



# Dark Matter Production from Bubbles

## Gravitational Wave Signals in Different Dark Matter Models



Montpellier-Sète

10/09/2025 – 12/09/2025



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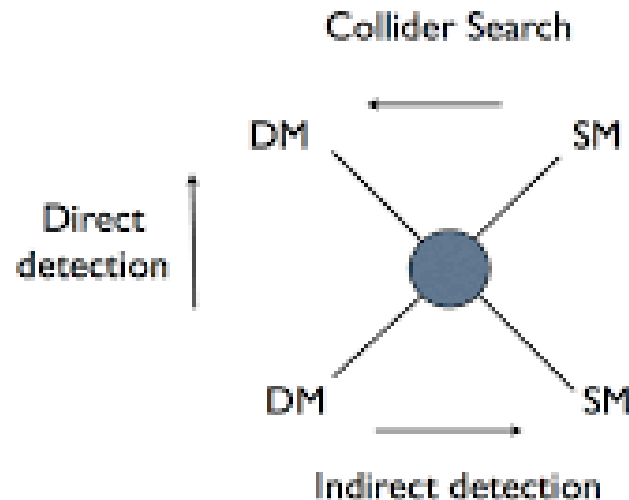
# Dark Matter Searches

## 1. It became standard to talk about:

1.a. Particle Production (Colliders)

1.b. Direct Detection

1.c. Indirect Detection (Cosmic rays)



# Dark Matter Searches

## 2. Other indirect searches:

### 2.a. Cosmological signatures:

2.a.1. Structure formation

2.a.2. Primordial abundances

2.a.3. Anomalies in the CMB

### 2.b. Astrophysical signatures:

2.b.1. Cooling of stellar objects

### 2.c. Laboratory signatures:

2.c.1. Electroweak precision observables.

2.c.2. anomalous magnetic moments (muon  $g-2$ ).

2.c.3. Torsion balance experiments.

# Gravitational waves as an evidence of Dark Matter

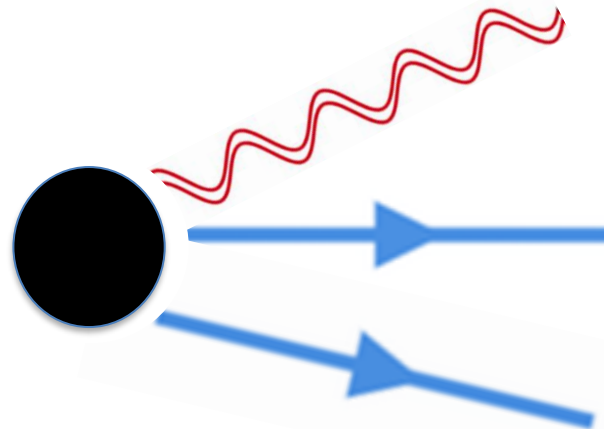
## 1. Gravitational waves as a proof of the Dark Matter framework

### 1.a. Proof of the Dark Matter production mechanism:

1.a.1. Freeze-in mechanism

1.a.2. Gravitational production

1.a.3. First order phase transitions

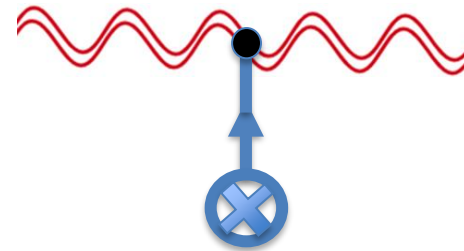


# Gravitational waves as an evidence of Dark Matter

## 2. Gravitational waves directly associated with Dark Matter

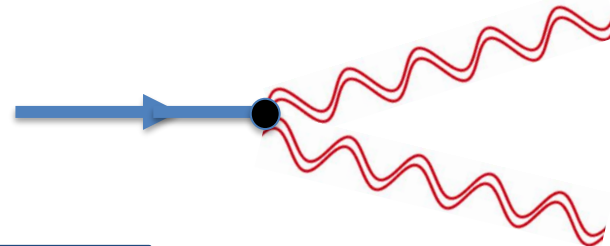
### 2.a. Gravitational waves modified by Dark Matter:

#### 2.a.1. Ultralight Dark Matter



### 2.b. GW produced by Dark Matter:

#### 2.b.1. Gravitational radiation or decays of Dark Matter



# Gravitational waves as an evidence of Dark Matter

## 1. Gravitational waves as a proof of the Dark Matter framework

### 1.a. Proof of the Dark Matter production mechanism:

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JARC, Mindaugas Karciauskas, 2311.00378 [hep-ph]

#### 1.a.2. Gravitational production

JARC, L. J. Garay, J.M. Sánchez Velázquez, arXiv:1910.13937 [hep-ph]

JARC, L. J. Garay, A. Parra-López, J.M. Sánchez Velázquez, arXiv:2301.04674 [gr-qc]

JARC, L. J. Garay, A. Parra-López, J.M. Sánchez Velázquez, 2310.07515 [gr-qc]

#### 1.a.3. First order phase transitions

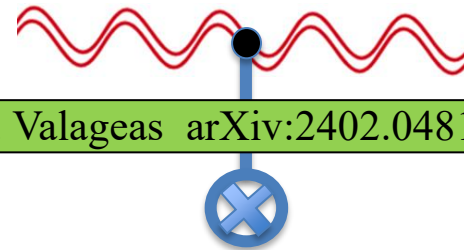
JARC, Jesús Luque, Javier Rubio, arXiv: 2407.14592 [hep-ph]

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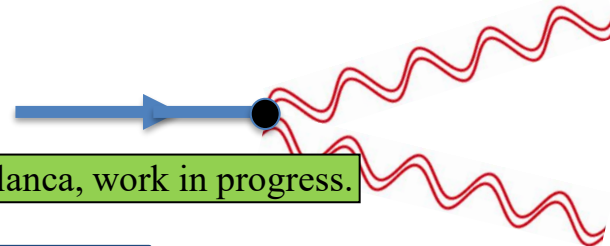
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JARC, P. Brax, C. Burrage, P. Valageas arXiv:2402.04819 [astro-ph.CO]

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JARC , A. Cendal, I. Mariblanca, work in progress.



