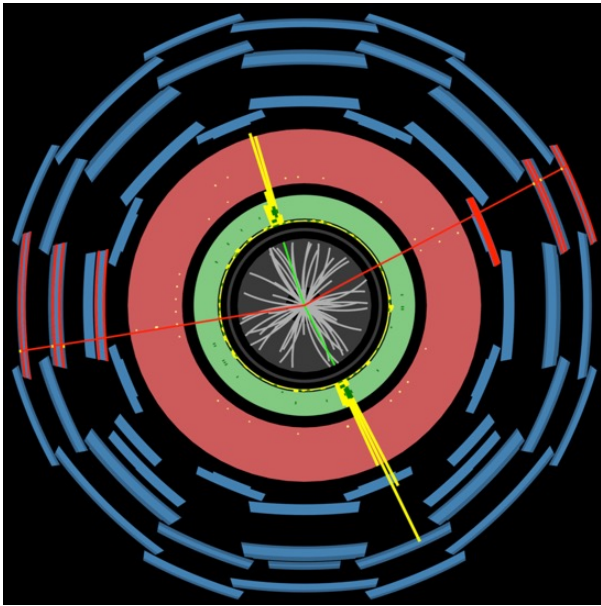


# Higgs and Electroweak physics (II)

Les futurs collisionneurs et leur physique



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# Higgs & EW physics part 2: Outline

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## Study of the gauge sector

### ★ Z parameter measurements @ $e^+e^-$ colliders ( $\sqrt{s} \sim 91$ GeV)

- \*  $M_Z, \Gamma_Z, \sigma_{\text{had}}^0, A_{\text{FB}}^0$

- \* Energy calibration and luminosity measurements

### ★ EW parameters measurements @ pp and $e^+e^-$ colliders

- \*  $\sin^2 \vartheta_{\text{eff}}$

- \*  $M_W, \Gamma_W$

### ★ Diboson processes

- \* Triple gauge couplings

- \* Vector boson scattering

# The gauge sector of the Standard Model

Strength tensor of EW gauge bosons and of gluons

$$D^\mu \gamma_\mu \equiv \not{D}^\mu$$

$$\mathcal{L}_{gauge} = -\frac{1}{4} F_{\mu\nu}^a F^{a\mu\nu} + i\bar{\psi} \not{D}\psi$$

**The gauge sector**

$$D^\mu = \partial^\mu - igW_i^\mu \frac{\sigma^i}{2} - ig' \frac{Y(\psi)}{2} B^\mu$$

$W_i, B = 4$  vector fields

- ★ Kinetic energy of gauge bosons (gluons and EW bosons)
- ★ Give rise to boson self-couplings for gluons and WEAK bosons



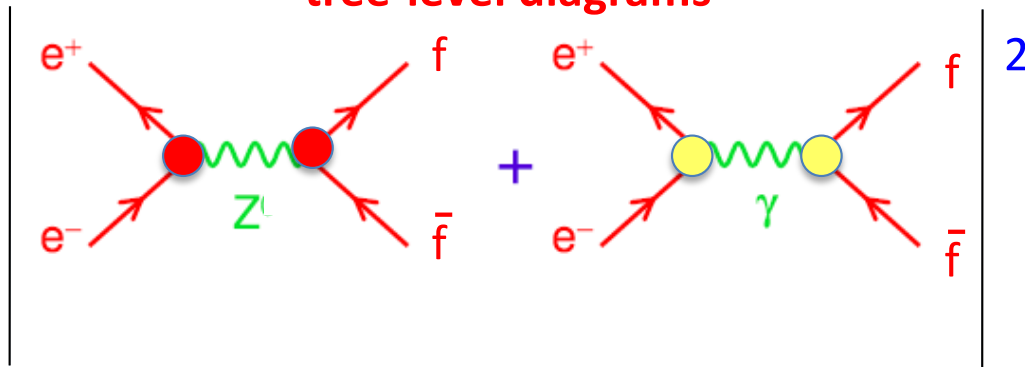
- ★ Kinetic energy of fermions and interactions between the fermions represented by spinor fields  $\psi$  and the gauge bosons
- ★ Interactions from the invariance of the  $L$  under local gauge transformations of the fermion fields

In this lecture we treat the study of the interactions mediated by  $Z/\gamma, W^\pm$

✓ **Motivation: we want to test the validity limits of SM**

# Z parameter measurements @ e<sup>+</sup>e<sup>-</sup> colliders ( $\sqrt{s} \sim 91$ GeV)

tree-level diagrams



$$\bullet = -i \frac{g}{\cos \vartheta_W} \gamma^\mu \left( \frac{g_V^f - g_A^f \gamma_5}{2} \right)$$

$g_V, g_A$  = Z couplings to fermions

$$g_V^f = T_f^3 - 2Q^f \sin^2 \vartheta_W$$

$$g_A^f = T_f^3$$

$T_f^3$  and  $Q^f$  :

EW fermion

quantum numbers

$$g_V = (c_L - c_R)/2$$

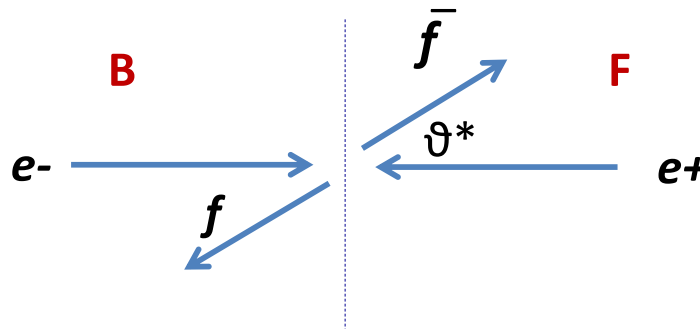
$$g_A = (c_L + c_R)/2$$

@  $\sqrt{s} = M_Z$ :

$$\sigma_{\text{had}}^0 \equiv \frac{12\pi}{m_Z^2} \frac{\Gamma_{ee}\Gamma_{\text{had}}}{\Gamma_Z^2} \quad \Gamma_{Z \rightarrow f\bar{f}} = N_c \frac{g_Z^2 M_Z}{48\pi} (g_V^2 + g_A^2)$$

$$R_\ell^0 \equiv \Gamma_{\text{had}}/\Gamma_{\ell\ell}$$

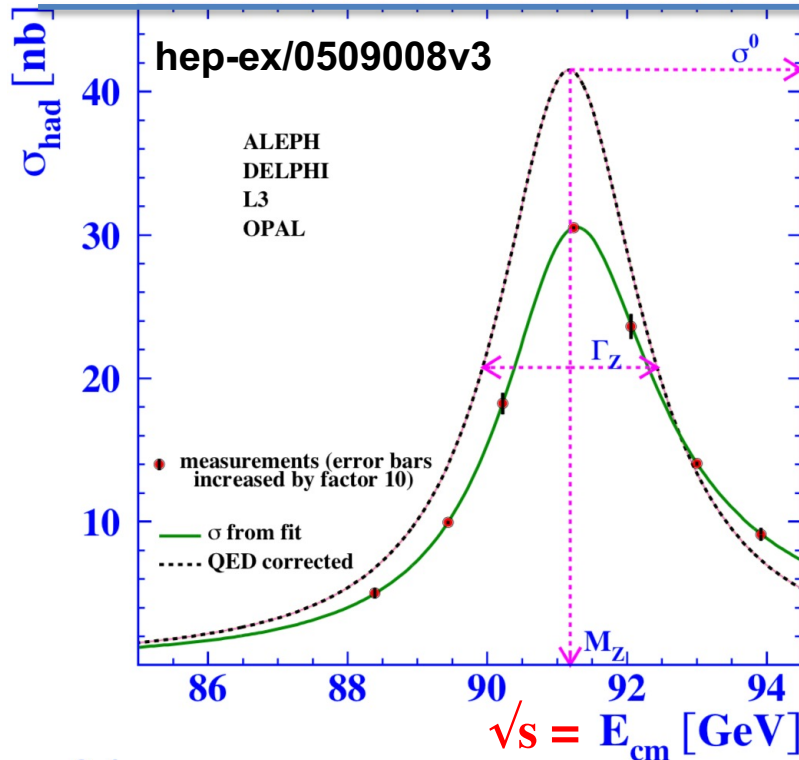
$$A_{\text{FB}} \equiv \frac{\sigma_F - \sigma_B}{\sigma_F + \sigma_B} = \frac{3}{4} A_e A_f$$



$$A_{e,f} = \frac{g_V^* g_A}{(g_V^2 + g_A^2)}$$

■  $M_Z, \Gamma_Z, \sigma_{\text{had}}^0, A_{\text{FB}}^0$

# $e^+e^-$ colliders @ $\sqrt{s} \sim 91$ GeV: $\sqrt{s}$ scan $\rightarrow M_Z, \sigma_{\text{had}}^0$



\*  $M_Z$  is used as input to EW calculations  
currently  $\Delta M_Z \sim 2$  MeV (LEP)

\* @ future  $e^+e^-$  colliders very high statistics:

$\rightarrow$  Achieve precision well beyond LEP:

\* Statistical uncertainty: **4 keV @ FCC-ee**

\* Dominant systematic:

o **Absolute beam energy calibration** (FCC-ee)  
resonant depolarisation:  $\Delta\sqrt{s} \sim \Delta M_Z \sim 100$  keV

o Absolute momentum scale (LCF)

$\Delta p \sim \Delta M_Z \sim 200$  keV with  $J/\psi$  mass ( $K_S \rightarrow \pi\pi$ )

\*  $\sigma_{\text{had}}^0$  peak cross-section

\* Sensitive to  $Zee$  coupling and total width  $\Gamma_Z$ , provides  $N_\nu$

\* Limited by **luminosity determination**,

$\delta L/L$  (Bhabha)  $\sim 10^{-4}$  (FCC-ee, LEP3, LCF)

$e^+e^- \rightarrow \gamma\gamma \sim 2(4) \times 10^{-5}$  (FCC-ee, LEP3)

$$\Gamma_Z = \sum_q \Gamma_{qq} + 3 \Gamma_{ll} + N_\nu \Gamma_{\nu\nu}$$

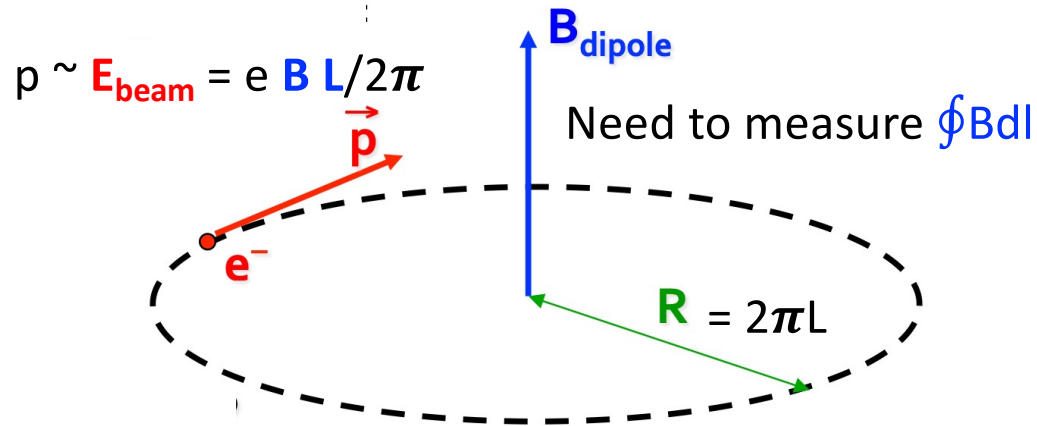
$$\sigma_{\text{had}}^0 \equiv \frac{12\pi}{m_Z^2} \frac{\Gamma_{ee}\Gamma_{\text{had}}}{\Gamma_Z^2}$$

$$N_\nu \left( \frac{\Gamma_{\nu\nu}}{\Gamma_{\ell\ell}} \right)_{\text{SM}} = \left( \frac{12\pi}{m_Z^2} \frac{R_\ell^0}{\sigma_{\text{had}}^0} \right)^{\frac{1}{2}} - R_\ell^0 - 3 - \delta_\tau$$

# Absolute beam energy calibration @ e<sup>+</sup>e<sup>-</sup> colliders @ $\sqrt{s} \sim 91$ GeV)

P. Janot

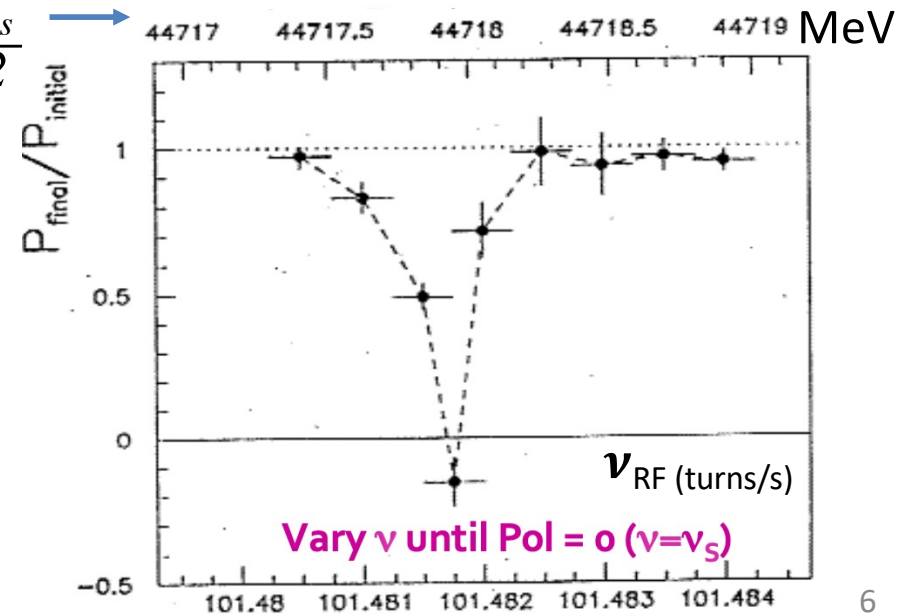
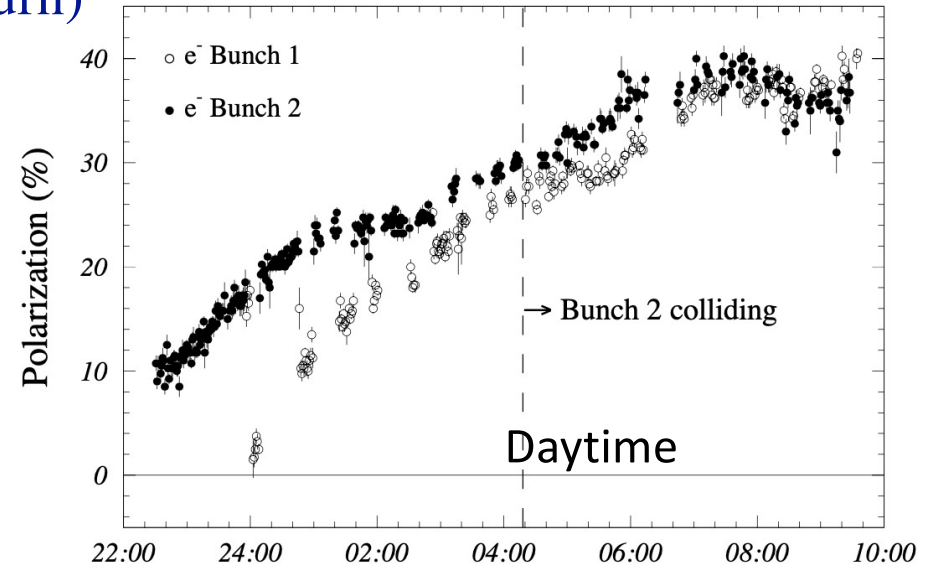
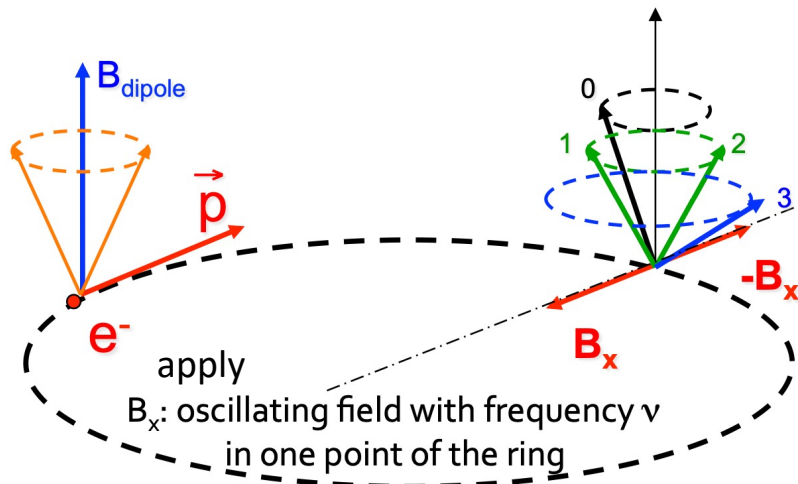
- $\sqrt{s}$  calibration from spin tune ( $\nu_s$ ) measurements via **resonant depolarisation** (spin tune = number of precessions per turn)



