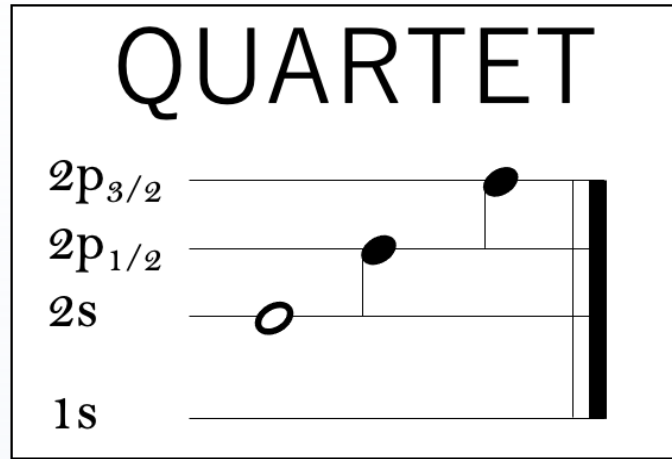


Mu4Rad: Muonic Atoms for Nuclear Radii

Lithium to Neon



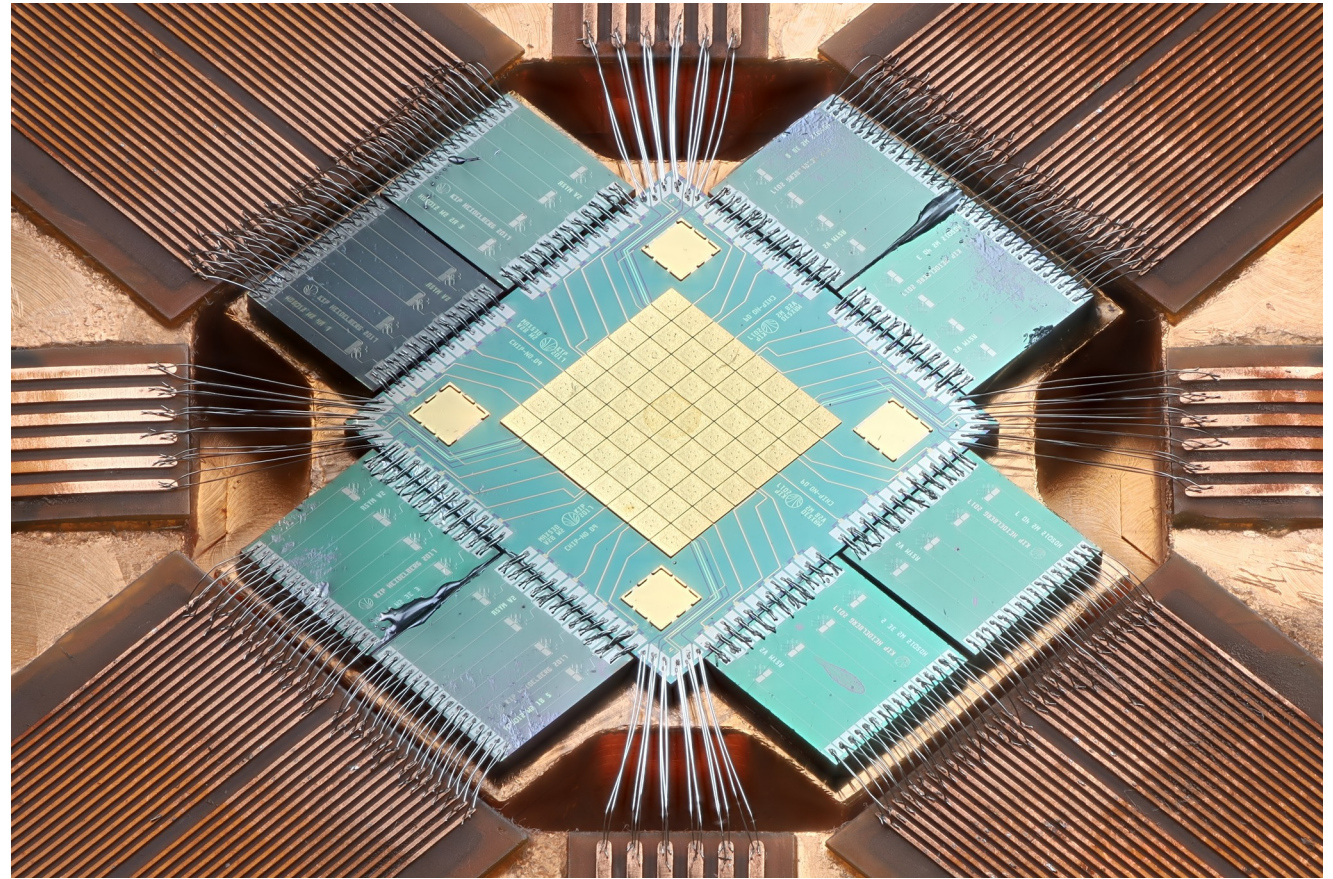
QUAntum inteRacTions with Exotic aToms

Randolf Pohl (JGU Mainz)

Nancy Paul (LKB Paris)

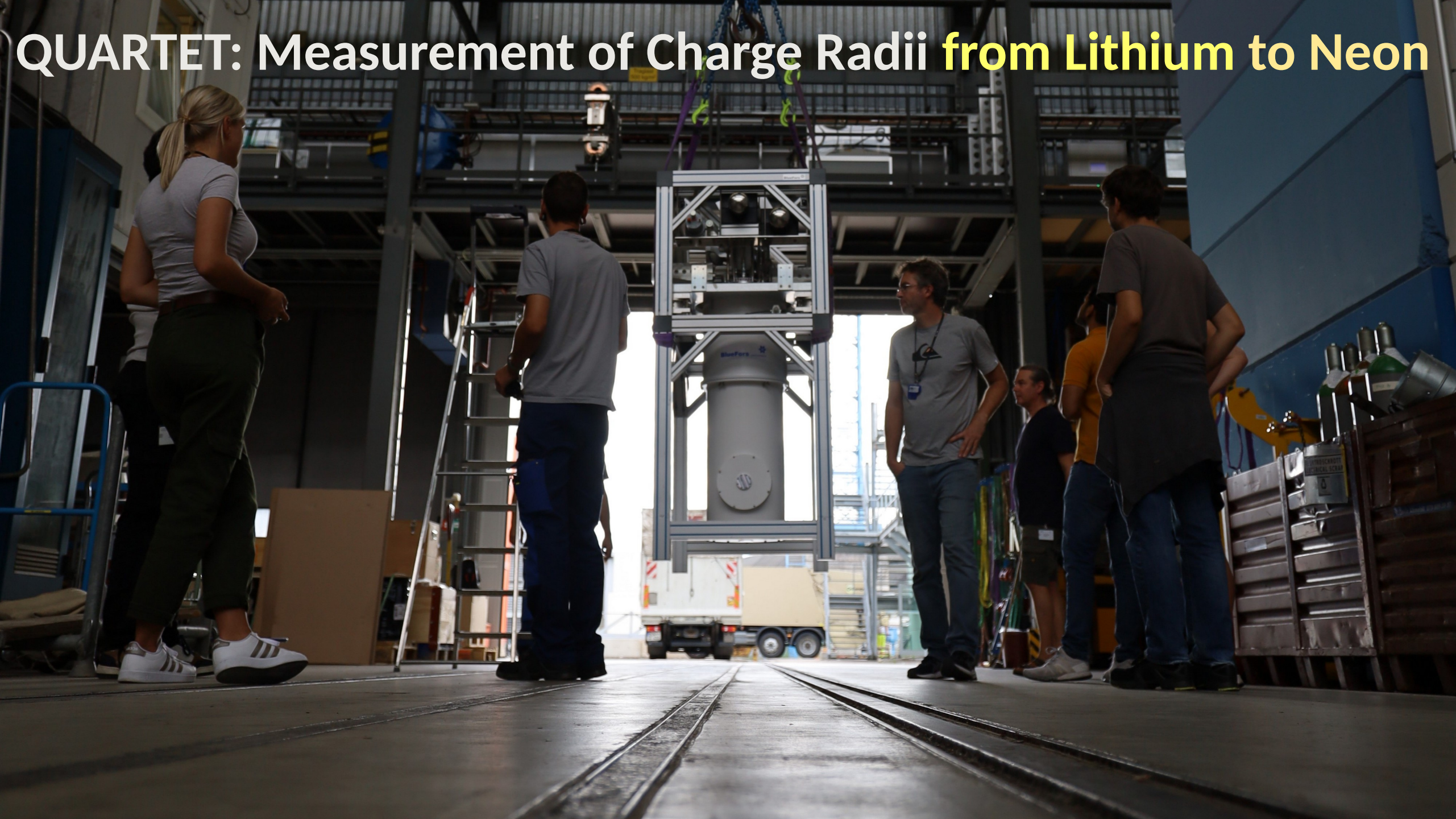
Ben Ohayon (Technion Haifa)

Loredana Gastaldo (KIP Heidelberg)

