Theoretical Inputs for Vector-Boson Scattering Measurements at the LHC

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IRN Terascale, Montpellier, France 25th of November 2025



FERMILAB-Pub-77/30-THY March 1977

Weak Interactions at Very High Energies: the Role of the Higgs Boson Mass

BENJAMIN W. LEE, C. QUIGG $^{\circ}$, and H. B. THACKER Fermi National Accelerator Laboratory † , Batavia, Illinois 60510

ABSTRACT

We give an S-matrix theoretic demonstration that if the Higgs boson mass exceeds $\rm M_{\rm c}=(8\pi\sqrt{2}/3G_{\rm F})^{\frac{1}{2}}$ partial-wave unitarity is not respected by the tree diagrams for two-body scattering of gauge bosons, and the weak interactions must become strong at high energies. We exhibit the relation of this bound to the structure of the Higgs-Goldstone Lagrangian, and speculate on the consequences of strongly-coupled Higgs-Goldstone systems. Prospects for the observation of massive Higgs scalars are noted.

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We give an S-matrix theoretic demonstration that if the Higgs boson mass exceeds $\mathrm{M_{C}}=(8\pi\sqrt{Z}/3G_{\mathrm{F}})^{\frac{1}{2}}$ partial-wave unitarity is not respected by the tree diagrams for two-body scattering of gauge bosons, and the weak interactions must become strong at high energies. We exhibit the relation of this bound to the structure of the Higgs-Goldstone Lagrangian, and speculate on the consequences of strongly-coupled Higgs-Goldstone systems. Prospects for the observation of massive Higgs scalars are noted.

Because we wish to explore a regime in which the weak interactions can become strong it is natural to approach the problem from an S-matrix point of view ⁸ with a particular concern for unitarity. ⁹ Our treatment provides a systematic investigation of the minimal Weinberg-Salam theory from this point of view. In Section II we discuss and calculate in tree approximation the Weinberg-Salam model amplitudes for all two-body reactions of gauge bosons with zero total electric charge in the s-channel. We display only those terms that are potentially relevant to the question of unitarity, omitting, for example, terms which are of ordinary electromagnetistrength at all energies. Logarithmic violations of unitarity that occur at exponentially high energies ~ $M_W e^{4/\alpha}$ will be of no concern to us here.

By focusing only on those amplitudes that constitute a potential threat to unitarity one finds a remarkable simplification of the problem. The relevant amplitudes are those which involve only longitudinal gauge bosons and the Higgs boson. The system of these particles is the subject of Section III. There it is shown that at energies large compared with the intermediate boson mass, this system is a clear reflection of the underlying Higgs-Goldstone system of the Weinberg-Salam model, with the longitudinal W^+ , W^- and Z^0 behaving much like the Goldstone bosons from which they sprang. Up to terms of order $M_W^{1/\sqrt{s}}$, the S-matrix for W_L^{\pm} , $Z_{L'}$ and H (the subscript L denotes longitudinal polarization) is identical to that for the self-interactions of a complex doublet of scalar particles, as we show in detail in an Appendix. Consequently exploration

 \rightarrow Probe longitudinal polarisation at high energies ...

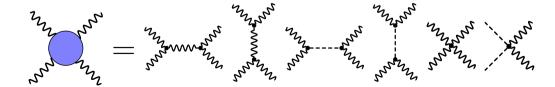
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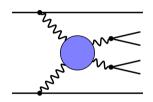
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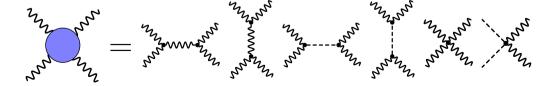
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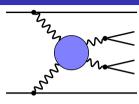
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Vector-boson scattering!



