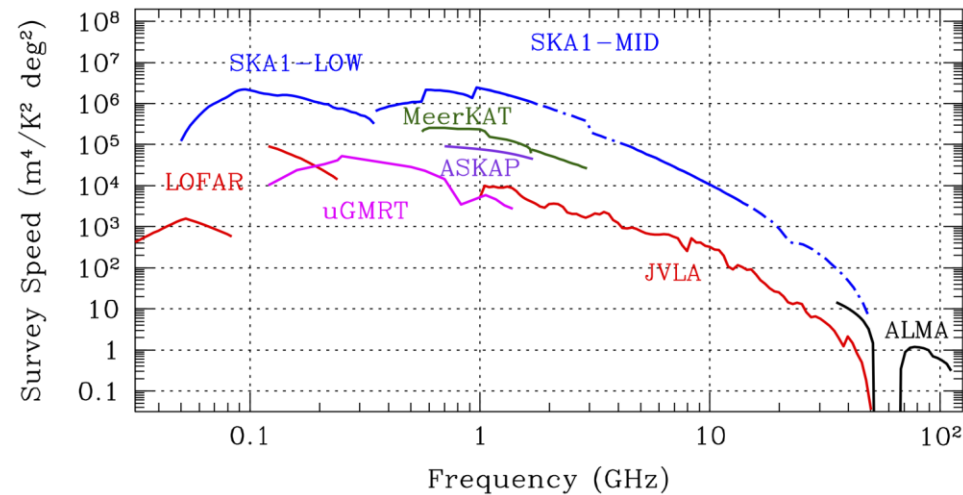
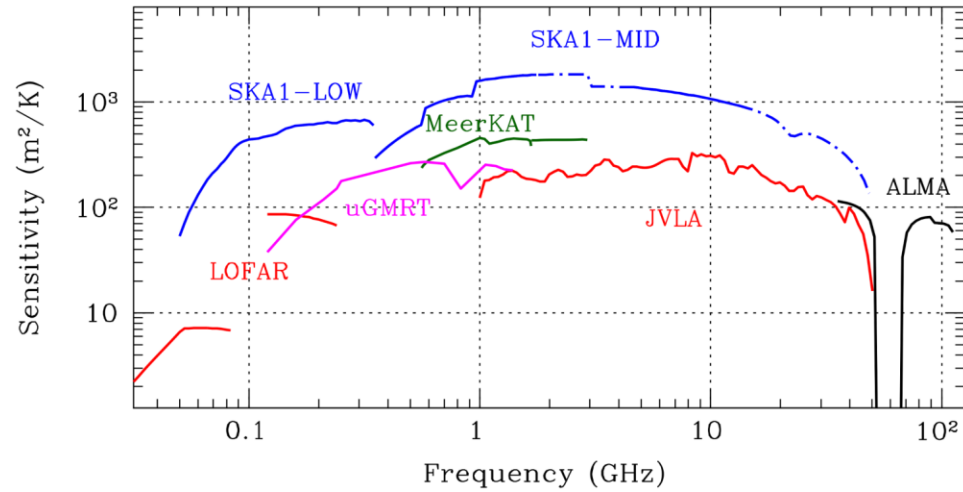


Decentralizing radio-interferometric image reconstruction by spatial frequency

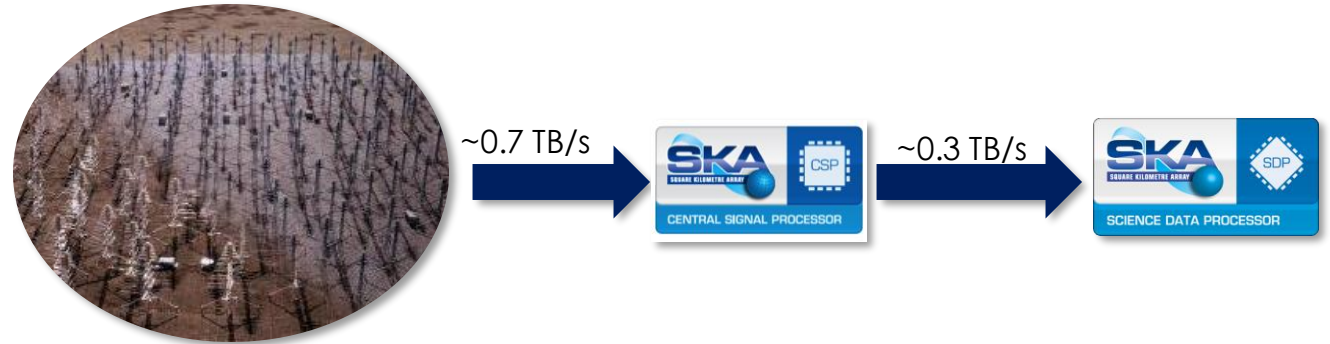
Sunrise Wang, Simon Prunet, Shan Mignot André Ferrari



Introduction



SKA-Low



SKA-Mid

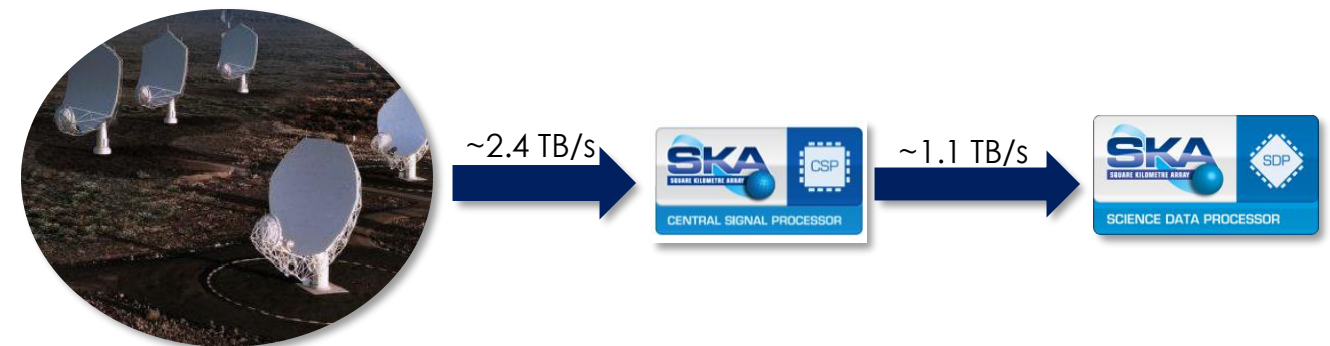
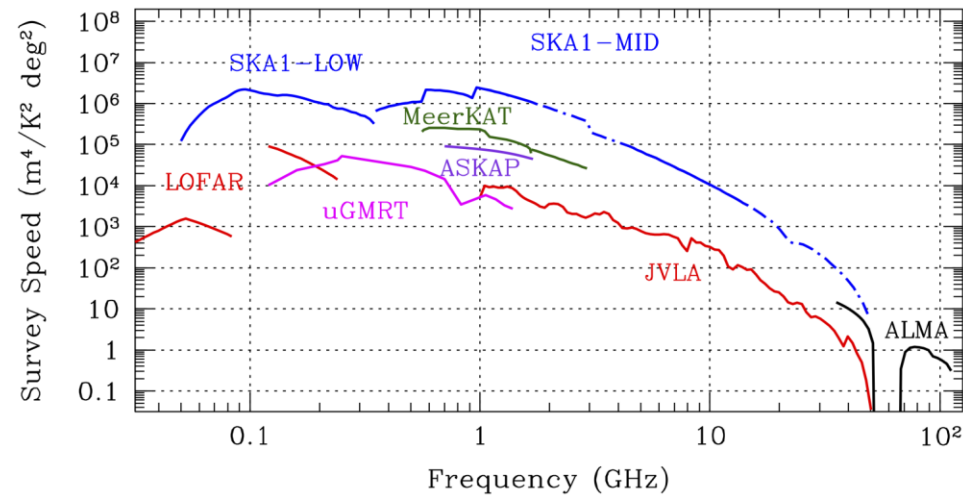
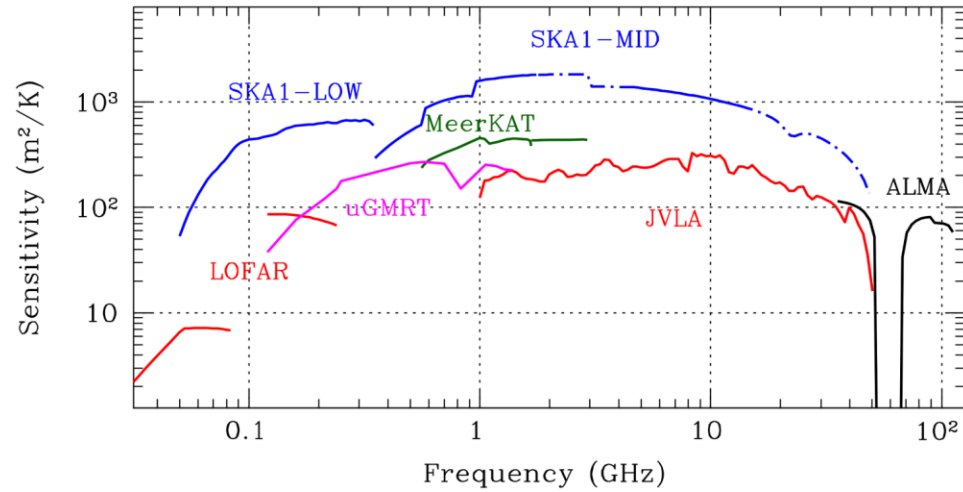


image sources: [3]
data source: [1, 2]

Introduction



SKA-Low



~0.7 TB/s



~0.3 TB/s



SKA-Mid



~2.4 TB/s

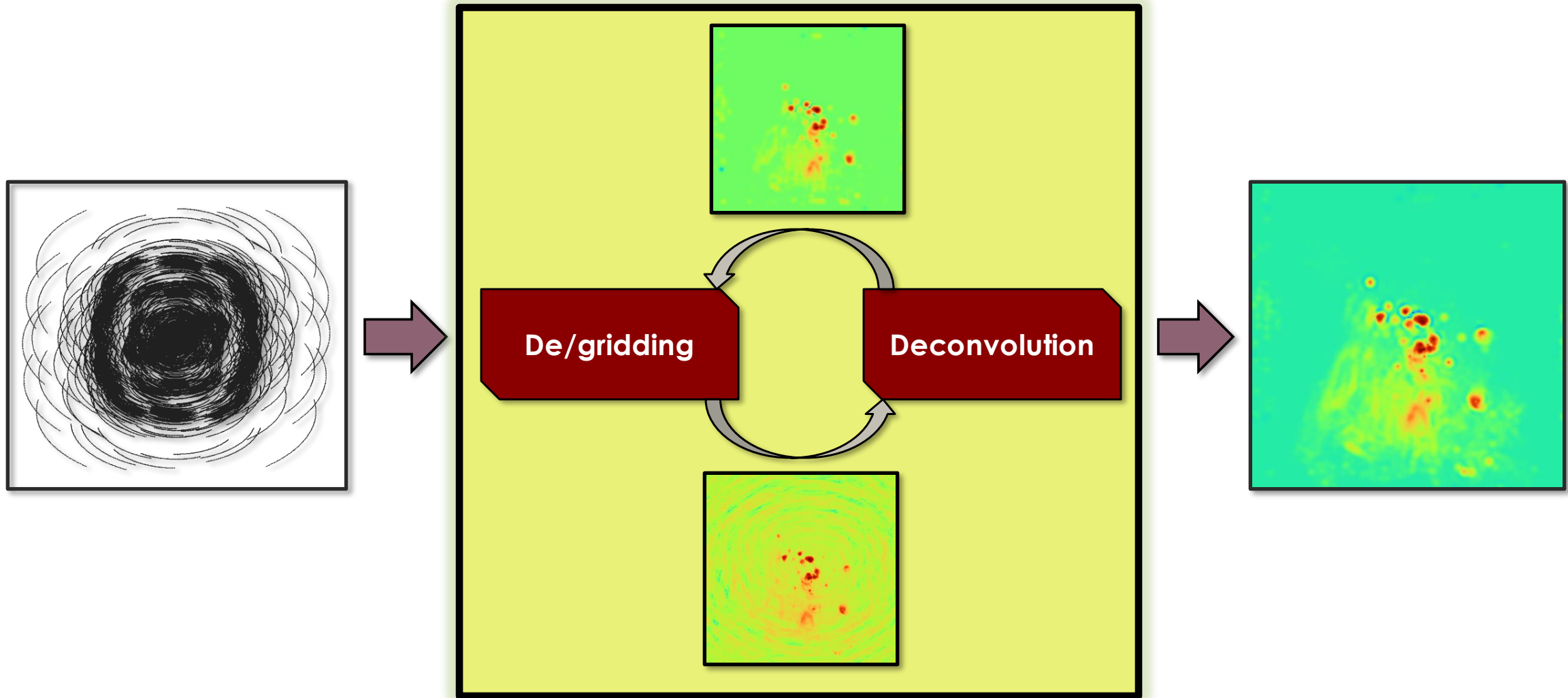


~1.1 TB/s

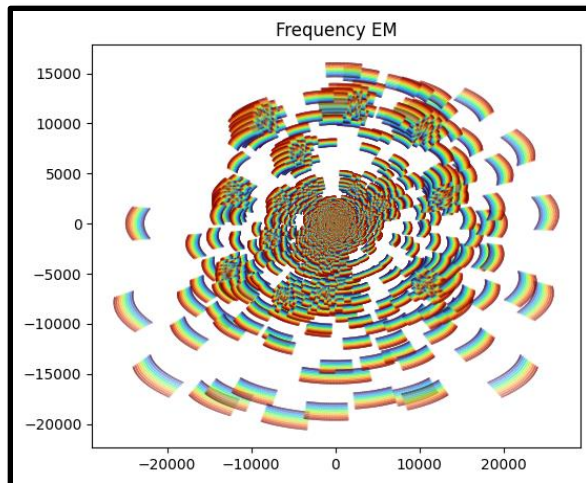
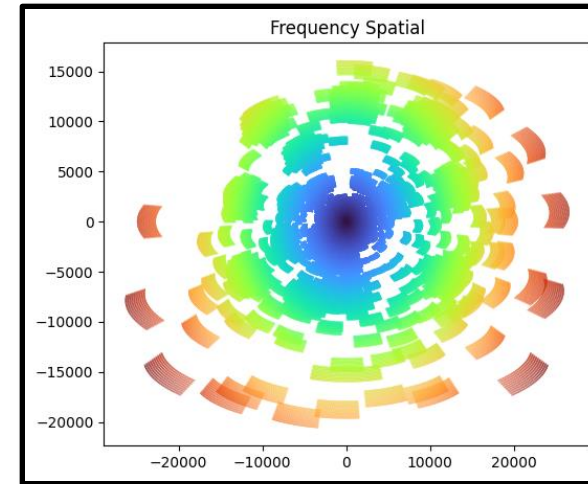
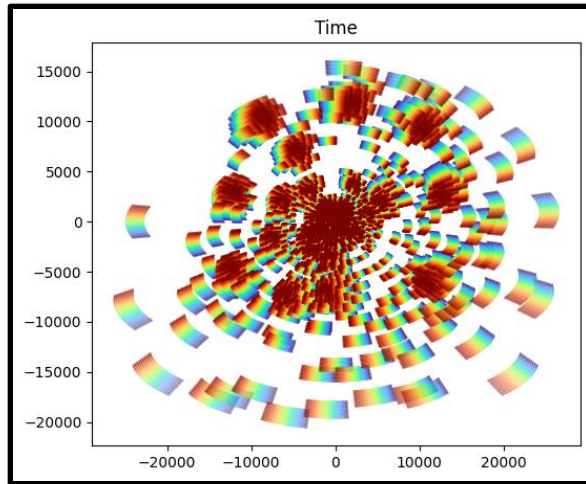


image sources: [3]
data source: [1, 2]

