



université
PARIS-SACLAY

Combined effective field theory interpretation of VBS measurements with ATLAS

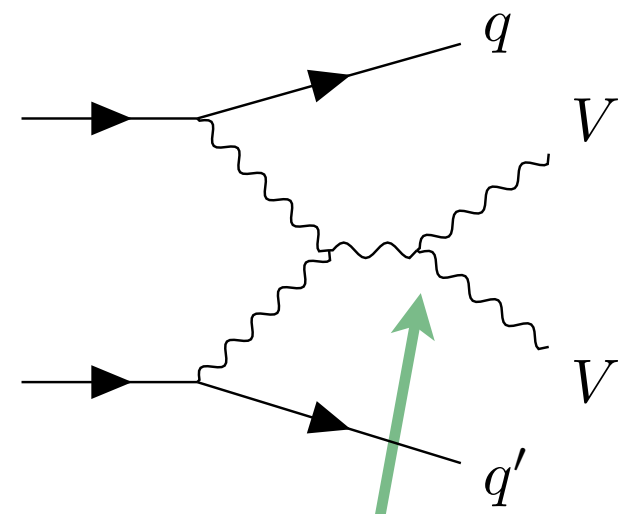
Zhuoran Feng

On behalf of the analysis team

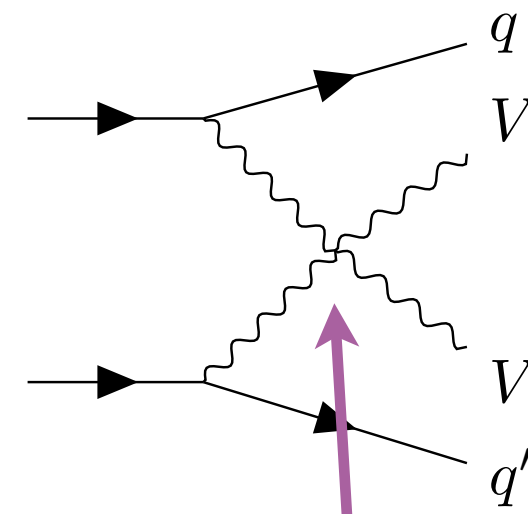
IRN Terascale @ IJCLab, Orsay, 20-22 April 2026



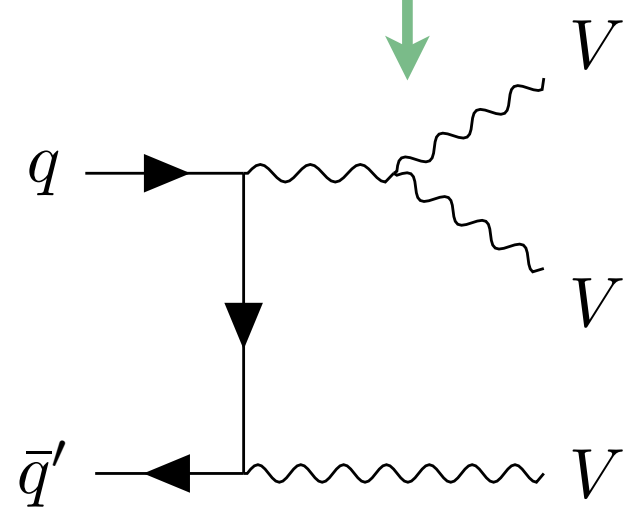
Vector boson scattering



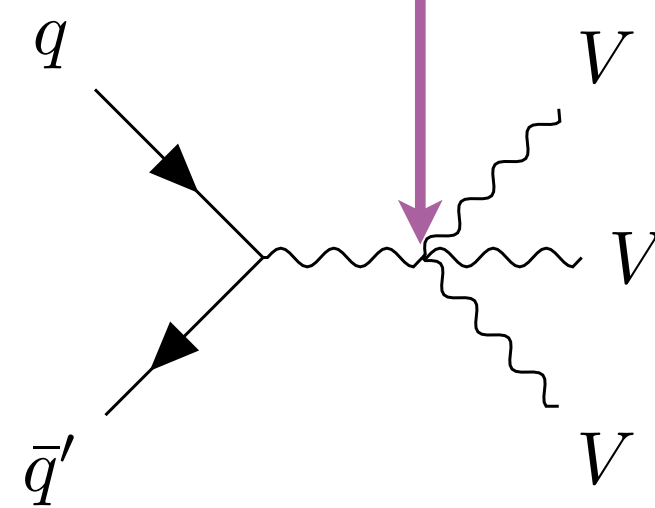
Triple gauge coupling (TGC)



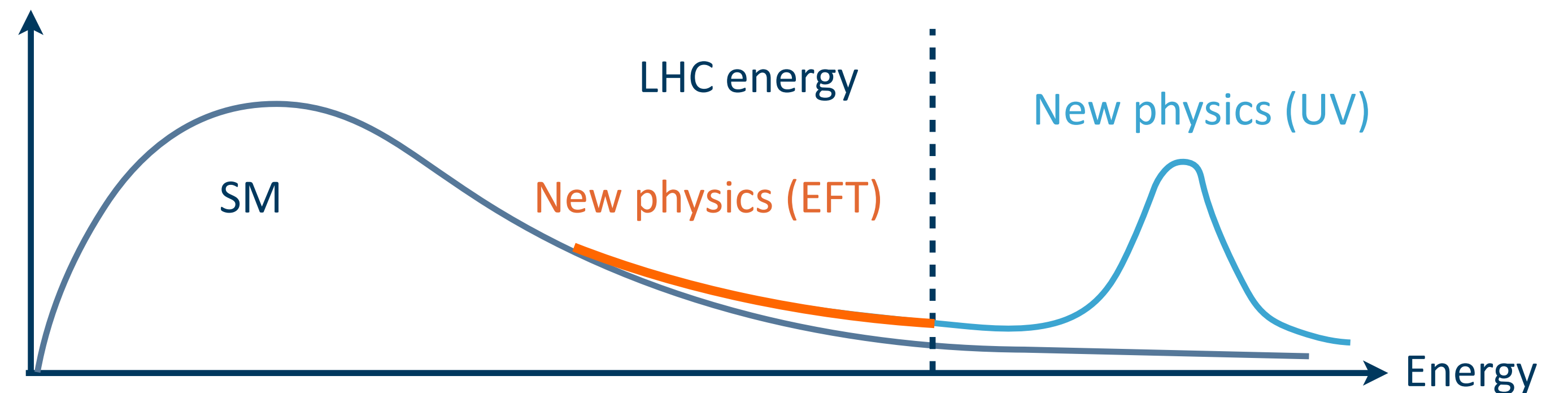
Quartic gauge coupling (QGC)



Tri-boson production



- Vector boson scattering (VBS) and tri-boson production processes probe many different kinds of gauge couplings
- Special interest in VBS and tri-boson: **anomalous QGCs (aQGCs)**
 - Many BSM models predict direct aQGCs or resonances at beyond TeV scale that could be experimentally measured as aQGCs
 - Can be studied in the SM Effective Field Theory (SMEFT) framework



Violating Lepton and Baryon numbers

$$\mathcal{L}_{SMEFT} = \mathcal{L}_{SM} + \sum_i \frac{c_i^{(5)}}{\Lambda} \mathcal{O}_i^{(5)} + \sum_i \frac{c_i^{(6)}}{\Lambda^2} \mathcal{O}_i^{(6)} + \sum_i \frac{c_i^{(7)}}{\Lambda^3} \mathcal{O}_i^{(7)} + \sum_i \frac{c_i^{(8)}}{\Lambda^4} \mathcal{O}_i^{(8)} + \dots$$

Dimension-6
Dimension-8

- Taylor expansion of the SM Lagrangian into local operators with mass dimension > 4
 - Λ : scale of new physics
 - $\mathcal{O}_i^{(n)}$: operators that introduce new interaction vertices
 - $c_i^{(n)}$: coefficients that indicate the strength of the couplings

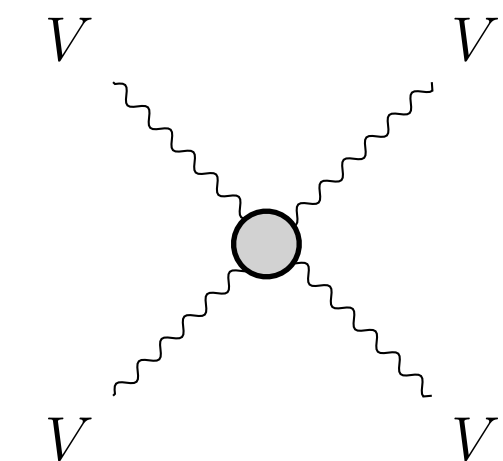
Violating Lepton and Baryon numbers

$$\mathcal{L}_{SMEFT} = \mathcal{L}_{SM} + \sum_i \frac{c_i^{(5)}}{\Lambda} \mathcal{O}_i^{(5)} + \sum_i \frac{c_i^{(6)}}{\Lambda^2} \mathcal{O}_i^{(6)} + \sum_i \frac{c_i^{(7)}}{\Lambda^3} \mathcal{O}_i^{(7)} + \sum_i \frac{c_i^{(8)}}{\Lambda^4} \mathcal{O}_i^{(8)} + \dots$$

Dimension-6
Dimension-8

Constrained by many other analyses

- Taylor expansion of the SM Lagrangian into local operators with mass dimension > 4
 - Λ : scale of new physics
 - $\mathcal{O}_i^{(n)}$: operators that introduce new interaction vertices
 - $c_i^{(n)}$: coefficients that indicate the strength of the couplings
- **Pure aQGC: first appear at dimension-8**
 - Existing dimension-6 measurements cannot constrain aQGC strongly
 - Dedicated dimension-8 SMEFT interpretations are needed



$$\mathcal{L}_{SMEFT} \sim \mathcal{L}_{SM} + \sum_j \frac{f_j^{(8)}}{\Lambda^4} \mathcal{O}_j^{(8)}$$



$$\mathcal{L}_{SMEFT} \sim \mathcal{L}_{SM} + \sum_j^{N_8} \frac{f_j^{(8)}}{\Lambda^4} \mathcal{O}_j^{(8)}$$

Éboli basis
C-even P-even
operators predicting aQGCs

- **Scalar operators:** containing only derivatives of the Higgs field (O_{S0}, O_{S1}, O_{S2})
- **Tensor operators:** containing only EW boson field strengths (O_{T0}, \dots, O_{T9})
- **Mixed operators:** mixture of the derivatives and field strengths (O_{M0}, \dots, O_{M7})

Vertices impacted by the operators

	WWWW	WWZZ	WW γ Z	WW $\gamma\gamma$	ZZZZ	ZZZ γ	ZZ $\gamma\gamma$	Z $\gamma\gamma\gamma$	$\gamma\gamma\gamma\gamma$
$O_{S,0}, O_{S,1}, O_{S,2}$	✓	✓			✓				
$O_{M,0}, O_{M,1}, O_{M,7}$	✓	✓	✓	✓	✓	✓	✓		
$O_{M,2}, O_{M,3}, O_{M,4}, O_{M,5}$		✓	✓	✓	✓	✓	✓		
$O_{T,0}, O_{T,1}, O_{T,2}, O_{T,3}$	✓	✓	✓	✓	✓	✓	✓	✓	✓
$O_{T,4}, O_{T,5}, O_{T,6}, O_{T,7}$		✓	✓	✓	✓	✓	✓	✓	✓
$O_{T,8}, O_{T,9}$					✓	✓	✓	✓	✓



$$\mathcal{L}_{SMEFT} \sim \mathcal{L}_{SM} + \sum_j \frac{f_j^{(8)}}{\Lambda^4} \mathcal{O}_j^{(8)}$$

Éboli basis
C-even P-even
operators predicting aQGCs

- Scalar operators: containing only derivatives of the Higgs field (O_{S0}, O_{S1}, O_{S2})
- Tensor operators: containing only EW boson field strengths (O_{T0}, \dots, O_{T9})
- Mixed operators: mixture of the derivatives and field strengths (O_{M0}, \dots, O_{M7})

Vertices impacted by the operators

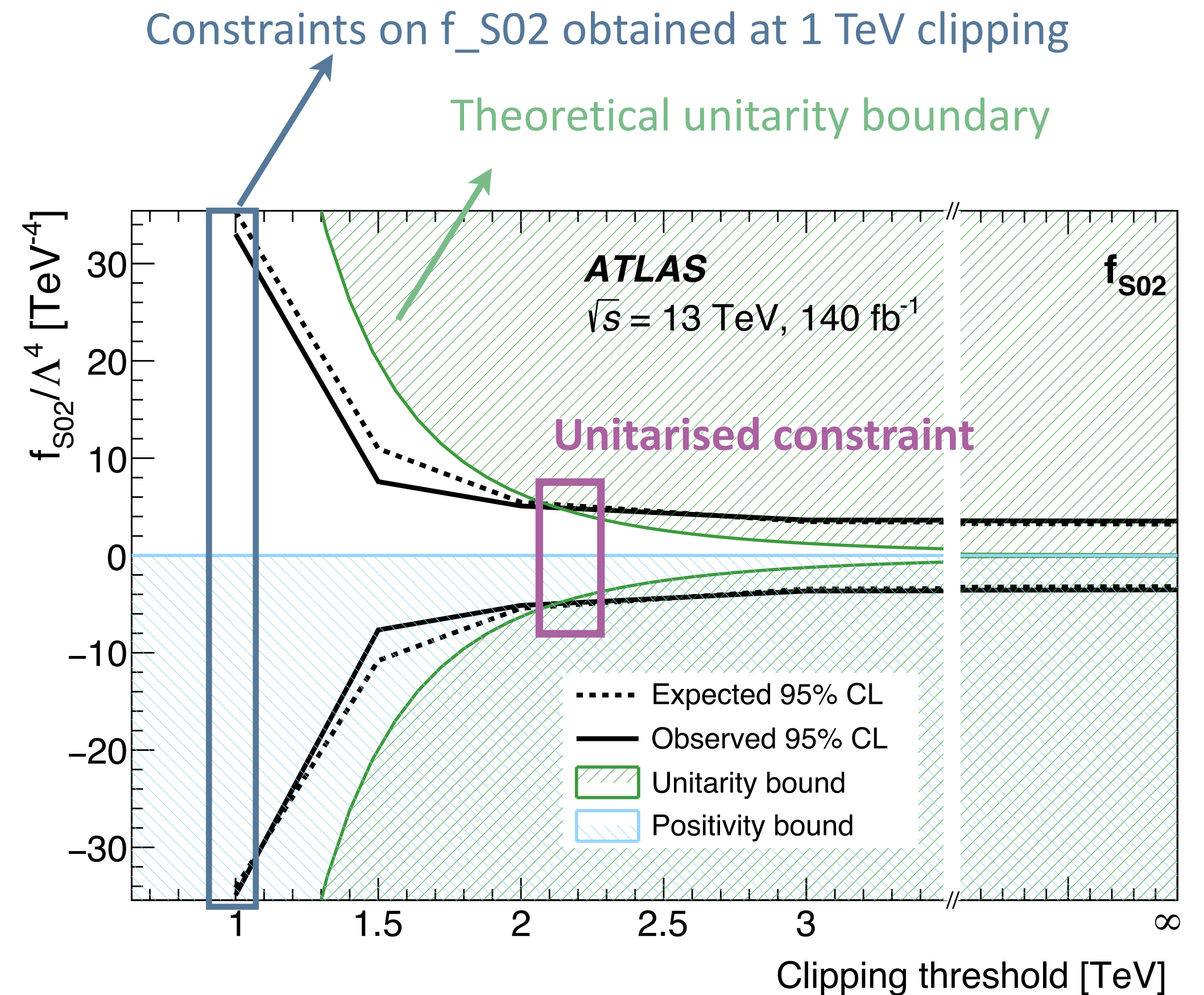
	WWWW	WWZZ	WW γ Z	WW $\gamma\gamma$	ZZZZ	ZZZ γ	ZZ $\gamma\gamma$	Z $\gamma\gamma\gamma$	$\gamma\gamma\gamma\gamma$
$O_{S,0}, O_{S,1}, O_{S,2}$	✓	✓			✓				
$O_{M,0}, O_{M,1}, O_{M,7}$	✓	✓	✓	✓	✓	✓	✓		
$O_{M,2}, O_{M,3}, O_{M,4}, O_{M,5}$		✓	✓	✓	✓	✓	✓		
$O_{T,0}, O_{T,1}, O_{T,2}, O_{T,3}$	✓	✓	✓	✓	✓	✓	✓	✓	✓
$O_{T,4}, O_{T,5}, O_{T,6}, O_{T,7}$		✓	✓	✓	✓	✓	✓	✓	✓
$O_{T,8}, O_{T,9}$					✓	✓	✓	✓	✓

