

Higher Order Statistics for Neutral Hydrogen Intensity Mapping

Pauline Gorbachev

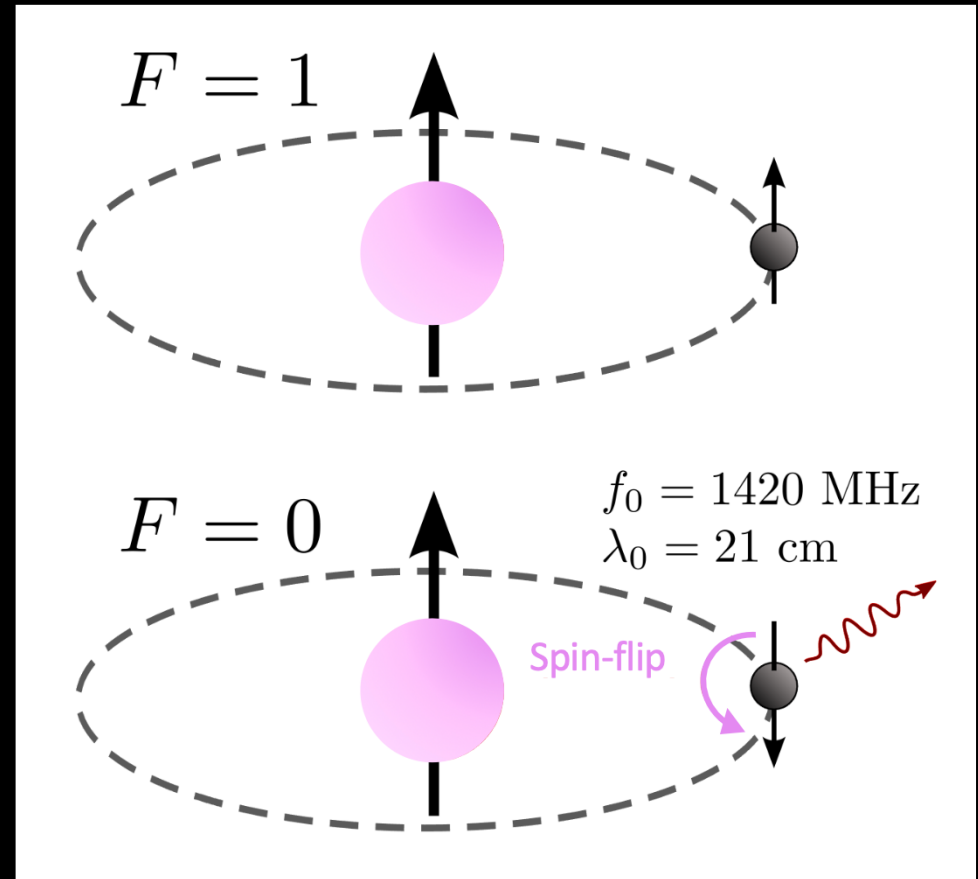
2025 Joint ARGOS-TITAN-TOSCA workshop



Physical background

- Hydrogen: most abundant element in the Universe.
- After reionization, HI is located inside galaxies.

⇒ **biased tracer** of the underlying **matter distribution** of the Universe.



HI hyperfine transition

Why using 21cm line ?

Benefits:

- Can be **measured from earth** (penetrates the atmosphere).
- thermal noise in HI surveys is less important than shot noise in galaxy surveys $\Rightarrow$ HI analysis is **more constraining than galaxies**.

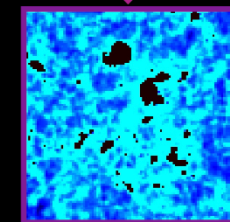
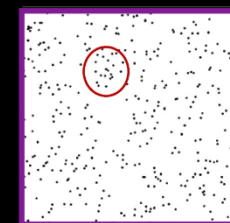
Uses:

- Reconstruct **DM density fields**.
- **Map 3D Large Scale Structures** of the Universe.
- Complementary measurement to optical surveys to **constrain cosmological parameters**.

What is Intensity Mapping?

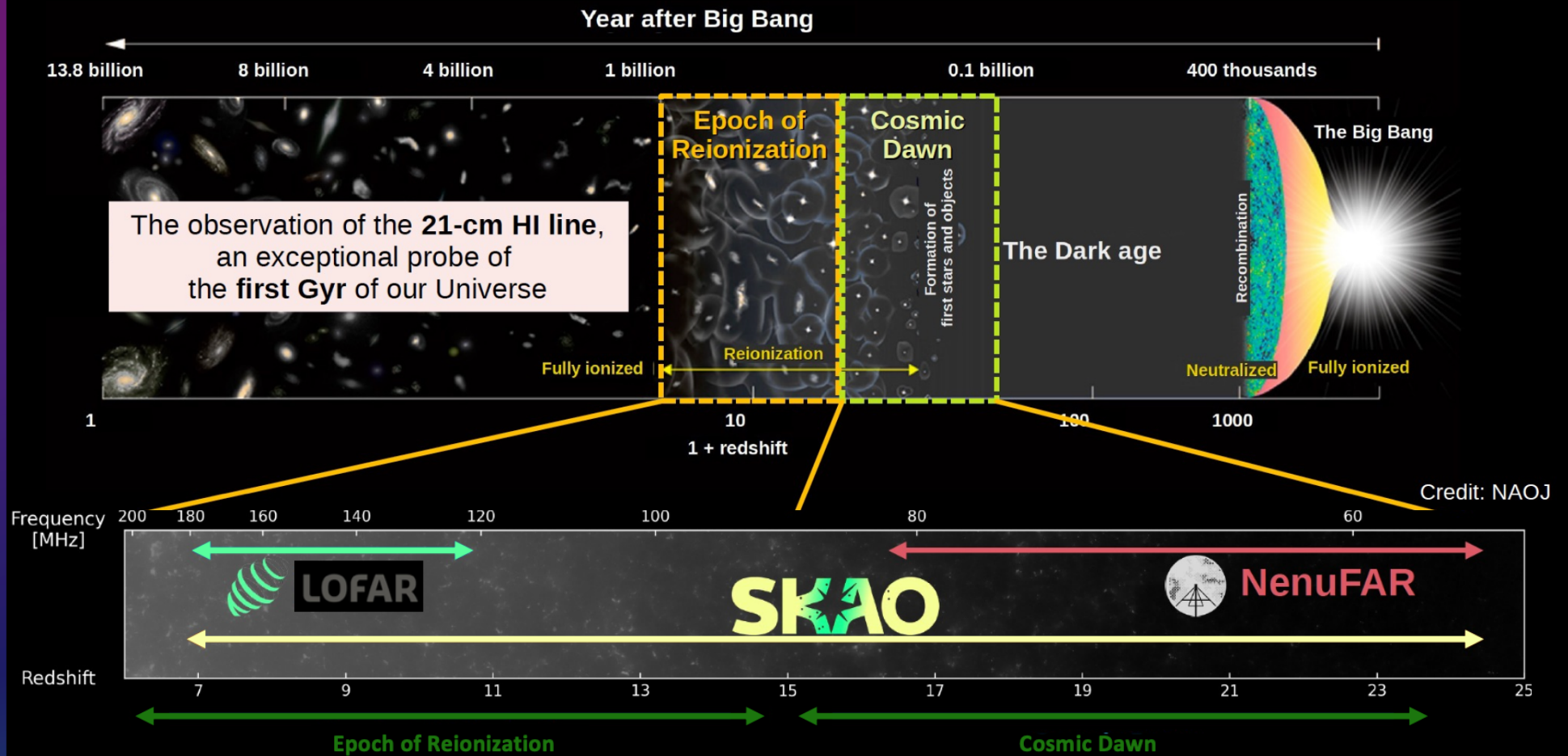
- Measurement of redshift and intensity of HI over the **whole sky**.
- Treats HI signal as a **diffuse background**.
- Large cosmological volume.
- Less costly, less time consuming.
- High spectral resolution $\Rightarrow$ **high redshift resolution**.
- Individual galaxy detection not needed for LSS study.

