

Vietnam Flavour Physics Conference 2025

Introduction to BSM and Dark Sector Physics

Lorenzo Calibbi



ICISE, Quy Nhon, August 22nd 2025

Vietnam Flavour Physics Conference 2025

Probing light new particles and high energy scales with flavour-violating processes

Lorenzo Calibbi



ICISE, Quy Nhon, August 22nd 2025

Dark Matter exists! (About 27% of the energy of the universe)

DM direct detection searches and LHC searches for heavy new physics are giving increasingly tight constraints on WIMP models

This is why people increasingly focus *also* on other paradigms, *e.g.* axions, dark photons, light DM/light dark sectors etc.

Example: axion-like-particles (ALPs) (*often flavour-violating*) from a broad class of models with spontaneously broken global U(1)

Key example: axion-like particles

Pseudo Nambu-Goldstone bosons: naturally *light* & *feebly* interacting

Many scenarios motivated by outstanding problems of the SM:

Puzzle	Broken global U(1) symmetry	PNGB
• Neutrino masses \rightarrow	Lepton Number	Majoron
• Strong CP problem \rightarrow	Peccei-Quinn	Axion
• Flavour problem \rightarrow	Flavour symmetry (Froggatt-Nielsen)	Familon

In general, the couplings to the SM fermions are of the form:

$$\mathcal{L}_{aff} = \frac{\partial_\mu a}{2f_a} \bar{f}_i \gamma^\mu (C_{f_i f_j}^V + C_{f_i f_j}^A \gamma_5) f_j$$

Signature at flavour experiments: lepton/meson decays *into* ALPs

$\Rightarrow K \rightarrow \pi a, D \rightarrow \pi a, B \rightarrow K a, \mu \rightarrow e a, \tau \rightarrow \mu a, \dots$

Key example: axion-like particles

Pseudo Nambu-Goldstone bosons: naturally *light* & *feebly* interacting

Many scenarios motivated by outstanding problems of the SM:

Puzzle	Broken global U(1) symmetry	PNGB
• Neutrino masses →	Lepton Number	Majoron
• Strong CP problem →	Peccei-Quinn	Axion
• Flavour problem →	Flavour symmetry (Froggatt-Nielsen)	Familon

Interesting interplay with cosmology/astrophysics:

- ALPs can be DM candidates or serve as portals to a light dark sector:

$$\mathcal{L}_{a\chi\chi} = \frac{\partial_\mu a}{2f_a} C_{\chi\chi}^A \bar{\chi} \gamma^\mu \gamma_5 \chi \quad \leftarrow \text{dark fermion}$$

- Bounds from star cooling/supernovae (if light and feeble enough)

Lepton-flavour-violating ALPs

General interactions to leptons (dimension 5 operators):

Shift symmetry (PNGB!) \rightarrow mass arises m_a from (small) explicit U(1) breaking

$$\mathcal{L}_{all} = \frac{\partial^\mu a}{2f_a} \left(C_{ij}^V \bar{\ell}_i \gamma_\mu \ell_j + C_{ij}^A \bar{\ell}_i \gamma_\mu \gamma_5 \ell_j \right)$$

\swarrow
 \nwarrow U(1)-breaking scale \rightarrow coupling suppression

In general, these coupling are *lepton flavour violating* (LFV)

- That's natural if lepton U(1) charges are flavour non-universal
- Alternatively, flavour-violating couplings can be loop-induced

(for several explicit models see [LC Redigolo Ziegler Zupan '20](#))

This generic Lagrangian induces 2-body LFV decays such as:

$$\Gamma(\ell_i \rightarrow \ell_j a) = \frac{1}{64\pi} \frac{m_{\ell_i}^3}{f_a^2} \left(|C_{\ell_i \ell_j}^V|^2 + |C_{\ell_i \ell_j}^A|^2 \right) \left(1 - \frac{m_a^2}{m_{\ell_i}^2} \right)^2$$

[Feng et al. '97](#)

Light NP coupling with hadrons

Flavour-violating axions/ALPs couplings to quarks

$$\mathcal{L}_{aff} = \frac{\partial_\mu a}{2f_a} \bar{f}_i \gamma^\mu (C_{f_i f_j}^V + C_{f_i f_j}^A \gamma_5) f_j$$

vector coupling

axial coupling

$$P_1 \rightarrow P_2 + a \text{ [e.g. } B \rightarrow K + a] \quad P_1 \rightarrow V_2 + a \text{ [e.g. } B \rightarrow K^* + a]$$

(because of parity conservation of strong interactions)

Martin Camalich et al. '20

Decay	sd	cu	bd	bs
$\text{BR}(P_1 \rightarrow P_2 + a)$	3×10^{-11} NA62 NEW!	No analysis	4.9×10^{-5} [90]	4.9×10^{-5} [90]
$\text{BR}(P_1 \rightarrow P_2 + a)_{\text{recast}}$	No need	8.0×10^{-6} [93]	2.3×10^{-5} [92]	7.1×10^{-6} [91]
$\text{BR}(P_1 \rightarrow V_2 + a)$	3.8×10^{-5} [98]	No analysis	No analysis	No analysis
$\text{BR}(P_1 \rightarrow V_2 + a)_{\text{recast}}$	No need	No data	No data	5.3×10^{-5} [91]

to be updated soon

News from $K \rightarrow \pi + \text{inv}$ (NA62) and $B \rightarrow K + \text{inv}$ (Belle II)

→ talks by Jacopo Pinzino and Roberta Volpe

but there are still gaps...

Flavour-violating axions/ALPs couplings to quarks

$$\mathcal{L}_{aff} = \frac{\partial_\mu a}{2f_a} \bar{f}_i \gamma^\mu (C_{f_i f_j}^V + C_{f_i f_j}^A \gamma_5) f_j$$

vector coupling

axial coupling

$$P_1 \rightarrow P_2 + a \text{ [e.g. } B \rightarrow K + a] \quad P_1 \rightarrow V_2 + a \text{ [e.g. } B \rightarrow K^* + a]$$

(because of parity conservation of strong interactions)

Martin Camalich et al. '20

Decay	sd	cu	bd	bs
$\text{BR}(P_1 \rightarrow P_2 + a)$	3×10^{-11} NA62 NEW!	No analysis	4.9×10^{-5} [90]	4.9×10^{-5} [90]
$\text{BR}(P_1 \rightarrow P_2 + a)_{\text{recast}}$	No need	8.0×10^{-6} [93]	2.3×10^{-5} [92]	7.1×10^{-6} [91]
$\text{BR}(P_1 \rightarrow V_2 + a)$	3.8×10^{-5} [98]	No analysis	No analysis	No analysis
$\text{BR}(P_1 \rightarrow V_2 + a)_{\text{recast}}$	No need	No data	No data	5.3×10^{-5} [91]

Example: No dedicated searches for D to axion decays

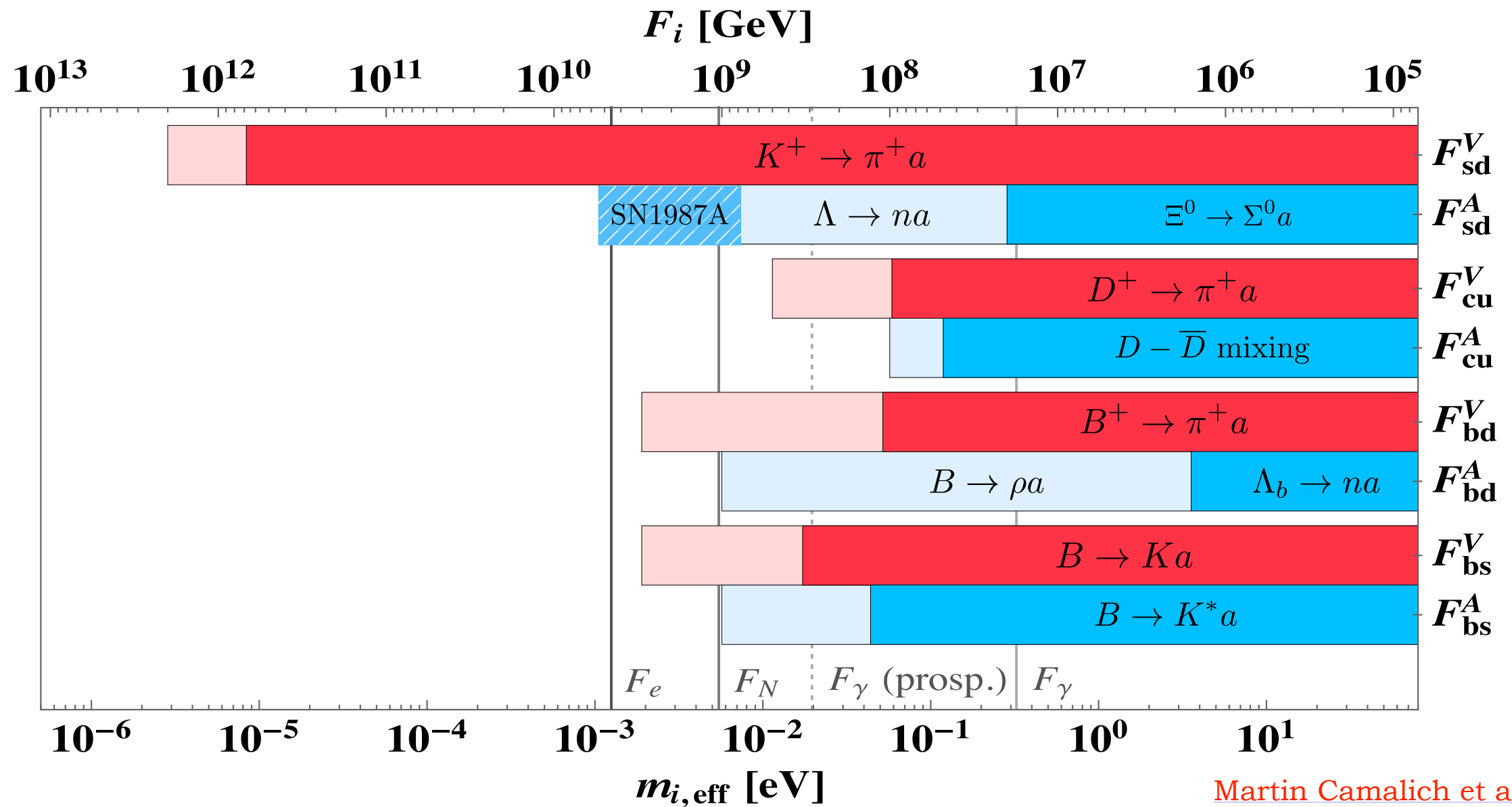
Recasting data from $D^+ \rightarrow \tau^+ (\rightarrow \pi^+ \nu) \nu$ (CLEO 2008):

$$\text{BR}(D^+ \rightarrow \pi^+ a) < 8 \times 10^{-6} \rightarrow \text{BESIII ? Belle II ?}$$

Flavour-violating axions/ALPs couplings to quarks

$$\mathcal{L}_{aff} = \frac{\partial_\mu a}{2f_a} \bar{f}_i \gamma^\mu (C_{f_i f_j}^V + C_{f_i f_j}^A \gamma_5) f_j$$

$$F_{f_i f_j}^{V,A} \equiv \frac{2f_a}{C_{f_i f_j}^{V,A}}$$



Another example: a flavour-violating Z'

Flavour non-universal **local** U(1) symmetry generating the hierarchies of fermion masses and mixing through the Froggatt-Nielsen mechanism

(anomalies cancelled by suitable UV completions [Smolkovič Tammara Zupan '19](#) [Bonney Dudas Pokorski '19](#))

Interactions of the new gauge boson Z' **flavour-violating** by construction:

$$\mathcal{L} = g_F Z'_\mu \left[\bar{u}_\alpha \gamma^\mu (C_{L\alpha\beta}^u P_L + C_{R\alpha\beta}^u P_R) u_\beta + \bar{d}_\alpha \gamma^\mu (C_{L\alpha\beta}^d P_L + C_{R\alpha\beta}^d P_R) d_\beta + \right. \\ \left. \bar{\ell}_\alpha \gamma^\mu (C_{L\alpha\beta}^\ell P_L + C_{R\alpha\beta}^\ell P_R) \ell_\beta + \bar{\nu}_\alpha \gamma^\mu C_{L\alpha\beta}^\nu P_L \nu_\beta \right],$$

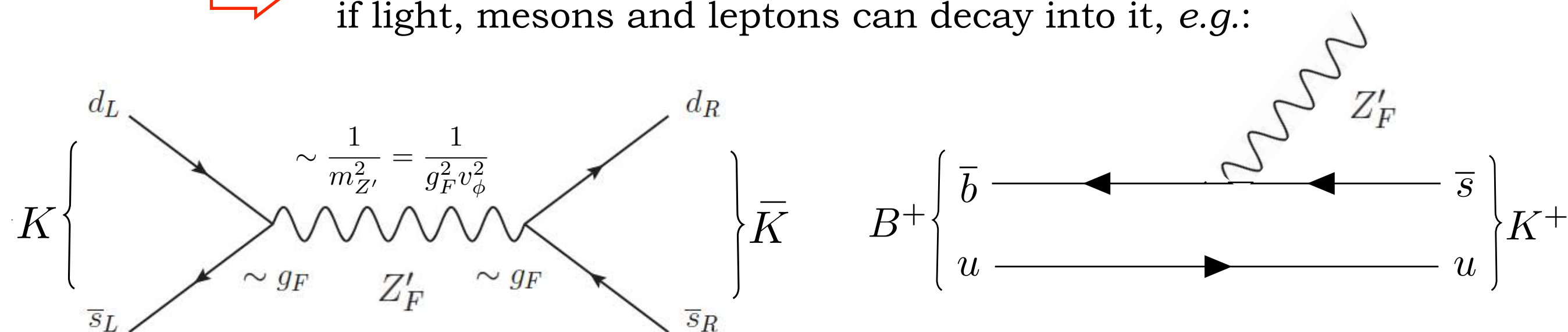
new U(1) gauge coupling

unitary rotations to the fermion mass basis

$C_{L\alpha\beta}^f \equiv V_{\alpha i}^f Q_{fLi} V_{\beta i}^{f*}$ $C_{R\alpha\beta}^f \equiv W_{\alpha i}^f Q_{fRi} W_{\beta i}^{f*}$ matrices of U(1) charges

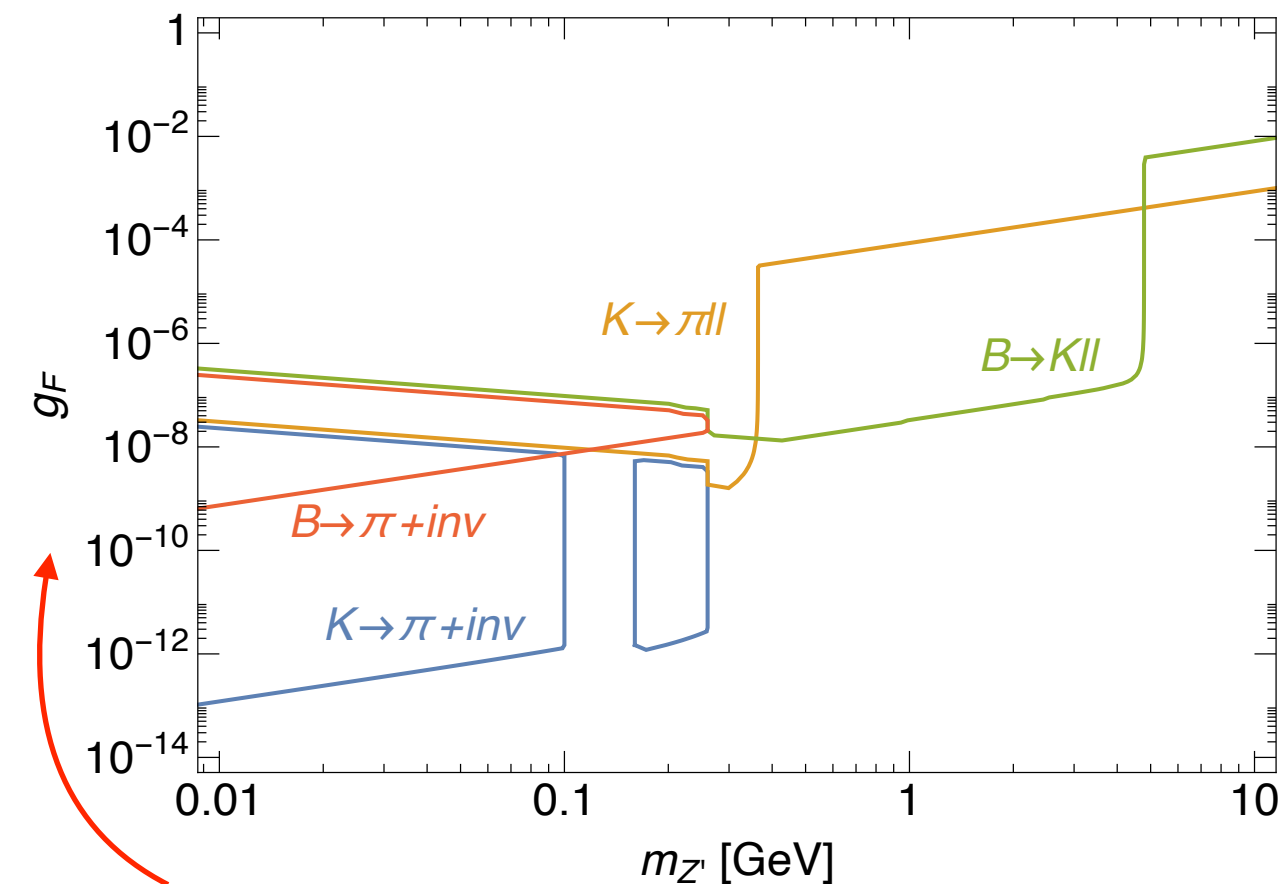
$C_{V,A}^f = \frac{C_R^f \pm C_L^f}{2}$

Z' mediates flavour-violating processes and, if light, mesons and leptons can decay into it, e.g.:

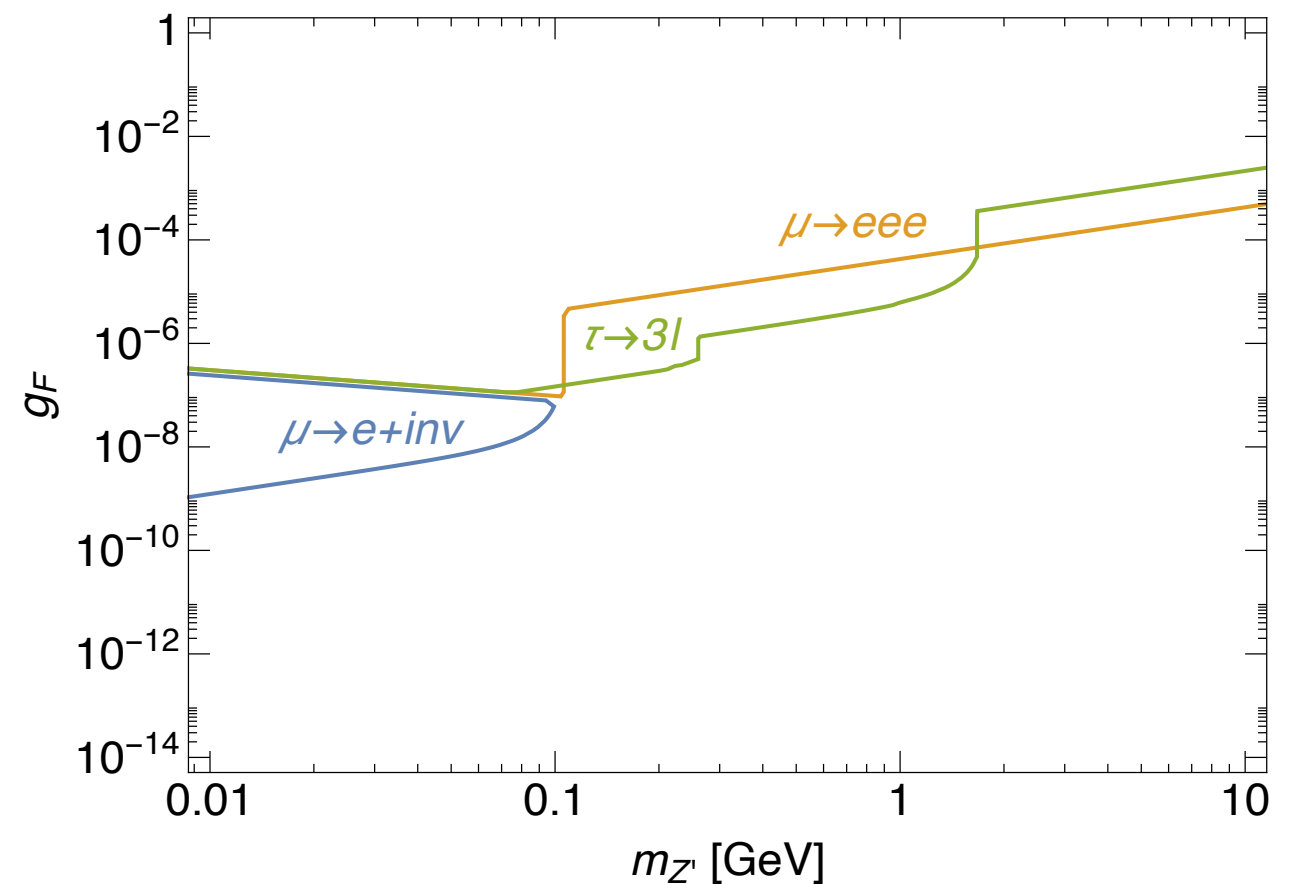


Flavour-violating Z' : flavour bounds

Meson decays into Z'



Lepton decays into Z'



U(1) coupling

$$m_{Z'} = \sqrt{2} g_F \langle \phi \rangle = g_F v_\phi$$

Z' boson mass

Flavour processes set stringent **lower bounds** on the U(1) breaking scale

$$K^+ \rightarrow \pi^+ Z' : v_\phi \gtrsim 8.3 \times 10^{10} \text{ GeV}, \quad B^+ \rightarrow K^+ Z' : v_\phi \gtrsim 3.0 \times 10^7 \text{ GeV}$$

$$\mu \rightarrow e Z' : v_\phi \gtrsim 1.3 \times 10^7 \text{ GeV}, \quad \tau \rightarrow \ell Z' : v_\phi \gtrsim 7.6 \times 10^5 \text{ GeV}$$

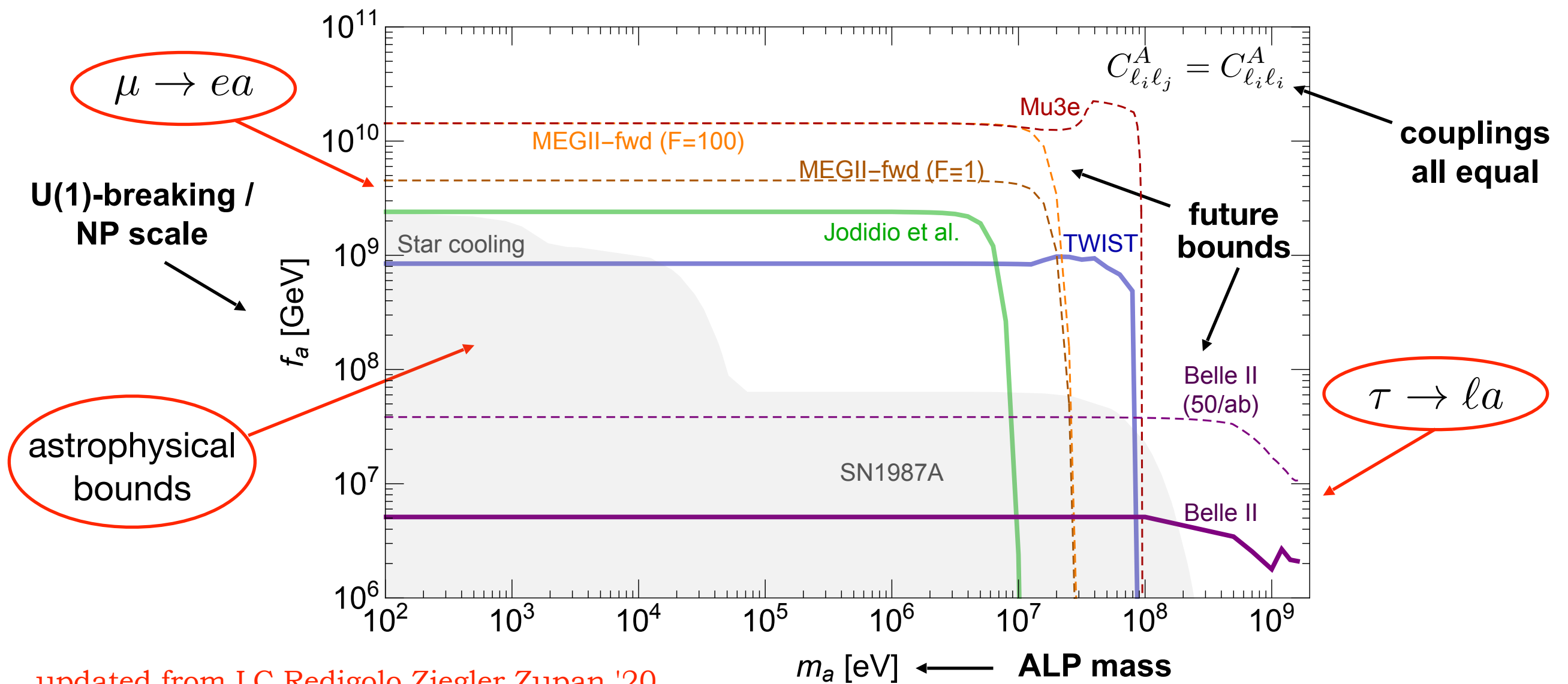
$$K - \bar{K} \text{ mix.} : v_\phi \gtrsim 6.5 \times 10^5 \text{ GeV}$$

Blasi LC Mariotti Turbang '24

Light NP coupling with leptons

Summary of searches for light *invisible* LFV ALPs

$$\mathcal{L}_{all} = \frac{\partial^\mu a}{2f_a} (C_{ij}^V \bar{\ell}_i \gamma_\mu \ell_j + C_{ij}^A \bar{\ell}_i \gamma_\mu \gamma_5 \ell_j) \Rightarrow \Gamma(\ell_i \rightarrow \ell_j a) = \frac{1}{64\pi} \frac{m_{\ell_i}^3}{f_a^2} (|C_{\ell_i \ell_j}^V|^2 + |C_{\ell_i \ell_j}^A|^2) \left(1 - \frac{m_a^2}{m_{\ell_i}^2}\right)^2$$



- Decays mediated by dimension-5 operators: one can reach NP scales even larger than $\mu \rightarrow e\gamma$, $\mu \rightarrow eee$ etc. (from dim-6 operators → **Yamanaka-san talk**)
- Mu/tau/astro interplay: if $m_a > m_\mu$ constraints mainly come from τ decays

$\mu \rightarrow e a$: signal and background

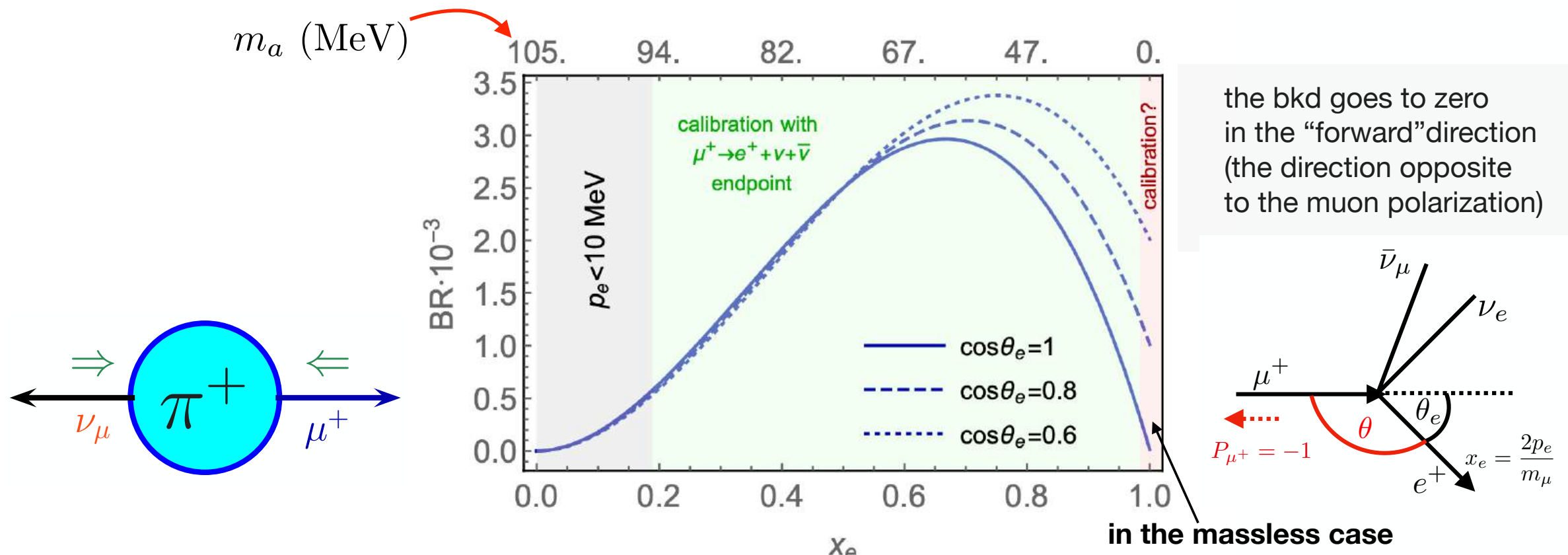
Signal: monochromatic positron with $p_e = \sqrt{\left(\frac{m_\mu^2 - m_a^2 + m_e^2}{2m_\mu}\right)^2 - m_e^2}$

