



Nuclear Physics at GANIL

Probing nuclear matter at the extremes

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Normandie Université , ENSICAEN, CNRS/IN2P3*

Profs au GANiL

Part I

Motivations

Describing the nucleus

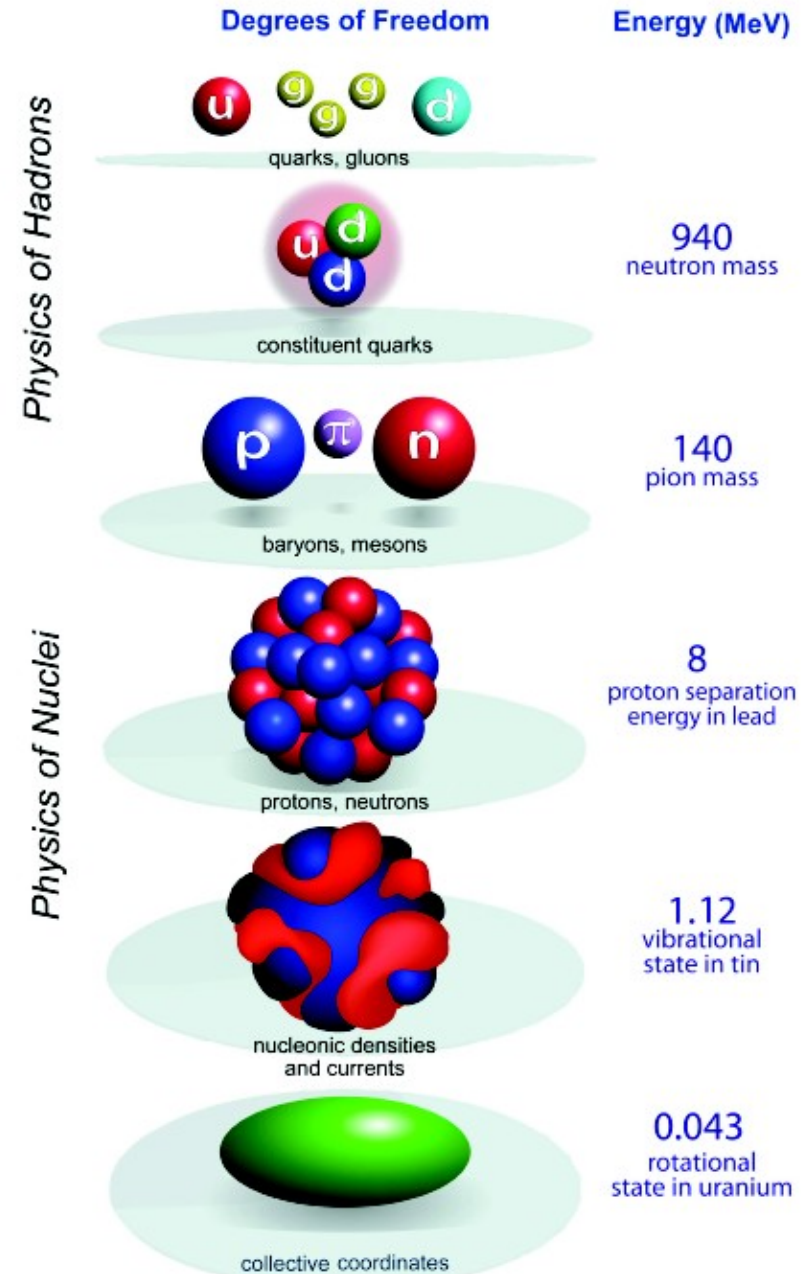
Energy scales in the subatomic world

Depending on scale/energy, systems are described by different **degrees of freedom** and are associated to **different (quasi-)particles**

De Broglie equation (spatial resolution) :

$$\lambda = \hbar / p$$

E_{inc} (MeV)	λ (fm)
1	8
10	1.5
100	0.5



$$1 \text{ MeV} = 1 \text{ méga-électronvolts} = 10^6 \text{ eV} = 1.6 \cdot 10^{-13} \text{ J}$$

Energy scales in the subatomic world

Depending on scale/energy, systems are described by different **degrees of freedom** and are associated to **different phenomena**

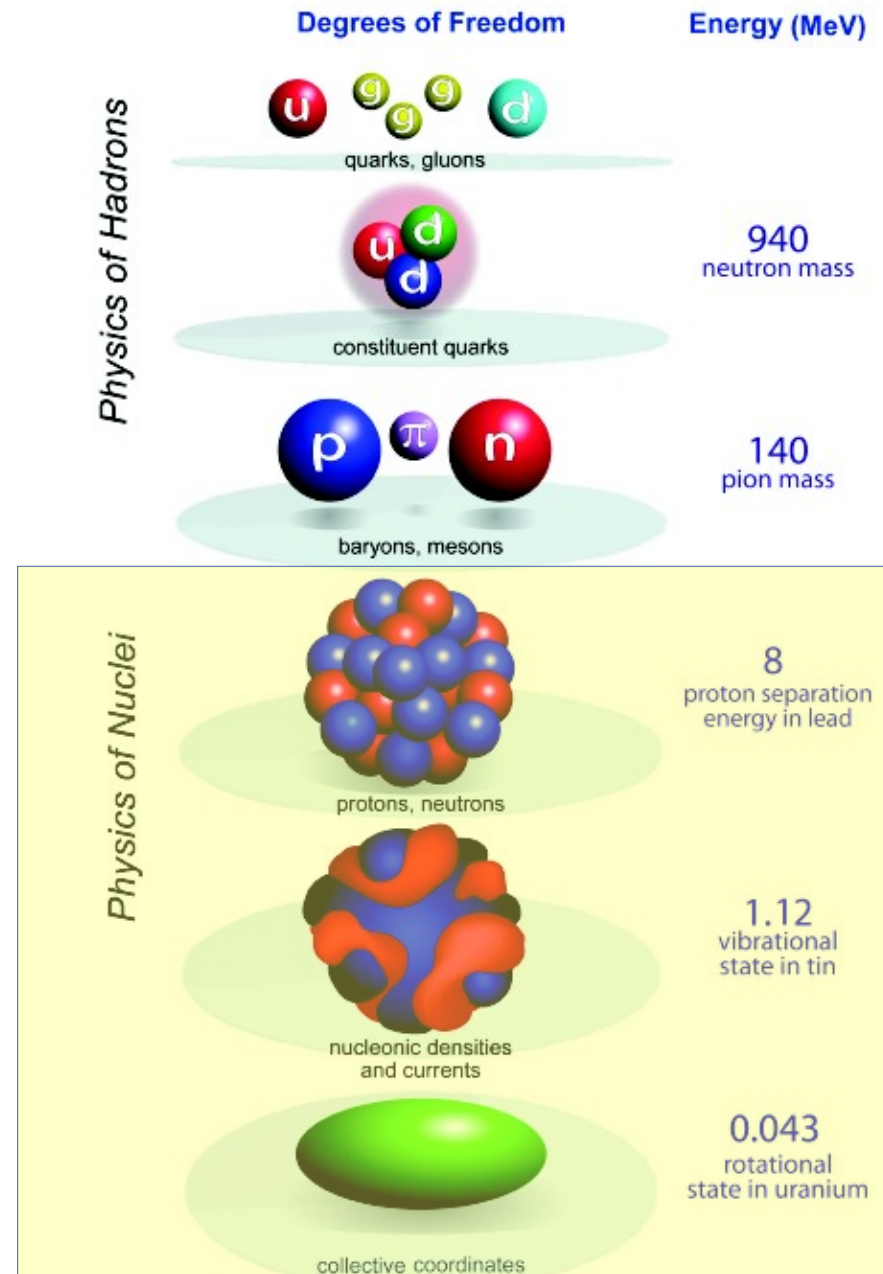
Nuclear physics at low E = nuclear degrees of freedom

- nucleus
- collective phenomena
- excited states
- bulk and surface properties in continuum states

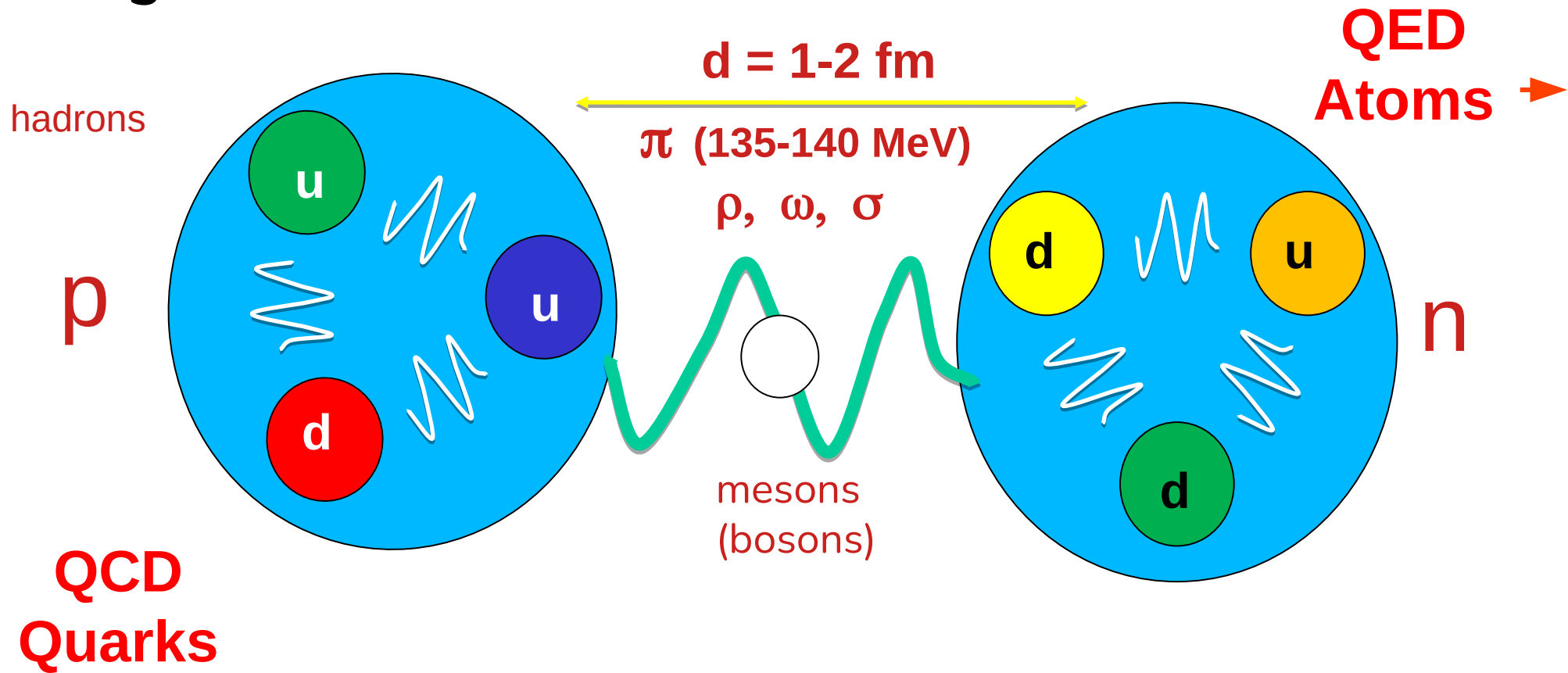
Nuclear reactions

$E_{\text{inc}} = 5 - 100 \text{ MeV/nucleon}$

$$1 \text{ MeV} = 1 \text{ méga-électronvolts} = 10^6 \text{ eV} = 1,6 \cdot 10^{-13} \text{ J}$$



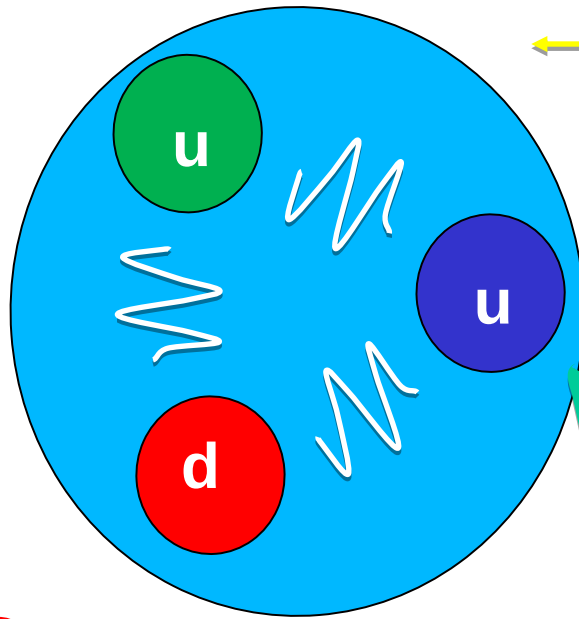
Strong .vs. Nuclear interaction



Strong .vs. Nuclear interaction

Hadrons

p



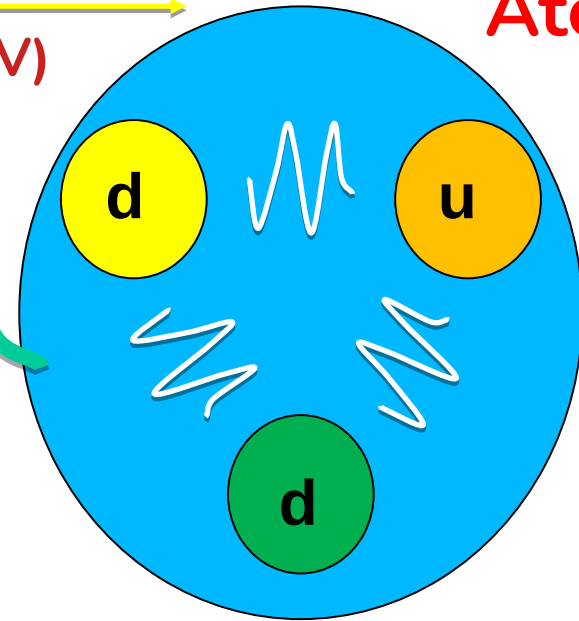
$d = 1-2 \text{ fm}$

π (135-140 MeV)

ρ, ω, σ

mesons
(bosons)

QED
Atoms →

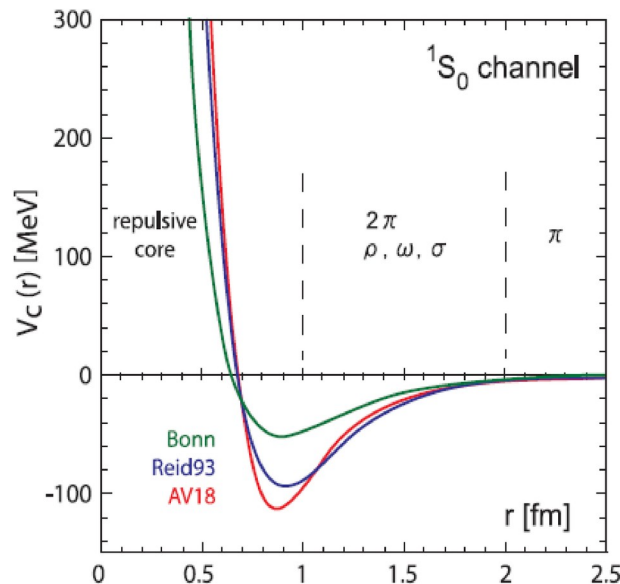


n

← QCD
Quarks

Nuclear interaction
= long range strong int.
(non perturbative regime)

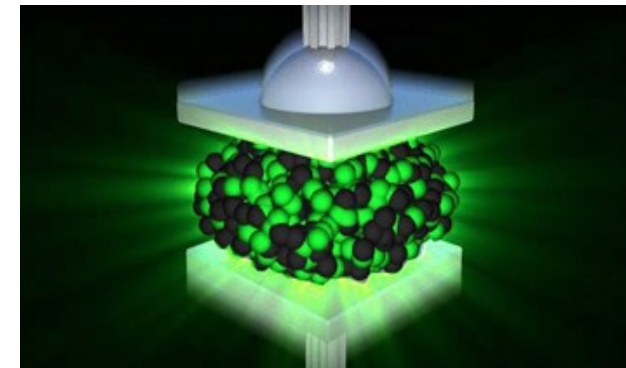
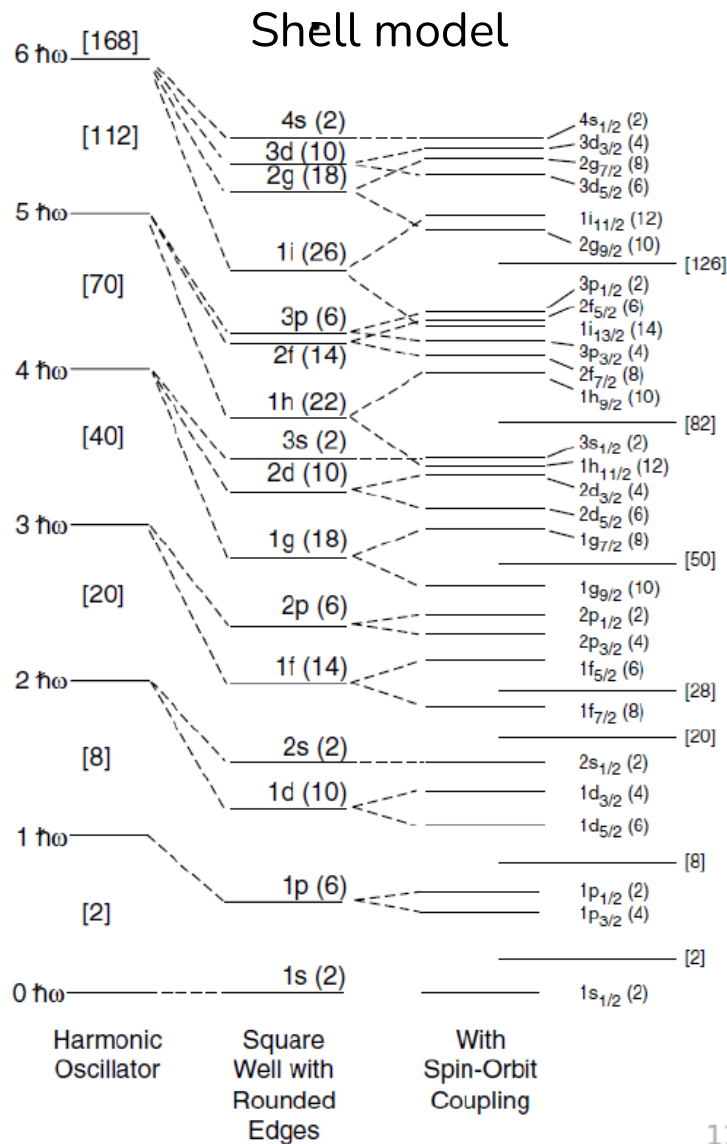
Hard core : $r < 1 \text{ fm}$
Small range : $r \approx 1 \text{ fm}$
Tensor and isovector: n,p



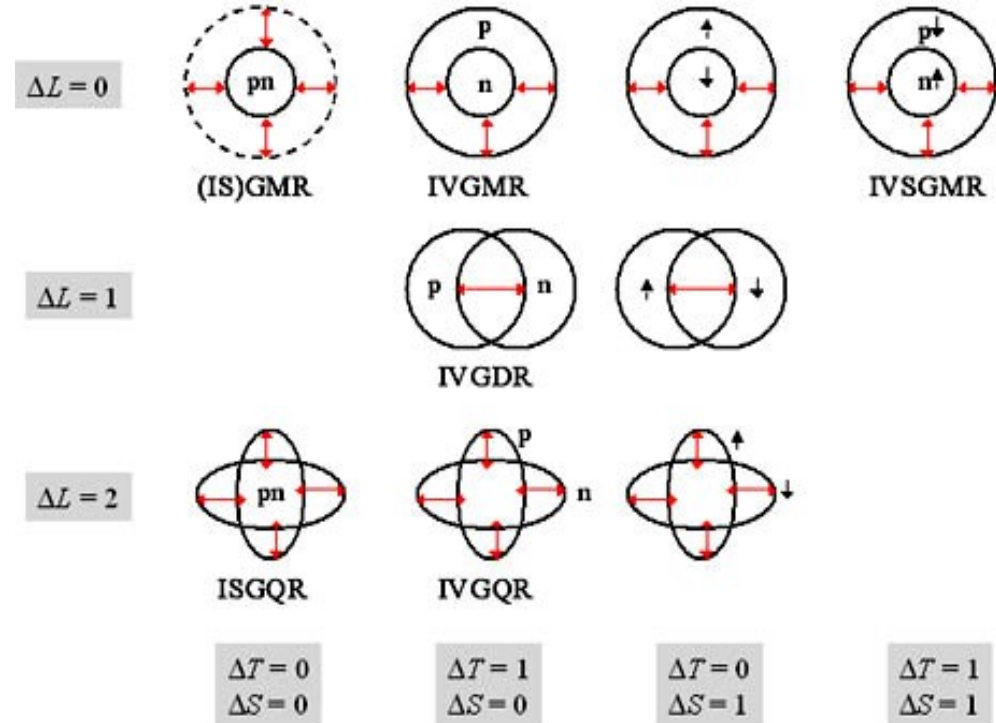
Relevant D.o.F.

Density $\rho = \rho_n + \rho_p$,
Angular mom. $J=L+S$
Isospin $I = (\rho_n - \rho_p) / \rho$

Nucleus at $T \approx 0$: quantum realm



Collective excitations
Giant resonances

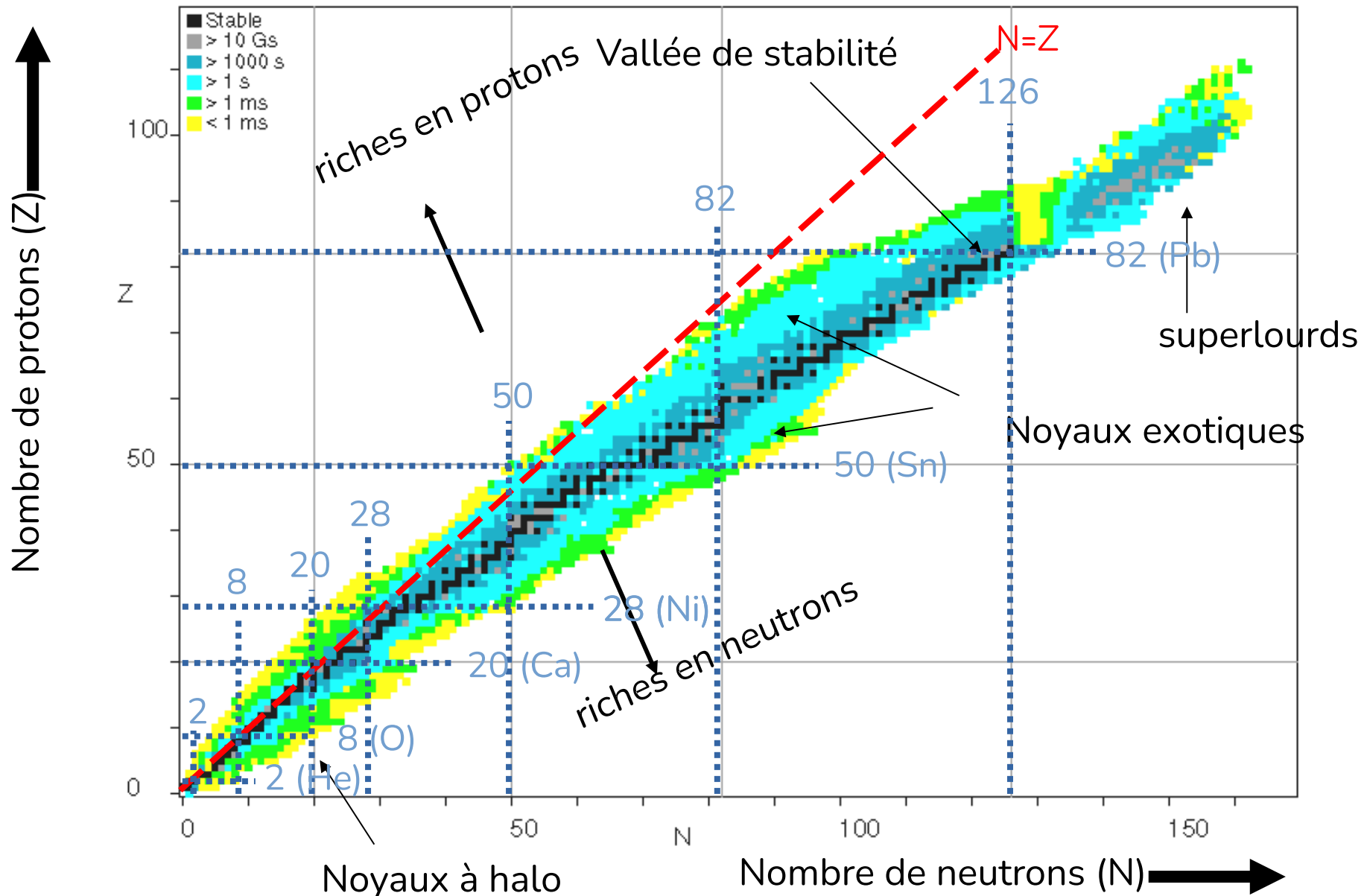


Quantum numbers for nucleon orbitals n, l, j : $1s_{1/2}$

Nuclear structure and limits of stability (driplines)

Des noyaux à la carte

Nombres magiques : 2, 8, 20, 28, 50, 82, 126, ...



Nuclear structure (I)

Thank to the advent of **radioactive ion beam facilities**, new phenomena have been investigated during the last two decades

- **new** magic numbers (harmonic shells for exotic nuclei)
- **haloes** nuclei (borromean)
- granular or **molecular** systems (clusters in nuclei)
- nuclear structure for **superheavy** elements (transfermium $Z > 100$)
- **new radioactivities** 2p, 2n, clusters (coupling to continuum)

Impact on theories

3-body and many-body forces

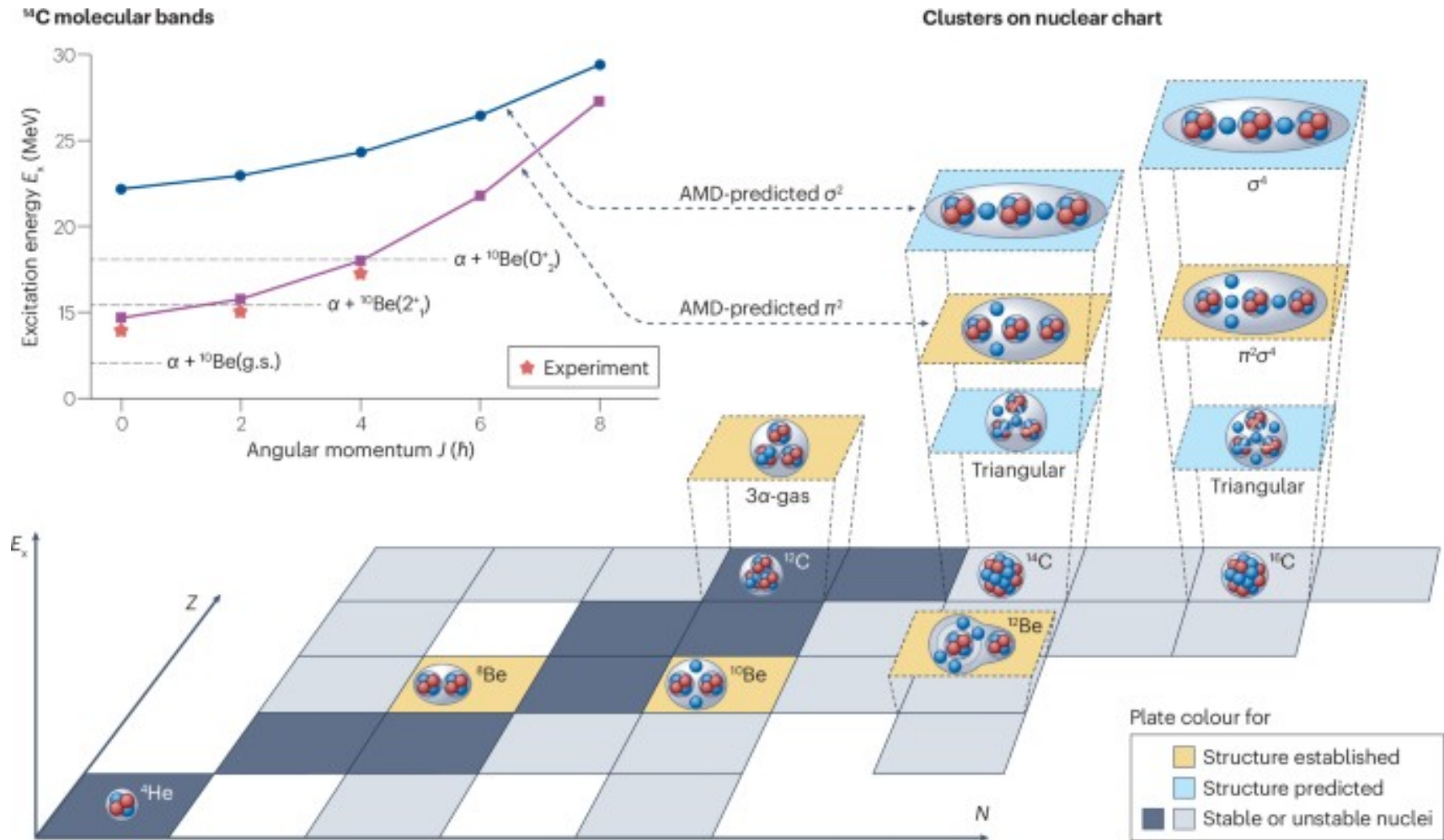
Isospin (N/Z) dependence

Loosely bound nuclei / coupling to continuum

Correlations : pairing, superfluidity, short range

Nuclear structure (II)

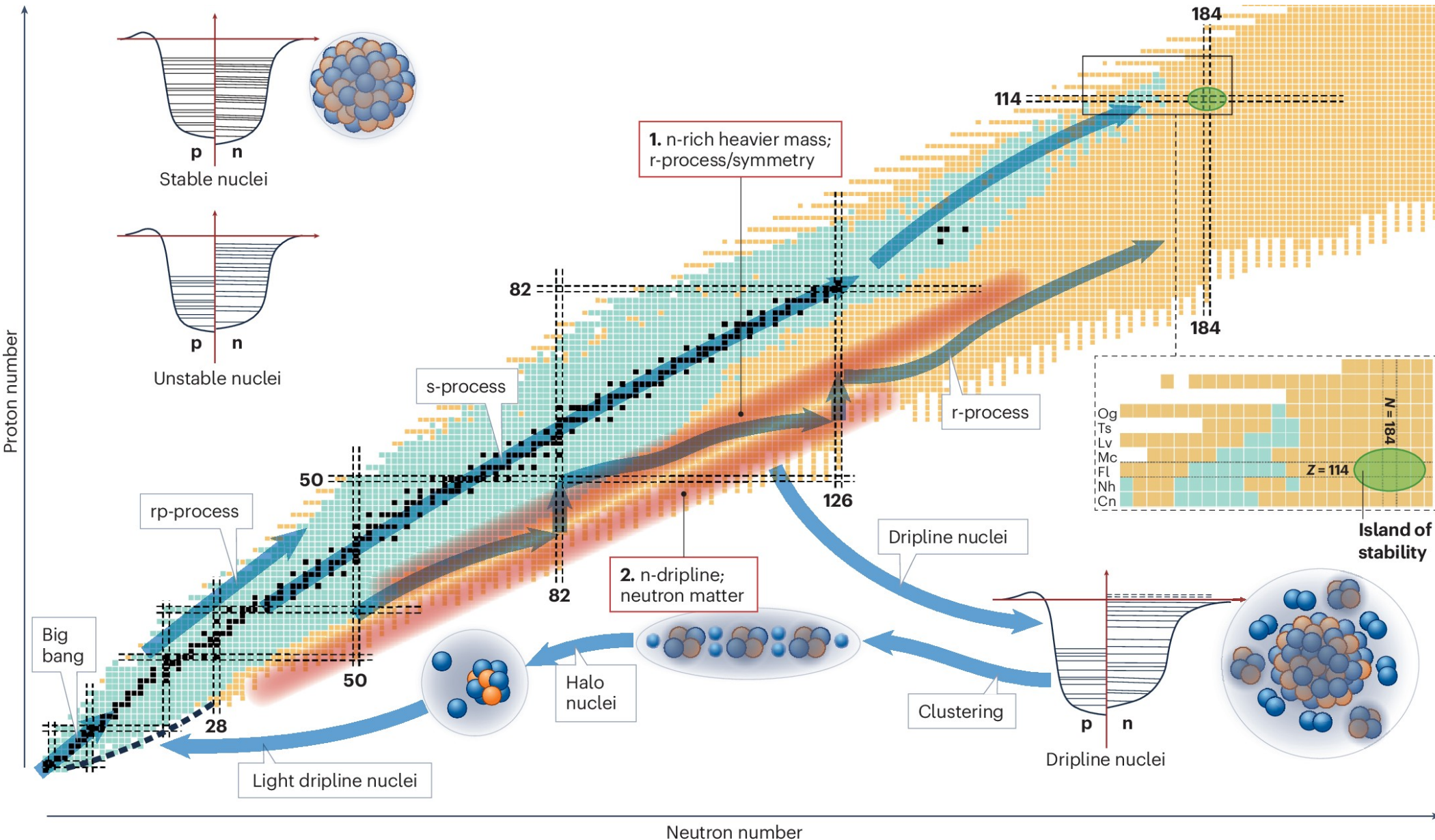
Light Nuclei : Clusters and molecular structure !