Galaxy distribution



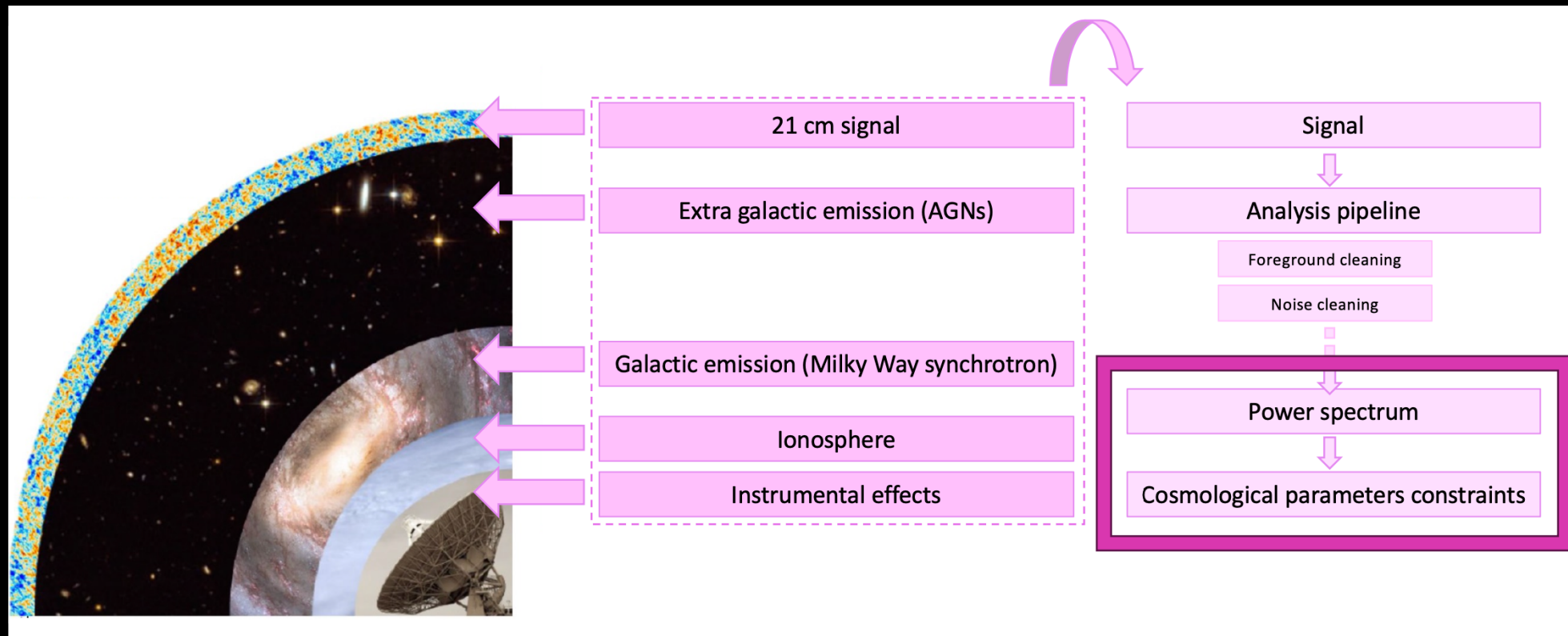
Intensity map

State of the Art for HI IM



Measurements scheme

Credits: :Marta Spinelli



Limitations of the power spectrum

- **Gaussian Assumption:**
 - The power spectrum is most effective for Gaussian random fields.
- **Non-Gaussian Features:**
 - The universe exhibits non-Gaussian features due to non-linear growth of structures and primordial non-Gaussianities.
- **Loss of Information:**
 - Higher order interactions and complex structures are not captured by the power spectrum.
 - Important information about the morphology and connectivity of cosmic structures is lost.

Make use of Higher order statistics which are sensitive to the non-Gaussianities.

