

# Longitudinal non-uniformity



Denys Klekots

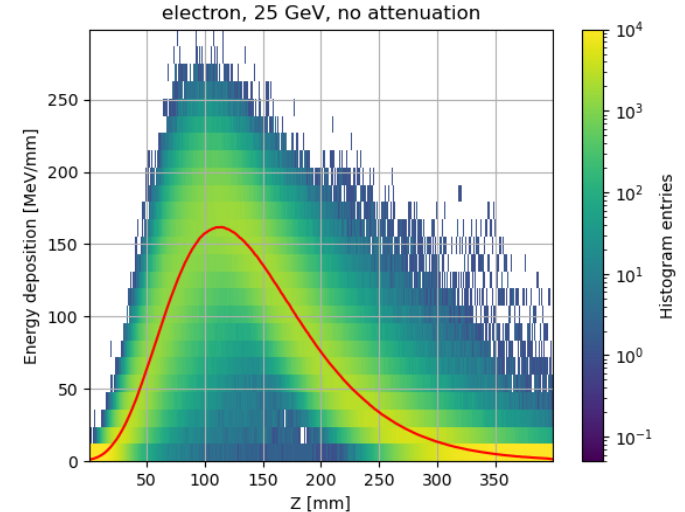
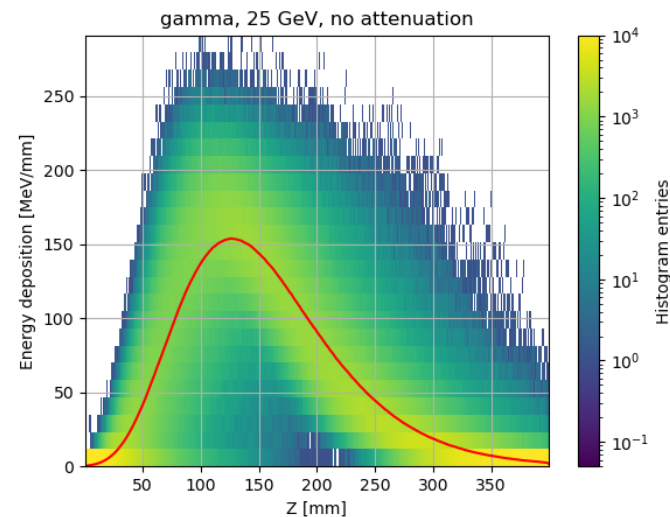
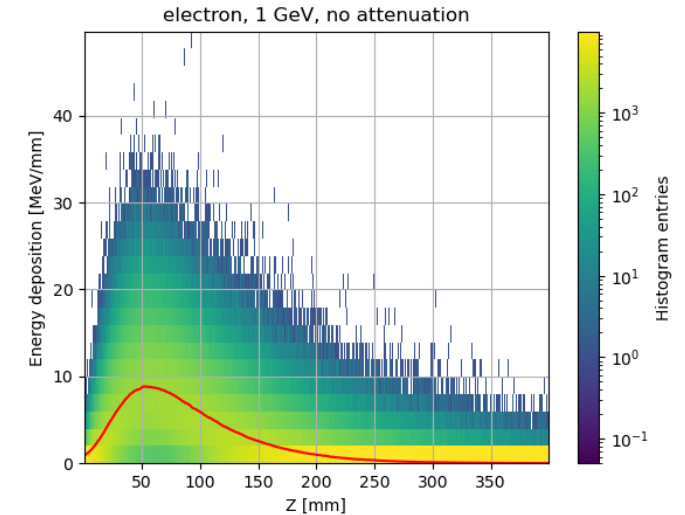
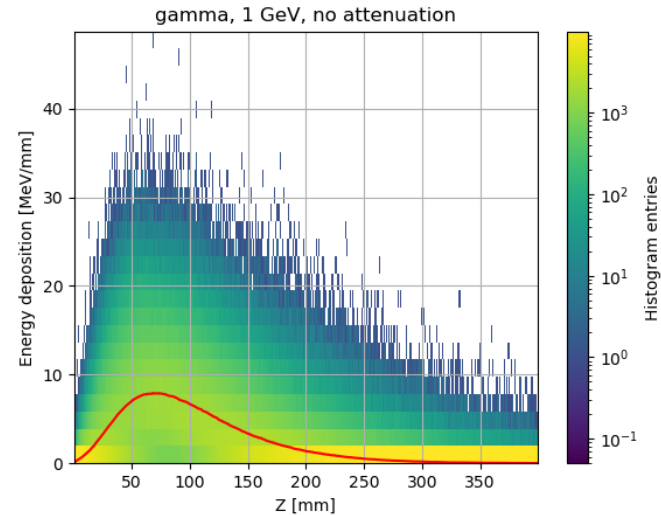
*(Taras Shevchenko National University of Kyiv)*

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[denys.klekots@gmail.com](mailto:denys.klekots@gmail.com)

