

Towards a few-% measurement of H_0 with the current network of GW detectors, without EM information

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GdR Ondes gravitationnelles
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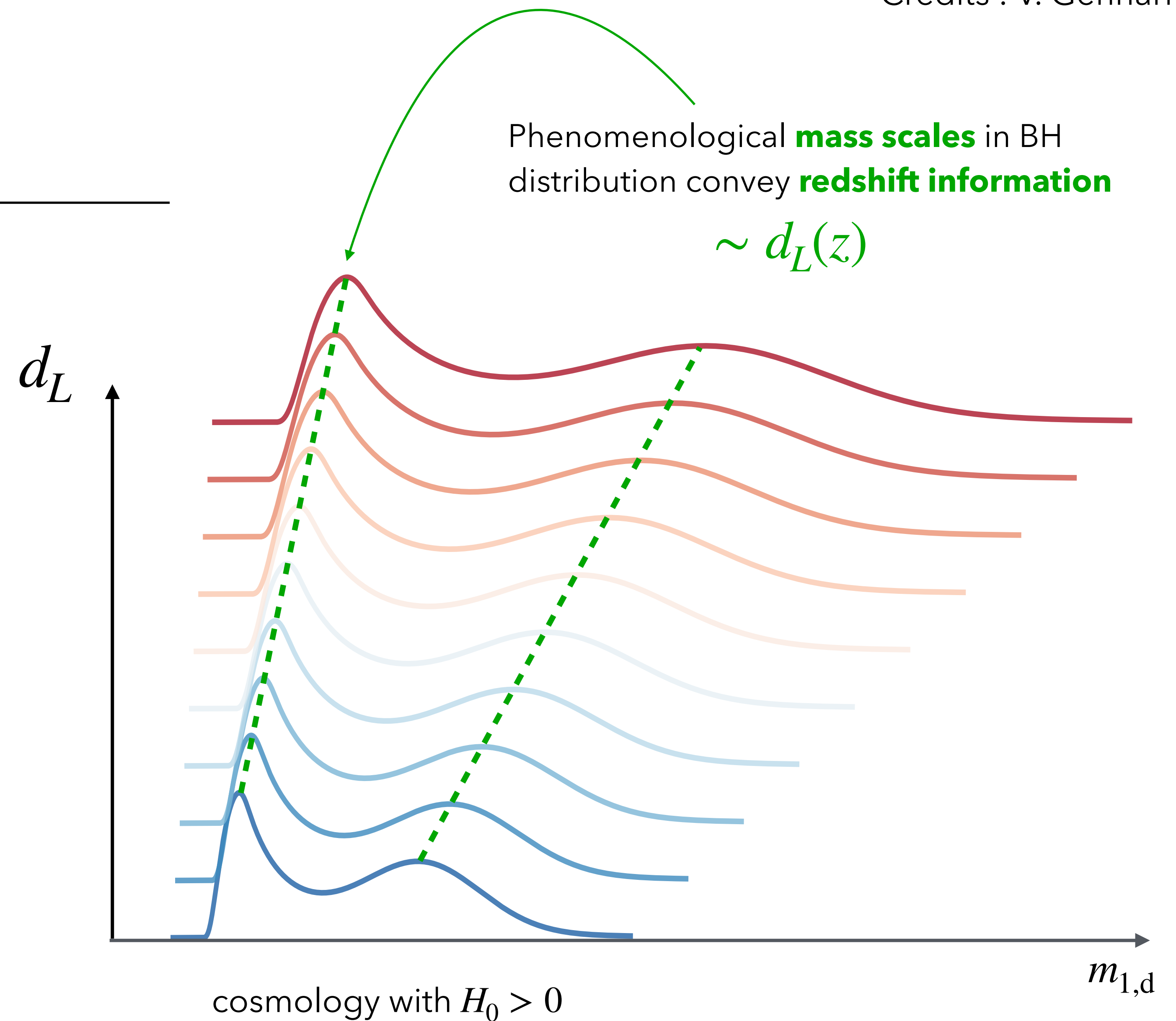
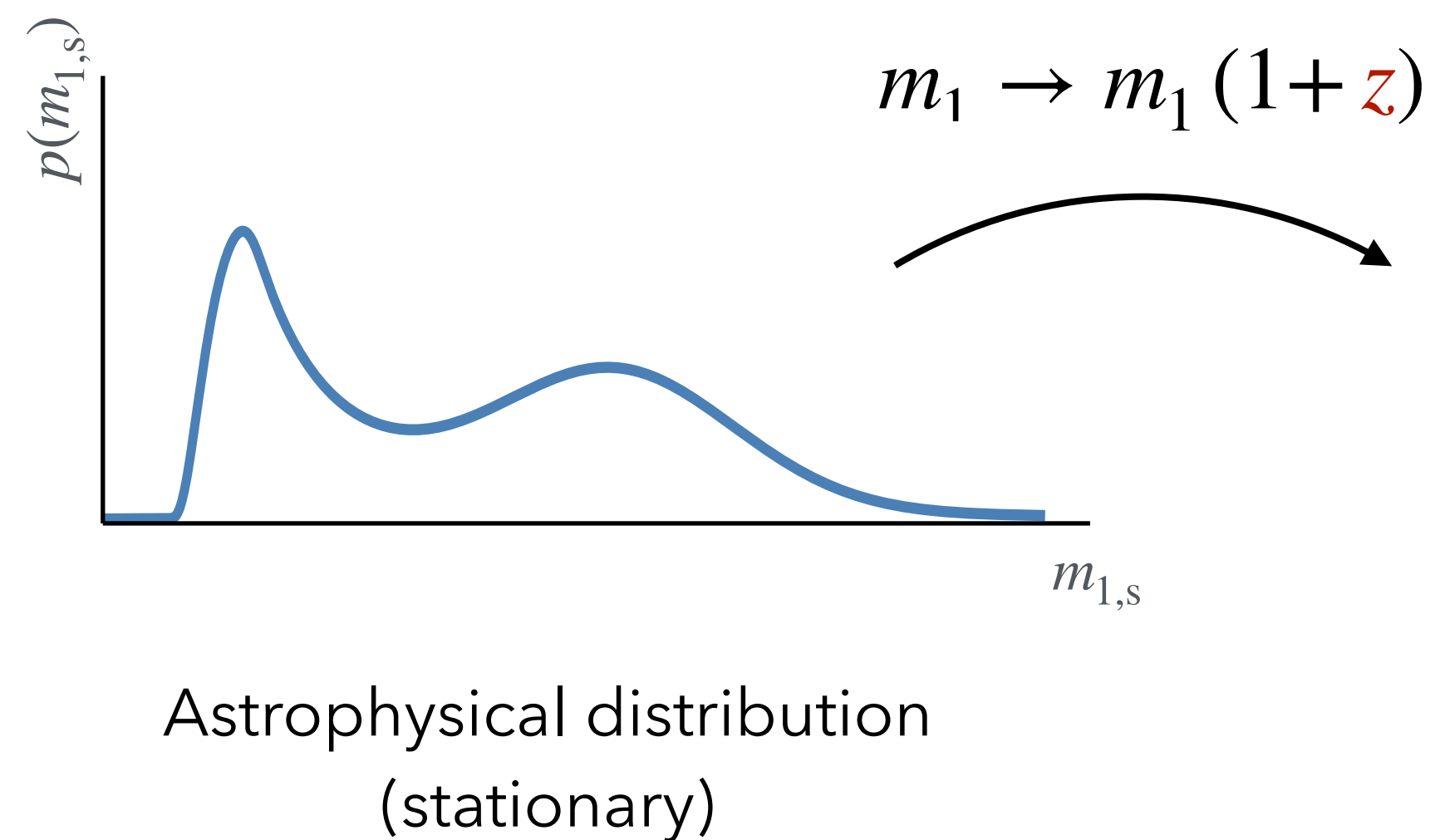
Outline

- Reminders about **spectral sirens**
- Parametric **mass models** used
- Re-analysis of **O3 data**
- **Simulations** setup
- **Forecasts** for O4 & O5

Spectral sirens

A quick reminder

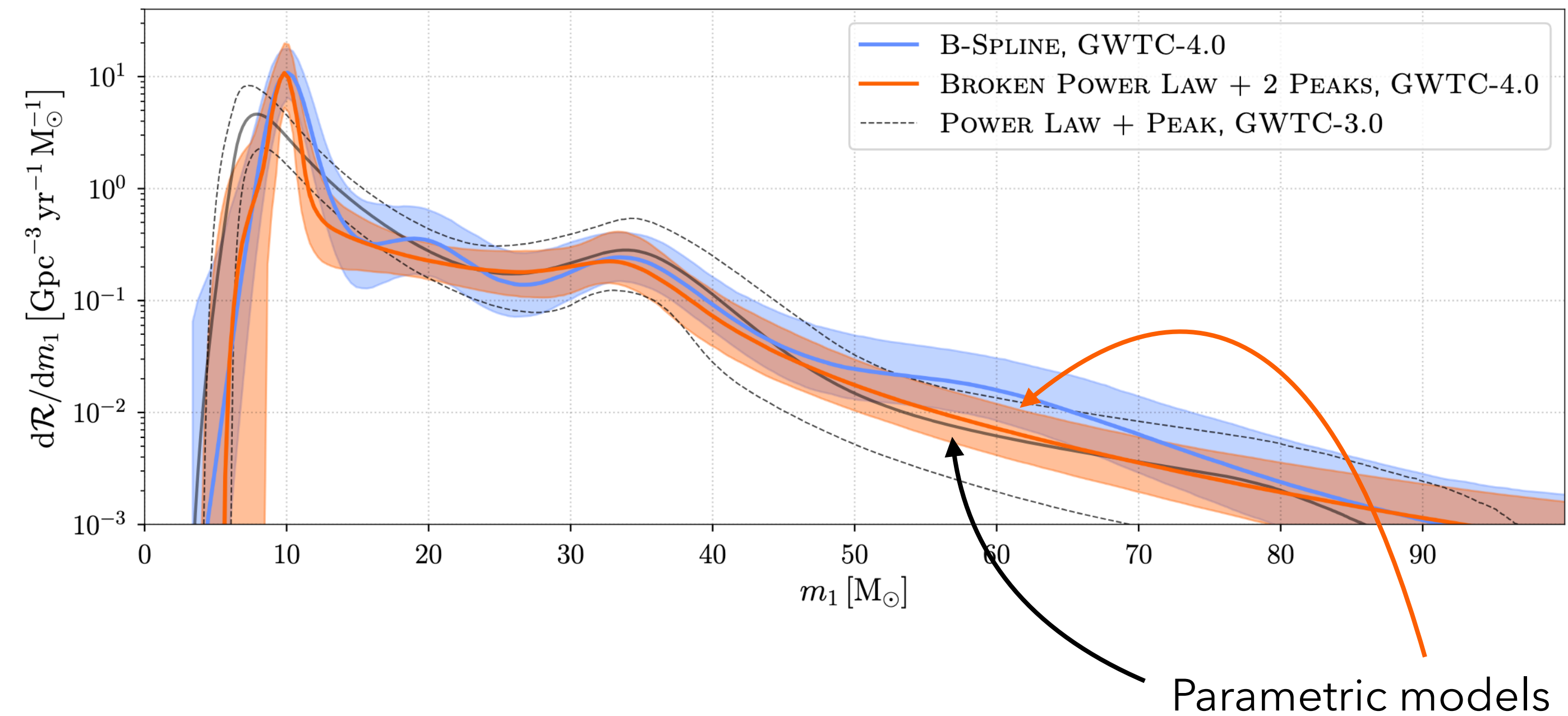
Credits : V. Gennari



Spectral sirens

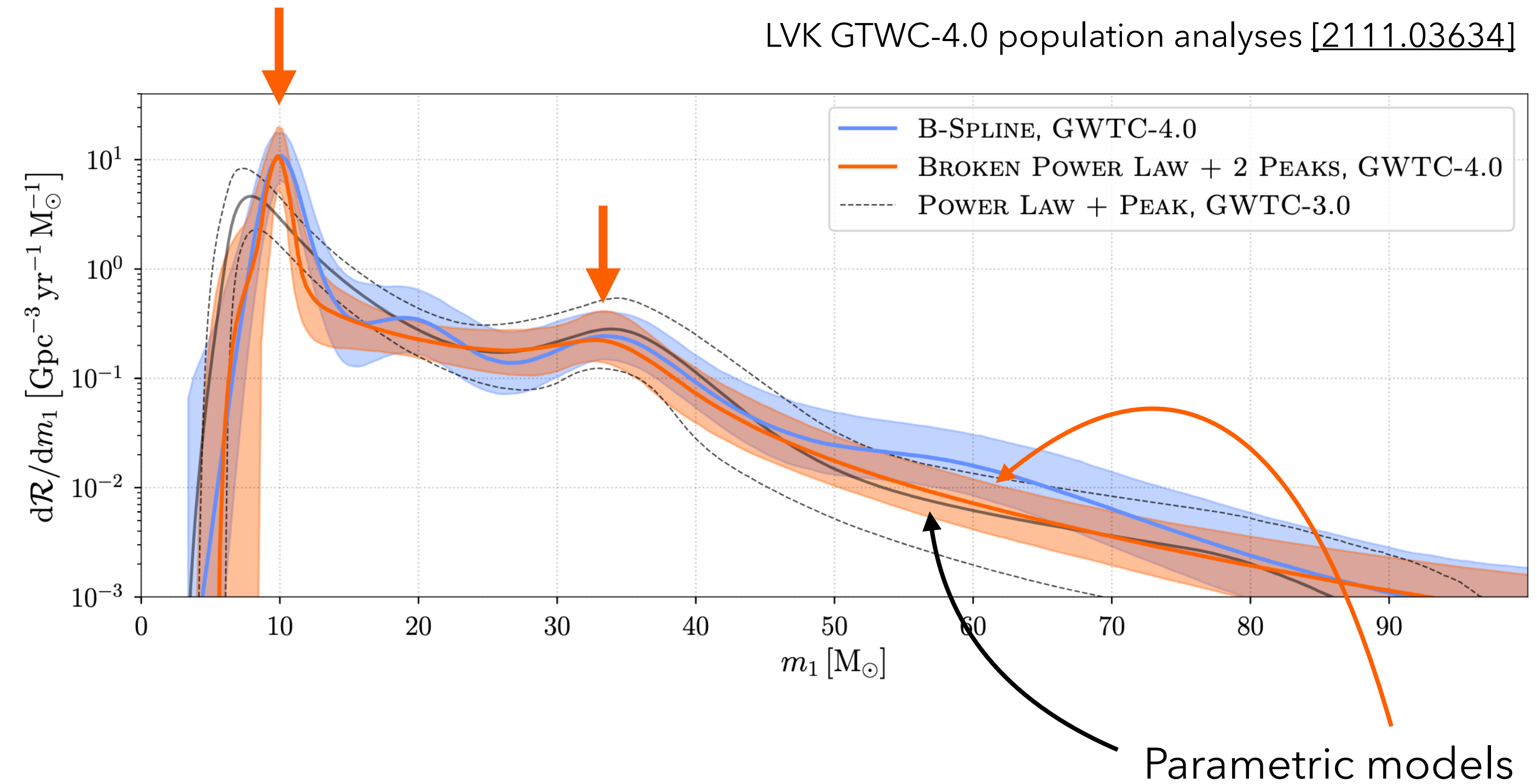
Looking for anchors

LVK GTWC-4.0 population analyses [2111.03634]



