P^0}{\Omega_{DM}^0}$$



Medium interactions.

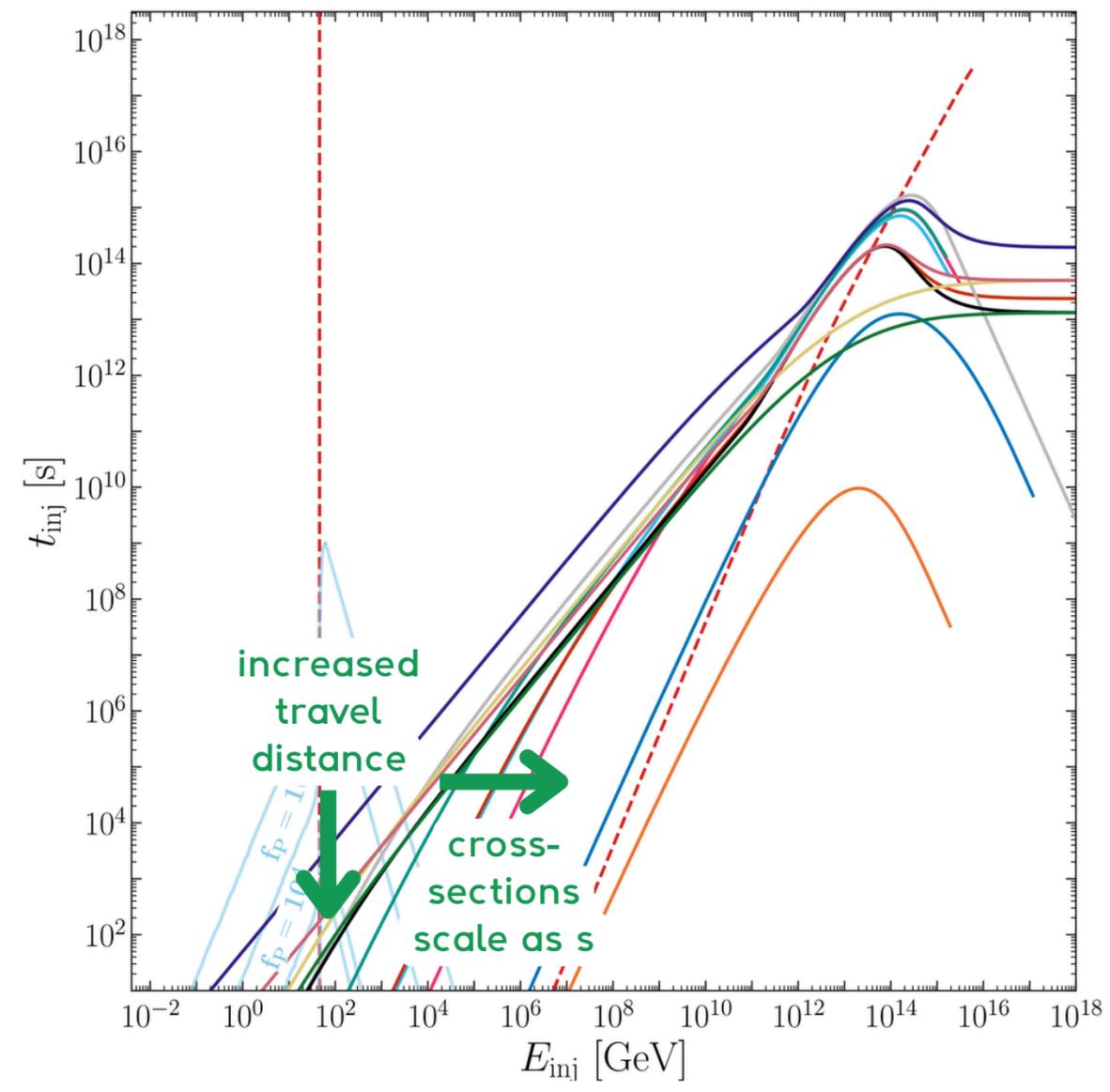
$$s = 2E_\nu E_{C\nu B}(1 - \cos(\theta))$$



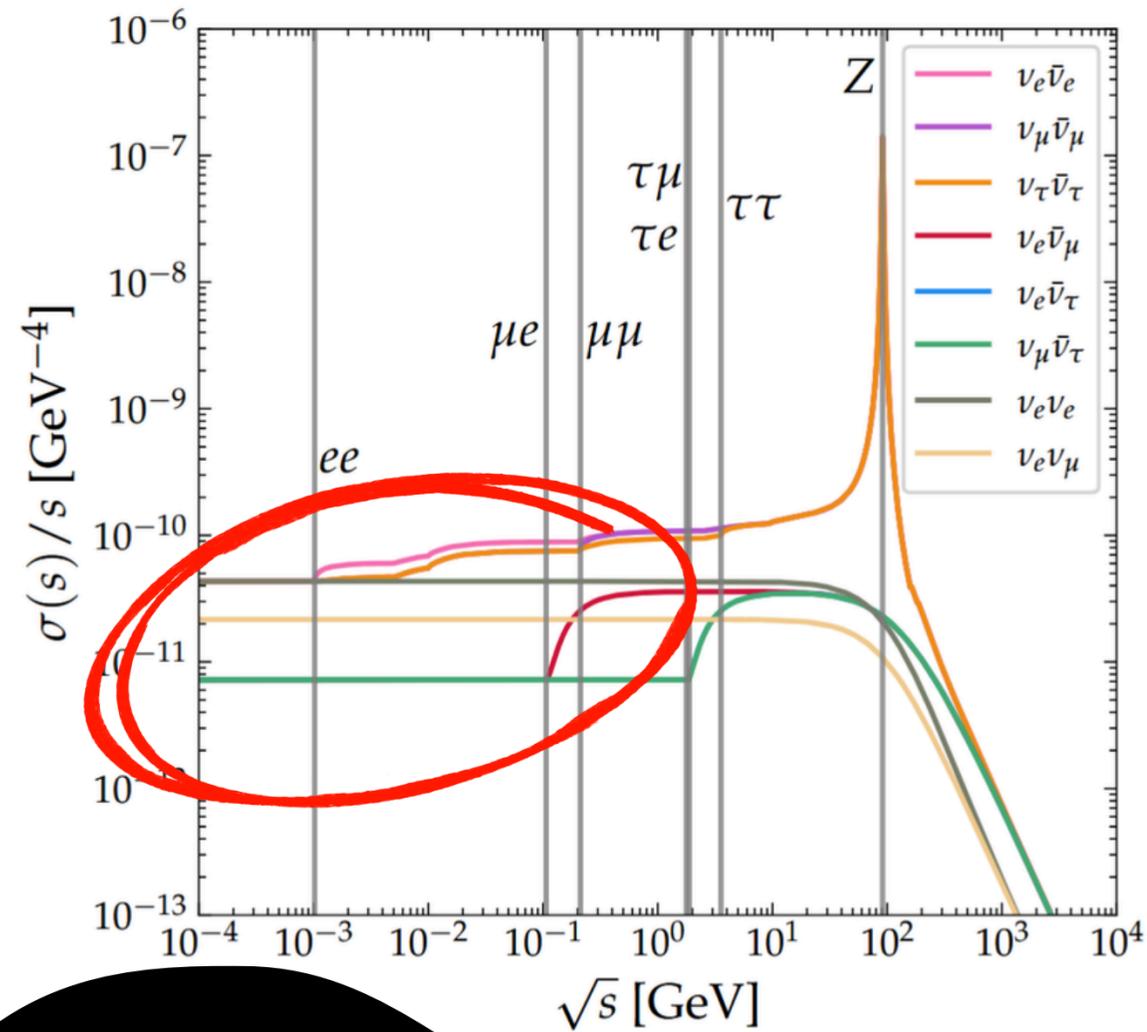
$$E_{inj} \ll E_\nu^{res}$$

$$E_\nu^{res} = \frac{m_Z^2}{4 \cdot 3.15 T_{\nu_{BG}}}$$

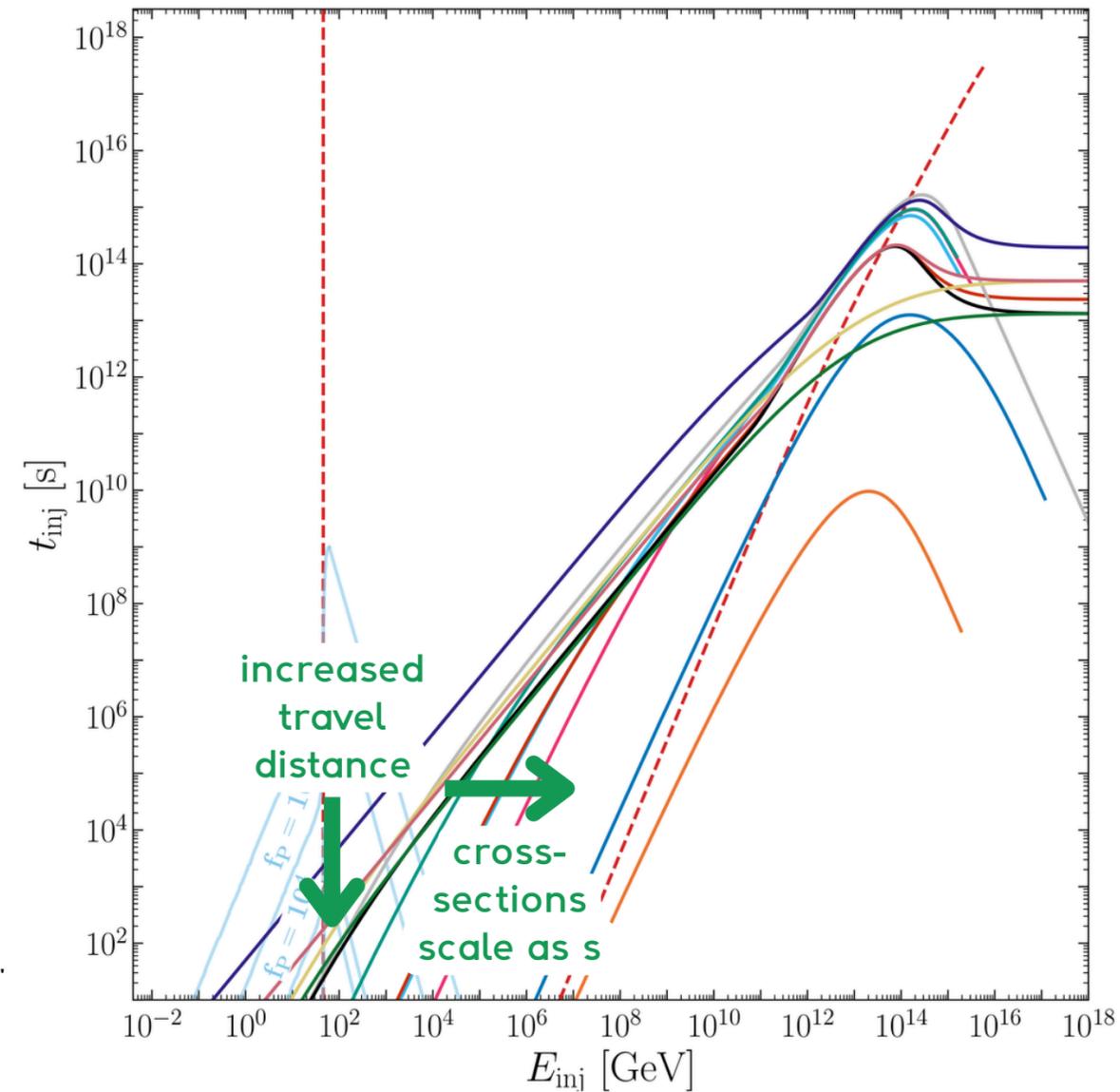
- $\nu_e \nu_{BG}^{(-)} \rightarrow \nu_x \nu_y^{(-)(-)}$
- $\nu_e \nu_{BG}^- \rightarrow e^- e^+$
- $\nu_e \nu_{BG}^- \rightarrow \mu^- e^+$
- $\nu_e \nu_{BG}^- \rightarrow e^- \mu^+$
- $\nu_e \nu_{BG}^- \rightarrow \mu^- \mu^+$
- $\nu_e \nu_{BG}^- \rightarrow \pi \pi$
- $\nu_e \nu_{BG}^- \rightarrow K \bar{K}$
- $\nu_e \nu_{BG}^- \rightarrow \tau^- \tau^+$
- $\nu_e \nu_{BG}^- \rightarrow D \bar{D}$
- $\nu_e \nu_{BG}^- \rightarrow B \bar{B}$
- $\nu_e \nu_{BG}^- \rightarrow W^- W^+$
- $\nu_e \nu_{BG}^- \rightarrow t \bar{t}$
- - - $s = m_Z^2$



Medium interactions.



Bianco, Depta, Frerick, Hambye, Hufnagel, Schmidt-Hoberg 25'

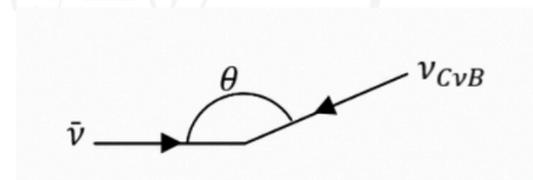


$S_\nu(z_i)$
 Average num
 of scatterin

ν_{BG}
 trino

Medium interactions.

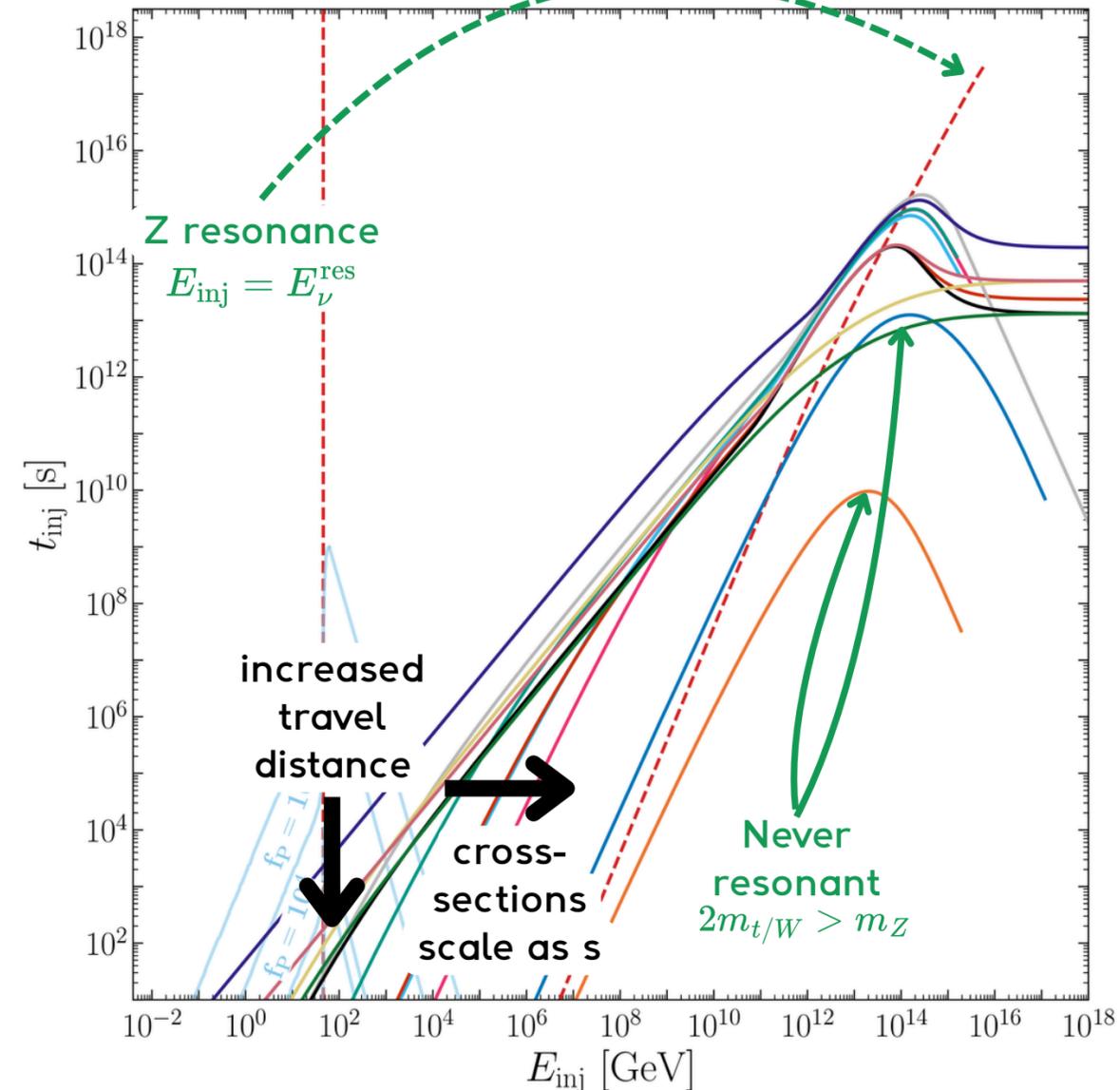
$$s = 2E_\nu E_{C\nu B}(1 - \cos(\theta))$$



$$E_{inj} \sim E_\nu^{res}$$

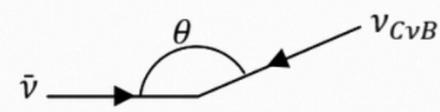
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- $\nu_e \nu_{BG}^- \rightarrow B \bar{B}$
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- $\nu_e \nu_{BG}^- \rightarrow t \bar{t}$
- $s = m_Z^2$



Medium interactions.

