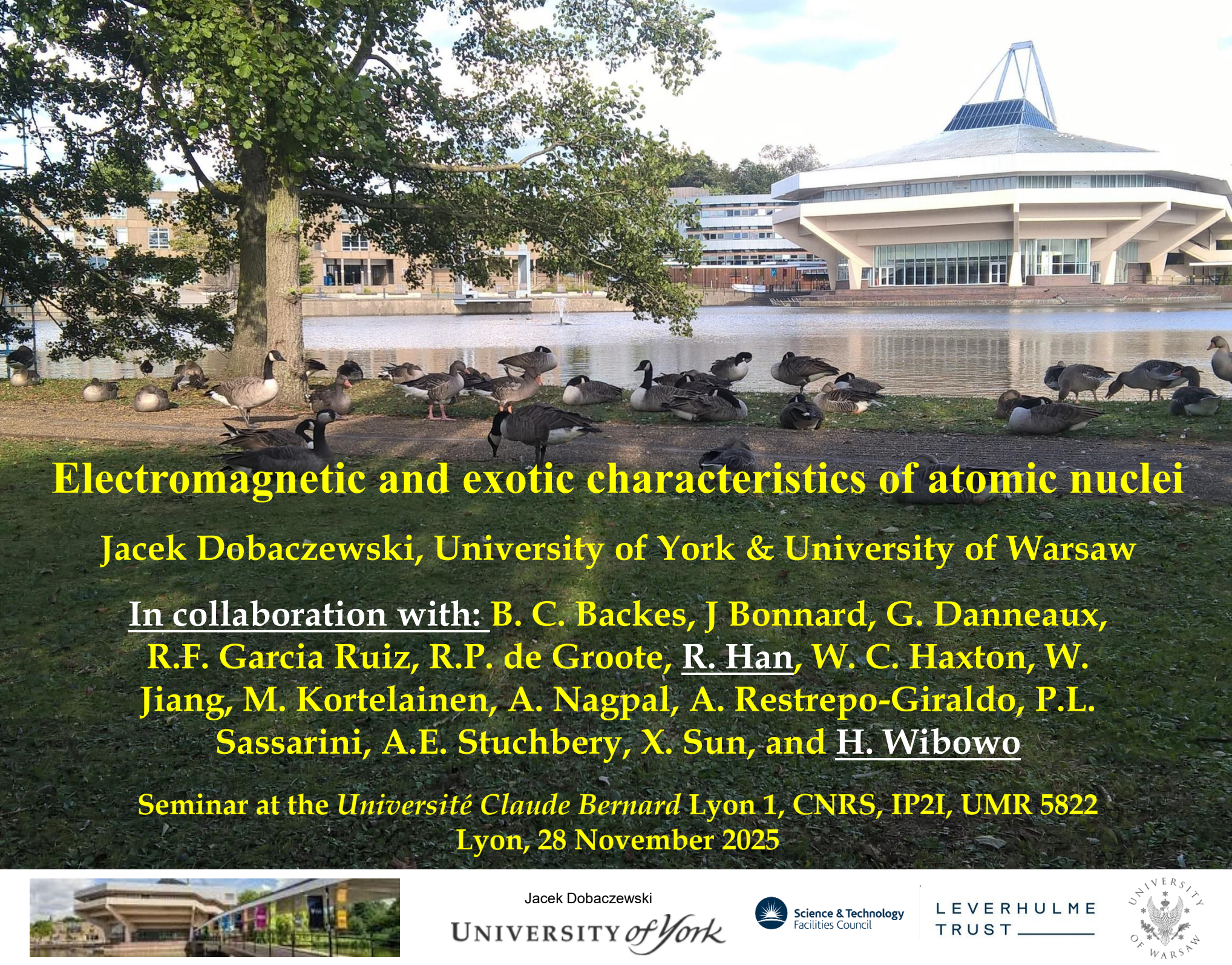




Electromagnetic and exotic characteristics of atomic nuclei

Jacek Dobaczewski, University of York & University of Warsaw

In collaboration with: B. C. Backes, J Bonnard, G. Danneaux,
R.F. Garcia Ruiz, R.P. de Groote, R. Han, W. C. Haxton, W.
Jiang, M. Kortelainen, A. Nagpal, A. Restrepo-Giraldo, P.L.
Sassarini, A.E. Stuchbery, X. Sun, and H. Wibowo

Seminar at the *Université Claude Bernard Lyon 1*, CNRS, IP2I, UMR 5822
Lyon, 28 November 2025



Outline

1. Nuclear shapes and currents
2. Experimental data
3. Methodology
 - a) Self-consistency
 - b) Polarization
 - c) Symmetry restoration
4. Ground states of near doubly magic nuclei
5. Ground and excited states of open-shell nuclei
6. Meson exchange currents for magnetic dipole moments
7. Electric dipole moments
8. Anapole moments
9. Conclusions



Nuclear shapes and currents

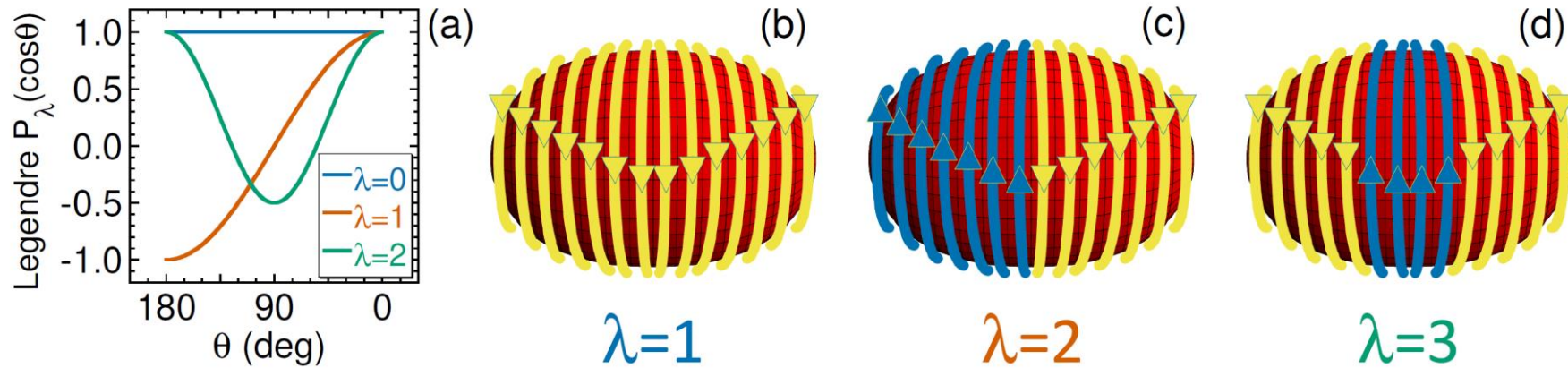


Figure 1: Legendre polynomials, $P_\lambda(\cos\theta)$ for $\lambda = 0, 1, 2$, (a), and the patterns of the current flows for the magnetic dipole (b), quadrupole (c), and octupole (d) moments of symmetry-broken aligned ground states of odd nuclei.

Nuclear shapes

$$R(\theta) = R_0 \sum_{\lambda=0,1,2,3\dots}^{\lambda_{\max}} \sqrt{\frac{2\lambda+1}{4\pi}} \beta_\lambda P_\lambda(\cos\theta), \quad \bar{\rho}(\mathbf{r}) = \begin{cases} \rho_0 & \text{for } r \leq R(\theta) \\ 0 & \text{for } r > R(\theta) \end{cases}$$

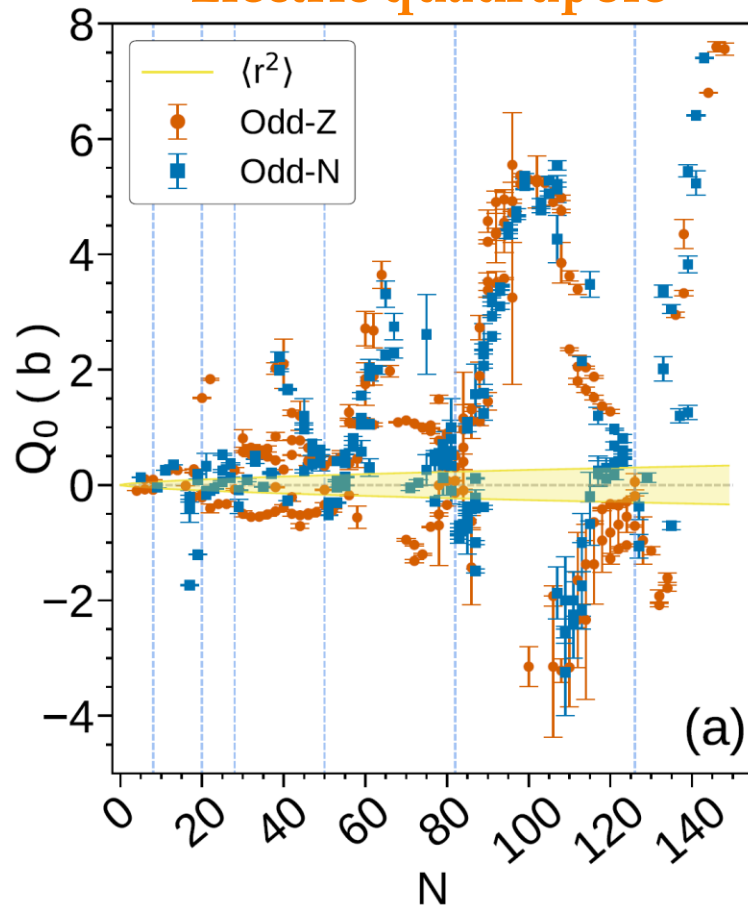
Nuclear currents

$$j_\phi(z, \eta) = \sum_{\lambda=1,2,3\dots}^{\lambda_{\max}} j_\lambda(r) P_{\lambda-1}(\cos\theta), \quad \text{with } r = \sqrt{\eta^2 + z^2}, \quad \cos\theta = \frac{z}{r},$$



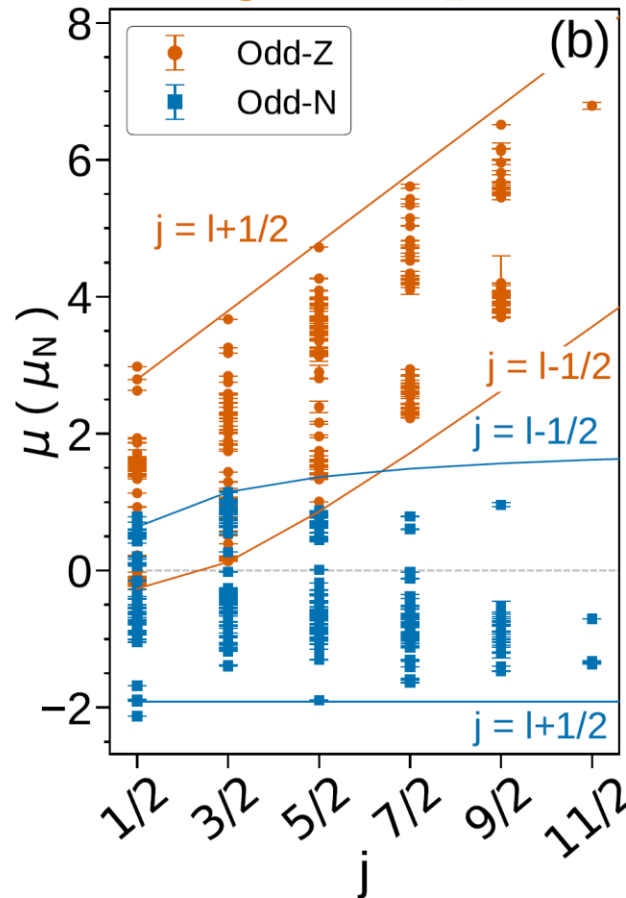
Experimental data

Electric quadrupole



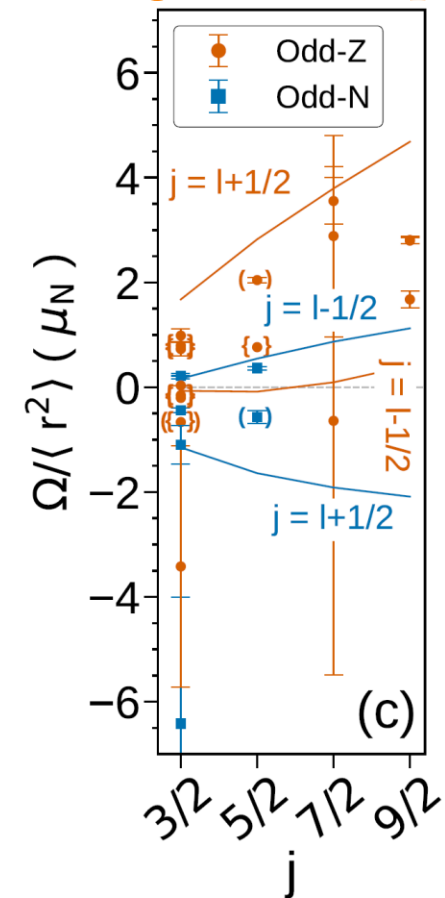
Shows the lowest-order deformation:
 $Q_0 > 0$ (prolate)
 $Q_0 = 0$ (spherical)
 $Q_0 < 0$ (oblate)

Magnetic dipole



Shows the lowest-order orbital and spin current flow

Magnetic octupole

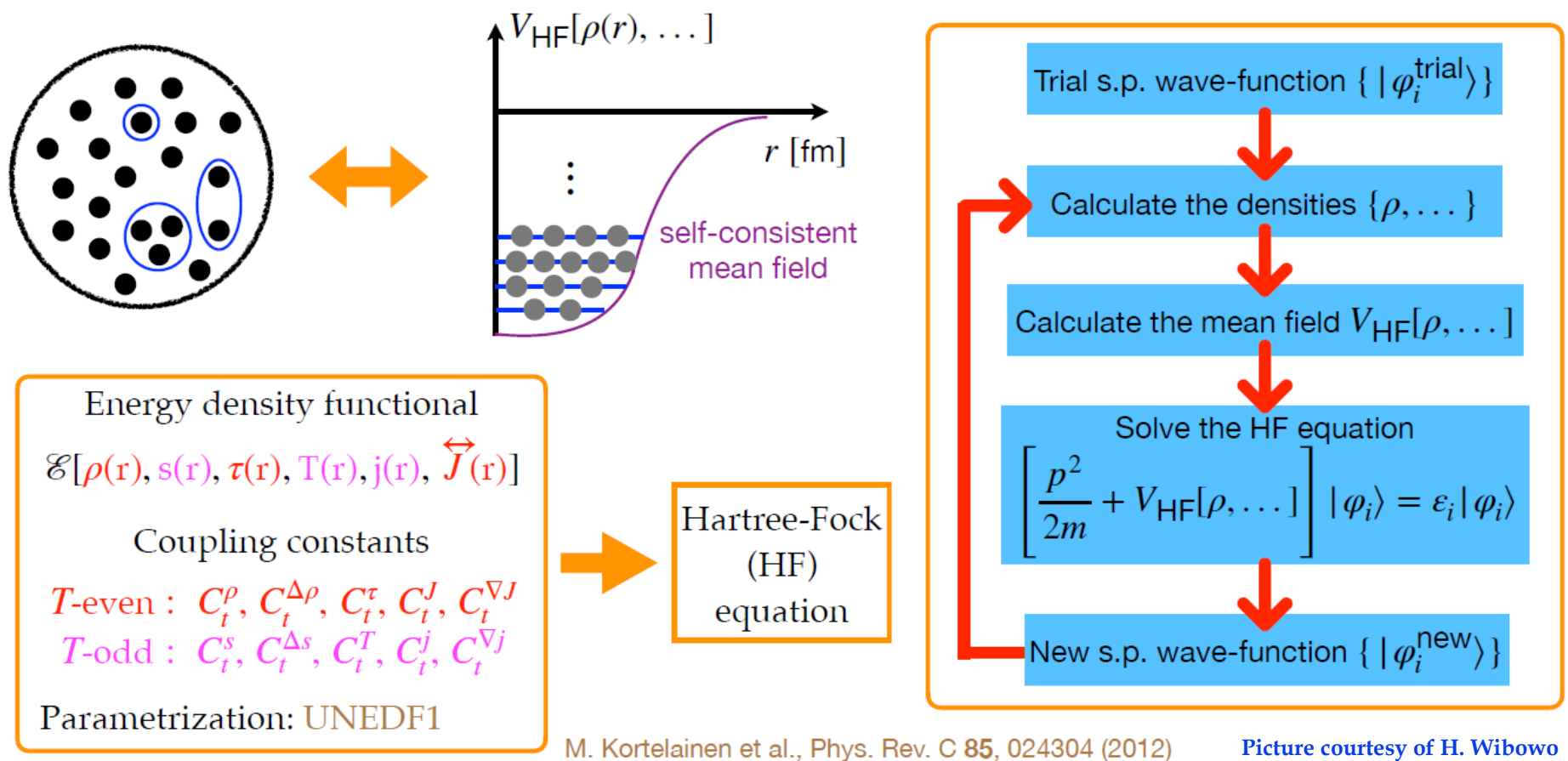


Shows the higher-order orbital and spin current flow

J. Dobaczewski *et al.*, [arXiv:2511.04632](https://arxiv.org/abs/2511.04632)



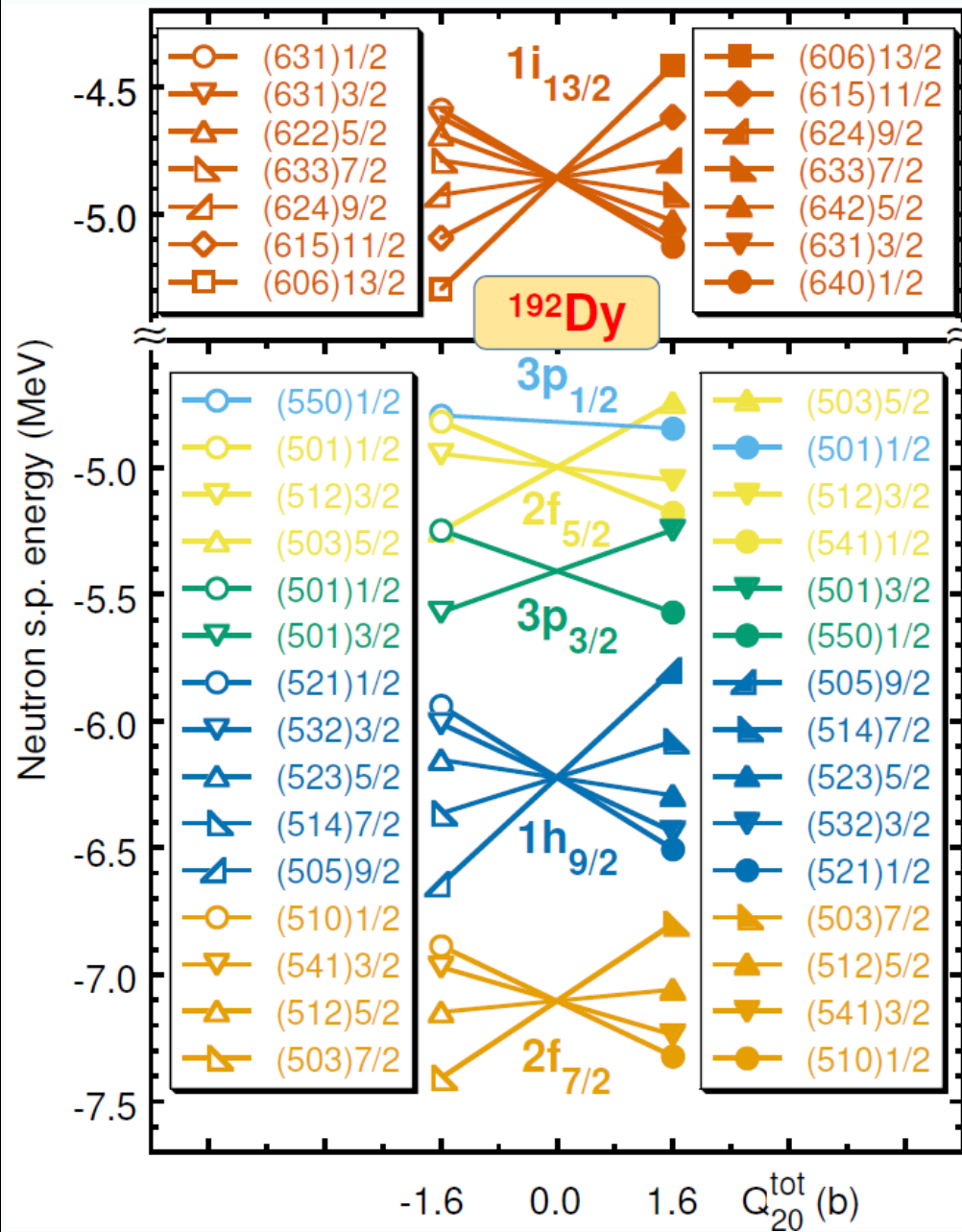
Nuclear density functional theory



Self-consistent equations are solved iteratively, which includes the polarization effects summed up to all orders without recurring to the lowest order perturbative coupling.