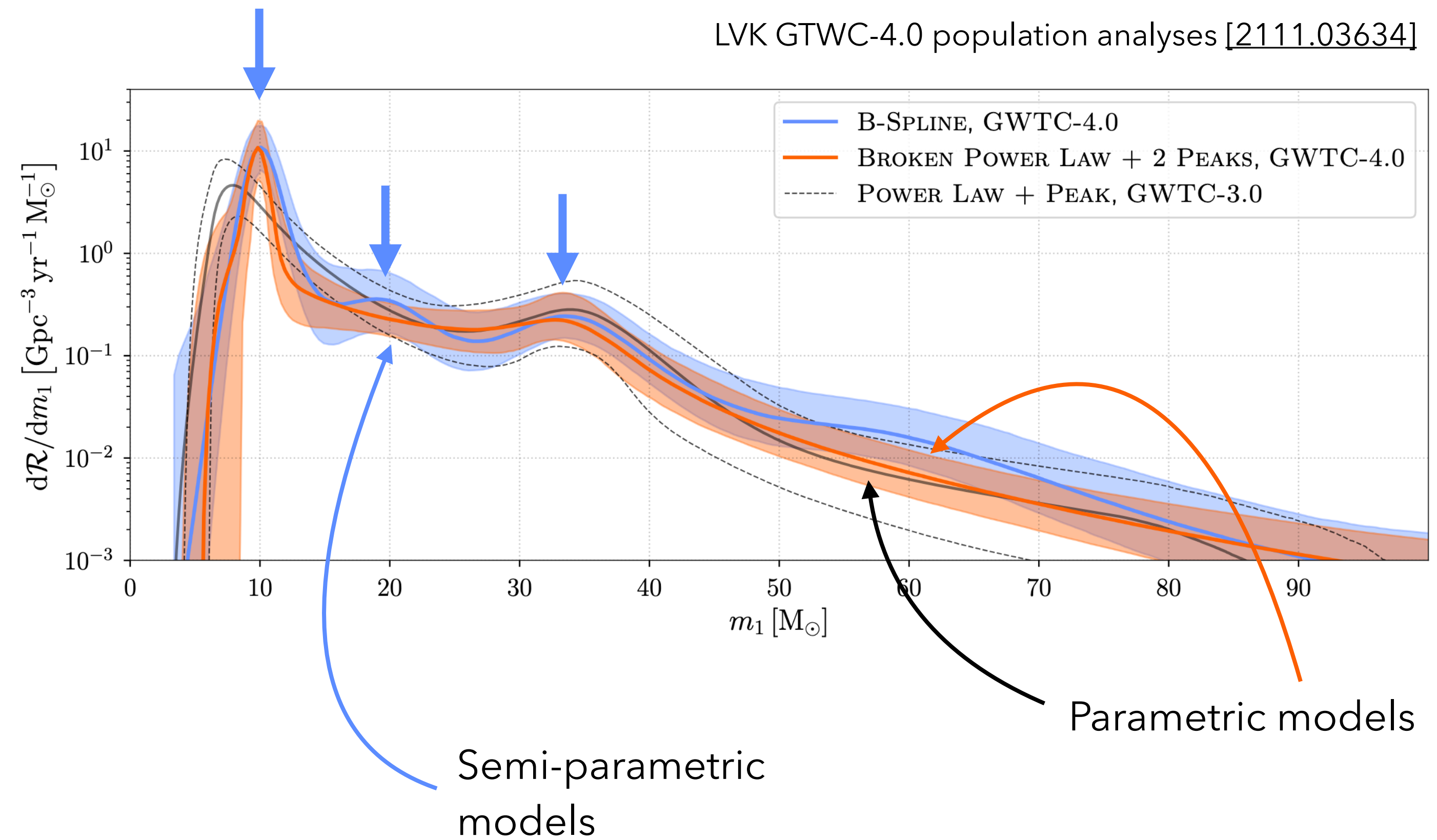
Spectral sirens

Looking for anchors



Spectral sirens

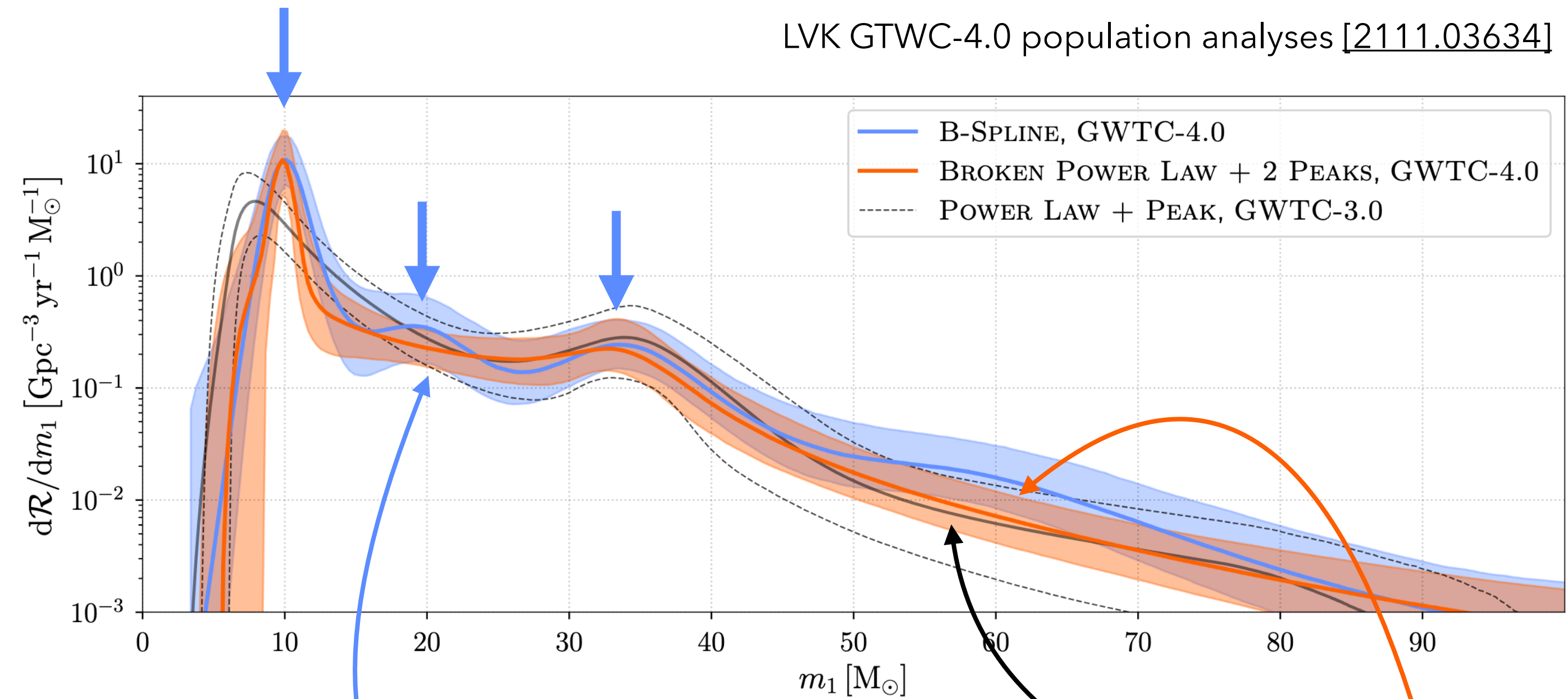
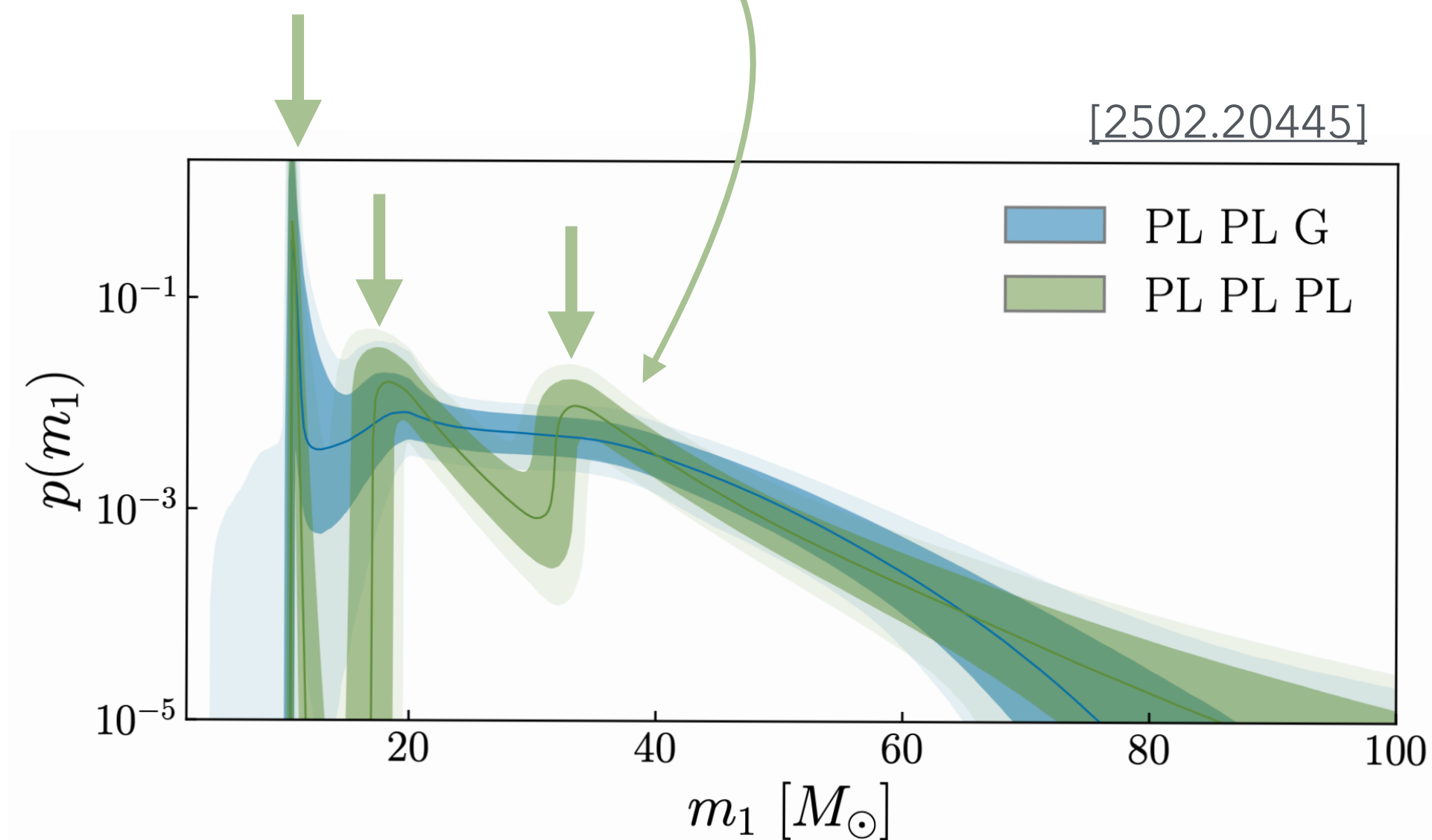
Looking for anchors



Spectral sirens

Looking for anchors

3 (sharp) features
parametric models



LVK GTWC-4.0 population analyses [2111.03634]

Semi-parametric
models

Parametric models

Methods

Mass models

Fiducial :

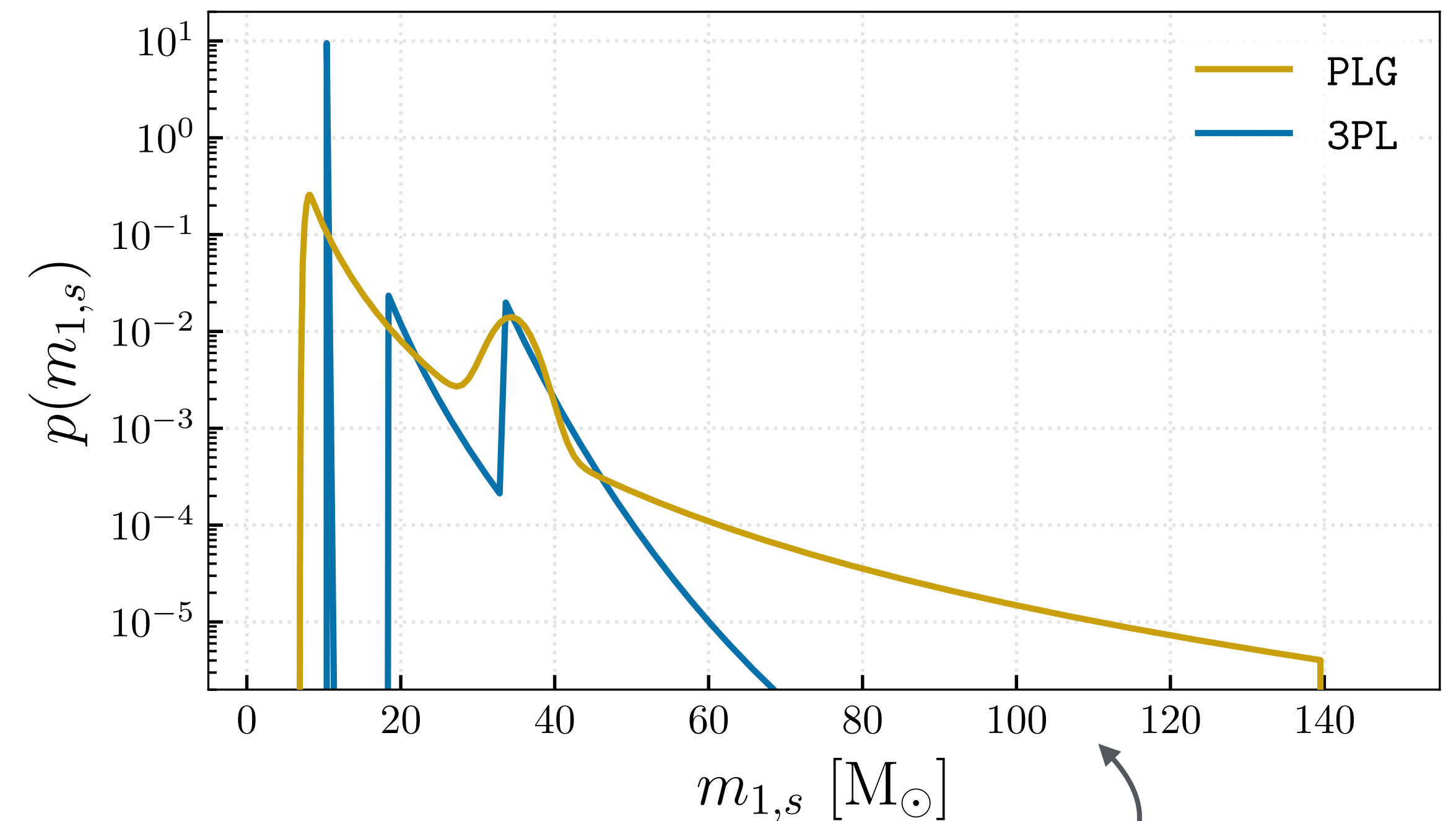
PowerLaw-Gaussian (PLG)

$$p(m_1) \sim PL + G$$

More (and sharper) features :

