



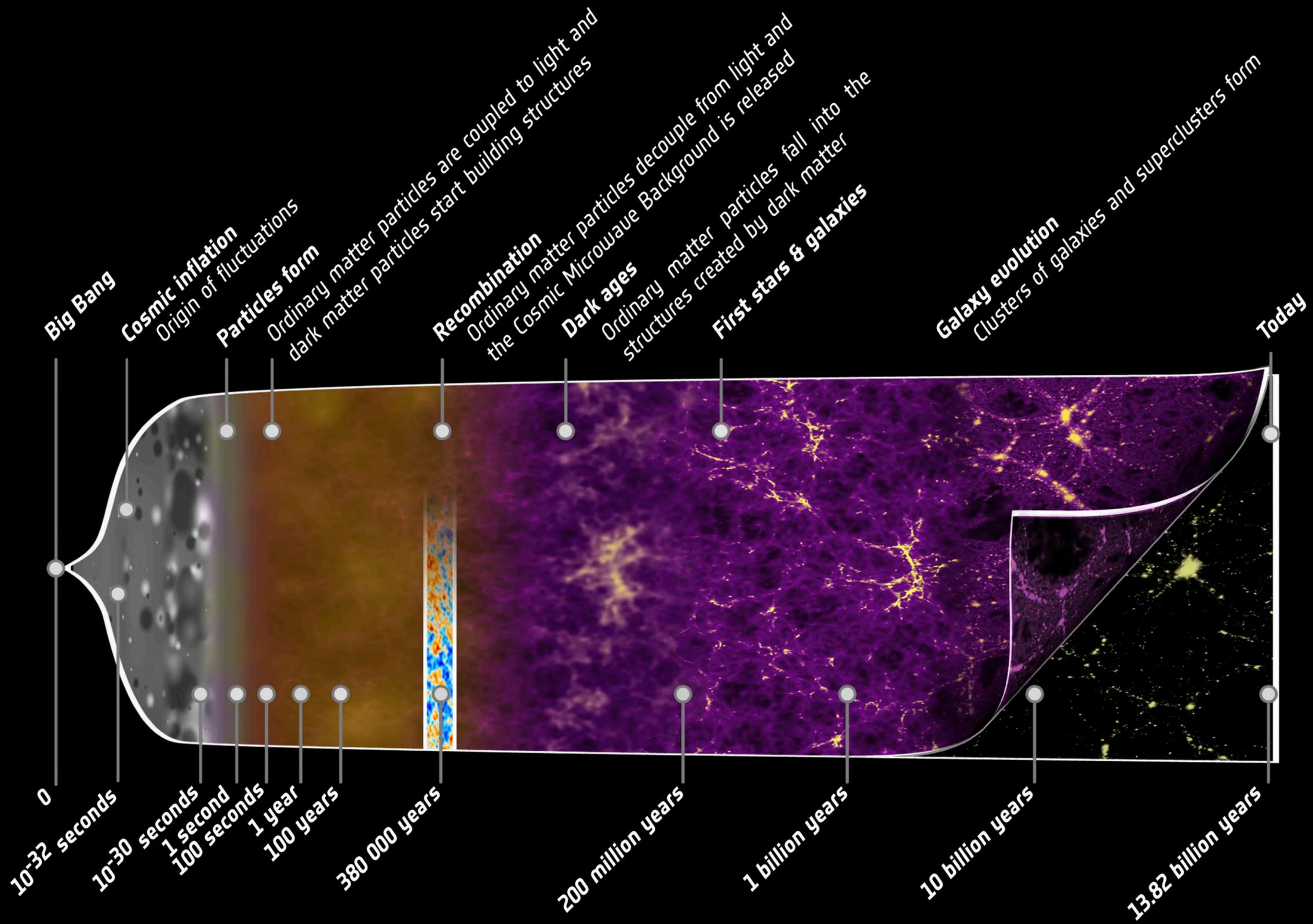
# Primordial lepton asymmetries: new constraints and consequences for sterile neutrino dark matter

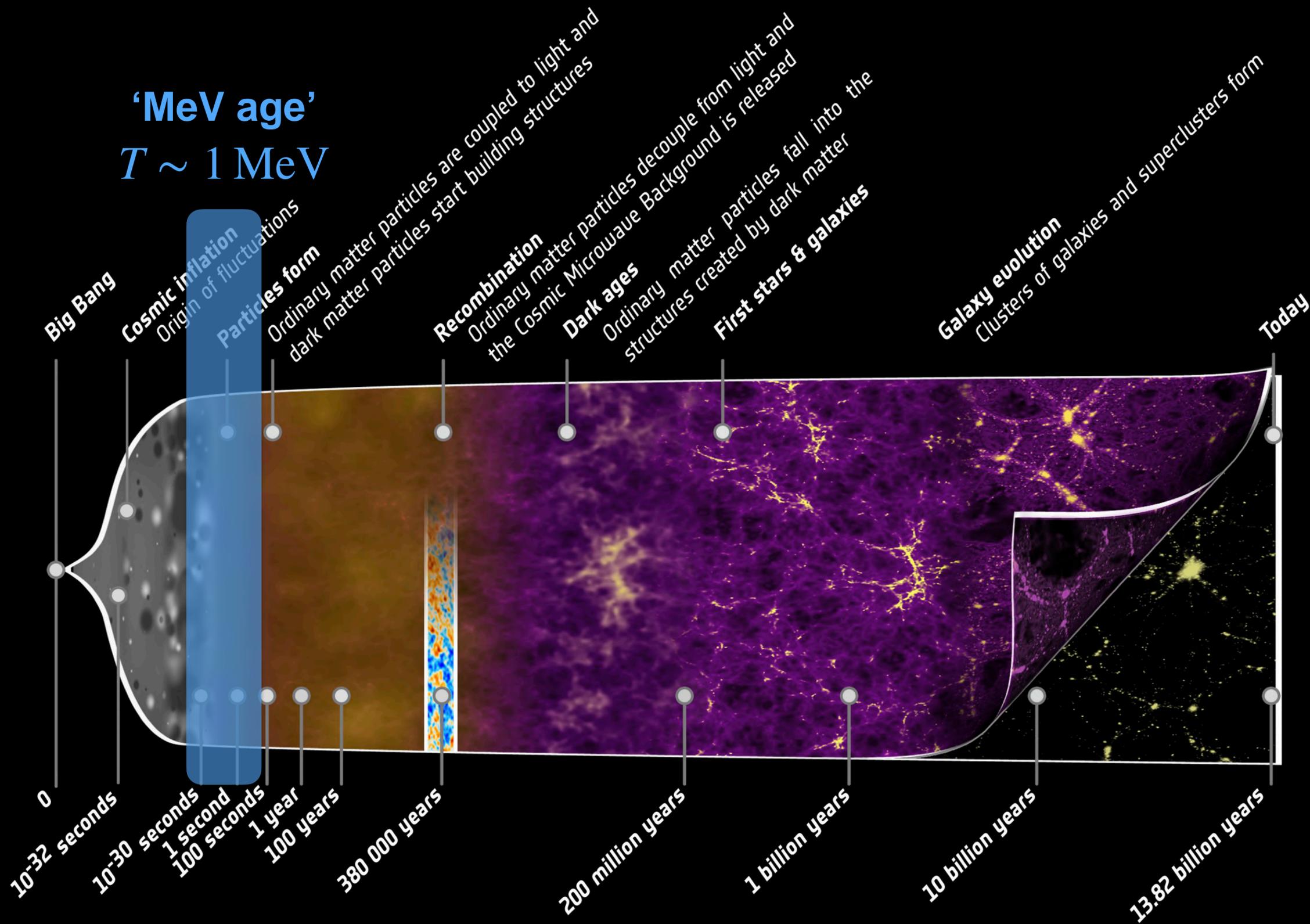
**Julien Froustey**

*Severo Ochoa Postdoctoral Fellow,  
IFIC, Valencia*

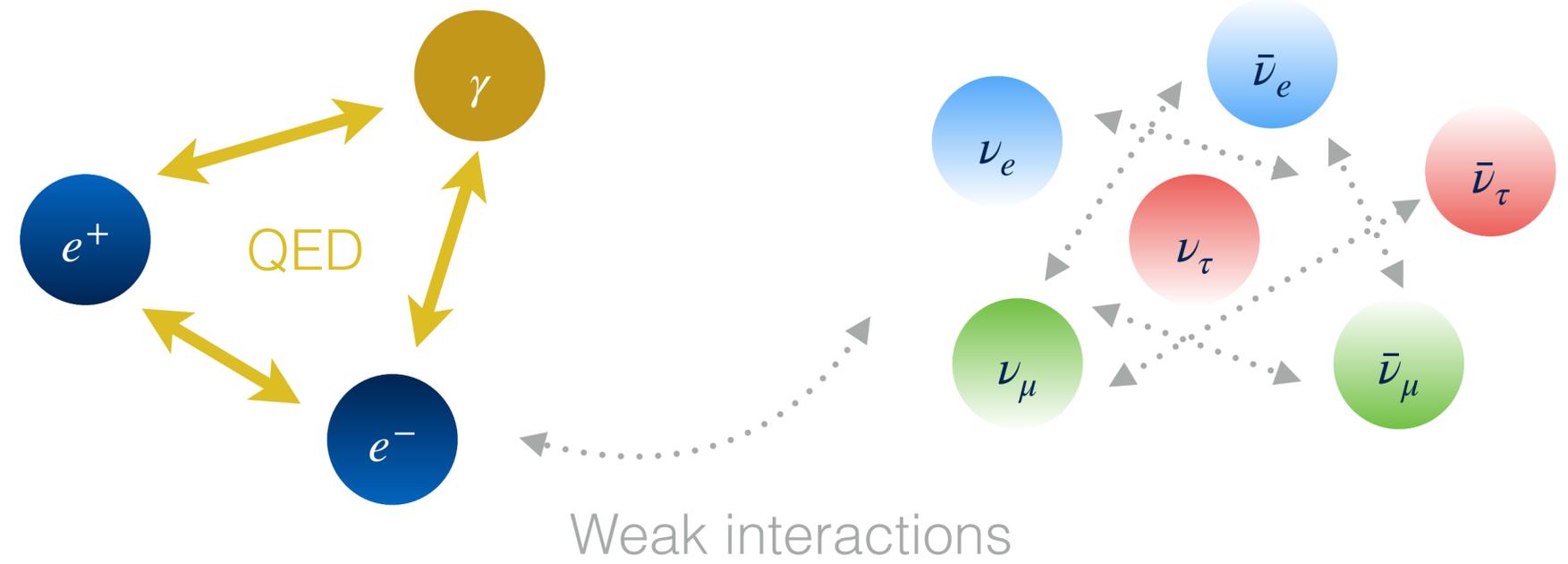
**Rencontres de Physique  
des Particules**

11/03/2026





# Neutrinos in the MeV age

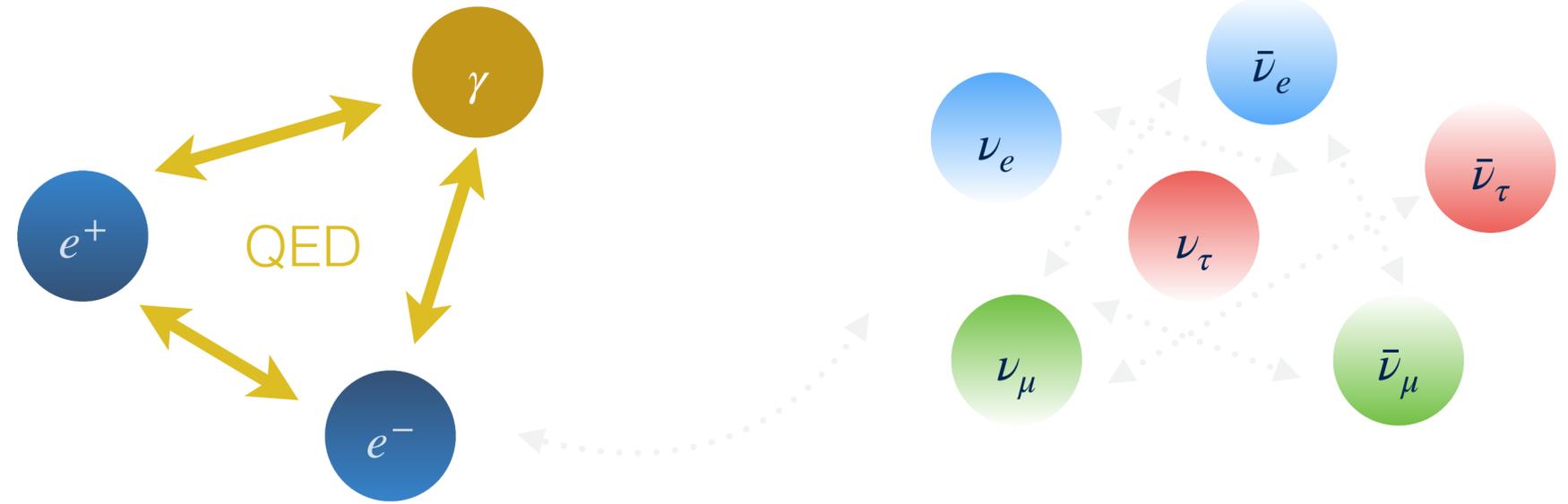


# Neutrinos in the MeV age

## NEUTRINO DECOUPLING

$$\frac{\text{collision rate}}{\text{expansion rate}} \quad \frac{\Gamma}{H} \simeq \frac{G_F^2 T^5}{\sqrt{g_*} T^2 / M_{\text{Pl}}}$$

$$\Gamma/H = 1 \iff T_{\text{dec}} \simeq 1 \text{ MeV}$$

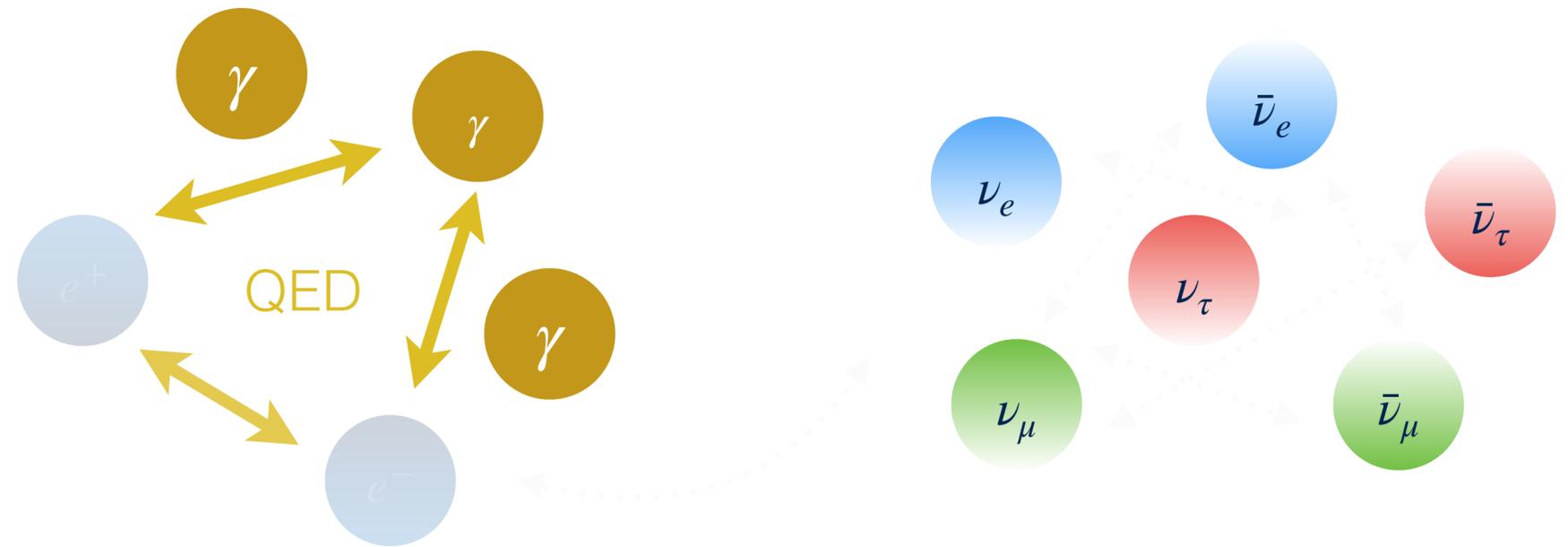


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## ELECTRON-POSITRON ANNIHILATIONS

