

Astrophysical Searches for Quantum Gravity: what multi-messenger observations can (and cannot) tell us

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BridgeQG Workshop
Annecy, February 4-6 2026

what if there are already QG signatures in the data?

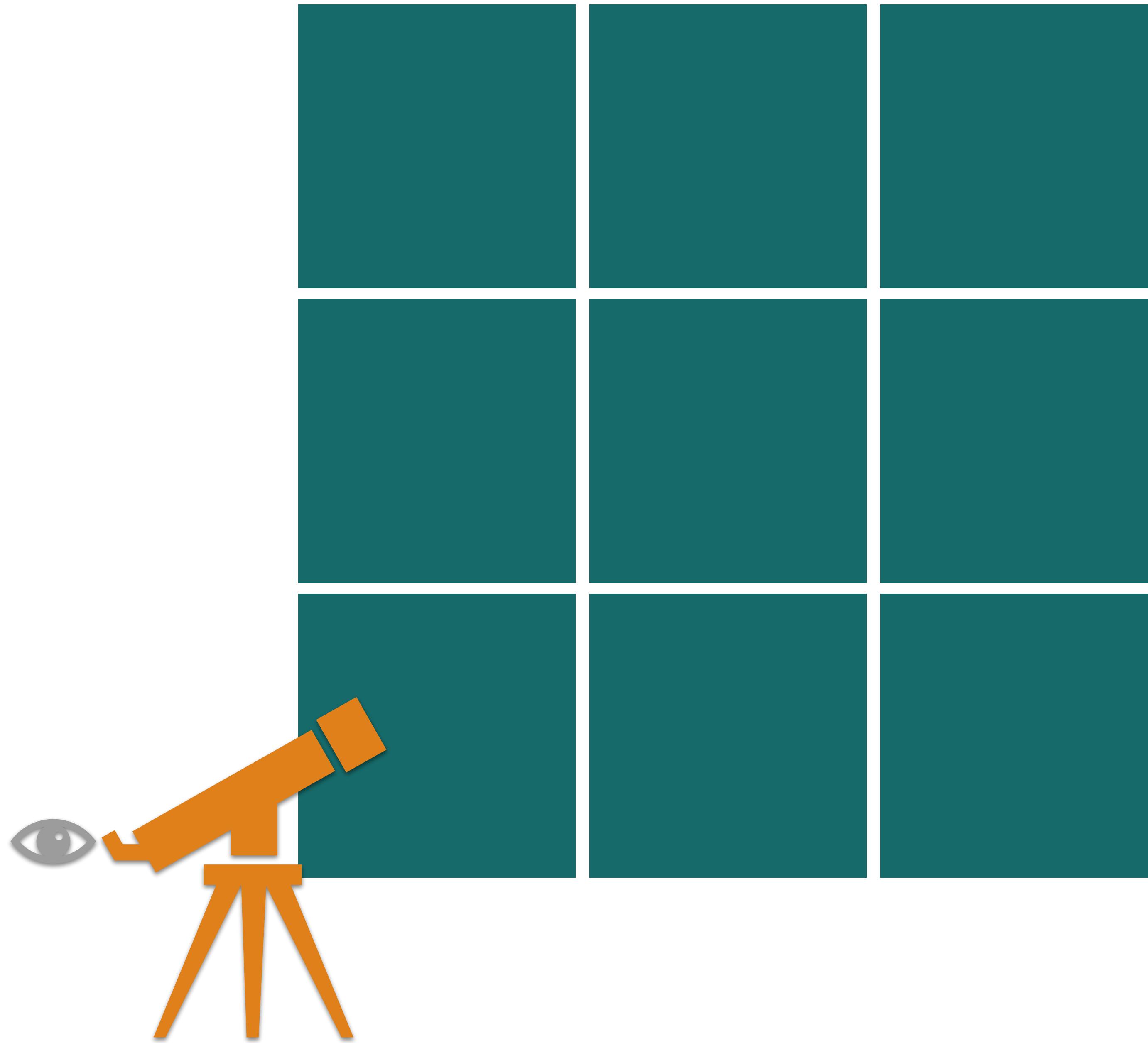
what if there are already QG signatures in the data?

would we be able to tell?

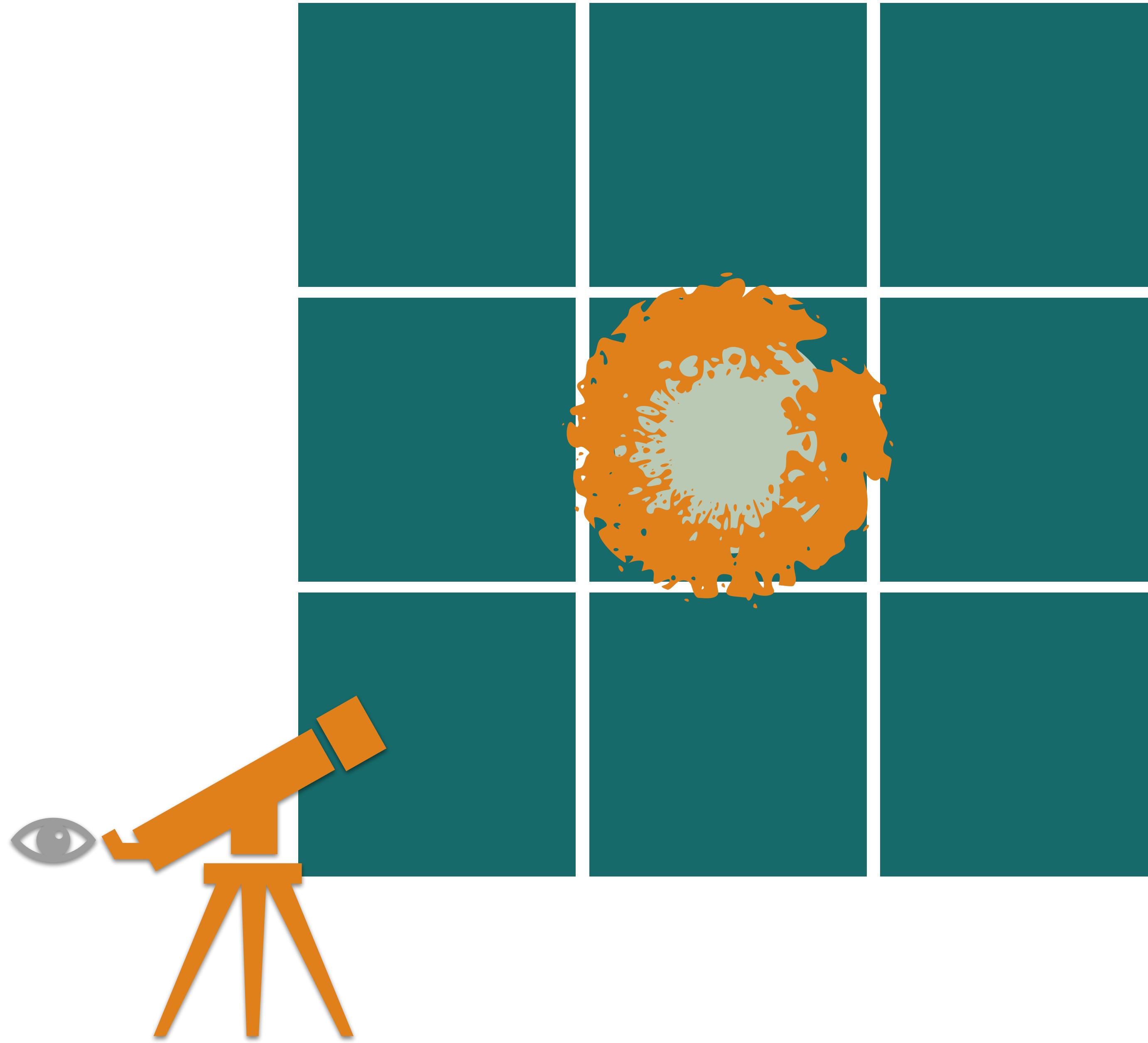
what do we observe?



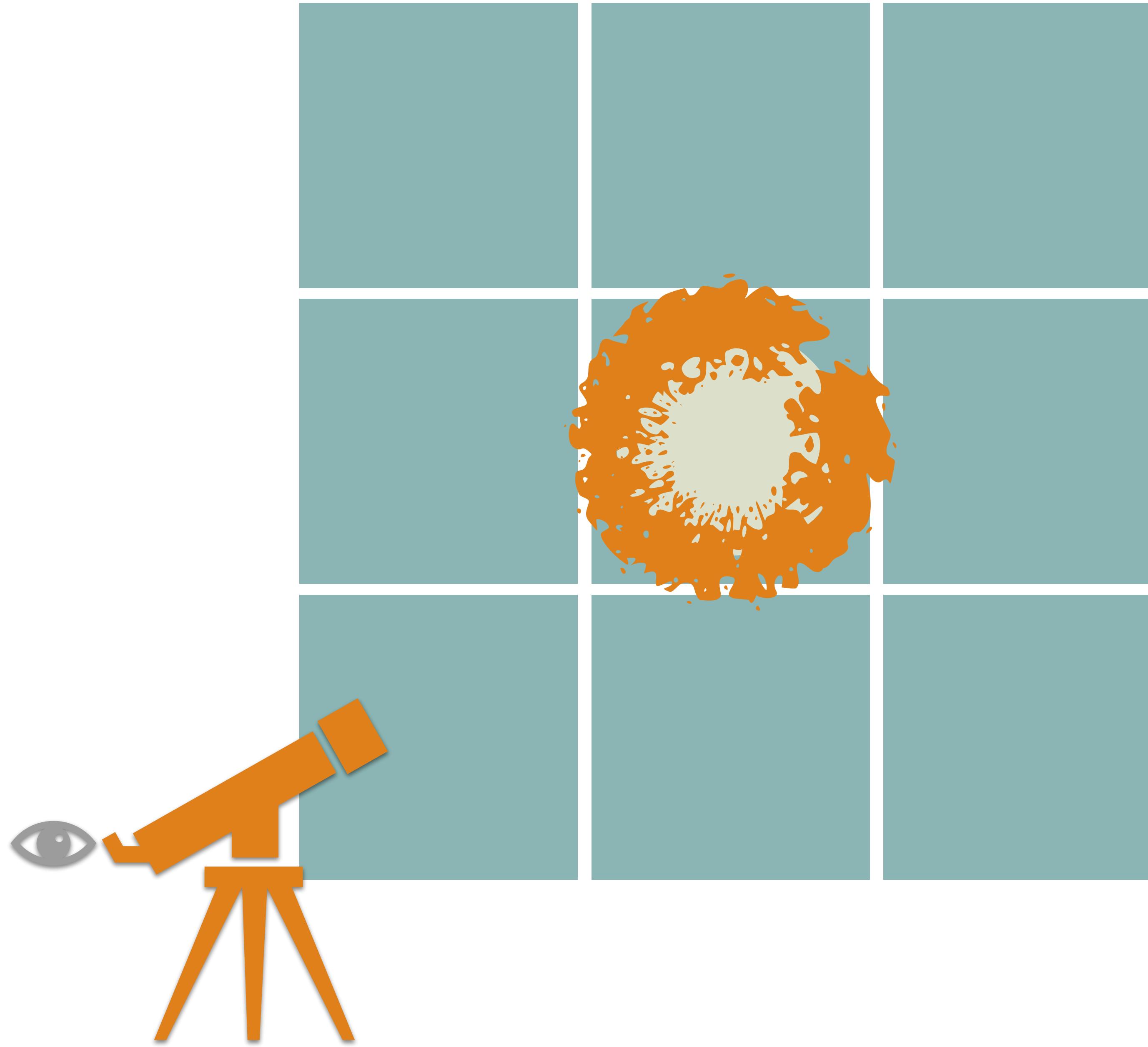
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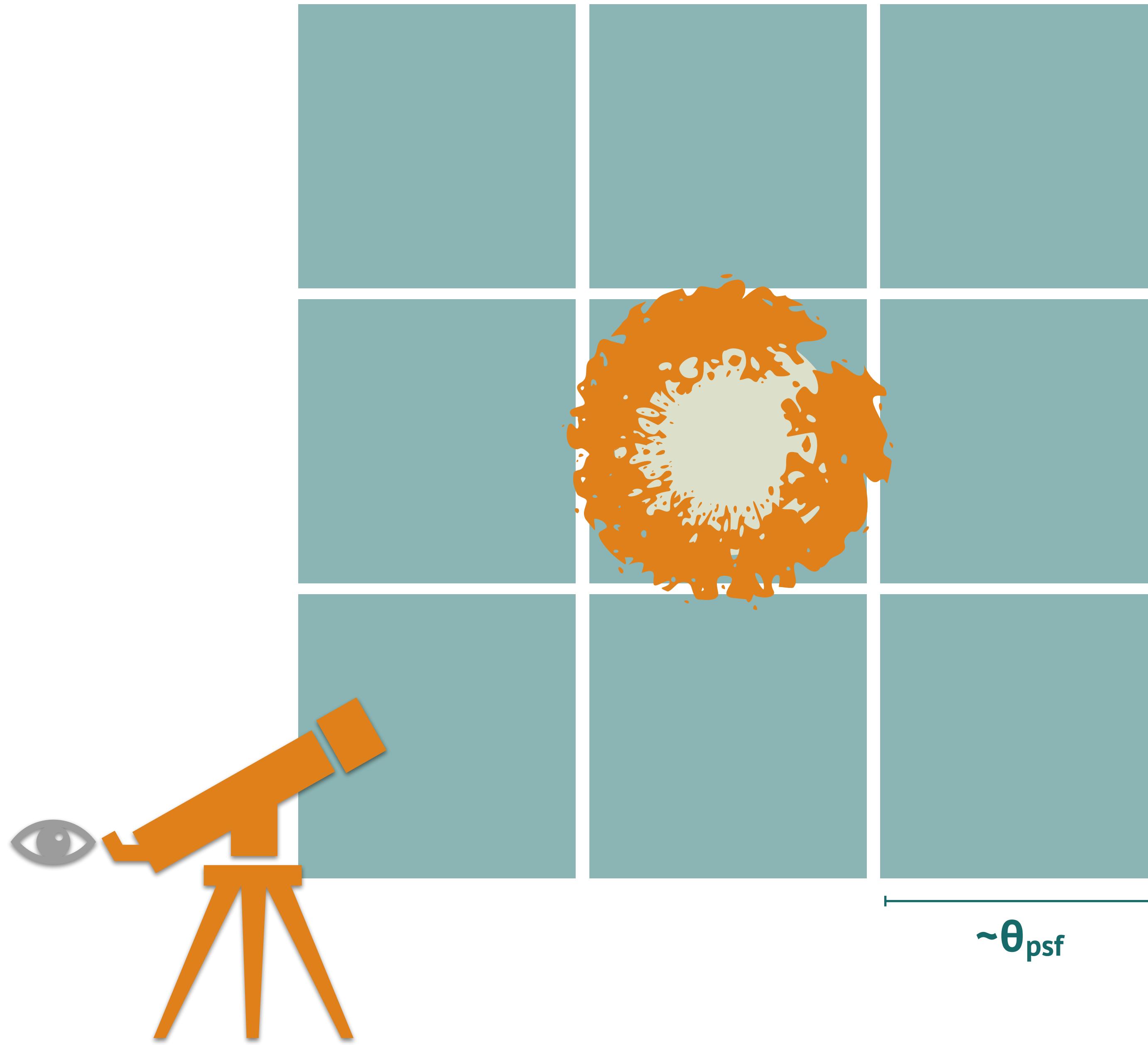
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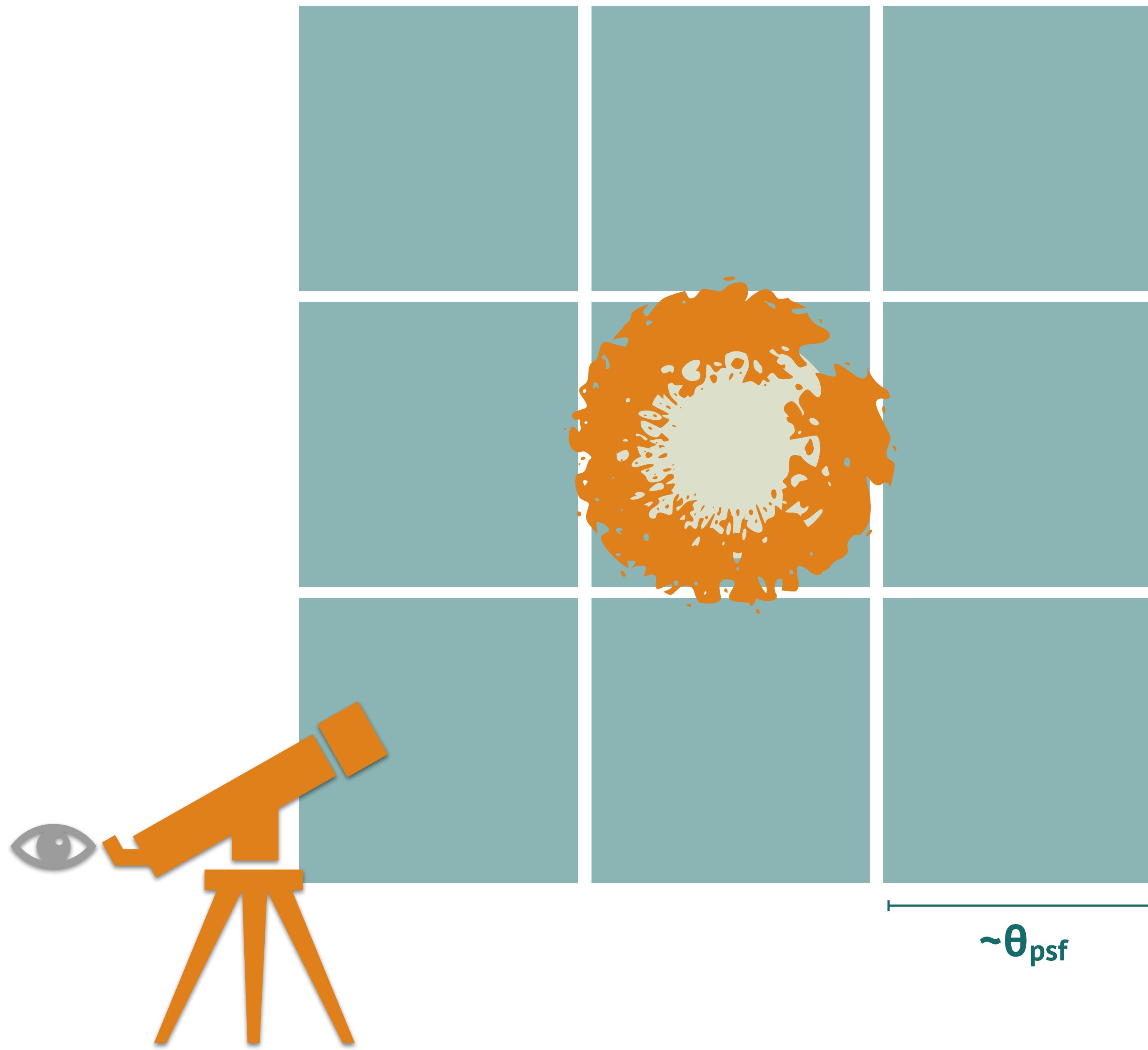
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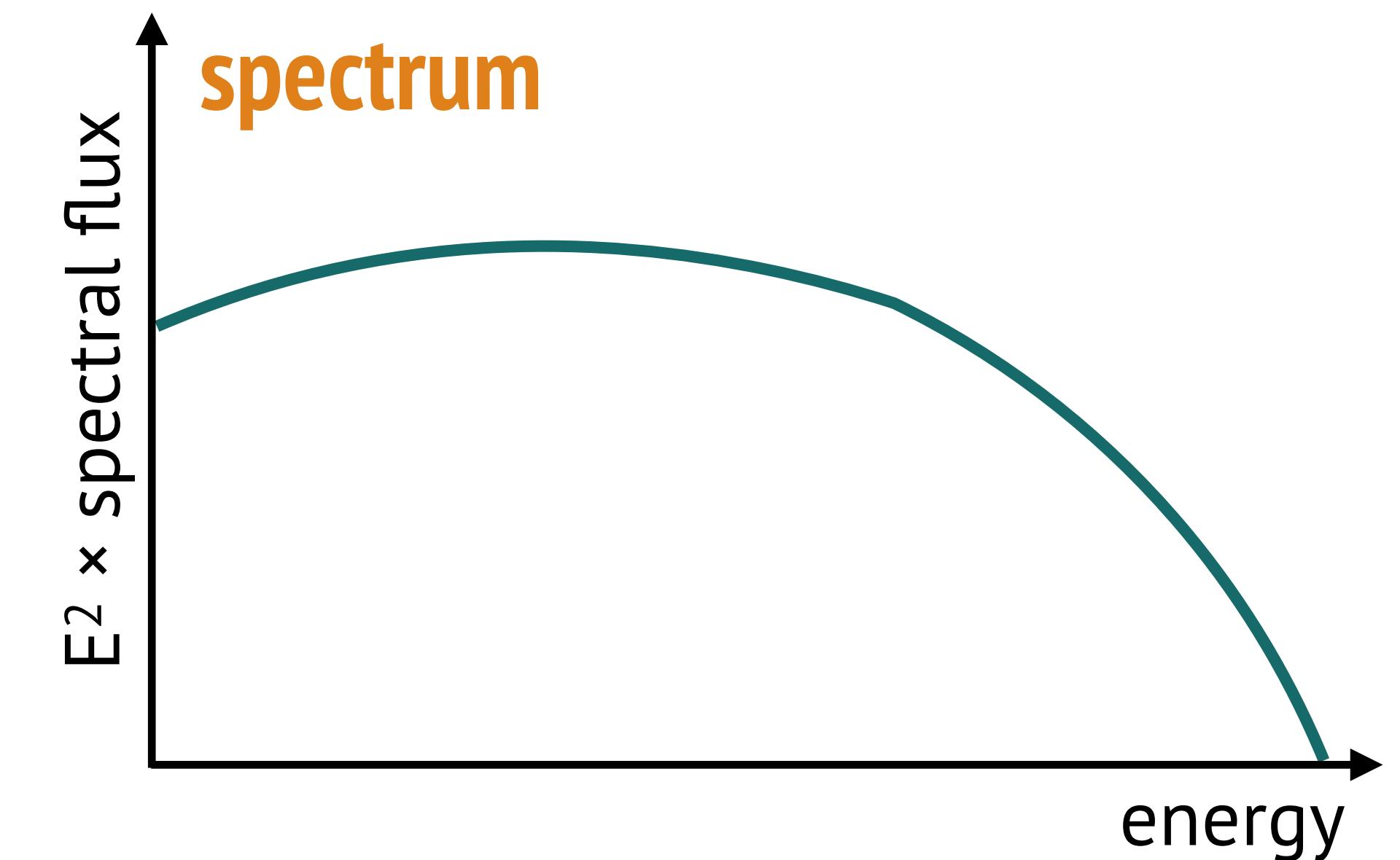
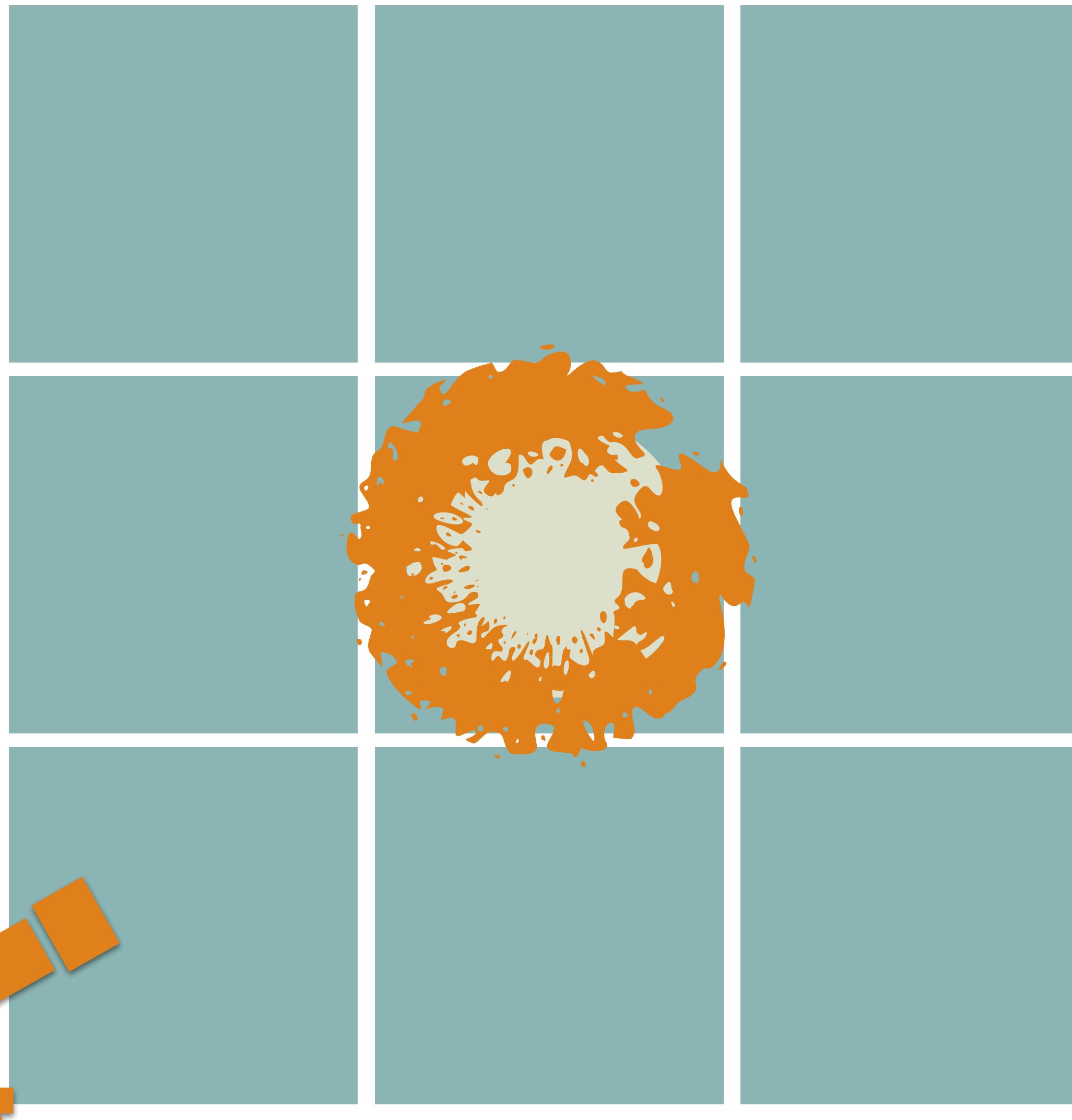
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arrival directions

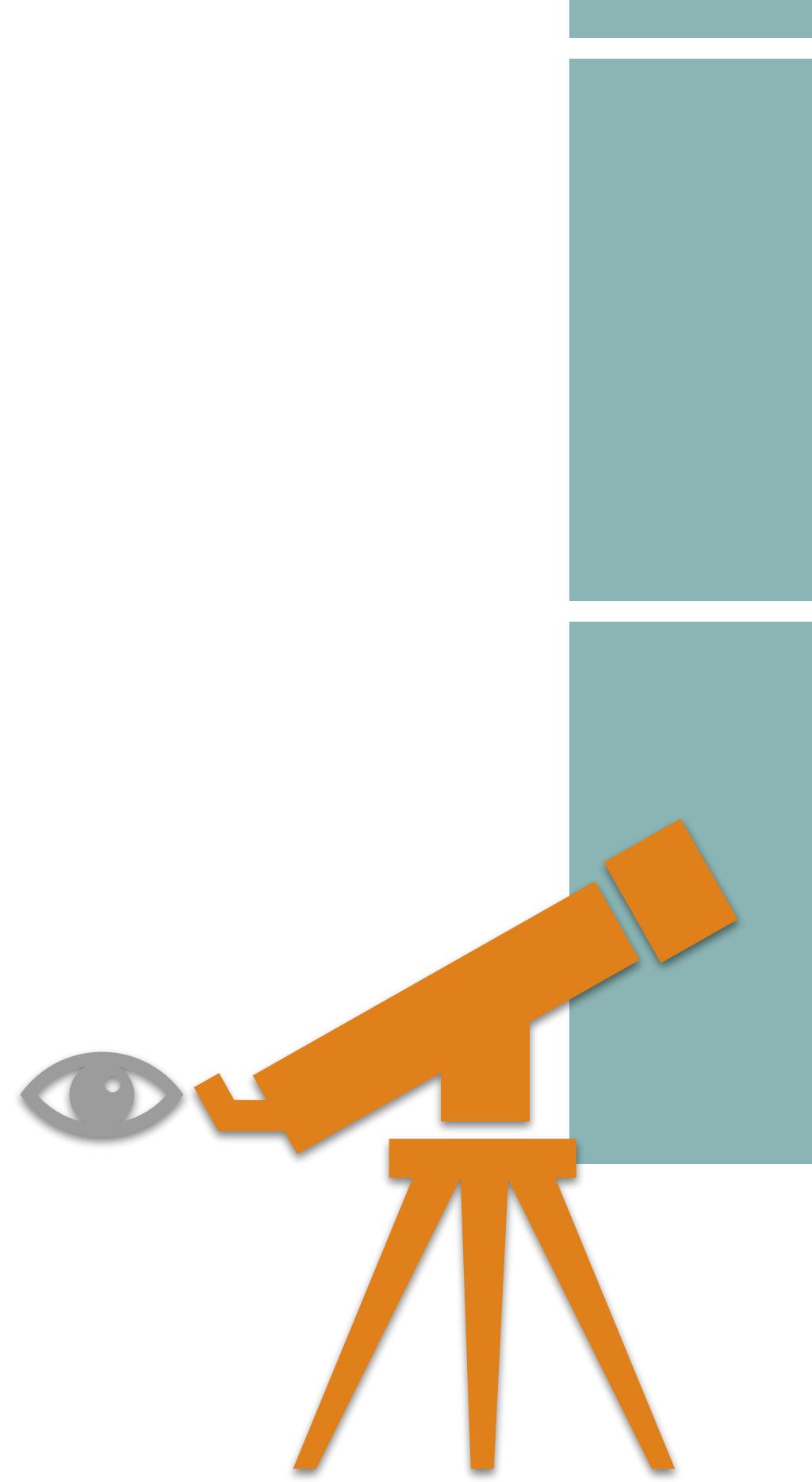


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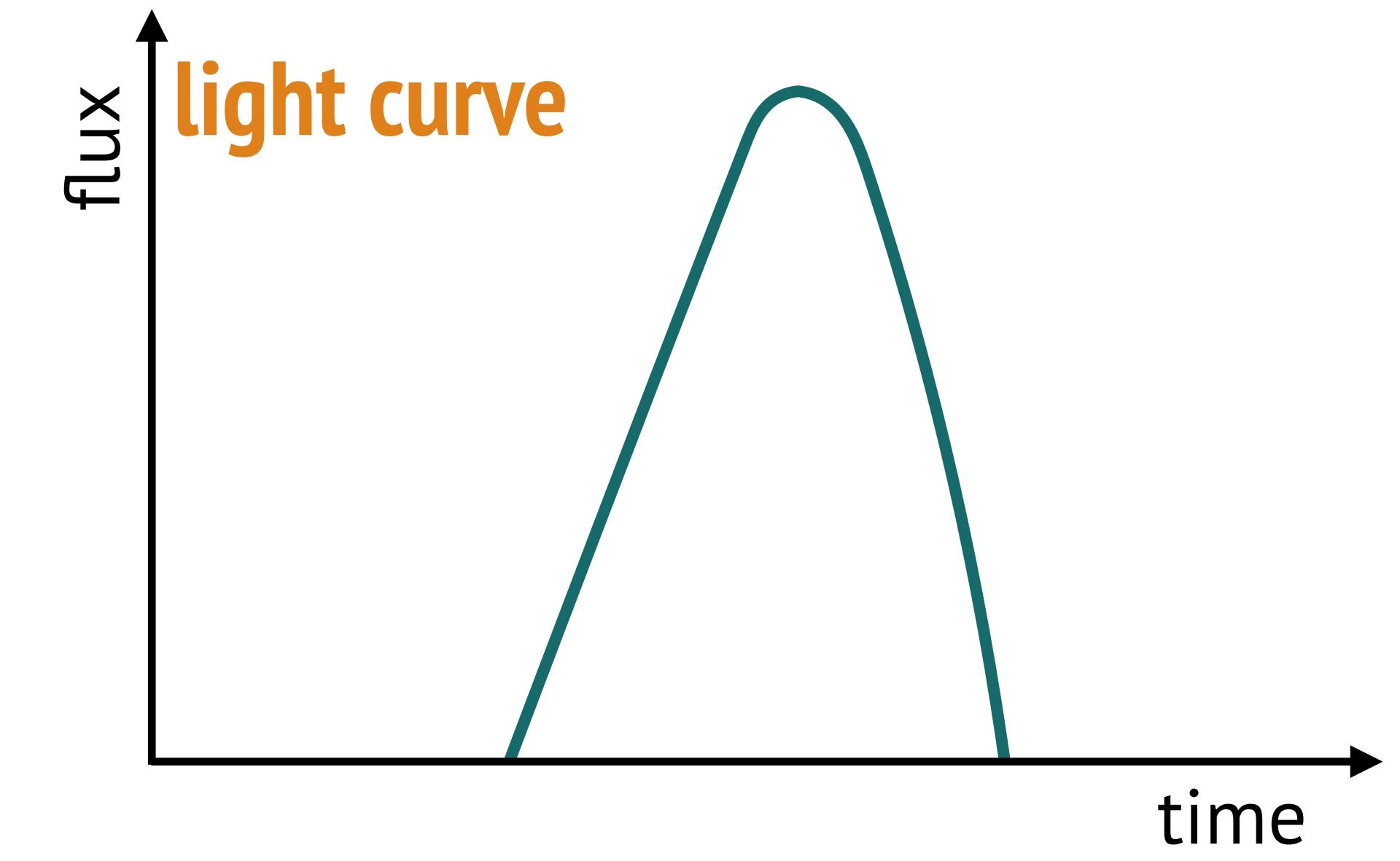
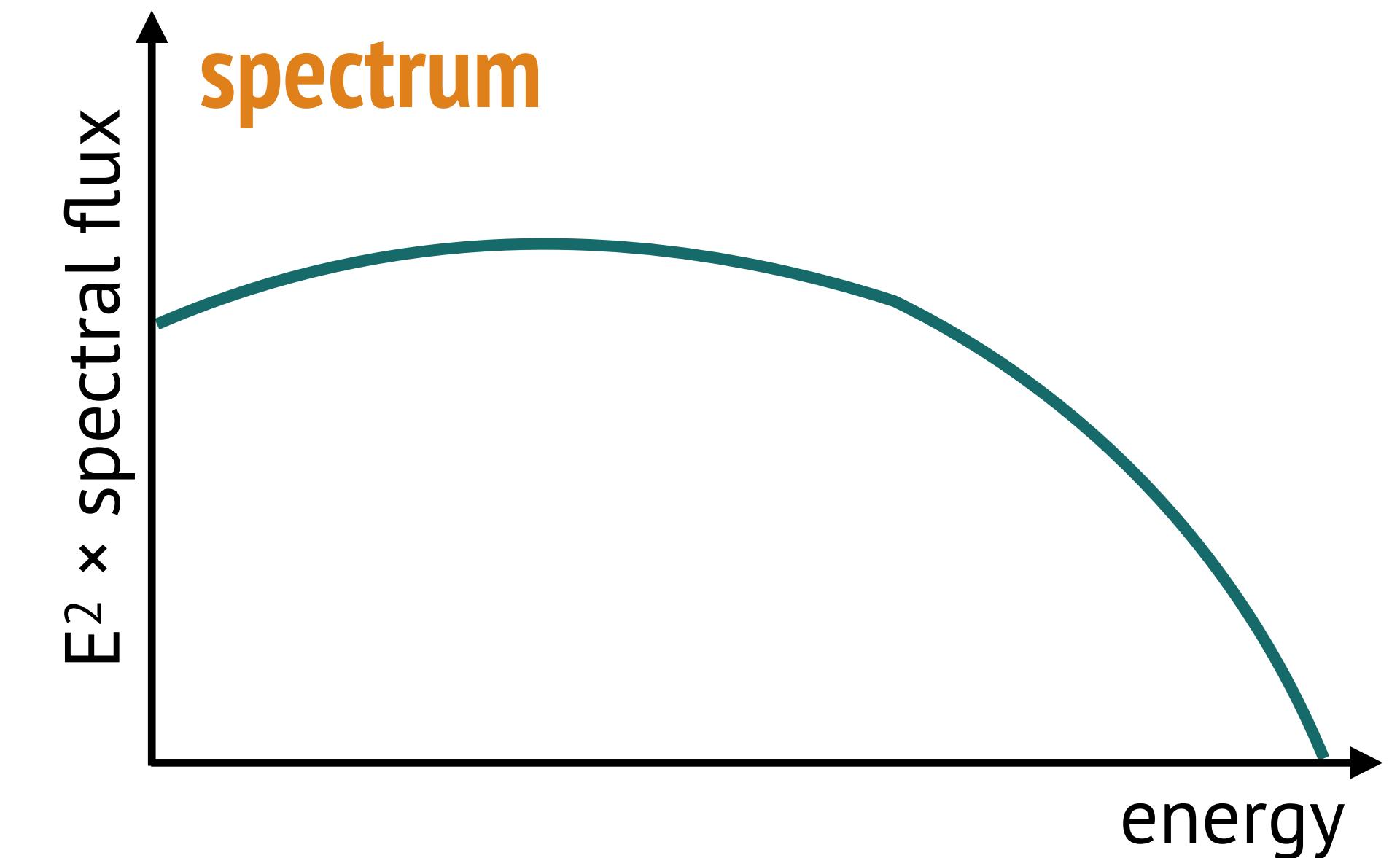


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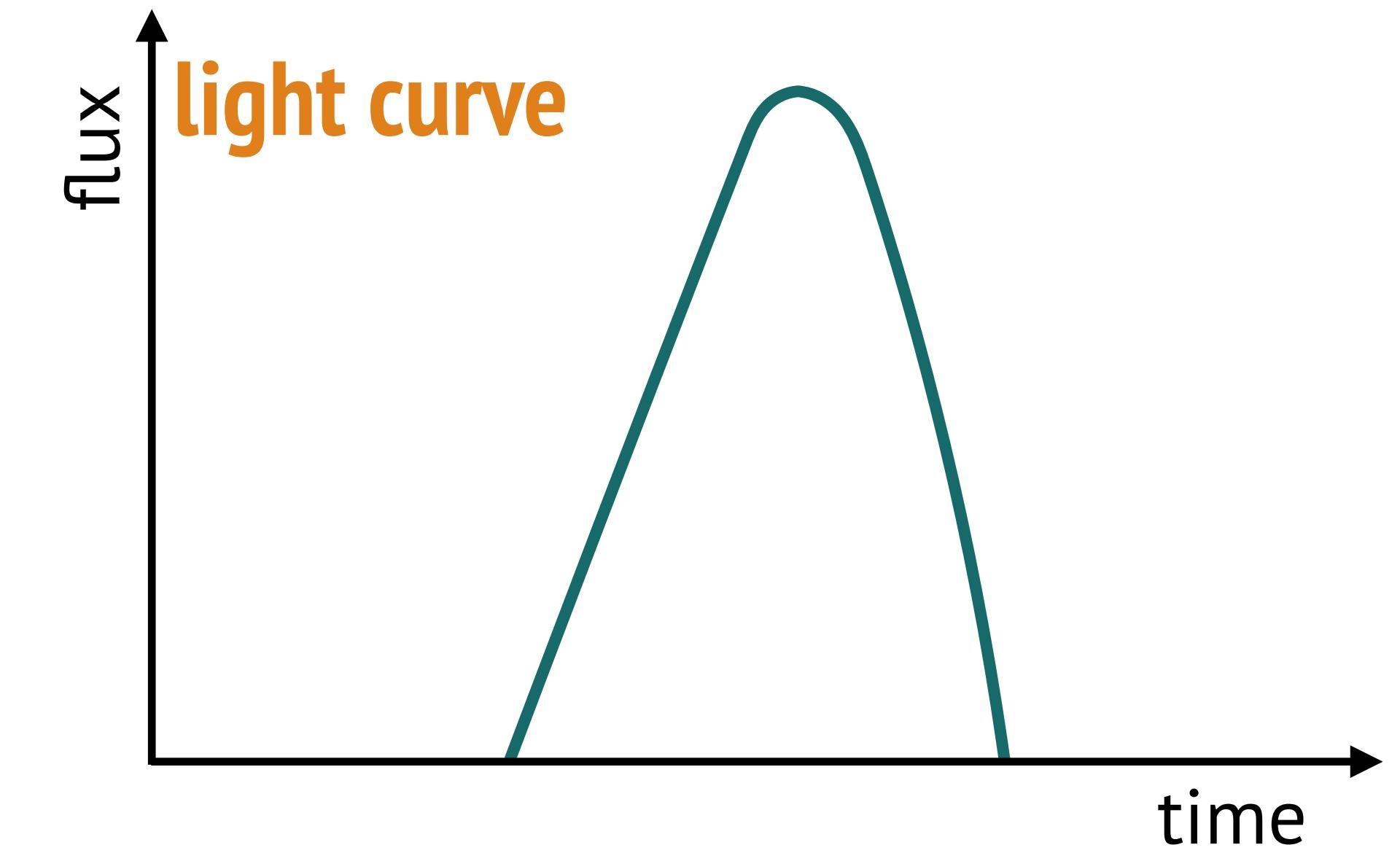
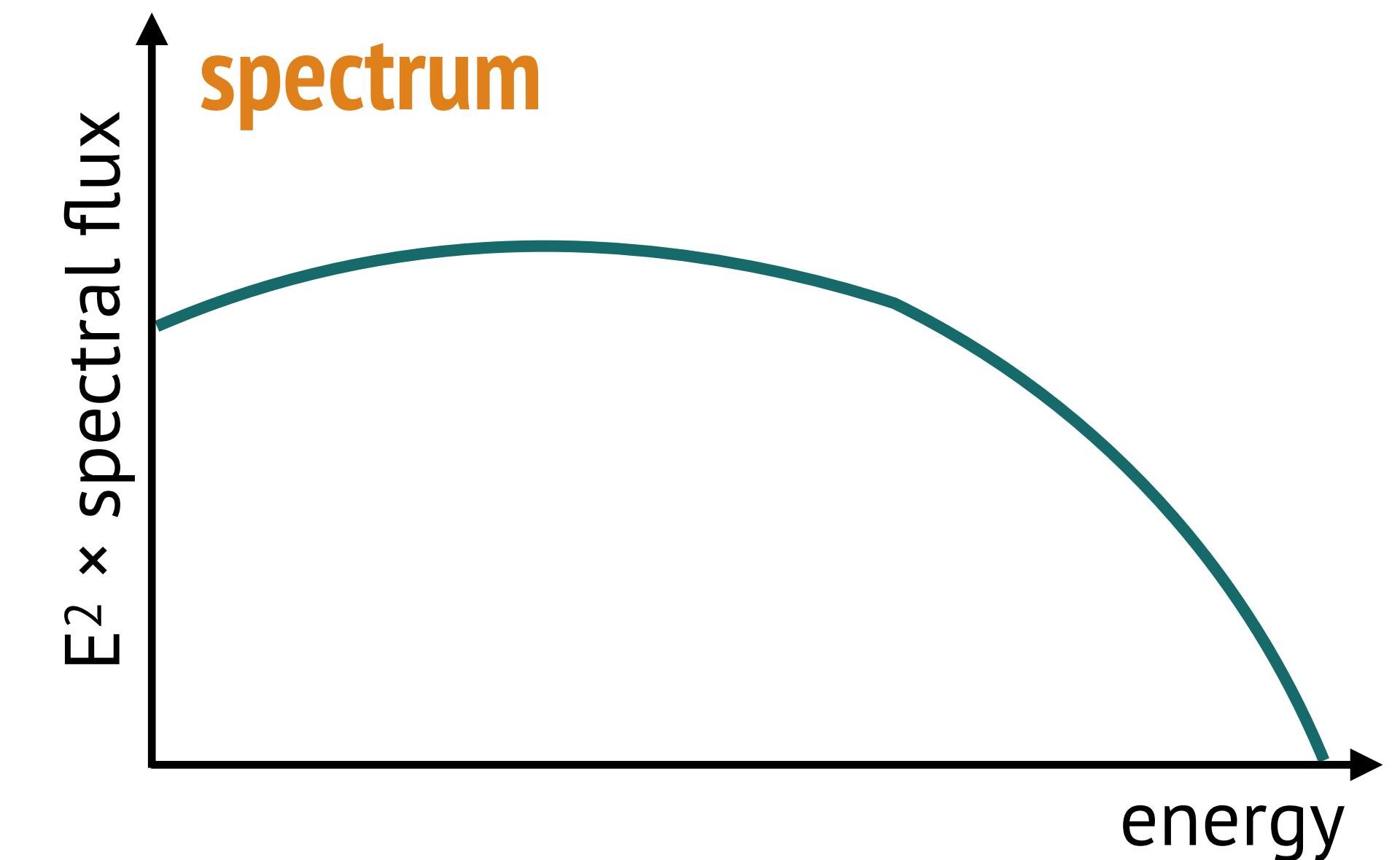
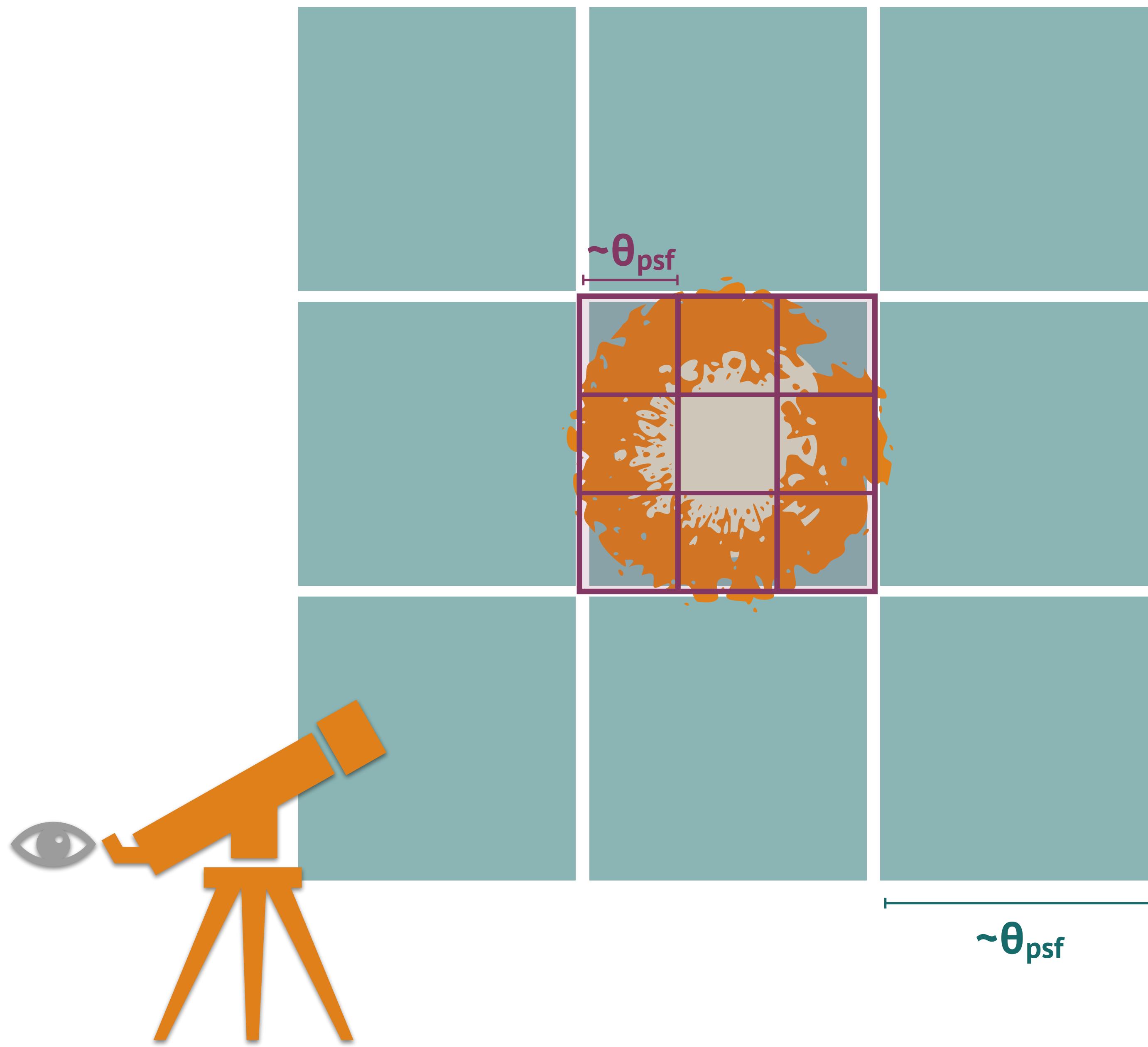
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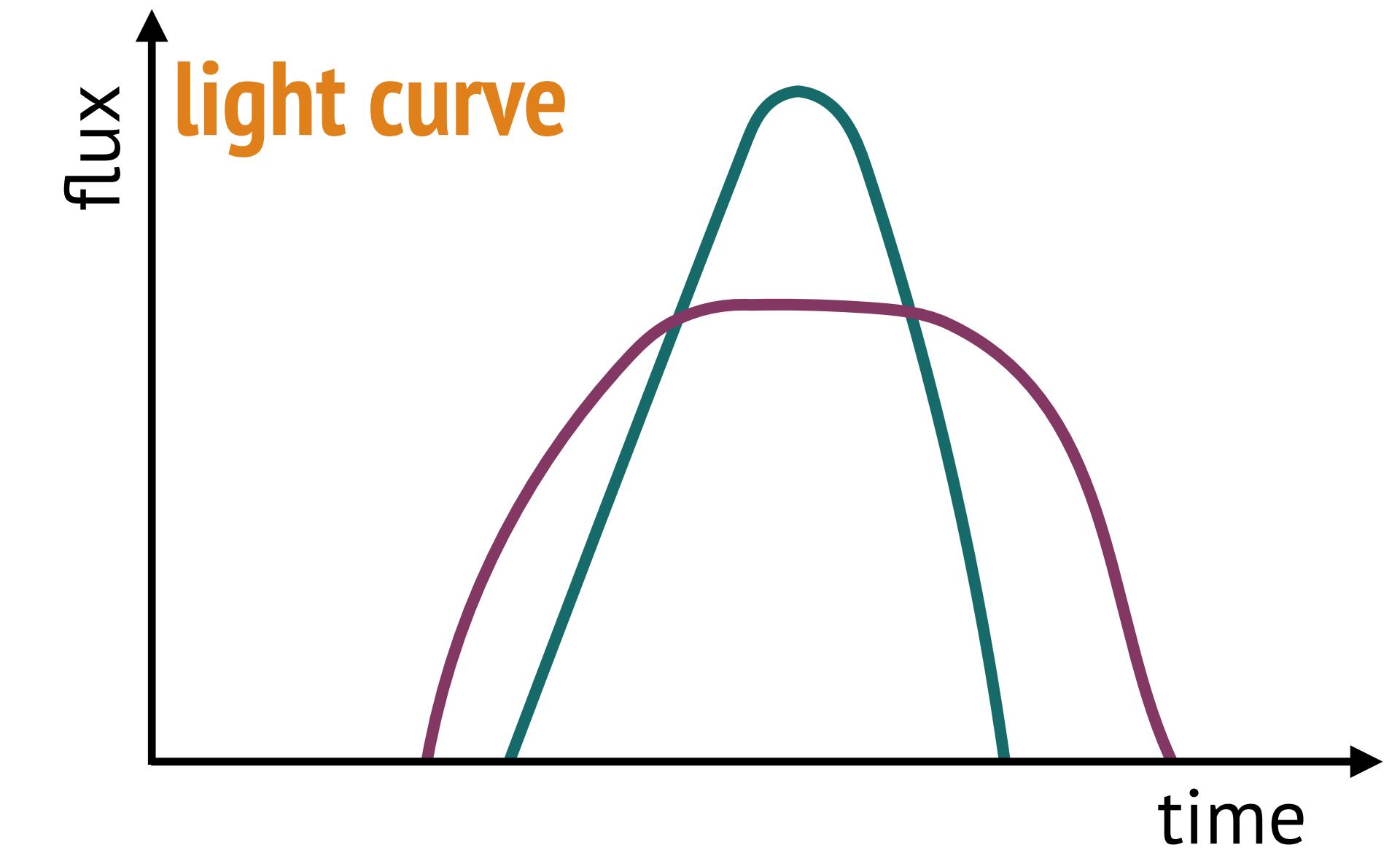
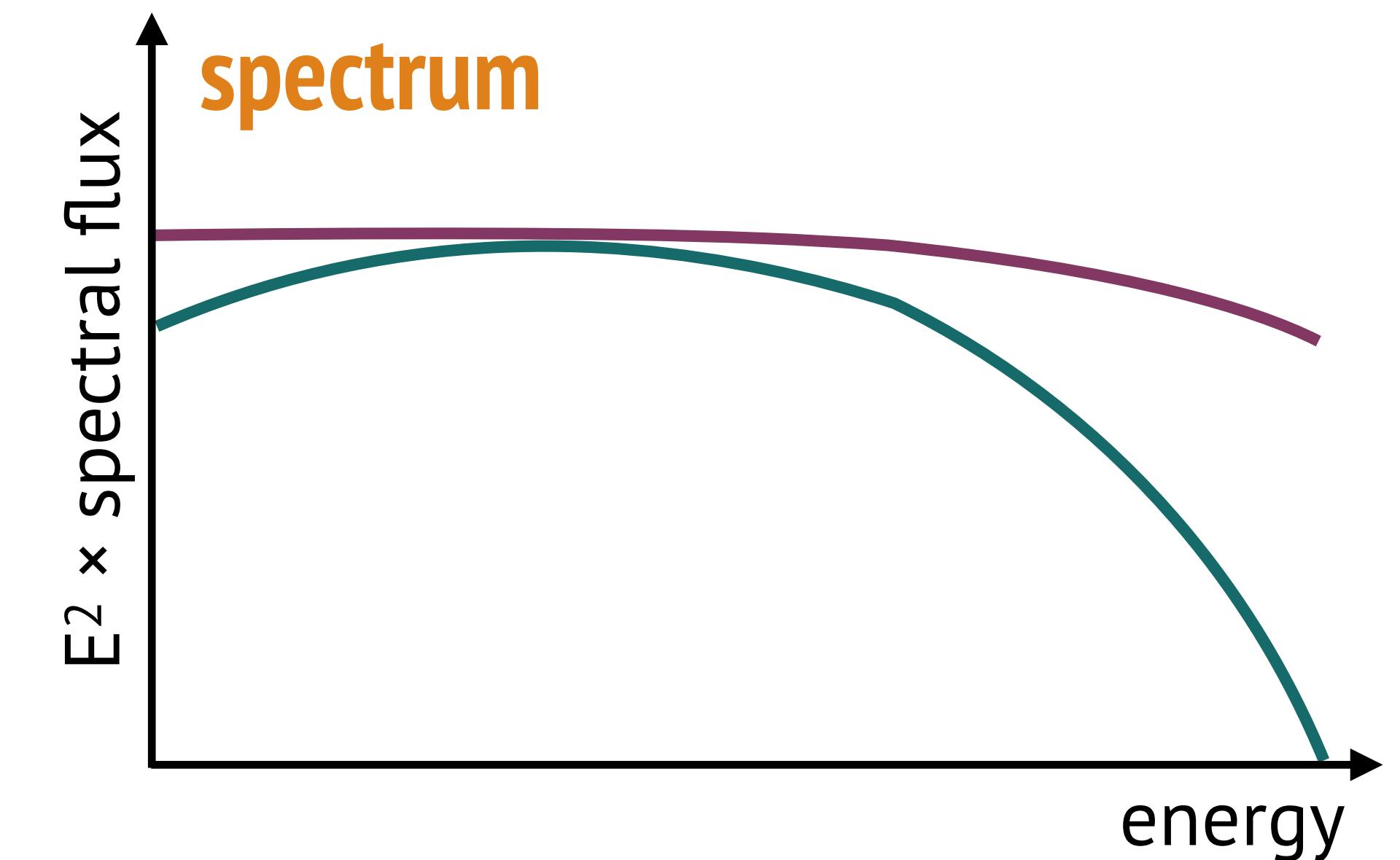
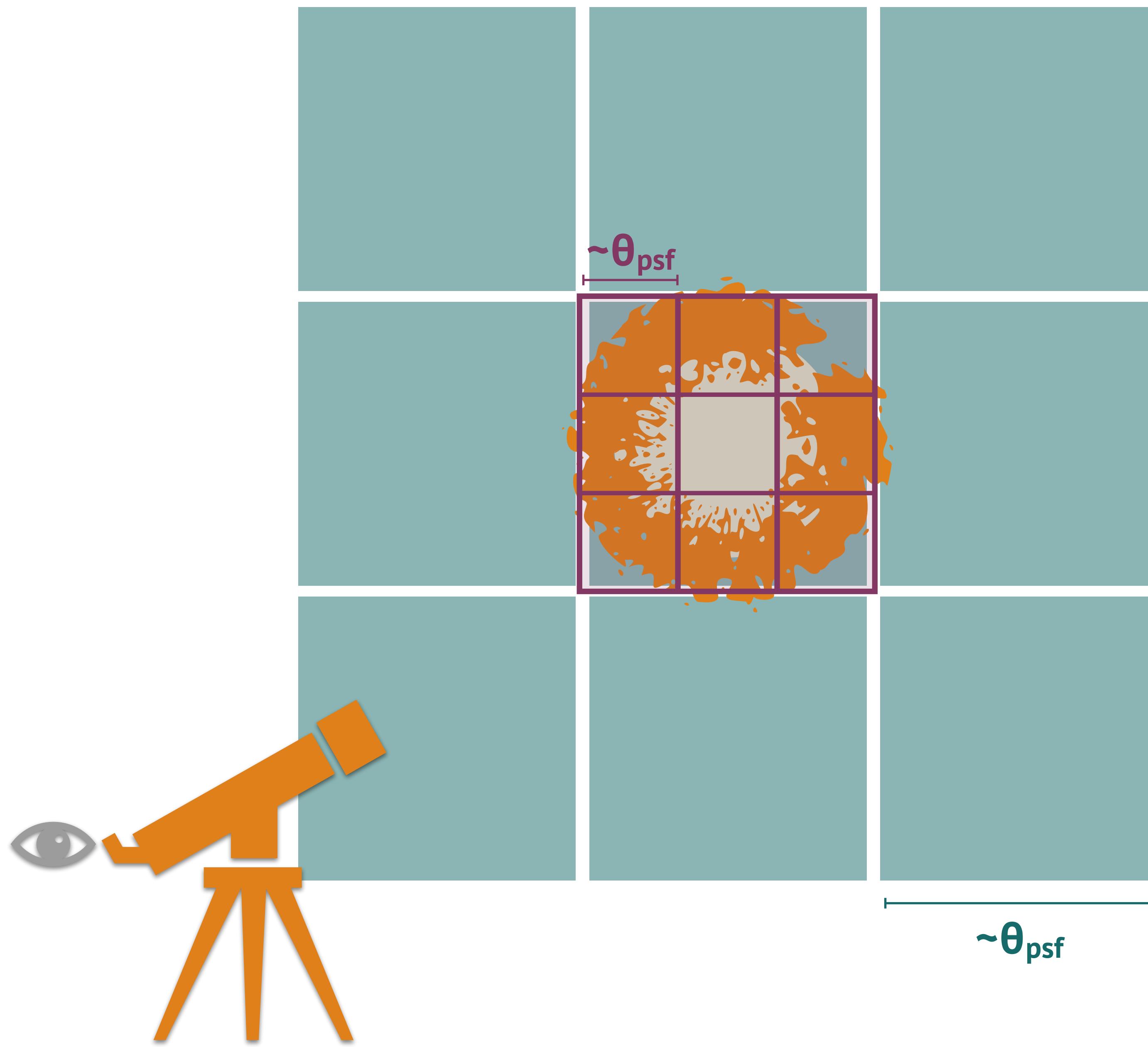
$\sim\theta_{\text{psf}}$