# Shape of average shower energy deposition.

$$\bar{E}(z_i) = \frac{1}{10000} \sum_{k=1}^{10000} E_k(z_i)$$

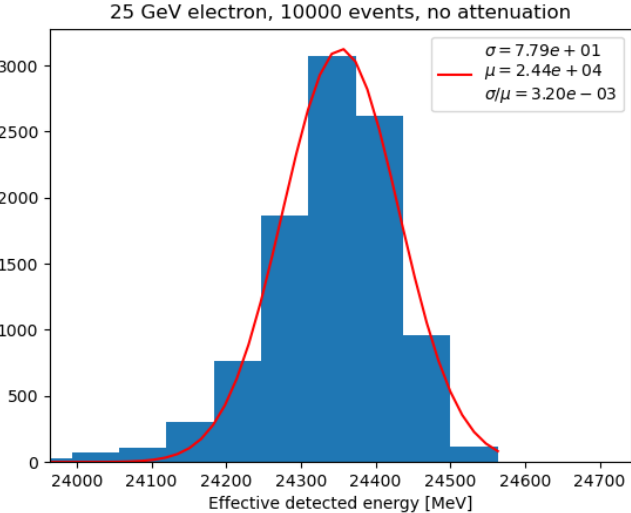
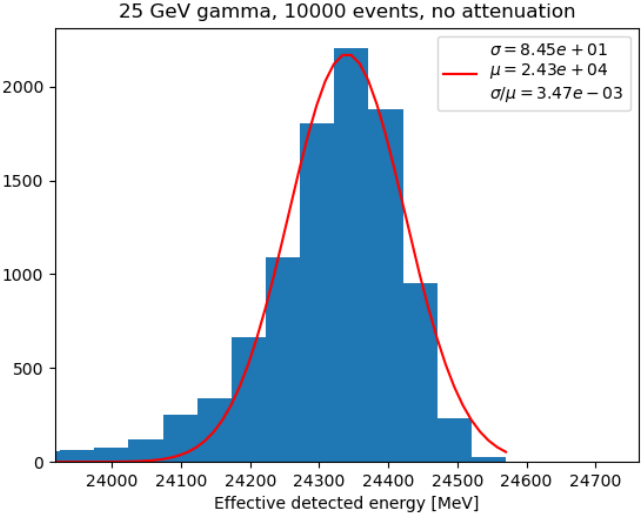
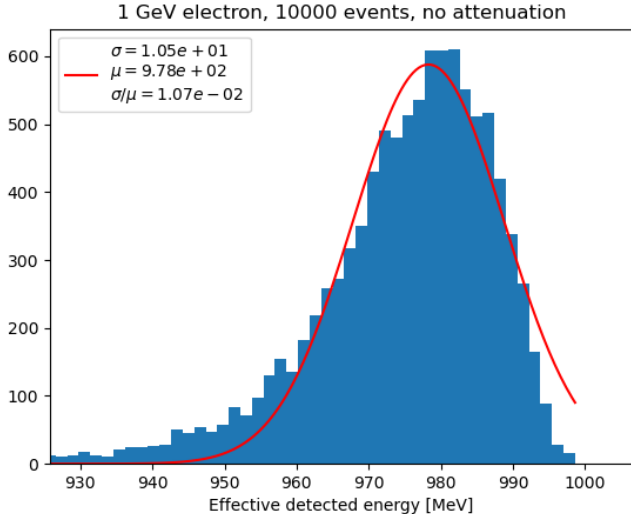
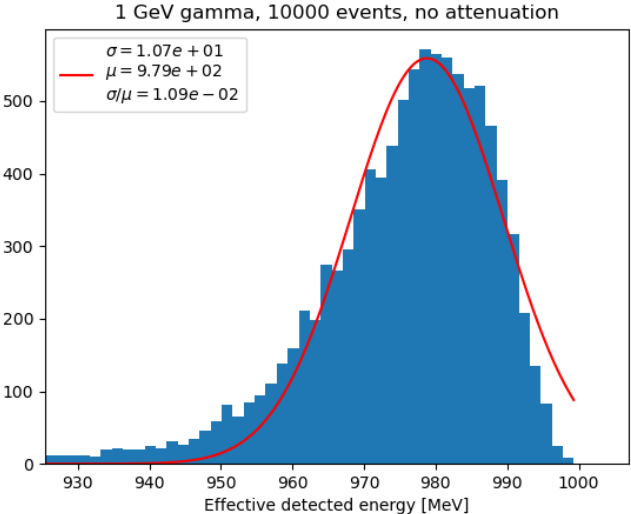
$E_k(z_i)$  - energy deposited in the  $i$ -th slice during  $k$ -th event.



# Event wise weighted deposited E. distribution .

$E_k = \sum_{i=1}^{400} E_k(z_i)$

$E_k(z_i)$  – energy deposited in the i–th slice during k–th event.

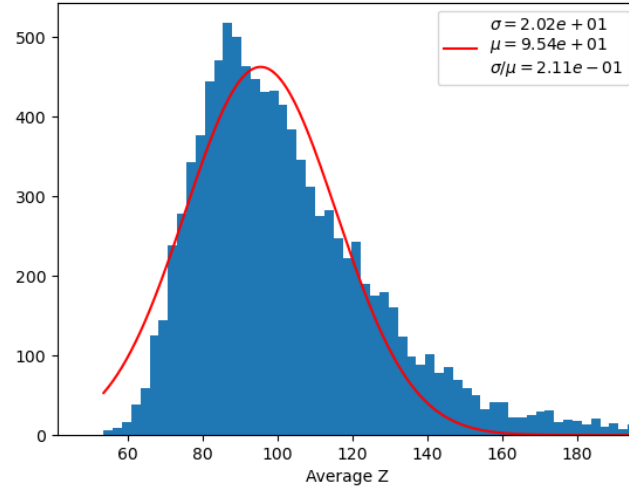


# Average Z coordinate of the shower

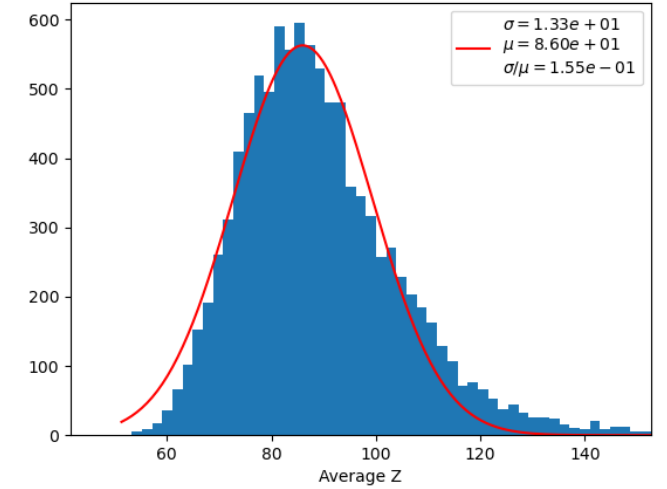
$$\overline{Z}_k = \frac{\sum_{i=1}^{400} z_i E_k(z_i)}{\sum_{i=1}^{400} E_k(z_i)}$$

$E_k(z_i)$  - energy deposited in the i-th slice during k-th event.