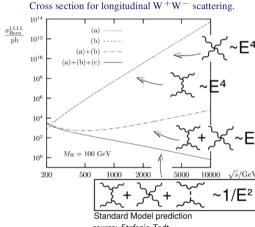


What is VBS and why this is interesting



- Electroweak symmetry breaking
- (longitudinal) Polarisation measurements
- Unitarisation due to Higgs boson
- Measurements of SM parameters
 - → Higgs width
- Triple/quartic gauge coupling
 - \rightarrow EFT

[Denner, Hahn, 1997]



source: Stefanie Todt.

https://indico.cern.ch/event/777988/contributions/3410603/

Precision physics for VBS

Assume scaling of uncertainties with 1/√L

▶ dedicated studies with detector simulation for example in CMS-PAS-SMP-14-008

Integrated Luminosity	36 fb	150 fb	300 fb	3000 fb-
Year	2016	2019	2022	2038
EW(VBS) W±W±	20%	10%	7%	2%
EW (VBS) ZZ	35%	18%	13%	6%
EW (VBS) WZ	35% personally anticipated	18%	13%	6%

source: Jakob Salfeld-Nebgen, https://indico.cern.ch/event/711256

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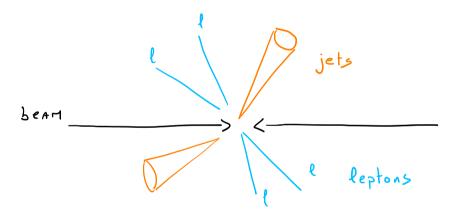
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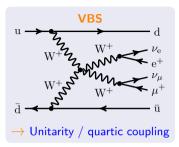
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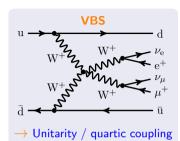
This talk

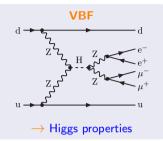
- → Mainly focused on Standard Model physics
 - How to get to per-cent uncertainties from the theory side
 - Importance of interplay between experiment and theory

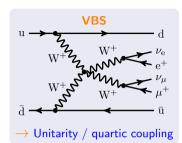
LHC collision producing VBS final state (simplified/theorist's view)