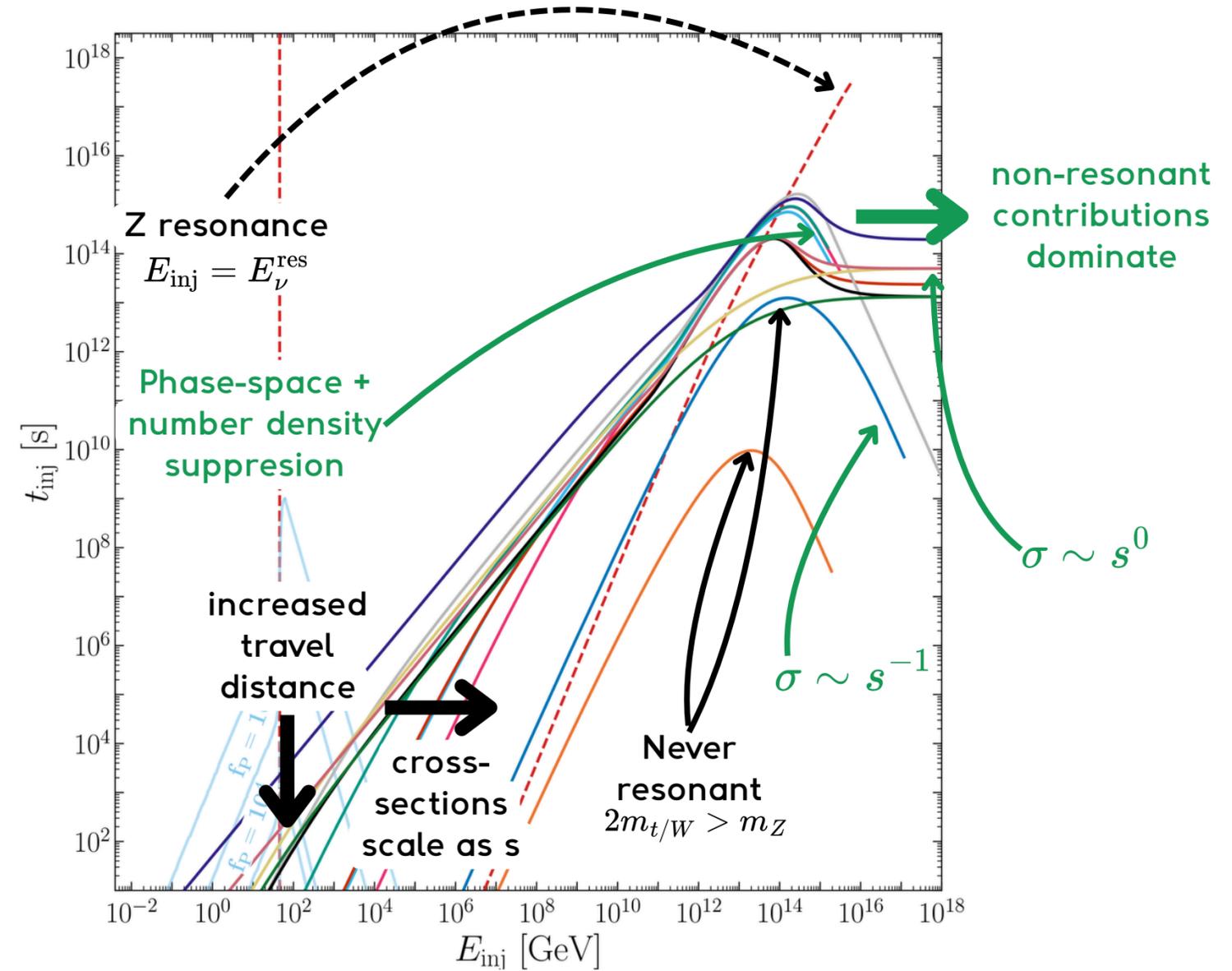
$$s = 2E_\nu E_{C\nu B}(1 - \cos(\theta))$$



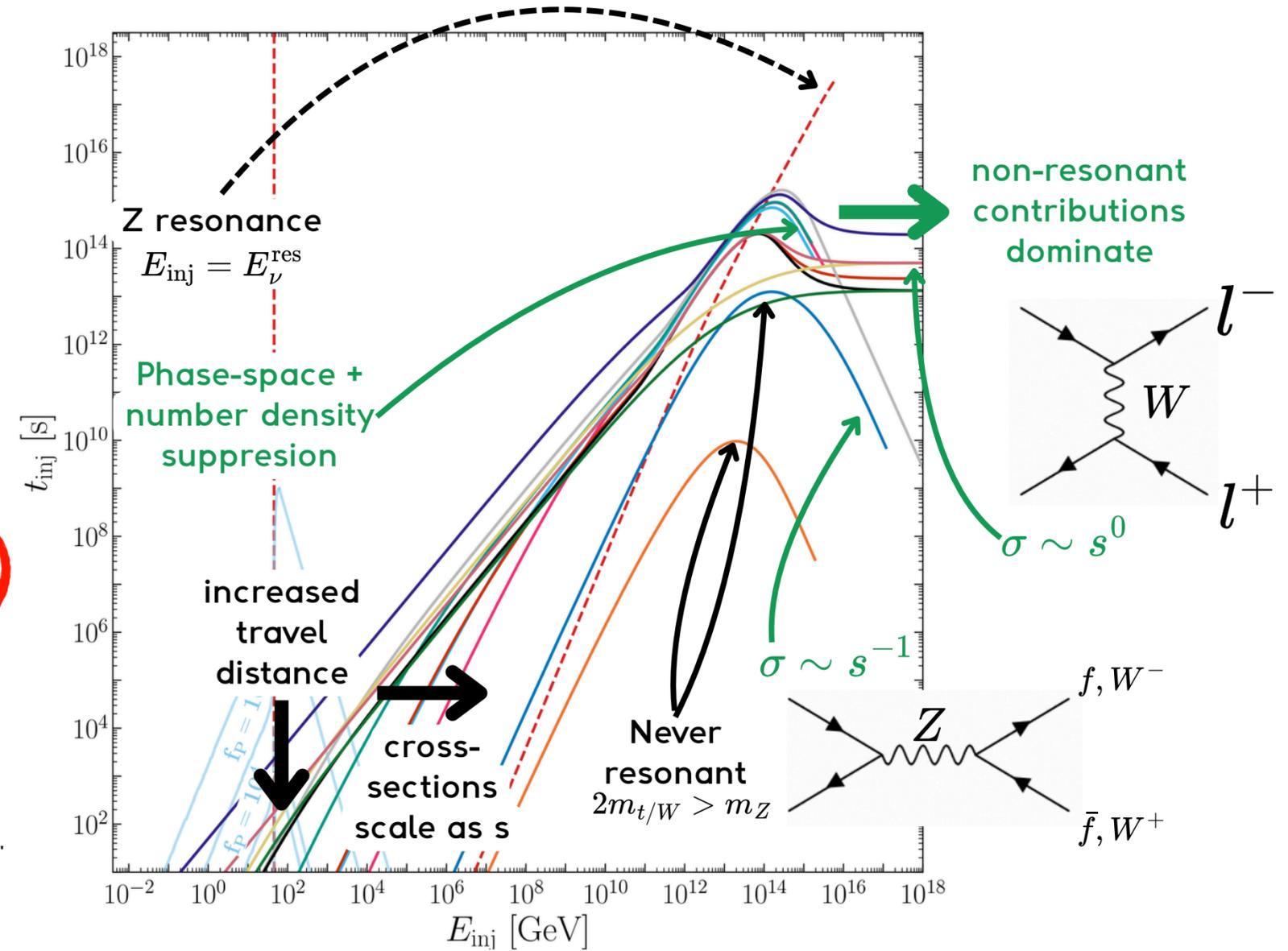
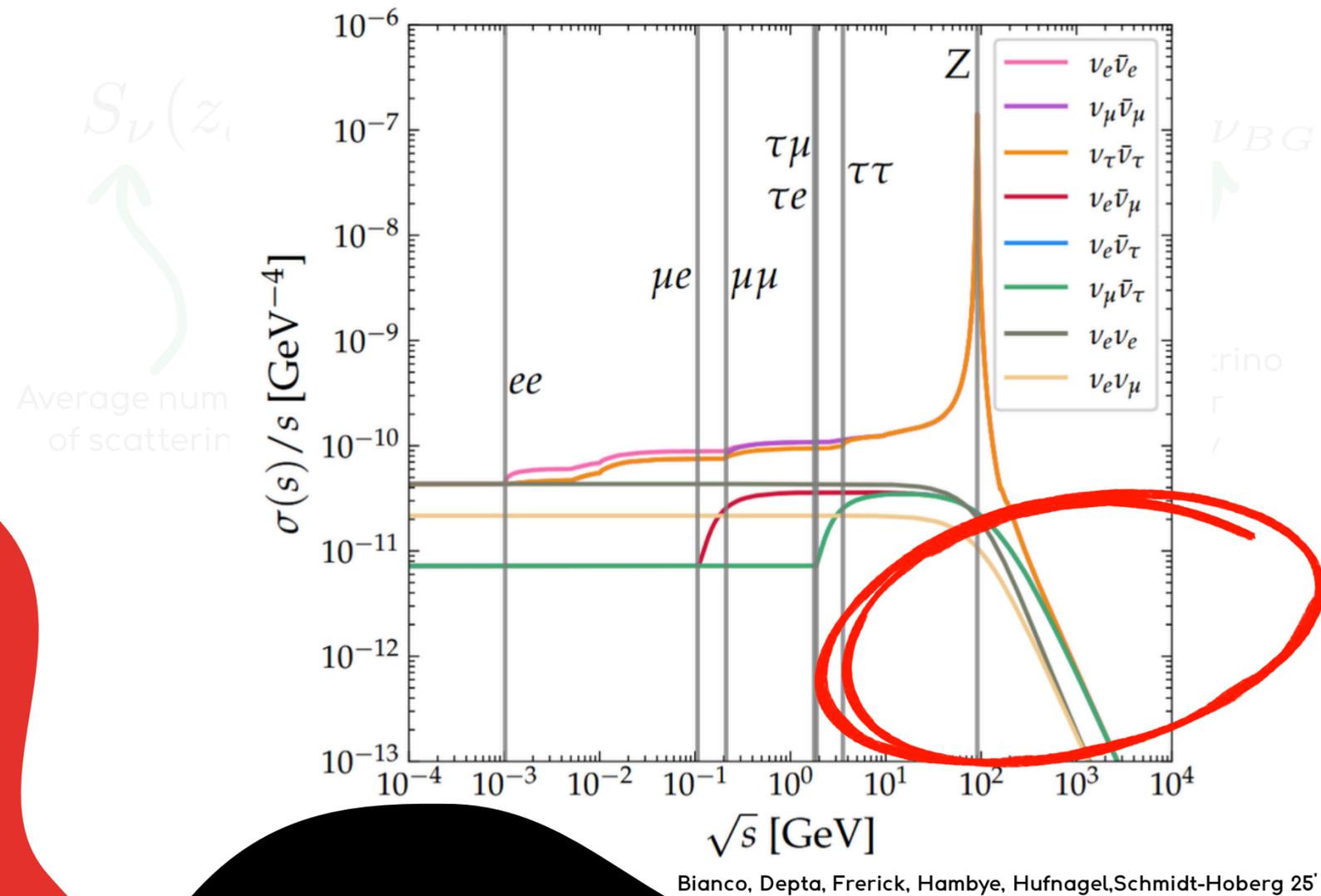
$$E_{inj} \gg \gg E_\nu^{res}$$

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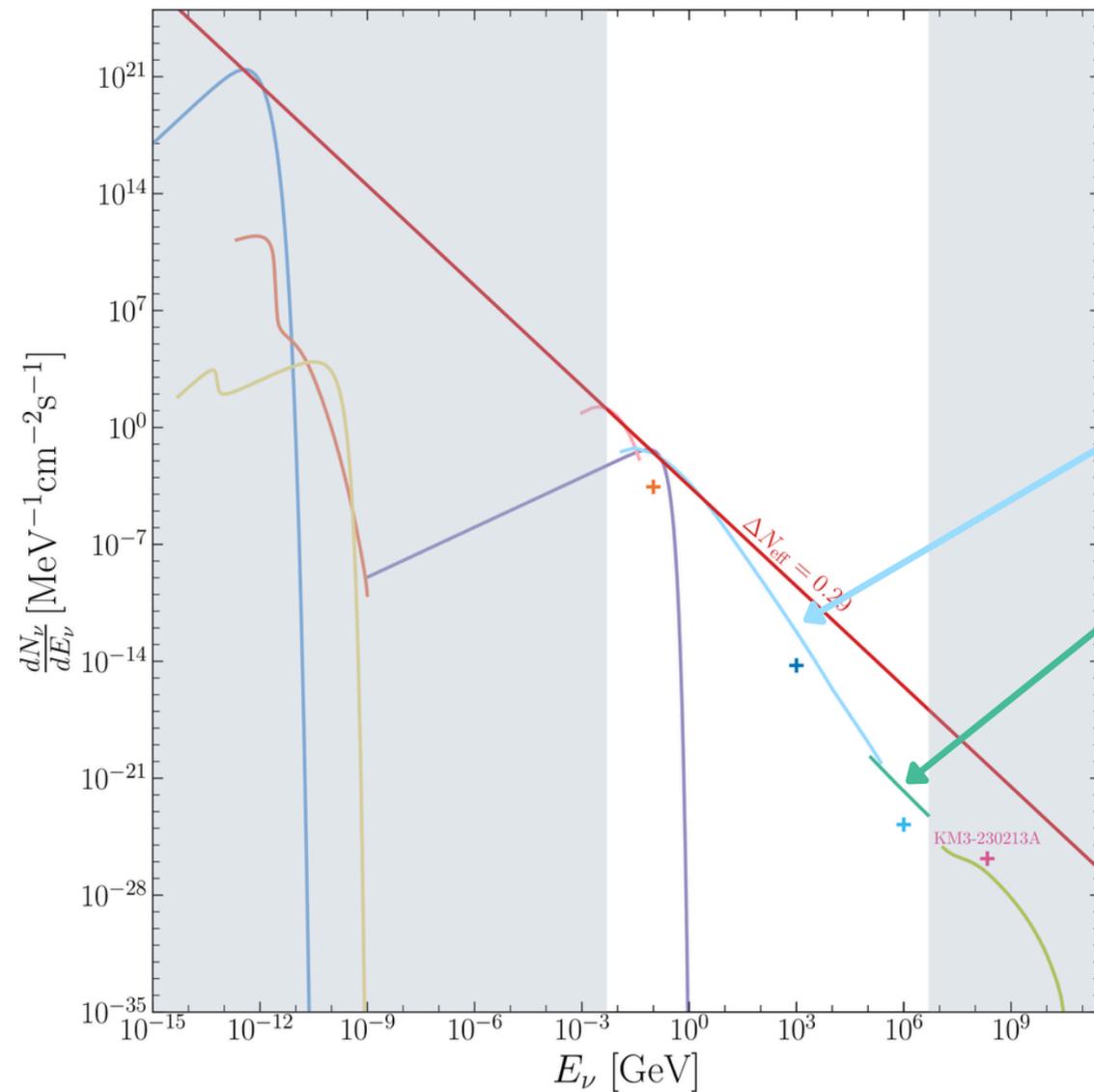
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- $\nu_e \nu_{BG}^- \rightarrow B \bar{B}$
- $\nu_e \nu_{BG}^- \rightarrow W^- W^+$
- $\nu_e \nu_{BG}^- \rightarrow t \bar{t}$
- $s = m_Z^2$



Medium interactions.



Constraints.