How to calculate odd nuclei in nuclear DFT?



without pairing

A even, $p > A$, $h \leq A$

$$|\Psi\rangle_{\text{HF}}^{\text{even}} = a_A^+ \dots a_2^+ a_1^+ |0\rangle$$

$$|\Psi\rangle_{\text{HF}}^{\text{odd}} = \begin{cases} a_p^+ |\Psi\rangle_{\text{HF}}^{\text{even}} \\ a_h |\Psi\rangle_{\text{HF}}^{\text{even}} \end{cases}$$

with pairing

$$|\Psi\rangle_{\text{HFB}}^{\text{even}} = \prod_{\mu>0} (u_{\mu} + v_{\mu} a_{\mu}^+ a_{\mu}^+) |0\rangle$$

$$|\Psi\rangle_{\text{HFB}}^{\text{odd}} = \beta_{\nu}^+ |\Psi\rangle_{\text{HFB}}^{\text{even}}$$

$$= a_{\nu}^+ \prod_{\nu \neq \mu > 0} (u_{\mu} + v_{\mu} a_{\mu}^+ a_{\mu}^+) |0\rangle$$

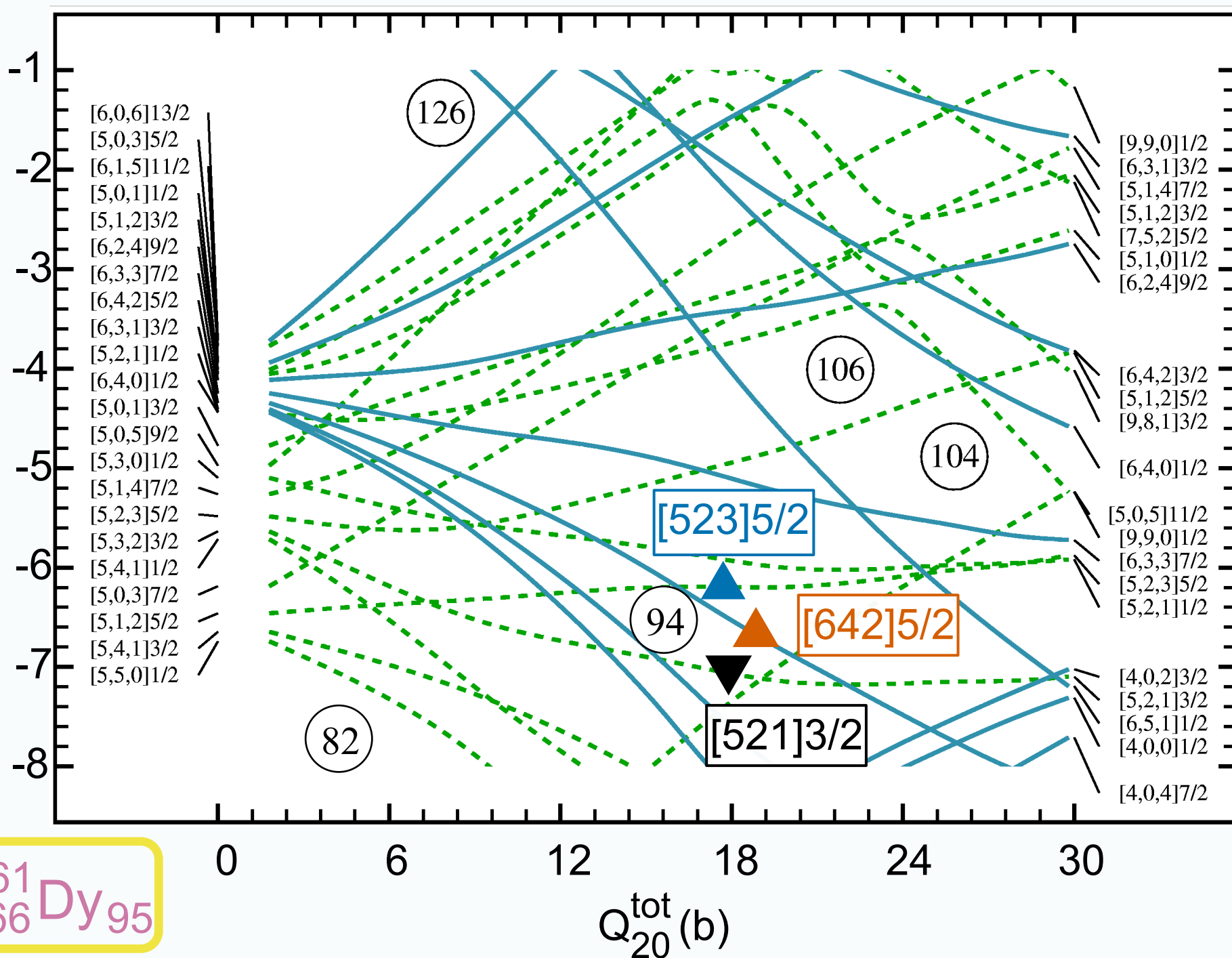
tagging quasiparticle states

$$\max_{\mu} \{ \langle \varphi_{\nu} | \phi_{\mu}^{\text{upper}} \rangle, \langle \varphi_{\nu} | \phi_{\mu}^{\text{lower}} \rangle \}$$

J. Dobaczewski *et al.*, [arXiv:2509.26549](https://arxiv.org/abs/2509.26549)



Neutron single-particle energies (MeV)



J. Dobaczewski et al., arXiv:2509.26549



Jacek Dobaczewski
UNIVERSITY of York

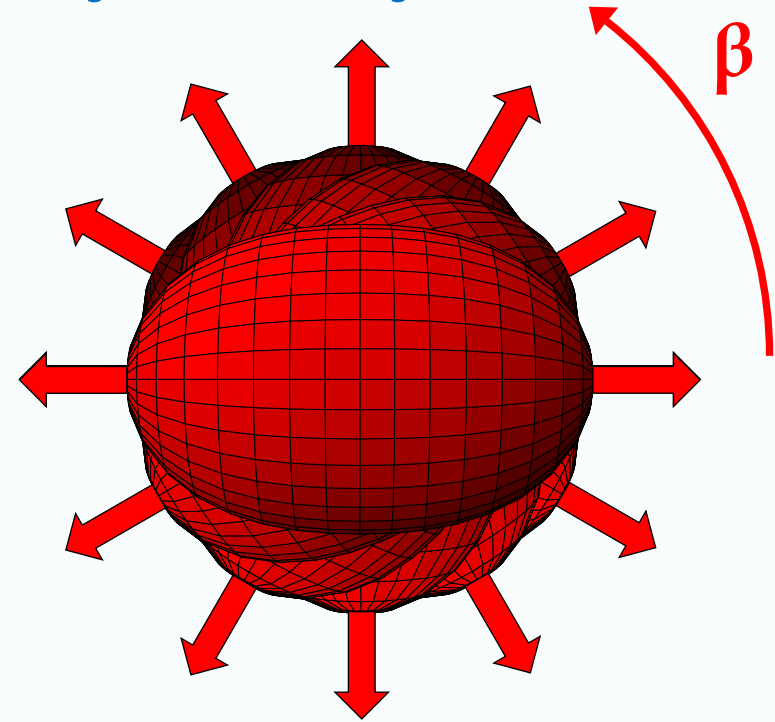
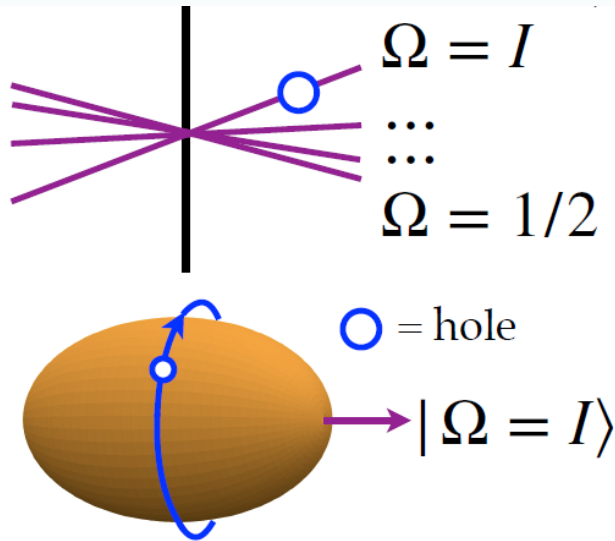
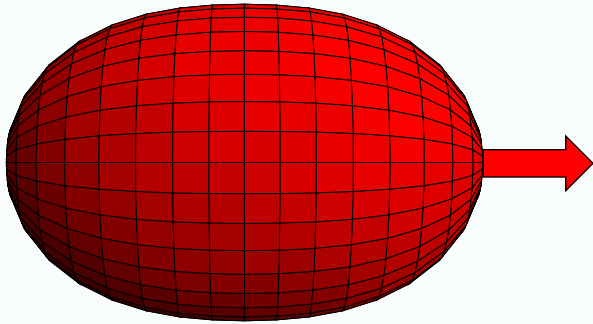


LEVERHULME
TRUST



Time-odd spin alignment & symmetry restoration

“Intrinsic”
Symmetry broken



“Laboratory”
Symmetry restored

$$|IM\rangle = \mathcal{N}_I \int_{\beta=0}^{\pi} d\beta d_{M\Omega}^I(\beta) |\Omega, \beta\rangle$$

Spectroscopic moments are determined for symmetry-restored wave functions without using effective charges or effective g-factors and compared with experimental data.



Basic definitions

The electric and magnetic moments are defined as

$$Q_{\lambda\mu} = \langle \Psi | \hat{Q}_{\lambda\mu} | \Psi \rangle = \int q_{\lambda\mu}(\vec{r}) d^3\vec{r},$$

$$M_{\lambda\mu} = \langle \Psi | \hat{M}_{\lambda\mu} | \Psi \rangle = \int m_{\lambda\mu}(\vec{r}) d^3\vec{r},$$

where $|\Psi\rangle$ is a many-body state, and $q_{\lambda\mu}(\vec{r})$ and $m_{\lambda\mu}(\vec{r})$ are the corresponding electric and magnetic-moment densities:

$$q_{\lambda\mu}(\vec{r}) = e\rho(\vec{r})Q_{\lambda\mu}(\vec{r}),$$

$$m_{\lambda\mu}(\vec{r}) = \mu_N \left[g_s \vec{s}(\vec{r}) + \frac{2}{\lambda+1} g_l (\vec{r} \times \vec{j}(\vec{r})) \right] \cdot \vec{\nabla} Q_{\lambda\mu}(\vec{r}),$$

and e , g_s , and g_l are the elementary charge, and the spin and orbital gyromagnetic factors, respectively. The multipole functions (solid harmonics) have the standard form: $Q_{\lambda\mu}(\vec{r}) = r^\lambda Y_{\lambda\mu}(\theta, \phi)$.



Nuclear quadrupole & dipole moments

Spectroscopic electric quadrupole Q and magnetic dipole μ moments are :

$$Q = \sqrt{\frac{16\pi}{5}} \langle II | \hat{Q}_{20} | II \rangle \quad \text{and} \quad \mu = \sqrt{\frac{4\pi}{3}} \langle II | \hat{M}_{10} | II \rangle .$$

P. Ring and P. Schuck, *The Nuclear Many-Body Problem*

$$\hat{Q}_{20} = \sqrt{\frac{5}{16\pi}} e \sum_{i=1}^A \left(\frac{1}{2} - t_3^{(i)} \right) \{ 3z_i^2 - r_i^2 \}; \quad \hat{M}_{10} = \sqrt{\frac{3}{4\pi}} \mu_N \sum_{i=1}^A \left\{ g_s^{(i)} s_{zi} + g_\ell^{(i)} \ell_{zi} \right\};$$

$$g_s^{(i)} = g_p(g_n) = 5.58(-3.82) \quad g_\ell^{(i)} = 1(0)$$

Intrinsic moments = moments of the symmetry-broken state
Spectroscopic moments = moments of the symmetry-restored state

Spectroscopic moments = moments measured experimentally



Open shell and near doubly magic nuclei

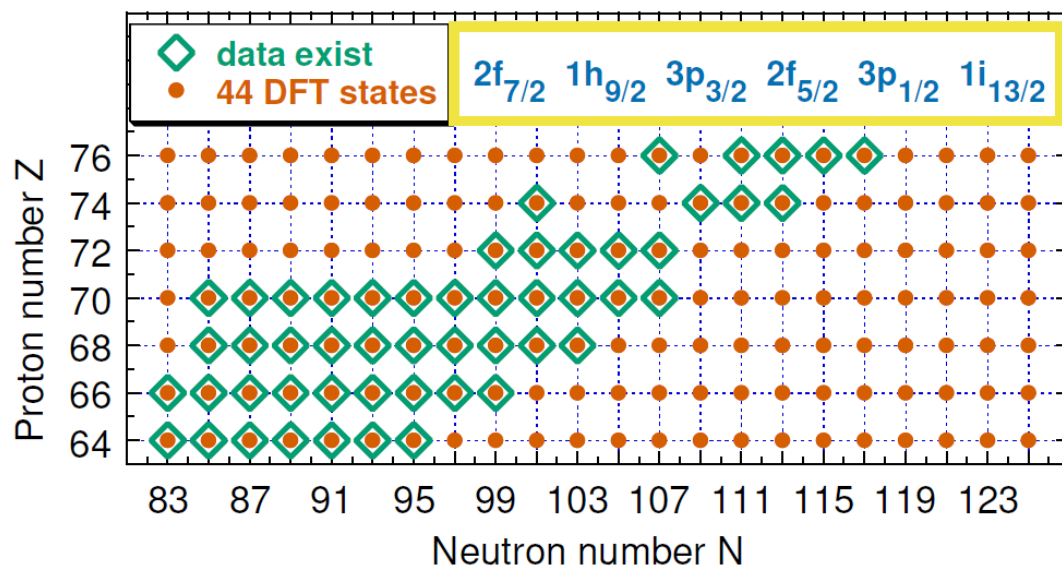


FIG. 1. Diagram illustrating the set of odd- N , even- Z open-shell elements and isotopes considered in this study for which (i) the calculations were performed (dots) and (ii) experimental data exist (diamonds).

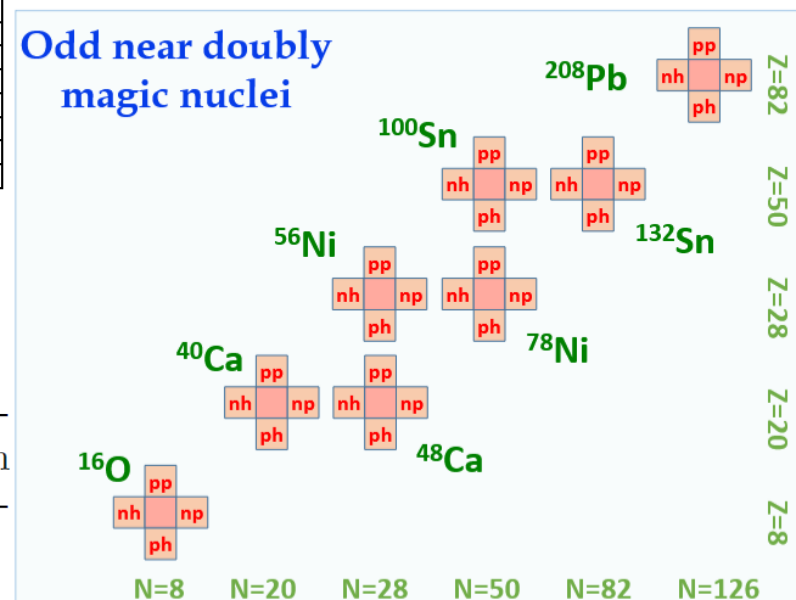


FIG. 1. Diagram illustrating the set of odd near doubly magic nuclei considered in this study. The symbols pp, ph, np, and nh represent the one-proton-particle, one-proton-hole, one-neutron-particle, and one-neutron-hole neighbors of the eight doubly magic nuclei.



Summary of results obtained near doubly magic nuclei

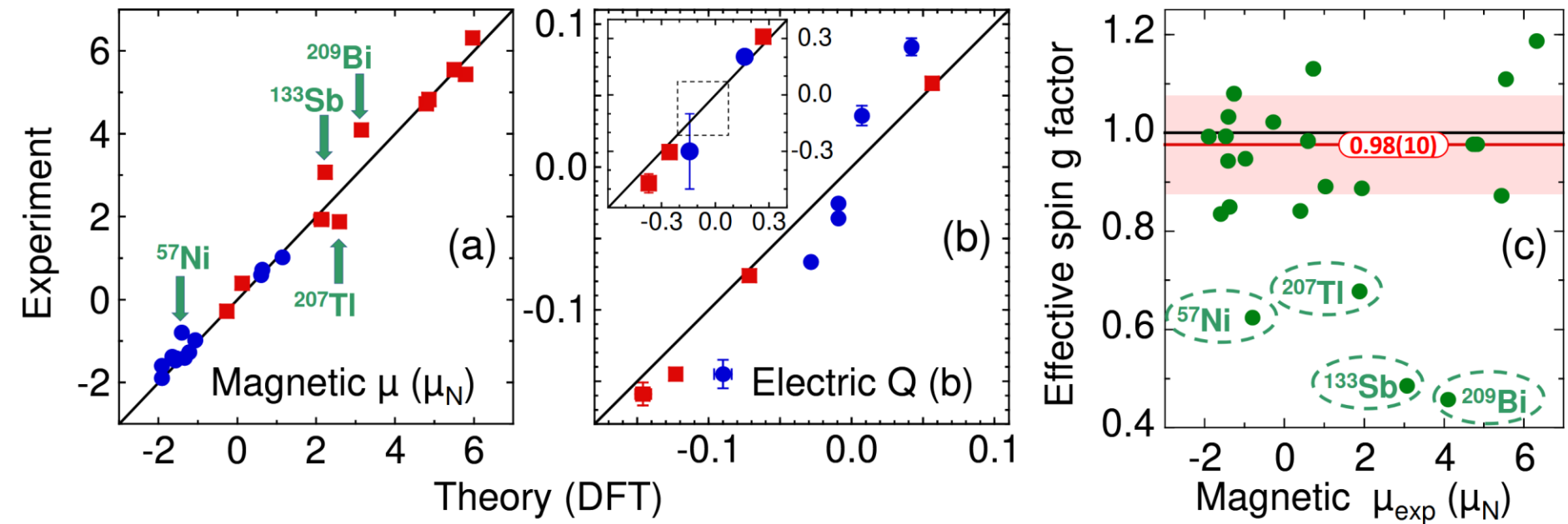
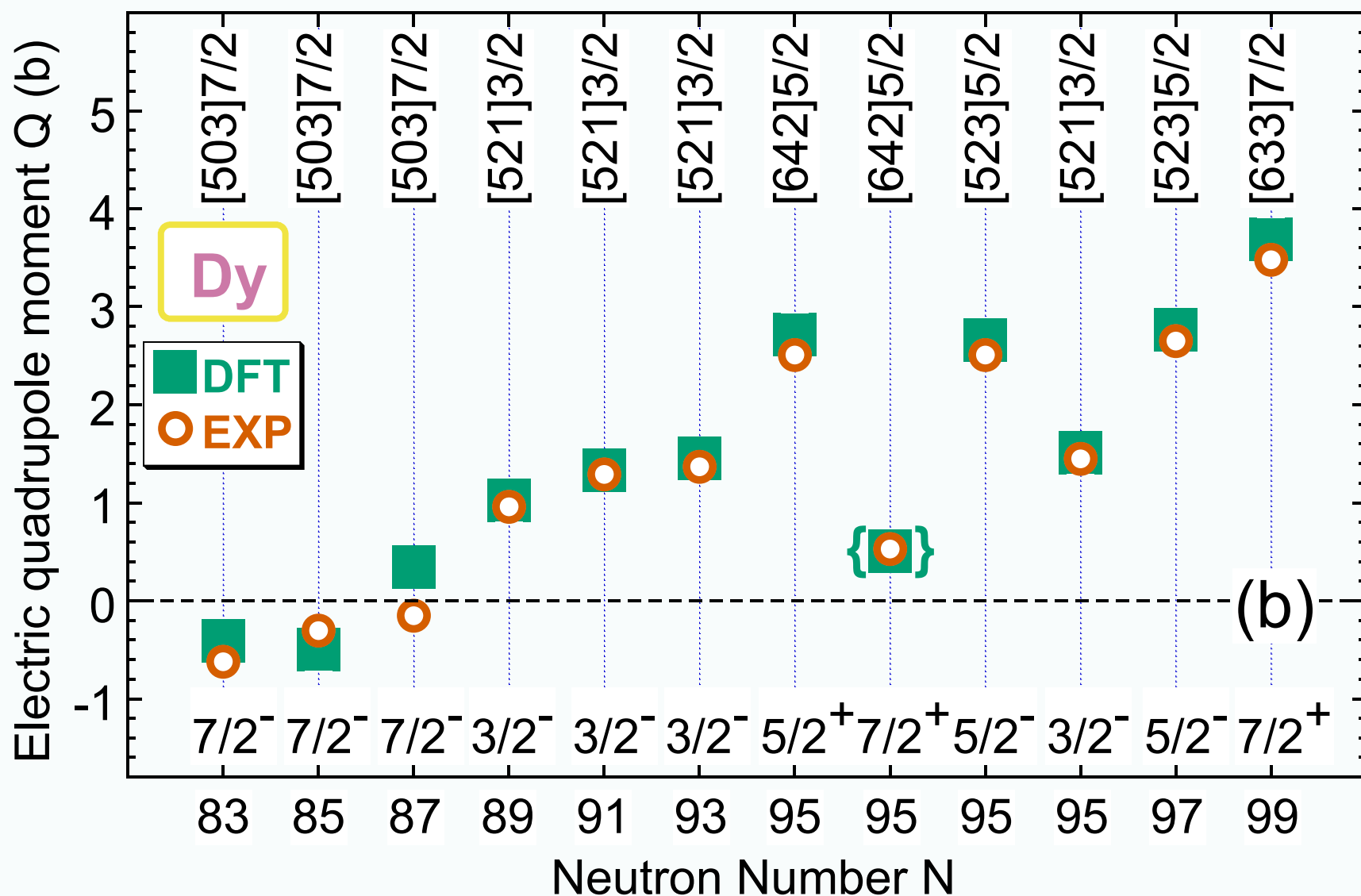


Figure 4: Calculated magnetic dipole moments μ (a) compared with 23 experimentally measured values (the arrows mark the outlier cases discussed in the text). Full circles (squares) show results obtained for odd- N (odd- Z) nuclei. Panel (b) shows the electric quadrupole moments Q compared with 15 experimentally measured values (the inset shows values that are outside the area of the main plot, as visualised by the dashed-line square drawn inside). Panel (c) shows the effective spin g factors described in the text, with ovals marking the outliers shown in panel (a).



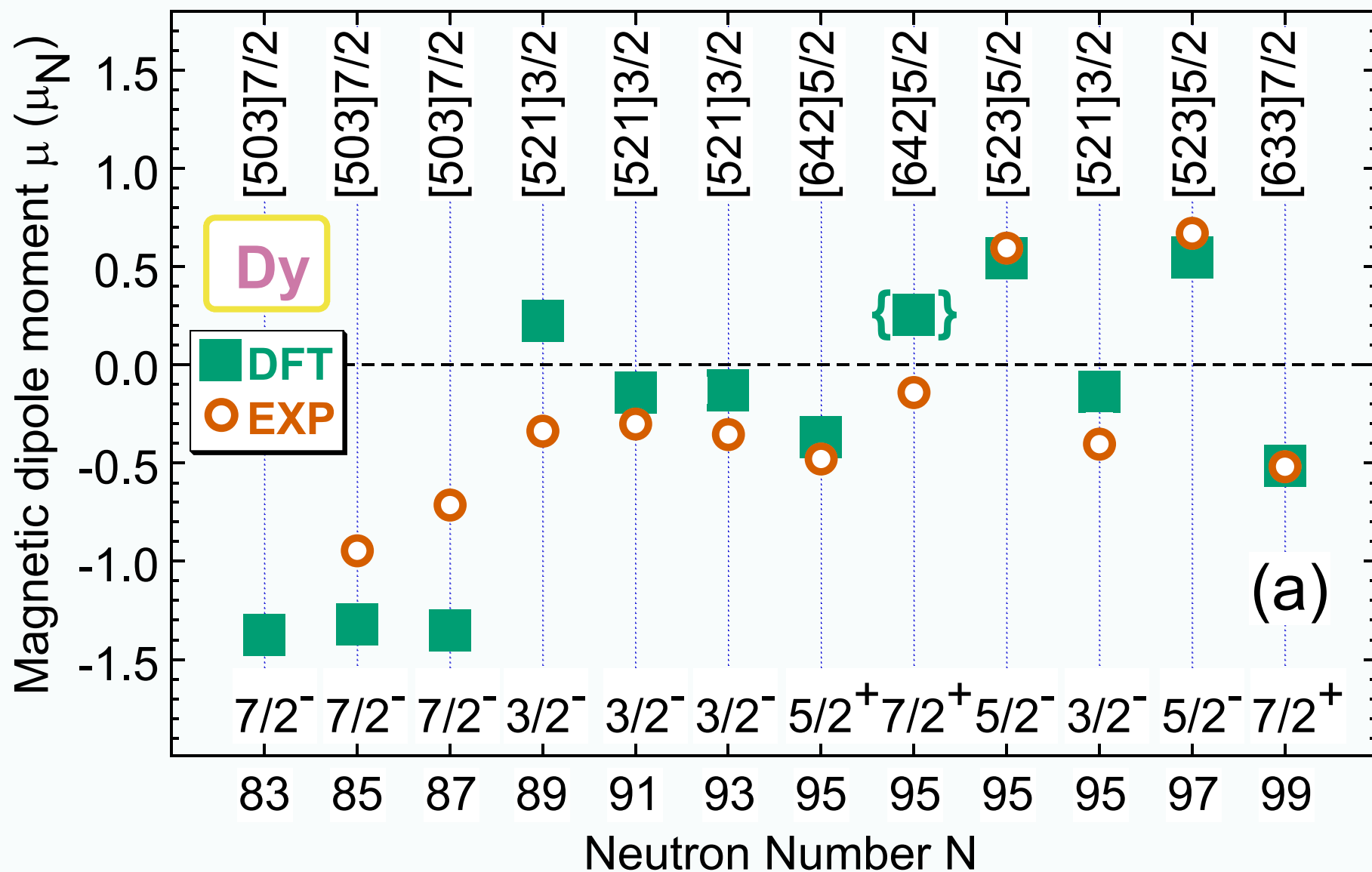
Dysprosium electric quadrupole moments vs. data