Precession frequency  $\nu_s$  proportional to B

To measure  $\nu_s \rightarrow$  apply RF e.m. field

$$\frac{E_{\text{beam}}}{m_e} = \frac{2}{g_e - 2} \nu_s$$



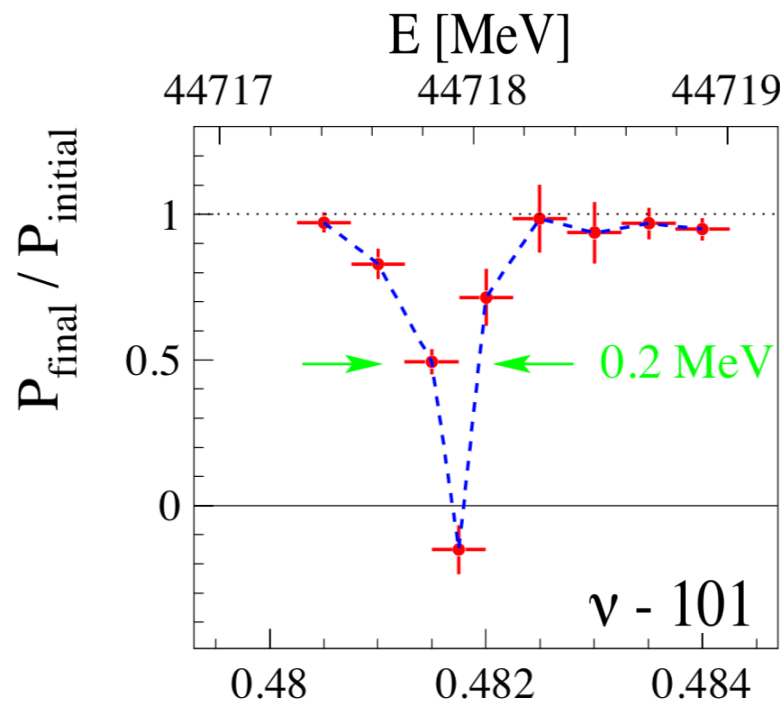


# Absolute beam energy calibration @ e<sup>+</sup>e<sup>-</sup> colliders

- Common uncertainty across experiments
- $\sqrt{s}$  calibration from spin tune ( $\nu_s$ ) measurements via resonant depolarisation

$$\frac{E}{m_e} = \frac{2}{g_{e^-} - 2} \nu_s$$

- Control of  $\sqrt{s}$  uncertainties essential for precision on  $M_Z$ ,  $\Gamma_Z$ ,  $A_{FB}$



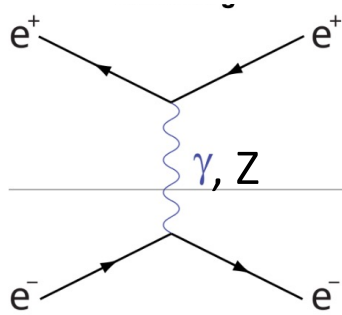
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Origin of correction	(approx. errors)	Error on	
		$m_Z$	$\Gamma_Z$
		[MeV]	[MeV]
Energy measurement by resonant depolarisation		0.4	0.5
Mean fill energy, from uncalibrated fills		0.5	0.8
Dipole field changes		<u>1.7</u>	0.6
Tidal deformations		0.0	0.1
e <sup>+</sup> energy difference		0.2	0.1
Bending field from horizontal correctors		0.2	0.1
IP dependent RF corrections		0.4	0.2
Dispersion at IPs		0.2	0.1

- Impact on EWPO uncertainty also from beam energy spread:  $\delta E$
- @ FCC :  $\delta E$  increases wrt LEP and may fluctuate (beamstrahlung)  
Measured with e<sup>+</sup>e<sup>-</sup> → μ<sup>+</sup>μ<sup>-</sup> (5') (arXiv:1812.01004)

# Luminosity measurement L @ e<sup>+</sup>e<sup>-</sup> colliders

- Luminosity **L** from **small-angle** Bhabha-scattering



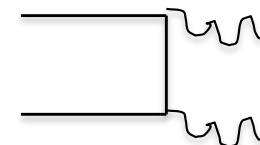
$$L = \frac{\frac{dN}{d(\cos\theta)}}{\frac{d\sigma}{d(\cos\theta)}}$$

measure  
(counting)
theory

$$\sigma = \frac{16\pi\alpha^2}{s} \left( \frac{1}{\theta_{\min}^2} - \frac{1}{\theta_{\max}^2} \right)$$

- **L** uncertainty important for  $\sigma_{\text{had}}^0$   
( @LEP after combination contributes to  $\sim$  half its total error )
- Main **experimental error** on **L** :  
Definition of geometrical acceptance (use of special methods, or W mask)
- **Theory error** is the biggest single contribution ( $\approx 0.5\%$  @ LEP)
- Total error @LEP :  $\Delta L/L \sim 10^{-3}$  (ADL)
- ⚠ (reanalysis 1908.01704 beam-beam effect:  $10^{-3}$  bias)

- @ **FCC-ee** (1812.01004) (use also  $ee \rightarrow \gamma\gamma$ ):  
 $\Delta L/L$ : absolute  $\sim 10^{-4}$  ( $\rightarrow$  reduction of factor 8 on  $\Delta N_\nu$ )  
 $\Delta L/L$ :  $\sqrt{s}$  point-to-point  $5 \times 10^{-5}$  (relevant for  $\Gamma_Z$ )





# Z total width : $\Gamma_Z$ @ $e^+e^-$ colliders ( $\sqrt{s} \sim 91$ GeV)

\* Z total width,  $\Gamma_Z$ , sensitive to fermion couplings and to BSM

In SM

At tree level:

$$\Gamma_{Z \rightarrow ff} = N_c \frac{g_Z^2 M_Z}{48 \pi} (g_V^2 + g_A^2)$$

$$\Gamma_Z = \sum_f \Gamma_{Z \rightarrow ff}$$

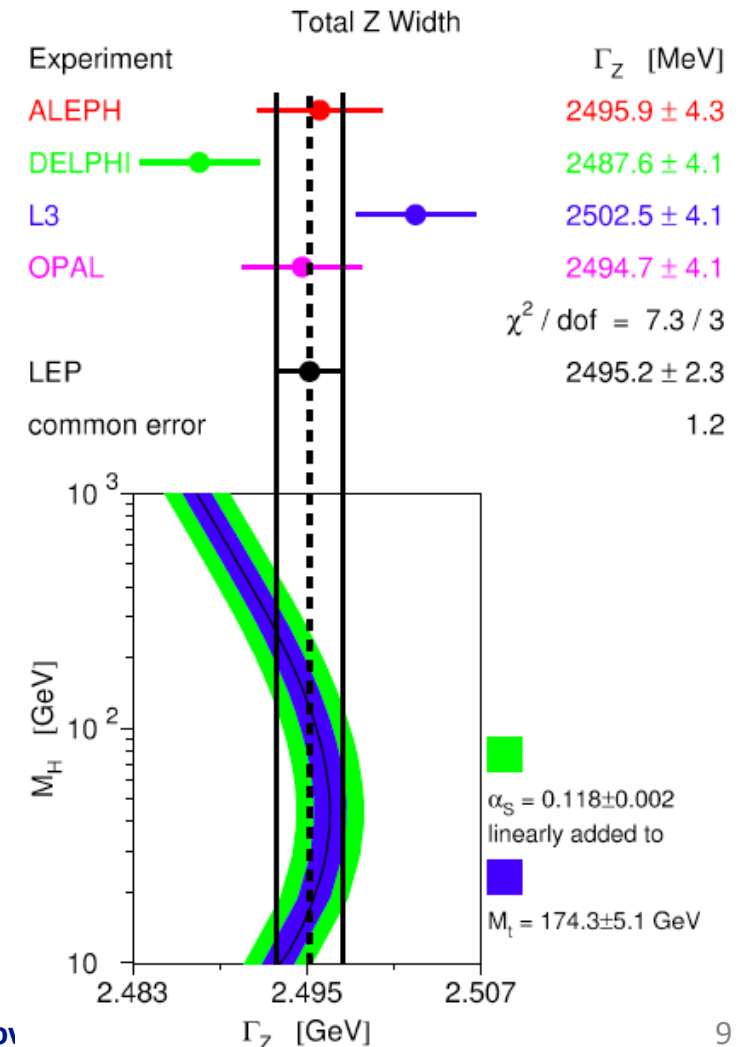
\* Dependence on  $\alpha_s, M_t, M_H$  through radiative corrections

\* Currently  $\Delta\Gamma_Z \sim 2$  MeV

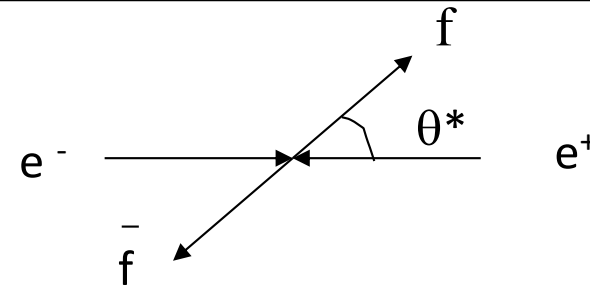
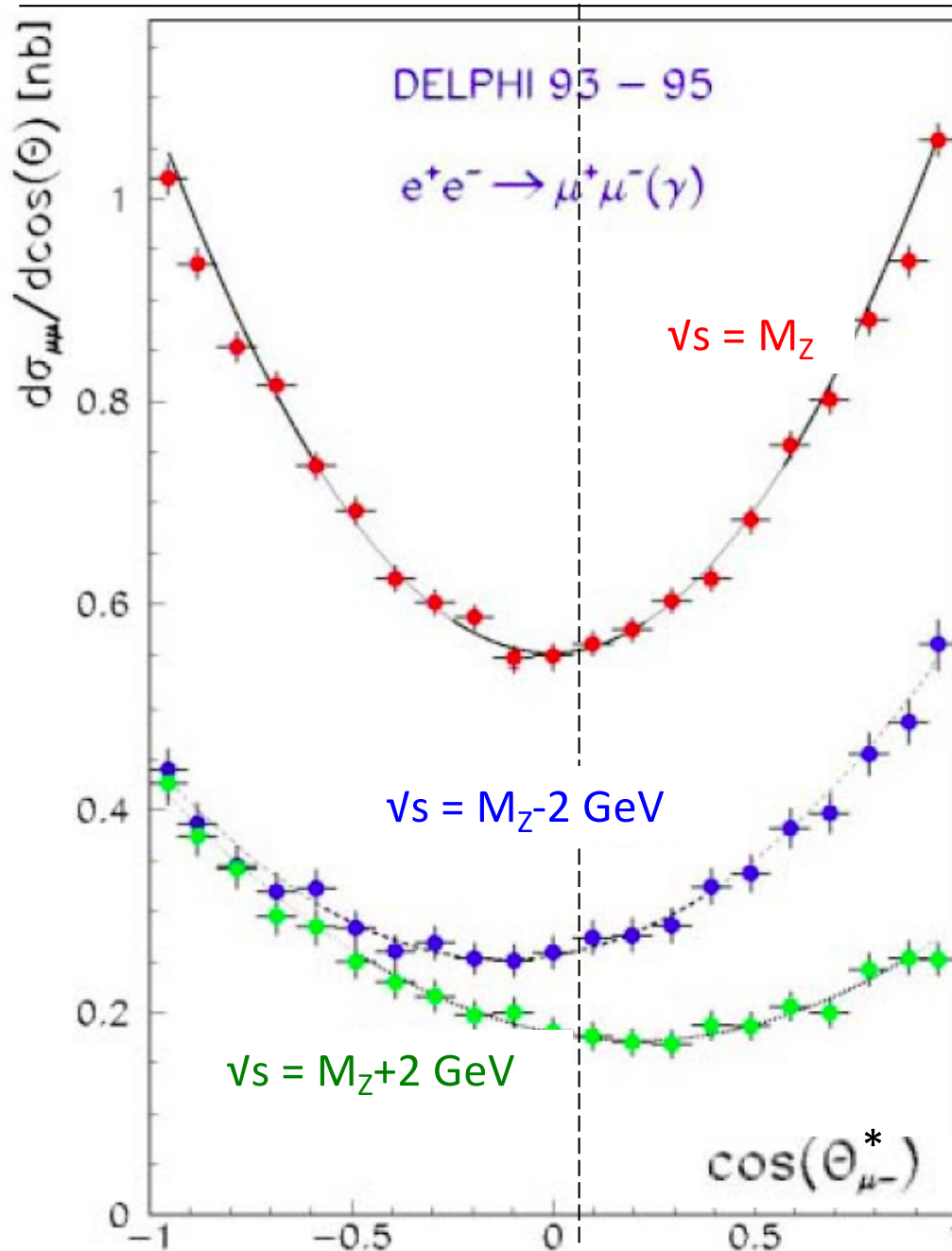
\* Dominant systematic:

$\Delta\sqrt{s}$  : point-to-point and absolute energy calibration  
can be measured in-situ with  $\mu\mu$  events

