

Silicon detectors

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APC & UPC







Outline

- Main applications, motivations and history
- Semiconductors physics

Silicon radiation detectors

Timing with silicon detectors

Perspectives

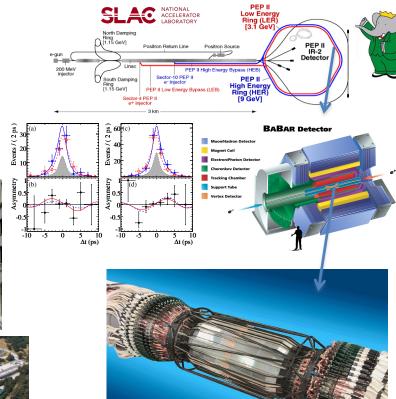
Yes, but who are you?





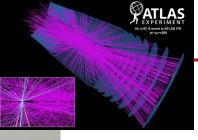




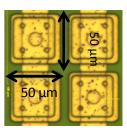


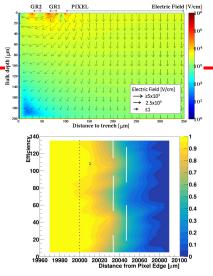
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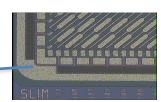


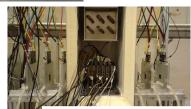








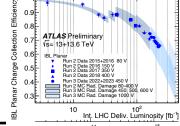




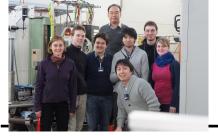








10¹⁴ 10¹⁵ Average Fluence [1 MeV n-eq cm⁻²]



Acknowlegments

Thanks to: I. Abt, V. Bonvicini, G. Calderini, S. Holland, M. Krammer, M. Moll, P. Wells, W. Riegler and more

- You can find great lectures here:
 http://www.hephy.at/fileadmin/user_upload/Lehre/Unterlagen/Praktikum/Halbleiterdetektoren.pdf
- And here: http://www.users.ts.infn.it/~bonvicin/Dottorandi08.pdf

References

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- •G. Lutz, Semiconductor Radiation Detectors: Device Physics, Springer (July 11, 2007)
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- •F. Hartmann, Silicon tracking detectors in high-energy physics, Nucl. Instr. and Meth. A666 (2012) 25-46
- •D. Renker and E. Lorenz, Advances in solid state photon detectors, 2009 JINST 4 P04004

• PDG

Outline

Main applications, motivations and history

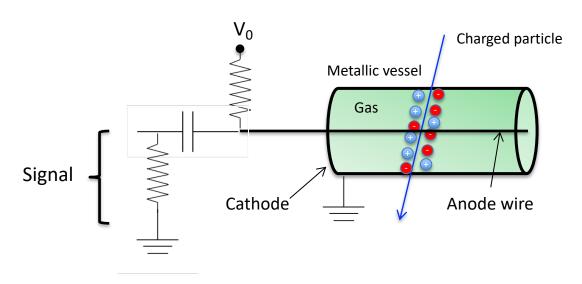
Semiconductors physics

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Before solid state detectors: gas detectors

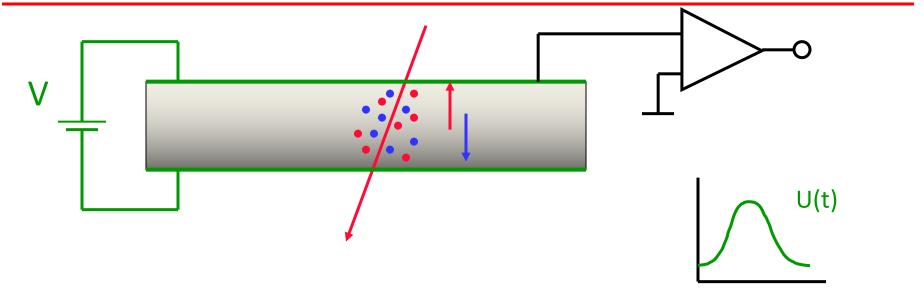


A voltage difference is applied between a central wire ("anode") and the metallic vessel containing the gas ("cathode", at ground).

Signal is readout from the anode

This basic model is a good representation for the three original gas detectors, i.e. the ionisation chamber, the proportional counter and the Geiger-Müller counter

The basics of a silicon detector



A solid state ionization chamber
Signal given by the drift of charges (electrons and holes) under the effect of the electric field

The signal is then amplified and shaped

Main applications

• γ spectroscopy with high energy resolution (10 keV – few MeV range)

Vertex and tracking detectors with high spatial resolution

Energy measurements of charged particles (few MeV) and Particle ID via dE/dx (multiple layers)

Why?

✓ Only few eV per electron-hole pair

✓ Use microchip technology; structures with sub µm precision can be produced at low cost; read-out electronics can be directly bonded to detector

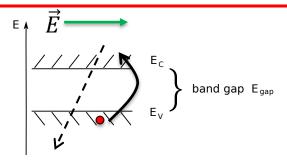
√ high density compared to gases - need only thin layers

✓ Solid material, no need for vessel/cryostat

Principle of operation

In semiconductors at T > 0 K few electrons populate the conduction band, and few holes are present in the valence band

Radiation can provide energy to an electron in valence band to be promoted to conduction band. At the same time a hole is created in valence band



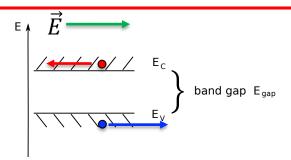
Principle of operation

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Radiation can provide energy to an electron in valence band to be promoted to conduction band. At the same time a hole is created in valence band

The detector is polarised, so the charge carriers move under the effect of the electric field

A current appears in my detector circuit



Outline

Main applications, motivations and history

Semiconductors physics

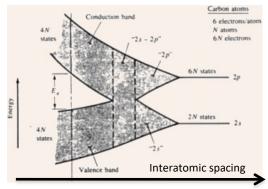
Silicon radiation detectors

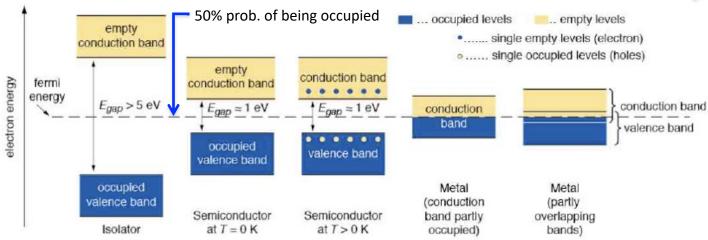
Timing with silicon detectors

Perspectives

What is a semiconductor?

- In an isolated atom the electrons have only discrete energy levels. In solid state material the atomic levels merge to energy bands.
- In metals the conduction and the valence band overlap,
- whereas in isolators and semiconductors these levels are separated by an energy gap (band gap).
- In semiconductors this gap is large (compared to kT ~ 1/40 eV)





A few semiconductors used in research

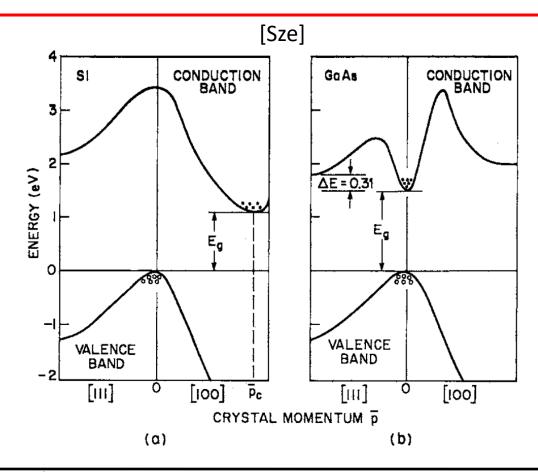
Germanium: Used in nuclear physics, due to small band gap (0.66 eV) needs cooling (usually done with liquid nitrogen at 77 K)

Silicon: Standard material for vertex and tracking detectors in high energy physics, can be operated at room temperature, synergies with micro electronics industry.

Diamond (CVD or single crystal): Large band gap (6 eV), requires no depletion zone, very radiation hard, drawback is a low signal and high cost

Compound semiconductors: GaAs (faster than Si, no good insulating layer), CdTe (large Z, hence efficient for photodection);

Indirect vs direct semiconductors



In Si (and Ge) a photon is not enough to create electron-hole pairs since it carries ~ 0 crystal momentum

Phonons are necessary

Important aspect for photon detection (and even more for photon emission)

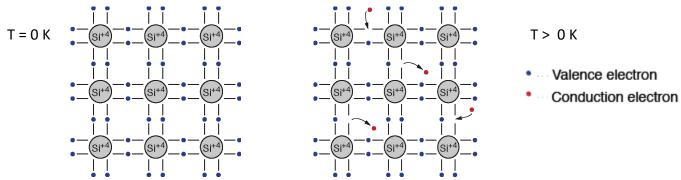
Some properties of Semiconductors

Table 8.2 Properties of silicon, germanium, gallium arsenide, cadmium telluride and diamond. D = diamond lattice, ZB = zinc blende lattice, temperature dependent quantities given at $300\,\mathrm{K}$.

	Property	Si	Ge	GaAs	CdTe	Diamond
	atomic number (Z)	14	32	31/33	48/52	6
	atom mass (u)	28.09	72.60	72.32	120.0	12.01
\rightarrow	density ρ (g/cm ³)	2.328	5.327	5.32	5.85	3.51
	crystal structure	D	D	ZB	ZB	D
	lattice constant (Å)	5.431	5.646	5.653	6.48	3.57
\longrightarrow	semiconductor type	indirect	indirect	direct	direct	indirect
\longrightarrow	band gap $E_G(eV)$	1.12	0.66	1.424	1.44	5.5
	intr. carrier density (cm^{-3})	1.01×10^{10}	2.4×10^{13}	2.1×10^{6}	10^{7}	≈ 0
	resistivity (Ωcm)	$2.3{ imes}10^{5}$	47	10^{8}	10^{9}	$\approx 10^{16}$
\longrightarrow	dielectric constant (ϵ)	11.9	16	13.1	10.2	5.7
\longrightarrow	radiation length X_0 (cm)	9.36	2.30	2.29	1.52	12.15
→	average energy for					
	(e/h) creation (eV)	3.65	2.96	4.2	4.43	13.1
	thermal conductivity $\left(\frac{W}{cmK}\right)$	1.48	0.6	0.55	0.06	>18
	mobility $\left(\frac{\text{cm}^2}{\text{Vs}}\right)$					
	electrons μ_n	1450	3900	8500	1050	≈ 1800
	holes μ_h	500	1800	400	90	≈ 2300
	lifetime					
	electrons τ_e	$>$ 100 μs	\sim ms	$110\mathrm{ns}$	$0.12\mu s$	$\approx 100 \mathrm{ns}$
	holes τ_h	$>$ 100 μs	\sim ms	$20\mathrm{ns}$	$0.11\mu s$	$\approx 50\mathrm{ns}$

Bond model of semiconductors

Example of column IV elemental semiconductor (2dim projection)



Each atom has 4 closest neighbors, the 4 electrons in the outer shell are shared and form covalent bonds. At low temperature all electrons are bound

At higher temperature thermal vibrations break some of the bonds → free e- (n) cause conductivity (electron conduction)

The remaining open bonds attract other e- \rightarrow The "holes" (p) change position (hole conduction) Intrinsic carrier concentration n_i : $n = p = n_i \sim 1.0 \times 10^{10}$ cm⁻³ (T=300K)

Transport of charge carriers

Transport of charge carriers in a semiconductor: diffusion and drift

Diffusion: proportional to the gradient of the carrier density Drift: proportional to the applied electric field

$$\vec{J}_n = \vec{J}_{n,drift} + \vec{J}_{n,diff} = q \left(\mu_n n \vec{E} + D_n \nabla n \right)$$
 D: diffusion coefficient [cm²/s] μ : mobility [cm²/(Vs)]
$$\vec{J}_p = \vec{J}_{p,drift} + \vec{J}_{p,diff} = q \left(\mu_p p \vec{E} - D_p \nabla p \right)$$

D: diffusion coefficient

Einstein's equation
$$D_n = \frac{kT}{q} \mu_n$$

$$D_p = \frac{kT}{q} \mu_p$$

$$\stackrel{
ightarrow}{v_{drift}} = \stackrel{
ightarrow}{\mu} \stackrel{
ightarrow}{E}$$

Valid at low/moderate fields; for large fields (>~ 5x10³ V/cm) the carriers velocities saturates (Si: $v \sim 10^7$ cm/s) \rightarrow 10-30 ns collection time in 100-300 μ m

μ depends on doping and temperature. For intrinsic silicon: $\mu_n \sim 1350 \text{ cm}^2/(\text{Vs})$, $\mu_p \sim 450 \text{ cm}^2/(\text{Vs})$

Estimate SNR in an intrinsic silicon detector

Let's make a simple calculation for silicon:

Mean ionization energy $I_0 = 3.62$ eV, mean energy loss per flight path dE/dx = 3.87 MeV/cm, intrinsic charge carrier density at T = 300 K $n_i = 1.45 \cdot 10^{10}$ cm⁻³.

Assuming a detector with a thickness of $d = 300 \, \mu \text{m}$ and an area of $A = 1 \, \text{cm}^2$.

→ Signal of a mip in such a detector:

$$\frac{dE/dx \cdot d}{I_0} = \frac{3.87 \cdot 10^6 \,\text{eV/cm} \cdot 0.03 \,\text{cm}}{3.62 \,\text{eV}} \approx 3.2 \cdot 10^4 \,\text{e}^-\text{h}^+ - \text{pairs}$$

→ Intrinsic charge carrier in the same volume (T = 300 K):

$$n_i dA = 1.45 \cdot 10^{10} \text{ cm}^{-3} \cdot 0.03 \text{ cm} \cdot 1 \text{ cm}^2 \approx 4.35 \cdot 10^8 \text{ e}^{-}\text{h}^{+}\text{-pairs}$$

→ Number of thermal created e⁻h⁺-pairs are four orders of magnitude larger than signal!!!

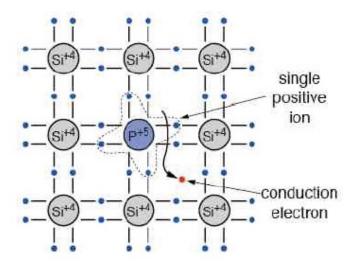
Have to remove the charge carrier!

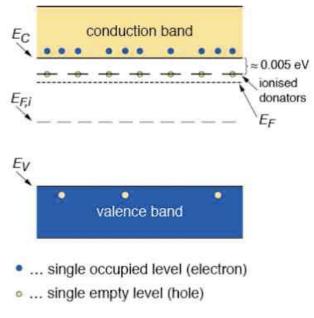
→ Depletion zone in reverse biased pn junctions

N-doping

Doping with an element 5 atom (e.g. P, As, Sb). The 5th valence electron is weakly bound.

The doping atom is called donor
The released conduction electron
leaves a positively charged ion



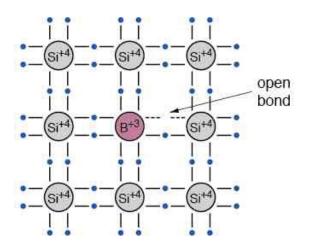


Electrons (holes) are called majority (minority) carriers.

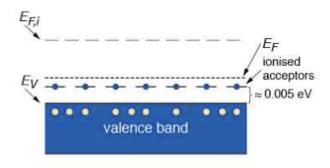
P-doping

Doping with an element 3 atom (e.g. B, Al, Ga, In). One valence bond remains open

The doping atom is called acceptor
The acceptor atom in the lattice
is negatively charged







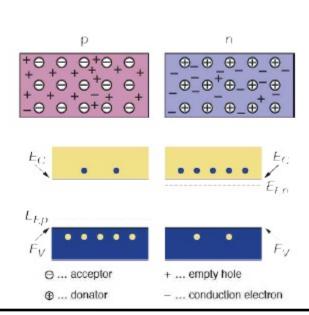
- ... single occupied level (electron)
- ... single empty level (hole)

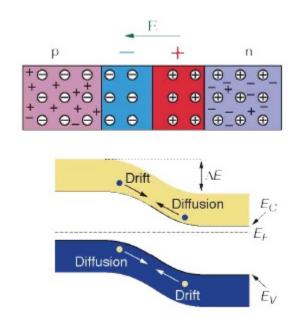
Holes (electrons) are called majority (minority) carriers.

The p-n junction

At n-type and p-type interface: diffusion of surplus carries to the other material until thermal equilibrium is reached.

The remaining ions create a space charge and an electric field stopping further diffusion. The stable space charge region is free of charge carries: the depletion zone.





The p-n junction – forward and reverse bias

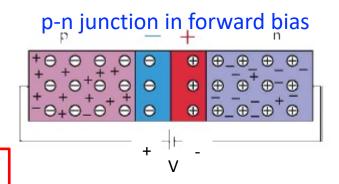
Applying a forward bias voltage *V,* e- and holes are refilled to the depletion zone.

The depletion zone becomes narrower

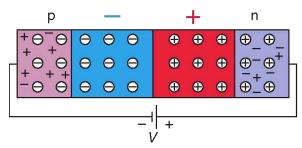
That's not what we want!

Applying a reverse bias voltage *V*, e- and holes are pulled out of the depletion zone.

The depletion zone becomes larger.



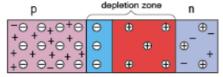
p-n junction in reverse bias



That's the way we operate our semiconductor detectors!

Electrical characteristics of p-n junction



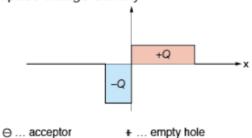


acceptor and donator concentration



space charge density

... donator



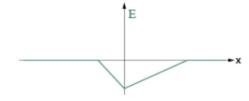
... conduction electron

concentration of free charge carriers

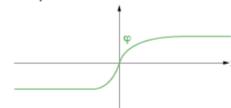


[Eckstein]

electric field



electric potential



P-n junction – width of the depletion zone

Example of a typical p+-n junction in a silicon detector:

Effective doping concentration $N_a = 10^{15}$ cm⁻³ in p+ region and $N_d = 10^{12}$ cm⁻³ in n bulk.

Without external voltage:

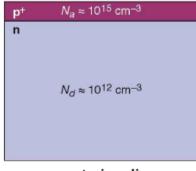
$$W_p = 0.02 \,\mu{\rm m}$$

$$W_n = 23 \, \mu \text{m}$$

Applying a reverse bias voltage of 100 V:

$$W_p = 0.4 \, \mu \text{m}$$

$$W_{p} = 363 \, \mu \text{m}$$



p+n junction

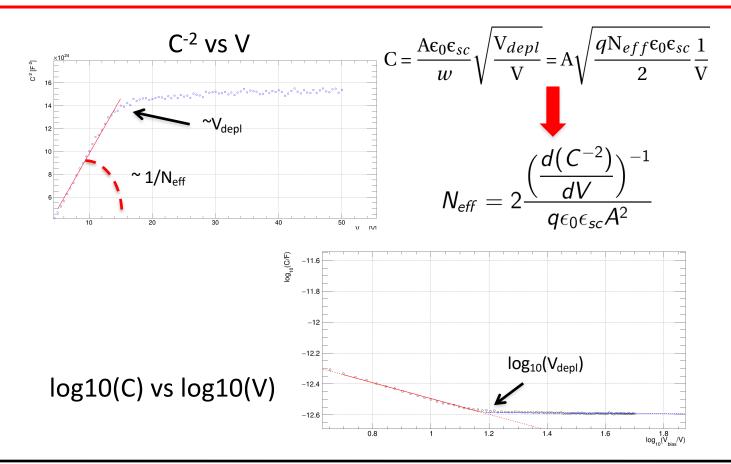
Width of depletion zone in n bulk:

$$W \approx \sqrt{2\varepsilon_0 \varepsilon_r \mu \rho |V|}$$

with
$$\rho = \frac{1}{e \mu N_{eff}}$$

 $\begin{array}{lll} \rho & \ldots & \text{specific resistivity} \\ \mu & \ldots & \text{mobility of majority charge carriers} \end{array}$... effective doping concentration

CV analysis: observables



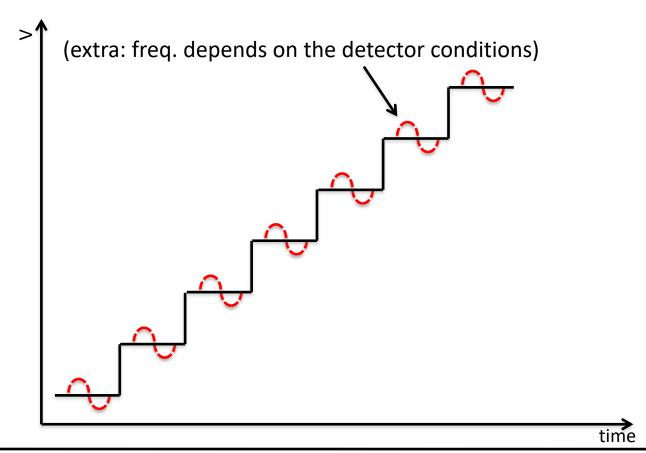
Depletion voltage: howto

 By definition, differential capacitance is the change in charge (Q) in a device in response to a change in voltage (V):

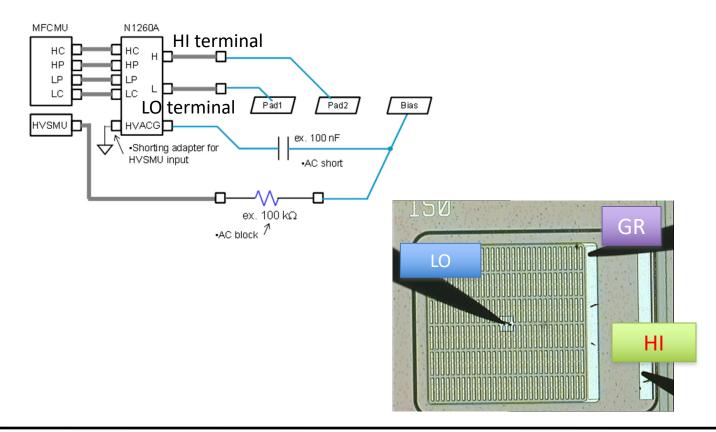
$$C = \Delta Q / \Delta V$$

- One general practical way to implement this is to apply a small AC ($v \sim 10^2 10^6$ Hz) voltage signal (millivolt range) to the device under test, and then measure the resulting current. Integrate the current over time to derive Q and then calculate C from Q and V.
- C-V measurements in a semiconductor device are made using two simultaneous voltage sources: an applied AC voltage signal (dVac) and a DC voltage (Vdc) that is swept in time, as illustrated in the next slide.