→ entropy release

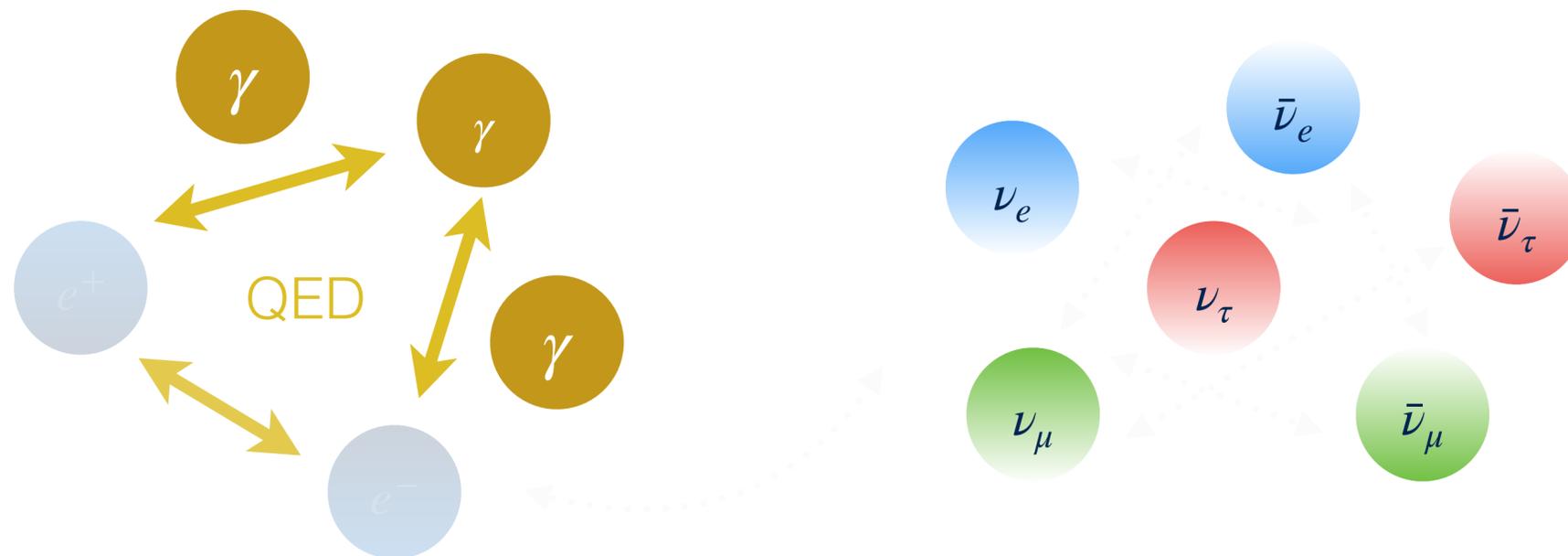
$$T_{e^\pm} = 0.511 \text{ MeV}$$

# Neutrinos in the MeV age

## NEUTRINO DECOUPLING

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$$\Gamma/H = 1 \longleftrightarrow T_{\text{dec}} \simeq 1 \text{ MeV}$$



## NEUTRINO OSCILLATIONS

$$\Omega_{\text{vac}} = \frac{\Delta m^2}{2E}$$

$$\Omega_{\text{matt}} = \frac{\sqrt{2}G_F}{m_W^2} E [\rho_{e^\pm} + P_{e^\pm}] = \frac{7\pi^2}{45} \frac{\sqrt{2}G_F}{m_W^2} E T^4$$

MSW transition for  $\Omega_{\text{vac}} = \Omega_{\text{matt}}$

$$T_{\text{MSW}} \in [12 \text{ MeV}, 2.8 \text{ MeV}]$$

## ELECTRON-POSITRON ANNIHILATIONS

→ entropy release

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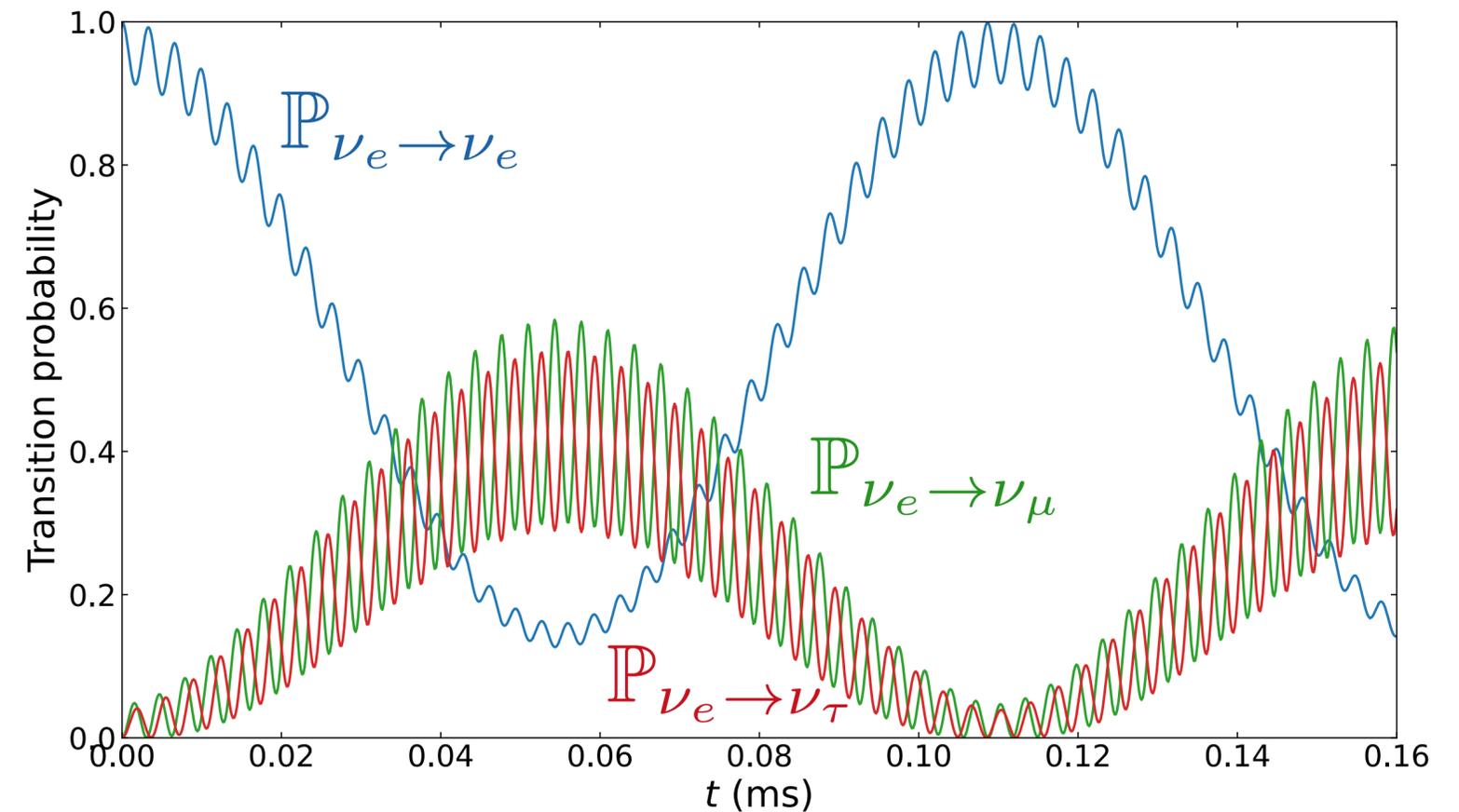
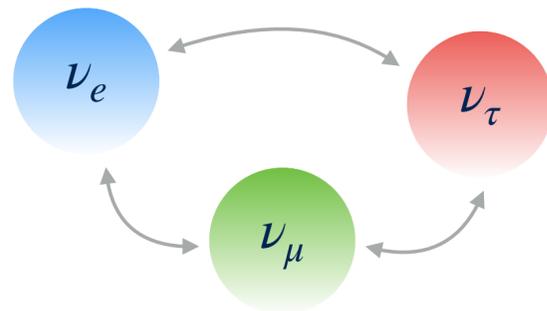
# Neutrino flavor oscillations

- Standard Model: 3 species of massless neutrinos  $\nu_L$
- Experimental evidence in the second half of the 20th century  
→ massive neutrinos

Flavor states  $\begin{pmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{pmatrix} = U \begin{pmatrix} \nu_1 \\ \nu_2 \\ \nu_3 \end{pmatrix} = \begin{pmatrix} U_{e1} & U_{e2} & U_{e3} \\ U_{\mu1} & U_{\mu2} & U_{\mu3} \\ U_{\tau1} & U_{\tau2} & U_{\tau3} \end{pmatrix} \begin{pmatrix} \nu_1 \\ \nu_2 \\ \nu_3 \end{pmatrix}$  Mass states

PMNS mixing matrix

⇒ neutrino oscillations



# Neutrino flavor oscillations

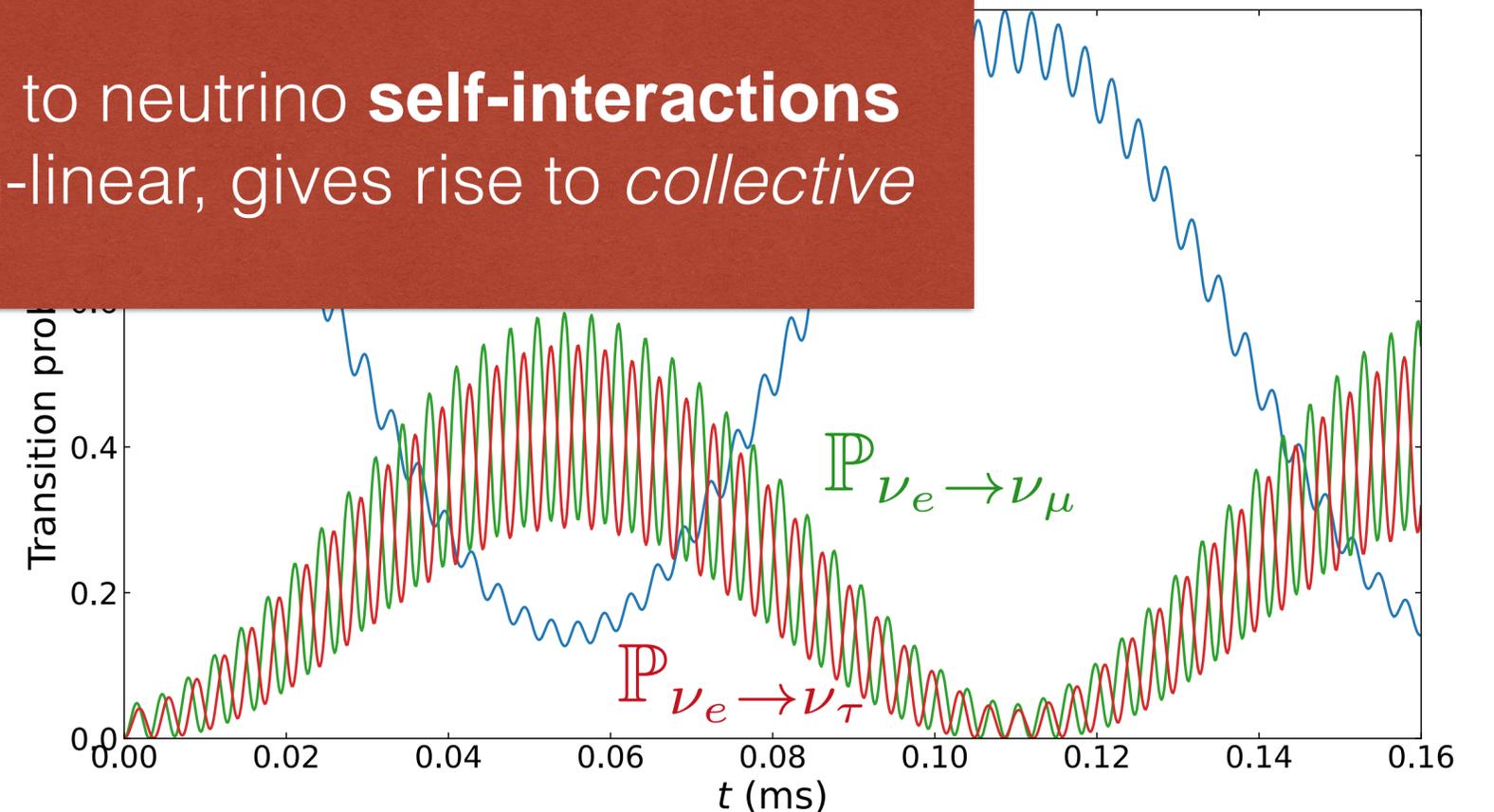
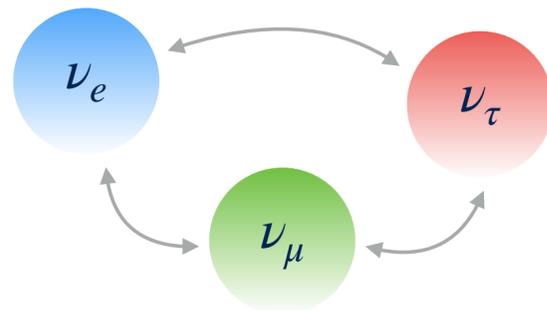
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→ massive neutrinos

Flavor states  $(\nu_e)$   $(\nu_\mu)$   $(\nu_\tau)$   $(U_{e1} U_{e2} U_{e3})$   $(\nu_1)$   $(\nu_2)$   $(\nu_3)$  mass states

Additional complexity in dense environments:

- ▶ Mean-field potential due to **interactions with matter**
- ▶ Mean-field potential due to neutrino **self-interactions**  
(makes the problem non-linear, gives rise to *collective oscillations*)

⇒ neutrino oscillations



# Neutrino transport in the early Universe

$$\frac{\partial \varrho}{\partial t} - Hp \frac{\partial \varrho}{\partial p} = -i [\mathcal{H}_{\text{vac}} + \mathcal{H}_{\text{mat}} + \mathcal{H}_{\nu\nu, \varrho}] + \mathcal{C}$$

- Calculation of **standard neutrino decoupling**:  $N_{\text{eff}} = 3.044$

$$\rho_{\text{tot}} = \rho_{\gamma} + \rho_{\nu, \bar{\nu}} = \left[ 1 + N_{\text{eff}} \times \frac{7}{8} \left( \frac{4}{11} \right)^{4/3} \right] \rho_{\gamma}$$



JF, C. Pitrou, M.C. Volpe [[2008.01074](#)]  
J. Bennett *et al.* [[2012.02726](#)]