Lognormal simulations

CAMB + GLASS

Input parameters: Ω_c , A_s and h (Ω_b fixed)

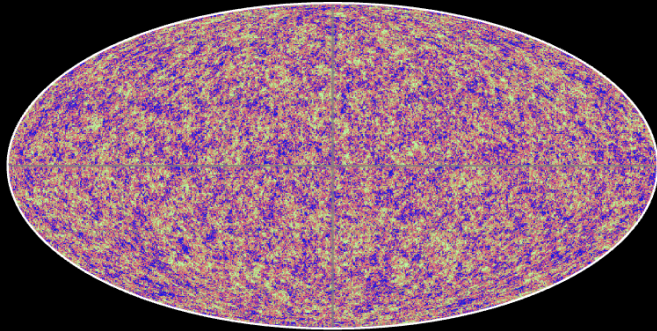
Different realizations (seed)

Option of adding **beam** and/or **noise** (MeerKLASS-like)

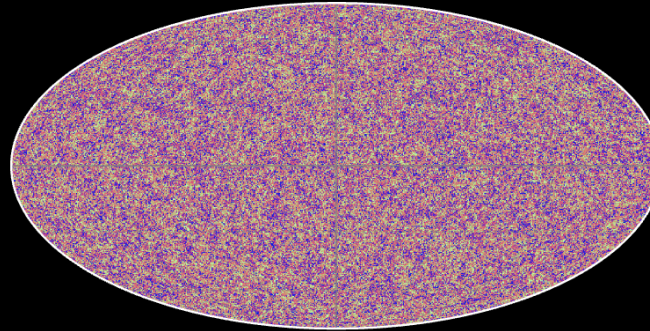
Output: Full sky HI brightness Temperature map of resolution 1024

Maps across cosmologies

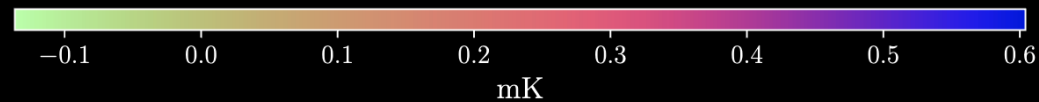
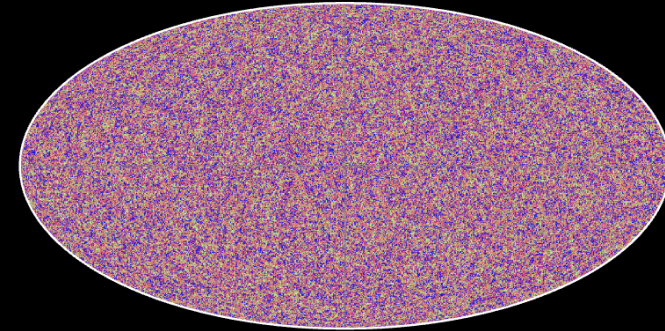
$h = 0.55, A_s = 1.0 \times 10^{-9}, \Omega_c = 0.15$



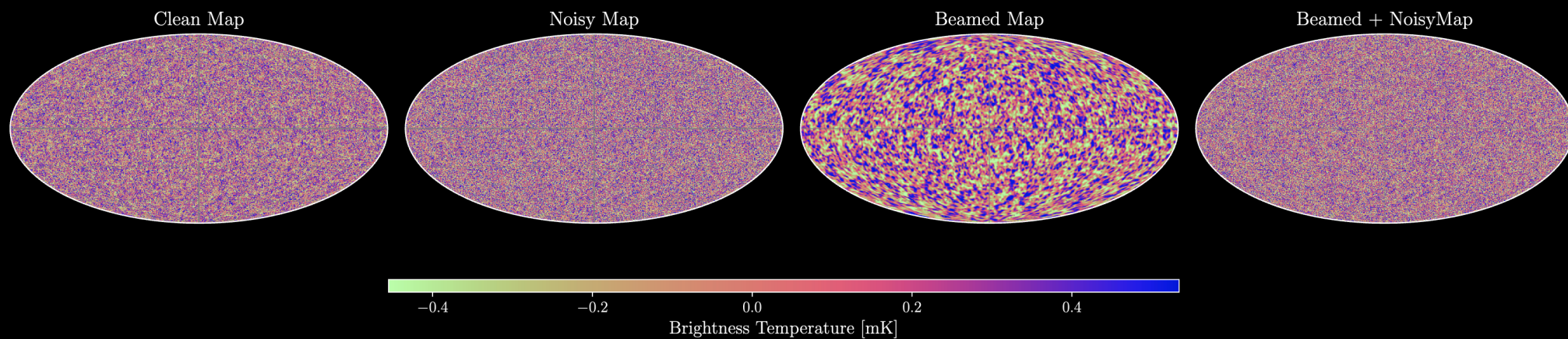
$h = 0.70, A_s = 2.0 \times 10^{-9}, \Omega_c = 0.25$



