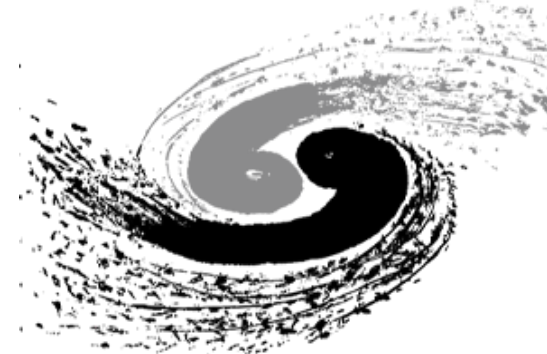




Simulation of Noble Liquid Calorimetry Performances

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for the ALLEGRO ECAL team

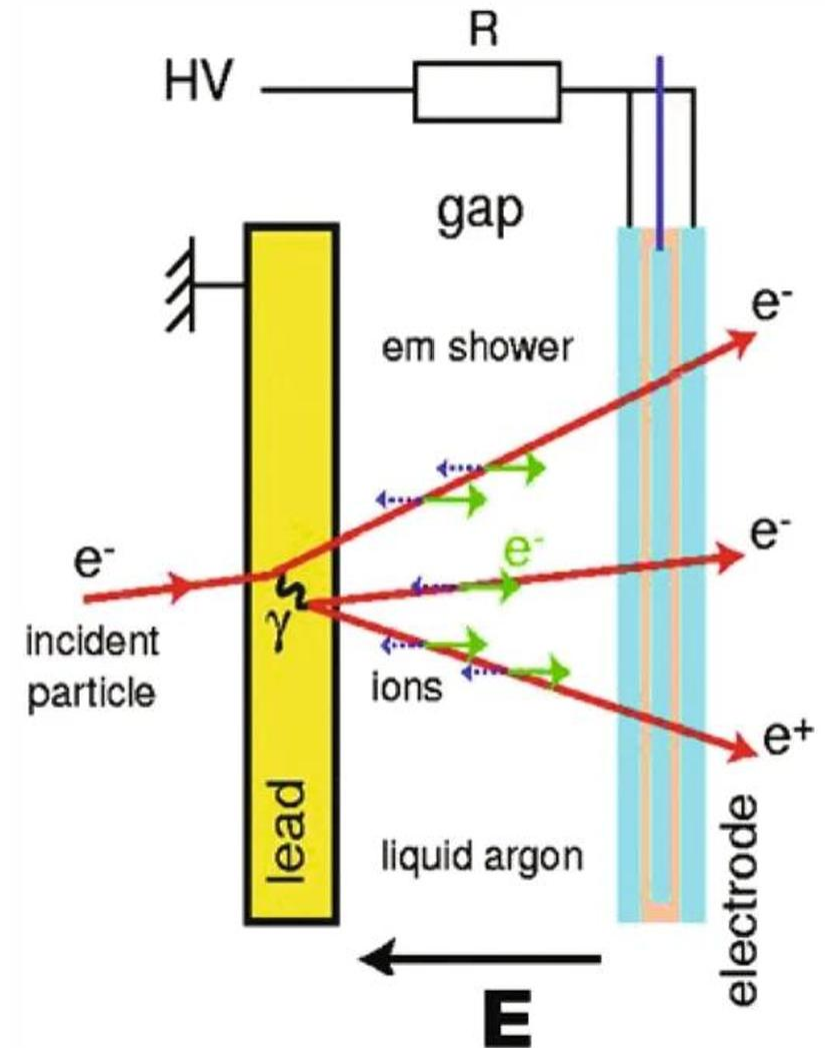
Noble Liquid Calorimeter

Sampling calorimeter: absorber + noble liquid active gap + read-out electrode

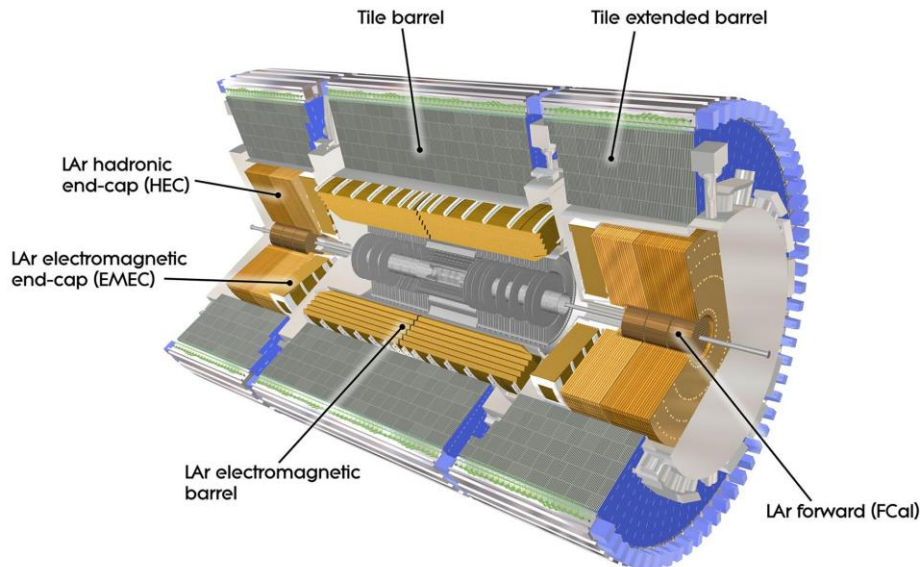
- Absorbers initiate electromagnetic showers
- Ionisation charge develops in noble liquid
- Electrons drift under high voltage to readout electrodes
- Induced current $\rightarrow$ reconstructed deposited energy