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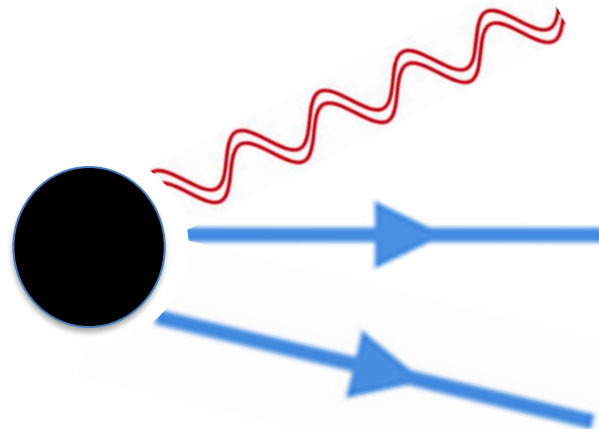
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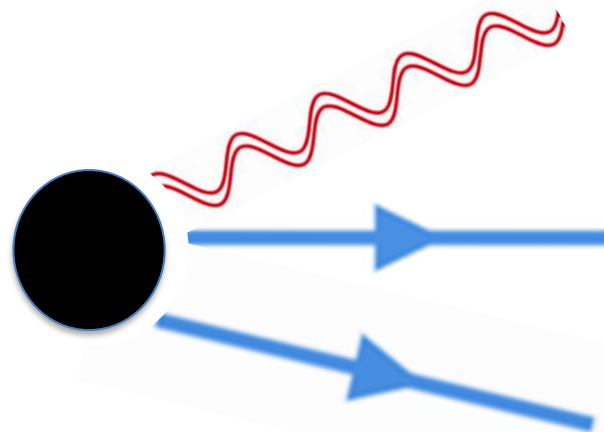
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2.a.3. First order phase transitions



# “Freeze-in” production and inflationary models

**Boltzmann equation:**

$$\frac{d}{dt}n + 3Hn = -\langle\sigma v\rangle(n^2 - n_{\text{EQ}}^2),$$

By assuming that all the DM has been produced during reheating and by modelling this stage with the following evolution:

$$H = H_R \left( \frac{a}{a_R} \right)^\beta, \quad T = T_R \left( \frac{a}{a_R} \right)^\alpha,$$

1. “Standard” reheating:  $\alpha = -3/8$      $\beta = -3/2$

2. Kinaton reheating:  $\alpha = -1$      $\beta = -3$

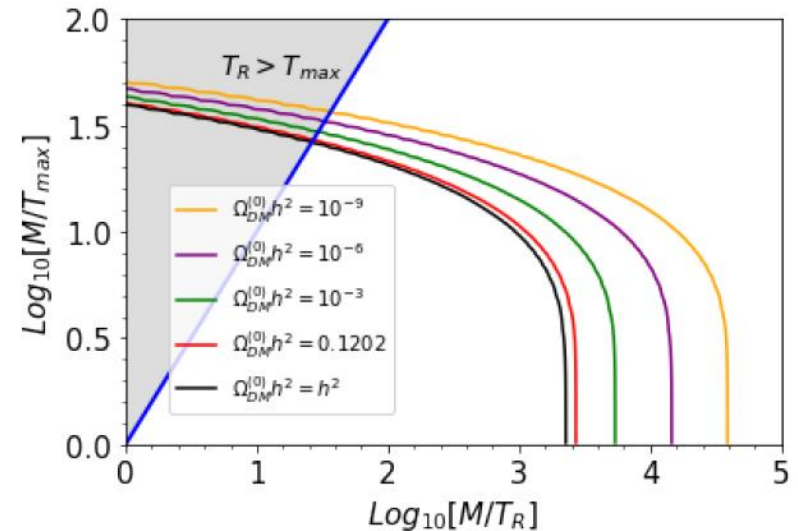
# “Freeze-in” production and inflationary models

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$$H = H_R \left( \frac{a}{a_R} \right)^\beta, \quad T = T_R \left( \frac{a}{a_R} \right)^\alpha,$$

Effective evolution for a model with radiation, inflaton and DM:

$$\begin{aligned} \dot{\rho}_\phi + 3H\rho_\phi + \Gamma_\phi\rho_\phi &= 0, \\ \dot{\rho}_\gamma + 4H\rho_\gamma - (1 - B_\chi)\Gamma_\phi\rho_\phi - \\ - \frac{\langle\sigma|v\rangle}{m_\chi} [\rho_\chi^2 - (\rho_\chi^{\text{EQ}})^2] - \Gamma_\chi(\rho_\chi - \rho_\chi^{\text{EQ}}) &= 0, \\ \dot{\rho}_\chi + 3H\rho_\chi - B_\chi\Gamma_\phi\rho_\phi + \\ + \frac{\langle\sigma|v\rangle}{m_\chi} [\rho_\chi^2 - (\rho_\chi^{\text{EQ}})^2] + \Gamma_\chi(\rho_\chi - \rho_\chi^{\text{EQ}}) &= 0. \end{aligned}$$