Y. Ye, X. Yang, H. Sakurai, and B. Hu, Nature Rev. Physics 7, 21 (2024)

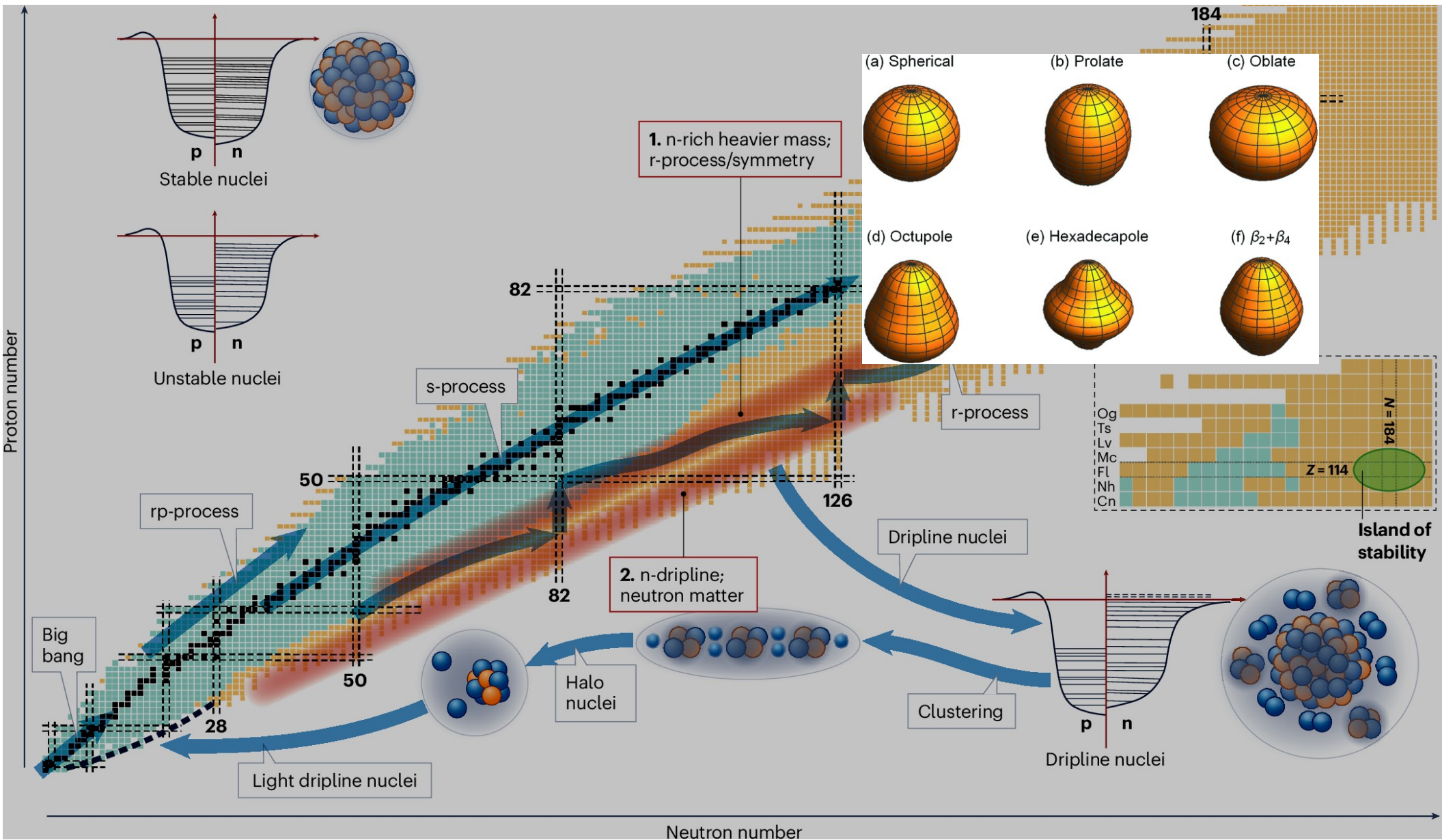
Nuclear structure (III)

Exotic nuclei : toward neutron/proton imbalance



Nuclear structure (V)

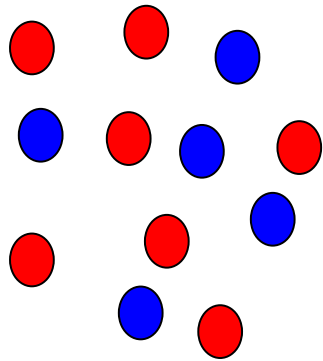
Exotic Nuclei : Deformed nuclei and shape coexistence



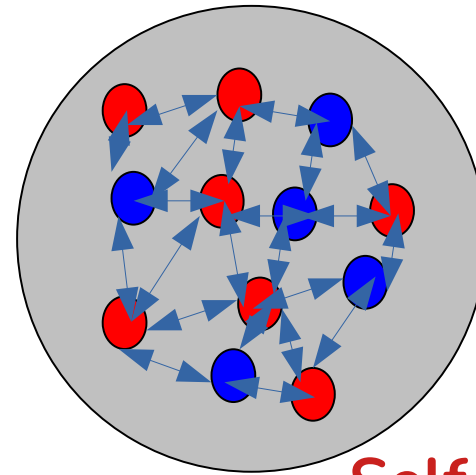
Microscopic description of nuclei : Mean-Field and beyond

Studying the limits of existence (A, I) of nuclei
What holds together nucleons and to what extend ?

Free nucleons



nucleus



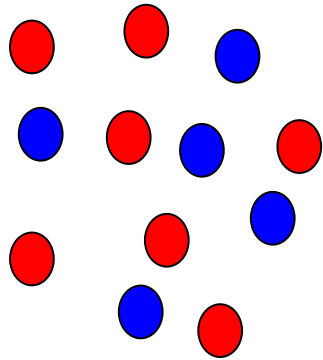
Bare NN interaction

Self-consistent
Mean-Field
Effective interaction (medium)

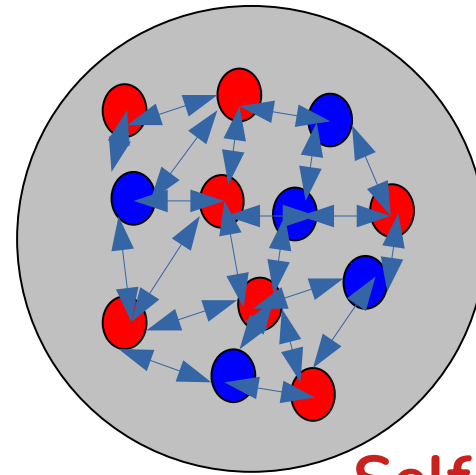
Microscopic description of nuclei : Mean-Field and beyond

Studying the limits of existence (A, I) of nuclei
What holds together nucleons and to what extend ?

Free nucleons



nucleus



Self-consistent
Mean-Field

Bare NN interaction

Effective interaction (medium)

Study of extreme states



Macroscopic description of nuclei : liquid drop

Bethe & Weisacker formula :

$$B = \overset{\text{volume}}{a_v A} - \overset{\text{surface}}{a_s A^{2/3}} - \overset{\text{coulomb}}{a_c Z^2/A^{1/3}} - \overset{\text{asymmetry n/p (isospin)}}{a_{\text{sym}} (A-2Z)^2/A} \dots$$

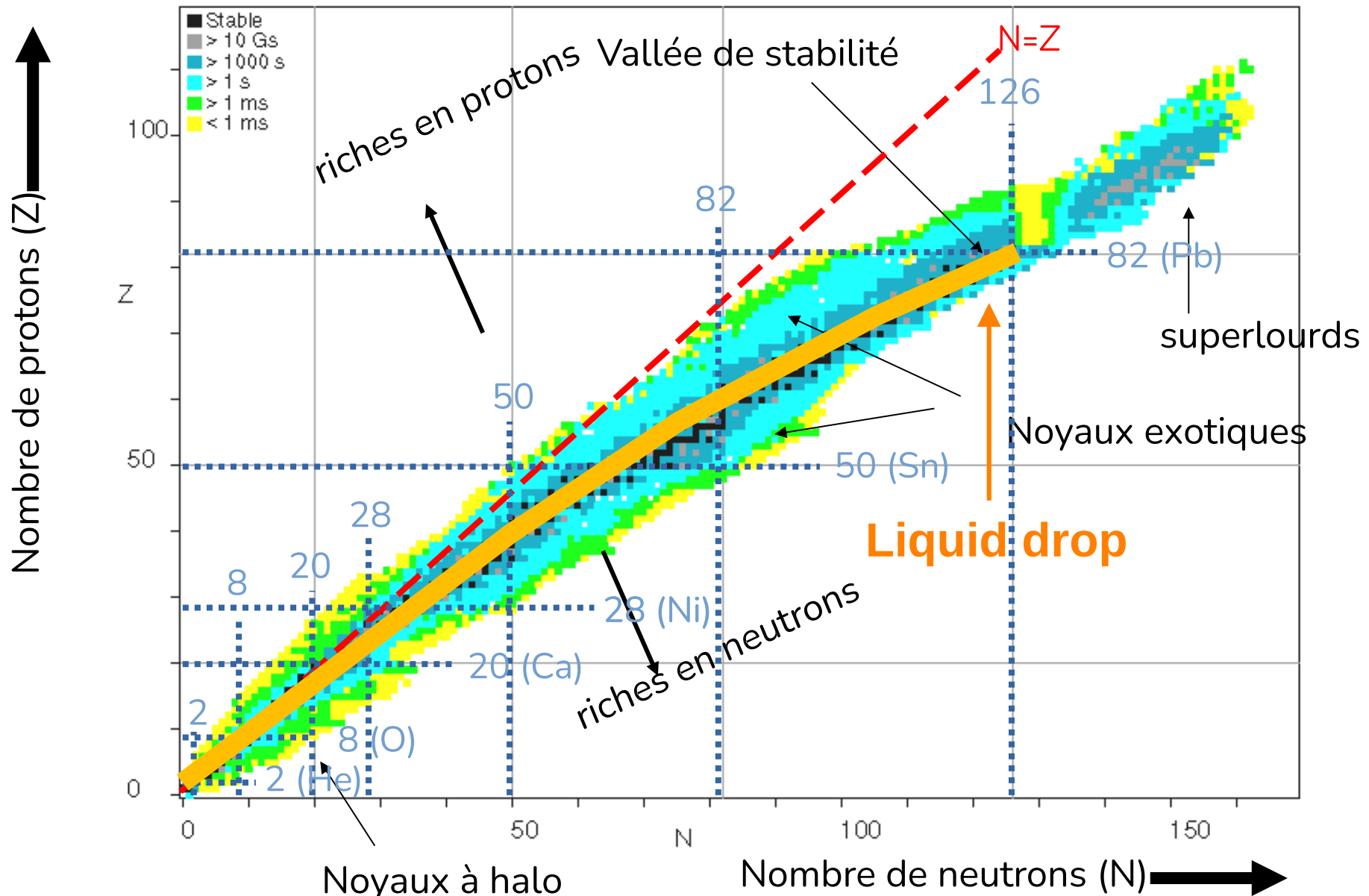
+ shell effects (magic numbers)
+ pairing (nn, pp, np)

β -stability valley, B maximum : $\partial B/\partial A = 0$

$$Z_{\text{stable}} \approx A/2 [1 + a_c/(4a_{\text{sym}}) A^{2/3}]^{-1}$$

Des noyaux à la carte

Nombres magiques : 2,8,20,28,50,82, 126, ...

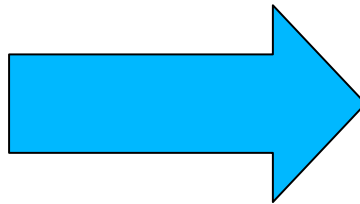
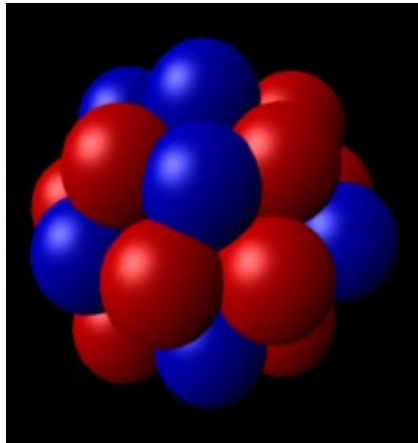


From nuclei to compact stars

Under pressure !

$$P = 10^{14} \text{ g/cm}^{-3} = 10^8 \text{ T/cm}^3$$

nucleus



Supernova / neutron star

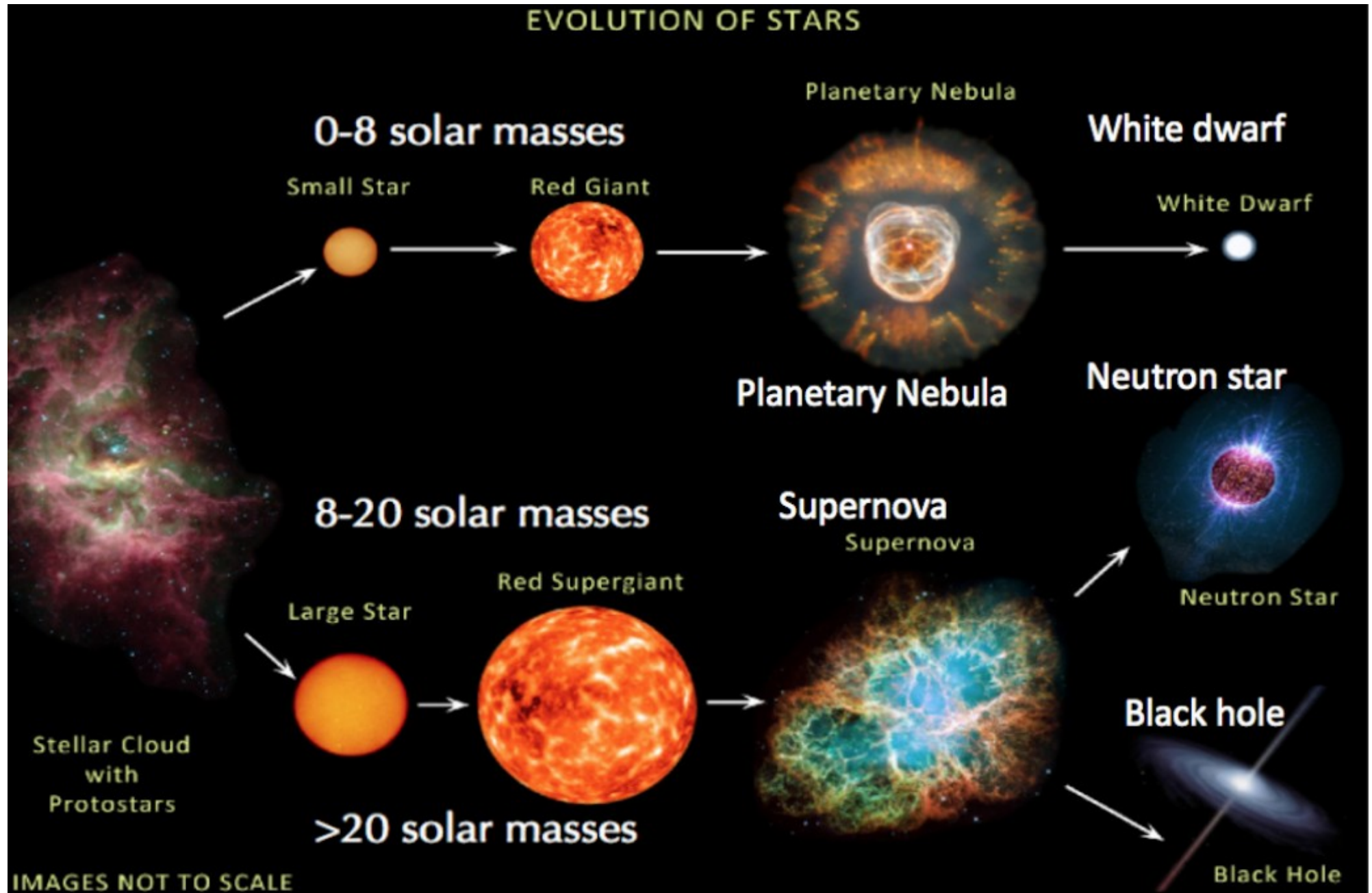


Nucleosynthesis above iron element

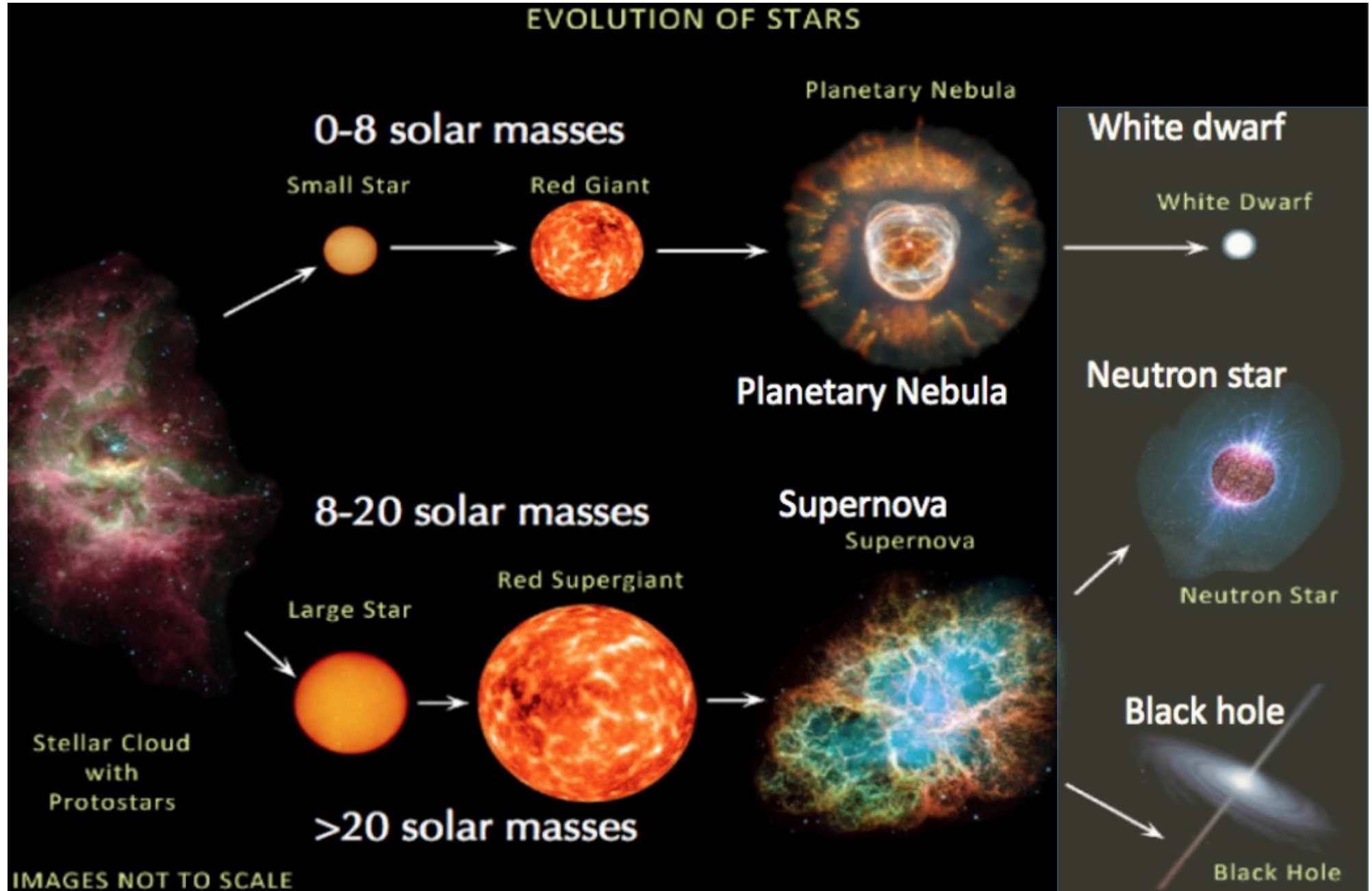
Core Collapse of Supernova : x 10,000,000,000 Sun luminosity ...

NS is ruled by the nuclear Equation of State $E(\rho, T, \delta)$

How a star becomes a neutron star ?



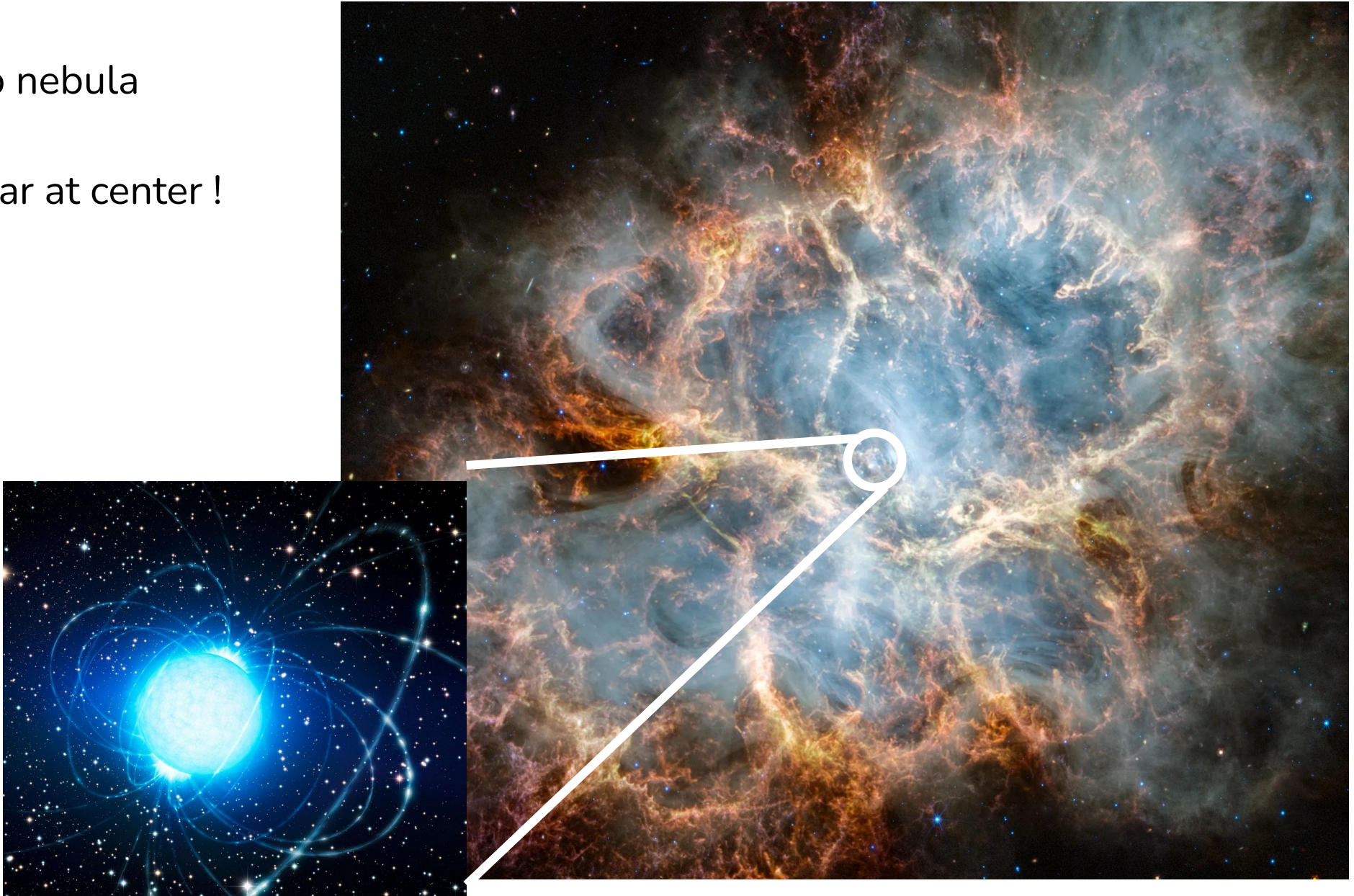
How a star becomes a neutron star ?



Neutron star : a dream for nuclear physicists ...

Crab nebula

Pulsar at center !

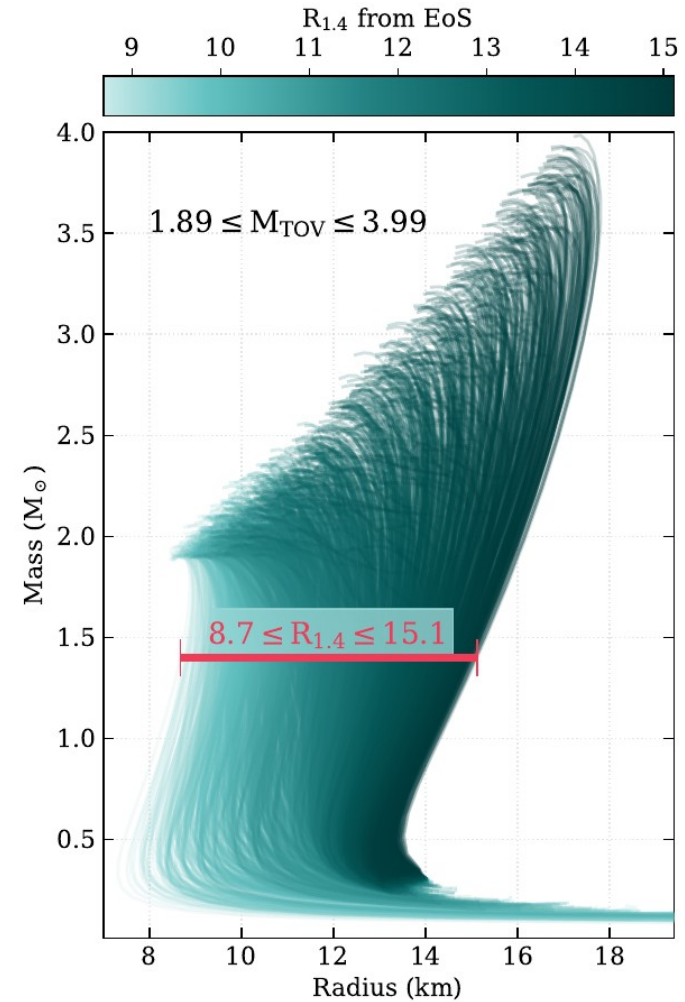
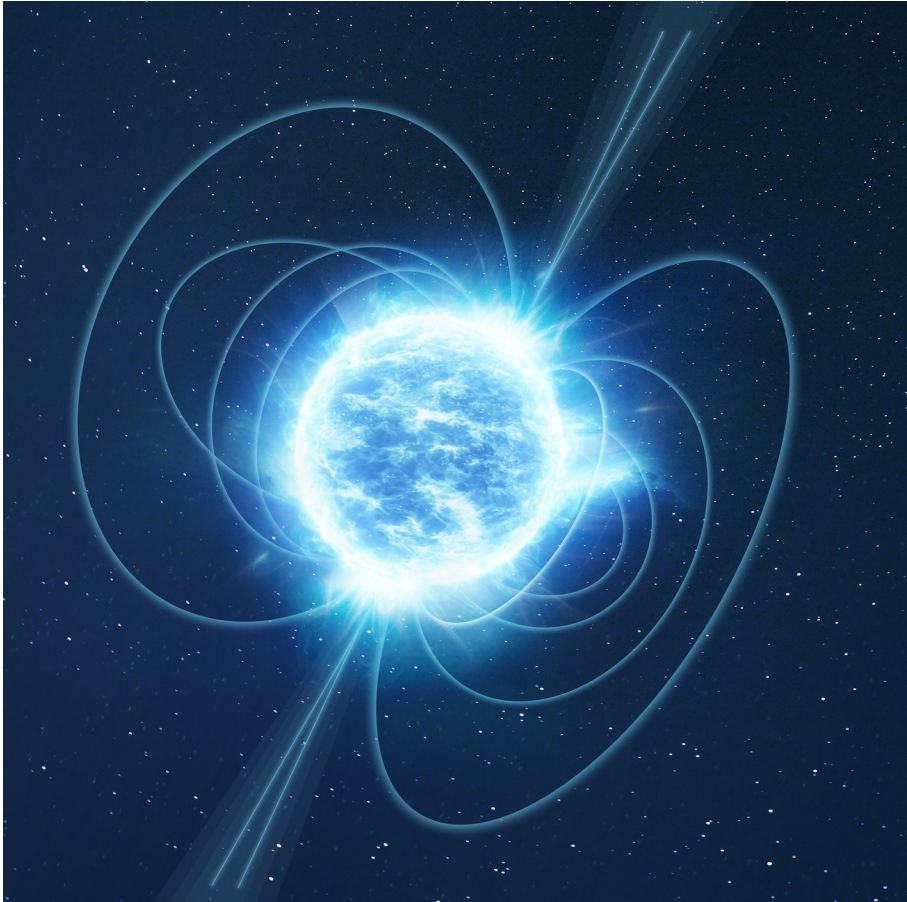


Combined image from James Webb Space Telescope

Credits NASA, ESA, CSA, STScI, T. Temim (Princeton University)

Mass – radius of a neutron star

Mass expressed as solar mass fraction



Different EOSs feature many various profiles !

Goal : try to find the best one...

Size of a big city ~ 10 km !