Differential decay rate: $\frac{d\Gamma(\ell_i \rightarrow \ell_j a)}{d\cos\theta} = \frac{m_{\ell_i}^3}{32\pi F_{\ell_i\ell_j}^2} \left(1 - \frac{m_a^2}{m_{\ell_i}^2}\right)^2 \left[1 + 2P_{\ell_i} \cos\theta \frac{C_{\ell_i\ell_j}^V C_{\ell_i\ell_j}^A}{(C_{\ell_i\ell_j}^V)^2 + (C_{\ell_i\ell_j}^A)^2}\right]$

signal anisotropy depends on the chirality of the couplings

Michel spectrum: $\frac{d^2\Gamma(\mu^+ \rightarrow e^+ \nu_e \bar{\nu}_\mu)}{dx_e d\cos\theta} \simeq \Gamma_\mu ((3 - 2x_e) - P_\mu(2x_e - 1)\cos\theta) x_e^2$ $x_e = \frac{2p_e}{m_\mu}$ μ polarisation

And “surface” muons are highly polarised (produced by pion decays at rest on the surface of the production target) \rightarrow the SM background can be suppressed



Currently strongest limit on $\mu \rightarrow e a$

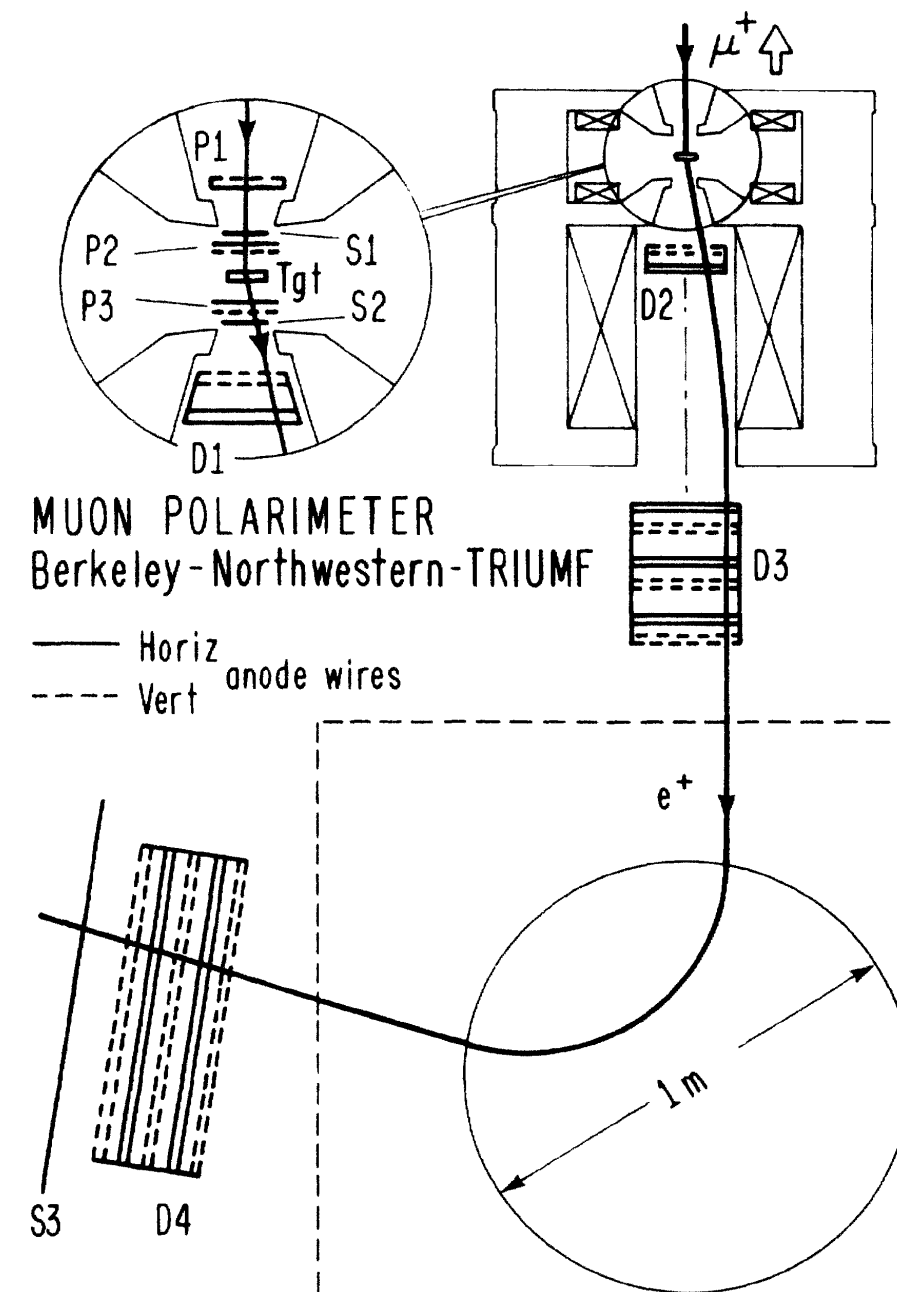
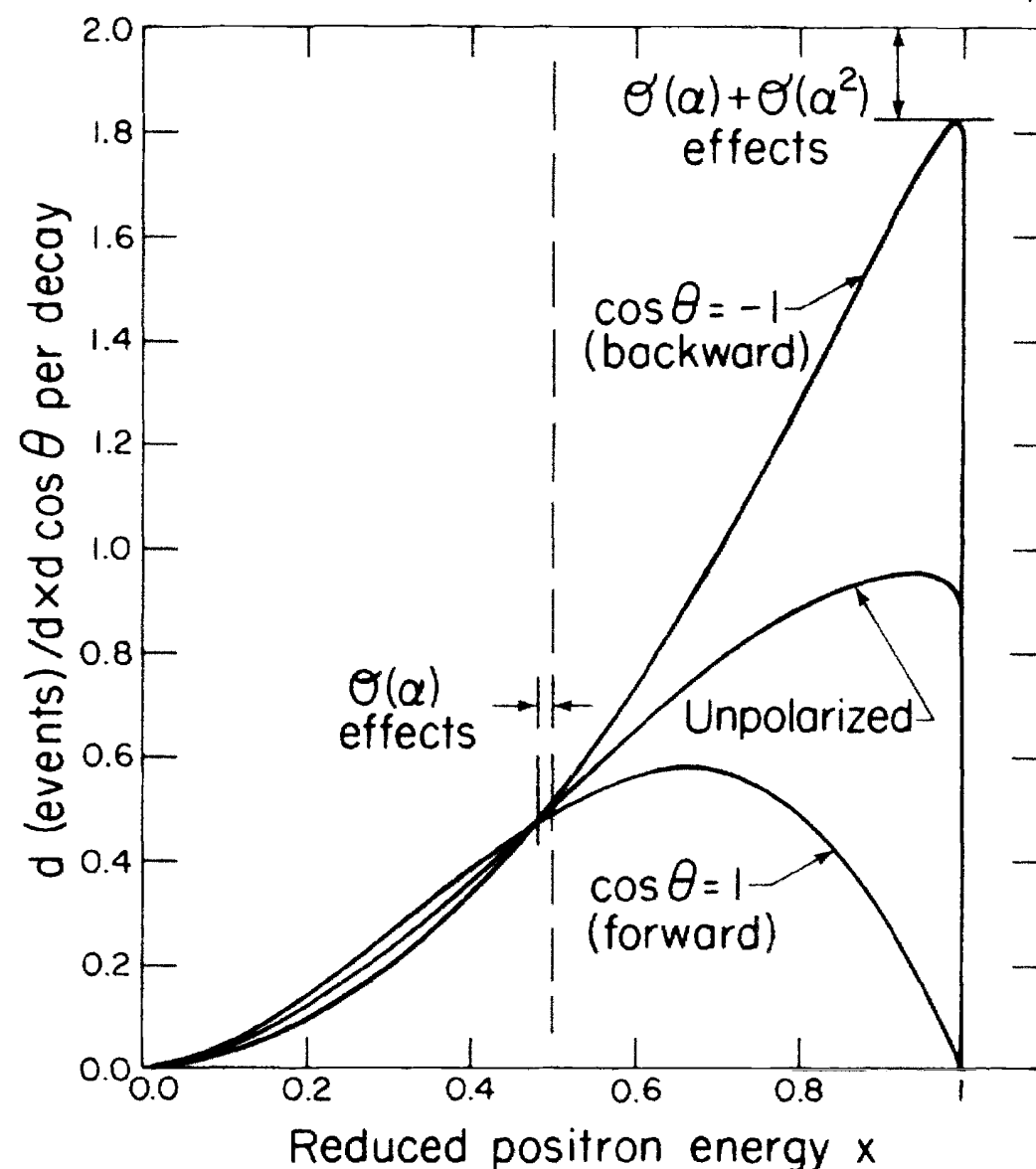
- Jodidio et al. (TRIUMF) 1986

Search for RH currents with 1.8×10^7 polarised μ^+

Ordinary $\mu \rightarrow e \bar{\nu} \nu$

$$\frac{d^2\Gamma}{dx d\cos\theta} = \Gamma_\mu ((3 - 2x) - P(2x - 1) \cos\theta) x^2$$

$$x = 2E_e/m_\mu$$



Very good e^+ momentum resolution
(~70 KeV at the e.p.)

Currently strongest limit on $\mu \rightarrow e a$

- Jodidio et al. (TRIUMF) 1986

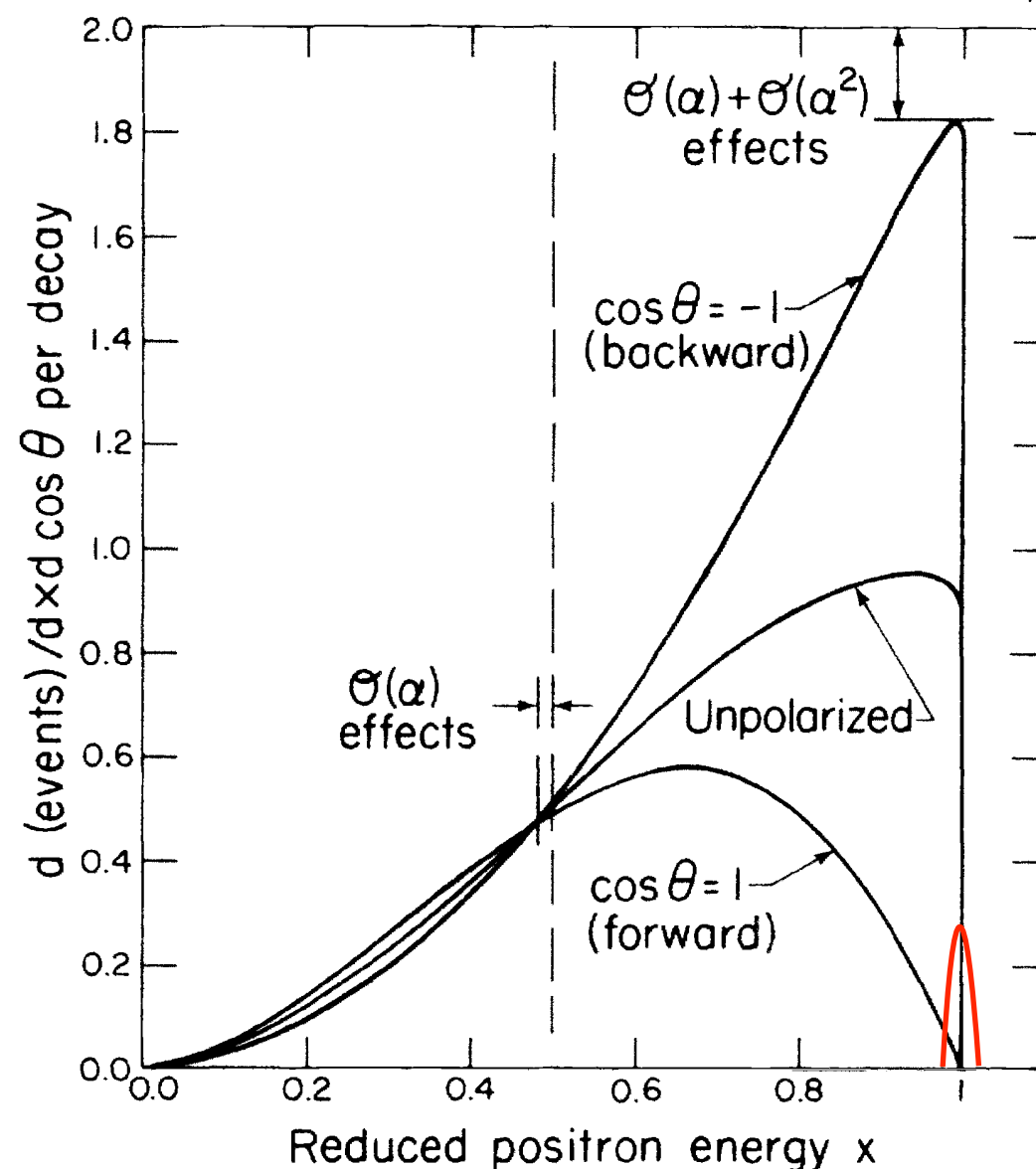
Search for RH currents with 1.8×10^7 polarised μ^+ interpreted in terms of $\mu \rightarrow e a$ too

Ordinary $\mu \rightarrow e \bar{\nu} \nu$

$$\frac{d^2\Gamma}{dx d\cos\theta} = \Gamma_\mu ((3 - 2x) - P(2x - 1) \cos\theta) x^2$$

$$x = 2E_e/m_\mu$$

$\mu \rightarrow e a$ signal for $m_a \approx 0$:
monochromatic e^+ at $m_\mu/2$



Unless it couples (V-A) like in the SM:

$$\frac{d\Gamma(\mu^+ \rightarrow e^+ a)}{d\cos\theta} = \frac{\Gamma_{\mu \rightarrow e a}}{2} \left[1 + 2P \cos\theta \frac{C_{e\mu}^V C_{e\mu}^A}{(C_{e\mu}^V)^2 + (C_{e\mu}^A)^2} \right]$$

for the *isotropic* case, they set the limit

$$\Rightarrow \text{BR}(\mu^+ \rightarrow e^+ a) < 2.6 \times 10^{-6}$$

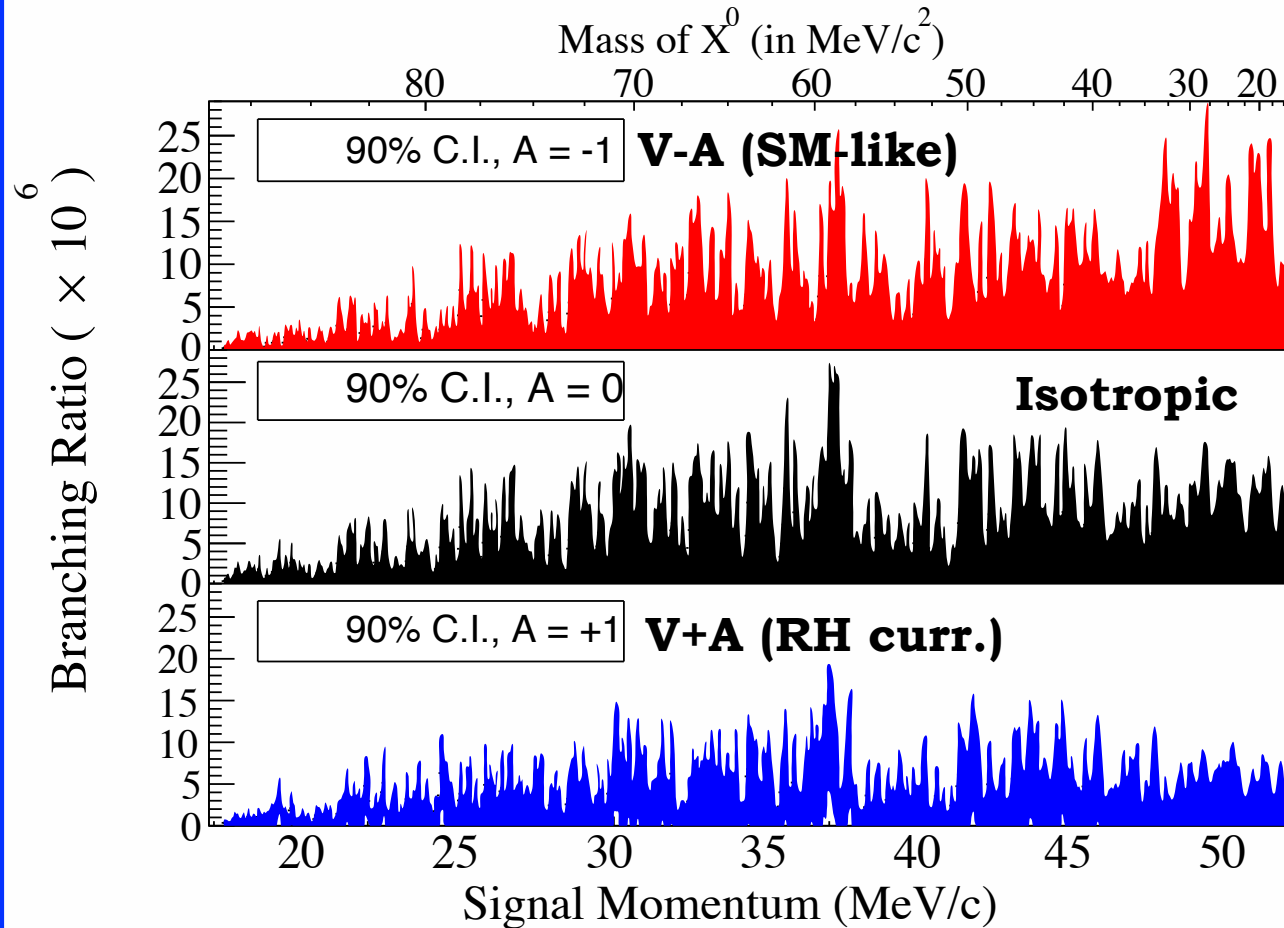
thus one gets

$$\Rightarrow f_a/C_{e\mu}^{V,A} > 2.4 \times 10^9 \text{ GeV}$$

Past searches: $\mu \rightarrow e a$

- **TWIST 2014** Precise measurement of Michel parameters plus dedicated search for $\mu \rightarrow e a$ in the whole m_a range considering anisotropy of the signal

Limits (with $5.8 \times 10^8 \mu^+$):



Decay Signal		90% C.L. (in ppm)	p-value
$A = 0$	Average	9	
	$p = 37.03 \text{ MeV}/c$	26	0.66
	Endpoint	21	0.81
$A = -1$ SM-like	Average	10	
	$p = 37.28 \text{ MeV}/c$	26	0.60
	Endpoint	58	0.80
$A = +1$	Average	6	
	$p = 19.13 \text{ MeV}/c$	6	0.59
	Endpoint	10	0.90

For V-A coupl. and $m_a \approx 0$: $\text{BR}(\mu \rightarrow e a) < 5.8 \times 10^{-5}$

$$\Rightarrow f_a / C_{e\mu}^{V,A} > 10^9 \text{ GeV}$$

Present bounds based on old experiments and/or moderate luminosities ($< 10^9$ total muon decays)

Modern facilities, e.g. $\pi E5$ beamline at PSI (where MEGII and Mu3e are located), can deliver $> 10^8$ muons *per second*:
next generation experiments must do better!

$\mu \rightarrow e a$: future prospects

Many ideas and proposals at running and upcoming experiments:

MEG II → Toshiyuki Iwamoto's talk

- Add a forward calorimeter to perform a Jodidio-like search [LC et al. '20](#)
- Run with a dedicated trigger to search for $\mu \rightarrow e a \gamma$ [Jho Knapen Redigolo '22](#)

Mu3e → Tamasi Kar's talk

- Search performed on e^+ momentum histograms filled with *online* reconstructed short tracks [Perrevoort \(Mu3e\) '18](#)
- Search for $\mu \rightarrow 3 e a$ from the internal conversion of virtual photon into $e^+ e^-$ [Knapen et al. '23](#)

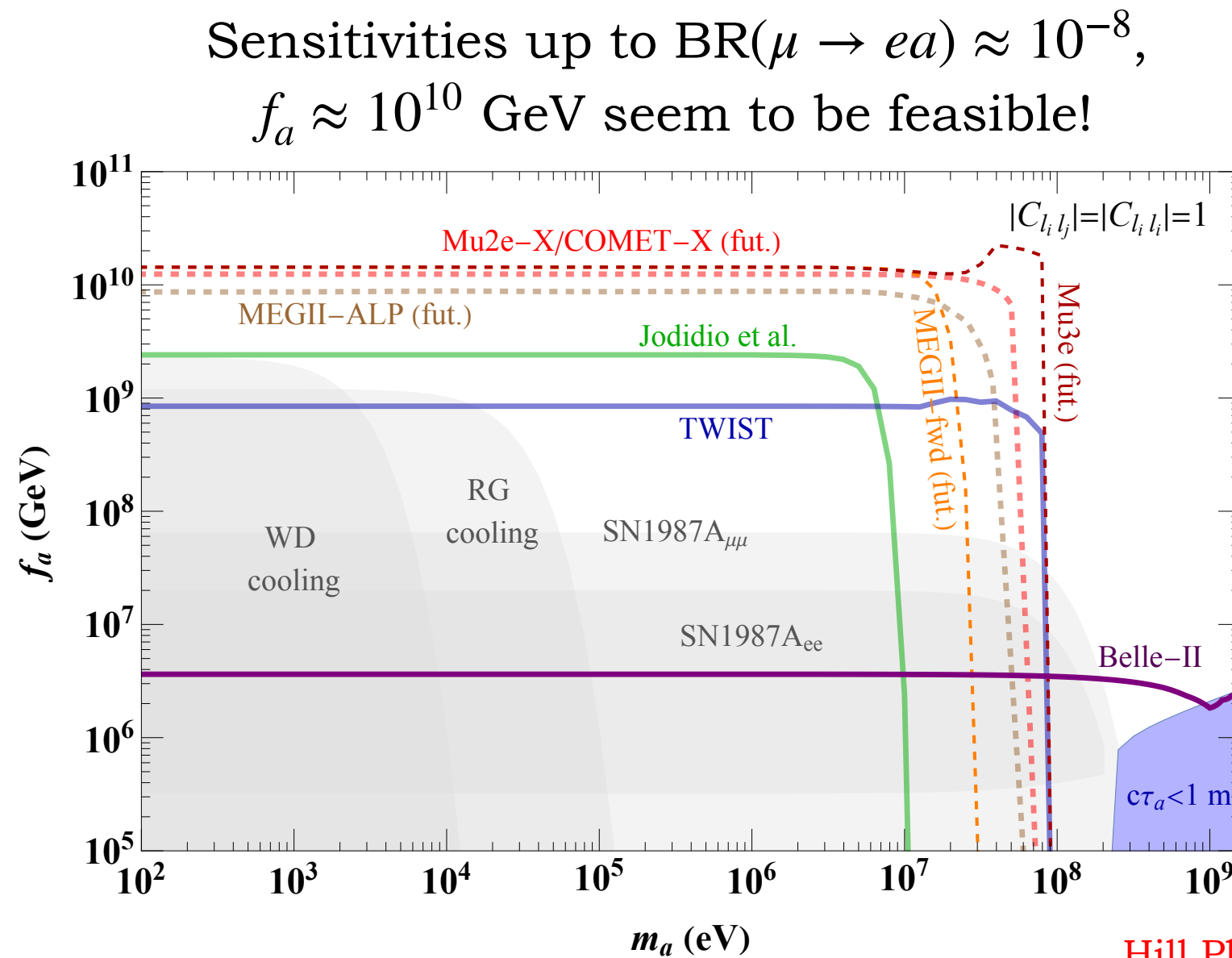
COMET/Mu2e → Truong Nguyen's talk

- search for excess over the Michel spectrum, using data from calibration runs employing *positive* muon beams [Hill Plestid Zupan '23](#)
- enlarge the $\mu \rightarrow e$ conversion signal window coping with a large ($\sim 100\text{kHz}$?) Michel background rate [Xing et al. '22](#)

cf. [backup slides](#) for details

$\mu \rightarrow e a$: future prospects

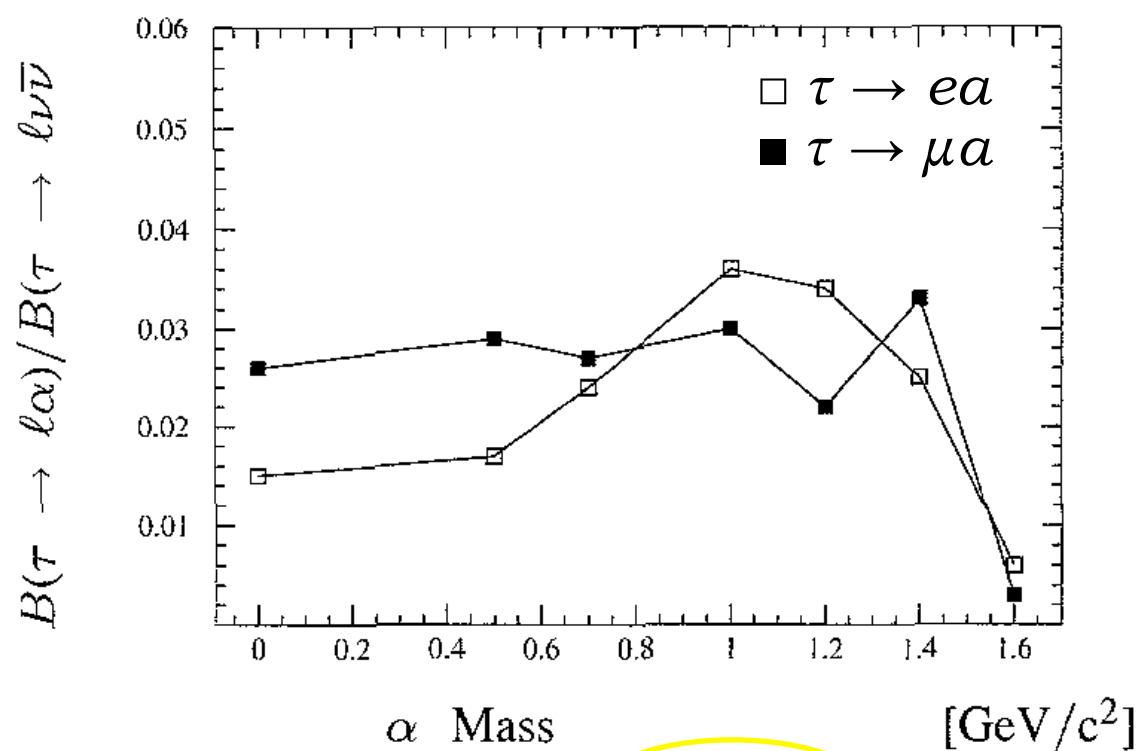
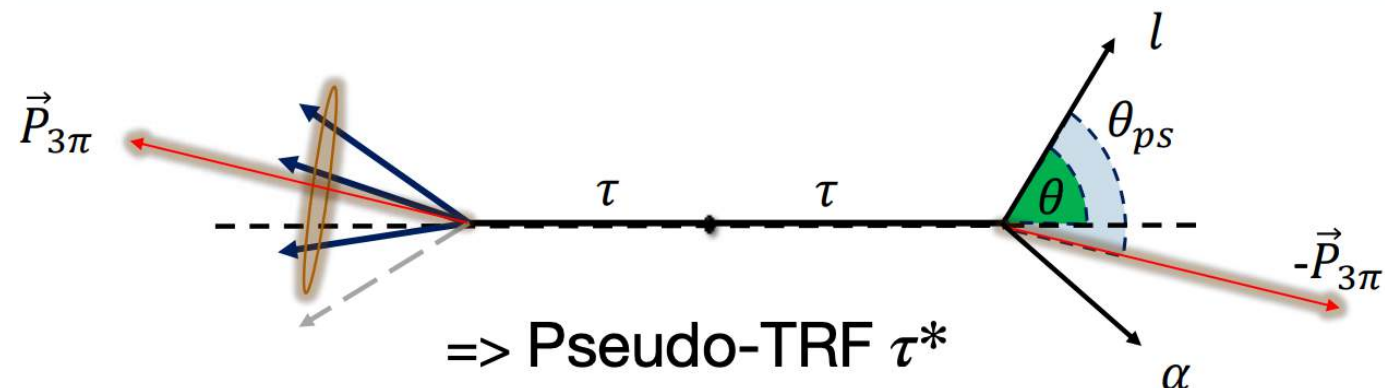
Many ideas and proposals at running and upcoming experiments:



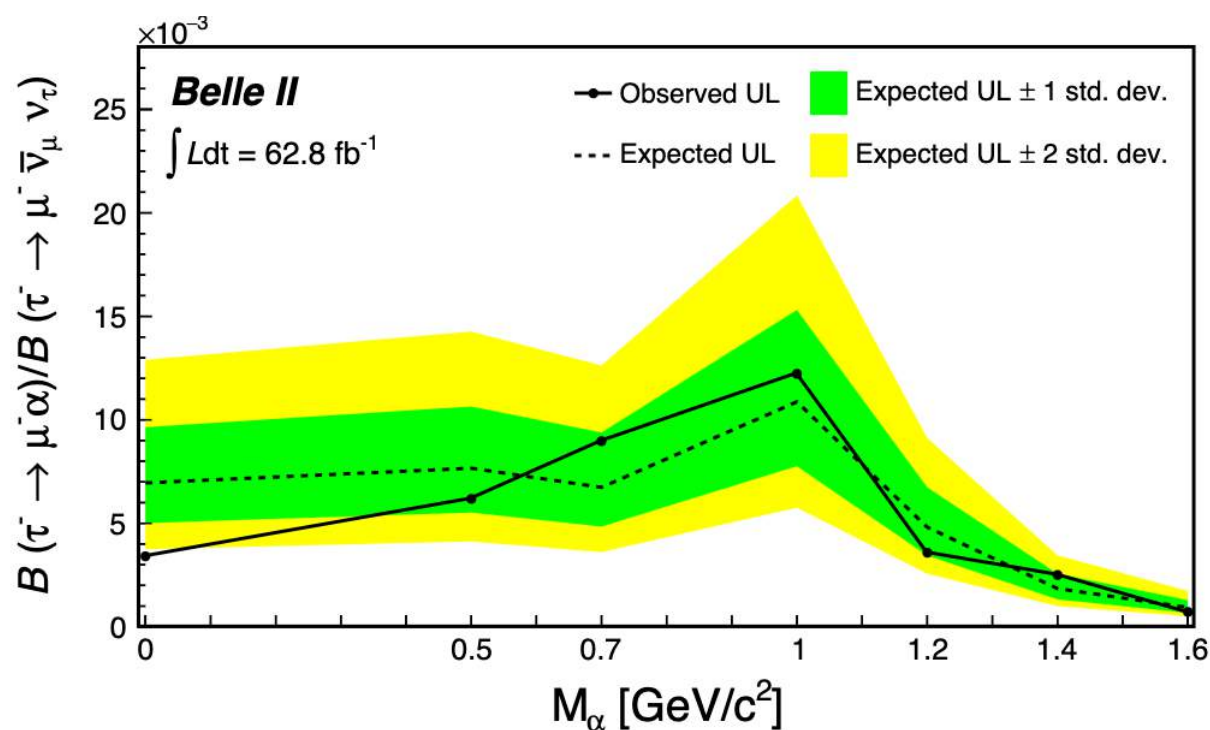
cf. backup slides for details

Present limits on $\tau \rightarrow e a$, $\tau \rightarrow \mu a$ (invisible a)

A challenging search:
tau momentum / rest frame
cannot be exactly reconstructed
BG: ordinary $\tau \rightarrow \ell \nu \bar{\nu}$



ARGUS 1995 (472 pb⁻¹)



Belle II 2023 (62.8 fb⁻¹)

up to O(10) improvement!