Voltage ramp for CV analysis



Connections for CV analysis

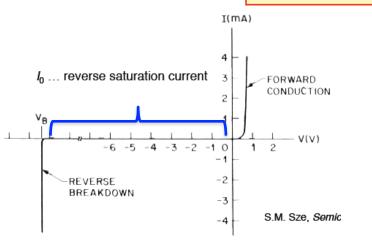


P-n junction – Current voltage characteristics

Typical current-voltage of a p-n junction (diode): exponential current increase in forward bias, small saturation in reverse bias.

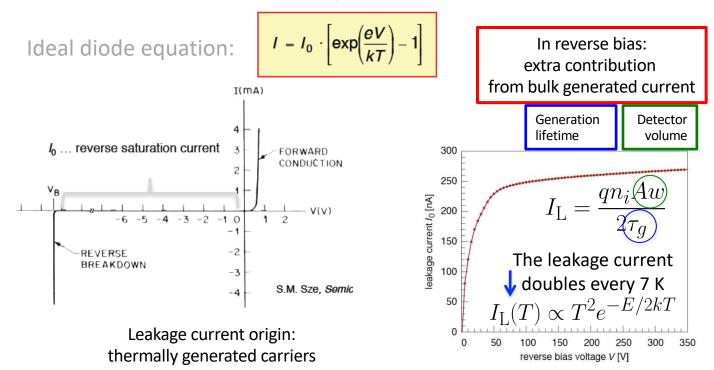
Ideal diode equation:

$$I = I_0 \cdot \left[\exp\left(\frac{eV}{kT}\right) - 1 \right]$$

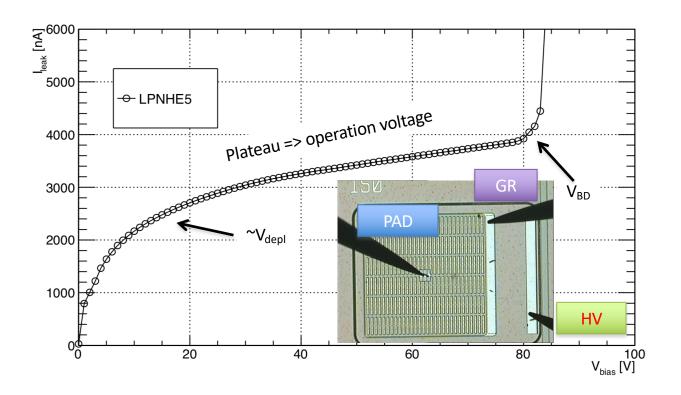


P-n junction – Current voltage characteristics

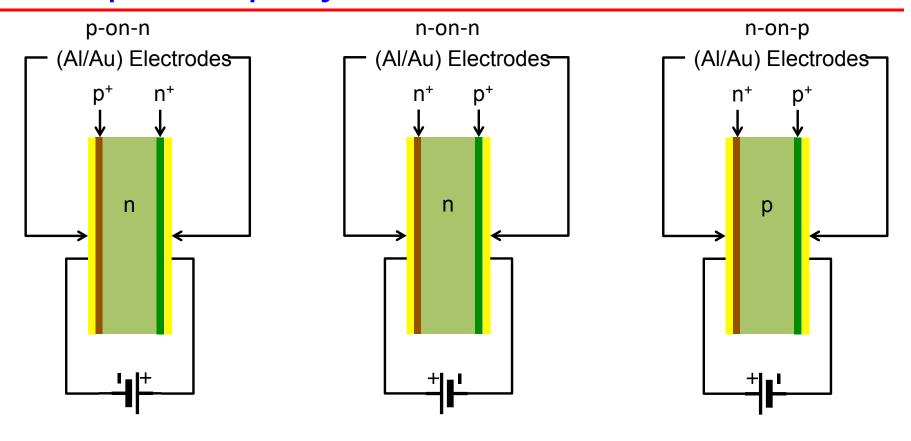
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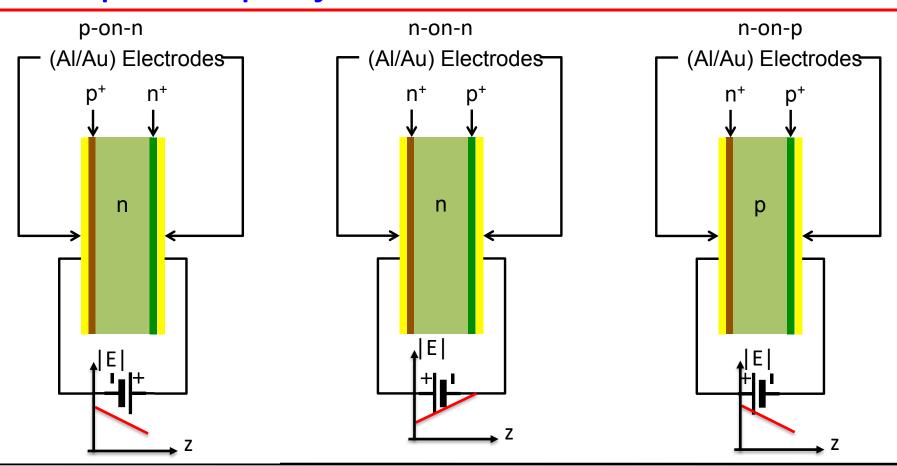
IV in real life



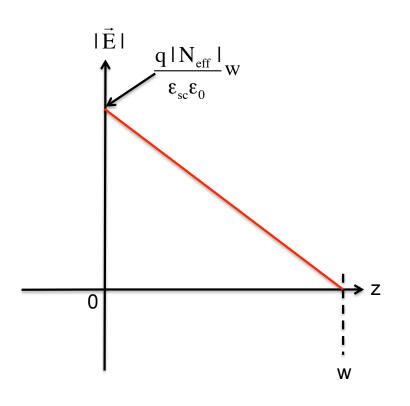
Examples of p-n junction diodes

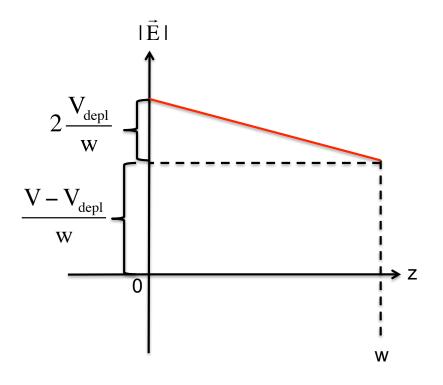


Examples of p-n junction diodes



Electric field at depletion and beyond





Quiz



Everywhere:
$$V(\vec{r}) = 0$$

 $\varrho(\vec{r}) = 0$

Quiz

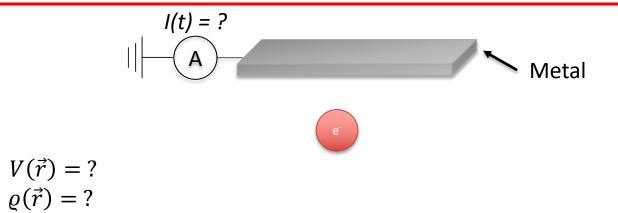


$$V(\vec{r}) = ?$$

 $\varrho(\vec{r}) = ?$



Quiz



Why does this matter?

Well, in your detector charges are moving towards electrodes at fixed voltage and you can measure currents...

Yes, you **ALWAYS MEASURE AN INDUCED SIGNAL DUE TO THE MOVEMENT OF CHARGE CARRIERS (electrons, holes – ions too)**

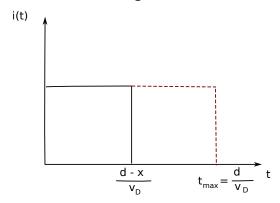
SIGNAL IS NEVER COLLECTED BY ELECTRODES BUT ALWAYS INDUCED ON THEM

More in slides from W. Riegler: https://indico.cern.ch/event/843083/

Signal formation in p-n junction

in principle like ionization chambers:

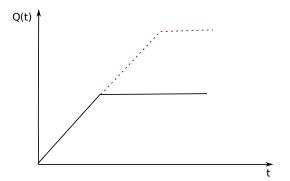
if E const: each drifting electron contributes to signal current while drifting



$$i = \frac{dq}{dt} = e \frac{dx}{d} \frac{1}{dx/v_D} = e \frac{v_D}{d}$$

d: width of depletion zone

x: location where electron was generated



capacitor charges:

$$Q = e \frac{v_D}{d} \cdot t = e \frac{v_D}{d} \frac{d - x}{v_D}$$

Signal from uniform deposition

line charge of electrons across the depletion layer (constant ionization along track):

$$i = N_0 e \frac{v_D}{d} \left(1 - \frac{t v_D}{d} \right) \Theta \left(1 - \frac{t v_D}{d} \right)$$

$$Q(t) = N_0 e \frac{v_D}{d} \left(t - \frac{t^2 v_D}{d} \right) \Theta \left(1 - \frac{t v_D}{d} \right)$$

integrated:

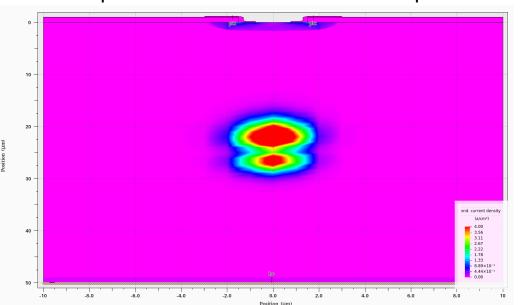
$$Q\left(t = \frac{d}{v_D}\right) = \frac{N_0 e}{2}$$

same signal for positive carriers (holes), thus in total

$$N_0 \cdot e = Q_{tot}$$

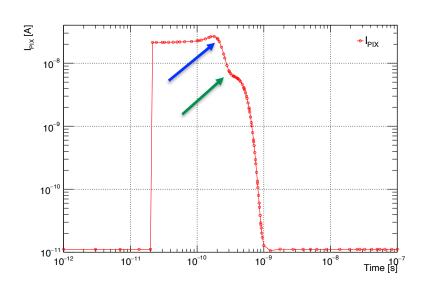
Signal from point deposition

Conduction current density between 50 and 600 ps after the conversion at ~ mid plane



Want to know more? Ask me about TCAD ∅

Photocurrent



At 200 ps first e- arrive at PIX By 300 ps they are gone



Ionization yield and Fano factor

mean energy per electron-hole pair

	$E_0^{300 \text{ K}}$	$E_0^{77 \text{ K}}$	$E_{\sf gap}$
Si	3.6 eV	3.8 eV	1.1 eV
Ge	_	2.9 eV	0.7 eV

 $\sim rac{2}{3}$ goes into excitation of crystal lattice

Energy loss
$$\Delta E$$
 \Rightarrow
$$\begin{cases} & \frac{\text{lattice vibrations: generation of phonons}}{\text{typical quantum energy } E_x = 0.037 \text{ eV}} \\ & \text{ionization:} & \text{characteristic energy } E_i = E_{\text{gap}} = 1.1 \text{ eV in Si}} \\ & \text{total:} & \Delta E = E_i N_i + E_x N_x \end{cases}$$

assume Poisson distributions for both processes with $\sigma_i = \sqrt{N_i}$ $\sigma_x = \sqrt{N_x}$

for a fixed energy loss $\Delta E\colon$ sharing between ionization and lattice excitation varies as

on average:

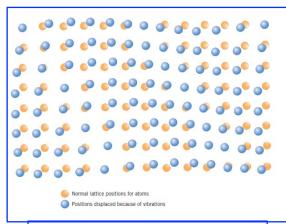
using
$$N_x = (\Delta E - E_i N_i)/E_x$$

$$E_{x}\Delta N_{x} + E_{i}\Delta N_{i} = 0$$

$$E_i \sigma_i = E_{\mathsf{x}} \sigma_{\mathsf{x}}$$

$$\sigma_i = \frac{E_x}{E_i} \sigma_x = \frac{E_x}{E_i} \sqrt{N_x}$$

$$\sigma_i = \frac{E_x}{E_i} \sqrt{\frac{\Delta E}{E_x} - \frac{E_i}{E_x} N_i}$$



Schematic representation of the generation of lattice waves in a crystal by means of atomic vibrations. Source: Callister & Rethwisch (2010)

Ionization yield and Fano factor

$$N_i = \frac{\Delta E}{F_0}$$
 in case of ideal charge collection without losses

$$\rightarrow \qquad \sigma_{i} = \frac{E_{x}}{E_{i}} \sqrt{\frac{\Delta E}{E_{x}} - \frac{E_{i}}{E_{x}}} \frac{\Delta E}{E_{0}} = \underbrace{\sqrt{\frac{\Delta E}{E_{0}}}}_{\sqrt{N_{i}}} \underbrace{\sqrt{\frac{E_{x}}{E_{i}}} \left(\frac{E_{0}}{E_{i}} - 1\right)}_{\sqrt{F}}$$
F: Fano factor

Si: $E_0 \cong 3.6 \text{ eV}$ $F \cong 0.1$ Ge: $E_0 \cong 2.9 \text{ eV}$ $F \cong 0.1$

$$\sigma_i = \sqrt{N_i}\sqrt{F}$$
 smaller than naive expectation

due to energy conservation, fluctuations are reduced for a given energy loss ΔE (the total absorbed energy does not fluctuate)

relative energy resolution

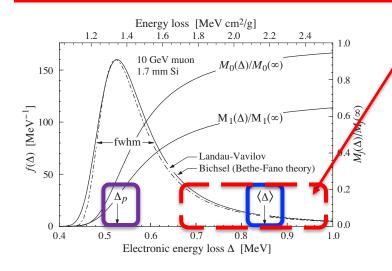
$$\boxed{\frac{\sigma_i}{N_i} = \frac{\sqrt{N_i \, F}}{N_i} = \frac{\sqrt{F}}{\sqrt{N_i}} = \frac{\sqrt{F \, E_0}}{\sqrt{\Delta E}} = \frac{\sigma_{\Delta E}}{\Delta E}}$$

> 60% discount on energy resolution ©

example: photon of 5 keV, $E_{\gamma}=\Delta E,~\sigma_{\Delta E}=40~\text{eV}\cong1\%$ instead of 2.7% w/o Fano factor

July 23, 2018

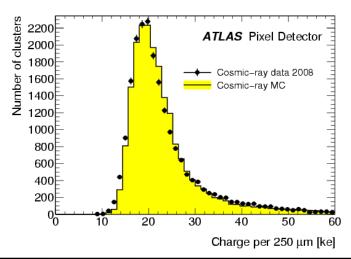
Intermezzo: Landau distribution



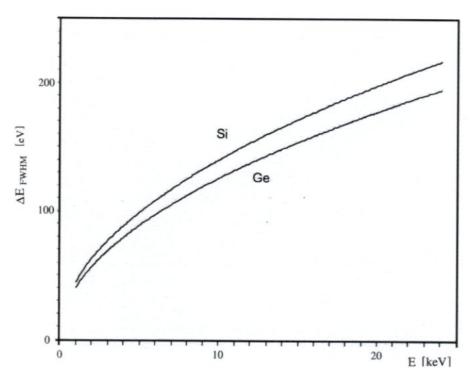
Very long tail

Average $<\Delta>$ and most probable value Δ_p (MPV) are very different

(If absorber is very thin Landau model fails)



Energy resolution



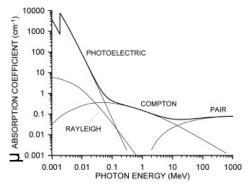
intrinsic resolution due to statistics of charge carriers generated, in addition noise and non-uniformities in charge-collection efficiency

Energy measurement – summary

Photons

Point-like interaction

Infinitesimal interaction probability: dP=µdx



- Photo: 1 e-h pair per conversion
- e- from X-ray can trigger secondary emission

Charged particles in Silicon

Charges created along the track

- 3.6 eV (E_i) to create an e-h pair => 80 e-h / μ m (most probable)
- Most probable charge (300 µm) ≈ 24000 e ≈ 4
 fC
- <-dE/dx> (MIP) ~ 3.87 MeV/cm

Energy *E* intrinsic resolution of a semiconductor detector:

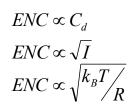
$$\Delta E_{FWHM} = 2.35 \cdot \sqrt{FEE_i}$$

F the Fano factor; F ~ 0.1 for Si.

E.g. for photons of few keV a 100 eV resolution can be achieved

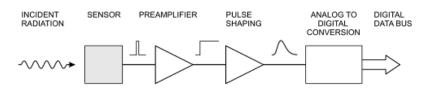
Intermezzo: noise

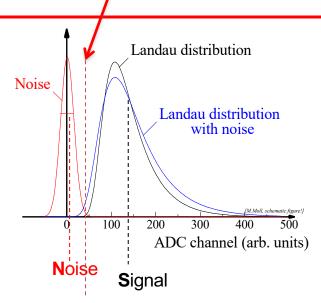
Cut (threshold)



- Landau distribution has a low energy tail
 - becomes even lower by noise broadening
 - Noise sources: (ENC = Equivalent Noise Charge)
 - Capacitance
 - Leakage Current
 - Thermal Noise (bias resistor)
 - Figure of Merit: Signal-to-Noise Ratio S/N
 - Typical values >10-15, people get nervous if < 10.
 Radiation damage severely degrades the S/N.
 - If threshold is too high → inefficiency
 - If threshold is too low → noise occupancy

The complete detecting chain



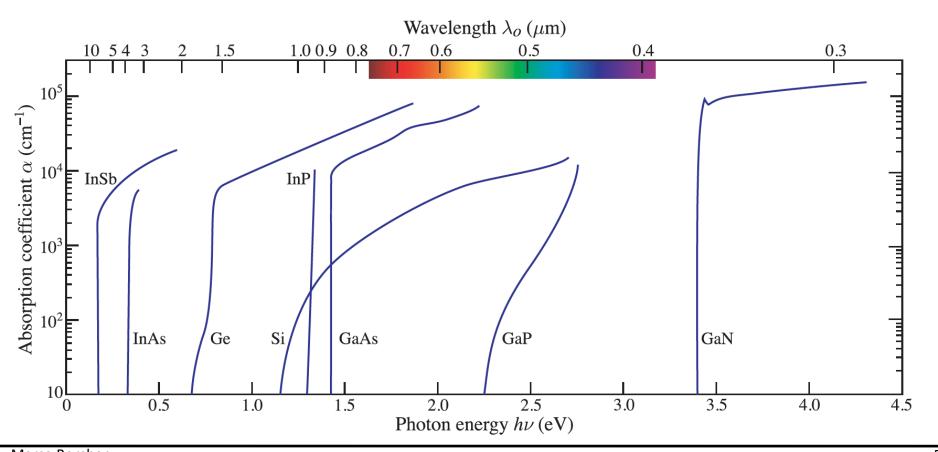


Preamplifier: signals in silicon (0.05-4 fC) must be amplified. Minimize noise amplification!

