

# Astrophysical Searches for Quantum Gravity: what multi-messenger observations can (and cannot) tell us

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🏠 [www.8rafael.com](http://www.8rafael.com)

BridgeQG Workshop  
Annecy, February 4-6 2026



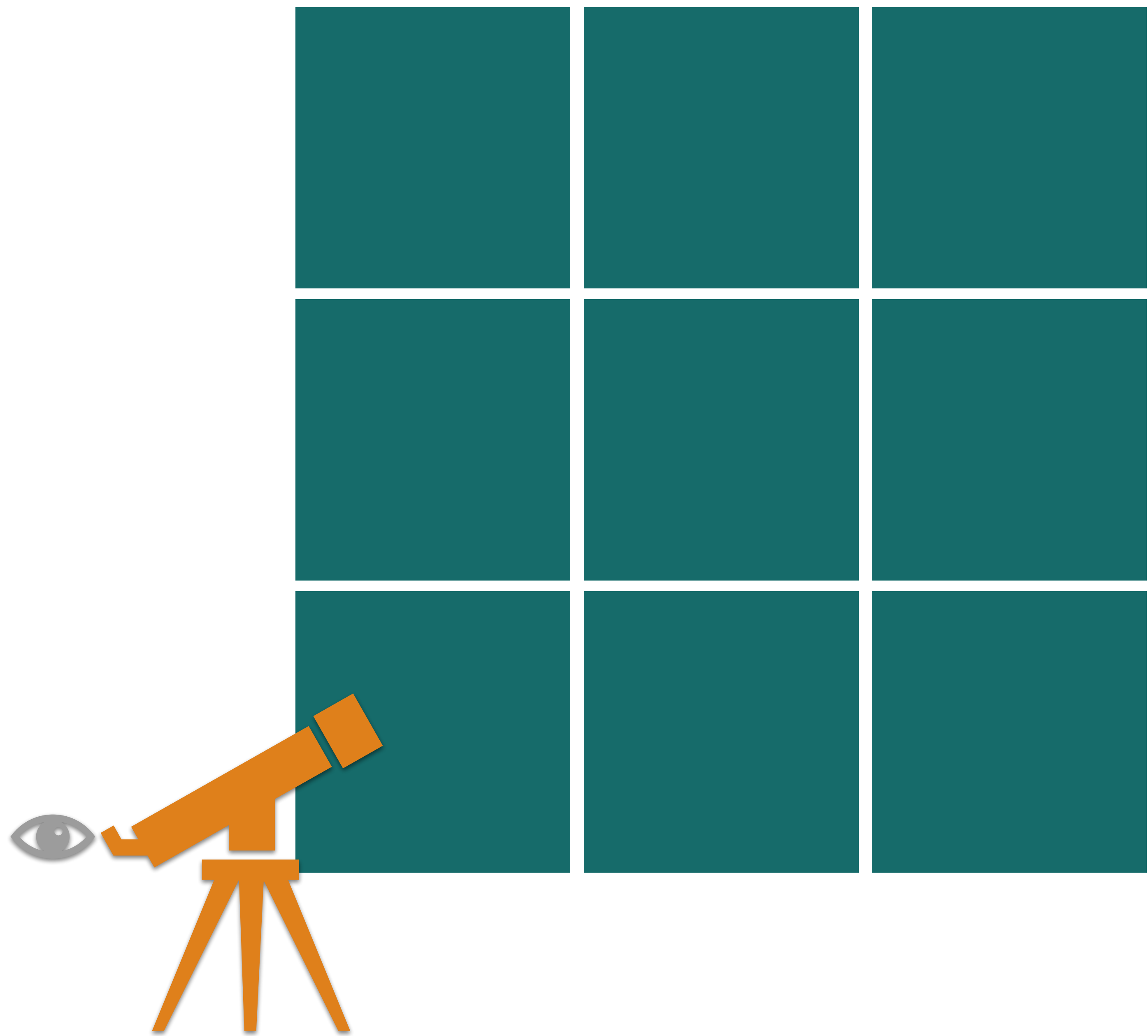
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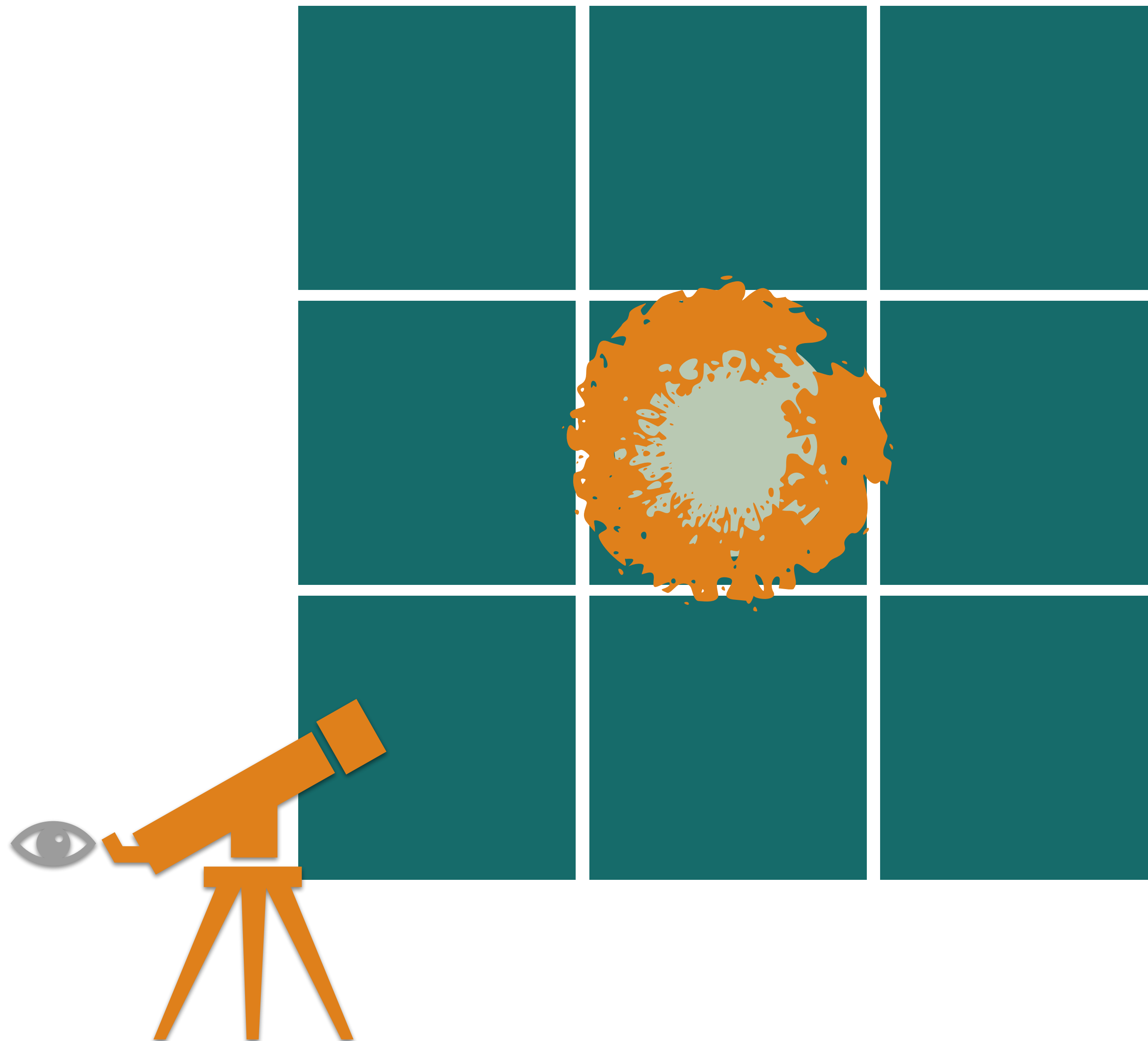
would we be able to tell?



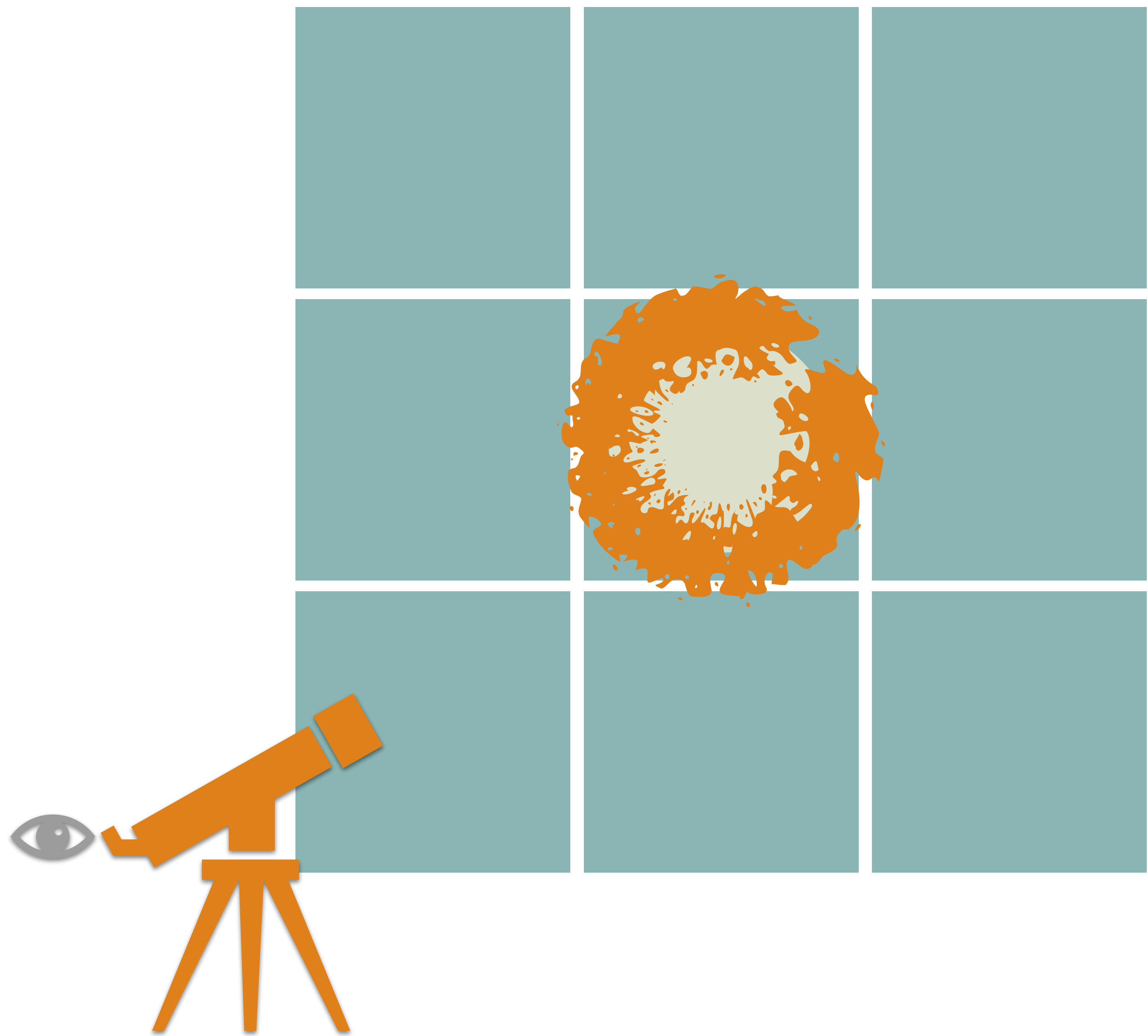




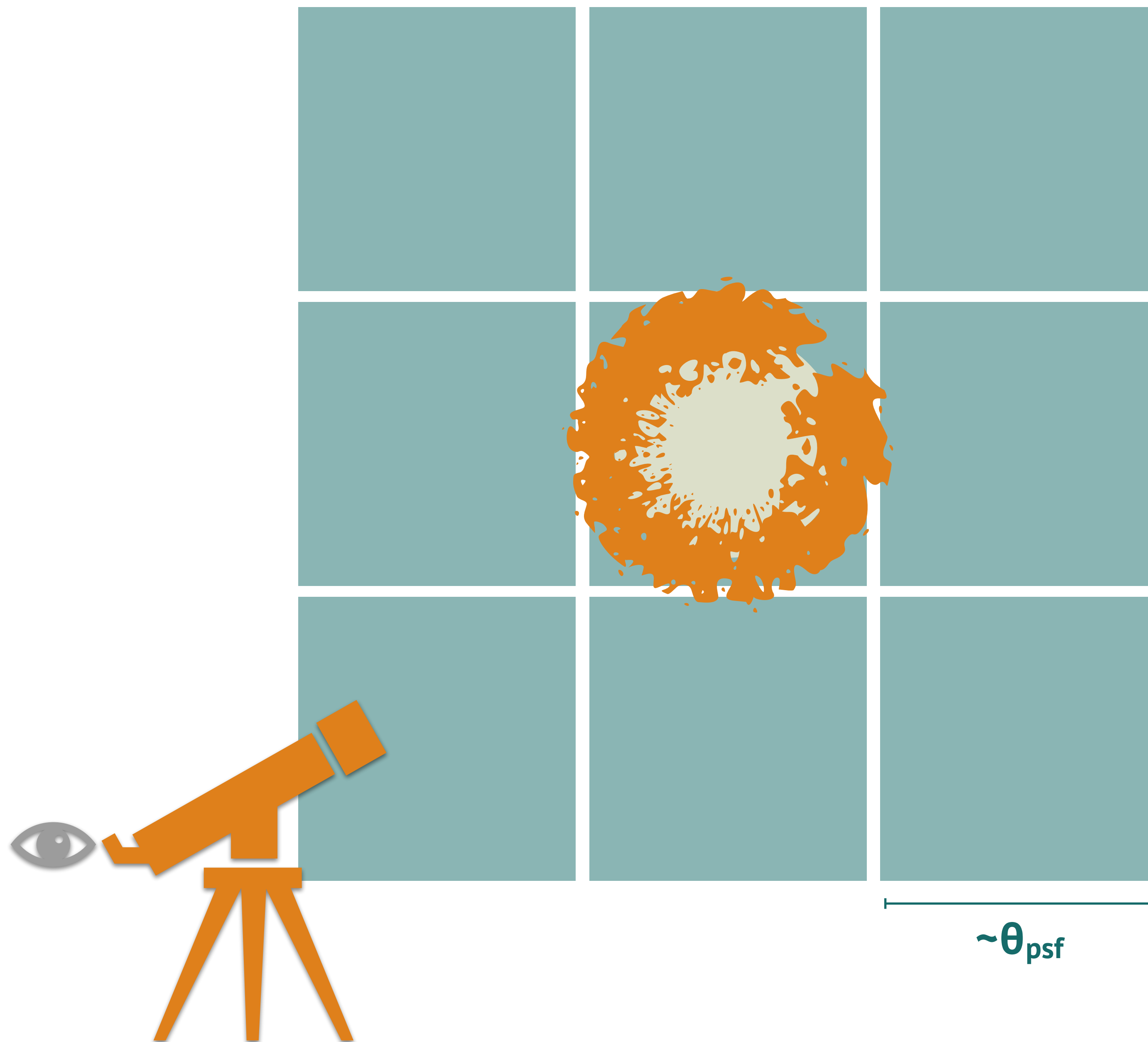
# what do we observe?



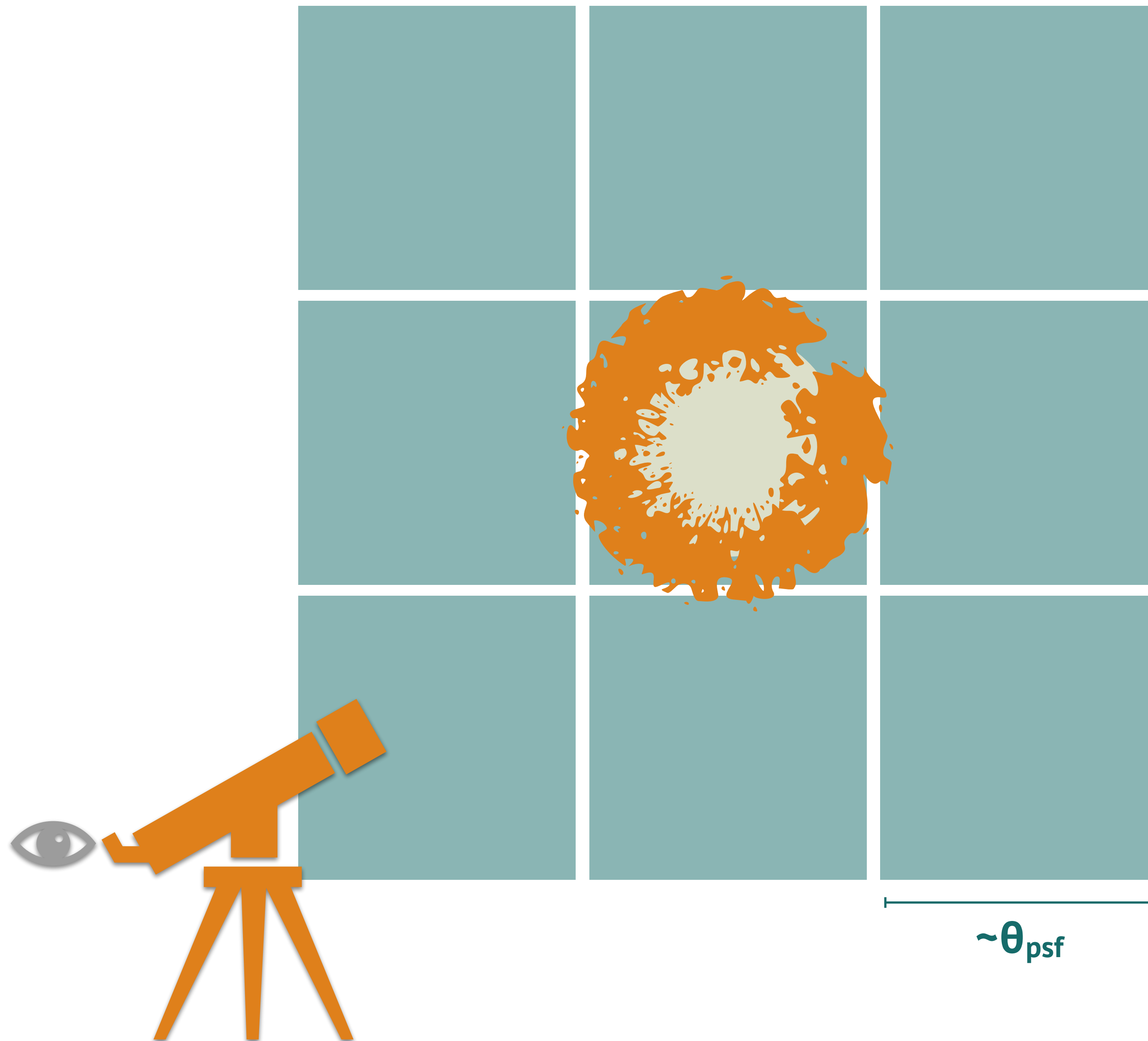
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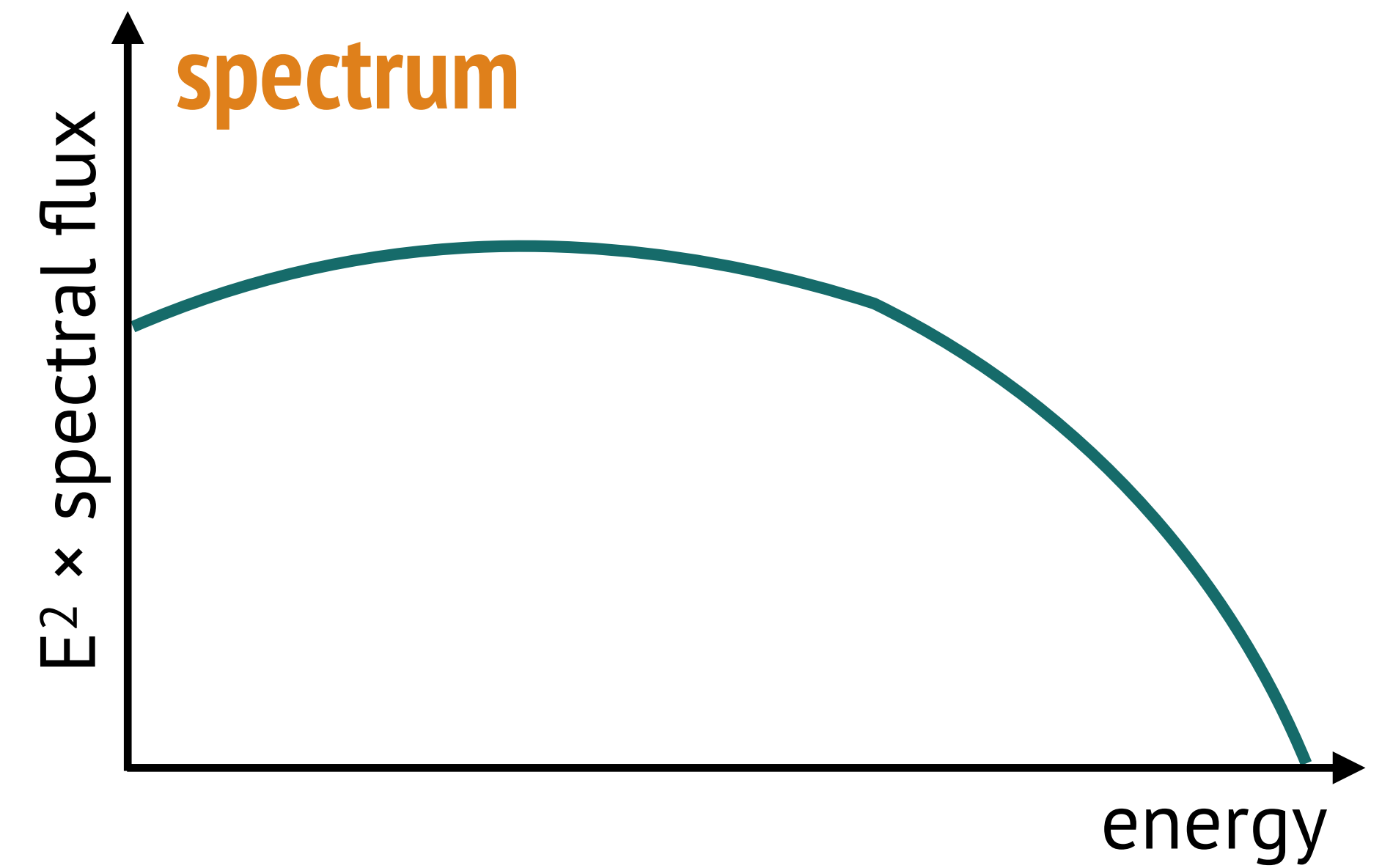
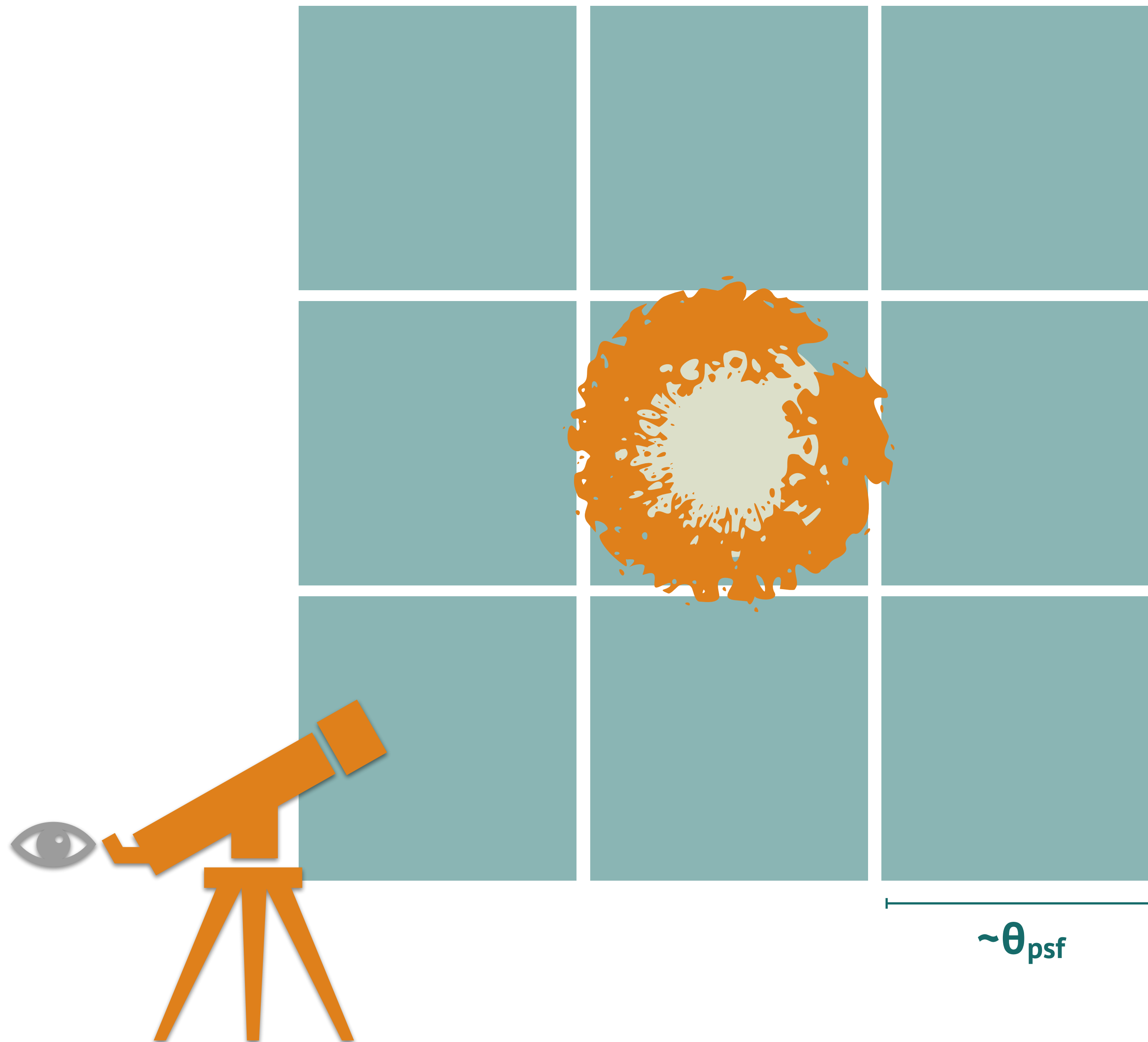