See G. Jackson's upcoming talk

# Neutrino transport in the early Universe

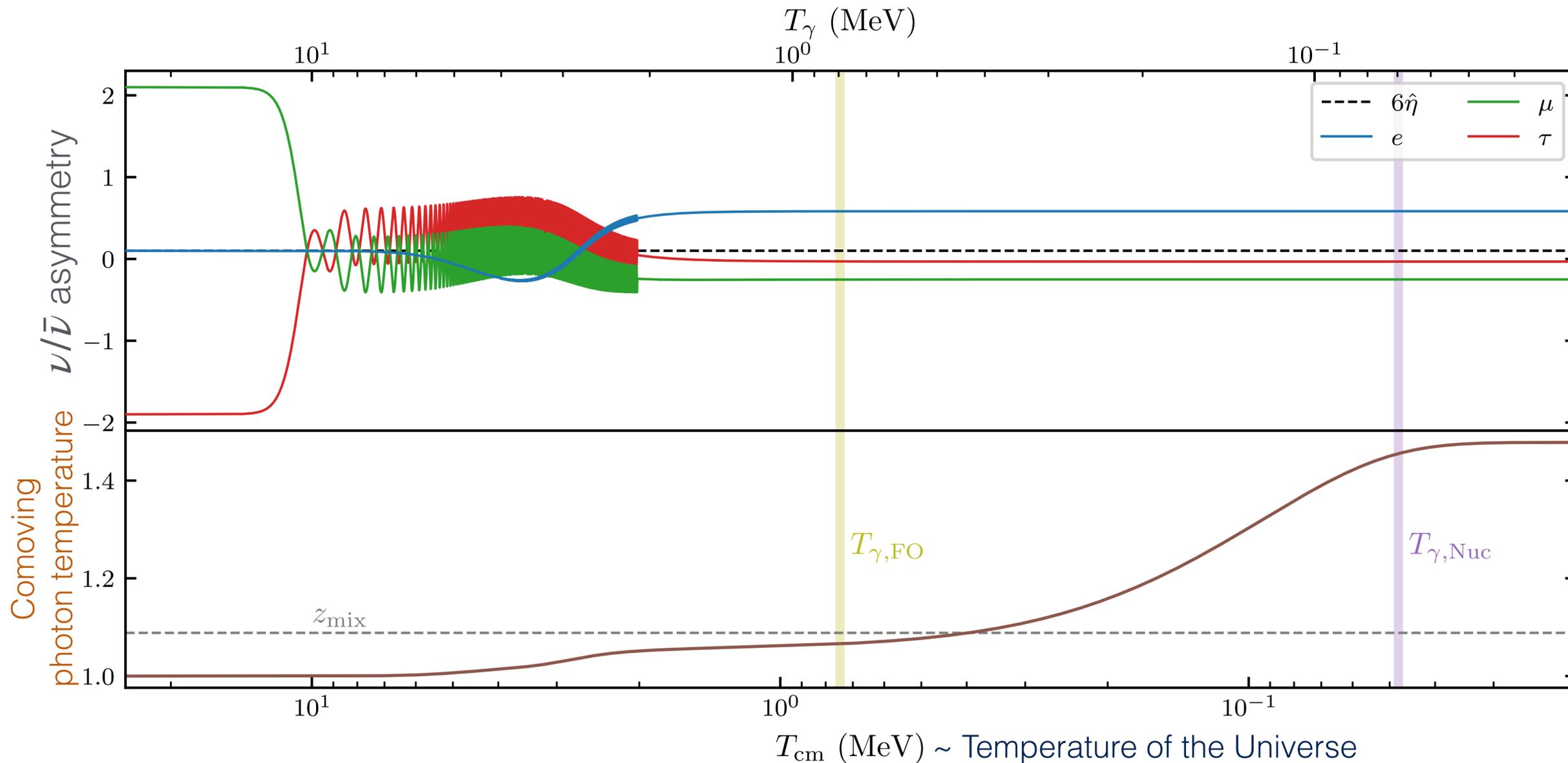
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JF, C. Pitrou, M.C. Volpe [2008.01074]  
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- Extension to the case of **nonzero neutrino/antineutrino asymmetries**



$$\eta_{\alpha} \equiv \frac{n_{\nu_{\alpha}} - n_{\bar{\nu}_{\alpha}}}{T^3}$$

Initial values

$$\eta_{\text{av}} = \eta_e = 0.1$$

$$\eta_{\mu} - \eta_{\tau} = 4$$



JF, C. Pitrou [2110.11889]  
JF, C. Pitrou [2405.06509]

# Neutrino transport in the early Universe

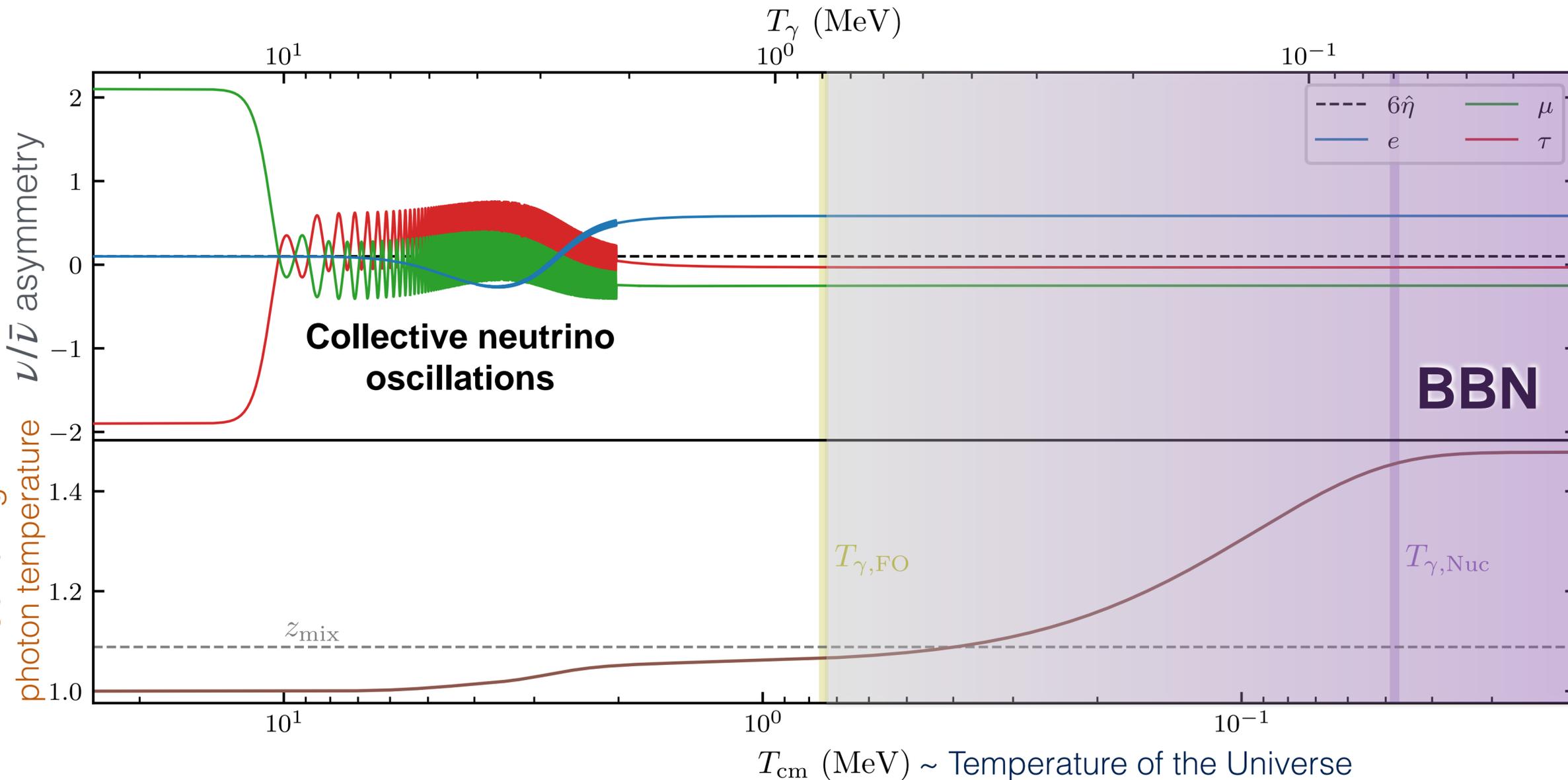
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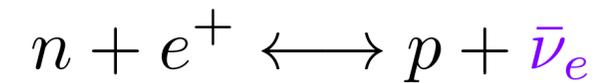
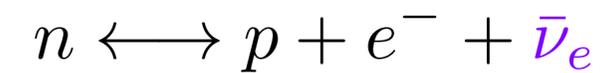
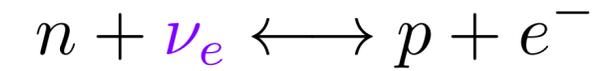
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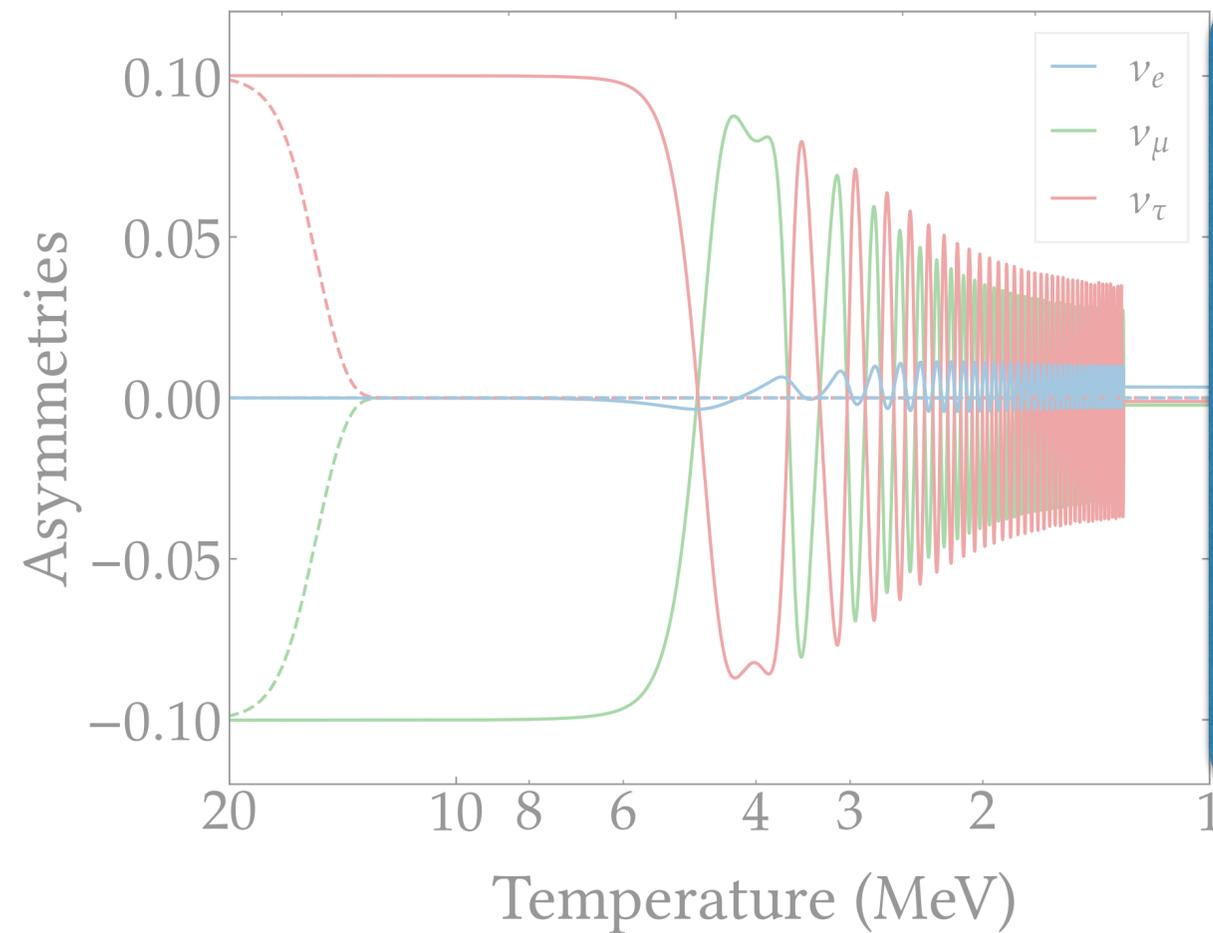
JF, C. Pitrou [2110.11889]  
JF, C. Pitrou [2405.06509]

# Constraining primordial neutrino asymmetries

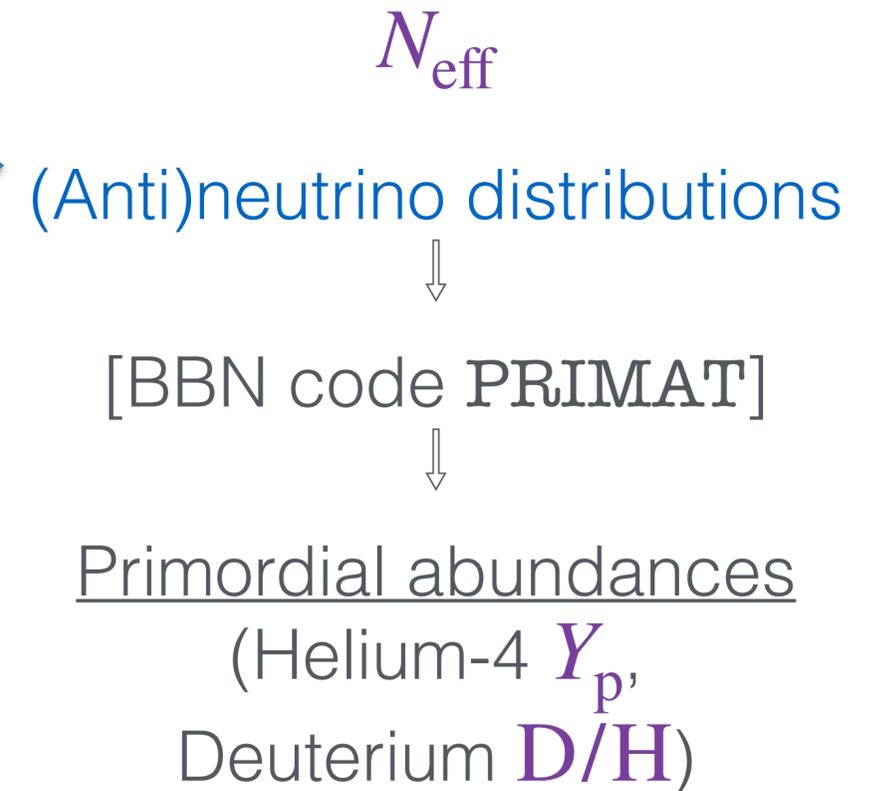
Effects of asymmetries:



$$\Delta N_{\text{eff}} \propto \sum_{\alpha=e,\mu,\tau} \eta_{\alpha}^2$$



**Asymmetries at the BBN epoch**



# Constraining primordial neutrino asymmetries

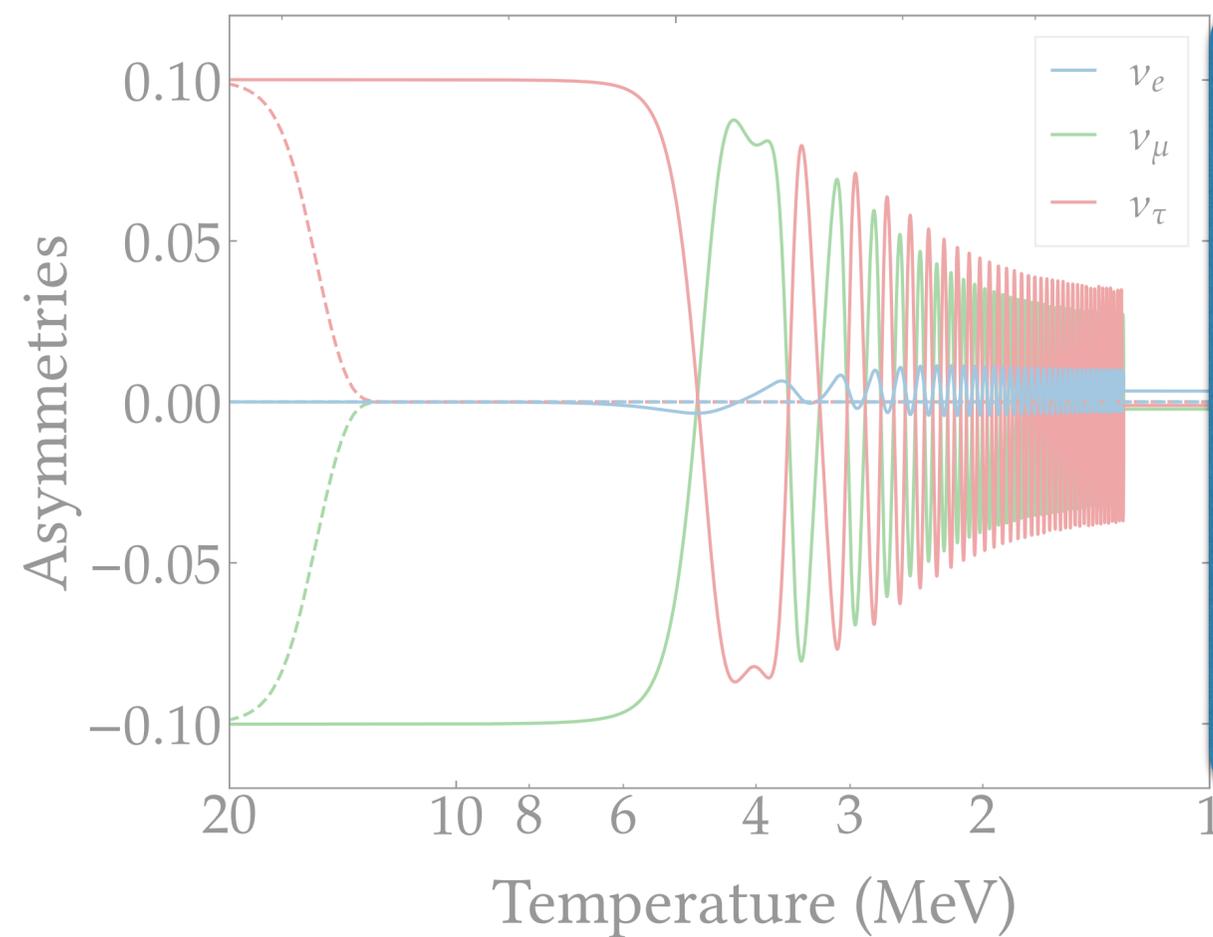
Oldengott & Schwarz [1706.01705],

Burns *et al.* [2206.00693],

Escudero *et al.* [2208.03201],

...