$\Delta\Gamma_Z \sim 12$  keV @ FCC-ee



# Z Forward-Backward (FB) Asymmetry (here in $\mu$ channel)



$$\frac{d\sigma}{d\cos\theta^*} \propto (g_v^{e^2} + g_a^{e^2})(g_v^{\mu^2} + g_a^{\mu^2})(1 + \cos^2\theta^*) + 8g_v^e g_a^e g_v^\mu g_a^\mu \cos\theta^*$$

★ Origin : parity violation in neutral weak interactions

$$\frac{d\sigma}{d\cos\theta^*} \propto (1 + \cos^2\theta^* + \frac{8}{3}A_{FB}^{0,\mu}\cos\theta^*)$$

↖ ~ 2%

$A_{FB}^0$  = Asymmetry @ peak

Asymmetries in Z final states

--> dependence on  $\sin^2\theta_W$

# Asymmetries @ $\sqrt{s} = 91 \text{ GeV}$

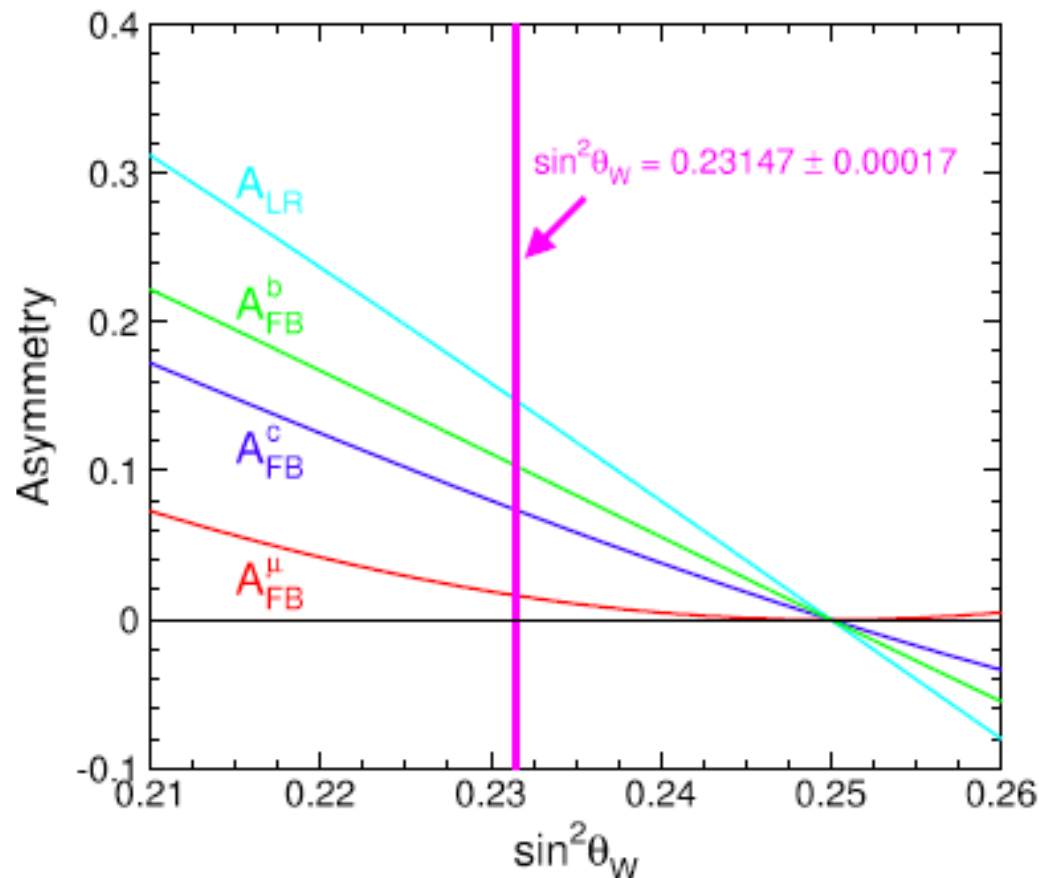
forward-backward

$$A_{\text{FB}} \equiv \frac{\sigma_{\text{F}} - \sigma_{\text{B}}}{\sigma_{\text{F}} + \sigma_{\text{B}}} = \frac{3}{4} A_{\text{e}} A_{\text{f}}$$

Left-right  
Beam  
polarization

$$A_{\text{LR}} \equiv \frac{\sigma(e_{\text{L}}) - \sigma(e_{\text{R}})}{\sigma(e_{\text{L}}) + \sigma(e_{\text{R}})} = A_{\text{e}}$$

$$A_{\text{f}} = 2 \frac{g_{\text{Vf}}/g_{\text{Af}}}{1 + (g_{\text{Vf}}/g_{\text{Af}})^2} = \frac{g_{\text{Lf}}^2 - g_{\text{Rf}}^2}{g_{\text{Lf}}^2 + g_{\text{Rf}}^2}$$



Asymmetries can be converted in a measurement of  $\sin^2 \theta_{\text{W}}$

$A_{\text{LR}}$  gives the largest asymmetry and greatest sensitivity (high slope)

Polarisation easier @ linear collider to work with polarised the beams

# EW parameter: $\sin^2 \vartheta_{\text{eff}}^{\text{lep}}$ @ pp colliders ( $\sqrt{s} \sim 91 \text{ GeV}$ )

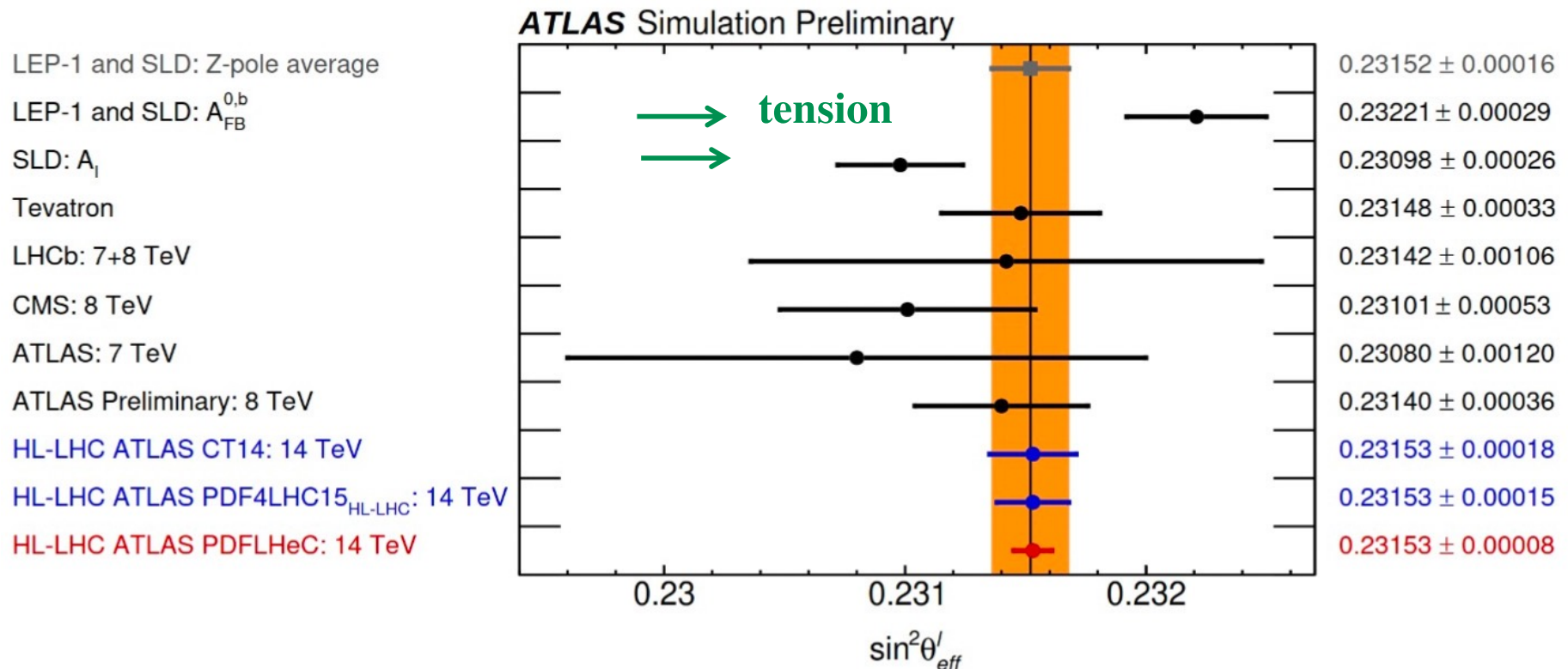
## ■ Tension between the most sensitive results

@  $p\bar{p}$  colliders :

- \* **Forward Backward Asymmetry** ( $A_{\text{FB}}$ ) in  $q\bar{q} \rightarrow Z (\rightarrow l\bar{l})$
- \* Angular decomposition of the cross-section  $q\bar{q} \rightarrow Z/\gamma^* \rightarrow l\bar{l}$
- \* **Parton Distribution Function (PDF)** source of main systematics
- \* **Prospects for reaching LEP+SLD uncertainty at the end of HL-LHC**

$$\sin_{\text{eff}}^2 \theta_W = \left(1 - \frac{m_W^2}{m_Z^2}\right) \kappa$$

↑  
e.w. corrections



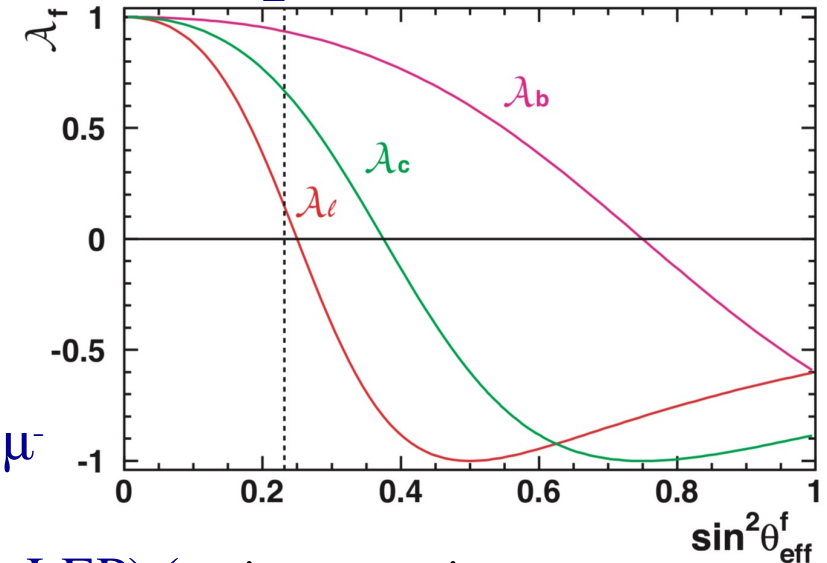
# Extraction of $\sin^2 \vartheta_{\text{eff}}^{\ell}$ @ $e^+e^-$ circular colliders ( $\sqrt{s} \sim 91$ GeV)

- \*  $e^+e^-$  colliders unique power for  $\sin^2 \vartheta_{\text{eff}}^{\ell}$  determination @  $M_Z$

$$A_{\text{FB}}^{0,f} = \frac{3}{4} \mathcal{A}_e \mathcal{A}_f \quad \mathcal{A}_f = 2 \frac{g_{Vf}/g_{Af}}{1 + (g_{Vf}/g_{Af})^2}$$

@ LEP  $A_F$  asymmetries used to extract  $\sin^2 \vartheta_{\text{eff}}^{\ell}$

$$\sin^2 \vartheta_{\text{eff}}^f = 0.23153 \pm 0.00016$$



- \* @FCC  $\rightarrow$  extraction of  $\sin^2 \vartheta_{\text{eff}}^{\ell}$  from  $e^+e^- \rightarrow \mu^+\mu^-$  assuming lepton universality

Uncertainty  $\sim 5 \cdot 10^{-6}$  (factor  $\sim 30$  smaller wrt LEP) (main uncertainty point-to-point energy error)

- \* Using  $\tau$  polarisation measurement avoids assumption on lepton universality

$$\mathcal{P}_\tau \equiv \frac{d(\sigma_r - \sigma_l)}{d \cos \theta} \bigg/ \frac{d(\sigma_r + \sigma_l)}{d \cos \theta} = - \frac{\mathcal{A}_f(1 + \cos^2 \theta) + 2\mathcal{A}_e \cos \theta}{(1 + \cos^2 \theta) + 2\mathcal{A}_f \mathcal{A}_e \cos \theta}$$

( $\nu_\tau$  flies in the same (opposite) direction as  $\tau$  for L(R) in the  $\tau$  center-of-mass)

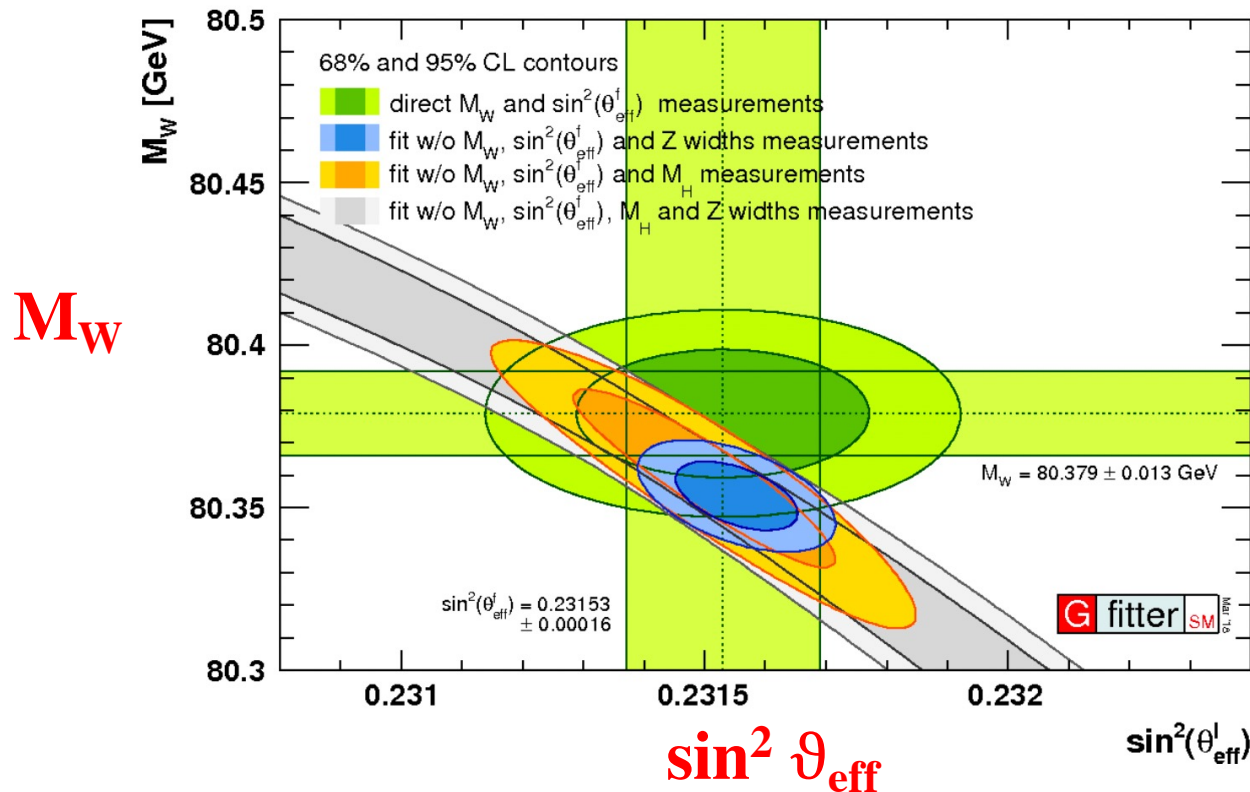
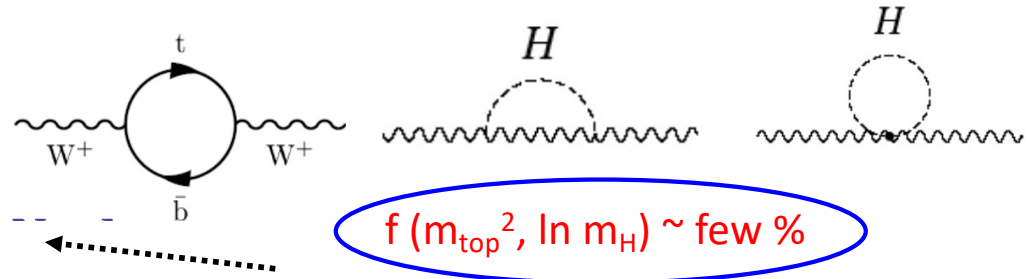
@ LEP several  $\tau$  decay modes were used. Main uncertainties: from  $\tau$  BR and hadronic  $\tau$  decay modelling