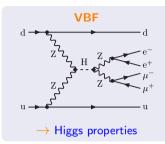


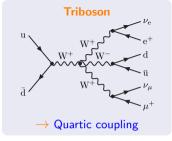


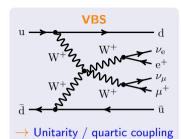


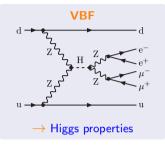


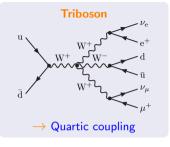


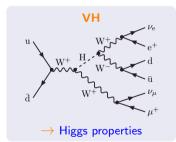


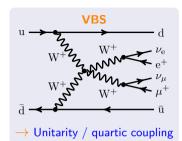


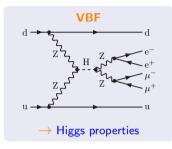


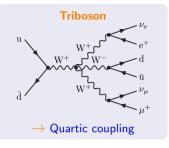


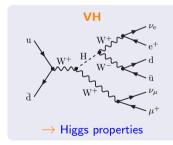


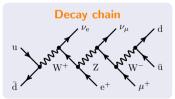


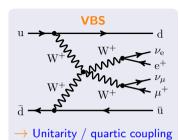


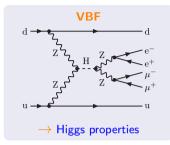


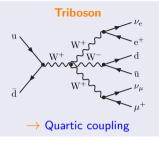


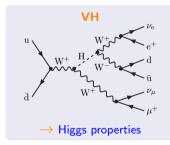


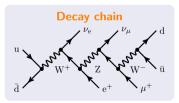


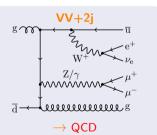


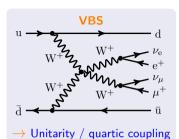


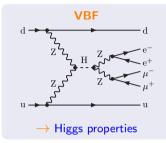


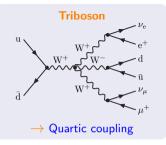


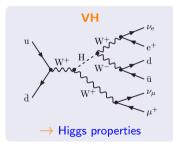


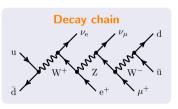


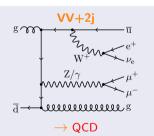








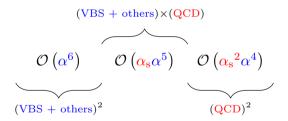




NB: For all contributions, interesting physics and access to gauge-boson polarisation

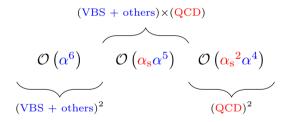
With 2 different amplitudes \rightarrow 3 different contributions:

- $\mathcal{O}(\alpha^6)$: EW contribution/signal
- $\mathcal{O}(\alpha_s \alpha^5)$: Interference
- $\mathcal{O}(\alpha_s^2 \alpha^4)$: QCD contribution/background

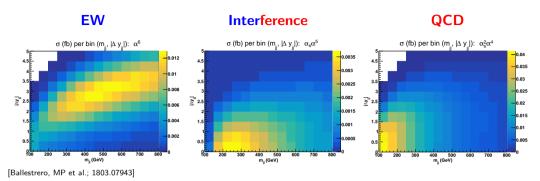


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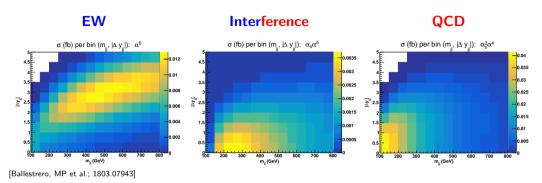
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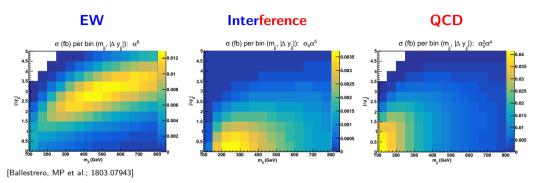
→ How to measure the EW component (including VBS) then?



- The contributions have different kinematics
 - → Back-to-back jets at large rapidity differences + central gauge bosons

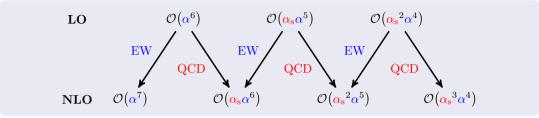


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- → Strategy: Use exclusive cuts and subtract irreducible background (int.+QCD)



- The contributions have different kinematics
 - → Back-to-back jets at large rapidity differences + central gauge bosons
- → Strategy: Use exclusive cuts and subtract irreducible background (int.+QCD)
- ∧ VBS contributions appear also in the interference
- ↑ Theory-dependent measurement

Moving to higher orders in perturbation theory



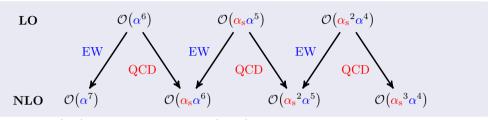
NB: leading order (LO), next to leading order (NLO)

ightarrow Order $\mathcal{O}\left(\alpha_{\rm s}\alpha^6\right)$ and $\mathcal{O}\left(\alpha_{\rm s}^2\alpha^5\right)$: QCD and EW corrections mix

At higher order

Meaningless distinction between EW and QCD component

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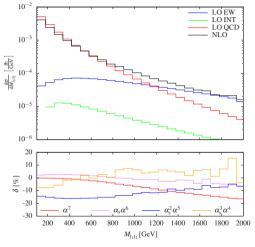
At higher order

Meaningless distinction between EW and QCD component

Solution: Combined measurement of all the contributions

→ clear physical interpretation

→ Example of ZZ channel



[Denner, Franken, MP, Schmidt; 2107.10688]

