

Recent results of (semi)leptonic decays of charm hadrons at BESIII

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(on behalf of the BESIII collaboration)

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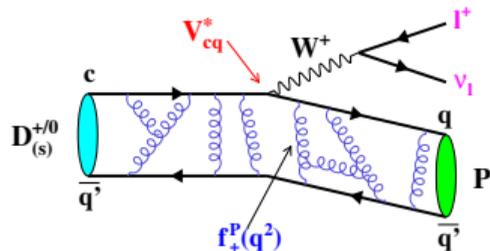
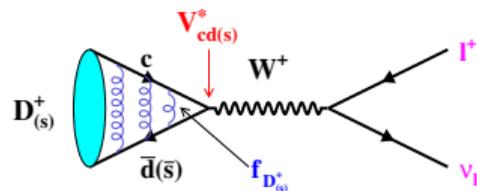


Outline

- 1 Main goal
- 2 BESIII experiment
- 3 Leptonic decays
 - $D^+ \rightarrow \mu^+ \nu_\mu$
 - $D^+ \rightarrow \tau^+ \nu_\tau$
- 4 Semileptonic decays
 - $D \rightarrow \bar{K} \ell^+ \nu_\ell$
 - $D^+ \rightarrow \eta' \ell^+ \nu_\ell$
 - $\Lambda_c^+ \rightarrow n e^+ \nu_e$
- 5 Comparison of $|V_{cs}|$ and $|V_{cd}|$
- 6 Comparison of decay constant f_{D^+} and FFs $f_+(0)$
- 7 Other highlight works
- 8 Summary and prospect

Main goal

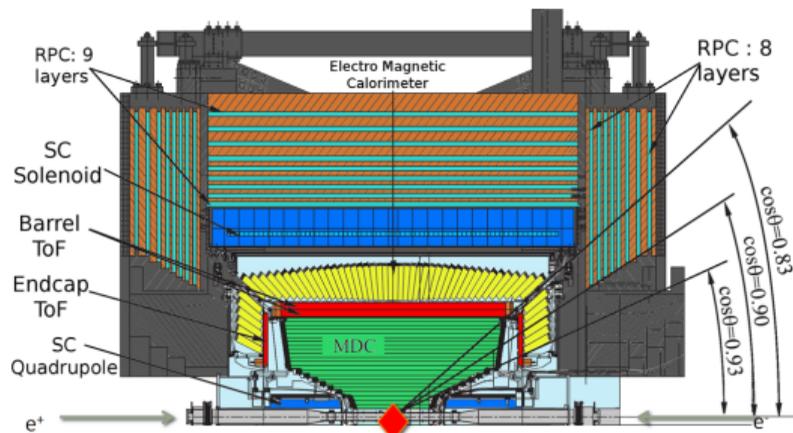
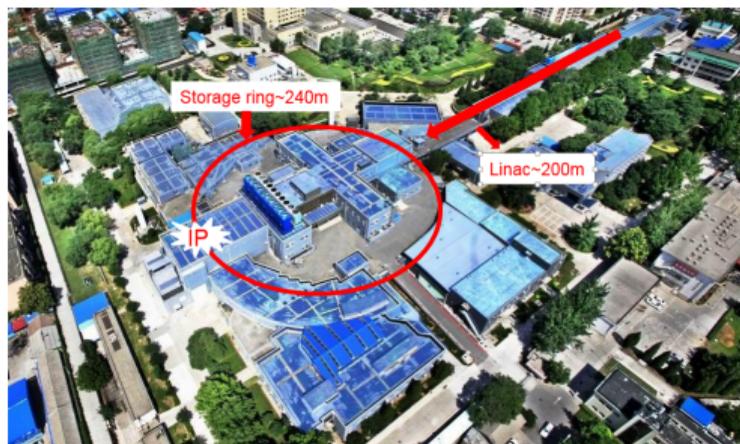
$$V_{\text{CKM}} = \begin{pmatrix} V_{ud} & V_{us} & V_{ub} \\ V_{cd} & V_{cs} & V_{cb} \\ V_{td} & V_{ts} & V_{tb} \end{pmatrix}$$



$$\Gamma = \frac{G_F^2}{8\pi} |V_{cq}|^2 |f_{D_{(s)}^+}|^2 m_\ell^2 m_{D_{(s)}^+} (1 - m_\ell^2/m_{D_{(s)}^+}^2)^2 \quad \frac{d\Gamma}{dq^2} = \chi \frac{G_F^2 |\bar{p}_P|^3}{24\pi^3} |V_{cq}|^2 |f_+(q^2)|^2$$

