

Long-Lived Particles at Spallation Neutron Sources

Salvador Urrea

arXiv:2509.14085

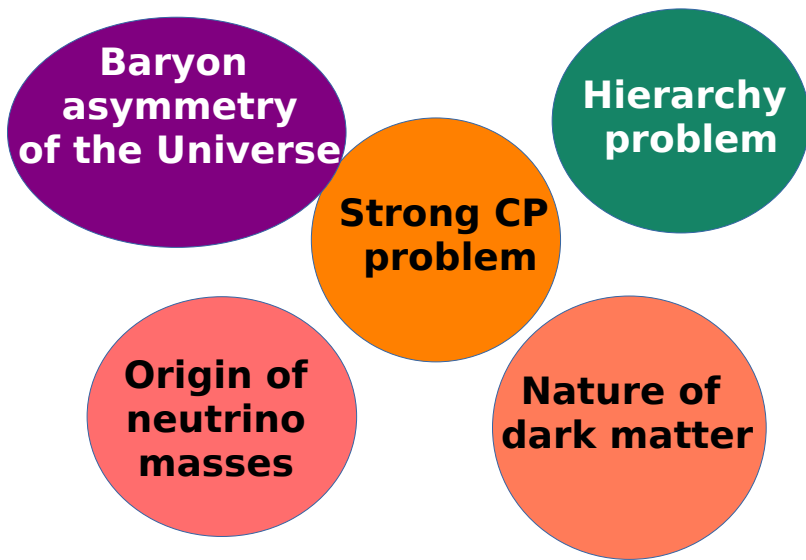
in collaboration with Matheus Hostert

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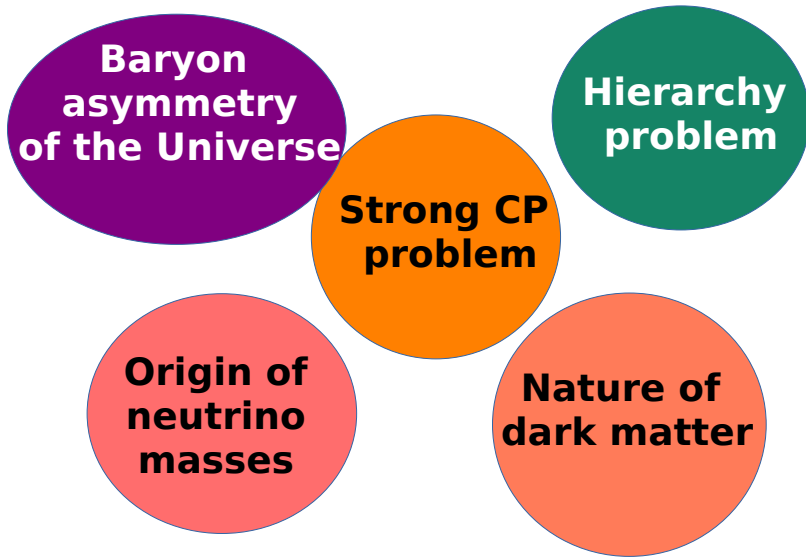


Open problems



Call for new physics

Open problems



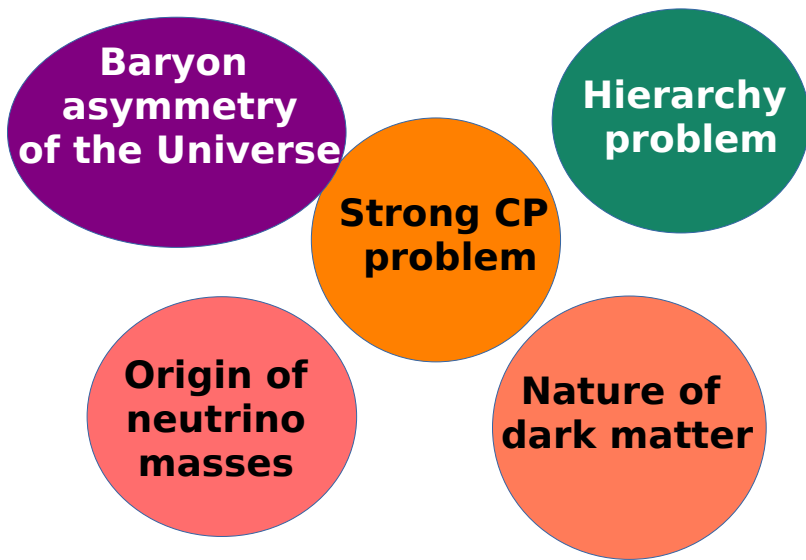
Call for new physics

New Physics



*Difficult to probe
directly*

Open problems



Call for new physics

New Physics

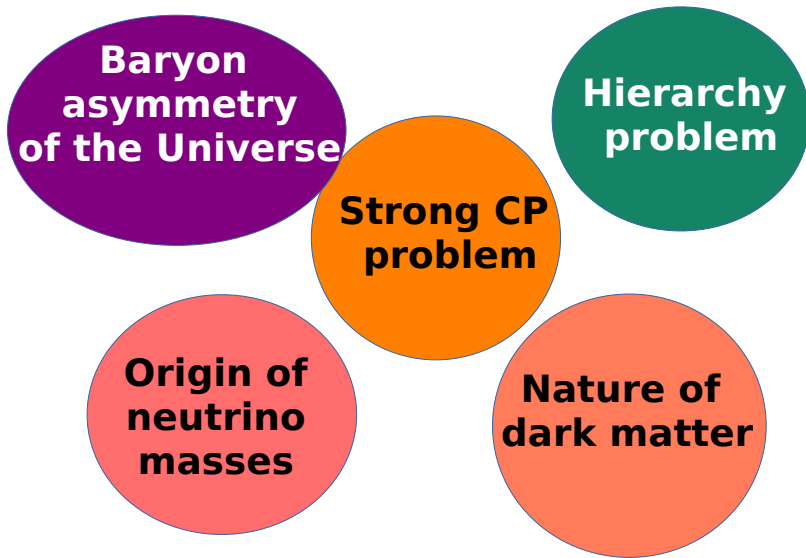


Difficult to probe directly



In this talk

Open problems

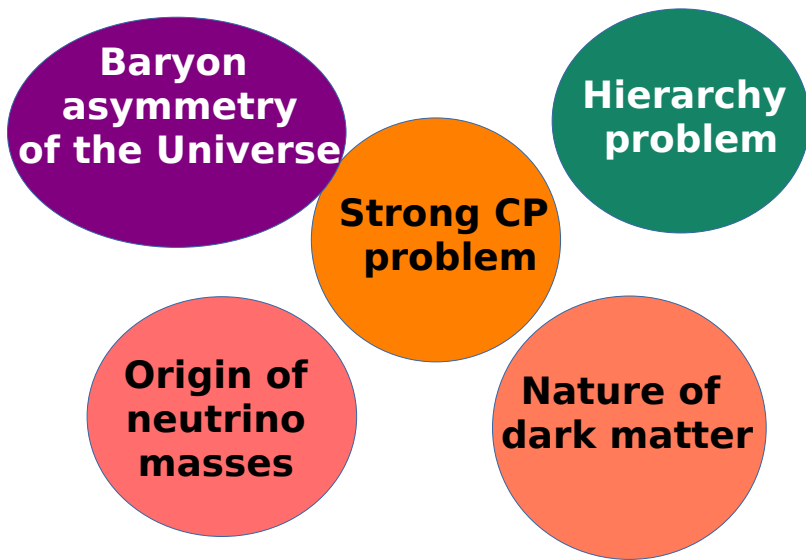


Call for new physics

- **Scalar** : Dark Higgs, Muon scalar etc
- **Pseudoscalar**: Axions, ALPs
- **Vector**: Dark Photon, etc
- **Fermions**: Heavy neutral leptons (HNLs)

Long lived particles

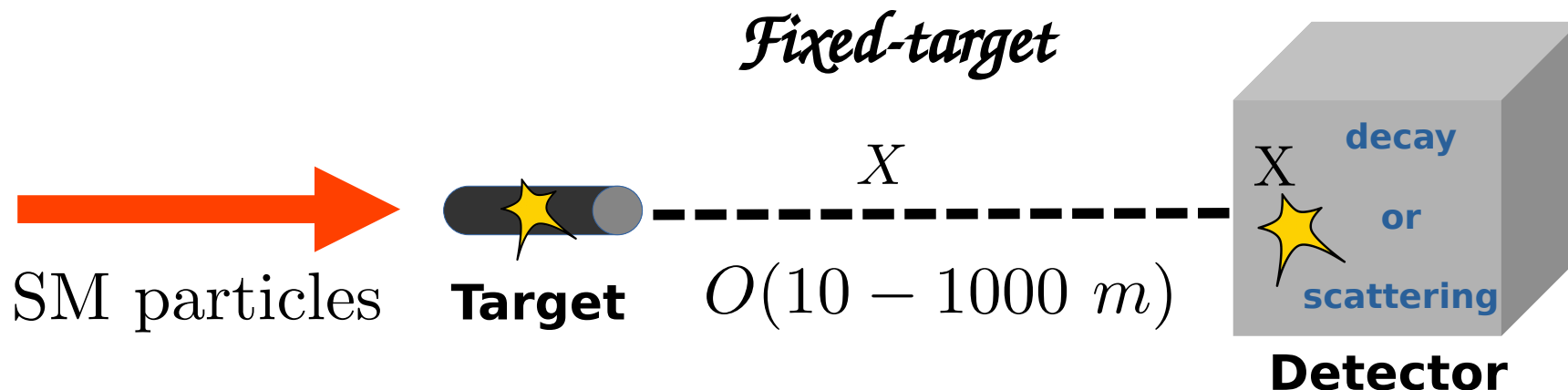
Open problems



Call for new physics

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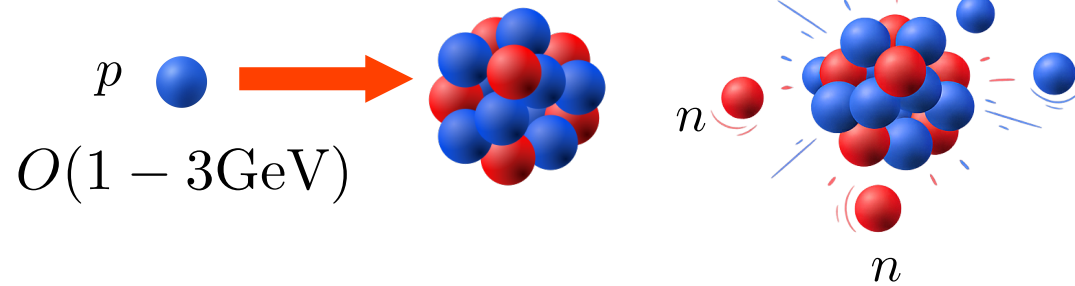
Long lived particles



$$m_{\text{NP}} \sim (1 \text{ MeV} - 2 \text{ GeV})$$

What is a spallation neutron source?

Intense beam



$$pp \rightarrow pn\pi^+ (pp\pi^0)$$

$$pp \rightarrow pp\pi^+\pi^-$$

$$pp \rightarrow pp\eta$$

$$pp \rightarrow p\Lambda^0 K^+$$

$$pp \rightarrow p\Sigma^+ K^0$$

$$pp \rightarrow ppK^+ K^-$$

Meson production

**Lose energy
and decay at rest**

$$\pi^+ / K^+ \rightarrow \mu^+ \nu_\mu$$

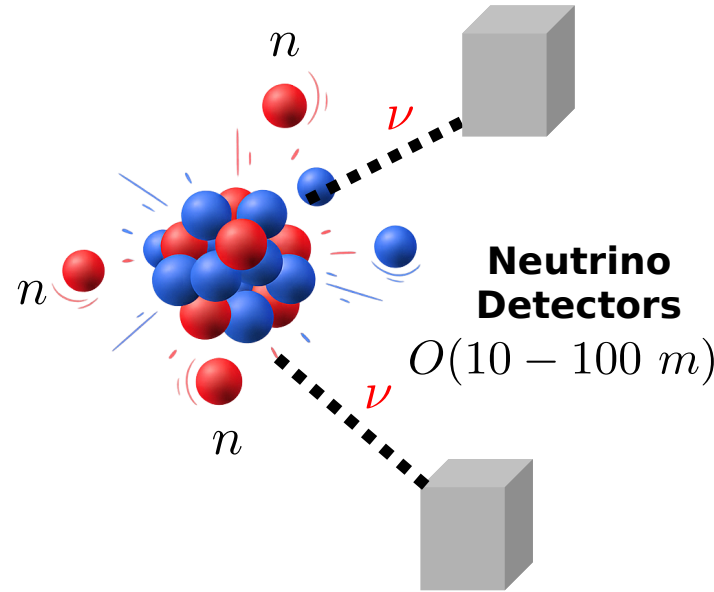
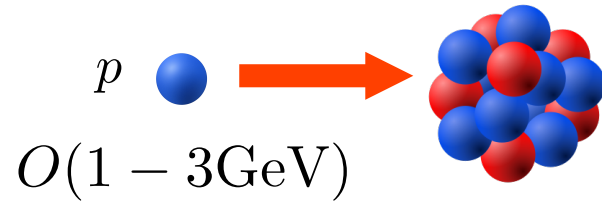
Captured

$$\pi^-, K^-$$

- **Nuclear Physics**
- **Material studies**

What is a spallation neutron source?

