



A computing exercise using ROOT

Aim: give a taste of data analysis @ LHC

- What is ROOT ?
 - ROOT is an object-oriented C++ analysis package
 - User-compiled code can be called to produce 1-d, 2-d, and 3-d graphics...



<https://root.cern.ch>

GRASPA 2022 - L. Di Ciaccio - LAPP, 19-26 July 2022

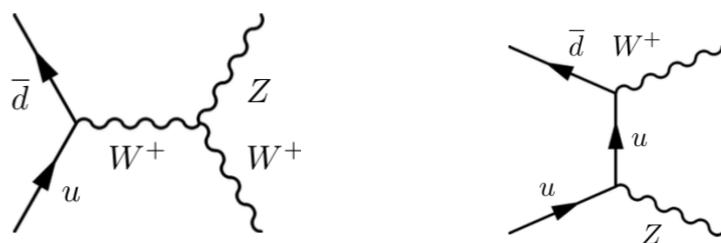
1

Hands-on on diboson physics

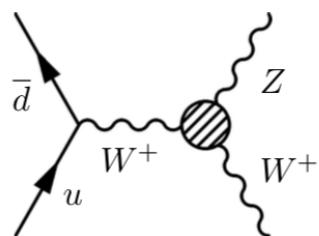


topic @ LHC

Test of SM



Discover New Physics



GRASPA 2022 - L. Di Ciaccio - LAPP, 19-26 July 2022

2

Outline

- Kinematic variables used in the analysis of $p - p$ collisions
- Useful relations
- Concept of invariant mass (example: ‘inclusive’ Z boson production)

- Analysis in $p - p$ collisions :
 - * Signal: Production of a W and a Z $p - p \rightarrow WZ X$
 - * Background: Production of a pair of top-antitop
- Example: Macro.C

In all the following slides we assume the speed of the light

$$c=1$$

Variables used in the analysis of $p - p$ collisions

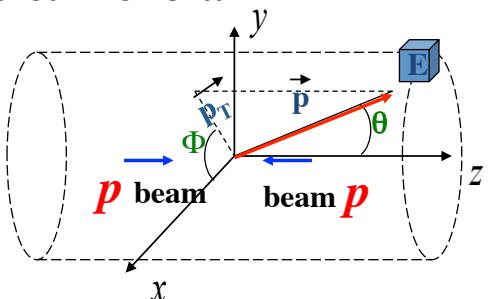
A particle (Z, W, e+, e-, etc ...) is described by its **four-momentum**:

$$\tilde{p} = (E, p_x, p_y, p_z)$$

The particle mass is $m = \sqrt{E^2 - p_x^2 - p_y^2 - p_z^2}$

When dealing with $p\bar{p}$ collisions the following variables are used:

For each particle (Z, W, e+, e-, etc ...):



• 1. Transverse momentum/energy : $\mathbf{p}_T = p \sin \theta$ $E_T = E \sin \theta$

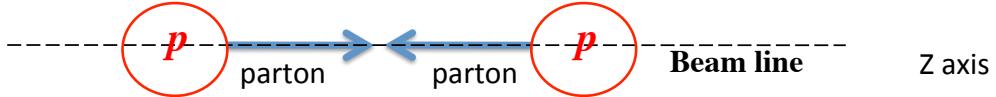
• 2. Rapidity $\mathbf{Y} = \frac{1}{2} \ln \frac{E+p_z}{E-p_z}$

or Pseudorapidity $\eta = -\ln (\tan \frac{\theta}{2})$

• 3. Azimuthal angle Φ Why?

Variables used in the analysis of p - p collisions

Why p_T , η ? Many reasons.