Major-Minor Loop Reconstruction

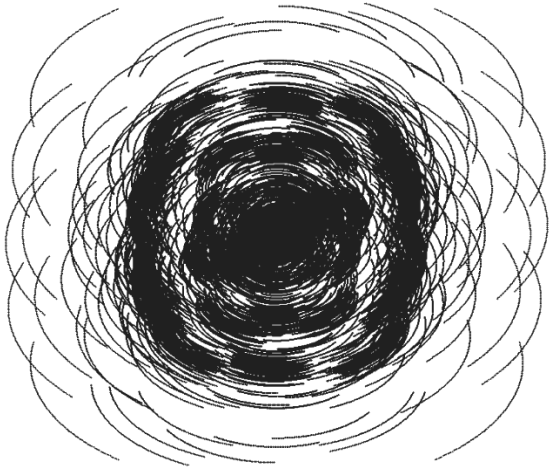


Scaling the computation



- Partition visibilities, process separately
- Commonly by time and em frequency, partitioning relatively trivial
- We look at spatial frequency, more complicated as not all frequencies are available for deconvolution

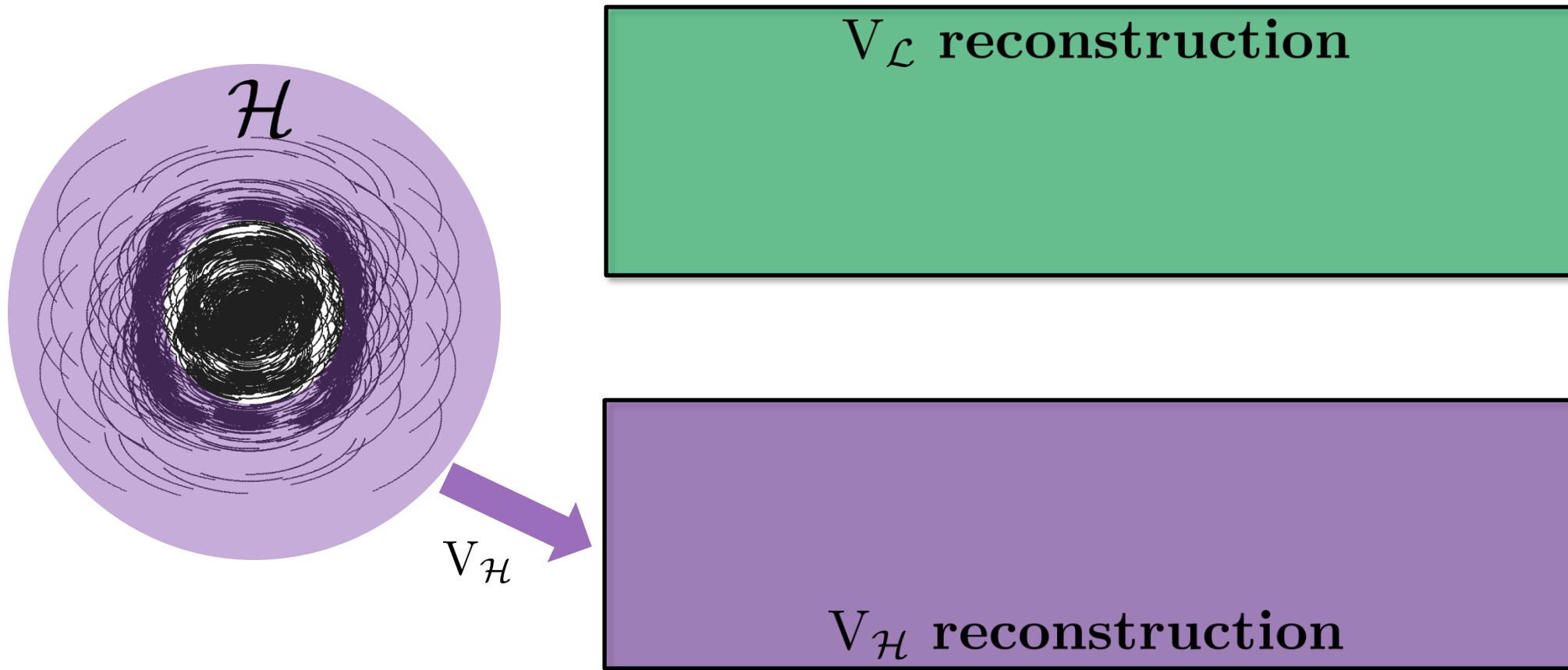
Parallelization Framework



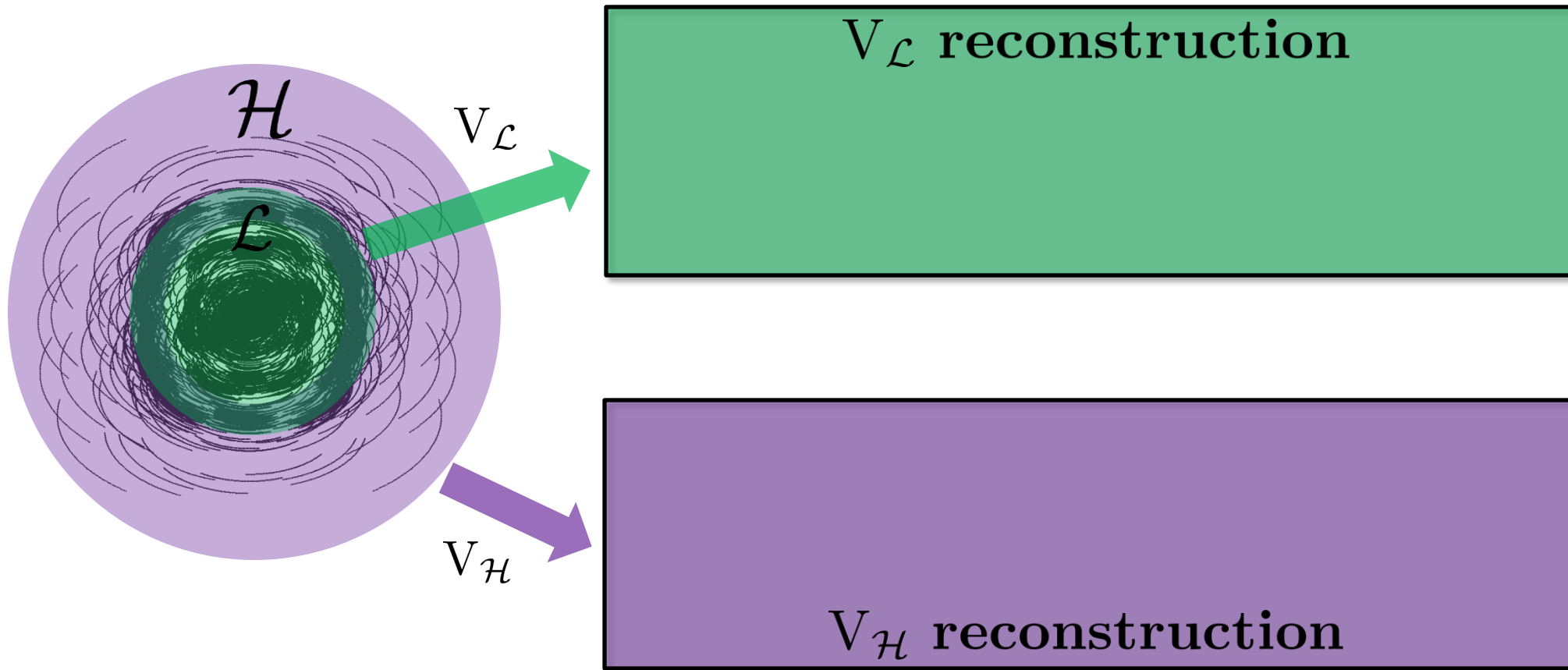
$V_{\mathcal{L}}$ reconstruction

$V_{\mathcal{H}}$ reconstruction

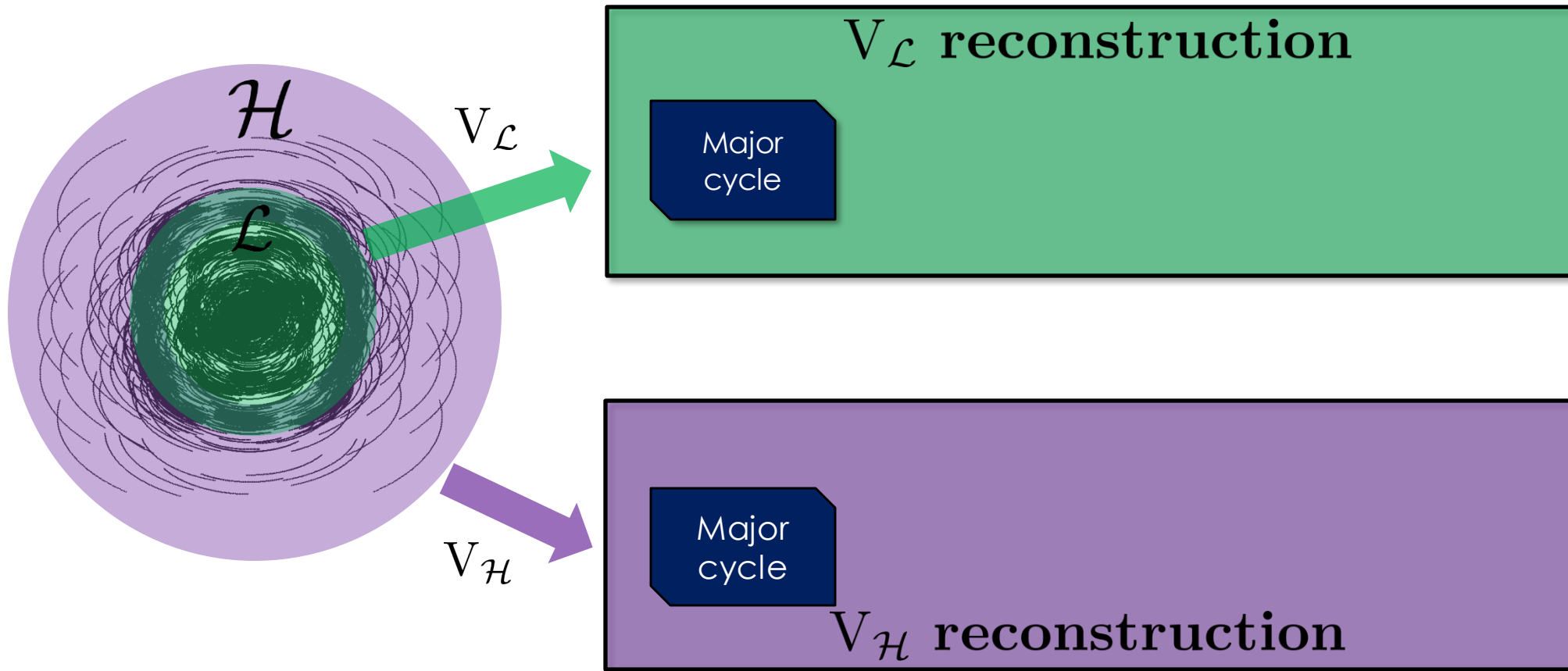
Parallelization Framework



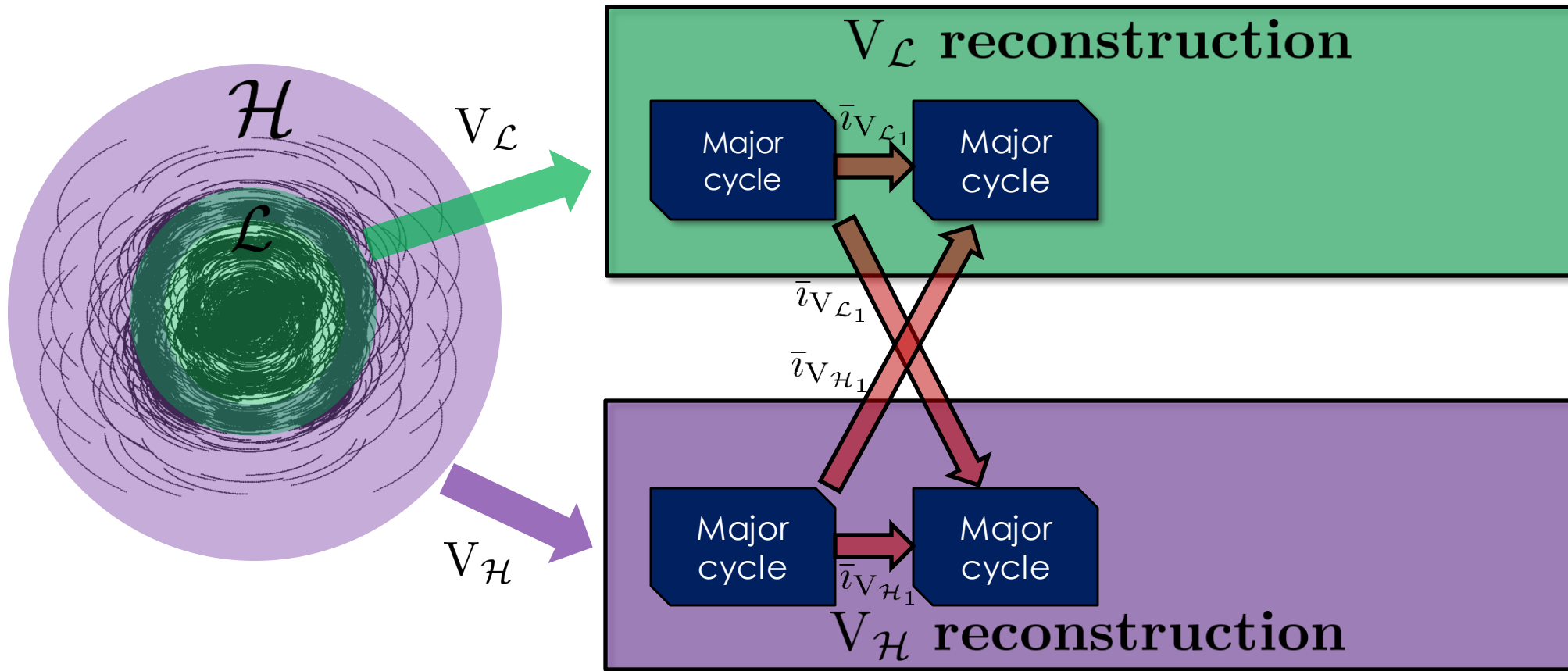
Parallelization Framework



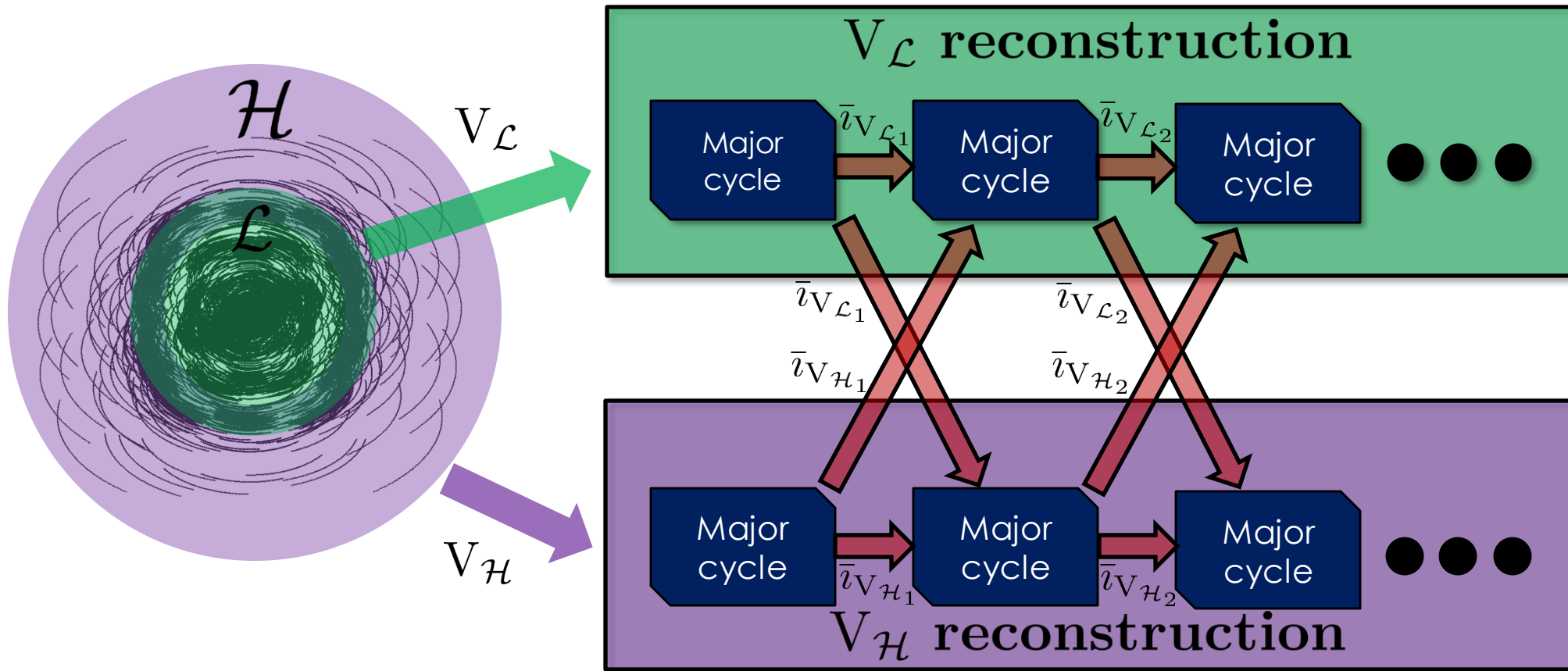
Parallelization Framework



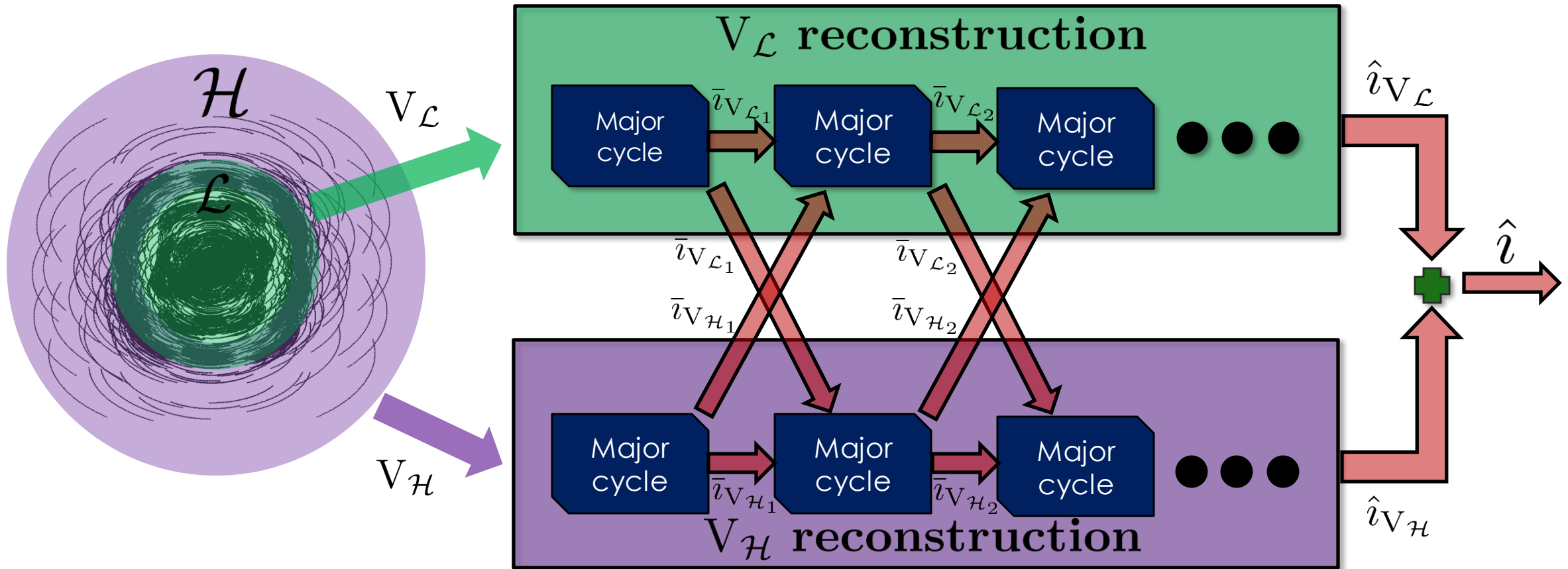
Parallelization Framework



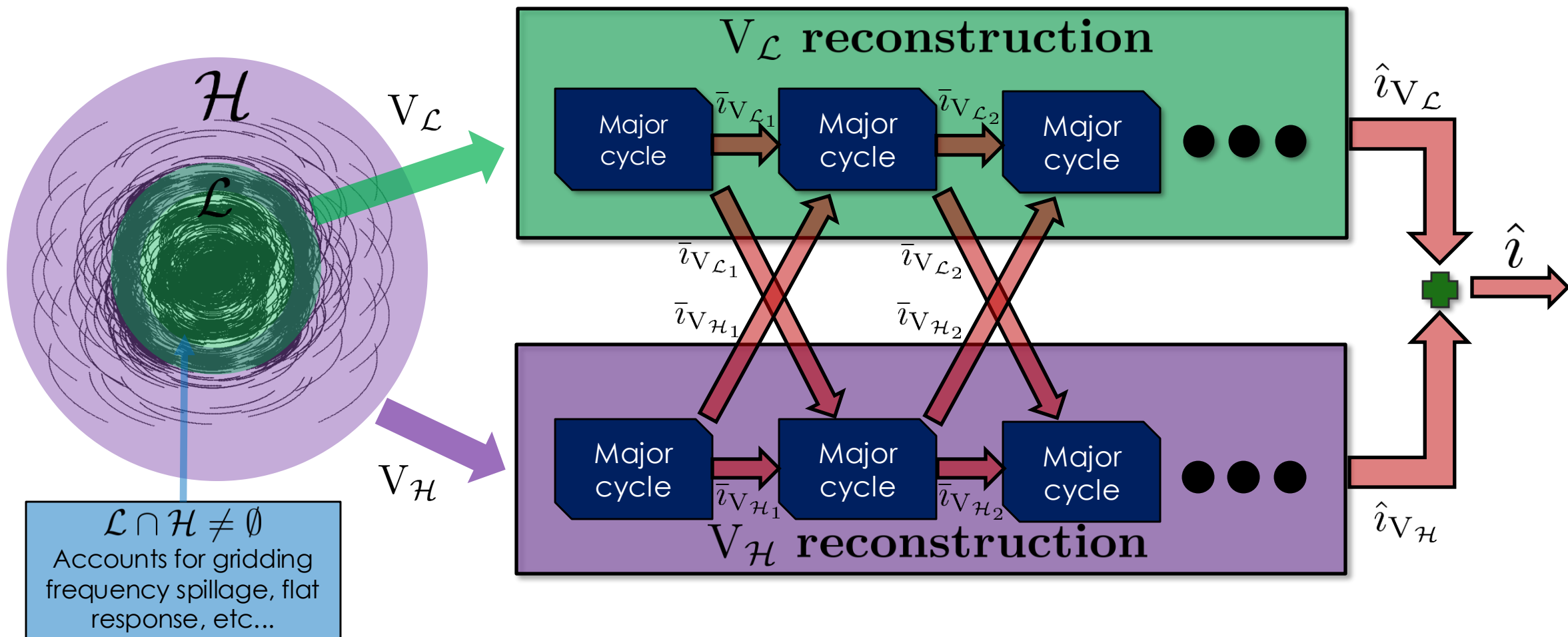
Parallelization Framework



Parallelization Framework



Parallelization Framework



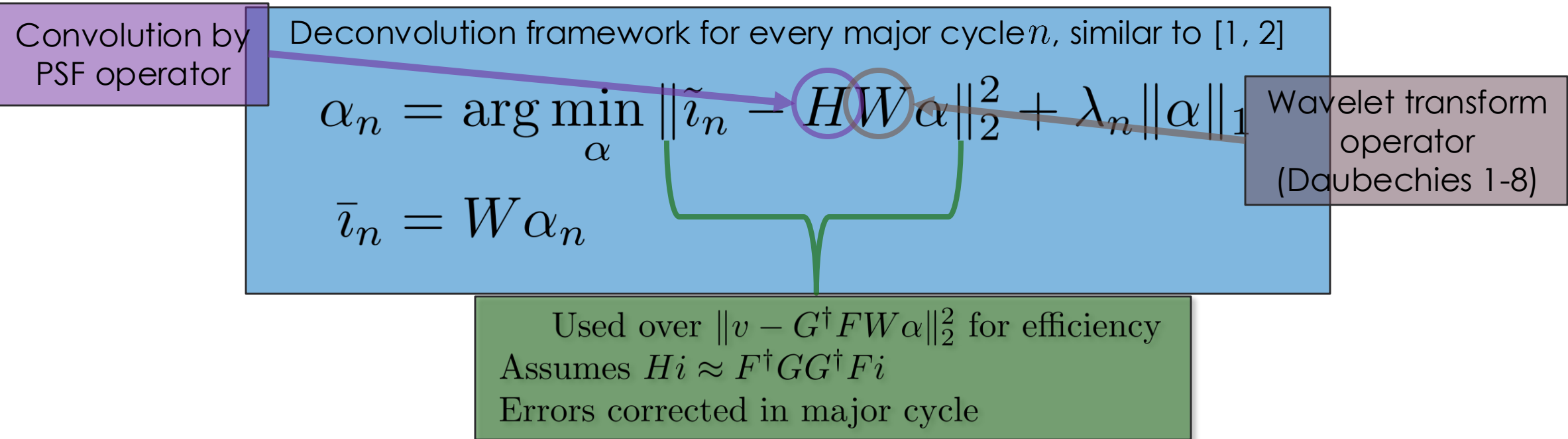
Example 1: Parallelized L1 reconstruction

Deconvolution framework for every major cycle n , similar to [1, 2]

$$\alpha_n = \arg \min_{\alpha} \|\tilde{i}_n - HW\alpha\|_2^2 + \lambda_n \|\alpha\|_1$$

$$\bar{i}_n = W\alpha_n$$

Example 1: Parallelized L1 reconstruction



Example 1: Parallelized L1 reconstruction

Deconvolution framework for every major cycle n , similar to [1, 2]

$$\alpha_n = \arg \min_{\alpha} \|\tilde{i}_n - HW\alpha\|_2^2 + \lambda_n \|\alpha\|_1$$

$$\bar{i}_n = W\alpha_n$$

$V_{\mathcal{L}}$ deconvolution

$$\alpha_{V_{\mathcal{L}_n}} = \arg \min_{\alpha} \|G_{\mathcal{L}}(\tilde{i}_{\mathcal{L}_n} - H_{\mathcal{L}}W\alpha)\|_2^2 + \|G_{\mathcal{H}}(h_n - W\alpha)\|_2^2 + \lambda_{V_{\mathcal{L}_n}} \|\alpha\|_1$$

$$\bar{i}_{V_{\mathcal{L}_n}} = W\alpha_{V_{\mathcal{L}_n}}, h_n = \sum_{j=1}^{n-1} \bar{i}_{V_{\mathcal{H}_j}} - \sum_{j=1}^{n-1} \bar{i}_{V_{\mathcal{L}_n}} = \hat{i}_{V_{\mathcal{H}_{n-1}}} - \hat{i}_{V_{\mathcal{L}_{n-1}}}$$

Example 1: Parallelized L1 reconstruction

Deconvolution framework for every major cycle n , similar to [1, 2]

$$\alpha_n = \arg \min_{\alpha} \|\tilde{i}_n - HW\alpha\|_2^2 + \lambda_n \|\alpha\|_1$$

$$\bar{i}_n = W\alpha_n$$