arrival directions



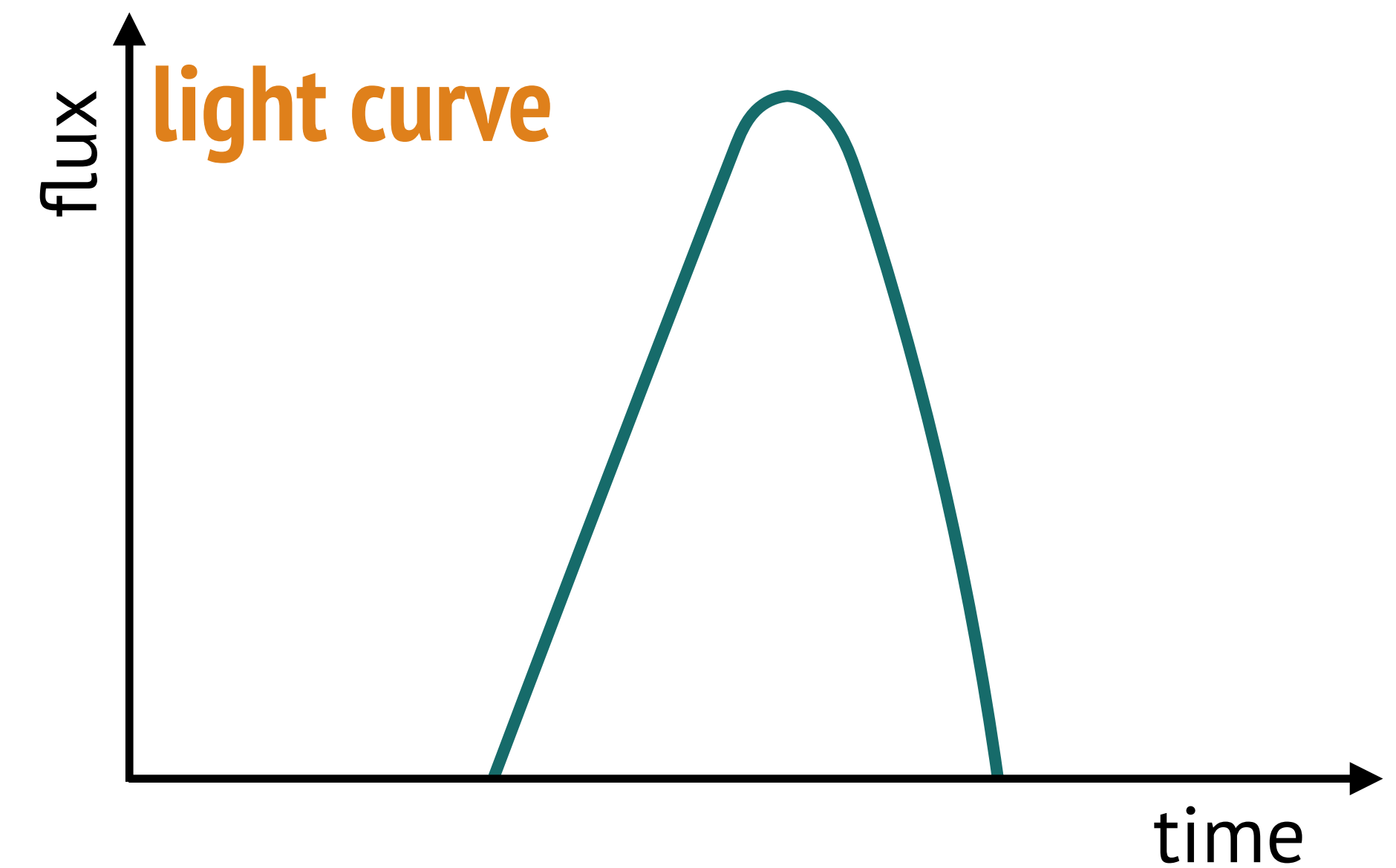
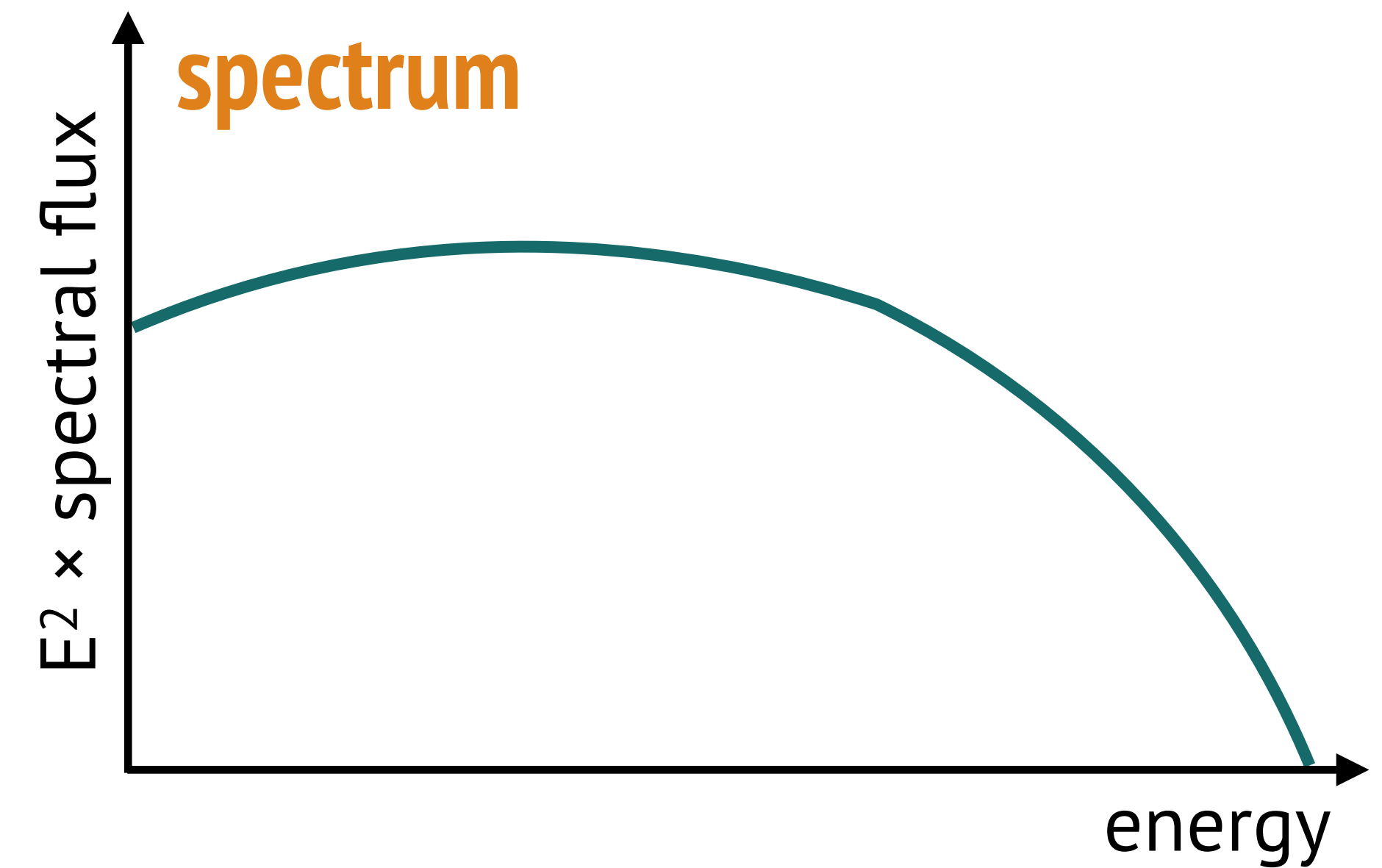
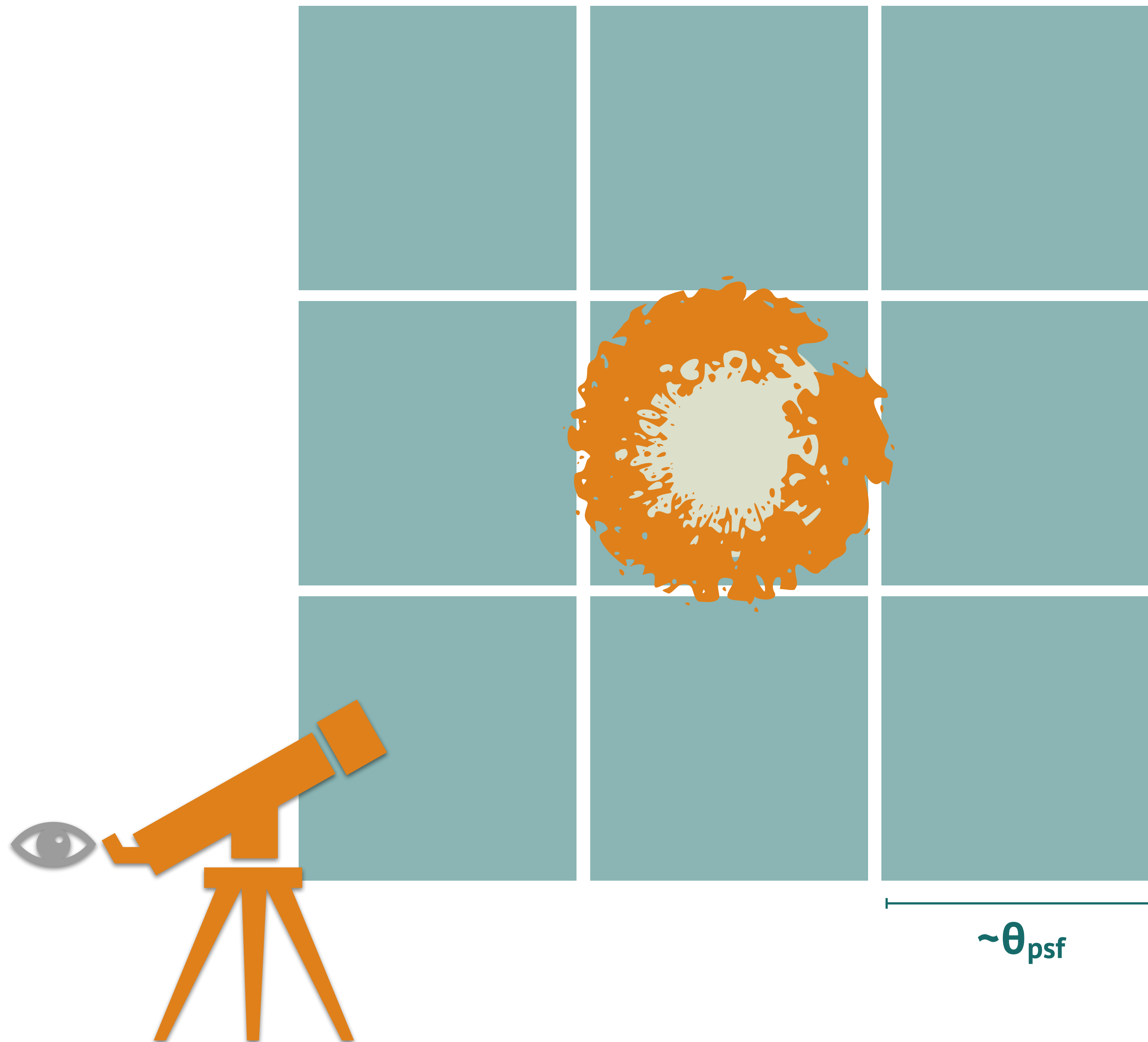
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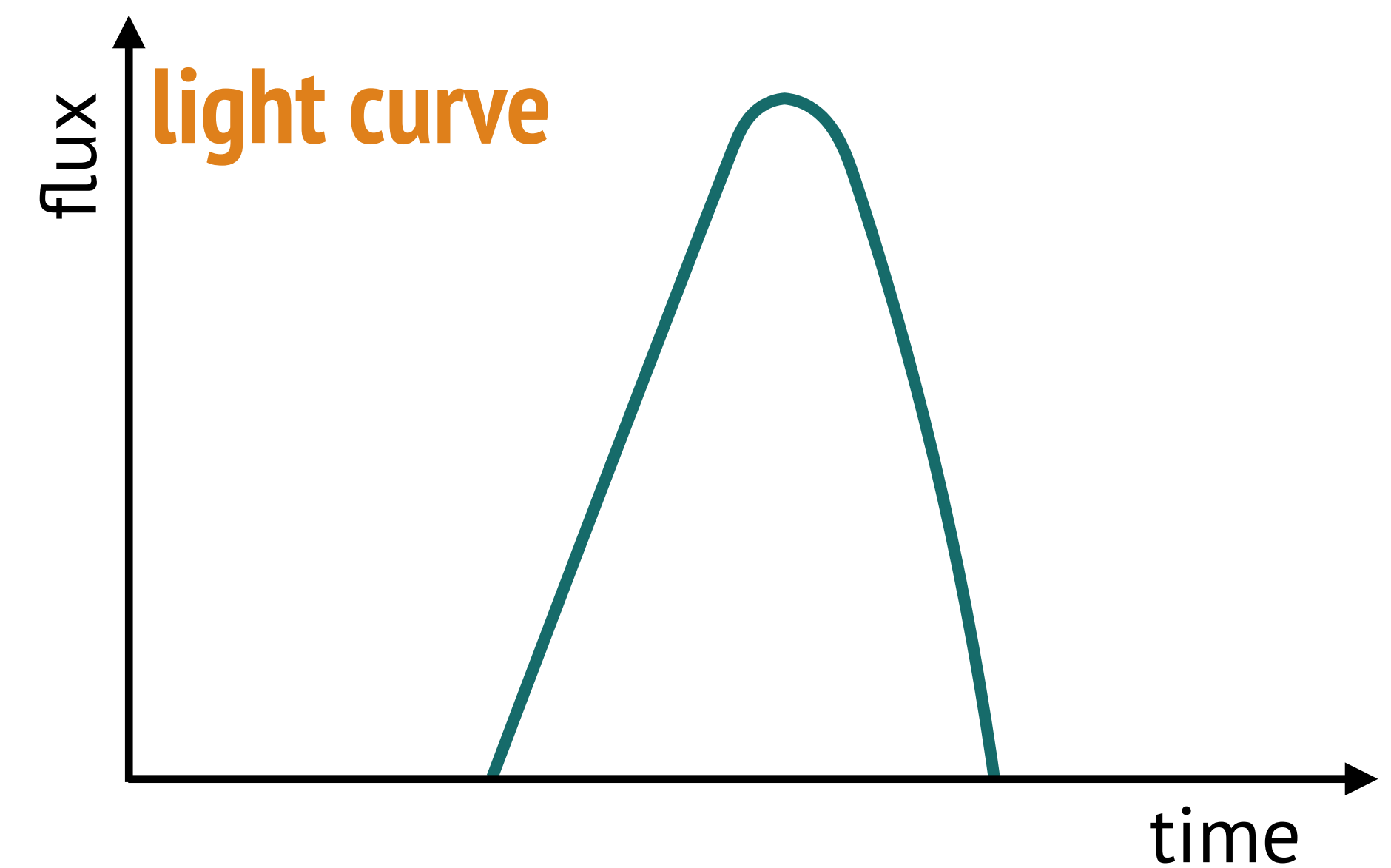
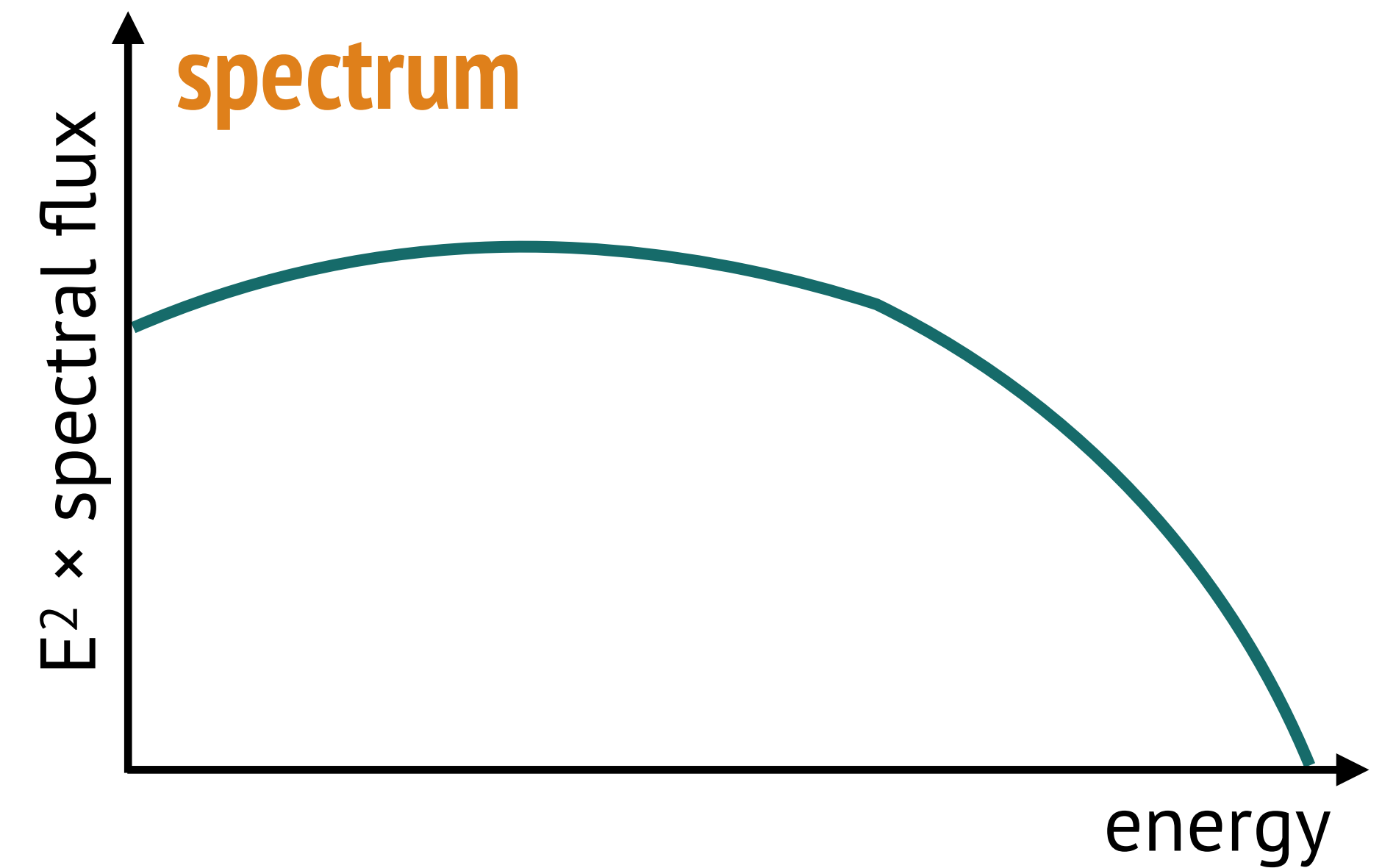
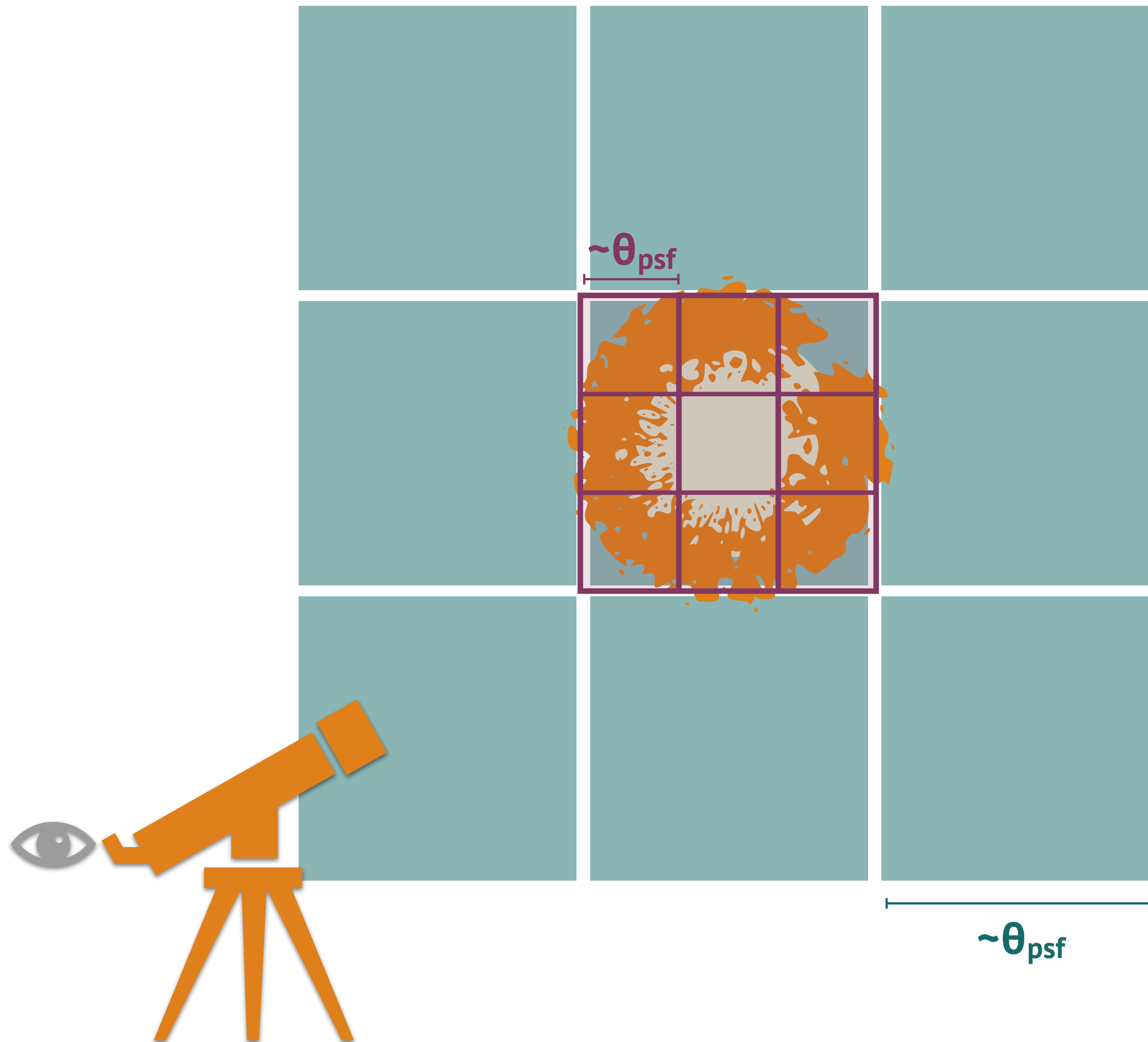
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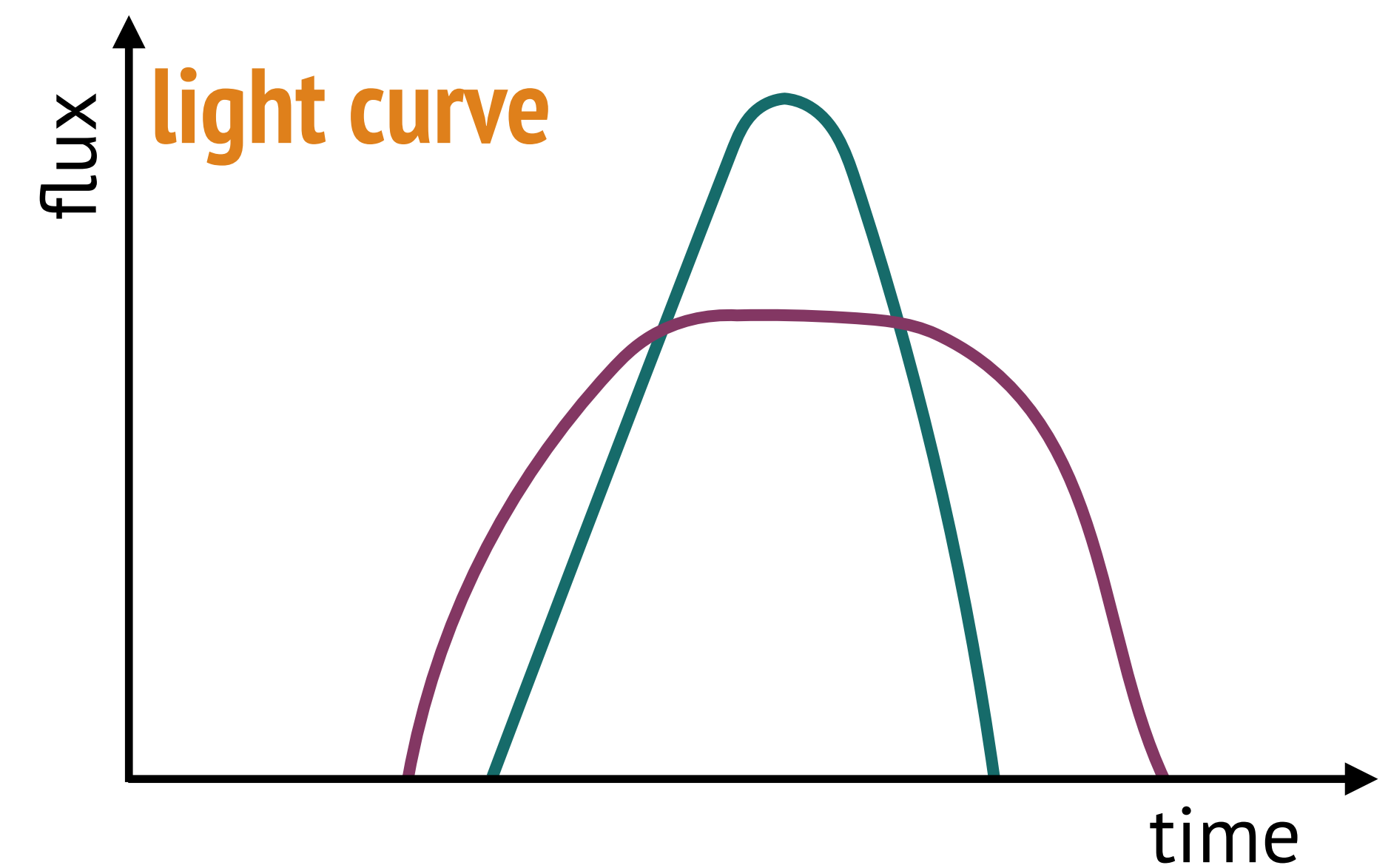
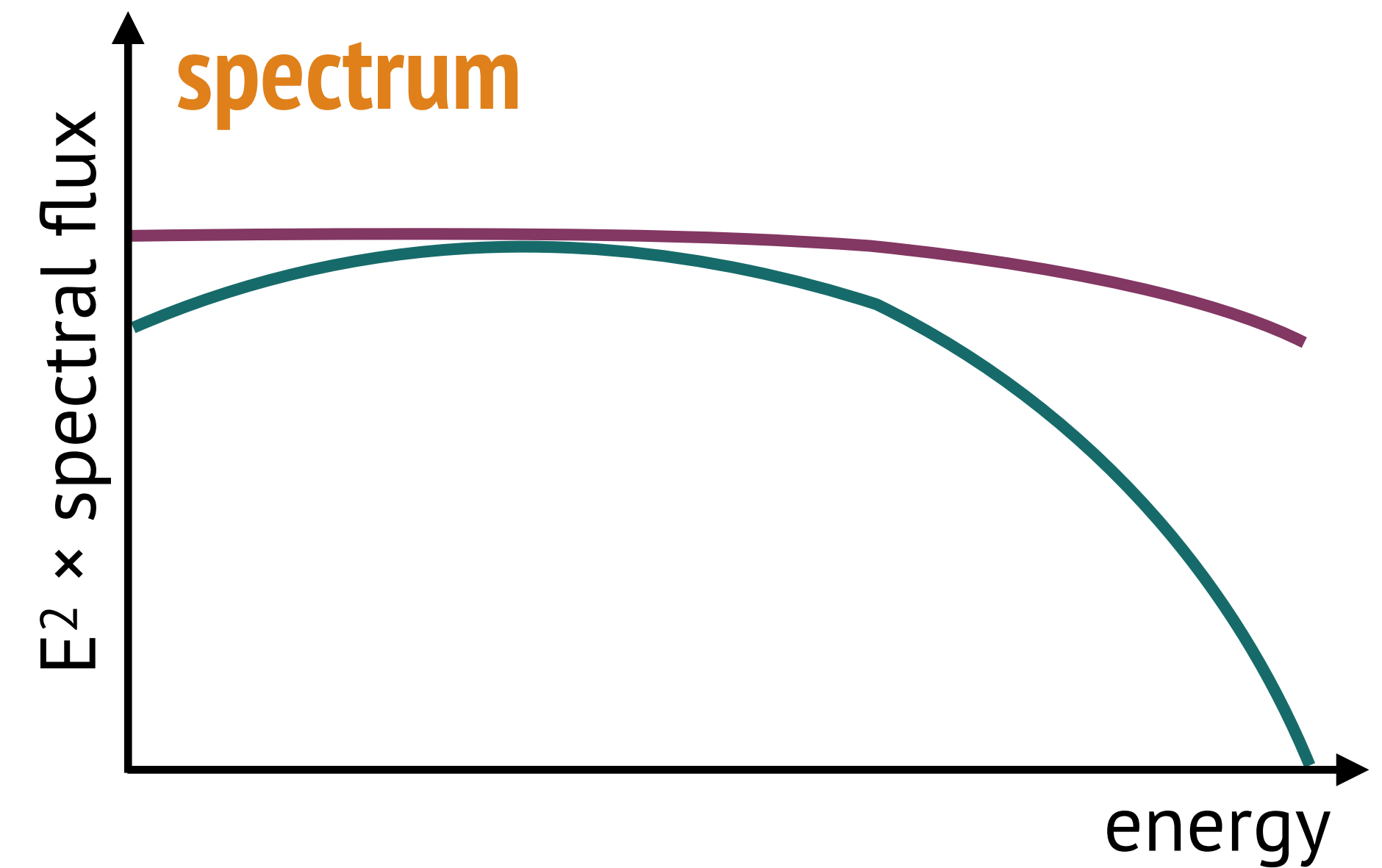
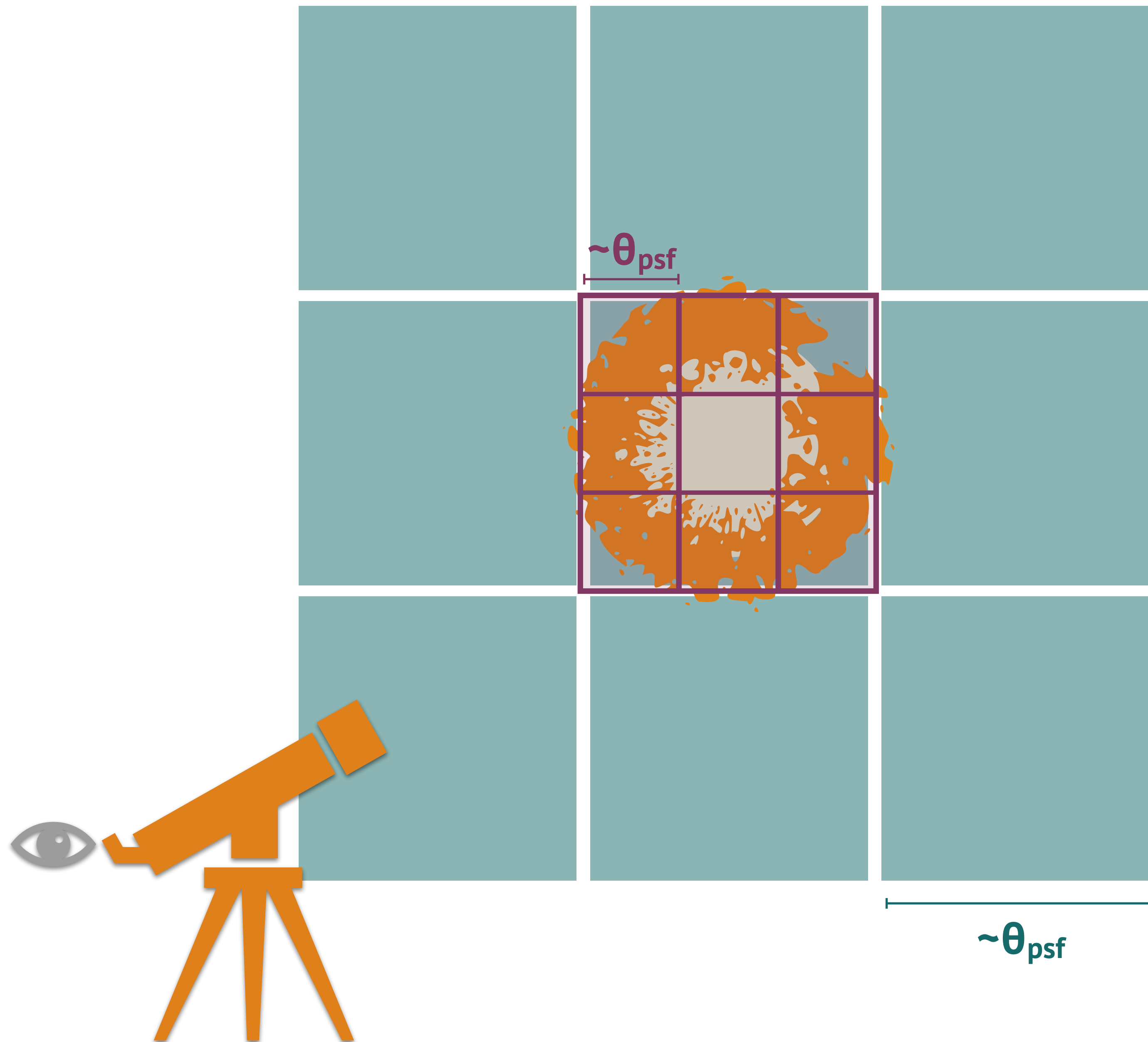
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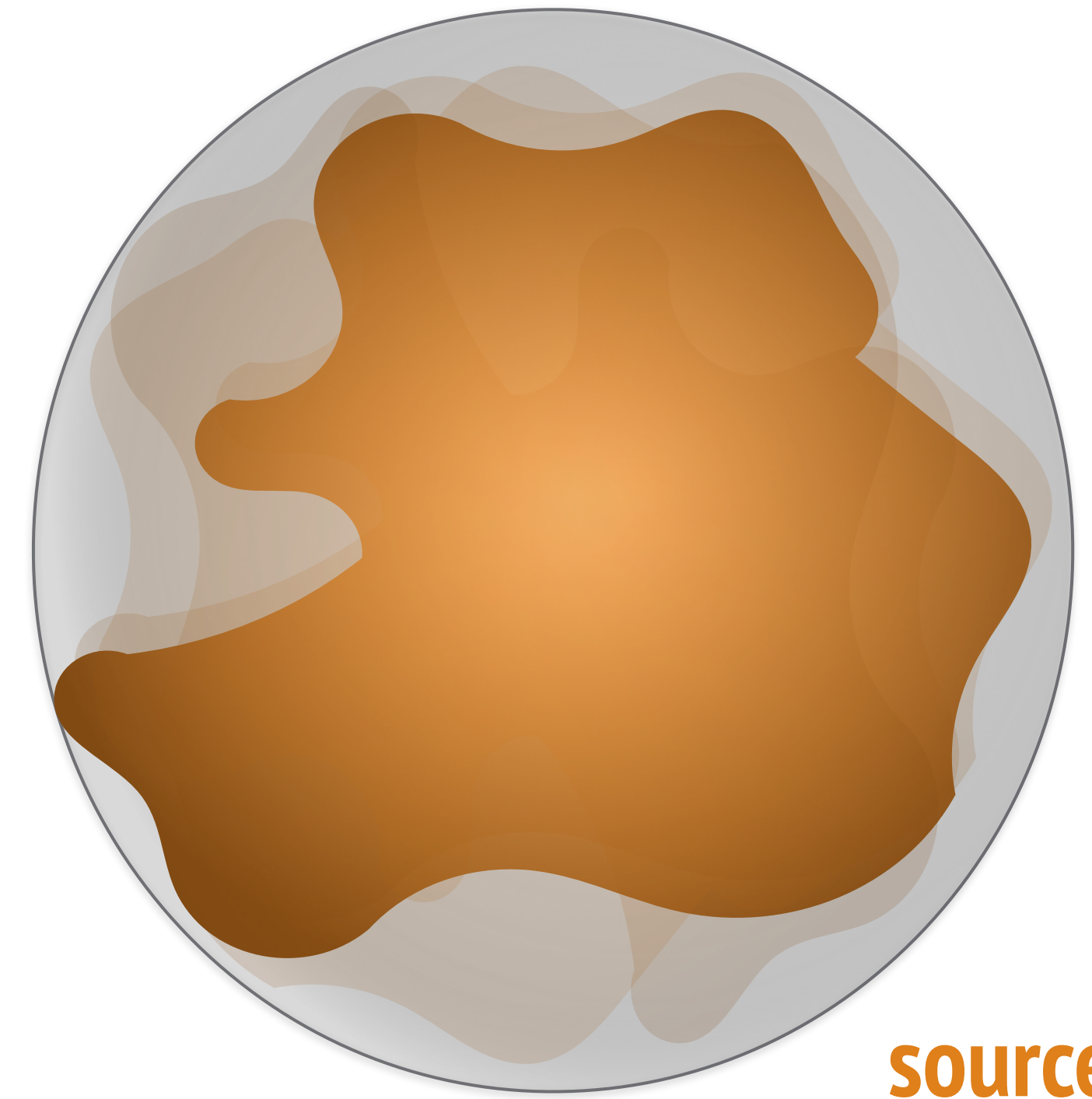
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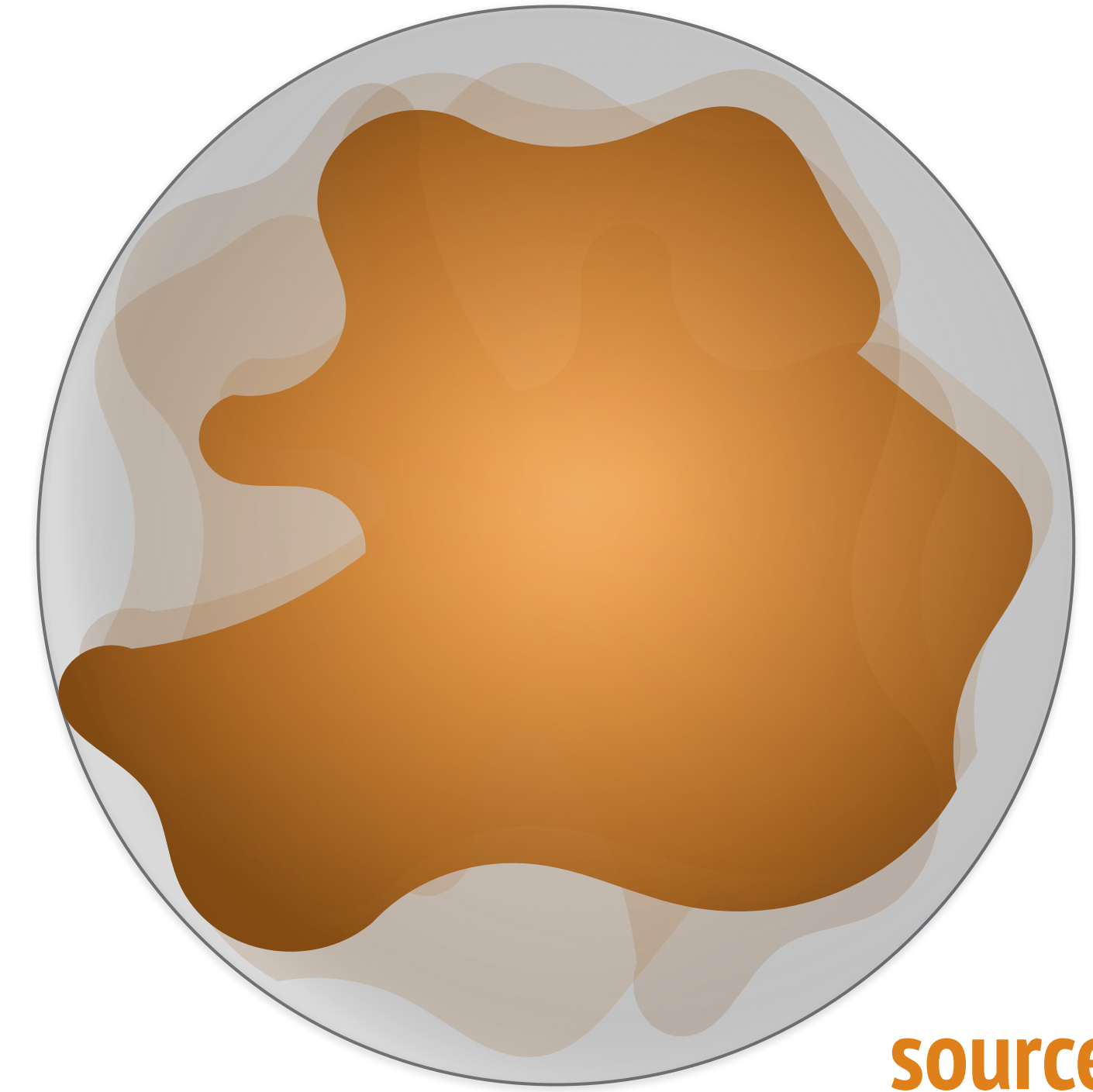
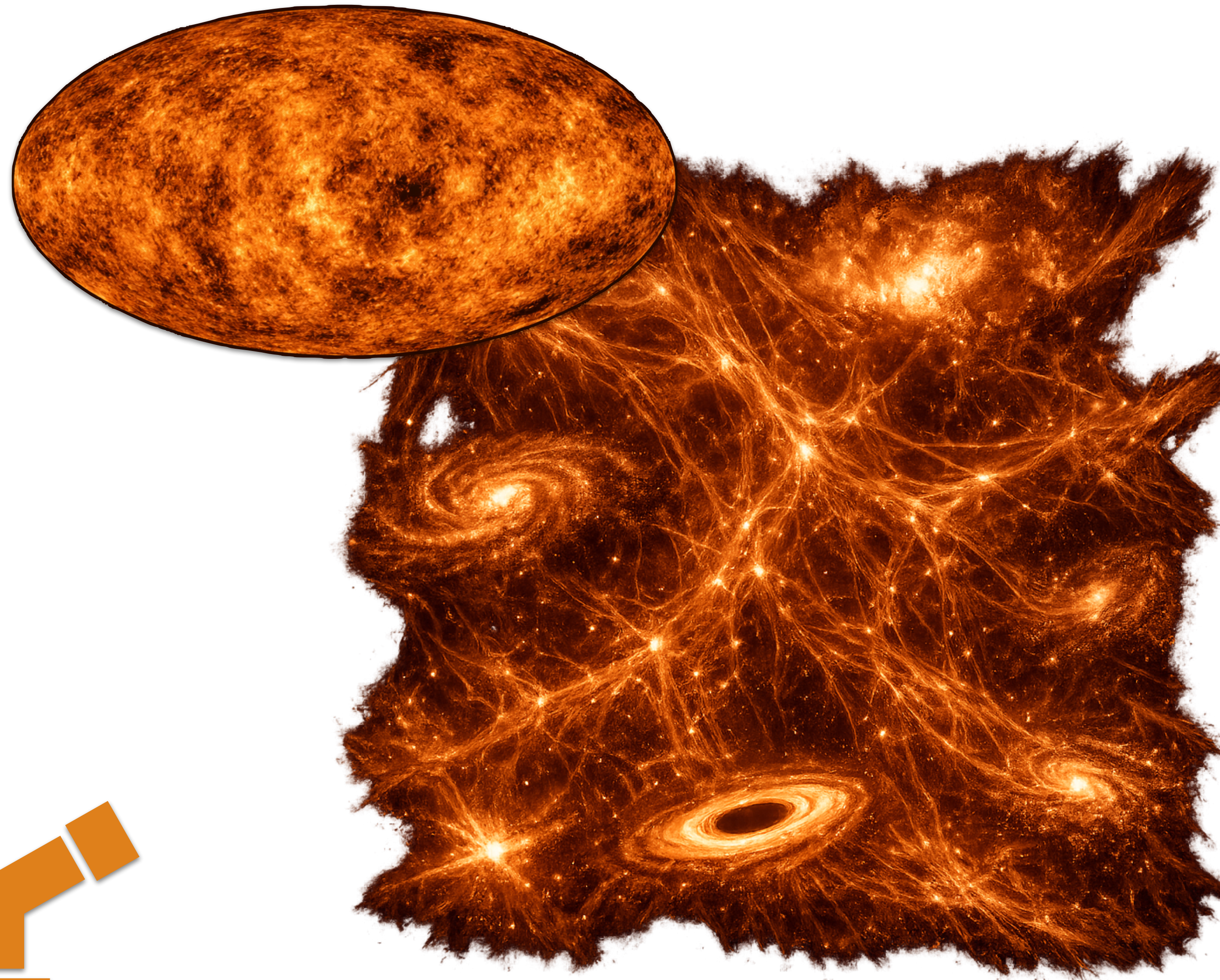




source



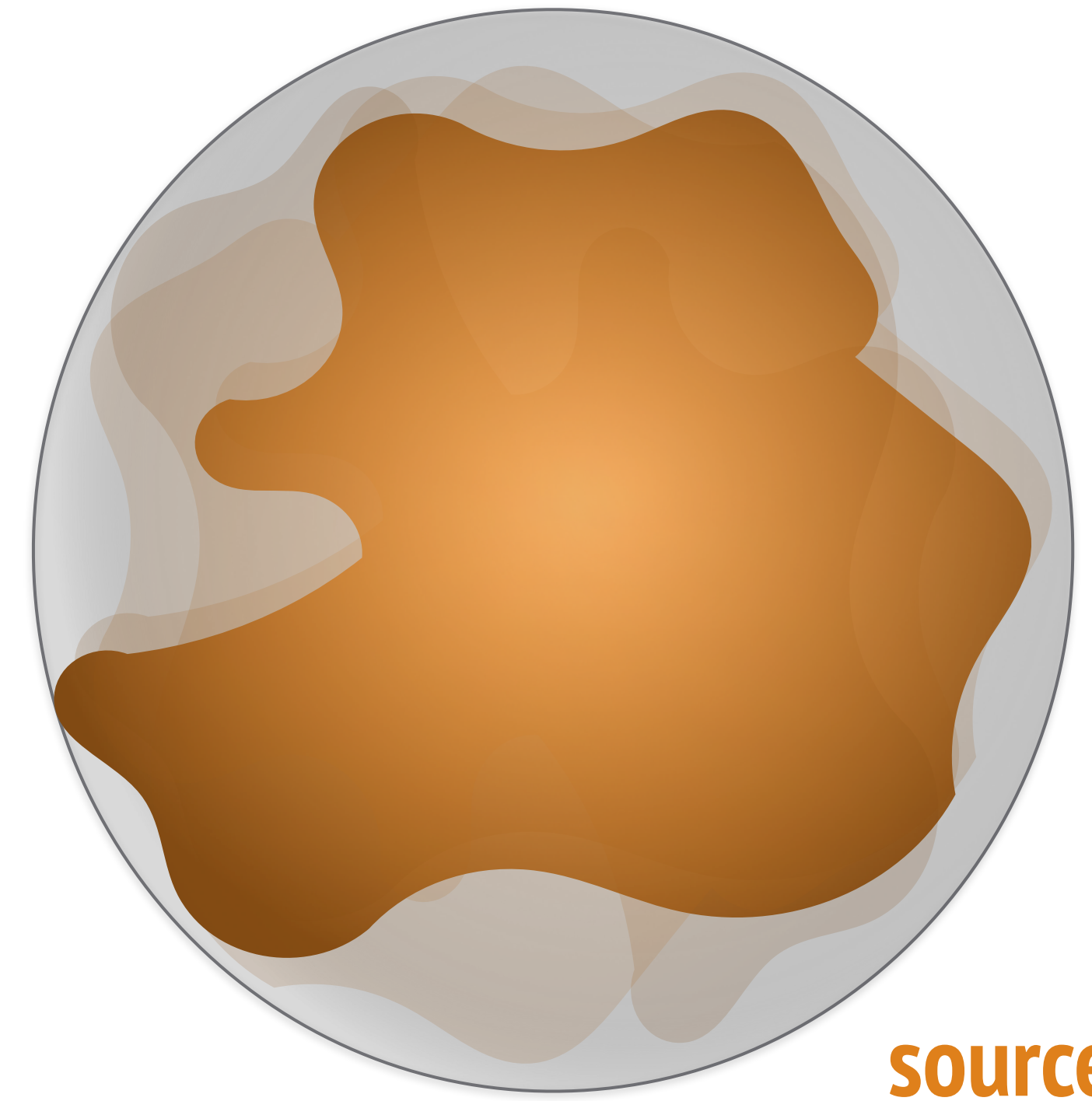
observations



source

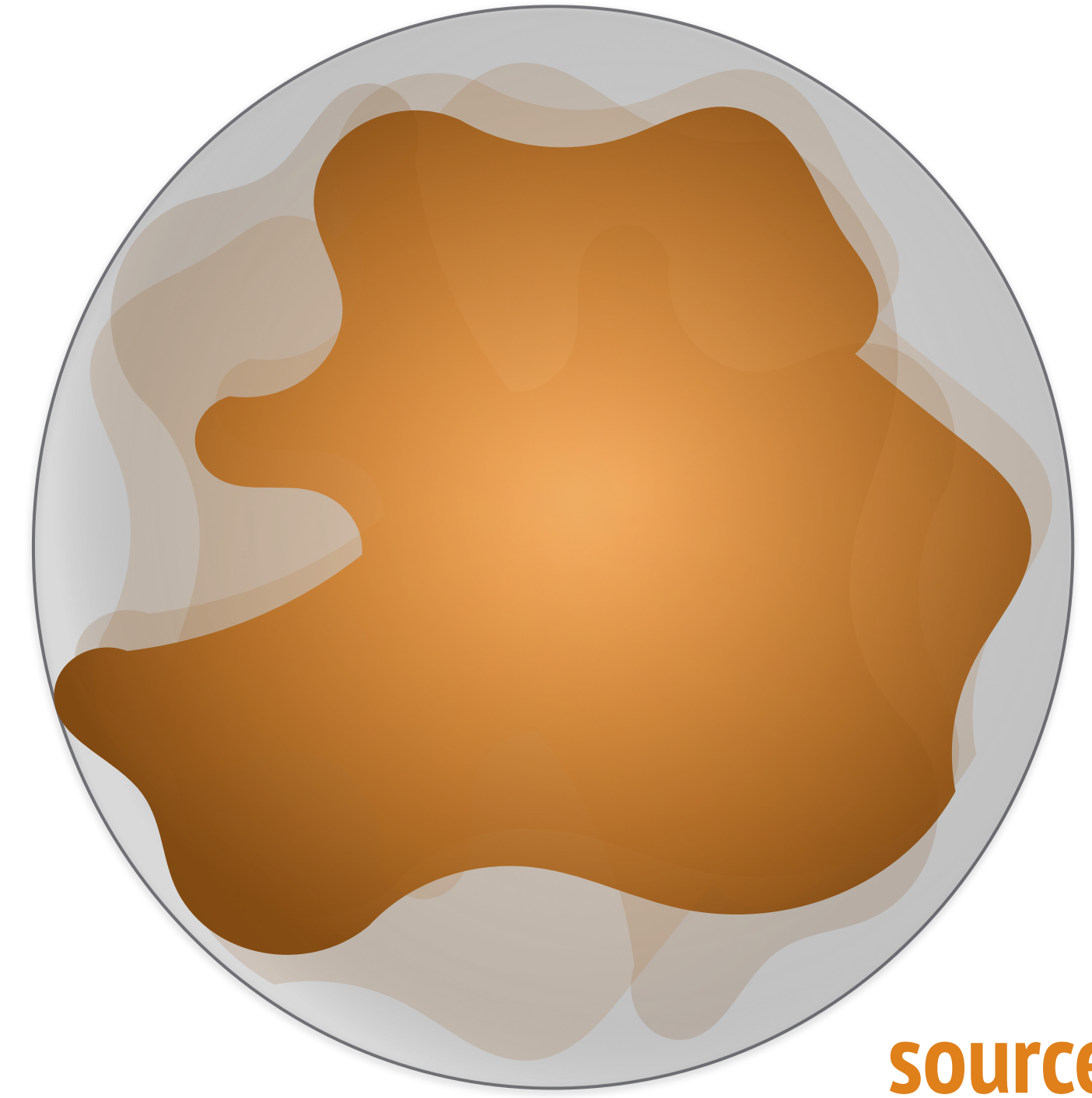
in-between





source



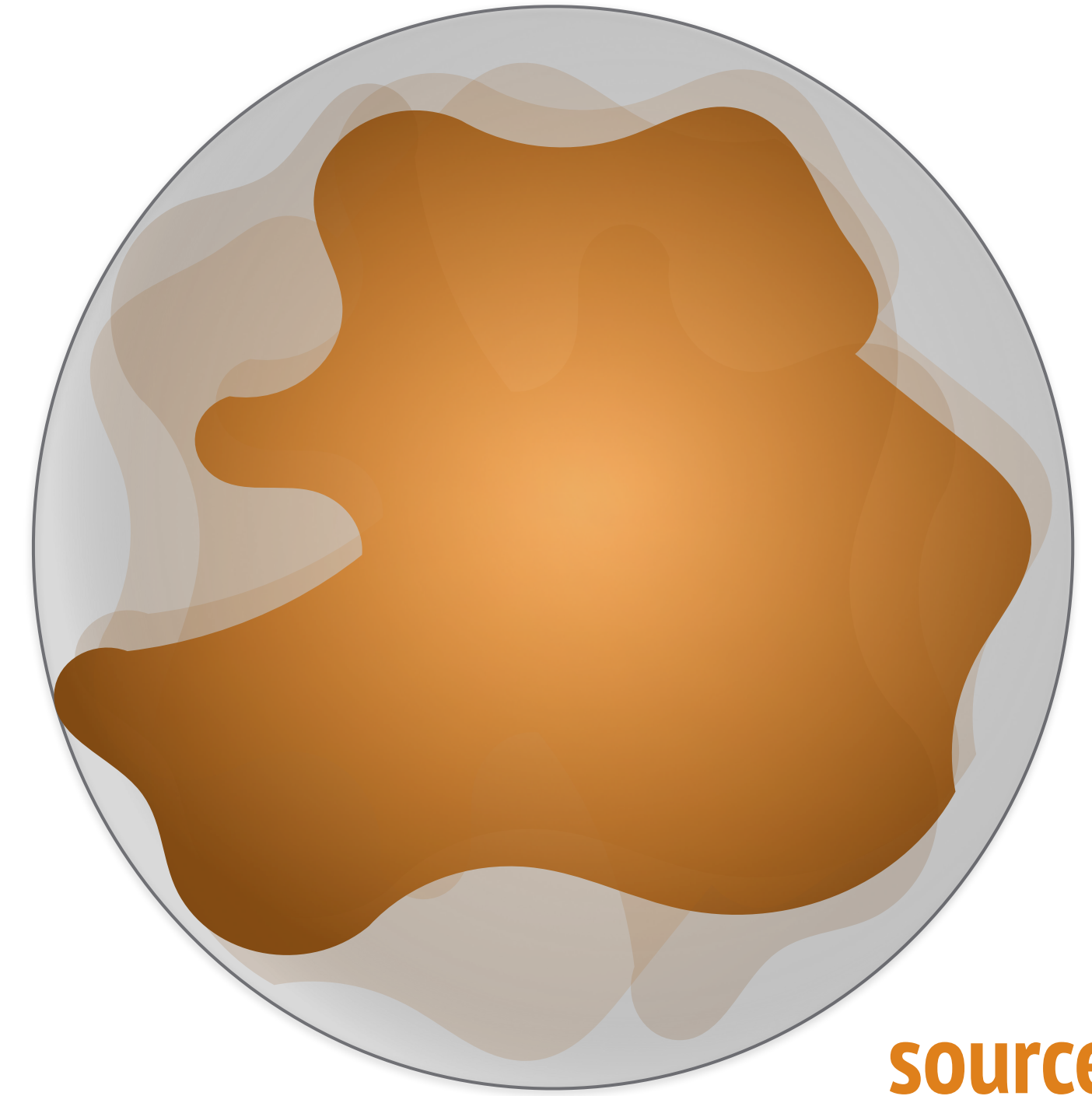


$$\frac{\text{number of particles}}{(\text{intervals of}) \text{ solid angle} \times \text{energy} \times \text{time}}$$



## type of particle

composition, flavour



source

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(intervals of)  **$\frac{\text{number of particles}}{\text{solid angle} \times \text{energy} \times \text{time}}$**

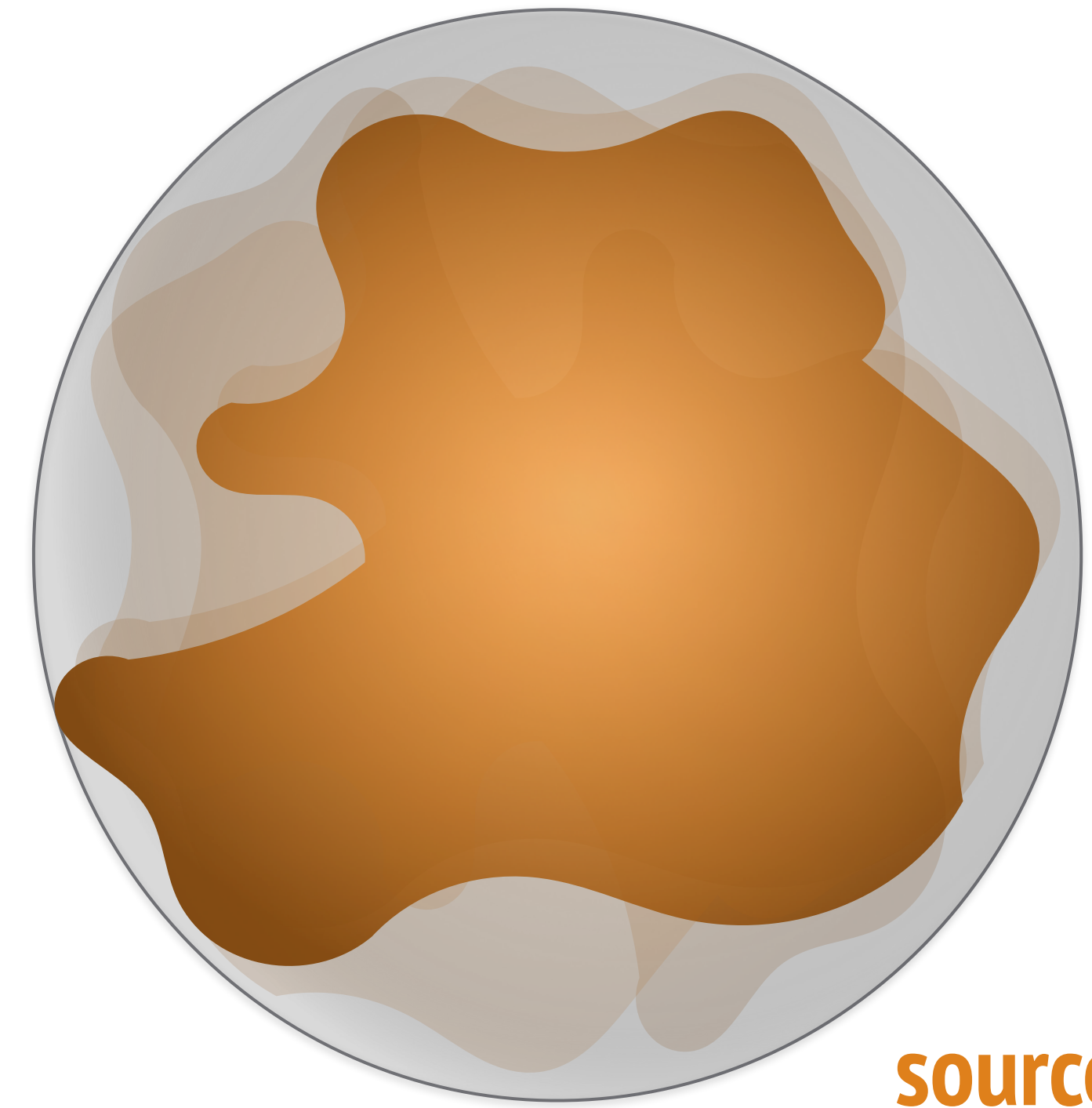


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## position of emission site

position of each source and within the source



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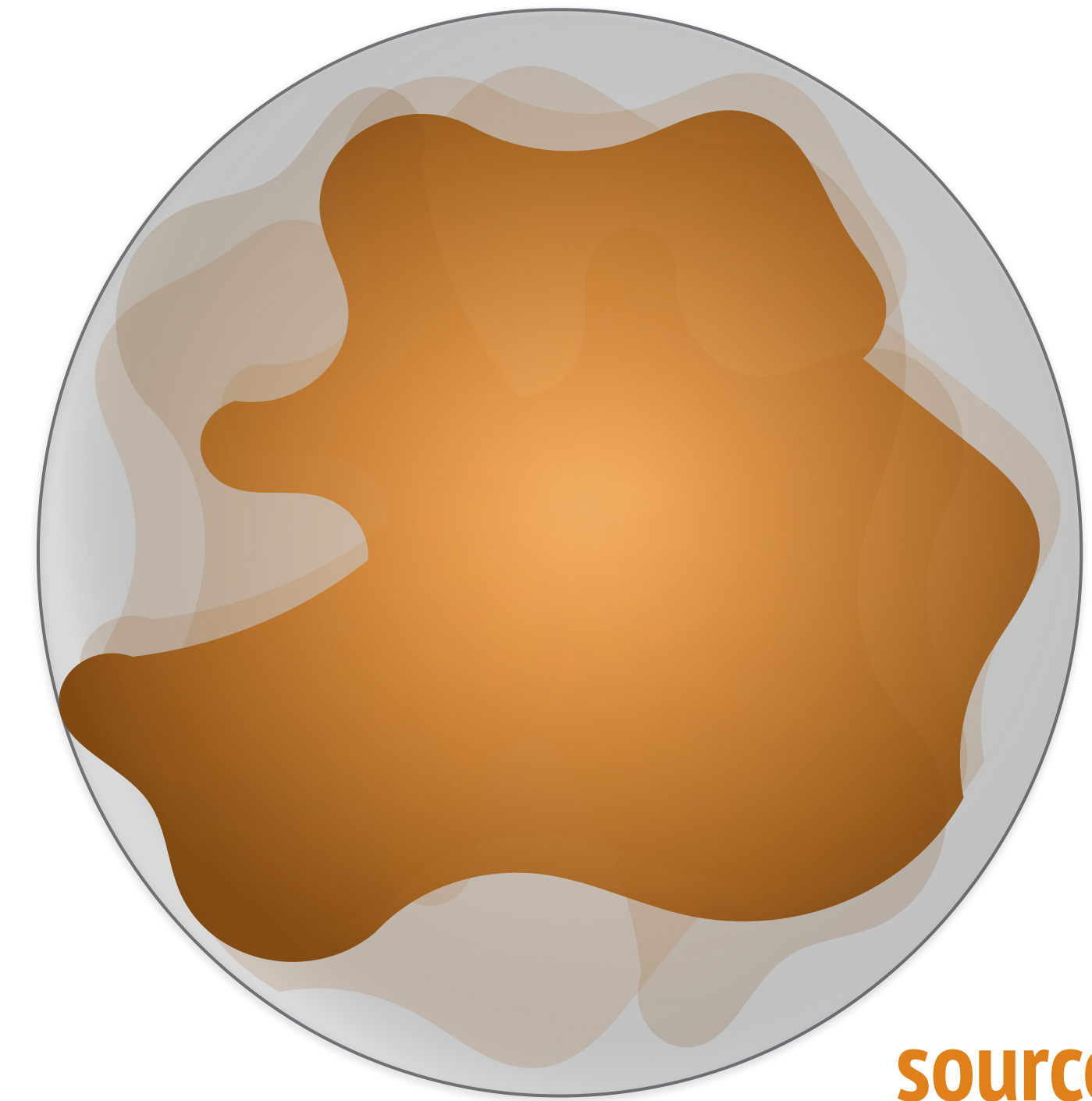
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light curves



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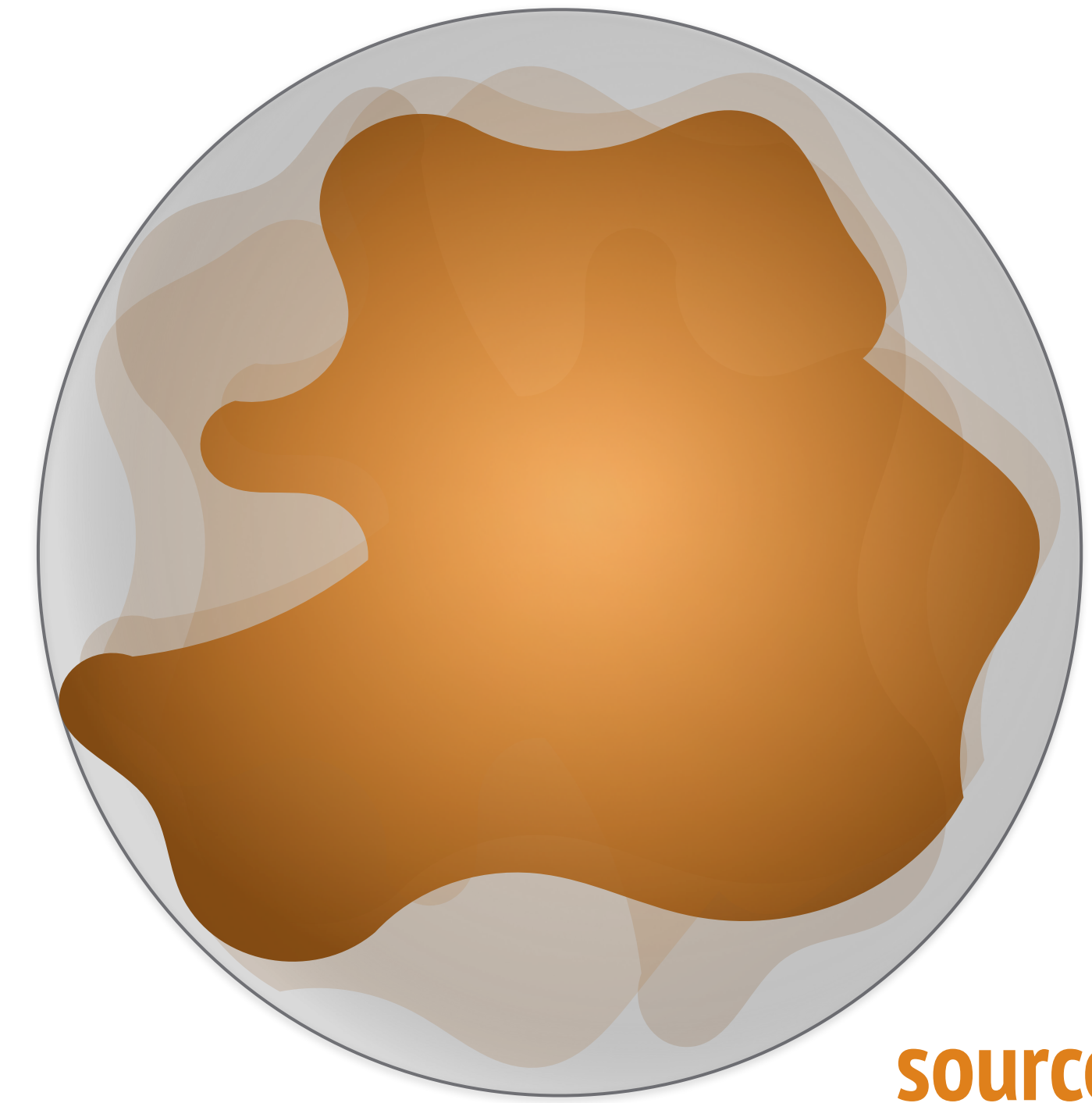
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## temporal emission profiles

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## intrinsic spectra

number of events in each energy bin



source

**number of particles**

(intervals of) **solid angle × energy × time**



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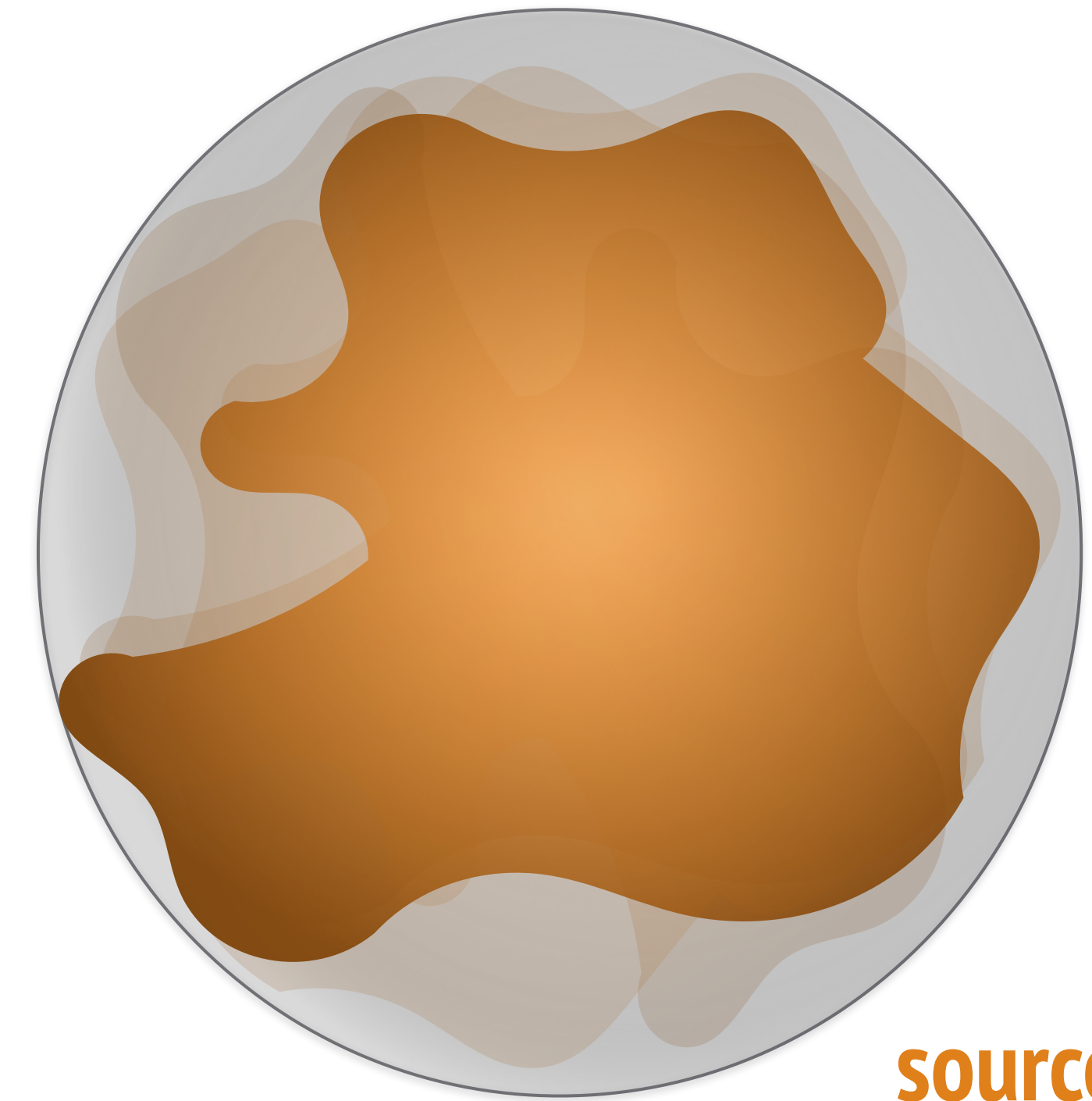
light curves