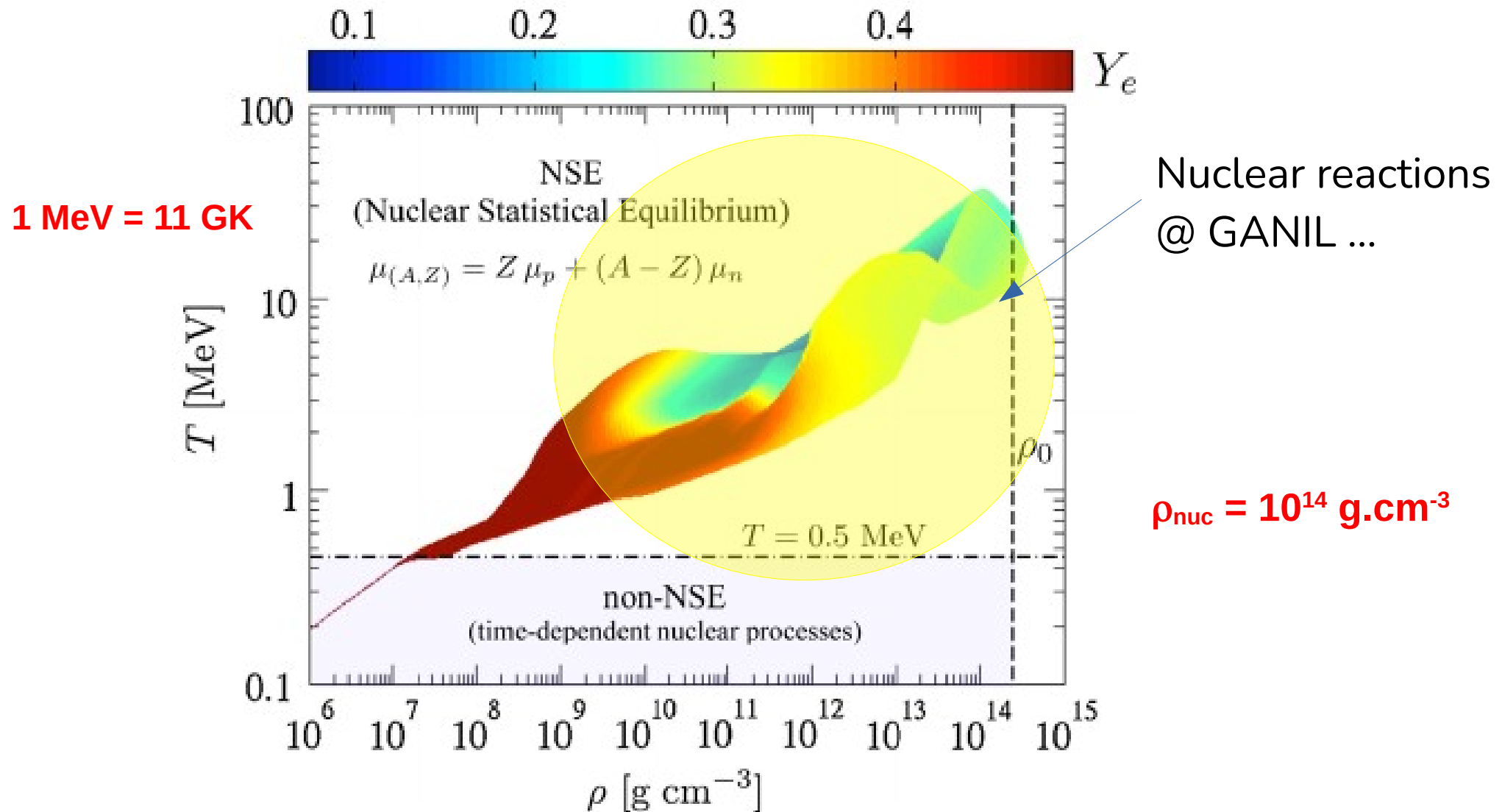
Size of a neutron star

Compared to Vancouver ...



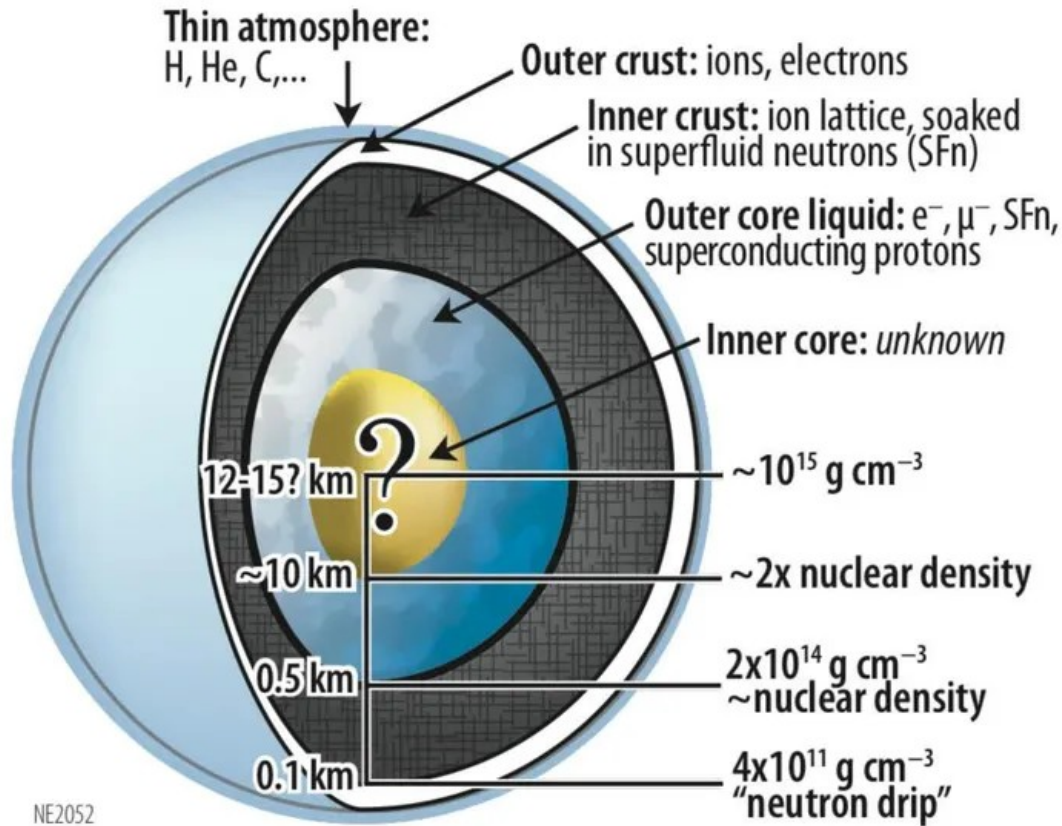
Covered domain in the plane (ρ, T)

Temperatures and densities reached during a CCSN simulation within 1s post-bounce



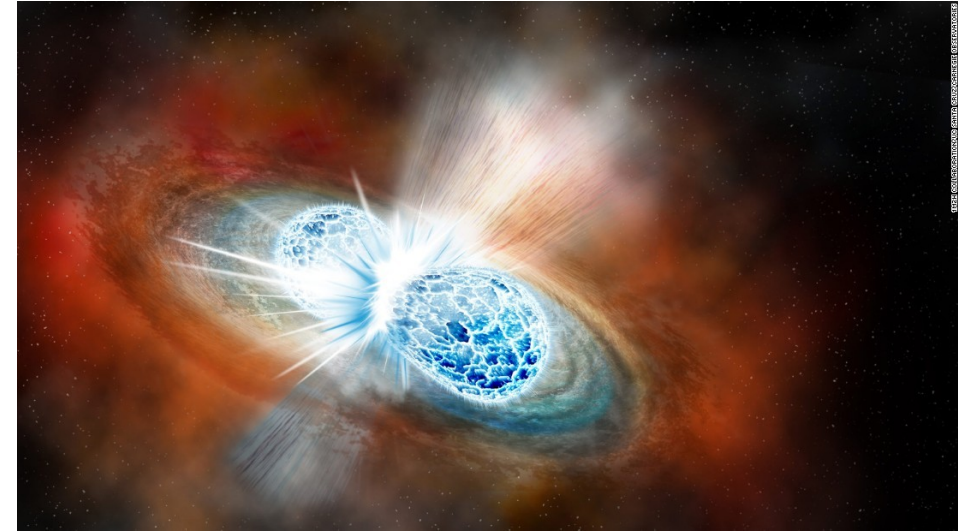
M. Oertel et al., Rev. Mod. Phys. 89, Vol. 1 (2017)

Neutron star : a dream for nuclear physicists ...



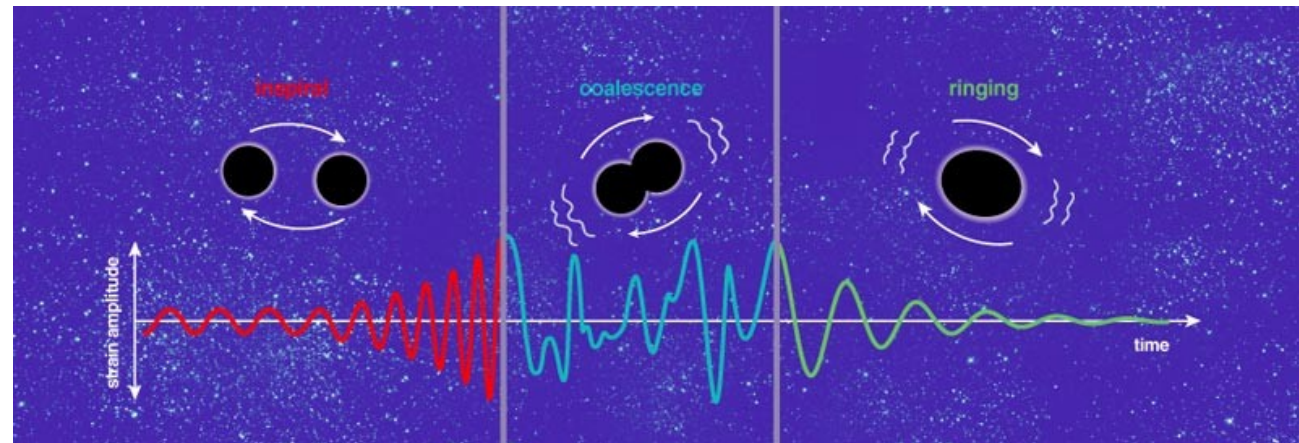
NE2052

NS – NS merger



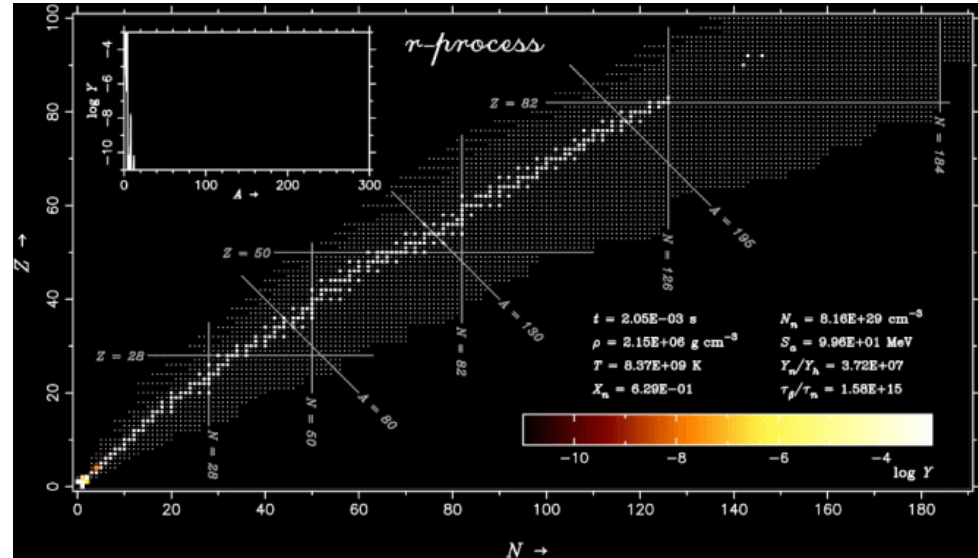
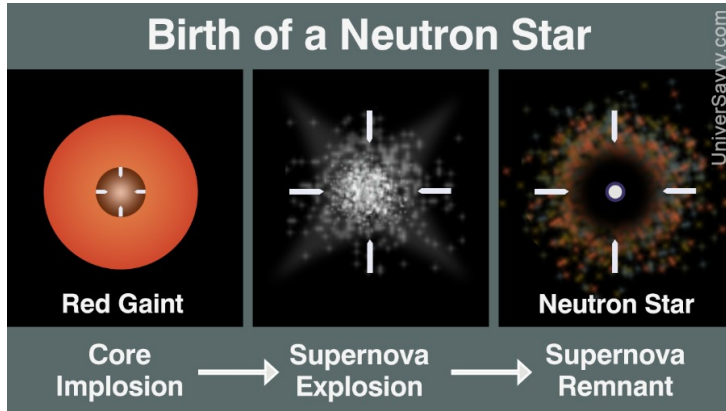
Gravitational waves

Ligo/Virgo



Nuclear EOS in Astrophysics

Neutron Stars (NS) are unique systems for investigating dense nuclear matter !



B.P. Abbott et al. (LIGO/VIRGO),
PRL **116**, 061102 (2016)
PRL **119**, 161101 (2017)

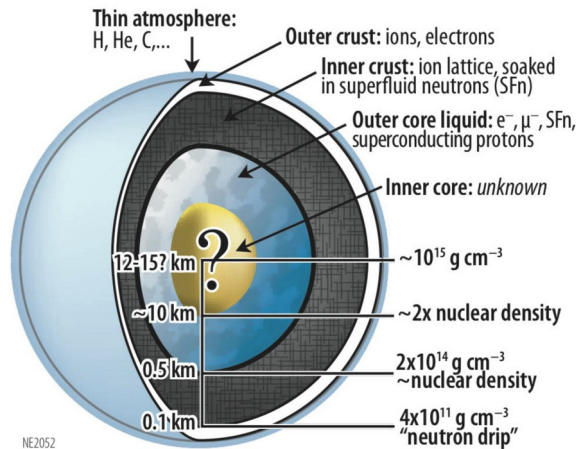
Detection of GW and multi-messenger observables (GW170817) considerably reinforces terrestrial EOS studies

Core Collapses Sne

- EoS (isoscalar/isovector) : **shock waves**
- E_{sym} : **r-process** and **nucleosynthesis**
- Cooling : **d-URCA** and **Neutrinosphere** (low density nuclear matter)

NS structure :

- Crust : **pasta phases** (frustration/clusters)
- Crust/Core transition: L, K_{sym}
- Core : **hyperons** (strange matter, QCD)



N. Yunes, M. Coleman Miller, and K. Yagi,
Nature Review Physics **4**, 237 (2022)

NS- NS merger (Kilonova)



Key questions in Nuclear Physics

How can we build the atomic nucleus starting from **QCD first principles** and the strong interaction ?

Effective interactions and ab-initio models

Nucleus as a **many-body quantum system** : how can we explain and predict the **observed regularities** : magic numbers, collective excitations, pairing, drip lines, ... ?

Shell model(s) and approaches beyond the Mean-Field

How can we describe **nuclear matter** at very **different scales** as in nuclei (microscopic) and in compact stars and neutron star mergers (macroscopic) ?

Equation of State of nuclear matter / phase transitions

Nucleosynthesis

Where the matter comes from ?

Abundance
of elements
in the Universe

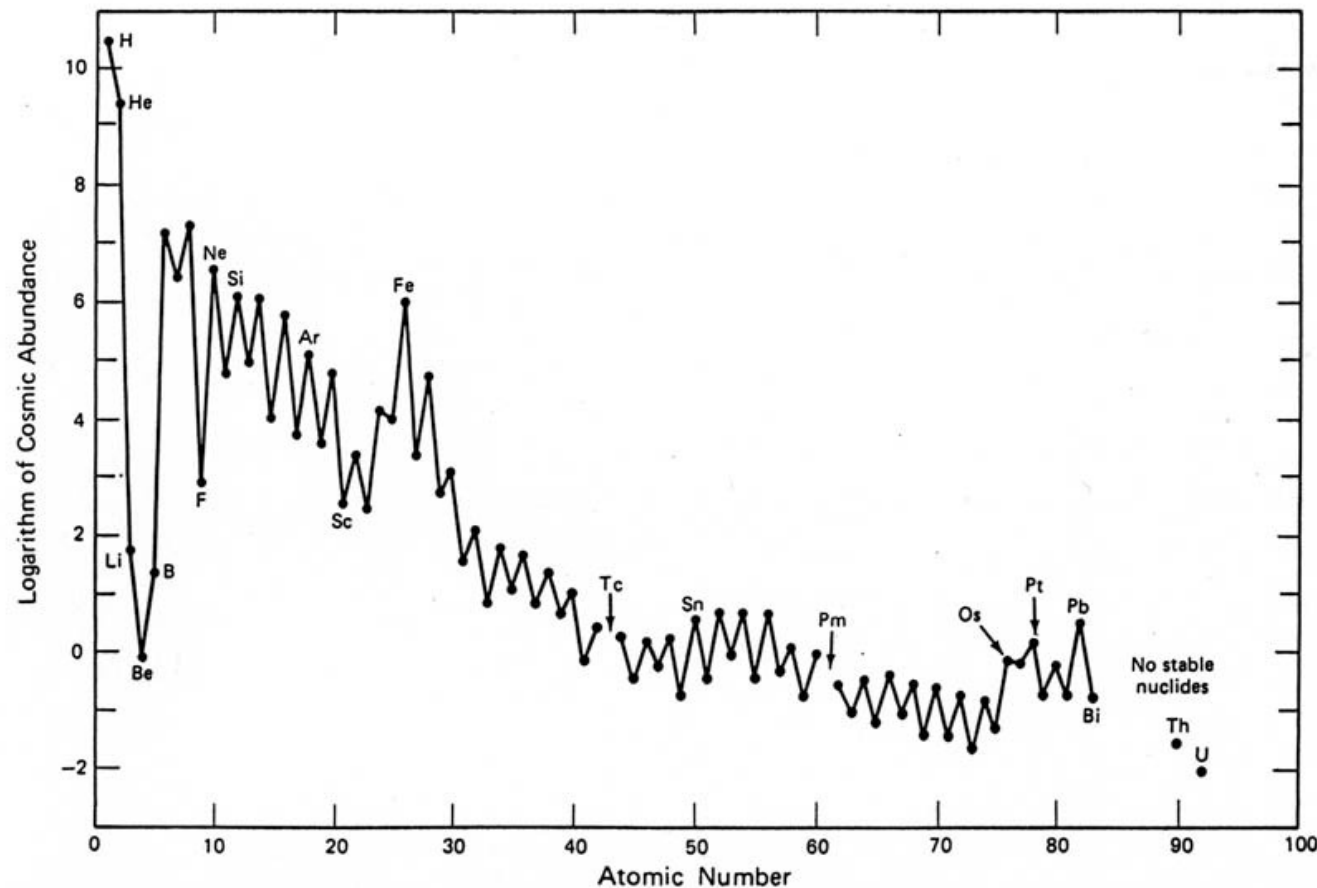


Figure 2.4 Plot of the abundances of the elements in the solar system versus their atomic number. The abundances are expressed as the logarithm of the number of atoms of each element relative to 10^6 atoms of silicon. (Data are listed in Table 2.2 after Anders and Ebihara, 1982.)

Nucleosynthesis : different origins

Primordial Hydrogen (Big Bang)
 $Z=1$

Stellar synthesis
 $Z=2-26$

Abundance
of elements
in the Universe

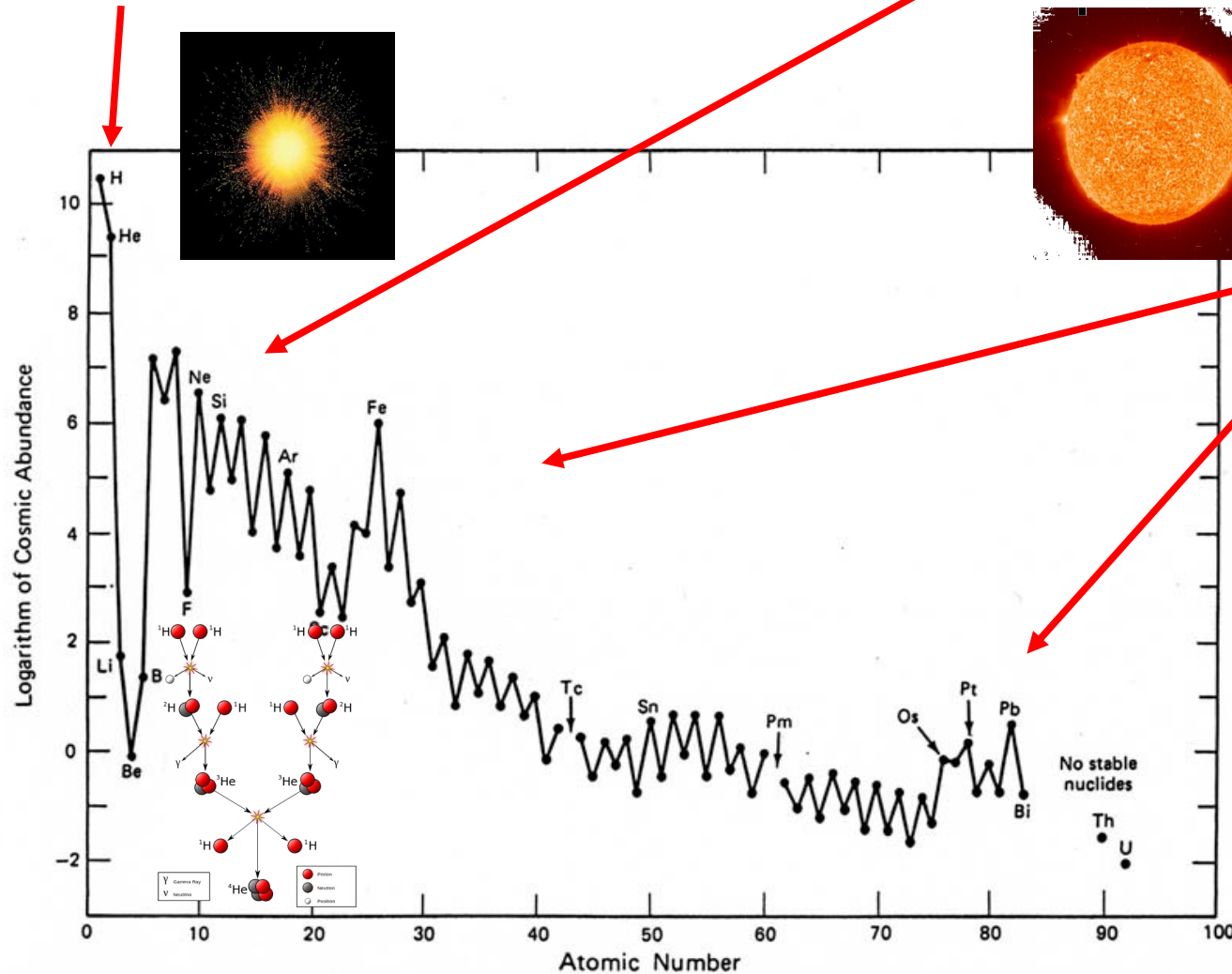


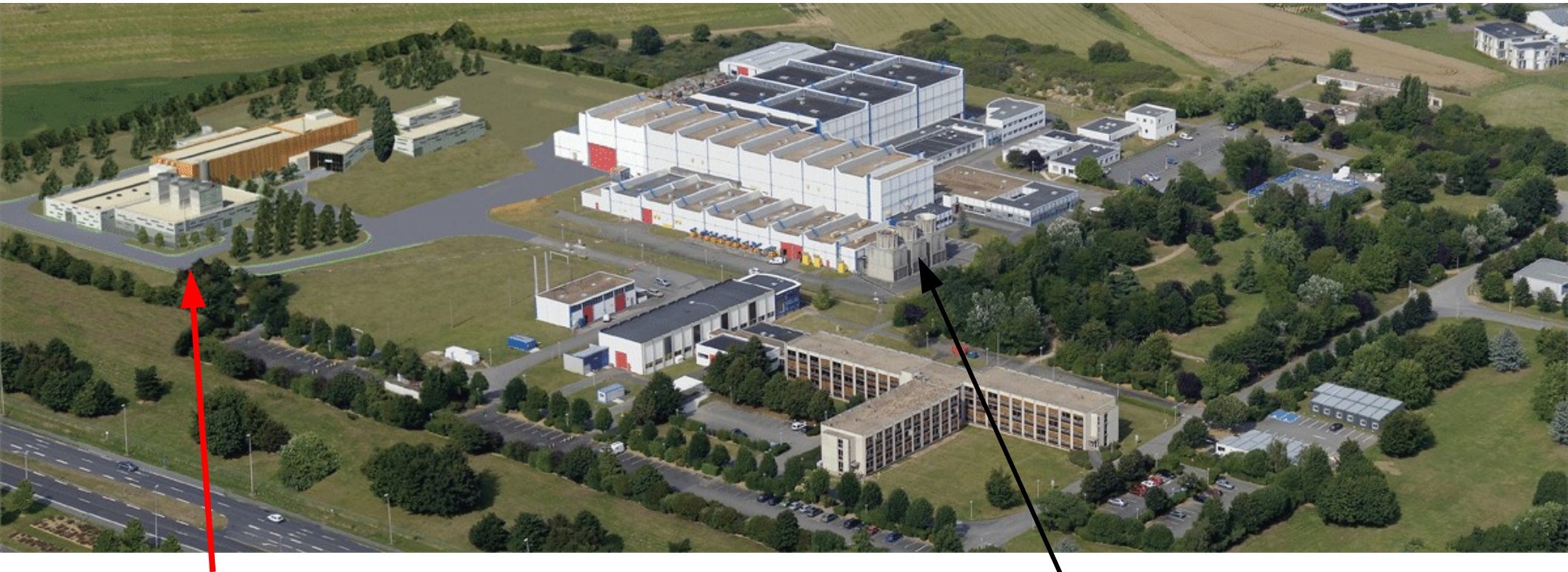
Figure 2.4 Plot of the abundances of the elements in the solar system versus their atomic number. The abundances are expressed as the logarithm of the number of atoms of each element relative to 10^6 atoms of silicon. (Data are listed in Table 2.2 after Anders and Ebihara, 1982.)



Extra-stellar
processes
r/s/p-processes
in supernovae
and NS-NS
mergers
 $Z>26$

Terrestrial experiments

At GANIL (Caen, Normandy, France), many teams study heavy ions induced nuclear reactions to investigate stable and exotic nuclei properties



SPIRAL2

New SC-LINAC :

Intense p,d and HI beams

$E_{inc} = 5 - 20 \text{ MeV/nucl.}$

GANIL/SPIRAL1

CSS1/CSS2/CIME :

Stable beams (He-U) $E_{inc} = 5 - 100 \text{ MeV/nucl.}$

Radioactive beams $E_{inc} = 5 - 15 \text{ MeV/nucl.}$

SPIRAL2

L'ACCÉLÉRATEUR LINÉAIRE SUPRACONDUCTEUR

délivre des faisceaux de particules de très grande intensité : le nombre de collisions entre les particules accélérées et les noyaux de la cible de matière est ainsi plus important.

GANIL

LES SALLES D'EXPÉRIENCES

renferment des systèmes de détection et de mesure très sophistiqués, permettant d'étudier les propriétés de noyaux très exotiques.

GANIL

L'ENSEMBLE ACCÉLÉRATEUR,

composé de cinq cyclotrons, accélère des faisceaux d'ions allant du carbone-12 à l'uranium-238 à différentes énergies adaptées aux types d'expériences réalisées. Les ions de carbone-12 peuvent par exemple atteindre 120 000 kilomètres par seconde, soit plus du tiers de la vitesse de la lumière.

SPIRAL2

LES SOURCES D'IONS DE SPIRAL2

permettent de produire un large éventail de particules, dont de très légères comme les deutons ou les protons.

GANIL

LES SOURCES

permettent de produire les ions stables ou radioactifs qui seront ensuite mis en faisceaux et accélérés.

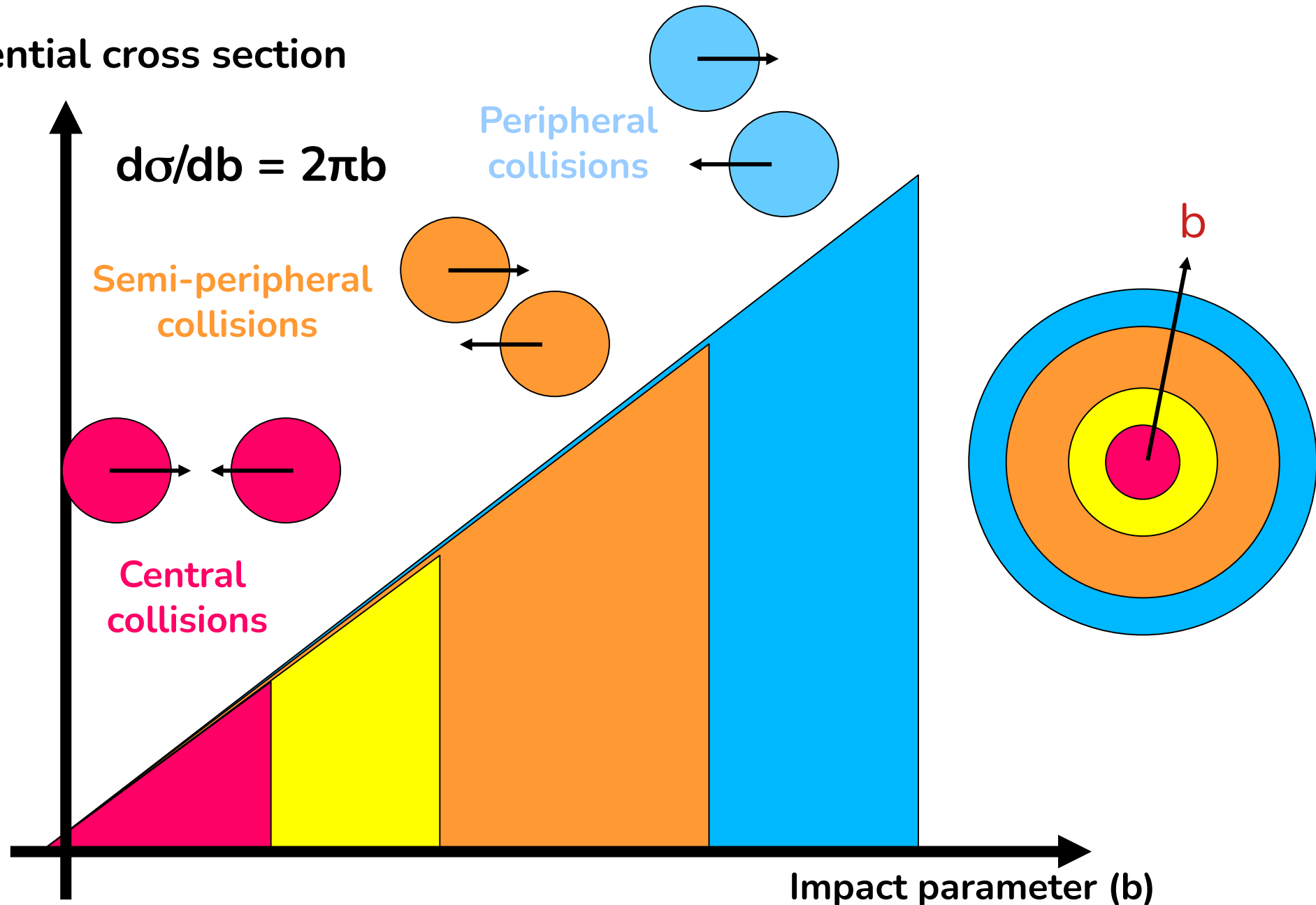
End part I

Part II

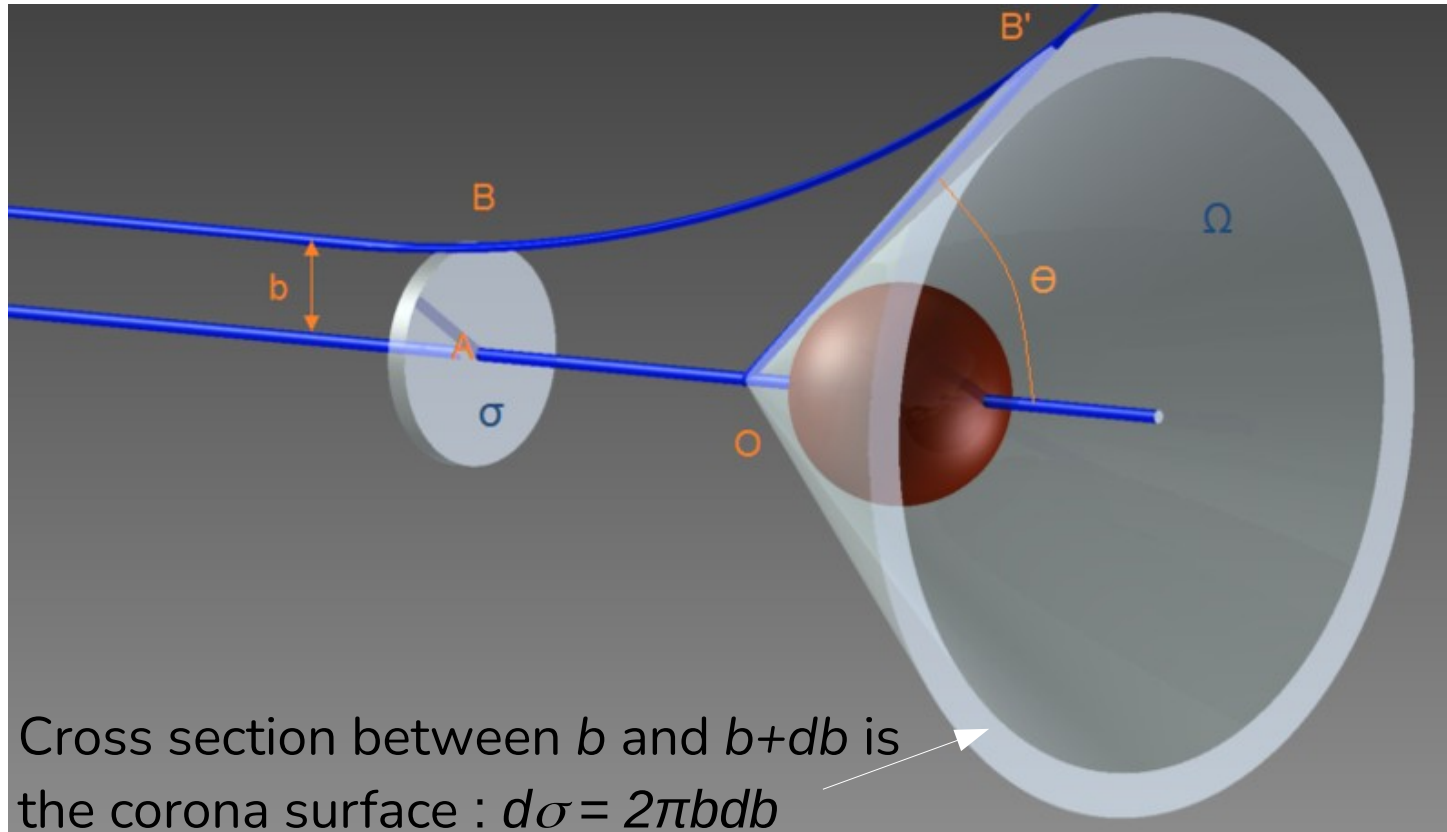
Some basic concepts of nuclear reactions

Nuclear reactions : playing darts ...