J. Dobaczewski *et al.*, [arXiv:2509.26549](https://arxiv.org/abs/2509.26549)



Dysprosium magnetic dipole moments vs. data



J. Dobaczewski *et al.*, [arXiv:2509.26549](https://arxiv.org/abs/2509.26549)



Summary of results obtained in open-shell nuclei

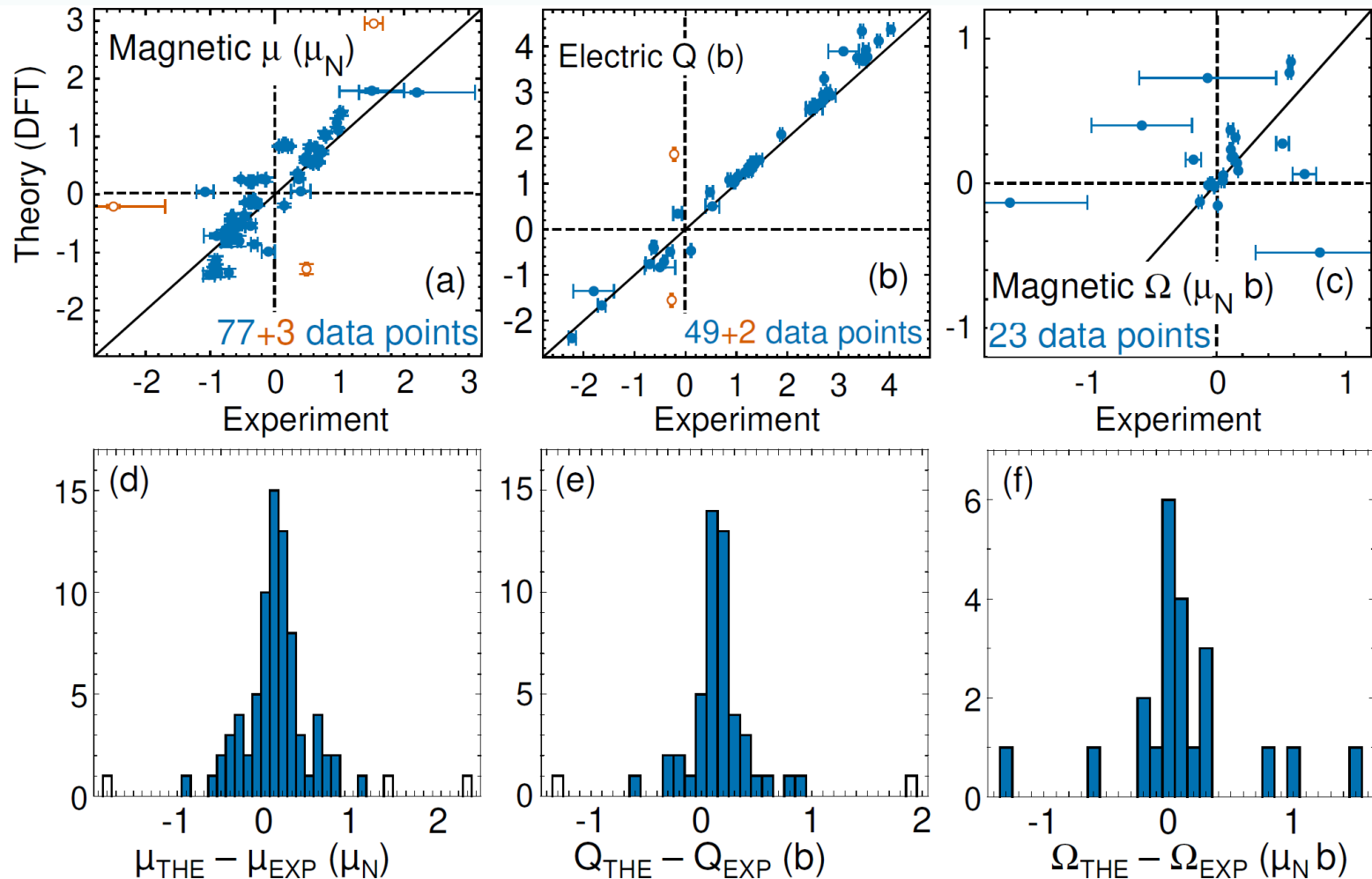
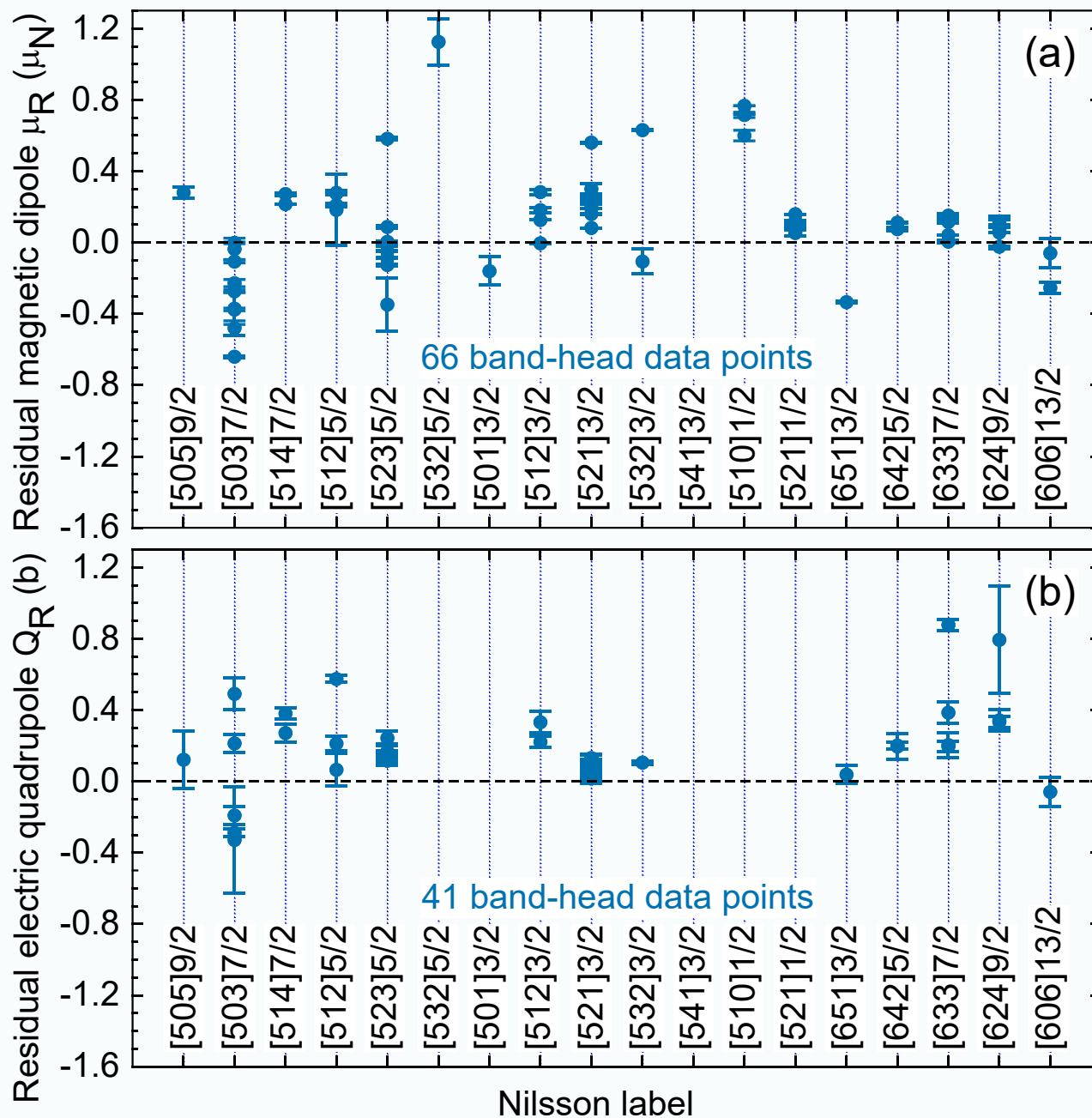


Figure 6: Summary comparison of the experimental and theoretical DFT magnetic dipole moments μ , (a) and (d), electric quadrupole moments Q , (b) and (e), in odd- N , even- Z isotopes between gadolinium and osmium (panels adapted from Reference (67)). Panels (c) and (f) show the analogous comparison of the magnetic octupole moments Ω across the mass chart. Open symbols and bars denote the outliers, see text.



Residuals in open-shell nuclei



J. Dobaczewski *et al.*, [arXiv:2509.26549](https://arxiv.org/abs/2509.26549)



Meson exchange currents in nuclear DFT

The two-body operator (40) has two terms, called the intrinsic term,

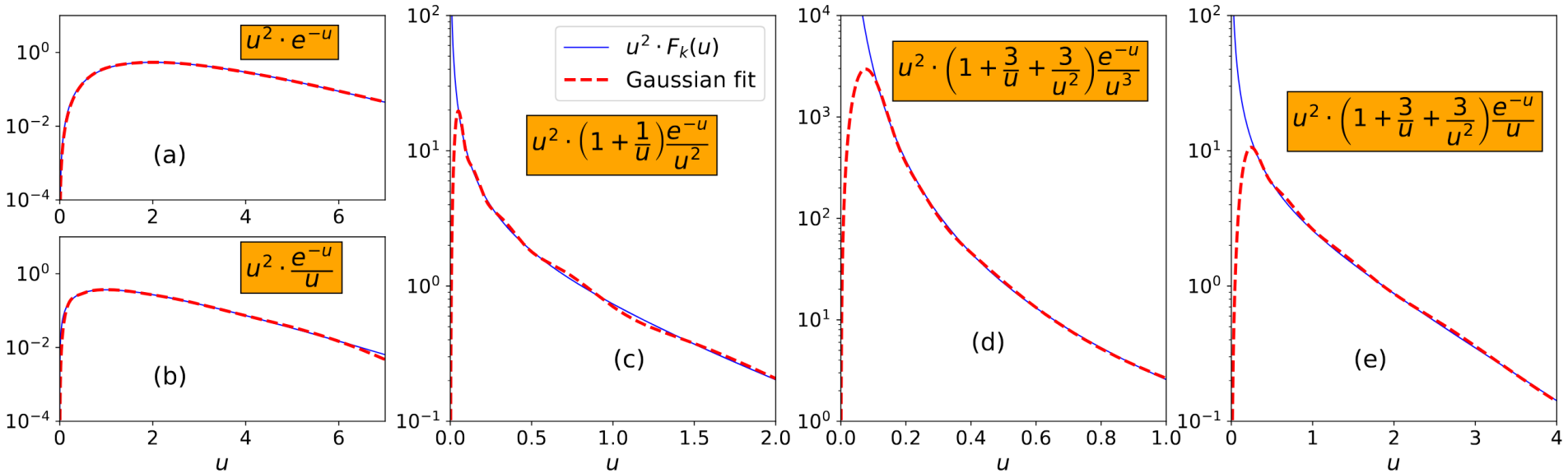
$$\hat{\mu}_{2b}^{\text{int}}(\mathbf{r}_1, \mathbf{r}_2) = -\frac{g_A^2 m_\pi}{32\pi F_\pi^2} (\hat{\boldsymbol{\tau}}_1 \times \hat{\boldsymbol{\tau}}_2)_z \left\{ \left(1 + \frac{1}{u}\right) [(\hat{\boldsymbol{\sigma}}_1 \times \hat{\boldsymbol{\sigma}}_2) \cdot \hat{\mathbf{r}}] \hat{\mathbf{r}} - (\hat{\boldsymbol{\sigma}}_1 \times \hat{\boldsymbol{\sigma}}_2) \right\} e^{-u},$$

and the Sachs term,

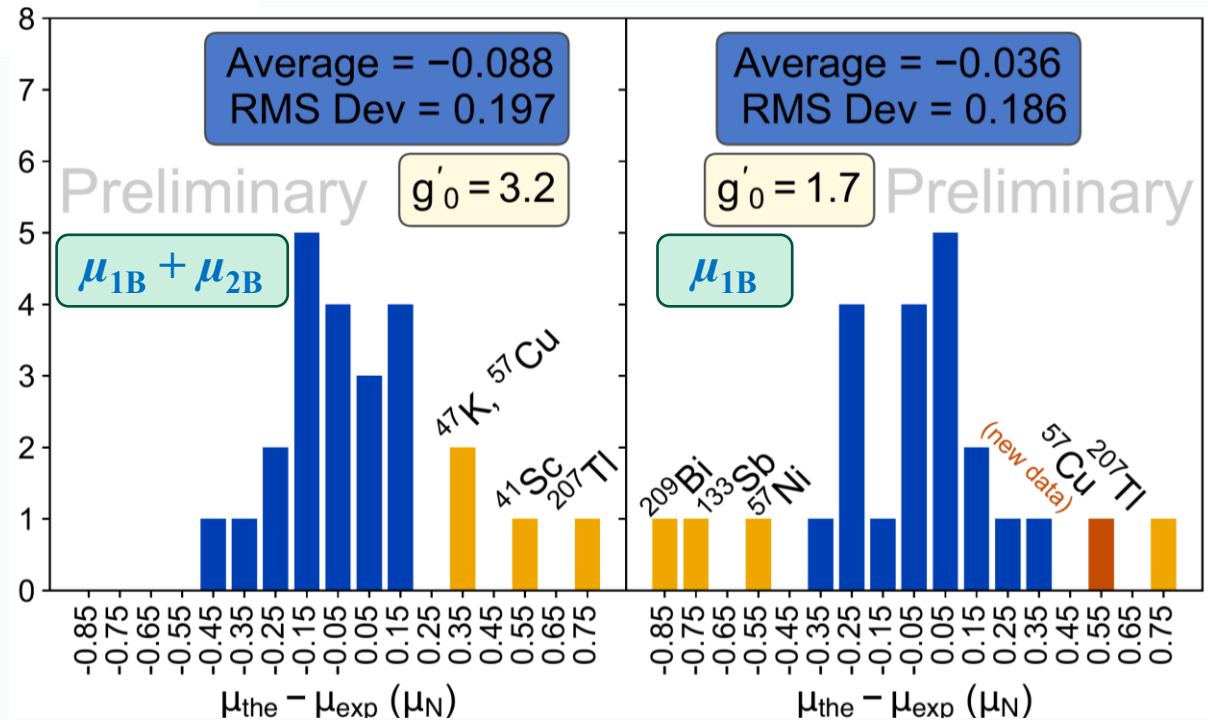
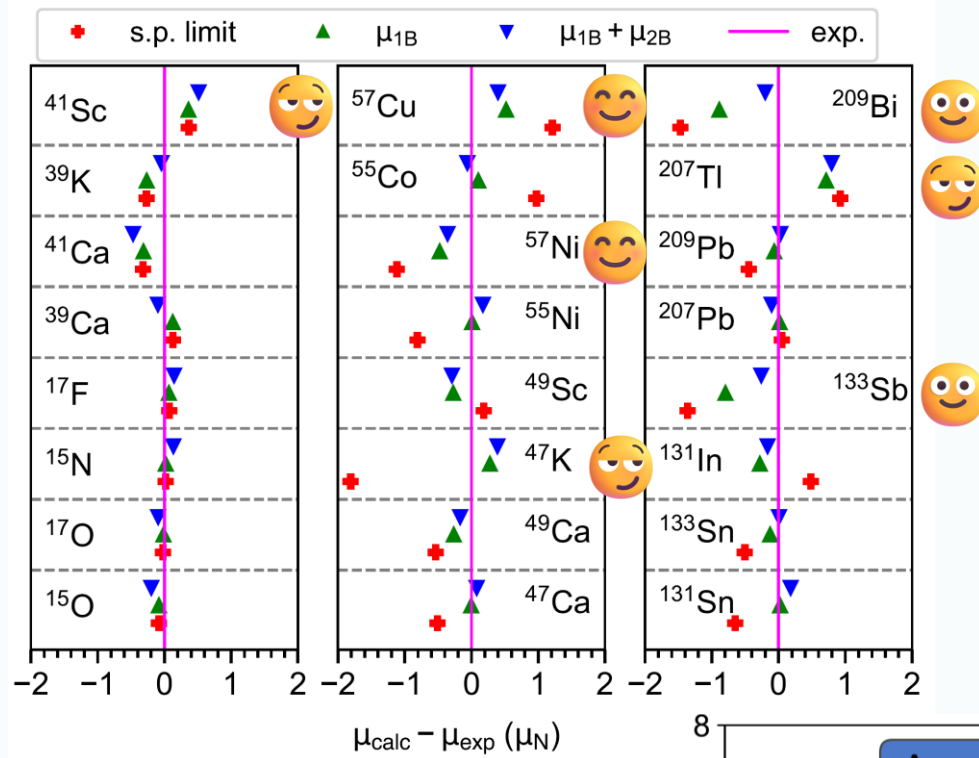
$$\hat{\mu}_{2b}^{\text{Sachs}}(\mathbf{r}_1, \mathbf{r}_2) = -\frac{m_\pi^3 g_A^2}{96\pi F_\pi^2} (\hat{\boldsymbol{\tau}}_1 \times \hat{\boldsymbol{\tau}}_2)_z (\mathbf{R} \times \mathbf{r}) \left[\hat{S}_{12} \left(1 + \frac{3}{u} + \frac{3}{u^2}\right) + \hat{\boldsymbol{\sigma}}_1 \cdot \hat{\boldsymbol{\sigma}}_2 \right] \frac{e^{-u}}{u}.$$

R. Seutin *et al.* [Phys. Rev. C 108 \(2023\) 054005](#); T. Miyagi *et al.* [Phys. Rev. Lett. 132 \(2024\) 232503](#)

H. Wibowo *et al.*, to be published



Meson exchange currents in nuclear DFT



H. Wibowo *et al.*, to be published



Electric dipole moments in nuclear DFT

The nuclear Schiff operator is defined as follows,

$$\hat{S}_z = \frac{e}{10} \sum_p \left(r_p^2 - \frac{5}{3} \langle r^2 \rangle_{\text{ch}} \right) z_p \quad 1.$$

The laboratory Schiff moment, S_z^{lab} , is determined using second-order perturbation theory,

$$S_z^{\text{lab}} \approx \sum_{i \neq 0} \frac{\langle \Psi_0 | \hat{S}_z | \Psi_i \rangle \langle \Psi_i | \hat{V}_{\text{PT}} | \Psi_0 \rangle}{E_0 - E_i} + \text{c.c.}, \quad 2.$$

where $|\Psi_0\rangle$ is the ground state and the sum is over excited states. The P, T -violating NN interaction, $\hat{V}_{\text{PT}}$ reads as follows,

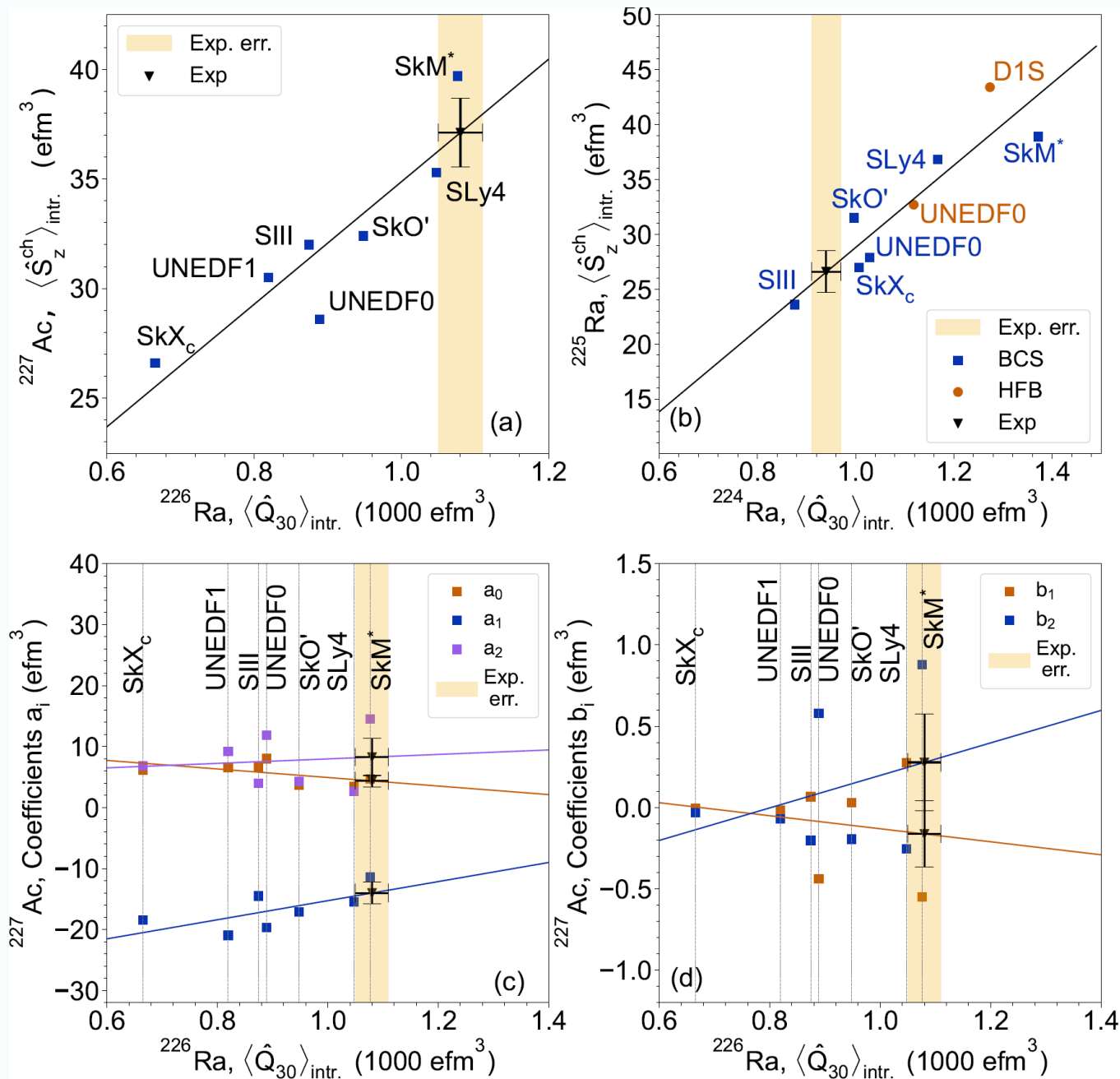
$$\begin{aligned} \hat{V}_{\text{PT}}(\mathbf{r}_1 - \mathbf{r}_2) = & -\frac{gm_\pi^2}{8\pi m_N} \left\{ (\hat{\boldsymbol{\sigma}}_1 - \hat{\boldsymbol{\sigma}}_2) \cdot (\mathbf{r}_1 - \mathbf{r}_2) \left[\bar{g}_0 \hat{\vec{\tau}}_1 \cdot \hat{\vec{\tau}}_2 - \frac{\bar{g}_1}{2} (\hat{\tau}_{1z} + \hat{\tau}_{2z}) + \right. \right. \\ & \left. \left. + \bar{g}_2 (3\hat{\tau}_{1z}\hat{\tau}_{2z} - \hat{\vec{\tau}}_1 \cdot \hat{\vec{\tau}}_2) \right] - \frac{\bar{g}_1}{2} (\hat{\boldsymbol{\sigma}}_1 + \hat{\boldsymbol{\sigma}}_2) \cdot (\mathbf{r}_1 - \mathbf{r}_2) (\hat{\tau}_{1z} - \hat{\tau}_{2z}) \right\} \\ & \times \frac{e^{-m_\pi r}}{m_\pi r^2} \left[1 + \frac{1}{m_\pi r} \right] + \frac{1}{2m_N^3} \left[\bar{c}_1 + \bar{c}_2 \hat{\vec{\tau}}_1 \cdot \hat{\vec{\tau}}_2 \right] (\hat{\boldsymbol{\sigma}}_1 - \hat{\boldsymbol{\sigma}}_2) \cdot \nabla \delta^3(\mathbf{r}_1 - \mathbf{r}_2). \quad 3. \end{aligned}$$

