



# Neutrino cross sections and their impact on oscillation measurements

Margherita Buizza Avanzini

# Layout

1. Neutrino cross section in neutrino oscillation (accelerator) experiments
2. Neutrino interactions and nuclear effects
3. Neutrino cross-section measurements
4. Neutrino cross-section extraction
5. How cross-section measurements are used in LBL experiments
6. Future perspectives

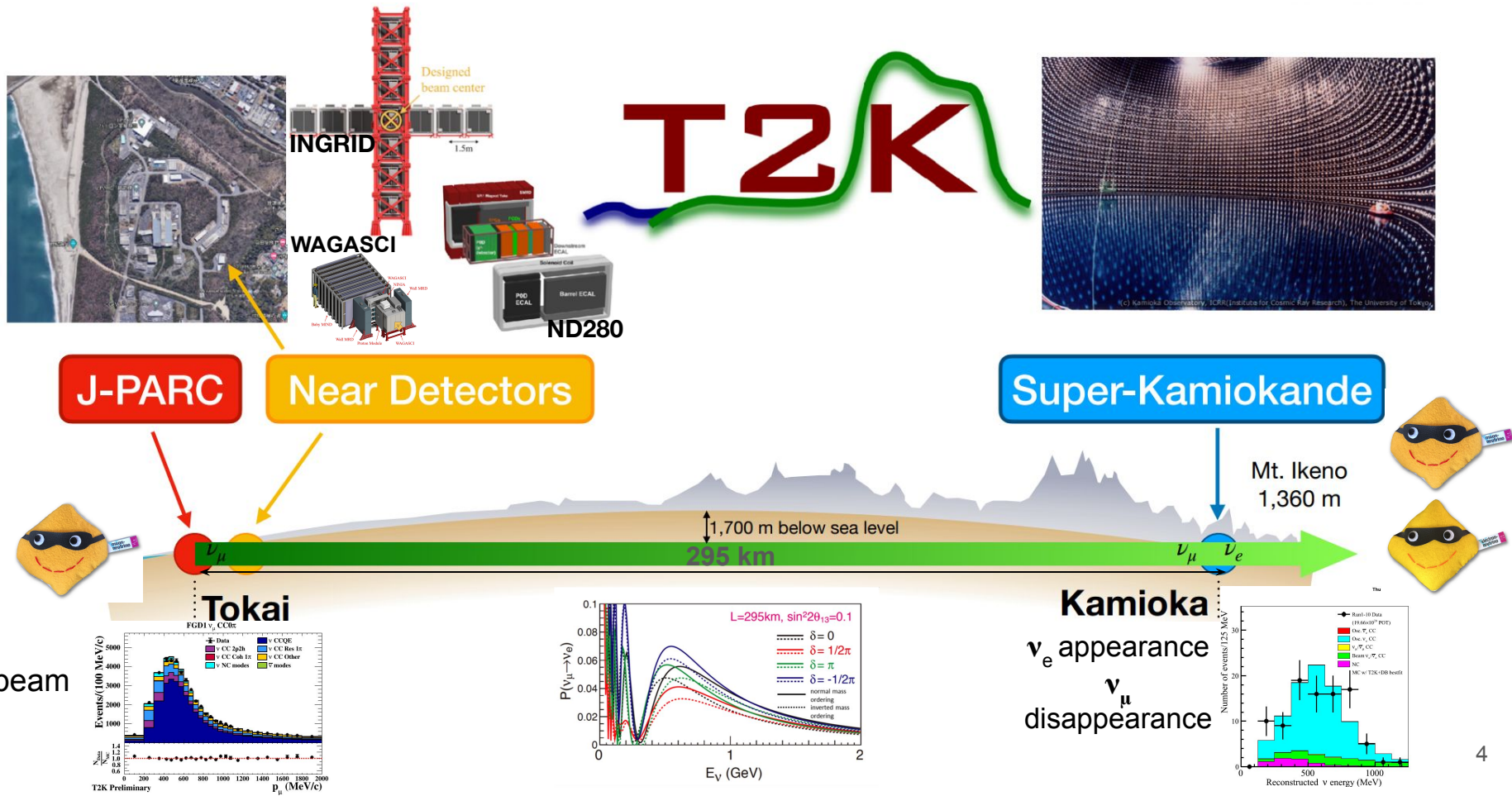
Caveat 1: personal choice on treated subjects

Caveat 2: most of materials taken from my personal activity in T2K

Caveat 3: impossible to cover everything in 90min ;-)

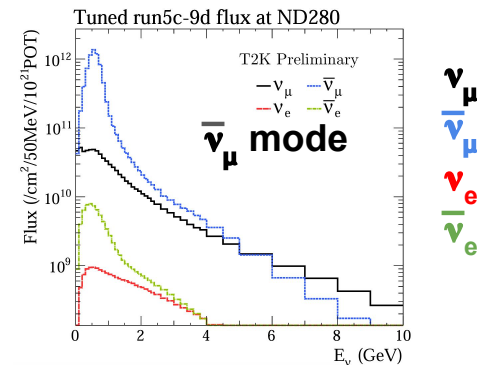
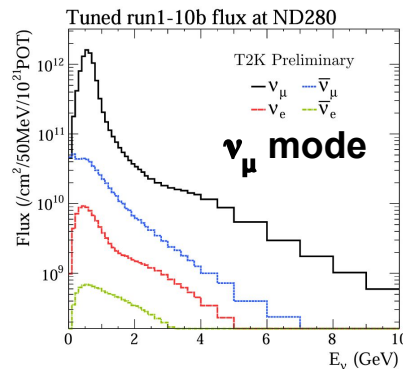
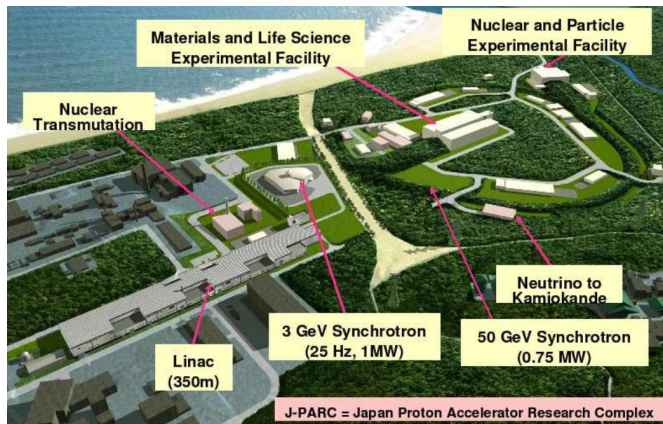
# Neutrino cross sections in LBL experiments

# Long baseline experiment principle





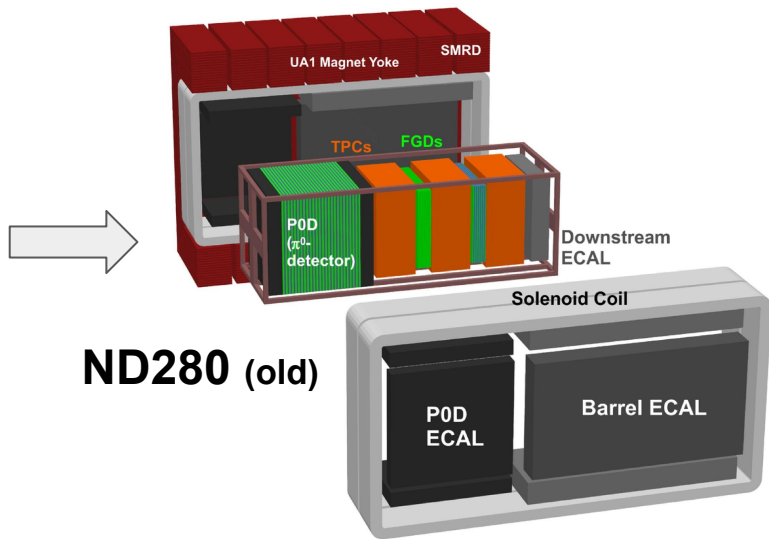
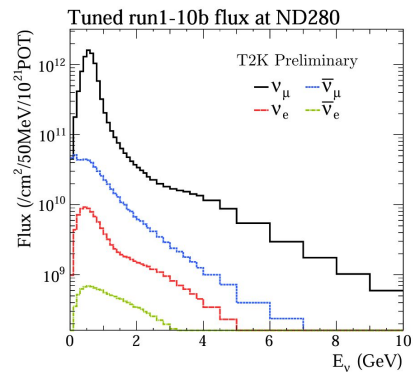
# A typical $\nu$ LBL oscillation experiment (exemple from T2K)



$\nu_\mu$   
 $\bar{\nu}_\mu$   
 $\nu_e$   
 $\bar{\nu}_e$

We start by  
producing a muon  
(anti-)neutrino beam  
at the accelerator

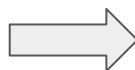
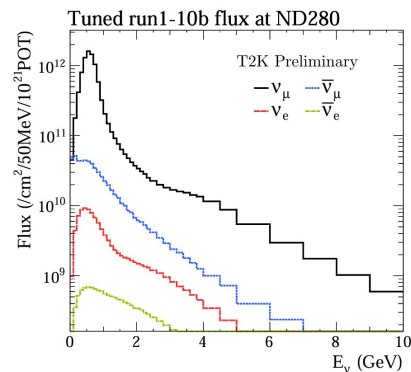
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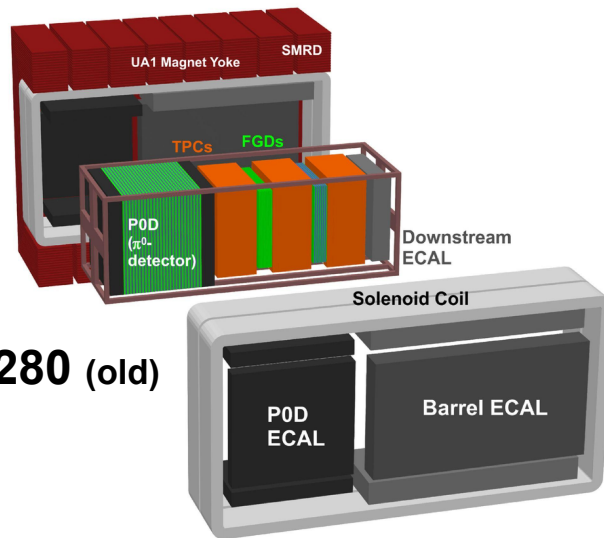
Produced muon  
(anti-)neutrinos first  
interact with our near  
detector matter

The target material is  
essentially made of  
plastic scintillator

# A typical $\nu$ LBL oscillation experiment (exemple from T2K)



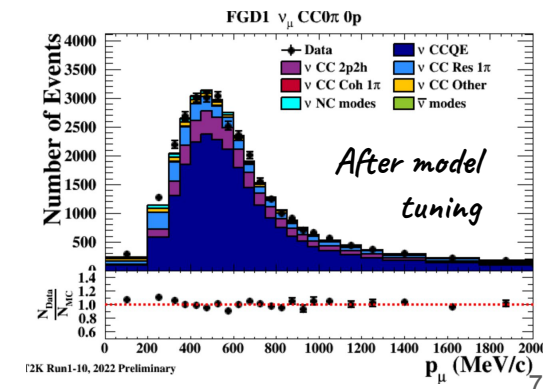
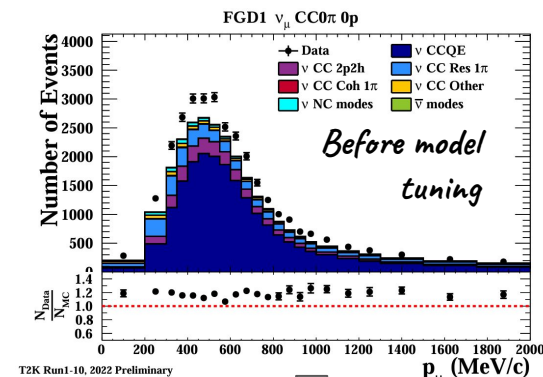
**ND280 (old)**



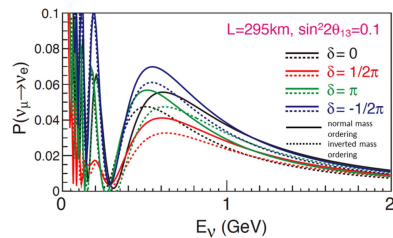
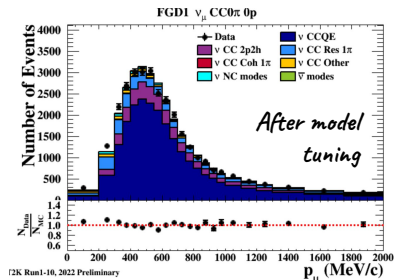
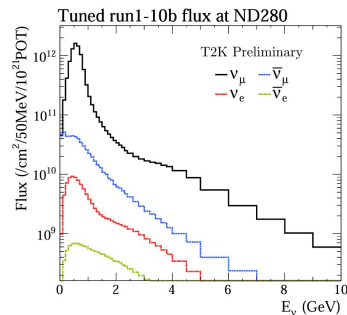
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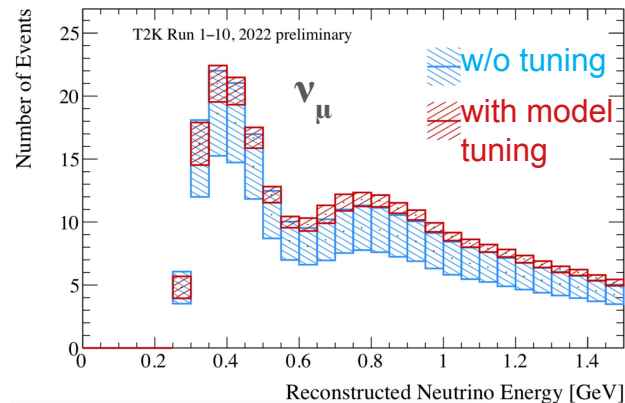
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# A typical $\nu$ LBL oscillation experiment (exemple from T2K)



& after oscillations

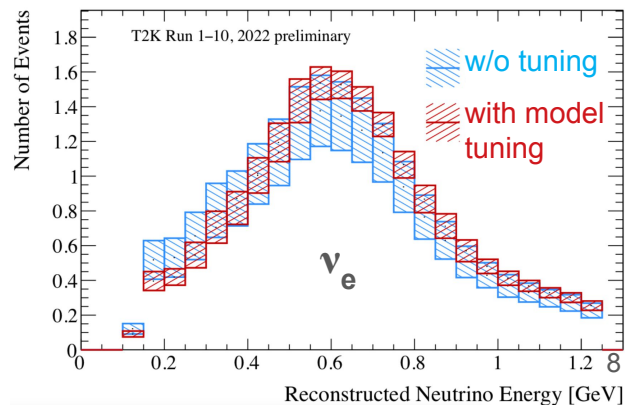
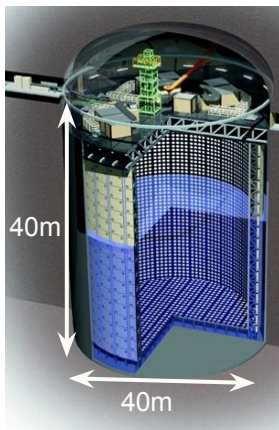


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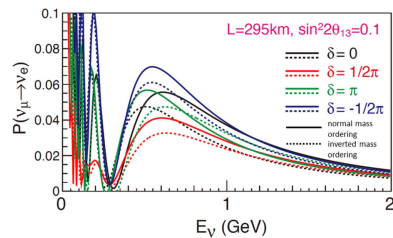
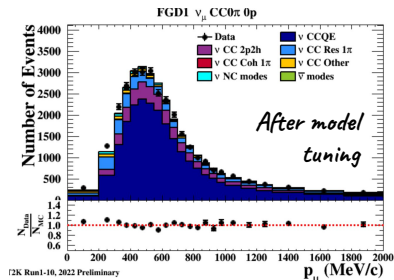
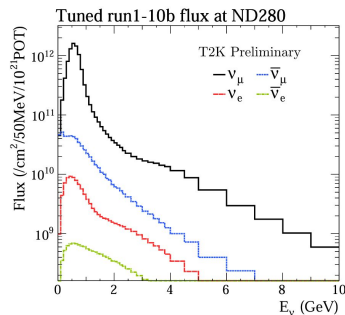
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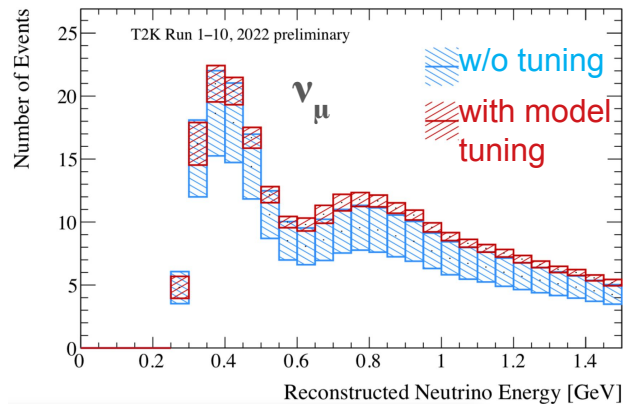
Super-Kamiokande,  
water cherenkov  
detector



# A typical $\nu$ LBL oscillation experiment (exemple from T2K)



& after oscillations

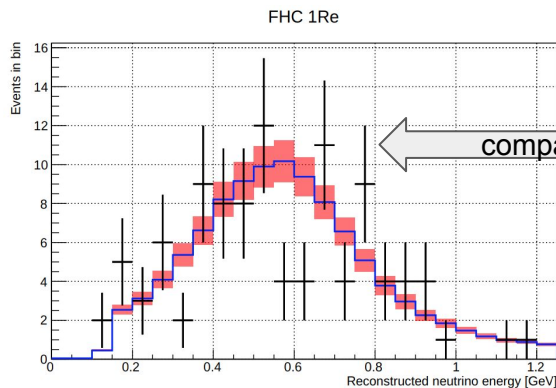


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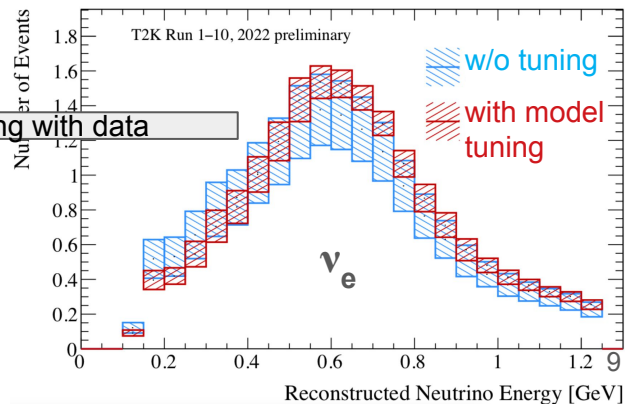
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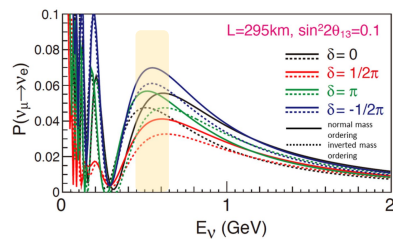
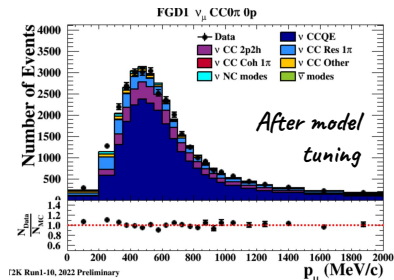
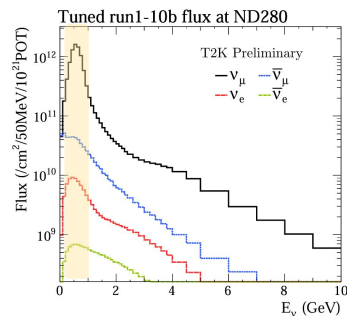
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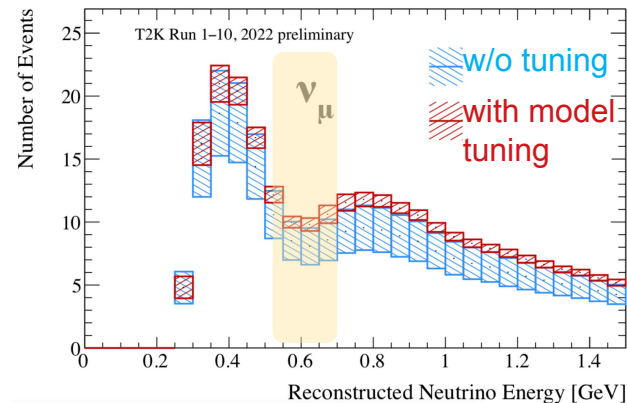
comparing with data



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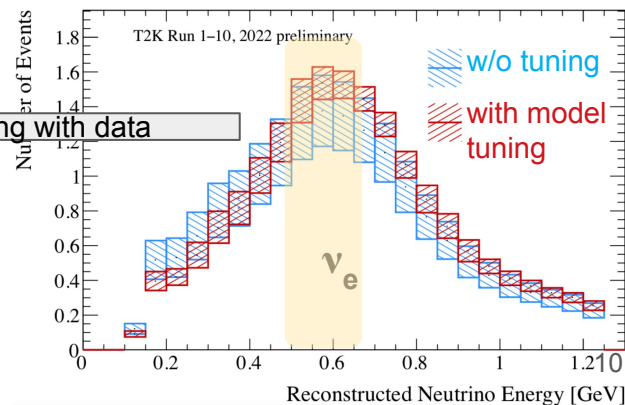
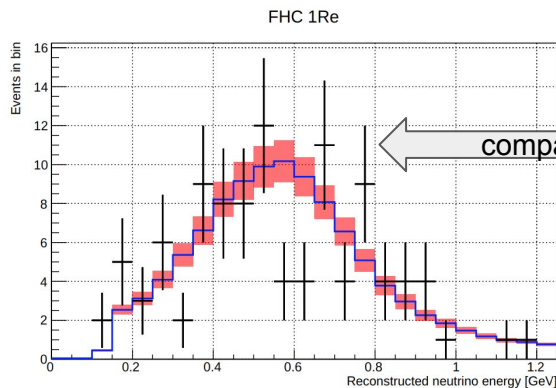


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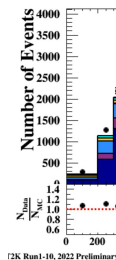
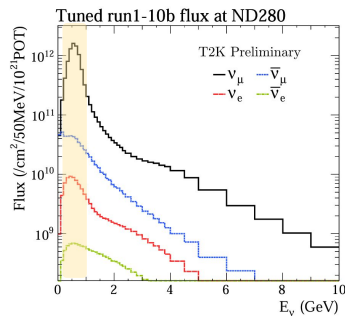
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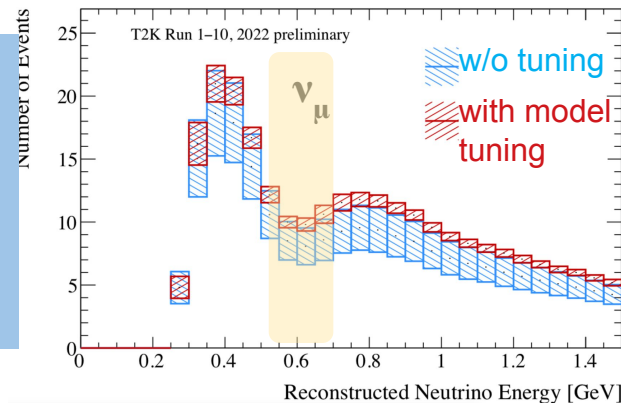




# A typical $\nu$ LBL oscillation experiment (exemple from T2K)



WOW! that's really clever!

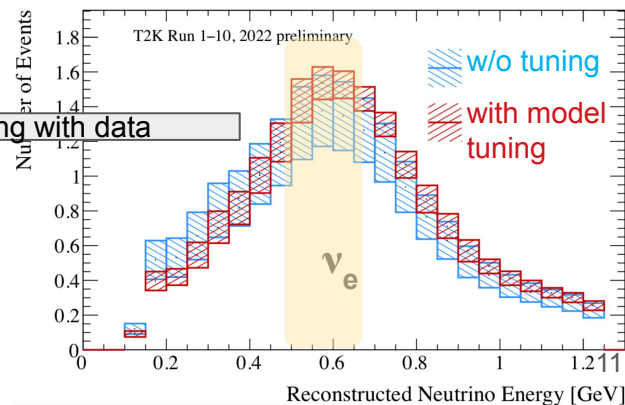
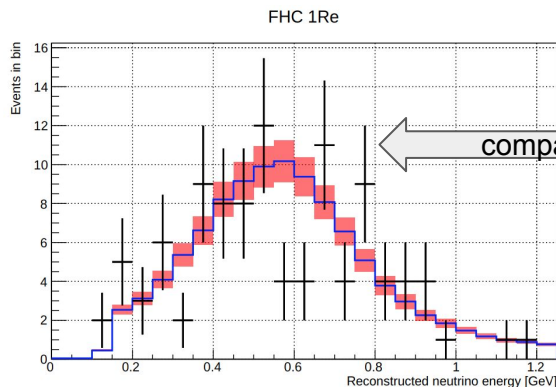


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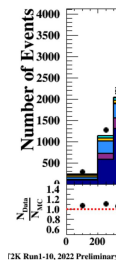
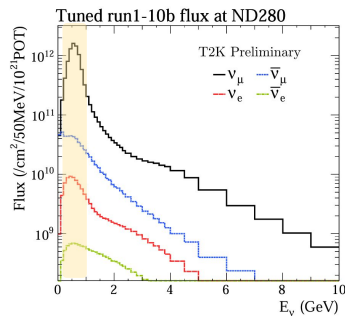
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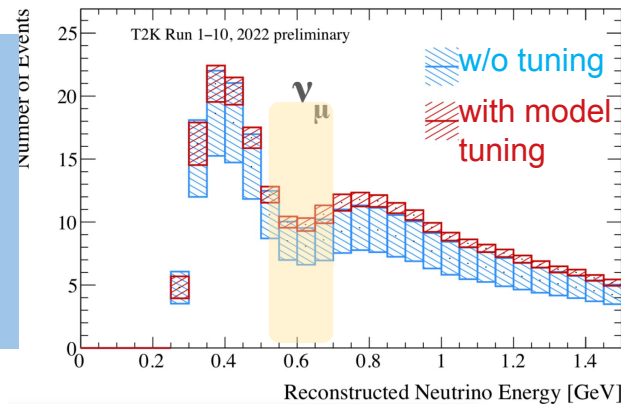
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WOW! that's really clever!



Well nothing strange here?

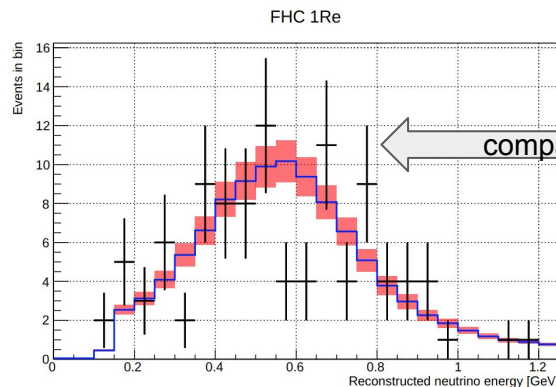


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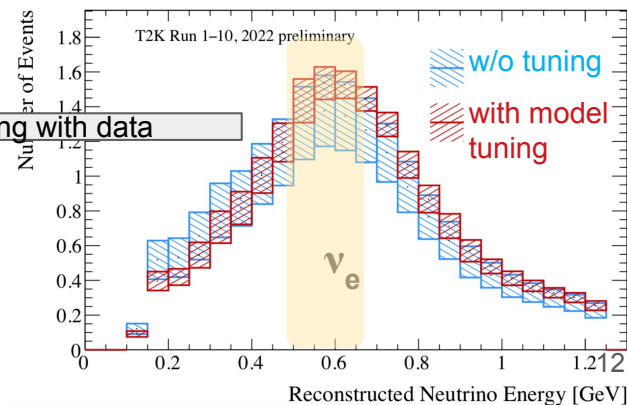
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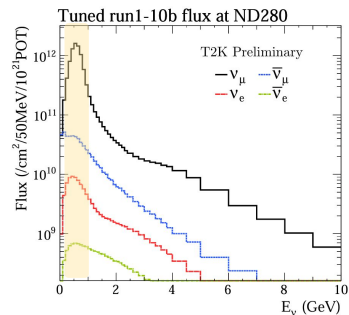


comparing with data





# A typical $\nu$ LBL oscillation experiment (exemple from T2K)



Produced muon (anti-)neutrinos interact with our near detector and we measure their flux

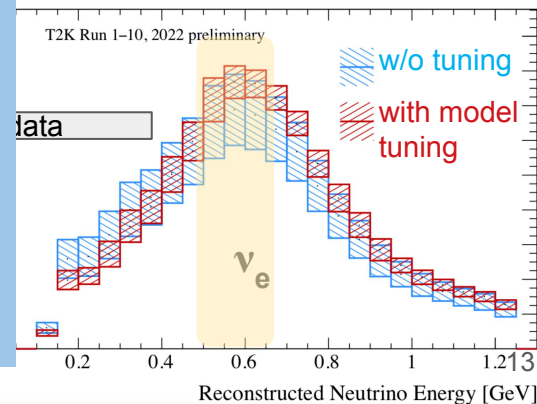
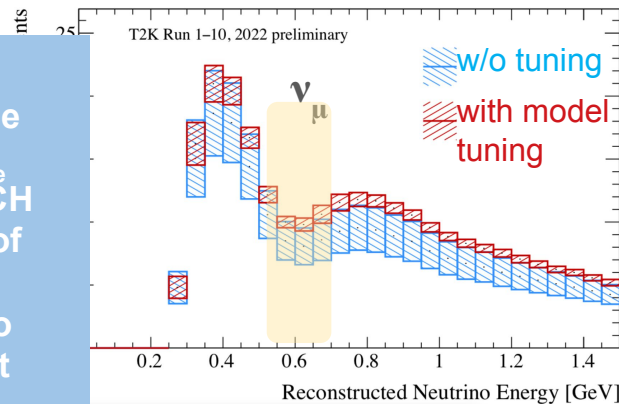
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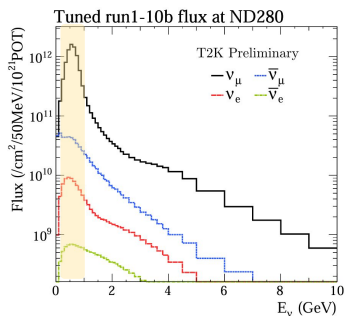
Finally, comparing the predicted spectra to real data, we extract the oscillation parameters

## Non-exhaustive list of challenges:

1. at the near detector we characterise  $\nu_\mu$  but at the far detector we are particularly interested in  $\nu_e$
2. at the near detector we have a dominance of CH target, while the far detector is entirely made of water
3. at the near detector we characterise a neutrino beam before the oscillation, while the shape at the far detector is definitely different



# A typical $\nu$ LBL oscillation experiment (exemple from T2K)



Produced muon (anti-)neutrinos interact with our near detector

We adjust the flux & neutrino in model predictions on the near data

We then use the tuned models to predict the  $\nu_\mu$  &  $\bar{\nu}_\mu$  spectra at the detector

Finally, comparing the real data, we extract oscillation parameters

## Non-exhaustive list of challenges:

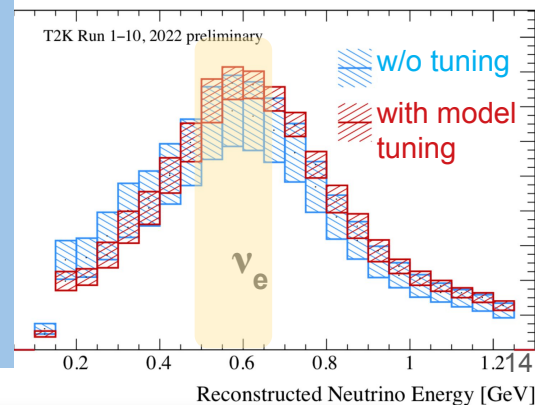
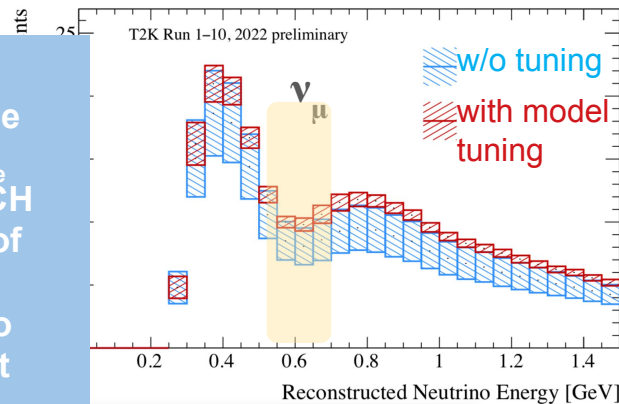
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⇒ all these aspects require an extrapolation from the near to the far detector

⇒ this extrapolation is usually based on theoretical models for neutrino interactions

⇒ we need very solid neutrino interaction models

Are we ready?