- Uncertainties of $V_{\text{CKM}} \Rightarrow$ mainly contributed by $|V_{cs}|$ ($\sigma = 0.6\%$) and $|V_{cd}|$ ($\sigma = 1.8\%$)
- Latest LQCD: $f_{D_s^+} = 249.9(05)$ MeV ($\sigma = 0.2\%$); $f_{D^+} = 212.1(07)$ MeV ($\sigma = 0.3\%$);
 $f_+^{D \rightarrow \bar{K}}(0) = 0.7452(31)$ ($\sigma = 0.4\%$); $f_+^{D \rightarrow \pi}(0) = 0.6300(51)$ ($\sigma = 0.8\%$)
- Decay constant $f_{D_{(s)}^+}$ and FF $f_+(0)$ measurements \Rightarrow Calibrate LQCD calculations
- $|V_{cq}|$ measurement \Rightarrow Test CKM matrix unitarity
- BF ratios \Rightarrow Test lepton flavor universality (LFU)

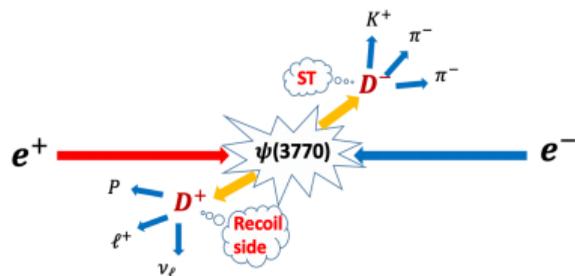
BESIII experiment



- $\sqrt{s} = (1.85 - 4.95) \text{ GeV}$
- Peak luminosity: $1.1 \times 10^{33} \text{ cm}^{-2} \text{ s}^{-1}$
@3.773 GeV
- MDC: $\sigma_P/P = 0.5\%$ @ 1 GeV; $\sigma_{dE/dx} = 6\%$

- TOF: $\sigma_T = 68(110) \text{ ps}$ for barrel (endcap);
endcap upgraded in 2015 $\sigma_T = 60 \text{ ps}$
- EMC: $\sigma_E/E = 2.5\%(5\%)$ for barrel (endcap)

BESIII dataset and double-tag method

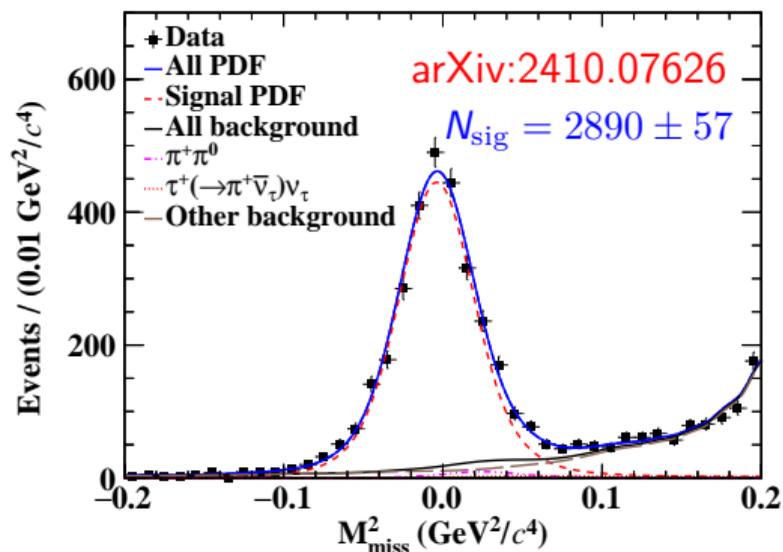


- e^+e^- annihilations data near threshold
 \Rightarrow Double-tag method & Clean environment
- Undetectable neutrinos \Rightarrow extract the (semi-)leptonic signals
 $U_{\text{miss}} = E_{\text{miss}} - |\vec{p}_{\text{miss}}|$, $M_{\text{miss}}^2 = E_{\text{miss}}^2 - |\vec{p}_{\text{miss}}|^2$
- Branching fraction with double-tag method: $\mathcal{B} = \frac{N_{\text{DT}}}{N_{\text{ST}}\epsilon_{\text{DT}}/\epsilon_{\text{ST}}}$
 \Rightarrow Systematic uncertainties on the ST mostly canceled

Data sample	E_{cm} (GeV)	\mathcal{L}_{int} (fb^{-1})	Single tag yields ($\times 10^6$)
$e^+e^- \rightarrow \psi(3770) \rightarrow DD$	3.773	20.3	$D^0 \sim 16.9$; $D^- \sim 11.0$
$e^+e^- \rightarrow D_s^\pm D_s^{*\mp}$	4.128-4.226	7.33	$D_s^- \sim 0.8$
$e^+e^- \rightarrow D_s^{*+} D_s^{*-}$	4.237-4.669	10.64	$D_s^- \sim 0.12$
$e^+e^- \rightarrow \Lambda_c^+ \bar{\Lambda}_c^-$	4.600-4.669	4.5	$\bar{\Lambda}_c^- \sim 0.12$