$h = 0.85, A_s = 3.0 \times 10^{-9}, \Omega_c = 0.35$

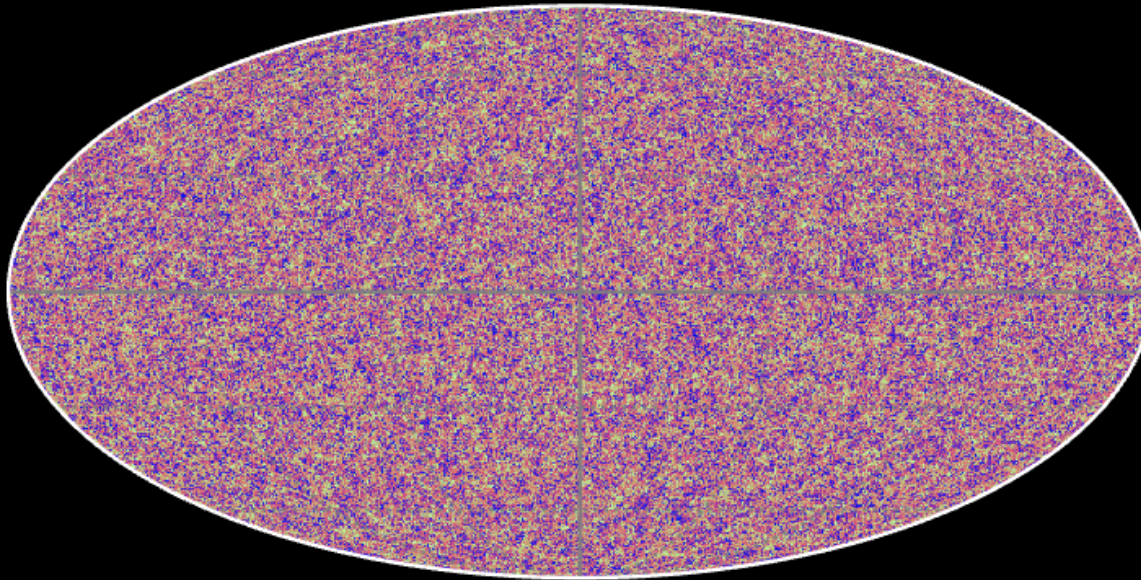


Instrumental effects



Starlet transform

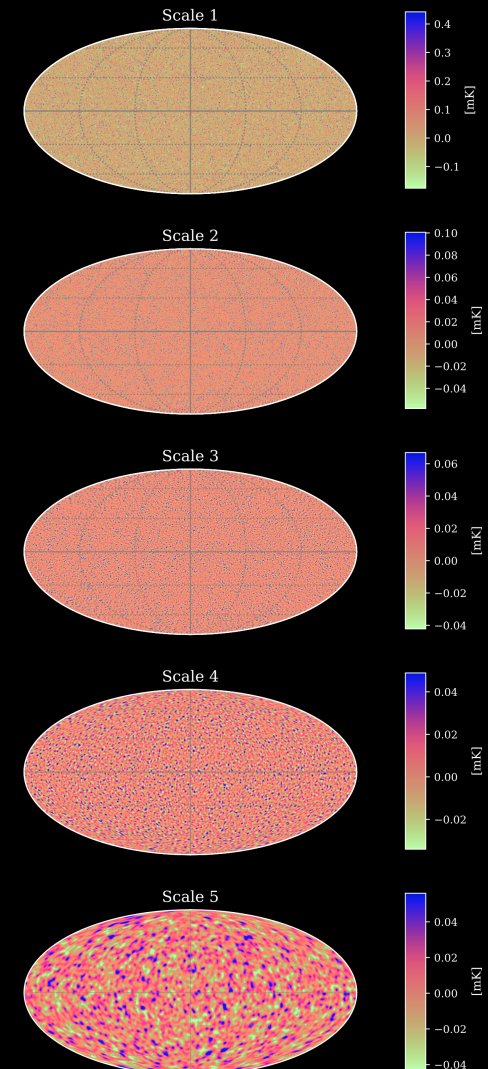
Clean Map



Decomposes the map into a set of wavelet coefficients + coarse residual map

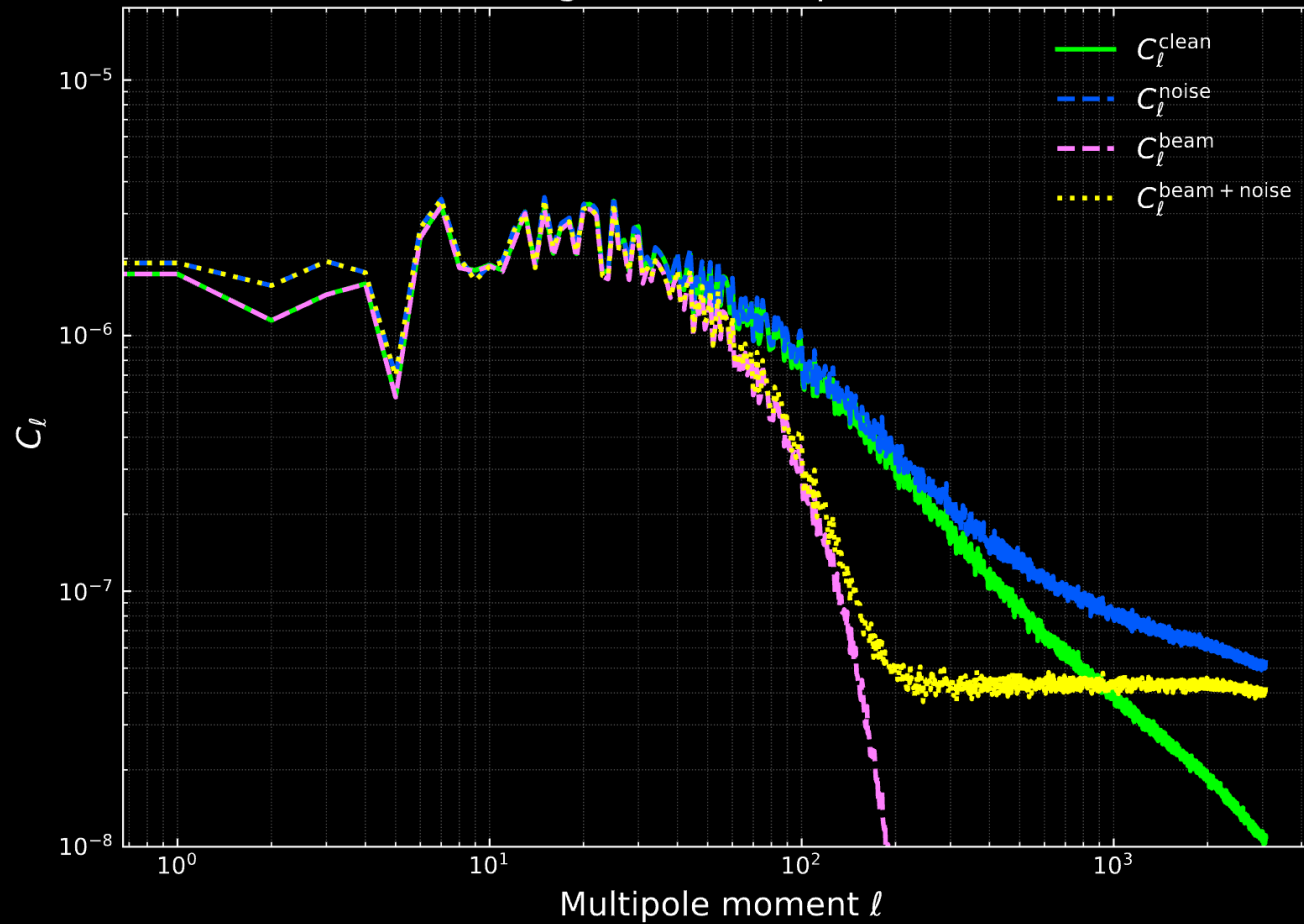
$$M(\hat{n}) = \sum_{j=1}^J w_j(\hat{n}) + c_J(\hat{n}).$$