- Experimentally: we focus on a set of C-even P-even operators giving rise to aQGCs, the Éboli basis operators
- The effect of these operators: modifying the cross-sections → Given the measured cross-sections, we can set constraints on the coefficients of these operators

$$\mathcal{A}^2 = \underbrace{|\mathcal{A}_{SM}|^2}_{\text{Pure SM}} + \underbrace{2 \sum_i \frac{c_i}{\Lambda^4} \Re(\mathcal{A}_i^* \mathcal{A}_{SM})}_{\text{EFT-SM interference (linear)}} + \underbrace{\sum_i \frac{c_i^2}{\Lambda^8} |\mathcal{A}_i|^2 + 2 \sum_{i \neq j} \frac{c_i c_j}{\Lambda^8} \Re(\mathcal{A}_i^* \mathcal{A}_j)}_{\text{Pure EFT, single operator or cross-terms (quadratic)}}$$

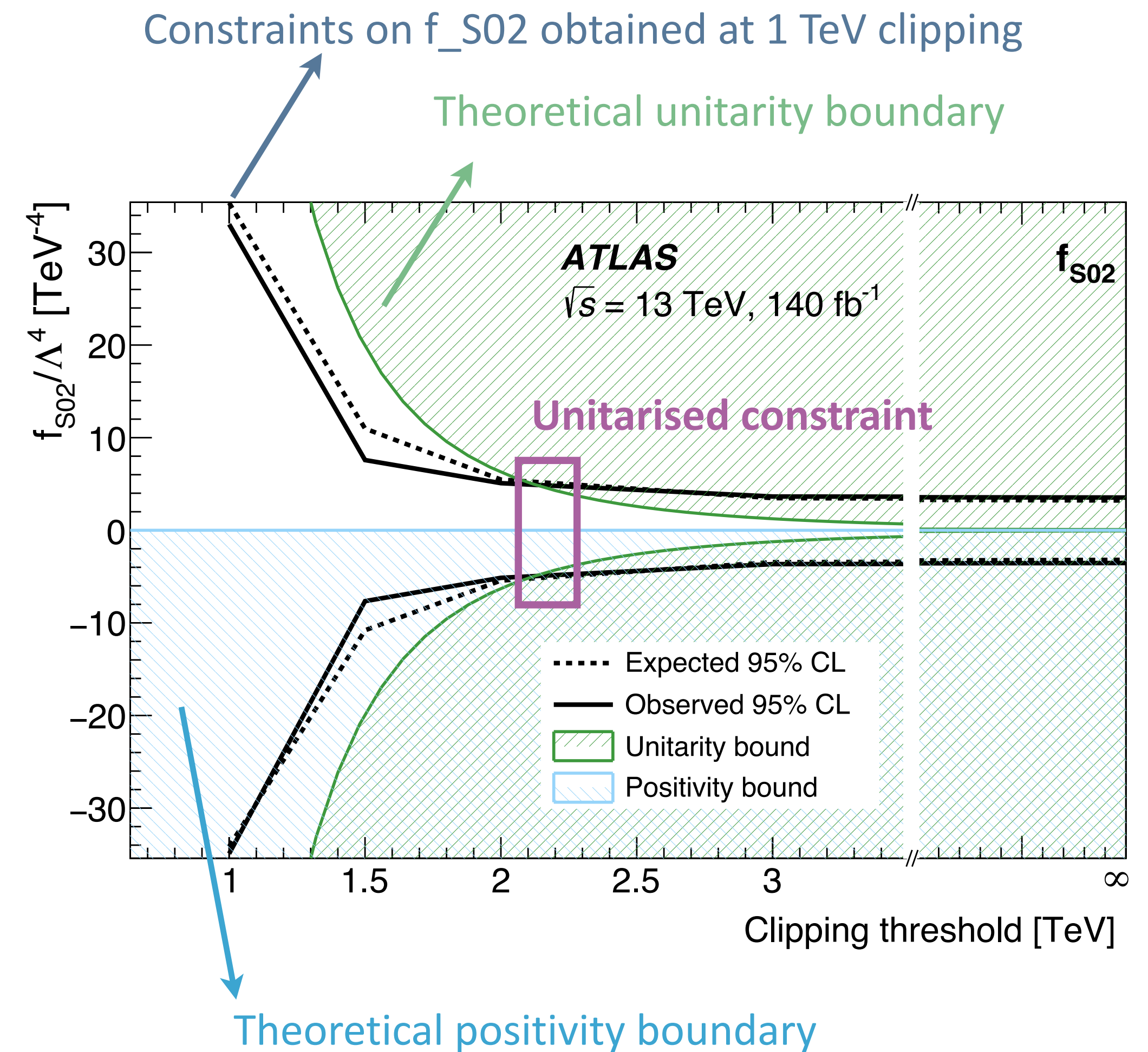


- Unitarity violation and clipping methods
 - Theoretically: require that perturbative partial-wave unitarity satisfied
 - Experimentally: **ad-hoc unitarisation procedure** — introducing a cut-off scale (**clipping threshold**), beyond which the coefficient is set to zero
 - In practice: a scan over several chosen clipping thresholds, at each threshold, obtain a constraint on the coefficient. The **final unitarised constraint** is taken from the intersection between the unitarity bound and the scan





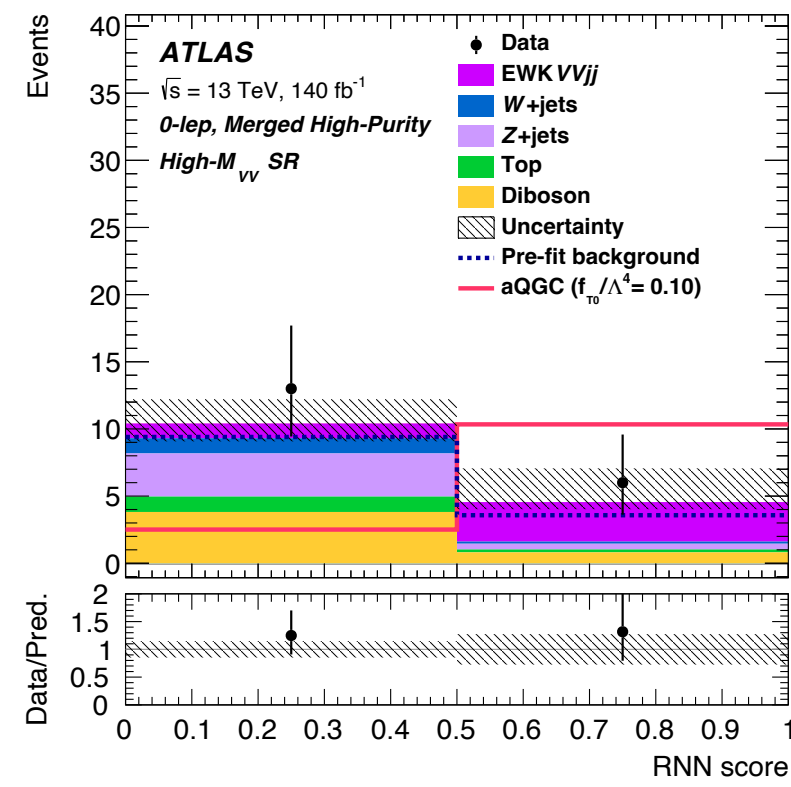
- Unitarity violation and clipping methods
 - Theoretically: require that perturbative partial-wave unitarity satisfied
 - Experimentally: **ad-hoc unitarisation procedure** — introducing a cut-off scale (**clipping threshold**), beyond which the coefficient is set to zero
 - In practice: a scan over several chosen clipping thresholds, at each threshold, obtain a constraint on the coefficient. The **final unitarised constraint** is taken from the intersection between the unitarity bound and the scan
- **Positivity boundaries**
 - UV theories assumed to obey the low-scale principles of unitarity, locality and causality
 - **Positive definite cross-sections on the helicity-amplitude**



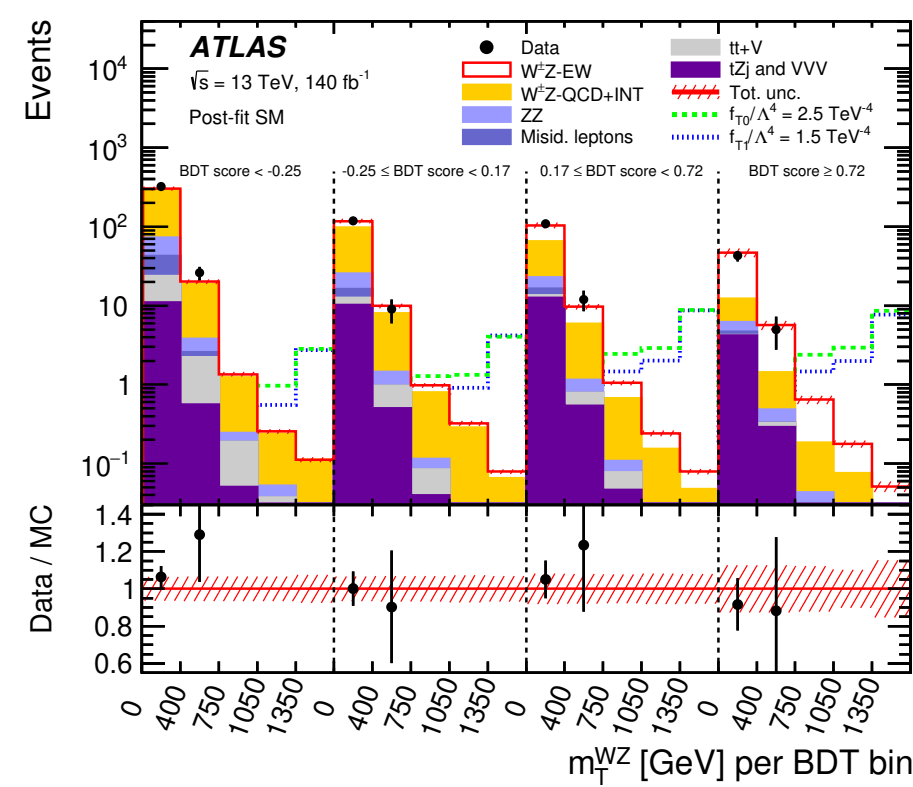


- 7 VBS analyses + 1 tri-boson analysis → constraints on coefficients of 17 Éboli basis operators — probe all gauge boson quartic vertices