PowerLaw-PowerLaw-PowerLaw (3PL)

$$p(m_1) \sim PL_1 + PL_2 + PL_3$$



This is max $\mathcal{L}$ from O3

Methods

Mass models

Fiducial :

PowerLaw-Gaussian (PLG)

$$p(m_1) \sim PL + G$$

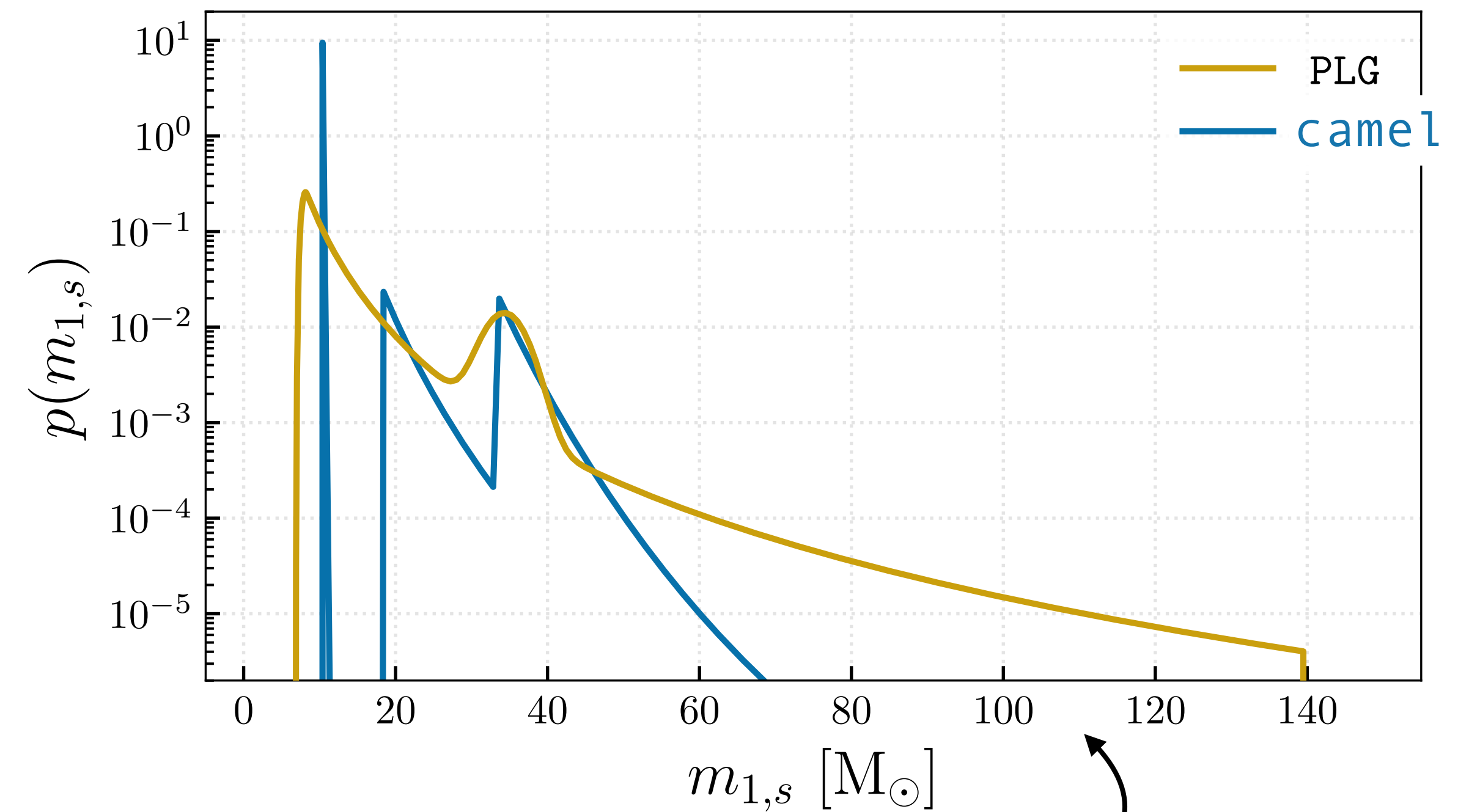
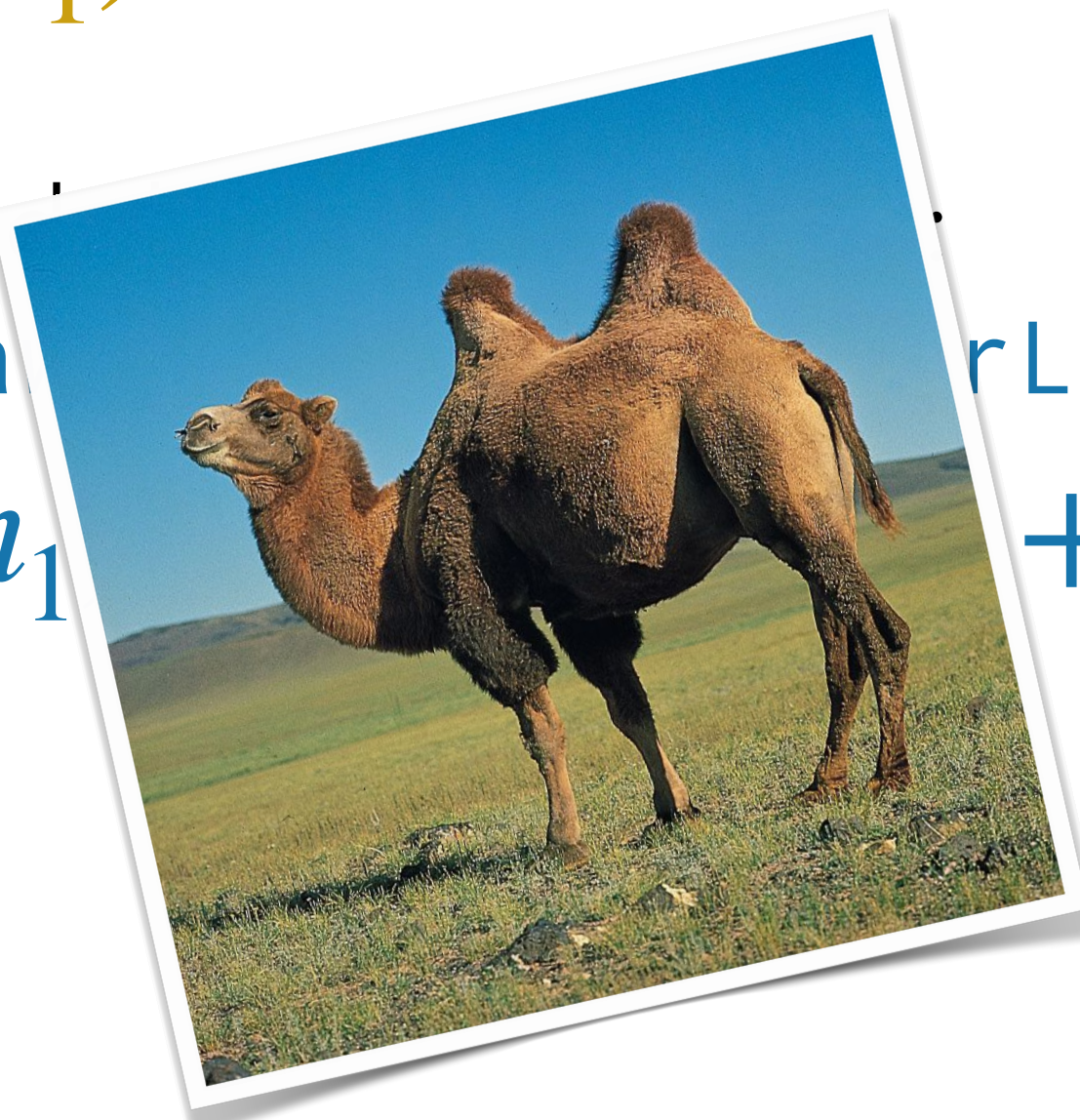
More (and)

PowerLaw

PowerLaw (camel)

$$p(m_1)$$

$$+ PL_3$$



This is max $\mathcal{L}$ from O3

Methods

Mass models

Fiducial :

PowerLaw-Gaussian (PLG)

$$p(m_1) \sim PL + G$$

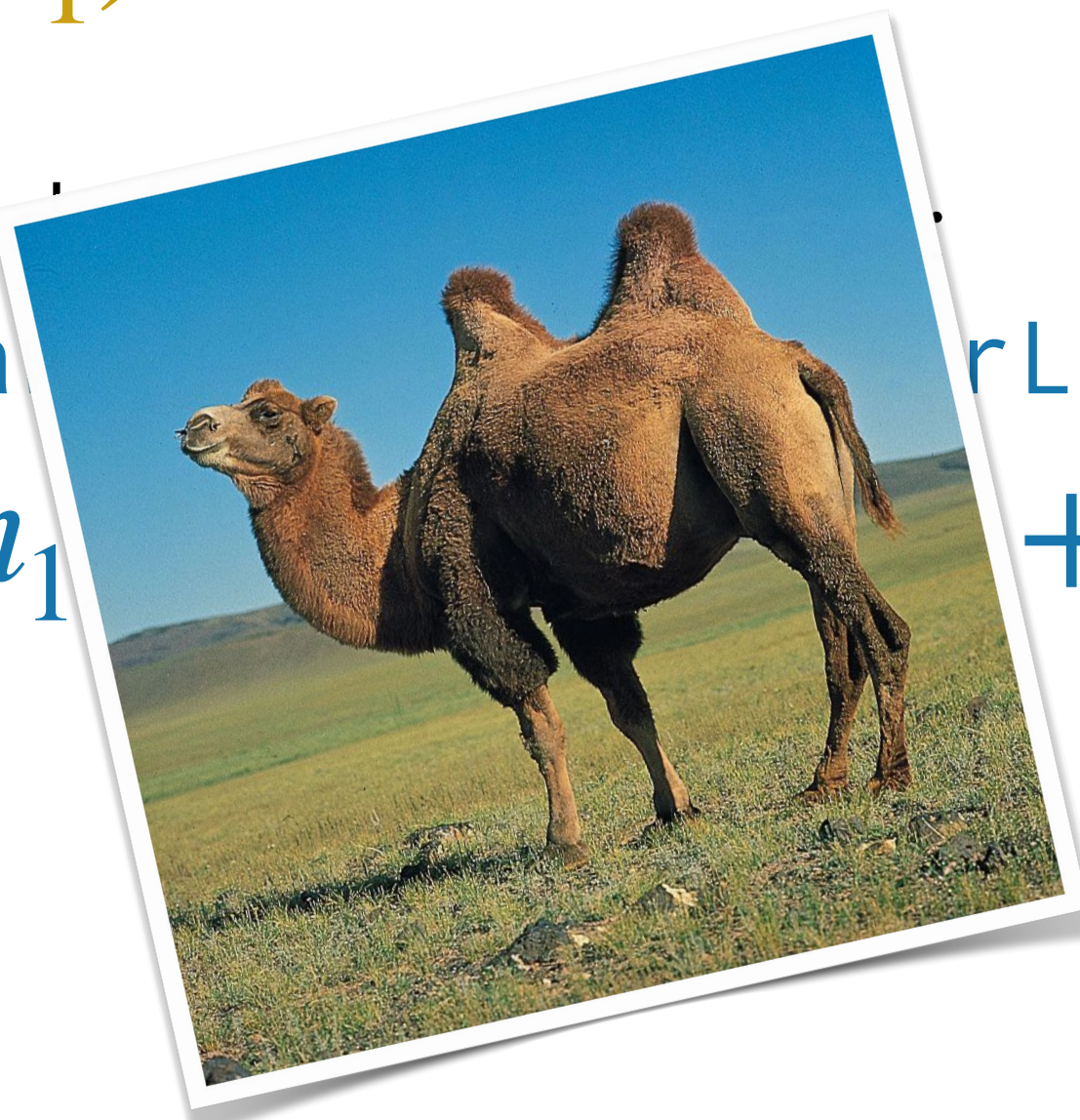
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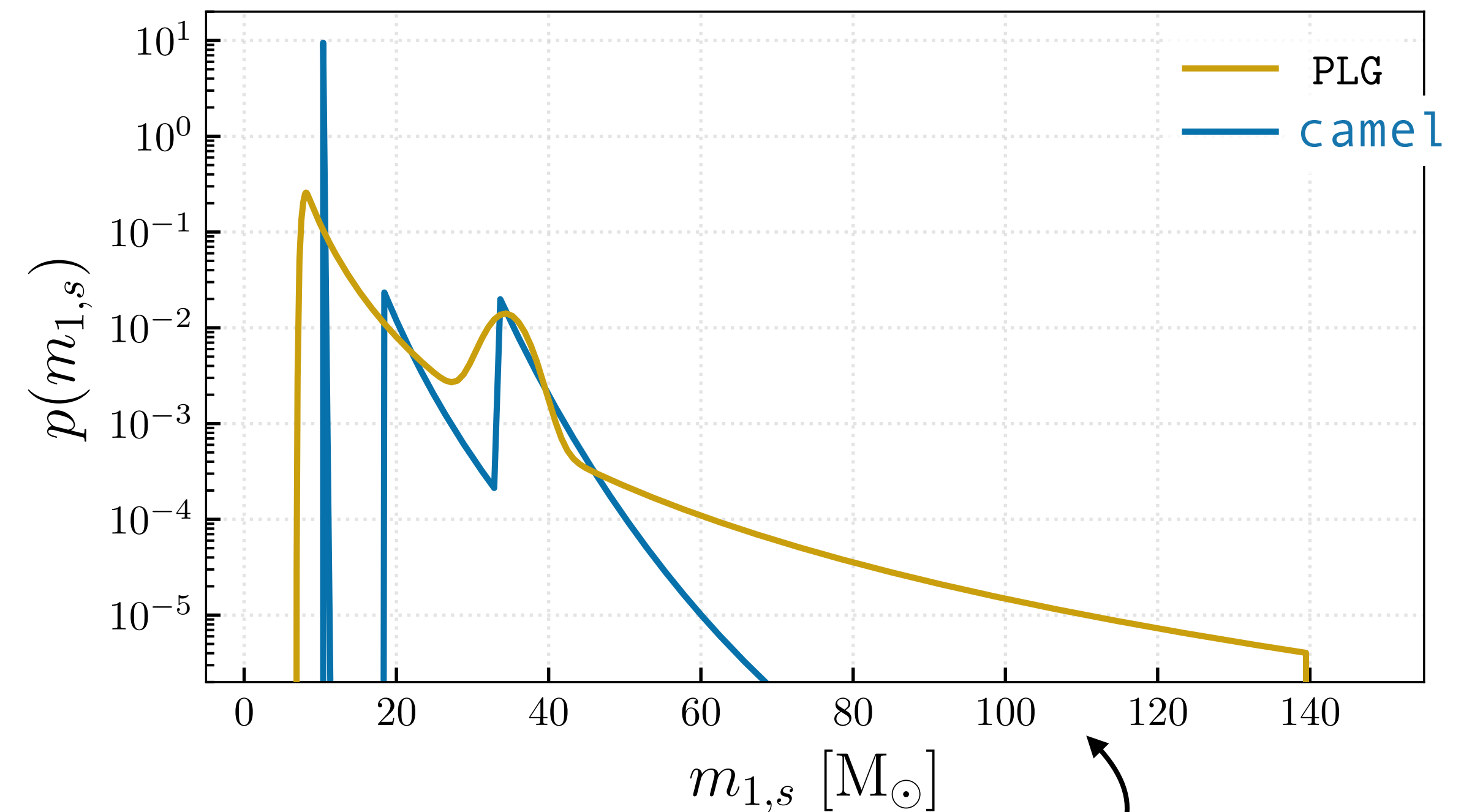
$$p(m_1)$$