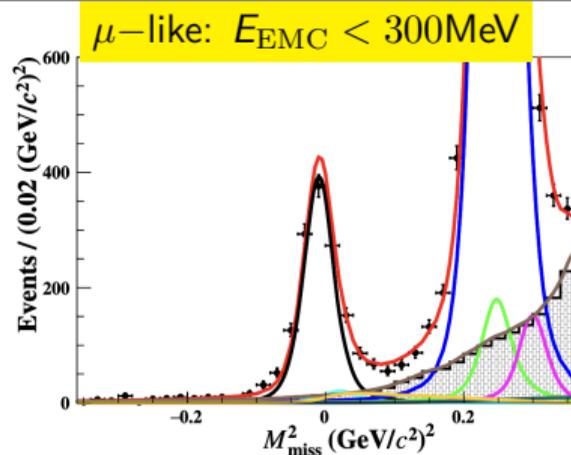
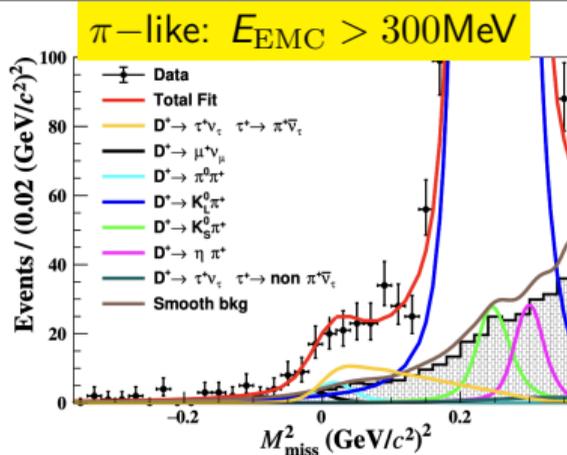
Precision measurement of the branching fraction of $D^+ \rightarrow \mu^+ \nu_\mu$

Reference	\mathcal{L} (fb $^{-1}$)	BF($\times 10^{-4}$)	f_{D^+} (MeV)	$ V_{cd} $	Precision (%)
CLEO, PRD78,052003	0.818	3.82(32)(09)	207.1(87)(24)(08)	0.2195(92)(26)(09)	4.4
BESIII, PRD89,051104	2.93	3.71(19)(06)	204.1(52)(17)(08)	0.2164(55)(17)(09)	2.7
BESIII, arXiv:2410.07626	20.3	3.981(79)(40)	211.5(21)(11)(08)	0.2242(23)(11)(09)	1.2 ★



Measurement of the branching fraction of $D^+ \rightarrow \tau^+ \nu_\tau$ via $\tau^+ \rightarrow \pi^+ \bar{\nu}_\tau$

Reference	\mathcal{L} (fb $^{-1}$)	BF($\times 10^{-3}$)	f_{D^+} (MeV)	$ V_{cd} $	Precision (%)
PRL123,211802	2.93	1.20(24)(12)	225(23)(11)(01)	0.238(24)(12)(01)	11
JHEP01(2025)89	7.93	0.99(11)(05)	204(11)(05)(01)	0.216(12)(06)(01)	6.1 ★

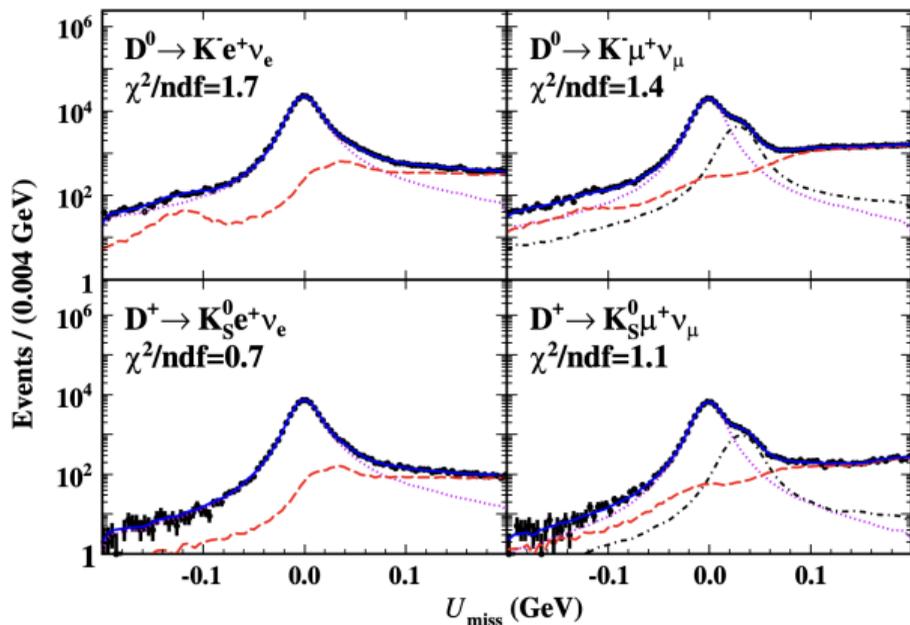


- LFU test:

$$\mathcal{R}_{\tau/\mu} = \Gamma_{D^+ \rightarrow \tau^+ \nu_\tau} / \Gamma_{D^+ \rightarrow \mu^+ \nu_\mu} = 2.49 \pm 0.31, \text{ consistent with } \mathcal{R}_{\tau/\mu}^{\text{SM}} = \frac{m_\tau^2 (1 - m_\tau^2/m_{D^+}^2)^2}{m_\mu^2 (1 - m_\mu^2/m_{D^+}^2)^2} = 2.69$$