Intense beam



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Meson production

- **Nuclear Physics**
- **Material studies**
- **Neutrino Physics**

$$\pi^+ / K^+ \rightarrow \mu^+ \nu_\mu$$

$$\mu^+ \rightarrow e^+ + \nu_e + \bar{\nu}_\mu$$

Sterile neutrinos **CEvNS**

**Lose energy
and decay at rest**

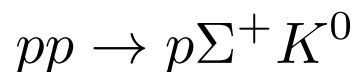
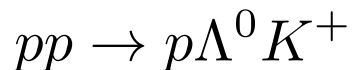
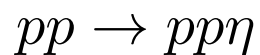
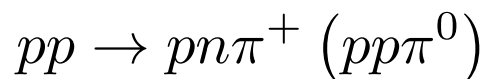
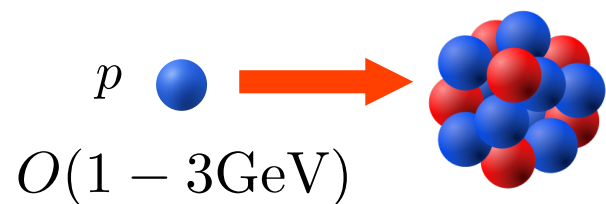
$$\pi^+ / K^+ \rightarrow \mu^+ \nu_\mu$$

Captured

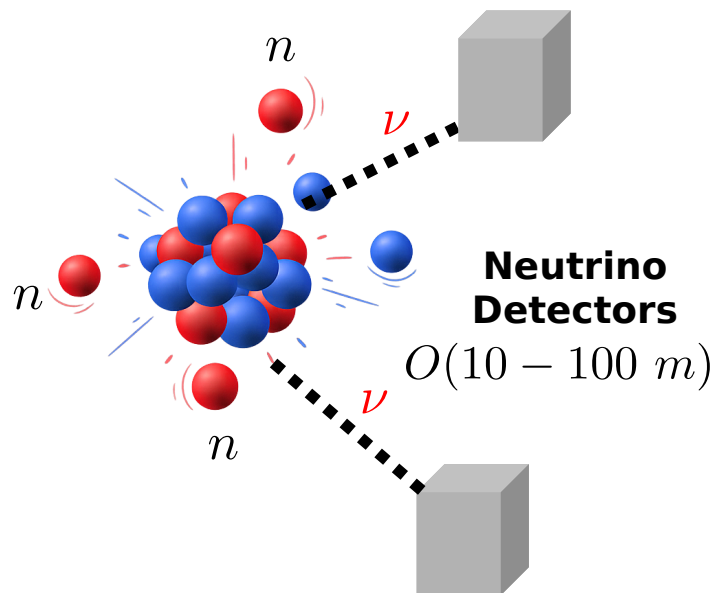
$$\pi^-, K^-$$

What is a spallation neutron source?

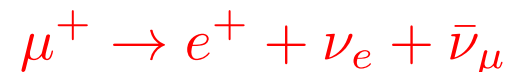
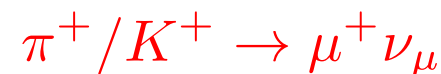
Intense beam



Meson production

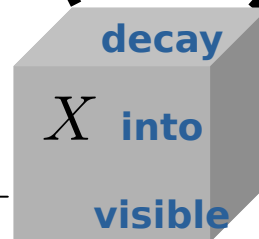
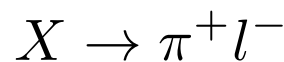
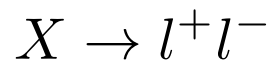
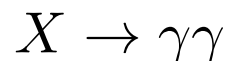


- **Nuclear Physics**
- **Material studies**
- **Neutrino Physics**



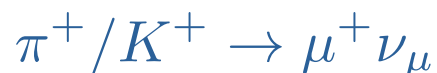
Sterile neutrinos **CEvNS**

- **FIPs searches**



Neutrino Detectors

**Lose energy
and decay at rest**



Captured



Overview of facilities

Past

KARMEN

ISIS (Rutherford, UK)

- 0.8 GeV p^+
- 180 kW and 225 μA
- 50 Hz
- 100 ns double-pulse (total 424 ns)
- About 4.3% $\pi\text{DAR}/\text{POT}$

CSNS-I $\rightarrow$ CSNS-II (IHEP, China)

- 1.6 GeV p^+
- (0.1 $\rightarrow$ 0.5) MW and (0.06 $\rightarrow$ 0.3) mA
- 25 Hz
- 100 ns double-pulse (total 800 ns)
- Expected 17% $\pi\text{DAR}/\text{POT}$

SINQ (PSI, Switzerland)

- 0.59 GeV p^+
- 1.4 MW and 2.4 mA
- Continuous
- Total of (—) $\pi\text{DAR}/\text{POT}$

LAMPF/LANSCE 93-98 (Los Alamos, USA)

- 0.8 GeV p^+
- 0.65 MW and 0.8 mA
- 120 Hz
- 600 μs (0.25 ns substructure)
- Range between (6.7%—9%) $\mu\text{DAR}/\text{POT}$

$\pi^+/\mu^+/K^+$ DAR sources

Current with neutrino detectors

Past or no neutrino detectors

Future with proposed neutrino detectors

LSND

Current

KARMEN

ISIS (Rutherford, UK)

- 0.8 GeV p^+
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COHERENT

SNS (Oak Ridge, USA)

- (1→1.3) GeV p^+
- (1.4→2.8) MW
- 60 Hz
- 400 ns single-pulse
- About (9%→11%) $\pi\text{DAR}/\text{POT}$

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- Expected 17% $\pi\text{DAR}/\text{POT}$

LANSCE current (Los Alamos, USA)

- 0.8 GeV p^+
- 0.1 MW and 0.125 mA
- 20 Hz
- 290 ns single-pulse → 100 ns (LANSCE-PSR)
- Total of 4.6% $\pi\text{DAR}/\text{POT}$

CCM

LAMPF/LANSCE 93-98 (Los Alamos, USA)

- 0.8 GeV p^+
- 0.65 MW and 0.8 mA
- 120 Hz
- 600 μs (0.25 ns substructure)
- Range between (6.7%—9%) $\mu\text{DAR}/\text{POT}$

LSND

JSNS (J-PARC, Japan)

- 3 GeV p^+
- 1 MW and 0.33 mA
- 25 Hz
- 100 ns double-pulse (total 800 ns)
- Total of 25% $\pi\text{DAR}/\text{POT}$
- Total of 0.38% $K\text{DAR}/\text{POT}$

JSNS, ND280 and KOTO

$\pi^+/\mu^+/K^+$ DAR sources

Current with neutrino detectors

Past or no neutrino detectors

Future with proposed neutrino detectors

Future

KARMEN

ISIS (Rutherford, UK)

- 0.8 GeV p^+
- 180 kW and 225 μ A
- 50 Hz
- 100 ns double-pulse (total 424 ns)
- About 4.3% π DAR/POT

ESS (Lund, Sweden)

- 1→2 GeV p^+
- 2→5 MW and 62.5mA
- 14 Hz
- Expected 2.8 ms
- Expected 30% π DAR/POT[†]

CSNS-I → CSNS-II (IHEP, China)

- 1.6 GeV p^+
- (0.1→0.5) MW and (0.06→0.3) mA
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LAMPF/LANSCE 93-98 (Los Alamos, USA)

- 0.8 GeV p^+
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- 120 Hz
- 600 μ s (0.25 ns substructure)
- Range between (6.7%→9%) μ DAR/POT

JSNS, ND280 and KOTO

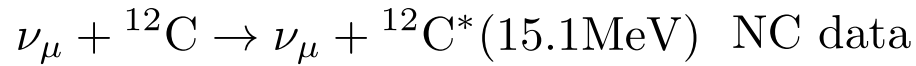
$\pi^+/\mu^+/K^+$ DAR sources

Current with neutrino detectors

Past or no neutrino detectors

Future with proposed neutrino detectors

Used in this work



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COHERENT

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CCM

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**JSNS, ND280
and KOTO**

$\pi^+/\mu^+/K^+$ DAR sources

Current with neutrino detectors

Past or no neutrino detectors

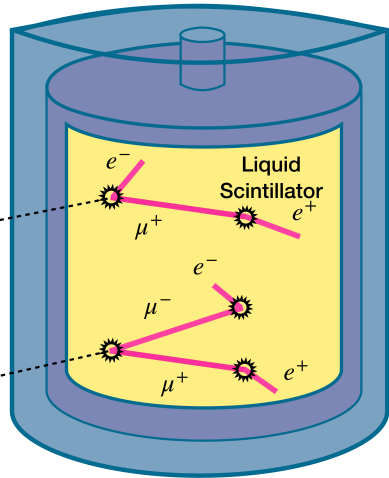
Future with proposed neutrino detectors



J-PARC

$$\pi^+ / K^+ \rightarrow X \quad \mu^+ \rightarrow X$$

$$X \rightarrow e^+ e^-, \gamma\gamma, \mu^+ \mu^-, \pi^+ \mu^-, \text{etc}$$



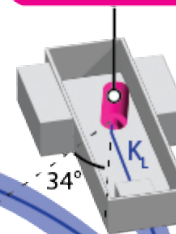
JSNS² (I and II): 20 m³, 36 m³

Pros: Closest to the source and largest vol

Cons: larger backgrounds, single flash events (e.g., e^+e^-) very challenging for $E_{\text{vis}} \lesssim 30$ MeV.

Best for: double/triple flash ($\mu\mu$, $\mu\pi$, or $\nu\mu e$).

KOTO @ 425 m

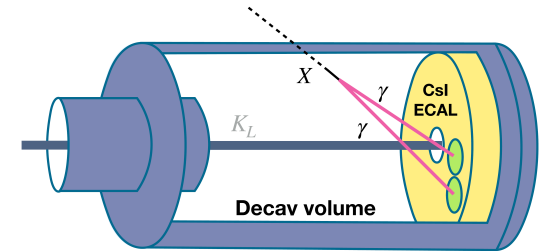


KOTO: 13 m³

Pros: Low-density vol and low bkg

Cons: Further away

Best for: π^0 and $\gamma\gamma$

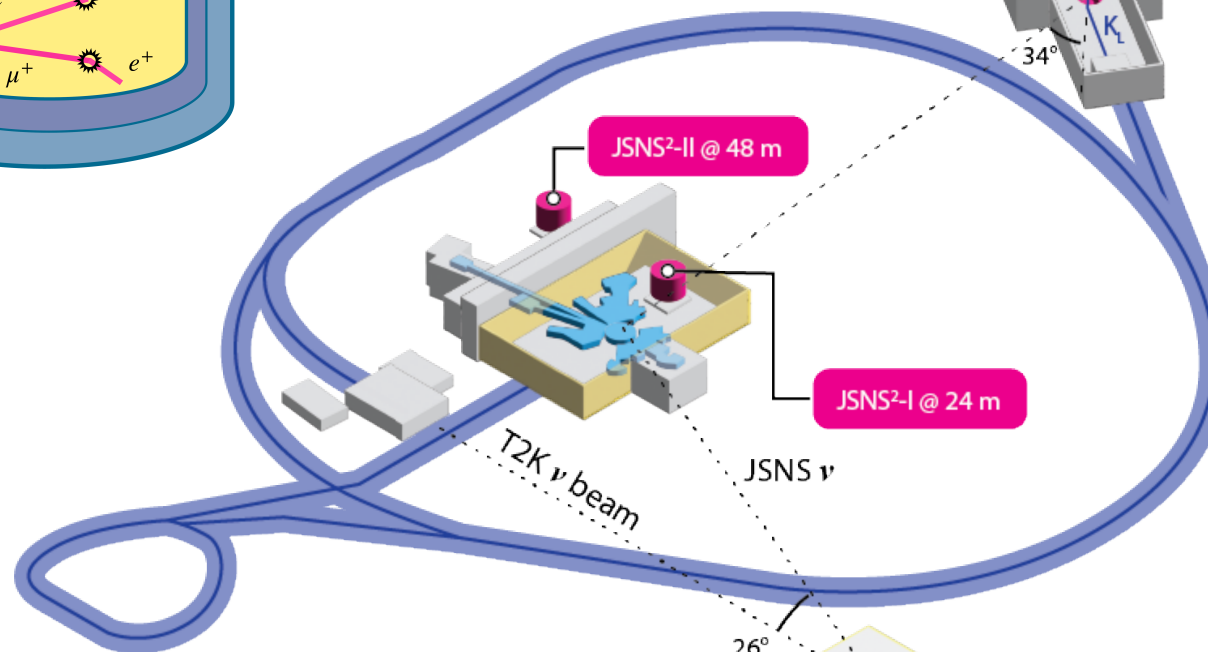
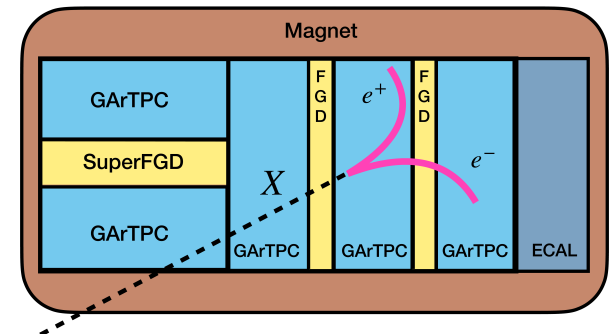


ND280: 11.7 m³

Pros: Low-density and magnetized

Cons: Further away

Best for: any charged final state



3 GeV protons

$1.1 \cdot 10^{23}$ PoT (3 years)

ND280 @ 270 m

SNS and LANSCE

$$\pi^+ \rightarrow X \quad \mu^+ \rightarrow X \quad X \rightarrow e^+e^-, \gamma\gamma$$

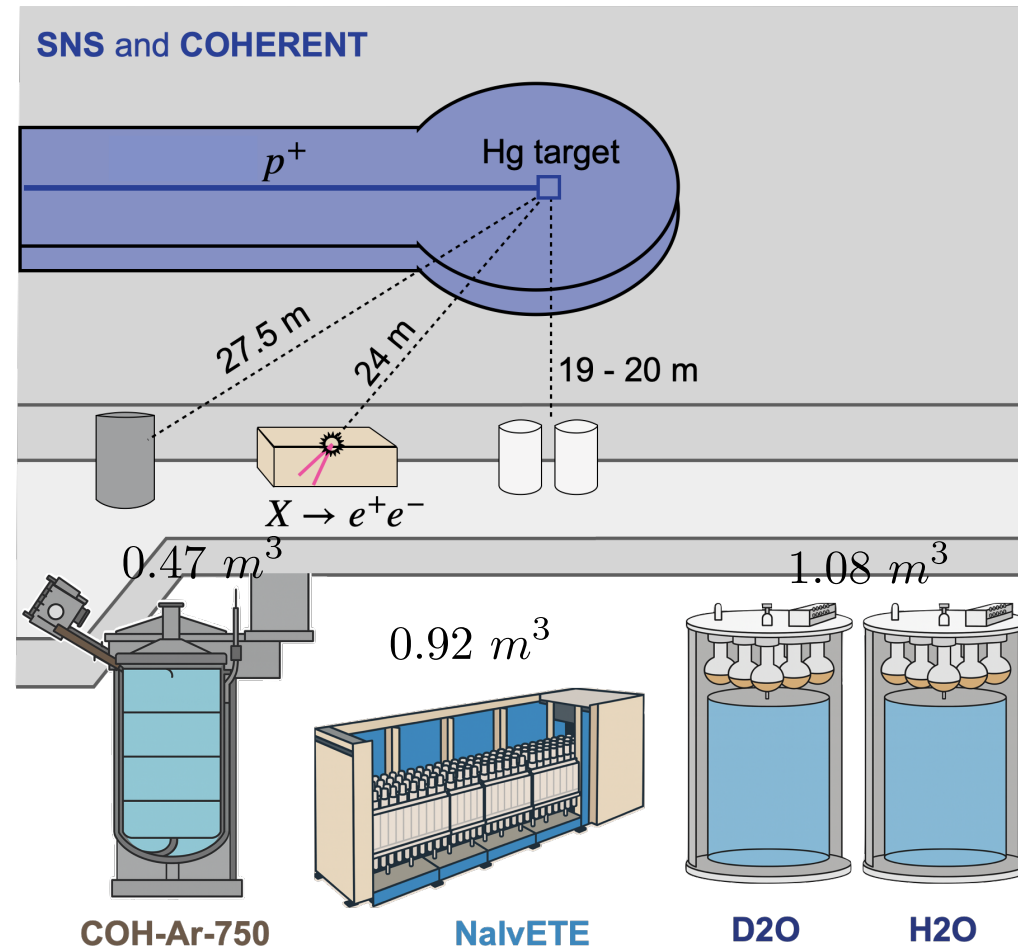
1 GeV protons

$4.5 \cdot 10^{23}$ PoT (3 years)