Vitagliano, Tamborra, Raffelt 19'

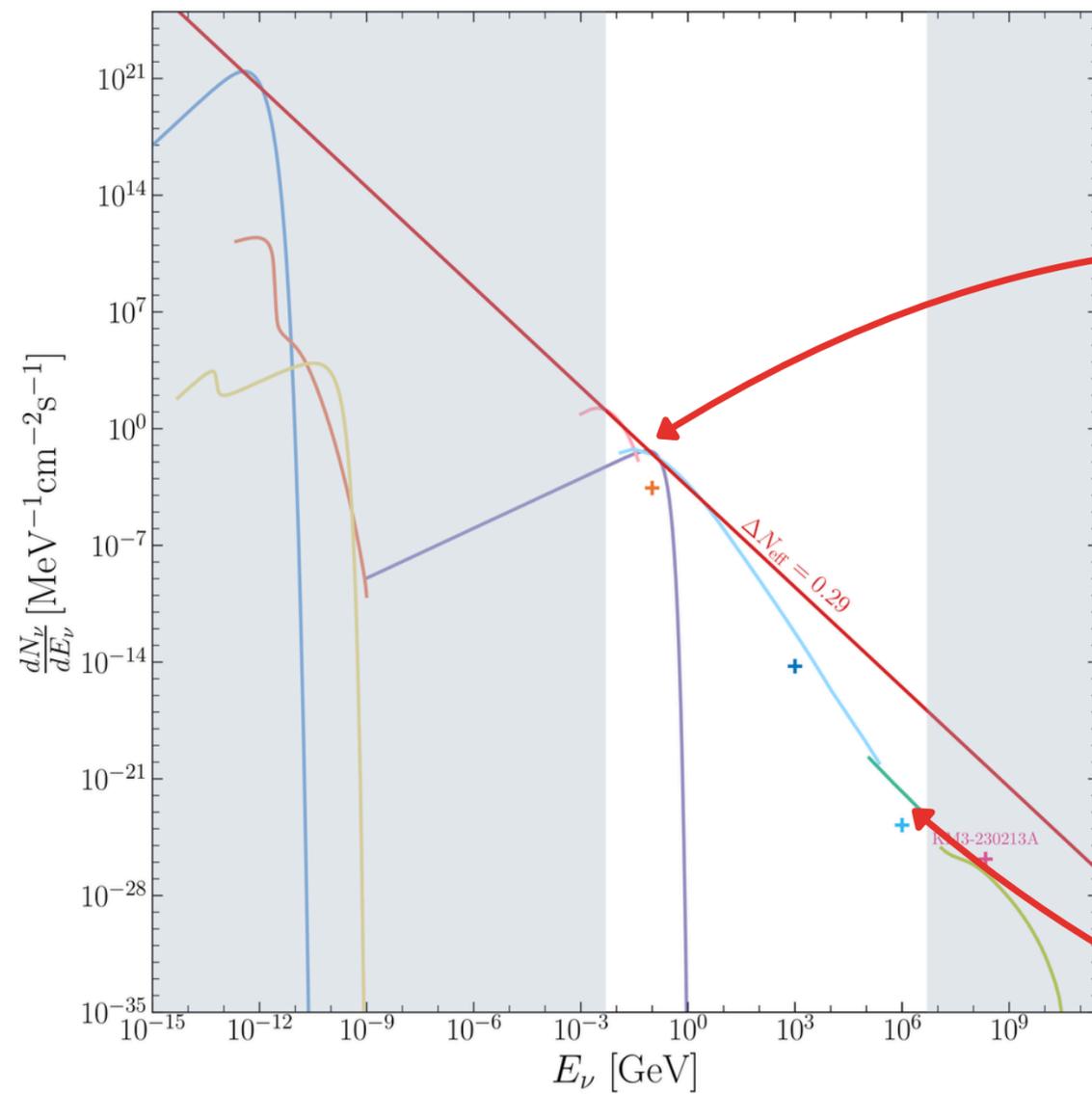
Observational:

- Atmospheric flux (SuperKamiokande, Icecube) > 50 MeV
- Astrophysical flux (Icecube) < 5 PeV
- DSNB > 5 MeV (Soon)

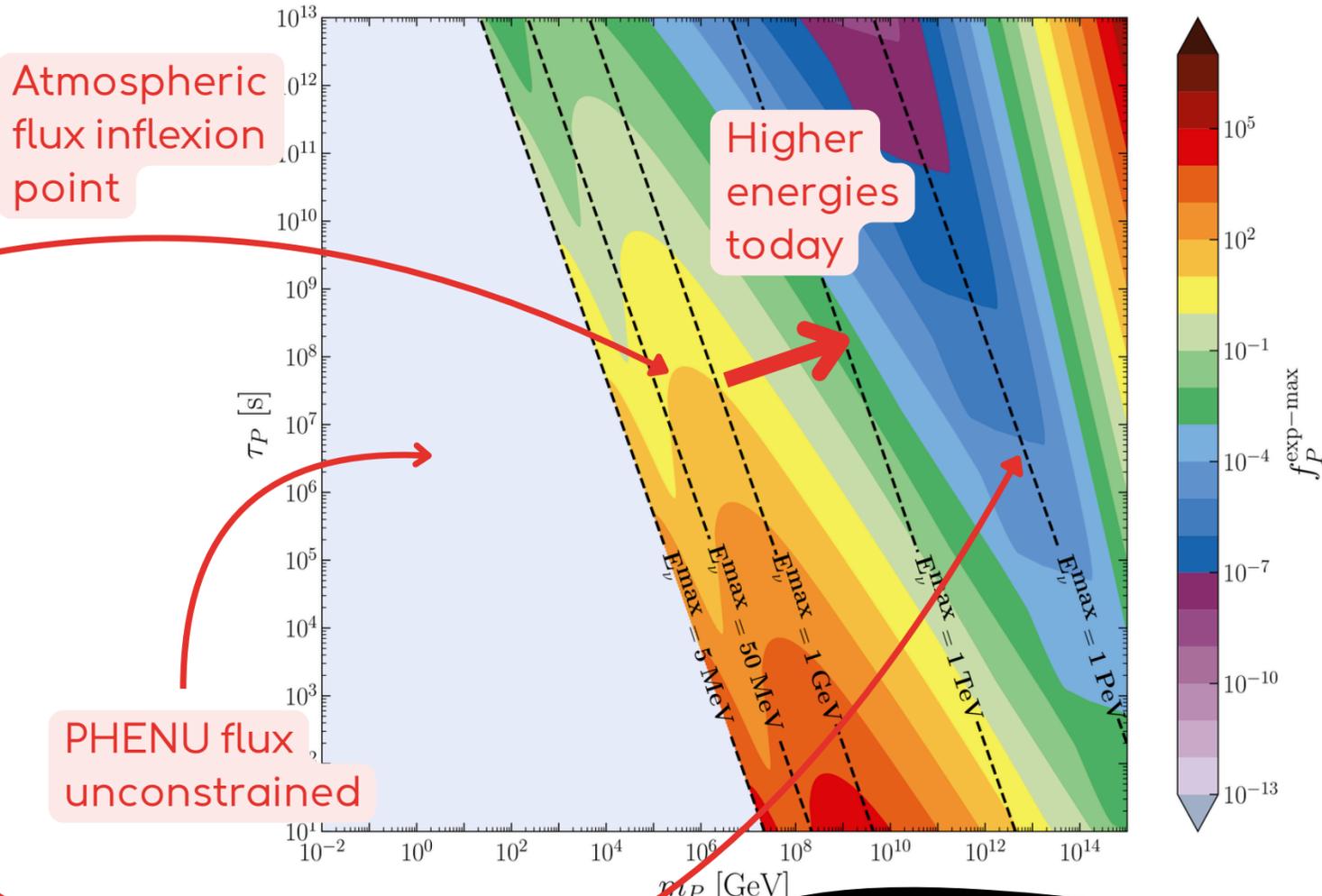
PHENU flux must be at most of the value of the observed flux

➔ Upper bound on f

Constraints.



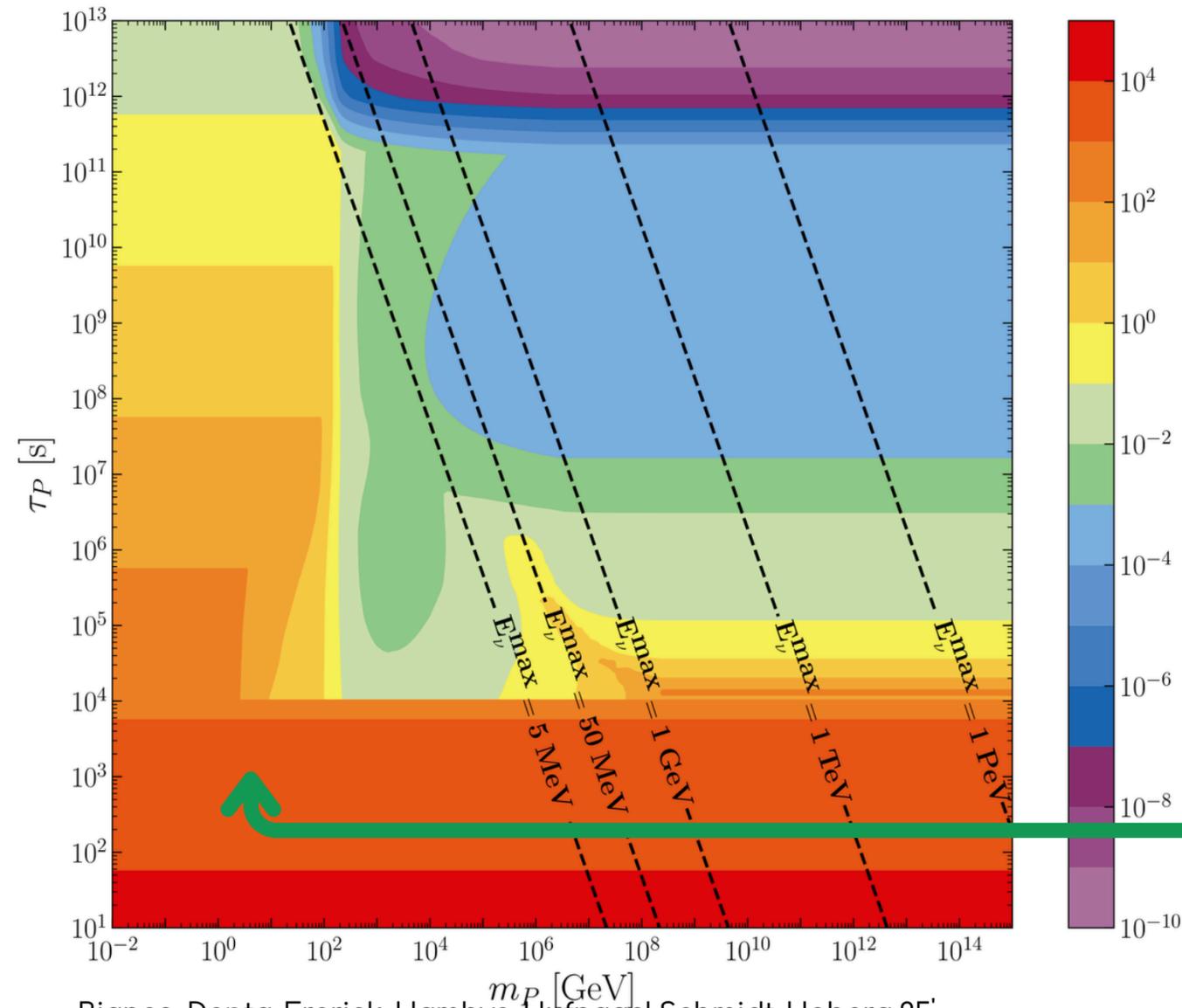
Vitagliano, Tamborra, Raffelt 19'



$$\frac{dN^{\text{PHENU}}}{dE} \propto E^{-2}$$

$$\frac{dN^{\text{Astro}}}{dE} \propto E^{-2}$$

Constraints



Bianco, Depta, Frerick, Hambye, Hufnagel, Schmidt-Hoberg 25'
 Hambye, Hufnagel, Lucca, 21'
 Acharya, Khatri, 19'

Cosmological:

Pl18[TT,TE,EE+lowE]	Λ CDM+ N_{eff}	$2.92^{+0.36}_{-0.37}$
		Planck '18

N_{eff} bound on additional neutrino energy density

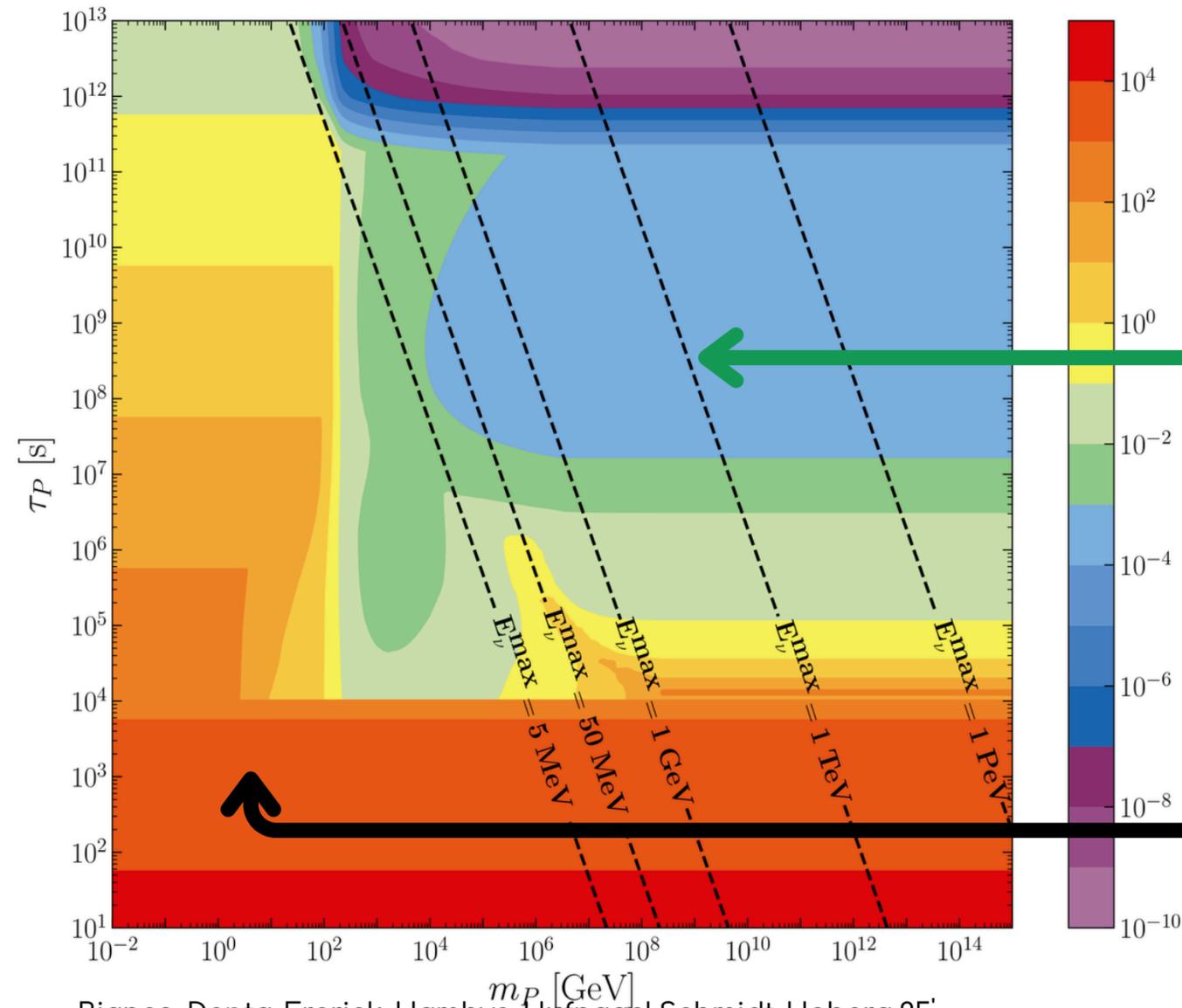
$$N_{\text{eff}}^{\text{SM}} \equiv \frac{8}{7} \left(\frac{11}{4} \right)^{4/3} \left(\frac{\rho_\nu}{\rho_\gamma} \right)$$

$$= 3.0432(2) \simeq 3.043$$

Cielo, Escudero, Mangano, Pisanti '23

Constraints

Cosmological:

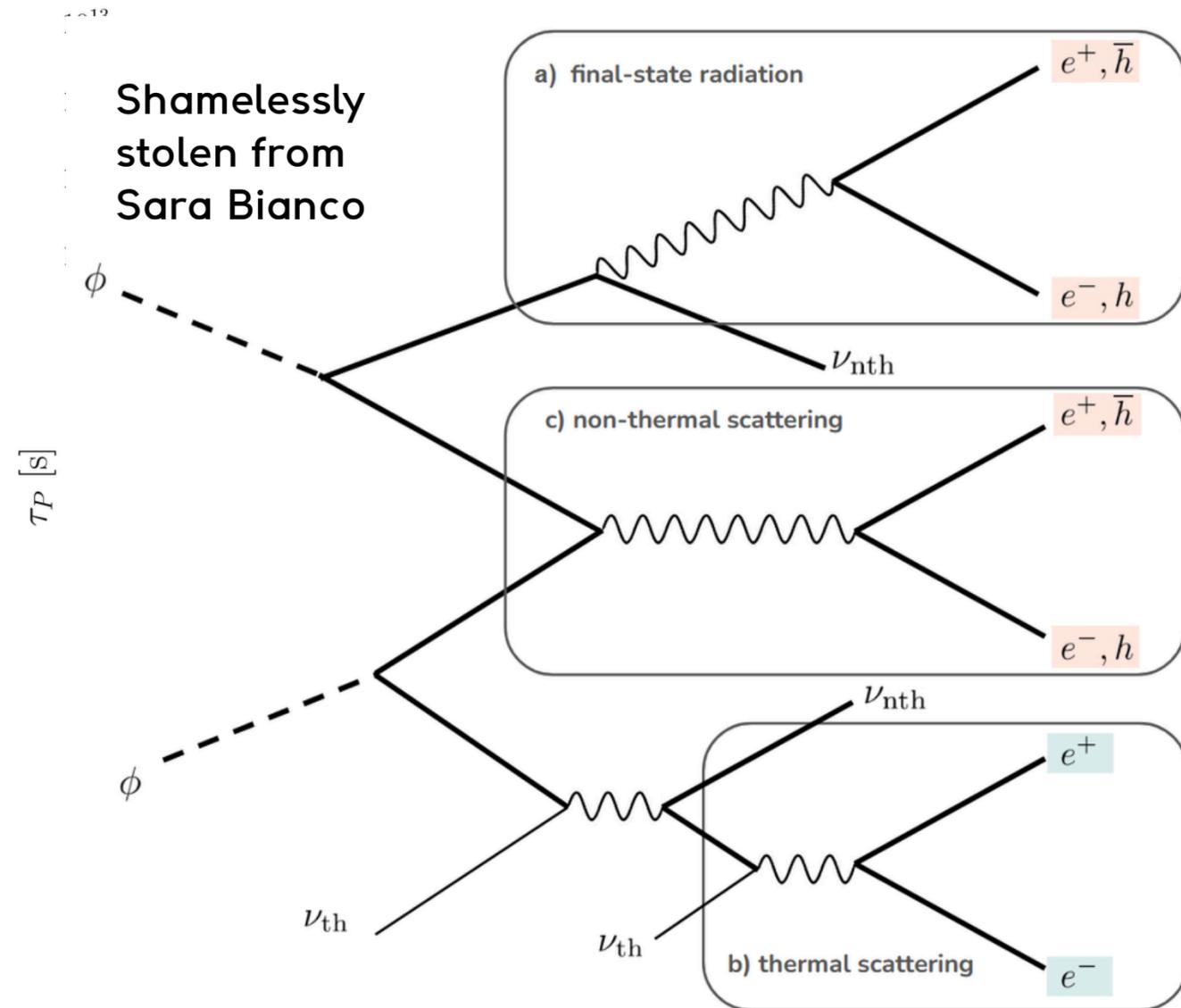


BBN bound from photo and hadro disintegration of light elements

N_{eff} bound on additional neutrino energy density

Bianco, Depta, Frerick, Hambye, Hufnagel, Schmidt-Hoberg 25'
 Hambye, Hufnagel, Lucca, 21'
 Acharya, Khatri, 19'

Constraints.