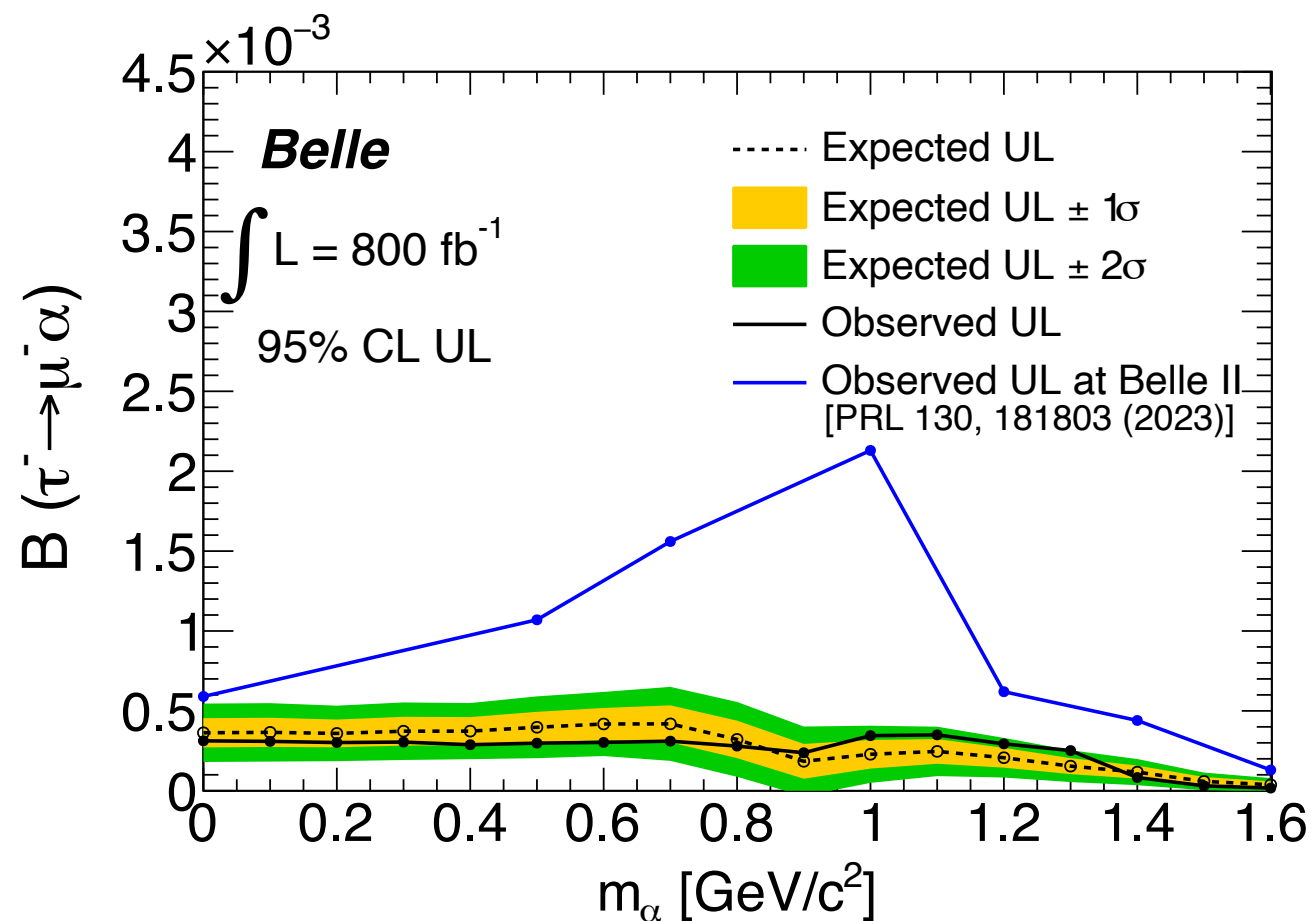
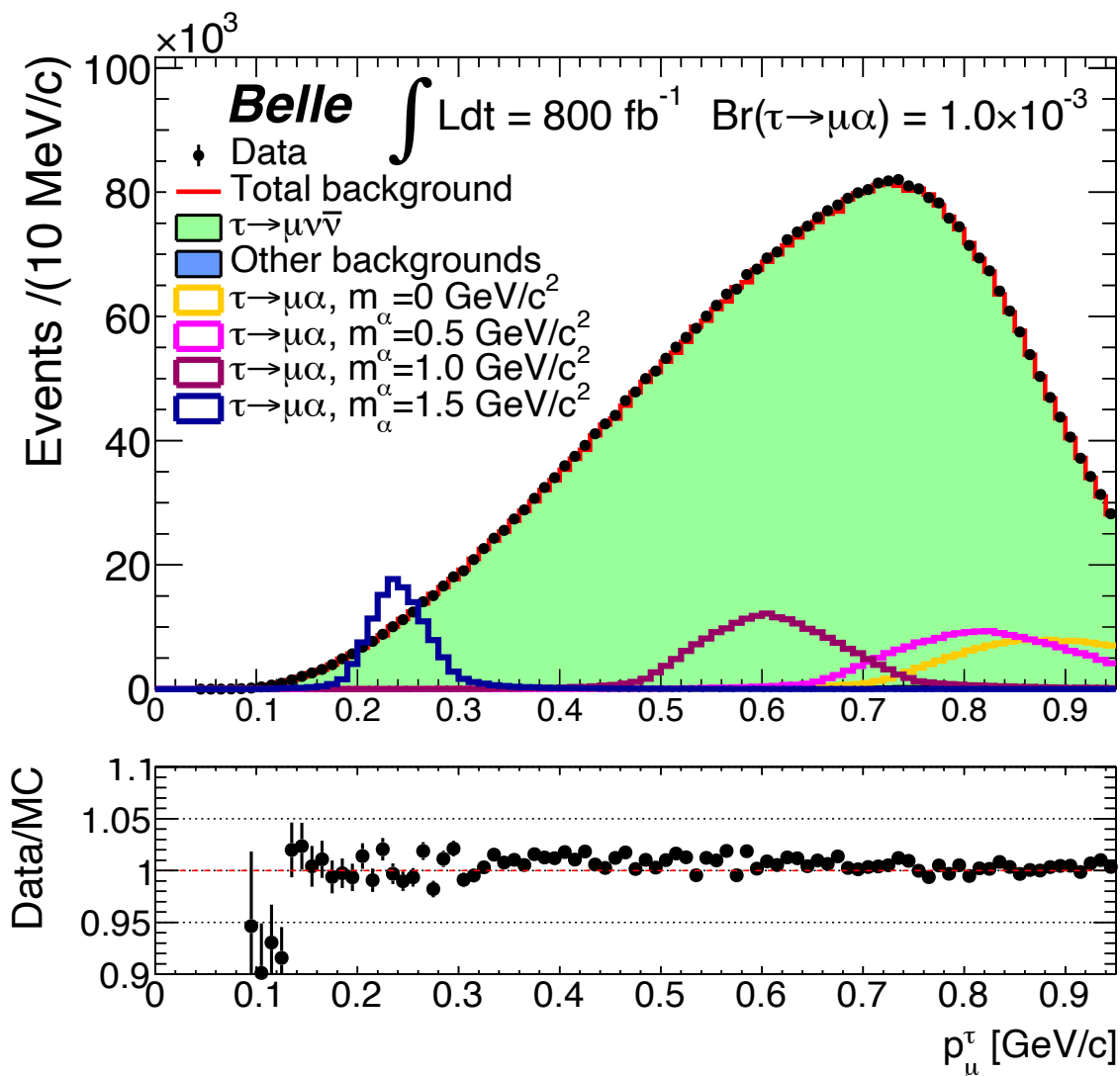
$$m_a \approx 0 : \quad \begin{aligned} \text{BR}(\tau \rightarrow \mu a) &< 4.7 \times 10^{-4} \text{ (90\% CL)} \Rightarrow f_a / C_{\mu\tau}^{V,A} > 5.1 \times 10^6 \text{ GeV} \\ \text{BR}(\tau \rightarrow e a) &< 7.6 \times 10^{-4} \text{ (90\% CL)} \Rightarrow f_a / C_{e\tau}^{V,A} > 4.0 \times 10^6 \text{ GeV} \end{aligned}$$

Present limits on $\tau \rightarrow e a$, $\tau \rightarrow \mu a$ (invisible a)

A challenging search:

• **NEW! Belle 2025** (800 fb^{-1})

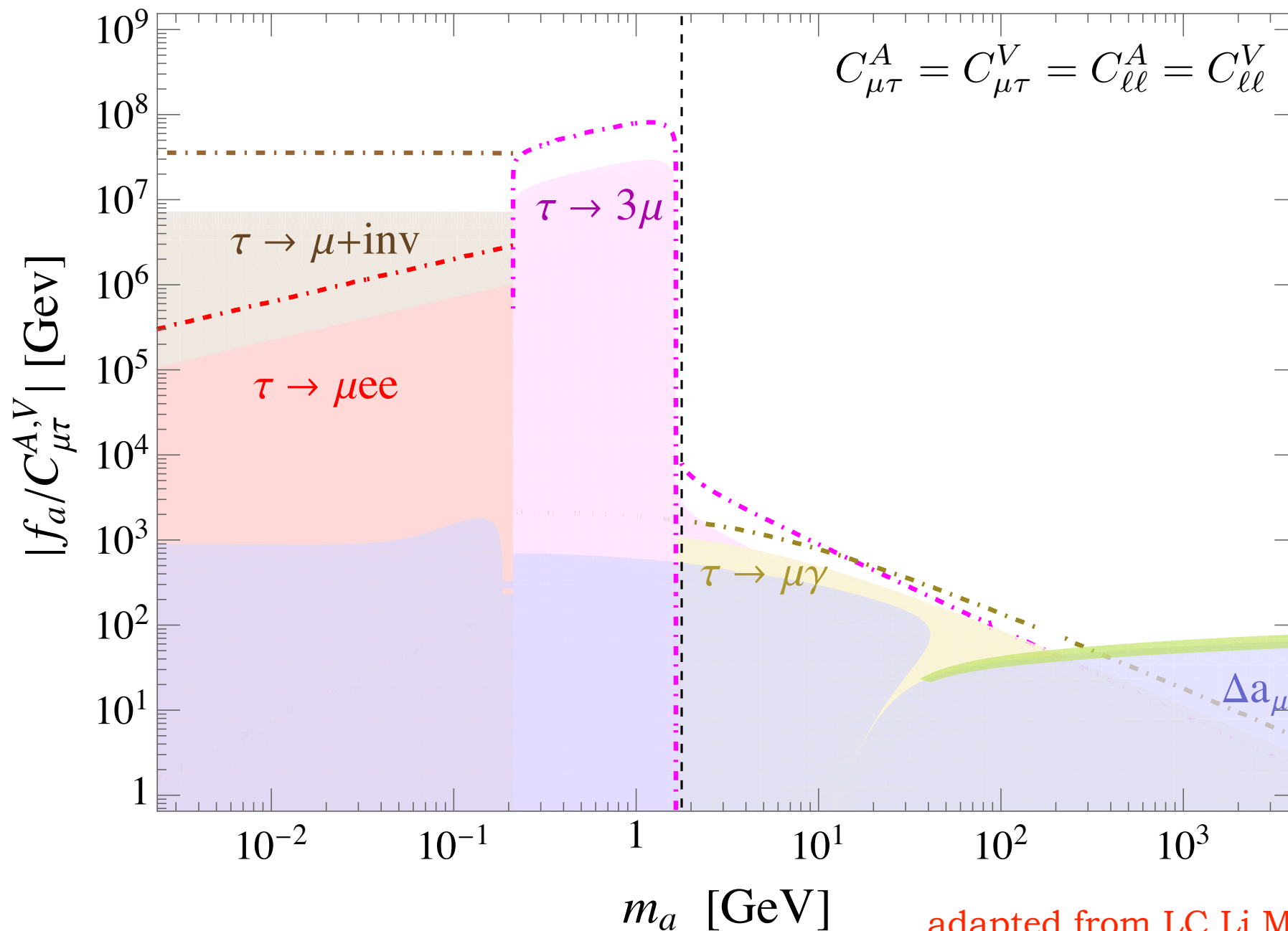
→ talk by Jing-Ge Shiu



$$m_a \approx 0 : \text{BR}(\tau \rightarrow e a) < 7.6 \times 10^{-4} \text{ (90\% CL)} \Rightarrow f_a / C_{e\tau}^{V,A} > 4.0 \times 10^6 \text{ GeV}$$

ALP-mediated tau LFV

If the ALP is not that light nor long-lived, it can decay on-shell
(or off-shell) back to leptons: $\tau \rightarrow \mu a^{(*)} \rightarrow \mu \ell \ell$
(or mediate radiative processes)

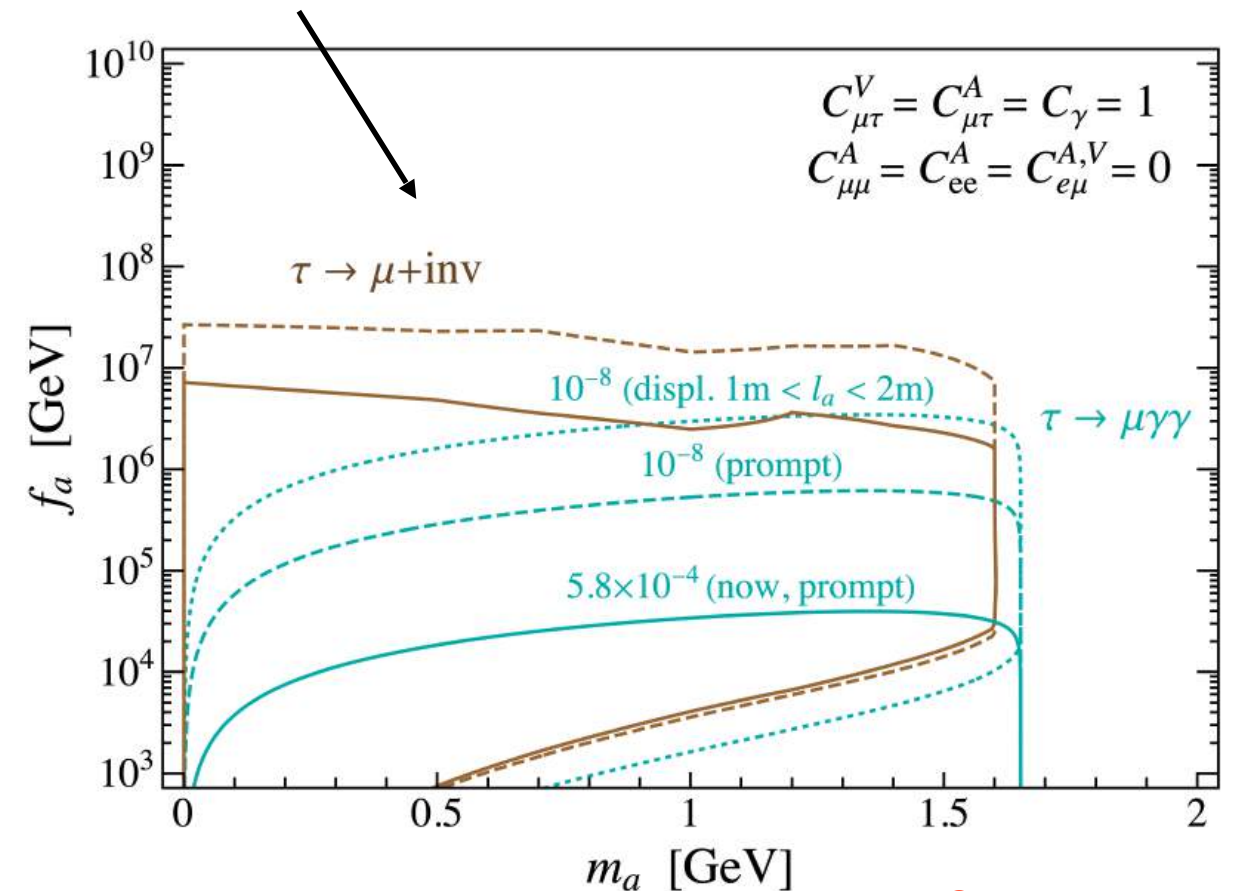
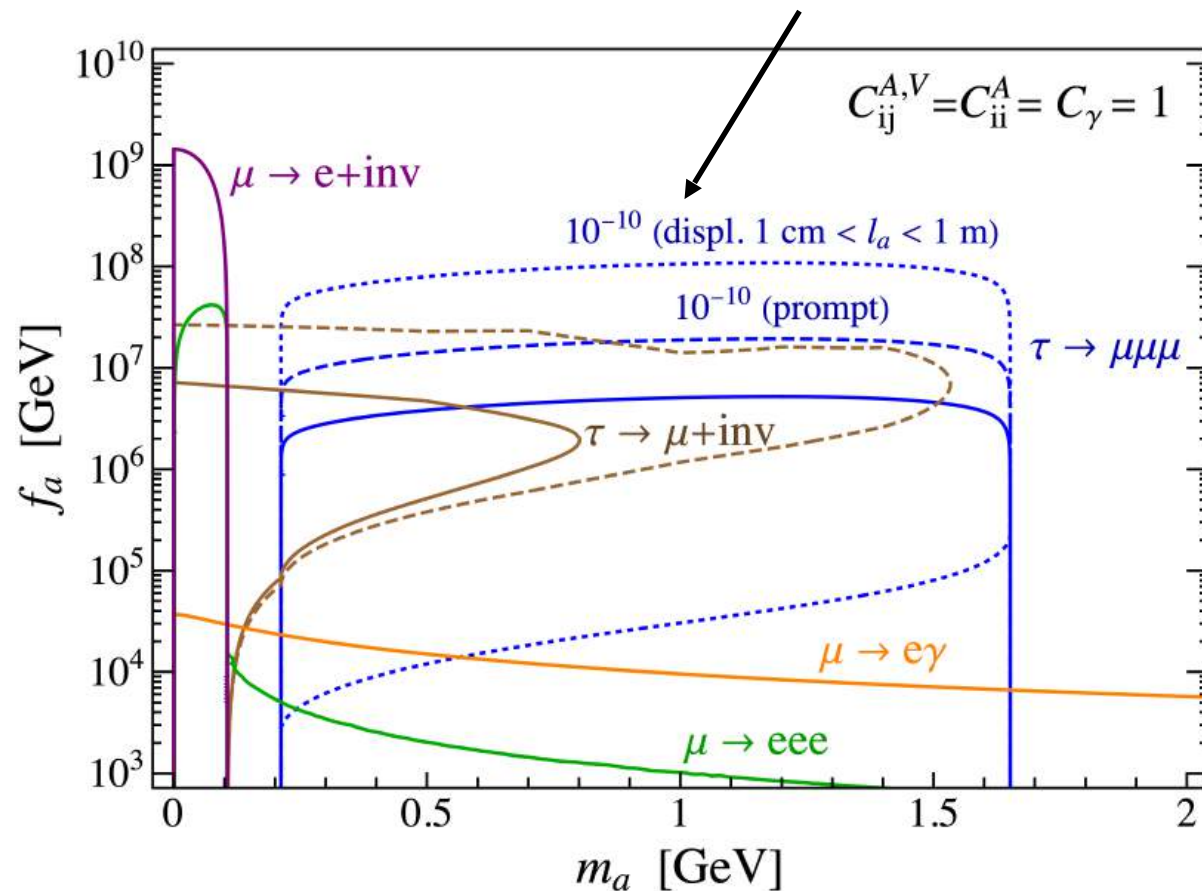


adapted from [LC Li Mukherjee Yang '24](#)
(see also [Cornella Paradisi Sumensari '19](#))

ALP-mediated tau LFV

If the ALP is not that light nor long-lived, it can decay on-shell
(or off-shell) back to leptons: $\tau \rightarrow \mu a^{(*)} \rightarrow \mu \ell \ell$
(or mediate radiative processes)

Belle II prospects for long-lived/displaced ALPs



LC to appear

Interplay between visible, invisible, and displaced searches!

What about Dark Matter?

- Obvious requirement, cosmological lifetime

$$\frac{H_0}{\Gamma_{\text{tot}}} = H_0 \tau_a > 1$$

- More stringent bound: extragalactic background light (from $a \rightarrow \gamma\gamma$)

Coupling to photons ($m_a \ll m_{\ell_i}$) : $\mathcal{L}_{\text{eff}} = E_{\text{UV}} \frac{\alpha_{\text{em}}}{4\pi} \frac{a}{f_a} F \tilde{F}$

depends on UV completion,
e.g. anomaly coefficient (QCD axion: $E_{\text{UV}} = E/2N$)

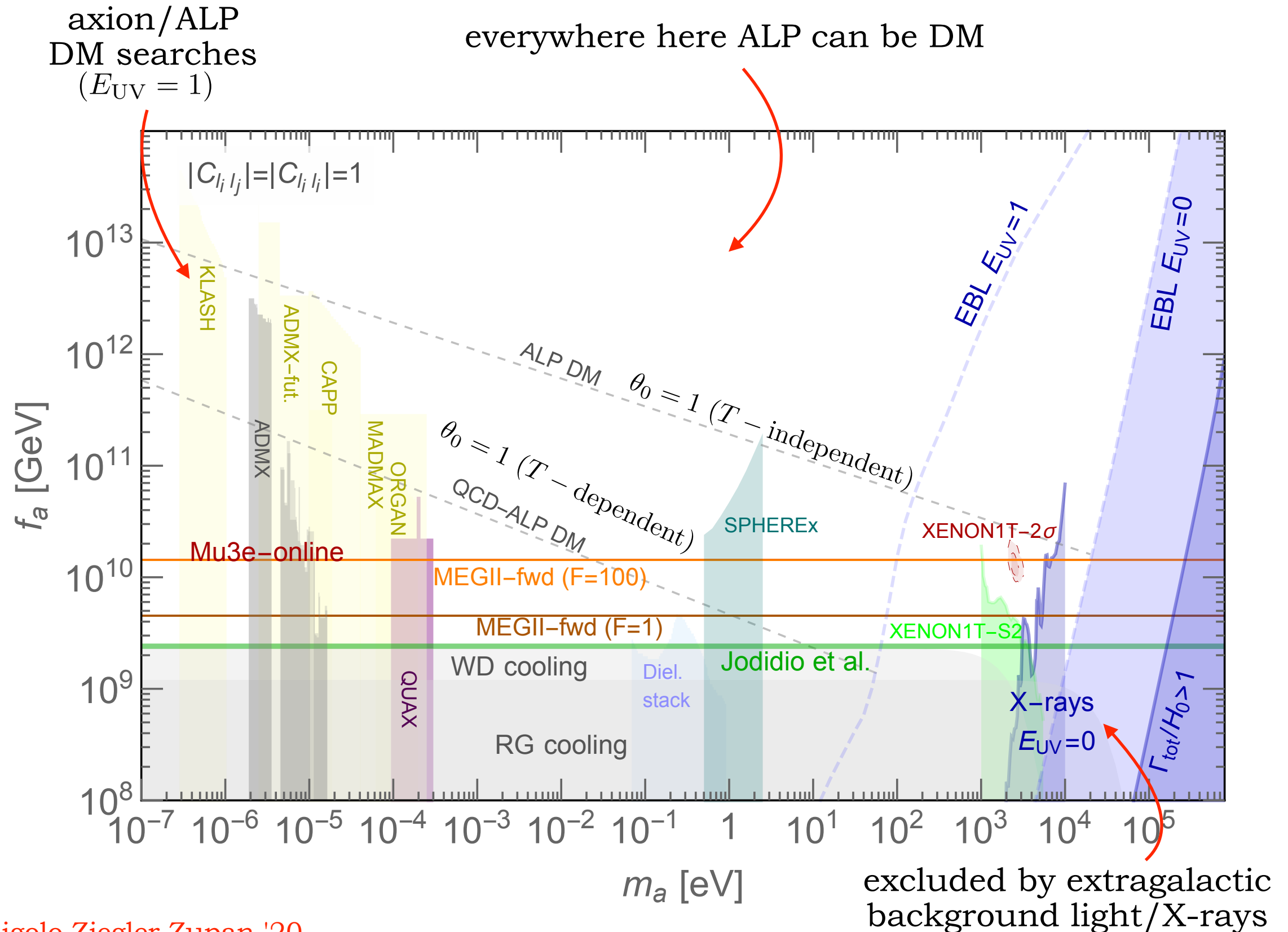
- Production: misalignment mechanism

$$\Omega_a^{T\text{-indep.}} h^2 = 0.12 \times 10^{-2} \sqrt{\frac{m_a}{\text{eV}}} \left(\frac{f_a}{10^{10} \text{GeV}} \right)^2 \left(\frac{\theta_0}{\pi} \right)^2 \left(\frac{90}{g_*(T_{\text{osc}})} \right)^{1/4}$$

misalign. angle

it can be enhanced if ALP mass suppressed at
finite temperature (e.g. QCD axion)

ALP dark matter



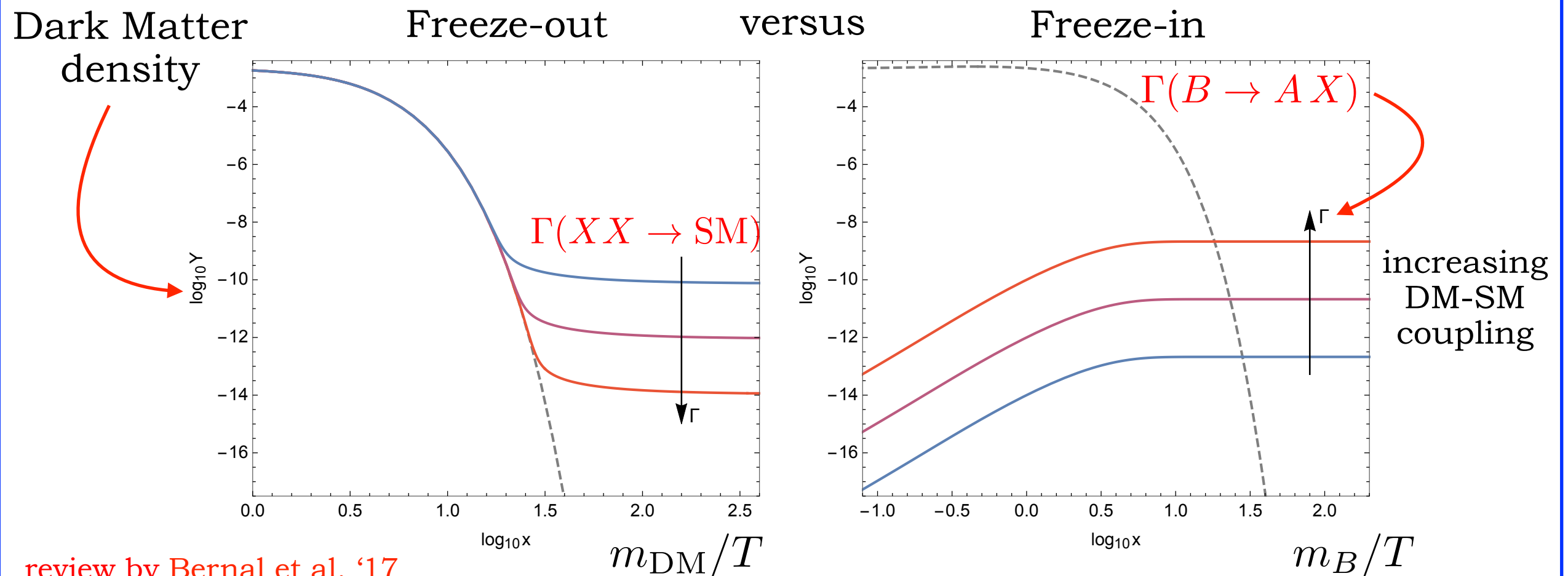
LC Redigolo Ziegler Zupan '20

LFV dark matter production?