Starlet Decomposition of HI IM Simulated Map

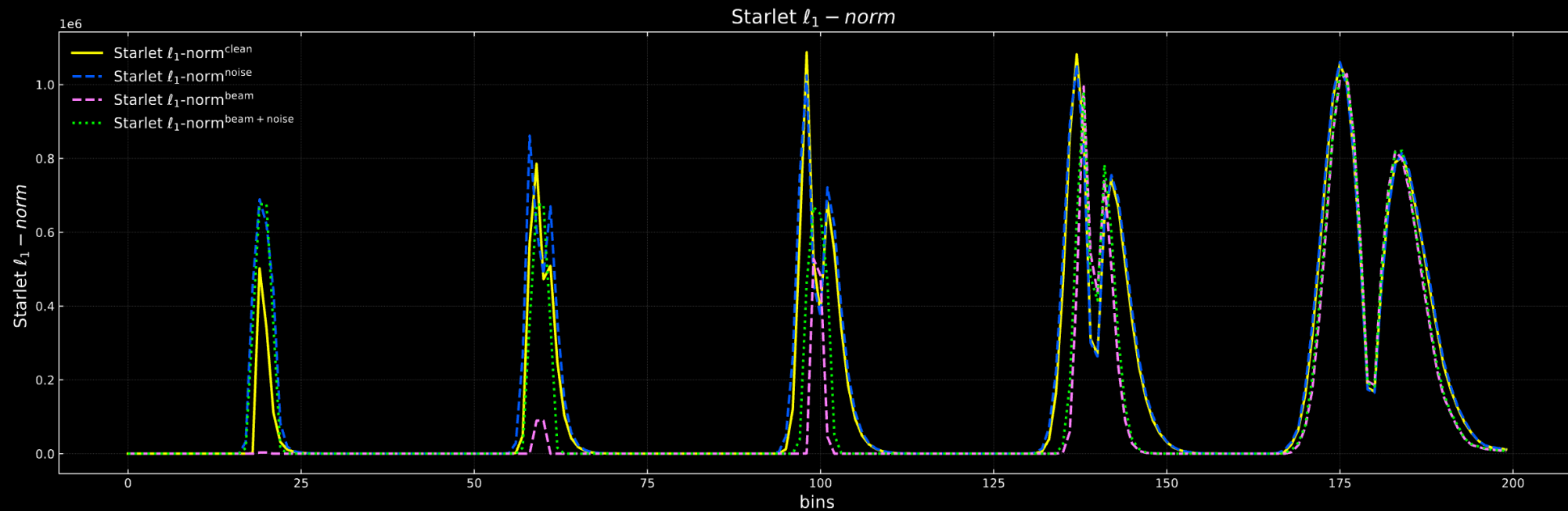


Summary statistics

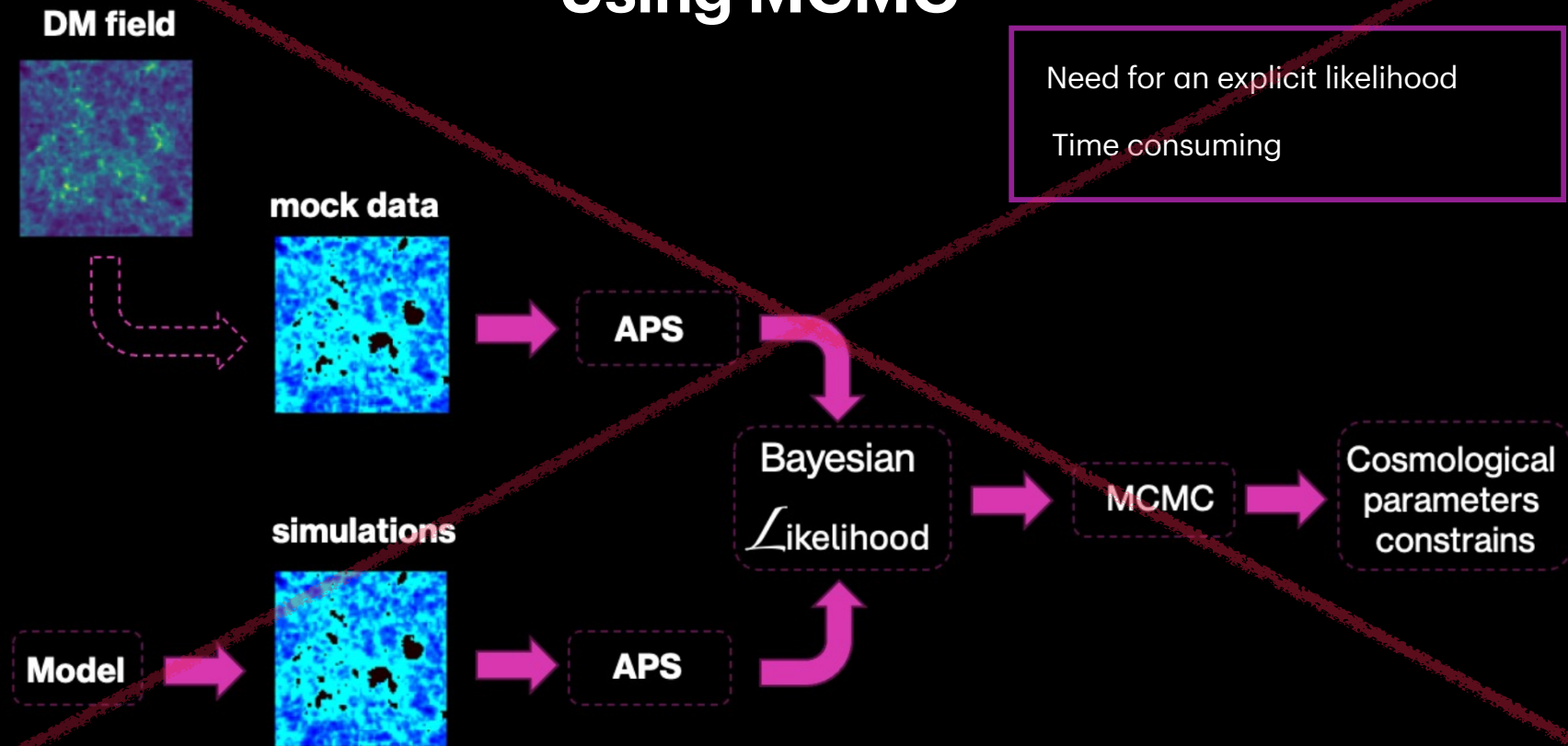
Angular Power Spectra



Summary statistics



Bayesian cosmological parameter inference Using MCMC



Simulation Based Inference (SBI)