Advantages:

- Good energy resolution
- Linearity, uniformity
- Stability
- Radiation hardness
- Mature technology verified in many HEP experiments
e.g. D0, H1, NA48/62, ATLAS



Design Evolution toward the FCC-ee ECAL

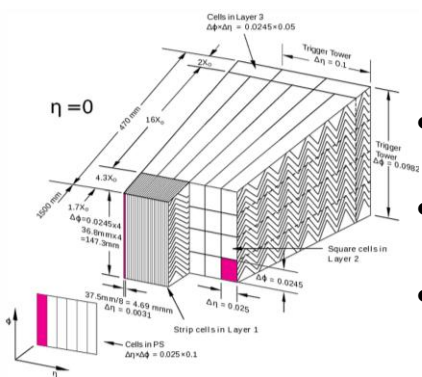


FCC-ee Calorimetry needs:

- Jet resolutions $\sim 30\%/\sqrt{E}$
- γ/π^0 separation
- Particle-flow



A Lepton Lepton collider Experiment with Granular Read-Out

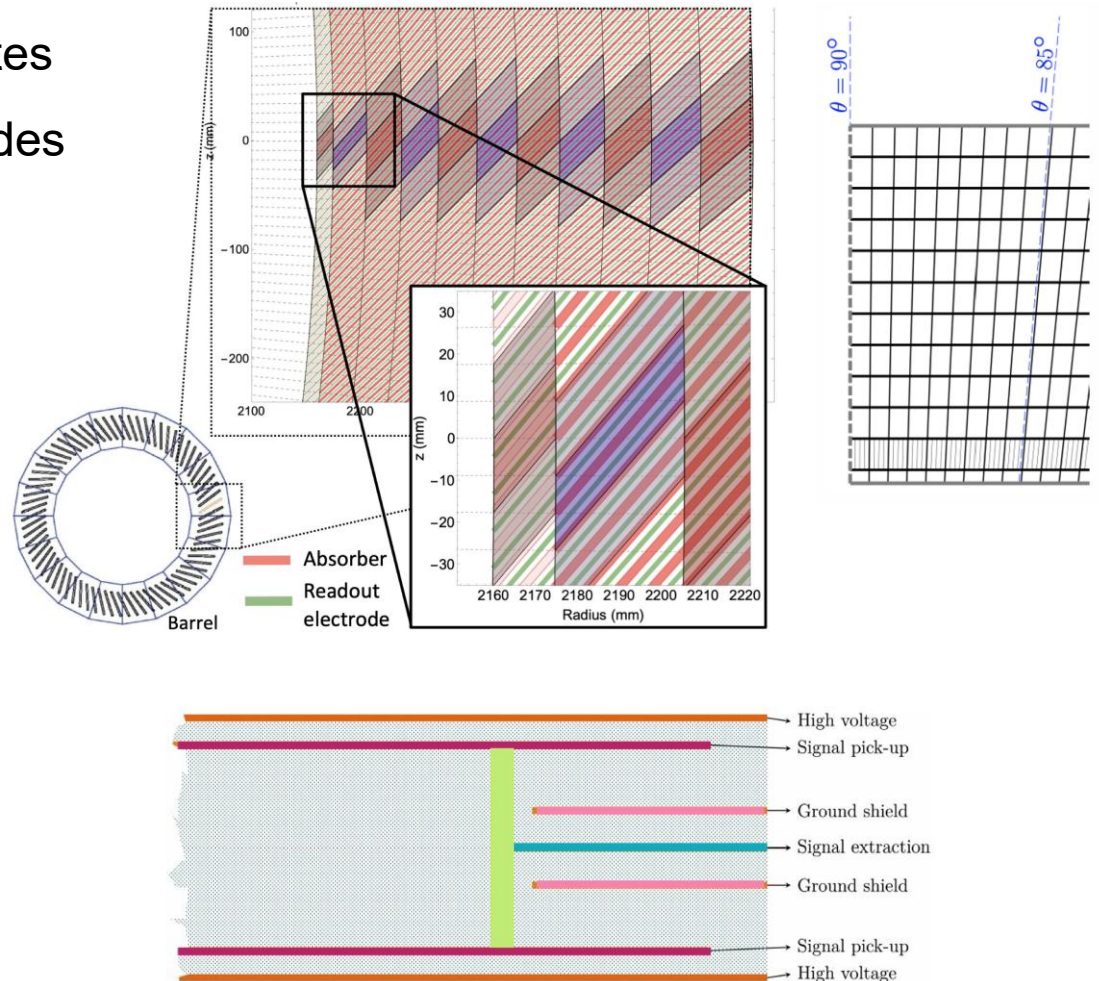


- Proven LAr technology
- Excellent energy resolution
- Limited granularity is not optimal for Particle Flow