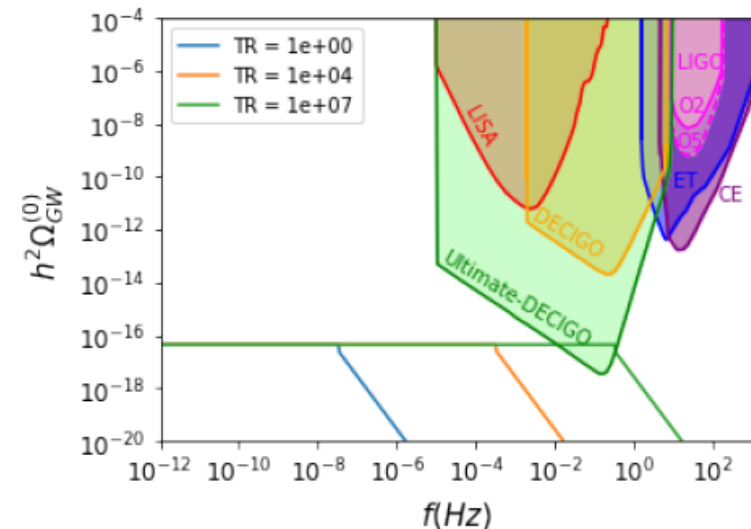
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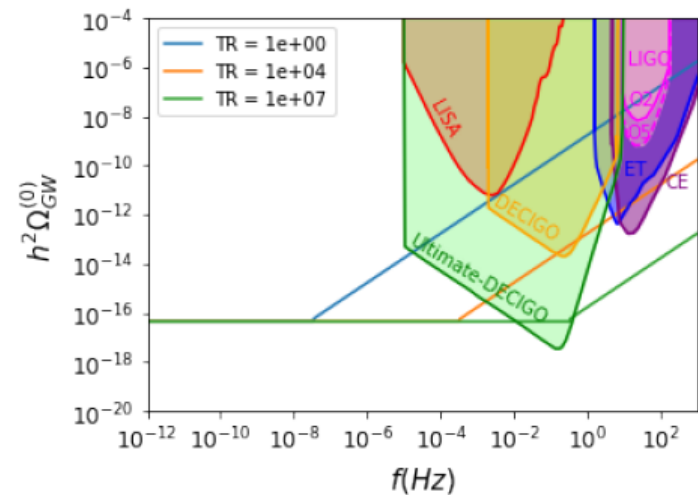
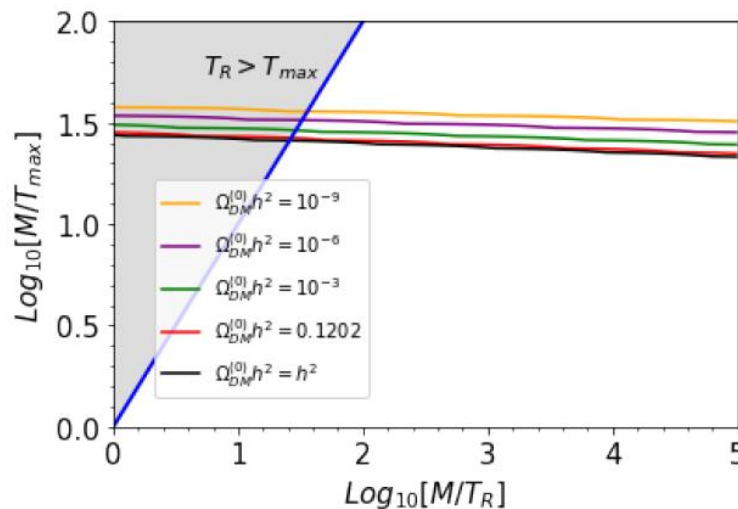
JARC, Mindaugas Karciauskas, 2311.00378 [hep-ph]

# “Freeze-in” production and inflationary models

2. Kinaton reheating:  $\alpha = -1$   $\beta = -3$

$$H = H_R \left( \frac{a}{a_R} \right)^\beta, \quad T = T_R \left( \frac{a}{a_R} \right)^\alpha,$$

Inflation followed by a kinaton dominated stage, radiation and DM.



JARC, Mindaugas Karciauskas, 2311.00378 [hep-ph]

# “Freeze-in” production and inflationary models

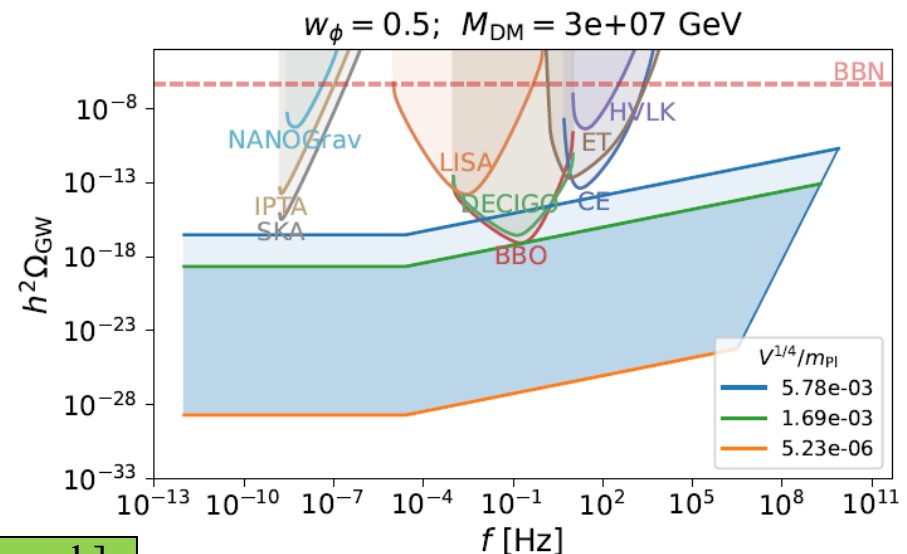
3. Between scenario 1. and 2., there are reheating models with power law minima for the inflaton:

$$V(\phi) \propto \phi^{2n}, \quad w_\phi = \frac{n-1}{n+1}.$$

$$\Omega_{\text{GW}} h^2(f) \simeq \Omega_{\text{GW}}^{\text{rd}} h^2 \times \begin{cases} 1 & f < f_{\text{reh}} \\ \mathcal{A}_s \left( \frac{f}{f_{\text{reh}}} \right)^{-2 \frac{1-3w_\phi}{1+3w_\phi}} & f > f_{\text{reh}} \end{cases},$$

In general:

$$H \simeq H_{\text{I}} \left( \frac{a}{a_{\text{I}}} \right)^{-\frac{3}{2}(1+w_\phi)}$$



# Gravitational waves as an evidence of Dark Matter

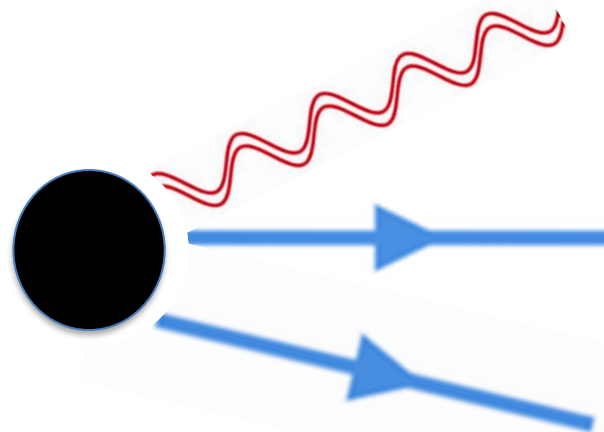
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# Gravitational production of Scalar DM