Improved measurements of $D^0 \rightarrow K^- \ell^+ \nu_\ell$ and $D^+ \rightarrow \bar{K}^0 \ell^+ \nu_\ell$

- Phys. Rev. D **110**, 112006 (2024)
- 7.93 fb⁻¹ data sample @3.773 GeV



- $\mathcal{B}(D^0 \rightarrow K^- e^+ \nu_e) = (3.521 \pm 0.009 \pm 0.016)\%$
- $\mathcal{B}(D^0 \rightarrow K^- \mu^+ \nu_\mu) = (3.419 \pm 0.011 \pm 0.016)\%$
- $\mathcal{B}(D^+ \rightarrow \bar{K}^0 e^+ \nu_e) = (8.864 \pm 0.039 \pm 0.082)\%$
- $\mathcal{B}(D^+ \rightarrow \bar{K}^0 \mu^+ \nu_\mu) = (8.665 \pm 0.046 \pm 0.084)\%$

- LFU test (SM: 0.975 ± 0.001) \sim consistent

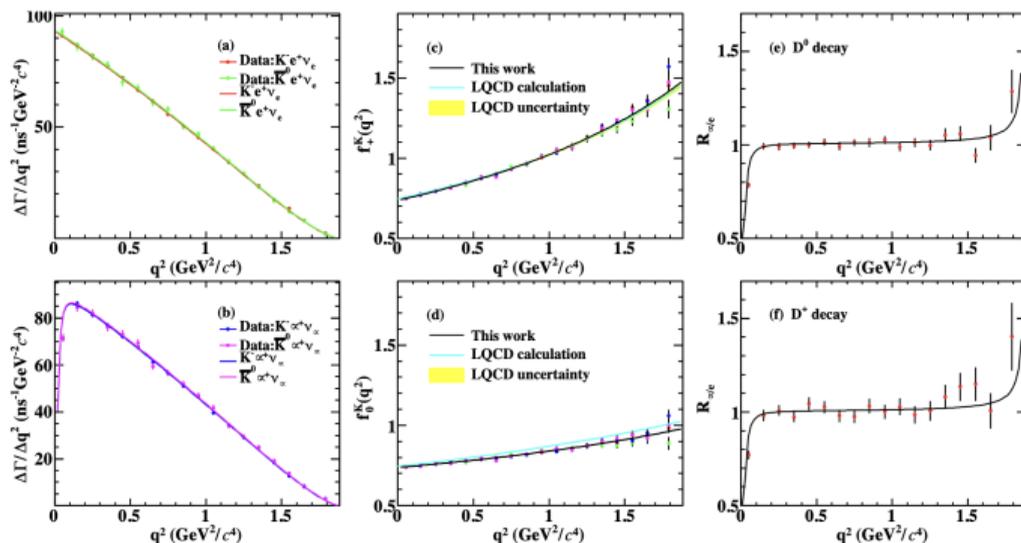
$$\frac{\mathcal{B}(D^0 \rightarrow K^- \mu^+ \nu_\mu)}{\mathcal{B}(D^0 \rightarrow K^- e^+ \nu_e)} = 0.971 \pm 0.004 \pm 0.006$$

$$\frac{\mathcal{B}(D^+ \rightarrow \bar{K}^0 \mu^+ \nu_\mu)}{\mathcal{B}(D^+ \rightarrow \bar{K}^0 e^+ \nu_e)} = 0.978 \pm 0.007 \pm 0.013$$

- Isospin test \sim consistent

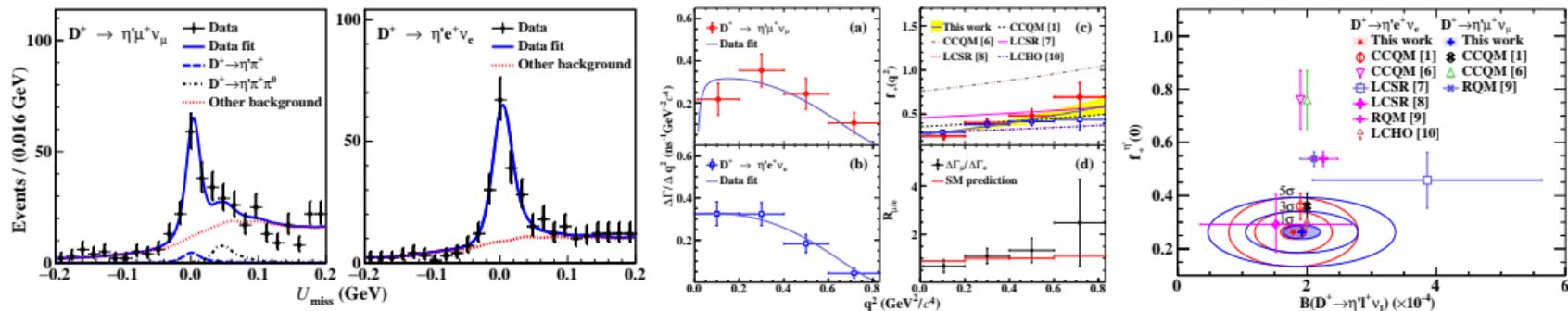
$$\frac{\Gamma(D^0 \rightarrow K^- e^+ \nu_e)}{\Gamma(D^+ \rightarrow \bar{K}^0 e^+ \nu_e)} = 1.000 \pm 0.007 \pm 0.012$$