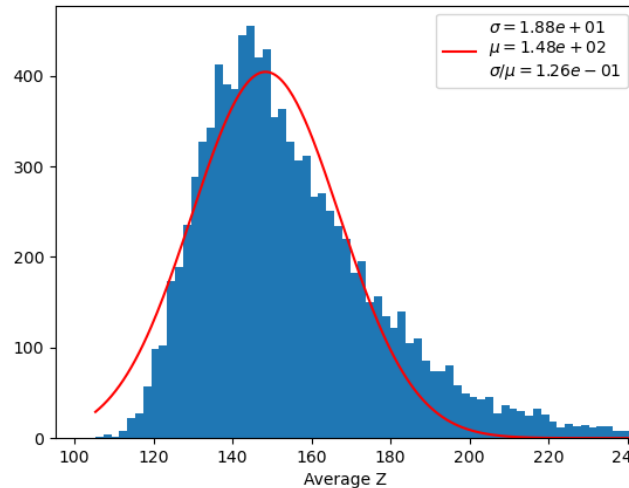
gamma, 1 GeV, event wise distribution of average Z, no attenuation



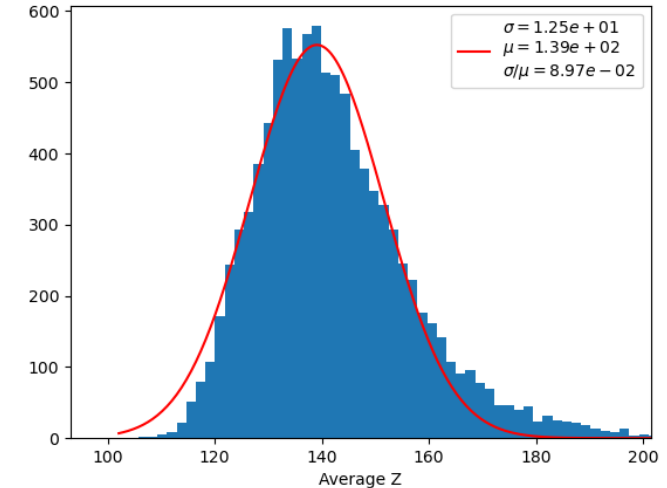
electron, 1 GeV, event wise distribution of average Z, no attenuation



gamma, 25 GeV, event wise distribution of average Z, no attenuation



electron, 25 GeV, event wise distribution of average Z, no attenuation

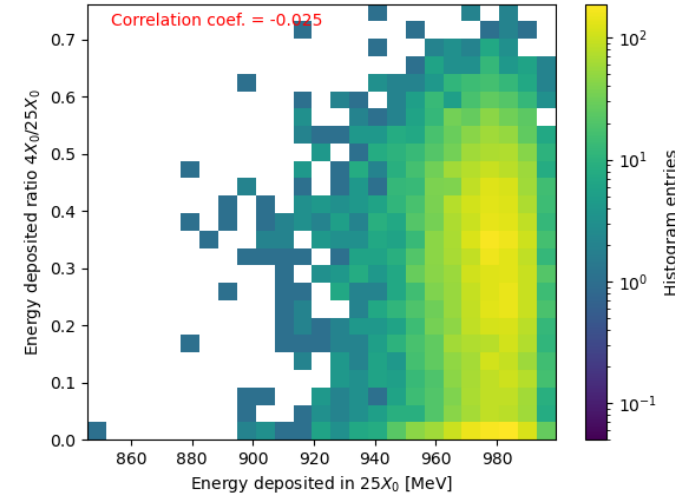


# 4X0/25X0 vs 25X0 correlations

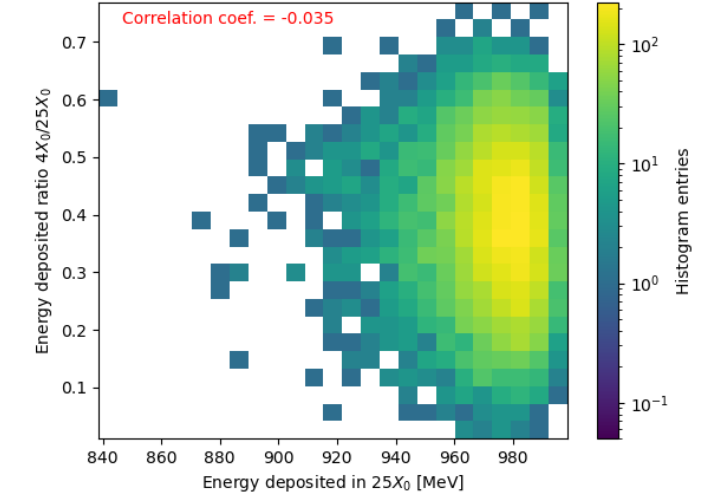
Correlation of two variables:

1. energy deposited in the entire detector
2. ratio of energy deposited in the first 64 mm (4X0) to energy deposited in the entire detector