Splitting of data set 10 000

Training set: 7 000

Validation set: 2 000

Test set: 1 000

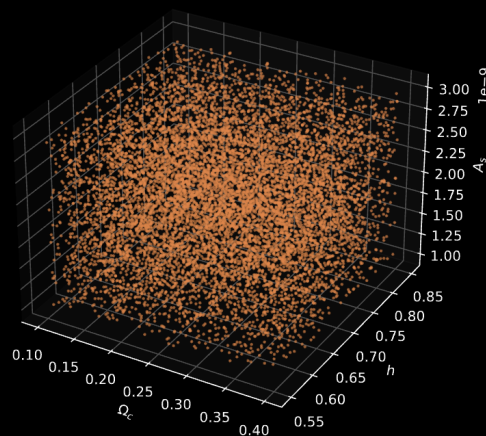
JAXILI

No Need for an explicit likelihood

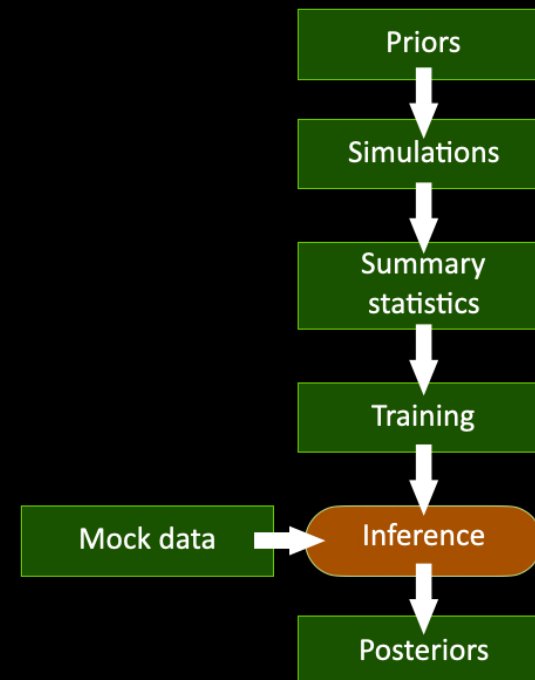
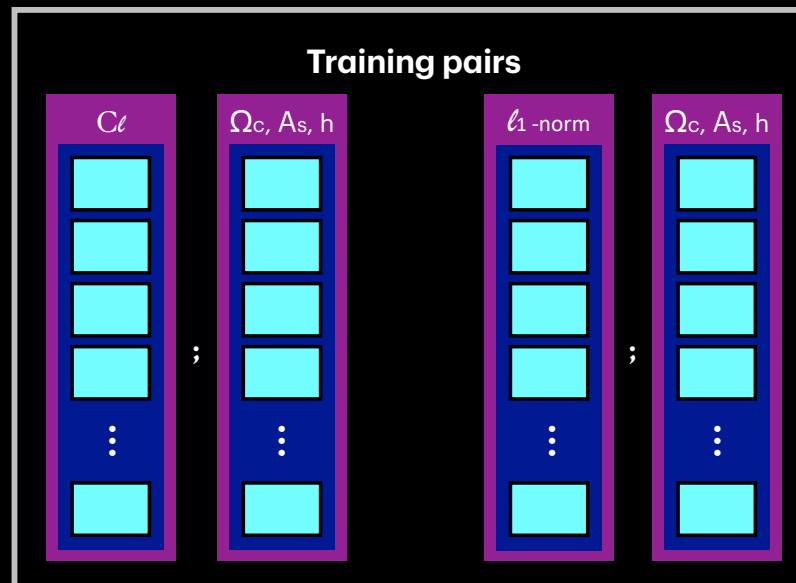
Training set computed **once**

Training time - few minutes (with JAXILI)