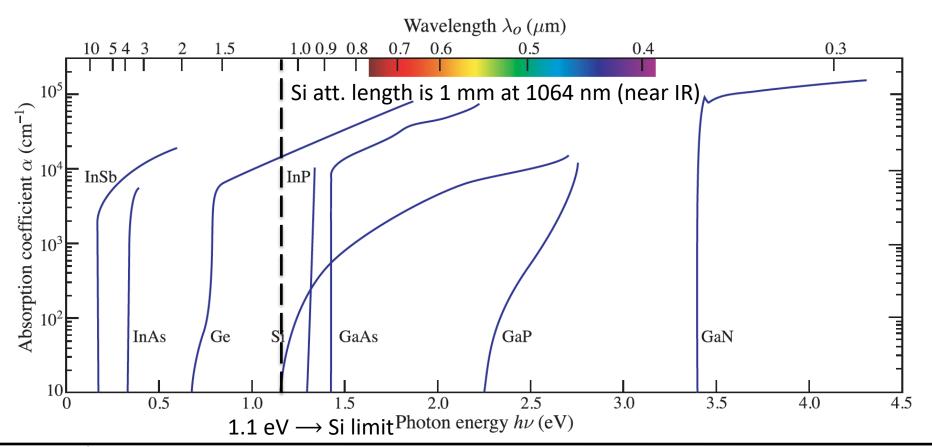
Pulse shaping: its primary function is to improve the signal-to-noise ratio. This is done by applying filters that tailor the frequency response

Typically bandwidth reduction which translates into an increase of the pulse duration ("shaping time")

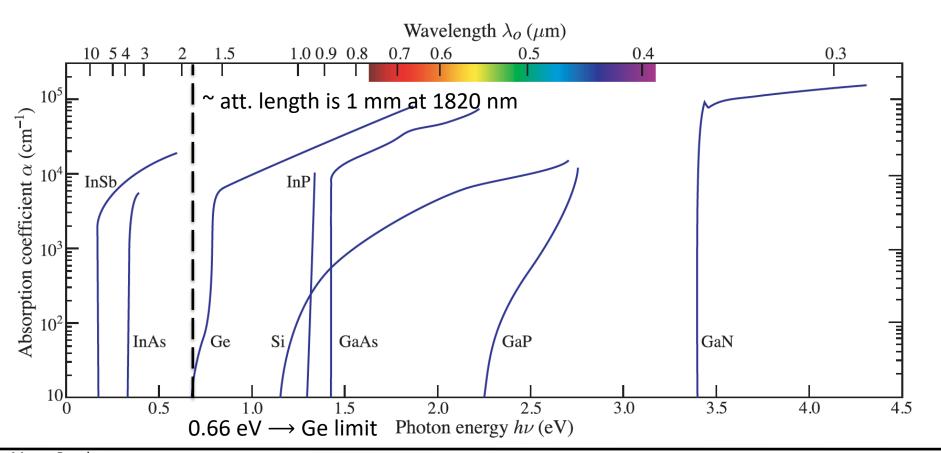
Absorption coefficient



Absorption coefficient

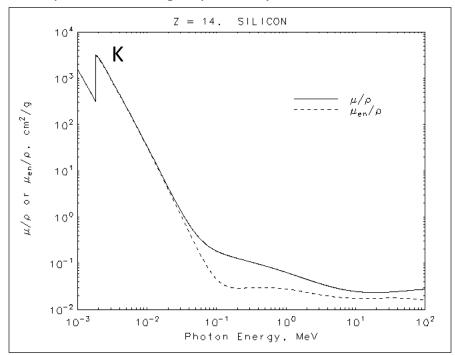


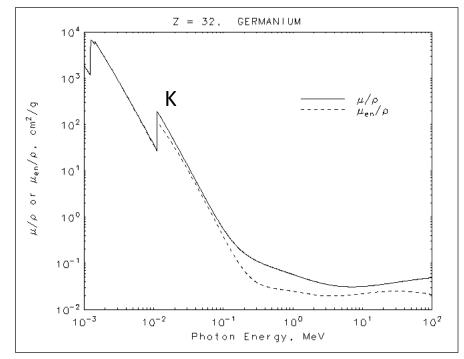
Absorption coefficient



Photon attenuation coeff. – keV to 100 MeV

[https://www.nist.gov/pml/x-ray-mass-attenuation-coefficients]



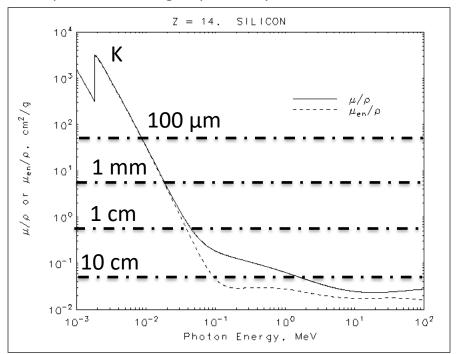


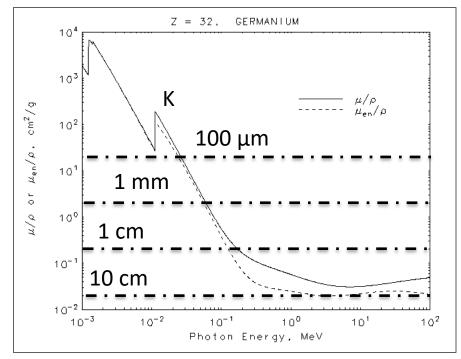
 $\rho_{\rm Si}$ ~ 2.3 g/cm³

 $ho_{\rm Ge}$ ~ 5.3 g/cm³

Photon attenuation coeff. – keV to 100 MeV

[https://www.nist.gov/pml/x-ray-mass-attenuation-coefficients]





 $\rho_{\rm Si} \sim 2.3 {\rm g/cm^3}$

$$\rho_{\rm Ge}$$
 ~ 5.3 g/cm³

Position measurement

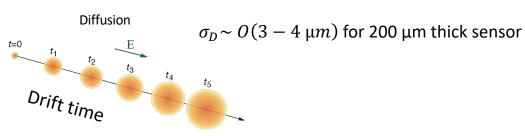
The position resolution depends on physical processes and on external parameters

Physical processes:

- statistical fluctuations in the energy loss
- diffusion: $\sigma_D = \sqrt{2Dt}$

External parameters:

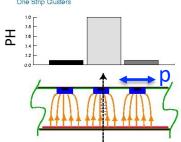
- analogue/binary signal readout
- detector segmentation ("pitch" p)
- signal-to-noise-ratio SNR



Single channel, binary r.o.

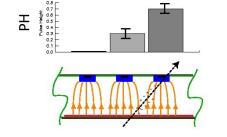
x = strip position

$$\sigma = p/\sqrt{12}$$



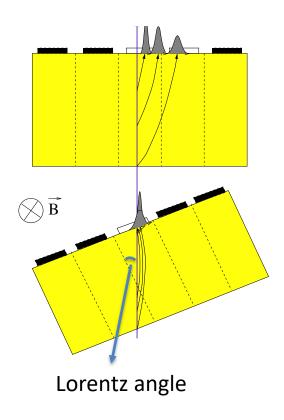
Analogue r.o.

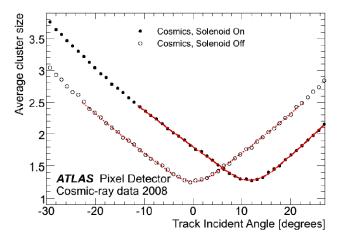
$$x = (x_1h_1 + x_2h_2)/(h_1 + h_2)$$
 $x_i = i-th \text{ strip pos.}$
 $\sigma \approx p/SNR$ $h_i = i-th \text{ strip PH}$



[Turchetta, 1993]

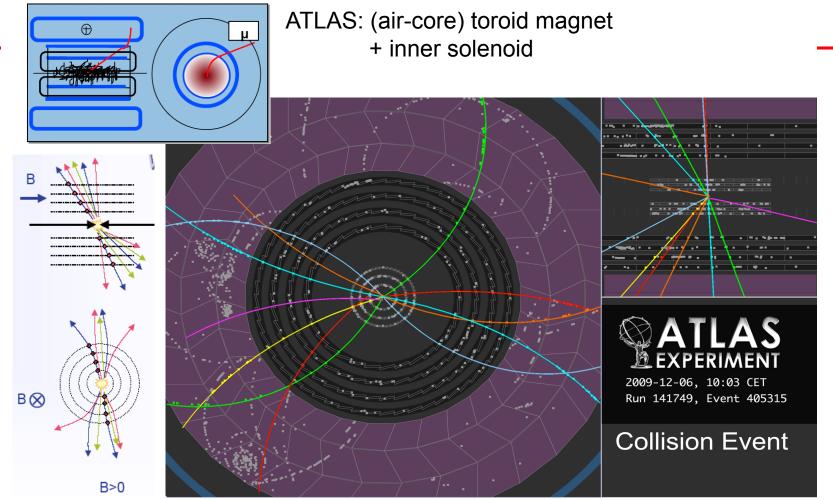
Position measurement in magnetic field





(a) Pixel Detector mean cluster width

Eur. Phys. J. C (2010) 70: 787–821 10.1140/epjc/s10052-010-1366-7



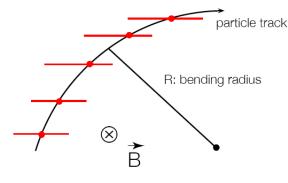
Tracking detectors

Momentum determination

in a cylindrical drift chamber ...

$$\frac{mv^2}{R} = evB \quad \Rightarrow \quad p = eB \cdot R$$

$$p\left[\frac{GeV}{c}\right] = 0.3 \text{ B[T] R[m]}$$



[Garutti]

momentum component perpendicular to the B-field transverse momentum p,

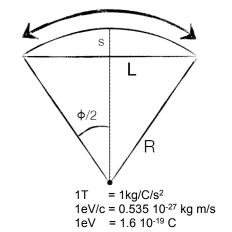
For Sagitta s:

$$s = R - R\cos\frac{\phi}{2} \approx R\frac{\phi^2}{8} \qquad \text{with } \phi = \frac{L}{R}$$

$$s = R\frac{L^2}{8R^2} = \frac{L^2}{8R} \quad \text{and} \quad R = \frac{L^2}{8s} \quad \text{radius is obtained by a circle fit through measurement points along}$$

with
$$\phi = \frac{L}{R}$$

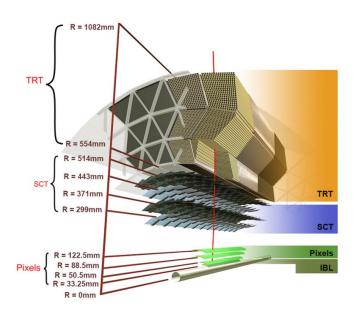
measurement points along the track with point resolution $\sigma_{r\phi}$

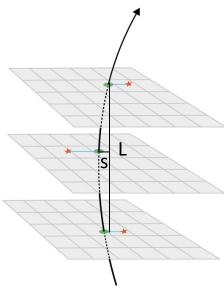


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Numerical example







$$p\left[\frac{GeV}{c}\right] = 0.3 \text{ B[T] R[m]}$$
 $s = \frac{L^2}{8R}$

If we assume L = 1 m and B = 2 T and p = 1 TeV/c then:

R = p/(0.3 * B) = 1000 / 0.6
$$\sim$$
 1670 m s = 1/(8*1670) m \sim 0.075 mm

If we want to measure the momentum with a relative precision of 20% at p = 1 TeV/c, then:

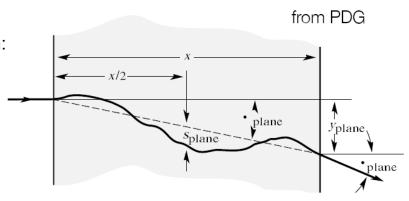
$$\Delta p/p \sim \Delta s/s = 20\% => \Delta s \sim 15 \mu m$$

Momentum resolution

Multiple scattering contribution:

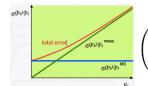
$$\sigma_{\phi} \approx \frac{14 \text{ MeV}/c}{p} \sqrt{\frac{L}{X_0}}$$

$$\frac{\sigma_p}{p} = \frac{\sigma_R}{R} = \frac{\sigma_\phi}{\phi}$$
 as $R = \frac{L}{\phi}$



At small momenta this limits resolution of momentum measurement ... momentum

 $\frac{\sigma_p}{p} = \frac{\sigma_\phi}{\phi} = \frac{14~\mathrm{MeV}/c}{p} \sqrt{\frac{L}{X_0}} \cdot \frac{R}{L} = \frac{14~\mathrm{MeV}/c}{p} \sqrt{\frac{1}{LX_0}} \cdot \frac{p}{eB} \sim \frac{1}{\sqrt{LX_0}B}$ independent



$$\left(\frac{\sigma_{p_t}}{p_t}\right)^2 = \operatorname{const} \cdot \left(\frac{p_t}{BL^2}\right)^2 + \operatorname{const} \cdot \left(\frac{1}{B\sqrt{LX_0}}\right)^2$$

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Take home message on momentum resolution

- At low momentum the resolution is dominated by multiple scattering
- \triangleright Important to reduce the material budget x/X_0

Si: $X_0 \sim 9.4$ cm

- At high momentum the sagitta determination is the dominant factor
- > Finer and finer segmentation is necessary
- ➤ Longer and longer lever arm
- > Stronger and stronger magnetic field

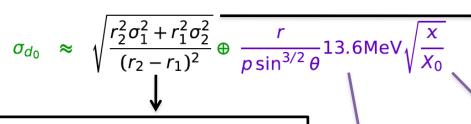
$$\frac{\sigma_{p_T}}{p_T} = \frac{8p_T}{0.3BL^2}\sigma_s$$

 \triangleright Very important: the larger the p_T the worse the resolution

Vertexing resolution

Looking for significant impact parameter IP, d_0 , and maybe form a reconstructed secondary vertex.

The IP resolutions depends on geometry, material and track momentum



Geometry: use small r_1 , large r_2 , and small intrinsic spatial resolution σ_1 , σ_2

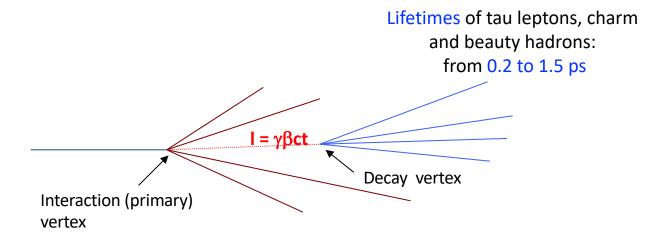
Multiple Scattering: important for low momentum tracks; best precision with small radius *r* and minimum thickness *x*

Marco Bomben

Simplified model w/ 2 layers only

Semiconductor detectors for vertexing

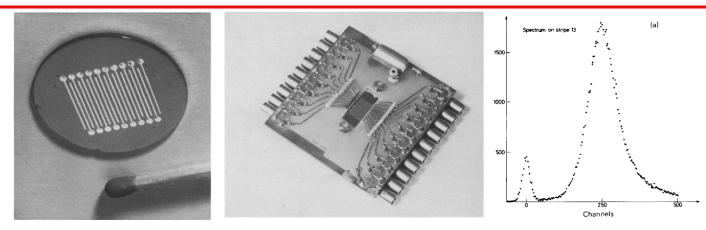
'70s-'80s: ~ps lifetime particles discovered



decay length $I = \gamma \beta ct$, so typically the decay vertex is at a distance of single millimeters from the interaction vertex

Marco Bomben 6-

History – MESD by Pisa group (1980)



MESD featured 12 mm long 300 μm wide aluminium strips on a high resistivity Silicon wafer.

The signal was proportional to the energy released by the impinging particle. It assured good spatial resolution with low noise at room temperature.

All the desirable features of silicon detectors were already exploited by the first high energy physics detectors

S. R. Amendolia et al., A Multi-Electrode Silicon Detector for High Energy Experiments, Nucl. Instr. Meth. 176 (1980)

Want to know more?

Silicon as detector material: summary

Reverse biased p-n junction as radiation detector: the depletion region is virtually free of mobile carriers \rightarrow in absence of radiation only the (small) diode reverse current flows in the junction

Energy deposition: creation of a e-h pair for $E \sim 3.6 \text{ eV}$ (gas: 15-30 eV) \rightarrow Large signals!

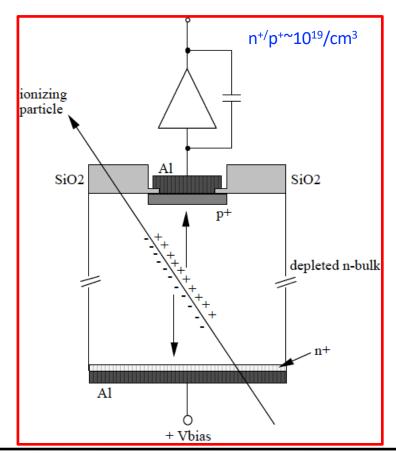
High electric field in the depleted bulk

→ elec's and holes drift very fast across the depletion zone: t_{coll} ~ 10-30 ns

Low doping concentration (high resistivity) of the bulk \rightarrow V_{depl} at low bias voltages (safely below V_{BD})

$$N_{\rm eff} \sim 10^{12} \, / {\rm cm}^3 \Leftrightarrow \rho \sim 5-10 \, {\rm k}\Omega$$

Excellent spatial resolution thanks to fine segmentation (due to progress in μ -electronics)



Outline

Main applications, motivations and history

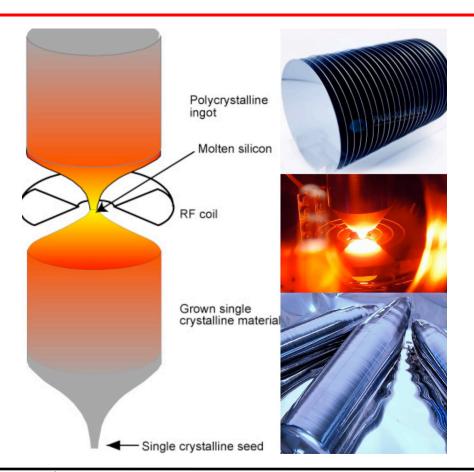
Semiconductors physics

Silicon radiation detectors

Timing with silicon detectors

Perspectives

Float Zone Silicon



Very pure Silicon is obtained

A polycrystalline rod of ultrapure electronic-grade silicon is passed through an RF heating coil

A seed crystal is used at one end to start the growth. The whole process is carried out in an evacuated chamber or in an inert gas purge

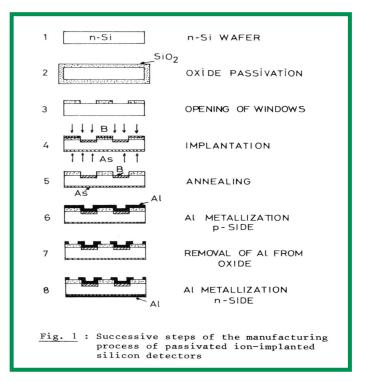
History – Planar process, Munich group ('80s)

NUCLEAR INSTRUMENTS AND METHODS 169 (1980) 499-502. © NORTH HOLLAND PUBLISHING CO

FABRICATION OF LOW NOISE SILICON RADIATION DETECTORS BY
THE PLANAR PROCESS

J KEMMER
Fachbereich Physik der Technischen Universität Munchen, 8046 Garching, Germany

"Combining the techniques of oxide passivation, photo engraving and ion implantation, it's possible to get a large number of detector chips with only small tolerances in their geometrical and electrical properties"



Performance:

- ✓ leakage current < 1 nA / cm²/100 µm
- ✓ energy resolution of 100 keV for 5486 keV alphas of ²⁴¹Am

Silicon pad diode

A single p-n diode in reverse bias is the simplest silicon radiation detector Often it is called pad diode The size varies between few mm² to few cm² Guard Rings (GRs) assure a smooth transition between the High Voltage (HV) and the GRs Ground (GND) potential n+ 100-1000 µm PAD Central openings in the aluminium layer for visible/IR photon detection p+

N-on-p production

Silicon PIN diodes

- Sixties evolution: the p-i-n (PIN) photodiode
- Wavelength range of some 150 to 1100 nm, covering:
 - the emission wavelength of almost all organic and inorganic scintillators
 - Cherenkov radiators used in particle physics
- Very successful device
- Still used in
 - high energy physics (PMTs replacemet)
 - radiation detection
 - and medical imaging



PIN diode: electrical properties

needs to be cooled permanently (liq. N_2) to avoid separation of Li from impurities by diffusion!

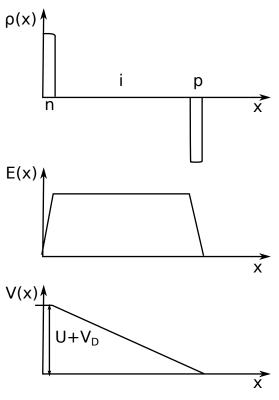
application: γ -spectroscopy

larger cross section for photo effect in $\ensuremath{\mathsf{Ge}}$ as compared to $\ensuremath{\mathsf{Si}}$

 \rightarrow Ge(Li) preferred

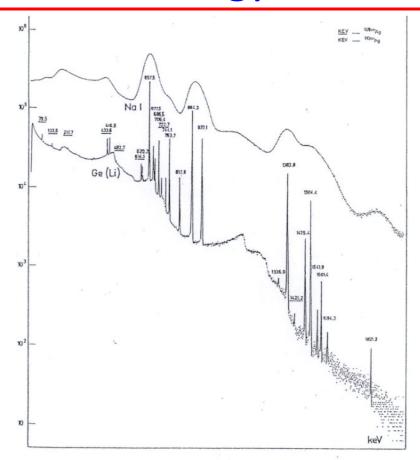
however: full energy peak contains only order of 10 % of the signal in a 50 cm³ crystal (30 % in a 170 cm³ crystal))

- resolution much better than Nal
- efficiency significantly lower



external voltage \it{U} and diffusion voltage $\it{V}_{\it{D}}$

PIN diode: energy resolution

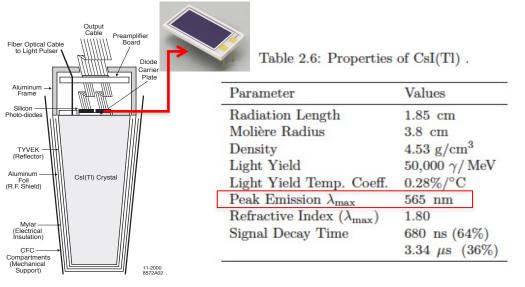


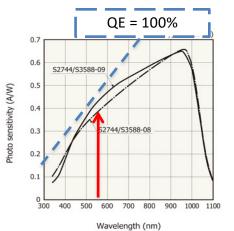
Ge(Li) detectors - a revolution in γ spectroscopy in the mid 1960ies: comparison of spectra obtained with NaI (state of the art technique until then) and Ge(Li)

comparative pulse height spectra recorded using a sodium iodide scintillator and a Ge(Li) detector source of γ radiation: decay of $^{108m}{\rm Ag}$ and $^{110m}{\rm Ag}$, energies of peaks are labeled in keV

July 23, 2018

Si PIN diodes for a CsI(TI) calorimeter (BaBar)



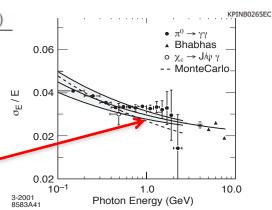




QE for peak emission close to 80%

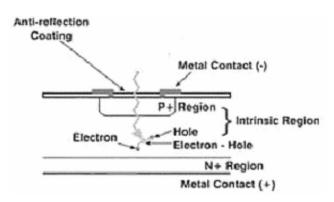
PMTs only 10-15%

Photon energy resolution ~ 2-3% @ 1GeV



Si PIN diodes: pros and cons

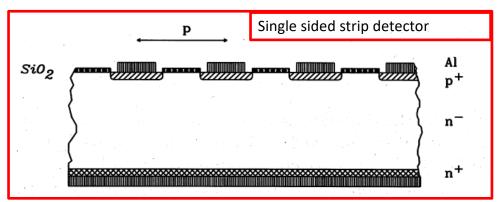
- ✓ Simple and reliable
- √ Can operate in B
- ✓ Low voltage wrt PMTs
- No internal gain:
- ✓ Output very stable
- X Charge sensitive preamplifier is needed
- X Low bandwidth filter is needed
 - To cope with noise (leakage current + capacitance)
- X Preamp & filter makes signal slow
- E.g.: minimal detectable signal: O(100)/cm² photons with a filter time constant of few μs



Position measurement: Silicon microstrip detector

Segmentation of the collecting electrode, independent readout of them position sensitive detector

Typical strip pitch 20-50 μm



The connection between the strips and the readout chips is done via micro-bonding techniques (wires $^{\sim}20 \mu m$ diameter)

Single sided microstrip detector

→ Excellent position resolution in one dimension

Reminder:

Binary r.o., single strip: $\sigma = p/\sqrt{12}$

Analogue r.o., 2 strips cluster: x (C.O.G.) = $(x_1h_1+x_2h_2)/(h_1+h_2)$, $\sigma \sim p/(SNR)$ (h_i =sign. amp.)