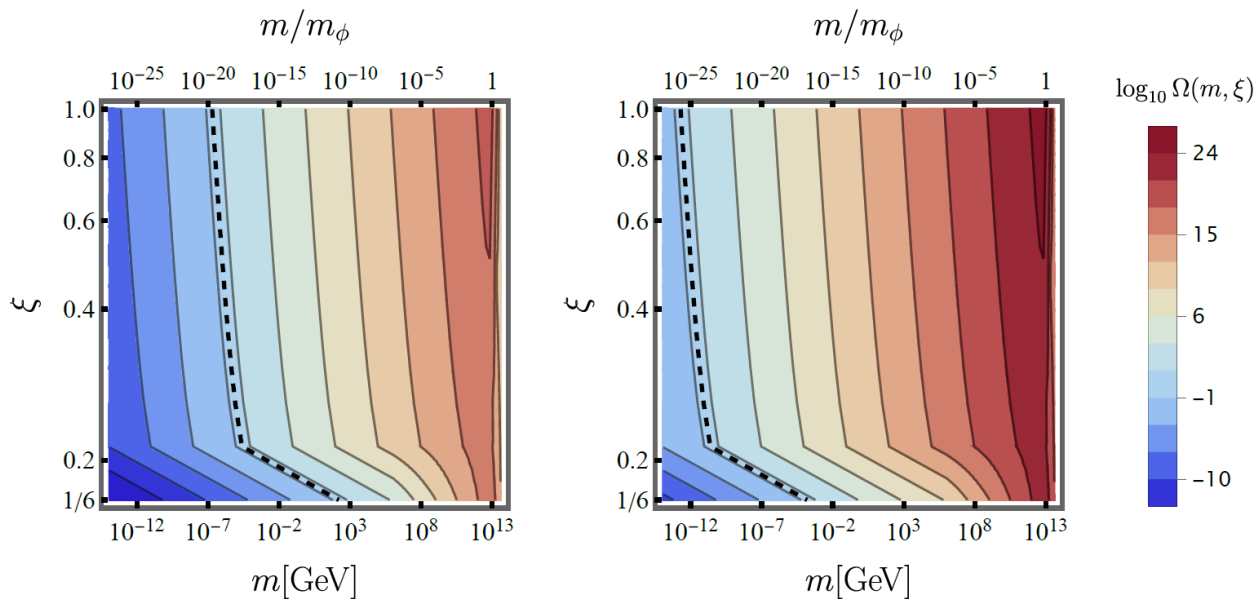
Non-interacting scalar field with action

$$S = -\frac{1}{2} \int d^4x \sqrt{-g} [\partial_\mu \phi \partial^\mu \phi + (m^2 + \xi R) \phi^2]$$

Non-minimal **coupling** to the **curvature**

$$T_{\text{reh}} = 10^{13} \text{ GeV}$$

$$T_{\text{reh}} = 10^{11} \text{ GeV}$$



JARC, L. J. Garay, J.M. Sánchez Velázquez, arXiv:1910.13937 [hep-ph]

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# Gravitational production of vector DM

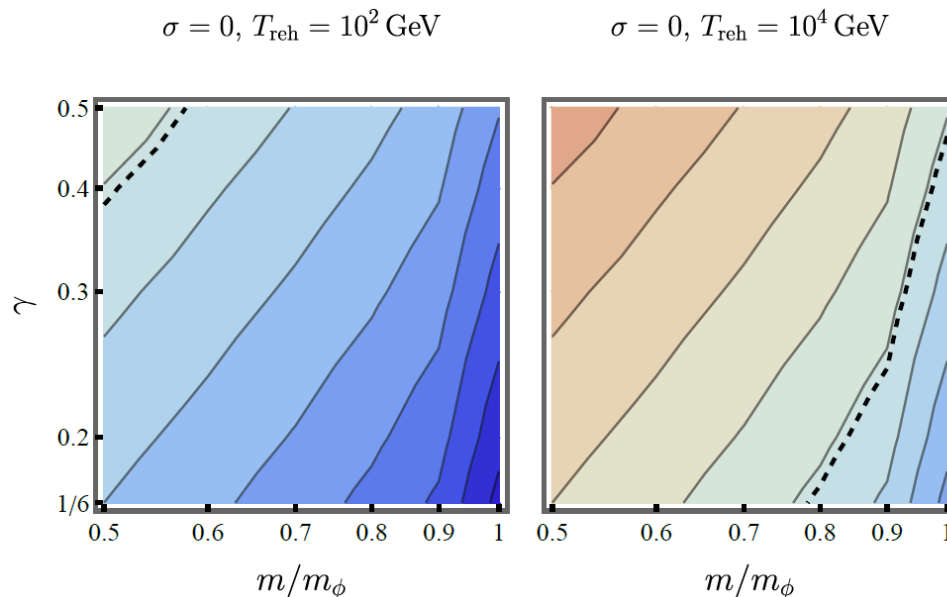
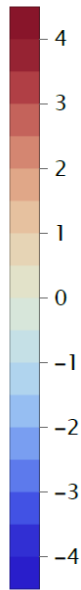
Non-interacting vector field with action

$$S = -\frac{1}{2} \int d^4x \left[ \frac{1}{2} F^{\mu\nu} F_{\mu\nu} + a^2 M^{\mu\nu} A_\mu A_\nu \right]$$

Effective tensor with couplings  $\gamma$  and  $\sigma$

$$M^{\mu\nu} = \eta^{\mu\nu} (m^2 + \gamma R) + \frac{\sigma}{a^2} \tilde{R}^{\mu\nu} \longrightarrow \tilde{R}^{\mu\nu} = R^{\mu\nu} - g^{\mu\nu} R/4$$

$\log_{10} \Omega(m, \gamma, \sigma)$



JARC, L. J. Garay, A. Parra-López, J.M. Sánchez Velázquez, 2310.07515 [gr-qc]