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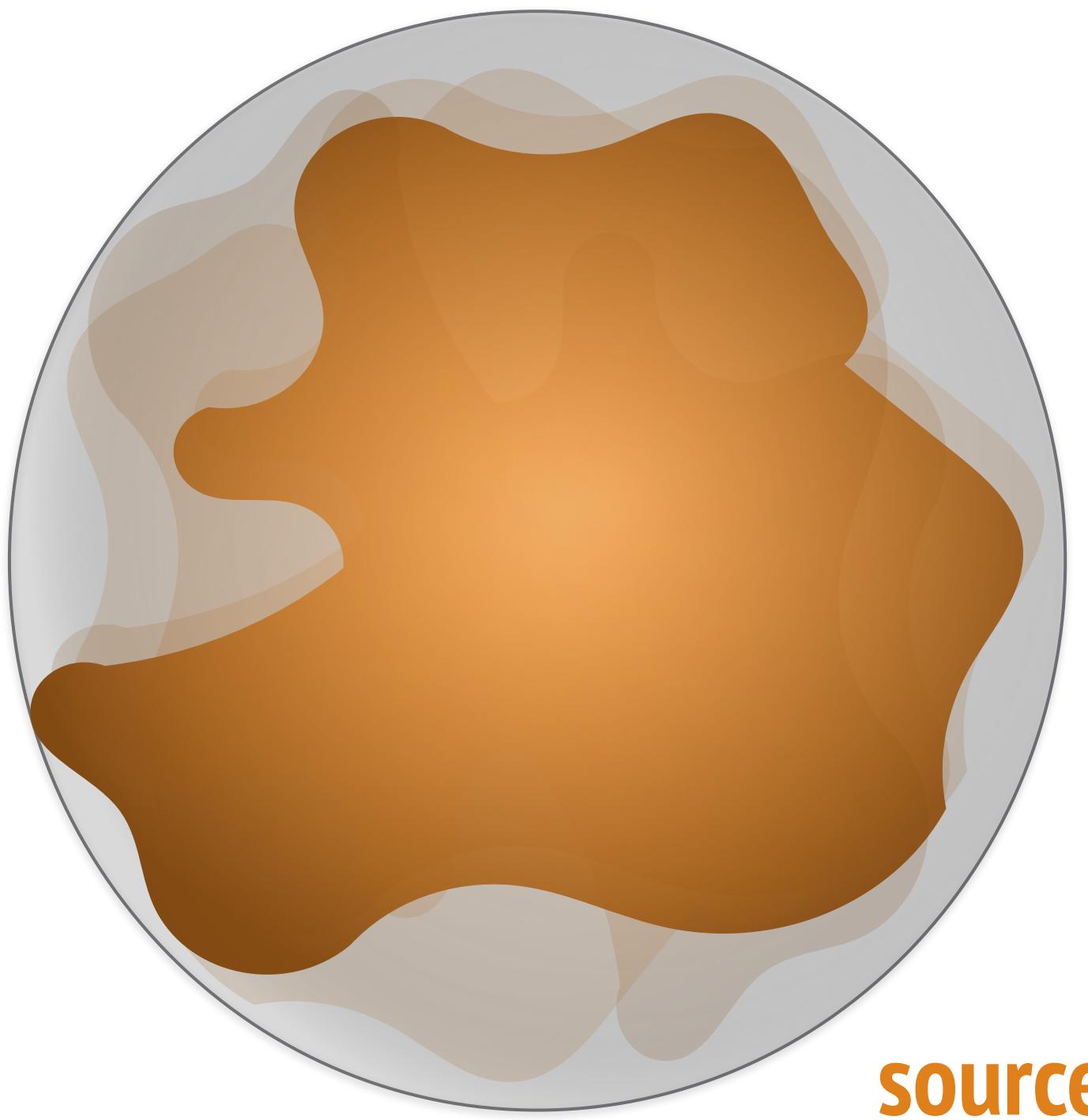
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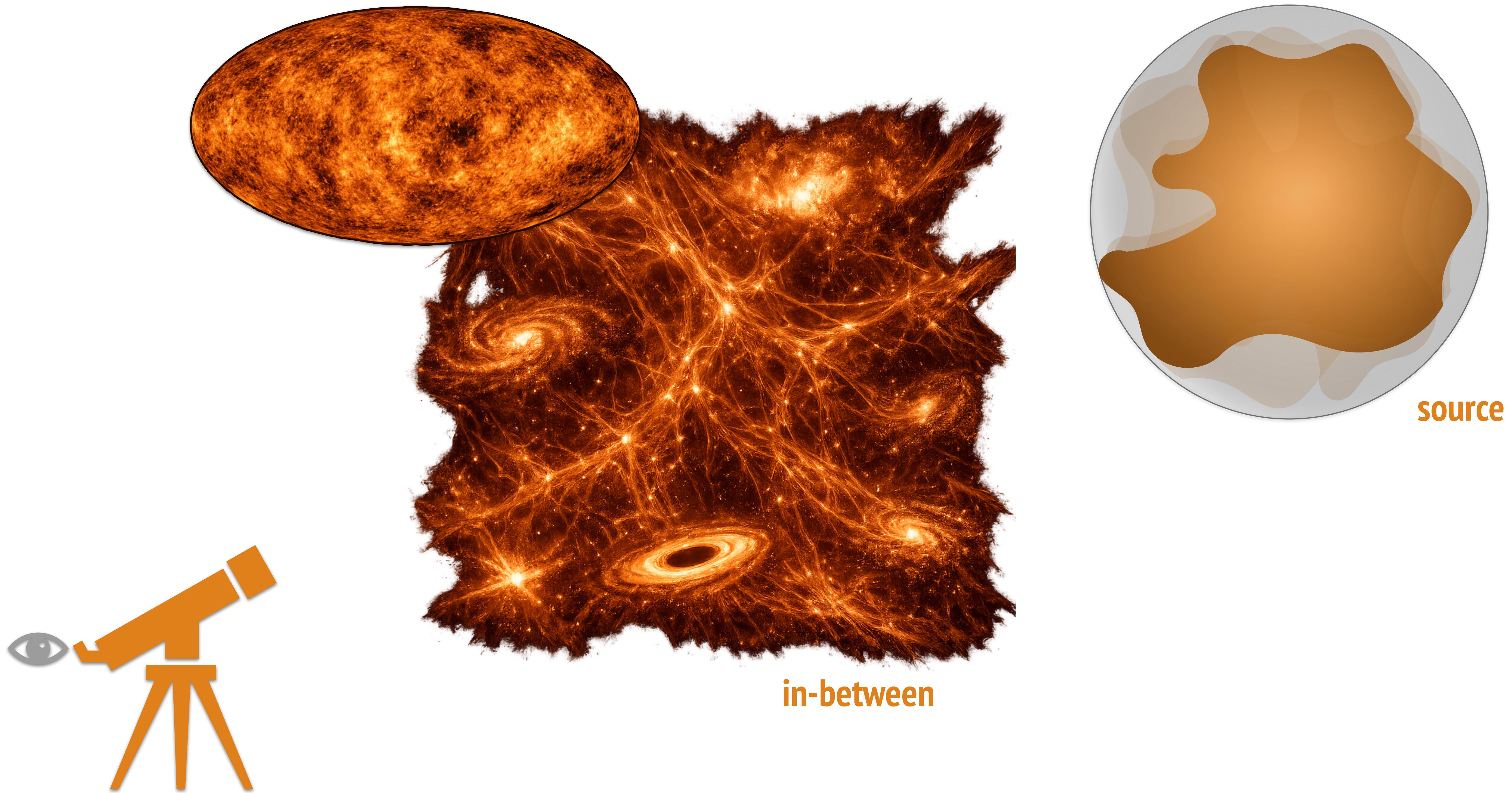
observations



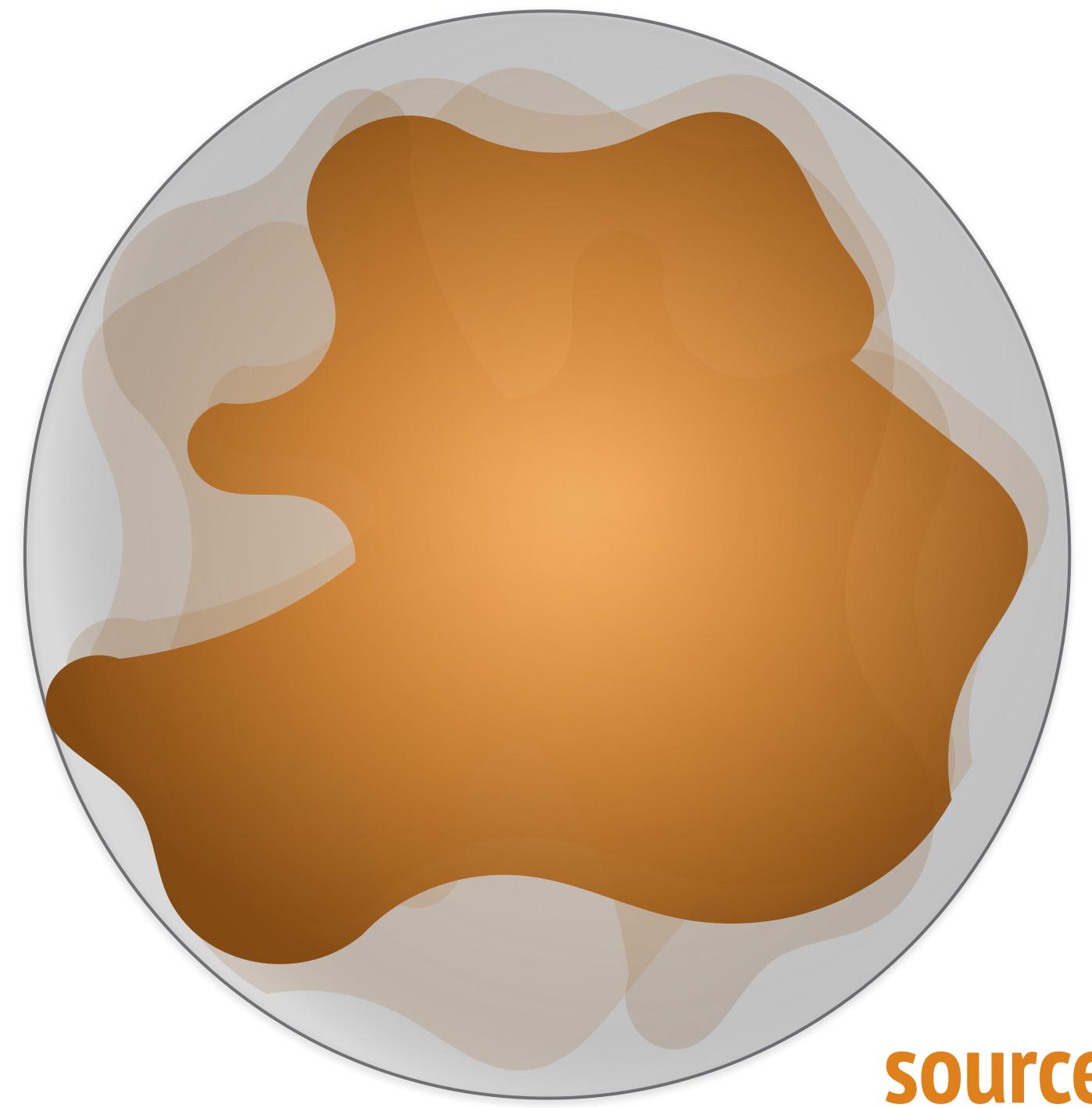
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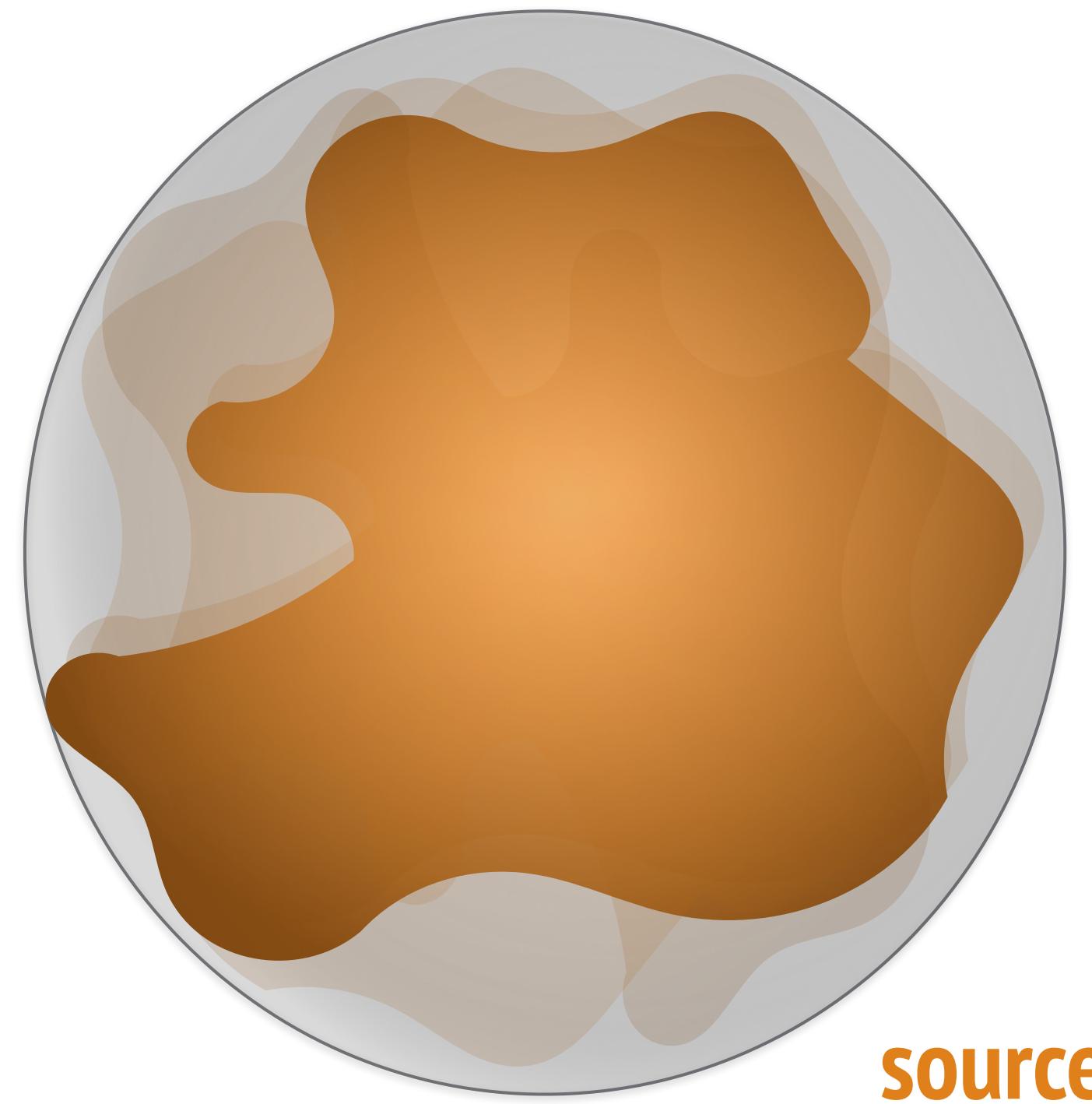
source properties. ingredients



source



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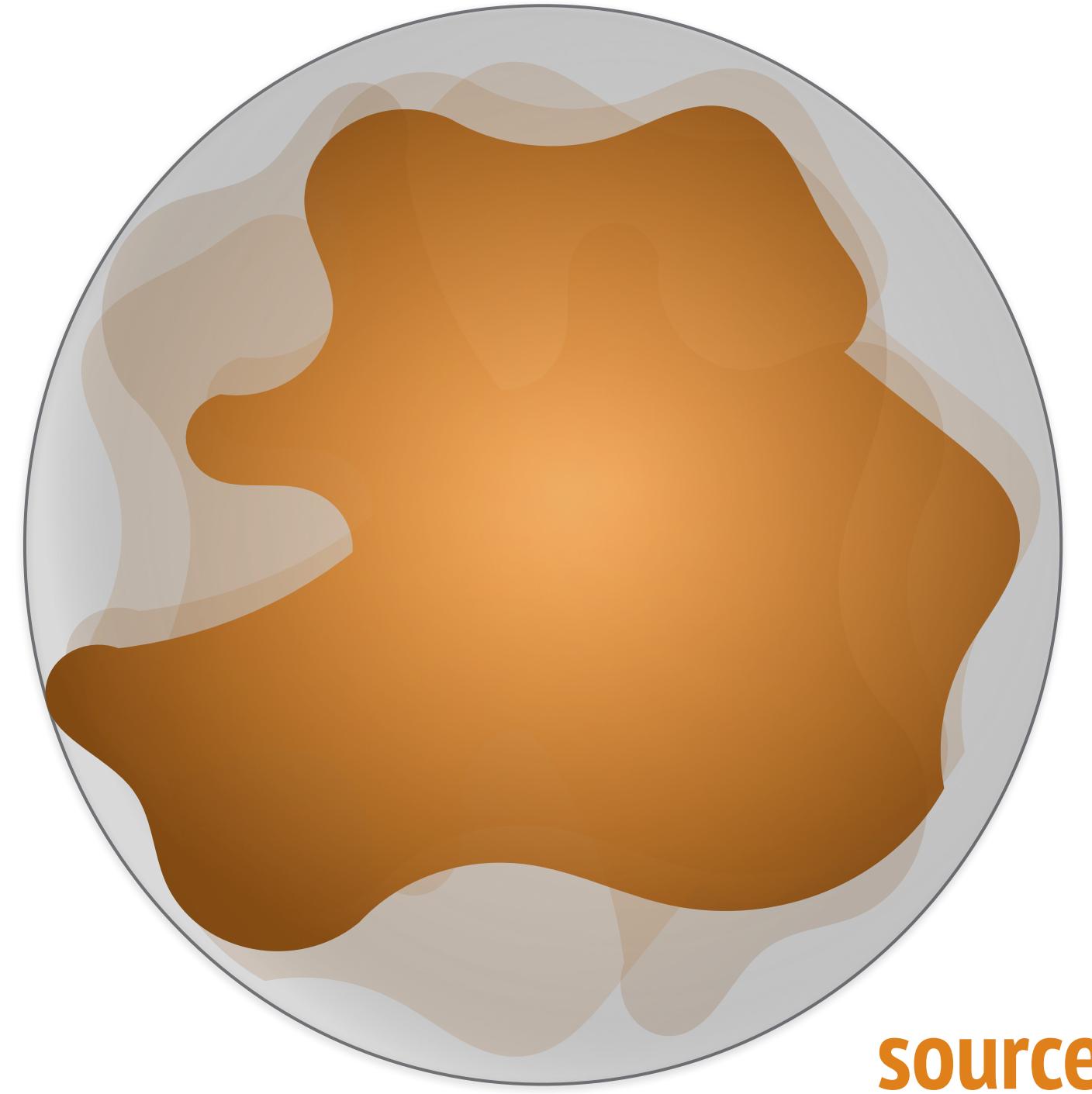
source

$$\frac{\text{number of particles}}{(\text{intervals of}) \text{ solid angle} \times \text{energy} \times \text{time}}$$



type of particle

composition, flavour



source

number of particles

(intervals of) **solid angle** \times **energy** \times **time**

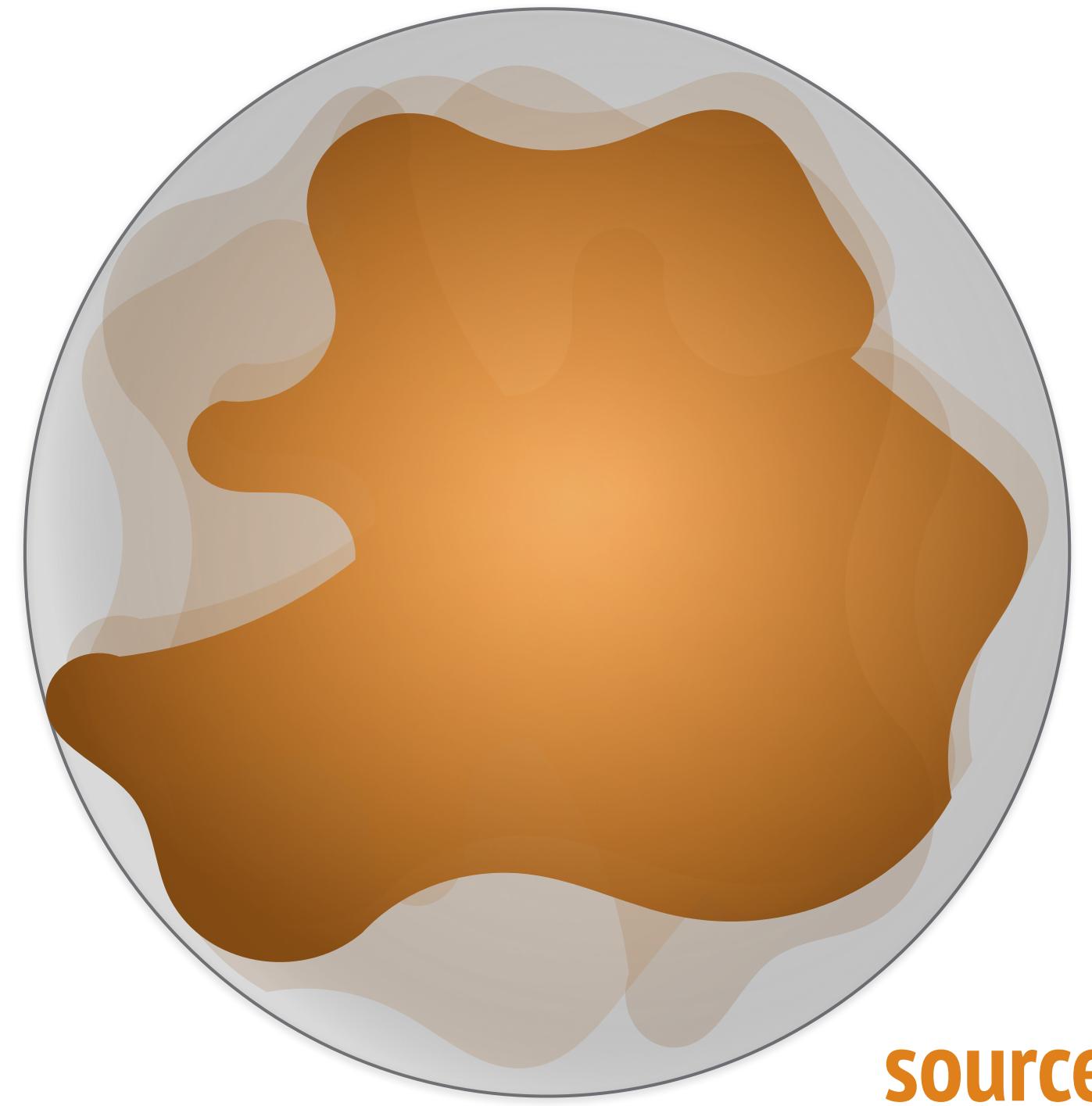


type of particle

composition, flavour

position of emission site

position of each source and within the source



number of particles

(intervals of) $\frac{\text{solid angle} \times \text{energy} \times \text{time}}{\text{time}}$



type of particle

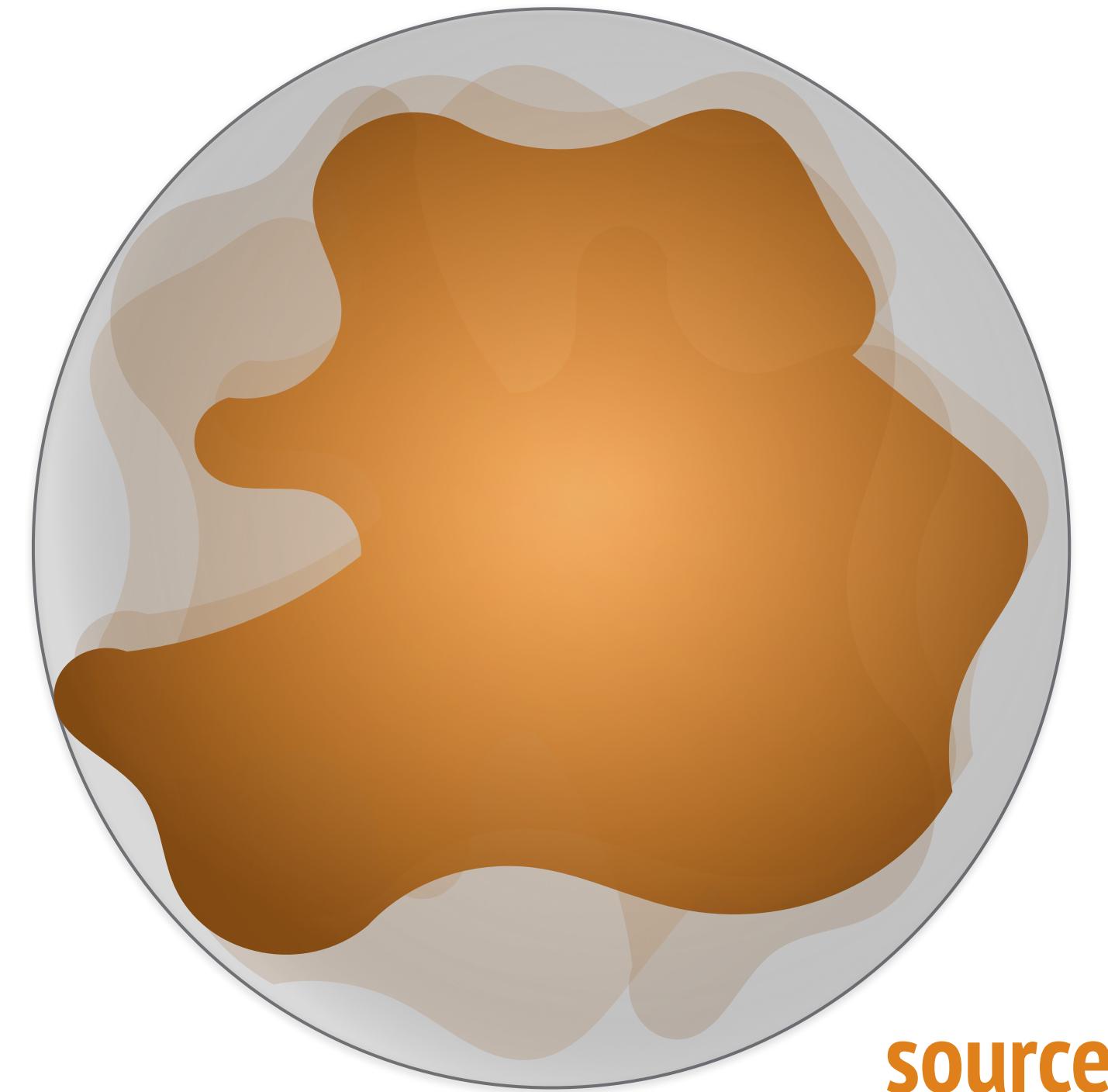
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temporal emission profiles

light curves



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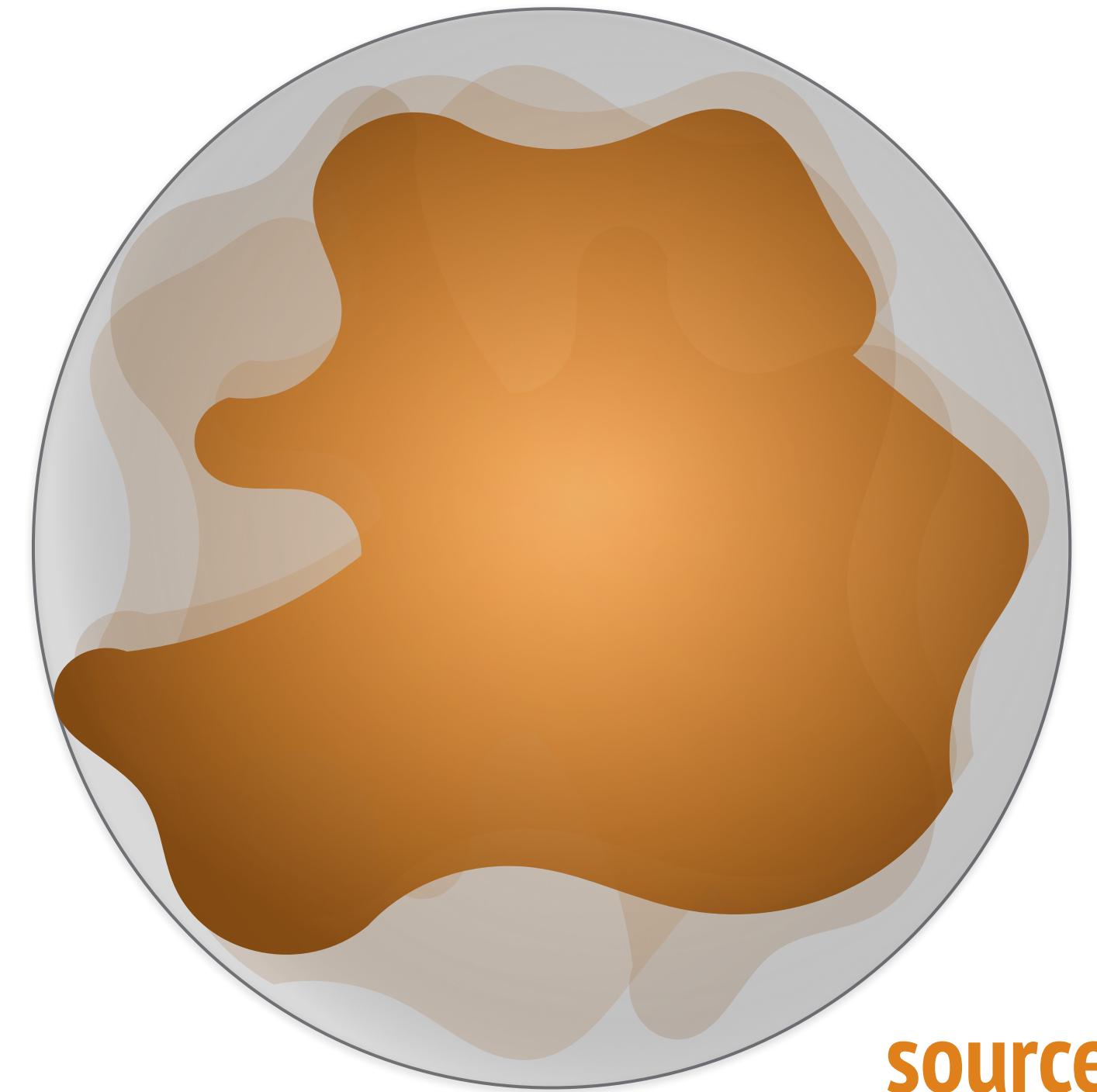
temporal emission profiles

light curves

intrinsic spectra

number of events in each energy bin

$$\frac{\text{number of particles}}{\text{(intervals of) solid angle} \times \text{energy} \times \text{time}}$$



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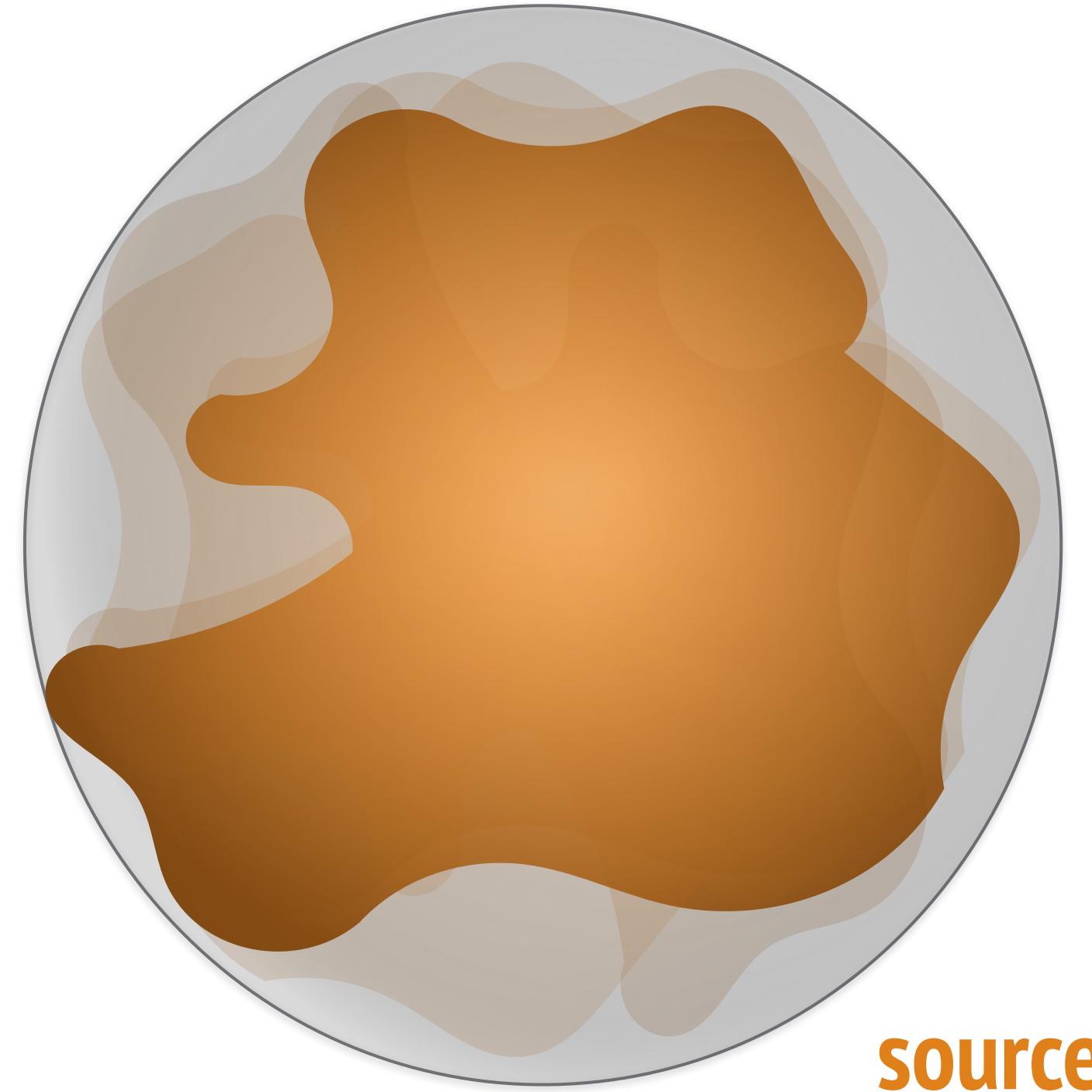
number of events in each energy bin

geometry of emission

isotropic, jet

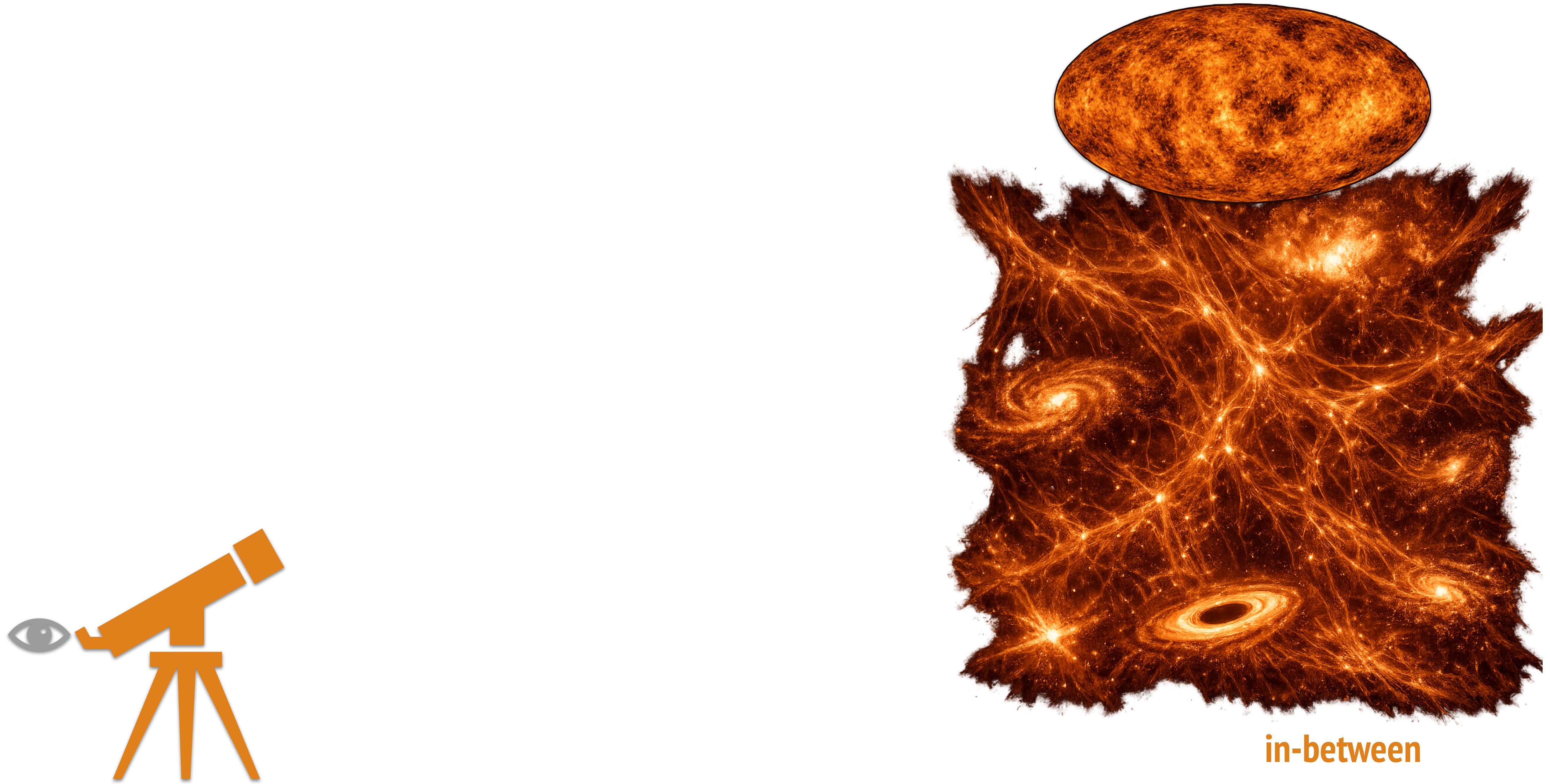
$$\frac{\text{number of particles}}{\text{solid angle} \times \text{energy} \times \text{time}}$$

(intervals of)