Visibility data-fidelity term

$V_{\mathcal{L}}$ deconvolution

$$\alpha_{V_{\mathcal{L}_n}} = \arg \min_{\alpha} \|G_{\mathcal{L}}(\tilde{i}_{\mathcal{L}_n} - H_{\mathcal{L}}W\alpha)\|_2^2 + \|G_{\mathcal{H}}(h_n - W\alpha)\|_2^2 + \lambda_{V_{\mathcal{L}_n}} \|\alpha\|_1$$

$$\bar{i}_{V_{\mathcal{L}_n}} = W\alpha_{V_{\mathcal{L}_n}}, h_n = \sum_{j=1}^{n-1} \bar{i}_{V_{\mathcal{H}_j}} - \sum_{j=1}^{n-1} \bar{i}_{V_{\mathcal{L}_j}} = \hat{i}_{V_{\mathcal{H}_{n-1}}} - \hat{i}_{V_{\mathcal{L}_{n-1}}}$$

Additional data-fidelity term for rest of frequency information (only from 2nd major cycle onwards)

High and low resolution filters
Normalizes data fidelity terms
Ensures visibilities in $\mathcal{L} \cap \mathcal{H}$ sum to 1

Example 2: Parallelized MS-CLEAN reconstruction

CLEAN iteratively removes the brightest source at the most relevant scale convolved by the PSF from the residual[1]. We can denote this as:

$$\bar{i} = \text{MS-CLEAN}(\tilde{i}, H)$$

Example 2: Parallelized MS-CLEAN reconstruction

CLEAN iteratively removes the brightest source at the most relevant scale convolved by the PSF from the residual[1]. We can denote this as:

$$\bar{i} = \text{MS-CLEAN}(\tilde{i}, H)$$

$V_{\mathcal{L}}$ deconvolution

$$\bar{i}_{V_{\mathcal{L}_n}} = \text{MS-CLEAN}(\alpha G_{\mathcal{L}} \tilde{i}_{\mathcal{L}_n} + \beta G_{\mathcal{H}} H_{\mathcal{H}} h_n, \alpha G_{\mathcal{L}} H_{\mathcal{L}} - \beta G_{\mathcal{H}} H_{\mathcal{H}})$$

$$h_n = \sum_{j=1}^{n-1} \bar{i}_{V_{\mathcal{H}}} - \sum_{j=1}^{n-1} \bar{i}_{V_{\mathcal{L}}}$$

Example 2: Parallelized MS-CLEAN reconstruction

CLEAN iteratively removes the brightest source at the most relevant scale convolved by the PSF from the residual[1]. We can denote this as:

$$\bar{i} = \text{MS-CLEAN}(\tilde{i}, H)$$

Pseudo full-resolution dirty

Pseudo full-resolution PSF

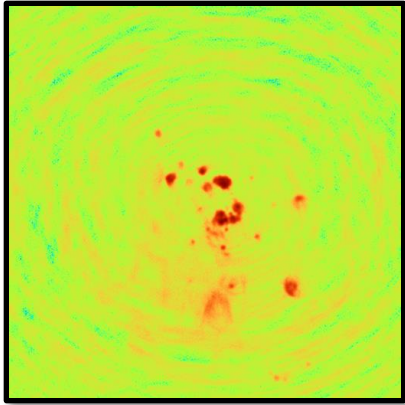
$V_{\mathcal{L}}$ deconvolution

$$\bar{i}_{V_{\mathcal{L}_n}} = \text{MS-CLEAN}(\alpha G_{\mathcal{L}} \tilde{i}_{\mathcal{L}_n} + \beta G_{\mathcal{H}} H_{\mathcal{H}} h_n, \alpha G_{\mathcal{L}} H_{\mathcal{L}} - \beta G_{\mathcal{H}} H_{\mathcal{H}})$$