The linearity of $\hat{V}_{\text{PT}}$ allows us to express the laboratory Schiff moment, S_z^{lab} , as a linear combination of the unknown coupling constants with the coefficients calculated in DFT, that is,

$$S_z^{\text{lab}} = a_0 g \bar{g}_0 + a_1 g \bar{g}_1 + a_2 g \bar{g}_2 + b_1 \bar{c}_1 + b_2 \bar{c}_2. \quad 4.$$



Electric dipole moments in nuclear DFT



J. Dobaczewski *et al.*, [Phys. Rev. Lett. 121 \(2018\) 232501](#)

M. Athanasakis-Kaklamanakis *et al.*, [Nature, in press](#)

J. Dobaczewski *et al.*, [arXiv:2511.04632](#)



Anapole moments in nuclear DFT

The nuclear anapole operator is the lowest-order parity non-conservation (PNC), time-reversal-odd multipole operator defined by Haxton, Liu, and Ramsey-Musolf as follows,

$$\hat{a}_\eta = -\frac{M^2}{9} \int d^3\mathbf{r} r^2 \left[\hat{j}_\eta(\mathbf{r}) + \sqrt{2\pi} \left[Y_2(\theta, \phi) \otimes \hat{\mathbf{j}}(\mathbf{r}) \right]_{1\eta} \right], \quad 5.$$

Analogous to the laboratory Schiff moment, S_z^{lab} , the laboratory anapole moment is

$$a_z^{\text{lab}} \approx \sum_{i \neq 0} \frac{\langle \Psi_0 | \hat{a}_z | \Psi_i \rangle \langle \Psi_i | \hat{V}_{\text{PNC}} | \Psi_0 \rangle}{E_0 - E_i} + \text{c.c.}, \quad 6.$$

where $\hat{V}_{\text{PNC}}$ is used in the form of the Desplanques Donoghue, and Holstein (DDH) potential, and has the form as follows,

$$\begin{aligned} \hat{V}^{\text{DDH}}(\mathbf{r}) = & \frac{i}{2\sqrt{2}} h_\pi^1 g_{\pi NN} (\hat{\boldsymbol{\tau}}_1 \times \hat{\boldsymbol{\tau}}_2)_z (\hat{\boldsymbol{\sigma}}_1 + \hat{\boldsymbol{\sigma}}_2) \cdot \frac{1}{2M} [\hat{\mathbf{p}}_1 - \hat{\mathbf{p}}_2, \omega_\pi(r)] \\ & - g_\rho \left(h_\rho^0 \hat{\boldsymbol{\tau}}_1 \cdot \hat{\boldsymbol{\tau}}_2 + \frac{1}{2} h_\rho^1 (\hat{\boldsymbol{\tau}}_1 + \hat{\boldsymbol{\tau}}_2)_z + \frac{1}{2\sqrt{6}} h_\rho^2 (3\hat{\tau}_{1z}\hat{\tau}_{2z} - \hat{\boldsymbol{\tau}}_1 \cdot \hat{\boldsymbol{\tau}}_2) \right) \\ & \times \frac{1}{2M} \left((\hat{\boldsymbol{\sigma}}_1 - \hat{\boldsymbol{\sigma}}_2) \cdot \{ \hat{\mathbf{p}}_1 - \hat{\mathbf{p}}_2, \omega_\rho(r) \} + i(1 + \chi_V) (\hat{\boldsymbol{\sigma}}_1 \times \hat{\boldsymbol{\sigma}}_2) \cdot [\hat{\mathbf{p}}_1 - \hat{\mathbf{p}}_2, \omega_\rho(r)] \right) \\ & - g_\omega \left(h_\omega^0 + \frac{1}{2} h_\omega^1 (\hat{\boldsymbol{\tau}}_1 + \hat{\boldsymbol{\tau}}_2)_z \right) \\ & \times \frac{1}{2M} \left((\hat{\boldsymbol{\sigma}}_1 - \hat{\boldsymbol{\sigma}}_2) \cdot \{ \hat{\mathbf{p}}_1 - \hat{\mathbf{p}}_2, \omega_\omega(r) \} + i(1 + \chi_S) (\hat{\boldsymbol{\sigma}}_1 \times \hat{\boldsymbol{\sigma}}_2) \cdot [\hat{\mathbf{p}}_1 - \hat{\mathbf{p}}_2, \omega_\omega(r)] \right) \\ & + \frac{1}{2} (\hat{\boldsymbol{\tau}}_1 - \hat{\boldsymbol{\tau}}_2)_z (\hat{\boldsymbol{\sigma}}_1 + \hat{\boldsymbol{\sigma}}_2) \cdot \frac{1}{2M} \left(g_\rho h_\rho^1 \{ \hat{\mathbf{p}}_1 - \hat{\mathbf{p}}_2, \omega_\rho(r) \} - g_\omega h_\omega^1 \{ \hat{\mathbf{p}}_1 - \hat{\mathbf{p}}_2, \omega_\omega(r) \} \right) \\ & - \frac{i}{2} g_\rho h_\rho^{1'} (\hat{\boldsymbol{\tau}}_1 \times \hat{\boldsymbol{\tau}}_2)_z (\hat{\boldsymbol{\sigma}}_1 + \hat{\boldsymbol{\sigma}}_2) \cdot \frac{1}{2M} [\hat{\mathbf{p}}_1 - \hat{\mathbf{p}}_2, \omega_\rho(r)]. \quad 7. \end{aligned}$$

W.C. Haxton *et al.*, [Phys. Rev. C 65 \(2002\) 045502](#)

B. Desplanques *et al.*, [Ann. Phys. 124 \(1980\) 449](#)

J. Dobaczewski *et al.*, [arXiv:2511.04632](#)



Conclusions

1. For the first time, in nuclear theory, we can systematically **calculate spectroscopic electromagnetic moments** in odd open-shell nuclei with arbitrary particle numbers and (axial) deformations.
2. Large nuclear-DFT single-particle phase space (well beyond the valence space) allows for using the **bare effective charges and g-factors**. (No adjustable “effective” values are needed.)
3. The calculated **magnetic dipole moments μ and electric quadrupole moments Q** reproduce the known experimental data in heavy open-shell nuclei.
4. It is essential to take into account **simultaneously**:
 - a) **Self-consistency**
 - b) **Polarization**
 - c) **Symmetry restoration**
5. The effects of the extended T-odd sector, triaxiality, octupolarity, two-body currents, K-mixing, and configuration interaction (...) **remain to be studied**.



Thank you

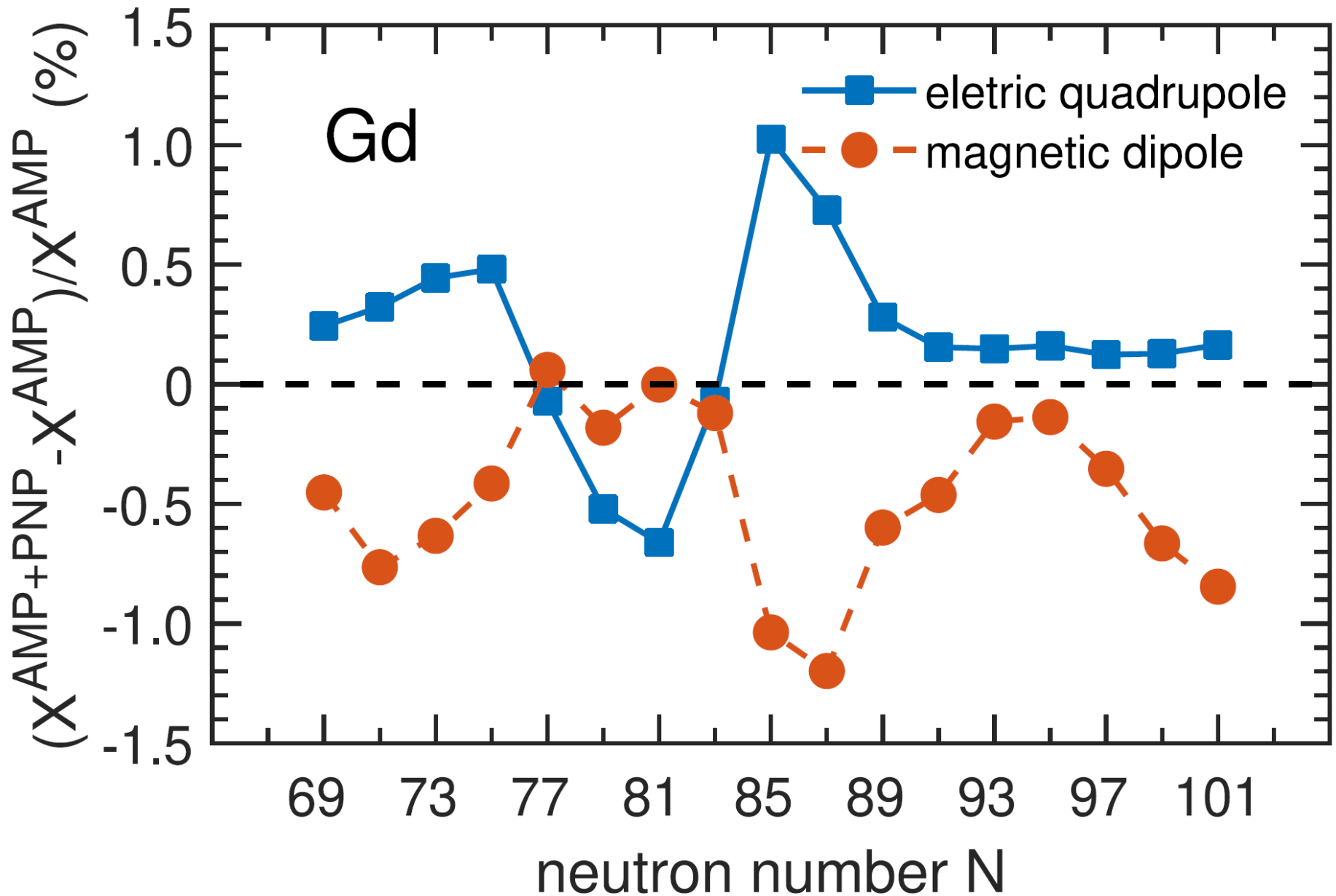


Recent publications:

1. Nuclear DFT analysis of electromagnetic moments in odd near doubly magic nuclei:
P.L. Sassarini, J. Dobaczewski, J. Bonnard, R.F. Garcia Ruiz
[J. Phys. G 49 \(2022\) 11LT01](#)
2. Nuclear DFT electromagnetic moments in heavy deformed open-shell odd nuclei:
J. Bonnard, J. Dobaczewski, G. Danneaux, M. Kortelainen
[Phys. Lett. B843 \(2023\) 138014](#)
3. Electromagnetic moments in the Sn-Gd region determined within the nuclear DFT:
H. Wibowo, B.C. Backes, J. Dobaczewski, R.P. de Groote, A. Nagpal, A. Sánchez-Fernández, X. Sun, J. L. Wood
[J. Phys. G 52 \(2025\) 065104](#)
4. Electromagnetic moments of ground and excited states calculated in heavy odd-N openshell nuclei:
J. Dobaczewski, A.E. Stuchbery, G. Danneaux, A. Nagpal, P.L. Sassarini, H. Wibowo
[arXiv:2509.26549, submitted to Physical Review C](#)
5. Electromagnetic and exotic moments in nuclear DFT:
J. Dobaczewski, B.C. Backes R.P. de Groote, A. Restrepo-Giraldo, X. Sun and H. Wibowo
[arXiv:2511.04632, submitted to Annual Review of Nuclear and Particle Science](#)
6. Nuclear DFT meson-exchange contributions to magnetic dipole moments of atomic nuclei:
H. Wibowo, R. Han, B.C. Backes, G. Danneaux, J. Dobaczewski, W.C. Haxton, W. Jiang, and M. Kortelainen, to be published
7. Extraction of ground-state nuclear deformations from ultra-relativistic heavy-ion collisions: Nuclear structure physics context:
J. Dobaczewski, A. Gade, K. Godbey, R. V. F. Janssens, W. Nazarewicz
[Phys. Rev. Res. 7 \(2025\) 043159](#)



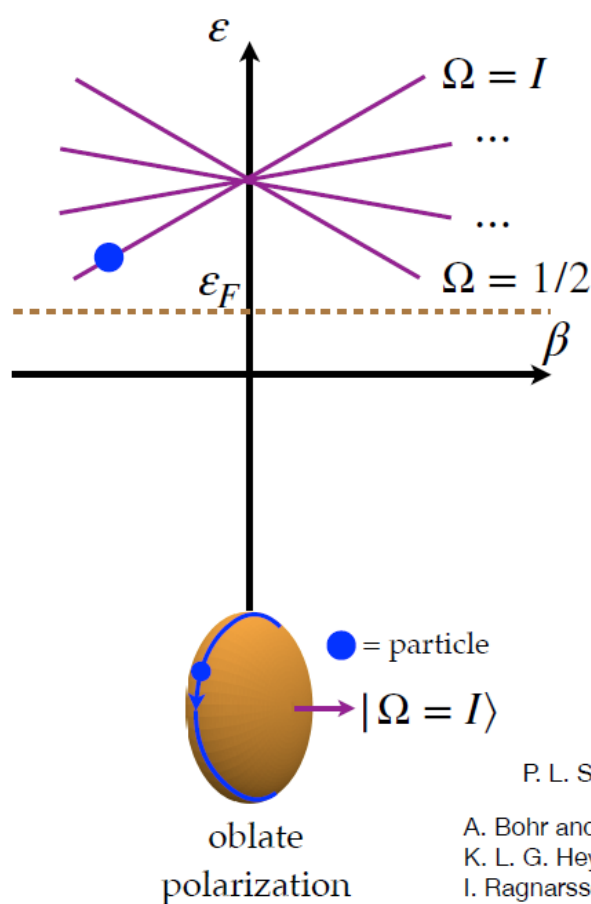
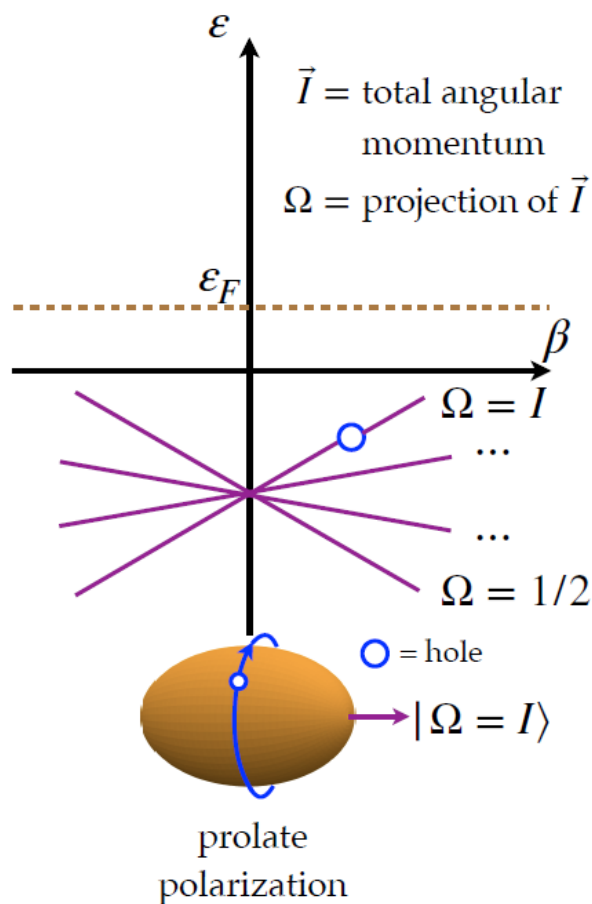
Particle-number symmetry restoration (PNP) is not worth the $100 \times$ increase in CPU time



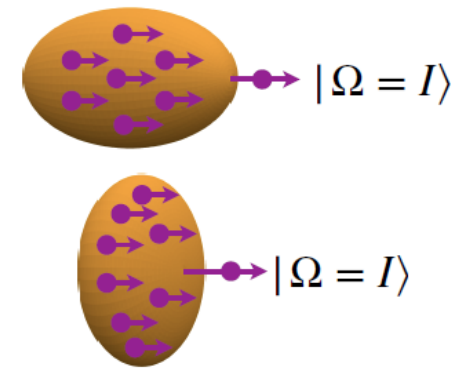
H. Wibowo *et al.*, J. Phys. G 52 (2025) 065104



Shape and spin polarization



Spin polarization



Landau parameter g'_0 ($g'_0 = 1.7$)

$$g'_0 = N_0 (2C_1^S + 2C_1^T (3\pi^2 \rho_0 / 2)^{2/3})$$

$$\frac{1}{N_0} \approx 150 \frac{m}{m^*} \text{ MeV} \cdot \text{fm}^3$$

P. L. Sassarini et al., J. Phys. G: Nucl. Part. Phys. **49**, 11LT01 (2022)

A. Bohr and B. R. Mottelson, *Nuclear Structure* Vol. 1

K. L. G. Heyde, *The Nuclear Shell Model*

I. Ragnarsson and S. G. Nilsson, *Shapes and Shells in Nuclear Structure*

Picture courtesy of H. Wibowo

In nuclear-DFT, we align the total angular momenta of odd nuclei along the intrinsic axial-symmetry axis with broken spherical and time-reversal symmetries. We fully account for the self-consistent charge, spin, and current polarizations, in particular through the inclusion of the crucial time-odd mean-field components of the functional.



Jacek Dobaczewski

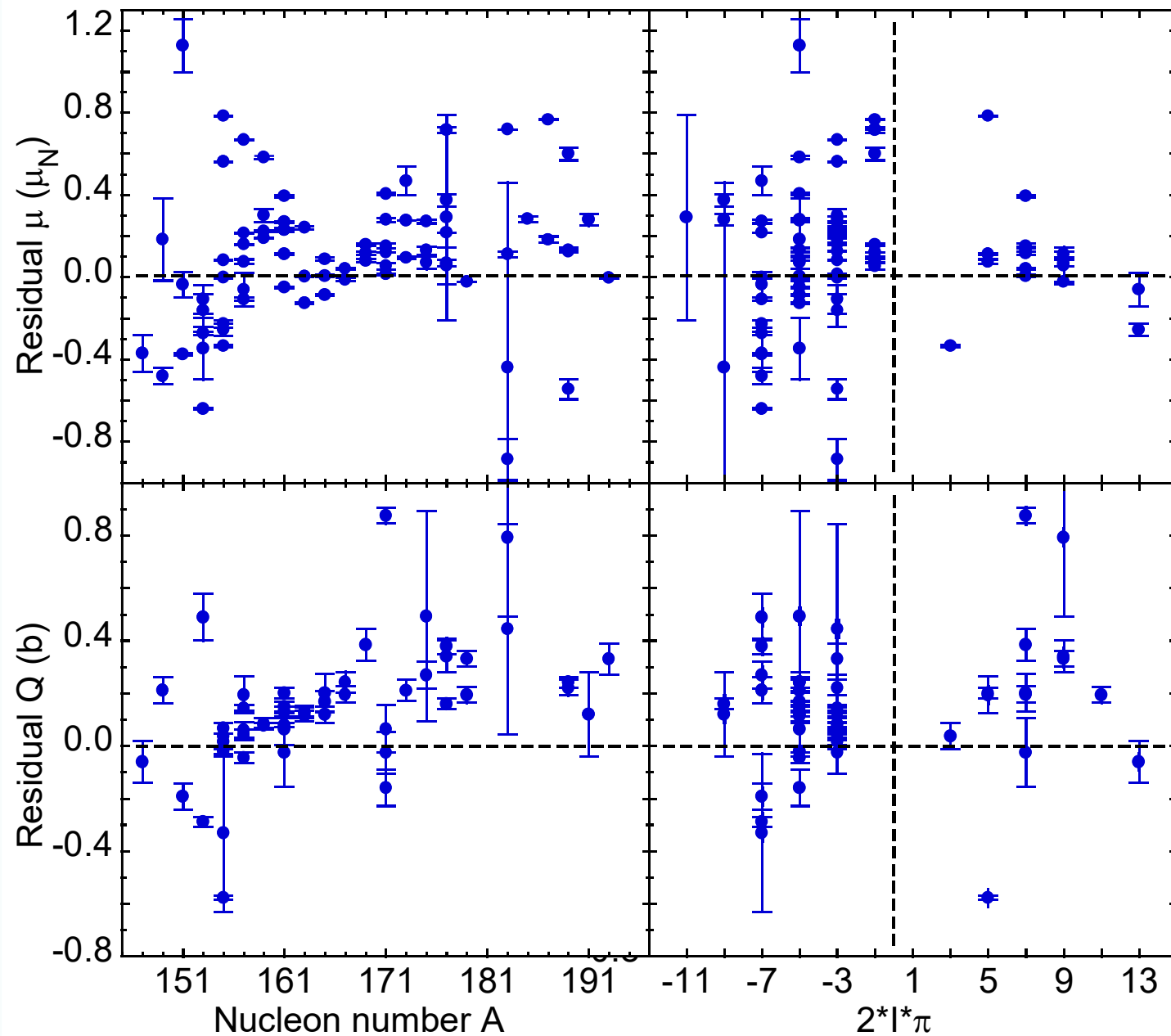
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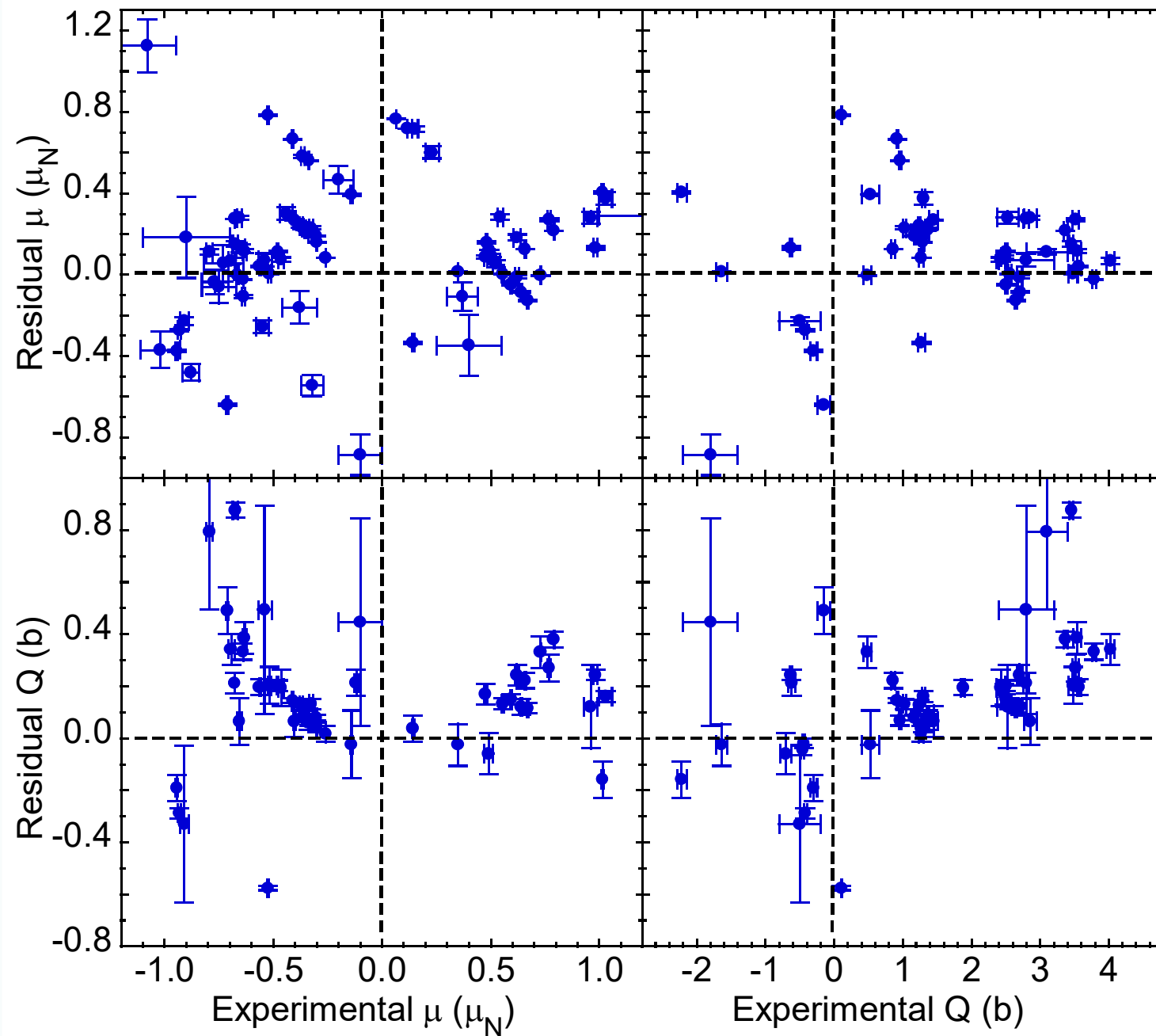
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Correlation of residuals with A and $2 \cdot I \cdot \pi$