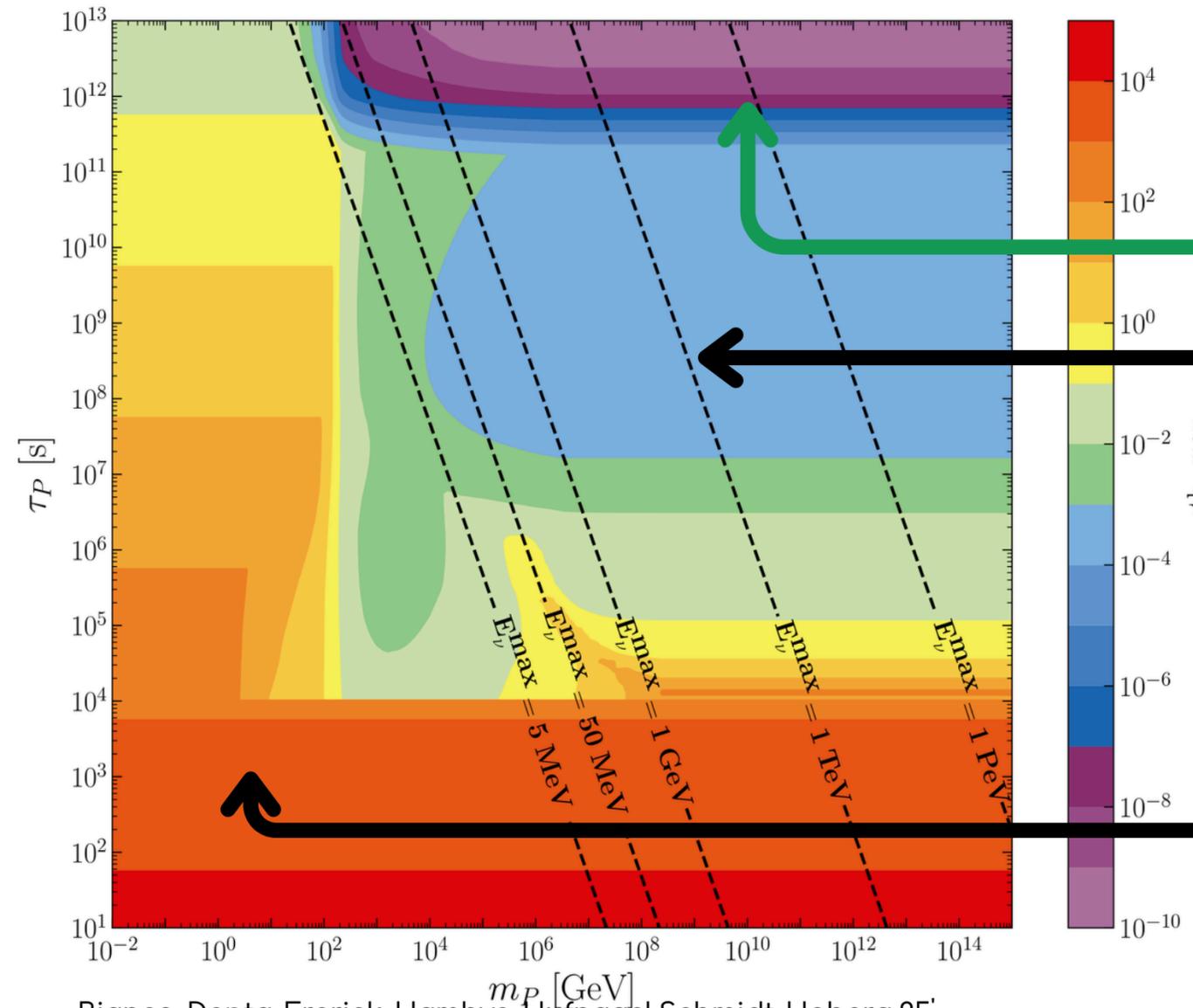
Cosmological:

BBN bound from photo and hadro disintegration of light elements

N_{eff} bound on additional neutrino energy density

Bianco, Depta, Frerick, Hambye, Hufnagel, Schmidt-Hoberg 25'
 Hambye, Hufnagel, Lucca, 21'
 Acharya, Khatri, 19'

Constraints



Cosmological:

CMB anisotropies bound

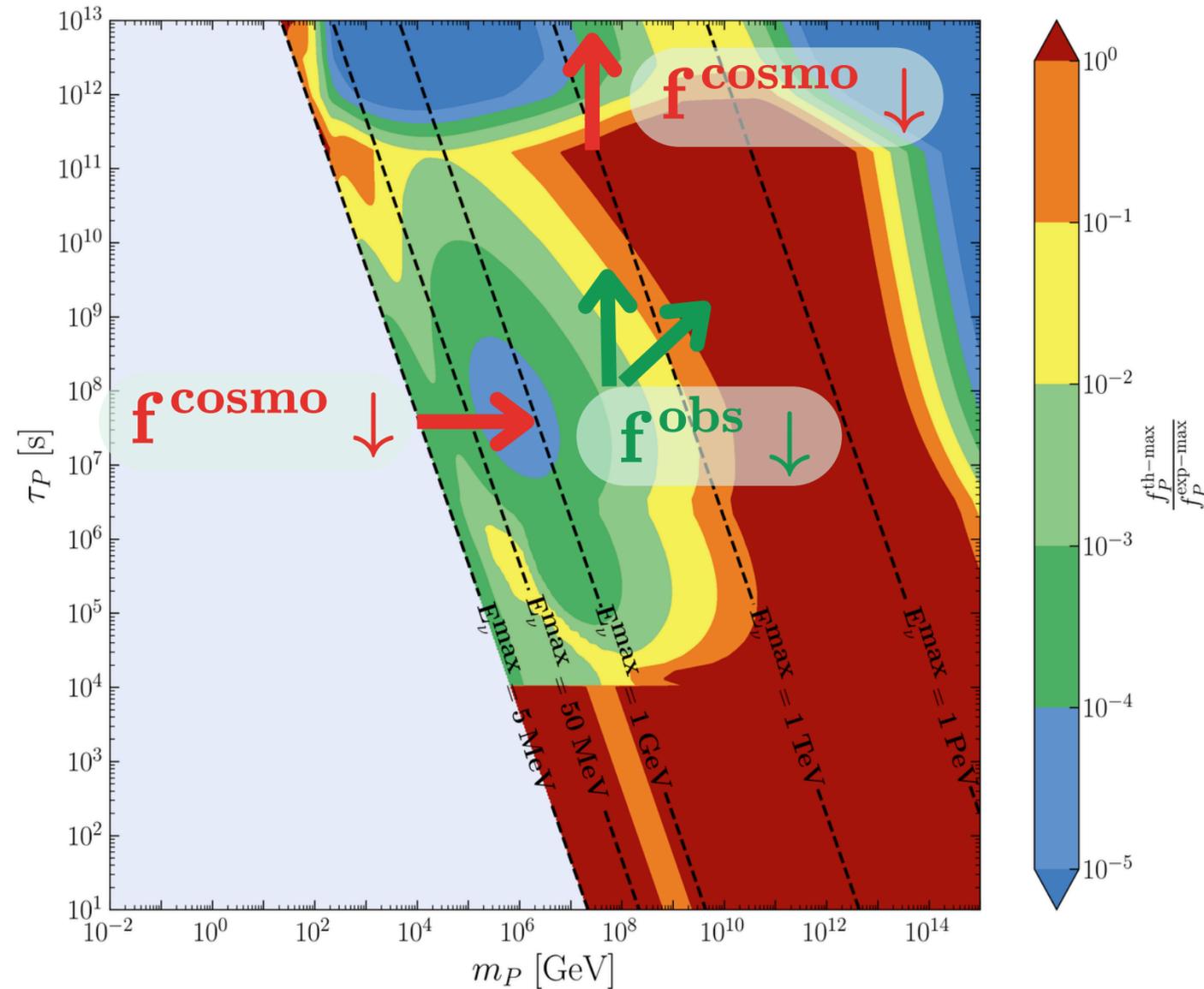
BBN bound from photo and hadro disintegration of light elements

N_{eff} bound on additional neutrino energy density

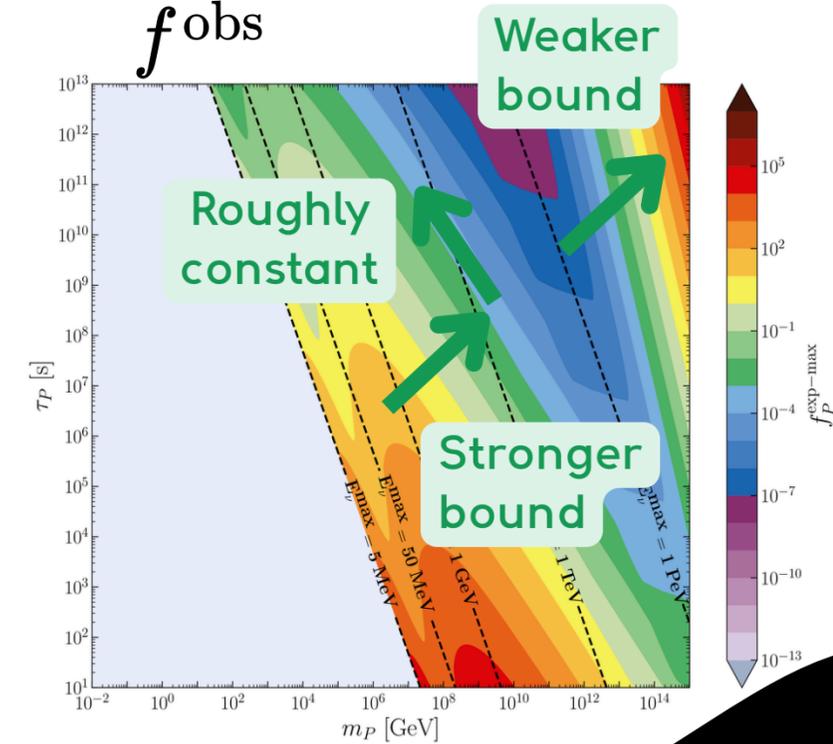
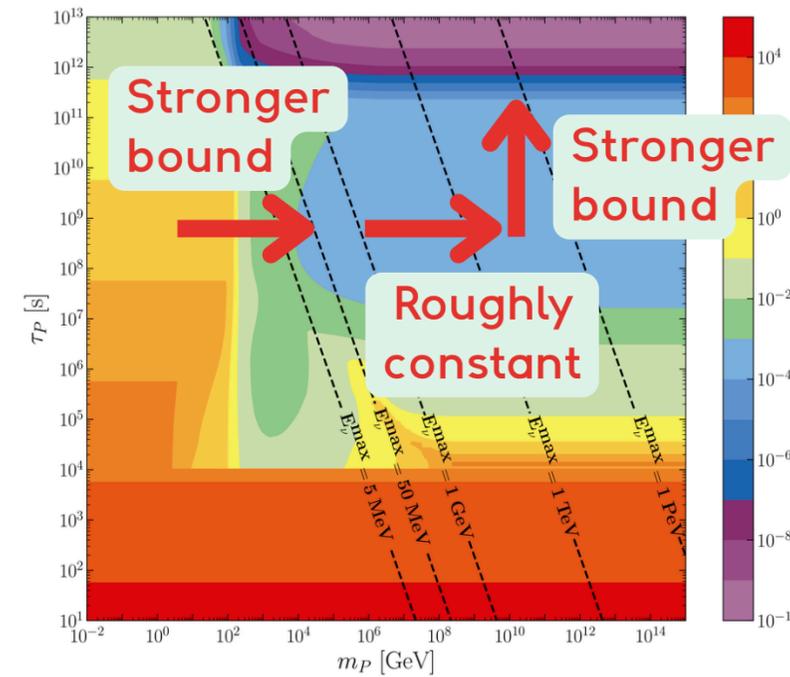
**Competing bounds
with observations**

Bianco, Depta, Frerick, Hambye, Hufnagel, Schmidt-Hoberg 25'
 Hambye, Hufnagel, Lucca, 21'
 Acharya, Khatri, 19'

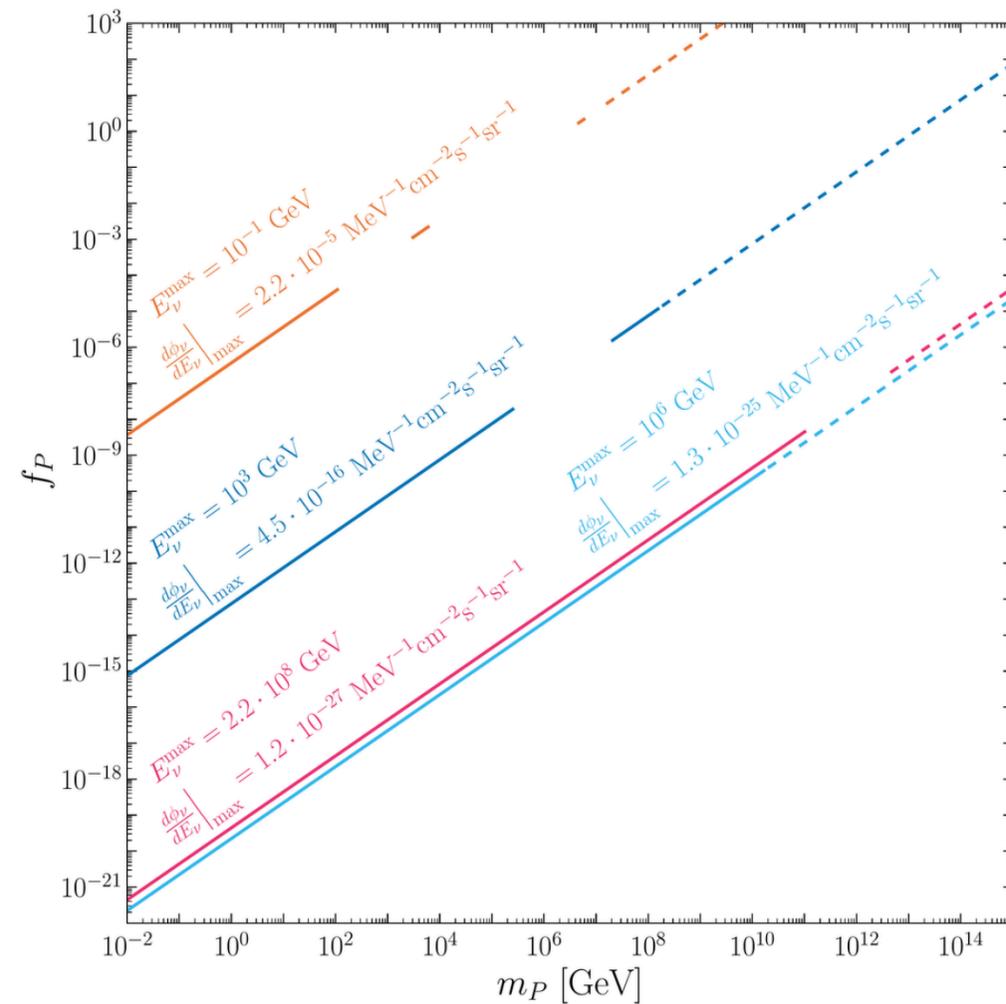
Constraints



Combination: $\frac{f^{\text{cosmo}}}{f^{\text{obs}}}$



Constraints.

