# Conformal versus Non-Conformal 2HDM: Phase Transitions and Gravitational Waves

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Conformal versus Non-Conformal 2HDM

## Outline of the talk

- 1. Introduction
- 2. Model
- 3. Results
- 4. Conclusion

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#### 1. Introduction

2. Model

3. Results

#### 4. Conclusion

## Phase transition in the early Universe



#### Bubbles of new phase and collision



## Order of phase transitions



Mazumdar, White, arXiv:1811.01948

- $1^{st}$ -order phase transitions are abrupt (existence of a barrier): the order parameter (VEV  $\phi$ ) changes *discontinuously* from zero to a non-zero value
- $2^{nd}$ -order phase transitions/crossovers are smooth (no barrier): the order parameter (VEV  $\phi$ ) changes *continuously* from zero to a non-zero value

#### Order of phase transitions



Senaha, Symmetry 2020, 12(5), 733

#### First-order phase transitions



Wang, Huang, Zhang, arXiv:2003.08892

#### Gravitational waves



spacetime

detection of gravitational waves

spacetime perturbation

#### Gravitational-wave production

High temperature



Wang, Huang, Zhang, arXiv:2003.08892

#### Gravitational-wave power spectrum



PLI sensitivity curves  $h^2\Omega_{\rm PLI}(f)$  for LISA, DECIGO and BBO, with  $t_{\rm obs} = 4$  yr and  $\rho_{\rm thrs} = 10$ .

• ----:  $\alpha$  increases •  $\cdots$ :  $\beta/H_*$  increases •  $-\cdots$ :  $T_*$  increases, while keeping  $\beta/H_*$  constant •  $-\cdots$ :  $T_*$  increases, considering  $H_* \sim T_*^2$ 

## Supercooled first-order phase transitions



Sagunski, Schicho, Schmitt, arXiv:2303.02450

For supercooled first-order phase transitions

- ullet the Universes remains trapped in the false vacuum until  $T\ll T_c$
- $\Delta V$  increases as T decreases
- for  $T < T_i$ , the Universe becomes vacuum dominated ( $\Delta V = \frac{\pi^2}{30}g_*T_i^4$ ) and enters a period of thermal inflation
- percolation may never happen if thermal inflation is too important
  - $\rightarrow$  the phase transition may never complete

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Conformal versus Non-Conformal 2HDM

# Outline of the talk

1. Introduction

#### 2. Model

3. Results

#### 4. Conclusion

• 2HDM is motivated by MSSM

• nearly conformal dynamics typically lead to large supercooling

• compare the results from phase transitions and gravitational waves between the 2HDM and its conformal version

The tree-level potential of the classically conformal CP-conserving 2HDM is given by

$$\begin{split} V_0 &= \frac{\lambda_1}{2} (\Phi_1^{\dagger} \Phi_1)^2 + \frac{\lambda_2}{2} (\Phi_2^{\dagger} \Phi_2)^2 + \lambda_3 \Phi_1^{\dagger} \Phi_1 \Phi_2^{\dagger} \Phi_2 \\ &+ \lambda_4 \Phi_1^{\dagger} \Phi_2 \Phi_2^{\dagger} \Phi_1 + \frac{\lambda_5}{2} \left[ (\Phi_1^{\dagger} \Phi_2)^2 + (\Phi_2^{\dagger} \Phi_1)^2 \right], \end{split}$$

where  $\Phi_1$  and  $\Phi_2$  denote the two SU(2)<sub>L</sub> Higgs doublets and where we have imposed  $\mathbb{Z}_2$  discrete symmetries to avoid FCNC at tree-level.

The two  $SU(2)_L$  Higgs doublets are given by

$$\Phi_1 = \frac{1}{\sqrt{2}} \begin{pmatrix} \rho_1 + i\eta_1 \\ v_1 + \phi_1 + i\psi_1 \end{pmatrix} \text{ and } \Phi_2 = \frac{1}{\sqrt{2}} \begin{pmatrix} \rho_2 + i\eta_2 \\ v_2 + \phi_2 + i\psi_2 \end{pmatrix},$$

with  $v_1 = v\cos\beta, v_2 = \sin\beta$  and  $v\simeq 246~{\rm GeV}$  the VEV of the SM Higgs doublets

Extremising  $V_0$  along  $\phi_1$  and  $\phi_2$  direction leads to the following conditions:

$$\frac{\lambda_1}{\lambda_2} = \tan^4 \beta, \qquad \sqrt{\lambda_1 \lambda_2} = -\lambda_{345},$$

where  $\lambda_{345} \equiv \lambda_3 + \lambda_4 + \lambda_5$ .