 Series of articles computing full NLO corrections for all VBS channels:

```
    ssWW: [Biedermann, Denner, MP; 1611.02951, 1708.00268],
    [Chiesa, Denner, Lang, MP; 1906.01863],
    WZ: [Denner, Dittmaier, Maierhöfer, Schwan, MP; 1904.00882],
    ZZ: [Denner, Franken, MP, Schmidt; 2009.00411, 2107.10688],
    W+W-: [Denner, Franken, Schmidt, Schwan; 2202.10844],
```

- Complex structure
 - → Intricate link between higher-order corrections and experimental cuts
- Large EW corrections
 [Biedermann, Denner, MP; 1611.02951]
 - $\rightarrow \sim -15\%$ for total cross section!

Comparison with data

 \rightarrow same-sign WW and WZ analysis of CMS with 137 fb⁻¹ [2005.01173]

Process	$\sigma\mathcal{B}$ (fb) CMS exp.	Theory LO (fb)	Theory NLO (fb)	Theory NLO (%)
EW WW	$3.98 \pm 0.37~\mathrm{stat} \pm 0.25~\mathrm{syst}$	3.93 ± 0.57	3.31 ± 0.47	-15.8
EW+QCD WW	$4.42\pm0.39~\mathrm{stat}\pm0.25~\mathrm{syst}$	$\textbf{4.34} \pm \textbf{0.69}$	3.72 ± 0.59	-14.3
EW WZ	$1.81 \pm 0.39~\mathrm{stat} \pm 0.14~\mathrm{syst}$	1.41 ± 0.21	1.24 ± 0.18	-12.1
EW+QCD WZ	$4.97 \pm 0.40~\mathrm{stat} \pm 0.23~\mathrm{syst}$	$\textbf{4.54} \pm \textbf{0.90}$	$\textbf{4.36} \pm \textbf{0.88}$	-4.0

- → "LO": MadGraph5_AMC@NLO + PYTHIA
- → "NLO": MadGraph5_AMC@NLO + PYTHIA + NLO corr. (non-trivial part):
 - [Biedermann, Denner, MP; 1708.00268]
 - [Denner, Dittmaier, Maierhöfer, MP, Schwan; 1904.00882]
- → Set basis of future precision measurements



- Full measurement vs. Full calculation (EW+QCD)
 - → [Measurement of leptons and jets]



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 Full EW (pb of interference)
 - → [Measurement of EW production]



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- Full measurement undesired (MC) vs. Desired process
 - \rightarrow [Measurement of process X] ...
 - ... extract quantities (mass, coupling, EFT coefficients, polarisation...)



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→ Is it enough?

More physical -Difficult interpretation



- Full measurement vs. Full calculation (EW+QCD)
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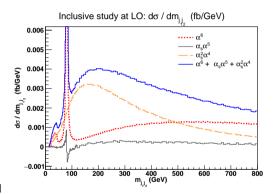
Less physical -Easy interpretation

→ Is it enough?

No... kinematics can also play a crucial role

- Typically cuts $m_{ij} > 500 \,\text{GeV}$
 - → Relaxed for rarest processes
 - $ightarrow m_{
 m jj} > 100\, {
 m GeV}$ (ZZ analysis of [CMS; 1708.02812])

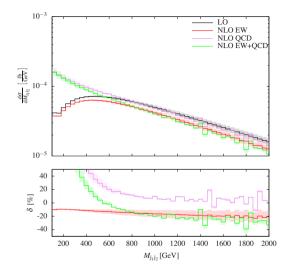
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[Ballestrero, MP et al.; 1803.07943]

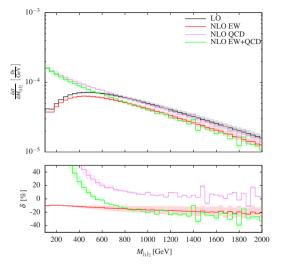
 \wedge EW component = VBS+tri-boson+other contributions

→ Naively, 100 GeV cut should do the job. Is it really the case?