$$+ PL_3$$



O3 data shows strong bayes evidence in favour of 3PL over PLG:

$$\ln \mathcal{B}_{3PL/PLG} > 5$$



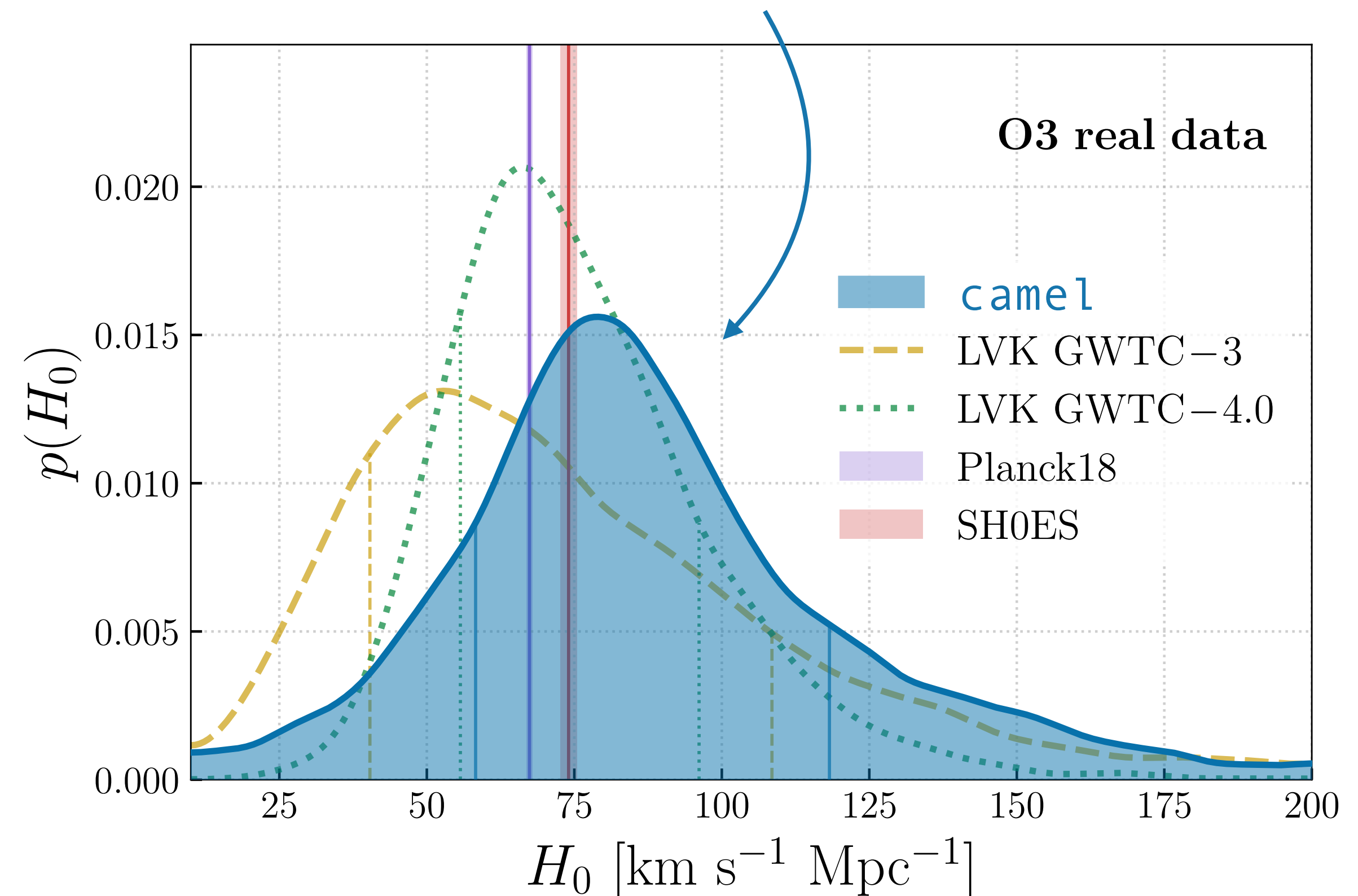
This is max $\mathcal{L}$ from O3

Results

O3 real data

- **3PL** = 30% accuracy improvement compared to **(LVK) O3 PLG**
- O3 H_0 measurement competitive with current **GWTC-4.0 results**

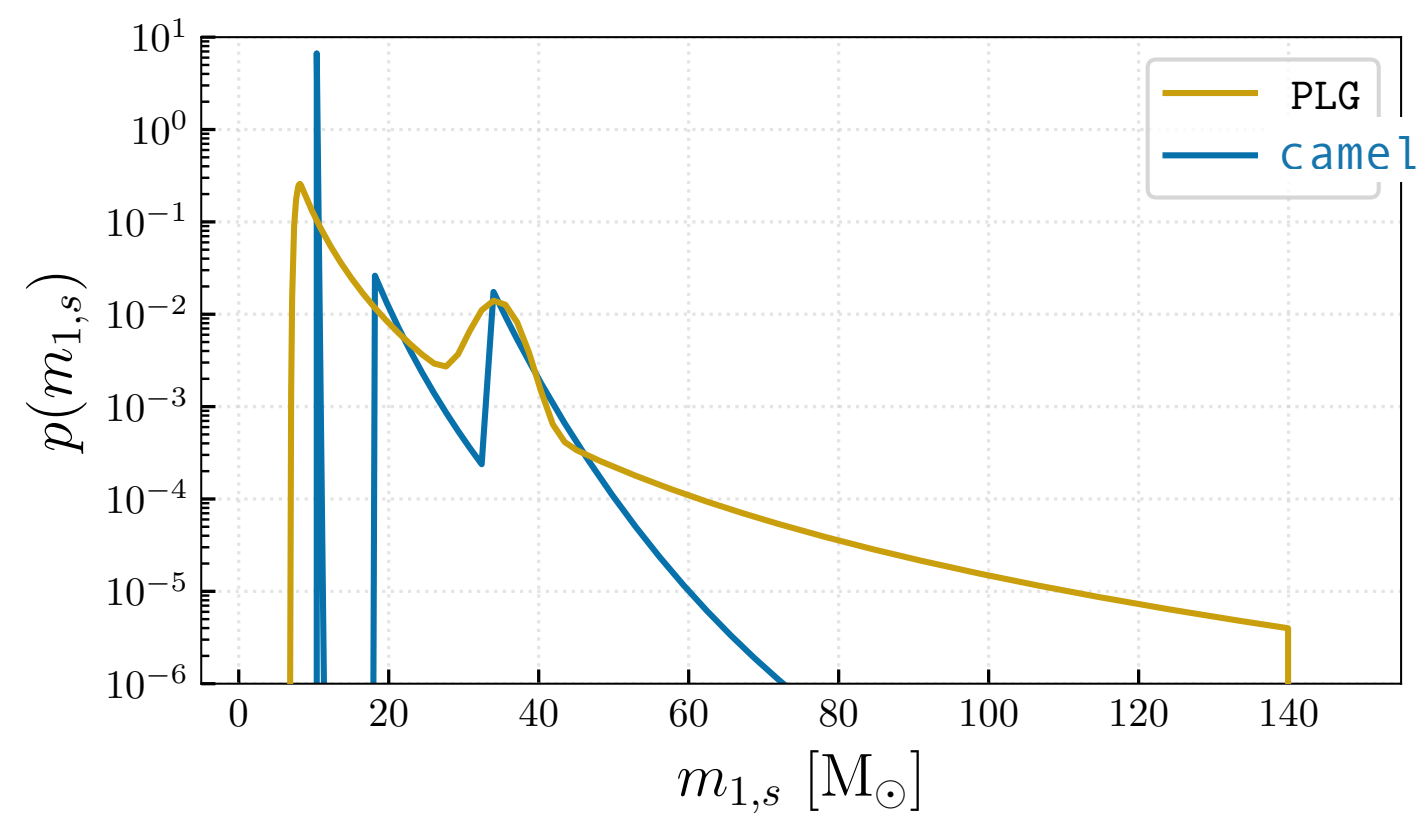
$$H_0 = 84^{+35}_{-25} \text{ km s}^{-1} \text{ Mpc}^{-1}$$



Methods

Simulating mock data sets

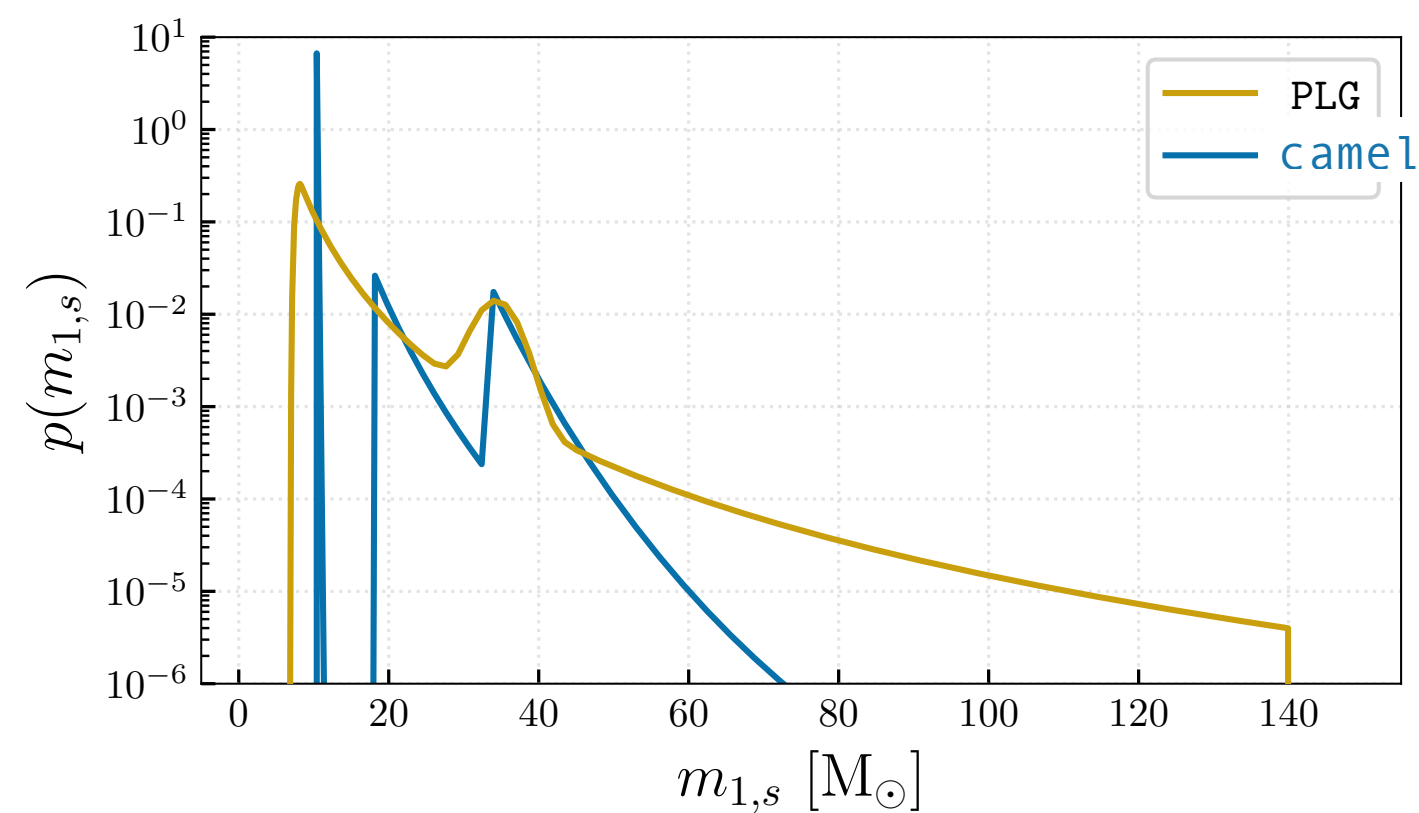
1. **Draw events** (m_1, m_2, z) from
O3 max $\mathcal{L}$ rates