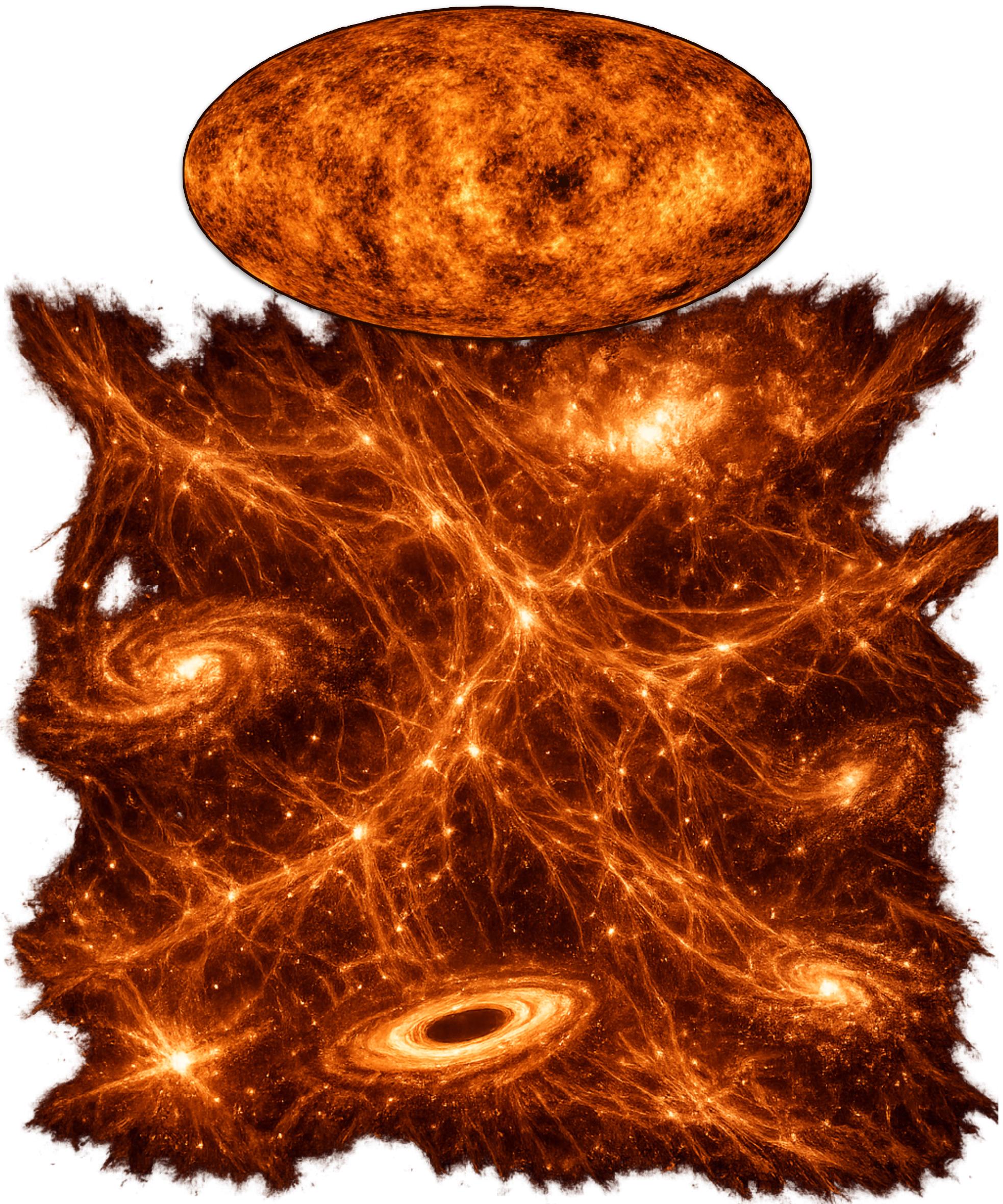
source





target distributions

photons (e.g., CMB, EBL)



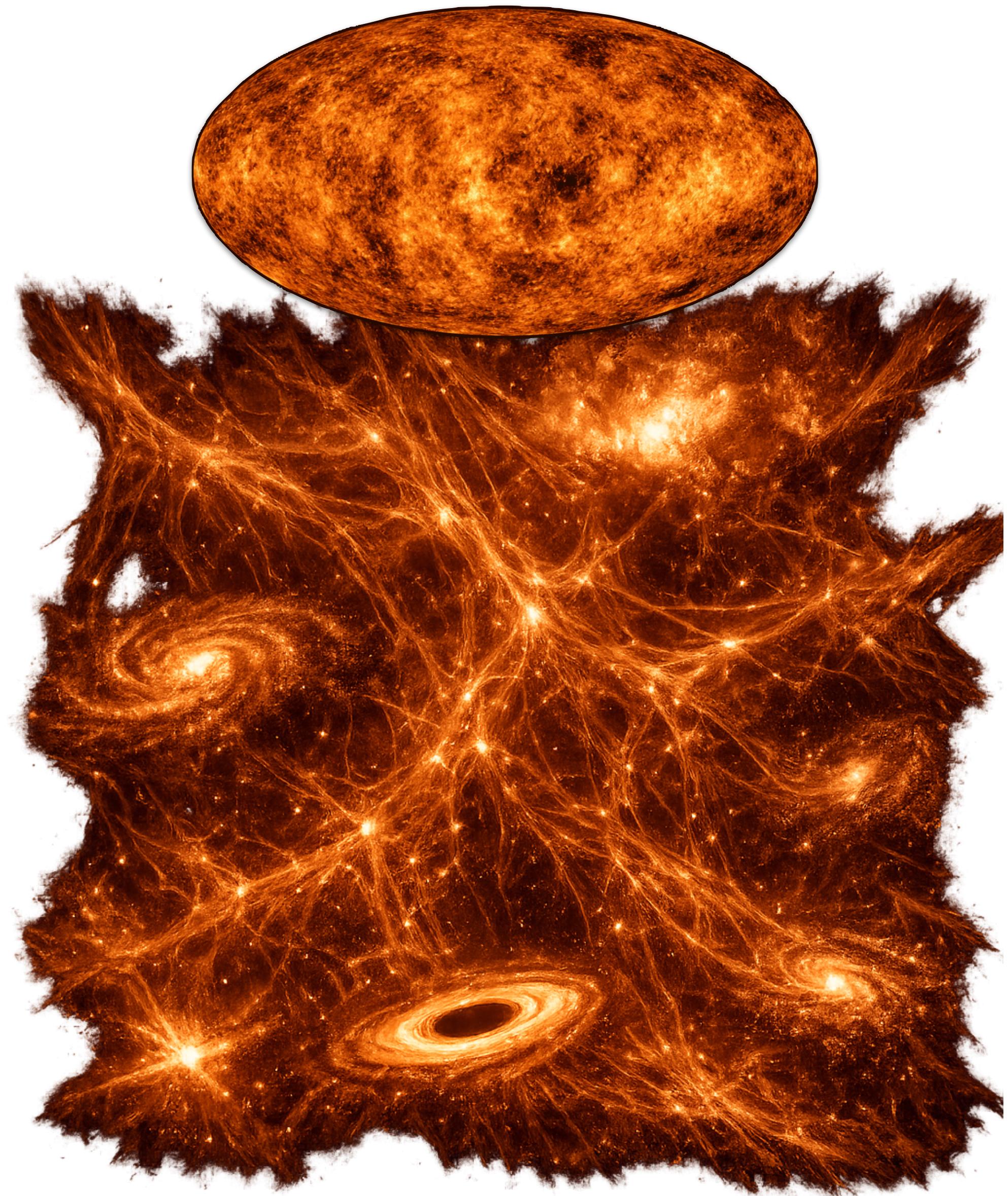
in-between

target distributions

photons (e.g., CMB, EBL)

magnetic fields

galactic, extragalactic



in-between

target distributions

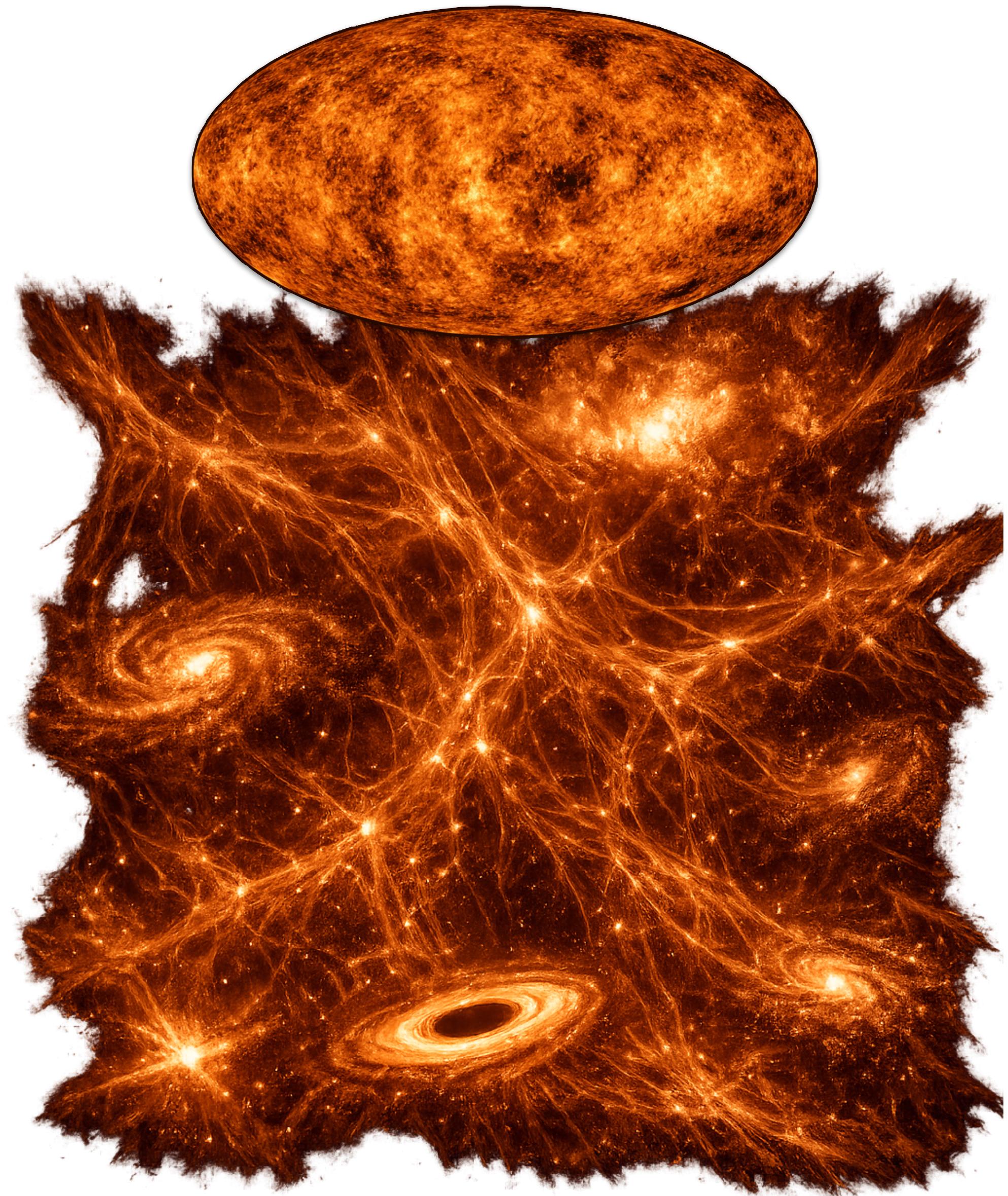
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gravitational fields

lenses



in-between

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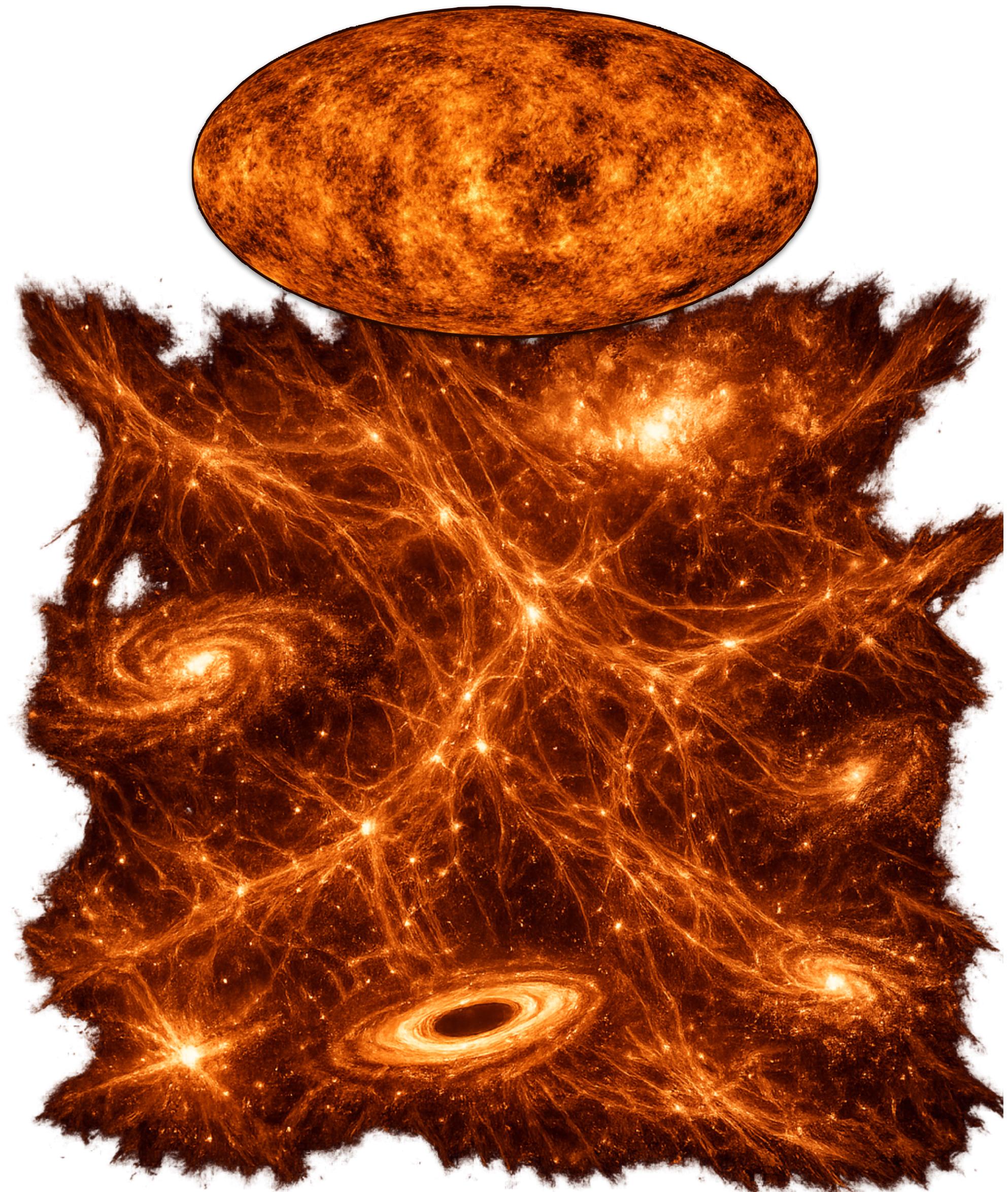
galactic, extragalactic

gravitational fields

lenses

physics of interactions

cross sections,



in-between



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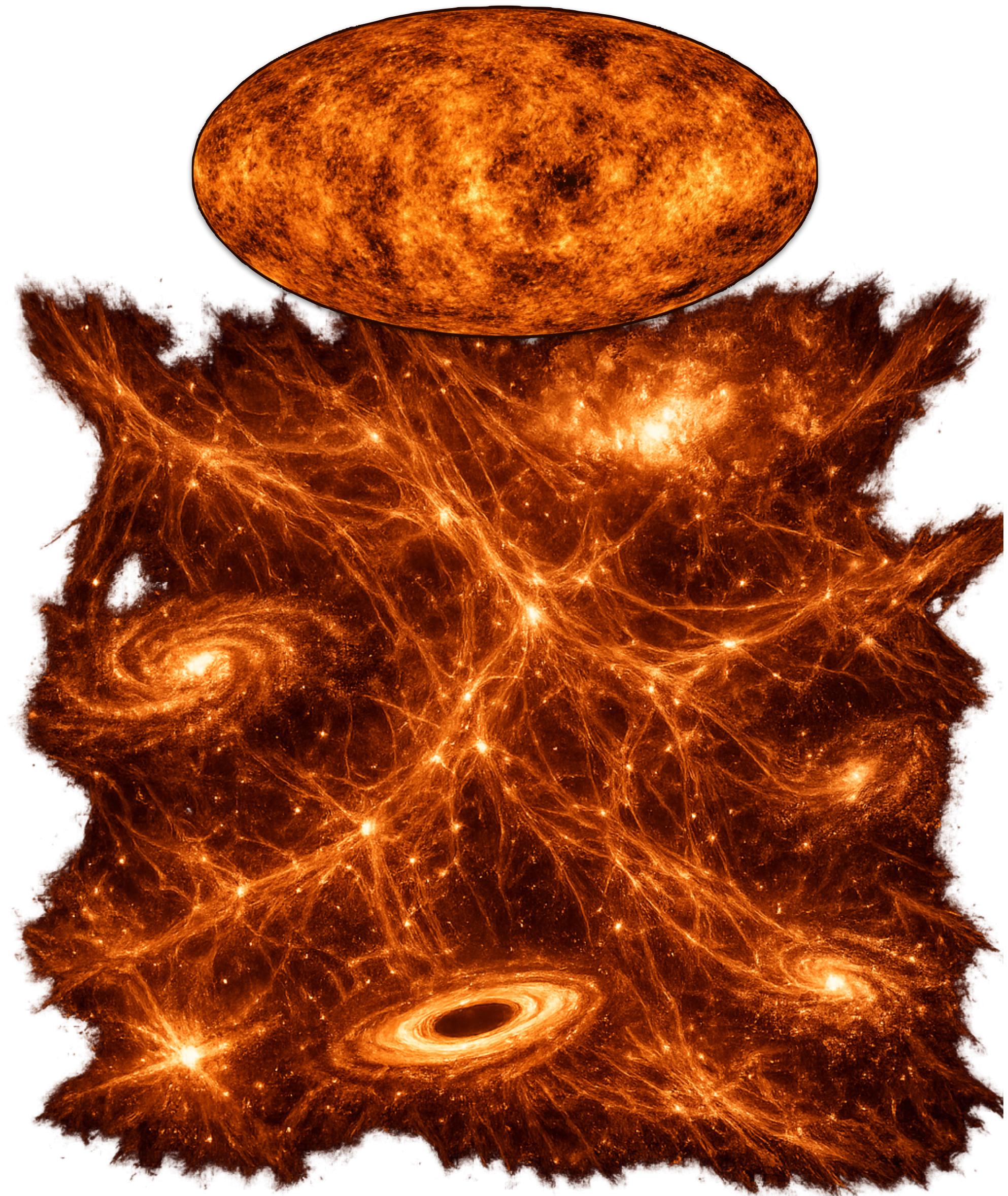
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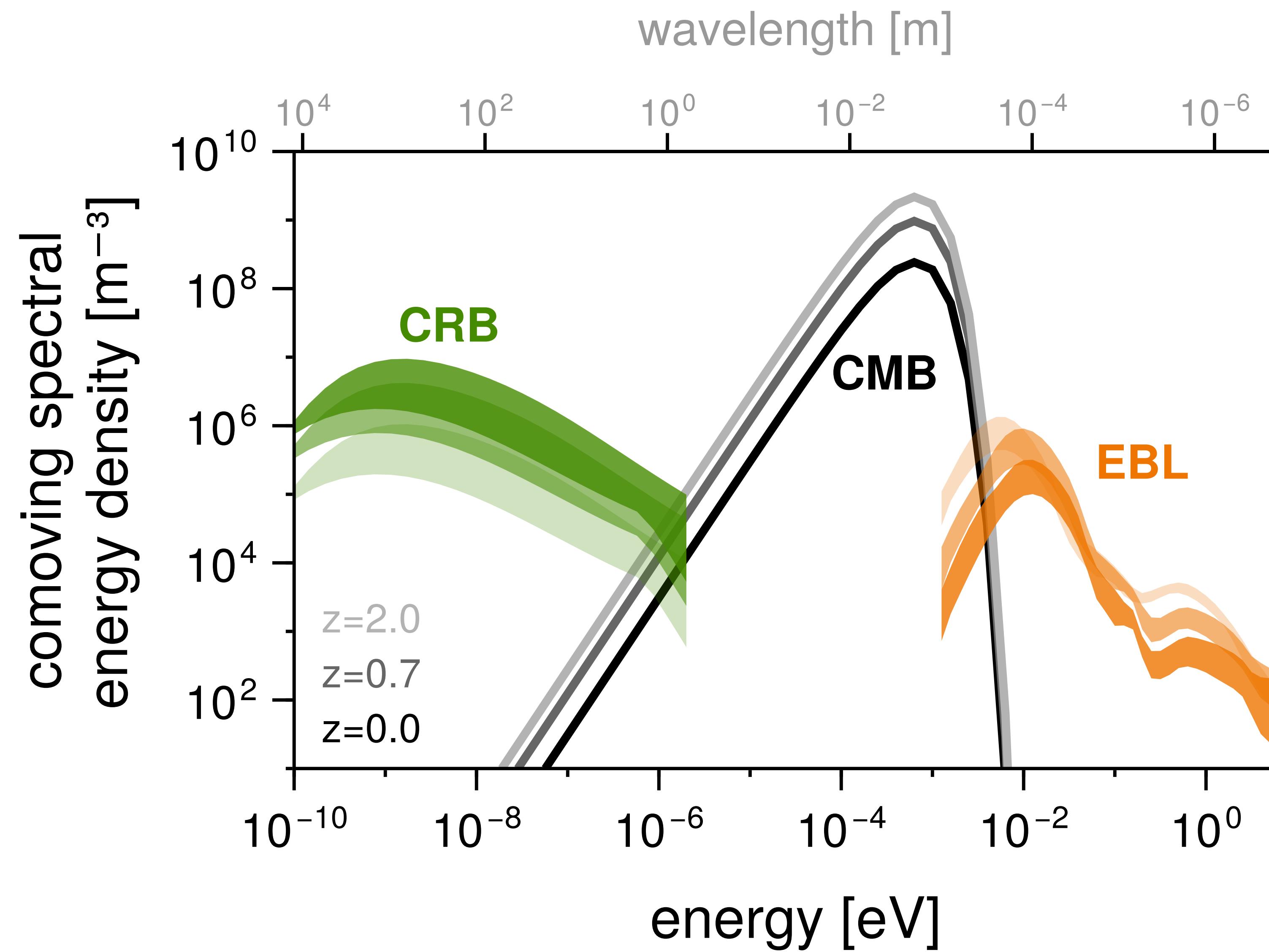
mesoscale physics

collective phenomena



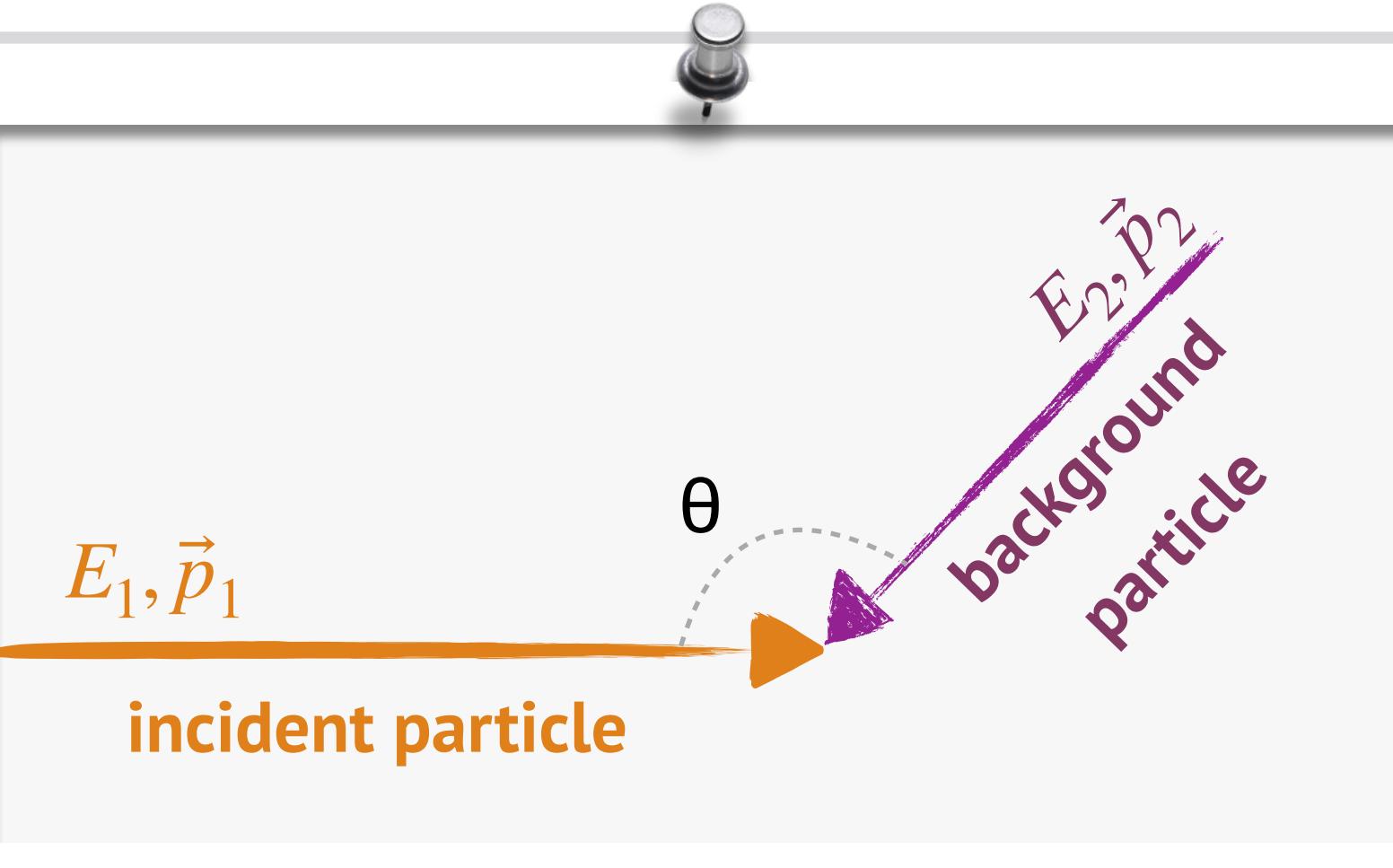
in-between

cosmological photon backgrounds

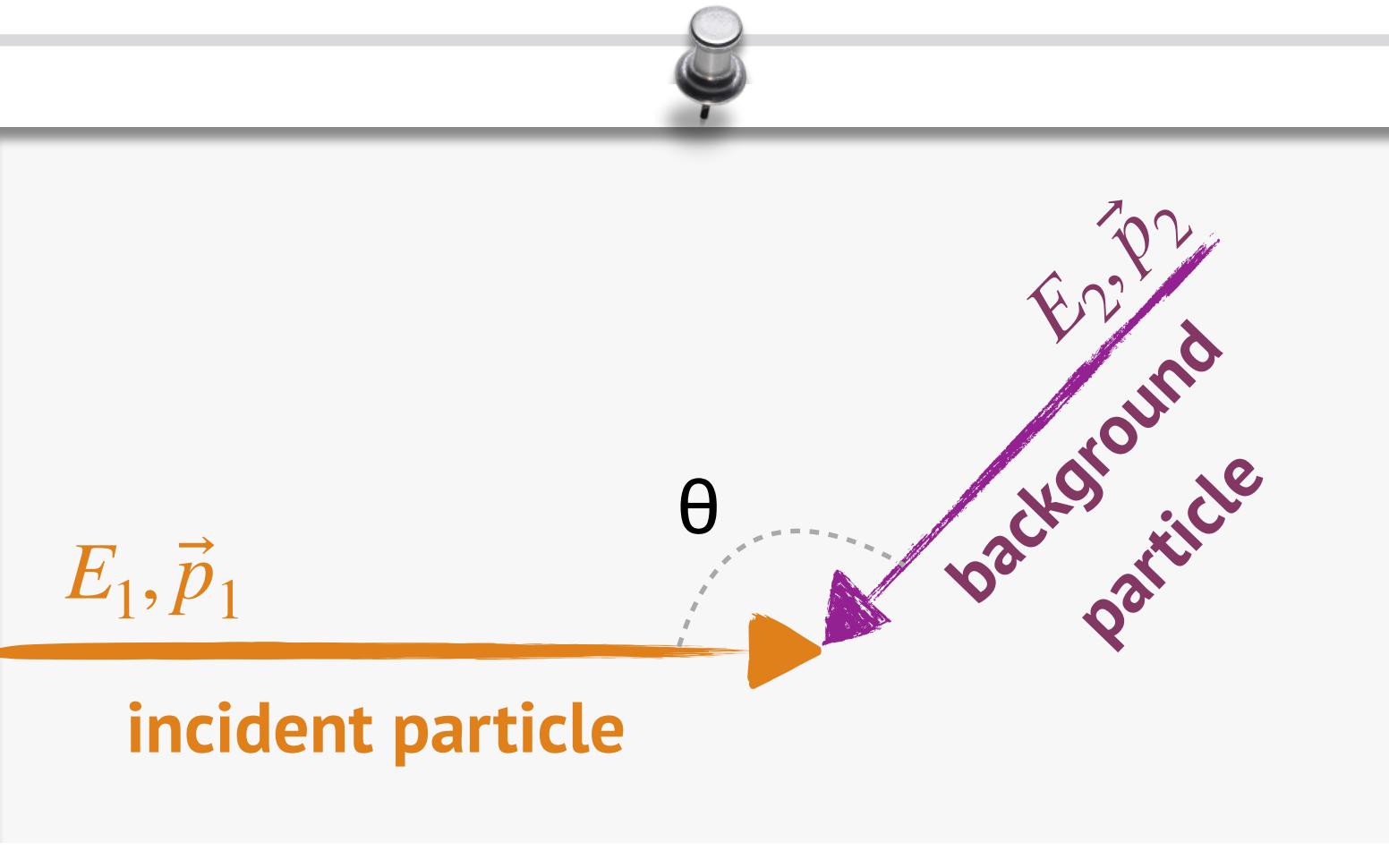


interactions and mean free path

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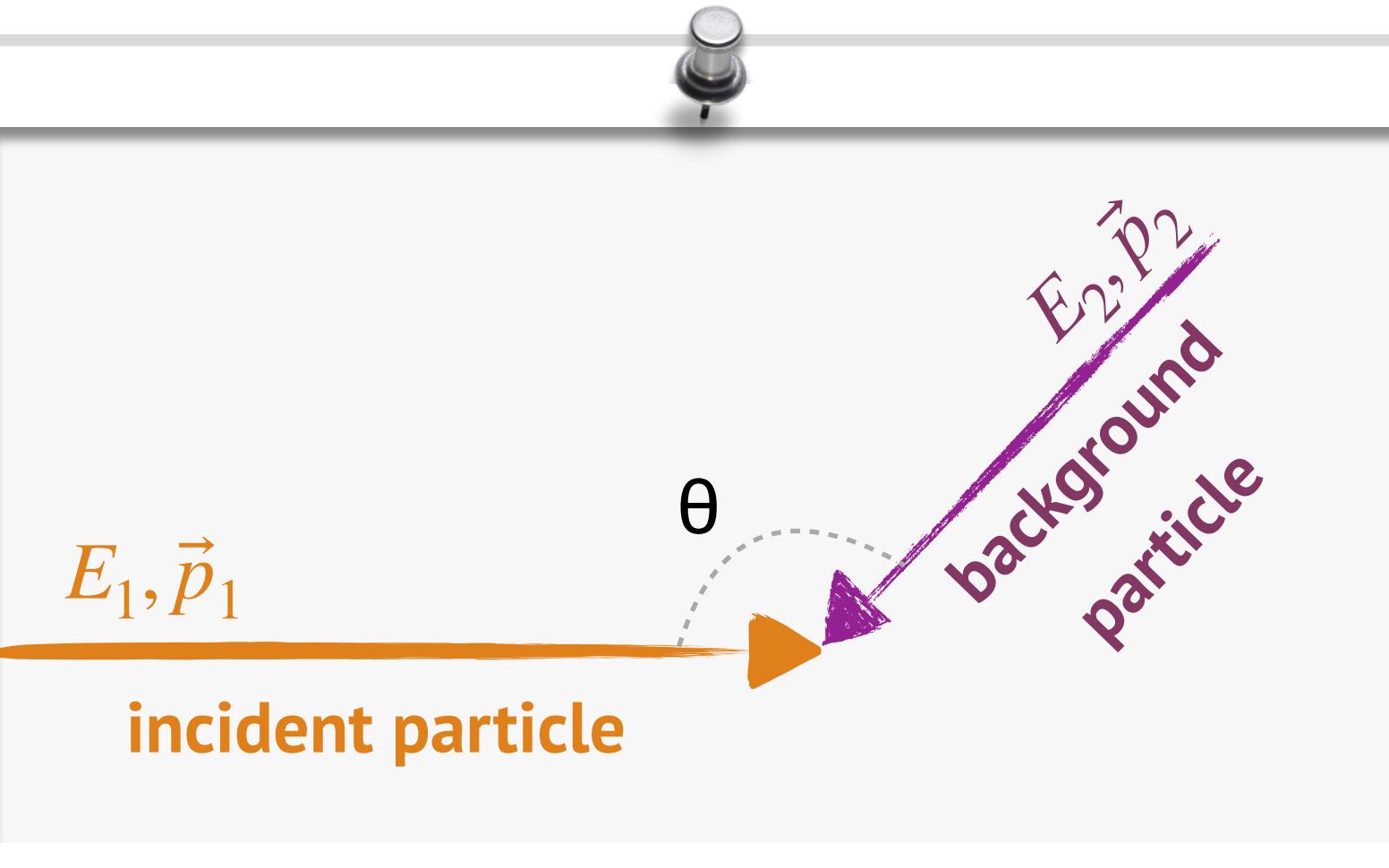
interactions and mean free path



centre of mass energy

$$s = m_1^2 c^4 + m_2^2 c^4 + 2E_1 E_2 (1 - \beta_1 \beta_2 \cos \theta)$$

interactions and mean free path



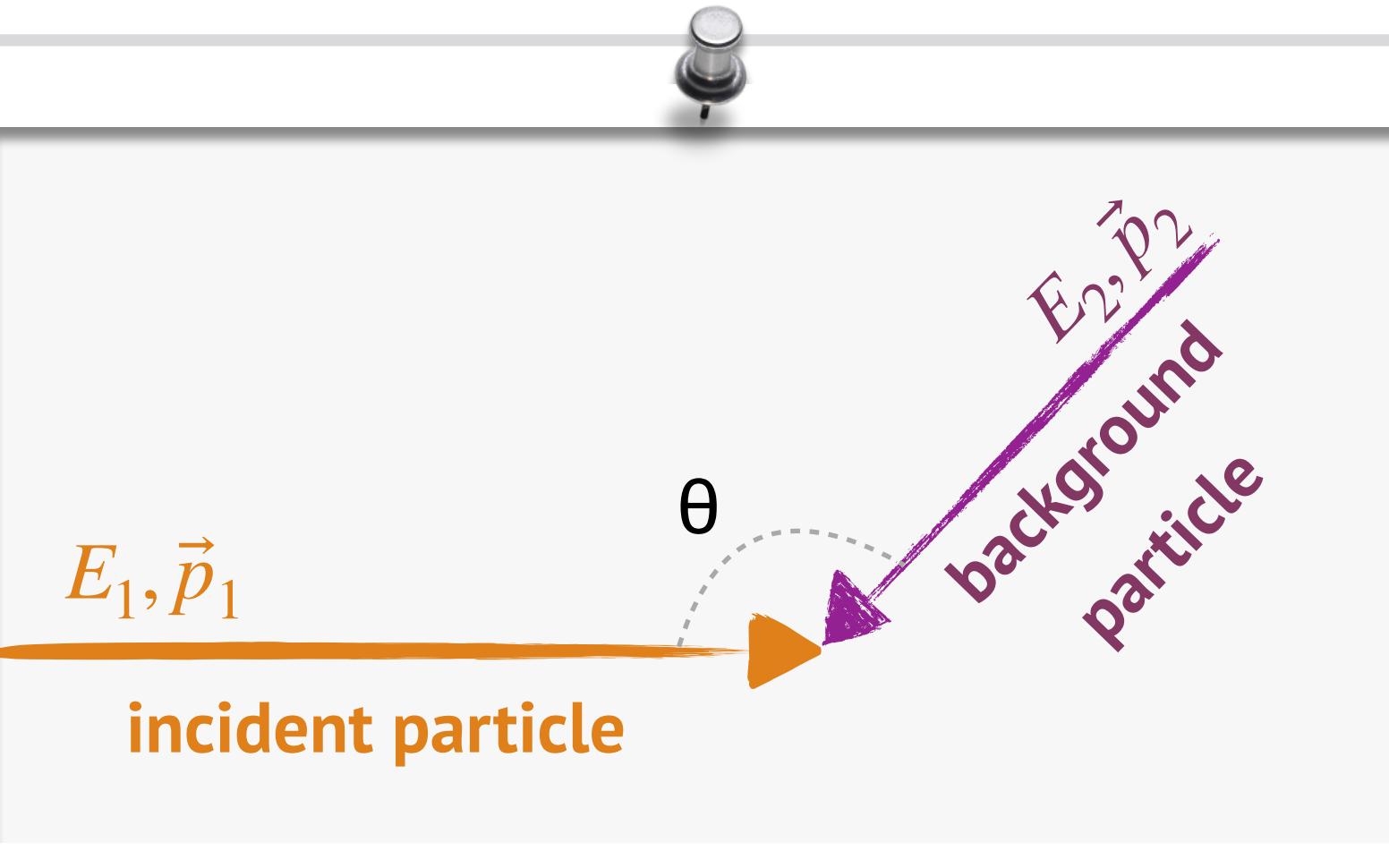
**centre of mass
energy**

**relative
velocity**

$$s = m_1^2 c^4 + m_2^2 c^4 + 2E_1 E_2 (1 - \beta_1 \beta_2 \cos \theta)$$

$$\beta_{\text{rel}} = \sqrt{\frac{(P_1 \cdot P_2)^2 - (m_1 m_2 c^2)^2}{(P_1 \cdot P_2)^2}}$$

interactions and mean free path



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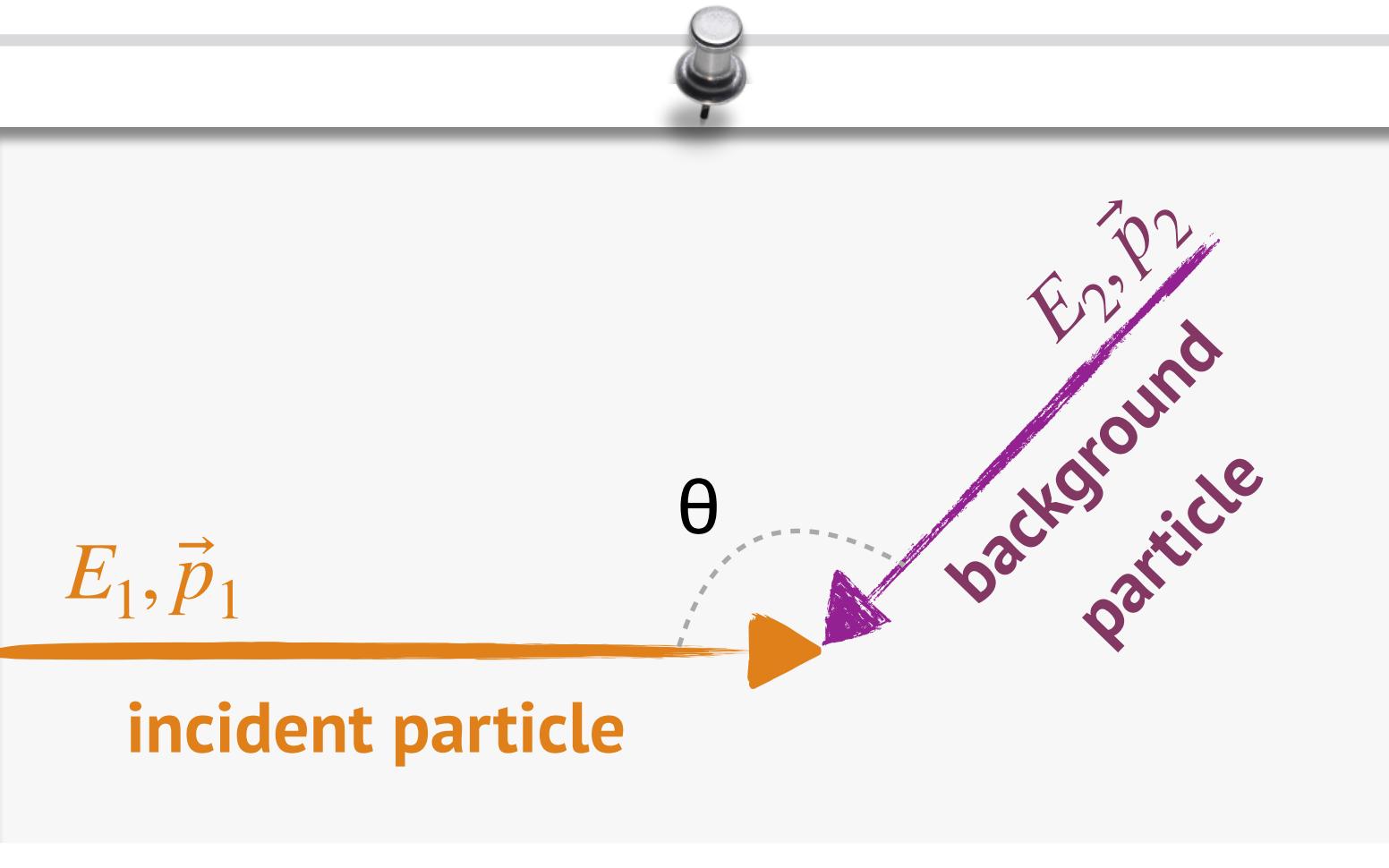
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interaction length

for particle of type 1
interacting with (isotropic)
background of type 2

interactions and mean free path



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centre of mass energy

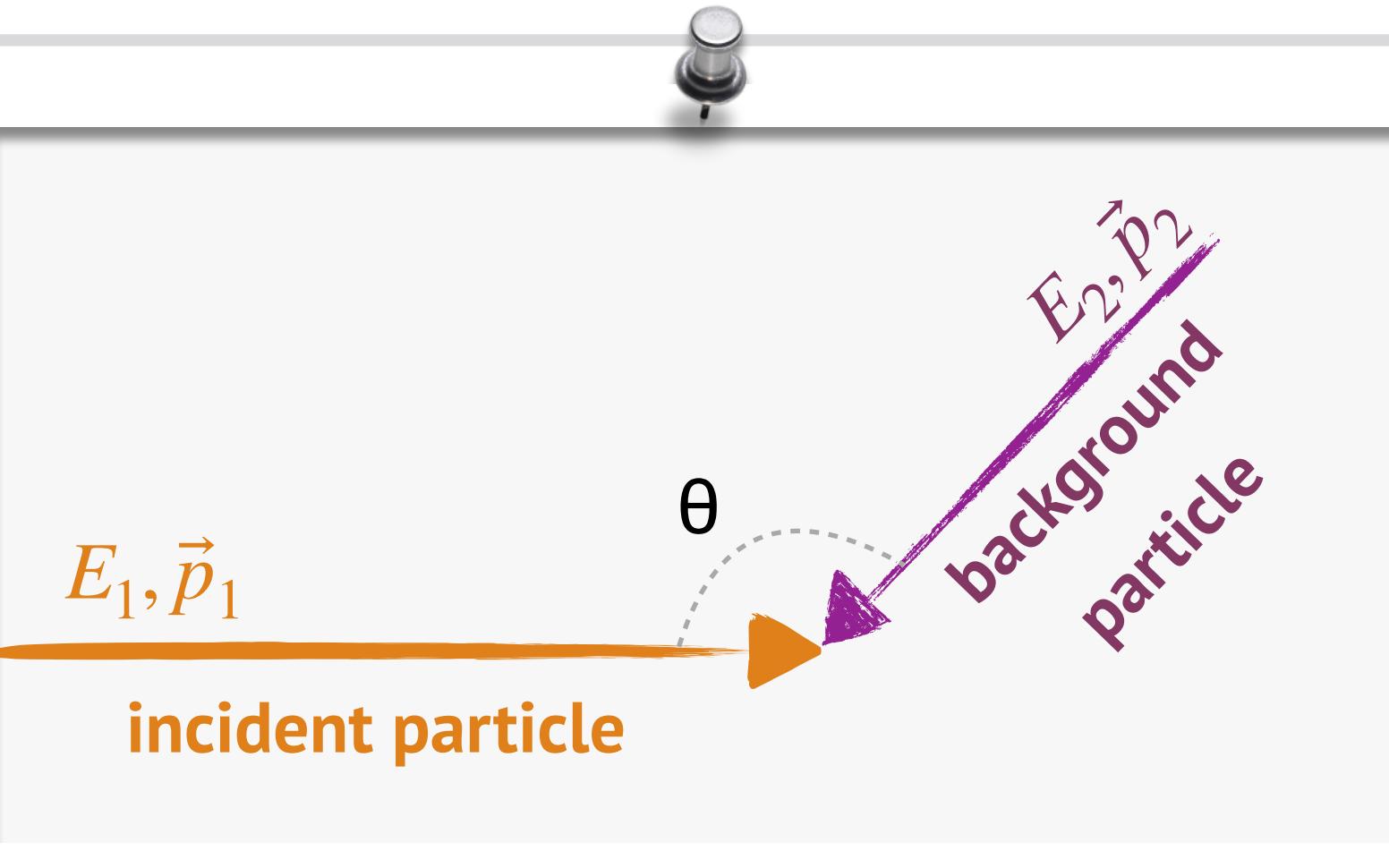
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generic $\lambda^{-1} = \frac{1}{2} \iint dp_2 \, d\cos \theta \, \sigma(s) \, \beta_{\text{rel}}(P_1, P_2) \, (1 - \beta_1 \beta_2 \cos \theta) \, \frac{dn_2(\vec{p}_2)}{dp_2}$

interactions and mean free path



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photons

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$$\lambda^{-1}(E, z) = \frac{1}{8\beta E^2} \int_{\varepsilon_{\min}(E)}^{+\infty} \frac{1}{\varepsilon^2} \frac{dn(\varepsilon, z)}{d\varepsilon} \int_{s_{\min}}^{s_{\max}(E, \varepsilon)} (s - m^2 c^4) \sigma(s) \, ds \, d\varepsilon$$

modified interactions with photon backgrounds

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can we use the same equation
with Lorentz violation?