$$\eta_e^{\text{BBN}} = 0.0024 \pm 0.0030$$



Asymmetries at  
the BBN epoch



$N_{\text{eff}}$

(Anti)neutrino distributions



[BBN code PRIMAT]



Primordial abundances

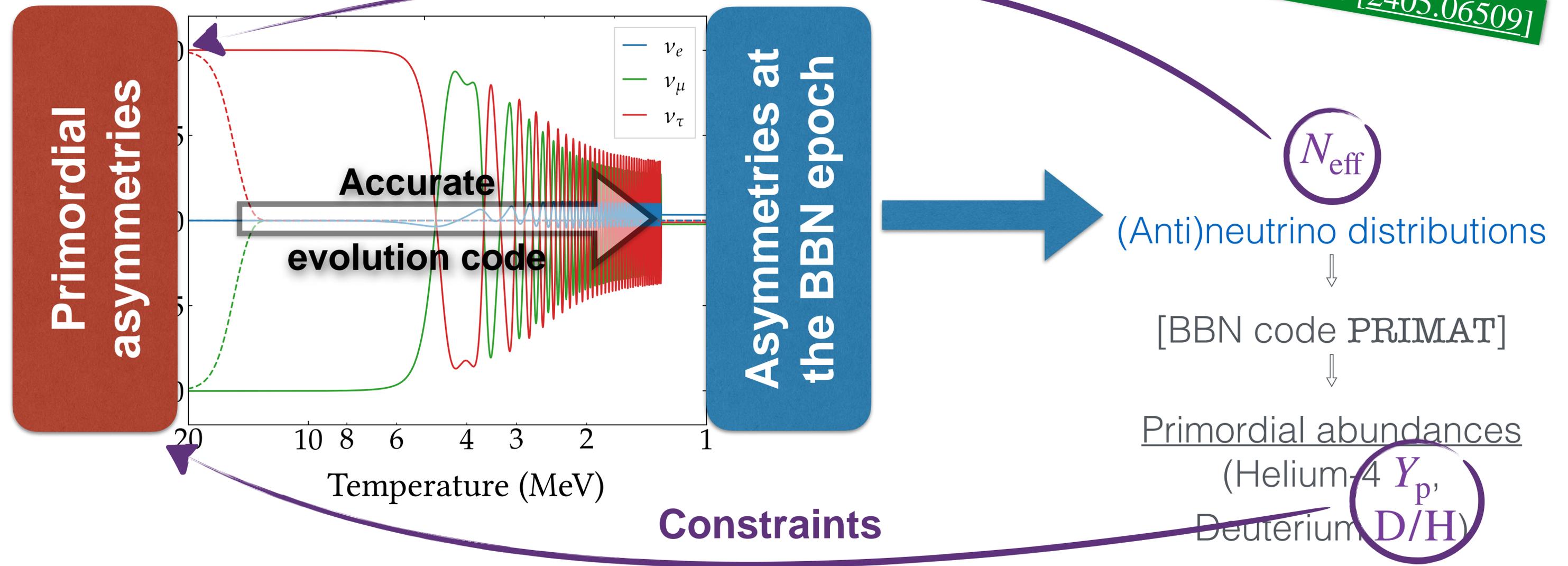
(Helium-4  $Y_p$ ,

Deuterium  $D/H$ )

Constraints

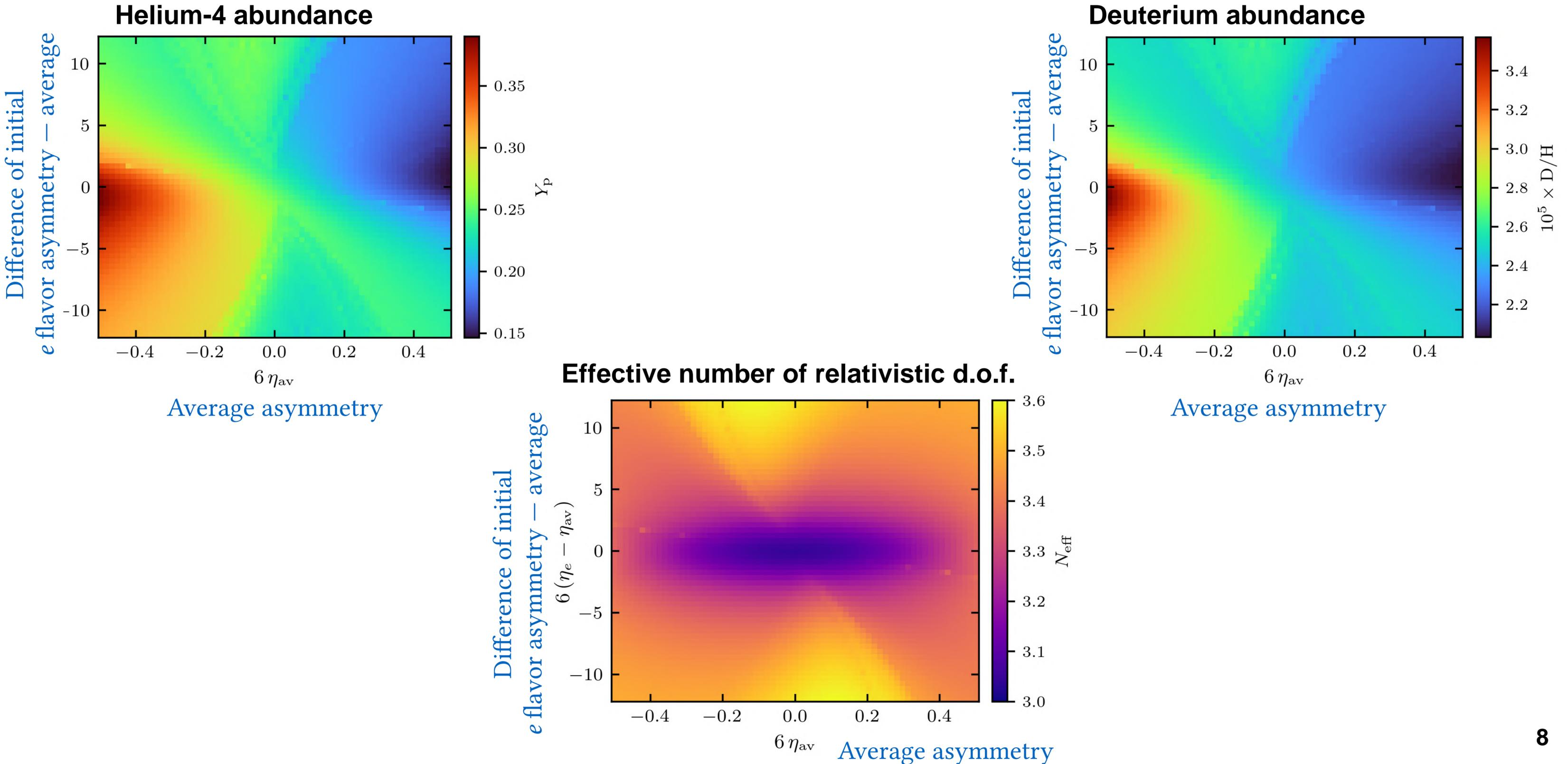
# Constraining primordial neutrino asymmetries

JF, C. Pitrou [2405.06509]



# Output of neutrino + BBN calculation

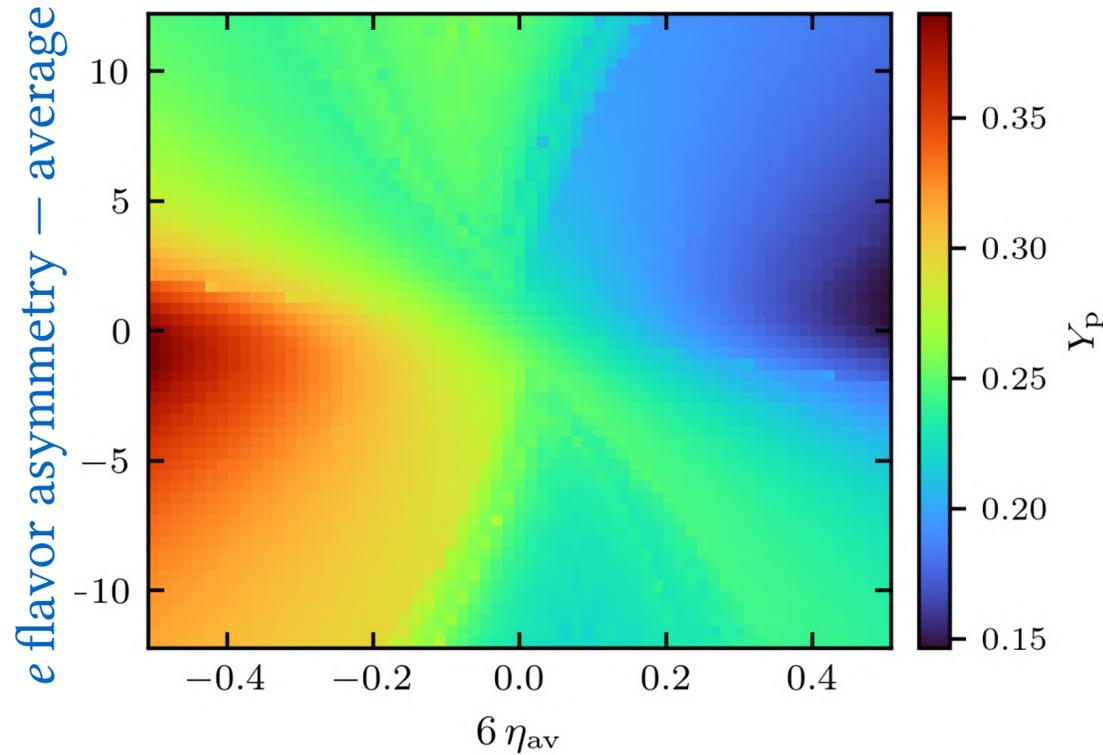
$$\eta_\mu = \eta_\tau$$



# Output of neutrino + BBN calculation

$$\eta_\mu = \eta_\tau$$

Helium-4 abundance



Spectroscopic measurements

$$Y_p = 0.2453 \pm 0.0034$$

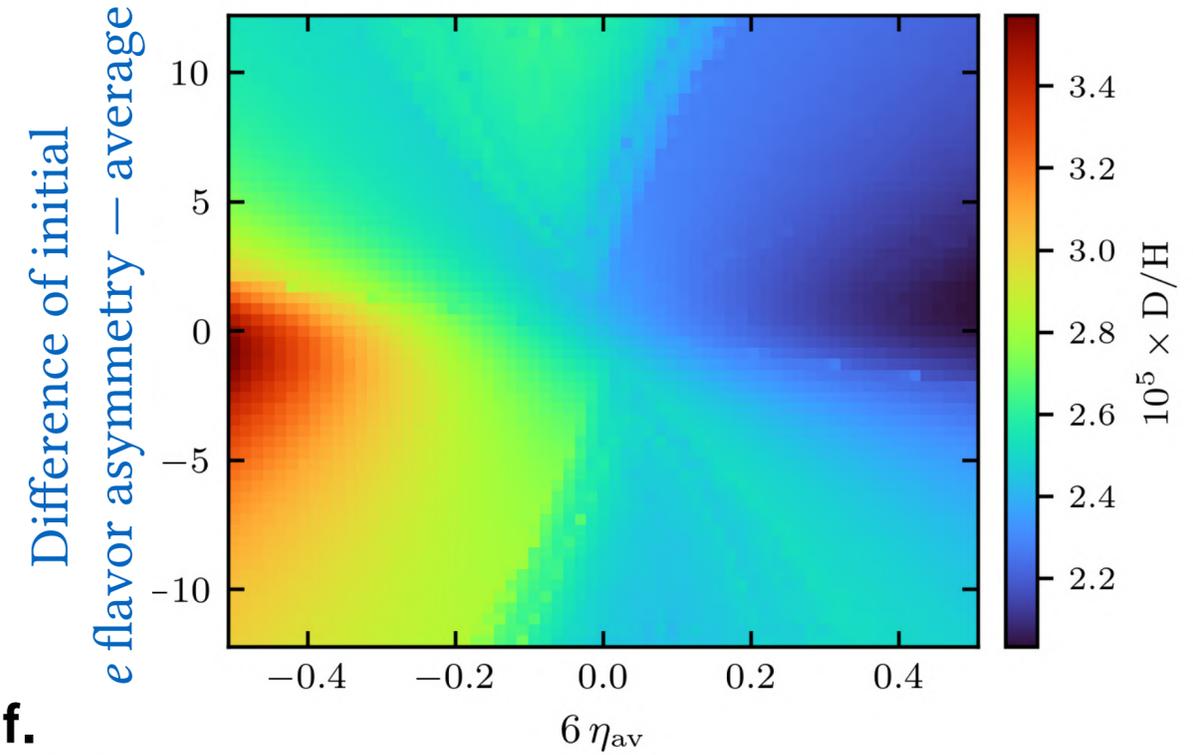
$$D/H = (2.53 \pm 0.03) \times 10^{-5}$$

*Aver et al.* [2010.04180]

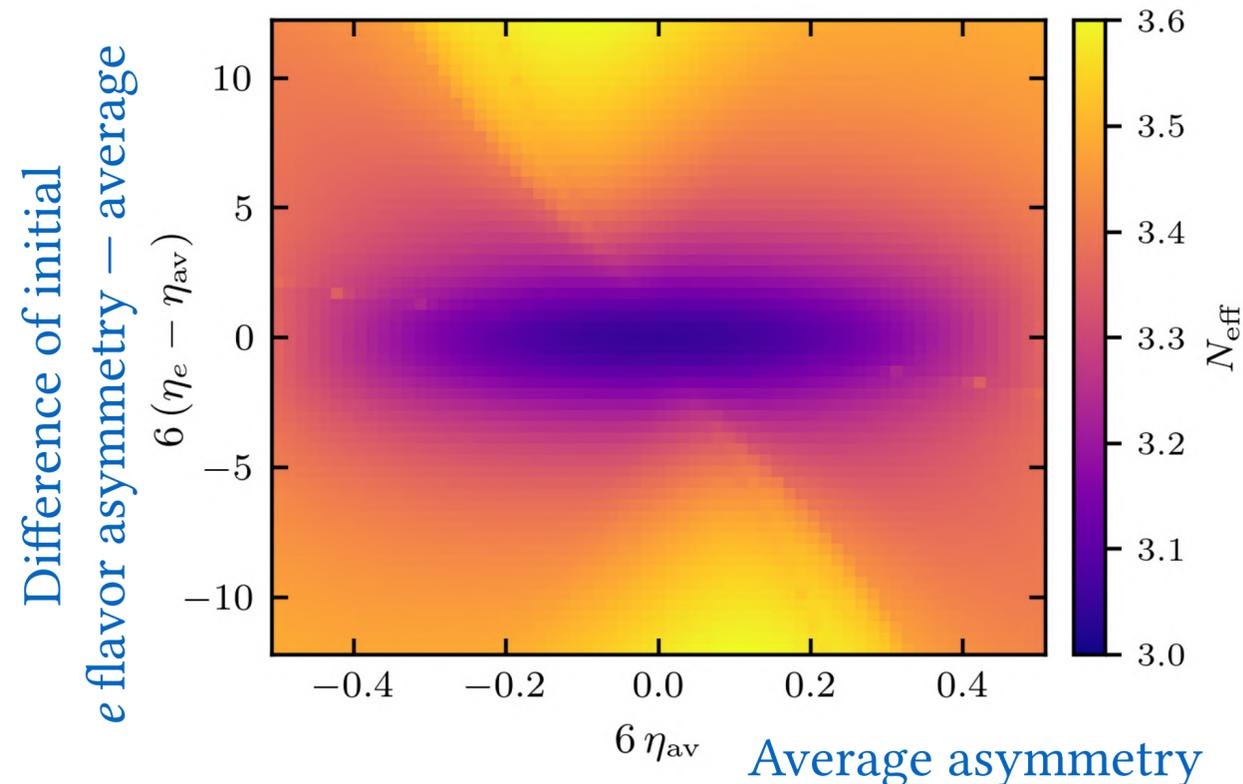
*Cooke et al.* [1710.11129]

*Kislitsyn et al.* [2401.12797]

Deuterium abundance



Effective number of relativistic d.o.f.



