

StarDICE: Calibration at the per mil level of a new generation of telescopes for dark energy measurement

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Presented by Thierry Souverin

25/09/2024



Presentation summary

I. General introduction

1. A brief introduction to cosmology
2. Type Ia supernovae
3. Photometric calibration

II. The StarDICE experiment

4. Description of the experiment
5. Collimated Beam Projector
6. On-sky measurements analysis with StarDICE

I. General introduction

1. A brief introduction to cosmology



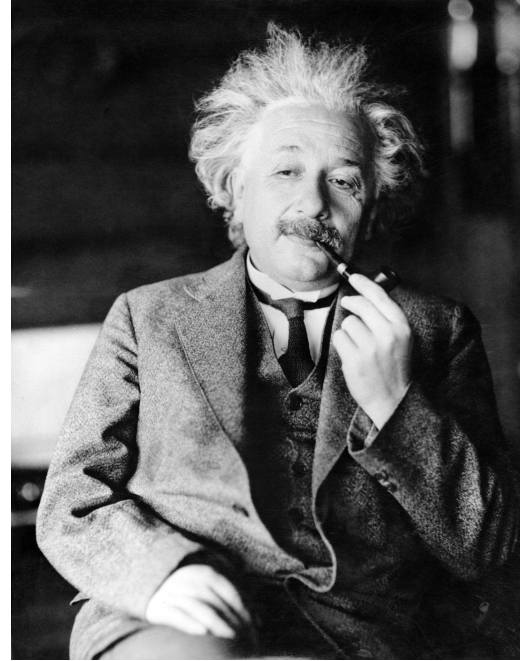
What is cosmology ?



What is cosmology ?

It is the field of physics describing the nature of the
Universe, its **structure** and its **evolution**

General relativity



Albert Einstein, pipe smoking

General relativity

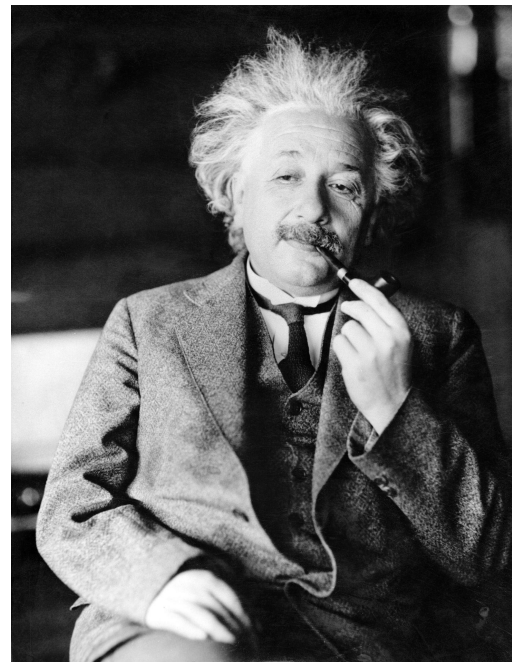
Einstein equation:

$$G_{\mu\nu} = \frac{8\pi G_N}{c^4} T_{\mu\nu}$$

4D spacetime curvature

Newtonian gravitational constant

Energy content of the Universe (baryonic matter, photons, neutrinos...)



Albert Einstein, pipe smoking

General relativity

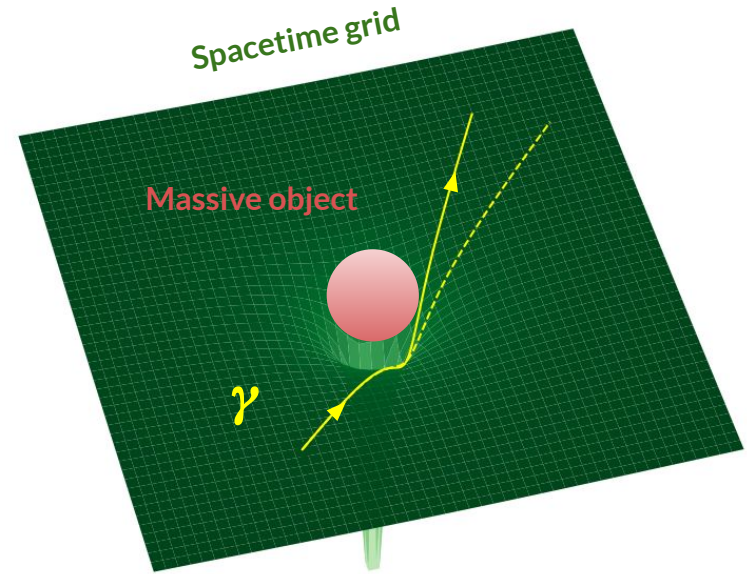
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2D representation of spacetime deformed by a massive object

General relativity

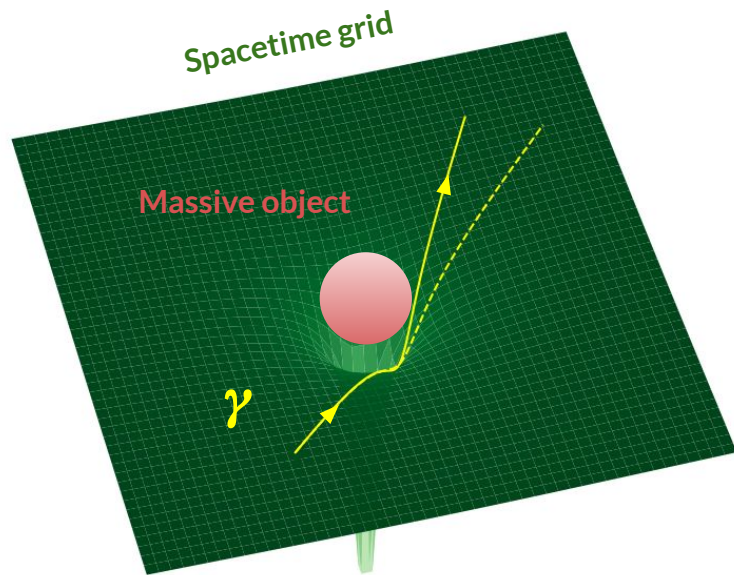
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4D spacetime curvature

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Energy content of the Universe (baryonic matter, photons, neutrinos...)



2D representation of spacetime deformed by a massive object

⇒ But the Universe is complex and full of materials, so how can we study it?

■ Cosmological principle

Cosmological principle: at cosmological scales, the Universe is **homogeneous** and **isotropic**

⇒ implies symmetry considerations for both $T_{\mu\nu}$ and $G_{\mu\nu}$

Cosmological principle

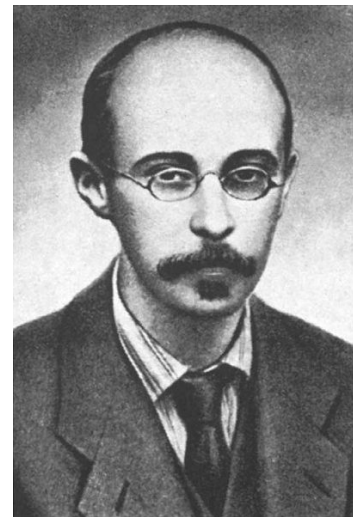
Cosmological principle: at cosmological scales, the Universe is **homogeneous** and **isotropic**

⇒ implies symmetry considerations for both $T_{\mu\nu}$ and $G_{\mu\nu}$

Friedmann's equations (solution to Einstein equation)

Scale factor — $\frac{\ddot{a}}{a} = \frac{4\pi G_N}{3} \left(\rho + \frac{3p}{c^2} \right)$

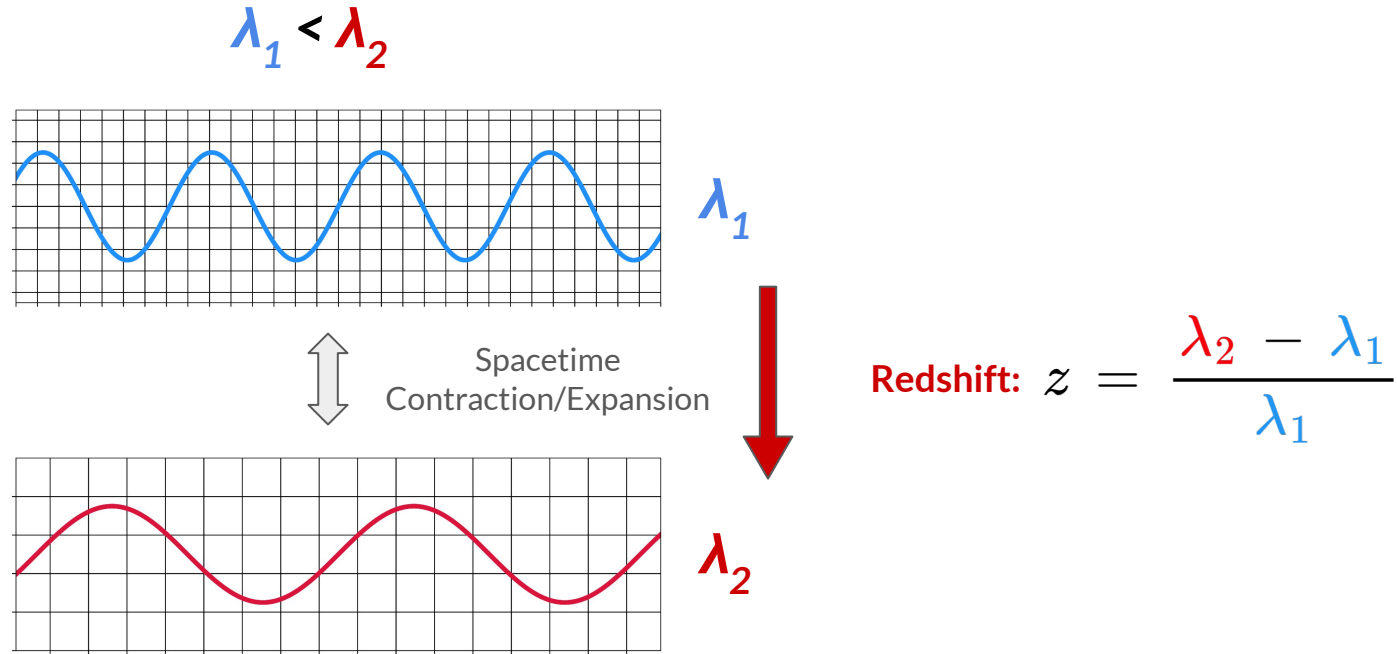
$$\left(\frac{\dot{a}}{a} \right)^2 = \frac{8\pi G_N}{3} \rho - \frac{kc^2}{a^2}$$



Aleksandr Friedmann, not pipe smoking

⇒ links the **dynamic behavior** of the Universe with its **energy content**

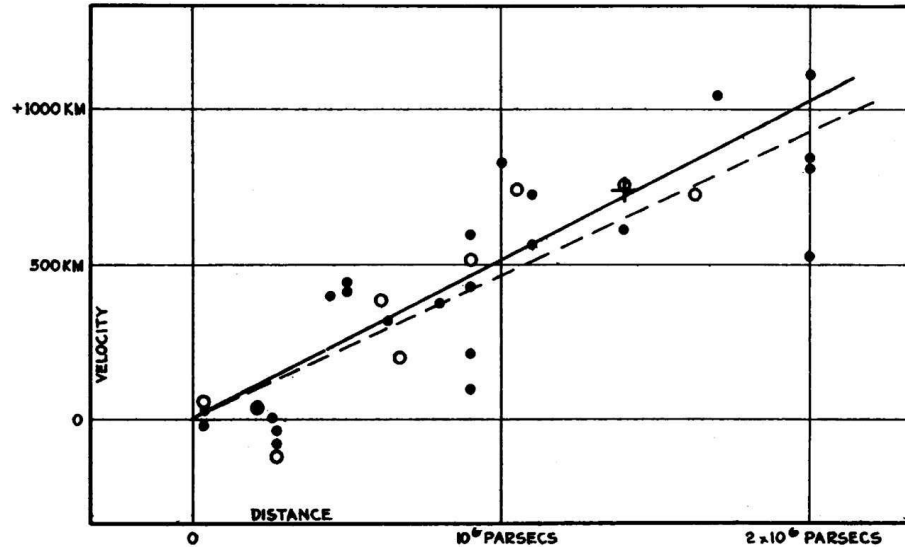
Redshift definition



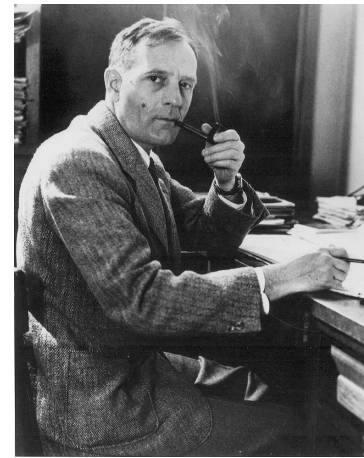
Spacetime expansion affects light **wavelength**

⇒ The redshift z is a tracer for studying spacetime evolution

Expansion of the Universe, 1929

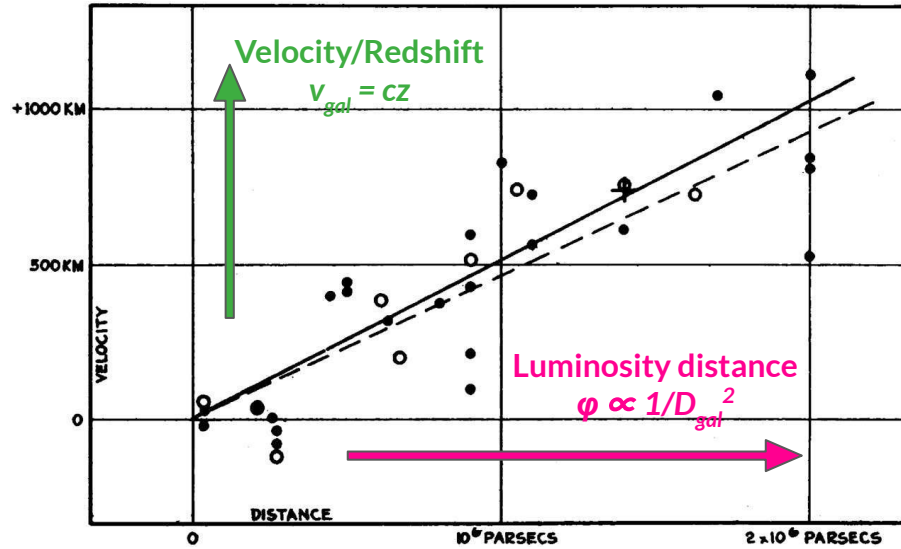


Galaxy velocities against their distances
(Hubble, 1929)

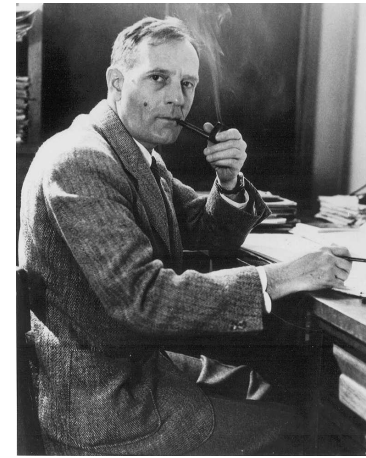


Edwin Hubble, pipe smoking

Expansion of the Universe, 1929



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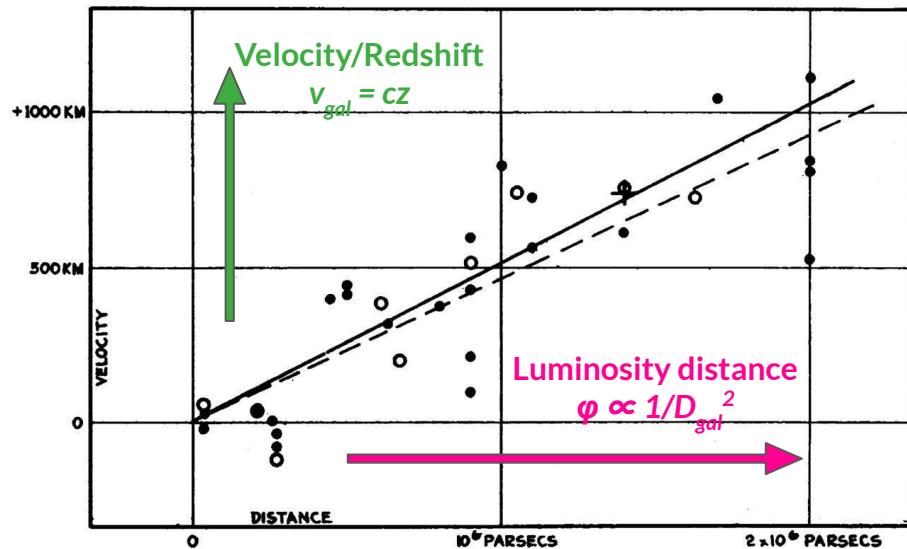
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$$v_{\text{gal}} \propto D_{\text{gal}}$$

\Leftrightarrow

$$cz \propto D_{\text{gal}}$$

Expansion of the Universe, 1929



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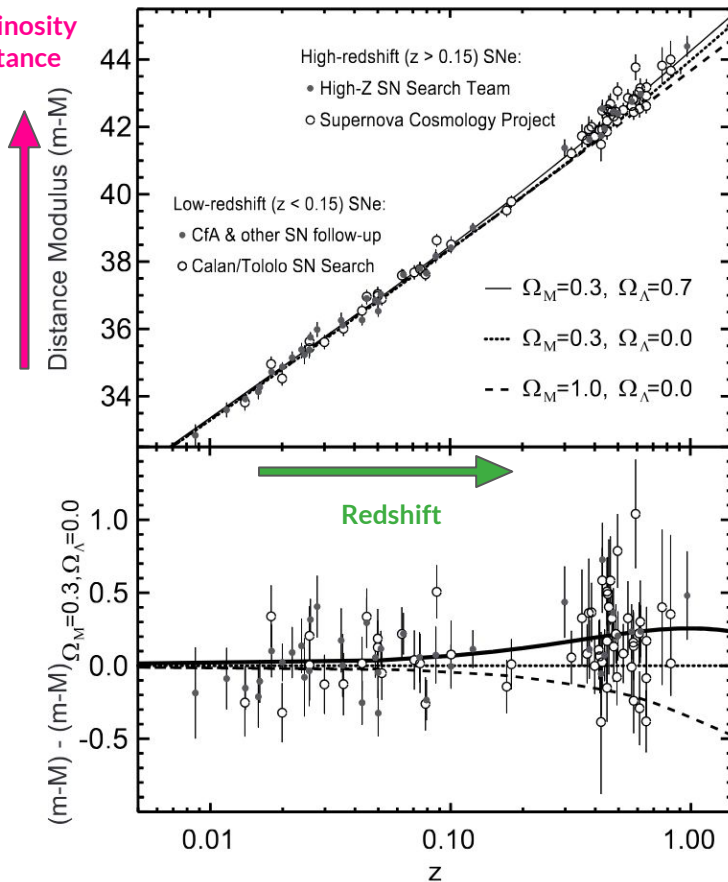
$$\Leftrightarrow$$

$$cz \propto D_{\text{gal}}$$

The redshift z increases with the galaxy distance D_{gal}
 \Rightarrow First evidence of the Universe's expansion

Expansion's acceleration, 1998/1999

Luminosity
distance

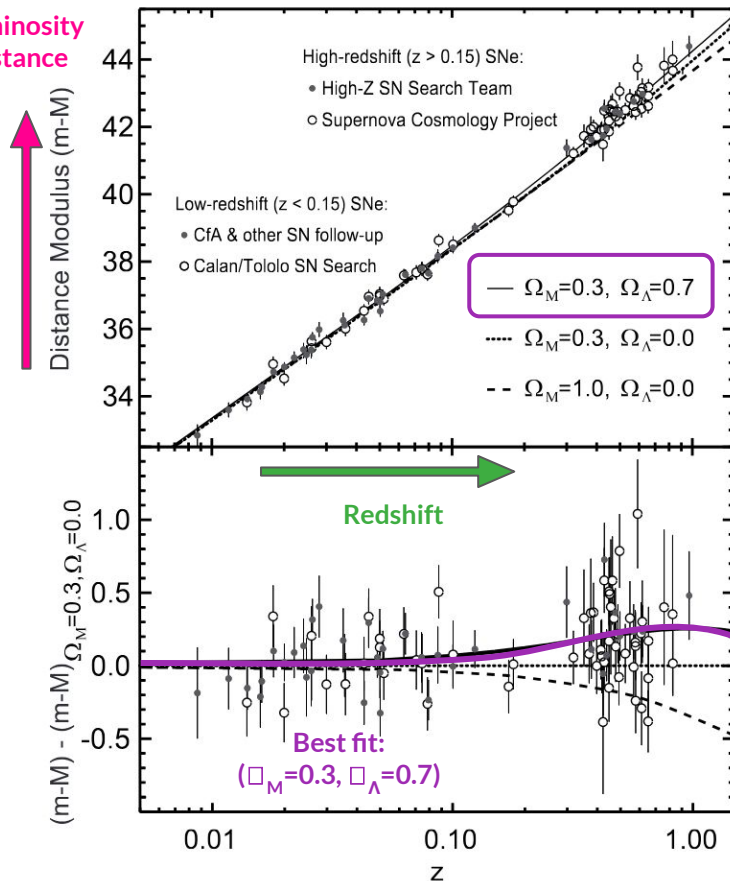


High-Z Supernova Search Team and Supernovæ Cosmology Project (SCP)

→ First evidence of the acceleration of the Universe's expansion

Expansion's acceleration, 1998/1999

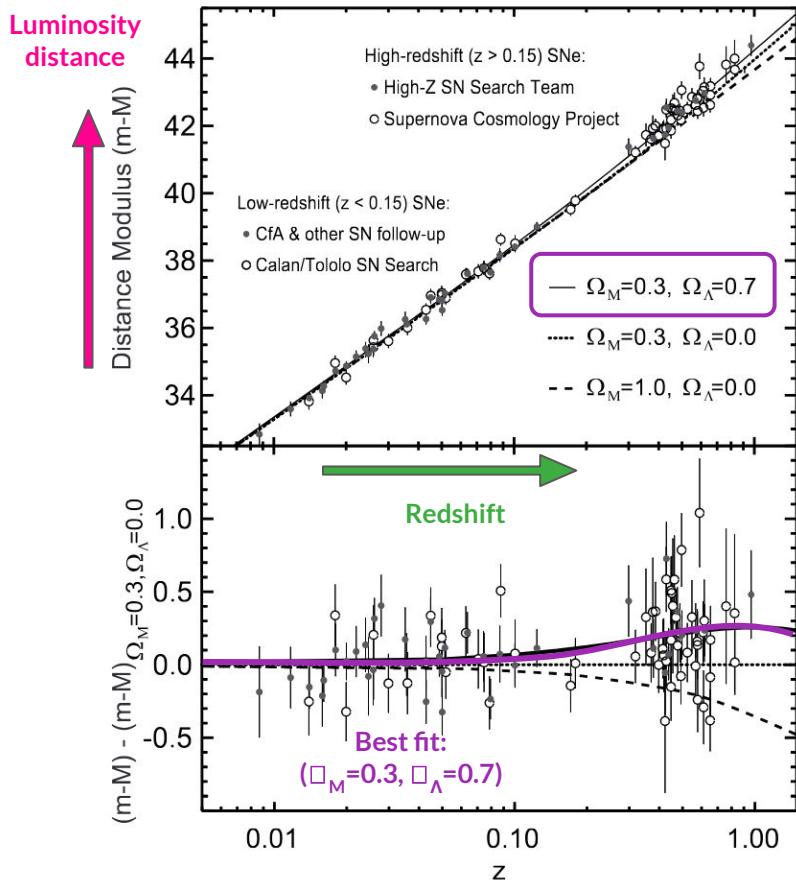
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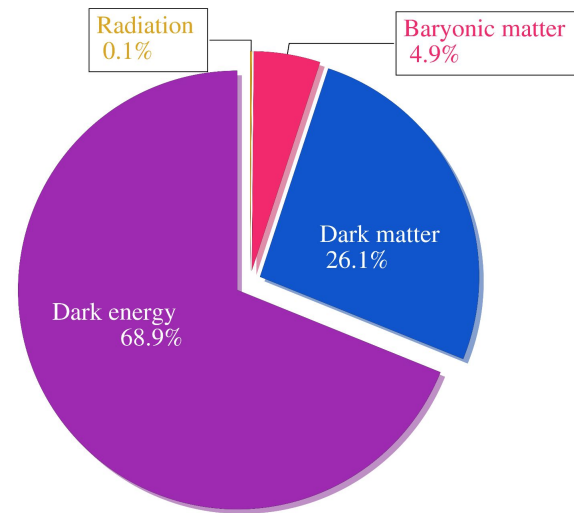
$$G_{\mu\nu} + \underbrace{\Lambda}_{\text{Cosmological constant}} g_{\mu\nu} = \frac{8\pi G_N}{c^4} T_{\mu\nu}$$

The cosmological constant can be seen as an additional component of the energy content
⇒ dark energy

Dark energy models

Dark energy → fluid described by an equation of state with the parameter w :

$$\rho_{\text{de}} \propto a^{-3(1+w)}$$



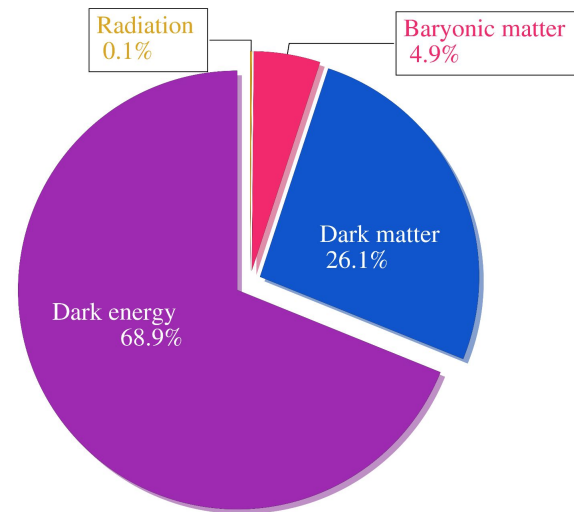
Pie chart of the energy contents distribution in the Universe today

Dark energy models

Dark energy → fluid described by an equation of state with the parameter w :

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- Λ CDM, the standard model
 - Λ for the cosmological constant, CDM for Cold Dark Matter, $w = -1$, and a flat Universe



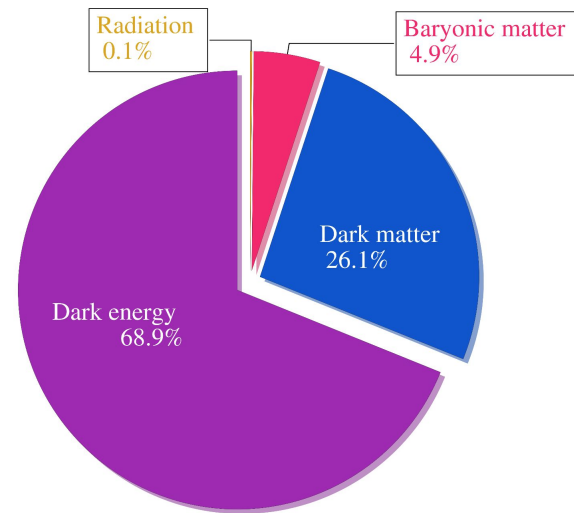
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Pie chart of the energy contents distribution in the Universe today

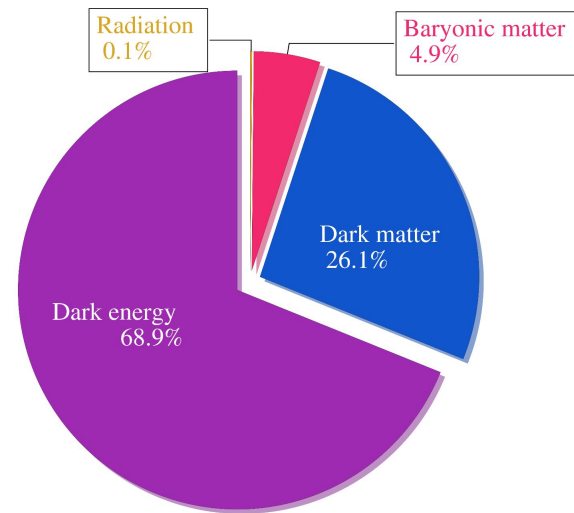
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⇒ Which model describes better the observations ?



Pie chart of the energy contents distribution in the Universe today

Cosmological probes

Several astrophysical probes can be observed to infer cosmological parameter constraints:

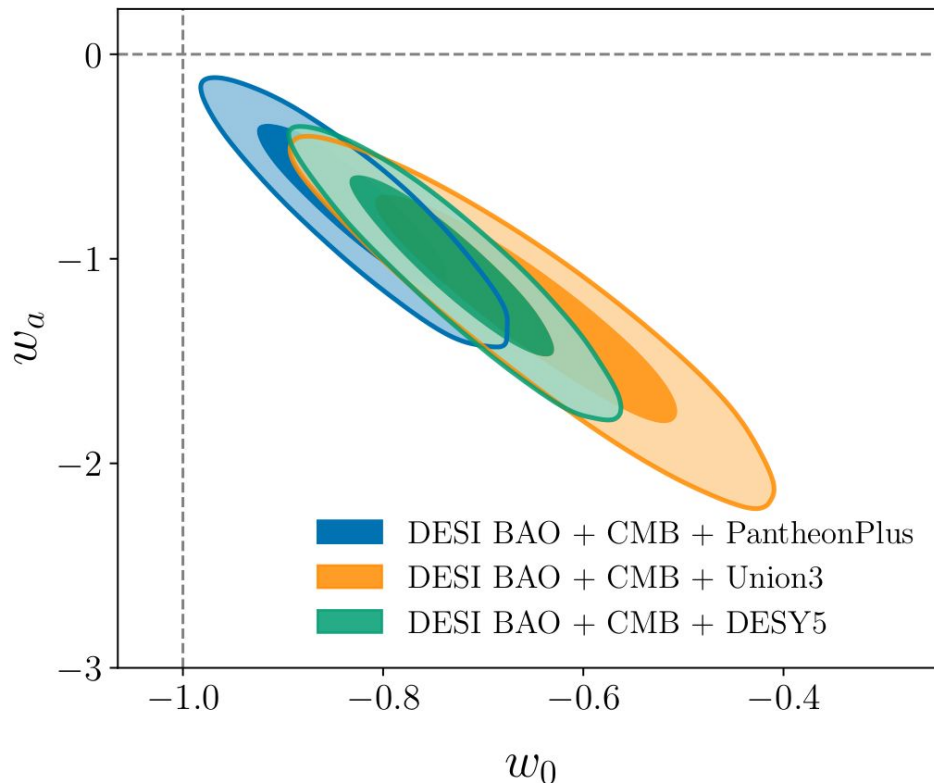
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- Baryon Acoustic Oscillations (BAO)
- Weak gravitational lensing
- **Type Ia supernovae (SNe Ia)**

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Probe combinations



Constraints in the w_0 - w_a plane parameters
(DESI Collaboration et al., 2024)

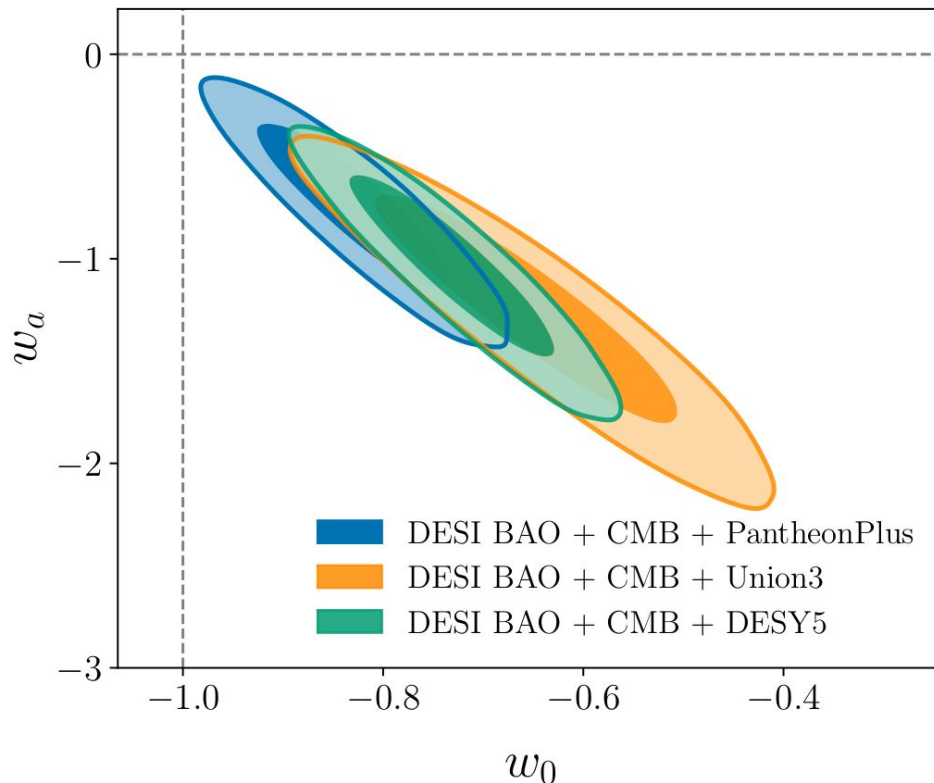
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⇒ 3.9σ tensions with the Λ CDM model
($w_0 = -1, w_a = 0$)

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Cosmological probes

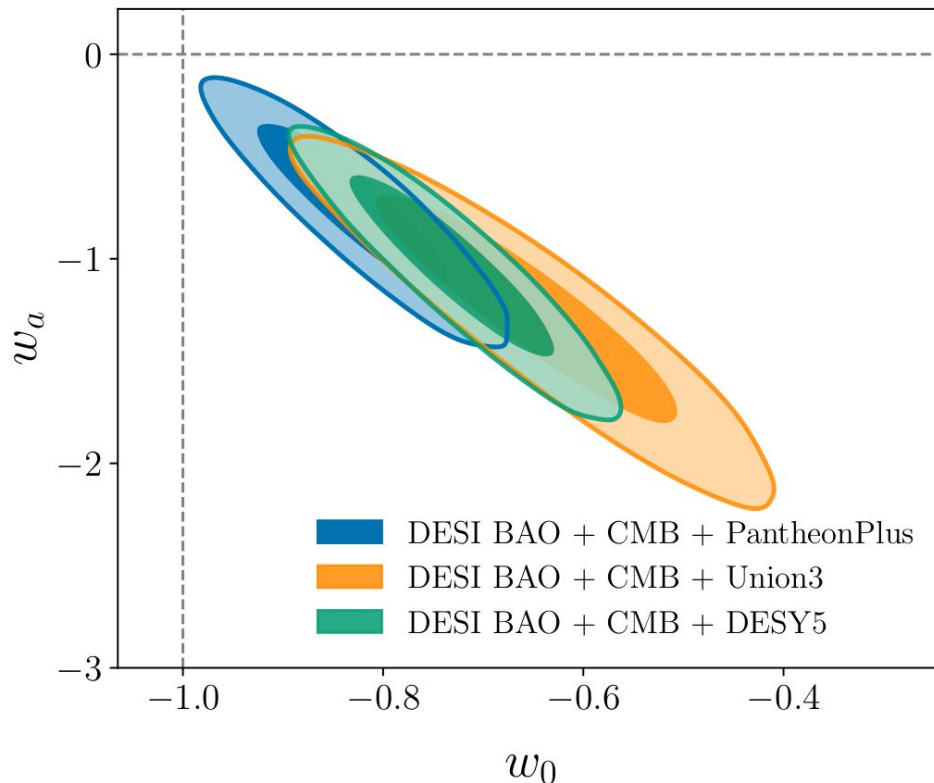
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⇒ Accurate measurements, or is there any source of bias, notably for SNe Ia ?

Probe combinations

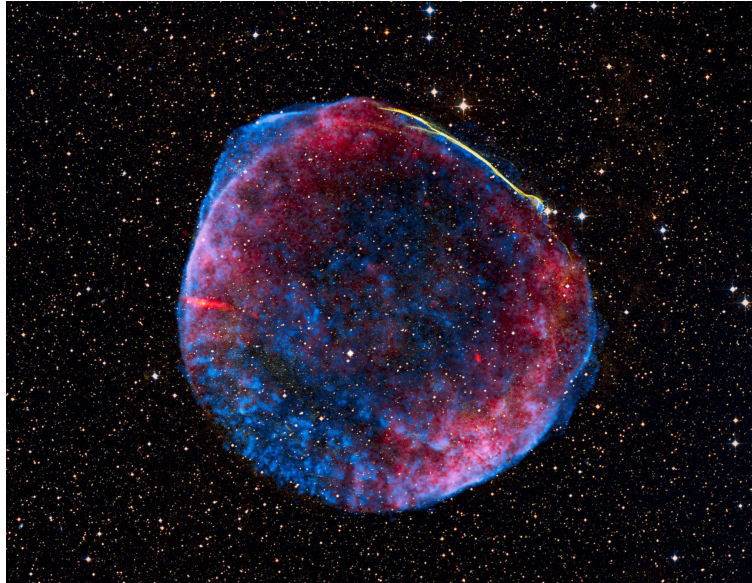


Constraints in the w_0 - w_a plane parameters
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2. Type Ia supernovae

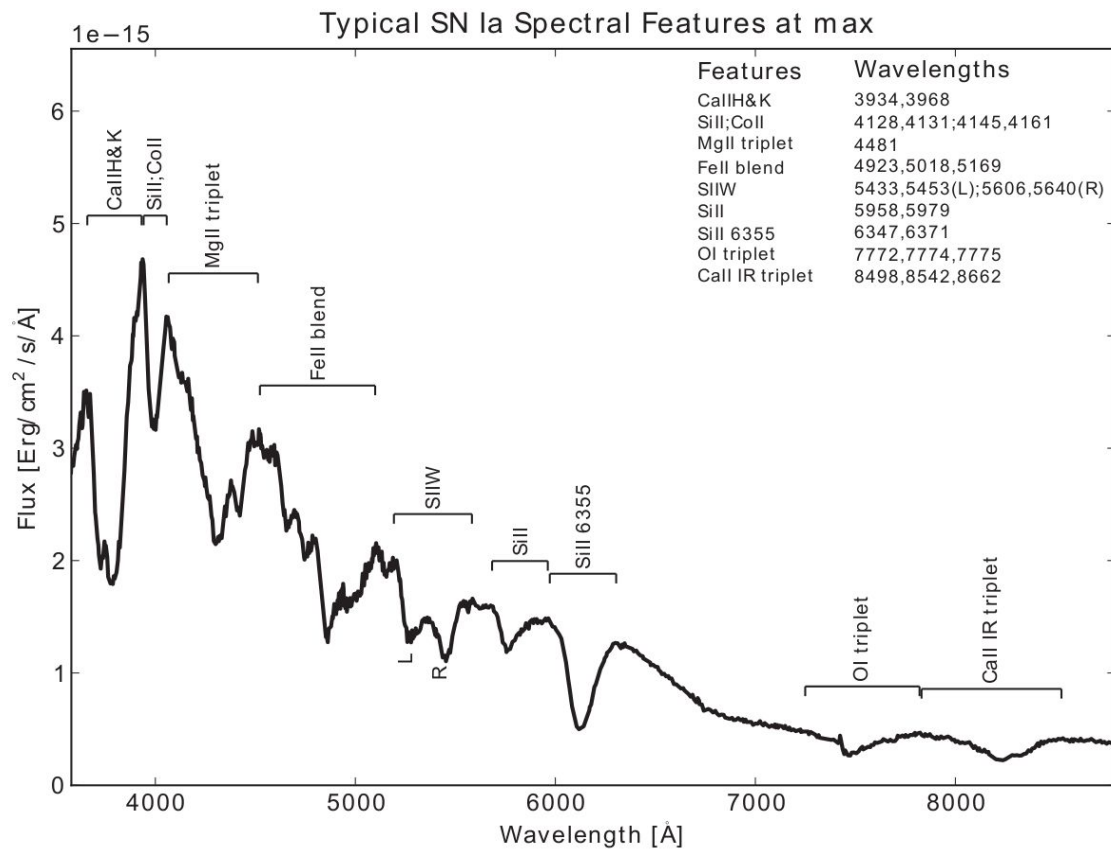
Explosion mechanism

- Explosion of a carbon-oxygen white dwarf (WD) with a mass $> 1.4 M_{\odot}$



Remnant of SN 1006
observed with the Chandra X-ray Observatory

Type Ia supernovae spectrum



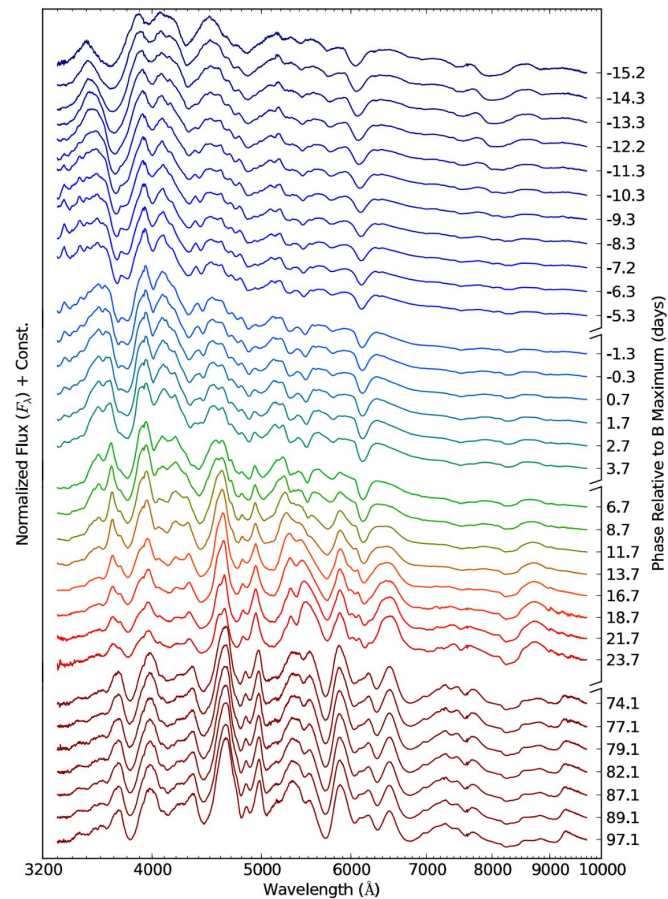
SN Ia spectrum (Chotard, 2011)

Characteristics:

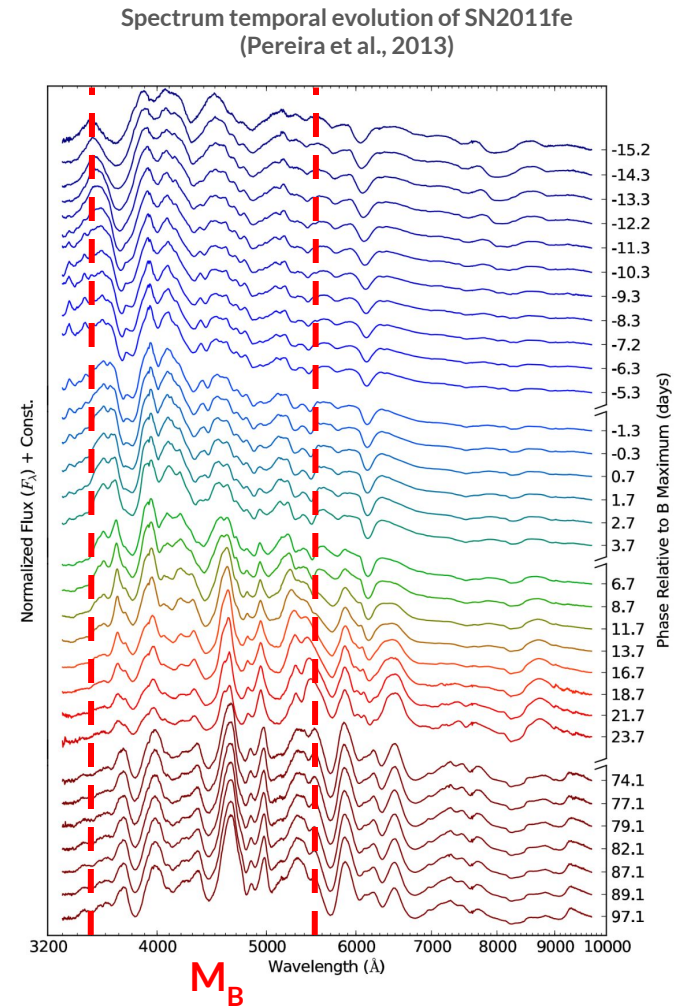
- Absence of hydrogen line
- Strong Si line (6355 Å)
- Intermediate-mass elements from oxygen to calcium

SNe Ia light curve

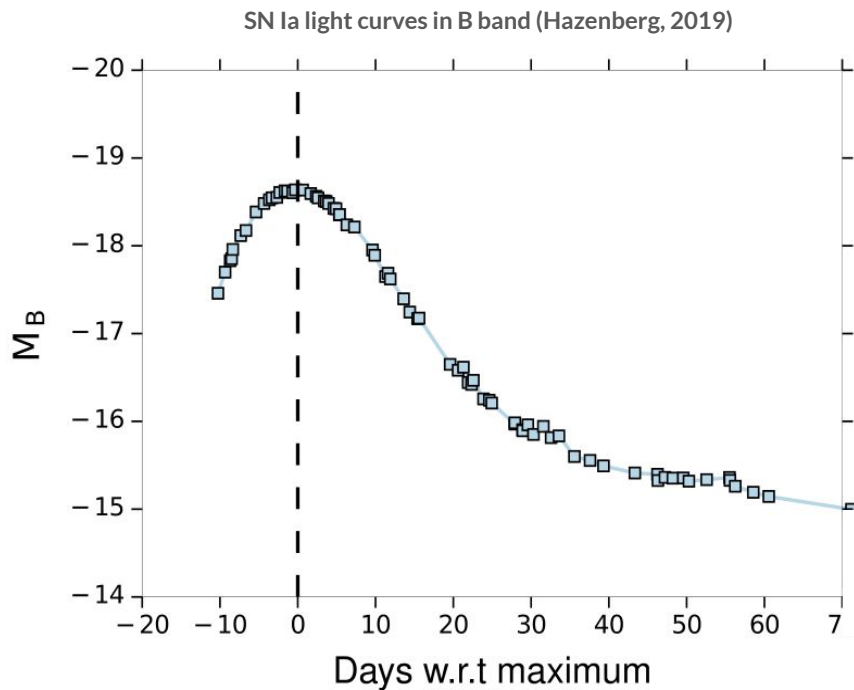
Spectrum temporal evolution of SN2011fe
(Pereira et al., 2013)



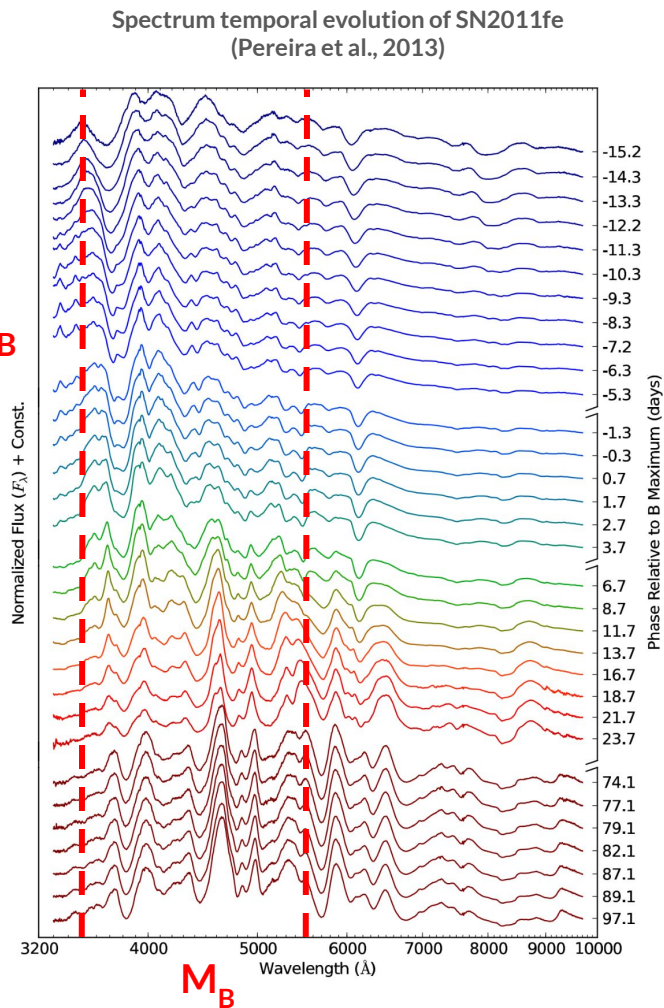
SNe Ia light curve



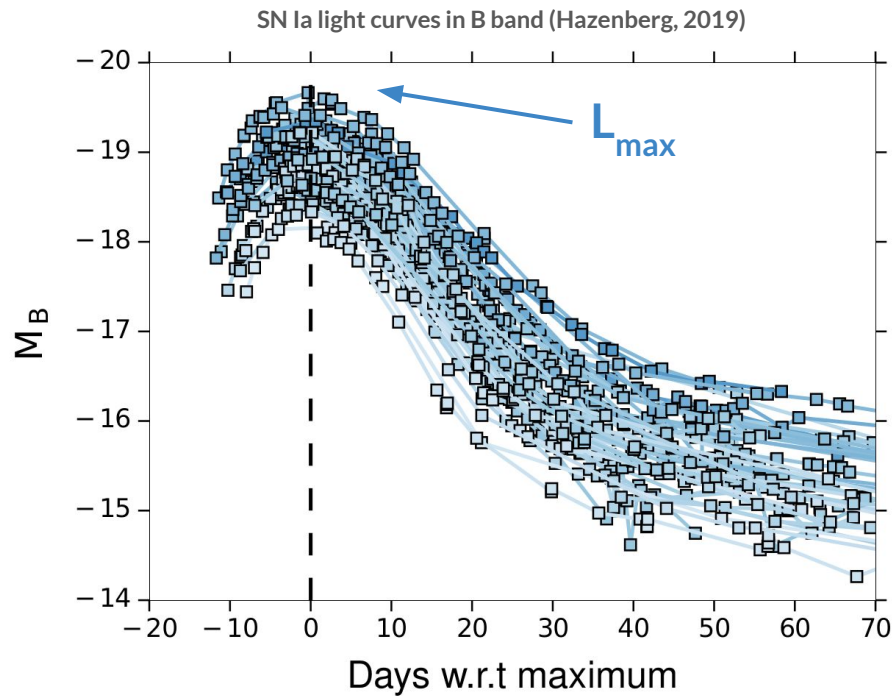
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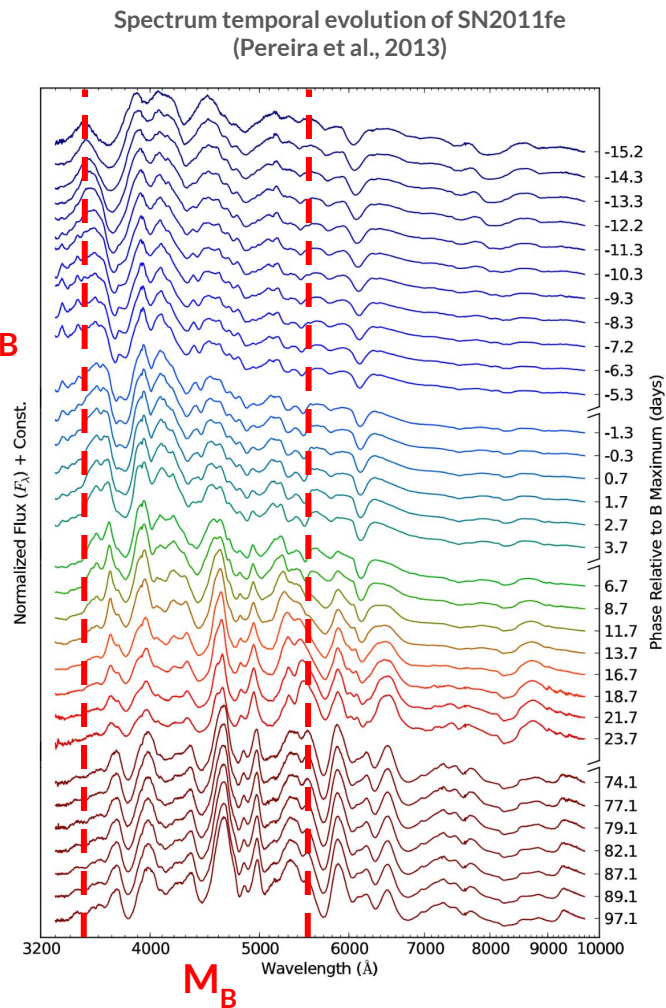
Restframe B
band



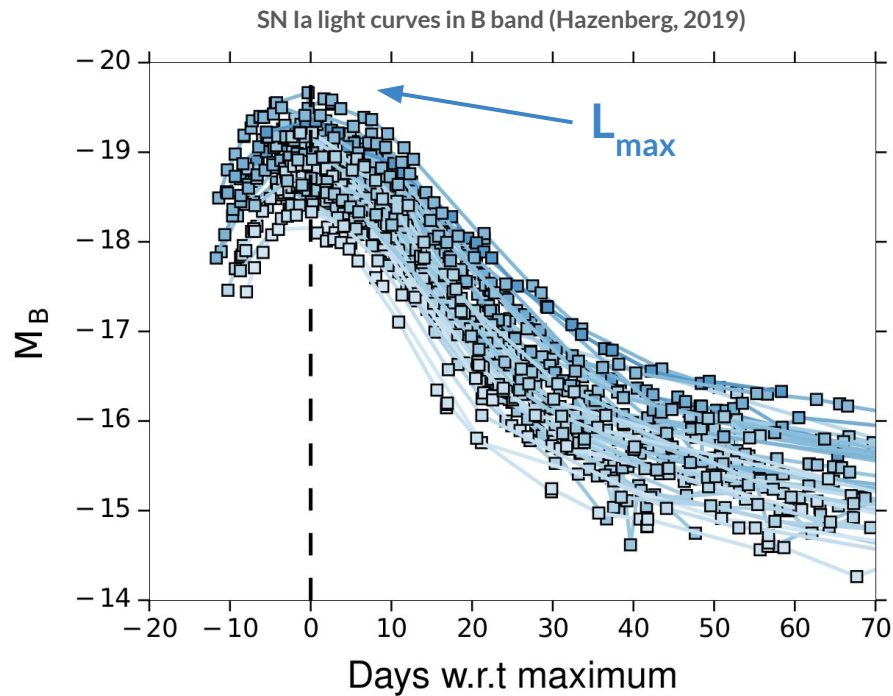
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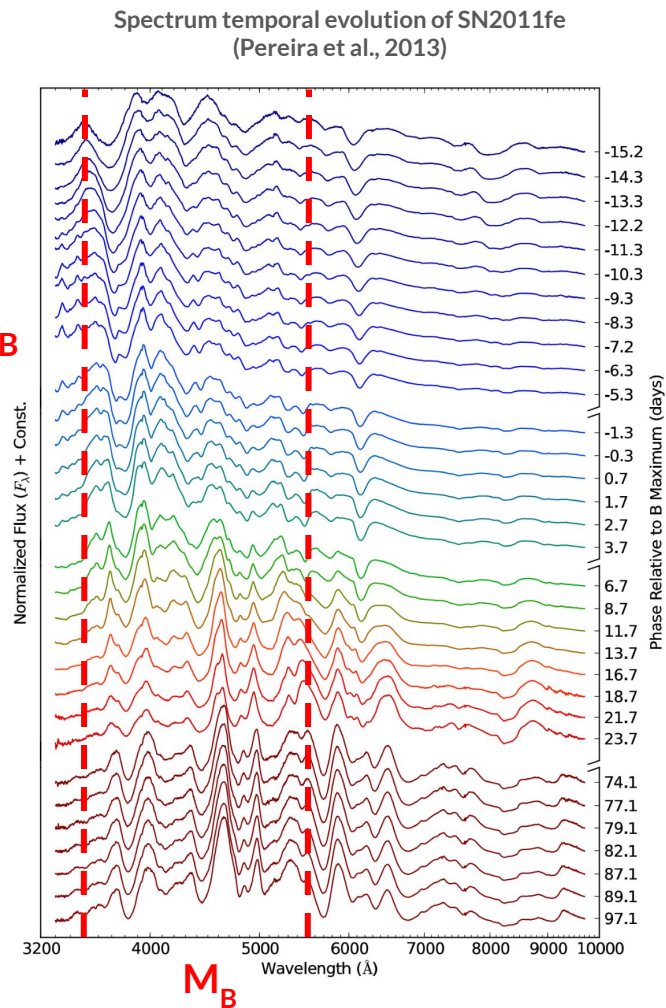
Restframe B
band