$\rightarrow$  @FCC use  $\tau \rightarrow \nu \gamma$  Uncertainty on  $\sin^2 \vartheta_{\text{eff}}^{\ell} \sim 6.6 \cdot 10^{-6}$

# $M_W$ measurement : probe BSM via electroweak precision tests

- \* Comparing indirect to direct  $M_W$  measurement tests SM internal consistency  
→ BSM probe

$$M_W = \sqrt{\frac{\pi\alpha}{\sqrt{2}G_F \sin\theta_W}} \frac{1}{\sqrt{1 - \Delta r}}$$



- \* Current results consistent with the SM relations

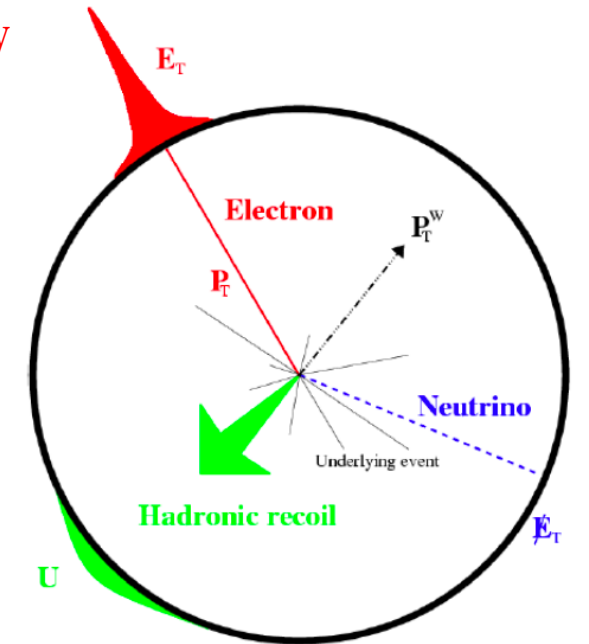
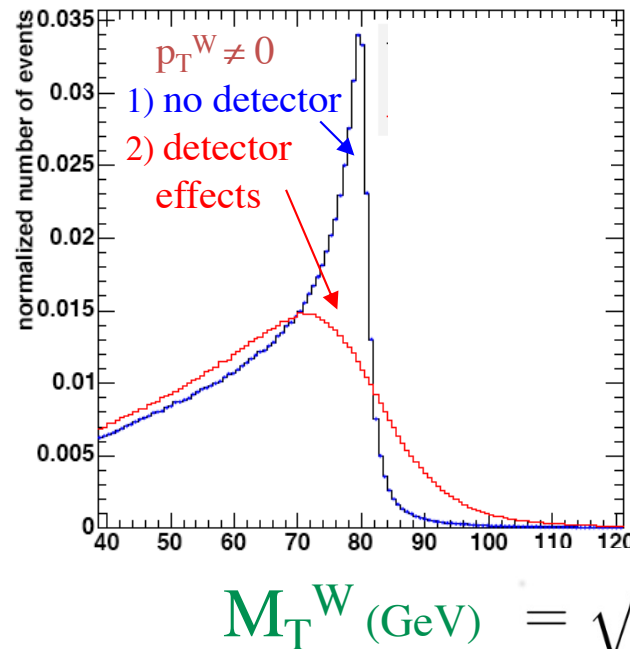
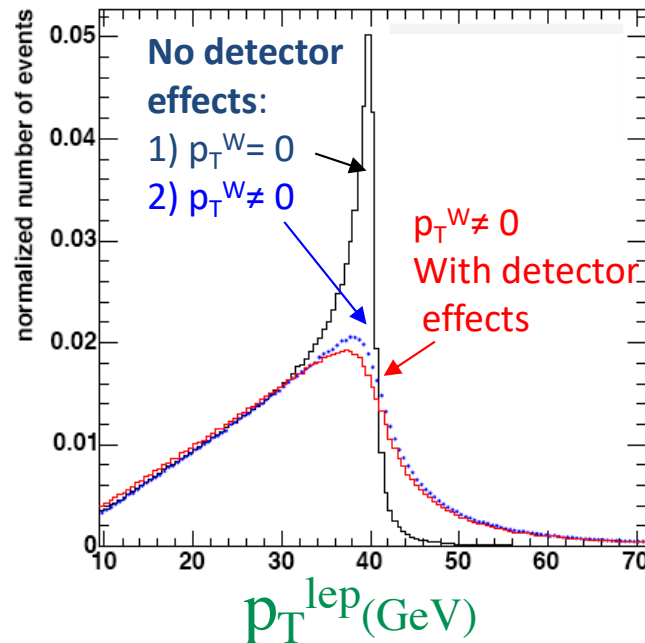


# $M_W$ measurement @ pp colliders

\* Use W leptonic decays with  $\mu$  or  $e$

\* Two main (**complementary**) variables sensitive to  $M_W$

$$pp \rightarrow W \rightarrow \ell \nu$$



$$M_T^W (\text{GeV}) = \sqrt{2p_T^\ell p_T^\nu (1 - \cos \Delta\phi(\ell, \nu))}$$

\*  $p_T^{\text{lep}}$  more dependent on physics modelling

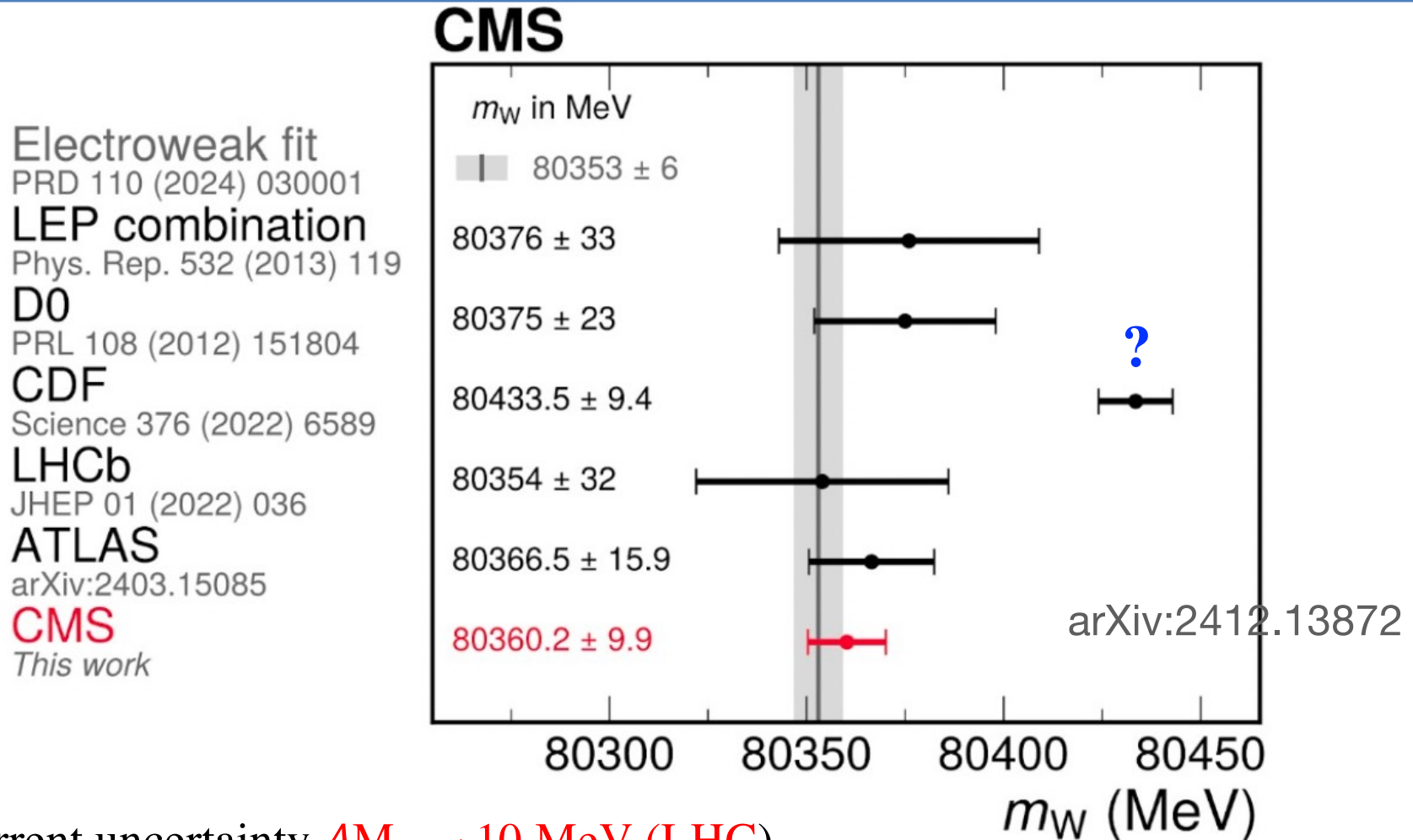
\*  $M_T^W$  degrades at high pile-up, but less dependent on modelling

Challenges:

Ultra-precise detector calibration  $\sim 10^{-4}$

Accurate theory predictions

# $M_W$ measurements



Current uncertainty  $\Delta M_W \sim 10$  MeV (LHC)

- @ pp colliders: PDF main source of systematics (followed by QCD modelling)

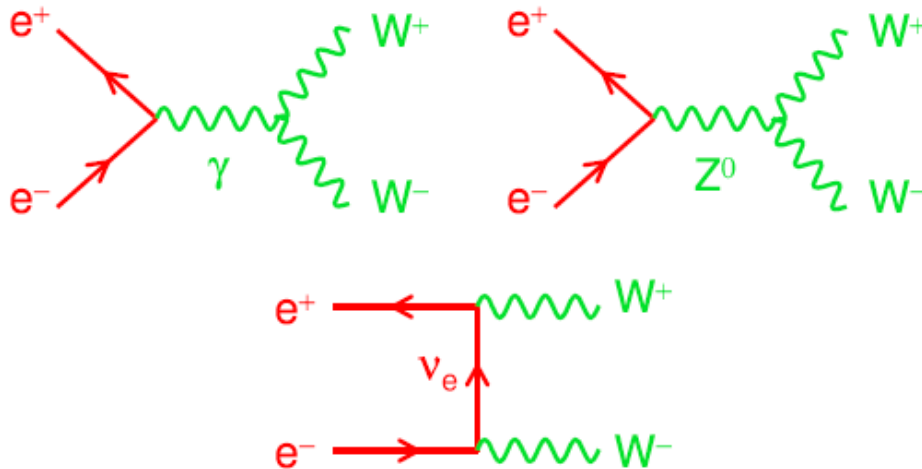
$$\Delta M_W^{\text{HL-LHC}} \sim 5 \div 10 \text{ MeV}$$

$$(\Delta M_W^{\text{PDF}} \sim 2 \text{ MeV with LHeC})$$

# Measurements of $M_W$ @ $e^+e^-$ colliders

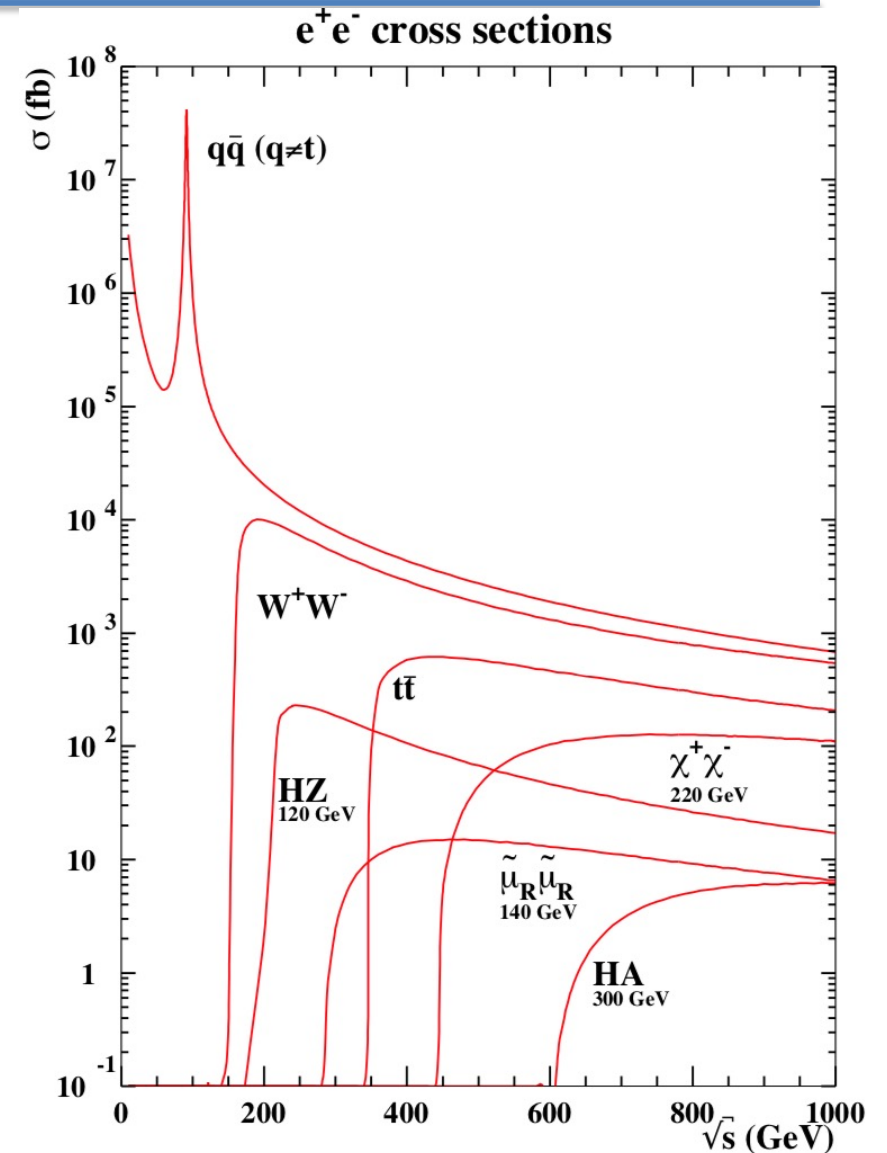
\*  **$e^+e^-$  colliders** have a unique power to measure directly  $M_W$