In the vacuum and using the tadpole conditions, the mass matrices, after diagonalisation, are given by

$$M_S^2 = \begin{pmatrix} m_H^2 & 0\\ 0 & 0 \end{pmatrix}, \quad M_P^2 = \begin{pmatrix} m_A^2 & 0\\ 0 & 0 \end{pmatrix}, \quad M_C^2 = \begin{pmatrix} m_{H^{\pm}}^2 & 0\\ 0 & 0 \end{pmatrix},$$

with

$$m_H^2 = -\lambda_{345}v^2 = \sqrt{\lambda_1\lambda_2}v^2, \quad m_A^2 = -\lambda_5v^2, \quad m_{H^{\pm}}^2 = -\frac{1}{2}(\lambda_4 + \lambda_5)v^2.$$

Finding  $m_h^2 = 0$  means the direction h is the flat direction (second derivative is zero)

The C2HDM is naturally aligned at tree-level:  $\alpha = \beta - \pi/2$  such that  $M_S$  is diagonalised.

Flat direction along

$$\phi \equiv h = -\sin\alpha\phi_1 + \cos\alpha\phi_2 = \cos\beta\phi_1 + \sin\beta\phi_2$$

$$\phi_1 = \phi \cos \beta, \quad \phi_2 = \phi \sin \beta,$$
  
$$\langle \phi \rangle = v, \quad \langle \phi_1 \rangle = v \cos \beta = v_1, \quad \langle \phi_2 \rangle = v \sin \beta = v_2$$

Using tadpole conditions and the relation of the mass matrices with the physical masses, we obtain the following parametrisation:

$$\begin{split} \lambda_1 &= \frac{m_H^2}{v^2} \tan^2 \beta, \quad \lambda_2 = \frac{m_H^2}{v^2 \tan^2 \beta}, \quad \lambda_3 = \frac{2m_{H^{\pm}}^2 - m_H^2}{v^2}, \\ \lambda_4 &= \frac{-2m_{H^{\pm}}^2 + m_A^2}{v^2}, \quad \lambda_5 = \frac{-m_A^2}{v^2}, \end{split}$$

for which  $V_0(\phi) = 0$ .

 $\Longrightarrow$  along the flat direction, the scalar potential is generated at one-loop order .

# Coleman-Weinberg potential

In Landau gauge, the Coleman-Weinberg potential  $V_{\rm CW}$  is defined in the  $\overline{\rm MS}$  scheme as

$$V_{\mathsf{CW}}(\phi) = \frac{1}{64\pi^2} \sum_{i} (-1)^F g_i \, m_i^4(\phi) \left[ \ln \frac{m_i^2(\phi)}{\mu^2} - C_i \right],$$

where

- $i \in \{t, W^{\pm}, Z, \gamma, h, H, G_0, A, G^{\pm}, H^{\pm}\}$
- $g_i$ : the number of degrees of freedom
- $m_i^2(\phi)$ :  $i^{\text{th}}$  eigenvalue of the field-dependent mass matrix  $(m^2)_{ab} \equiv \partial^2 V / \partial \phi_a \partial \phi_b$
- $\mu$ : renormalisation scale
- F = 1 for fermions and F = 0 for bosons
- $C_i = 3/2$  for scalars, fermions and  $C_i = 5/6$  for gauge bosons

#### One-loop improved tadpole conditions

Tree-level tadpole conditions:

$$T_{\phi_1} \equiv \left\langle \frac{\partial V_0}{\partial \phi_1} \right\rangle = v_1 \left( \lambda_1 v_1^2 + \frac{1}{2} \lambda_{345} v_2^2 \right) = 0$$
$$T_{\phi_2} \equiv \left\langle \frac{\partial V_0}{\partial \phi_2} \right\rangle = v_2 \left( \lambda_2 v_2^2 + \frac{1}{2} \lambda_{345} v_1^2 \right) = 0$$