SNe Ia light curve



Restframe B band



Luminosity distance:

$$F_{\max} = \frac{L_{\max}}{4\pi D_L^2} ; \quad M_B = m_B^* - 5 \log_{10} \frac{D_L}{10\text{pc}}$$

● Hubble diagram

Plot μ against $z \rightarrow$ Hubble Diagram

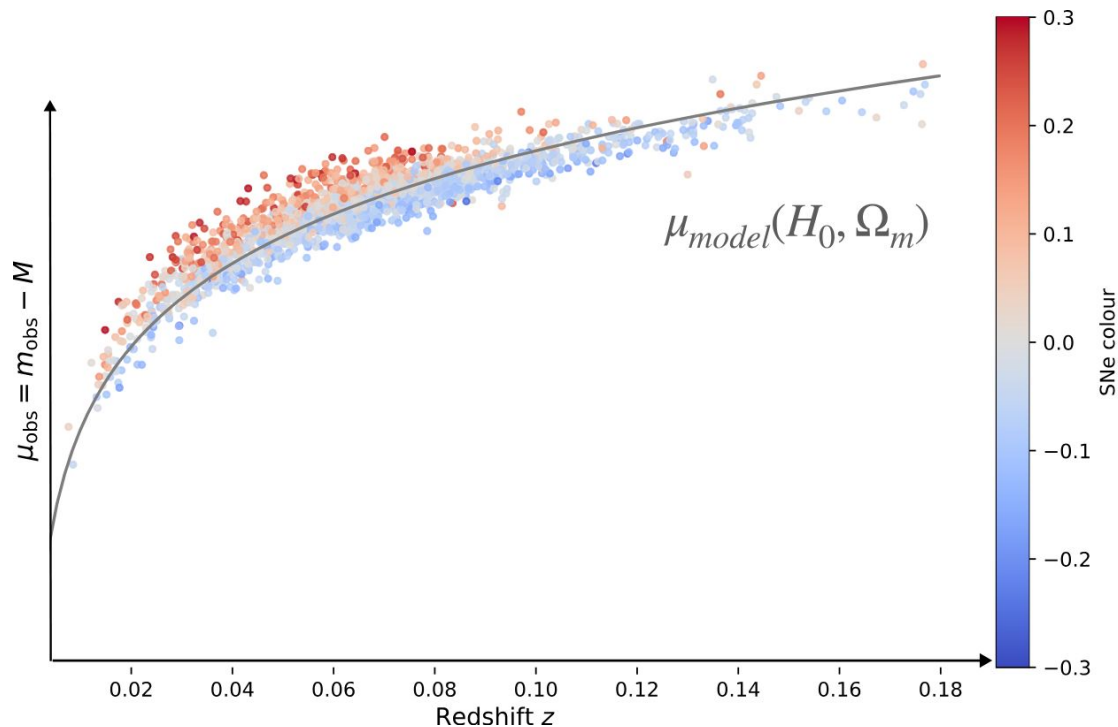
Distance modulus:

$$\mu = m_B^* - M_B$$

Restframe
magnitude

Absolute
magnitude

\Rightarrow dispersion in μ of $\sim 40\%$

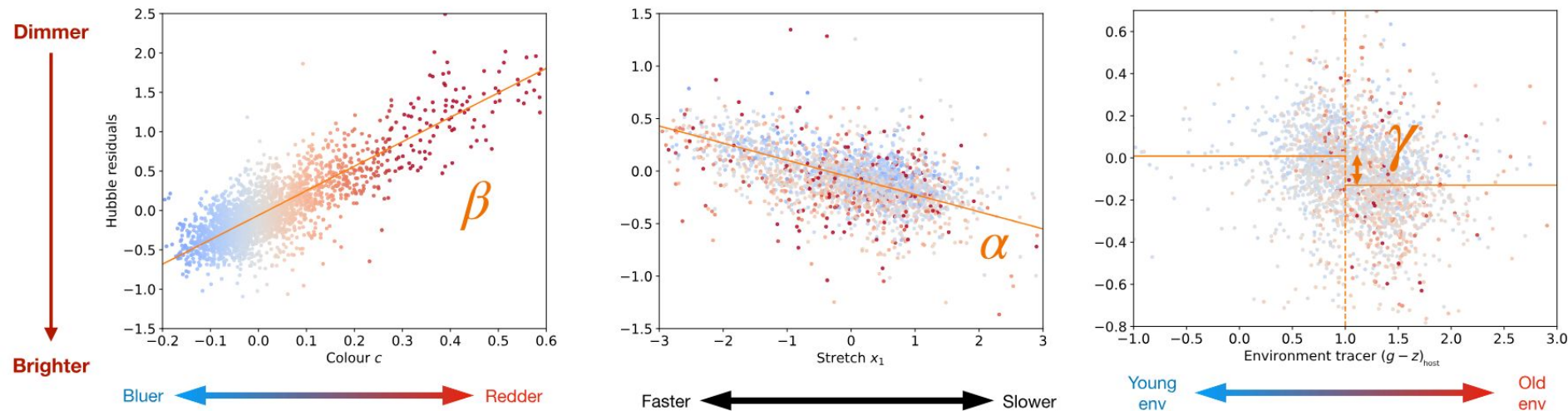


Hubble diagram

Standardization parameters

Standardization parameters

(https://moriond.in2p3.fr/2024/Cosmology/transparencies/2_tuesday/1_morning/05_Ginolin.pdf)



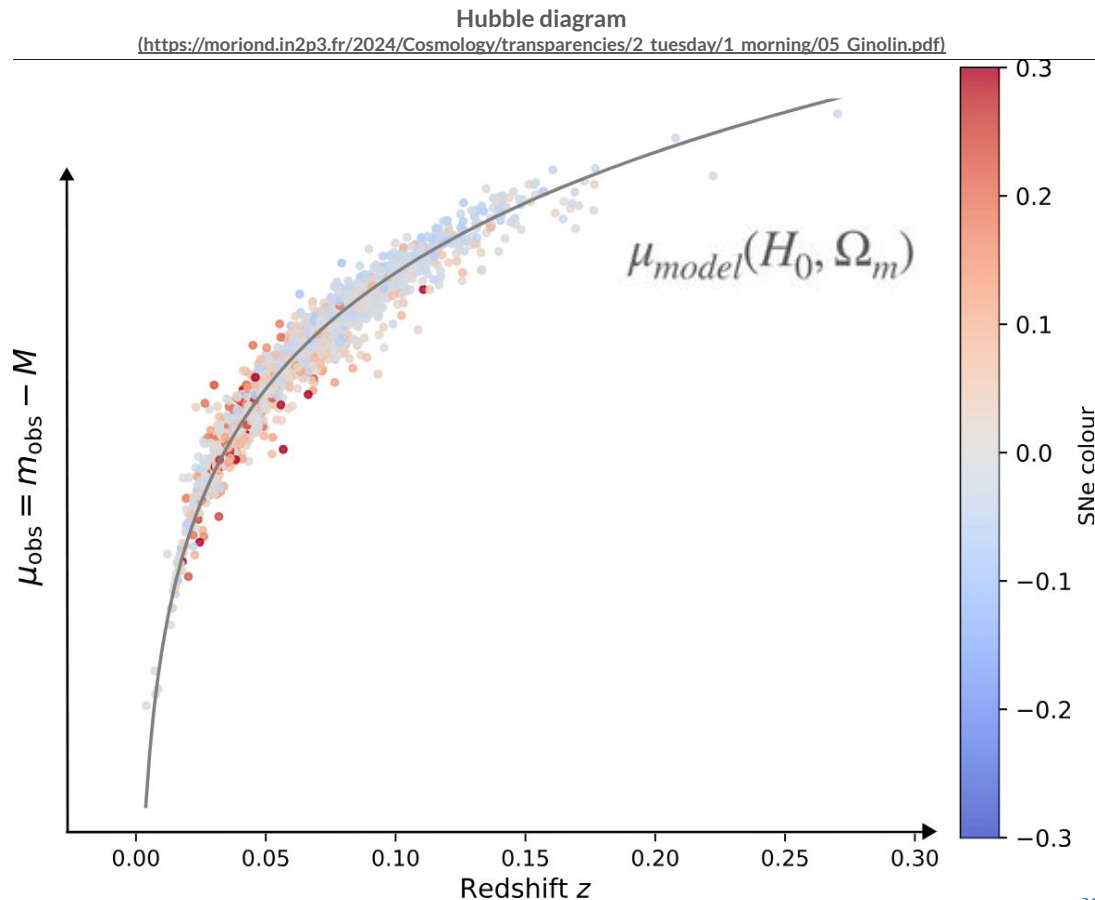
$$\mu = m_B^* - M_B - \beta c + \alpha x_1 - \gamma p$$

Standardized Hubble diagram

Distance modulus:

$$\mu = m_B^* - M_B - \beta c + \alpha x_1 - \gamma p$$

⇒ μ dispersion reduced to ~14%



Standardized Hubble diagram

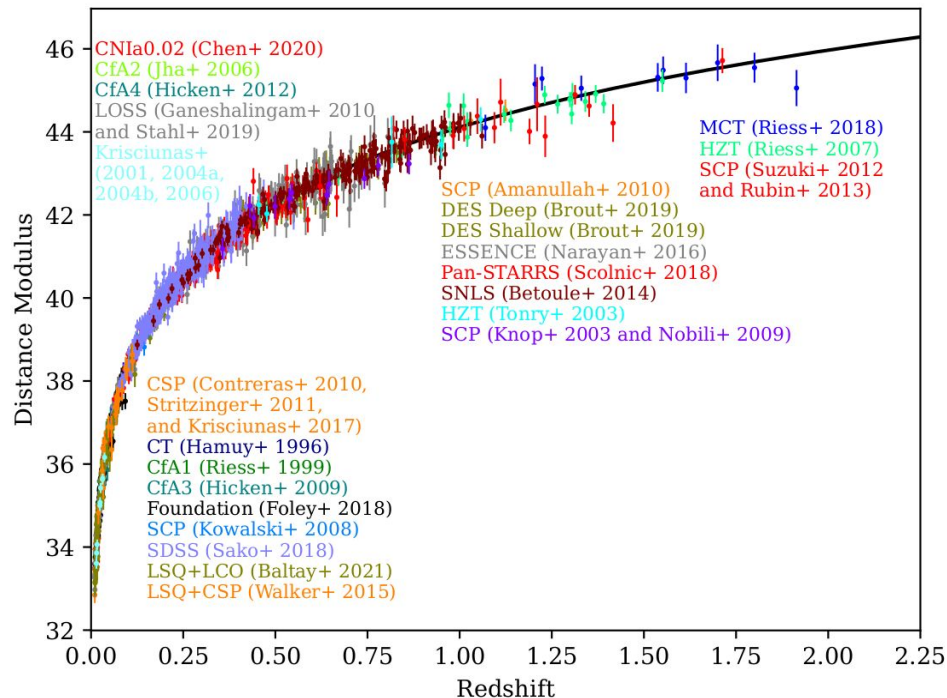
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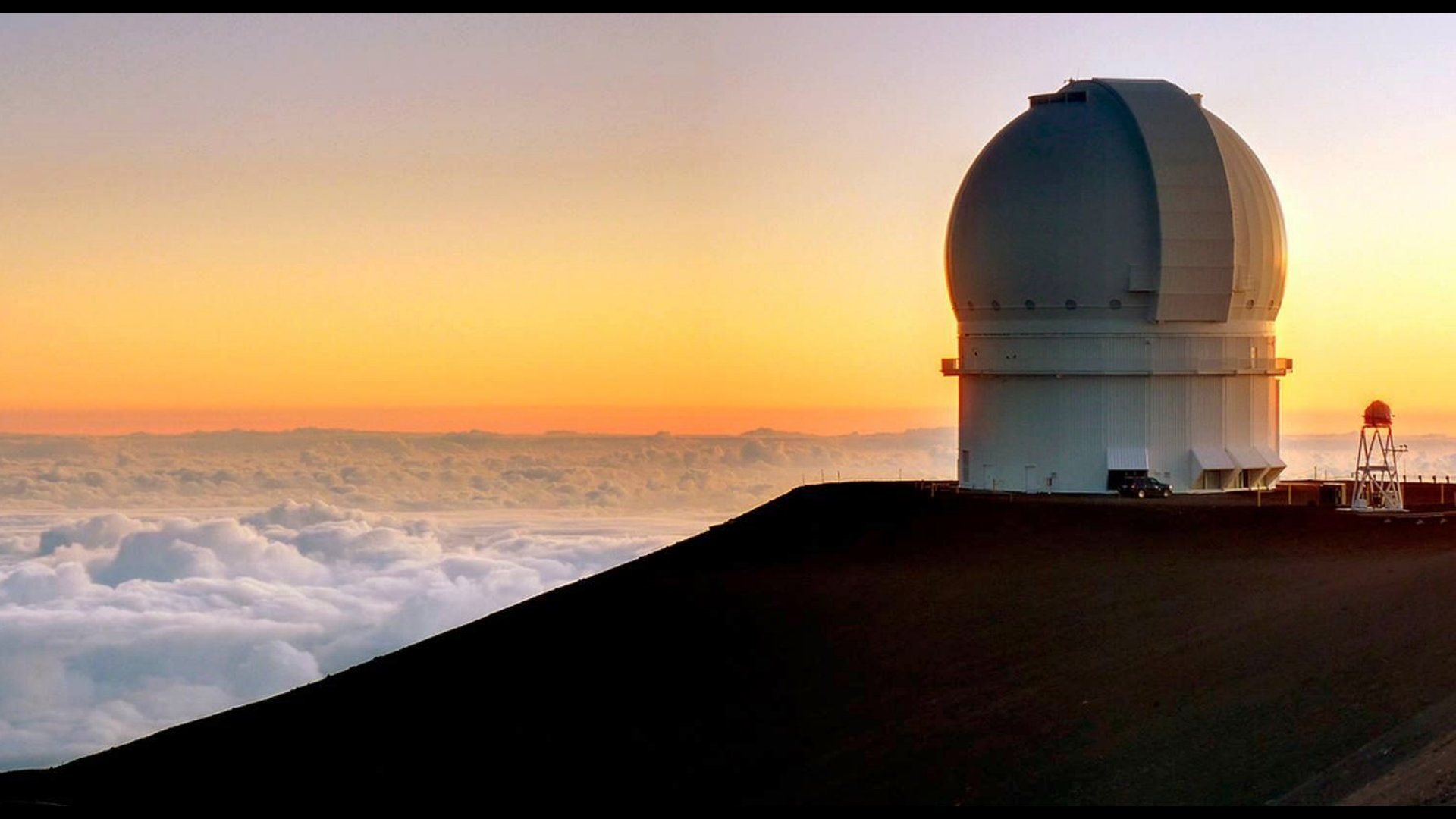
⇒ μ dispersion reduced to ~14%

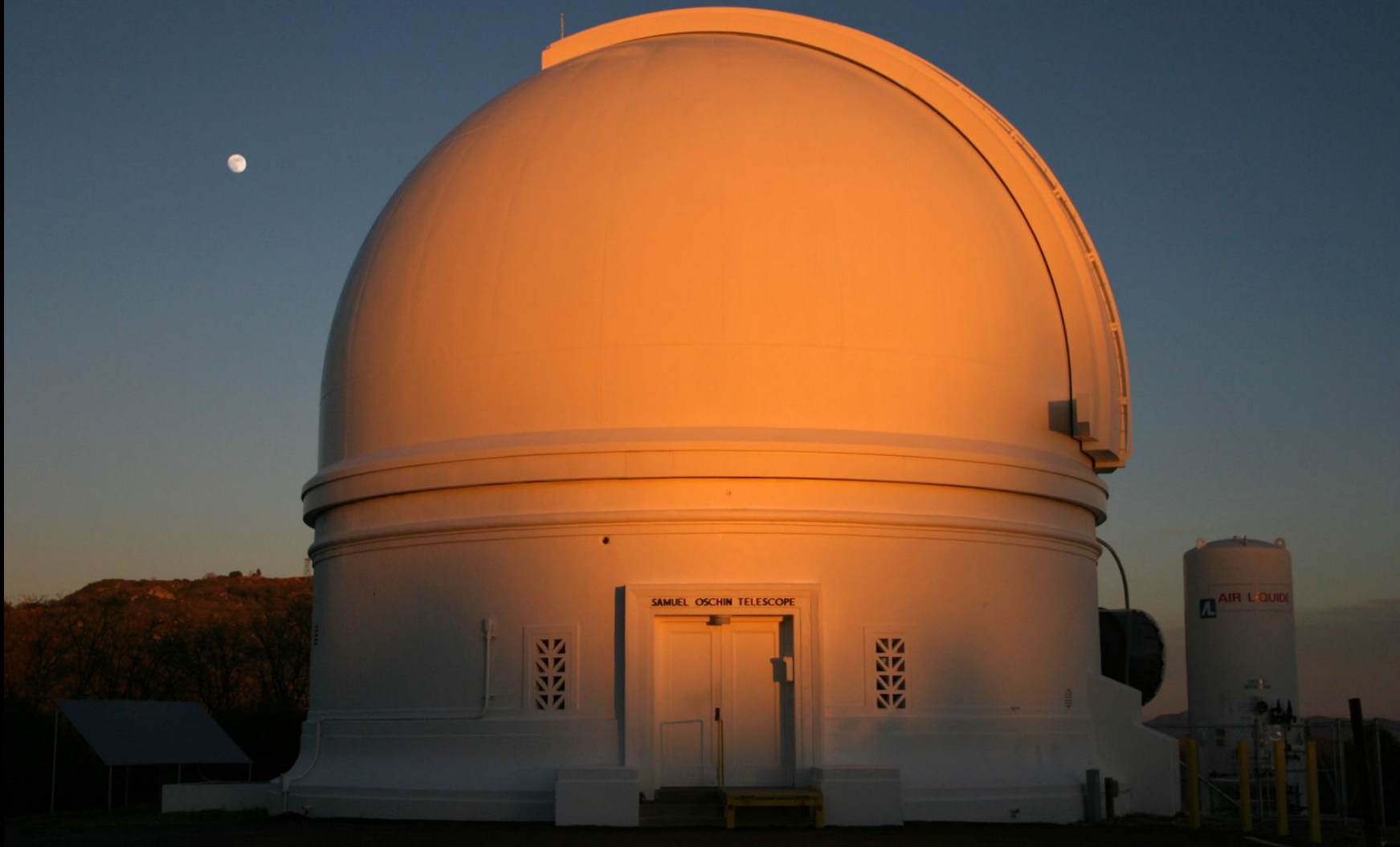
⇒ Infer constraints on cosmological parameters such as w

Hubble diagram (Rubin et al., 2023)



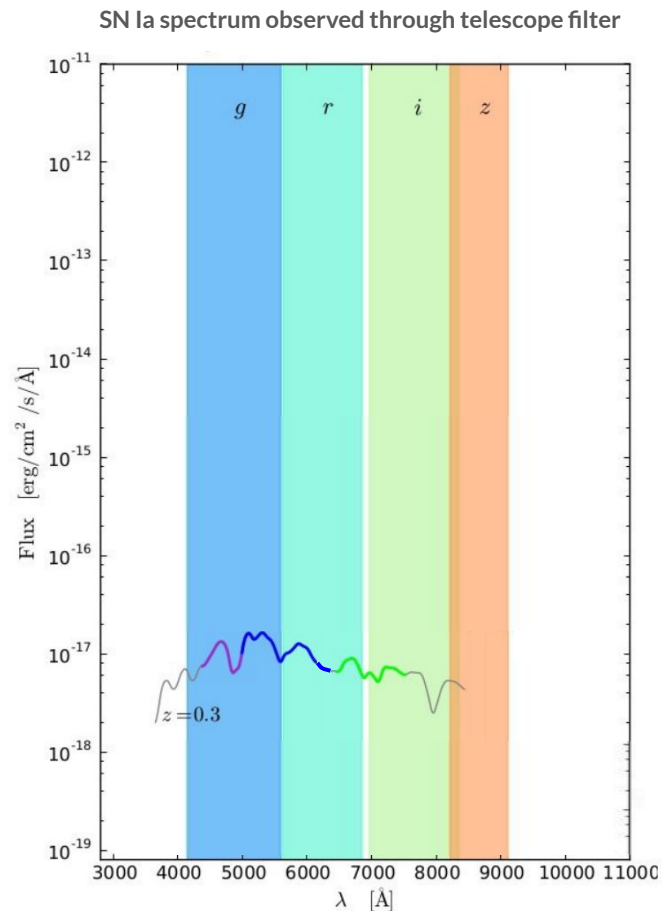
3. Photometric calibration





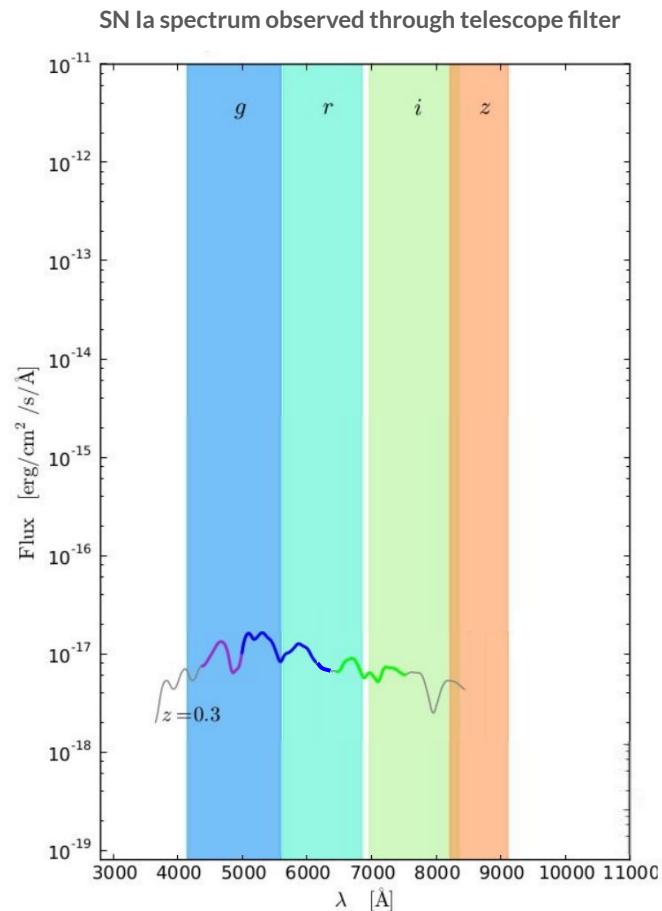


SNe Ia flux measurement



$$F_X = \int \lambda d\lambda \times \overset{\text{SN spectrum}}{S_\star(\lambda)} \overset{\text{X filter transmission}}{T_X(\lambda)} \overset{\text{Atmosphere transmission}}{T_{\text{atm}}(\lambda)}$$

SNe Ia flux measurement



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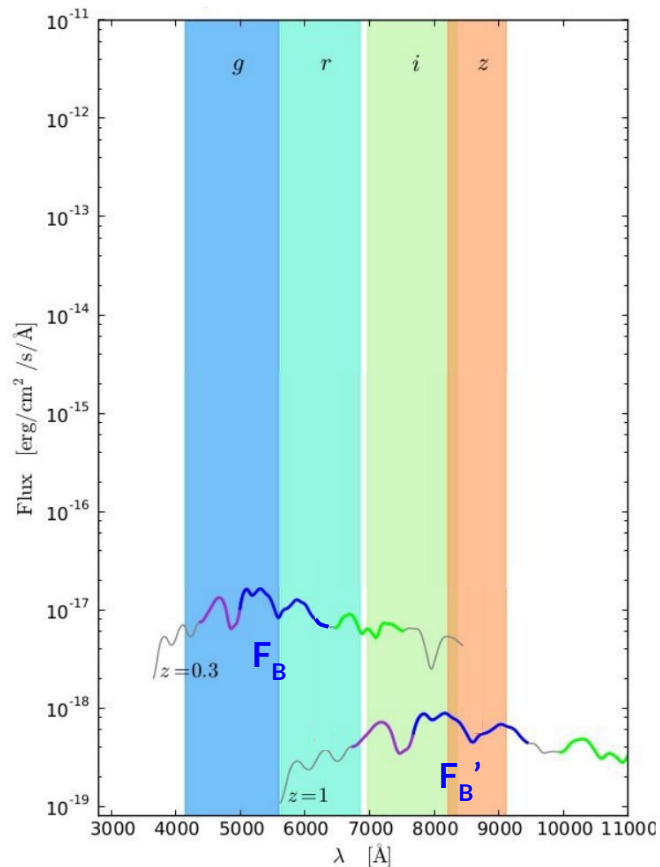
Section 5

Section 6

SNe Ia flux measurement

$$F_X = \int \lambda d\lambda \times S_{\star}(\lambda) T_X(\lambda) T_{\text{atm}}(\lambda)$$

SN Ia spectrum observed through telescope filter



Goal : Measure relatively F_B of SNe spectra at different redshift z

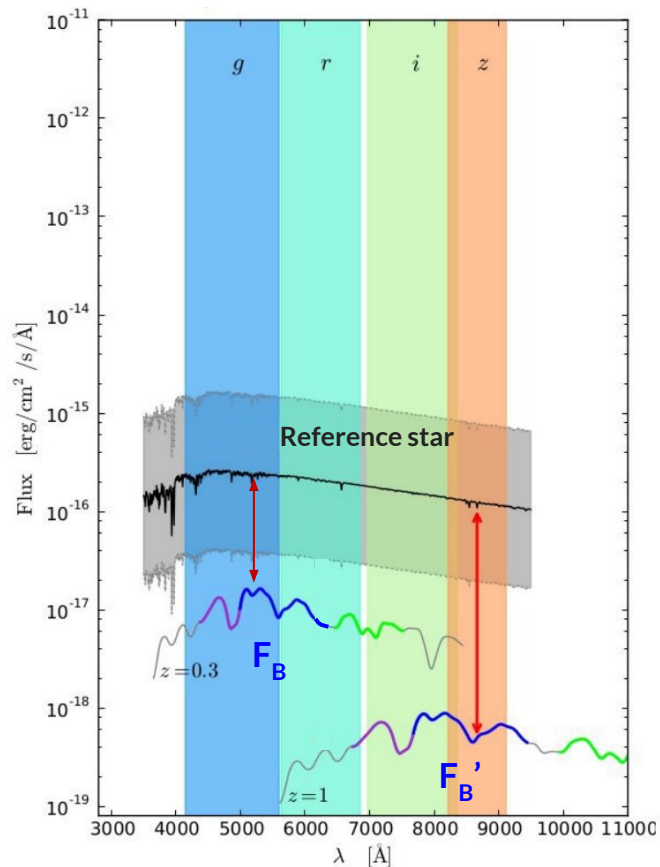
But :

- spectra extend on several filters
- F_B for different redshift z is measured in different bands

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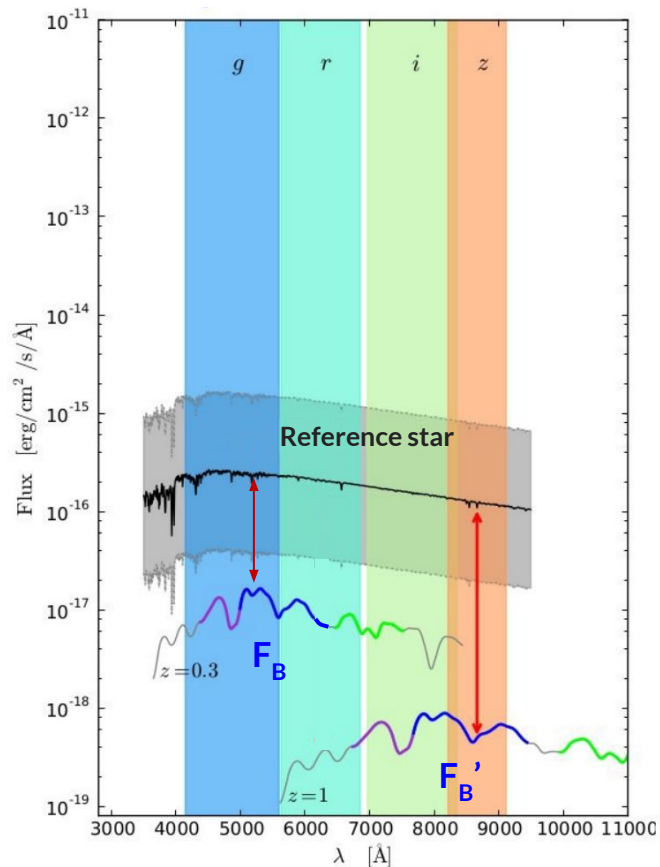
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Reference star \Rightarrow calibrate the flux transmission for each filter

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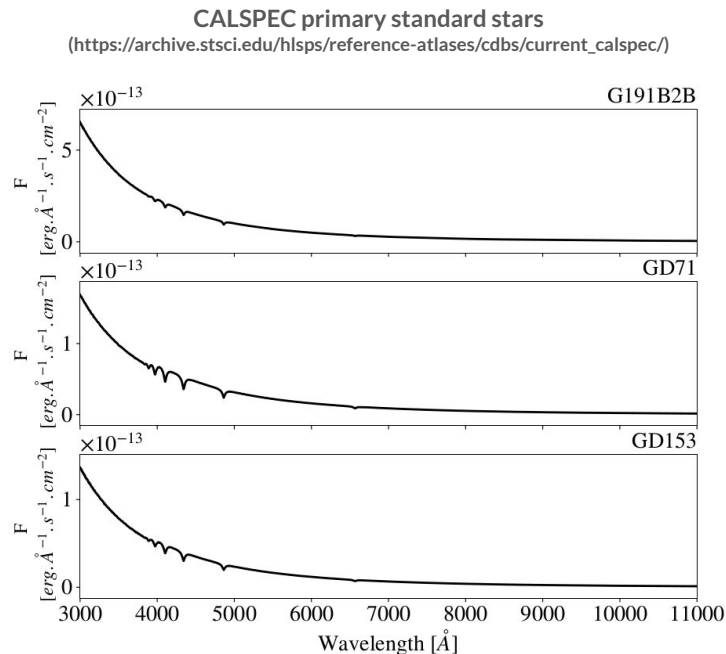
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Reference star \Rightarrow calibrate the flux transmission for each filter

\Rightarrow CALSPEC calibration

CALSPEC calibration

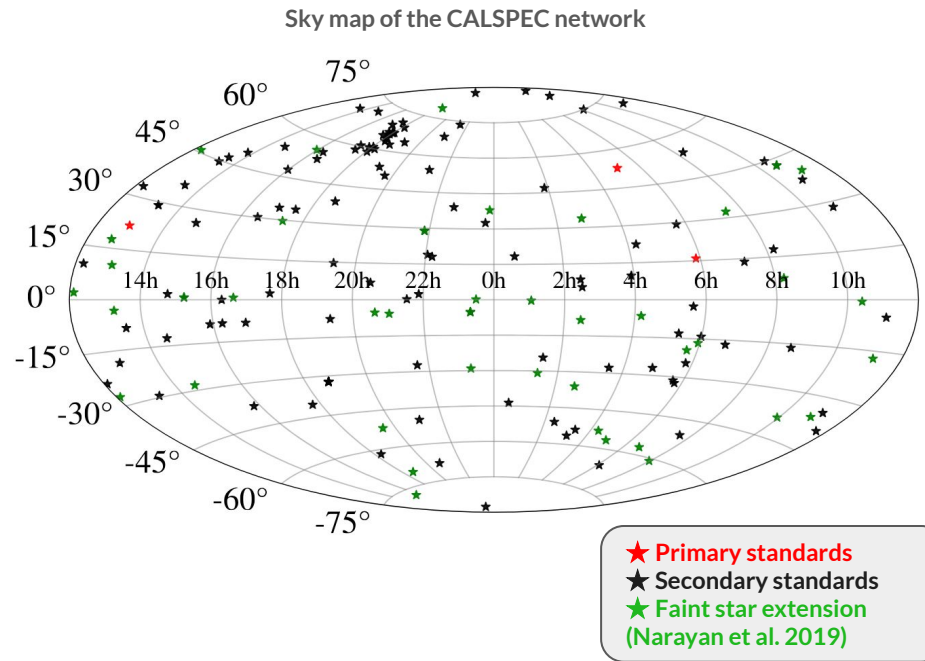
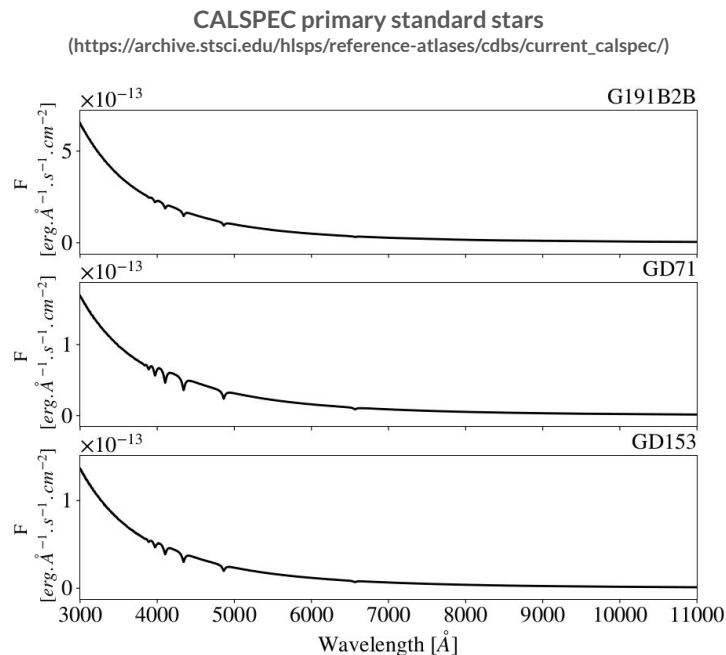
WD atmosphere model coupled with observations
with the Hubble Space Telescope



⇒ ~0.5% uncertainties in the optical wavelengths

CALSPEC calibration

WD atmosphere model coupled with observations
with the Hubble Space Telescope

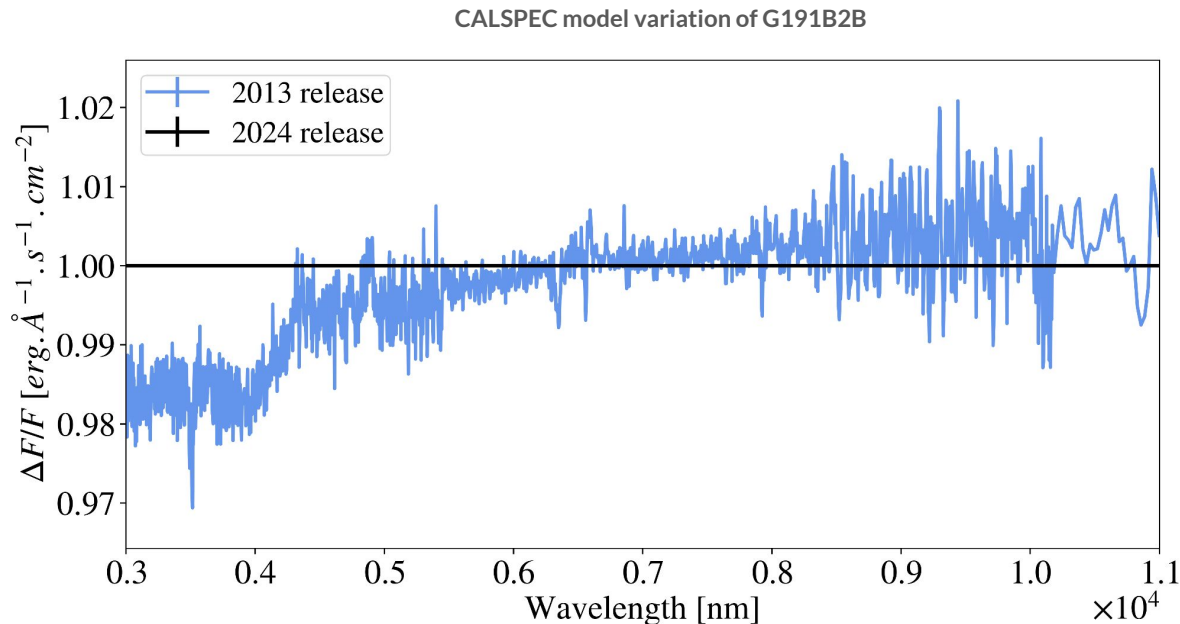


⇒ Network of calibrated sources covering
the full sky

⇒ ~0.5% uncertainties in the optical wavelengths

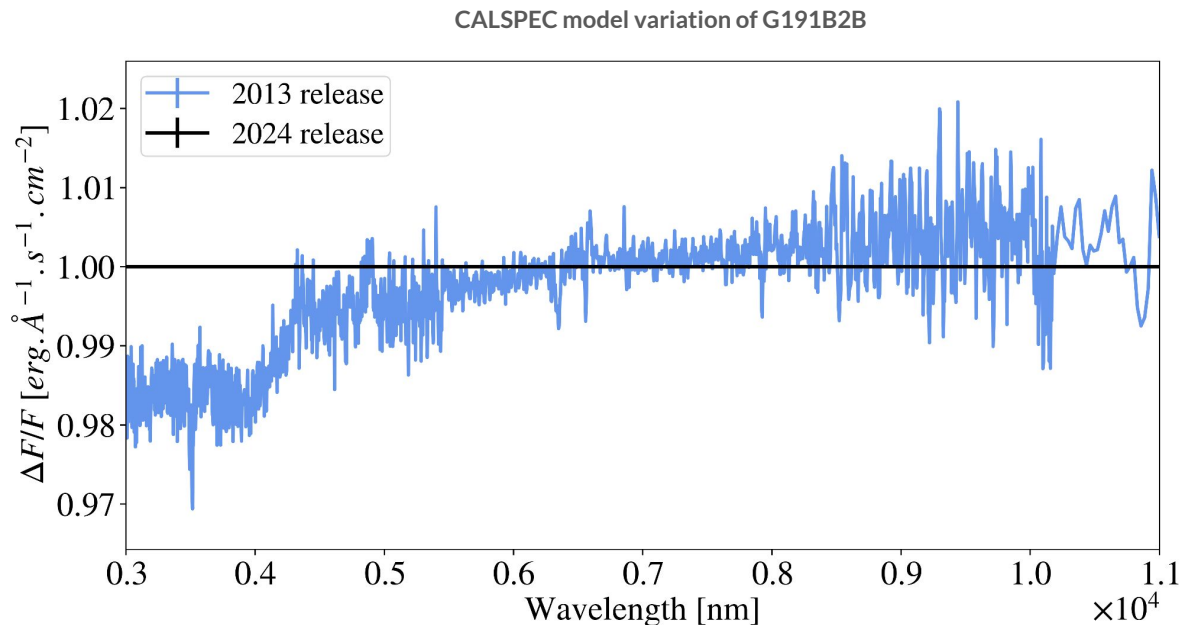
● Variations of CALSPEC model

- The white dwarf atmosphere model has evolved in the past 10 years
- **Chromatic variations of ~2%** between the first and last model



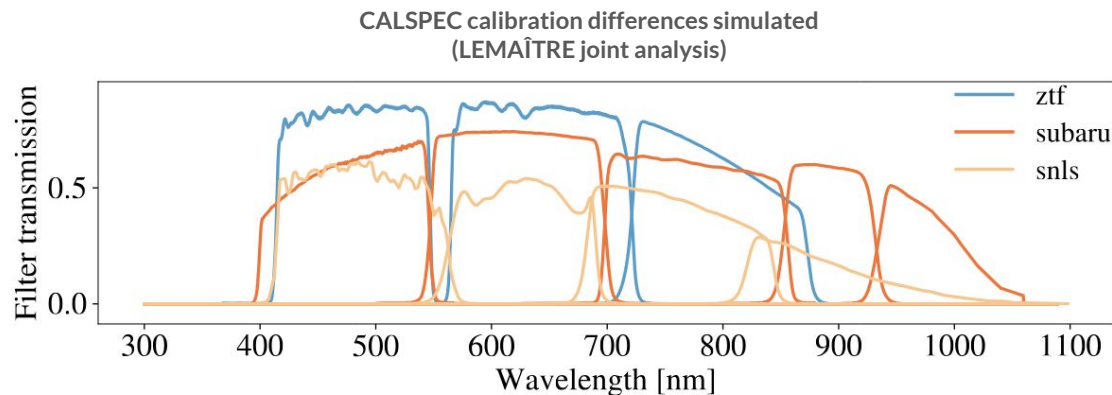
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Impact cosmological parameters inference? \Rightarrow Hubble diagram with simulated SNe Ia

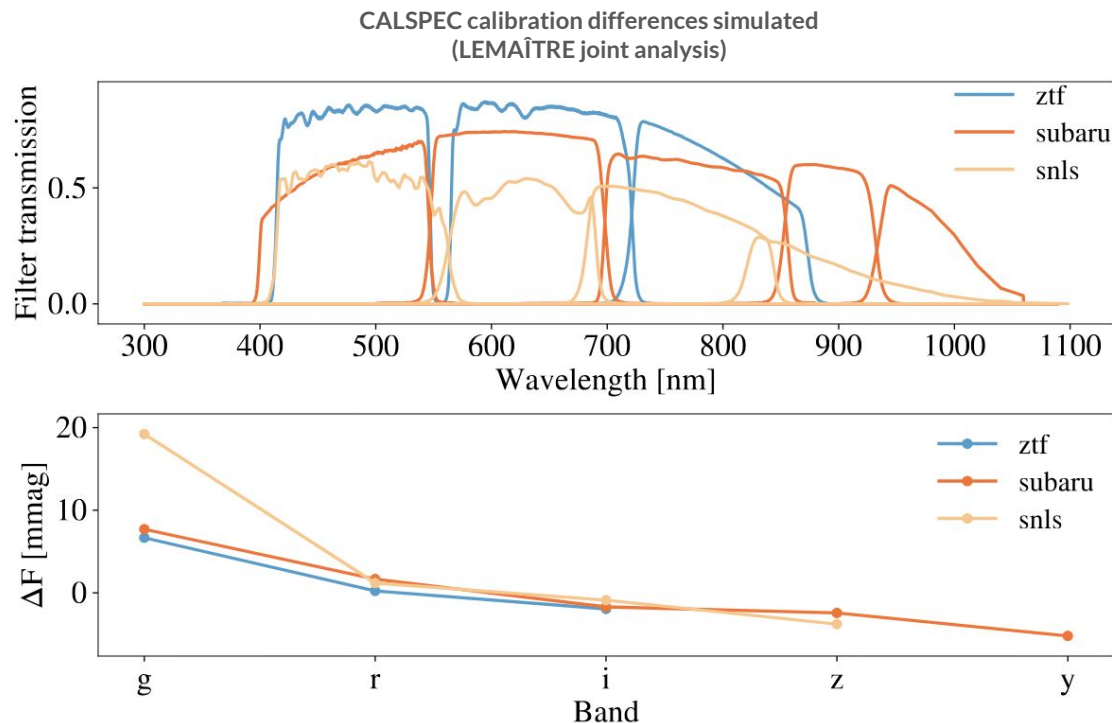
☐ Variations of CALSPEC model



Simulation of 3 SNe Ia surveys:

- Low-z: **ZTF DR2**
 - Intermediate-z: **SNLS yr5**
 - High-z: **Subaru**
-
- Calibration of the bandpass with each CALSPEC release

Variations of CALSPEC model



Simulation of 3 SNe Ia surveys:

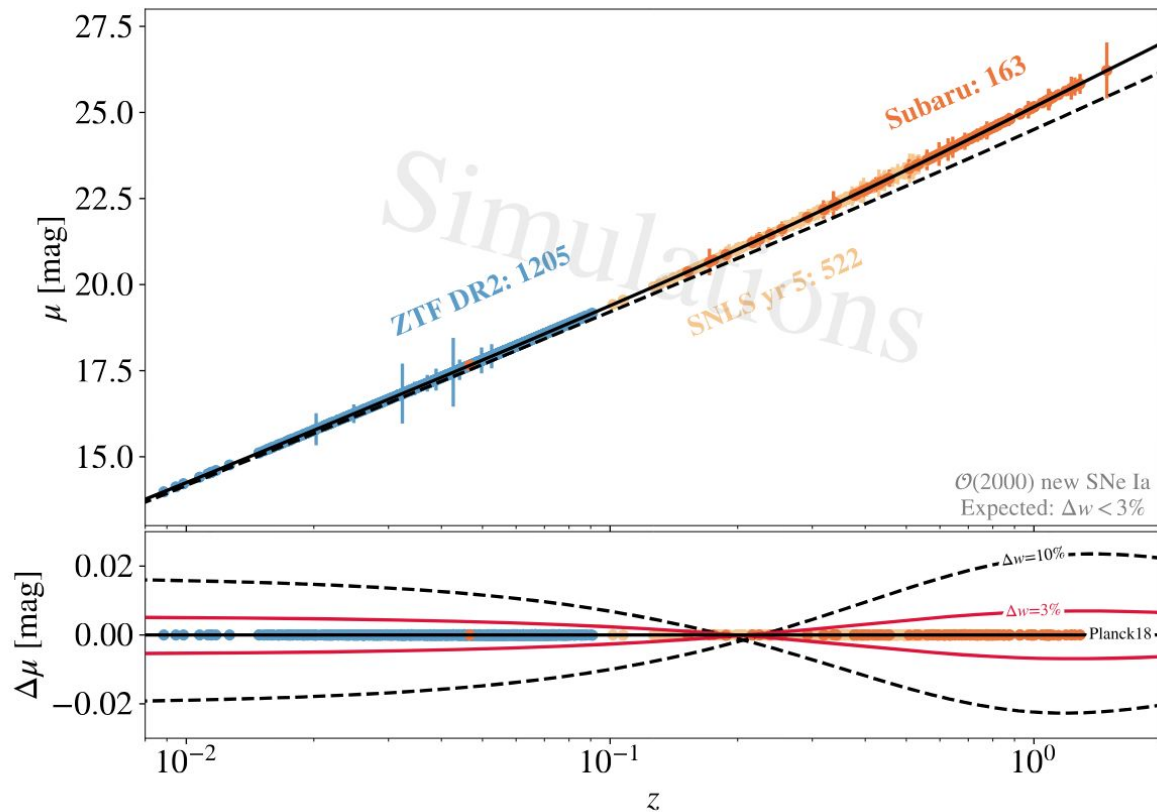
- Low-z: **ZTF DR2**
- Intermediate-z: **SNLS yr5**
- High-z: **Subaru**

- Calibration of the bandpass with each CALSPEC release

⇒ up to **20 milli-mag** difference

Variations of CALSPEC model

Hubble diagram obtained with LEMAÎTRE simulations

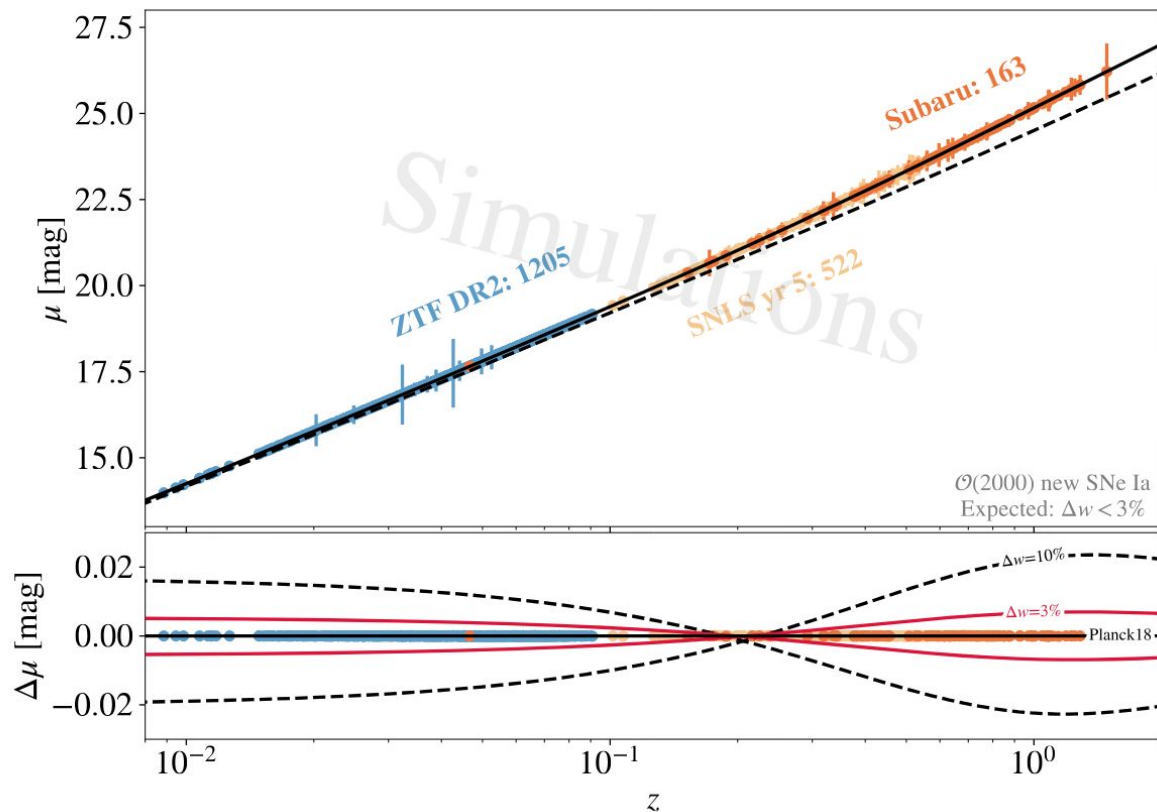


- Fitting distance moduli μ of simulated SNe Ia

⇒ Hubble diagram

Variations of CALSPEC model

Hubble diagram obtained with LEMAÎTRE simulations



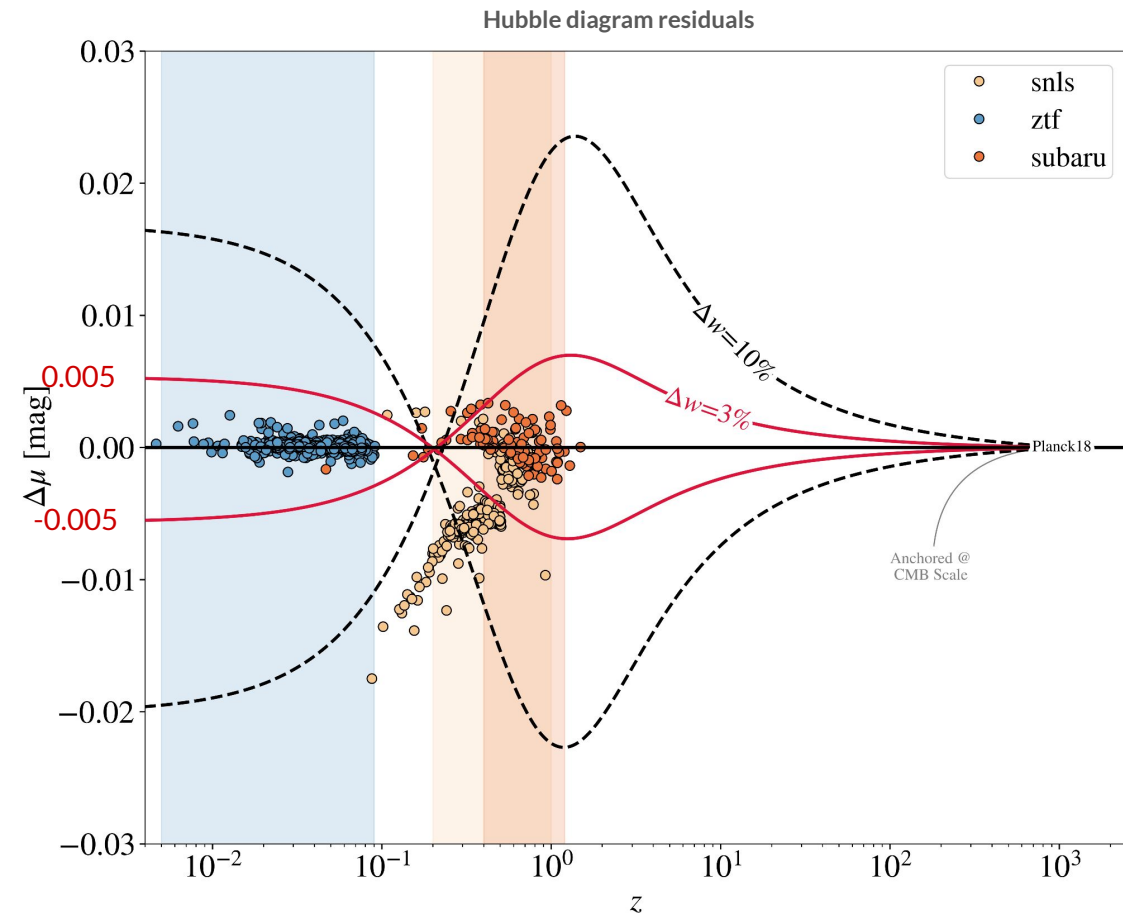
- Fitting distance moduli μ of simulated SNe Ia

⇒ Hubble diagram

- Adding flux calibration bias estimated with CALSPEC releases

⇒ focus on the residuals to the Λ CDM model

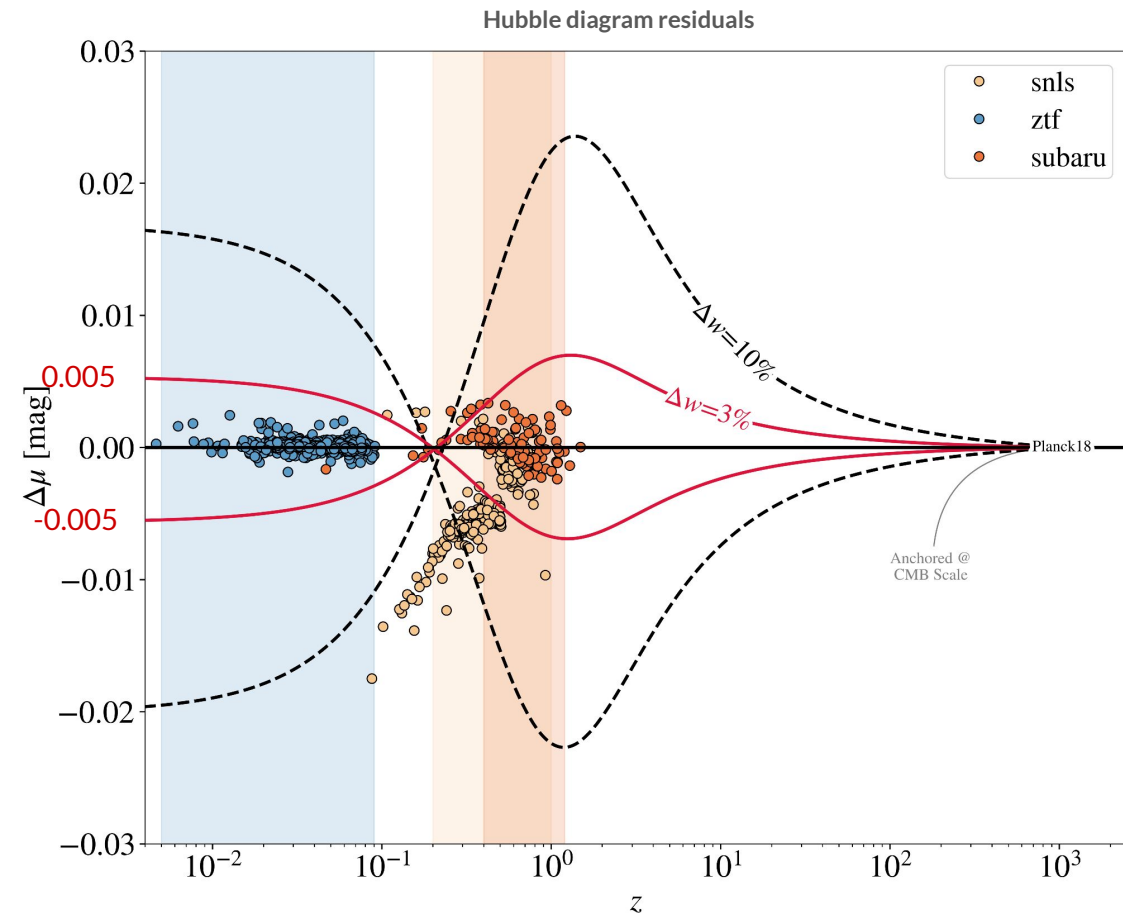
Variations of CALSPEC calibration



• 3% deviation of w from Λ CDM

$\Leftrightarrow \sim 0.005$ mag deviation in μ ($0.01 < z < 1$)

Variations of CALSPEC calibration



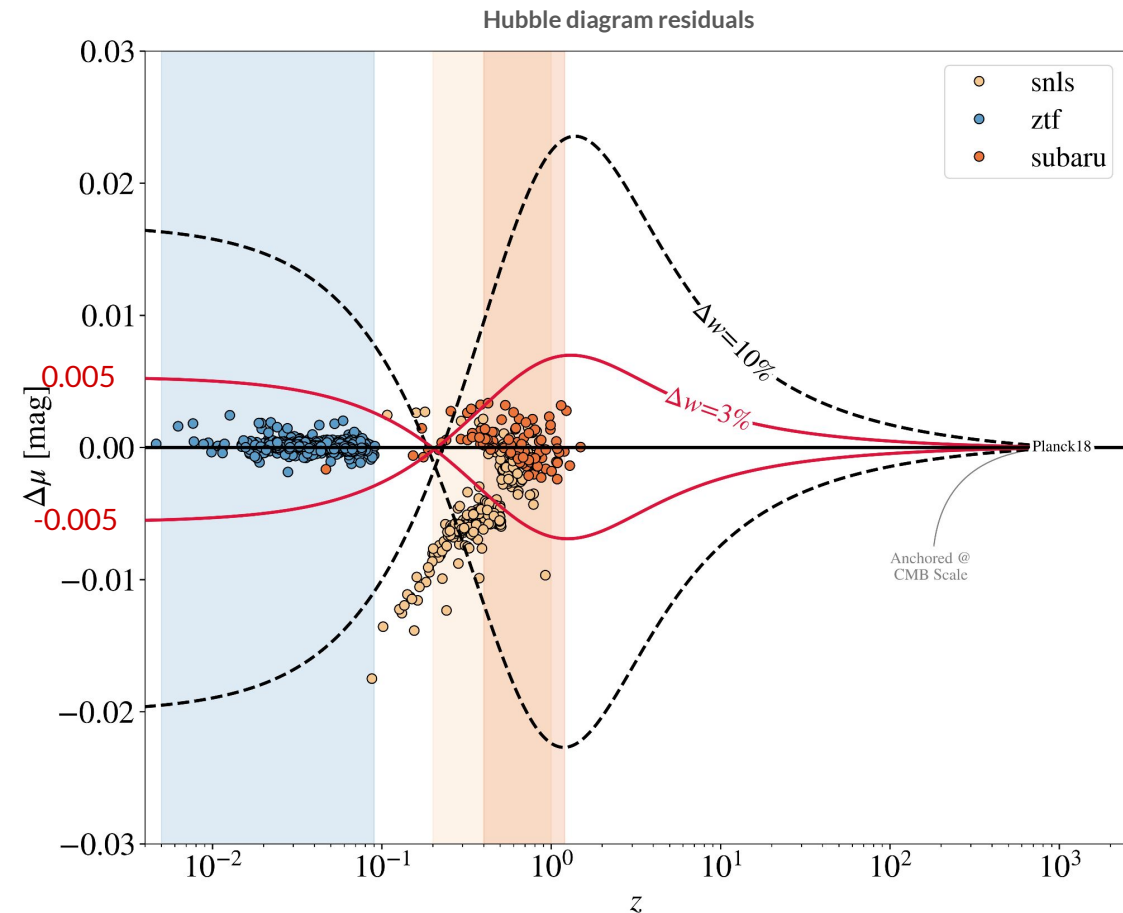
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2% chromatic bias $\Rightarrow \Delta\mu > 0.005$ mag

\Rightarrow deviation similar than $\Delta w > 3\%$

Variations of CALSPEC calibration



• 3% deviation of w from Λ CDM

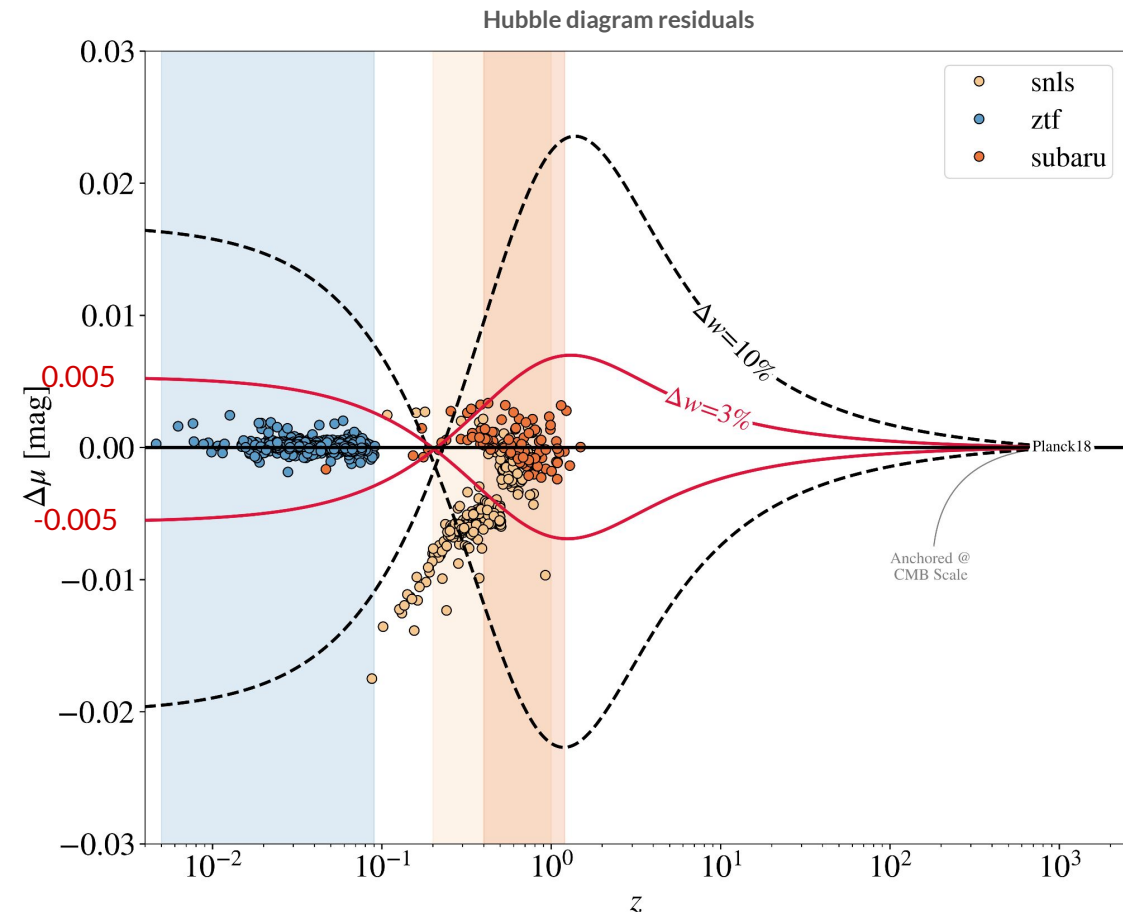
$\Leftrightarrow \sim 0.005$ mag deviation in μ ($0.01 < z < 1$)

2% chromatic bias $\Rightarrow \Delta\mu > 0.005$ mag

\Rightarrow deviation similar than $\Delta w > 3\%$

How much confident are we about WD atmosphere models?