× 10 finer readout granularity
than ATLAS ECAL

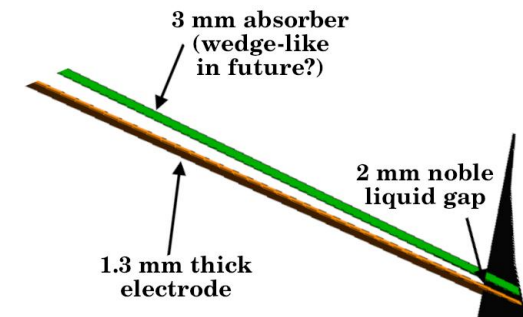
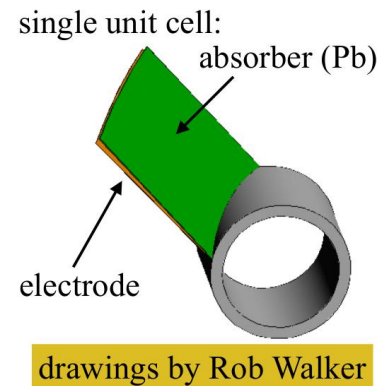
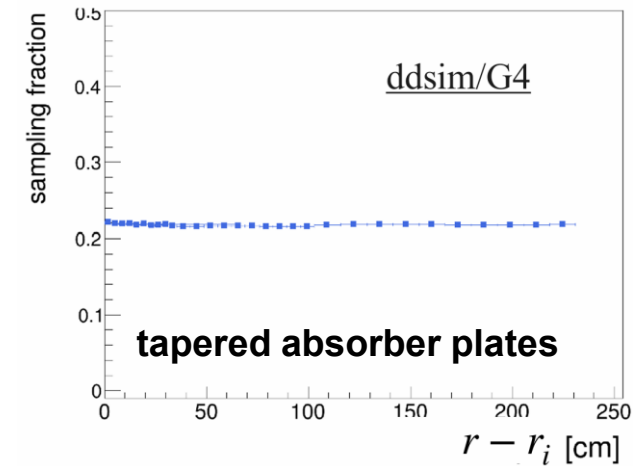
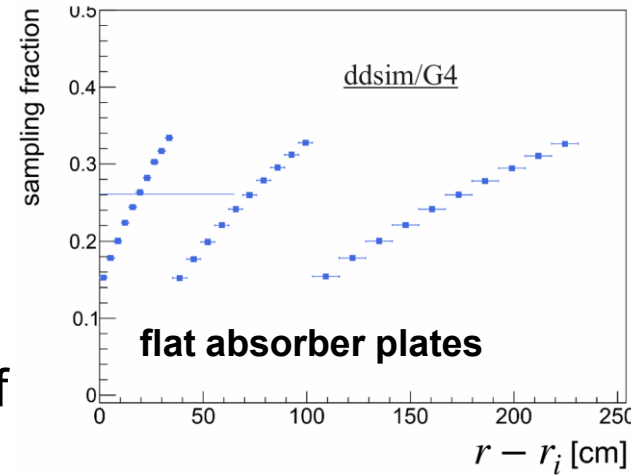
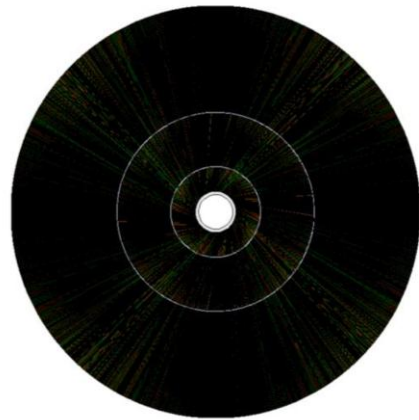
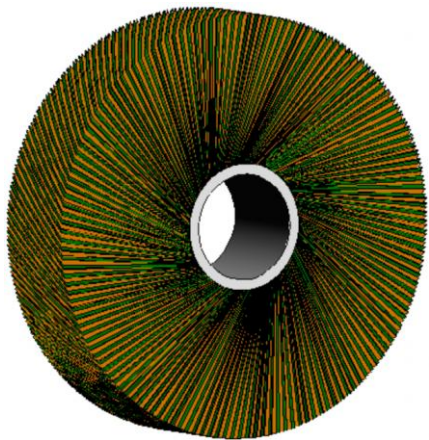
ALLEGRO ECAL Barrel