## intrinsic spectra

number of events in each energy bin

## geometry of emission

isotropic, jet

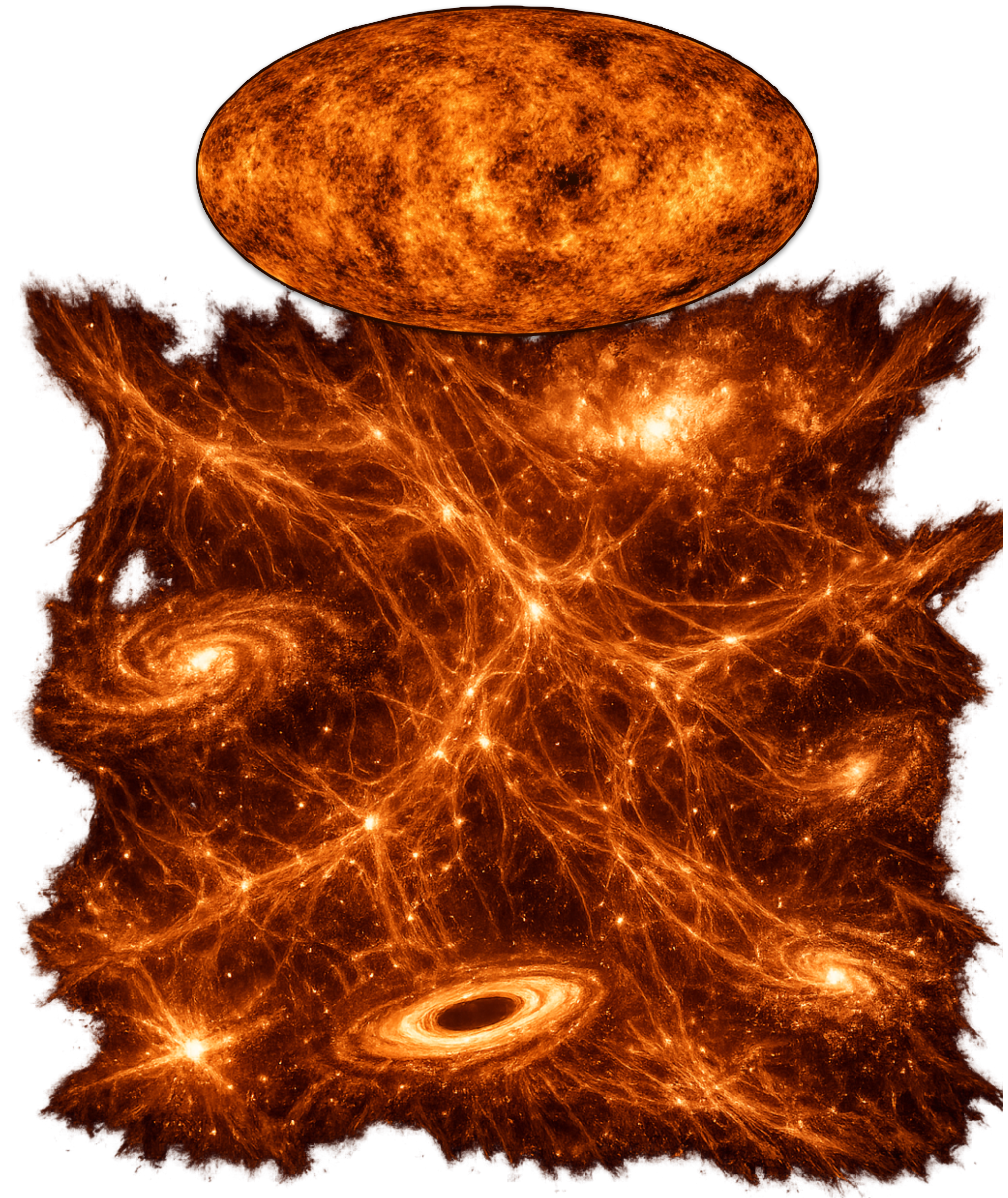


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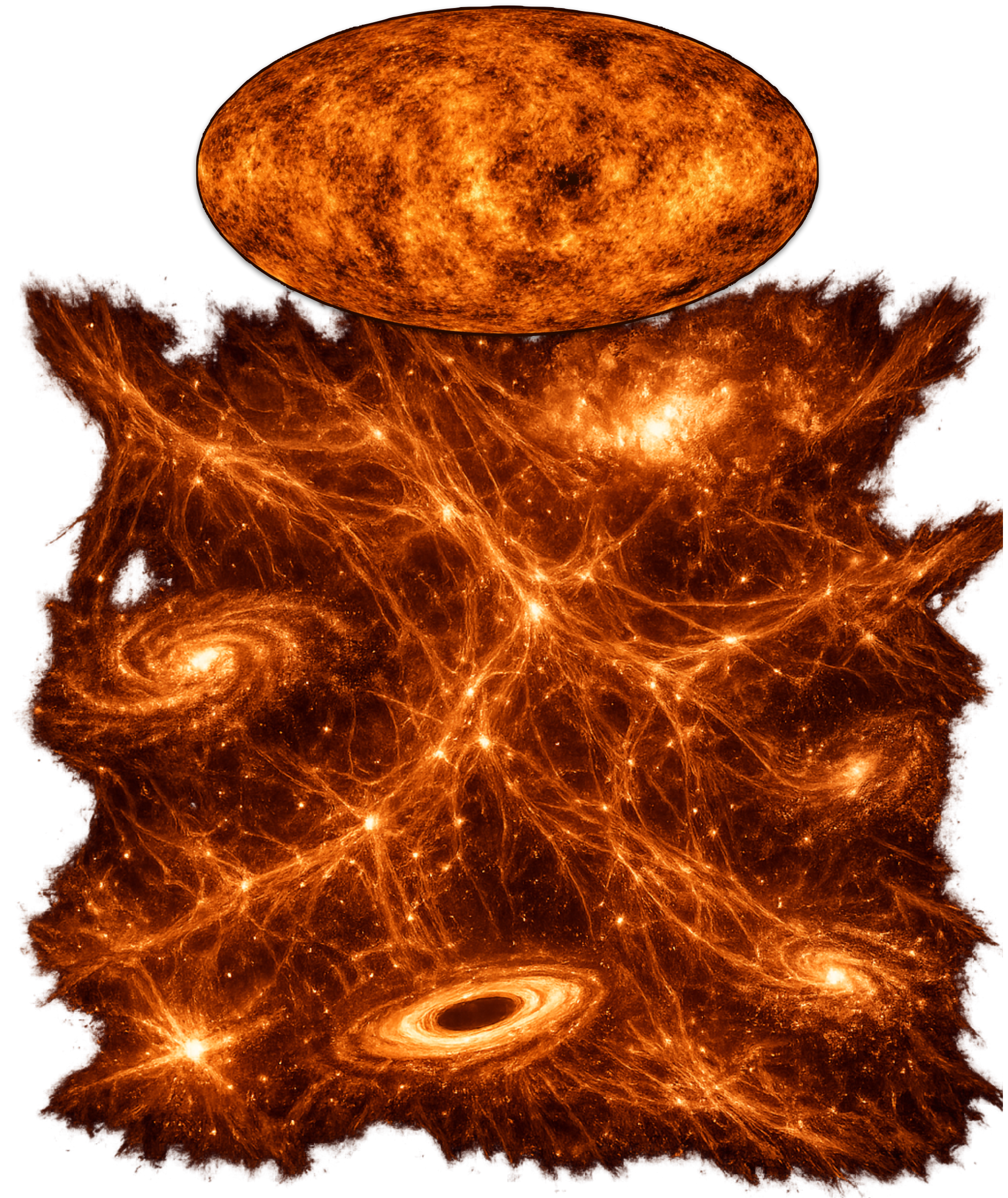




in-between

## target distributions

photons (e.g., CMB, EBL)



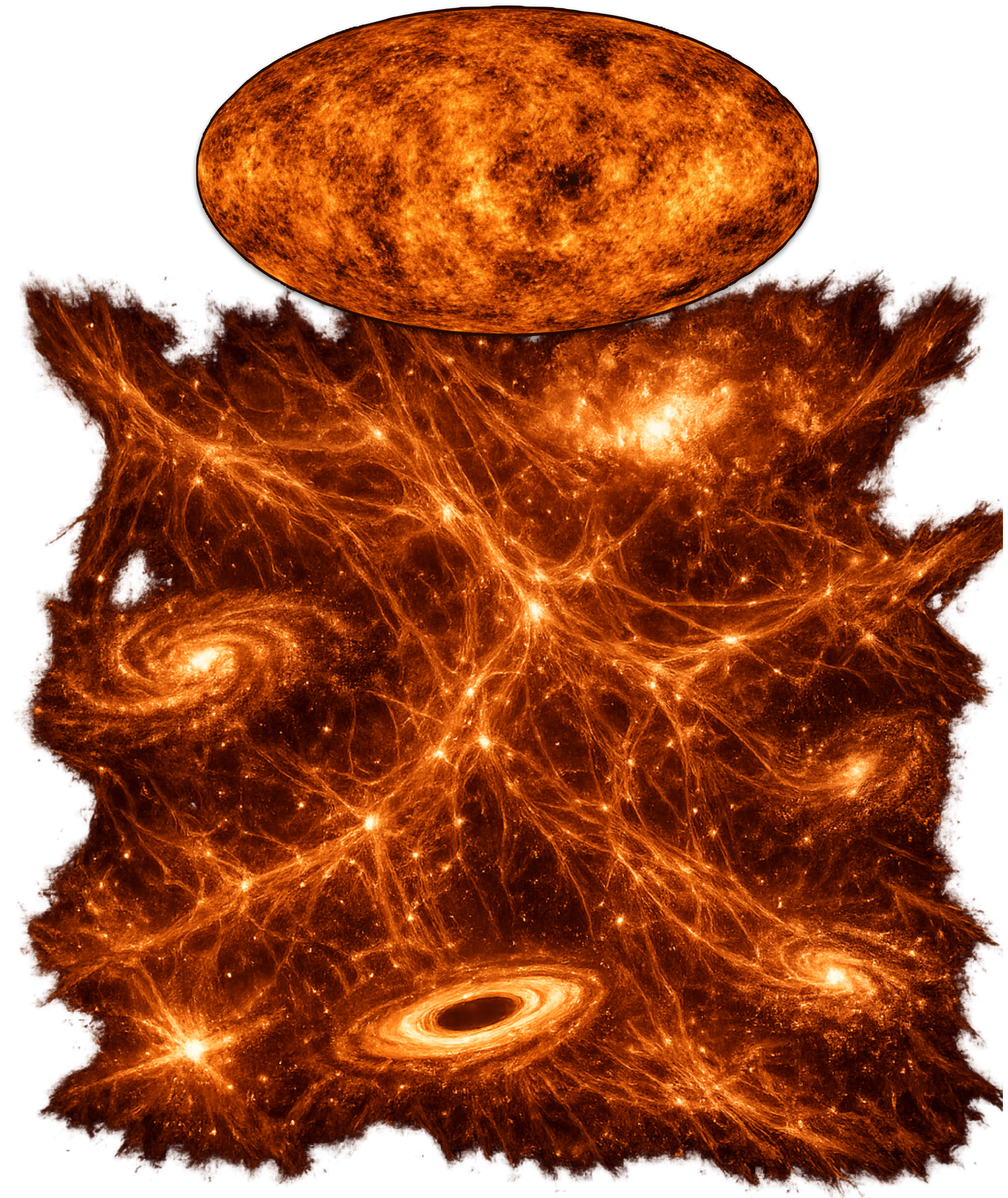
in-between

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galactic, extragalactic



in-between

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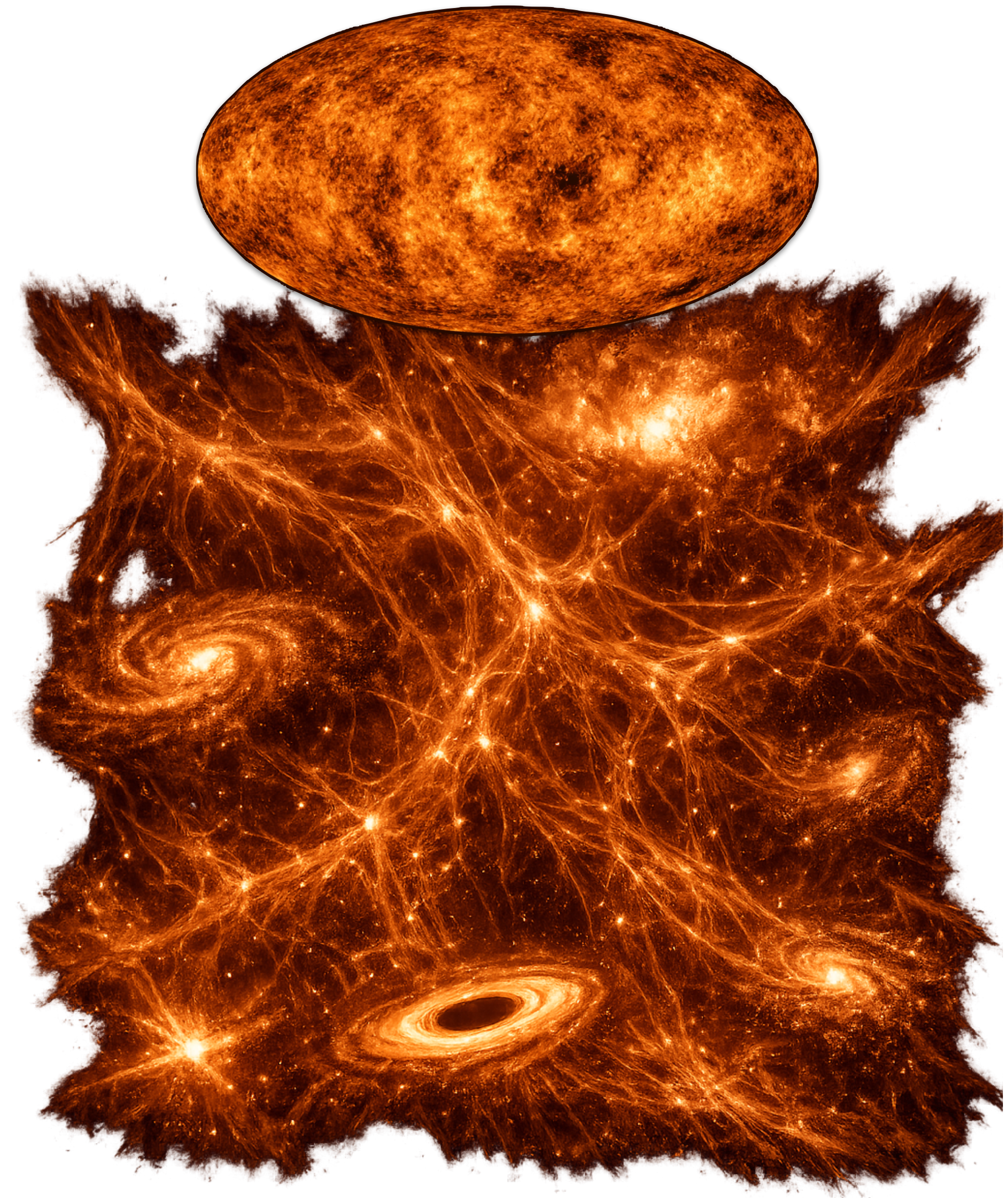
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in-between

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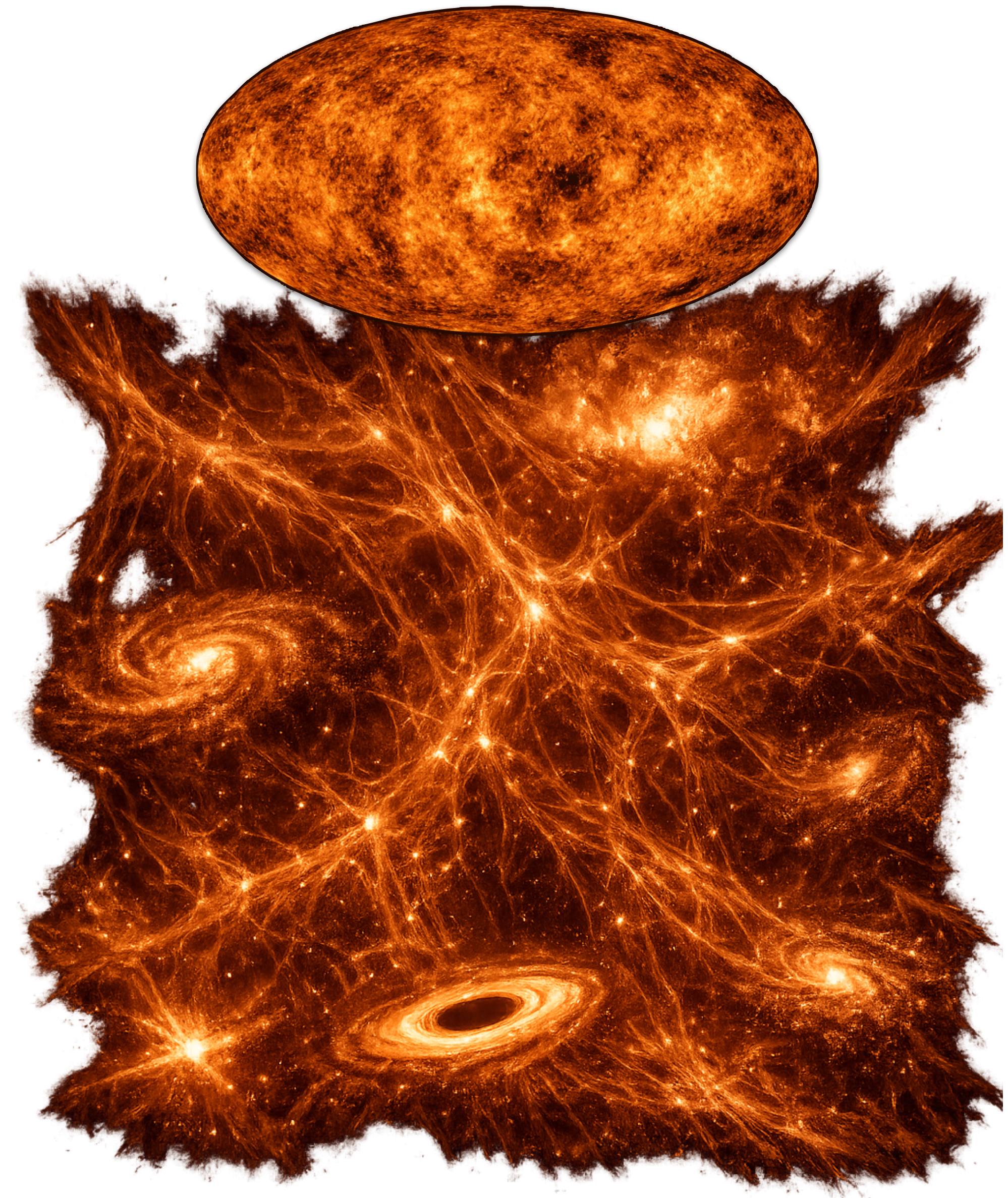
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## gravitational fields

lenses

## physics of interactions

cross sections, ....



in-between

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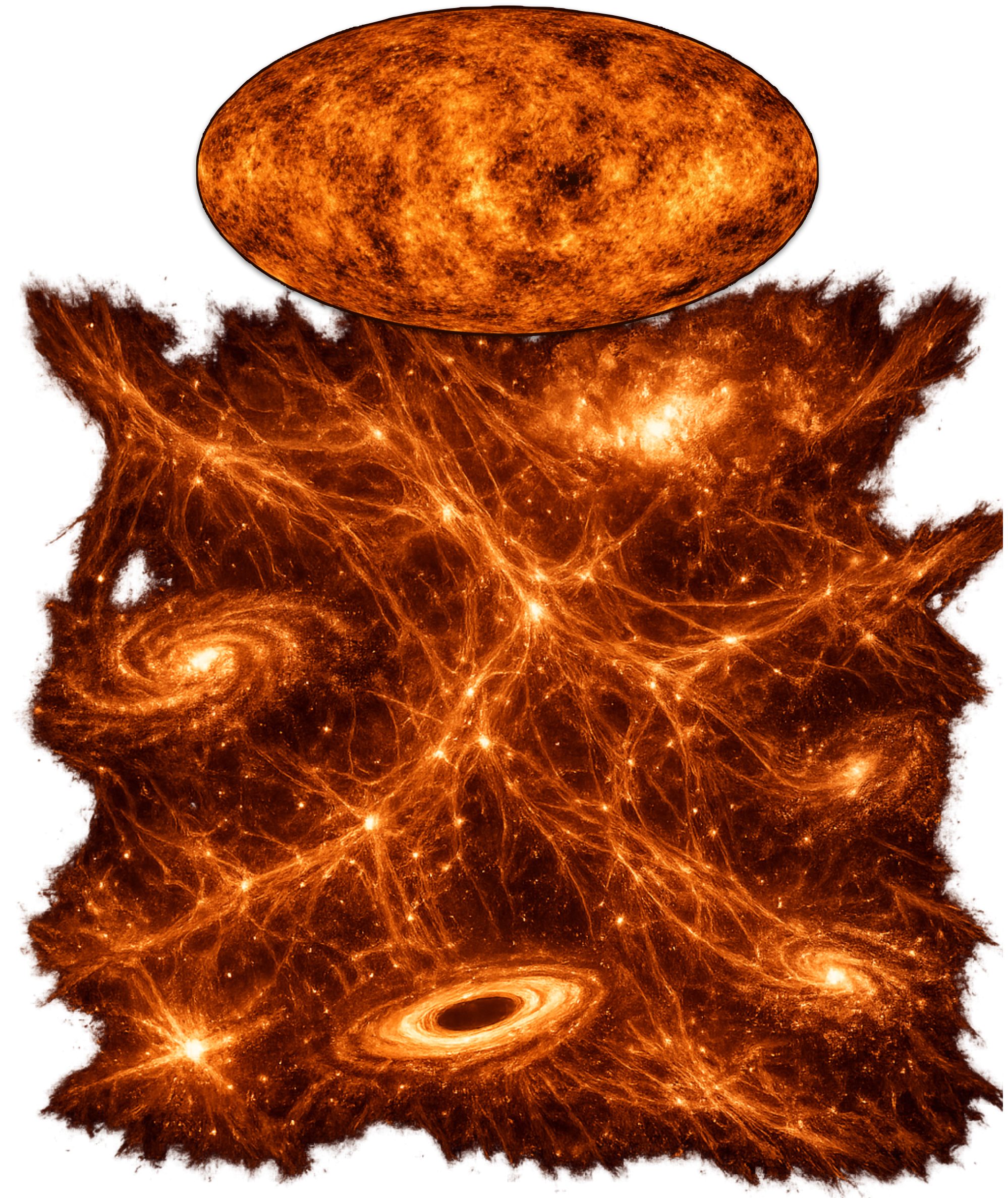
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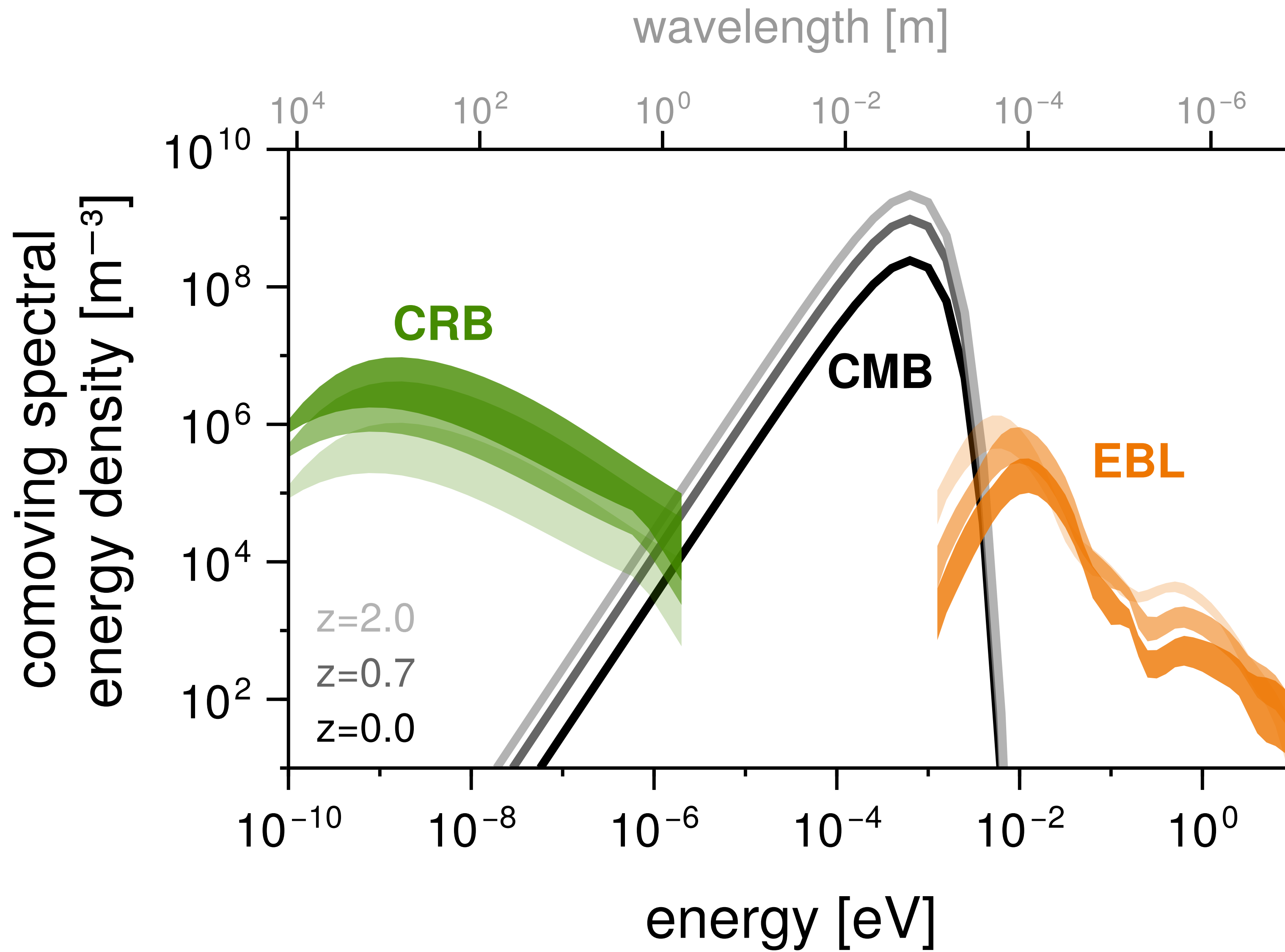
## mesoscale physics

collective phenomena



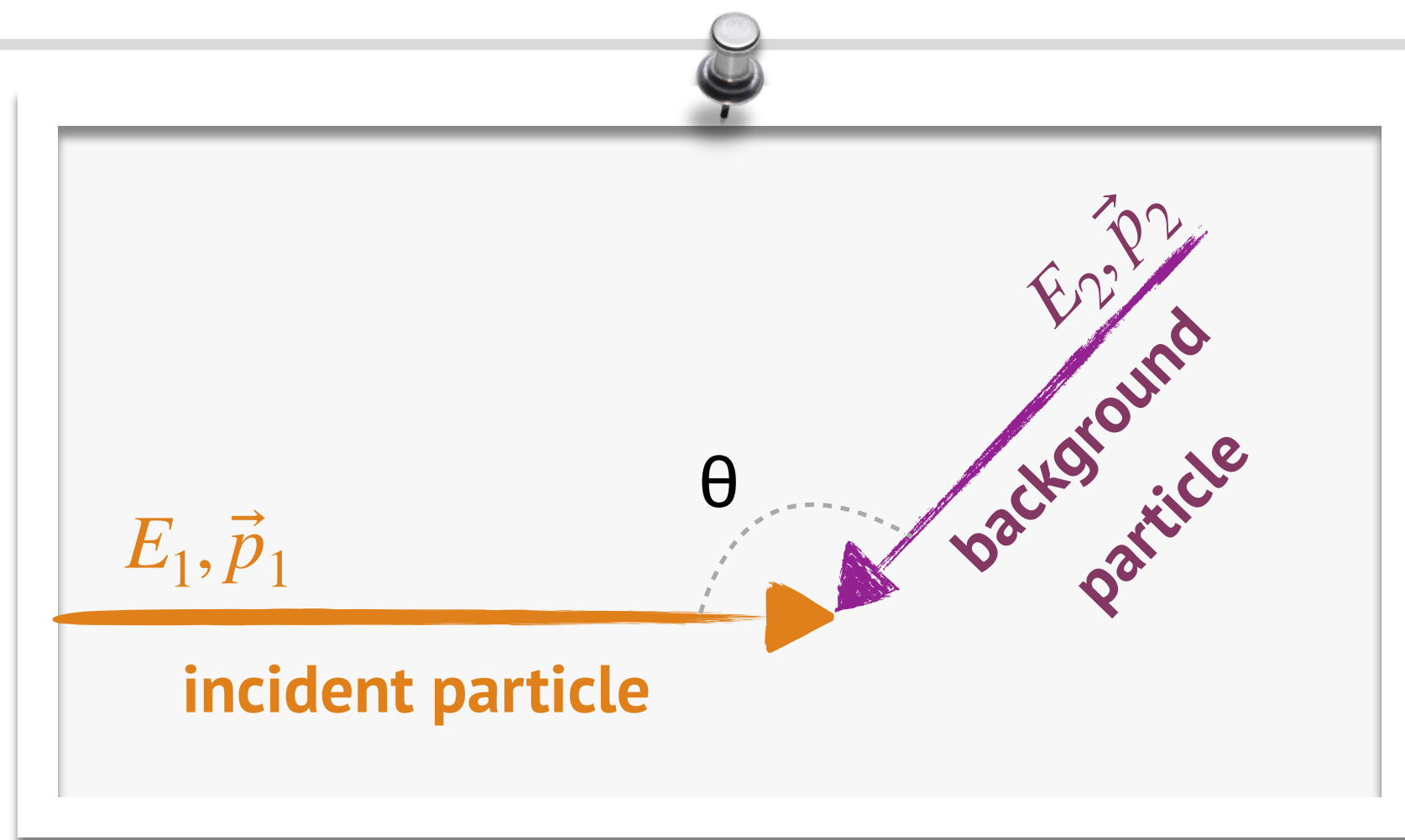
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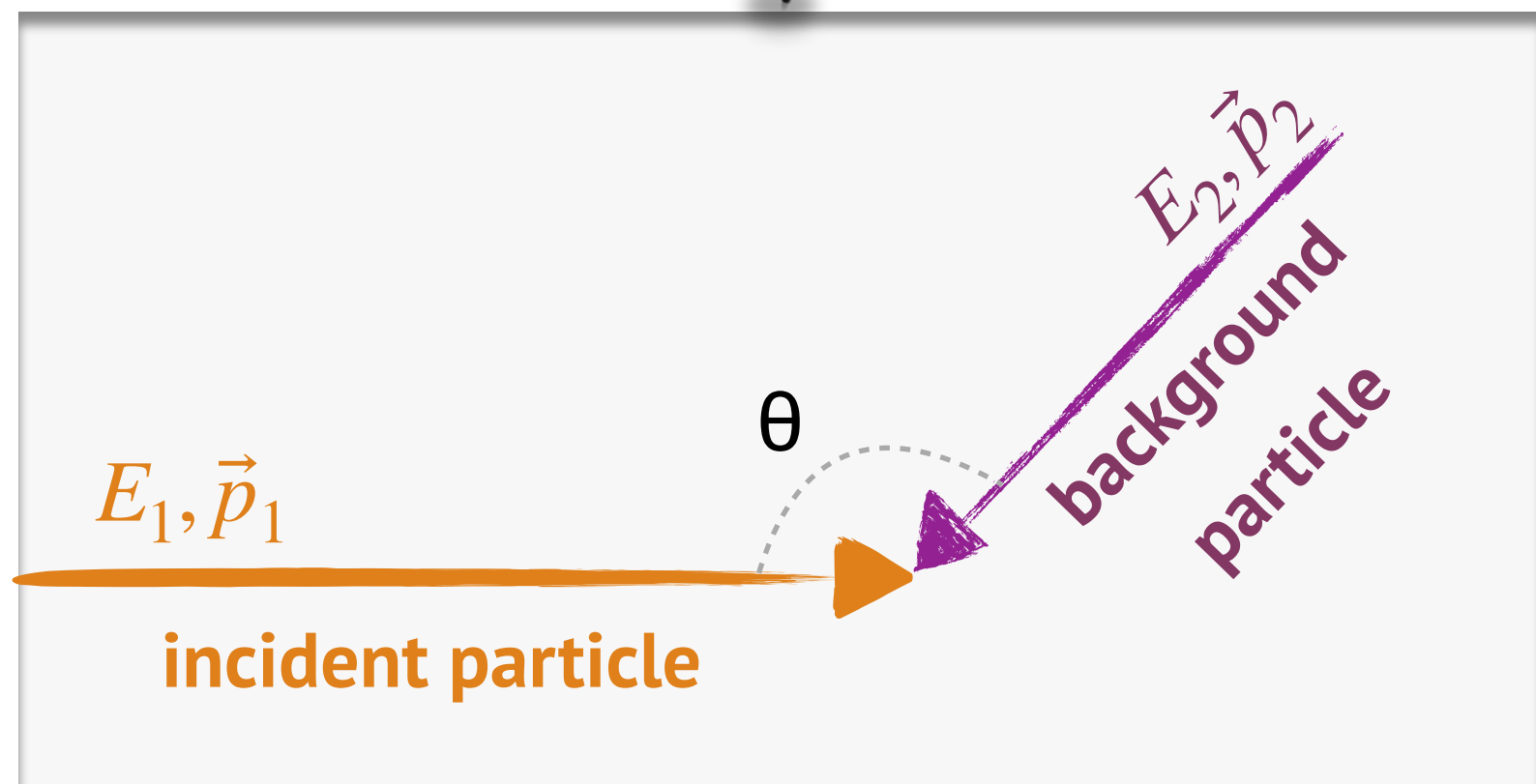
# cosmological photon backgrounds





# interactions and mean free path

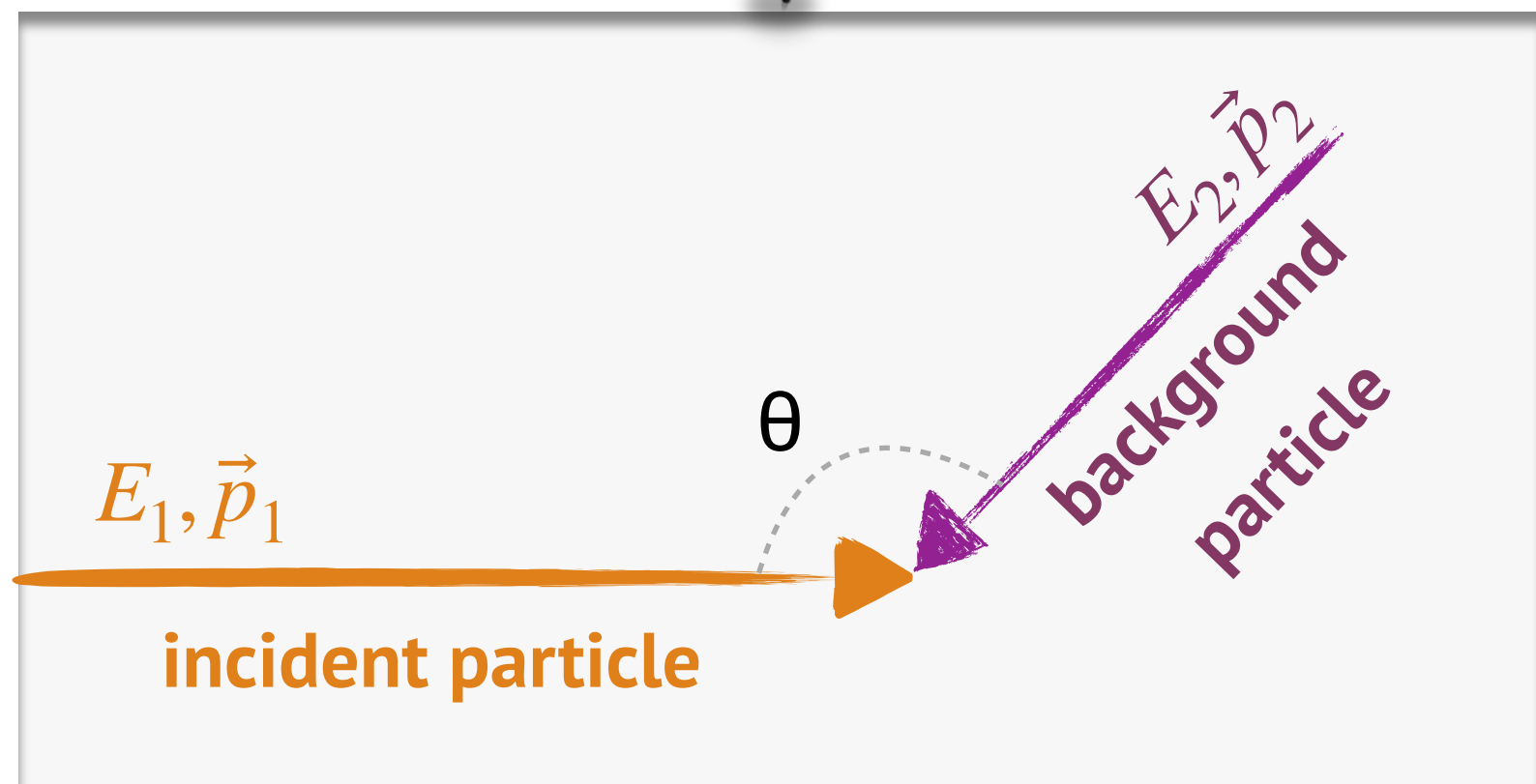




**centre of mass  
energy**

$$s = m_1^2 c^4 + m_2^2 c^4 + 2E_1 E_2 (1 - \beta_1 \beta_2 \cos \theta)$$

# interactions and mean free path



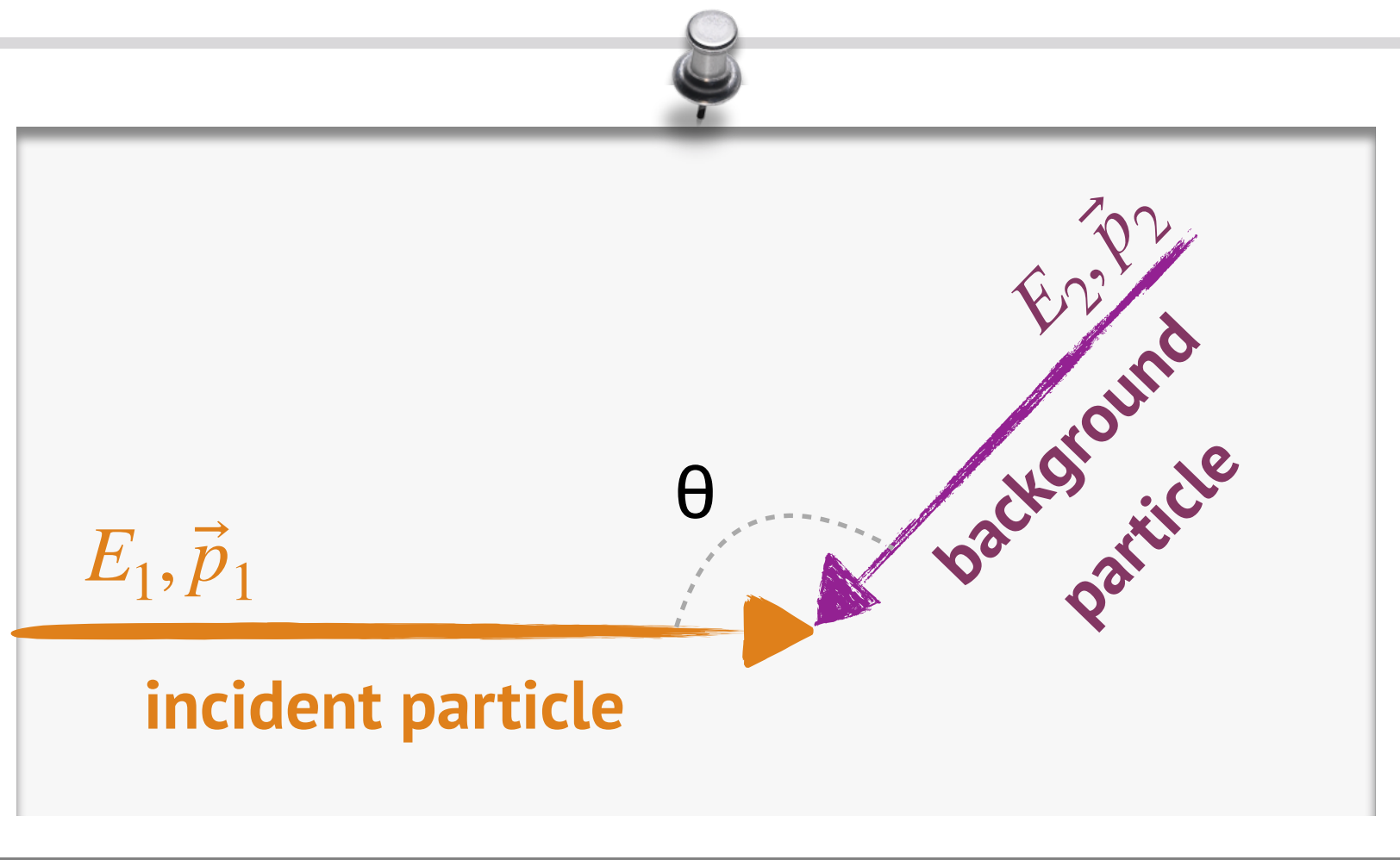
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$$\beta_{\text{rel}} = \sqrt{\frac{(P_1 \cdot P_2)^2 - (m_1 m_2 c^2)^2}{(P_1 \cdot P_2)^2}}$$

# interactions and mean free path



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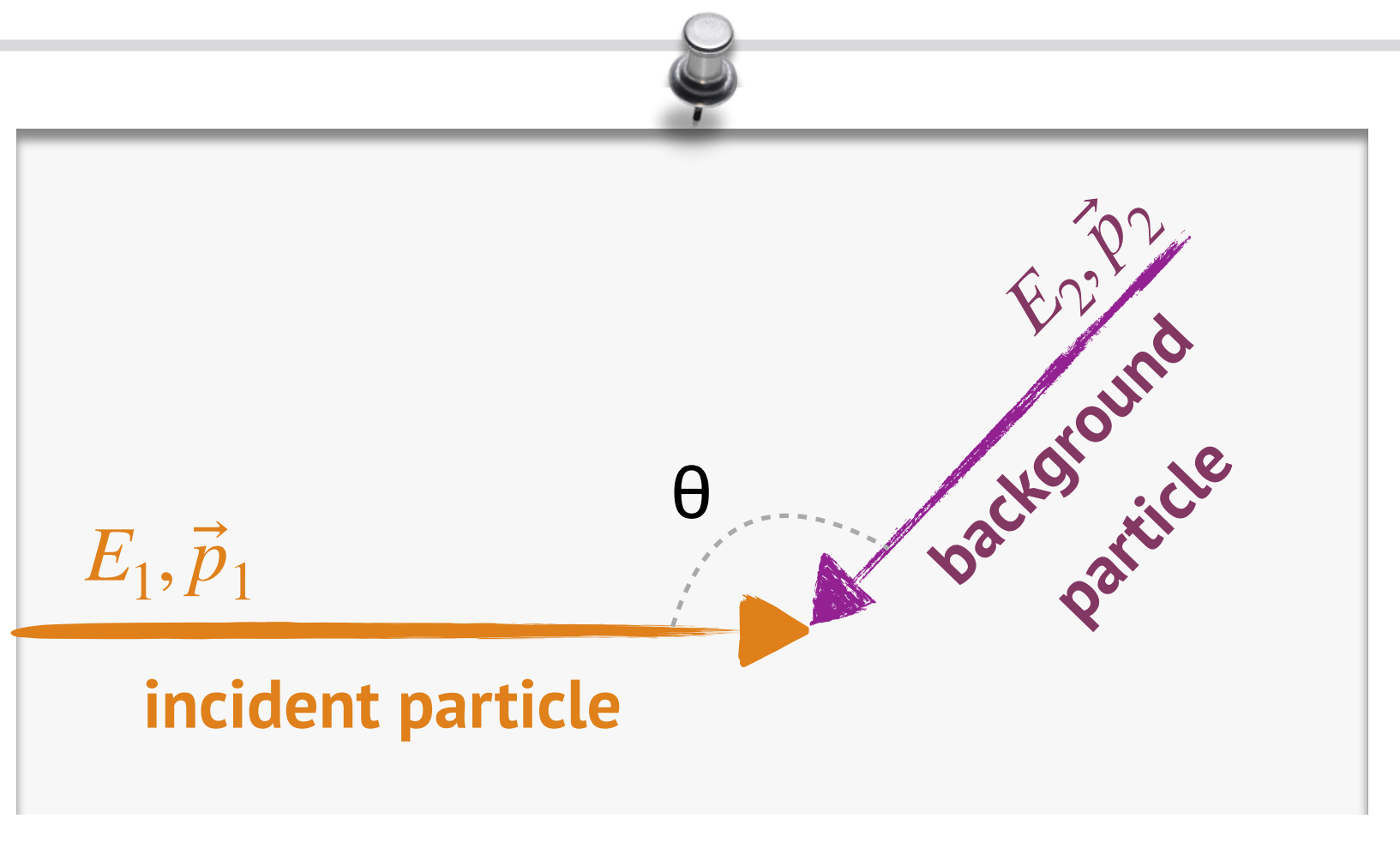
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**interaction  
length**

for particle of type 1  
interacting with (isotropic)  
background of type 2



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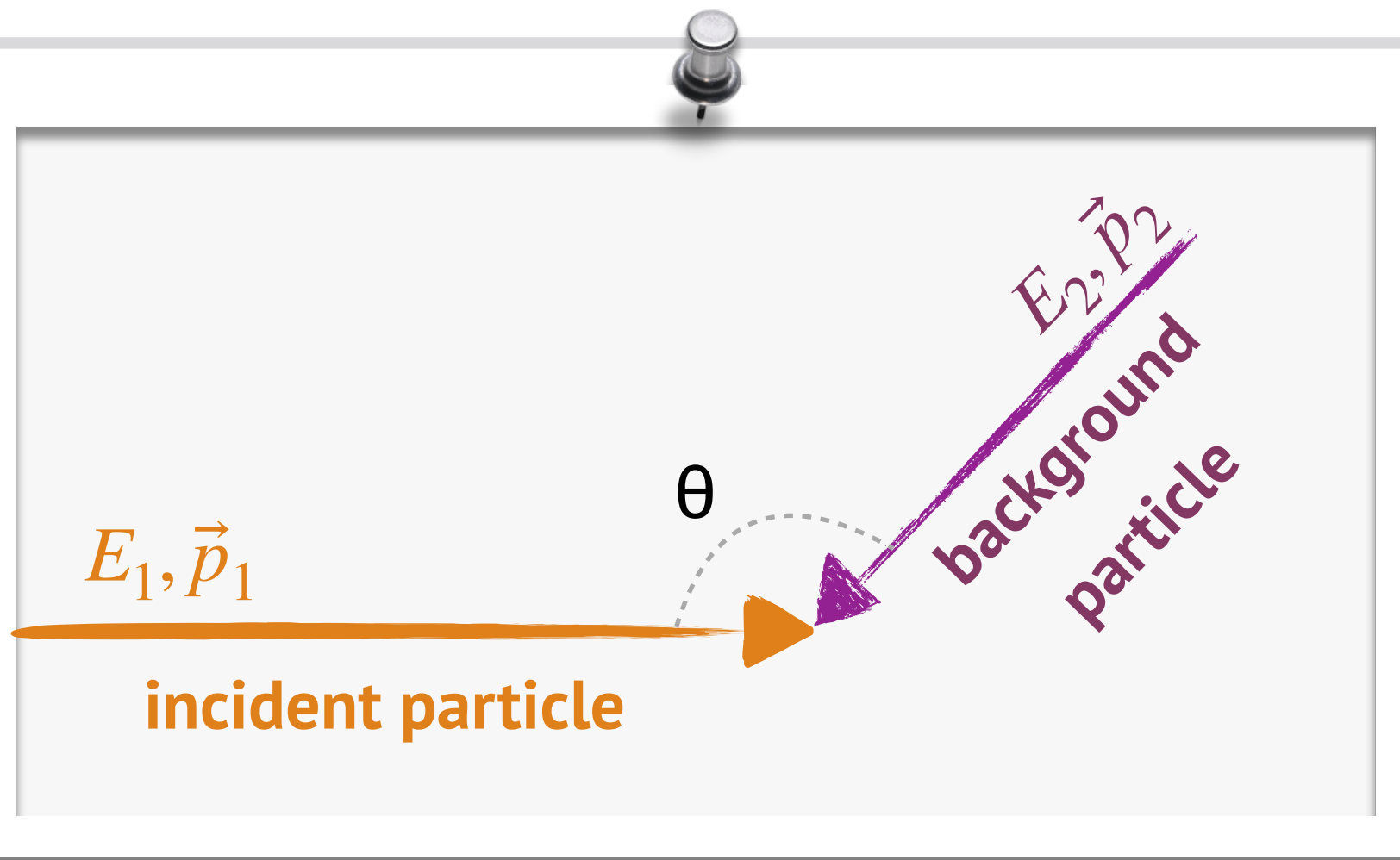
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**generic**  $\lambda^{-1} = \frac{1}{2} \iint dp_2 \, d \cos \theta \, \sigma(s) \, \beta_{\text{rel}}(P_1, P_2) \, (1 - \beta_1 \beta_2 \cos \theta) \, \frac{dn_2(\vec{p}_2)}{dp_2}$

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# interactions and mean free path



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**photons**  $\lambda^{-1}(E, z) = \frac{1}{8\beta E^2} \int_{\epsilon_{\min}(E)}^{+\infty} \frac{1}{\epsilon^2} \frac{dn(\epsilon, z)}{d\epsilon} \int_{s_{\min}}^{s_{\max}(E, \epsilon)} (s - m^2 c^4) \sigma(s) \, ds d\epsilon$

# modified interactions with photon backgrounds

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change:

$$\varepsilon_{\min}, s, s_{\min}, s_{\max}, \beta_{\text{rel}}$$

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  - ✦ *but*: unobserved gamma rays at higher energies

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**necessary conditions** to state the a flux of a messenger is primary

- ▶ know the **intrinsic spectrum** well to exclude **cascade contribution**
  - ✦ *but*: unobserved gamma rays at higher energies
- ▶ know the **flux of other particles** along the **line of sight**
  - ✦ degeneracy between absorption of parent and observations of the messenger

# cosmic rays

## LIV-induced modifications

$$E^2 = m_a^2 c^4 + p^2 c^2 + f_a(E, \vec{p})$$

$$f_a(E, \vec{p}) \approx f_a(p) = p^2 c^2 \sum_{n=0}^{\infty} \chi_n^{(a)} \left( \frac{pc}{E_\star} \right)^n$$

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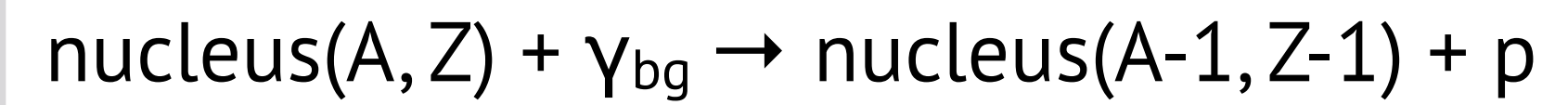
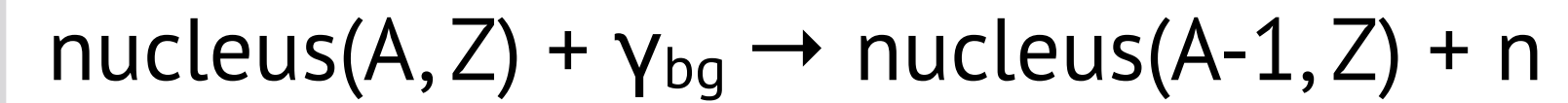
## photodisintegration

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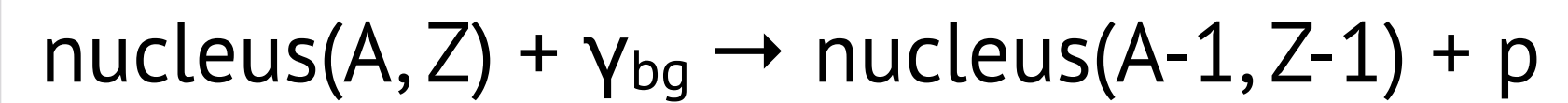
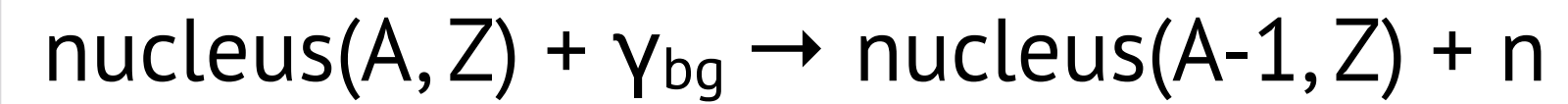
....