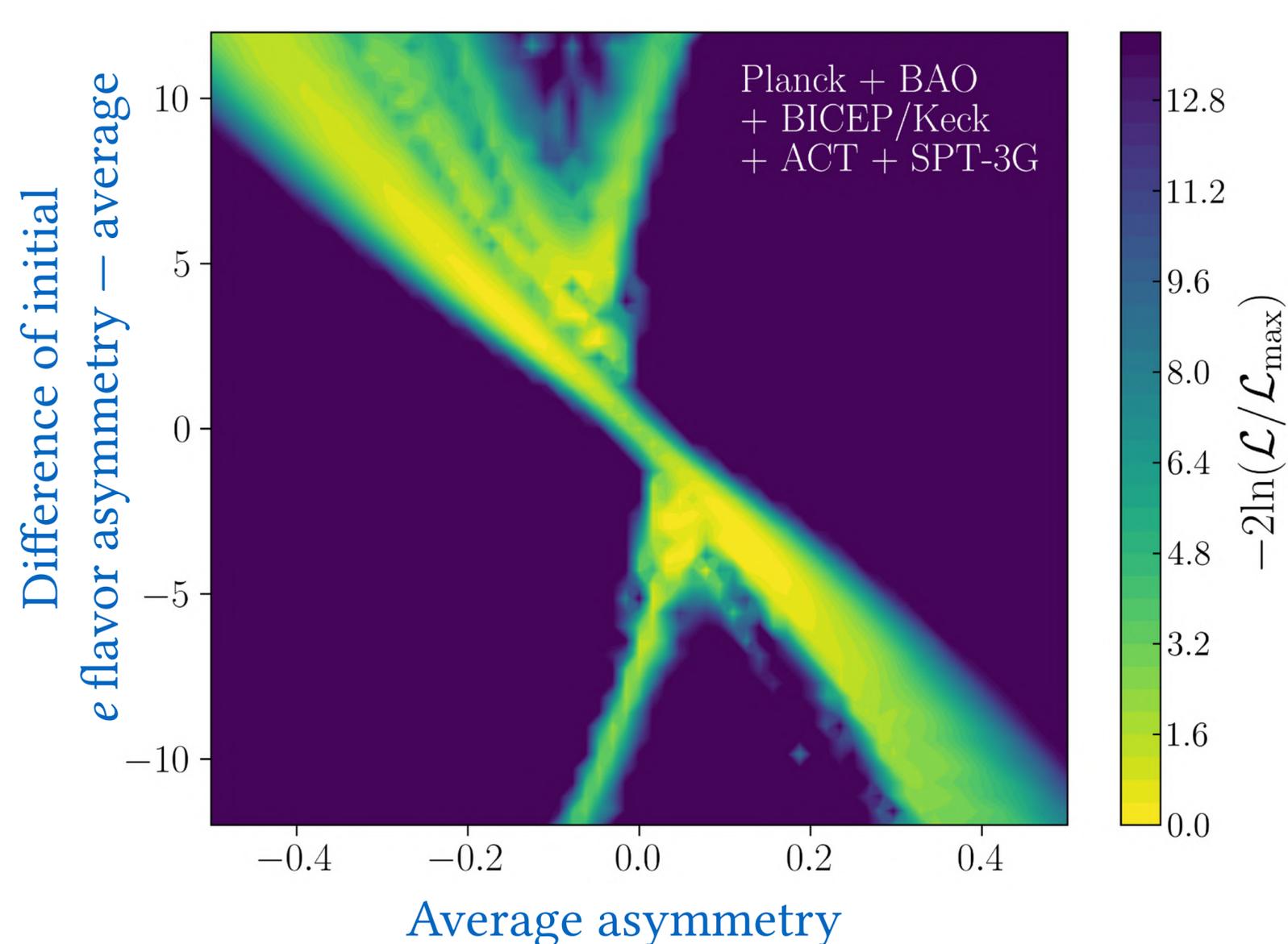
Average asymmetry

Planck + SPT + ACT+ BAO

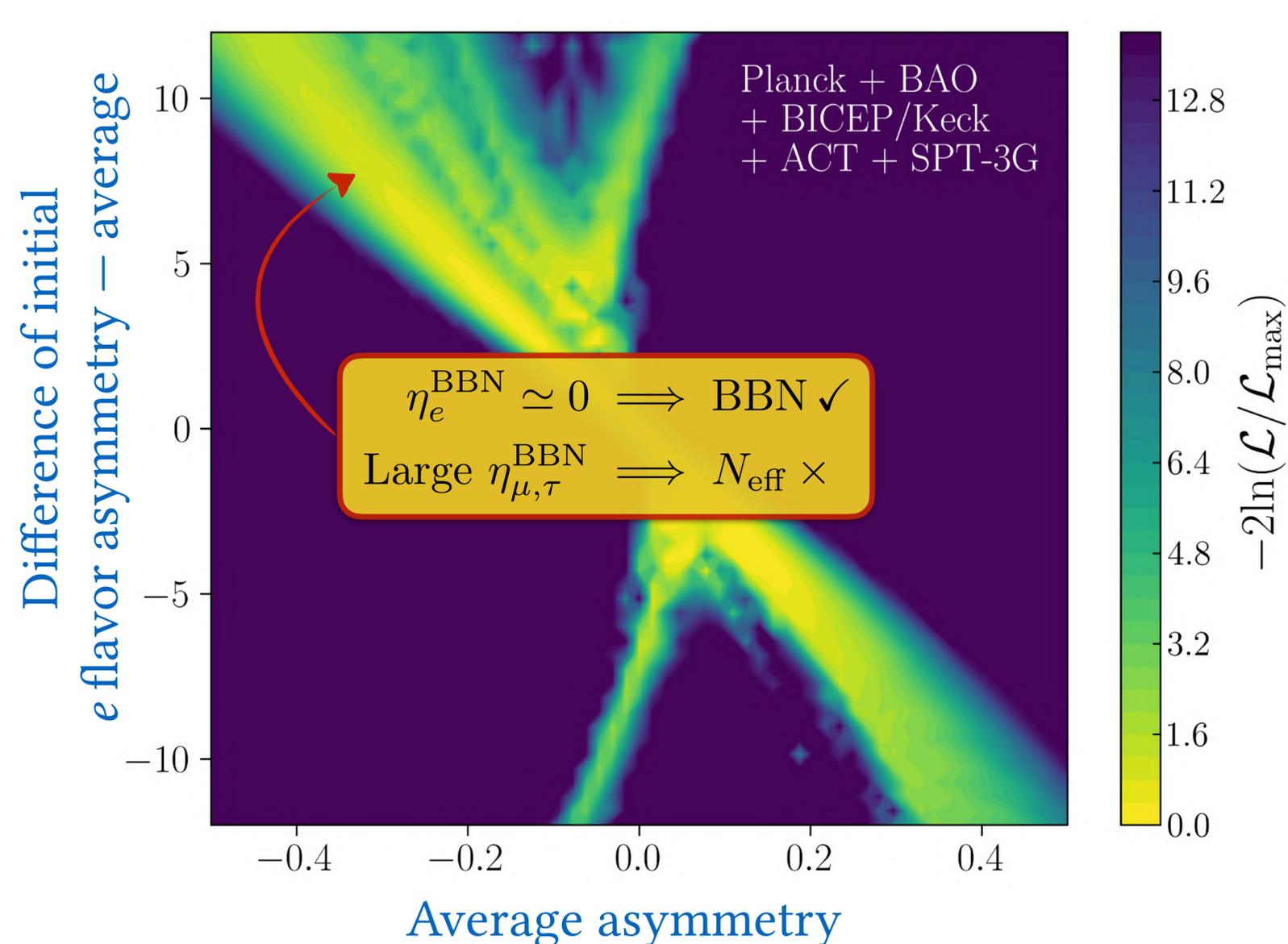
$$N_{\text{eff}} = 2.86 \pm 0.13 \quad (68\%)$$

[2411.06000]

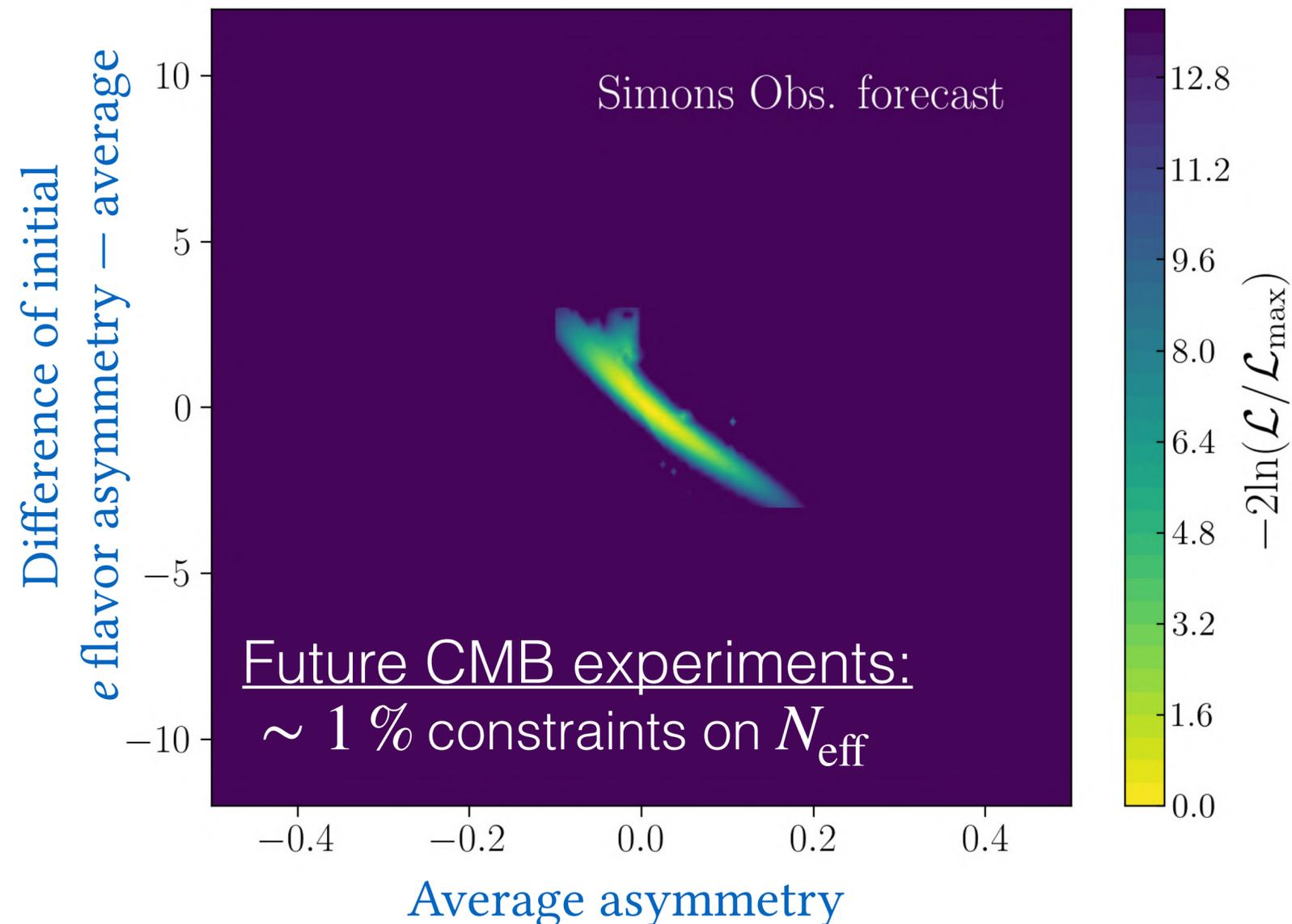
- **Large lepton asymmetries are allowed**, with a complicated landscape due to the dynamics of flavor oscillations.



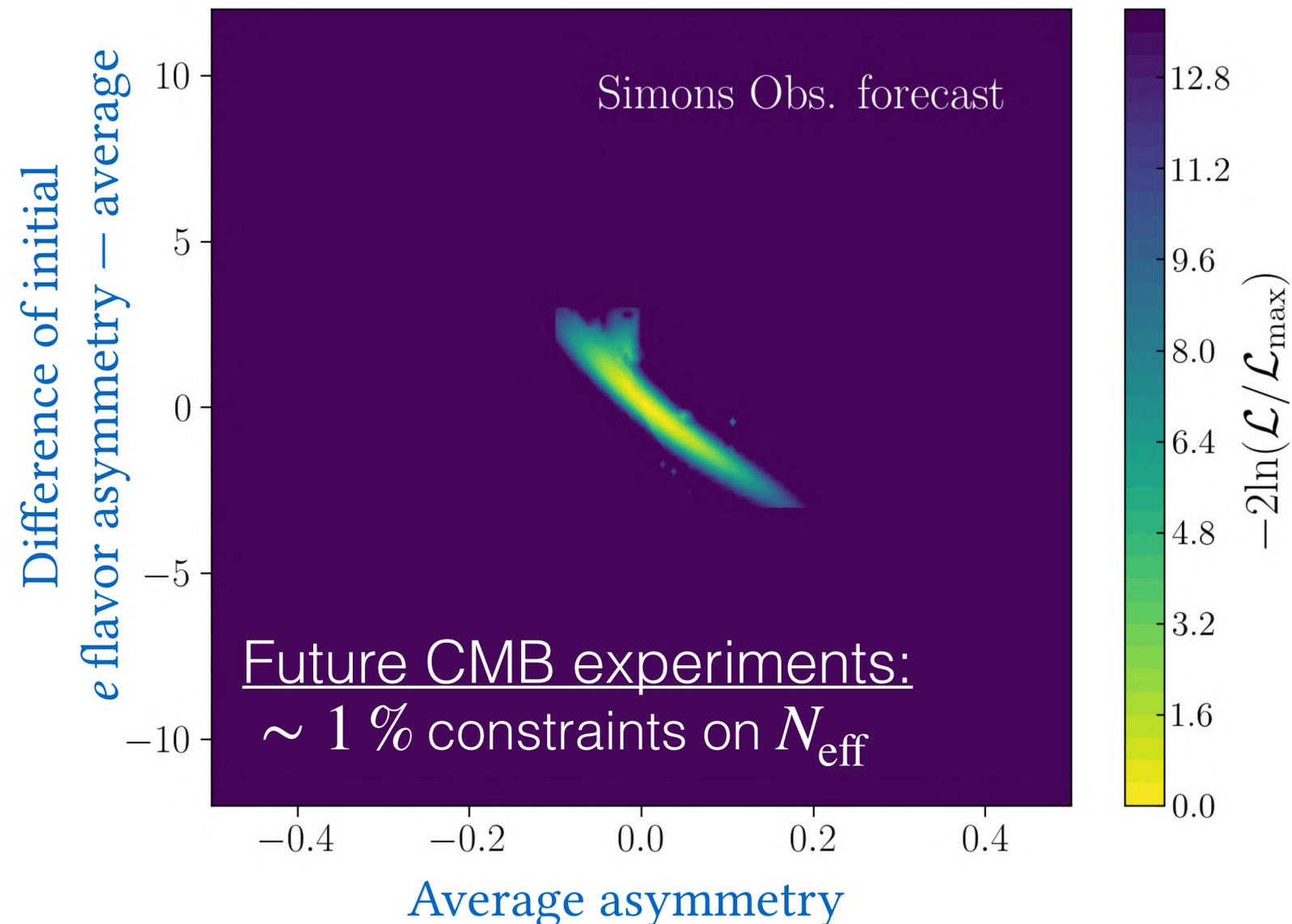
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- Large lepton asymmetries are allowed, with a complicated landscape due to the dynamics of flavor oscillations.



- Large lepton numbers are needed for some nonstandard scenarios, e.g., the **resonant production of sterile neutrino dark matter** (*Shi-Fuller* mechanism).