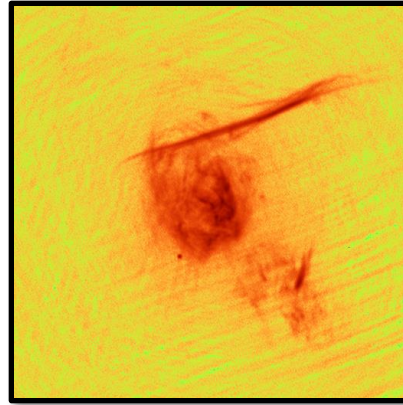
$$h_n = \sum_{j=1}^{n-1} \bar{i}_{V_{\mathcal{H}}} - \sum_{j=1}^{n-1} \bar{i}_{V_{\mathcal{L}}}$$

Experiment Datasets

Simulated

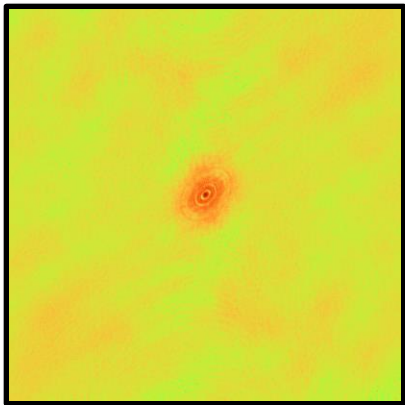


Sgr B2

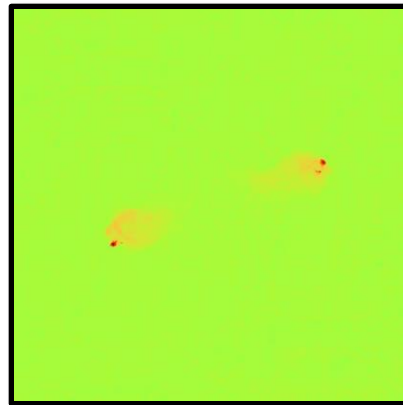


Sgr C

Real



HL Tau

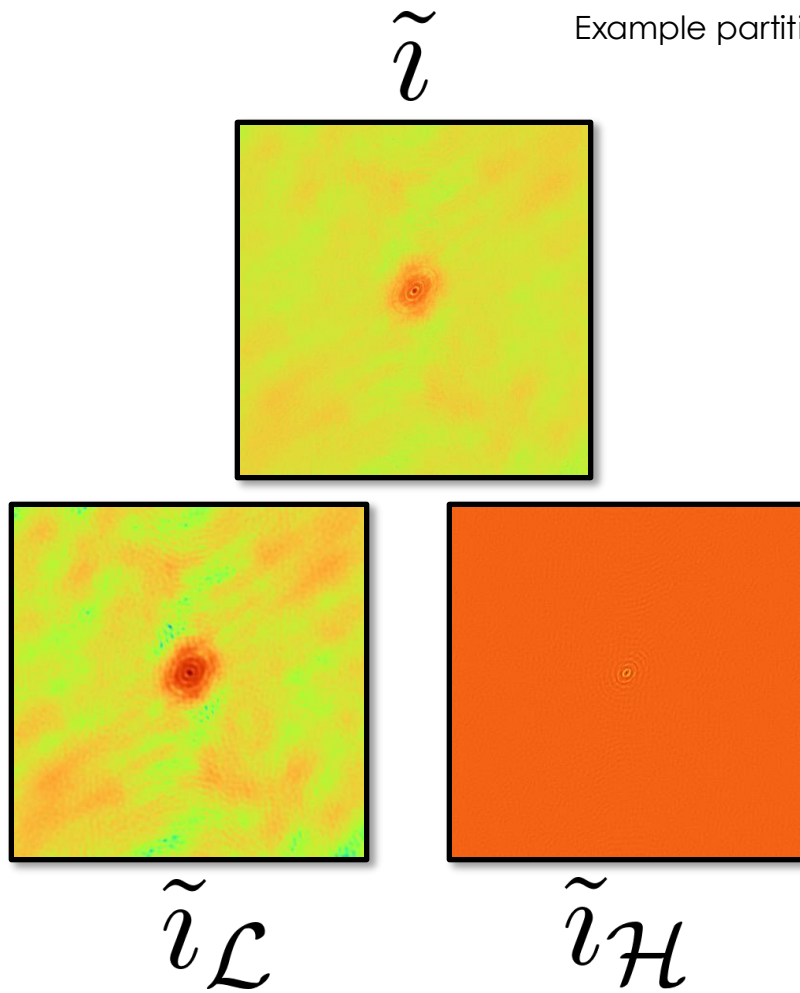


Cygnus A

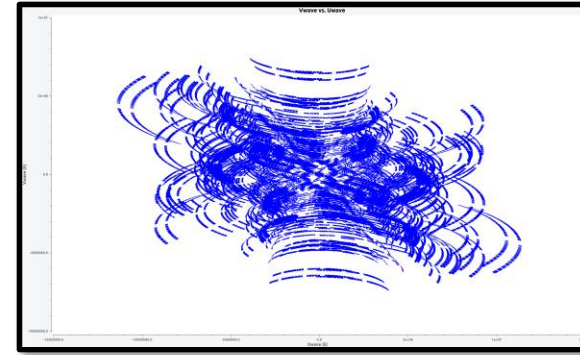
- Initial images tapered and cutout from 1.28GHz mosaic produced in [1]
- Visibilities generated with SKA-Mid AA4, and SKA-Low AA4 configurations
- Observation time of HA=[-2,2] with integration times of 30s, and 120s respectively, 1 channel at a pseudo-frequency of 1GHz
- Degrid to get visibility values
- Visibility noise artificially added (to be ~2% of average signal)
- Angular resolutions of 0.18" and 0.429" respectively
- Pixel resolutions of 512x512
- Pseudo declinations also used to vary uv-coverages (-35 and -50 respectively)

- Datasets taken from ALMA long baselines survey[2] and the VLA observation described in [3] for HL Tau and Cygnus A respectively
- ALMA Band 6 observation used for HL Tau (224.750GHz - 228.750GHz, 239.250 - 243.250 GHz, 4 spectral windows, 4 channels per spectral window, configuration 10)
- First spectral window (of 8) of VLA S-band used for Cygnus A (64 channels @ 1988.5 MHz – 2020.5 MHz, all 4 configurations)
- Angular resolutions of 0.005" and 0.125" respectively
- Pixel resolutions of 1500x1500 and 1728x1728 respectively

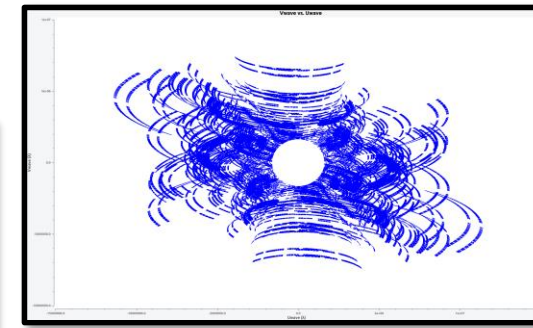
[1] Heywood, I., et al. "The 1.28 GHz MeerKAT galactic center mosaic." *The Astrophysical Journal* 925.2 (2022): 165.
[2] https://casaguides.nrao.edu/index.php/ALMA2014_LBC_SVDATA
[3] Sebokolodi, M. Lerato L., et al. "A Wideband Polarization Study of Cygnus A with the Jansky Very Large Array. I. The Observations and Data." *The Astrophysical Journal* 903.1 (2020): 36.



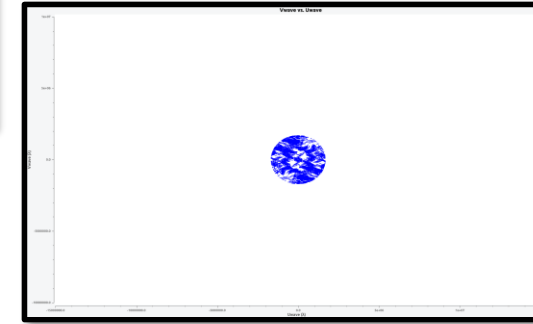
Example partition images are of the HL-Tau B6 dataset



V



$V_{\mathcal{H}}$



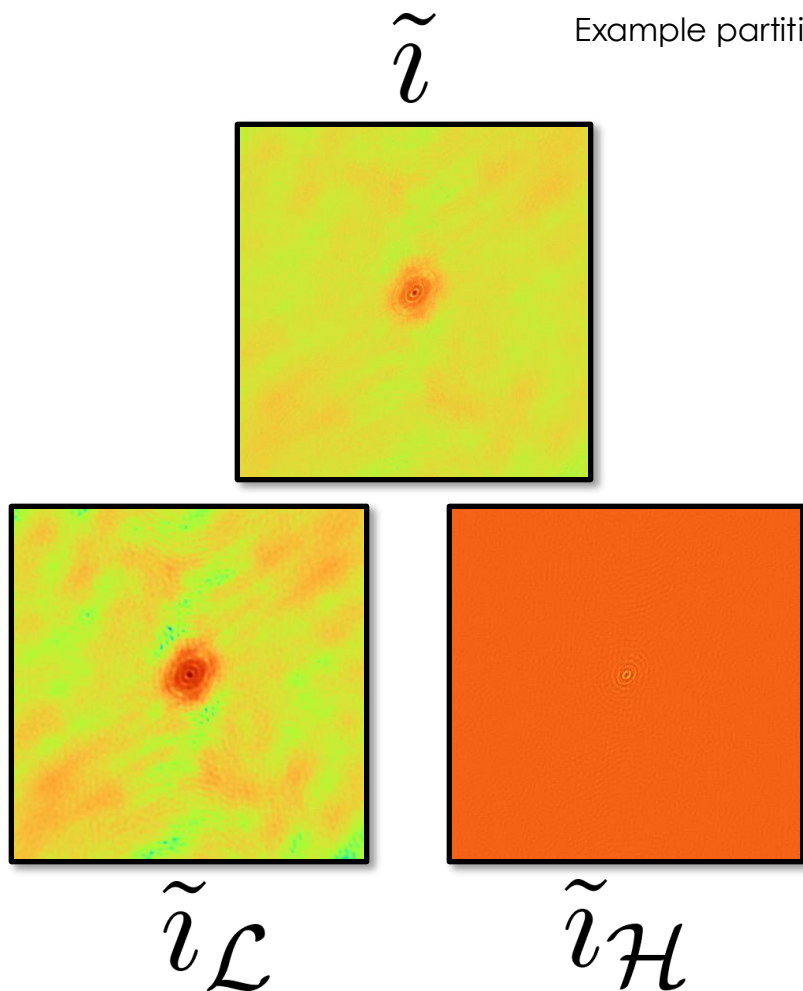
$V_{\mathcal{L}}$

Dataset	ℓ	$V_{\mathcal{L}}$	$V_{\mathcal{H}}$	$V_{\mathcal{L} \cap \mathcal{H}}$
Sgr B2	20	6.99M(.75)	2.53M(.27)	0.16M(.02)
Sgr C	25	9.05M(.57)	6.81M(.43)	0.11M(.01)
HL Tau	60	39.86M(.47)	46.24M(.54)	0.61M(.01)
Cygnus A	40	41.65M(.51)	41.83M(.51)	1.22M(.01)

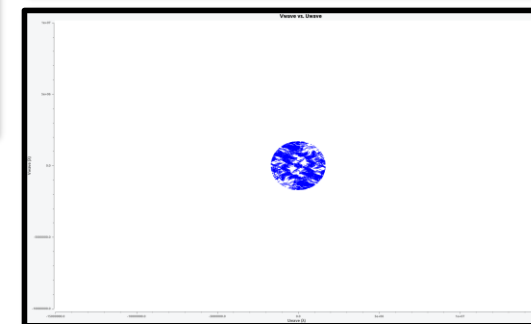
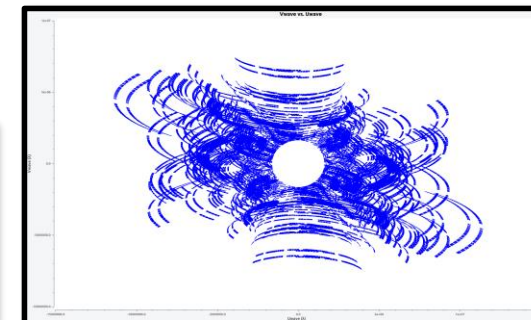
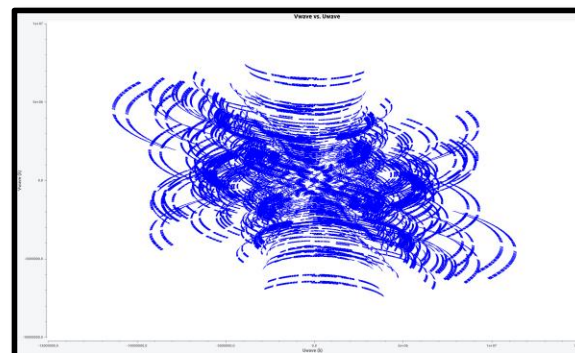
Dataset partitioning

- Ideally want to create partitions with equal number visibilities and similar amounts of spatial freq info
- Difficult for Sgr B2 dataset due to SKA-Mid AA4 array (BDA[1] or something similar may be needed)

Example partition images are of the HL-Tau B6 dataset



Dataset partitioning



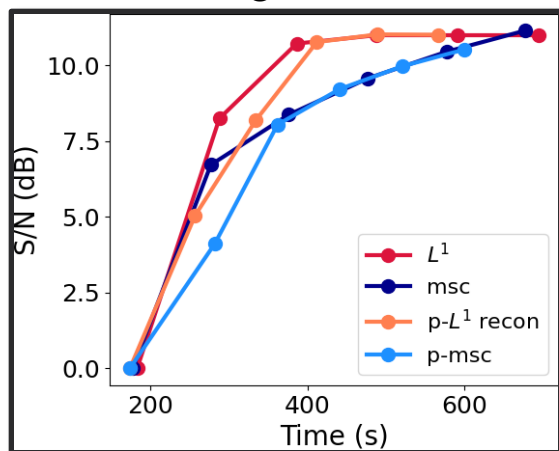
Dataset	ℓ	$V_{\mathcal{L}}$	$V_{\mathcal{H}}$	$V_{\mathcal{L} \cap \mathcal{H}}$
Sgr B2	20	6.99M(.75)	2.53M(.27)	0.16M(.02)
Sgr C	25	9.05M(.57)	6.81M(.43)	0.11M(.01)
HL Tau	60	39.86M(.47)	46.24M(.54)	0.61M(.01)
Cygnus A	40	41.65M(.51)	41.83M(.51)	1.22M(.01)

- Ideally want to create partitions with equal number visibilities and similar amounts of spatial freq info
- Difficult for Sgr B2 dataset due to SKA-Mid AA4 array (BDA[1] or something similar may be needed)