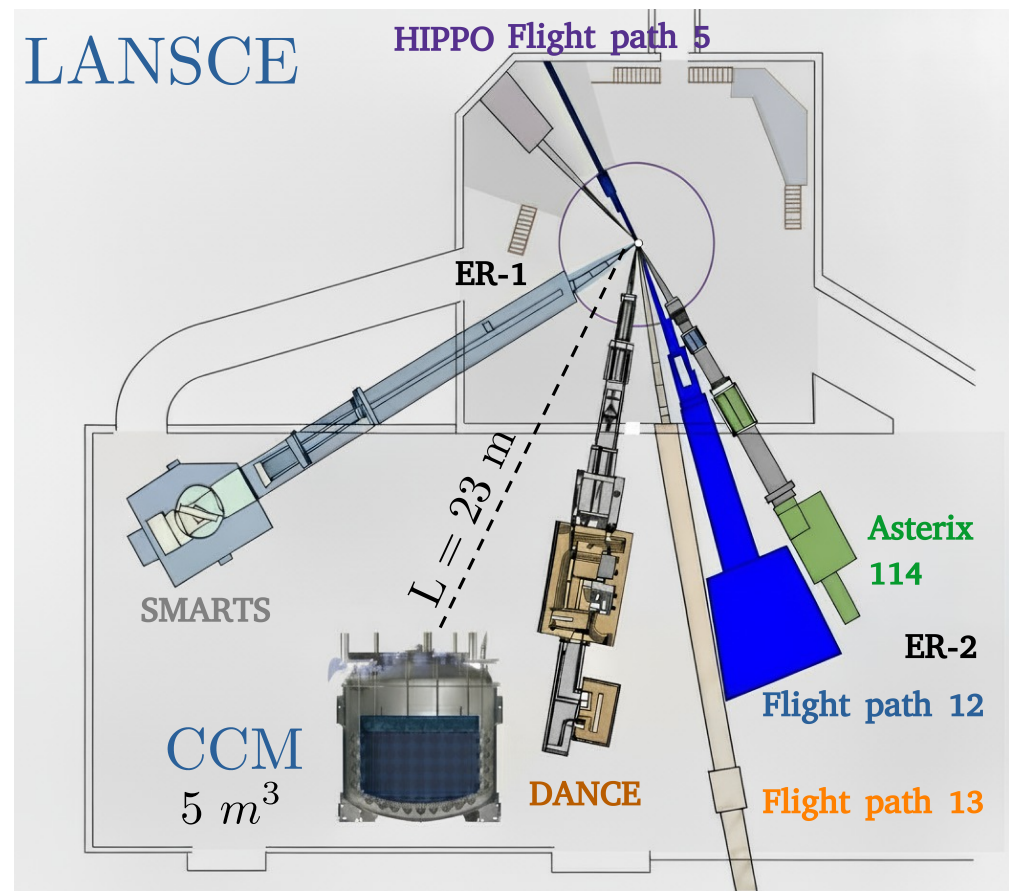
0.8 GeV protons

$2.25 \cdot 10^{22}$ PoT (3 years)

SNS and COHERENT



LANSCE



Results

Models studied in this work

- **Scalar : Higgs portal scalar, Muon scalar**
- **Pseudoscalars: ALPs**
- **Fermions: Heavy neutral leptons**

Models studied in this work

- **Scalar : Higgs portal scalar, Muon scalar**

- **Pseudoscalars: ALPs**

- **Fermions: Heavy neutral leptons**

In this talk

HNLs

How do we give mass to neutrinos?

ΔL conserved

**Higgs
mechanism**

$$m_\nu \sim y_\nu \frac{v}{\sqrt{2}}$$

$$y_\nu < 6.5 \cdot 10^{-13}$$

Why so small?

ΔL largely violated

**High scale
See-saw**

$$m_\nu \sim \frac{y_\nu^2 v^2}{M}$$

$$\text{If } y_\nu^2 \sim O(1) \rightarrow M \sim 10^{11} \text{ GeV,}$$

$$\text{If } y_\nu^2 \sim O(y_e^2) \rightarrow M \sim 1 \text{ GeV,}$$

Schechter and Valle 1980; Mohapatra and Senjanovic 1979; Minkowski 1977; Gell-Mann, Ramond and Slansky 1979; Yanagida 1980

ΔL approximately conserved

**Low scale see-
saw**

$$m_\nu \sim \frac{v^2}{M^2} \mu$$

$$\mu \ll 1$$

**Symmetry protected
scenarios**

Mohapatra, & Valle 1986 ; Akhmedov, Lindner, Schnapka, and Valle 1996; Gonzalez-Garcia and Valle 1989; Gavela, Hambye, Hernandez 2009; Bernabéu, Santamaria, Vidal, Mendez, and Valle 1987; Mohapatra 1986

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**Low scale see-
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This work

$$m_\nu \sim \frac{v^2}{M^2} \mu$$

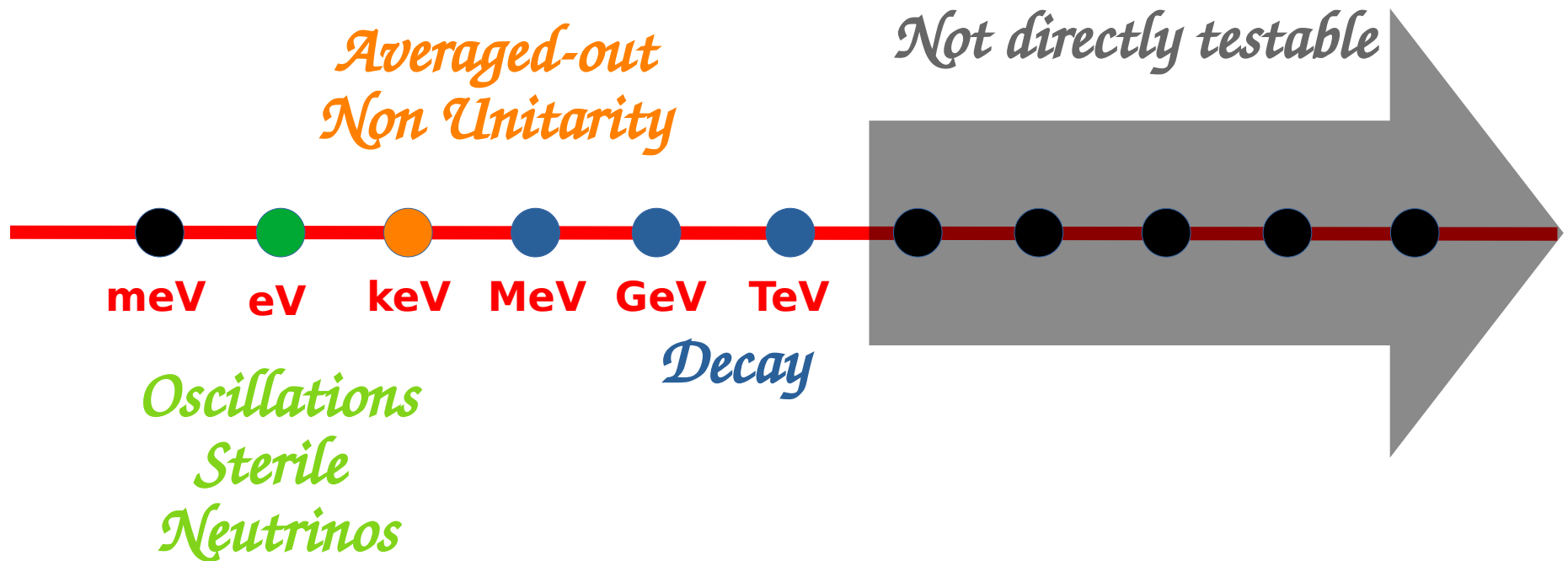
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**Symmetry protected
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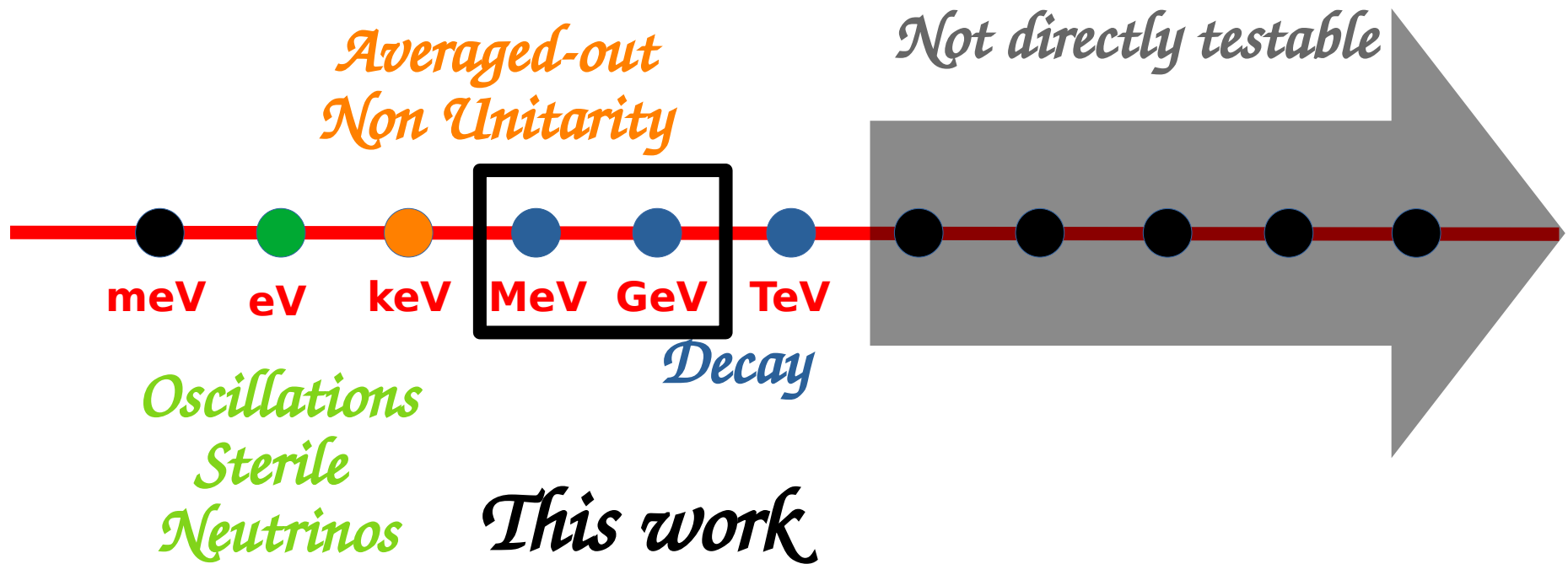
How do we give mass to neutrinos?

New Physics scale M



How do we give mass to neutrinos?