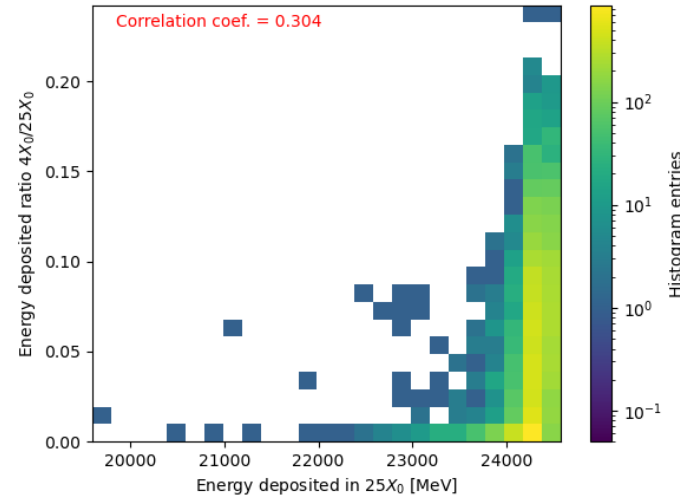
4X0/25X0 vs 25X0 correlations, gamma, 1 GeV, no attenuation



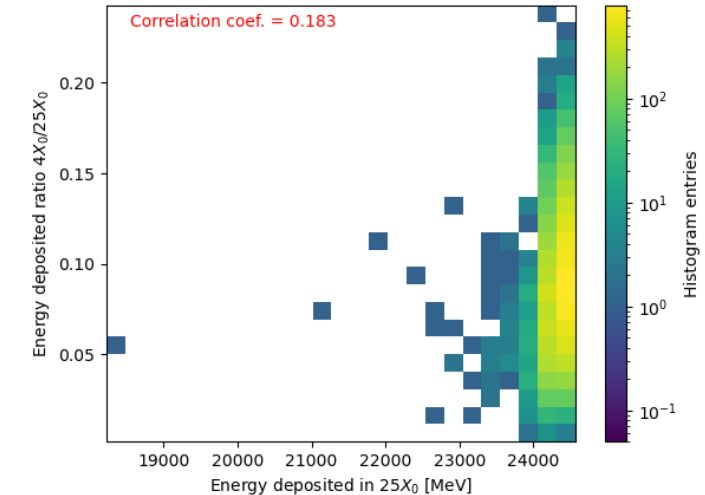
4X0/25X0 vs 25X0 correlations, electron, 1 GeV, no attenuation



4X0/25X0 vs 25X0 correlations, gamma, 25 GeV, no attenuation



4X0/25X0 vs 25X0 correlations, electron, 25 GeV, no attenuation



# Slice weight calculation

- No mirrors at the entry facet:

$$W(z_i) = A e^{-\frac{500[\text{mm}] - z_i[\text{mm}]}{L}}$$

- With mirrors at the entry facet:

$$W(z_i) = A \left( e^{-\frac{500[\text{mm}] - z_i[\text{mm}]}{L}} + 0,7 e^{-\frac{500[\text{mm}] + z_i[\text{mm}]}{L}} \right)$$

- Coefficient  $A$  ensures that  $\int W(z) dz = 1$

- $L = 667$  mm for O2 fibers

- $L = 1500$  mm for Y11 fibers

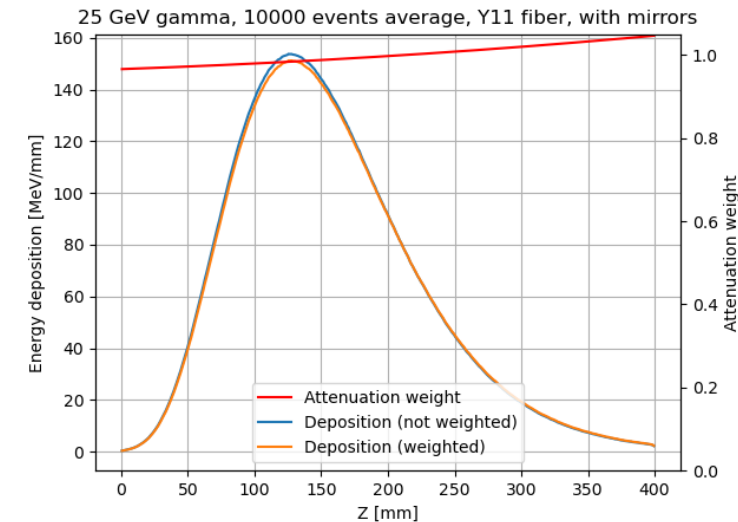
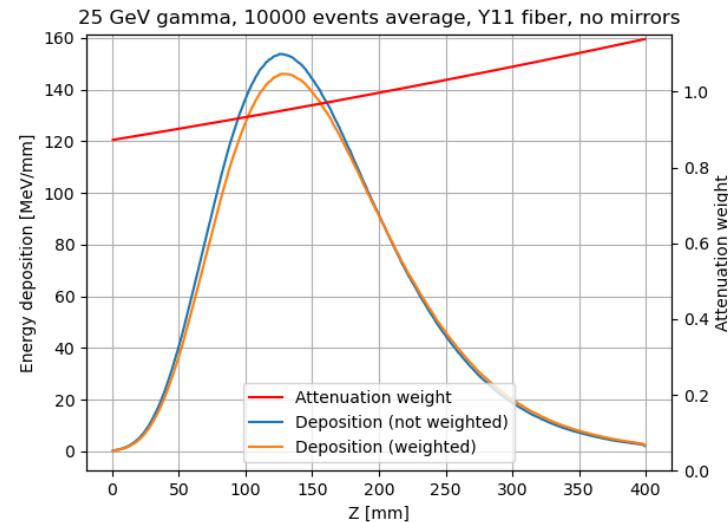
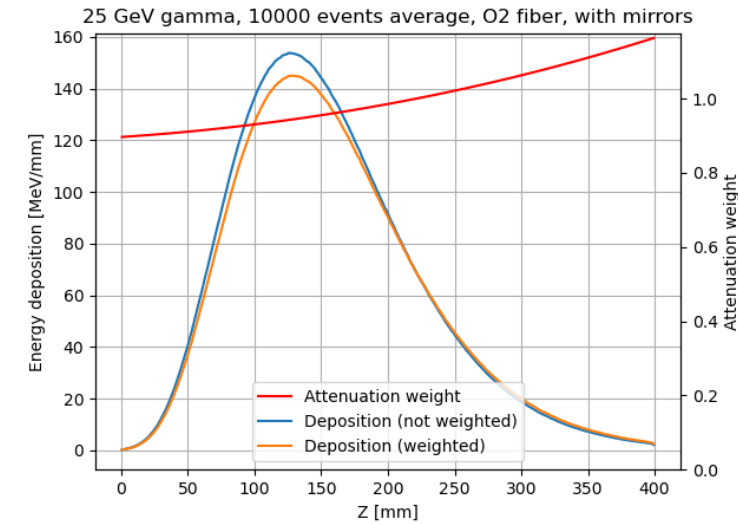
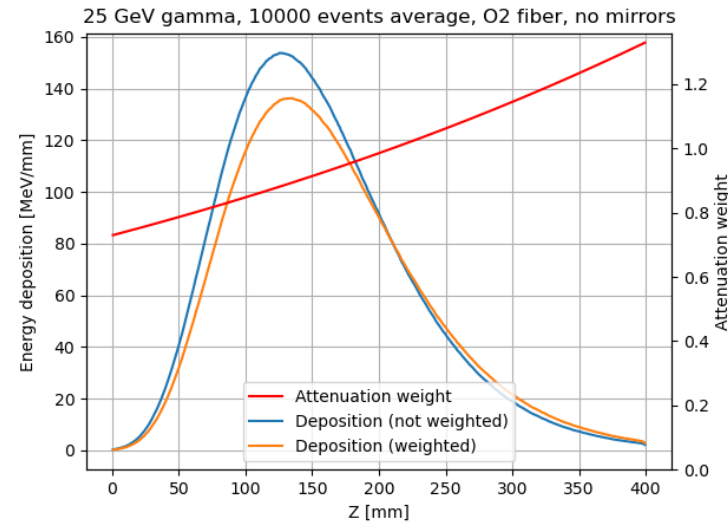
25 GeV Gamma