- 1536 straight inclined(50°) 1.8 mm absorber plates
- Segmented multi-layer PCBs as readout electrodes
- 1.2-2.4 mm noble liquid gaps
- 40cm deep(22 X0)
- Segmentation:
 - $\Delta\theta = 10(2.5)$ mrad in regular(strip) layer
 - $\Delta\phi = 8$ mrad
 - 11 longitudinal layers
- Material choices:
 - Baseline : LAr, Pb absorbers
 - LKr and W absorbers under investigation



ECAL Endcap

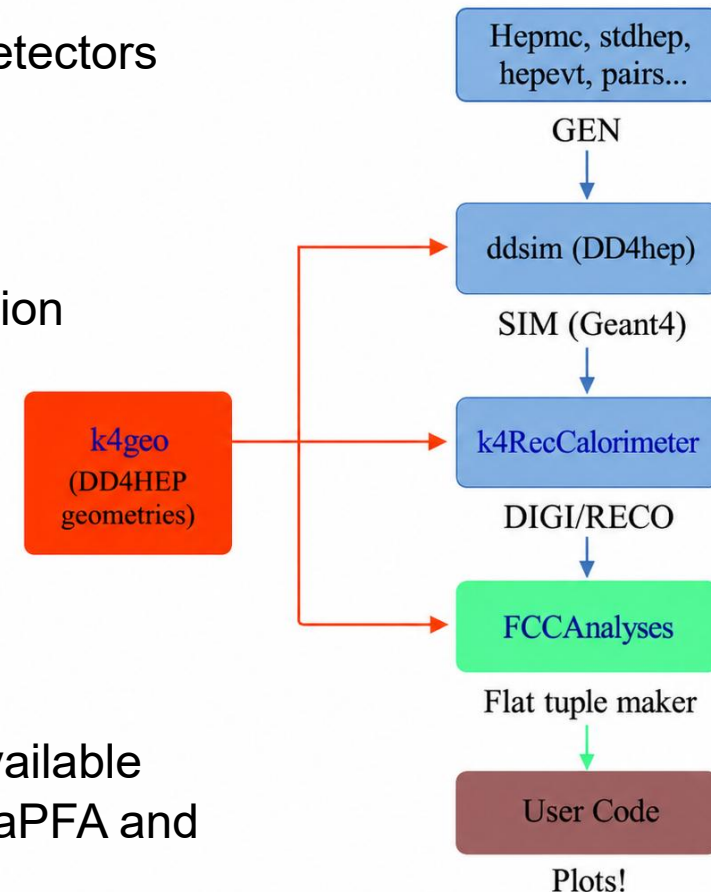
- Similar concept to the barrel
- Turbine-like structure with azimuthally repeated absorber plates
- $420 \text{ mm} < R < 2750 \text{ mm}$
- 3 nested wheels to mitigate the variation of gaps with radius
- Flat absorber plates / tapered (variable thickness) absorbers (being investigated)



Simulation Tools

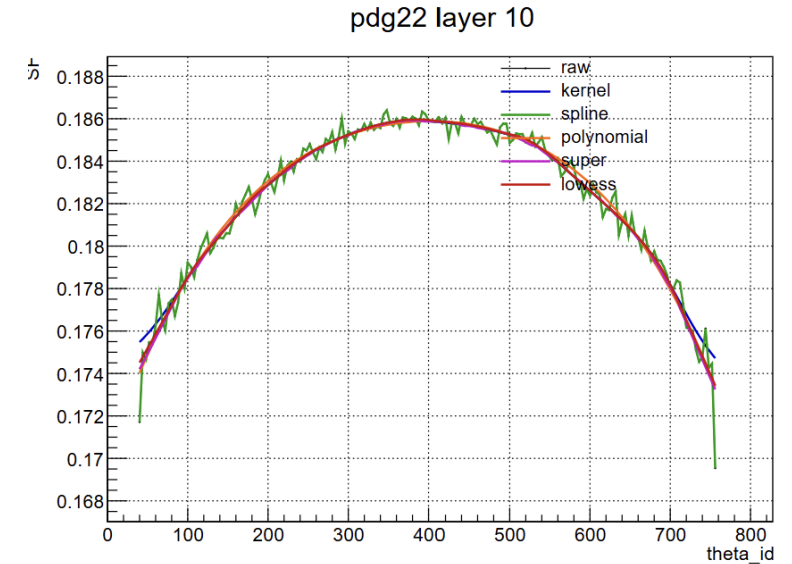
- ALLEGRO simulation is fully integrated in the Key4hep framework
 - Modular approach, ability to simulate with other sub-detectors
- Geometry described with DD4hep / k4geo
 - Detector structure defined in C++
 - Configurable parameters read from XML files
 - Convenient for geometry scans and detector optimization
- Digitization:
 - Electronic noise and cross-talk effects
 - Developments of detailed digitization ongoing
- Reconstruction includes:
 - Sliding window, topological clustering
 - π^0/γ separation
 - MVA-based energy calibration and theta correction available
 - Particle-flow object (PFO) reconstruction with PandoraPFA and ML-PFlow is under development

Simulation and reconstruction chain



Sampling Fraction of ECAL barrel

- Sampling fraction calibrates the active noble-liquid signal to the total energy deposited in the ECAL.
- Layer-dependent SF introduced to account for the depth-dependent sampling structure.
- For e/γ showers, a residual θ -dependent response observed after layer SF calibration.
- EM shower development and the θ -dependent non-uniformity of the projective barrel geometry induces θ dependence.
- Therefore, the layer SF is extended to a layer- θ SF for EM shower calibration.