Correlation of residuals with μ and Q



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Schmidt limits

The magnetic operator $\bar{\mu}$ is a one-body operator and the magnetic dipole moment μ is the expectation value of $\bar{\mu}_z$. The M1 operator acting on a composed state $|Im\rangle$ can then be written as the sum of single particle M1 operators $\bar{\mu}_z(j)$ acting each on an individual valence nucleon with total momentum j :

$$\mu = g_L \mathbf{L} + g_s \mathbf{s}$$

$$\mu(I) \equiv \left\langle I(j_1, j_2, \dots, j_n), m = I \left| \sum_{i=1}^n \bar{\mu}_z(i) \right| I(j_1, j_2, \dots, j_n), m = I \right\rangle \quad (2.1)$$

The single particle magnetic moment $\mu(j)$ for a valence nucleon around a doubly magic core is uniquely defined by the quantum numbers l and j of the occupied single particle orbit [22]:

$$\text{for an odd proton: } \left\{ \begin{array}{ll} \mu = j - \frac{1}{2} + \mu_p & \text{for } j = l + \frac{1}{2} \\ \mu = \frac{j}{j+1} \left(j + \frac{3}{2} - \mu_p \right) & \text{for } j = l - \frac{1}{2} \end{array} \right. \quad (2.2)$$

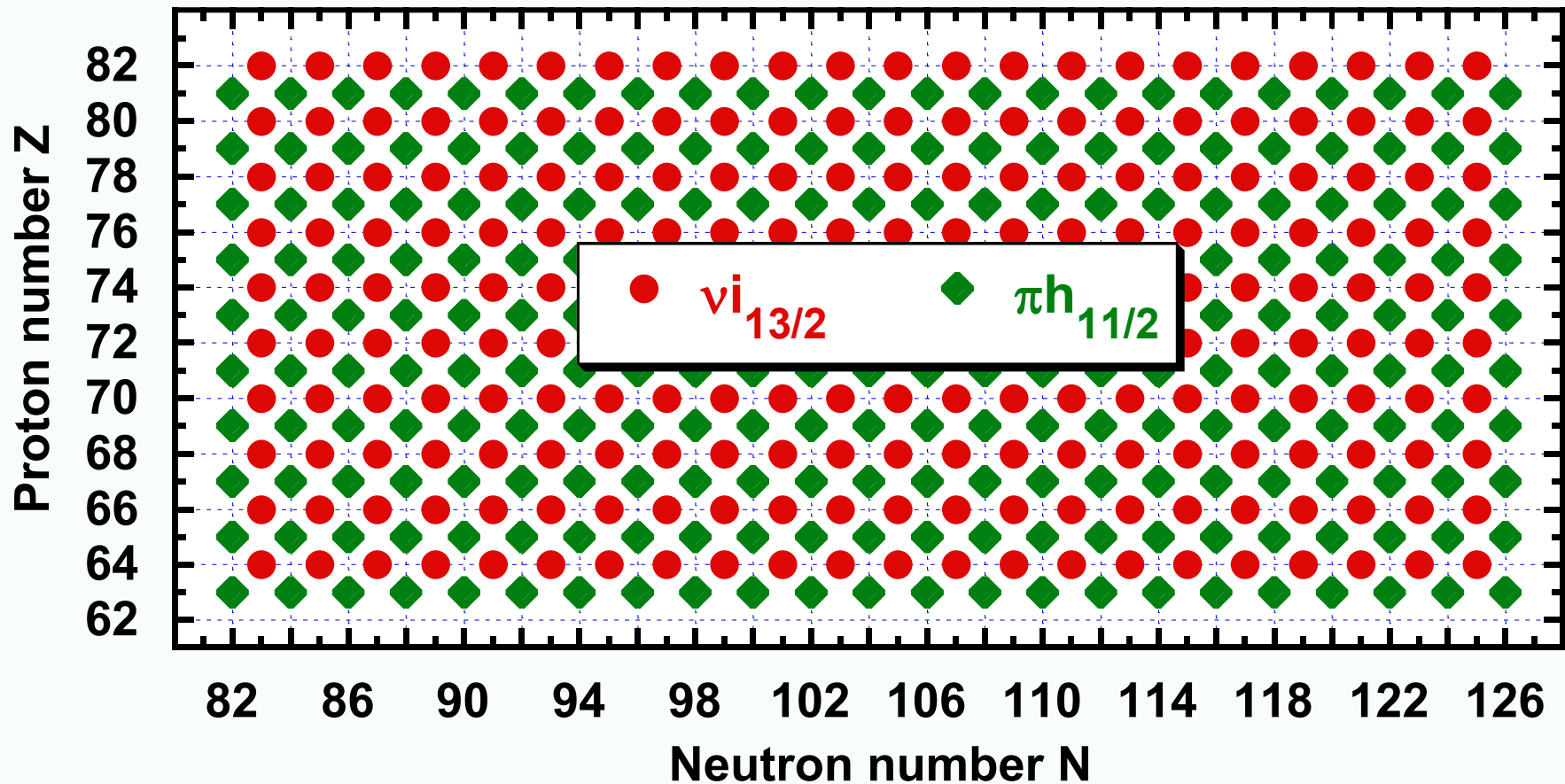
$$\text{for an odd neutron: } \left\{ \begin{array}{ll} \mu = \mu_n & \text{for } j = l + \frac{1}{2} \\ \mu = -\frac{j}{j+1} \mu_n & \text{for } j = l - \frac{1}{2} \end{array} \right. \quad (2.3)$$

**Schmidt
limits**

These single particle moments calculated using the free proton and free neutron moments ($\mu_p = +2.793$, $\mu_n = -1.913$) are called the Schmidt moments. In a nucleus, the magnetic



The first systematic nuclear-DFT analysis of the electromagnetic moments in heavy deformed open-shell odd nuclei



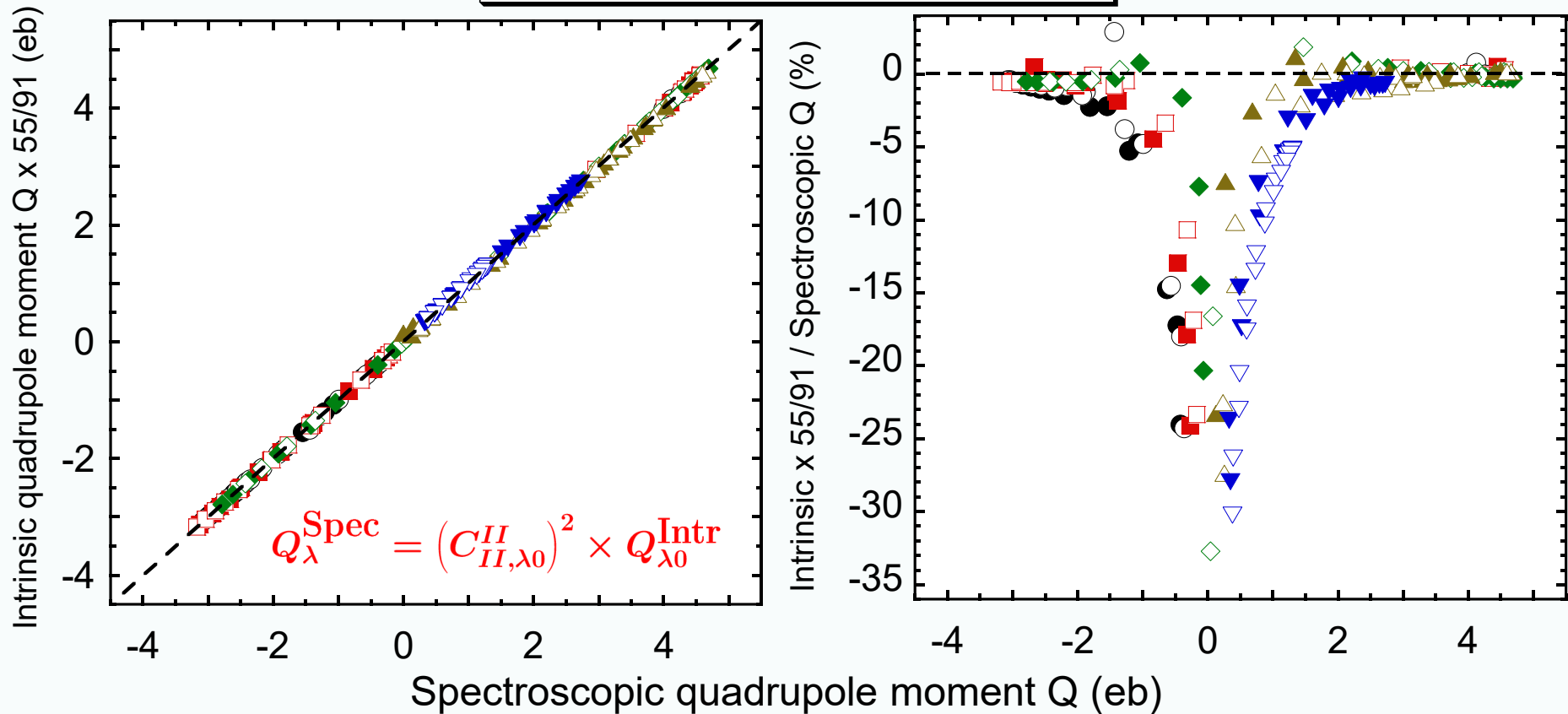
Blocked quasiparticles were tagged by the neutron $i_{13/2}$ ($\Omega=+13/2$) or proton $h_{11/2}$ ($\Omega=+11/2$) single-particle orbitals

J. Bonnard *et al.*, Phys. Lett. B 843 (2023) 138014



Heavy deformed $\pi 11/2^-$ odd-Z nuclei

J. Bonnard *et al.*, Phys. Lett. B 843 (2023) 138014



Conclusion:

Spectroscopic electric quadrupole moments can be inferred from the intrinsic ones at $\sim 5\%$ precision only at $|Q| > 1b$



Jacek Dobaczewski

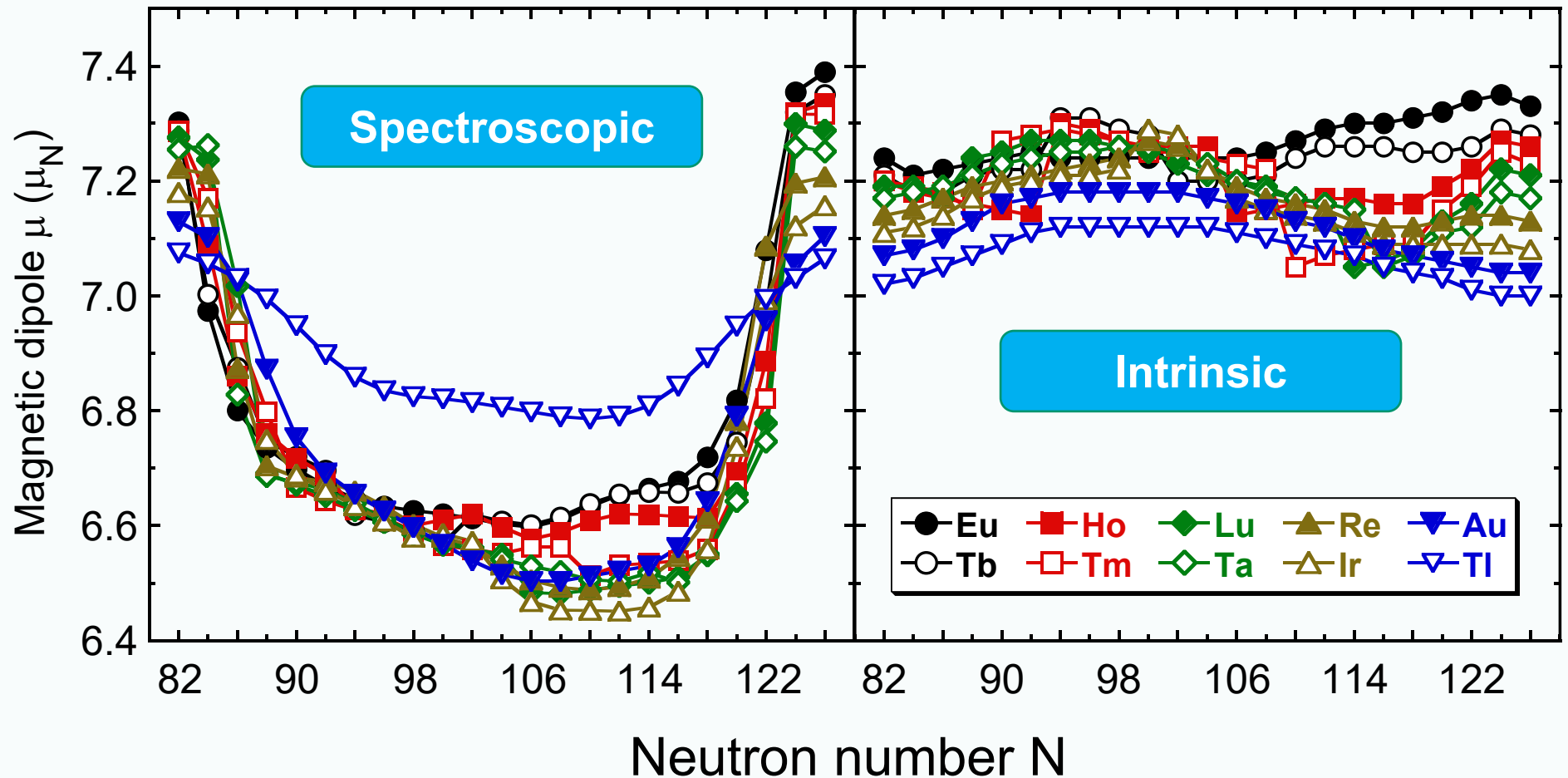
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Heavy deformed $\pi 11/2^-$ odd-Z nuclei

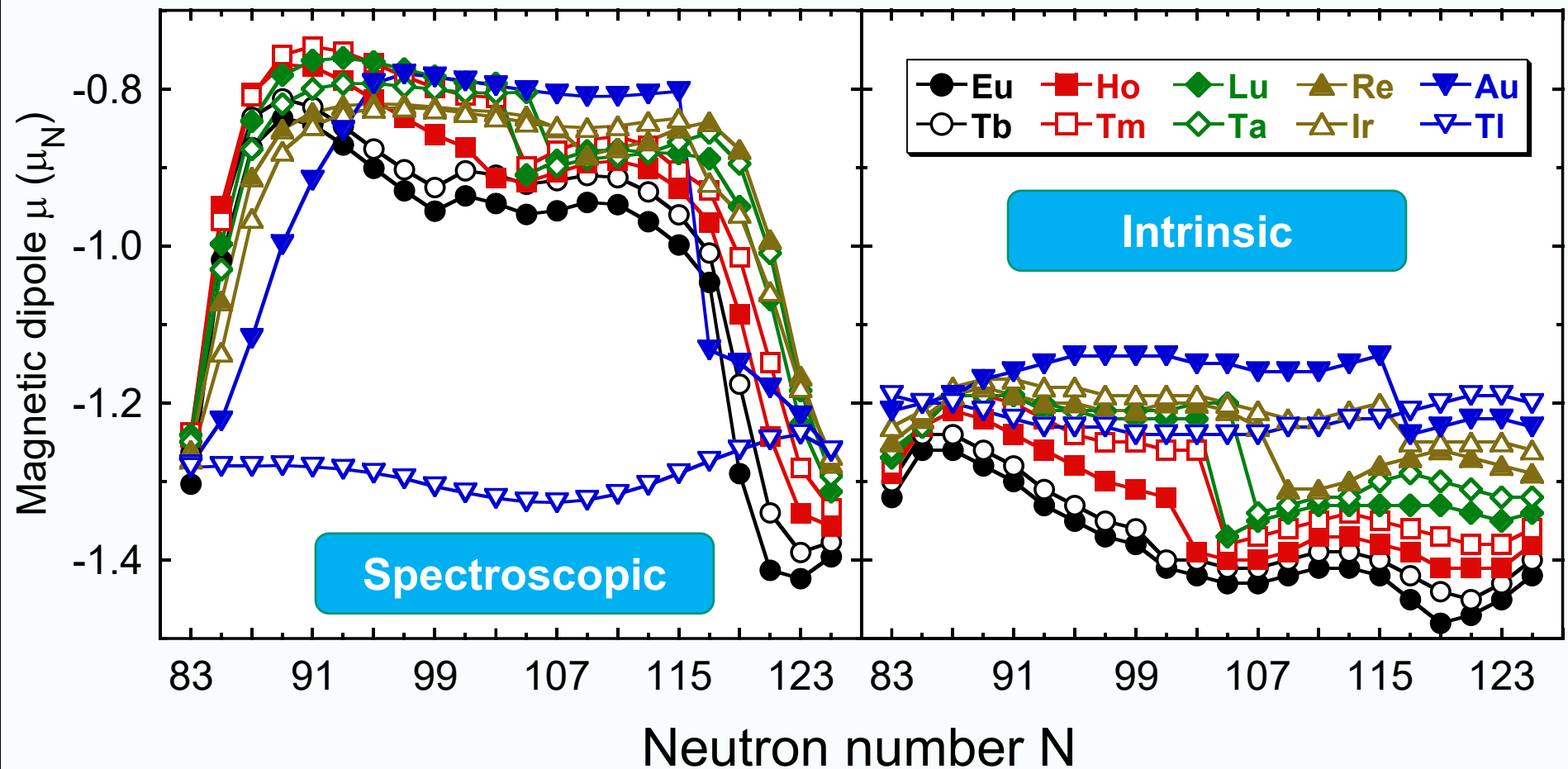


Conclusion:

Spectroscopic magnetic dipole moments cannot be inferred from the intrinsic ones



Heavy deformed $\nu 13/2^+$ odd-N nuclei

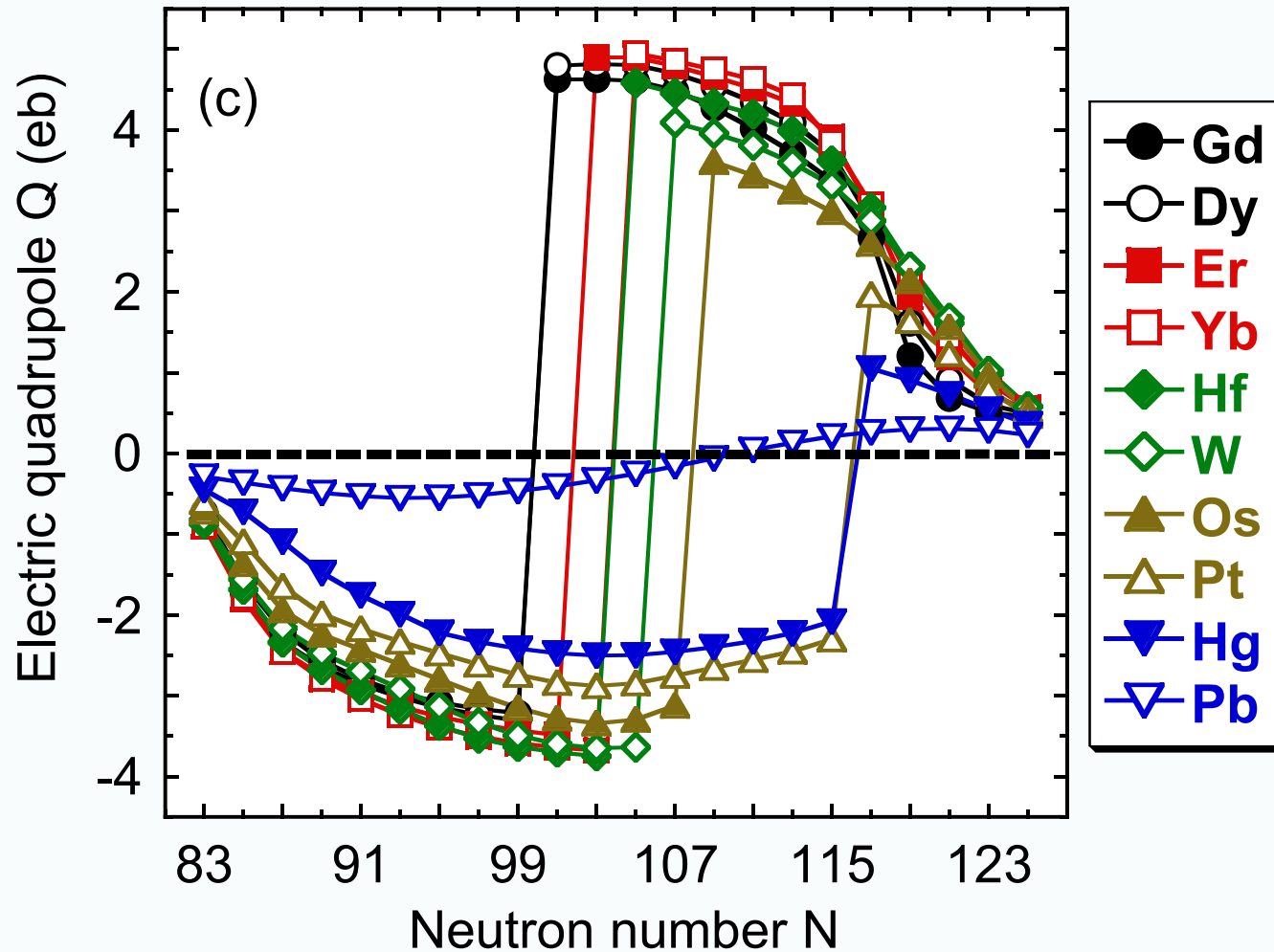


Conclusion:

Spectroscopic magnetic dipole moments cannot be inferred from the intrinsic ones



Heavy deformed $v13/2^+$ odd-N nuclei

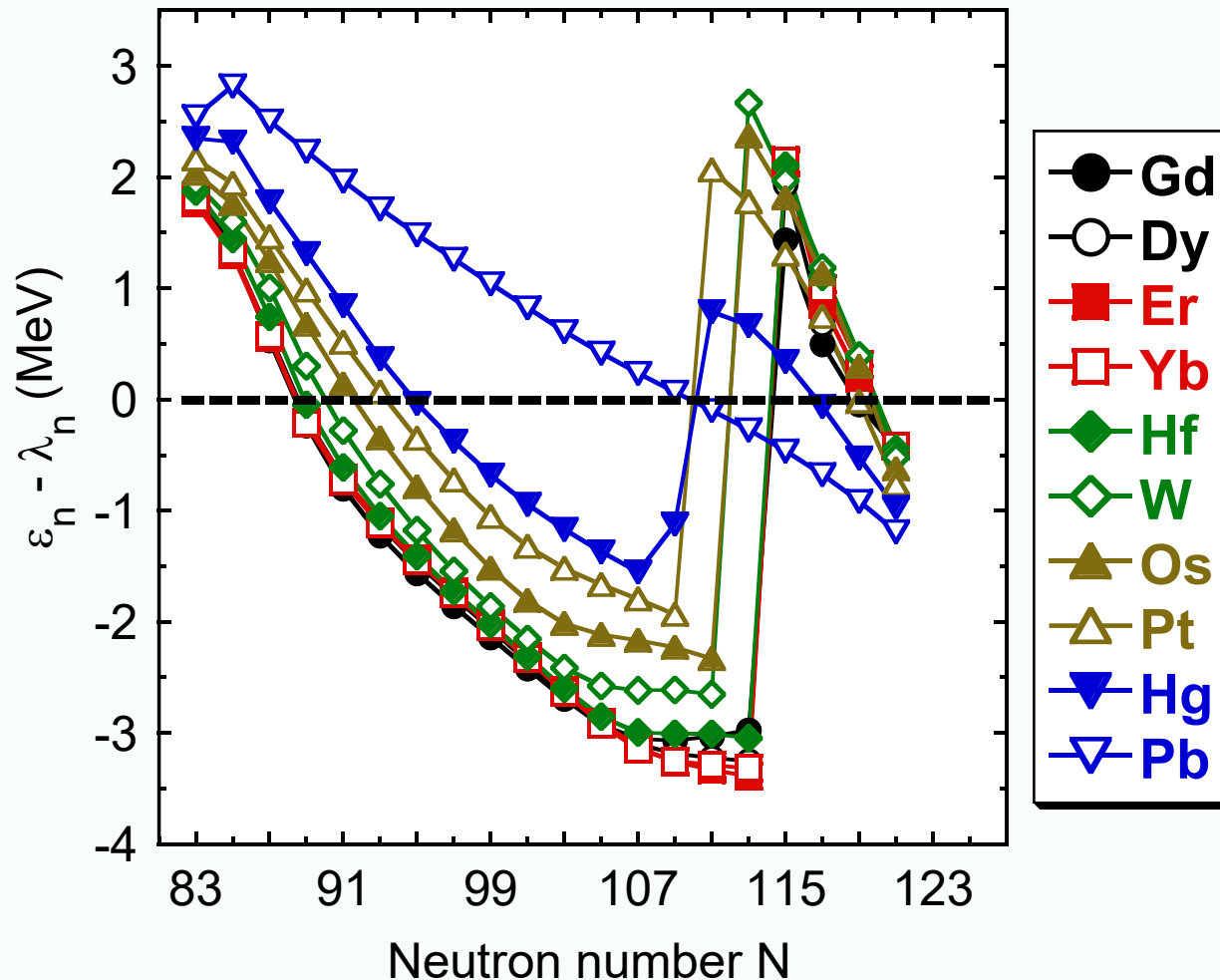


Conclusion:

Rules of oblate and prolate polarizations do extend from the magicity towards the open shell systems.