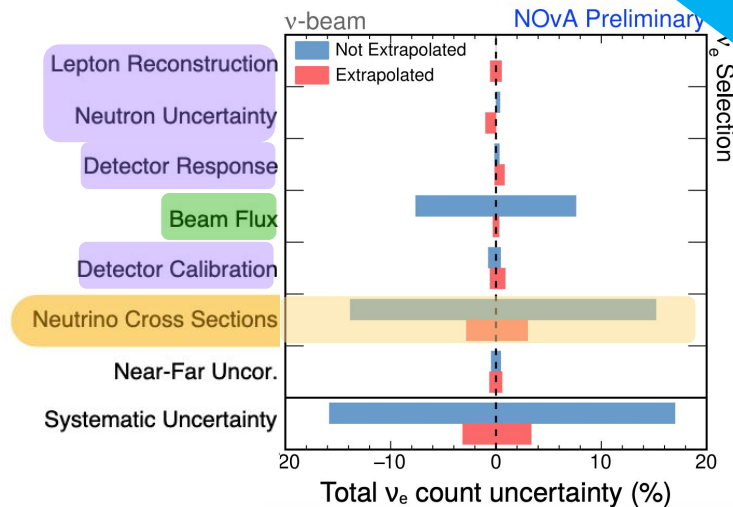
# Why neutrino cross sections matter?

Neutrino 2024 conference

T2K

NOVA

Error source	$\nu_e$ appearance
Flux	2.8
$\nu$ cross section (ND tuned)	3.8
$\nu$ cross section untunable	2.9
SK detector	2.7
Total	4.9



J. Wolcott @Neutrino2024

Neutrino interaction uncertainties are the ~ dominant source of systematics in current long-baseline experiments

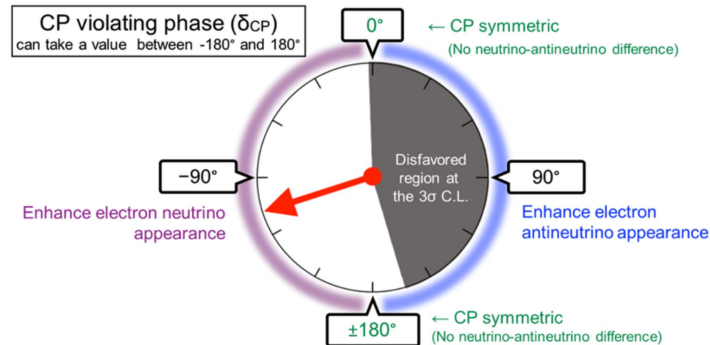
$$\frac{N_{events}^{far}(\vec{x})}{N_{events}^{near}(\vec{x})} = \frac{\sigma(E_\nu, \vec{x}) \otimes \Phi^{far}(E_\nu) \otimes D^{far}(\vec{x}) \otimes P_{osc}(E_\nu)}{\sigma(E_\nu, \vec{x}) \otimes \Phi^{near}(E_\nu) \otimes D^{near}(\vec{x})}$$

Today not the major problem, we have ~150  $\nu_e$  appearance events... but this will become a problem soon (Hyper-Kamiokande, DUNE)

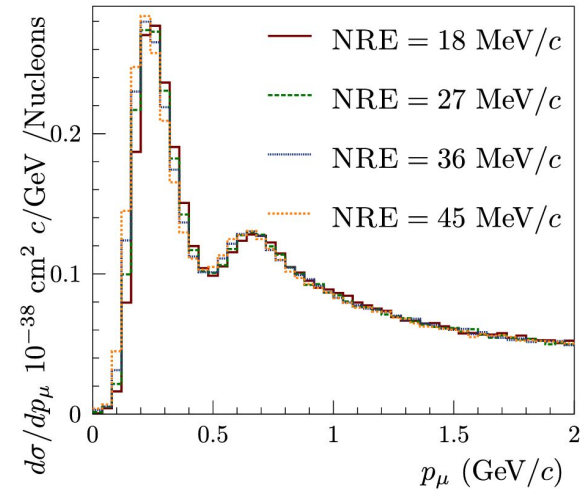
# Concrete exemple from T2K



Publishing on Nature (in 2020) the first hints toward a CP violation



c	1e0de $\nu$ -mode	1e0de $\bar{\nu}$ -mode
$\nu_\mu \rightarrow \nu_e$	59.0	3.0
$\bar{\nu}_\mu \rightarrow \bar{\nu}_e$	0.4	7.5
Background	13.8	6.4
Total predicted	73.2	16.9
Systematic uncertainty	8.8%	7.1%
Data	75	15



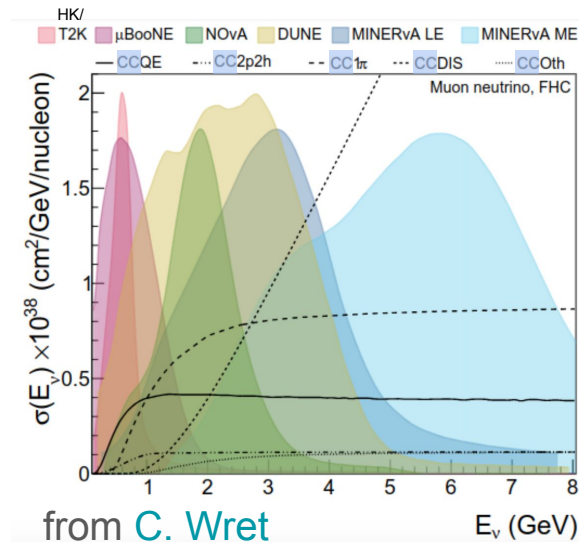
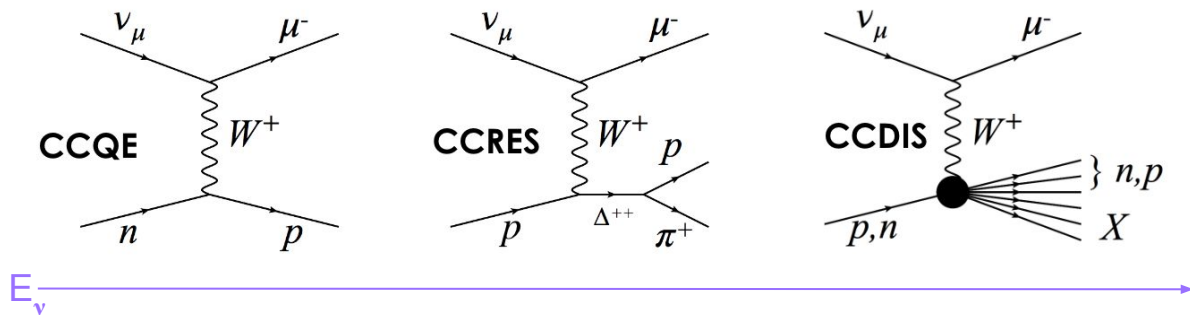
For that analysis, over a total 9% systematics in the appearance channel, 8% effect came by the uncertainties on the Nucleon Removal Energy (NRE)

*Lot of work has been done since then, but neutrino interactions remain the main reason of systematics uncertainties in LBL experiments*

# Neutrino interactions

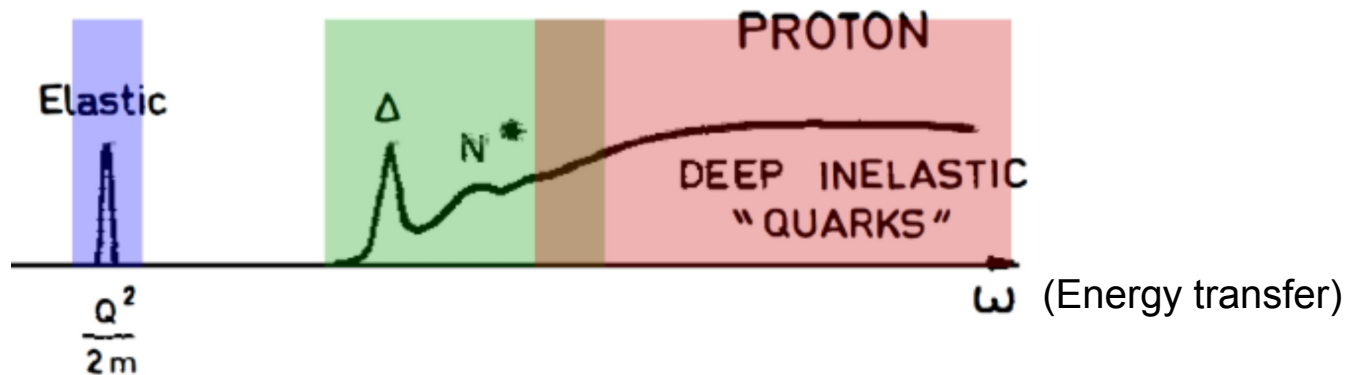
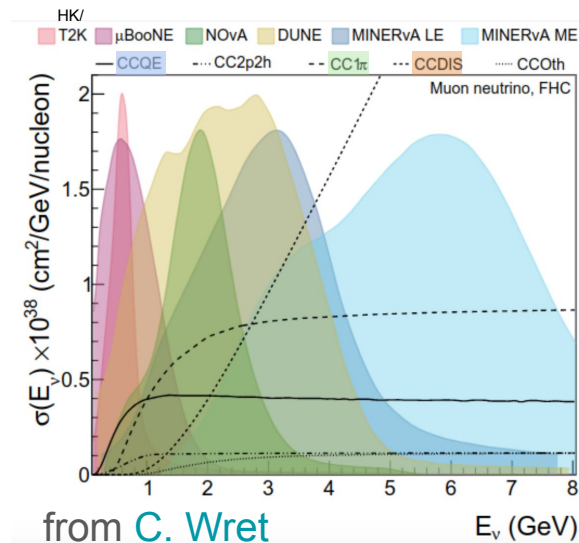
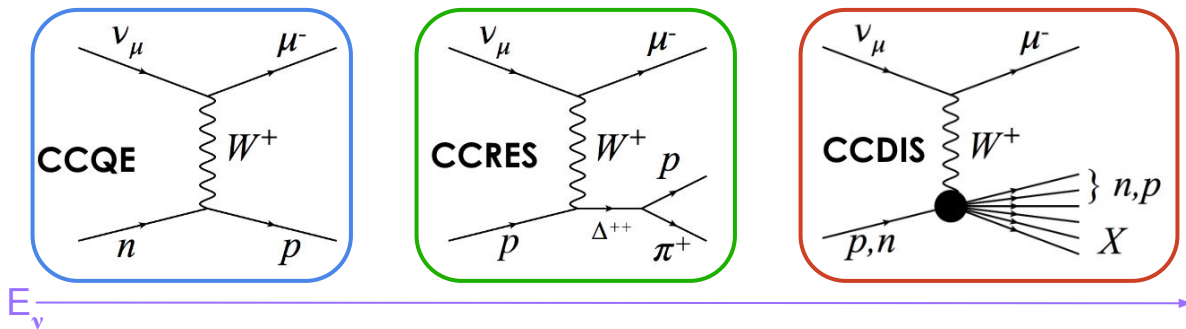
# Neutrino-nucleon interactions

Our current detectors are especially sensitive to **Charged Current** interactions. Depending on the incoming flux ( $E_\nu$ ), different interactions are the most probable:



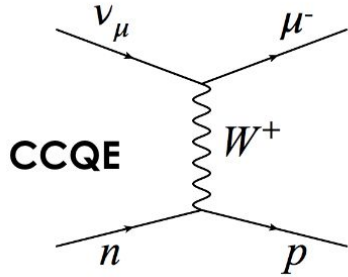
# Neutrino-nucleon interactions

Our current detectors are especially sensitive to **Charged Current** interactions. Depending on the incoming flux ( $E_\nu$ ) or on the energy transfer ( $\omega$ ), different interactions are the most probable:



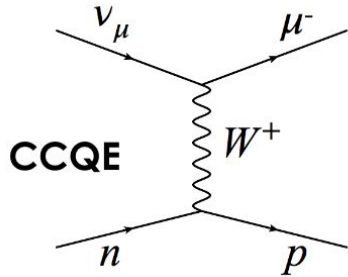
# Charged Current Quasi Elastic (CCQE)

Let's start with the “easiest” **neutrino-nucleon** interaction: the so-called CCQE. This is an interaction widely used in accelerator experiments





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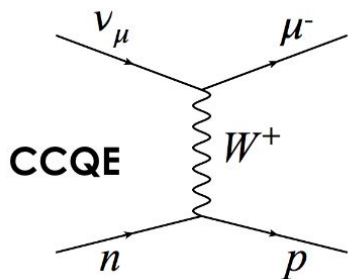
General cross-section formula

$$\frac{d\sigma}{dQ^2} = \frac{1}{64\pi M^2 E_\nu^2} |\mathcal{M}|^2$$

nucleon mass       $\nu$  energy      Interaction amplitude

$$Q^2 = (p_\nu - p_\mu)^2 = \text{momentum transfer (to the nucleon)}$$

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Interaction  
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nucleon mass      ν energy

$$|\mathcal{M}|^2 = \frac{G_F^2 \cos^2 \theta_C}{2} L^{\mu\nu} H_{\mu\nu}$$

$$Q^2 = (p_\nu - p_\mu)^2 = \text{momentum transfer (to the nucleon)}$$

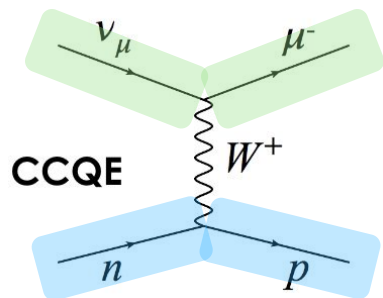
Specifically for CCQE:

$$\mathcal{M} = \frac{G_F \cos \theta_C}{\sqrt{2}} [\bar{u}_\mu \gamma^\mu (1 - \gamma^5) u_\nu] \cdot \langle p | J_\mu^{\text{had}} | n \rangle$$

$$G_F = 1.1803 \times 10^{-5} \text{ GeV}^{-2}, \quad \cos \theta_c = 0.97425$$

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Fermi constant      Cabibbo angle      Hadronic part (4x4 tensor)

Leptonic part (4x4 tensor)

$$Q^2 = (p_\nu - p_\mu)^2 = \text{momentum transfer (to the nucleon)}$$

Specifically for CCQE:

$$\mathcal{M} = \frac{G_F \cos \theta_C}{\sqrt{2}} [\bar{u}_\mu \gamma^\mu (1 - \gamma^5) u_\nu] \cdot \langle p | J_\mu^{\text{had}} | n \rangle$$

Leptonic current (4-vector)      Hadronic current (4-vector)

Remember: only for left handed ν ; -)  
(or right-handed ν̄)

$$G_F = 1.1803 \times 10^{-5} \text{ GeV}^{-2}, \quad \cos \theta_c = 0.97425$$

# Charged Current Quasi Elastic (CCQE)

## Hadronic current

$$\langle p | J_\mu^{\text{had}} | n \rangle = \bar{u}_p \left[ F_1(Q^2) \gamma_\mu + F_2(Q^2) i \sigma_{\mu\nu} \frac{q^\nu}{2M} + F_A(Q^2) \gamma_\mu \gamma_5 + F_P(Q^2) q_\mu \gamma_5 \right] u_n$$

Various nucleon form factors to take into account that nucleons have a structure (they are not point like)

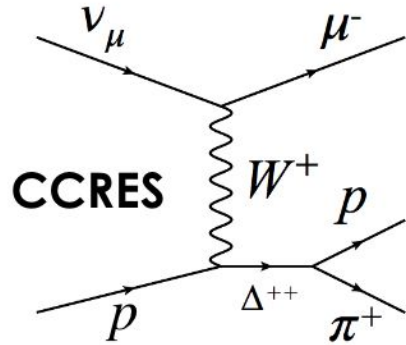
$F_1$  and  $F_2$  are related to the vector part of the interaction (as in the electromagnetic interaction, similar between electrons and neutrinos).  $F_1$  is related to the nucleon electric charge distribution,  $F_2$  to the magnetic moment

$F_A$  and  $F_P$  are related to the axial part of the interaction (specific to neutrinos). In particular  $F_A$ , the most relevant for us, describes how the axial component of the interactions “distributes” within the nucleon

*Dipole description*

$$F_A(Q^2) = \frac{F_A(0)}{\left(1 + \frac{Q^2}{(M_A^{QE})^2}\right)^2}$$

# Charged Current Resonant (CCRES)

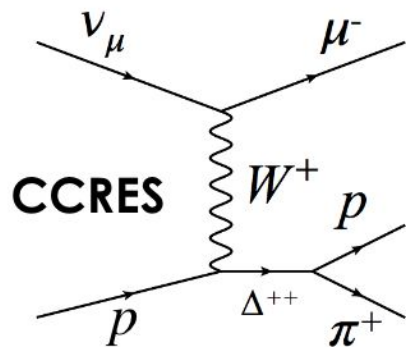


CCRES happens at higher energy (and higher energy transfer) than CCQE

In this case, a resonance (often a  $\Delta$ ) is produced, with a subsequent decay in pions and nucleons

$$\begin{aligned}\nu_\mu p &\rightarrow \mu^- p \pi^+, & \bar{\nu}_\mu p &\rightarrow \mu^+ p \pi^- \\ \nu_\mu n &\rightarrow \mu^- p \pi^0, & \bar{\nu}_\mu p &\rightarrow \mu^+ n \pi^0 \\ \nu_\mu n &\rightarrow \mu^- n \pi^+, & \bar{\nu}_\mu n &\rightarrow \mu^+ n \pi^-\end{aligned}$$

# Charged Current Resonant (CCRES)



CCRES happens at higher energy (and higher energy transfer) than CCQE

In this case, a resonance (often a  $\Delta$ ) is produced, with a subsequent decay in pions and nucleons

Describe the interaction now is more complex (several possible resonances, interferences terms...)

The reference model is pretty old (>50y ago)

Clear need to better understand this process, very relevant for instance for DUNE

$$\nu_{\mu} p \rightarrow \mu^{-} p \pi^{+}, \quad \bar{\nu}_{\mu} p \rightarrow \mu^{+} p \pi^{-}$$

$$\nu_{\mu} n \rightarrow \mu^{-} p \pi^{0}, \quad \bar{\nu}_{\mu} p \rightarrow \mu^{+} n \pi^{0}$$

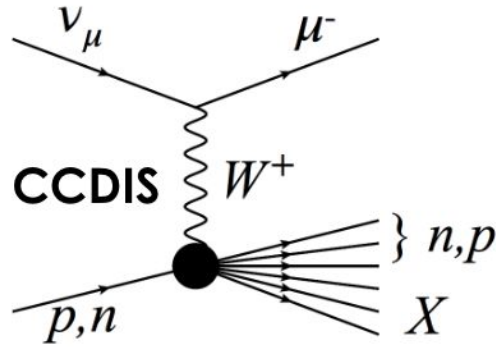
$$\nu_{\mu} n \rightarrow \mu^{-} n \pi^{+}, \quad \bar{\nu}_{\mu} n \rightarrow \mu^{+} n \pi^{-}$$

Axial form factor for CCRES (?)

Described in the same way as for CCQE

$$C_5^A(Q^2) = \frac{C_5^A(0)}{\left(1 + \frac{Q^2}{(M_A^{\text{RES}})^2}\right)^2}$$

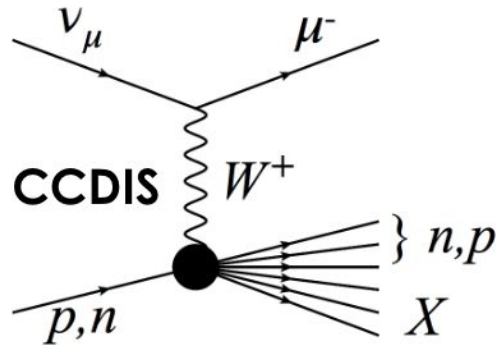
# Charged Current Deep Inelastic Scattering (CCDIS)



CCDIS happens at higher energy (and higher energy transfer) than CCRES

At very high energy, the interactions happens with the nucleon quarks → pretty well understood mechanism (via the so called perturbative QCD ~ parton model)

# Charged Current Deep Inelastic Scattering (CCDIS)



CCDIS happens at higher energy (and higher energy transfer) than CCRES

At very high energy, the interactions happens with the nucleon quarks → pretty well understood mechanism (via the so called perturbative QCD ~ parton model)

The cross section can be written as a function of the Bjorken variables  $x$  and  $y$

$$x = \frac{Q^2}{2M\omega} \quad y = \frac{\omega}{E_\nu}$$

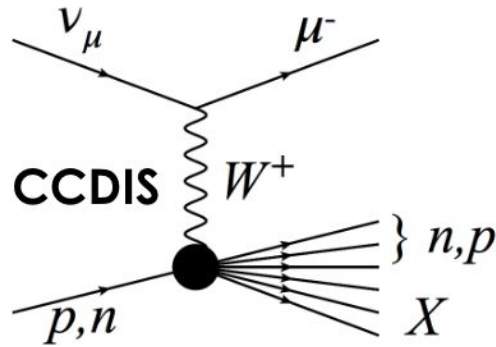
$\omega = E_\nu - E_l$  energy transfer to the nucleon

$$\frac{d^2\sigma^{\nu(\bar{\nu})}}{dx dy} = \frac{G_F^2 M E_\nu}{\pi} \left( \frac{M_W^2}{Q^2 + M_W^2} \right)^2 \left[ xy^2 F_1(x, Q^2) + \left( 1 - y - \frac{Mxy}{2E_\nu} \right) F_2(x, Q^2) \pm xy \left( 1 - \frac{y}{2} \right) F_3(x, Q^2) \right]$$

$F_1$ ,  $F_2$  and  $F_3$  are the nuclear structure functions and describe how quarks and gluons “react” to the neutrino interaction.  $F_1$  and  $F_2$  are for the vectorial part, while  $F_3$  for the axial part (only for  $\nu$ !)



# Charged Current Deep Inelastic Scattering (CCDIS)

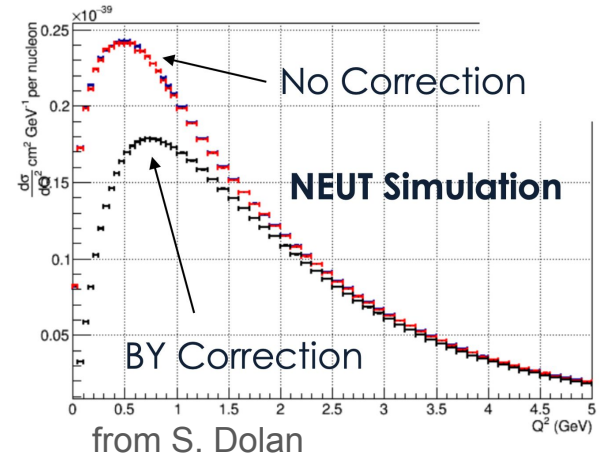


CCDIS happens at higher energy (and higher energy transfer) than CCRES

But for  $Q^2 < 2\text{GeV}^2$ , describing the CCDIS process become complex  $\rightarrow$  QCD is not anymore perturbative and we need approximation

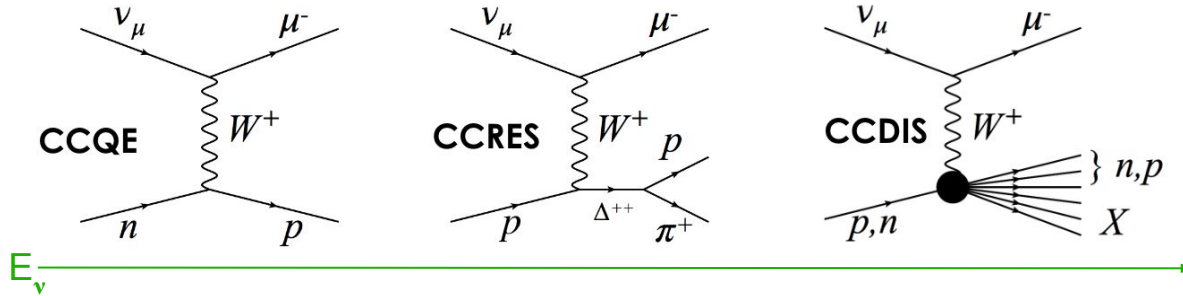
**Bodek-Yang model allows to extrapolate the QCD at lower  $Q^2$ .** It also covers the so called RES to DIS transition region

Parameters are introduced to correct the various structure function, based on comparisons with available data (empirical model)



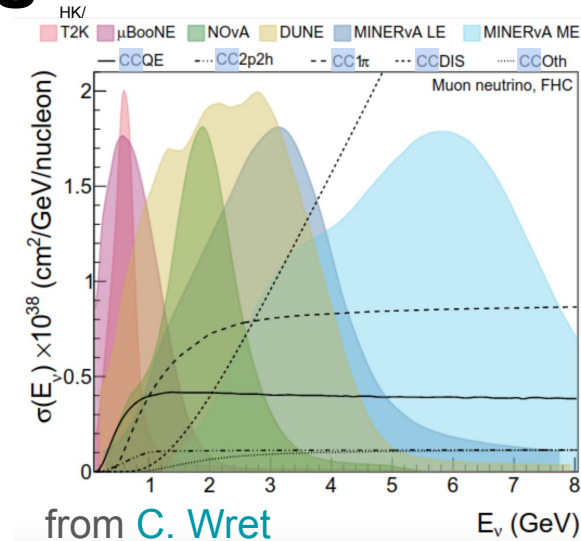
# Let's start measuring

Although complex and difficult to test, we have models, so let's start measuring neutrino cross sections and validate those models!

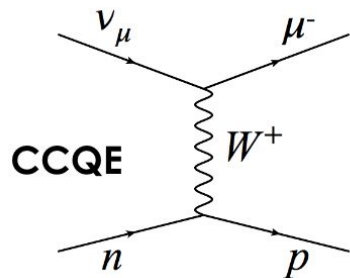


Neutrino energy reconstruction methods rely on the final state particle kinematics (and on the detector technology).

What we can detect are the products of the neutrino interactions.  
For the charged current interactions we look for a lepton in the final state and eventually (some) hadrons (proton and pions)



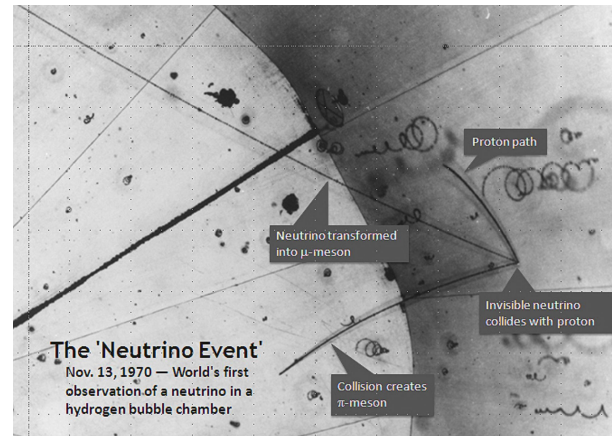
# Measuring the axial mass in neutrino-nucleon scattering



axial-vector coupling constant

$$F_A(Q^2) = \frac{F_A(0)}{\left(1 + \frac{Q^2}{(M_A^{QE})^2}\right)^2}$$

axial mass



Experiment $\nu_\mu d \rightarrow \mu^- p p_s$	QE events	$Q^2$ range $GeV/c^2$	$M_A$ (published)
<i>Mann</i> <sub>73</sub>	166	.05 – 1.6	$0.95 \pm .12$
<i>Barish</i> <sub>77</sub>	500	.05 – 1.6	$0.95 \pm .09$
<i>Miller</i> <sub>82,77,73</sub>	1737	.05 – 2.5	$1.00 \pm .05$
<i>Baker</i> <sub>81</sub>	1138	.06 – 3.0	$1.07 \pm .06$
<i>Kitagaki</i> <sub>83</sub>	362	.11 – 3.0	$1.05^{+.12}_{-.16}$
<i>Kitagaki</i> <sub>90</sub>	2544	.10 – 3.0	$1.070^{+.040}_{-.045}$
<i>Allasia</i> <sub>90</sub>	552	.1-3.75	$1.080 \pm .08$

Bubble chamber experiments  
measure  $M_A^{QE}$  close to 1 GeV.

Here the target is essentially made of  
deuterium (ie 1p and 1n)

# What changes when we move to a neutrino-nucleus interaction?

Current neutrino detectors use more complex nuclei (CH, H<sub>2</sub>O, Ar,...), thus neutrino interactions happen with **nucleons bound in nuclei**

Need to take into account that initial state nucleons are not static → how can we model the nucleus ?