New Physics scale M



$\mathcal{HNL}$

$$\mathcal{L} \supset -\frac{g}{\sqrt{2}} (W_\mu^- \bar{l}_{L\alpha} \gamma_\mu U_{\alpha 4} N + \text{h.c.}) - \frac{g}{\cos \theta_W} (Z_\mu \bar{N} \gamma^\mu U_{\alpha 4}^* \nu_{L\alpha} + \text{h.c.})$$

We consider the simplified phenomenological benchmarks of
one HNL mixing with one SM neutrino of a given flavour

Production

$$U_{e4}$$

$$K^+ \rightarrow e^+ N$$

$$\pi^+ \rightarrow e^+ N$$

$$\mu \rightarrow e \nu_e N$$

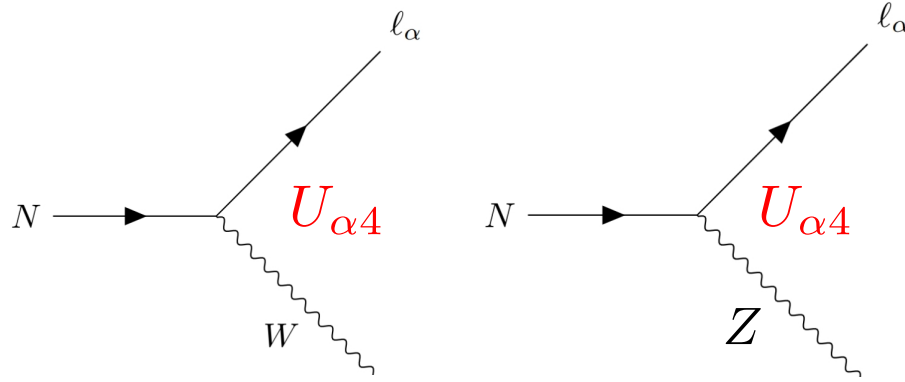
$$U_{\mu 4}$$

$$K^+ \rightarrow \mu^+ N$$

$$\pi^+ \rightarrow \mu^+ N$$

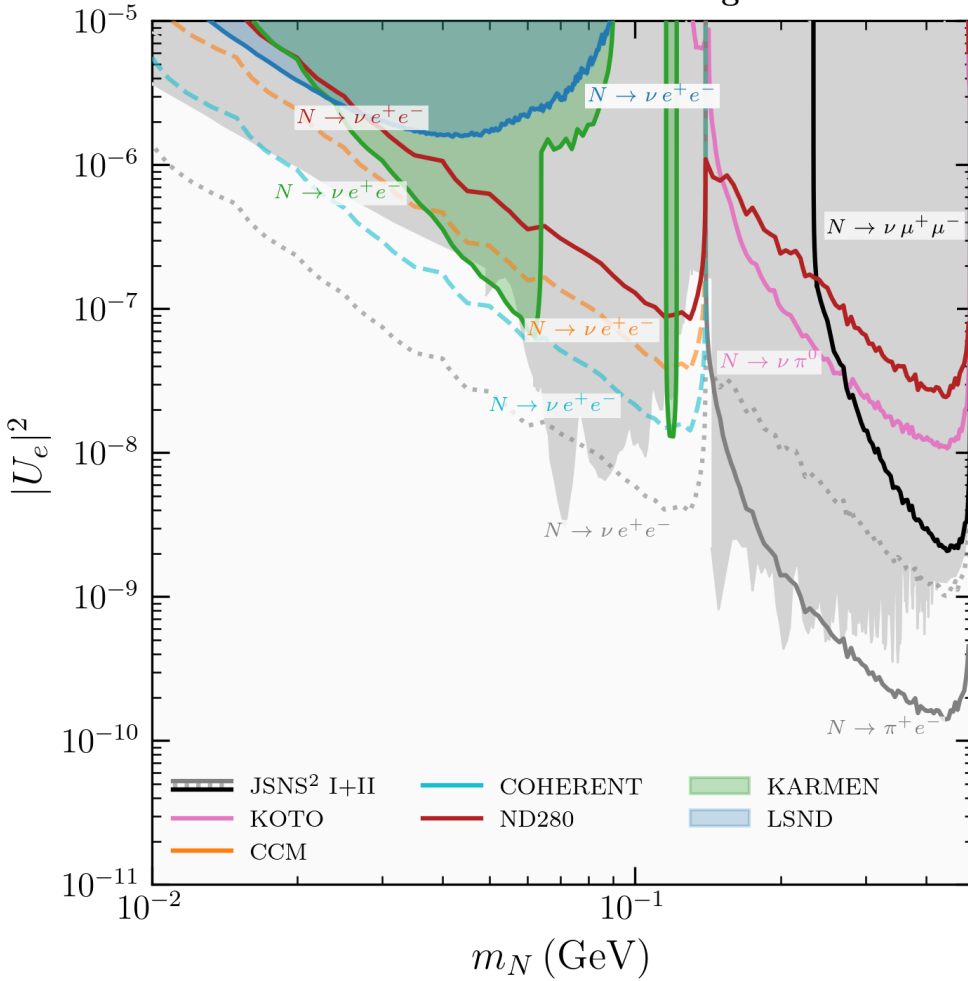
$$\mu \rightarrow e \nu_\mu N$$

HNL

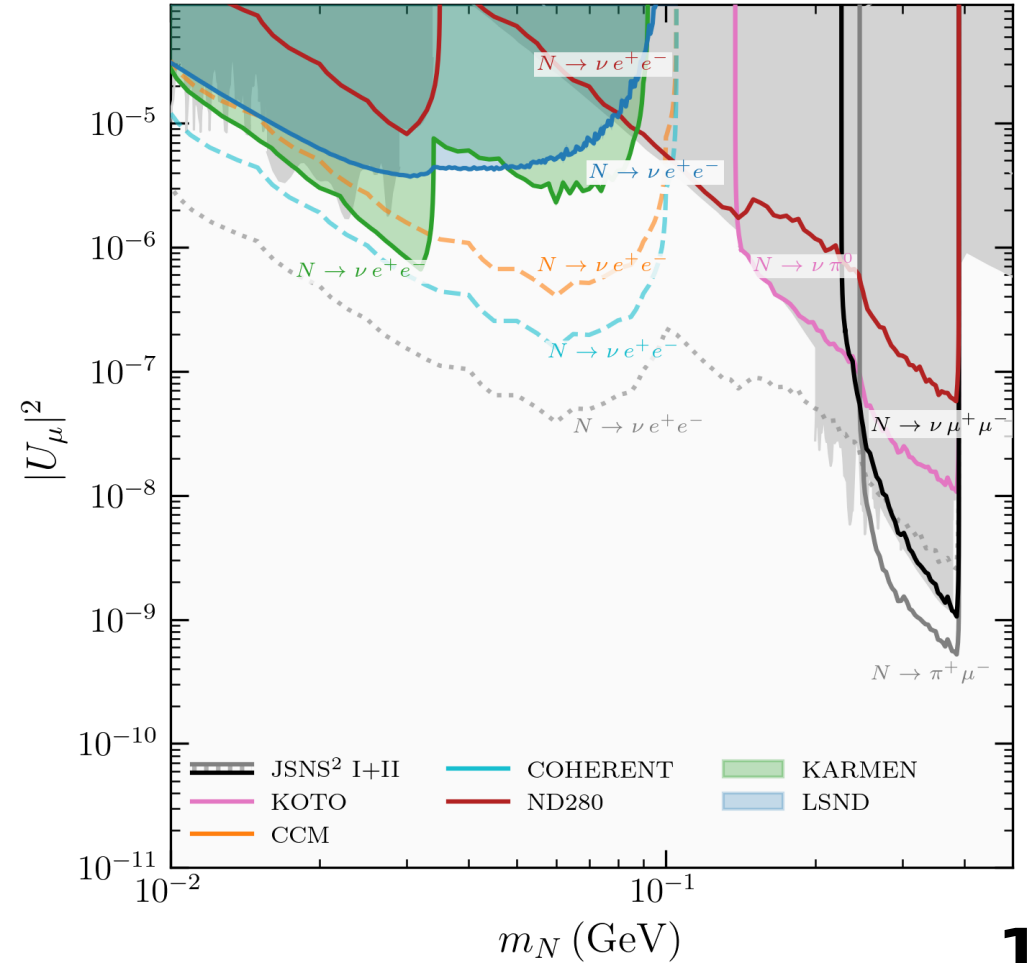


- $N \rightarrow \nu e^+ e^-$ (NC and CC),
- $N \rightarrow \nu e^\pm \mu^\mp$ (CC),
- $N \rightarrow \nu \mu^+ \mu^-$ (NC and CC),
- $N \rightarrow \nu \pi^0$ (NC),
- $N \rightarrow e^- \pi^+$ (CC),
- $N \rightarrow \mu^- \pi^+$ (CC),

HNL Electron Mixing



HNL Muon Mixing



ALPs

ALPs

Appear in many
new Physics
models

Warm dark
matter

QCD Axion solution and Strong CP problem

$$\mathcal{L}_{\text{QCD}} + \frac{\theta g_s^2}{32\pi^2} \epsilon_{\mu\nu\alpha\beta} G_a^{\mu\nu} G^{\alpha\beta}$$

Neutron electric dipole moment

$$d_n = (5.2 \times 10^{-16} e \cdot \text{cm}) \theta.$$

Why so small?

$$\theta < 10^{-10}$$



$$\frac{a g_s^2}{32\pi^2} \epsilon_{\mu\nu\alpha\beta} G_a^{\mu\nu} G_a^{\alpha\beta}$$

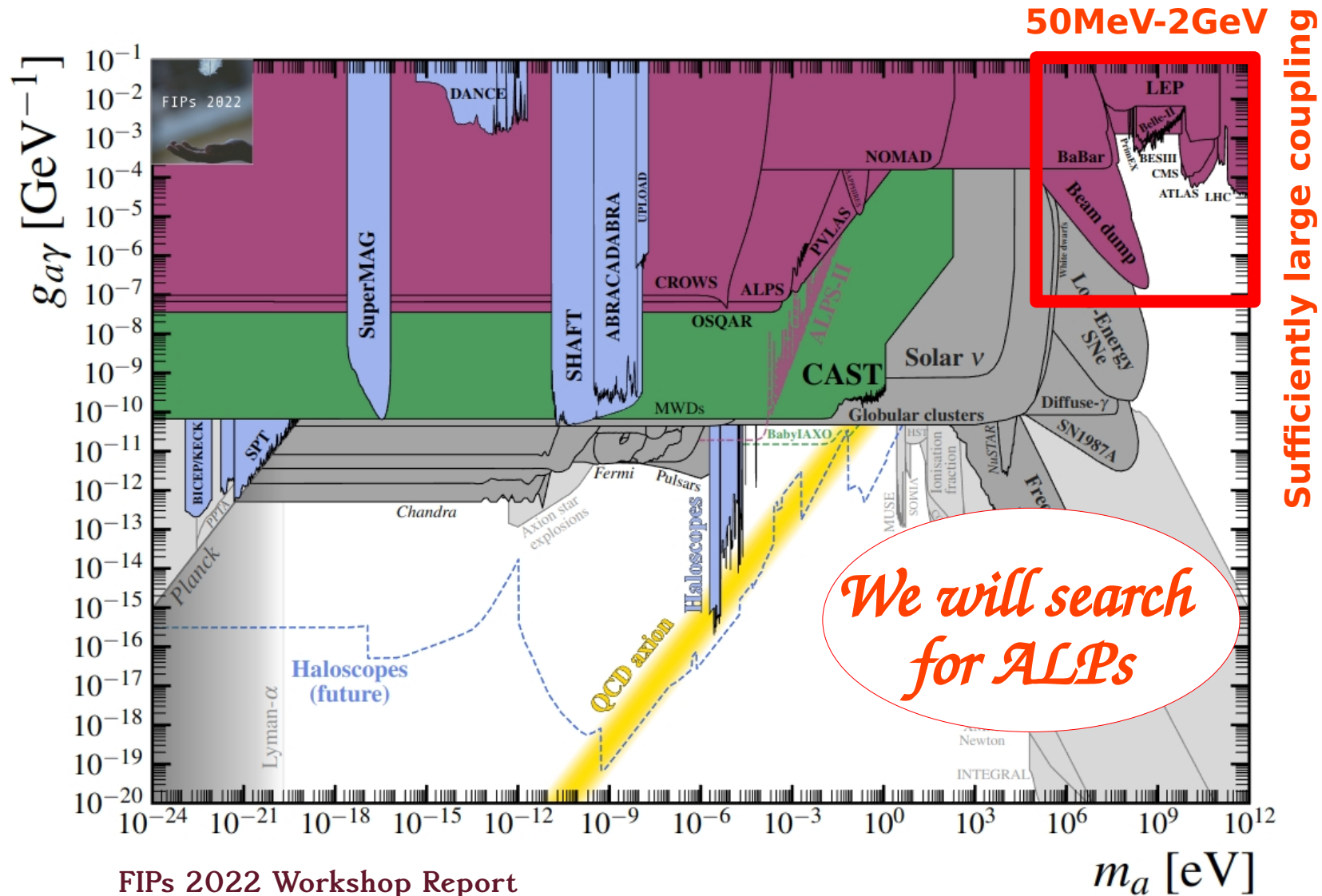
**Solves dynamically the
Strong CP problem**

Peccei, Quinn 1977

Weinberg 1978

How do we search for ALPs?

Neutrino Detectors



ALPs: Higgs coupled

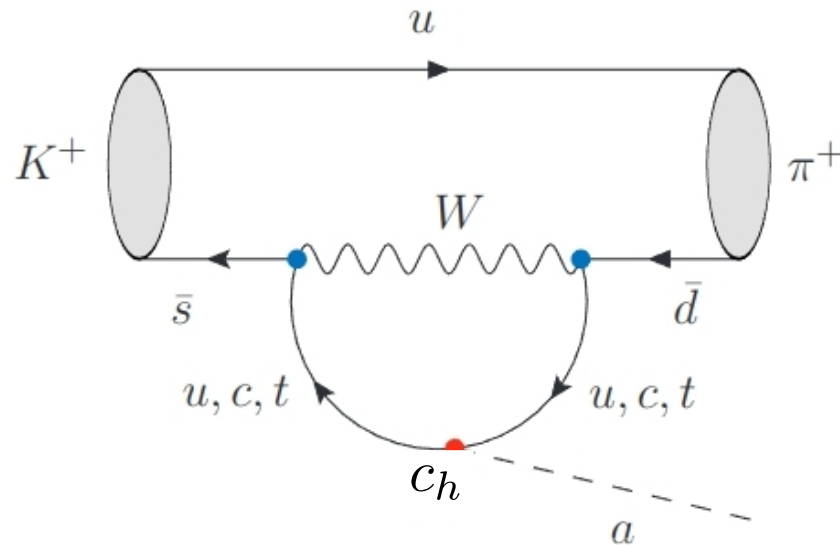
$$L_{\text{ALP}} \supset \frac{1}{2} (\partial_\mu a) (\partial^\mu a) - \frac{m_a^2}{2} a^2 + \frac{\partial_\mu a}{f_a} c_h \left(H^\dagger i \overleftrightarrow{D}^\mu H \right)$$

Hypercharge rotation

$$c_h \left(H^\dagger i \overleftrightarrow{D}^\mu H \right) \quad \longrightarrow \quad c_{ff} \sum_f \bar{f} \gamma^\mu \gamma_5 f$$