Heavy deformed $v13/2^+$ odd-N nuclei



Conclusion:

Rules of particle and hole polarizations do not extend from the magicity towards the open shell systems.



J. Bonnard *et al.*, Phys. Lett. B 843 (2023) 138014

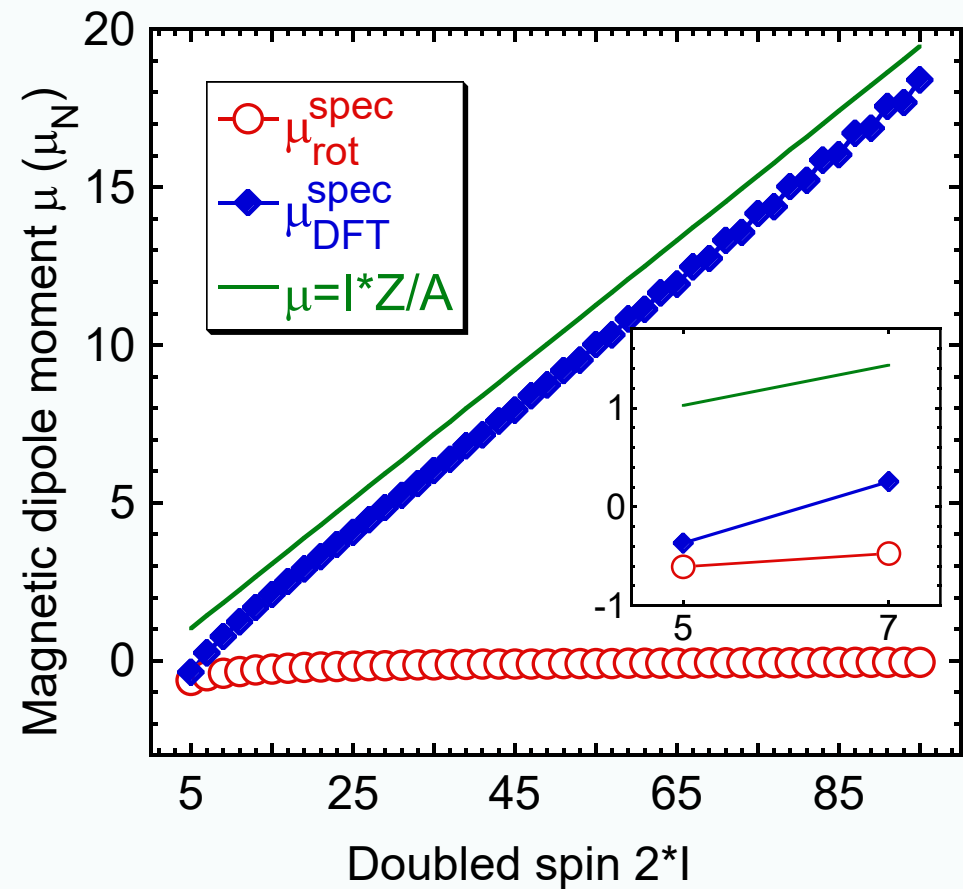
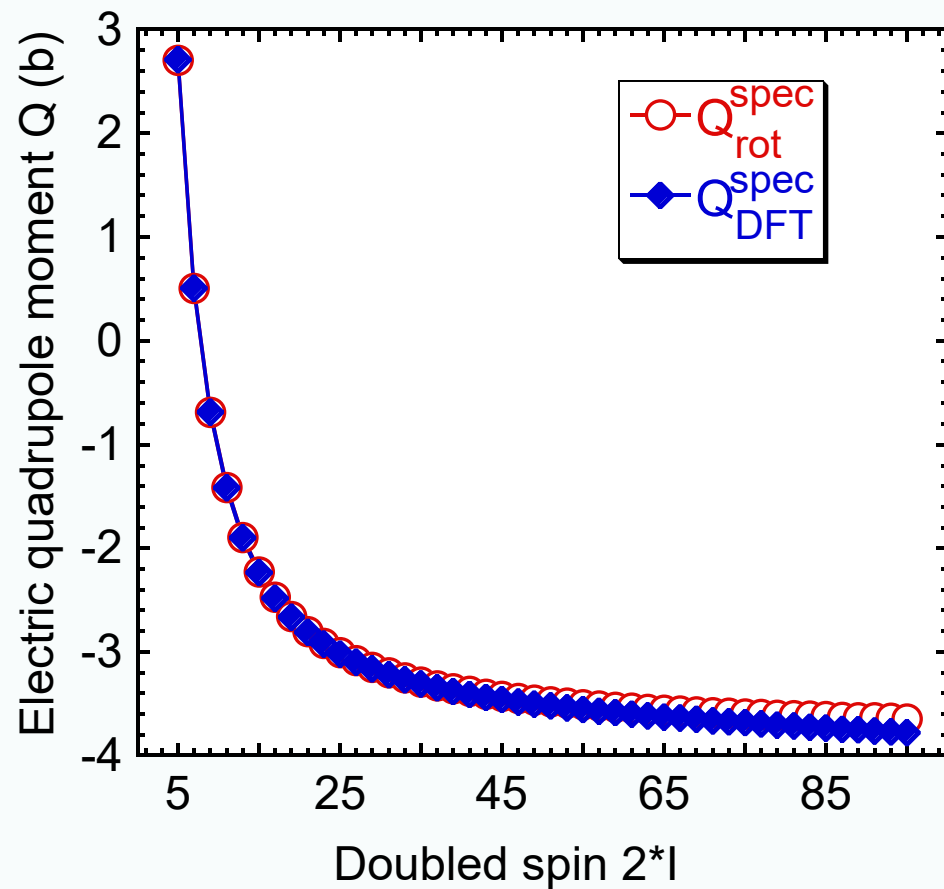


Electromagnetic moments – the rigid-rotor approximation

$^{161}\text{Dy } 5/2^+ \text{ UNEDF1, } g'_0=1.7$

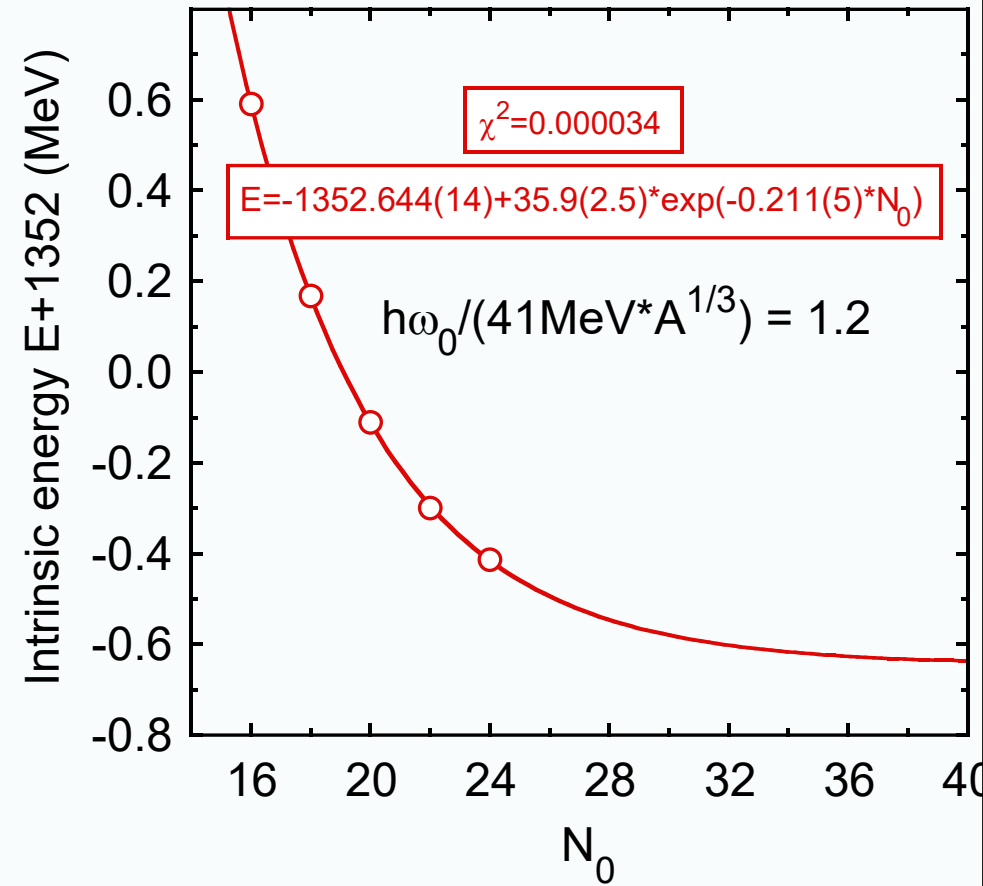
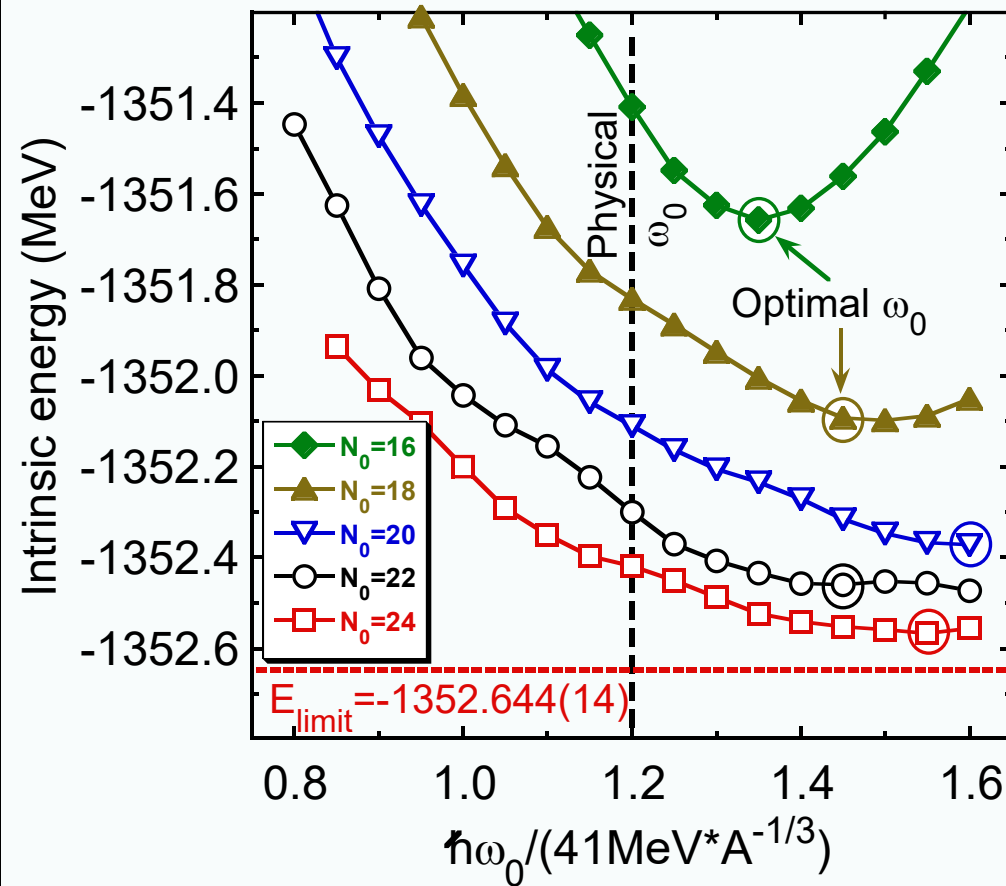
$$Q_{\text{rot}}^{\text{spec}} = Q_{20}^{\text{intr}} \times C_{\text{II},20}^{\text{II}} \times C_{\text{IK},20}^{\text{IK}}$$

$$\mu_{\text{rot}}^{\text{spec}} = \mu_z^{\text{intr}} \times C_{\text{II},10}^{\text{II}} \times C_{\text{IK},10}^{\text{IK}}$$



Convergence of the total HFB intrinsic energy

$^{167}\text{Ho } 11/2^-, \text{ UNEDF1, } g'_0=1.7$

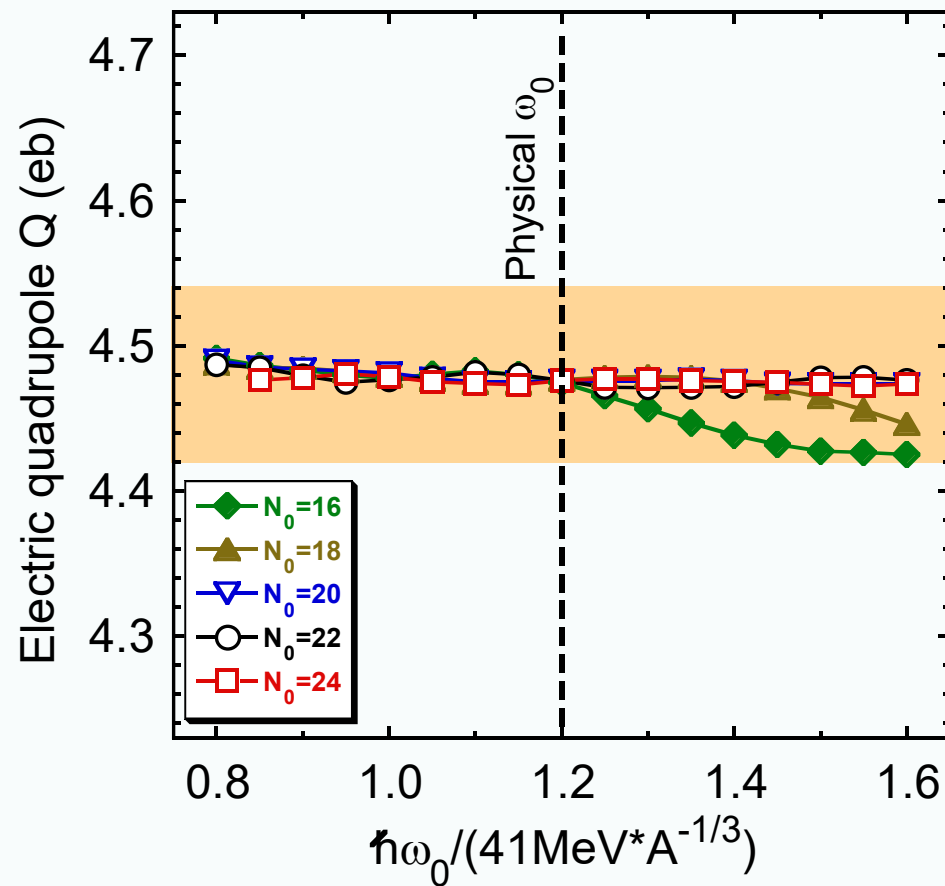
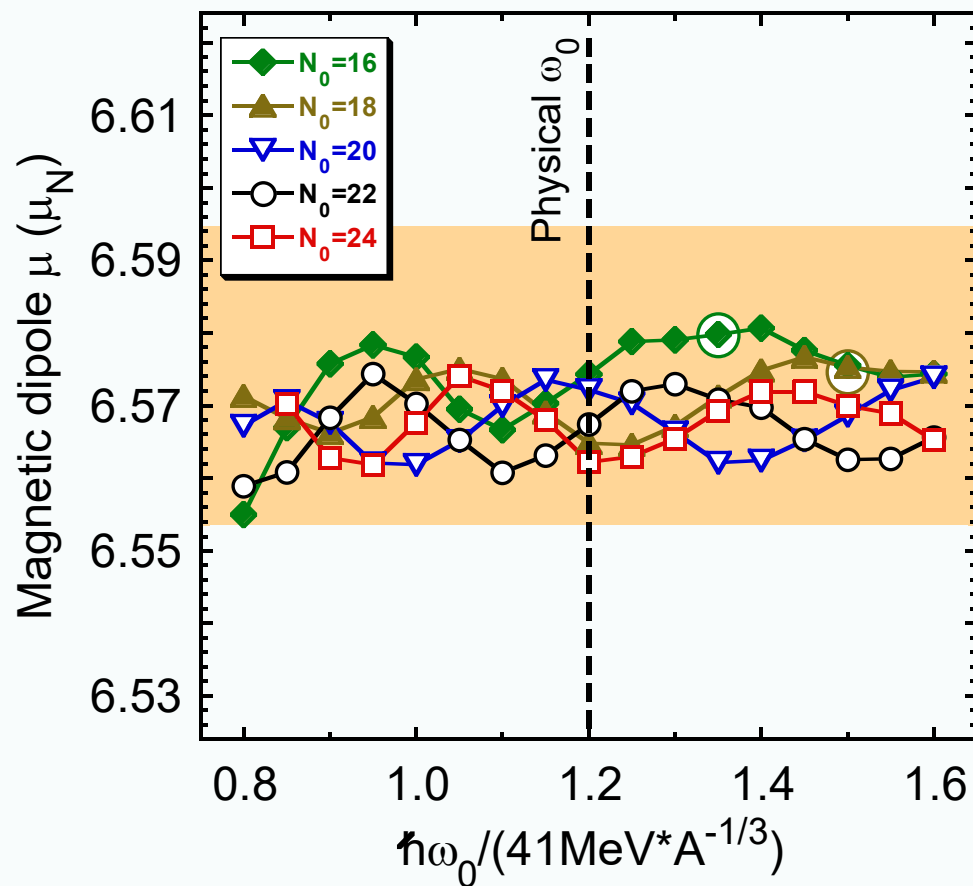


$E_{\text{exp}} = -1357.77346$

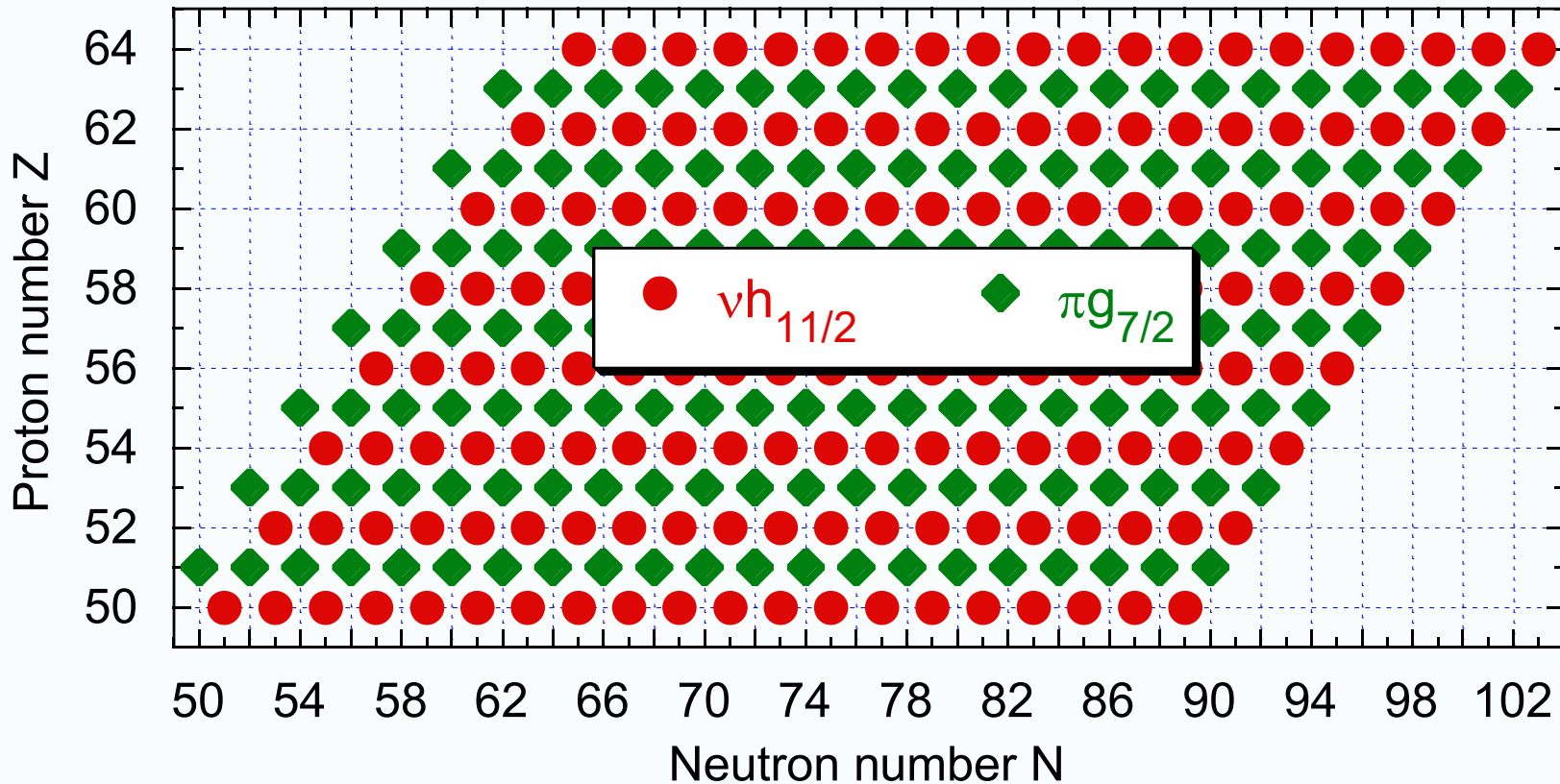


Convergence of the spectroscopic moments

^{167}Ho 11/2-, UNEDF1, $g'_0=1.7$



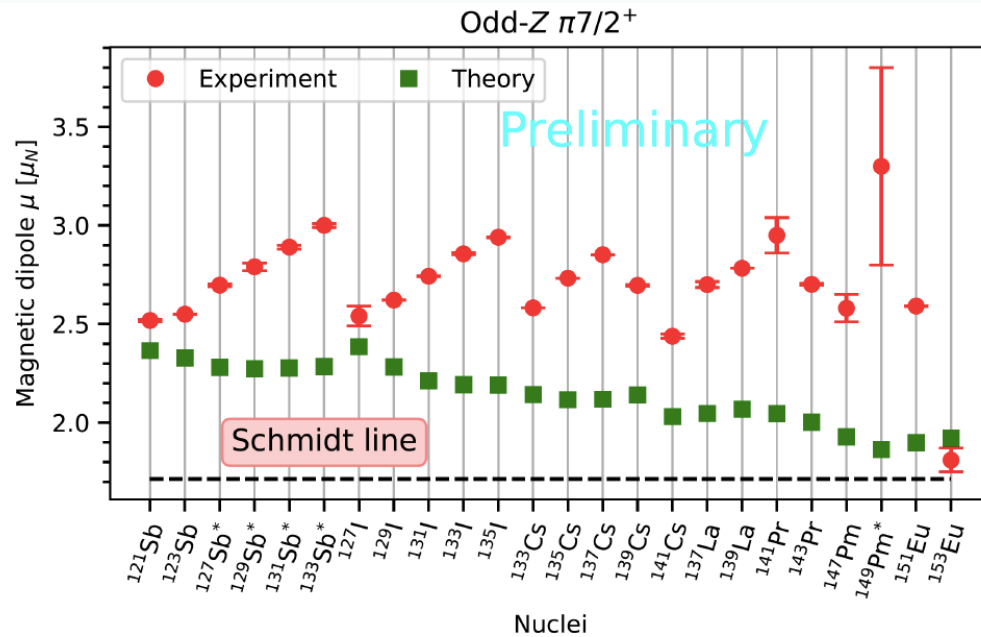
Nuclear-DFT analysis of electromagnetic moments between the Sn and Gd isotopes