Variations of CALSPEC calibration



- 3% deviation of w from Λ CDM

$\Leftrightarrow \sim 0.005$ mag deviation in μ ($0.01 < z < 1$)

2% chromatic bias $\Rightarrow \Delta\mu > 0.005$ mag

\Rightarrow deviation similar than $\Delta w > 3\%$

How much confident are we about WD atmosphere models?

\Rightarrow Better not rely on model-dependant reference stars

II. The StarDICE experiment

4. Description of the experiment

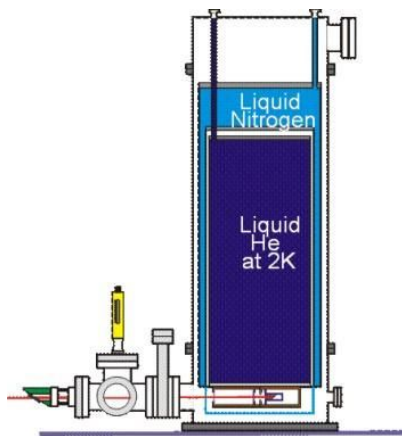
Photometric calibration transfer

Standard watt
(NIST)

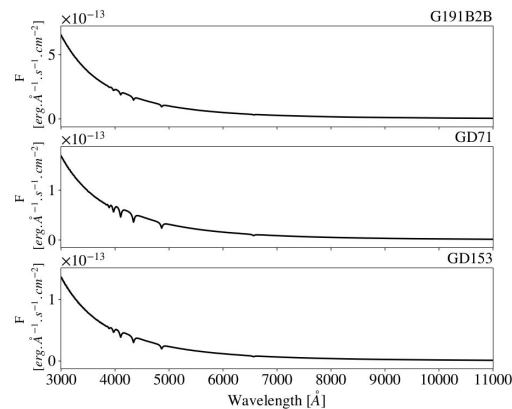
???

CALSPEC
standard stars

1 W

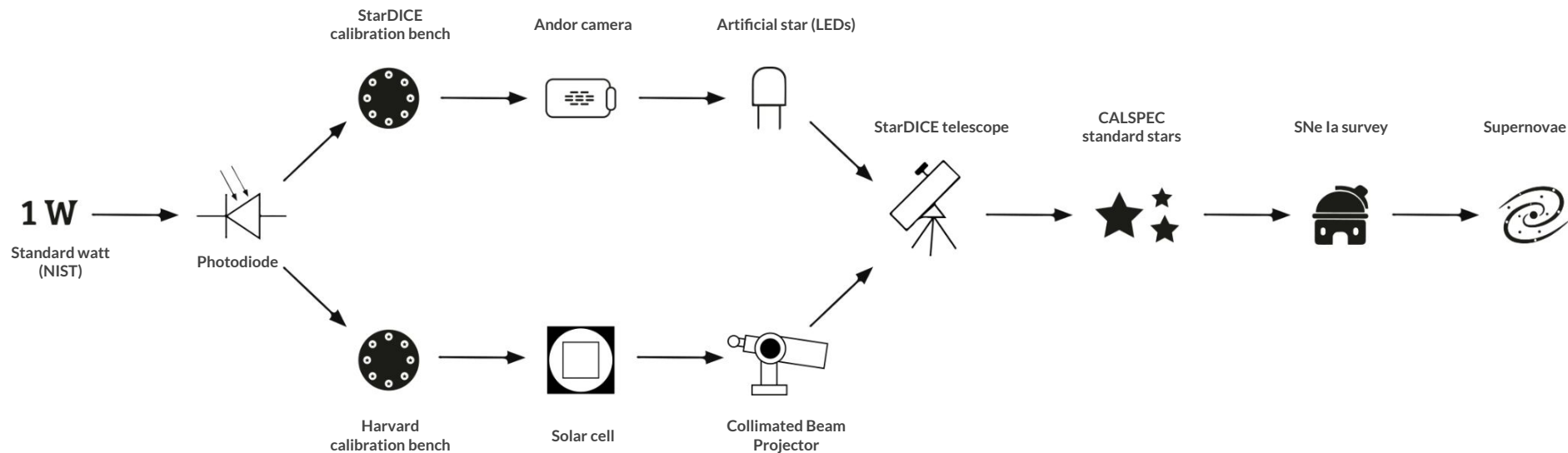


POWR facility
Houston et al. 2006



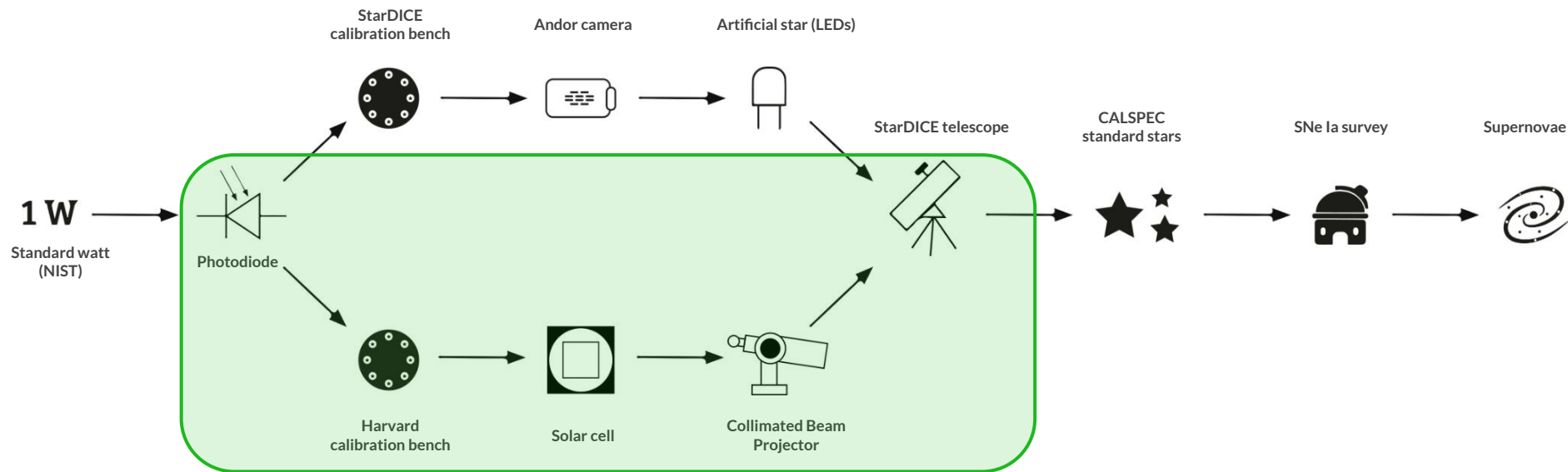
CALSPEC primary standard stars

Photometric calibration transfer



More sensitive detectors

Photometric calibration transfer



Pros: High wavelength resolution

Cons: Laboratory conditions, partial mirror illumination

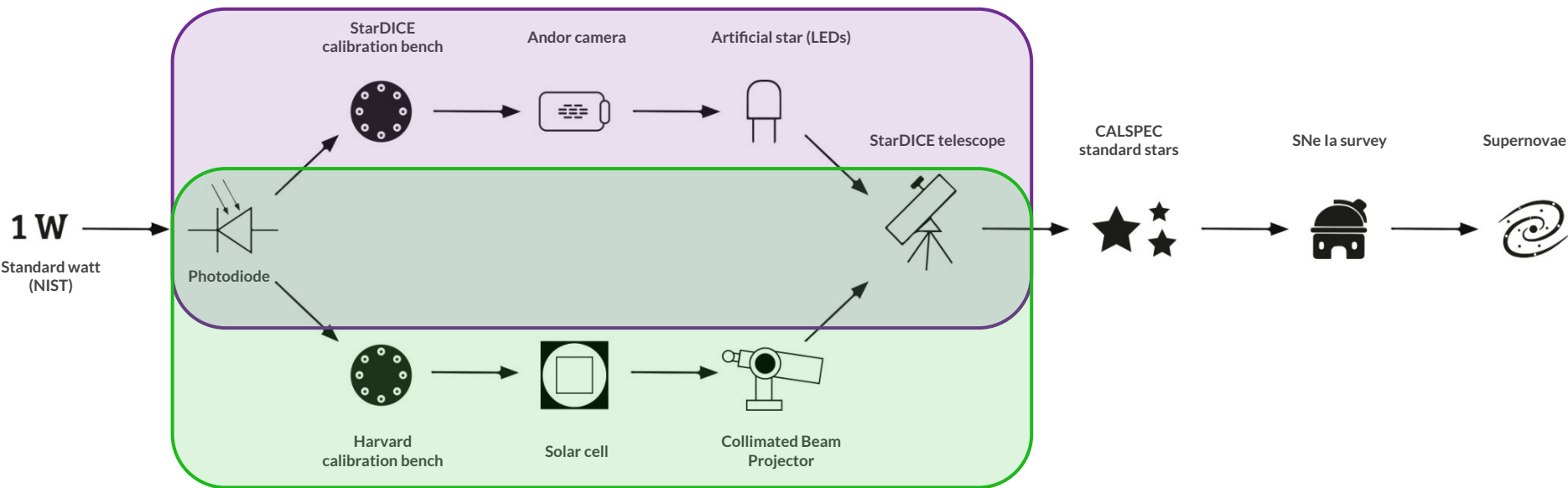
Section 5

More sensitive detectors

Photometric calibration transfer

Pros: In situ conditions, full pupil illumination

Cons: Broadband fluxes



Pros: High wavelength resolution

Cons: Laboratory conditions, partial mirror illumination

Section 5

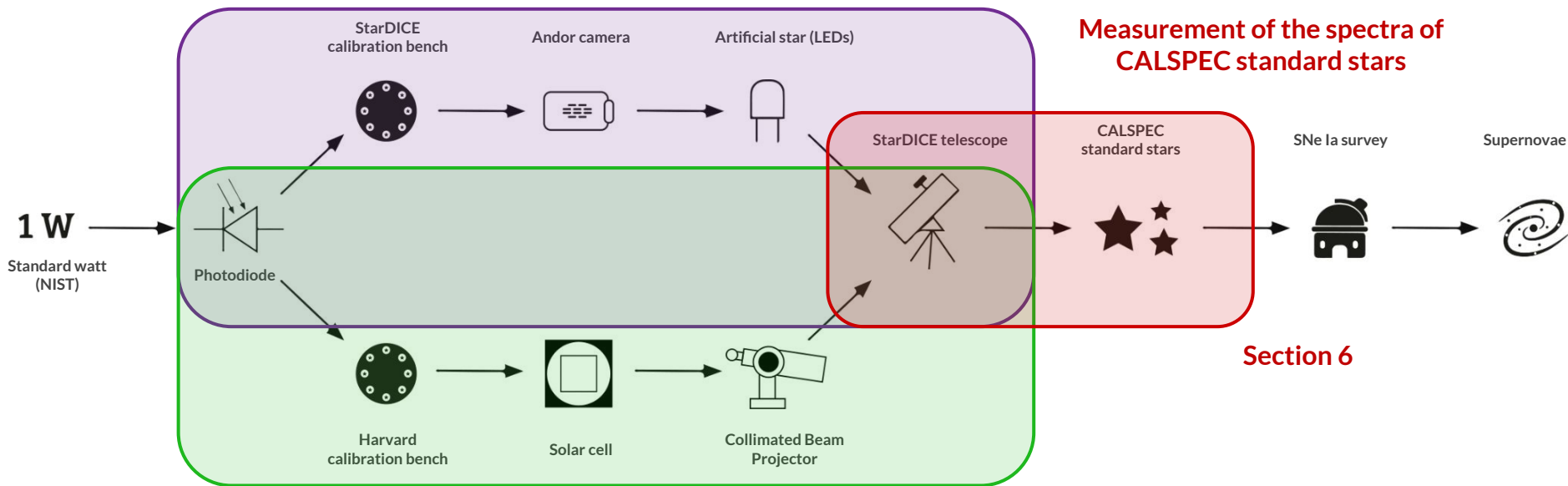
More sensitive detectors

Photometric calibration transfer

Pros: In situ conditions, full pupil illumination

Cons: Broadband fluxes

Measurement of the spectra of
CALSPEC standard stars



Pros: High wavelength resolution

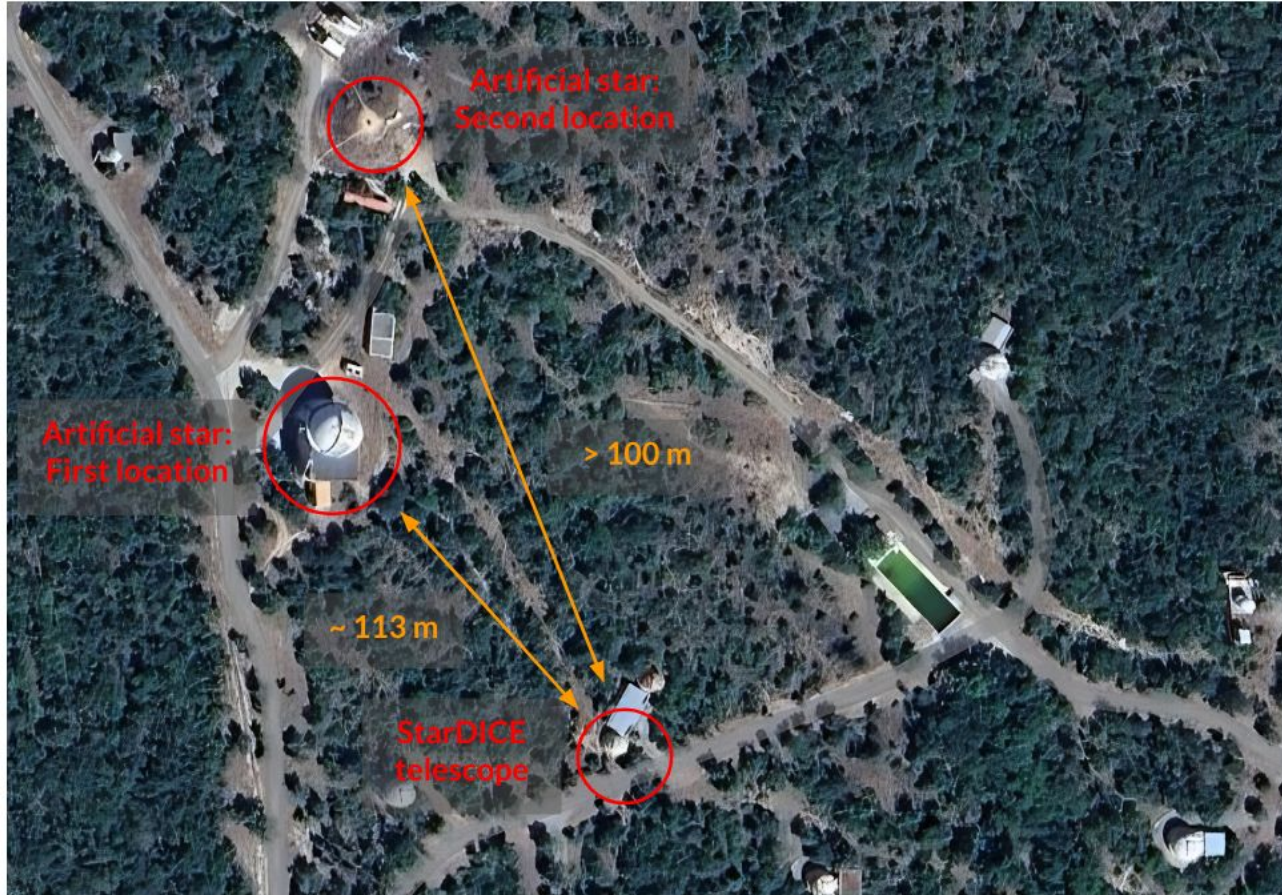
Cons: Laboratory conditions, partial mirror illumination

Section 5

Section 6

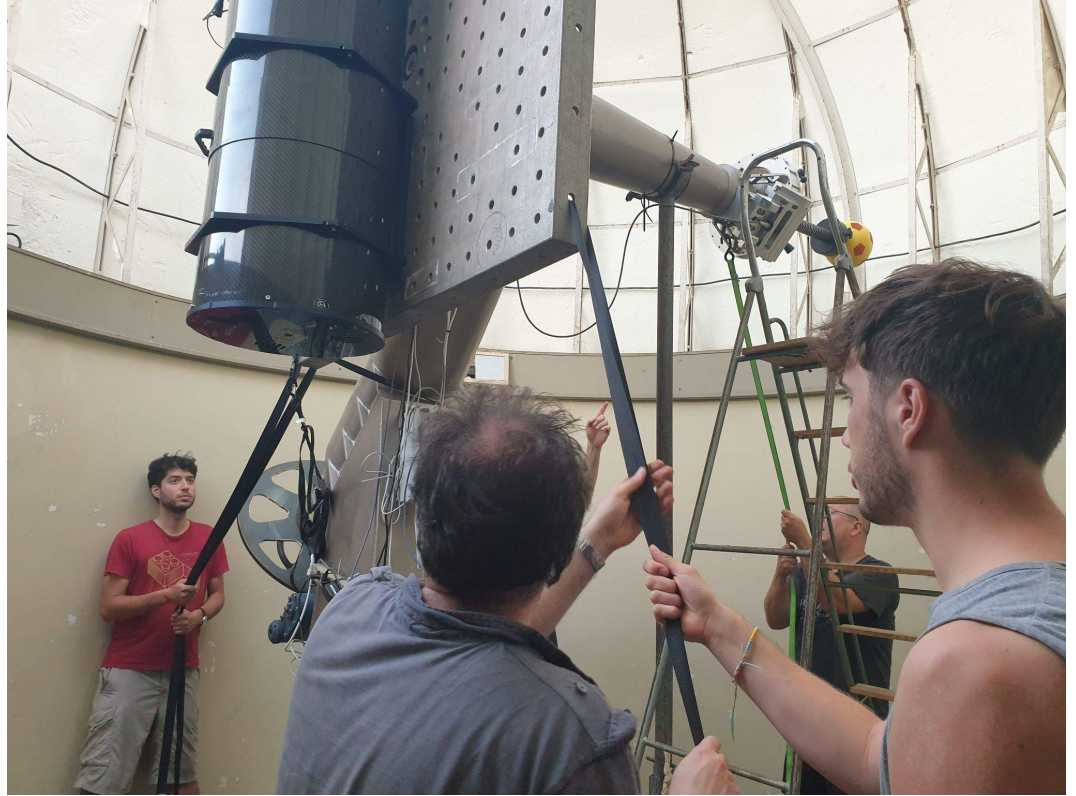
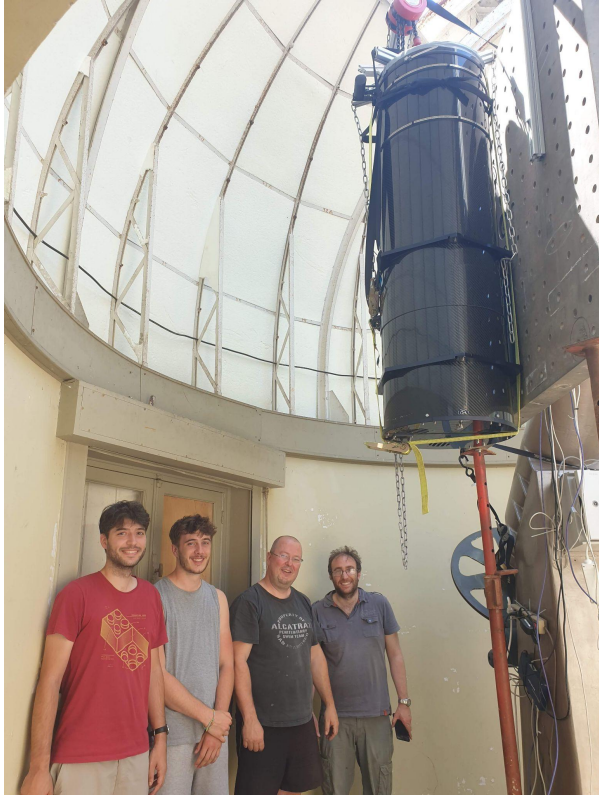
More sensitive detectors

Observatory of Haute-Provence



Observatoire de Haute-Provence satellite view

Installation of the telescope



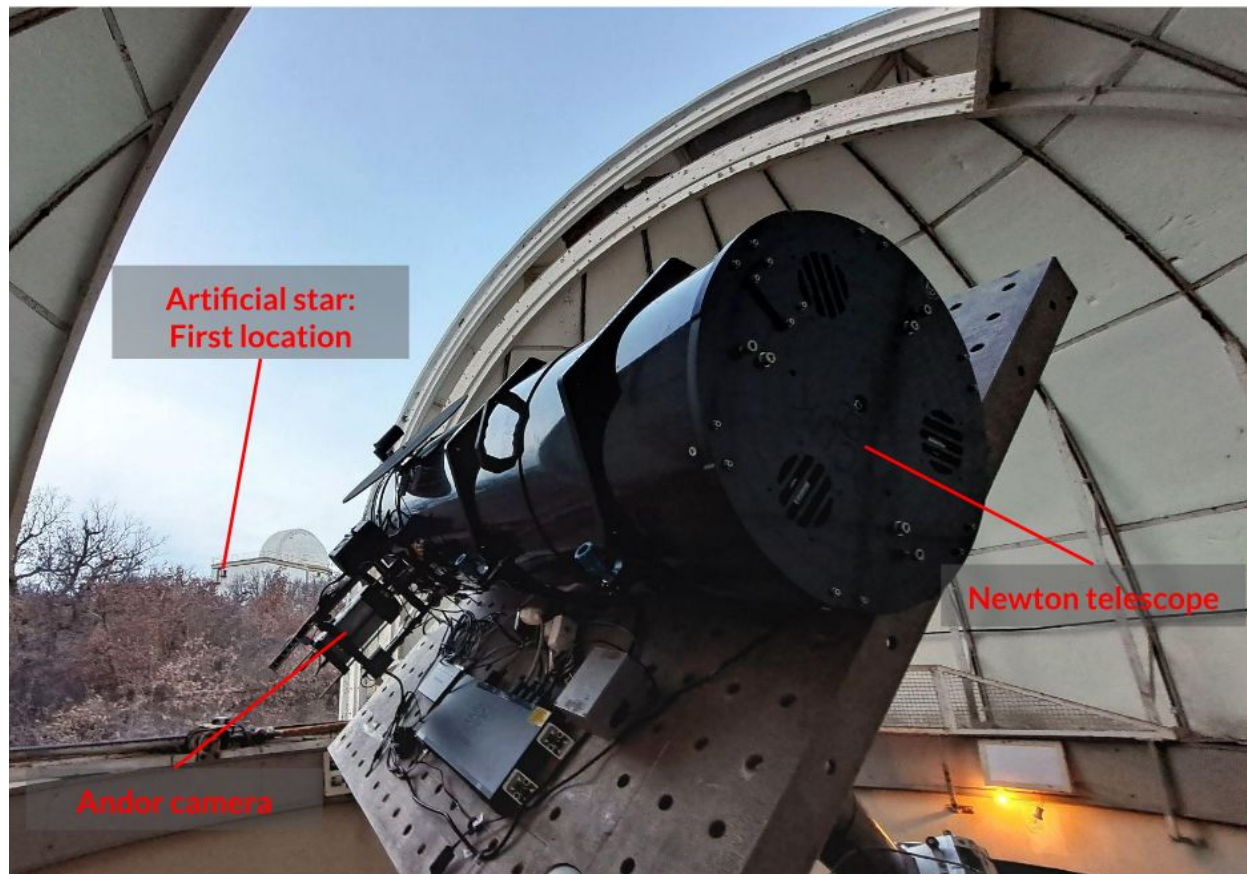
A happy StarDICE team (not pipe smoking) balancing the telescope they have installed

StarDICE telescope

StarDICE telescope on its mount

Newton telescope:

- $D=40\text{cm}$
- $f=1.6\text{m}$
- $1.68''$ resolution
- $28.6' \times 28.6'$ field of view



StarDICE telescope

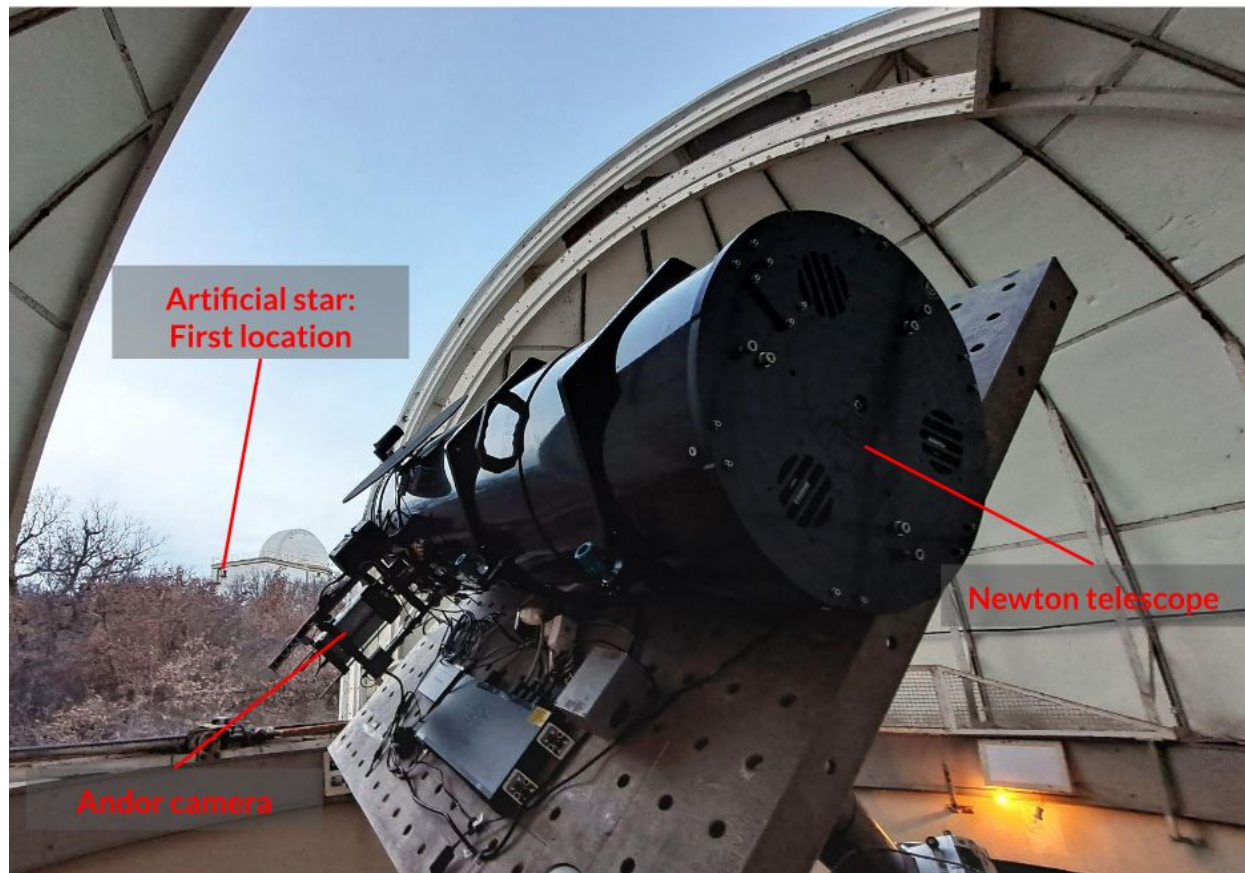
StarDICE telescope on its mount

Newton telescope:

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Filterwheel:

- “ugrizy” photometric filters
- Diffraction grating



StarDICE telescope

StarDICE telescope on its mount

Newton telescope:

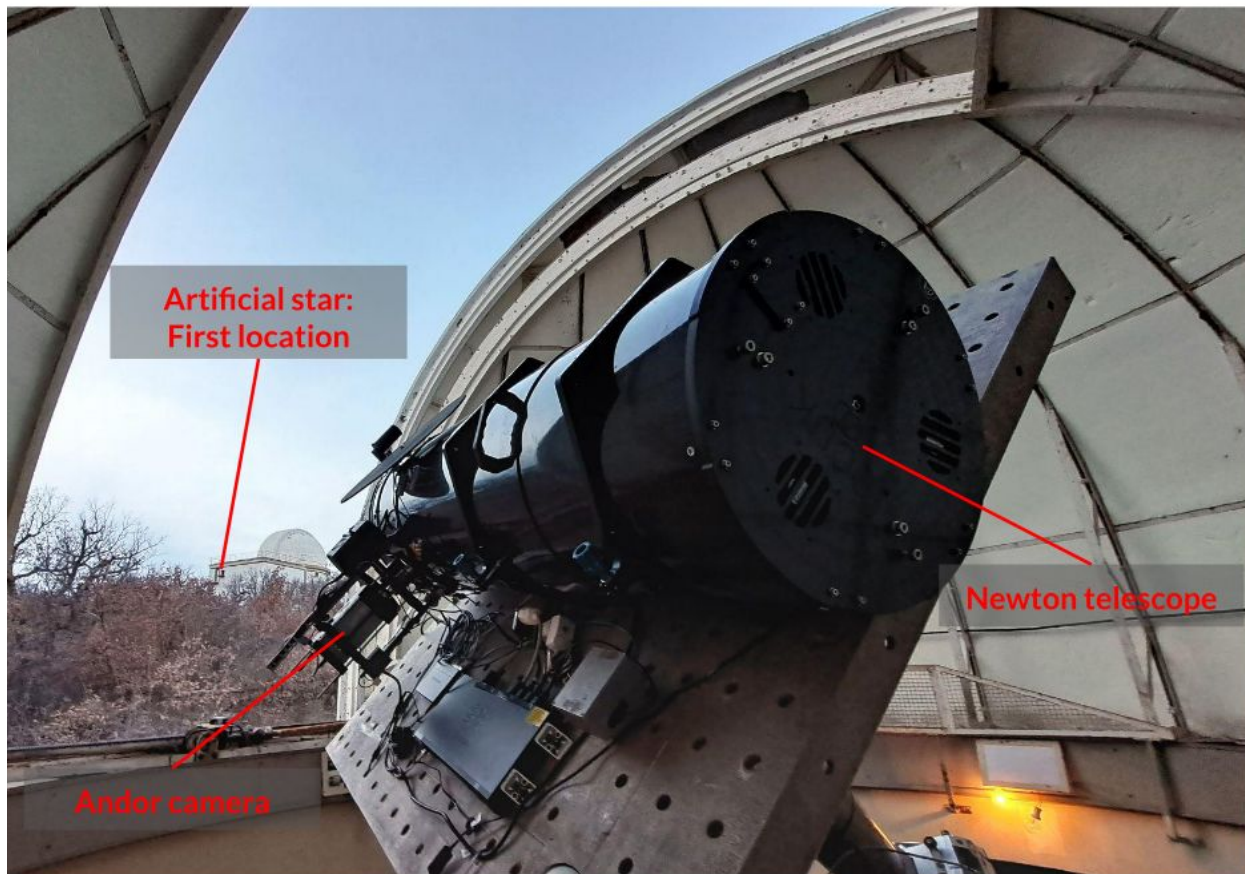
- $D=40\text{cm}$
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Filterwheel:

- “ugrizy” photometric filters
- Diffraction grating

Monitoring instruments:

- Hygrometer
- Thermometers
- Barometer
- Rain detector



StarDICE telescope

StarDICE telescope on its mount

Newton telescope:

- $D=40\text{cm}$
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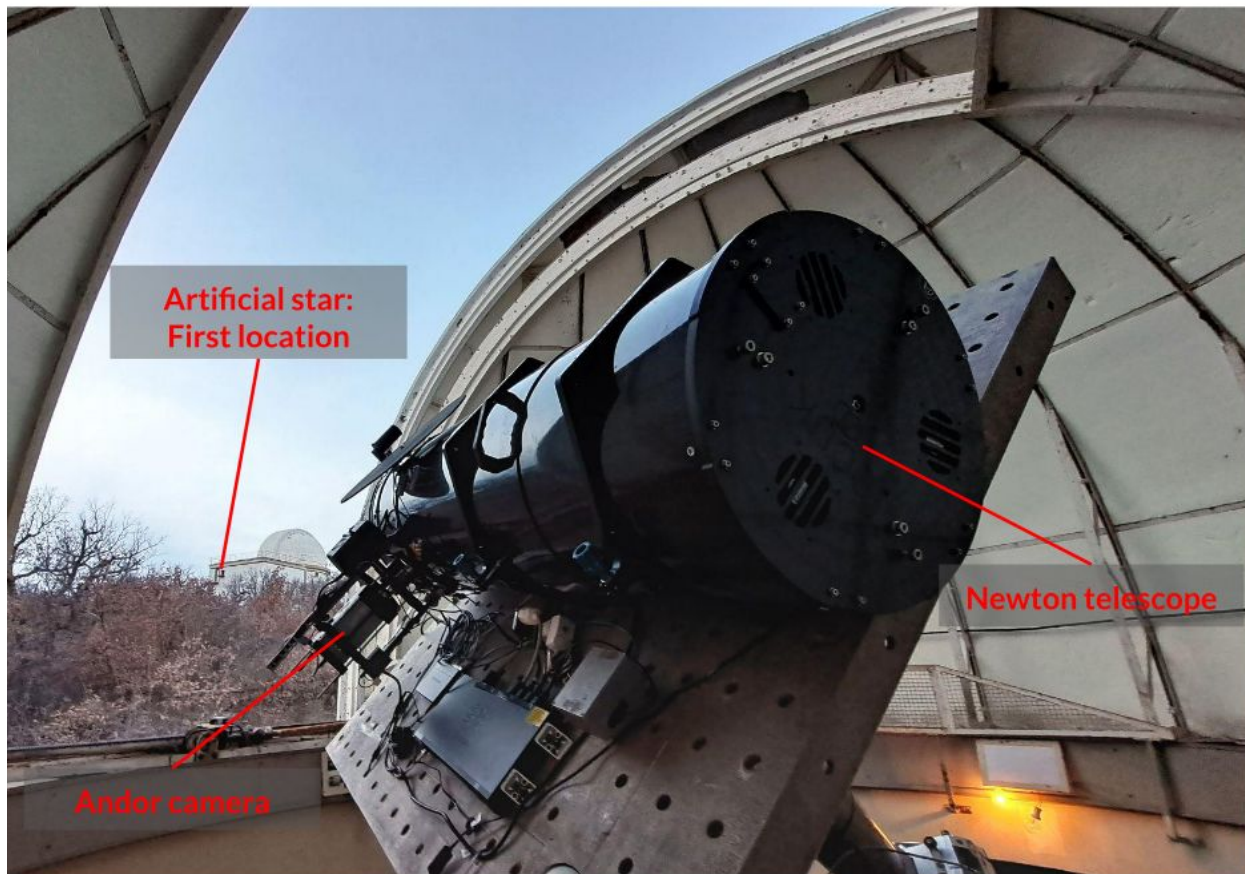
Filterwheel:

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Monitoring instruments:

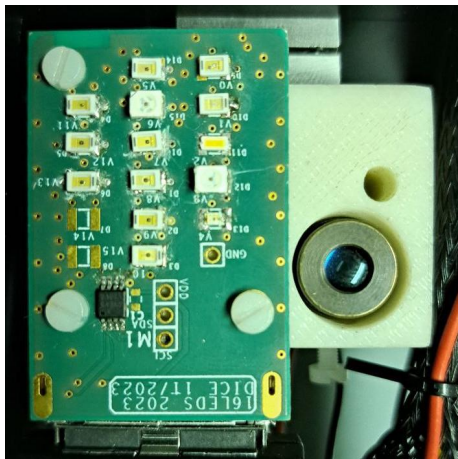
- Hygrometer
- Thermometers
- Barometer
- Rain detector

Fully robotic

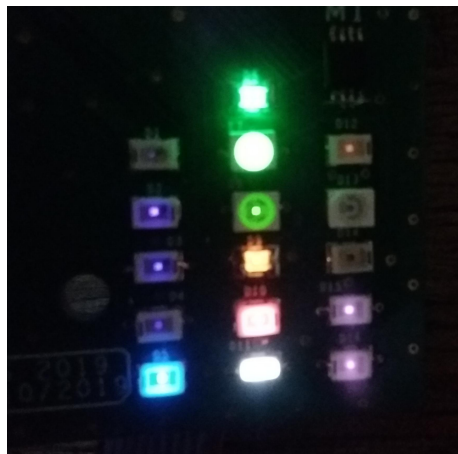


Artificial star

- 16 LEDs covering visible and near-IR range
- Flux calibrated in laboratory
- Mounted in July 2024 (after all the analyses I will present)



Artificial stars LEDs off



Artificial stars LEDs on

Helmet enclosing the artificial star



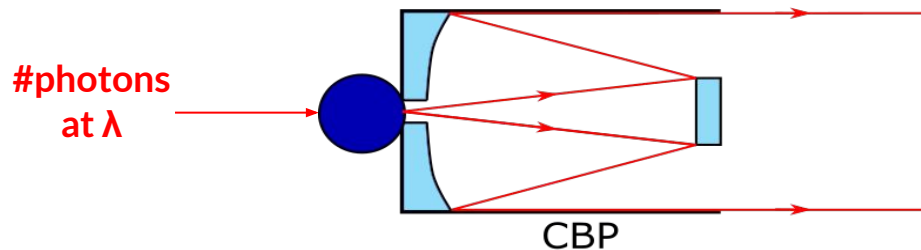
5. Collimated Beam Projector

a. Setup description

What is a CBP ?

CBP, for **Collimated Beam Projector**, is a **calibration device** emitting a **monochromatic light** of **known flux**, in a **parallel beam**

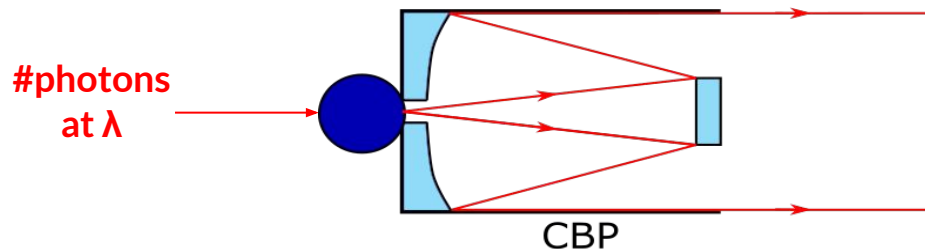
⇒ **calibrate** the **response** of a photometric instrument and its filters.



What is a CBP ?

CBP, for **Collimated Beam Projector**, is a **calibration device** emitting a **monochromatic light** of **known flux**, in a **parallel beam**

⇒ **calibrate** the **response** of a photometric instrument and its filters.



Two purposes:

- Calibrate the StarDICE telescope response
- Proof of concept for the CBP at Rubin Observatory for the LSST

How to use a CBP ?

Ingredients:

- A tunable laser
- A mounted-backward telescope to recreate a parallel beam from a point source
- A PhD student locked in the basement to make it work

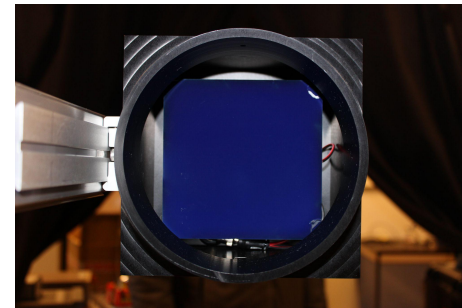
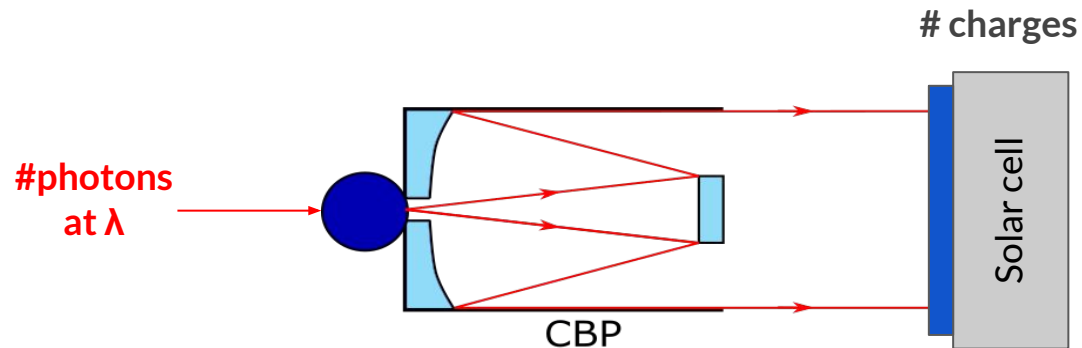
How to use a CBP ?

Ingredients:

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Recipe:

- (1) Shoot light inside a calibrated sensor to measure CBP optics throughput R_{CBP}



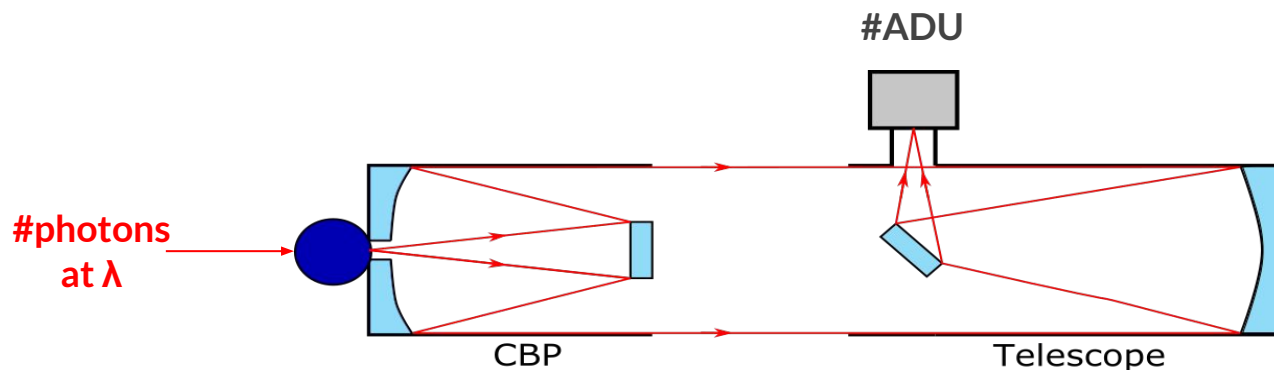
How to use a CBP ?

Ingredients:

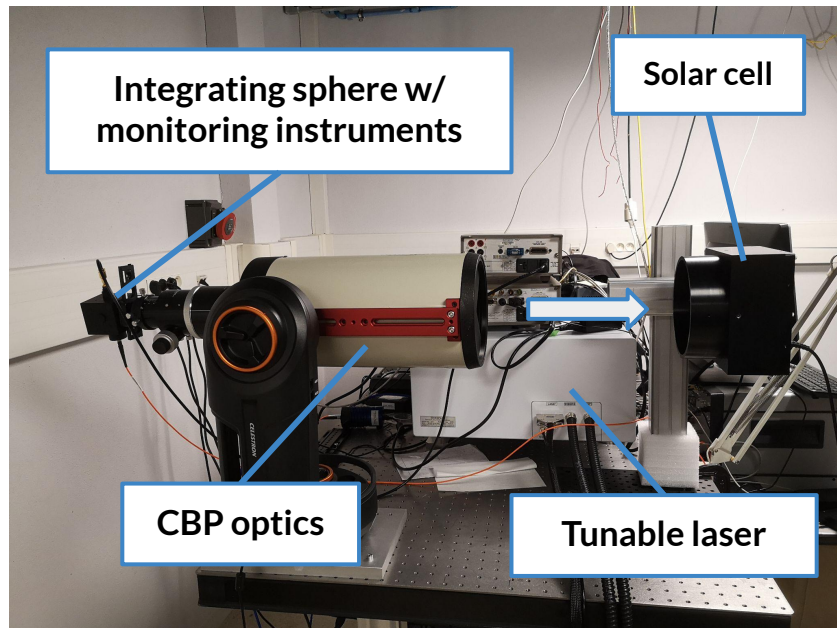
- A tunable laser
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Recipe:

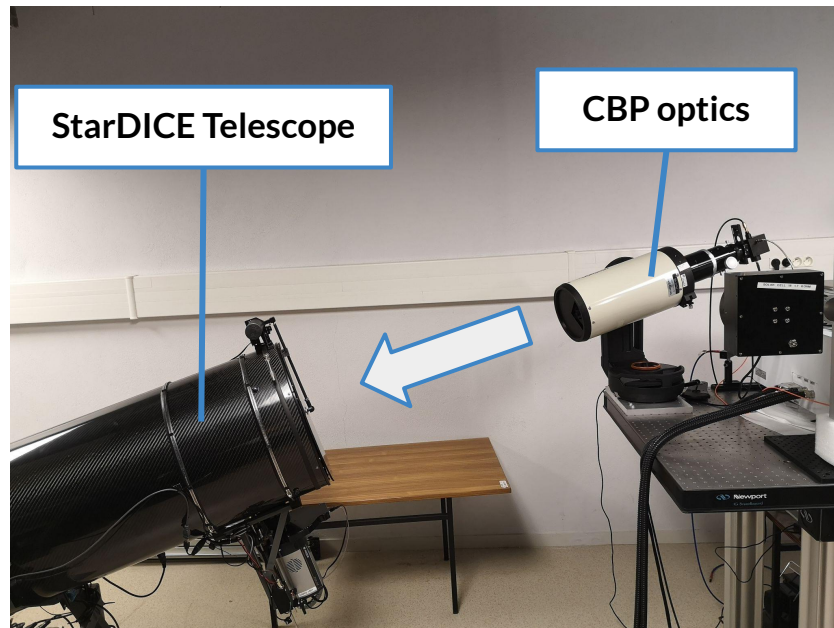
- (1) Shoot light inside a calibrated sensor to measure CBP optics throughput R_{CBP}
- (2) Shoot light inside the instrument to calibrate, using R_{CBP}



Setup device

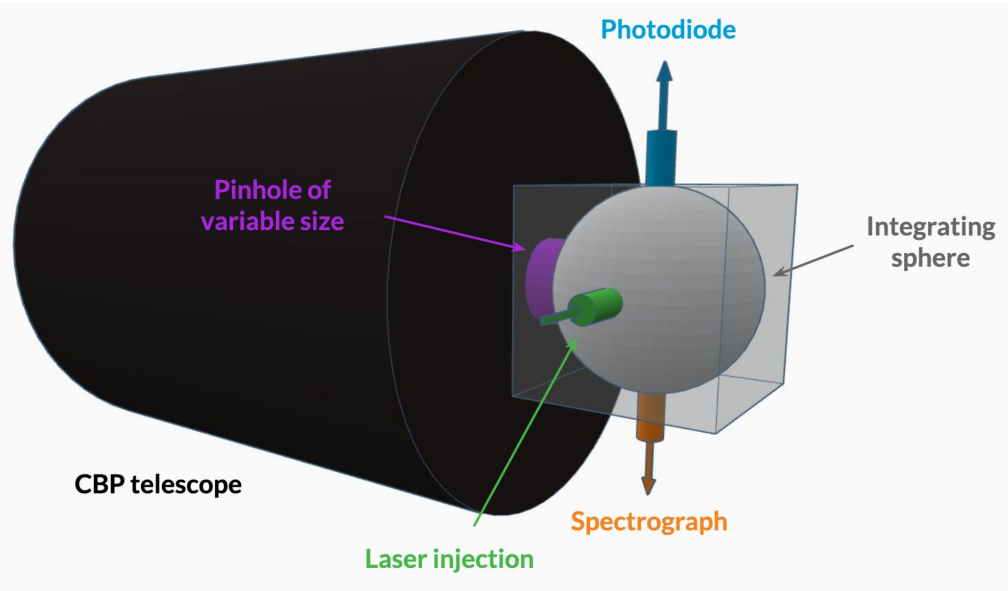


(1) CBP response measurement



(2) StarDICE response measurement

Integrating sphere



Two instruments in the integrating sphere, to monitor the input light:

- a **spectrograph** to monitor the laser **wavelength**
- a **photodiode** to monitor the **flux quantity**

How do we measure our responses ?