“Simplest” models used a Fermi gas assumption

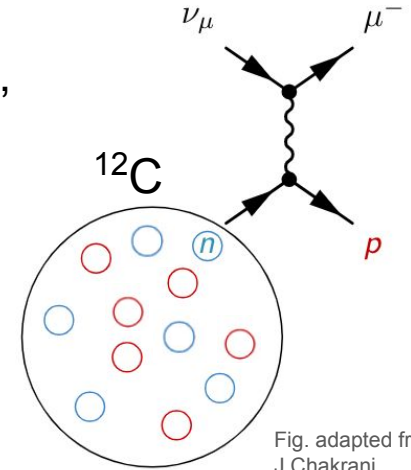


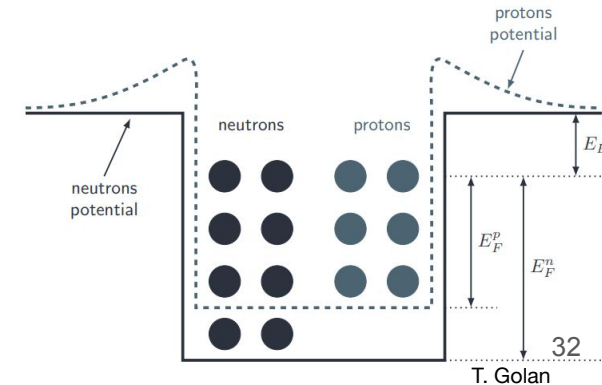
Fig. adapted from J.Chakrani

## Relativistic Fermi Gas (RFG)

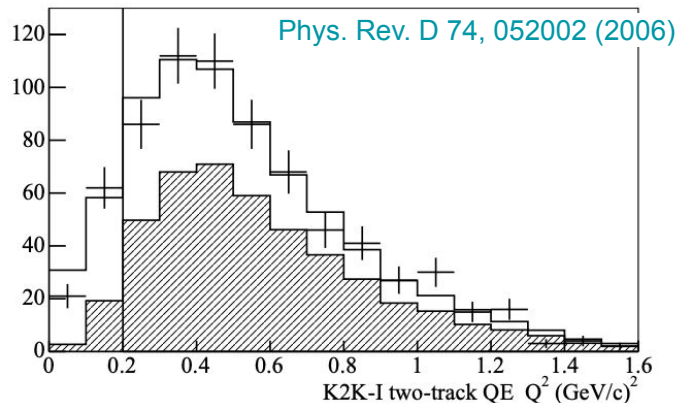
Nucleons move freely in a constant binding energy within the nuclear volume

## Local Fermi Gas (LFG)

The nucleus is described with the local density approximation

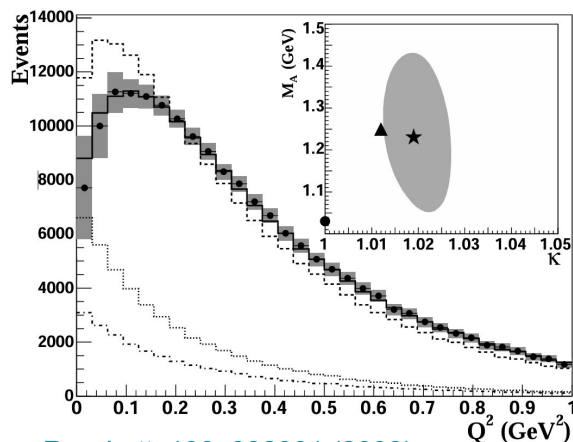


# Measuring the axial mass in neutrino-nucleus interactions



*K2K measures  $M_A^{QE}$  from neutrino- $H_2O$  interactions*

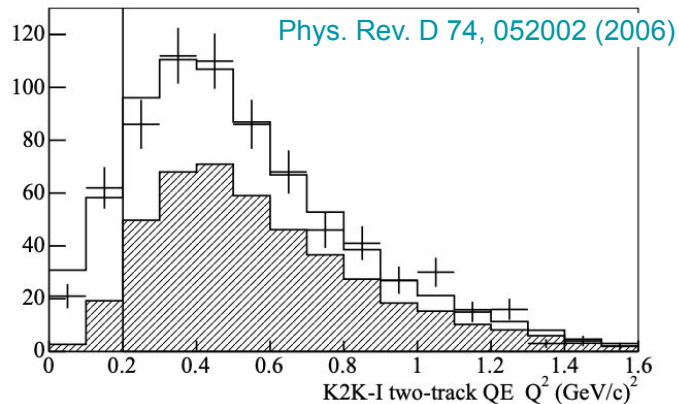
*“We use a relativistic Fermi gas model for oxygen and assume the form factor is approximately a dipole with one parameter, the axial vector mass  $M_A$ , and fit to the shape of the distribution of the square of the momentum transfer from the nucleon to the nucleus. Our best fit result for  $M_A = 1.20 \pm 0.12$  GeV.”*



*MiniBooNE measures  $M_A^{QE}$  from neutrino-CH interactions*

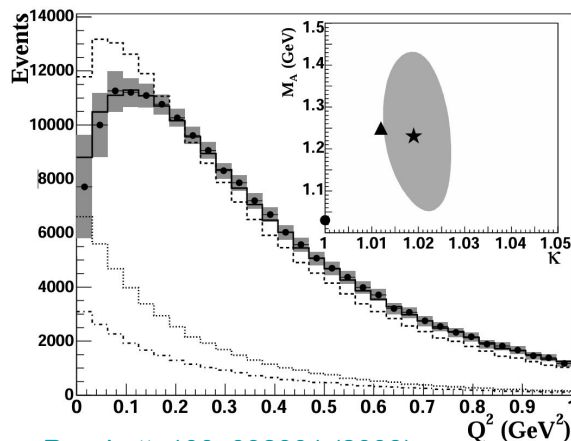
*“Using a high-statistics sample of  $\nu_\mu$  CCQE events, MiniBooNE finds that a simple Fermi gas model, with appropriate adjustments, accurately characterizes the CCQE events observed in a carbon-based detector. The extracted parameters include an effective axial mass,  $M_A^{eff} = 1.23 \pm 0.20$  GeV”*

# Measuring the axial mass in neutrino-nucleus interactions



*K2K measures  $M_A^{QE}$  from neutrino- $H_2O$  interactions*

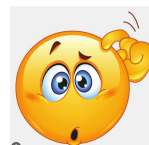
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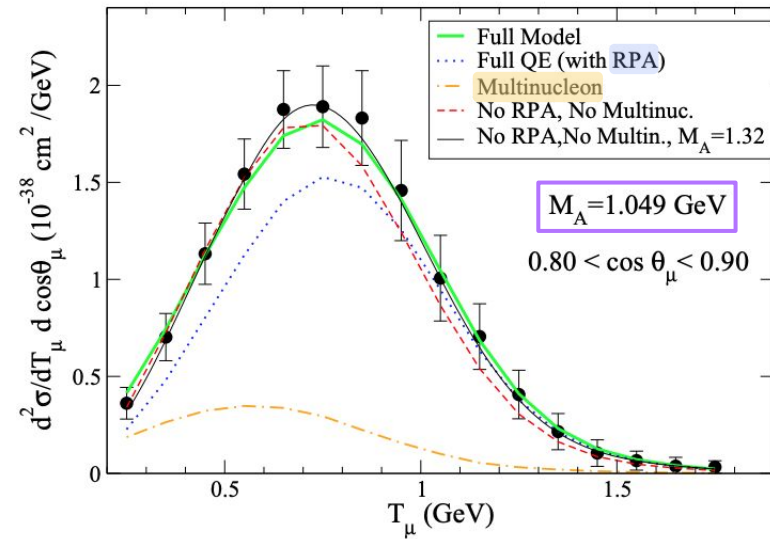
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*The axial mass shouldn't depend on the nucleus, right?*



# Solving the $M_A^{\text{QE}}$ puzzle

By accounting for additional nuclear effects (here named **RPA** and **multinucleon**) it is possible to explain MiniBooNE “CCQE” results with a more **reasonable value of  $M_A^{\text{QE}}$** , close to the one obtained by bubble chamber experiments



<https://doi.org/10.1016/j.physletb.2011.11.061>

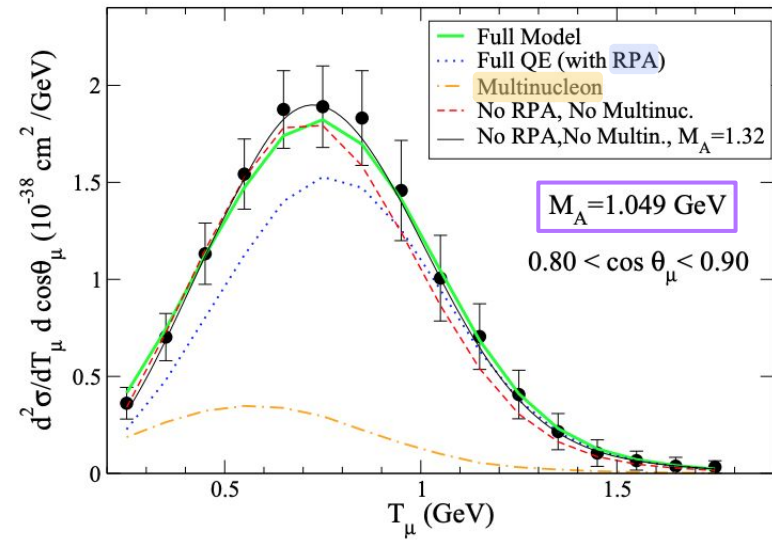
**RPA (Random Phase Approximation)** is a correction added to take into account correlations between nucleons that affect the nuclear response. They generally suppress the cross section for low momentum transfer interactions

**Multinucleon effects (often known as 2p2h)** account for neutrino interactions that happen with a pair of correlated nucleons (np, nn, pp)



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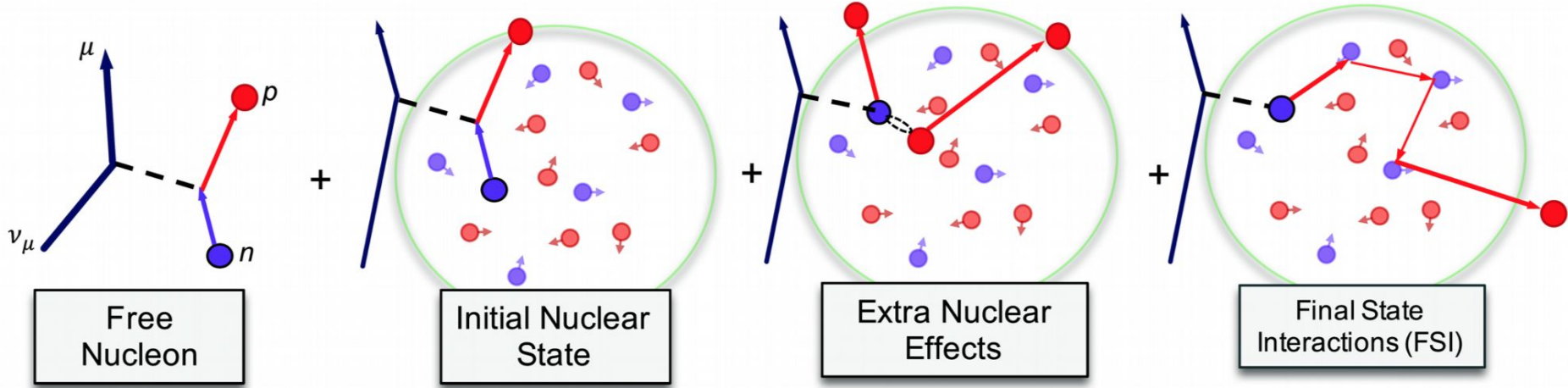
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**Multinucleon effects (often known as 2p2h)** account for neutrino interactions that happen with a pair of correlated nucleons (np, nn, pp)

**Nuclear effects!!!!**



# The role of nuclear effects



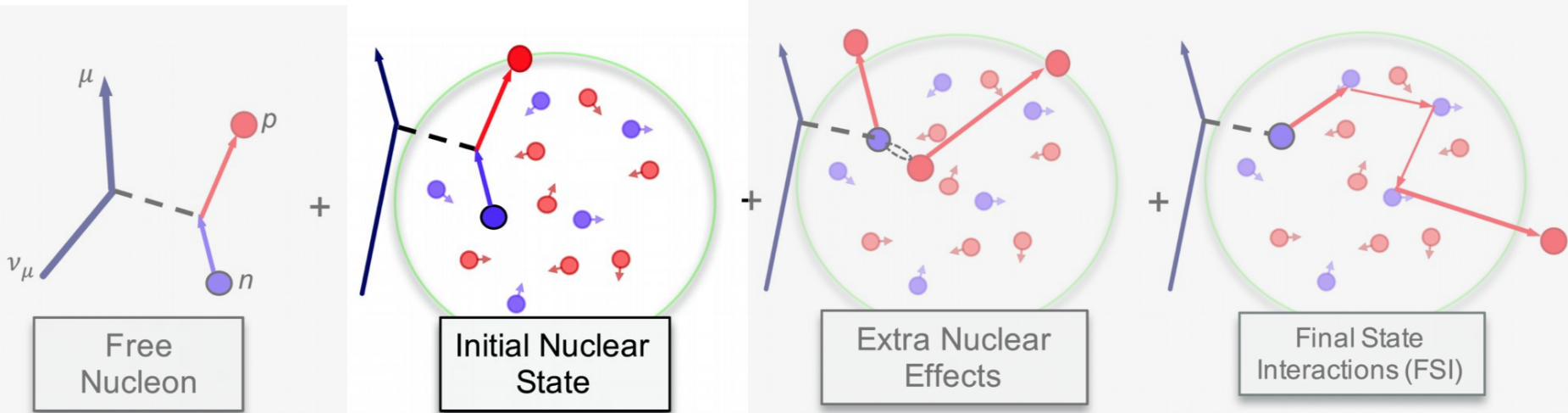
Nucleons are bounded in nuclei

Neutrinos interact with nucleons that have an initial (Fermi) momentum

They can interact with a pair of correlated nucleons (2p2h) since nucleon can be affected by short and long range correlation

The resulting nucleon can reinteract within the nucleus before exiting it

# The role of nuclear effects



Nucleons are bounded in nuclei

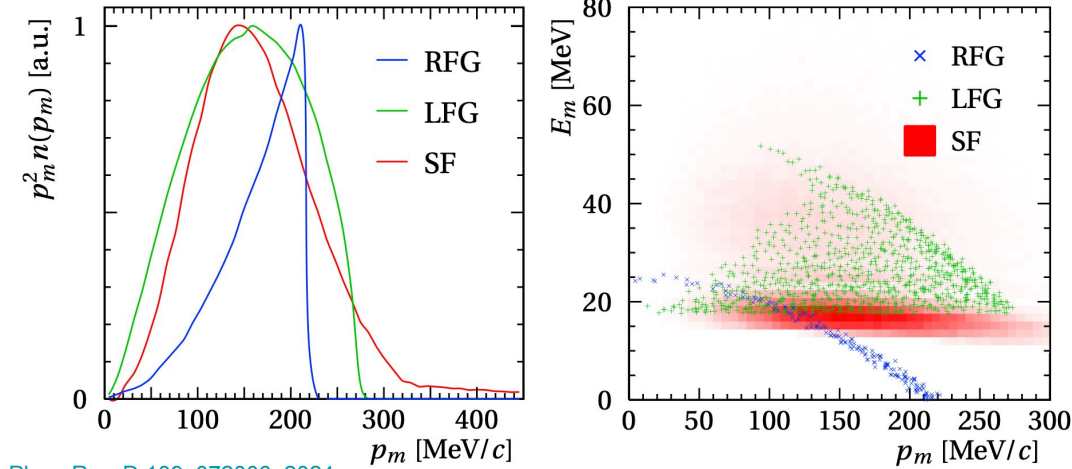
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# Nuclear models

*~ initial nucleon momentum and energy*

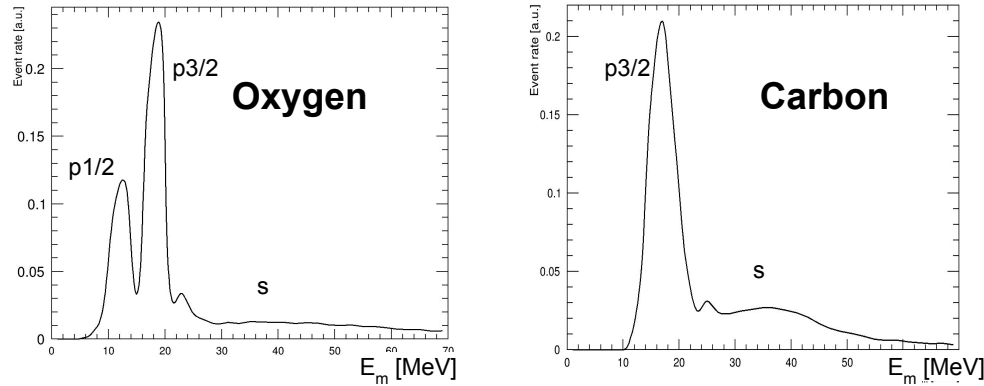


Phys. Rev. D 109, 072006, 2024

**More sophisticated** (wrt Fermi gas)  
**nuclear models as Spectral**  
**Function (SF)**

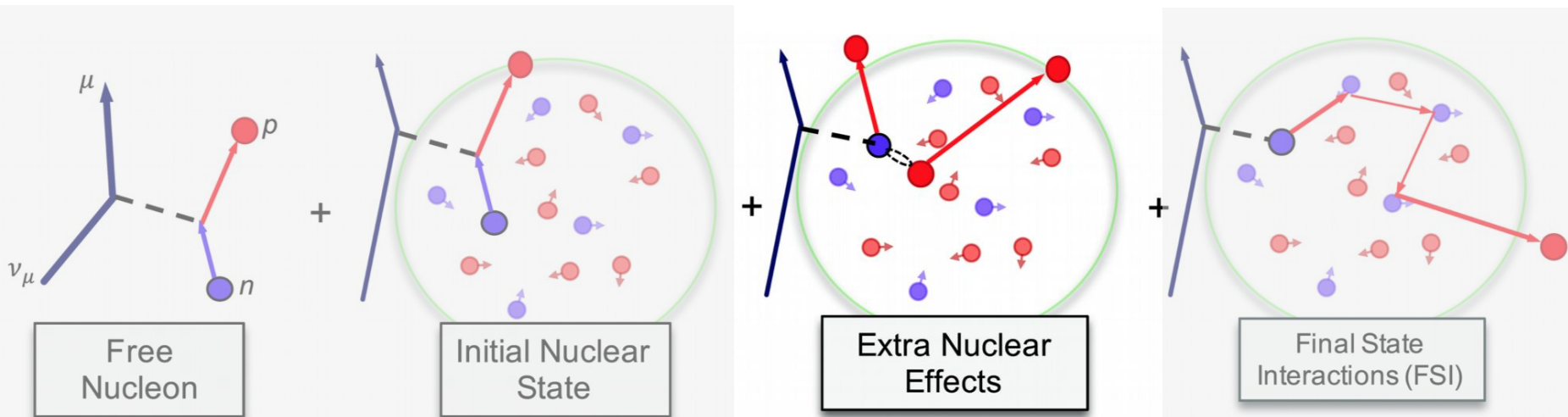
try to reproduce the nuclear shell structure

**Shell occupancy in SF model**



The final state particle kinematics depend on the initial state kinematics  
 → need to precisely model the initial state if we want to interpret the final state  
 → we thus now tend to **use more sophisticated available nuclear models**

# The role of nuclear effects



Nucleons are bounded in nuclei

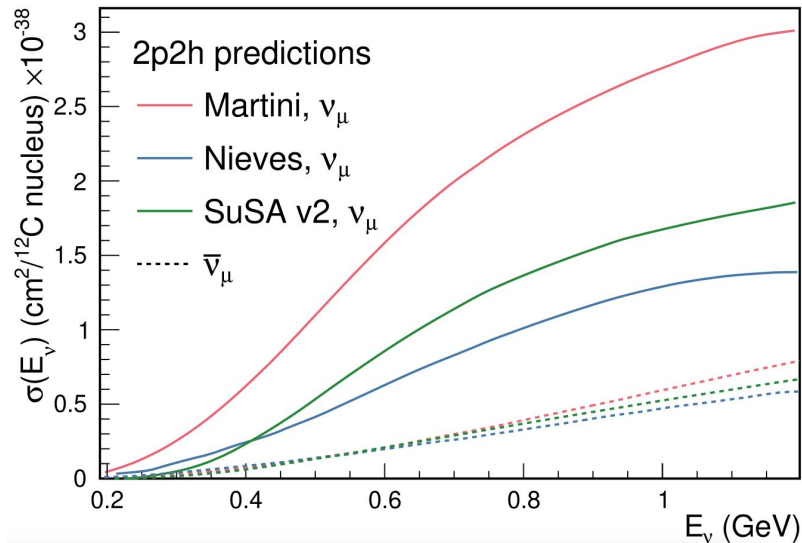
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# 2p2h models

Eur. Phys. J. C (2023) 83:782



Now we know that we need to describe 2p2h interactions.

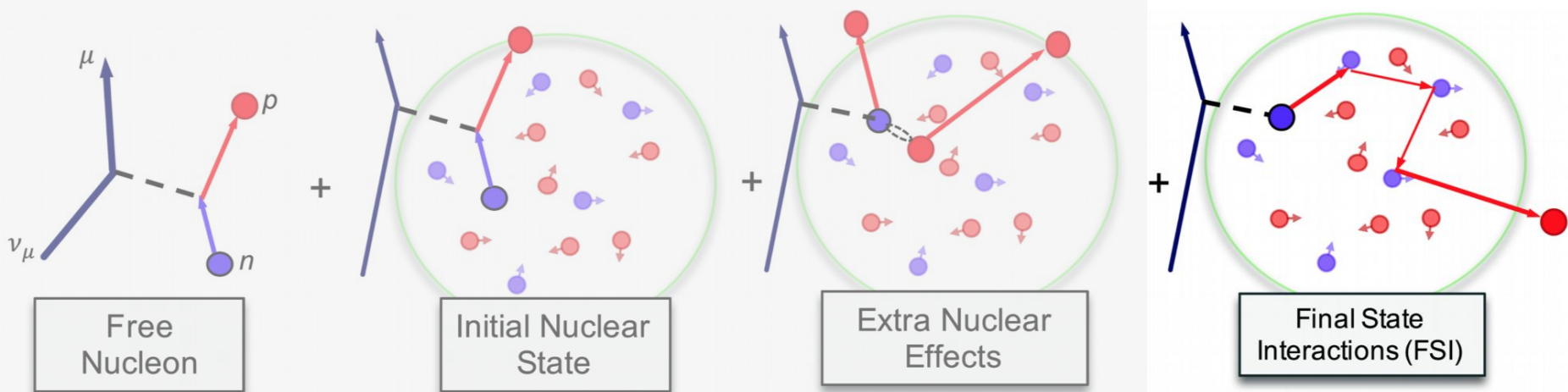
Several models describing 2p2h are also available and they predict pretty different cross section values → **this is source of systematics uncertainties**

How many 2p2h interactions do we have?

Which kind of final state kinematics they give?

If you have 2 protons in the final state and one is under threshold?

# The role of nuclear effects



Nucleons are bounded in nuclei

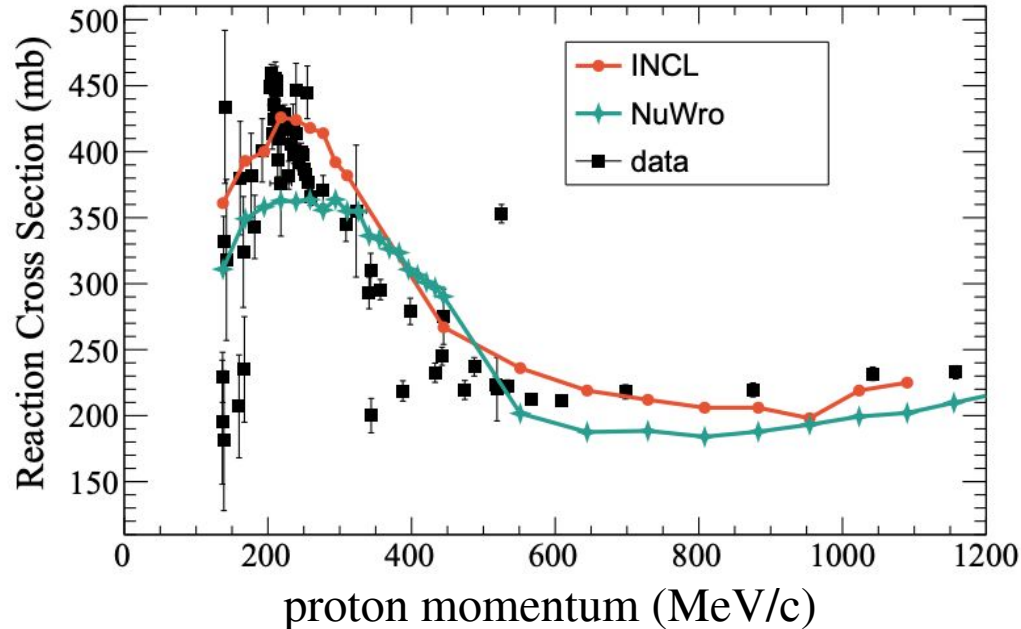
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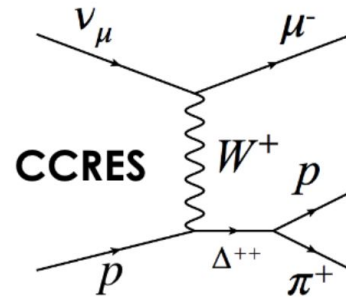
The resulting nucleon can reinteract within the nucleus before exiting it

# FSI models

Finally FSI can drastically change the aspect of the final state kinematics and even the nature of the final state particles: deviate hadrons, re-absorb hadrons (pions or protons), create new ones, nucleus excited state to de-excite



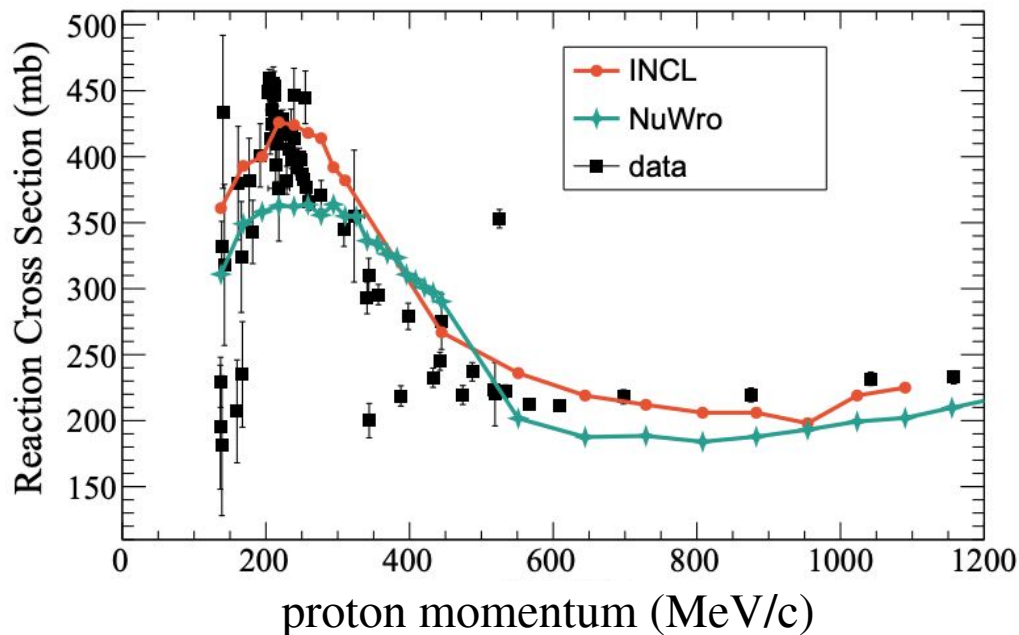
Once more, different models predict different things



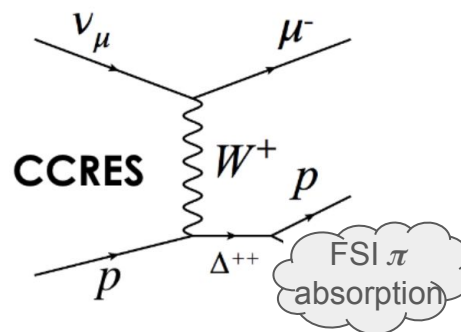


# FSI models

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Once more, different models predict different things



*This final state  
look like a  
CCQE one*



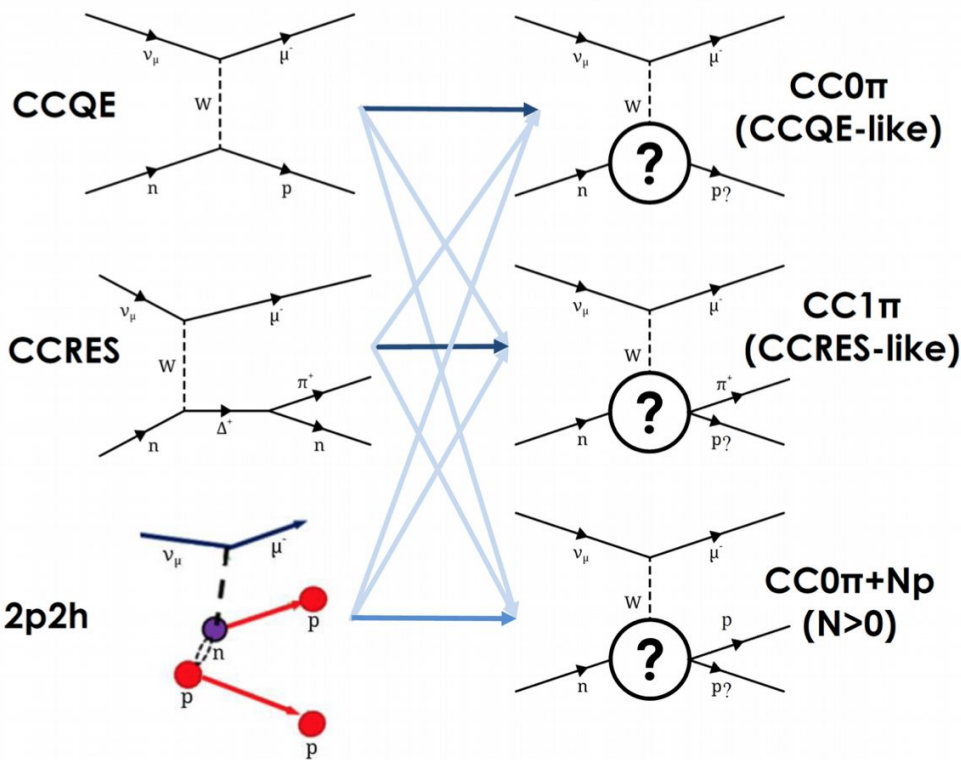
⇒ when looking for a muon and a proton in the final state, what were K2K and MiniBooNE selecting?