## $W^+W^-$ Pair Production



Two approaches:

1. Measurements at  $WW$  threshold
2. Direct reconstruction of the  $W$  mass (+ **kinematic fit**)



# Measurements of $M_W$ @ WW threshold (@ $e^+e^-$ colliders )

- \* Scan : cross-section vs. beam energy
- \* Best sensitivity @  $\sqrt{s} \sim 162.3$  GeV where dependence on  $\Gamma_W \sim$  vanishes

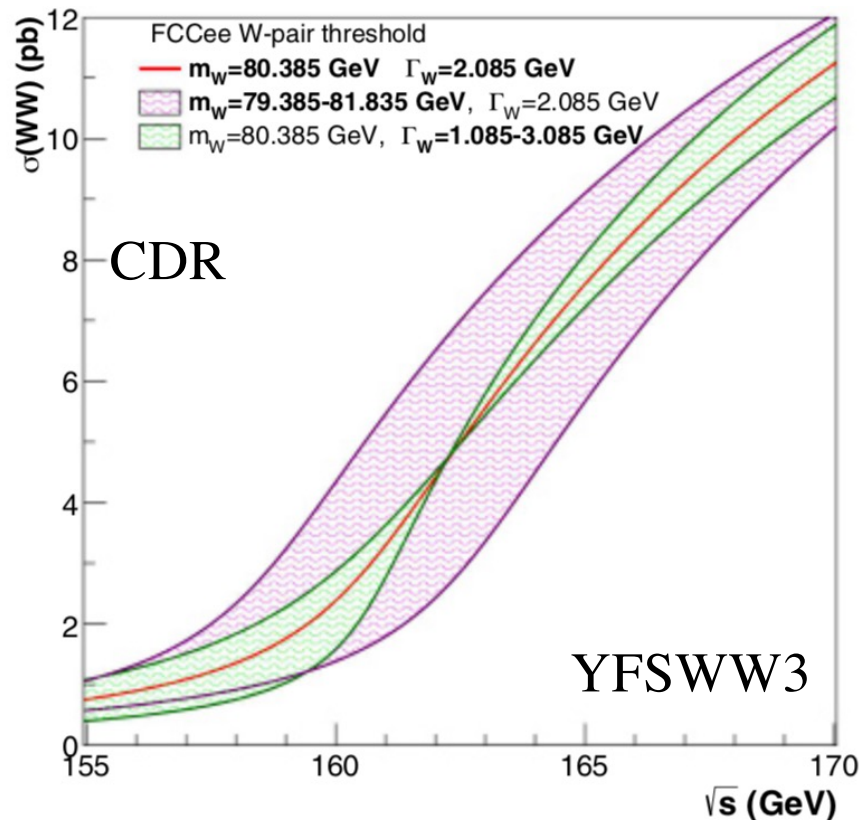
- \* With 2 or more energy points measure mass  $M_W$  and width  $\Gamma_W$  simultaneously

$$\Delta M_W^{\text{stat}} \sim 400 \text{ keV (FCC-ee)}$$

$$\Delta \Gamma_W^{\text{stat}} \sim 1 \text{ MeV (FCC-ee)}$$

- \* Dominant systematics  
absolute beam energy calibration
- \* Assuming 300 keV on  $\sqrt{s}$  with resonant depolarisation

$$\Delta M_W^{\text{syst}} \sim 150 \text{ keV (FCC-ee)}$$



→ With  $12 \text{ ab}^{-1}$  :  $\Delta M_W^{\text{tot}} \sim 0.5 \text{ MeV}$  within reach

# Direct Measurements of $M_W$ (@ $e^+e^-$ colliders )

@  $\sqrt{s} \sim 160$  GeV (WW threshold) &  $\sqrt{s} \sim 240$  GeV

\*  $M_W$  through direct reconstruction of decay products **with kinematic fit**( as in LEP2)

\* Best sensitivity from the **WW  $\rightarrow$  qq $\ell\nu$  channel**

★ Avoid issues with **color reconnection**

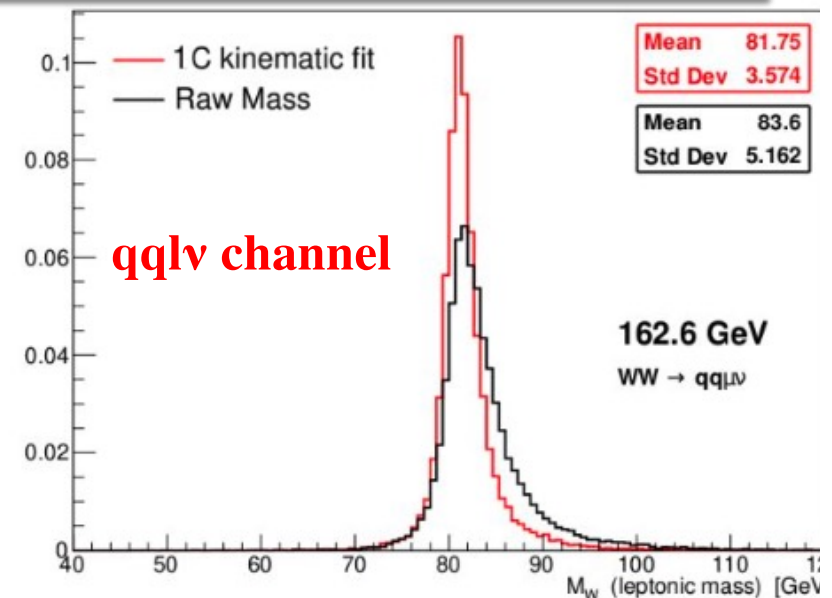
★ Allows to fully resolve the neutrino kinematics in the **kinematics fit** (4-3 = 1 constraint )

★ Use also the constraint that W masses are equal (2C fit)

★ Dominant systematics :

Absolute energy and beam energy scale calibration

Hadronization



Observable	present value	±	uncertainty	FCC-ee Stat.	FCC-ee Syst.	Comment and leading uncertainty
$m_Z$ (keV)	91 187 600	±	2000	<b>4</b>	100	From Z line shape scan Beam energy calibration
$\Gamma_Z$ (keV)	2 495 500	±	2300	<b>4</b>	12	From Z line shape scan Beam energy calibration
$\sin^2 \theta_W^{\text{eff}} (\times 10^6)$	231,480	±	160	<b>1.2</b>	1.2	From $A_{\text{FB}}^{\mu\mu}$ at Z peak Beam energy calibration
$1/\alpha_{\text{QED}}(m_Z^2) (\times 10^3)$	128 952	±	14	<b>3.9</b> <b>0.8</b>	small tbc	From $A_{\text{FB}}^{\mu\mu}$ off peak From $A_{\text{FB}}^{\mu\mu}$ on peak QED&EW uncert. dominate
$R_\ell^Z (\times 10^3)$	20 767	±	25	<b>0.05</b>	0.05	Ratio of hadrons to leptons Acceptance for leptons
$\alpha_S(m_Z^2) (\times 10^4)$	1 196	±	30	<b>0.1</b>	1	Combined $R_\ell^Z$ , $\Gamma_{\text{tot}}^Z$ , $\sigma_{\text{had}}^0$ fit
$\sigma_{\text{had}}^0 (\times 10^3)$ (nb)	41 480.2	±	32.5	<b>0.03</b>	0.8	Peak hadronic cross section Luminosity measurement
$N_\nu (\times 10^3)$	2 996.3	±	7.4	<b>0.09</b>	0.12	Z peak cross sections Luminosity measurement
$R_b (\times 10^6)$	216 290	±	660	<b>0.25</b>	0.3	Ratio of $b\bar{b}$ to hadrons
$A_{\text{FB}}^{b,0} (\times 10^4)$	992	±	16	<b>0.04</b>	0.04	b-quark asymmetry at Z pole From jet charge
$A_{\text{FB}}^{\text{pol},\tau} (\times 10^4)$	1 498	±	49	<b>0.07</b>	0.2	$\tau$ polarisation asymmetry $\tau$ decay physics
$\tau$ lifetime (fs)	290.3	±	0.5	<b>0.001</b>	0.005	ISR, $\tau$ mass
$\tau$ mass (MeV)	1 776.93	±	0.09	<b>0.002</b>	0.02	estimator bias, ISR, FSR
$\tau$ leptonic ( $\mu\nu_\mu\nu_\tau$ ) BR (%)	17.38	±	0.04	<b>0.00007</b>	0.003	PID, $\pi^0$ efficiency
$m_W$ (MeV)	80 360.2	±	9.9	<b>0.18</b>	0.16	From WW threshold scan Beam energy calibration
$\Gamma_W$ (MeV)	2 085	±	42	<b>0.27</b>	0.2	From WW threshold scan Beam energy calibration
$\alpha_S(m_W^2) (\times 10^4)$	1 010	±	270	<b>2</b>	2	Combined $R_\ell^W$ , $\Gamma_{\text{tot}}^W$ fit
$N_\nu (\times 10^3)$	2 920	±	50	<b>0.5</b>	small	Ratio of invis. to leptonic in radiative Z returns

Many measurements  
(top measurement  
not included)

Systematic projections  
should be intended as  
targets for detectors/th.  
calculations



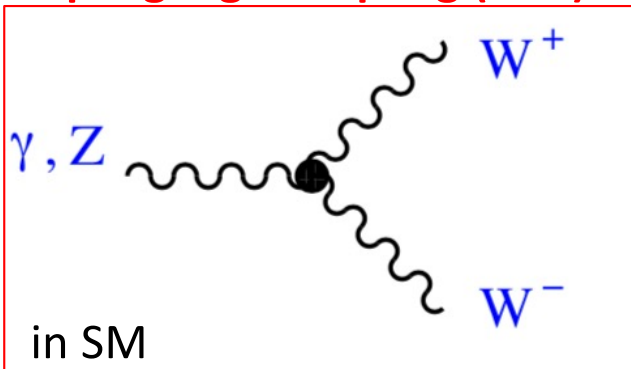
# Study of multiboson processes. Why ?

Because it allows us to study **this piece** of the e.w. SM lagrangian(\*) :

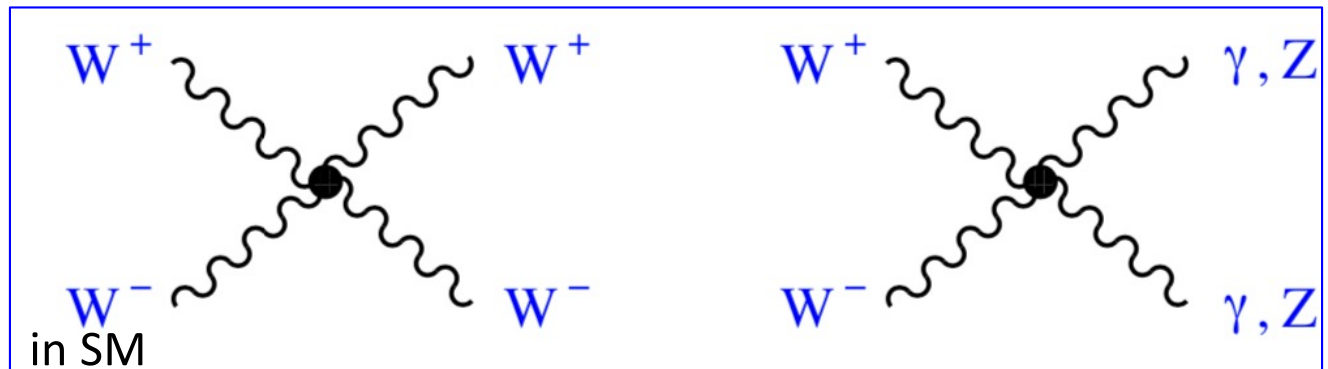
$$\mathcal{L}_{\text{Kin}} = -\frac{1}{4} B_{\mu\nu} B^{\mu\nu} - \frac{1}{4} W_{\mu\nu}^i W_i^{\mu\nu} \quad i=1,2,3 \quad B_{\mu\nu} \equiv \partial_\mu B_\nu - \partial_\nu B_\mu$$

$$W_{\mu\nu}^i = \partial_\mu W_\nu^i - \partial_\nu W_\mu^i - g \epsilon^{ijk} W_\mu^j W_\nu^k$$

**Triple gauge coupling (TGC)**



**Quartic GC**

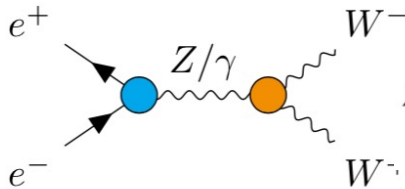
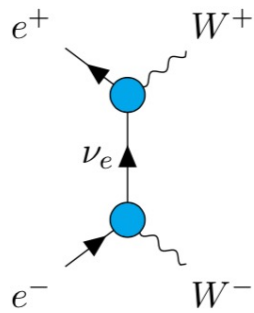


- \* Test of **the non-abelian structure** of the EW interactions
- \* Constraint on BSM
- \* **Probing the EWSB through the scattering of EW gauge bosons**

Goldstone equivalence theorem:

At  $E \gg M_V$  the amplitude for scattering of a **longitudinally polarised massive gauge boson** becomes equal to the amplitude for scattering of the **Goldstone bosons** ( $\sim -m_H^2/v^2$ )