Differential cross section



Cross section in Classical Physics



Integrating over b , we get : $\sigma(b) = \pi b^2$

Unit is the barn (b), $1b = 10^{-28}m^2 = 10^{-24}cm^2$

For a typical nuclear reaction between Hl , we have $b_{\text{grazing}} \approx 10 \text{ fm}$,

then $\sigma_{\text{nuc}} = 3,142 b = 3142 \text{ mb}$

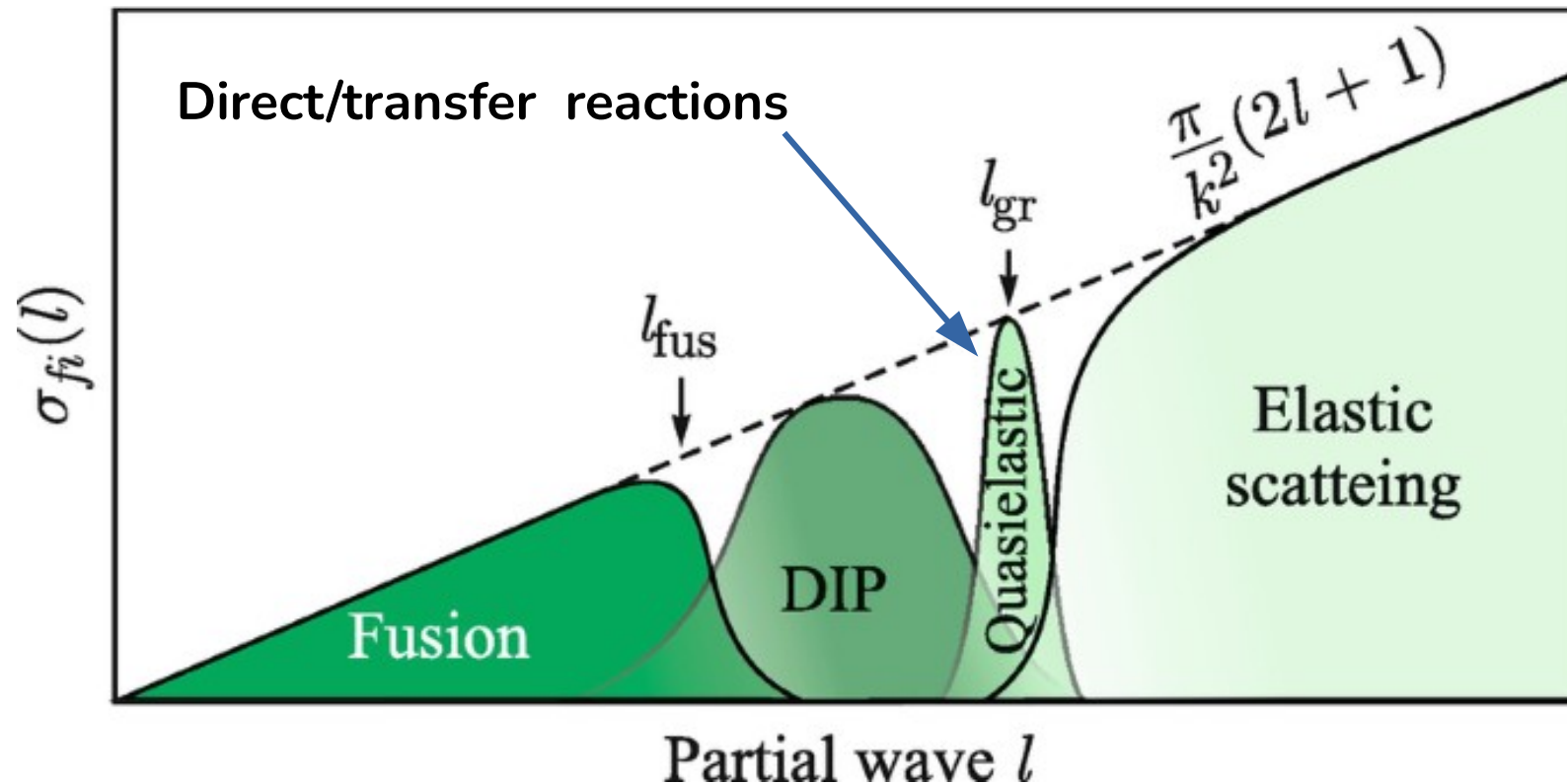
Cross section in Quantum Mechanics : partial waves

Total nuclear cross-section

$$\sigma_{nuc} = \pi b_{gr}^2 \approx \pi \ell_{gr}(\ell_{gr} + 1) \hbar^2 / \mu v$$

Classical ansatz :

$$|\ell| = \sqrt{l(l+1)} \hbar = \mu v b$$



$$\sigma_r = \frac{\pi}{k^2} \sum_{\ell=0}^{\ell_{max}} (2\ell + 1)(1 - \eta_{\ell}^2)$$

η_{ℓ} is the **inelasticity coefficient** for partial wave ℓ
 $\eta_{\ell} = 0$ for **elastic** and $0 < \eta_{\ell} < 1$ for **absorption**

Cross section and event rate

Event rate Er (s^{-1}) for a specific reaction cross section σ_r :

$$Er_{\text{reac}} = \mathcal{F} \rho \mathcal{N} e \sigma_r / A$$

where :

- $\mathcal{F}$ is the incident flux of particles per unit of time (s^{-1})
- ρ is the density of the target material ($g.cm^{-3}$)
- e is the target thickness (cm)
- A is the molar mass of the target material ($g.mol^{-1}$)
- $\mathcal{N} = 6.022.10^{23}$ is the Avogadro number
- σ_r is the reaction cross section (cm^2)

Cross section and event rate

Event rate E (s^{-1}) for a specific reaction cross section σ_r :

$$E_{\text{reac}} = \mathcal{F} \rho \mathcal{N} e \sigma_r / A$$

Thin target
e=300 μm , Au

Reaction $\mathcal{F} = 10^9$ pps	Cross section	Event rate
Coulomb scattering	100 b	1000 s^{-1}
Deep Inelastic/ Multi-nucleon Transfer	1 b	10 s^{-1}
Central collision ($b < 1$ fm)	50 mb	1 mn^{-1}
Transfer/direct reaction	10 mb	10 hr^{-1}
Fusion reaction	1 mb	1 week^{-1}

Nuclear reactions

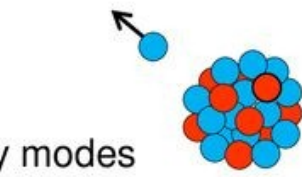
Producing exotic nuclei

Physics cases for nuclear reactions : driplines

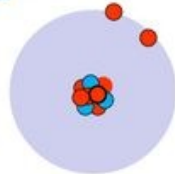
Nuclear chart at the borders : Driplines & SHE

118 known elements
~ 3000 known isotopes
~ 4000 still unknown isotopes

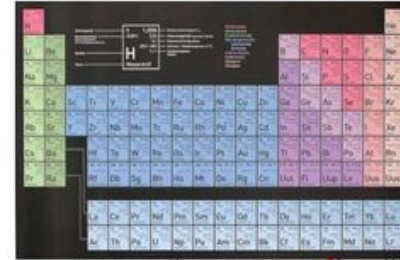
New decay modes
Proton emission



Exotic nuclear structure
Halo nuclei



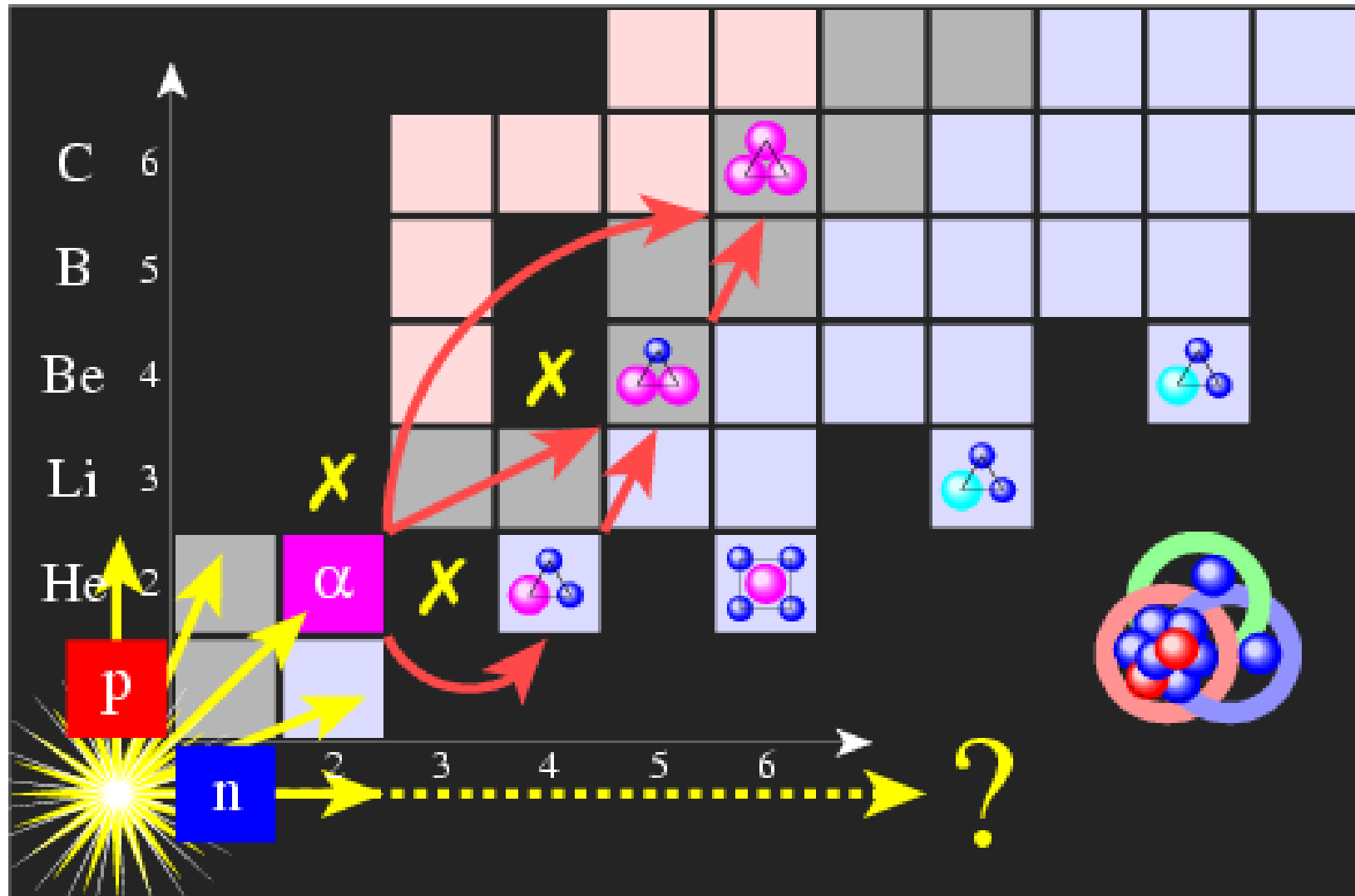
Superheavy nuclei



**Astrophysical
nucleosynthesis**

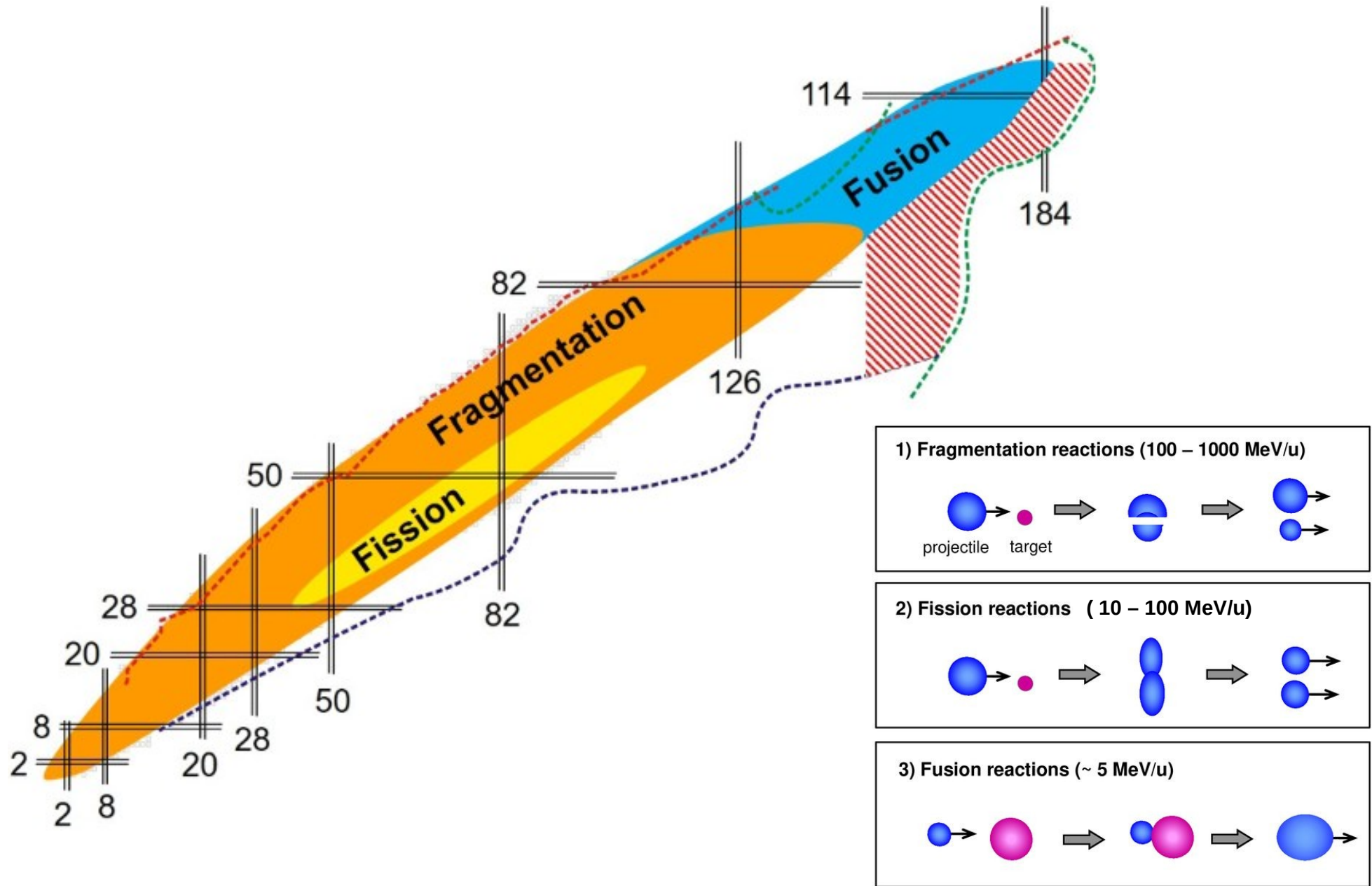
Also Haloes nuclei...

► les noyaux légers à (N, Z) extrêmes :

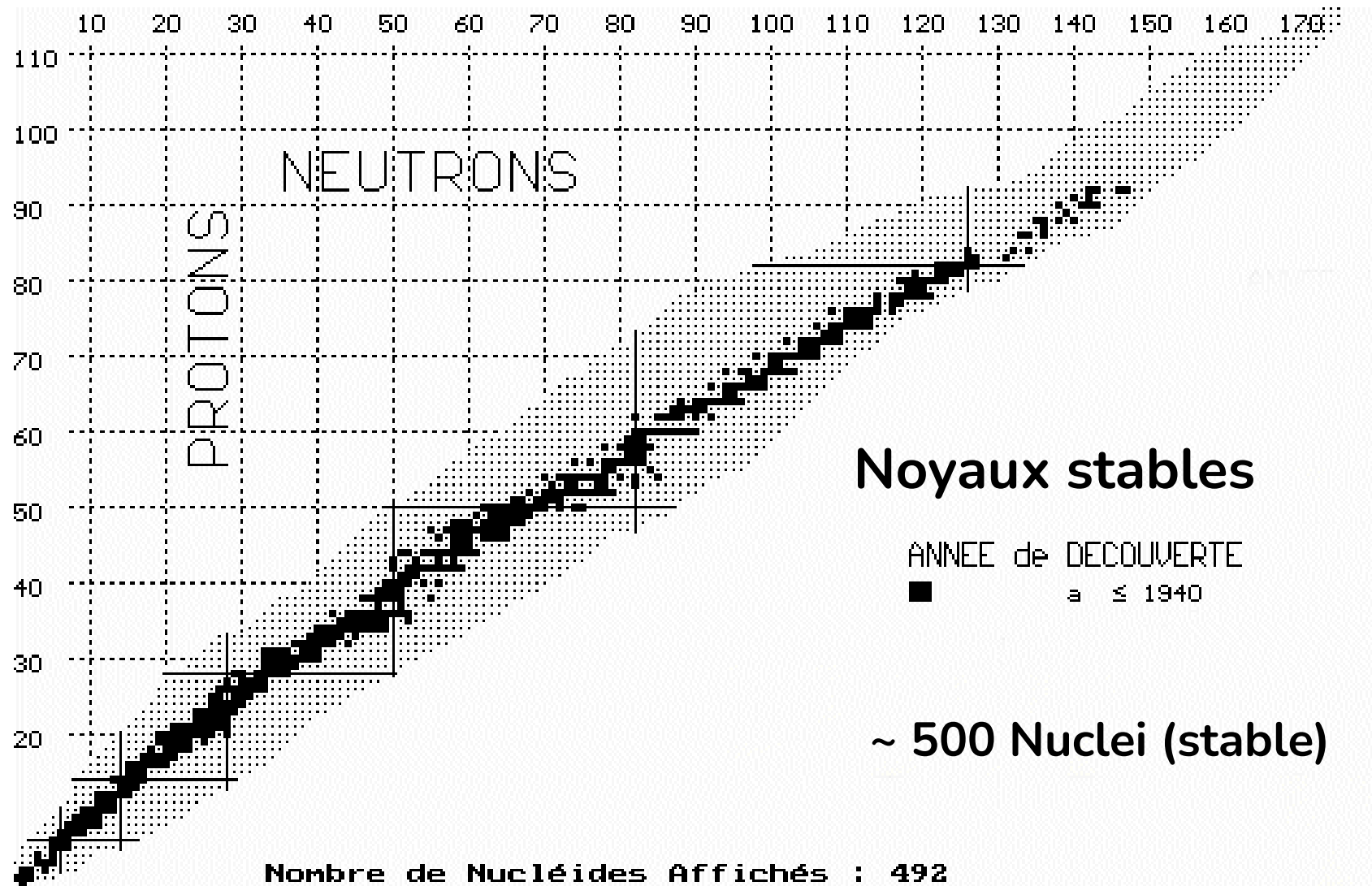


Courtesy Miguel Marques (LPC Caen)

Production of exotic nuclei with HI beams

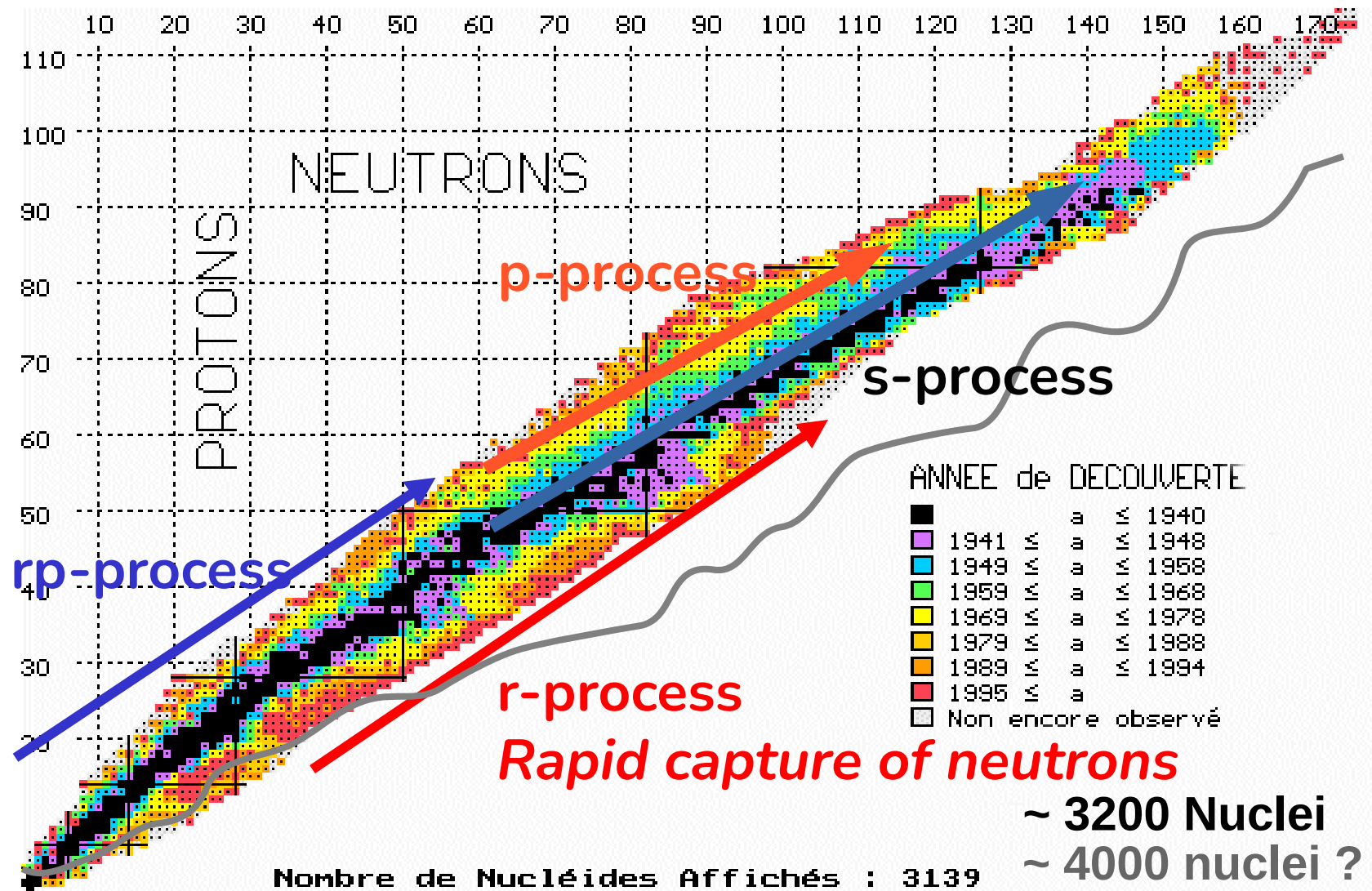


Known nuclei before WW2



Known Nuclei now : astrophysical processes

“Terra Incognita”



Nuclear reactions

Reaction Mechanisms

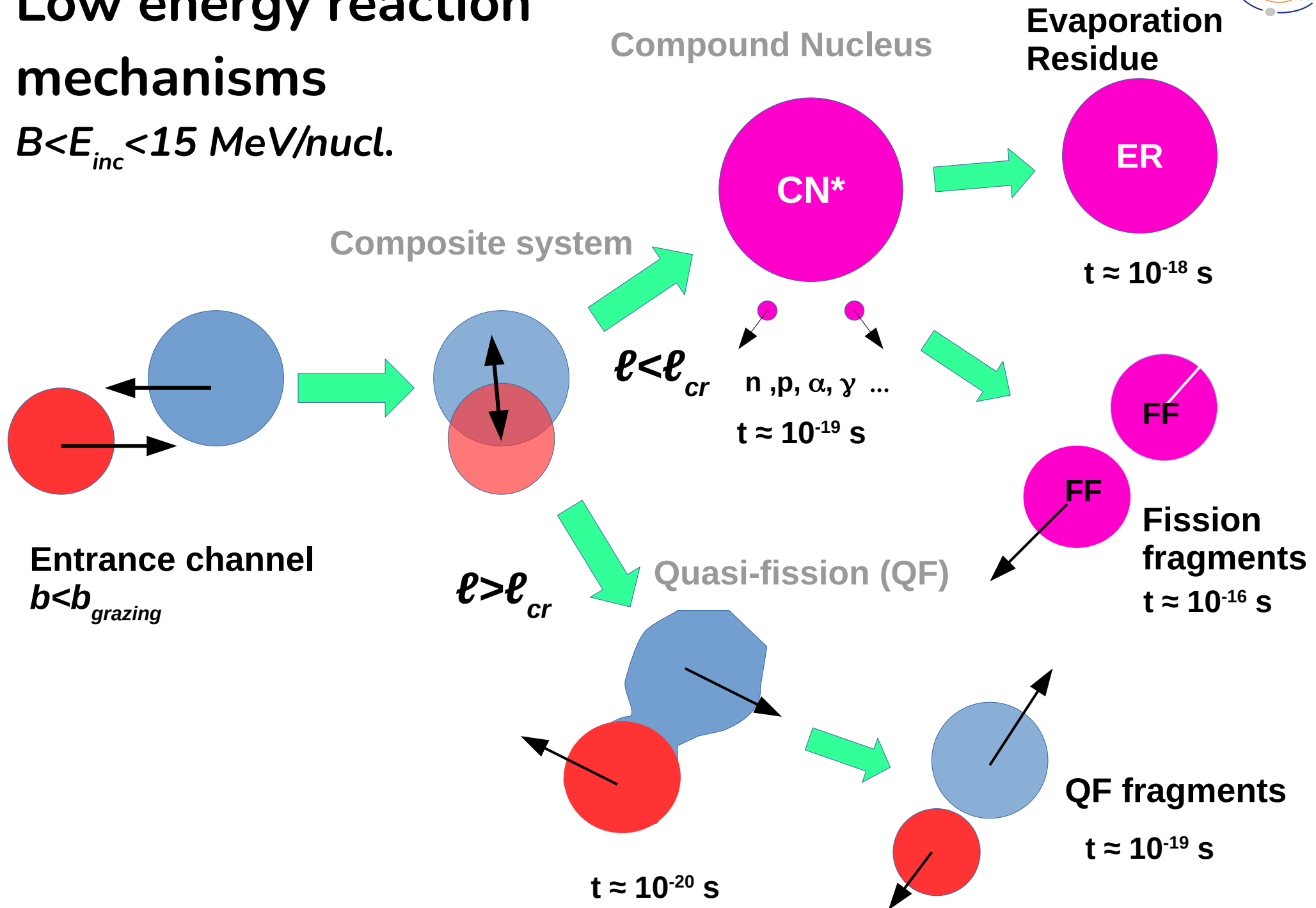
Nuclear reactions

Low incident energy

5 – 15 MeV/nucleon

Low energy reaction mechanisms

$$B < E_{inc} < 15 \text{ MeV/nucl.}$$



Nuclear reactions

Fermi incident energy

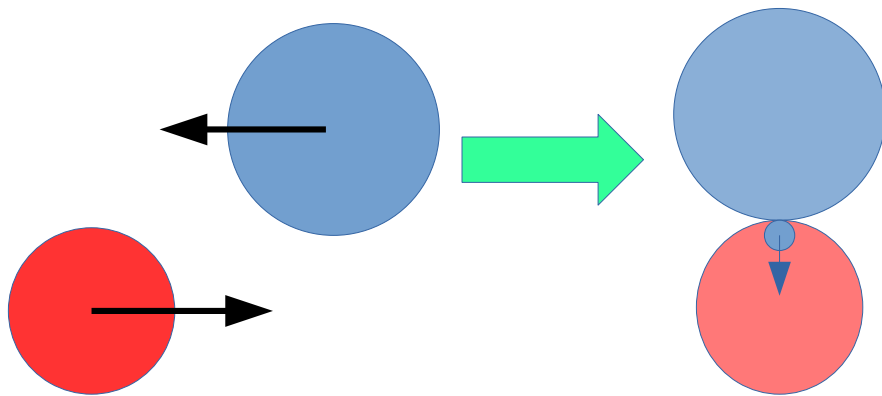
15 – 50 MeV/nucleon

Fermi energy reaction mechanisms

$15 < E_{inc} < 50 \text{ MeV/nuc.}$

Transfer or direct reactions $b \approx b_{grazing}$

Stripping/pick up of nucleon(s)



Entrance channel

$b \approx b_{grazing}$

Examples :

(d,p) : +1n transfer (r-process)

(t,p) : +2n transfer (r-process)

(p,t) : -2n transfer (rp-process)

(^3He ,d) : +1p transfer (rp-process)

...