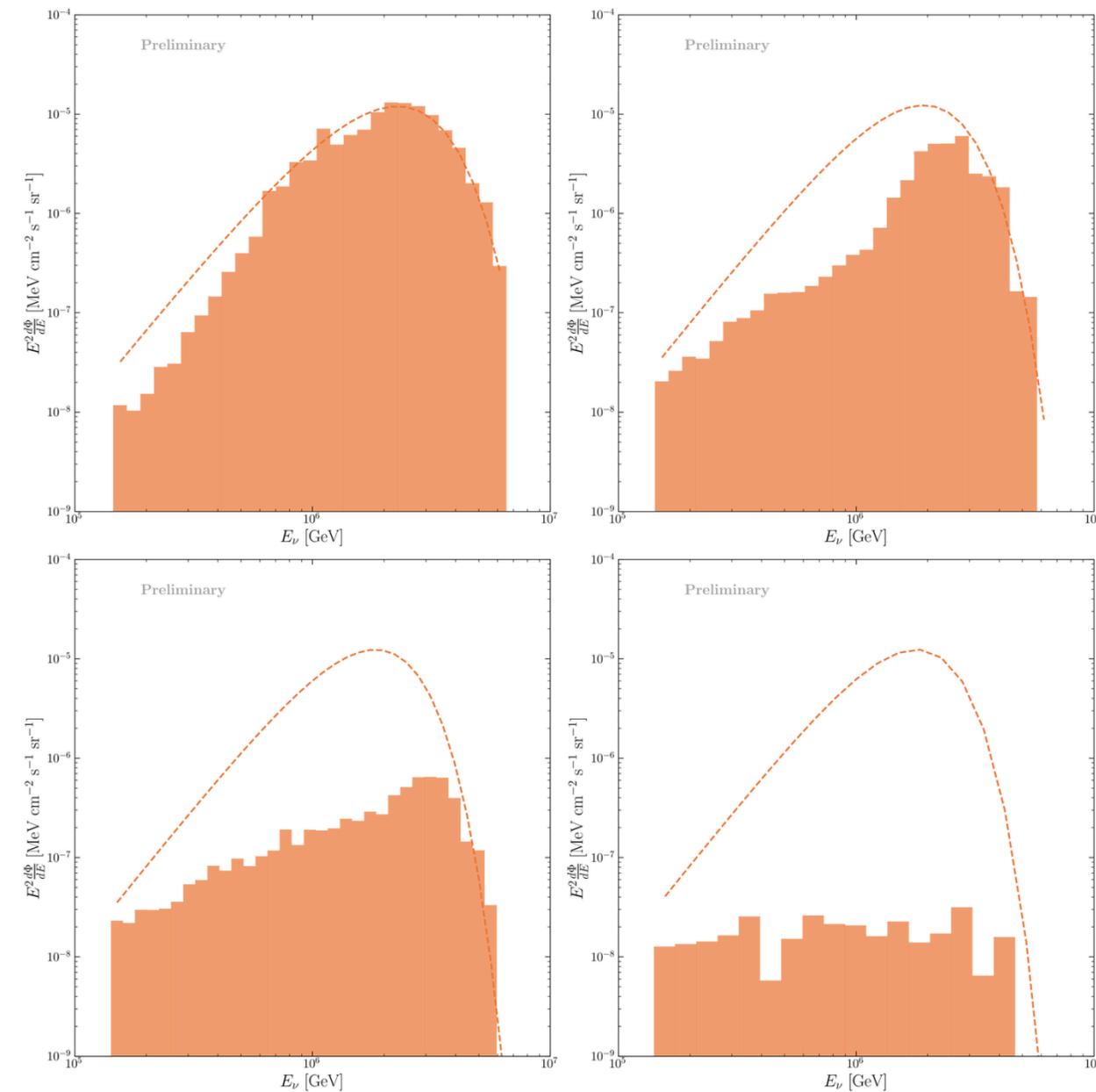
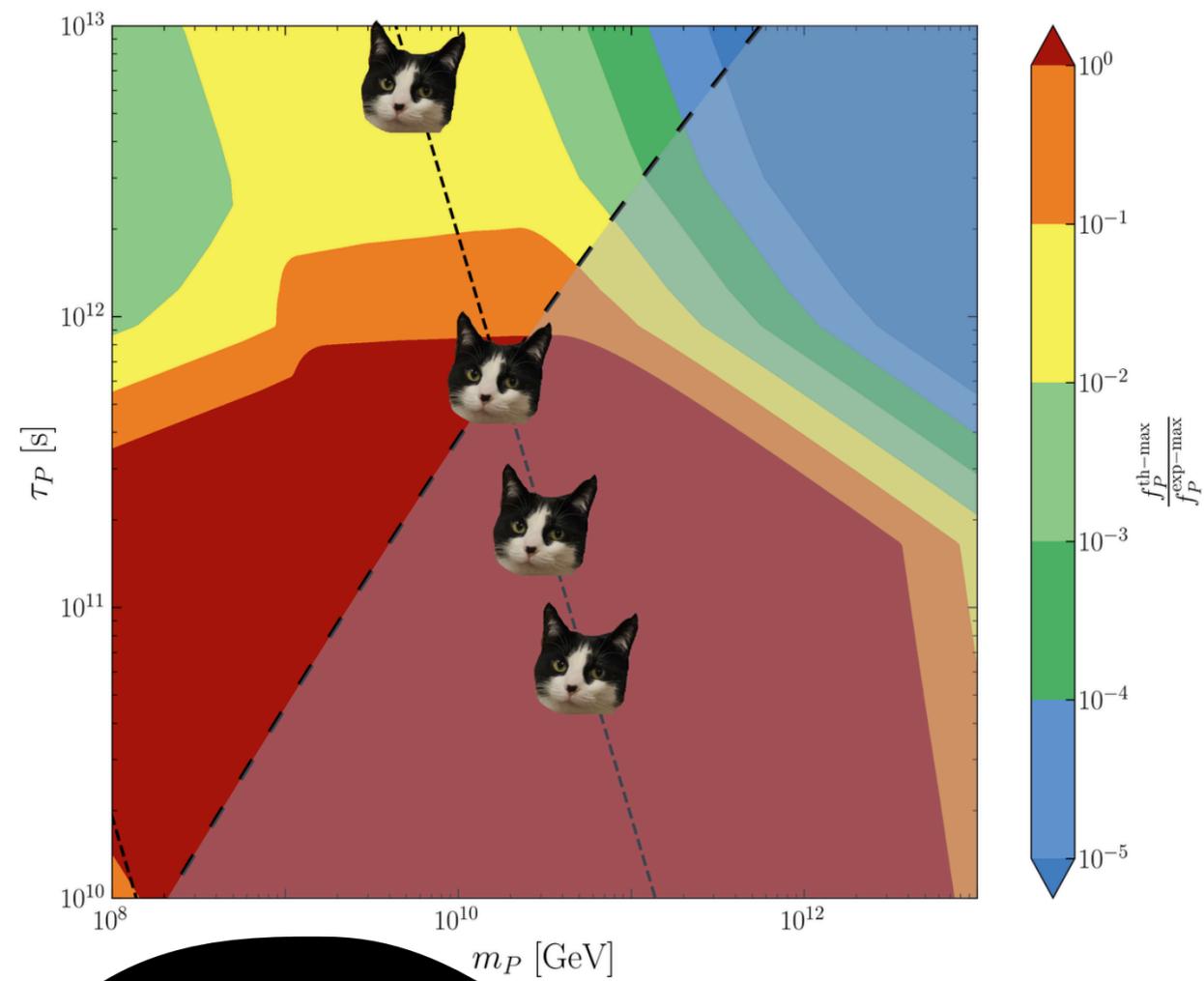


Reconstruction of the heavy relic parameters:

Given the energy at the peak and the amplitude of a spectrum, 2 parameters can be reconstructed:

- Abundance and mass

Medium interactions II.



Decay Spectra.

$$\frac{d\phi_\nu}{dE_\nu} = \frac{2\Omega_P^0 \rho_{crit}^0}{m_P H \tau_P E_\nu} e^{-t/\tau_P} \Theta\left(\frac{m_P}{2} - E_\nu\right)$$

$$\frac{d\phi_\nu}{dE_\nu} = \frac{6\Omega_P^0 \rho_{crit}^0}{\pi m_P^4 \tau_P E_\nu} \int_{E_\nu}^{\frac{m_P}{2}} dx x^2 \frac{e^{-t(E_\nu/x)/\tau_P}}{H(E_\nu/x)}$$

$$\frac{d\phi_\nu}{dE_\nu} = \frac{4\Omega_0^P \rho_{crit}^0}{\pi m_P^2 \tau_P E_\nu \sqrt{1 - (1 - \Delta)^2}} \int_{\max(E_\nu, E_-)}^{E_+} dx \frac{e^{-t(E_\nu/x)/\tau_P}}{H(E_\nu/x)}$$

$$\Delta = 1 - \frac{2m_{P'}}{m_P} \quad E^\pm = \frac{m_P}{4} (1 \pm \sqrt{1 - (1 - \Delta)^2})$$

2-body decay $\frac{dN}{dE} = \delta(E - m_P/2)$

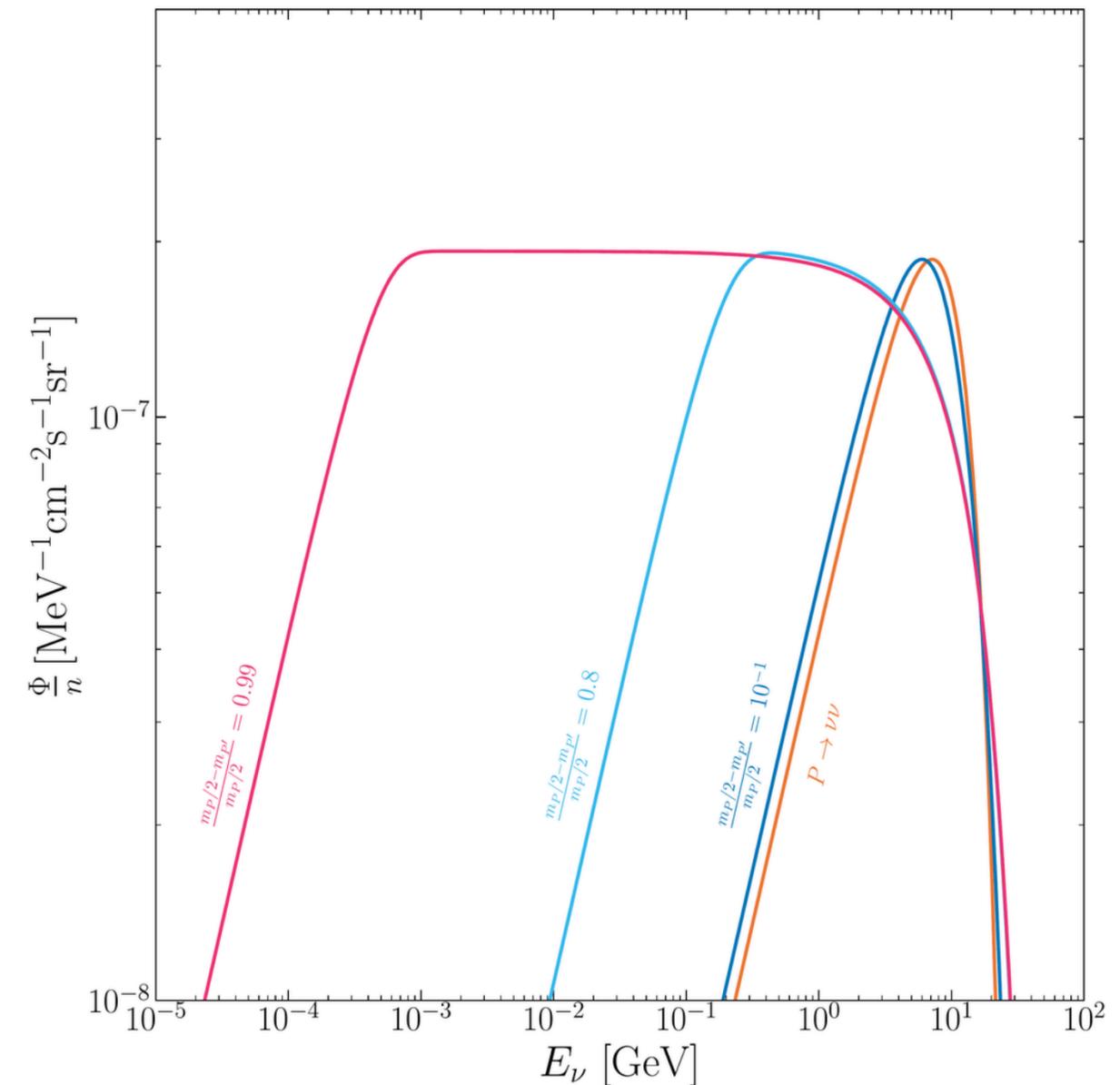
3-body decay $\frac{dN}{dE} = \Theta(m_P/2 - E) \cdot 24 \frac{E^2}{m_P^3}$

Box shaped $\frac{dN}{dE} = \frac{8}{m_P \sqrt{1 - \frac{4m_{P'}^2}{m_P^2}}} \Theta(E - E_-) \Theta(E_+ - E)$

Decay Spectra.

Δ controls the width of the box.

In the limit where $\Delta = 0$ we recover the 2-body decay spectrum



Annihilation.

$$\frac{d\phi_\nu}{dE_\nu} = \frac{\Delta n_\nu}{8\pi} \frac{(\Omega_P^0 \rho_{crit}^0)^2 m_P \langle \sigma v \rangle}{E_\nu^4 H} \frac{1}{\left(1 - \frac{\langle \sigma v \rangle s}{H} \left(1 - \frac{E_\nu(1+z_*)}{m_P}\right) \frac{n}{s} \Big|_{t_*}\right)^2}$$

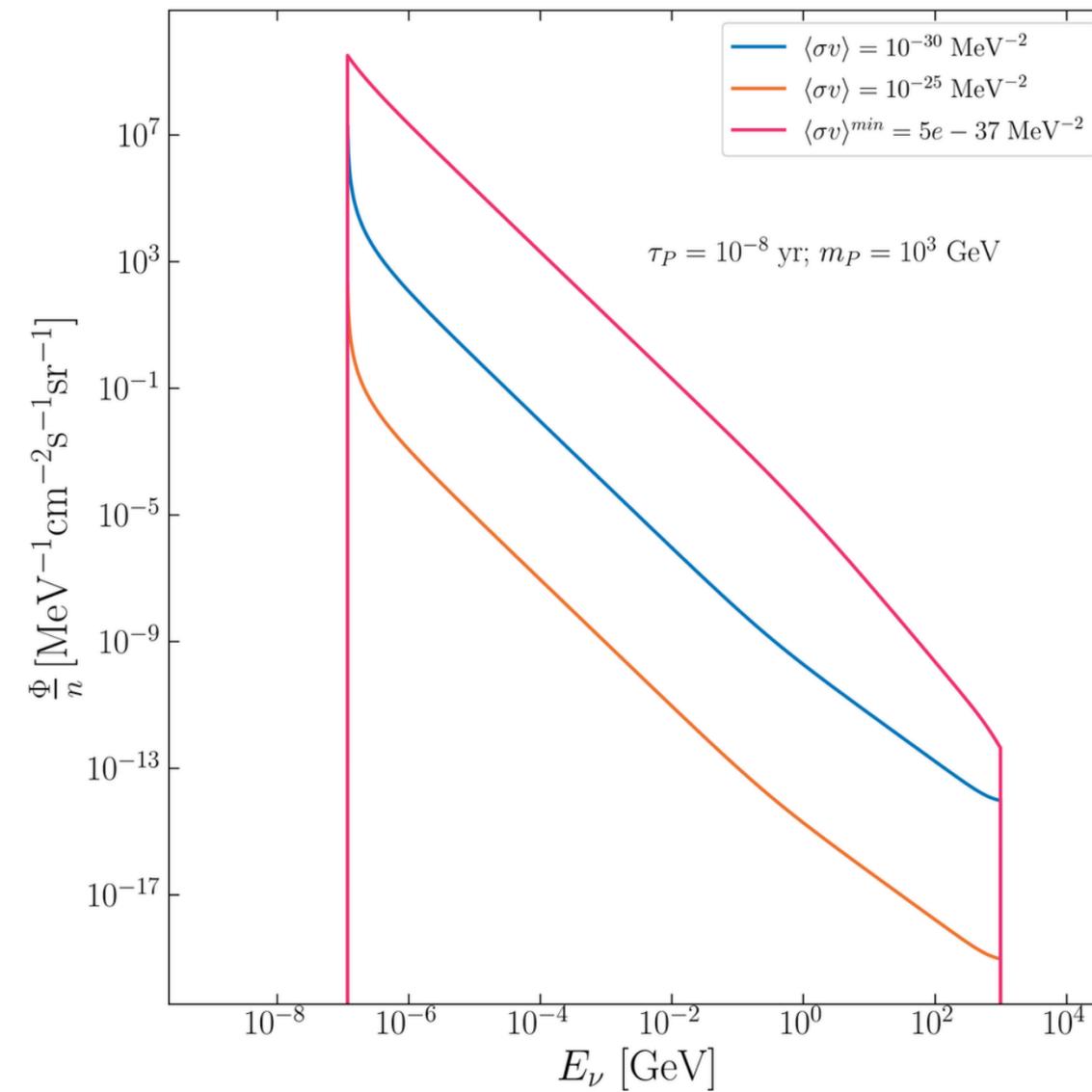
$$\langle \sigma v \rangle n_P^{eq} < H(t^{inj}) \rightarrow \langle \sigma v \rangle < \left(\frac{2\pi}{m_P T^{inj}}\right)^{3/2} \frac{e^{m_P/T^{inj}}}{2g_i t^{inj}}$$

$$\langle \sigma v \rangle n_P^{inj} > H(t^{inj}) \rightarrow \langle \sigma v \rangle > \frac{m_P}{2\Omega_P^0 \rho_{crit}^0} \sqrt{\frac{t^{inj}}{t_r^3}}$$