# Final state topologies

## Initial state interactions

## Final state topologies



Our detectors can only reconstruct final state particles after nuclear effect

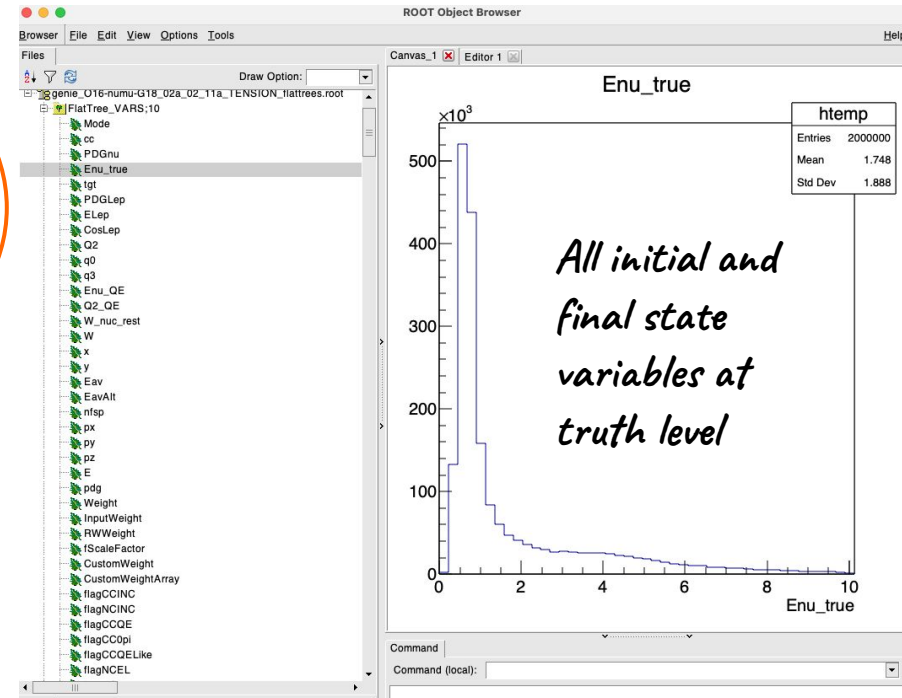
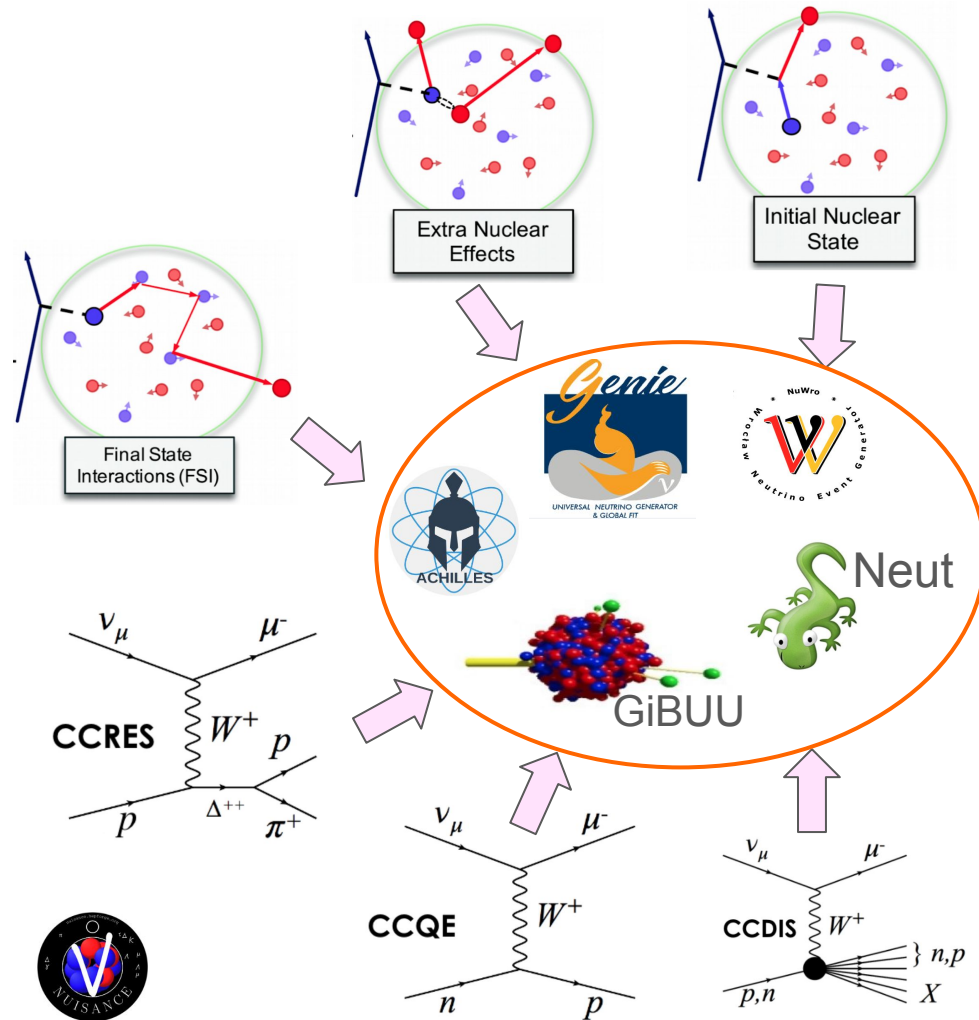
- charged lepton (CC) or no lepton (NC)
- w. or w/o pions:  $0\pi^{+-0}$ ,  $1\pi^{+-0}$
- w. or w/o protons:  $0p$ ,  $1p$ ,  $Np$

**Final state topologies** are the only categories we can access w/o referring to theoretical models, but they are **composed of a mixture of initial state interactions**

**Difficult task for the xsec community is to try to characterize these initial state interactions to check/tune theoretical models** (and for the theory community to try to predict our final state topologies starting from the initial state interactions)

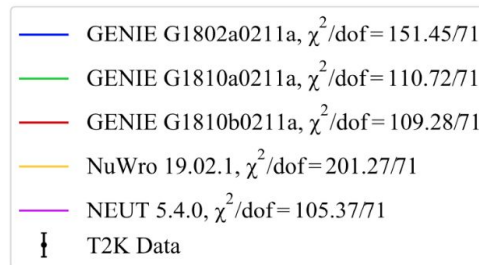
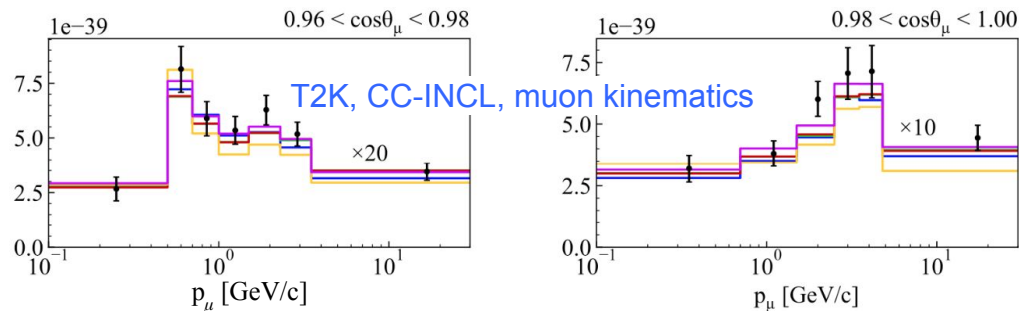
# Neutrino Generators

They usually contain several models for each kind of interaction and of nuclear effect. You need to provide the incoming neutrino flux, the desired target and can choose the models

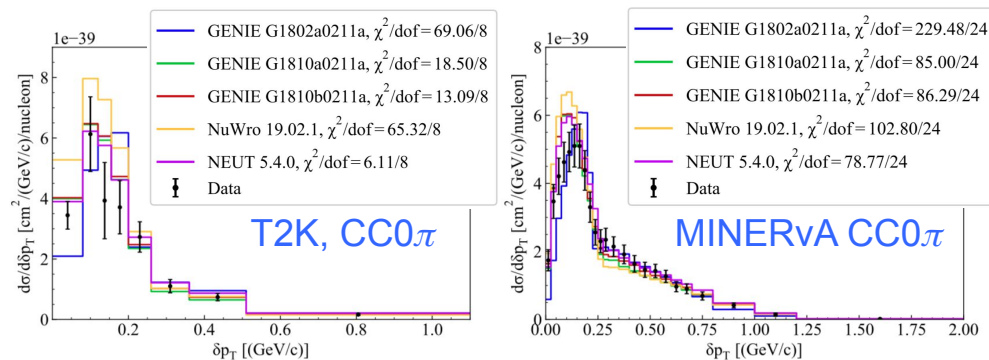


# XSEC experiments: Comparisons and challenges as from TENSION 2019

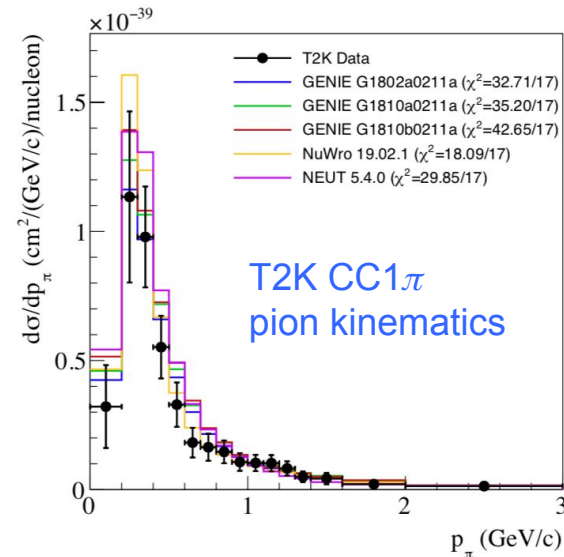
M.B.A. et al., Phys. Rev. D 105, 092004 (2022)



Despite the increasing availability and quality of cross-section data and extraction techniques, as well as of the available interaction models, TENSION is still the right word to use...

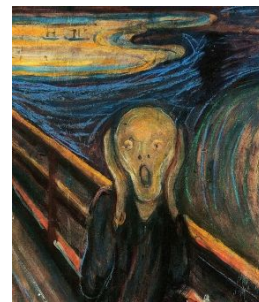
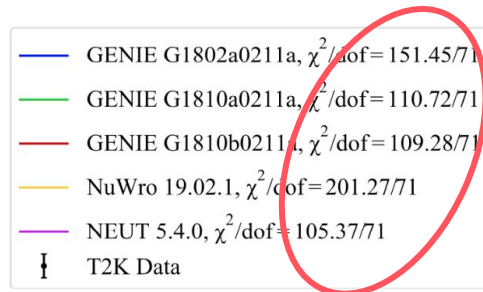
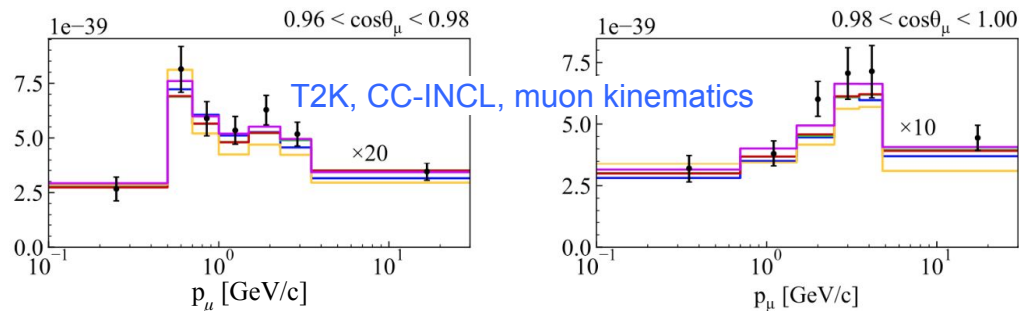


Transverse Kinematic Imbalance Variables

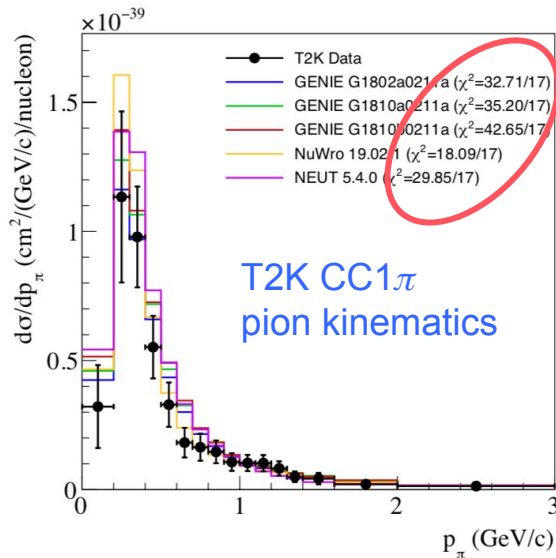
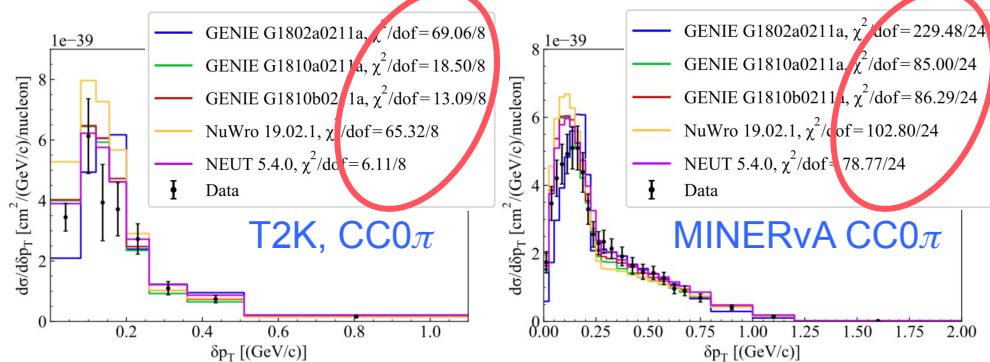


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Transverse Kinematic Imbalance Variables



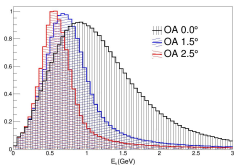
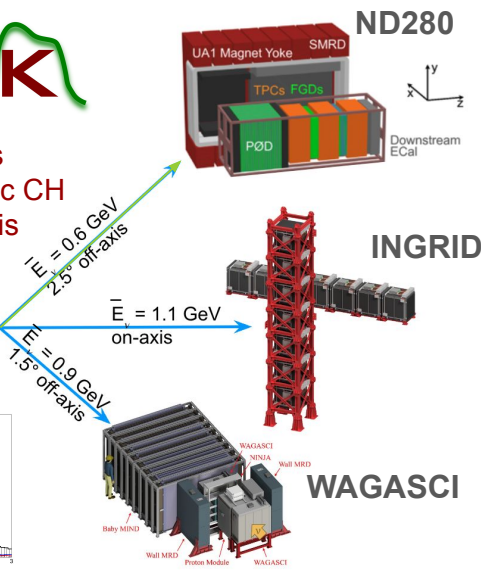
**KEEP  
CALM  
AND  
MEASURE  
v XSEC**

# Neutrino cross section measurements

# Main actors in the field



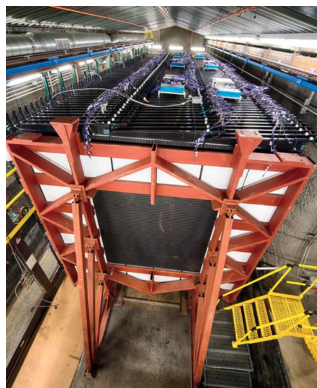
1. Near detectors
2. H<sub>2</sub>O and plastic CH
3. different off-axis



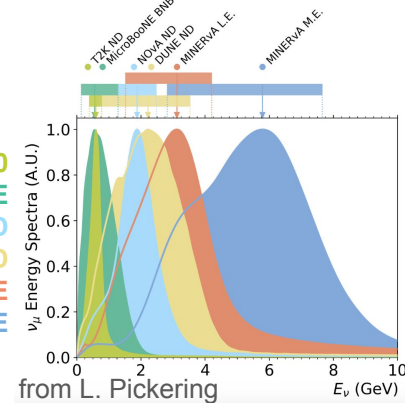
1. Liquid scintillator
2. off-axis

Fermilab  
NuMI beam

$\bar{E}_\nu = 1.8 \text{ GeV}$   
0.8° off-axis



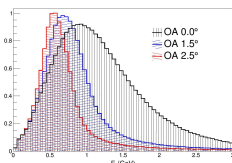
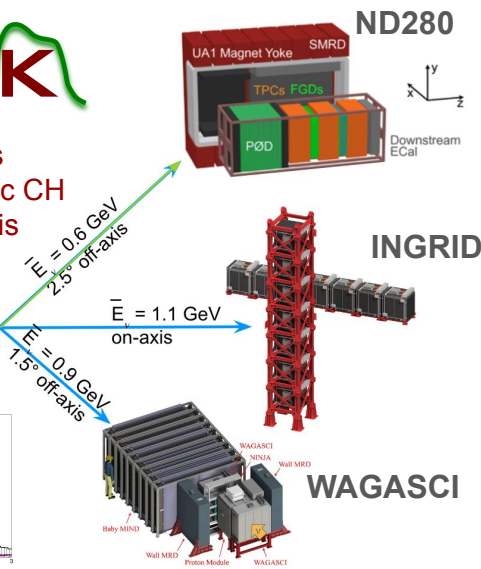
T2K ND280  
MicroBooNE  
NOvA ND  
DUNE ND  
MINERvA LE  
MINERvA ME



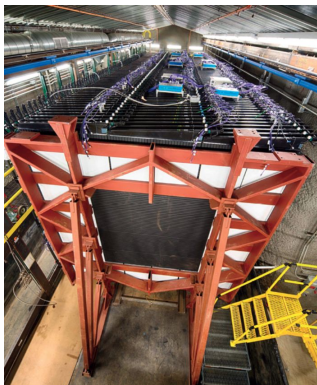
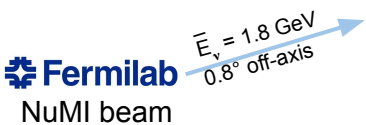


# T2K

1. Near detectors
2. H<sub>2</sub>O and plastic CH
3. different off-axis

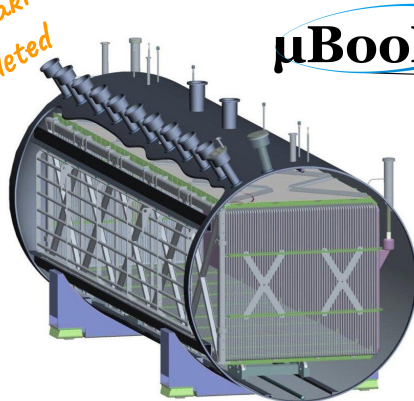


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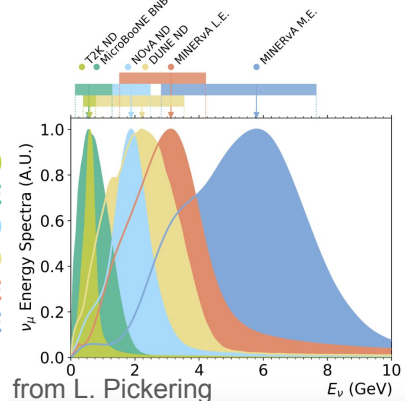
## Main actors in the field

Data taking completed

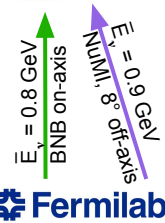


μBooNE

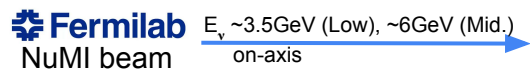
- T2K ND280
- MicroBooNE
- NOvA ND
- DUNE ND
- MINERvA LE
- MINERvA ME



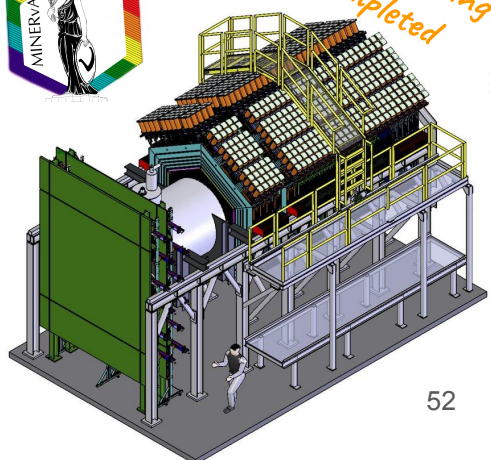
1. LArTPC
2. BNB beam on-axis
3. NuMI beam off-axis



1. Several targets: C, CH, Fe, Pb, H<sub>2</sub>O, He
2. two beams ~3GeV and ~6GeV



Data taking completed





# Priorities of neutrino cross-section community

- **Limit model dependence**, by defining the signal depending on the final state topology (instead of the true interaction), by carefully choosing the observables (detectable variables) and applying the efficiency corrections
- Characterise the **dominant channels  $CC0\pi$  and  $CC1\pi$** , while also exploring subdominant or rare ones (characterise the background)
- **Promote combined measurements** (multi-flux, multi-target, multi-channel) that allow to provide correlations between measurements and explore E- and A- dependences
- **Explore nuclear effects**, that are the main responsible of systematics in the oscillation analysis
- Provide new measurements on **different targets**: CH, water, Argon (but also Pb and Fe)
- Provide **data release** allowing to preserve useful data results over the next decades and in the simplest format for theoreticians to be used
- Develop and maintain **sophisticated tools and careful procedures** for the cross section extraction (unfolding and error propagation) and diagnostic

# What is a cross section?

*x, y = generic observables*

$$\frac{d\sigma}{dx_i dy_j} = \frac{N_{ij}^{\text{signal}}}{\epsilon_{ij} \Phi N_{\text{nucleons}}^{\text{FV}}} \times \frac{1}{\Delta x_i \Delta y_j}$$

# What is a cross section?

After background subtraction and unfolding of detector effects

$x, y = \text{generic observables}$

$$\frac{d\sigma}{dx_i dy_j} = \frac{N_{ij}^{\text{signal}}}{\epsilon_{ij} \Phi N_{\text{nucleons}}^{\text{FV}}} \times \frac{1}{\Delta x_i \Delta y_j}$$

true variables
efficiency correction
double (or more?) differential

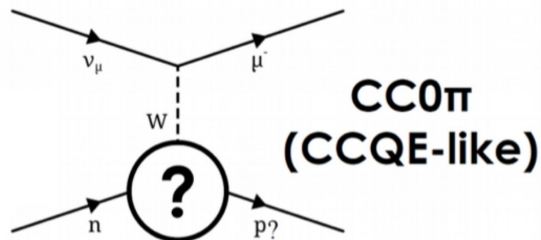
- Signal, to be defined considering the detector capabilities  $\Rightarrow$  **final state topology**
- Selected signal samples contain also some background  $\Rightarrow$  need of **background samples**
- Observables, to be chosen considering the detector capabilities  $\Rightarrow$  **usually lepton and/or hadron kinematics**
- Limit the model dependence of the efficiency correction  $\Rightarrow$  perform **2D (or more) differential measurements**, phase space restriction,...
- Cross section to be extracted as a function of the true observables  $\Rightarrow$  **unfolding of detector effects**

# What do we need to measure a cross section?

(taking as an example the [Oxygen and Carbon CC0 \$\pi\$  measurement from T2K](#))

**A signal definition,**  
for instance CC0 $\pi$ , that  
lives in the truth space

*CC0 $\pi$ : we look for a  
reconstructed  $\mu$ ,  
potentially a reco  $p$  and  
NO pions*

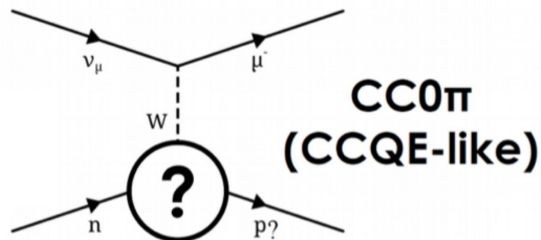


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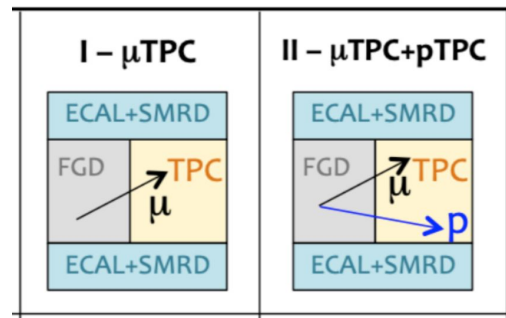
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**A signal selection,**  
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kinematics

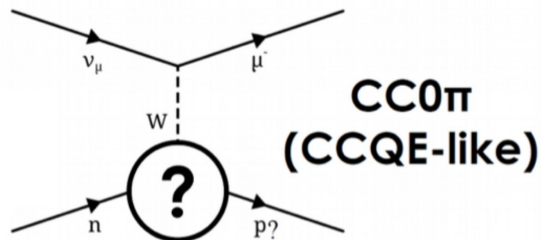


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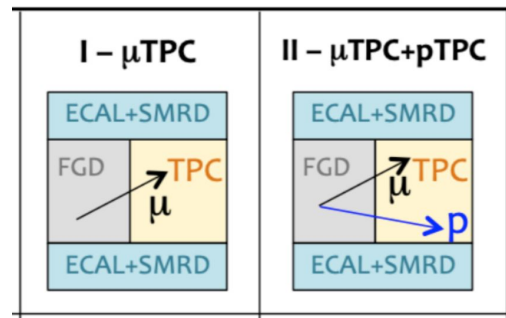
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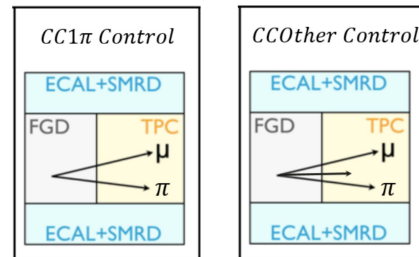
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## A background selections



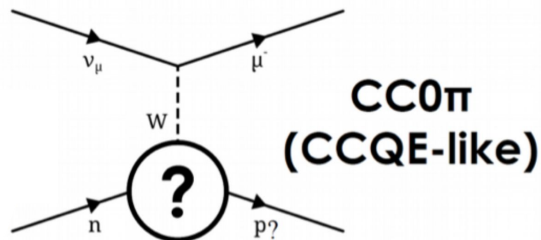
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remaining in the signal samples

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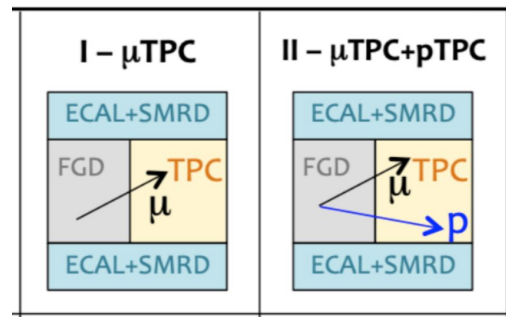
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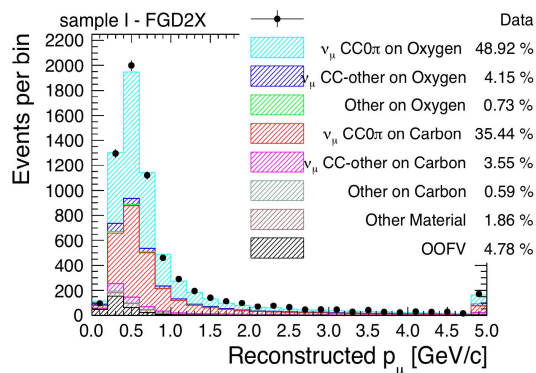


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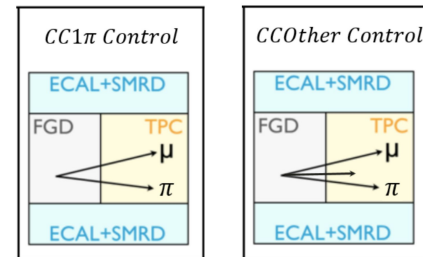


**A Montecarlo prediction,** that is  
the fundamental tool to:

1. have an idea of the background contamination and sample purity
2. move from the reco to the truth space (detector unfolding matrix and efficiency correction)
3. find the needed MC adjustments when compared to data

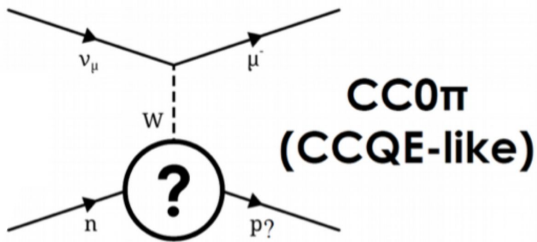


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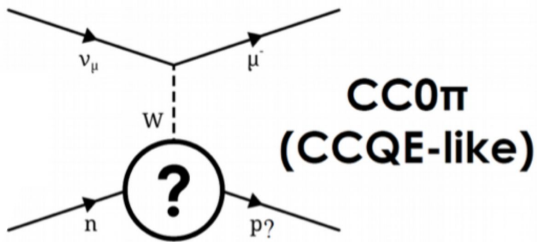
# What are the best observables to exploit?



We select a muon and eventually a proton.  
We can be tempted to try to extract the cross section as a function of the neutrino energy, the observable really needed for the oscillation analysis



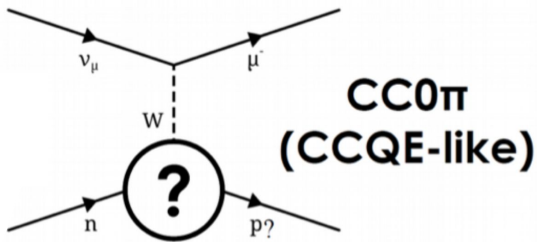
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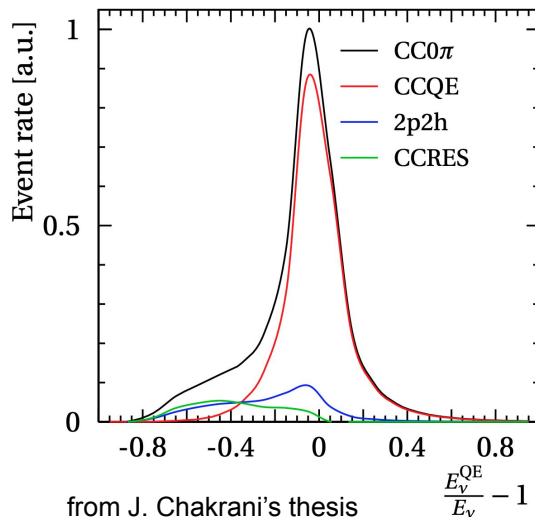
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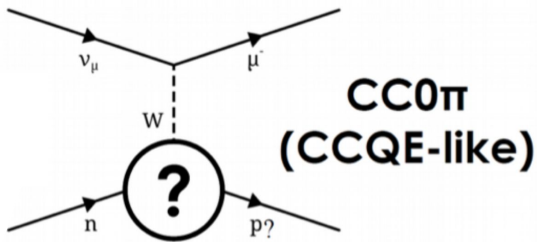
How can we reconstruct the neutrino energy from the final state w/o knowing the occurred interaction and exploiting essentially the muon information?



Essentially... we can't!