 D. Gorbunov, D. Kalashnikov and G. Krugan [2502.17374]  
C. Vogel, H. Escudero, JF and K. Abazajian [2507.18752]  
K. Akita, K. Hamaguchi and M. Ovchinnikov [2507.20659]

# Sterile neutrino dark matter production

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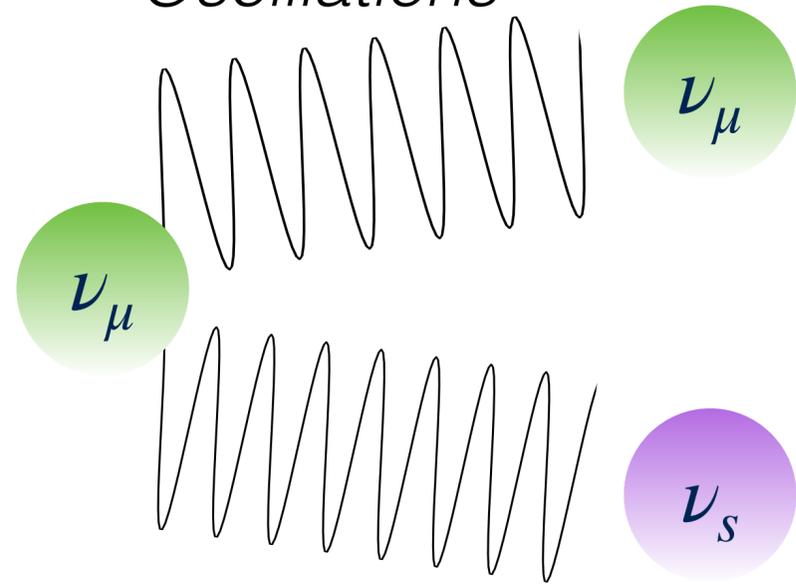


$\nu_\mu$

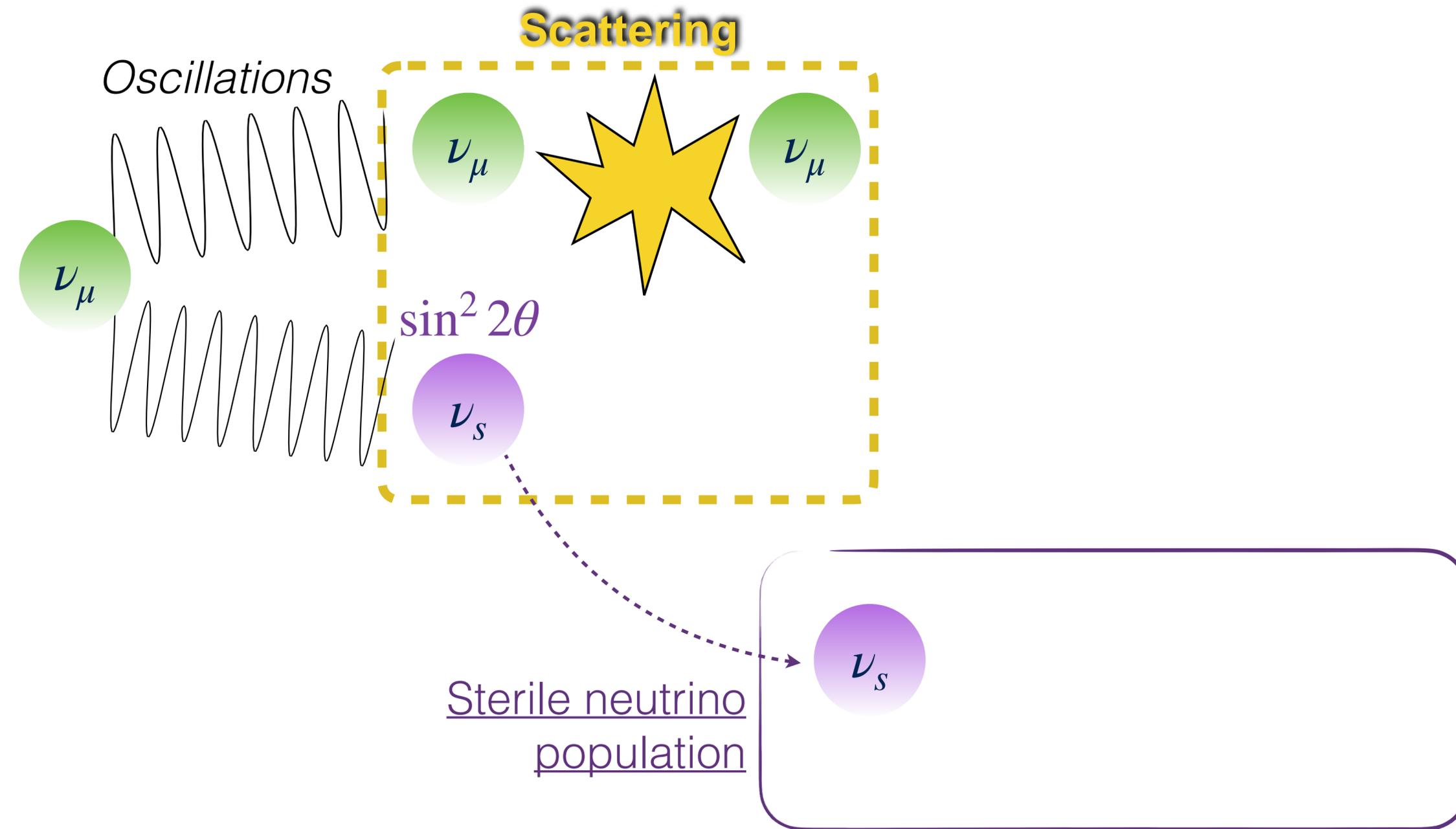
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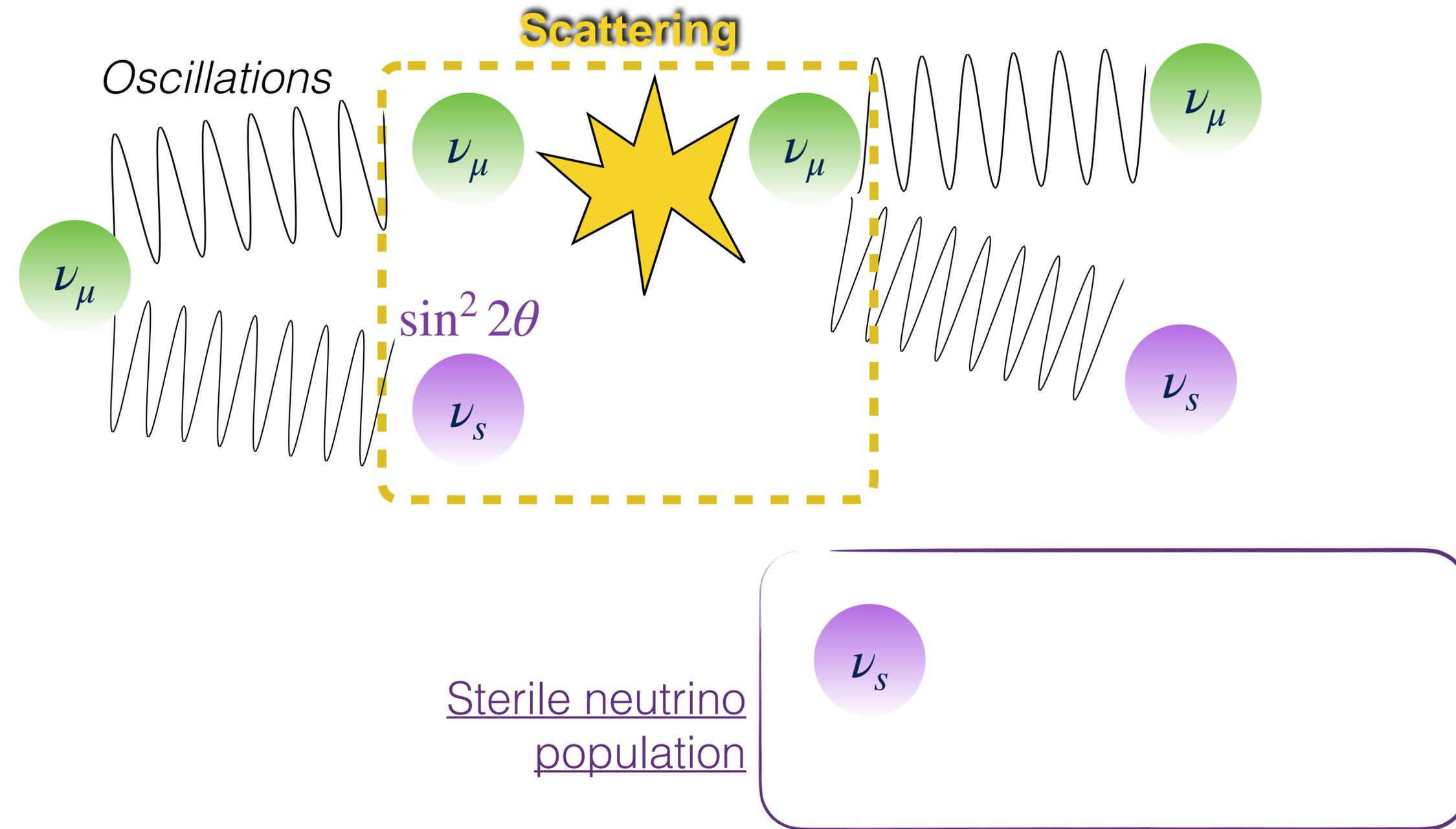
*Oscillations*



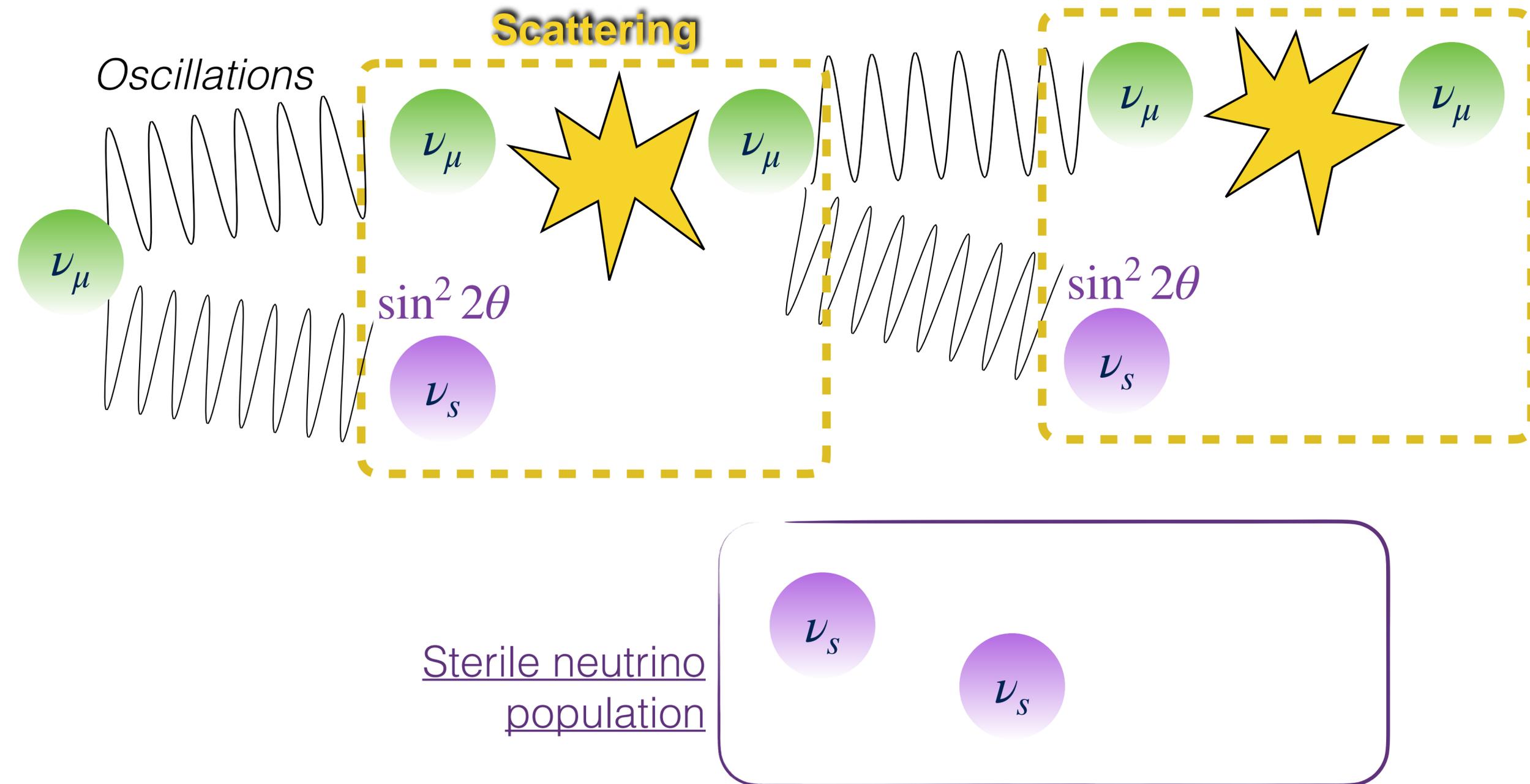
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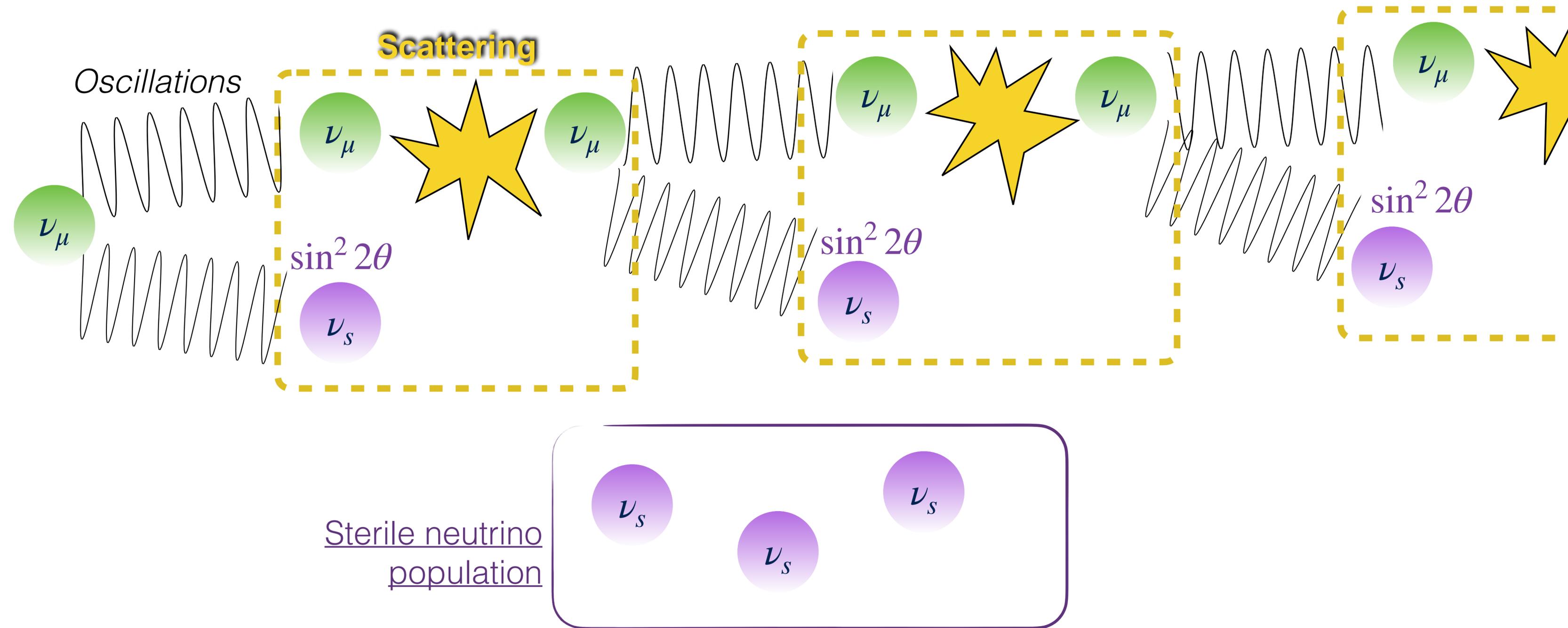
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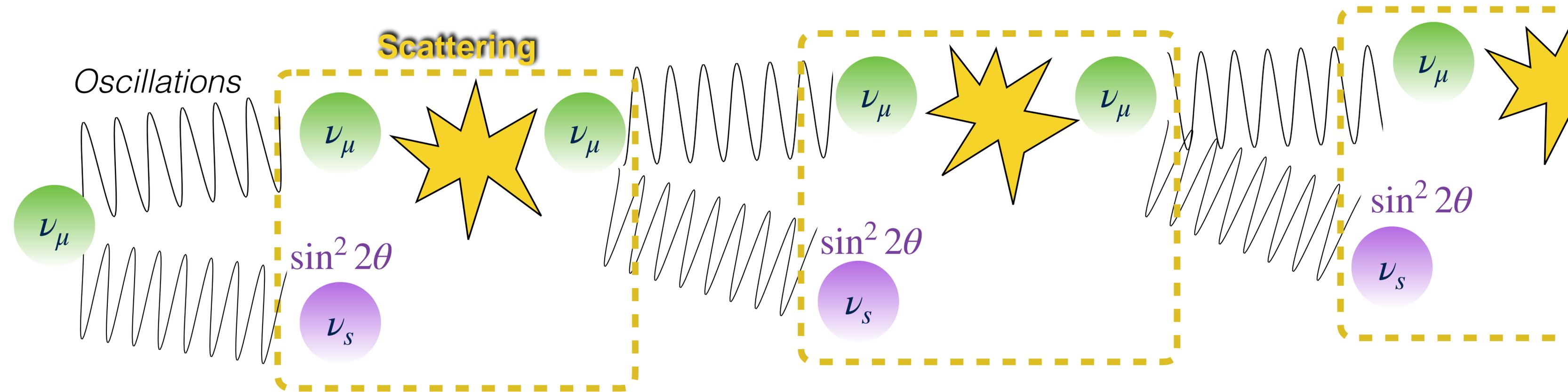
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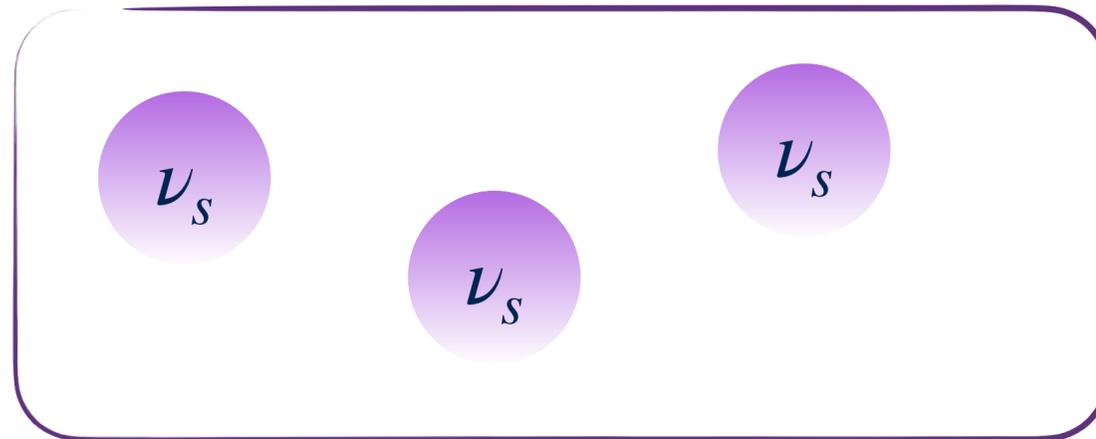
# Sterile neutrino dark matter production