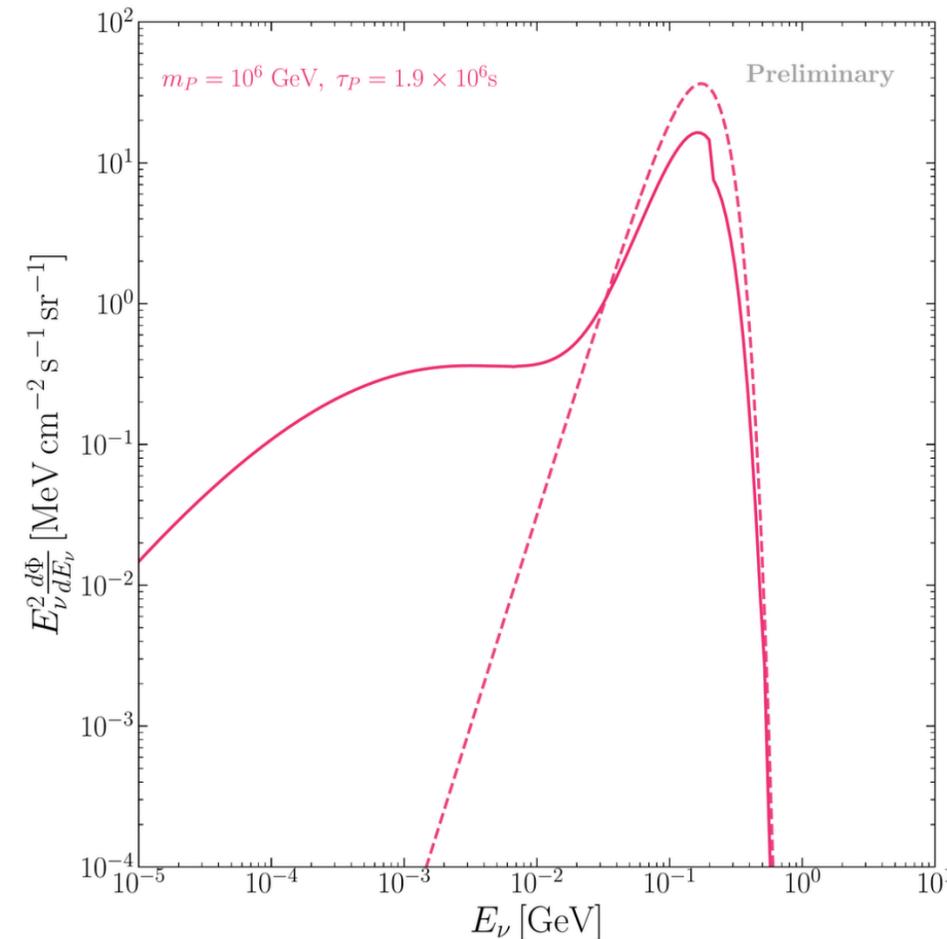
Not too constraining for large mass as it is satisfied as long as T_{inj} is sufficiently lower than m_P

Annihilation.

$$\langle\sigma v\rangle > \frac{m_P}{2\Omega_P^0\rho_{crit}^0} \sqrt{\frac{t^{inj}}{t_r^3}}$$



Sharp Spectral Features.

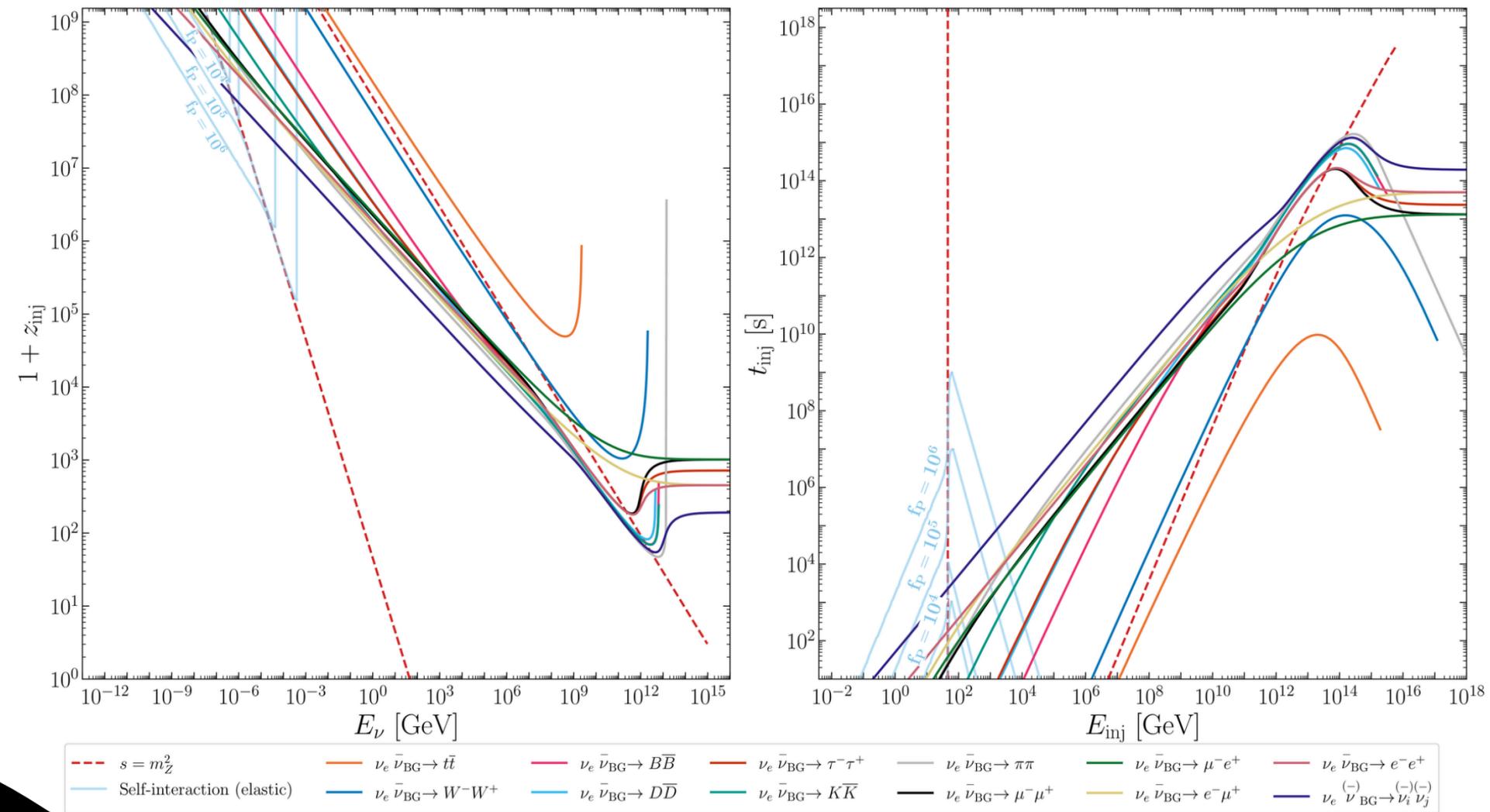


Final state radiation broadening

- If $E_\nu > M_{Z/W}$, gauge bosons can be radiated and generate a shower
- Production of (many) secondary neutrinos of lower energies
- Energy dependent process

Sharp feature mostly unaffected

Medium interactions.



Cross-sections.

Elastic

$$\frac{d\sigma}{dt} = \frac{g^4}{64\pi \cos(\theta_W)^4} \frac{C(s, t, m_Z)}{(t - m_Z^2)^2}$$

Process	$C(s, t, m_Z)$
$\nu_l \bar{\nu}_l \rightarrow \nu_l \bar{\nu}_l$	$\frac{(s+t)^2 (s+t-2m_Z^2)^2}{s^2 (s-m_Z^2)^2}$
$\nu_l \bar{\nu}_l \rightarrow \nu_{l'} \bar{\nu}_{l'}$	$\frac{(s+t)^2 (t-m_Z^2)^2}{s^2 (s-m_Z^2)^2}$
$\nu_l \nu_l \rightarrow \nu_l \nu_l$	$\frac{(s+2m_Z^2)^2}{(s+t+m_Z^2)^2}$
$\nu_l \bar{\nu}_{l'} \rightarrow \nu_l \bar{\nu}_{l'}$	$\frac{(s+t)^2}{s^2}$
$\nu_l \nu_{l'} \rightarrow \nu_l \nu_{l'}$	1

Cross-sections.

Inelastic $\nu_l \bar{\nu}_l \rightarrow l^- l^+$

$$\frac{d\sigma}{dt} = \frac{g^4}{64\pi s^2 (s - m_Z^2)(t - m_W^2)} \left\{ K_1 + \frac{s - m_Z^2}{t - m_W^2} K_2 + \frac{(t - m_W^2) \tan(\theta_W)^4}{s - m_Z^2} K_3 \right\}$$

$$K_1 = (2 \sin(\theta_W)^2 - 1) \left(s \frac{m_l^4}{2m_W^2} + (s + t - m_l^2)^2 \right) + 2 \sin(\theta_W)^2 m_l^2 \left(s + \frac{(m_l^2 - t)^2}{2m_W^2} \right)$$

$$K_2 = (s + t)(s + t + 2m_l^2) + m_l^4 \left(1 + \frac{s}{m_W^2} + \frac{(m_l^2 - t)^2}{4m_W^4} \right),$$

$$K_3 = s^2 + 2(m_l^4 - 2m_l^2 t + t(s + t)) - \frac{m_l^2 s + (s + t - m_l^2)^2}{\sin(\theta_W)^2} + \left(\frac{s + t - m_l^2}{2 \sin(\theta_W)^2} \right)^2.$$

Cross-sections.

Inelastic $\nu_l \bar{\nu}_l \rightarrow l'^+ l'^-$

$$\frac{d\sigma}{dt} = \frac{g^4 \tan(\theta_W)^4}{64\pi s^2 (s - m_Z^2)^2} K_3$$

$$K_1 = (2 \sin(\theta_W)^2 - 1) \left(s \frac{m_l^4}{2m_W^2} + (s + t - m_l^2)^2 \right) + 2 \sin(\theta_W)^2 m_l^2 \left(s + \frac{(m_l^2 - t)^2}{2m_W^2} \right)$$

$$K_2 = (s + t)(s + t + 2m_l^2) + m_l^4 \left(1 + \frac{s}{m_W^2} + \frac{(m_l^2 - t)^2}{4m_W^4} \right),$$

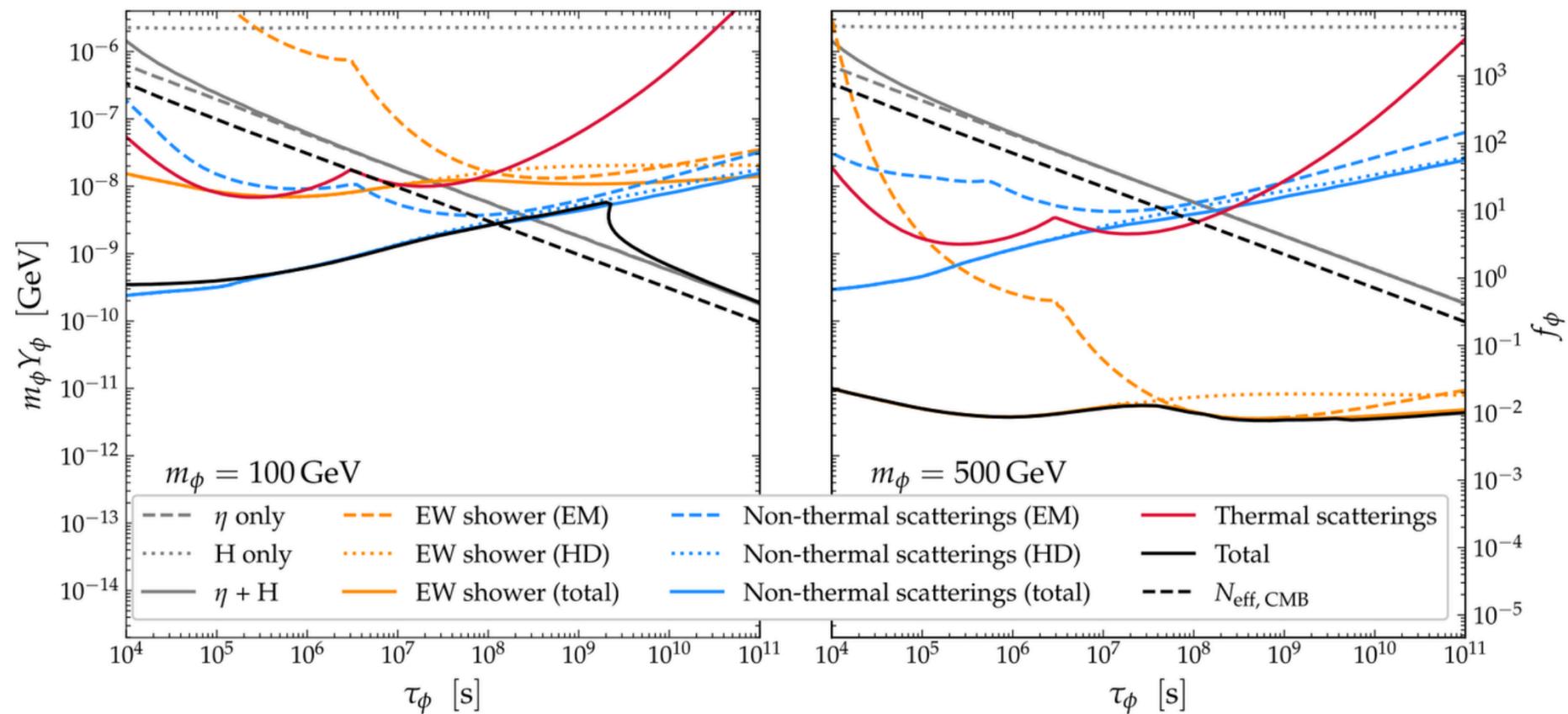
$$K_3 = s^2 + 2(m_l^4 - 2m_l^2 t + t(s + t)) - \frac{m_l^2 s + (s + t - m_l^2)^2}{\sin(\theta_W)^2} + \left(\frac{s + t - m_l^2}{2 \sin(\theta_W)^2} \right)^2.$$

Self-scattering.

$$S_\nu(z, E_\nu^0) = \int_0^z \frac{dz'}{(1+z')H(z')} \Gamma(E_\nu^0(1+z'), z')$$

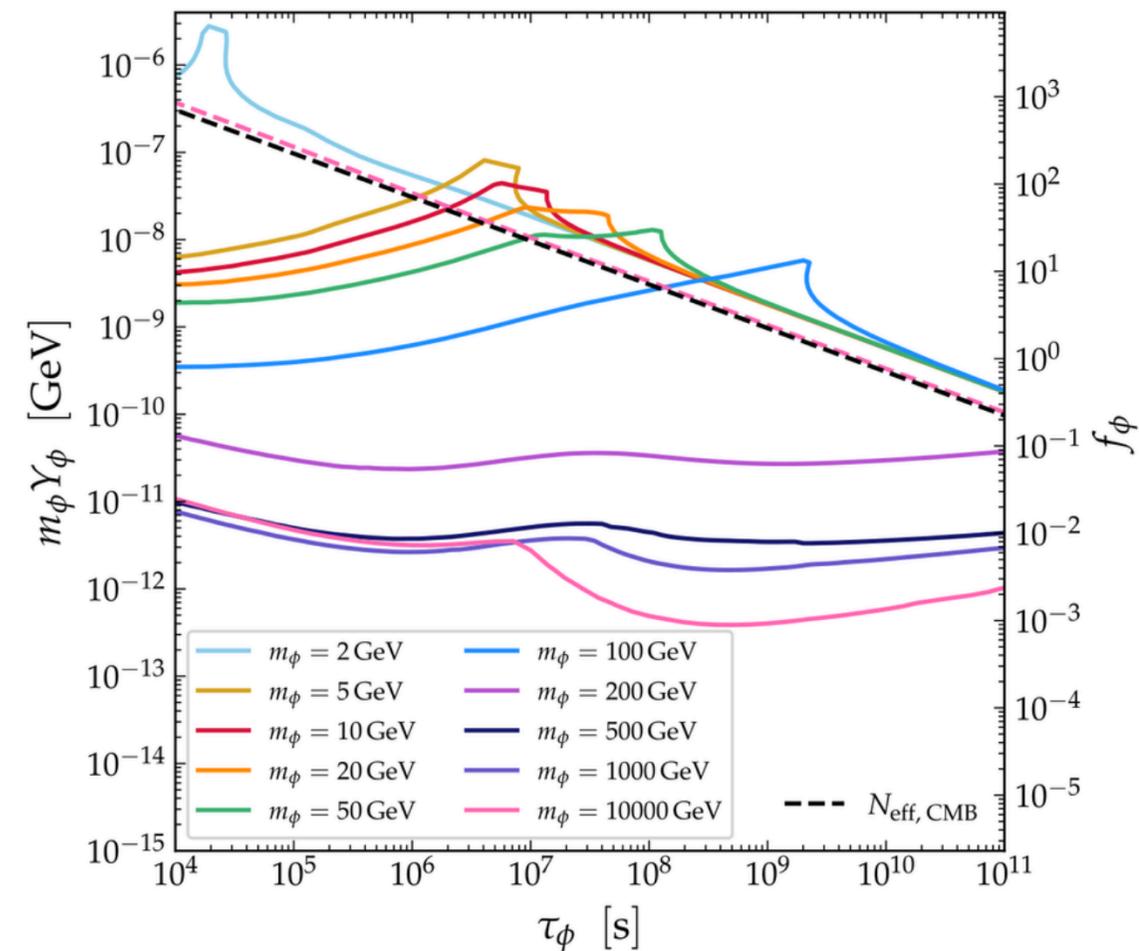
$$\langle \Gamma(E_0, z) \rangle = \frac{\Omega_P^0 \rho_{crit}^0 (1+z)^3}{4E_0^2 (1+z)^2 m_P \tau_P} \int_0^{2E_0(1+z)m_P} ds \sigma(s) s \int_{\frac{s}{4E_0(1+z)}}^{m_P/2} \frac{dE}{E^3} \frac{e^{-t(a_E)/\tau_P}}{H(a_E)}$$

BBN constraints.