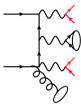


 \rightarrow Example: ZZ VBS at NLO

[Denner, Franken, MP, Schmidt; 2009.00411]



→ Example: ZZ VBS at NLO



 \rightarrow Effects of tri-boson (at NLO) even when using $m_{\rm ii} > 100 \, {\rm GeV}$

[Denner, Franken, MP, Schmidt; 2009.00411]

→ How to ensure that all effects are under control?

→ How to ensure that all effects are under control?

Solution:

- Different definition of the process
 - → With and without QCD component
- Different phase spaces
 - → Sensitive to different effects
- Example:
 - \rightarrow CMS ZZ measurement with 137 fb⁻¹

[2008.07013]

- → Disentangles all physical effects
- → Great for exp./th. comparisons

Particle type	Selection				
ZZjj inclusive					
Leptons	$p_{ m T}(\ell_1) > 20 { m GeV} \ p_{ m T}(\ell_2) > 10 { m GeV} \ p_{ m T}(\ell) > 5 { m GeV}$				
Z and ZZ	$ \eta(\ell) < 2.5$ $60 < m(\ell\ell) < 120 \text{GeV}$ $m(4\ell) > 180 \text{GeV}$				
Jets	at least 2 $p_{\rm T}({\rm j}) > 30{\rm GeV}$ $ \eta({\rm j}) < 4.7$ $m_{\rm jj} > 100{\rm GeV}$ $\Delta R(\ell,{\rm j}) > 0.4$ for each $\ell,{\rm j}$				
VBS-enriched (loose)					
Jets	ZZjj inclusive + $ \Delta \eta_{\rm jj} > 2.4$ $m_{\rm jj} > 400{ m GeV}$				
VBS	enriched (tight)				
Jets	ZZjj inclusive + $ \Delta \eta_{\rm jj} > 2.4$ $m_{\rm jj} > 1{ m TeV}$				

→ Theory status for ss-WW: (more in Review [Covarelli, MP, Zaro; 2102.10991])

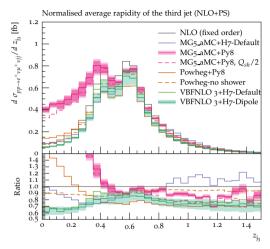
Order	$\mathcal{O}\left(\alpha^{7}\right)$	$\mathcal{O}\left(\alpha_{\mathrm{s}}\alpha^{6}\right)$	$\mathcal{O}\left(\frac{\alpha_s^2\alpha^5}{\alpha}\right)$	$\mathcal{O}\left(\frac{\alpha_{s}^{3}\alpha^{4}}{\alpha}\right)$
NLO	√	√	√	√
NLO+PS	√	√ *	X	√

- $\mathcal{O}\left(\alpha^7\right)$ [Biedermann, Denner, MP; 1611.02951, 1708.00268] \rightarrow +PS: [Chiesa, Denner, Lang, MP; 1906.01863]
- $\mathcal{O}\left(\alpha_{s}\alpha^{6}\right)$ [Biedermann, Denner, MP; 1708.00268], [Jäger, Oleari, Zeppenfeld; 0907.0580],* [Denner, Hošeková, Kallweit; 1209.2389]* \rightarrow +PS: [Jäger, Zanderighi; 1108.0864]*. Also, +1j: [Jäger, Lopez Portillo Chavez; 2408.12314]*
- $\mathcal{O}\left(\alpha_s^2\alpha^5\right)$ [Biedermann, Denner, MP; 1708.00268]
- $\mathcal{O}\left(\alpha_s^3\alpha^4\right)$ [Biedermann, Denner, MP; 1708.00268], [Melia et al.; 1007.5313, 1104.2327], [Campanario et al.; 1311.6738] \rightarrow +PS; [Melia et al.; 1102.4846]. [Melia et al.; 1102.4846]
- (*) Computations in the VBS-approximation *i.e.* t-u interferences and tri-boson contributions neglected
 - ullet Experimental uncertainty \sim few per cent at high-luminosity LHC
 - → We should tick all the boxes by then! NNLO QCD might even be needed...
 - → Effect of non-perturbative physics

[Jäger, Karlberg, Scheller; 1812.05118], [Bittrich, Kirchgaeßer, Papaefstathiou, Plätzer, Todt; 2110.01623]

→ What about parton shower?