Double-sided microstrip detectors (DSSD)

Single sided detector measures only one coordinate. To measure second coordinate requires second detector layer

Double sided strip detector measures two coordinates in one detector layer (minimizes material)

In n-type detector the n⁺ backside becomes segmented, e.g. strips

orthogonal to p⁺ strips

Drawback: expensive as production, handling, and tests are more complicated

Reminder

Single channel, binary r.o.

$$x = strip position$$

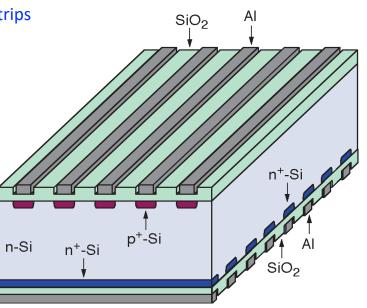
 $\sigma = p/\sqrt{12}$

Analogue r.o.

$$x = (x_1h_1 + x_2h_2)/(h_1 + h_2)$$

$$\sigma \approx p/SNR$$

Scheme of a double sided strip detector (biasing structures not shown):

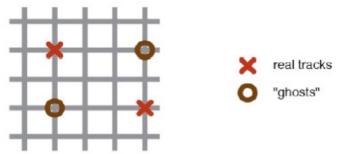


DSSD limitations

DSSD measure the 2 dimensional position of a particle track.

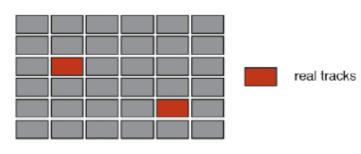
However, if more than one particle hits the strip detector the measured position is no longer unambiguous. "Ghost"-hits appear!

True hits and ghost hits in a double sided strip detector in case of two particles traversing the detector:



Pixel detectors produce unambiguous hits!

Measured hits in a pixel detector in case of two particles traversing the detector:



Hybrid Pixel Detectors

HPD: Typical size is (50-400) μm x 50 μm

If signal pulse height is not recorded, resolution is the digital resolution: $\sigma=p/\sqrt{12}$

 $e.g. \sigma = 14 \mu m$ for p = 50 μm

Reminder: better resolution is achieved with analogue readout

Small pixel area → low detector capacitance (~ few fF/pixel) → large SNR (>> 10)

Small pixel volume → low leakage current (~ few pA/pixel)

Drawbacks of HPD: large number of readout channels

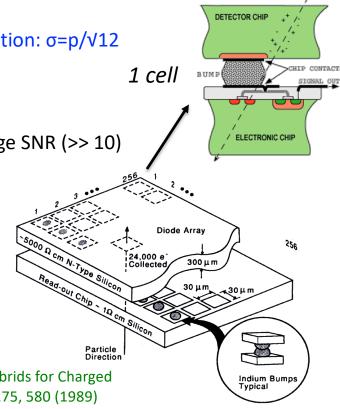
DSSD ~ 2n

HPD $\sim n^2$

Large number of electrical connections in case of HPD

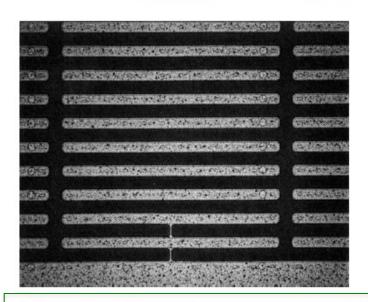
Large power consumptions of electronics

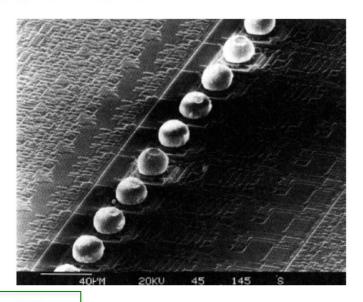
S.L. Shapiro et al., Si PIN Diode Array Hybrids for Charged Particle Detection, Nucl. Instr. Meth. A 275, 580 (1989)



HPD – bump bonding process

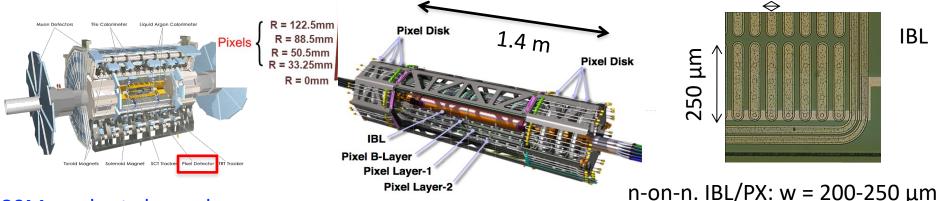
Electron microscope picture of pixel detector with long strip. Left: Detector chip, right: readout chip with bump bonds applied.





G. Lutz, Semiconductor Radiation Detectors, Springer-Verlag, 1999

Example: ATLAS IBL & Pixel Detector 50 μm

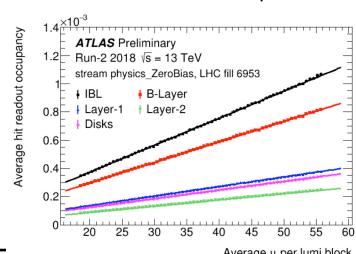


80M readout channels

Average number of pixel hits per module per event for each layer vs number of pp collisions per bunch crossing

IBL/PX: 26880/46080 pixels per module

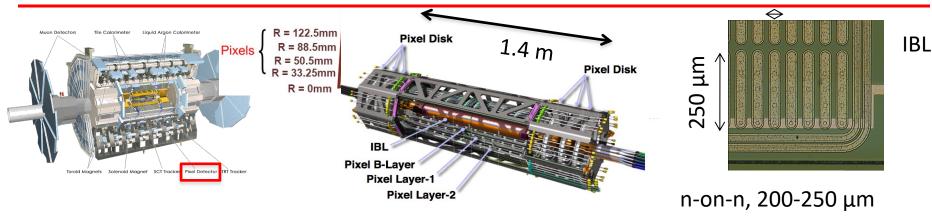
A very "quiet" detector"!

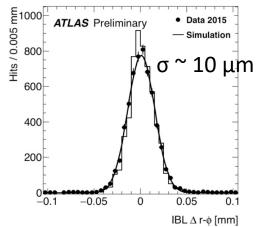


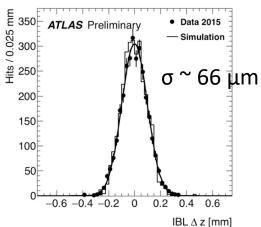
81

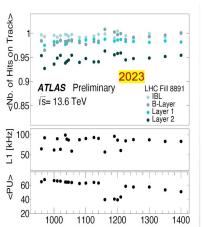
Marco Bomben Average μ per lumi block

Example: ATLAS IBL & Pixel Detector 50 μm





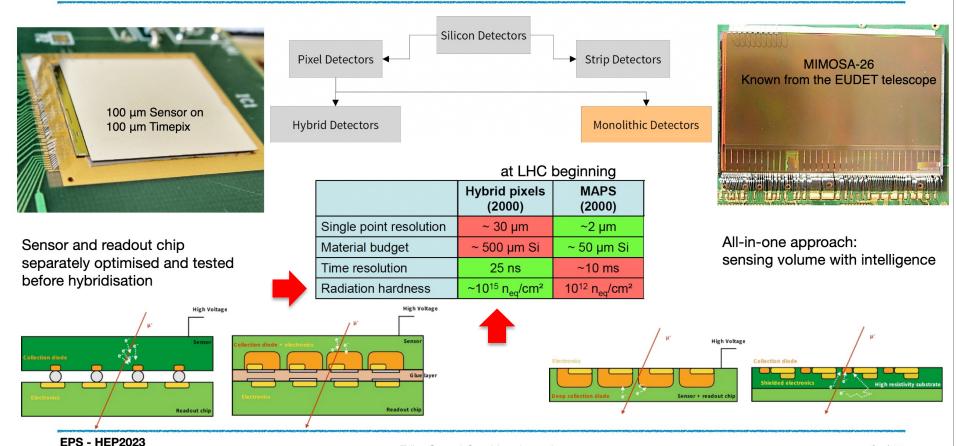




Efficiency high despite the radiation damage to sensors and electronics

Segmented silicon detectors

various design concepts



Marco Brown by erg, August 2023

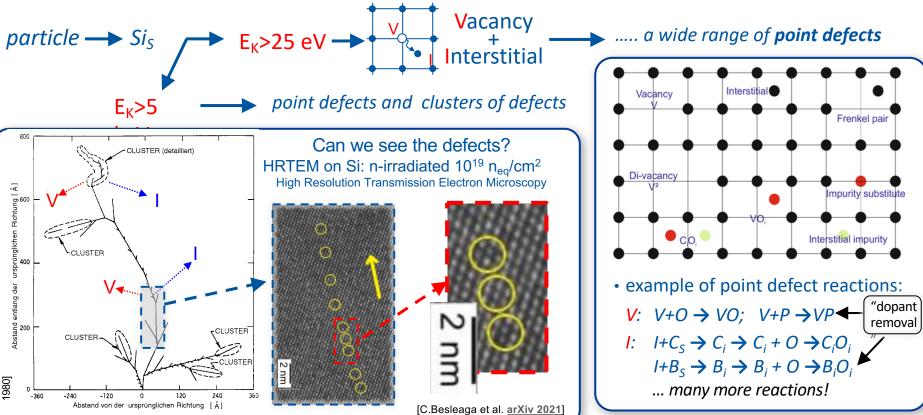
Erika.Garutti @ uni-hamburg.de

8 / 30

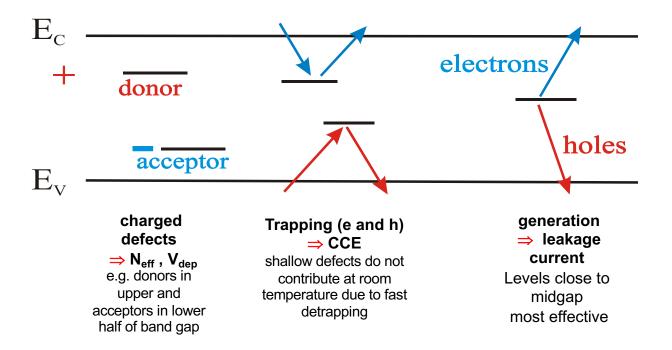


Displacement Damage

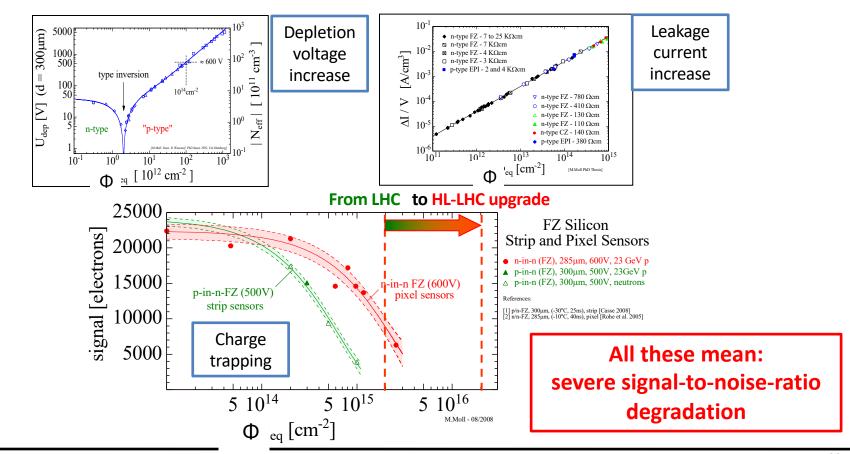




Radiation damage in Silicon



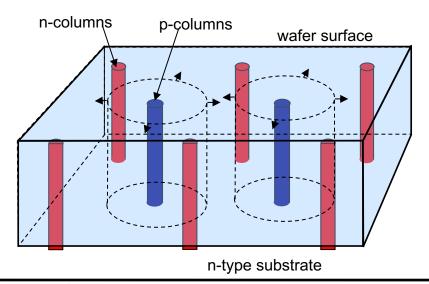
Radiation damage: macroscopic effects

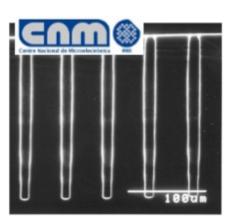


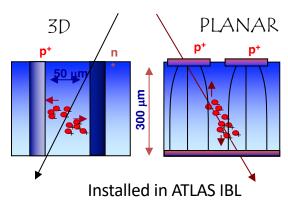
3D sensor technology

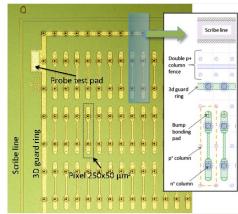
S. Parker et. al. NIMA 395 (1997) 328

- "3D" electrodes:
- narrow columns along detector thickness,
- diameter: 10mm, distance: 50 100mm
- Lateral depletion:
- lower depletion voltage needed
- thicker detectors possible
- fast signal
- radiation hard: smaller collection path!









3D sensors in ATLAS IBL

ATLAS, 2024 JINST 19 P10008

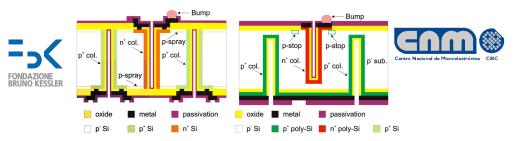
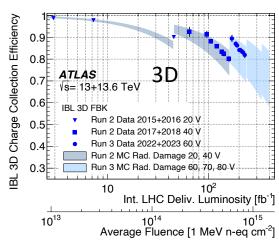


Figure 2. Pixel layout and schematic cross-sections of IBL 3D sensors from FBK (left) with columns passing fully through the substrate and CNM (right), where both column types stop about $20 \,\mu m$ from the surface. In both cases the substrate thickness is $230 \,\mu m$ and the inter-electrode spacing is $67.3 \,\mu m$. Reproduced from [10]. Published under licence by IOP Publishing Ltd. All rights reserved.

Superior radiation tolerance

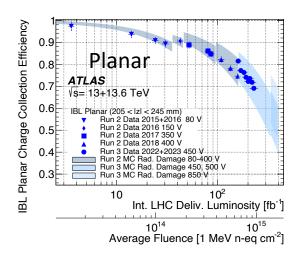
Testbench for high luminosity phase



First time in HEP experiment

Two vendors

Two designs



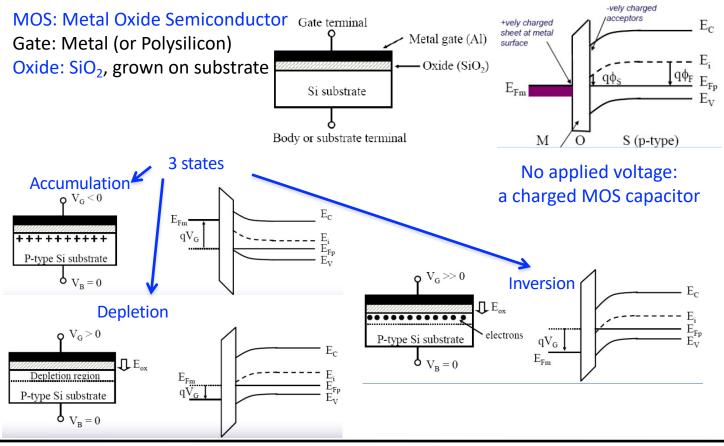
Other Si Detector Structures

Silicon (PIN) diodes, Silicon Single and Double Sided Strip detectors and Hybrid Pixels detectors are mature technologies employed in almost every experiment in High Energy Physics

Let's now look at other interesting Silicon Detector Structures

- Charged Coupled Devices (CCD)
- Silicon Drift Detectors (SDD) not enough time
- Avalanche Photo Diode (APD)
- Silicon Photo Multipliers (SiPM or Pixelized Photon Detector (PPD) or Multi-Pixel Photo Counters (MPPC))

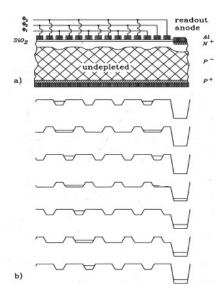
Intermezzo: the MOS structure



MOS CCDs detectors

Invented in 1969, CCDs have been used for a long time as memories (storing and transfer of charge) and as optical sensors (image devices in video cameras)

Most important field of application as detectors: imaging in Astrophysics, from near infrared to X-rays.



Conceptually: an array of MOS capacitors operated in overdepletion mode.

Electrons are created by ionization in the thin depleted region close to the silicon- oxide interface.

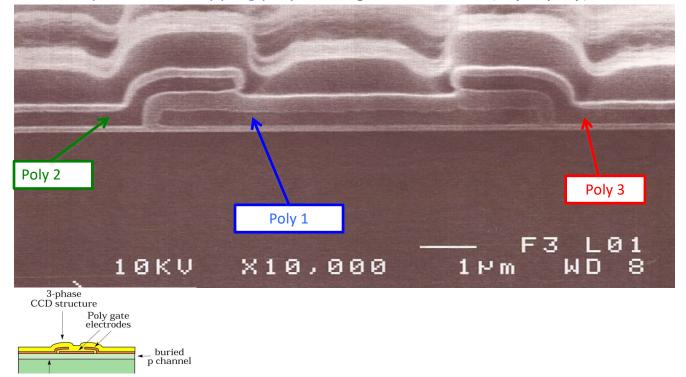
Charges are stored in the local energy minima at the Si-SiO₂ interface.

The charge can be moved towards the collecting electrode by periodically switching the voltages $\phi 1$, $\phi 2$ and $\phi 3$.

Slow device, hence not suitable for fast detectors Problem: charge losses during transport are high because of the large density of trapping defects at the Si-SiO2 interface.

CCDs for astronomy and astrophysics today

Scientific CCDs typically use the same 3-phase clocking as in the original Boyle and Smith concept with overlapping polysilicon gate electrodes (triple poly)



Scientific CCDs: front vs back illumination

Front illumination: Quantum efficiency loss from absorption in polysilicon gates
Reflections from complicated thin film stack

Poly gate electrodes

n buried channel

p- epi (20 to 50 Ω-cm)

photosensitive volume (≈20 μm)

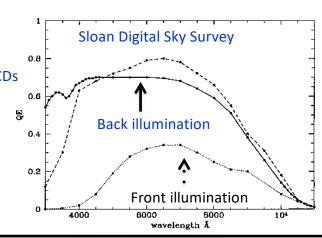
Back illumination of thinned CCDs

Remove p+ substrate

http://www.astro.princeton.edu/PBOOK/camera/camera.htm

To overcome the problem of charge losses, the "buried channel" CCD (BCCD) has been developed.

An n-doping region shifts the electrons energy minimum from to the surface into the bulk



Scientific CCDs for Astronomy

Scientific charge-coupled devices are the detector of choice for astronomy

Wavelength range: $\lambda \sim 350$ nm to 1100 nm (from atmospheric cutoff to Silicon bandagap) \rightarrow UV, visible and near-infrared wavelengths

Back illuminated: for high QE → up to 90% at peak

Slow readout for low noise: less than 5 e- at 100 kpixels/s readout

Cryogenically cooled for low dark current: for -100° C < t < -140° C few e-/pixel/hour

Quite expensive (10MPixel ~ 100k€)

In the following some examples of astronomy cameras

LSST: Large Synoptic Survey Telescope



The Large Synoptic Survey Telescope (LSST) is a planned wide-field "survey" telescope

It photographs the entire available sky every few nights The telescope is located in northern Chile Science first light in 2025 (this year!)