# Average weighted energy deposition shape. 25 GeV, $\gamma$

$$\square \bar{E}(z_i) = \frac{1}{10000} \sum_{k=1}^{10000} E_k(z_i) W(z_i)$$

$\square E_k(z_i)$  - energy deposited in the  $i$ -th slice during  $k$ -th event.

$\square W(z_i)$  - attenuation weight



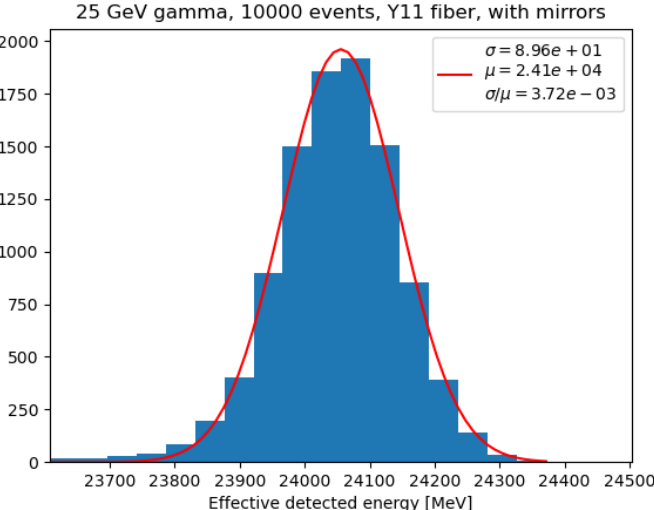
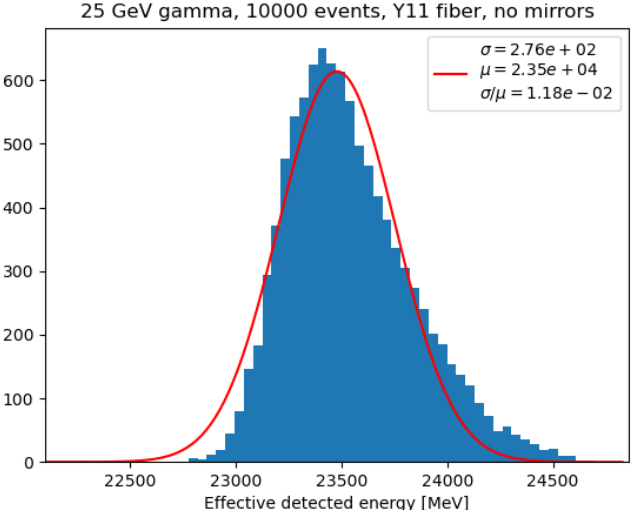
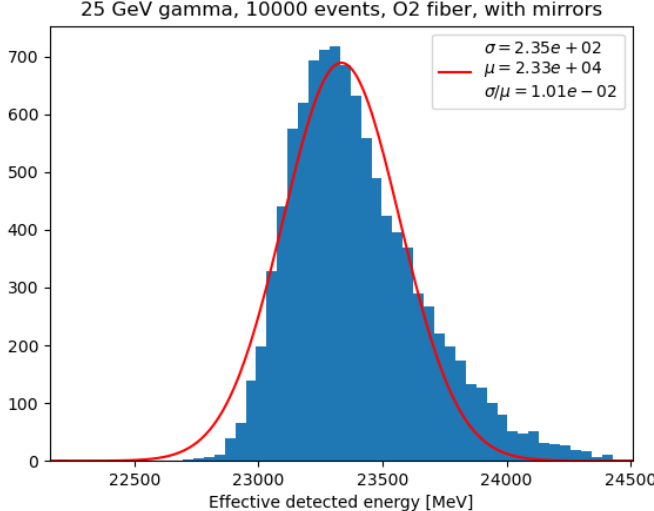
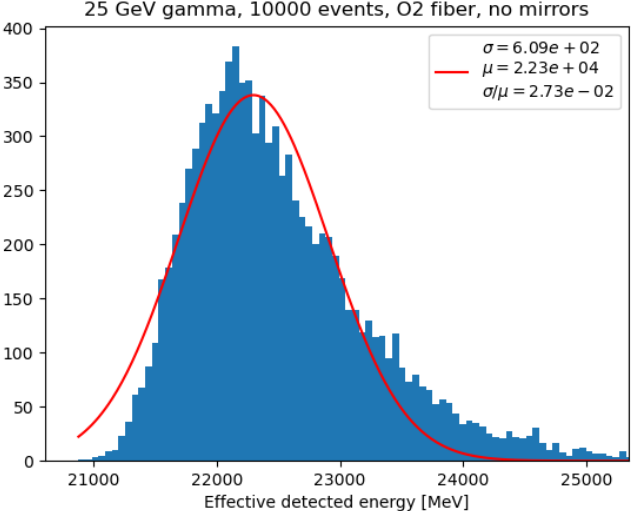