H. Wibowo *et al.*, to be published

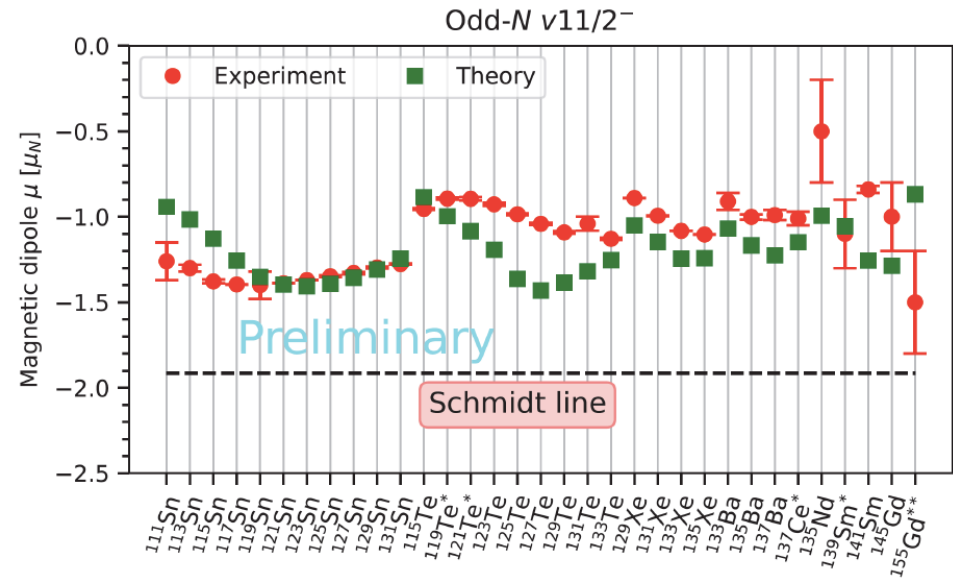


Magnetic dipole moments: theory vs. experiment



N. J. Stone, *Table of nuclear magnetic dipole and electric quadrupole moments* (2014), INDC, report INDC(NDS)-0658

Schmidt lines represent the value of magnetic dipole moment of an odd-mass nucleus which is completely determined by the ℓ and j values of the unpaired nucleon (single-particle model).

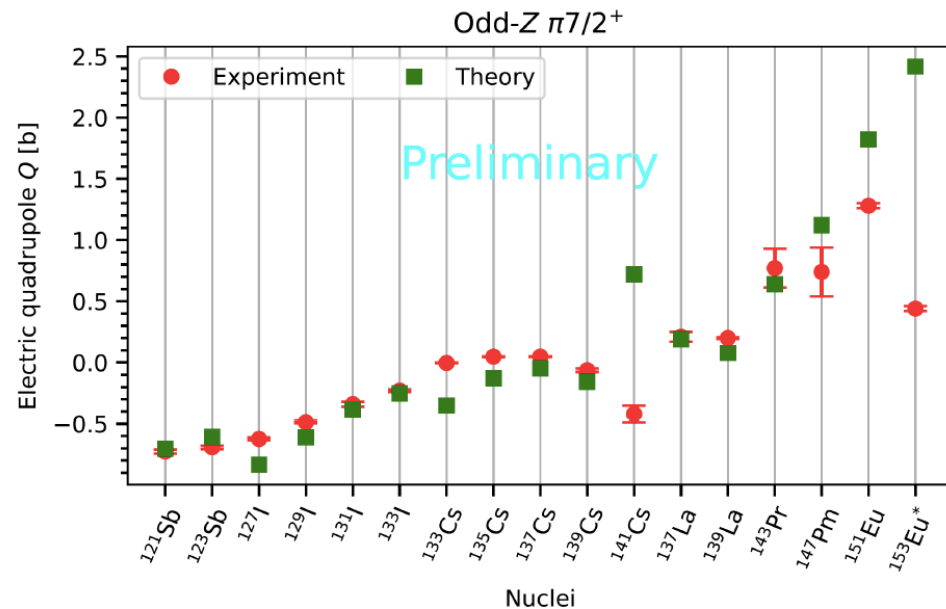


Picture: courtesy H. Wibowo

H. Wibowo *et al.*, to be published

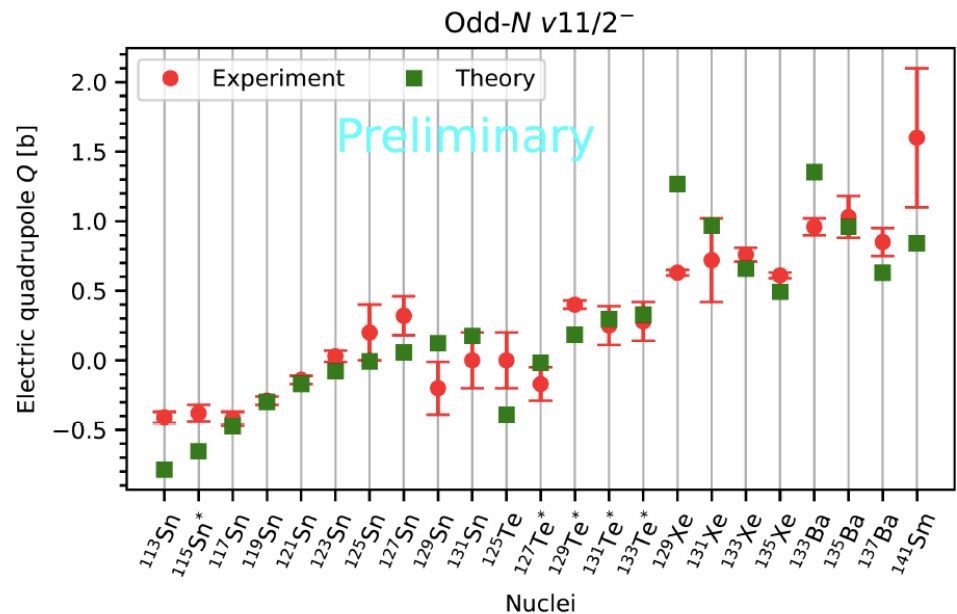


Quadrupole moments: theory vs. experiment



N. J. Stone, *Table of nuclear magnetic dipole and electric quadrupole moments* (2014), INDC, report INDC(NDS)-0658

N. J. Stone, *Table of nuclear electric quadrupole moments*, ADNDT 111-112, 1 (2016)

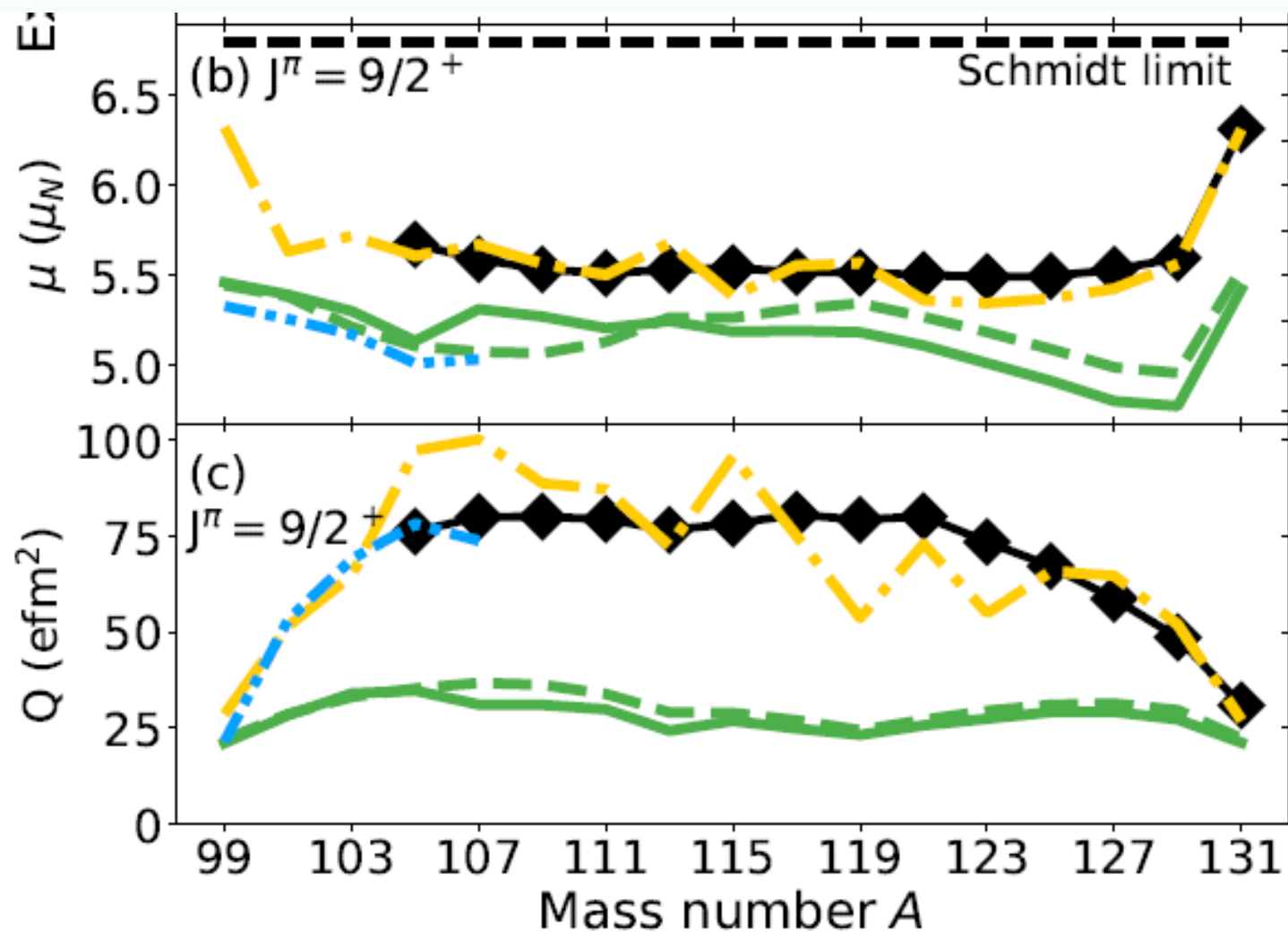


Picture: courtesy H. Wibowo

H. Wibowo *et al.*, to be published



Moments of the 9/2 states in In

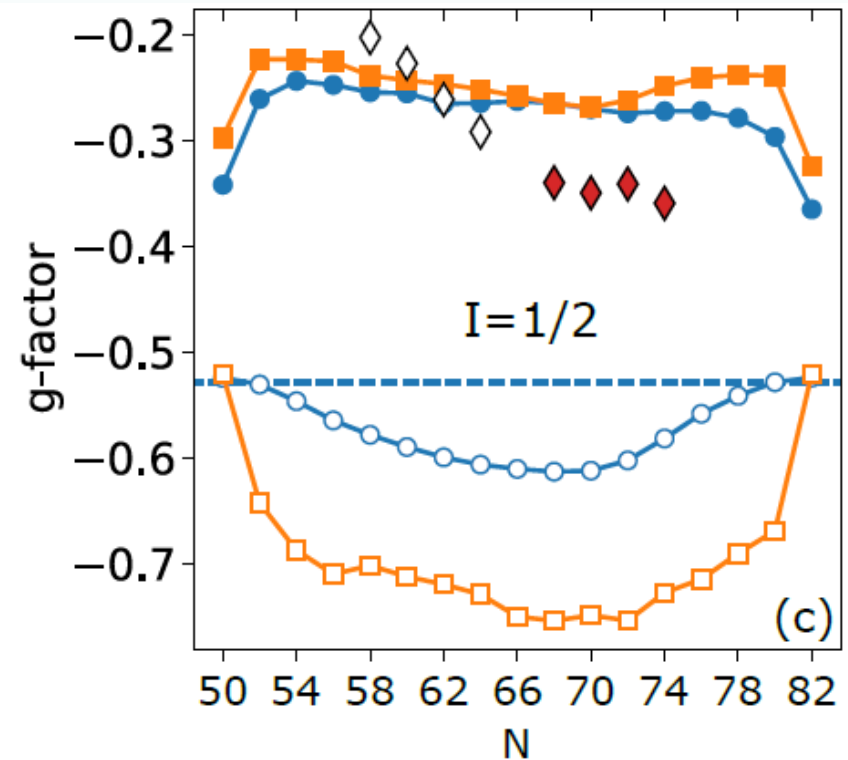
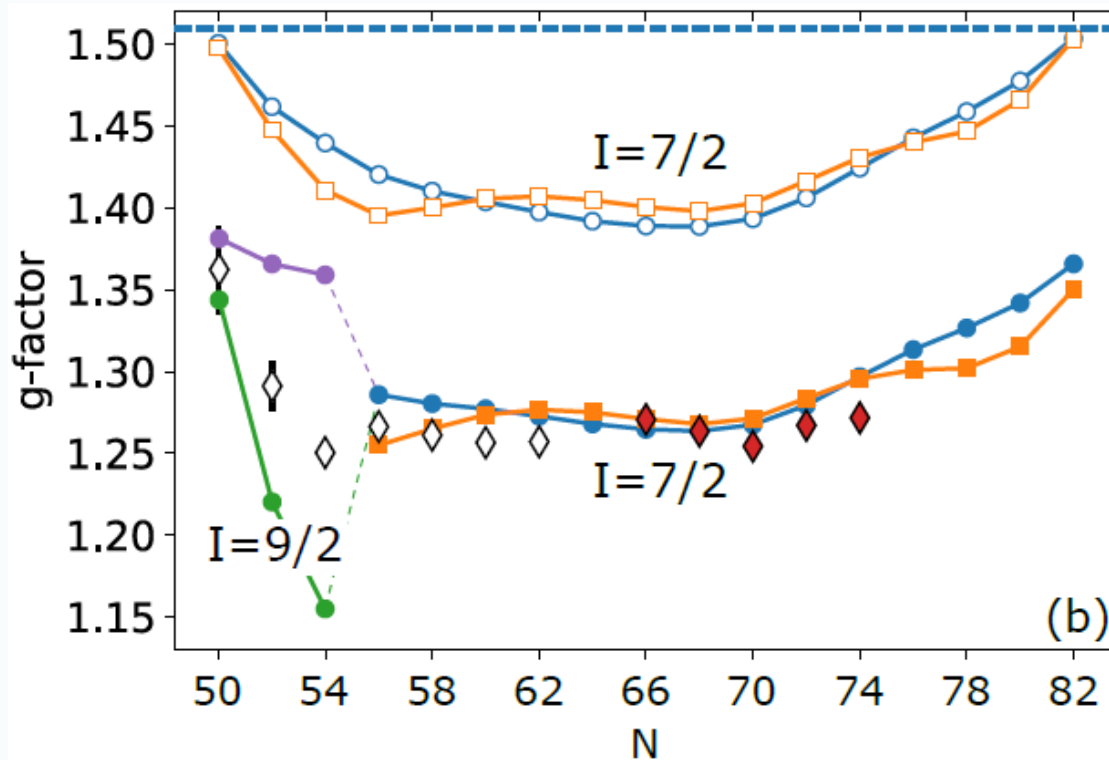


A.R. Vernon *et al.*, Nature 607, 260 (2022)

L. Nies *et al.*, Phys. Rev. Lett. 131, 022502 (2023)



Moments of the 1/2, 7/2 & 9/2 states in Ag



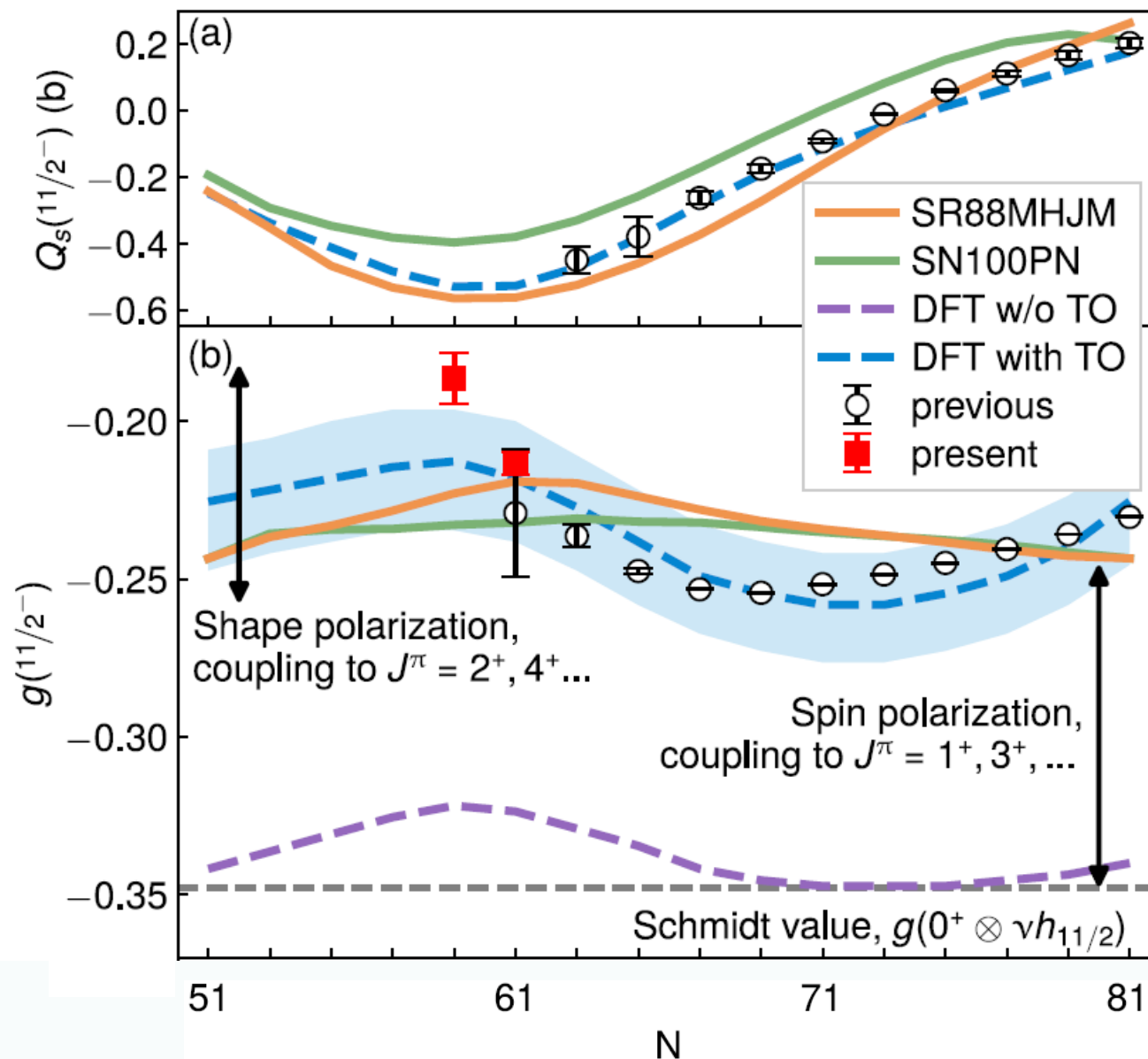
Experiment ◆ This work
◇ Literature

UNEDF1 □ $g'_0 = 0$ UNEDF1_{so} ○ $g'_0 = 0$ ● $g'_0 = 1.7$ $I = 9/2$ (7/2)
■ $g'_0 = 1.7$ ● $g'_0 = 1.7$ ● $g'_0 = 1.7$ $I = 9/2$