 $\Rightarrow$  one-loop improved tadpole conditions:

Lee, Pilaftsis, arXiv:1201.4891

$$\left\langle \frac{\partial (V_0 + V_{\mathsf{CW}})}{\partial \phi_i} \right\rangle = T_{\phi_i} + \frac{v_i v^2}{64\pi^2} \Delta \hat{t}_i = 0, \quad i = 1, 2$$

$$\begin{aligned} \Delta \hat{t}_i &= \frac{1}{v^2} \left[ 4\lambda_{345} m_H^2 \left( 1 - \log \frac{m_H^2}{\mu^2} \right) + 4\lambda_5 m_A^2 \left( 1 - \log \frac{m_A^2}{\mu^2} \right) + 4\lambda_{45} m_{H^\pm}^2 \left( 1 - \log \frac{m_{H^\pm}^2}{\mu^2} \right) \\ &- 6g_2^2 m_W^2 \left( \frac{1}{3} - \log \frac{m_W^2}{\mu^2} \right) - 3(g_1^2 + g_2^2) m_Z^2 \left( \frac{1}{3} - \log \frac{m_Z^2}{\mu^2} \right) + 24y_f^2 m_t^2 \left( 1 - \log \frac{m_t^2}{\mu^2} \right) \delta_{Ii} \end{aligned}$$

#### One-loop improved mass matrices

$$M_{S}^{2} = \begin{pmatrix} \lambda_{1}v_{1}^{2} + \frac{T_{\phi_{1}}}{v_{1}} + \left\langle \frac{\partial^{2}V_{\text{CW}}}{\partial\phi_{1}^{2}} \right\rangle & \lambda_{345}v_{1}v_{2} + \left\langle \frac{\partial^{2}V_{\text{CW}}}{\partial\phi_{1}\partial\phi_{2}} \right\rangle \\ \lambda_{345}v_{1}v_{2} + \left\langle \frac{\partial^{2}V_{\text{CW}}}{\partial\phi_{1}\partial\phi_{2}} \right\rangle & \lambda_{2}v_{2}^{2} + \frac{T_{\phi_{2}}}{v_{2}} + \left\langle \frac{\partial^{2}V_{\text{CW}}}{\partial\phi_{2}^{2}} \right\rangle \end{pmatrix}$$

$$\left\langle \frac{\partial^2 V_{\rm CW}}{\partial \phi_i \partial \phi_j} \right\rangle = \frac{1}{64\pi^2} (v^2 \Delta \hat{t}_i \delta_{ij} + v_i v_j \Delta \hat{m}_{ij}^2),$$

$$\begin{split} \Delta \hat{m}_{ij}^2 &\equiv 8\lambda_{345}^2 \log \frac{|m_H^2|}{\mu^2} + 8\lambda_5^2 \log \frac{m_A^2}{\mu^2} + 4\lambda_{45}^2 \log \frac{m_{H^\pm}^2}{\mu^2} + g_2^4 \left(2 + 3\log \frac{m_W^2}{\mu^2}\right) \\ &+ \frac{g_1^4 + g_2^4}{2} \left(2 + 3\log \frac{m_Z^2}{\mu^2}\right) - 24y_f^4 \log \frac{m_t^2}{\mu^2} \delta_{ij} \delta_{Ii} \end{split}$$

$$M_{S}^{2} = \begin{pmatrix} \lambda_{1}v_{1}^{2} + \frac{T_{\phi_{1}}}{v_{1}} + \frac{1}{64\pi^{2}}(v^{2}\Delta\hat{t}_{1} + v_{1}^{2}\Delta\hat{m}_{11}^{2}) & \lambda_{345}v_{1}v_{2} + \frac{1}{64\pi^{2}}v_{1}v_{2}\Delta\hat{m}_{12}^{2} \\ \lambda_{345}v_{1}v_{2} + \frac{1}{64\pi^{2}}v_{1}v_{2}\Delta\hat{m}_{12}^{2} & \lambda_{2}v_{2}^{2} + \frac{T_{\phi_{2}}}{v_{2}} + \frac{1}{64\pi^{2}}(v^{2}\Delta\hat{t}_{2} + v_{2}^{2}\Delta\hat{m}_{22}^{2}) \end{pmatrix}$$