$$\frac{\Gamma(D^0 \rightarrow K^- \mu^+ \nu_\mu)}{\Gamma(D^+ \rightarrow \bar{K}^0 \mu^+ \nu_\mu)} = 0.993 \pm 0.008 \pm 0.012$$

Improved measurements of $D^0 \rightarrow K^- \ell^+ \nu_\ell$ and $D^+ \rightarrow \bar{K}^0 \ell^+ \nu_\ell$ 

- $f_+^K(0) = 0.7366 \pm 0.0011_{\text{stat}} \pm 0.0013_{\text{sys}}$; $|V_{cs}| = 0.9623 \pm 0.0015_{\text{stat}} \pm 0.0017_{\text{sys}} \pm 0.0040_{\text{LQCD}}$
- Experimental uncertainties of $f_+^K(0)$ and $|V_{cs}|$: 0.23%
- Additional uncertainty of the input $f_+^K(0)$ calculated by LQCD: 0.42%

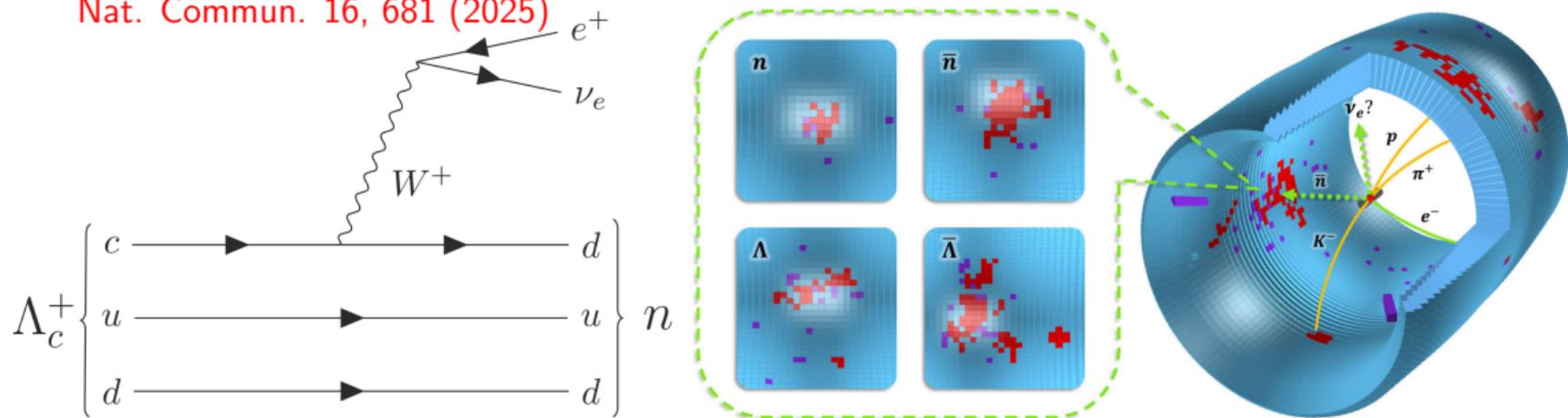
First study of $D^+ \rightarrow \eta' \ell^+ \nu_\ell$ decay dynamics



- Data: 20.3 fb^{-1} @ 3.773 GeV [PRL134(2025)111801]
- First observation of $D^+ \rightarrow \eta' \mu^+ \nu_\mu$ with significance of 8.6σ
 $\mathcal{B}(D^+ \rightarrow \eta' \mu^+ \nu_\mu) = (1.92 \pm 0.28 \pm 0.08) \times 10^{-4}$; $\mathcal{B}(D^+ \rightarrow \eta' e^+ \nu_e) = (1.79 \pm 0.19 \pm 0.07) \times 10^{-4}$
- First extraction of the FF of $D^+ \rightarrow \eta' \ell^+ \nu_\ell$: $f_+^{\eta'}(0) = 0.263 \pm 0.025 \pm 0.006$
- LFU test: $\mathcal{R}_{\mu/e}^{\eta'} = 1.07 \pm 0.19 \pm 0.03$
- $\eta - \eta'$ mixing angle: $\phi_P = (39.8 \pm 0.8 \pm 0.3)^\circ$ ($\cot^4 \phi_P = \frac{\Gamma_{D_s^+ \rightarrow \eta' \ell^+ \nu_\ell} / \Gamma_{D_s^+ \rightarrow \eta \ell^+ \nu_\ell}}{\Gamma_{D^+ \rightarrow \eta' \ell^+ \nu_\ell} / \Gamma_{D^+ \rightarrow \eta \ell^+ \nu_\ell}}$)