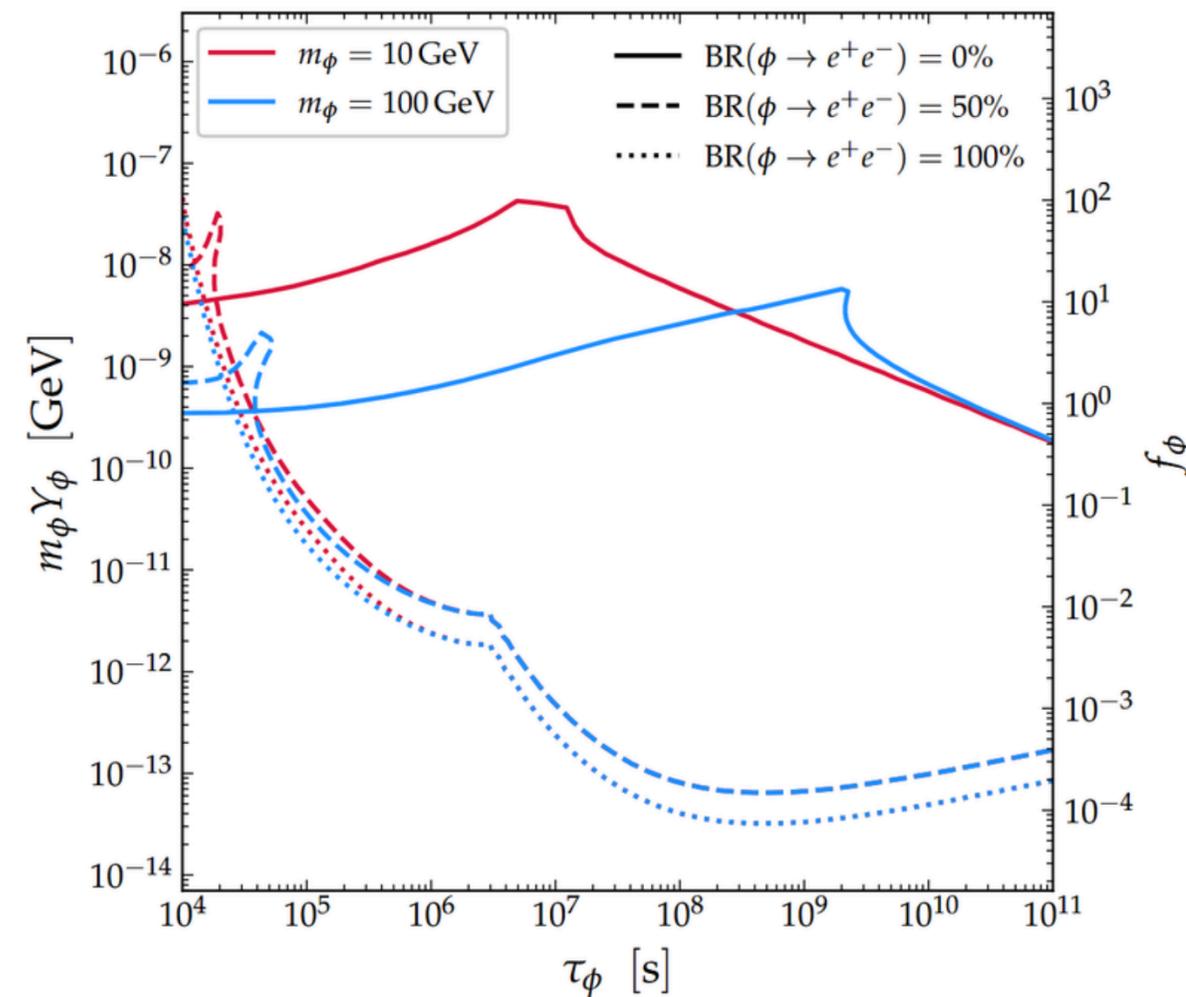
Bianco, Depta, Frerick, Hambye, Hufnagel, Schmidt-Hoberg 25'

BBN constraints.

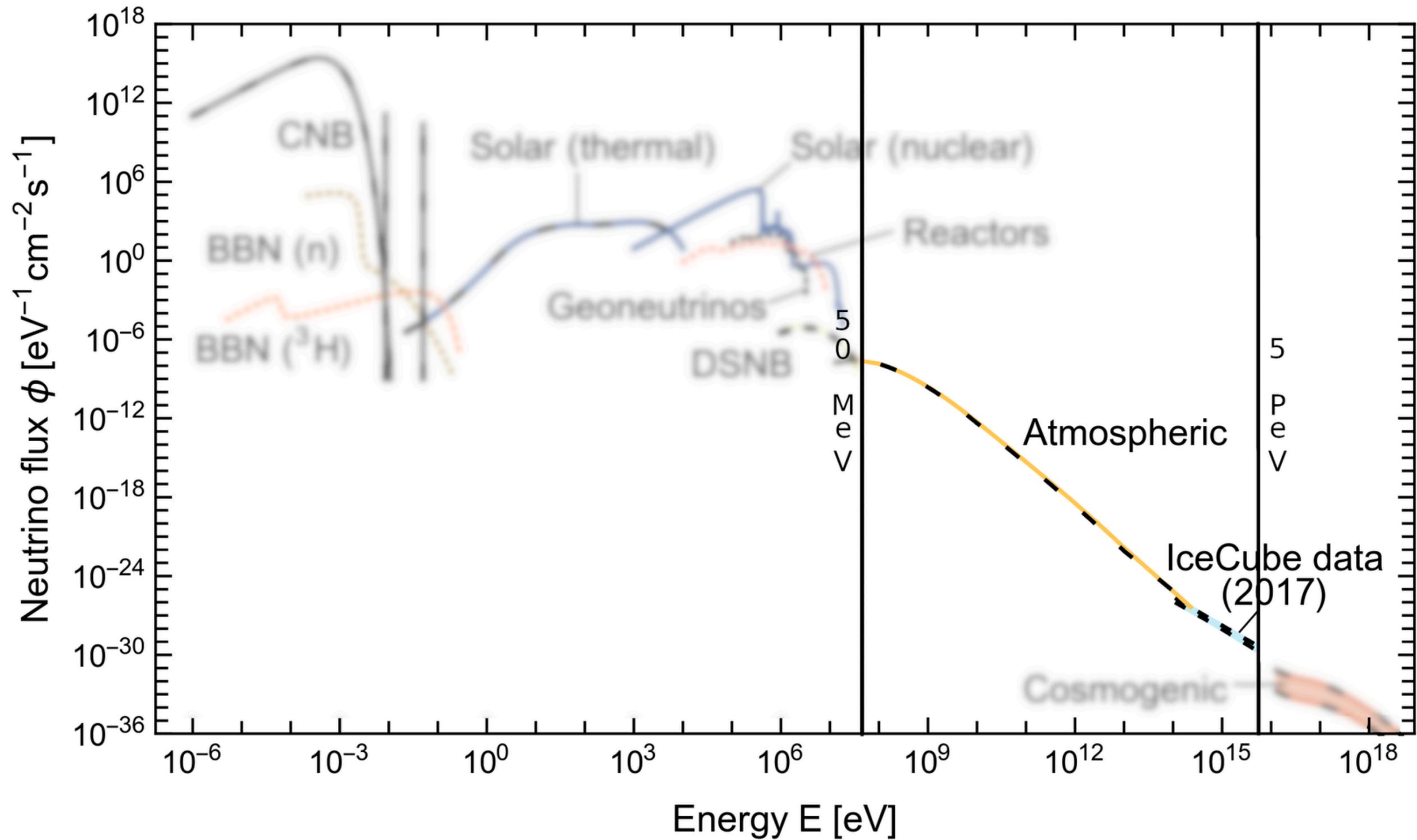


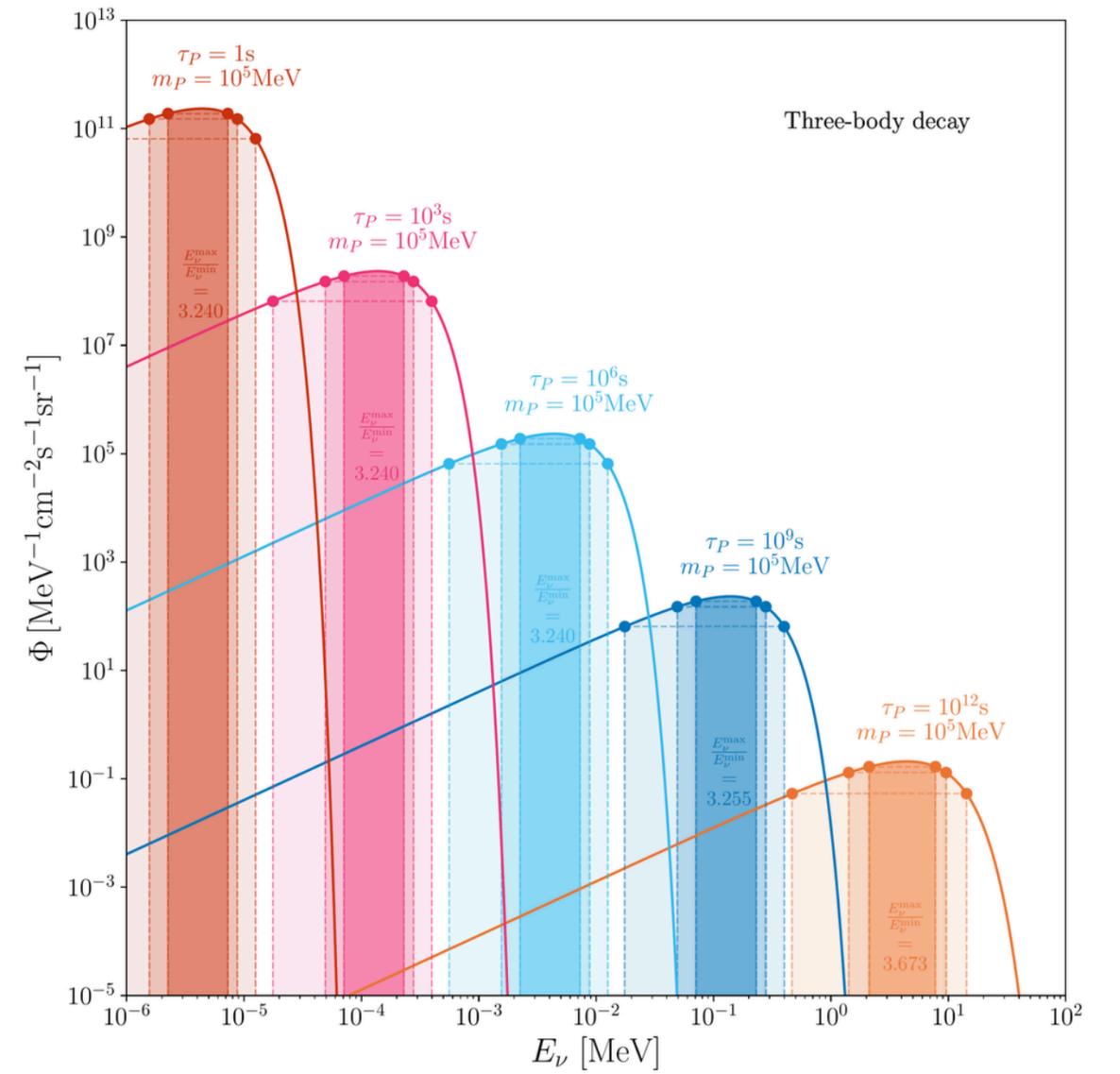
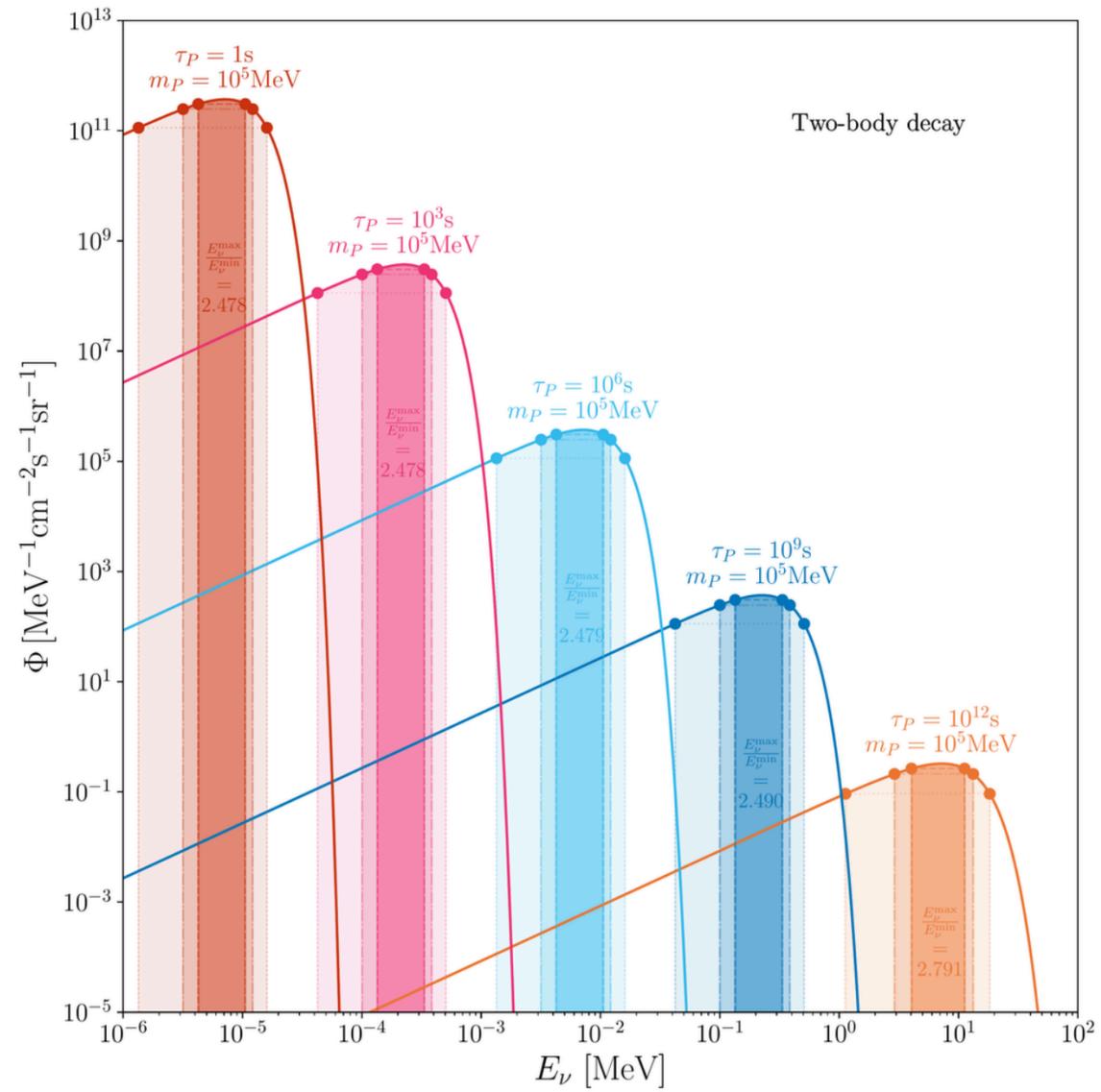
Bianco, Depta, Frerick, Hambye, Hufnagel, Schmidt-Hoberg 25'

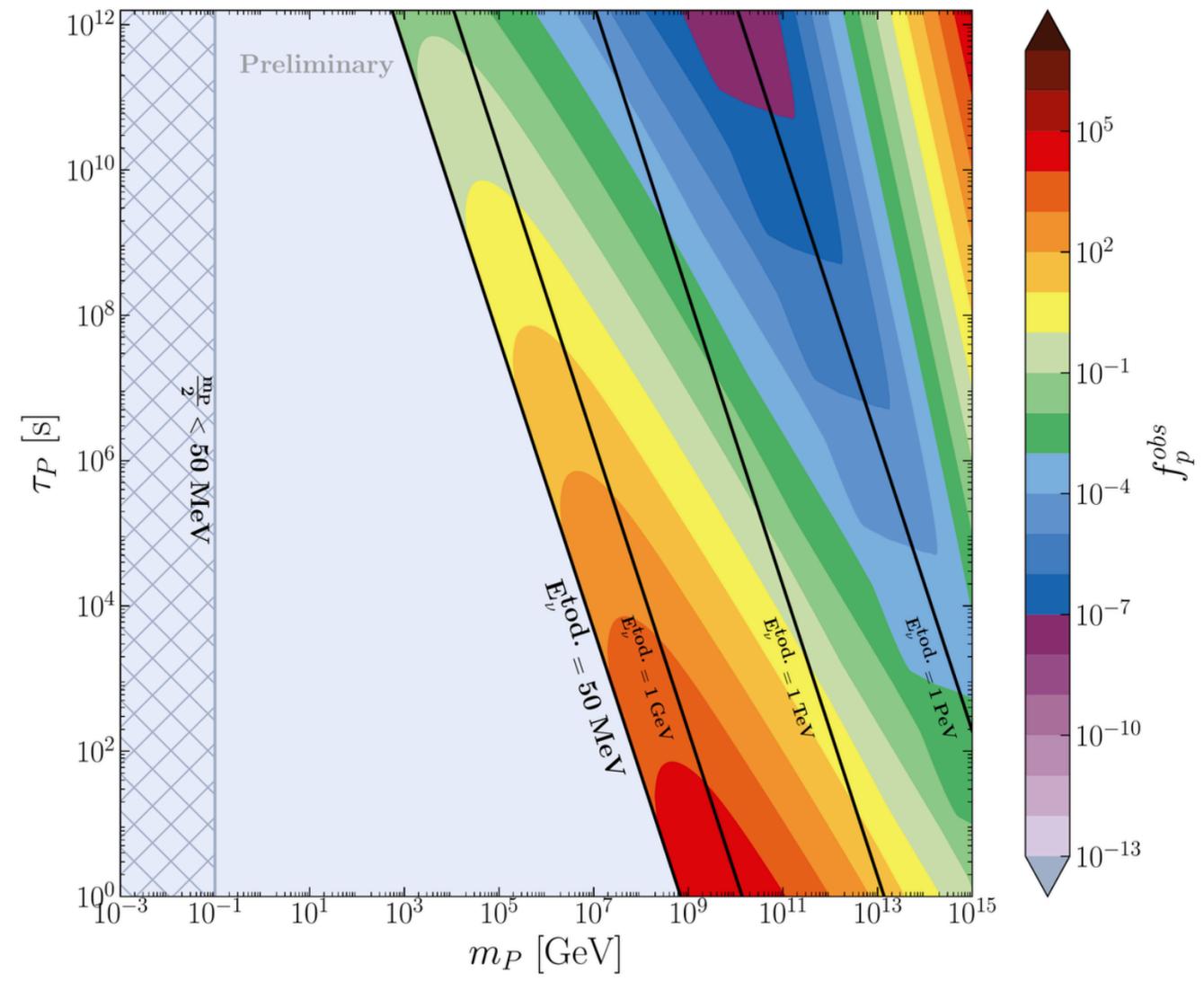
BBN constraints.