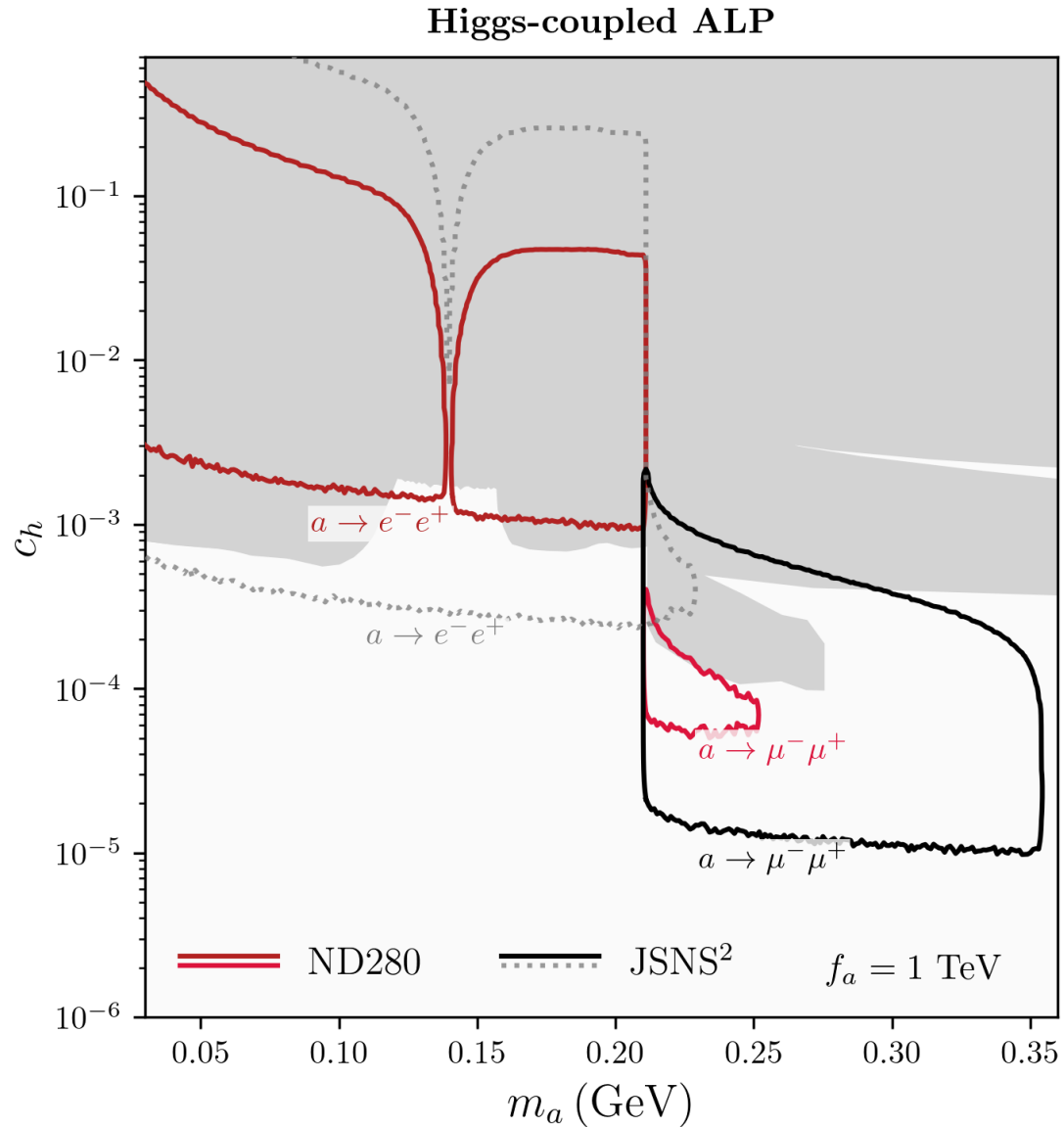
Production

$$K^+ \rightarrow \pi^+ a_h$$



ALPs: Higgs coupled

$$\Gamma_{a_h \rightarrow \ell^+ \ell^-} = |c_h|^2 \frac{m_a m_\ell^2}{8\pi f_a^2} \sqrt{1 - 4r_\ell^2} \text{ where } r_\ell = m_\ell/m_a$$



Summary

- Past experimental data keeps giving us nice surprises, such as those from KARMEN and LSND.
- Spallation sources provide a valuable complementary venue to search for FIPs, particularly those produced in muon and pion decays.
- Reducing backgrounds will greatly enhance the ultimate reach of these facilities.

Thank you

Back up

ALPs: Leptophilic

$$L_{\text{ALP}} \supset \frac{1}{2} (\partial_\mu a) (\partial^\mu a) - \frac{m_a^2}{2} a^2 + \frac{\partial_\mu a}{2f_a} j^\mu,$$

$$j_\ell^\mu = \sum_{i,j}^{e,\mu,\tau} c_{ij}^L \bar{\ell}_L^i \gamma^\mu \ell_L^j + c_{ij}^\nu \bar{\nu}_L^i \gamma^\mu \nu_L^j + c_{ij}^R \bar{\ell}_R^i \gamma^\mu \ell_R^j.$$

**Lepton Flavour conserving
(LFC)**

$$c_{ij}^{L,R,\nu} = \delta_{ij} \times c_j^{L,R,\nu},$$

- Weak conserving (WC)**

$$c_{ii}^L = -c_{ii}^R, \quad c_{ii}^\nu = -c_{ii}^L.$$

- Weak violating (WV)**

$$c_{ii}^L = -c_{ii}^R, \quad c_{ii}^\nu = 0.$$

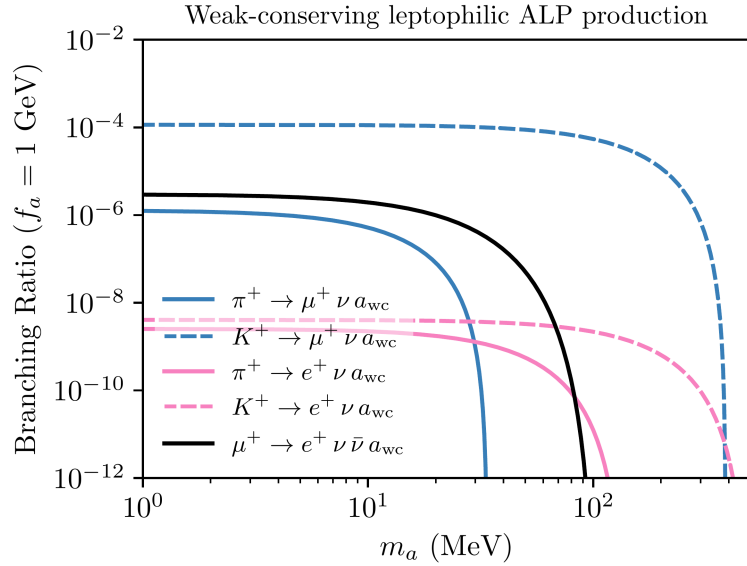
**Lepton Flavour violating
(LFV)**

$$c_{ij}^{L,R,\nu}$$

$$c_{ij}^L = -c_{ij}^R \text{ and } c_{ij}^\nu = -c_{ij}^L.$$

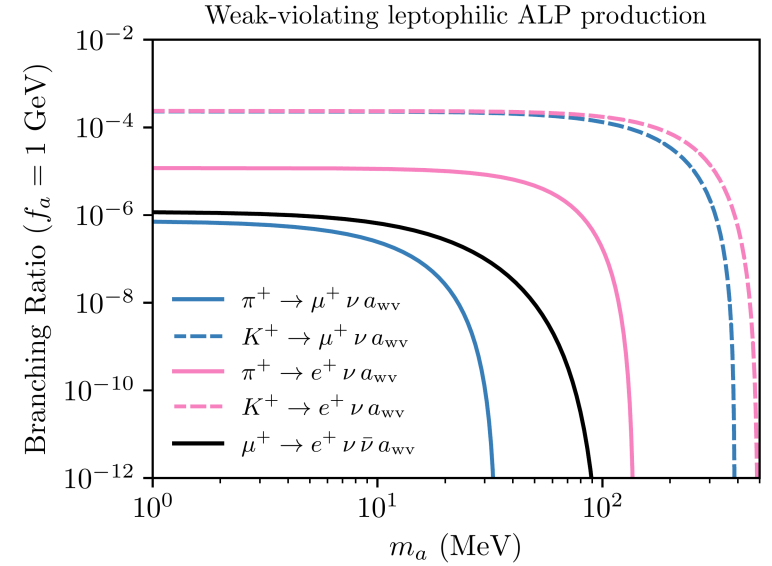
Production

Lepton Flavour conserving (LFC)



Helicity suppression lifted

$$M^+ \rightarrow e^+ \nu_e a_\ell$$



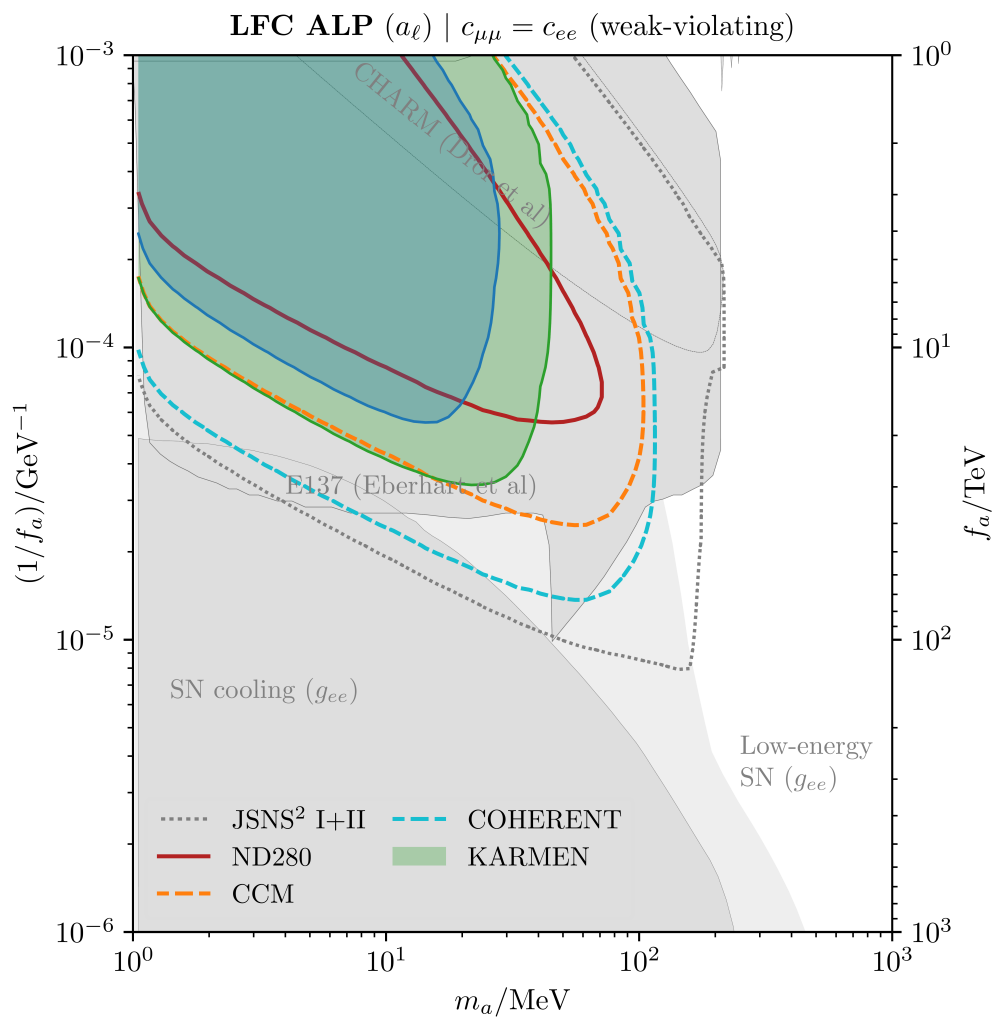
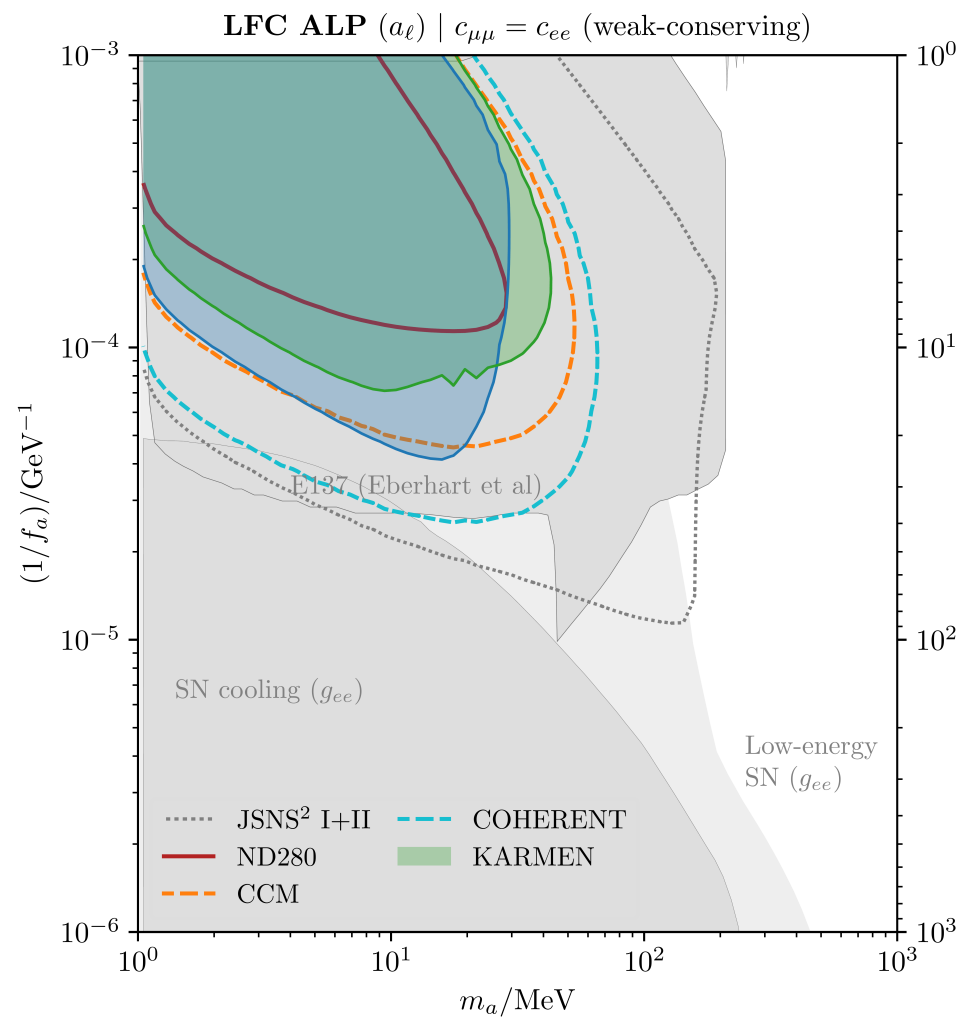
Lepton Flavour violating (LFV)

$$\Gamma(\mu^+ \rightarrow e^+ a_\ell) \simeq \left(|c_{e\mu}^L|^2 + |c_{e\mu}^R|^2 \right) \frac{m_\mu^3}{32\pi f_a^2} f(r_e, r_a),$$

where $f(r_e, r_a) = (1 + r_e)^2 \left[(1 - r_e)^2 - r_a^2 \right] \lambda^{1/2}(1, r_e, r_a)$ with $r_i = m_i^2/m_\mu^2$.