- one-loop improved tadpole conditions:  $\frac{T_{\phi_i}}{v_i} + \frac{1}{64\pi^2}v^2\Delta \hat{t}_i = 0$
- $\Delta \hat{m}_{ij}^2 = 0$  for  $M_P^2$  and  $M_C^2 \Longrightarrow (M_{P,C}^2)_{\text{one-loop}} = (M_{P,C}^2)_{\text{tree-level}}$
- $M_S^2$  has now a second non-zero eigenvalue  $m_h^2 \neq 0$  as a consequence of the breaking of scale invariance at loop order

#### Coleman-Weinberg potential

Along the flat direction we have  $m_i^4(\phi) = m_i^4(v)\phi^4/v^4$ . We can then rewrite  $V_{\rm CW}$  as

$$V_{\mathsf{CW}}(\phi) = \phi^4 \left( A + B \ln \frac{\phi^2}{\mu^2} \right),$$

$$A = \frac{1}{64\pi^2 v^4} \sum_i (-1)^F g_i \, m_i^4(v) \left[ \ln \frac{m_i^2(v)}{\mu^2} - C_i \right],$$
$$B = \frac{1}{64\pi^2 v^4} \sum_i (-1)^F g_i \, m_i^4(v).$$

By minimising  $V_{\rm CW},$  we find that  $\mu=\Lambda_{\rm GW}$  is defined as

$$\ln \frac{\Lambda_{\mathsf{GW}}}{v} = \frac{A}{2B} + \frac{1}{4}.$$

At this scale  $\Lambda_{\text{GW}}$ , the minimum of  $V_{\text{CW}}$  is at  $\phi = v$ .

#### Bounds on heavy scalar masses



- sum rule:  $m_{H}^{4} = 8\pi^{2}v^{2}m_{h}^{2} + 12m_{t}^{4} 6m_{W^{\pm}}^{4} 3m_{Z}^{4} m_{A}^{4} 2m_{H^{\pm}}^{4}$
- we need  $m_{H}^4>0$  in order to have  $m_{H}^2\in\mathbb{R}\to$  upper bounds for  $m_{H},m_{A}$  and  $m_{H^{\pm}}$
- with the constraint  $m_H > m_h \simeq 125$  GeV (otherwise perturbation theory breaks down), the sum rule is a reliable method to compute  $m_H$  Eichten, Lane, arXiv:2209.06632

We study the phase transitions in the early Universe: large temperature  $\Rightarrow$  finite-temperature quantum field theory must be used to take thermal effects into account.

The resulting one-loop thermal effective potential in the C2HDM reads

$$V_{\rm eff} = V_{\rm 0} + V_{\rm CW} + V_{\rm 1L}^T$$

- V<sub>0</sub>: tree-level potential
- V<sub>CW</sub>: Coleman-Weinberg potential
- $V_{1L}^T$ : one-loop thermal corrections

# One-loop thermal effective potential

$$V_{\text{eff}} = V_0 + V_{\text{CW}} + V_{1\text{L}}^T.$$

The last term,  $V_{1L}^T$ , is defined as

$$V_{1\mathsf{L}}^{T}(\phi,T) = \frac{T^4}{2\pi^2} \sum_{i} g_i J_{\mathsf{B}/\mathsf{F}}\left(\frac{m_i^2(\phi)}{T^2}\right) - \frac{\pi^2}{90}g'_*T^4$$

$$J_{\mathsf{B/F}}(y^2) = (-1)^F \int_0^\infty x^2 \log\left[1 \mp e^{-\sqrt{x^2 + y^2}}\right]$$

- T: temperature
- $g_i$ : degrees of freedom of the  $i^{th}$  particle
- $m_i^2(\phi)$ :  $i^{\text{th}}$  eigenvalue of the field-dependent mass matrix  $(m^2)_{ab} \equiv \partial^2 V / \partial \phi_a \partial \phi_b$
- $g'_*$ : relativistic degrees of freedom of the remaining (light) particles

In the high-temperature limit ( $|y^2| = |m_i^2/T^2| \ll 1$ ), we can expand the thermal function J as following:

Curtin, Meade, Ramani, arXiv:1612.00466

$$J_B(y^2) \approx -\frac{\pi^4}{45} + \frac{\pi^2}{12}y^2 - \frac{\pi}{6}y^3 - \frac{1}{32}y^4 \log\left(\frac{y^2}{a_b}\right)$$
$$J_F(y^2) \approx -\frac{7\pi^4}{360} + \frac{\pi^2}{24}y^2 + \frac{1}{32}y^4 \log\left(\frac{y^2}{a_f}\right)$$

• 
$$a_b = \pi^2 \exp(3/2 - 2\gamma_E)$$
  
•  $a_f = 16\pi^2 \exp(3/2 - 2\gamma_E)$ 

with  $\gamma_E \simeq 0.577$ , the Euler–Mascheroni constant.

#### High-temperature expansion



#### Conformal versus Non-Conformal 2HDM

# Imaginary contributions

The cubic term in

$$J_B(y^2) \approx -\frac{\pi^4}{45} + \frac{\pi^2}{12}y^2 - \frac{\pi}{6}y^3 - \frac{1}{32}y^4 \log\left(\frac{y^2}{a_b}\right)$$

can be imaginary for  $m_i^2 < 0$ . Indeed,

$$y^{3} = (y^{2})^{3/2} = \left(\frac{m_{i}^{2}}{T^{2}}\right)^{3/2}$$
$$\Rightarrow \operatorname{Im} y^{3} \neq 0 \text{ for } m_{i}^{2} < 0$$

Likewise for the 
$$\ln m_i^2$$
 term in  $V_{\sf CW}$ .

 $\Rightarrow$  Thus we always consider the real part of  $V_{\text{eff}}$  in our calculations.

Finally, we use the thermally improved finite-temperature potential, which is obtained by adding to the field-dependent masses in  $V_{CW}$  and  $V_{1L}^T$  the leading thermal corrections:

$$m_i^2(\phi) \to m_i^2(\phi) + c_i T^2,$$

where the coefficients  $c_i$  are given by

$$c_h = \frac{1}{16}(g_1^2 + 3g_2^2) + \frac{3\lambda_1 + 2\lambda_3 + \lambda_4}{12},$$
  
$$c_H = \frac{1}{16}(g_1^2 + 3g_2^2) + \frac{1}{4}y_t^2 + \frac{3\lambda_2 + 2\lambda_3 + \lambda_4}{12}$$

for the scalars.

NC2HDM tree-level potential:

$$\begin{aligned} V_0 &= m_{11}^2 \Phi_1^{\dagger} \Phi_1 + m_{22}^2 \Phi_2^{\dagger} \Phi_2 - m_{12}^2 \left[ \Phi_1^{\dagger} \Phi_2 + \Phi_2^{\dagger} \Phi_1 \right] \\ &+ \frac{\lambda_1}{2} (\Phi_1^{\dagger} \Phi_1)^2 + \frac{\lambda_2}{2} (\Phi_2^{\dagger} \Phi_2)^2 + \lambda_3 \Phi_1^{\dagger} \Phi_1 \Phi_2^{\dagger} \Phi_2 \\ &+ \lambda_4 \Phi_1^{\dagger} \Phi_2 \Phi_2^{\dagger} \Phi_1 + \frac{\lambda_5}{2} \left[ (\Phi_1^{\dagger} \Phi_2)^2 + (\Phi_2^{\dagger} \Phi_1)^2 \right]. \end{aligned}$$

#### Parametrisation

In the alignment limit we have

$$\begin{split} m_{11}^2 &= -\frac{m_h^2}{2} + m_{12}^2 \tan\beta, \\ m_{22}^2 &= -\frac{m_h^2}{2} + \frac{m_{12}^2}{\tan\beta}, \\ \lambda_1 v^2 &= m_h^2 + m_H^2 \tan^2\beta - M^2 \tan^2\beta, \\ \lambda_2 v^2 &= m_h^2 + \frac{m_H^2}{\tan^2\beta} - \frac{M^2}{\tan^2\beta}, \\ \lambda_3 v^2 &= m_h^2 - m_H^2 + 2m_{H^\pm}^2 - M^2, \\ \lambda_4 v^2 &= M^2 + m_A^2 - 2m_{H^\pm}^2, \\ \lambda_5 v^2 &= M^2 - m_A^2, \end{split}$$

with

$$M^2 \equiv \frac{m_{12}^2}{\sin\beta\cos\beta}.$$

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#### Conformal versus Non-Conformal 2HDM