What if $\mu \rightarrow ea$, $\tau \rightarrow \mu a$ also produce DM ALPs in the early universe, via the *freeze-in* mechanism? [Panci Redigolo Schwetz Ziegler '22](#)

Freeze-in: a production mechanism for DM that was never in thermal equilibrium with the Standard Model bath (because too *feebly-coupled*), but can be produced via scattering or decays of bath particles

[Hall Jedamzik March-Russell West '09](#)



LFV dark matter production?

What if $\mu \rightarrow ea$, $\tau \rightarrow \mu a$ also produce DM ALPs in the early universe, via the *freeze-in* mechanism?

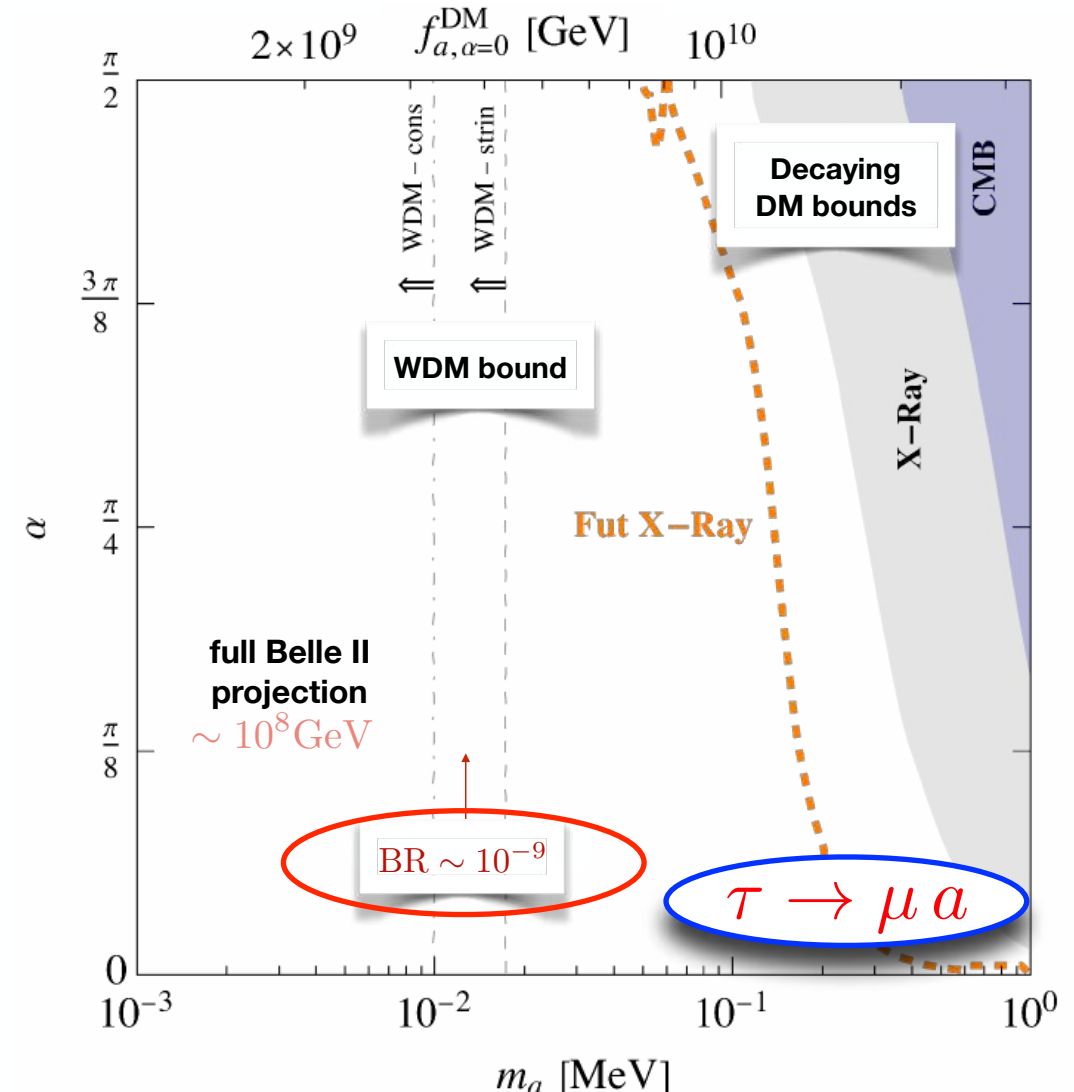
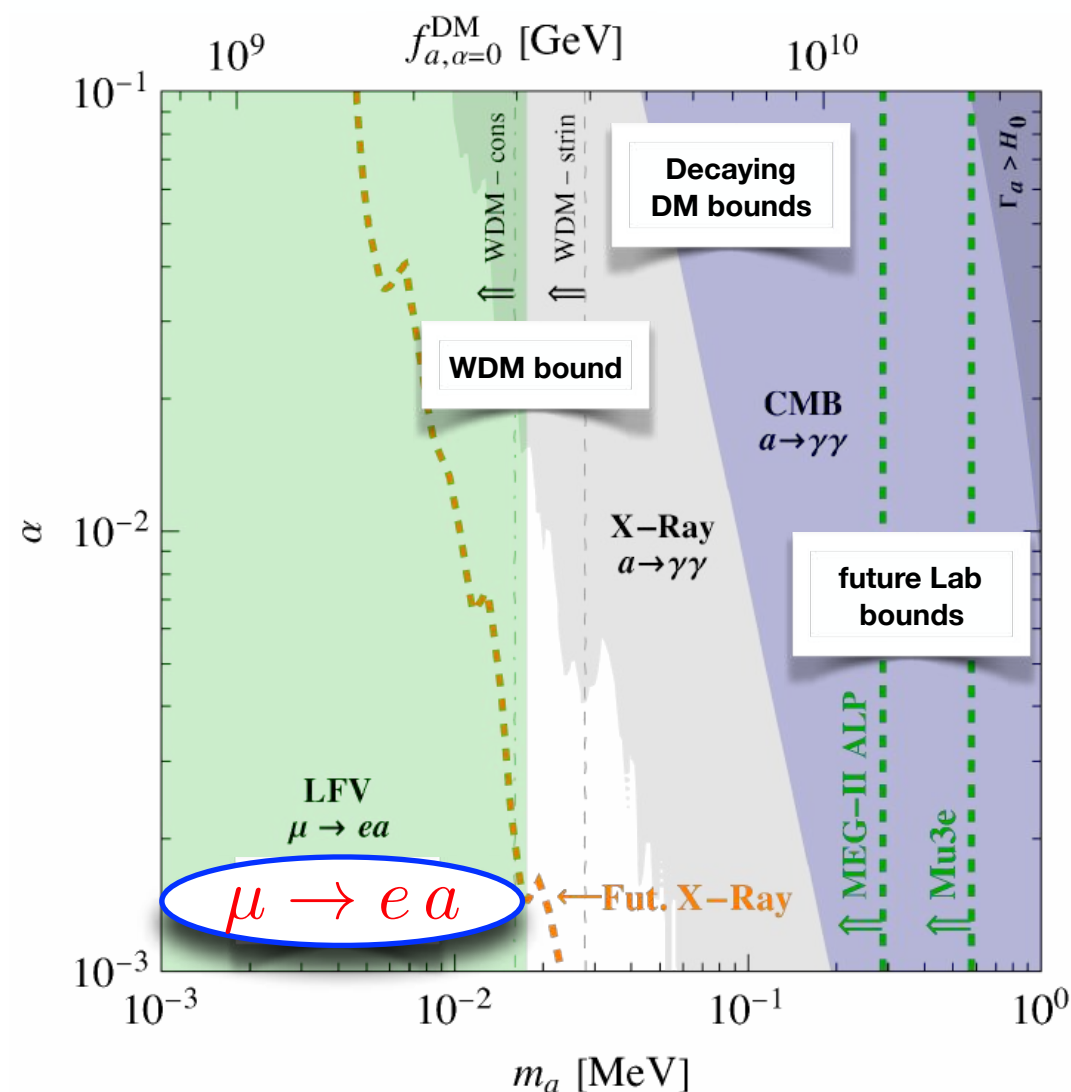
$$\mathcal{L}_a = \frac{\partial_\nu a}{2f_a} [\cos \alpha \cdot \bar{\tau} \gamma^\nu \gamma_5 \mu + \sin \alpha \cdot \bar{\tau} \gamma^\nu \gamma_5 \tau - \sin \alpha \cdot \bar{\mu} \gamma^\nu \gamma_5 \mu] - \frac{1}{2} m_a^2 a^2$$

overall coupling strength

relative coupling strength

ALP mass

ALP mass / couplings fixed by matching the observed DM abundance:



courtesy of R. Ziegler, based on [Panci Redigolo Schwetz Ziegler '22](#)

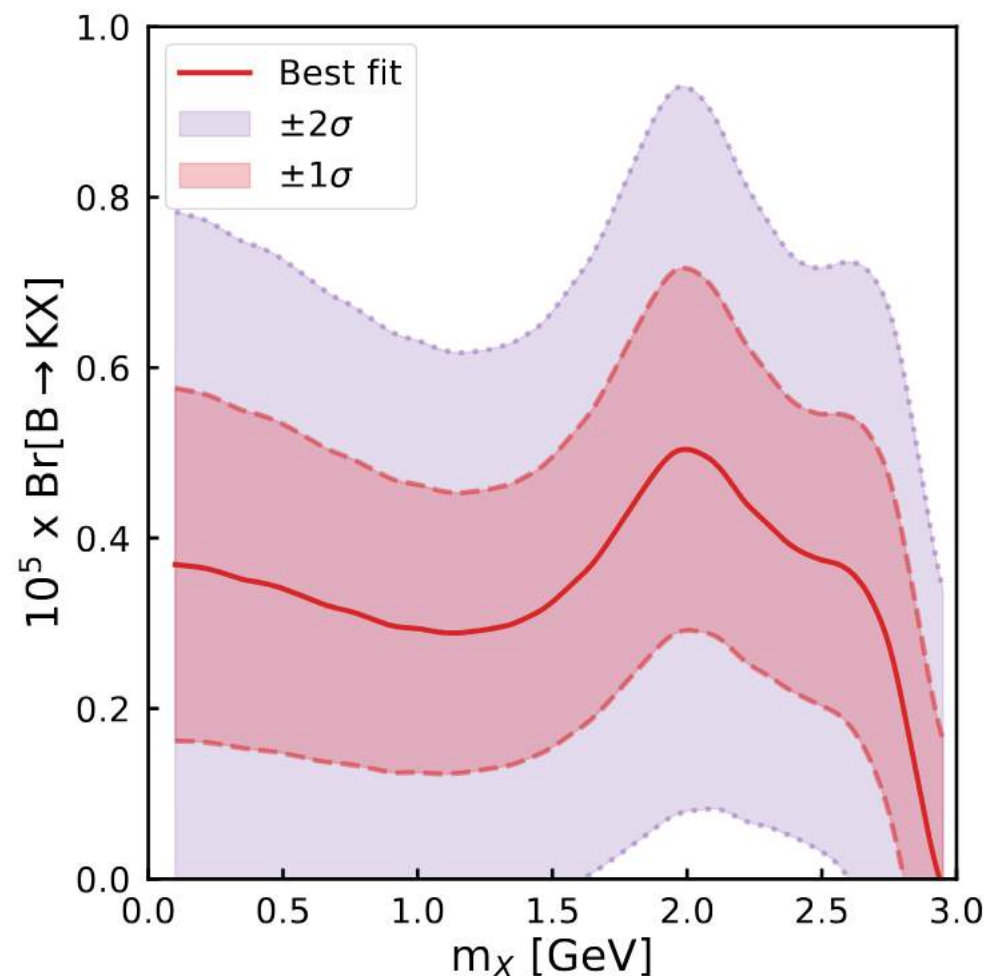
ALP portal to DM for the Belle II excess

Belle II observed a $\sim 2.7\sigma$ excess over the SM prediction for $B^+ \rightarrow K^+ \nu \bar{\nu}$

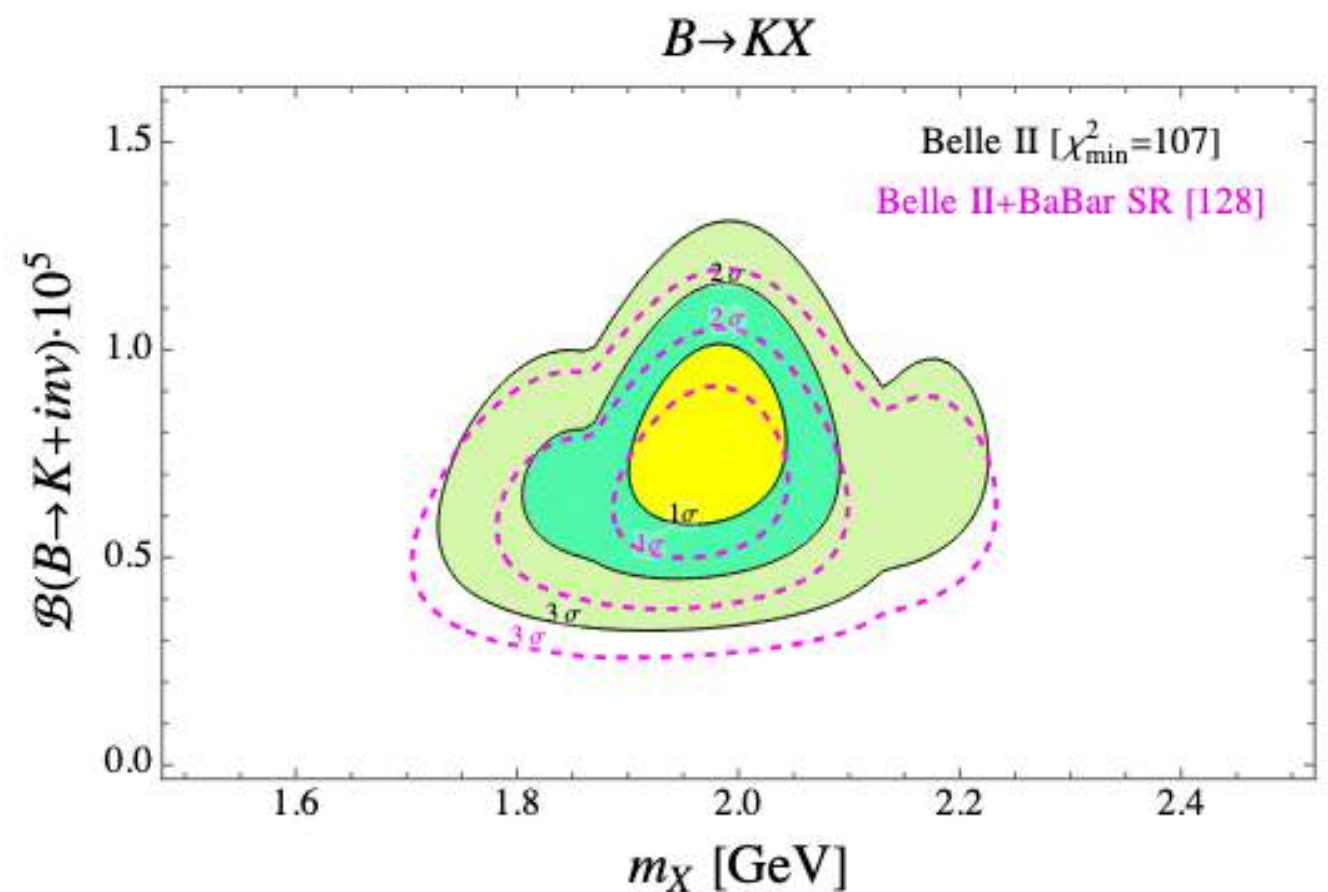
[Belle II '23](#)

→ talk by Roberta Volpe

Despite some tension with previous limits from BaBar,
the contribution of a two-body decay into an invisible ~ 2 GeV boson
is somewhat preferred to the SM alone



[Altmannshofer et al. '23](#)



[Fridell et al. '23](#)

ALP portal to DM for the Belle II excess

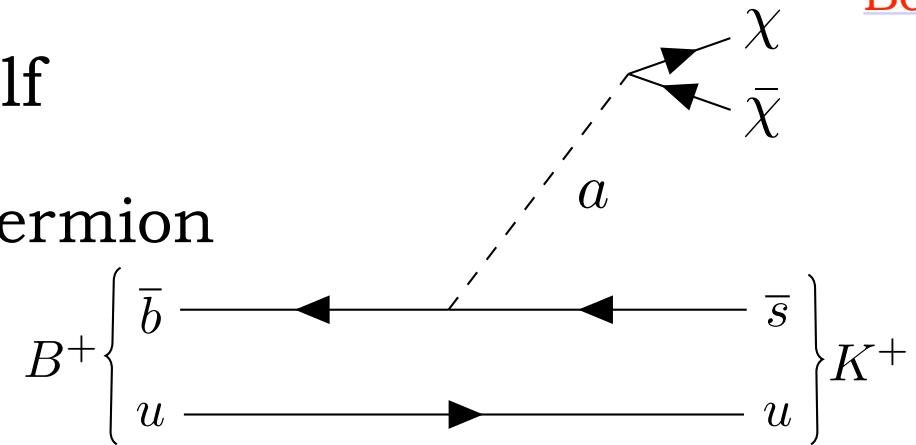
Belle II observed a $\sim 2.7\sigma$ excess over the SM prediction for $B^+ \rightarrow K^+ \nu \bar{\nu}$

Belle II '23

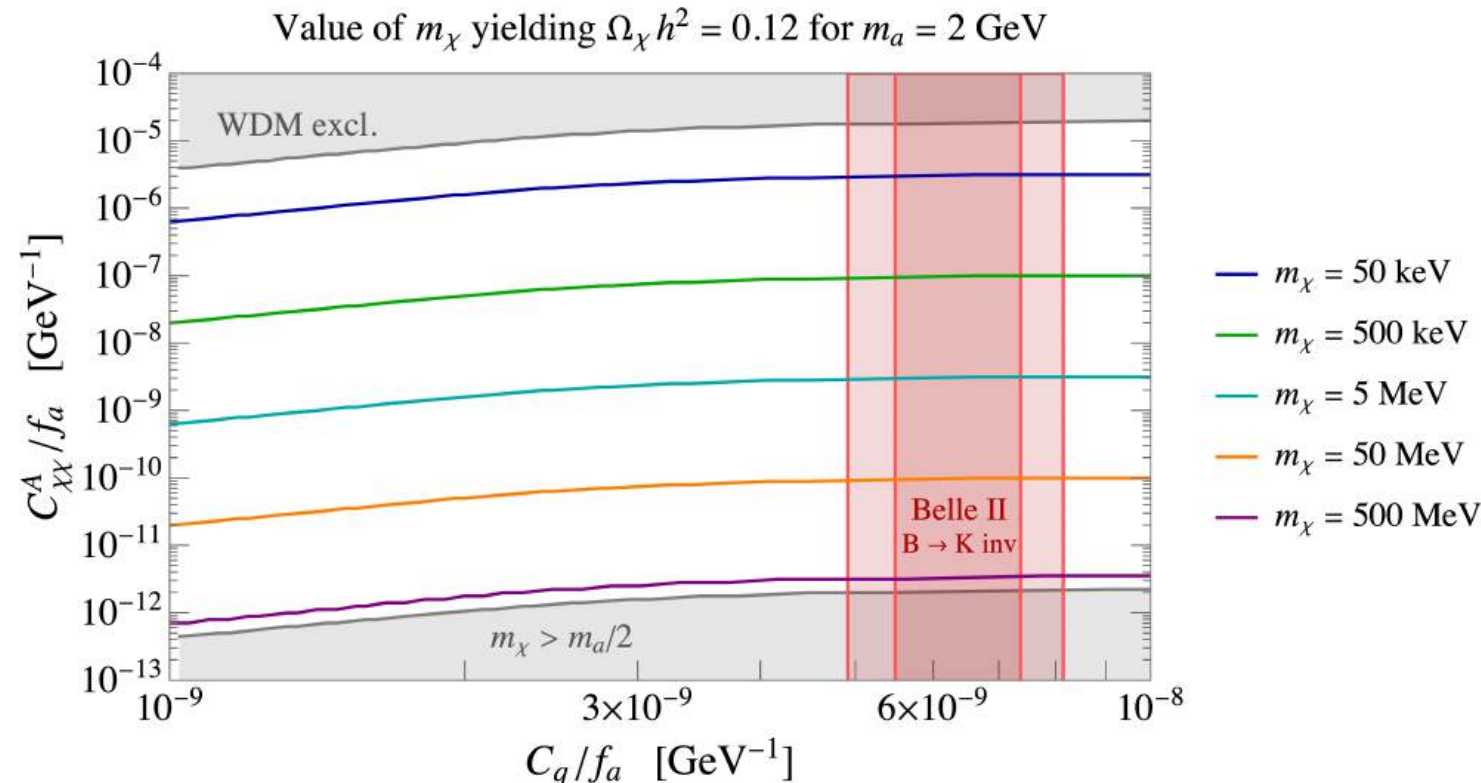
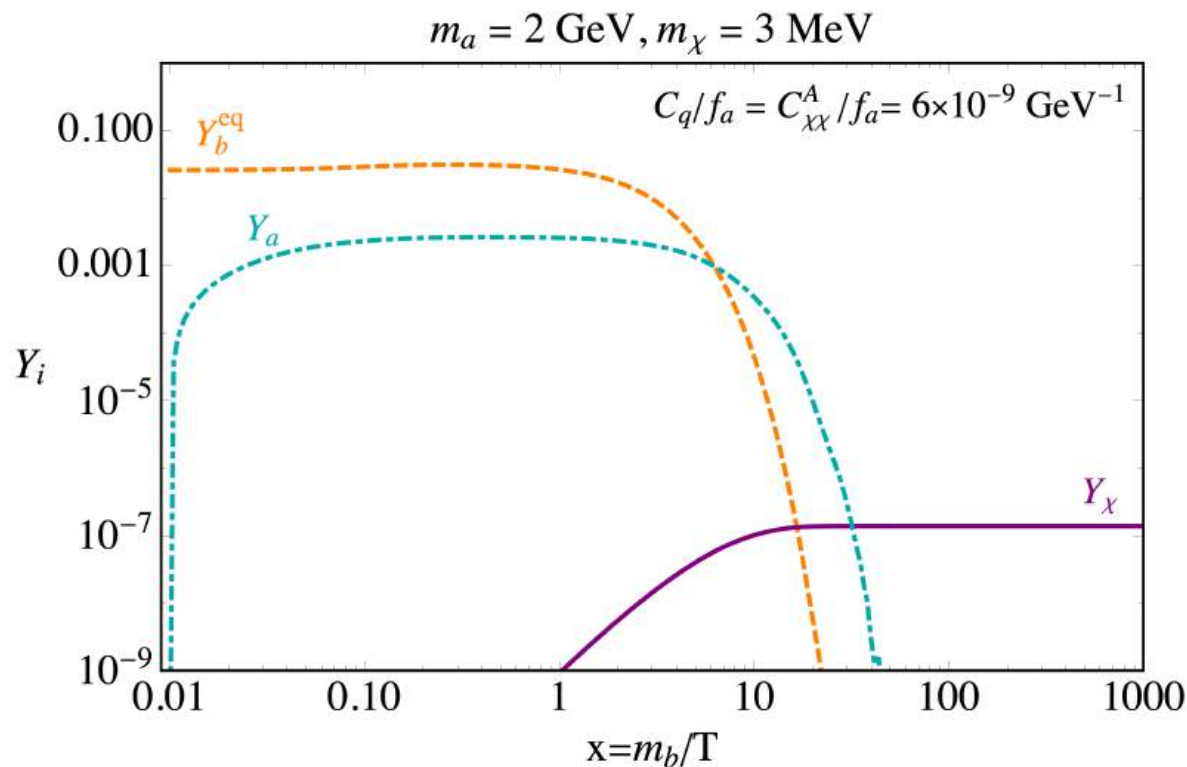
A 2 GeV ALP can not be dark matter itself
but can act as portal to DM:

$$\mathcal{L}_{a\chi\chi} = \frac{\partial_\mu a}{2f_a} C_{\chi\chi}^A \bar{\chi} \gamma^\mu \gamma_5 \chi$$

dark fermion



ALP decays into light fermion DM can explain the excess at the same time yielding 100% of the observed DM abundance via freeze-in:



LC Li Mukherjee Schmidt '25

Summary

A wide class of new physics models entails light new physics with flavour-violating couplings to SM fermions

Past (upcoming) searches for muon/kaon decays into invisible ALPs can test new physics scales up to $10^{10}/10^{12}$ GeV

Interesting complementary to tau and B decays, as well as astrophysical/cosmological bounds

Models of light dark matter (accounting for 100% of the measured density) can give rise to observable signals in lepton, kaon or bottom decays

Huge room for improvement over old limits: next generation flavour experiments may discover light new physics

Cảm ơn!
Thanks!
Questions?