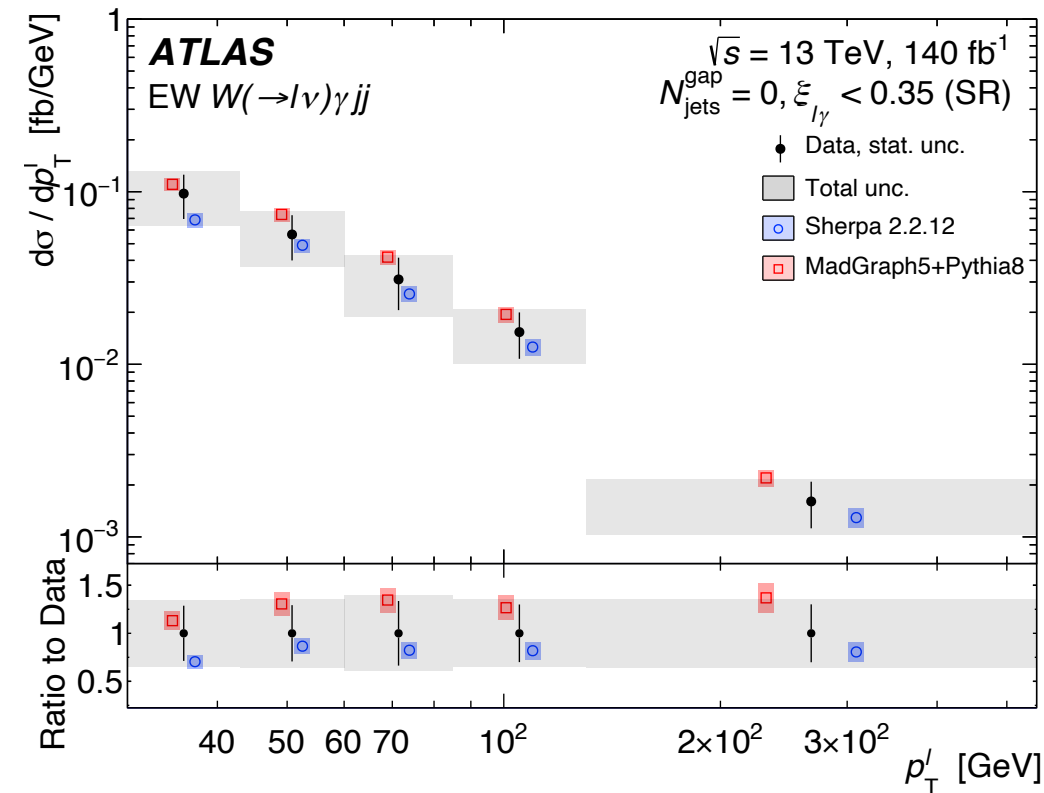
Semileptonic $VVjj$



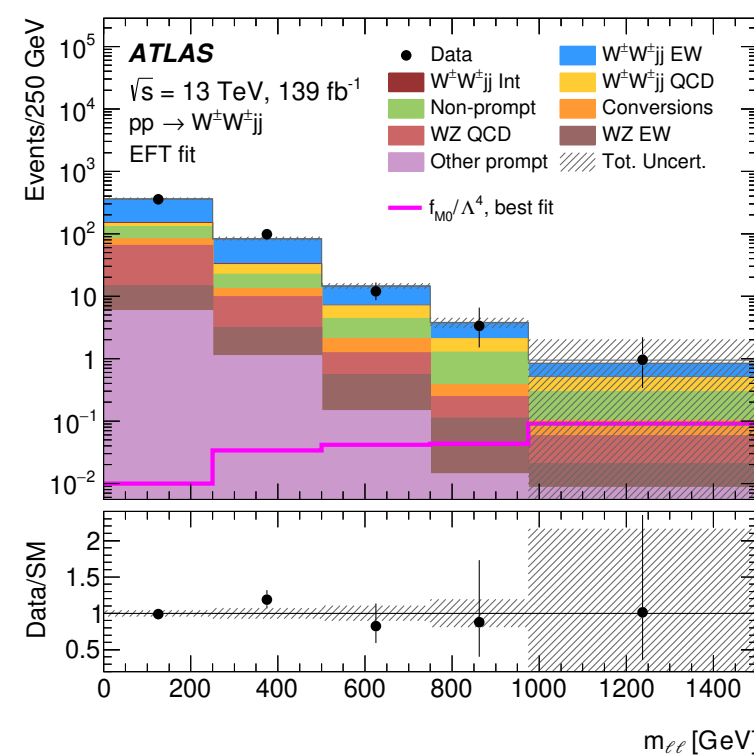
$WZjj$



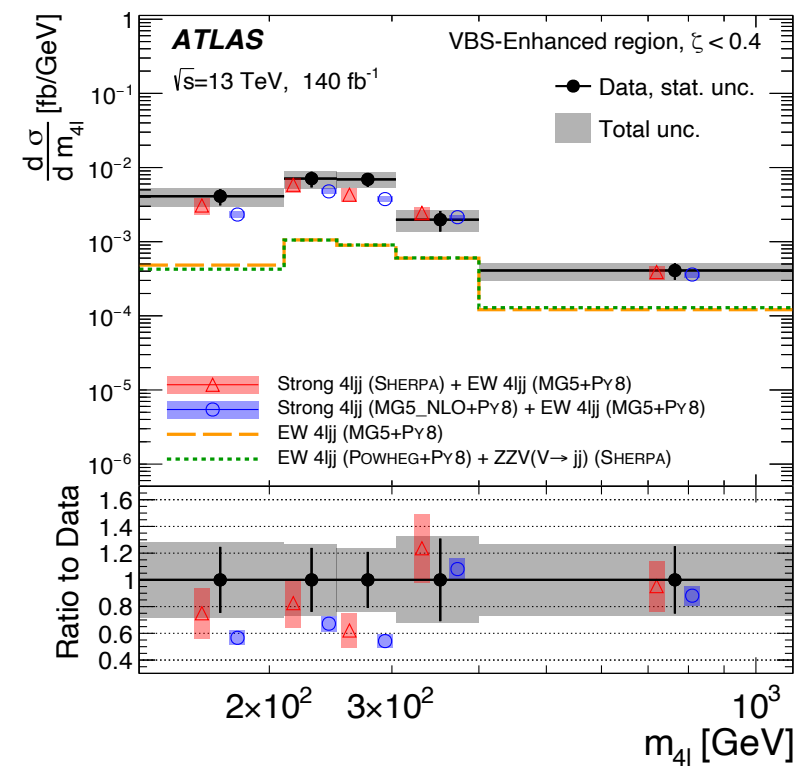
$W\gamma jj$



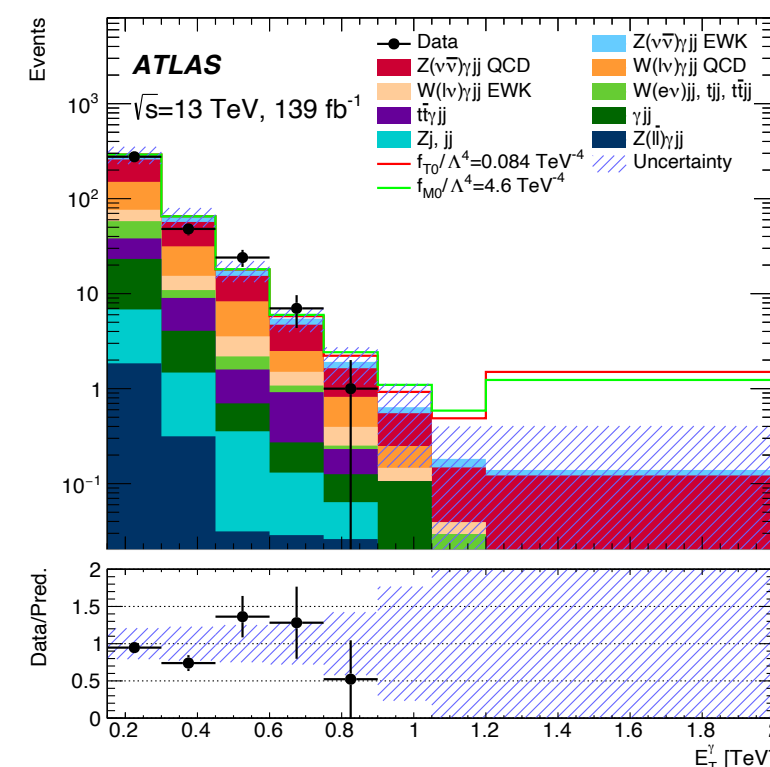
$WWjj$



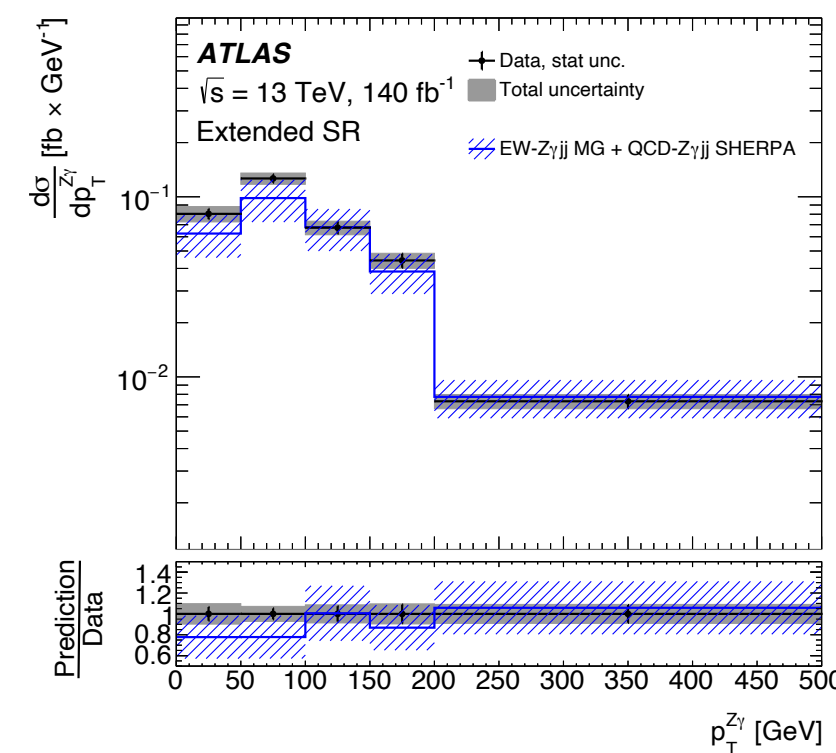
$ZZ(4l)jj$



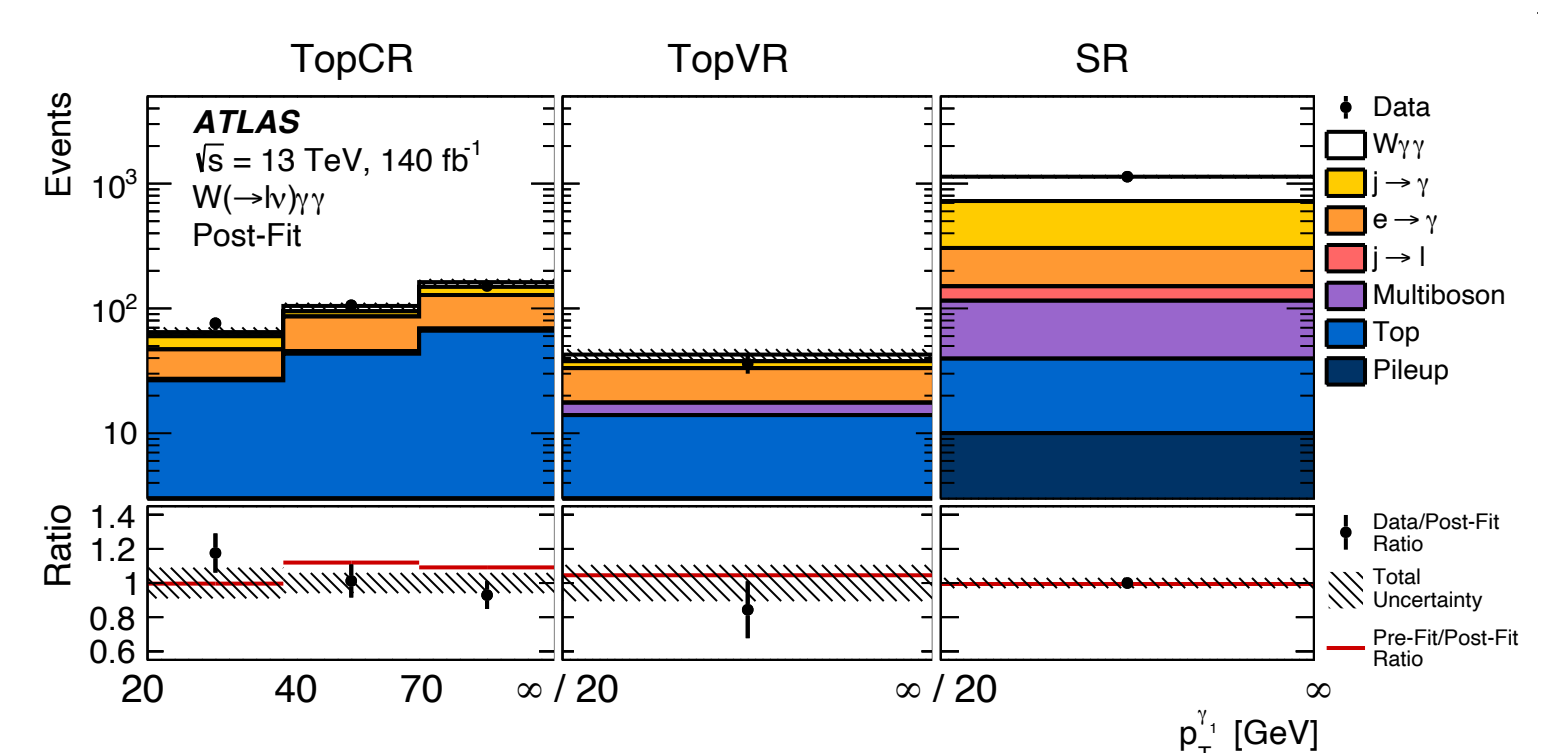
$Z(\nu\nu)\gamma jj$



$Z(ll)\gamma jj$



$W\gamma\gamma$



VBS analyses

- Semileptonic $VVjj$ ([2503.17461](#))
- $WZjj$ ([2403.15296](#)), $WWjj$ ([2312.00420](#)), $ZZ(4l)jj$ ([2308.12324](#))
- $W\gamma jj$ ([2403.02809](#)), $Z(\nu\nu)\gamma jj$ ([2208.12741](#)), $Z(ll)\gamma jj$ ([2305.19142](#))

Tri-boson analysis

- $W\gamma\gamma$ ([2308.03041](#))



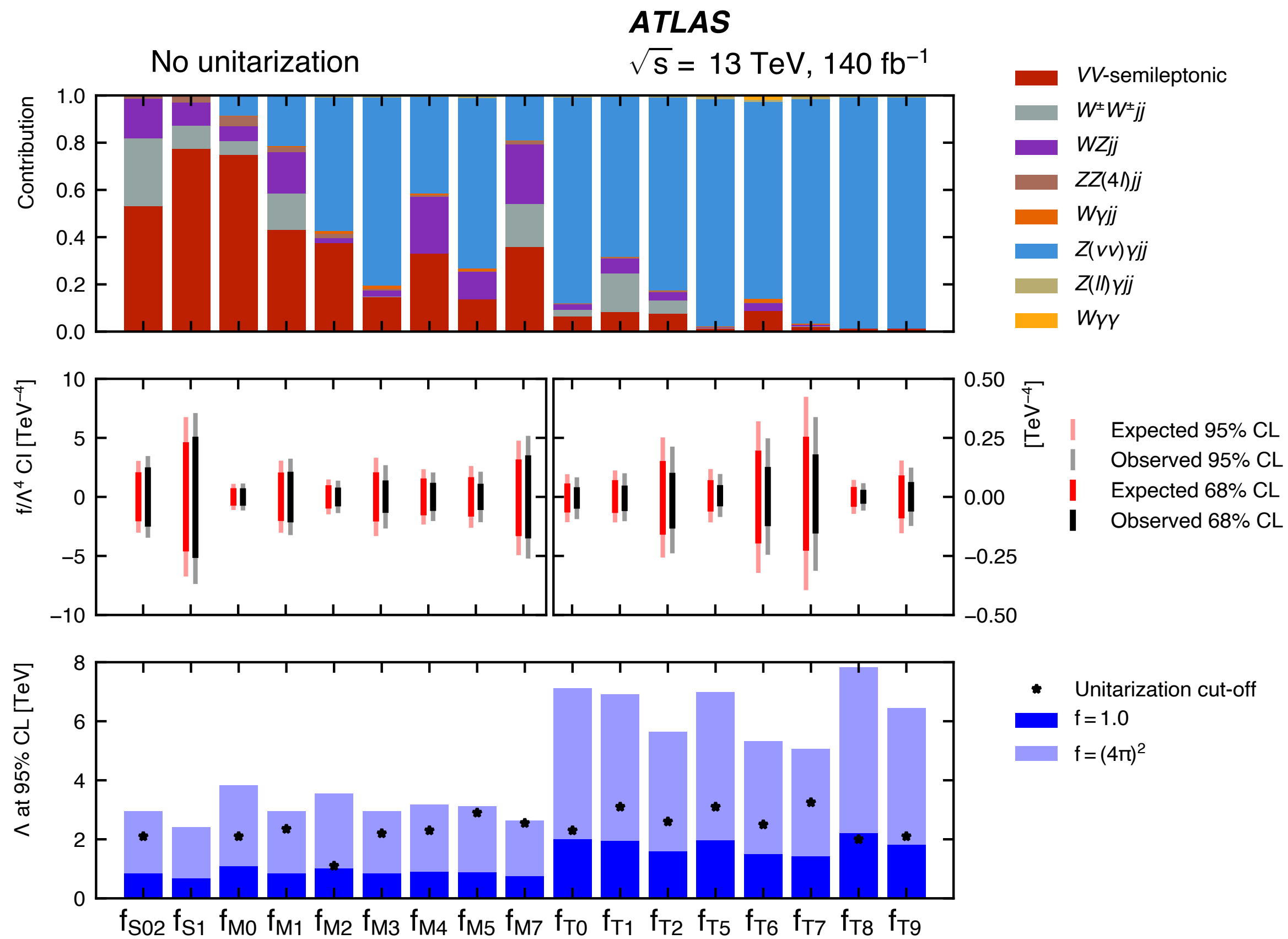
- Overlapped phase spaces
 - No significant overlap in signal sample; for background, some overlaps appear, but mostly negligible statistical effect
 - Exception: **one WW_{jj} control region overlap with WZ_{jj} signal region**. Removing this CR changes the constraints on operators at $\sim 0.5\%$ level \rightarrow **control region removed**