(1) CBP response $R_{\text{CBP}} [\gamma \cdot \text{C}^{-1}]$

$$R_{\text{CBP}} = \frac{Q_{\text{solar}}}{Q_{\text{phot}} \times \epsilon_{\text{solar}} \times e}$$

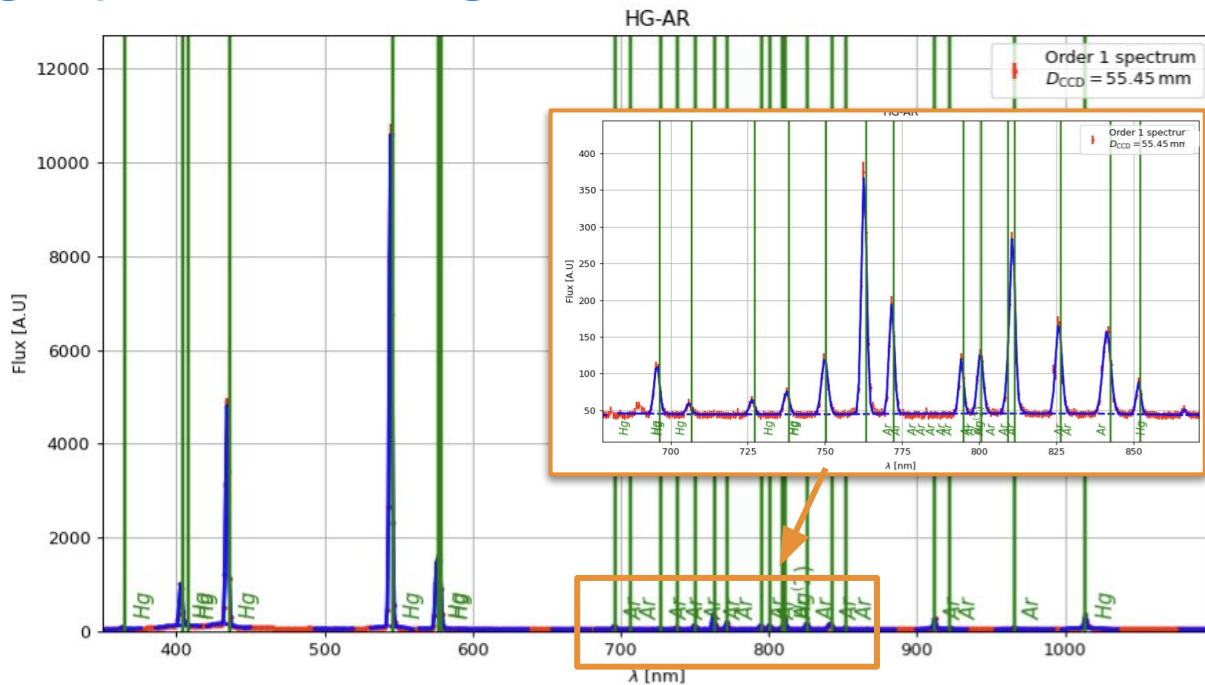
(2) StarDICE response $R_{\text{SD}} [\text{ADU} \cdot \gamma^{-1}]$

$$R_{\text{tel}} = \frac{Q_{\text{ccd}}}{Q_{\text{phot}} \times R_{\text{CBP}}}$$

- Q_{solar} : solar cell charges [C]
- Q_{phot} : photodiode charges [C]
- Q_{ccd} : stardice charges [ADU]
- ϵ_{solar} : solar cell quantum efficiency $[\gamma^{-1}]$
- $e = 1.6 \times 10^{-19}$ [C]

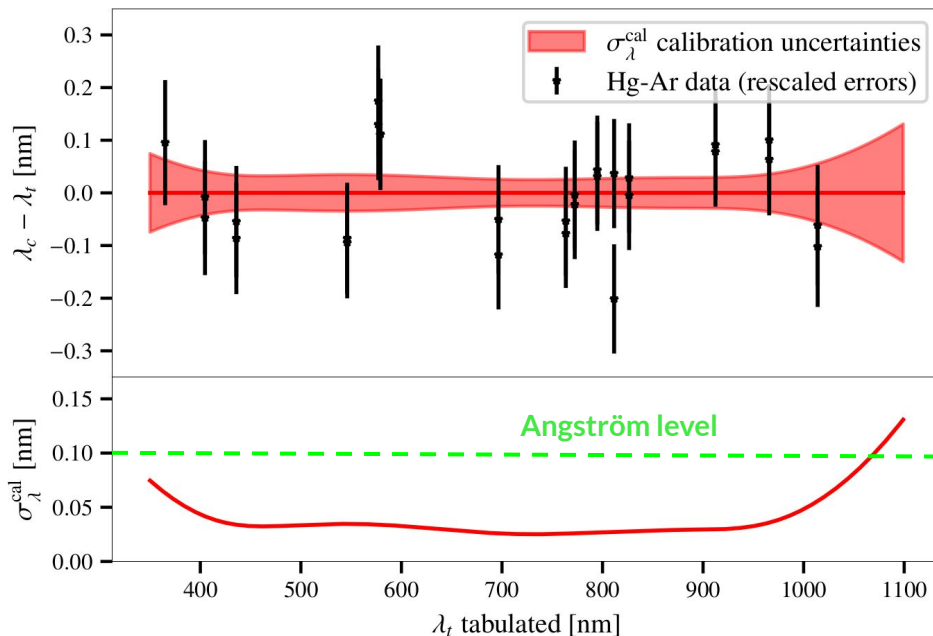
5.b. Data presentation and reduction

Spectrograph wavelength calibration



- Acquisition of Hg-Ar spectrum before and after measurements campaign
- Line detection with gaussian fit
- Compute the difference between tabulated and measured wavelengths

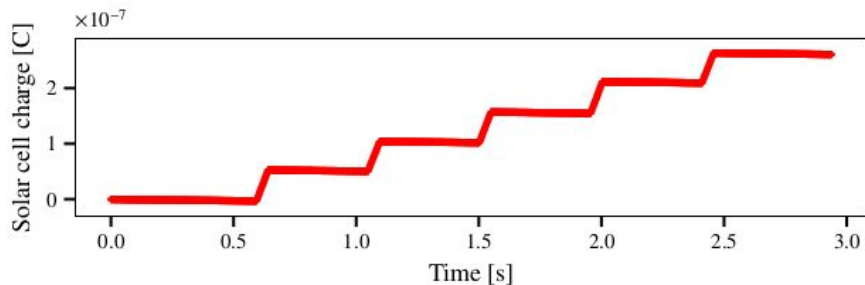
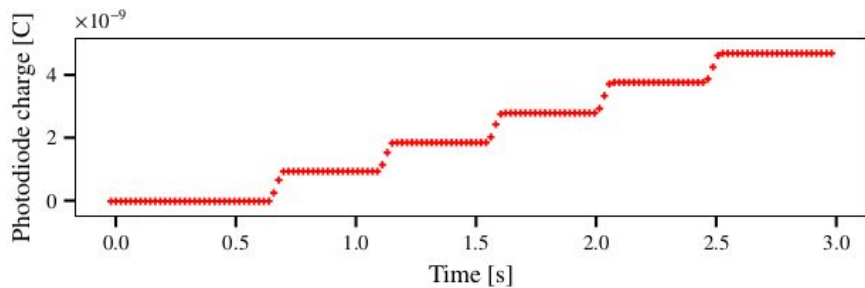
Spectrograph wavelength calibration



- Acquisition of Hg-Ar spectrum before and after measurements campaign
- Line detection with gaussian fit
- Compute the difference between tabulated and measured wavelengths

⇒ Total uncertainties below the Angström level: $\sigma_\lambda < 0.1\text{nm}$ for [350 - 1080] nm

Photodiode and solar cell dataset

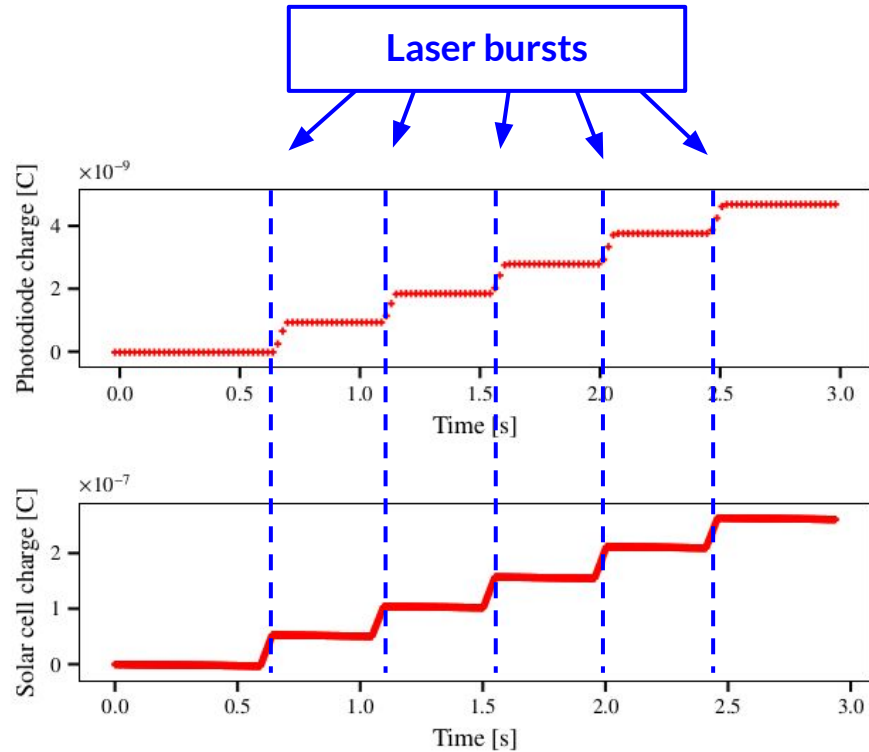


Two electrometers measuring charges [C]:

- monitoring photodiode (Q_{phot})
- solar cell (Q_{solar})

$$R_{\text{CBP}} = \frac{Q_{\text{solar}}}{Q_{\text{phot}} \times \epsilon_{\text{solar}} \times e}$$

Photodiode and solar cell dataset

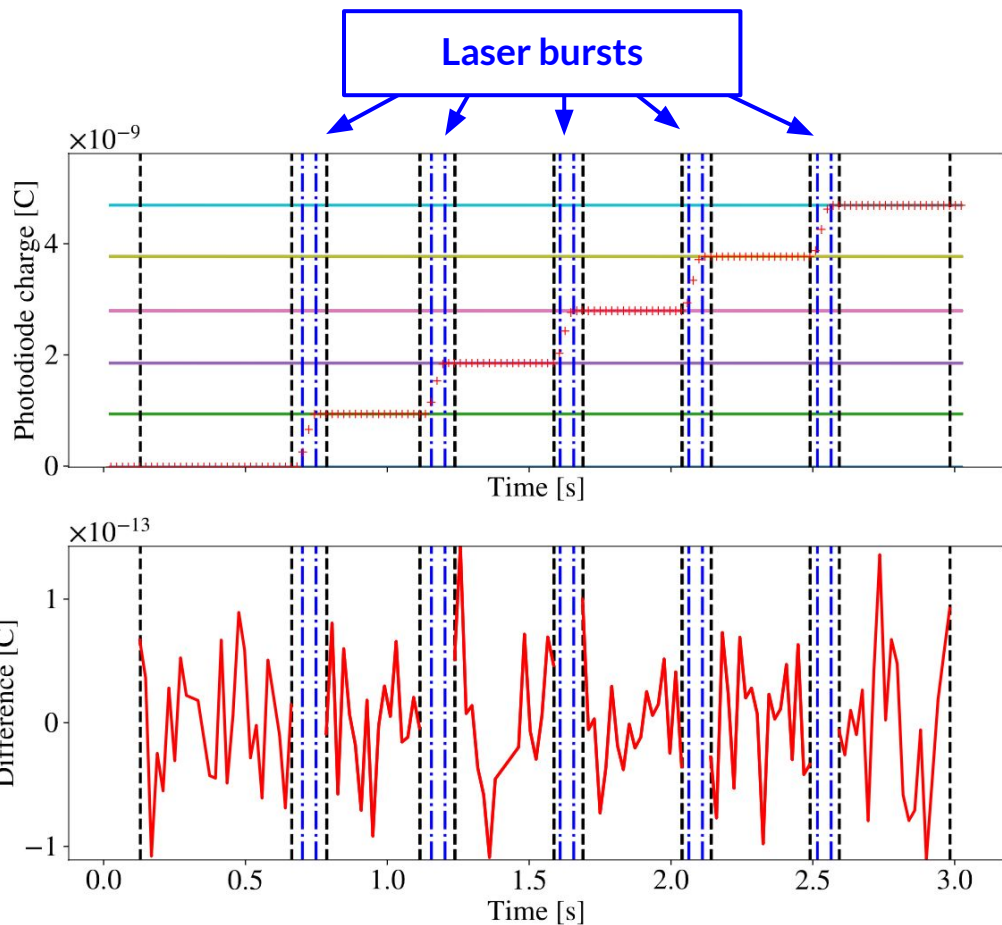


Two electrometers measuring charges [C]:

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$$R_{\text{CBP}} = \frac{Q_{\text{solar}}}{Q_{\text{phot}} \times \epsilon_{\text{solar}} \times e}$$

Photodiode reduction

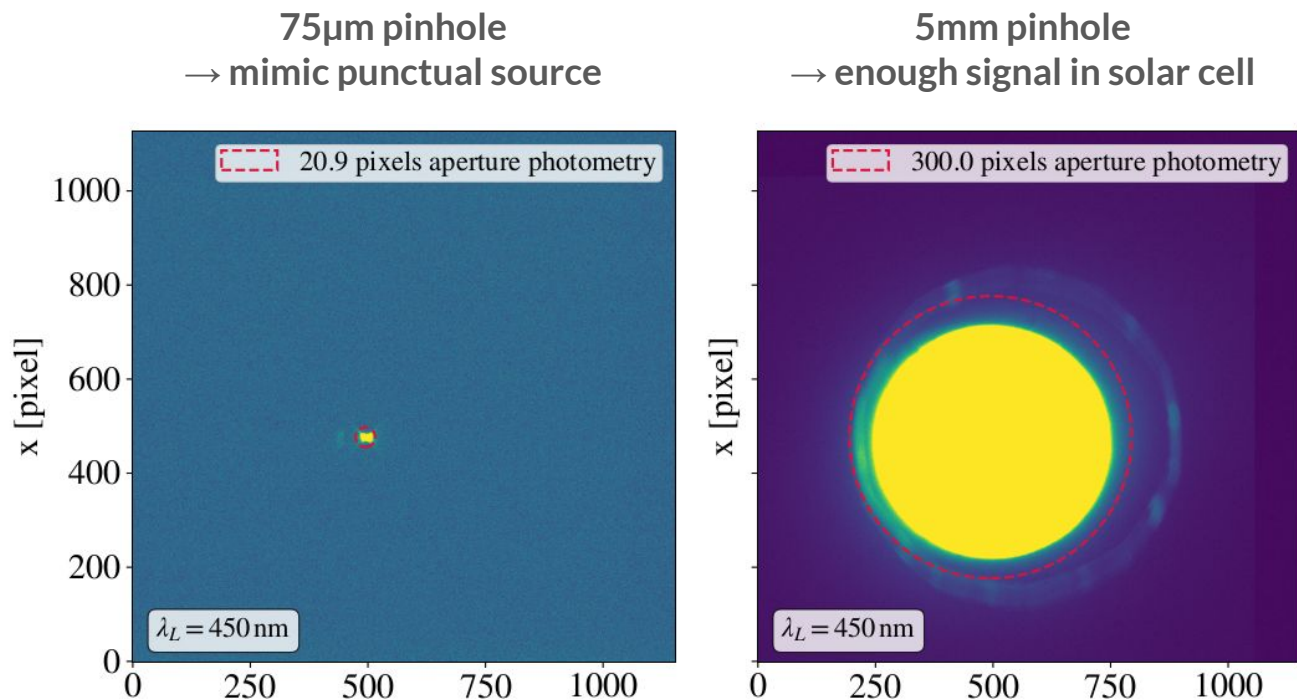


- Compute the differences between dark sequences
- Residuals 4 orders of magnitude smaller

⇒ Monitor total charges Q_{phot} and Q_{solar}

$$R_{\text{CBP}} = \frac{Q_{\text{solar}}}{Q_{\text{phot}} \times \epsilon_{\text{solar}} \times e}$$

StarDICE telescope



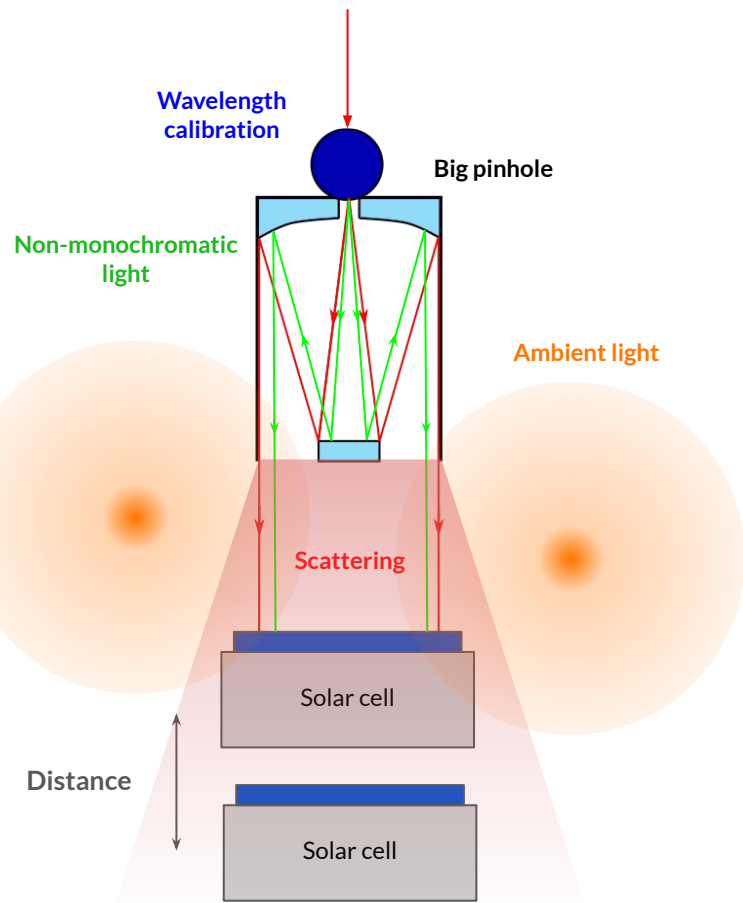
- Background subtraction + aperture photometry at optimized radius

⇒ Measure Q_{CCD} the photons collected in ADU

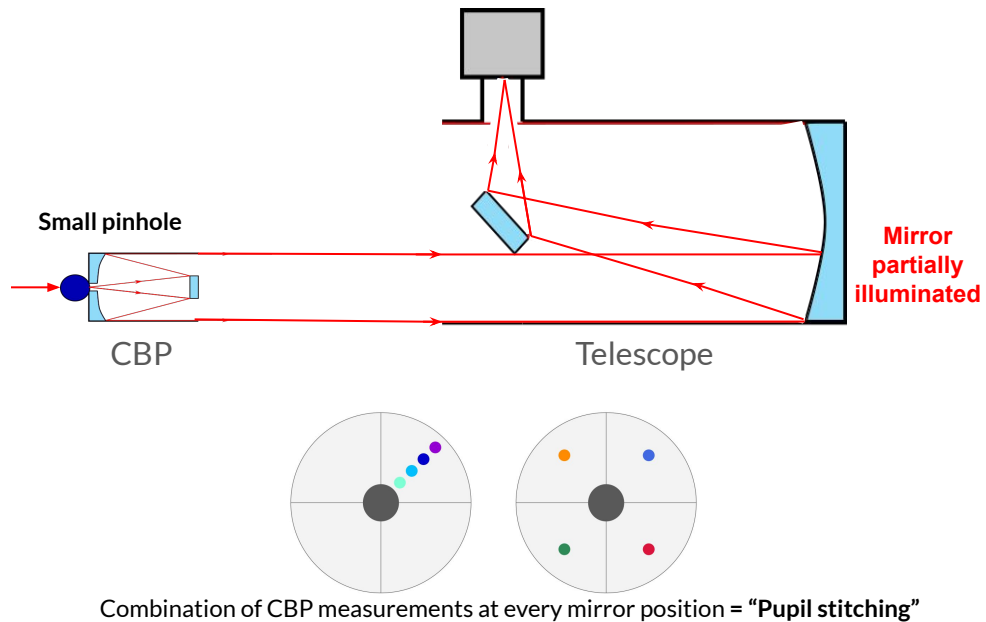
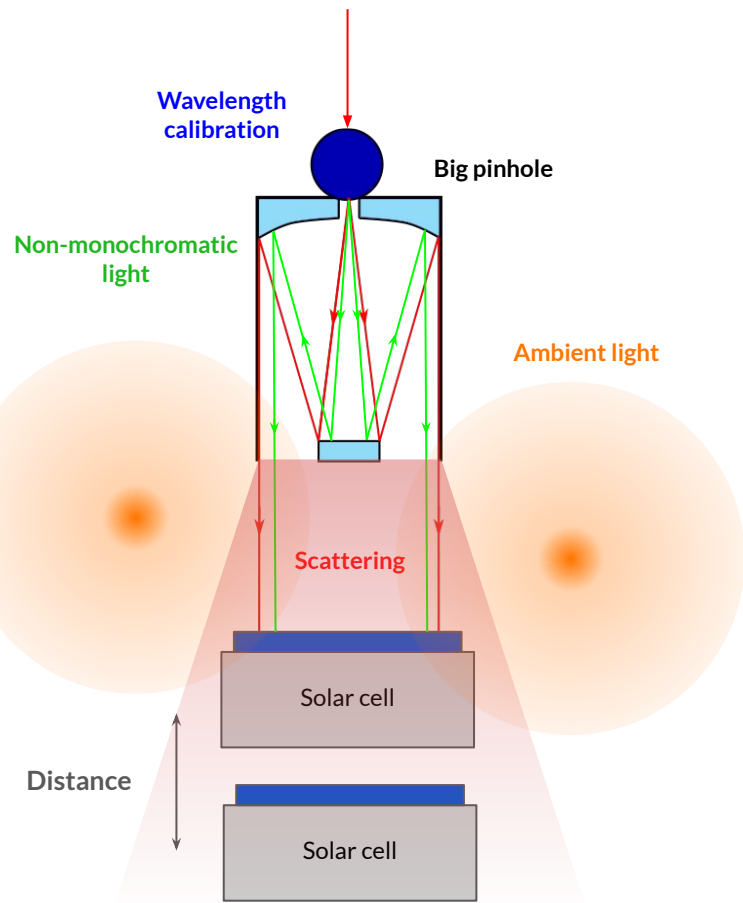
$$R_{\text{tel}} = \frac{Q_{\text{ccd}}}{Q_{\text{phot}} \times R_{\text{CBP}}}$$

5.c. Systematics

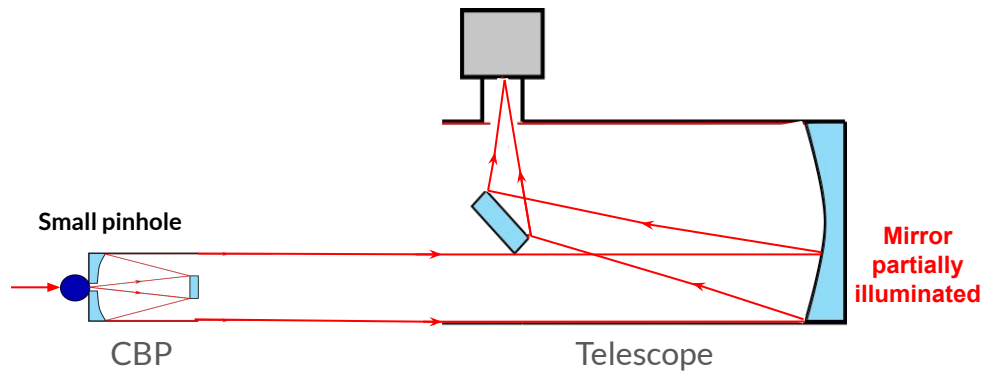
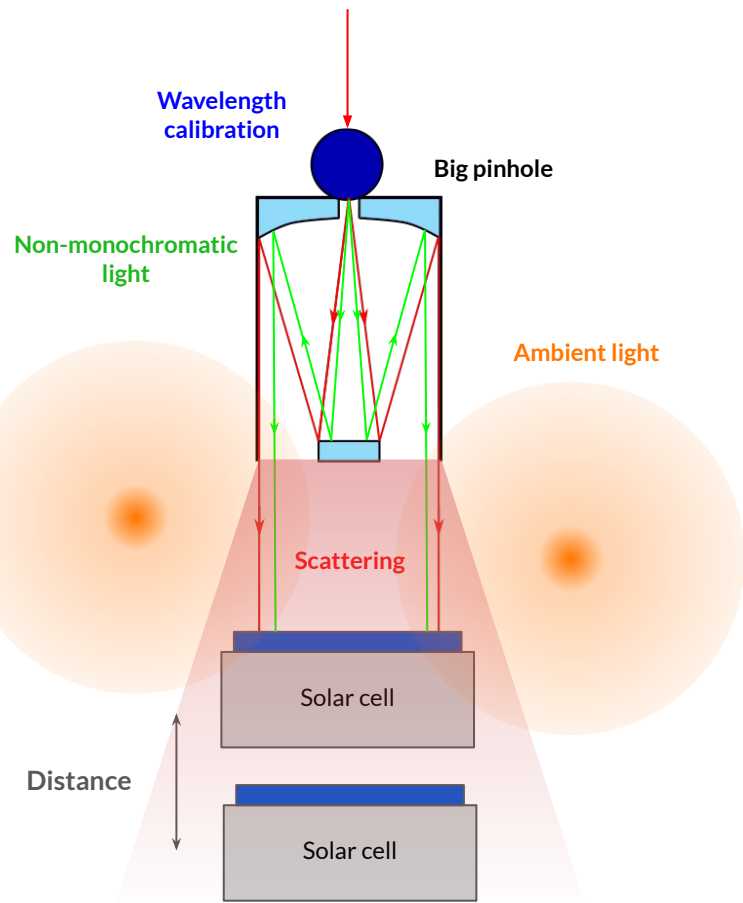
CBP in real life



CBP in real life

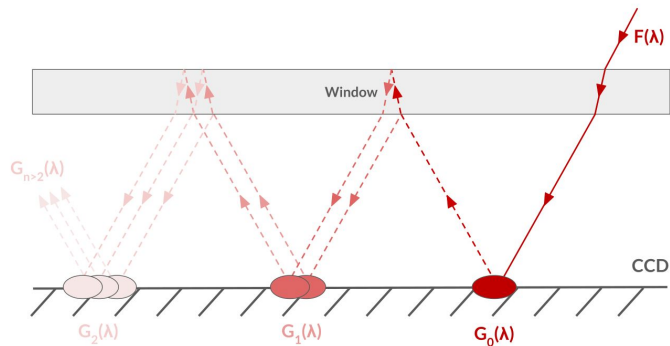


CBP in real life

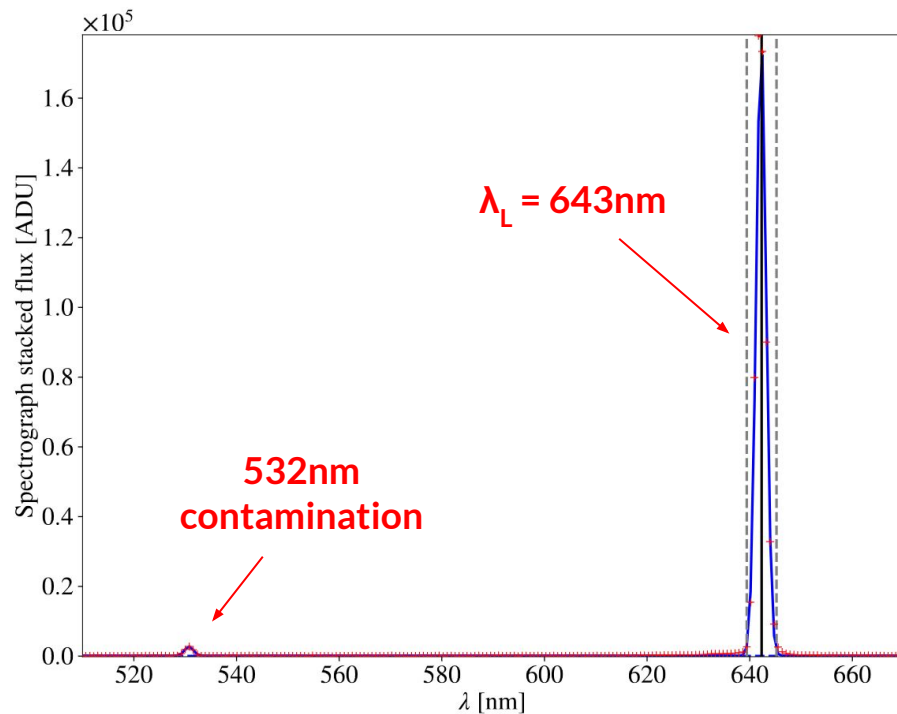
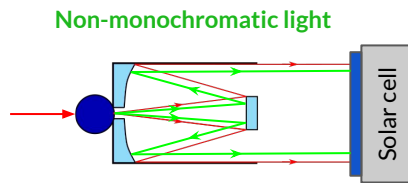


Combination of CBP measurements at every mirror position = "Pupil stitching"

Ghosts



Laser light contamination

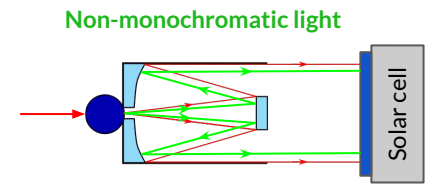


Signal: $\lambda_L + 532\text{nm}$ contamination

Charges $Q_{\text{spectro}}(\lambda)$ measured with a gaussian fit

\Rightarrow Estimate the ratio of contamination light over main wavelength

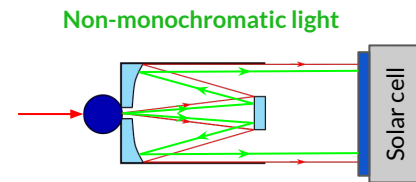
Laser light contamination



Similar ratio contamination/main wavelength in **spectrograph** and **photodiode**:

$$\alpha(\lambda_L) = \frac{Q_{\text{phot}}^{532}(\lambda_L)}{Q_{\text{phot}}(\lambda_L)} = \frac{Q_{\text{spectro}}^{532}(\lambda_L)}{Q_{\text{spectro}}(\lambda_L)} \times \frac{\epsilon_{\text{spectro}}(\lambda_L)}{\epsilon_{\text{spectro}}(532)} \times \frac{\epsilon_{\text{phot}}(532)}{\epsilon_{\text{phot}}(\lambda_L)}.$$

Laser light contamination



Similar ratio contamination/main wavelength in **spectrograph** and **photodiode**:

$$\alpha(\lambda_L) = \frac{Q_{\text{phot}}^{532}(\lambda_L)}{Q_{\text{phot}}(\lambda_L)} = \frac{Q_{\text{spectro}}^{532}(\lambda_L)}{Q_{\text{spectro}}(\lambda_L)} \times \frac{\epsilon_{\text{spectro}}(\lambda_L)}{\epsilon_{\text{spectro}}(532)} \times \frac{\epsilon_{\text{phot}}(532)}{\epsilon_{\text{phot}}(\lambda_L)}.$$

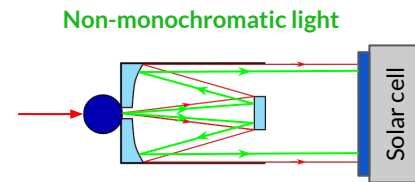
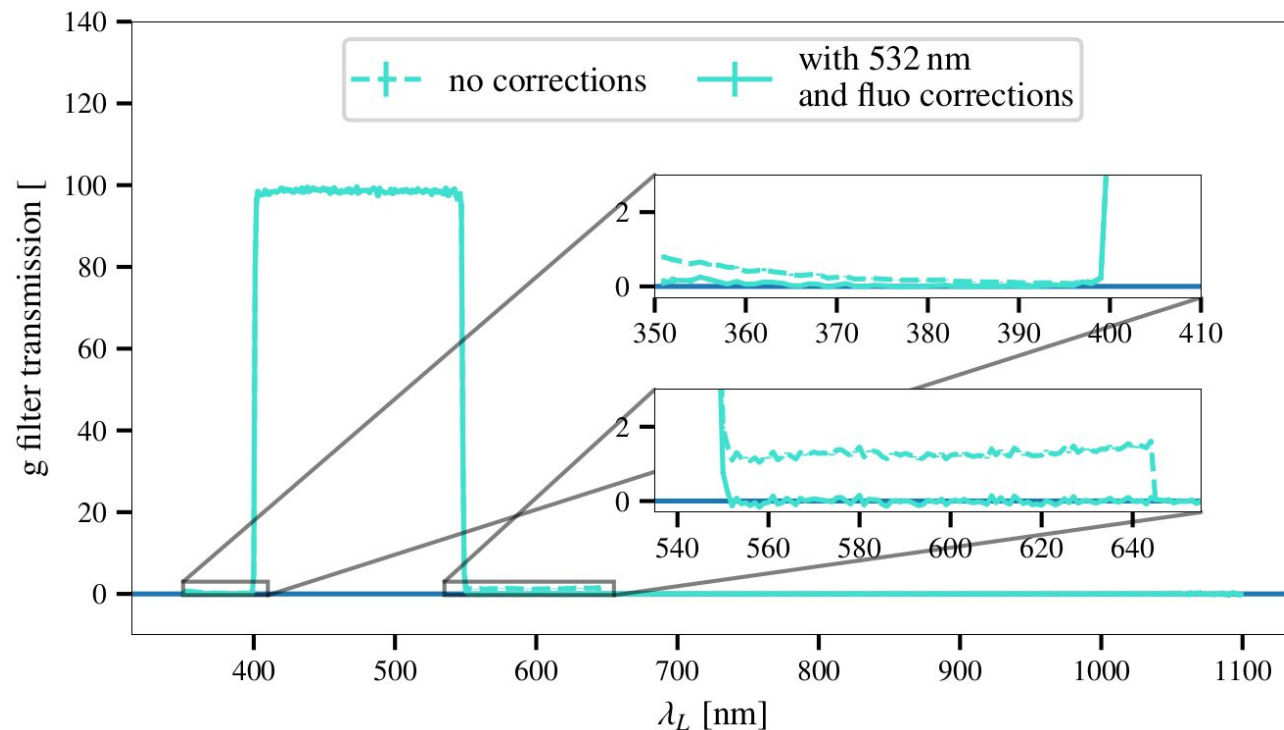
Calibrate the charges measure with α :

$$Q_{\text{phot}}^{\lambda_L} = \frac{Q_{\text{phot}}^{\text{mes}}}{1 + \alpha(\lambda_L)}$$

$$Q_{\text{solar}}^{\lambda_L} = Q_{\text{solar}}^{\text{mes}} - R_{\text{CBP}}(532) \alpha(\lambda_L) Q_{\text{phot}}^{\text{mes}}$$

$$Q_{\text{ccd}}^{\lambda_L} = Q_{\text{ccd}}^{\text{mes}} - R_{\text{CBP}}(532) R_{\text{tel}}(532) \alpha(\lambda_L) Q_{\text{phot}}^{\text{mes}}$$

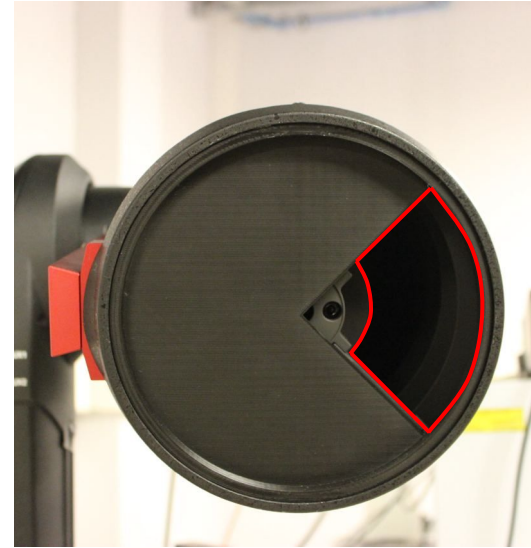
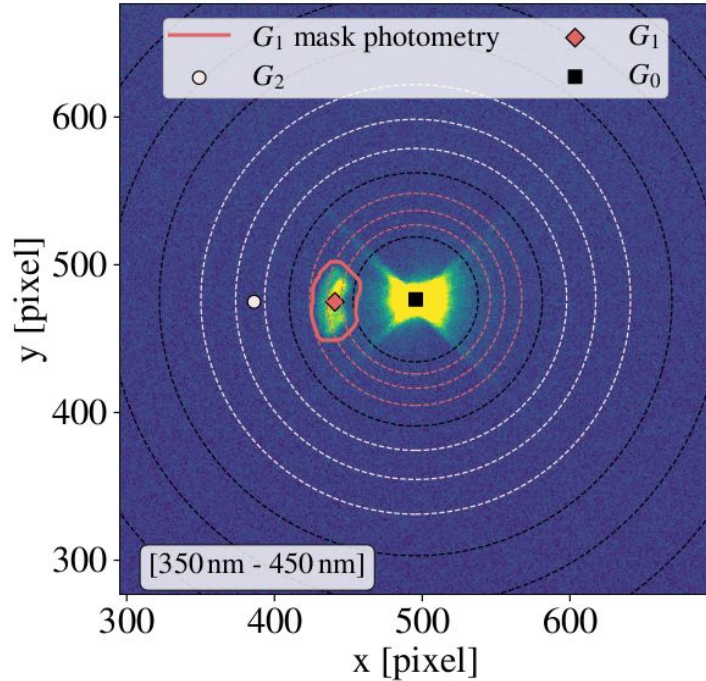
Laser light contamination



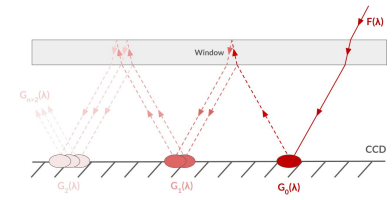
$$Q_{\text{phot}}^{\text{cal}}(\lambda_L) \equiv \frac{Q_{\text{phot}}^{\text{mes}}(\lambda_L)}{1 + \alpha(\lambda_L)}$$

Plus: 532nm contamination
used to monitor wavelength
calibration

Ghost contamination



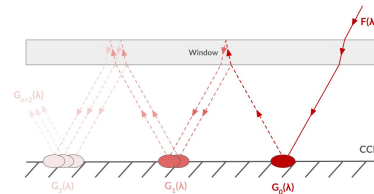
CBP output



⇒ Parasite signal when performing aperture photometry

Ghost contamination

#Method 1: PSF fit with successive aperture photometry with radius r

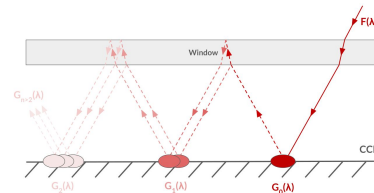


$$F(r, \lambda) = A(\lambda) \times \frac{\text{Moffat distribution } M(r, \lambda) + \text{Ghost contribution } K_{G/A}(r, \lambda)}{1 + K_{G/A}(+\infty, \lambda)} + \text{Background } \text{bkg}(\lambda) \times \pi r^2$$

Ghost contamination

#Method 1: PSF fit with successive aperture photometry with radius r

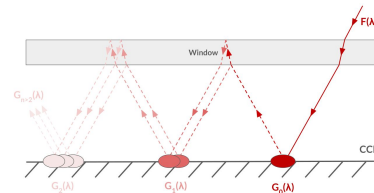
$$F(r, \lambda) = A(\lambda) \times \frac{\overset{\text{Moffat}}{\text{distribution}} \overset{\text{Ghost}}{\text{contribution}} M(r, \lambda) + K_{G/A}(r, \lambda)}{1 + K_{G/A}(+\infty, \lambda)} + \overset{\text{Background}}{\text{bkg}(\lambda)} \times \pi r^2$$



#Method 2: Ghost photometry with a custom mask:

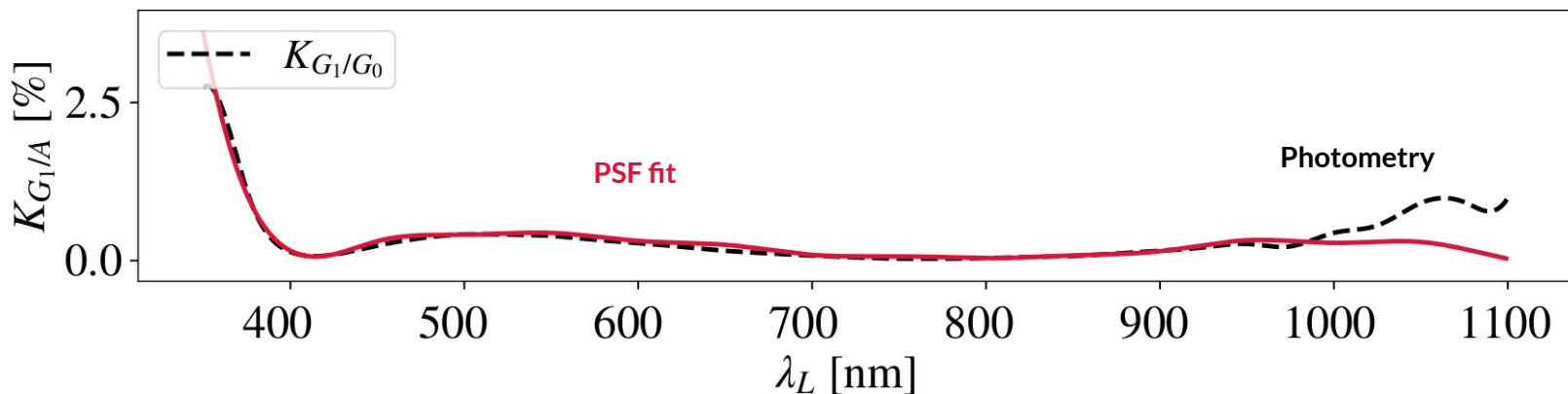
$$K_{G_1/G_0}(\lambda) = \frac{G_1(\lambda)}{G_0(\lambda)}$$

Ghost contamination



#Method 1: PSF fit with successive aperture photometry with radius r

$$F(r, \lambda) = A(\lambda) \times \frac{\text{Moffat distribution } M(r, \lambda) + \text{Ghost contribution } K_{G/A}(r, \lambda)}{1 + K_{G/A}(+\infty, \lambda)} + \text{Background } \text{bkg}(\lambda) \times \pi r^2$$



#Method 2: Ghost photometry with a custom mask:

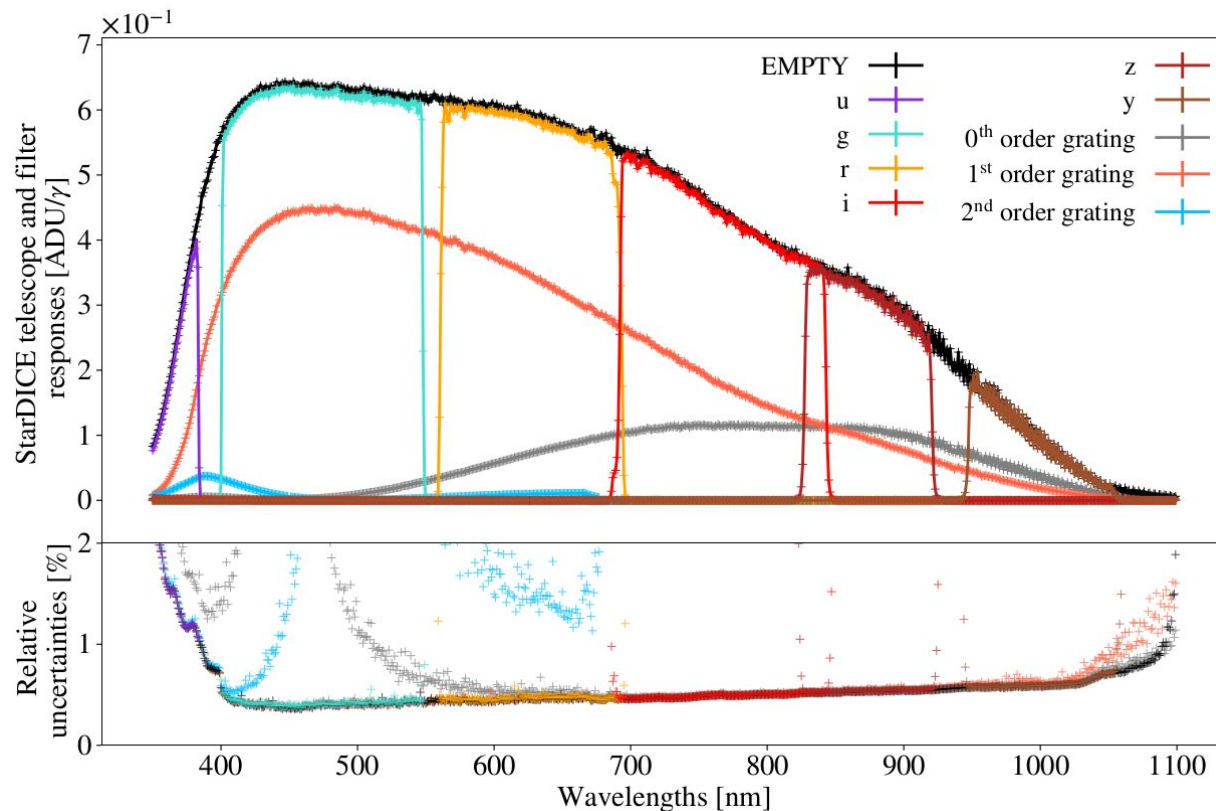
$$K_{G_1/G_0}(\lambda) = \frac{G_1(\lambda)}{G_0(\lambda)}$$

5.d. Results

StarDICE filters transmission

$$R_{\text{tel}} = \frac{Q_{\text{ccd}}}{Q_{\text{phot}} \times R_{\text{CBP}}}$$

- ~0.5 % per nm uncertainty over [400 - 1000] nm range for every filter
- Wavelength resolution high enough to see the slopes of the filter edges

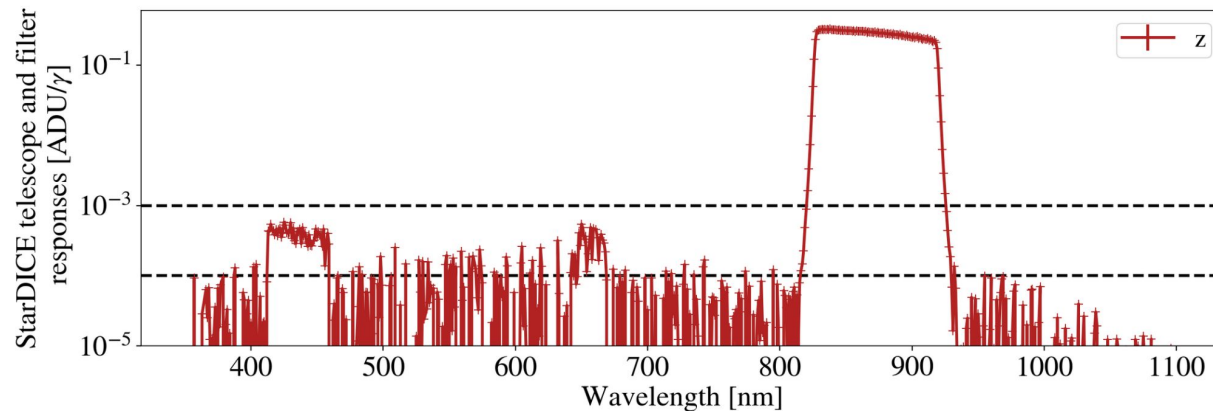
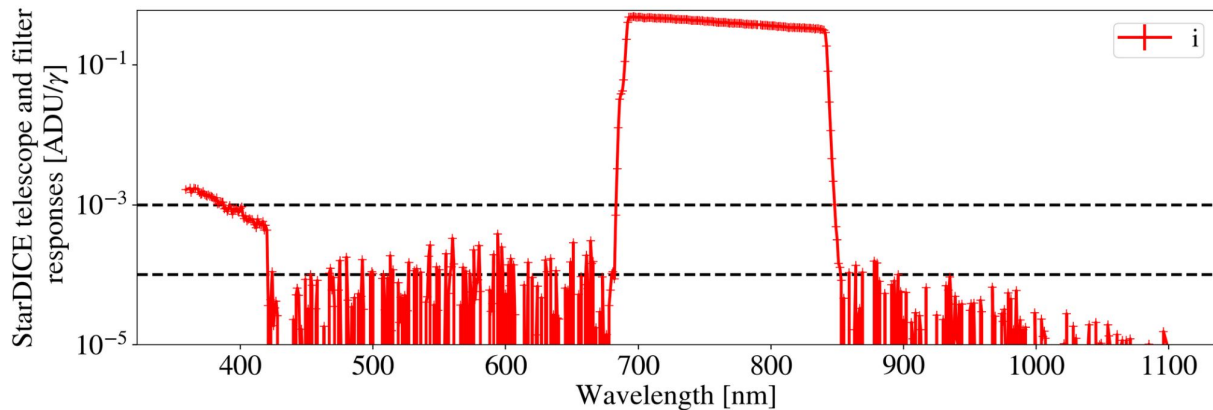


Filter leakages

Example of i and z filters:

Detection of out-of-band leakages below **0.1%** level

→ crucial for accurate photometric measurement

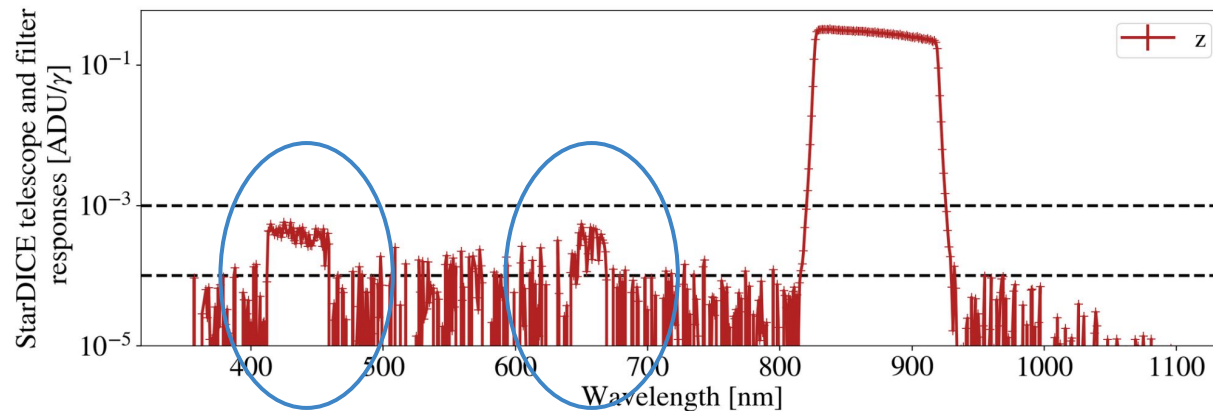
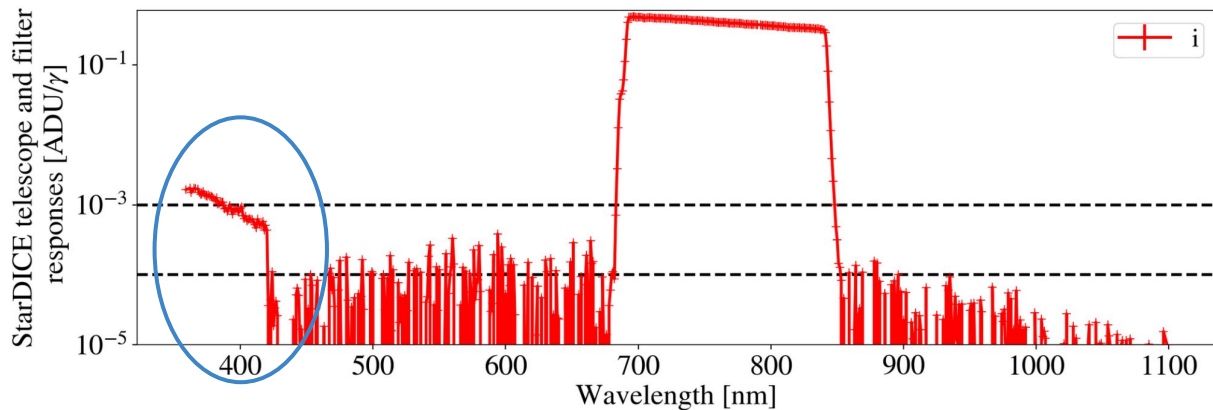


Filter leakages

Example of i and z filters:

Detection of out-of-band leakages below **0.1%** level

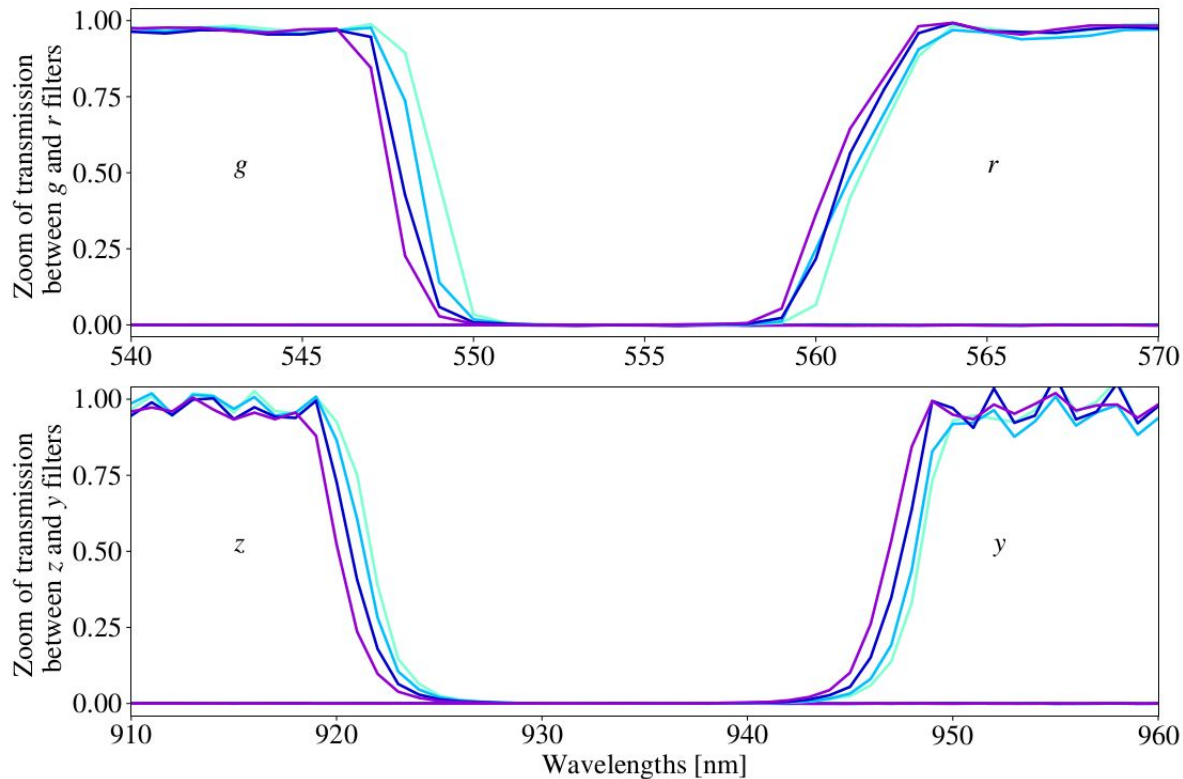
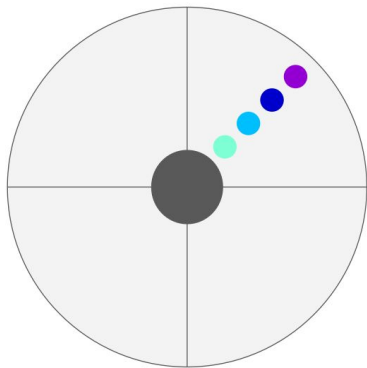
→ crucial for accurate photometric measurement



Filter edges : blueshift

$$\lambda_{\text{eff}} = \lambda_0 \sqrt{1 - \frac{\sin^2(\theta)}{n_{\text{eff}}^2}}$$

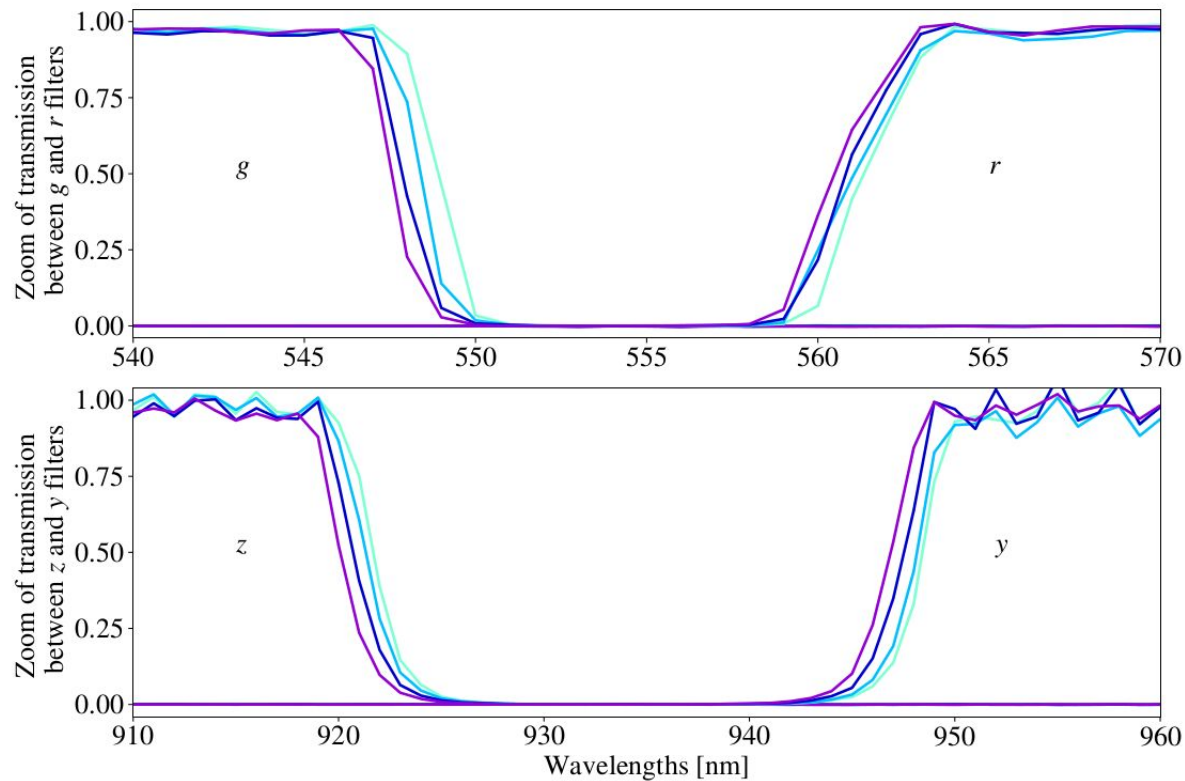
Blue-shift of filter edges when high incident angles