# Event wise weighted deposited E. distribution . 25 GeV, $\gamma$

$E_k = \sum_{i=1}^{400} E_k(z_i) W(z_i)$

$E_k(z_i)$  – energy deposited in the  $i$ -th slice during  $k$ -th

$W(z_i)$  - attenuation weight



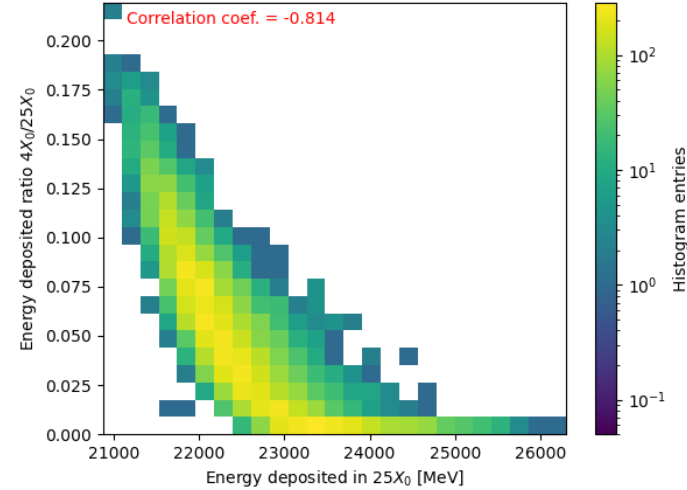
# 4X0/25X0 vs 25X0 weighted correlations. 25 GeV, $\gamma$

Correlation of two variables:

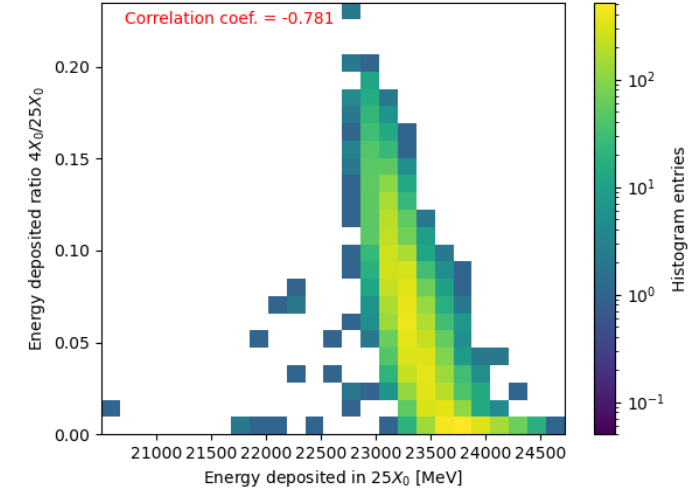
1. energy deposited in the entire detector
2. ratio of energy deposited in the first 64 mm (4X0) to energy deposited in the entire detector

Energy deposited for each corresponding slice was weighted

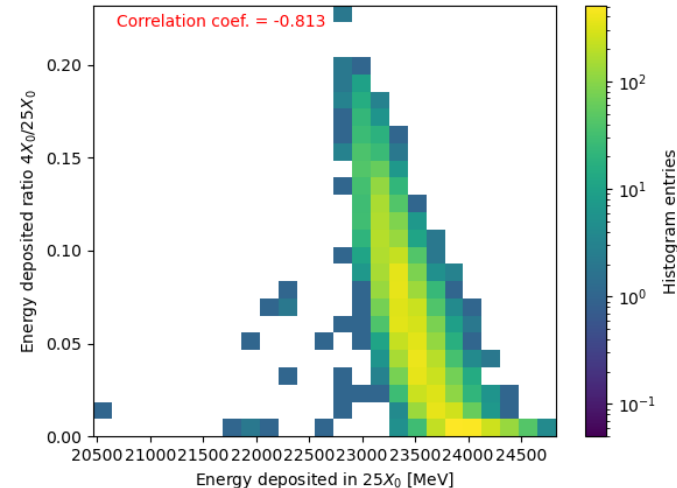
4X0/25X0 vs 25X0 correlations, gamma, 25 GeV, O2 fiber, no mirrors