# WW: anomalous Triple Gauge Couplings

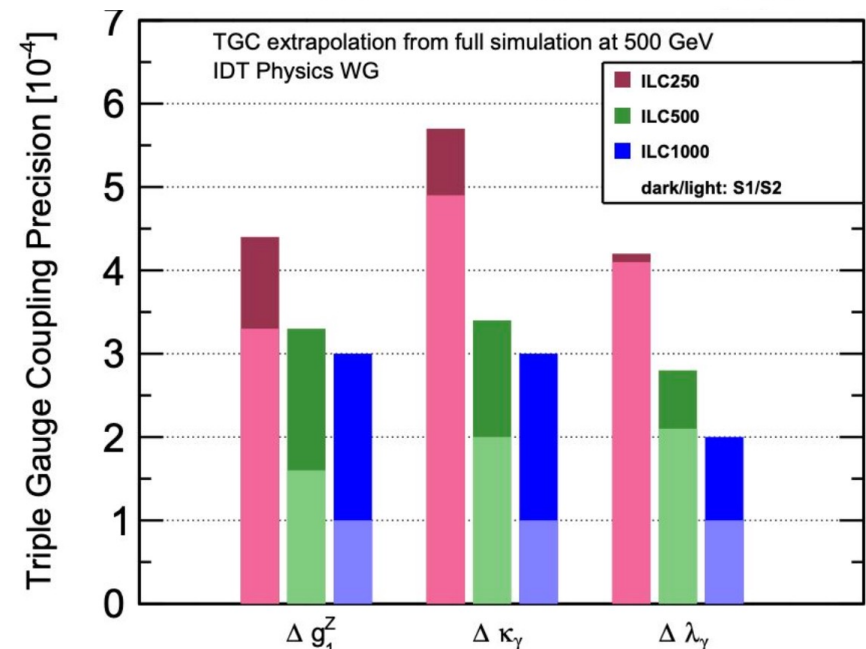
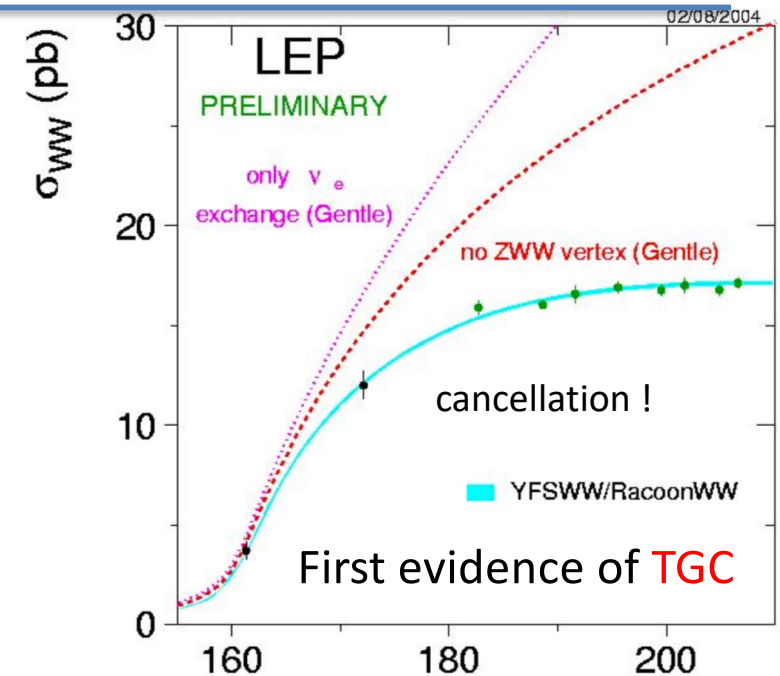


$$\mathcal{L}_{\text{dim-6}} = \sum_i \frac{f_i^{(\text{dim-6})}}{\Lambda^2} \mathcal{O}_i^{(\text{dim-6})}$$

$$\Delta \{g_1^Z, \kappa_\gamma\} \lambda_\gamma \sim \{c_i \cdot m_{W/Z}^2\}$$

Very active field @ LHC

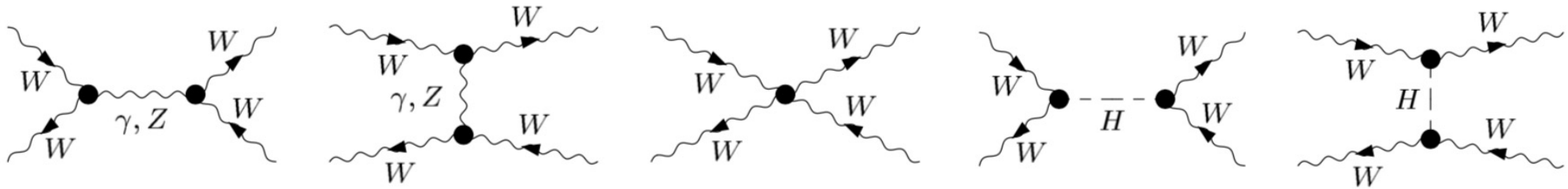
- \* High statistic and energy very important  
(energy growth of relevant operators)
- pp collider favoured but the precision allowed by kinematic fits helps when angular variables are exploited
- \* LCF has powerful constraints thanks to initial state polarisation



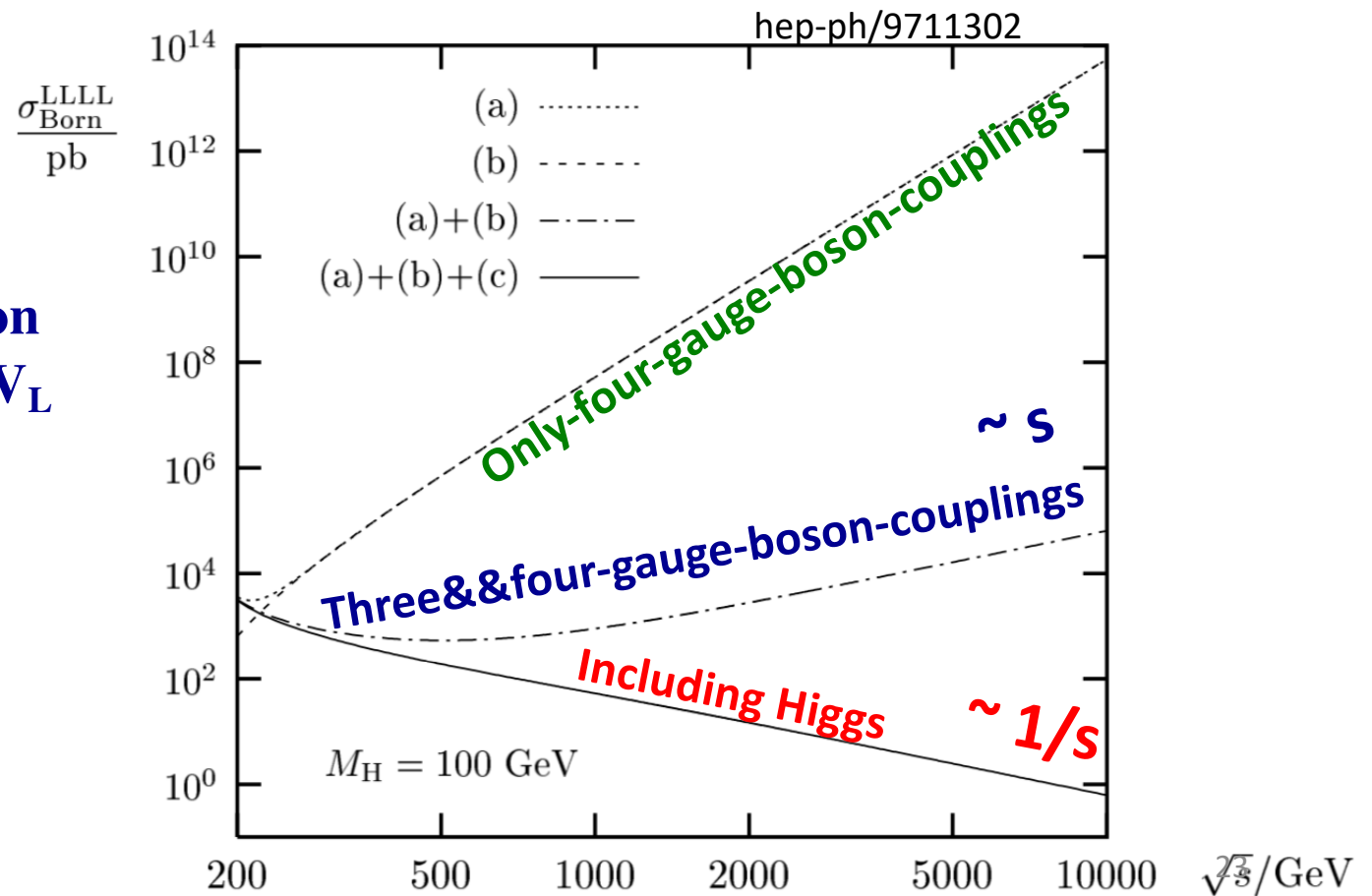
# Scattering of EW gauge bosons

( Effective W approximation )

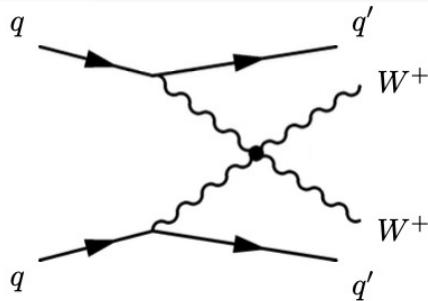
$WW \rightarrow WW$



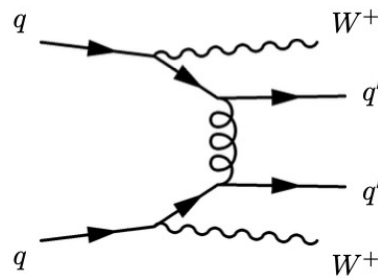
The unitarity cancellation ensure that  $V_L V_L \rightarrow V_L V_L$  'cross-section' decrease as  $1/s$  at high energies



# Scattering of EW gauge bosons



EW production



Strong production

★ Look for VV jj

★ Challenges:

- \*  $pp \rightarrow VV jj$  low cross section

- \* The LL component is  $\sim 10\%$

- \* High bkg from strong production

@ pp colliders **same sign WW scattering** is the golden channel greatly reduces background from strong production and removes s-channel Higgs process

★ @LHC (Run 2, ATLAS) **first  $3.3 \sigma$**  evidence for at least one **longitudinally** polarised W boson in  $W^\pm W^\pm$  scattering

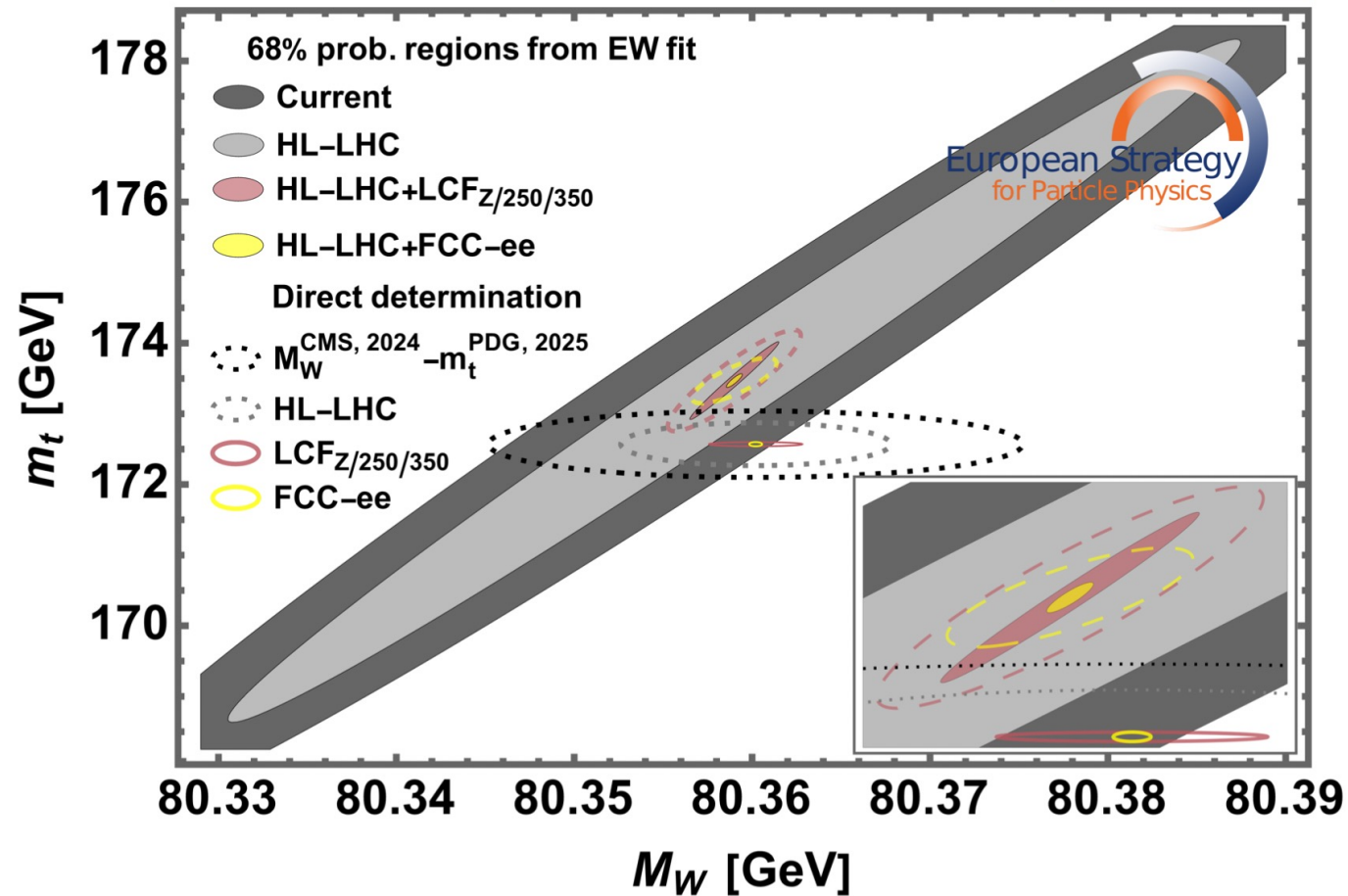
★ @HL-LHC expect to observe with  $> 5\sigma$  and measure  $W_L W_L jj$  [[arXiv:2504.00672](#)]

★  $V_L V_L$  can be probed @

FCC-hh

muon collider (up to 10 TeV)

linear colliders (ILC, CLIC, ... ) (up to 500-3 TeV)



Dashed ellipses indicate “conservative scenario” for theoretical uncertainties (likely realised improvements)

# Conclusion

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Accelerators offer a **unique opportunity : high intensity and energy with known and tunable initial conditions**

Many aspects of cosmology and astroparticle rely on particle physics

The LHC the most versatile science machine ever built:

SM: EW, Higgs, QCD, flavour, BSM searches, quark-gluon plasma

A lot of data in the near future : Runs 3–5 are 95% of the full (HL-) LHC dataset  
→ for the next 25 years the LHC will be THE machine to explore the TeV scale

**In the longer term an accelerator (whatever it is) capable to do the most precise Z, H, WW, top physics is the best option**