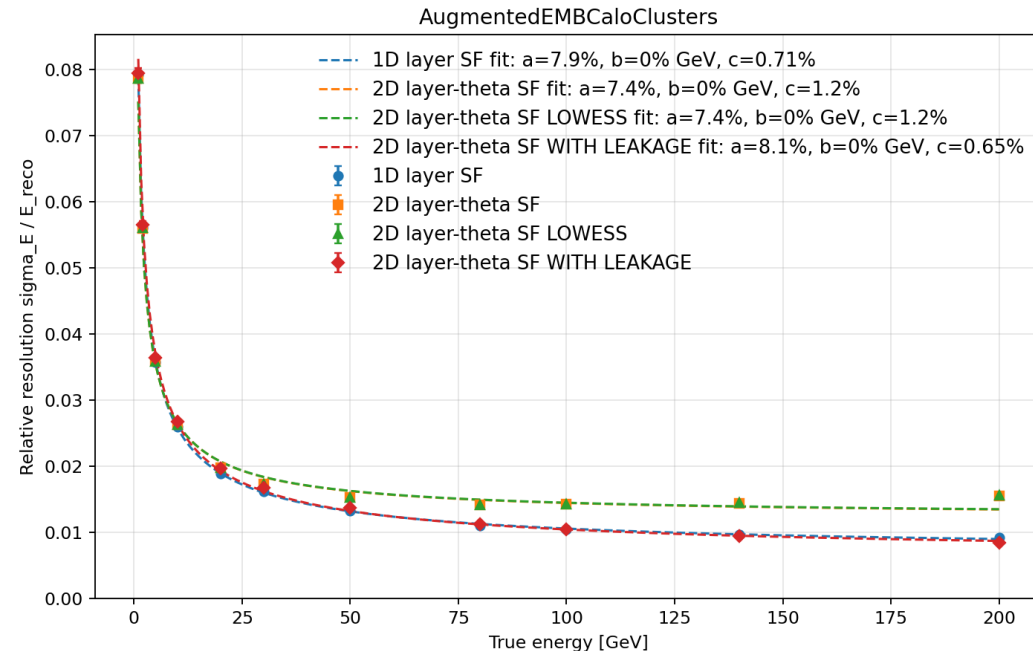
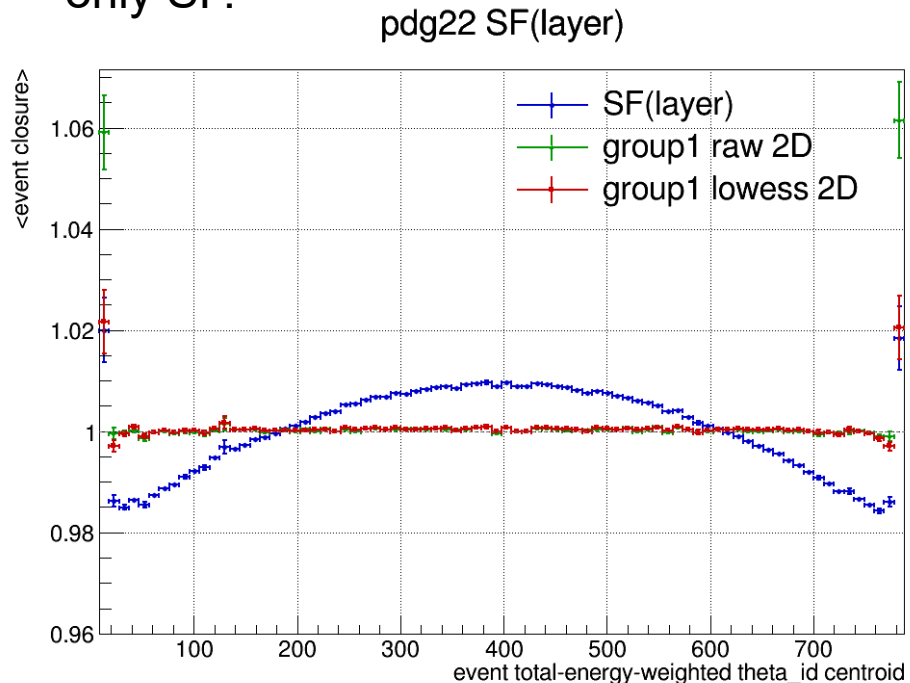


$$\text{SF}(\text{layer}_i) = \text{Gaussian mean of } \frac{E_{\text{active}}^i}{E_{\text{total}}^i}$$

$$\text{SF}(\text{layer}_i, \theta_j) = \frac{\langle E_{\text{active}}^{i,j} \rangle}{\langle E_{\text{total}}^{i,j} \rangle}$$

Validation of Sampling Fraction

- A layer- θ sampling fraction improves closure to the total energy deposited inside the ECAL.
- To recover the incident particle energy, θ -dependent leakage must also be considered; with this correction, a small improvement in energy resolution is observed compared with layer-only SF.