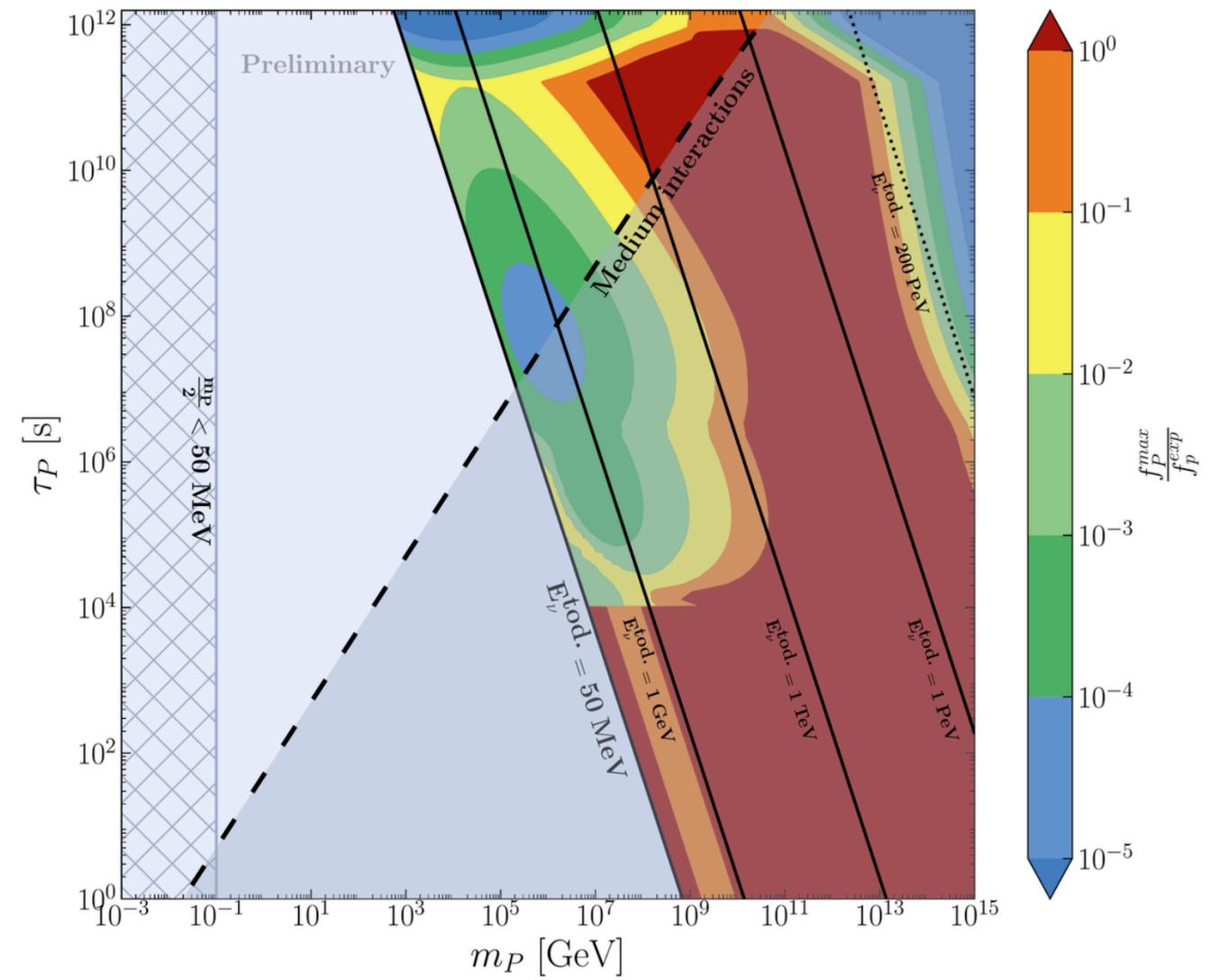
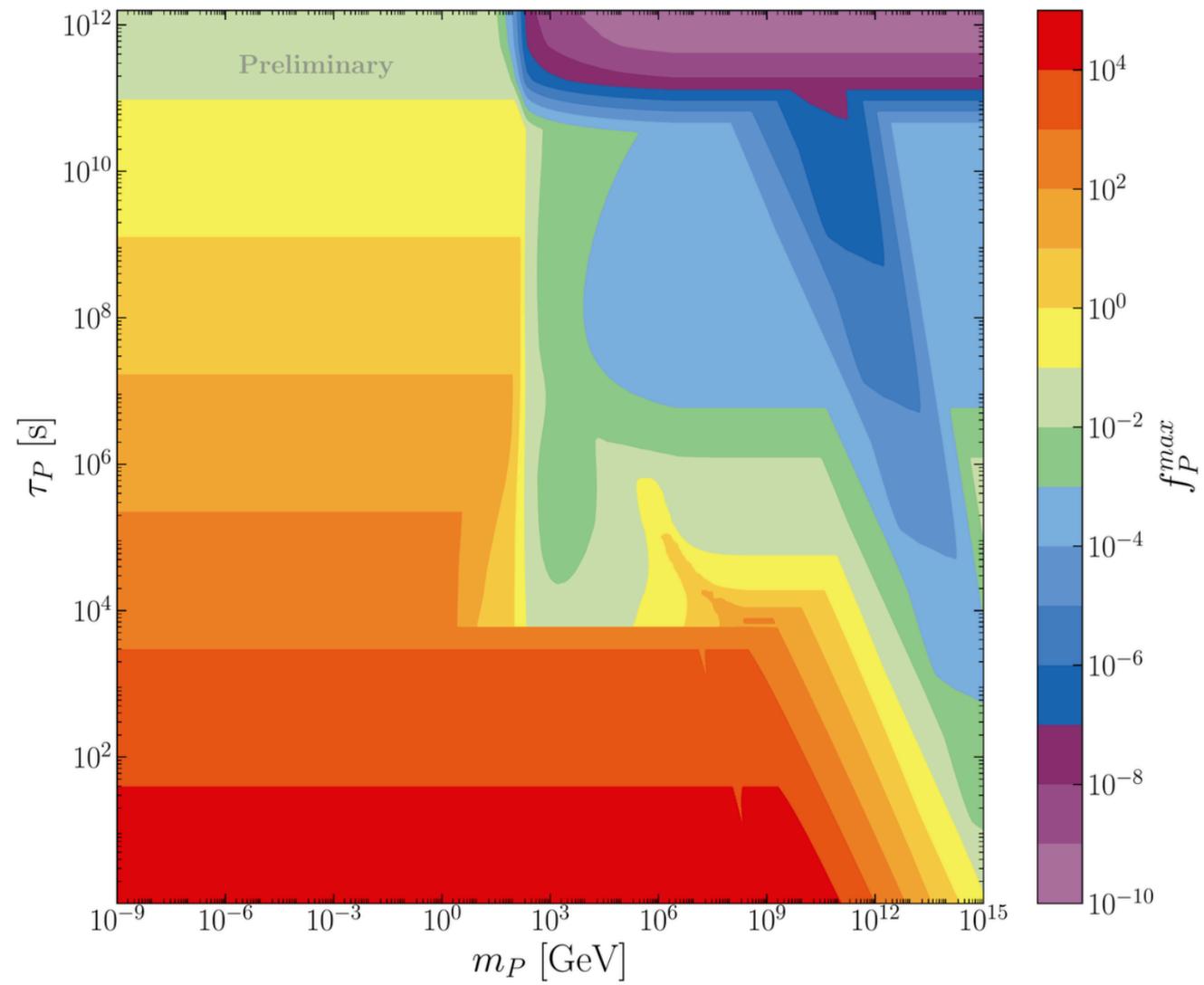


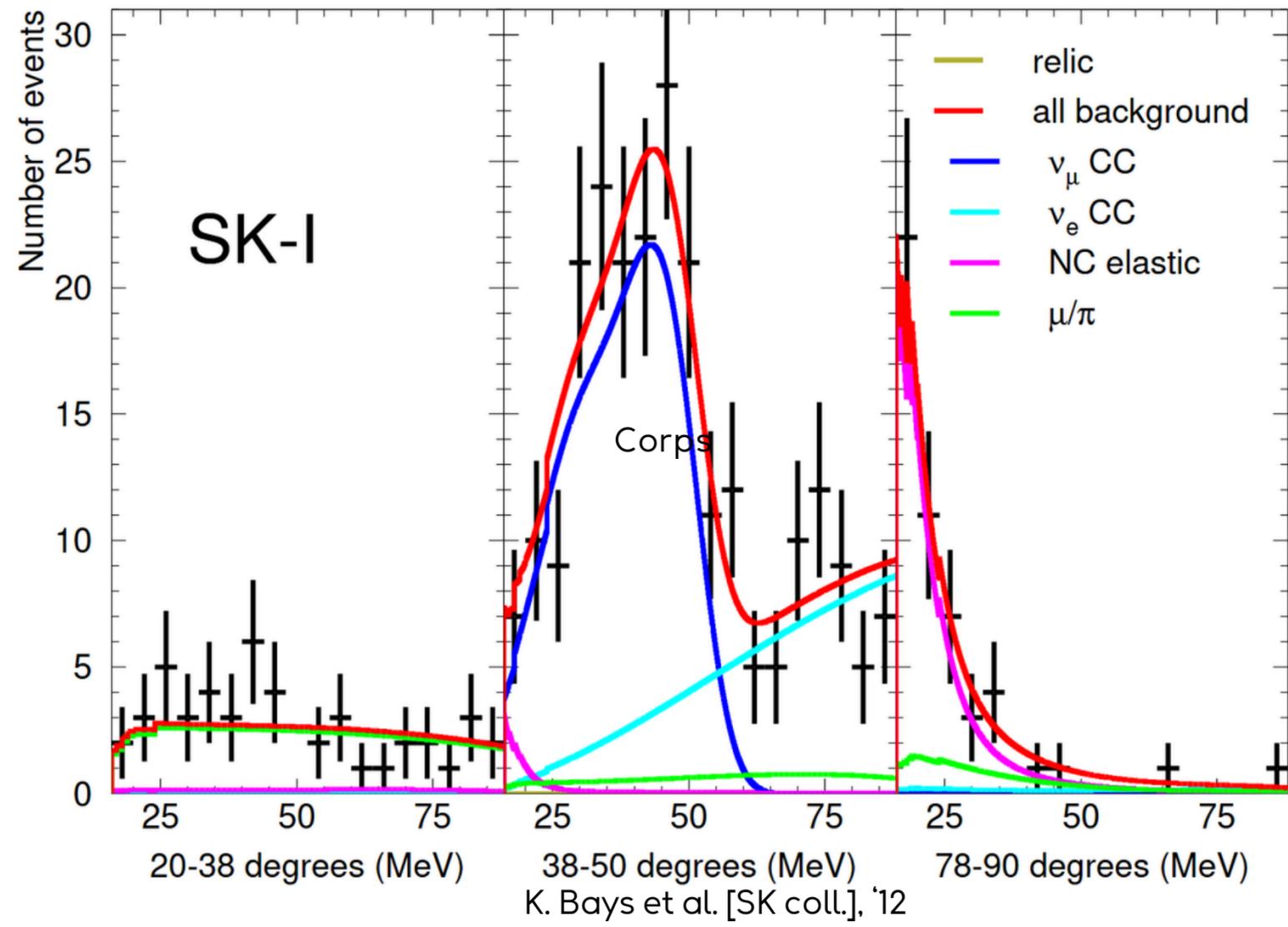
Bianco, Depta, Frerick, Hambye, Hufnagel, Schmidt-Hoberg 25'

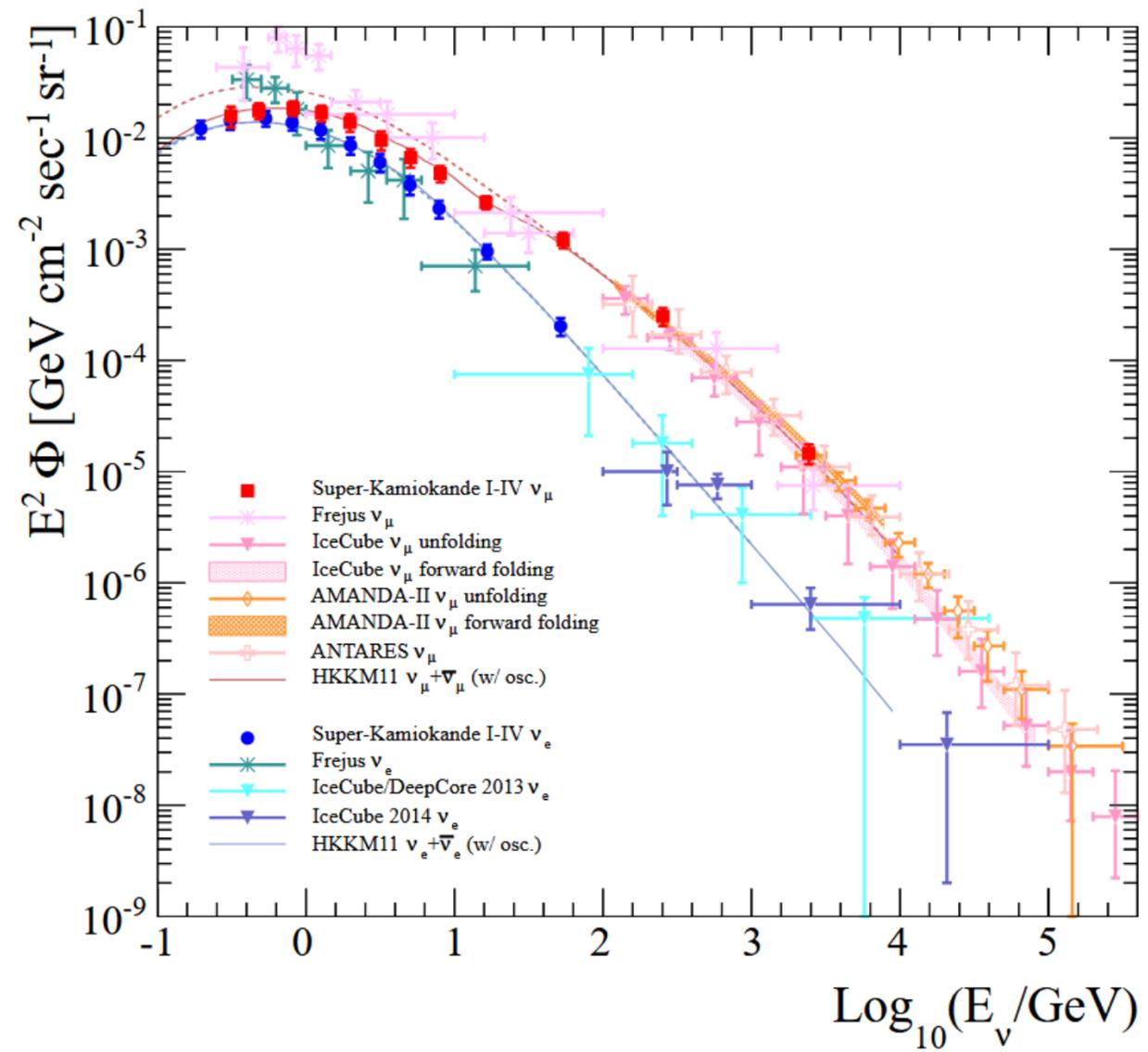












Richard et al. [SK Coll.] 15'

Models

- Scalar triplet
- Majoron
- Vector decay (Coy, Hambye '20)