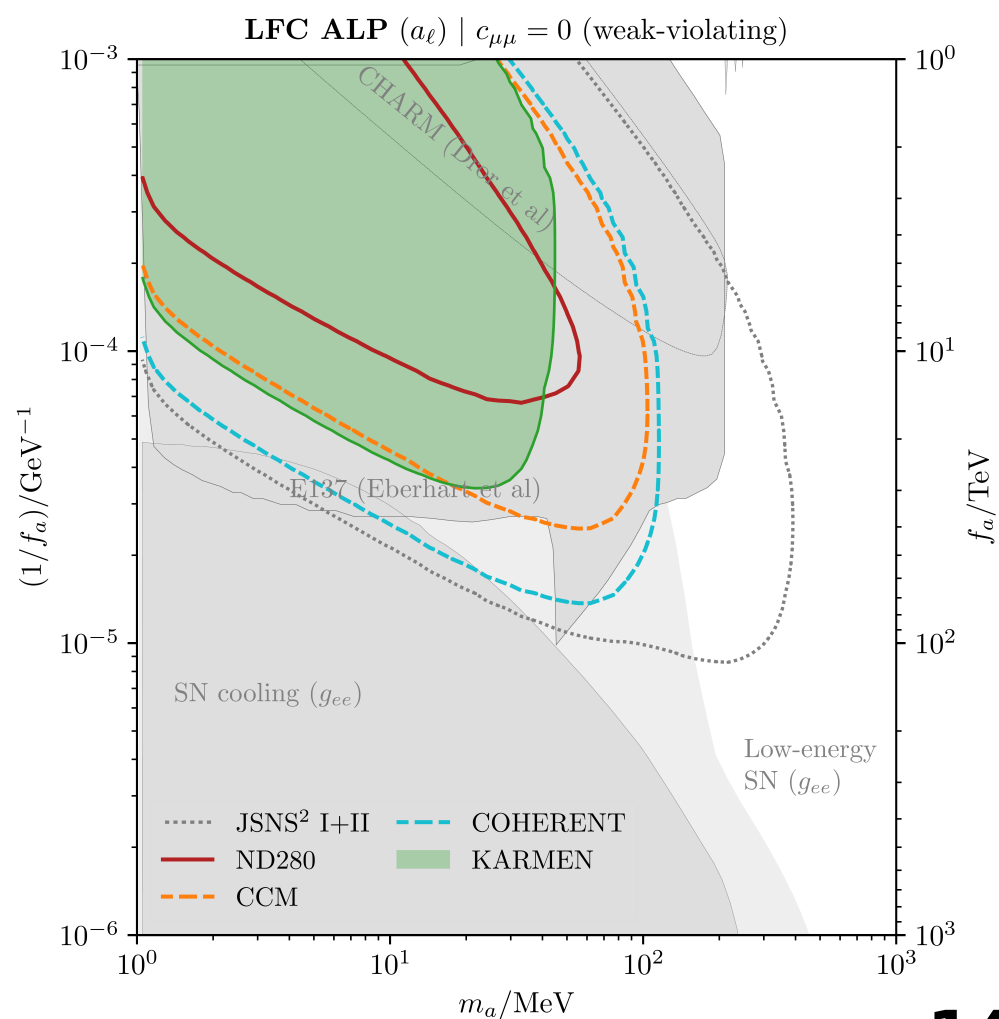
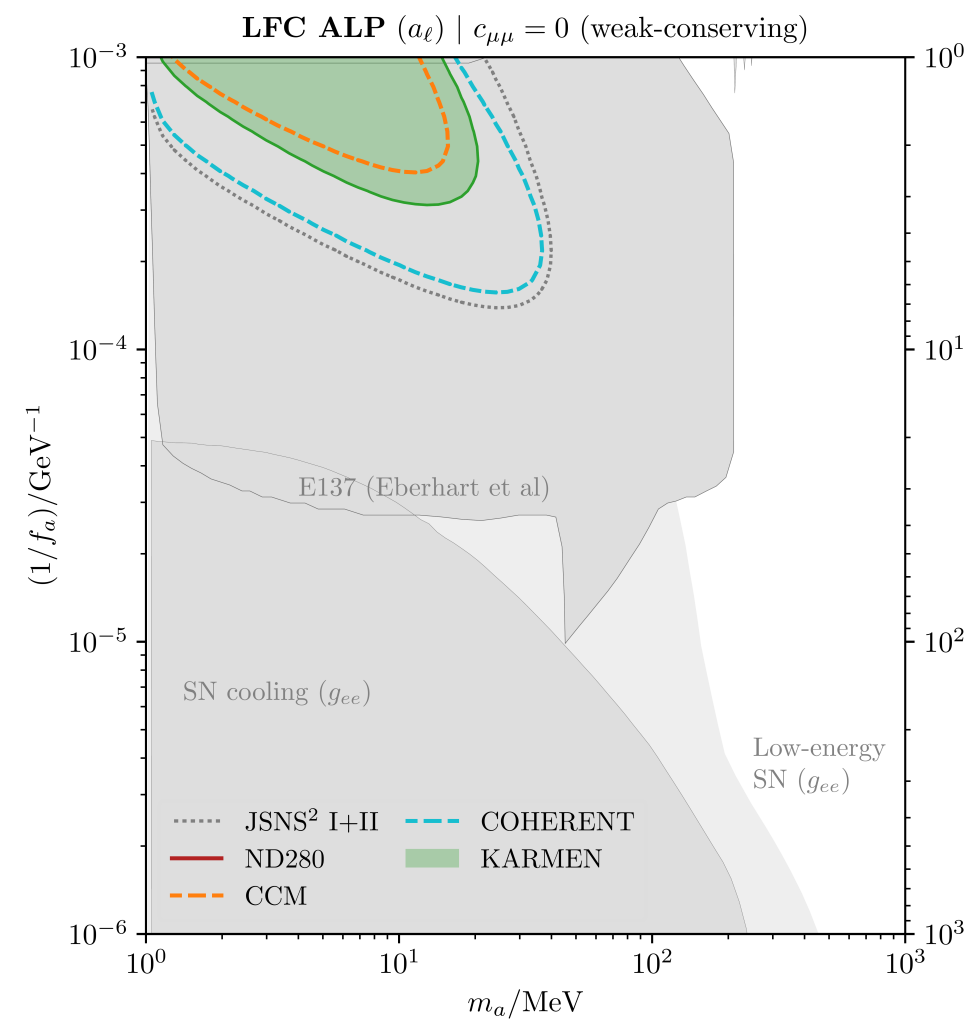
Lepton Flavour conserving (LFC): universal

$$a_\ell \rightarrow e^+ e^-$$

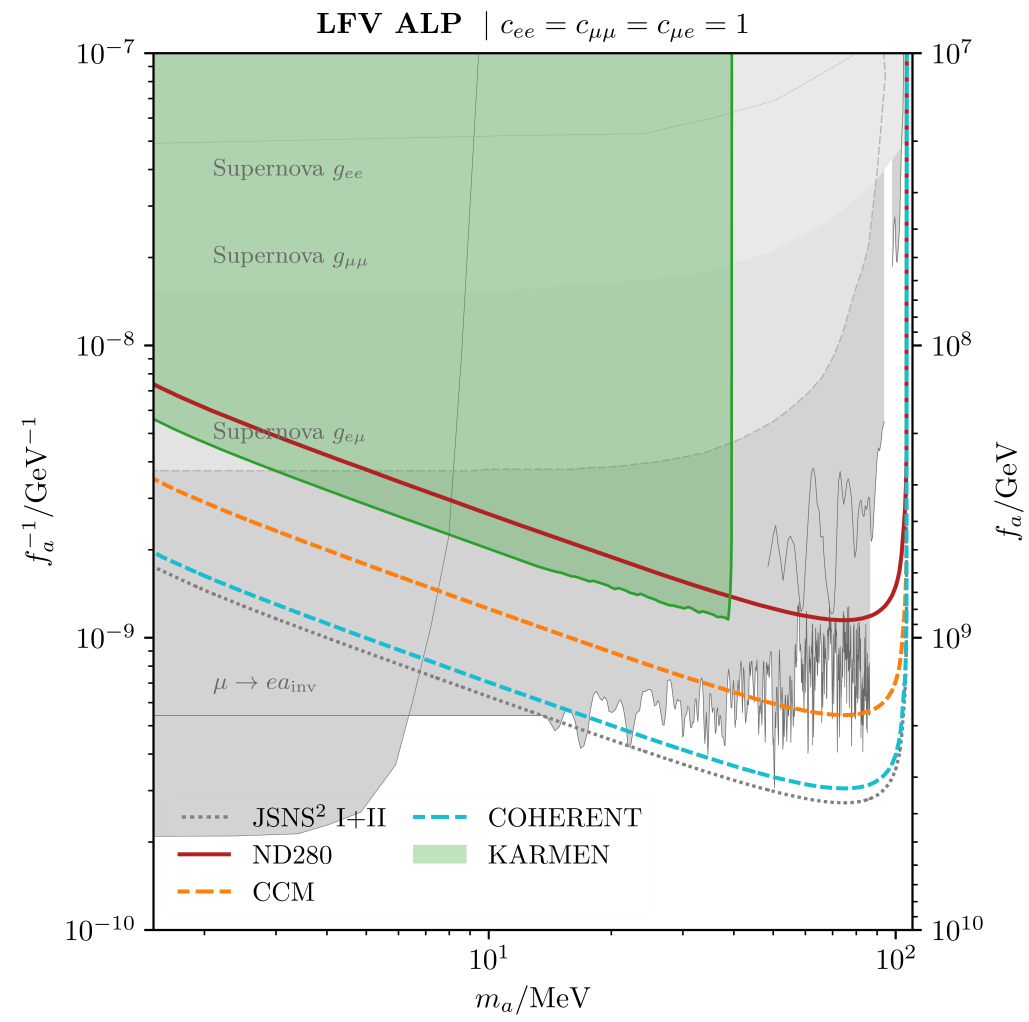


Lepton Flavour conserving (LFC): electron dominance

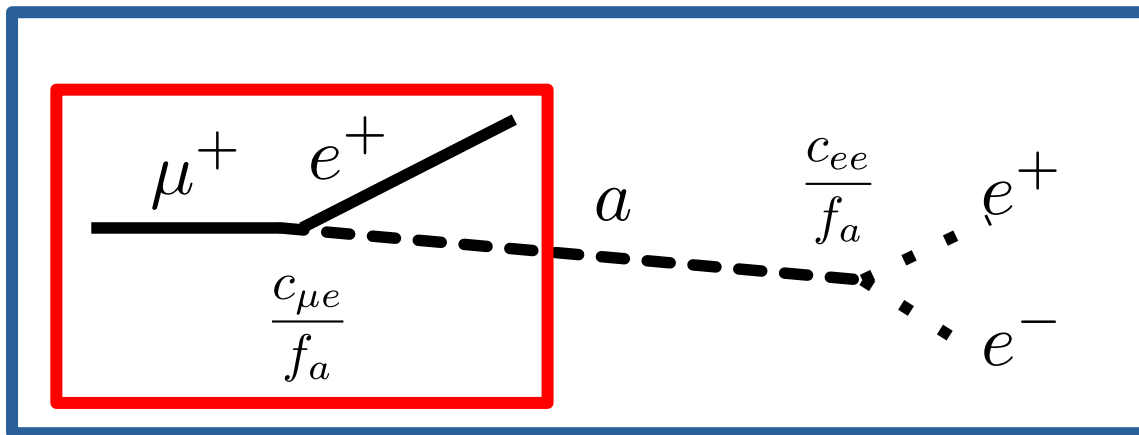
$$a_\ell \rightarrow e^+ e^-$$



Lepton Flavour violating (LFV)



Lepton Flavour violating (LFV)