- Overlapped phase spaces
 - No significant overlap in signal sample; for background, some overlaps appear, but mostly negligible statistical effect
 - Exception: **one $WWjj$ control region overlap with $WZjj$ signal region**. Removing this CR changes the constraints on operators at $\sim 0.5\%$ level \rightarrow **control region removed**
- Fitted distribution changes
 - $Z(\nu\nu)\gamma jj$: additional observable bins for probing more operators simultaneously
 - $W\gamma\gamma$: finer observable bins to improve the constraints (**around 40% better**)
 - $W\gamma jj$: unify the observable used for EFT interpretations (**up to 20% better constraints**)



- Overlapped phase spaces
 - No significant overlap in signal sample; for background, some overlaps appear, but mostly negligible statistical effect
 - Exception: **one $WWjj$ control region overlap with $WZjj$ signal region**. Removing this CR changes the constraints on operators at $\sim 0.5\%$ level \rightarrow **control region removed**
- Fitted distribution changes
 - $Z(\nu\nu)\gamma jj$: additional observable bins for probing more operators simultaneously
 - $W\gamma\gamma$: finer observable bins to improve the constraints (**around 40% better**)
 - $W\gamma jj$: unify the observable used for EFT interpretations (**up to 20% better constraints**)
- Complementary / added EFT interpretations
 - $Z(ll)\gamma jj$, $ZZ(4l)jj$, $W\gamma\gamma$: no Éboli model interpretations in publication, newly added in this combination
 - $Z(\nu\nu)\gamma jj$, $WZjj$: extended interpretations in more operators
 - Cross-term effects are considered in this combination



- Main contribution: semileptonic $VVjj$ and $Z(\nu\nu)\gamma jj$
- Non-unitarised constraints
 - Current best constraints on T5, T6, T7, T8 and T9 across experiments
 - Compared to individual analyses: scalar and mixed-type operators get up to 30% tighter constraints, tensor-type operators have similar constraints as $Z(\nu\nu)\gamma jj$
- Probed energy scale given illustrative values of Wilson coefficients

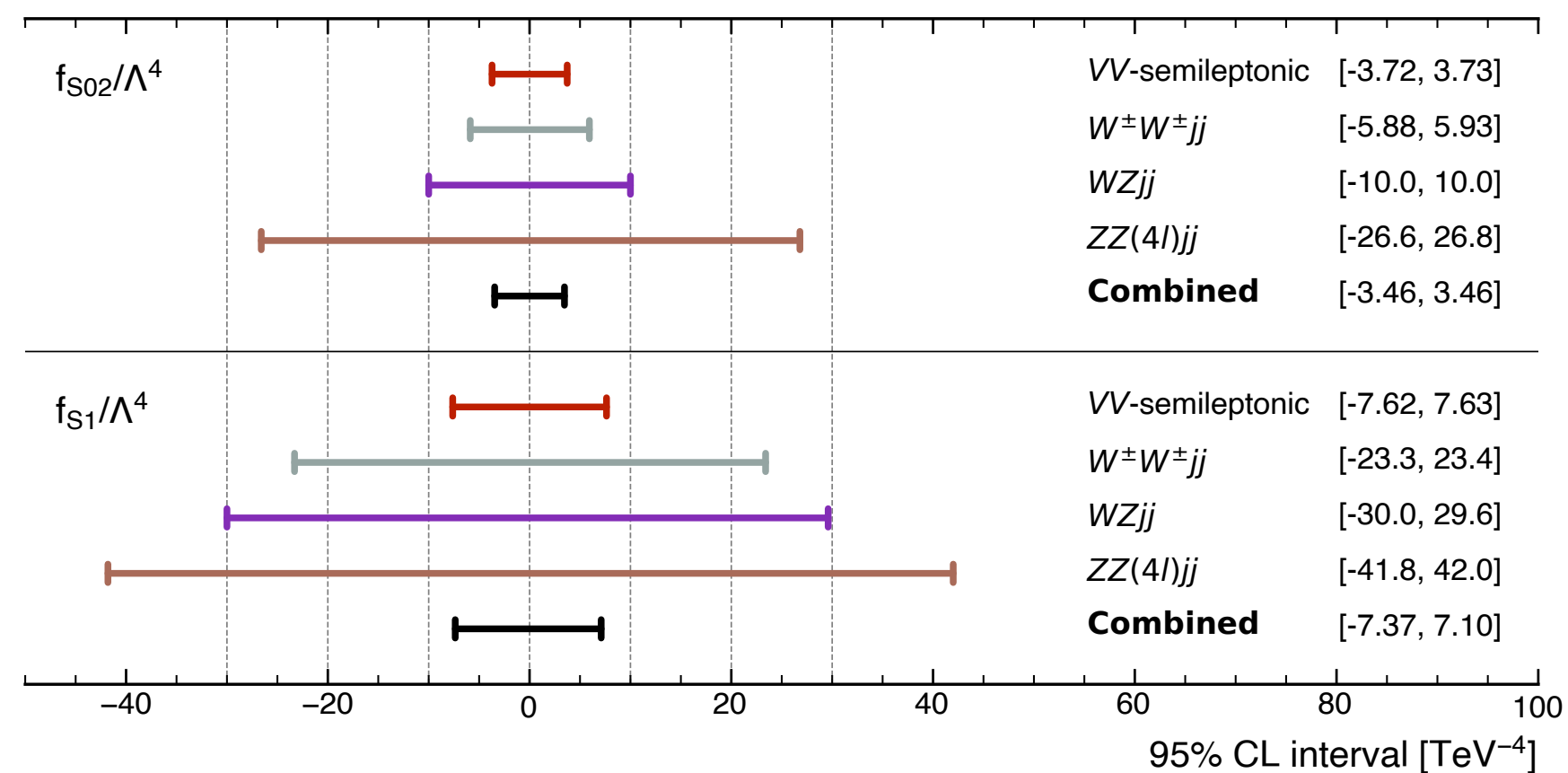


Results: 1-dimensional constraints

ATLAS

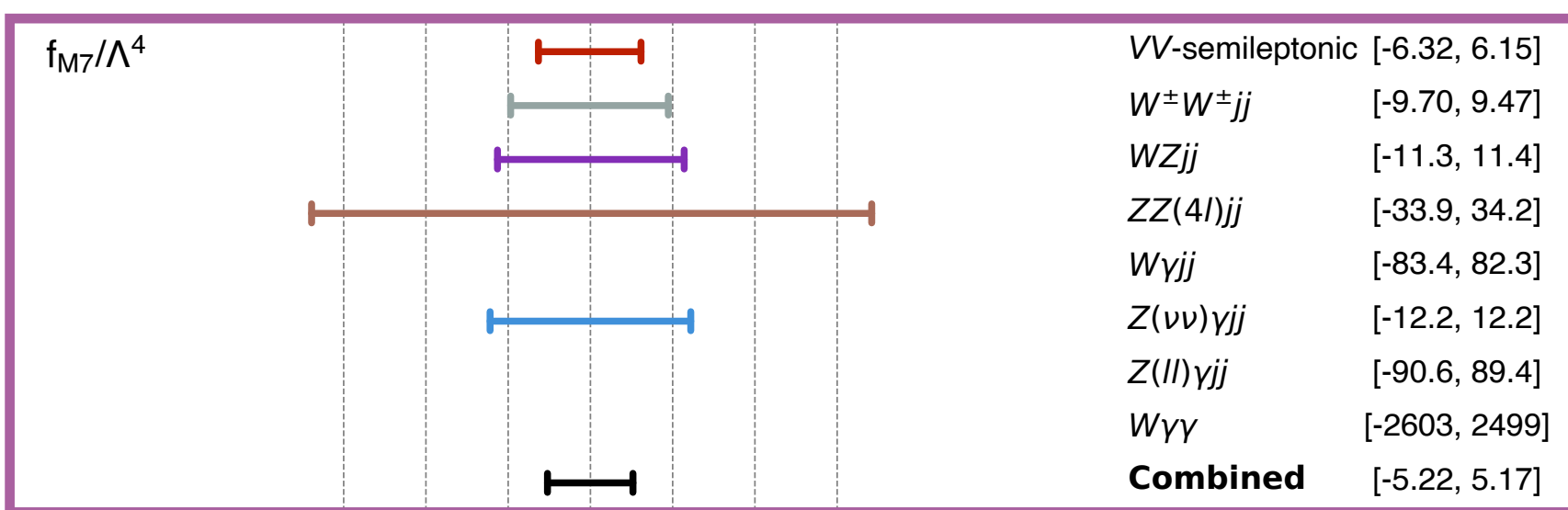
$\sqrt{s} = 13 \text{ TeV}, 140 \text{ fb}^{-1}$

No unitarization



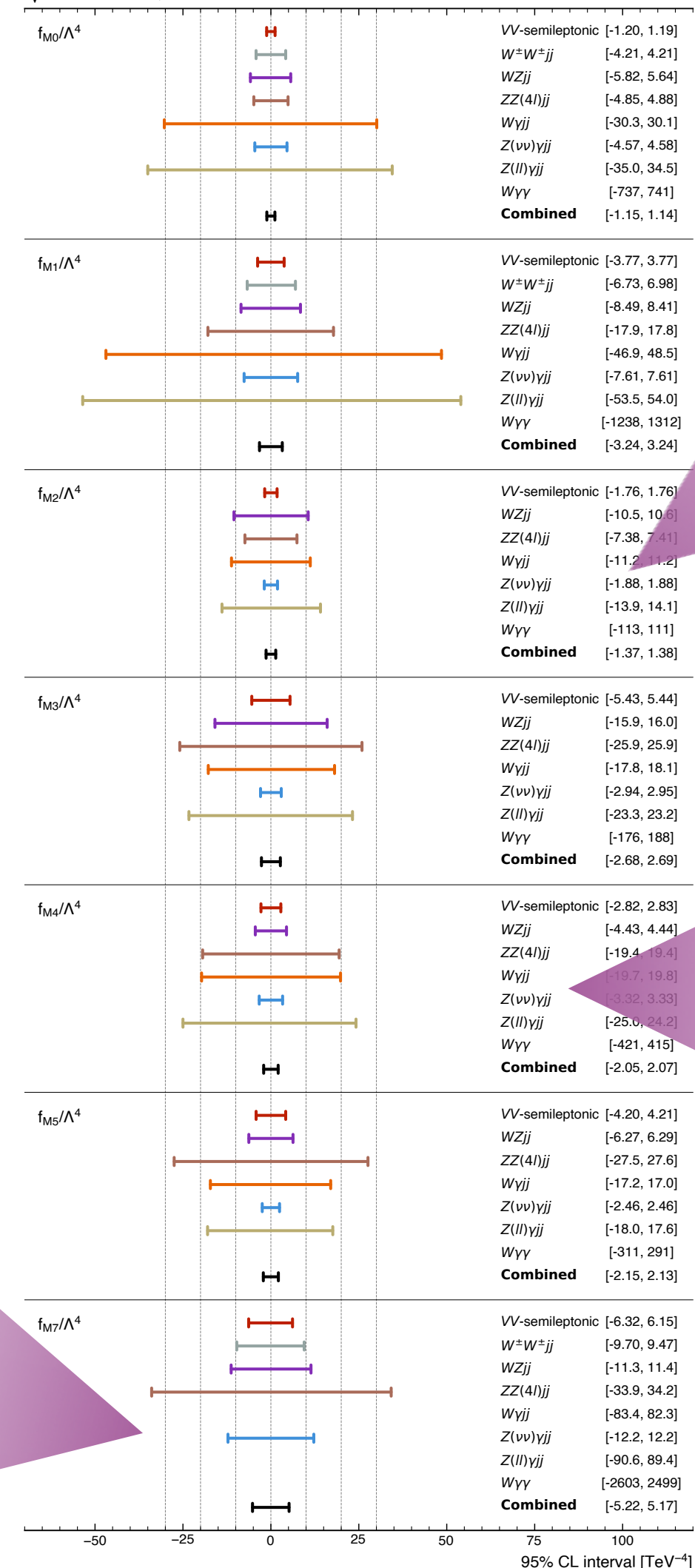
Scalar operators: around 5% better w.r.t. individual analyses