Additional slides

Past searches: $\mu \rightarrow e \gamma a$

- Crystal Box 1988

PHYSICAL REVIEW D

VOLUME 38, NUMBER 7

1 OCTOBER 1988

Search for rare muon decays with the Crystal Box detector

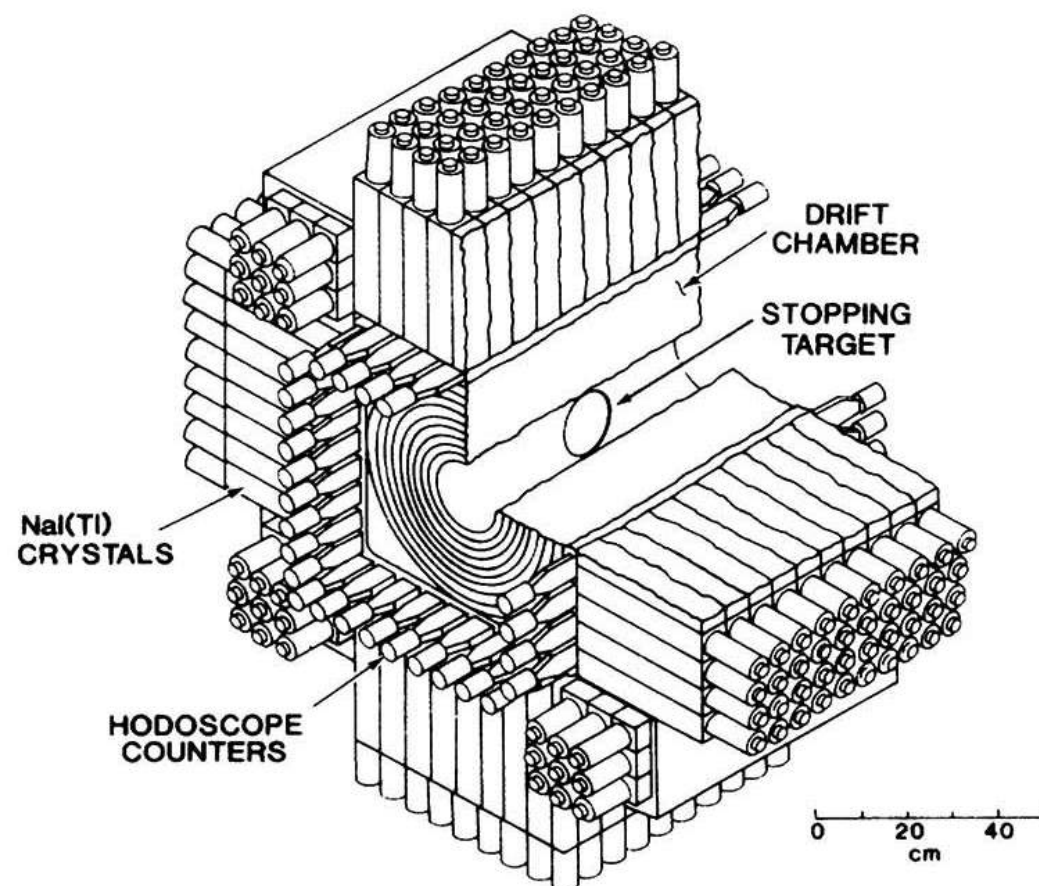


TABLE I. Types of events generated with the Monte Carlo program.

Process	Trigger
$\mu^+ \rightarrow e^+ \gamma$	$e-\gamma$
$\mu^+ \rightarrow e^+ \gamma \nu \bar{\nu}$	$e-\gamma, 1-\gamma$
$\mu^+ \rightarrow e^+ \gamma \gamma$	$e-\gamma-\gamma, e-\gamma$
$\mu^+ \rightarrow e^+ e^+ e^-$	$e-e-e$
$\mu^+ \rightarrow e^+ e^+ e^- \nu \bar{\nu}$	$e-e-e$
$\mu^+ \rightarrow e^+ \nu \bar{\nu}$	$1-e$
$\mu^+ \rightarrow e^+ \gamma f$ ($f = \text{familon}$)	$e-\gamma$
$\pi^0 \rightarrow \gamma \gamma$	$\gamma-\gamma, 1-\gamma$
$\pi^- p \rightarrow n \gamma$	$1-\gamma$

Past searches: $\mu \rightarrow e \gamma a$

- Crystal Box 1988

Analysis for massless familon $m_a \approx 0$
(with 1.4×10^{12} stopped μ^+) yields:

$$\text{BR}(\mu \rightarrow e a \gamma) < 1.1 \times 10^{-9} \quad (90\% \text{ CL})$$

$$\text{BR}(\mu \rightarrow e a \gamma) \approx \frac{\alpha_{\text{em}}}{2\pi} \mathcal{I}(x_{\min}, y_{\min}) \text{BR}(\mu \rightarrow e a) \quad \text{Hirsch et al. '09}$$

$$\mathcal{I}(x_{\min}, y_{\min}) = \int_{x_{\min}, y_{\min}}^1 dx dy \frac{(x-1)(2-xy-y)}{y^2(1-x-y)}$$

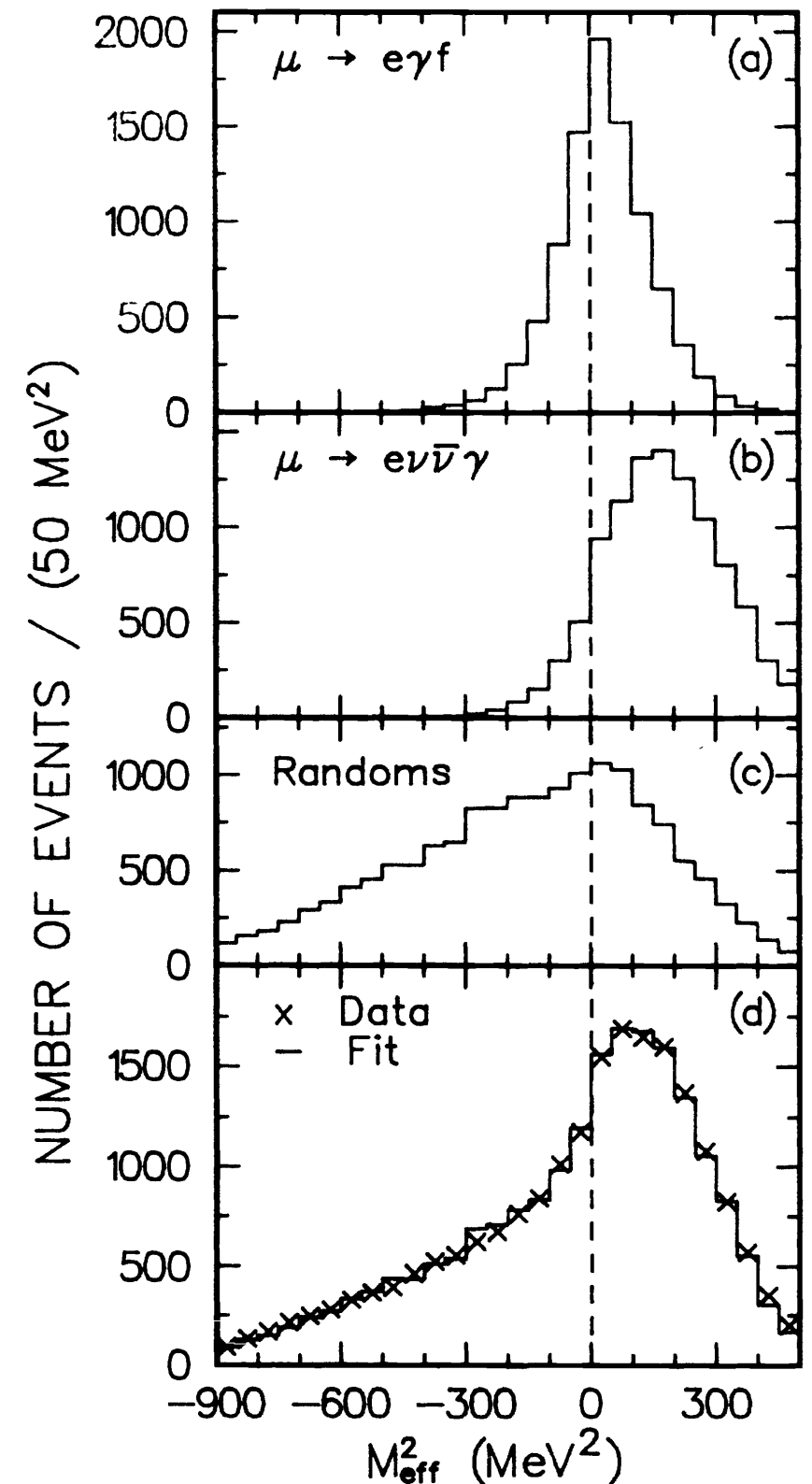
$$x = 2E_e/m_\mu \quad y = 2E_\gamma/m_\mu$$

Crystal Box energy thresholds:

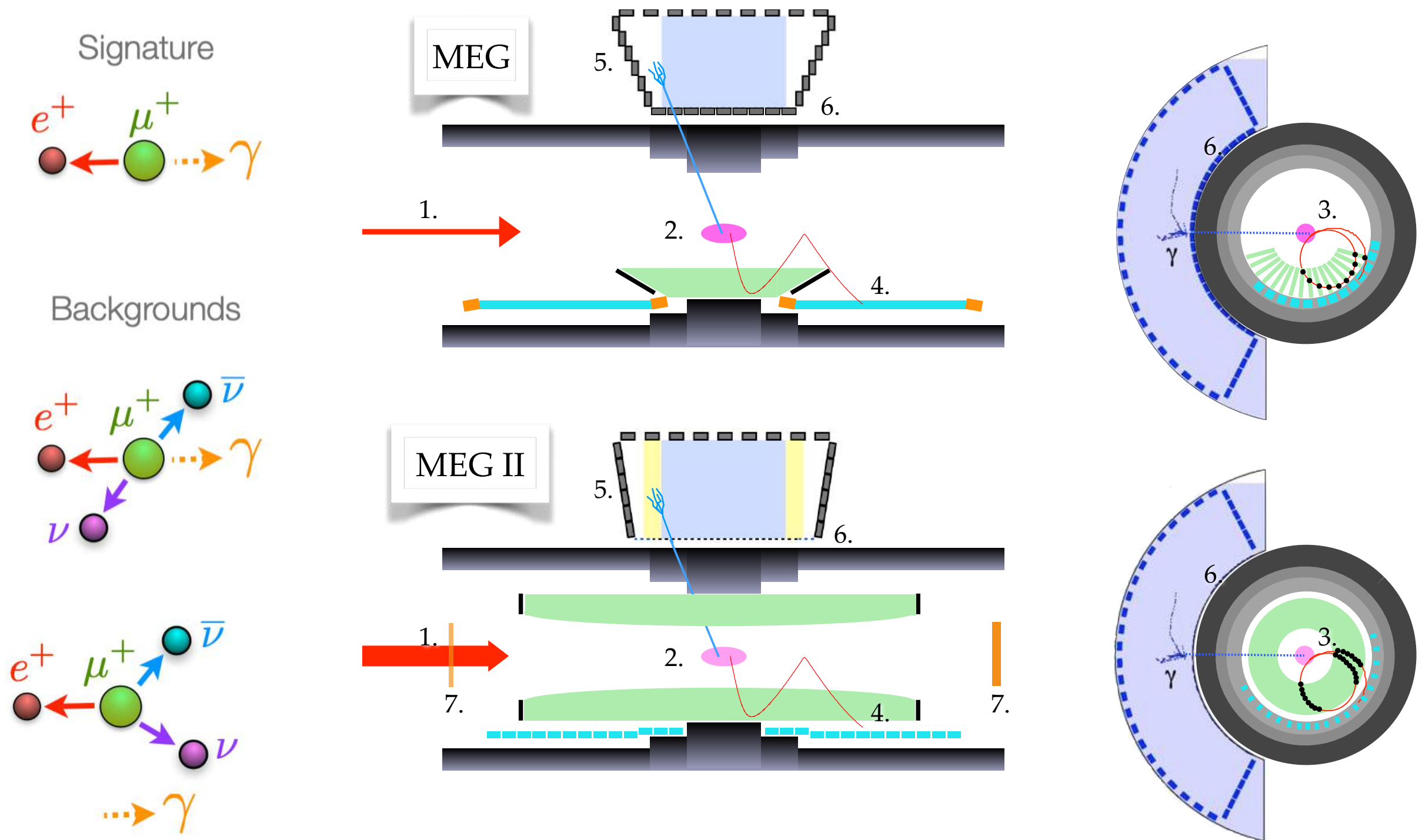
$$E_e > 38 - 43 \text{ MeV}, \quad E_\gamma > 38 \text{ MeV} \quad \Rightarrow \quad x_{\min} = 0.72 - 0.81, \quad y_{\min} = 0.72$$

$$\Rightarrow F_{e\mu} > (5.1 - 8.3) \times 10^8 \text{ GeV}$$

weaker but independent
of V/A nature of the couplings



Future prospects: MEG II

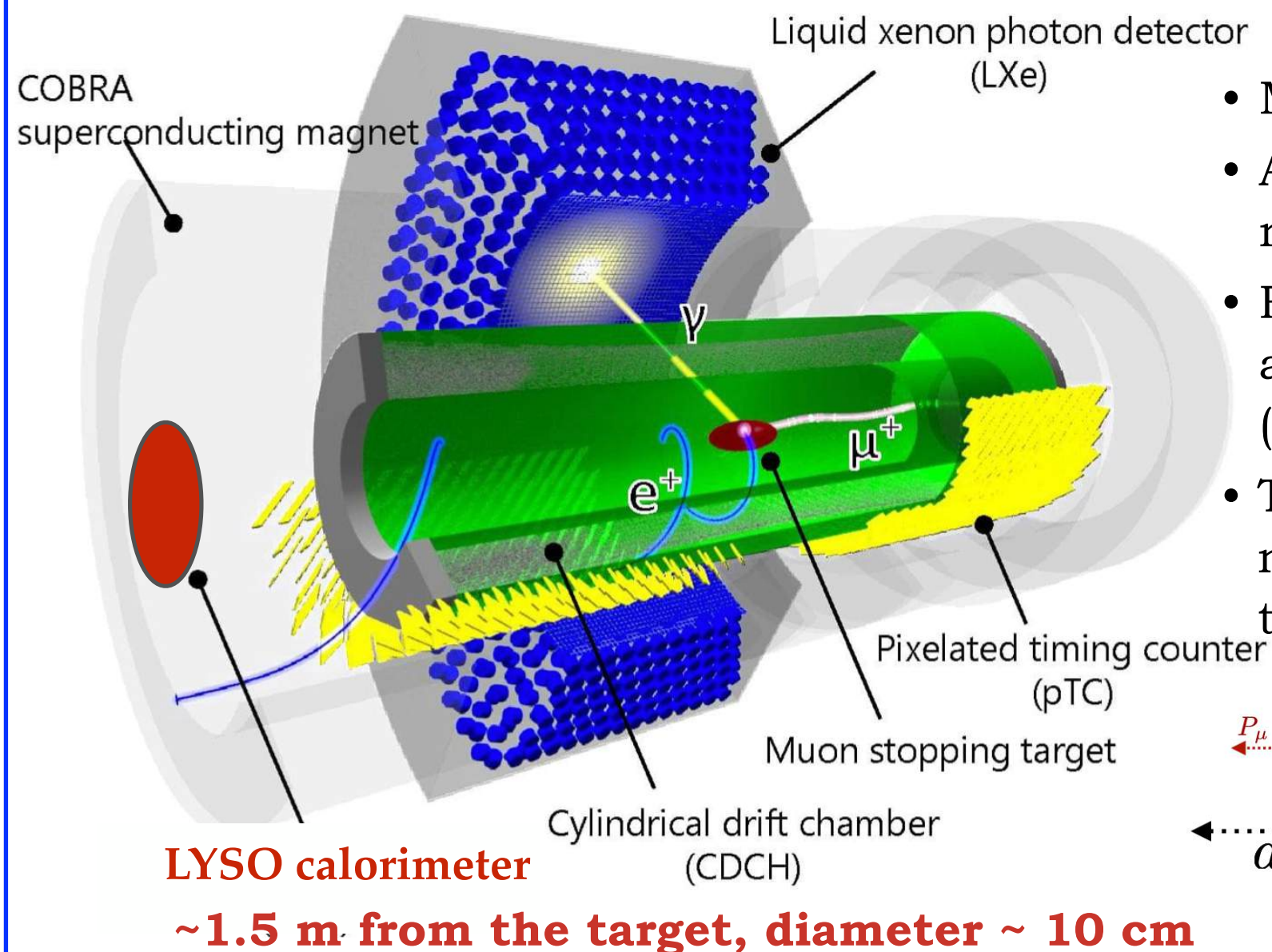


Future prospects: MEG II

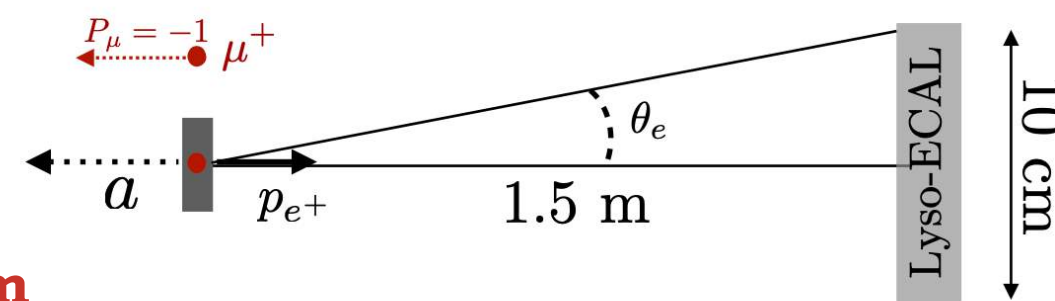
LC Redigolo Ziegler Zupan '20

- Prospect at MEG II for $\mu \rightarrow e a$

What about a Jodidio-like search at MEG II for $m_a \approx 0$ with a *forward calorimeter*?
We propose a modified setup of MEG II (“MEGII-fwd”) and ~2 weeks dedicated run
idea from discussions with A. Papa and G. Signorelli, thanks!



- Muon beam already polarized
- A suitable magnetic field can reduce depolarization effects
- Reconfiguring the field we can also increase the acceptance (“*magnetic focusing*” up to $F \sim 100$)
- Two weeks of run after MEG II main run are enough to improve the bound (even with $F=0$)



Future prospects: MEG II

LC Redigolo Ziegler Zupan '20

• Prospect at MEG II for $\mu \rightarrow e a$

What about a Jodidio-like search at MEG II for $m_a \approx 0$ with a *forward calorimeter*?
We propose a modified setup of MEG II (“MEGII-fwd”) and ~2 weeks dedicated run
idea from discussions with A. Papa and G. Signorelli, thanks!

Our estimate of the sensitivity of a dedicate run (2 weeks with $10^8 \mu^+/\text{s}$):

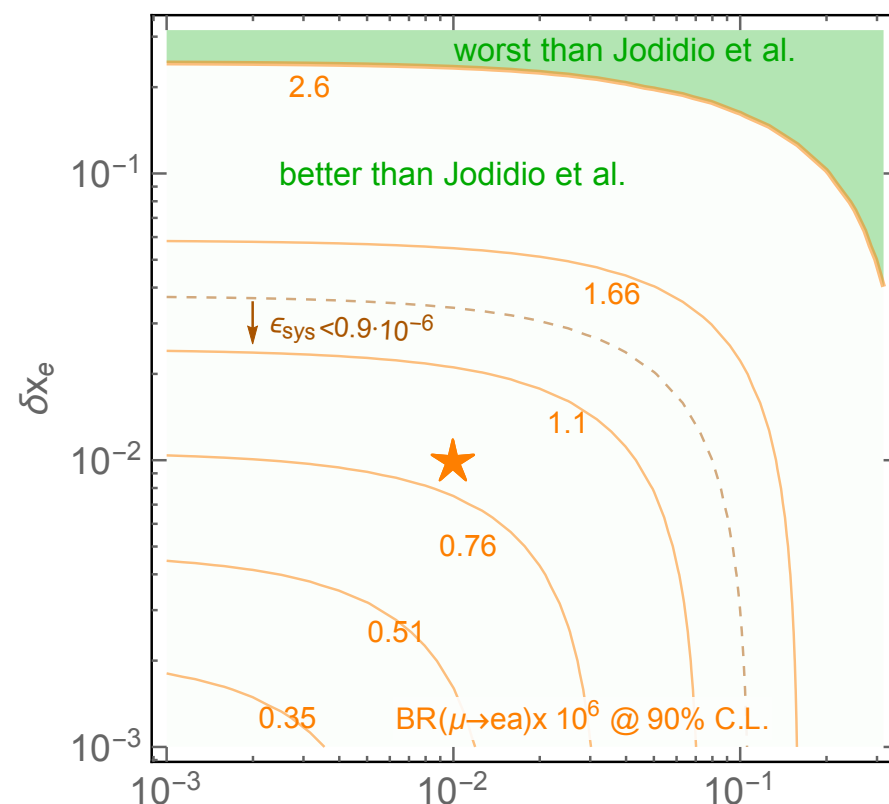
MEGII-fwd : $10^{14} \mu^+$

magnetic
focusing

$F = 0$

no focusing

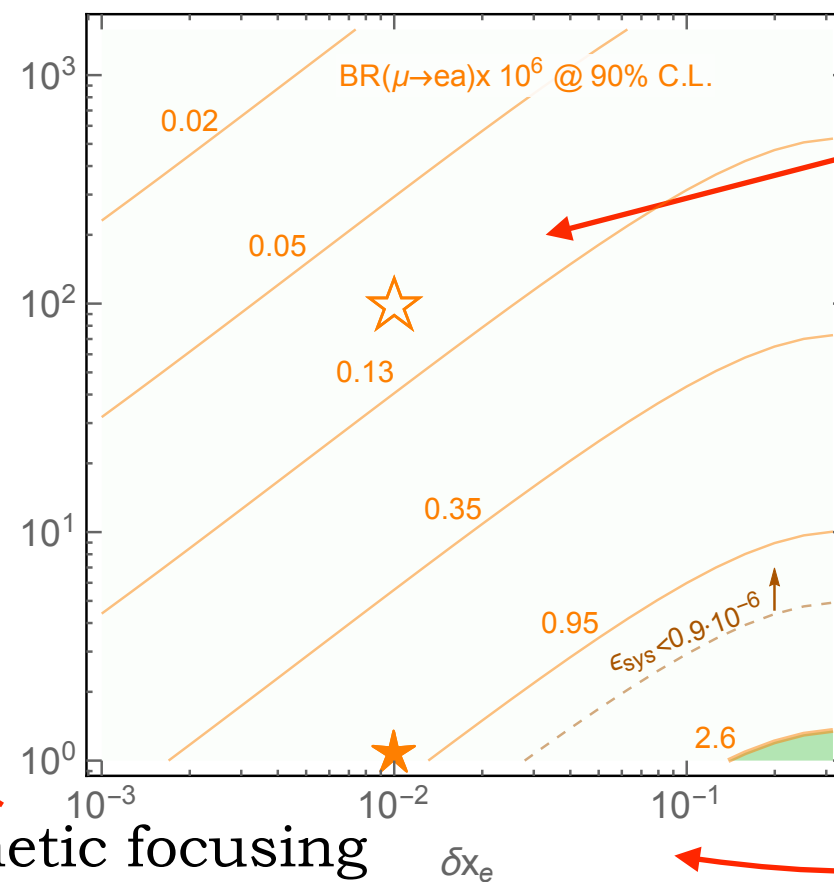
$\delta x_e = \langle P_\mu \rangle + 1$



polarization

$\langle P_\mu \rangle + 1$

magnetic focusing



$F = 100$
 $\text{BR} \sim 10^{-7}$

Positron
momentum
resolution

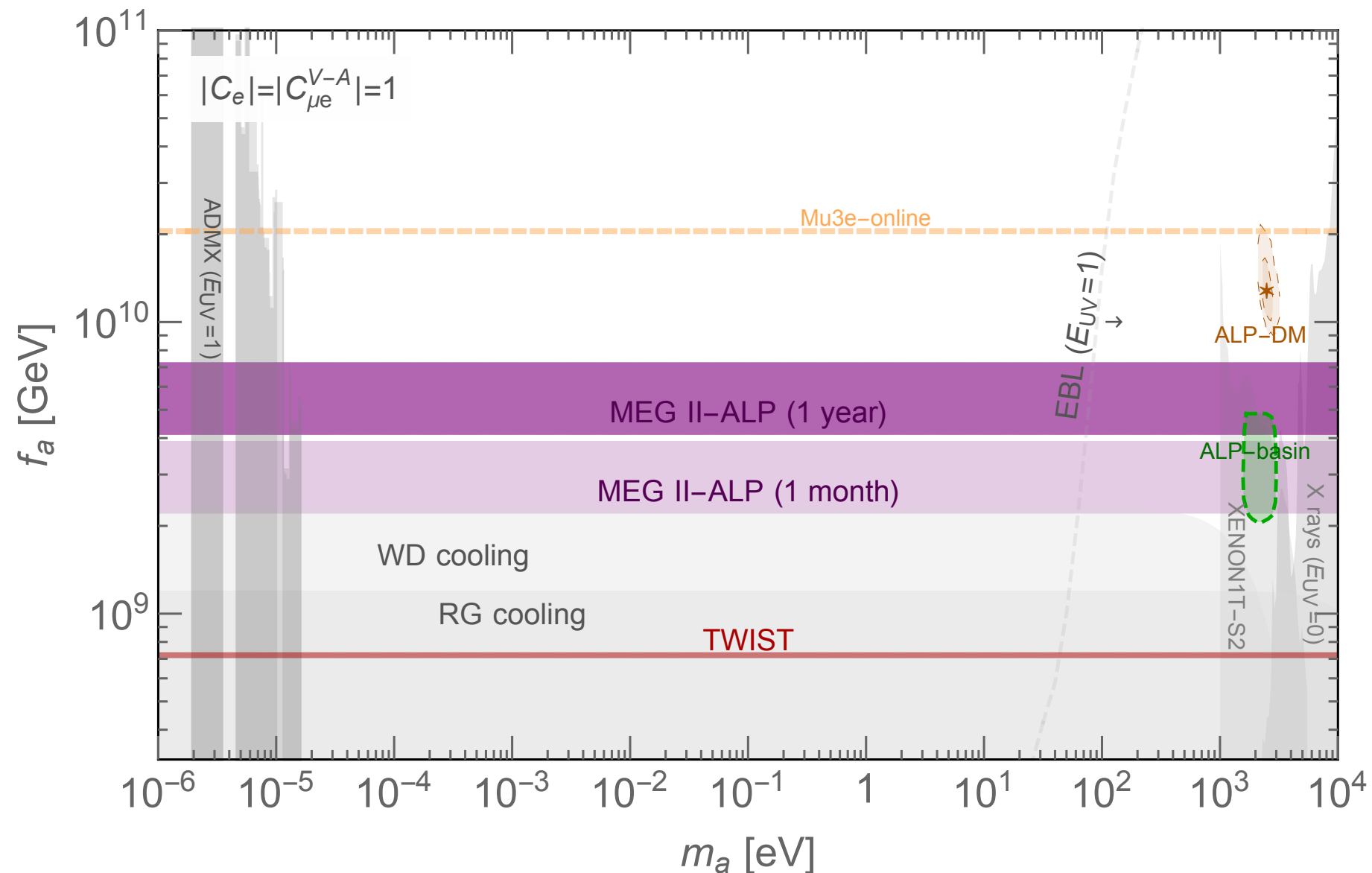
$$x_e = \frac{2p_e}{m_\mu}$$

Future prospects: MEG II

- Prospect at MEG II for $\mu \rightarrow e a \gamma$

Jho Knapen Redigolo '22

Search sensitive to V-A couplings too, requires a dedicated trigger:

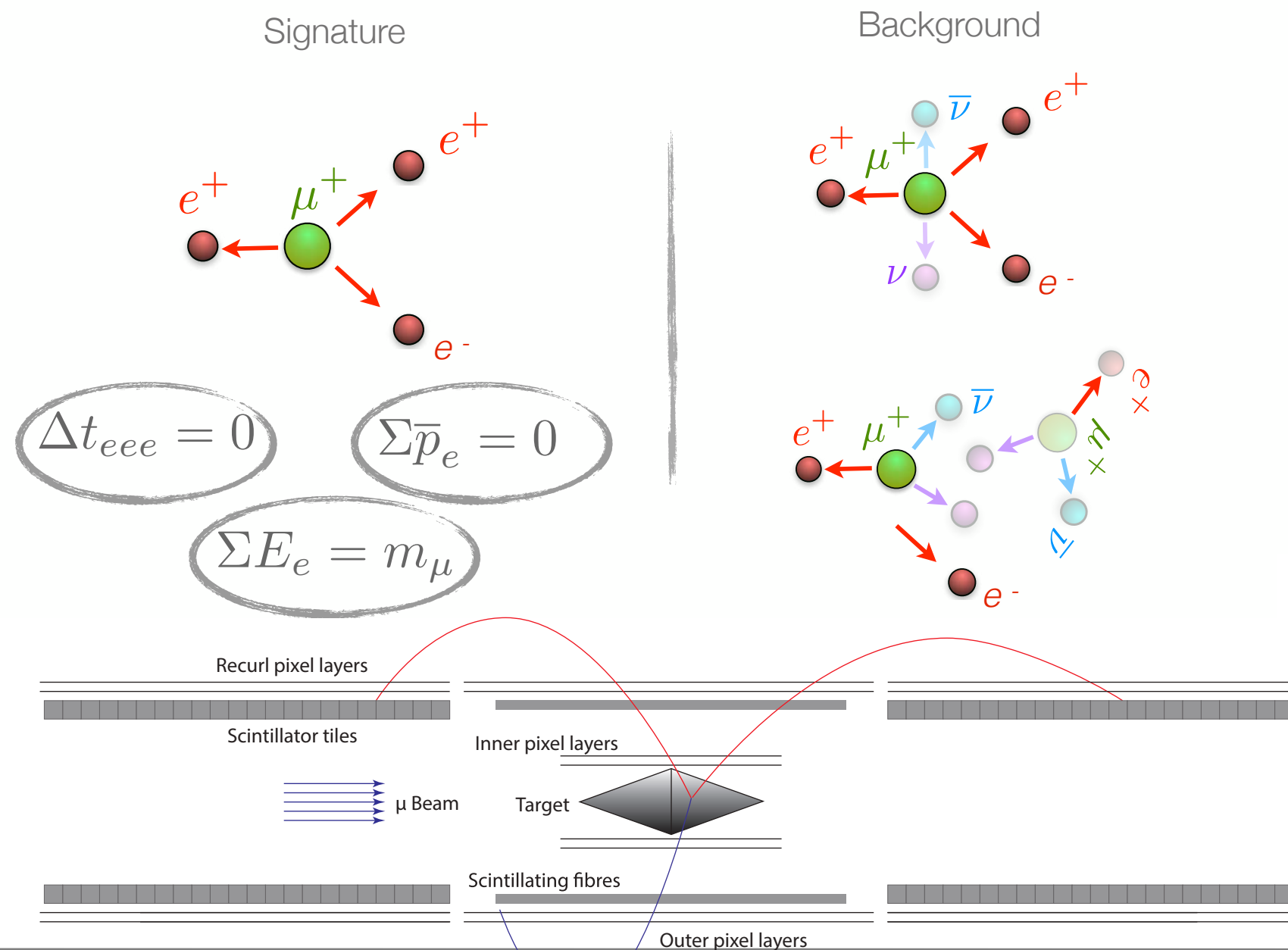


Future prospects: Mu3e

Mu3e: The $\mu^+ \rightarrow e^+ e^+ e^-$ search

slide borrowed from A. Papa

- The Mu3e experiment aims to search for $\mu^+ \rightarrow e^+ e^+ e^-$ with a sensitivity of $\sim 10^{-15}$ (Phase I) up to down $\sim 10^{-16}$ (Phase II). Previous upper limit $\text{BR}(\mu^+ \rightarrow e^+ e^+ e^-) \leq 1 \times 10^{-12}$ @90 C.L. by SINDRUM experiment)
- Observables (E_e , t_e , vertex) to characterize $\mu \rightarrow eee$ events