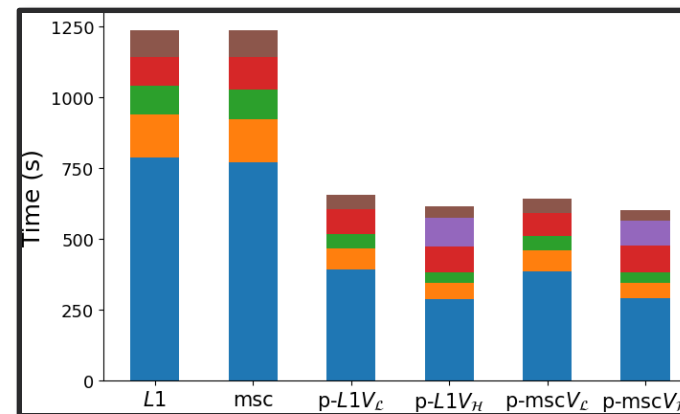
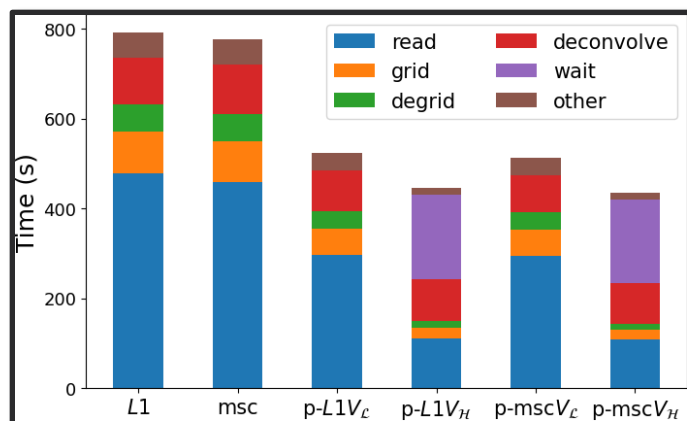
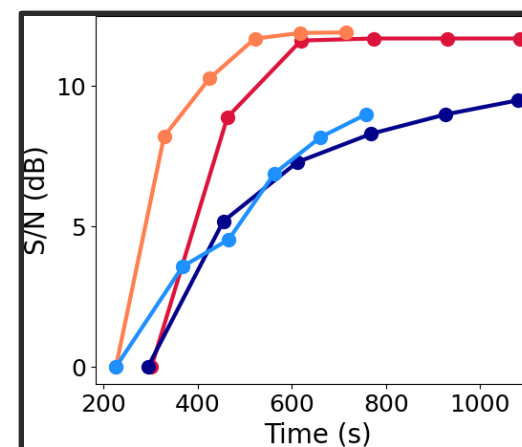
Results – Simulated

S/N obtained with comparison to ground truth

Sgr B2



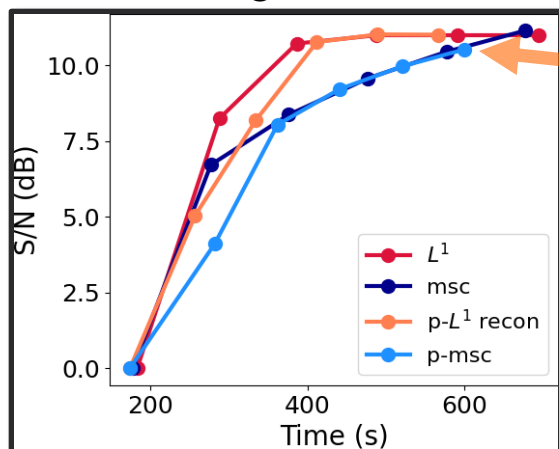
Sgr C



Results – Simulated

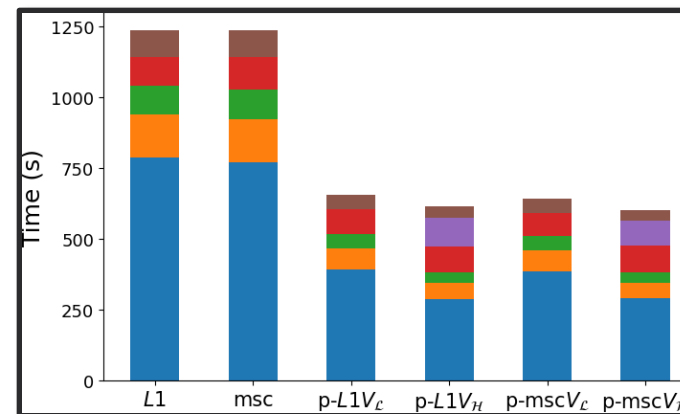
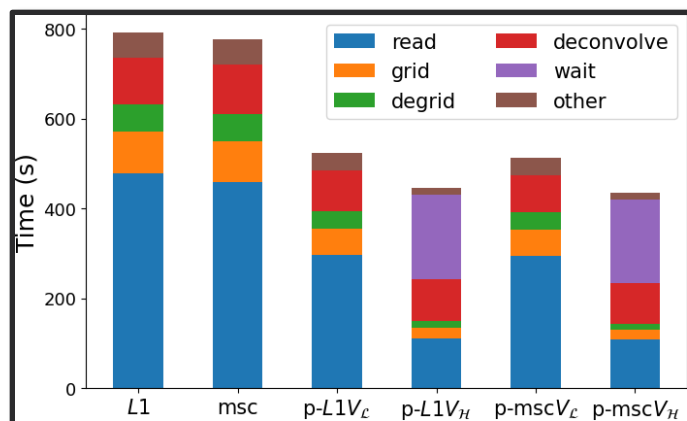
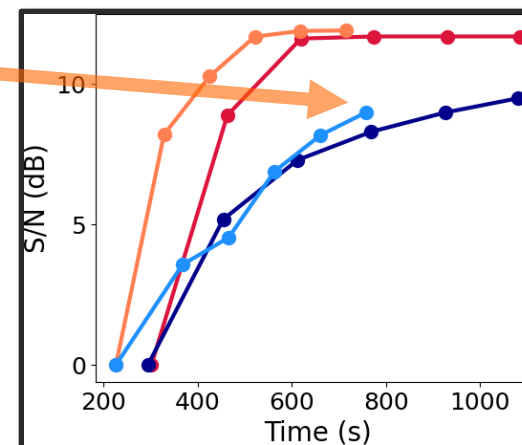
S/N obtained with comparison to ground truth

Sgr B2



Poor parallelization for Sgr B2, much better for Sgr C. Mainly due to uneven partitioning.

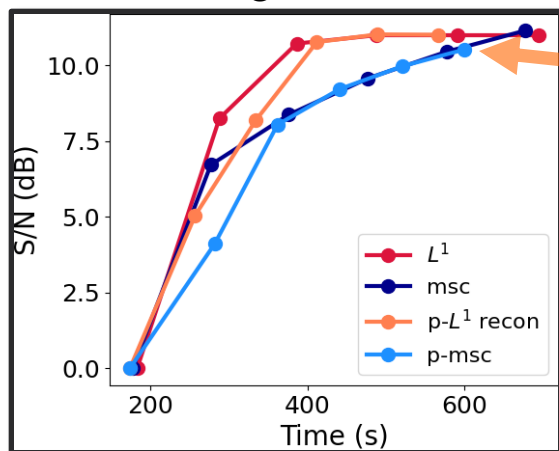
Sgr C



Results – Simulated

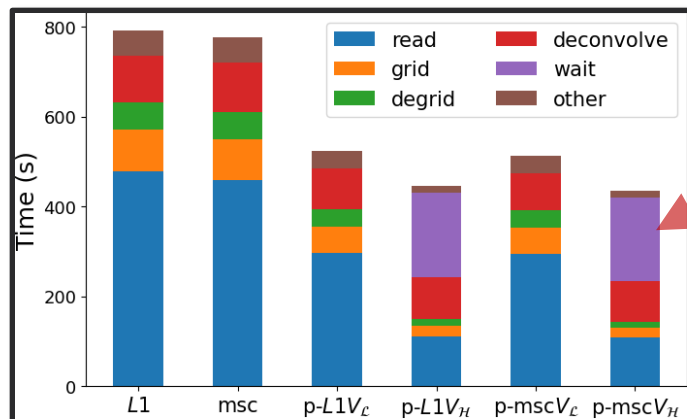
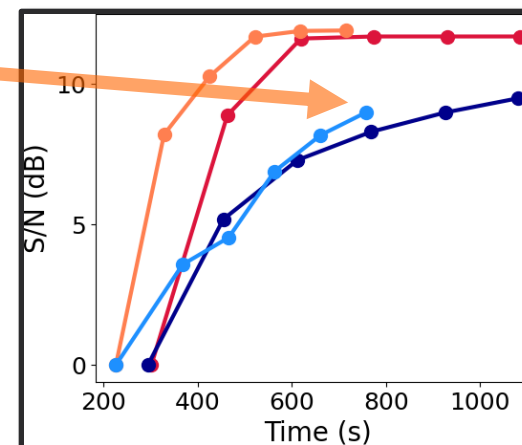
S/N obtained with comparison to ground truth

Sgr B2

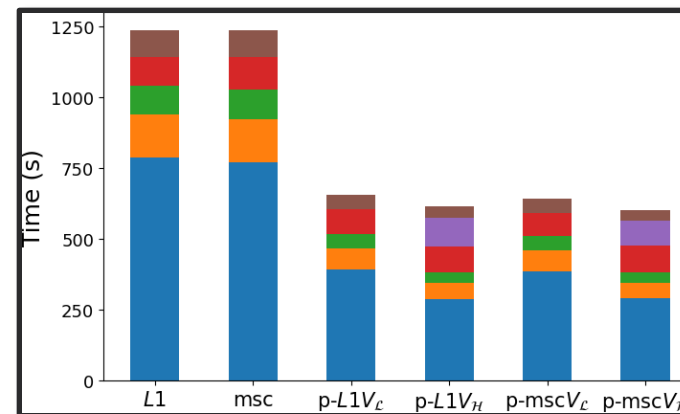


Poor parallelization for Sgr B2, much better for Sgr C. Mainly due to uneven partitioning.

Sgr C



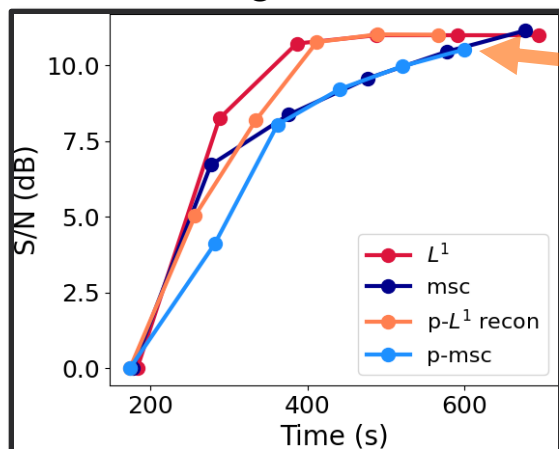
Poor partitioning causes a lot of idle time for node with less visibilities.



Results – Simulated

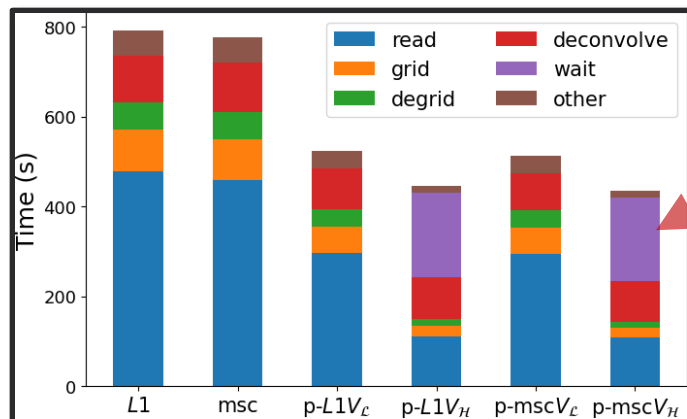
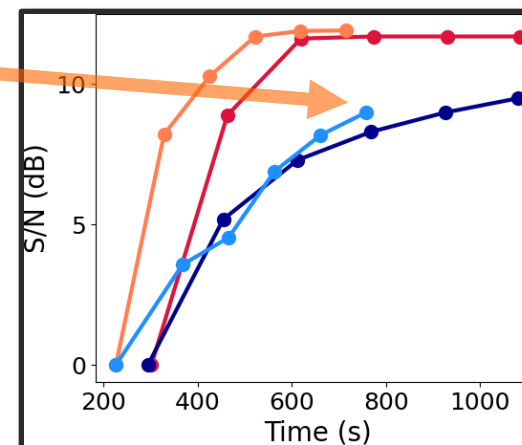
S/N obtained with comparison to ground truth

Sgr B2



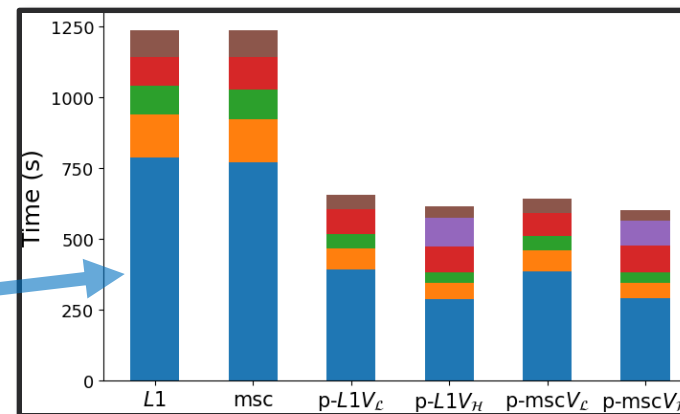
Poor parallelization for Sgr B2, much better for Sgr C. Mainly due to uneven partitioning.

Sgr C



Poor partitioning causes a lot of idle time for node with less visibilities.

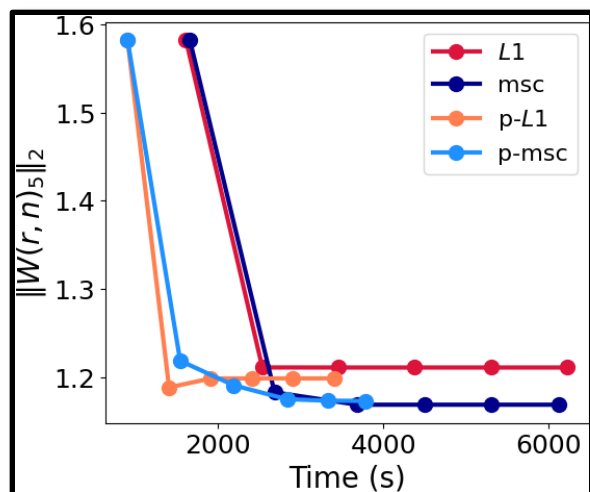
Read uses a lot of time due to implementation and RASCIL overhead



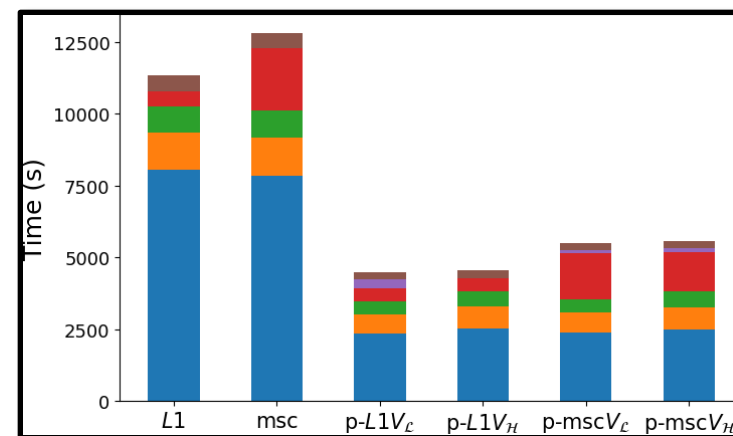
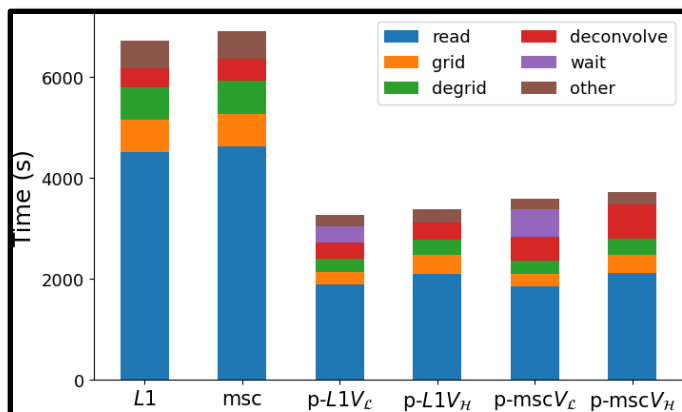
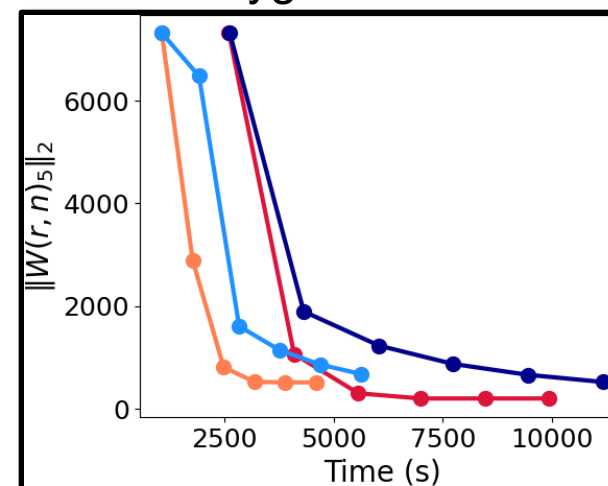
Results – Real

Wasserstein-1 distance between residual and ideal residual obtained via visibility negation. Computed per pixel (windowed), with L2 being plotted.