And a cross section extracted as a function of the true neutrino energy will be by definition model dependent (using conventional neutrino beams)

# What are the best observables to exploit?

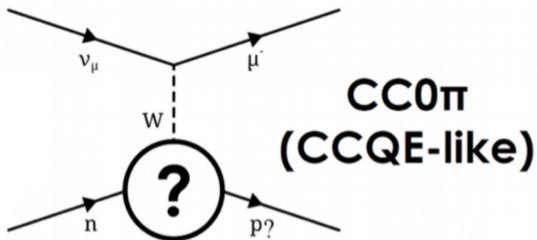


$p_\mu$  and/or  $\cos\theta_\mu$



We usually consider the muon kinematics (direction and momentum), that are in general well reconstructed by the detector

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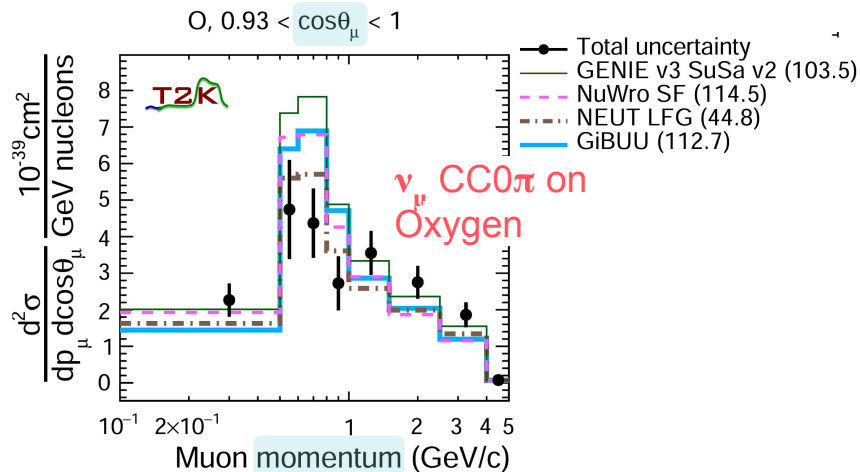


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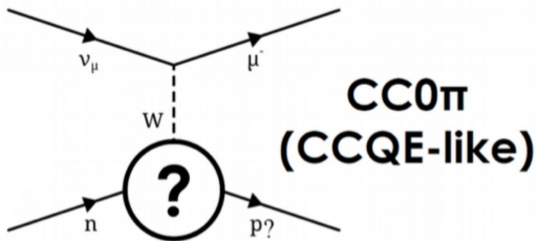


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*In addition, providing multi dimensional measurements is encouraged, since this allows a better mapping of the phase space*



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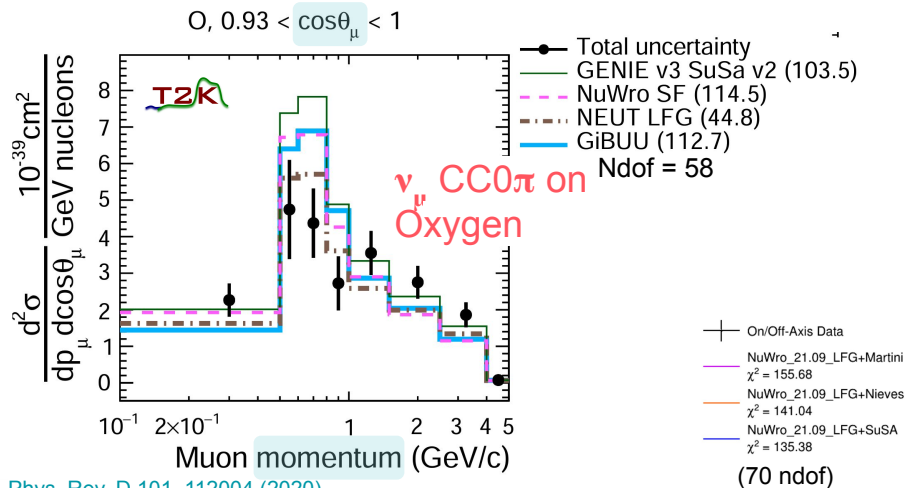
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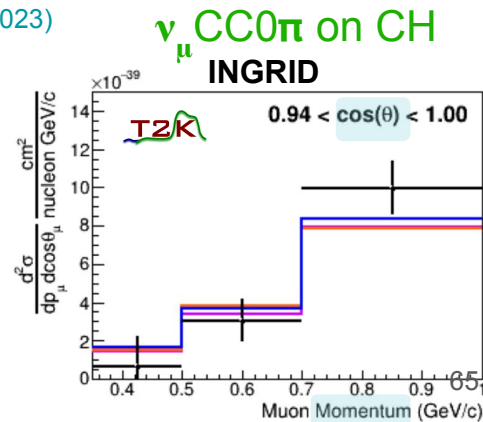
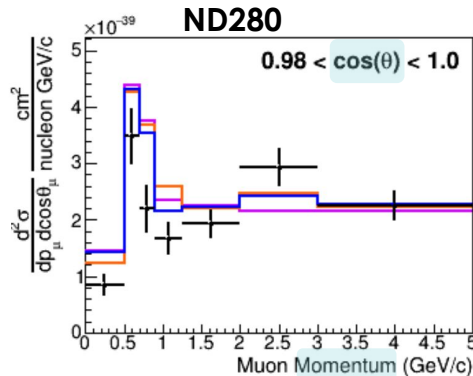
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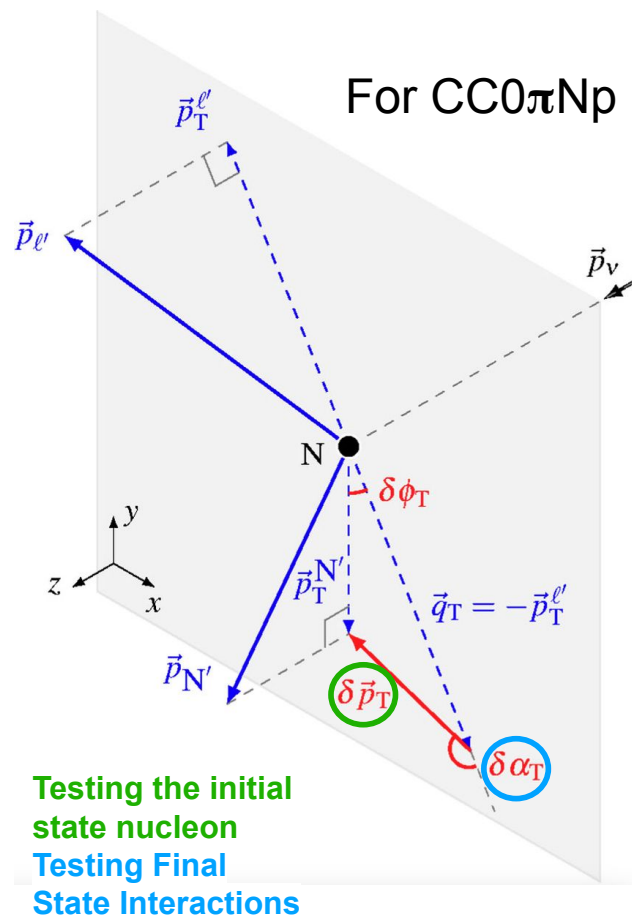
*At T2K we can also study the same interaction at different energy spectra by combining different near detectors*



Phys. Rev. D 108, 112009 (2023)



# Transverse kinematic imbalance variables (TKI)

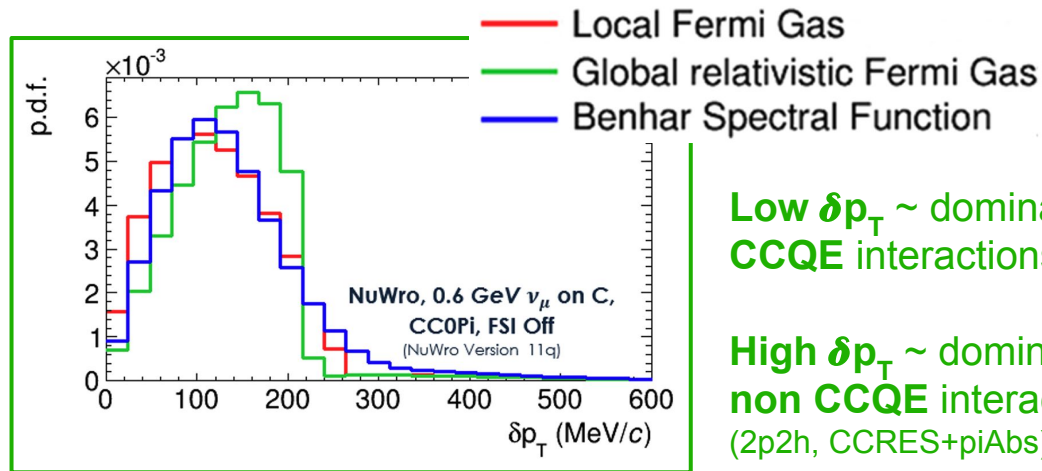
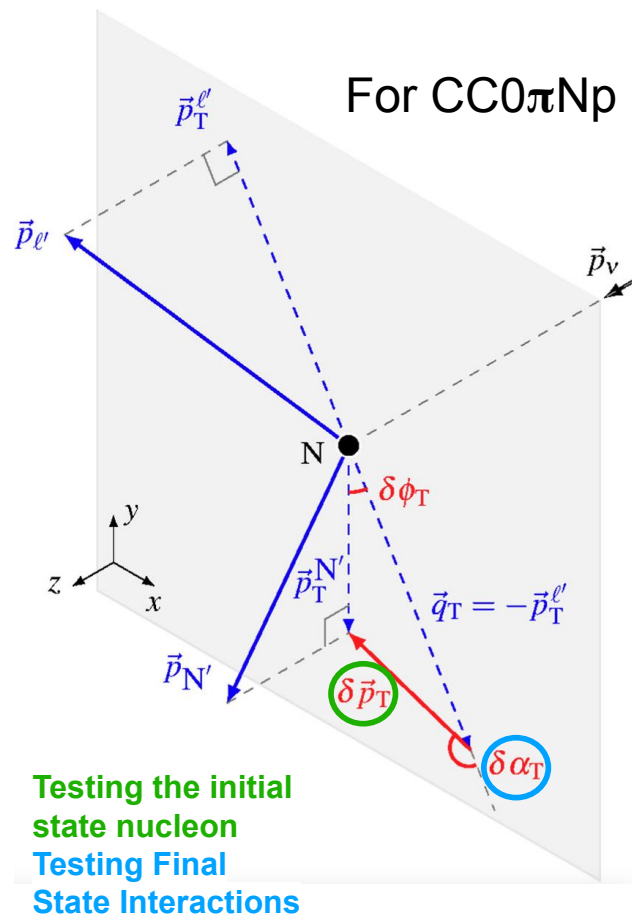


On free nucleon, there is no final state transverse imbalance.

If TKI exist, this means that there is a transverse kinematic imbalance, i.e. some nuclear effects

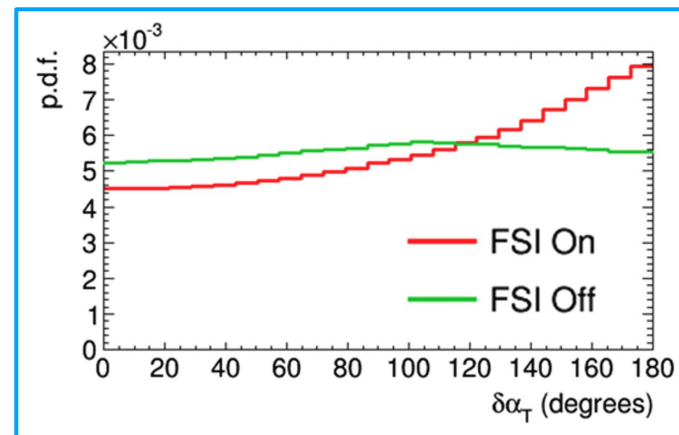
Using TKI variables is a way to study nuclear effects

# Transverse kinematic imbalance variables (TKI)



Low  $\delta p_T \sim$  dominance of CCQE interactions

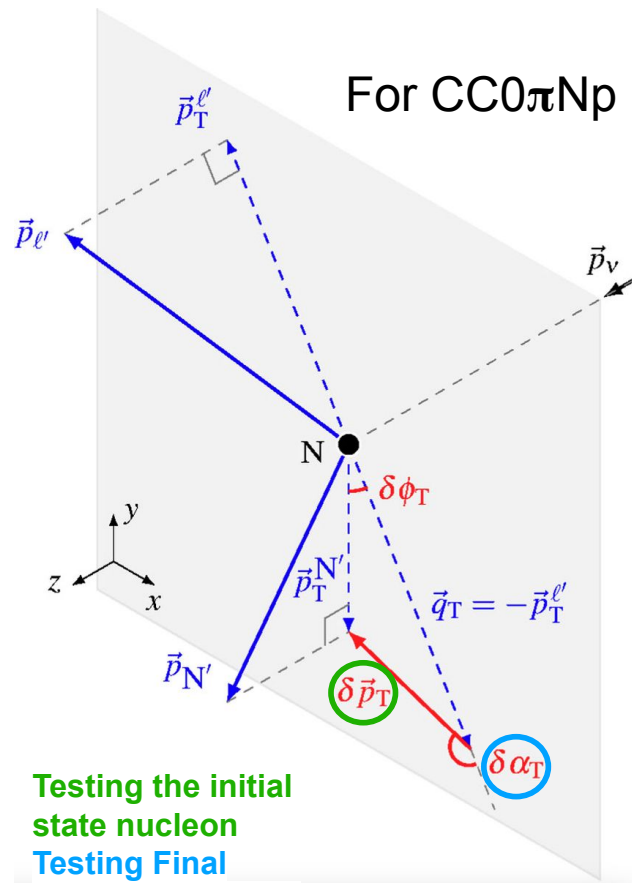
High  $\delta p_T \sim$  dominance of non CCQE interactions (2p2h, CCRES+piAbs)



Low  $\delta \alpha_T \sim$  low FSI effects

High  $\delta \alpha_T \sim$  high FSI effects

## Transverse kinematic imbalance variables (TKI)



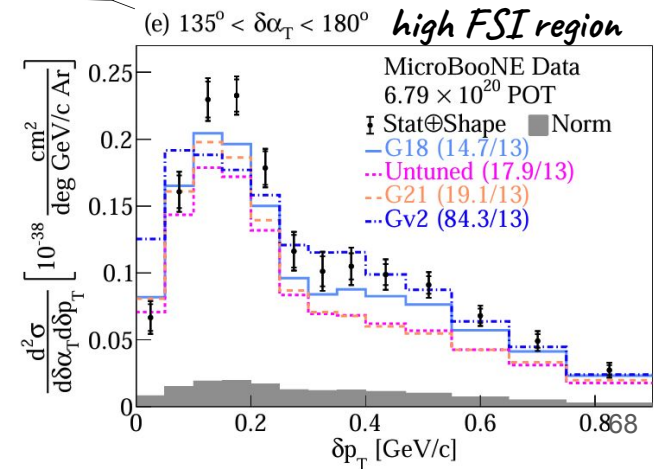
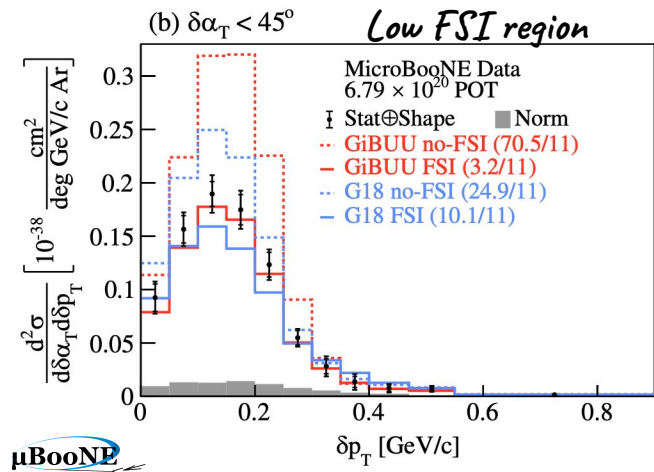
Again, even better discrimination power when using simultaneously 2 variables → deeper tests of nuclear effect models

$\delta p_T$  distribution is definitely not the same at high and low  $\delta\alpha_T$  regions

First TKI measurement on Ar!

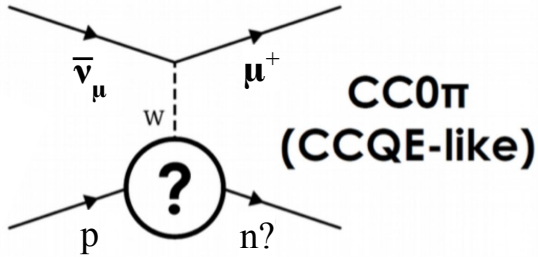
Phys. Rev. Lett. 131, 101802 (2023),

Phys. Rev. D 108, 053002 (2023)





# TKI and anti-neutrinos



Antineutrinos interact with the protons in the detector.

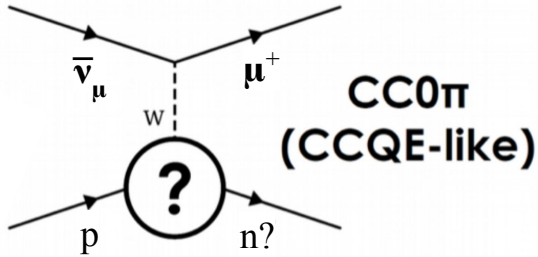
Let's consider plastic scintillator target, essentially made of CH. C contains 6 protons and Hydrogen?? Only 1!!

That means that **antineutrino interactions with H are essentially interaction on a free proton → no nuclear effects!!!**

Nature, 614, 48-53 (2023)



# TKI and anti-neutrinos



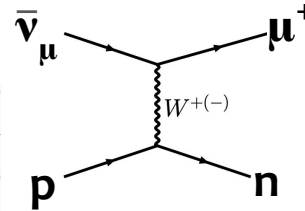
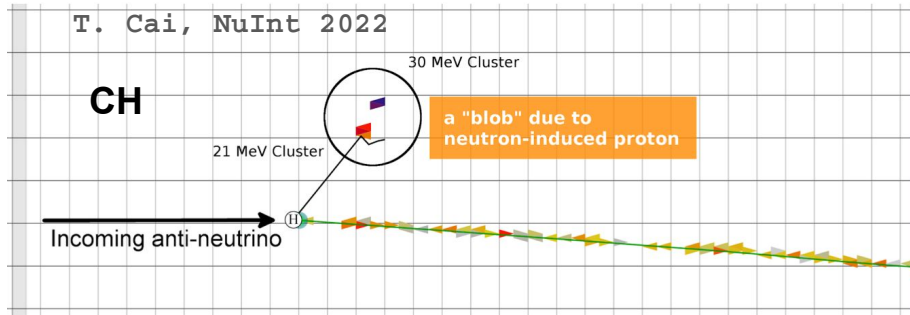
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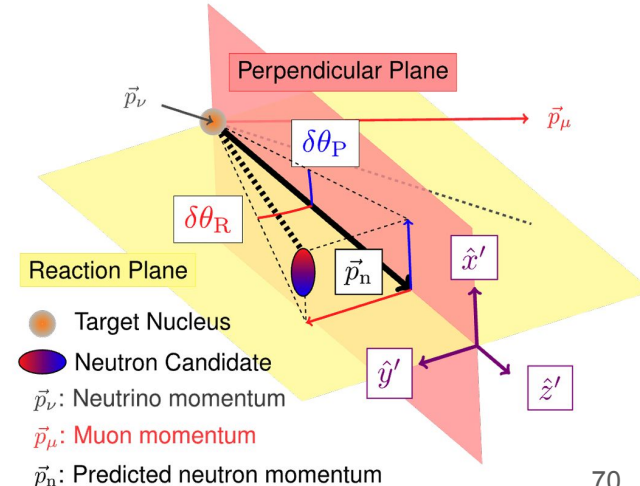
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Nature, 614, 48-53 (2023)

*Neutrons by definition are difficult to detect → look at  
n Secondary Interactions that produce visible p*

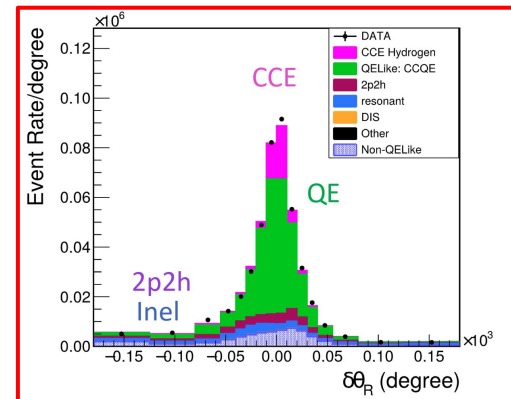
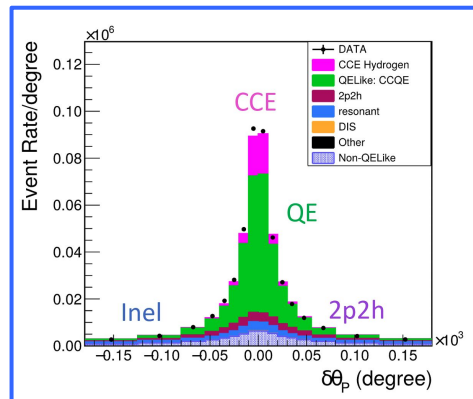
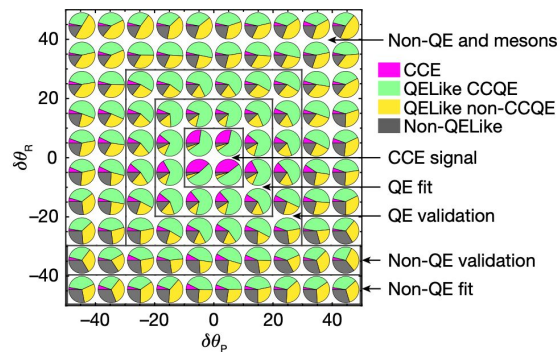


*Only need the neutron direction!*



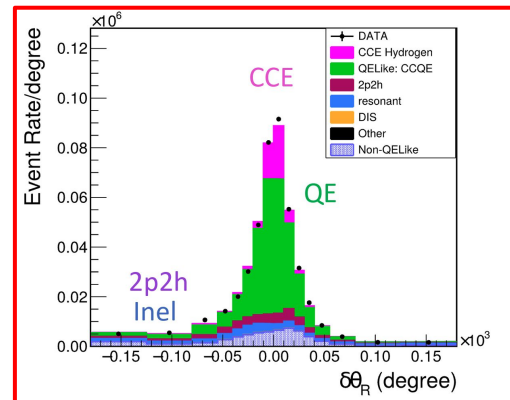
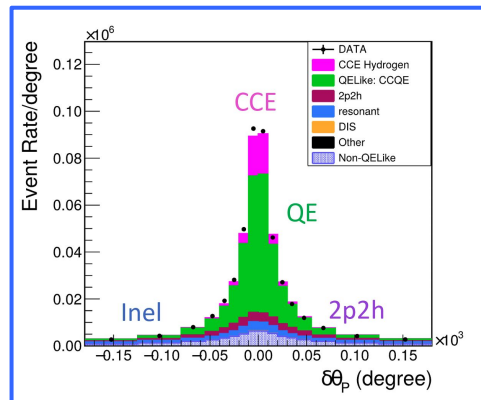
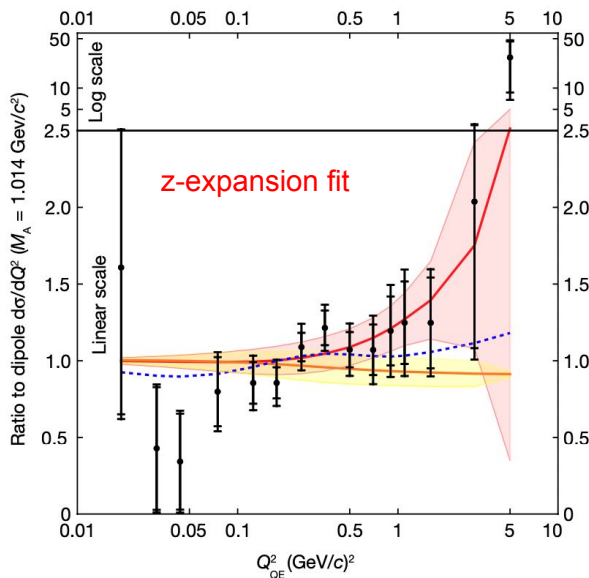
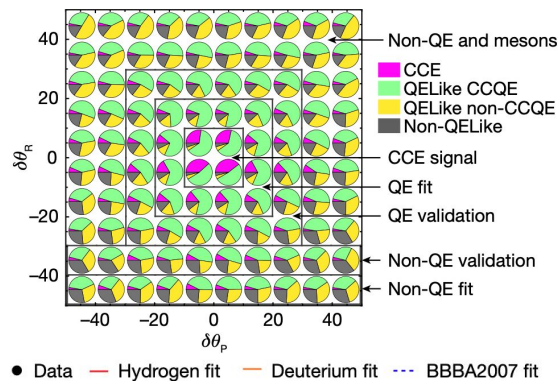
# Neutrons @MINERvA

*Only need the neutron direction!*



# Neutrons @MINERvA

Only need the neutron direction!



CCE xsec measured vs  $Q^2_{QE}$ : **first statistically significant measurement of the anti-ν CCE scattering on the free p!**

Results used to **measure the axial vector form factor** → first measurements on free p!

Favors larger  $F_A$  at higher  $Q^2$  → **deviation from dipole  $F_A$**

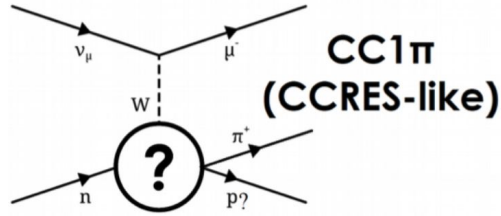
*Dipole*

$$F_A(Q^2) = \frac{F_A(0)}{\left(1 + \frac{Q^2}{(M_A^{QE})^2}\right)^2} \quad \text{?}$$

*z-expansion*

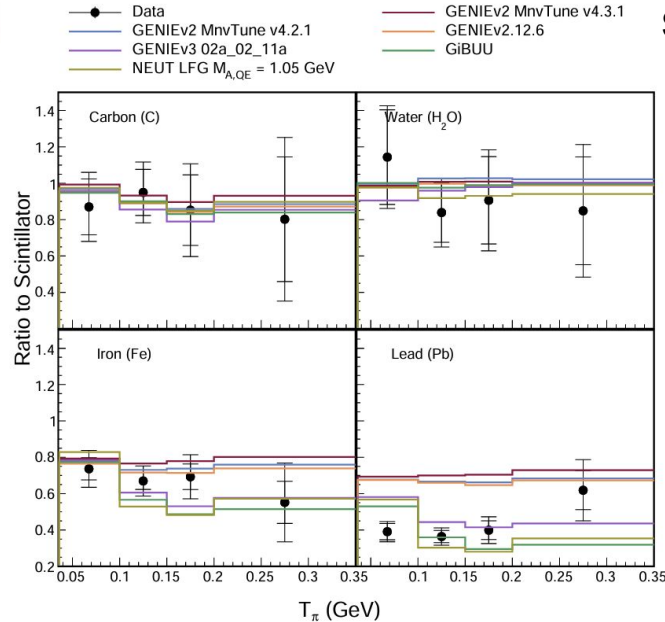
$$F_A(Q^2) = \sum_{k=0}^{k_{\max}} a_k z(Q^2)^k$$

# Pion kinematics

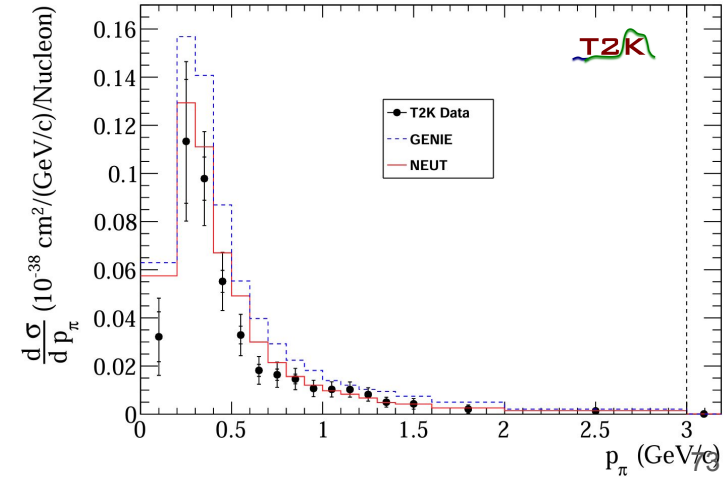


Studying the pion kinematics is also fundamental and help characterizing the CCRES interactions.

As well as studying xsec on different targets simultaneously



Phys. Rev. D 101, 012007 (2020)



# Electron neutrinos

Most of  $\nu_{\mu}$  measurements done with  $\nu_{\mu}$  beam at near detectors, but far detectors particularly interested to  $\nu_e$ . Can we extrapolate from  $\nu_{\mu}$  to  $\nu_e$  → need to study them also at the ND! ( $m_{\mu} \neq m_e$ )

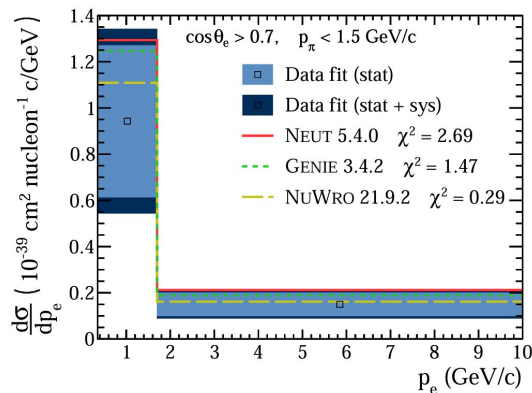
$$E_{\nu}^{\text{peak}} \sim 0.6 \text{ GeV}$$

T2K

First  $\nu_e$  CC1 $\pi^+$  measurement!

Important  $\nu_e$  appearance channel

3D measurement ( $p_e$ ,  $\theta_e$ ,  $p_{\pi}$ ) projected in 1D

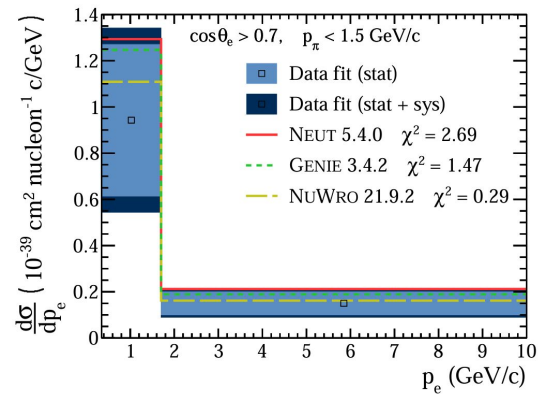


Still low statistics (~100 events), but models seems to overpredict the data

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arXiv:2505.00516

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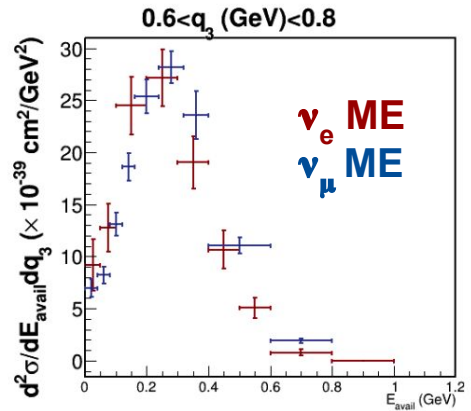
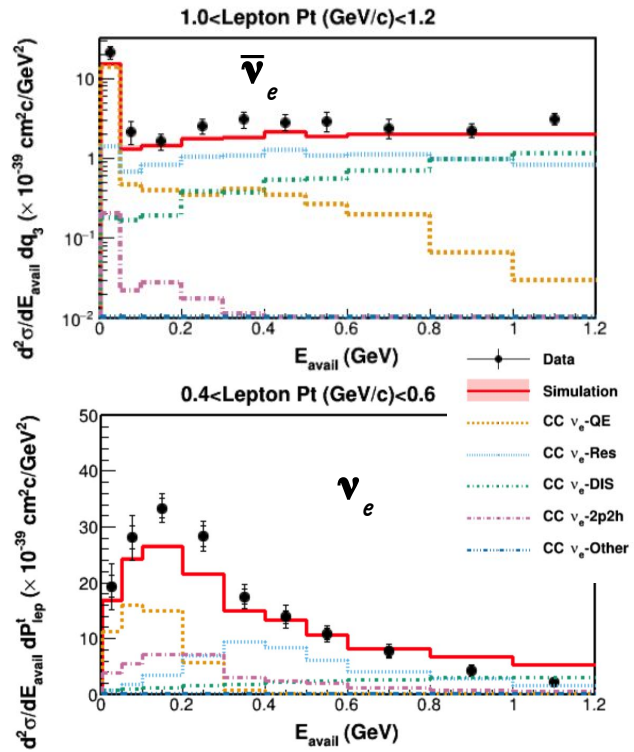
**High statistics (~10<sup>4</sup> events), CC-Inclusive, low  $E_{avail}$  (bkg limit),  $E_e > 2.5 \text{ GeV}$ , ME beam, CH target**

Two 2D cross section measurements ( $E_{avail}, q_3$ ), ( $E_{avail}, p_T$ )



$\langle E_\nu \rangle \sim 6 \text{ GeV}$

Phys. Rev. D 109, 092008 (2024)



Comparison with equivalent  $\nu_\mu$  measurement

# How we concretely extract a cross section



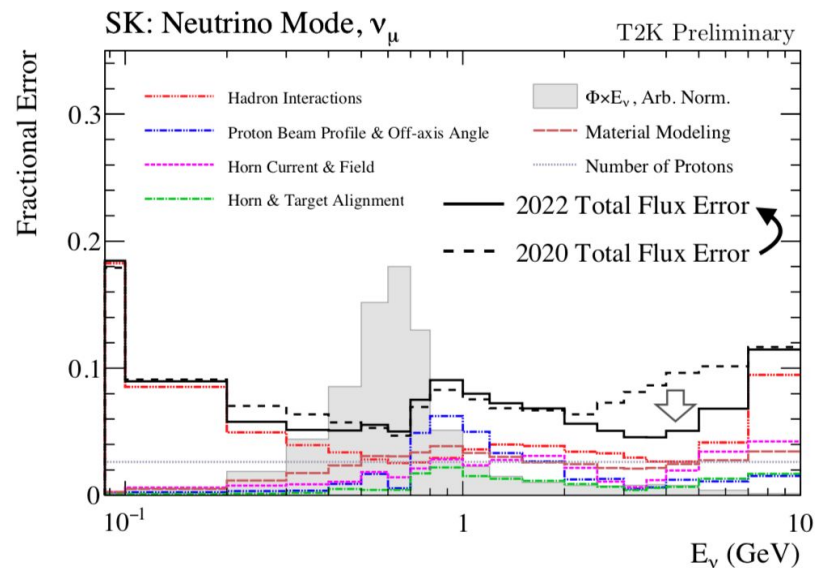
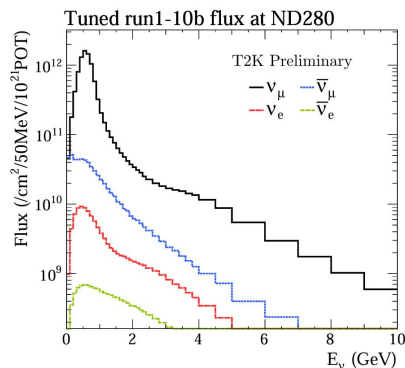
# What are the main systematic sources in a cross-section measurement?