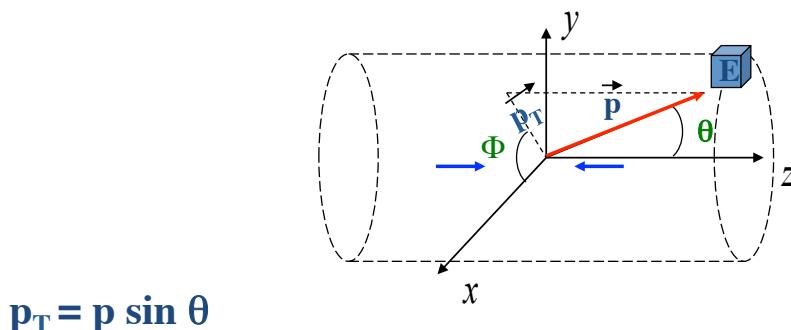
1. p_T and ΔY are invariants for Lorentz transformations along the z axis
2. The longitudinal momentum of an initial parton is ‘unknown’ while we know that $\vec{p}_T^{\text{initial parton}} \sim 0$
→ Exploit momentum conservation
use transverse quantities (in the plane \perp to the beam) → Example:
$$\sum_{\text{initial partons}} \vec{p}_T = \sum_{\text{vis fin}} \vec{p}_T + \sum_{\text{invis fin}} \vec{p}_T \approx 0 \quad \rightarrow \text{Allows to evaluate the } p_T \text{ of not detected (v) particles}$$

$$\sum_{\text{invis fin}} \vec{p}_T = - \sum_{\text{vis fin}} \vec{p}_T \quad |\sum_{\text{invis }} \vec{p}_T| \text{ is the “missing } E_T \text{”}$$
3. The “interesting” physics is due to hard scattering processes → high p_T particles (selection of high p_T particles assures “interesting” physics)

GRASPA 2022 - L. Di Ciaccio - LAPP, 19-26 July 2022

5

Useful relations



$$p_T = p \sin \theta$$

$$\begin{aligned} px &= p_T * \cos(\Phi); \\ py &= p_T * \sin(\Phi); \\ pz &= E * \tanh(\eta); \end{aligned} \quad \eta = -\ln(\tan \frac{\theta}{2})$$

NB:

- $m \ll E \rightarrow Y \approx \eta$ (η doesn't require particle identification)
- $m \ll E \rightarrow p_T \approx E_T \quad E_T = E \sin \theta$

Concept of *invariant mass*: inclusive Z boson production

$p - p \rightarrow Z (X)$

With $Z \rightarrow e^+e^-$

(X) = part1, part2, part3, ...

Very 'clean' processes (low bkg)!!

Invariant mass M_{ee} of ee system from the

4-momentum conservation

(it allows to measure the Z mass, M_Z):

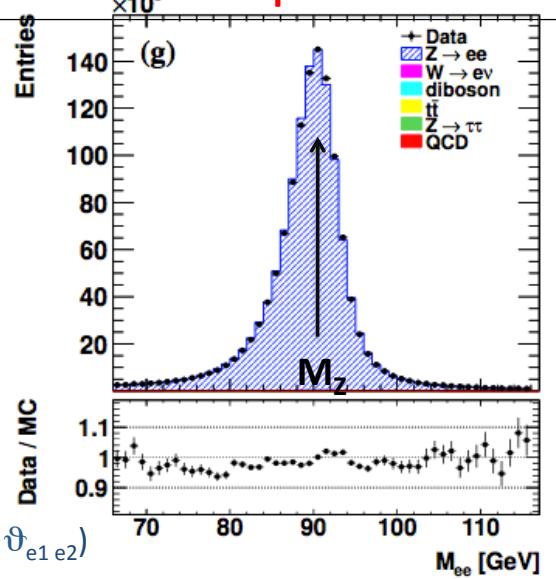
$$\tilde{p}_Z^2 = (\tilde{p}_{e1} + \tilde{p}_{e2})^2$$

$$M_{ee}^2 = (\tilde{p}_{e1} + \tilde{p}_{e2})^2 \approx 2(E_{e1}E_{e2} - |\vec{p}_{e1}| |\vec{p}_{e2}| \cos \vartheta_{e1e2})$$

$$M_{ee} \approx \sqrt{2E_{e1}E_{e2}(1-\cos \vartheta_{e1e2})}$$

(the electron mass is neglected)

Why M_{ee} gives a distribution
and not a single value?