Some of the LSST Physics Goals:

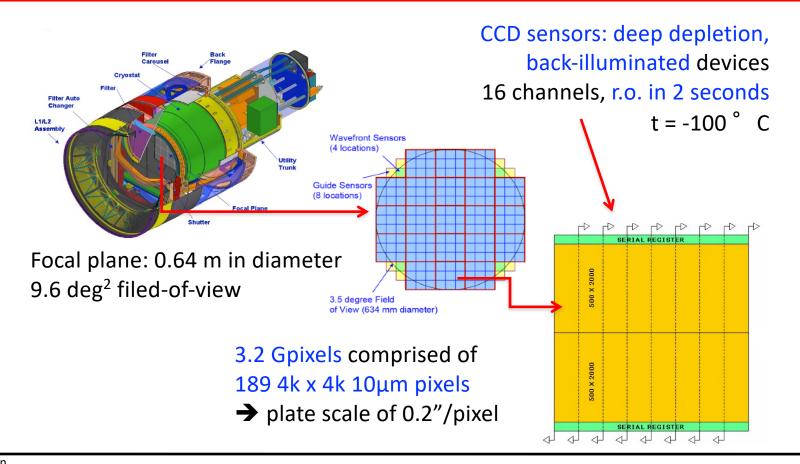
Measure gravitational lensing for DE/DM detection Map small objects in Solar System (Super)Novæ detection Milky Way mapping



LSST Science Book http://arxiv.org/pdf/0912.0201v1.pdf

LSST camera and CCDs







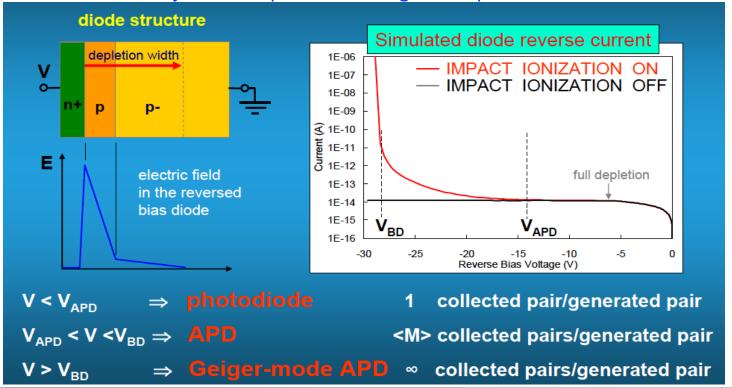




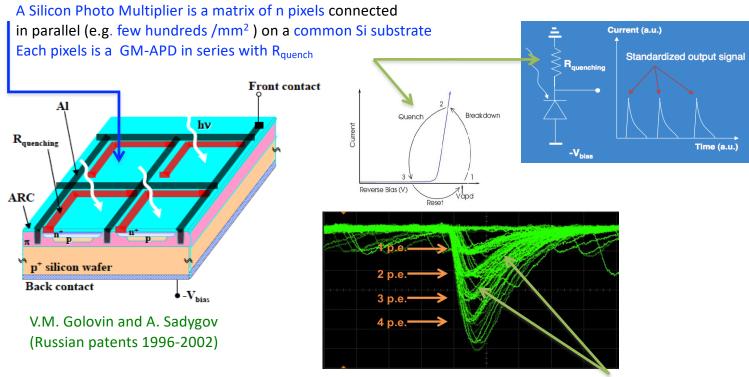
This image combines 678 separate images taken by NSF-DOE Vera C. Rubin Observatory in just over seven hours of observing time. Combining many images in this way clearly reveals otherwise faint or invisible details, such as the clouds of gas and dust that comprise the Trifid nebula (top right) and the Lagoon nebula, which are several thousand light-years away from Earth. © NSF-DOE Vera C. Rubin Observatory

Avalanche Photo Diodes (APDs)

The avalanche photodiode (APD): p-n device with internal gain due to the high internal field at the junction of positive and negative doped silicon



Silicon Photo Multiplier (SiPM)



A single GM-APD gives no information about light intensity → in a SiPM the output charge is proportional to the number of triggered cells, that is (for PDE = 1) the number of photons

SiPM features

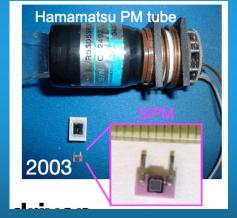
The characteristics of a SiPM are:

- possibility to detect single photons and give a signal proportional to the number of photons for low fluxes;
- extremely fast response (determined by avalanche spreading):

in the order of few hundreds of ps.

Other features are:

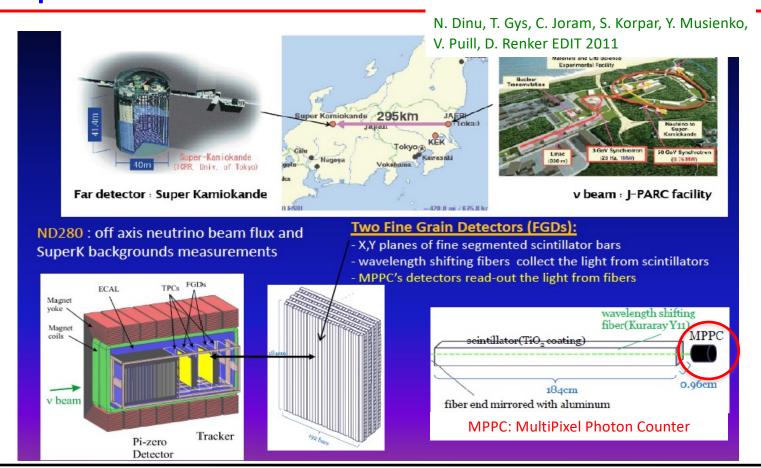
- Low bias voltage (20-60V)
- Low power consumption
- Insensitive to magnetic fields
- Compact and rugged



Possible applications are: scintillator read-out, PET, photon correlation studies, calorimetry...)

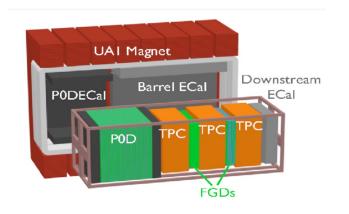
Example: T2K ND280

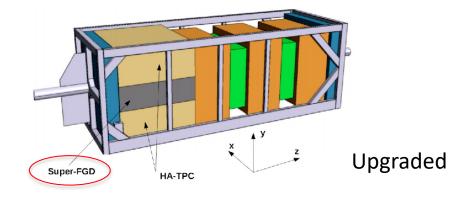
T2K: Measure v_{μ} disappearance and v_{e} appearance



Example: T2K ND280

UPGRADED NEAR DETECTOR ND280: CONFIGURATION



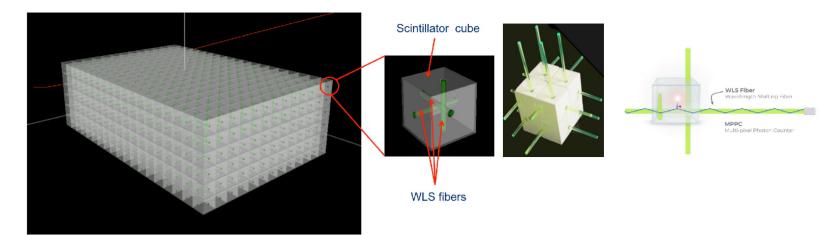


- 2 new High Angle TPC (HA-TPC)
- New Time Of Flight detector (TOF)
- 1 Super-fine-grained-detector (super-FGD) => the core of the detector where the LLR is involved

NGUYEN Quoc Viet 7

Example: T2K ND280

SUPER FGD DETECTOR



• Super-FGD: 192 \times 192 \times 56 scintillator cubes (2 million) with 3D readout => 2 tons of fully active target

- ·Wavelength shifting (WLS) fibers are used to collect light from scintillator cubes. (70 km of WLS fiber in total)
- •One end of the fibers is connected to a Multi-Pixel Photon Counter (MPPC) the other end is mirrored. => around 60.000 channels.

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105

Outline

Main applications, motivations and history

- Semiconductors physics
- Silicon radiation detectors

Timing with silicon detectors

Perspectives

Time resolution of silicon sensors

Werner Riegler, CERN, werner.riegler@cern.ch October 15, 2021

W. Riegler, CERN seminar

Abstract

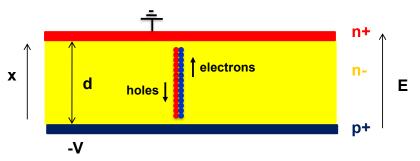
Precision timing with solid state detectors is being employed in many areas of particle physics instrumentation. Applications for pileup rejection and time of flight measurements at the LHC are just two of many notable examples.

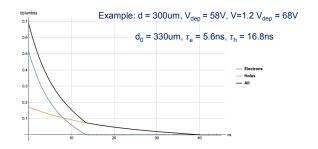
During the past years the principal contributions to the time resolution for various types of silicon sensors have been studied. The principal contributors to the time resolution are Landau fluctuations, electronics noise, signal shape fluctuations due to a varying pad response function as well as gain fluctuations.

We discuss silicon pad and silicon pixel sensors, LGAD sensors as well as SPADs and SiPMs. These sensors have been simulated using the Garfield++ toolkit. The analytic statistical analysis of the contributions to the time resolution has been performed, resulting in elementary expressions for the timing performance of these sensors. These expressions show the basic directions for optimization of these sensors as well as the fundamental limits to the time resolution.

Time resolution of silicon sensors W. Riegler, CERN seminar

Intrinsic time resolution of a 'large' silicon pad detector





In silicon sensors the signal edge is instantaneous (i.e. sub ps level)

- acceleration of electrons to 10⁷cm/s in vacuum is 0.14ps
- passage of the particle through a 50um sensor takes 0.16ps

In Wire Chambers the electrons first have to move to the wires before an avalanche at the wire leads to an appreciable signal → intrinsic resolution limit.

In RPCs the avalanche starts instantly, but it still takes some time until the signal reaches the threshold → intrinsic resolution limit.

- → The intrinsic time resolution of a silicon sensor is infinite (sub ps).
- → The time resolution in a planar silicon sensor without gain is a question of signal/noise/electronics and specifically the Landau fluctuations within the electronics integration time.

Electronics processing of a detector signal

Signal duration of T i.e. f(t) = 0 for t>T

Electronics peaking time t_p >> T

We are interested in times t>T

$$v(t) = \int_{0}^{t} h(t - t') f(t') dt'$$

$$\approx \int_{0}^{T} [h(t) - h'(t)t'] f(t') dt'$$

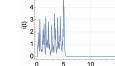
$$= h(t) \int_{0}^{T} f(t') dt' - h'(t) \int_{0}^{T} t' f(t') dt'$$

$$= \int_{0}^{T} f(t') dt' \left[h(t) - h'(t) \frac{\int_{0}^{T} t' f(t') dt'}{\int_{0}^{T} f(t') dt'} \right]$$

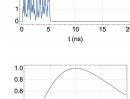
$$= q [h(t) - h'(t) t_{cog}]$$

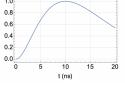
$$= q h(t - t_{cog})$$

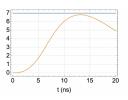
In case the electronics peaking time $t_{\text{\tiny p}}$ is longer than the signal duration T, the electronics output signal has



- the same shape as the delta response
- a pulse-height equal to the total charge of the signal
- a 'time displacement' of this delta response by the center of gravity time t_{cog} of the signal.
- → An amplifier that is 'slower' than the signal measures the center of gravity time of the signal



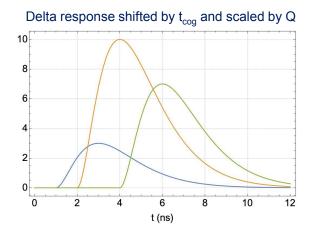




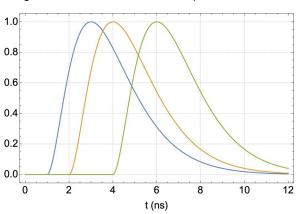
$$q = \int_0^T f(t')dt'$$
 $t_{cog} = \frac{\int_0^T t'f(t')dt'}{\int_0^T f(t')dt'} = \frac{1}{q}\int_0^T t'f(t')dt'$

W. Riegler, CERN seminar

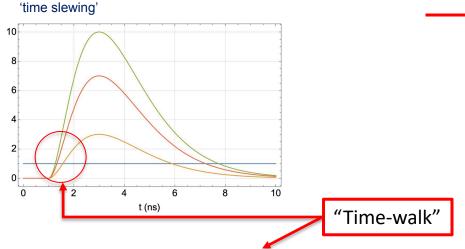
Electronics 'slower' than the detector signal, time slewing



Signal normalized to same amplitude → time



10/21/2021



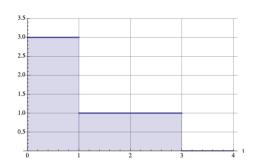
There are many different ways to correct for this slewing effect

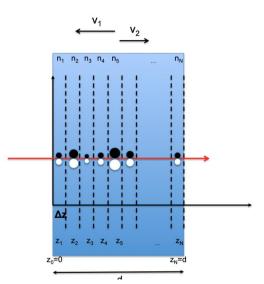
- Constant Fraction discrimination
- Standard discrimination using time over threshold to correct for pulse-height
- · Standard discrimination + pulseheight to correct for pulse-height
- Standard discrimination + total charge to correct for pulse-height
- Multiple sampling and 'fitting' the know signal shape
- ..

→ What is the c.o.g. time resolution of a silicon sensor?

W. Riegler, CERN seminar

Center of gravity time of a silicon detector signal





Single e-h pair

$$i(t) = -\frac{qv_1}{d}\Theta(z/v_1 - t) - \frac{qv_2}{d}\Theta((d - z)/v_2 - t)$$
(4.1)

with $\Theta(t)$ being the Heaviside step function. An example is shown in figure 3b. We have $\int i(t)dt =$ -q and according to eq. (3.1) the centroid time of this signal is then

$$\tau = \frac{1}{2d} \left[\frac{z^2}{v_1} + \frac{(d-z)^2}{v_2} \right] \tag{4.2}$$

If n_1, n_2, \ldots, n_N charges are produced at positions z_1, z_2, \ldots, z_N and are moving to the electrodes with v_1 and v_2 , the resulting centroid time of the signal is

$$\tau(n_1, n_2, \dots, n_N) = \frac{1}{2d\left(\sum_{k=1}^N n_k\right)} \sum_{k=1}^N n_k \left[\frac{z_k^2}{v_1} + \frac{(d - z_k)^2}{v_2} \right]$$
(4.3)

We now divide the sensor of thickness d into N slices of $\Delta z = d/N$ as shown in figure 1. The probability to have n_k e/h pairs in slice k is given by the Landau distribution $p(n_k, \Delta z)$ and if we

After some lengthy evaluation:

$$\Delta_{\tau}^2 = \overline{\tau^2} - \overline{\tau}^2 \tag{4.4}$$

with $\overline{\tau}$ and $\overline{\tau^2}$ being the average and the second moment of τ . The evaluation is given in B and we find

$$\Delta_{\tau} = w(d) \sqrt{\frac{4}{180} \frac{d^2}{v_1^2} - \frac{7}{180} \frac{d^2}{v_1 v_2} + \frac{4}{180} \frac{d^2}{v_2^2}}$$

$$w(d)^2 = \frac{d}{\lambda} \int_0^{\infty} \left[\int_0^{\infty} \frac{n_1^2 p_{\text{clu}}(n_1)}{(n_1 + n)^2} dn_1 \right] p(n, d) dn$$

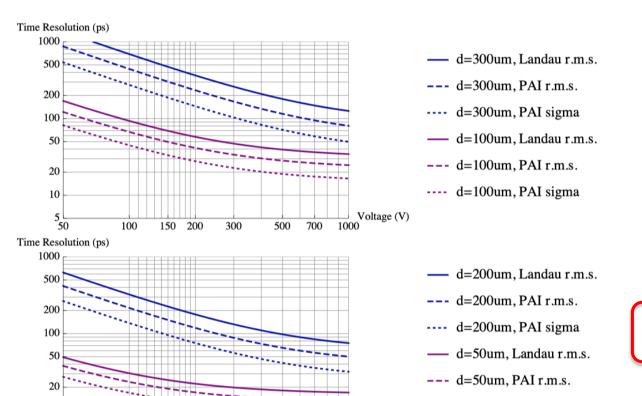
with

$$w(d)^{2} = \frac{d}{\lambda} \int_{0}^{\infty} \left[\int_{0}^{\infty} \frac{n_{1}^{2} p_{\text{clu}}(n_{1})}{(n_{1} + n)^{2}} dn_{1} \right] p(n, d) dn$$

(4.6)

W. Riegler, CERN seminar

Center of gravity time resolution for silicon sensors



700

1000

10

5 50

100

150 200

300

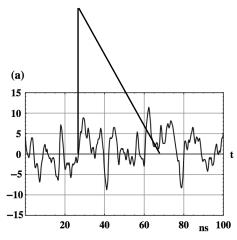
50um sensor, 10ps

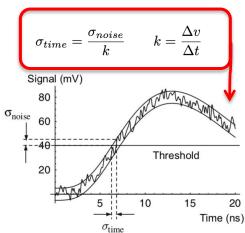
W. Riegler, CERN seminar

Marco Bomben 112

Voltage (V)

d=50um, PAI sigma





Noise and Optimum filters

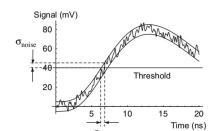
Let us assume we have a signal f(t) with superimposed noise of a given noise power spectrum and we want to find the amplifier transfer function that maximizes

- the signal to noise ratio for the best amplitude measurement, or
- the slope to noise ratio for the best time measurement
- → Theory of optimum filters

W. Riegler, Detector Signals

W. Riegler, CERN seminar

Optimum filter for best slope to noise ratio



$$\sigma_{time} = rac{\sigma_{noise}}{k} \qquad k = rac{\Delta v}{\Delta t}$$

We want to minimise the time resolution i.e. maximise the slope to noise

$$\left(\frac{k}{\sigma}\right)^2 = \left(\frac{g'(t_m)}{\sigma}\right)^2 = \frac{1}{\pi} \frac{\left(\int_{-\infty}^{\infty} i\omega F(i\omega) H(i\omega) e^{i\omega t_m} d\omega\right)^2}{\int_{-\infty}^{\infty} w(\omega) |H(i\omega)|^2 d\omega}.$$

Following the steps from before we find an upper bound for the slope to noise ratio of

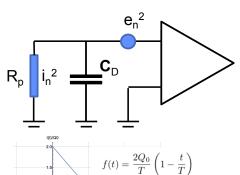
$$\left(rac{k}{\sigma}
ight)^2 \leq rac{2}{\pi} \int_0^\infty rac{|\omega F(i\omega)|^2}{w(\omega)} \, d\omega$$

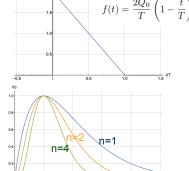
And the optimum transfer function as well as the output signal are

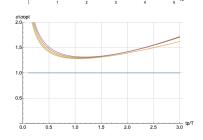
$$H(i\omega)=i\omegarac{F^*(i\omega)}{w(\omega)}\,e^{-i\omega t_m} \qquad G(i\omega)=i\omegarac{|F(i\omega)|^2}{w(\omega)}e^{-it_m\omega}.$$

Since multiplication with $i\omega$ refers to the derivative in the time domain we have the following relation:

The filter maximising the slope to noise ratio, i.e. the filter giving the best time resolution, is equal to the time derivative of the filter that maximises the signal to noise ratio!







Realistic preamp transfer function

Preamp delta response

$$h(t) = e^n n^{-n} \left(\frac{nt}{t_p}\right)^n e^{-nt/t_p} \qquad H(i\omega) = \frac{t_p e^n n!}{(n + i\omega t_p)^{n+1}}$$

For the noise we assume series noise and parallel noise together with a detector capacitance C_D

$$\sigma^{2}(t_{p}) = \frac{1}{2\pi} \int_{0}^{\infty} w(\omega) |H(i\omega)|^{2} d\omega = a^{2} K_{p} t_{p} + b^{2} \frac{K_{s}}{t_{p}}$$

$$K_{p} = \frac{1}{2} \left(\frac{e}{2n}\right)^{2n} (2n - 1)!$$

$$K_{s} = \frac{1}{2} \left(\frac{e}{2n}\right)^{2n} n^{2} (2n - 2)!$$

The output signal is

$$g(t) = \int_0^t h(t - t')g(t')dt'$$

And the maximum slope evaluates to

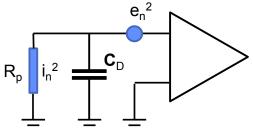
$$k(t_p) = \frac{2Q_0}{T^2} \frac{e^n}{n^{n+1}} \left(e^{-nt/t_p} nT (nt/t_p)^n - t_p n! + t_p \Gamma(n+1, nt/t_p) \right)$$

$$\lim_{t_p \to 0} k(t_p) = \frac{2Q_0}{T}$$

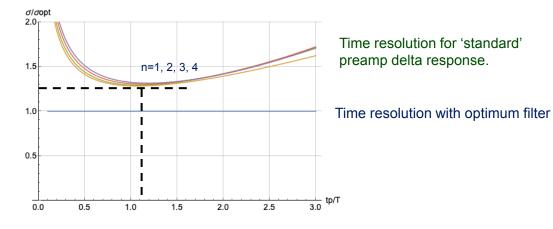
To find the optimum peaking time and best time resolution we therefore have to minimise the function

$$\frac{\sigma(t_p)^2}{k(tp)^2} \rightarrow min$$

W. Riegler, CERN seminar



Realistic preamp transfer function



 $f(t) = \frac{2Q_0}{T} \left(1 - \frac{t}{T}\right)$

Neglecting parallel noise (which is a good approximation in most practical applications) the optimum electronics peaking time t_p is between T and 1.5T.

The achieved time resolution is only about 30% worse than the best achievable one with the optimum filter!

This will give the smallest noise contribution to the time resolution.

W. Riegler, CERN seminar

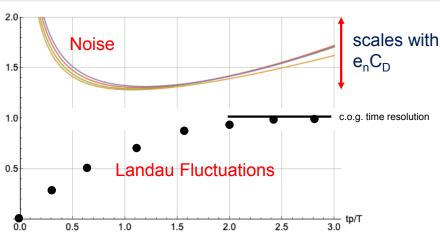
Combined effect of Landau fluctuations and noise

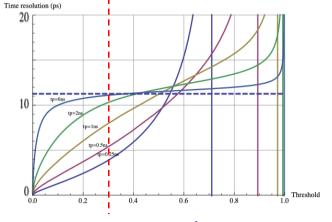
If the noise dominates, the optimum peaking time is about $t_p \sim 1-1.5T$

If the noise is at a similar level to the contribution from Landau fluctuations, the optimum peaking time is still around the same level $t_p \sim 1-1.5T$ and the time resolution is equal to the the c.o.g. time resolution of the silicon sensor.

If the noise is subdominant, shorter peaking times can be improve the time resolution, but with the divergence of the noise contribution at low t_{D} this will not reach far below the c.o.g. time resolution.

In short: $t_p \sim T$ and $\sigma = \sigma_{c.o.q.} \oplus \sigma_{noise}$ give a good order of magnitude for the achievable time resolution





Landau Fluctuations ⊕ Noise

W. Riegler, CERN seminar

Time resolution of 'standard' silicon sensors

In case noise is not dominant, the time resolution of a silicon sensor is somewhere between zero and the c.o.g. time resolution.

For a silicon detector signal with total duration T, the series noise contribution is minimised for amplifiers of $t_n \sim T$.