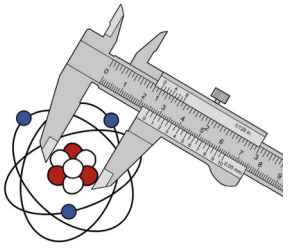


Metallic Magnetic Calorimeter (MMC)
maXs-30

QUARTET: Measurement of Charge Radii from Lithium to Neon

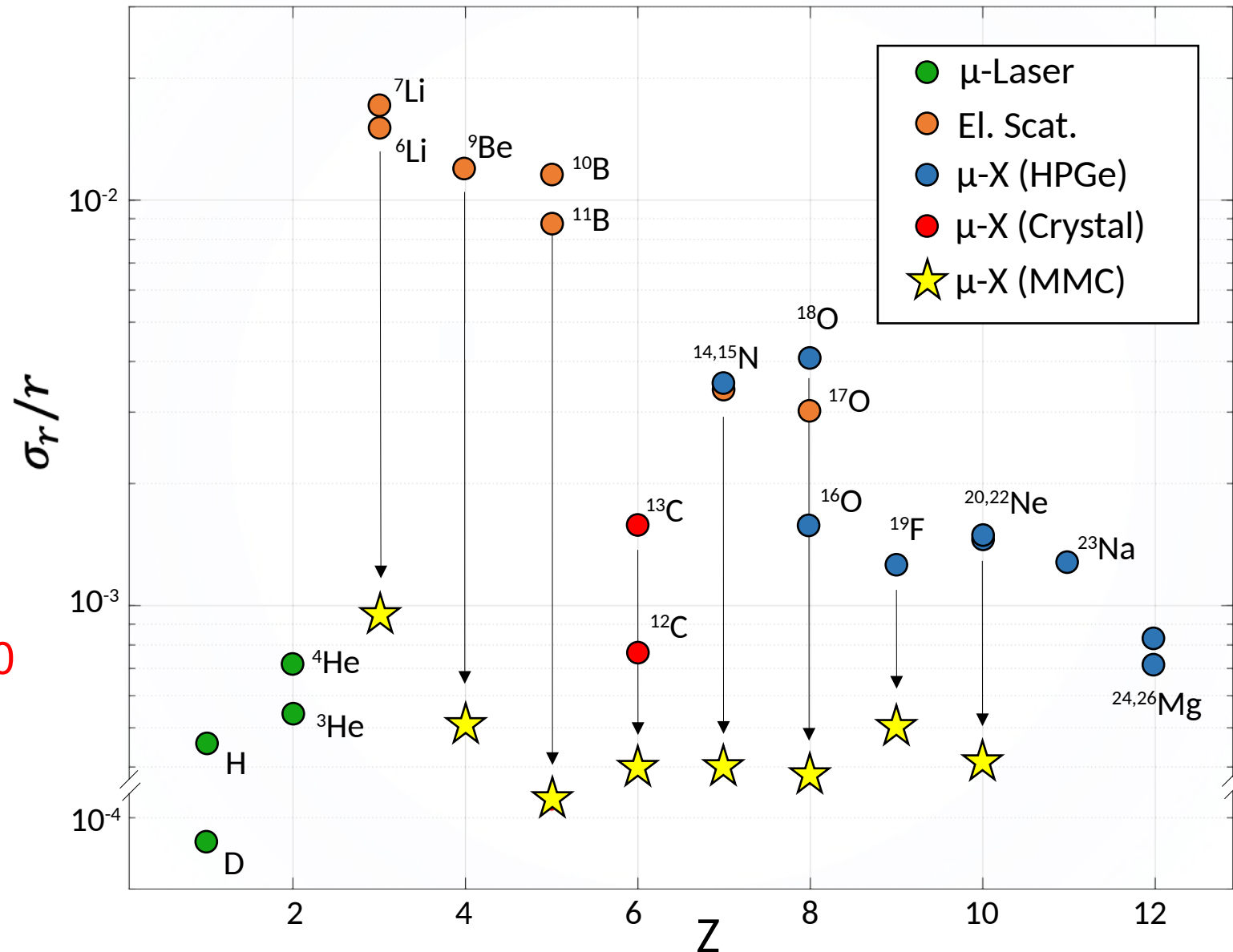


The QUARTET collaboration and precision goals



Goals

- Determine $E(2P-1S)$ for $3 \leq Z \leq 10$ with few ppm accuracy i.e. 0.2-1 eV .
- Improve radii by factor 3-10.



Why does it work?

Muonic atoms are highly sensitive to nuclear properties

Muonic atoms in a nutshell

Regular hydrogen:

Bohr radius $\sim 50'000 \times$ nuclear radius

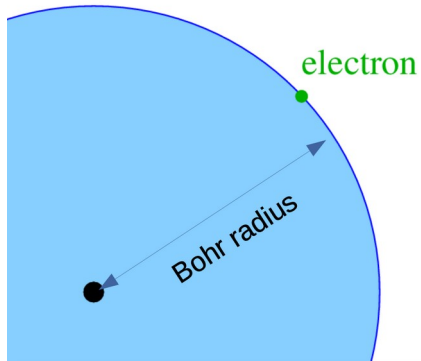
Muonic hydrogen:

Muon mass = **200** * electron mass

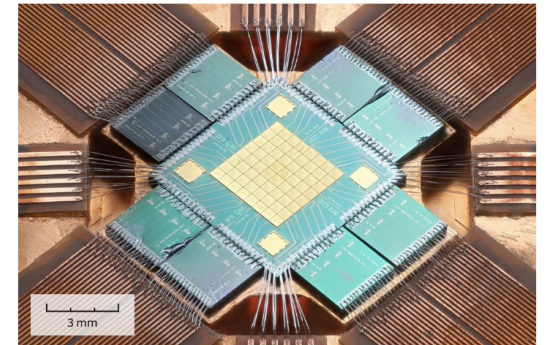
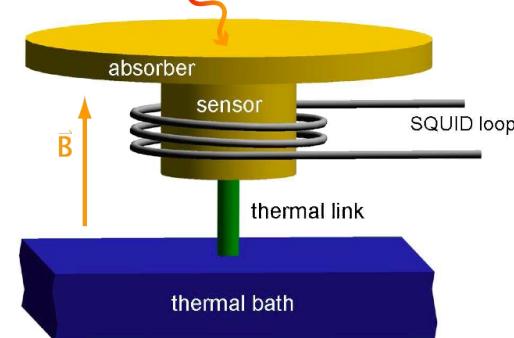
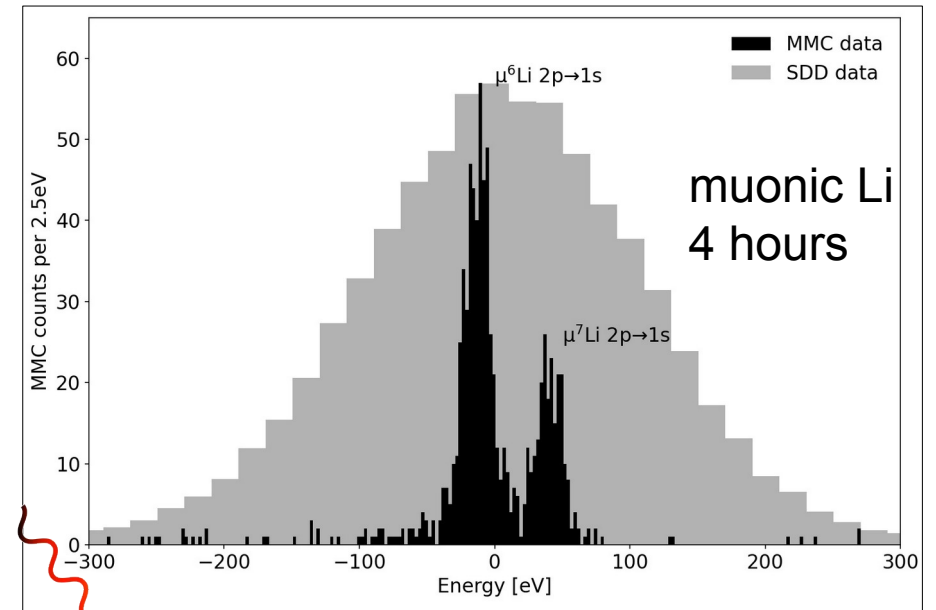
Bohr radius = **1/200** of H

200^3 = a **ten million times** more sensitive to nuclear size & structure

==> Our laser spectroscopy at **10^{-5}** level can compete with **10^{-12}** from normal atoms

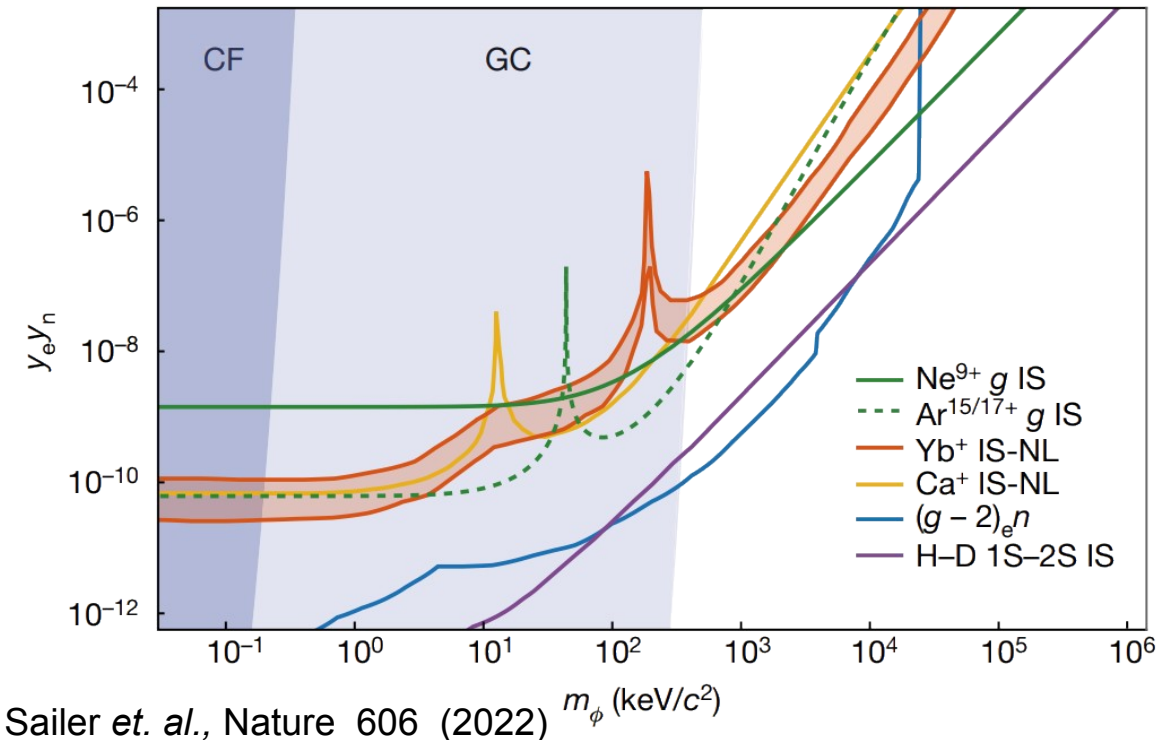
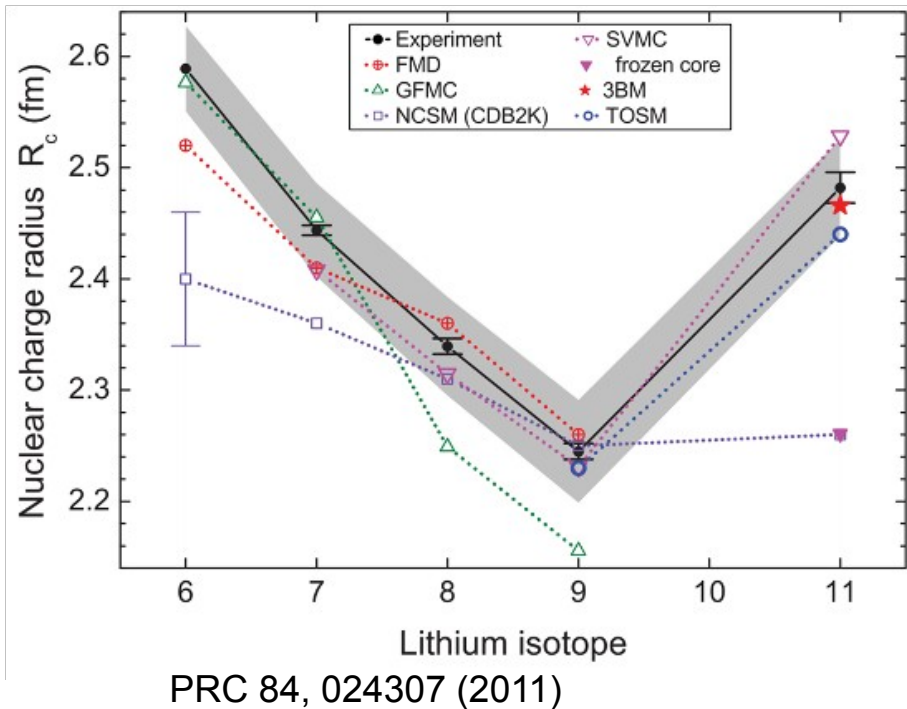


New quantum sensing microcalorimeter detectors
50X gain in intrinsic resolution for x rays



What are radii good for?