Energy Resolution of Single Particle

Sampling term(a):

- Depends on absorber thickness, active gap size, material
- Barrel: 8% with baseline option (Pb + LAr), ~5-6% achievable with Pb/W + LKr

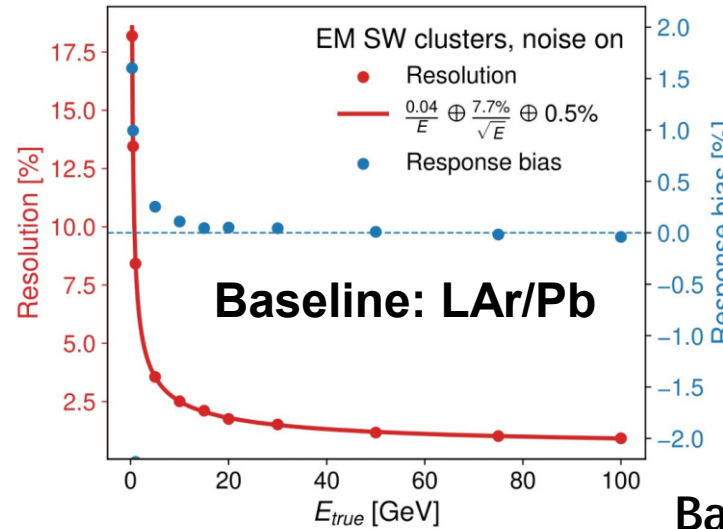
Noise term(b):

- Dominates the energy resolution at low energies(down to 200 MeV)
- Dominated by readout electronics and detector conditions, including capacitance (C_d), temperature (T), and peaking time (τ_p).

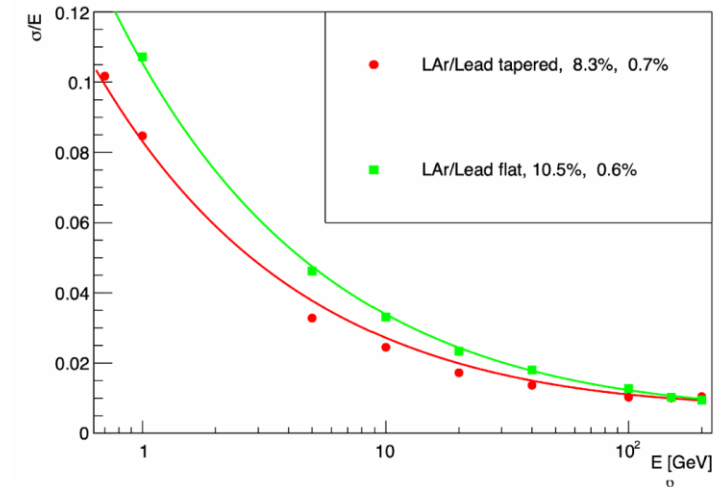
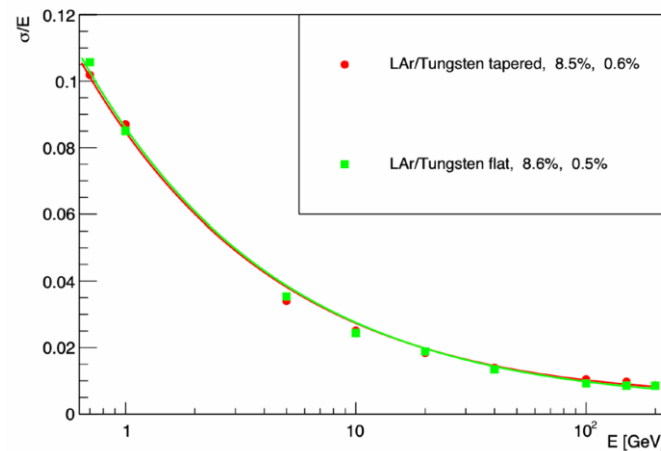
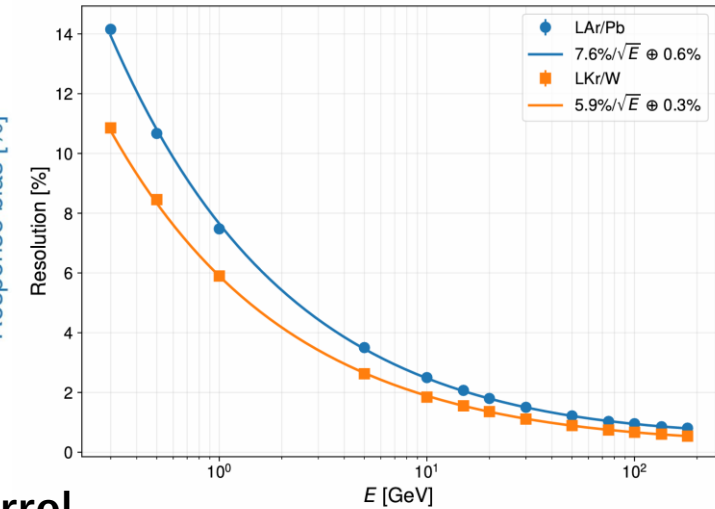
Constant term(c) :