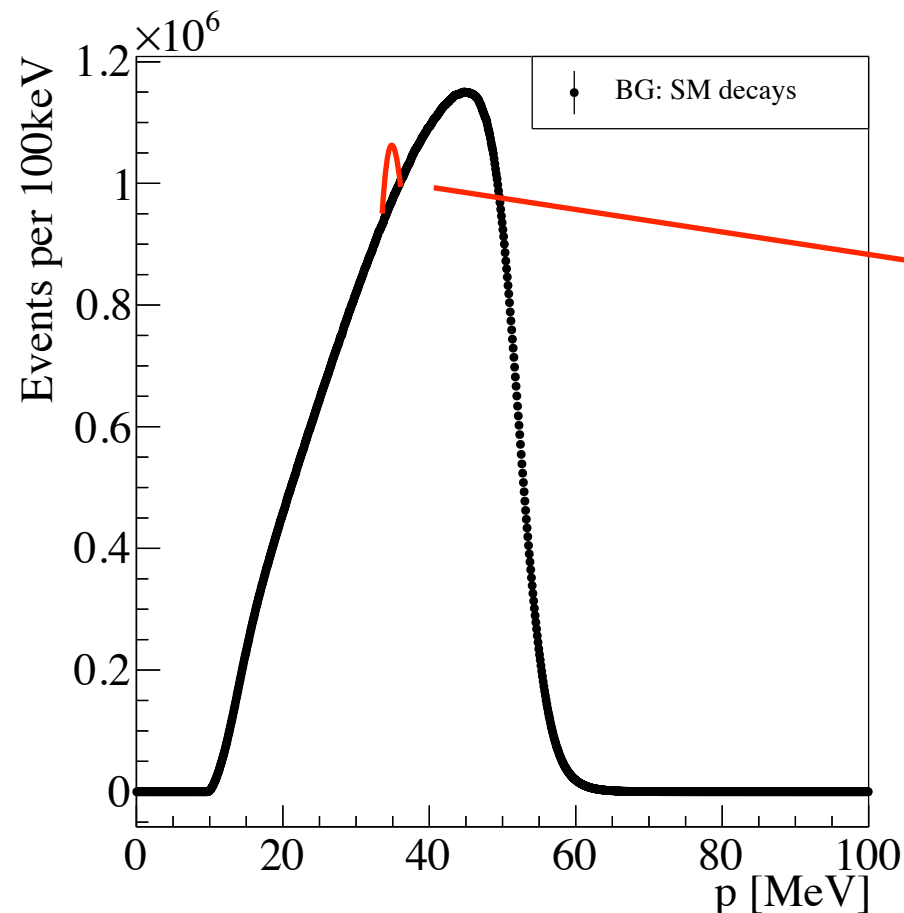


Future prospects: Mu3e

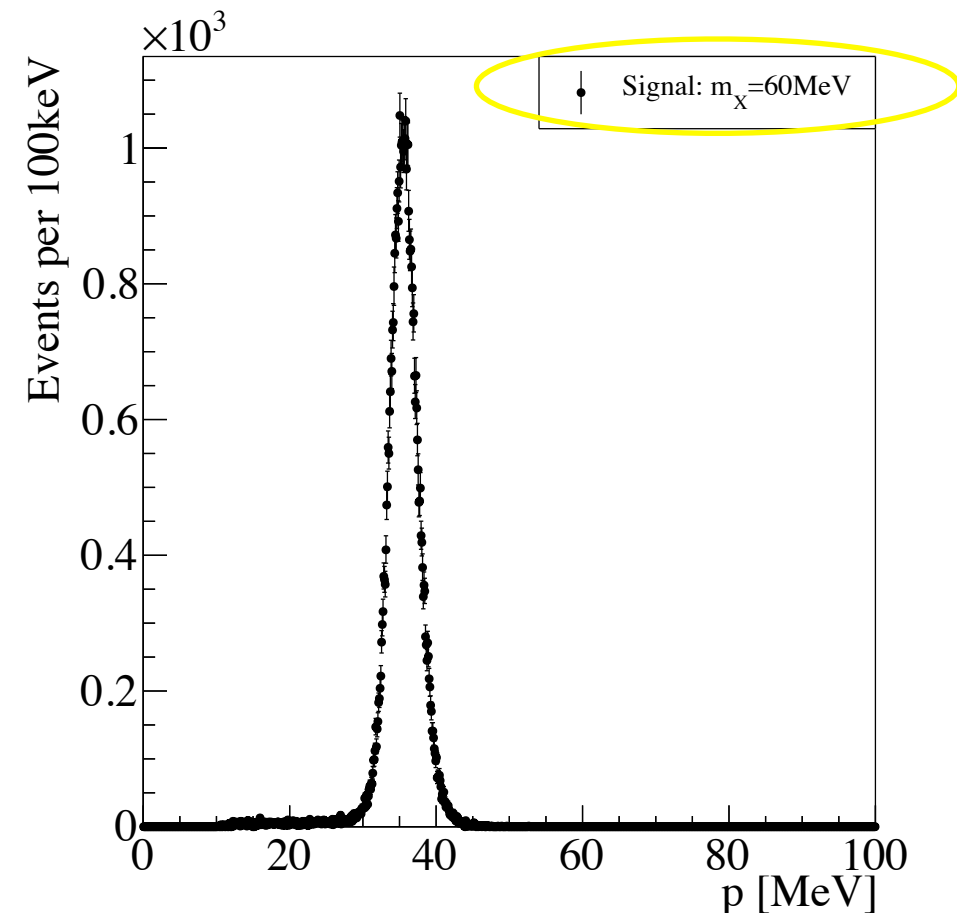
- Mu3e prospect for $\mu \rightarrow e a$

Perrevoort (Mu3e) '18

Potential search performed on positron momentum histograms filled with *online* reconstructed short tracks



(a) Simulated background events.



(b) Simulated $\mu \rightarrow eX$ signal events.

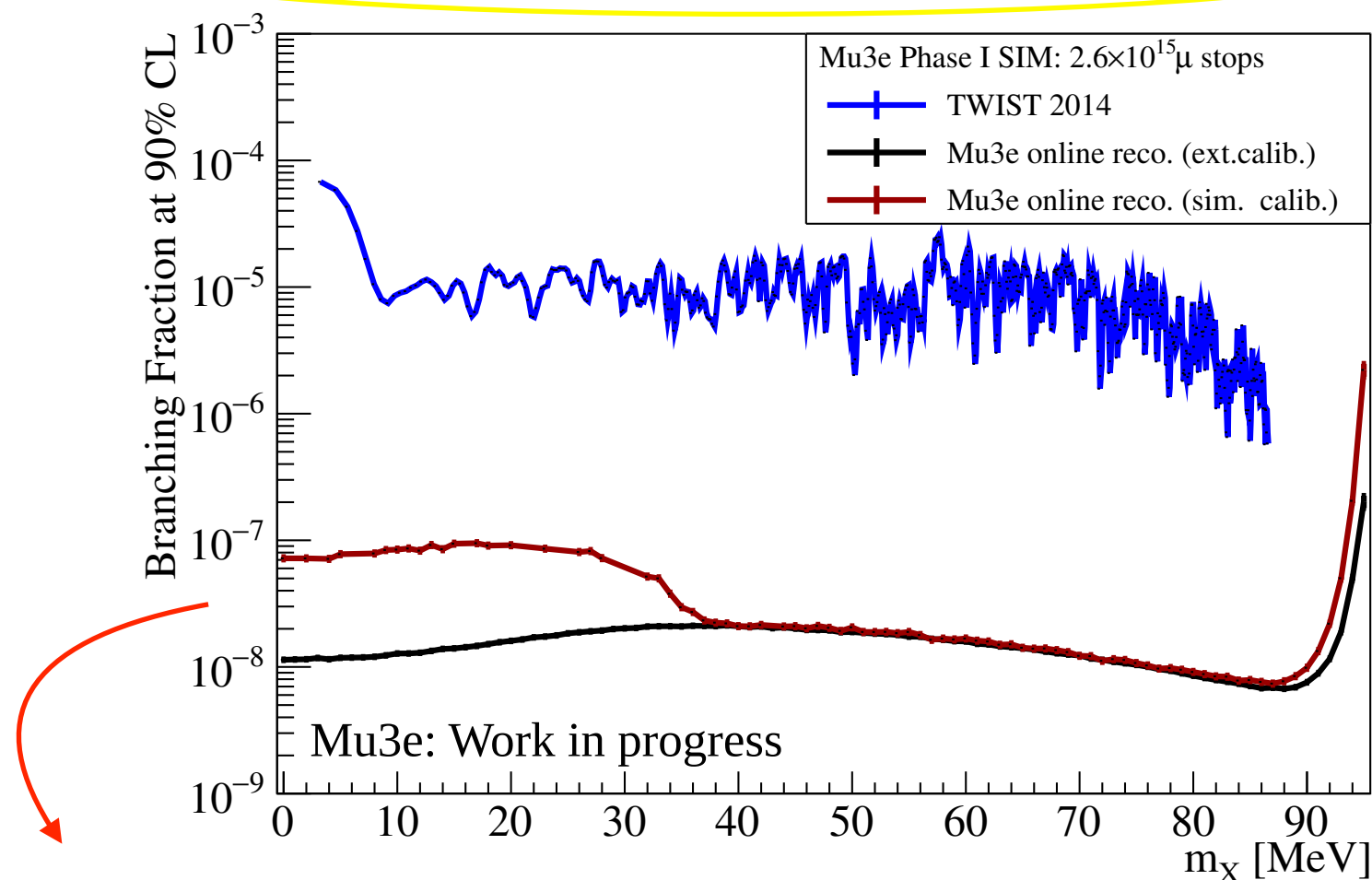
Future prospects: Mu3e

- Mu3e prospect for $\mu \rightarrow e a$

Perrevoort (Mu3e) '18

Potential search for performed on positron momentum histograms filled with *online* reconstructed short tracks

Expected limit for phase I ($2.6 \times 10^{15} \mu^+$):



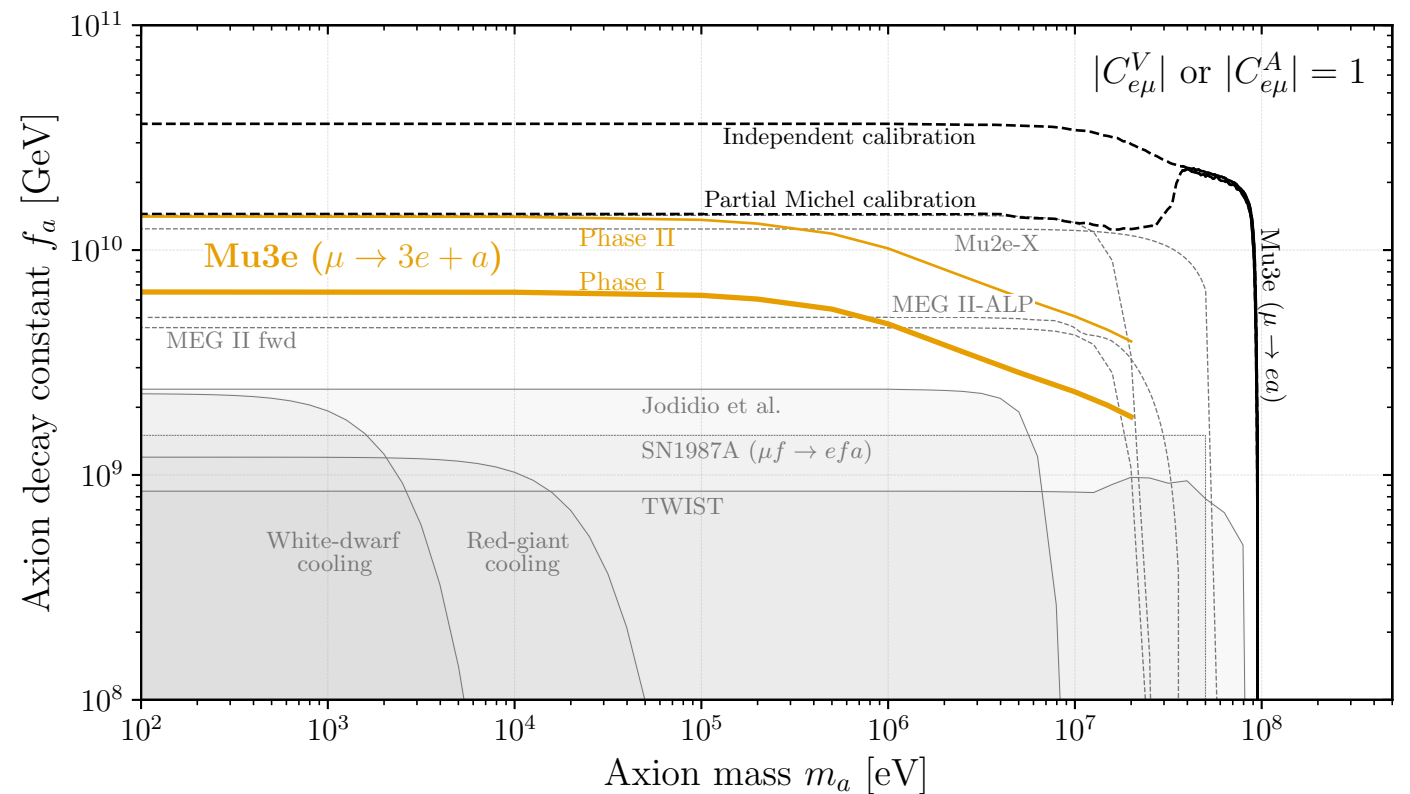
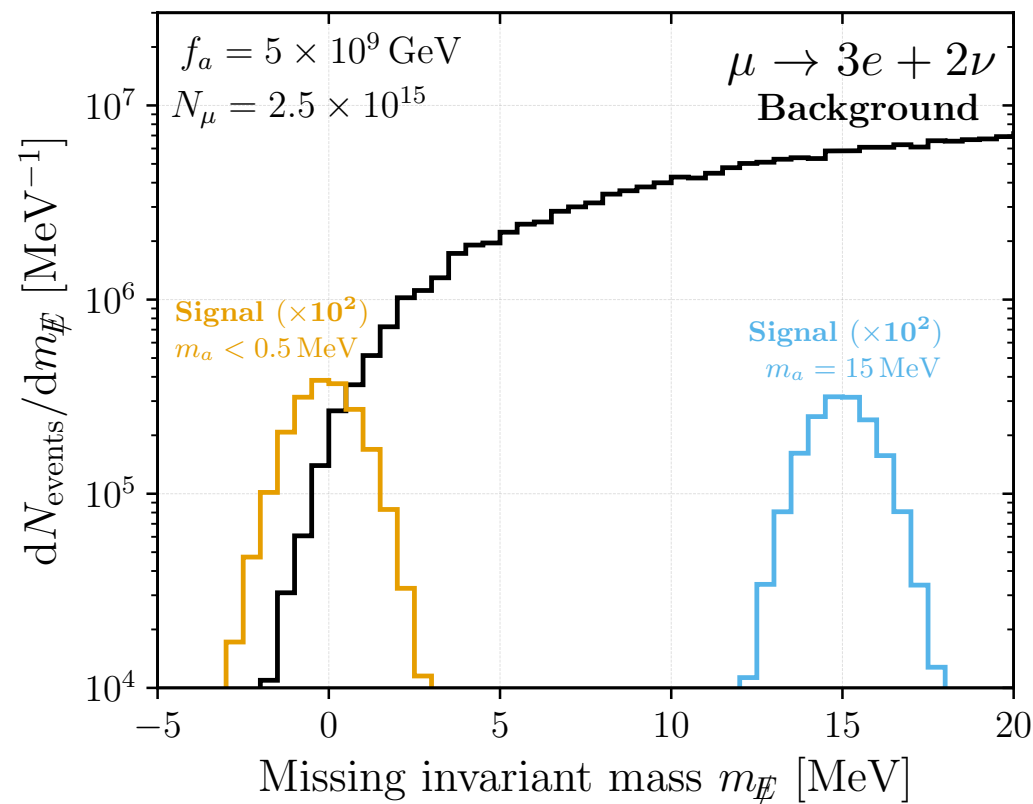
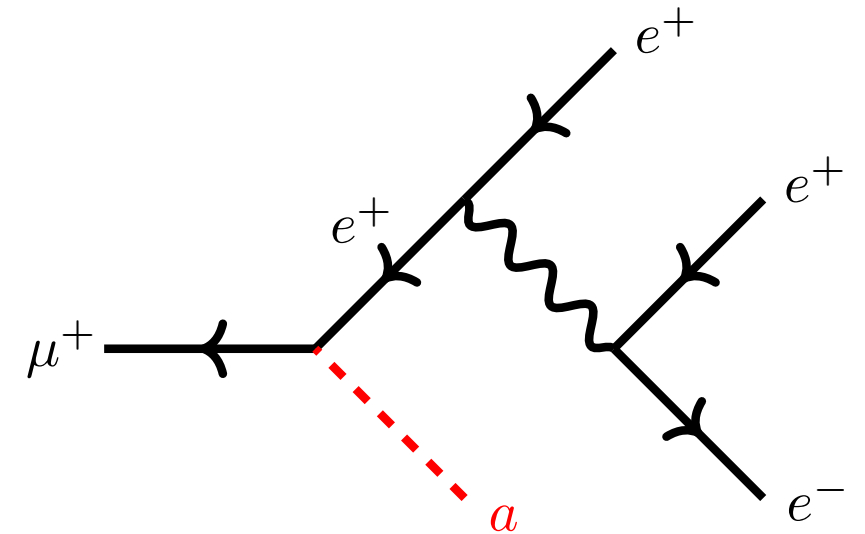
$$m_a \approx 0 : \quad \text{BR}(\mu \rightarrow e a) < 7 \times 10^{-8} \quad \Rightarrow \quad F_{\mu e} \gtrsim 3 \times 10^{10} \text{ GeV}$$

Future prospects: Mu3e

- Mu3e prospect for $\mu \rightarrow 3e a$

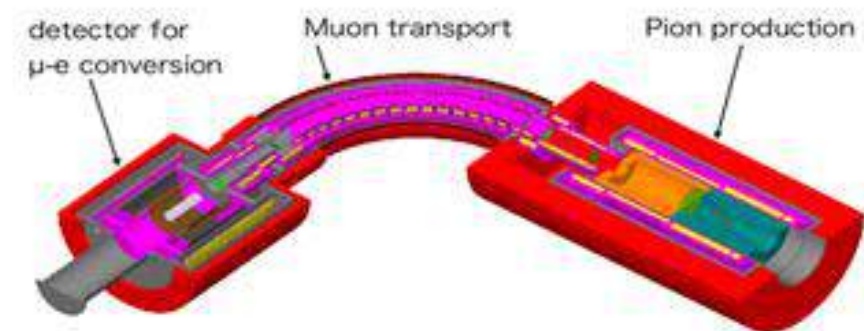
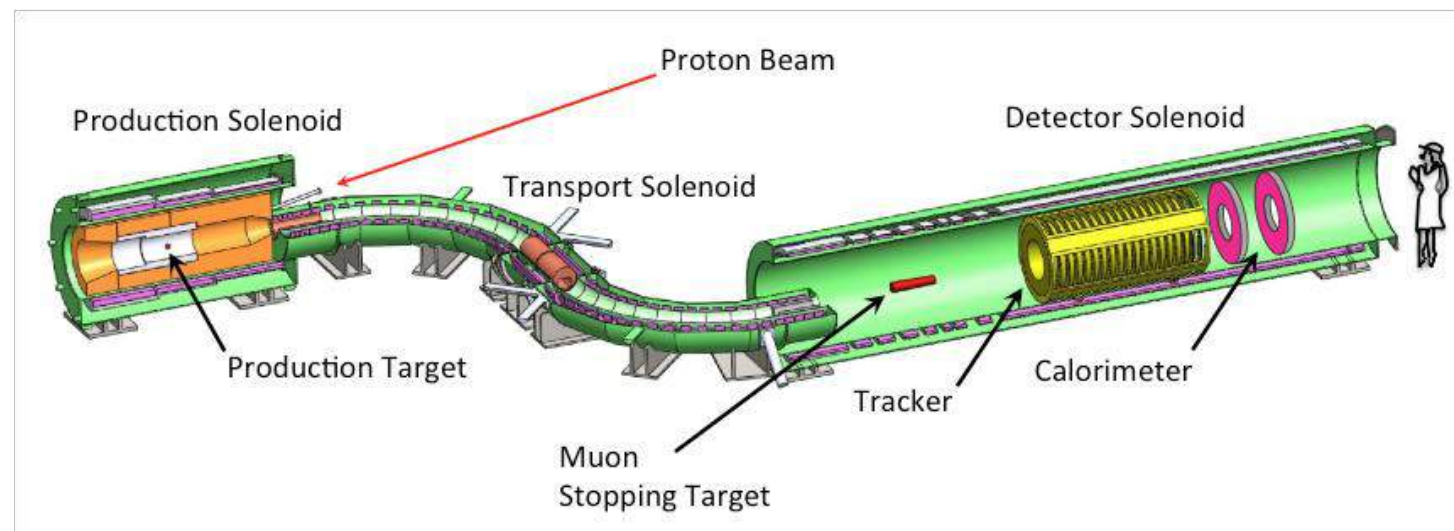
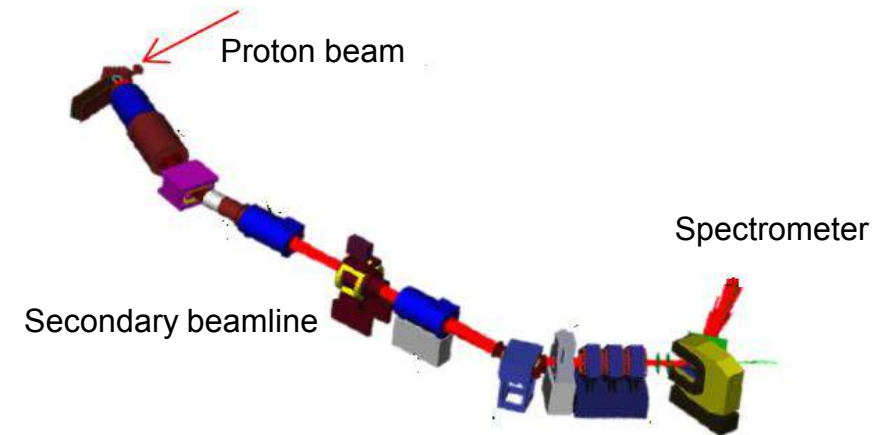
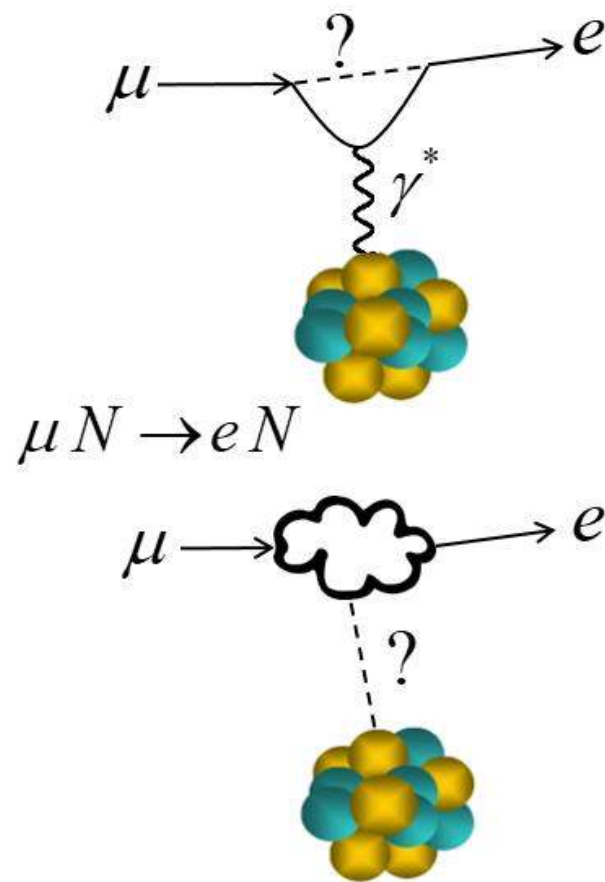
Knapen Langhoff Opferkuch Redigolo '23

Search for $3e + \text{invisible}$ from the internal conversion of virtual photon into a e^+e^- pair:



Future prospects: COMET/Mu2e

$\mu \rightarrow e$ conversion in nuclei experiments



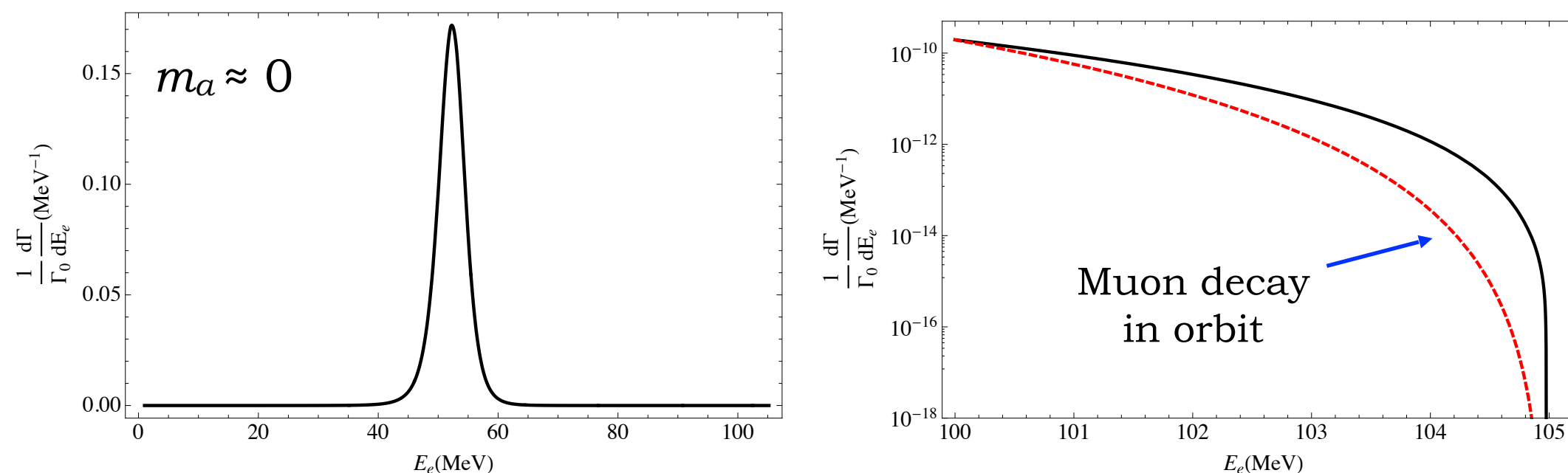
David Hitlin
Beijing CLFV School
June 3-7, 2019
Lecture 1

Future prospects: COMET/Mu2e

• Prospect at $\mu \rightarrow e$ conversion experiments

Garcia i Tomo et al. '11

Spectrum of $\mu \rightarrow ea$ emission in orbit (for Al):



Sensitivity in terms of the $\mu \rightarrow e$ conv. limit:

$$B(\mu \rightarrow eJ) \sim \frac{N_R R_{\mu e}}{f_J} \frac{\Gamma_{\text{capture}}}{\Gamma(\mu \rightarrow e \nu_\mu \bar{\nu}_e)} \sim \frac{N_R R_{\mu e}}{f_J} 1.5 \Rightarrow 2 \times 10^{-6}$$

Phase-space correction factor \rightarrow 27 (in Al)

Fraction of $\mu \rightarrow ea$ events in the signal region $\rightarrow 2 \times 10^{-10} (E_e > 100 \text{ MeV})$

10^{-17}

Possible bound at the level of Jodidio et al.