# Sterile neutrino dark matter production



Sterile neutrino population  
 $\propto \sin^2 (2\theta)$



## DODELSON-WIDROW MECHANISM

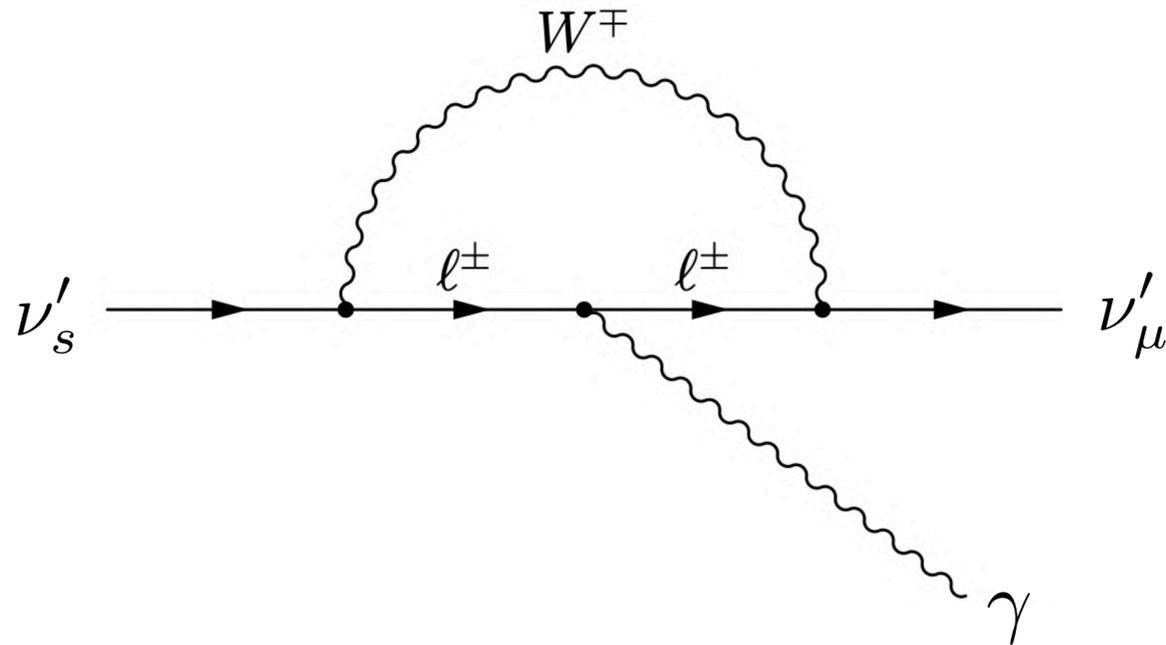
“Scattering-induced decoherence”

Dodelson & Widrow,  
*Phys. Rev. Lett.* **72**, 17 (1994)

# Sterile neutrino dark matter production

Oscillations

Radiative decay



$$\Gamma_{\text{decay}} \propto m_s^5 \sin^2 2\theta$$

$$E_\gamma = \frac{m_s}{2}$$

X-ray line

$\sin^2 2\theta$

$\nu_s$

Sterile neutrino population  
 $\propto \sin^2(2\theta)$

$\nu_s$

$\nu_s$

$\nu_s$

**DODELSON-WIDROW MECHANISM**

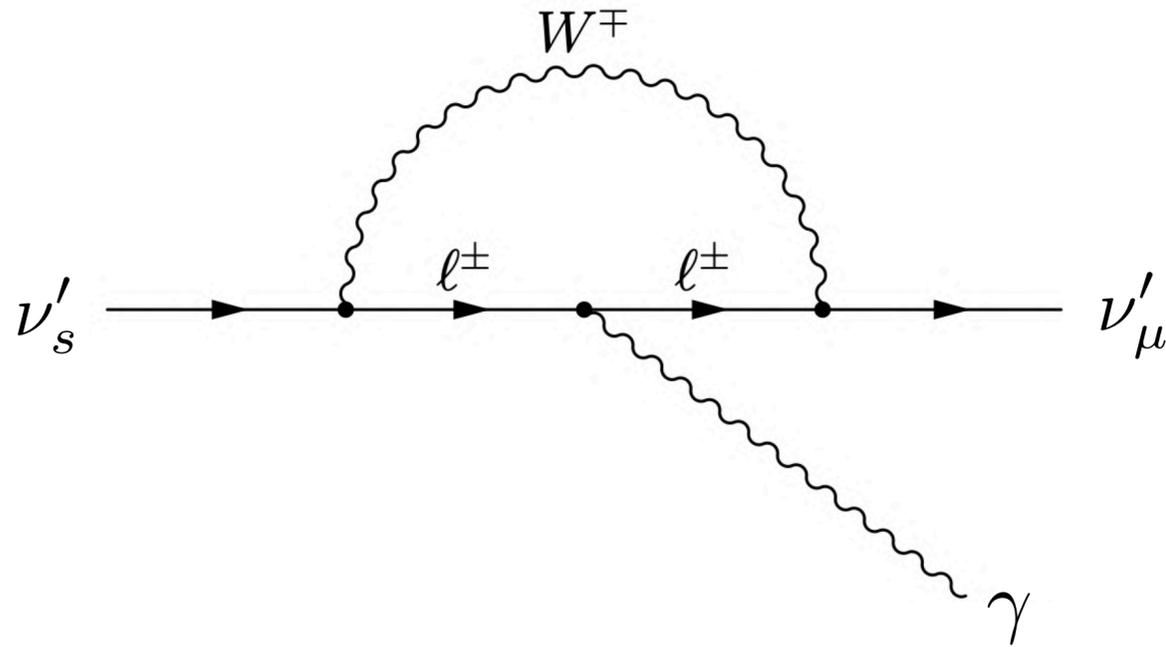
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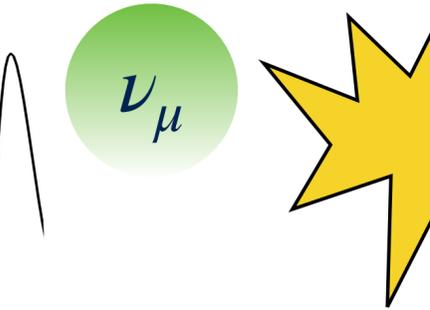
Oscillations

Radiative decay



$$\Gamma_{\text{decay}} \propto m_s^5 \sin^2 2\theta$$

$$E_\gamma = \frac{m_s}{2} \longrightarrow \text{X-ray line}$$



$\sin^2 2\theta$



Sterile neutrino population

$$\propto \sin^2 (2\theta)$$

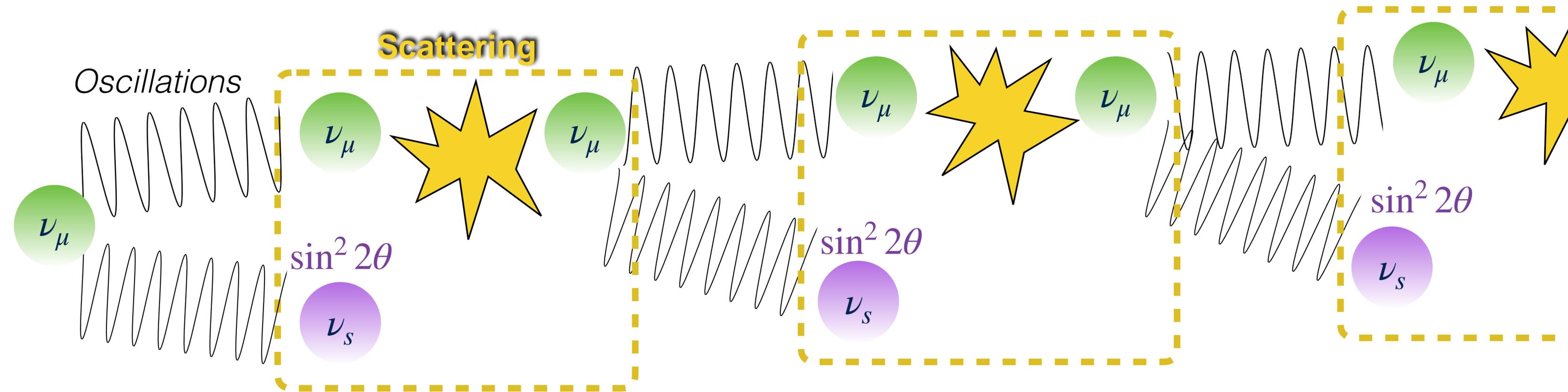


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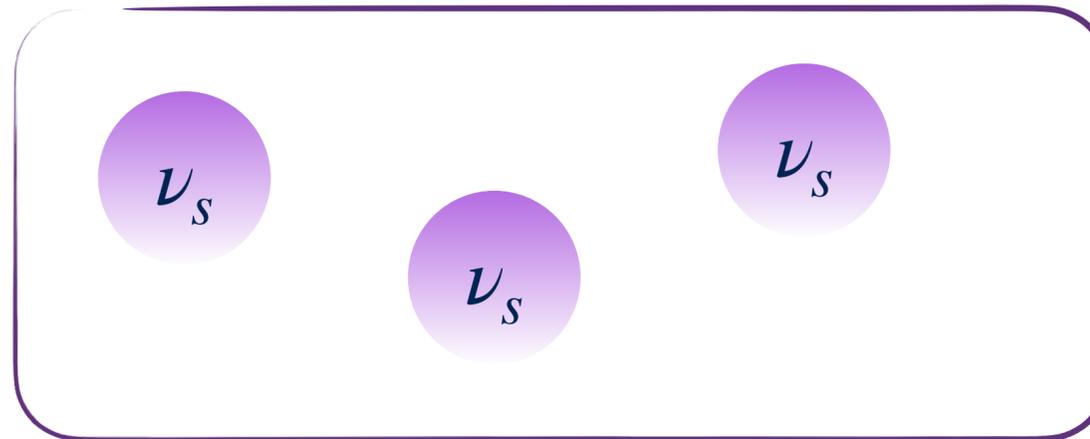
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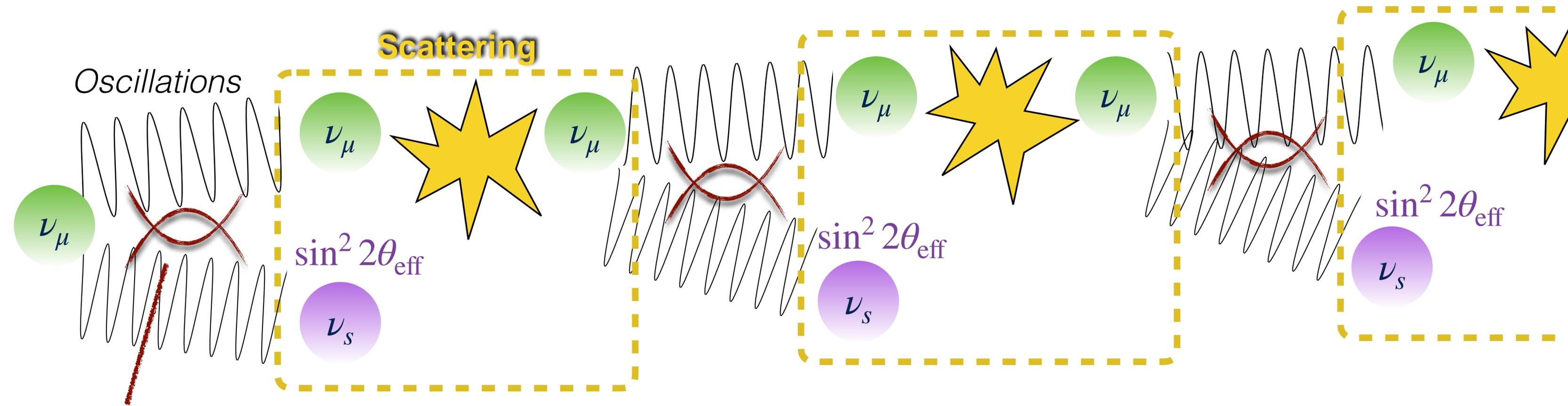


## DODELSON-WIDROW MECHANISM

“Scattering-induced decoherence”

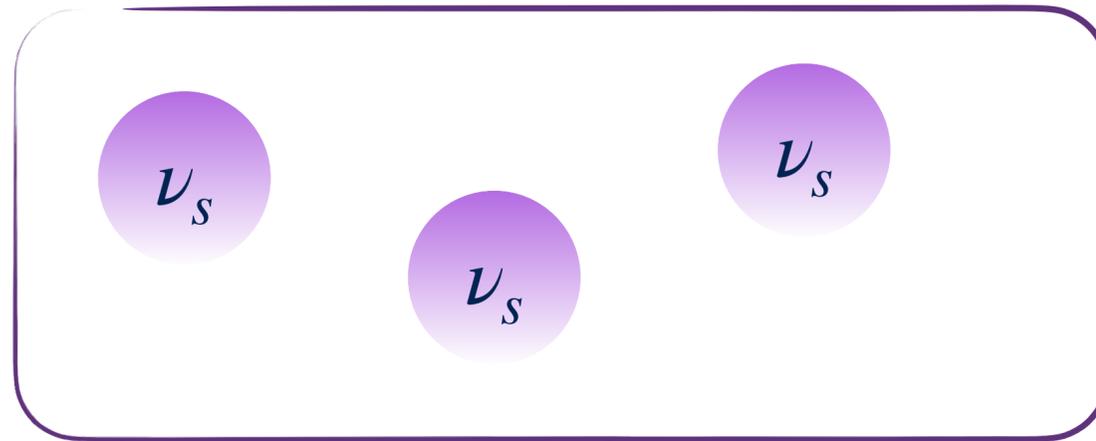
Dodelson & Widrow,  
*Phys. Rev. Lett.* **72**, 17 (1994)

# Sterile neutrino dark matter production



**Asymmetry-  
induced  
resonance**

Sterile neutrino  
population  
 $\propto \sin^2(2\theta_{\text{eff}}) \gg \sin^2(2\theta)$