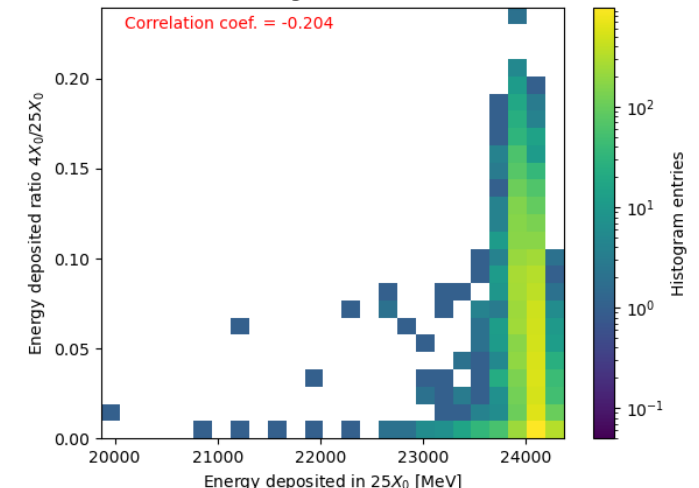
X0/25X0 vs 25X0 correlations, gamma, 25 GeV, O2 fiber, with mirrors



X0/25X0 vs 25X0 correlations, gamma, 25 GeV, Y11 fiber, no mirrors



X0/25X0 vs 25X0 correlations, gamma, 25 GeV, Y11 fiber, with mirrors



# Aggregated numbers

Variable	Fiber type	Mirror	25 GeV gamma	25 GeV electron	1 GeV gamma	1 GeV electron
Energy resolution $\sigma/\mu$	no attenuation		3,47E-03	3,20E-03	1,09E-02	1,07E-02
	O2	no mirror	2,73E-02	1,85E-02	3,40E-02	2,47E-02
		with mirror	1,01E-02	7,07E-03	1,57E-02	1,32E-02
	Y11	no mirror	1,18E-02	8,13E-03	1,86E-02	1,49E-02
		with mirror	3,72E-03	3,38E-03	1,14E-02	1,09E-02
Correlations 4X0/totval vs total	no attenuation		0,304	0,183	-0,025	-0,035
	O2	no mirror	-0,814	-0,781	-0,814	-0,756
		with mirror	-0,781	-0,698	-0,604	-0,445
	Y11	no mirror	-0,813	-0,742	-0,695	-0,548
		with mirror	-0,204	-0,227	-0,281	-0,190

# Conclusions

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- ❑ The system with O2 optical fiber gives energy resolution worse than 2%.
- ❑ The energy resolution for gammas is slightly worse than for electrons.
- ❑ The energy deposited in the first 4X0 (64 mm) is correlated with totally deposited energy. Interesting: the worse the resolution is the better the correlation.
- ❑ The characteristics of the system with Y11 fibers are close to the system without attenuation at all.

Thank you for your  
attention

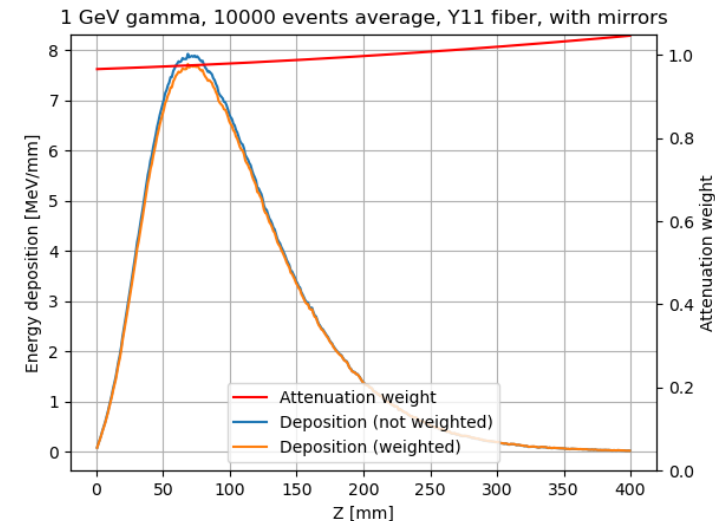
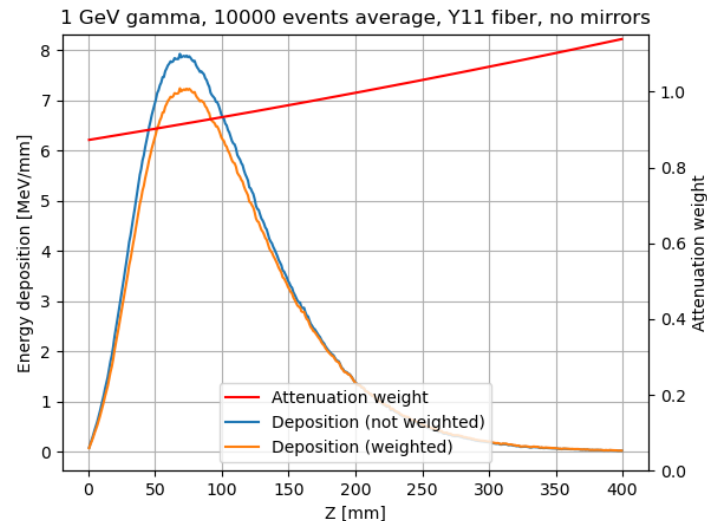
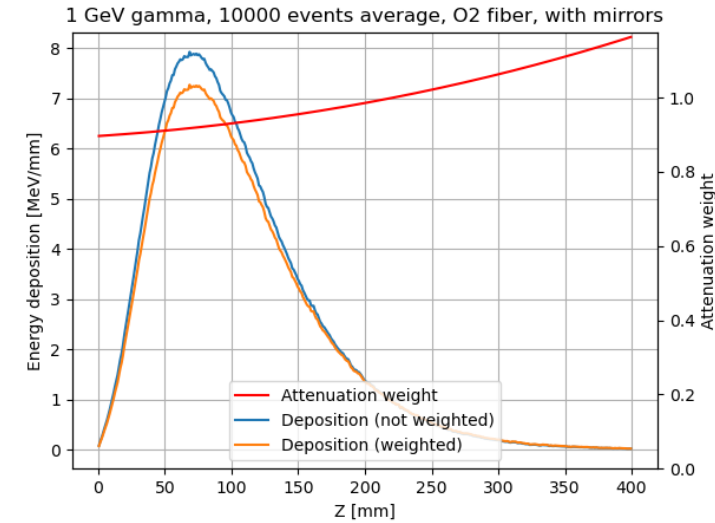
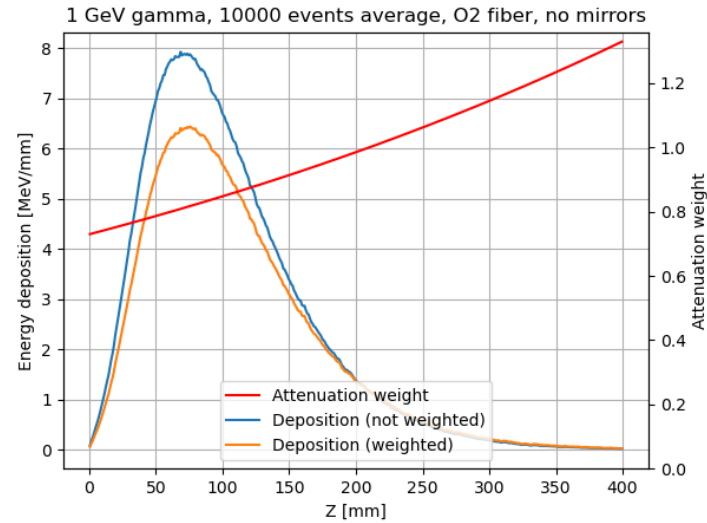
# 1 GeV Gamma