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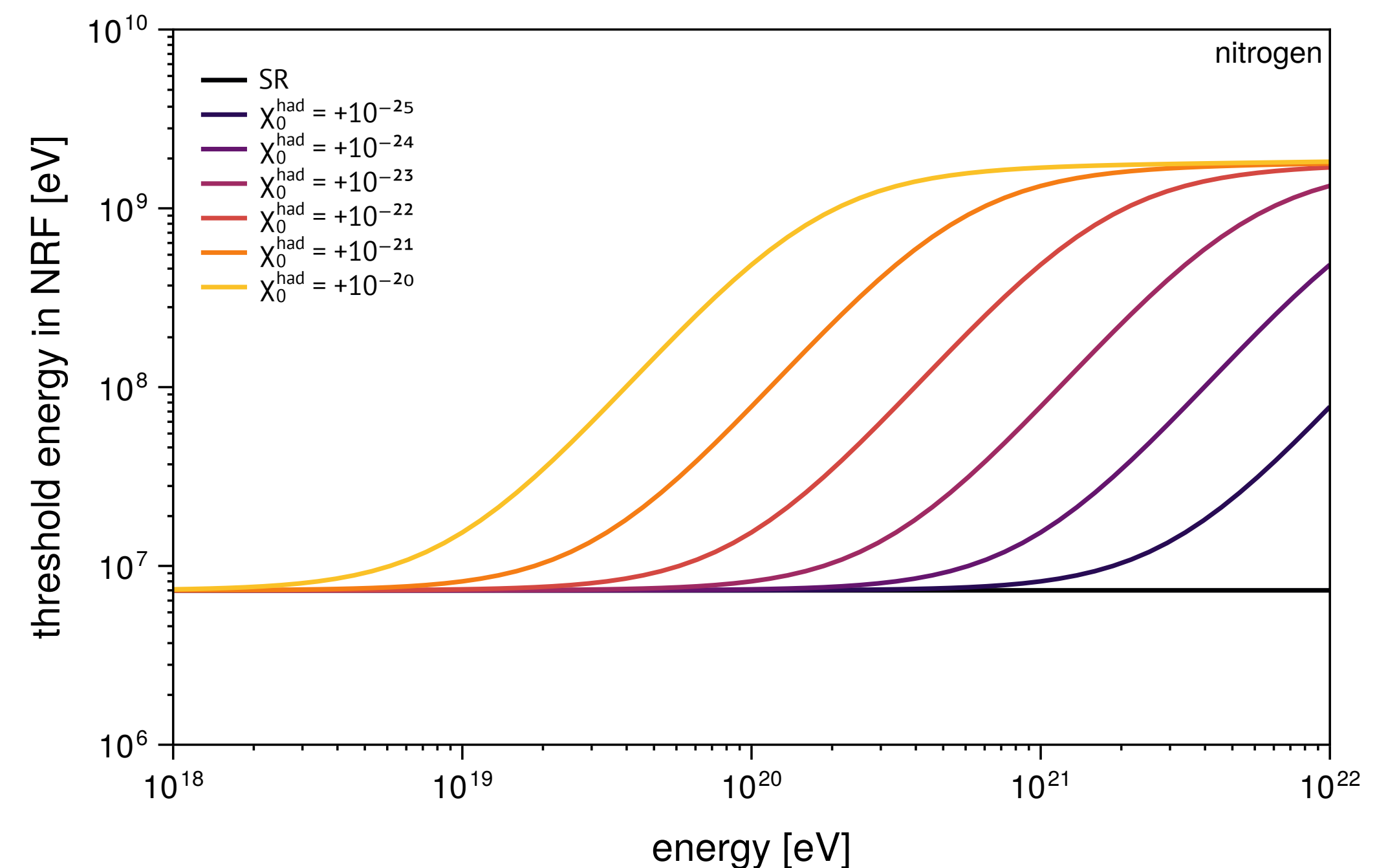
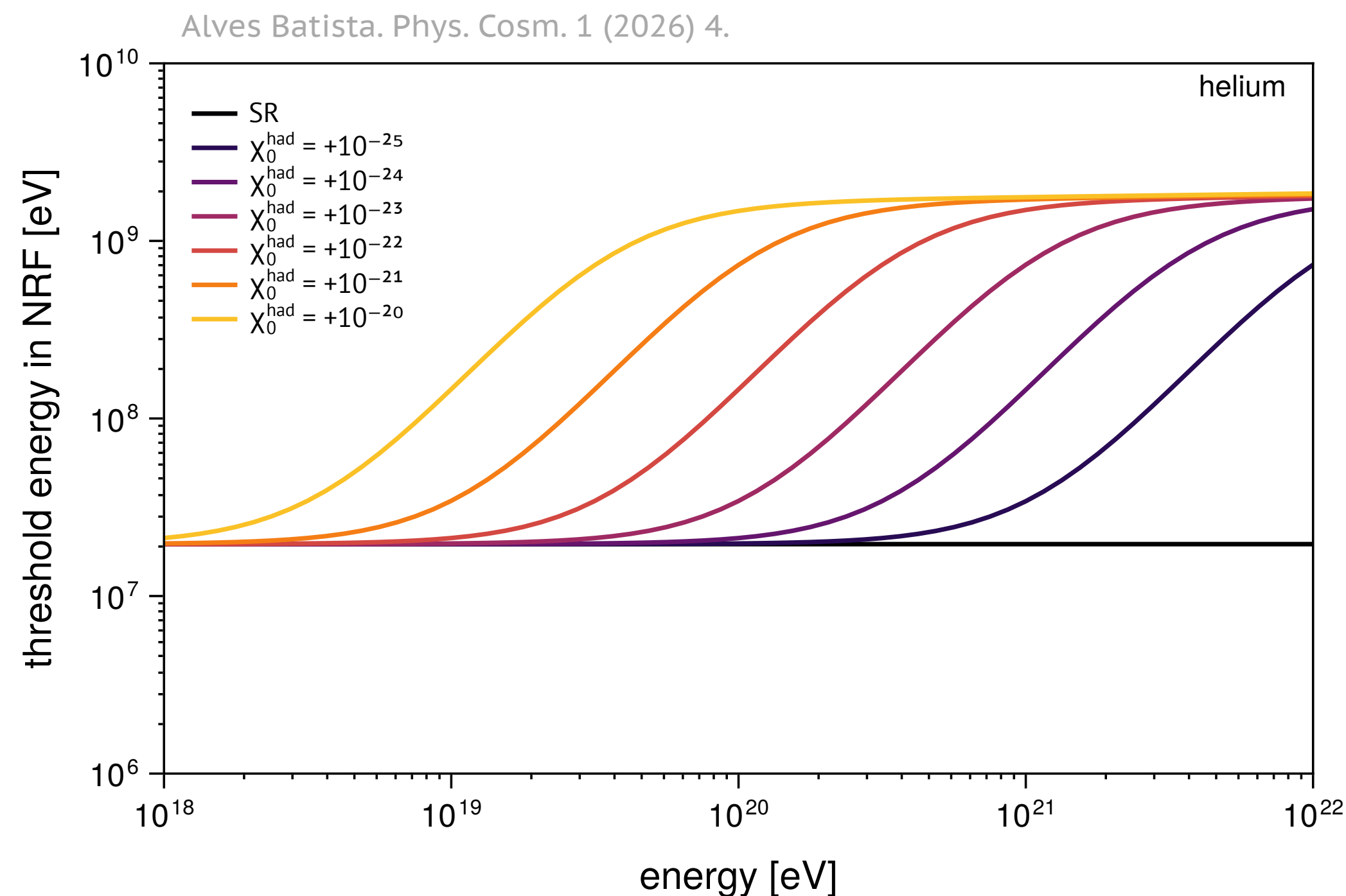
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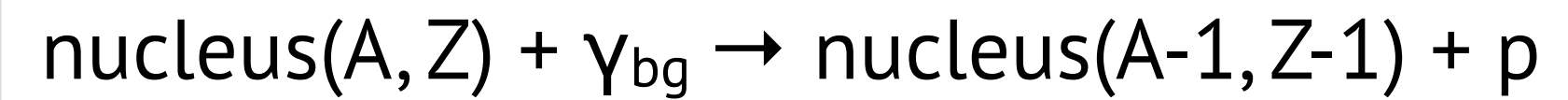
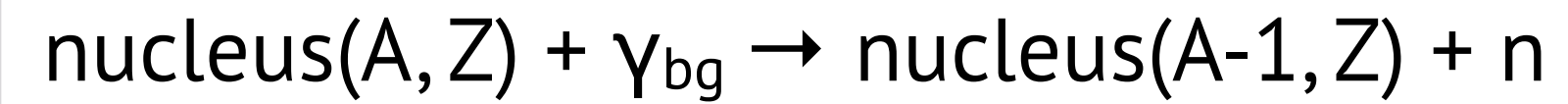
# modified interaction thresholds

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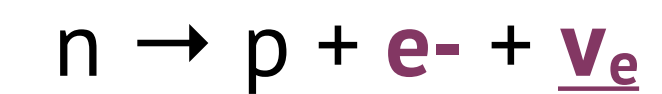
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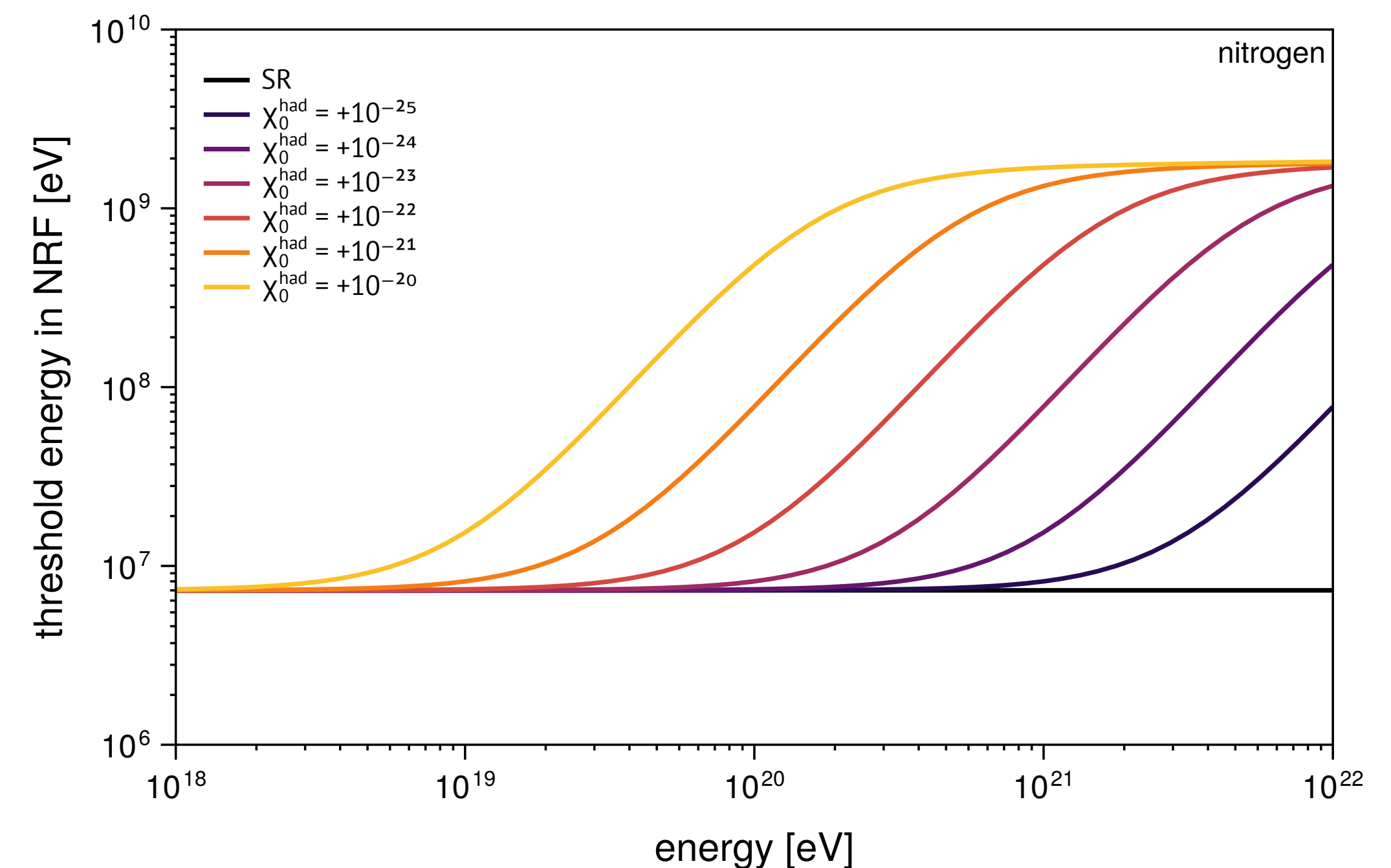
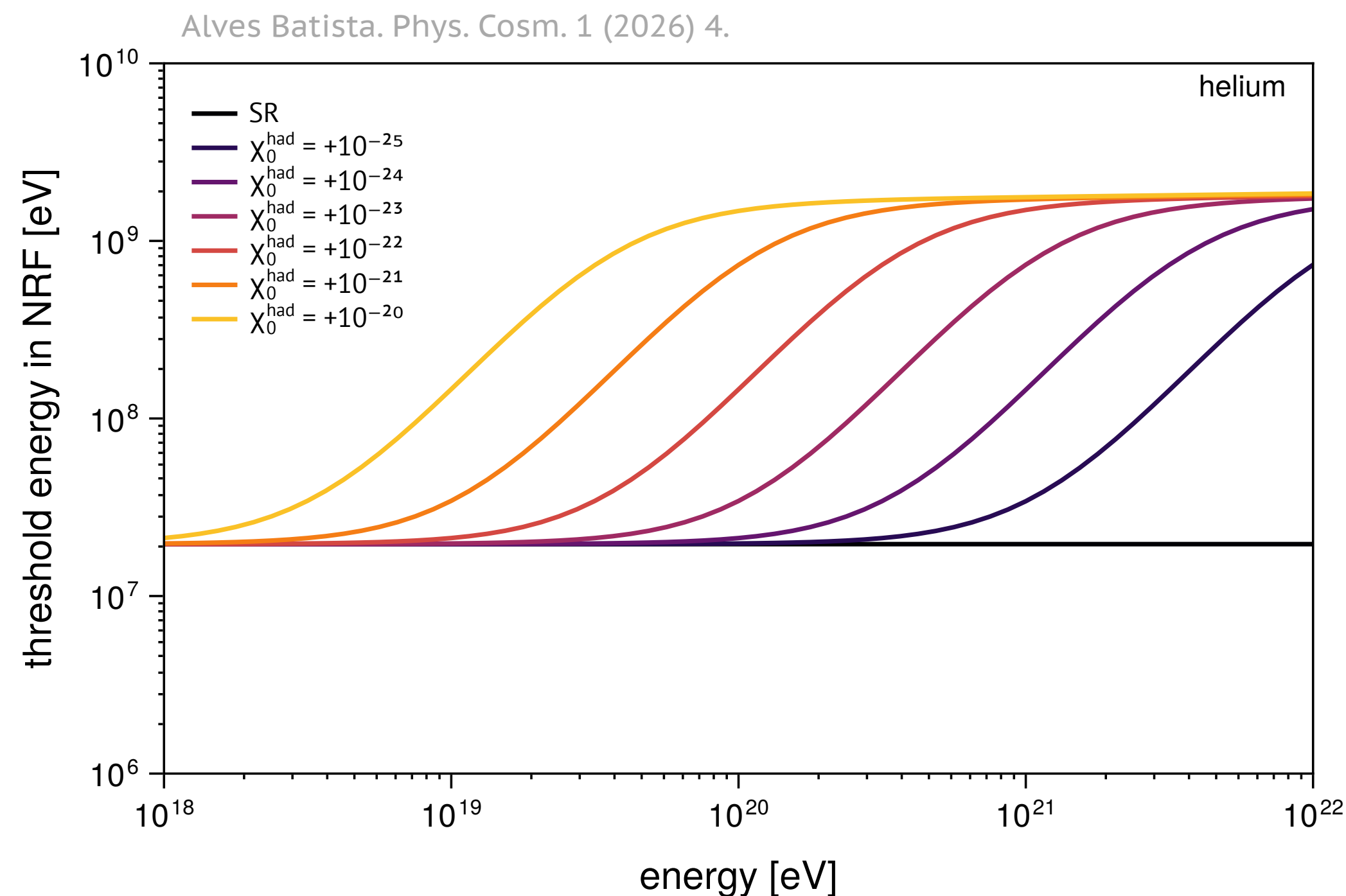
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cosmogenic particles



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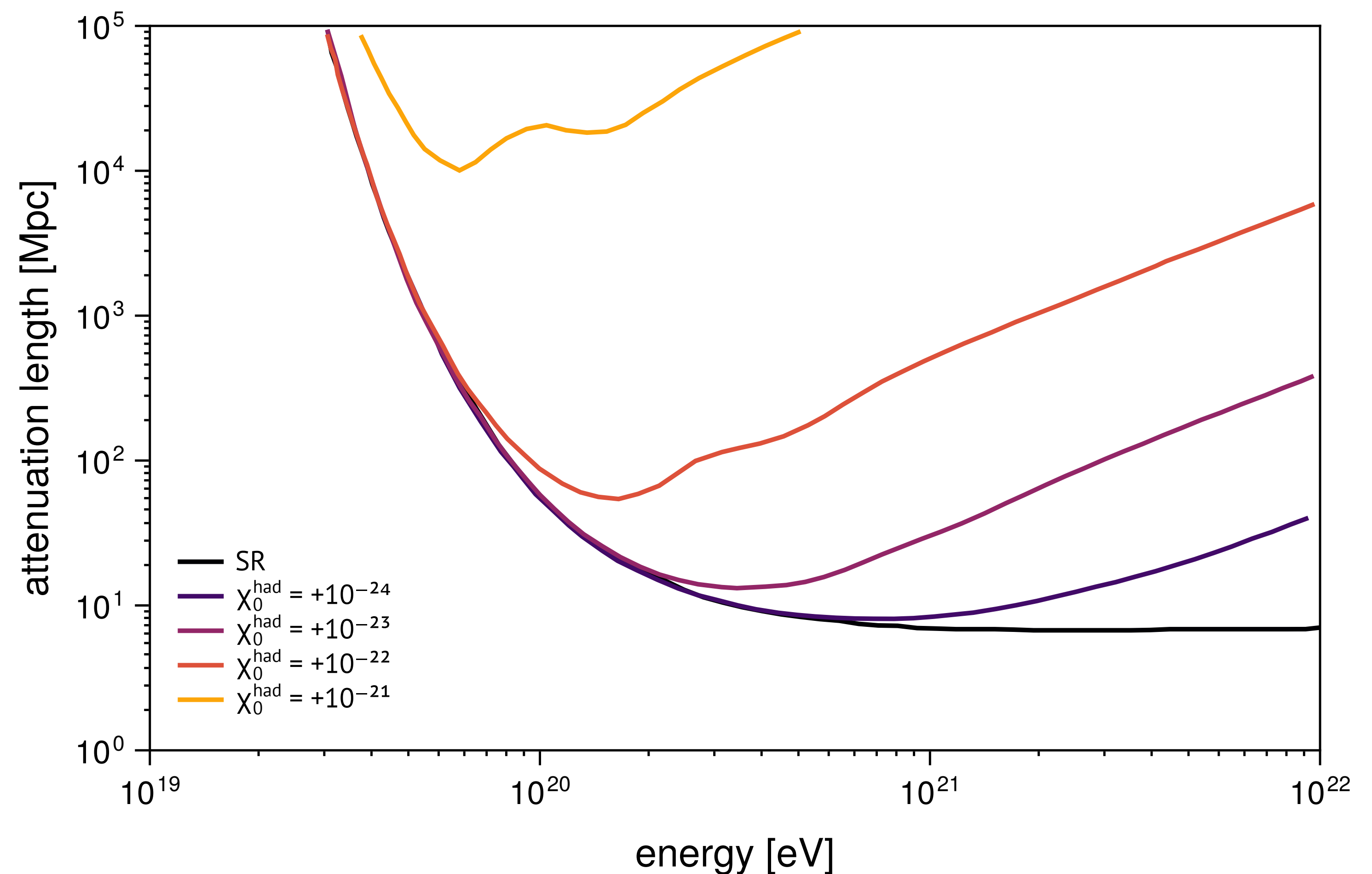
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$$p + \gamma_{bg} \rightarrow p + \pi^0$$

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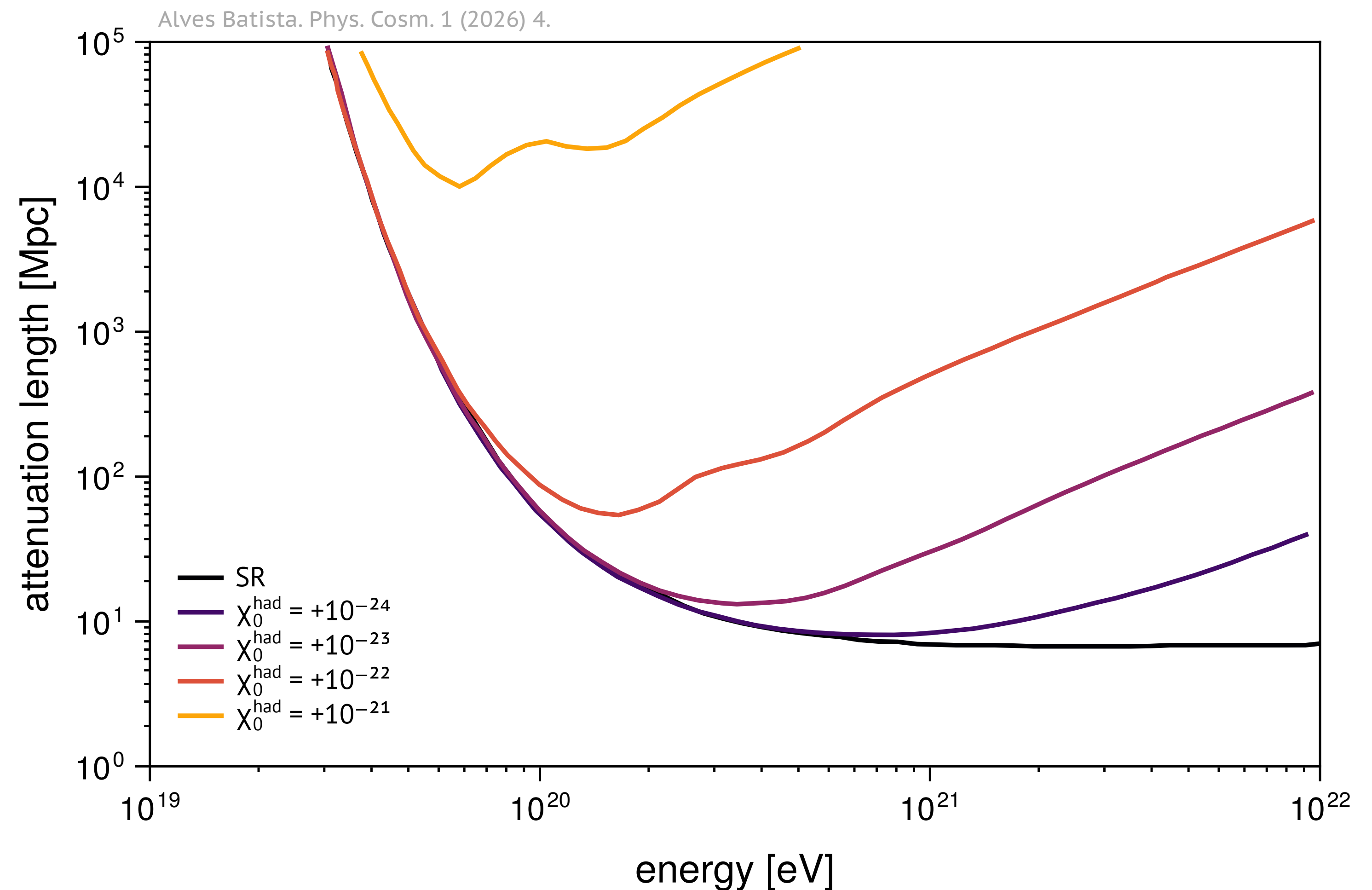
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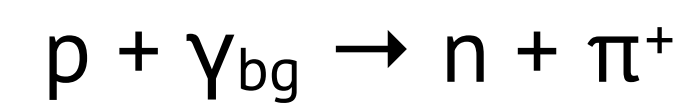
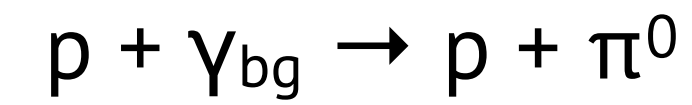


## LIV-induced modifications

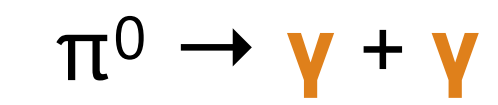
$$E^2 = m_a^2 c^4 + p^2 c^2 + f_a(E, \vec{p})$$

$$f_a(E, \vec{p}) \approx f_a(p) = p^2 c^2 \sum_{n=0}^{\infty} \chi_n^{(a)} \left( \frac{pc}{E_\star} \right)^n$$

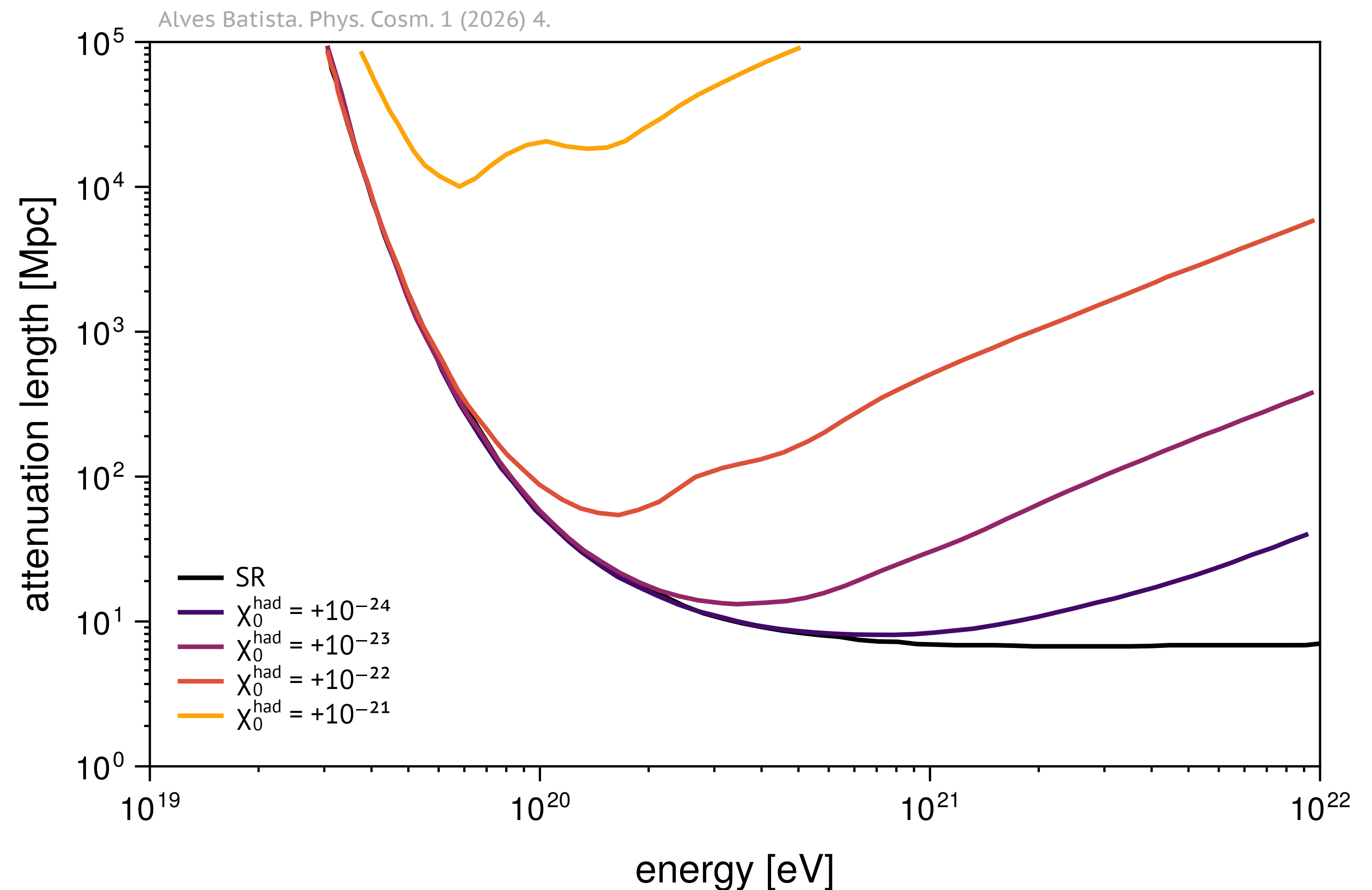
## photoproduction of mesons



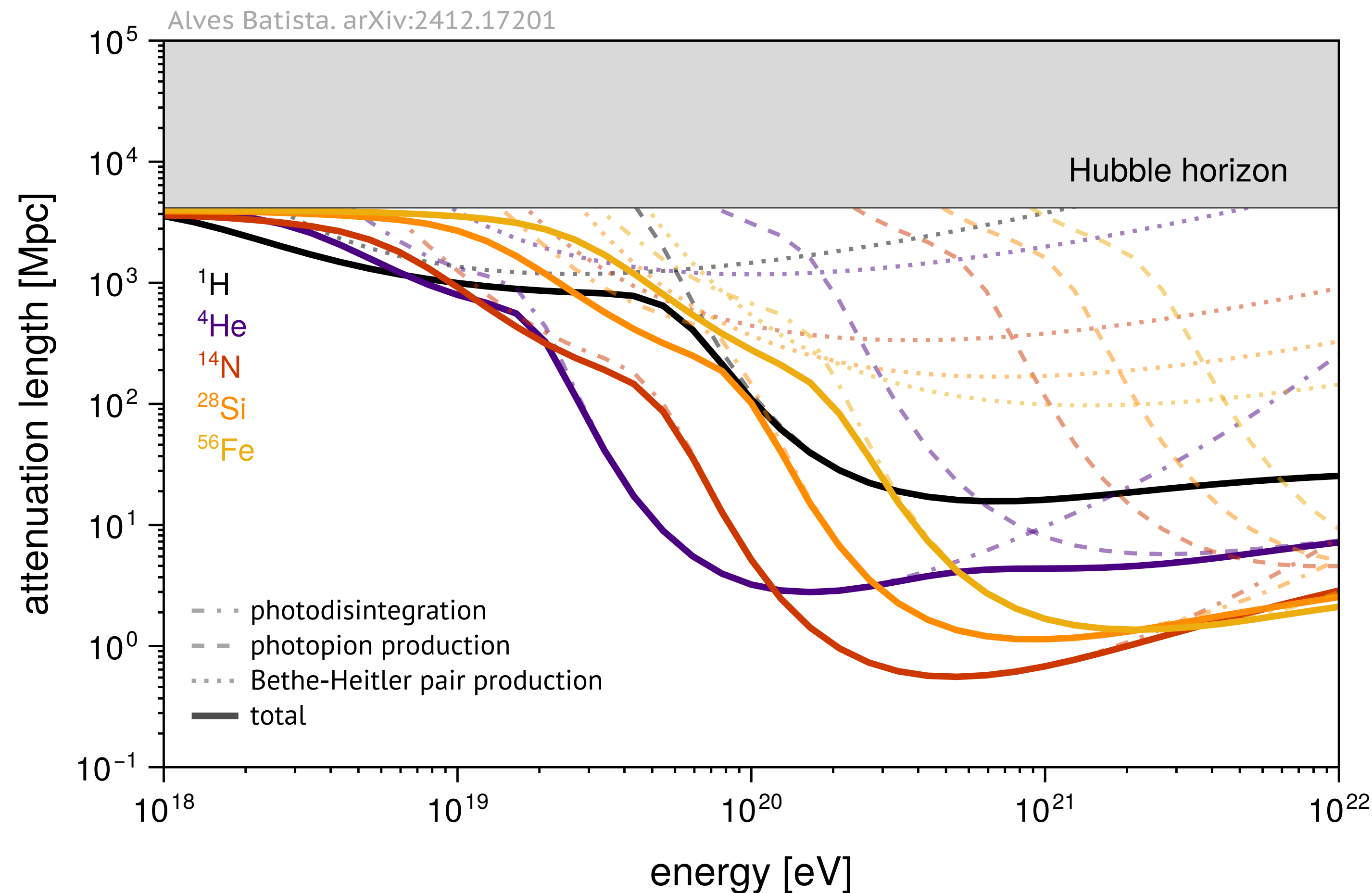
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cosmogenic particles



# UHECR propagation



## photoproduction of mesons

$$p + \gamma_{\text{bg}} \rightarrow p + \pi^0$$

$$\pi^0 \rightarrow \gamma + \gamma$$

$$p + \gamma_{\text{bg}} \rightarrow n + \pi^+$$

$$\pi^+ \rightarrow \nu_{\mu} + \mu^+$$

$$\mu^+ \rightarrow e^+ + \nu_e + \bar{\nu}_{\mu}$$

(similar for nuclei)

## Bethe-Heitler pair production

$$\text{nucleus}(A, Z) + \gamma_{\text{bg}} \rightarrow \text{nucleus}(A, Z) + e^- + e^+$$

## photodisintegration

$$\text{nucleus}(A, Z) + \gamma_{\text{bg}} \rightarrow \text{nucleus}(A-1, Z) + n$$

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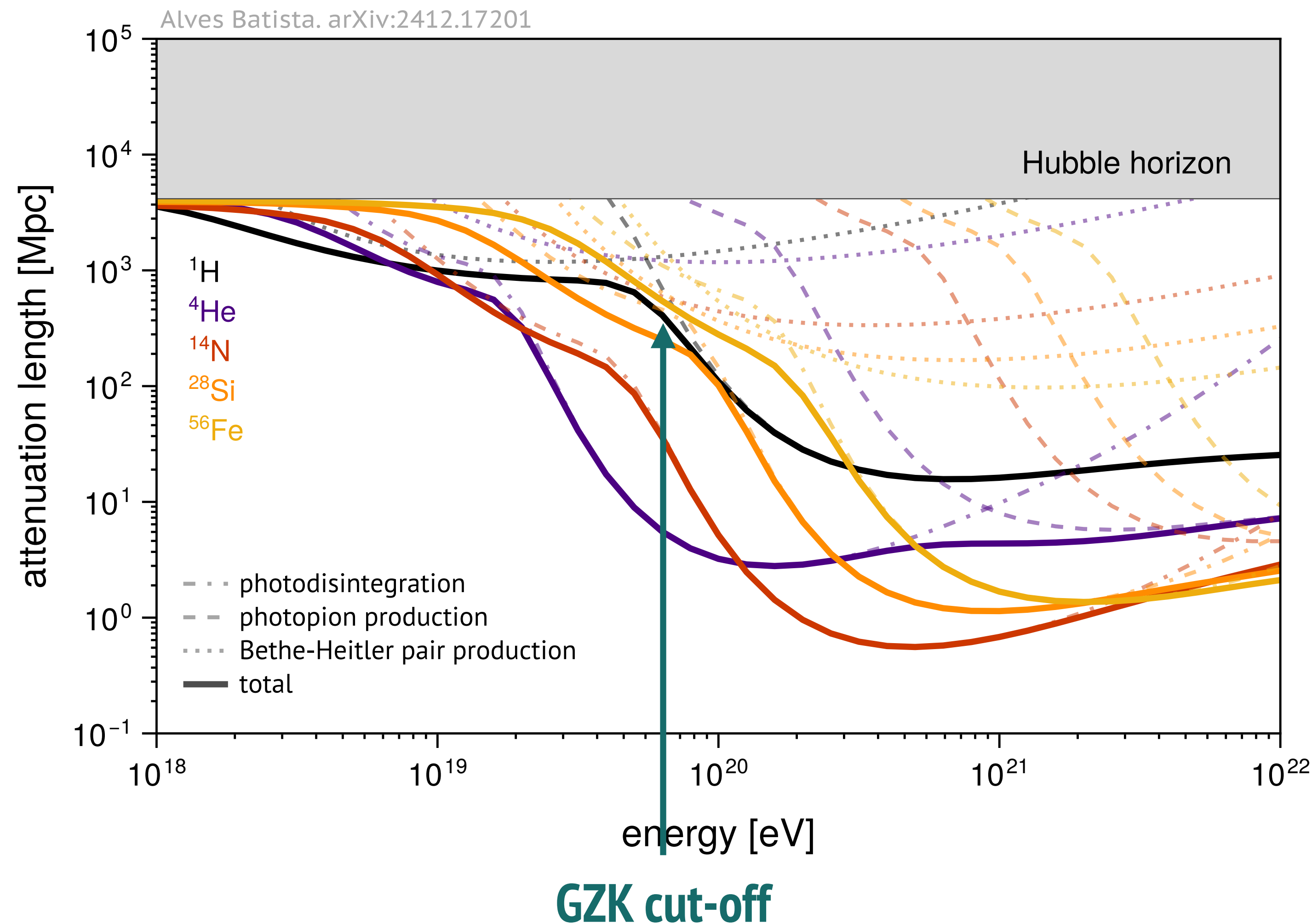
$$\text{nucleus}(A, Z) \rightarrow \text{nucleus}(A-4, Z-2) + \alpha$$