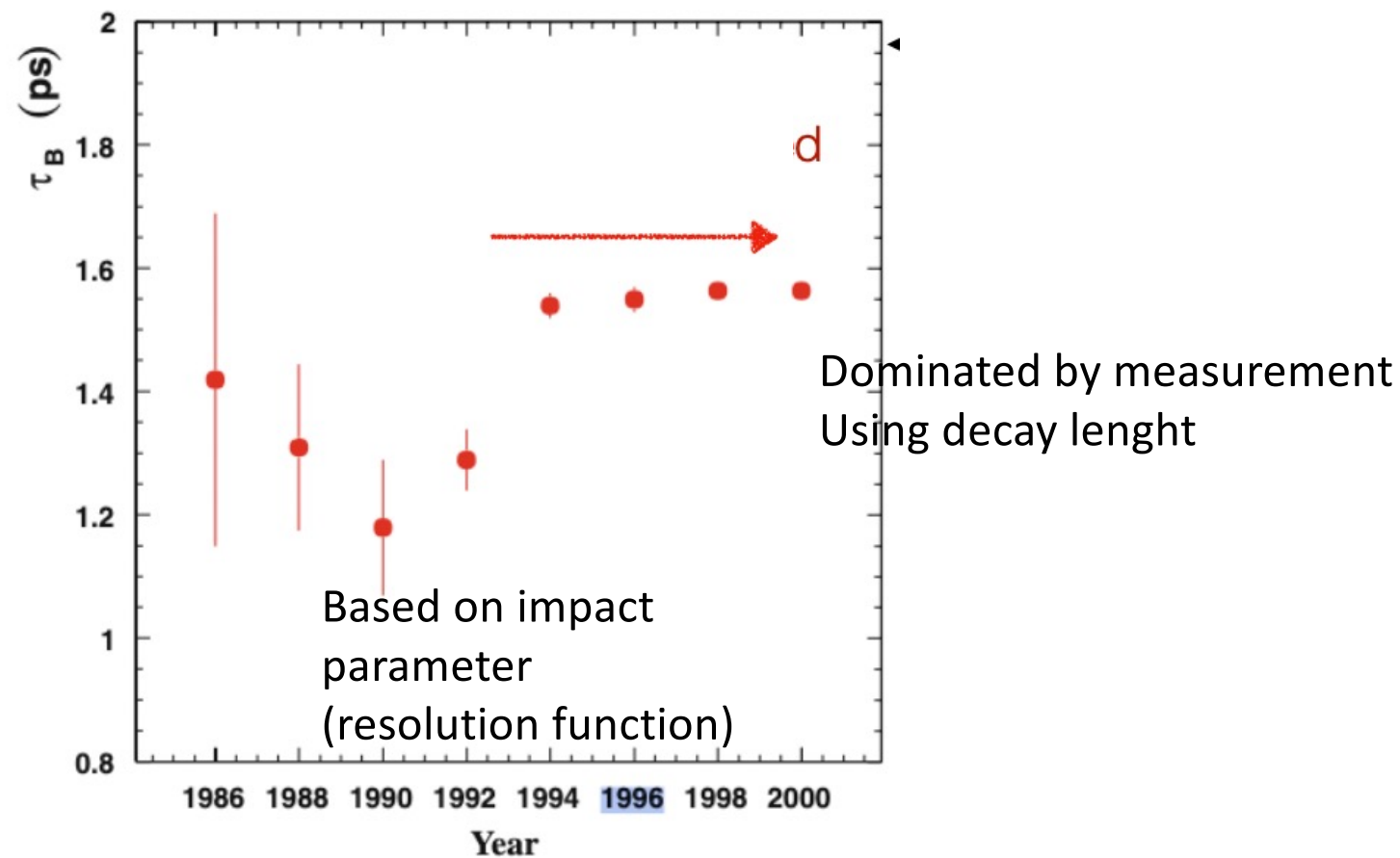
The FCC integrated programme has (overall) an impressive reach for exploring fundamental interactions at energy scales of tens of TeV and beyond.

The (physics) program of the LHC is filled with exciting opportunities for Early Career Scientist



It is very valuable when doing precise measurements to use very different methods

### AVERAGE B HADRON LIFETIME



# Kinematical fit

Final state has known energy and momentum:  $(\sqrt{s}, 0, 0, 0)$

Total energy and momentum are conserved :

$$E_1 + E_2 + E_3 + E_4 - \sqrt{s} = 0$$

$$\mathbf{p}_1^{x,y,z} + \mathbf{p}_2^{x,y,z} + \mathbf{p}_3^{x,y,z} + \mathbf{p}_4^{x,y,z} = 0$$

$e^+e^- \rightarrow W(qq)W(qq)$

$e^+e^- \rightarrow W(l\nu)W(qq)$

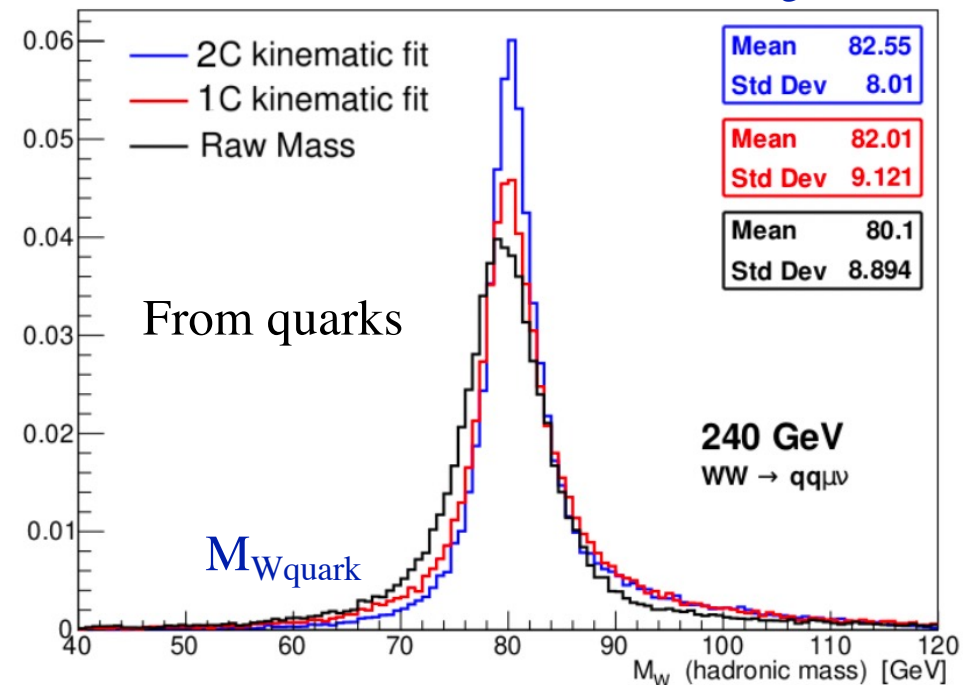
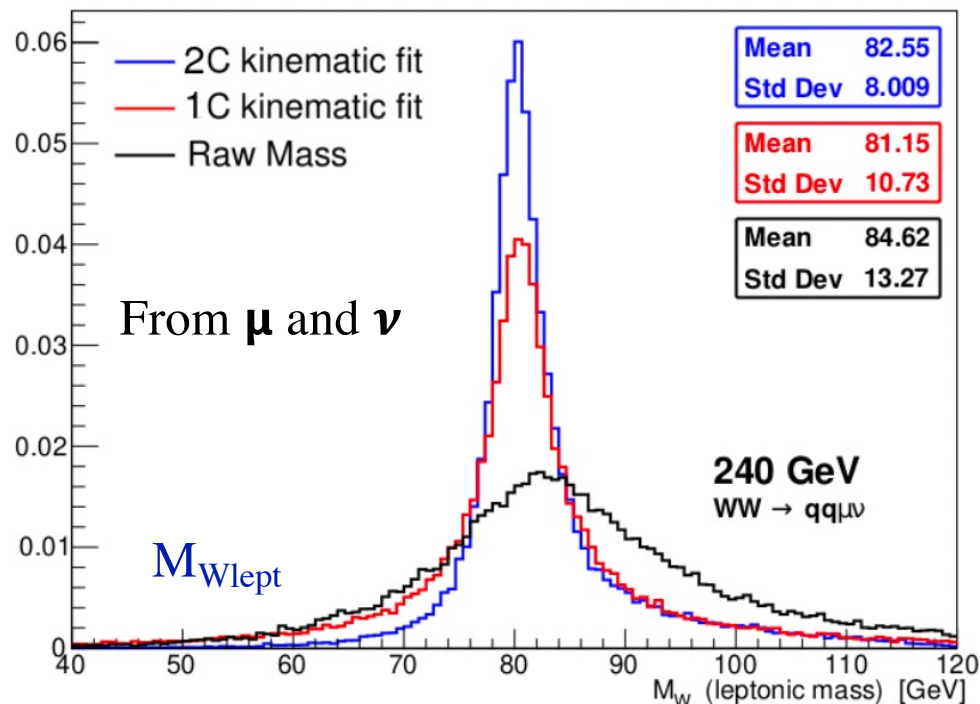
$e^+e^- \rightarrow f_1+f_2+f_3+f_4$

In semileptonic final state **1C** fit (neutrino kinematics unknown)

In fully hadronic final state **4C** fit

Additional constraints from the W masses ( $M_{W\text{lept}} = M_{W\text{quark}}$ )

Thesis Beguin



# Kinematical fit

Final state has known energy and momentum:  $(\sqrt{s}, 0, 0, 0)$

Total energy and momentum are conserved :

$e^+e^- \rightarrow W(qq)W(qq)$

$$E_1 + E_2 + E_3 + E_4 - \sqrt{s} = 0$$

$$p_1^{x,y,z} + p_2^{x,y,z} + p_3^{x,y,z} + p_4^{x,y,z} = 0$$

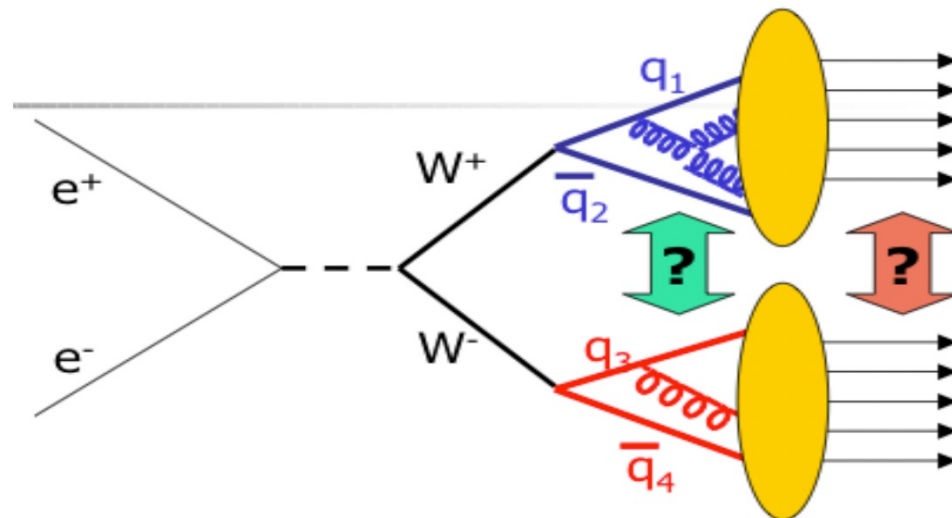
$$\begin{bmatrix} 1 & 1 & 1 & 1 \\ \beta_1^x & \beta_2^x & \beta_3^x & \beta_4^x \\ \beta_1^y & \beta_2^y & \beta_3^y & \beta_4^y \\ \beta_1^z & \beta_2^z & \beta_3^z & \beta_4^z \end{bmatrix} \begin{bmatrix} E_1 \\ E_2 \\ E_3 \\ E_4 \end{bmatrix} = \begin{bmatrix} \sqrt{s} \\ 0 \\ 0 \\ 0 \end{bmatrix}$$

Jet directions ( $\beta_i = p_i/E_i$ ) are very well measured  $\rightarrow$

Jet energies determined analytically by inverting the matrix

Additional constraints from the W masses

# Color reconnection



## EW bosonic operators

$Q_W$	$\varepsilon^{IJK} W_{\mu}^I W_{\nu}^J W_{\rho}^K$
$Q_{\tilde{W}}$	$\varepsilon^{IJK} \tilde{W}_{\mu}^I W_{\nu}^J W_{\rho}^K$
$Q_{\varphi W}$	$\varphi^\dagger \varphi W_{\mu\nu}^I W^{I\mu\nu}$
$Q_{\varphi \tilde{W}}$	$\varphi^\dagger \varphi \tilde{W}_{\mu\nu}^I W^{I\mu\nu}$
$Q_{\varphi B}$	$\varphi^\dagger \varphi B_{\mu\nu} B^{\mu\nu}$
$Q_{\varphi \tilde{B}}$	$\varphi^\dagger \varphi \tilde{B}_{\mu\nu} B^{\mu\nu}$
$Q_{\varphi WB}$	$\varphi^\dagger \tau^I \varphi W_{\mu\nu}^I B^{\mu\nu}$
$Q_{\varphi \tilde{W} B}$	$\varphi^\dagger \tau^I \varphi \tilde{W}_{\mu\nu}^I B^{\mu\nu}$

## From effective lagrangian to SMEFT

$$\delta g_1^Z = \frac{v^2}{\Lambda^2} \frac{1}{c_W^2 - s_W^2} \left( \frac{s_W}{c_W} C_{HWB} + \frac{1}{4} C_{HD} + \delta v \right),$$

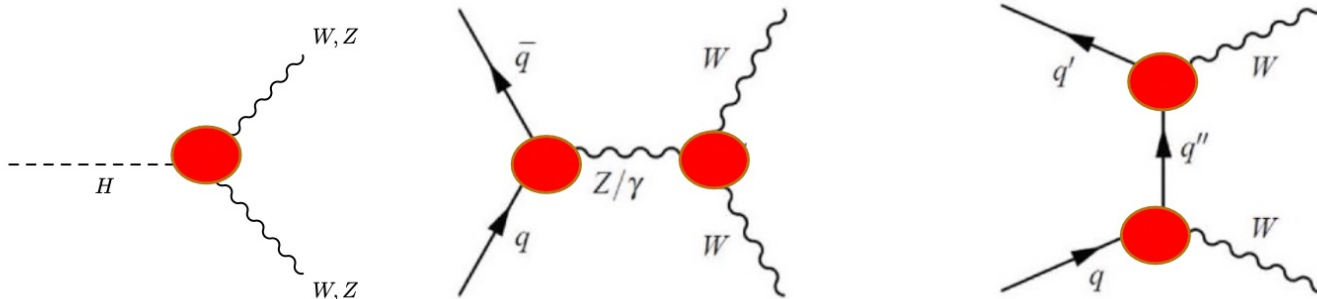
$$\delta \kappa^Z = \frac{v^2}{\Lambda^2} \frac{1}{c_W^2 - s_W^2} \left( 2s_W c_W C_{HWB} + \frac{1}{4} C_{HD} + \delta v \right)$$