Methods

Simulating mock data sets

1. **Draw events** (m_1, m_2, z) from
O3 max $\mathcal{L}$ rates



2. Realistic **detection** simulation:

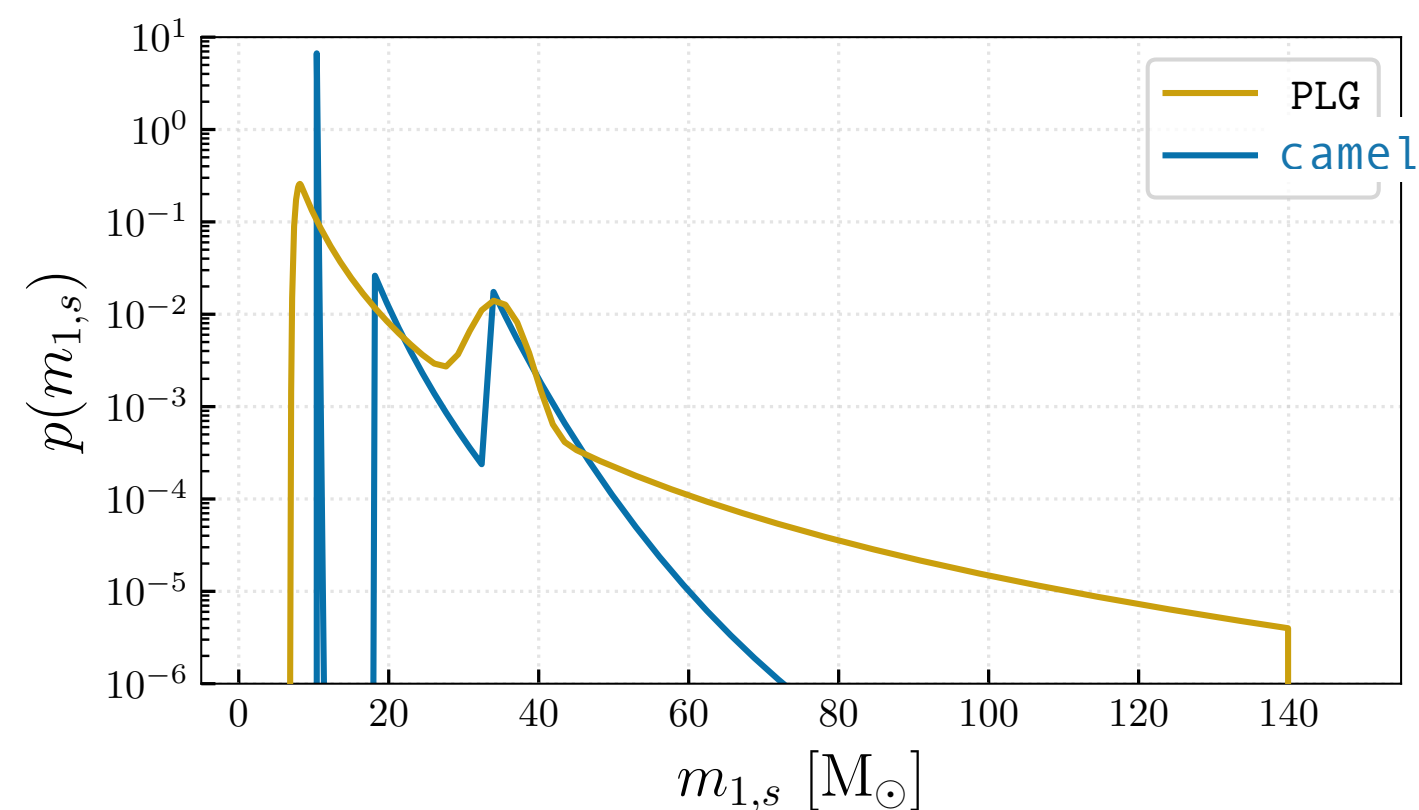
- Duty cycles based on observing plans (O4 1.5yrs / O5 3yrs)
- Coloured gaussian noise from design PSDs
- Signal with IMRPhenomXHM
- Matched-filter SNR > 12

	O4	O5
PLG	142	1823
3PL	149	1862

Methods

Simulating mock data sets

1. **Draw events** (m_1, m_2, z) from
O3 max $\mathcal{L}$ rates



2. Realistic **detection** simulation:

- Duty cycles based on observing plans (O4 1.5yrs / O5 3yrs)
- Coloured gaussian noise from design PSDs
- Signal with IMRPhenomXHM
- Matched-filter SNR > 12

3. Realistic **parameter estimation**:

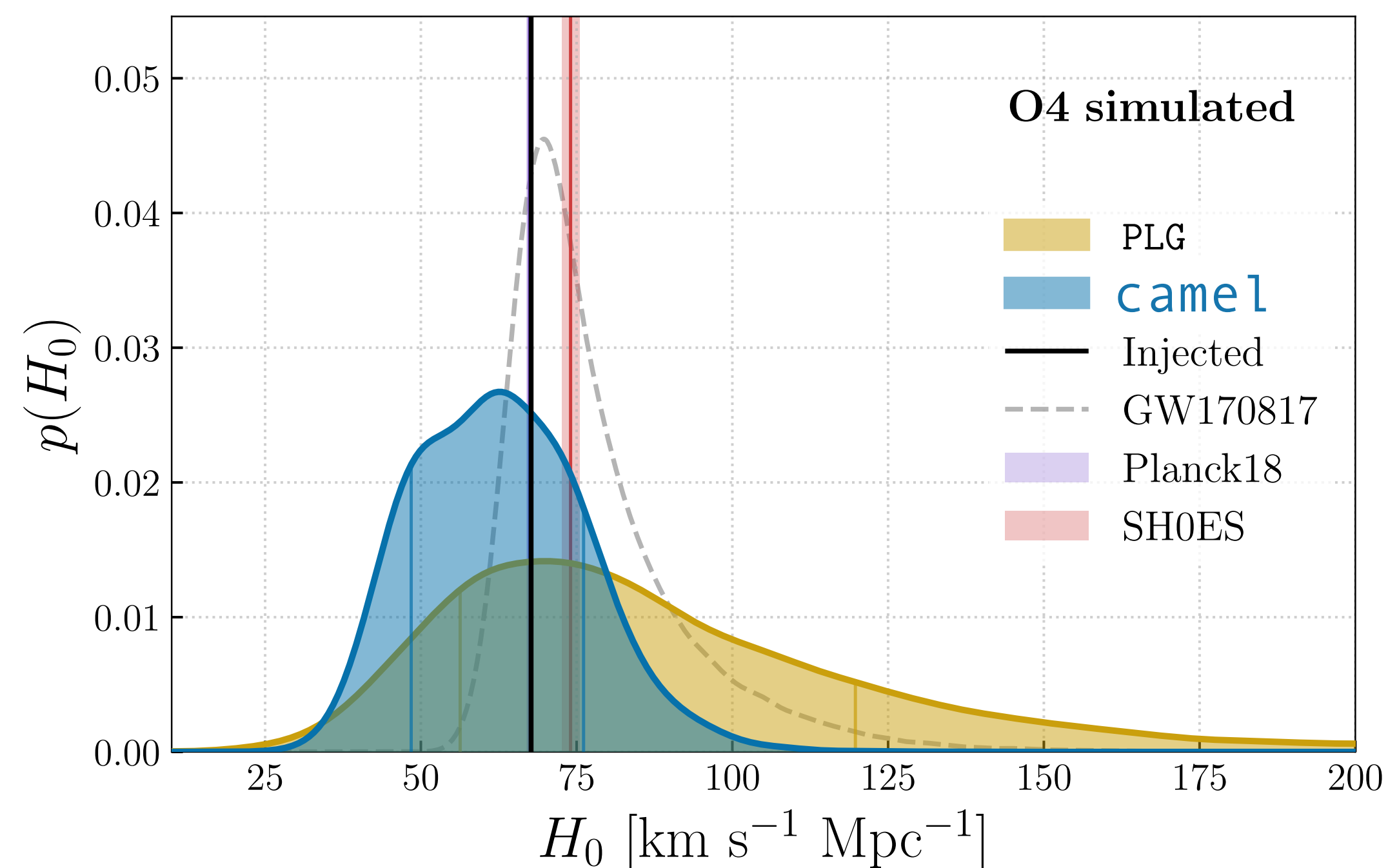
- Full realistic PE procedure on each event
- Gaussian likelihood
- samples generated with the `nessai` sampler from `bilby`

	O4	O5
PLG	142	1823
3PL	149	1862

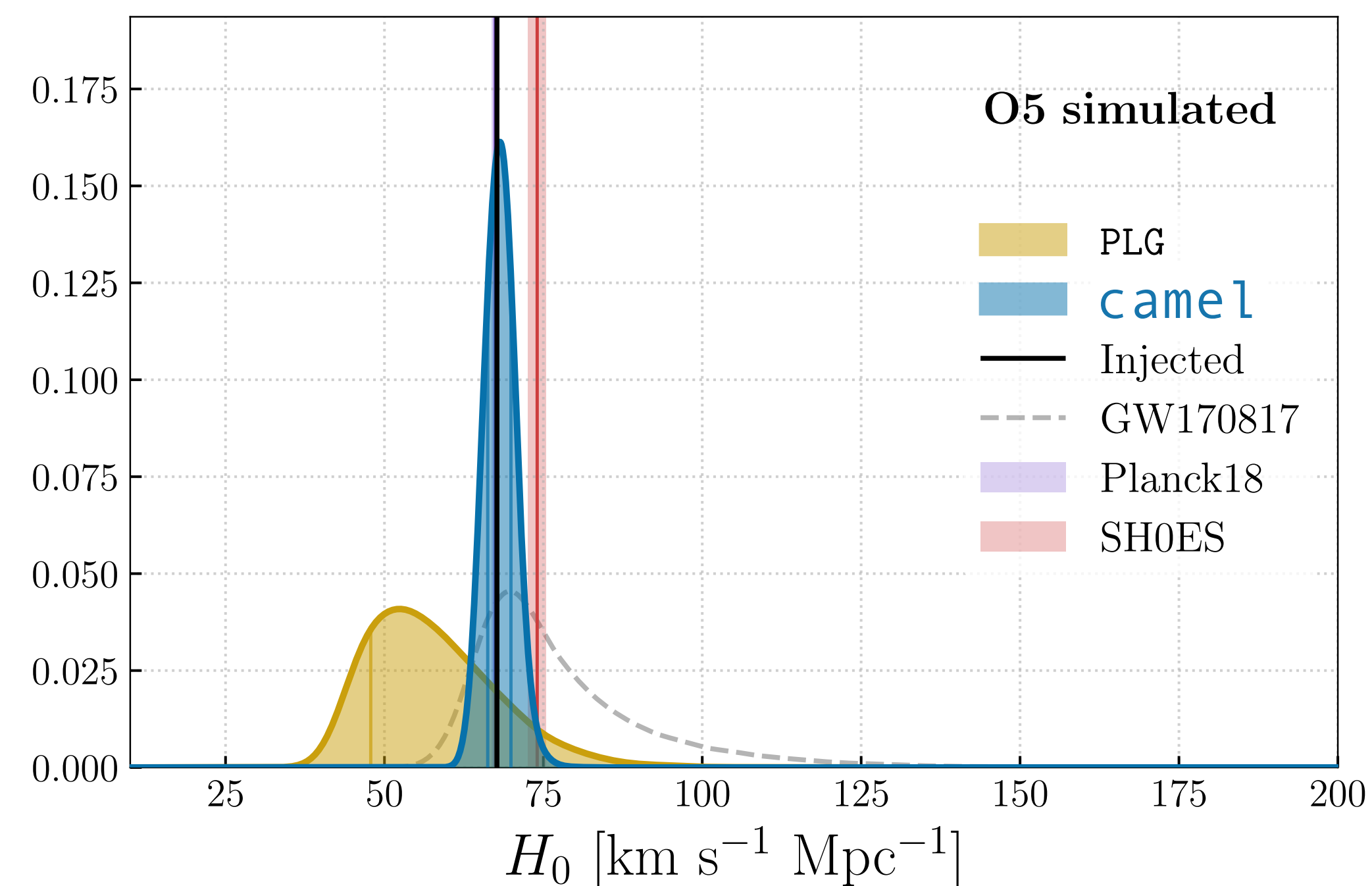
Similar procedure as LVK's MDC study [2412.14244]

Results

H_0 constraints forecasts



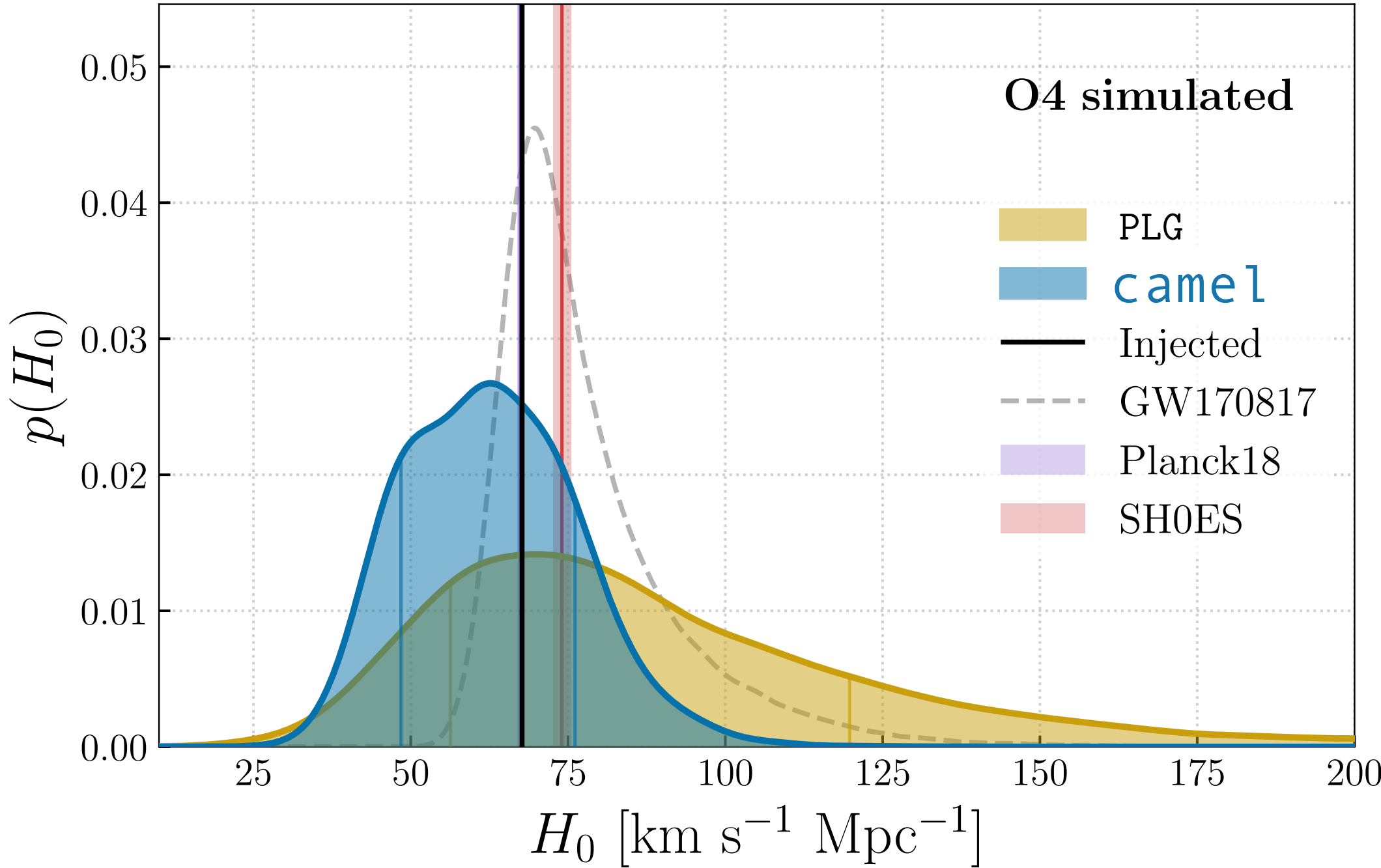
O4	H_0 [km s ⁻¹ Mpc ⁻¹]
PLG	80^{+39}_{-24} (73)
<i>camel</i>	62^{+14}_{-14} (23) (20)