First observation of $\Lambda_c^+ \rightarrow ne^+\nu_e$ with a graph neural network

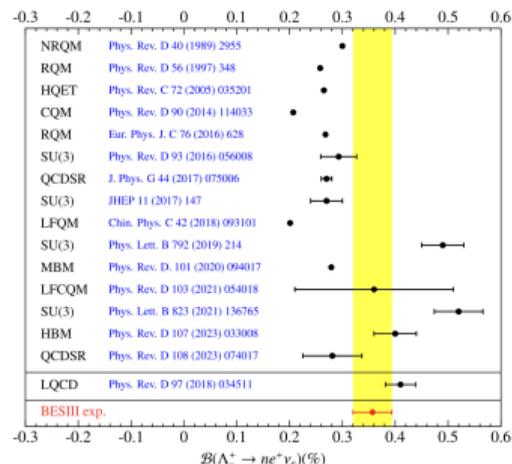
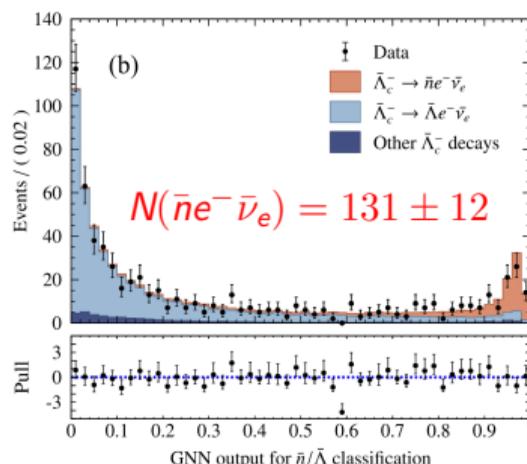
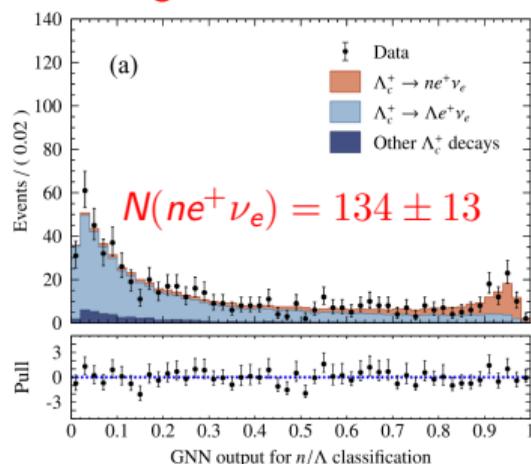
Nat. Commun. 16, 681 (2025)