R. P. de Groote *et al.*, submitted to Phys. Lett. B



Moments of the $\nu h_{11/2}$ isomers in Sn

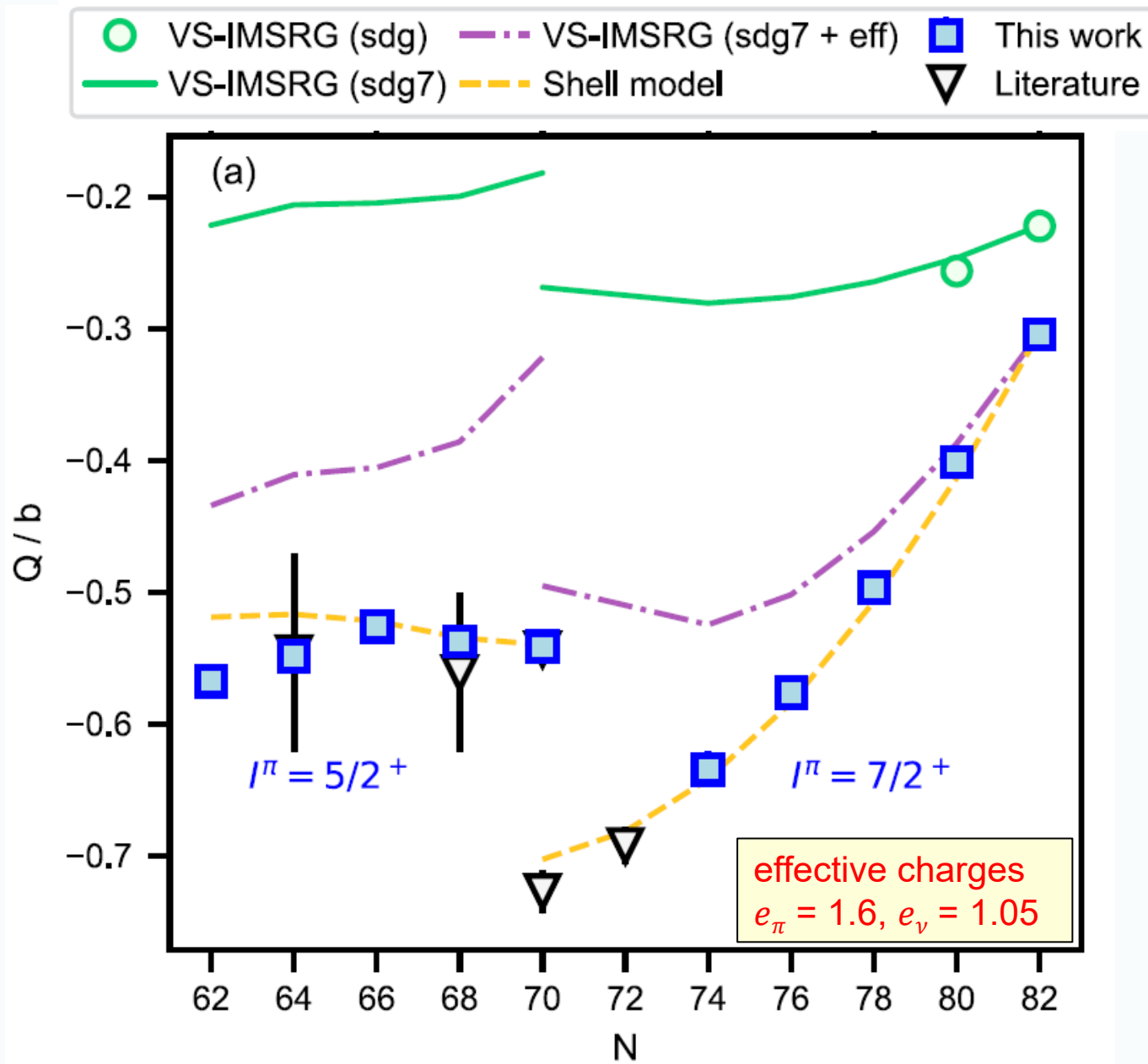


$$g = \mu/I$$

T.J. Gray et al., Phys. Lett. B 847 (2023) 138268



Quadrupole moments in Sb

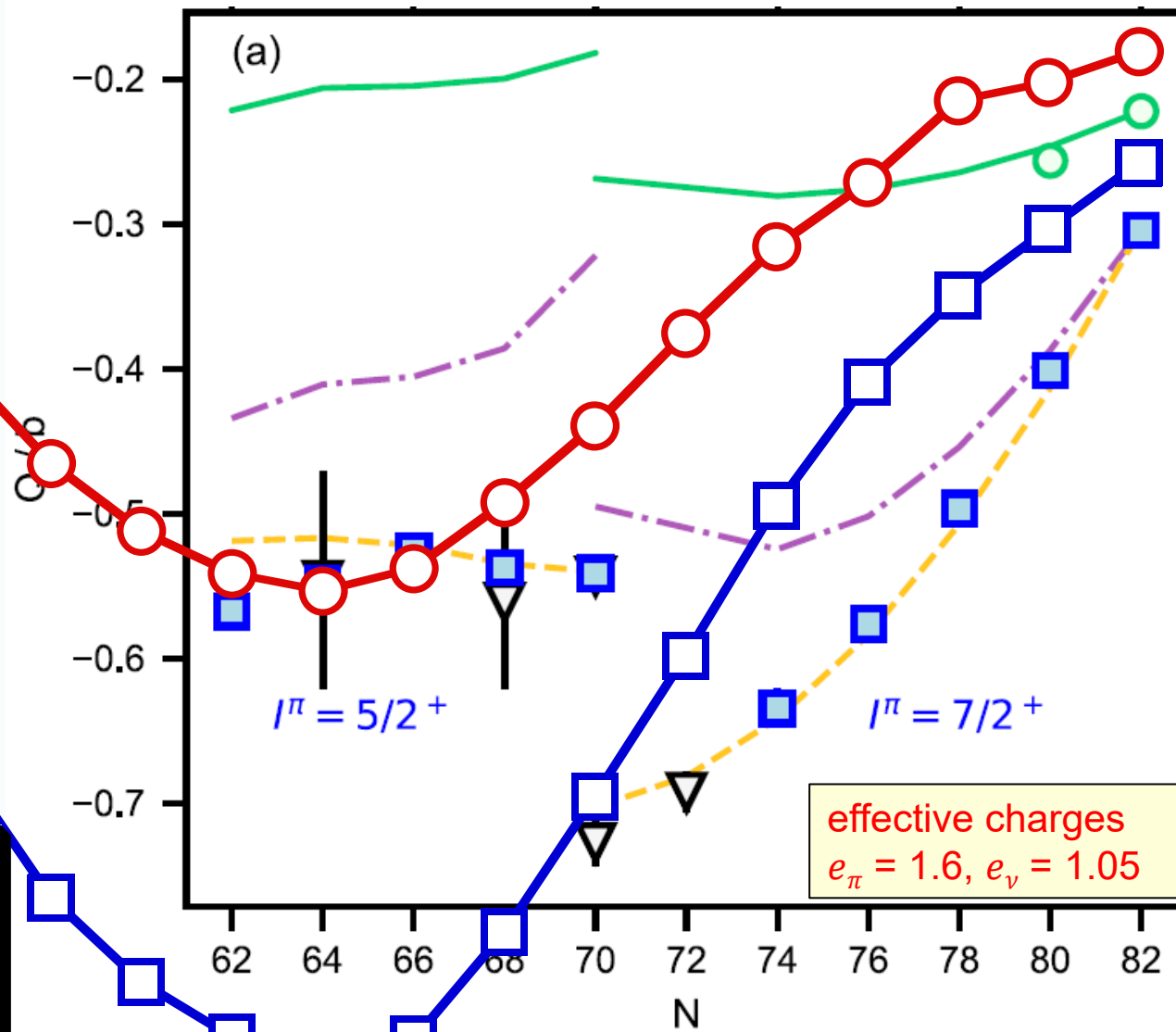


S. Lechner *et al.*, Phys. Lett. B 847 (2023) 138278



Quadrupole moments in Sb

○ VS-IMSRG (sdg) - - - VS-IMSRG (sdg7 + eff) □ This work
— VS-IMSRG (sdg7) - - - Shell model ▽ Literature



no effective charges !!!

□ DFT $g_{7/2}$
○ DFT $d_{5/2}$

S. Lechner *et al.*, Phys. Lett. B 847 (2023) 138278



Jacek Dobaczewski

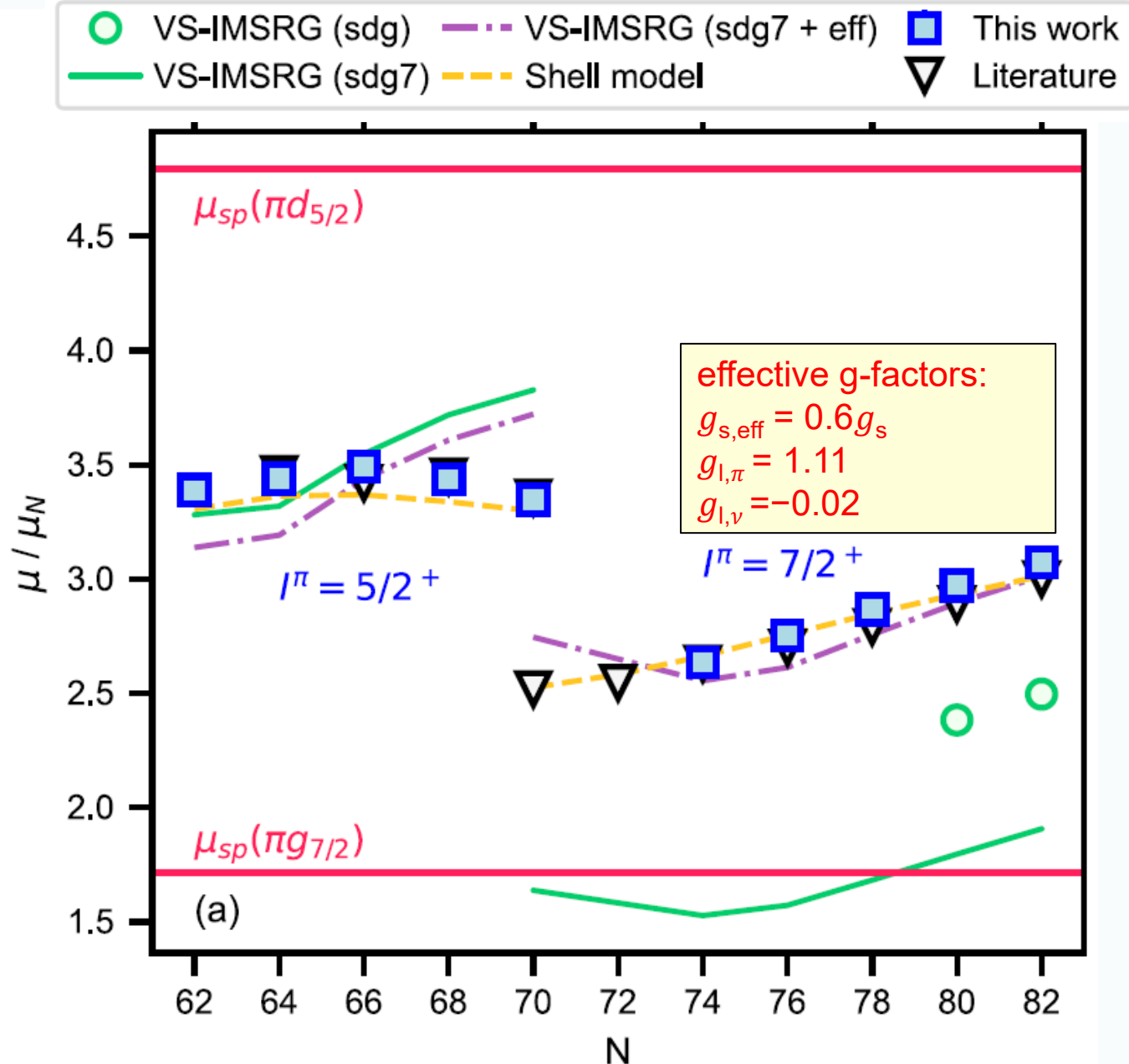
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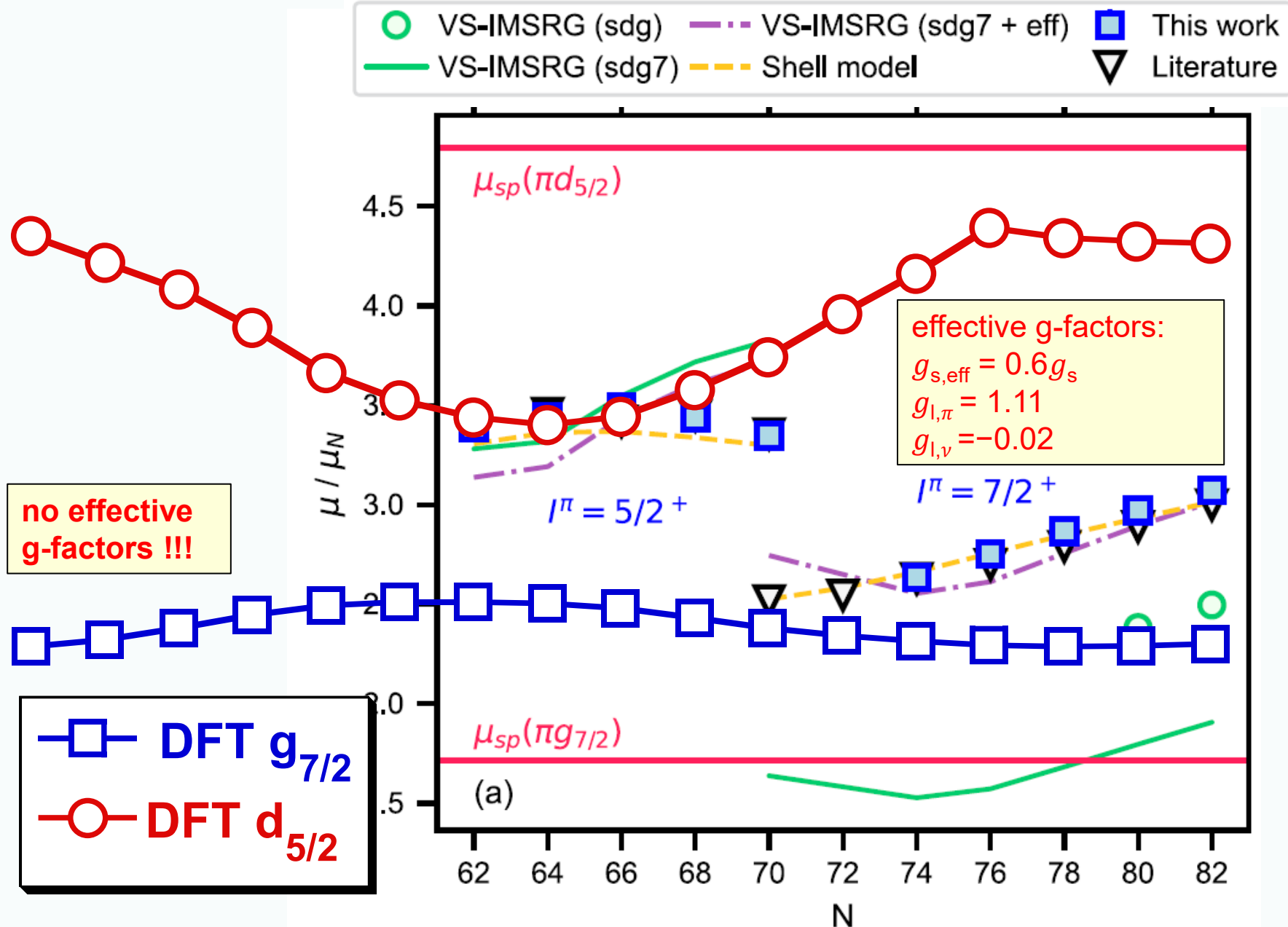
Magnetic dipole moments in Sb



S. Lechner *et al.*, Phys. Lett. B 847 (2023) 138278



Magnetic dipole moments in Sb



S. Lechner *et al.*, Phys. Lett. B 847 (2023) 138278



Jacek Dobaczewski

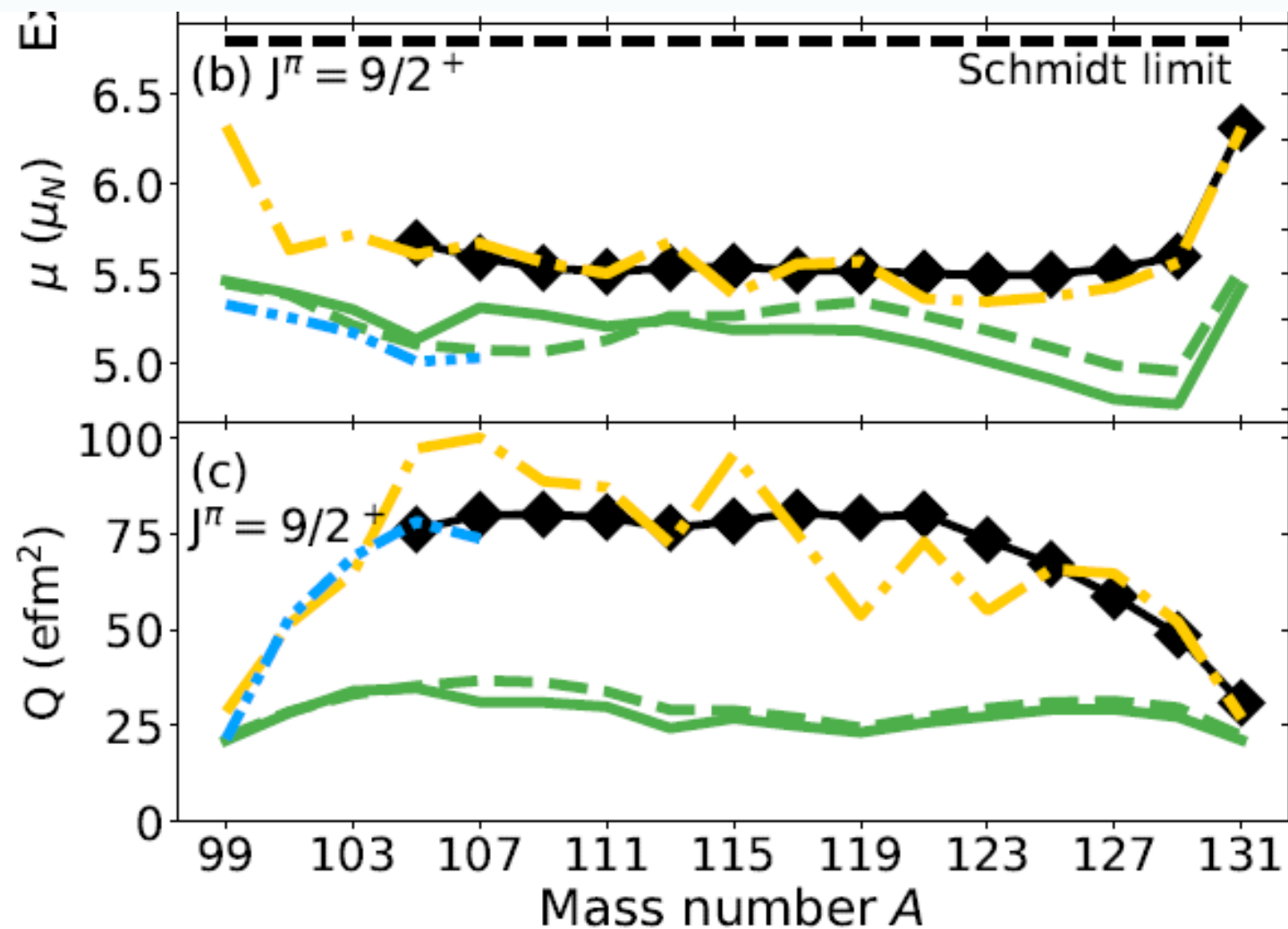
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Moments of the 9/2 states in In



A.R. Vernon *et al.*, Nature 607, 260 (2022)

L. Nies *et al.*, Phys. Rev. Lett. 131, 022502 (2023)



Two-body-current corrections to magnetic moments

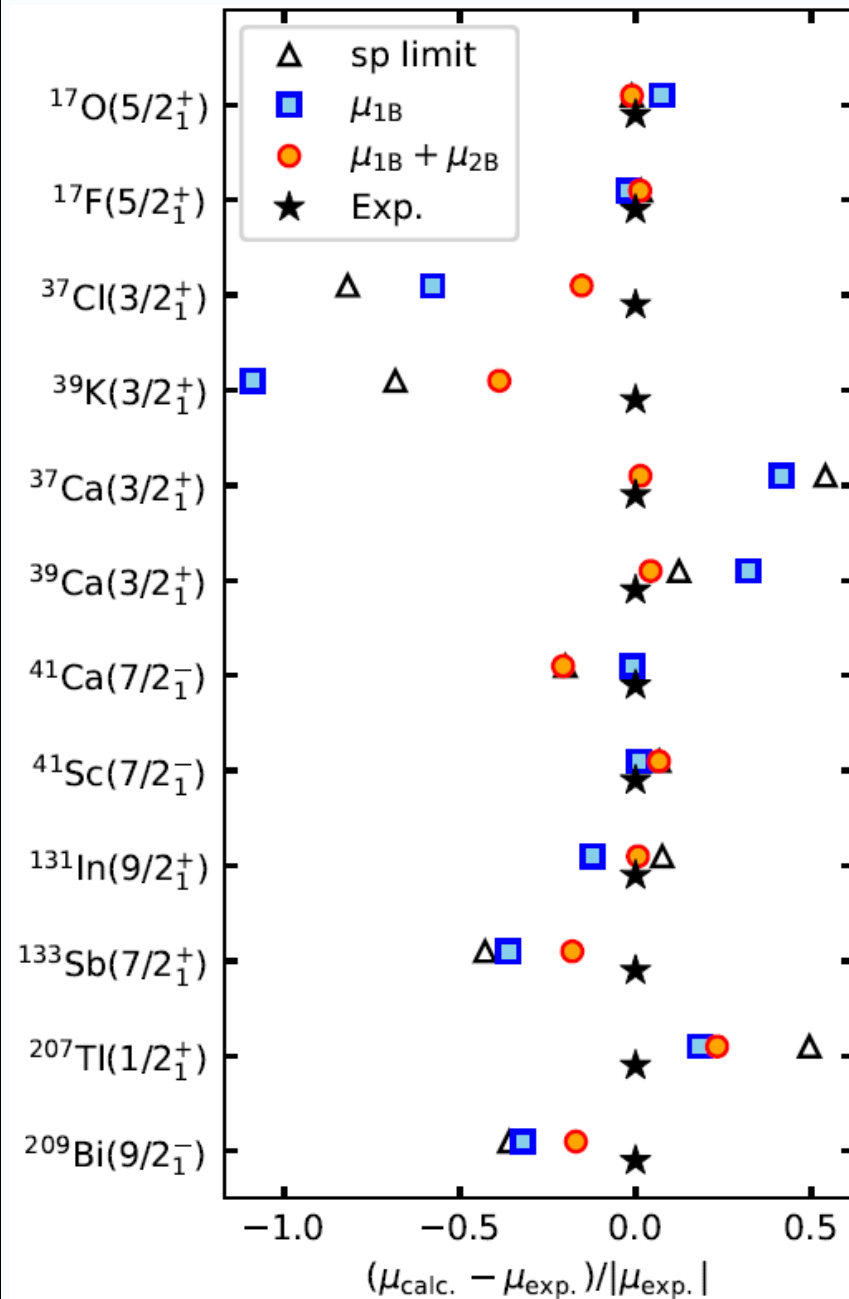


FIG. 1. Magnetic dipole moments of near doubly magic nuclei from $A = 17 - 209$ computed with the VS-IMSRG(2) relative to the experimental values. Results are shown at the one-body level, μ_{1B} (blue squares), and including 2BC, $\mu_{1B} + \mu_{2B}$ (red circles) based on the 1.8/2.0 (EM) NN+3N interactions. The experimental dipole moments (stars) are taken from Ref. [21, 35]. In addition, we show the simple single-particle (sp) limit (without many-body correlations and without 2BC).

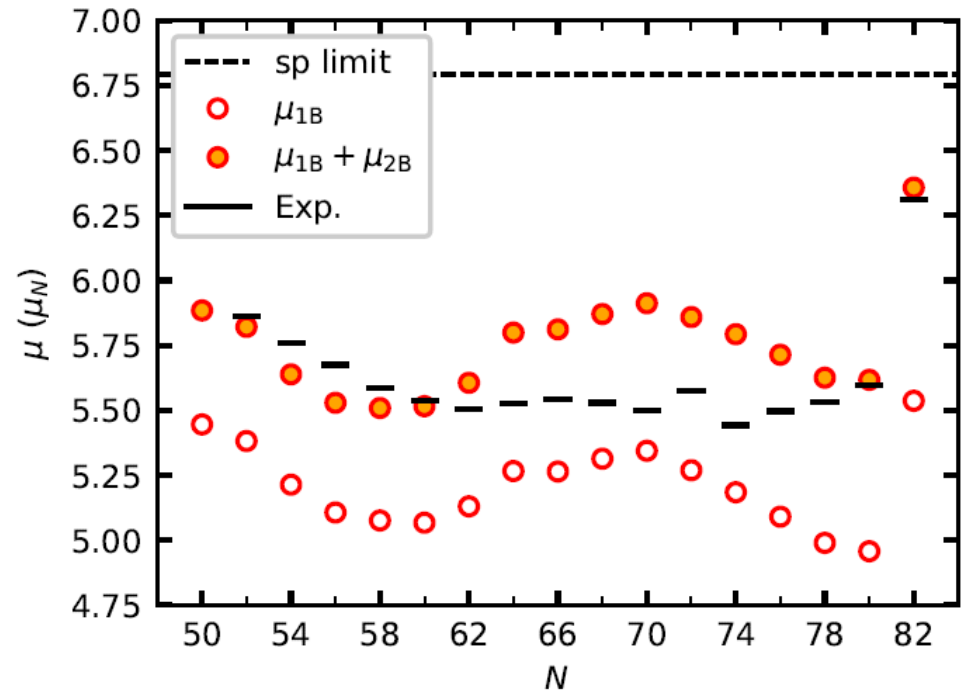


FIG. 4. Magnetic dipole moments of the $9/2^+$ ground state for the odd-mass indium isotopes computed with the VS-IMSRG(2) including 2BC, in comparison to experiment [21, 52].

T. Miyagi et al., arXiv:2311.14383