For very low noise a time resolution better than the c.o.g. time resolution can be achieved, but the divergence of the noise contribution for $t_p \to 0$ will limit this improvement.

$$\Delta_{\tau} = w(d) \sqrt{\frac{4}{180} \frac{d^2}{v_1^2} - \frac{7}{180} \frac{d^2}{v_1 v_2} + \frac{4}{180} \frac{d^2}{v_2^2}}$$

$$w(d)^{2} = \frac{d}{\lambda} \int_{0}^{\infty} \left[\int_{0}^{\infty} \frac{n_{1}^{2} p_{\text{clu}}(n_{1})}{(n_{1} + n)^{2}} dn_{1} \right] p(n, d) dn$$

W. Riegler, CERN seminar

Time resolution of 'standard' silicon sensors

No time di discuss segmented sensors...

Good time resolution demands thin sensors.

Thin sensors give small charge and large capacitance i.e. unfavorable S/N and k/N.

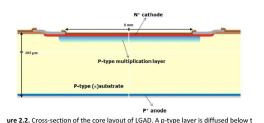
Capacitance can be reduced by making the pixels small.

If the pixel size is in the same order as the sensor thickness, the weighting field fluctuations start to dominate ... and there will be many channels ...

- ... between a rock and a hard place ...
- → Sensors with internal gain to overcome the noise limit (like gas detectors!)
- → Turn the by sensor 90 degrees and realise a parallel plate geometry in 3D! (see slide 62, 63)

W. Riegler, CERN seminar

Avalanche Photo Diode, Low Gain Avalanche Diode



Idea goes back to the 1960ies.

A high field region is implemented in a silicon sensor by doping.

Electrons will produce an avalanche in this high field region.

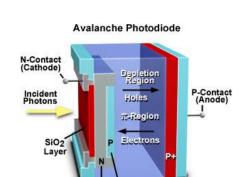
The high field region is implemented by doping and related 'space-charge' in the volume.

The sensor is operated in a region where there is electron multiplication but not yet hole multiplication.

This allows to have thin sensors (high field, short signal) but still have enough signal charge to overcome the limitation from noise.

For higher fields → electron+hole multiplication → avalanche divergence → guench resistor → SiPM





N-Layer P-Layer

Figure 1

IEEE TRANSACTIONS ON ELECTRON DEVICES, JUNE 1972





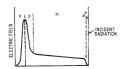
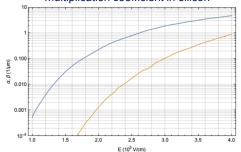


Fig. 1. Sketeches of reach-through avalanche-diode structure impurity-concentration profile, and electric-field distribution.

Electron (alpha) and hole (beta) multiplication coefficient in silicon



10/0/10

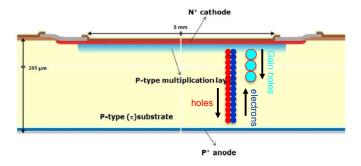
Cianala in Dartiala Datastara III Disalar/CEDNI

AvalanchePhotoDiode

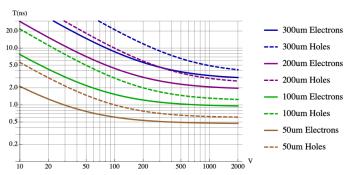
Nuclear Instruments and Methods in Physics Research A 796 (2015) 141-148

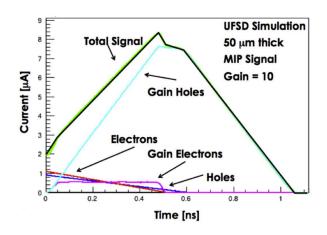
Design optimization of ultra-fast silicon detectors

N. Cartiglia ^{a,e}, R. Arcidiacono ^c, M. Baselga ^e, R. Bellan ^b, M. Boscardin ^f, F. Cenna ^a, G.F. Dalla Betta ^g, P. Fernndez-Martnez ^e, M. Ferrero ^{a,b}, D. Flores ^e, Z. Galloway ^d, V. Greco ^e, S. Hiddago ^e, F. Marchetto ^a, V. Monaco ^b, M. Obertino ^c, L. Pancheri ^g, G. Paternoster ^f, A. Picerno ^b, G. Pellegrini ^e, D. Quirion ^e, F. Ravera ^b, R. Sacchi ^b, H.F.-W. Sadrozinski ^d, A. Seiden ^d, A. Solano ^b, N. Spencer ^d



Total drift time for a given sensor thickness





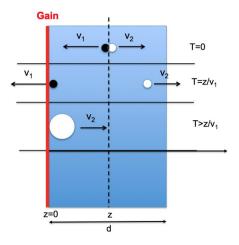
A high field region is implemented in a silicon sensor by doping.

Electrons will produce an avalanche in this high field region.

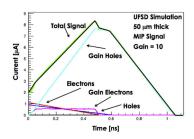
W. Riegler, CERN seminar

12/2/19

LGAD



$$w(d)^{2} = \frac{d}{\lambda} \int_{0}^{\infty} \left[\int_{0}^{\infty} \frac{n_{1}^{2} p_{\text{clu}}(n_{1})}{(n_{1} + n)^{2}} dn_{1} \right] p(n, d) dn$$



An e-h pair is produced at position z.

The electron arrives at z=0 at time $T=z/v_1$.

The electron multiplies in the high field in the layer at z=0 (infinitely thin).

The holes move back to z=d inducing the dominant part of the signal (all in this approximation).

Centroid time resolution for standard silicon sensor:

$$\Delta_{\tau} = w(d) \sqrt{\frac{4}{180} \frac{d^2}{v_1^2} - \frac{7}{180} \frac{d^2}{v_1 v_2} + \frac{4}{180} \frac{d^2}{v_2^2}}$$

Centroid time resolution for LGAD

$$\Delta_{\tau} = w(d) \, \frac{d}{\sqrt{12} v_1}$$

The signal is now defined by the arrival time distribution of the electrons at the gain layer.

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LGAD

LGAD centroid time resolution

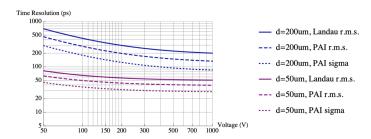


Figure 22. Time resolution for the centroid time from eq. (5.4) for 50, 100, 200, 300 μ m silicon sensors with internal gain of electrons, assuming a signal only from gain holes. The three curves for each sensor thickness correspond to the Landau theory, the PAI model and a Gaussian fit to the PAI model.

50um sensor at 200V: 30ps

200um sensor at 200V: 140ps

Standard silicon sensor centroid time resolution

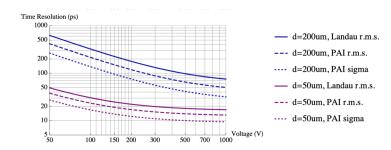


Figure 6. Time resolution from eq. (4.5) for different values of silicon sensor thickness as a function of applied voltage V for the Landau model, the PAI model and a Gaussian fit to the PAI model results.

50um sensor at 200V: 13ps

200um sensor at 200V: 70ps

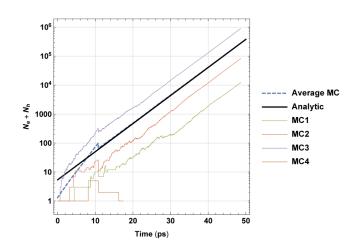
The c.o.g. time resolution of LGADs is worse than the one for standard silicon sensors due to the very different signal characteristics – essentially an electron arrival time distribution.

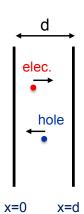
Of course – the fact that the signal is larger by a factor 10-15 allows much more relaxed noise requirements, larger pixels etc. ...

For very large electric fields, also the holes start to contribute to the avalanche.

 α dx = probability for an electron to produce an additional e-h pair along a distance dx

 β dx = probability for a hole to produce an additional e-h pair along a distance dx



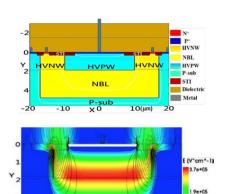




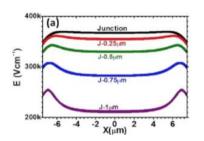


SIMULATION OF ELECTRIC FIELD DISTRIBUTION IN CMOS SINGLE PHOTON AVALANCHE DIODES AT BREAKDOWN VOLTAGE

<u>Jau-Yang Wu</u> and Sheng-Di Lin
Department of Electronics Engineering, National Chiao Tung University, Hsinchu, Taiwan
E-mail: judevu.ee95g@nctu.edu.tw



10 (µm)

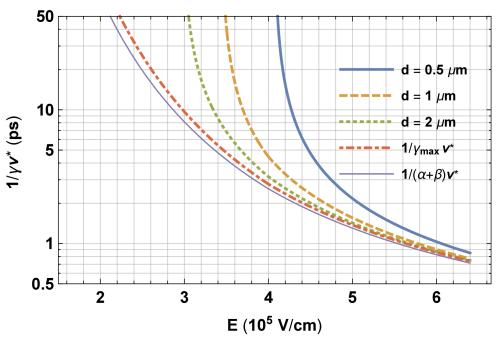


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Time resolution aSPAD

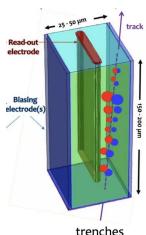
Approximate r.m.s. SPAD time resolution 1/γv*

<10ps is in the cards ...



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3D sensor realising a parallel plate geometry, TimeSPOT



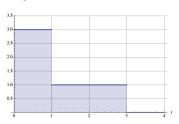
Total charge from the 200um sensor but timing characteristics from a 25um sensor!

L. Anderlini et al., *Intrinsic time resolution* of 3D-trench silicon pixels for charged particle detection. JINST 15, P09029, 2020.

D. Brundu et al., Accurate modelling of 3D-trench silicon sensor with enhanced timing performance and comparison with test beam measurements. JINST 16, P09028. 2021.

For a perfectly perpendicular track: 'box' signals from electrons and holes.

Landau fluctuations affect just the total pulseheight, which can be corrected.



$$i(t) = -\frac{qv_1}{d}\Theta(z/v_1 - t) - \frac{qv_2}{d}\Theta((d-z)/v_2 - t)$$

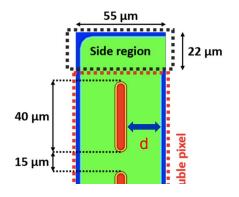
c.o.g. time of the signal

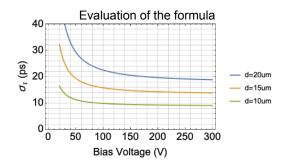
$$\tau(z) = \frac{1}{2d} \left(\frac{z^2}{v_e} + \frac{(d-z)^2}{v_h} \right)$$

Variance of the c.o.g. Time for uniform distribution of tracks

$$\overline{ au} = rac{1}{d} \int_0^d au(z) dz \qquad \overline{ au^2} = rac{1}{d} \int_0^d au(z)^2 dz$$

$$\sigma_{\tau} = \sqrt{\overline{\tau^2} - \overline{\tau}^2} = \sqrt{\frac{4}{180} \frac{d^2}{v_e^2} - \frac{7}{180} \frac{d^2}{v_e v_h} + \frac{4}{180} \frac{d^2}{v_h^2}}$$





→ 10-20ps achievable and indeed achieved!

10/21/2021

W. Riegler, CERN seminar

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Outline

Main applications, motivations and history

Semiconductors physics

Silicon radiation detectors

Timing with silicon detectors

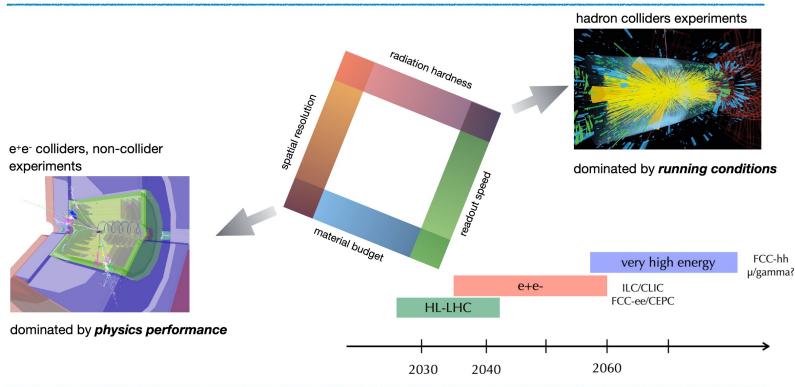
Perspectives

Perspectives ... but already here

New detector development

application driven

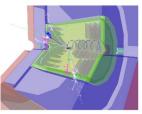




Challenges

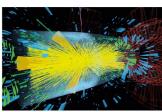
the challenges

e+e- colliders, non-collider



dominated by physics performance

hadron colliders



dominated by running conditions

	Lepton Colliders	(HL-) LHC (ATLAS/CMS)
Material budget	< 1% X ₀	10% X ₀ * 2% for ALICE
Single-point resolution	≤ 3 µm	~ 15µm
Time resolution	~ ps – ns	25ns
Granularity	≤ 25 µm x 25 µm	50μm x 50μm
Radiation tolerance	$< 10^{11} \rm n_{eq} / cm^2$	O(10 ¹⁶ n _{eq} / cm ²)
Max. hit rate	20 MHz / cm ²	2-4 GHz / cm ² *)

Survival optimisation

Performance optimisation

*) max. output rate for LHCb

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CMOS Monolithic Active Pixel Sensors

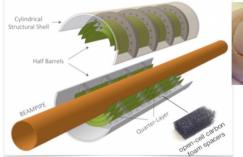
sensor and readout elements all-in-one

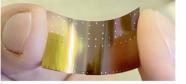
Monolithic Detectors

CMOS MAPS for ALICE ITS3 (Run 4):

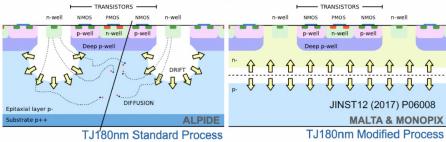
(LOI: CERN-LHCC-2019-018, M. Mager)

- Three fully cylindrical, wafer-sized layers based on curved ultra-thin sensors (20-40 µm), air flow cooling
- Very low mass, < 0.02-0.04% per layer





Radiation hardness of MAPS: From ALPIDE to MALTA/Monopix with modified Tower Jazz 180 nm process



 \rightarrow Up to 97% efficiency after fluence of 1×10¹⁵ n_{eg}/cm²

New CMOS TPSCo 65 nm technology

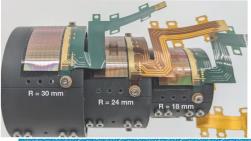
Validated on Digital and Analog Pixel Test Structures up to 10¹⁵ cm⁻² and 100 kGy

Currently testing **stitching** for wafer scale sensors (now 26 x 1.4 cm²)

A. Kotliarov

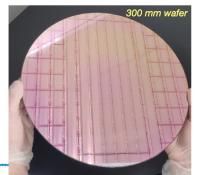
→ Efficiency > 99.9% independent on bending radius

Erika.Garutti @ uni-hamburg.de

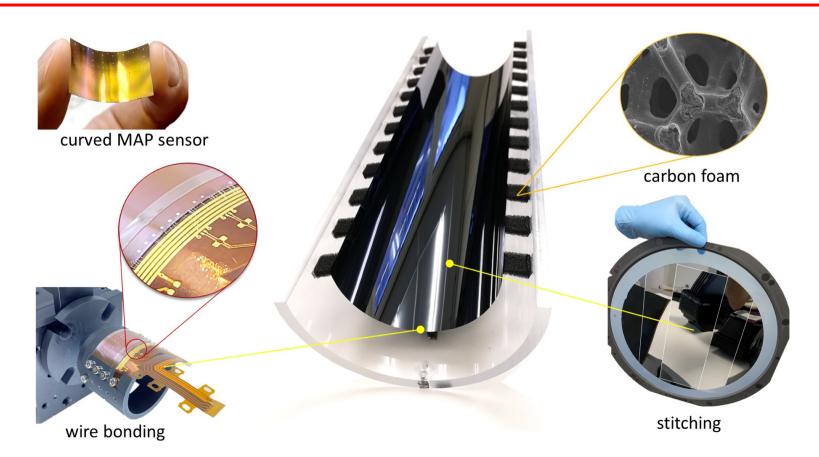


EPS - HEP2023

Hamburg, August 2023



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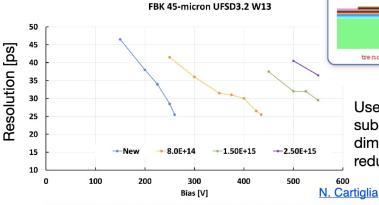
Low Gain Avalange Detectors

fast timing

Hybrid Detectors

Sensors for 4D-Tracking:

- Position resolution: ~ 10 μm
 ~ 5% of electrodes distance
- Time resolution: ~ 25 ps for 50 μm sensors
- Radiation Hardness up to
 ~ 2 x 10¹⁵ cm⁻²



LGAD: Fill factor & performance improvements



Two opposing requirements:

Trench Isolation LGAD

Use Carbon enriched

substrates (C helps to

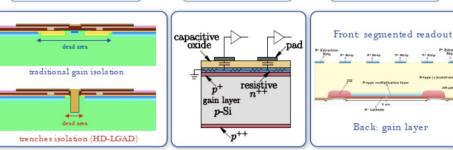
diminish the effect of gain

reduction with irradiation)

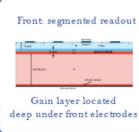
- Good timing reconstruction needs homogeneous signal (i.e. no dead areas and homogeneous weighting field)
- · A pixel-border termination is necessary to host all structures controlling the electric field

AC-LGAD

Several new approaches to optimize/mitigate followed:



Deep Junction LGAD



Concepts simulated, designed, produced and tested in 2018/19

..new concept 2020

Ongoing:

Improve fill factor and signal homogeneity

Invers LGAD

Next employed in ATLAS / CMS fast timing layers

EPS - HEP2023 Marco Rambban August 2023

Erika.Garutti @ uni-hamburg.de

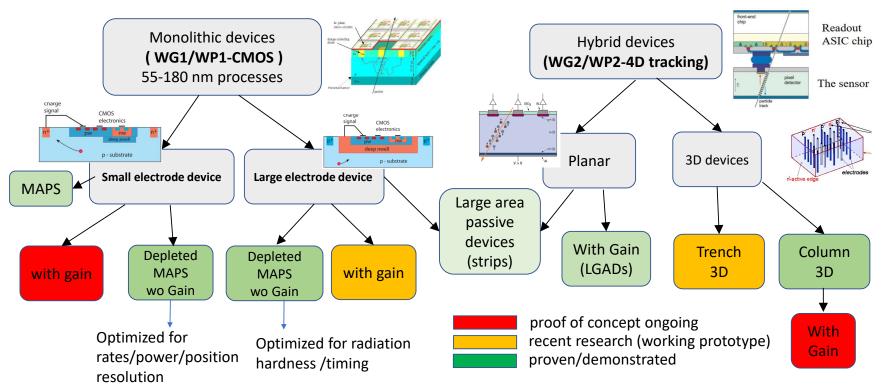
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Paths of present silicon sensor R&D DRD3







WG3,6/WP3 extreme fluence and WBS



Improve the radiation hardness of the semiconductor detectors and exploitation of the benefits of WGS for particle physics

Projects running, proposal draft submitted (work ongoing), proposals in preparation (work ongoing):

- Understanding silicon at extreme fluences (devices developed with in WP2)
 - Radiation damage in Si PiN and LGAD sensors
 - Many RD50 projects running on the radiation hardness
- Wide-Bandgap-Semiconductors
 - SiC LGAD Detector (one running one in preparation)
 - Development of radiation-hard GaN devices for MIP detection
 - Radiation hardness of 25um 3D diamond detectors.
 - Graphene/SiC Detector

Main challenges and developments:

Silicon at extreme fluences:

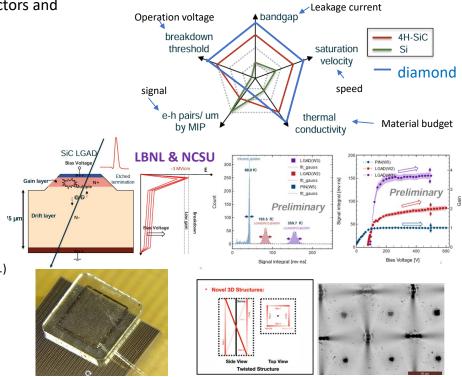
- understanding material properties (impact ionization, mobility, trapping...)
- understanding the operation

SiC/GaN

- understanding the material properties defects formation
- processing of large device SiC-LGADs

Diamond:

- scalability of 3D column processing
- availability of high quality large diameter wafers



G. Kramberger, DRD3 collaboration, DRD Jamboree, CERN

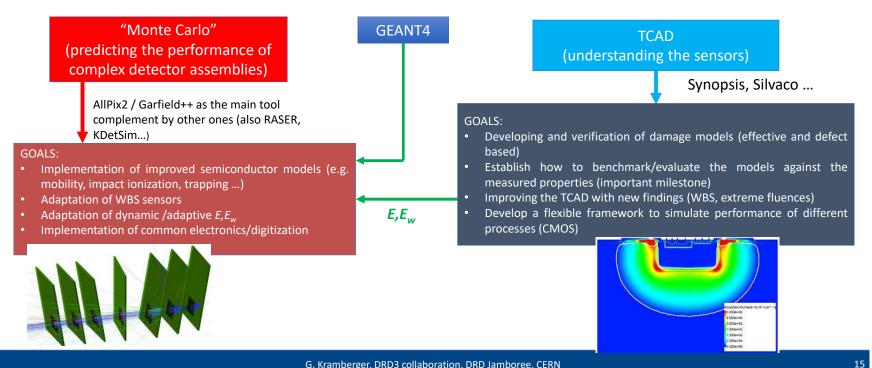


https://indico.cern.ch/event/1552124/

WG 4: Simulations



Simulations are essential for planning, understanding the performance and designing of devices. Aim to develop tools that could be (easily) implemented to simulate any specific detector or measurement.