- 1. $\Delta E * \Delta t > \hbar/2$ $\Delta m * \tau > \hbar/2$
 $\Gamma * \tau > \hbar/2$
 width lifetime
- 2. Experimental resolution

GRASPA 2022 - L. Di Ciaccio - LAPP, 19-26 July 2022

7

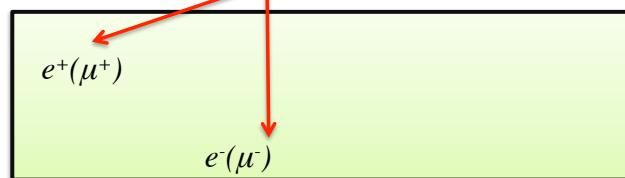
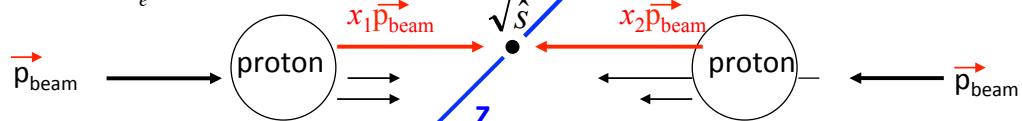
Our signal : production of a W and a Z

$p - p$ 'hard' collisions in the $q_1 \bar{q}_2$ center of mass:

$p - p \rightarrow W Z (X)$

Our 'signal'