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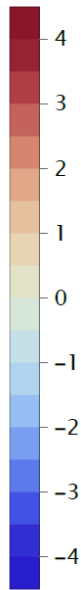
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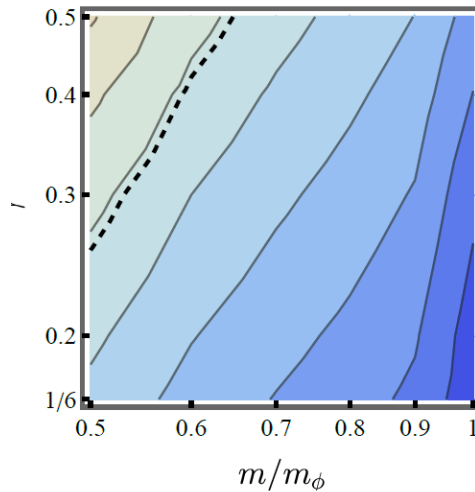
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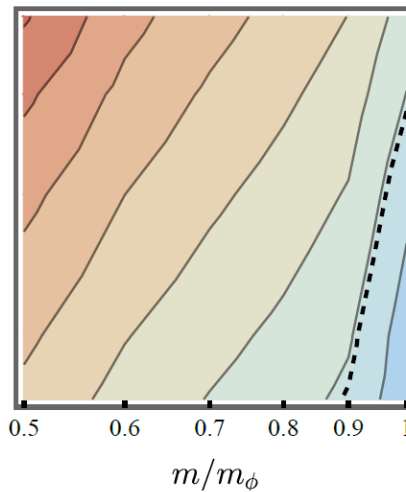
$\log_{10} \Omega(m, \gamma, \sigma)$



$\sigma = -1, T_{\text{reh}} = 10^2 \text{ GeV}$



$\sigma = -1, T_{\text{reh}} = 10^4 \text{ GeV}$



JARC, L. J. Garay, A. Parra-López, J.M. Sánchez Velázquez, 2310.07515 [gr-qc]

# Gravitational waves as an evidence of Dark Matter

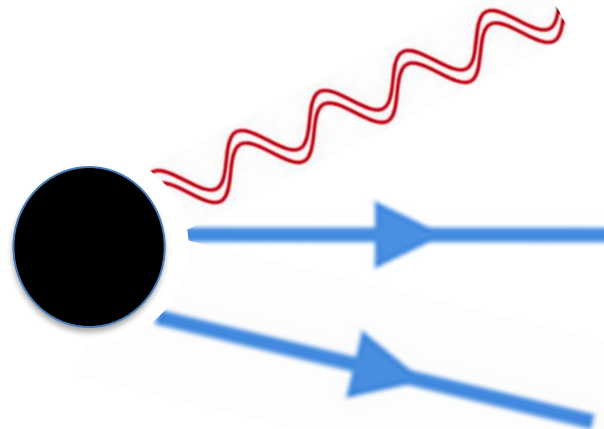
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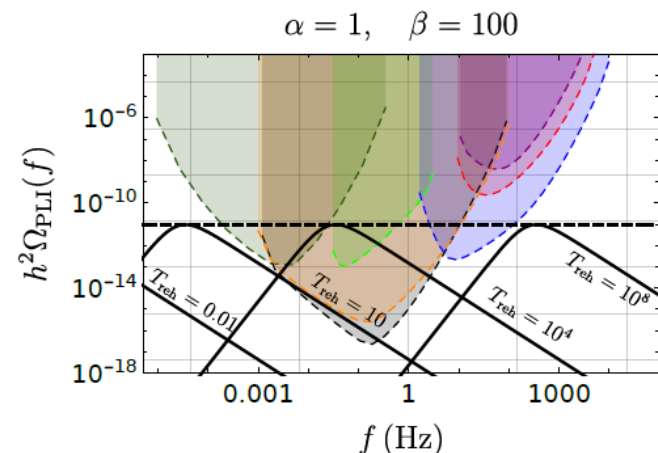
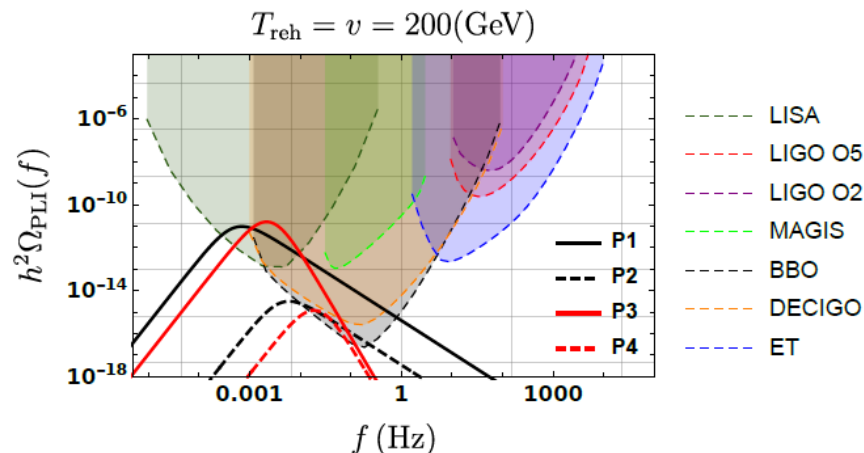


# Production in first order phase transitions

## Dark Matter production by bubble expansion

In this regimen, efficient production of particles with mass:  $M \sim \sqrt{\gamma_w} T_{\text{nuc}}$ ,

This mechanism dominates the one associated to bubble collisions in large portion of parameter space