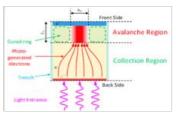


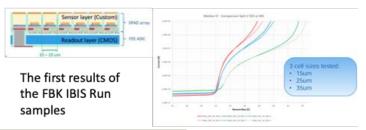
WP1: Solid-State Photodetectors

Examples of ongoing activities

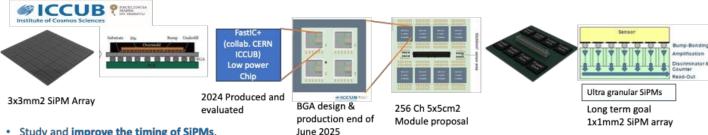
Backside illuminated (BSI) SiPMs: potential for an enhanced PDE and a better radiation tolerance.







Timing of SSPD & Developing ultra-granular SIPM that integrates with the readout electronics



- Study and improve the timing of SiPMs.
- Optimised, reliable, cost-effective integration and packaging with integrated cooling.
- Vertical integration of SiPM arrays to FEE: optimise timing by reducing the interconnections' parasitic inductances and capacitances.

https://indico.cern.ch/event/1552124/

Take home message

- Semiconductors are excellent for tracking and spectroscopy
- Energy to create charge carrier is 10x lower than gas
 - → large signals without amplification and
 - → less material hence better vertex/tracking resolution
- No need for container
- μ-electronics development helped to have finest segmentation and electronics readout
- Fast signal collection is possible → timing applications
- Main limitations are cost and ageing (radiation damage)
- Towards 5D measurements (no time to talk about calorimetry...)



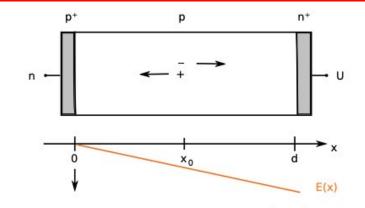
THANK YOU FOR YOUR ATTENTION!

Backup

Signal from uniform deposition in a real diode

more realistic treatment: E-field depends on x

simple ansatz:
$$|\vec{E}| = \frac{e \, N_A}{\epsilon \epsilon_0} \cdot x$$
 and with $\sigma = \frac{1}{\rho} = e \, N_A \, \mu_+$ and $\tau = \frac{\epsilon \epsilon_0}{\sigma}$ $|\vec{E}| = \frac{x}{\mu_+ \tau} \qquad (\tau \cong 1 \text{ ns})$



for an electron generated at location x inside depletion zone and mobilities independent of E:

total drift time of electrons:

charge signal for
$$t < t_d$$

analogously for hole

$$v_{-} = -\mu_{-}E = \frac{\mu_{-}}{\mu_{+}} \frac{x}{\tau} \quad \Rightarrow \quad x = x_{0} \exp\left(\frac{\mu_{-}t}{\mu_{+}\tau}\right)$$

$$t_{d} = \tau \frac{\mu_{+}}{\mu_{-}} \ln\left(\frac{d}{x_{0}}\right)$$

$$Q_{-}(t) = -\frac{e}{d} \int \frac{dx}{dt} dt = \frac{e}{d} x_{0} \left(1 - \exp\left(\frac{\mu_{-}t}{\mu_{+}\tau}\right)\right)$$

$$v_{+} = \mu_{+}E = -\frac{x}{\tau} \quad \Rightarrow \quad x = x_{0} \exp\left(-t/\tau\right)$$

$$Q_{+}(t) = -\frac{e}{d} x_{0} \left(1 - \exp\left(-t/\tau\right)\right)$$

July 23, 2018

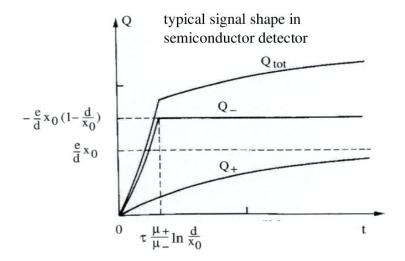
Total charge

Total charge signal:

$$Q_-(t_d)+Q_+(t o\infty)=-e$$

signal rise time essentially determined by

$$\tau = \rho \cdot \epsilon \cdot \epsilon_0$$

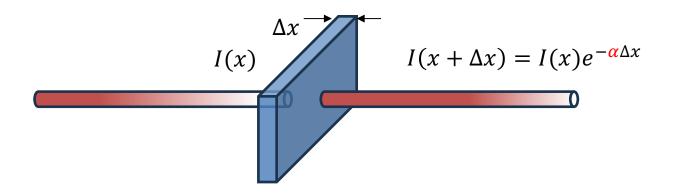


in reality a bit more complicated:

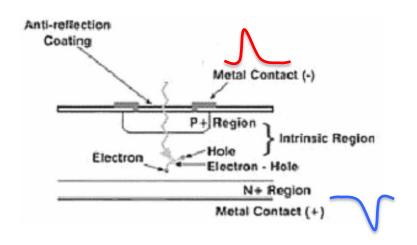
- track not exactly a line charge (distributed over typically 50 μm width)
- $\mu_{\pm} \neq \text{constant}$
- some loss of charges due to recombination at impurities for Si $\tau=\rho\cdot 10^{-12}$ s (ρ in Ω cm), $\rho=1000~\Omega$ cm $\to \tau=1$ ns

July 23, 2018

Absorption coefficient



Silicon PIN photodiode



A piece of intrinsic high-ohmic silicon

Sandwiched between two heavily doped n+ and p+ regions

- ✓ Thick bulk: low capacitance (less noise) + sensible to longer wavelengths
- ✓ Undoped bulk: low depletion voltage; longer generation/recombination lifetime → small charge losses, low leakage current

HPGe

4.5.4 High purity or intrinsic Ge detectors

from late 1970ies

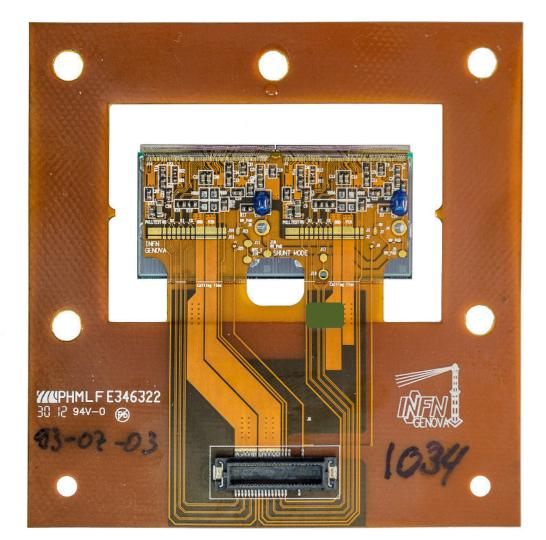
similar to Li doped Ge or Si detectors, but dark current is kept low not by compensating impurities, but by making material very clean itself

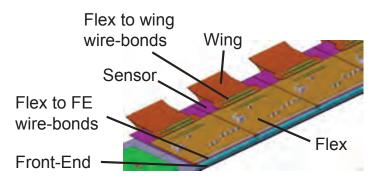
by repeating the purification process (zone melting), extremely pure Ge can be obtained ($\leq 10^9$ impurity atoms per cm³) intrinsic layer like compensated zone in Ge(Li), similar sizes possible advantage: cooling only needed during use to reduce noise

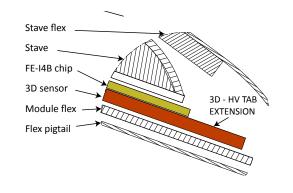
other applications

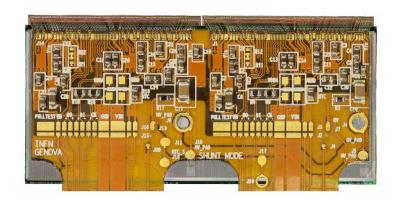
- low energy electrons
- strongly ionizing particles
- dE/dx for particle identification

useful energy range determined by range of particle vs. size of detector

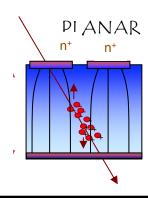


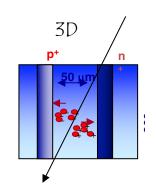








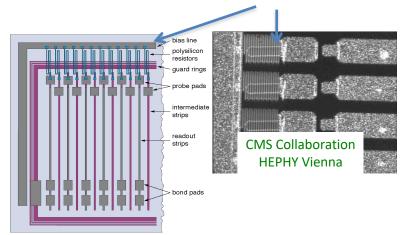




Biasing circuits

For an AC-coupled a DC path must be provided for the strip leakage currents

Two possible methods: via a resistor or by the punch-through method



a)

undepleted

undepleted

Atlas, TU Dortmund & MPI-HLL

Deposition of polycristalline silicon between p+ implants and a common bias line

Drawback: Additional production steps and photo lithographic masks required.

Small potential difference between strip implant and the bias dot

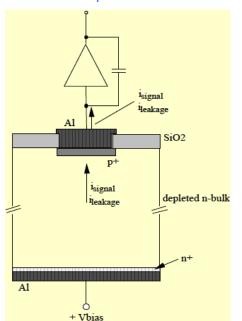
This solution allows avoiding the technological steps required for polysilicon deposition in the detector processing; same technology DC and AC strips Radiation damage?

Microstrip detectors with AC-coupled readout

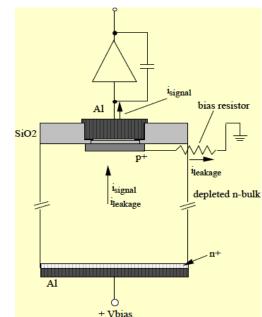
AC-coupling the detector with the electronics allows to avoid the DC detector leakage current to offset the working point of the preamplifier. Coupling capacitors of suitable value could be integrated in the detector itself (another benefit of the planar process)

 $C_C >> C_{S,tot}$

DC-coupled detector

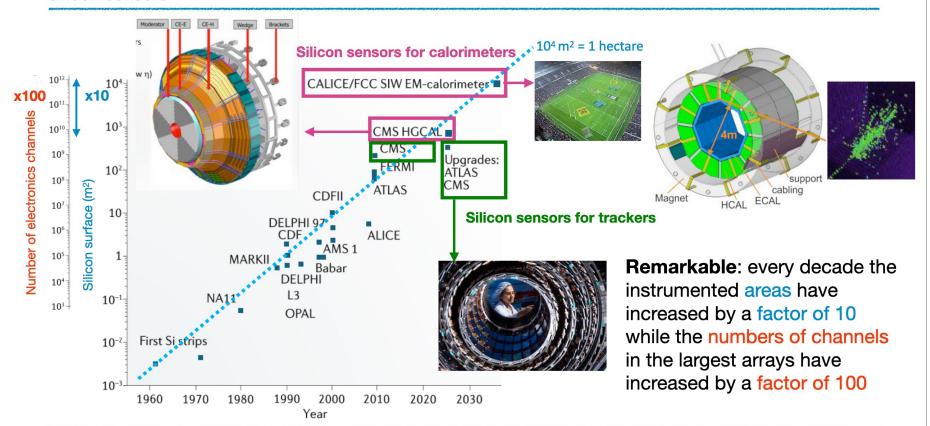


AC-coupled detector with integrated coupling capacitance



Historical development

silicon sensors



EPS - HEP2023

Hamburg, August 2023

Marco Bomben

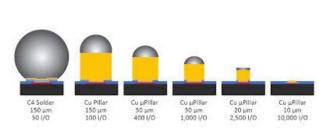
149

Silicon detectors

a continuous growth

Tremendous technological improvements

- The silicon wafer size increased from 2" to 12"
- The size of bump bonds decreased to < 10 μm and other technologies for hybridisation
- Technology node decreasing steadily, 65 nm in HEP



From metal solder sphere to micro-pillars

From solder bonding to bonding without Solder: Gold µ-pillar Thermo-Compression Bonding



Feature size or "Node" refers to the size of different features of a transistor including gate length and half-pitch specific of a <u>semiconductor manufacturing process</u>

~ first year of production

65 – 250 nm (detector electronics in production in HEP)
28 nm (detector electronics under preparation)
5 nm ~50 atom digital electronics of smart phones

After 28 nm → FinFETs have a completely different geometry, do not seem so promising in terms of radiation hardness

1996

2001

2005*

2011

2012

2014

2016

2018

≻28

22

HL-LHC

frontier for HEP

28 nm next

Momentum resolution

Momentum measurement uncertainty:

$$\frac{\sigma_p}{p} = \frac{L^2}{8Rs} \cdot \frac{\sigma_s}{s} = \frac{L^2}{8R} \cdot \frac{\sigma_s}{L^4/64R^2} = \frac{\sigma_s}{L^2} \cdot 8R = \frac{\sigma_s}{L^2} \cdot \frac{8p}{eB} \sim p \frac{\sigma_s}{BL^2}$$

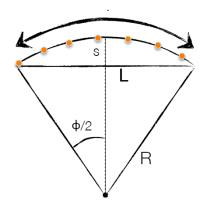
Uncertainty σ_s depends on number and spacing of track point measurements; for equal spacing and large N:

$$\sigma_s = \frac{\sigma_{r\phi}}{8} \sqrt{\frac{720}{N+5}} \quad \text{see: Glückstern, NIM 24 (1963) 381 or}$$

Blum & Rolandi. Particle Detection ...

Good momentum resolution:

- [Garutti]
- large path length L
- large magnetic field B
- good Sagitta measurement



For generally in experiment measure p. momentum p:

$$\left(\frac{\sigma_p}{p}\right)^2 = \left(\left(\frac{\sigma_{p_t}}{p_t}\right)^2\right) + \left(\left(\frac{\sigma_{\theta}}{\sin\theta}\right)^2\right) \quad \text{multiple scattering term conts. in p_t}$$

Examples:

Argus:
$$\sigma_{pt}/p_t = 0.009^2 + (0.009 p_t)^2$$

ATLAS: $\sigma_{pt}/p_t = 0.001^2 + (0.0005 p_t)^2$

track uncertainty ≈ p₊

[ATLAS nominal: TDR]

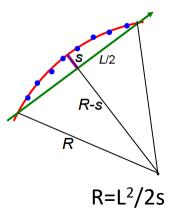
Momentum resolution

Charged particles: circular motion transverse to uniform B field $p_T[\text{GeV/c}] = 0.3 \times B [\text{T}] \times R [\text{m}]$

Measuring the sagitta s we can measure the transverse momentum p_T

Transverse momentum resolution - Need strong B, long path length L and excellent sagitta resolution σ_s

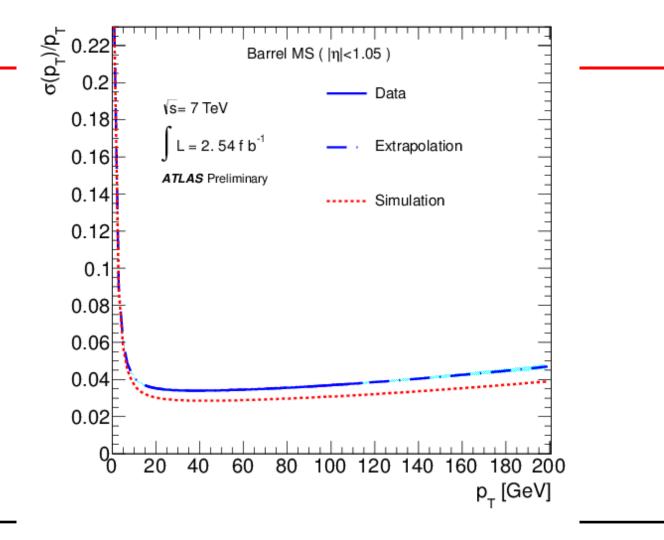
$$\frac{\sigma_{p_T}}{p_T} = \frac{8p_T}{0.3BL^2} \sigma_s$$



The sagitta resolution σ_s depends on the position resolution $\sigma_{\phi r}$ which depends on the sensor intrinsic resolution; $\sigma_{\phi r}$ is limited by multiple scattering

$$\sigma_{r\phi} = \sigma_{int} \oplus \sigma_{MS}$$

Requirement: best possible space point resolution, material at minimum



FE chip –150 μm thick

Sensor –200 μm thick

Flex

Vertex Resolution

x1, x2 = measurement planes

$$y1$$
, $y2$ = measured points, with errors δy

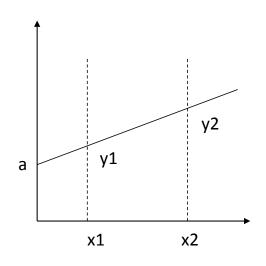
$$y = a + bx$$

$$b = \text{slope} = \frac{y1 - y2}{x1 - x2} = \frac{y1 - y2}{\Delta x}$$

$$a = \text{intercept} = \frac{1}{2}(y1 + y2) - \frac{1}{2}(y1 - y2)\left(\frac{x1 + x2}{\Delta x}\right) = \overline{y} - b\overline{x}$$

$$(\delta b)^2 = \left(\frac{\partial b}{\partial y^1}\right)^2 (\delta y)^2 + \left(\frac{\partial b}{\partial y^2}\right)^2 (\delta y)^2 \Rightarrow \delta b = \frac{\sqrt{2}\delta y}{\Delta x}$$

$$\delta a = \frac{\delta y}{2} \sqrt{1 + \frac{8\overline{x}}{\Delta x}}$$

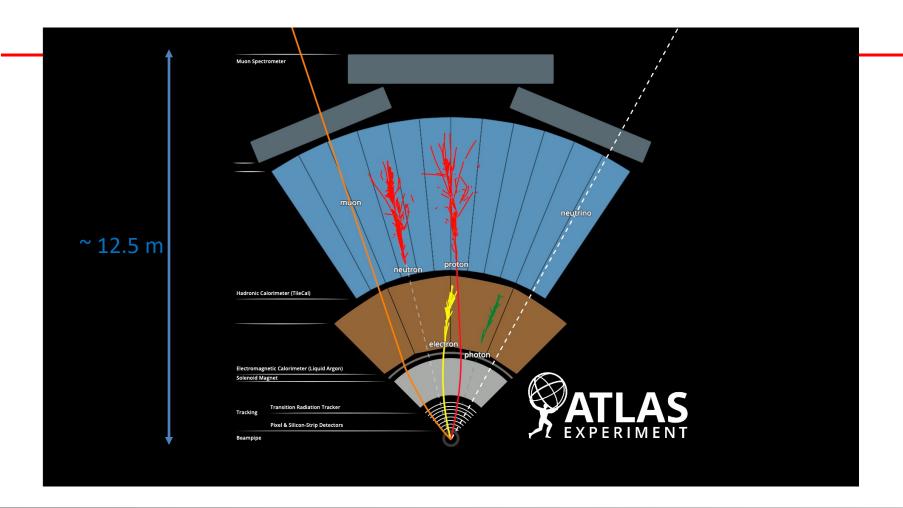


for good resolution on angles (f and q) and intercepts (d, z₀)

- Precision track point measurements
- •Maximize separation between planes for good resolution on intercepts
- •Minimize extrapolation first point close to interaction

June 10, 2011

155



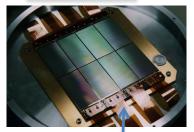
CCD cameras for astronomy

SDSS Photometric Camera – 30 2k x 2k, (24 µm)²-pixel Sloan Digital Sky Survey Telescope 2000 – 2008



CCD: Thinned (10-20µm) partially depleted

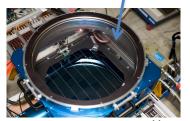
64 MPixels



SuprimeCam – 8¹2k x 4k, (15 μm)²-pixel CCDs Subaru 8-m Telescope (1998)

CCD: 40 µm thick, partially depleted

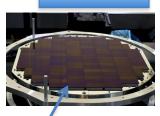
PS1 camera $60 ext{ 4.8k x 4.8k, } (10 ext{ } \mu m)^2$ -pixel Pan-STARRS telescope (2010)



1.4 GPixels

CCD: 75 μm thick, fully depleted

870 MPixels



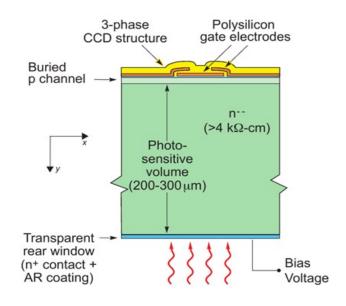
157

HyperSuprimeCam 116 2k x 4k, (15 μm)²-pixel Subaru 8-m Telescope 1st light achieved 28Aug2012

CCD: 200 µm thick, fully depleted

Trend: thick, full depleted CCDs

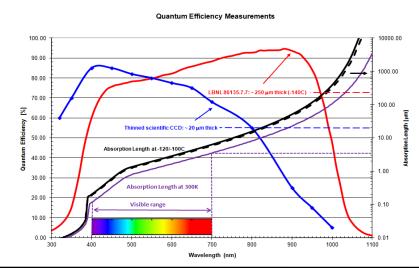
Thick, fully depleted CCDs



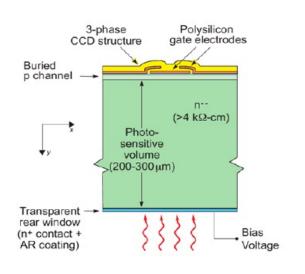
Fully Depleted, Back-Illuminated Charge-Coupled Devices Fabricated on High-Resistivity Silicon Stephen E. Holland et al., IEEE TRANSACTIONS ON ELECTRON DEVICESVOL. 50, NO. 1 (2003) 225

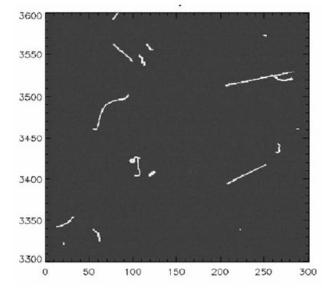
Merging of p-i-n and CCD technology: A conventional CCD on a thick, high-resistivity Si substrate (> $4 \text{ k}\Omega\text{-cm}$), fully depleted

The large thickness results in high near-infrared QE
The fully depleted operation results in the ability to control
the spatial resolution



Drawbacks of thick, fully depleted CCDs





Cosmic rays and Compton electrons from background radiation leave long tracks

30 minute dark 200 μm thick CCD Small sub-image

LSST sensor specifications



High quantum effciency from 320 to 1080 nm thanks to a large depletion depth (100 μ m) and implementation of the sensor in a back-illuminated configuration

To reduce charge diffusion the sensor is fully depleted, and a high internal field is maintained within the depletion region. This is made possible by the use of high resistivity substrates and high applied voltages.