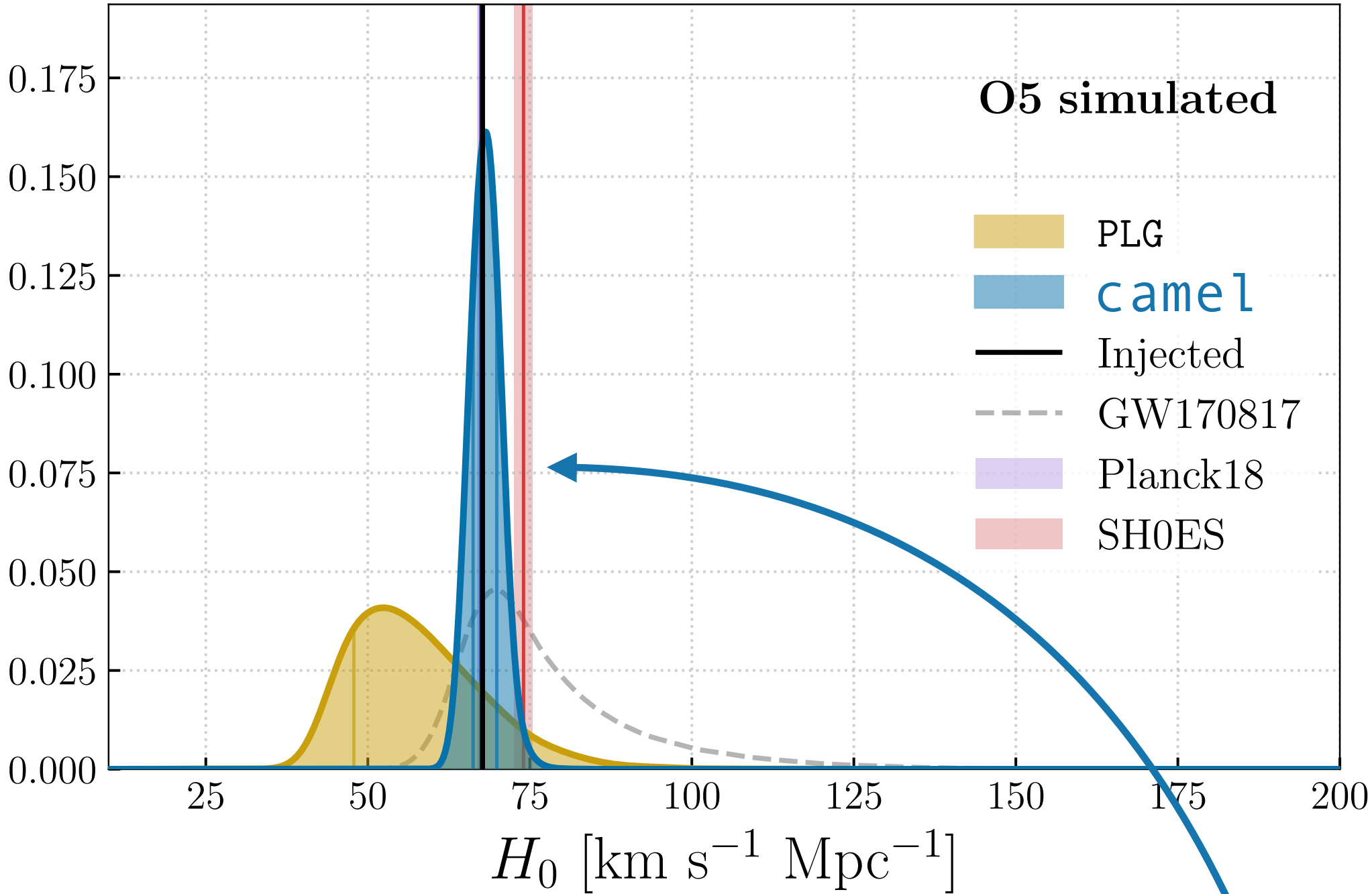
O5	H_0 [km s ⁻¹ Mpc ⁻¹]
PLG	56^{+12}_{-8} (20) (11)
<i>camel</i>	$68.2^{+1.7}_{-2.0}$ (3.1) (2.9)

Results

H_0 constraints forecasts



O4	H_0 [km s ⁻¹ Mpc ⁻¹]
PLG	80^{+39}_{-24} (73)
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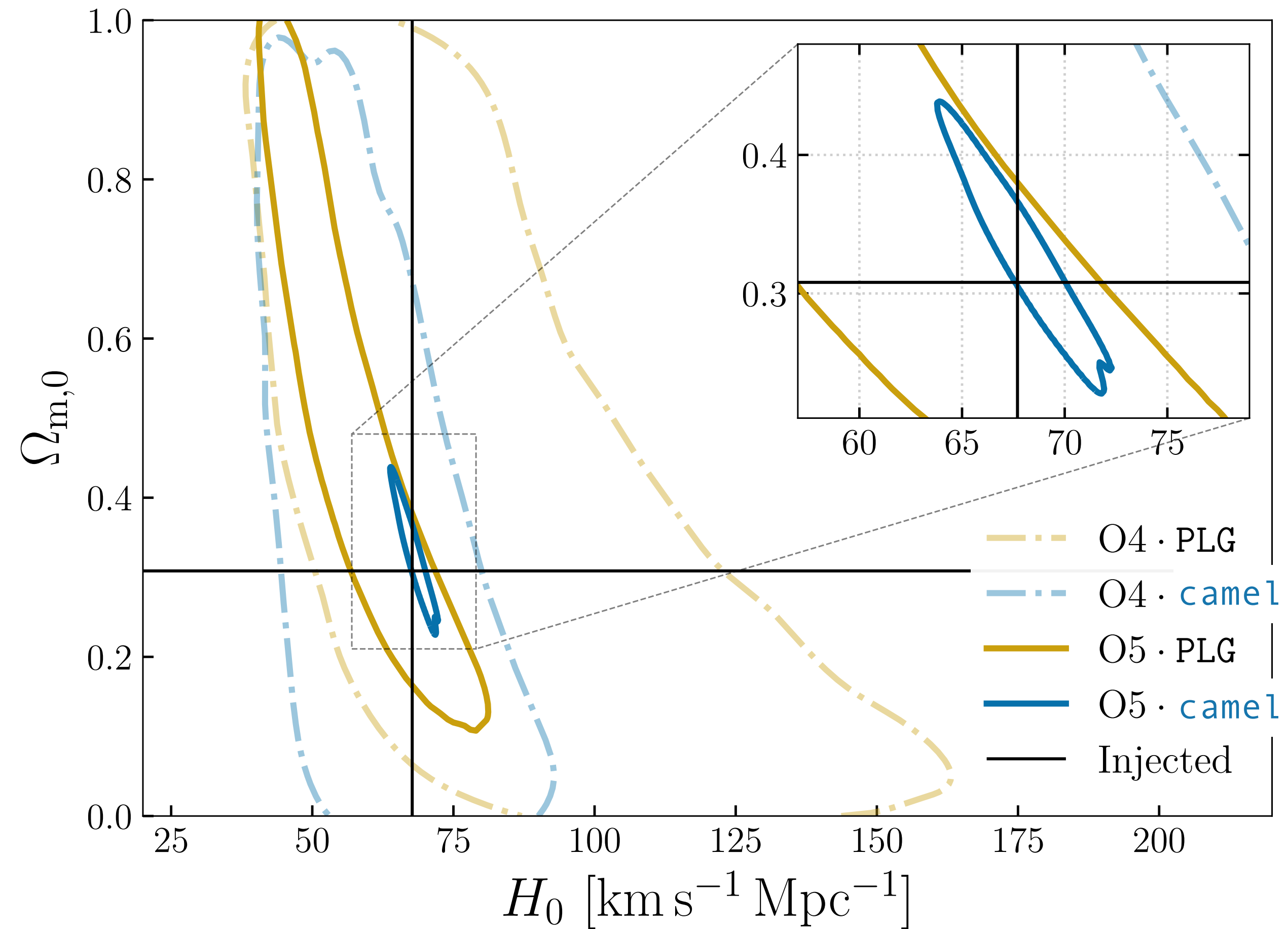


O5	H_0 [km s ⁻¹ Mpc ⁻¹]
PLG	56^{+12}_{-8} (20)
camel	$68.2^{+1.7}_{-2.0}$ (3.1)

2.7% accuracy!

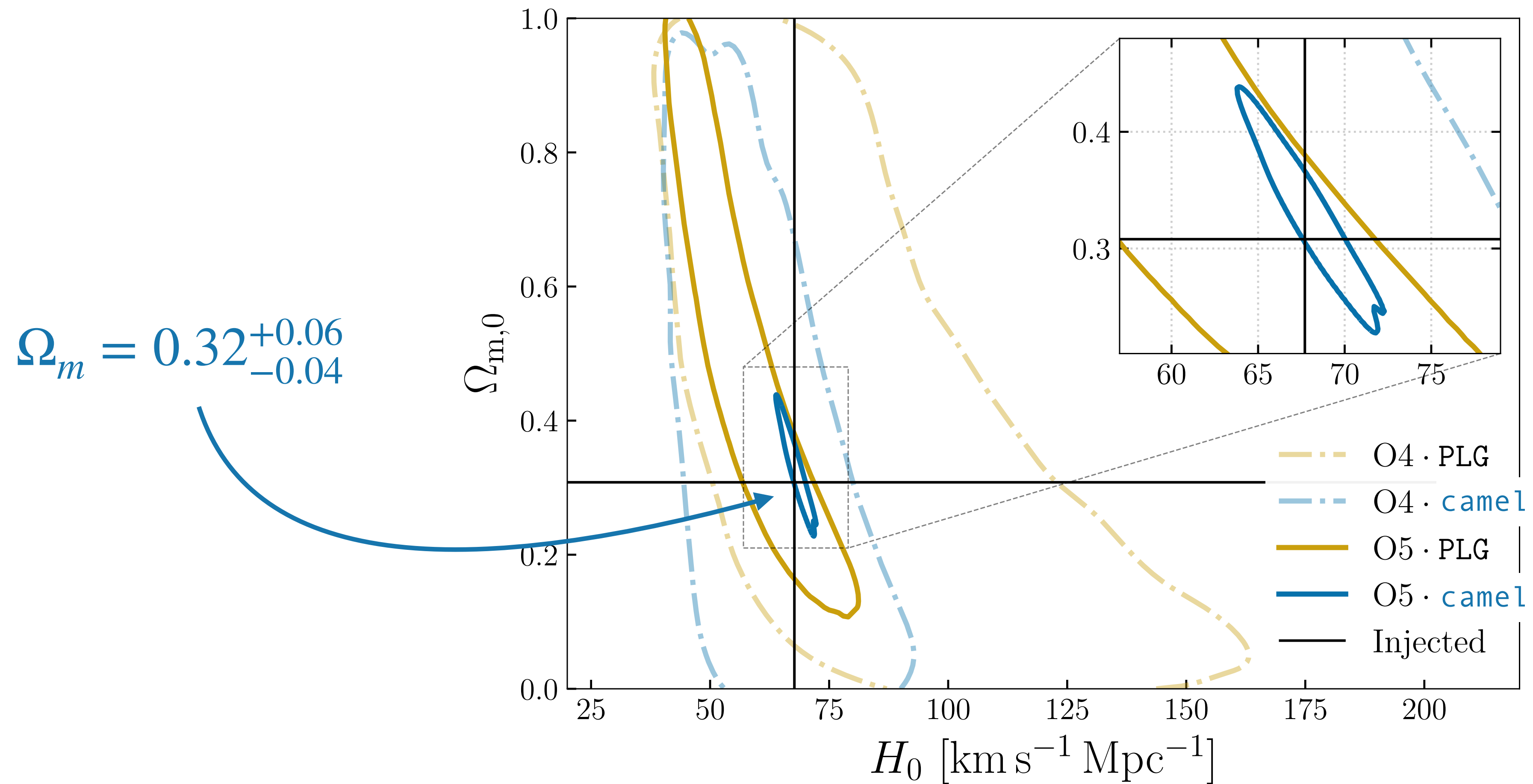
Results

Beyond H_0 : constraining $\Omega_{m,0}$



Results

Beyond H_0 : constraining $\Omega_{m,0}$



Conclusions

- **O3: 30% accuracy increase** with 3PL compared to LVK's PLG
- **Forecasts:** accuracy on H_0 by 3PL (resp. PLG) (X% accuracy at 68% CL)
 - O4:** 20% (resp. 40%)
 - O5:** 2.7% (resp. 18%)

- Our results are optimistic (for spectral sirens) **but** in reality we expect **EM counterparts** + contribution from **galaxy catalogs**

→ **towards %-level measurement of H_0 with O5 !**

- **Next ?** Extend to: GWTC-4.0, beyond Λ CDM cosmology, etc.