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change:

$\varepsilon_{\min}, s, s_{\min}, s_{\max}, \beta_{\text{rel}}$

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necessary conditions to state the a flux of a messenger is primary

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- ▶ know the **intrinsic spectrum** well to exclude **cascade contribution**
 - ◆ *but:* unobserved gamma rays at higher energies

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necessary conditions to state the a flux of a messenger is primary

- ▶ know the **intrinsic spectrum** well to exclude **cascade contribution**
 - ◆ *but:* unobserved gamma rays at higher energies
- ▶ know the **flux of other particles** along the **line of sight**
 - ◆ degeneracy between absorption of parent and observations of the messenger

cosmic rays

LIV-induced modifications

$$E^2 = m_a^2 c^4 + p^2 c^2 + f_a(E, \vec{p})$$

$$f_a(E, \vec{p}) \approx f_a(p) = p^2 c^2 \sum_{n=0}^{\infty} \chi_n^{(a)} \left(\frac{pc}{E_{\star}} \right)^n$$

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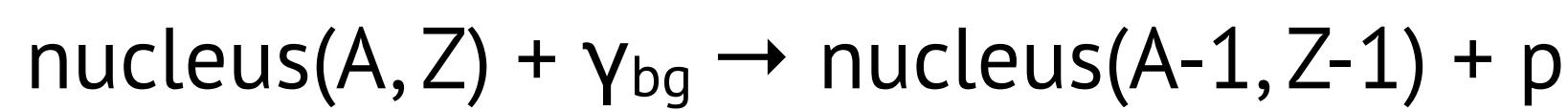
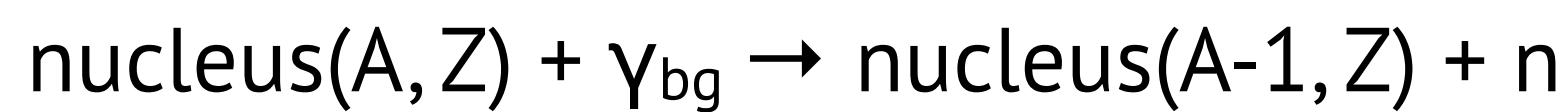
photodisintegration

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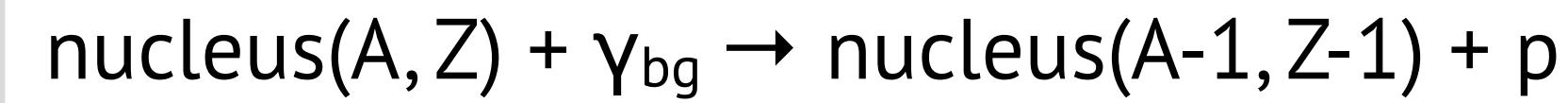
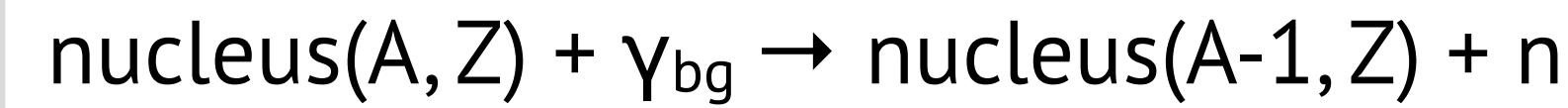
modified interaction thresholds

LIV-induced modifications

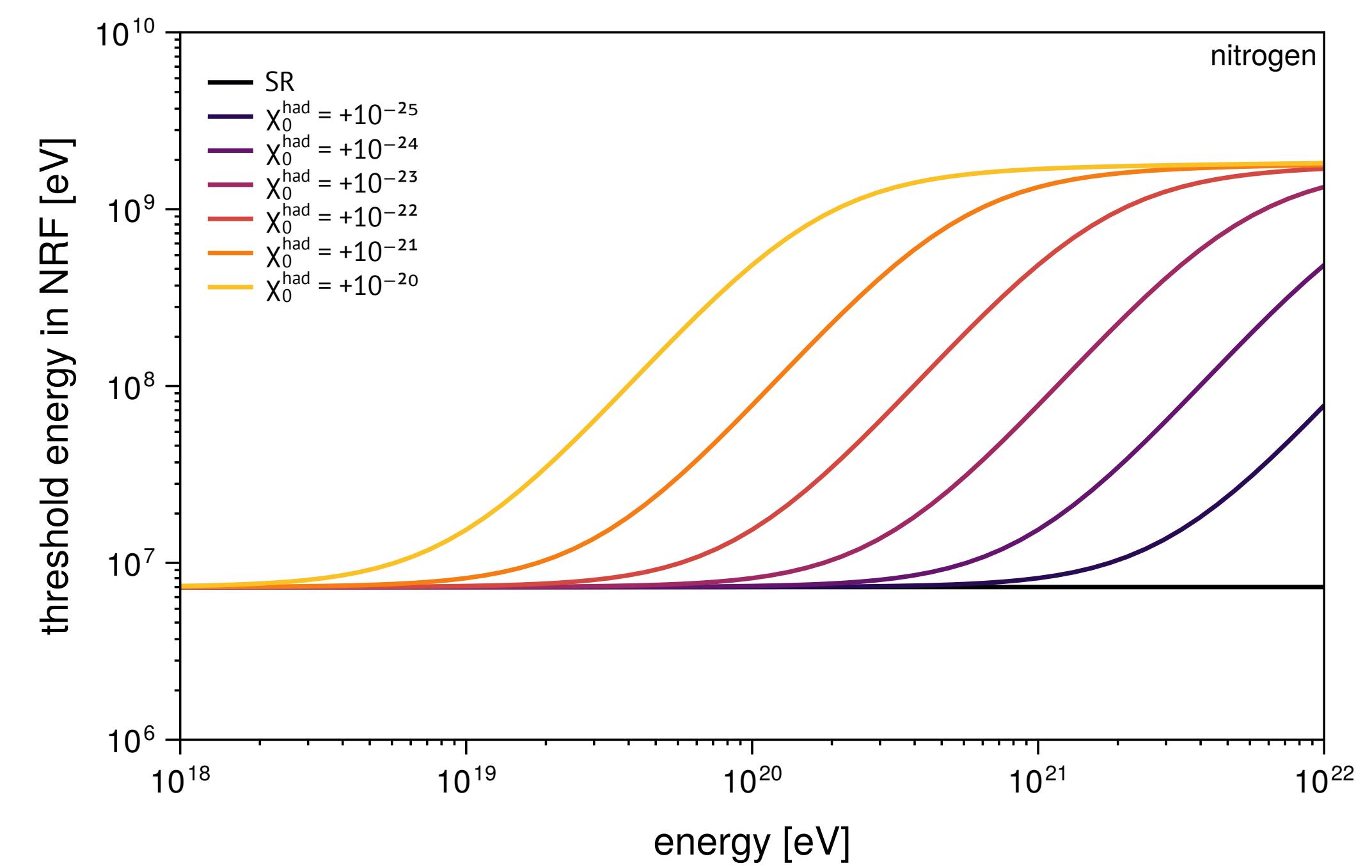
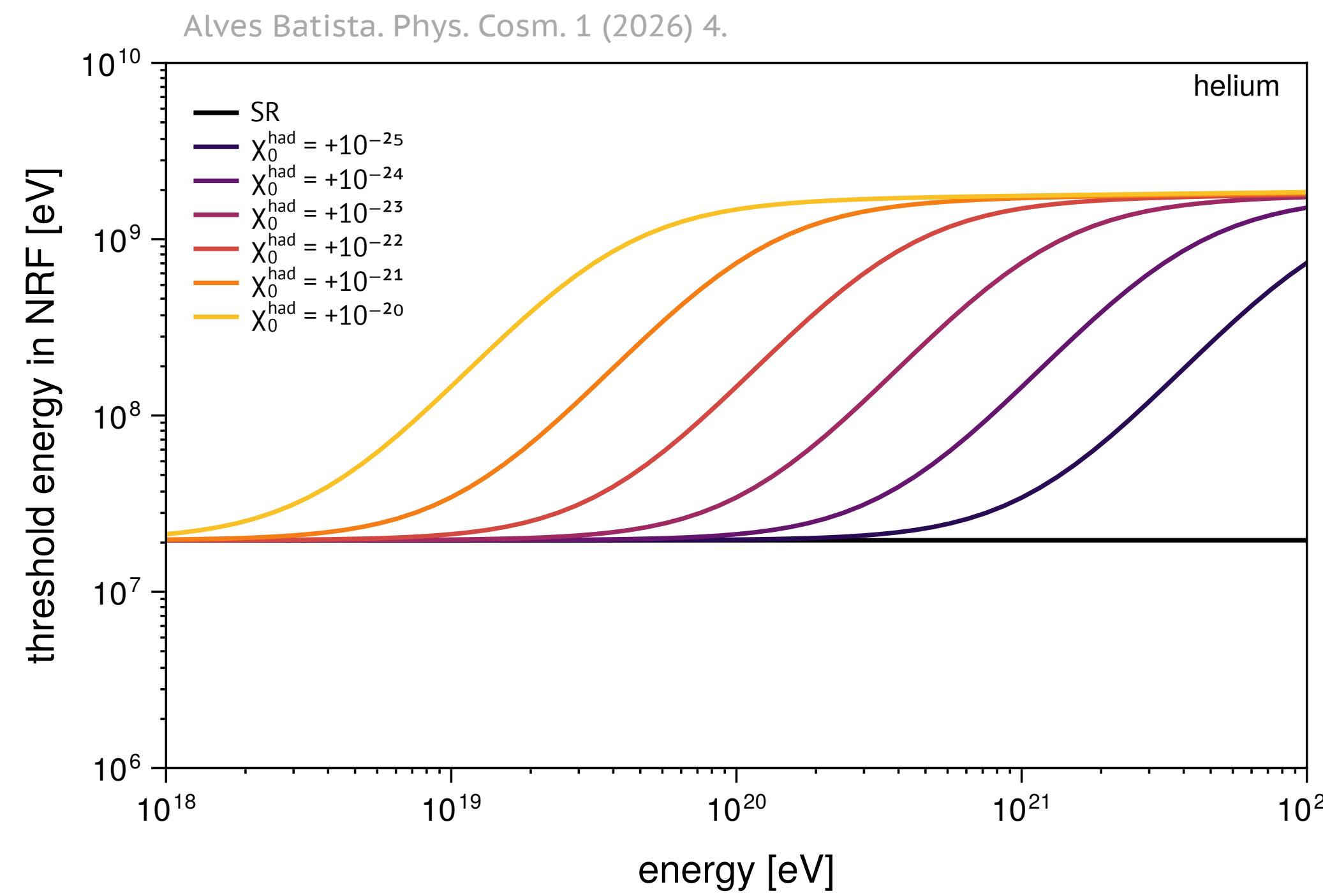
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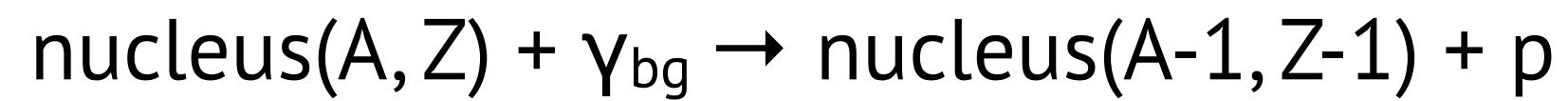
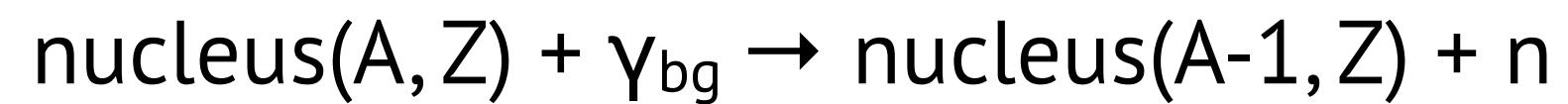
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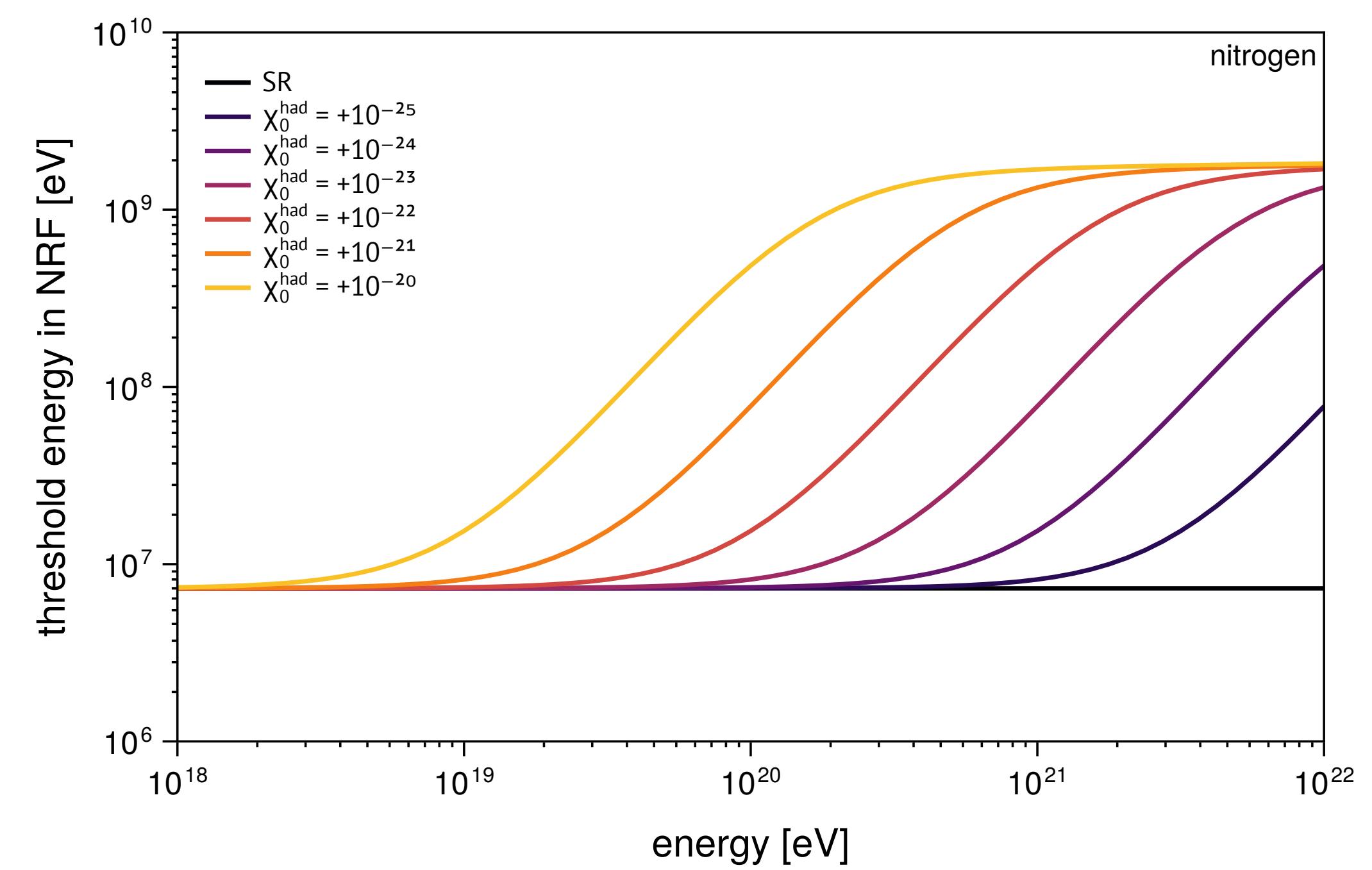
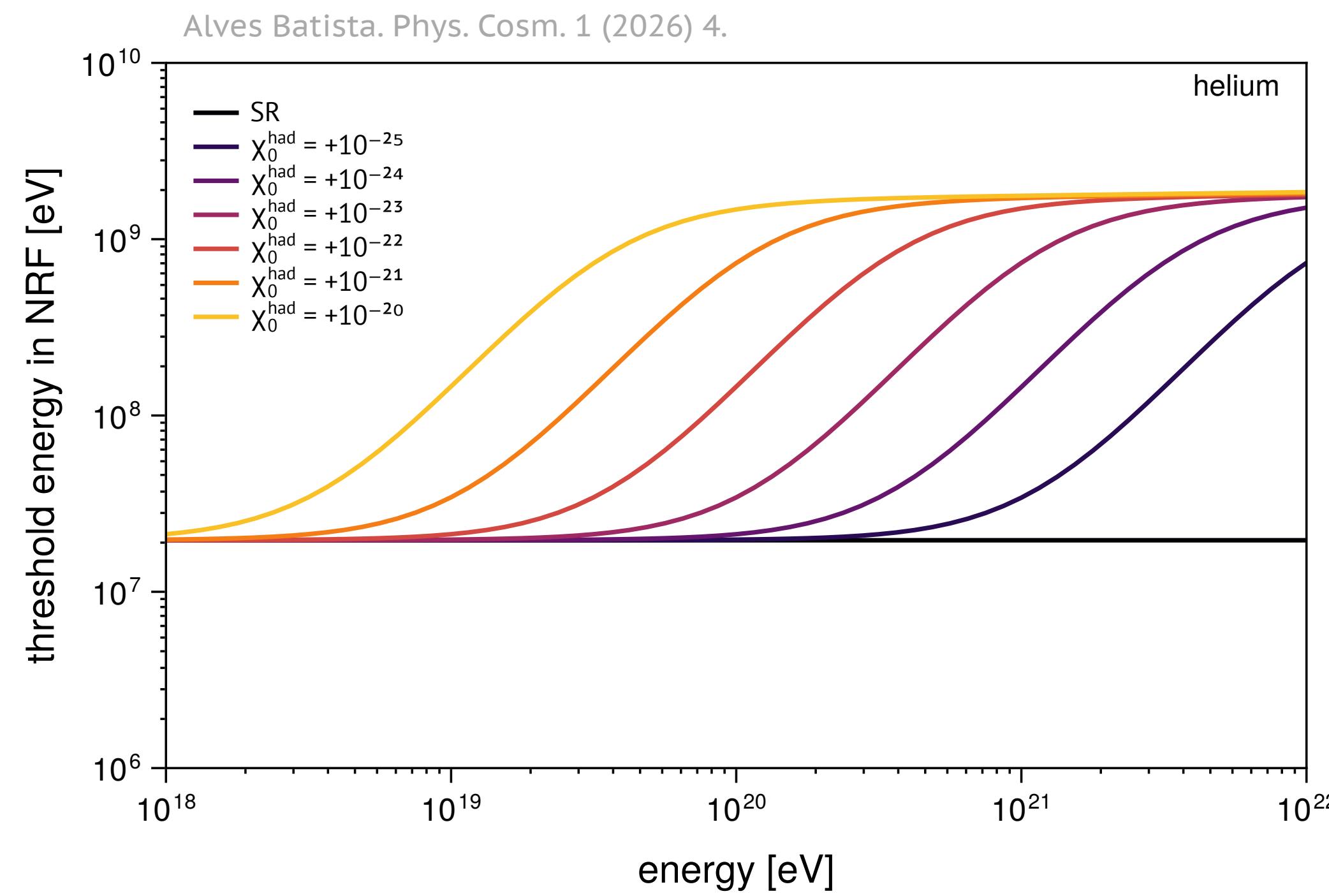
photodisintegration



....



cosmogenic particles

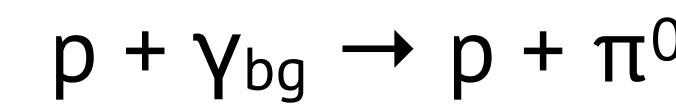


LIV-induced modifications

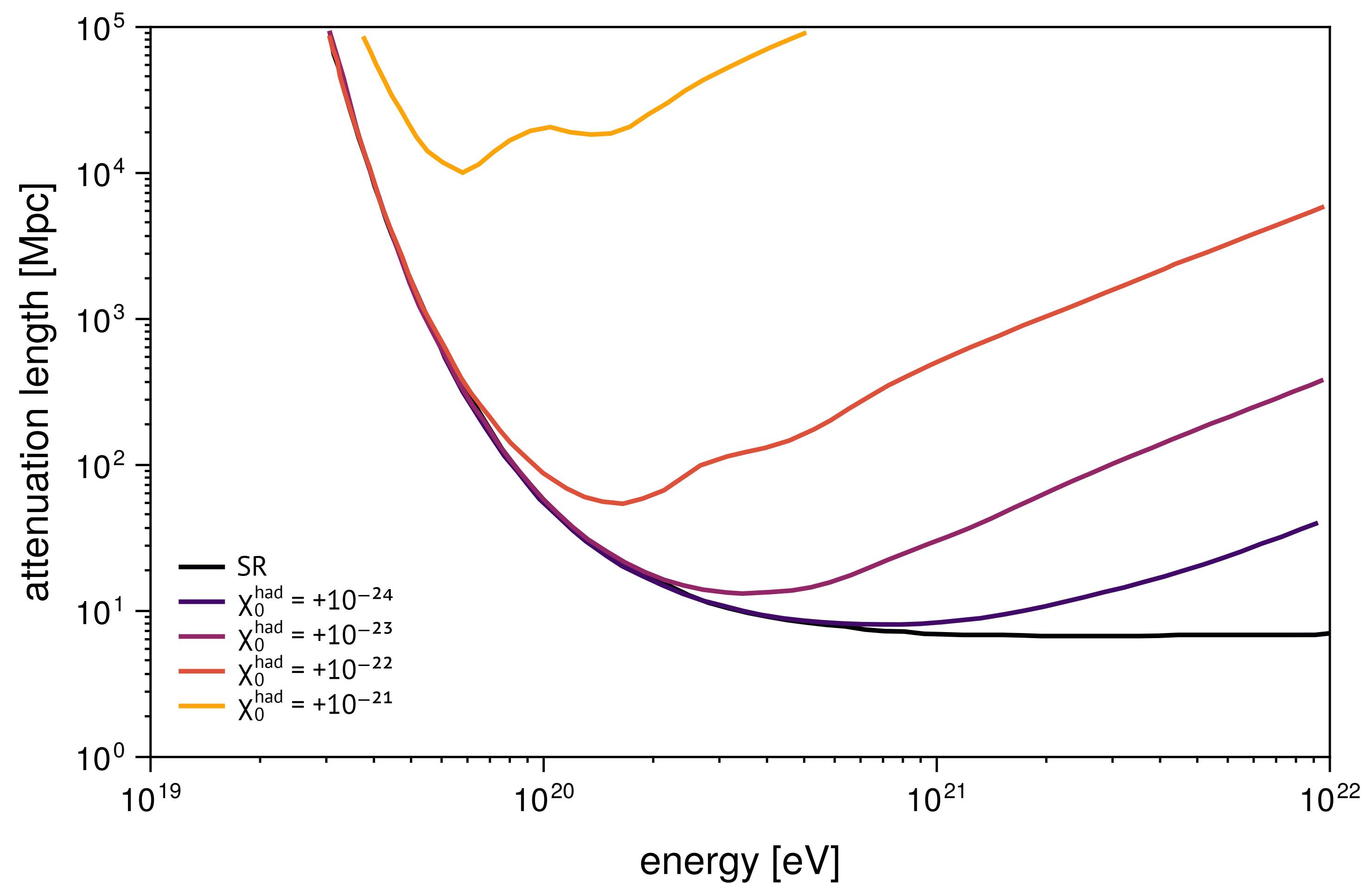
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photoproduction of mesons



(similar for nuclei)

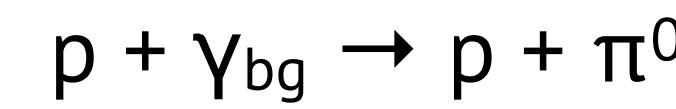


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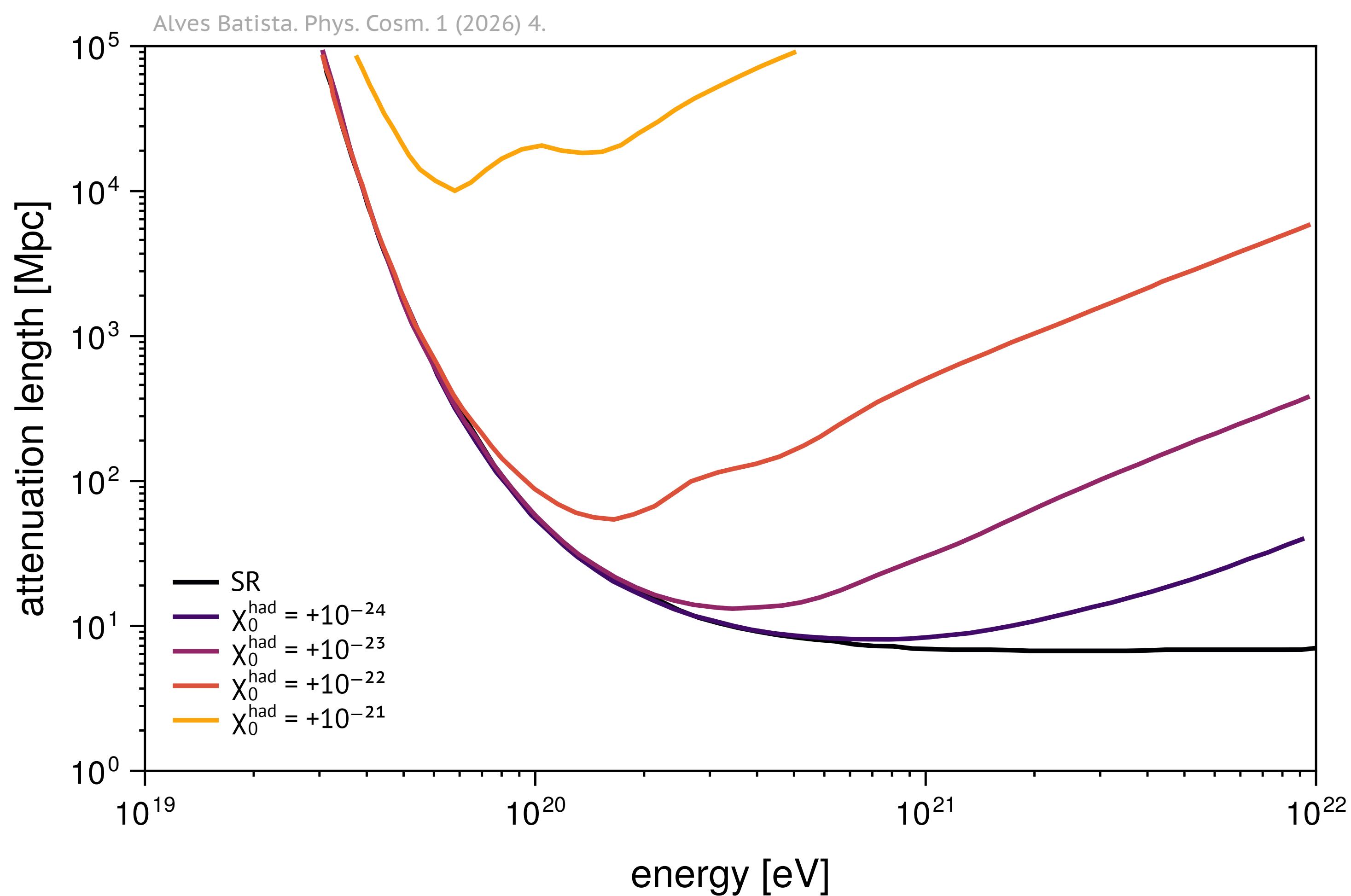
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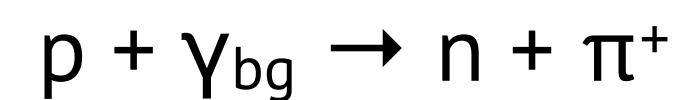
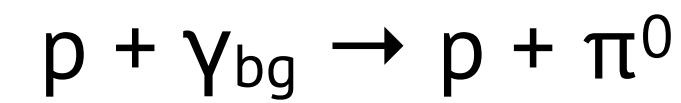


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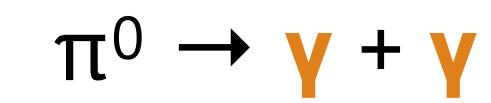
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$$f_a(E, \vec{p}) \approx f_a(p) = p^2 c^2 \sum_{n=0}^{\infty} \chi_n^{(a)} \left(\frac{pc}{E_{\star}} \right)^n$$

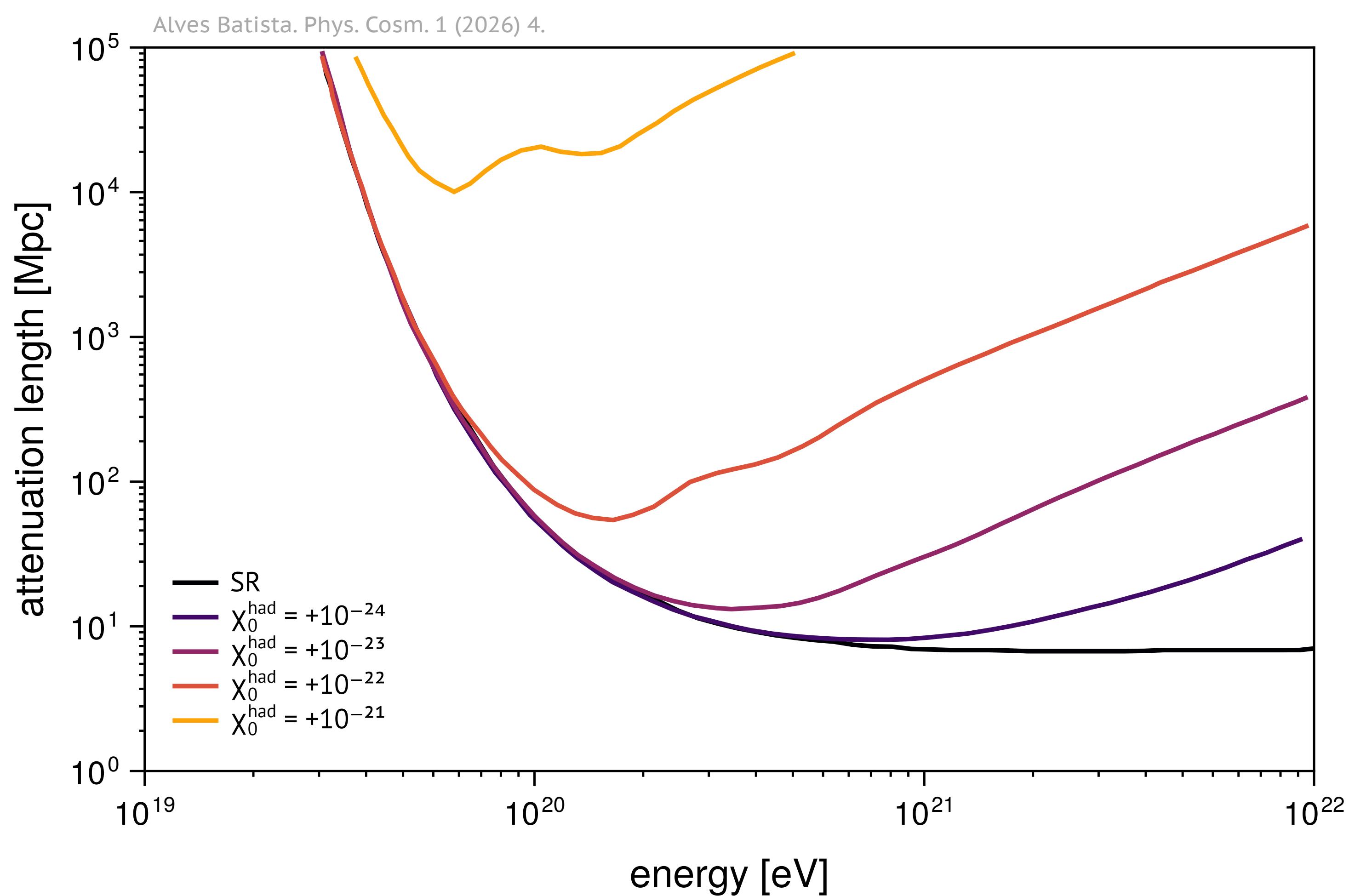
photoproduction of mesons

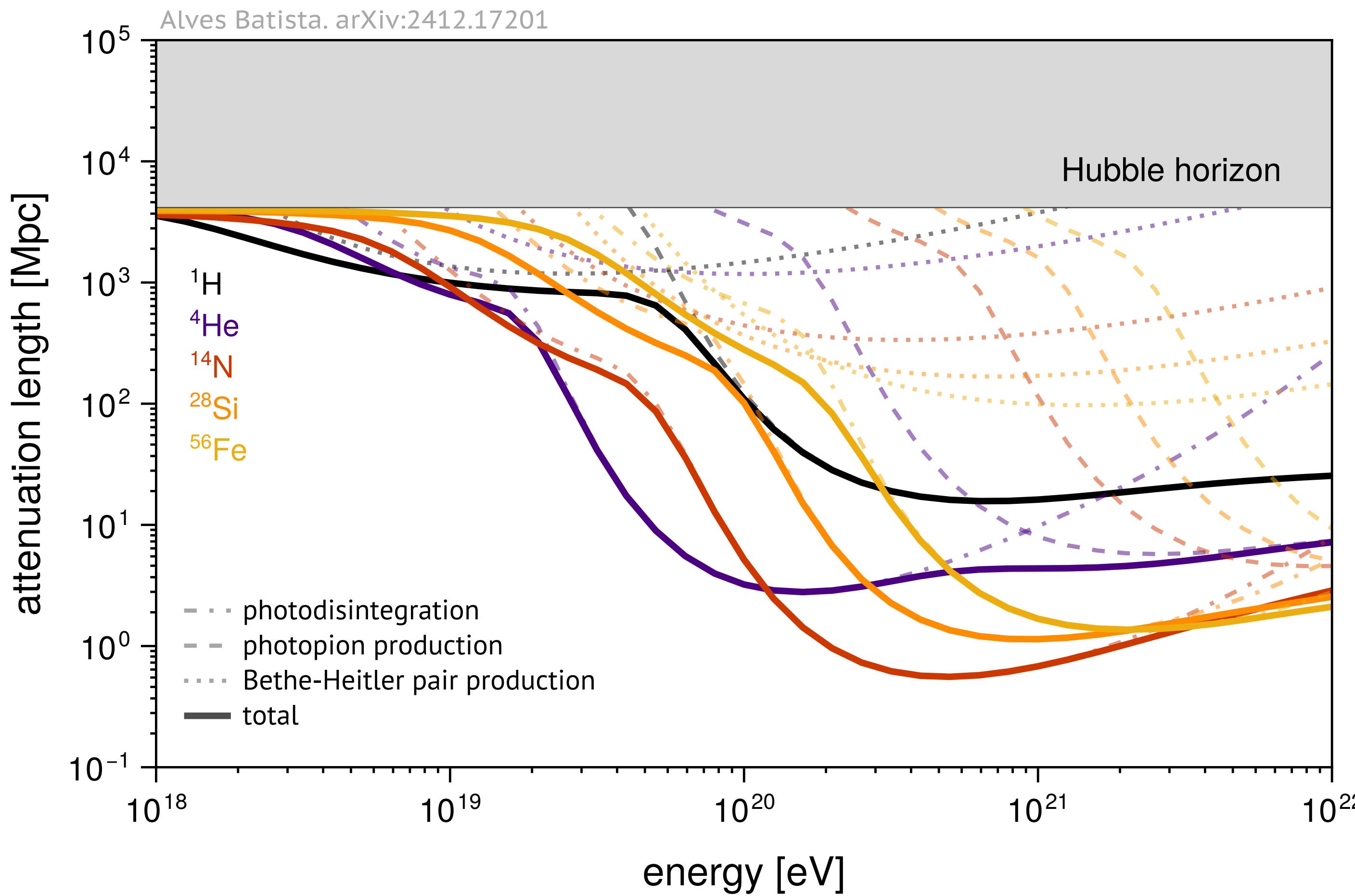


(similar for nuclei)

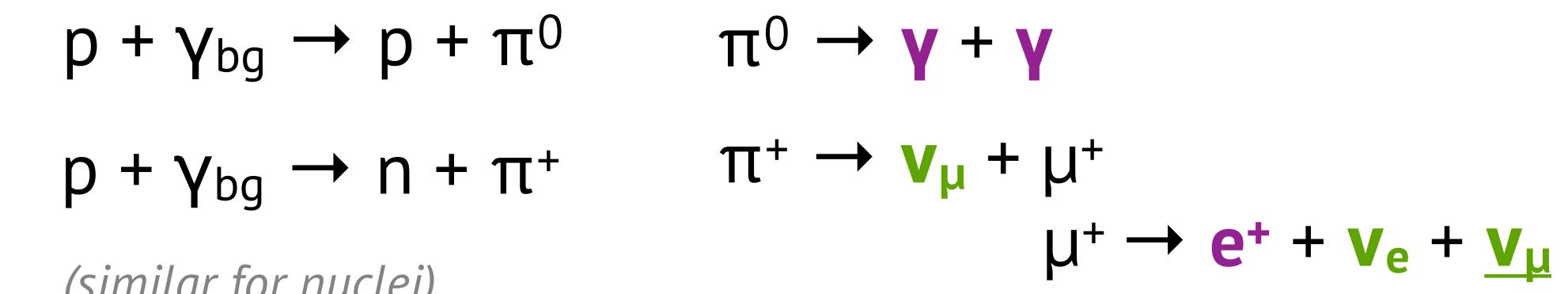


cosmogenic particles

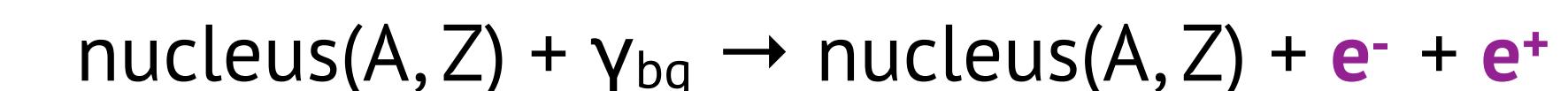




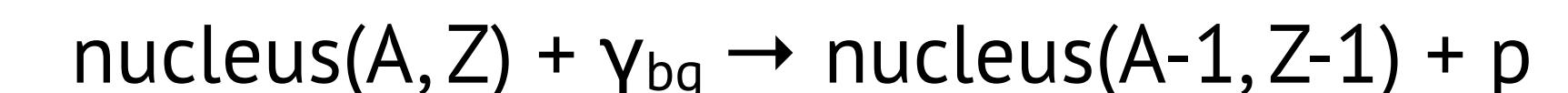
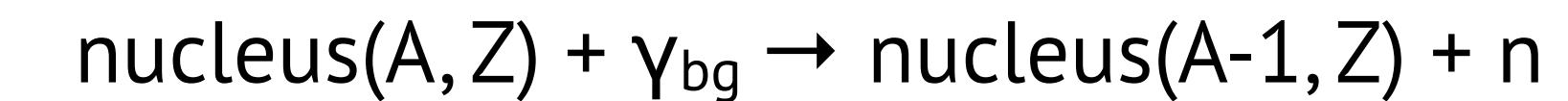
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Bethe-Heitler pair production

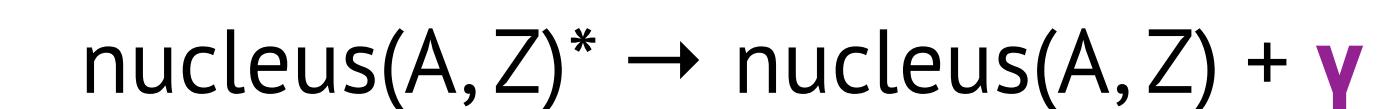


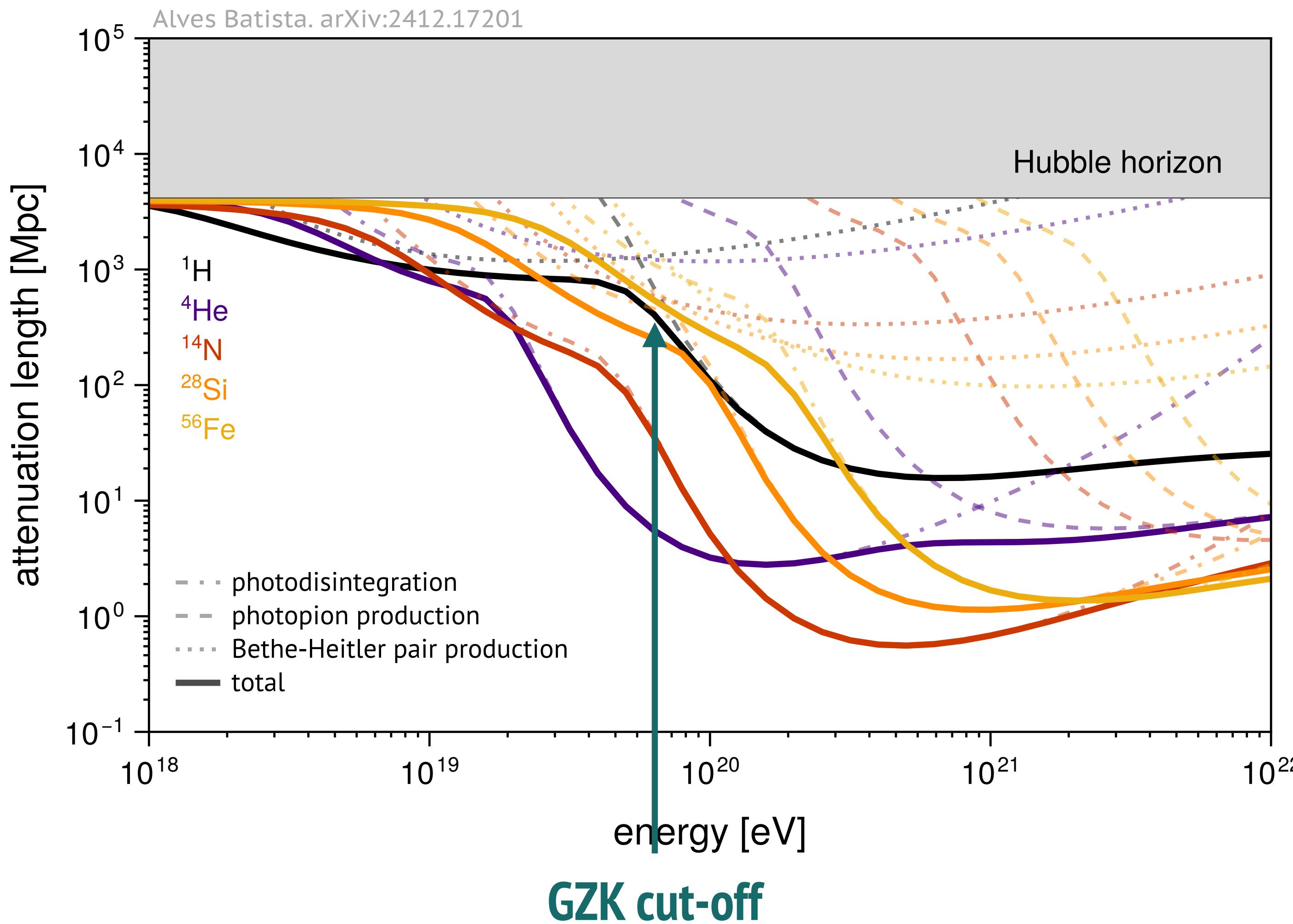
photodisintegration



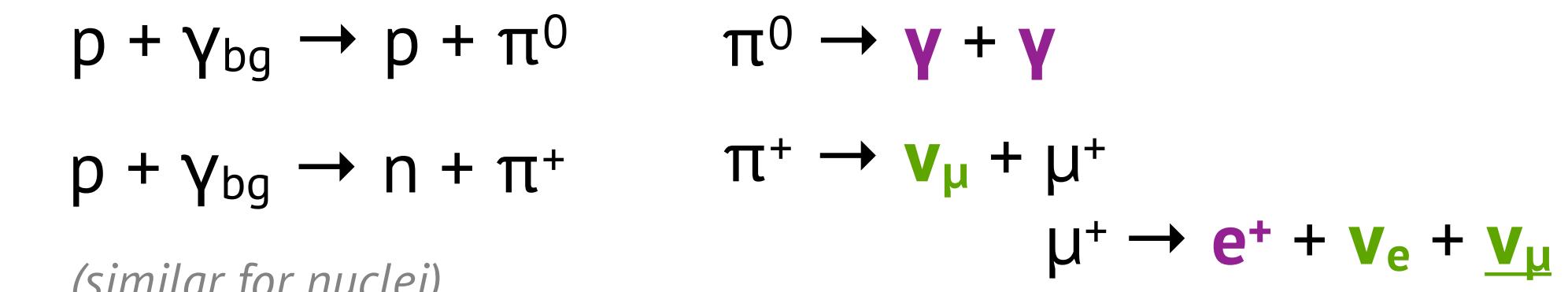
...

nuclear decays

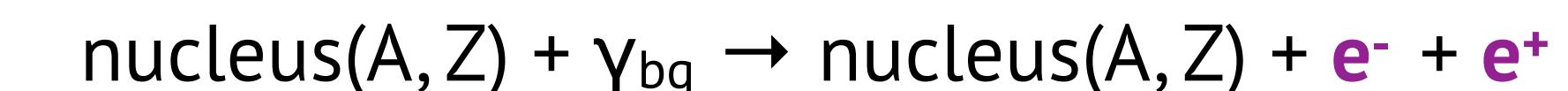




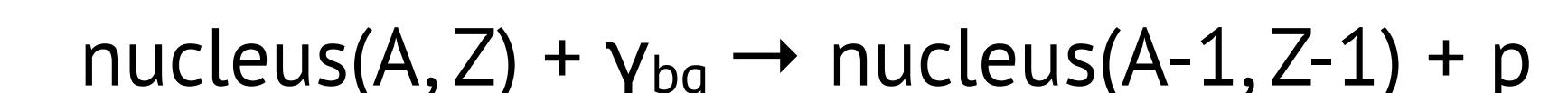
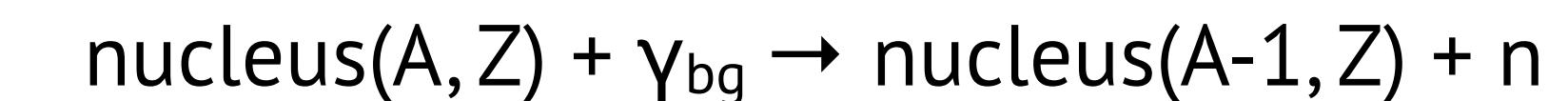
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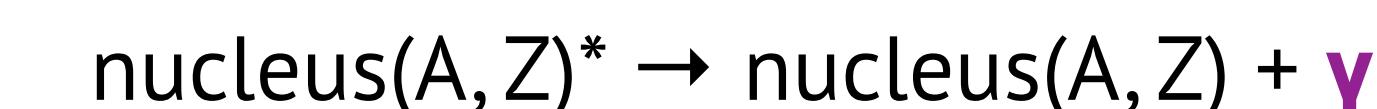


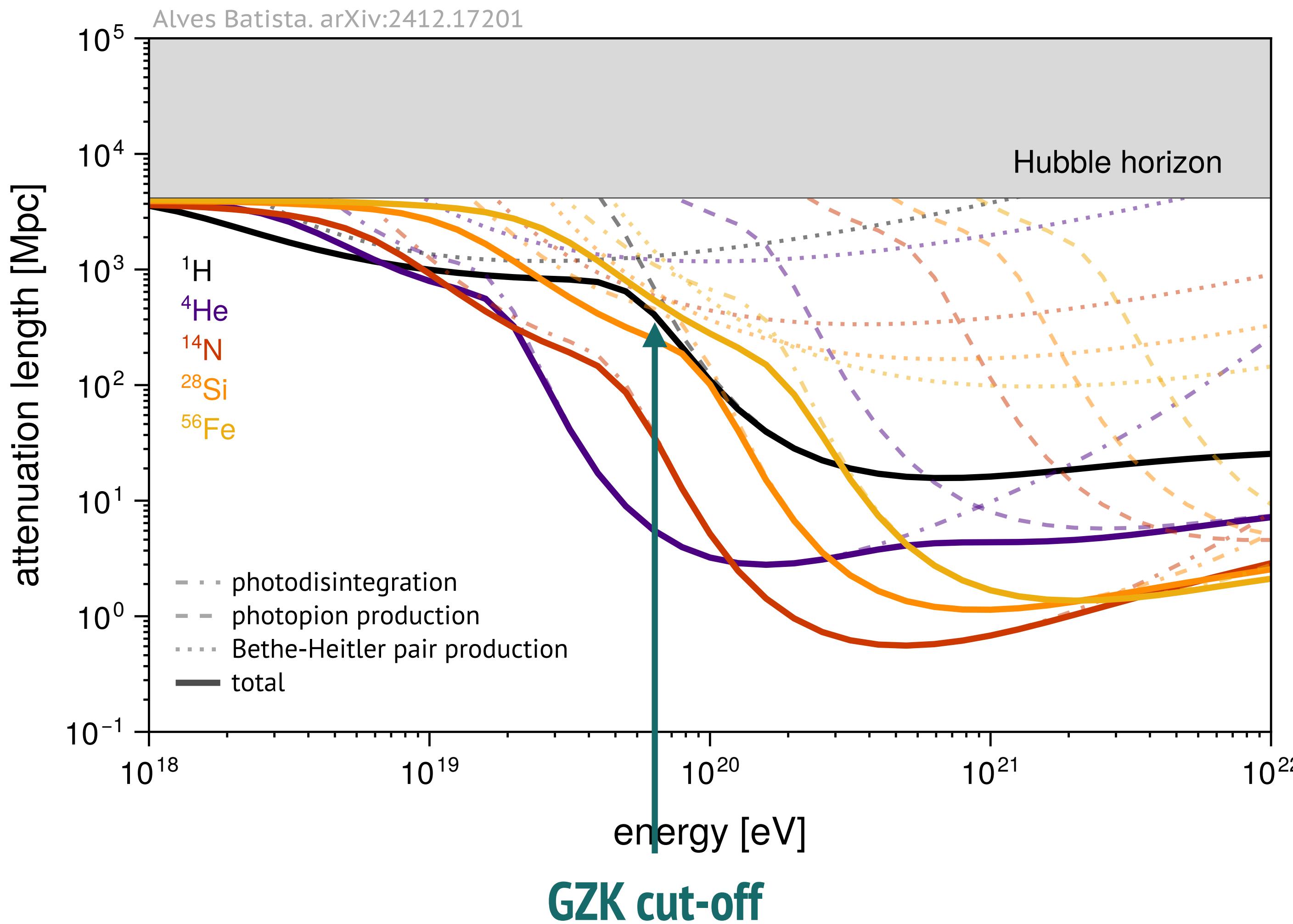
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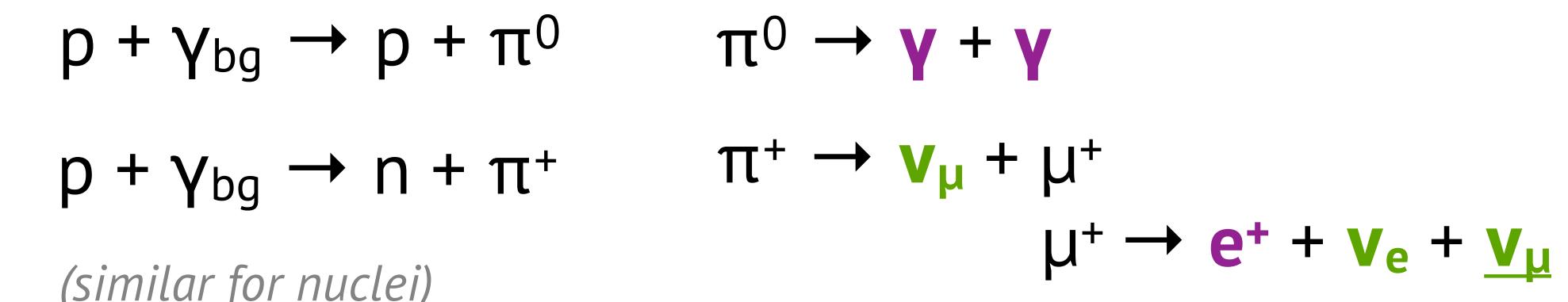




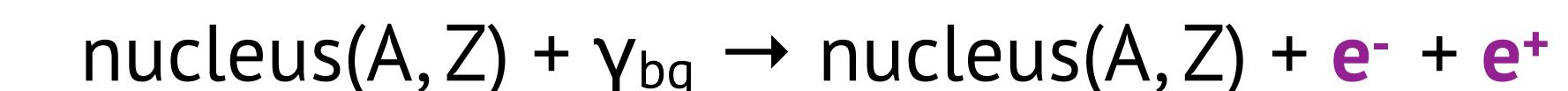
$$s = m^2 + 2E\varepsilon(1 - \beta \cos \theta)$$