With $Z \rightarrow e^+e^-$
and $W \rightarrow e^+\nu_e$



$$E_{beam} = \sqrt{s}/2 \approx p_{beam}$$

x_i = fraction of the beam momentum carried by
the parton i

Kinematics of $p - p$ collisions

* 4-mom of the initial partons : $[(x_1+x_2)E_{beam}, 0, 0, (x_1-x_2)p_{beam}]$

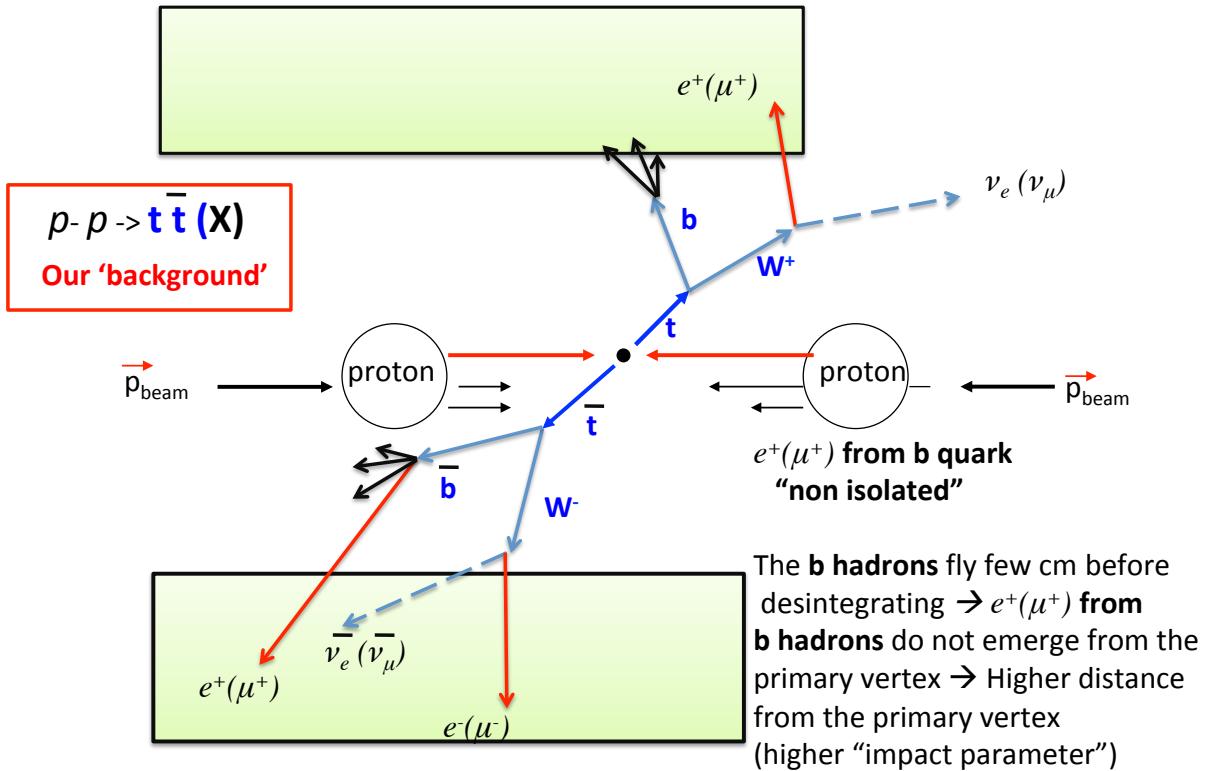
$$0 < x_{1,2} < 1$$

GRASPA 2022 - L. Di Ciaccio - LAPP, 19-26 July 2022

8

Our background: Production of a pair of top-antitop

p - p 'hard' collisions. In the $q_1 \bar{q}_2$ center of mass:



GRASPA 2022 - L. Di Ciaccio - LAPP, 19-26 July 2022

9

Aim of the exercise (note, this are steps of an analysis):

- 1) look at some important variables,
- 2) build the Z invariant mass,
- 3) how one can discriminate between the 'signal' and the 'background' ?

You will have:

GRASPA2022explanation.pptx.pdf (this slides)

Exercise2022.pdf (what we ask to do)

Selected_All_EEM.root (« data » (simulated data))

macro.C (draft of an analysis program)

macro_final.C (solution: final analysis program)

[https://root.cern.ch/root/html/doc/guides/primer\(ROOTPrimer.html](https://root.cern.ch/root/html/doc/guides/primer(ROOTPrimer.html)

1) an input file containing the physics: **Selected_All_EEM.root**

```
==== MOST ENERGETIC LEPTON FROM THE Z  
Br 4 :pt1 : pt1  
Br 5 :etal1 : etal1  
Br 6 :phi1 : phi1  
Br 7 :E1 : E1  
  
==== SECOND ENERGETIC LEPTON FROM THE Z  
Br 8 :pt2 : pt2  
Br 9 :eta2 : eta2  
Br 10 :phi2 : phi2  
Br 11 :E2 : E2  
  
==== LEPTON FROM W  
Br 12 :pt3 : pt3  
Br 13 :eta3 : eta3  
Br 14 :phi3 : phi3  
Br 15 :E3 : E3
```

List of variables given per each collision event (kinematics of the final state leptons)

11

2) Instructions to make the computing exercise : **Exercise2022.pdf**



COMPUTING EXERCISE

Study of the production of a pair of gauge bosons (W and Z) at the LHC

The data to analyse are organised into a 'Root n-tuple' which we will provide to you. The Root n-tuple is a file containing information about the kinematics of "events", each resulting from a proton-proton interaction.

These events have three leptons (electrons or muons) and are of two kinds:

12

3) A skeleton of an analysis program using ROOT: macro.C

```
#include "TCanvas.h"
#include "TROOT.h"
#include "TFile.h"
#include "TTree.h"
#include "TBrowser.h"
#include "TH2.h"
#include "TRandom.h"

void tree1r()
{
    // Read Selected_All_EEM.root file
    //Root file
    TFile *f = new TFile("Selected_All_EEM.root");

    // Signal events
    TTree *sig = (TTree*)f->Get("WZSignal");
    Double_t pt1, eta1, phi1, E1;
    Double_t pt2, eta2, phi2, E2;
    Double_t pt3, eta3, phi3, E3;
    Double_t MZ, MET, trackd0cutWMu, TrackIsoWmu;
    Double_t Weight;

    //get some variables for SIGNAL EVENTS
    sig->SetBranchAddress("pt1",&pt1);
```