Main **assumptions**:

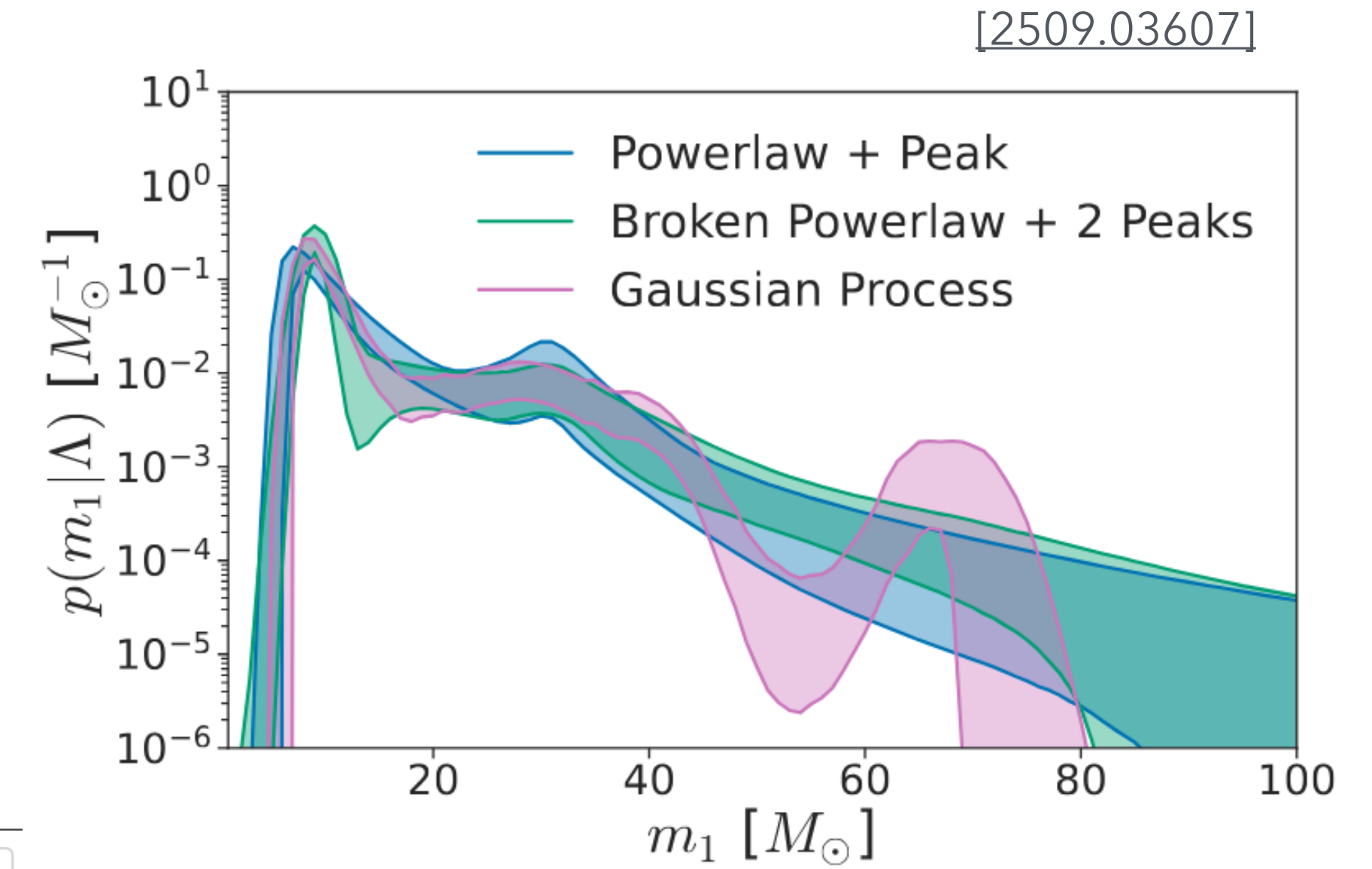
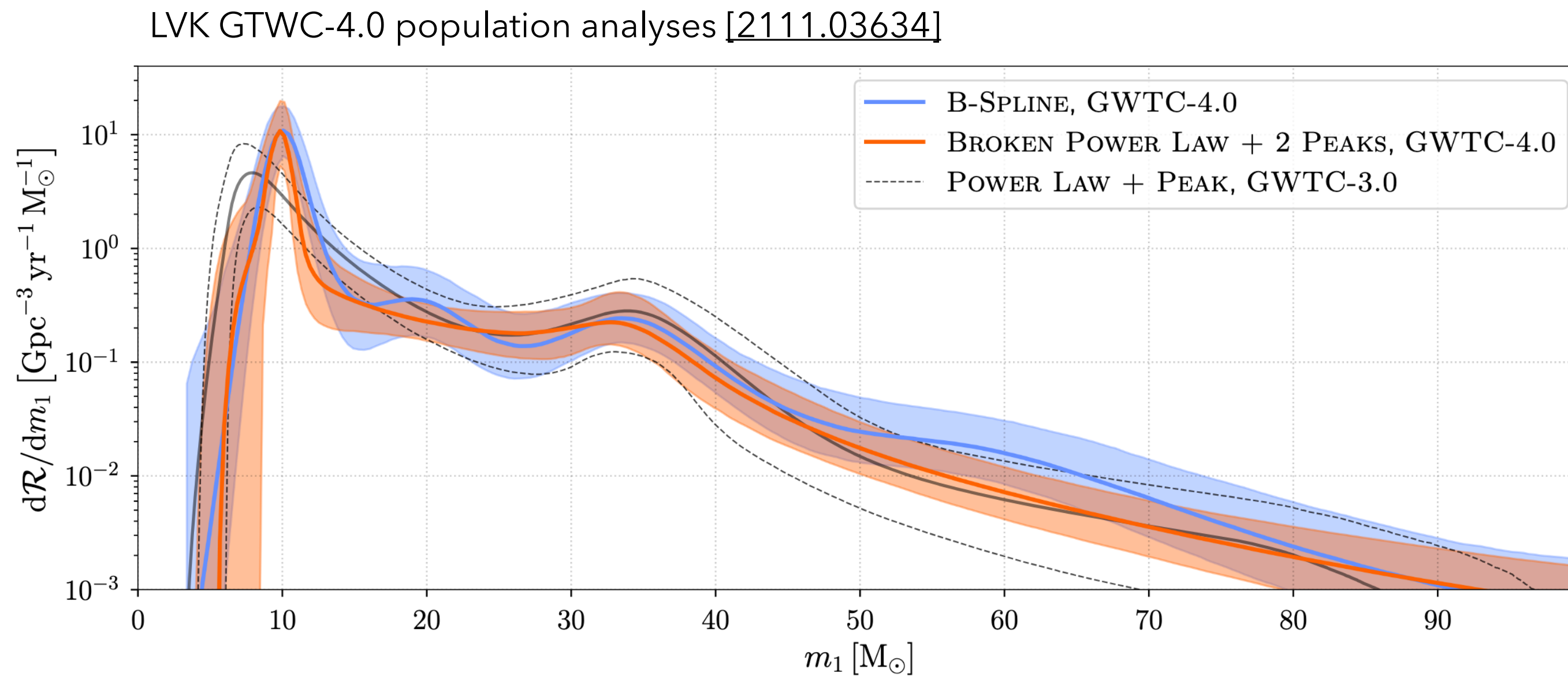
- Negligible redshift evolution of the mass function
- Likely over constraining features in the mass spectrum

Thanks for your attention !

backup

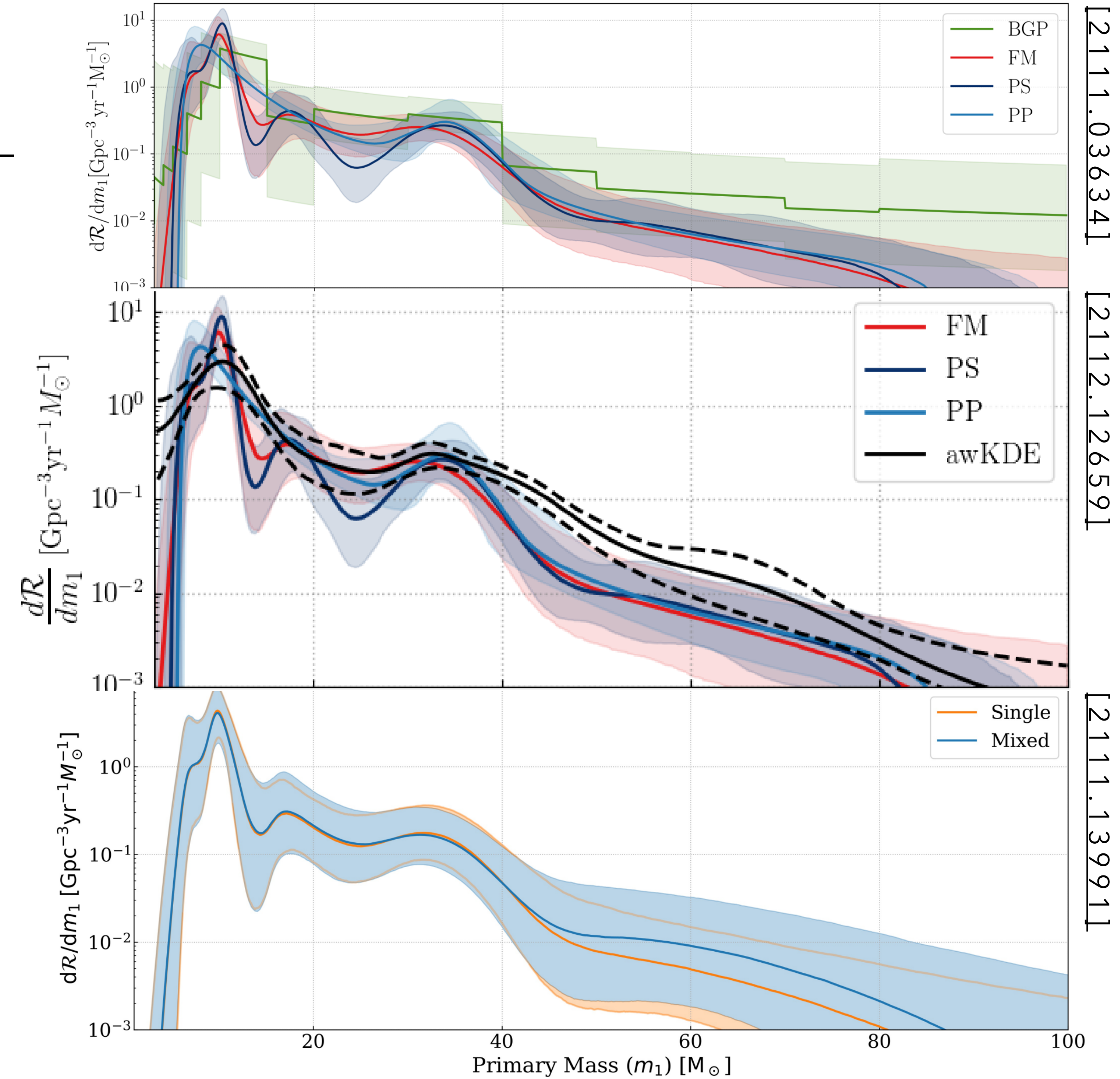
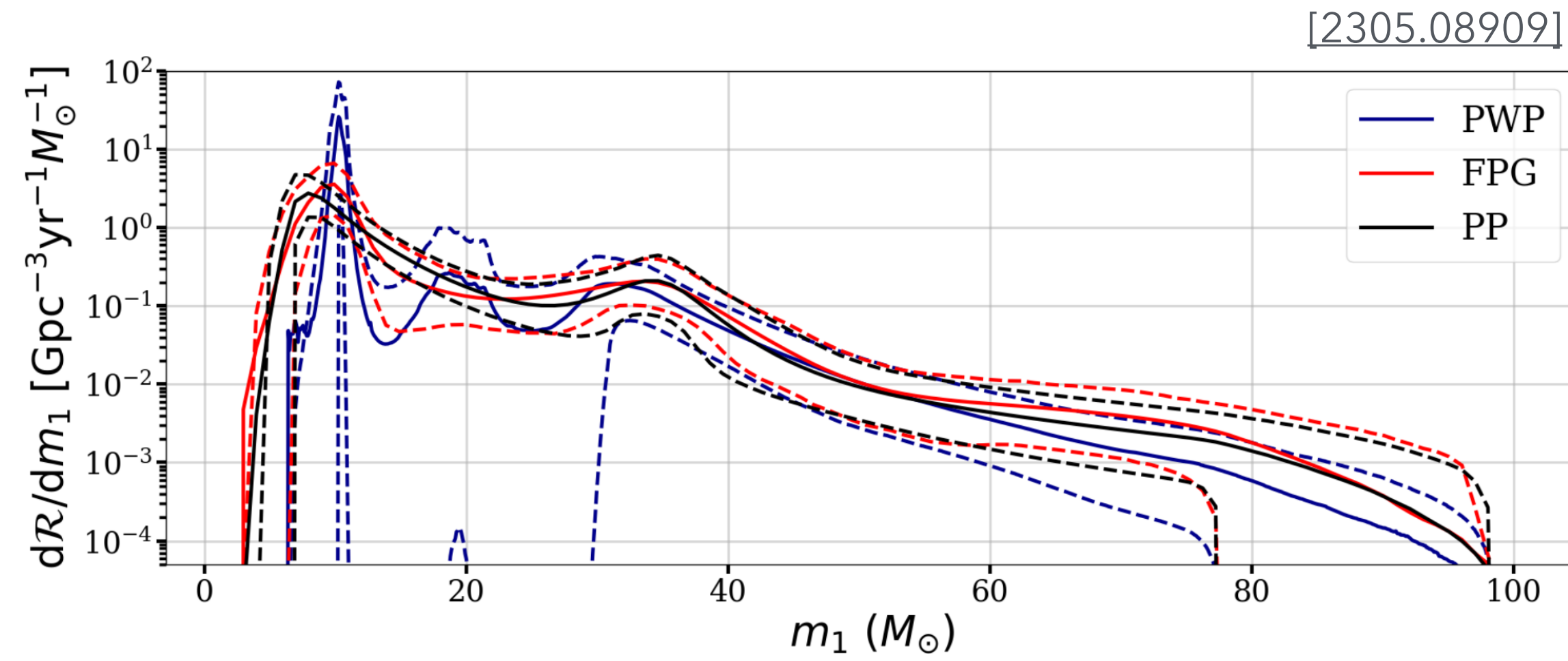
Spectral sirens