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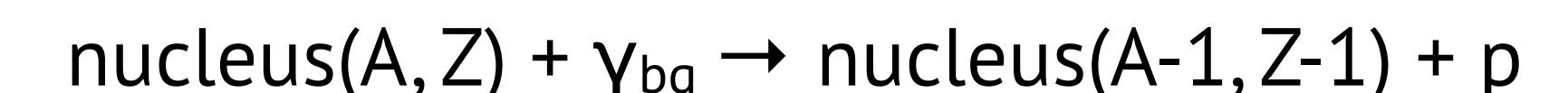
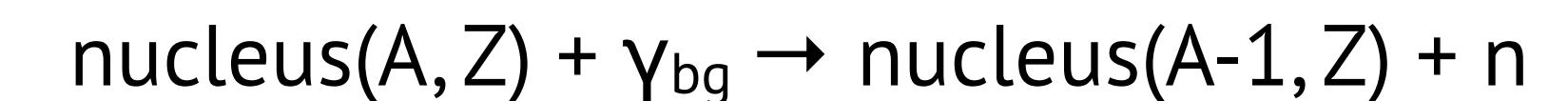
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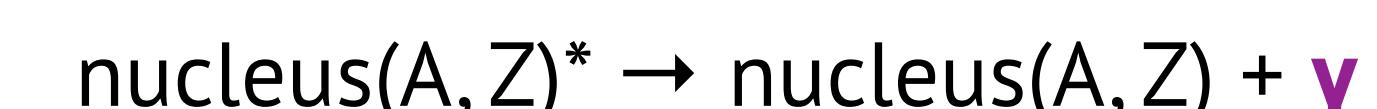


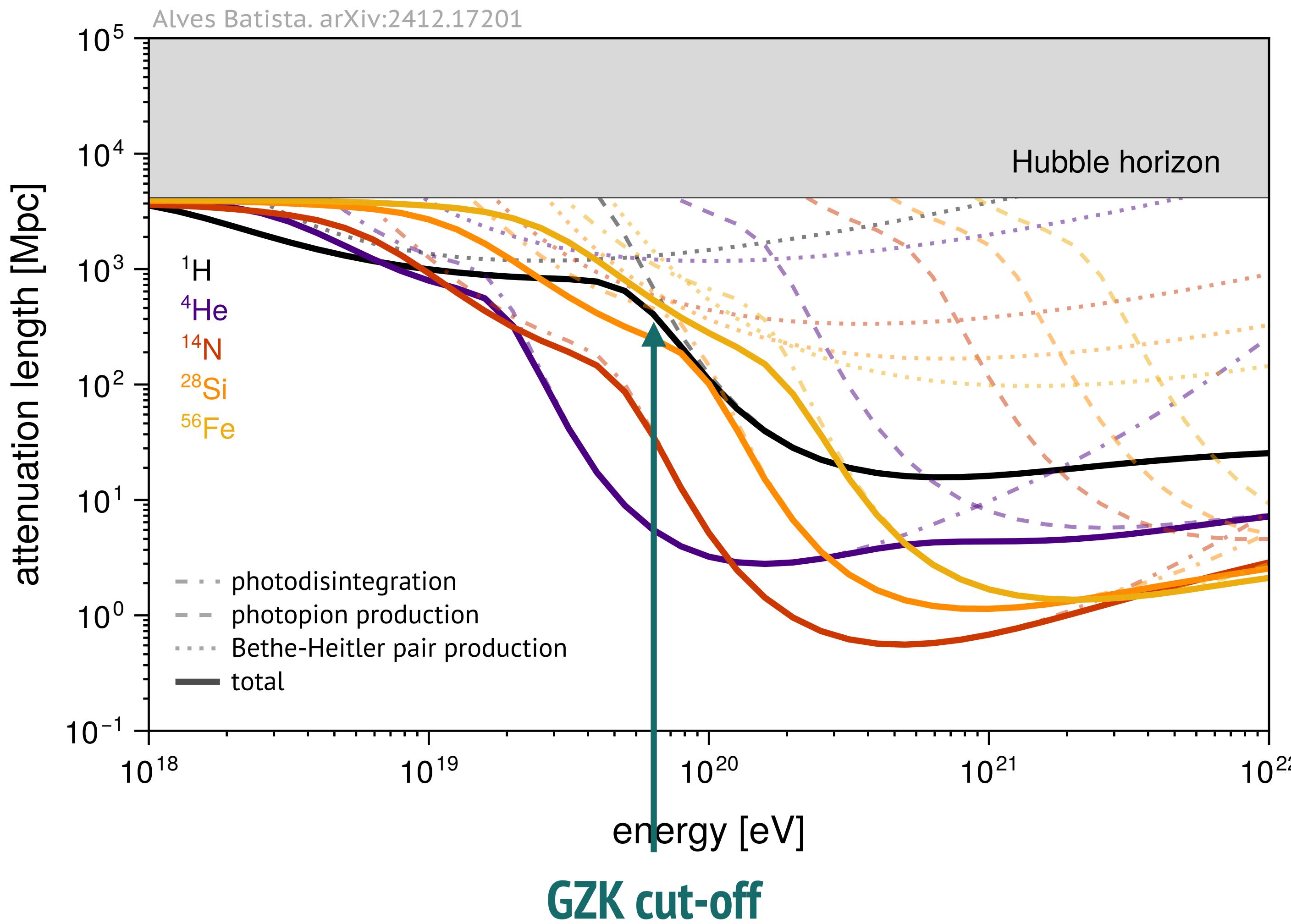
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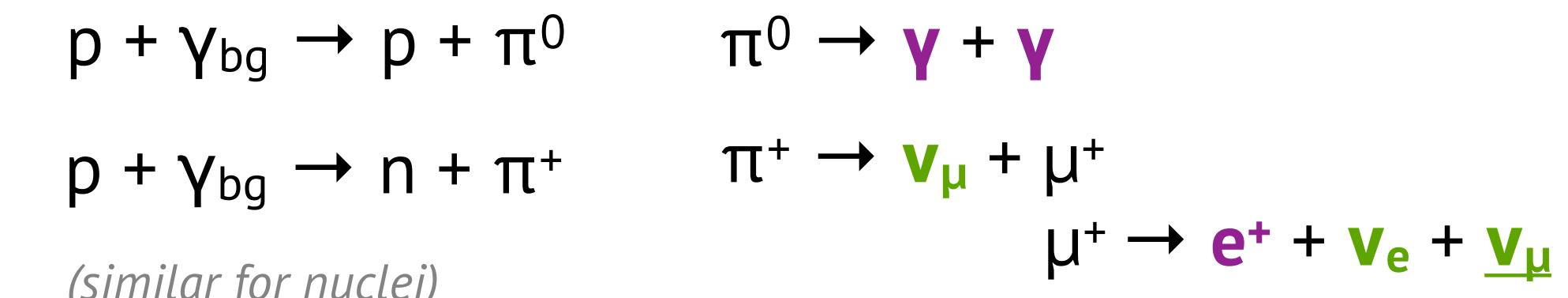


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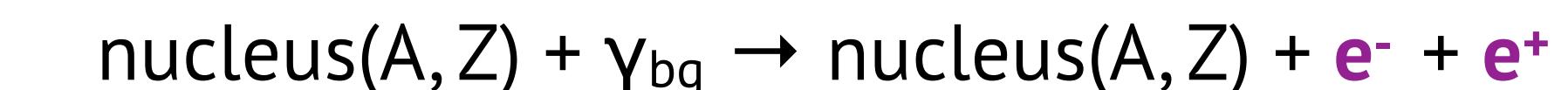
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$$E_{\text{GZK}} \simeq 6 \text{ EeV} \equiv 6 \times 10^{19} \text{ eV}$$

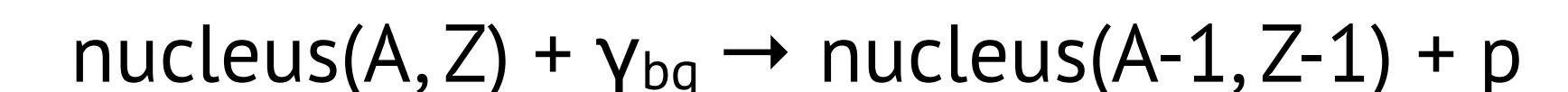
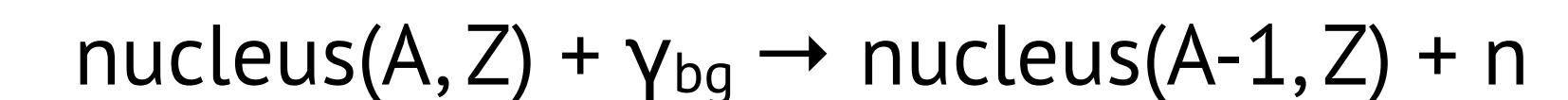
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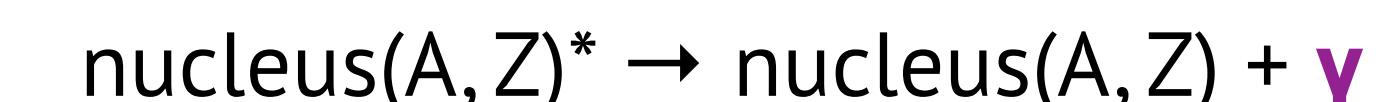


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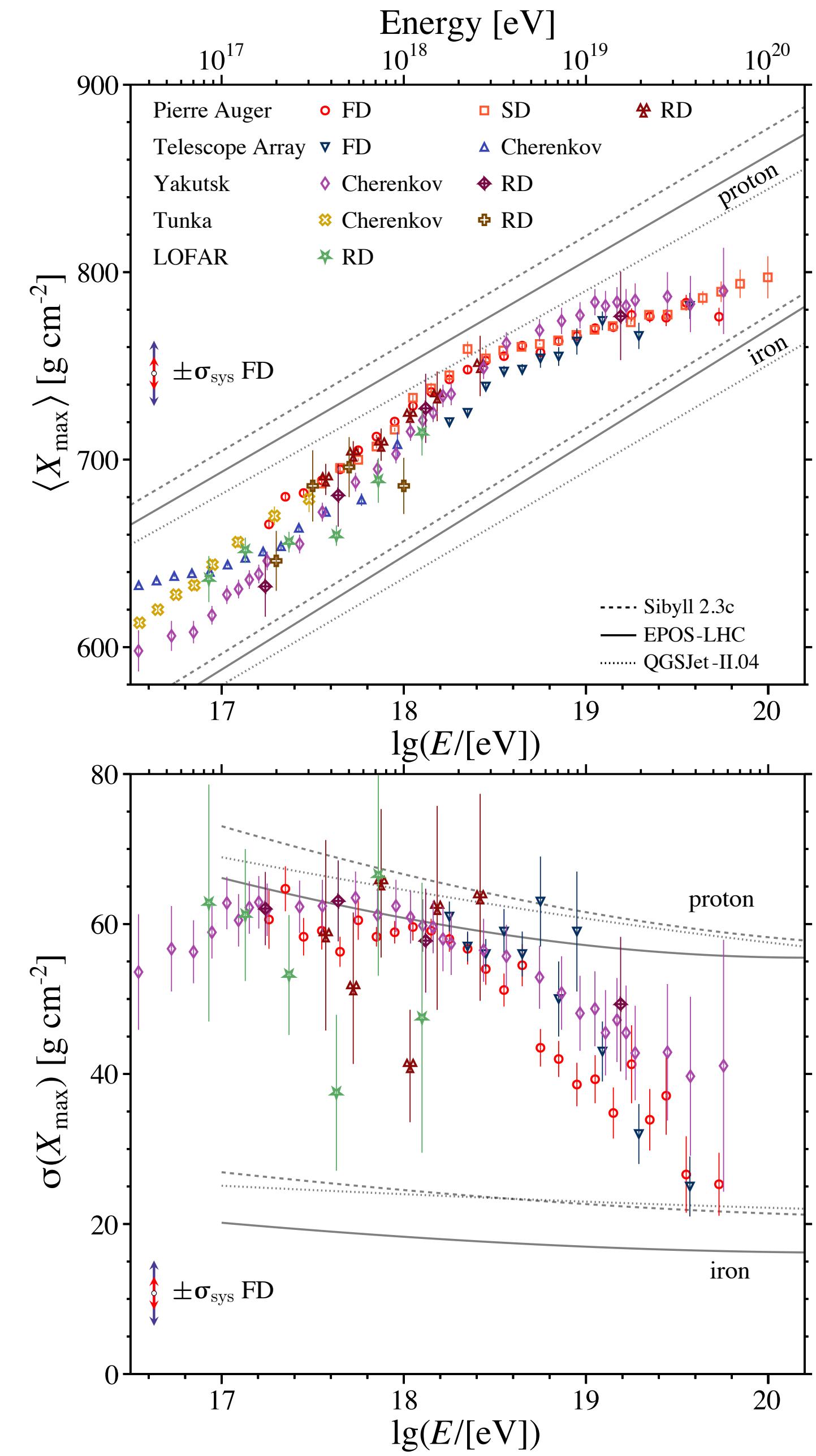
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self-consistent constraints in hadronic sector

Coleman et al. Astroparticle Physics 149 (2023) 102819. arXiv:2205.05845

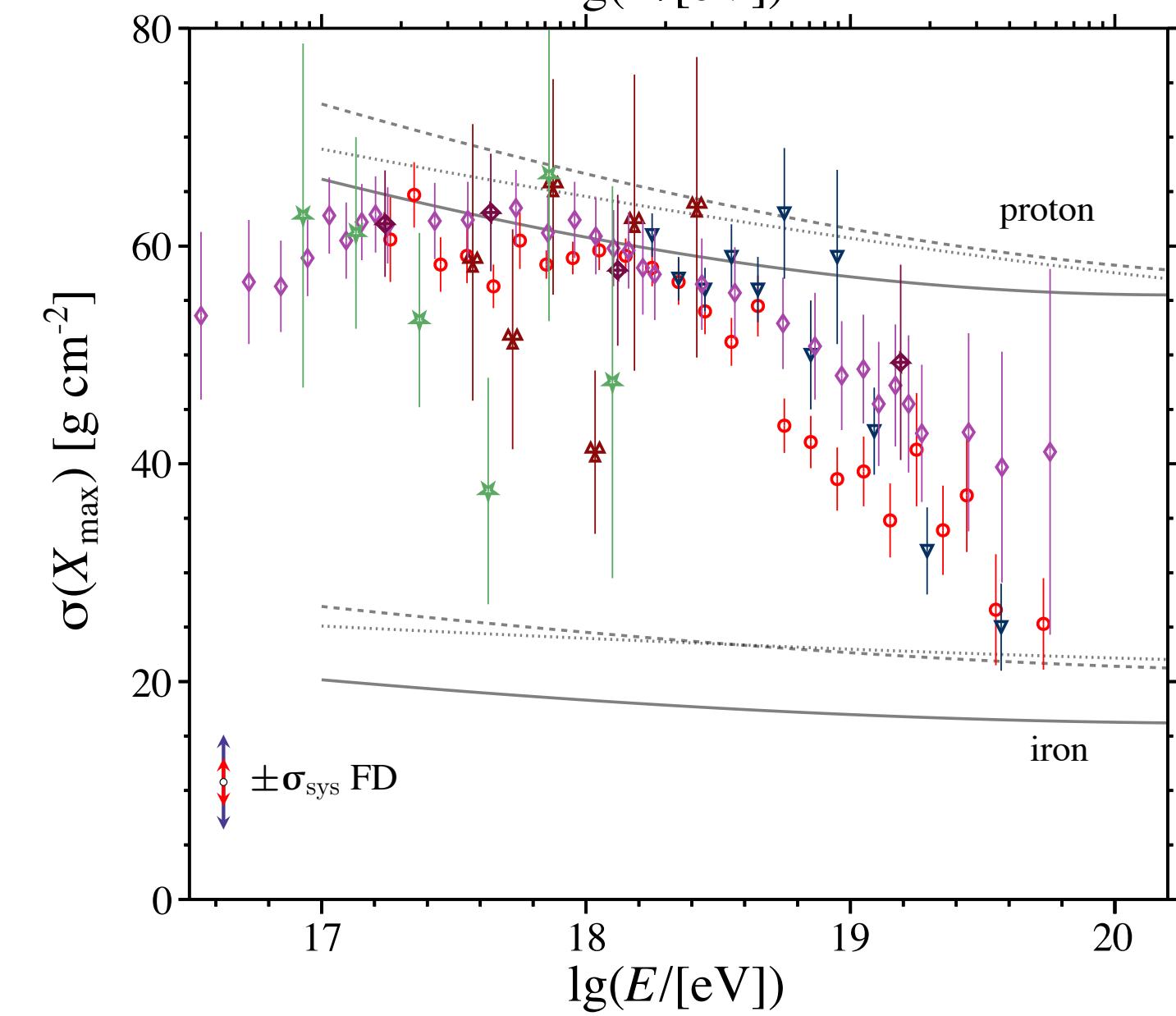
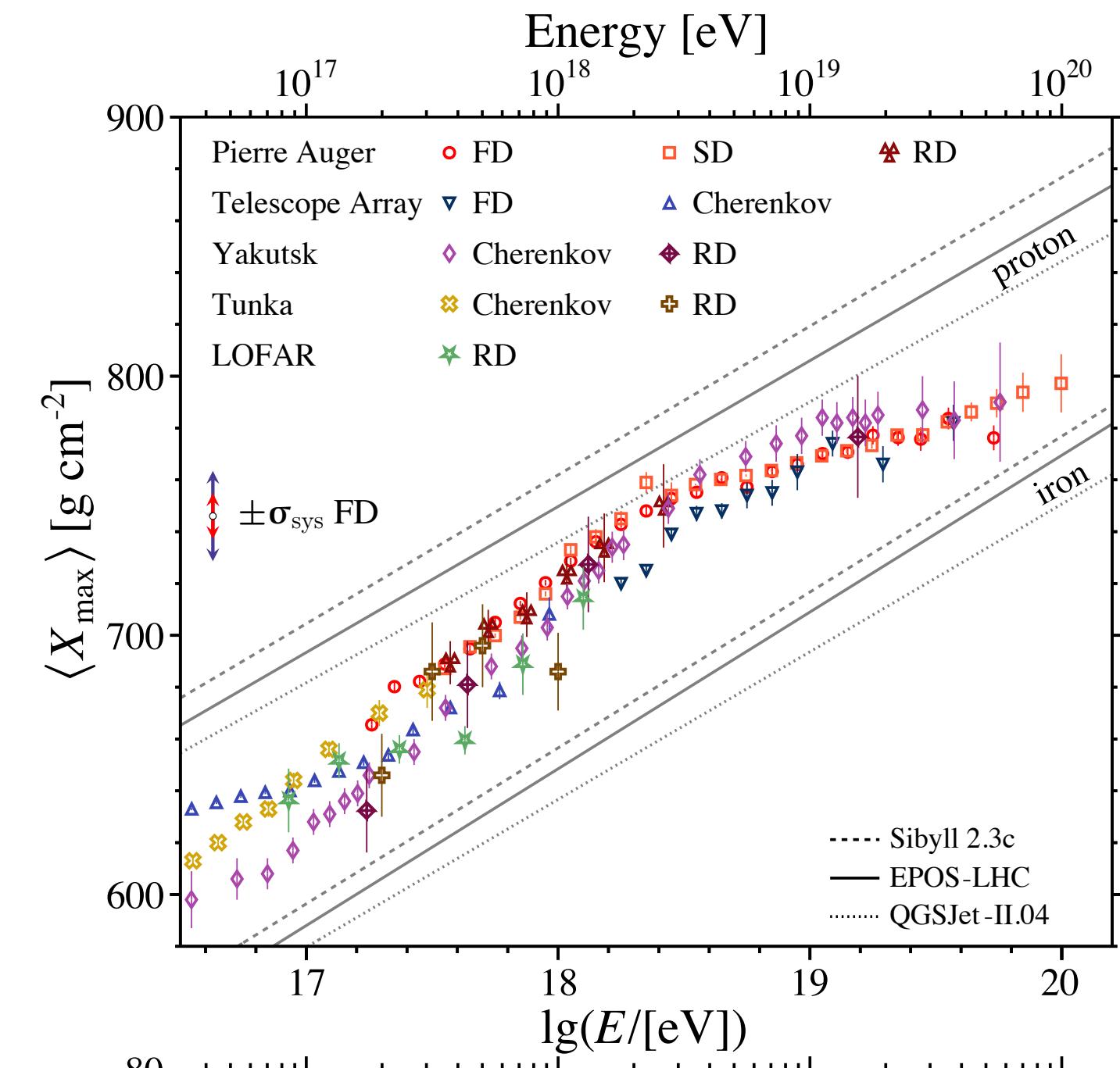
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- ▶ **problem:** effects in the hadronic sector also affects the showers
- ▶ what we measure is X_{\max}
- ▶ **how to tackle that?** LIV-CORSIKA working group



gamma rays

the usual approach to gamma-ray propagation

the usual approach to gamma-ray propagation

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attenuation

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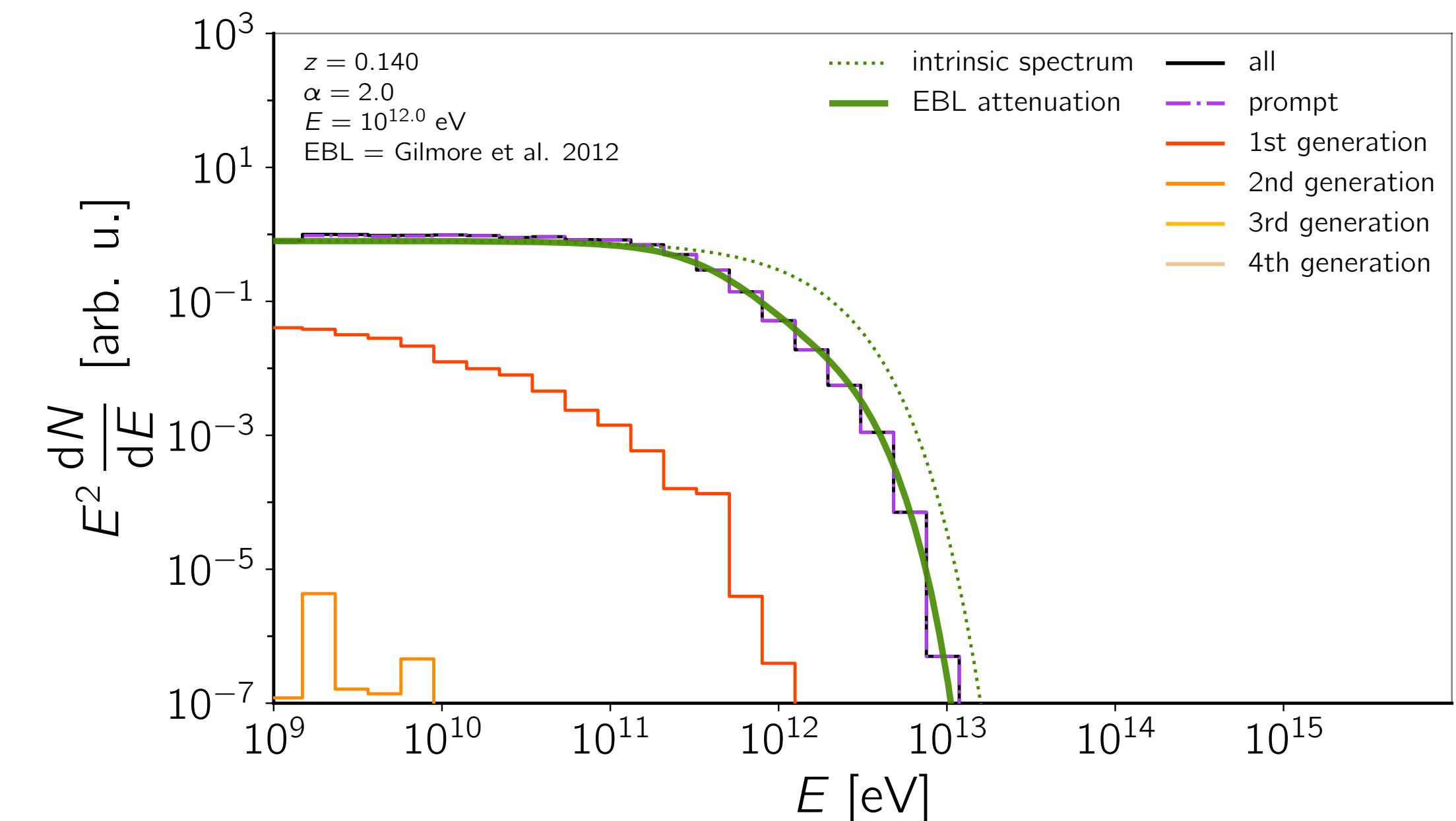
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simulations performed with **CRPropa**