HL Tau



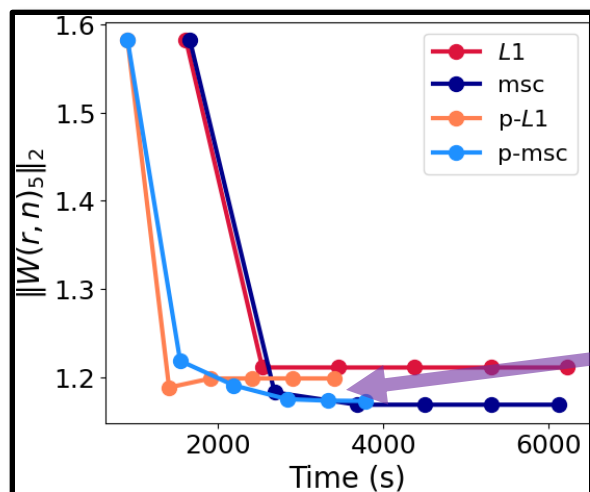
Cygnus A



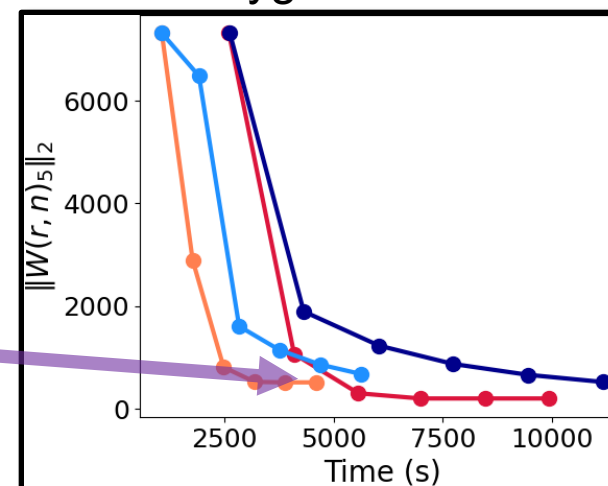
Results – Real

Wasserstein-1 distance between residual and ideal residual obtained via visibility negation. Computed per pixel (windowed), with L2 being plotted.

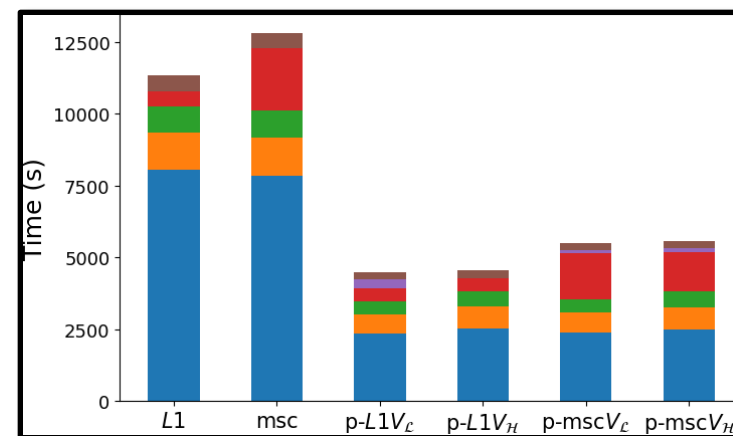
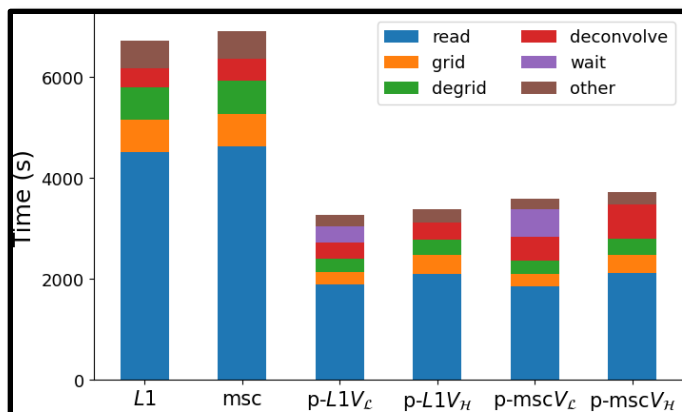
HL Tau



Cygnus A



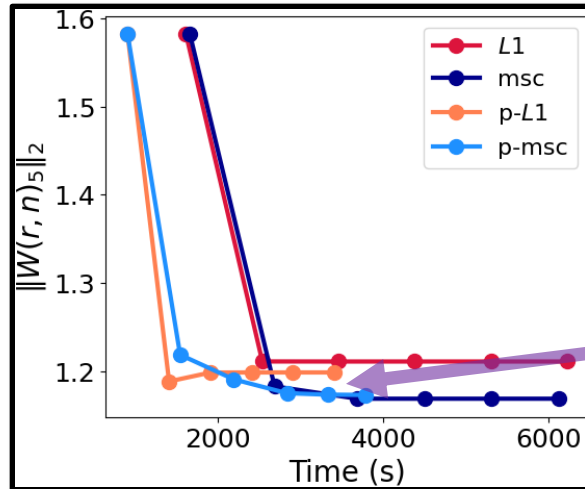
Speedup much better for real datasets, close to optimal 2x



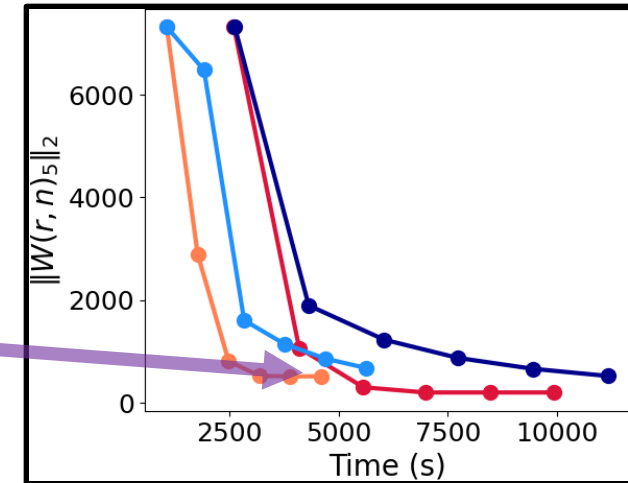
Results – Real

Wasserstein-1 distance between residual and ideal residual obtained via visibility negation. Computed per pixel (windowed), with L2 being plotted.

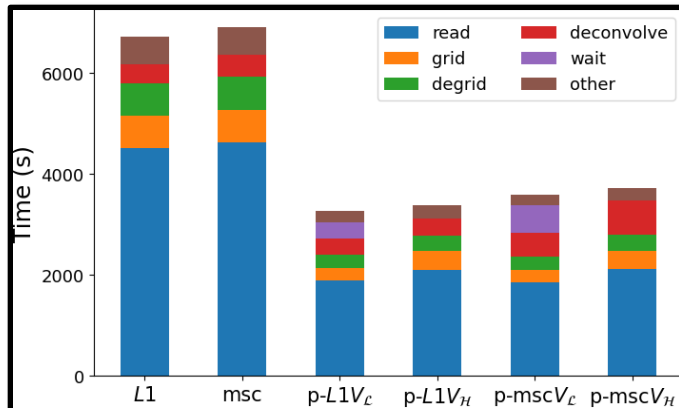
HL Tau



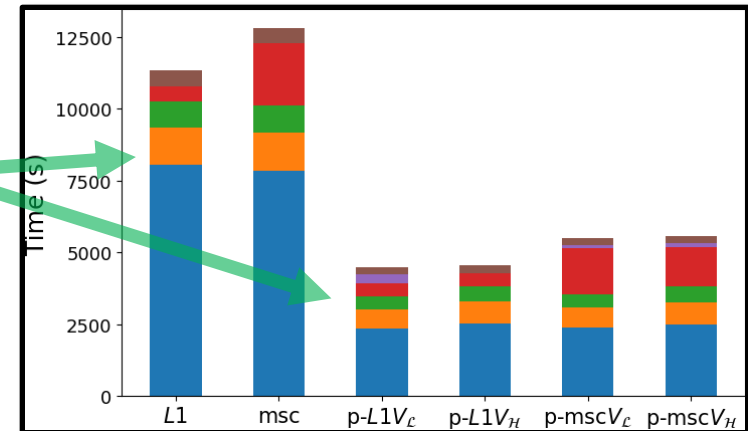
Cygnus A



Speedup much better for real datasets, close to optimal 2x



Over 2x speedup can be due to RASCIL overheads.



Results – Scaling to larger image sizes

Average processing times for Cygnus A dataset per major cycle

Alg.	Node	Pix. res.	Deconv.	Degridd	Grid	Disk I/O	Transf.	Other
p-msc	$V_{\mathcal{L}}$	1728×1728	354.70s	92.27s	117.21s	342.12s	0.01s	13.51s
	$V_{\mathcal{H}}$	1728×1728	288.83s	109.84s	129.62s	353.67s	0.01s	11.88s
	$V_{\mathcal{L}}$	$10k \times 10k$	17778.44s ($\times 50$)	1450.58s ($\times 16$)	2519.88s ($\times 21$)	358.31s ($\times 1$)	0.45s ($\times 52$)	21.35s ($\times 2$)
	$V_{\mathcal{H}}$	$10k \times 10k$	18014.80s ($\times 62$)	2159.66s ($\times 20$)	2533.84s ($\times 20$)	362.50s ($\times 1$)	0.67s ($\times 51$)	21.11s ($\times 2$)
p-L1	$V_{\mathcal{L}}$	1728×1728	91.66s	92.44s	111.52s	332.31s	0.02s	11.52s
	$V_{\mathcal{H}}$	1728×1728	89.33s	108.17s	126.85s	359.43s	0.02s	13.49s
	$V_{\mathcal{L}}$	$10k \times 10k$	3595.75s ($\times 39$)	1449.08s ($\times 16$)	2457.80s ($\times 22$)	365.53s ($\times 1$)	0.59s ($\times 30$)	20.16s ($\times 2$)
	$V_{\mathcal{H}}$	$10k \times 10k$	3573.73s ($\times 40$)	2173.30s ($\times 20$)	2555.44s ($\times 20$)	363.62s ($\times 1$)	0.60s ($\times 25$)	20.22s ($\times 1$)

Results – Scaling to larger image sizes

Average processing times for Cygnus A dataset per major cycle

Alg.	Node	Pix. res.	Deconv.	Degridd	Grid	Disk I/O	Transf.	Other
p-msc	V_L	1728×1728	354.70s	92.27s	117.21s	342.12s	0.01s	13.51s
	V_H	1728×1728	288.83s	109.84s	129.62s	353.67s	0.01s	11.88s
	V_L	$10k \times 10k$	17778.44s ($\times 50$)	1450.58s ($\times 16$)	2519.88s ($\times 21$)	358.31s ($\times 1$)	0.45s ($\times 52$)	21.35s ($\times 2$)
	V_H	$10k \times 10k$	18014.80s ($\times 62$)	2159.66s ($\times 20$)	2533.84s ($\times 20$)	362.50s ($\times 1$)	0.67s ($\times 51$)	21.11s ($\times 2$)
p-L1	V_L	1728×1728	91.66s	92.44s	111.52s	332.31s	0.02s	11.52s
	V_H	1728×1728	89.33s	108.17s	126.85s	359.43s	0.02s	13.49s
	V_L	$10k \times 10k$	3595.75s ($\times 39$)	1449.08s ($\times 16$)	2457.80s ($\times 22$)	365.53s ($\times 1$)	0.59s ($\times 30$)	20.16s ($\times 2$)
	V_H	$10k \times 10k$	3573.73s ($\times 40$)	2173.30s ($\times 20$)	2555.44s ($\times 20$)	363.62s ($\times 1$)	0.60s ($\times 25$)	20.22s ($\times 1$)

Primary bottlenecks seem to be deconvolution and de/gridding (to a lesser extent).

Results – Scaling to larger image sizes

Average processing times for Cygnus A dataset per major cycle

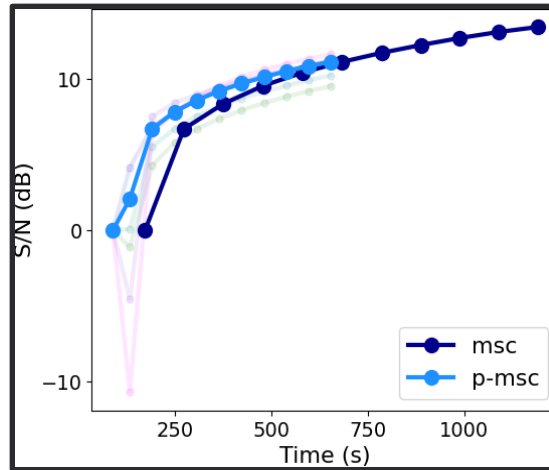
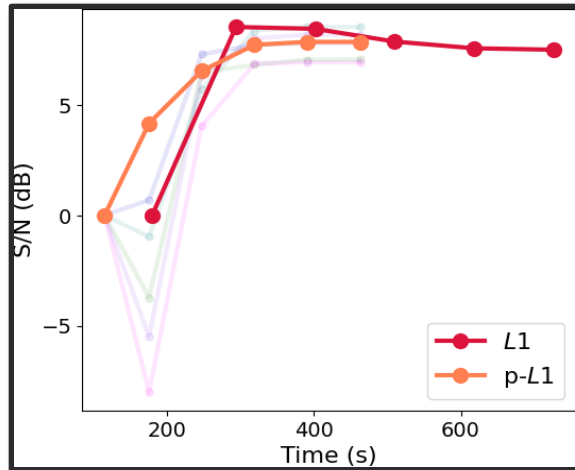
Alg.	Node	Pix. res.	Deconv.	Degrad	Grid	Disk I/O	Transf.	Other
p-msc	V_L	1728×1728	354.70s	92.27s	117.21s	342.12s	0.01s	13.51s
	V_H	1728×1728	288.83s	109.84s	129.62s	353.67s	0.01s	11.88s
	V_L	$10k \times 10k$	17778.44s ($\times 50$)	1450.58s ($\times 16$)	2519.88s ($\times 21$)	358.31s ($\times 1$)	0.45s ($\times 52$)	21.35s ($\times 2$)
	V_H	$10k \times 10k$	18014.80s ($\times 62$)	2159.66s ($\times 20$)	2533.84s ($\times 20$)	362.50s ($\times 1$)	0.67s ($\times 51$)	21.11s ($\times 2$)
p-L1	V_L	1728×1728	91.66s	92.44s	111.52s	332.31s	0.02s	11.52s
	V_H	1728×1728	89.33s	108.17s	126.85s	359.43s	0.02s	13.49s
	V_L	$10k \times 10k$	3595.75s ($\times 39$)	1449.08s ($\times 16$)	2457.80s ($\times 22$)	365.53s ($\times 1$)	0.59s ($\times 30$)	20.16s ($\times 2$)
	V_H	$10k \times 10k$	3573.73s ($\times 40$)	2173.30s ($\times 20$)	2555.44s ($\times 20$)	363.62s ($\times 1$)	0.60s ($\times 25$)	20.22s ($\times 1$)

Primary bottlenecks seem to be deconvolution and de/gridding (to a lesser extent).