M7: 17% better w.r.t. individual analyses

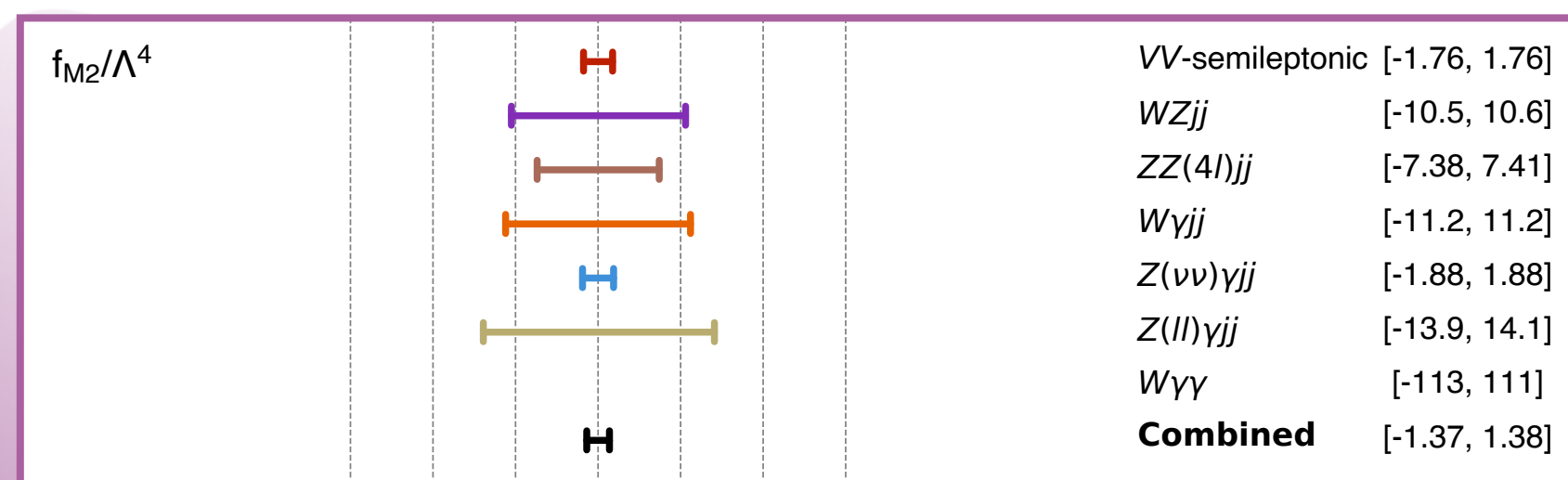


ATLAS
 $\sqrt{s} = 13 \text{ TeV}, 140 \text{ fb}^{-1}$

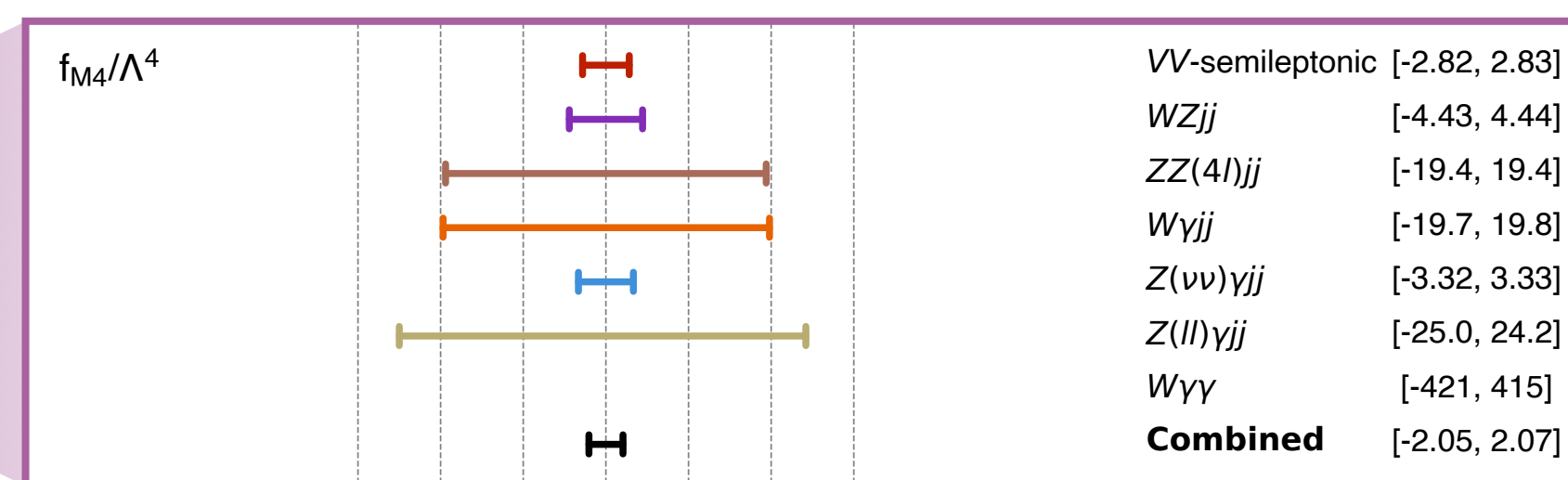
No unitarization



M2: 22% better w.r.t. individual analyses

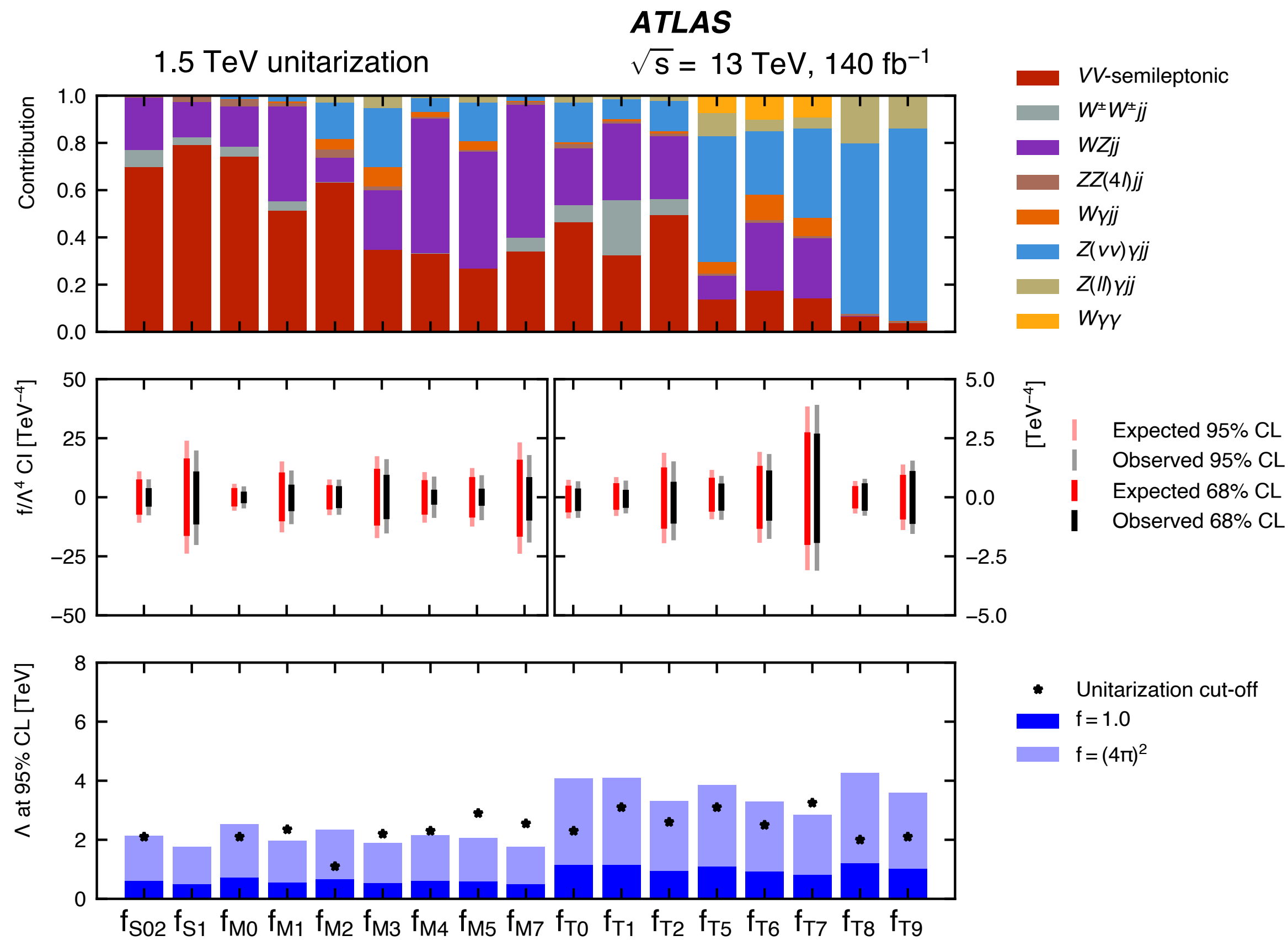


M4: 27% better w.r.t. individual analyses

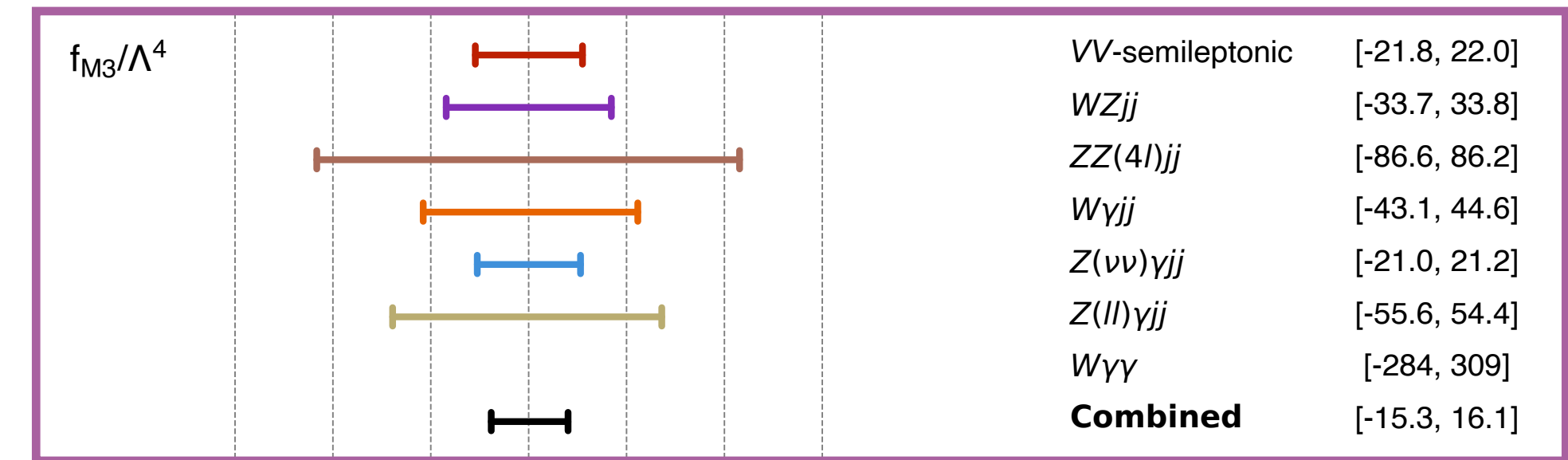




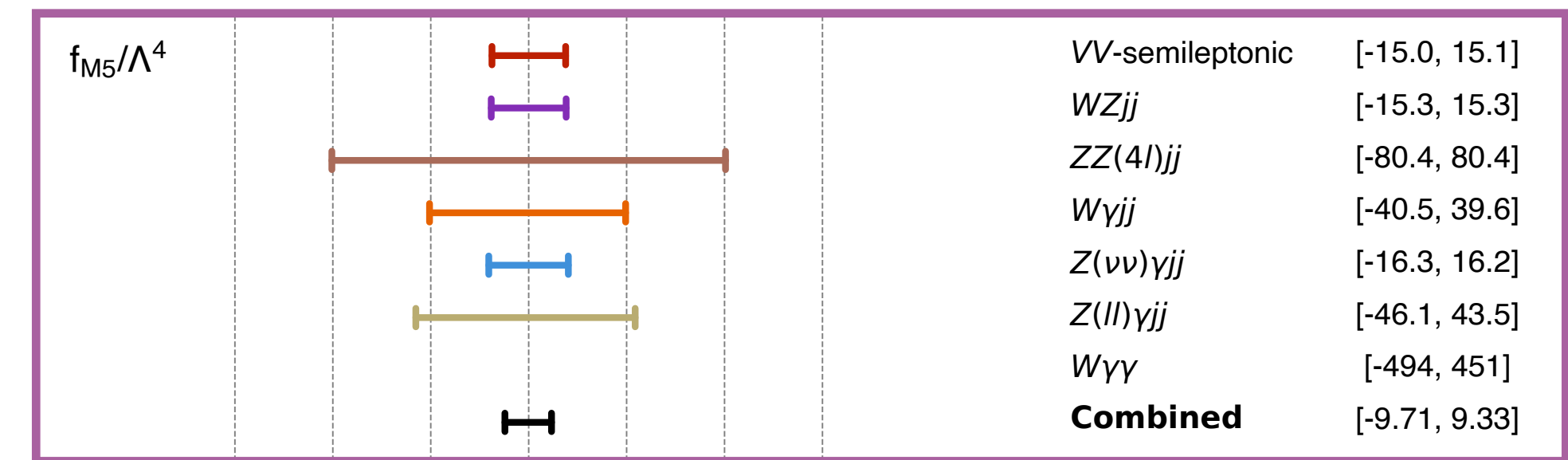
- At 1.5 TeV clipping: more even contribution from different analyses



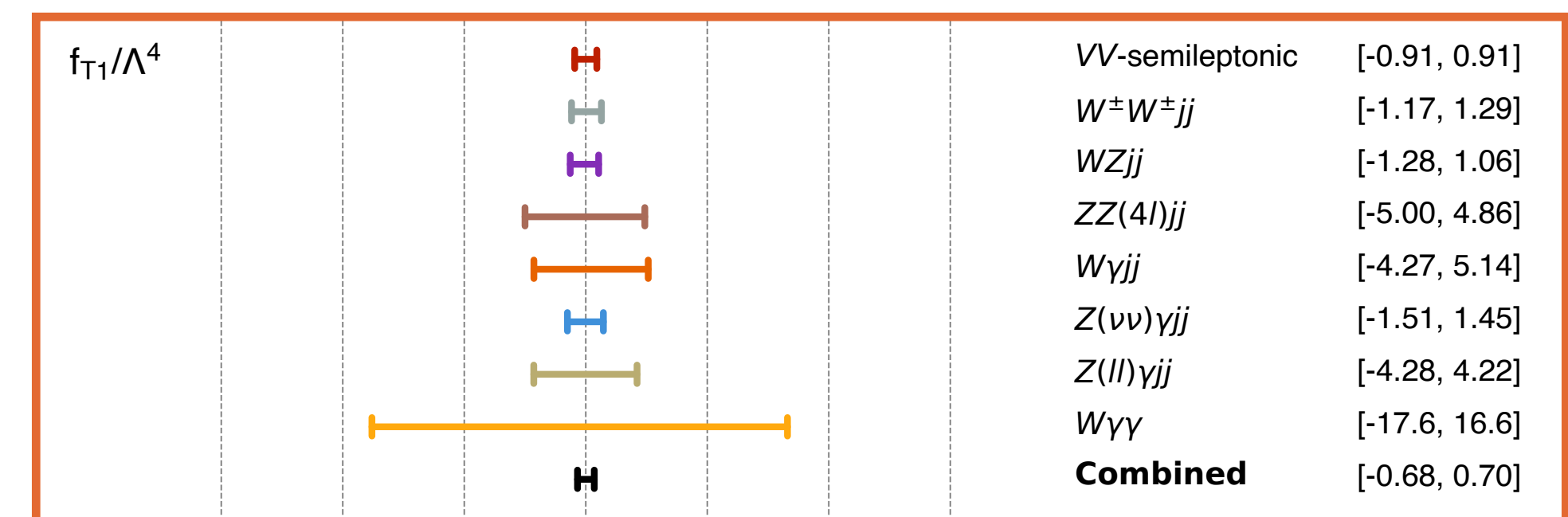
M3: 26% better w.r.t. individual analyses