Non parametric studies



Spectral sirens

Non parametric studies



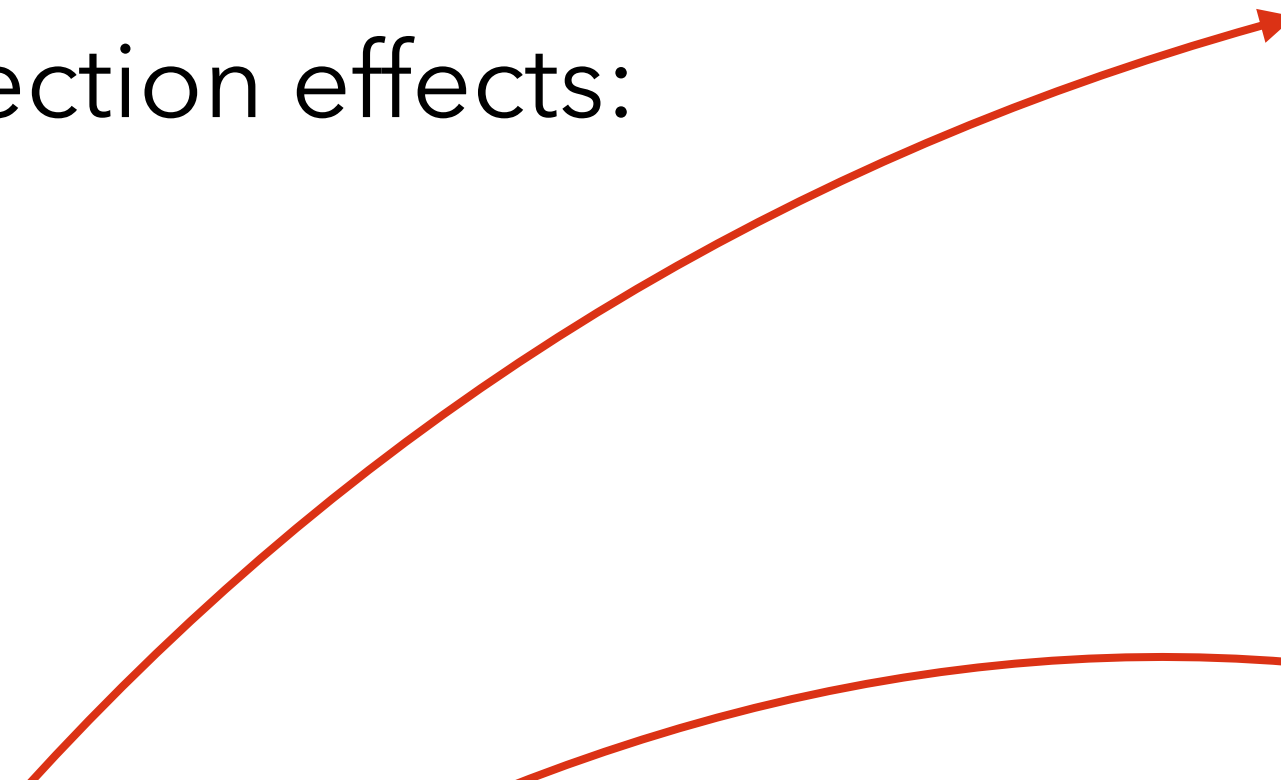
Numerical stability

- # of (detected) **injections** for selection effects:

- O4 : 500,000
- O5 : 6,000,000

- Numerical stability indicators:

- **Effective number of injections**
- **Effective number of PE samples** (per event)



Neffinj / 4*Nobs	O4	O5
3PL	13	12
PLG	220	211



(min) NeffPE	O4	O5
3PL	19	15
PLG	81	103

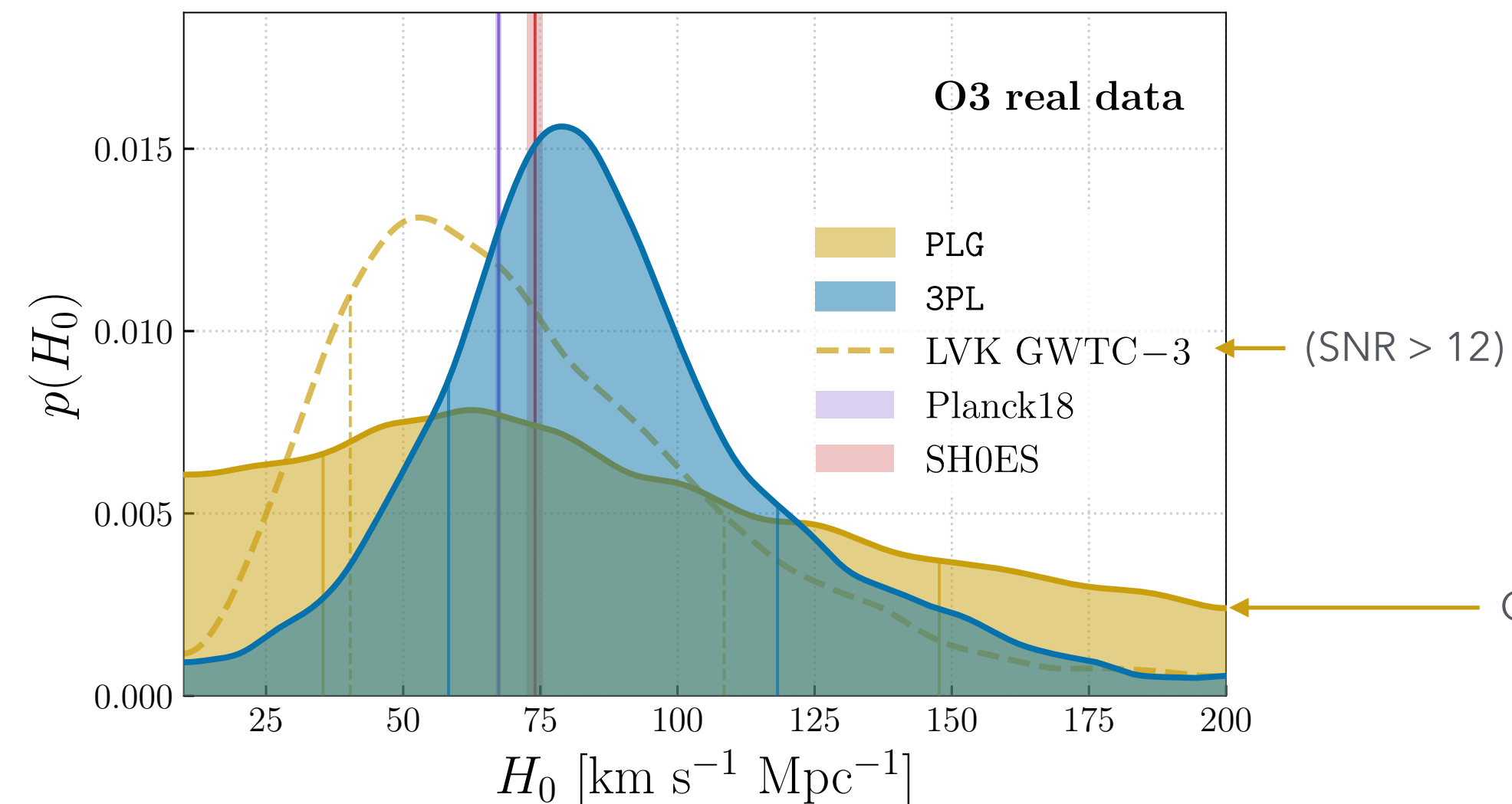
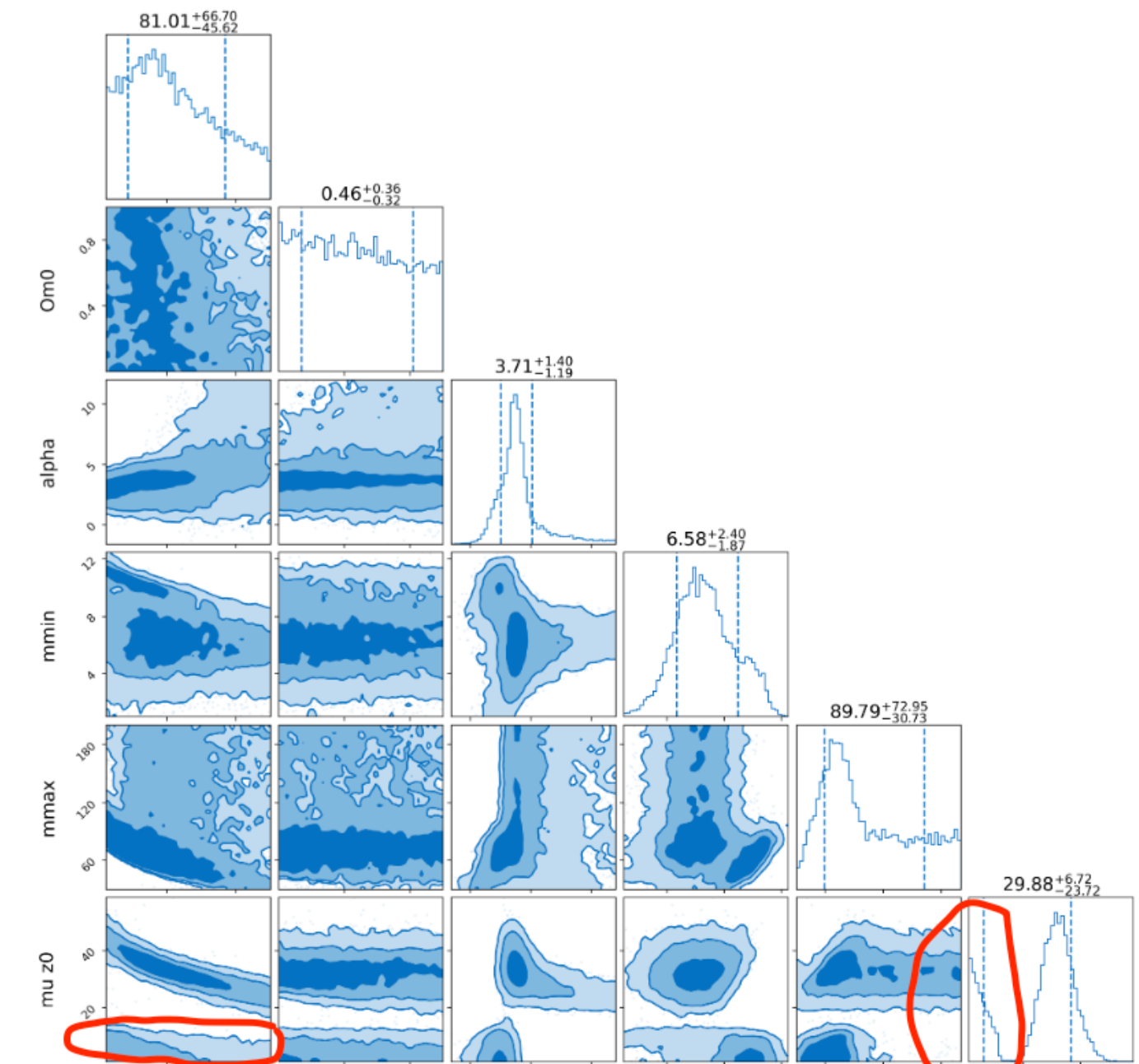
- We had to remove some 3PL events because of numerical stability. We checked that it does not affect the results (it is negligible wrt Poisson noise)

PLG results

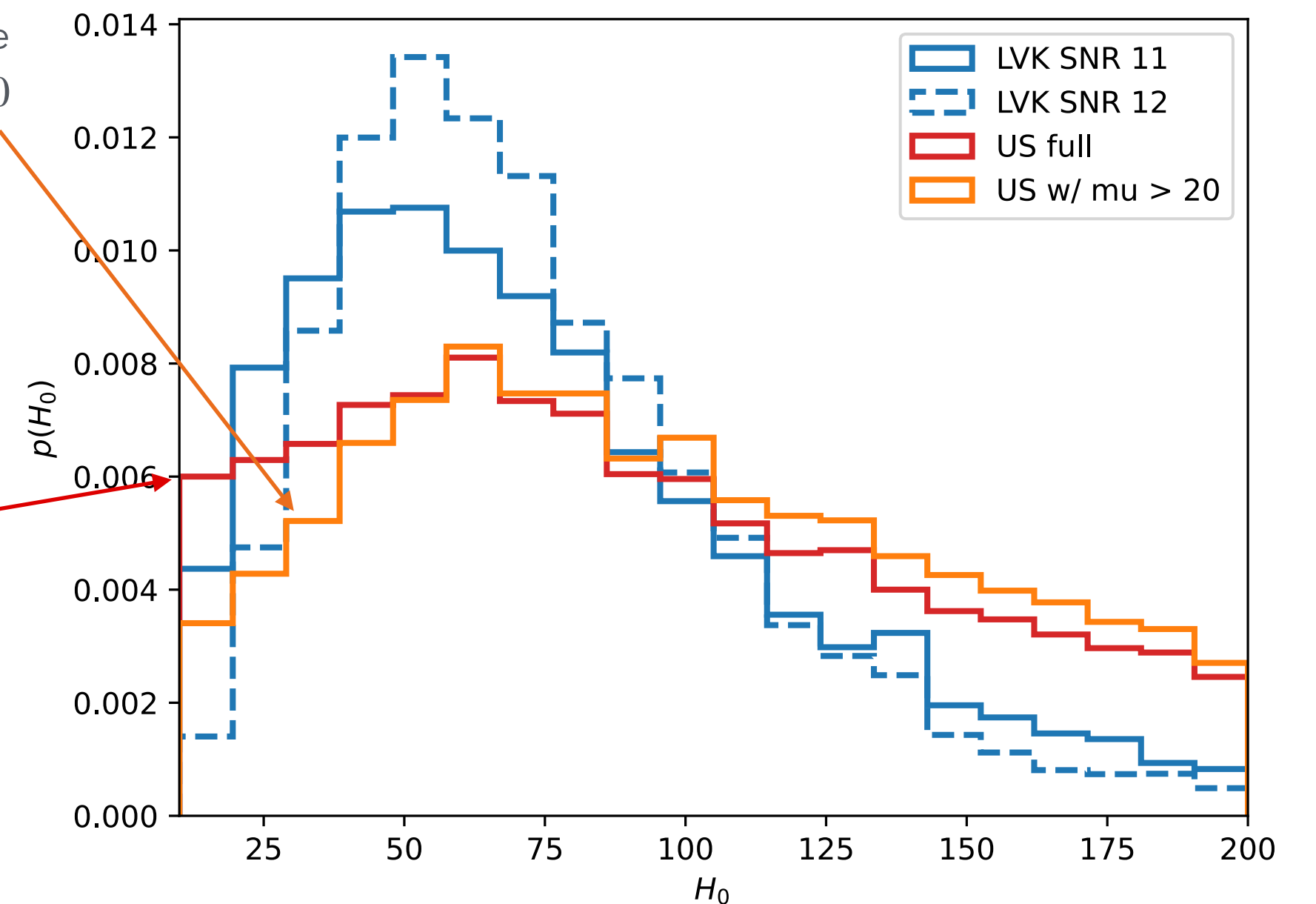
LVK's vs ours

We use :

- wider priors for some parameters ($\mu_g, m_{\min}, \dots$)
- different dataset (IFAR > 4yr, 50 events)



Our results removing the samples with $\mu_g < 20$



Additional checks

- **Stability of results** (in particular for 3PL)
- For O4 :
 - multiple realisations (estimate Poisson noise in the # of detected events)
 - deterministically sampled population