- **Absolute radius:**
 - calibrate entire chains, test nuclear chiral EFT
 - laser spectroscopy of helium-like Li to C: test QED & SM, determine fundamental constants
- **Isotope shifts:** compare electronic and muonic atoms to search for new lepton-neutron interactions
 - King plots, 1-electron g-factors



MMCs and ADCs

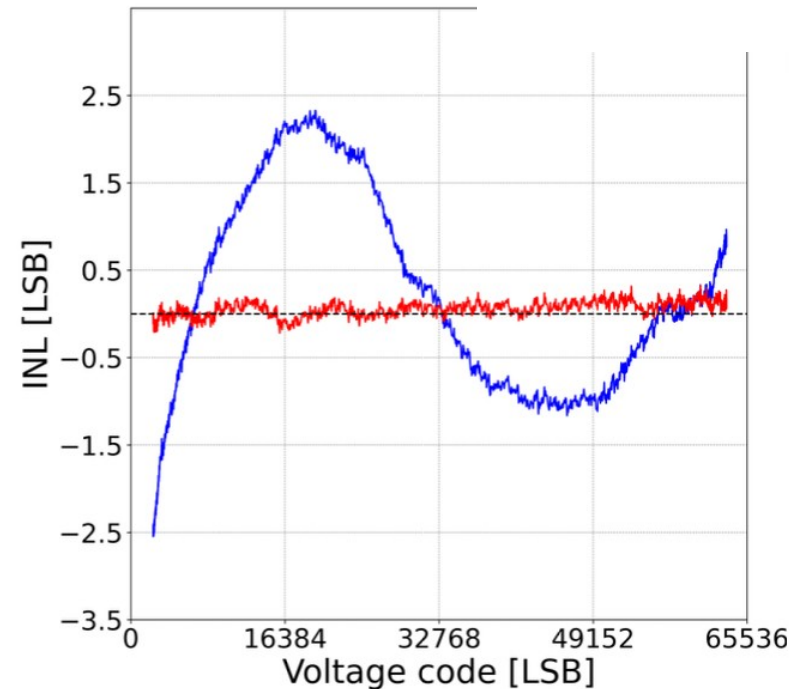
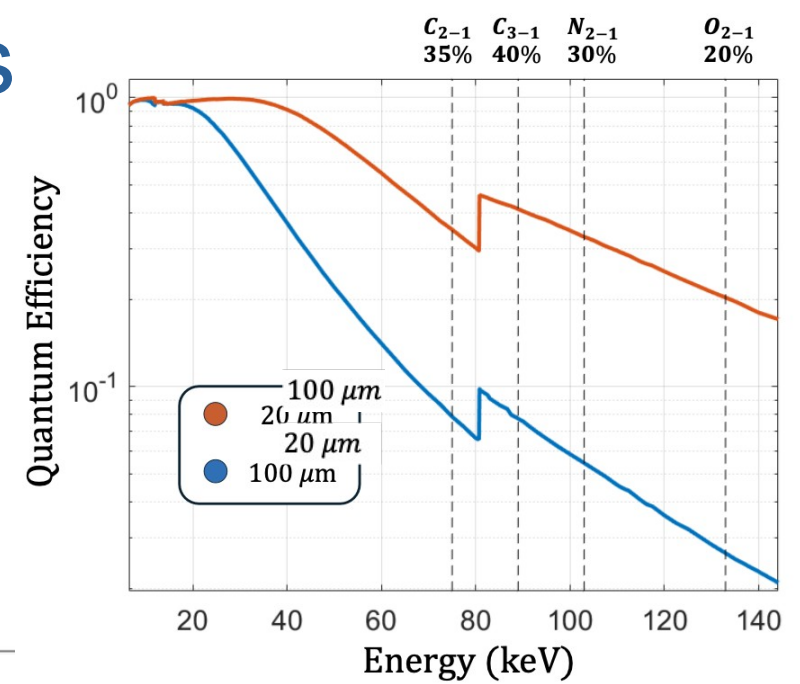
current MMCs are optimized for lower energy (lower Z)

→ Ne (207 keV) needs new detectors (100 μm thickness)

current ADCs (Struck SIS3316) introduce significant systematics:

”How much is 1 LSB worth?”

→ development SIS3315, 18 bit ADC,
(15 MSPS, 16channels)



Summary

QUARTET @ PSI aims at $\sim 10\times$ improved charge radii of the stable isotopes up to $Z=10$
→ anchor nucleus for isotope chains, nuclear physics, BSM, fundamental constants

1 PhD student (exp) for $Z=10$ (neon)

(DFG: 61,200 EUR p.a.)

50 kEUR for improved MMCs and SQUIDs (Heidelberg)

120 kEUR for improved 18-bit WFDs (Struck GmbH) with 18bit

280 kEUR travel support (beam times & analysis) → TNA for PSI?

30 kEUR for two workshops (detectors, nuclear theory)

dream: total 906 kEUR (incl. 25% indirect costs)

Backup

Comprehensive theory of the Lamb shift in light muonic atoms

K. Pachucki,¹ V. Lensky,² F. Hagelstein,^{2,3} S. S. Li Muli,² S. Bacca,^{2,4} and R. Pohl⁵

¹*Faculty of Physics, University of Warsaw, Pasteura 5, 02-093 Warsaw, Poland*

²*Institut für Kernphysik, Johannes Gutenberg-Universität Mainz, 55128 Mainz, Germany*

³*Paul Scherrer Institut, CH-5232 Villigen PSI, Switzerland*

⁴*Helmholtz-Institut Mainz, Johannes Gutenberg Universität Mainz, 55099 Mainz, Germany*

⁵*Institut für Physik, Johannes Gutenberg-Universität Mainz, 55099 Mainz, Germany*

(Dated: May 19, 2023) Rev. Mod. Phys. **96** (2024) 1, 015001

E_{QED}	point nucleus	206.034 4(3)	228.774 0(3)	1644.348(8)	1668.491(7)
$\mathcal{C} r_C^2$	finite size	$-5.225\,9\,r_p^2$	$-6.107\,4\,r_d^2$	$-103.383\,r_h^2$	$-106.209\,r_\alpha^2$
E_{NS}	nuclear structure	0.028 9(25)	1.750 3(200)	15.499(378)	9.276(433)
$E_L(\text{exp})$	experiment ^a	202.370 6(23)	202.878 5(34)	1258.598(48)	1378.521(48)
r_C	this work	0.840 60(39)	2.127 58(78)	1.970 07(94)	1.678 6(12)
r_C	previous ^a	0.840 87(39)	2.125 62(78)	1.970 07(94)	1.678 24(83)

μH:

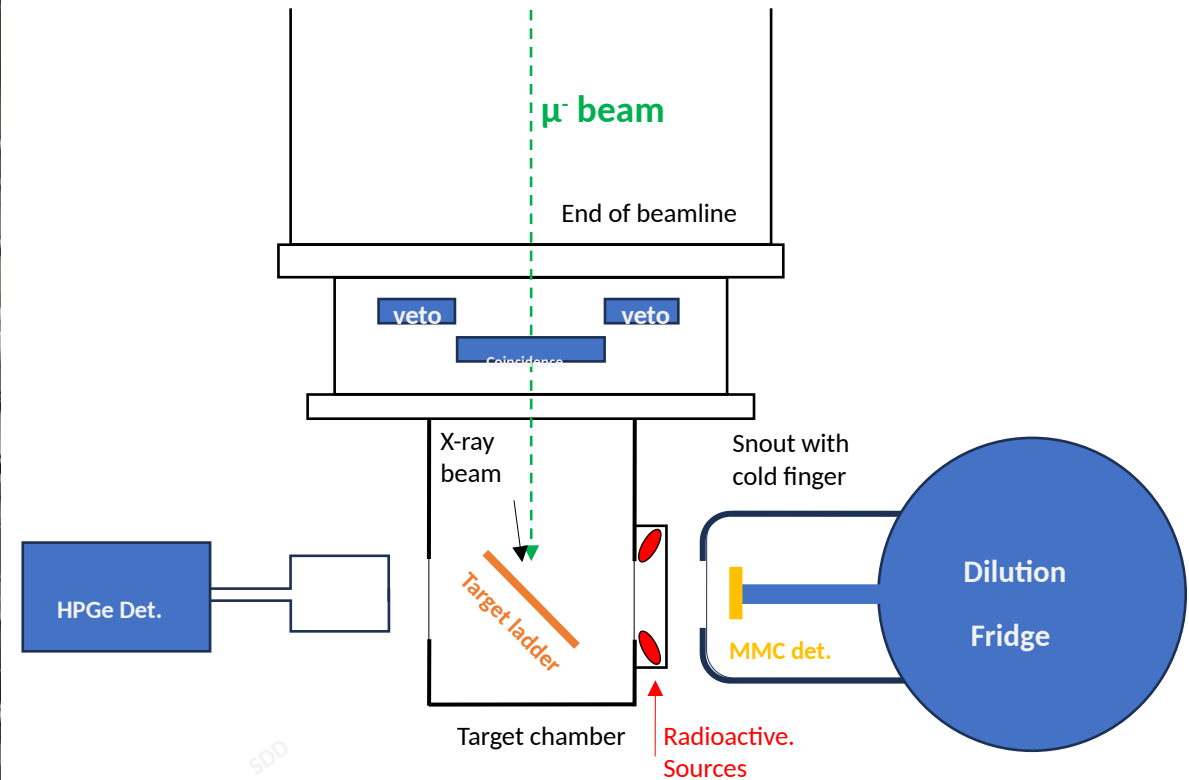
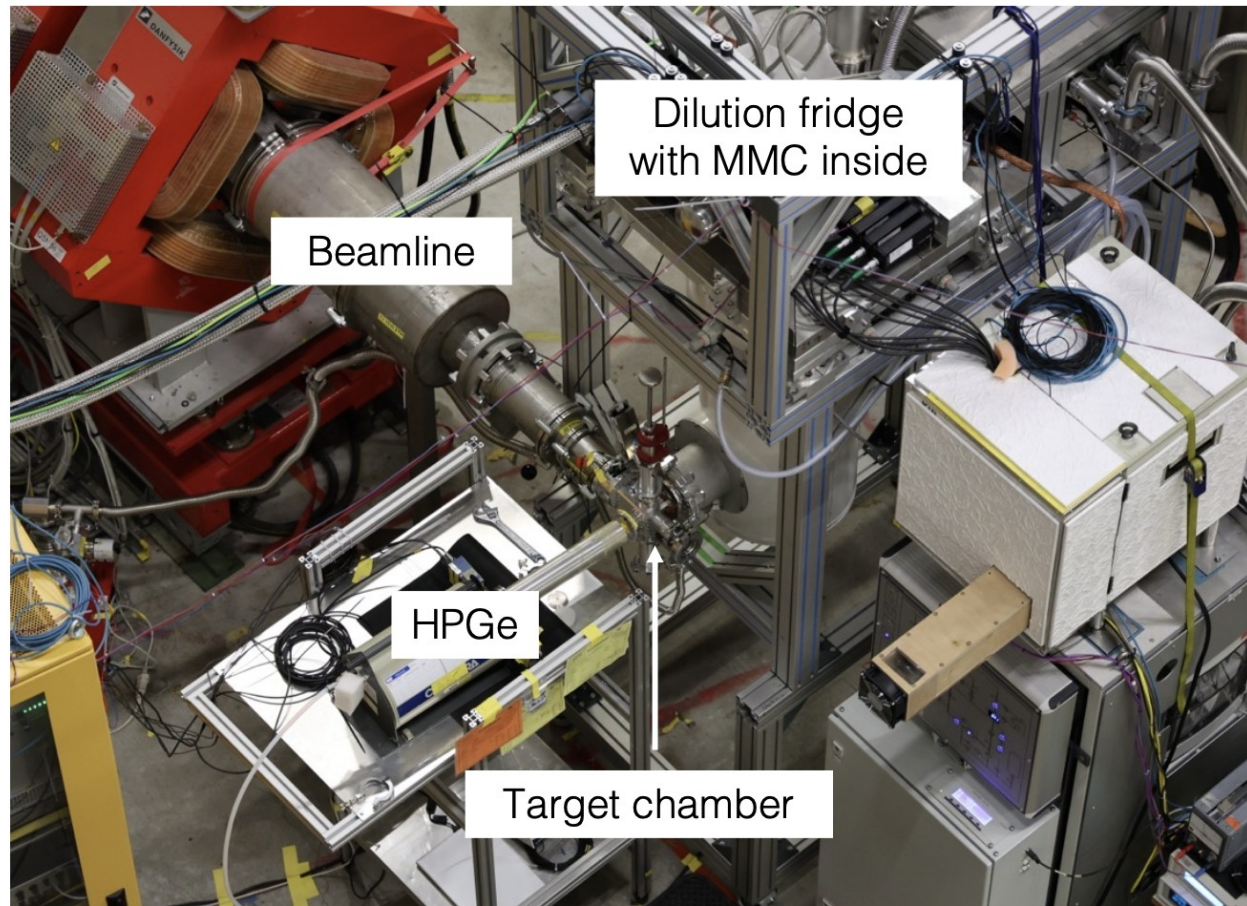
present accuracy comparable with experimental precision

μD, μ³He⁺, μ⁴He⁺:

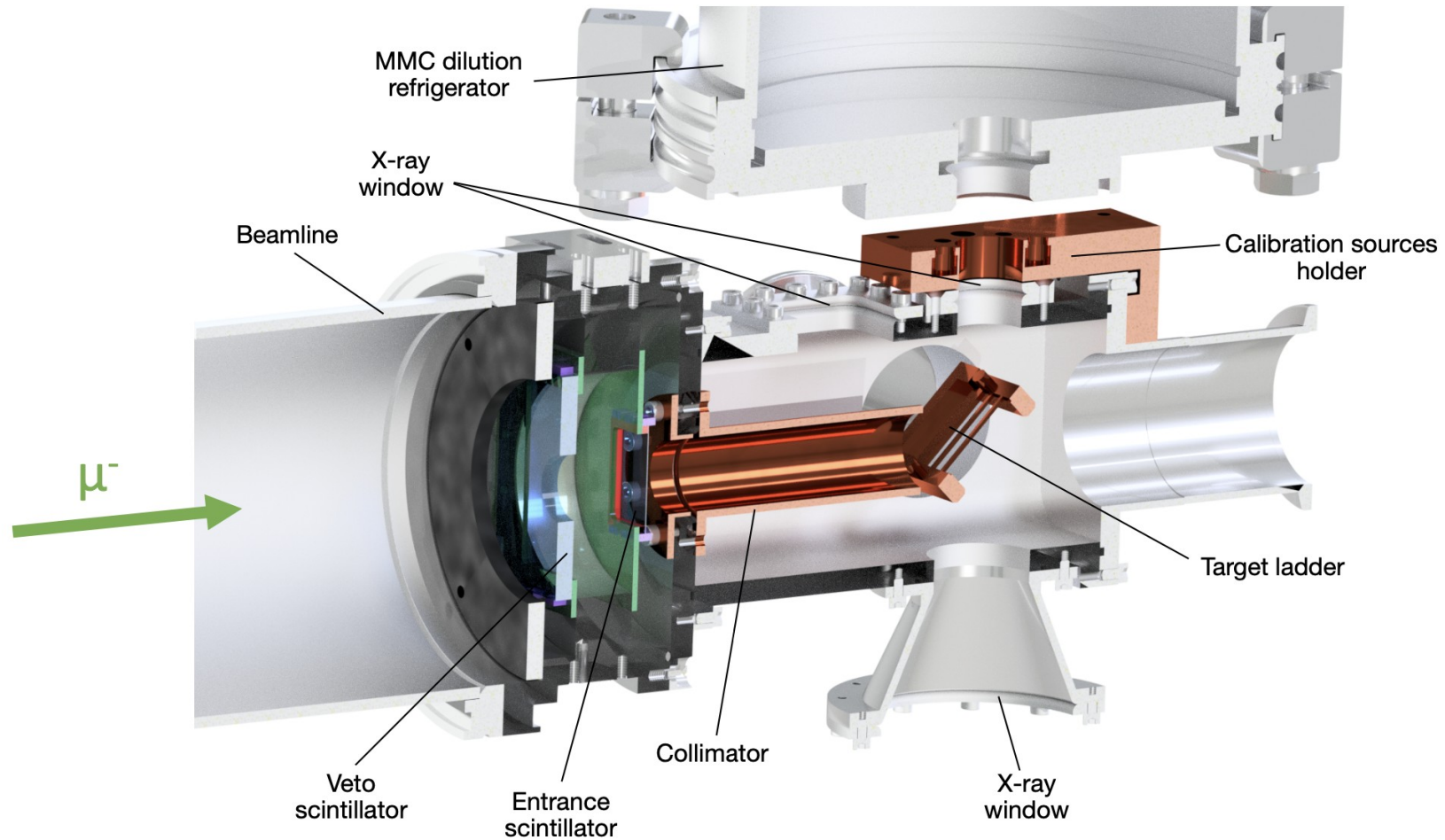
present accuracy factor 5-10 worse than experimental precision

- Experiments will improve by up to a factor of 5
- Theoretical improvement needed for nuclear/nucleon 2- and 3-photon exchange