*Examples from T2K*

Since your starting point is a Montecarlo prediction, you should take into account three main systematic sources that will affect it:

## The neutrino flux prediction

Thanks to simulations and external experiments, we are able to quote the uncertainty on our flux predictions in bins of true neutrino energy



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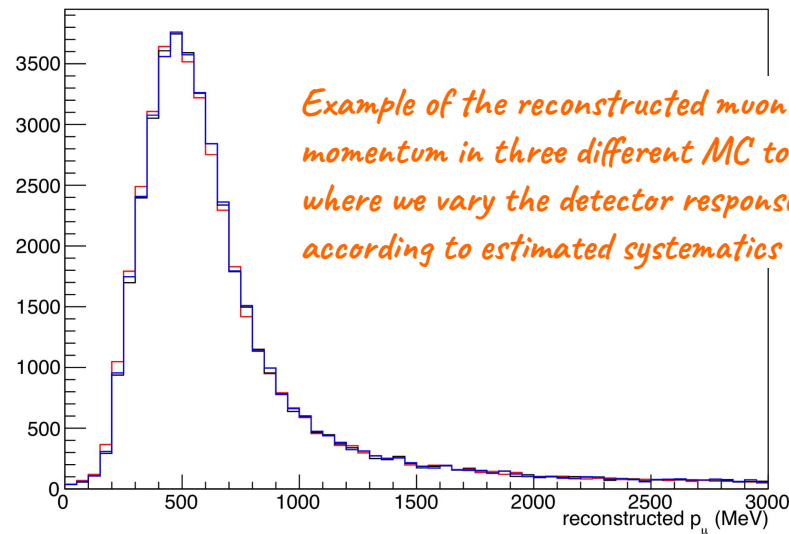
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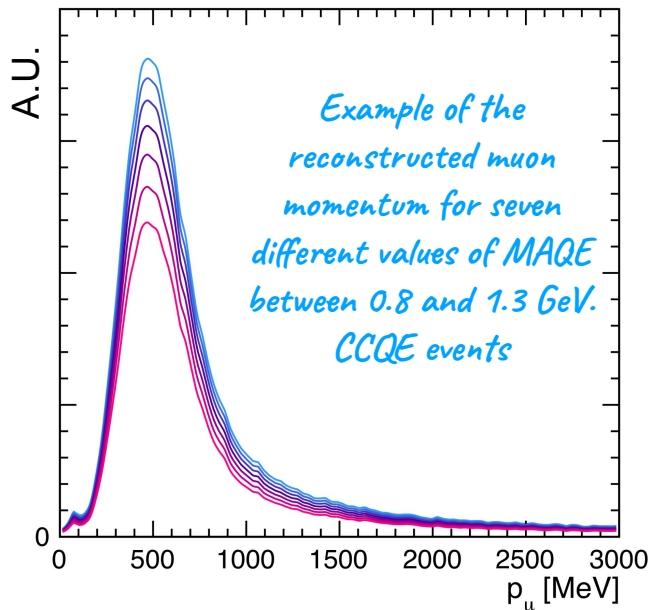
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We have a tool that allows to estimate the reweight to be applied to each event when we vary the value of specific parameters affecting the neutrino interaction predictions



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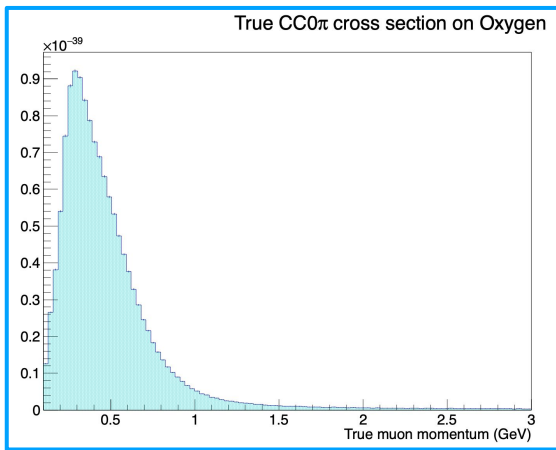
We have a tool that allows to estimate the reweight to be applied to each event when we vary the value of specific parameters affecting the neutrino interaction predictions

$$\frac{d\sigma}{dx_i dy_j} = \frac{\overbrace{N_{ij}^{\text{signal}}}^{\text{green}}}{\underbrace{\epsilon_{ij}}_{\text{cyan}} \underbrace{\Phi}_{\text{green}} \underbrace{N_{\text{nucleons}}^{\text{FV}}}_{\text{orange}}} \times \frac{1}{\Delta x_i \Delta y_j}$$

The effect of these uncertainties will propagate on several elements of the cross-section calculation.

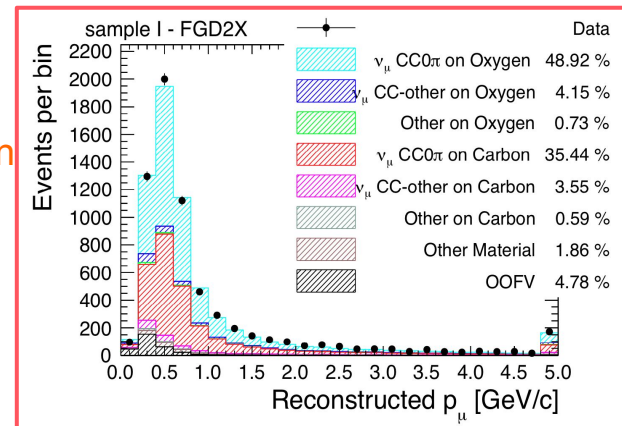
However we have a prior knowledge of these systematics

# The unfolding problem



Detector effects: selection efficiency,  
detector acceptance, observable resolution

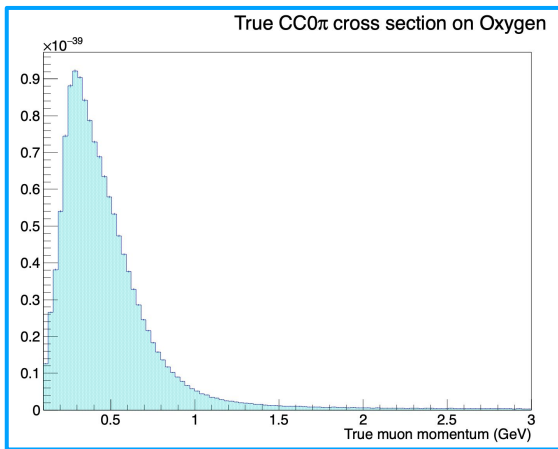
*All these in principle simulated with  
the detector simulation*



*to compare with theoretical  
models we need to provide our  
measurements in the truth space*

*Reconstructed space (the one  
accessible with the detector).*

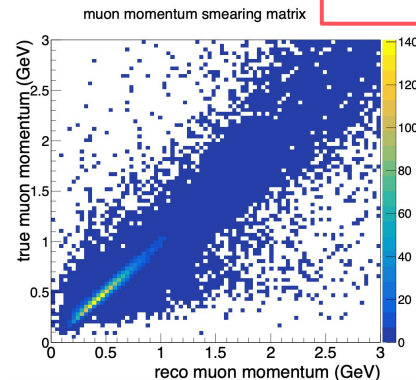
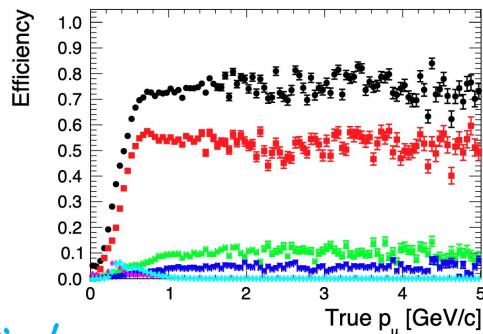
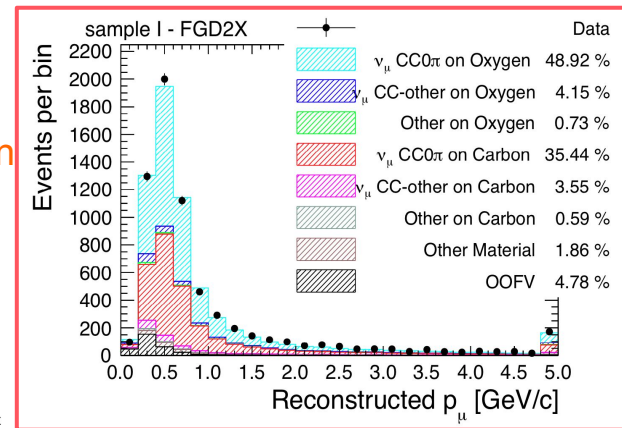
# The unfolding problem



Detector effects: selection efficiency,  
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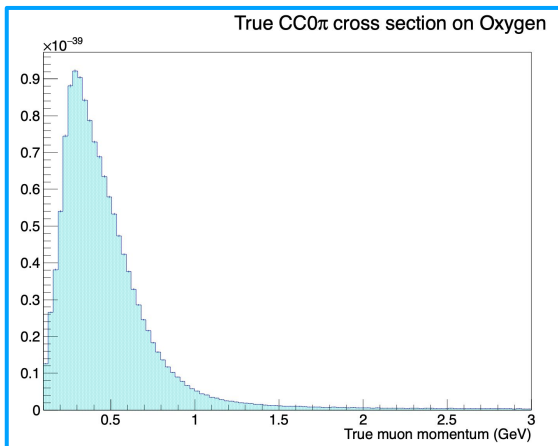
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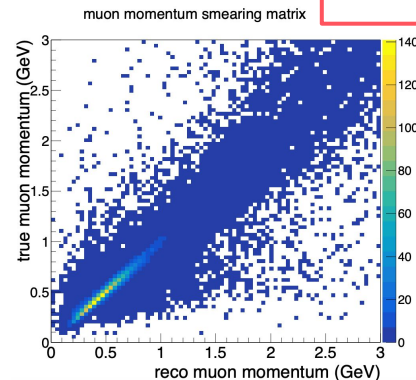
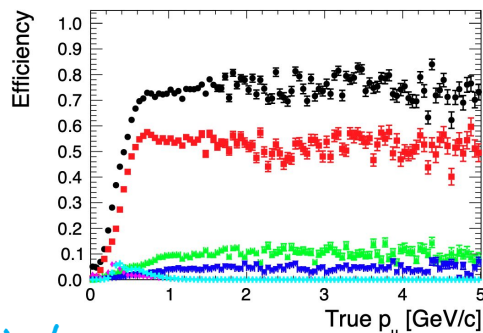
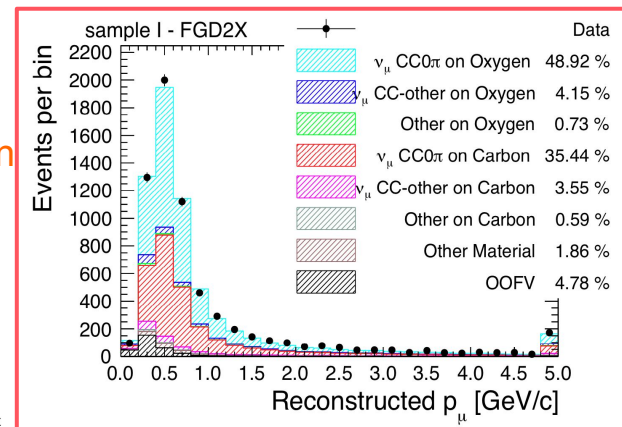
# The unfolding problem



Detector effects: selection efficiency,  
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*All these in principle simulated with  
the detector simulation*



*to compare with theoretical  
models we need to provide our  
measurements in the truth space*

UNFOLDING  
the detector effects

*Reconstructed space (the one  
accessible with the detector).*

# Several unfolding methods exist

1. **Iterative D'Agostini unfolding** (favorite method by MINERVA collab)  
<https://arxiv.org/abs/1010.0632>
2. **Wiener Singular Value Decomposition** (favorite one by MicroBooNE collab)  
<https://doi.org/10.1088/1748-0221/12/10/P10002>
3. **Likelihood fitting** (favorite one by T2K collab)  
[Phys. Rev. D 101, 112004 \(2020\)](#)

**All facing the same (ill-posed) problems**

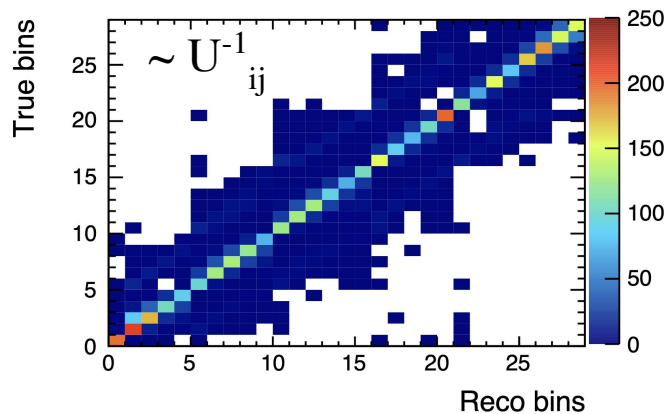
*no time to cover here,  
see [L. Koch](#) for a recap*

Also new methods under development based on Machine Learning techniques :

**Omnifold** [Phys. Rev. Lett. 124, 182001 \(2020\)](#)



# Unfolding via likelihood fitting (in a nutshell)



Essentially you want to export you measurement from the reco to the truth space: you need to unfold the detector effects

*Num. of background events in the true bin  $i$  according to the MC*

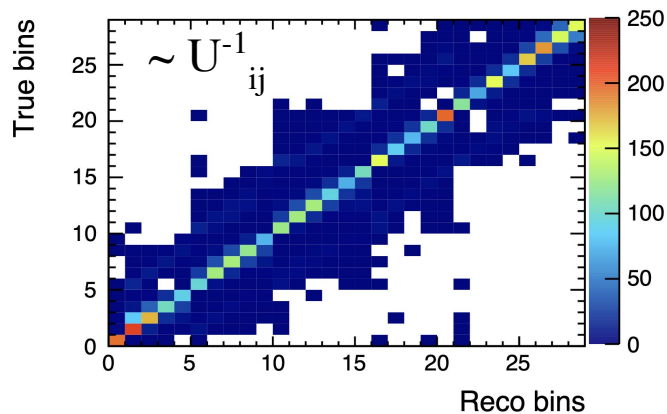
*Smearing matrix to move from the truth to the reco bins*

$$N_j^{\text{reco}} = \sum_i^{\text{true bins}} \left[ c_i N_i^{\text{sig}} + N_i^{\text{bkg}} \right] U_{ij}^{-1}$$

*Num. of reco events in the reco bin  $j$*

$N_i^{\text{signal}}$  = *what we want to extract*

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Standard iterative unfolding requires to know the smearing matrix and essentially invert them to do the unfolding. In the likelihood fitting we don't concretely use a matrix, we leave the fitter to tell us what is the value of  $c_i$

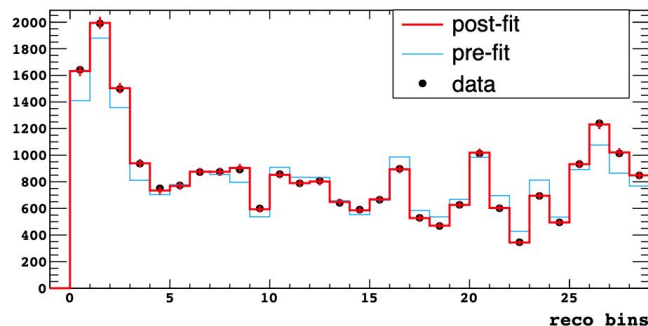
# Zoom on the template parameters

Template parameters are **FREE** parameters that **rescale the MC signal events** (eventually corrected by some systematics) and thus they have the dominant effect (wrt the systematics parameters)

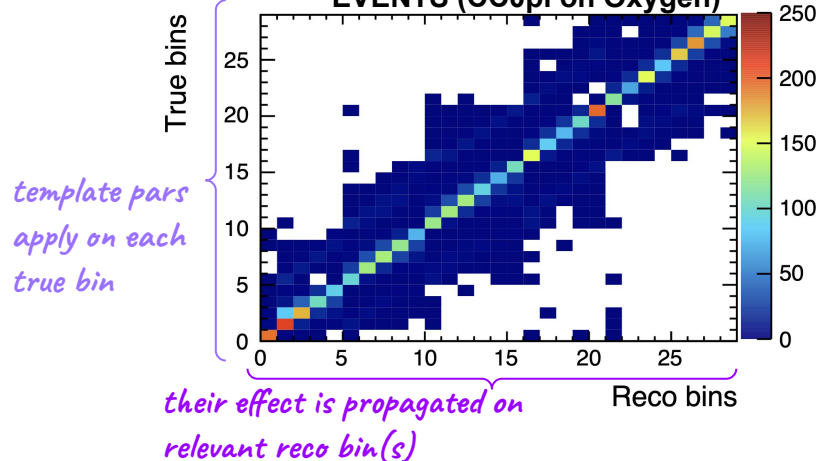
There is **one** template parameter **per truth signal bin** (in which you want to extract your cross section)

They thus **apply on the MC truth space and on MC truth bins of signal events** but they try **to adjust the data/MC agreement in the reco space** (the one that we really measure)  $\Rightarrow$  we don't explicitly use a matrix

## RECO SPACE



Condensed true vs reco bins matrix for SIGNAL EVENTS (CC0pi on Oxygen)



Num. of signal events in the true bin  $i$  according to the MC      Num. of background events in the true bin  $i$  according to the MC

$$N_j^{\text{reco}} = \sum_{i \text{ true bins}} \left[ c_i N_i^{\text{sig}} + N_i^{\text{bkg}} \right] U_{ij}^{-1}$$

Num. of reco events in the reco bin  $j$

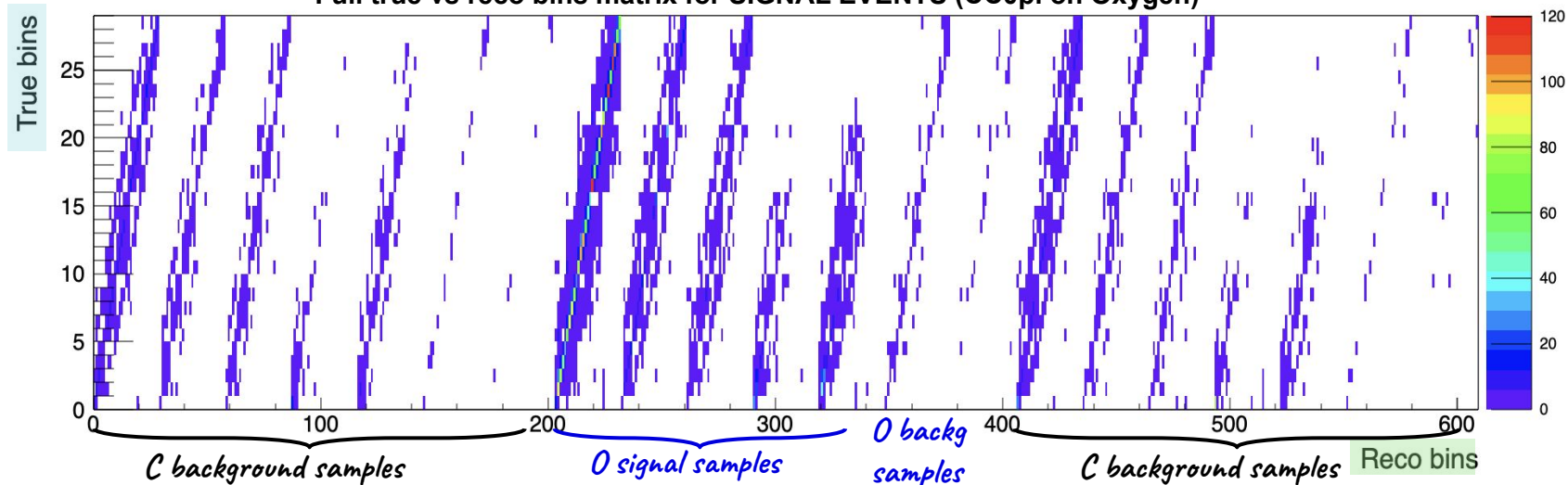
Data/MC correction, aka template parameters

Smearing matrix to move from the truth to the reco bins

# Zoom on the template parameters

from O and C CC0pi analysis

Full true vs reco bins matrix for SIGNAL EVENTS (CC0pi on Oxygen)



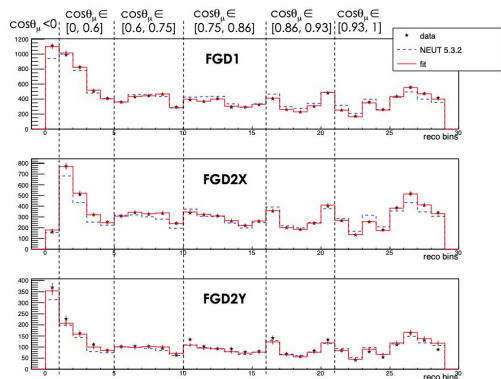
Num. of signal events in the true bin  $i$  according to the MC  
 Num. of background events in the true bin  $i$  according to the MC

$$N_j^{\text{reco}} = \sum_{i \text{ true bins}} \left[ c_i N_i^{\text{sig}} - N_i^{\text{bkg}} \right] U_{ij}^{-1}$$

Num. of reco events in the reco bin  $j$

$c_i$  Data/MC correction, aka template parameters

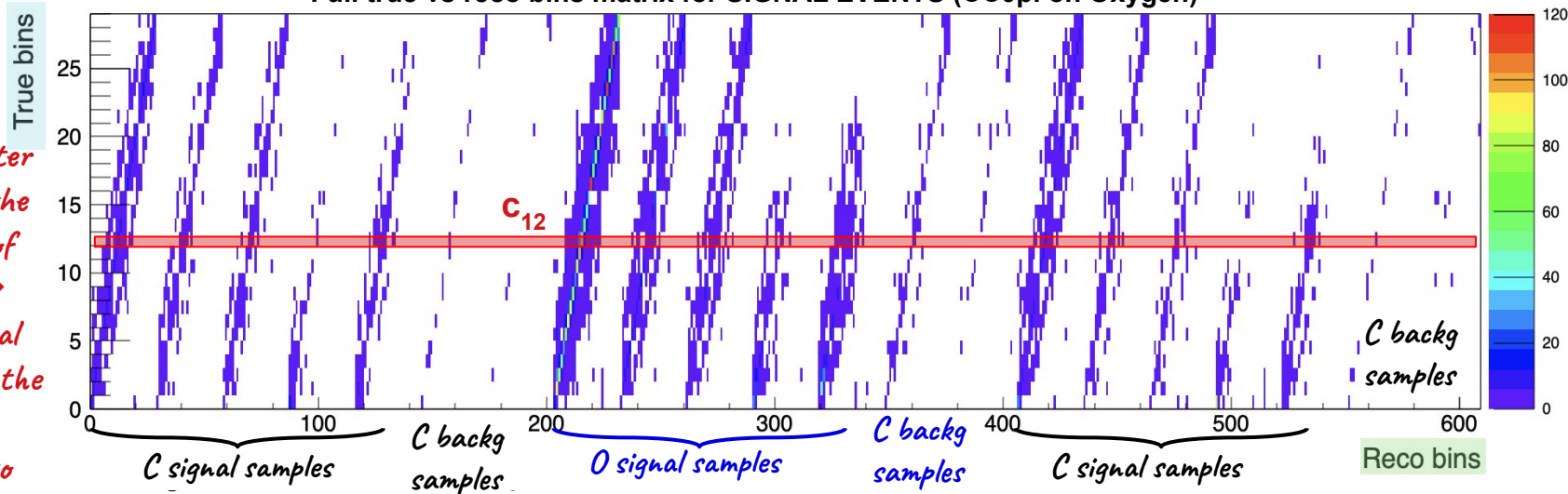
Smearing matrix to move from the truth to the reco bins



# Zoom on the template parameters

from O and C CC0pi analysis

Full true vs reco bins matrix for SIGNAL EVENTS (CC0pi on Oxygen)



Moving parameter  $c_{12} \Leftrightarrow$  moving the signal content of truth bin 12  $\Leftrightarrow$  moving the signal content of ALL the reco bins corresponding to true bin 12  $\Leftrightarrow$  agreement with data is checked in the reco space over all the reco bins depending on true bin 12

Num. of signal events in the true bin  $i$  according to the MC Num. of background events in the true bin  $i$  according to the MC

$$N_j^{\text{reco}} = \sum_i^{\text{true bins}} \left[ c_i N_i^{\text{sig}} - N_i^{\text{bkg}} \right] U_{ij}^{-1}$$

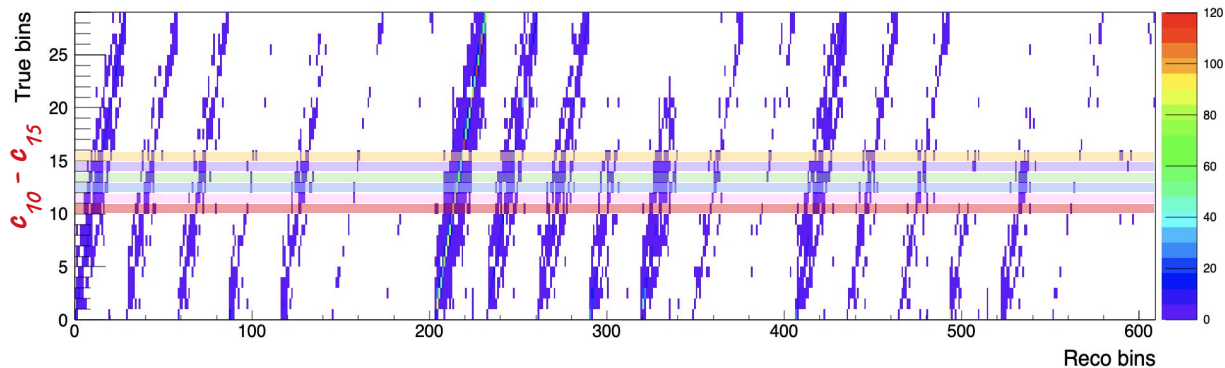
Num. of reco events in the reco bin  $j$

Data/MC correction, aka template parameters

Smearing matrix to move from the truth to the reco bins

# Zoom on the template parameters

from O and C CCOpi analysis



Num. of signal events in the true bin  $i$  according to the MC

Num. of background events in the true bin  $i$  according to the MC

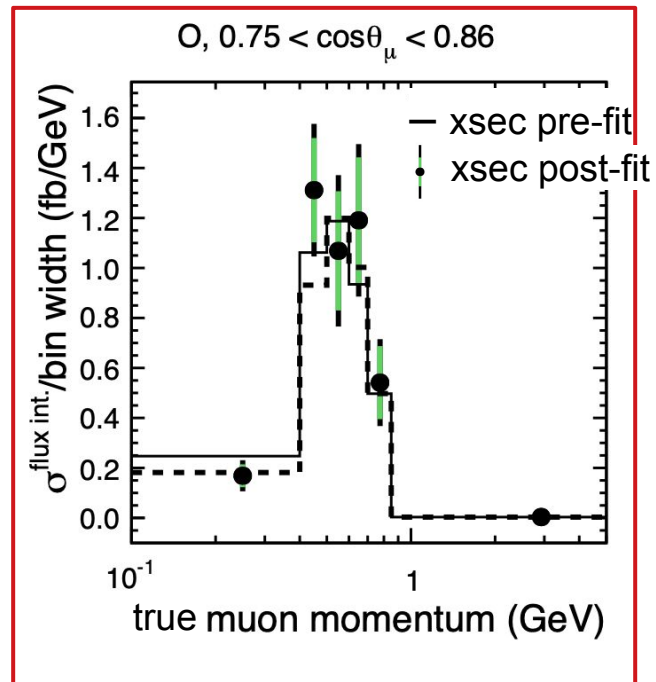
$$N_j^{\text{reco}} = \sum_i^{\text{true bins}} [c_i N_i^{\text{sig}} - N_i^{\text{bkg}}] U_{ij}^{-1}$$

Num. of reco events in the reco bin  $j$

Data/MC correction, aka template parameters

Smearing matrix to move from the truth to the reco bins

## TRUE SPACE

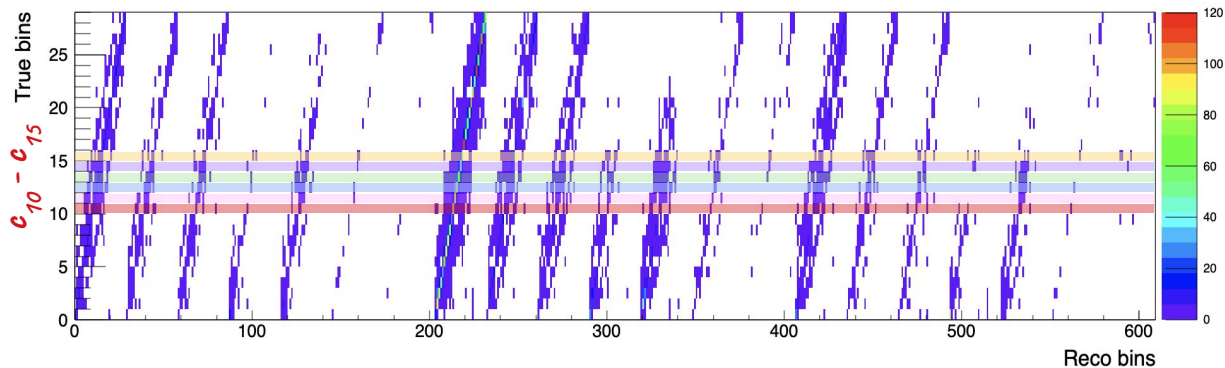


$\text{xsec post-fit} \sim c_i * (\text{xsec pre-fit})$



# Zoom on the template parameters

from O and C CCOpi analysis



Num. of signal events in the true bin  $i$  according to the MC

Num. of background events in the true bin  $i$  according to the MC

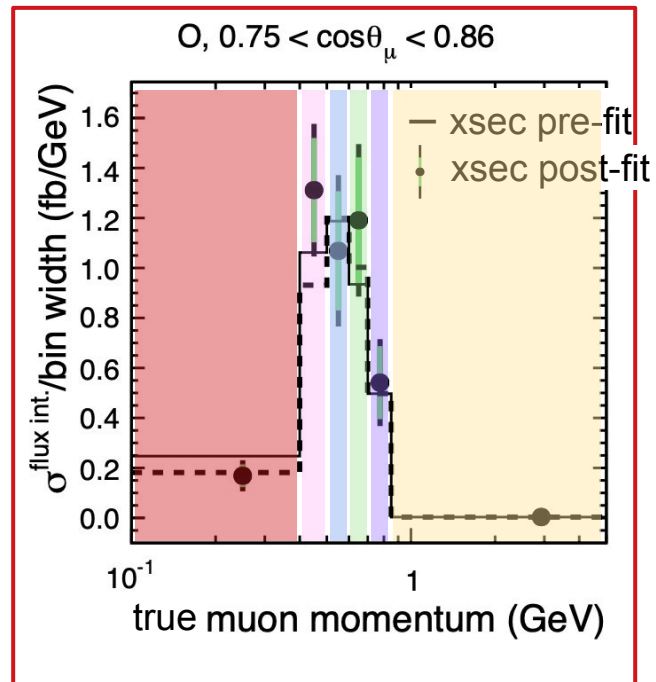
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## TRUE SPACE



$\text{xsec post-fit} \sim c_i * (\text{xsec pre-fit})$

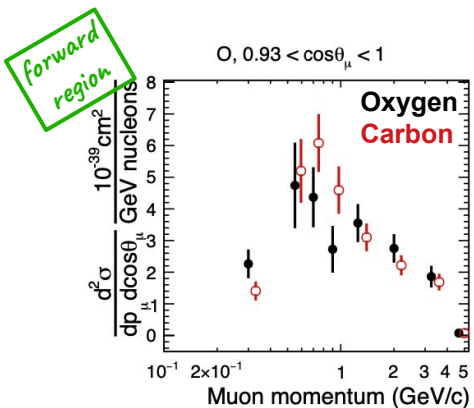
How neutrino cross section measurements help reducing cross section systematics in neutrino oscillation experiments?