Transfer reactions at low incident energy

$E_{\text{inc}} < 50 \text{ MeV/nuc.}$

Projectile $X(N)$ on a deuteron target with the pickup of one neutron to obtain $Y = X(N+1) \rightarrow$ more neutron-rich nucleus

Peripheral collision

with $b \approx b_{\text{grazing}}$

Sizeable cross section (b)

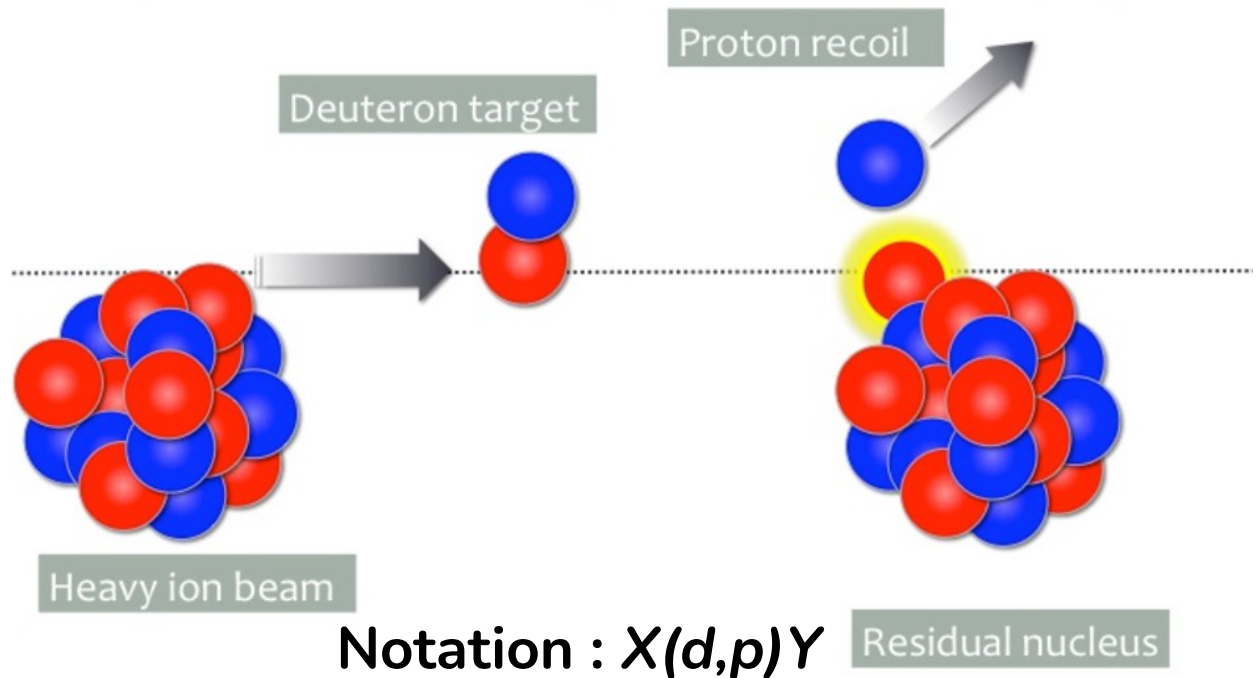


Complete kinematical reconstruction of the reaction / decay

Master the decay process

Limited to few nucleons transfer/pickup

Small excursion toward drip lines



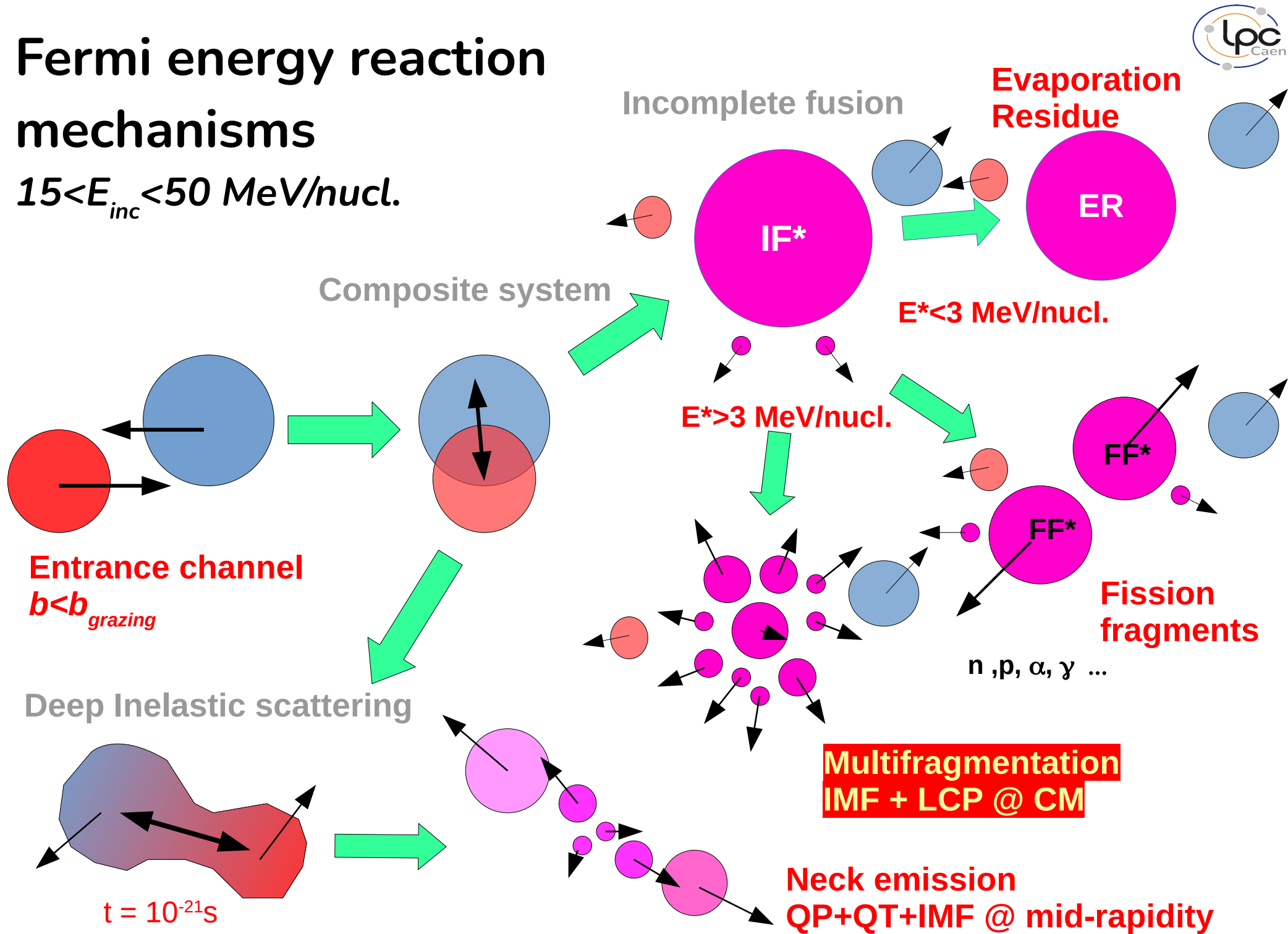
Limited angular momentum selectivity (few $\hbar$)

Few discrete states accessible



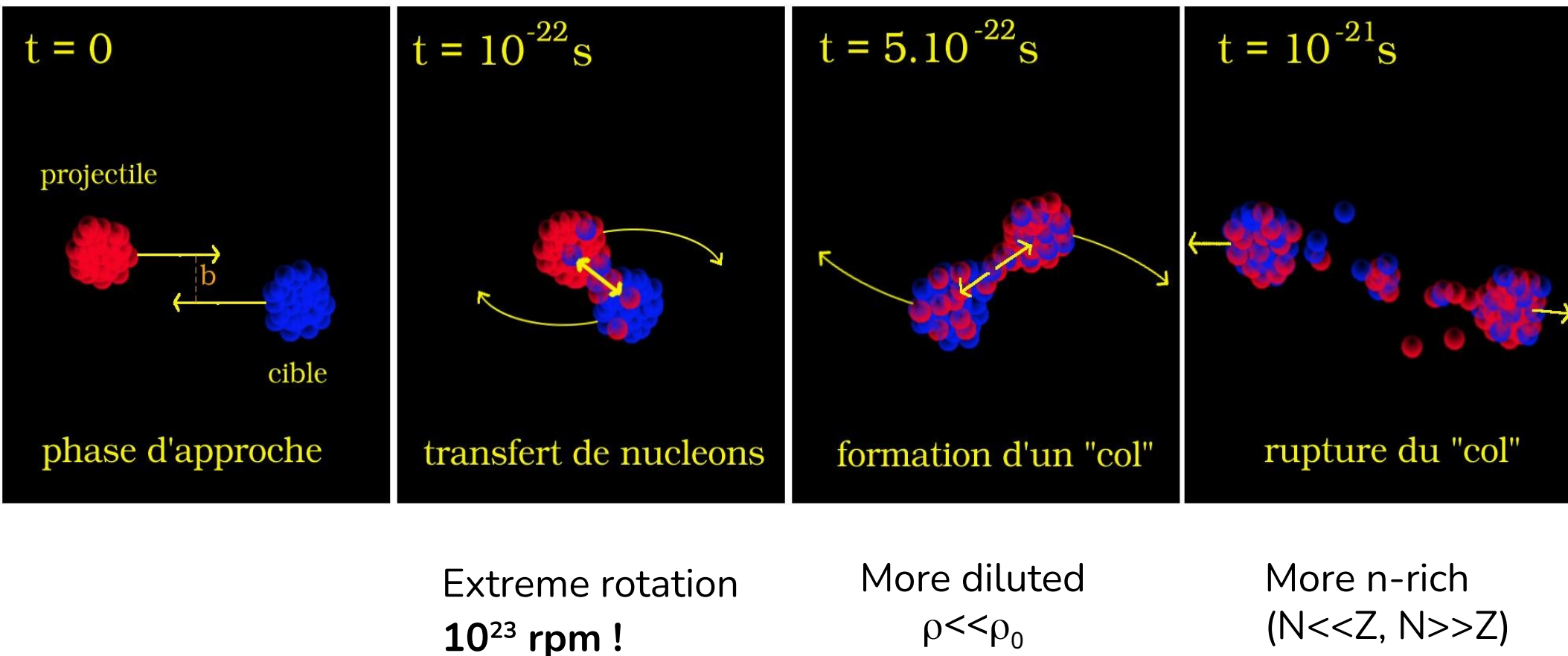
Fermi energy reaction mechanisms

$15 < E_{inc} < 50 \text{ MeV/nucl.}$



Deep Inelastic collisions ... toward the limits

« semi-peripheral » collision ($b=6$ fm)



Simulation Xe+Sn at 39 MeV/nucleon $b=4$ fm

Nuclear Collision Simulation

($Z=54, A=129$) on ($Z=50, A=119$) @ $E/A = 50 \text{ MeV}$, $b=4.0 \text{ fm}$
HIPSE model - Phys. Rev. C69, 054604 (2004)
D. Lacroix (GANIL) and D. Durand (LPC Caen)

Simulation done by O. Lopez (lopezo@in2p3.fr)
Details at <http://www.lpc-caen.in2p3.fr>

Nuclear Collision Simulation

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Simulation done by O. Lopez (lopezo@in2p3.fr)
Details at <http://www.lpc-caen.in2p3.fr>

Deep Inelastic Scattering

$$15 < E_{inc} < 50 \text{ MeV/nucleon}$$

Projectile is **damped** and **rotate** around the target

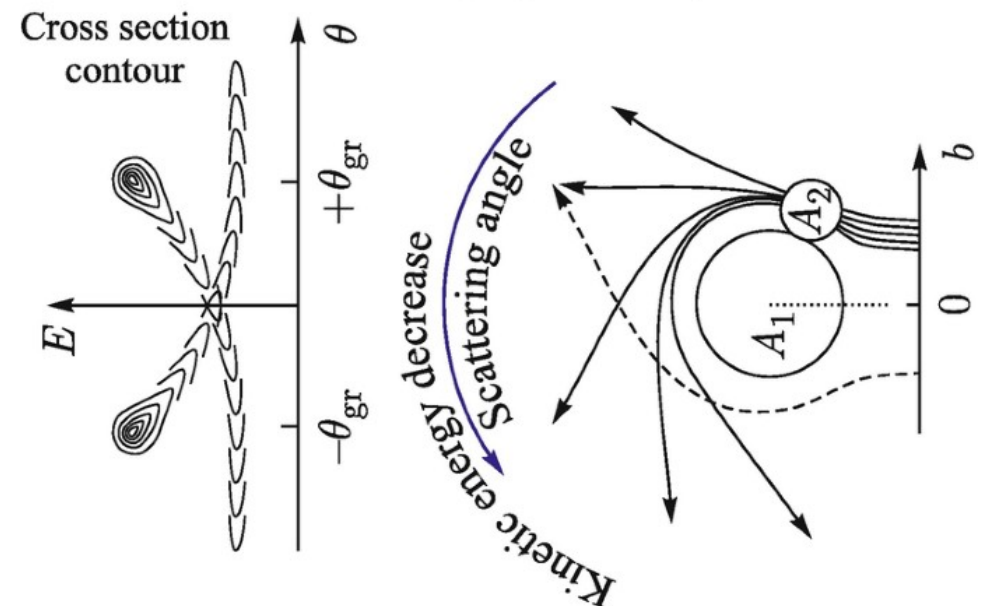
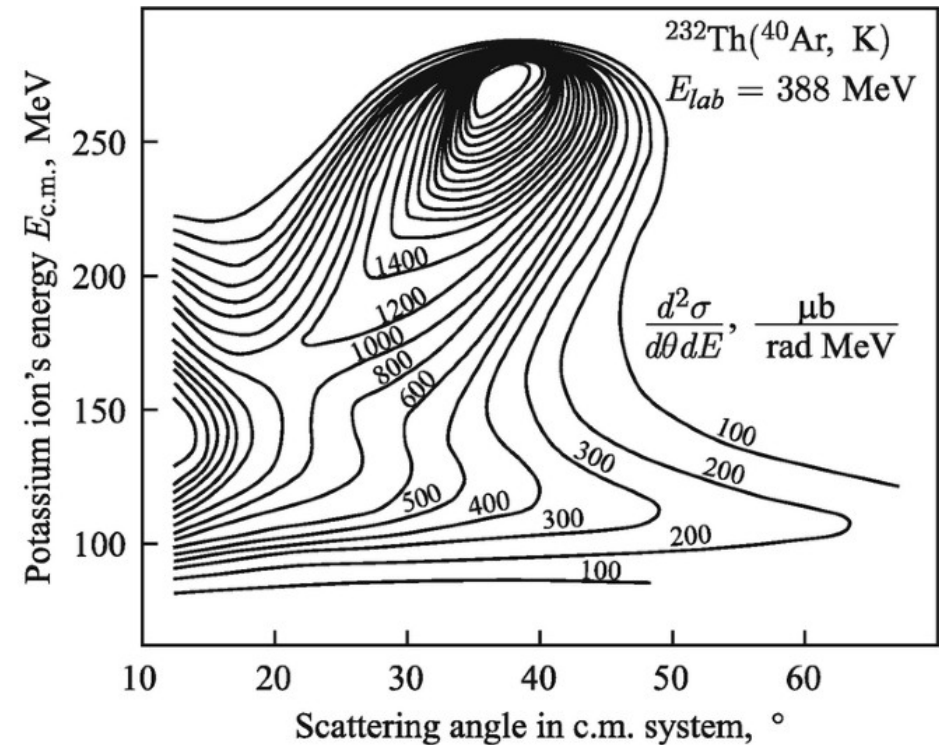
Kinetic energy is associated to the **energy dissipation** via **multi-nucleon transfer (MNT)**

Angle is associated to the **timescale** of the process

Energy is used to estimate **excitation energy**

Angle is used as a **clock** for nuclear timescales

$$100 \text{ fm/c} = 10^{-21} \text{ s (1 zs)}$$



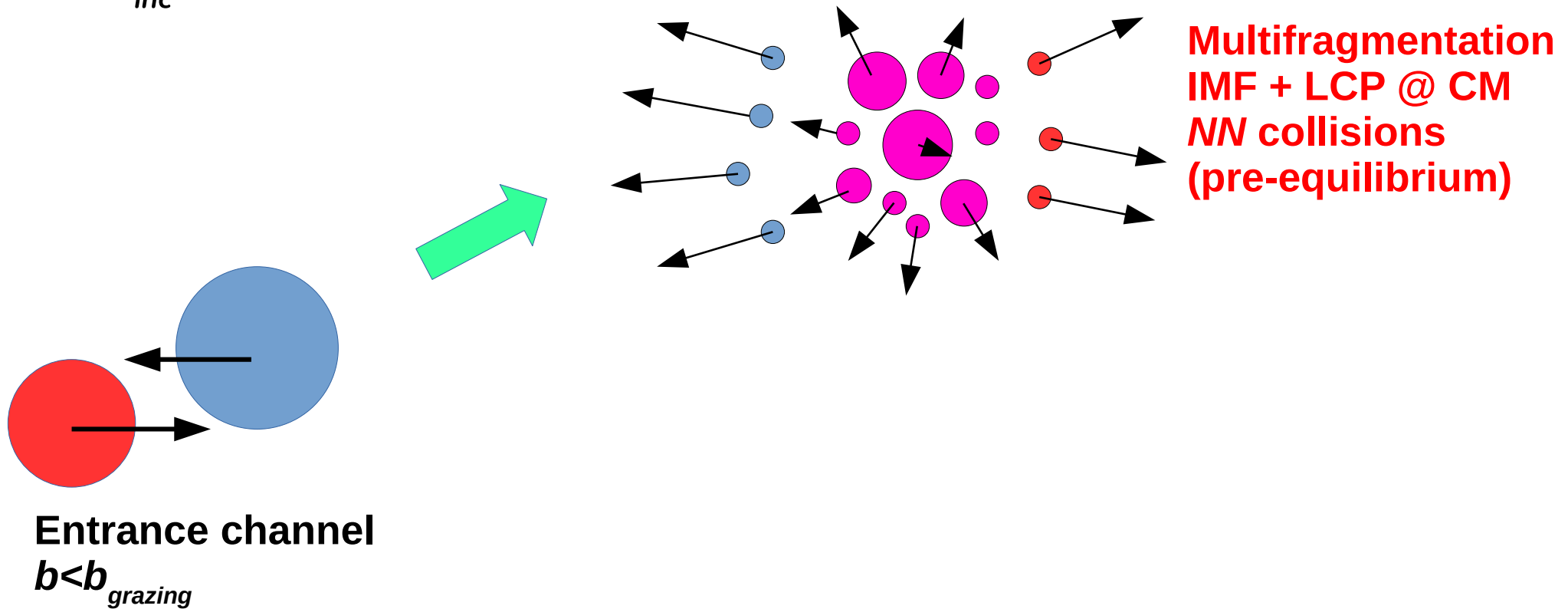
Nuclear reactions

Intermediate incident energy

50 – 100 MeV/nucleon

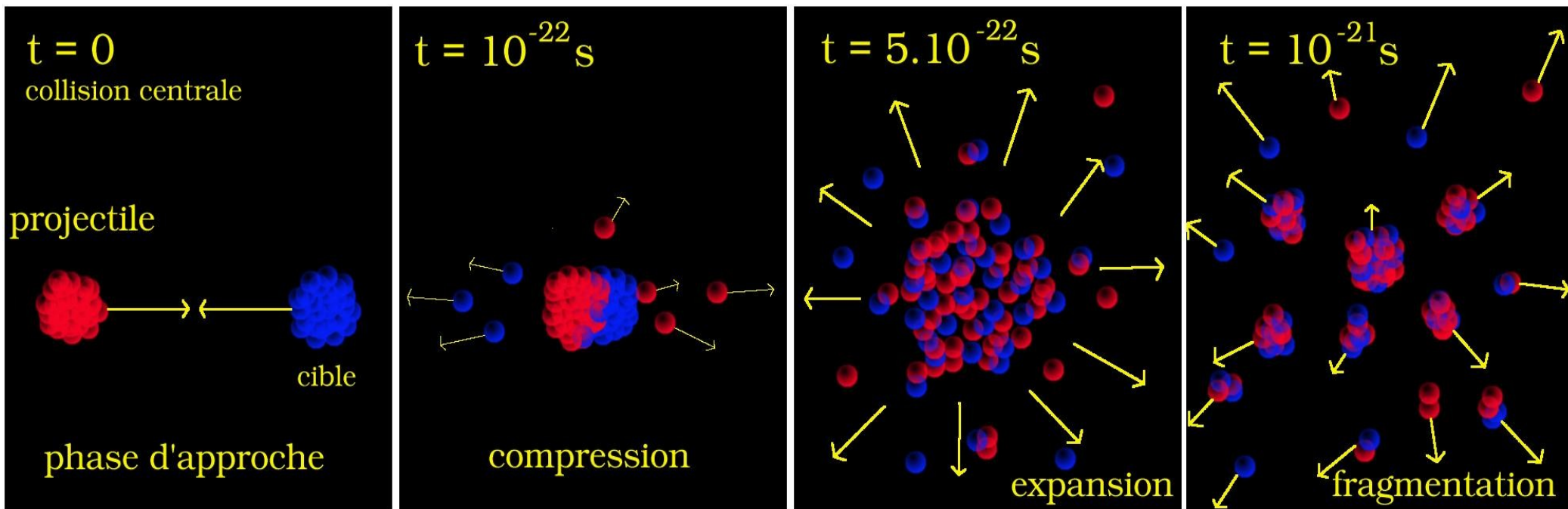
Intermediate energy reaction mechanisms

$50 < E_{inc} < 100 \text{ MeV/nucl.}$



Central collisions ... **Little Big Bang** !

Central collision ($b=0$)

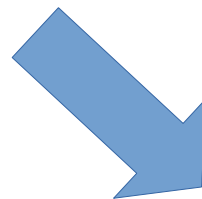
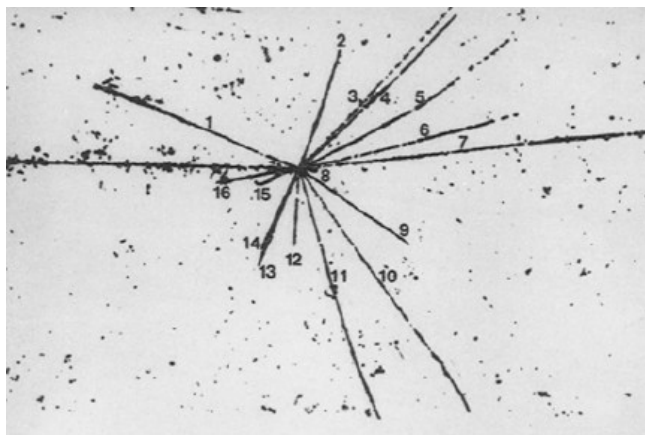


More dense
 $\rho / \rho_0 > 2-3$

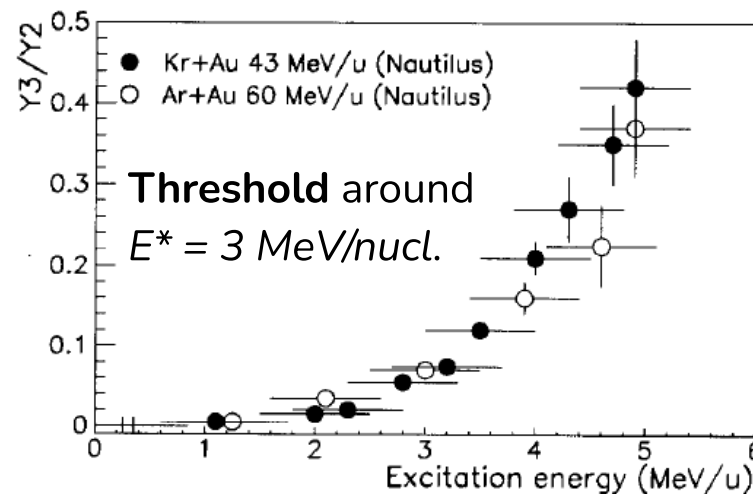
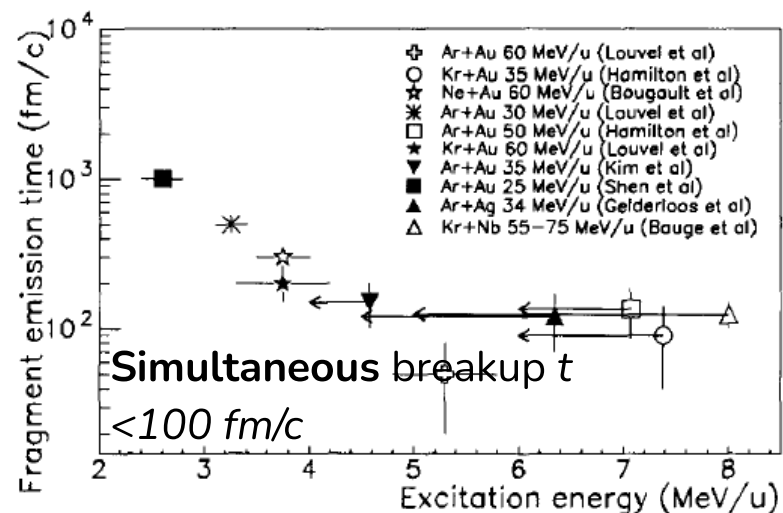
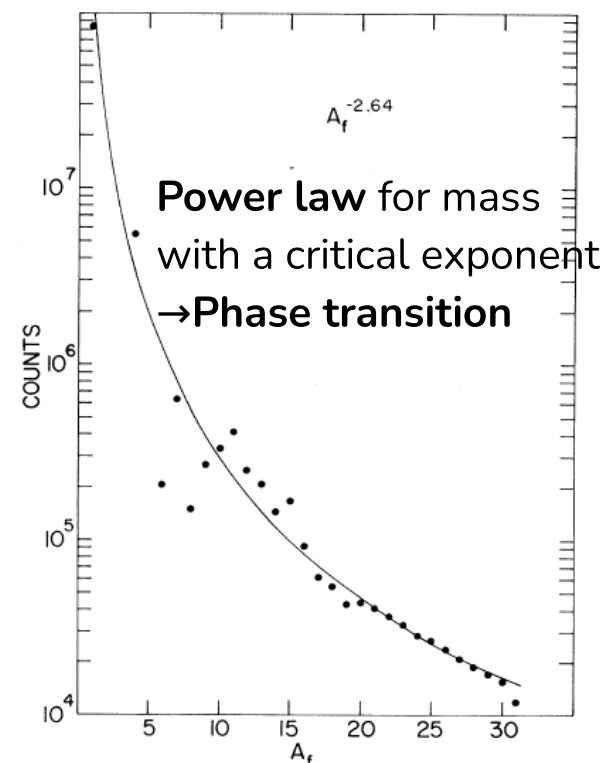
Hotter
 $T > 5 \text{ MeV}$
 $1 \text{ MeV} = 10^{10} \text{ K} !$

Fragmented
and diluted
 $N > 10-100$

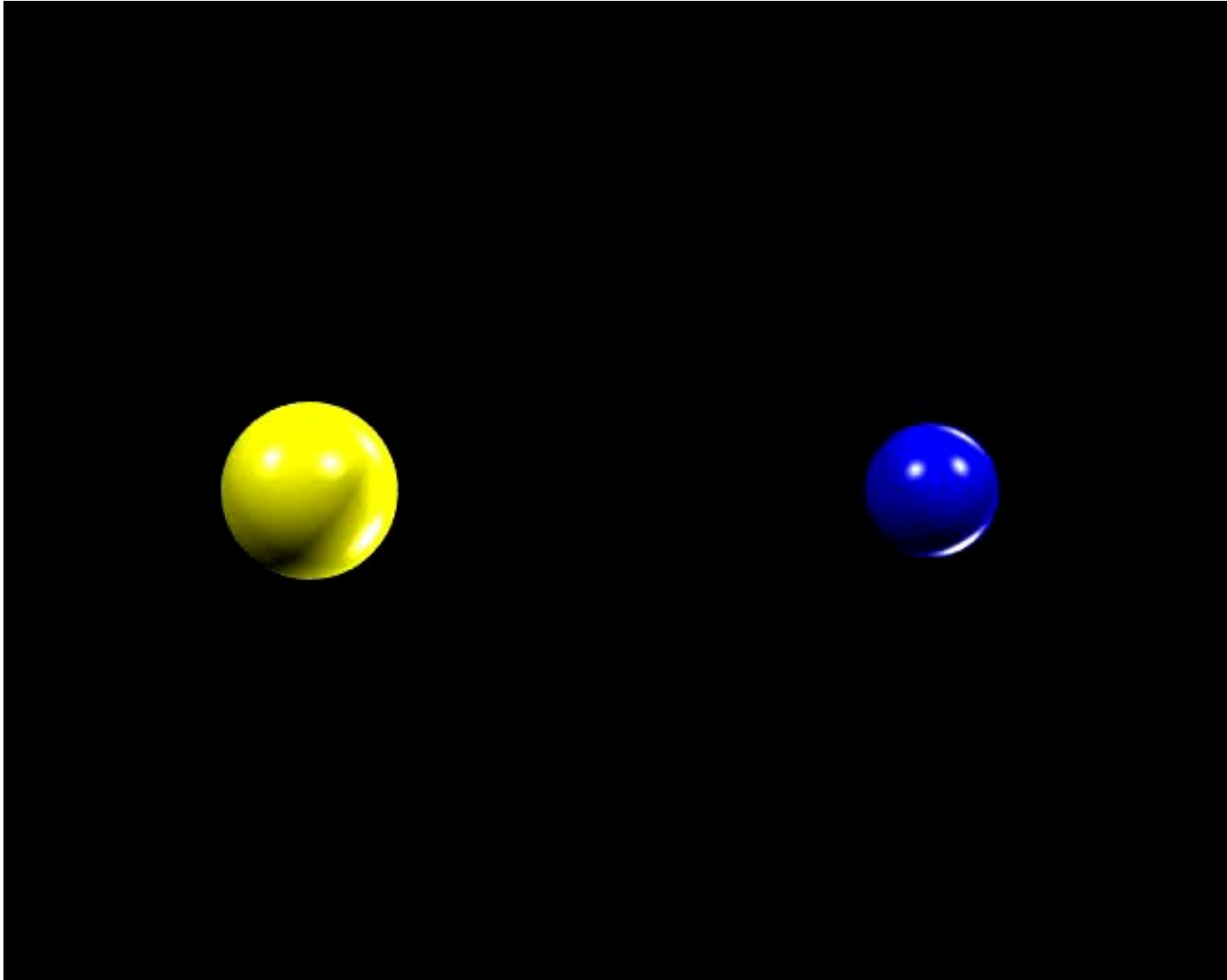
Multifragmentation as Liquid-gas PT



Breakup reactions with
more than 2 fragments...