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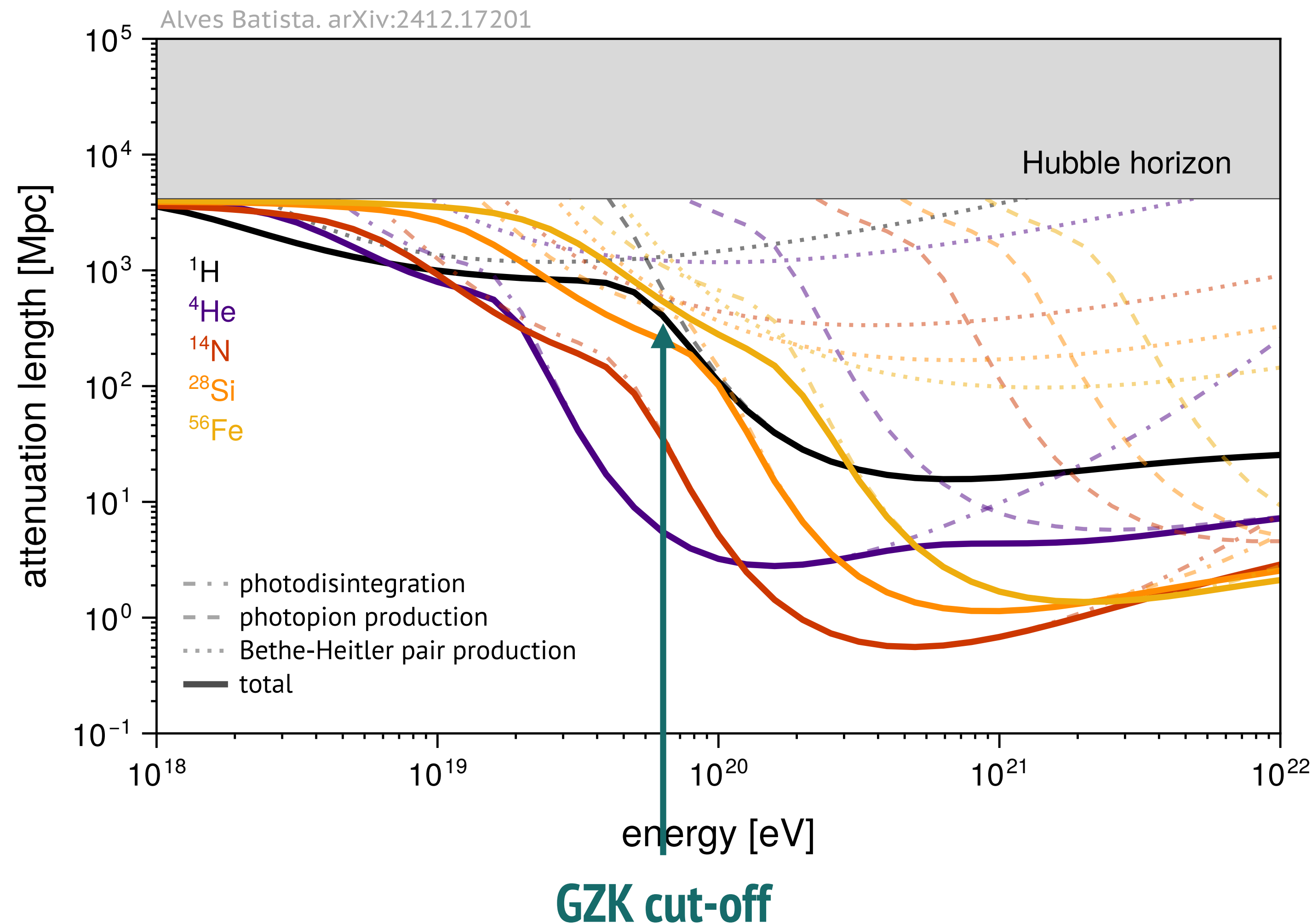
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# UHECR propagation



$$s = m^2 + 2E\epsilon(1 - \beta \cos \theta)$$

$$s = (m_p + m_\pi)^2 \simeq m^2 + 2E_p\epsilon_{\text{CMB}}$$

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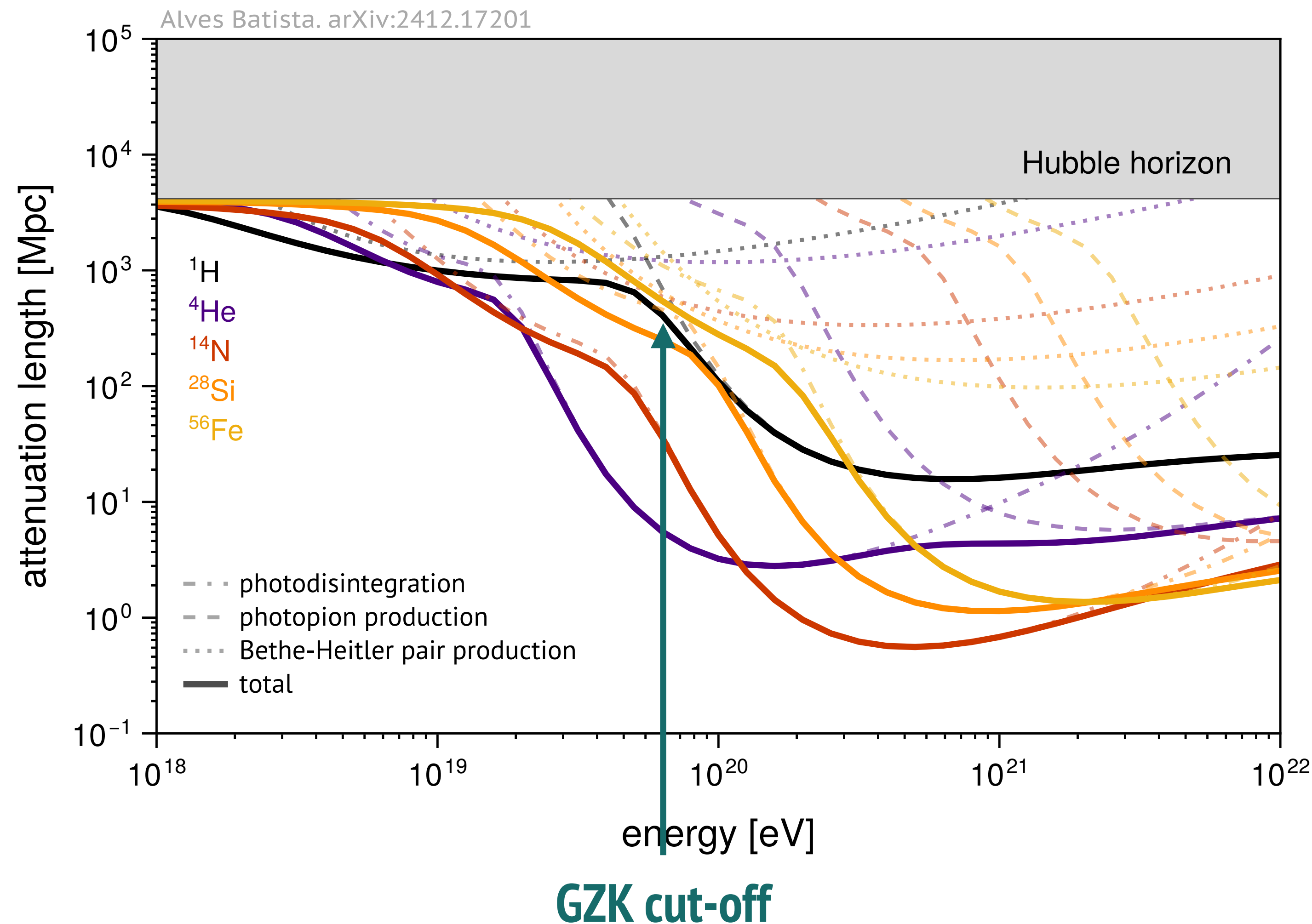
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$$E_{\text{GZK}} \simeq 6 \text{ EeV} \equiv 6 \times 10^{19} \text{ eV}$$

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# self-consistent constraints in **hadronic sector**

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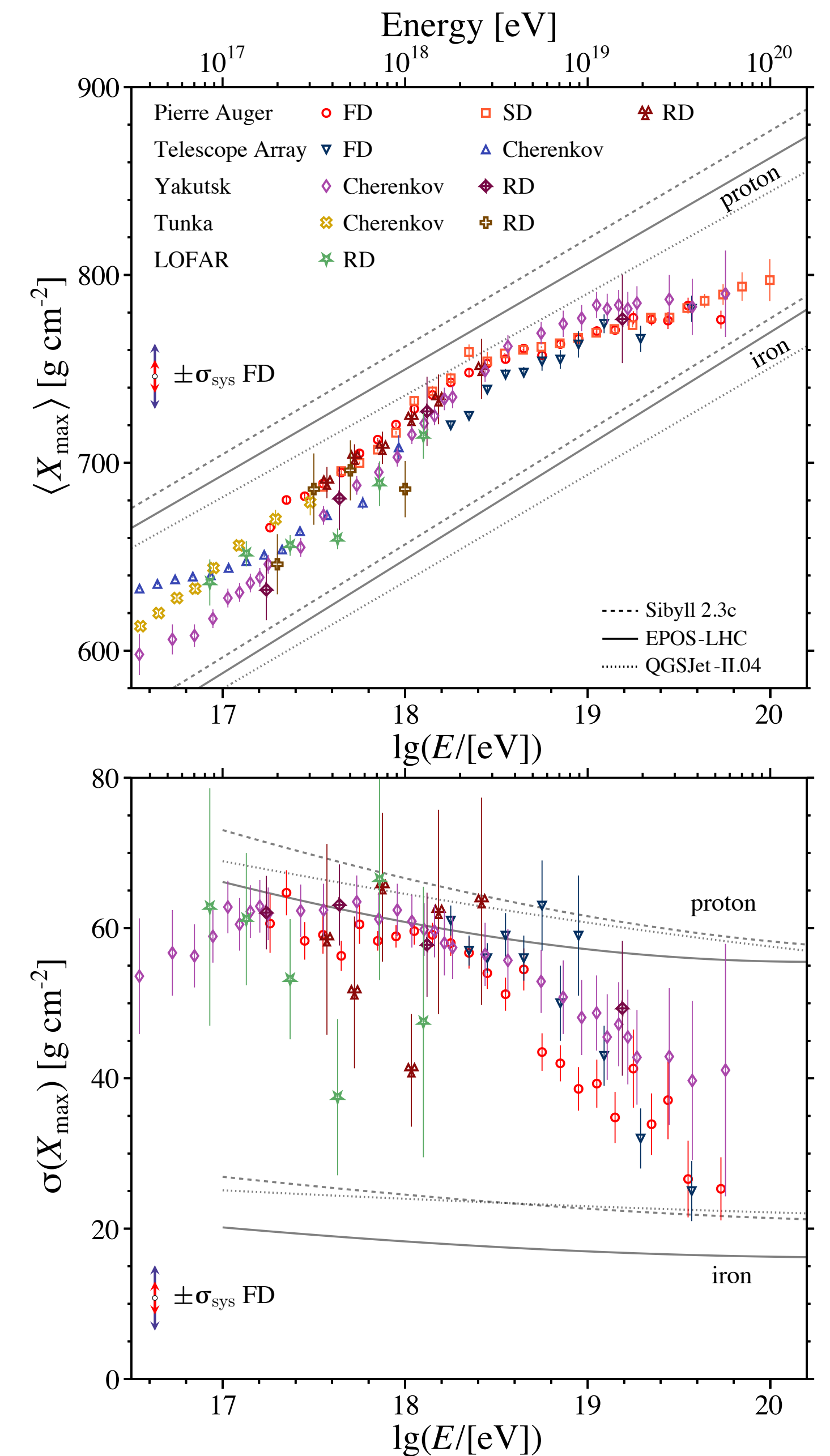
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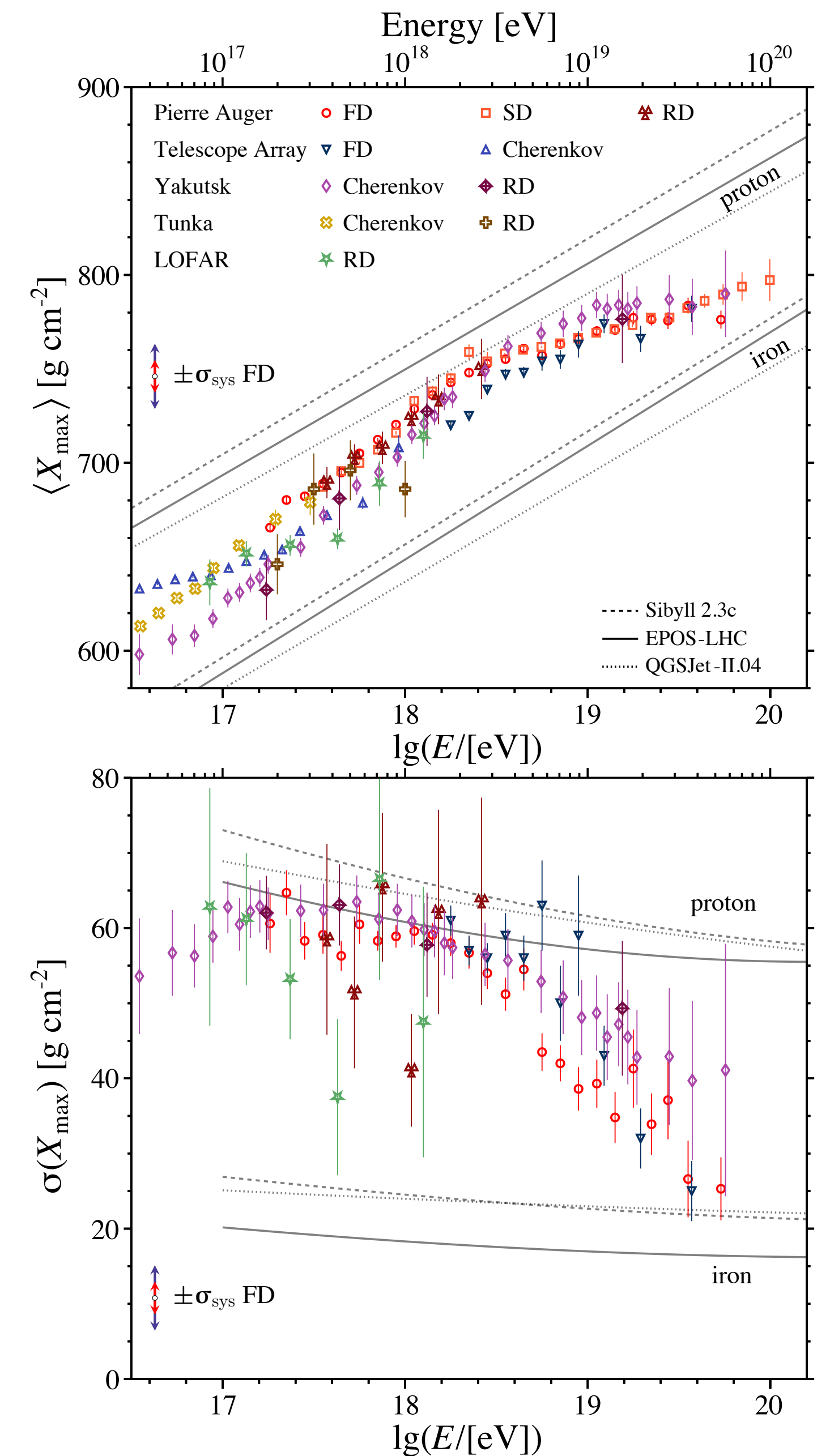
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- ▶ **problem:** effects in the hadronic sector also affects the showers
- ▶ what we measure is  $X_{\max}$
- ▶ **how to tackle that?** LIV-CORSIKA working group



# gamma rays

# the usual approach to gamma-ray propagation

---

# the usual approach to gamma-ray propagation

flux  
attenuation

$$\Phi_o(E_o; z_s) = \Phi_s(E_{o,s}) \exp \left[ -\tau(E_o, z_s) \right]$$

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$$\tau(E_o, z_s) = \int_0^{z_s} dz \, \lambda^{-1} \left( \frac{E_{o,s}}{1+z}, z \right) \frac{d\ell}{dz}$$

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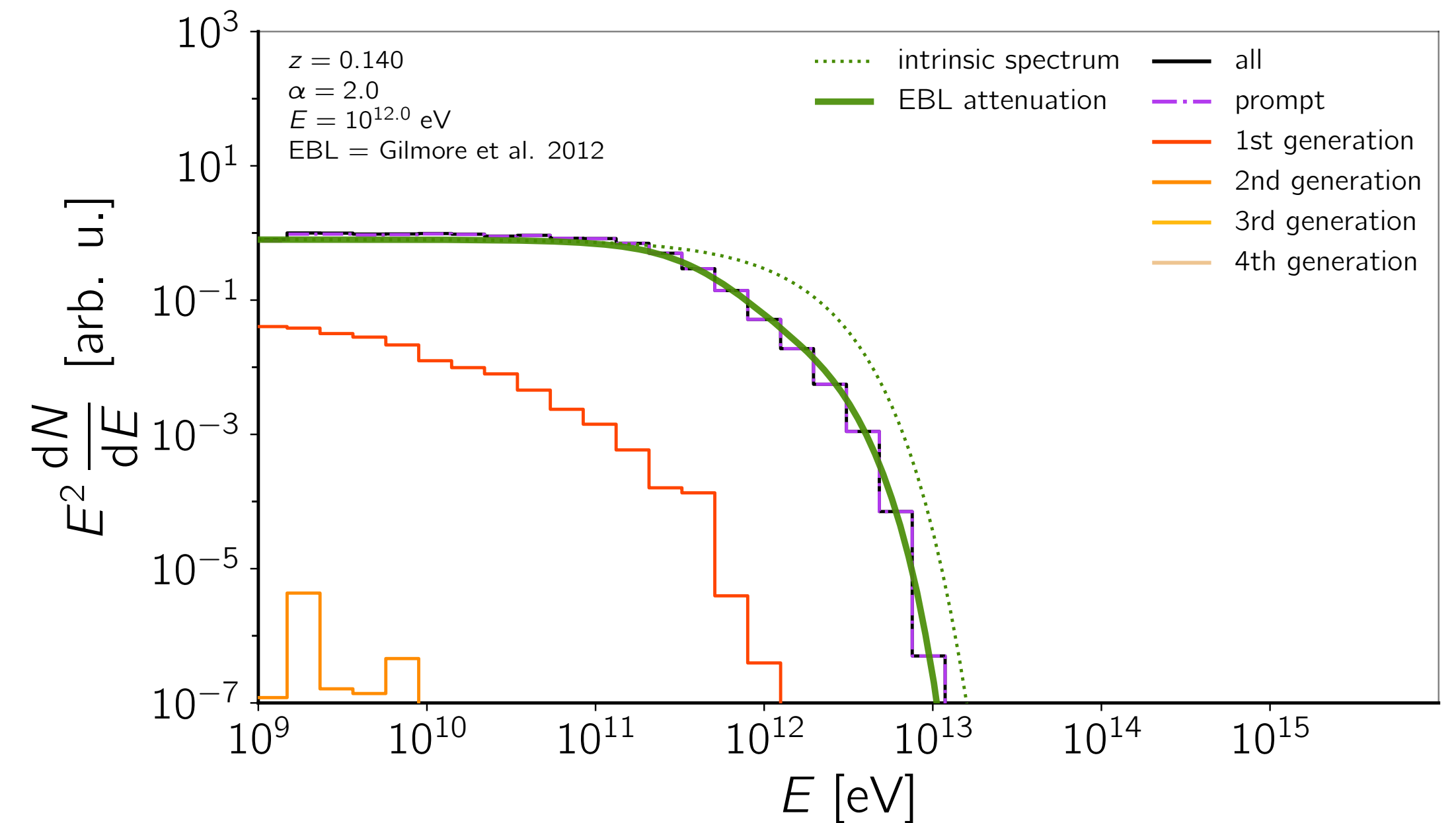
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simulations performed with **CR/Propa**