# How these measurements are used?

Simultaneous 2D CC0 $\pi$   
measurement on O and C  
@ND280 in  $p_\mu$  and  $\cos\theta_\mu$

*example from recent T2K developments*

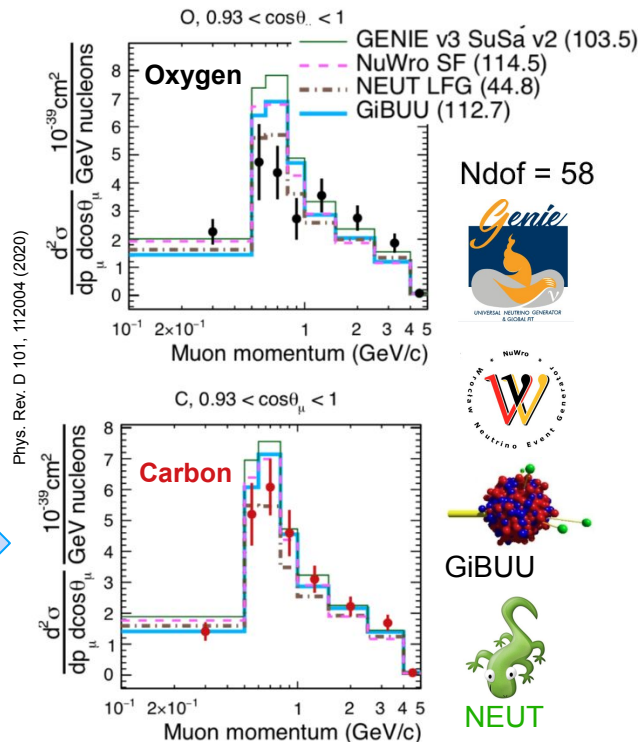
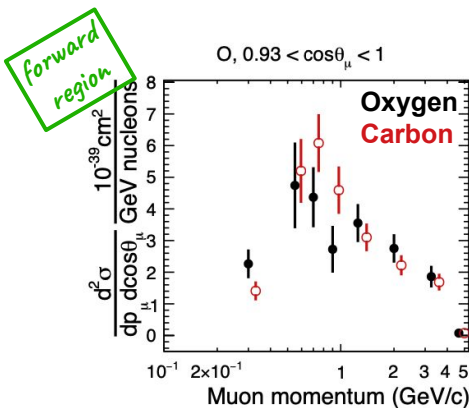


Phys. Rev. D 101, 112004 (2020)

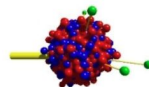
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Ndof = 58



GiBUU



NEUT

Phys. Rev. D 101, 112004 (2020)

*comparison of data against  
different models (SuSav2, SF,  
LFG) and generators (NuWro,  
GENIE, NEUT, GiBUU)*

Other previous tuning examples: MINERvA, MicroBooNE, NOvA

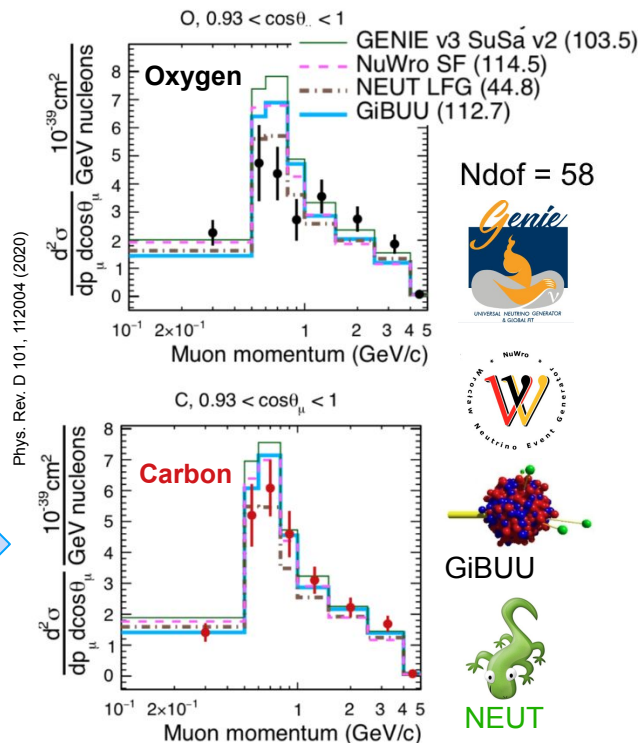
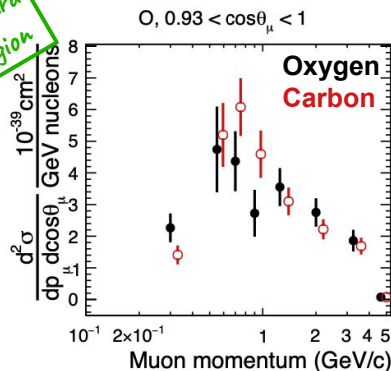
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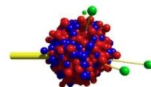
*example from recent T2K developments*

*clear disagreement with most sophisticated  
nuclear model in this region*

*forward  
region*



Ndof = 58



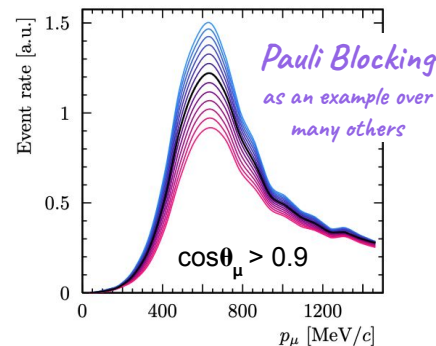
GiBUU



NEUT

Need to develop a **systematics  
parameterisation** of  $\nu$  interaction  
models able to recover enough freedom

Phys. Rev. D 109, 072006 (2024)



Example: Pauli blocking is  
simply modeled in our MC,  
but more complex models  
exist  $\rightarrow$  introduce freedom  
to our PB model

95

*comparison of data against  
different models (SuSv2, SF,  
LFG) and generators (NuWro,  
GENIE, NEUT, GiBUU)*

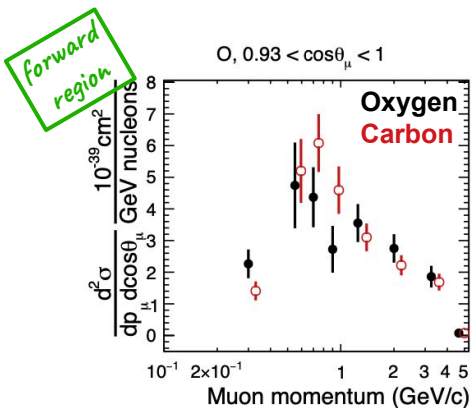
Other previous tuning examples: MINERvA, MicroBooNE, NOvA



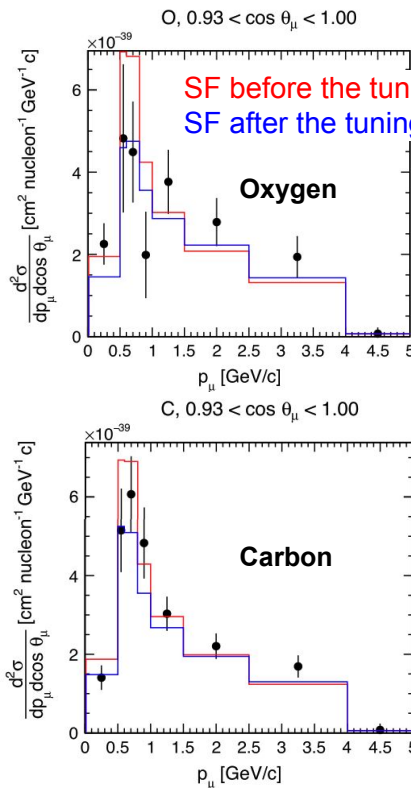
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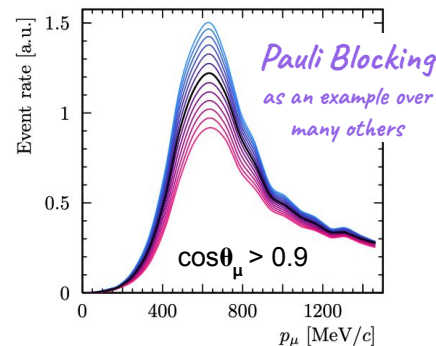


Phys. Rev. D 101, 112004 (2020)



Need to develop a **systematics parameterisation** of  $\nu$  interaction models able to recover enough freedom

Phys. Rev. D 109, 072006 (2024)



*is the parameterisation allowing a good tuning?  
Check on O&C xsec results*

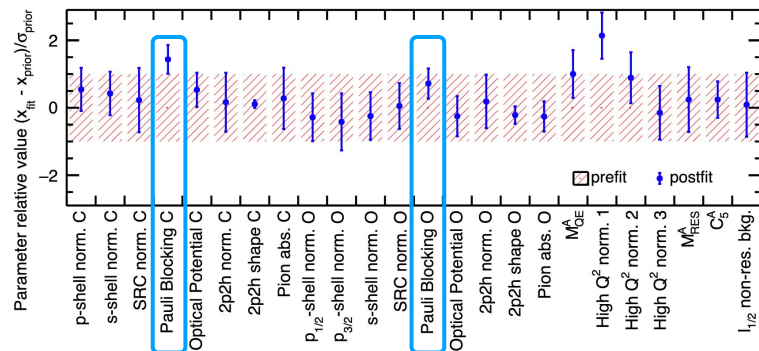
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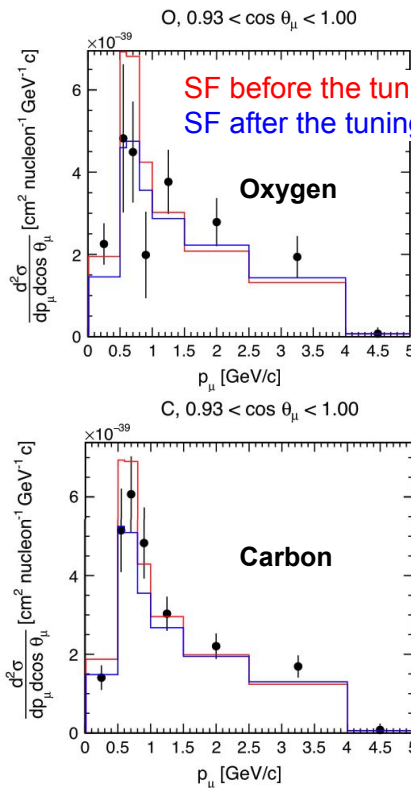
exemple from recent T2K developments



The post tuning agreement is obtained thanks to a fit where we make the SF models to move according to a series of systematics parameters, including PB

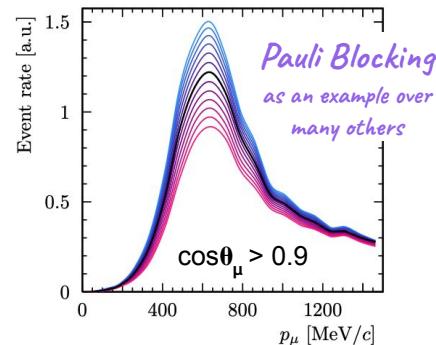


Pauli Blocking has significantly moved, in order to recover the data/MC agreement in the forward region



Need to develop a **systematics parameterisation** of  $\nu$  interaction models able to recover enough freedom

Phys. Rev. D 109, 072006 (2024)



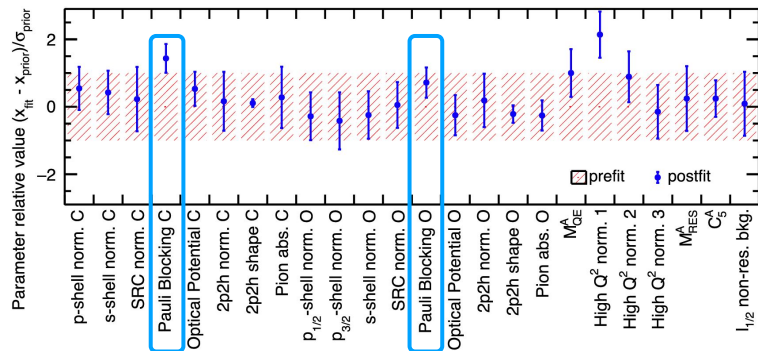
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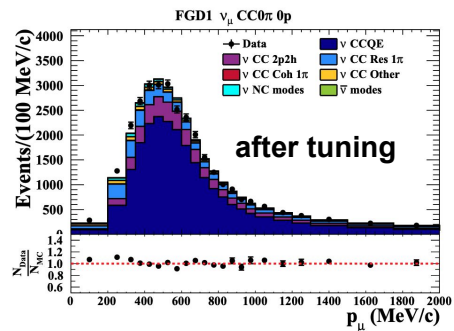
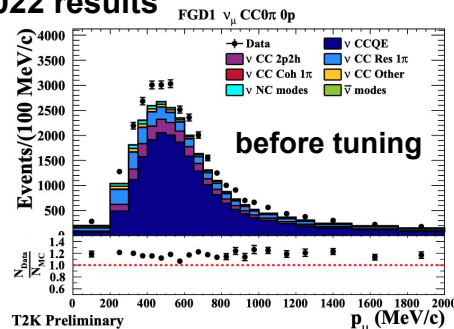
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New parameterisation applied in the official model tuning for the oscillation analysis

Near Detector:  
2022 results

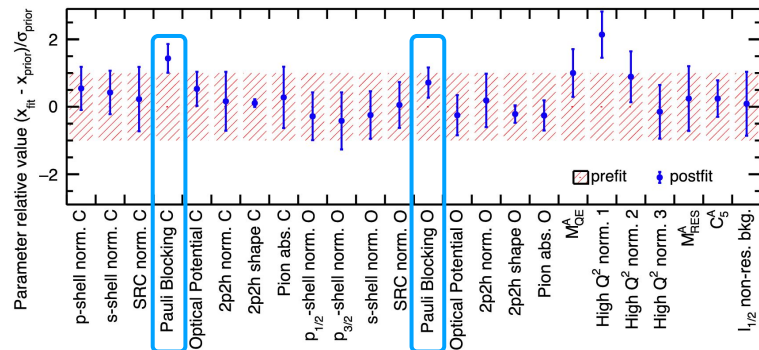




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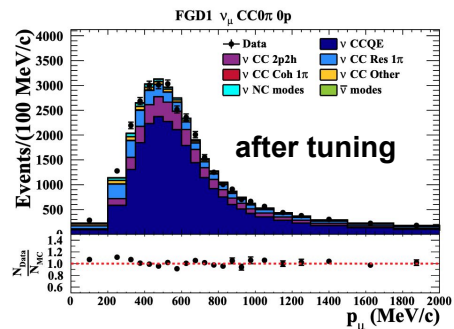
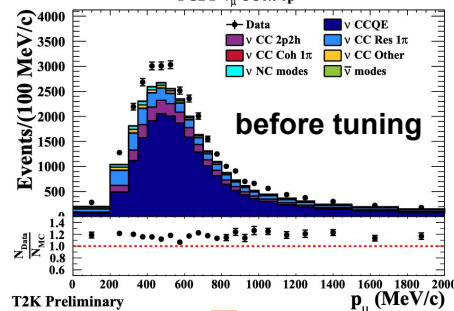


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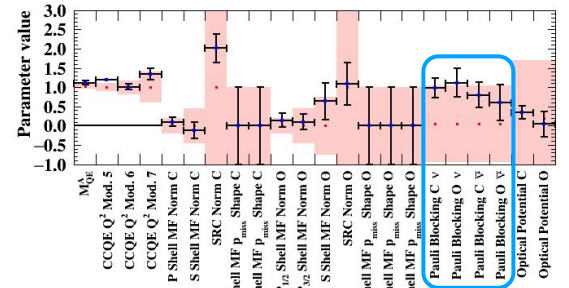
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**Near Detector:  
2022 results**

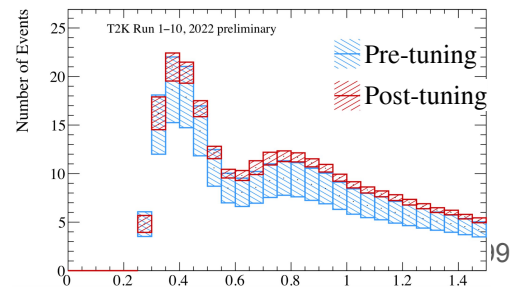


The **tuned model** is used to predict the spectra at the far detector SK: reduced error bars and modified shape/norm

**Near Detector:  
2022 results**



**Far Detector  
predictions**

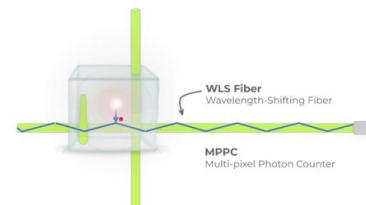
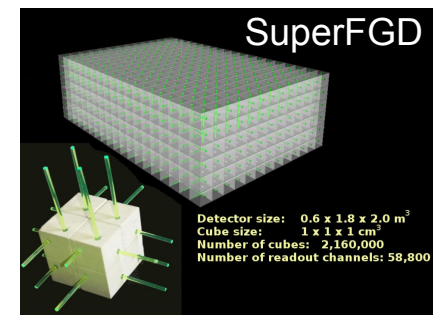
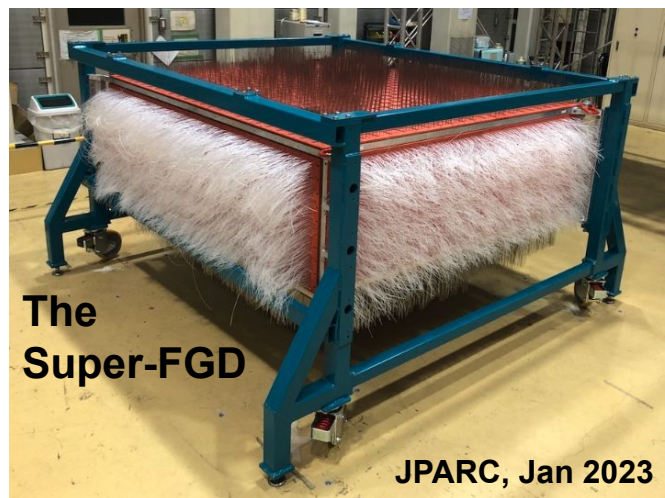
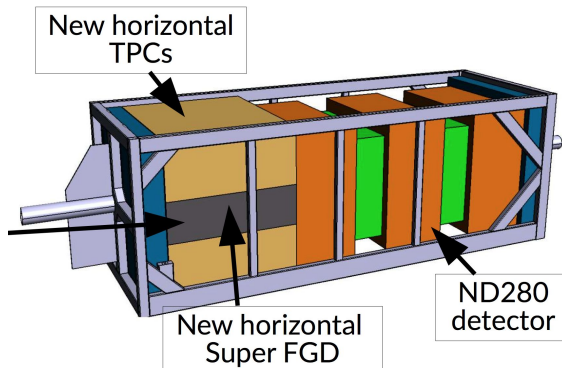
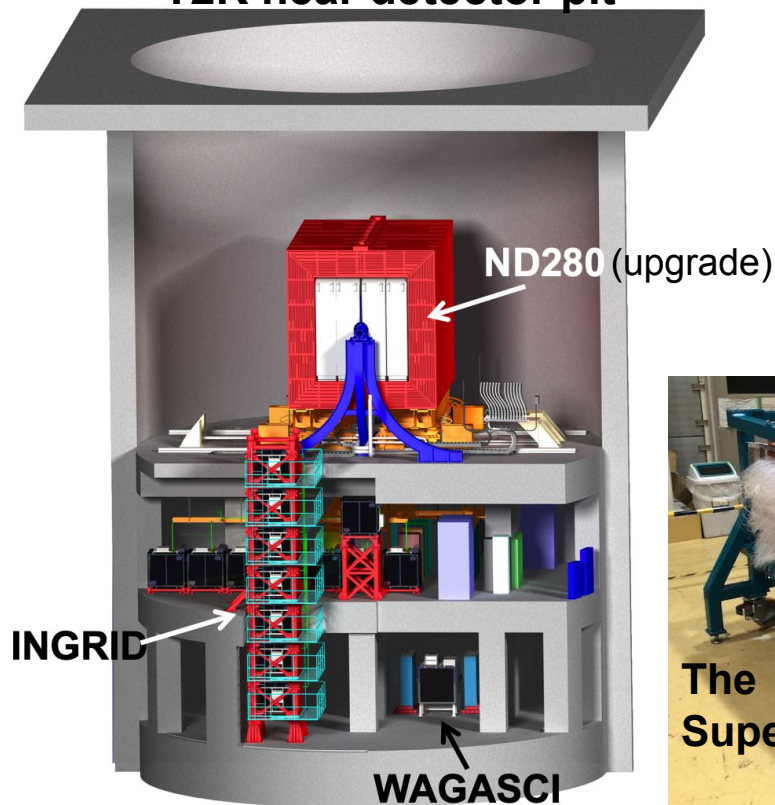


# Future perspectives



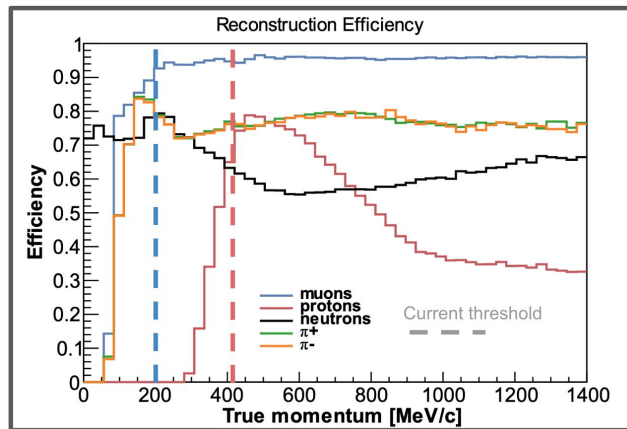
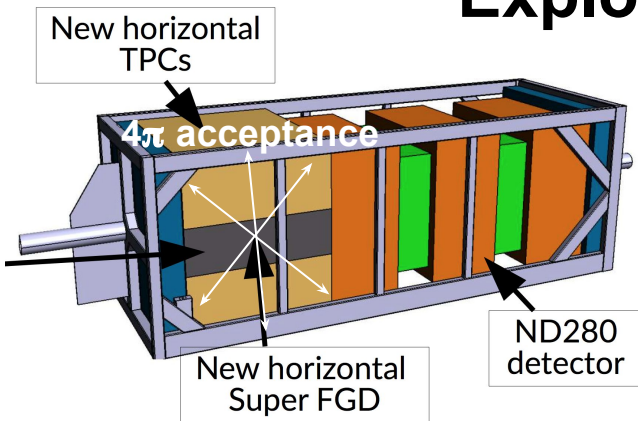
# ND280-Upgrade and the Super-FGD

T2K near detector pit

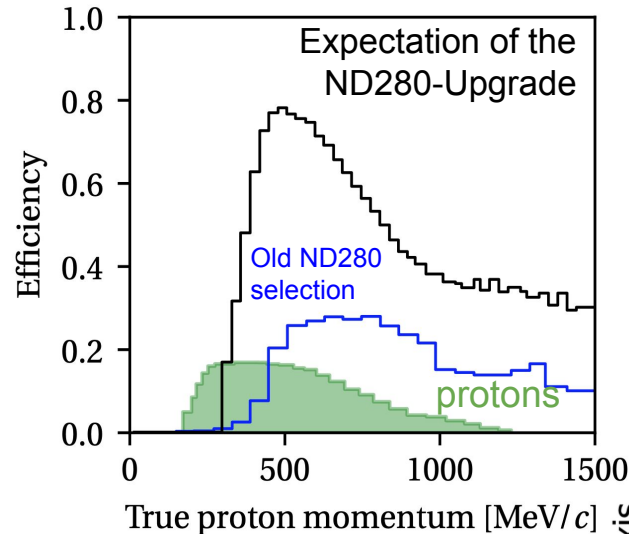


Super-FGD:  $192 \times 192 \times 56$  scintillator cubes (**2 million**) with **3D readout** => 2 tons of fully active target

# Exploiting the ND280-Upgrade capabilities

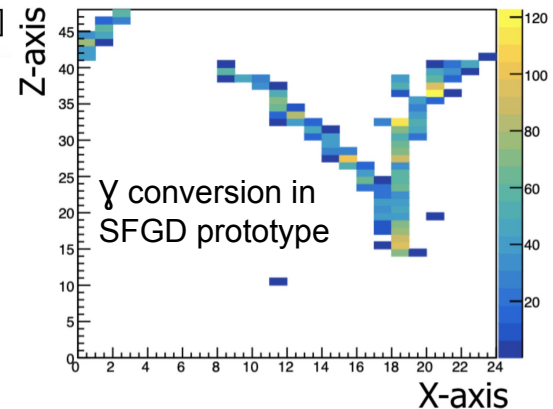
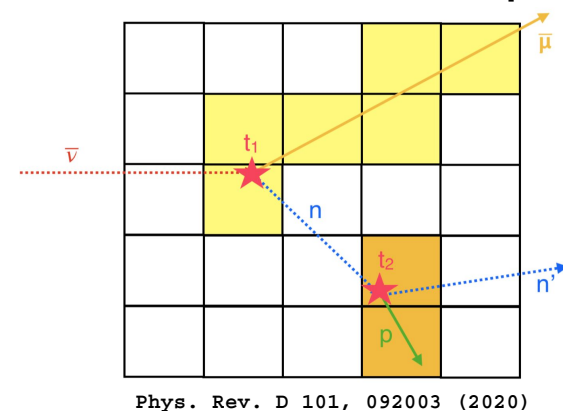


Updated version of plot from [Phys. Rev. D 105, 032010](#) (by Noë Roy)



- + Acceptance!
- + Protons!
- + Pions!
- + Neutrons!
- + better  $\nu_e$  reco!