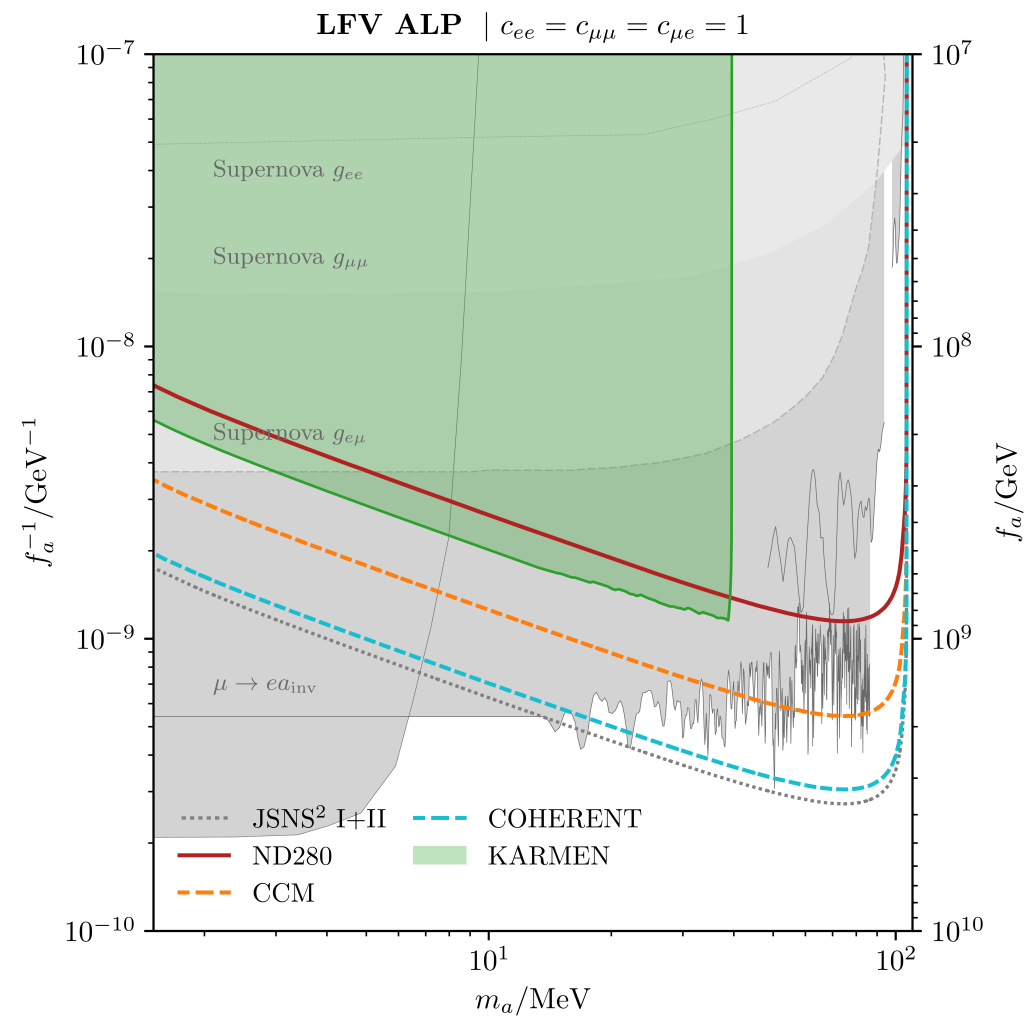


Rare muon decays

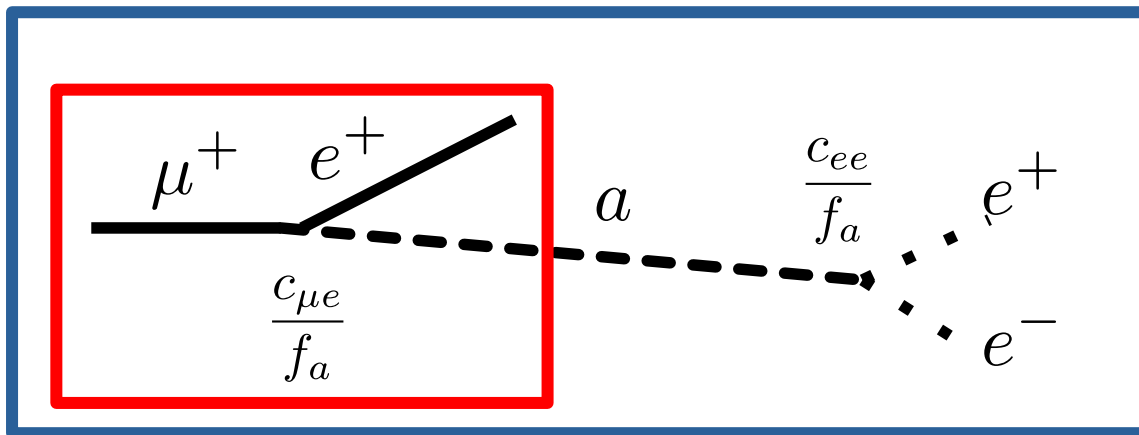
$$\propto \frac{c_{\mu e}^2}{f_a^2}.$$

Decay in flight

$$\propto \frac{c_{\mu e}^2 c_{ee}^2}{f_a^4}.$$



Lepton Flavour violating (LFV)

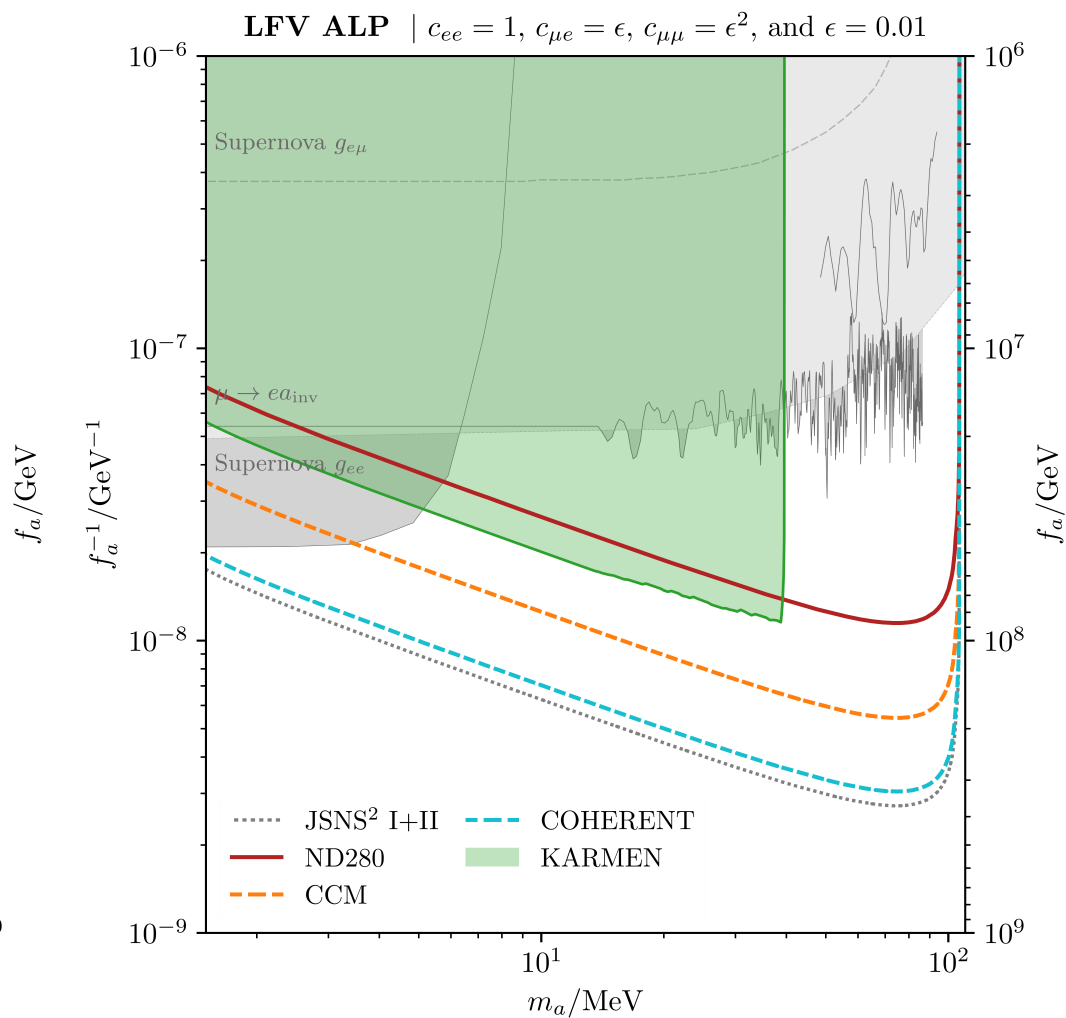
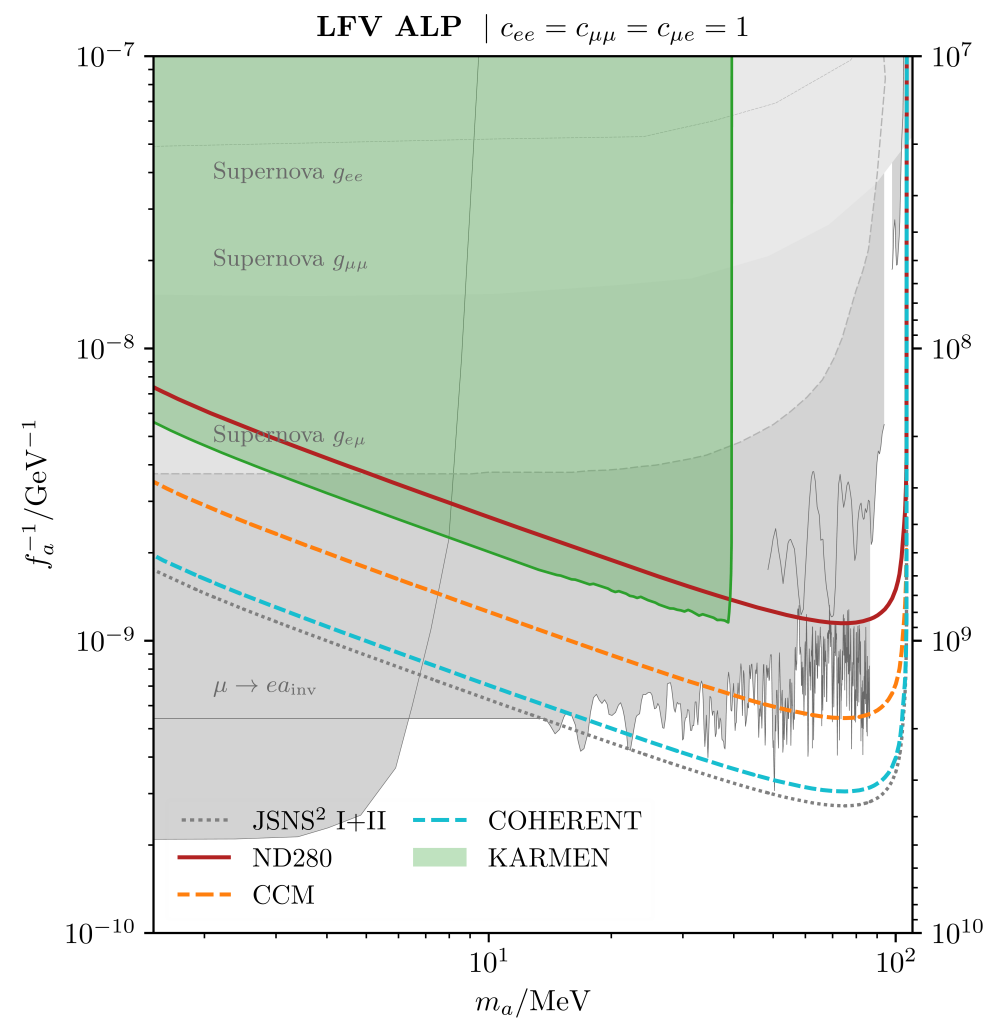


Rare muon decays

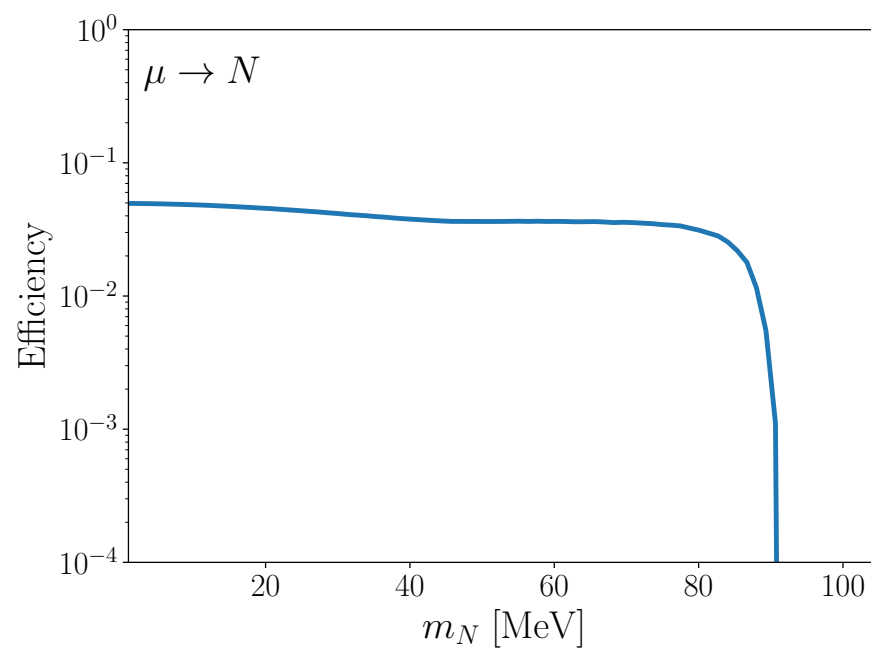
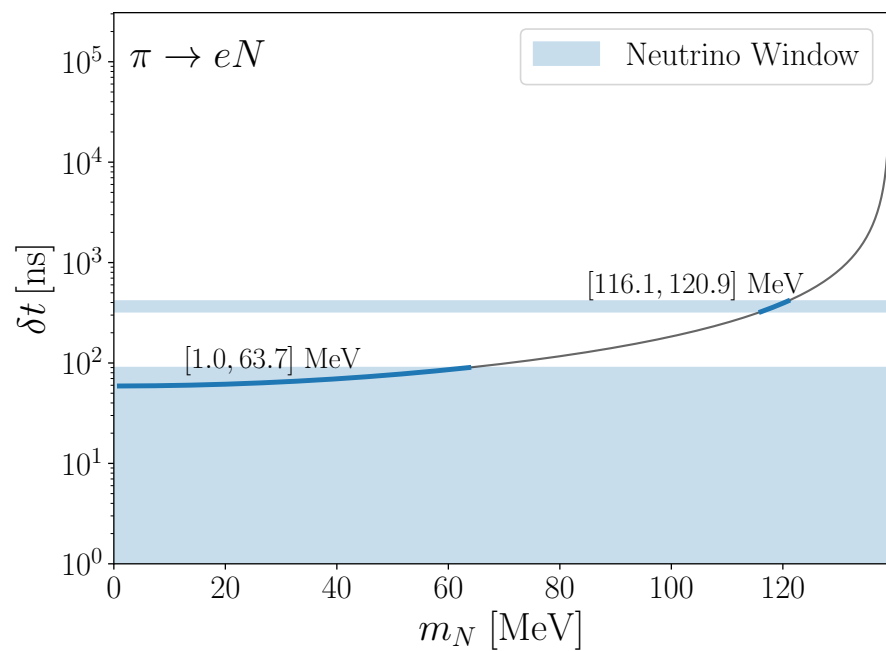
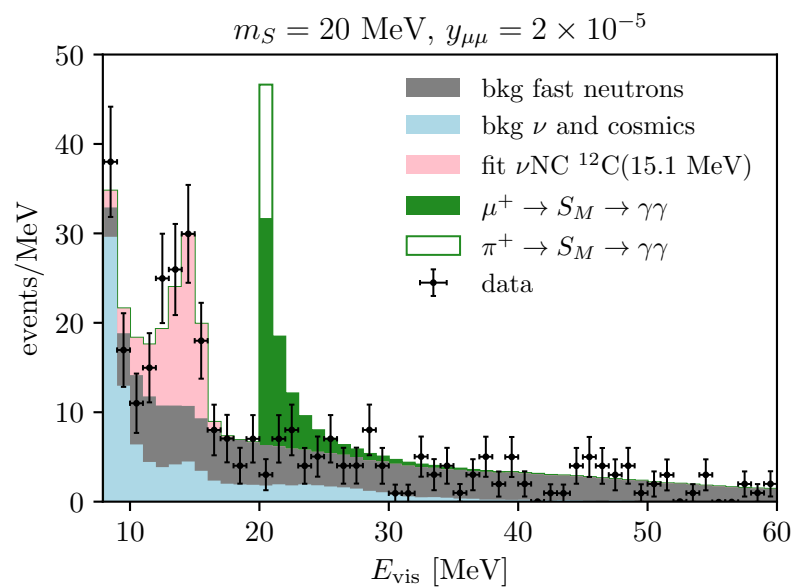
$$\propto \frac{c_{\mu e}^2}{f_a^2}.$$