Latin Hypercube Sampling



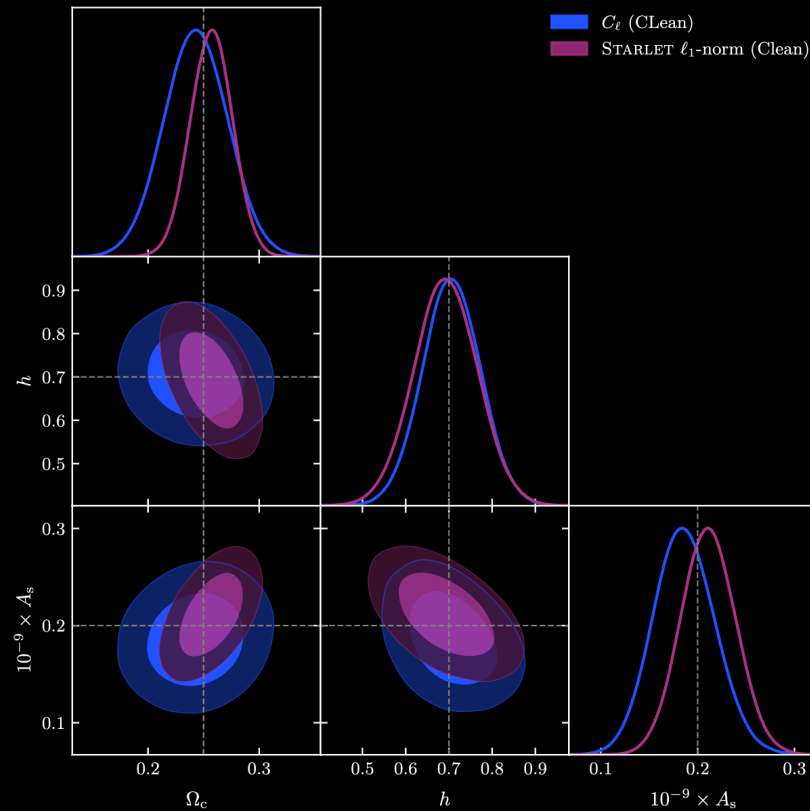
Training pairs



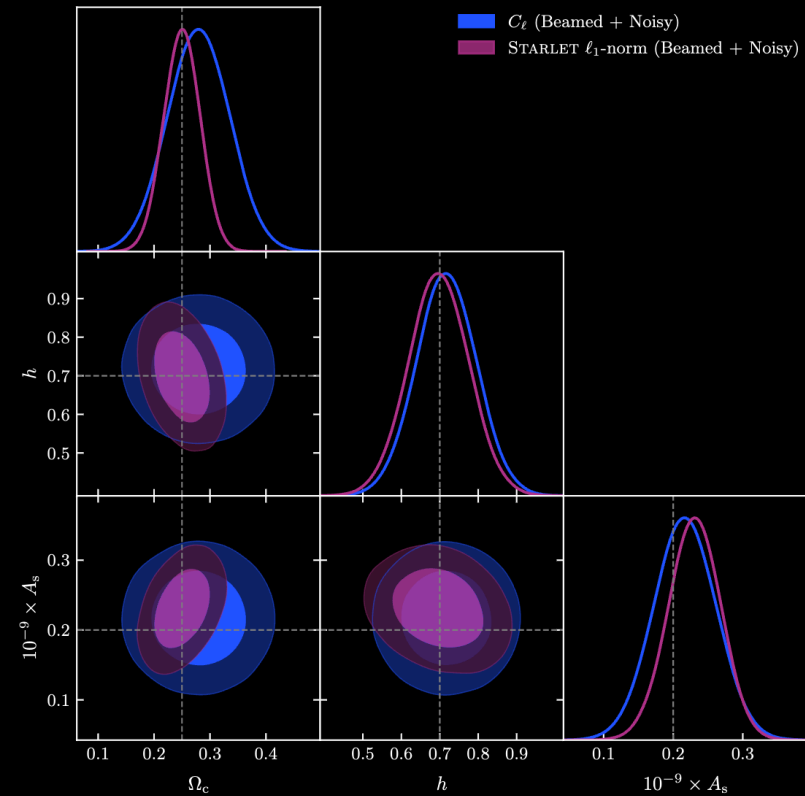
Results

Cosmological parameter constraints (Ω_m , h , A_s).

Posterior Comparison: Starlet ℓ_1 -norm vs C_ℓ (Clean maps)

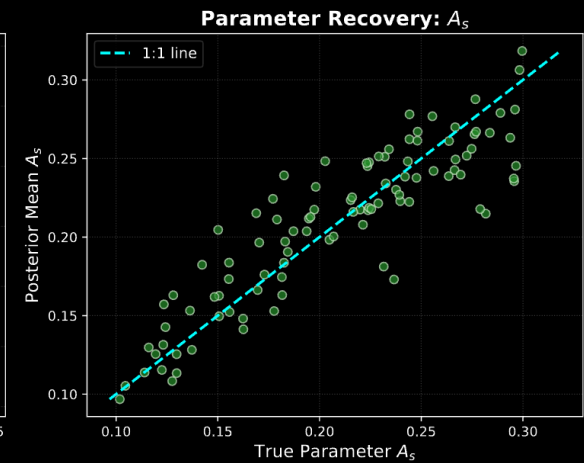
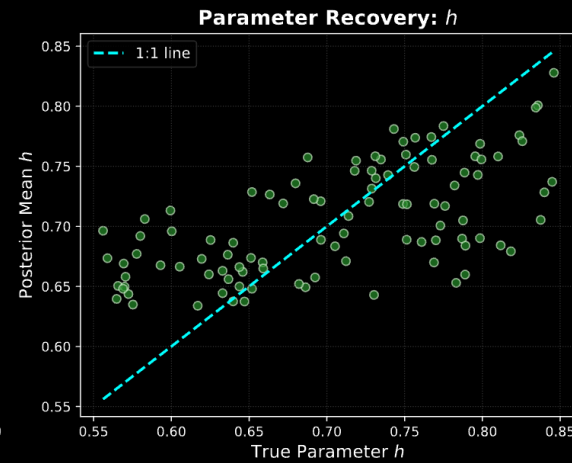
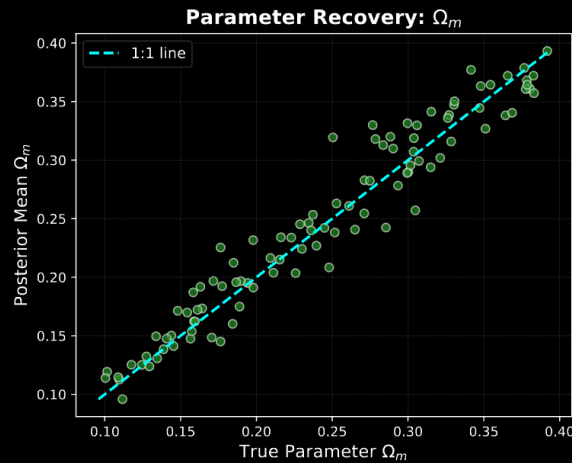


Posterior Comparison: Starlet ℓ_1 -norm vs C_ℓ (Beamed + Noisy maps)

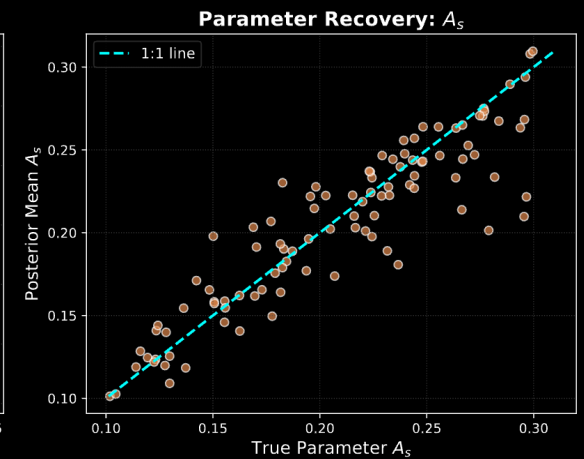
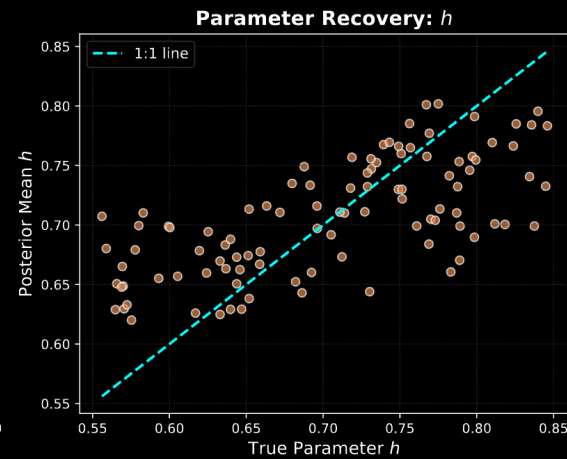
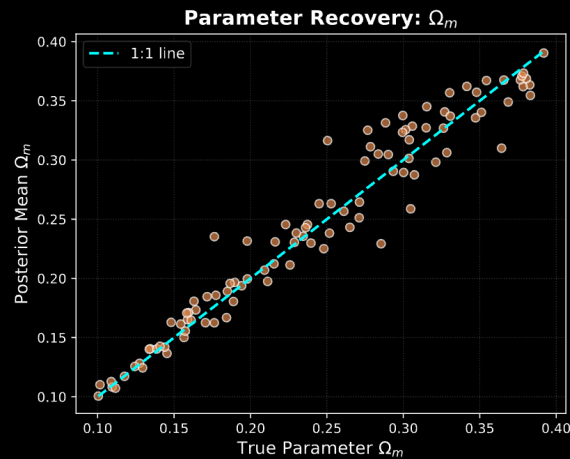