- Upstream material, $\frac{\sigma_E}{E} = \frac{a}{\sqrt{E}} \oplus \frac{b}{E} \oplus c$
- Longitudinal leakage
- non-uniformity

$$\text{Noise} \sim C_d \sqrt{\frac{4kT}{g_m \tau_p}}$$



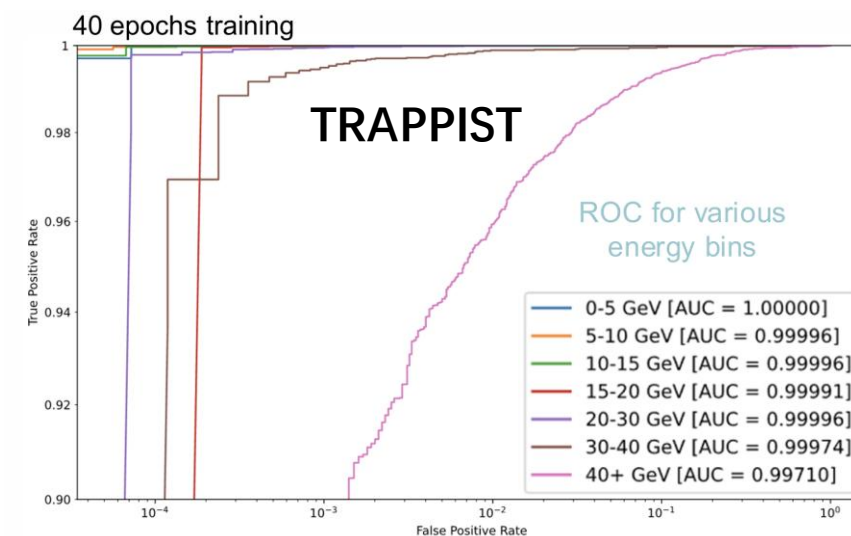
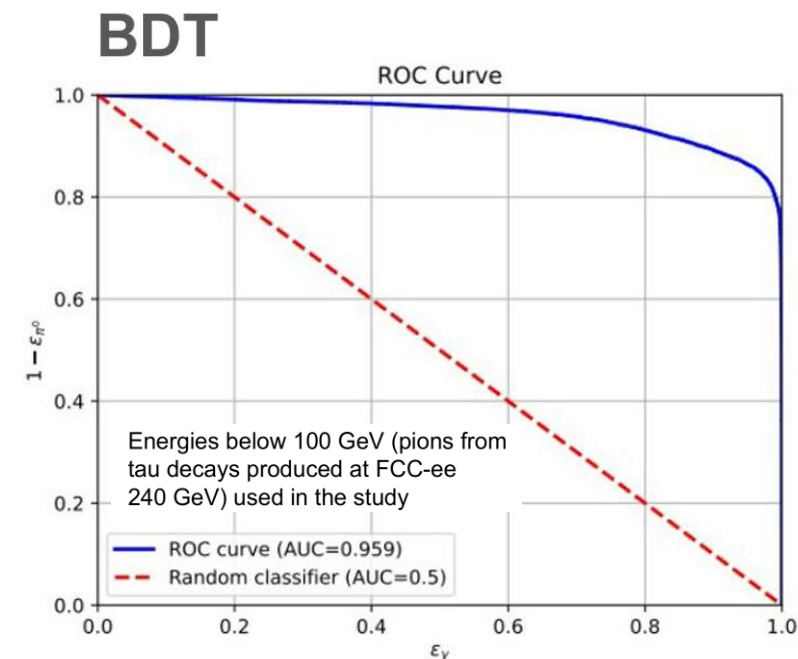
Barrel



Endcap

γ/π^0 Separation

- **Critical for**
 - Background rejection
 - Tau hadronic decay mode identification ($Z \rightarrow \text{tau tau}$, $H \rightarrow \text{tau tau}$)
 - Axion-Like Particles searches
- **BDT baseline**
 - Uses reconstructed cluster energy and shower-shape variables.
 - Targets unresolved π^0 showers after resolved π^0 reconstruction with invariant-mass-based cluster pairing.
 - Reference performance: AUC ≈ 0.959
 - Performance is excellent for single- π^0 identification, while multi- π^0 decay modes remain challenging because of merged showers and clustering ambiguities.
- **Transformer-based model TRAPPIST**
 - Uses calorimeter hit position and energy inside selected clusters.
 - Geometric Algebra Transformer: hits treated as graph nodes and encoded as geometric objects.
 - Photon ID eff. $>99.5\%$ with $<1\%$ mis-identification of π^0
- **Studies used for the optimization of the position of the strip layer**