Filter edges : blueshift

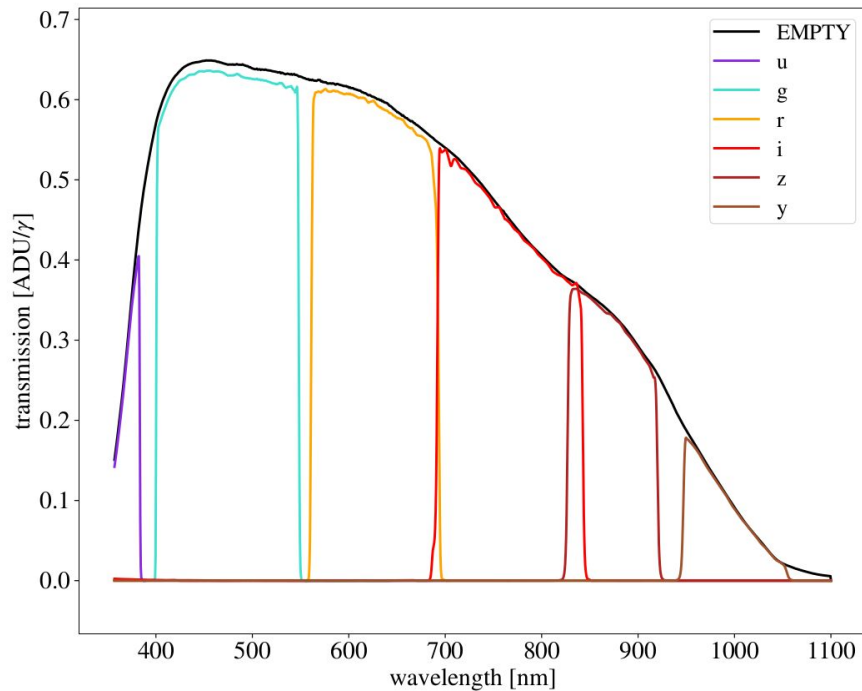


$$\lambda_{\text{eff}} = \lambda_0 \sqrt{1 - \frac{\sin^2(\theta)}{n_{\text{eff}}^2}}$$



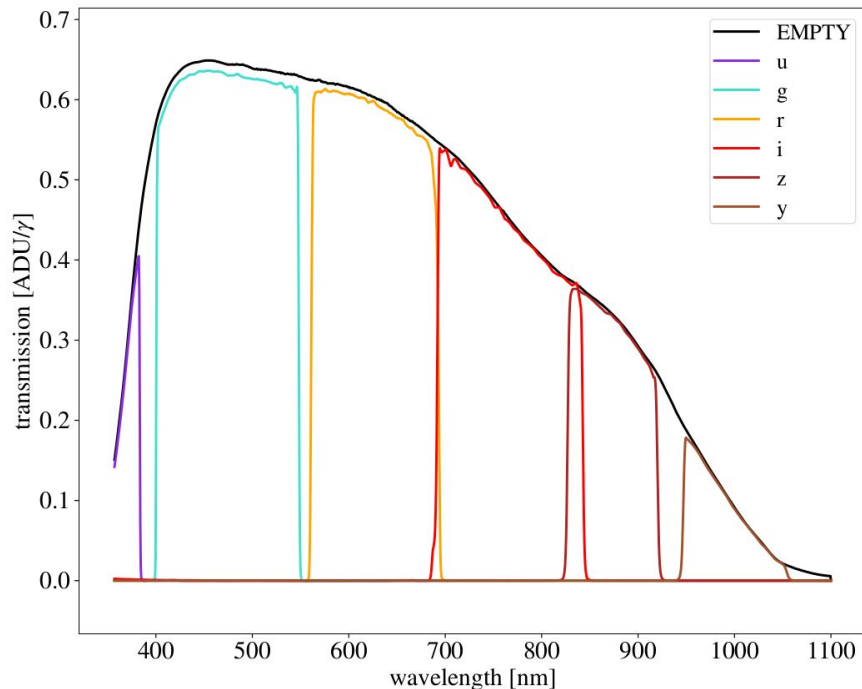
Full illumination synthesis

$$T(\lambda, \theta) = \mathcal{T} \left(\frac{\lambda}{\sqrt{1 - (\sin(\theta)/n_{\text{eff}})^2}} \right)$$



Full illumination synthesis

$$T(\lambda, \theta) = \mathcal{T} \left(\frac{\lambda}{\sqrt{1 - (\sin(\theta)/n_{\text{eff}})^2}} \right)$$



Uncertainty propagation for **on-sky** flux measurements, **after** simulating the recalibration with the **artificial star**:

| Filter | Uncertainty [%] |
|--------|-----------------|
| u | 0.08 |
| g | 0.08 |
| r | 0.13 |
| i | 0.11 |
| z | 0.11 |
| y | 0.24 |

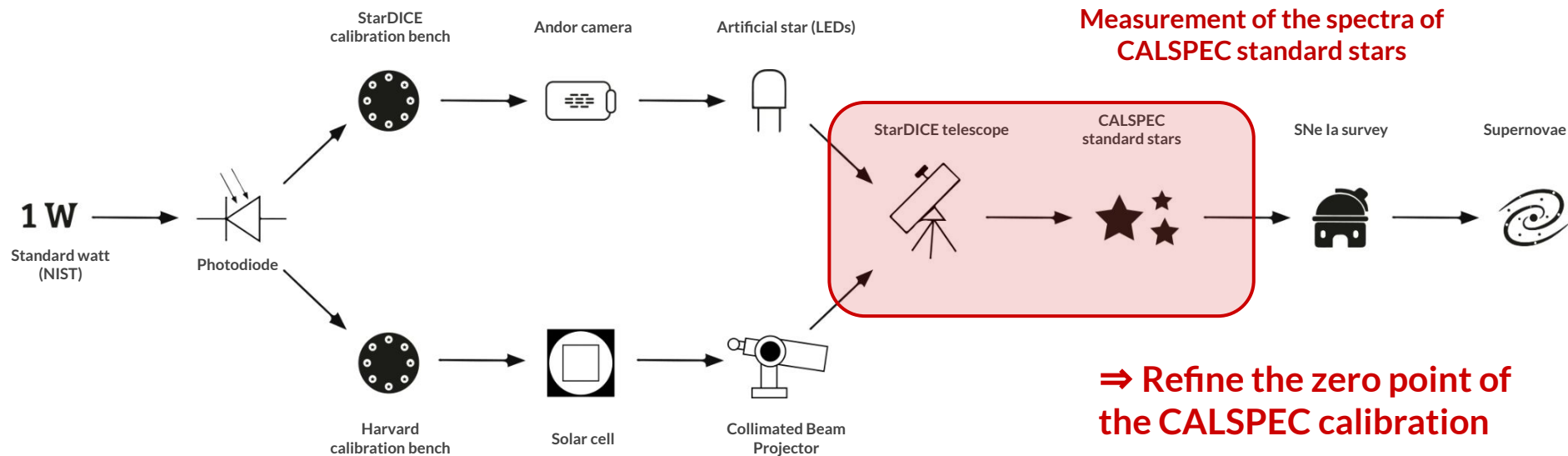
Conclusion

- Filter bandpasses measured with a precision of **~ 0.2 nm**
- Detected **out-of-band leaks** at relative level 0.01%
- When coupled with **artificial star** \Rightarrow **flux measurement** at a precision of **$\sim 0.1\%$** for *ugriz* with StarDICE

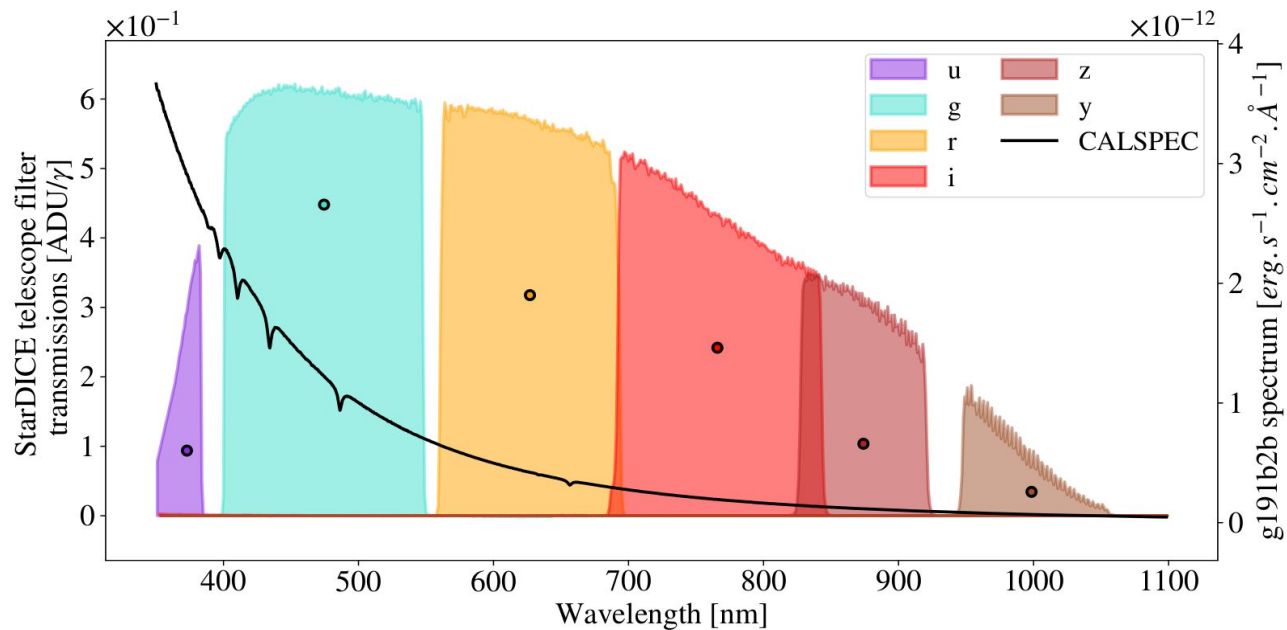
\Rightarrow Proof of concept **validated** for **Rubin-CBP**

6. On-sky measurements analysis with StarDICE

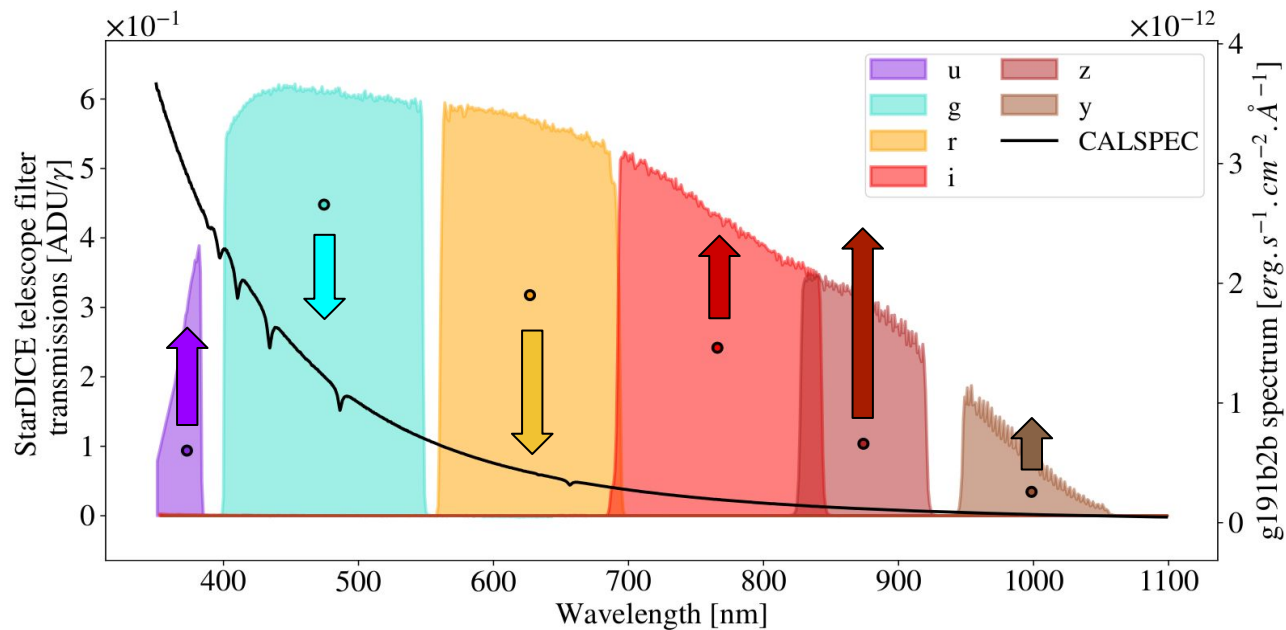
StarDICE goals



Zero point definition



Zero point definition

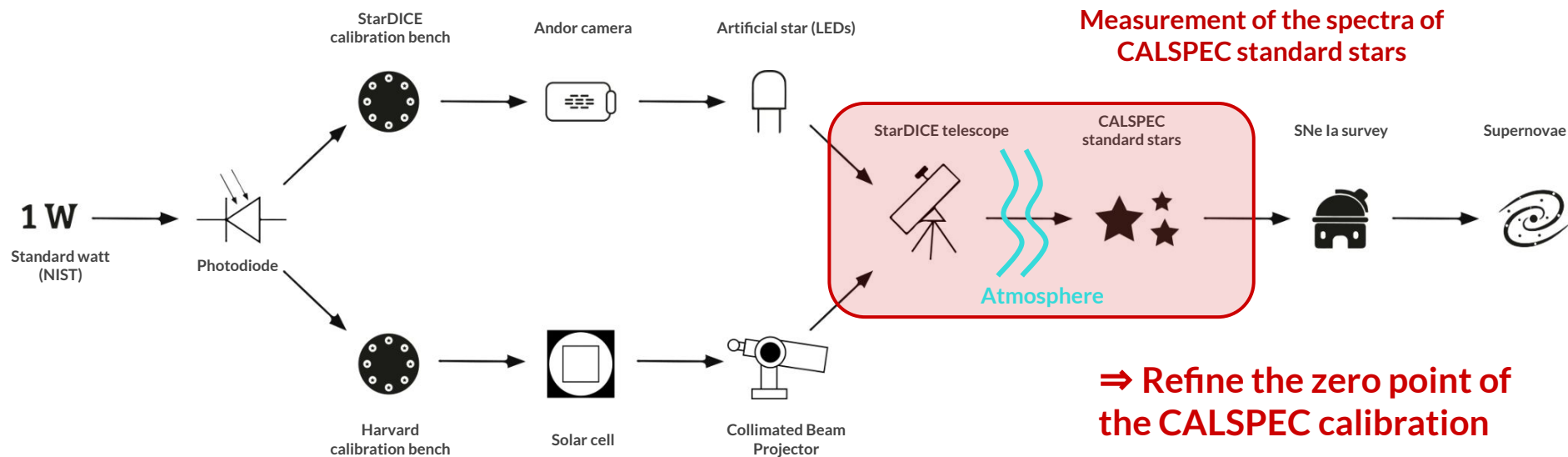


StarDICE is observing photometric standards:

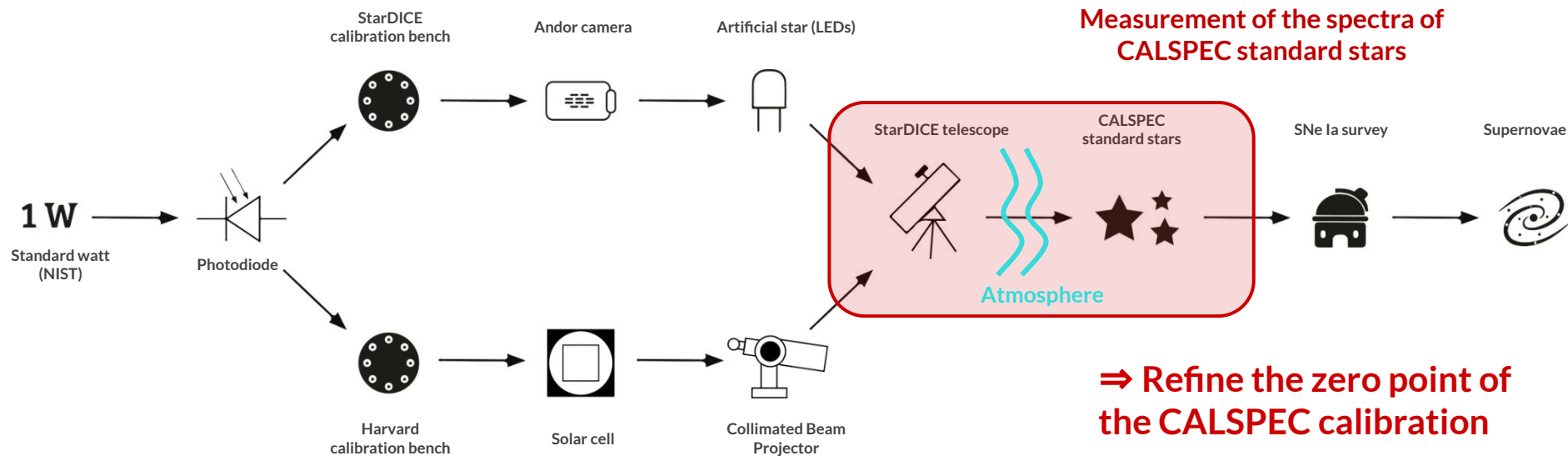
- Prior spectra given by CALSPEC
- Prior knowledge of filter transmissions (CBP + Artificial star)

⇒ Theory/Measurements to adjust the zero points

StarDICE goals



StarDICE goals

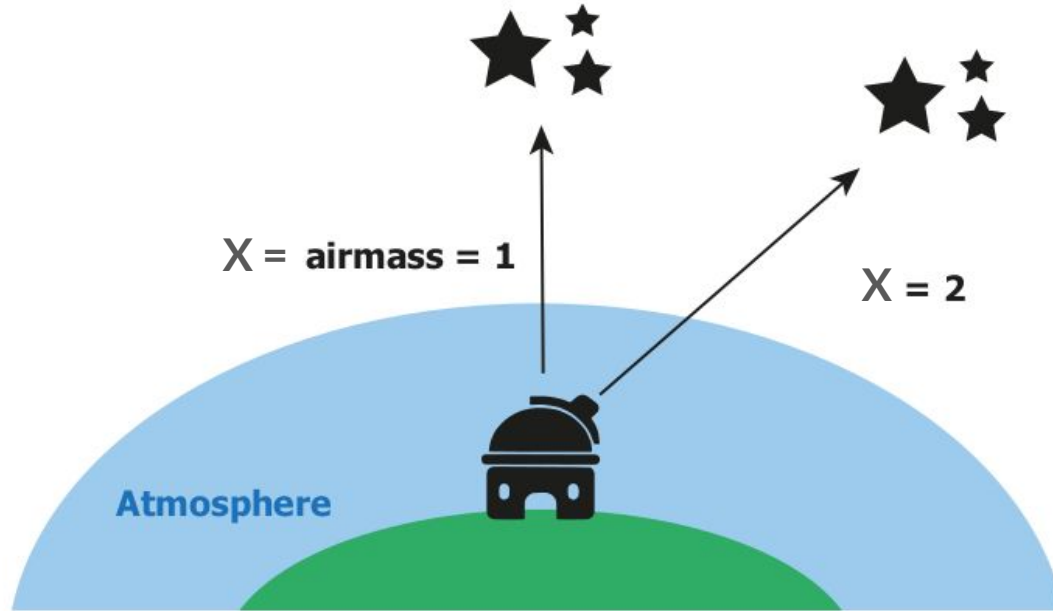


Two paths:

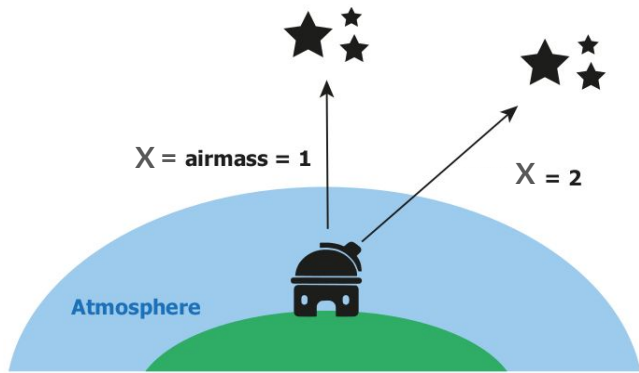
- Photometry at different elevations
- Spectrophotometric measurements

6.a. Photometric analysis

Airmass

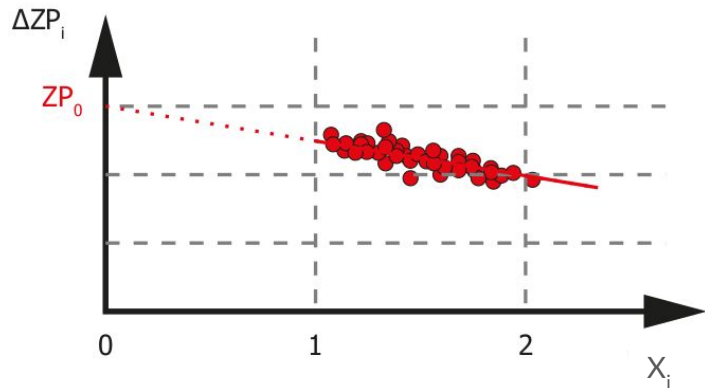


Atmospheric considerations

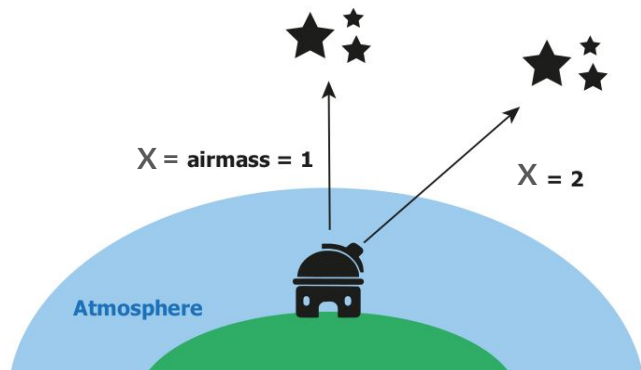


Airmass regression:

- Take images of a reference star at different airmass values X_i
- Compute zero point difference ΔZP_i for each image i



Atmospheric considerations

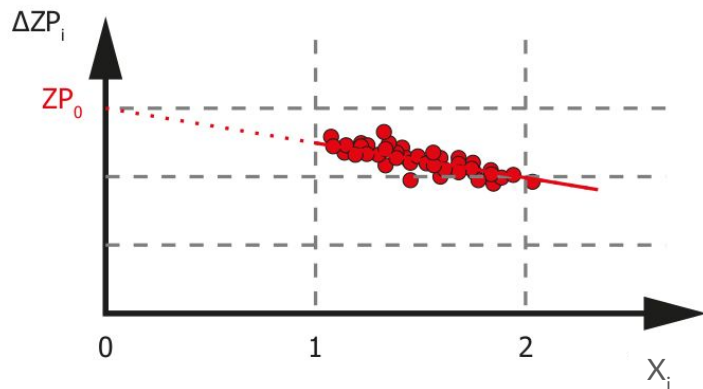


Airmass regression:

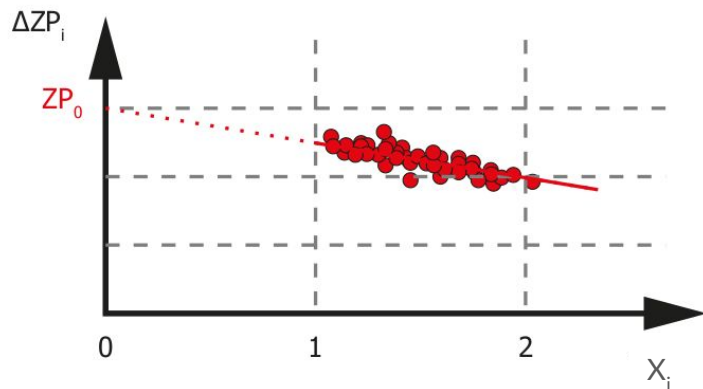
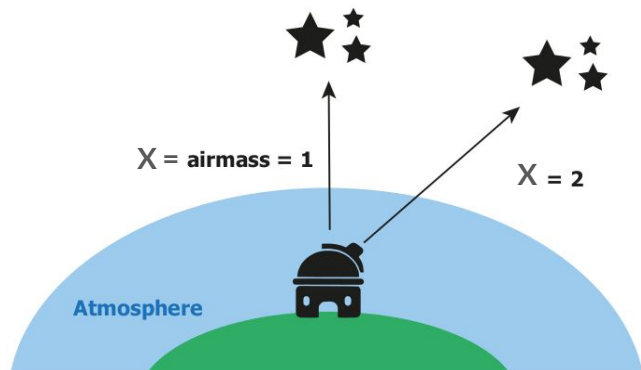
- Take images of a reference star at different airmass values X_i
- Compute zero point difference ΔZP_i for each image i

Final goal:

- Estimate the out-of-atmosphere zero point ZP_0 by extrapolating the value at $X=0$



Atmospheric considerations



Airmass regression:

- Take images of a reference star at different airmass values X_i
- Compute zero point difference ΔZP_i for each image i

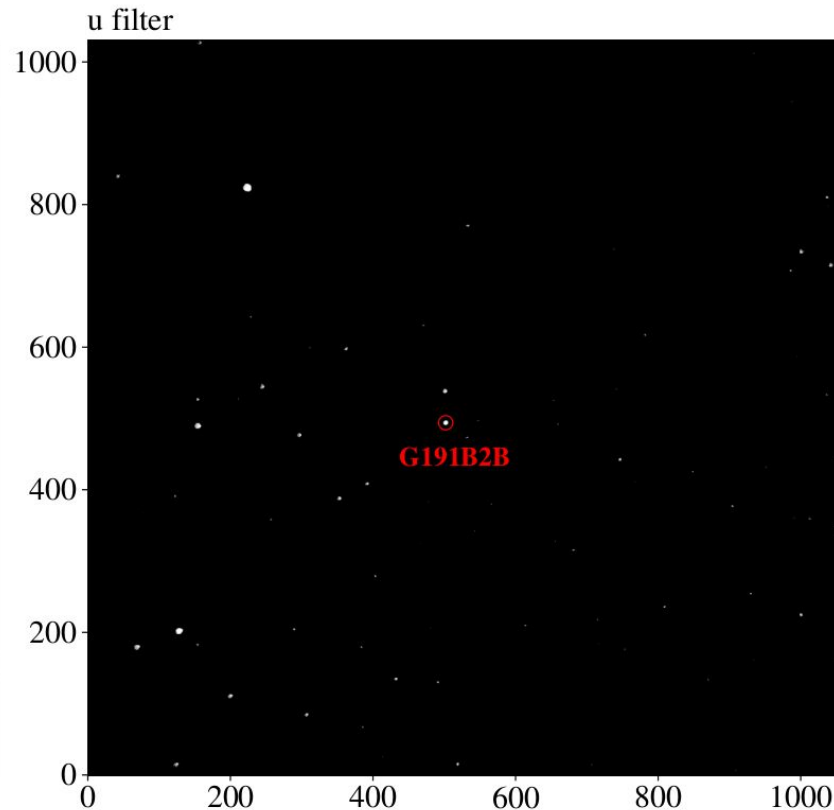
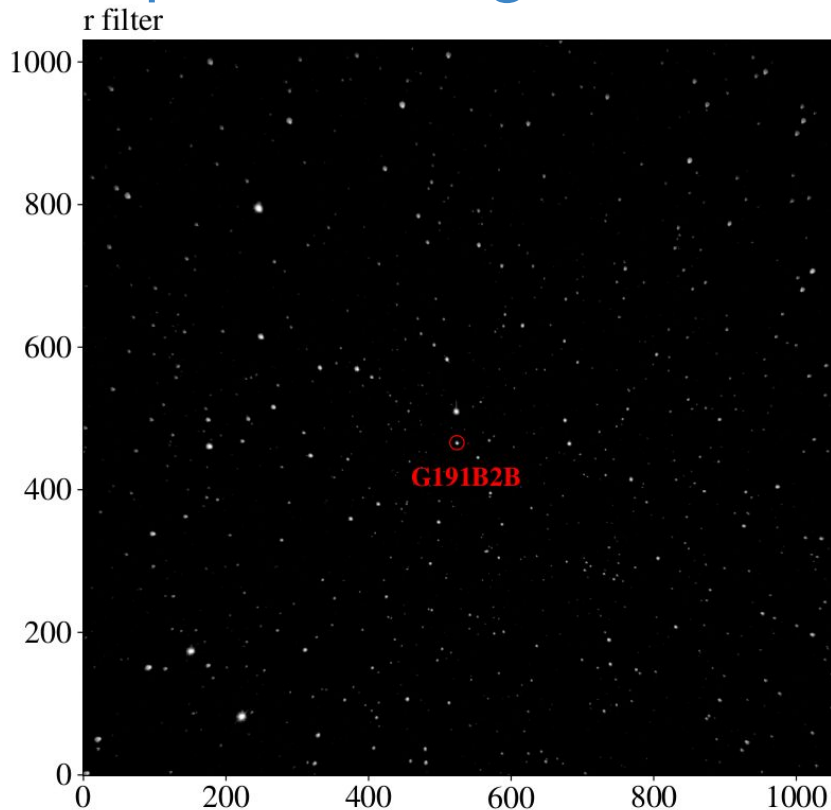
Final goal:

- Estimate the out-of-atmosphere zero point ZP_0 by extrapolating the value at $X=0$

This analysis:

- Estimate the StarDICE performance of refining the ZP_0 with a 2-year survey

Examples of image



Pre-survey: 23 observation nights of the CALSPEC primary standard G191B2B

■ Synthetic photometry

$$F^{\text{synth}} = \int_{\lambda} S_{\star}(\lambda) \times R_{\text{tel}}(\lambda) \times T_{\text{atm}}(\lambda, P_a) \times t_{\text{exp}} \times A_{\text{mirror}} \times \frac{\lambda d\lambda}{hc}$$

StarDICE flux

Star spectral energy density (SED)

StarDICE telescope response

Atmosphere transmission

Exposition time

StarDICE collection surface

■ Synthetic photometry

$S_{\star}(\lambda)$ → GAIA catalog low resolution spectra

$R_{\text{tel}}(\lambda)$ → CBP measurements

$T_{\text{atm}}(\lambda)$ → Libradtran simulations with **airmass**, **pressure** and **humidity**
(ozone, aerosols and PWV are fixed)

■ Fitting zero points

Magnitude difference for every star s in every image i :

$$\Delta\hat{m}_{i,s} = m_{i,s}^{\text{obs}} - m_{i,s}^{\text{synth}}$$

⇒ Estimate the variation ΔZP_i from an image to another, accounting for a star variance model

■ Fitting zero points

Magnitude difference for every star s in every image i :

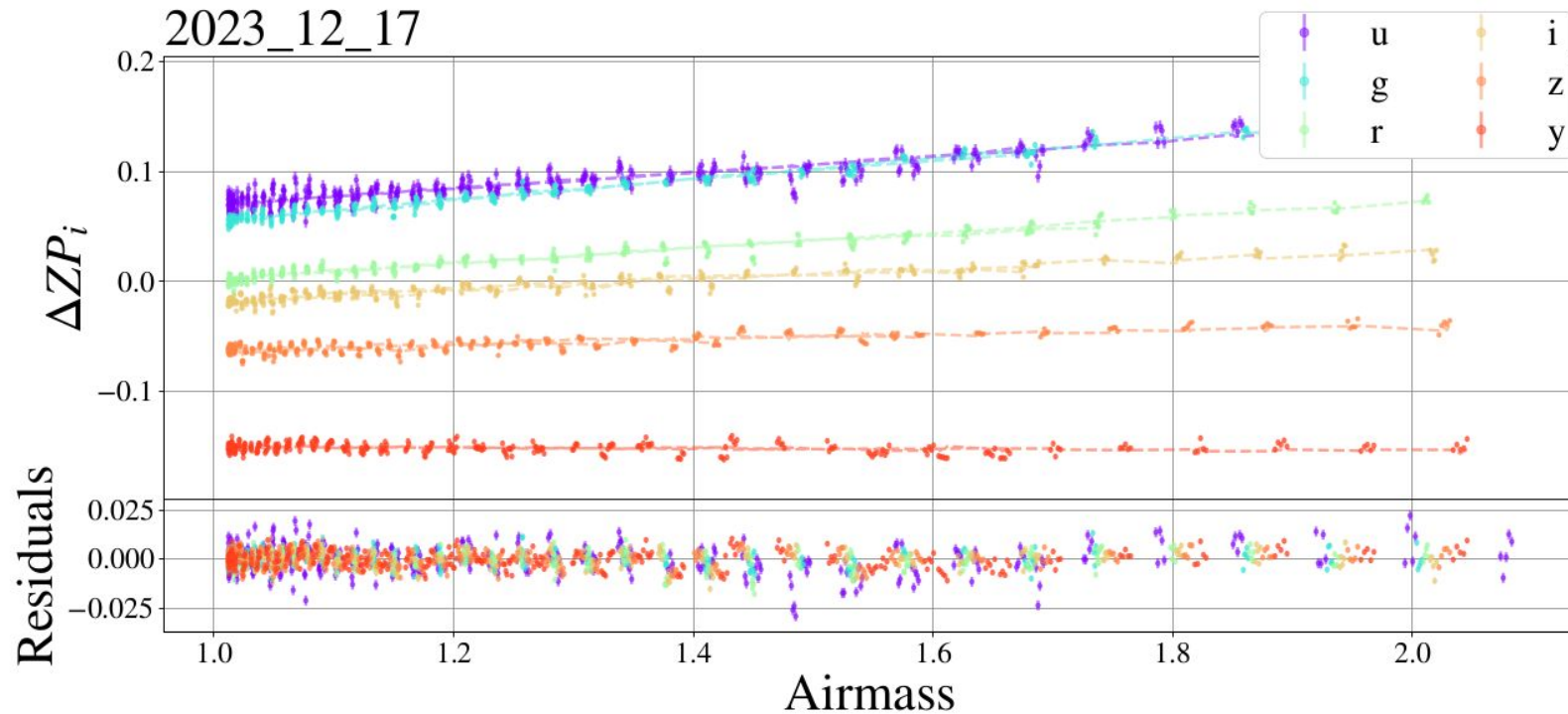
$$\Delta\hat{m}_{i,s} = m_{i,s}^{\text{obs}} - m_{i,s}^{\text{synth}}$$

⇒ Estimate the variation ΔZP_i from an image to another, accounting for a star variance model

Variation from an image to another for a band b :

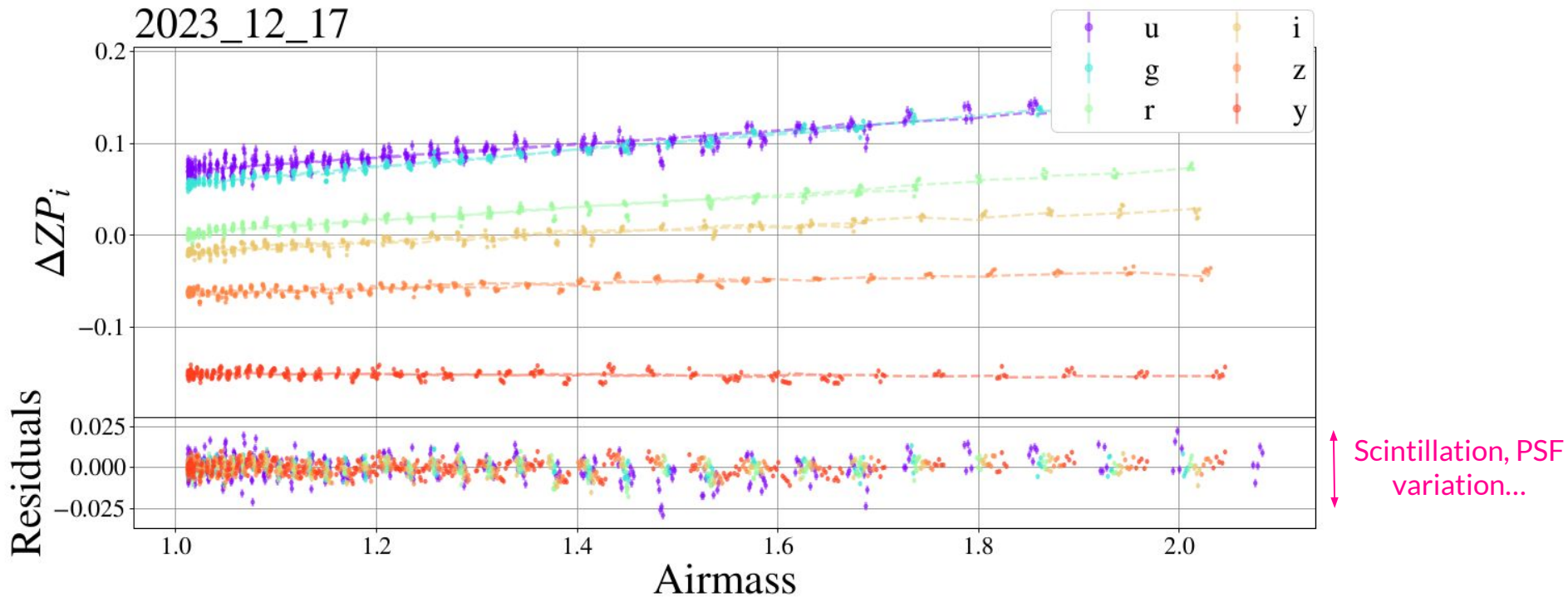
$$\Delta ZP_{b,i}(X) = \overset{\text{Atmosphere}}{k_b} X_i + \overset{\text{Out-of-atmosphere zero point}}{ZP_{0,b}}$$

ΔZP_i vs airmass



$$\Delta ZP_{b,i}(X) = k_b X_i + ZP_{0,b}$$

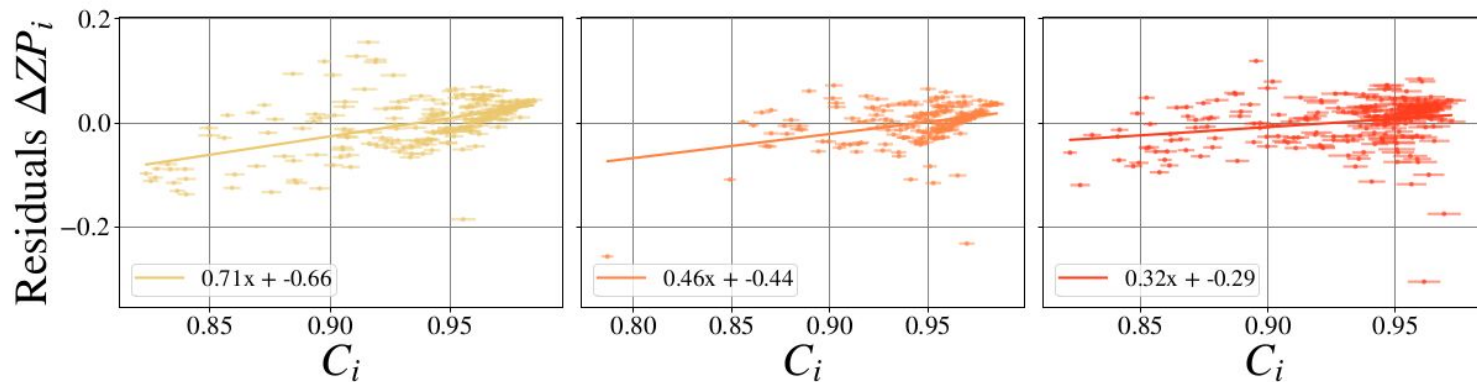
ΔZP_i vs airmass



$$\Delta ZP_{b,i}(X) = k_b X_i + ZP_{0,b}$$

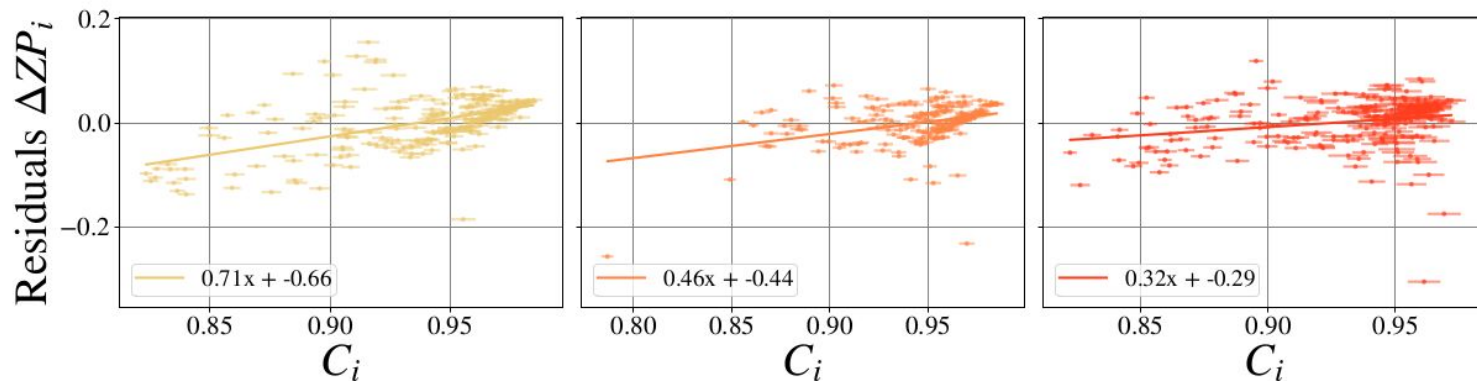
Aperture correction

$$C_i = \frac{1}{20} \sum_s \frac{F_{i,s}^{\text{obs}} (5.6\text{px})}{F_{i,s}^{\text{obs}} (7.7\text{px})} \Rightarrow \text{Proxy to estimate PSF variations}$$



Aperture correction

$$C_i = \frac{1}{20} \sum_s \frac{F_{i,s}^{\text{obs}} (5.6\text{px})}{F_{i,s}^{\text{obs}} (7.7\text{px})} \Rightarrow \text{Proxy to estimate PSF variations}$$



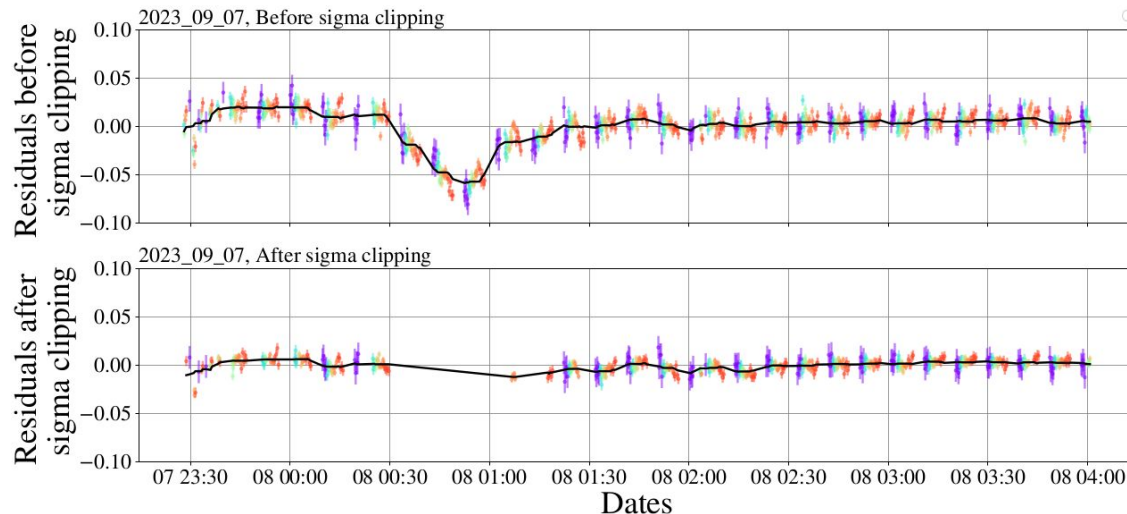
Atmosphere

Out-of-atmosphere
zero point

$$\Delta ZP_{b,i}(X, C) = k_b X_i + \alpha_b C_i + ZP_{0,b}$$

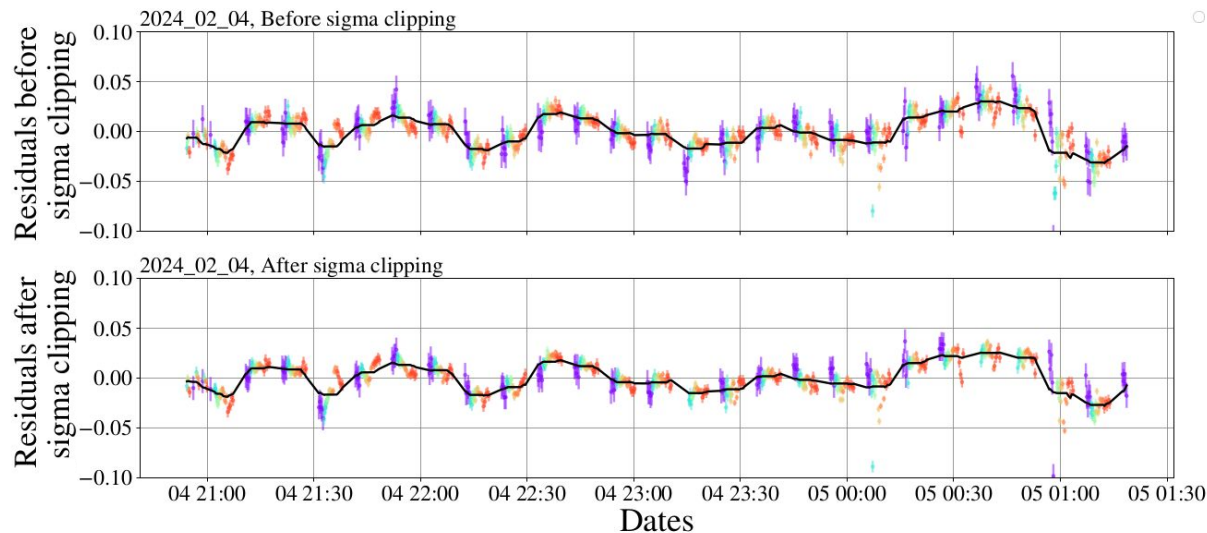
Aperture
correction

Rejection of non-photometric nights



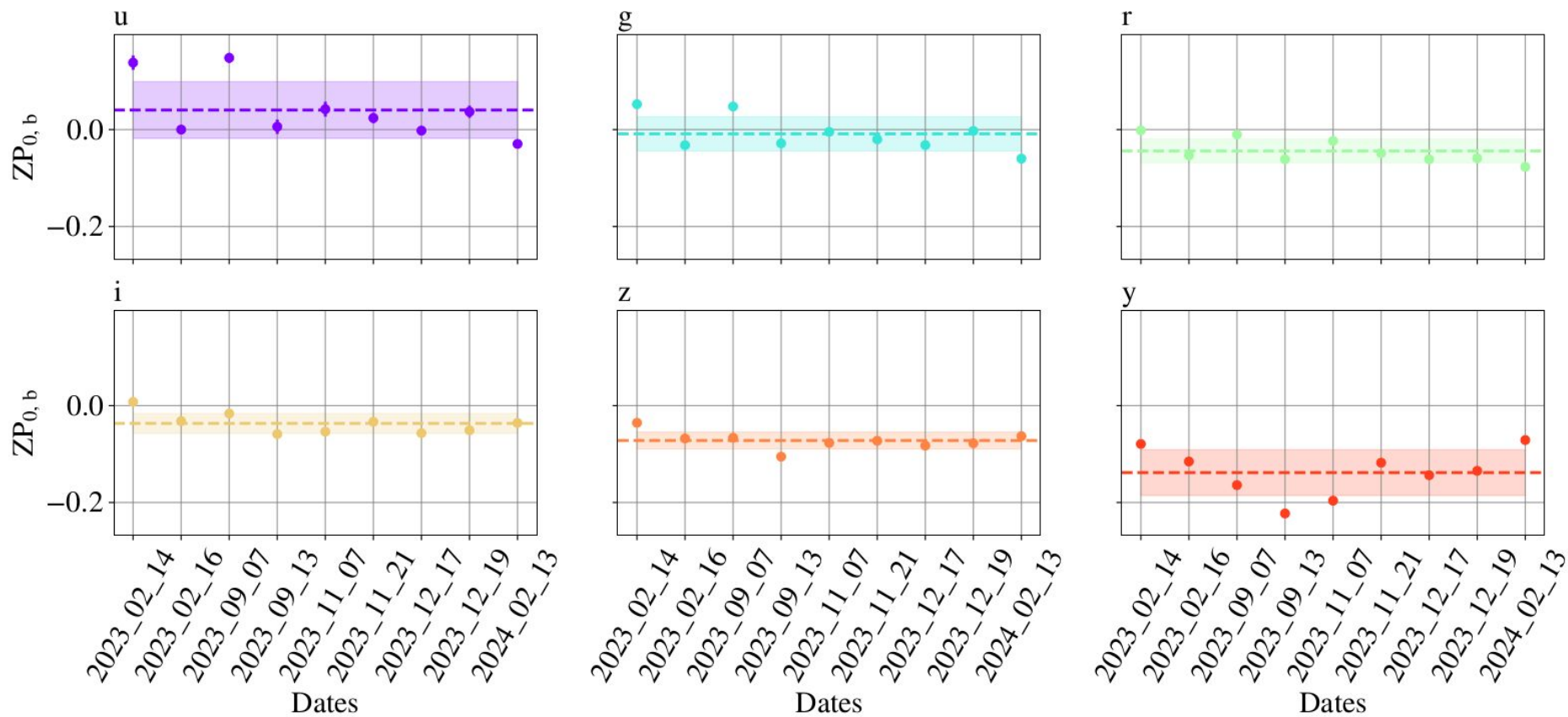
- **Gray extinction** between $\sim 00:30$ and $\sim 01:20 \Rightarrow$ **cloud extinction**
- Compute **rolling mean** μ_{rolling} in **all bands**
- Cut every points higher than $3\sigma_{\text{rolling}}$

Rejection of non-photometric nights

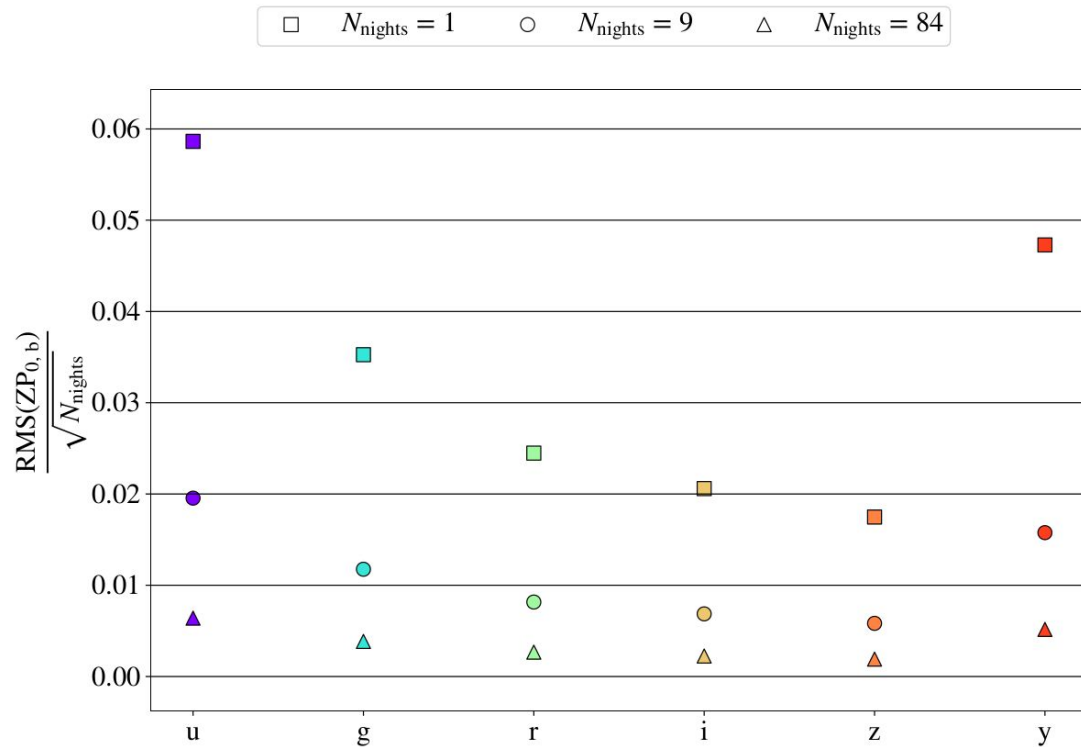


- Faint oscillations lower than $3\sigma_{\text{rolling}} \Rightarrow$ no cut performed
- Set the threshold $\sigma_{\text{rolling}} > 0.005$ to detect non-photometric nights
- Ends up with 9 photometric nights kept

Results

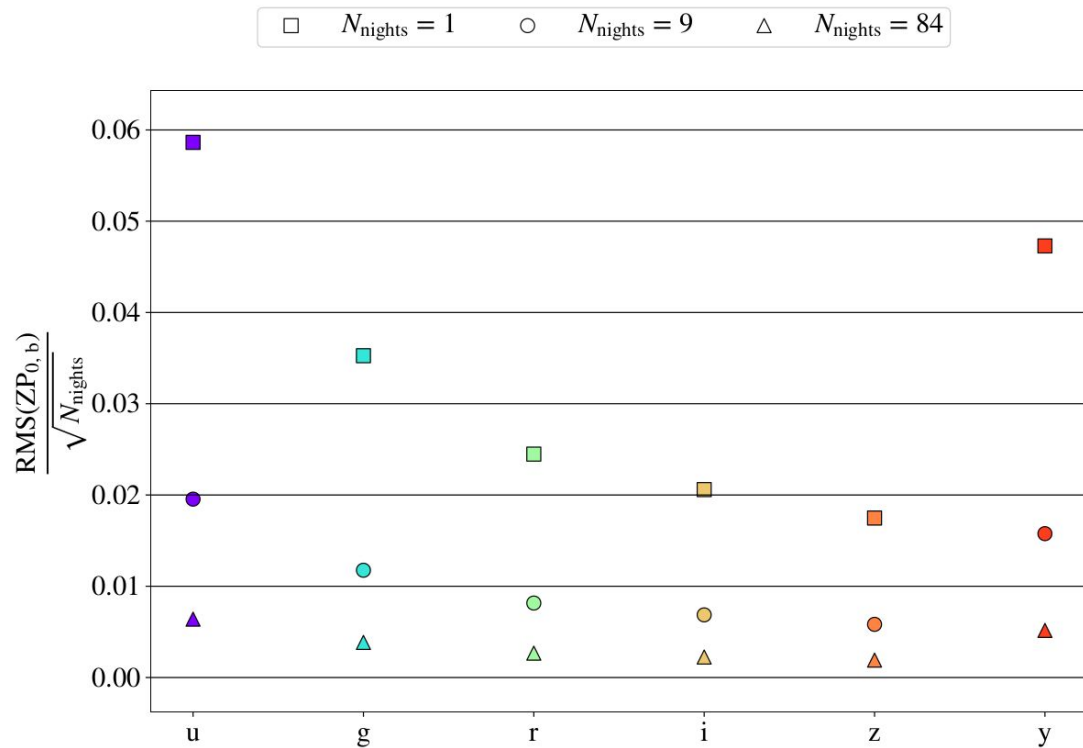


StarDICE performances projection



- 9 photometric nights
- StarDICE 2-year survey estimation \Rightarrow 84 nights
- ~ 0.2 to 0.4% uncertainty

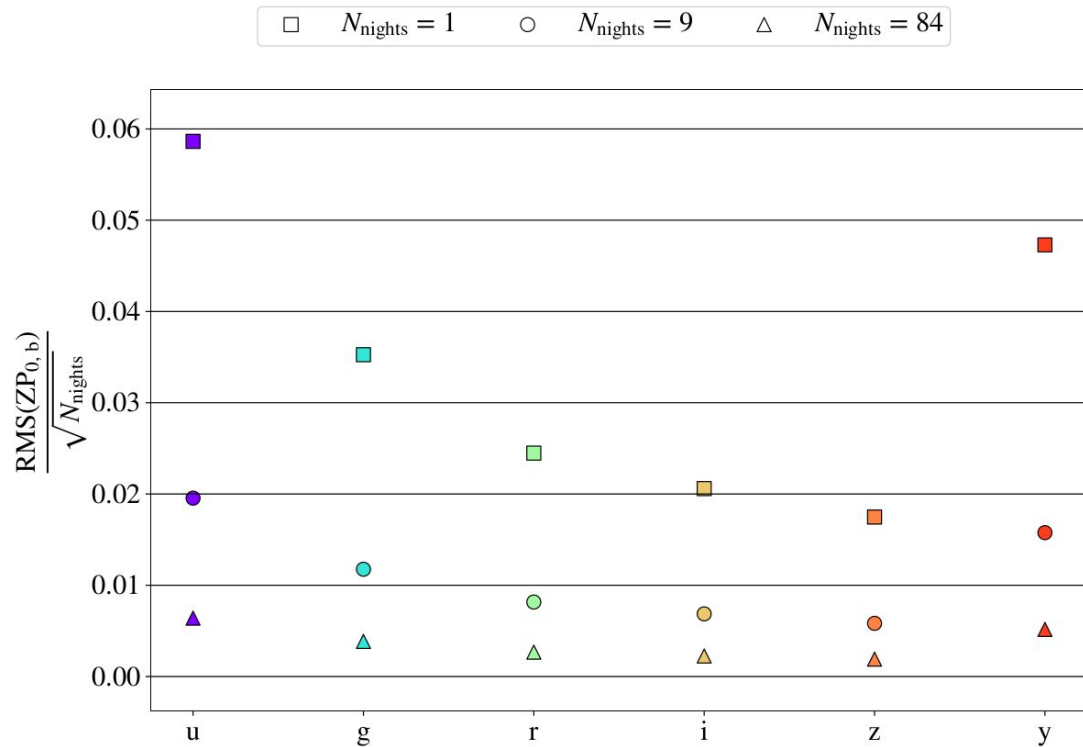
StarDICE performances projection



- 9 photometric nights
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\Rightarrow 2 to 4 times the suitable value to fully exploit the future LSST SNe Ia dataset