The QUARTET experimental setup—2024

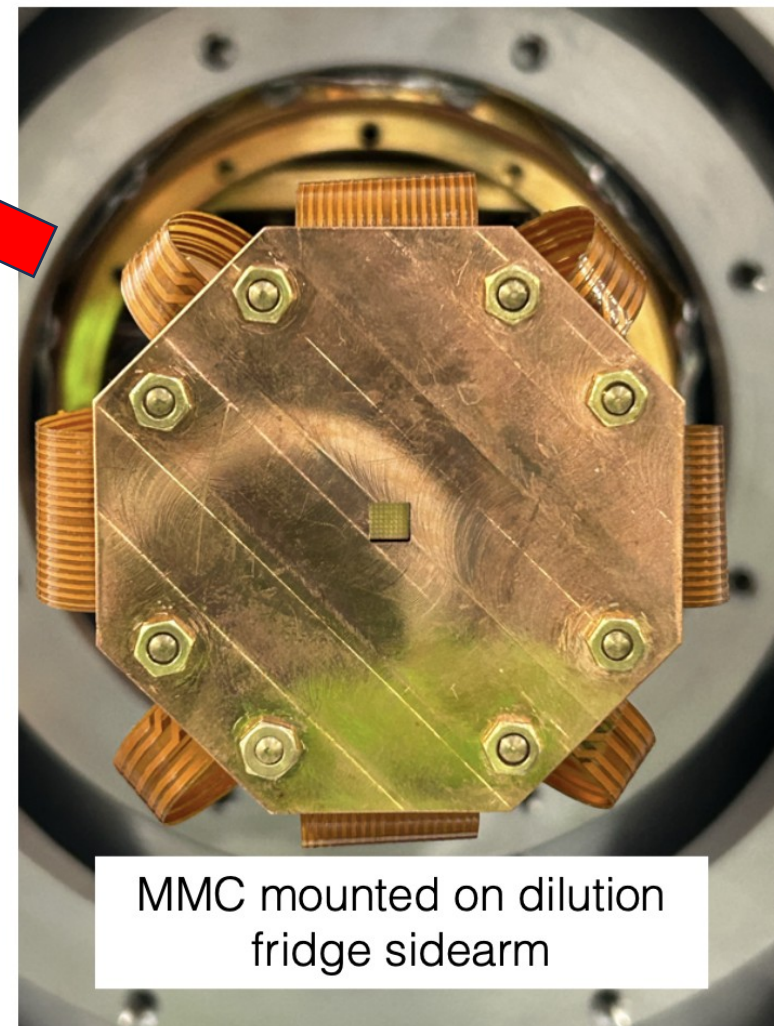
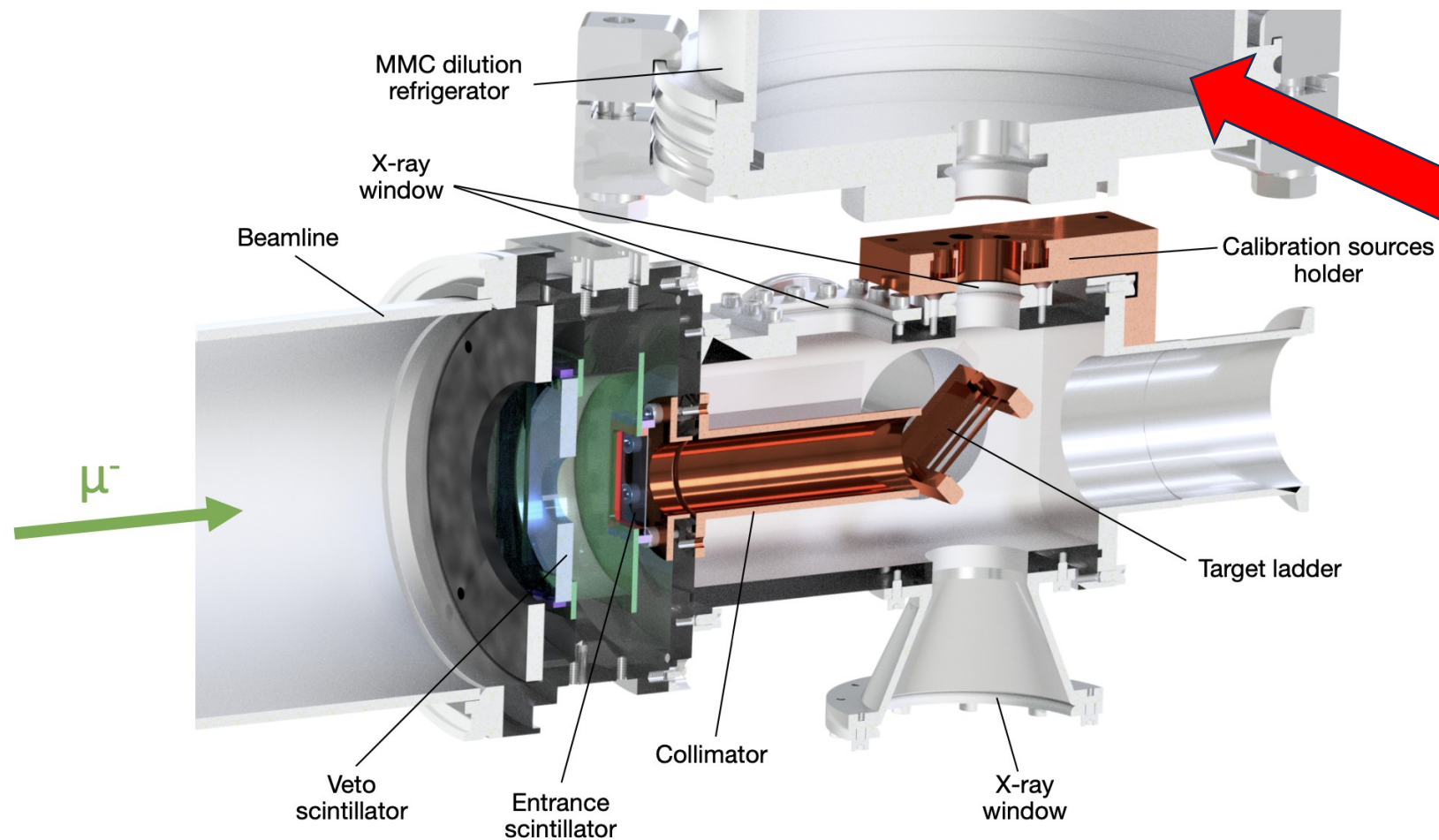


The QUARTET experimental setup—2024

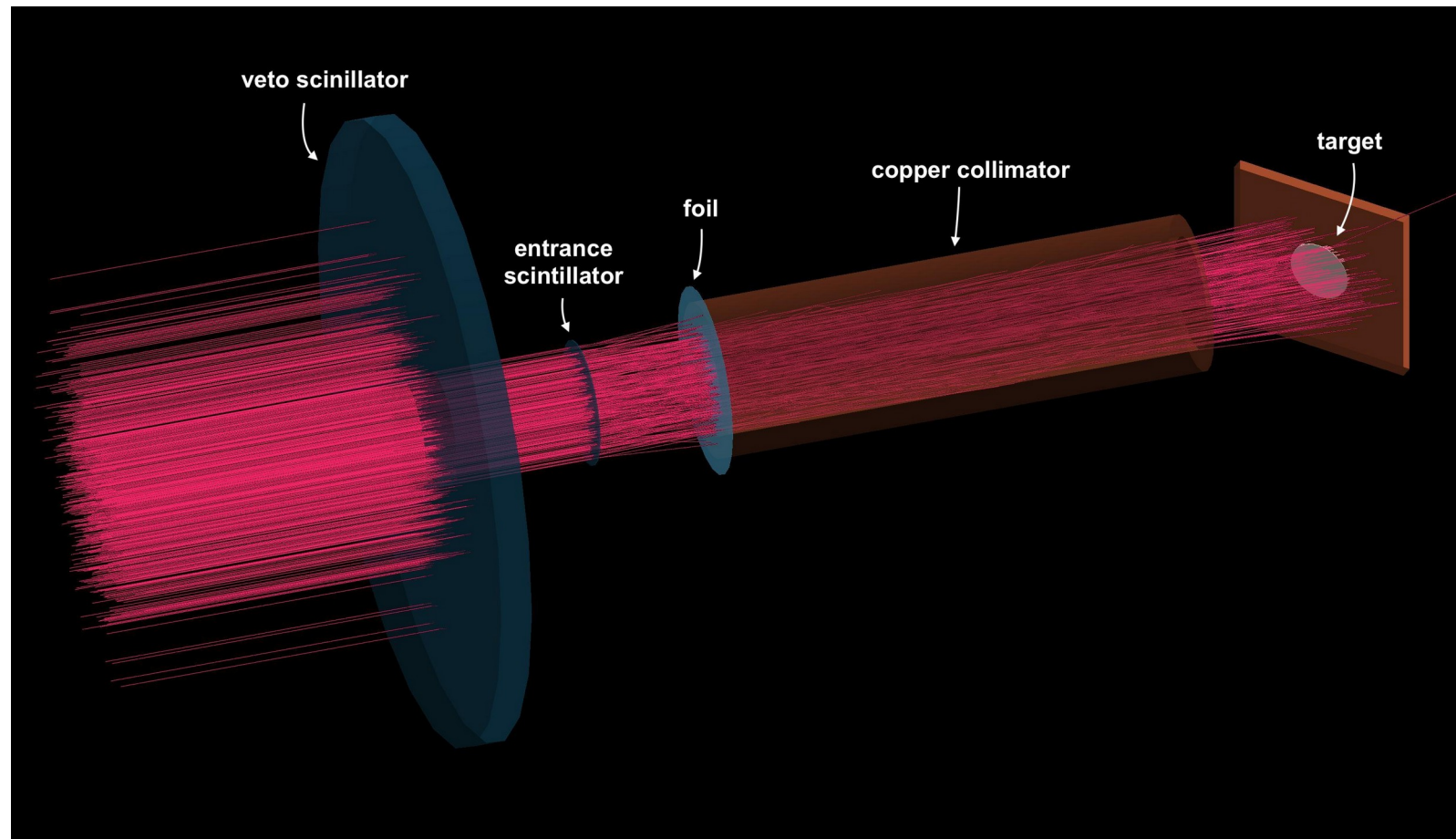


(View from below)