$$\delta \kappa^\gamma = -\frac{v^2}{\Lambda^2} \frac{c_W}{s_W} C_{HWB},$$

$$\lambda^\gamma = \frac{v}{\Lambda^2} 3M_W C_{3W},$$

$$\lambda^Z = \frac{v}{\Lambda^2} 3M_W C_{3W},$$

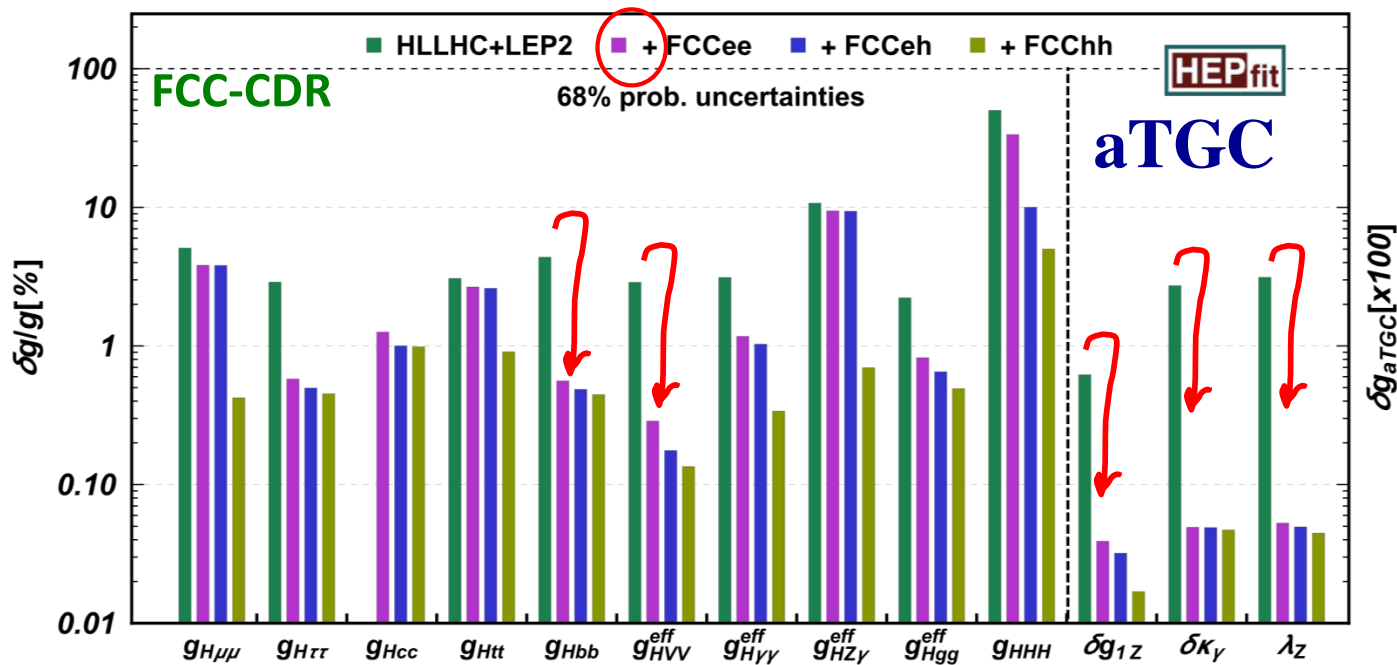
Operators contributing to VVV vertices and Higgs-VV vertices



Changing  $(Z/\gamma)WW$ ,  
vertices spoils high  
energy cancellations  
between contributions  
  
Leads to concept of  
global fits

- **Motivation: test of the SM consistency → improve mass reach in indirect search (equiv. to factor 5-10 in mass)**

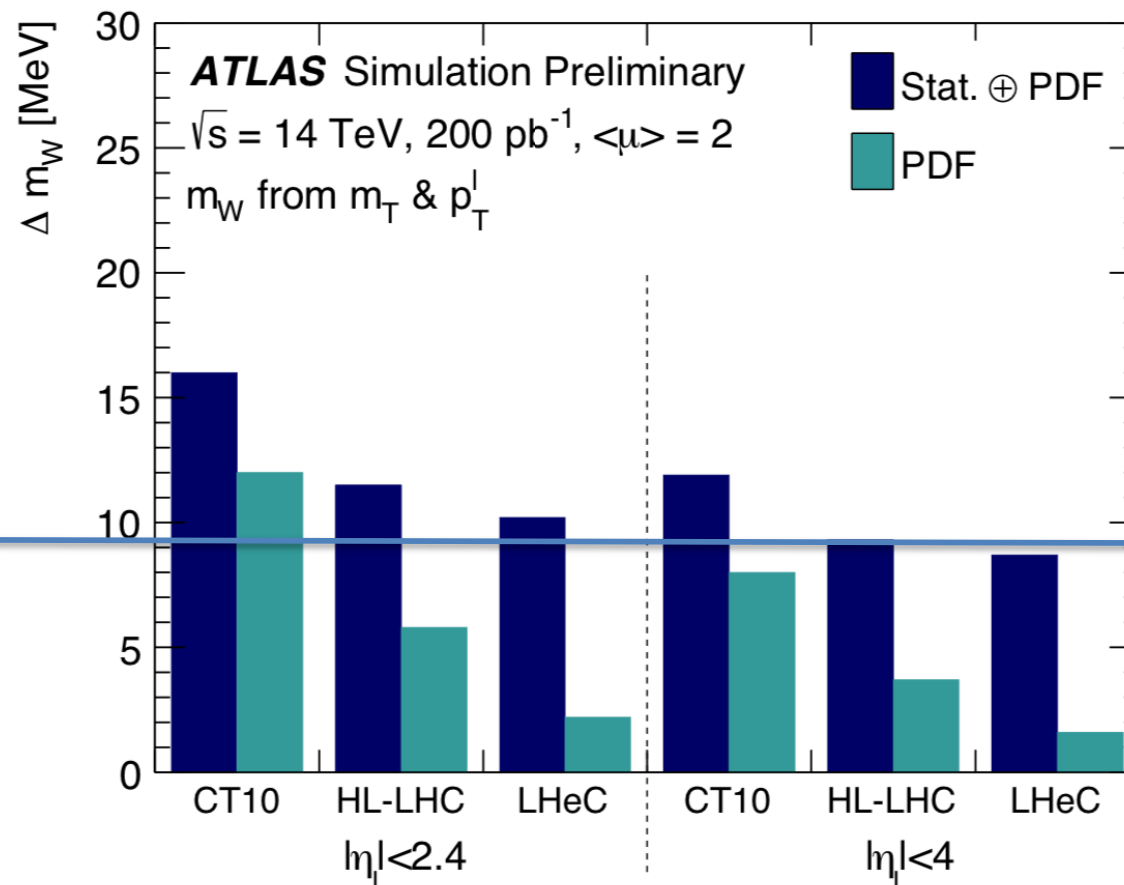
### EFT fits of EW+WW+Higgs observables



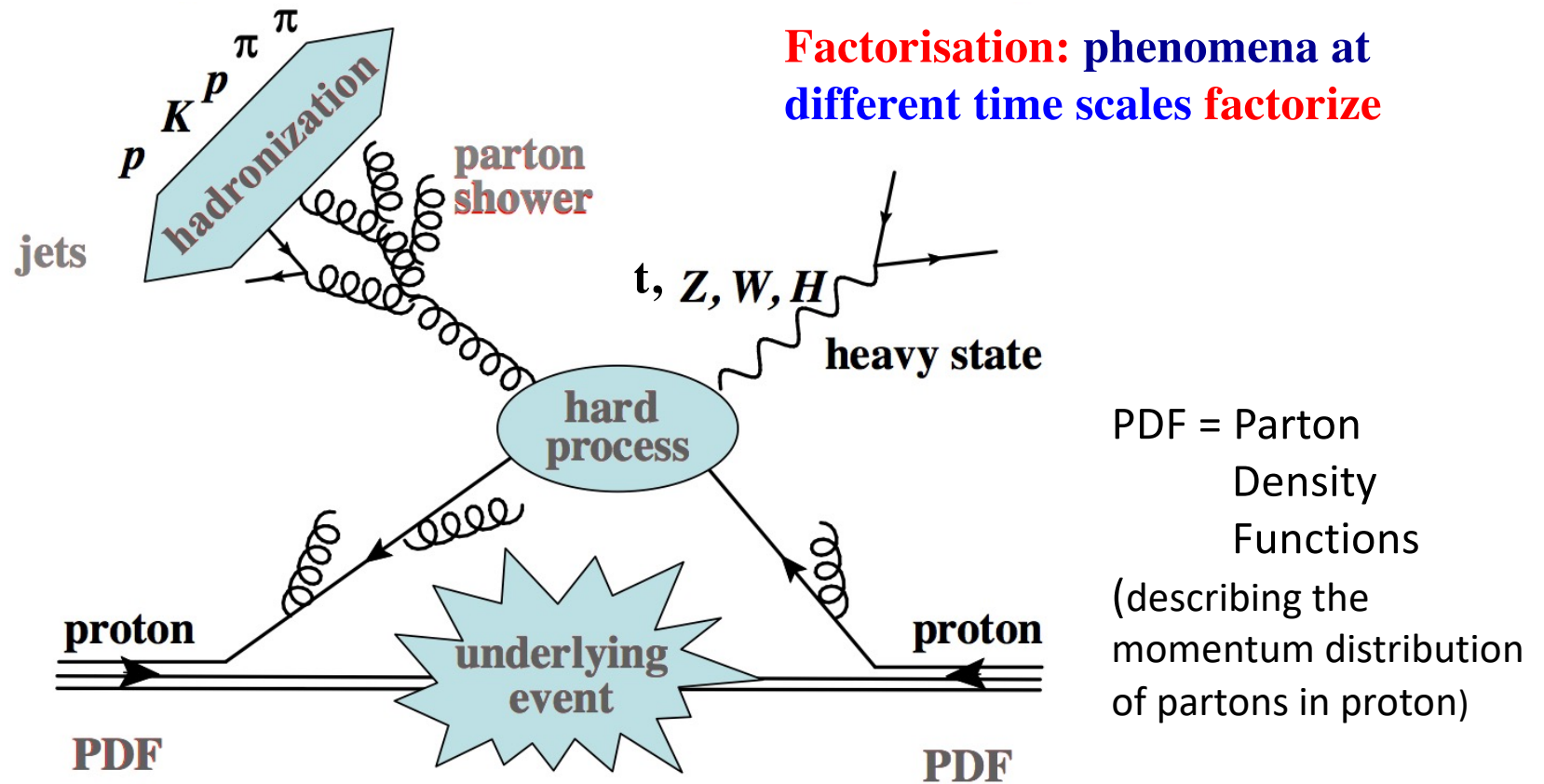
- **A Z-pole program important for the robust extraction of the Higgs couplings**



## Expected sensitivity on $m_W \sim 10$ MeV (with 200 pb<sup>-1</sup> of low- $\mu$ data)



# At Hadron Colliders: a Complex Picture



→ separation between phenomena @ high- and small- $Q$  scale  
The former are computed exactly, the latter are approximated or modeled  
The factorisation scale  $\mu_F$  arbitrarily separates hard from soft scales

**Many aspects of QCD can/must be understood !**

# Variables used in the analysis of $p - p$ collisions

Boost of **parton-parton center of mass** along beam line **unknown**

→ use transverse quantities (**in the plane  $\perp$  to the beam**):

• Transverse momentum/energy :

$$\mathbf{p}_T = p \sin \theta$$

$$E_T = E \sin \theta$$

• **Missing Transverse Energy** :

$$\vec{\mathbf{p}}_T^{\text{mis}} = - \sum_{\text{vis}} \vec{\mathbf{p}}_T \quad E_T^{\text{mis}} = |\vec{\mathbf{p}}_T^{\text{mis}}|$$

• rapidity

$$Y = \frac{1}{2} \ln \frac{E + p_z}{E - p_z}$$

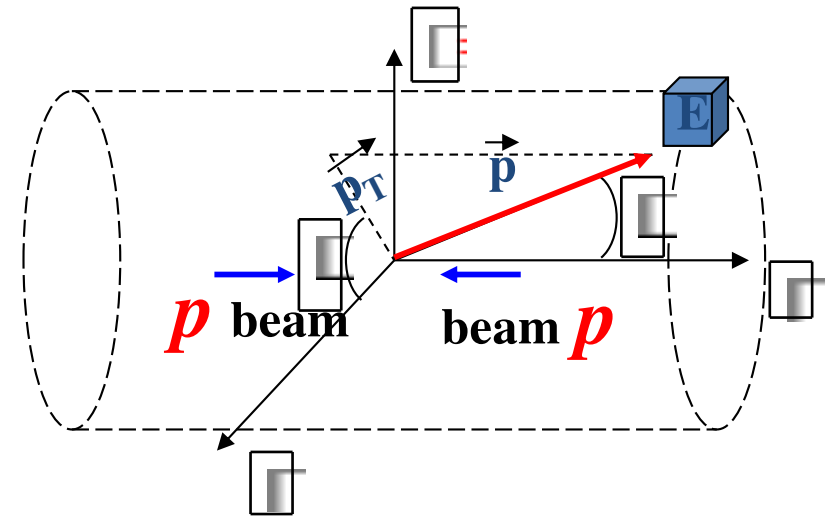
Angles :

• pseudorapidity

$$\eta = - \ln \left( \tan \frac{\theta}{2} \right)$$

• azimuthal angle

$$\Phi$$

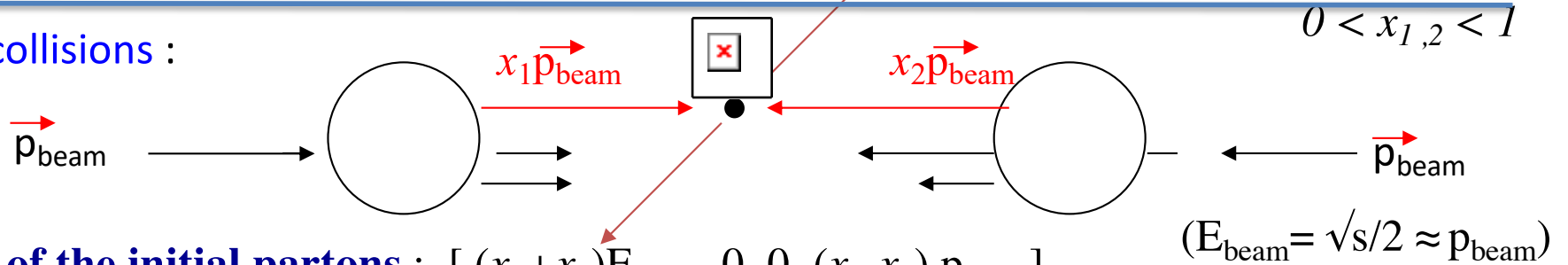


**Important:**

- $\sum^{\text{in}} \vec{\mathbf{p}}_T = \sum_{\text{vis}} \vec{\mathbf{p}}_T \approx 0 \rightarrow$  Allows to evaluate the  $\vec{\mathbf{p}}_T$  of particles not detected ( $\nu$ )
- $p_T$  and  $\Delta Y$  are invariants for Lorentz transformations along the  $z$  axis
- $m \ll E \rightarrow Y \approx \eta$  ( $\eta$  doesn't require particle identification)
- $m \ll E \rightarrow p_T \approx E_T$

# Kinematics of $p - p$ collisions

$p - p$  collisions :



★ **4-mom of the initial partons** :  $[(x_1 + x_2)E_{\text{beam}}, 0, 0, (x_1 - x_2)p_{\text{beam}}]$

★ **Effective collision energy**  $= \sqrt{\hat{s}} = Q = \sqrt{x_1 x_2 s}$

★  $x_{1,2} = \frac{Q}{\sqrt{s}} e^{\pm y_{\text{cm}}}$

$y_{\text{cm}}$  = rapidity of the c.o.m. of the parton system