Limited by the $\mu \rightarrow e$ conv. signal region (only the tail included): dedicated search?

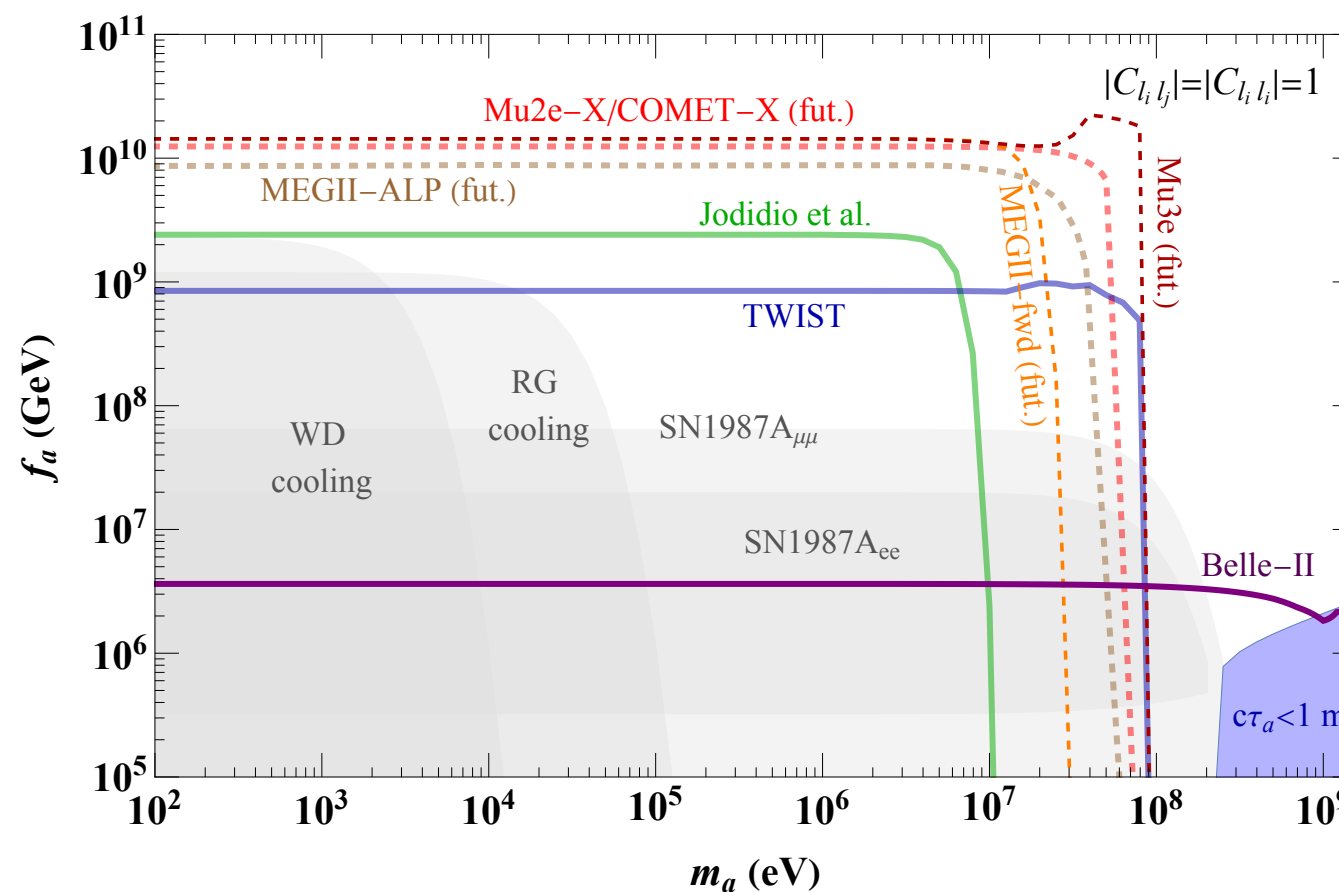
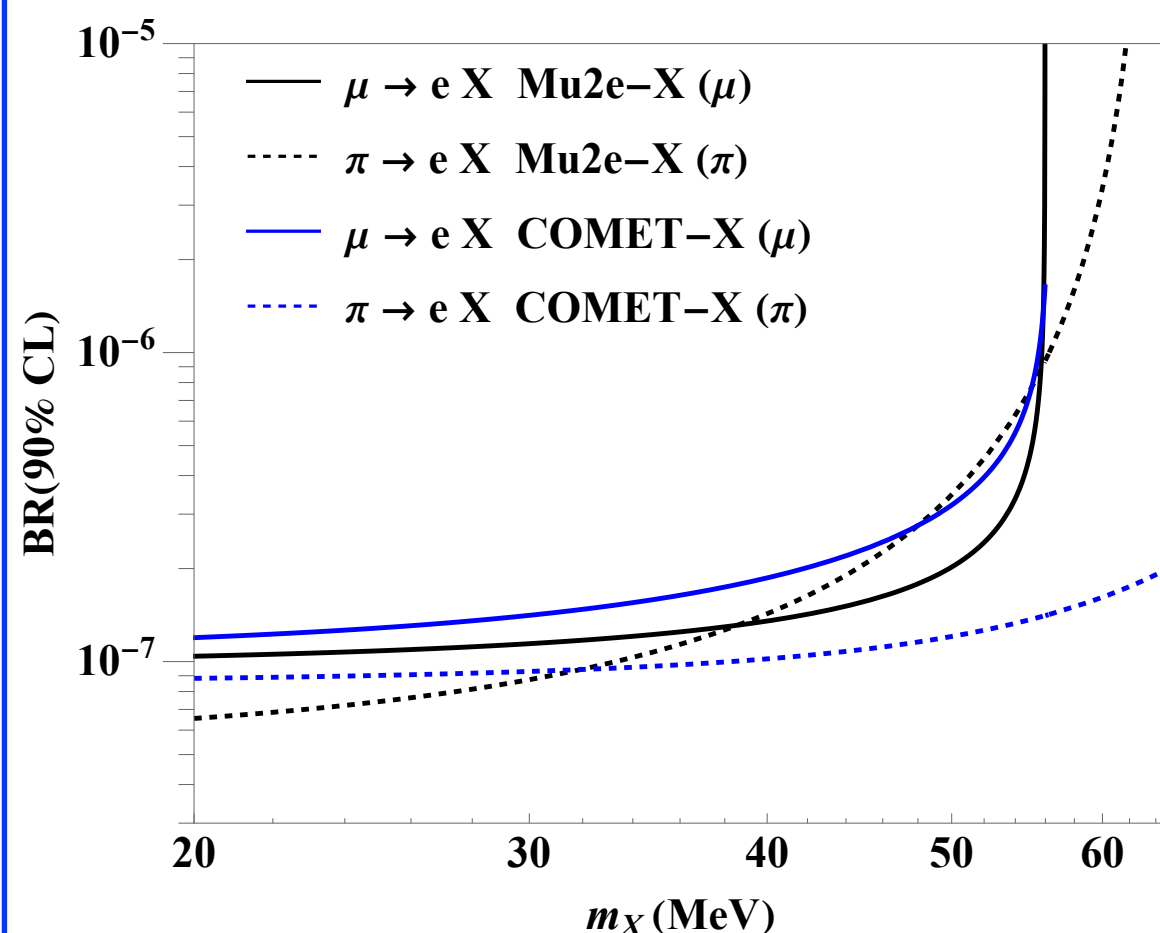
Future prospects: COMET/Mu2e

• Prospect at $\mu \rightarrow e$ conversion experiments

Hill Plestid Zupan '23

Conversion experiments employ μ^- beams to form muonic atoms: in the signal window for $\mu \rightarrow e$ conversion, the SM bg is suppressed, but $\mu \rightarrow ea$ would be too

Idea: search for a mono-energetic positron excess over the Michel spectrum, using data from calibration runs employing *positive* muon beams ($10^{13} - 10^{14} \mu^+$)

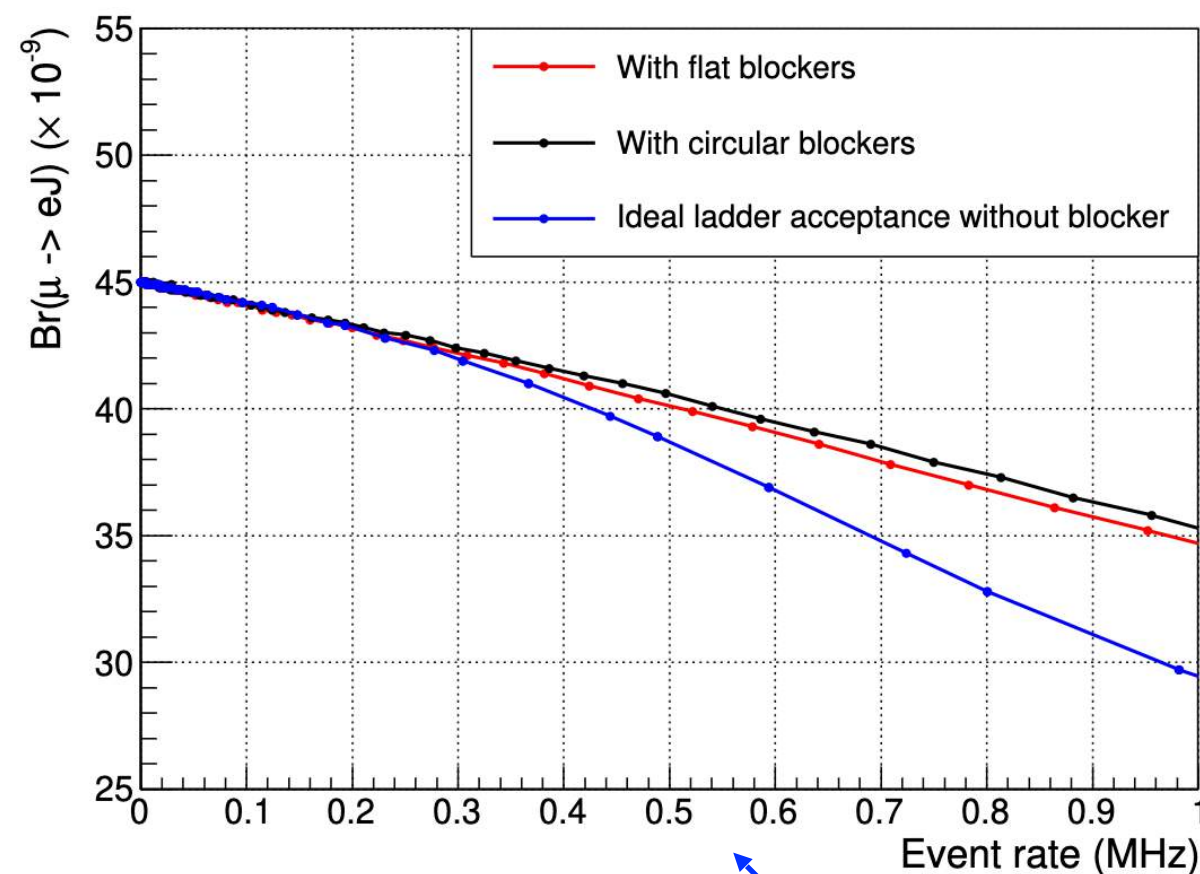
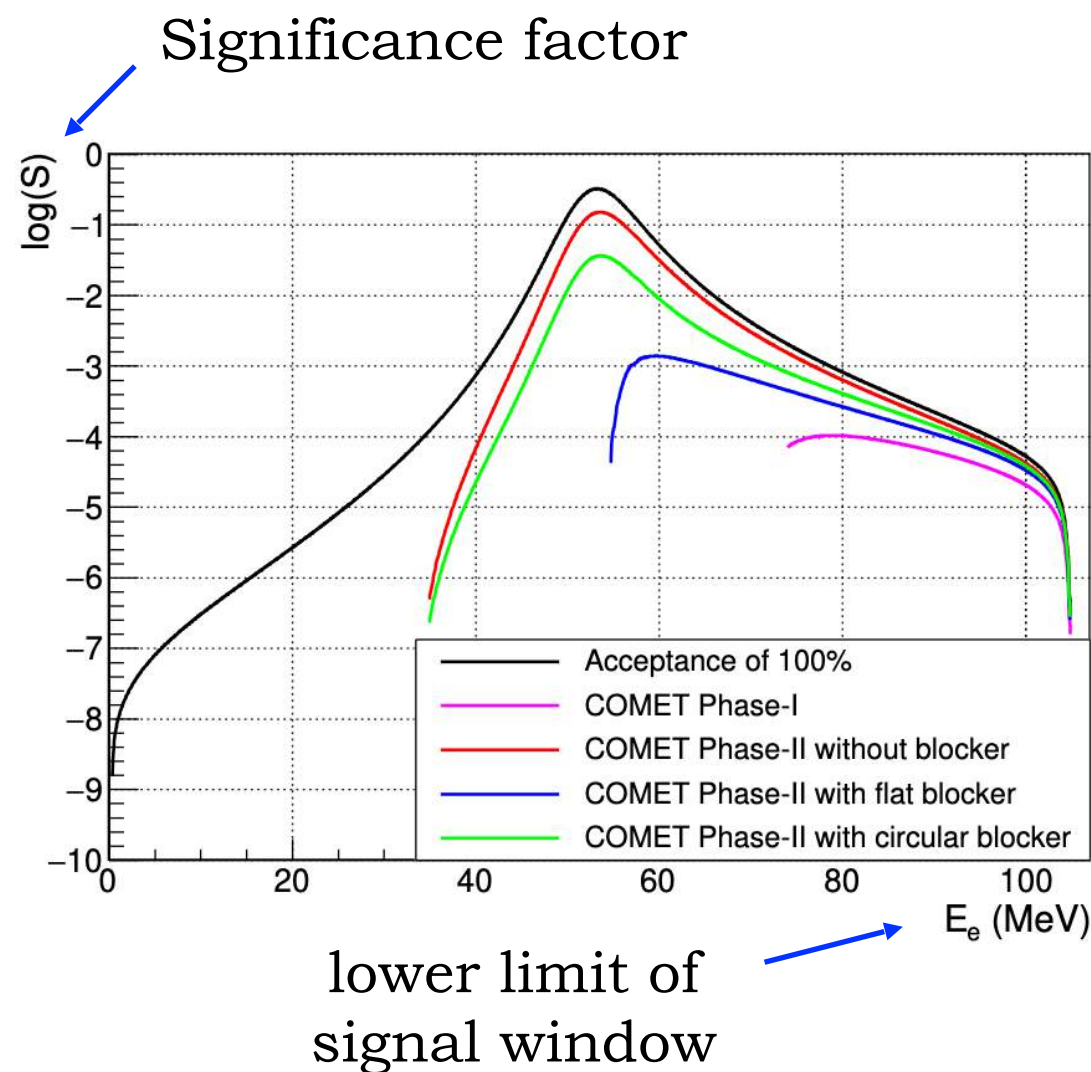


Future prospects for ALP searches: a COMET study

- Prospect at $\mu \rightarrow e$ conversion experiments

Xing et al. '22

One can try to lower the lower limit of the signal window
(very large background from muons decaying in orbit)



COMET Phase II can reach $\sim 10^{-8}$ coping with a bg rate $\sim O(100)\text{kHz}$

What about heavier ALPs?

If muons can not decay to on-shell ALPs (i.e. $m_a > m_\mu$),
constraints on LFV ALPs are much weaker

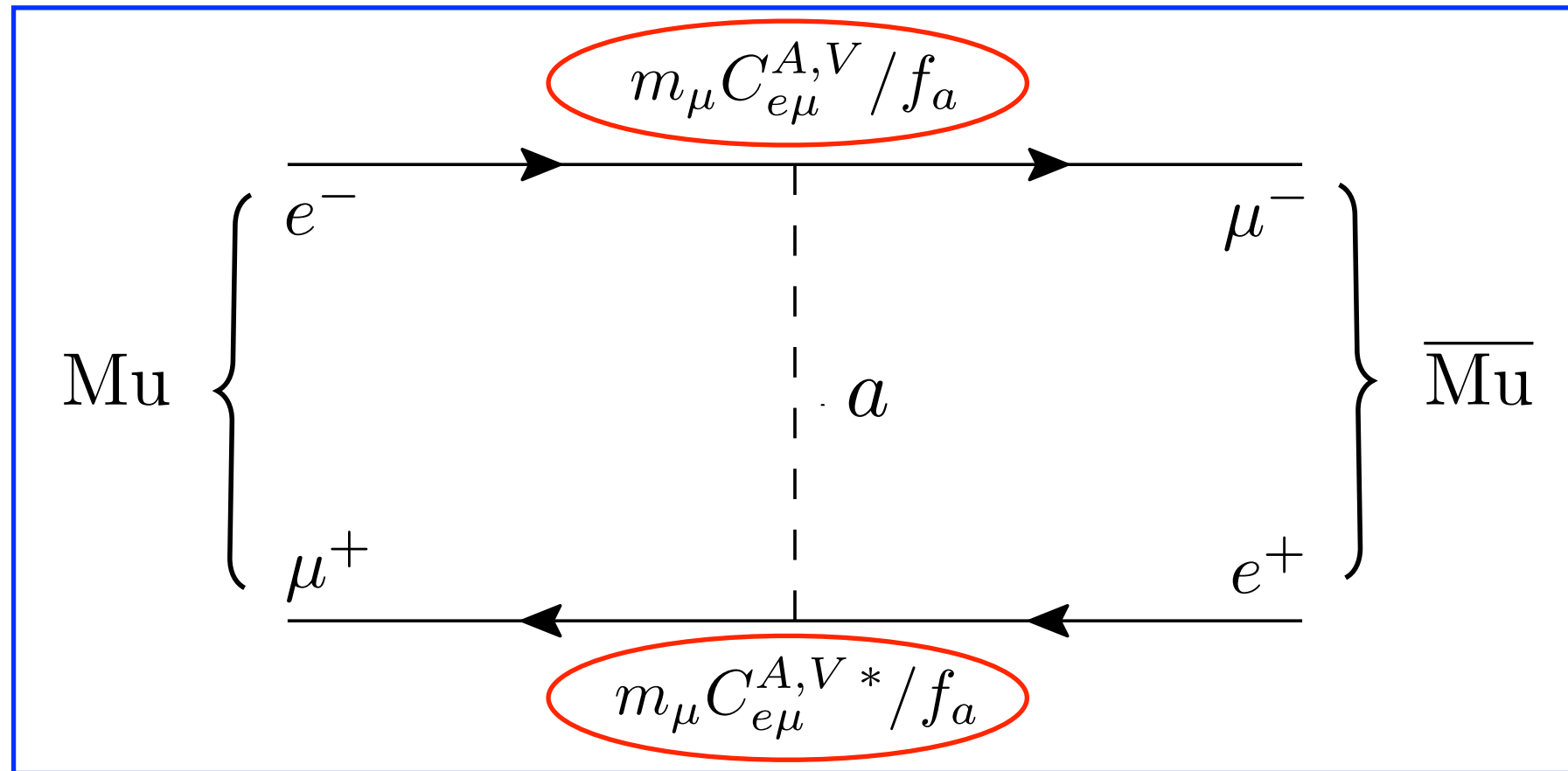
We have two possible strategies to test the μ - e interaction:

Indirect tests through processes they induce:
e.g. muonium-antimuonium conversion

Direct production in muon beam collisions,
e.g. $\mu^+ e^- \rightarrow a \gamma$ at the proposed μ TRISTAN project

Hamada et al. '22

Low-energy test: muonium to antimuonium conversion



$$P_{\text{Mu} \overline{\text{Mu}}} = \frac{m_\mu^4}{2\pi^2 a_B^6 \Gamma_\mu^2 [(m_\mu^2 - m_a^2)^2 + \Gamma_a^2 m_a^2] f_a^4} \left[|c_{0,0}|^2 \left| (C_{e\mu}^V)^2 - \left(1 + \frac{1}{\sqrt{1+X^2}} \right) (C_{e\mu}^A)^2 \right|^2 + |c_{1,0}|^2 \left| (C_{e\mu}^V)^2 - \left(1 - \frac{1}{\sqrt{1+X^2}} \right) (C_{e\mu}^A)^2 \right|^2 \right],$$

Limits on the conversion probability:

Present: $P_{\text{Mu} \overline{\text{Mu}}} < 8.3 \times 10^{-11}$ $\xrightarrow[\text{improvement}]{\times 1000}$ Future: $P_{\text{Mu} \overline{\text{Mu}}} < 7 \times 10^{-14}$

MACS '98 MACE '24

High-energy option: the μ TRISTAN proposal

μ TRISTAN proposal : $\mu^+\mu^+$ and μ^+e^- colliders



Hamada et al. '22

- The idea is to cool and focus μ^+ beams, a technology developed at JPARC [Abe et al., 1901.03047]
- The μ^+ beams could be accelerated up to 1 TeV and made to collide with :

30 GeV e^- beam

- “Higgs factory” with $\sqrt{s} \simeq 346$ GeV
- Expected integrated luminosity $\mathcal{L} = 1 \text{ ab}^{-1}$

OR

1 TeV μ^+ beam

- “Discovery machine” with $\sqrt{s} = 2$ TeV
- Expected integrated luminosity $\mathcal{L} = 100 \text{ fb}^{-1}$

slide borrowed from L. Mukherjee

μ TRISTAN proposal : $\mu^+\mu^+$ and μ^+e^- colliders

PTEP

Prog. Theor. Exp. Phys. 2022 053B02(16 pages)
DOI: 10.1093/ptep/ptac059

μ TRISTAN

μ^+e^- collisions would make μ TRISTAN
an ideal environment to study cLFV!

- The

[A]

- The

For possible applications see

[Fridell et al. '23](#), [Lichtenstein et al. '23](#)

- “Higgs factory” with
 $\sqrt{s} \simeq 346$ GeV
- Expected integrated
luminosity $\mathcal{L} = 1 \text{ ab}^{-1}$

OR

- “Discovery machine” with
 $\sqrt{s} = 2$ TeV
- Expected integrated
luminosity $\mathcal{L} = 100 \text{ fb}^{-1}$

slide borrowed from L. Mukherjee

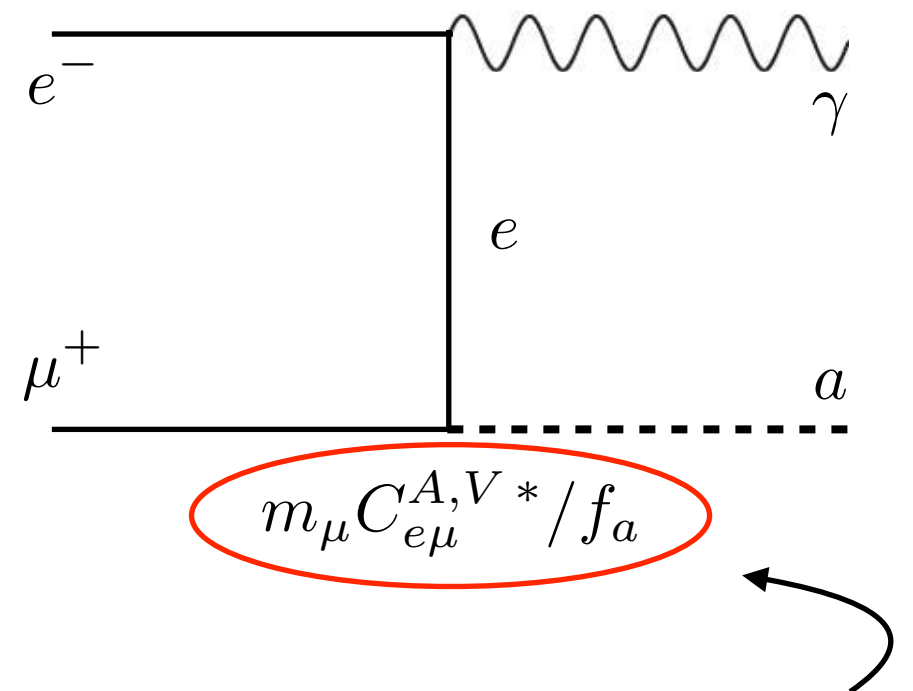
ALP production and decay at μ TRISTAN

Most promising production mode
(see backup for other processes):

$$\sigma(e^- \mu^+ \rightarrow a \gamma) \simeq \alpha \frac{m_\mu^2}{f_a^2} \frac{|C_{e\mu}^A|^2 + |C_{e\mu}^V|^2}{4s} |\eta|_{\max}$$

$$= 0.03 \text{ fb} \left(\frac{200 \text{ GeV}}{F_{e\mu}} \right)^2 \left(\frac{346 \text{ GeV}}{\sqrt{s}} \right)^2 \left(\frac{|\eta|_{\max}}{2.5} \right)$$

LC Li Mukherjee Yang '24



Heavier ALPs can decay promptly through the same LFV interactions

Charge combination $a \rightarrow \mu^- e^+$ virtually background-free:

Signal:

$$e^- \mu^+ \rightarrow \gamma a \rightarrow \gamma \mu^- e^+$$

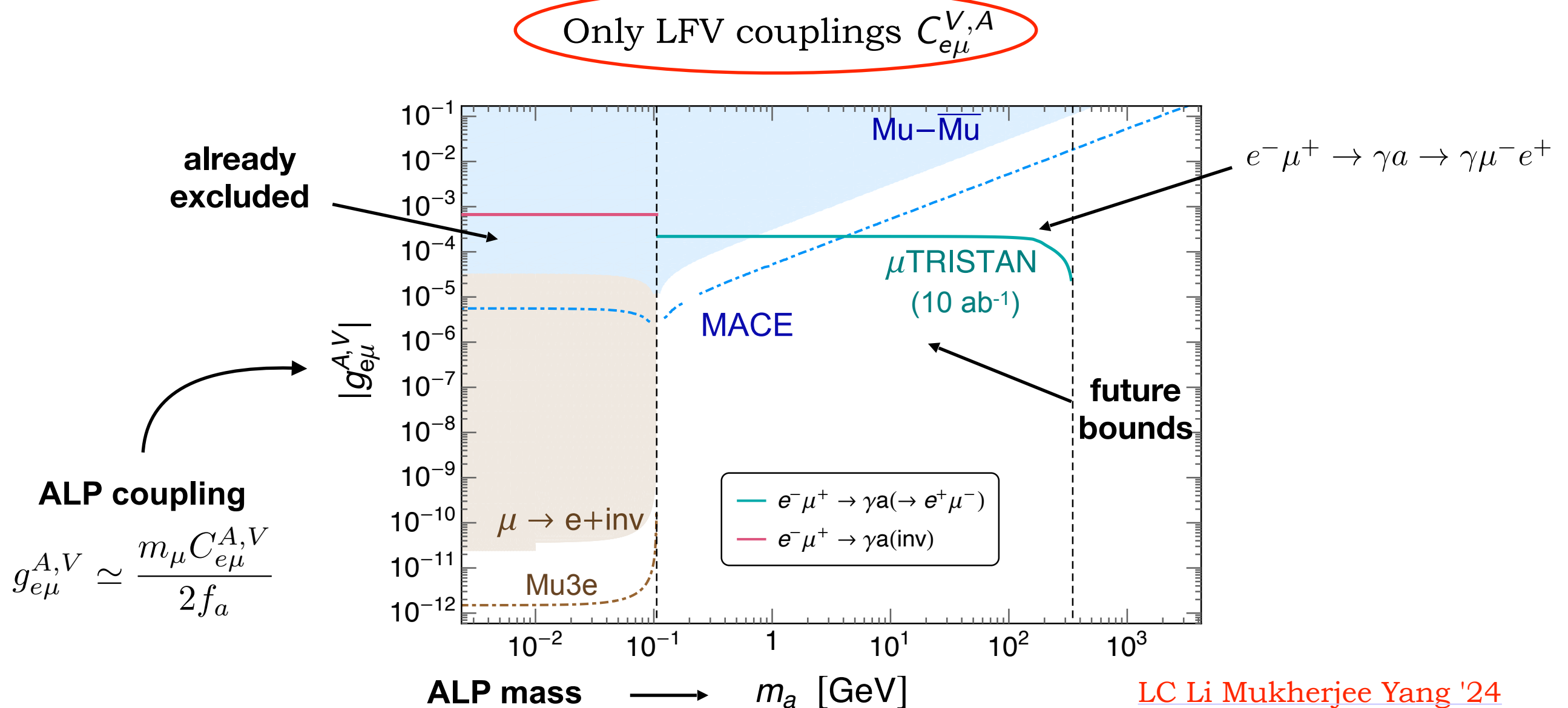
SM bg:

$$e^- \mu^+ \rightarrow \gamma \nu_e \bar{\nu}_\mu W^- (\rightarrow \mu^- \bar{\nu}_\mu) W^+ (\rightarrow e^+ \nu_e) \quad [\sigma_B \simeq 2 \times 10^{-5} \text{ fb}]$$

However, asymmetric beams reduce signal efficiency:

About 70% (50%) of ALP decay products fly outside the geometric acceptance for a detector with $|\eta| < 2.5$ (3.5)

Future sensitivity to ALP μ - e interactions



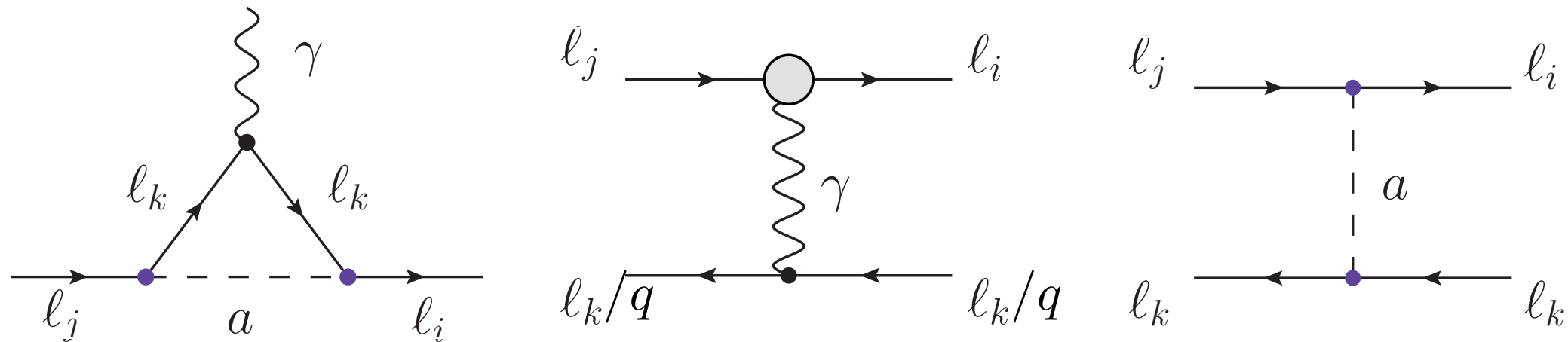
Interesting **interplay** between MACE and μ TRISTAN

What if there are also substantial *flavour-conserving* (LFC) couplings?