Alves Batista et al. JCAP 05 (2016) 038. arXiv:1603.07142

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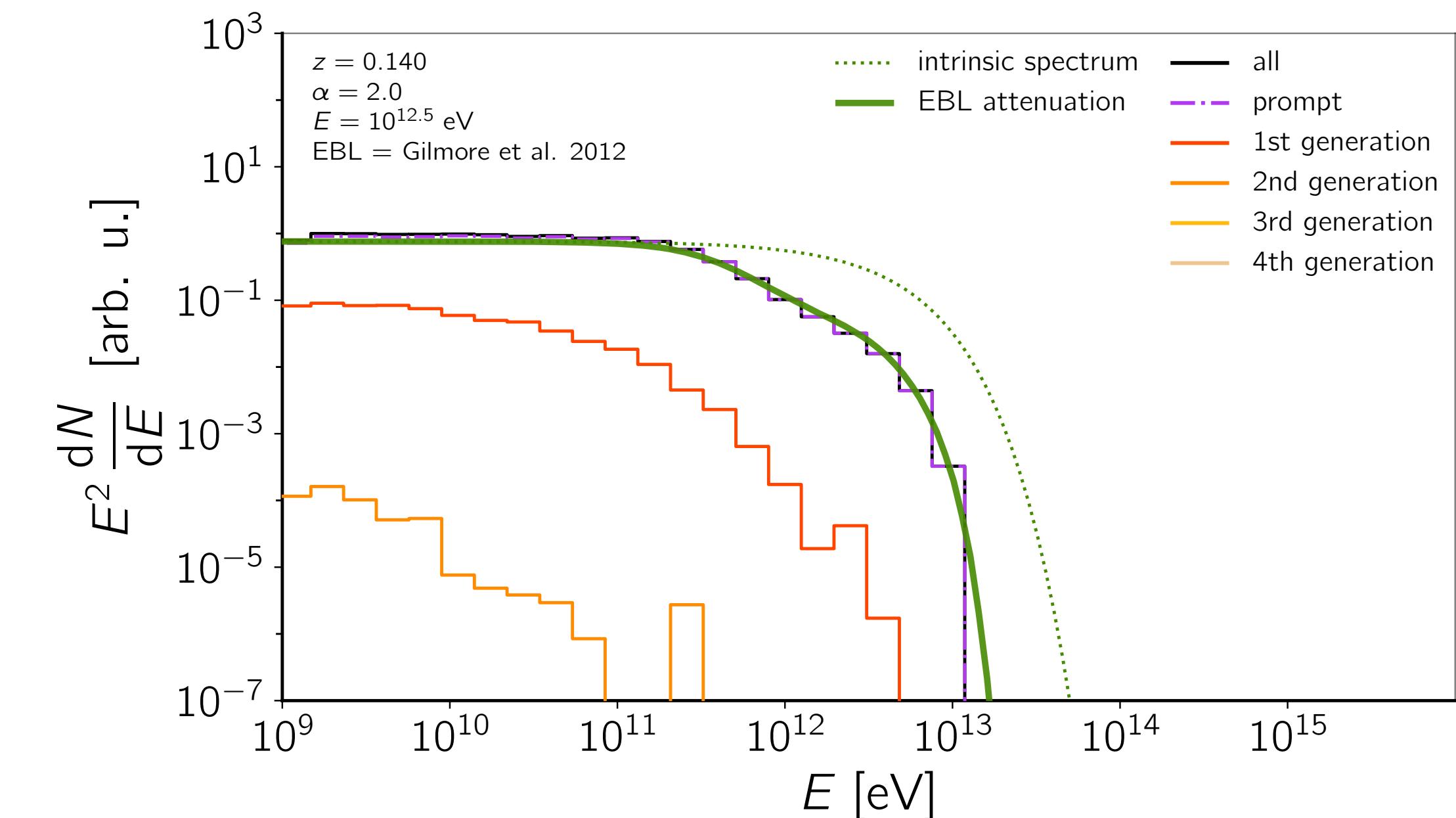
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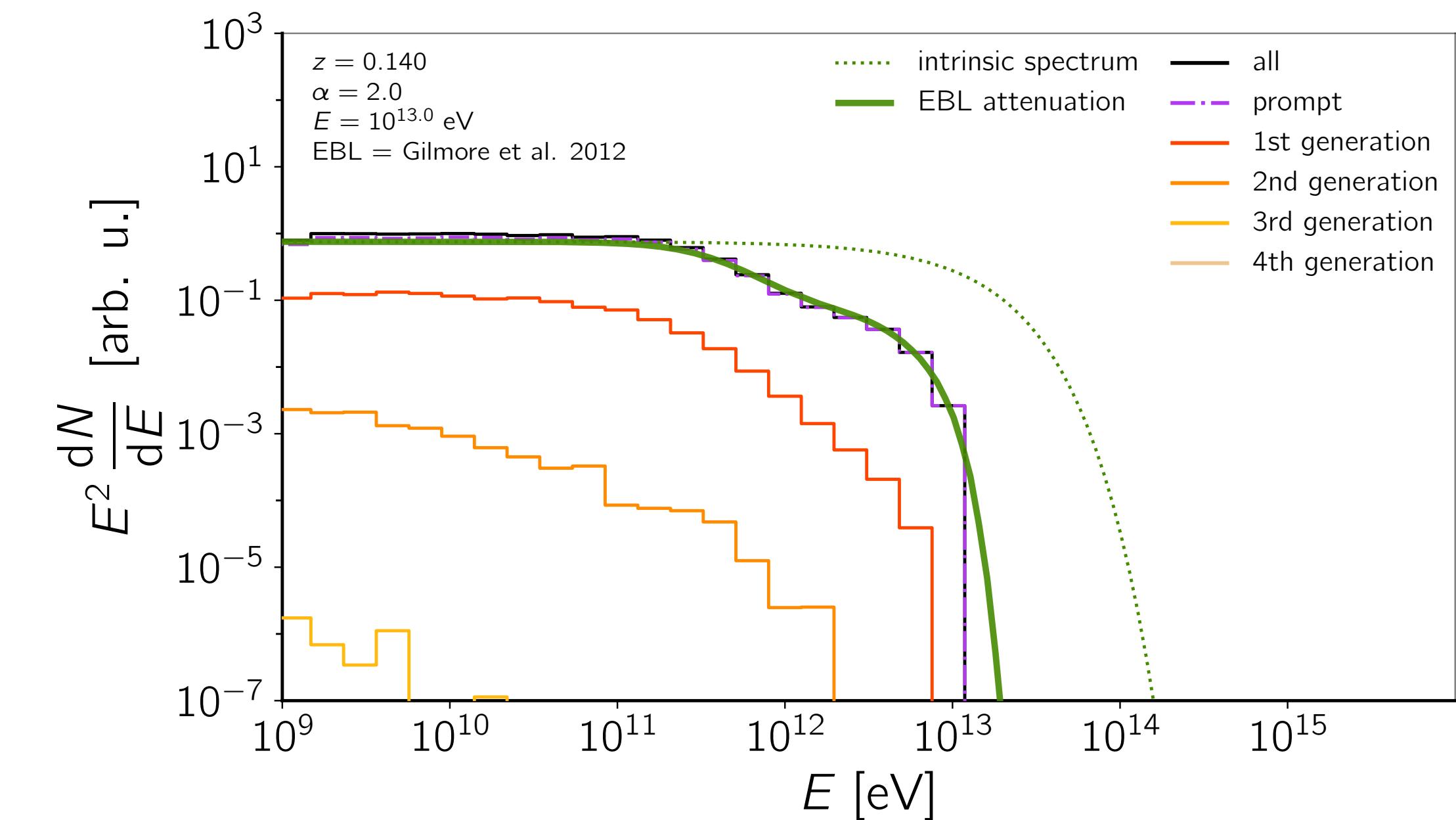
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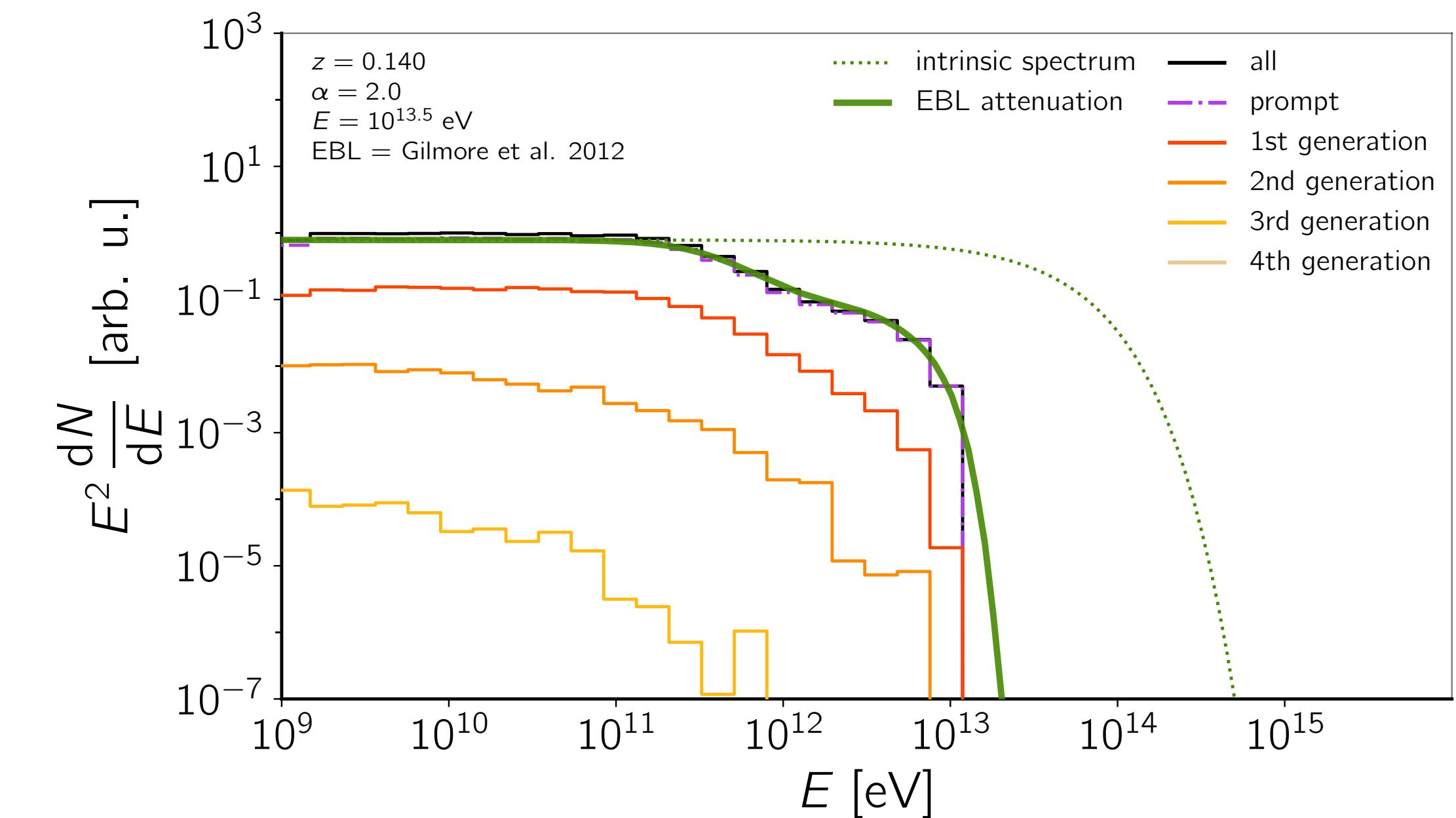
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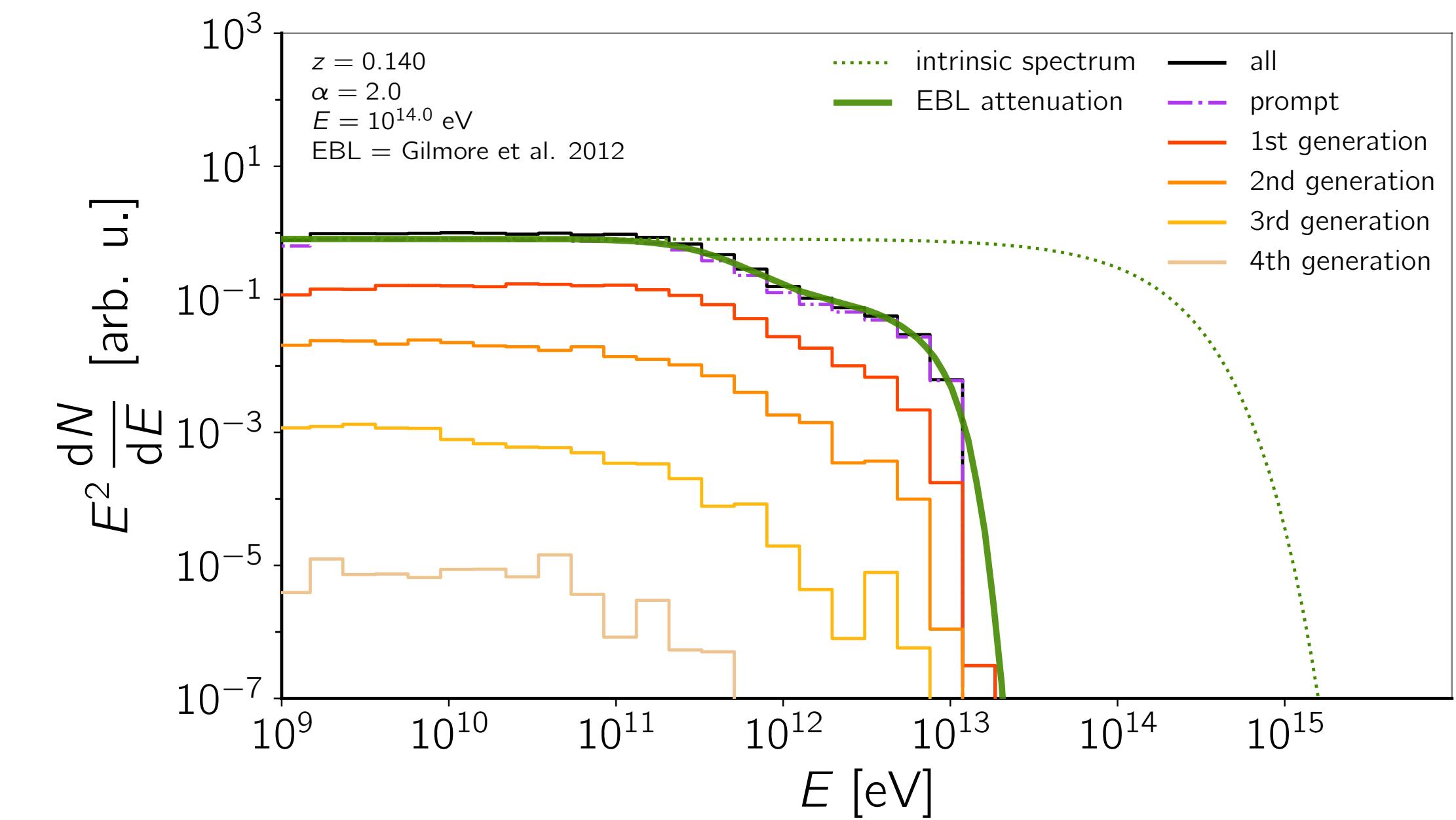
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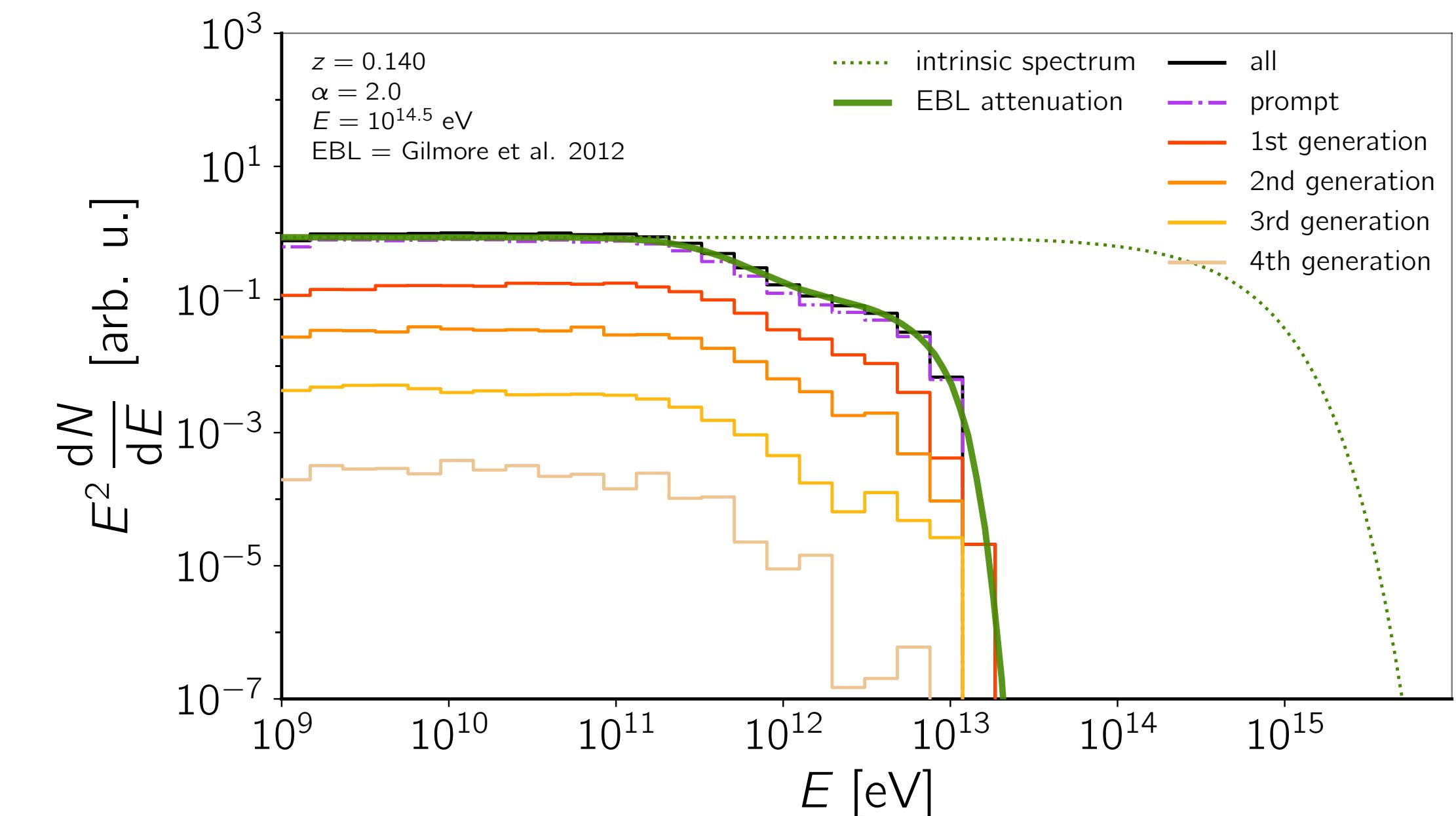
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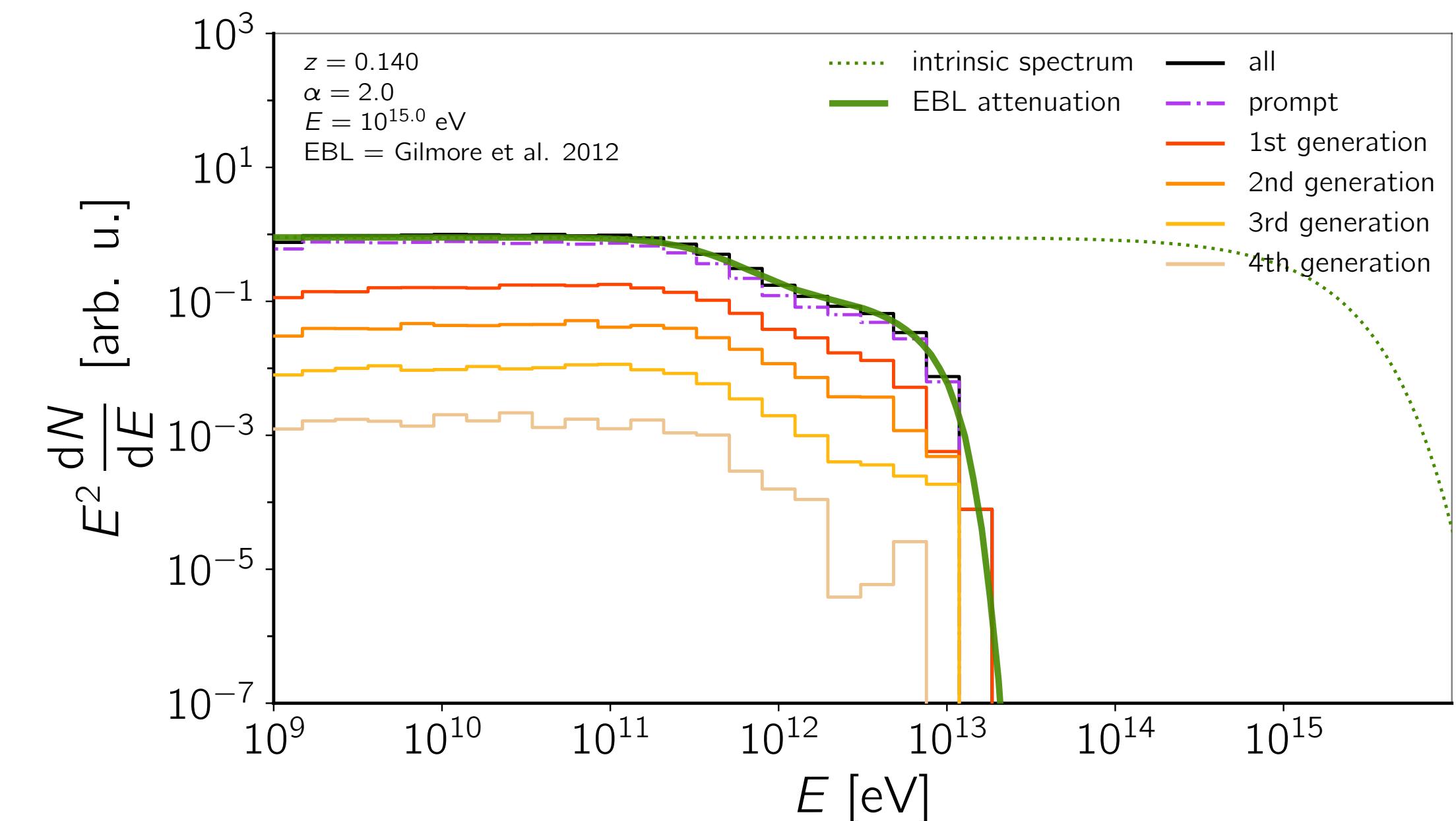
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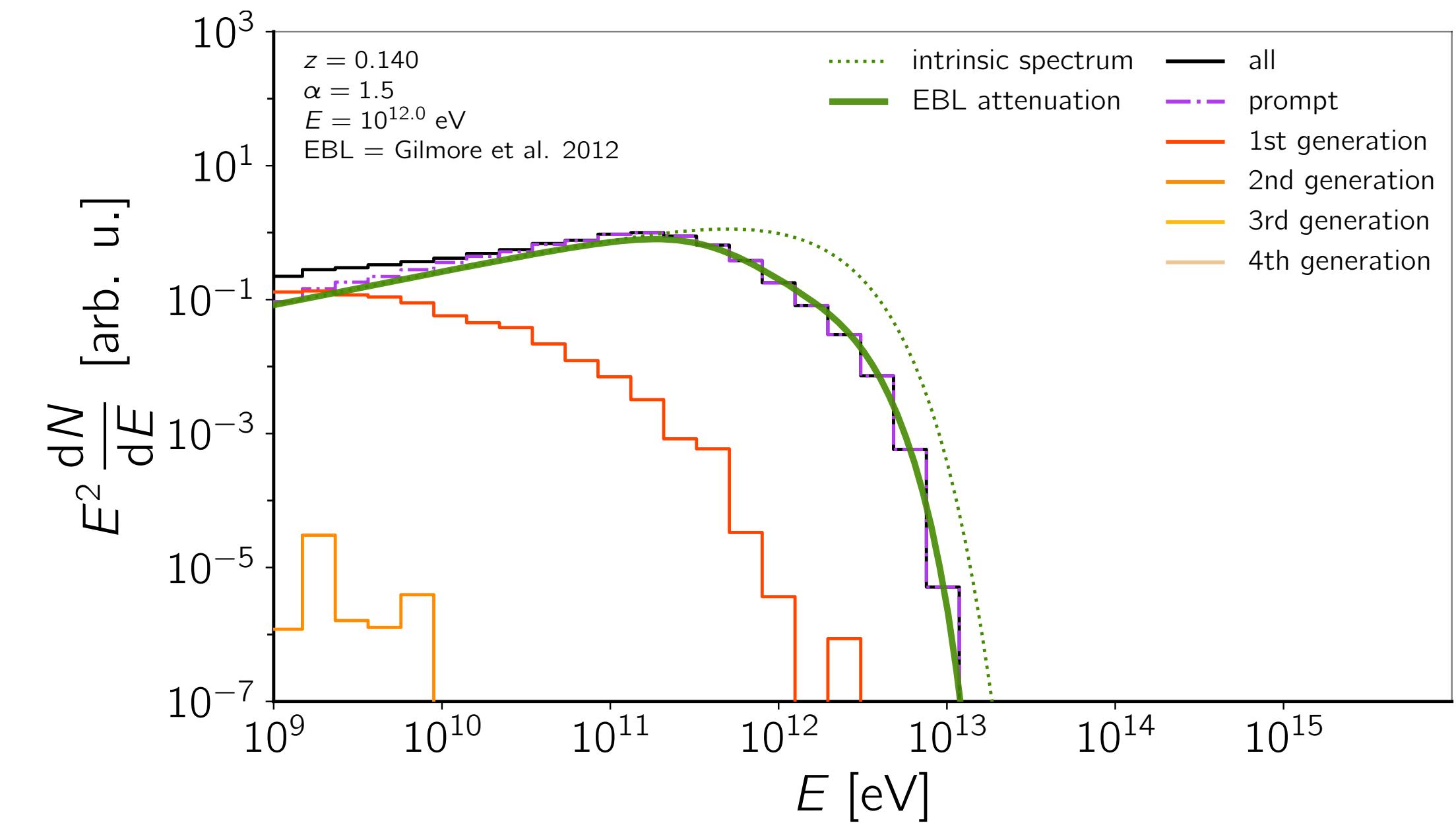
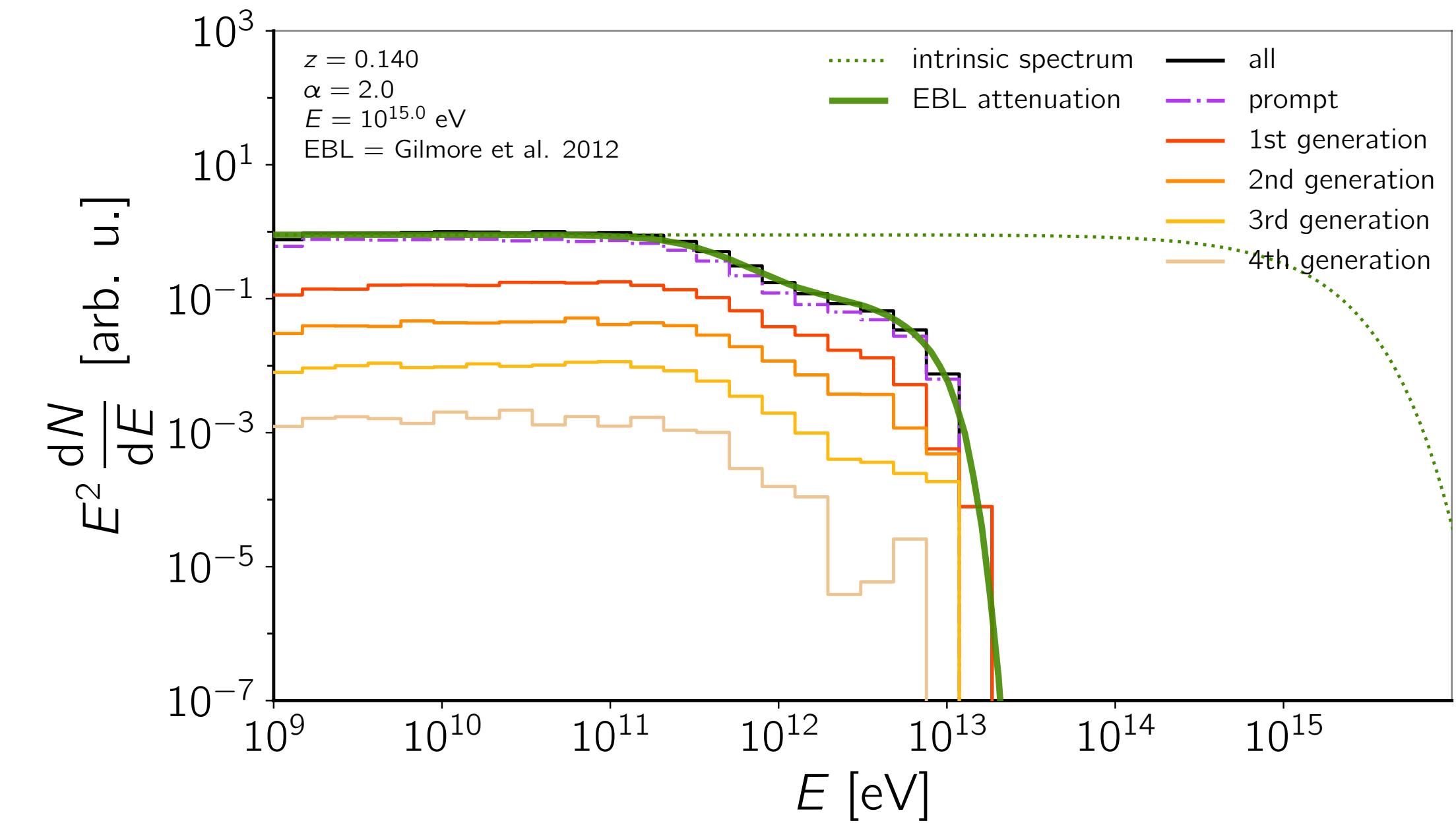
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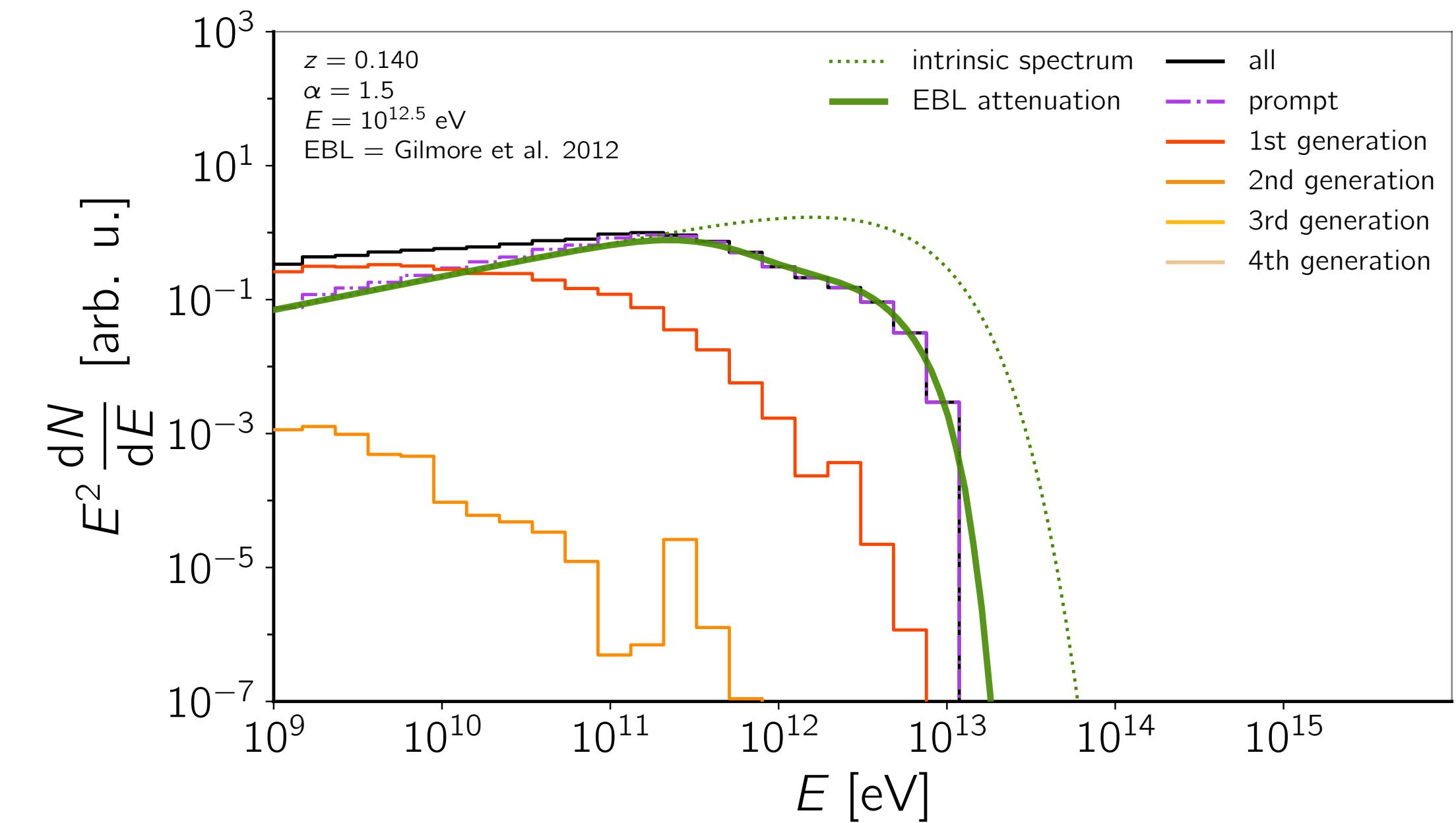
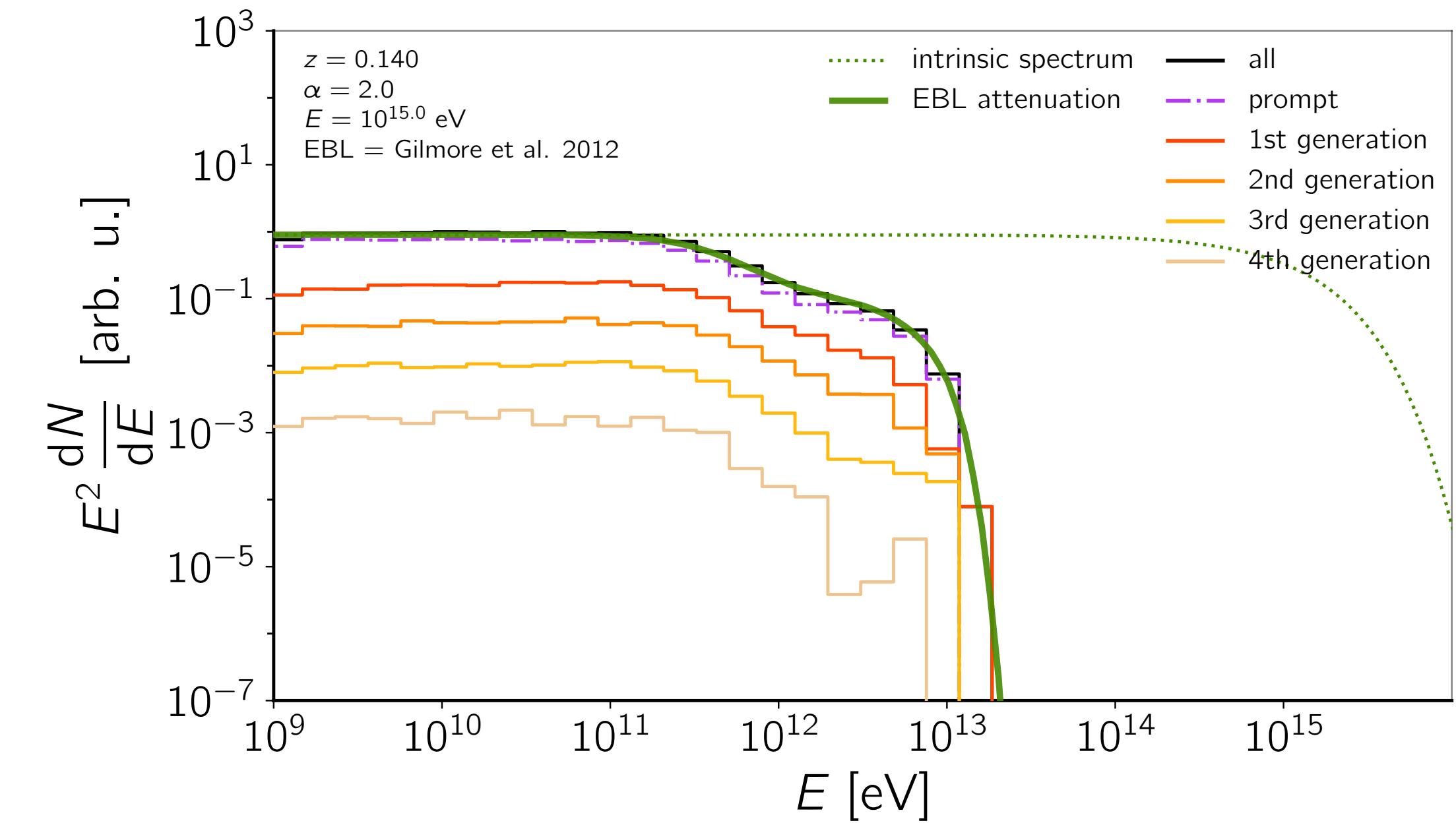
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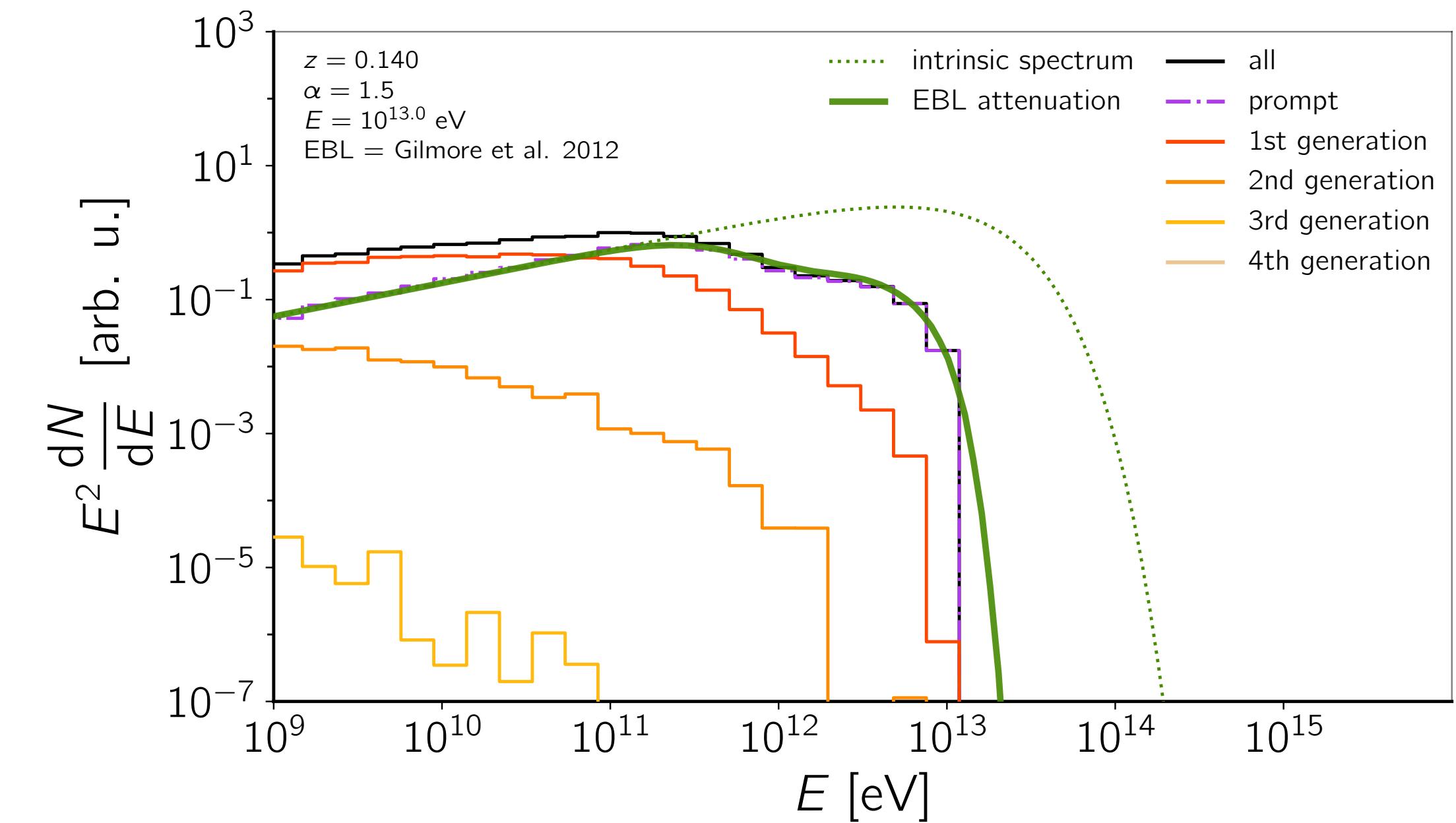
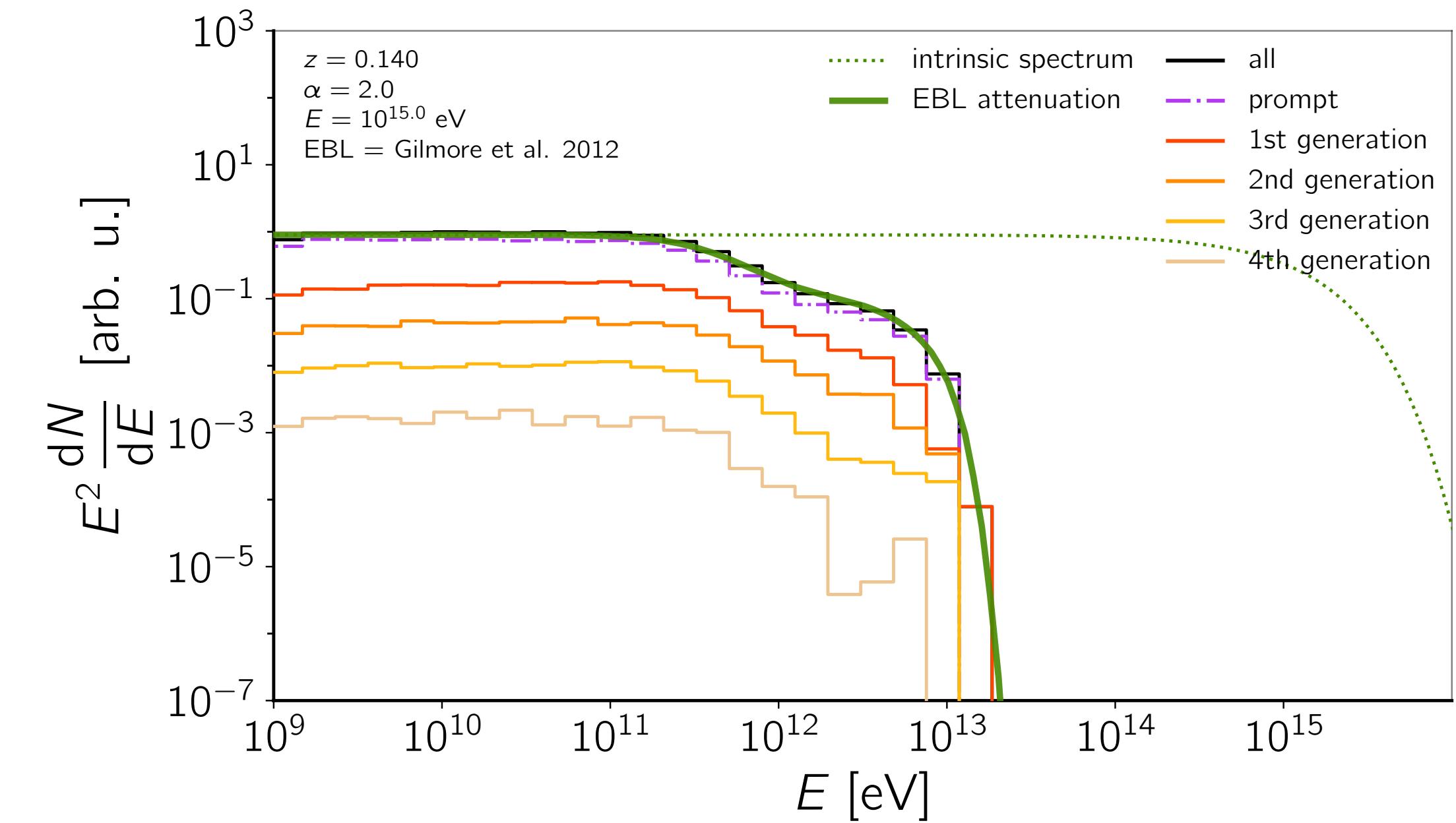
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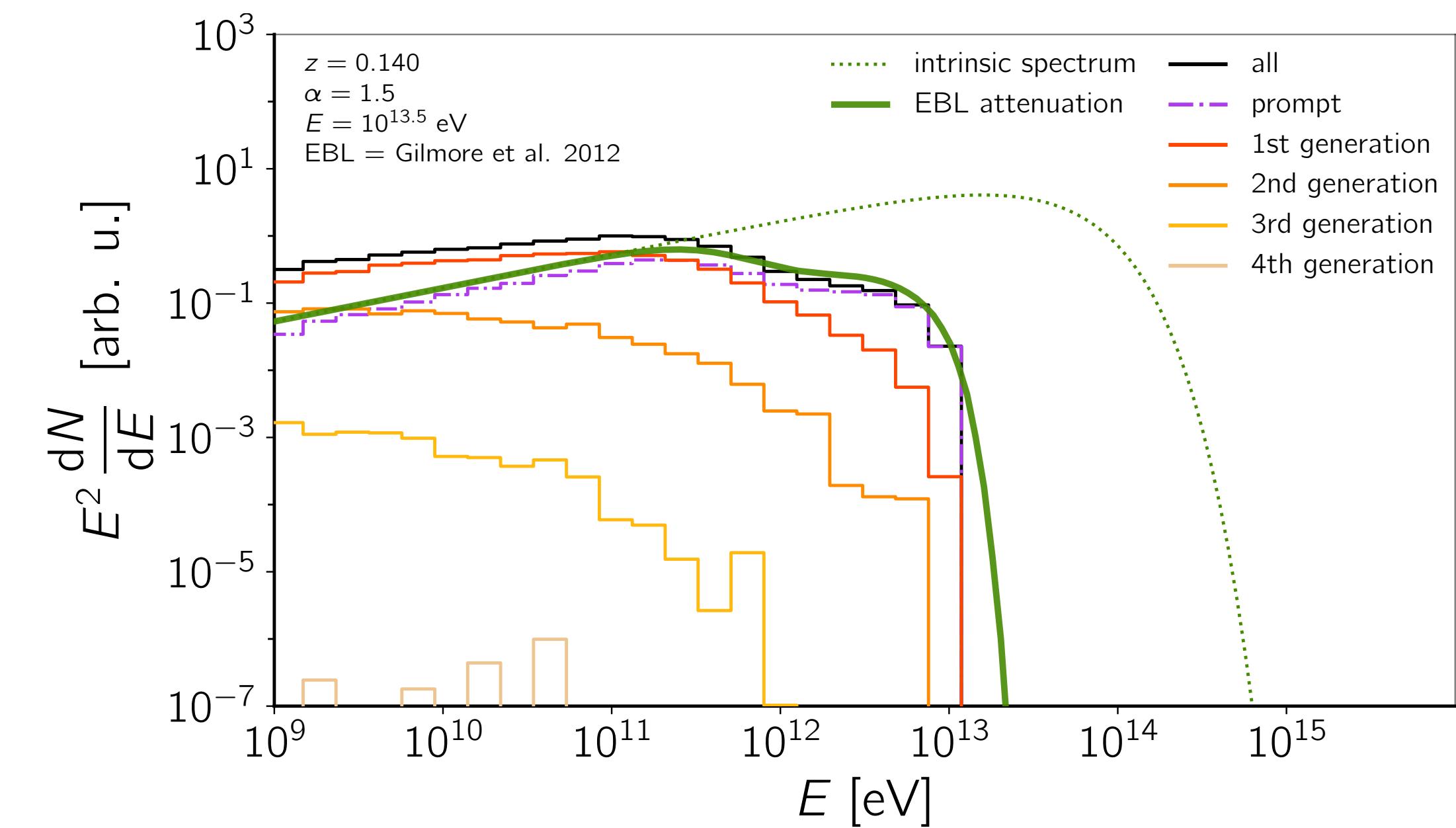
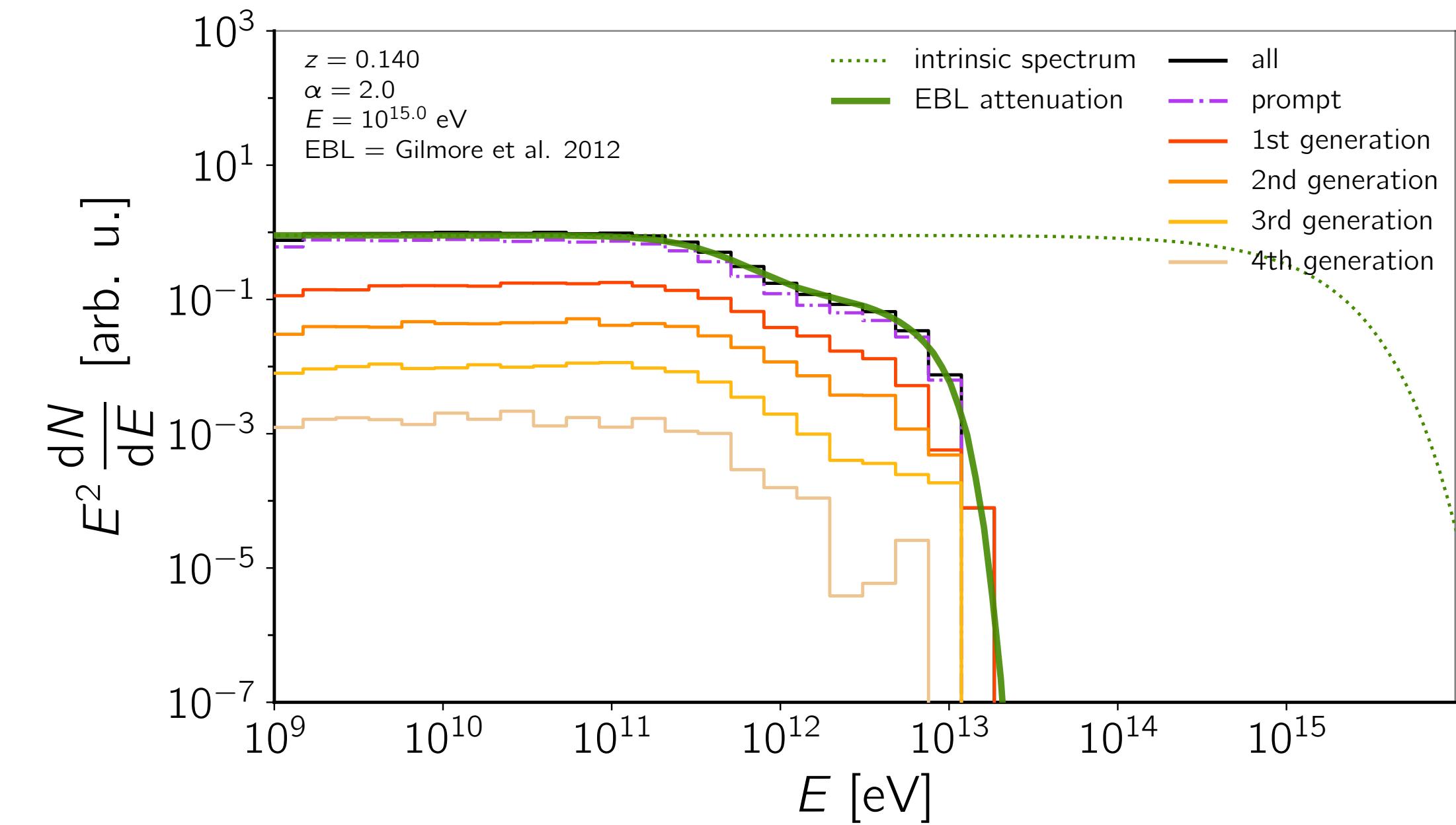
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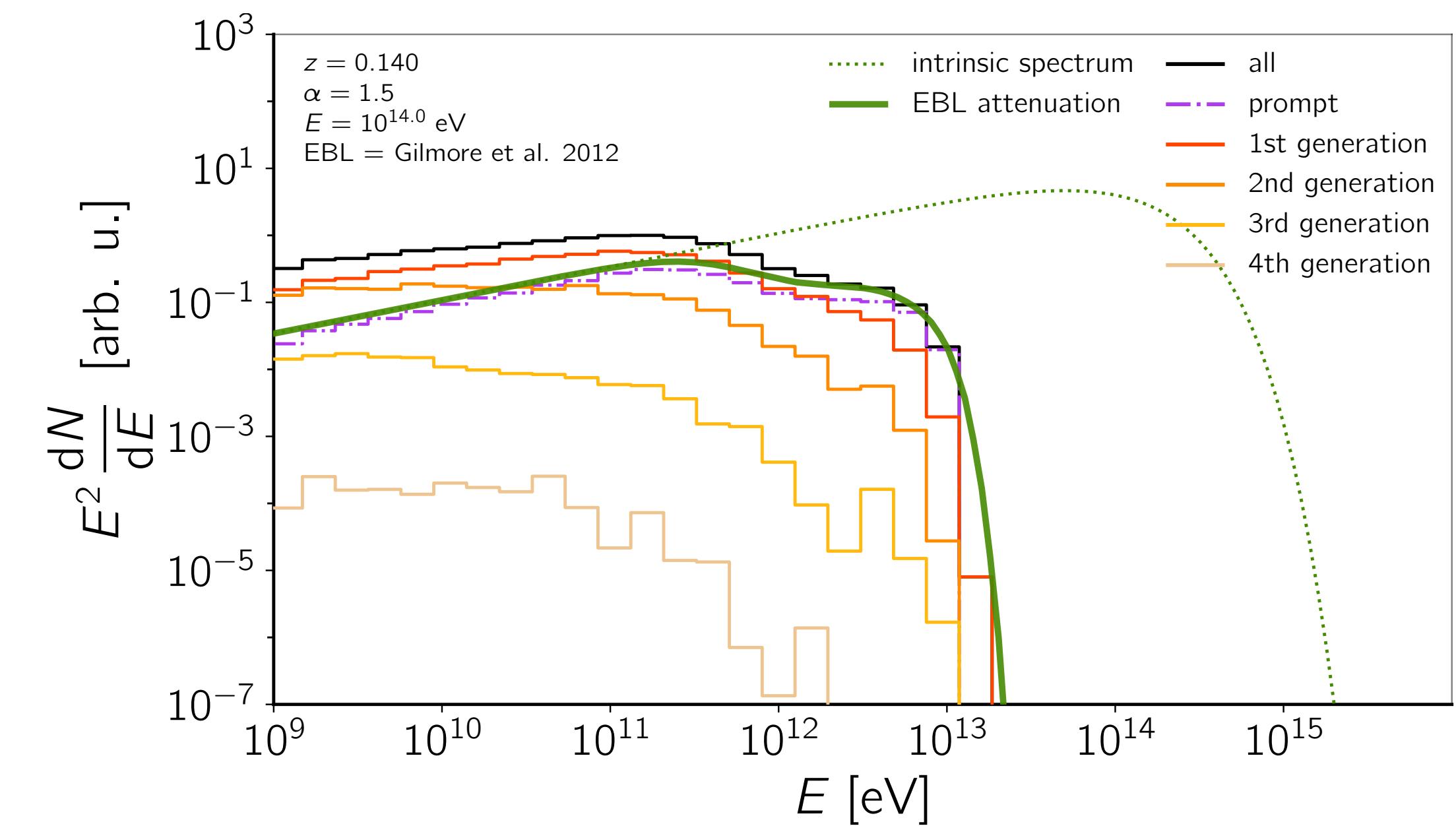
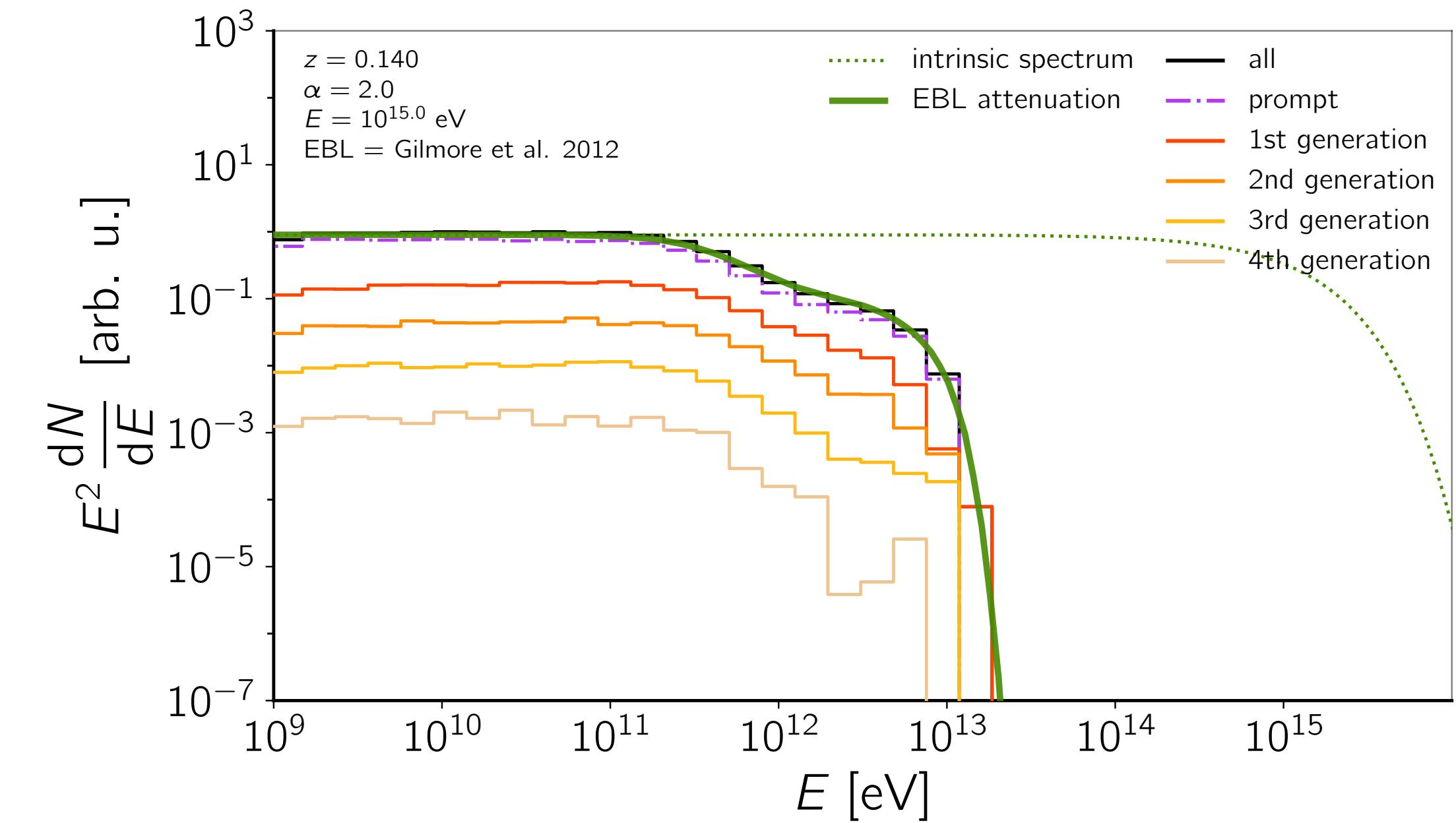
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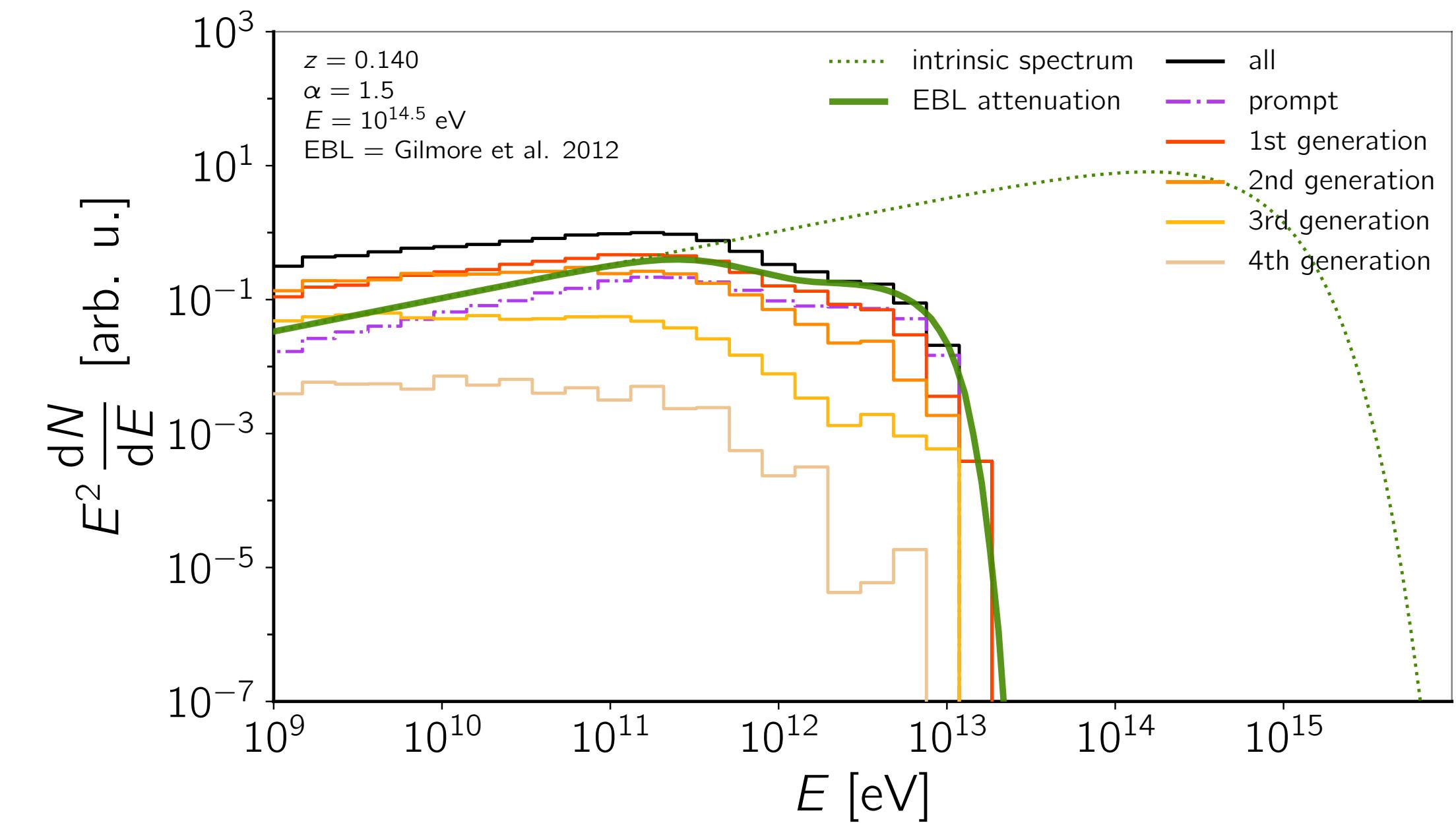
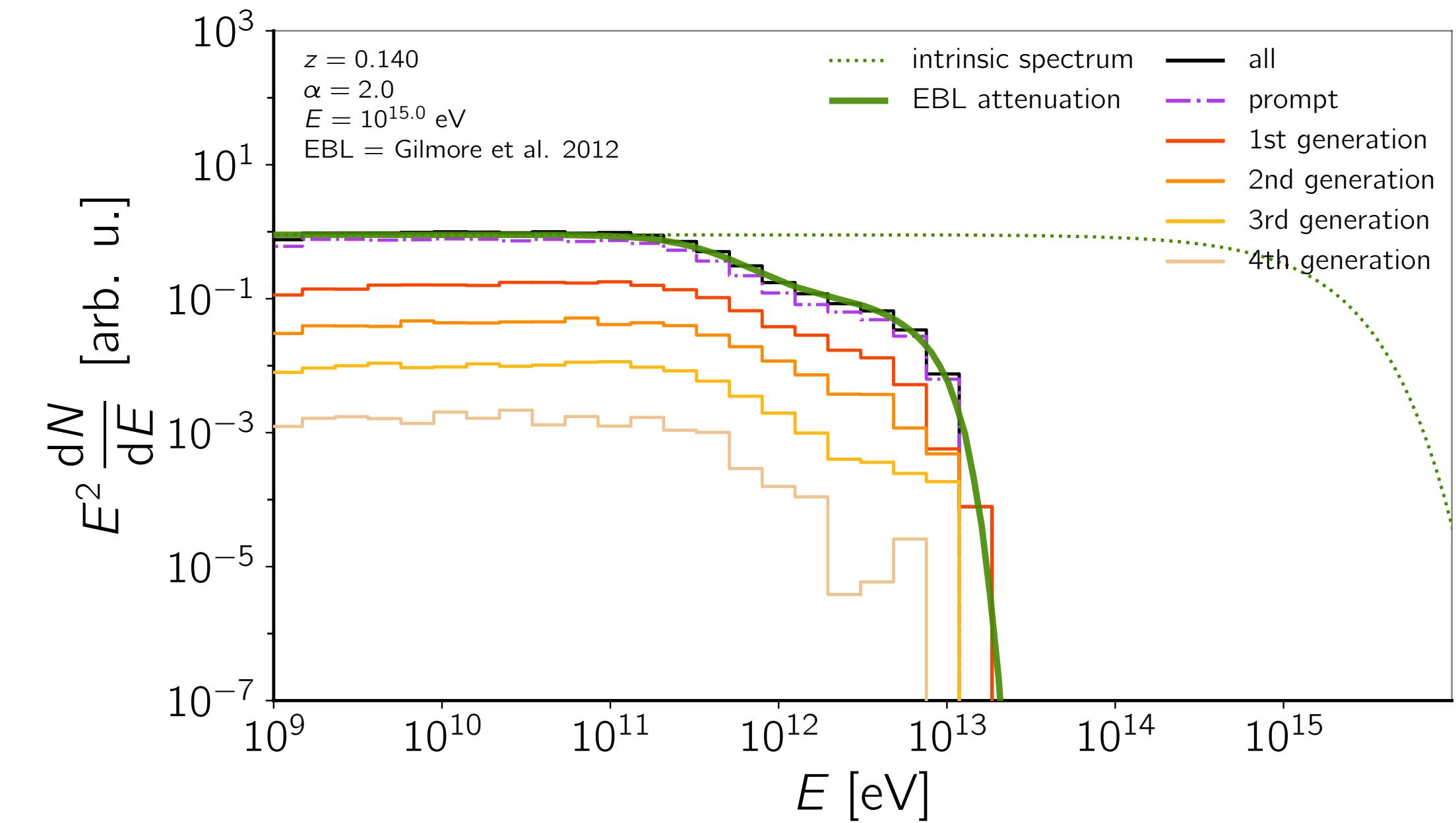
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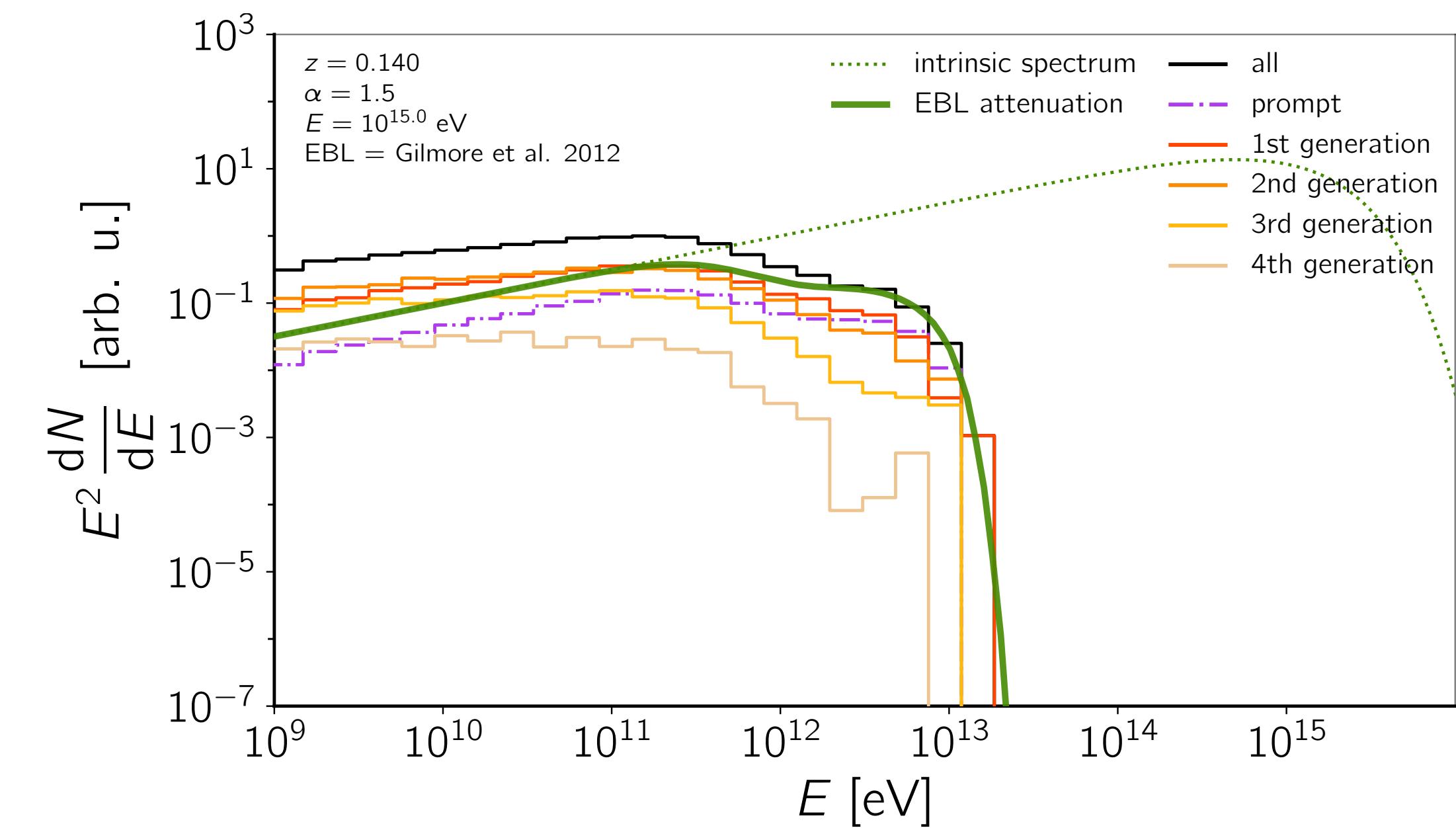
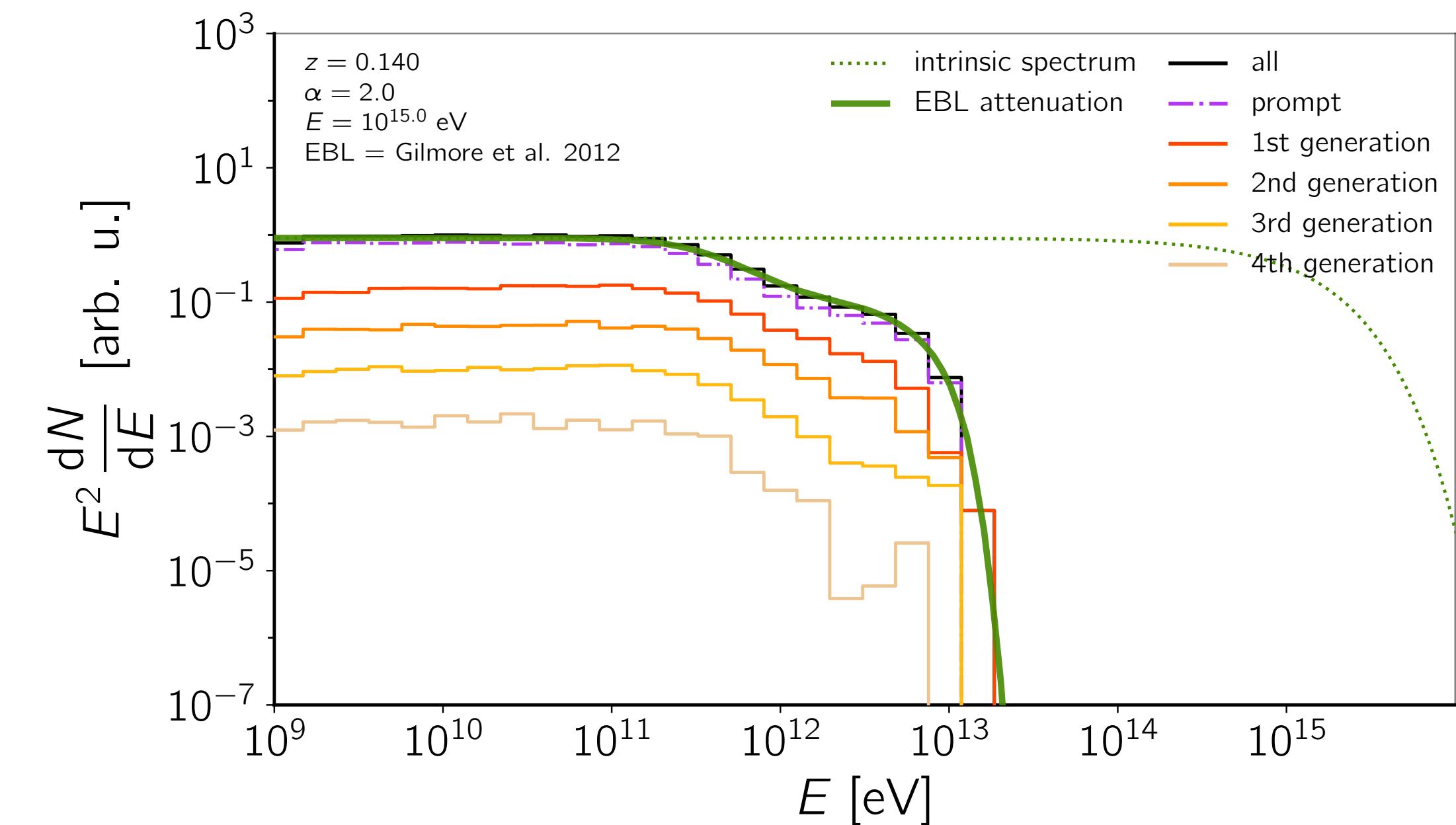
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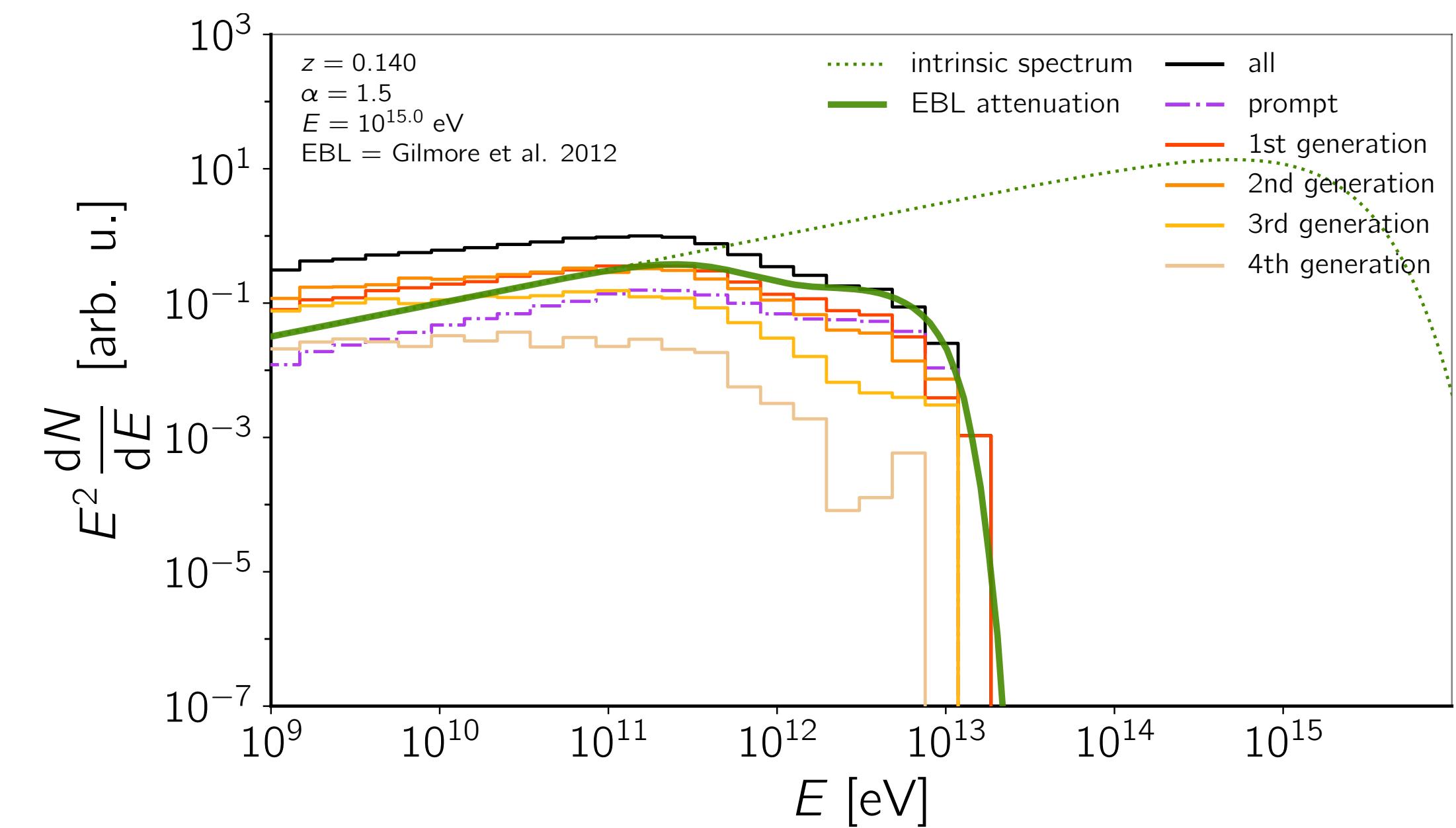
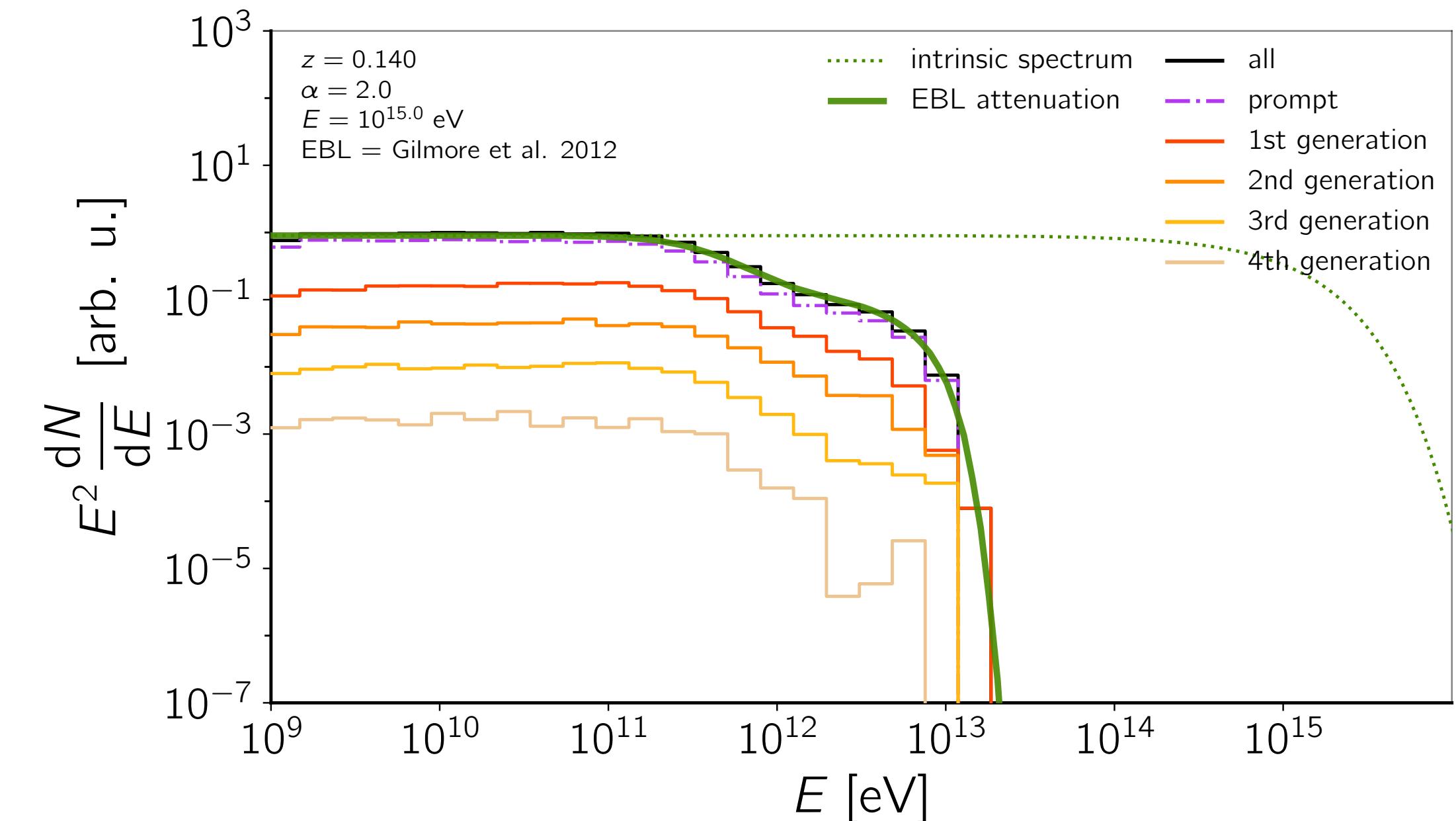
$$\tau(E_o, z_s) = \int_0^{z_s} dz \lambda^{-1} \left(\frac{E_{o,s}}{1+z}, z \right) \frac{d\ell}{dz}$$