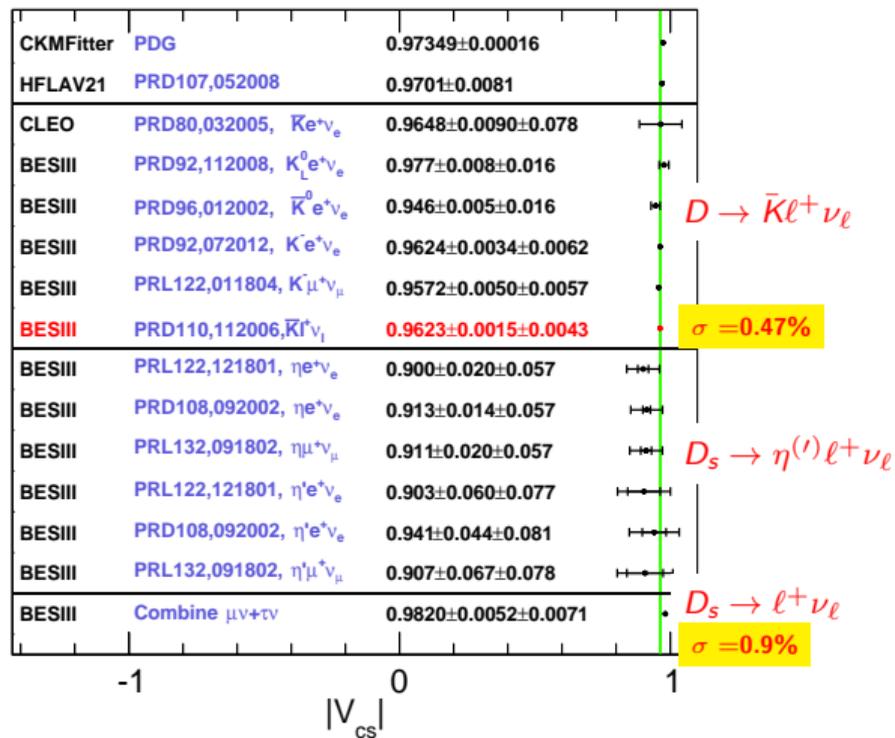
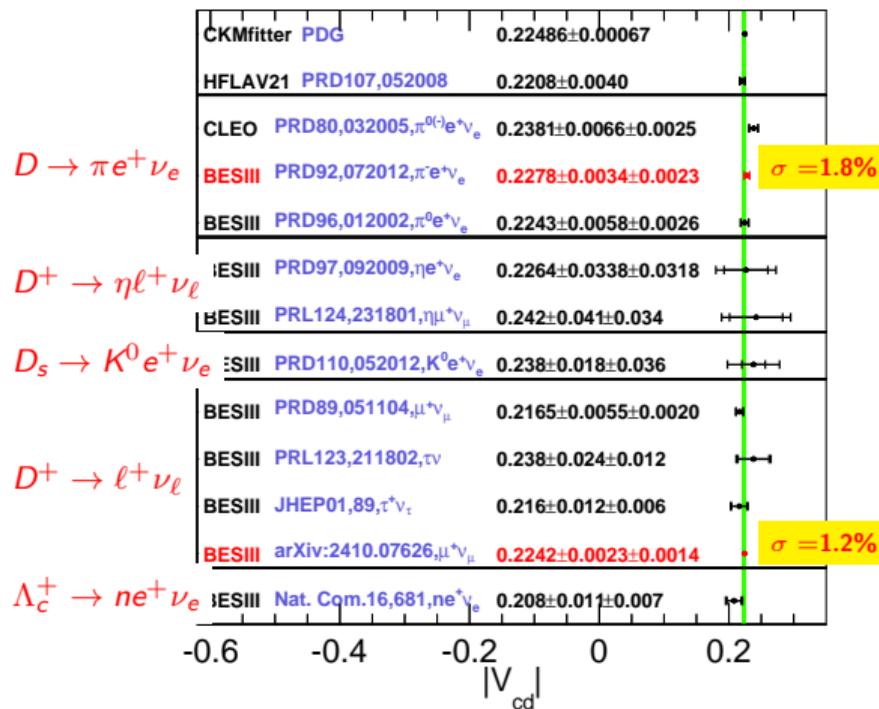
- Data: 4.5 fb^{-1} @ 4.6-4.7 GeV
- Significant challenges: two missing particles, neutron and neutrino;
- Dominant background: $\Lambda_c^+ \rightarrow \Lambda e^+ \nu_e$, $\Lambda \rightarrow n\pi^0$
- Machine learning of graph neural network \Rightarrow discriminate the energy deposition patterns of neutrons from those of Λ in the Electromagnetic Calorimeter of BESIII detector

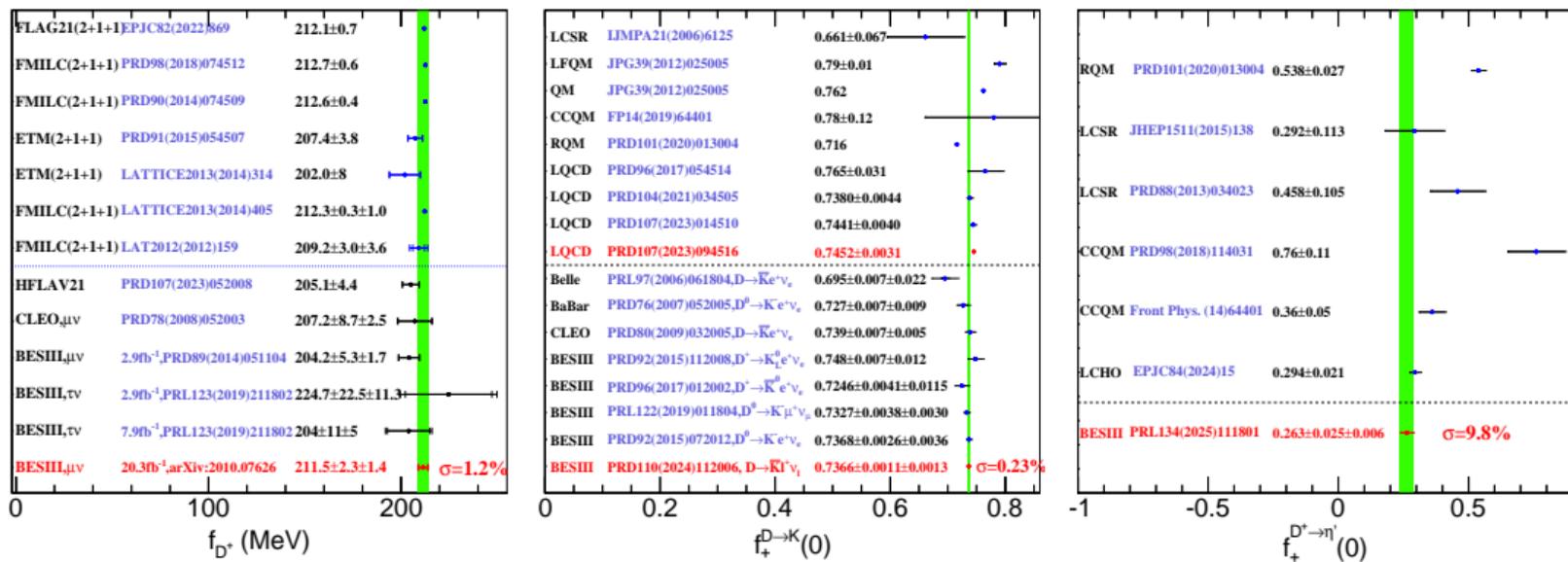
First observation of $\Lambda_c^+ \rightarrow ne^+\nu_e$ with a graph neural network