A. Azatova, M. Vanvlasselaera, W. Yind, JHEP 288 (2021)

J. A. R. Cembranos

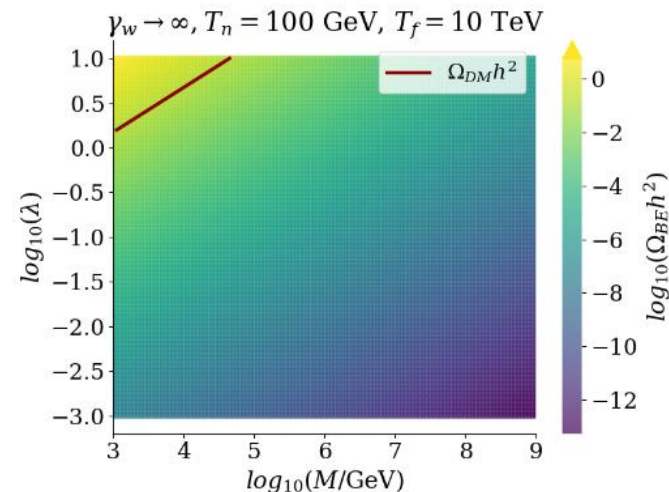
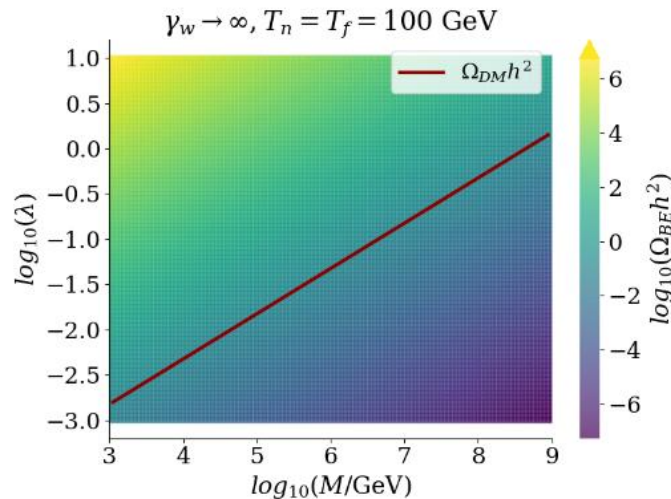
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$$\mathcal{L}_{\text{int}} = -\lambda h^2 \phi^2 / 2$$

$$\Omega_{BE}^0 h^2 = 1,35 \cdot 10^5 \frac{\lambda^2}{g_{\star s}} \frac{v^2}{M_\phi \text{ GeV}} \left( \frac{T_{\text{nuc}}}{T_{\text{reh}}} \right)^3$$

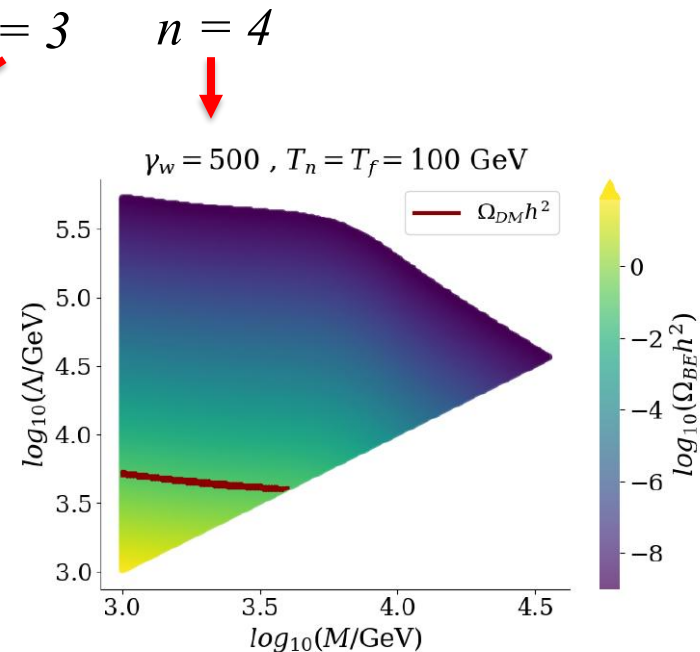
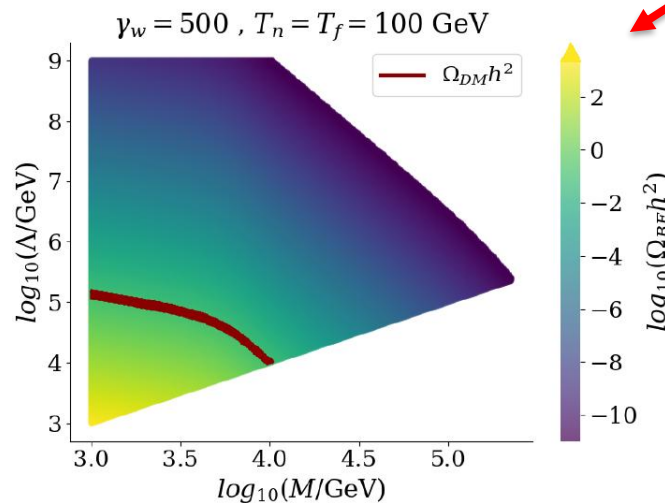


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$$\mathcal{L}_{\text{int}} = \lambda \phi^2 h^n / (n \Lambda^{n-2})$$

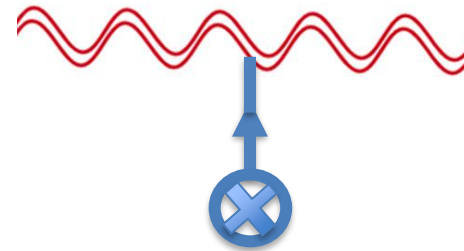


# Gravitational waves as an evidence of Dark Matter

## 2. Gravitational waves directly associated with Dark Matter

### 2.a. Gravitational waves modified by Dark Matter:

#### 2.a.1. Ultralight Dark Matter



### 2.b. GW produced by Dark Matter:

#### 2.b.1. Gravitational decays of Dark Matter



# Ultralight dark matter

**Ultralight Dark Matter related to coherent scalar fields form high density structures (solitons).**

These scalar fields oscillates rapidly with a frequency associated to their mass:  $\phi(\vec{x}, t) = A(\vec{x}, t) \cos[m_\phi t + \alpha(\vec{x}, t)]$ .