The one-loop thermal effective potential in the NC2HDM reads

$$V_{\rm eff} = V_0 + V_{\rm CW} + V_{\rm CT} + V_{\rm 1L}^T$$

- V<sub>0</sub>: tree-level potential
- V<sub>CW</sub>: Coleman-Weinberg potential
- V<sub>CT</sub>: counterterms
- $V_{1L}^T$ : one-loop thermal corrections
## One-loop thermal effective potential

For the treatment of the phase transitions, we suppose that excursions in the field space occur only along the direction  $\phi$  ( $\phi_1 = \phi \cos \beta$ ,  $\phi_2 = \phi \sin \beta$ ).  $\Rightarrow$  the tree-level potential

$$\begin{split} V_0 &= m_{11}^2 \Phi_1^{\dagger} \Phi_1 + m_{22}^2 \Phi_2^{\dagger} \Phi_2 - m_{12}^2 \left[ \Phi_1^{\dagger} \Phi_2 + \Phi_2^{\dagger} \Phi_1 \right] \\ &+ \frac{\lambda_1}{2} (\Phi_1^{\dagger} \Phi_1)^2 + \frac{\lambda_2}{2} (\Phi_2^{\dagger} \Phi_2)^2 + \lambda_3 \Phi_1^{\dagger} \Phi_1 \Phi_2^{\dagger} \Phi_2 \\ &+ \lambda_4 \Phi_1^{\dagger} \Phi_2 \Phi_2^{\dagger} \Phi_1 + \frac{\lambda_5}{2} \left[ (\Phi_1^{\dagger} \Phi_2)^2 + (\Phi_2^{\dagger} \Phi_1)^2 \right], \end{split}$$

becomes

$$V_{0}(\phi) = \frac{1}{2}m_{11}^{2}\phi^{2}\cos^{2}\beta + \frac{1}{2}m_{22}^{2}\phi^{2}\sin^{2}\beta - m_{12}^{2}\phi^{2}\cos\beta\sin\beta + \frac{1}{8}\lambda_{1}\phi^{4}\cos^{4}\beta + \frac{1}{8}\lambda_{2}\phi^{4}\sin^{4}\beta + \frac{1}{4}\lambda_{345}\phi^{4}\cos^{2}\beta\sin^{2}\beta.$$

### One-loop thermal effective potential

$$V_{\rm eff} = V_{\rm 0} + V_{\rm CW} + V_{\rm CT} + V_{\rm 1L}^T$$

The third term,  $V_{CT}$ , contains the finite parts of the counterterms that are fixed such that the scalar VEVs and masses remain at their tree-level values at the T = 0 global minimum  $(v_1, v_2)$ :

$$V_{\mathsf{CT}}(\phi_1,\phi_2) = \delta m_{11}^2 \phi_1^2 + \delta m_{22}^2 \phi_2^2 + \delta \lambda_1 \phi_1^4 + \delta \lambda_2 \phi_2^4 + \delta \lambda_{345} \phi_1^2 \phi_2^2$$

such that the following renormalisation conditions are satisfied:

$$\begin{split} & \left. \frac{\partial V_{\text{CT}}}{\partial \phi_i} \right|_{\text{vev}} = -\frac{\partial V_{\text{CW}}}{\partial \phi_i} \right|_{\text{vev}}, \quad i = 1, 2, \\ & \left. \frac{\partial^2 V_{\text{CT}}}{\partial \phi_i^2} \right|_{\text{vev}} = \left( -\frac{\partial^2 V_{\text{CW}}|_{G \equiv 0}}{\partial \phi_i^2} + \frac{1}{32\pi^2} \sum_{G = G^0, G^{\pm}} \left( \frac{\partial m_G^2}{\partial \phi_i} \right)^2 \ln\left( \frac{m_{\text{IR}}^2}{\mu^2} \right) \right) \right|_{\text{vev}}, \quad i = 1, 2, \\ & \left. \frac{\partial^2 V_{\text{CT}}}{\partial \phi_1 \partial \phi_2} \right|_{\text{vev}} = \left( -\frac{\partial^2 V_{\text{CW}}|_{G \equiv 0}}{\partial \phi_1 \partial \phi_2} + \frac{1}{32\pi^2} \sum_{G = G^0, G^{\pm}} \frac{\partial m_G^2}{\partial \phi_1} \frac{\partial m_G^2}{\partial \phi_2} \ln\left( \frac{m_{\text{IR}}^2}{\mu^2} \right) \right) \right|_{\text{vev}}. \end{split}$$