Significance: $> 10\sigma$



- $\mathcal{B}(\Lambda_c^+ \rightarrow ne^+\nu_e) = (3.57 \pm 0.34 \pm 0.14) \times 10^{-3}$
 - $\Gamma(\Lambda_c^+ \rightarrow ne^+\nu_e) = |V_{cd}|^2(0.405 \pm 0.016 \pm 0.020) \text{ ps}^{-1}$ [PRD97(2018)034511]
- $\implies |V_{cd}| = 0.208 \pm 0.011 \pm 0.007 \pm 0.001$ First determination from charmed baryon decays

Comparison of $|V_{cs}|$ and $|V_{cd}|$ 

Comparison of decay constant f_{D^+} and FFs $f_+(0)$ 

- Precisions of measured f_{D^+} , $f_+^{D \rightarrow \bar{K}}(0)$, and $f_+^{D^+ \rightarrow \eta'}(0)$ are 1.2%, 0.23%, and 9.8%, respectively
- Measured FF $f_+^{D \rightarrow \bar{K}}(0)$ is consistent with the LQCD calculations within 2.5σ

Other highlight works

Channel	\mathcal{L}_{int} (fb $^{-1}$) / E_{cm} (GeV)	Reference
$D^+ \rightarrow e^+ \nu_e$	20.3 / 3.773	arXiv:2501.04760
$D_s^+ \rightarrow \ell^+ \nu_\ell, \ell = \mu \text{ or } \tau$	10.64 / 4.237-4.699	PRD110(2024)052002
$D^{*+} \rightarrow \ell^+ \nu_\ell, \ell = e \text{ or } \mu$	6.32 / 4.178-4.226	PRD110(2024)012003
$D^0 \rightarrow K^- \pi^0 \mu^+ \nu_\mu$	7.93 / 3.773	PRL134(2025)011803
$D^0 \rightarrow \bar{K}^0 \pi^- e^+ \nu_e$	7.93 / 3.773	arXiv:2412.10803
$D^+ \rightarrow K_S^0 \pi^0 e^+ \nu_e$	7.93 / 3.773	JHEP10(2024)199
$D^0 \rightarrow \pi^- \pi^0 e^+ \nu_e$	7.93 / 3.773	PRD110(2024)112018
$D^{0(+)} \rightarrow b_1(1235)^{-(0)} e^+ \nu_e$	7.93 / 3.773	arXiv:2407.20551
$D^{0(+)} \rightarrow \bar{K}_1(1270)^{-(0)} e^+ \nu_e$	20.3 / 3.773	arXiv:2503.02196
$D^{0(+)} \rightarrow \bar{K}_1(1270)^{-(0)} \mu^+ \nu_\mu$	7.93 / 3.773	arXiv:2502.03828
$D^0 \rightarrow a_0(980)^- _{\eta\pi^-} e^+ \nu_e$	7.93 / 3.773	arXiv:2411.07730
$D \rightarrow P \eta e^+ \nu_e, P = \eta, \bar{K}$	7.93 / 3.773	PRD110(2024)112001
$D_s^+ \rightarrow K^0 e^+ \nu_e$	7.33 / 4.128-4.226	PRD110(2024)052012
$D_s^+ \rightarrow P e^+ \nu_e, P = \eta^{(\prime)}, K^0$	10.64 / 4.237-4.699	PRD110(2024)072017

Summary

- Purely and semileptonic decays of charm hadrons are important for determining CKM matrix elements, calibrating LQCD, testing LFU, *et al.*;
- Precisions of $|V_{cs}|$ and $|V_{cd}|$ have been reduced to 0.5% and 1.2%, respectively;
- Precisions of f_{D^+} and $f_+^{D \rightarrow \bar{K}}(0)$ have been reduced to 1.2% and 0.23%, respectively;
- No evidence of LFU violation is found within precisions of 0.74% for $\mathcal{R}(\mu/e)$ via $D \rightarrow \bar{K} \ell^+ \nu_\ell$ and 12% for $\mathcal{R}(\tau/\mu)$ via $D^+ \rightarrow \ell^+ \nu_\ell$;
- Isospin conservation is verified within precision of 1.5% via $D \rightarrow \bar{K} \ell^+ \nu_\ell$;
- Machine learning has demonstrated the power in experimental particle physics, offering the possible in searching for the rare decays of charm hadrons in future.

Prospect

- 20.3 fb⁻¹ data @ 3.773 GeV is ready at Jul. 2024, more precision measurements and searching for rare semileptonic decays will be presented;
- Additional 3 fb⁻¹ data @ 4.178 GeV in future [CPC44(2020)040001] will further improve the precisions in D_s sector.

Thank you