Binary systems allow to prove these DM structures by inducing variations in the frequency of the gravitational waves related to a similar effect to the well-known Sachs-Wolfe of the CMB:

$$\frac{\Delta f}{f} = \Psi_N(\vec{x}, t) - \Psi_N(\vec{x}_e, t_e),$$

Ultralight DM modifies the Newtonian potential as

$$\Psi_N(\vec{x}, t) = \Psi_0(\vec{x}) + \Psi_{\text{osc}}(\vec{x}) \cos[\omega t + 2\alpha(\vec{x})], \quad \omega = 2m_\phi.$$

# Ultralight dark matter

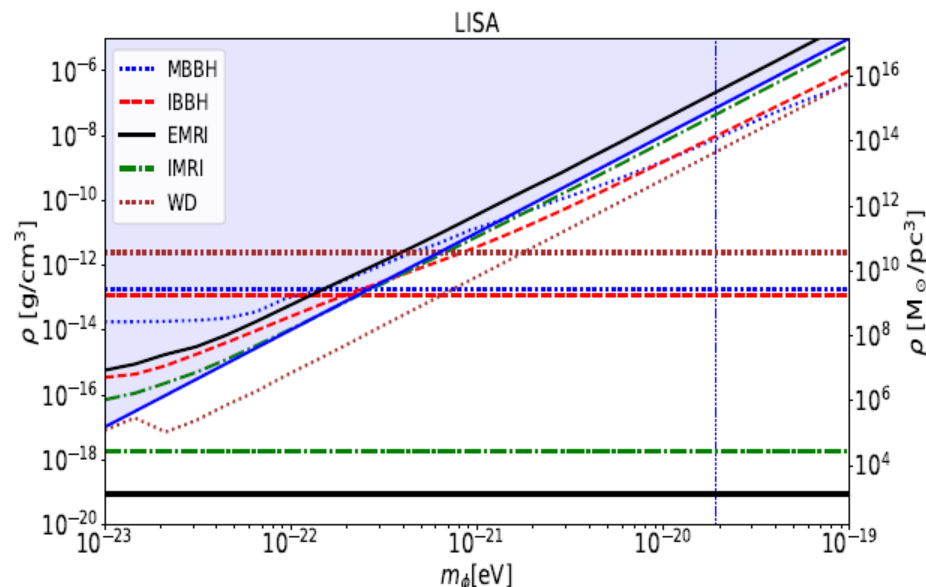
**Ultralight Dark Matter related to coherent scalar fields form high density structures (solitons).**

Identified backgrounds for this signal:

- Impact of the DM halo
- Mass increase effect of compact objects
- Gravitational friction

B. LISA

	$m_1 (M_\odot)$	$m_2 (M_\odot)$	SNR
MBBH	$10^6$	$5 \times 10^5$	$3 \times 10^4$
IBBH	$10^4$	$5 \times 10^3$	708
IMRI	$10^4$	10	64
EMRI	$10^5$	10	22
WD	0.4	0.3	7

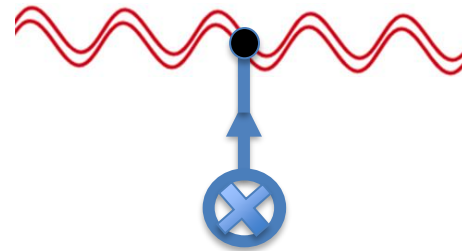


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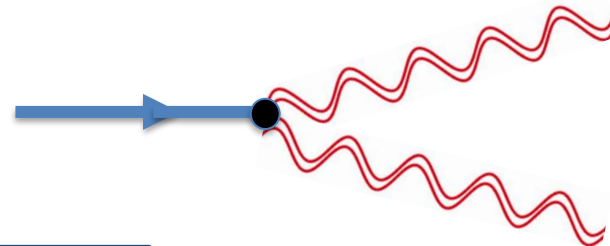
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# Unstable DM decaying into gravitons

## Assumptions:

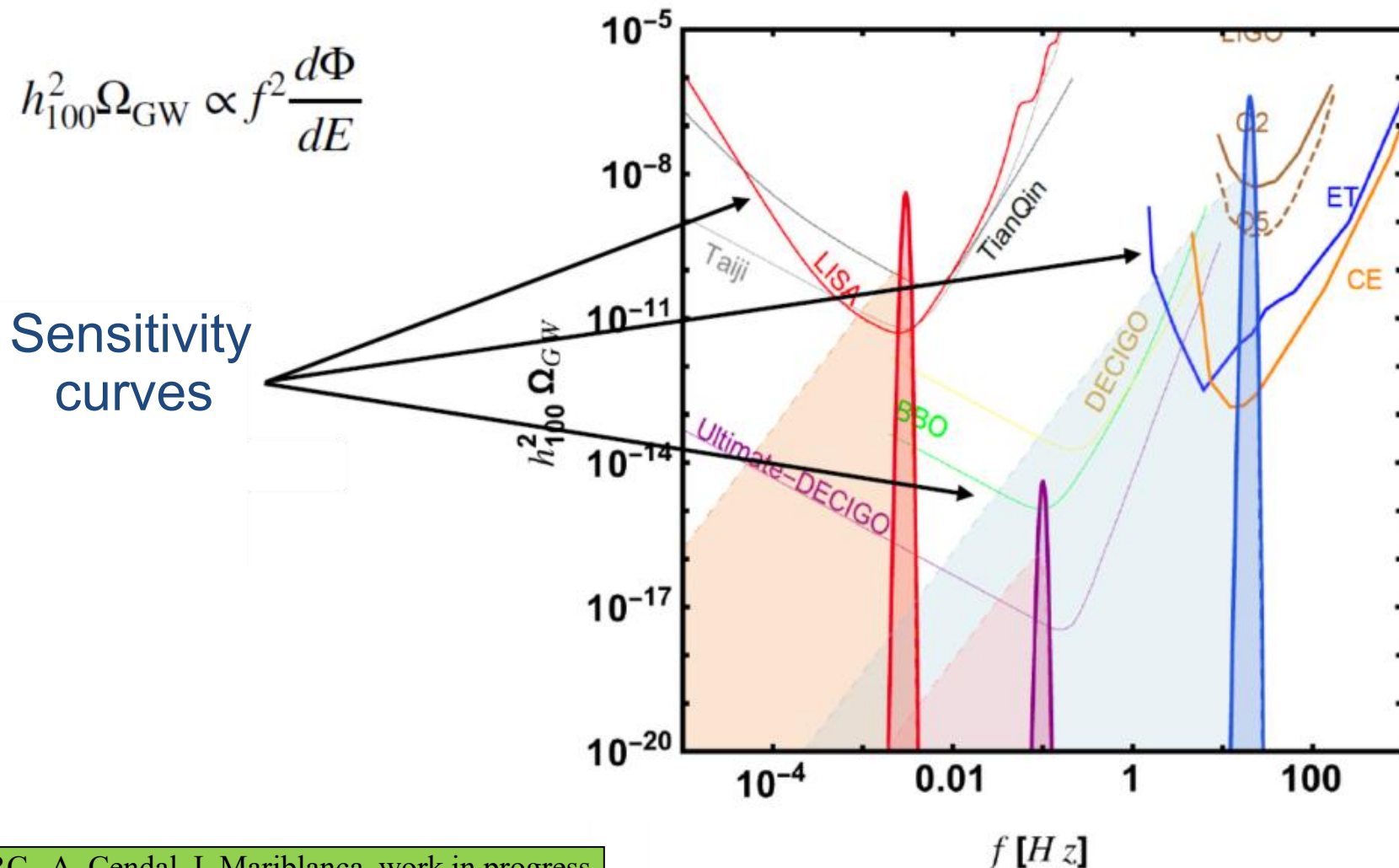
- Unstable DM
- Main decay channel produce gravitons  
Example:  $\phi \rightarrow 2h$  (monochromatic GWs:  $m_\phi/2$ )
- General study in terms of
  - $m_\phi$ : mass of the particle
  - $\tau$ : DM lifetime
- Limits:
  - $m_\phi > 10^{-22}$  eV.
  - $\tau > t_0$ .