Alves Batista et al. JCAP 05 (2016) 038. arXiv:1603.07142

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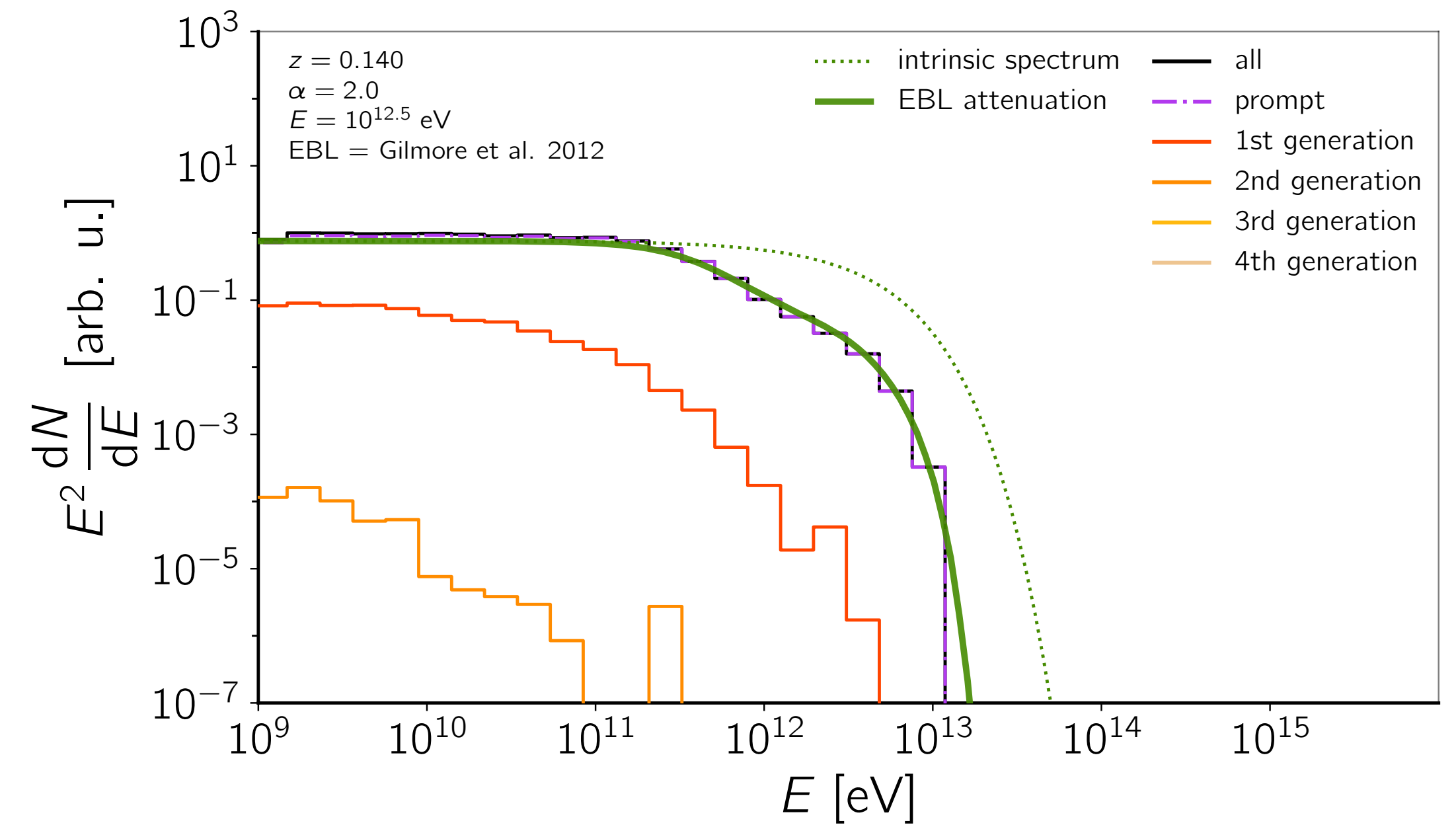
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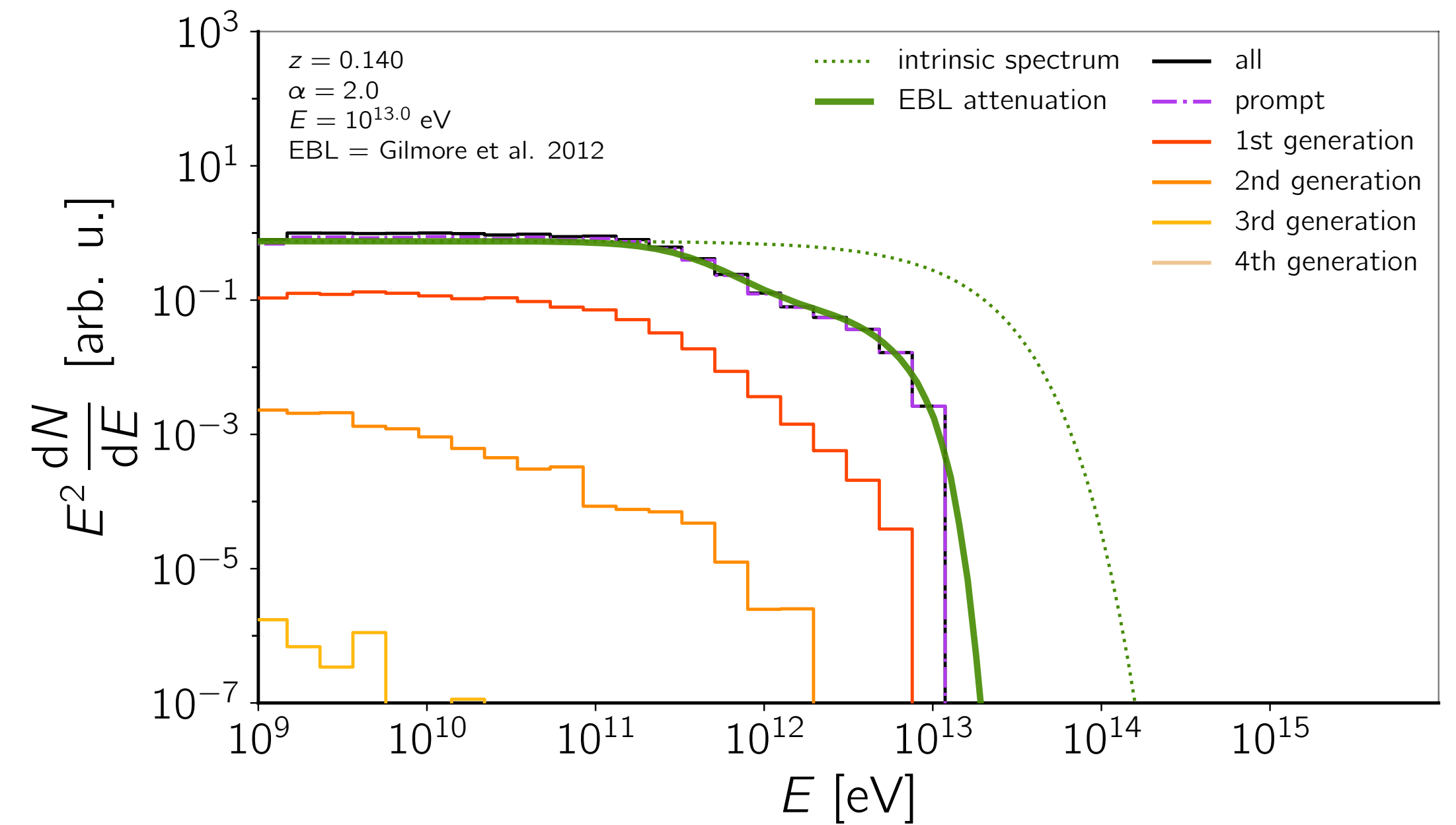
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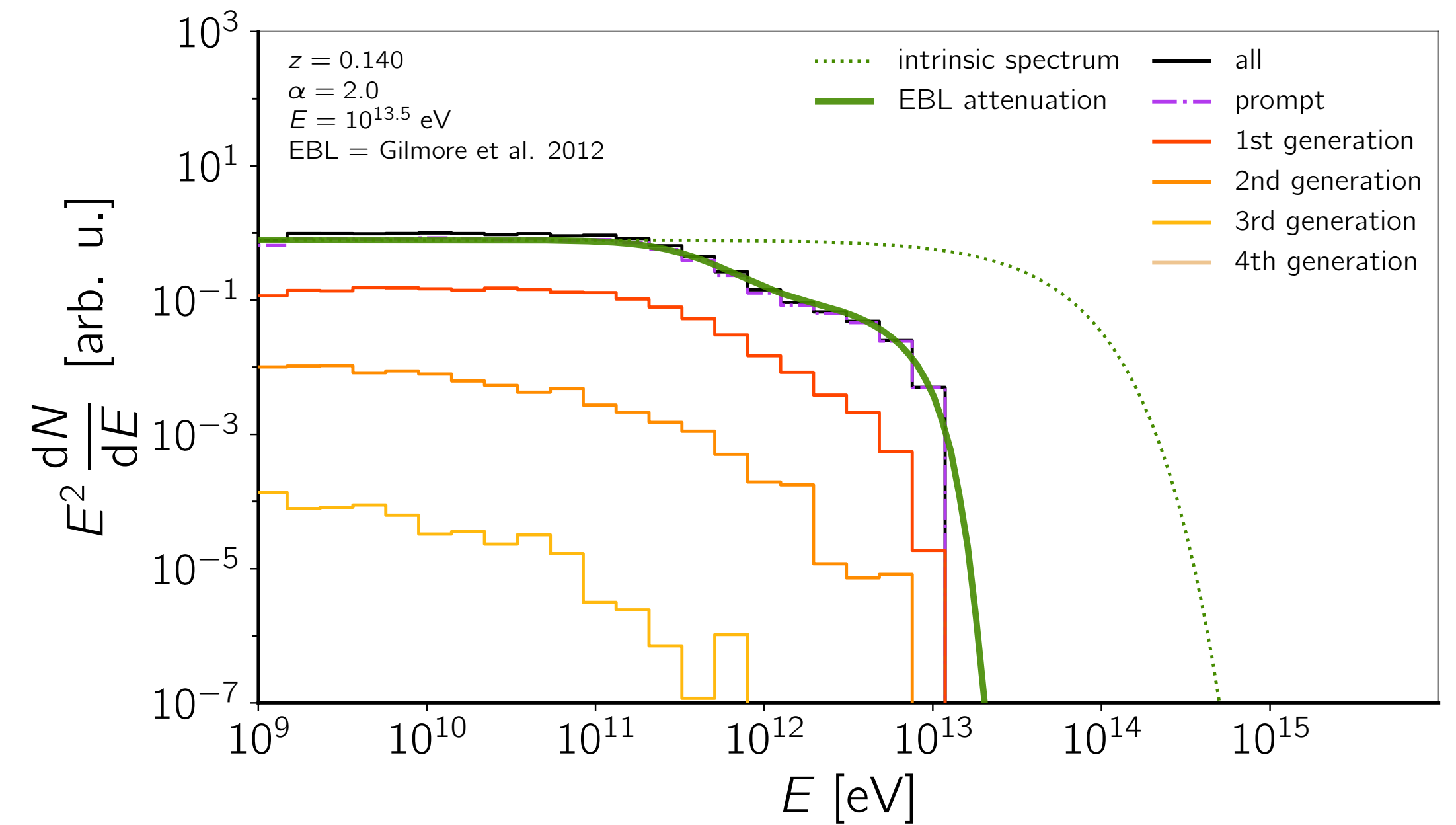
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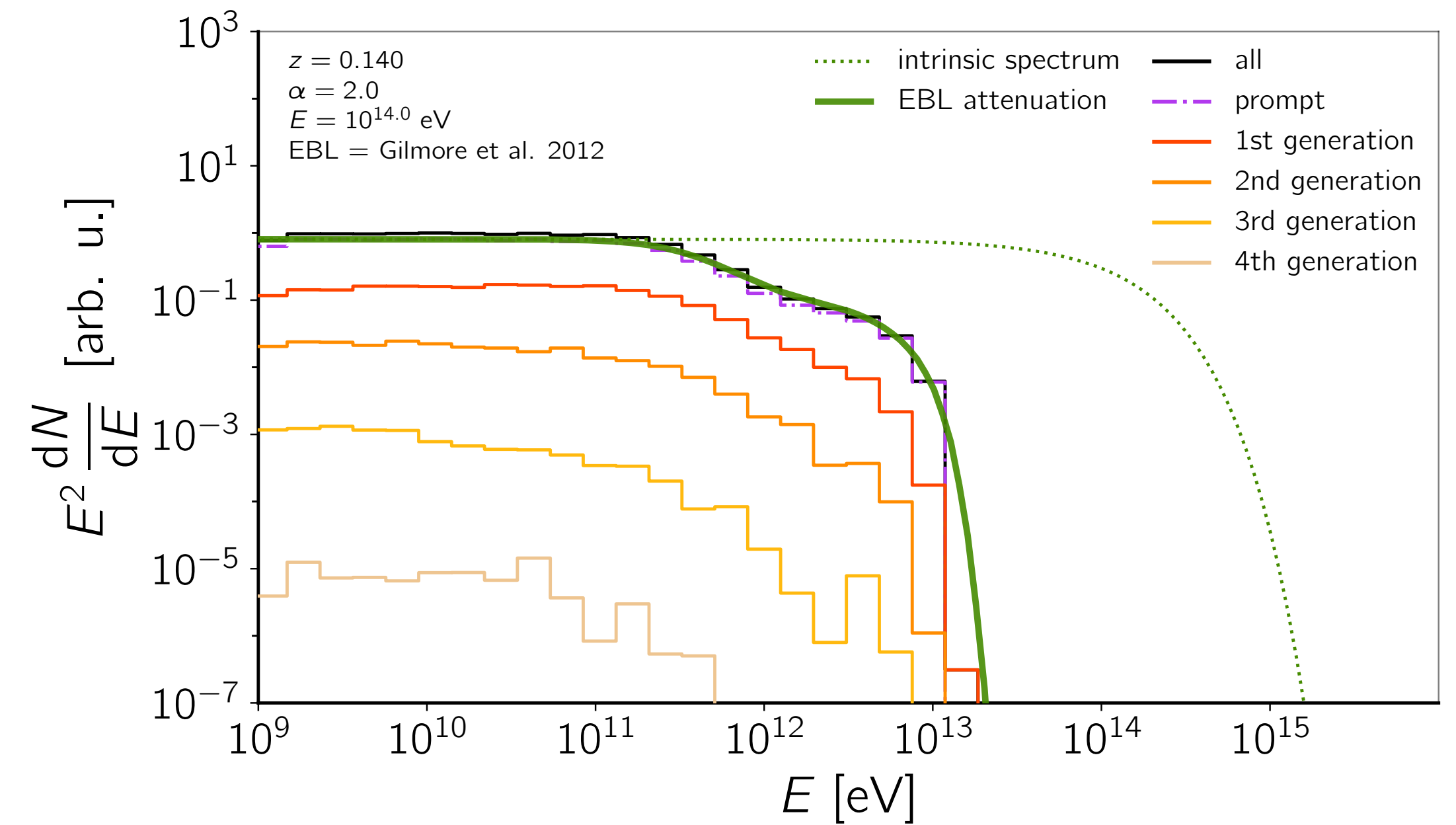
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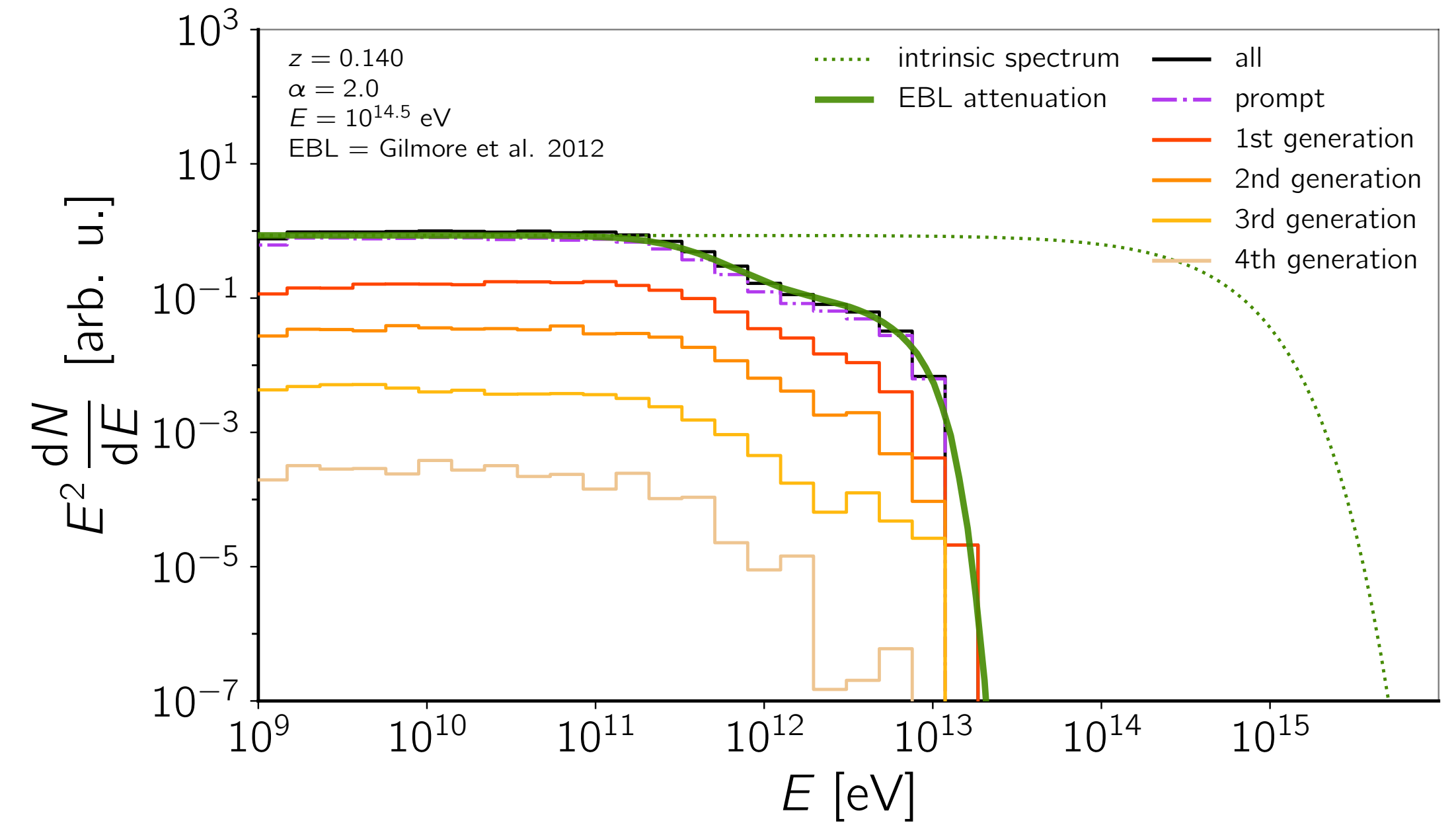
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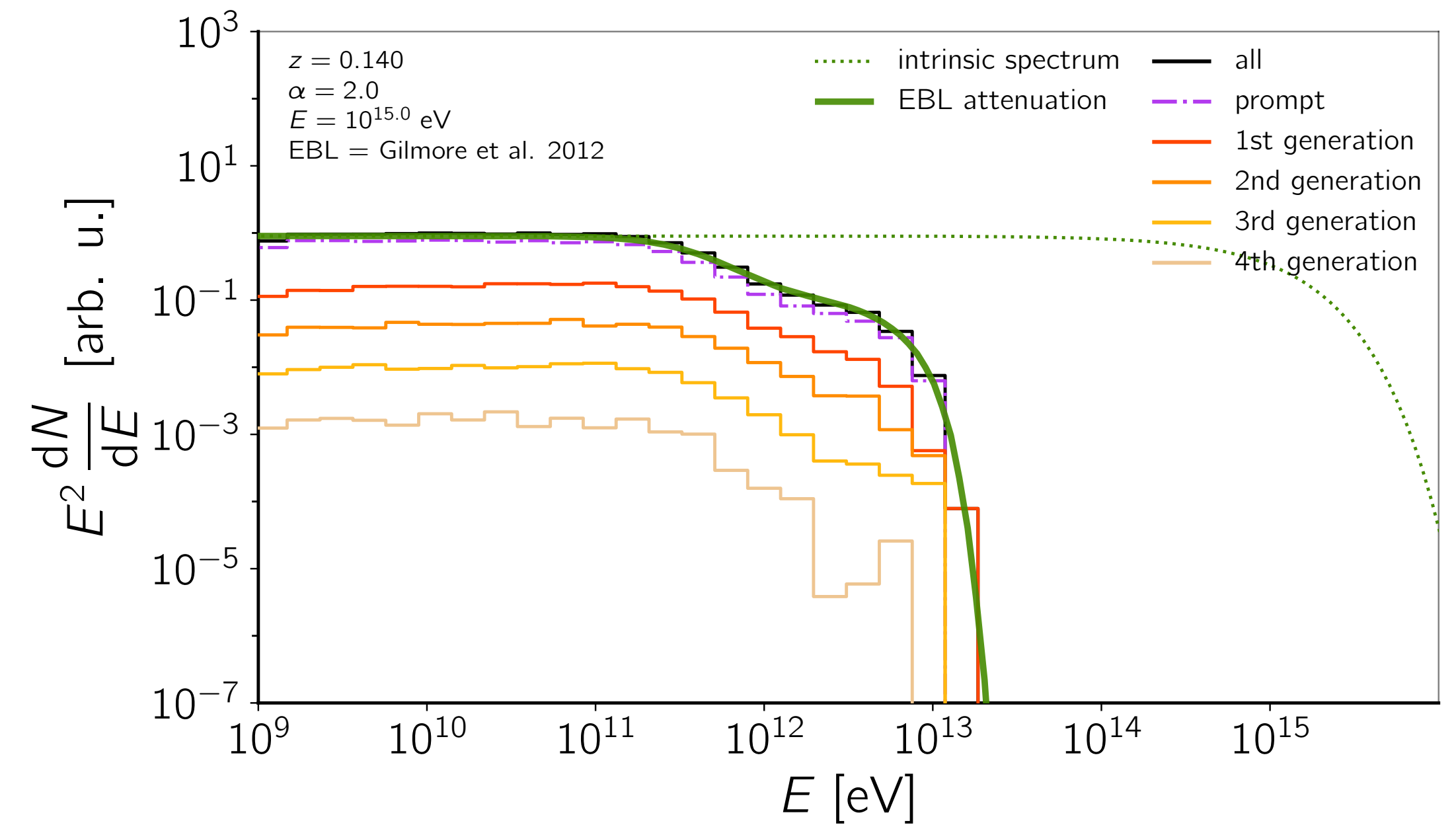
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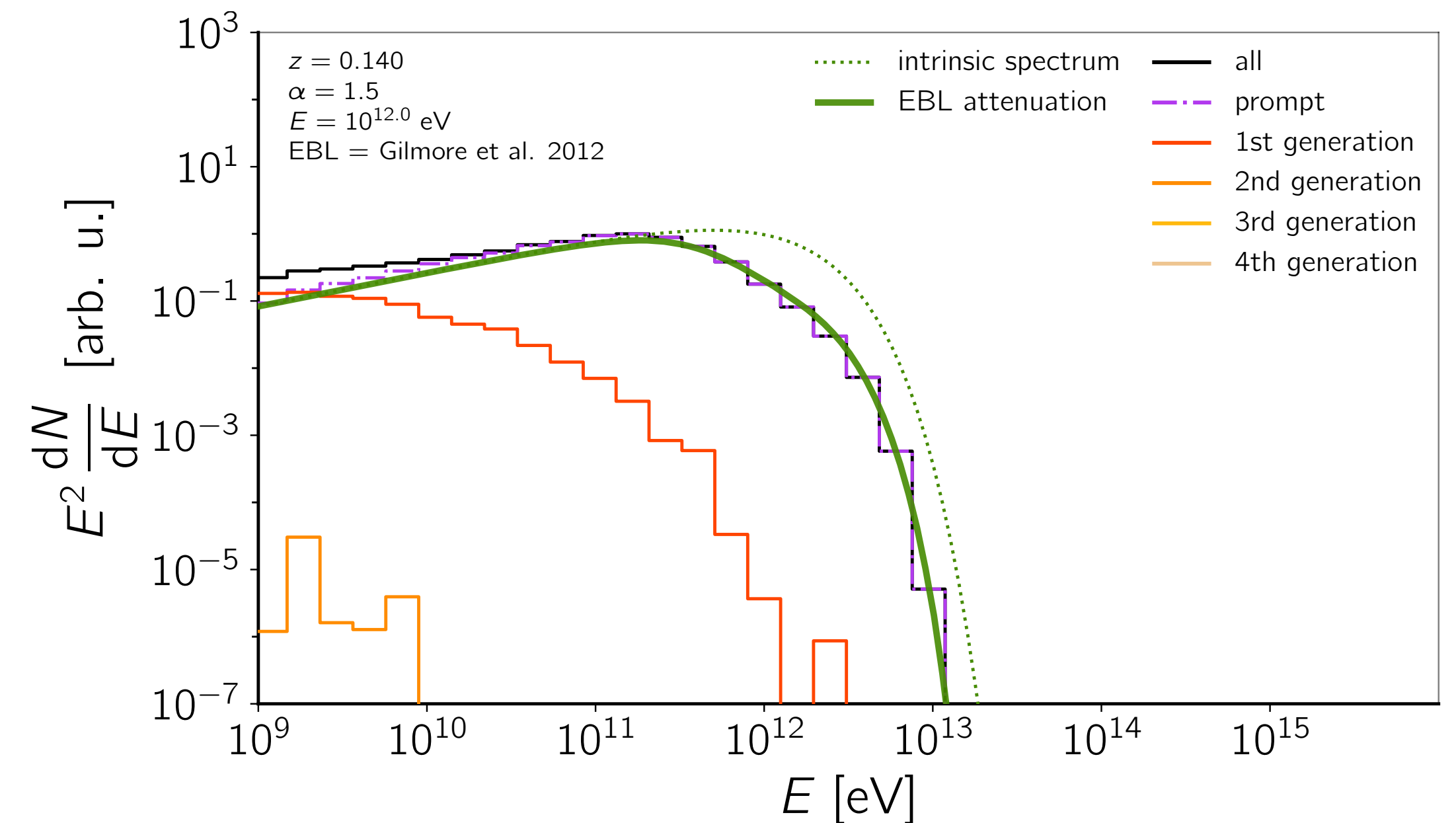
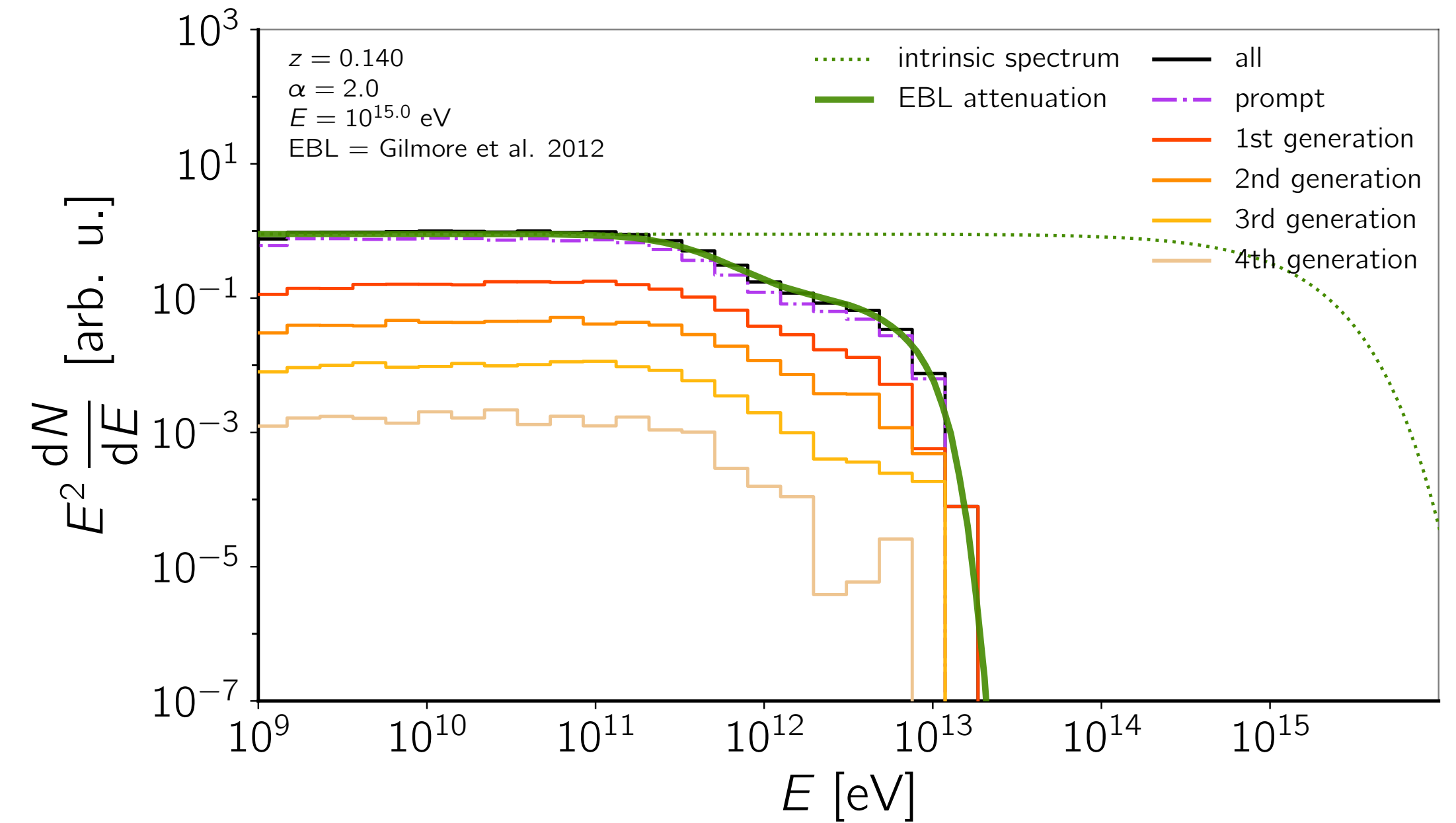
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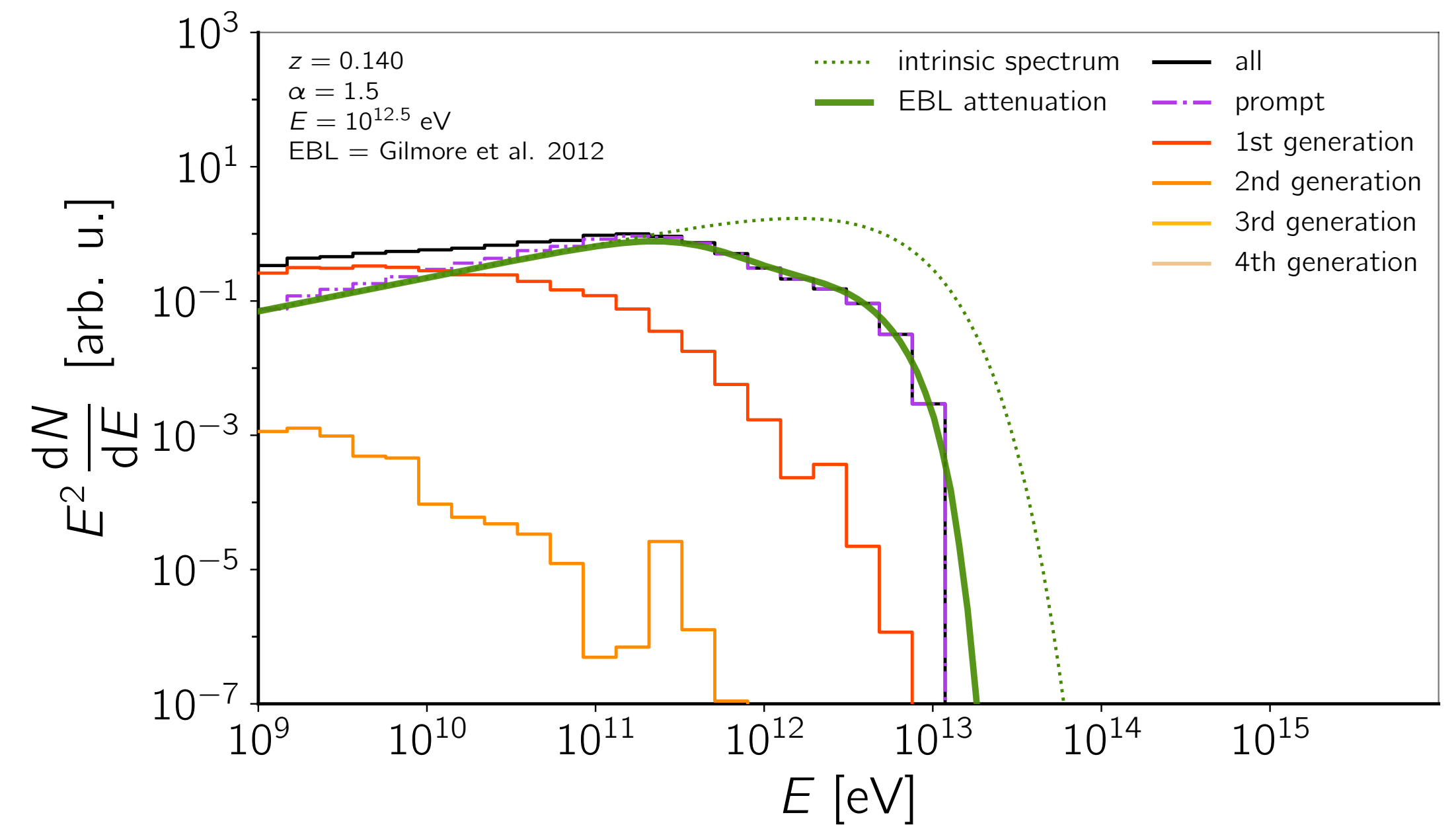
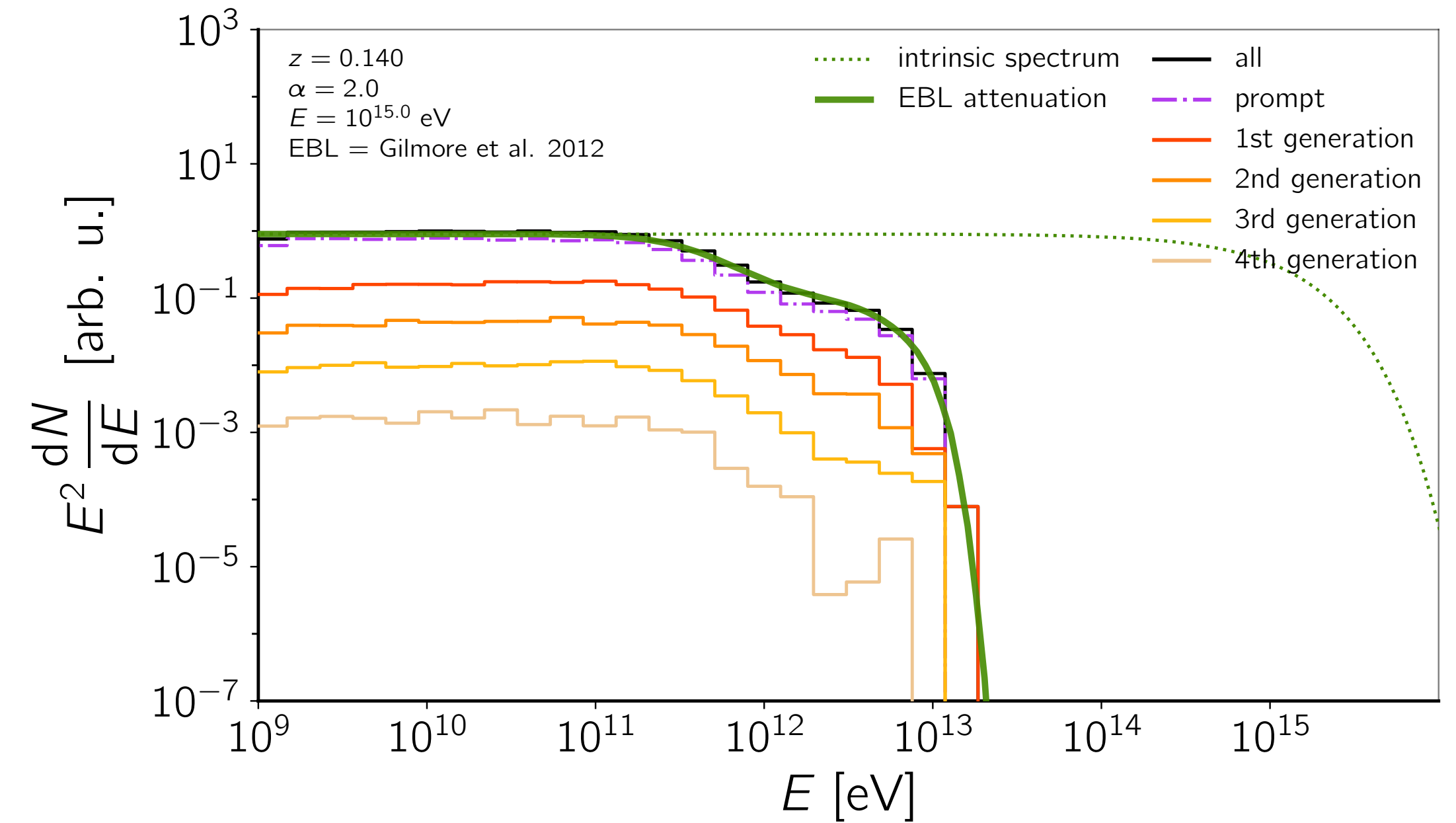
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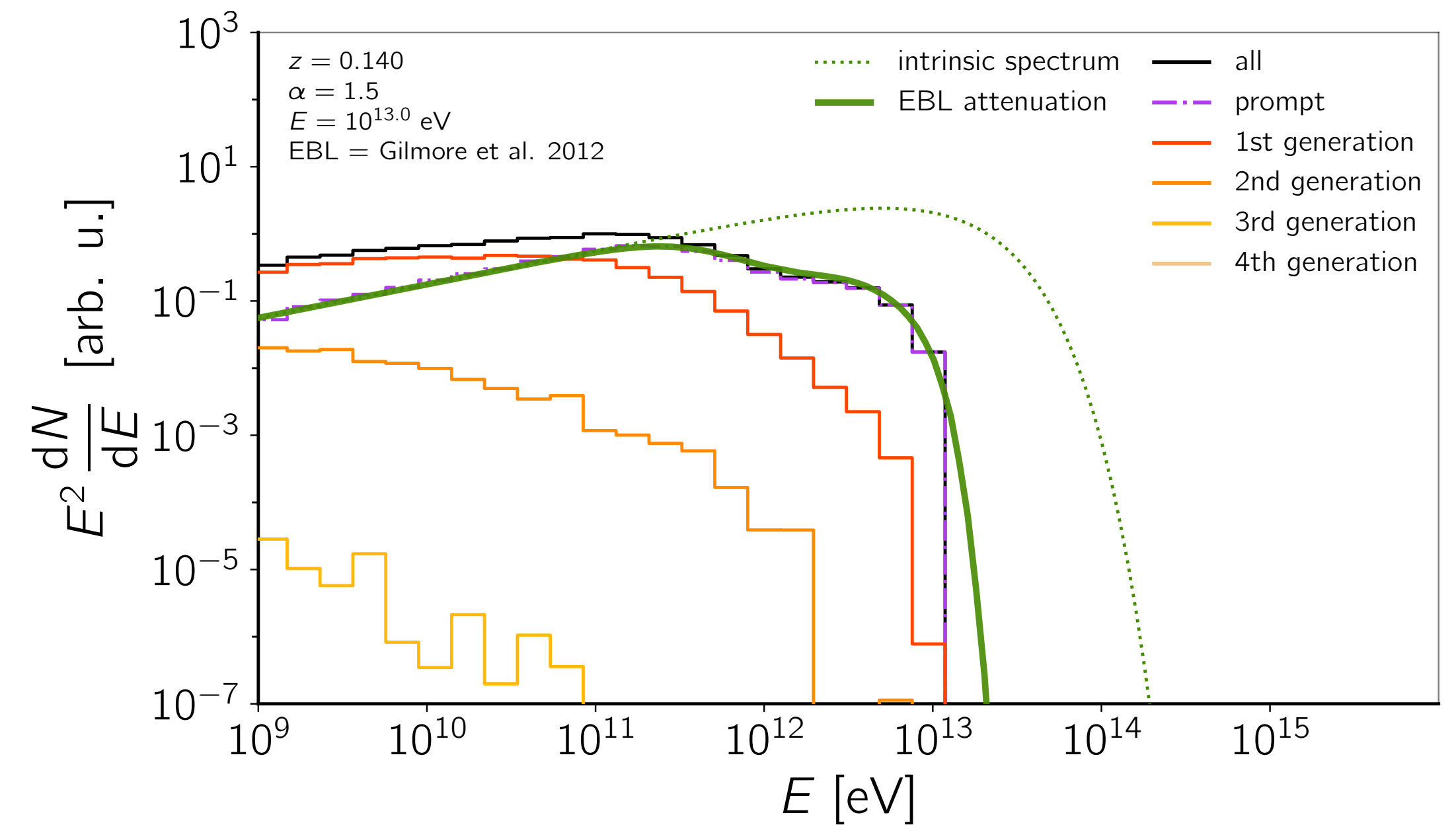
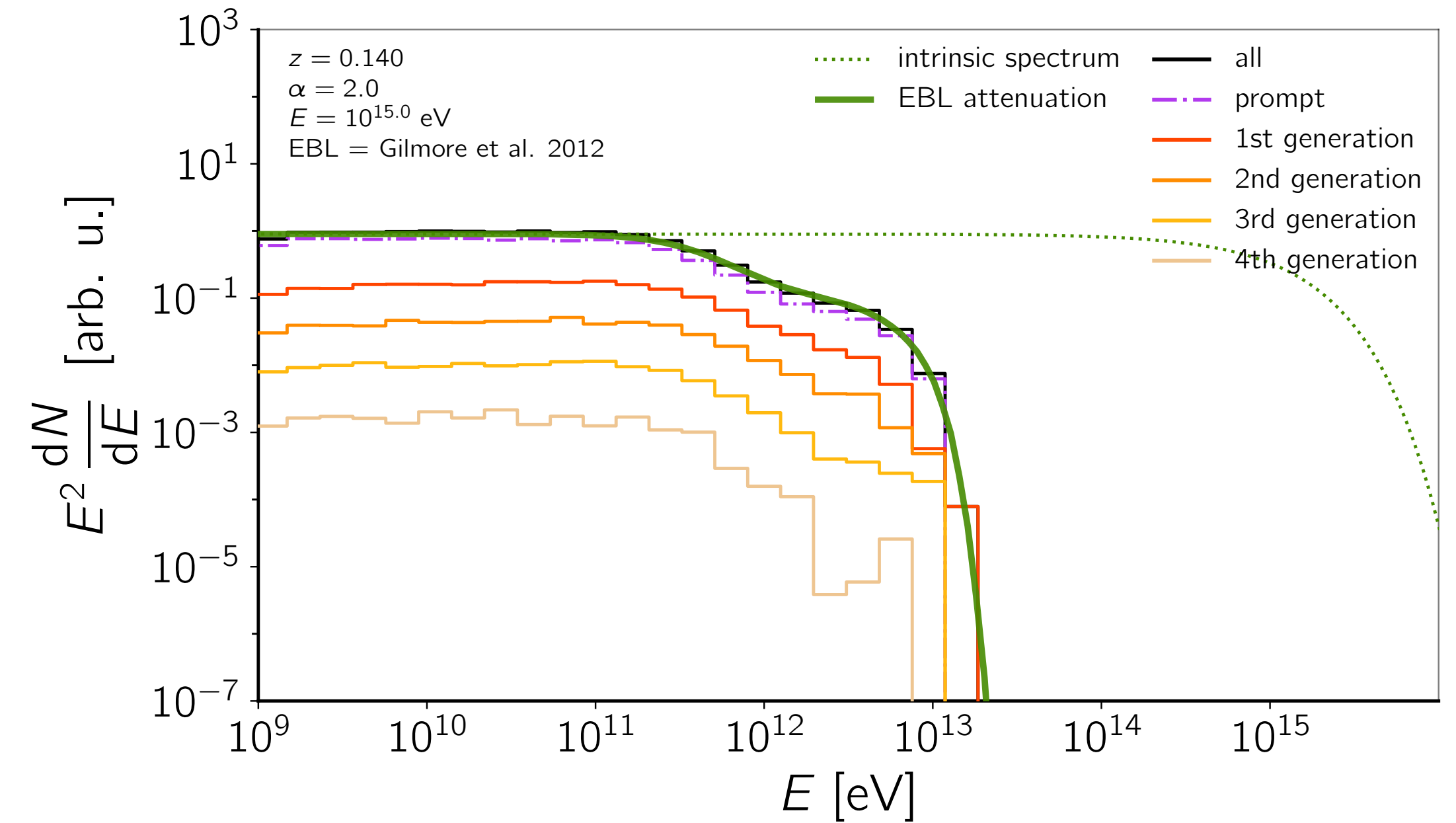
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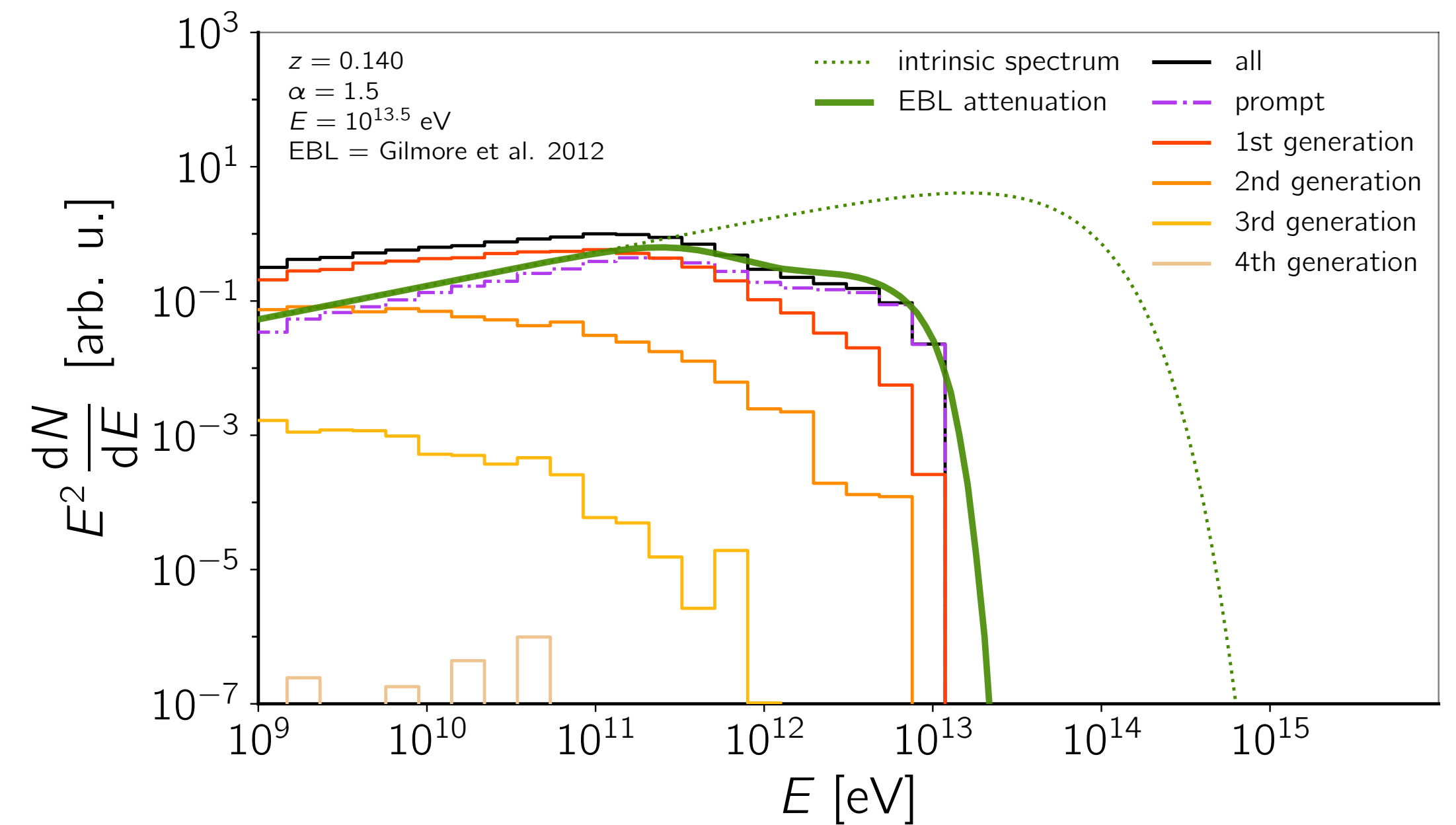
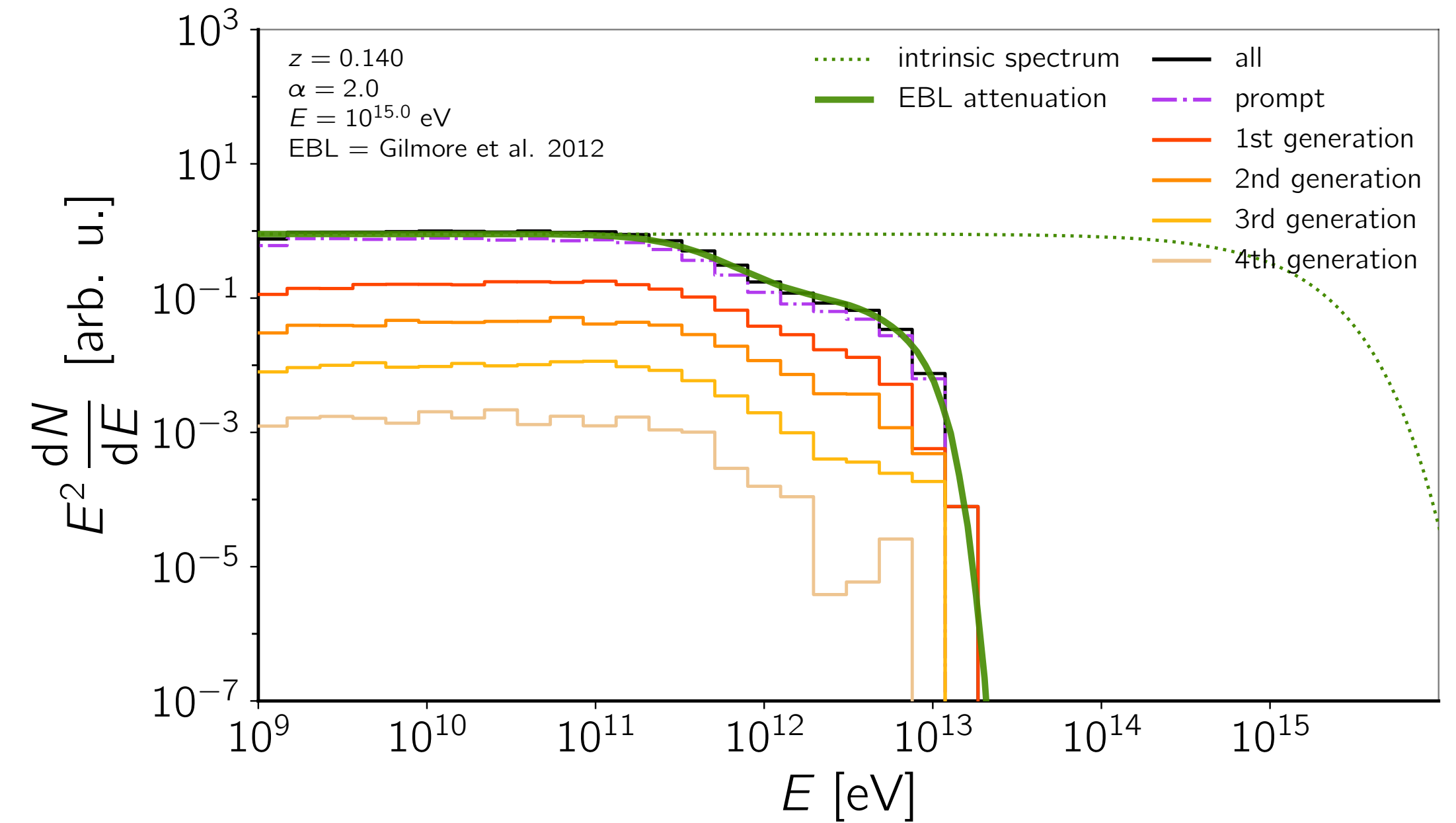
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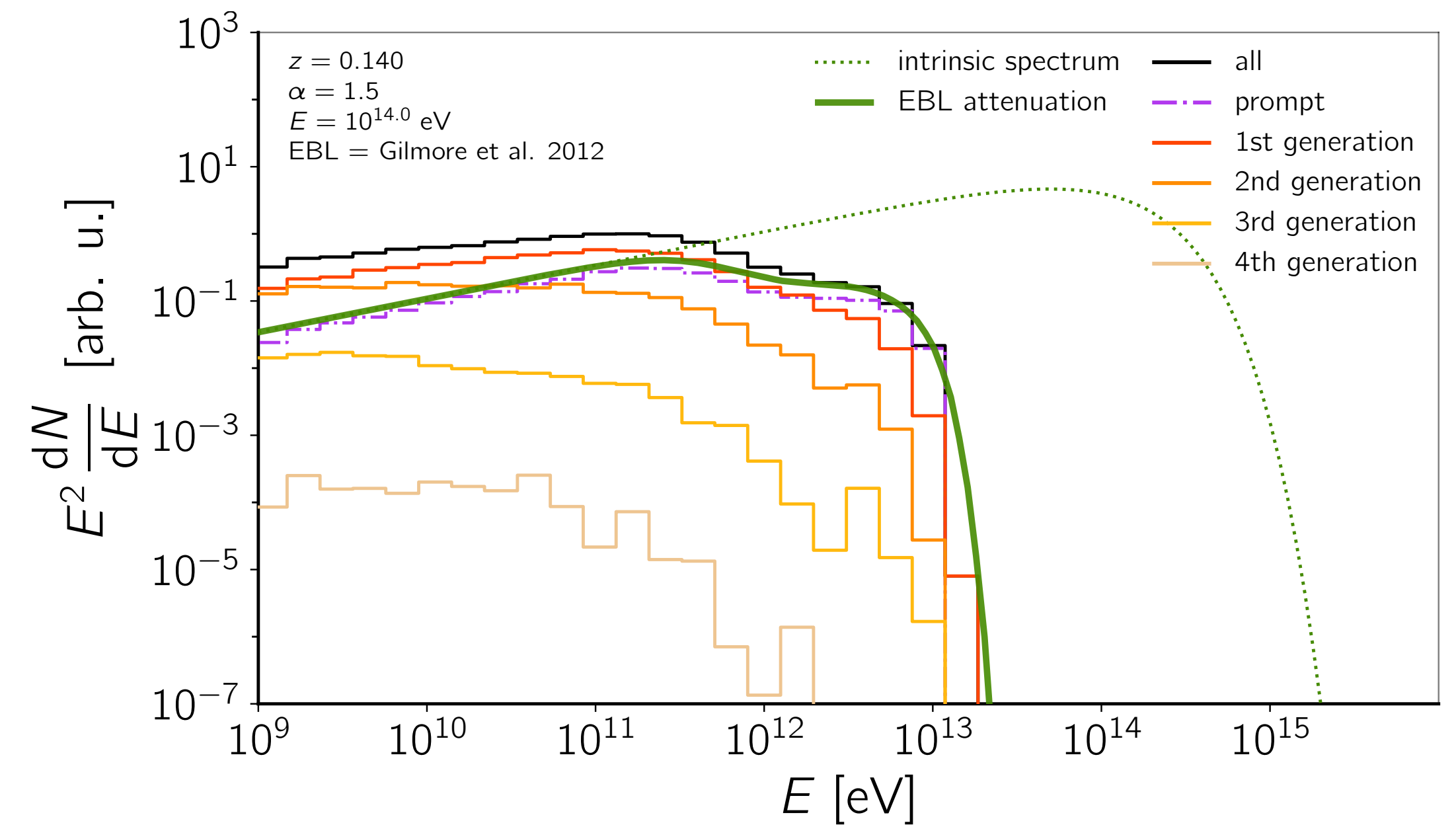
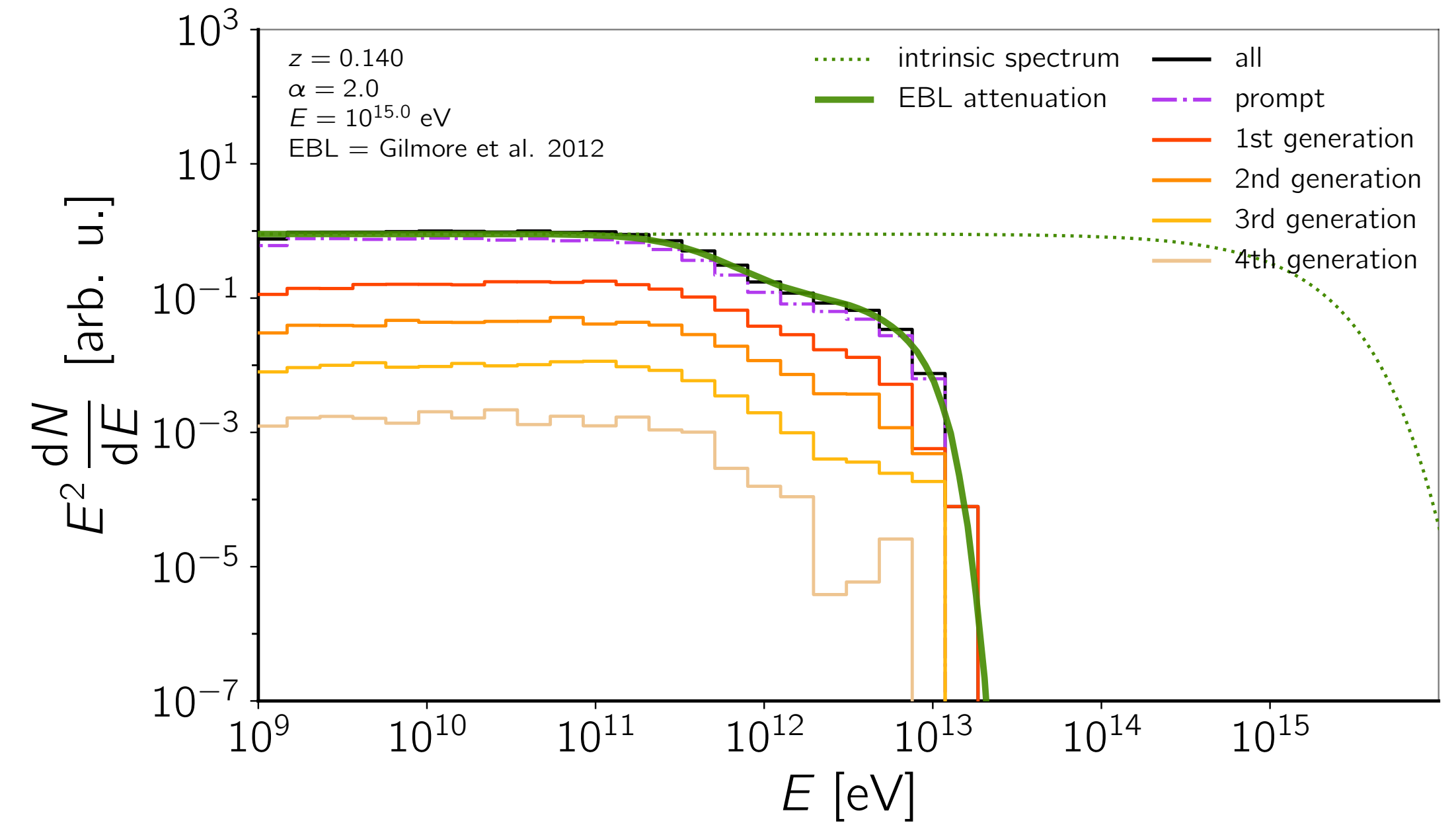
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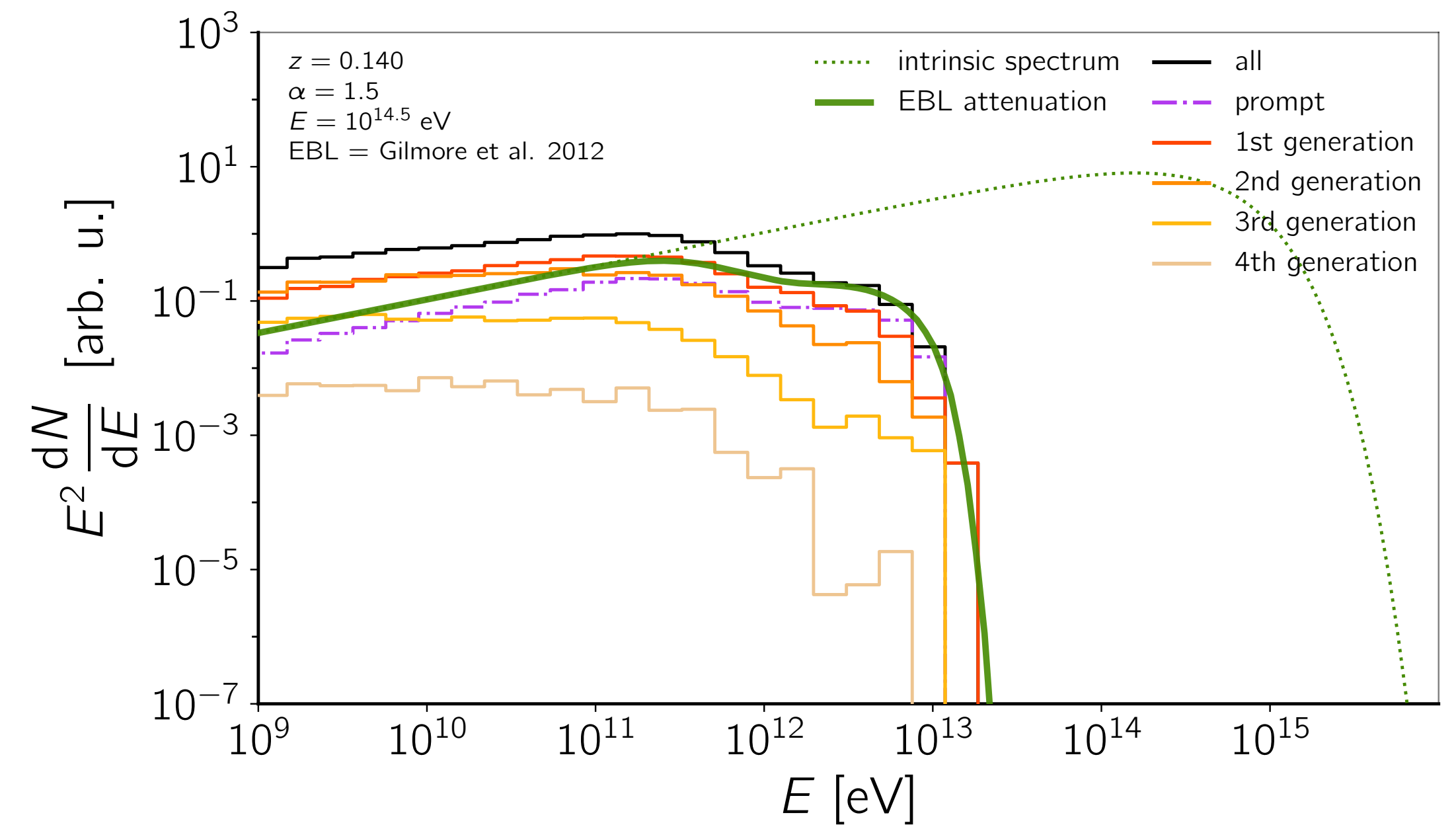
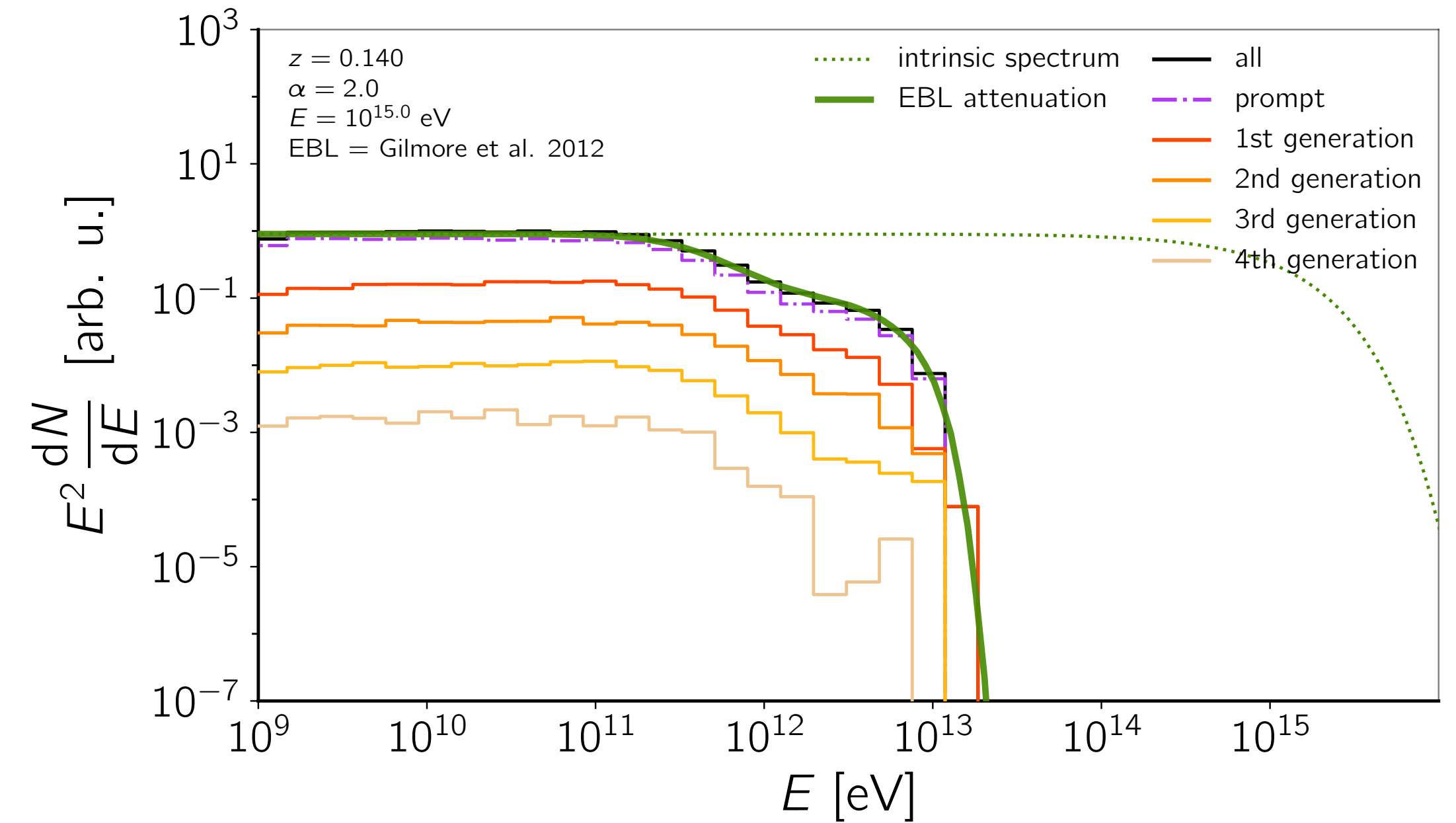
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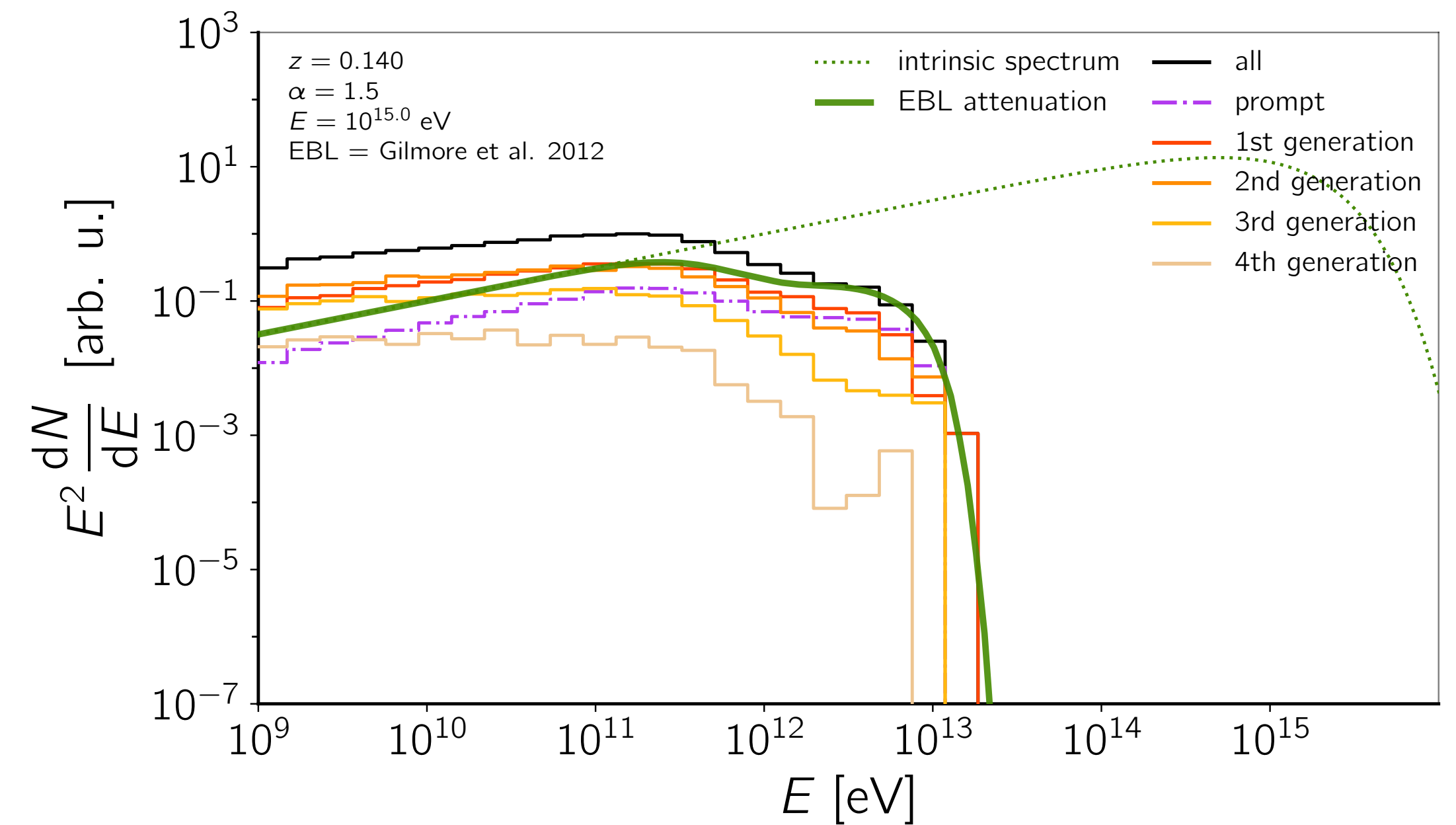
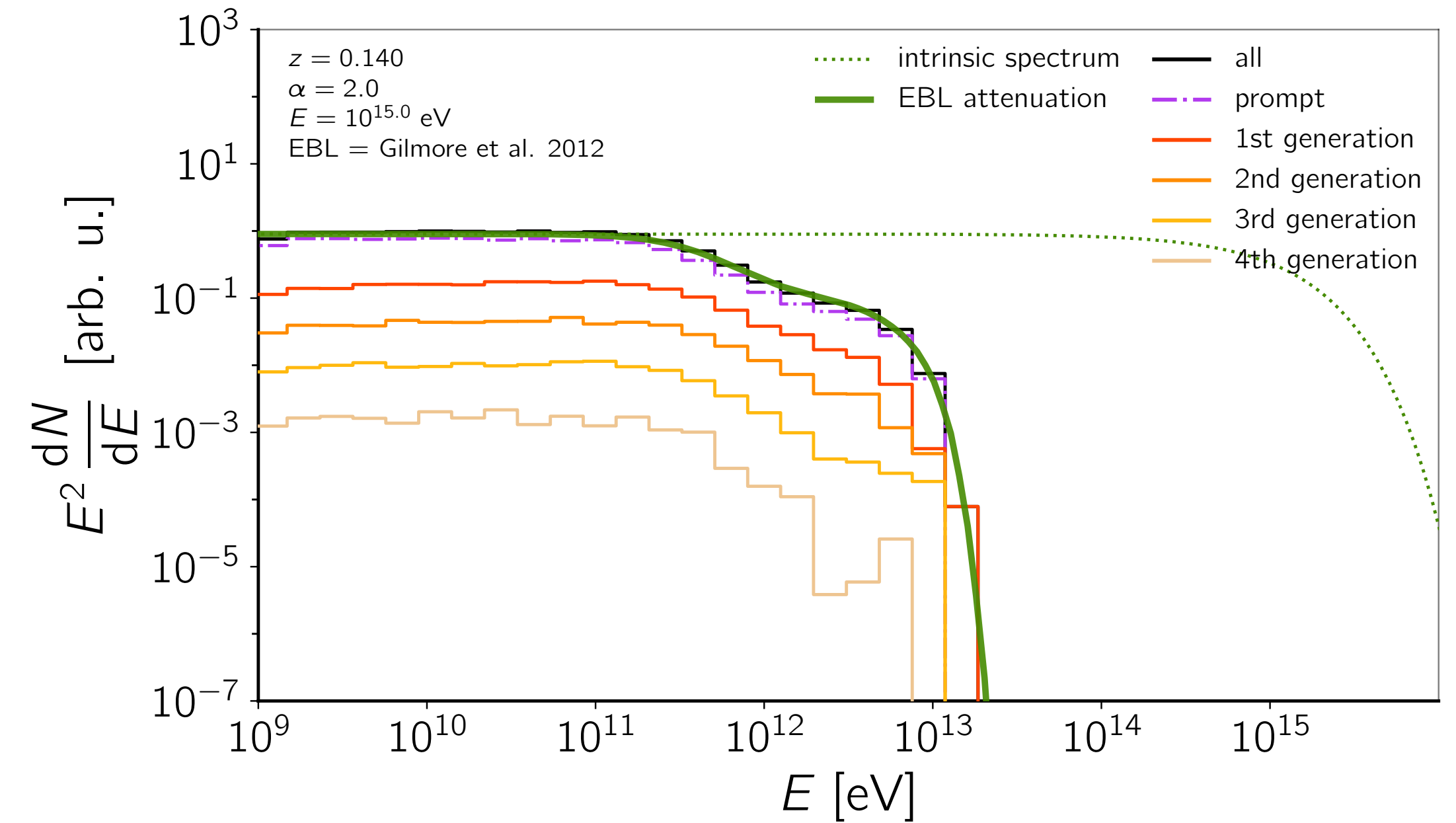
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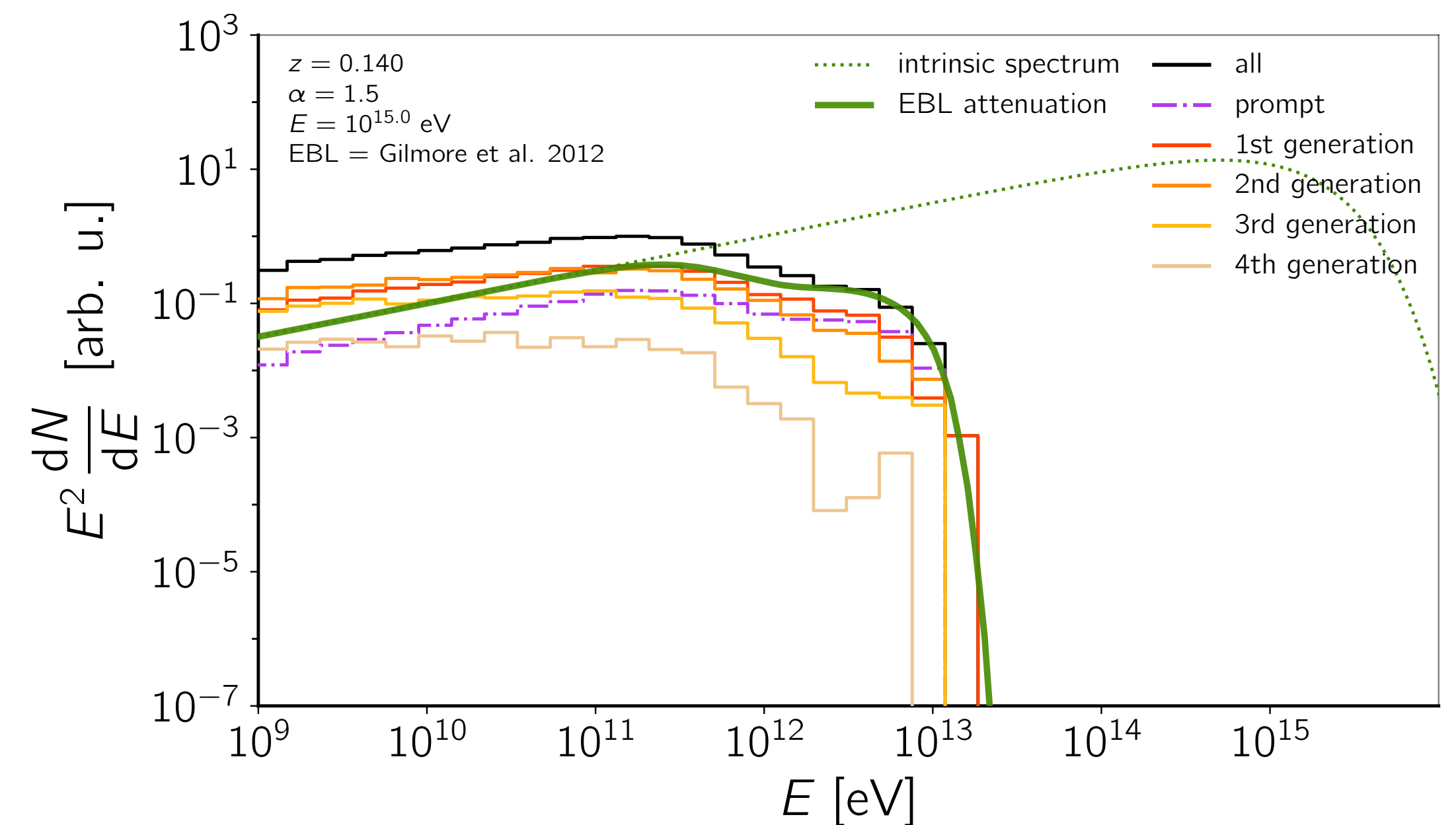
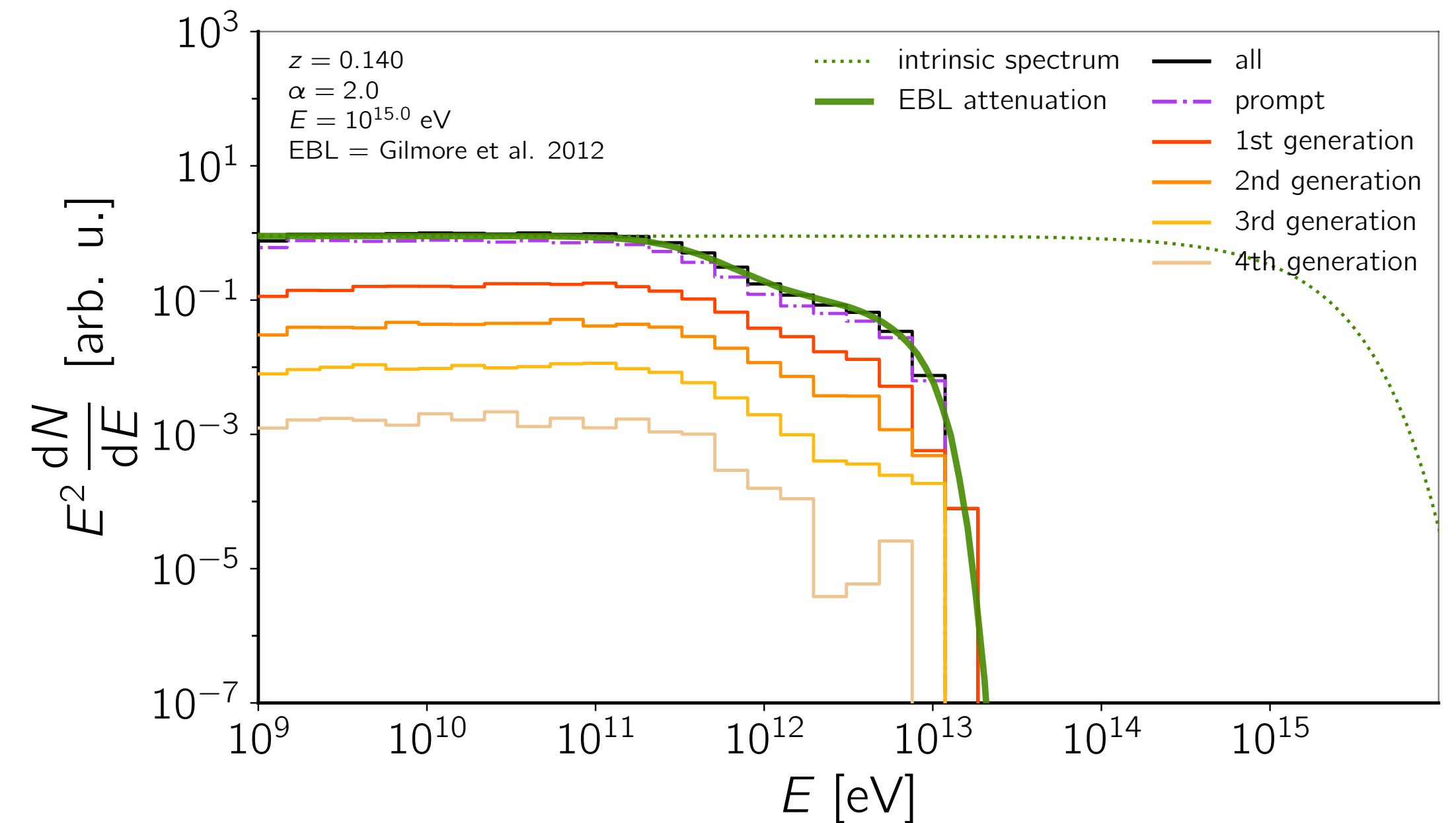
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- ▶ other processes can be important
  - ✦ inverse Compton in this case
- ▶ it is always better to perform full simulations
  - ✦ *but not faster* 😞

simulations performed with **CR/Propa**

Alves Batista et al. JCAP 05 (2016) 038. arXiv:1603.07142

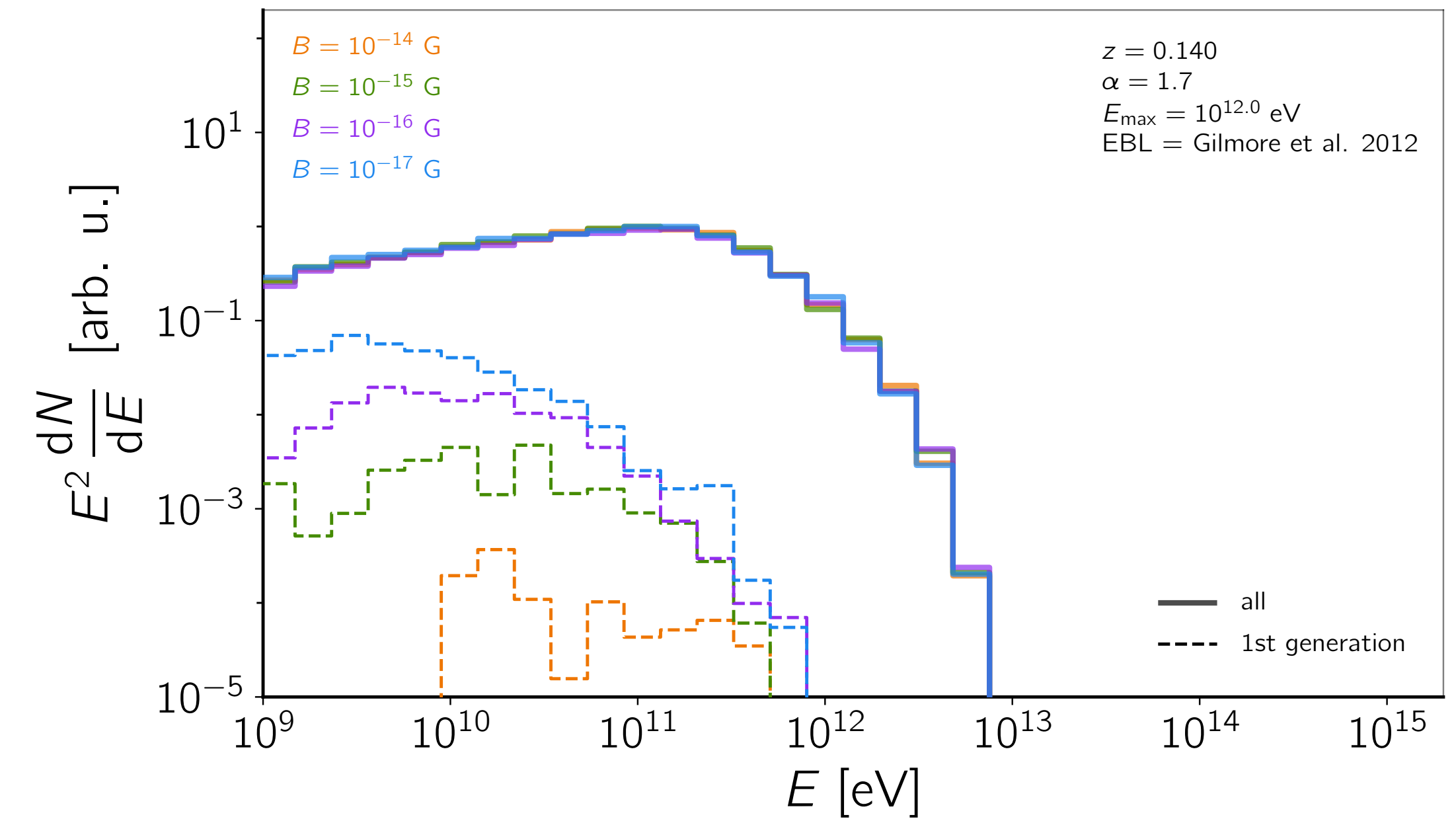
Alves Batista et al. JCAP 09 (2022) 035. arXiv:2208.00107