StarDICE performances projection



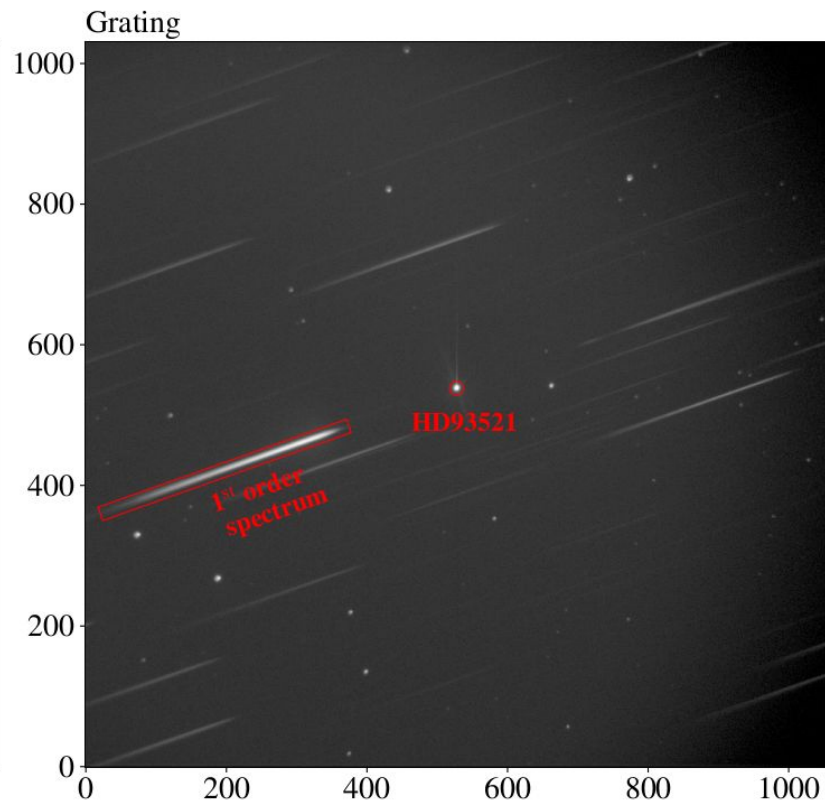
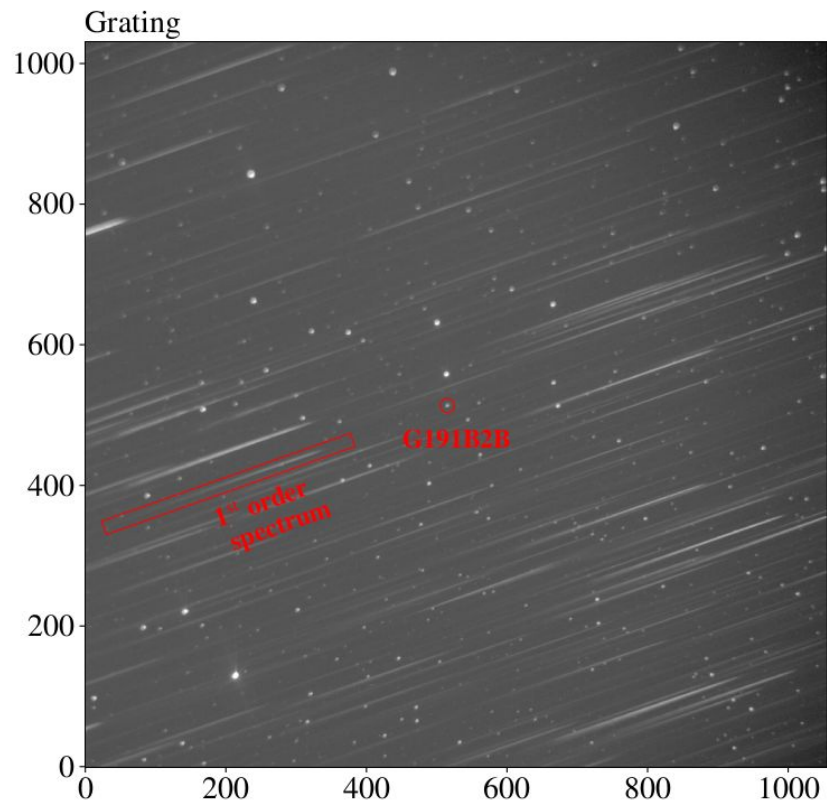
- 9 photometric nights
- StarDICE 2-year survey estimation \Rightarrow 84 nights
- ~ 0.2 to 0.4% uncertainty

\Rightarrow 2 to 4 times the suitable value to fully exploit the future LSST SNe Ia dataset

\Rightarrow Improve the atmosphere transmission prior by fitting live parameters

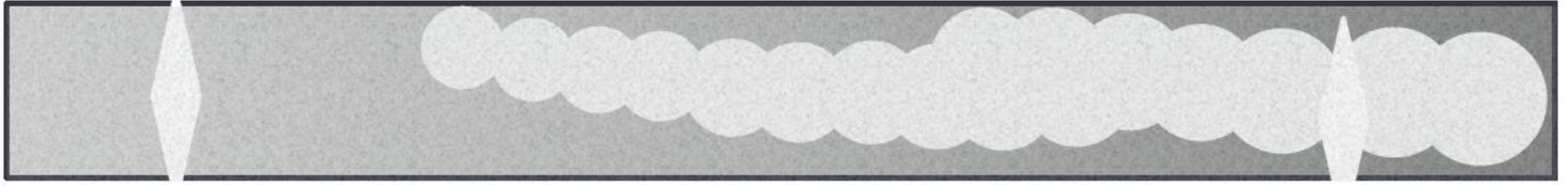
6.b. Spectrophotometric analysis

Image examples



Slitless spectrophotometry

Spectractor software (Neveu et al. 2021)

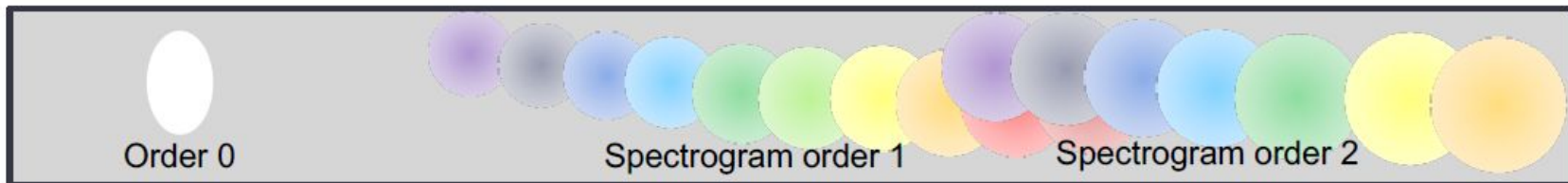


Slitless spectrophotometry

Spectractor software (Neveu et al. 2021)



Spectractor + prior knowledge of PSF

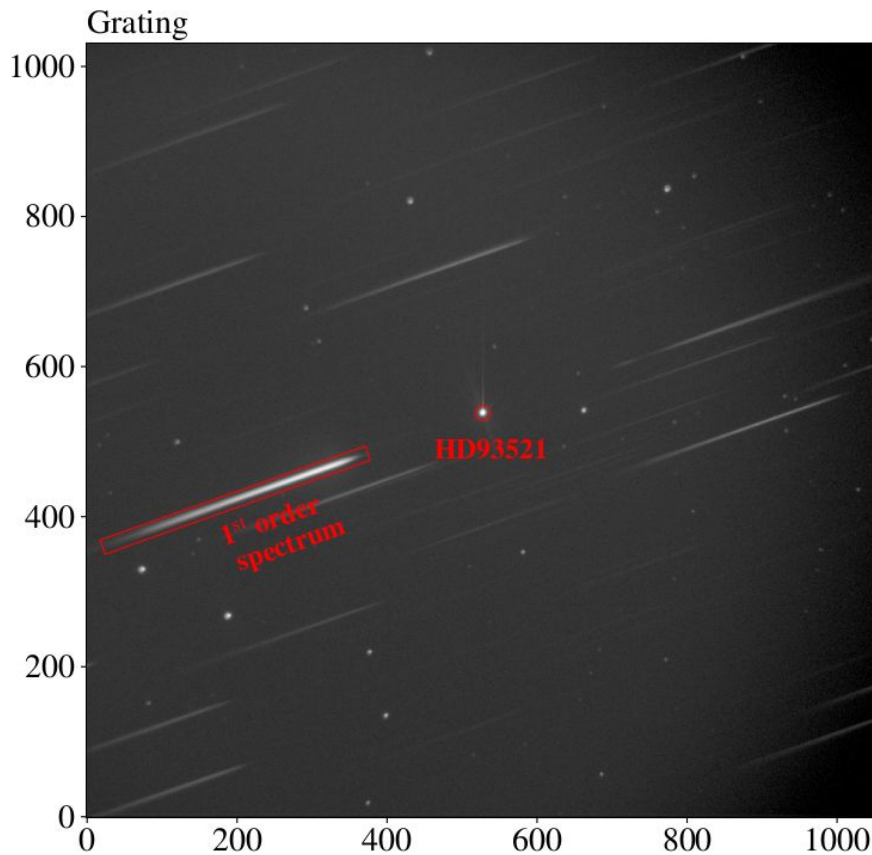


HD93521 spectrum

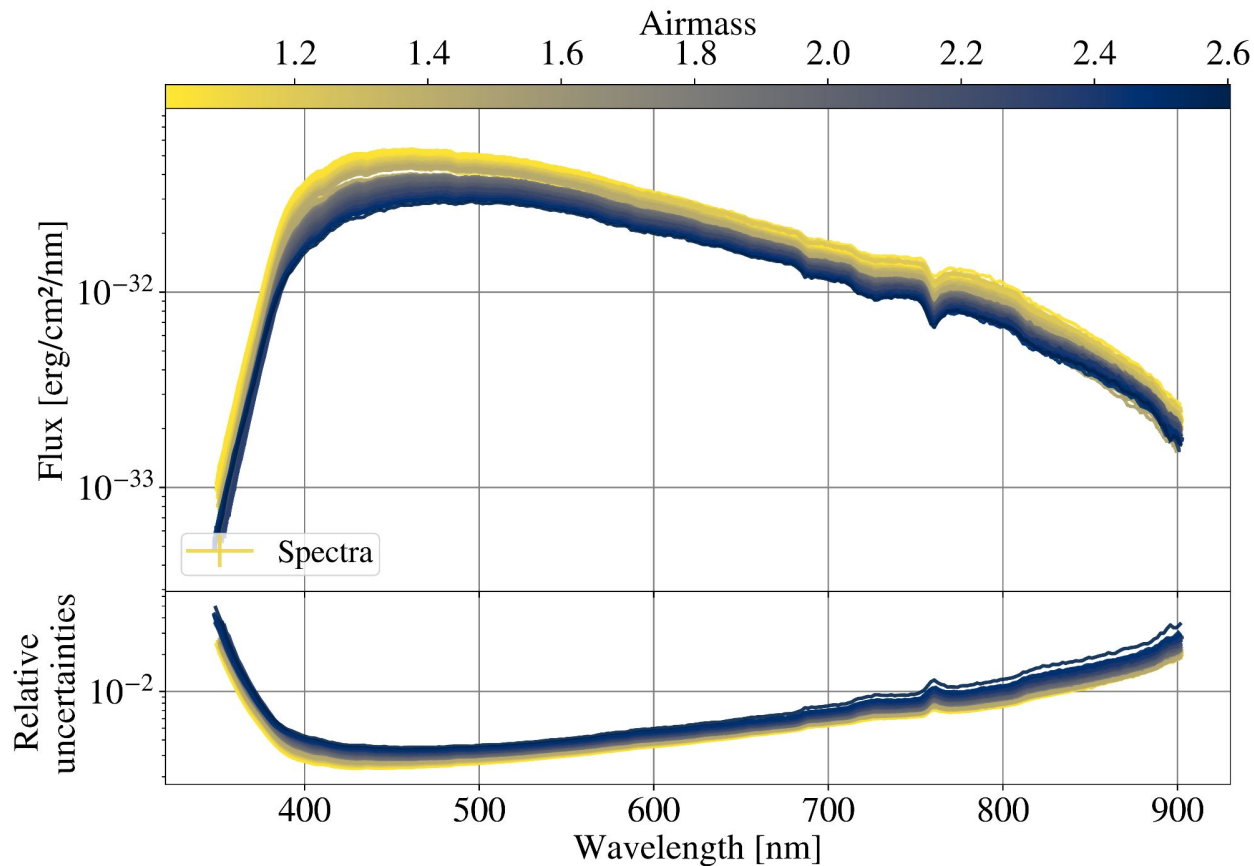
Spectrum extraction of HD93521

- Part of CALSPEC calibration
- Bright: $m_{\text{HD93521}} = 6.99$
- Isolated field

Image of HD93521 observed by StarDICE with the grating in the filterwheel



HD93521 spectra extraction



- ~300 images at different airmasses
- Spectra extracted with <0.1% uncertainties in [360-750]nm

⇒ Validated method for a bright and isolated star

Atmosphere extraction

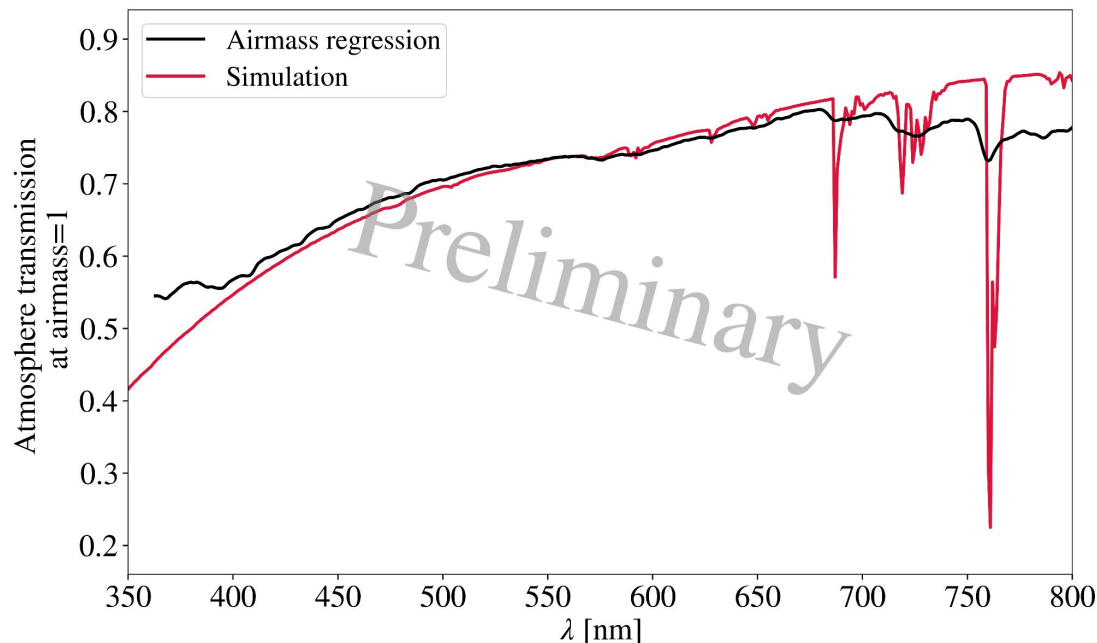
Two methods:

- Fit the atmosphere transmission with prior on the star SED and telescope response

Atmosphere extraction

Two methods:

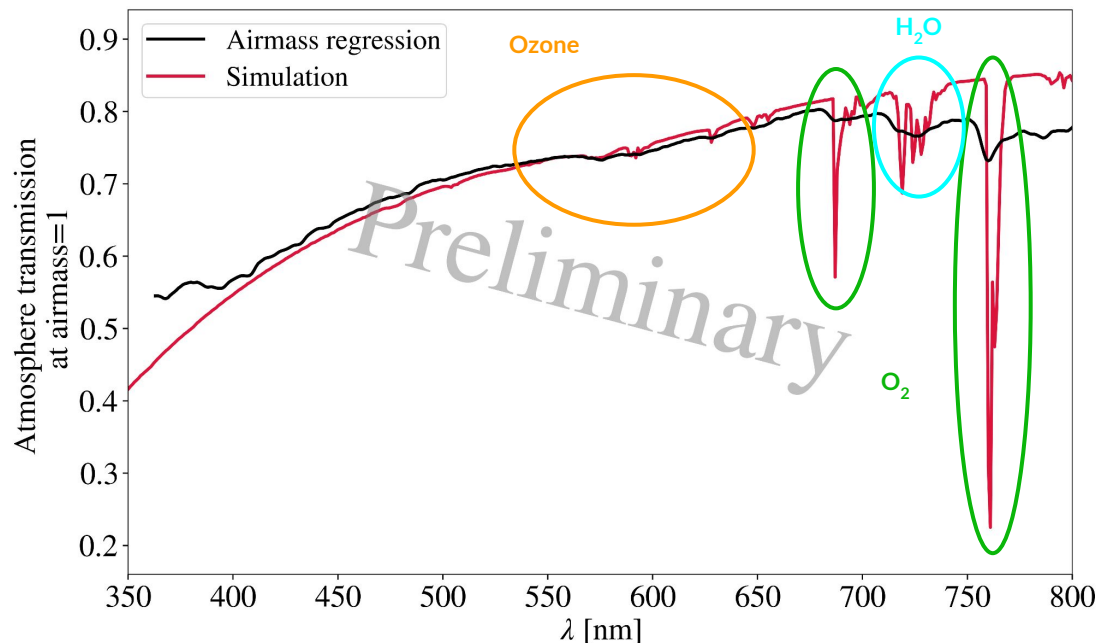
- Fit the atmosphere transmission with prior on the star SED and telescope response
- Perform an airmass regression



Atmosphere extraction

Two methods:

- Fit the atmosphere transmission with prior on the star SED and telescope response
- Perform an airmass regression

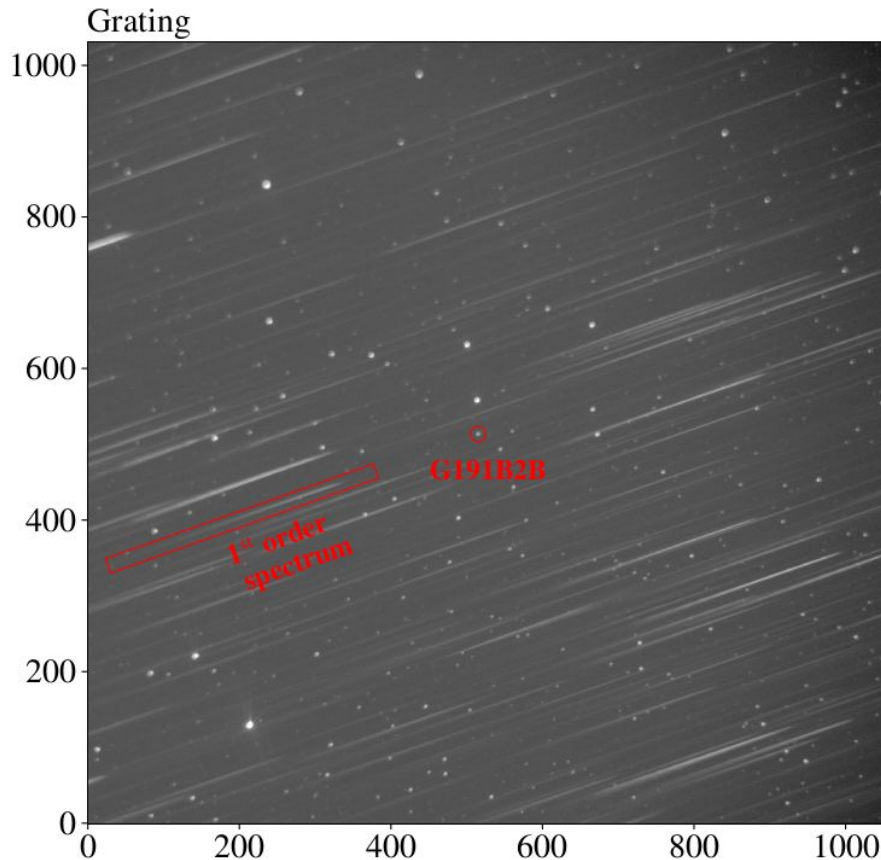


G191B2B spectrum

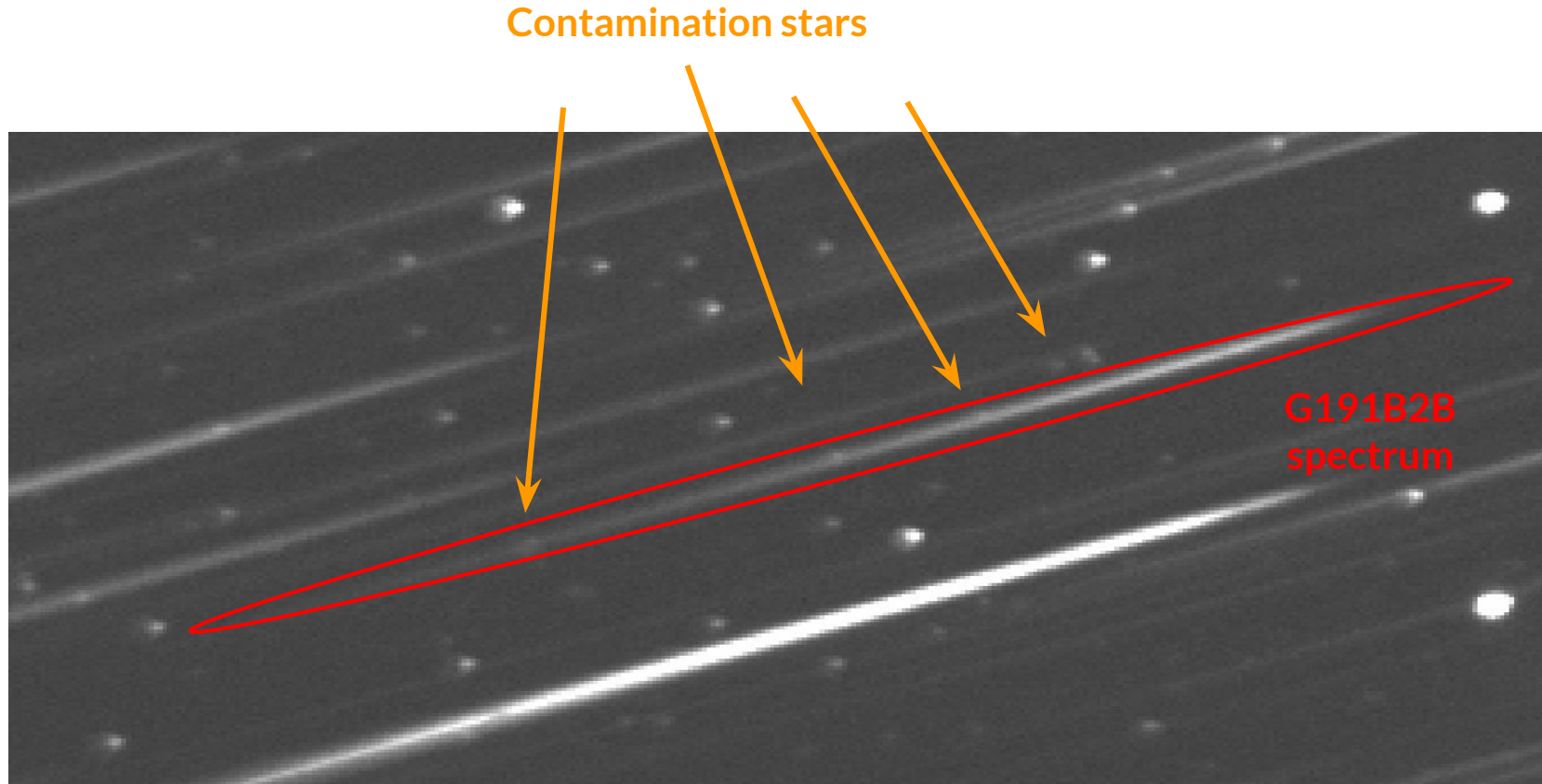
Spectrum extraction of G191B2B

- Primary CALSPEC standard
- Faint: $m_{\text{G191B2B}} = 11.69$
- Very crowded field

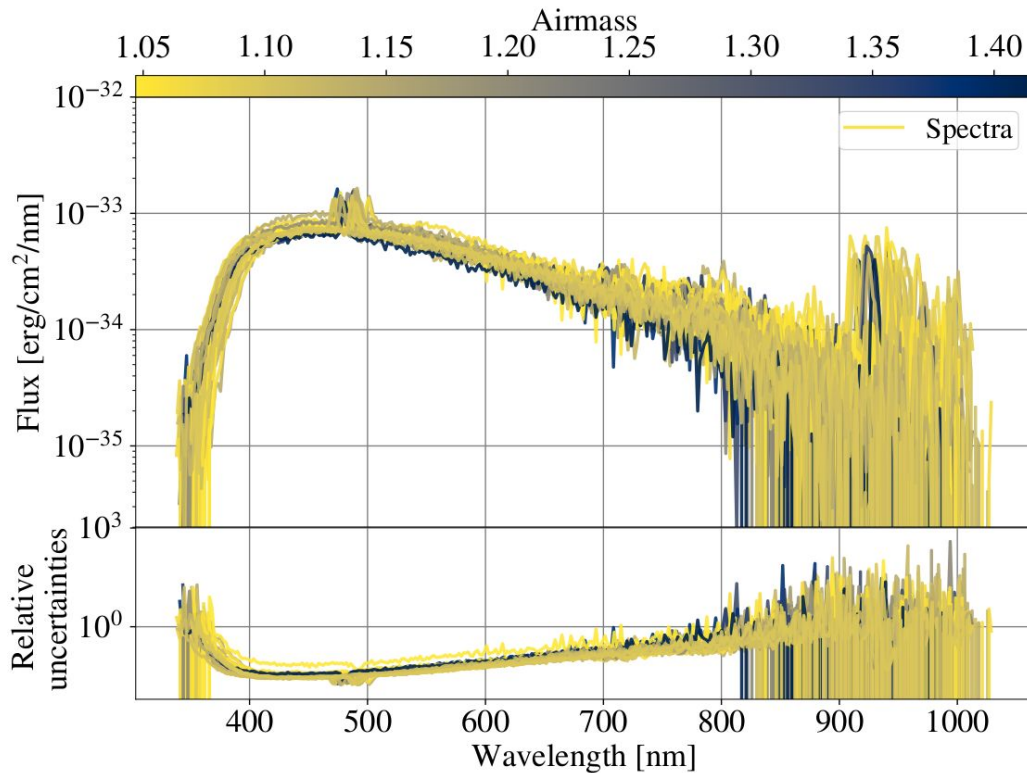
Image of G191B2B observed by StarDICE with the grating in the filterwheel



Zoom on G191B2B spectrum



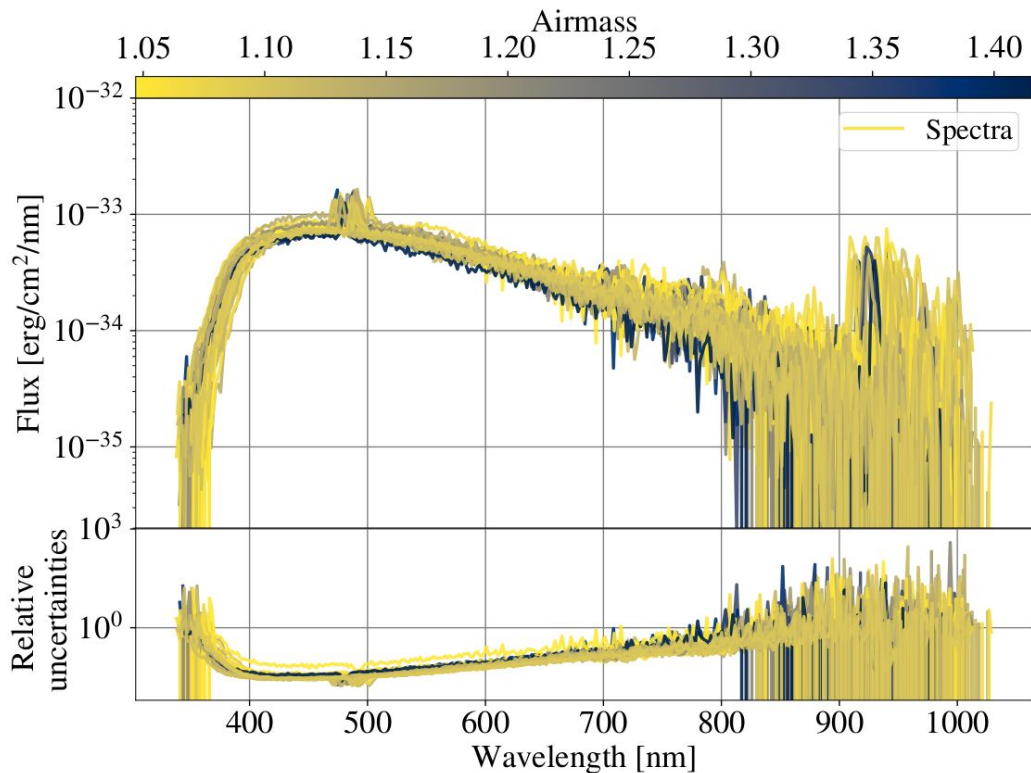
G191B2B spectra extraction



- ~100 images at different airmasses

⇒ The fit crashes because of stars overlapping with the spectrum

G191B2B spectra extraction



- ~100 images at different airmasses

⇒ The fit crashes because of stars overlapping with the spectrum

Solutions:

- Develop full-forward model of the star field (work in progress)
- Extract brighter stars in the field

6.c. Conclusion

Photometry

- Measurements of ZP_0 for StarDICE filters

Future developments:

- Priors improveable (**artificial star + atmosphere transmission fit**)
- **Forced photometry** to prevent selection bias for faint stars
- Infrared data to measure **smaller gray extinction from clouds**

Spectrophotometry

- **Feasibility** of extracting spectra on **StarDICE images**
- Joint effort with the **Auxiliary Telescope (AuxTel)** at Rubin observatory to measure **atmospheric transmissions**

Future developments:

- Atmosphere fit → **PWV, ozone, aerosols**
⇒ crucial for photometric analysis
- **Forward model** of the **starfield** for crowded images

7. General conclusion

General conclusion

- SNe Ia cosmology needs to **improve photometric calibration (CBP, StarDICE...)** to be certain of **unbiased dark energy measurements**

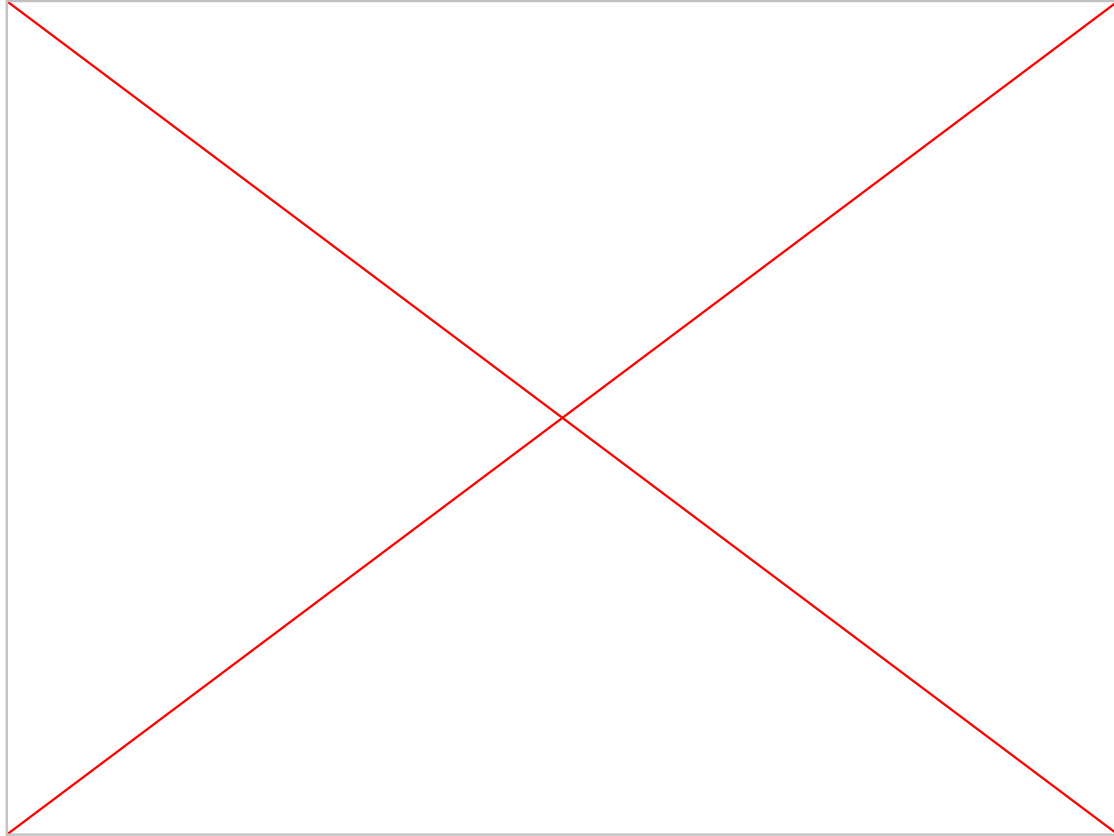
General conclusion

- SNe Ia cosmology needs to **improve photometric calibration (CBP, StarDICE...)** to be certain of **unbiased dark energy measurements**
- **CBP:**
 - **Results** will be detailed in a **paper** soon (**Souverein et al., in prep.**)
 - Measured **bandpasses** with **high resolution**, and detected **out-of-band leaks**
 - Proof of concept **validated** for measuring SNe Ia survey telescopes (**Rubin-CBP** for **LSST**, **Traveling-CBP** for **ZTF...**)

General conclusion

- SNe Ia cosmology needs to **improve photometric calibration (CBP, StarDICE...)** to be certain of **unbiased dark energy measurements**
- **CBP:**
 - **Results** will be detailed in a **paper** soon (**Souverein et al., in prep.**)
 - Measured **bandpasses** with **high resolution**, and detected **out-of-band leaks**
 - Proof of concept **validated** for measuring SNe Ia survey telescopes (**Rubin-CBP** for **LSST**, **Traveling-CBP** for **ZTF...**)
- **StarDICE:**
 - Pre-survey → Validated the method to **refine zero point** of **CALSPEC** calibration
 - The **2-year survey** will benefit from the **artificial star**, an **infrared camera**, improving the photometric accuracy
 - **Slitless spectrophotometry** is a **powerful tool**, for both **atmospheric considerations**, and measuring the whole spectrum of a target in **one image**

Thank you for your attention



Backup slides

Cosmo

■ Cosmological principle

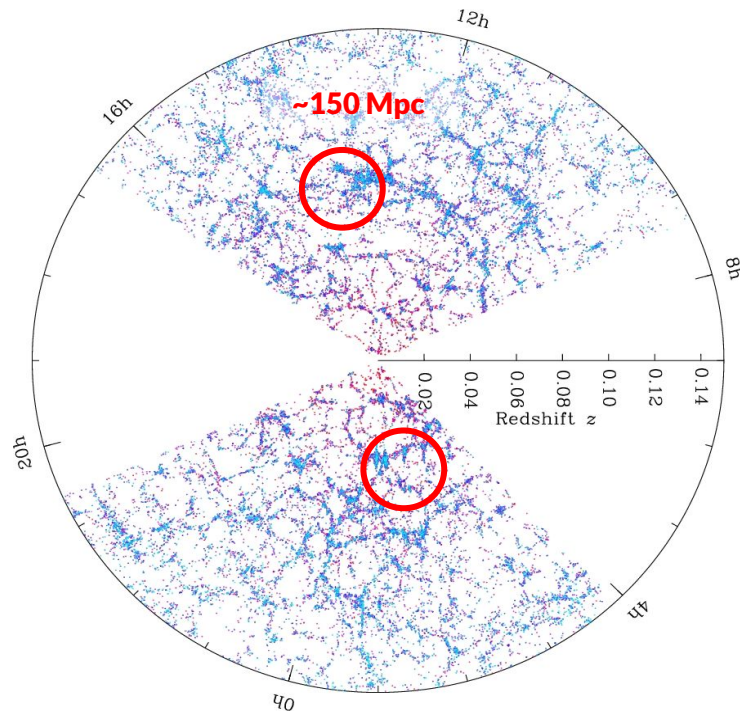
But the Universe is vast and full of stuffs, how can we study it?

Cosmological principle

But the Universe is vast and full of stuffs, how can we study it?

On cosmological scales, the Universe is considered:

- Homogeneous



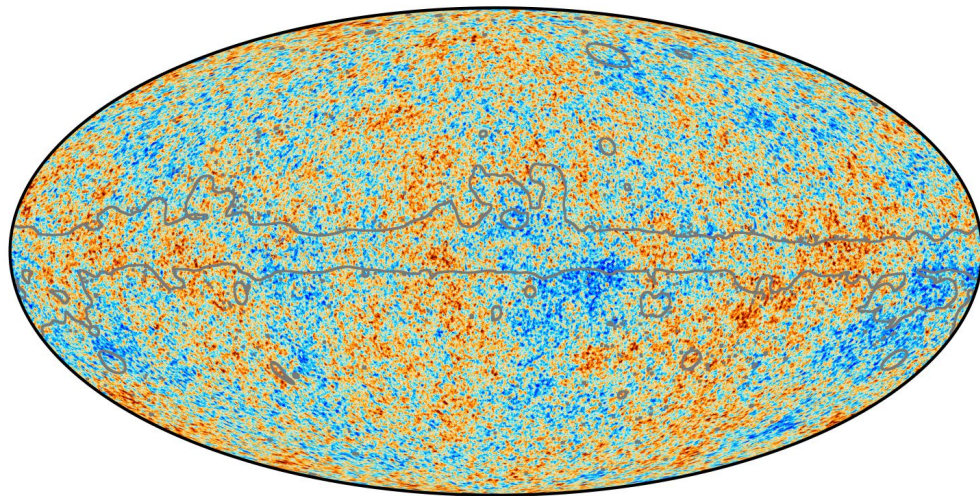
SDSS map of the distribution of galaxies

■ Cosmological principle

But the Universe is vast and full of stuffs, how can we study it?

On cosmological scales, the Universe is considered:

- Homogeneous
- Isotropic



-300 300 μK

CMB map from Planck Collaboration et al. 2020a

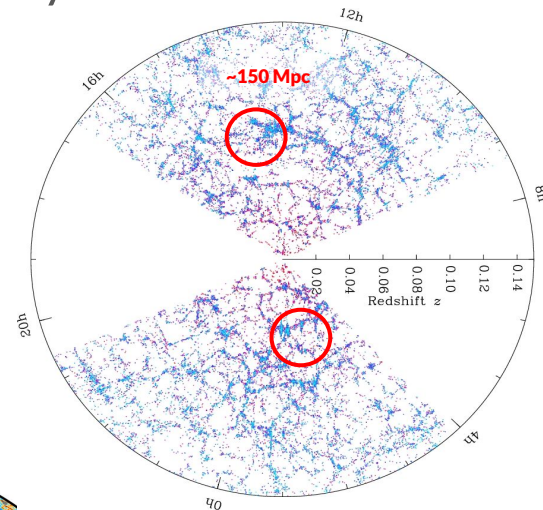
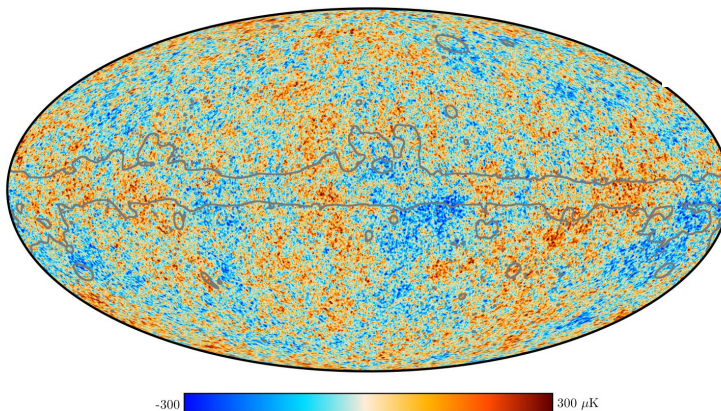
Cosmological principle

But the Universe is vast and full of stuffs, how can we study it?

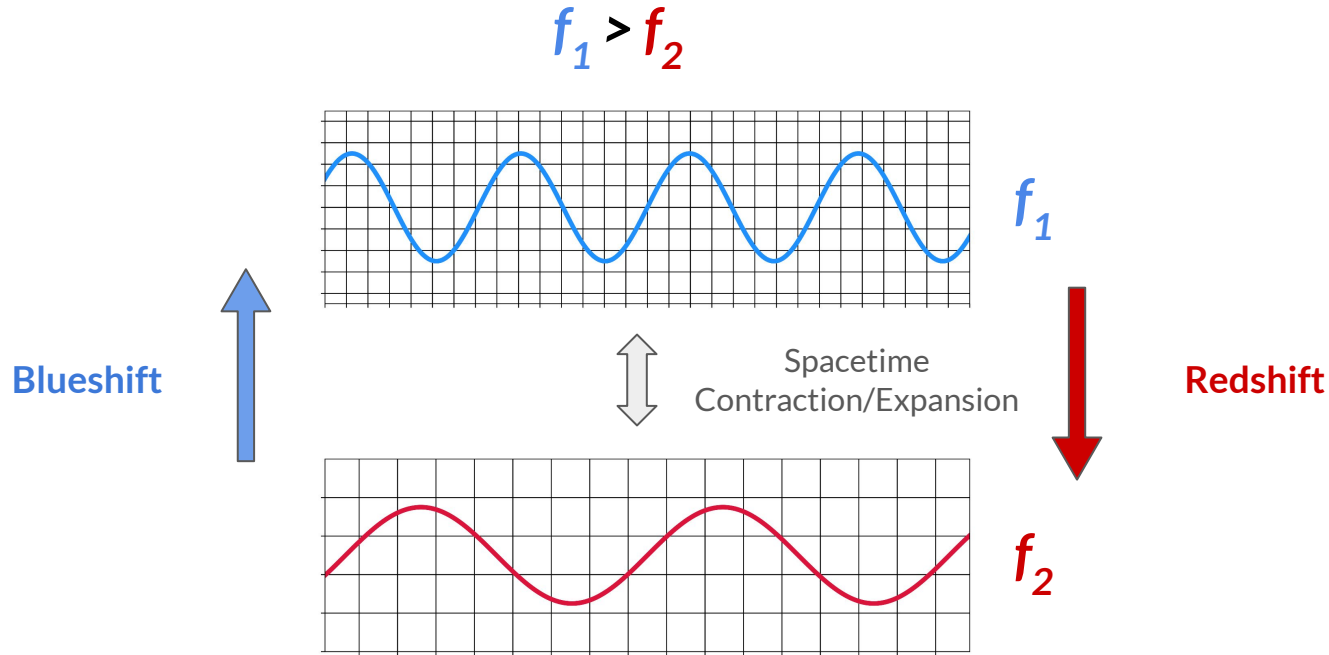
On cosmological scales, the Universe is considered:

- Homogeneous
- Isotropic

⇒ Cosmological principle



Spacetime evolution



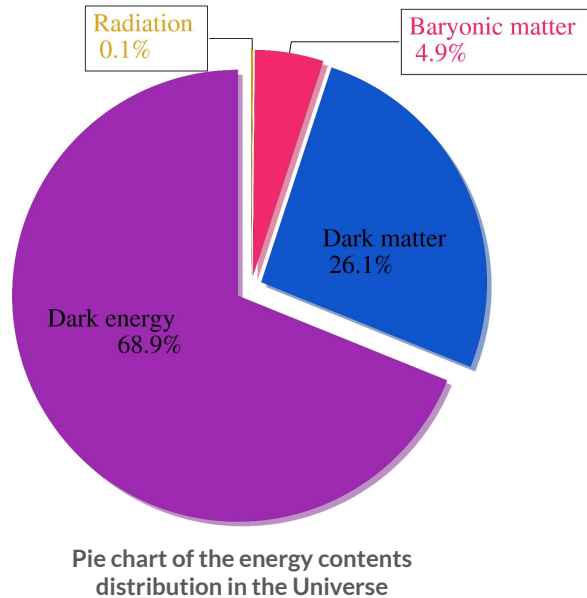
Spacetime deformations affect both light **trajectory** and **wavelength**
⇒ **Light is a tracer for studying spacetime evolution**

Dark energy models

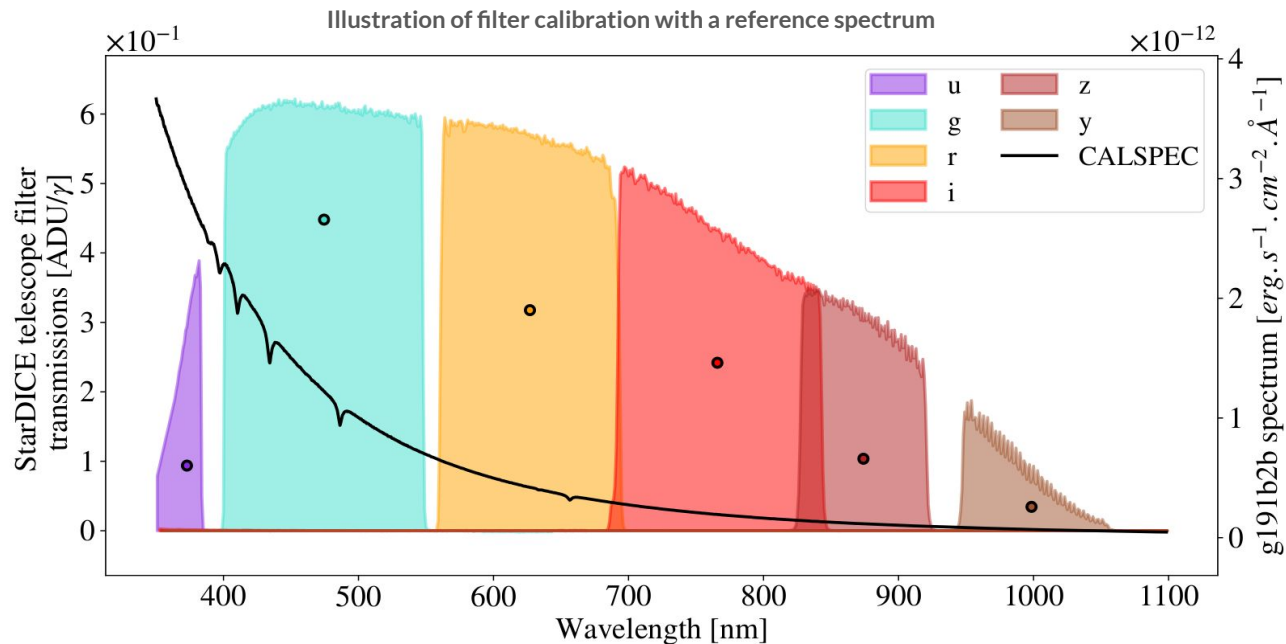
Dark energy → fluid described by an equation of state with the parameter w :

$$\rho_{\text{de}} \propto a^{-3(1+w)}$$

- Λ CDM, the standard model
 - $w = -1$, Λ for the cosmological constant, CDM for Cold Dark Matter, and a flat Universe
- w CDM
 - constant w but with $w \neq -1$
- $w_0 w_a$ CDM
 - w is sets dynamic with: $w(a) = w_0 + \left(1 - \frac{a}{a_0}\right)w_a$



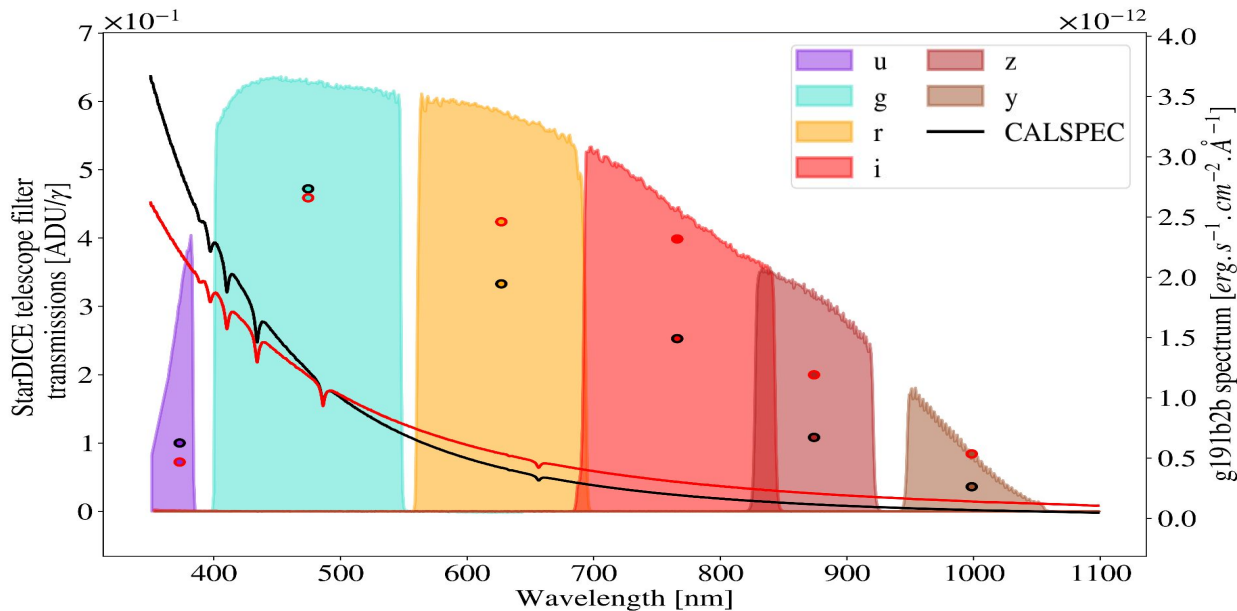
Adjusting bandpasses from CALSPEC



Observations of **CALSPEC** photometric standards
⇒ Calibration of the survey's bands

Adjusting bandpasses from CALSPEC

Illustration of filter calibration with a reference spectrum



Observations of **CALSPEC** photometric standards

⇒ Calibration of the survey's bands

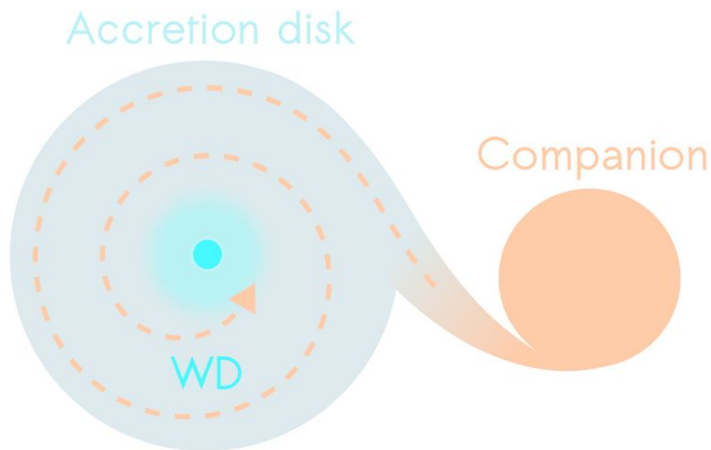
⇒ A chromatic difference in the model induces a biased calibration

SNe Ia

Explosion mechanism

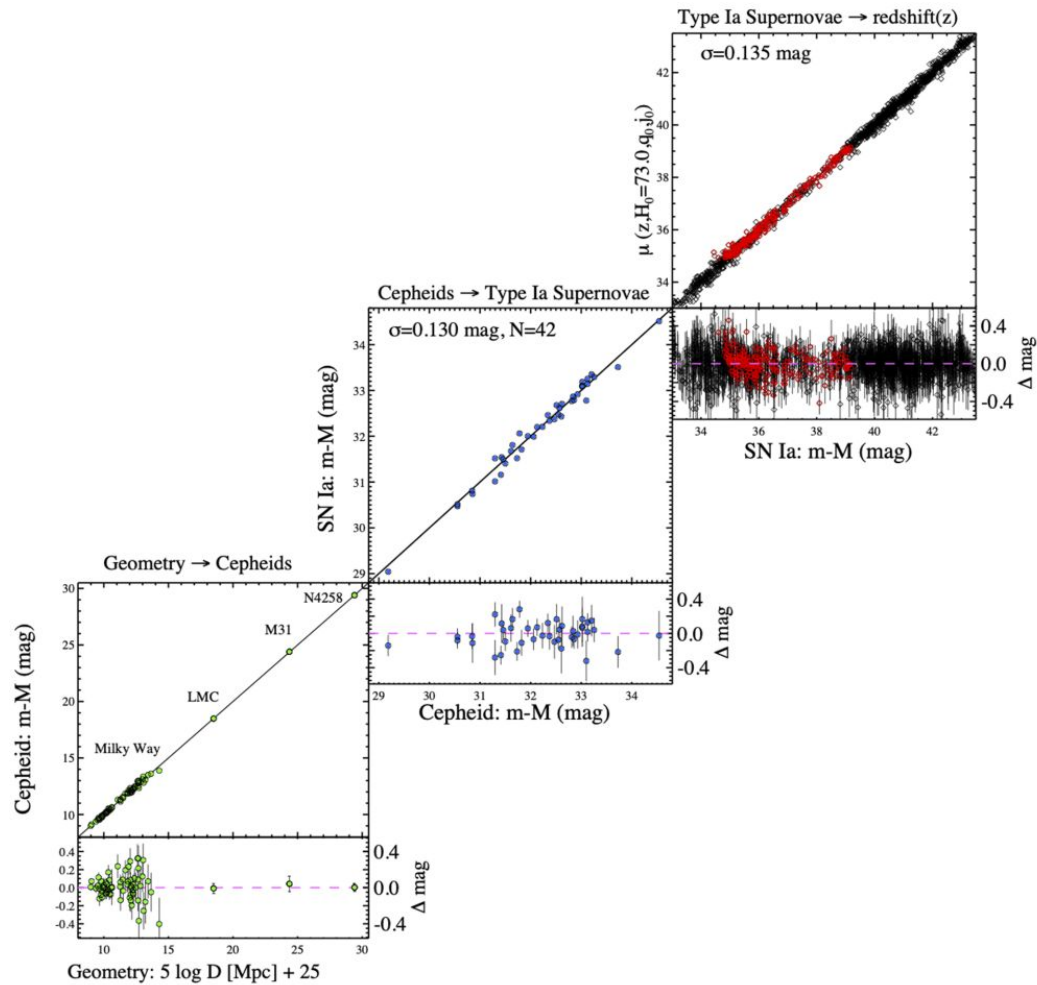
- Explosion of a carbon-oxygen white dwarf (WD) with a mass $> 1.4 M_{\odot}$
- Two scenarios:

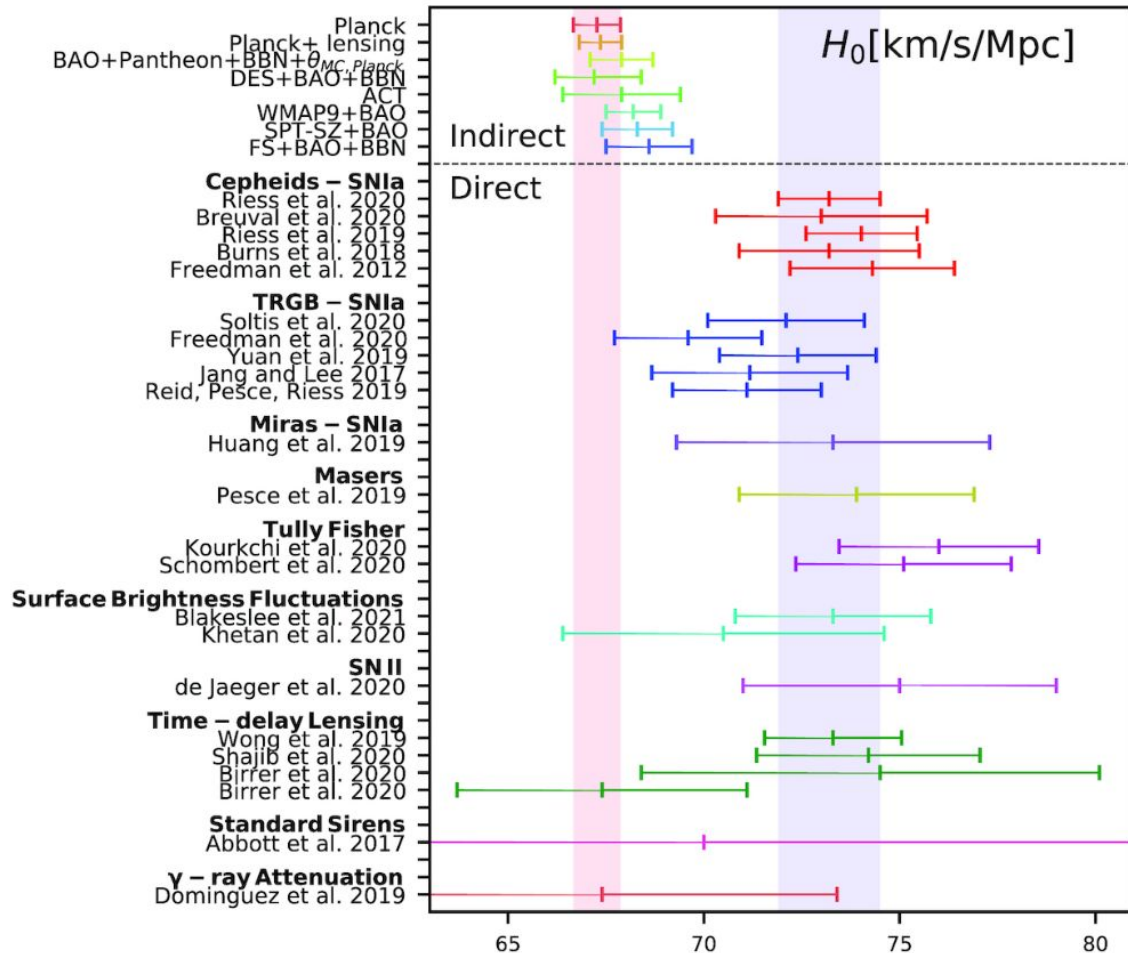
Single degenerate

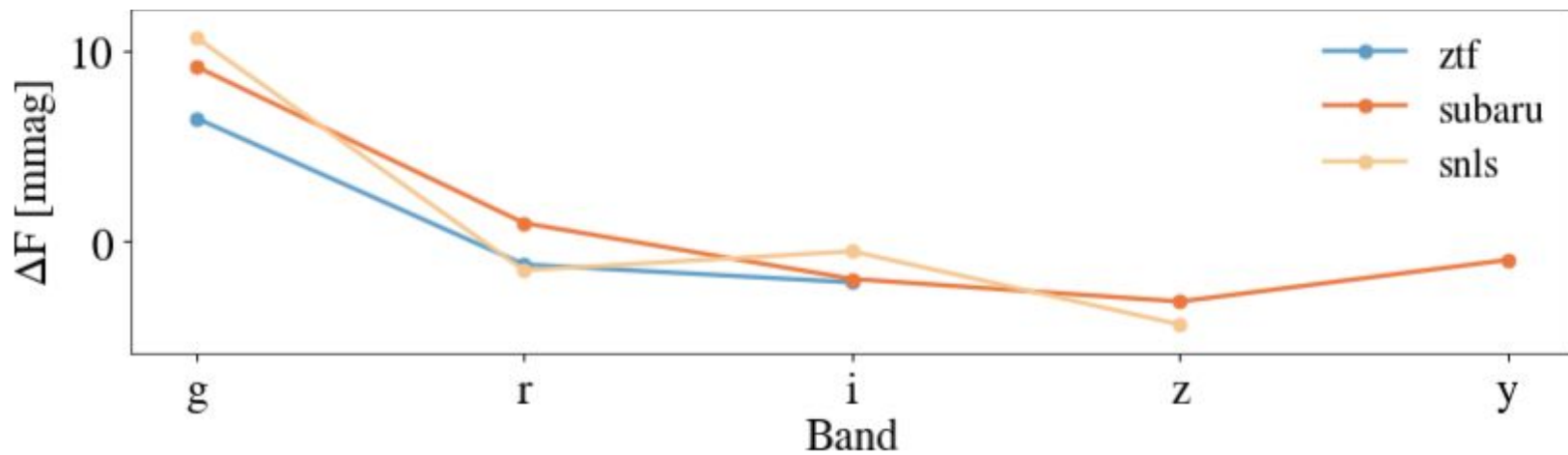
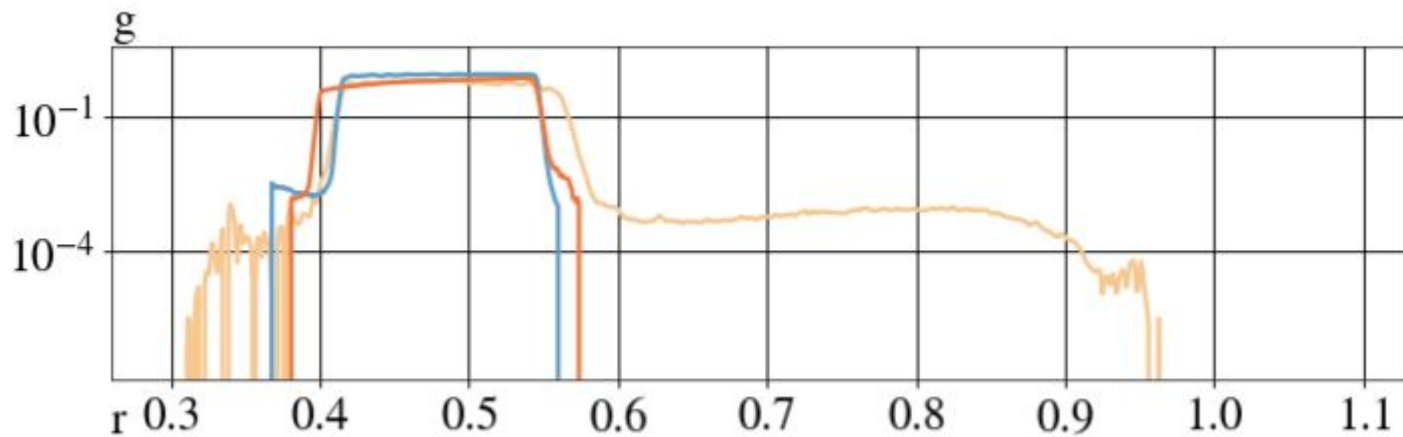


Double degenerate





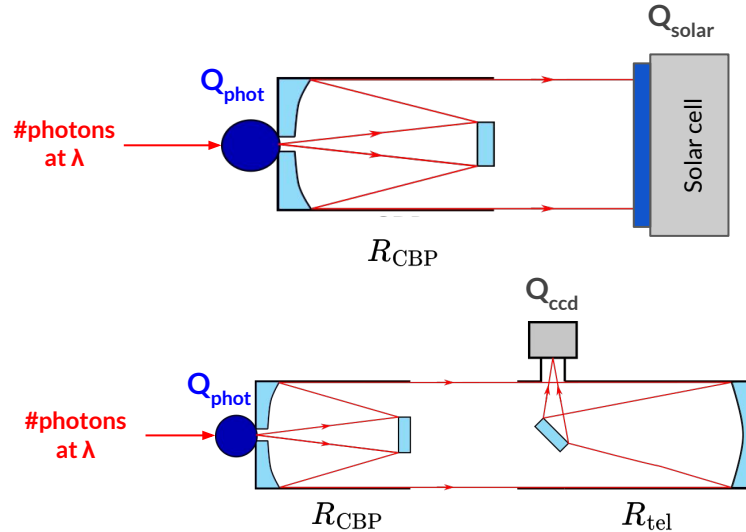




CBP

CBP guideline

Want to calibrate a telescope ? Simple, use another reverse-mounted telescope !



$$R_{\text{CBP}} = \frac{Q_{\text{solar}}}{Q_{\text{phot}} \times \epsilon_{\text{solar}} \times e}$$

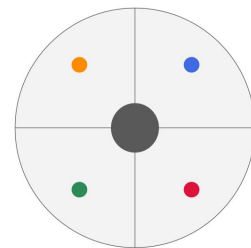
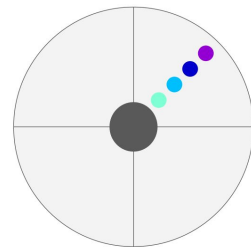
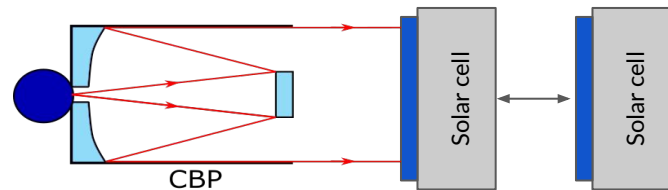
$$R_{\text{tel}} = \frac{Q_{\text{ccd}}}{Q_{\text{phot}} \times R_{\text{CBP}}}$$

Congratulations, calibration is done !

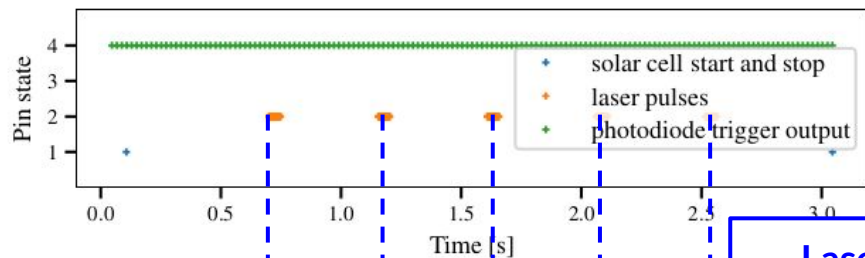
Acquisition plan

Measurements in different conditions to evaluate systematics and make pupil stitching:

- Spectrograph calibration
- CBP response:
 - Solar Cell measurement; 5mm pinhole
 - Long and short distance ($\sim 16\text{cm}$ difference); 5mm pinhole
 - Cap on the CBP to measure ambient light
- StarDICE response:
 - Same position; every camera filter; $75\mu\text{m}$ & 5mm pinhole
 - 8 positions on the mirror; $75\mu\text{m}$ pinhole (“pupil stitching”)
 - 4 positions on different quadrants but same radius
 - 4 positions at different radius but same quadrant
 - (4×4) positions on the CCD; $75\mu\text{m}$ pinhole

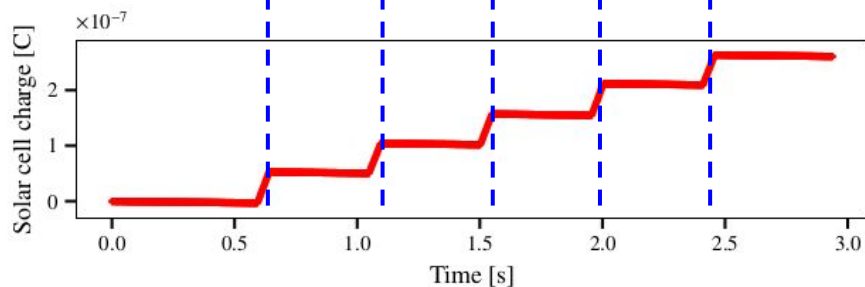
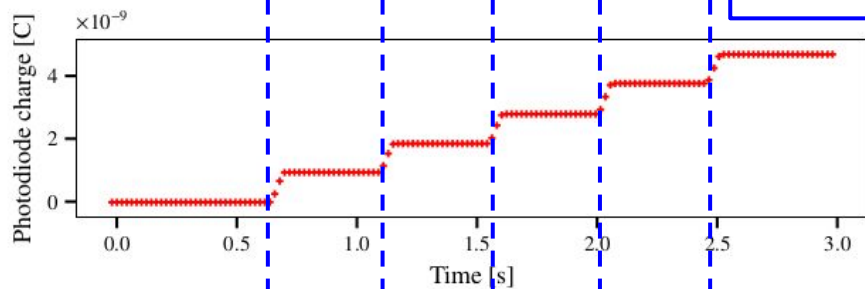


Photodiode and solar cell dataset



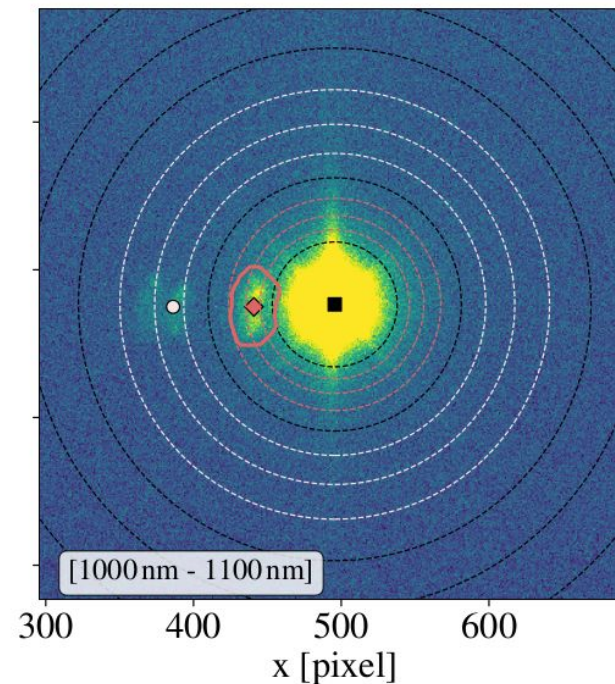
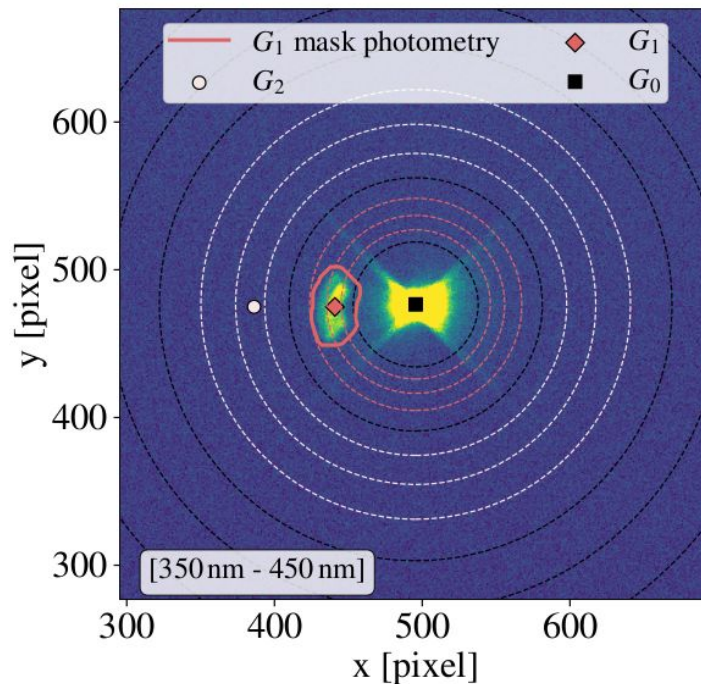
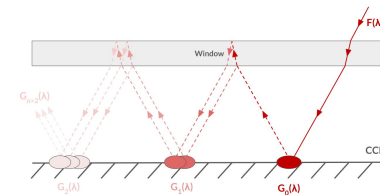
Logic timer device \Rightarrow synchronizing clocks of every electrometers with the laser

Laser bursts

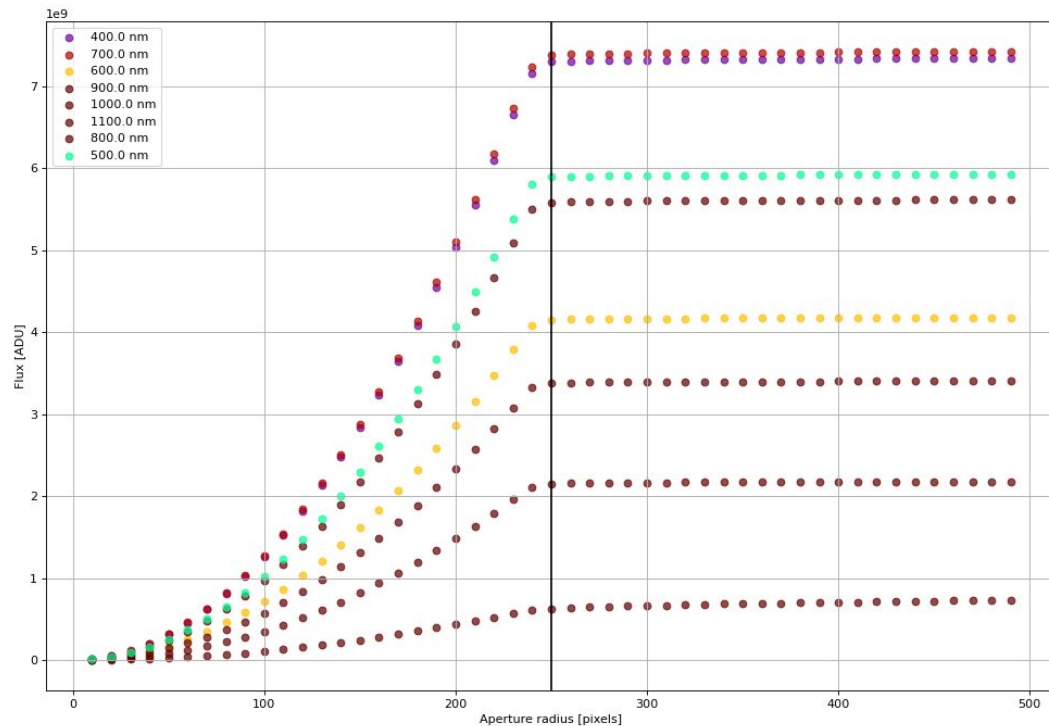


Two electrometers measuring charges [C]: one for the **photodiode** and one for the **solar cell**

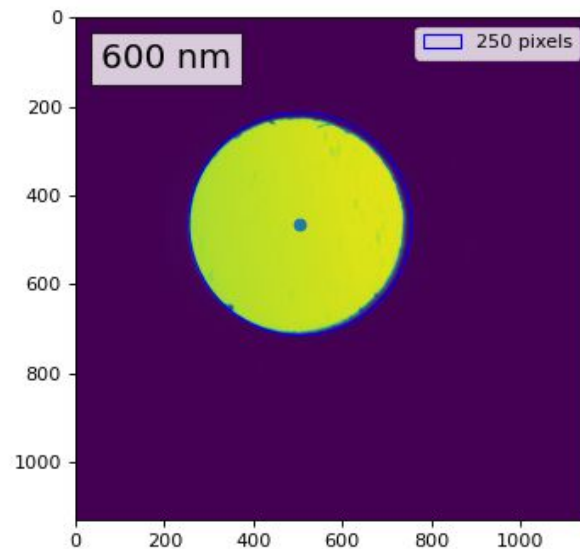
Ghost contamination



Growth curve



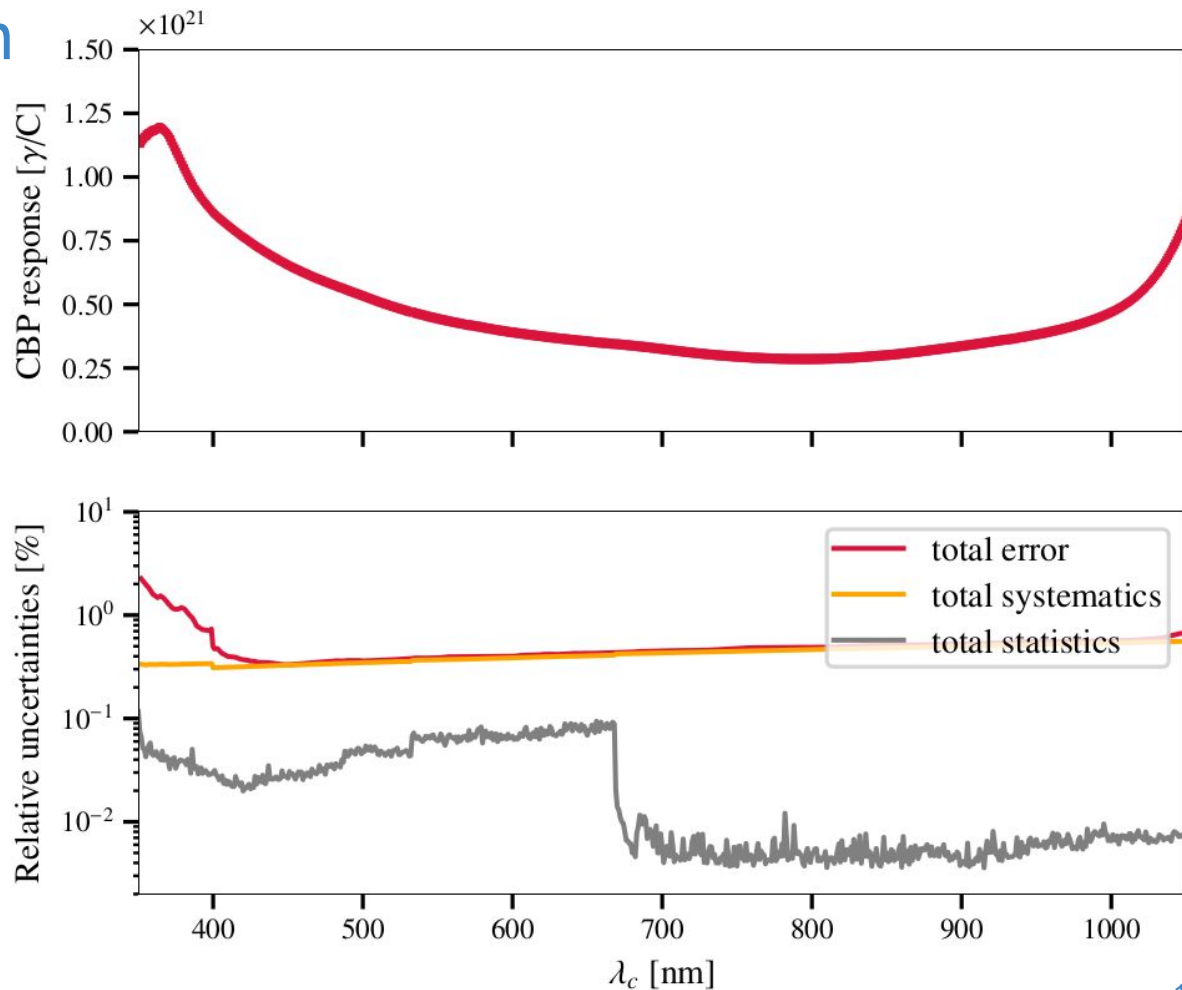
→ Break at 250 pixels

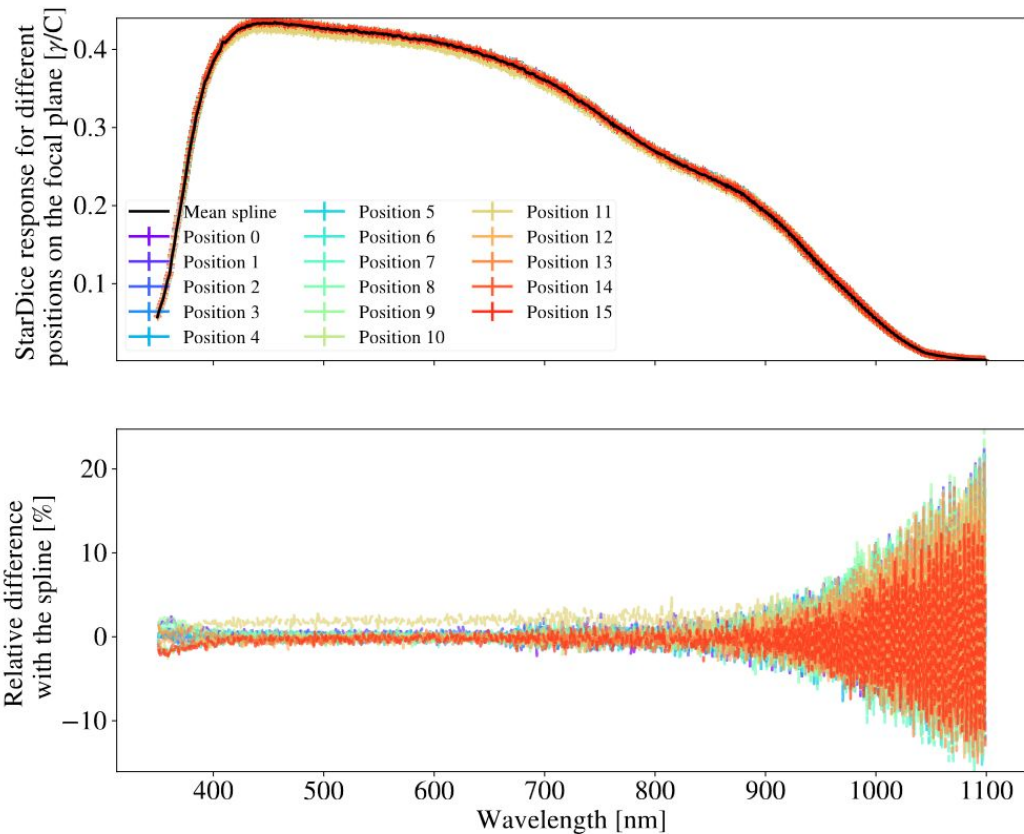


CBP transmission

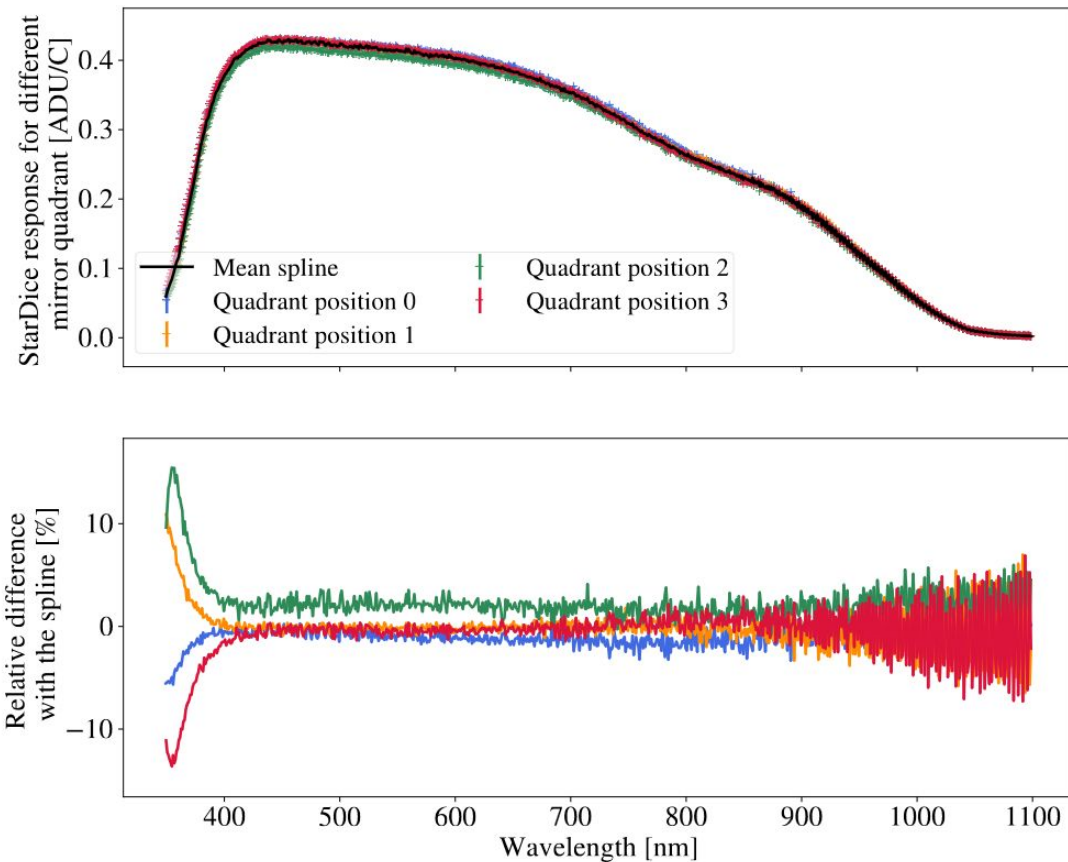
$$R_{\text{CBP}} = \frac{Q_{\text{solar}}}{Q_{\text{phot}} \times \epsilon_{\text{solar}} \times e}$$

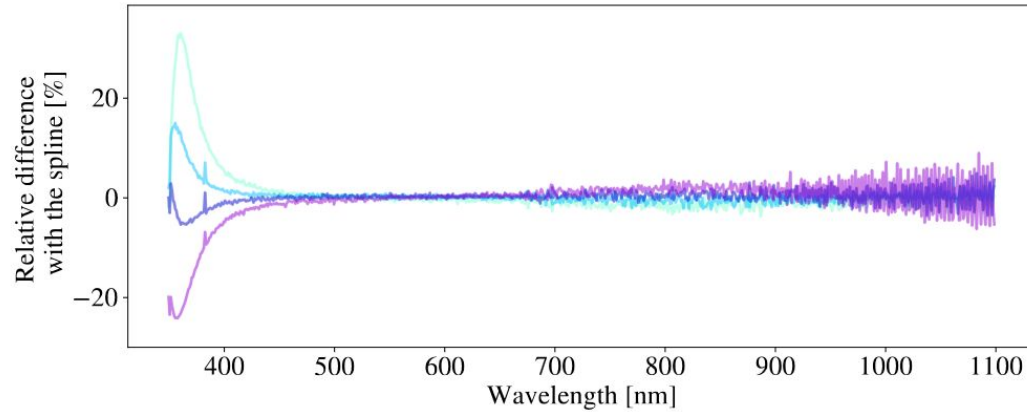
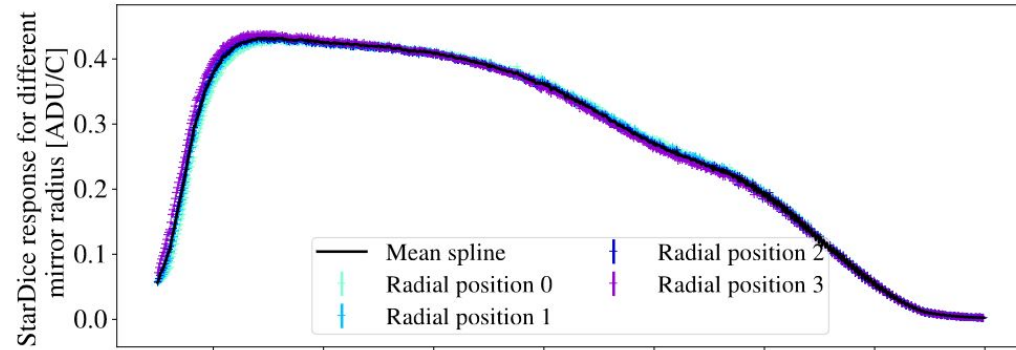
~0.4 % per nm uncertainty
over [400 - 1000] nm range



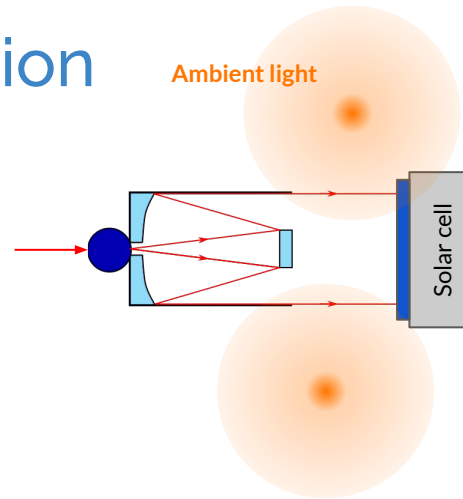
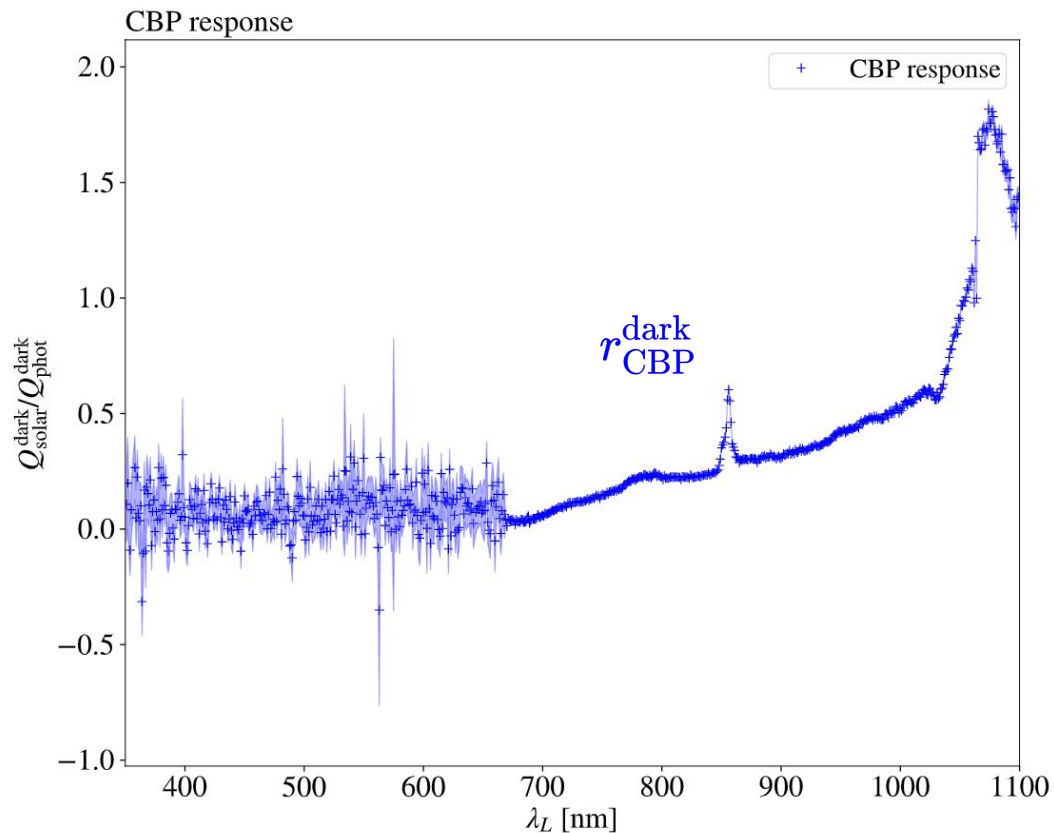


Quadrant positions





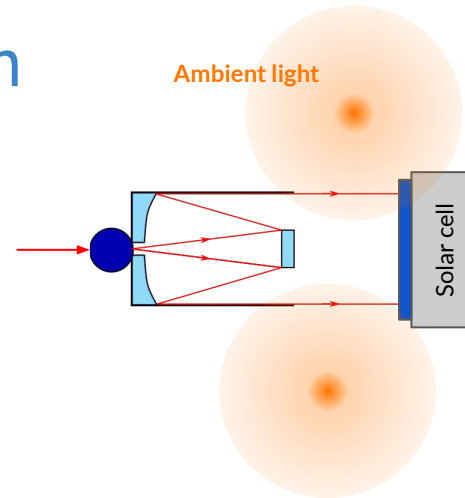
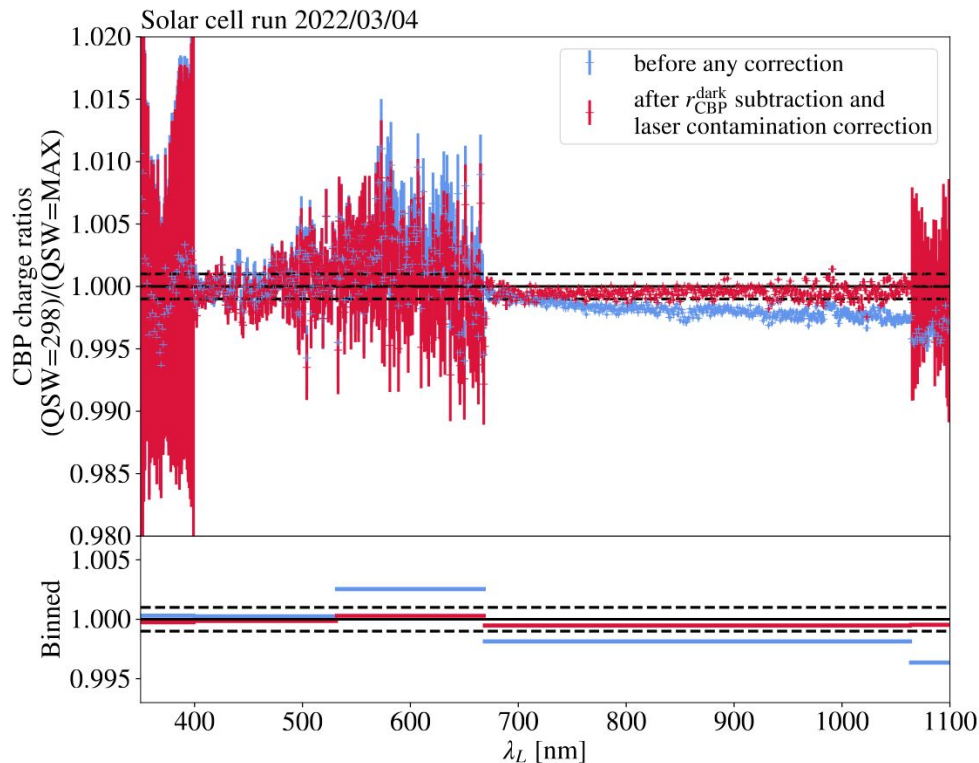
■ Ambient light contribution: presentation



Ambient light contamination depend
on wavelength \rightarrow laser box is not
perfectly light tight

$$Q_{\text{solar}}^{\text{cal}} = Q_{\text{solar}}^{\lambda_L} - r_{\text{CBP}}^{\text{dark}} \times Q_{\text{phot}}$$

Ambient light contribution: correction

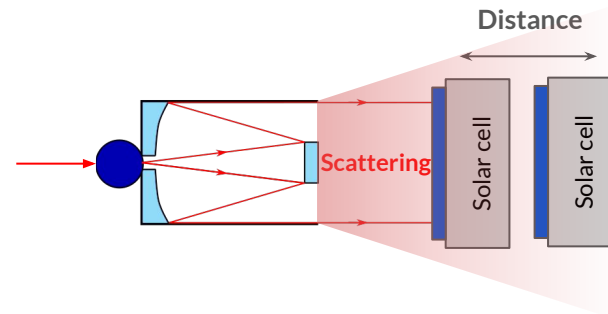
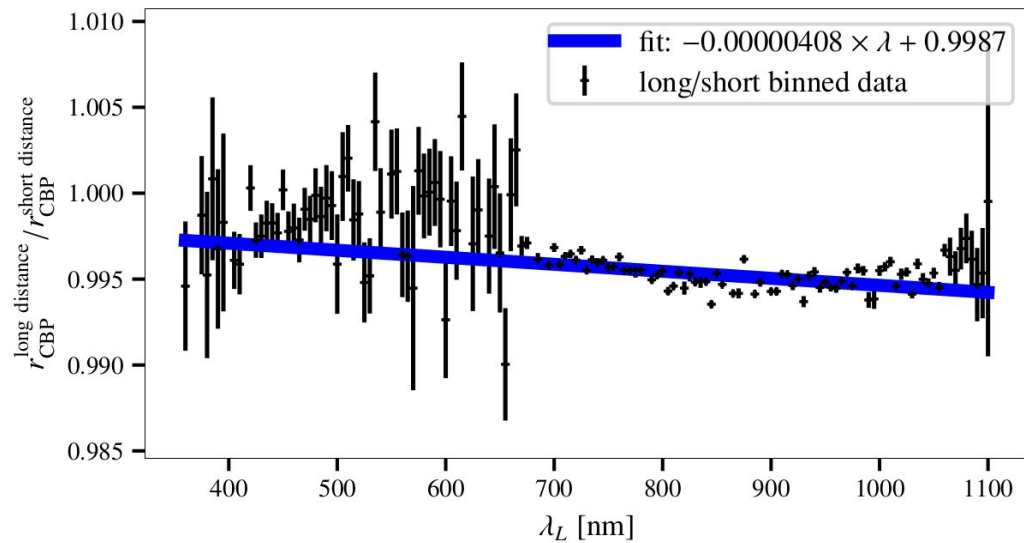


Ratio of two runs at different laser powers (different by a factor 2)

⇒ once corrected by the background, ratio contained below the per mil

$$Q_{\text{solar}}^{\text{cal}} = Q_{\text{solar}}^{\lambda_L} - r_{\text{CBP}}^{\text{dark}} \times Q_{\text{phot}}$$

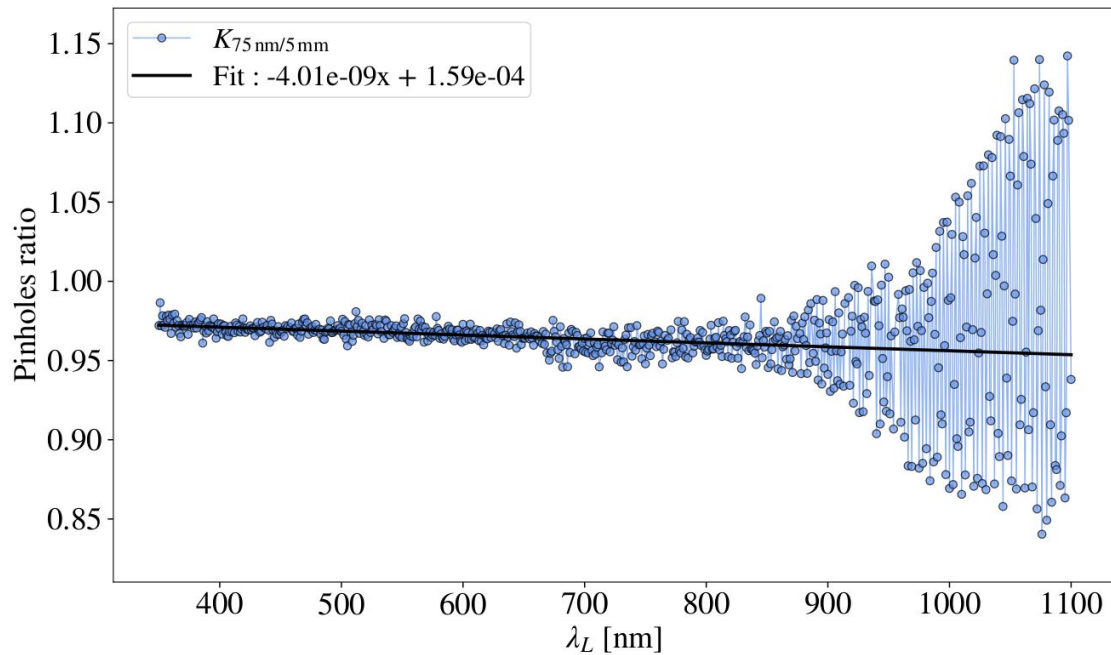
Scattered light



Ratio of two run at different distance
between the CBP and the Solar Cell
(~ 16cm)

- Decrease of 2.5‰ of light flux in [350 - 1100]nm
- Dominant systematics for CBP throughput

Intercalibration 5mm/75μm



$$K_{75\mu\text{m}/5\text{mm}}(\lambda) = \frac{R_{\text{CBP}}^{5\text{mm}}(\lambda)}{R_{\text{CBP}}^{75\mu\text{m}}(\lambda)} \quad \Rightarrow \quad \text{Infer } R_{\text{CBP}}^{75\mu\text{m}}(\lambda) \text{ from } R_{\text{CBP}}^{5\text{mm}}(\lambda)$$

Ghost contamination

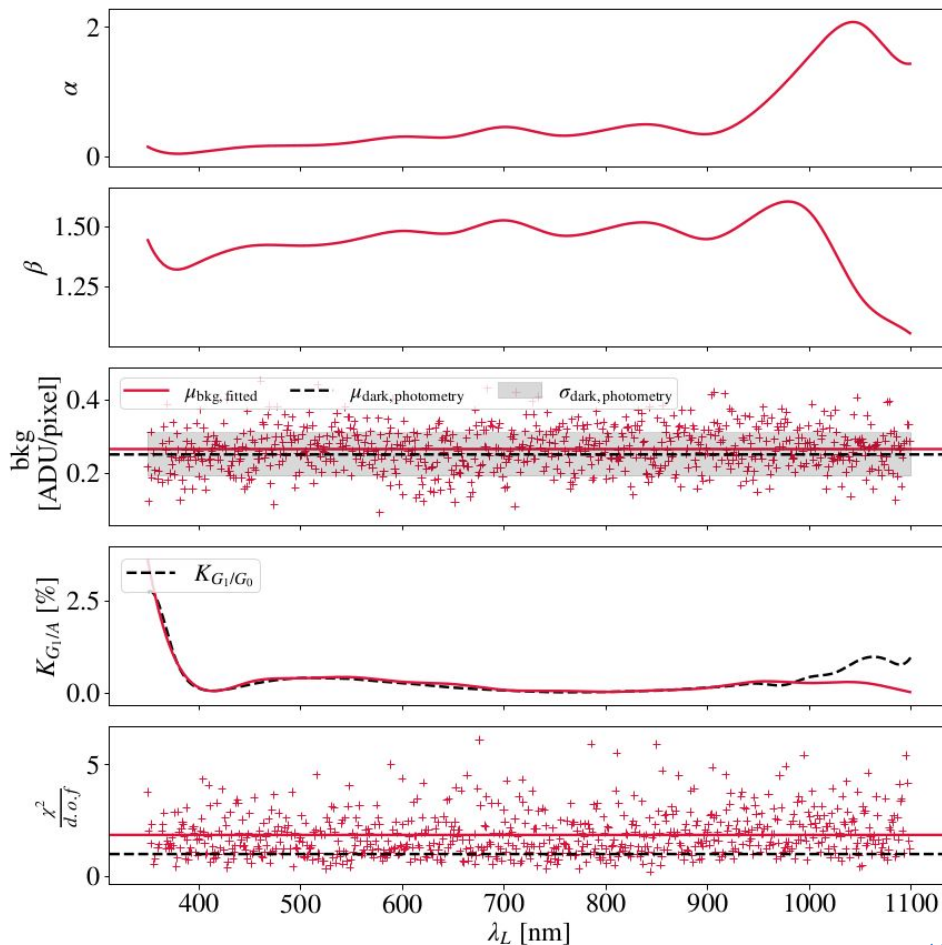
PSF fit with successive aperture photometry with radius r :

$$F(r, \lambda) = A(\lambda) \times \frac{\text{Moffat distribution } M(r, \lambda) + \text{Ghost contribution } K_{G/A}(r, \lambda)}{1 + K_{G/A}(+\infty, \lambda)} + \text{Background } \text{bkg}(\lambda) \times \pi r^2$$

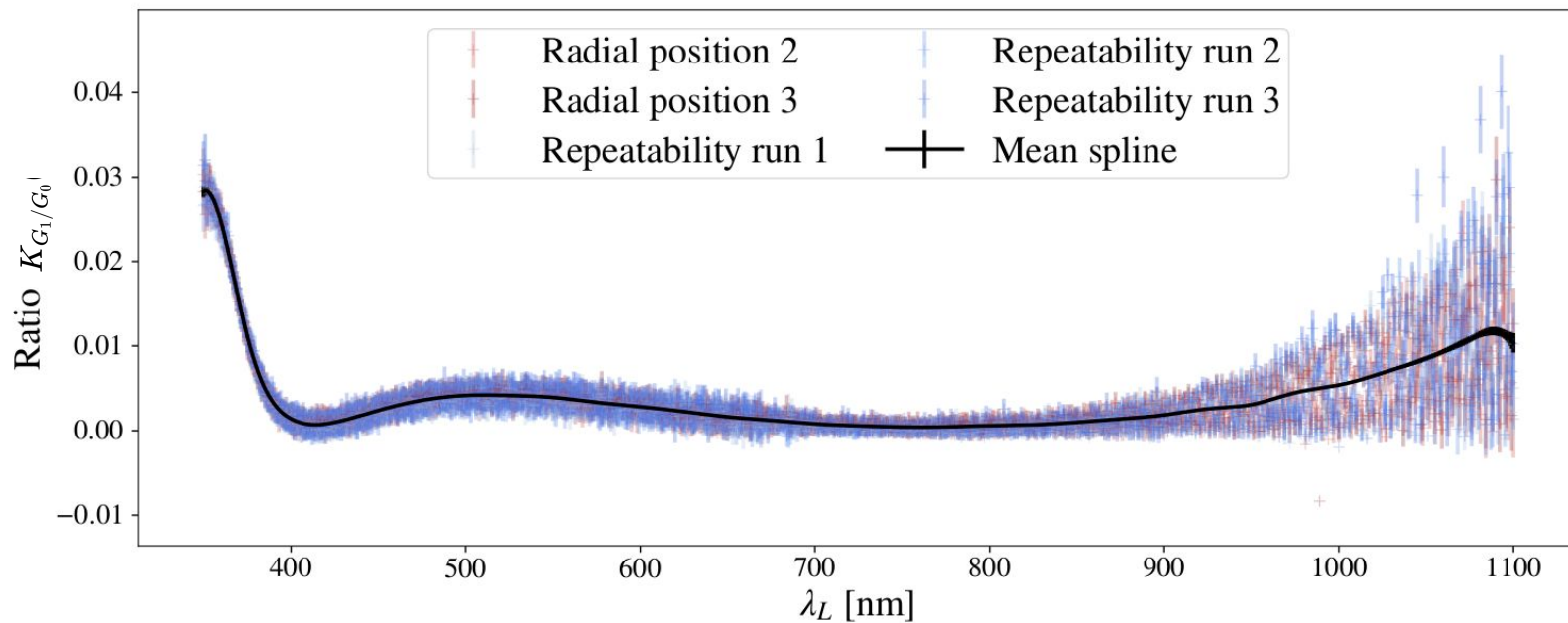
Fit results consistent with ghost photometry:

$$K_{G_1/G_0}(\lambda) = \frac{G_1(\lambda)}{G_0(\lambda)}$$

⇒ Ghost contribution well characterized with wavelength

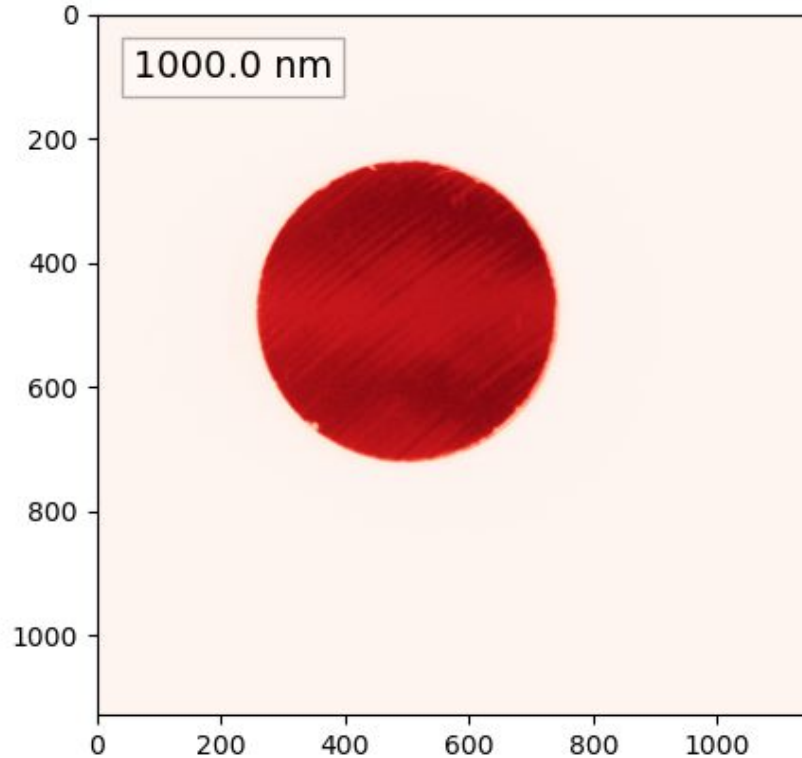


Ghost contamination in StarDICE

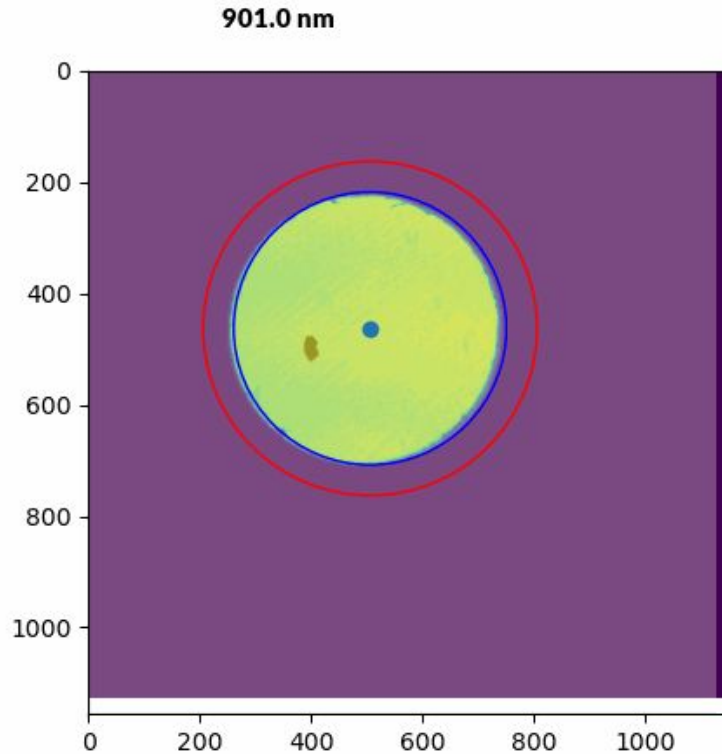


$$K_{G_1/G_0}(\lambda) = \frac{G_1(\lambda)}{G_0(\lambda)}$$

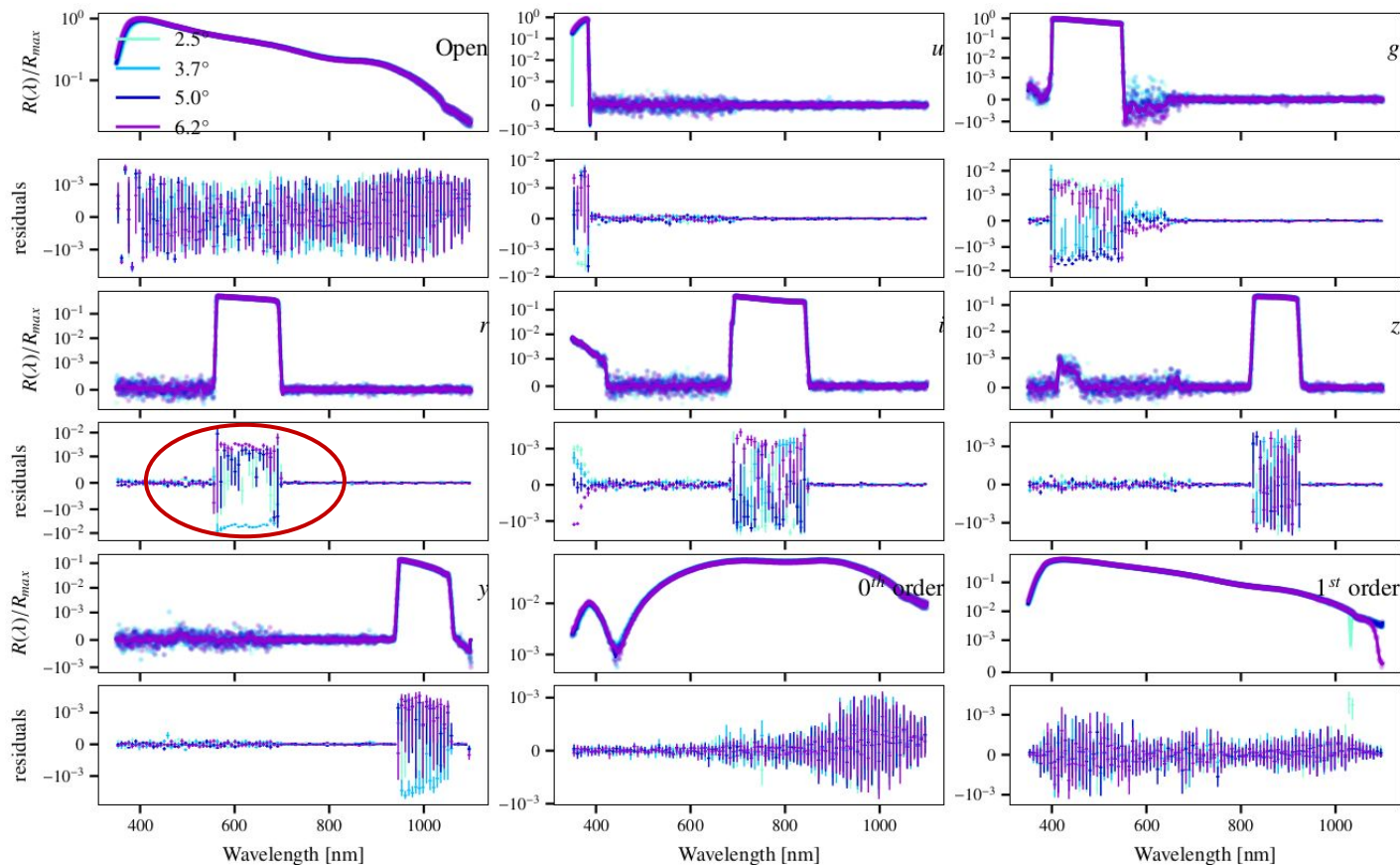
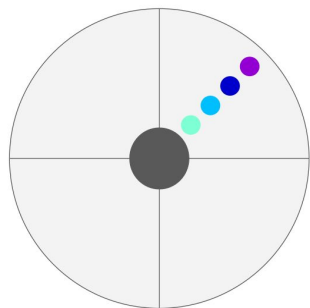
Fringing depending on position