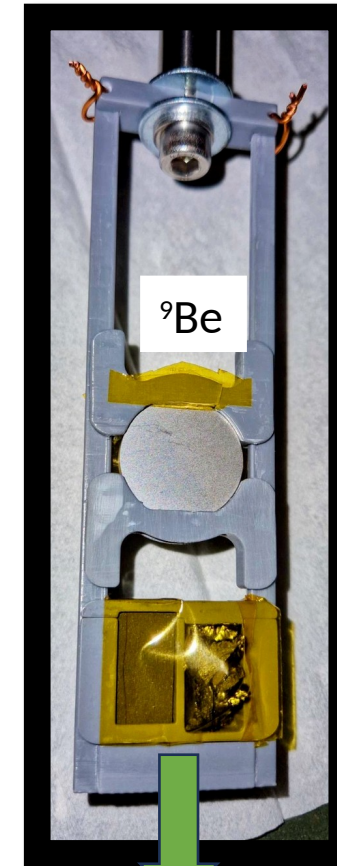
The QUARTET experimental setup—2024



Muon beam and 2024 targets

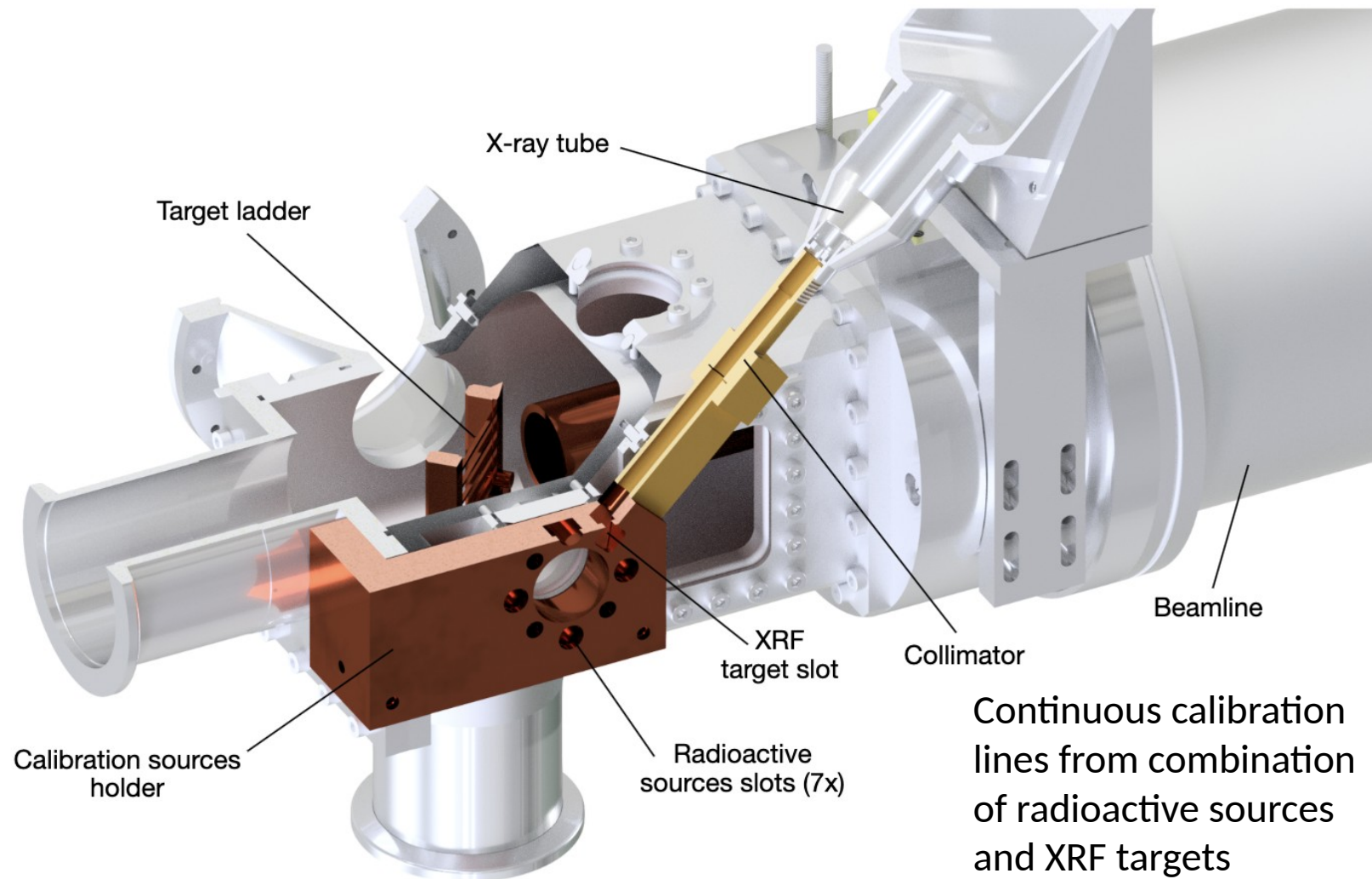


*Many thanks to Dieter Ries and
the PSI neutron group !*

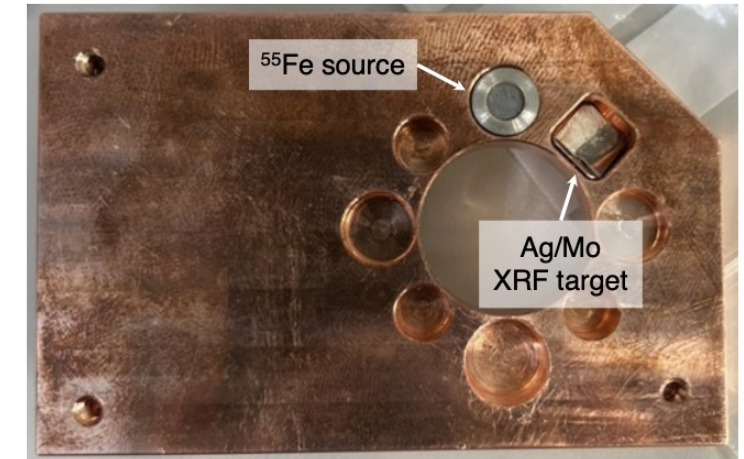


natB , ^{10}B (obtained
from PSI)

Calibration—combination of XRF and gamma-ray standards

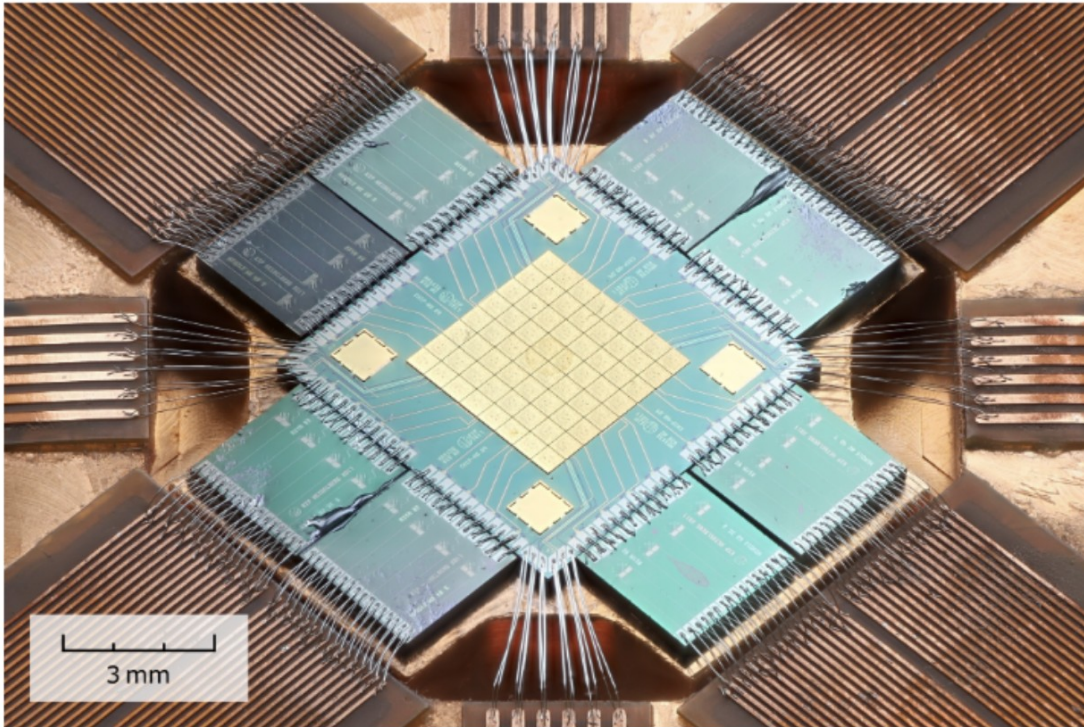


Continuous calibration lines from combination of radioactive sources and XRF targets

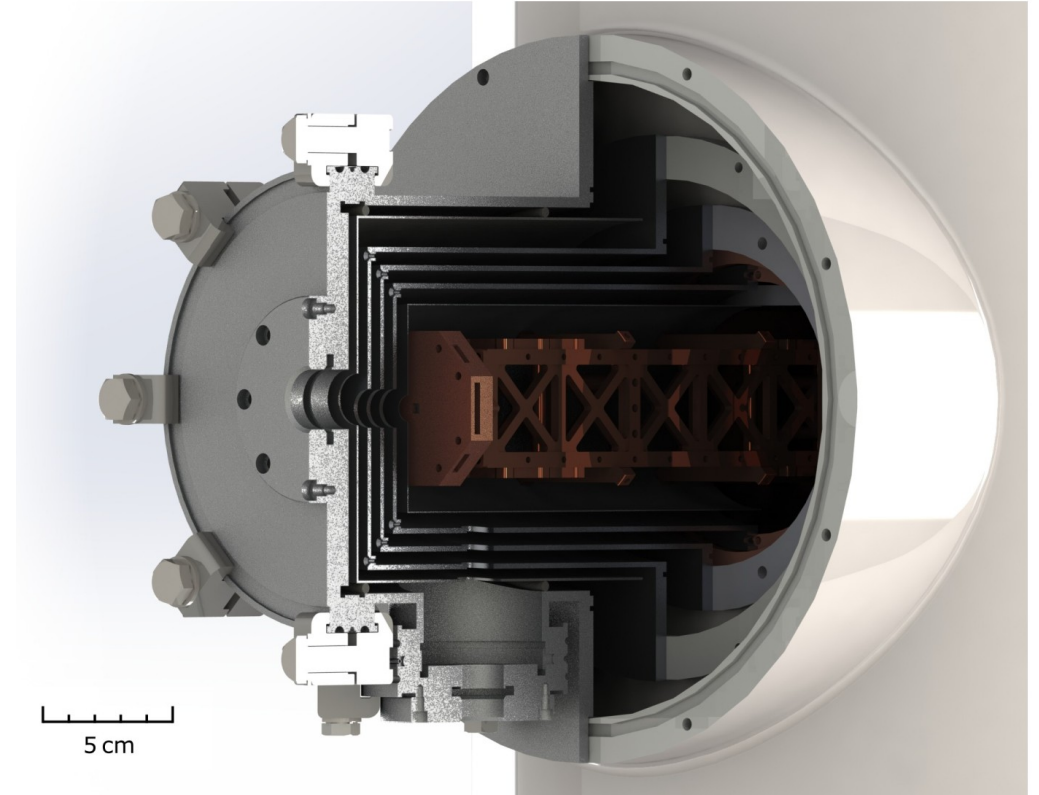


Many thanks to PSI radiochemistry for the ^{133}Ba source !

The QUARTET detector

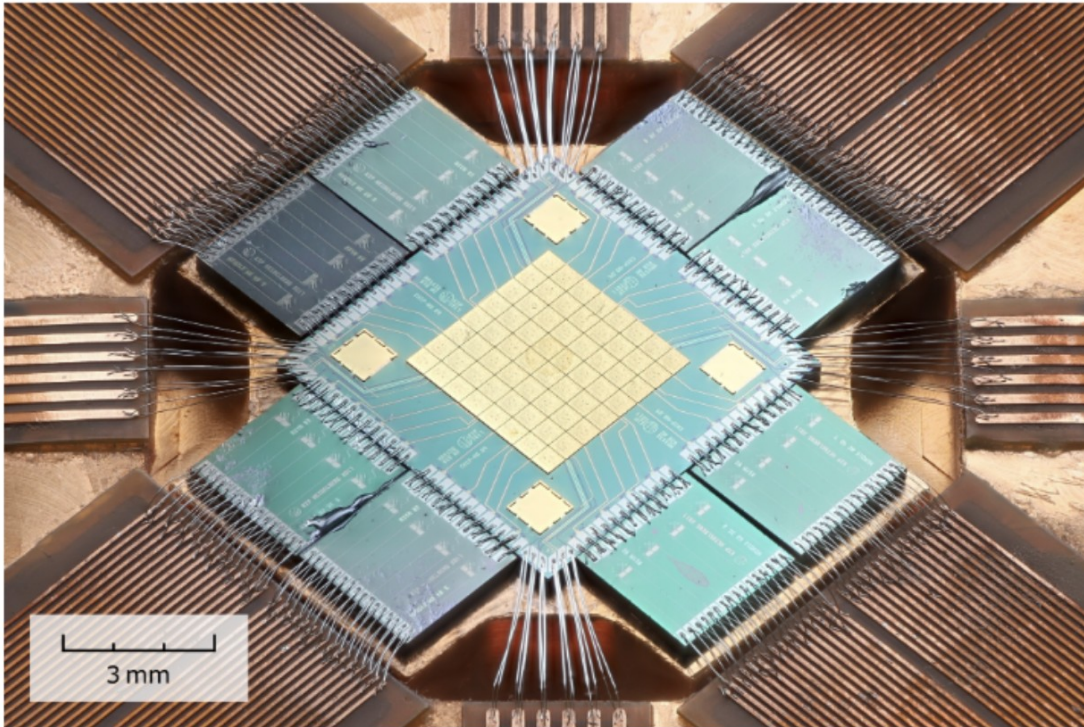


- 64 pixel maX-30 MMC detector, *developed for IAXO experiment*
- Mounted in custom sidearm designed to reduce vibrations
- 5 thermal shields and x-ray windows
- Calibration sources mounted outside the detector