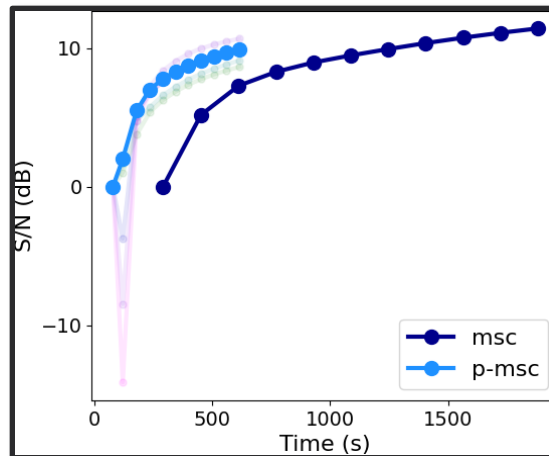
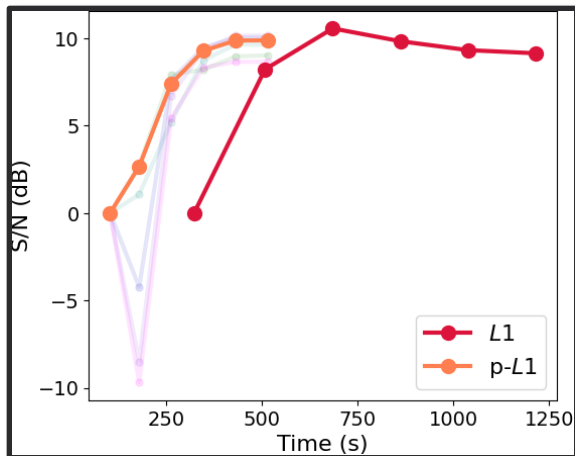
Transfer time also increases similarly to deconvolution, but cost negligible. Even for 100kx100k images, with the current cost increases, a transfer only takes ~72s which is substantially less than even the 10kx10k deconvolution.

Results – 5 partitions on simulated

Sgr B2



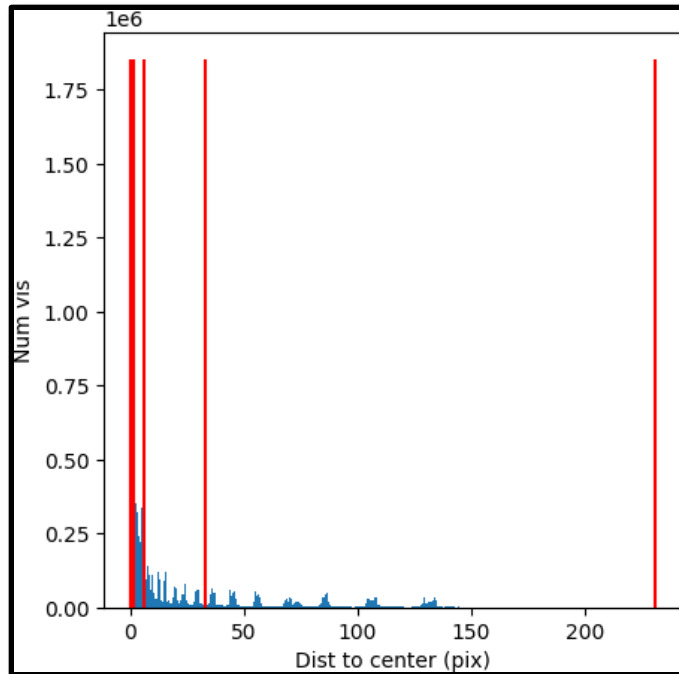
Sgr C



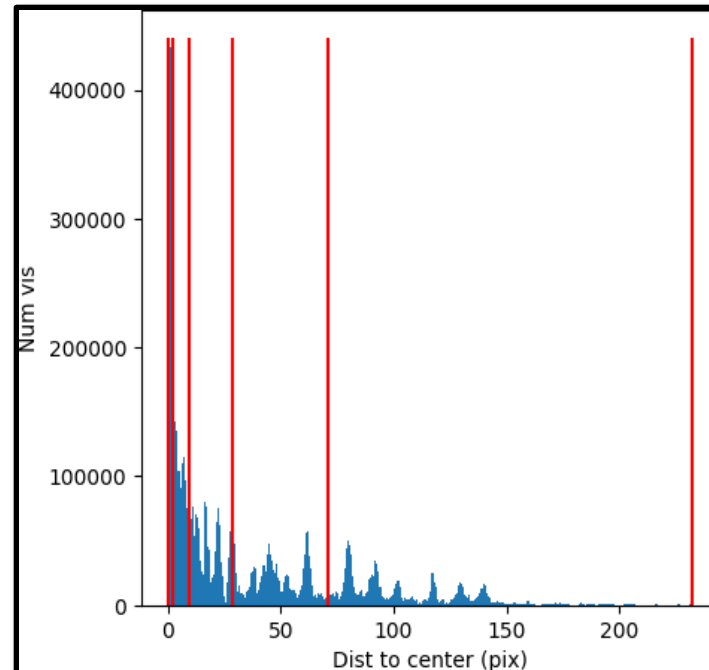
- Partition configurations
 - Cuts made at <4, 2-11, 9-36, 34-71, >69
 - Visibilities per partition for Sgr B2: 4710396, 2569876, 1565927, 922346, 942517
 - Visibilities per partition for Sgr C: 4196451, 3975415, 3910825, 2742692, 3152216
- Total processing times:
 - Sgr B2:
 - 726.66s (serial) vs 462.46s (parallel) for l1 after 5 major cycles
 - 1192.22s (serial) vs 654.69s (parallel) for msc after 10 major cycles
 - Sgr C:
 - 1215.17s (serial) vs 514.02s (parallel) for l1 after 5 major cycles
 - 1880.88s (serial) vs 615.99s (parallel) for msc after 10 major cycles
- 1.57x (l1) and 1.82x (msc) speedup for Sgr B2
- 2.36x (l1) and 3.05x (msc) speedup for Sgr C

Short-baselines density problem

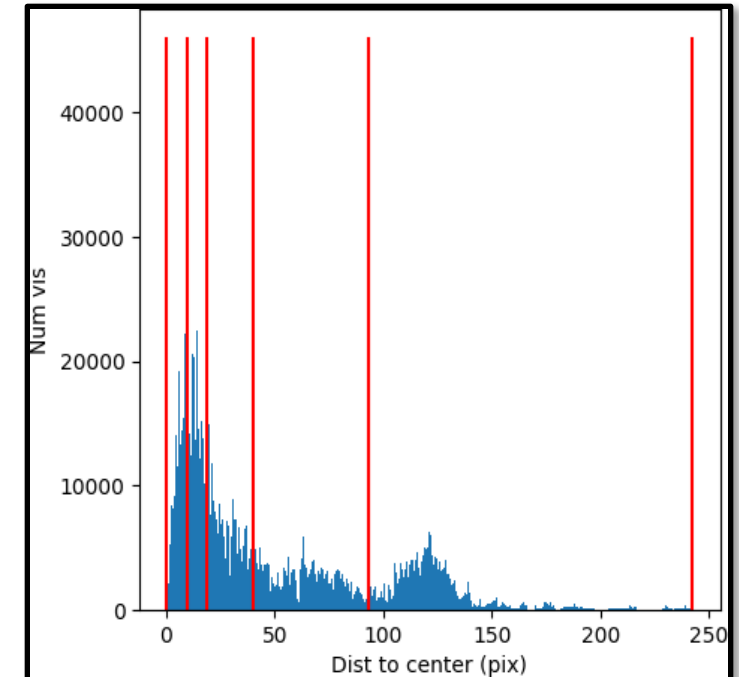
SKA AA4 Mid



SKA AA4 Low



Meerkat



Baseline Dependent Averaging

Baseline dependent averaging (BDA)[1] averages visibilities based on decorrelation.

- Shorter baselines -> less decorrelation
- Evens out visibility distributions

Time and frequency decorrelation

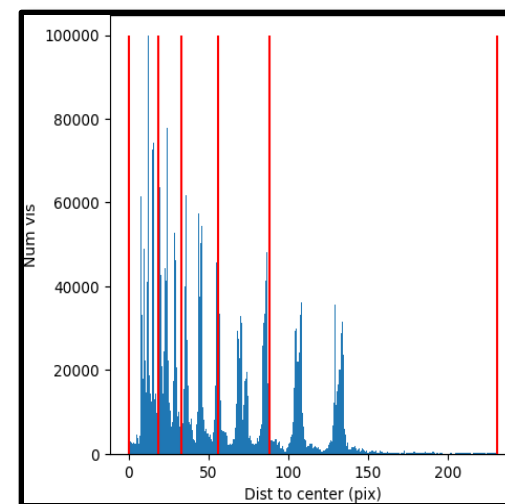
$$\rho_{total} = \rho_t \times \rho_f$$

$$\rho_t = 1 - \frac{\pi^2 T^2}{6} \left(\frac{du}{dt} l + \frac{dv}{dt} m \right)^2$$

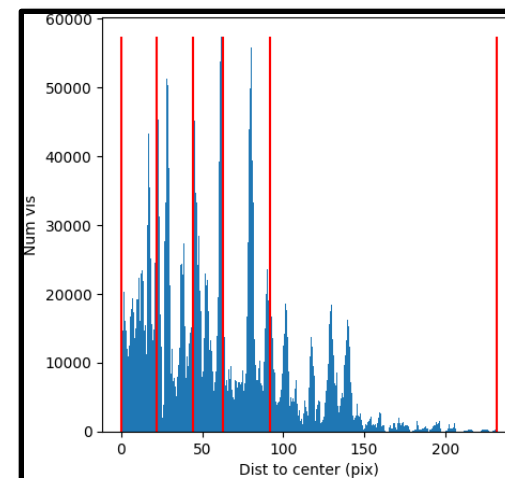
$$\rho_f = \left\| \text{sinc}\left(\frac{\pi \Delta \nu \tau_g}{2}\right) \right\|$$

Visibilities averaged with
 $\max(\rho_{total}) = 0.99$

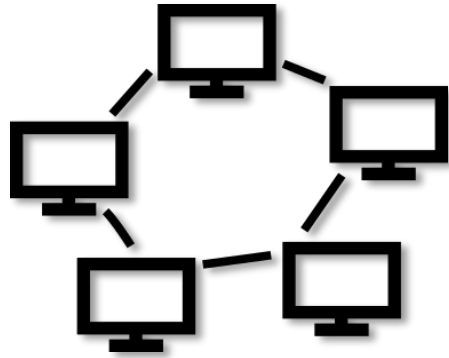
SKA AA4 Mid



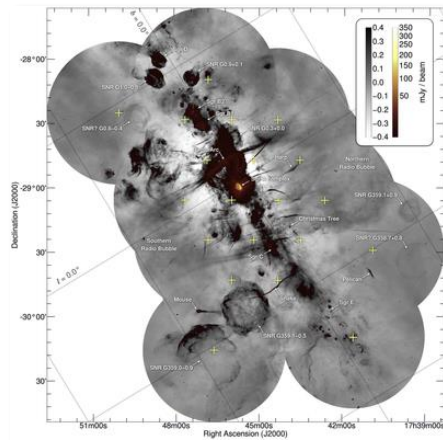
SKA AA4 Low



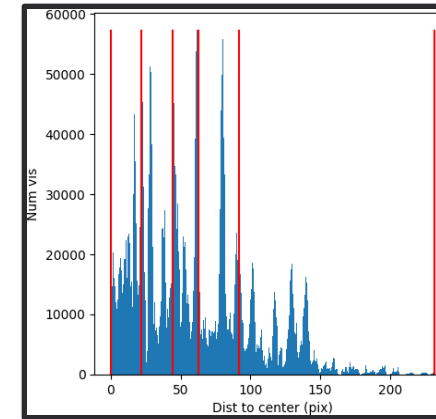
Future Work



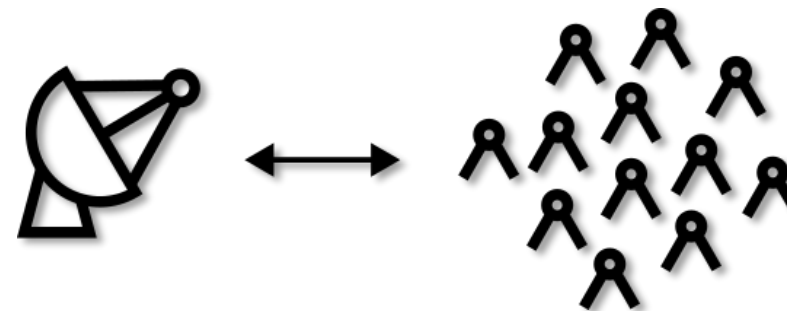
More complex network topologies



Reconstruct very large images (32k x 32k – 100k x 100k), image source[1]