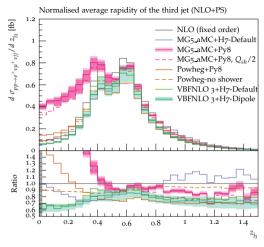
NLO+PS for VBS



[Ballestrero, MP, et al.; 1803.07943]

→ Huge differences, uncovered inconsistent use of Pythia for VBS/VBF topologies

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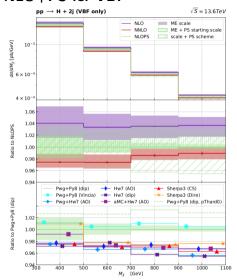
$H \rightarrow WW$

Uncertainty source	$\Delta \mu / \mu$	$\Delta \mu_{\rm ggH} / \mu_{\rm ggH}$	$\Delta \mu_{VBF} / \mu_{VBF}$	$\Delta \mu_{WH} / \mu_{WH}$	$\Delta \mu_{\rm ZH} / \mu_{\rm ZH}$
Theory (signal)	4%	5%	13%	2%	<1%
Theory (background)	3%	3%	2%	4%	5%
Lepton misidentification	2%	2%	9%	15%	4%
Integrated luminosity	2%	2%	2%	2%	3%
b tagging	2%	2%	3%	<1%	2%
Lepton efficiency	3%	4%	2%	1%	4%
Jet energy scale	1%	<1%	2%	<1%	3%
Jet energy resolution	<1%	1%	<1%	<1%	3%
p _T ^{miss} scale	<1%	1%	<1%	2%	2%
PDF	1%	2%	<1%	<1%	2%
Parton shower	<1%	2%	<1%	1%	1%
Backg. norm.	3%	4%	6%	4%	6%
Stat. uncertainty	5%	6%	28%	21%	31%
Syst. uncertainty	9%	10%	23%	19%	11%
Total uncertainty	10%	11%	36%	29%	33%

[CMS; 2206.09466]

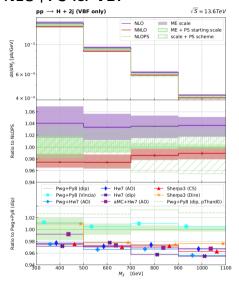
ightarrow Still > 10% error on parton-shower uncertainty

NLO+PS for VBF



[Barone, MP, et al.; 2507.22574]

NLO+PS for VBF



[Barone, MP, et al.: 2507,22574]

→ Work in between:

[Jäger, Karlberg, Plätzer, Scheller, Zaro; 2003.12435], [Buckley et al.; 2105.11399], [Höche, Mrenna, Payne, Preuss, Skands: 2106.10987]

- → [Barone, MP, et al.; **2507**.22574]:
 - Part of the Higgs Cross section WG Yellow Report 5
 - State-of the art predictions at fixed order + Parton-shower study
 - Recommendations for parton-shower uncertainty (usable also for VBS):

Based on these observations, we propose the following recommendation for a more robust estimation of NLOPS uncertainty, which comprises both the matching and the shower variations 1. Generate (at least) three predictions: - one with Powurg-Rox and any Pictura 8 shower - one with any HERWIG 7 shower: 12 = one with any SHERPA 3 shower Make sure that at least one of these prediction is based on POWHEG matching, and one on MC@NLO matching.13 Then, construct an envelope14 out of these predic-2. For one of the curves computed in sten 1: = compute a shower starting scale variation band (or a nThand variation in the context of DOWNEG-BOY ADVENTA & matching): - compute the renormalisation and factorisation scale variation band, possibly including also scale variations in the shower. Sum these bands in quadrature and combine this uncertainty in quadrature with the first envelope uncertainty