Multifragmentation



Simulation Xe+Sn at 39 MeV/nucleon b=0 fm

Nuclear Collision Simulation

(Z=54,A=129) on (Z=50,A=119) @ E/A= 39MeV, b=0.0fm

HIPSE model - Phys. Rev. C69, 054604 (2004)
D. Lacroix (GANIL) and D. Durand (LPC Caen)

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Details at <http://www.lpc-caen.in2p3.fr>

Nuclear Collision Simulation

(Z=54,A=129) on (Z=50,A=119) @ E/A= 39MeV, b=0.0fm

HIPSE model - Phys. Rev. C69, 054604 (2004)
D. Lacroix (GANIL) and D. Durand (LPC Caen)

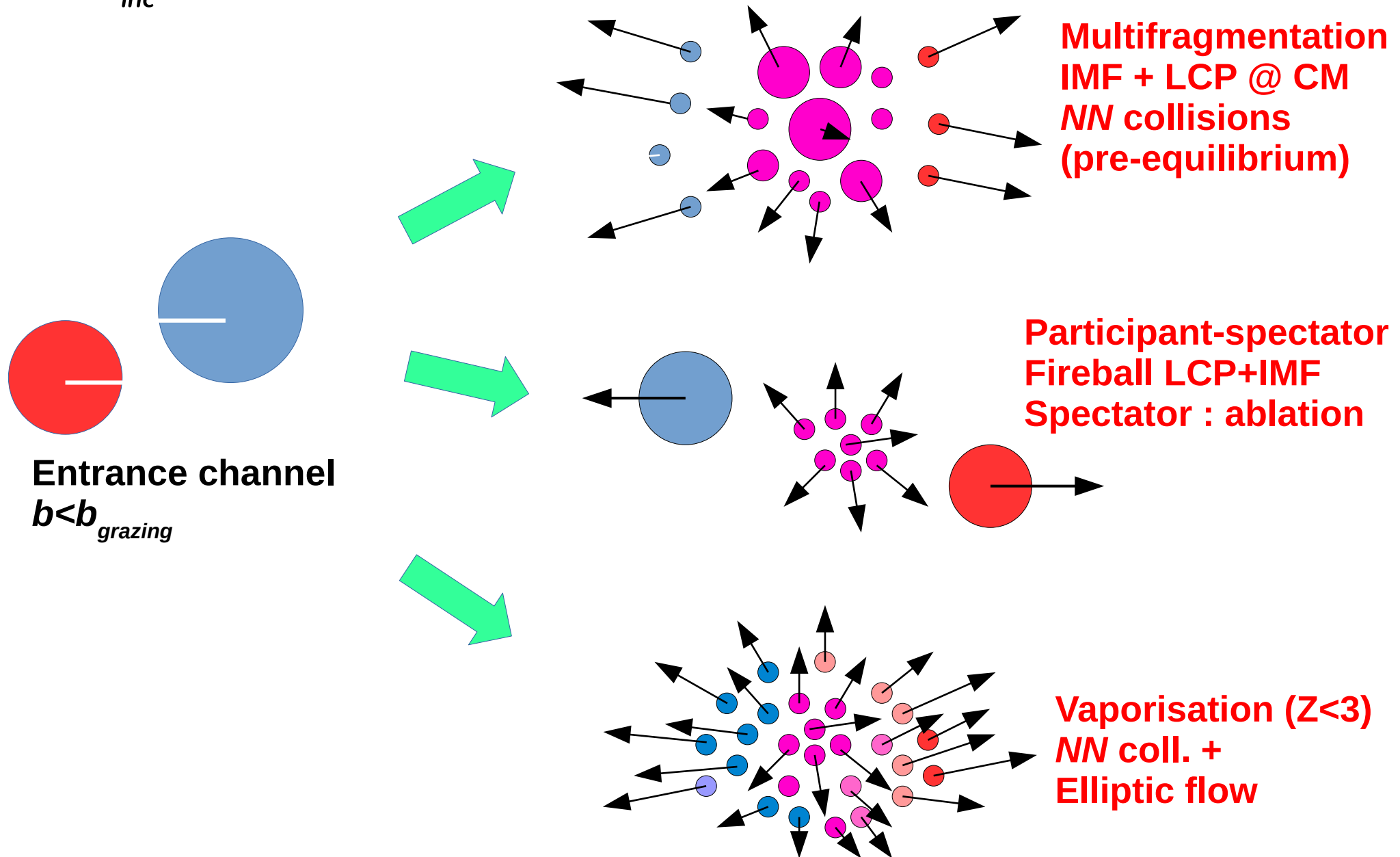
Simulation done by O. Lopez (lopezo@in2p3.fr)
Details at <http://www.lpc-caen.in2p3.fr>

More videos available on this YouTube channel :

<https://www.youtube.com/watch?v=azCjJx6REKg>

Intermediate energy reaction mechanisms

$50 < E_{inc} < 100 \text{ MeV/nucl.}$



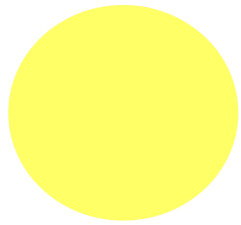
Hot nuclear matter (nuclei) ; from liquid to gas phase

Evaporation

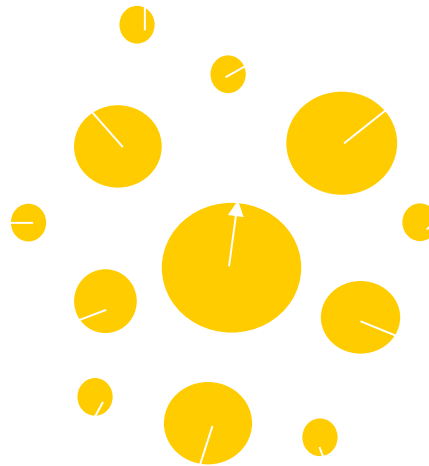
Multifragmentation

Vaporization

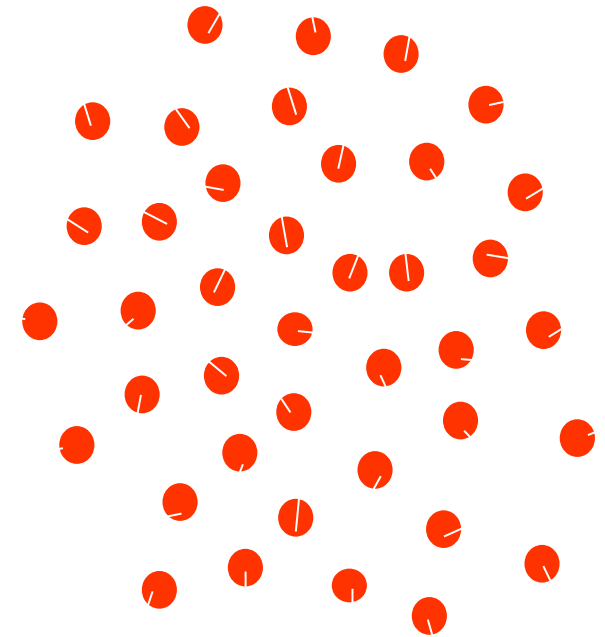
E^*/A (MeV)



$\rho \sim \rho_0$
 $T < 5$ MeV



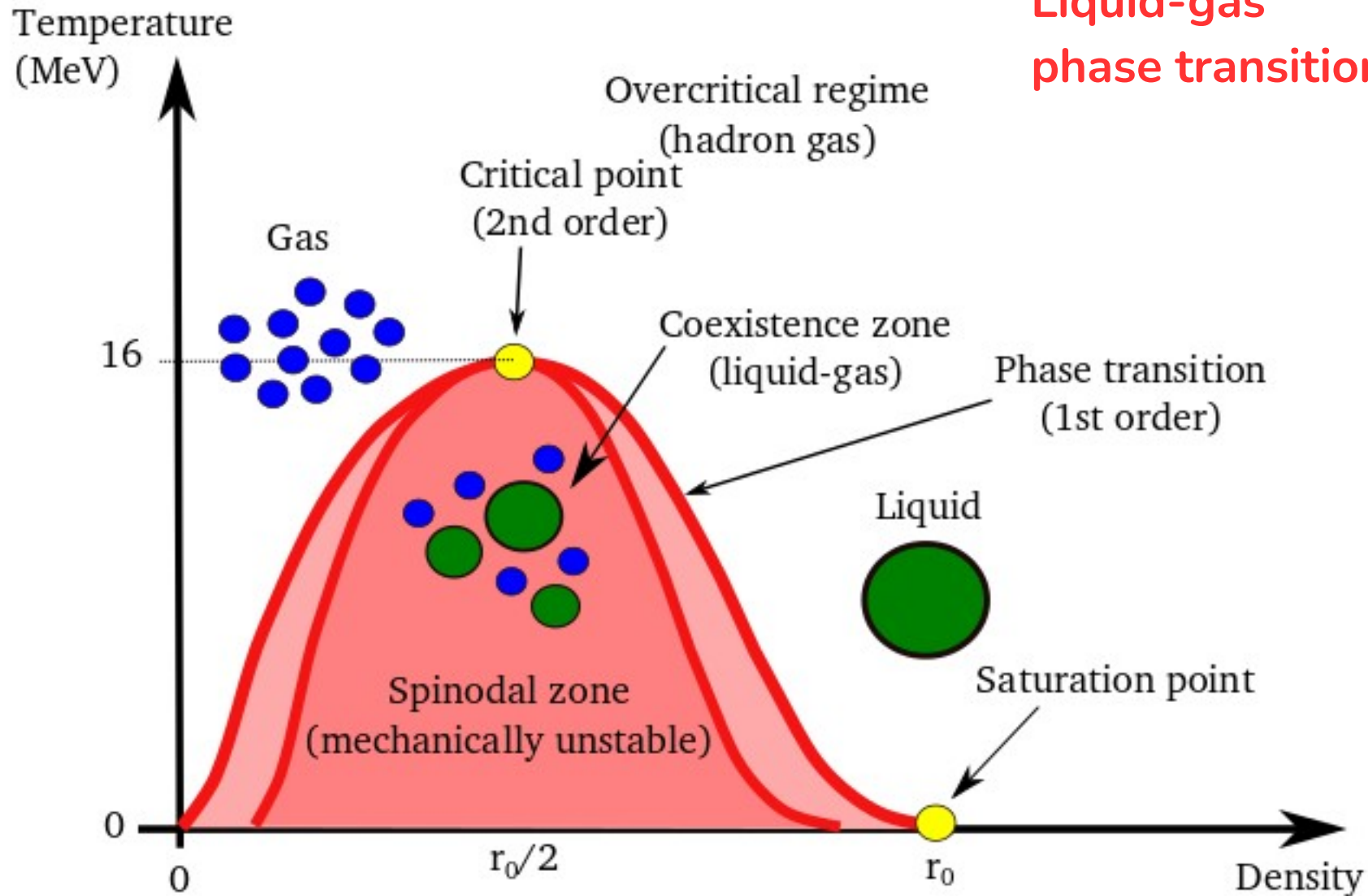
$\rho < \rho_0$
 $T = 5-10$ MeV



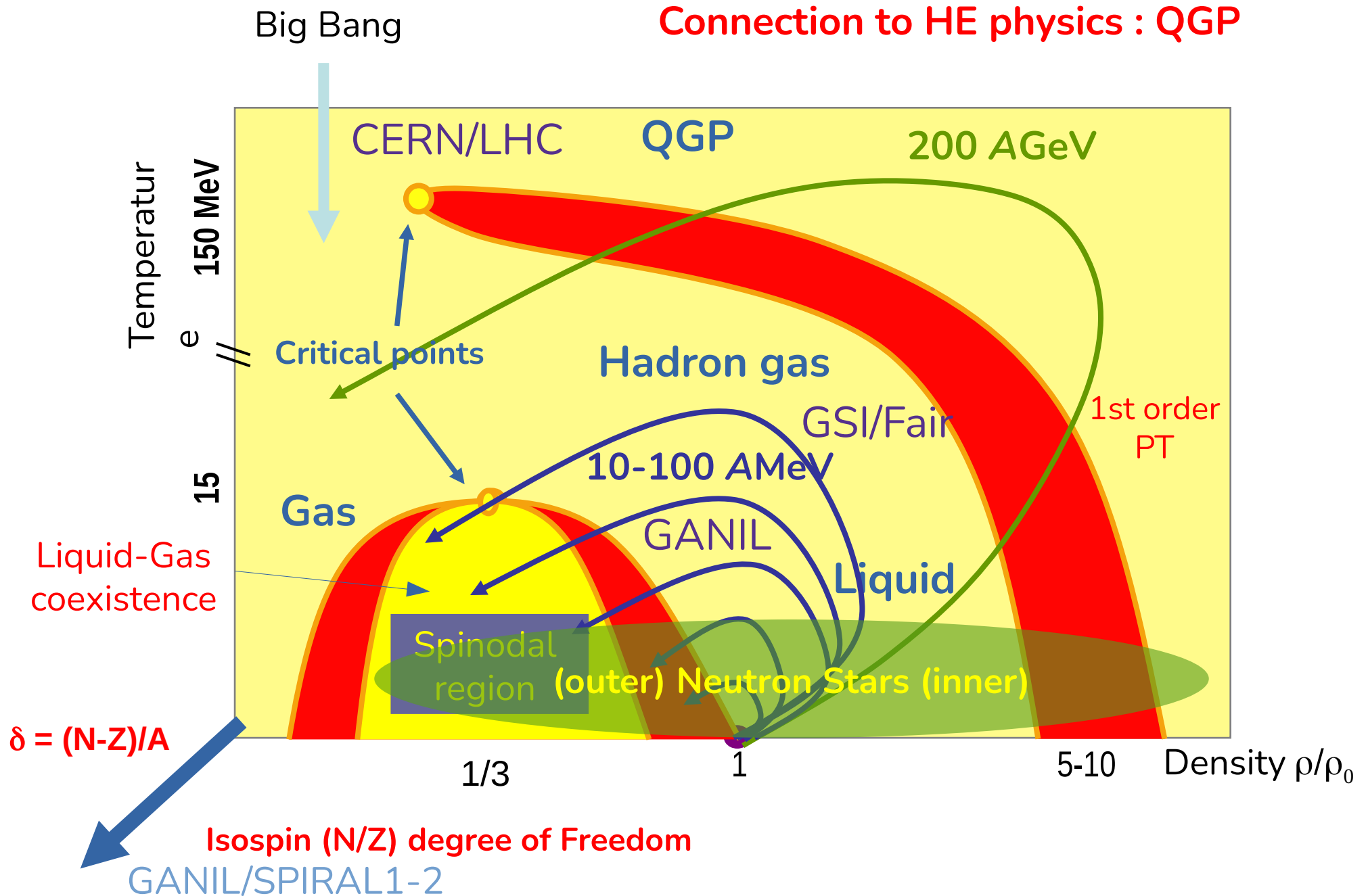
$\rho \ll \rho_0$
 $T > 10$ MeV

Multifragmentation : Mean-Field density instabilities

Liquid-gas
phase transition



Phase diagram of Nuclear Matter



End part II

Part III

Nuclei at extremes

Nuclear Equation of state

Novae & Supernovae



Nova Monocerotis V838, Licorne
May - December 2002
Hubble Telescope (NASA)

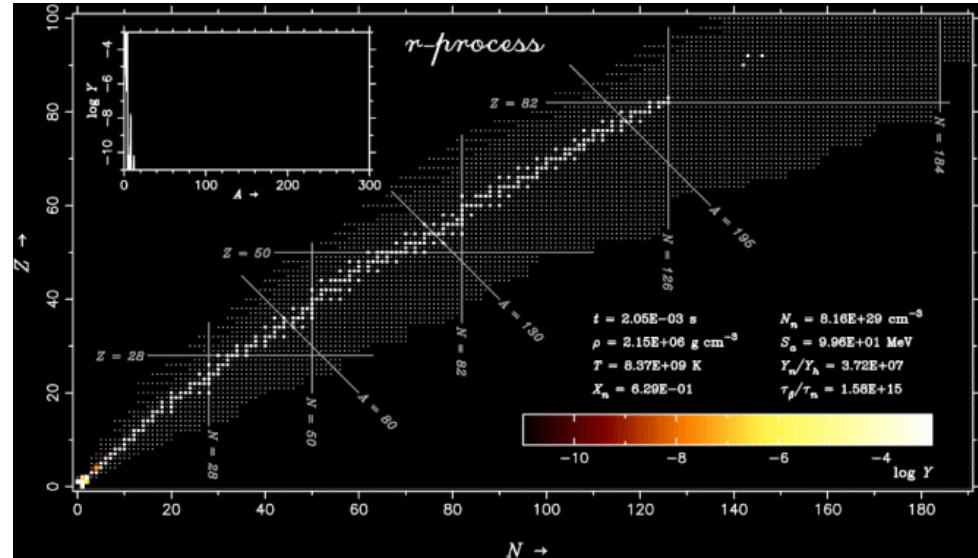
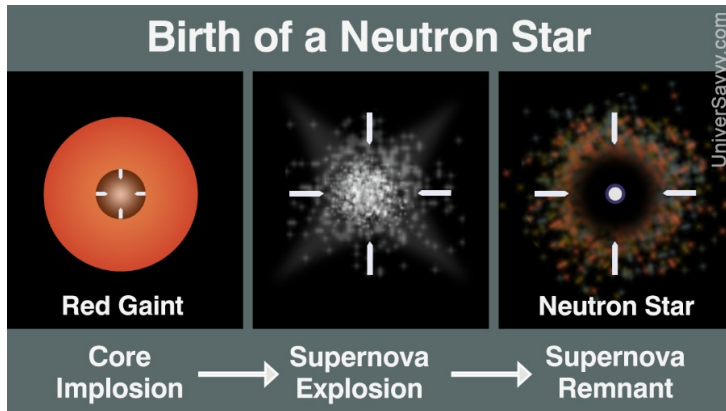
$$E = 10^{38} \text{ J}, L \times 1000 !$$



Crab Nebula (M1) - 1054
Hubble Telescope (NASA)

Nuclear EOS in Astrophysics

Neutron Stars (NS) are unique systems for investigating dense nuclear matter !



B.P. Abbott et al. (LIGO/VIRGO),
PRL **116**, 061102 (2016)
PRL **119**, 161101 (2017)

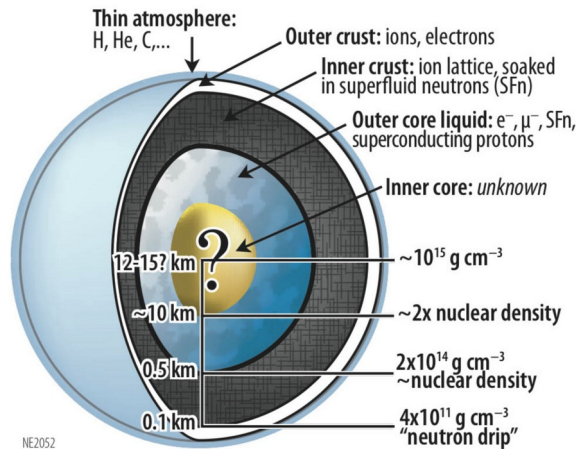
Detection of GW and multi-messenger observables (GW170817) considerably reinforces terrestrial EOS studies

Core Collapses Sne

- EoS (isoscalar/isovector) : **shock waves**
- E_{sym} : **r-process** and **nucleosynthesis**
- Cooling : **d-URCA** and **Neutrinosphere** (low density nuclear matter)

NS structure :

- Crust : **pasta phases** (frustration/clusters)
- Crust/Core transition: L, K_{sym}
- Core : **hyperons** (strange matter, QCD)



N. Yunes, M. Coleman Miller, and K. Yagi,
Nature Review Physics **4**, 237 (2022)

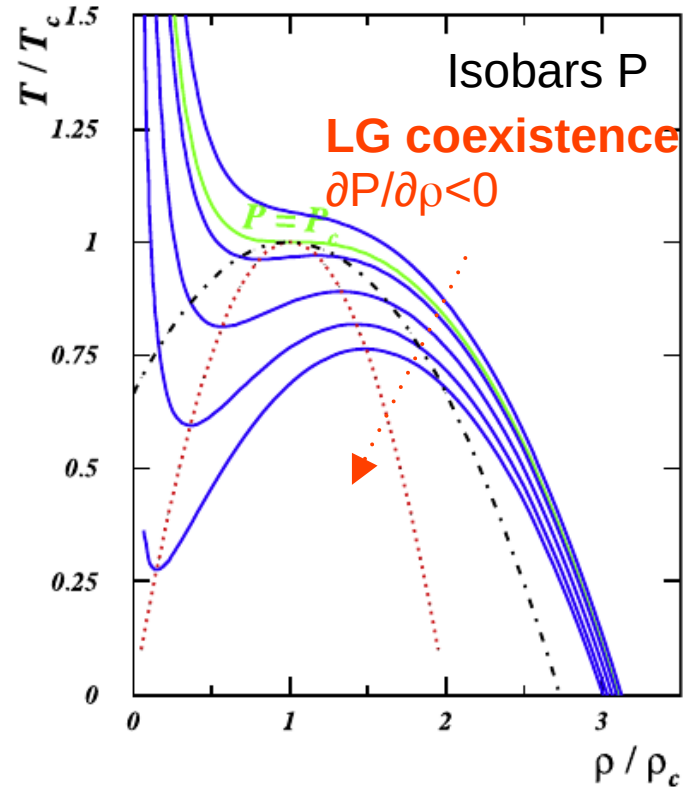
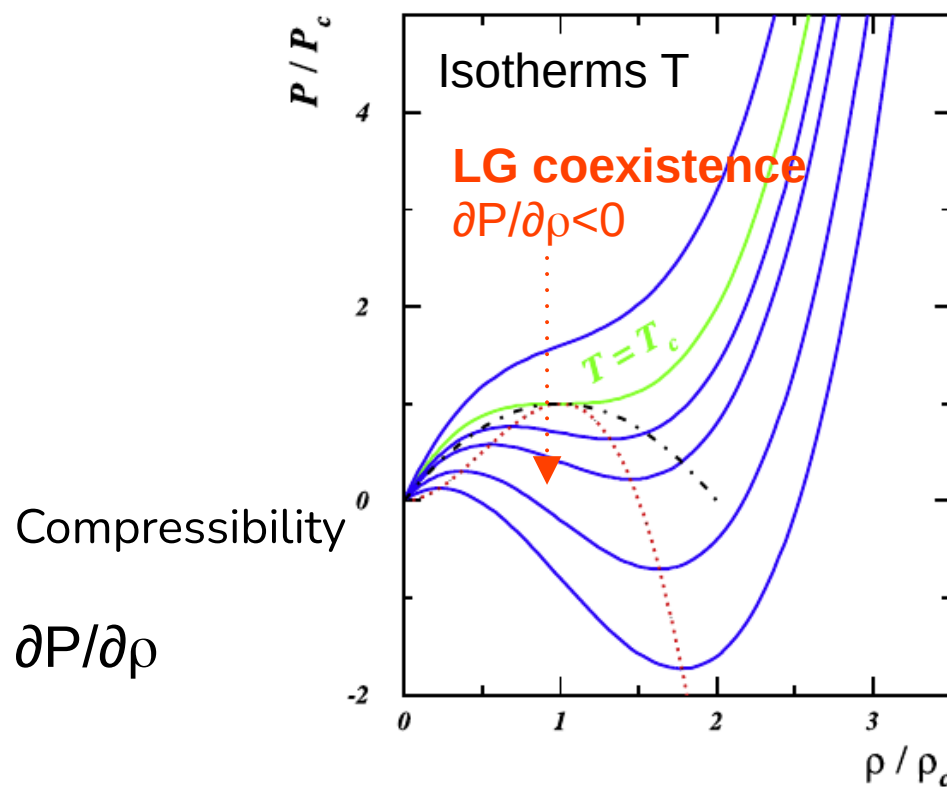
NS- NS merger (Kilonova)



Equation of State of nuclear matter

$$E \text{ (or } P) = f(\rho, T, \delta)$$

Thermodynamical relation between state variables



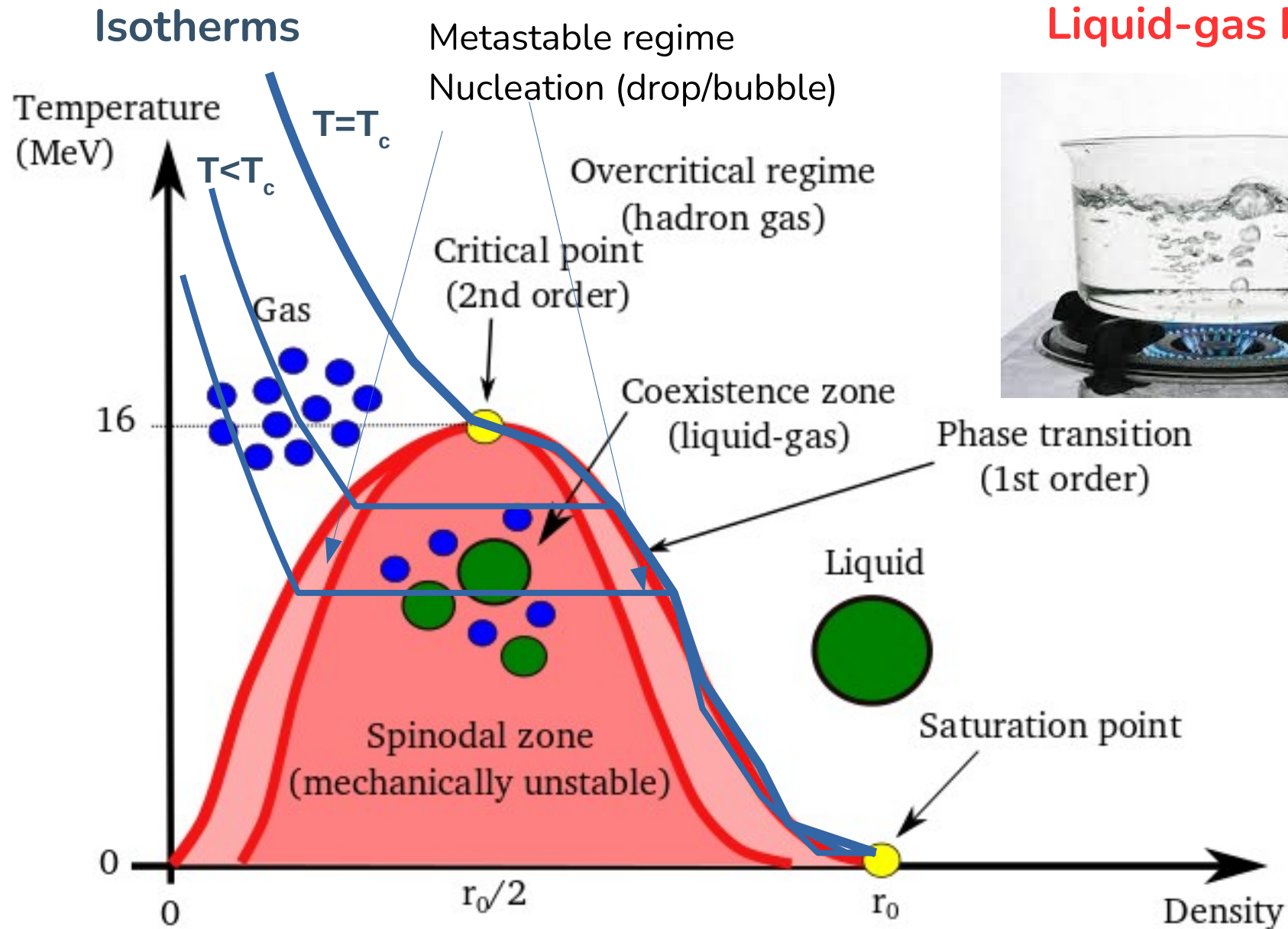
Skyrme HF
at finite T

B. Borderie,
J. Phys. G:
Nucl. Part.
Phys. 28 (2002)
R217

Pressure : $P(\rho) = \rho^2 \left(\partial E / \partial \rho \right)_\rho$

P_c, T_c, r_c : critical point of the liquid-gas phase transition with $T_c = 16-18 \text{ MeV}$, $\rho_c = 0.3-0.5 \rho_{\text{sat}}$

Spinodal decomposition : Mean-Field instabilities



Liquid-gas PT



$$E = f(\rho, T, \delta)$$

$$\delta = (N-Z)/A$$

Astrophysical context (NS)

Nuclear matter :
Bulk properties

Extensive systems
(volume, size)

Pure **neutron matter** ($\delta=1$)

Terrestrial Labs

Nuclei :
Finite-size effects

Non-extensive systems
(surface, Coulomb)

Asymmetric NM
($|\delta| \sim 0-0.4$, E_{sym})

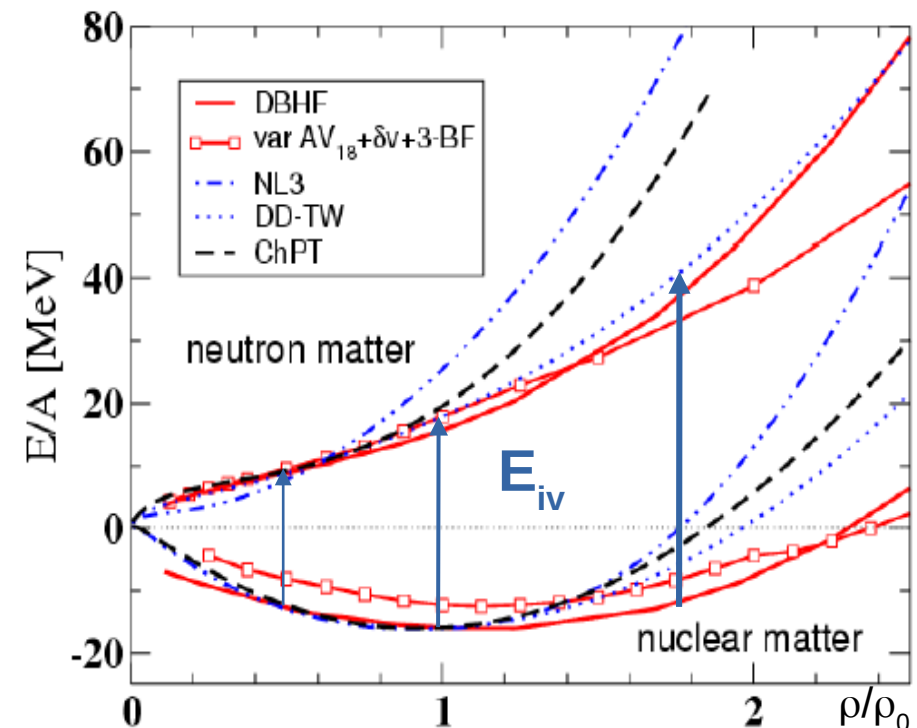
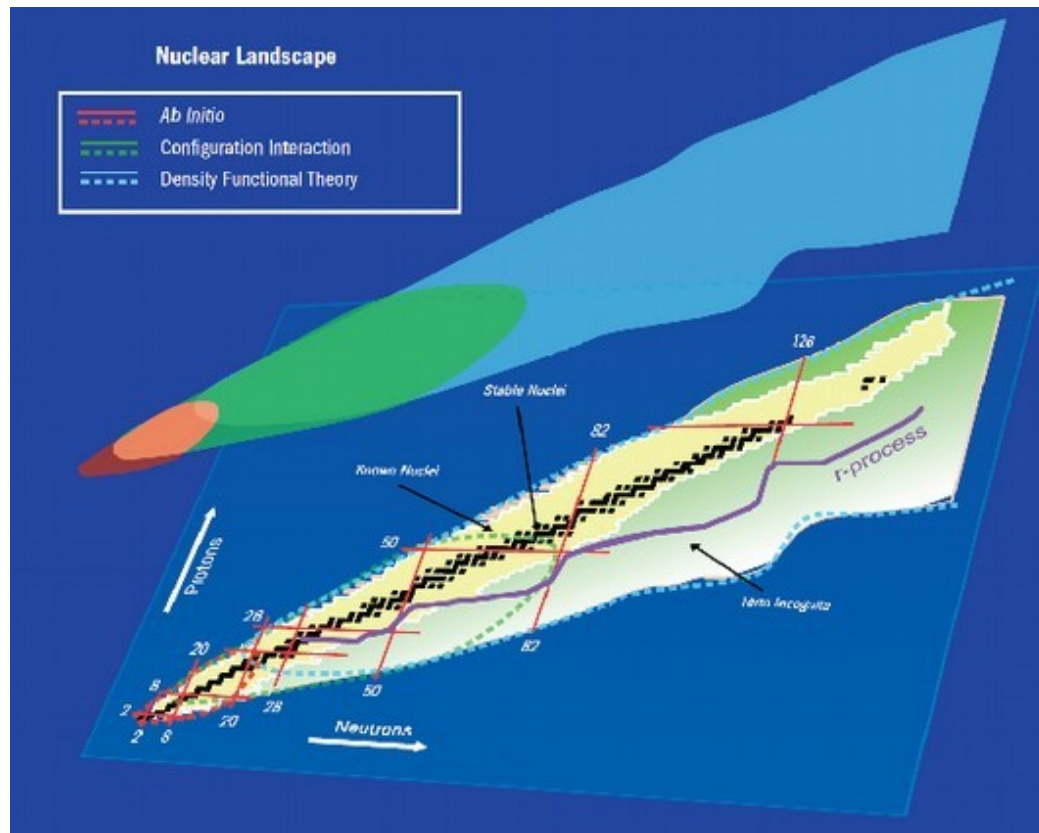
Phase Diagram and Phase Transitions in finite systems

EoS in Nuclear Physics

Energy-density functionals modelization is probably the best possible framework to understand the structure of medium and heavy nuclei.