High Fill factor. A total of 189 4 K x 4 K sensors are required to cover the 3200 cm²

focal plane. To maintain high throughput, the sensors are mounted in four-side buttable packages and are positioned in close proximity to one another with gaps of less than a few hundred μ m. The resulting fill factor, *i.e.*, the fraction of the focal plane covered by pixels, is 93%.

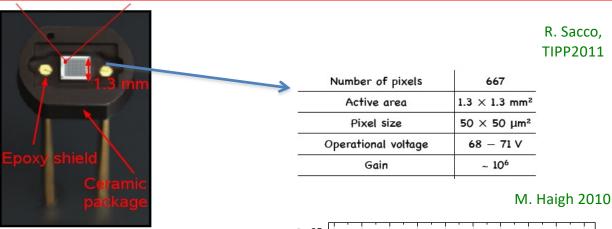
Prototype sensors mounted on a raft baseplate - http://www.lsst.org/News/enews/focal-plane-201101.html

Caméras CCD vs CMOS

Les capteurs CCD présentent encore des avantages significatifs pour l'imagerie haute performance à faible niveau de lumière, mais la technologie CMOS a rattrapé le retard.

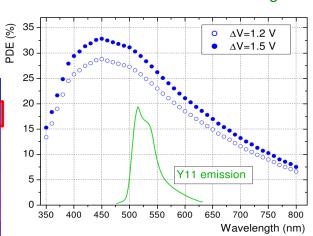
Paramètre	CCD	CMOS	Gagnant
Disponibilité	Certaines grandes lignes de capteurs CCD deviennent obsolètes. Capteurs spécialisés coûteux.	Les entreprises investissent massivement, et la technologie s'améliore rapidement.	Le CMOS est l'avenir pour la plupart des applications. Le CCD continue à servir des niches spécialisées.
Coût	Les grands capteurs CCD sont coûteux, et l'électronique est complexe.	Les grands capteurs CMOS sont également coûteux. l'électronique est plus complexe.	CMOS
Efficacité Quantique	60 % - 95 %, bien que les capteurs à haute QE soient très coûteux.	75 % - 95 %	Le CMOS a un meilleur rapport qualité-prix.
Vitesse en mégapixels par second (MPS)	1 à 40 MPS	100 à 400 MPS	CMOS
Bruit de Lecture	5-10 électrons pour les CCD standards, 1 électron pour les dispositifs de multiplication d'électrons complexes (EMCCD).	1-3 électrons sont courants pour les capteurs CMOS modernes, et cela continue de s'améliorer.	CMOS / EMCCD
Refroidissement	Un refroidissement élevé est relativement facile à obtenir.	Les capteurs génèrent une grande quantité de chaleur et ne peuvent pas être refroidi à des températures trop baisses.	CCD
Taille des Pixels	3 à 25 microns	2 à 9 microns	CCD/CMOS
Well-Depth (Capacité)	40,000 à 200,000	30,000 à 75,000. Compensé par empilement grâce au faible bruit de lecture.	CCD / CMOS
Binning	Facilement réalisé au niveau analogique avec zéro bruit ajouté.	Le binage analogique sur puce est limité; la plupart des capteurs disponibles ne peuvent effectuer que du binage 2×2.	CCD
Imagerie Infrarouge	Les capteurs à peuvent atteindre une efficacité quantique élevée entre 650 et 1000 nm.	Actuellement quasi-impossible avec les capteurs CMOS basés sur le silicium.	CCD
Qualité de l'image	Les techniques pour les CCD sont bien établies et efficaces.	Peut être plus complexe, comme les modes HDR.	CCD

The T2K ND280 MultiPixel Photon Counter

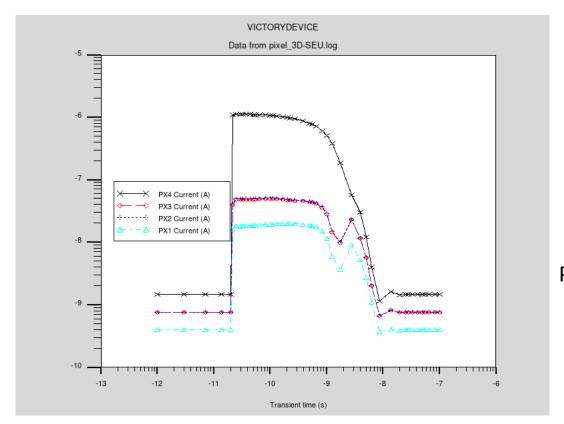


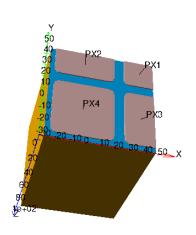
Total number of SiPMs in T2K = 56000 First large experiment to use this type of sensor.

System	Channels	Bad channels	Fraction
ECAL (DSECAL)	22336 (3400)	35 (11)	0.16% (0.32%)
SMRD	4016	7	0.17%
POD	10400	7	0.07%
FGD	8448	20	0.24 %
INGRID	10796	18	0.17 %
Total	55996	87	0.16 %

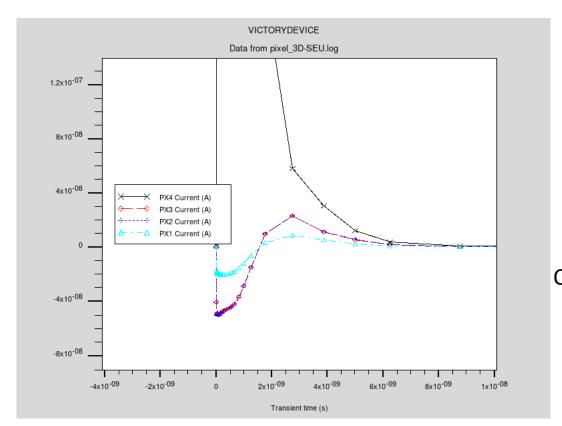


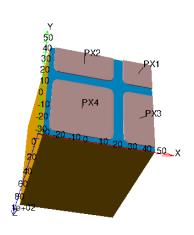
R. Sacco, **TIPP2011**



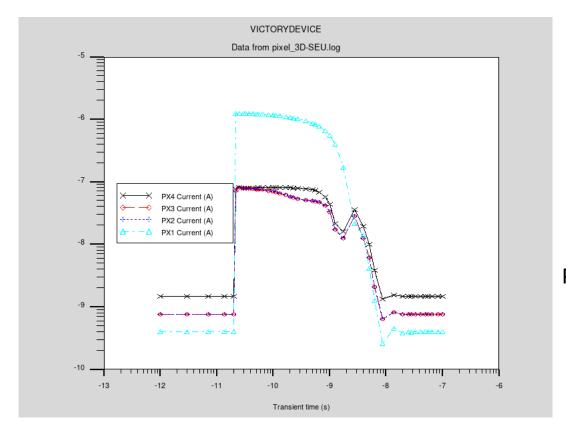


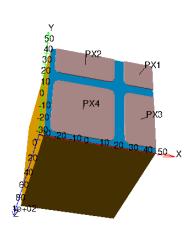
Particle striking in the middle of PX4



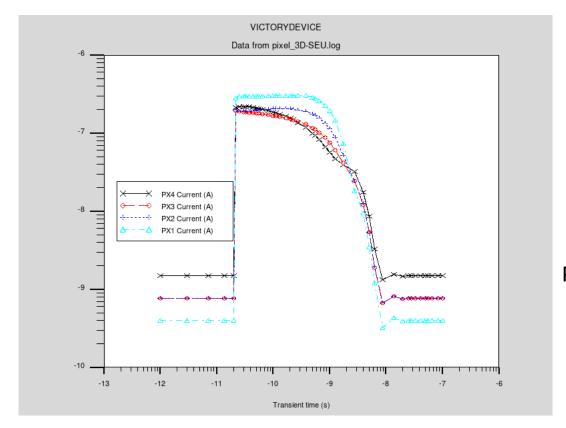


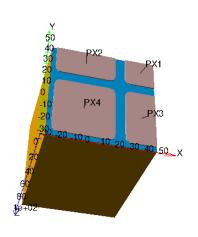
Opposite signal induced on neighbours



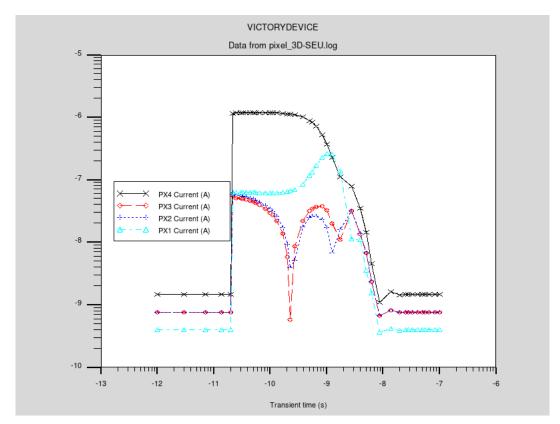


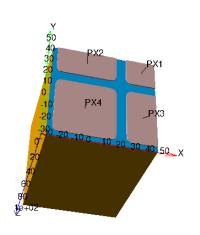
Particle striking in the middle of PX1





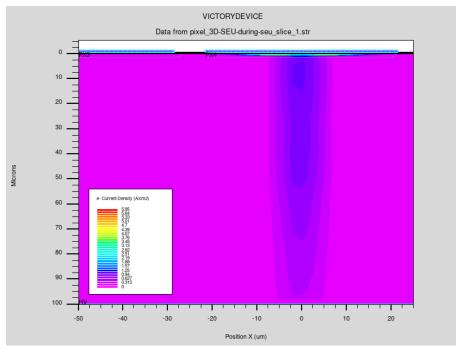
Particle striking in between pixels

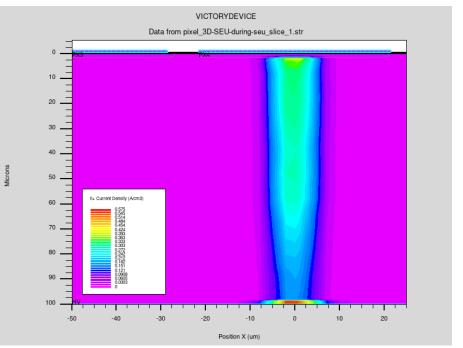




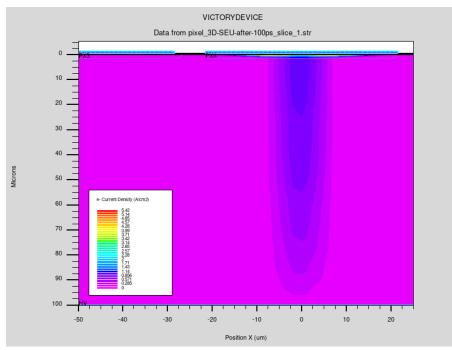
Particle striking diagonally

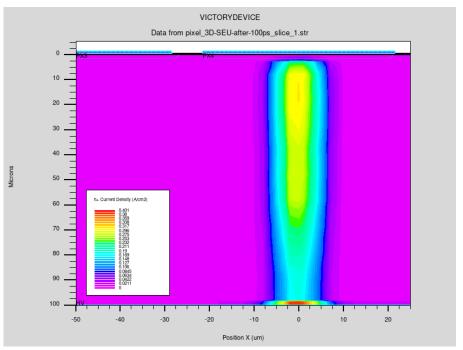




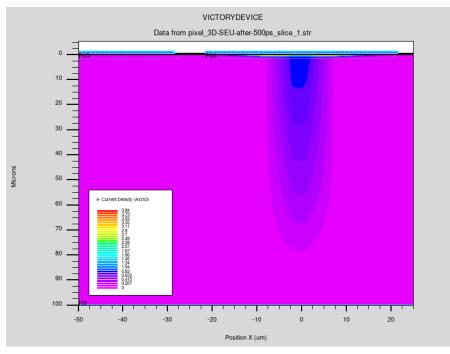


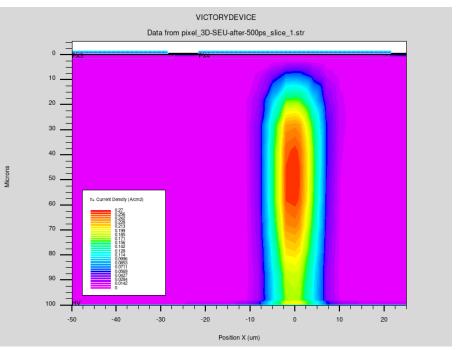




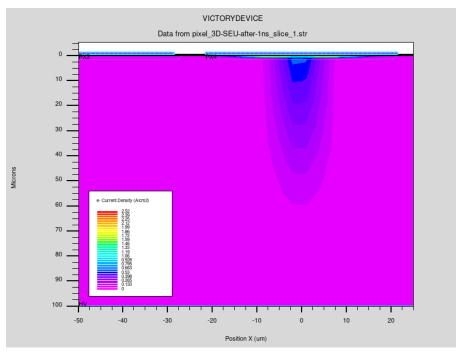


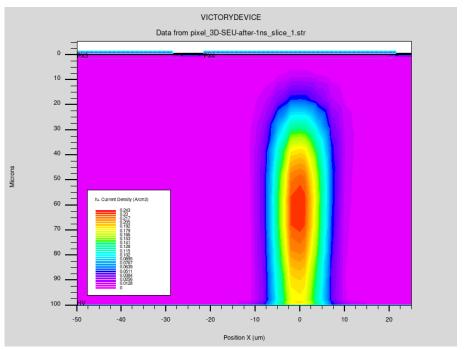




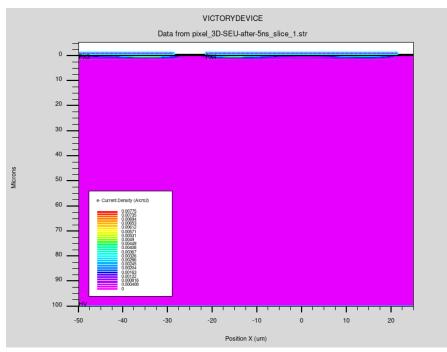


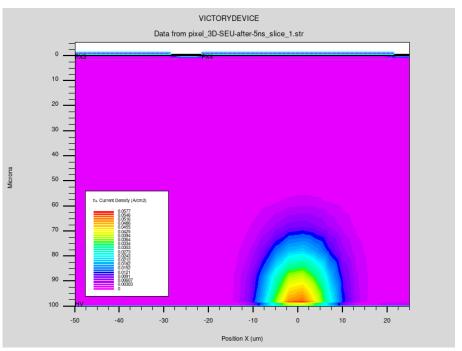




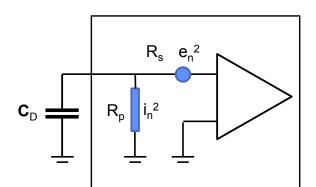








Noise



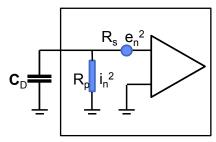
For a sensor that is represented by a capacitance, the noise is determined by the amplifier only. The amplifier noise can be characterized by the parallel and series noise power spectrum.

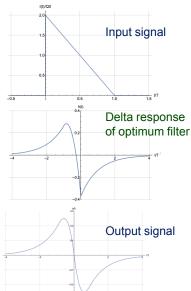
In case the parallel and series noise power spectra are 'white' we can formulate this as noise resistance R_s and R_p .

The level of this noise is a specification of the amplifier, there is no intrinsic noise in the sensor.

This noise level is very specific to the technology, but in general, lower noise requires more power (current through the input transistor etc.).

This places practical limits on the achievable noise level in systems with high granularity i.e. many channels on a small surface.





Optimum filter for best timing

Assuming a silicon sensor with negligible depletion voltage and saturated drift-velocity, the signal shape is a triangle:

$$f(t) = \frac{2Q_0}{T} \left(1 - \frac{t}{T} \right)$$
 $F(i\omega) = \frac{2Q_0}{\omega^2 T^2} \left(1 - e^{-i\omega T} - i\omega T \right)$

For the noise we assume series noise and parallel noise together with a detector capacitance C_D

$$w(\omega)=rac{4kT}{R_p}+4kTR_sC_D^2\omega^2=a^2+b^2\omega^2$$
 $e_n^2(\omega)=4kTR_s$ $i_n^2(\omega)=rac{4kT}{R_p}$

The maximum slope to noise ratio is

$$\left(\frac{k}{\sigma}\right)^2 \le \frac{4Q_0^2}{a^3T^4} \left(2e^{-aT/b}(b+aT) + \frac{a^2T^2}{b} - 2b\right)$$

If we neglect parallel noise we have

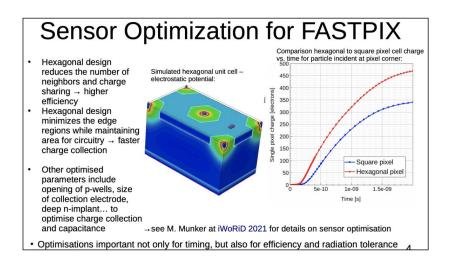
$$\left(\frac{k}{\sigma}\right)^2 \le \frac{8Q_0^2}{3b^2T}$$

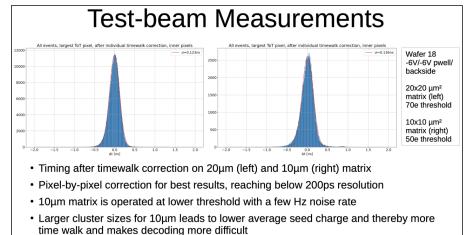
This filter is a-causal and can only be approximated in practise.

W. Riegler, Detector Signals

W. Riegler, CERN seminar

FASTPIX: a monolithic CMOS Sensor with <200ps timing





WORKSHOP ON PICO-SECOND TIMING DETECTORS FOR PHYSICS

9–11 Sep 2021 University of Zurich

Eric Buschmann

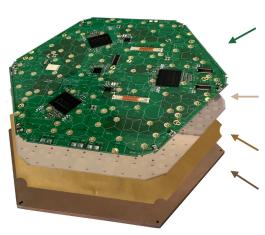
https://indico.cern.ch/event/861104/contributions/4503032/

< 200ps achieved with a MAPS sensor!

W. Riegler, CERN seminar

Silicon modules

- Hexagon-shaped modules tiling the electromagnetic calorimeter and partially the hadronic section
 - Hexagonal sensor shape to maximise area on wafer, partial sensors at borders
- High Density (HD) sensors: 0.6 cm² cells; Low Density (LD) sensors: 1.2 cm² cells



Hexaboard

- Readout of sensor cells with HGCROC custom ASICs and connection to electronics for data transfer
- Bias and low voltage distribution

Silicon sensor

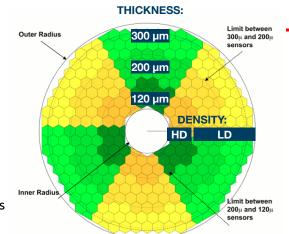
- 8-inch wafers
- Planar, DC-coupled, p-type sensors

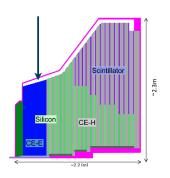
Cu-in-kapton isolation

• Grounded for electric noise reduction

CuW baseplate (CE-E) or titanium (CE-H)

- Contributes to absorber material in CE-E
- Gives mechanical stability





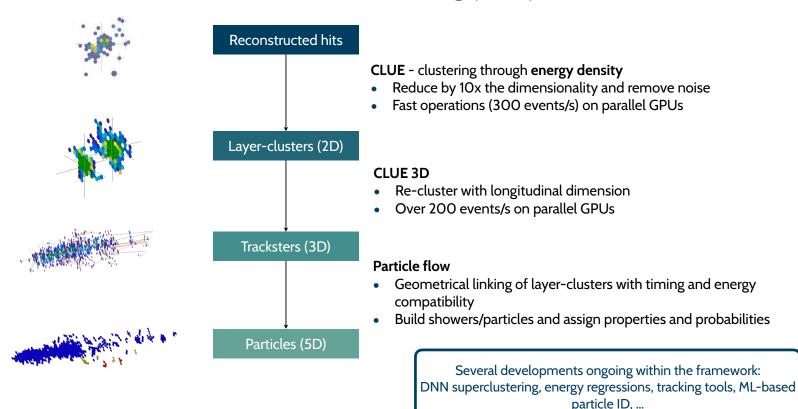
https://indico.cern.ch/event/1596761/

C. Amendola

31/10/2025

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Reconstruction with the Iterative Clustering (TICL) framework



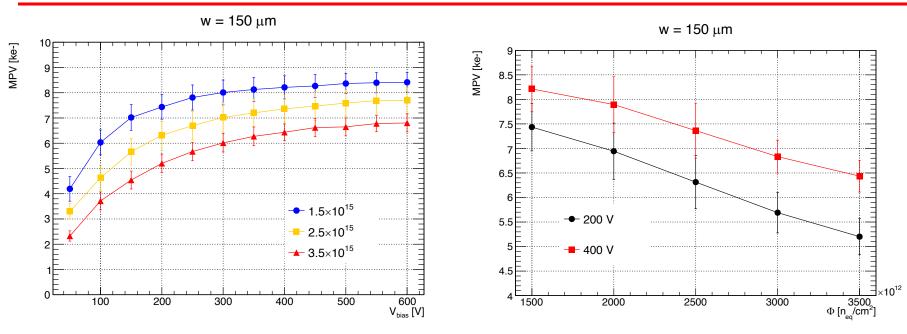
https://indico.cern.ch/event/1596761/

31/10/2025

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C. Amendola

ATLAS ITk, Q vs fluence - simulations



(before irr. Q ~ 10 ke-)

https://doi.org/10.1016/j.nima.2025.171000