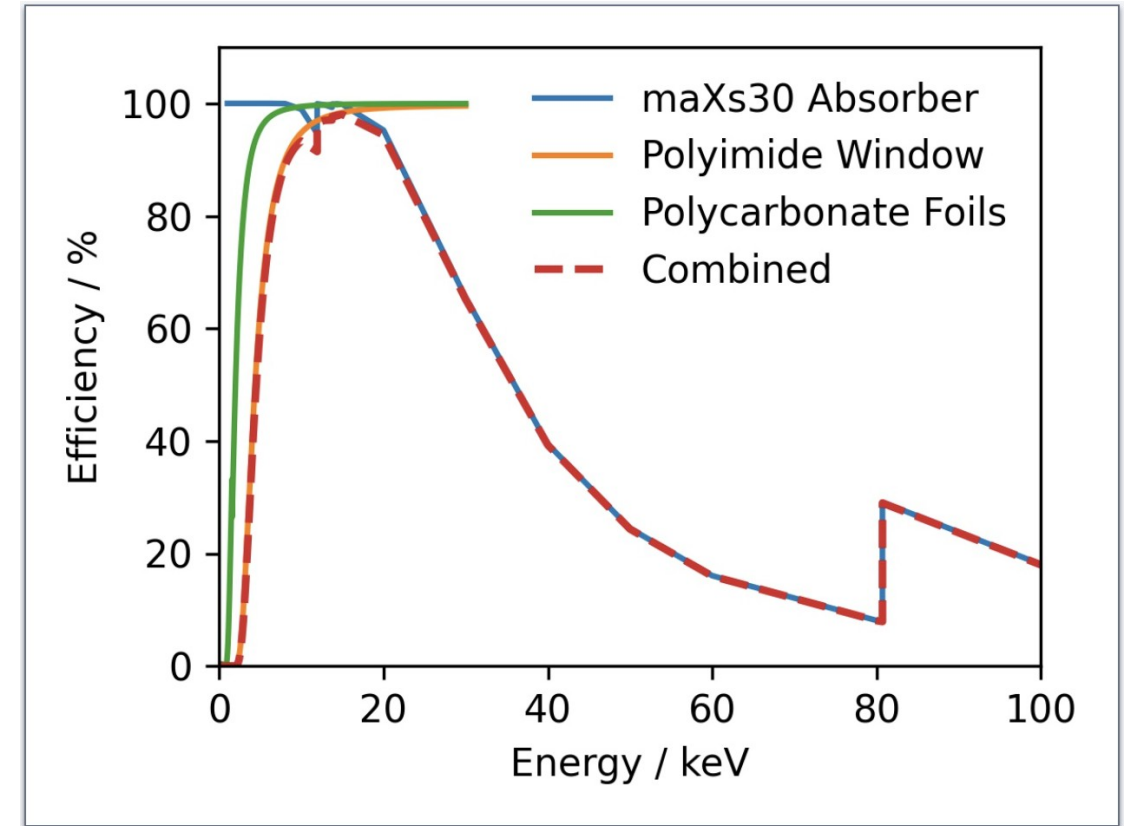


Figures from D. Unger et al LTD2023 proceeding, for the QUARTET collaboration

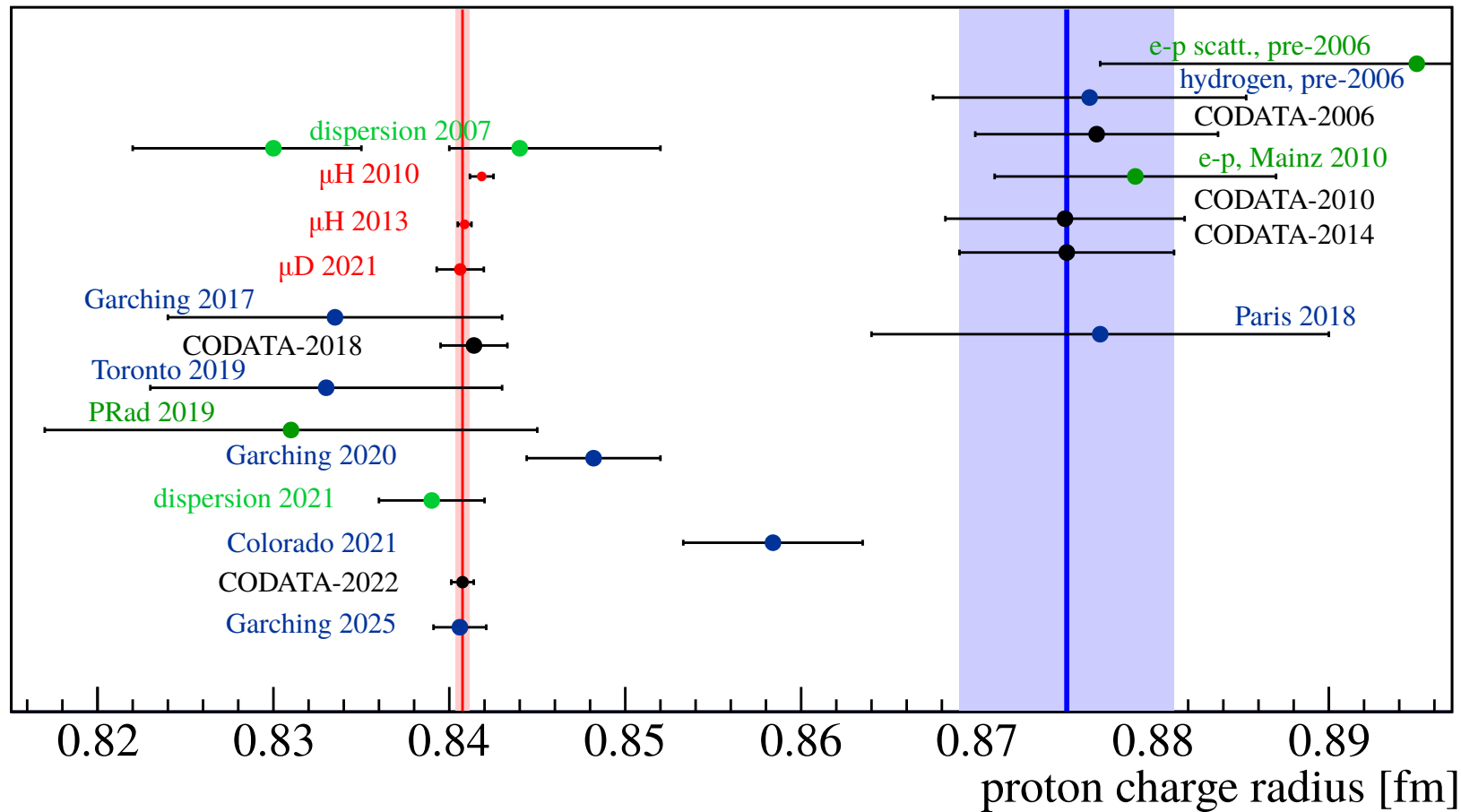
The QUARTET detector



- 64 pixel maX-30 MMC detector, *developed for IAXO experiment*
- Mounted in custom sidearm designed to reduce vibrations
- 5 thermal shields and x-ray windows
- Calibration sources mounted outside the detector



Muonic Hydrogen and the Proton CHARGE Radius



e-p scattering
slope of G_E at $Q^2 = 0$

$$r_p^2 \equiv -6 \left. \frac{dG_E}{dQ^2} \right|_{Q^2=0}$$

hydrogen spectroscopy
muonic atoms
Lamb shift

$$\Delta E = \frac{2}{3} \pi \alpha |\Psi_S(0)|^2 r_p^2$$

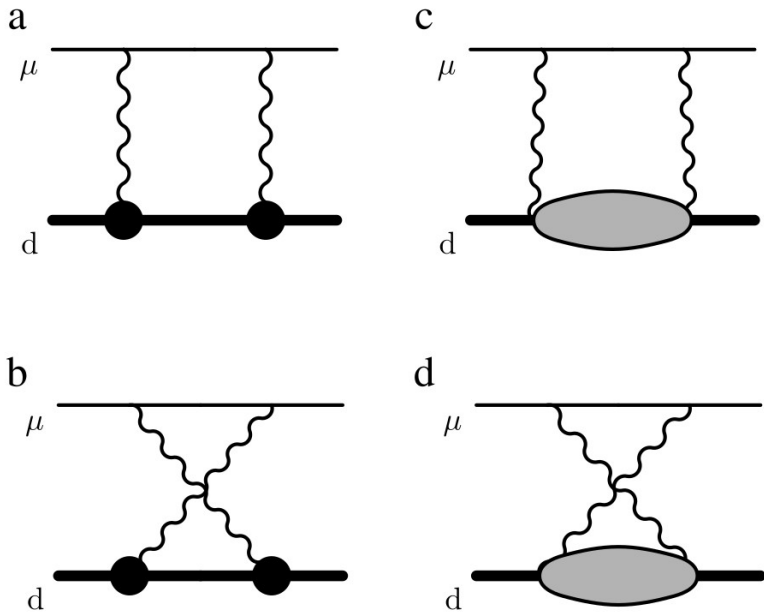
CODATA / PDG average

Theory: Lamb shift in muonic D

$$\Delta E_{\text{Lamb}}^{\mu\text{D}} = 228.7740 (3) \text{ meV}_{\text{QED}} + 1.7503 (200) \text{ meV}_{\text{TPE}} - 6.1074 \text{ meV/fm}^2 * R_d^2$$

$$\Delta E_{\text{LS}}^{\text{exp}} = 202.8785(31)_{\text{stat}}(14)_{\text{syst}} \text{ meV}$$

Nuclear structure **two (and three!)-photon contributions** to the Lamb shift in muonic deuterium.