- ▶ other processes can be important
 - ◆ inverse Compton in this case
- ▶ it is always better to perform full simulations
 - ◆ *but not faster* 😕

simulations performed with **CRPropa**

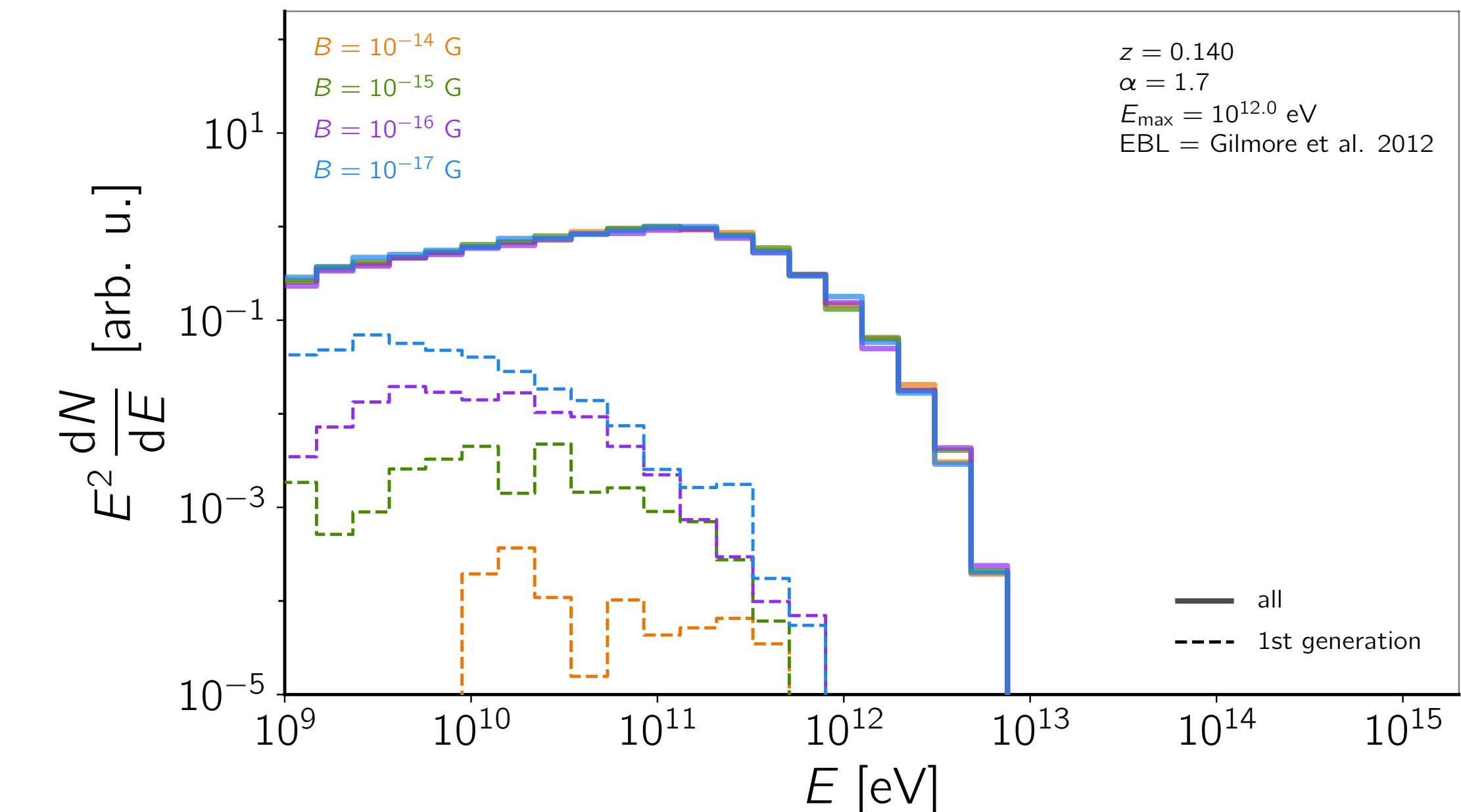
Alves Batista et al. JCAP 05 (2016) 038. arXiv:1603.07142

Alves Batista et al. JCAP 09 (2022) 035. arXiv:2208.00107

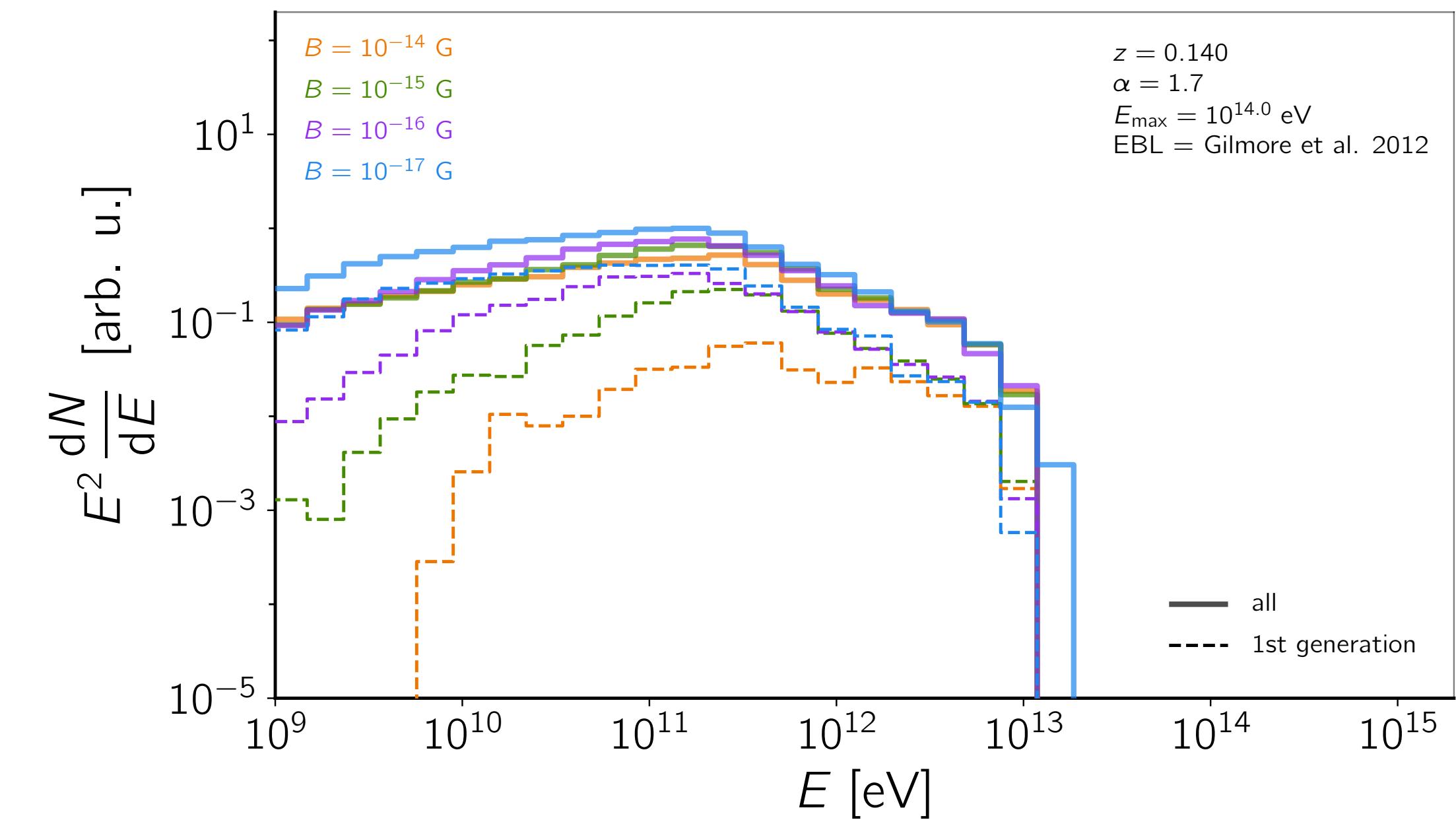
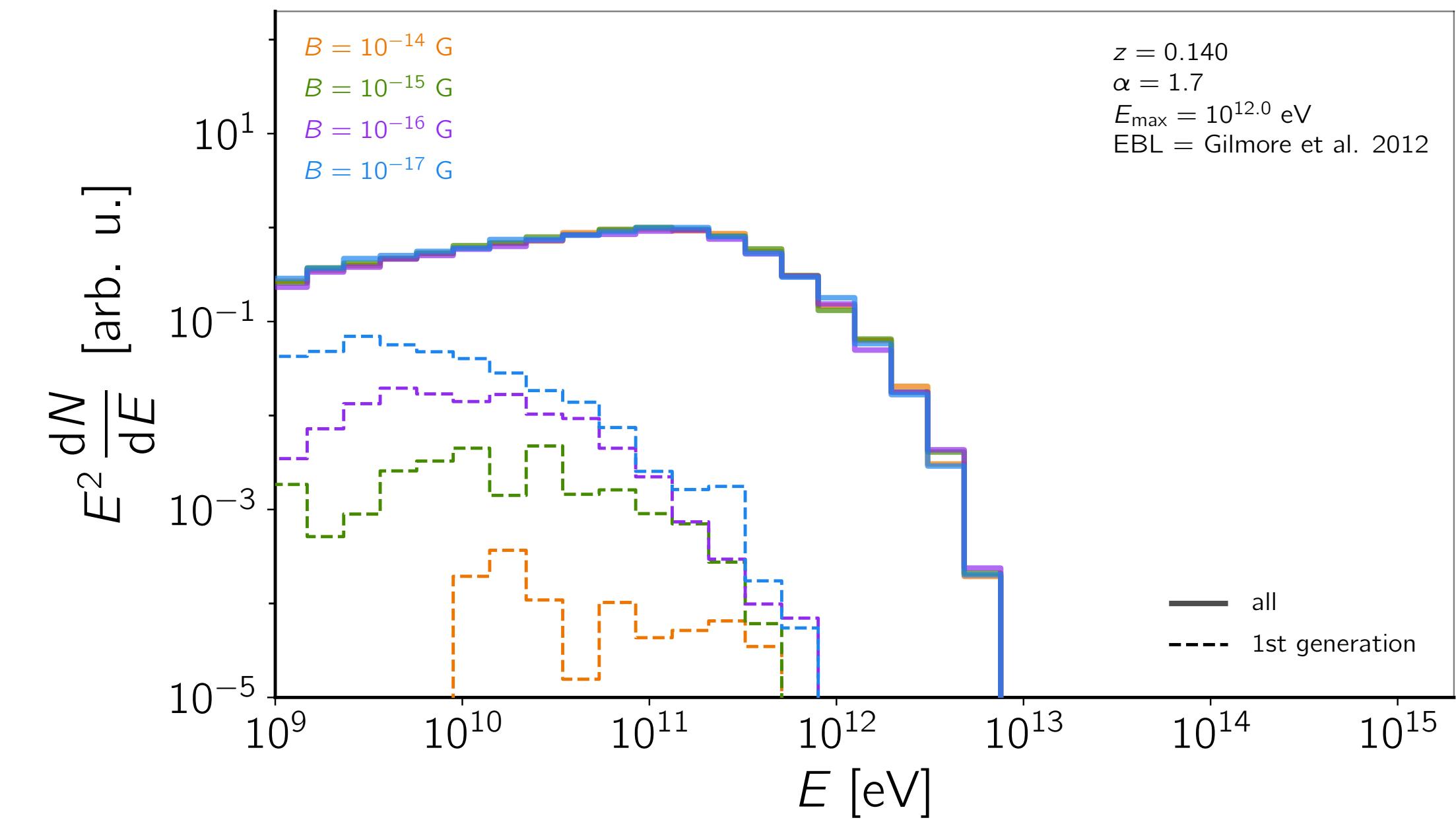


the usual approach to gamma-ray propagation

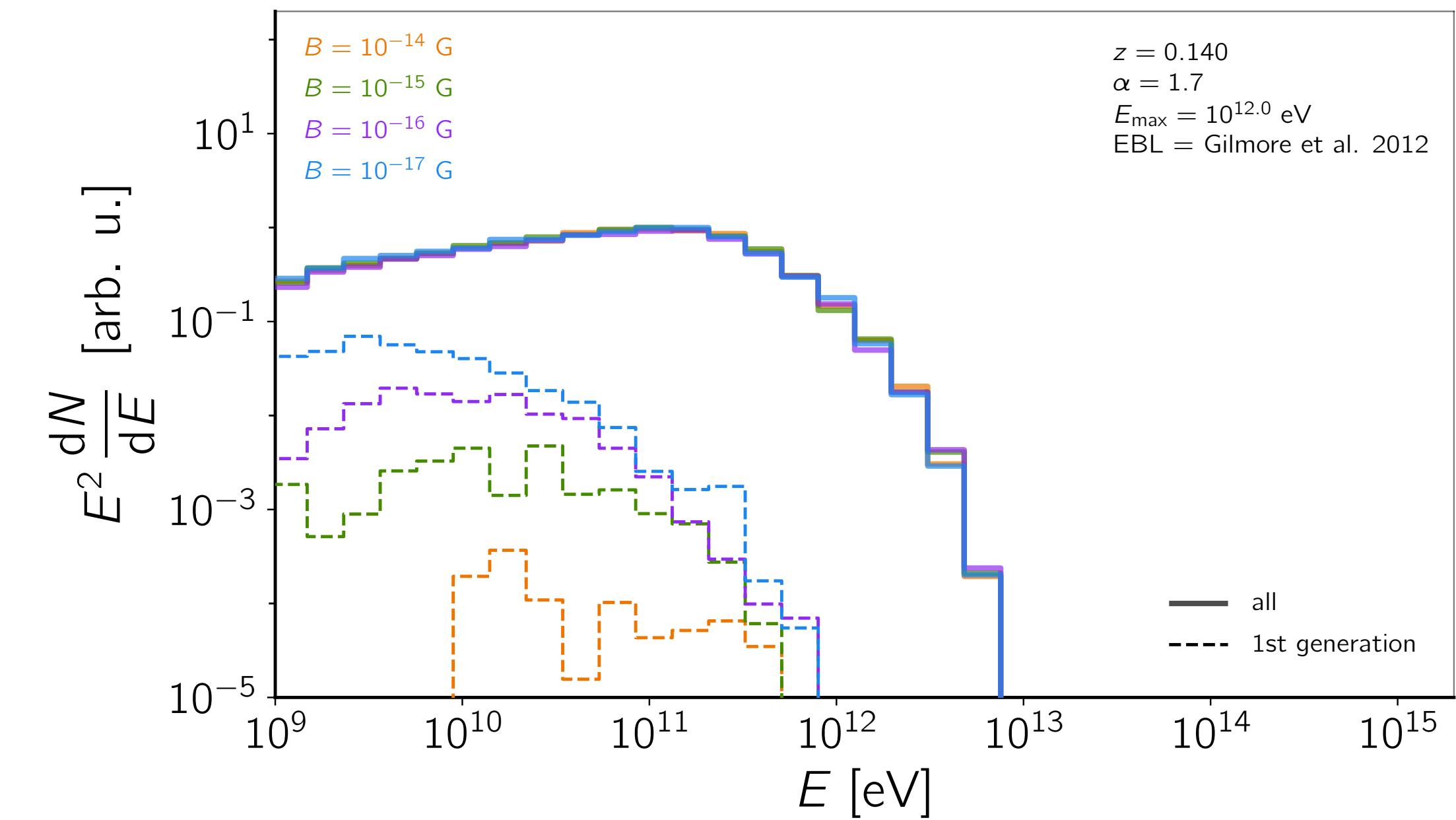
the usual approach to gamma-ray propagation



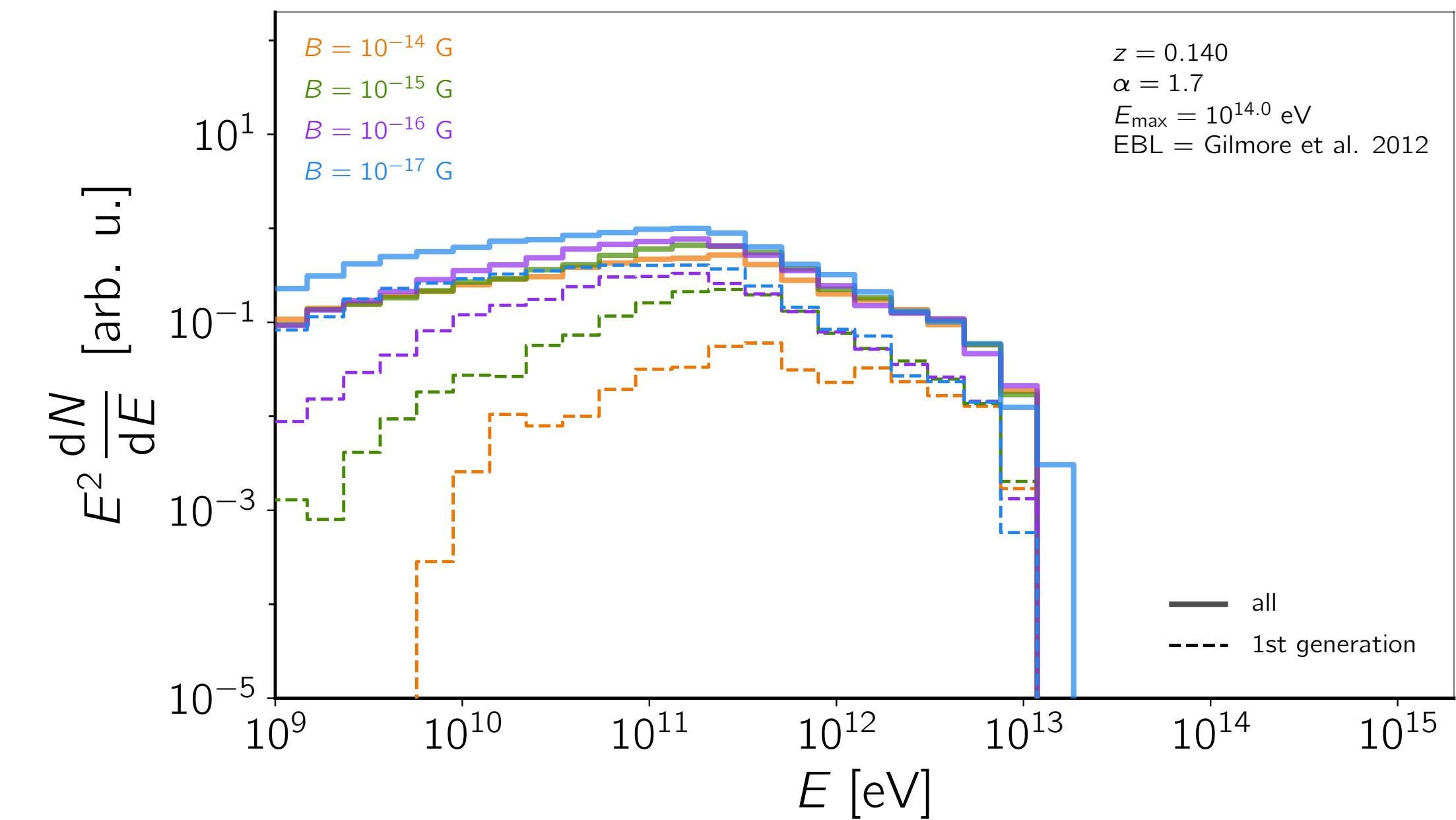
the usual approach to gamma-ray propagation



the usual approach to gamma-ray propagation



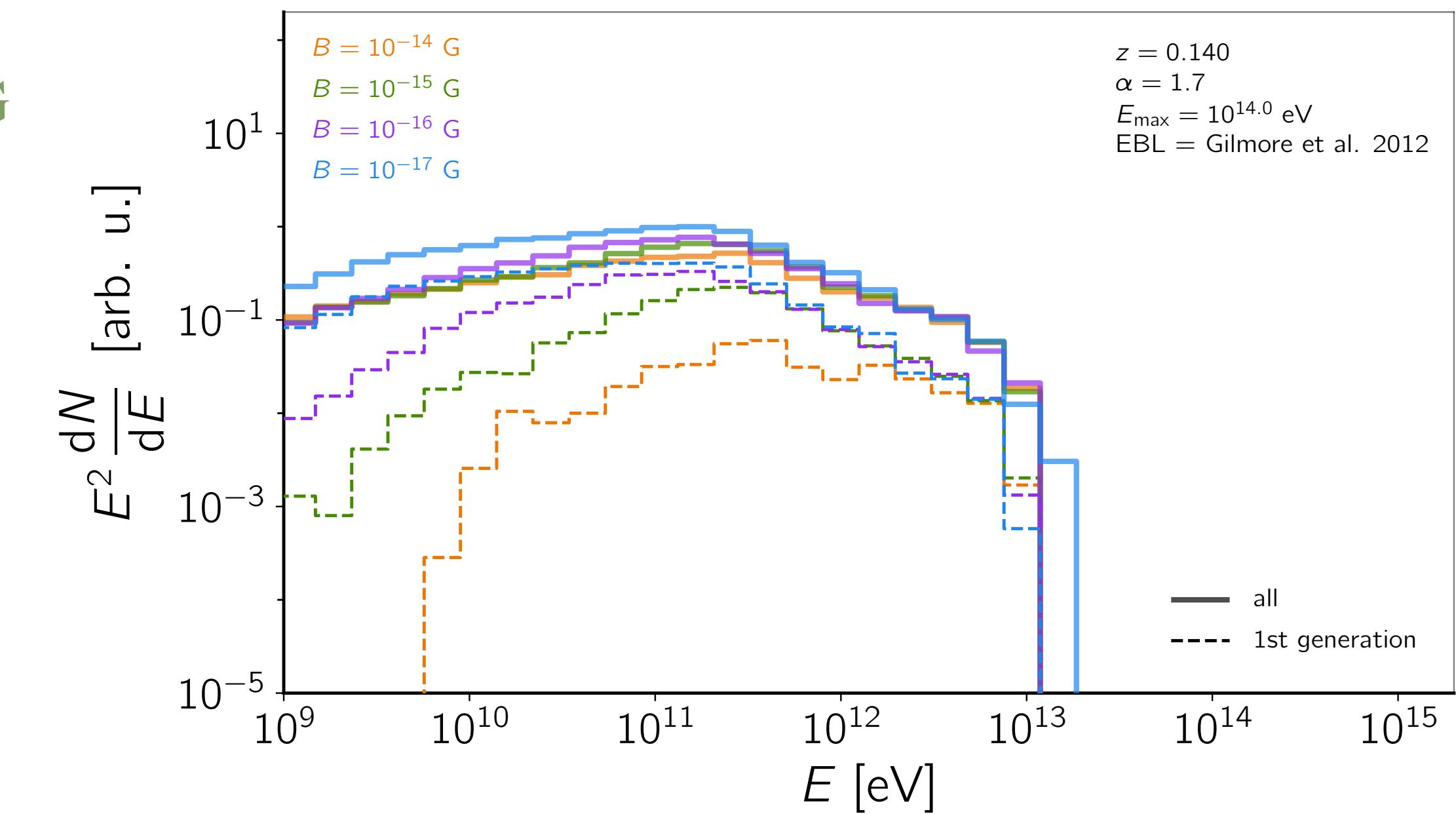
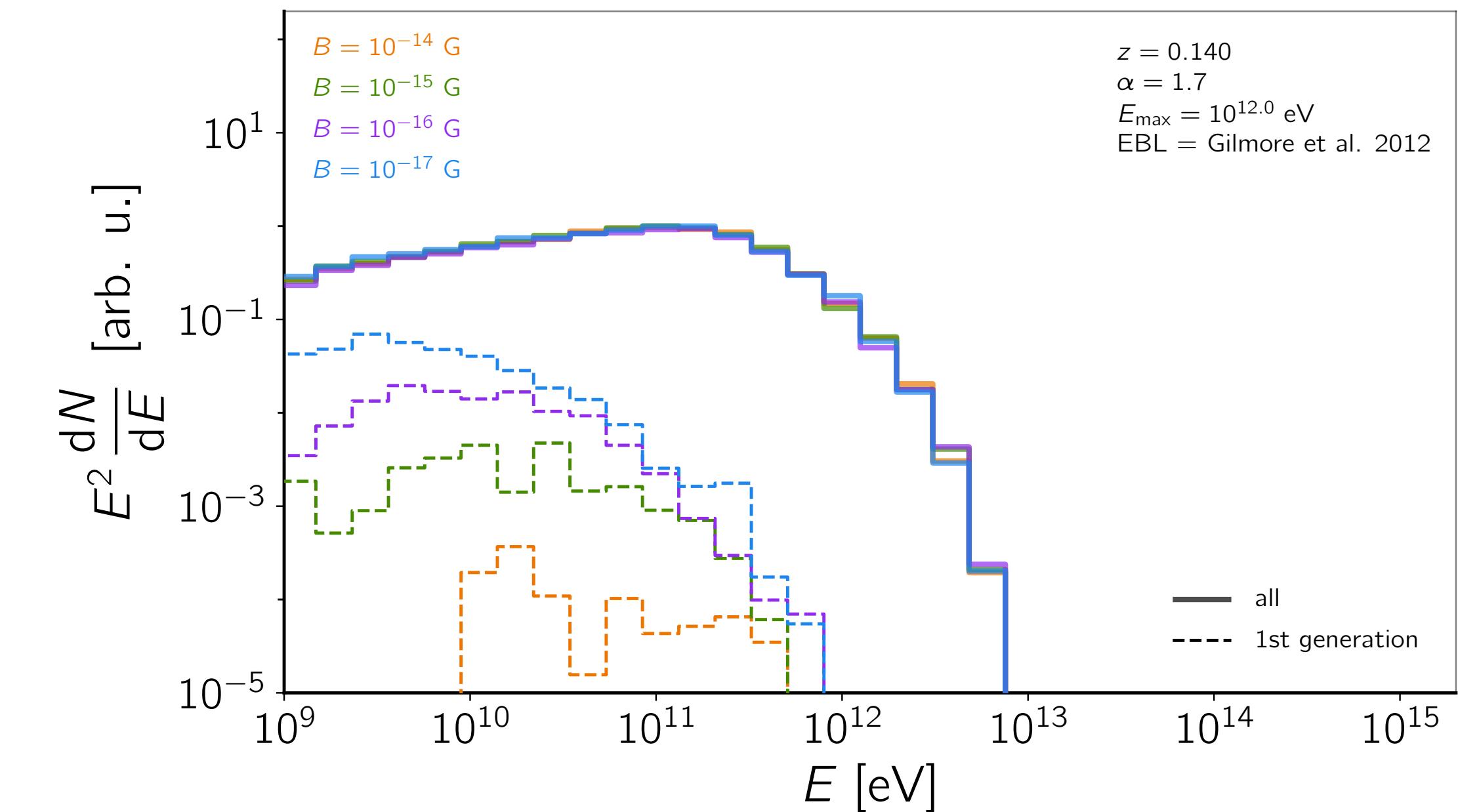
$$\Delta t_{\text{obs}} = \Delta t_{\text{QG}} + \mathfrak{T} + \Delta t_B + \dots$$



the usual approach to gamma-ray propagation

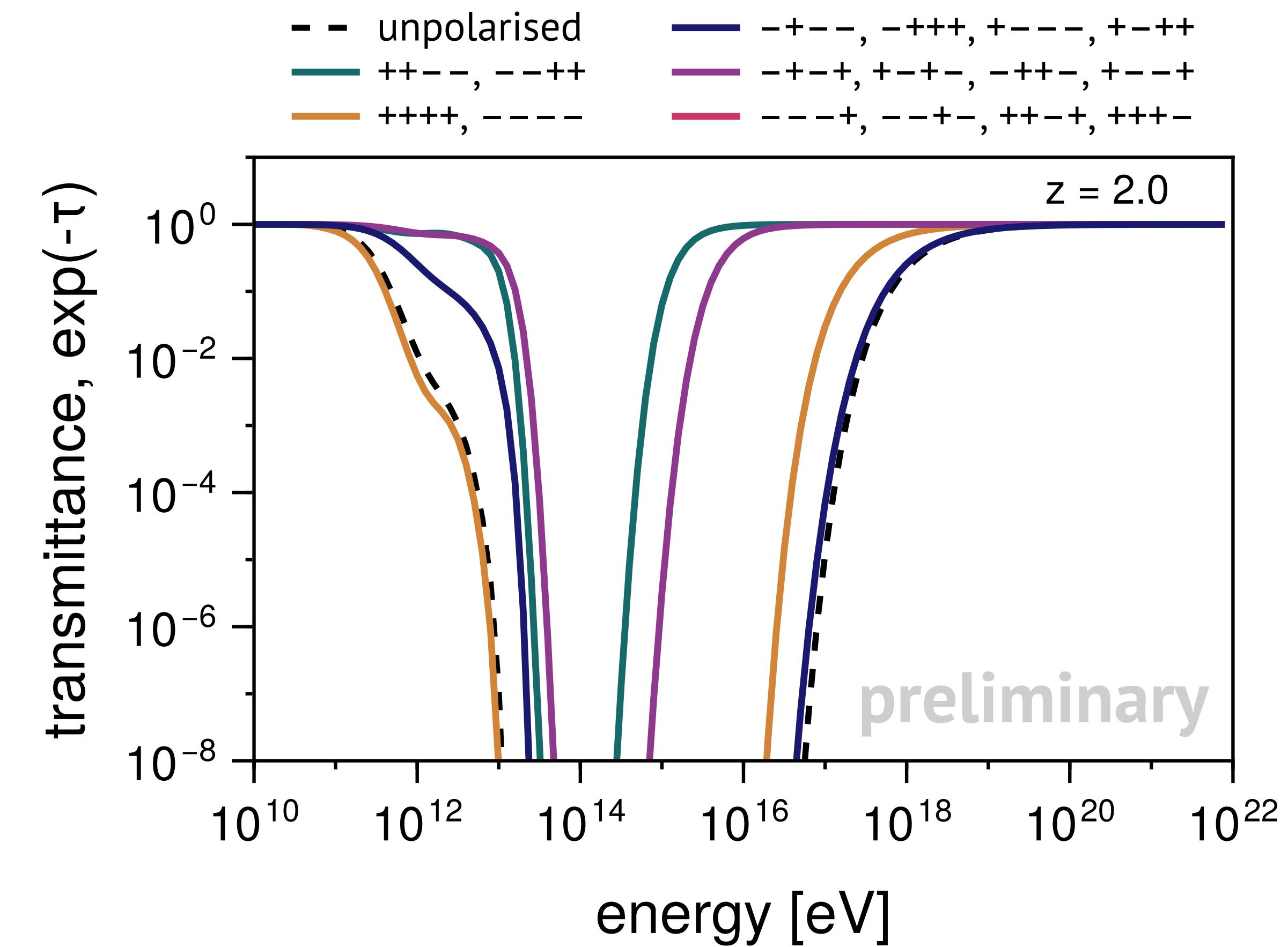
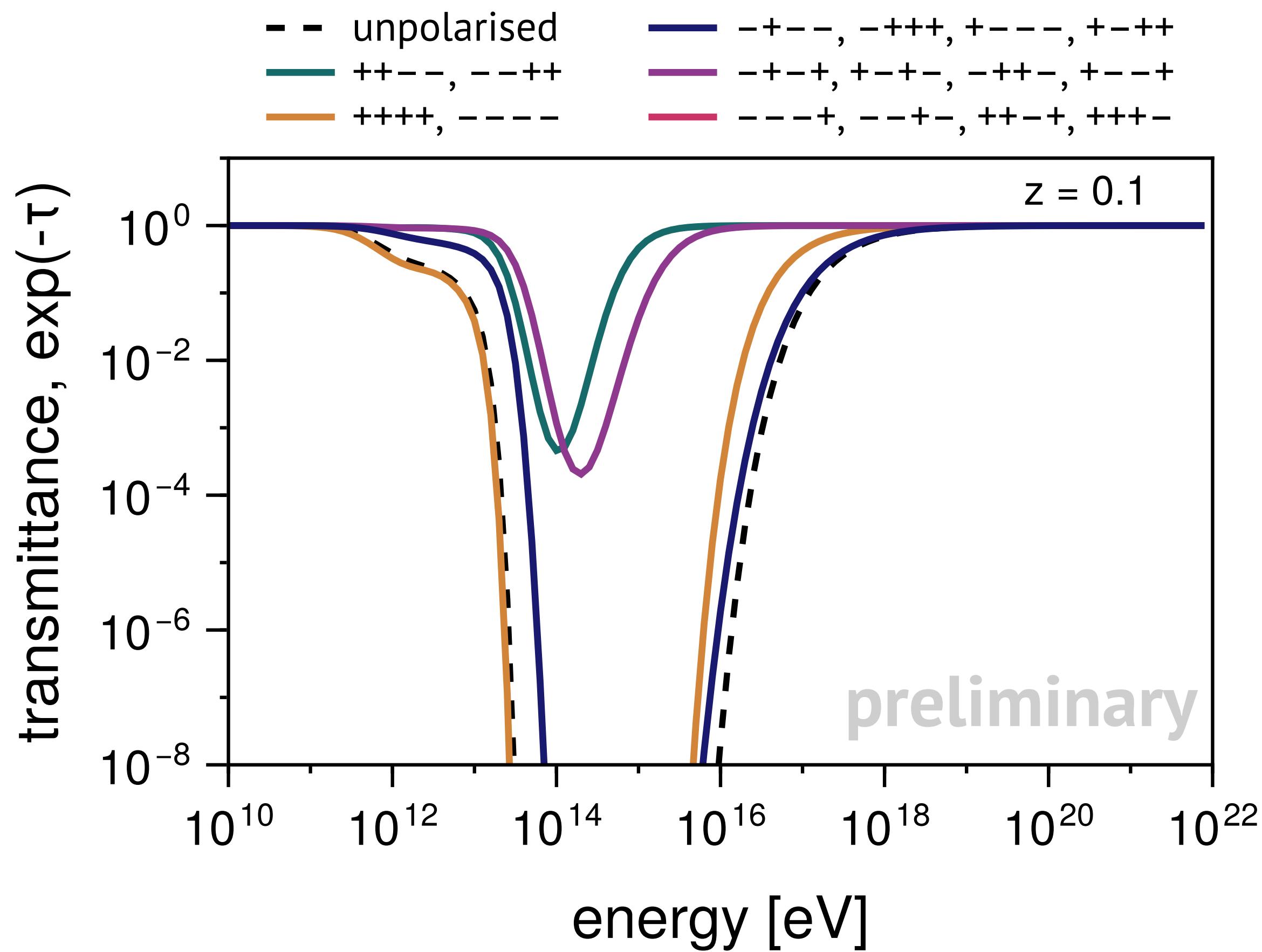
$$\Delta t_{\text{obs}} = \Delta t_{\text{QG}} + \Sigma + \Delta t_B + \dots \rightarrow \Delta t_{\text{src}} + \Delta t_B^? \gg \Delta t_{\text{QG}}$$

difficult to identify QG signatures
with confidence



gamma-ray propagation. polarisation-dependent effects

Alves Batista, Cermeño, Mantoni. In preparation.



complete simulations of gamma-ray propagation with LIV

complete simulations of gamma-ray propagation with LIV

► **complete simulations** including LIV

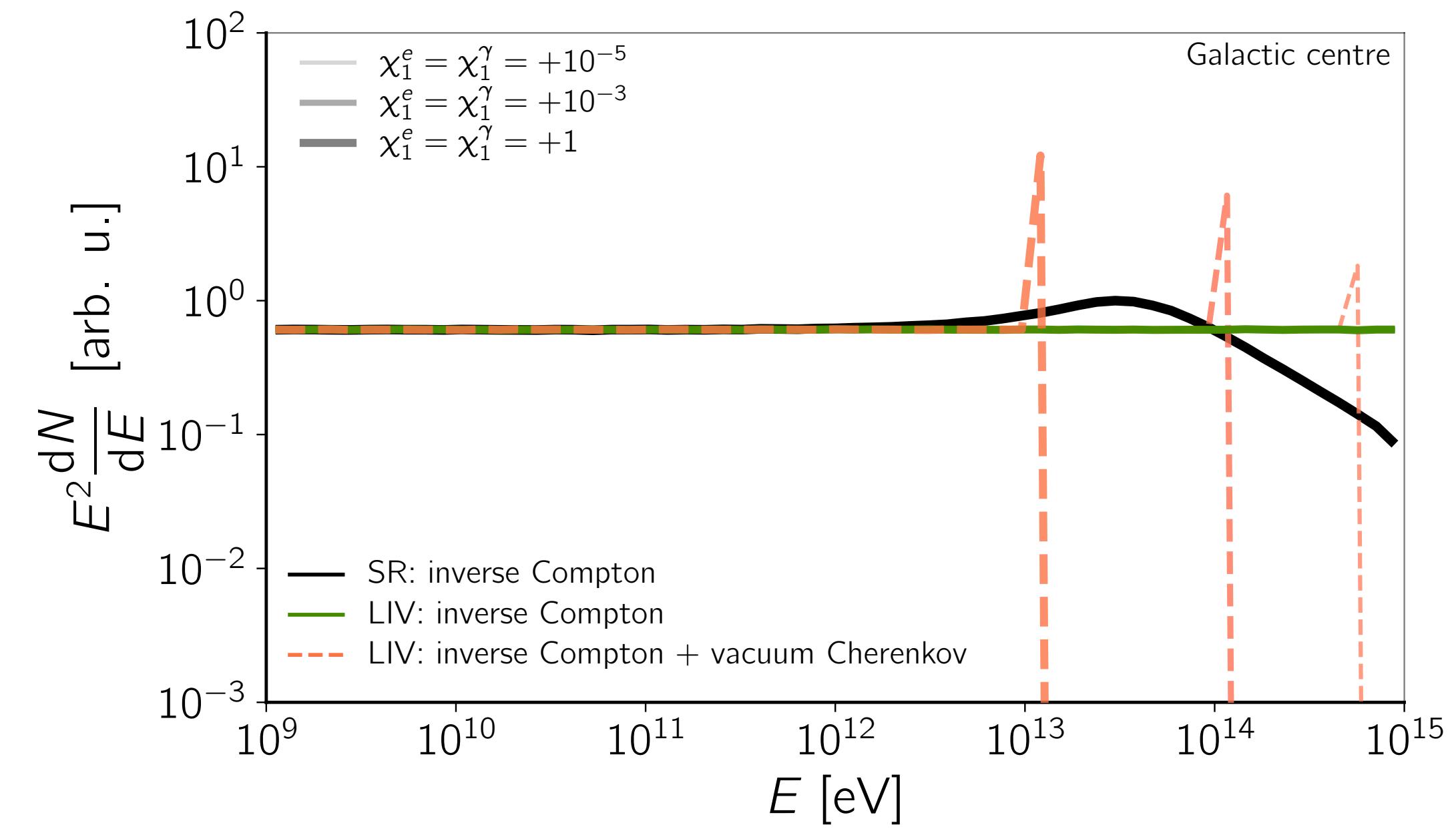
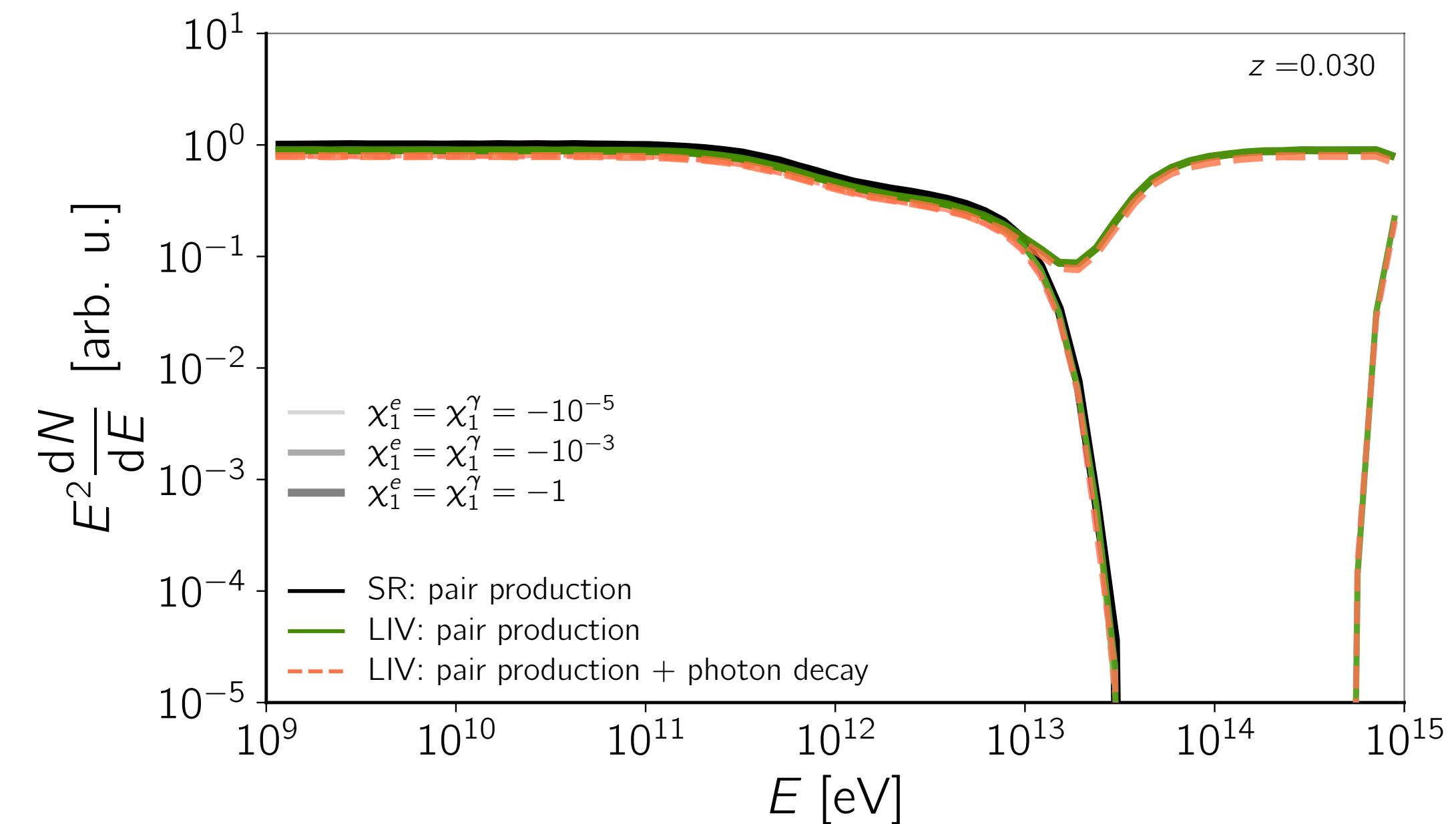
- ◆ modification of pair production
- ◆ including inverse Compton scattering
- ◆ including vacuum Cherenkov
- ◆ including photon decay

complete simulations of gamma-ray propagation with LIV

Saveliev & Alves Batista. Class. Quant. Grav. 41 (2024) 115011. arXiv:2312.10803

► complete simulations including LIV

- ◆ modification of pair production
- ◆ including inverse Compton scattering
- ◆ including vacuum Cherenkov
- ◆ including photon decay