Clean maps

Starlet l1 norm

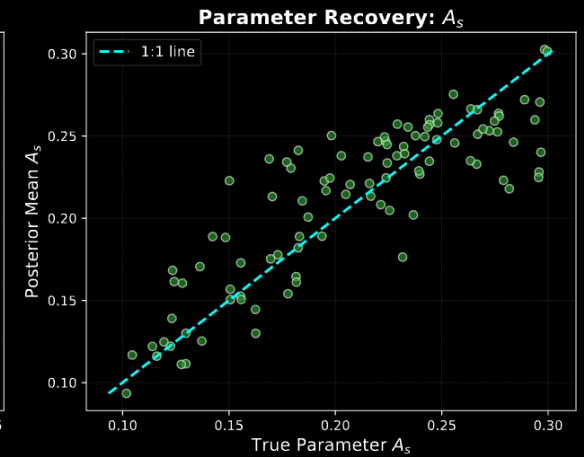
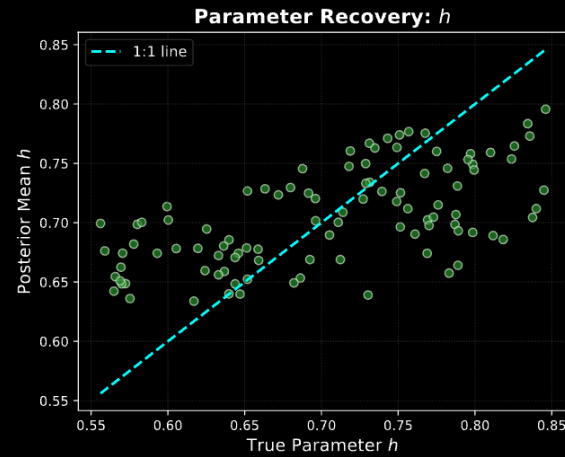
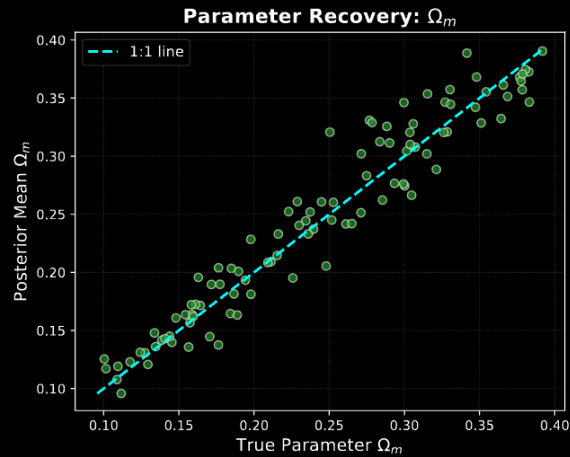


CI

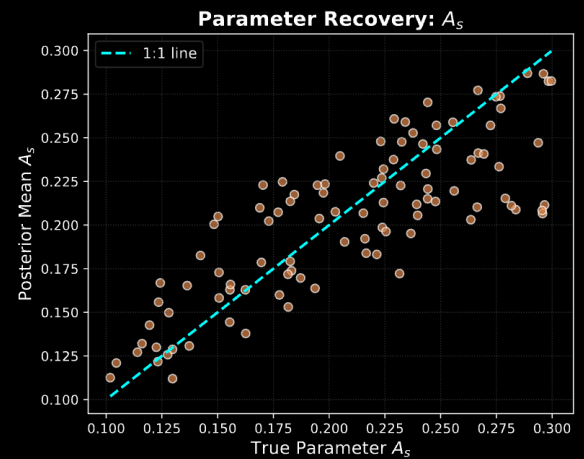
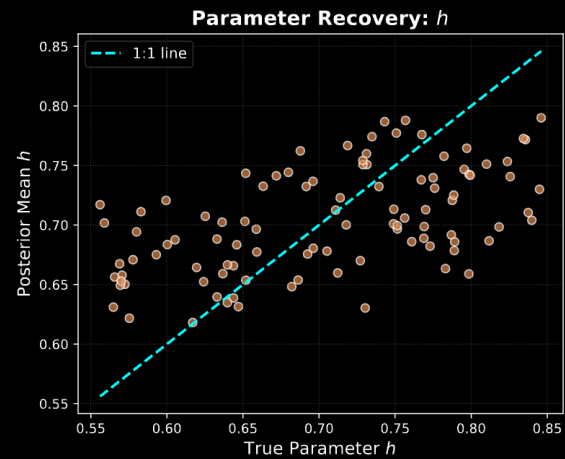
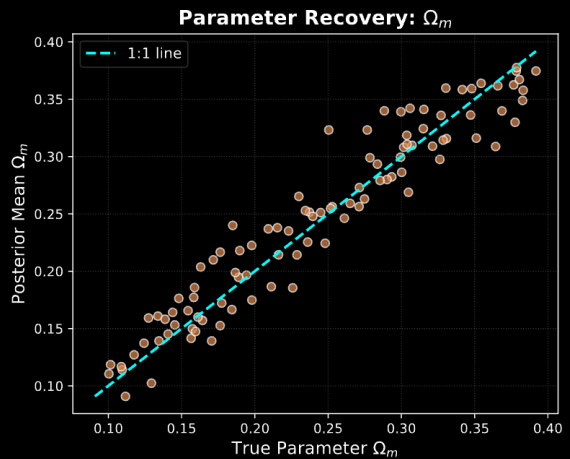


Beamed + noisy maps

Starlet l1 norm



CI



Next steps

N-body simulations instead of lognormal maps

Addition of **other systematics** (e.g. satellites trails) for more **realistic case**