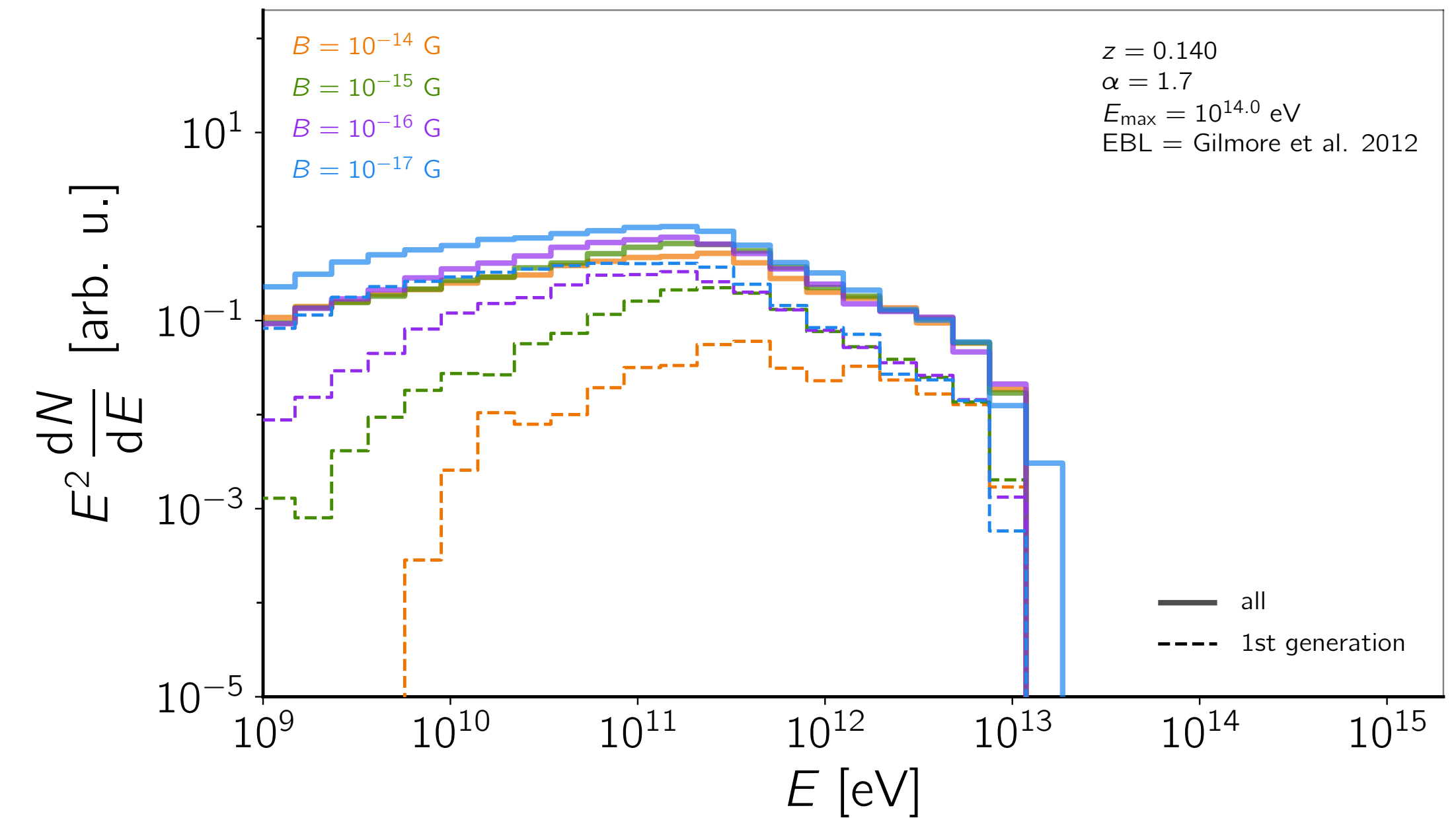
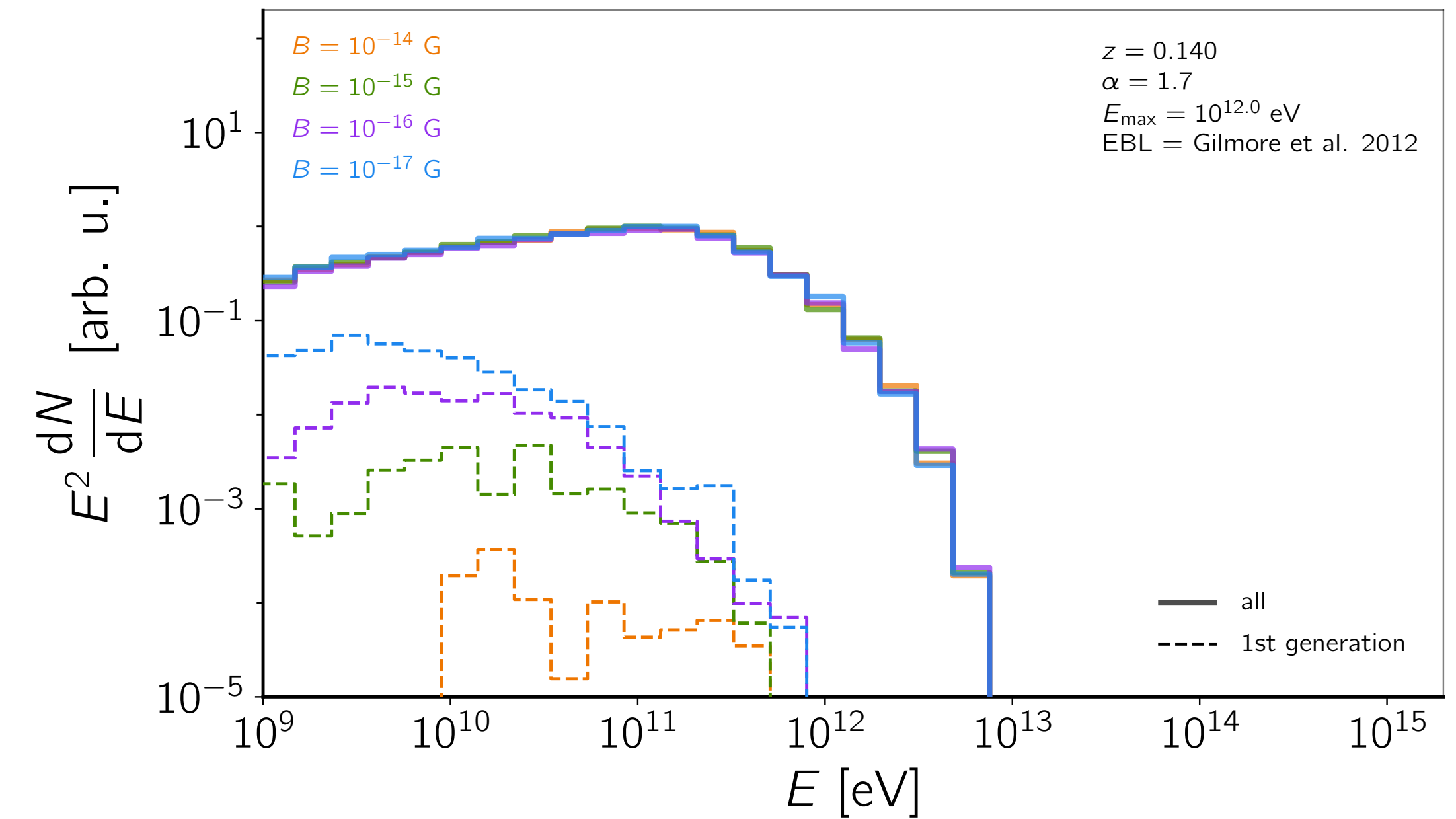
# the usual approach to gamma-ray propagation

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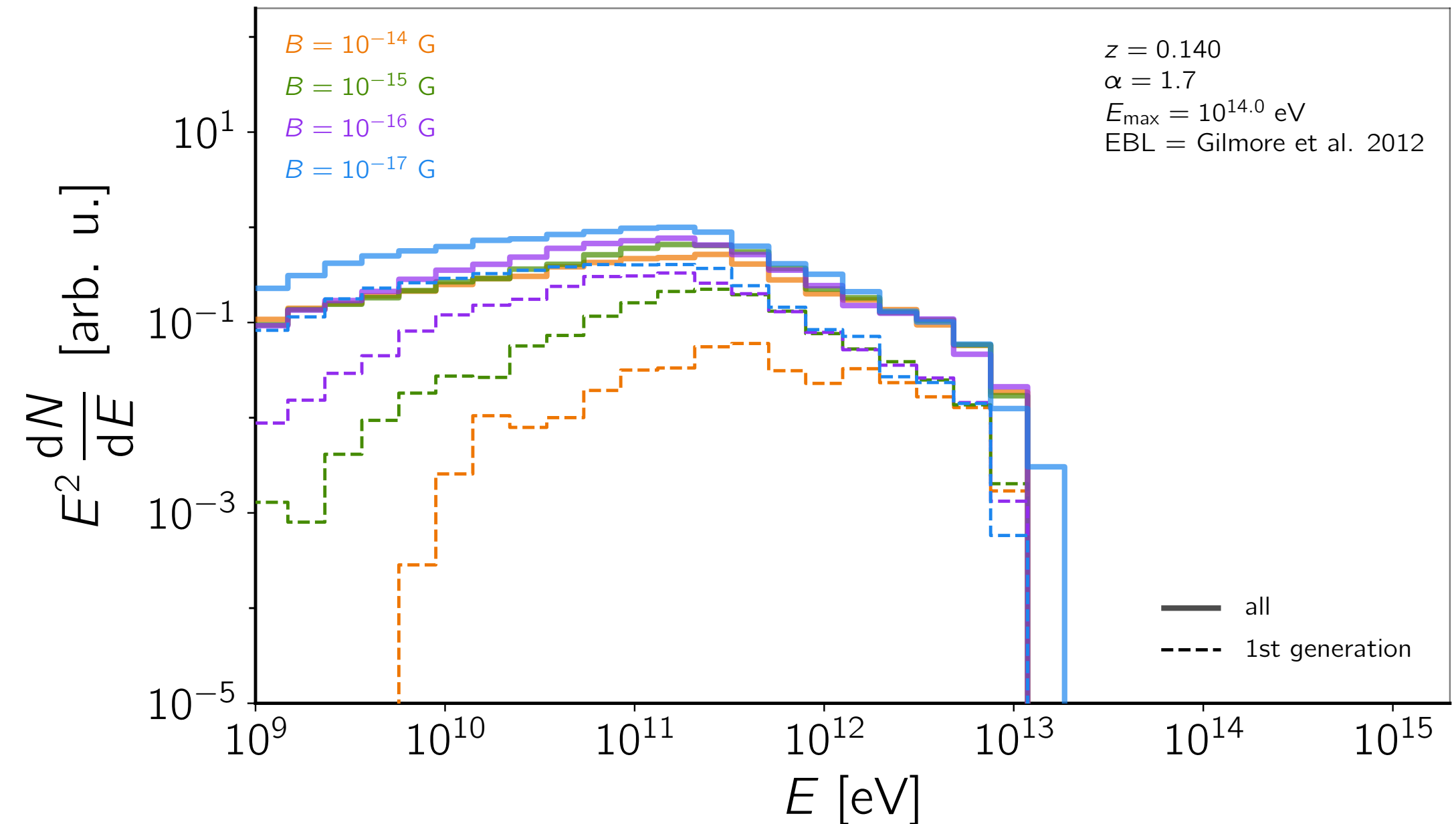
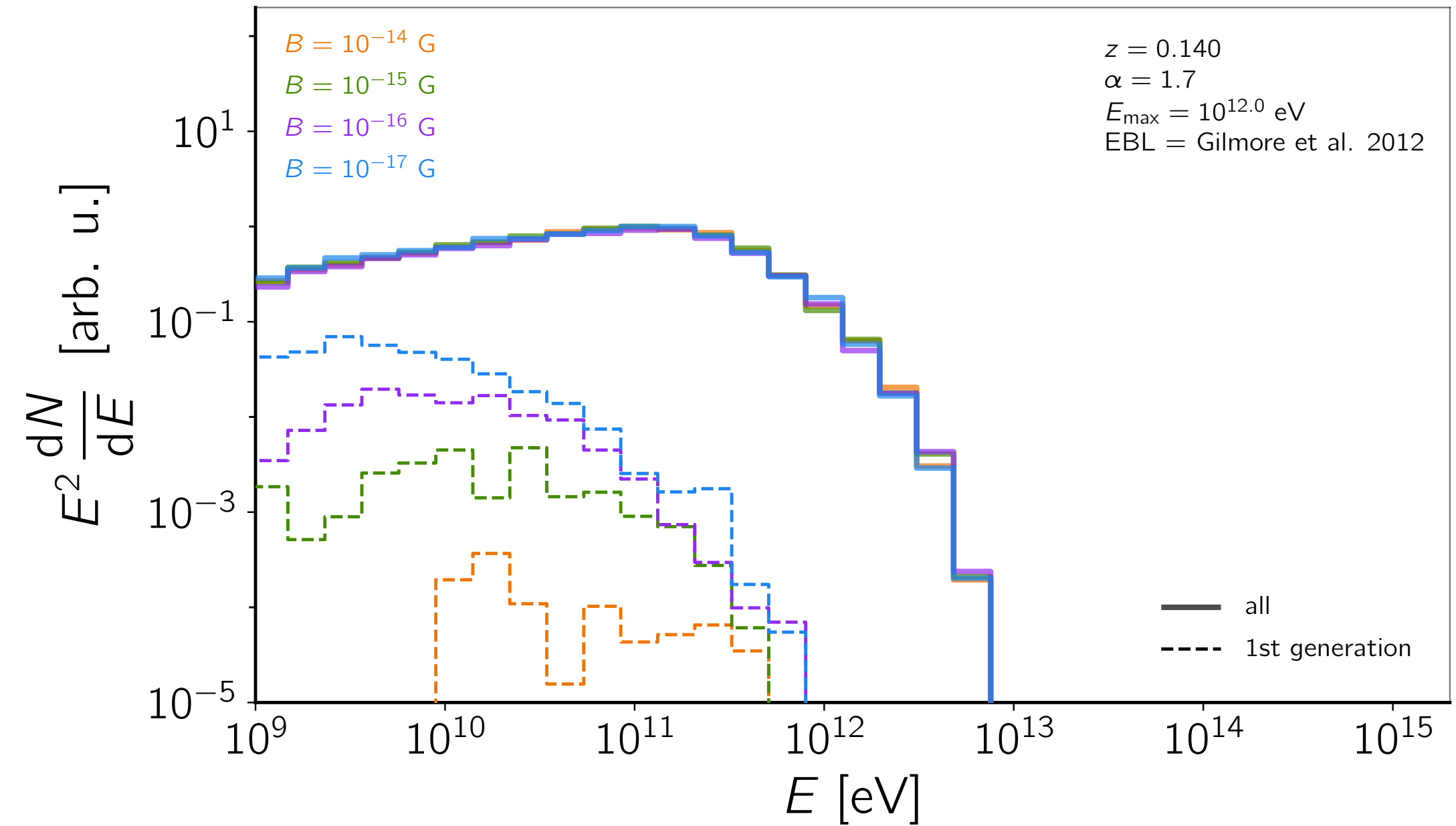
# the usual approach to gamma-ray propagation



# the usual approach to gamma-ray propagation

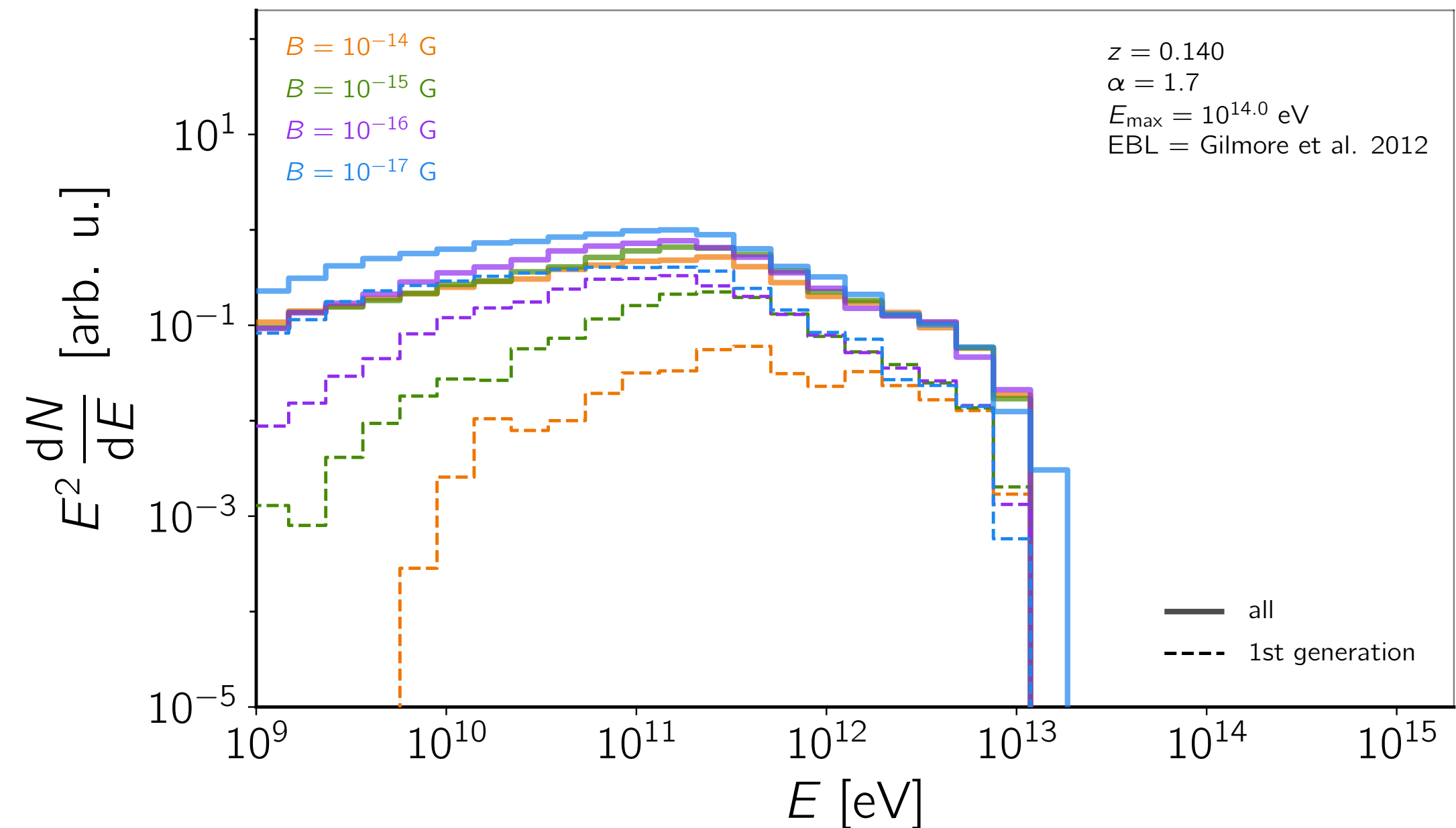
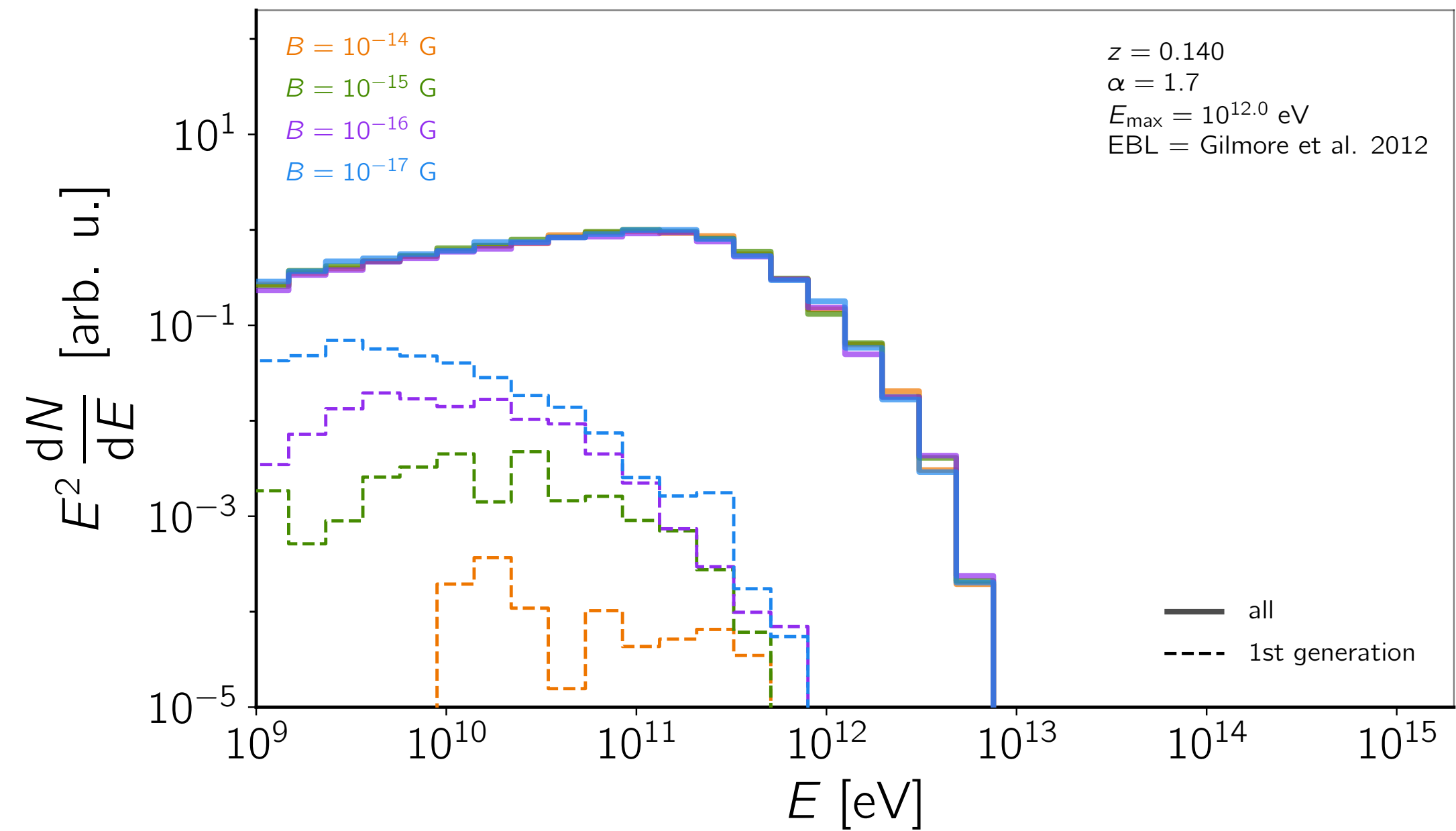


# the usual approach to gamma-ray propagation



$$\Delta t_{\text{obs}} = \Delta t_{\text{QG}} + \mathfrak{Z} + \Delta t_B + \dots$$

# the usual approach to gamma-ray propagation

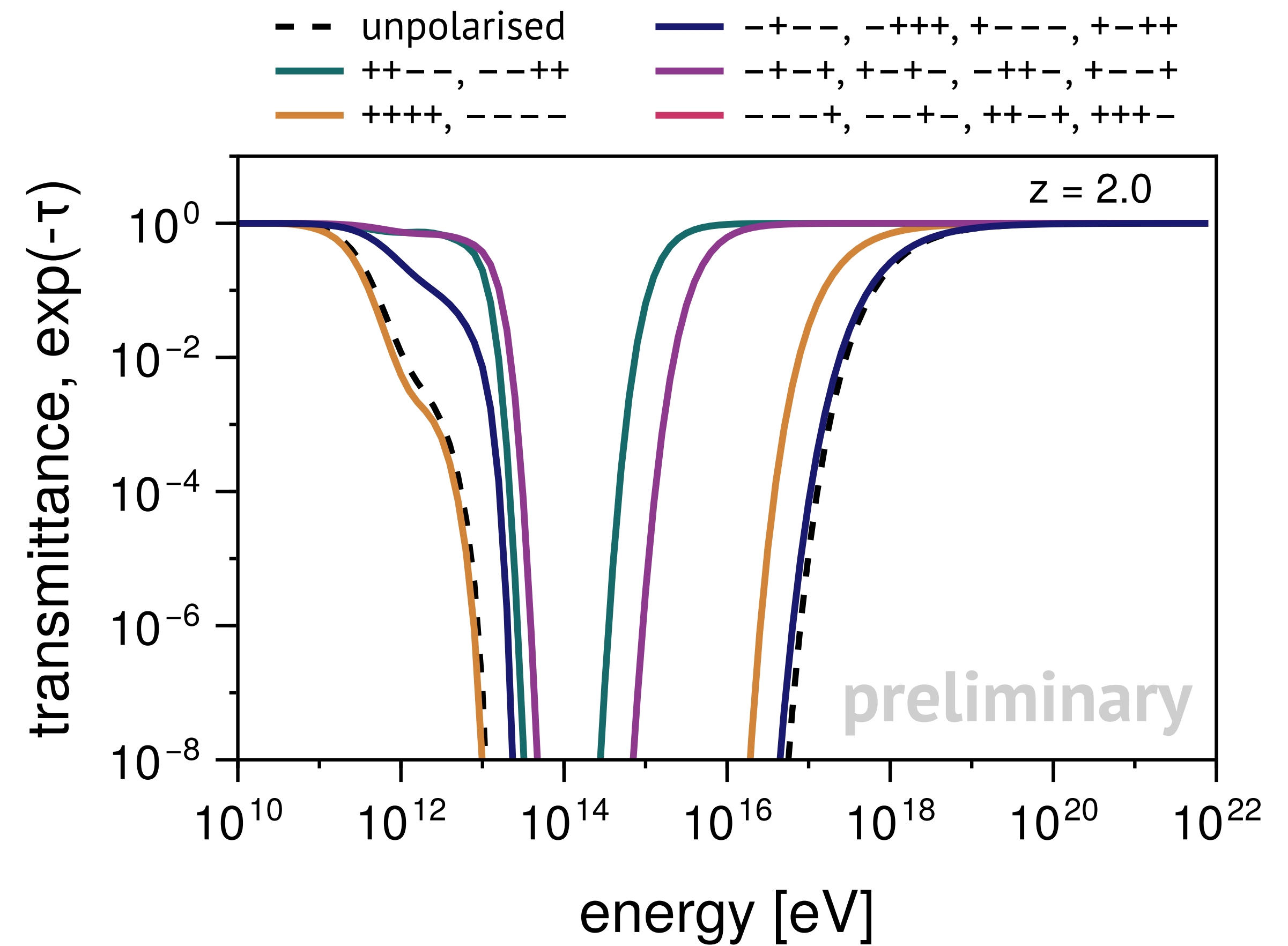
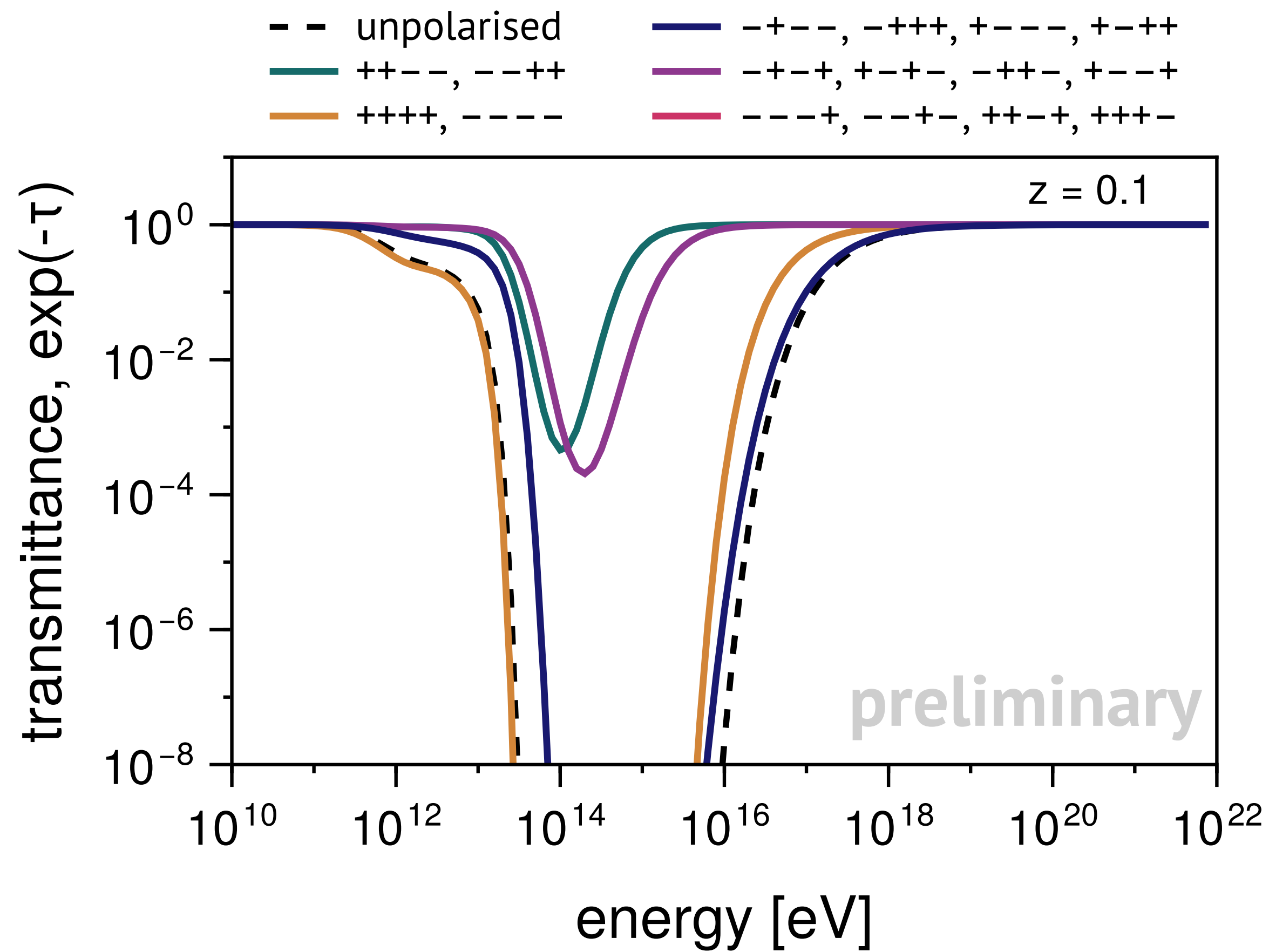


$$\Delta t_{\text{obs}} = \Delta t_{\text{QG}} + \left( \mathfrak{Z} + \Delta t_B \right) + \dots \longrightarrow \Delta t_{\text{src}} + \overset{?}{\Delta t_B} \gg \Delta t_{\text{QG}}$$

difficult to identify QG signatures  
with confidence

# gamma-ray propagation. polarisation-dependent effects

Alves Batista, Cermeño, Mantoni. In preparation.



# complete simulations of **gamma-ray propagation with LIV**

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# complete simulations of **gamma-ray propagation with LIV**

## ► **complete simulations** including LIV

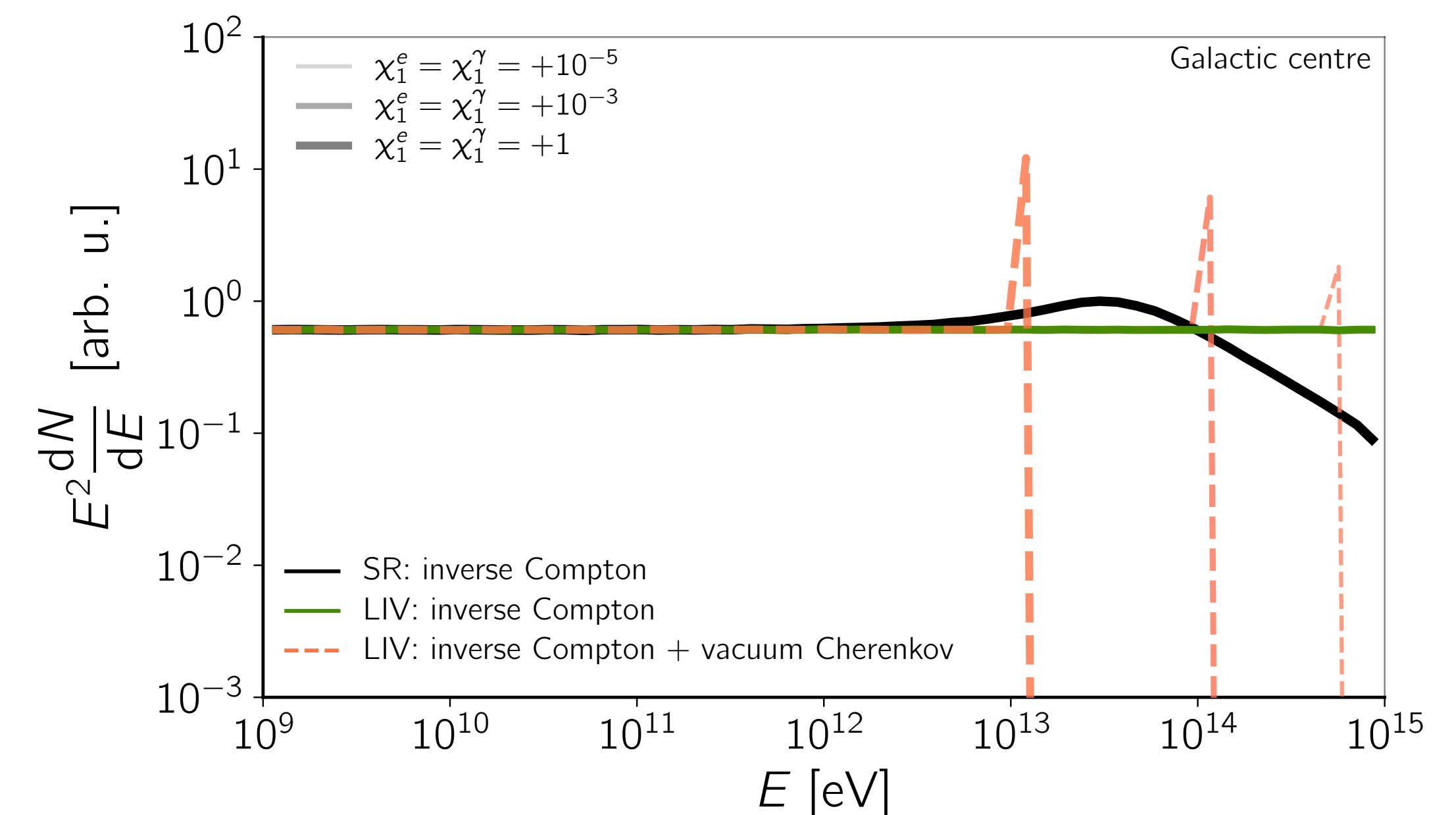
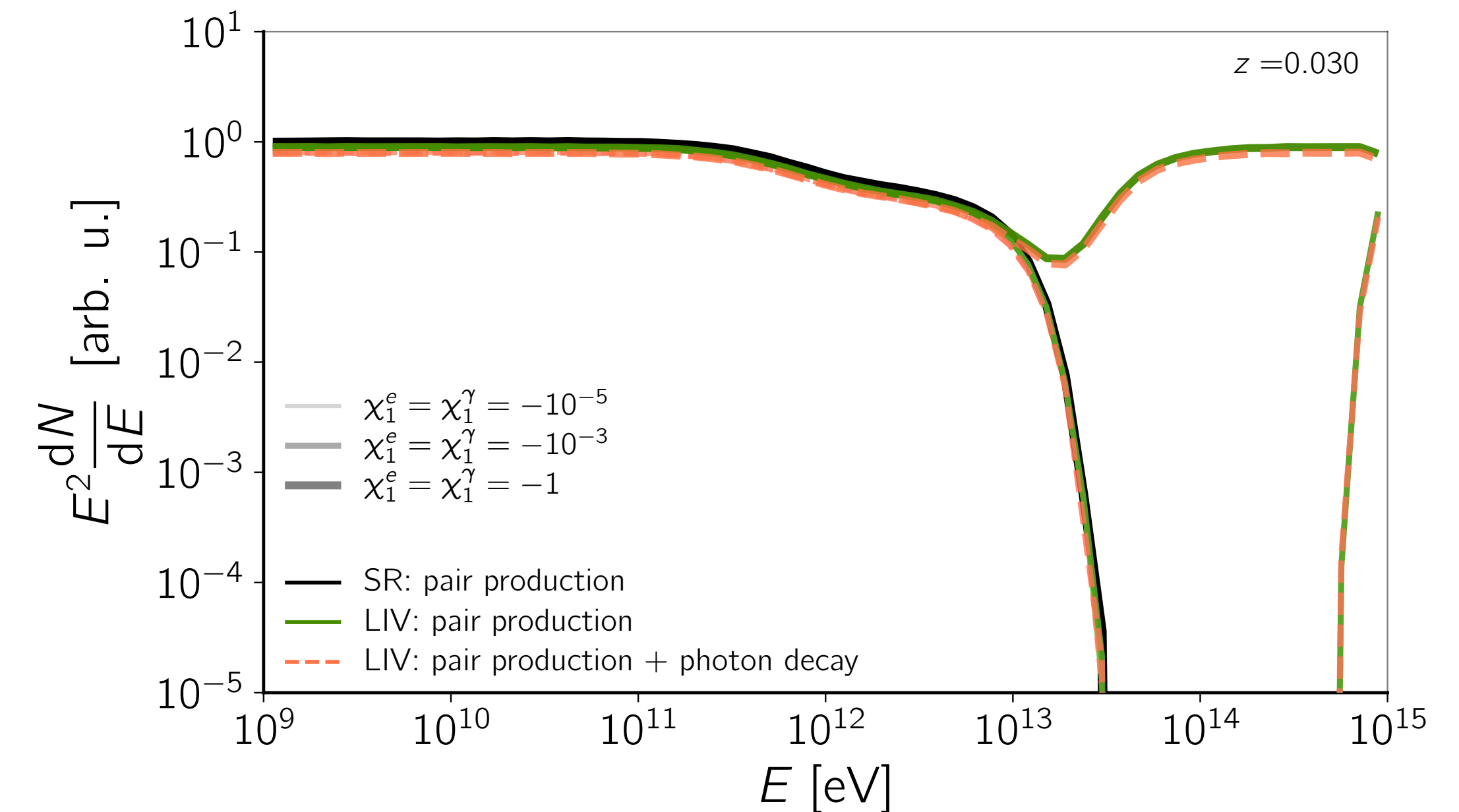
- ✦ modification of pair production
- ✦ including inverse Compton scattering
- ✦ including vacuum Cherenkov
- ✦ including photon decay

# complete simulations of gamma-ray propagation with LIV

Saveliev & Alves Batista. Class. Quant. Grav. 41 (2024) 115011. arXiv:2312.10803

## ► complete simulations including LIV

- ♦ modification of pair production
- ♦ including inverse Compton scattering
- ♦ including vacuum Cherenkov
- ♦ including photon decay