Energy-Density Functionals

(Hohenberg-Kohn theorem) : $H_{\text{eff}} = E[\rho]$



Direct link to EOS and Symmetry Energy (isovector term)

$$E_{iv} \text{ (aka } S) = E(\rho, \delta=1) - E(\rho, \delta=0)$$

EOS density and isospin dependence

Energy per nucleon in the parabolic (2nd order) approximation is the sum of isoscalar (ρ) and isovector (δ) terms:

$$\text{Isospin ratio : } \delta = (N-Z)/A$$

$$\rho_{\text{sat}} \approx 0.17 \text{ fm}^{-3}$$

$$E(\rho, \delta) = E_0(\rho) + S(\rho) \cdot \delta^2 + O(\delta^4)$$

Each term (isoscalar and isovector) can be decomposed in **Taylor expansion** (up to the fourth order) in $\chi = (\rho - \rho_0)/3\rho_0$:

$$E_0(\rho) = E_{\text{sat}}(\rho_0) + 1/2 K_0 \chi^2 + 1/3 ! Q_0 \chi^3 + 1/4 ! Z_0 \chi^4 + O(\chi^5)$$

$$S(\rho) = J + L\chi + 1/2 K_{\text{sym}} \chi^2 + 1/3 ! Q_{\text{sym}} \chi^3 + 1/4 ! Z_{\text{sym}} \chi^4 + O(\chi^5)$$

E_{sat} is the **saturation energy** at $\rho = \rho_0$

K_0 is the **compressibility** (curvature) around ρ_0

Q_0 and Z_0 are the **cubic** and **quartic** terms needed for ρ far from ρ_0

J is the **symmetry energy** at $\rho = \rho_0$

L_{sym} is the **slope** (conn. to P) of the symmetry energy around ρ_0

K_{sym} is the **curvature** of the symmetry energy

Q_{sym} and Z_{sym} are the **cubic** and **quartic** terms needed for ρ far from ρ_0

$$E/A(\rho, \delta) = E/A(\rho, 0) + \delta^2 \cdot S(\rho)$$

$$\delta = (\rho_n - \rho_p) / (\rho_n + \rho_p) = (N - Z) / A$$

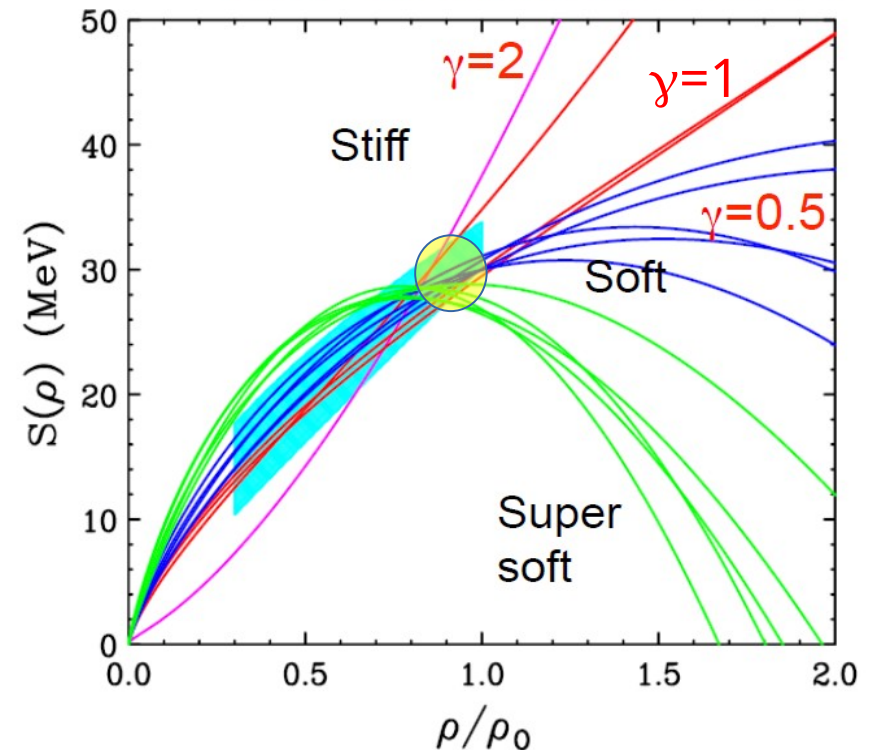
- Constraints for **Astrophysics** (NS) and for laboratory experiments
- Needed for **transport models** and nuclear matter studies (Thermodyn.)
- Link to the **NN interaction** (isovector) in the nuclear medium

Density dependence of SE

Poorly constrained ...

Need experimental data !

M.B. Tsang, Prog. Part.Nucl.Phys. 66, 400 (2011)
Brown, Phys. Rev. Lett. 85, 5296 (2001)

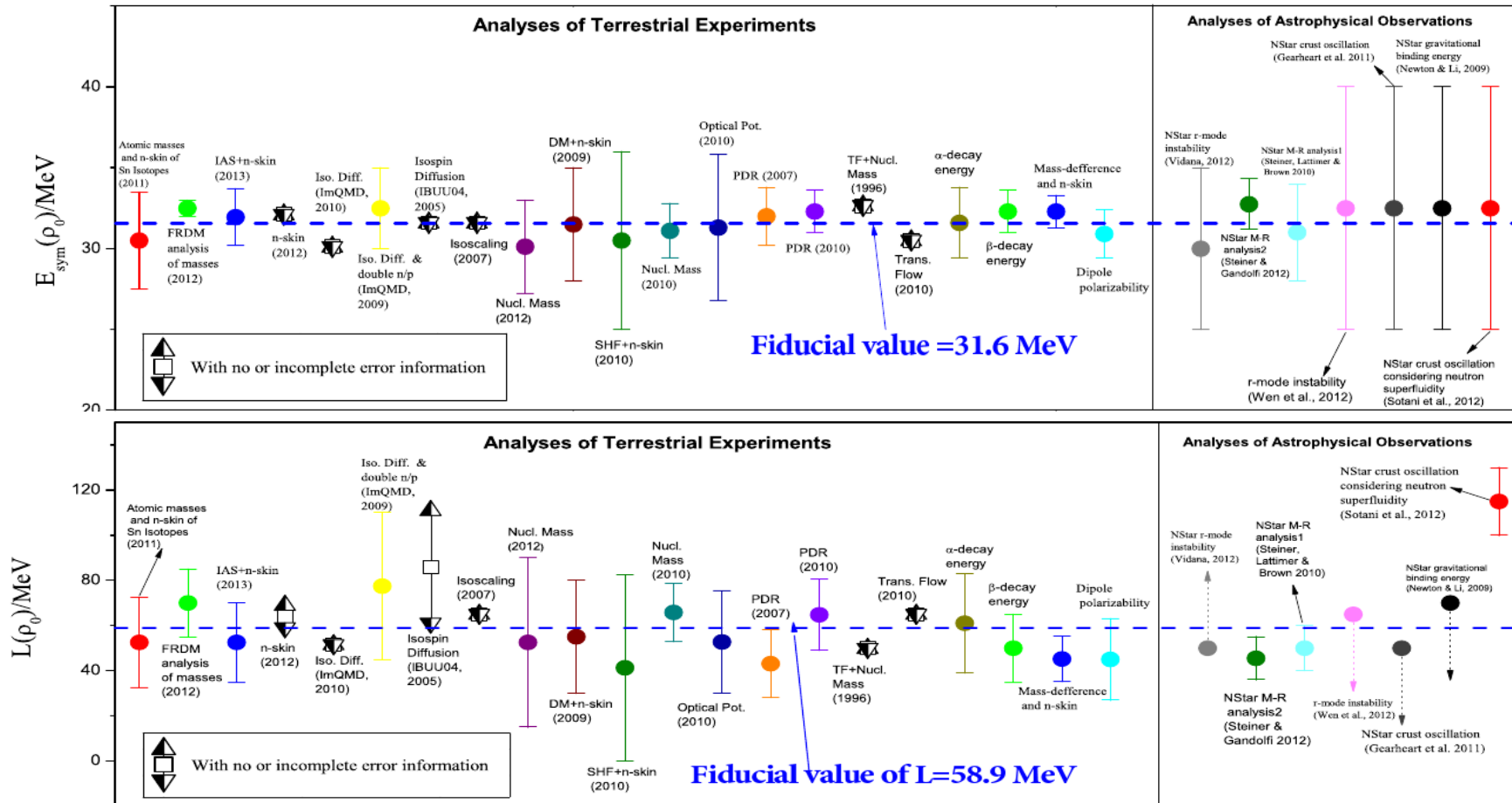


$$S(\rho) = \underbrace{S_k(\rho/\rho_0)^{2/3}}_{\text{Kinetic (FG)}} + \underbrace{S_i(\rho/\rho_0)^\gamma}_{\text{Potential (int.)}}$$

Symmetry Energy around $\rho_0(l)$

Evaluations for E_{sym} , slope L , curvature K_{sym} , ...

B.A. Li and X. Han, Phys. Lett. B727 (2018) 276

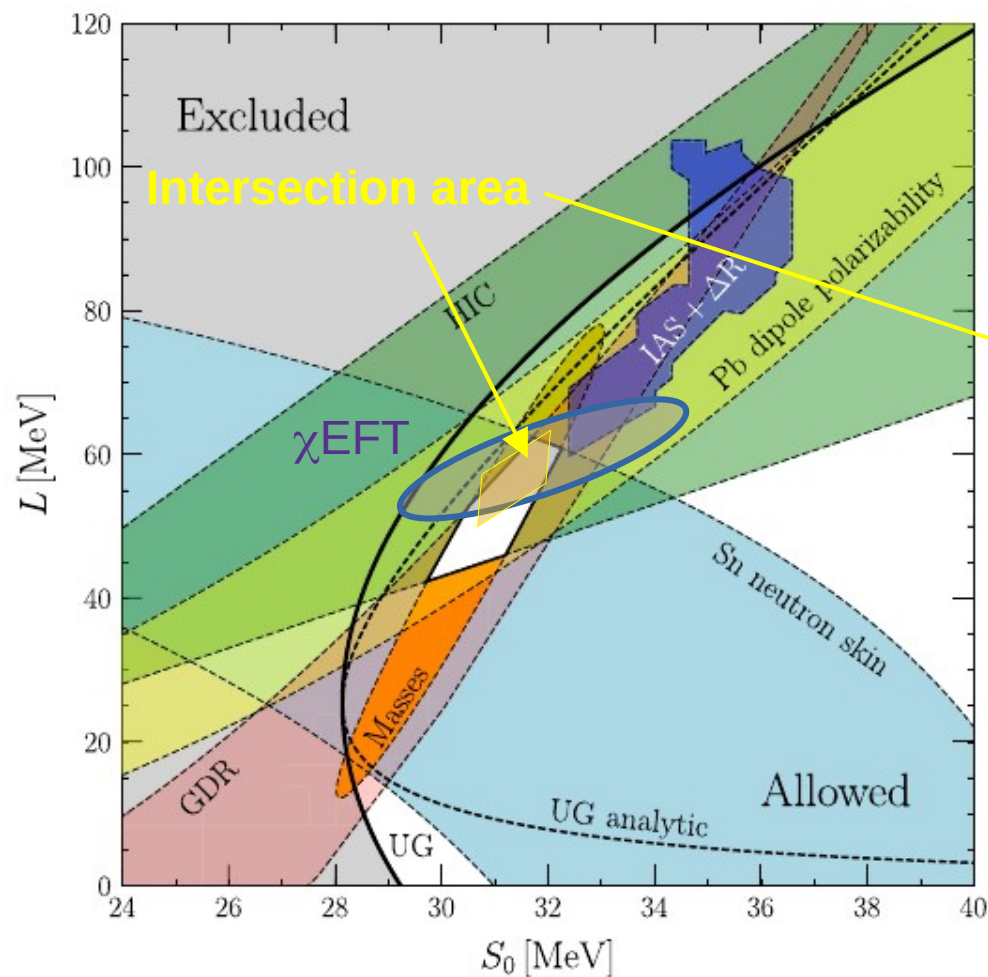


	~1%	~10%		~30%		???				
P_α	E_{sat} MeV	E_{sym} MeV	ρ_0 fm^{-3}	L_{sym} MeV	K_{sat} MeV	K_{sym} MeV	Q_{sat} MeV	Q_{sym} MeV	Z_{sat} MeV	Z_{sym} MeV
$\langle P_\alpha \rangle$	-15.8	32	0.155	60	230	-100	300	0	-500	-500
σ_{P_α}	± 0.3	± 2	± 0.005	± 15	± 20	± 100	± 400	± 400	± 1000	± 1000

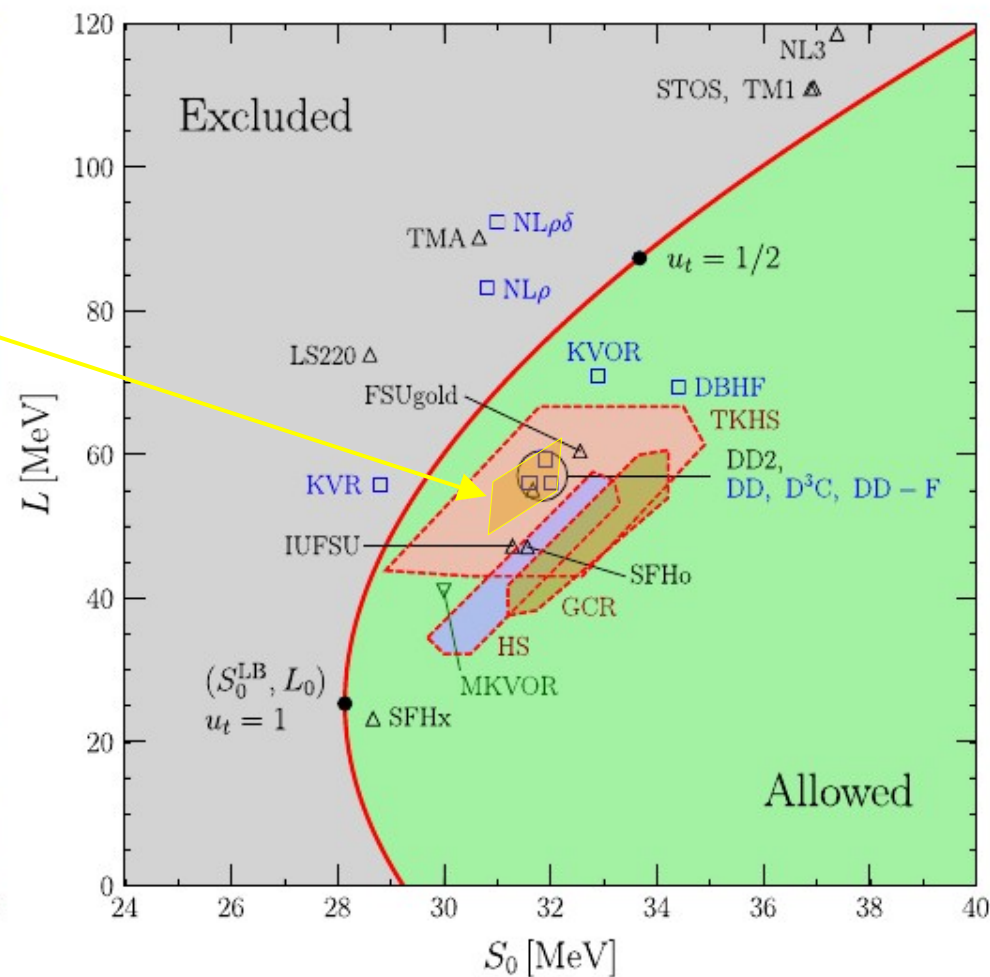
J. margueron et al., PRC 97, 025805 (2020)

Symmetry Energy around ρ_0

Experimental constraints



Model predictions

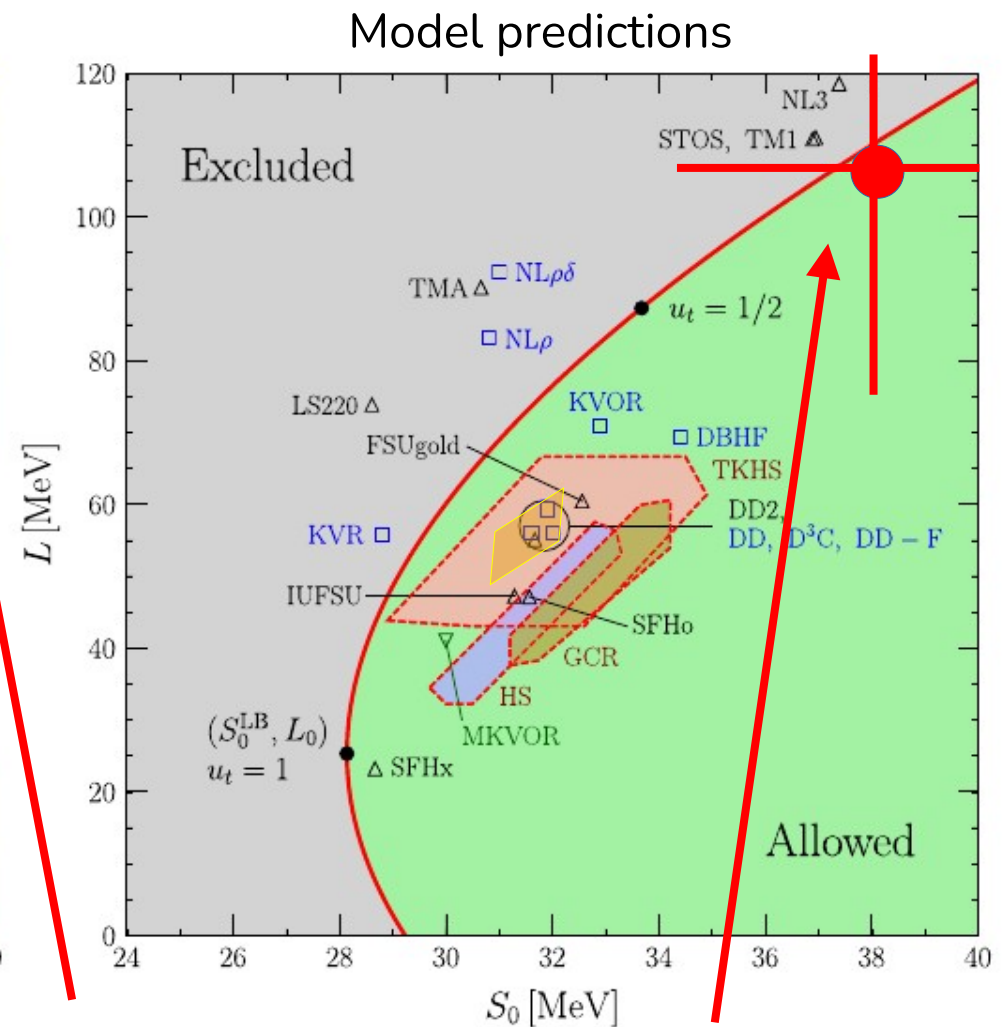
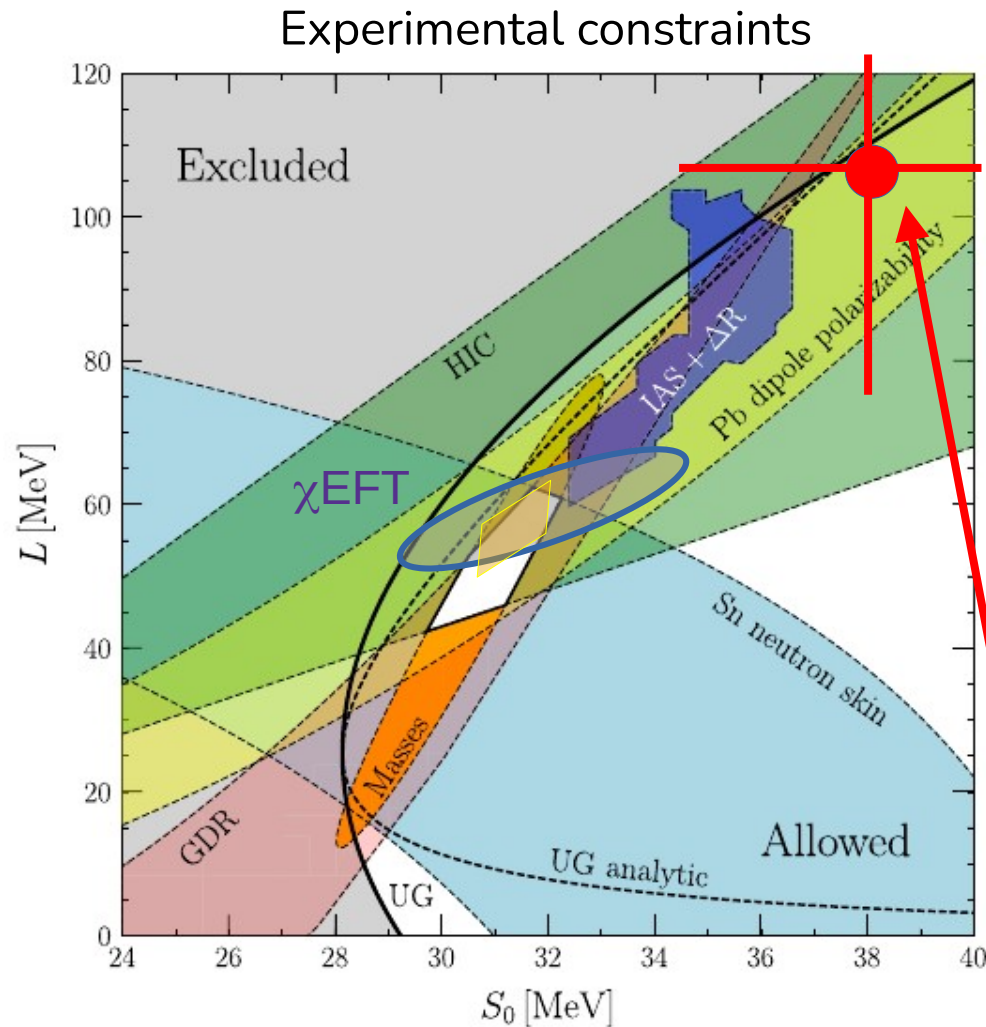


I. Tews et al., *Astroph. J.* **848** (2017) 105

C. Drischler et al., *PRL* **125** (2020) 202702

Symmetry Energy around ρ_0 : newcomer in 2021

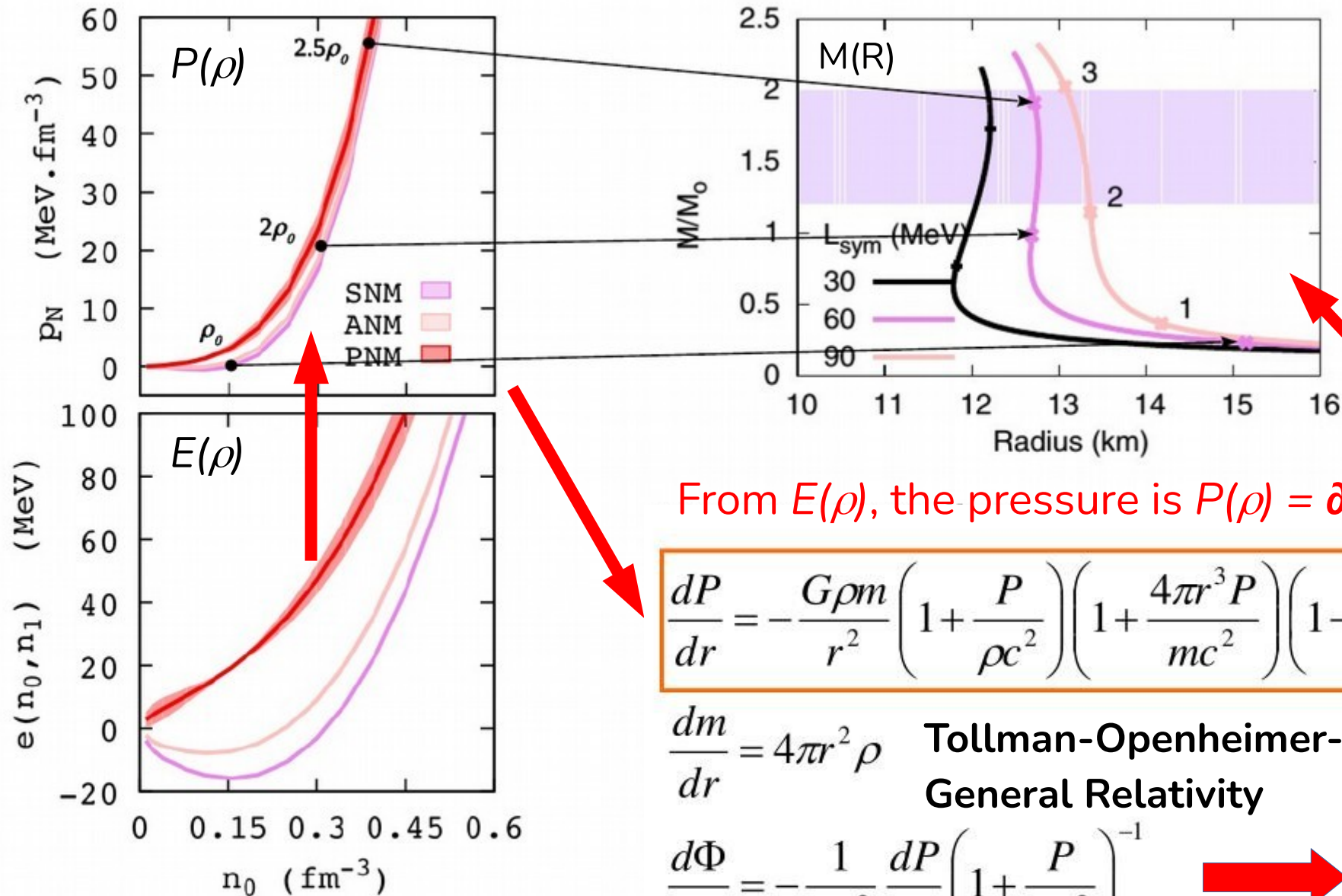
Tension between PREX-2 and other experimental / theoretical evaluations



I. Tews et al., *Astroph. J.* **848** (2017) 105
C. Drischler et al., *PRL* **125** (2020) 202702

PREX-2, B. T. Reed et al., *PRL* **126** (2021) 172503
 $S_0 = 38.1 \pm 4.7$ MeV
 $L_{\text{sym}} = 106 \pm 37$ MeV

Constraints on Neutron Stars : link with nuclear EOS



$$\frac{dP}{dr} = -\frac{G\rho m}{r^2} \left(1 + \frac{P}{\rho c^2}\right) \left(1 + \frac{4\pi r^3 P}{mc^2}\right) \left(1 - \frac{2Gm}{rc^2}\right)^{-1}$$

$$\frac{dm}{dr} = 4\pi r^2 \rho$$

**Tollman-Openheimer-Volkov Eqs.
General Relativity**

$$\frac{d\Phi}{dr} = -\frac{1}{\rho c^2} \frac{dP}{dr} \left(1 + \frac{P}{\rho c^2}\right)^{-1}$$

→ M(R)

$$P = P(\rho)$$

Margueron PRC **97** (2018) 025805
Margueron PRC **97** (2018) 025806

Part IV

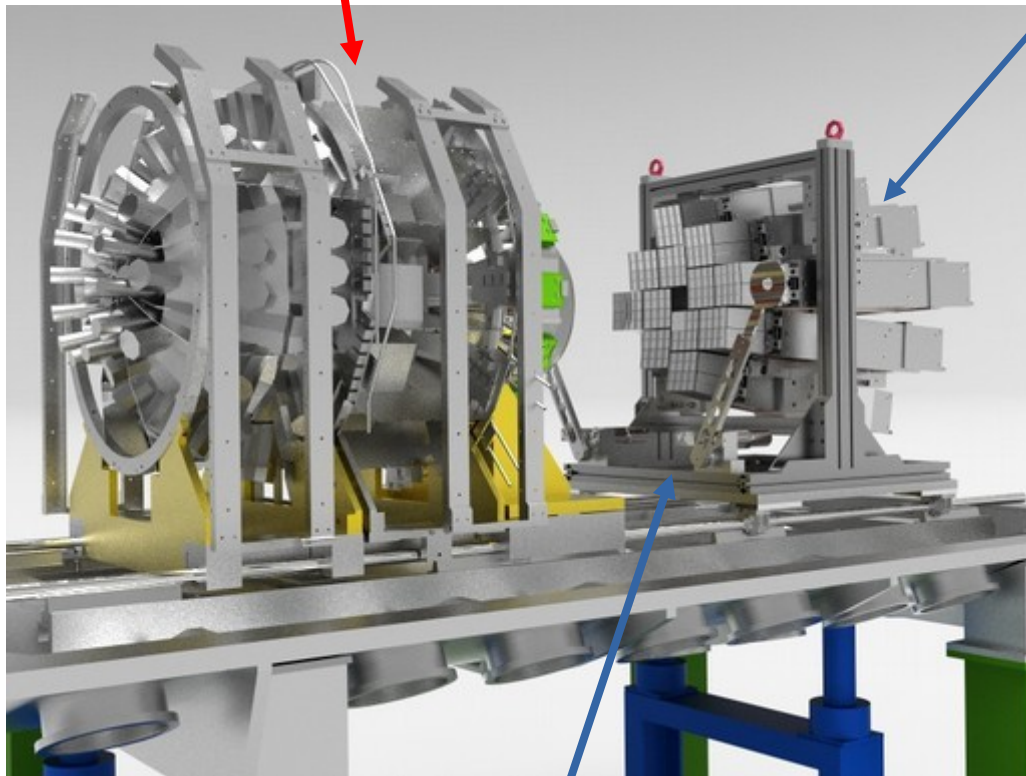
Some experimental tools and instrumentation

Coupling FAZIA demonstrator with INDRA@GANIL

$^{58/64}\text{Ni} + ^{58/64}\text{Ni}$ @ 32 and 52 MeV/nucl : E789 performed in 2019

INDRA in D5

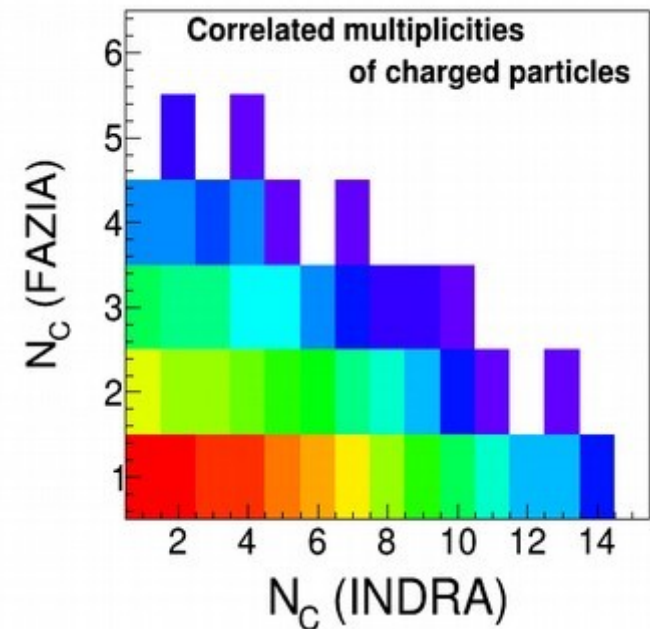
- 240 detection modules (rings 1,2/3,4/5 removed)
- 96 Si-CsI from 16 to 45 deg.
- 144 CsI from 45 to 176 deg.