Constraints on  $\lambda$ 's from

- perturbativity
- perturbative unitarity
- bounded-from-below potential

## Experimental constraints

### Constraints on heavy scalar masses from

Arcadi, N.B., Djouadi, Kannike, arXiv:2212.14788

- LEP2 search:  $m_A \gtrsim 90$  GeV  $(e^+e^- \rightarrow hA)$  and  $m_{H^{\pm}} \gtrsim 80$  GeV  $(e^+e^- \rightarrow H^+H^-)$
- constraint from FCNC via the loop-induced decay process  $B \to X_s \gamma$   $(b \to s \gamma)$ :
  - type II:  $m_{H^{\pm}} \gtrsim 800$  GeV for any  $\tan \beta$
  - type I:  $m_{H^{\pm}} \gtrsim 500$  GeV for  $\tan \beta \gtrsim 1$
- EW precision measurements: mass splitting between  $m_H, m_A$  and  $m_{H^\pm}$  cannot be too large

To analyse the phase transition dynamics in the C2HDM, we scan the parameter space over the following range:

 $m_A \in [90, 1000] \ {\rm GeV}, \quad m_{H^\pm} \in [80, 1000] \ {\rm GeV}, \quad \tan\beta \in [0.1, 50].$ 

In the NC2HDM, in addition, we scan over

 $m_H \in [m_h, 1000] \text{ GeV}, \quad |m_{12}| \in [100, 1000] \text{ GeV}.$ 

We then analyse the points which pass the aforementioned theoretical and experimental constraints.

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3. Results

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# PT parameters: definition

• inverse time duration  $\beta$  of PT normalised to the Hubble parameter:

$$\frac{\beta}{H_*} = (8\pi)^{1/3} \frac{v_w}{R_* H_*}$$

with  $R_*$  the mean bubble separation

• PT strength  $\alpha$ :

$$\alpha = \frac{1}{\frac{\pi^2}{30}g_*T_p^4} \left( \Delta V - \frac{T_p}{4} \Delta \frac{\partial V}{\partial T} \right) \bigg|_{T_p}$$

• probability P(T) of being in the false vacuum :

$$P(T) = e^{-I(T)},$$

with I(T), the fraction of the Universe that has transitioned • percolation temperature  $T_p$ :

$$I(T_p) = 0.34$$

### Parameter space



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## PT parameters: results



### PT parameters: results



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$M_h \; [{\rm GeV}]$	$T_c \; [\text{GeV}]$	$T_p [{ m GeV}]$	α
35	[43.38 - 59.92]	[5.55 - 28.46]	[0.246 - 134.941]
65	[61.39 - 71.52]	[32.48 - 54.58]	[0.054 - 0.401]
95	[78.99 - 90.22]	[57.11 - 79.38]	[0.021 - 0.083]
125	[96.12 - 108.52]	[78.36 - 102.10]	[0.011 - 0.037]
155	[113.00 - 124.35]	[97.69 - 120.05]	[0.007 - 0.021]
185	[129.62 - 138.40]	[116.16 - 135.53]	[0.005 - 0.014]
215	[145.40 - 150.99]	[133.66 - 148.31]	[0.004 - 0.010]

## Scalon mass impact on PT strength



### Gravitational-wave power spectrum



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# Conclusion

- nearly-conformal dynamics typically lead to significant supercooling because the thermal barrier remains until  $T\to 0$
- in the C2HDM however the amount of supercooling is very limited
- NC2HDM offers a larger variability in the amount of supercooling: it can be smaller but also bigger than in the C2HDM case
- a smaller value for the scalon mass (a softer breaking of the scale invariance) leads to stronger FOPT
- C2HDM could not provide a strong enough GW signal to be detected by e.g. LISA, contrary to NC2HDM