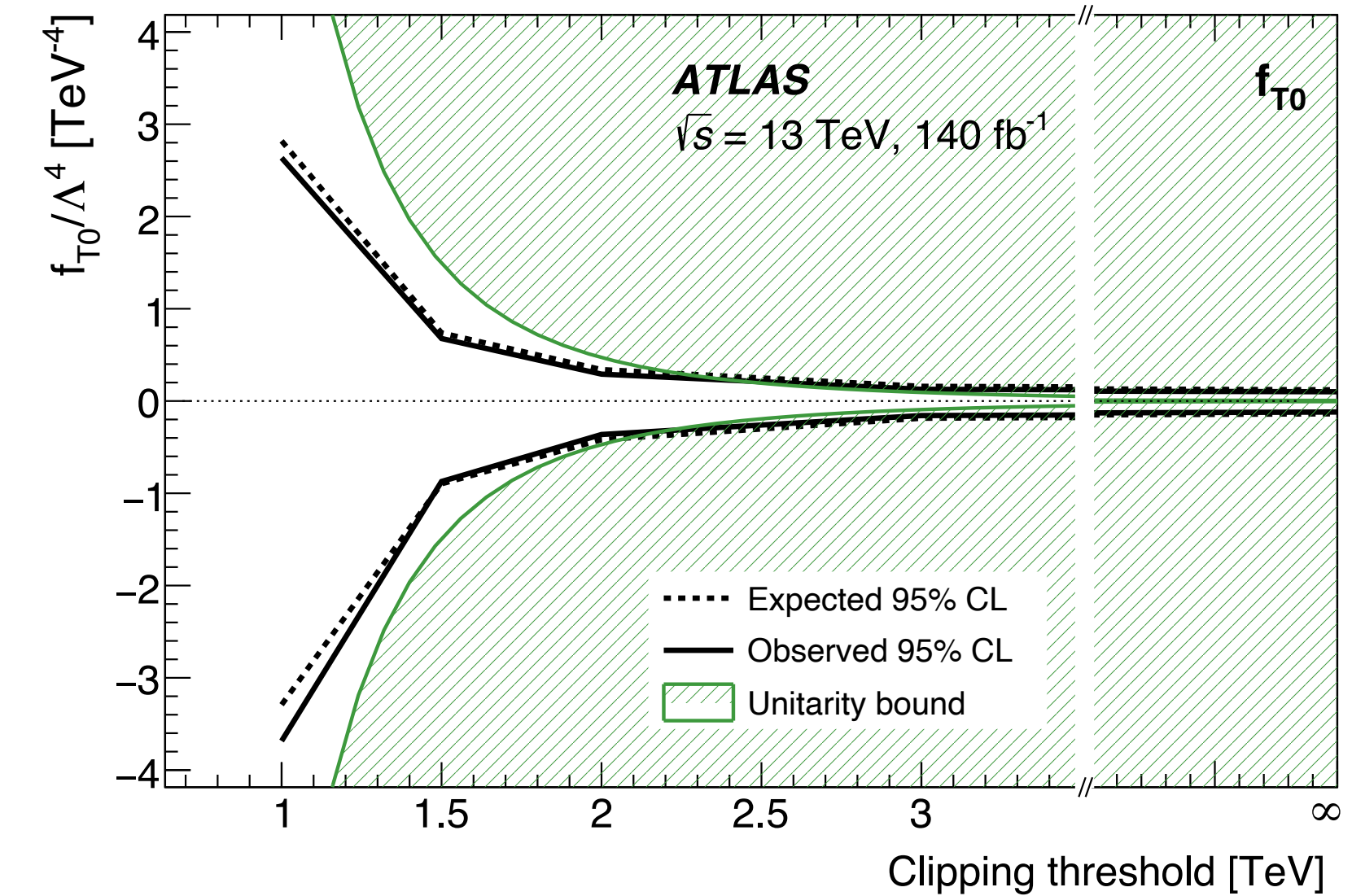
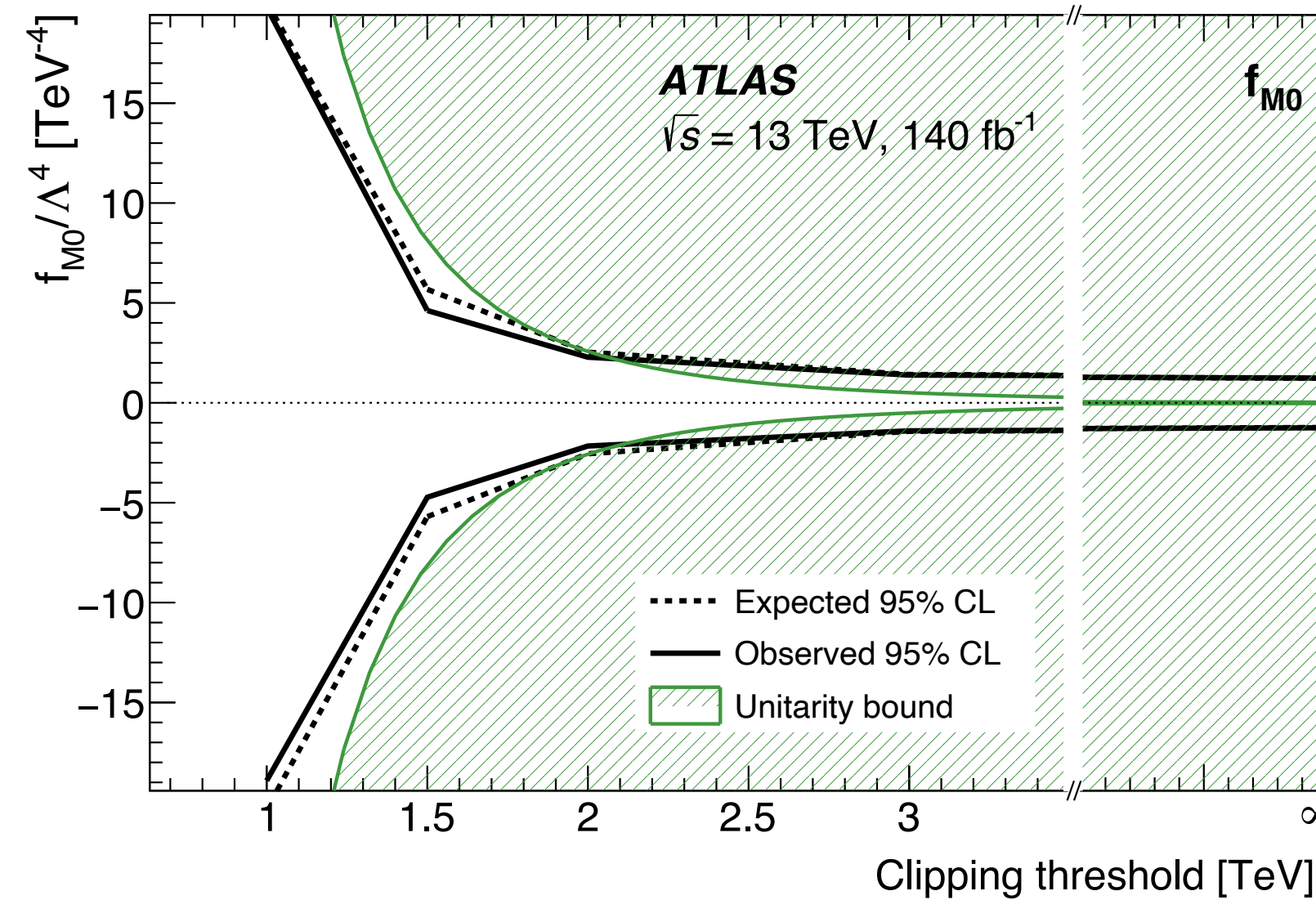
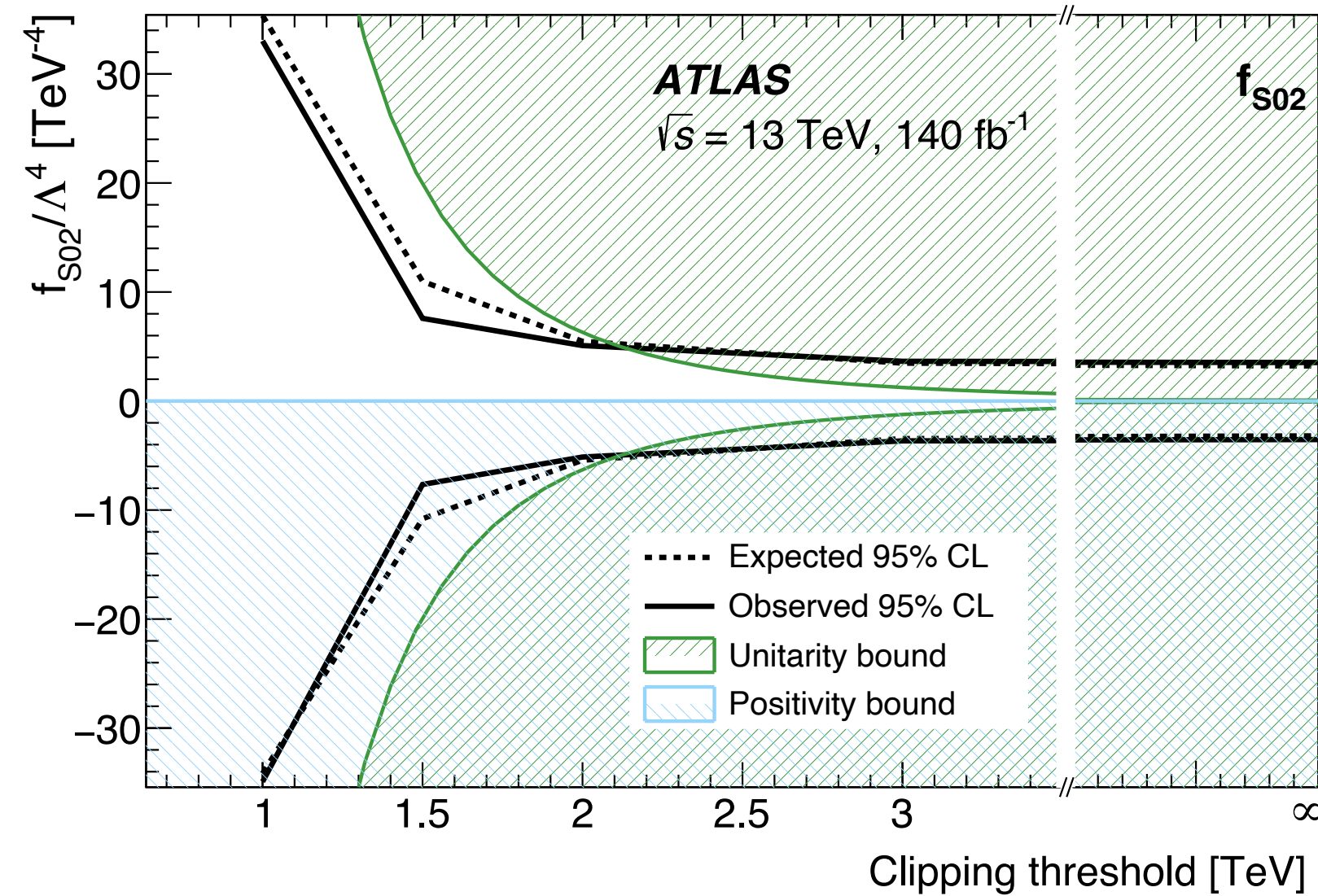