FAZIA demonstrator: 12 blocks of 16 telescopes
192 High-Quality Si-Si-CsI telescopes
from 2 to 14 deg. + dedicated Full Digital Electronics

FAZIA geom. acceptance 82% (90%)
Granularity x2 as compared to INDRA

Beam Tests in June-July 2018

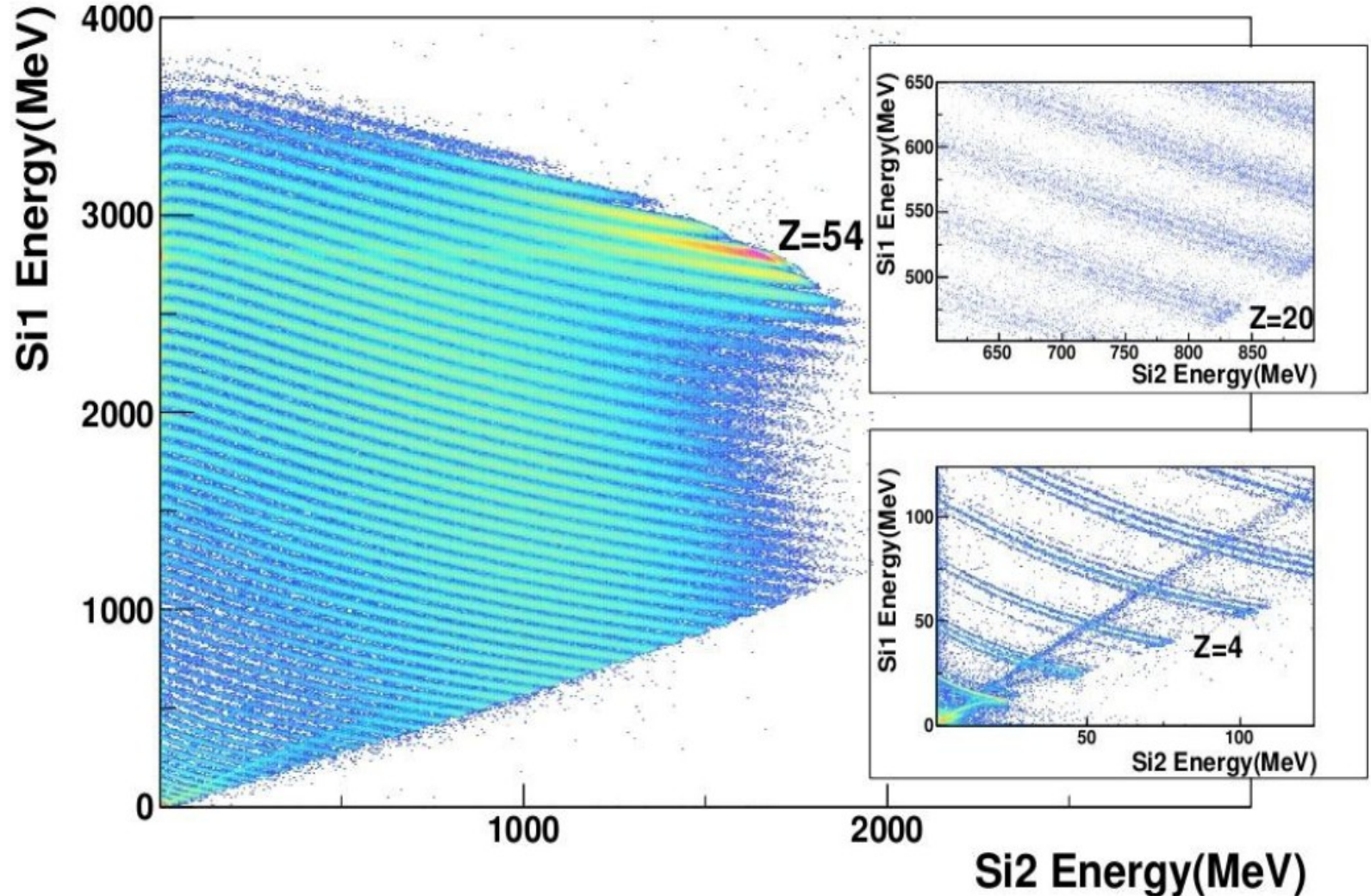
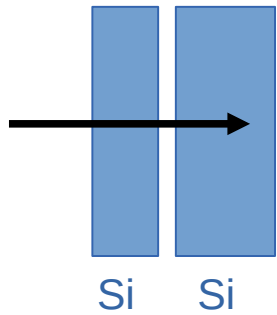


Experiment E789 performed at GANIL
in April-May 2019 :

$^{58/64}\text{Ni} + ^{58/64}\text{Ni}$ @ 32,52 MeV/nucleon

FAZIA : E-E identification

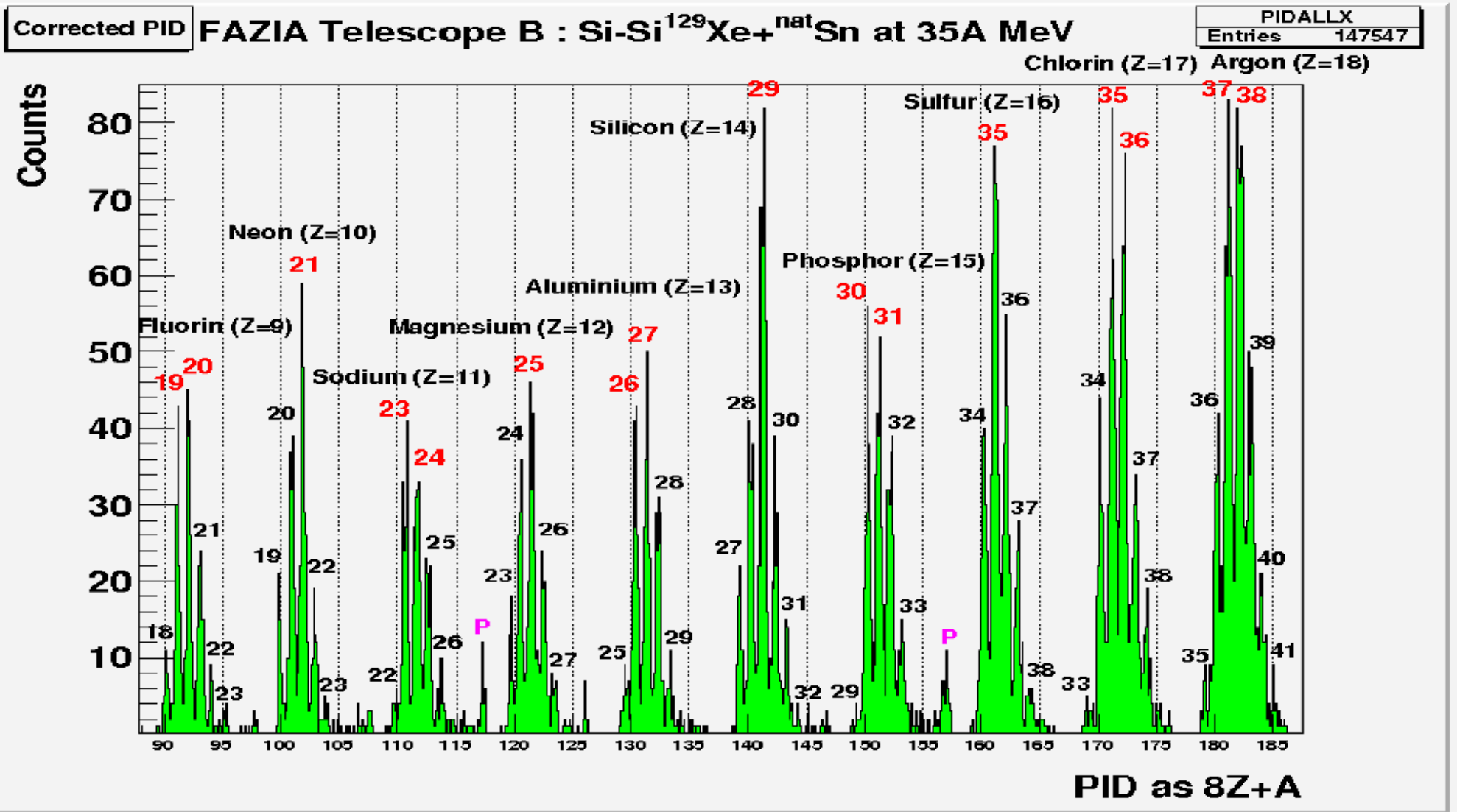
Some results at the end of phase 1: $\Delta E(\text{Si1}) - E(\text{Si2})$



S. Carboni et al., NIMA 664 (2012) 251 *Energy = max of shaped signal (trapezoidal filter)*

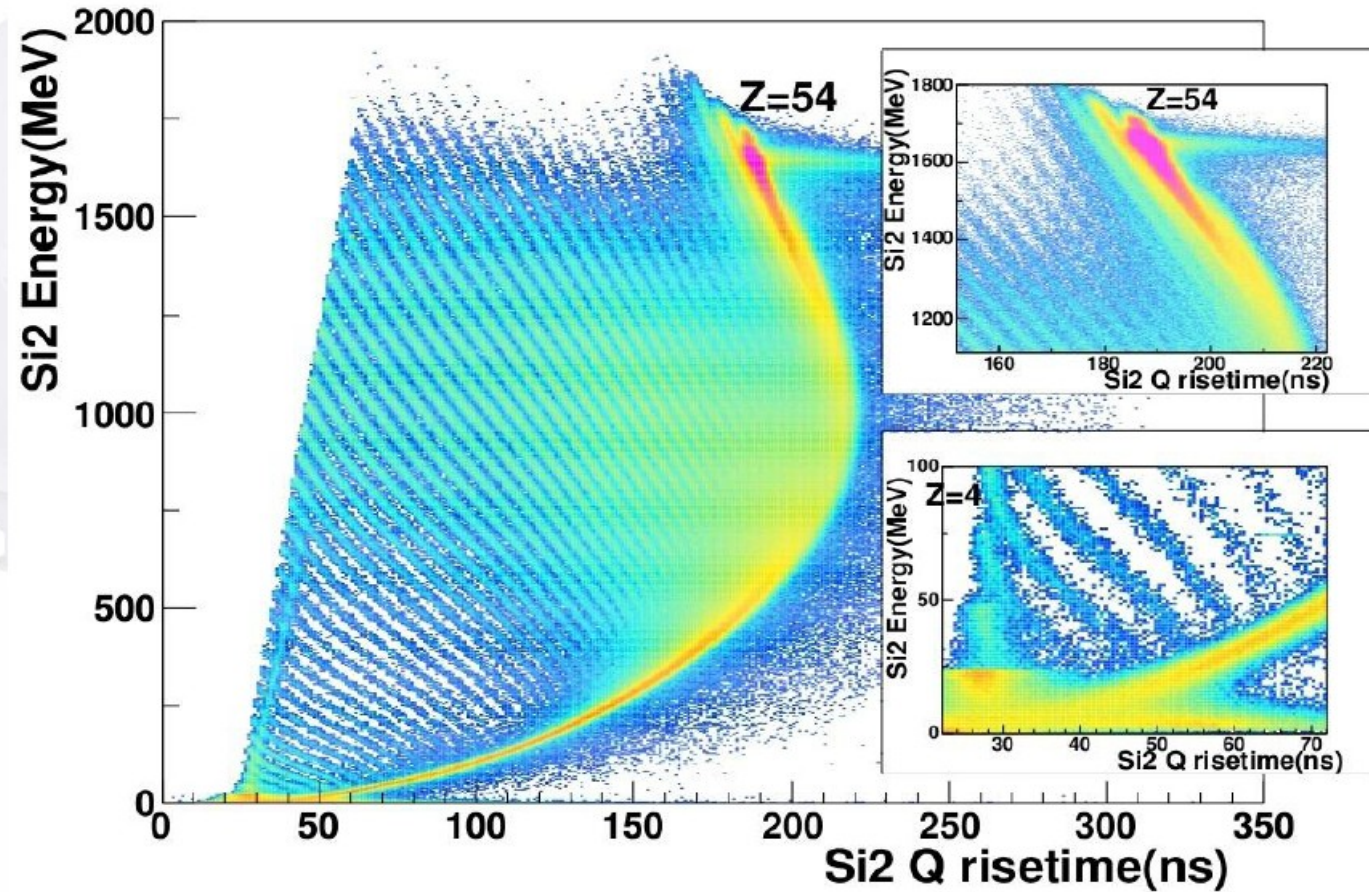
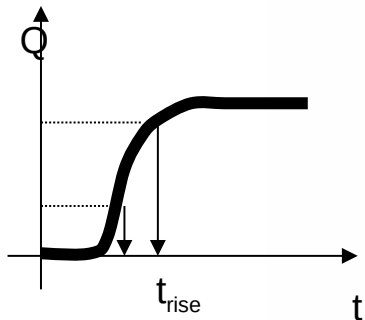
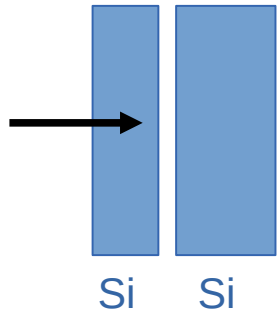
FAZIA improvements for $E-E$ identification

Improving standard $E-E$ identification method up to $Z=25-30$!



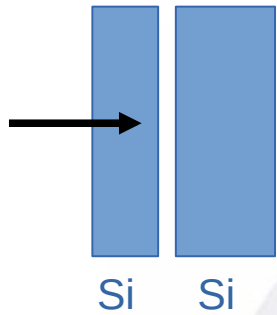
FAZIA : Pulse Shape Analysis

Some results at the end of phase 1:
Pulse Shape Analysis from E – Charge Rise Time



S. Carboni et al., NIMA 664 (2012) 251

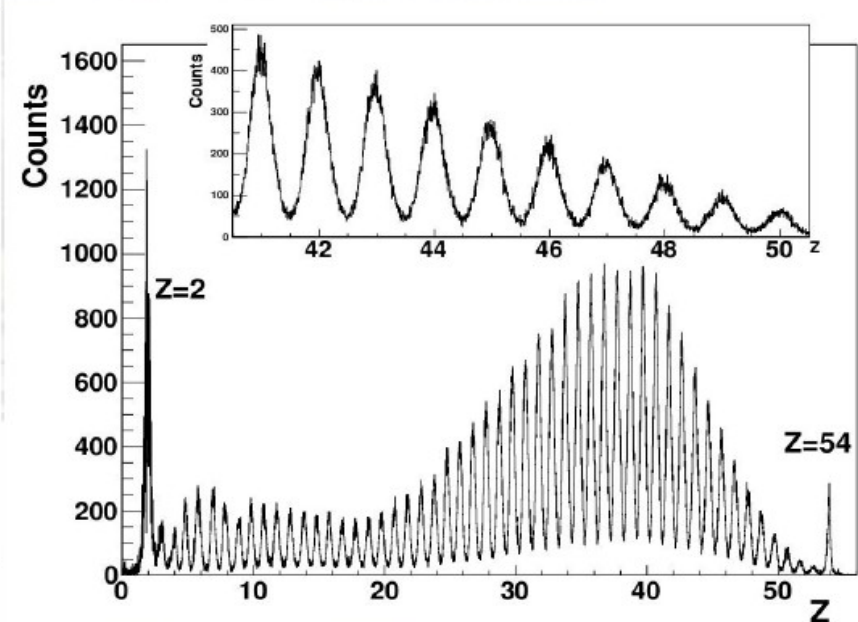
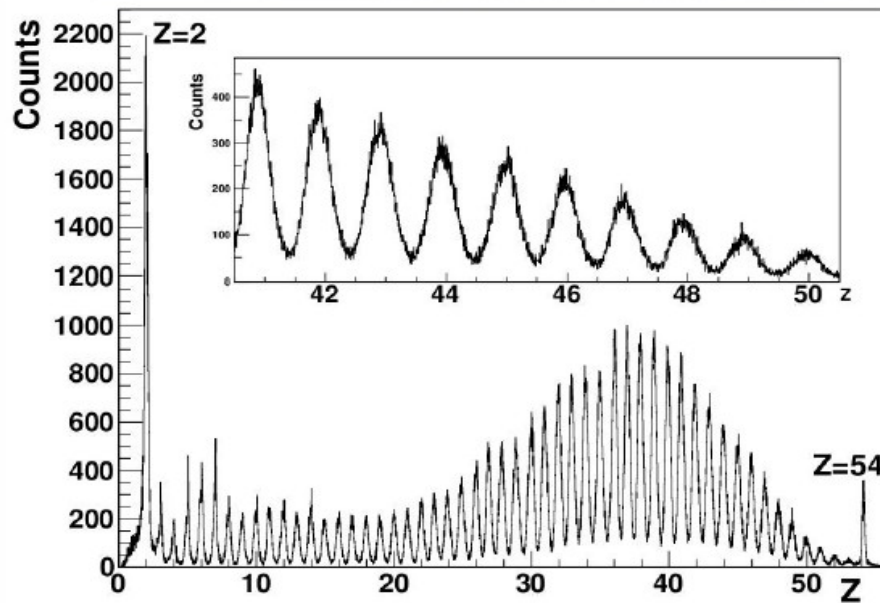
FAZIA : Pulse Shape Analysis



Some results at the end of phase 1:
Particle Identification from Pulse Shape Analysis

Energy vs. charge rise time

Energy vs. maximum of current signal

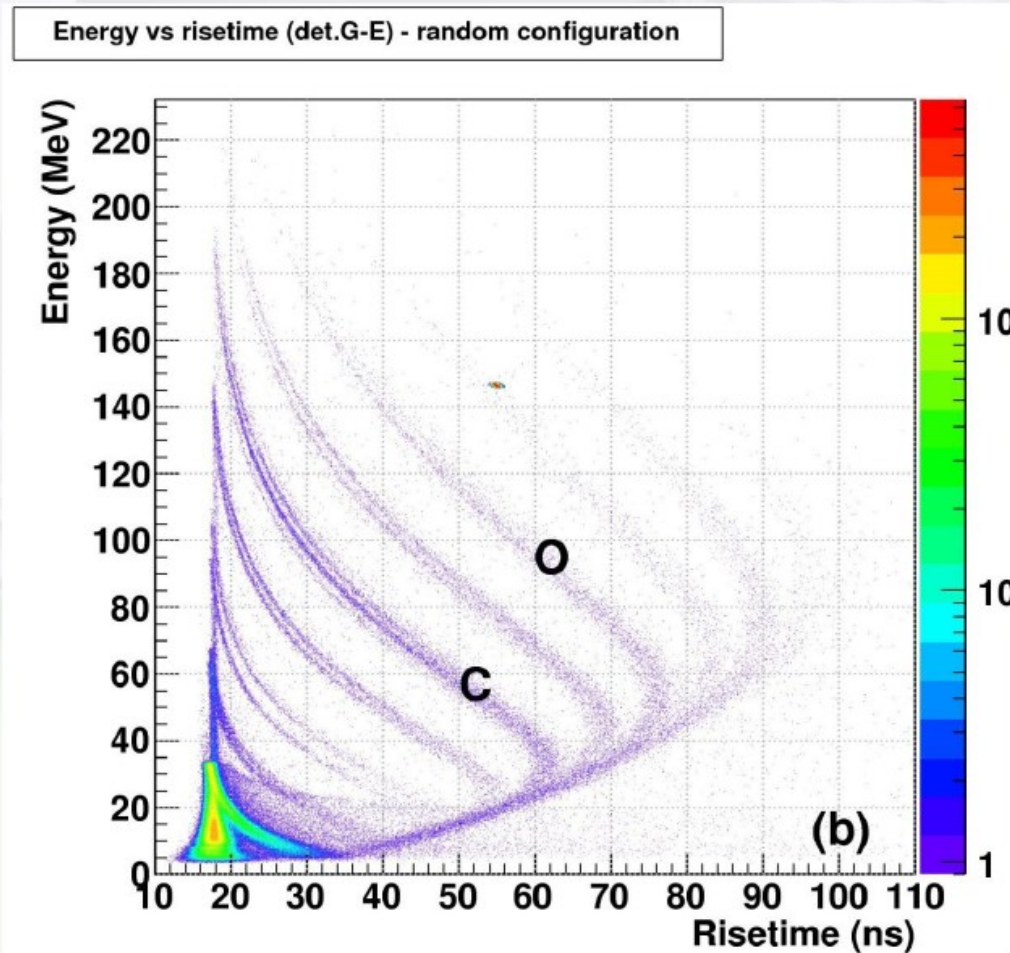
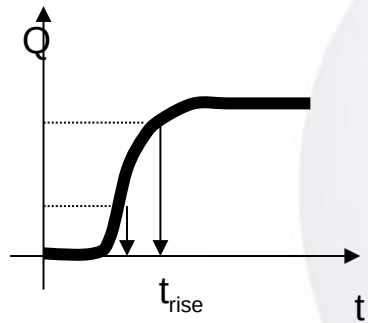


➤ Z identification can be achieved in the **first Silicon** detector

S.Carboni et al., NIMA 664 (2012) 251

FAZIA : Pulse Shape Analysis

Some results at the end of phase 1: Mass resolution from Pulse Shape Analysis Energy vs. charge rise time

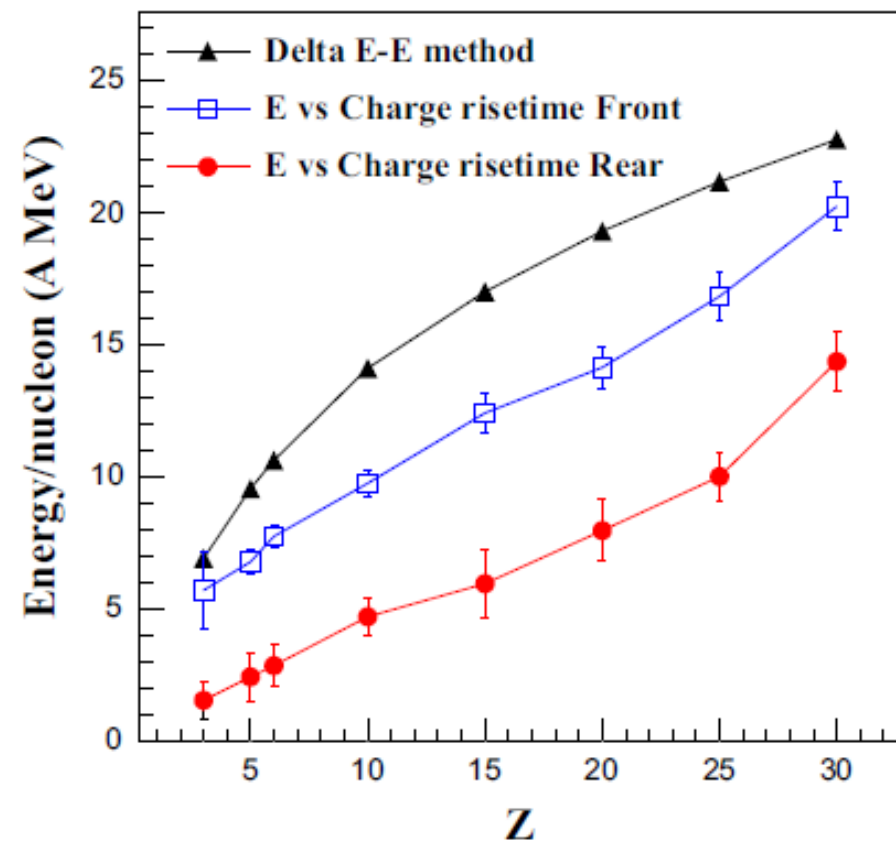
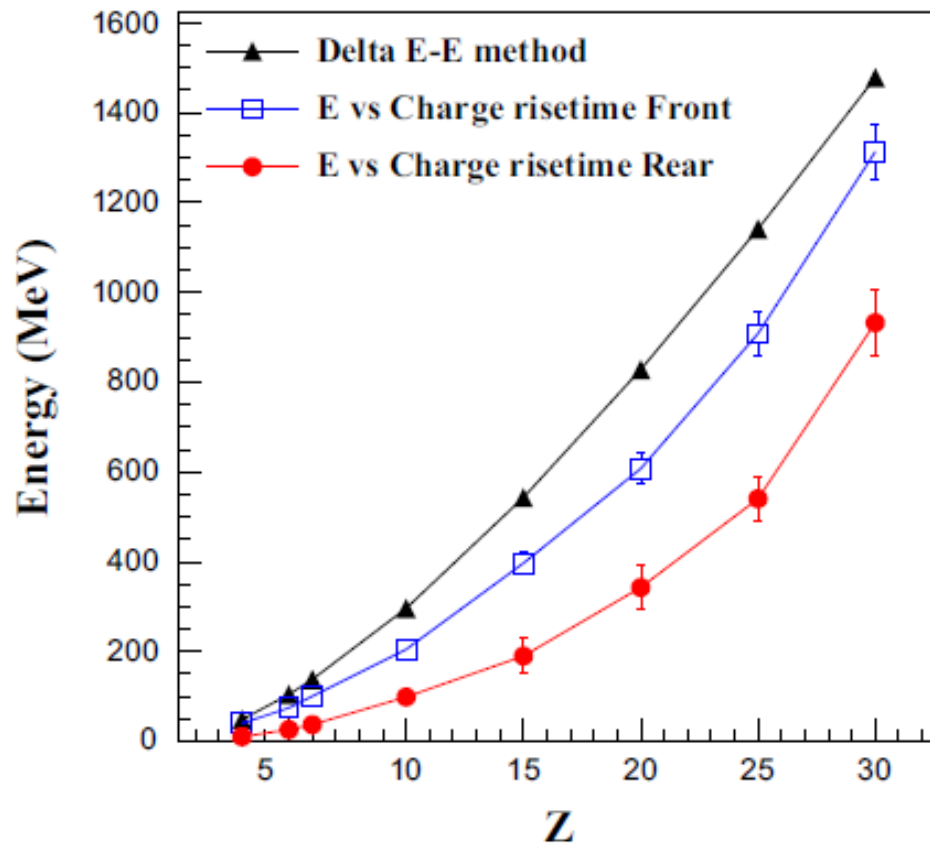


High gain
 ^{32}S beam@473MeV

L.Bardelli et al., NIMA 654 (2011) 272

➤ Isotopic identification for $Z=3-8$

FAZIA : ID thresholds (Z)



- **Pulse Shape Analysis** lowers significantly the Z (and A) thresholds
- **Rear-side** injection (low Electric Field entrance) is preferred
- « **dead** » range in Silicon is between **30** and **150 μm** for **Z=30**

N. Le Neindre et al., NIM A 701(2013) 145–152

Large diversity of nuclear reactions between 5 – 100 MeV/nucleon

Produce many different nuclear systems :

- in terms of *density* ρ , *excitation energy* E^* , *temperature* T , *spin* J , *isospin* δ
- variety of conditions for the **EOS characterization**

Allow the production and study of exotic nuclei :

- direct/transfer reactions: **effective interactions** in nuclei, **quantum shells**, **continuum**
- multi-nucleon transfer and deep inelastic scattering : toward large N/Z **exotic nuclei**
- multifragmentation : **phase transitions**, order, latent heat and **criticality (universality)**
- complete/incomplete fusion : toward **superheavy nuclei**

Mimick violent phenomena in Astrophysics of compact objects :

- Core Collapse of Supernovae: **CCSNe**
- Neutron stars mergers + **multi-messenger astrophysics** (GW+EM): NS-NS, X-ray bursts
- Stellar and extra-stellar nucleosynthesis: **r-, p-,s-processes**

Investigate EOS at low density and phase transitions in strongly corr. systems :

- EOS at **low densities**
- Density and Isospin Instabilities: LG coexistence regions, **spinodal decomposition**
- finite (nuclei) vs infinite (NS): **finite-size effects**

Some references

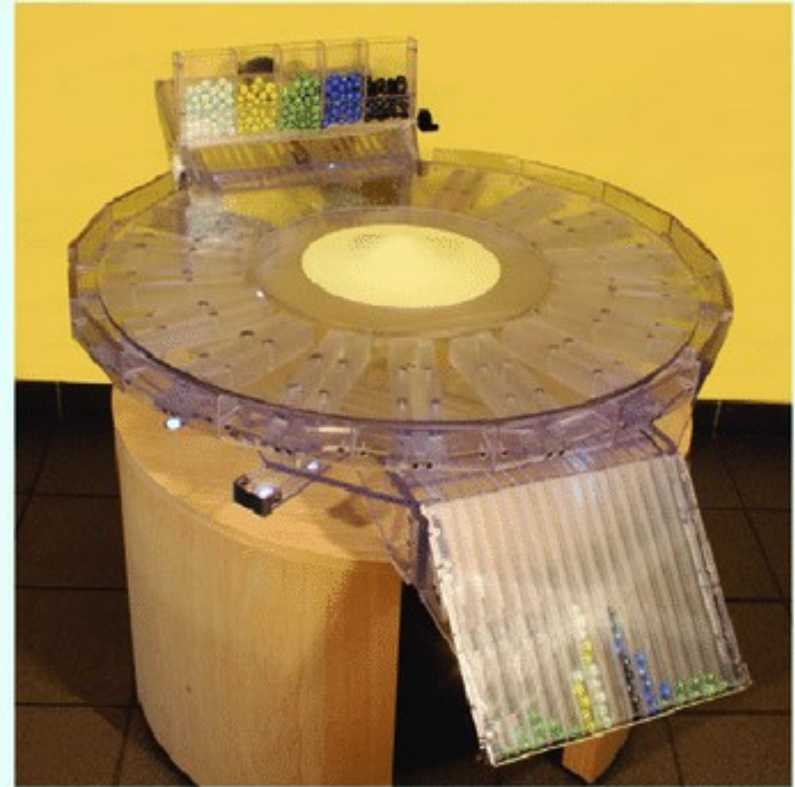
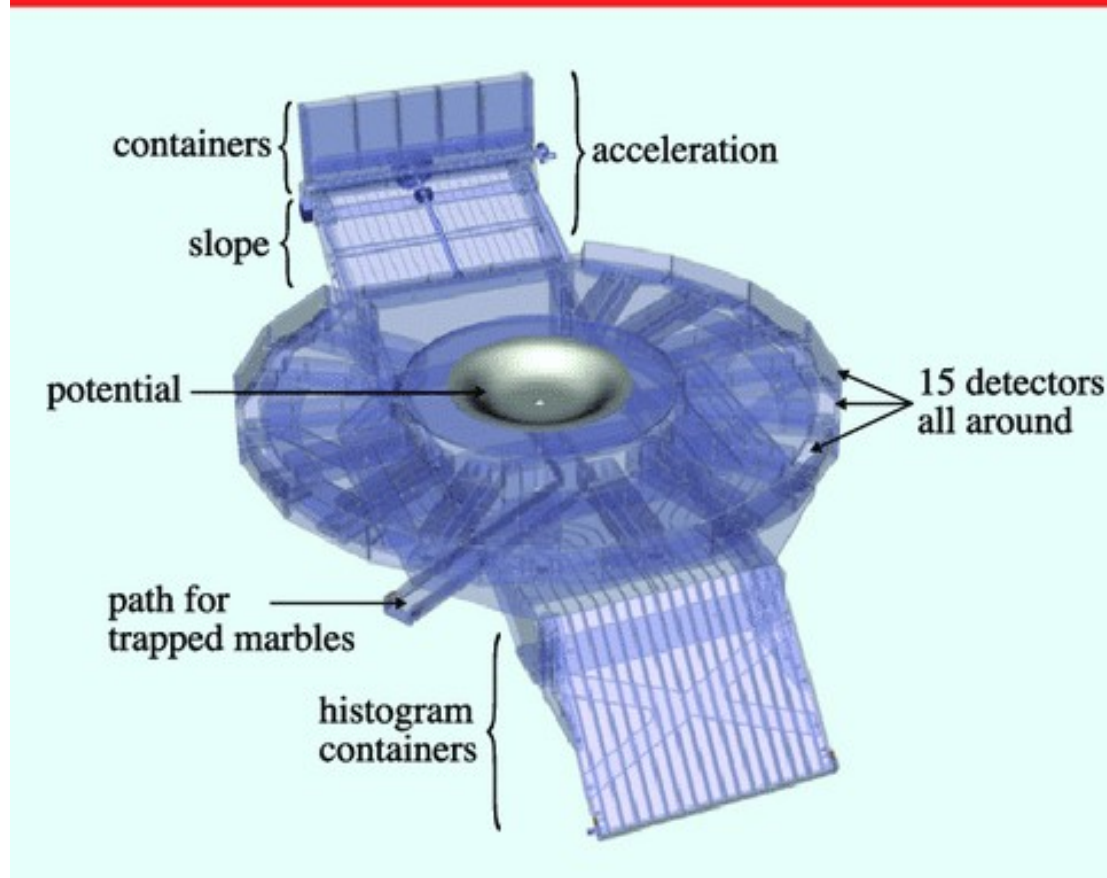
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More infos and also scientific outreach contents :

<https://www.lpc-caen.in2p3.fr/en/lpc-caen/>

Rutherford scattering with marble balls : Billotron

<https://www.lpc-caen.in2p3.fr/grand-public-rencontrer/le-billotron/>

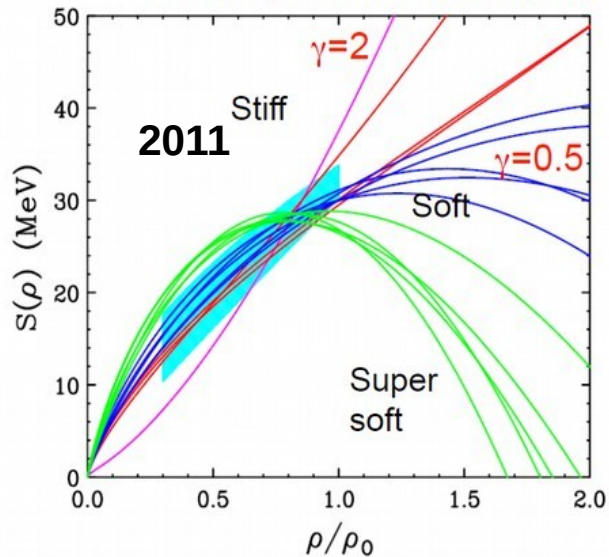


https://youtu.be/_KcK-jS2QQQ

A. Chapon, J. Gibelin, O. Lopez, D. Cussol, D. Dominique Durand, Ph. Desrues, H. Franck De Préaumont, Y. Lemièrre, J. Perronnel, and J.C. Steckmeyer. *The Billotron: a way to experimentally apprehend the subatomic world*. Physics Education, 50(4):453, 2015. doi: 10.1088/0031-9120/50/4/453. URL <http://hal.in2p3.fr/in2p3-01177619>.

Symmetry Energy around ρ_0 (II)

M.B. Tsang, Prog. Part.Nucl.Phys. 66, 400 (2011)
Brown, Phys. Rev. Lett. 85, 5296 (2001)



$$L_{\text{sym}} \approx 60 \pm 15 \text{ MeV}$$

~30%

Uncertainties can be reduced
but **covariance analysis / Bayesian Inference** is mandatory

$$S(\rho) = S_k(\rho/\rho_0)^{2/3} + S_i(\rho/\rho_0)^\gamma$$