## Contributions:

- Extragalactic contribution
- Local contribution

JARC, A. Cendal, I. Mariblanca, work in progress.

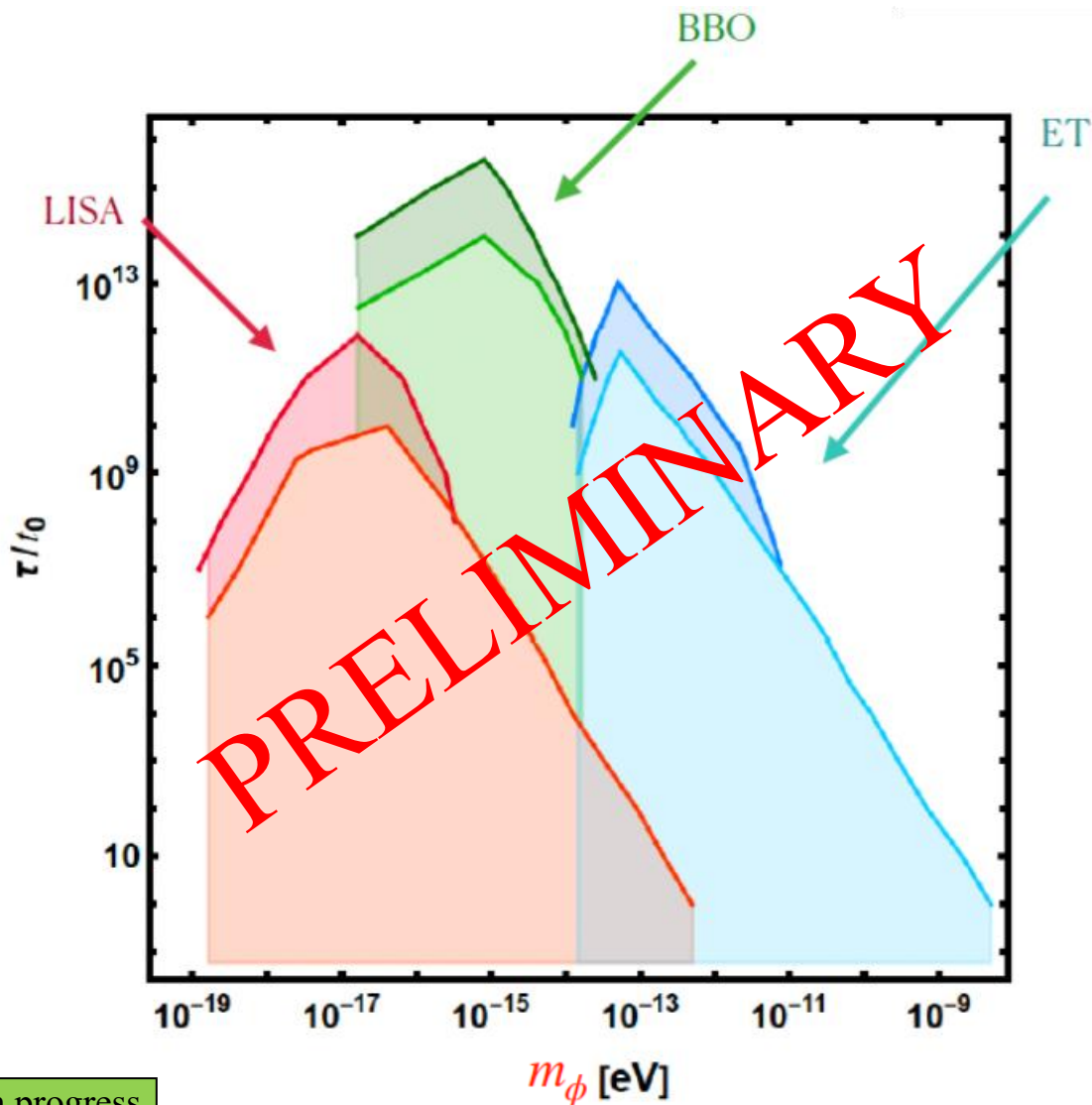
# Unstable DM decaying into gravitons



JARC, A. Cendal, I. Mariblanca, work in progress.

# Unstable DM decaying into gravitons

Range of parameters that allow indirect detection of dark matter with gravitational wave telescopes



JARC, A. Cendal, I. Mariblanca, work in progress.

# Conclusions

**We have discussed the connection between different dark matter models and their gravitational signatures. In particular, they can help to determine features of the dark matter:**

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