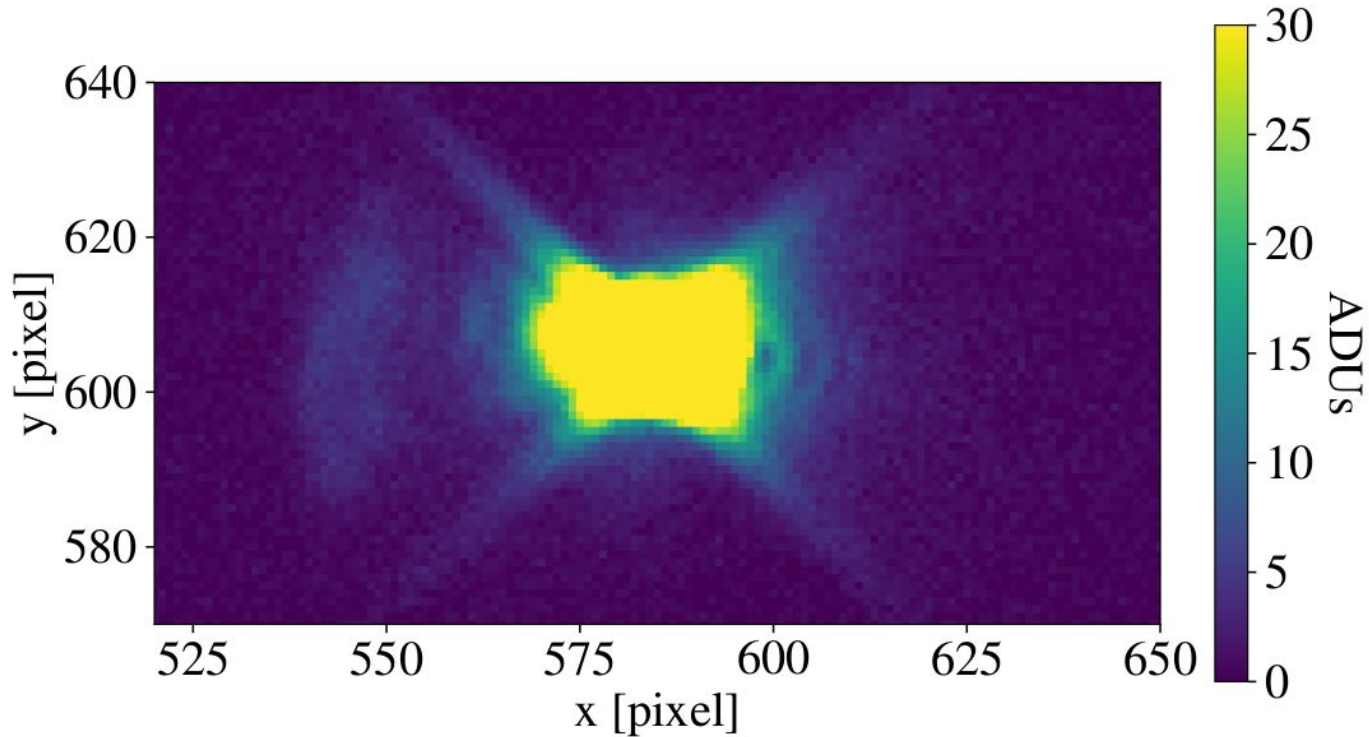
● Ghost photometry : IR oscillations



Pupil stitching

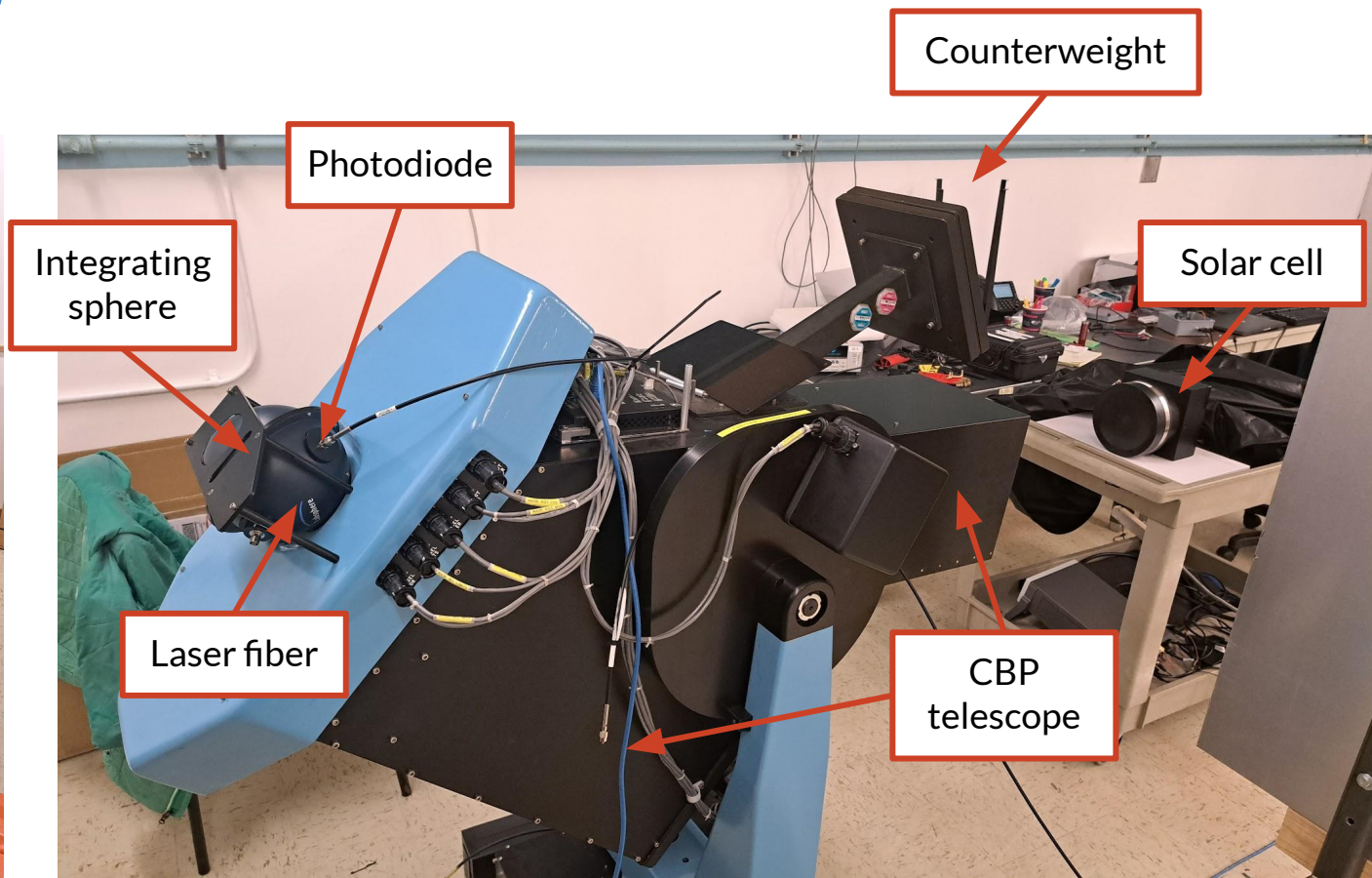
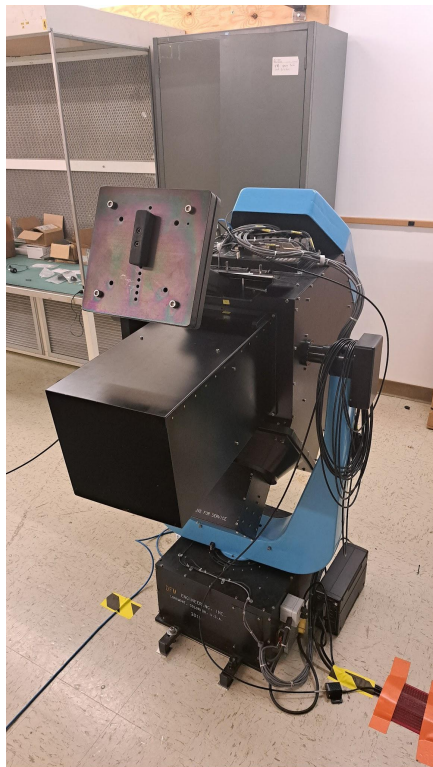


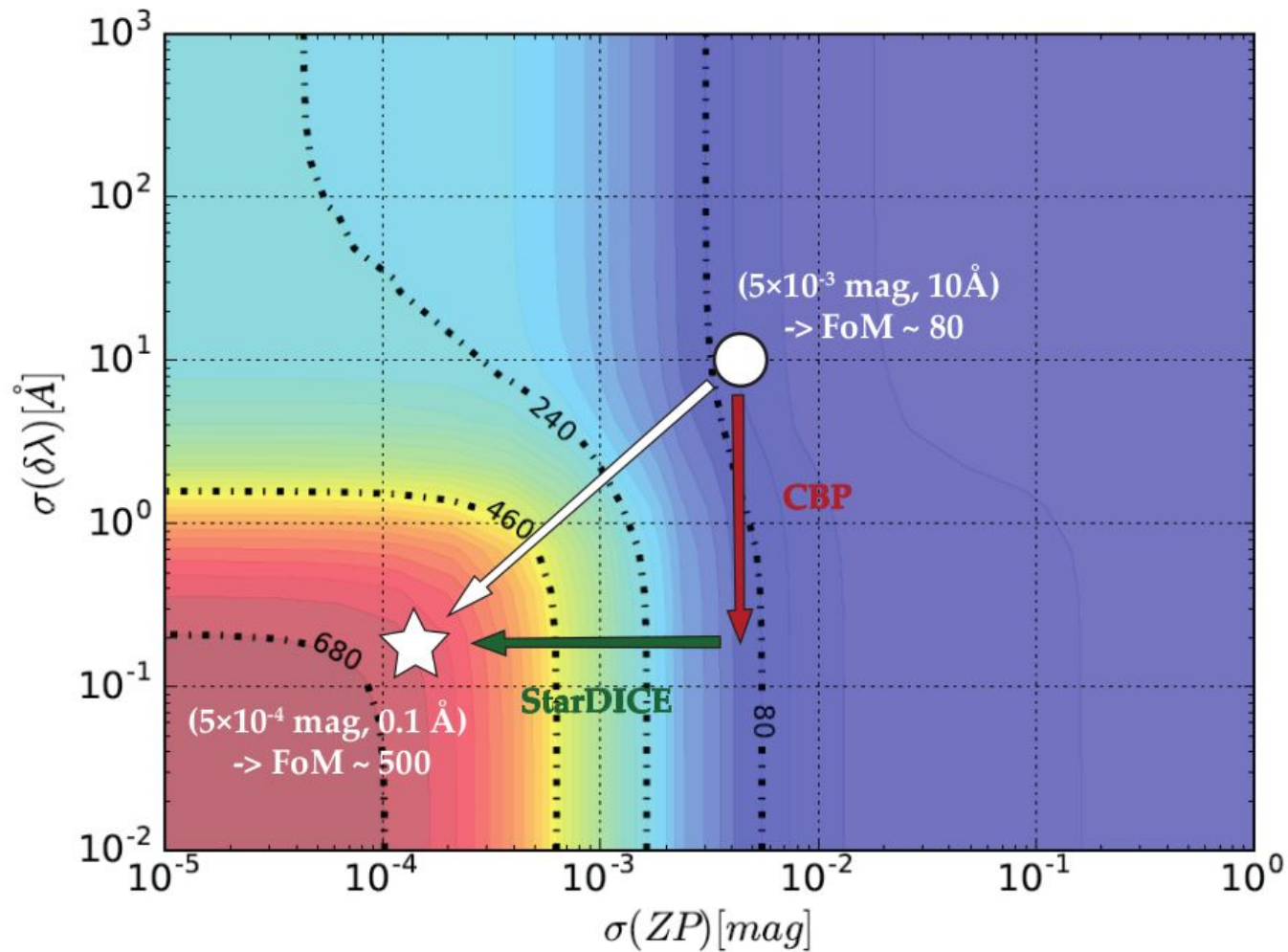
● Dust on the filter



Dust particle of about 200-300 μm diameter intercepting the CBP beam
 \Rightarrow consistent with the flux discrepancy

Rubin CBP



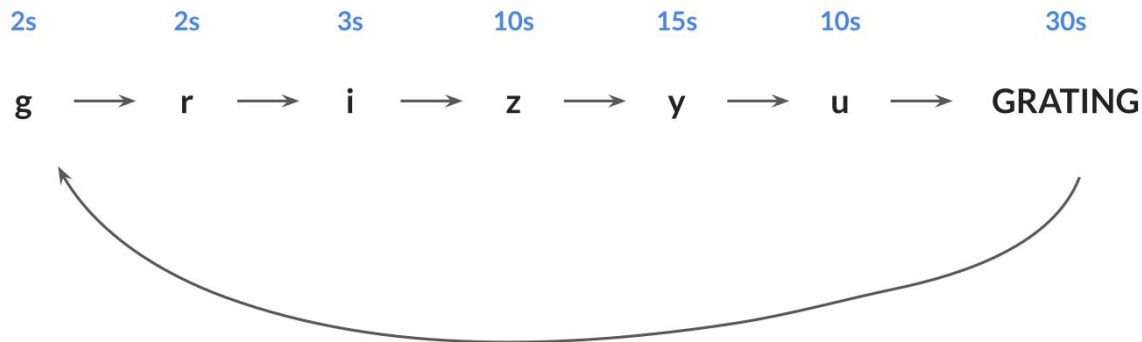


Photometry

Dataset description

Follow-up of the CALSPEC primary standard G191B2B

- 23 observation nights
- ~3000 images by filter → total of ~20 000 images
- Observations in “ugrizy” filters + “grating”
- ~800 stars studied in the field



Fitting zero points

Fit initialization for every star s in every image i :

$$\Delta \hat{m}_{i,s} = m_{i,s}^{\text{obs}} - m_{i,s}^{\text{synth}} = -2.5 \times \log_{10} \left(\frac{F_{i,s}^{\text{obs}}}{F_{i,s}^{\text{synth}}} \right)$$

Magnitude variation model:

$$\Delta m_{i,s} = \Delta ZP_i + \Delta m_s + \epsilon_{i,s}$$

Diagram labels for the magnitude variation model equation:

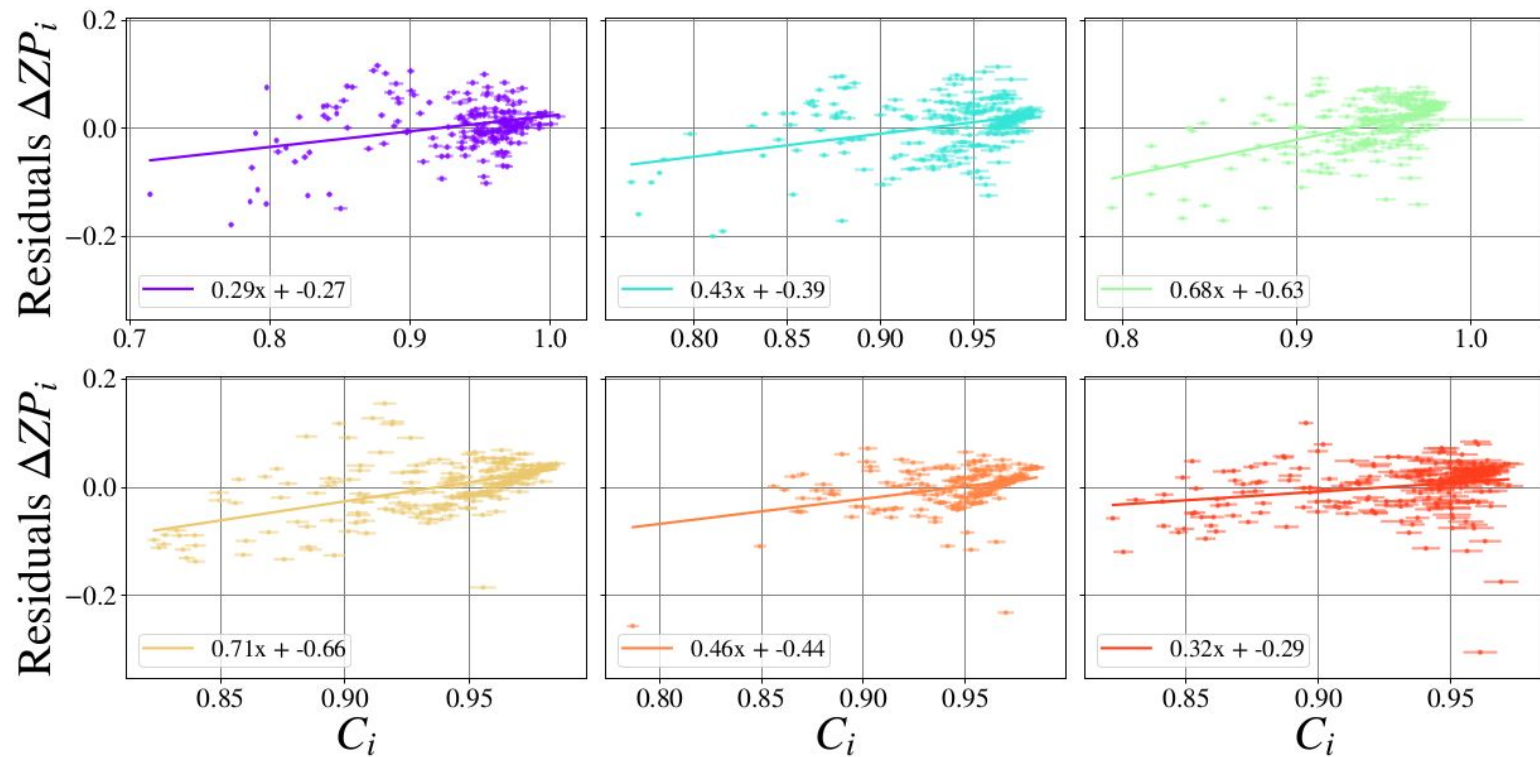
- Image variations (points to ΔZP_i)
- Average offset synth/obs (points to Δm_s)
- Variance model (points to $\epsilon_{i,s}$)

Zero point model per band:

$$\Delta ZP_{b,i}(X, C) = k_b X_i + \alpha_b C_i + ZP_{0,b}$$

Diagram labels for the zero point model equation:

- Atmosphere (points to k_b)
- Aperture photometry (points to α_b)
- Out-of-atmosphere zero point (points to $ZP_{0,b}$)



$\Delta m_{i,s} = \text{fit_init}(F_{is}^{\text{obs}}, F_{is}^{\text{synth}})$

$\sigma_F = \text{vect}(1)$

$\Delta m_s = \text{vect}(0)$

for p in range(N_p)

for q in range(N_q):

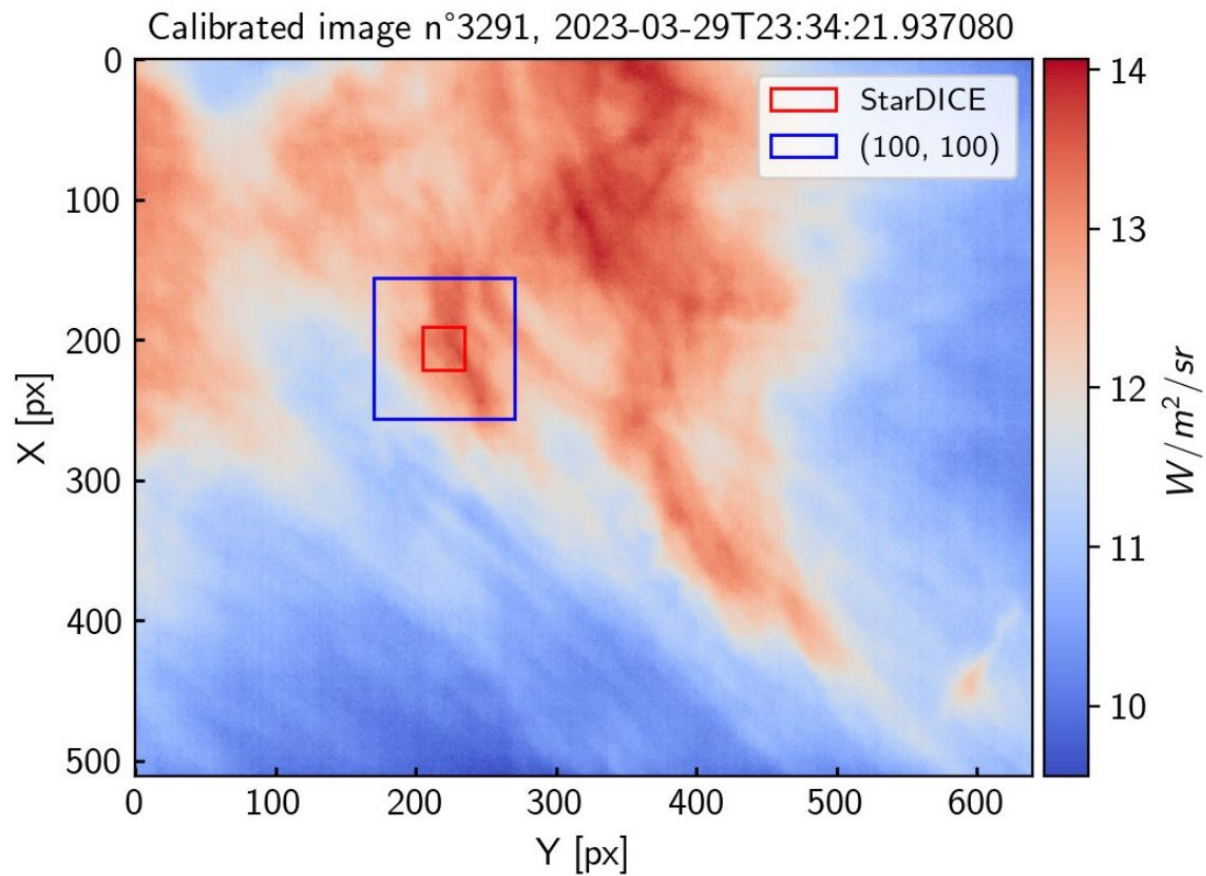
$\Delta ZP_i, \Delta m_s = \text{mag_variation_model}(\Delta m_{i,s}, \Delta m_s, \sigma_F)$

$r_{i,s} = \Delta m_{i,s} - (\Delta ZP_i + \Delta m_s)$

$\sigma_F = \text{error_model_variance}(r_{i,s})$

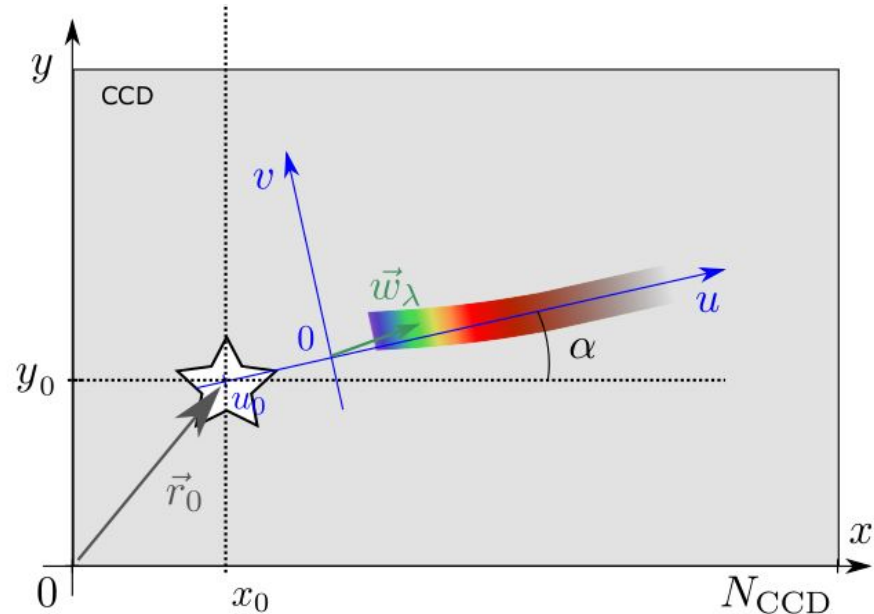
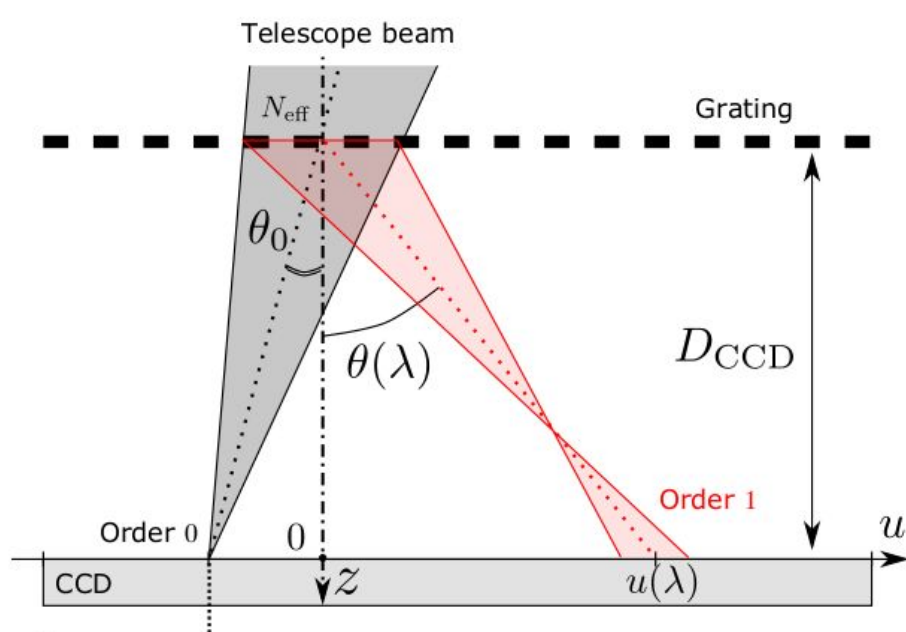
$k_b, ZP_{0,b}, \alpha_b = \text{zero_point_model}(\Delta ZP_i, X_i, C_i)$

● Infrared image

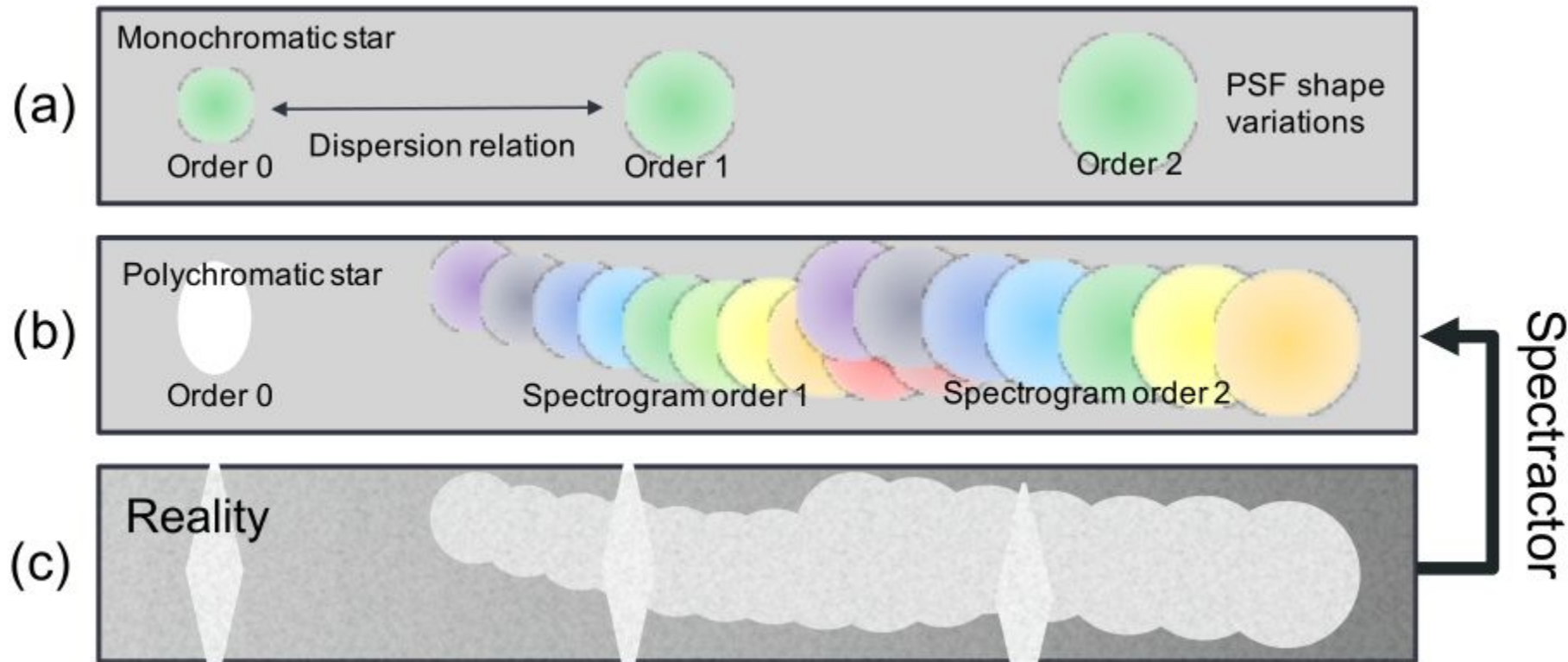


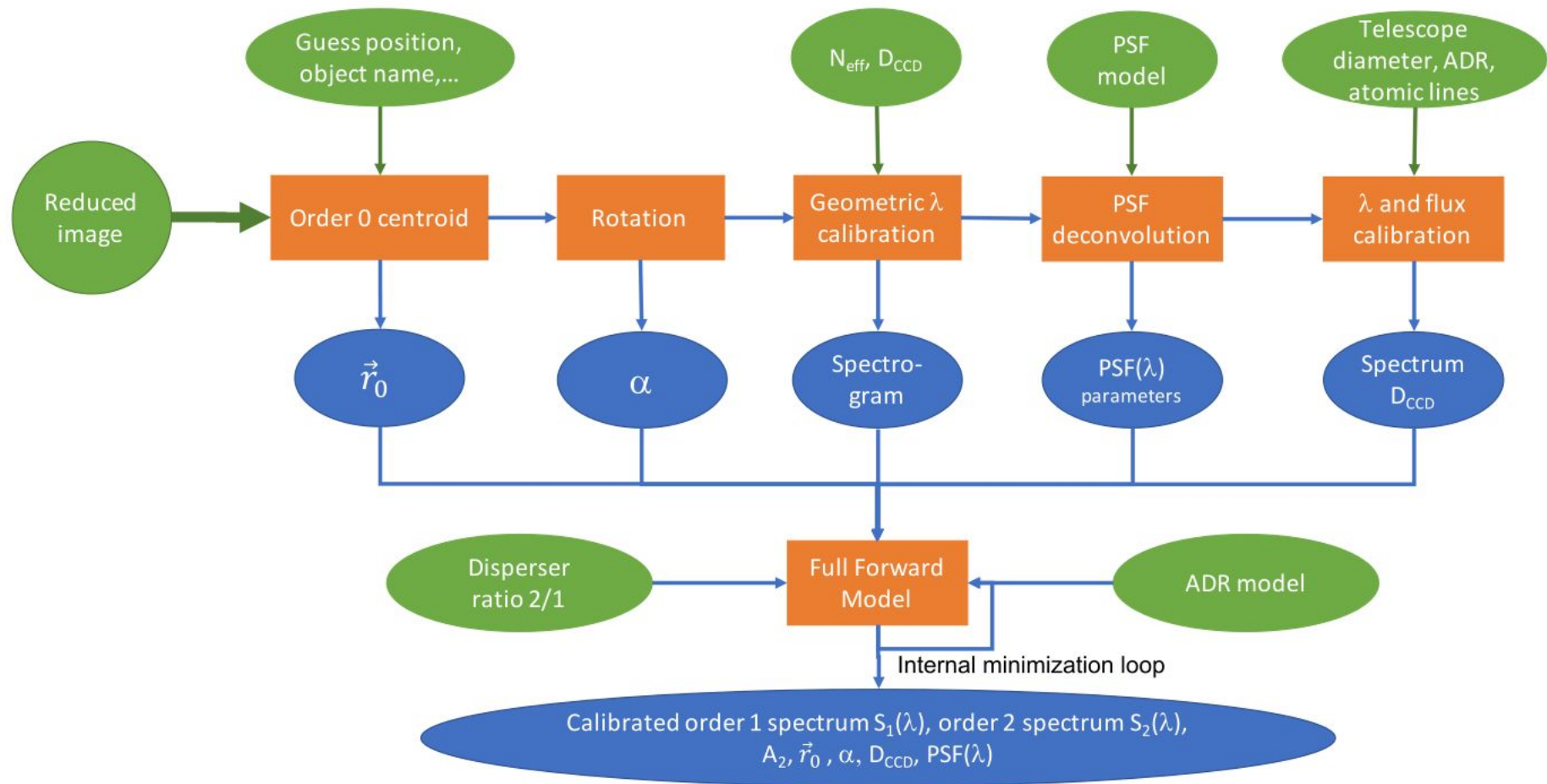
Spectrophotometry

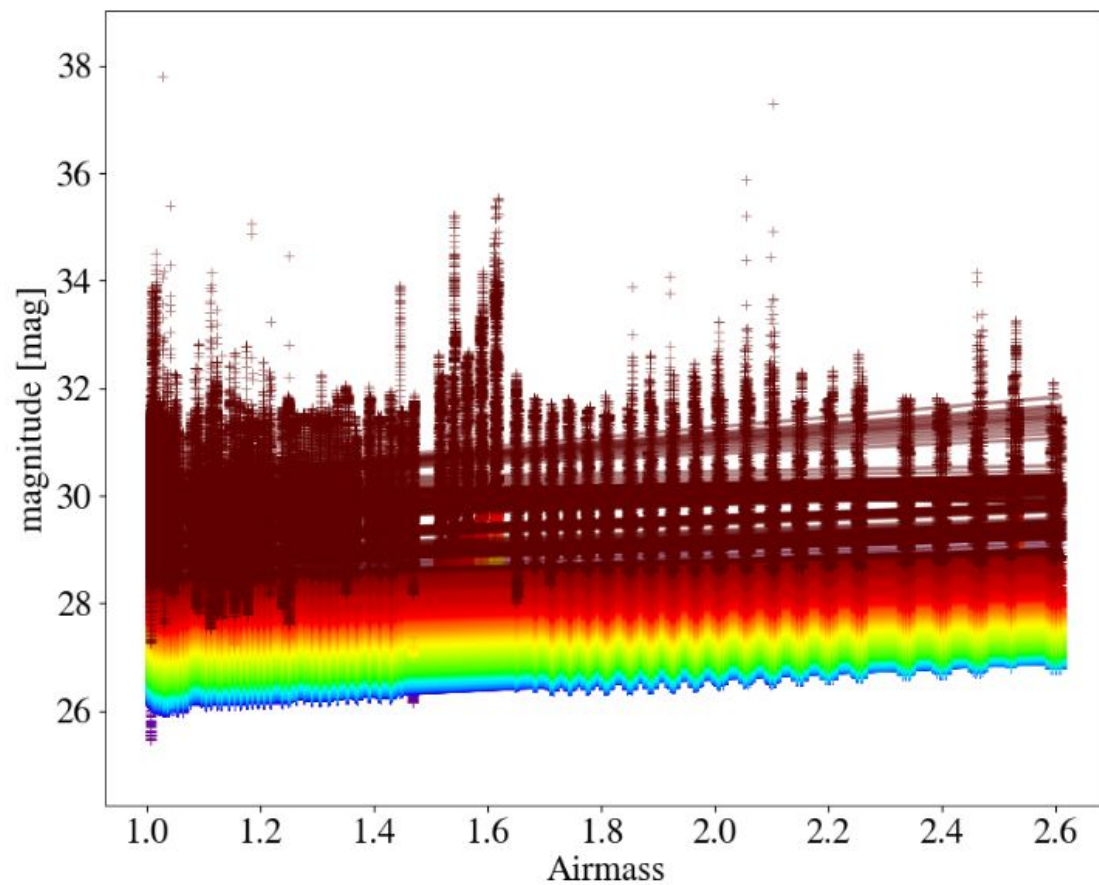
Grating dispersion



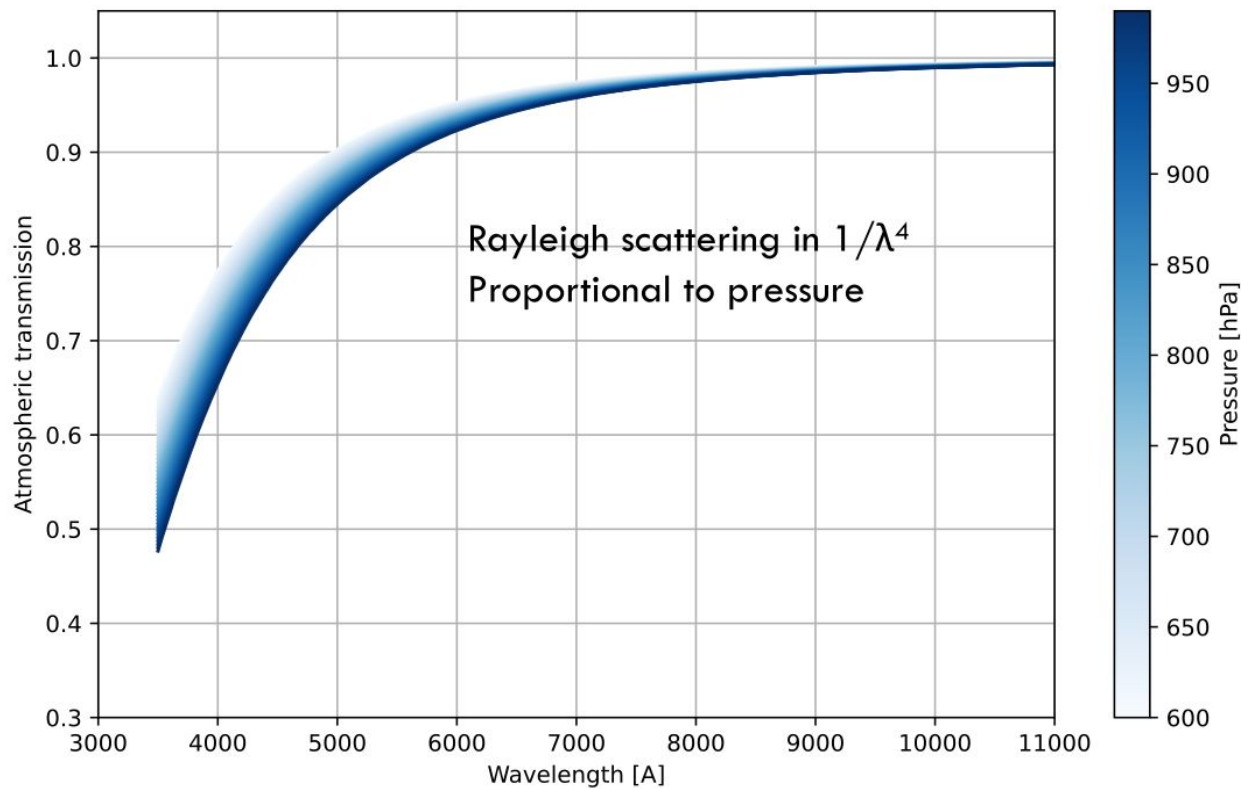
⇒ Disperse the light of the entire field of view on the camera



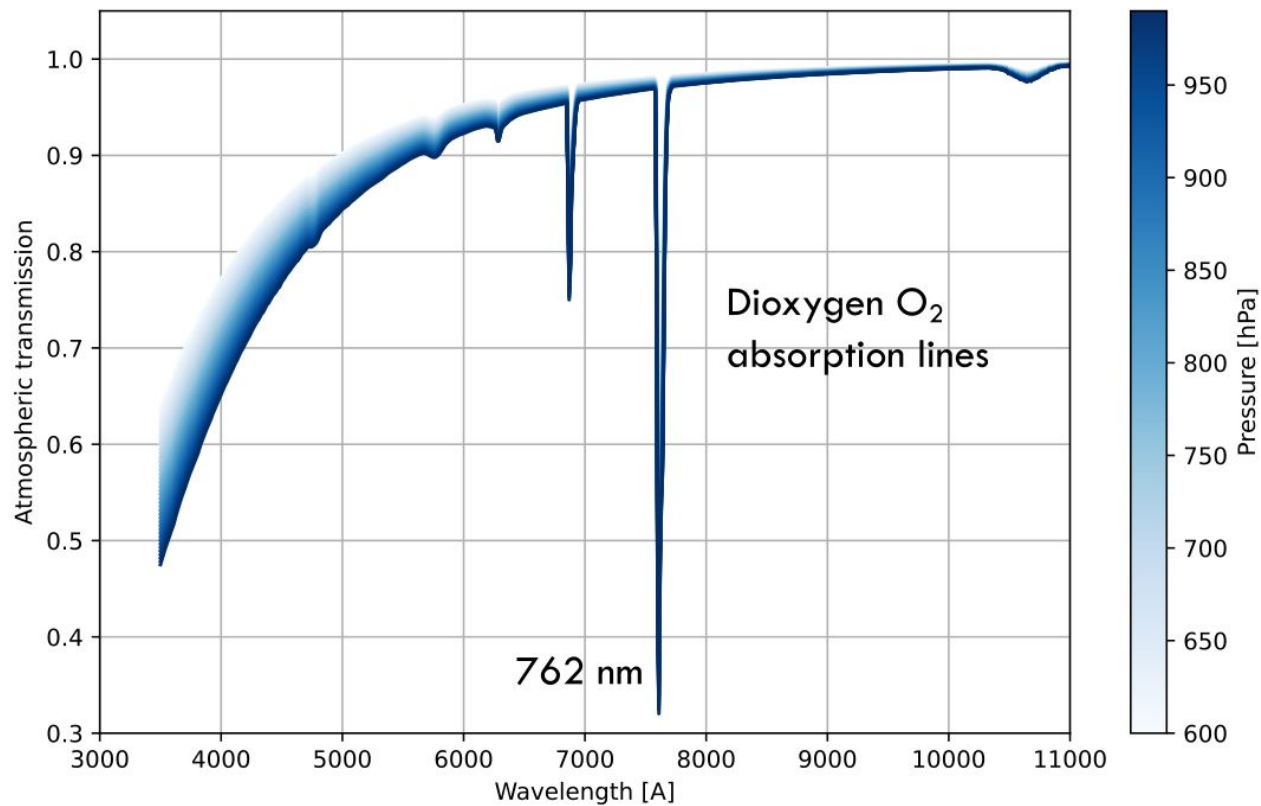




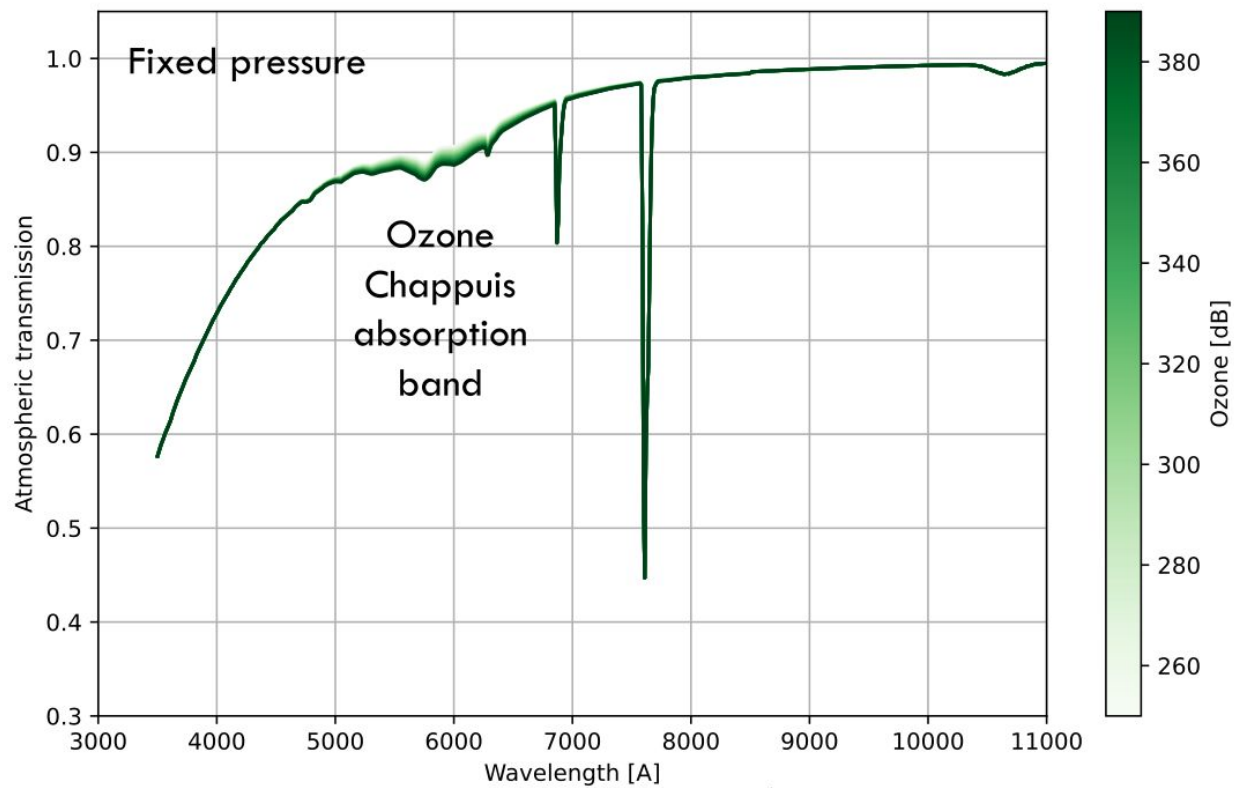
(1)



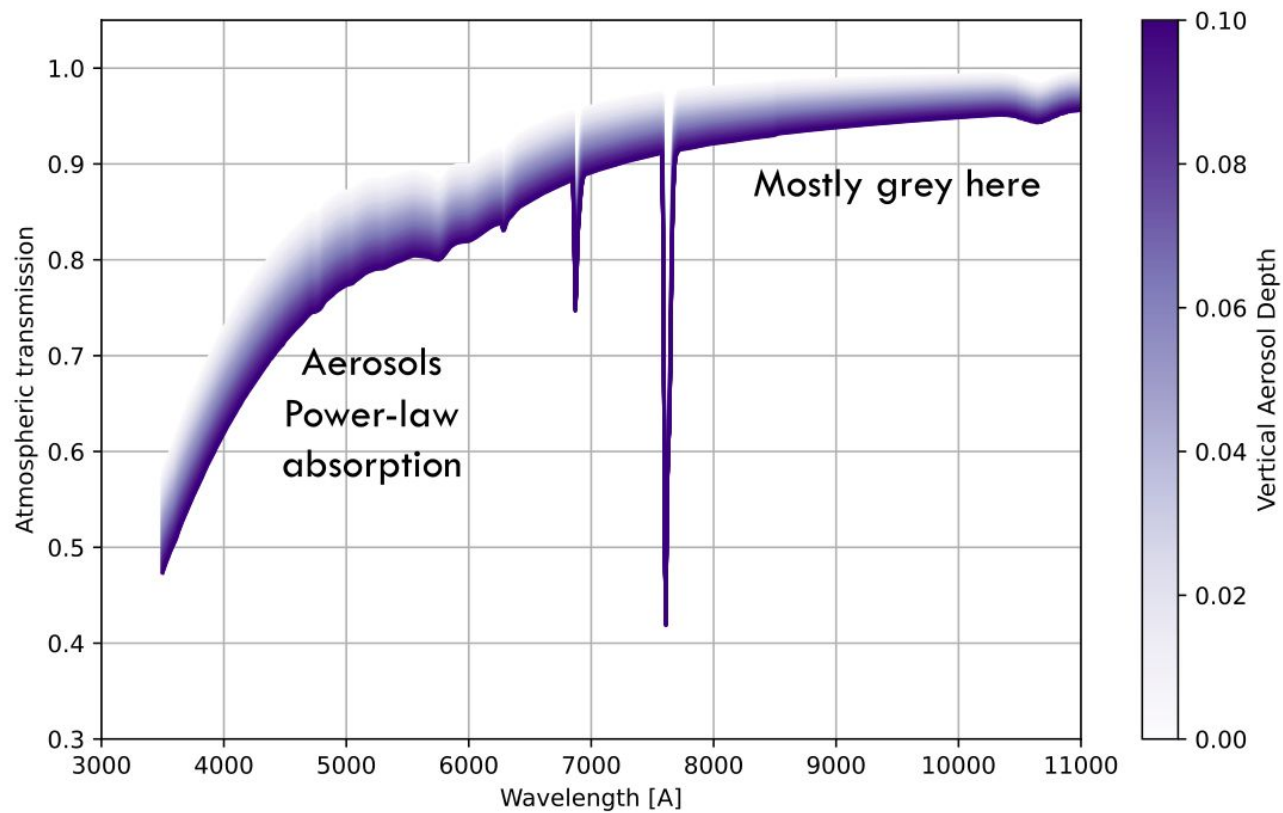
(2)



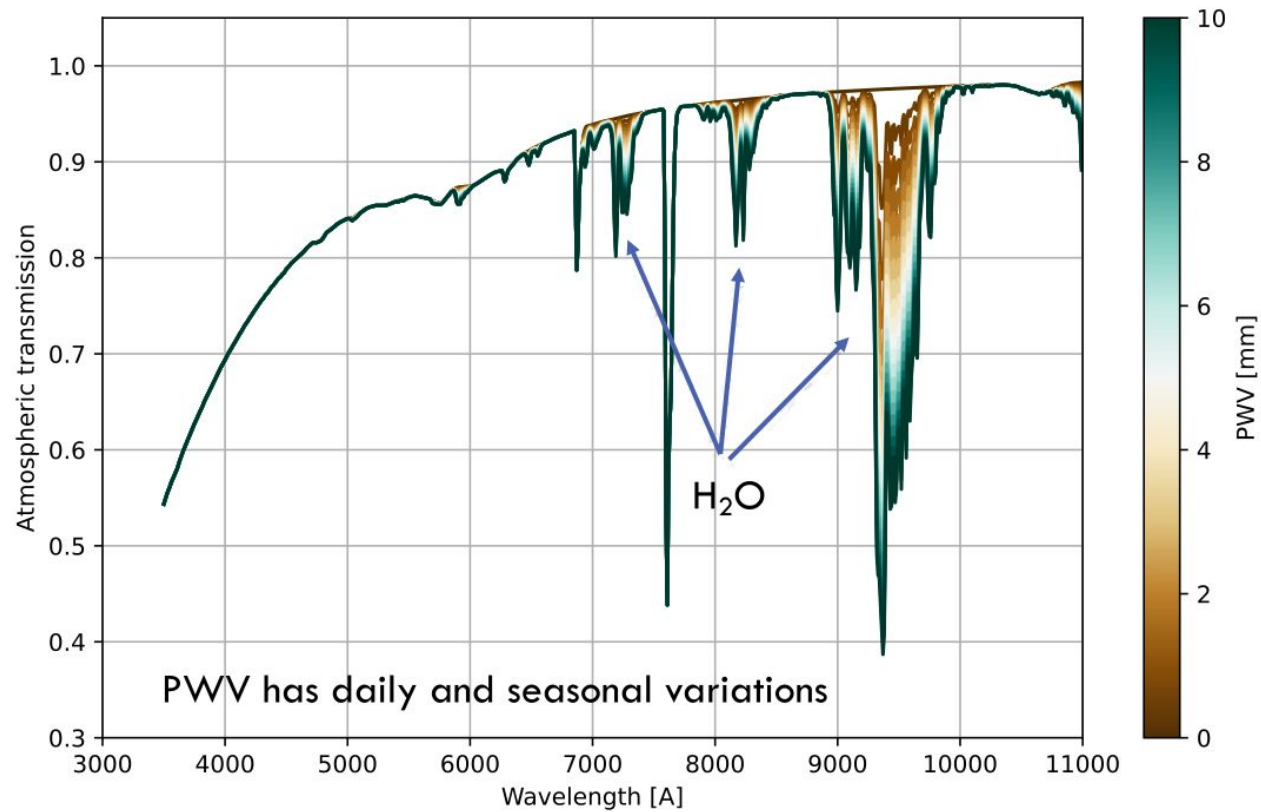
(3)

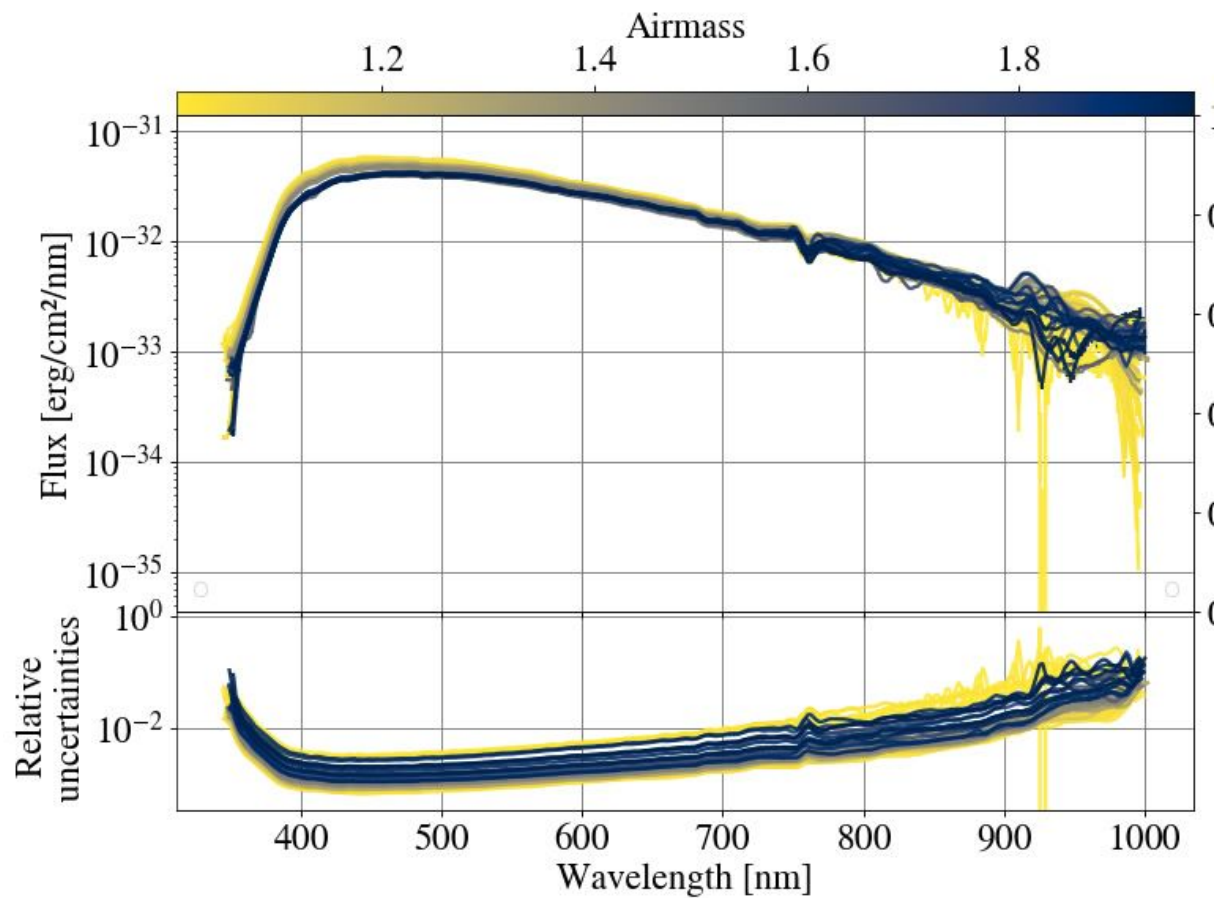


(4)



(5)





Field simulation