Incorporate BDA

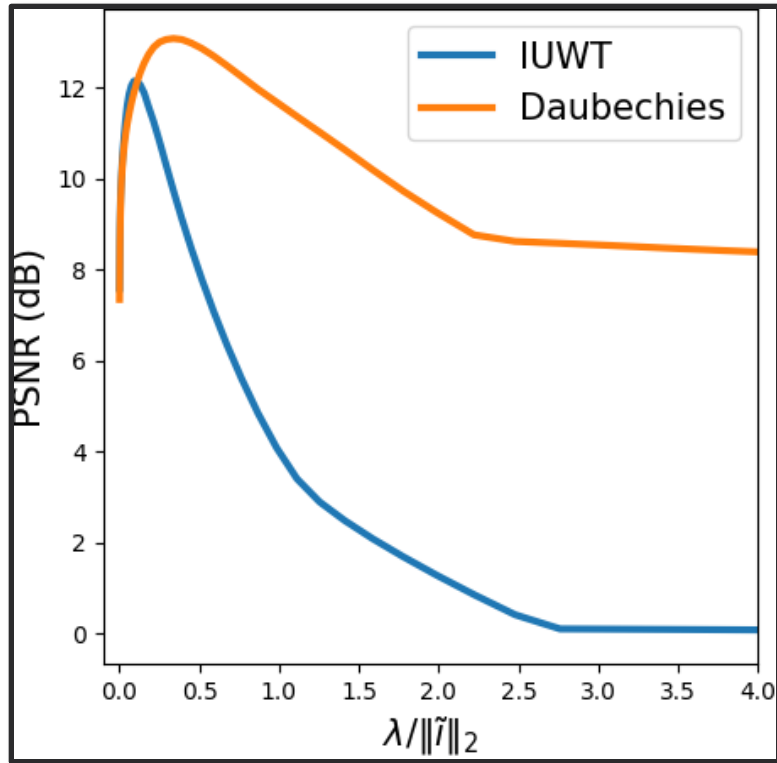


Reconstruct single-dish + interferometric



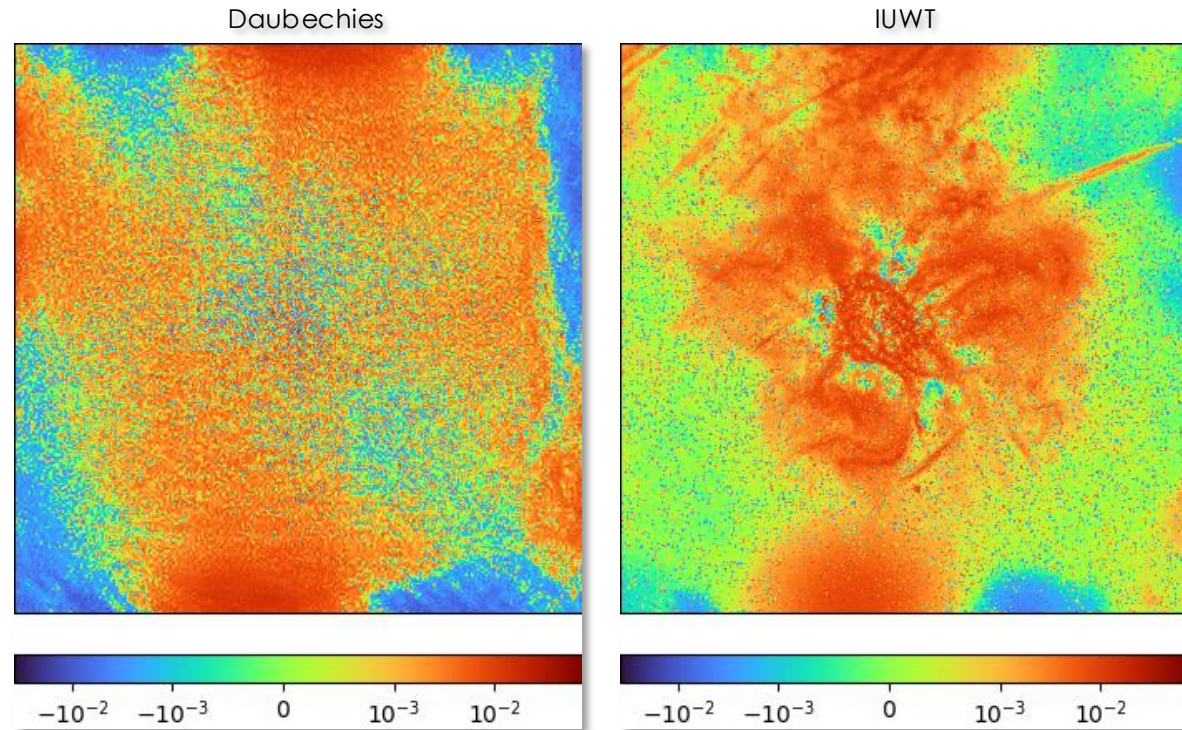
Appendices

IUWT vs Daubechies

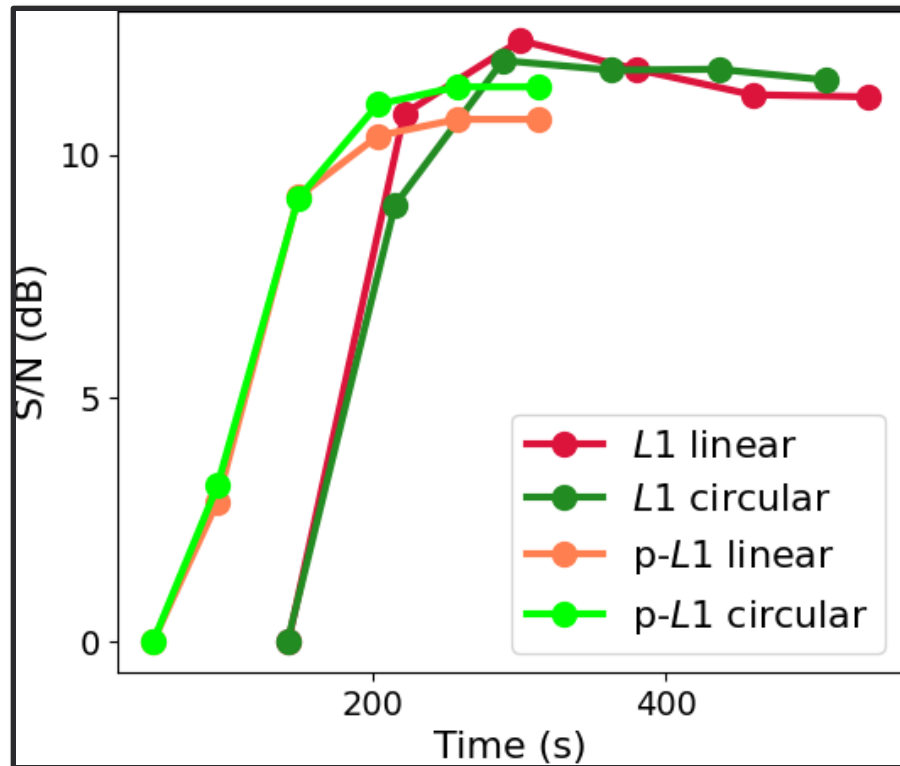


IUWT seems worse at reconstructing large-scale anisotropic extended emissions.

First major-cycle residuals for Sgr A



Linear vs circular convolution



- Using linear convolution instead of circular can be desired so that bright extended sources don't wrap around.
- More complicated to find the step size as operator does not diagonalize with Fourier transform, have to rely on something like power iteration.
- Results don't necessarily seem better as shown on the left.
- More expensive to compute

Filters

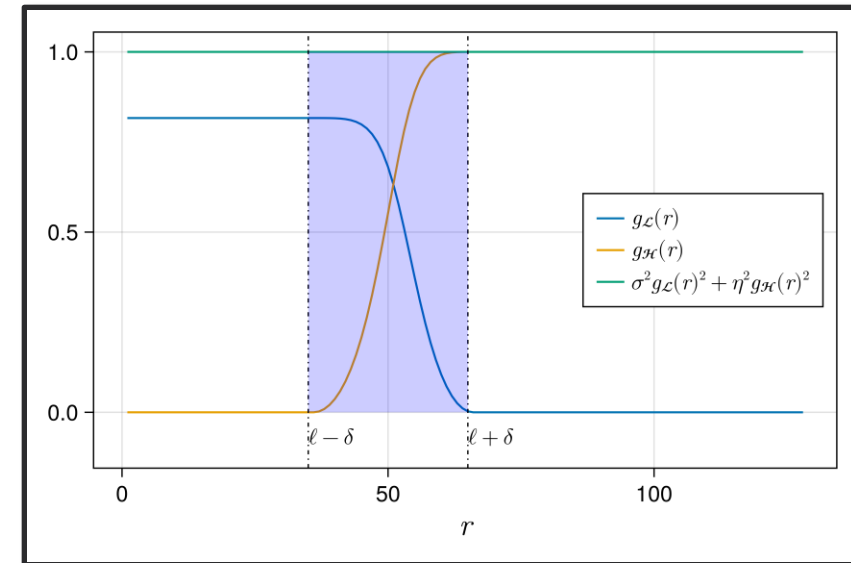
$$r > \ell + \delta : |g_{\mathcal{H}}(r)|^2 = 1/\sigma^2, g_{\mathcal{L}}(u) = 0$$

$$r < \ell - \delta : g_{\mathcal{H}}(r) = 0, |g_{\mathcal{L}}(r)|^2 = 1/\eta^2$$

$$\ell - \delta < r < \ell + \delta : \sigma^2 |g_{\mathcal{H}}(r)|^2 + \eta^2 |g_{\mathcal{L}}(r)|^2 = 1$$

$$g_{\mathcal{L}}(r) = \alpha(r) \left(1 - \sin \left(\frac{\pi}{2\delta} (r - \ell) \right) \right)$$

$$g_{\mathcal{H}}(r) = \alpha(r) \left(1 + \sin \left(\frac{\pi}{2\delta} (r - \ell) \right) \right)$$



- 1-D filters used as distance in 2-D, resulting in an annulus
- Filters have hard cut-off in Fourier domain, may result in either oscillations or infinite support in spatial domain
- Testing with windowed-sinc and Parks-McClellan, no conclusive results yet, but preliminary experiments suggest no large difference.

Selection of λ

Preliminary results suggested that lambda should be normalized by the norm of the image, and be increased as the major-cycles progress to maximize S/N. We use:

$$\lambda_{\mathcal{L}_n} = 0.05 \|\tilde{i}_{\mathcal{L}_n}\|_2 \times 2^n$$

$$\lambda_{\mathcal{H}_n} = 0.05 \|\tilde{i}_{\mathcal{H}_n}\|_2 \times 2^n$$

$$\lambda_n = 0.01 \|\tilde{i}_n\|_2 \times 2^n$$

The above strategy no longer works well for larger numbers of partitions. For this case, and onwards, For the multipartition problem:

$$\|G_j(\tilde{i} - HW\alpha)\|^2 + \sum_{\substack{i=1 \\ i \neq j}} \|G_i C_i - W\alpha\|^2 + \lambda \|W\alpha\|_1$$

We use:

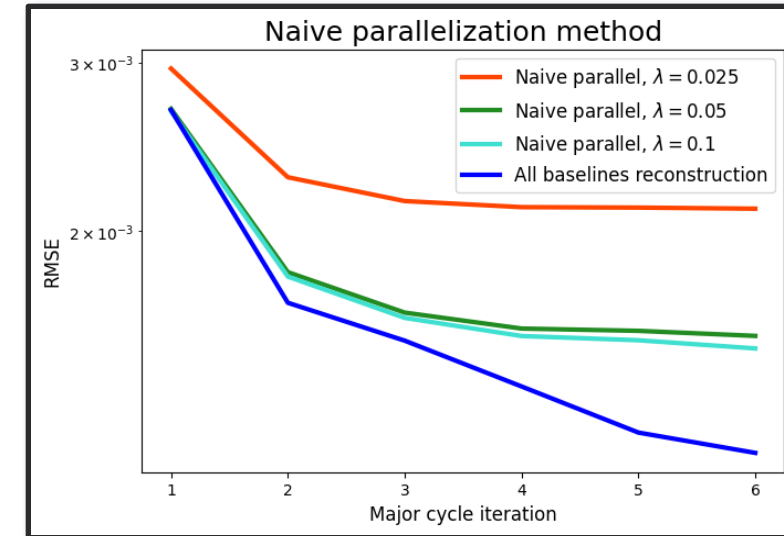
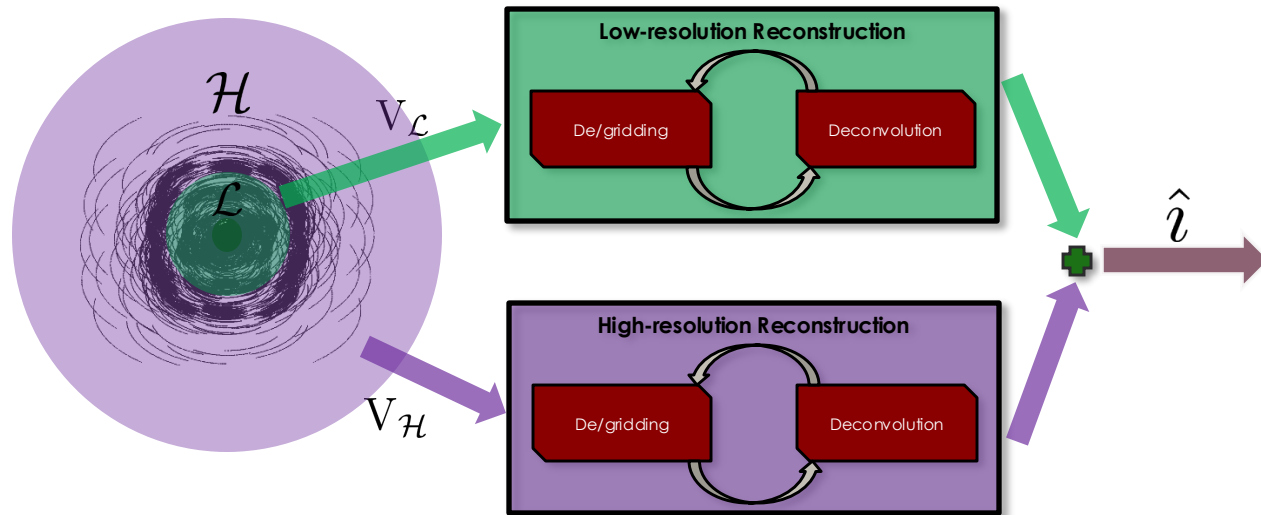
$$\lambda_n = \eta_n \lambda_{max_n}$$

$$\eta_n = \alpha + (1 - \alpha) \frac{e^{\beta t_n} - 1}{e^{\beta} - 1}$$

$$t_n = \frac{n}{N - 1}$$

$$\lambda_{max_n} = 2 \|W^\dagger (H_j^\dagger G_j^\dagger G_j \tilde{i}_{n_j} + \sum_{i=1, i \neq j} G_i^\dagger G_i C_{n_i})\|_\infty$$

Naively adding separately deconvolved images

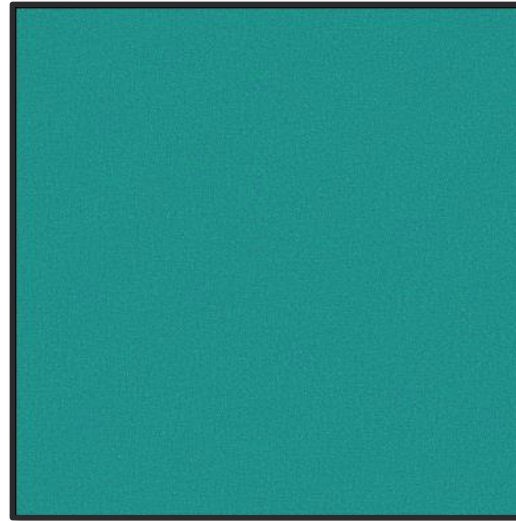


- Naïve parallel reconstructions seem always worse.
- Possibly due to terms not regularized together, which introduces some assumptions on sparsity.
- Can probably tune lambda so that the same result is obtained, but unclear how.

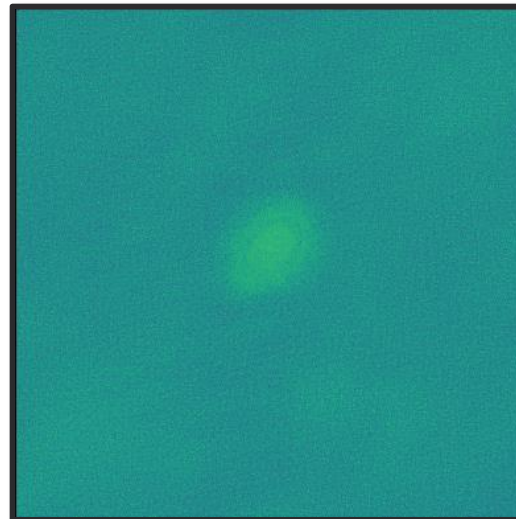
Evaluating on real datasets

- Reference residual obtained by randomly negating half of the visibilities
- Residual after imaging compared to reference statistically in a per-pixel manner
- 5x5 sliding window used as only 1 realization of imaging residual
- Wasserstein-1 distance used for statistical test
- L2 norm of Wasserstein distances used as final metric

Reference residual



Imaging residual



Wasserstein-1 distances using 5x5 sliding window