One can also search for $a \rightarrow \mu^+ \mu^-$ but low-energy LFV becomes stronger

ALP-induced muon LFV decays

Other interactions (LFC ones, in particular) lead to muon LFV decays:



see e.g. [Cornella Paradisi Sumensari '19](#)

Stringent limits from:

$$\mu \rightarrow e\gamma$$

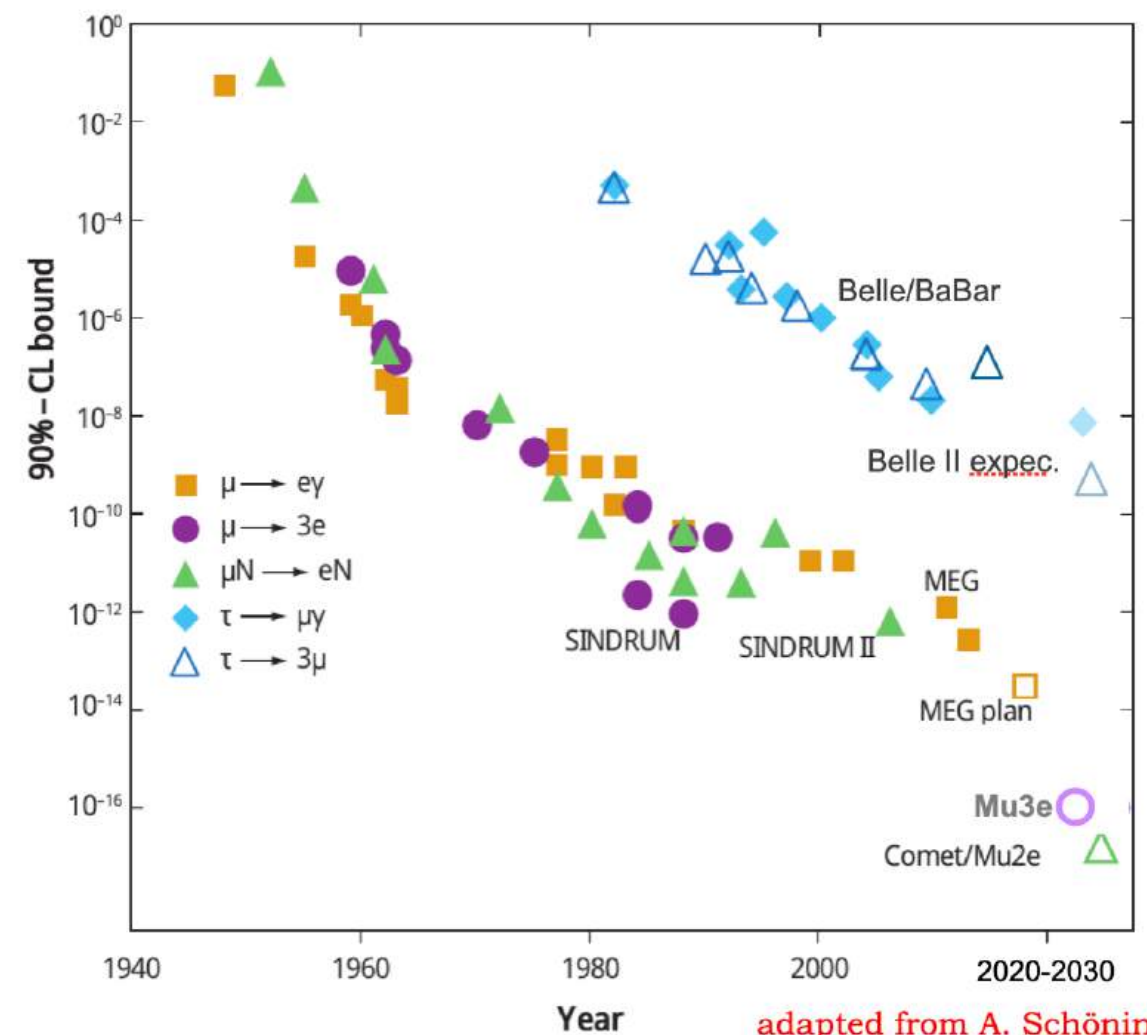
$$\mu \rightarrow eee$$

$$\mu N \rightarrow e N$$



For a pedagogical introduction (exp + th)

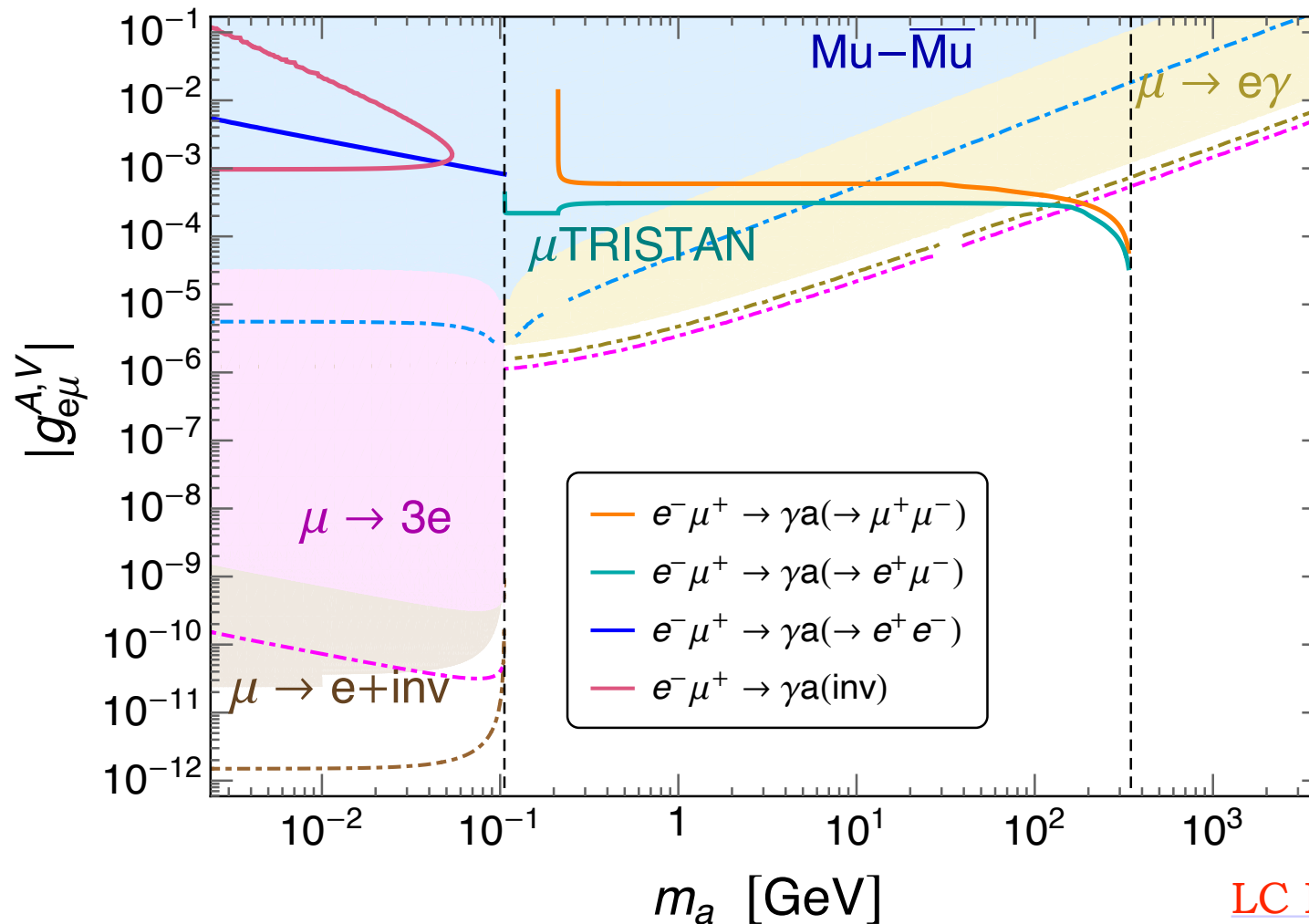
cf. [LC and Signorelli '17](#)



adapted from A. Schöning

Future sensitivity to ALP μ - e interactions

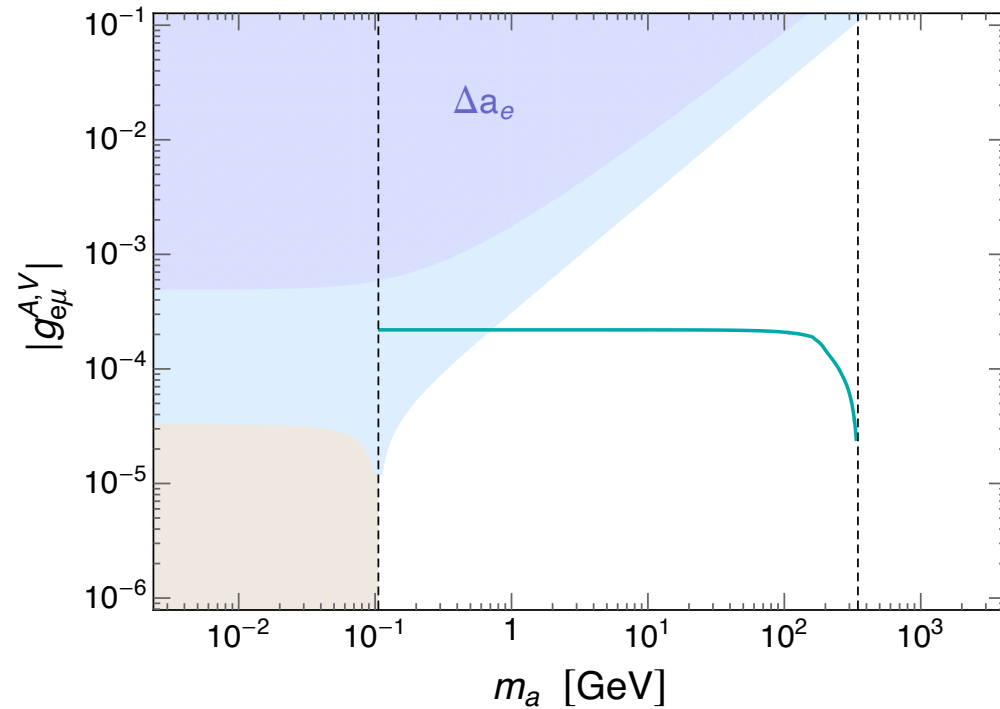
$$\text{LFV+LFC: } C_{e\mu}^{V,A} = C_{ee}^A = C_{\mu\mu}^A$$



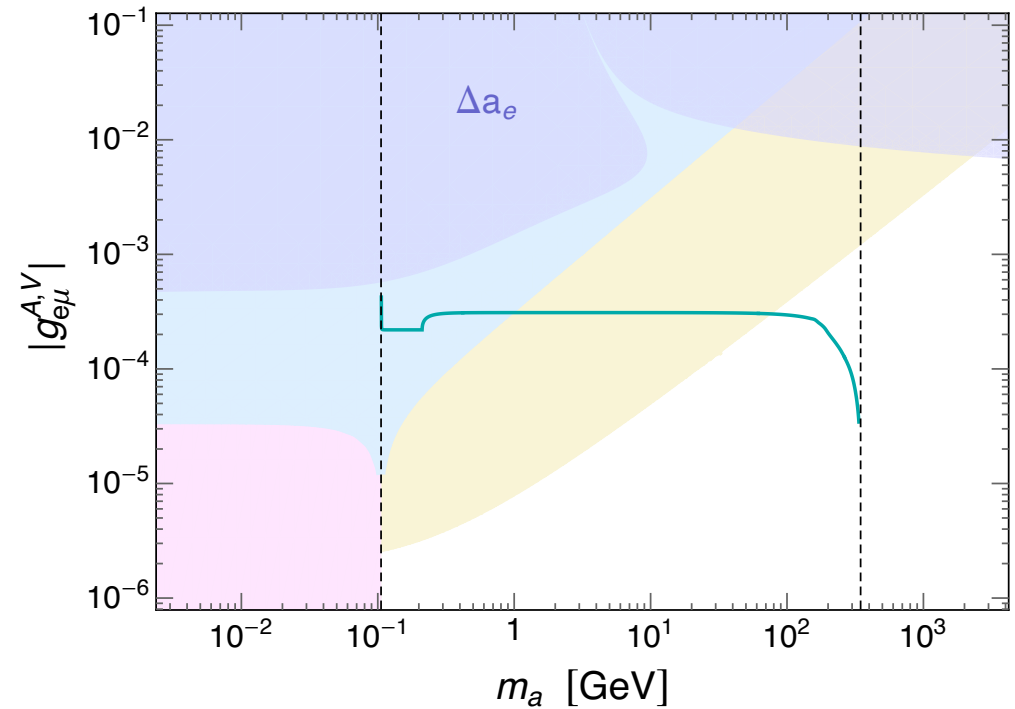
LC Li Mukherjee Yang '24

μ TRISTAN sensitivity could go beyond low-energy LFV constraints, only for very heavy ALPs, $m_a \gtrsim \mathcal{O}(100)$ GeV

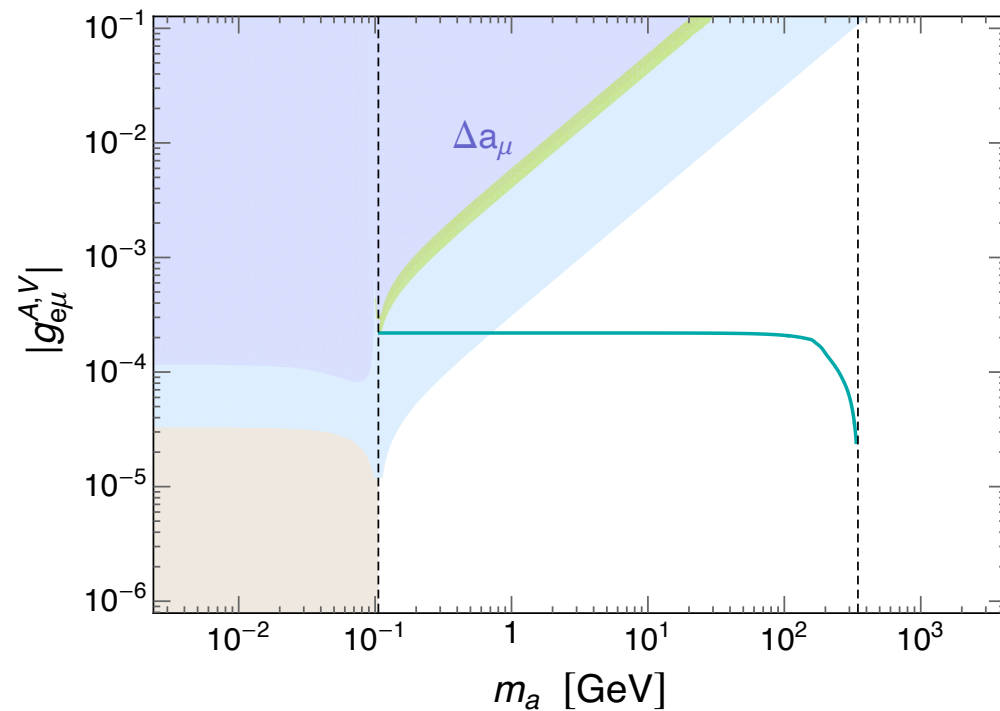
Muon and electron g-2 constraints



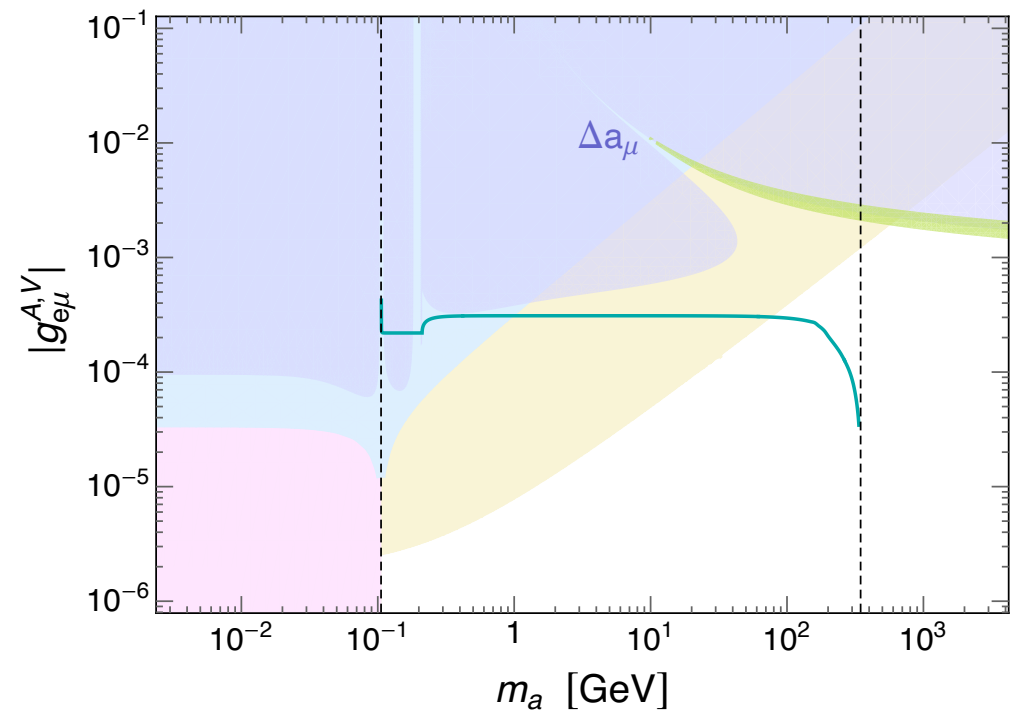
(a) LFV (e - μ) couplings only



(b) LFV (e - μ) and LFC couplings



(c) LFV (e - μ) couplings only



(d) LFV (e - μ) and LFC couplings

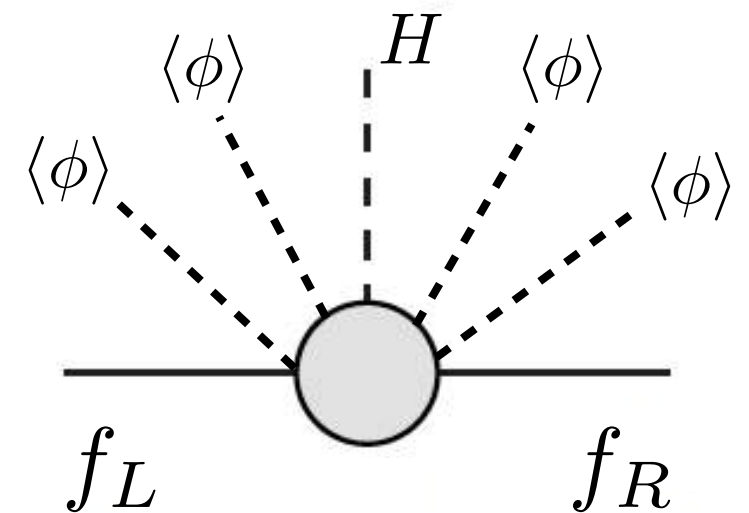
Froggatt-Nielsen flavour models

- SM fermions charged under a new horizontal symmetry G_F
- G_F forbids Yukawa couplings at the renormalisable level
- G_F spontaneously broken by the vev(s) of one or more scalars (the “flavons”)
- Yukawas arise as higher dimensional operators

Froggatt Nielsen '79
 Leurer Seiberg Nir '92, '93
 ...

$$-\mathcal{L} = a_{ij}^u \left(\frac{\phi}{\Lambda} \right)^{n_{ij}^u} \bar{Q}_i u_j \tilde{H} + a_{ij}^d \left(\frac{\phi}{\Lambda} \right)^{n_{ij}^d} \bar{Q}_i d_j H$$

flavour-anarchical
 O(1) coefficients



$\langle \phi \rangle < \Lambda \quad \Rightarrow \quad \epsilon \equiv \langle \phi \rangle / \Lambda$ small expansion parameter ($\Lambda = \text{UV scale}$)
 n_{ij}^f dictated by the symmetry

G_F could be abelian or non-abelian, continuous or discrete, local or global

The simplest option: Froggatt-Nielsen U(1)

Quark sector

FN charges

	ϕ	Q_i	u_i	d_i	H
U(1)	1	\mathcal{Q}_{Q_i}	\mathcal{Q}_{u_i}	\mathcal{Q}_{d_i}	0



$$Y_{ij}^u = a_{ij}^u \epsilon^{\mathcal{Q}_{Q_i} - \mathcal{Q}_{u_j}}$$

$$Y_{ij}^d = a_{ij}^d \epsilon^{\mathcal{Q}_{Q_i} - \mathcal{Q}_{d_j}}$$

Rotation matrices $Y^f = V^{f\dagger} \hat{Y}^f W^f \Rightarrow V_{ij}^{u,d} \sim \epsilon^{|\mathcal{Q}_{Q_i} - \mathcal{Q}_{Q_j}|} \quad W_{ij}^{u,d} \sim \epsilon^{|\mathcal{Q}_{u_i, d_i} - \mathcal{Q}_{u_j, d_j}|}$

Successful predictions for $V_{\text{CKM}} = V^u V^{d\dagger}$:

$$V_{ud} \approx V_{cs} \approx V_{tb} \approx 1 \quad V_{ub} \approx V_{td} \approx V_{us} \times V_{cb}$$

(independent of charge assignment)

Example:

$$(\mathcal{Q}_{Q_1}, \mathcal{Q}_{Q_2}, \mathcal{Q}_{Q_3}) = (3, 2, 0), \quad (\mathcal{Q}_{u_1}, \mathcal{Q}_{u_2}, \mathcal{Q}_{u_3}) = (-4, -2, 0), \quad (\mathcal{Q}_{d_1}, \mathcal{Q}_{d_2}, \mathcal{Q}_{d_3}) = (-4, -2, -2)$$

$$Y^u \sim \begin{pmatrix} \epsilon^7 & \epsilon^5 & \epsilon^3 \\ \epsilon^6 & \epsilon^4 & \epsilon^2 \\ \epsilon^4 & \epsilon^2 & 1 \end{pmatrix}, \quad Y^d \sim \begin{pmatrix} \epsilon^7 & \epsilon^5 & \epsilon^5 \\ \epsilon^6 & \epsilon^4 & \epsilon^4 \\ \epsilon^4 & \epsilon^2 & \epsilon^2 \end{pmatrix} \quad V_{\text{CKM}} \sim \begin{pmatrix} 1 & \epsilon & \epsilon^3 \\ \epsilon & 1 & \epsilon^2 \\ \epsilon^3 & \epsilon^2 & 1 \end{pmatrix}$$

$$\epsilon = \langle \phi \rangle / \Lambda \approx 0.2$$

Lepton sector

$$-\mathcal{L} \supset \left[a_{ij}^\ell \left(\frac{\langle \phi \rangle}{\Lambda_\ell} \right)^{\mathcal{Q}_{L_i} - \mathcal{Q}_{e_j}} \bar{L}_i e_j H + h.c. \right] + \kappa_{ij}^\nu \left(\frac{\langle \phi^* \rangle}{\Lambda_\ell} \right)^{\mathcal{Q}_{L_i} + \mathcal{Q}_{L_j}} \frac{(\bar{L}_i^c \tilde{H})(\tilde{H}^T L_j)}{\Lambda_N}$$

$$\Rightarrow Y^\ell = V^\ell \hat{Y}^\ell W^{\ell\dagger}, \quad m^\nu = V^\nu \hat{m}^\nu V^{\nu T} \quad V_{ij}^{\ell,\nu} \sim \epsilon_\ell^{|\mathcal{Q}_{L_i} - \mathcal{Q}_{L_j}|}, \quad W_{ij}^\ell \sim \epsilon_\ell^{|\mathcal{Q}_{e_i} - \mathcal{Q}_{e_j}|}$$

LH charges can be chosen to give a (quasi-)anarchical $U_{\text{PMNS}} = V^\nu V^{\ell\dagger}$
 RH charges then responsible for charged leptons hierarchy

Examples:

Altarelli Feruglio Masina Merlo '12

- Anarchy $(\mathcal{Q}_{L_1}, \mathcal{Q}_{L_2}, \mathcal{Q}_{L_3}) = (\mathcal{Q}_L, \mathcal{Q}_L, \mathcal{Q}_L)$
- Mu-tau anarchy $(\mathcal{Q}_{L_1}, \mathcal{Q}_{L_2}, \mathcal{Q}_{L_3}) = (\mathcal{Q}_L + 1, \mathcal{Q}_L, \mathcal{Q}_L)$
- Hierarchy $(\mathcal{Q}_{L_1}, \mathcal{Q}_{L_2}, \mathcal{Q}_{L_3}) = (\mathcal{Q}_L + 2, \mathcal{Q}_L + 1, \mathcal{Q}_L)$

Charged lepton hierarchy, e.g. : $(\mathcal{Q}_{e_1}, \mathcal{Q}_{e_2}, \mathcal{Q}_{e_3}) = (\mathcal{Q}_L - 4, \mathcal{Q}_L - 2, \mathcal{Q}_L - 1)$
 (with $\epsilon_\ell \approx \epsilon^2 \approx 0.04$)

Local Froggatt-Nielsen U(1)

Flavour non-universal **local** U(1) symmetry generating the hierarchies of fermion masses and mixing through the Froggatt-Nielsen mechanism

(anomalies cancelled by suitable UV completions)

Smolkovič Tammara Zupan '19
Bonney Dudas Pokorski '19

Below the cutoff Λ , only **two** new particles:

$$\phi = \frac{v_\phi + \varphi}{\sqrt{2}} e^{i a / v_\phi}$$

longitudinal component of

Physical flavon

U(1) gauge boson, Z'

$$m_\varphi^2 = \frac{1}{2} \lambda_\phi v_\phi^2$$

$$m_{Z'} = \sqrt{2} g_F \langle \phi \rangle = g_F v_\phi$$

$$\mathcal{L} = n_{ij}^f \frac{m_{ij}^f}{v_\phi} \bar{f}_i P_R f_j \varphi$$

$$\mathcal{L} \supset g_F \bar{f} \gamma^\mu (\mathcal{Q}_{fL} P_L + \mathcal{Q}_{fR} P_R) f Z'_\mu$$

→ both fields decay into SM fermions and are produced in the early universe by thermal interactions (O(1) couplings with the fields at Λ)

→ we have to require their lifetime < 0.1 s in order not to affect **BBN**