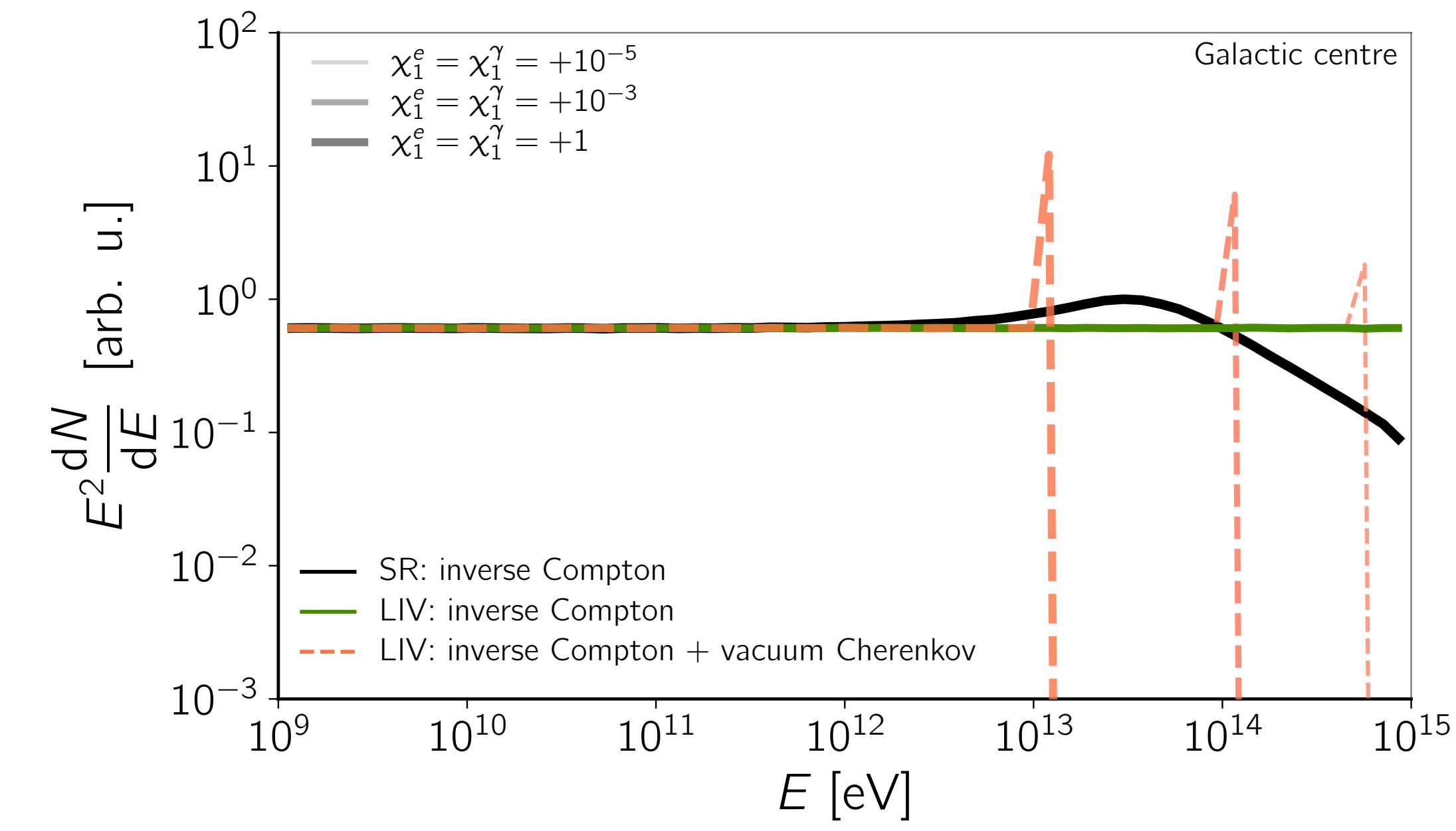
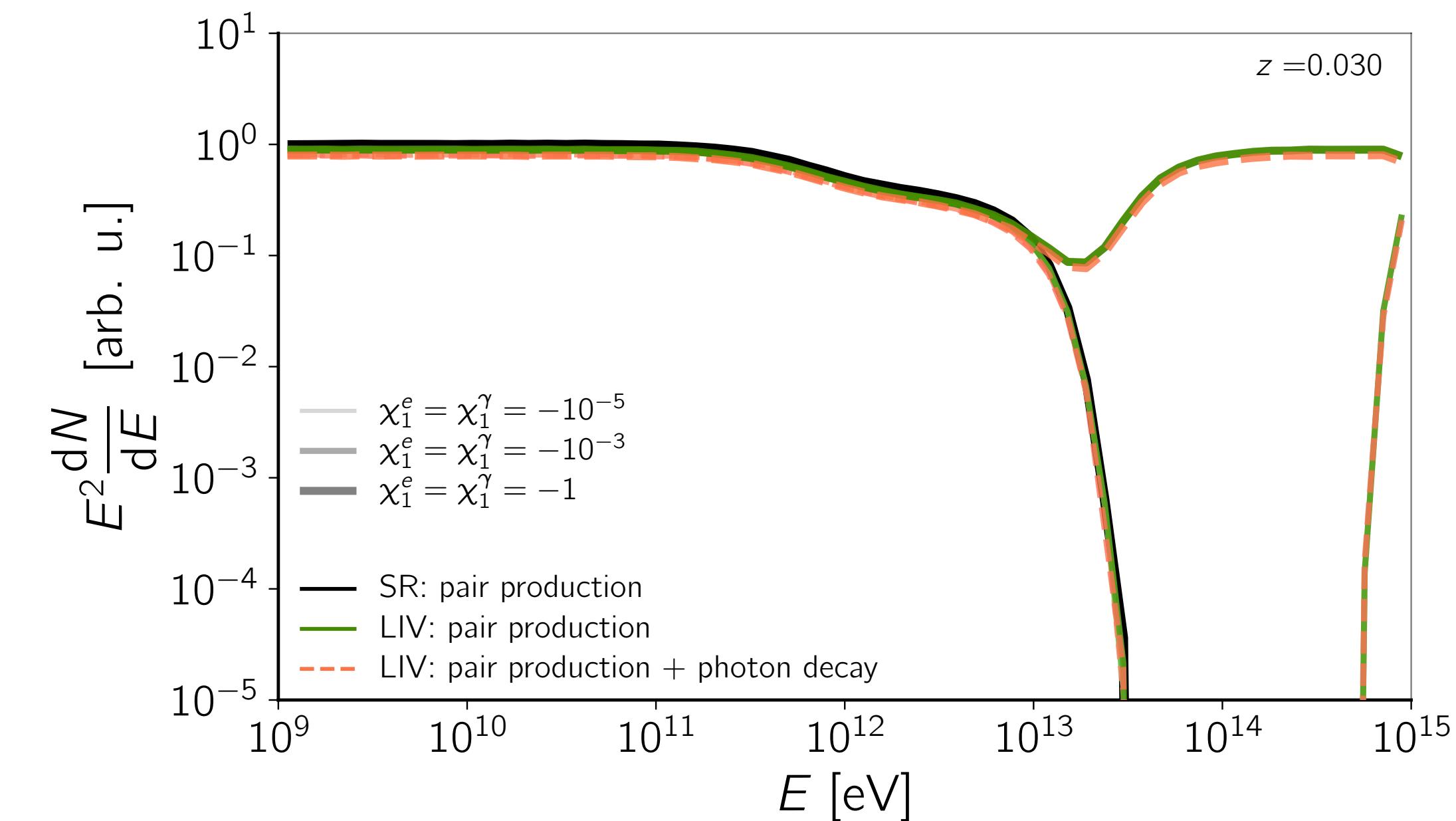
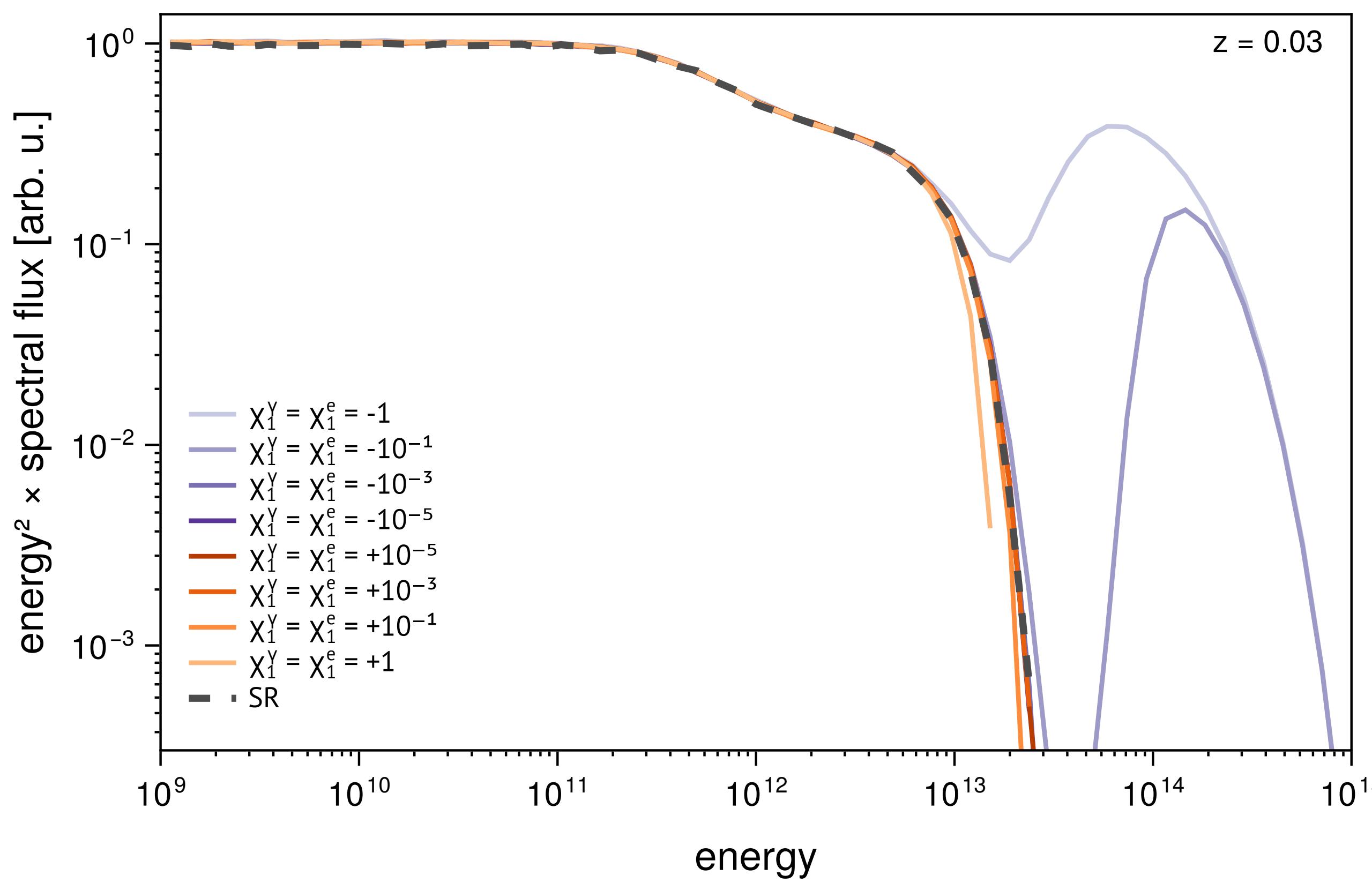


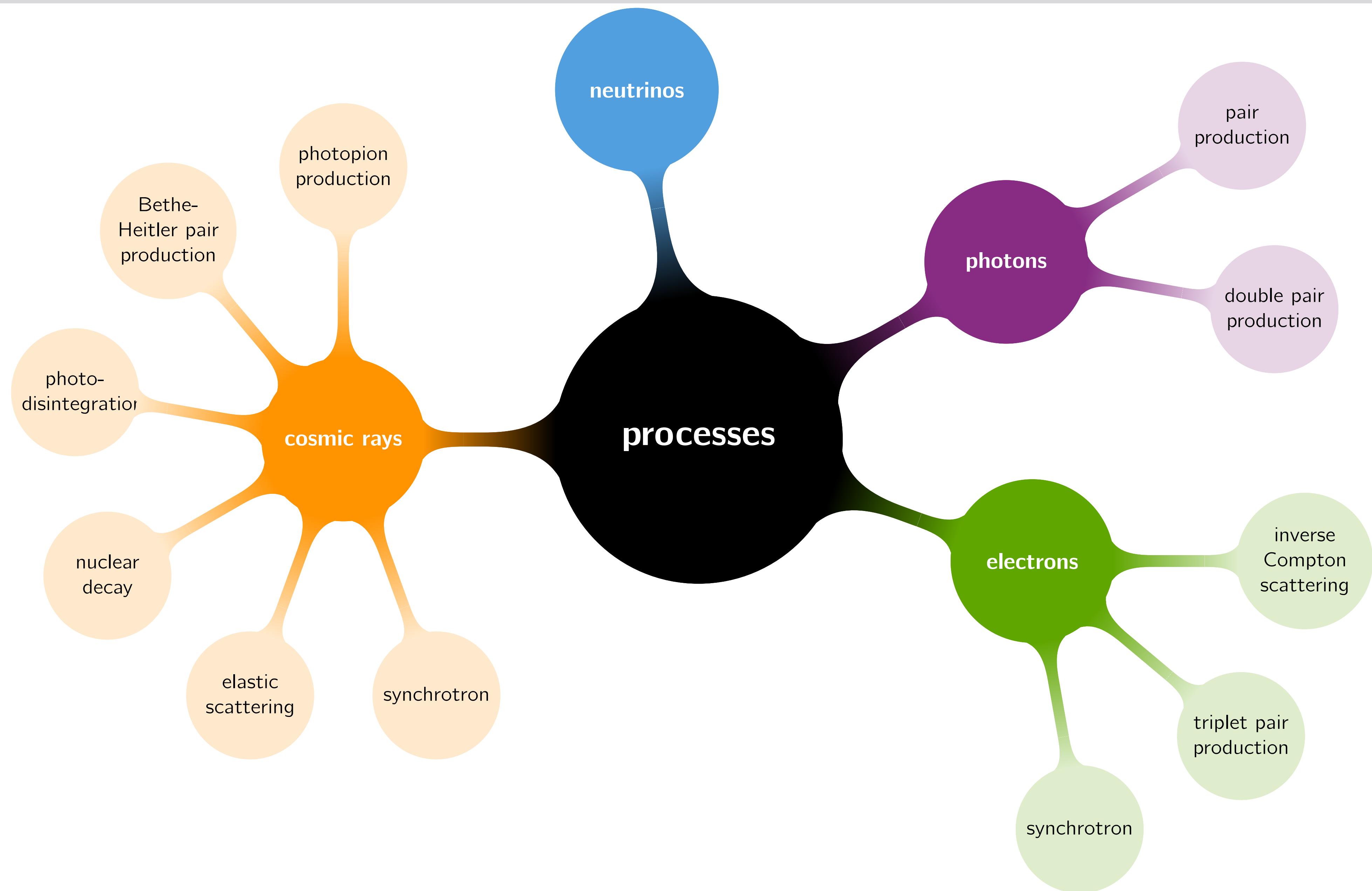
complete simulations of gamma-ray propagation with LIV

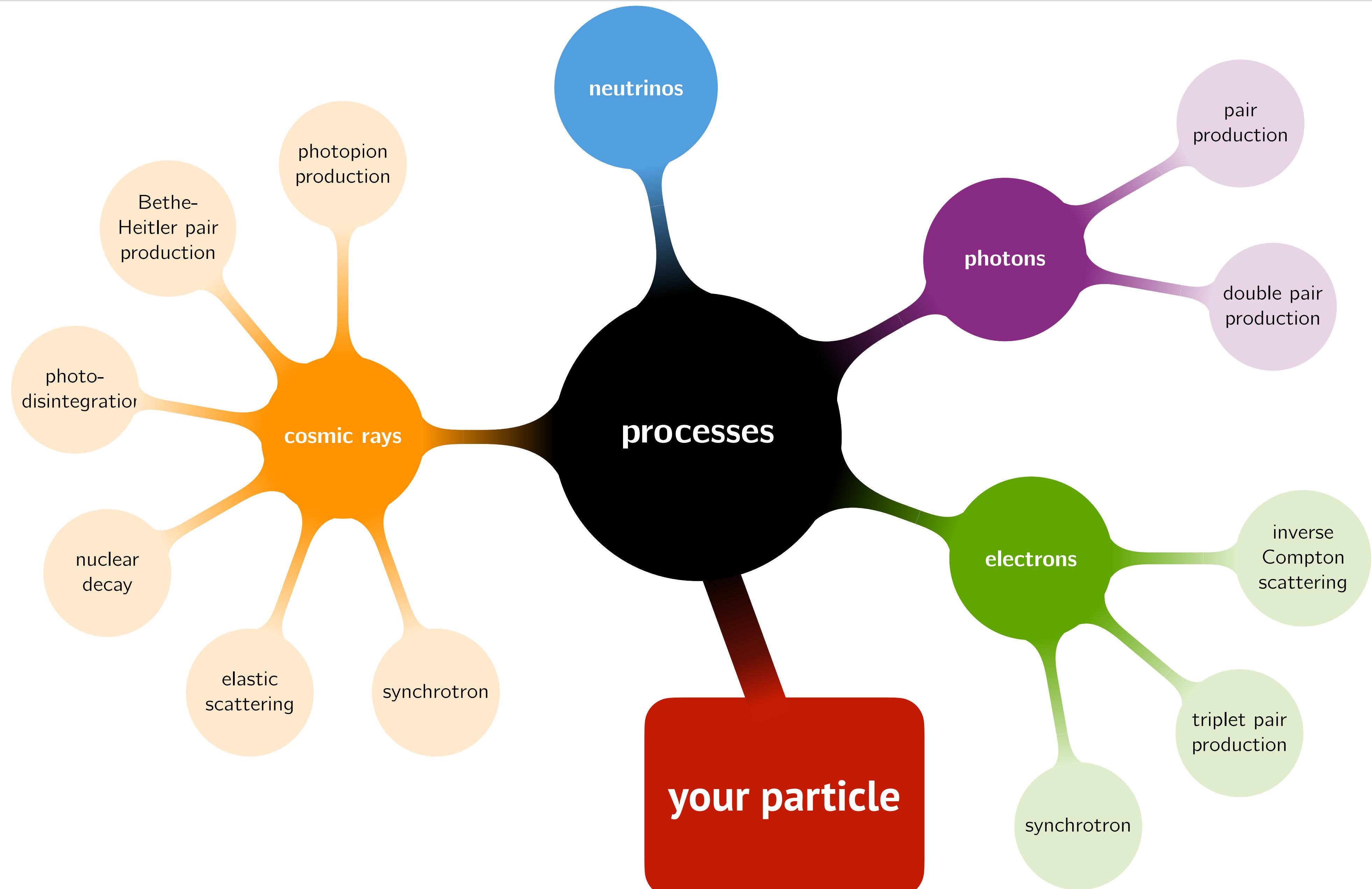
Saveliev & Alves Batista. Class. Quant. Grav. 41 (2024) 115011. arXiv:2312.10803

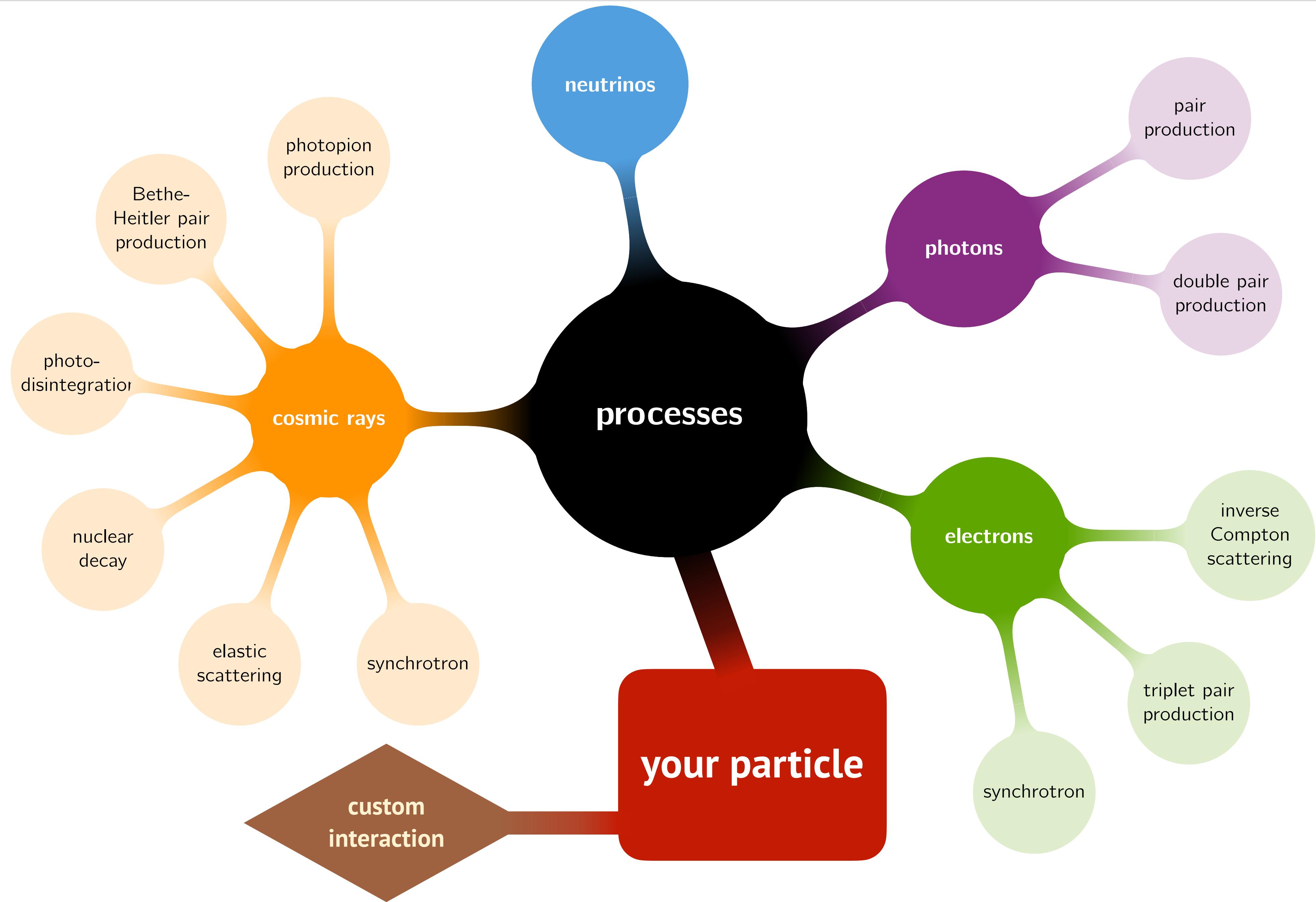
► complete simulations including LIV

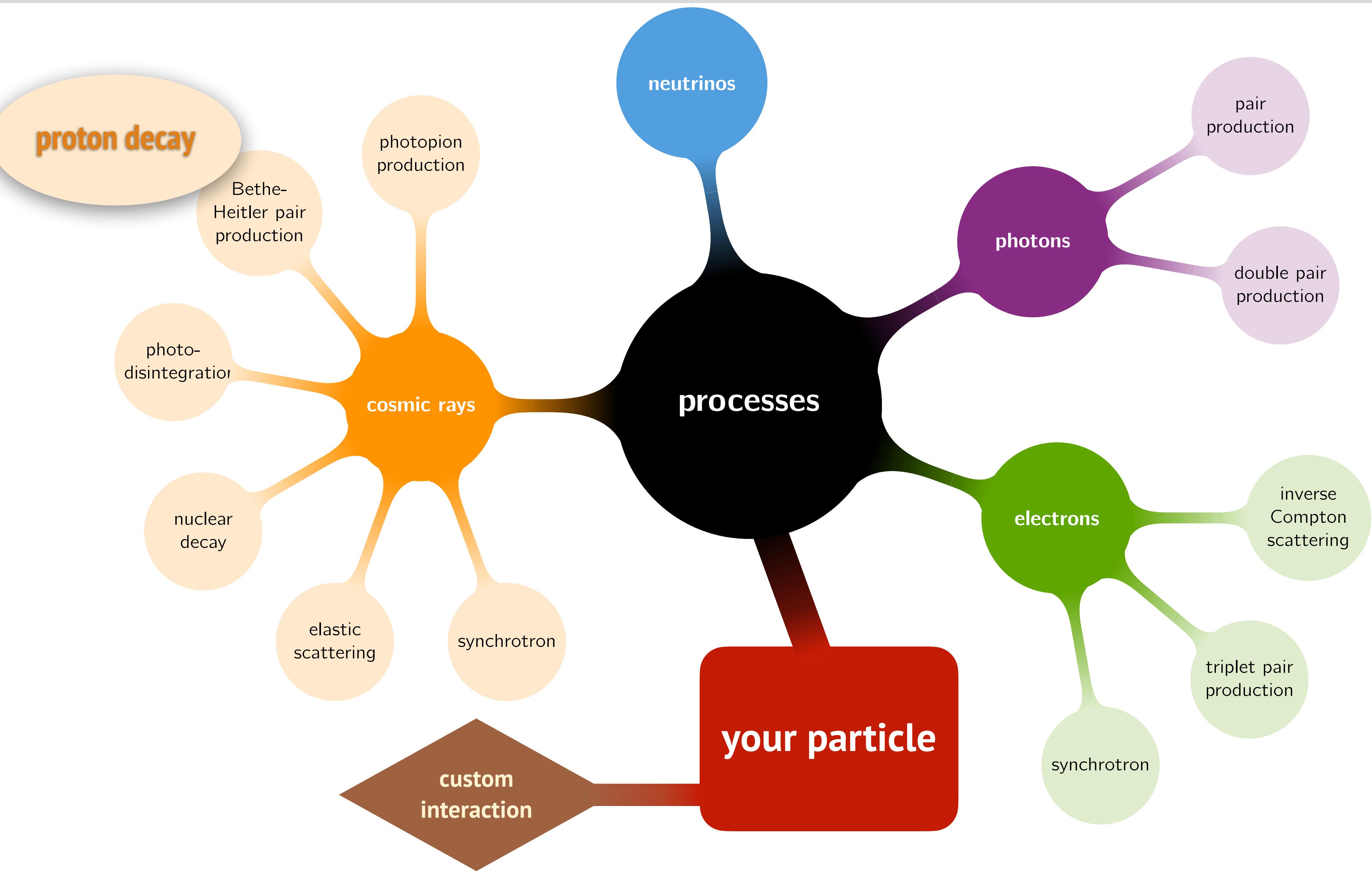
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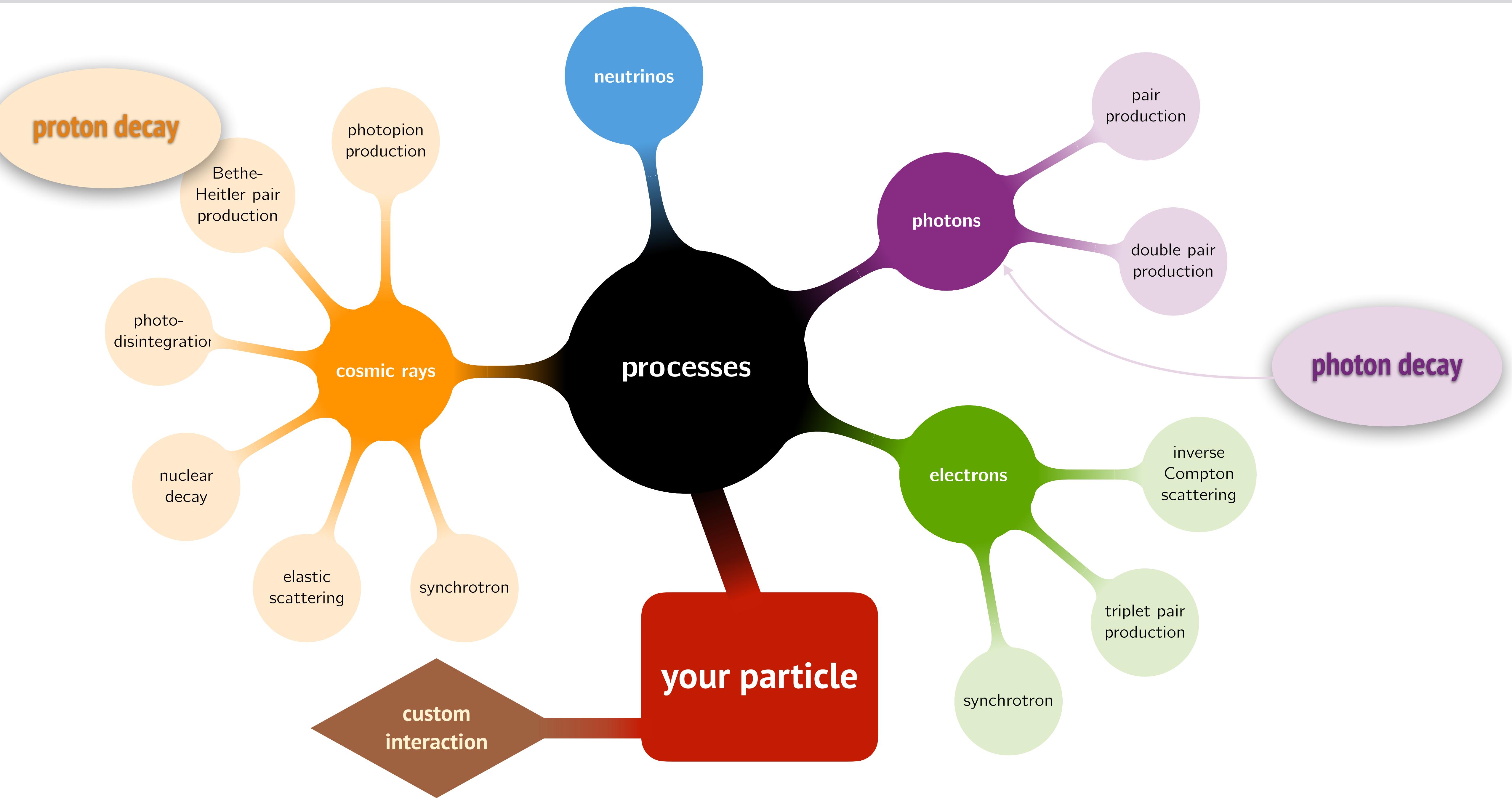


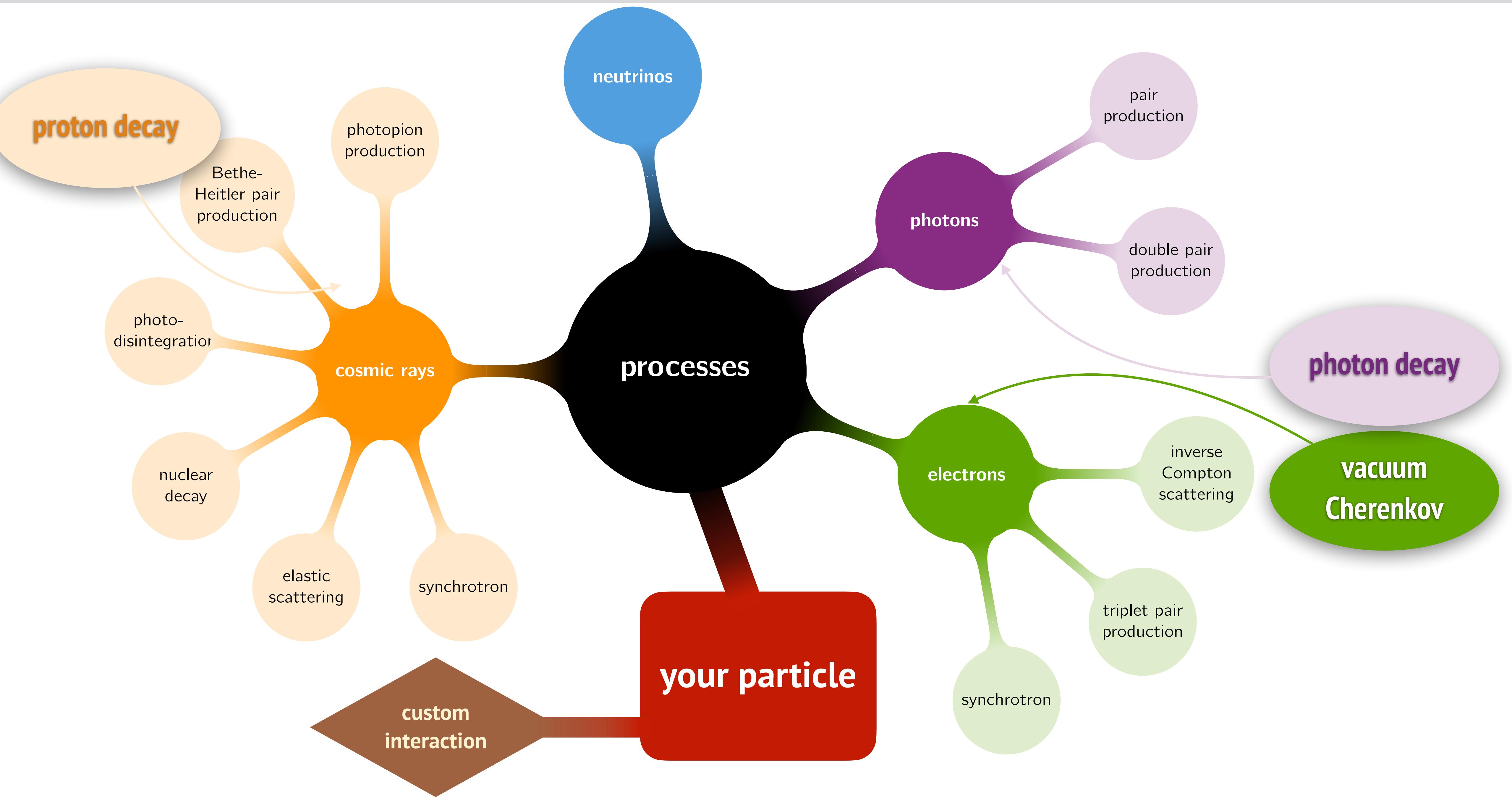












on time lags

$$\Delta t_{\text{obs}}(E_1, E_2) =$$

$$\Delta t_{\text{obs}}(E_1, E_2) = \Delta t_{\text{acc}}(E_1, E_2)$$

acceleration

$$\Delta t_{\text{obs}}(E_1, E_2) = \Delta t_{\text{acc}}(E_1, E_2) + \Delta t_{\text{emi}}(E_1, E_2)$$

acceleration emission

$$\Delta t_{\text{obs}}(E_1, E_2) = \Delta t_{\text{acc}}(E_1, E_2) + \Delta t_{\text{emi}}(E_1, E_2) + \Delta t_G(E_1, E_2)$$

acceleration

emission

gravitational

$$\Delta t_{\text{obs}}(E_1, E_2) = \Delta t_{\text{acc}}(E_1, E_2) + \Delta t_{\text{emi}}(E_1, E_2) + \Delta t_G(E_1, E_2) + \Delta t_B(E_1, E_2)$$

acceleration

emission

gravitational

magnetic

$$\Delta t_{\text{obs}}(E_1, E_2) = \Delta t_{\text{acc}}(E_1, E_2) + \Delta t_{\text{emi}}(E_1, E_2) + \Delta t_G(E_1, E_2) + \Delta t_B(E_1, E_2) + \Delta t_{\text{QG}}(E_1, E_2)$$

acceleration **emission** **gravitational** **magnetic** **QG signal**

$$\Delta t_{\text{obs}}(E_1, E_2) = \Delta t_{\text{acc}}(E_1, E_2) + \Delta t_{\text{emi}}(E_1, E_2) + \Delta t_G(E_1, E_2) + \Delta t_B(E_1, E_2) + \Delta t_{\text{QG}}(E_1, E_2) + \dots$$

acceleration **emission** **gravitational** **magnetic** **QG signal**

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acceleration **emission** **gravitational** **magnetic** **QG signal**

$$\Delta t_{\text{obs}}(E_1, E_2) = \Delta t_{\text{acc}}(E_1, E_2) + \Delta t_{\text{emi}}(E_1, E_2) + \Delta t_G(E_1, E_2) + \Delta t_B(E_1, E_2) + \Delta t_{\text{QG}}(E_1, E_2) + \dots$$

acceleration	emission	gravitational	magnetic	QG signal
---------------------	-----------------	----------------------	-----------------	------------------

charged particles

$$\Delta t_B \approx \begin{cases} q^2 c \frac{B^2 L_{\text{src}}^2 L_B}{18 E^2} = 10^6 \left(\frac{q}{e}\right)^2 \left(\frac{B}{10^{-15} \text{ T}}\right)^2 \left(\frac{E}{100 \text{ EeV}}\right)^{-2} \left(\frac{L_{\text{src}}}{100 \text{ Mpc}}\right)^2 \left(\frac{L_B}{1 \text{ Mpc}}\right) \text{ yr} & \text{if } L_{\text{src}} \gg L_B, \\ q^2 c \frac{B^2 L_{\text{src}}^3}{24 E^2} = 4200 \left(\frac{q}{e}\right)^2 \left(\frac{B}{10^{-15} \text{ T}}\right)^2 \left(\frac{E}{100 \text{ EeV}}\right)^{-2} \left(\frac{L_{\text{src}}}{100 \text{ Mpc}}\right)^3 \text{ yr} & \text{if } L_{\text{src}} \ll L_B. \end{cases}$$

$$\Delta t_{\text{obs}}(E_1, E_2) = \Delta t_{\text{acc}}(E_1, E_2) + \Delta t_{\text{emi}}(E_1, E_2) + \Delta t_G(E_1, E_2) + \Delta t_B(E_1, E_2) + \Delta t_{\text{QG}}(E_1, E_2) + \dots$$

acceleration **emission** **gravitational** **magnetic** **QG signal**

$$\Delta t_{\text{obs}}(E_1, E_2) = \Delta t_{\text{acc}}(E_1, E_2) + \Delta t_{\text{emi}}(E_1, E_2) + \Delta t_G(E_1, E_2) + \Delta t_B(E_1, E_2) + \Delta t_{\text{QG}}(E_1, E_2) + \dots$$

acceleration emission gravitational magnetic QG signal

gamma rays (approximation including cascade effects) [Neronov & Semikoz 2009]

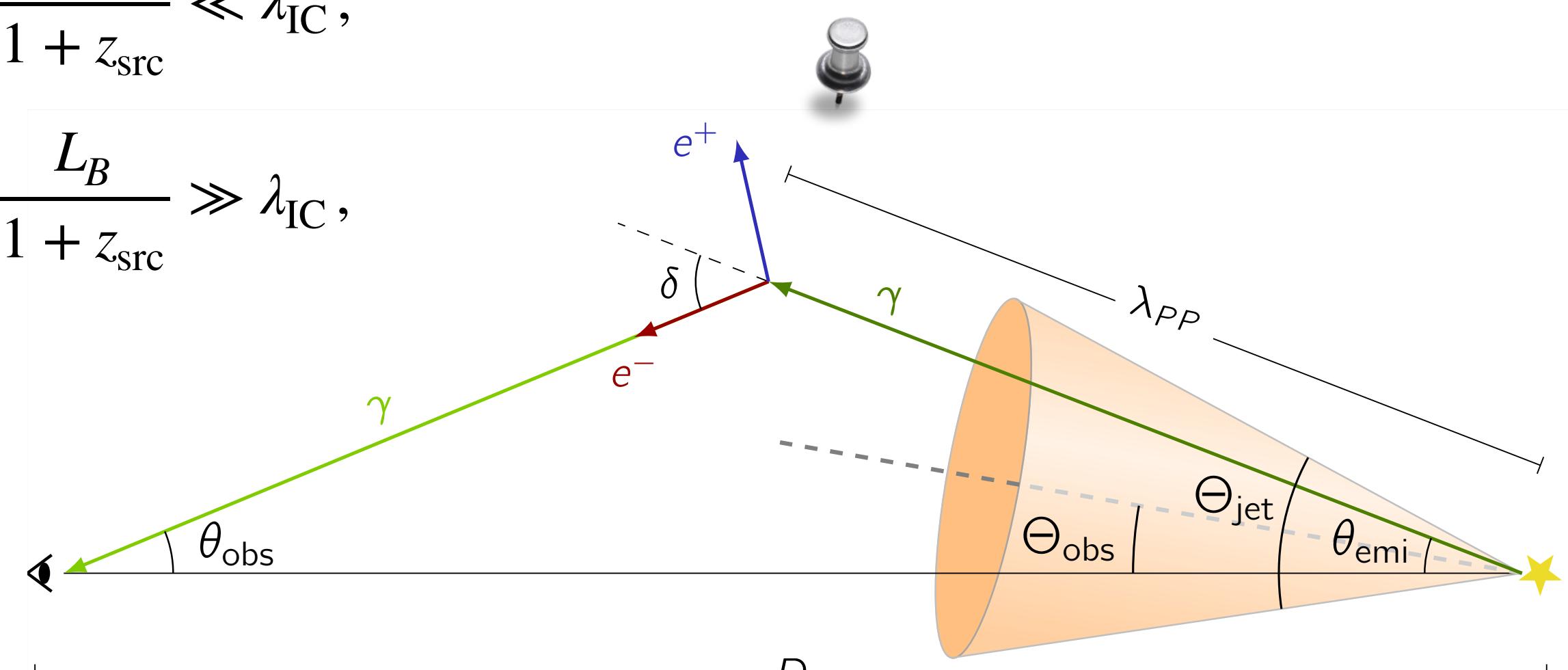
$$\Delta t_B \simeq \begin{cases} 1.0 \times 10^4 \frac{\kappa(1 - \tau_\theta^{-1})}{(1 + z_{\text{src}})^2} \left(\frac{E}{1 \text{ TeV}}\right)^{-2} \left(\frac{B}{10^{-21} \text{ T}}\right)^2 \left(\frac{L_B}{1 \text{ kpc}}\right) \text{ s} & \text{if } \frac{L_B}{1 + z_{\text{src}}} \ll \lambda_{\text{IC}}, \\ 2.2 \times 10^5 \frac{\kappa(1 - \tau_\theta^{-1})}{(1 + z_{\text{src}})^5} \left(\frac{E}{1 \text{ TeV}}\right)^{-\frac{5}{2}} \left(\frac{B}{10^{-21} \text{ T}}\right)^2 \text{ s} & \text{if } \frac{L_B}{1 + z_{\text{src}}} \gg \lambda_{\text{IC}}, \end{cases}$$

$$\Delta t_{\text{obs}}(E_1, E_2) = \Delta t_{\text{acc}}(E_1, E_2) + \Delta t_{\text{emi}}(E_1, E_2) + \Delta t_G(E_1, E_2) + \Delta t_B(E_1, E_2) + \Delta t_{\text{QG}}(E_1, E_2) + \dots$$

acceleration emission gravitational magnetic QG signal

gamma rays (approximation including cascade effects) [Neronov & Semikoz 2009]

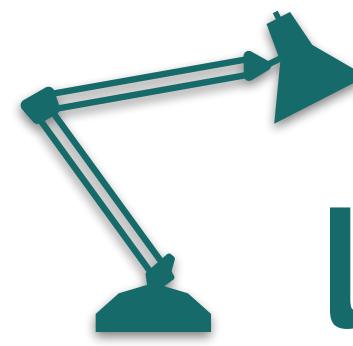
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Alves Batista & Saveliev. Universe 7 (2021) 223. arXiv:2105.12020

discussion

two approaches: lamp and lighthouse



lamp approach

rigorous focused approach

look at few observables / effects at a time

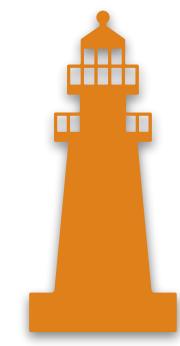
phenomenologically-motivated

excellent for clean signals

empirically adequate

allow for inconsistencies

parsimonious and descriptive



lighthouse approach

complex brute-force approach

exploits correlations → reduces parameter space

phenomenologically- or theoretically-motivated

weaker but sturdier constraints

empirically adequate

imposes internal consistency

complex and more explanatory

some thoughts on model-building

are there QG signatures in the data?

are there QG signatures in the data?

$$p(\theta_{\text{QG}} | D) \propto p(D | \theta_{\text{QG}}) p(\theta_{\text{QG}})$$

are there QG signatures in the data?

$$p(\theta_{\text{QG}} | D) \propto p(D | \theta_{\text{QG}}) p(\theta_{\text{QG}})$$

$$p(D | \theta_{\text{QG}}) = \iiint$$

are there QG signatures in the data?

$$p(\theta_{\text{QG}} | D) \propto p(D | \theta_{\text{QG}}) p(\theta_{\text{QG}})$$

$$p(D | \theta_{\text{QG}}) = \prod p(D | \theta_{\text{QG}})$$

are there QG signatures in the data?

$$p(\theta_{\text{QG}} | D) \propto p(D | \theta_{\text{QG}}) p(\theta_{\text{QG}})$$

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$$p(D | \theta_{\text{QG}}) = \iiint p(D | \theta_{\text{QG}}, \theta_{\text{prop}} \text{ propagation uncertainties}) p(\theta_{\text{prop}}) d\theta_{\text{prop}}$$

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$$p(D | \theta_{\text{QG}}) = \iiint p(D | \theta_{\text{QG}}, \theta_{\text{prop}}, \theta_{\text{src}}) p(\theta_{\text{prop}}) p(\theta_{\text{src}}) d\theta_{\text{src}} d\theta_{\text{prop}}$$

propagation uncertainties source uncertainties

are there QG signatures in the data?

$$p(\theta_{\text{QG}} | D) \propto p(D | \theta_{\text{QG}}) p(\theta_{\text{QG}})$$

$$p(D | \theta_{\text{QG}}) = \iiint p(D | \theta_{\text{QG}}, \theta_{\text{prop}}, \theta_{\text{src}}, \quad) \quad p(\theta_{\text{prop}}) \quad p(\theta_{\text{src}}) \quad d\theta_{\text{src}} d\theta_{\text{prop}}$$

propagation
uncertainties source
uncertainties

are there QG signatures in the data?

$$p(\theta_{\text{QG}} | D) \propto p(D | \theta_{\text{QG}}) p(\theta_{\text{QG}})$$

$$p(D | \theta_{\text{QG}}) = \iiint p(D | \theta_{\text{QG}}, \theta_{\text{prop}}, \theta_{\text{src}}, \theta_{\text{inst}}) \ p(\theta_{\text{prop}}) \ p(\theta_{\text{src}}) \ d\theta_{\text{src}} d\theta_{\text{prop}}$$

propagation
uncertainties source
uncertainties

are there QG signatures in the data?

$$p(\theta_{\text{QG}} | D) \propto p(D | \theta_{\text{QG}}) p(\theta_{\text{QG}})$$

$$p(D | \theta_{\text{QG}}) = \iiint p(D | \theta_{\text{QG}}, \theta_{\text{prop}}, \theta_{\text{src}}, \theta_{\text{inst}}) \ p(\theta_{\text{prop}}) \ p(\theta_{\text{src}}) \ p(\theta_{\text{inst}}) \ d\theta_{\text{inst}} d\theta_{\text{src}} d\theta_{\text{prop}}$$

propagation
uncertainties source
uncertainties instrumental
uncertainties

- ▶ **sink terms** affecting propagation are considered
- ▶ rarely new **source terms** are considered on top of standard ones (new processes)
- ▶ results are only as good as the models on which they are based
- ▶ problem with lamp strategy: *dutch book argument*
- ▶ combine **multiple messengers**
- ▶ build models covering **larger parameter space**
 - ◆ dimensional reduction from correlations / couplings
- ▶ epistemic goal: coherence over tightness