GRASPA 2022 - L. Di Ciaccio - LAPP, 19-26 July 2022

13

Example of analysis program

macro.C

23/07/2013 00:21

```
#include "TCanvas.h"
#include "TROOT.h"
#include "TFile.h"
#include "TTree.h"
#include "TBrowser.h"
#include "TH2.h"
#include "TRandom.h"

void tree1r()
{
    // Read Selected_All_EEM.root file
    //Root file
    TFile *f = new TFile("Selected_All_EEM.root");

    // Signal events
    TTree *sig = (TTree*)f->Get("WZSignal");
    Double_t pt1, eta1, phi1, E1;
    Double_t pt2, eta2, phi2, E2;
    Double_t pt3, eta3, phi3, E3;
    Double_t MZ, MET, trackd0cutWMu, TrackIsoWmu;
    Double_t Weight;

    //get some variables for SIGNAL EVENTS
    sig->SetBranchAddress("pt1",&pt1);
    sig->SetBranchAddress("eta1",&eta1);
    sig->SetBranchAddress("phi1",&phi1);
    sig->SetBranchAddress("E1",&E1);
    sig->SetBranchAddress("MZ",&MZ);
    sig->SetBranchAddress("Weight",&Weight);
    // add other variables ...
```

Header files

Open the input file

Access the Signal info

Define the name
variables per each SIGNAL lepton

GRASPA 2022 - L. Di Ciaccio - LAPP, 19-26 July 2022

14

```

////get some variables for BACKGROUND EVENTS
TTree *ttbar = (TTree*)f->Get("ttbar");
Double_t pt1_bkg, eta1_bkg, phi1_bkg, E1_bkg;
Double_t MZ_bkg;
Double_t Weight_bkg;

//get some variables for ttbar
ttbar->SetBranchAddress("pt1",&pt1_bkg);
ttbar->SetBranchAddress("eta1",&eta1_bkg);
ttbar->SetBranchAddress("phi1",&phi1_bkg);
ttbar->SetBranchAddress("E1",&E1_bkg);
ttbar->SetBranchAddress("MZ",&MZ_bkg);
ttbar->SetBranchAddress("Weight",&Weight_bkg);
// add other variables ...

//create two histograms (for sig and ttbar)
TH1F *h_MZ    = new TH1F("h_MZ","MZ distribution All events",40,65,115);
TH1F *h_MZ_bkg = new TH1F("h_MZ_bkg","MZ distribution BKG",40,65,115);
TH1F *h_MZ_sig = new TH1F("h_MZ_sig","MZ distribution SIG",40,65,115);

//read all SIGNAL entries and fill the histograms
Int_t nentries = (Int_t)sig->GetEntries();

for (Int_t i=0;i<nentries_bkg;i++) {
    ttbar->GetEntry(i);
    h_MZ_bkg->Fill(MZ_bkg,Weight_bkg);
    h_MZ->Fill(MZ_bkg,Weight);
}

```

Access the background info

**Define the name
variables per each bkg lepton**

Loop on events

Page 1 of 2

GRASPA 2022 - L. Di Ciaccio - LAPP, 19-26 July 2022

15

```

// example how Draw and save histograms
TCanvas *c = new TCanvas();
c->cd();
h_MZ_sig->Draw();
h_MZ_bkg->SetLineColor(kRed);
h_MZ_bkg->Draw("same");

c->Print("test_MZ.eps");
}

void macro()
{
    tree1r();
}

```

Draw and save histograms

Main program

To start root you may type:

root -l

root [1] .x macro.C

and look at what you get

Useful in-line commands:

```
TFile f("Selected_All_EEM.root");
f.ls();
WZSignal->Scan();
WZSignal->Print();
```

[https://root.cern.ch/root/html/doc/guides/primer\(ROOTPrimer.pdf](https://root.cern.ch/root/html/doc/guides/primer(ROOTPrimer.pdf)

Have fun !!