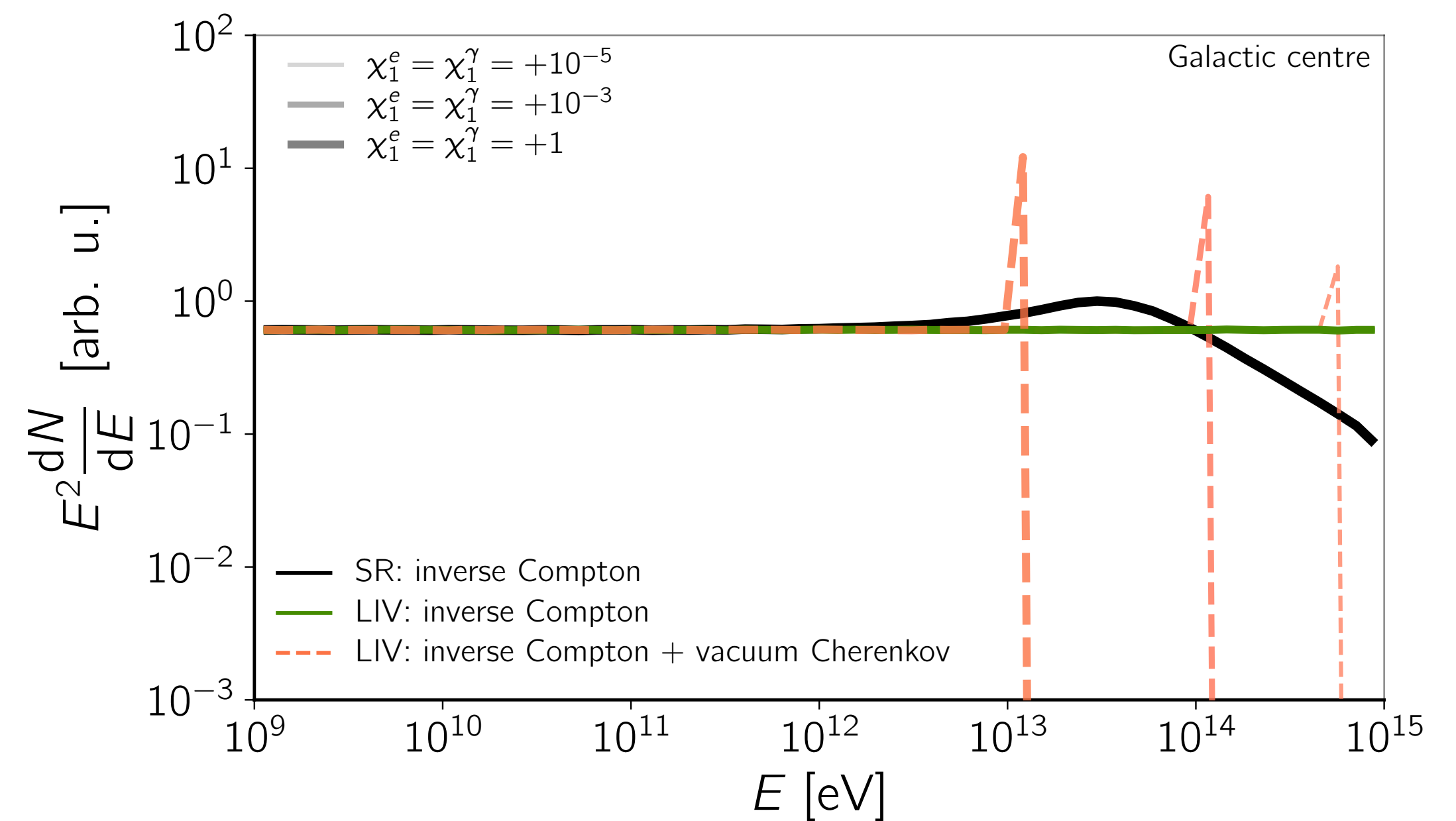
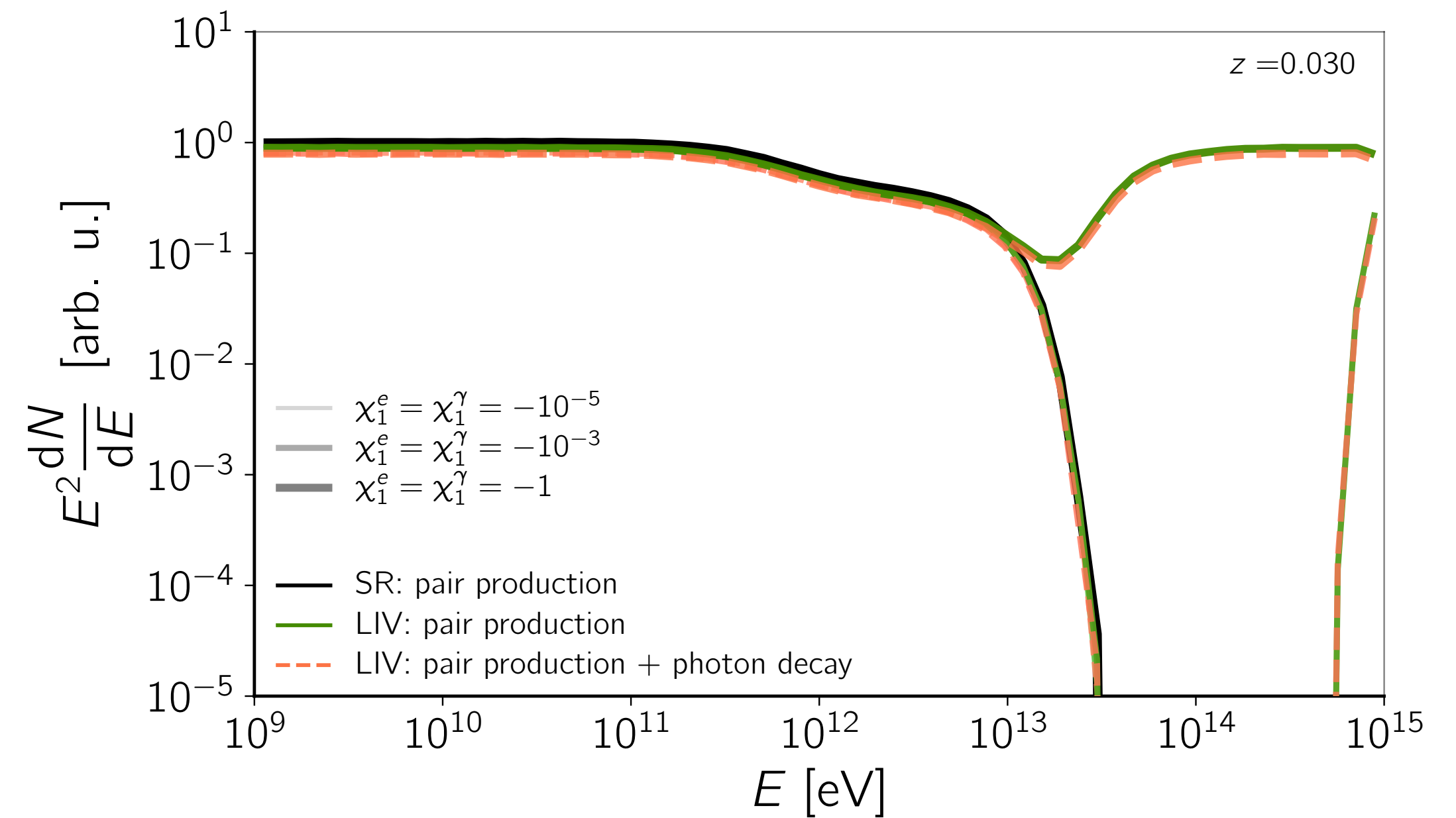
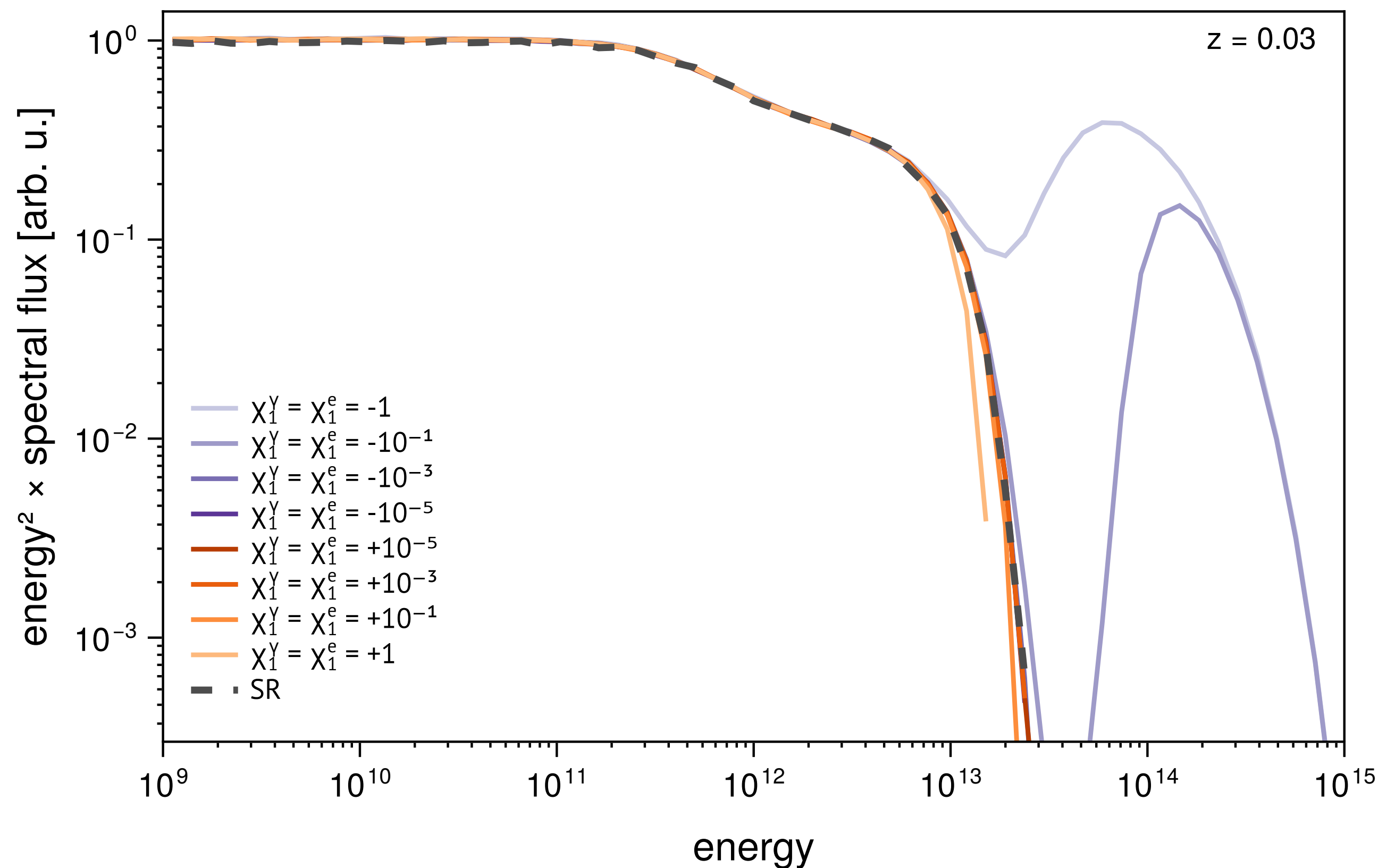


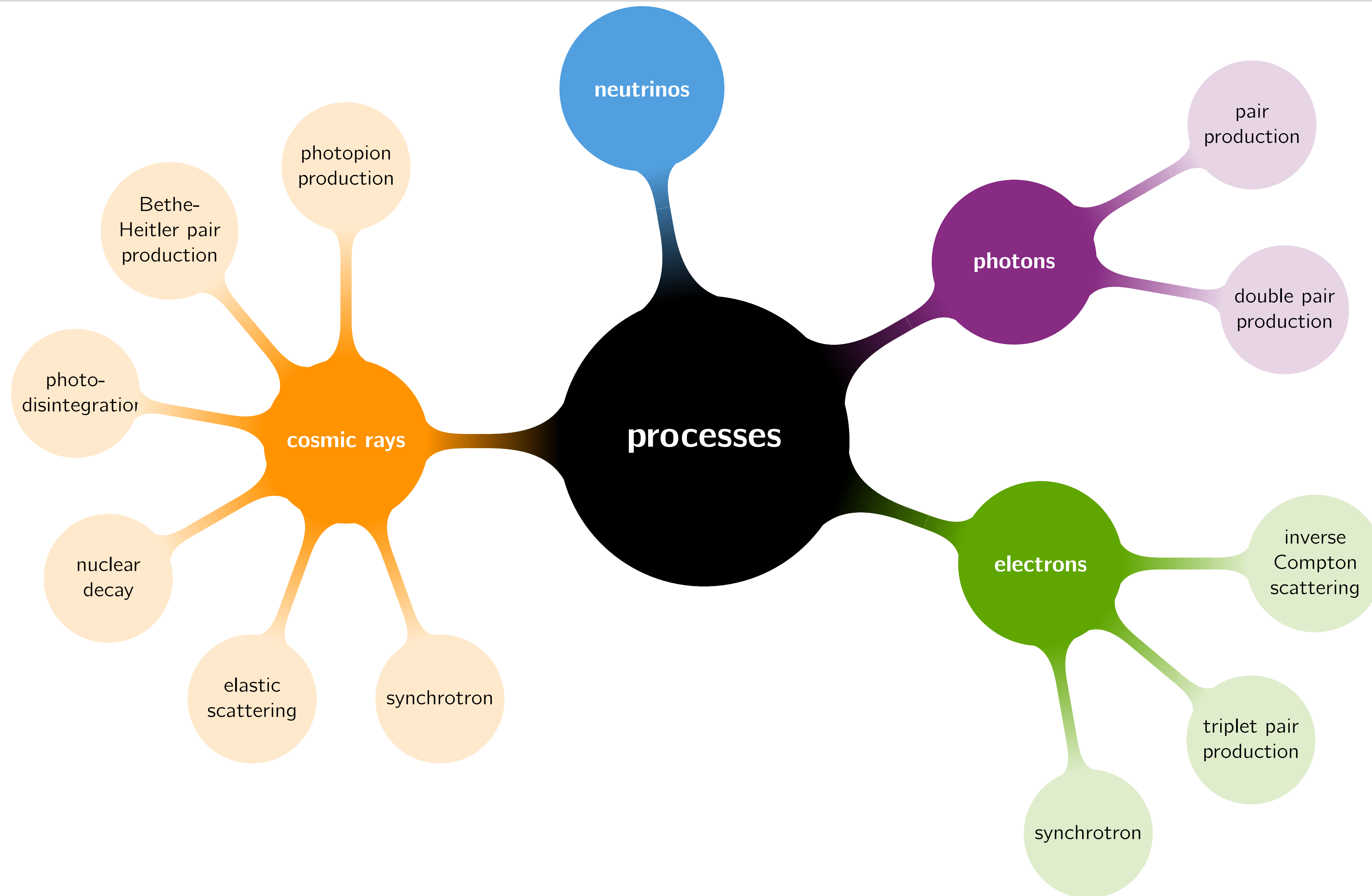
# complete simulations of gamma-ray propagation with LIV

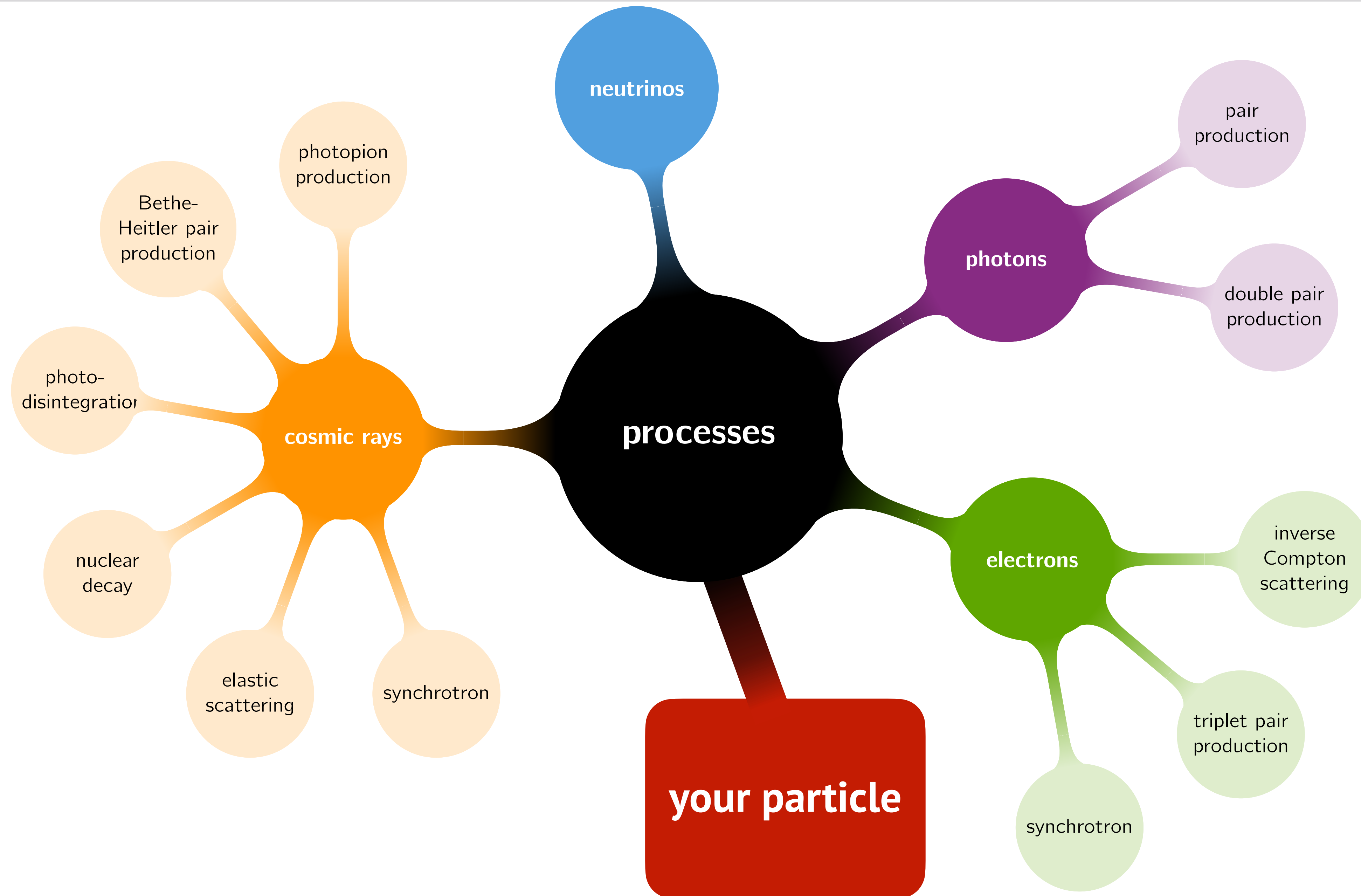
Saveliev & Alves Batista. Class. Quant. Grav. 41 (2024) 115011. arXiv:2312.10803

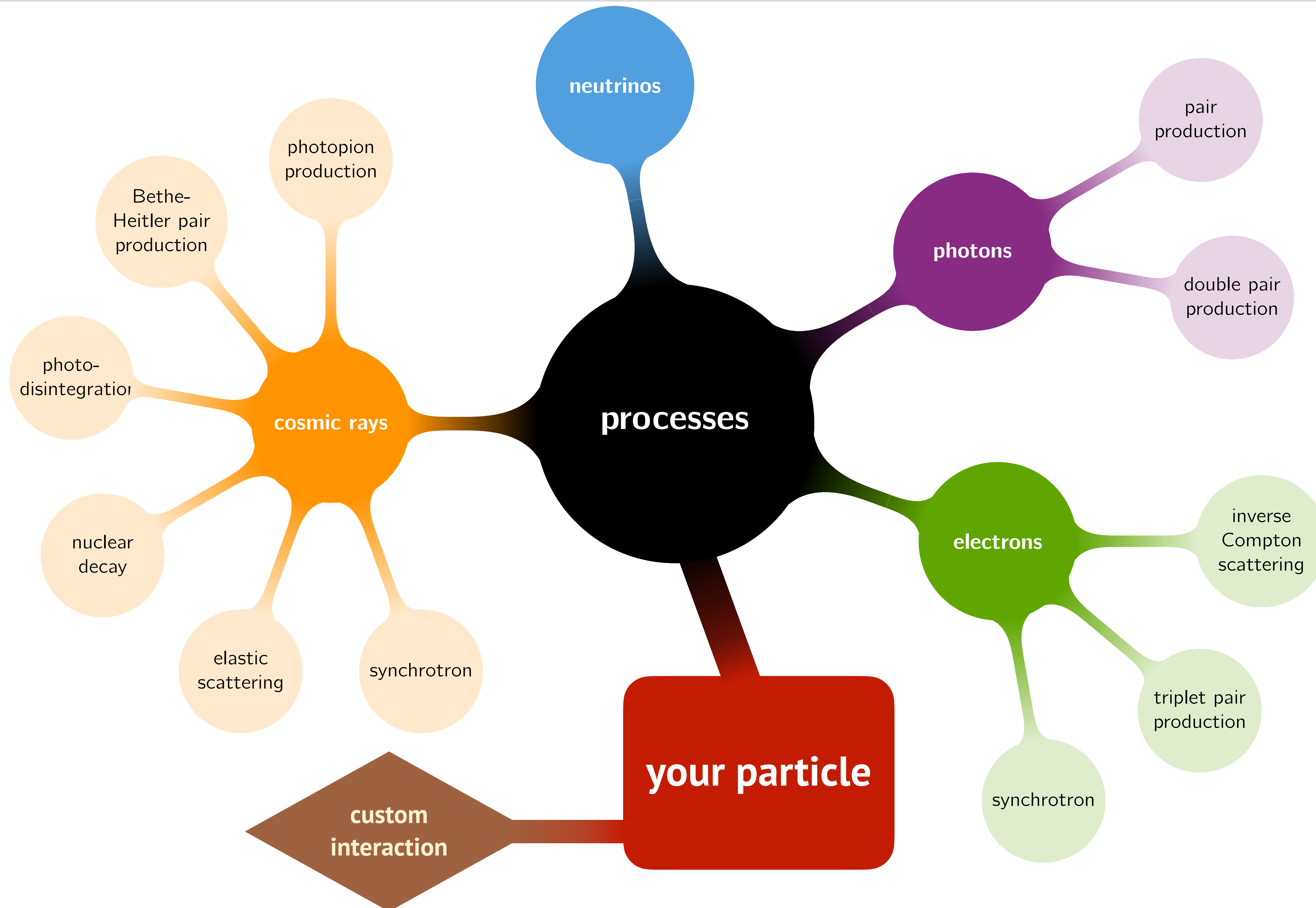
## complete simulations including LIV

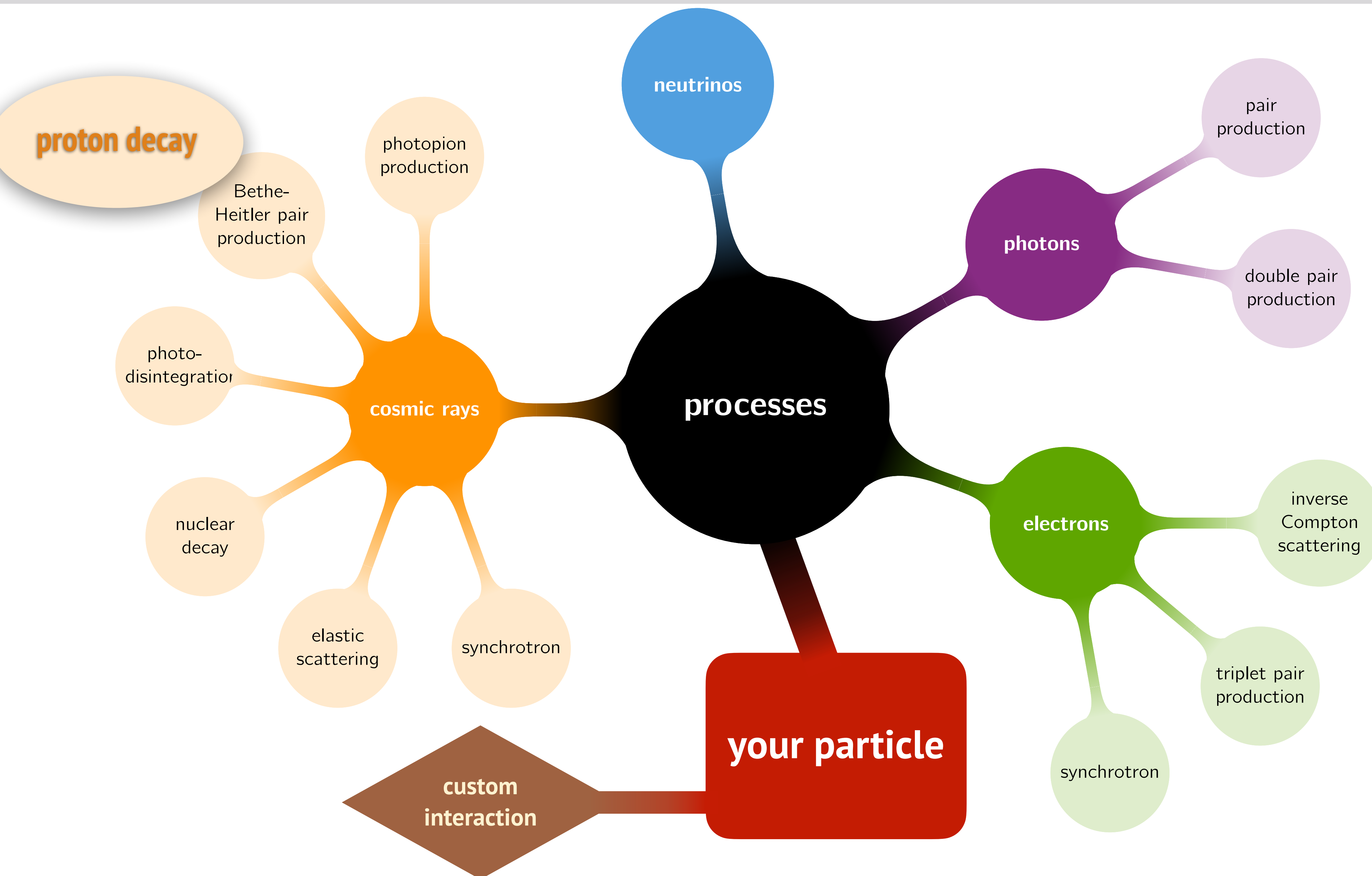
- modification of pair production
- including inverse Compton scattering
- including vacuum Cherenkov
- including photon decay

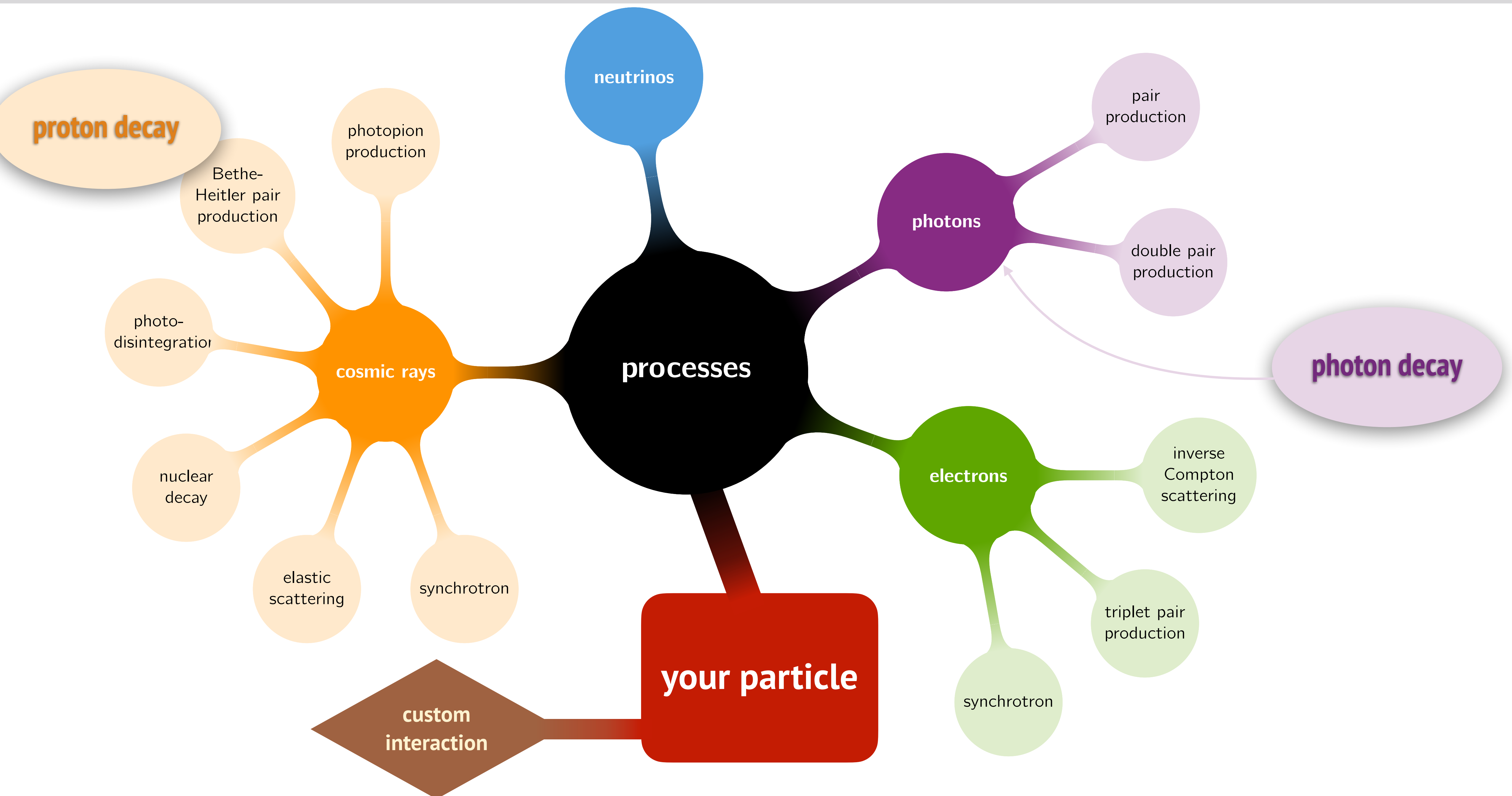


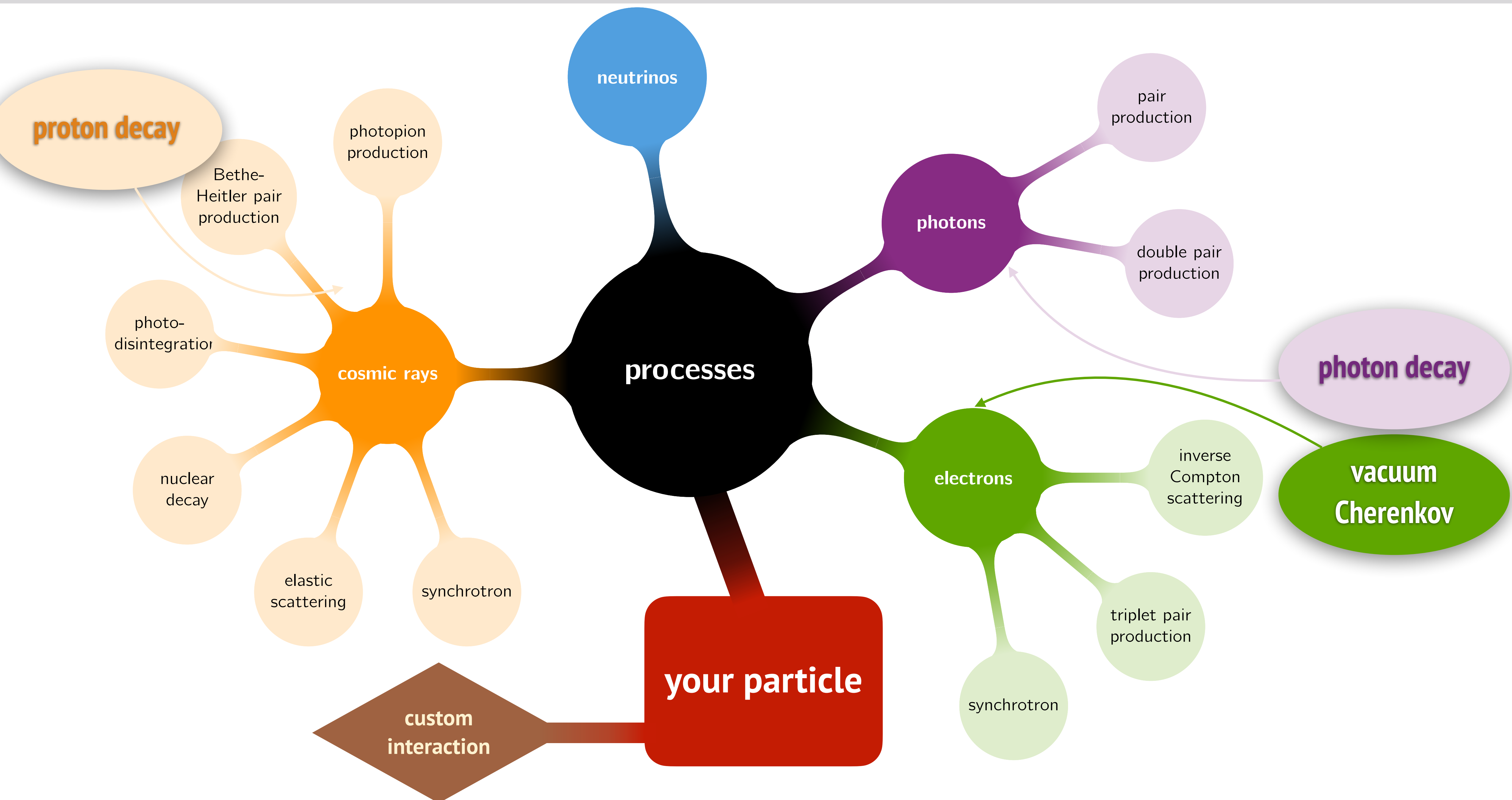












# on time lags

$$\Delta t_{\text{obs}}(E_1, E_2) =$$

$$\Delta t_{\text{obs}}(E_1, E_2) = \Delta t_{\text{acc}}(E_1, E_2)$$

**acceleration**

$$\Delta t_{\text{obs}}(E_1, E_2) = \Delta t_{\text{acc}}(E_1, E_2) + \Delta t_{\text{emi}}(E_1, E_2)$$

**acceleration**      **emission**

$$\Delta t_{\text{obs}}(E_1, E_2) = \Delta t_{\text{acc}}(E_1, E_2) + \Delta t_{\text{emi}}(E_1, E_2) + \Delta t_G(E_1, E_2)$$

**acceleration      emission      gravitational**

$$\Delta t_{\text{obs}}(E_1, E_2) = \Delta t_{\text{acc}}(E_1, E_2) + \Delta t_{\text{emi}}(E_1, E_2) + \Delta t_G(E_1, E_2) + \Delta t_B(E_1, E_2)$$

**acceleration**

**emission**

**gravitational**

**magnetic**

$$\Delta t_{\text{obs}}(E_1, E_2) = \Delta t_{\text{acc}}(E_1, E_2) + \Delta t_{\text{emi}}(E_1, E_2) + \Delta t_G(E_1, E_2) + \Delta t_B(E_1, E_2) + \Delta t_{\text{QG}}(E_1, E_2)$$

**acceleration**

**emission**

**gravitational**

**magnetic**

**QG signal**

$$\Delta t_{\text{obs}}(E_1, E_2) = \Delta t_{\text{acc}}(E_1, E_2) + \Delta t_{\text{emi}}(E_1, E_2) + \Delta t_G(E_1, E_2) + \Delta t_B(E_1, E_2) + \Delta t_{\text{QG}}(E_1, E_2) + \dots$$

**acceleration**

**emission**

**gravitational**

**magnetic**

**QG signal**

$$\Delta t_{\text{obs}}(E_1, E_2) = \Delta t_{\text{acc}}(E_1, E_2) + \Delta t_{\text{emi}}(E_1, E_2) + \Delta t_G(E_1, E_2) + \Delta t_B(E_1, E_2) + \Delta t_{\text{QG}}(E_1, E_2) + \dots$$

**acceleration**

**emission**

**gravitational**

**magnetic**

**QG signal**

$$\Delta t_{\text{obs}}(E_1, E_2) = \Delta t_{\text{acc}}(E_1, E_2) + \Delta t_{\text{emi}}(E_1, E_2) + \Delta t_G(E_1, E_2) + \Delta t_B(E_1, E_2) + \Delta t_{\text{QG}}(E_1, E_2) + \dots$$

acceleration
emission
gravitational
magnetic
QG signal

## charged particles

$$\Delta t_B \approx \begin{cases} q^2 c \frac{B^2 L_{\text{src}}^2 L_B}{18 E^2} = 10^6 \left( \frac{q}{e} \right)^2 \left( \frac{B}{10^{-15} \text{ T}} \right)^2 \left( \frac{E}{100 \text{ EeV}} \right)^{-2} \left( \frac{L_{\text{src}}}{100 \text{ Mpc}} \right)^2 \left( \frac{L_B}{1 \text{ Mpc}} \right) \text{ yr} & \text{if } L_{\text{src}} \gg L_B, \\ q^2 c \frac{B^2 L_{\text{src}}^3}{24 E^2} = 4200 \left( \frac{q}{e} \right)^2 \left( \frac{B}{10^{-15} \text{ T}} \right)^2 \left( \frac{E}{100 \text{ EeV}} \right)^{-2} \left( \frac{L_{\text{src}}}{100 \text{ Mpc}} \right)^3 \text{ yr} & \text{if } L_{\text{src}} \ll L_B. \end{cases}$$

$$\Delta t_{\text{obs}}(E_1, E_2) = \Delta t_{\text{acc}}(E_1, E_2) + \Delta t_{\text{emi}}(E_1, E_2) + \Delta t_G(E_1, E_2) + \Delta t_B(E_1, E_2) + \Delta t_{\text{QG}}(E_1, E_2) + \dots$$

**acceleration**

**emission**

**gravitational**

**magnetic**

**QG signal**

$$\Delta t_{\text{obs}}(E_1, E_2) = \Delta t_{\text{acc}}(E_1, E_2) + \Delta t_{\text{emi}}(E_1, E_2) + \Delta t_G(E_1, E_2) + \Delta t_B(E_1, E_2) + \Delta t_{\text{QG}}(E_1, E_2) + \dots$$

acceleration

emission

gravitational

magnetic

QG signal

**gamma rays** (approximation including cascade effects) [Neronov & Semikoz 2009]

$$\Delta t_B \simeq \begin{cases} 1.0 \times 10^4 \frac{\kappa (1 - \tau_\theta^{-1})}{(1 + z_{\text{src}})^2} \left( \frac{E}{1 \text{ TeV}} \right)^{-2} \left( \frac{B}{10^{-21} \text{ T}} \right)^2 \left( \frac{L_B}{1 \text{ kpc}} \right) \text{ s} & \text{if } \frac{L_B}{1 + z_{\text{src}}} \ll \lambda_{\text{IC}}, \\ 2.2 \times 10^5 \frac{\kappa (1 - \tau_\theta^{-1})}{(1 + z_{\text{src}})^5} \left( \frac{E}{1 \text{ TeV}} \right)^{-\frac{5}{2}} \left( \frac{B}{10^{-21} \text{ T}} \right)^2 \text{ s} & \text{if } \frac{L_B}{1 + z_{\text{src}}} \gg \lambda_{\text{IC}}, \end{cases}$$

$$\Delta t_{\text{obs}}(E_1, E_2) = \Delta t_{\text{acc}}(E_1, E_2) + \Delta t_{\text{emi}}(E_1, E_2) + \Delta t_G(E_1, E_2) + \Delta t_B(E_1, E_2) + \Delta t_{\text{QG}}(E_1, E_2) + \dots$$

acceleration

emission

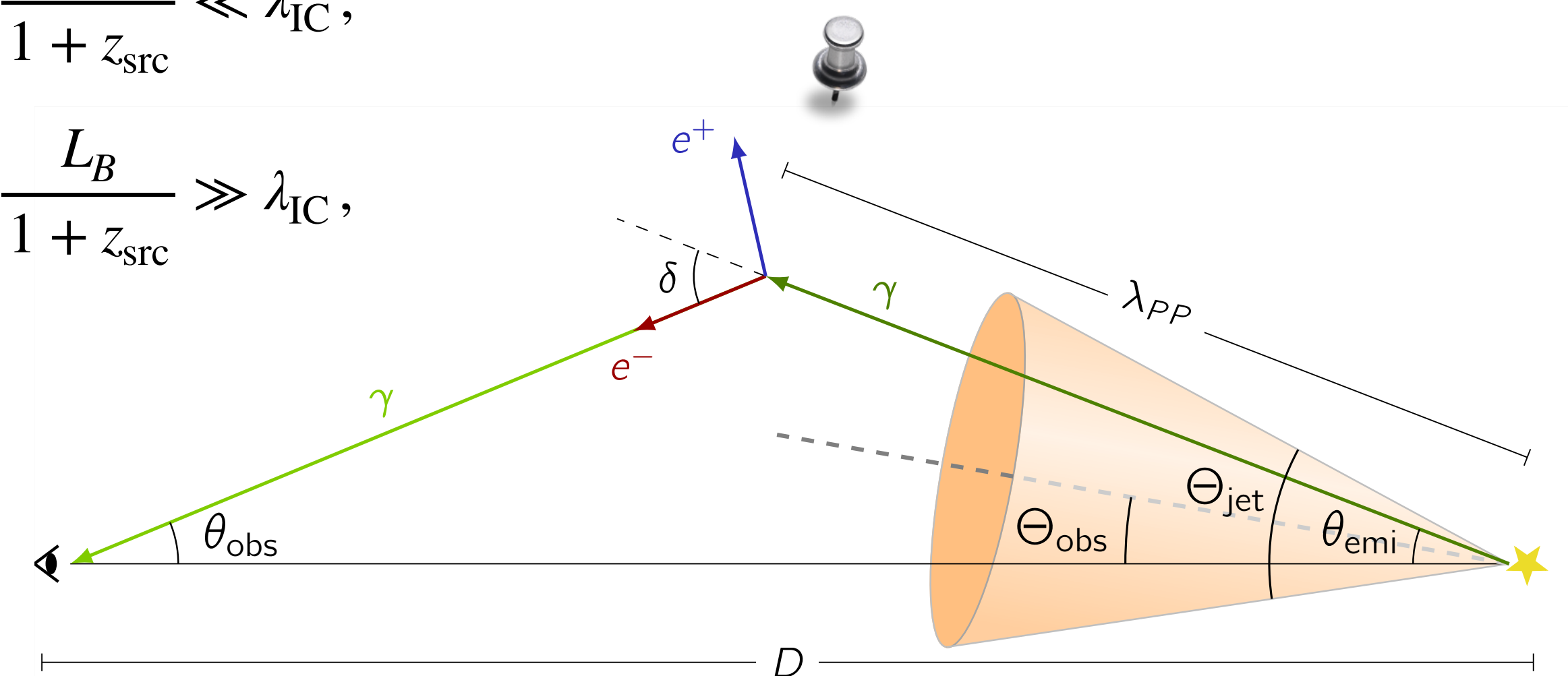
gravitational

magnetic

QG signal

**gamma rays** (approximation including cascade effects) [Neronov & Semikoz 2009]

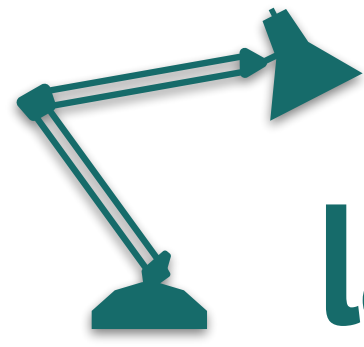
$$\Delta t_B \simeq \begin{cases} 1.0 \times 10^4 \frac{\kappa (1 - \tau_\theta^{-1})}{(1 + z_{\text{src}})^2} \left( \frac{E}{1 \text{ TeV}} \right)^{-2} \left( \frac{B}{10^{-21} \text{ T}} \right)^2 \left( \frac{L_B}{1 \text{ kpc}} \right) \text{ s} & \text{if } \frac{L_B}{1 + z_{\text{src}}} \ll \lambda_{\text{IC}}, \\ 2.2 \times 10^5 \frac{\kappa (1 - \tau_\theta^{-1})}{(1 + z_{\text{src}})^5} \left( \frac{E}{1 \text{ TeV}} \right)^{-\frac{5}{2}} \left( \frac{B}{10^{-21} \text{ T}} \right)^2 \text{ s} & \text{if } \frac{L_B}{1 + z_{\text{src}}} \gg \lambda_{\text{IC}}, \end{cases}$$



Alves Batista & Saveliev. Universe 7 (2021) 223. arXiv:2105.12020

# discussion

# two approaches: lamp and lighthouse



## lamp approach

rigorous focused approach

look at few observables / effects at a time

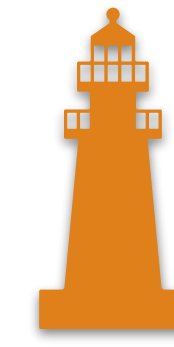
phenomenologically-motivated

excellent for clean signals

empirically adequate

allow for inconsistencies

parsimonious and descriptive



## lighthouse approach

complex brute-force approach

exploits correlations → reduces parameter space

phenomenologically- or theoretically-motivated

weaker but sturdier constraints

empirically adequate

imposes internal consistency

complex and more explanatory



are there **QG** signatures in the data?

are there **QG** signatures in the data?

$$p\left(\theta_{\text{QG}} \mid D\right) \propto p\left(D \mid \theta_{\text{QG}}\right) p\left(\theta_{\text{QG}}\right)$$

are there QG signatures in the data?

$$p(\theta_{\text{QG}} | D) \propto p(D | \theta_{\text{QG}}) p(\theta_{\text{QG}})$$

$$p(D | \theta_{\text{QG}}) = \iiint$$

are there QG signatures in the data?

$$p(\theta_{\text{QG}} | D) \propto p(D | \theta_{\text{QG}}) p(\theta_{\text{QG}})$$

$$p(D | \theta_{\text{QG}}) = \iiint p(D | \theta_{\text{QG}})$$

are there QG signatures in the data?

$$p(\theta_{\text{QG}} | D) \propto p(D | \theta_{\text{QG}}) p(\theta_{\text{QG}})$$

$$p(D | \theta_{\text{QG}}) = \iiint p(D | \theta_{\text{QG}}, \quad )$$

are there QG signatures in the data?

$$p(\theta_{\text{QG}} | D) \propto p(D | \theta_{\text{QG}}) p(\theta_{\text{QG}})$$

$$p(D | \theta_{\text{QG}}) = \iiint p(D | \theta_{\text{QG}}, \theta_{\text{prop}}) \overset{\substack{\text{propagation} \\ \text{uncertainties}}}{p(\theta_{\text{prop}})} d\theta_{\text{prop}}$$

are there QG signatures in the data?

$$p(\theta_{\text{QG}} | D) \propto p(D | \theta_{\text{QG}}) p(\theta_{\text{QG}})$$

$$p(D | \theta_{\text{QG}}) = \iiint p(D | \theta_{\text{QG}}, \theta_{\text{prop}}, \text{propagation uncertainties}) p(\theta_{\text{prop}}) d\theta_{\text{prop}}$$

are there QG signatures in the data?

$$p(\theta_{\text{QG}} | D) \propto p(D | \theta_{\text{QG}}) p(\theta_{\text{QG}})$$

$$p(D | \theta_{\text{QG}}) = \iiint p(D | \theta_{\text{QG}}, \theta_{\text{prop}}, \theta_{\text{src}}) \overset{\text{propagation}}{\underset{\text{uncertainties}}{p(\theta_{\text{prop}})}} \overset{\text{source}}{\underset{\text{uncertainties}}{p(\theta_{\text{src}})}} d\theta_{\text{src}} d\theta_{\text{prop}}$$

are there QG signatures in the data?

$$p(\theta_{\text{QG}} | D) \propto p(D | \theta_{\text{QG}}) p(\theta_{\text{QG}})$$

$$p(D | \theta_{\text{QG}}) = \iiint p(D | \theta_{\text{QG}}, \theta_{\text{prop}}, \theta_{\text{src}}, \overset{\text{propagation}}{\underset{\text{uncertainties}}{\theta_{\text{prop}}}}, \overset{\text{source}}{\underset{\text{uncertainties}}{\theta_{\text{src}}}}) p(\theta_{\text{prop}}) p(\theta_{\text{src}}) d\theta_{\text{src}} d\theta_{\text{prop}}$$

are there QG signatures in the data?

$$p(\theta_{\text{QG}} | D) \propto p(D | \theta_{\text{QG}}) p(\theta_{\text{QG}})$$

$$p(D | \theta_{\text{QG}}) = \iiint p(D | \theta_{\text{QG}}, \theta_{\text{prop}}, \theta_{\text{src}}, \theta_{\text{inst}}) \overset{\text{propagation}}{\underset{\text{uncertainties}}{p(\theta_{\text{prop}})}} \overset{\text{source}}{\underset{\text{uncertainties}}{p(\theta_{\text{src}})}} d\theta_{\text{src}} d\theta_{\text{prop}}$$

are there QG signatures in the data?

$$p(\theta_{\text{QG}} | D) \propto p(D | \theta_{\text{QG}}) p(\theta_{\text{QG}})$$

$$p(D | \theta_{\text{QG}}) = \iiint p(D | \theta_{\text{QG}}, \theta_{\text{prop}}, \theta_{\text{src}}, \theta_{\text{inst}}) \overset{\text{propagation}}{\underset{\text{uncertainties}}{p(\theta_{\text{prop}})}} \overset{\text{source}}{\underset{\text{uncertainties}}{p(\theta_{\text{src}})}} \overset{\text{instrumental}}{\underset{\text{uncertainties}}{p(\theta_{\text{inst}})}} d\theta_{\text{inst}} d\theta_{\text{src}} d\theta_{\text{prop}}$$

- ▶ **sink terms** affecting propagation are considered
- ▶ rarely new **source terms** are considered on top of standard ones (new processes)
- ▶ results are only as good as the models on which they are based
- ▶ problem with lamp strategy: *dutch book argument*
- ▶ combine **multiple messengers**
- ▶ build models covering **larger parameter space**
  - ✦ dimensional reduction from correlations / couplings
- ▶ epistemic goal: coherence over tightness