## SHI-FULLER MECHANISM

*“Resonant  
production”*

Shi & Fuller,  
*Phys. Rev. Lett.* **82**, 2832 (1999)

# Constraints on SF sterile neutrino dark matter

 C. Vogel *et al.* [[2507.18752](#)]

Mass  $m_s$

Mixing angle  $\theta$

Initial lepton number

$$L = L_\mu = \frac{n_{\nu_\mu} - n_{\bar{\nu}_\mu}}{n_\gamma} \simeq 4\eta_\mu$$

sterile-dm

Venumadhav *et al.* [[1507.06655](#)]

$L(T)$

Phase-space distributions

$[\Omega_{\text{DM}} h^2](T)$

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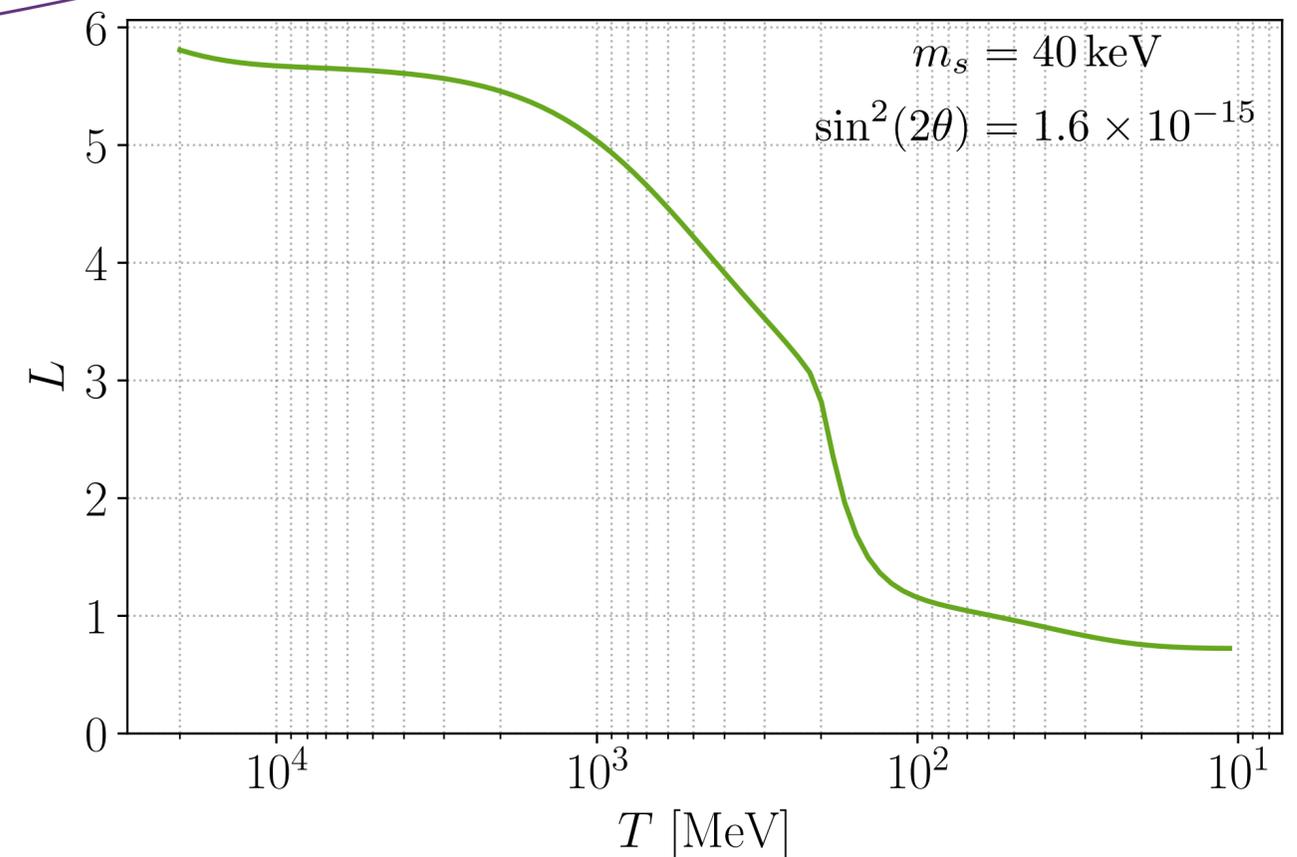
Venumadhav *et al.* [[1507.06655](#)]

$L(T)$

Phase-space distributions

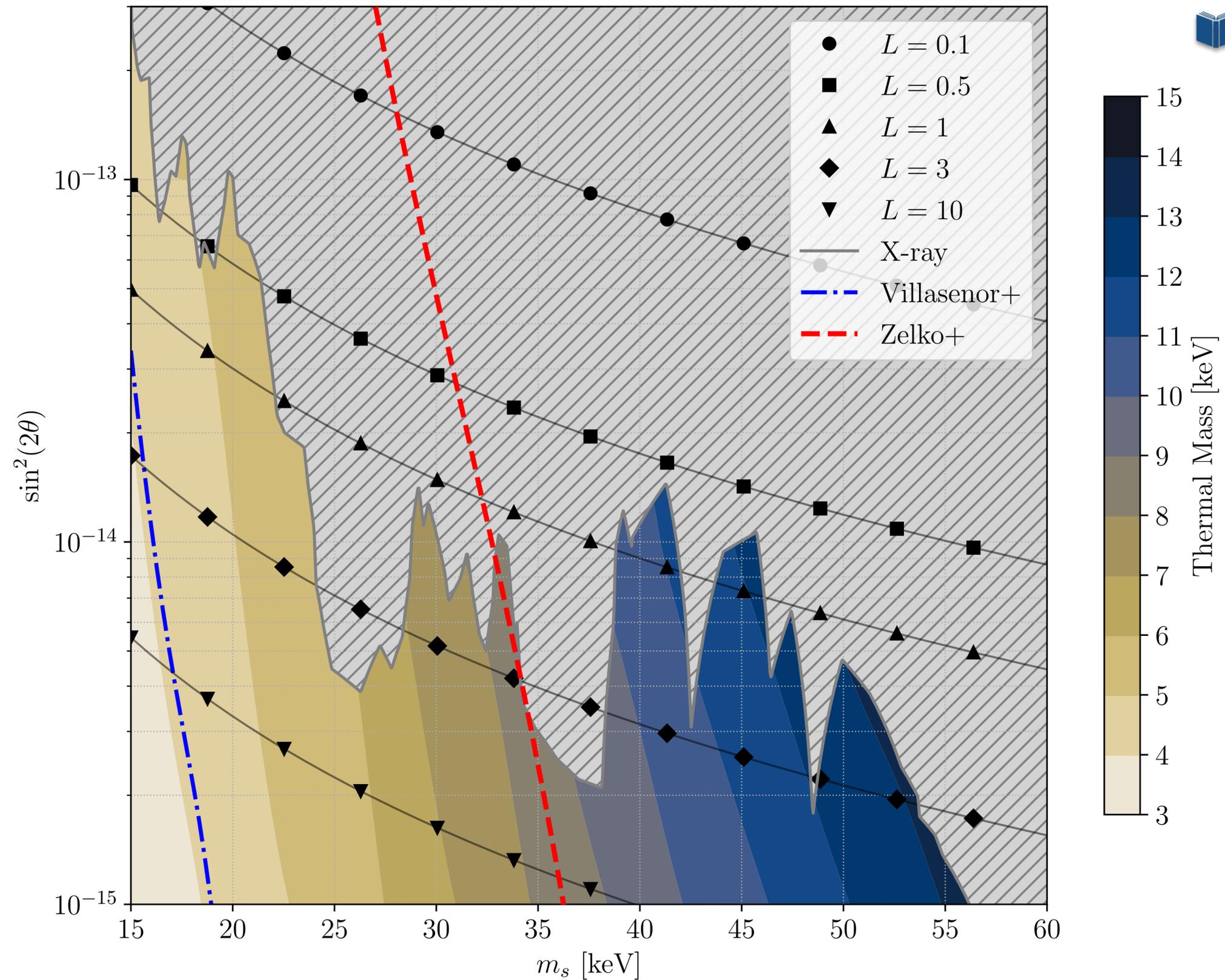
$[\Omega_{\text{DM}} h^2](T)$

root finder



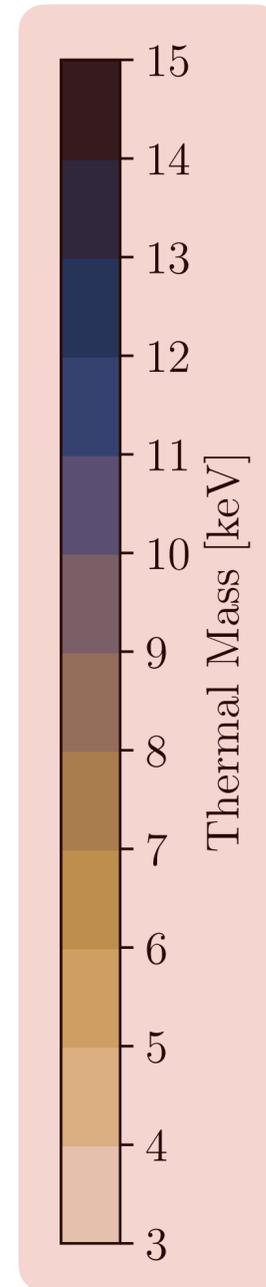
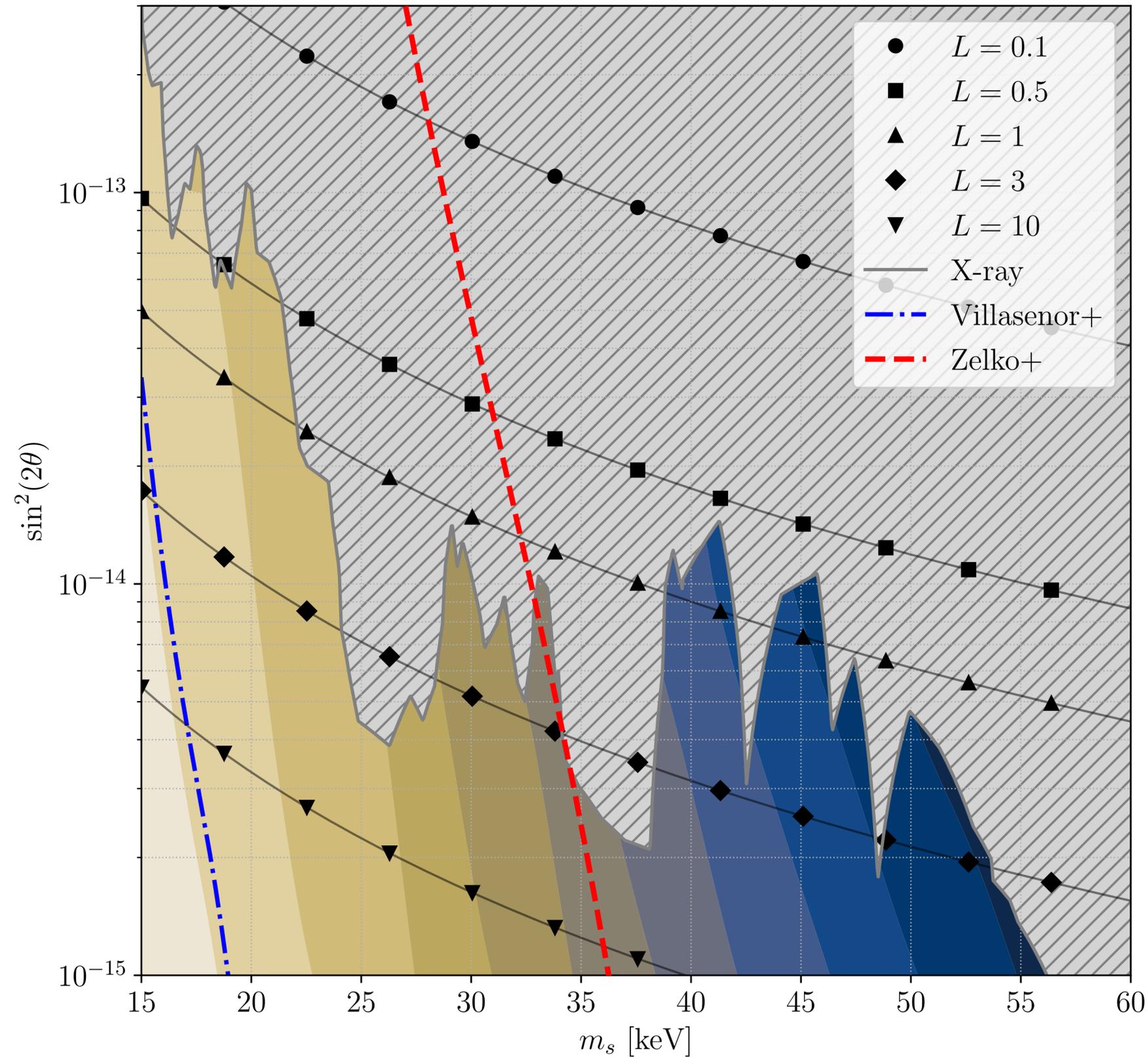
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 C. Vogel et al. [[2507.18752](https://arxiv.org/abs/2507.18752)]



# Constraints on SF sterile neutrino dark matter

C. Vogel et al. [2507.18752]



Equivalent thermal warm dark matter mass, for structure formation constraints

# Summary

---

- We combined a full quantum kinetic transport code for neutrinos with a BBN network to connect primordial asymmetries to cosmological observables.
- *Large primordial neutrino asymmetries* **are allowed**.
- Asymmetries are mixed, but **not perfectly equilibrated** in general  
→ complicated landscape of allowed asymmetries
- Future CMB experiments should have enough constraining power to be able to set actual constraints.
- This (re-)opens the parameter space for **resonant production of sterile neutrino dark matter** via the Shi-Fuller mechanism.
- Importance of future X-ray observatories in the  $\sim 20$  keV range!

 JF, C. Pitrou [[2110.11889](#)]  
JF, C. Pitrou [[2405.06509](#)]  
V. Domcke *et al.*  
[[2502.14960](#), [2510.02438](#)]

 C. Vogel *et al.* [[2507.18752](#)]  
K. Akita *et al.* [[2507.20659](#)]



# Quantum Kinetic Equation

Classical distribution functions  $\begin{pmatrix} f_{\nu_e} & & \\ & f_{\nu_\mu} & \\ & & f_{\nu_\tau} \end{pmatrix} \longrightarrow \varrho = \begin{pmatrix} \varrho_{ee} & \varrho_{e\mu} & \varrho_{e\tau} \\ \varrho_{e\mu}^* & \varrho_{\mu\mu} & \varrho_{\mu\tau} \\ \varrho_{e\tau}^* & \varrho_{\mu\tau}^* & \varrho_{\tau\tau} \end{pmatrix}$  **Density matrix**

## Generalization of Boltzmann's equation for quantum transport

$$i \left[ \frac{\partial}{\partial t} - H p \frac{\partial}{\partial p} \right] \varrho(p, t) = \left[ U \frac{M^2}{2p} U^\dagger, \varrho \right] - 2\sqrt{2}G_F p \left[ \frac{\mathbb{E}_{\text{lep}} + \mathbb{P}_{\text{lep}}}{m_W^2}, \varrho \right] + \sqrt{2}G_F [\mathbb{N}_\nu - \mathbb{N}_{\bar{\nu}}, \varrho] + i \mathcal{C}(\varrho, \bar{\varrho})$$

**Vacuum**

**Self-interactions**  
(effective potential due to the  $\nu, \bar{\nu}$  background)

$$\mathbb{E}_{\text{lep}} + \mathbb{P}_{\text{lep}} = \begin{pmatrix} \rho_{e^\pm} + P_{e^\pm} & 0 & 0 \\ 0 & \rho_{\mu^\pm} + P_{\mu^\pm} & 0 \\ 0 & 0 & 0 \end{pmatrix}$$

**Lepton mean-field**  
(effective potential due to the charged lepton background)

**Collisions**

$$\mathcal{C} = \mathcal{C}[\nu e^- \rightarrow \nu e^-] + \mathcal{C}[\nu e^+ \rightarrow \nu e^+] + \mathcal{C}[\nu \bar{\nu} \rightarrow e^- e^+] + \mathcal{C}[\nu \nu]$$

# Connection with thermal warm dark matter

Transfer function  $T(k) = \sqrt{\frac{P(k)}{P_{\Lambda\text{CDM}}(k)}}$