M5: 37% better w.r.t. individual analyses



T1: 24% better w.r.t. individual analyses



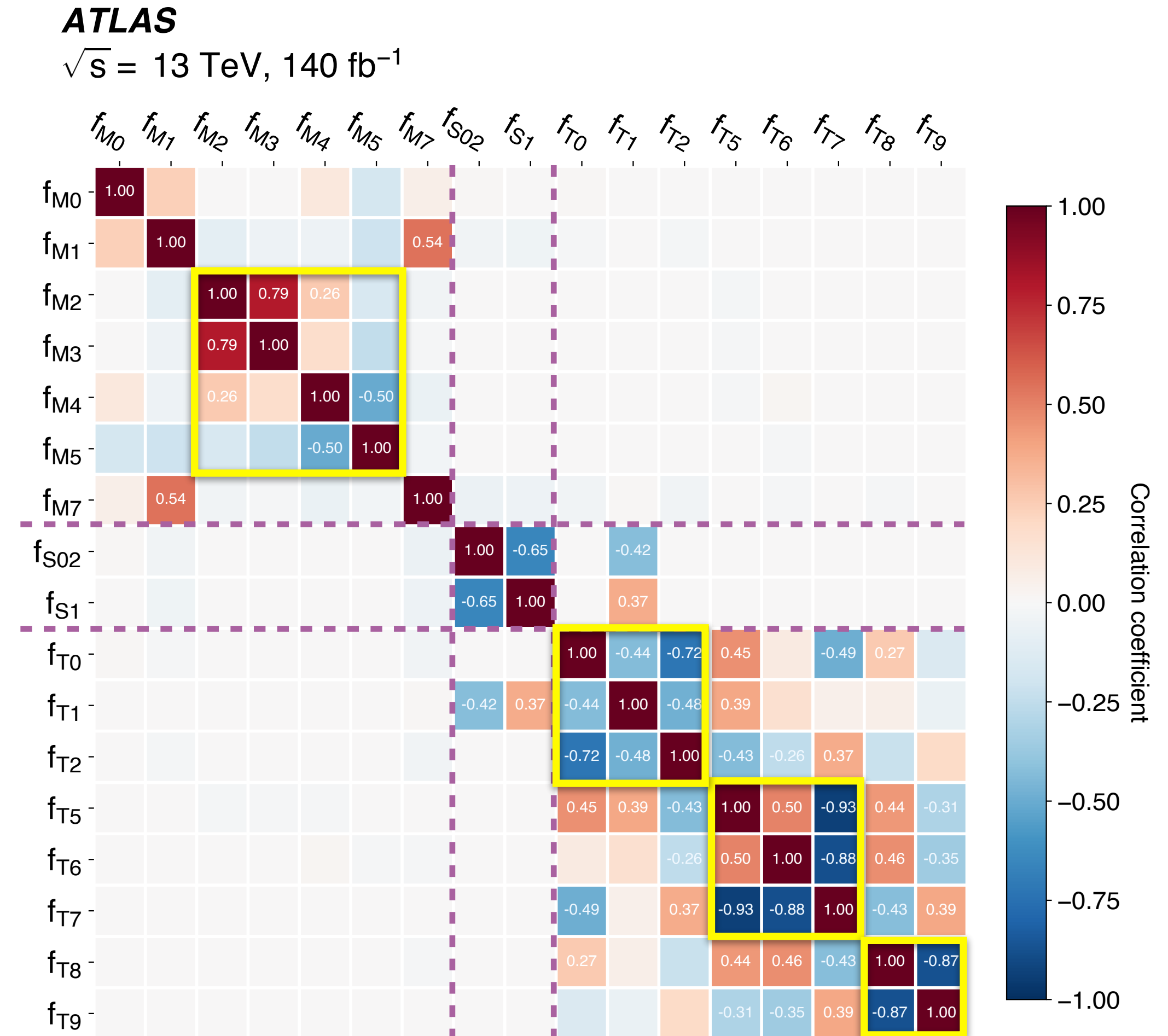


- The unitarisation cut-offs are usually around 2-3 TeV
- No unitarisation cut-off found for S1, as the theory bound set better constraints than the experimental interval
- Unitarised confidence intervals: 17-96% improvements compared to the published results



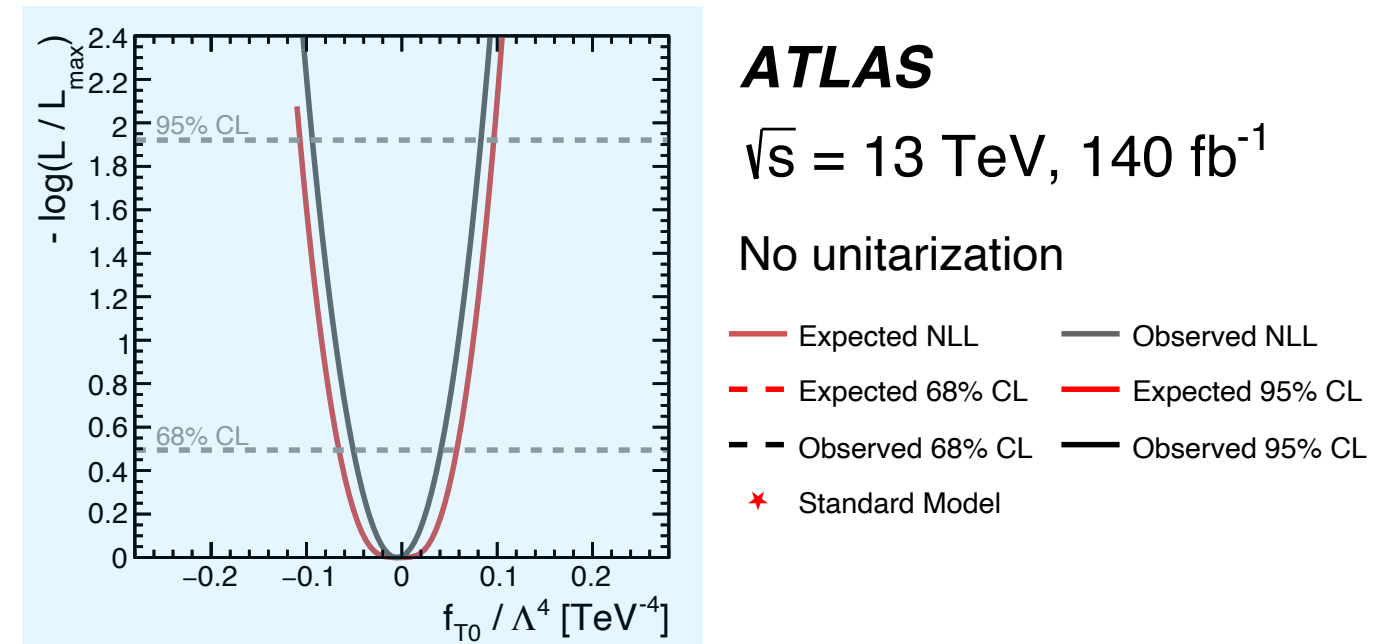
$$\mathcal{A}^2 = \underbrace{|\mathcal{A}_{SM}|^2}_{\text{Pure SM}} + \underbrace{2 \sum_i A_i \frac{c_i}{\Lambda^4}}_{\text{Linear term}} + \sum_i B_i \frac{c_i^2}{\Lambda^8} + \underbrace{2 \sum_{i \neq j} \frac{c_i c_j}{\Lambda^8} \Re(\mathcal{A}_i^* \mathcal{A}_j)}_{\text{EFT cross-terms (quadratic)}}$$

- Correlation structure of the Éboli operators affect the sizes of cross-terms:
 - Between different operator families (mixed, scalar or tensor), the cross-terms are highly suppressed
 - Within each family, the several blocks are formed:
 - f_{M0}, f_{M1}, f_{M7} / $f_{M2}, f_{M3}, f_{M4}, f_{M5}$
 - f_{S02}, f_{S1}
 - f_{T0}, f_{T1}, f_{T2} / f_{T5}, f_{T6}, f_{T7} / f_{T8}, f_{T9}

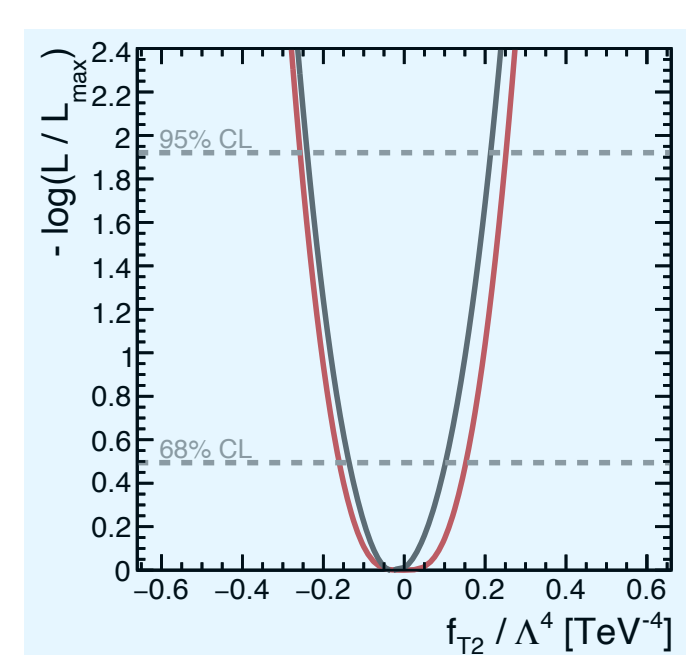
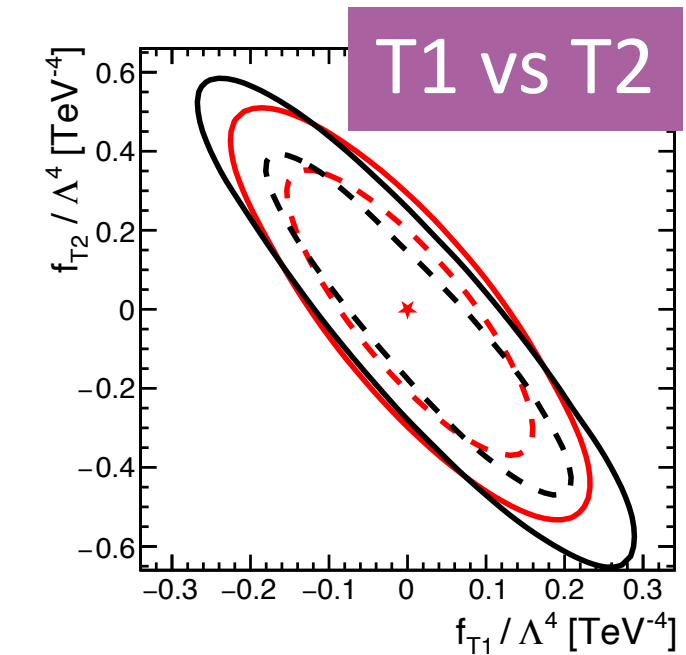
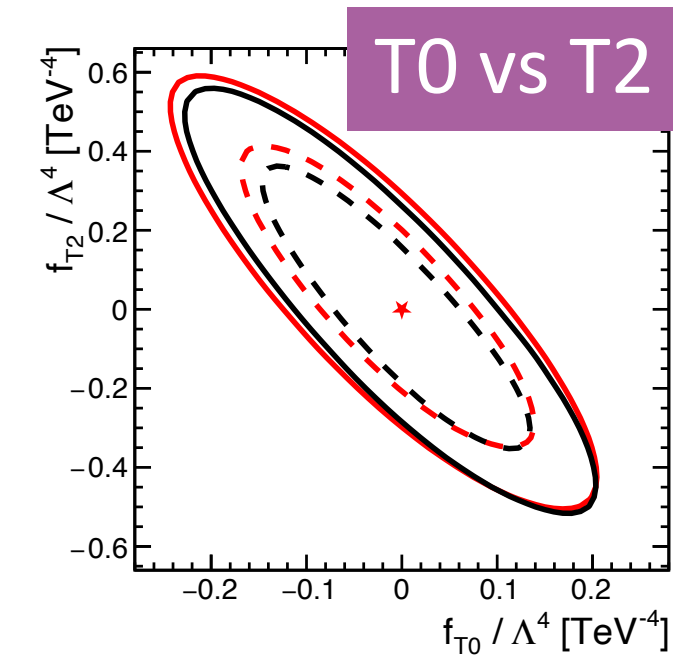
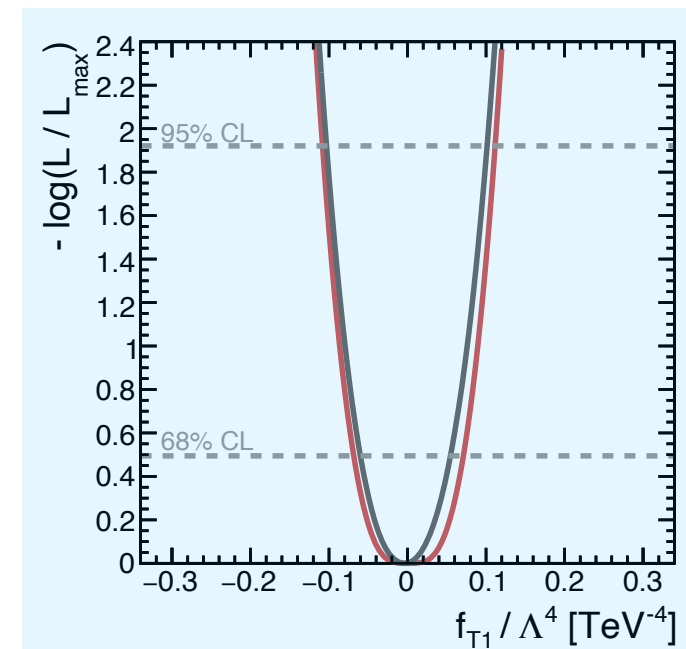
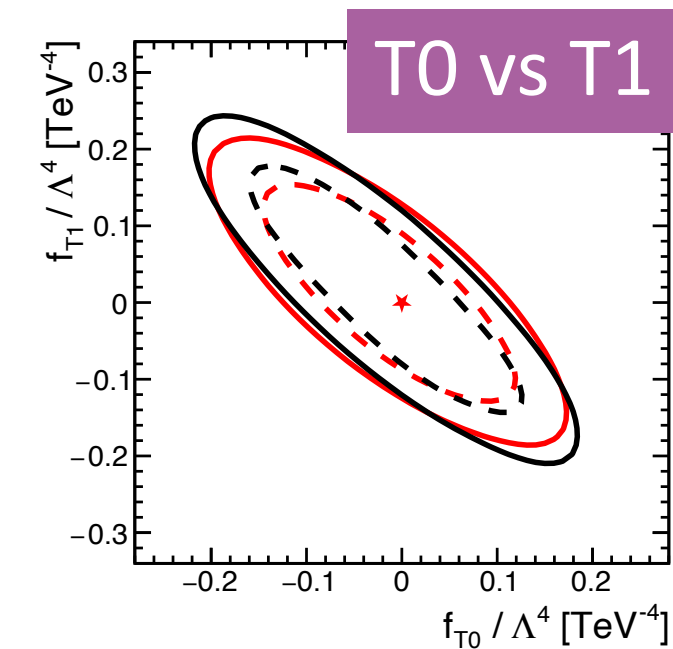




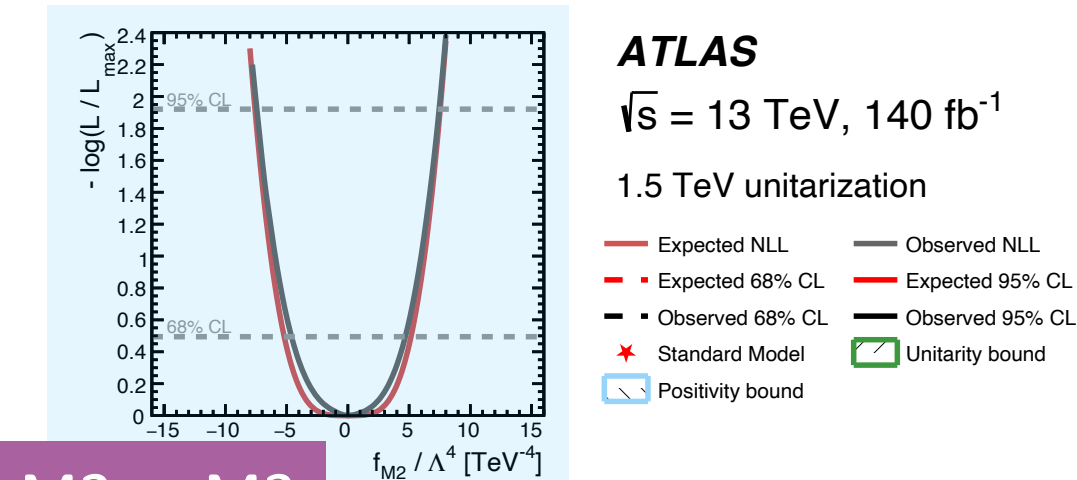
No unitarisation cut-off applied, T0, T1 & T2