Pachucki, RP et al, arXiv 2212.13782

see also Krauth, RP et al. (2016) using calculations from Pachucki (2011), Friar (2013), Carlson, Gorchtein, Vanderhaeghen (2014), Hernandez et al. (2014), Pachucki + Wienczek (2015)

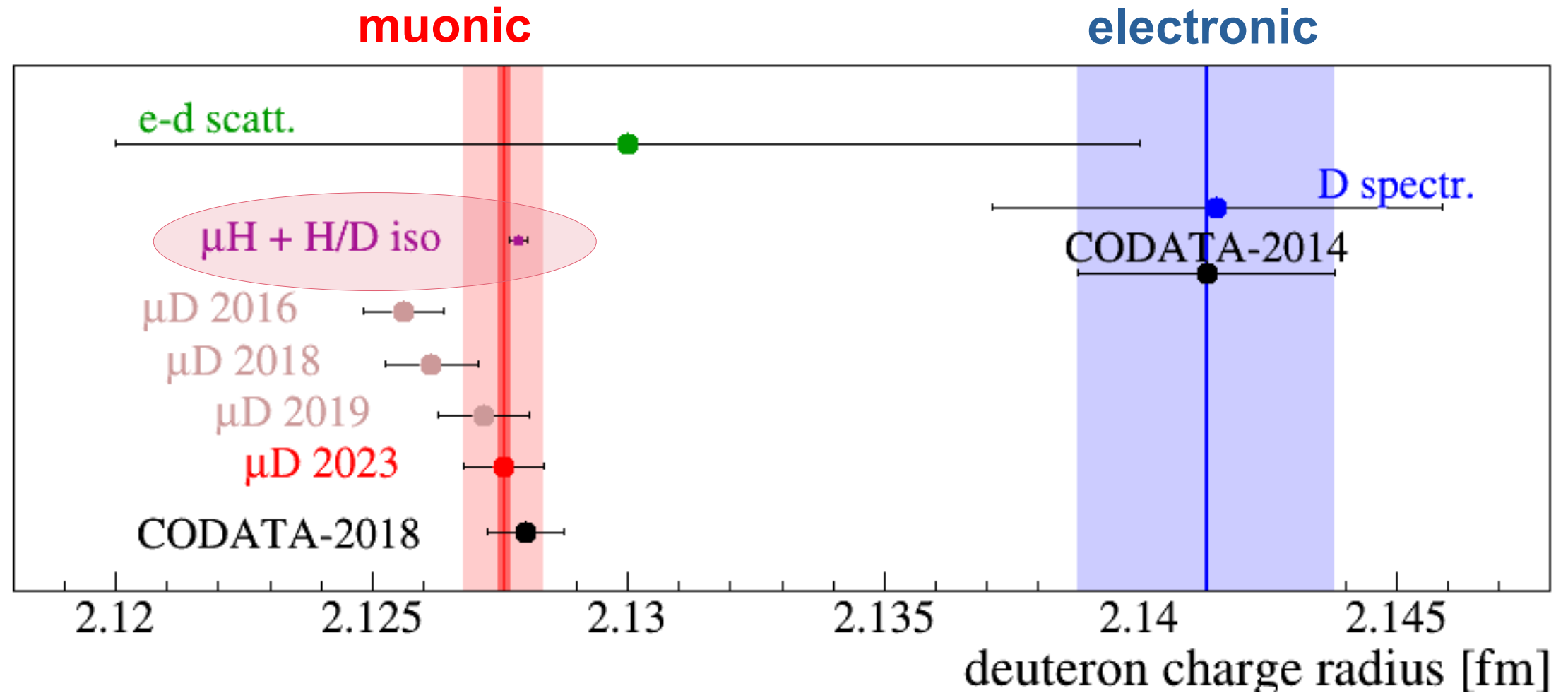
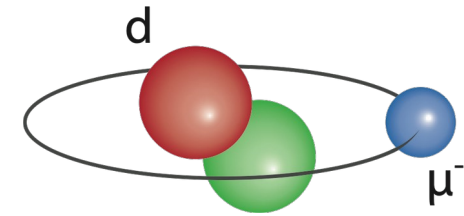
+ Pachucki et al., PRA 97, 062511 (2018): Sizeable three-photon !!

+ Hernandez et al., PLB 778, 377 (2018): χEFT

+ Kalinowski (2019): eVP to nucl. struct.

+ Acharya et al., PRC 103, 024001 (2021)
 χEFT + Dispersion relations

Muonic Deuterium



μD : $2.12758 \text{ (13)}_{\text{exp}} \text{ (78)}_{\text{theo}} \text{ fm}$

$\mu\text{H} + \text{H/D(1S-2S)}$: $2.12785 \text{ (17)} \text{ fm}$

Theory in muonic D

$$\Delta E_{\text{Lamb}}^{\mu\text{D}} = 228.7740 (3) \text{ meV}_{\text{QED}} + 1.7503 (200) \text{ meV}_{\text{TPE}} - 6.1074 \text{ meV/fm}^2 * R_d^2$$

$\Delta E_{\text{TPE}} (\text{theo}) = 1.7503 \pm 0.0200 \text{ meV}$ **Bacca group**
vs. $\pm 0.0034 \text{ meV}$ **experimental uncertainty**

(1) **charge radius**, using **calculated TPE**

$$r_d (\mu\text{D}) = 2.12758 (13)_{\text{exp}} (78)_{\text{theo}} \text{ fm}$$

(2) **polarizability**, using **charge radius from isotope shift**

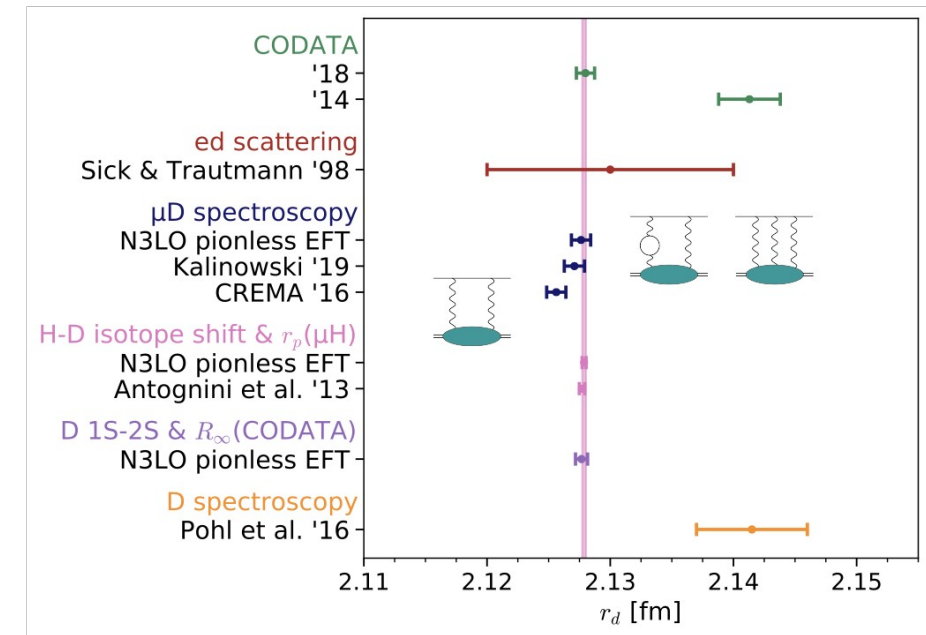
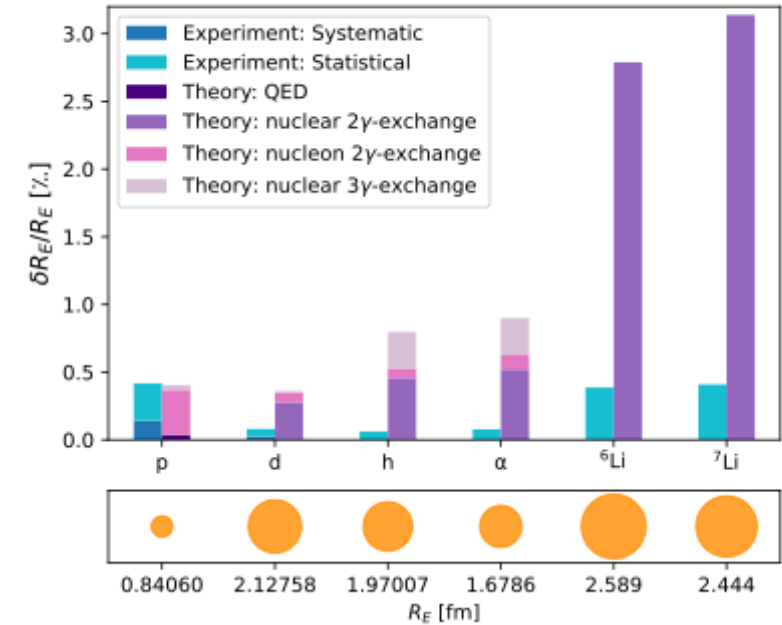
$$\Delta E_{\text{TPE}} (\text{theo}) = 1.7503 (200) \text{ meV vs.}$$

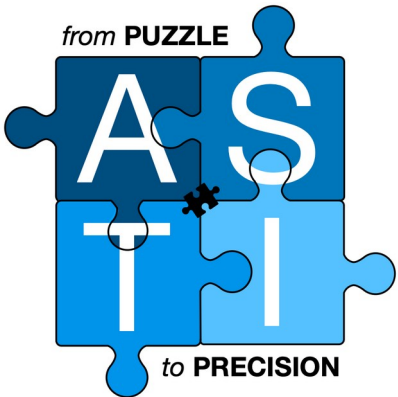
$$\Delta E_{\text{TPE}} (\text{exp}) = 1.7591 (59) \text{ meV} \quad 3\text{x more accurate}$$

Muonic Deuterium Lamb Shift

- ❑ Deuteron (proton) charge radius extractions from μH & μD Lamb shift, and 1S-2S H-D isotope shift are consistent
- ❑ Higher-order radiative corrections are important
 - Nuclear and nucleon two-photon exchange (2γ)
 - Three-photon exchange (3γ)
 - Radiative corrections to 2γ , e.g., electron vacuum polarization
- ❑ Extraction of nuclear structure from atomic spectroscopy factor 4 more precise than (chiral and pionless) EFT predictions or data-driven evaluations
 - Experiment as benchmark for nuclear theory

Error Budget of Nuclear Charge Radii





Muonic Atom Spectroscopy Theory Initiative

<https://asti.uni-mainz.de>

- ❑ Coordinated effort to support the experiments (inspired by “Muon g-2 Theory Initiative”)
- ❑ Initial objectives:
 - Accurate theory predictions for light muonic atoms to test fundamental interactions by comparing to electronic atoms
 - Community consensus on SM predictions
 - Emphasis on the hyperfine splitting in μH
- ❑ Steering committee: Aldo Antognini (PSI), Carl Carlson (William & Mary), Franziska Hagelstein (Mainz), Paul Indelicato (CNRS), Krzysztof Pachucki (Warschau), Vladimir Pascalutsa (Mainz)
- ❑ So far 5 (satellite-)workshops @ PSI, Crete, Mainz, Stony Brook, ETH Zurich
- ❑ Next workshop: “New perspectives in the charge radii determination of light nuclei”, ECT* Trento, 28.07.25 — 01.08.25