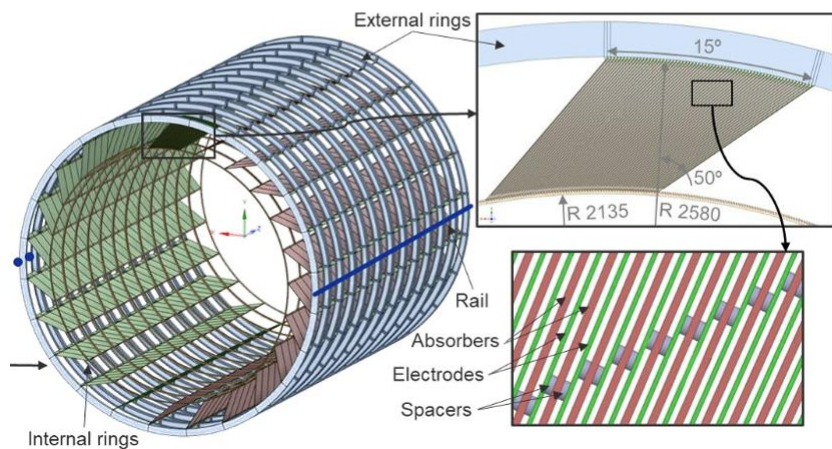
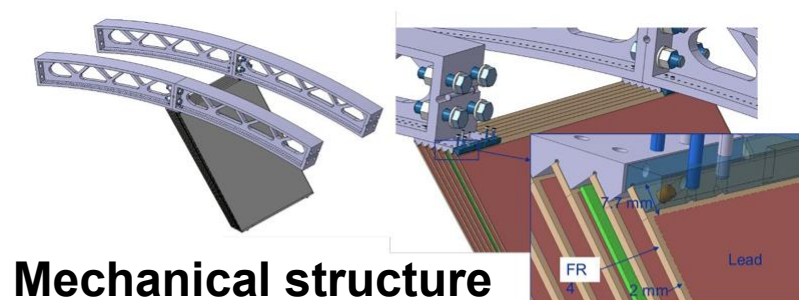
Summary

- Noble-liquid calorimetry is a mature and robust technology for future high-precision lepton-collider experiments.
- The ALLEGRO ECAL design combines proven LAr calorimeter performance with much finer granularity for FCC-ee physics requirements.
- The current simulation framework enables detailed studies of geometry, calibration and reconstruction performance.
- Single-particle energy resolution, γ/π^0 separation and particle-flow reconstruction provide key benchmarks for the ECAL design.
- Calibration studies, such as fine sampling-fraction and leakage corrections, are part of the ongoing effort to validate and optimize the detector response.

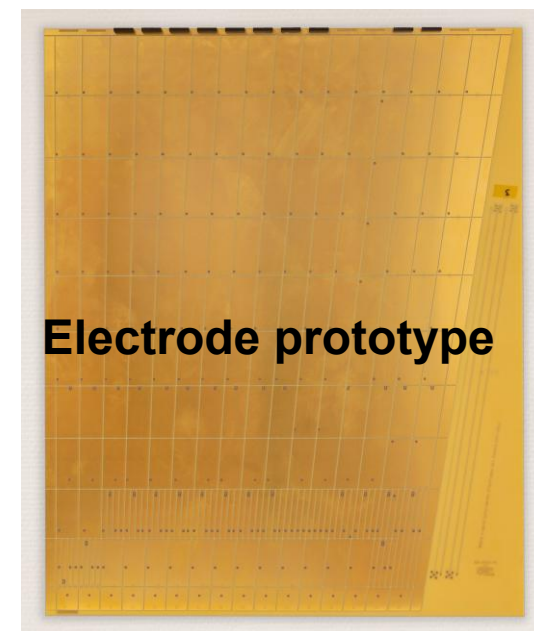
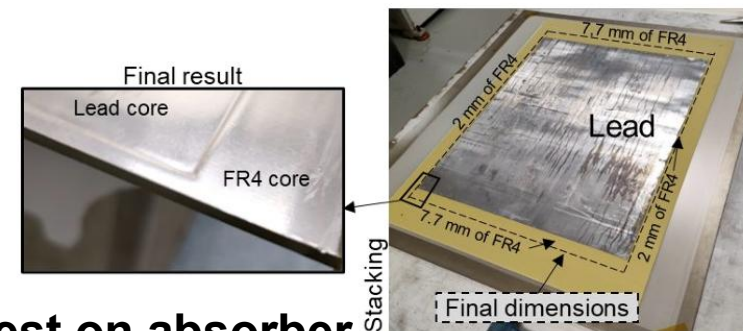
backup

Hardware R&D

Not a complete overview!



Electrical bench test



Electrode prototype