Decay in flight

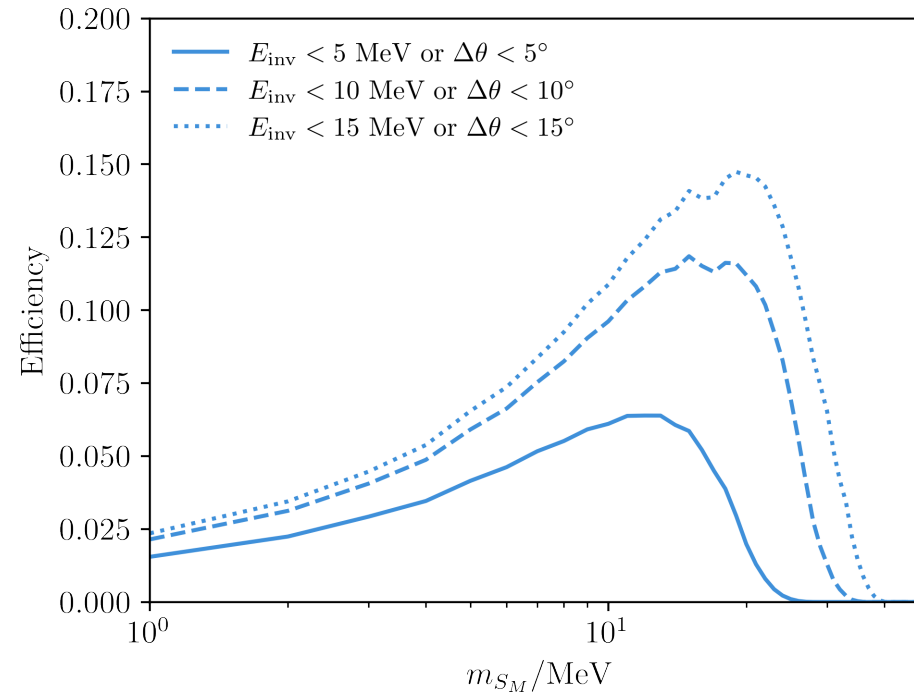
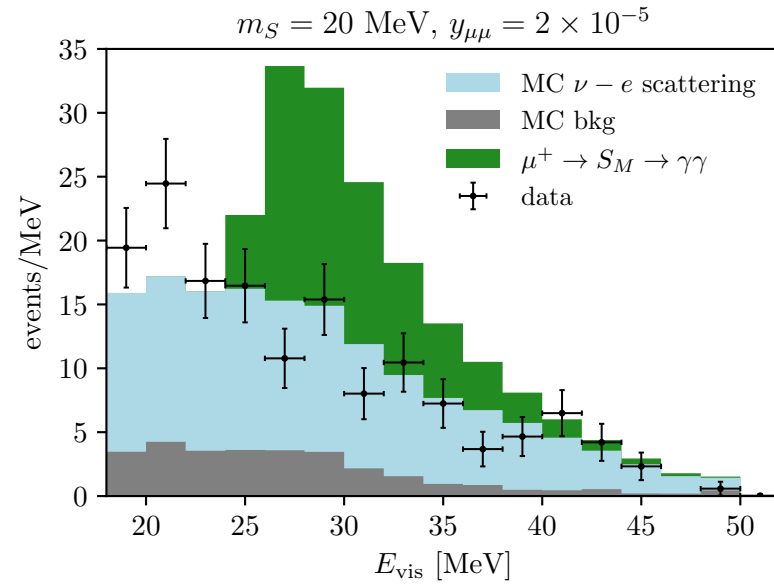
$$\propto \frac{c_{\mu e}^2 c_{ee}^2}{f_a^4}.$$



KARMEN



LSND



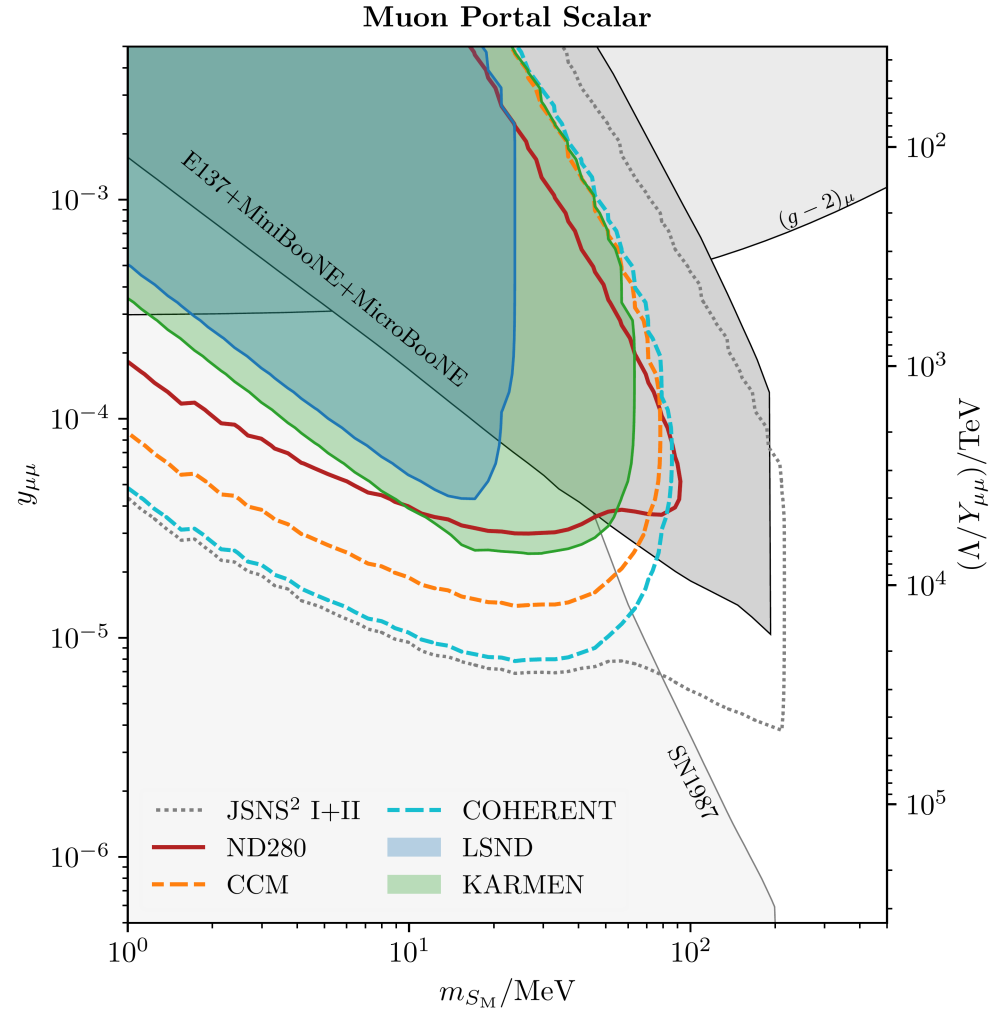
Muon scalar

$$\mathcal{L}_{S_M} \supset \frac{1}{2} \partial_\mu S_M \partial^\mu S_M - \frac{m_{S_M}^2}{2} S_M^2 - y_{\mu\mu} S_M \bar{\mu} (c_S + c_P \gamma_5) \mu$$

$$\Gamma_{S_M \rightarrow \gamma\gamma} = \frac{\alpha^2 m_{S_M}^3}{64\pi^3} \left| \frac{y_{\mu\mu}}{m_\mu} x [1 + (1-x)f(x)] \right|^2,$$

with the loop function

$$f(x) = \begin{cases} \arcsin^2 \left(\sqrt{x^{-1}} \right), & x > 1 \\ -\frac{1}{4} \left[\ln \left(\frac{1+\sqrt{1-x}}{1-\sqrt{1-x}} \right) - i\pi \right]^2, & x \leq 1 \end{cases}$$



Higgs portal scalar

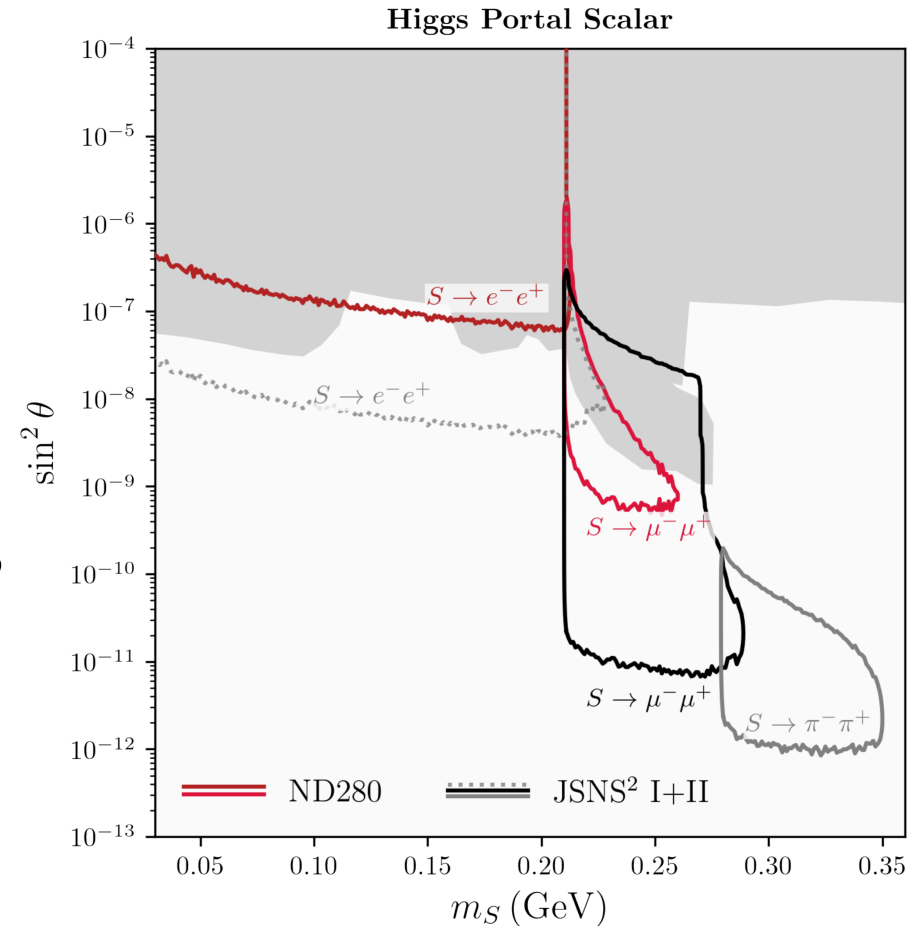
$$L_S \supset \frac{1}{2} \partial_\mu S \partial^\mu S - \frac{m_{S_M}^2}{2} S^2 - \sin \theta S \sum_f \left(\frac{m_f}{v} \bar{f} f \right)$$

$$K^+ \rightarrow \pi^+ S$$

$$\Gamma_{S \rightarrow \ell^+ \ell^-} = \sin^2 \theta \frac{m_\ell^2 m_S}{v^2 8\pi} \left(1 - \frac{4m_\ell^2}{m_S^2} \right)^{3/2}.$$

$$\Gamma_{S \rightarrow \pi\pi} = \sin^2 \theta \frac{3 |G_\pi(m_S^2)|^2}{32\pi v^2 m_S} \left(1 - \frac{4m_\pi^2}{m_S^2} \right)^{1/2},$$

where $G_\pi(s) = (2s + m_\pi^2) / 9$



We add two new neutrinos to the SM particle content

$$N_R^1$$

$$N_R^2$$

$$L = 1$$

$$L = -1$$

$$\mathcal{L} \supset - \left(\underbrace{Y_\alpha \bar{\ell}_\alpha \tilde{\phi} N_R^1}_{\text{Linear seesaw}} + \underbrace{\epsilon Y'_\alpha \bar{\ell}_\alpha \tilde{\phi} N_R^2}_{\text{Linear seesaw}} + \frac{\Lambda}{2} \bar{N}_R^{1c} N_R^2 + \frac{\mu}{2} \bar{N}_R^{2c} N_R^2 \right) + \text{h.c.}$$

Sources of lepton number violation

$$M = \begin{pmatrix} 0 & \mathbf{Y} v & \epsilon \mathbf{Y}' v \\ \mathbf{Y}^T v & 0 & \Lambda \\ \epsilon \mathbf{Y}'^T v & \Lambda & \mu \end{pmatrix}$$

Linear-inverse seesaw (LISS) = Linear seesaw + Inverse seesaw

$$|Yv|, |\epsilon Y'v|, |\mu| \ll \Lambda$$

$$U_B^T M_{\text{LISS}} U_B = \begin{pmatrix} m_{\text{light}}^{3 \times 3} & 0_{3 \times 1} & 0_{3 \times 1} \\ 0_{1 \times 3} & & \\ 0_{1 \times 3} & M_{\text{heavy}}^{2 \times 2} & \end{pmatrix}$$

$$m_\nu \equiv m_{\text{light}} \simeq \frac{1}{\Lambda} \left(\mu \frac{Y_N Y_N^T v^2}{\Lambda} - (\epsilon v^2 Y_N Y_N'^T + \epsilon v^2 Y_N' Y_N^T) \right)$$

$$M_{\text{heavy}} \simeq \begin{pmatrix} 0 & \Lambda \\ \Lambda & \mu \end{pmatrix} \qquad m_{4,5} \simeq \Lambda \pm \frac{1}{2} |\mu|$$

The two heavy neutrinos form a pseudo-Dirac pair