FERMILAB-Pub-77/30-THY March 1977

Weak Interactions at Very High Energies: the Role of the Higgs Boson Mass

BENJAMIN W. LEE, C. QUIGG[®], and H. B. THACKER Fermi National Accelerator Laboratory[†], Batavia, Illinois 60510

ABSTRACT

We give an S-matrix theoretic demonstration that if the Higgs boson mass exceeds $\mathrm{M_{\odot}} = (8\pi\sqrt{2}/3\mathrm{G_p})^{\frac{1}{2}}$ partial-wave unitarity is not respected by the tree diagrams for two-body scattering of gauge bosons, and the weak interactions must become strong at high energies. We exhibit the relation of this bound to the structure of the Higgs-Goldstone Lagrangian, and speculate on the consequences of strongly-coupled Higgs-Goldstone systems. Prospects for the observation of massive Higgs scalars are noted.

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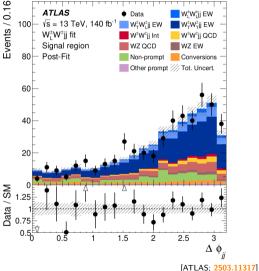
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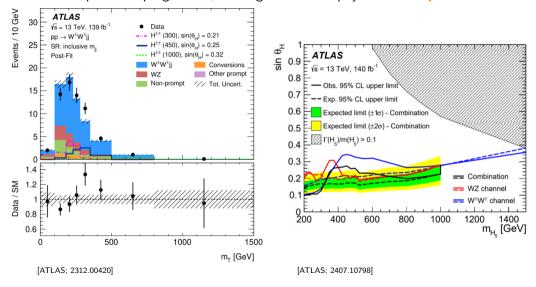
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We give an S-matrix theoretic demonstration that if the Higgs boson mass exceeds $M_o = (8\pi \sqrt{2}/3G_{pp})^{\frac{1}{2}}$ partial-wave unitarity is not respected by the tree diagrams for two-body scattering of gauge bosons, and the weak interactions must become strong at high energies. We exhibit the relation of this bound to the structure of the Higgs-Goldstone Lagrangian, and speculate on the consequences of strongly-coupled Higgs-Goldstone systems. Prospects for the observation of massive Higgs scalars are noted.

After almost 50 years, exciting time!



→ With this precision programme, we might find new physics! Example of H⁺⁺



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 - Better theory predictions
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"High-luminosity LHC vicious circle"



[source: bing image creator]

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 - → Make interpretation difficult
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- Challenges at High Luminosity:
 - Better measurements
 - Better theory predictions
 - More complex interpretation
- One way out:

Different meas. in different fiducial regions!

→ STXS for multiboson - activity in LHC EW WG https://indico.cern.ch/event/1593081

"High-luminosity LHC vicious circle"



[source: bing image creator]

Outlook

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- → Explore fundamental aspect of particle physics
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A bit of propaganda Final word:



Back-up slides

BACK-UP

Polarisation studies

Experiment:

- → Measurements in ss-WW
 - O [CMS; 2009.09429]
 - [ATLAS; 2503.11317]
 - → Compared to [Hoppe, Schönherr, Siegert; 2310.14803]
 - + [Denner, Haitz, Pelliccioli; 2409.03620]

Theory:

- [Denner, Haitz, Pelliccioli; 2409.03620]
 - → NLO QCD+EW for ss-WW
- [Hoppe, Schönherr, Siegert; 2310.14803]
 - \rightarrow Approximate NLO QCD+PS in SHERPA
- [Carrivale et al.; 2505.09686] (for diboson)
 - \rightarrow Benchmarking exercise + description of tools + references