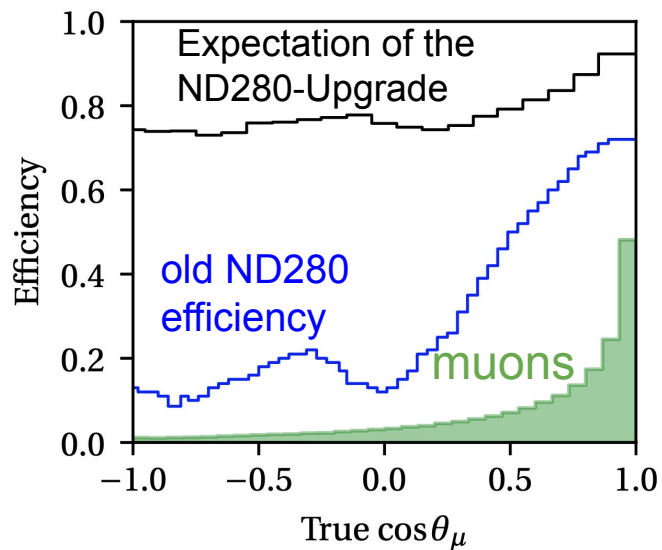
## Neutron detection concept



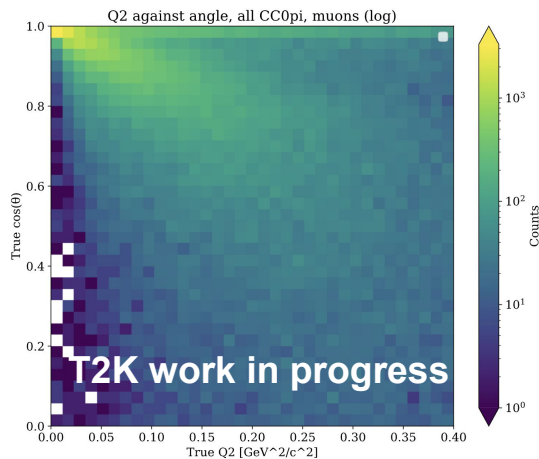
# Measuring high angle muons

Expected almost flat efficiency in  $\cos\theta$  from -1 to 1 with the ND280 Upgrade

detecting higher angle muons

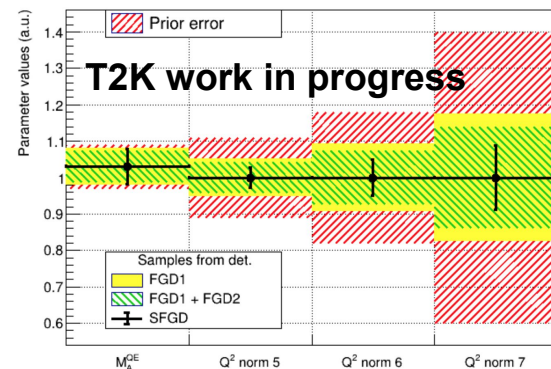


~ exploring higher  $Q^2$  regions



From JB Plancon

~ better characterize the form factor models (as a function of  $Q^2$ )

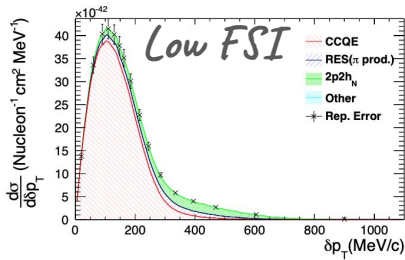
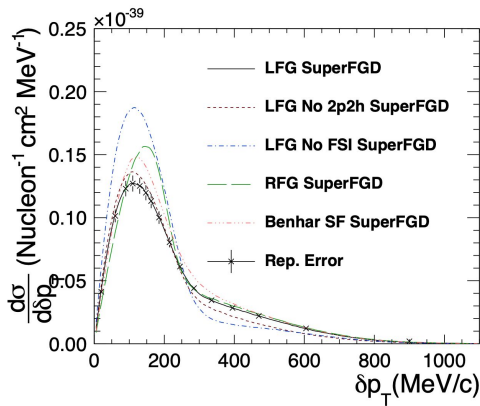


From S. Joshi

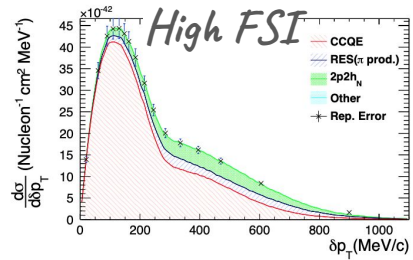
*CC0pi selection*

# Measuring low momentum protons

Discrimination of nuclear models on CH!  
Even better when 2D approach is used

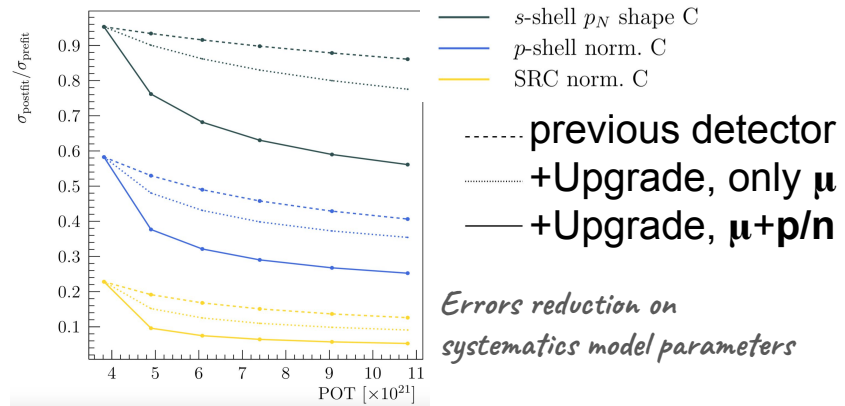


(a) LFG - Low  $\delta\alpha_T$



(b) LFG - High  $\delta\alpha_T$

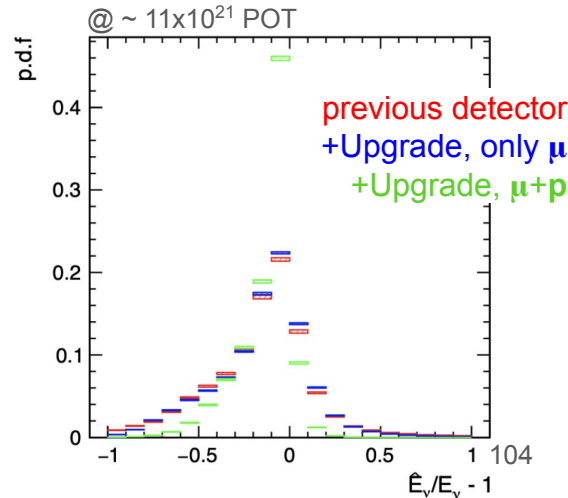
TKI like variables (including Evis) are also good candidates for the model tuning



Errors reduction on systematics model parameters

Better reconstruction of the final state = expected improvements in characterising CCQE and 2p2h interactions

Phys. Rev. D 101, 092003 (2020)

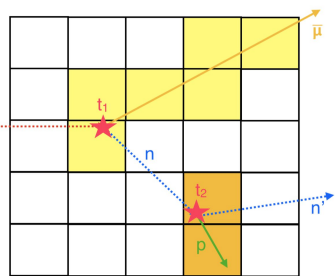


# Measuring neutrons

With time of flight techniques it is possible to reconstruct also the **neutron momentum**  $\rightarrow$  better characterisation of the final state. But also possible to measure  $\delta p_T$

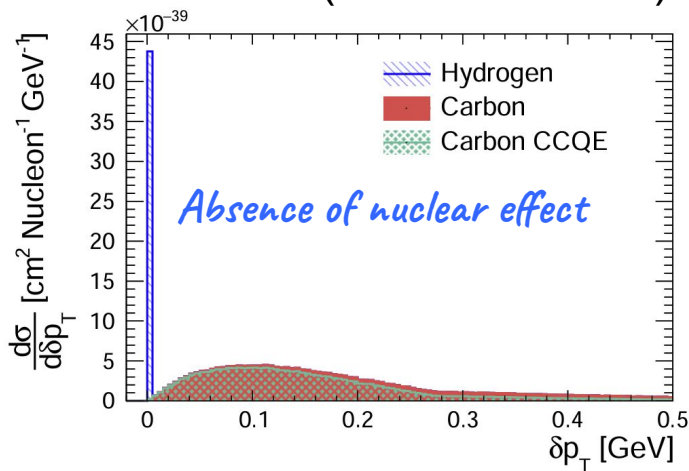
**Possible to isolate interactions on free protons** applying cuts on  $\delta p_T$

$$\delta p_T = |\vec{p}_T^l + \vec{p}_T^n|$$

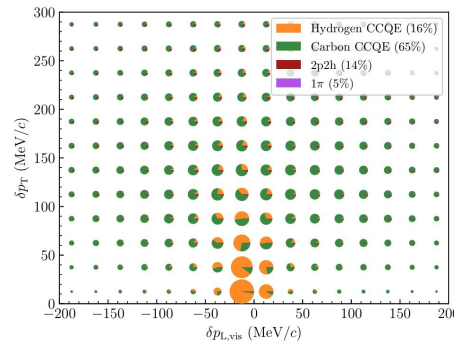
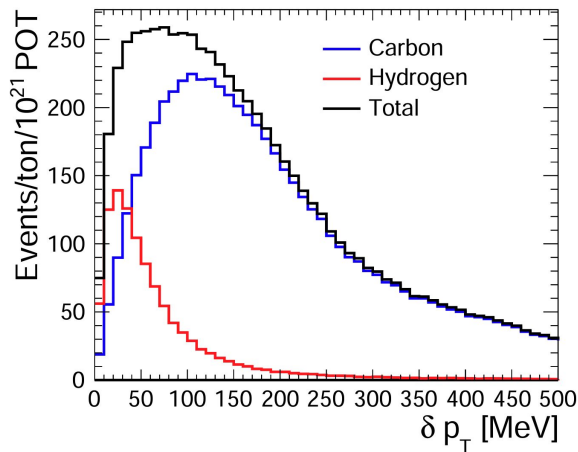


Phys. Rev. D 101, 092003 (2020)

True CCQE (T2K simulation)



Reco CC0π (T2K simulation)

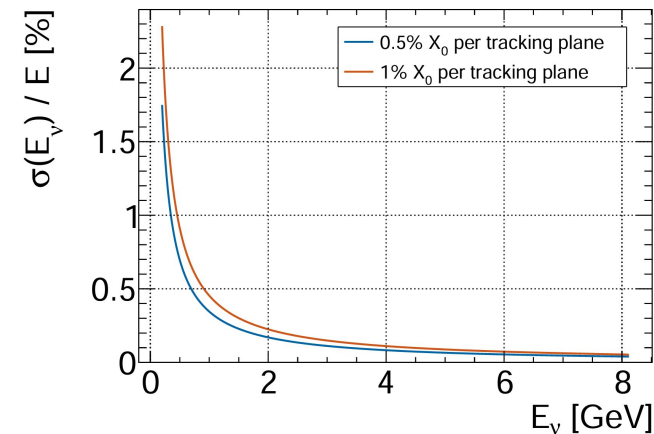


Phys. Rev. D 110, 032019 (2024)

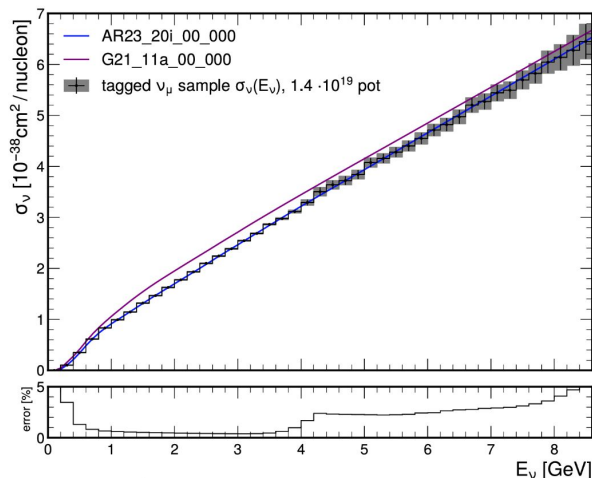
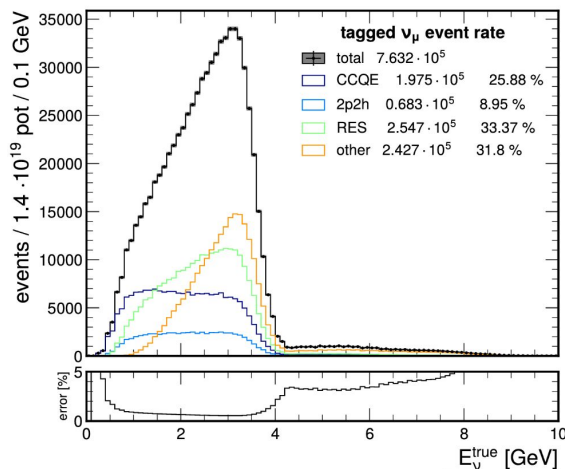
Possible better measurement of  $F_A(Q^2)$



# Prospect with a tagged neutrino beam @CERN (NuSCOPE)



With a tagged neutrino beam we should be able to know the neutrino energy BEFORE the interaction → major breakthrough since for **the first time we could be able to measure neutrino xsec as a function of  $E_\nu$  !!**



See back  
Mathieu's [lecture](#)

# Final thoughts

- Neutrino cross sections are a **very active and pretty fundamental field** to ensure neutrino oscillation experiment success
- A **variety of experiments** involved in the quest for the neutrino interaction understanding → complementarity of the measurement and sharing of best practice
- Impressive progresses in recent years, the community has grown and learned a lot of things
- Also, new measurements from other experiments will come soon: **ICARUS**, **SBND**, **ArgonCube** (Argon), the **ND280-Upgrade** (CH), **NINJA** (water et al), **Annie** (water), nuSCOPE (?)
- Still many things to do from both the experimental and the theoretical point of view
- Need to **act as a community together with theoreticians and generator developers**, (like **NuStec**)
- Amount of available data is increasing and complexifying: towards a **standardised Data Release format** for **data preservation** ~HepData







# A typical $\nu$ oscillation experiment

Oscillation experiments require to know  $\Phi(E_\nu)$ ,  $\sigma(E_\nu, \vec{x})$  &  $D(\vec{x})$ ...  
simplified version:

$$\frac{N_{events}^{far}(\vec{x})}{N_{events}^{near}(\vec{x})} =$$

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Oscillation probability  
depends on true  $E_\nu$

$$\frac{N_{events}^{far}(\vec{x})}{N_{events}^{near}(\vec{x})} = \frac{\sigma(E_\nu, \vec{x}) \otimes \Phi^{far}(E_\nu) \otimes D^{far}(\vec{x}) \otimes P_{osc}(E_\nu)}{\sigma(E_\nu, \vec{x}) \otimes \Phi^{near}(E_\nu) \otimes D^{near}(\vec{x})}$$

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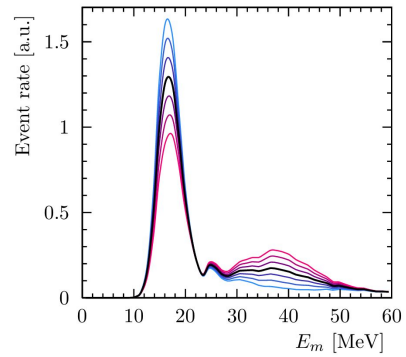
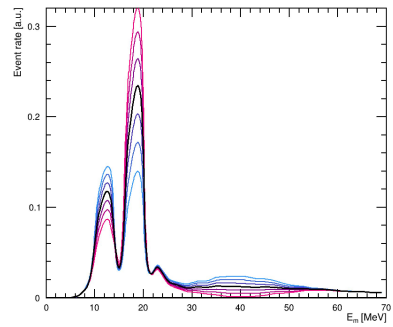
$\nu$  beam is not monochromatic

Detector effects  
(efficiency, acceptance, target, resolution)

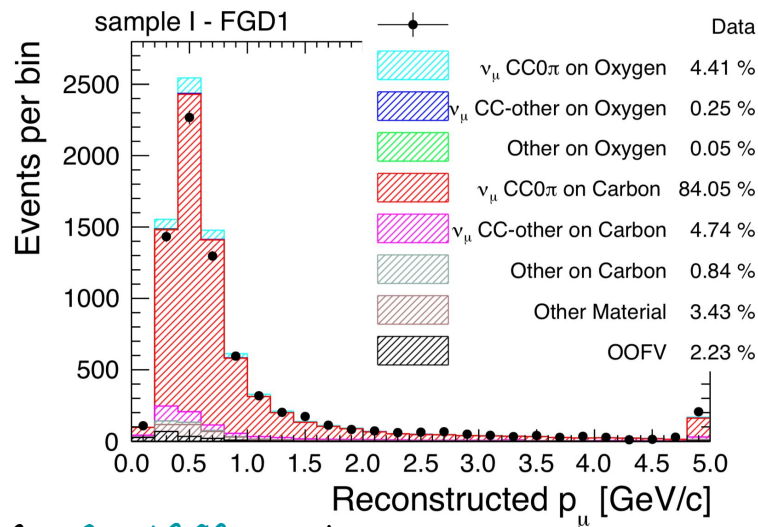
Near/far ratios don't fully cancel systematics:

- $\Phi(E_\nu)$  change due to geometry and oscillation
- Acceptance, efficiency and targets different in the 2 detectors (near and far)
- ND is  $\nu_\mu$  dominated, but used to infer (via model)  $\nu_e$

## **Delicate analysis!**



# What are the info contained in the reco bins?



We usually have several reconstructed signal samples as well as several reconstructed background samples

We usually bin reconstructed events in well reconstructable observables (like  $\cos\theta_\mu$  and/or  $p_\mu$ ), that are also the variable we could use to extract the cross section

In a reconstructed CC0 $\pi$  ( $\cos\theta_\mu$ ,  $p_\mu$ ) bin ( $j$ ) we have  $N_j$  reco events:

from O and C CC0pi analysis

$$N_j^{\text{reco}} = \sum_i^{\text{true bins}} \left[ \underbrace{c_i w_i^{\text{signal}} N_i^{\text{signal}}}_{\boxed{N_i^{\text{signal}}} = \text{what we want to extract}} + \underbrace{w_i^{\text{bkg}} N_i^{\text{bkg}}}_{\text{Reweight due to the systematics effect}} \right] \underbrace{U_{ij}^{-1}}_{\text{Smearing matrix to move from the truth to the reco bins}}$$

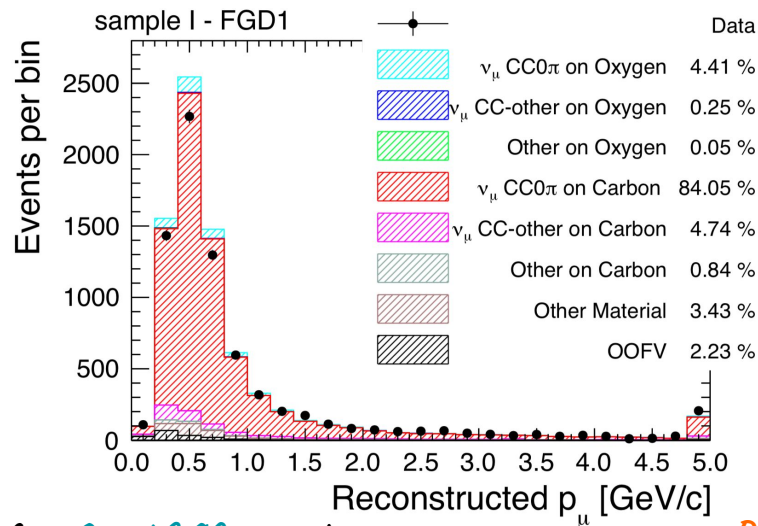
*Num. of reco events in the reco bin  $j$  and sample  $s$*

*Num. of background events in the true bin  $i$  according to the MC*

*Smearing matrix to move from the truth to the reco bins*



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*Num. of signal events the systematics effect according to the MC*

*Num. of background events in the true bin  $i$  according to the MC*

*Smearing matrix to move from the truth to the reco bins*

*Num. of reco events in the reco bin  $j$  and sample  $s$*

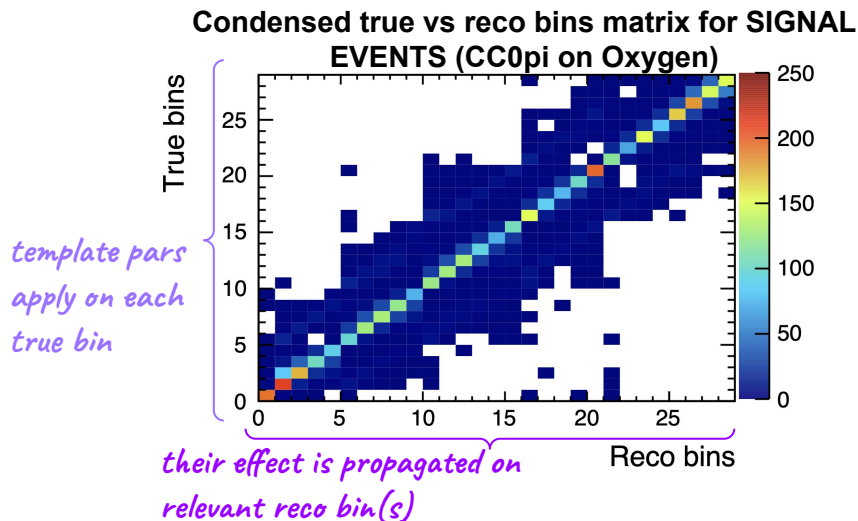
# Zoom on the template parameters

Template parameters ARE the **parameters of interest** in our xsec analyses

They are **FREE** parameters that rescale the MC signal events (eventually corrected by some systematics) and thus they have the dominant effect (wrt the systematics parameters)

There is **one** template parameter **per truth signal bin** (in which you want to extract your cross section)

They thus **apply on the MC truth space and on MC truth bins of signal events** but they try to adjust the **data/MC agreement in the reco space** (the one that we really measure)



$$N_j^{\text{reco}} = \sum_i^{\text{true bins}} \left[ \begin{array}{c} \text{Reweight due to the systematics effect} \\ c_i w_i^{\text{signal}} \end{array} \begin{array}{c} \text{Num. of signal events according to the MC} \\ N_i^{\text{signal}} \end{array} + \begin{array}{c} \text{Reweight due to the systematics effect} \\ w_i^{\text{bkg}} \end{array} \begin{array}{c} \text{Num. of background events in the true bin } i \text{ according to the MC} \\ N_i^{\text{bkg}} \end{array} \right] U_{ij}^{-1}$$

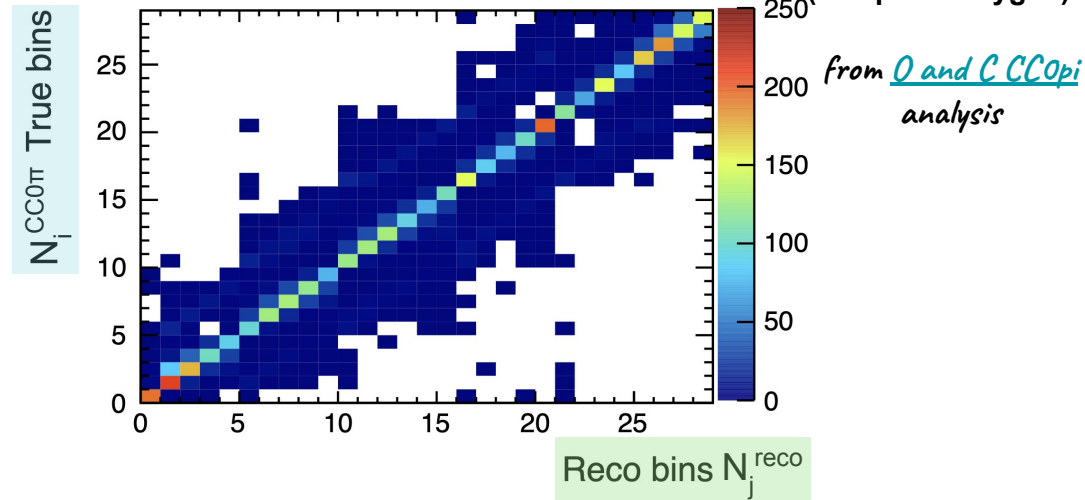
Num. of reco events in the reco bin  $j$  and sample  $s$

Data/MC correction, aka template parameters

Smearing matrix to move from the truth to the reco bins

# Zoom on the template parameters

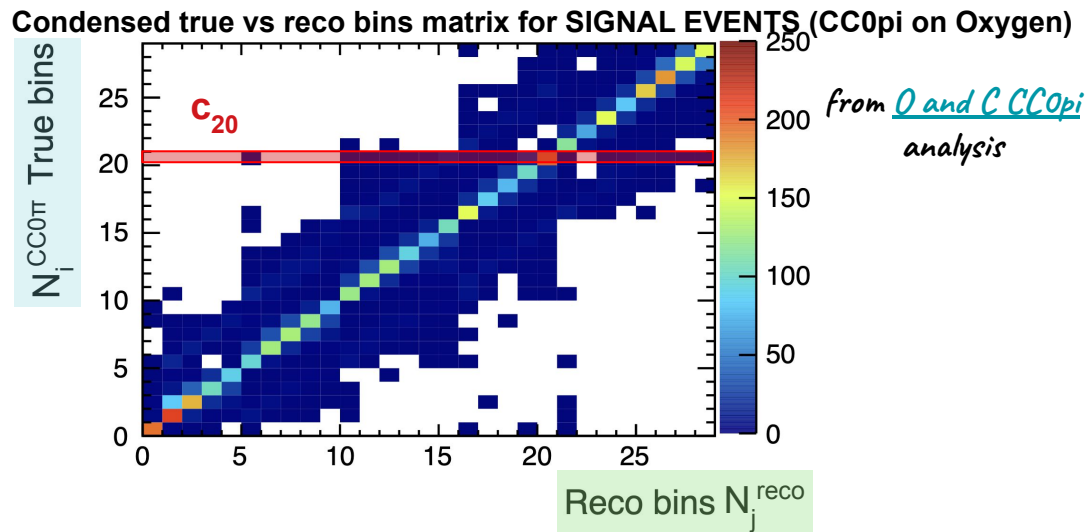
Condensed true vs reco bins matrix for SIGNAL EVENTS (CC0pi on Oxygen)



$$\begin{aligned}
 & \text{Num. of reco events in the reco bin } j \text{ and sample } s \\
 & N_j^{\text{reco}} = \sum_i^{\text{true bins}} \left[ \begin{array}{l} \text{Reweight due to the systematics effect} \quad \text{Num. of signal events in the true bin } i \text{ according to the MC} \\ c_i w_i^{\text{signal}} N_i^{\text{signal}} \end{array} + \begin{array}{l} \text{Num. of background events in the true bin } i \text{ according to the MC} \\ w_i^{\text{bkg}} N_i^{\text{bkg}} \end{array} \right] U_{ij}^{-1} \\
 & \text{Data/MC correction, aka template parameters} \quad \text{Reweight due to the systematics effect} \quad \text{Smearing matrix to move from the truth to the reco bins}
 \end{aligned}$$

# Zoom on the template parameters

Moving parameter  $c_{20} \Leftrightarrow$  moving the signal content of truth bin 20  $\Leftrightarrow$  moving the signal content of ALL the reco bins corresponding to true bin 20  $\Leftrightarrow$  agreement with data is checked in the reco space



$$N_j^{\text{reco}} = \sum_i^{\text{true bins}} \left[ \begin{array}{l} \text{Reweight due to the systematics effect} \quad \text{Num. of signal events in the true bin } i \text{ according to the MC} \\ c_i w_i^{\text{signal}} N_i^{\text{signal}} \end{array} + \begin{array}{l} \text{Num. of background events in the true bin } i \text{ according to the MC} \\ w_i^{\text{bkg}} N_i^{\text{bkg}} \end{array} \right] U_{ij}^{-1}$$

Num. of reco events in the reco bin  $j$  and sample  $s$

Data/MC correction, aka template parameters

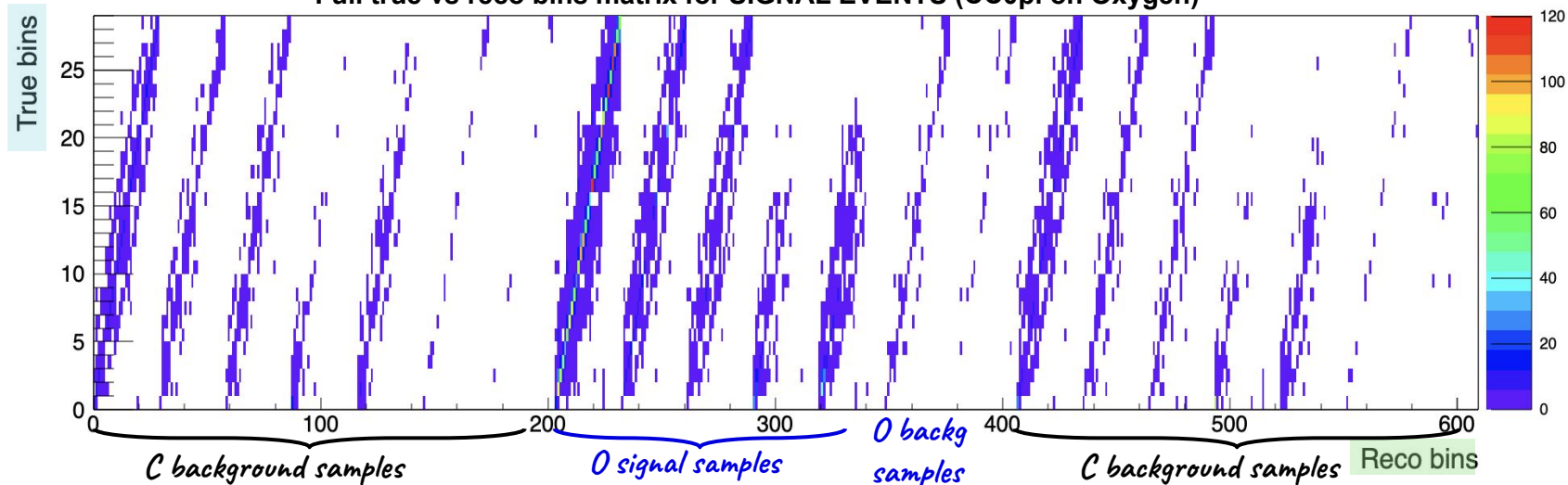
Reweight due to the systematics effect

Smearing matrix to move from the truth to the reco bins

# Zoom on the template parameters

from O and C CC0pi analysis

Full true vs reco bins matrix for SIGNAL EVENTS (CC0pi on Oxygen)



$$N_j^{\text{reco}} = \sum_i^{\text{true bins}} \left[ \underbrace{c_i w_i^{\text{signal}}}_{\text{Data/MC correction, aka template parameters}} N_i^{\text{signal}} + \underbrace{w_i^{\text{bkg}}}_{\text{Reweight due to the systematics effect}} N_i^{\text{bkg}} \right] \underbrace{U_{ij}^{-1}}_{\text{Smearing matrix to move from the truth to the reco bins}}$$

Num. of reco events in the reco bin  $j$  and sample  $s$

Reweight due to the systematics effect

Num. of signal events in the true bin  $i$  according to the MC

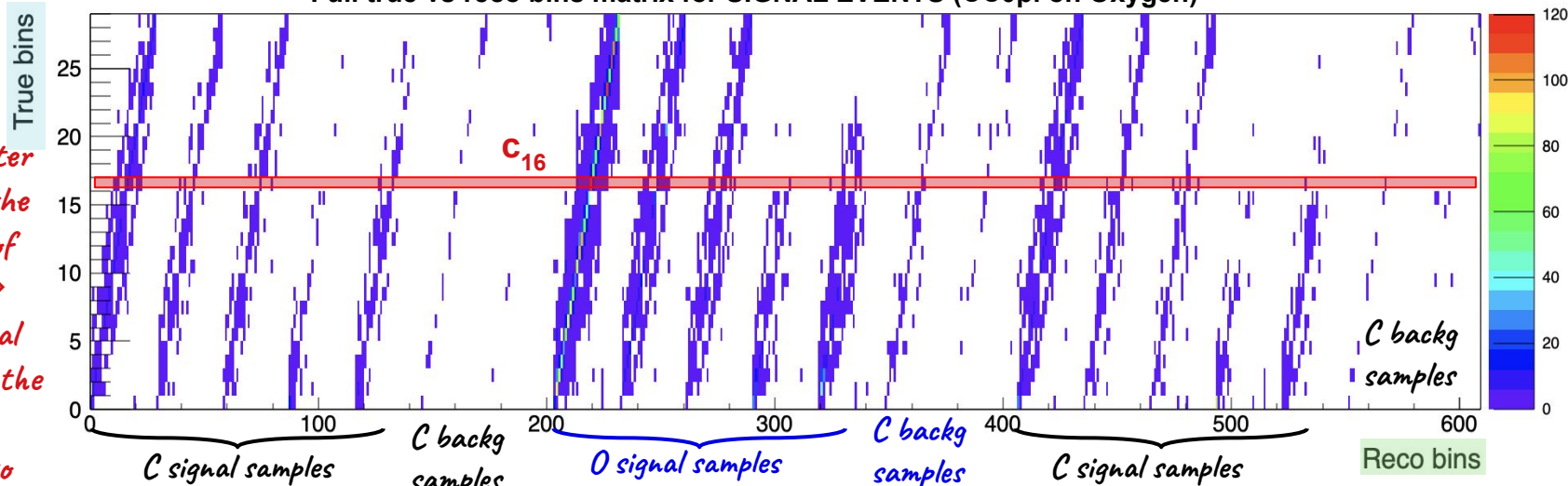
Num. of background events in the true bin  $i$  according to the MC

Smearing matrix to move from the truth to the reco bins

# Zoom on the template parameters

from O and C CC0pi analysis

Full true vs reco bins matrix for SIGNAL EVENTS (CC0pi on Oxygen)



Moving parameter  $c_{16} \Leftrightarrow$  moving the signal content of truth bin 16  $\Leftrightarrow$  moving the signal content of ALL the reco bins corresponding to true bin 16  $\Leftrightarrow$  agreement with data is checked in the reco space

$$N_j^{\text{reco}} = \sum_i^{\text{true bins}} \left[ \underbrace{c_i w_i^{\text{signal}}}_{\text{Data/MC correction, aka template parameters}} N_i^{\text{signal}} + \underbrace{w_i^{\text{bkg}}}_{\text{Reweight due to the systematics effect}} N_i^{\text{bkg}} \right] \underbrace{U_{ij}^{-1}}_{\text{Smearing matrix to move from the truth to the reco bins}}$$

Num. of reco events in the reco bin  $j$  and sample  $s$

Reweight due to the systematics effect according to the MC

Num. of background events in the true bin  $i$  according to the MC