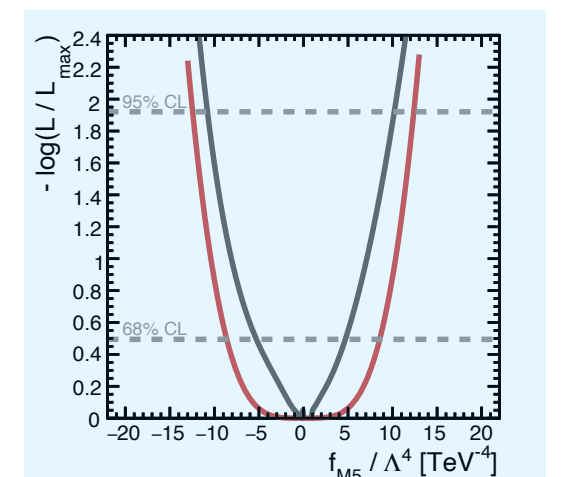
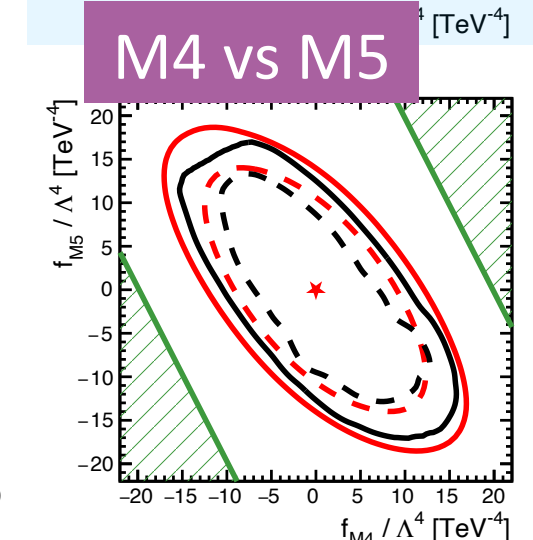
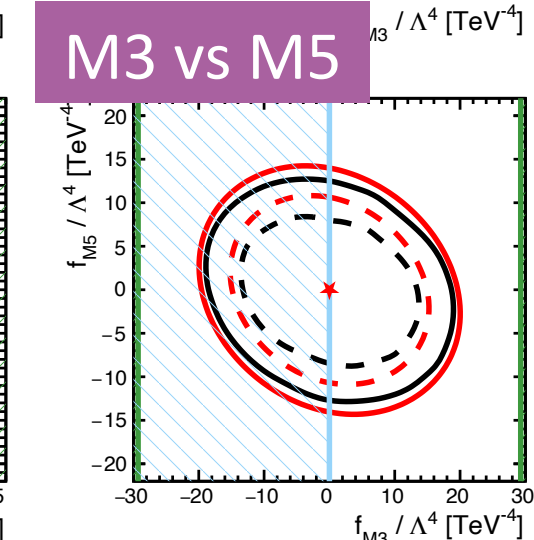
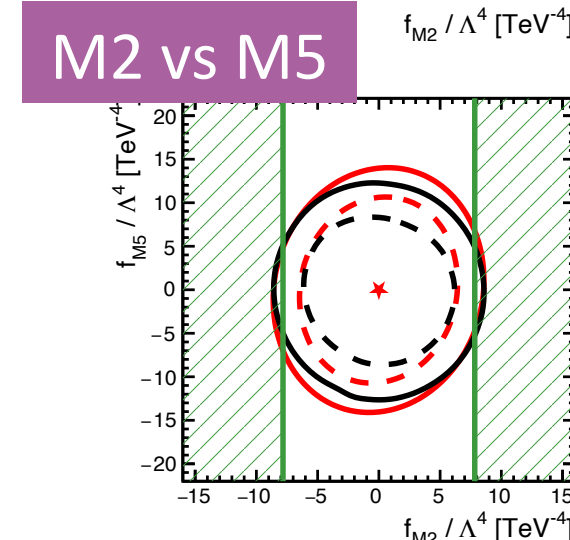
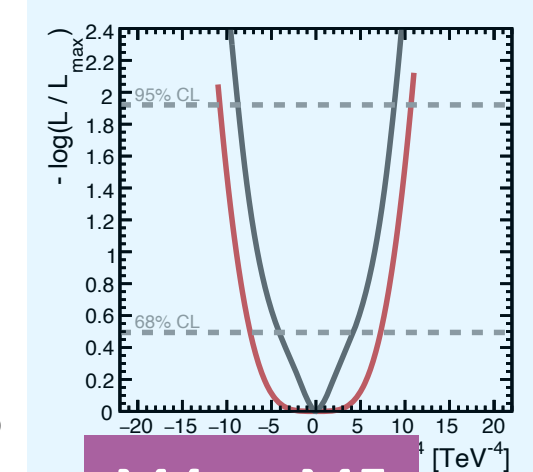
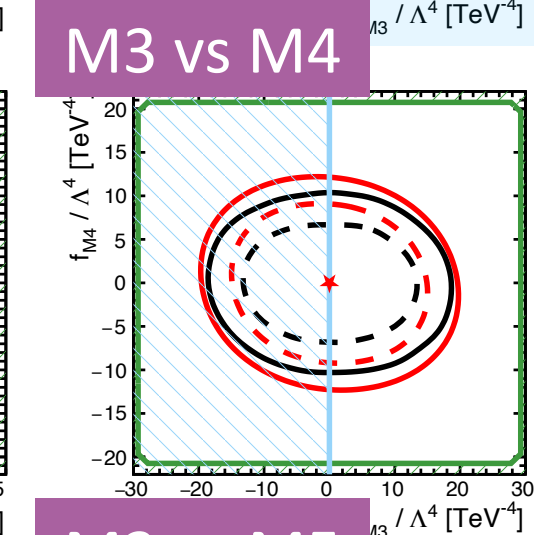
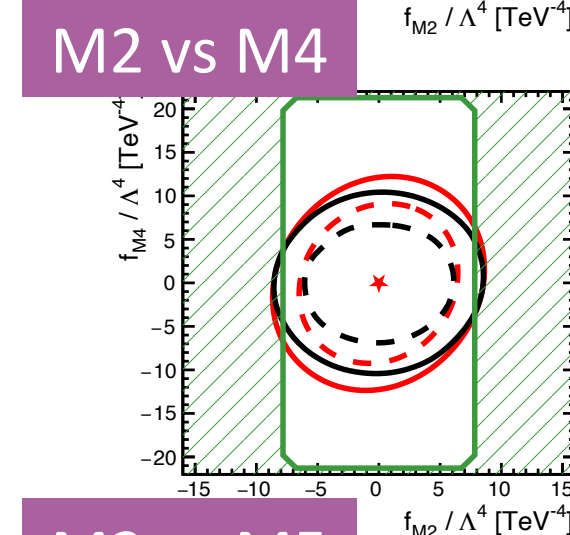
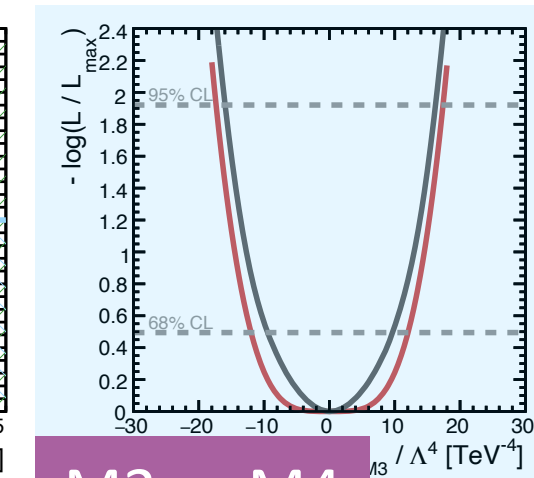
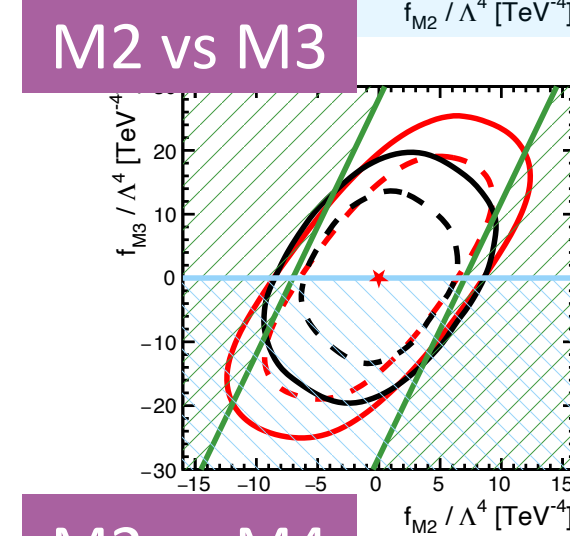
1-dimensional LLH scans of T0, T1 and T2



Unitarisation cut-off applied at 1.5 TeV, M2, M3, M4 & M5



1-dimensional LLH scans of M2, M3, M4 and M5





- Profiled constraints:
 - Obtained through likelihood scans for each operator, **allowing other operators to freely float**
 - Enable interpretation with models predicting simultaneously changing coefficients

Coefficient	Profiled expected confidence intervals [TeV ⁻⁴]	Profiled observed confidence intervals [TeV ⁻⁴]
f_{S02}/Λ^4	[-4.06, 4.08]	[-4.87, 4.88]
f_{S1}/Λ^4	[-8.72, 8.73]	[-9.82, 9.82]
f_{M0}/Λ^4	[-1.67, 1.68]	[-1.68, 1.65]
f_{M1}/Λ^4	[-8.13, 7.52]	[-9.05, 8.58]
f_{M2}/Λ^4	[-1.91, 1.91]	[-1.97, 1.99]
f_{M3}/Λ^4	[-4.16, 4.16]	[-3.89, 3.92]
f_{M4}/Λ^4	[-3.15, 3.15]	[-2.55, 2.56]
f_{M5}/Λ^4	[-3.48, 3.49]	[-2.77, 2.77]
f_{M7}/Λ^4	[-16.6, 15.7]	[-12.4, 12.9]
f_{T0}/Λ^4	[-0.33, 0.24]	[-0.34, 0.22]
f_{T1}/Λ^4	[-0.199, 0.211]	[-0.254, 0.283]
f_{T2}/Λ^4	[-0.578, 0.639]	[-0.665, 0.599]
f_{T5}/Λ^4	[-0.405, 0.384]	[-0.319, 0.289]
f_{T6}/Λ^4	[-0.658, 0.642]	[-0.490, 0.370]
f_{T7}/Λ^4	[-1.51, 1.58]	[-1.17, 1.13]
f_{T8}/Λ^4	[-0.196, 0.181]	[-0.163, 0.147]
f_{T9}/Λ^4	[-0.360, 0.384]	[-0.281, 0.280]



- Profiled constraints:
 - Obtained through likelihood scans for each operator, **allowing other operators to freely float**
 - Enable interpretation with models predicting simultaneously changing coefficients
- Compared to normal 1 dimensional scan:
 - Operators having smaller cross-terms with others are not much affected (\sim a few percents)
 - Higher cross-terms — significant changes

Coefficient	Profiled expected confidence intervals [TeV ⁻⁴]	Profiled observed confidence intervals [TeV ⁻⁴]
f_{S02}/Λ^4	[-4.06, 4.08]	[-4.87, 4.88]
f_{S1}/Λ^4	[-8.72, 8.73]	[-9.82, 9.82]
f_{M0}/Λ^4	[-1.67, 1.68]	[-1.68, 1.65]
f_{M1}/Λ^4	[-8.13, 7.52]	[-9.05, 8.58]
f_{M2}/Λ^4	[-1.91, 1.91]	[-1.97, 1.99]
f_{M3}/Λ^4	[-4.16, 4.16]	[-3.89, 3.92]
f_{M4}/Λ^4	[-3.15, 3.15]	[-2.55, 2.56]
f_{M5}/Λ^4	[-3.48, 3.49]	[-2.77, 2.77]
f_{M7}/Λ^4	[-16.6, 15.7]	[-12.4, 12.9]
f_{T0}/Λ^4	[-0.33, 0.24]	[-0.34, 0.22]
f_{T1}/Λ^4	[-0.199, 0.211]	[-0.254, 0.283]
f_{T2}/Λ^4	[-0.578, 0.639]	[-0.665, 0.599]
f_{T5}/Λ^4	[-0.405, 0.384]	[-0.319, 0.289]
f_{T6}/Λ^4	[-0.658, 0.642]	[-0.490, 0.370]
f_{T7}/Λ^4	[-1.51, 1.58]	[-1.17, 1.13]
f_{T8}/Λ^4	[-0.196, 0.181]	[-0.163, 0.147]
f_{T9}/Λ^4	[-0.360, 0.384]	[-0.281, 0.280]

$$\mathcal{L}_{SMEFT} = \mathcal{L}_{SM} + \sum_i \frac{c_i^{(5)}}{\Lambda} \mathcal{O}_i^{(5)} + \underbrace{\sum_i \frac{c_i^{(6)}}{\Lambda^2} \mathcal{O}_i^{(6)}}_{\text{Dimension-6}} + \sum_i \frac{c_i^{(7)}}{\Lambda^3} \mathcal{O}_i^{(7)} + \underbrace{\sum_i \frac{c_i^{(8)}}{\Lambda^4} \mathcal{O}_i^{(8)}}_{\text{Dimension-8}} + \dots$$

- The first combination paper focusing on dimension-8 EFT operators that induce aQGCs
 - Many modifications to input analyses to facilitate the combination
 - 1-dimensional, 2-dimensional and profiled constraints on 17 Éboli basis operators are obtained, with different unitarisation bounds considered
 - Competitive results with the CMS collaboration. For several operators, this combination provides the most sensitive constraints to date
- Future: more multi-boson analyses to be included, optimisation of analysis designs for EFT interpretation, a larger set of EFT operators... — a very exciting field to explore!



Related CMS papers on aQGC operators

[ZZ\(4l\)jj 2008.07013](#), [Zγjj 2106.11082](#), [W/Zγγ 2105.12780](#),
 leptonic [WZ/WW 2005.01173](#), semileptonic [VV 2510.00118](#),
 high-mass $\gamma\gamma \rightarrow WW/ZZ$ [2211.16320](#)

Back-up