# Average weighted energy deposition shape. 1 GeV, $\gamma$

$$\square \bar{E}(z_i) = \frac{1}{10000} \sum_{k=1}^{10000} E_k(z_i) W(z_i)$$

$\square E_k(z_i)$  - energy deposited in the i-th slice during k-th event.

$\square W(z_i)$  - attenuation weight

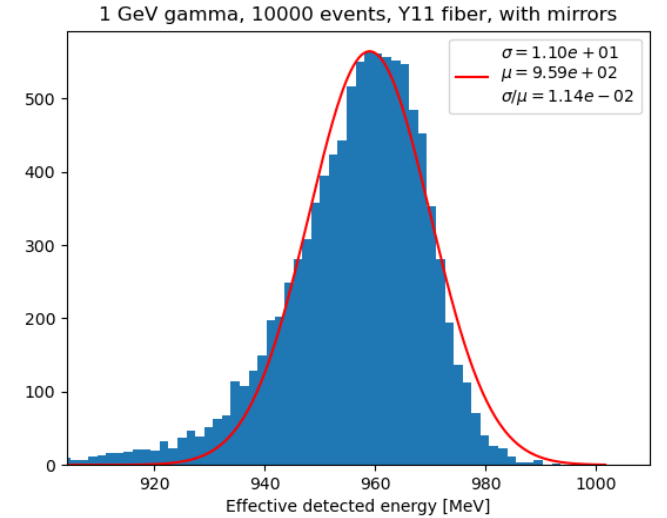
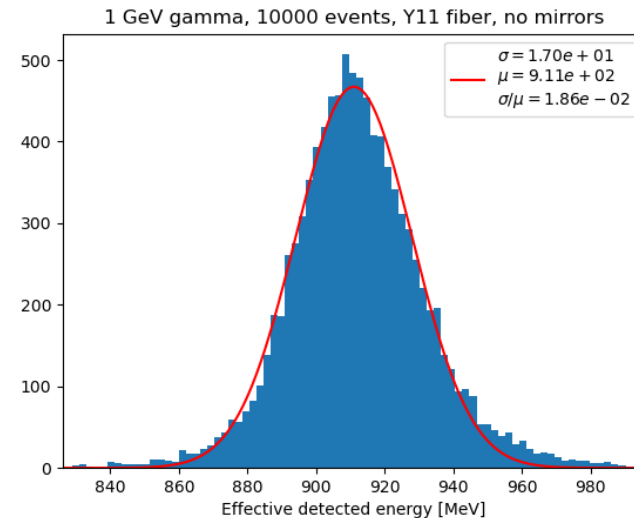
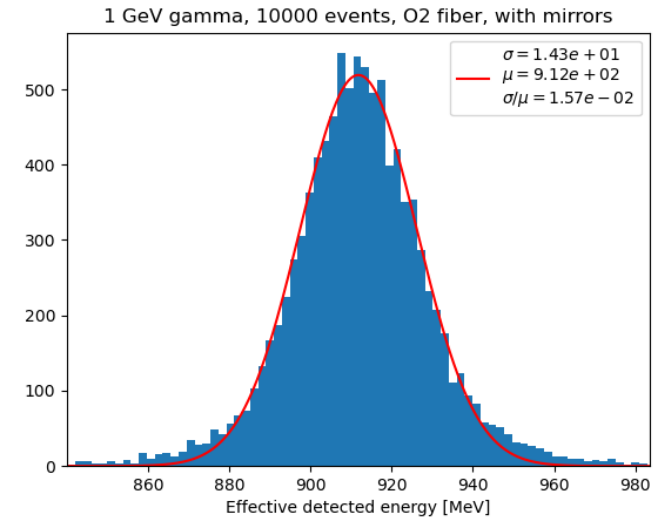
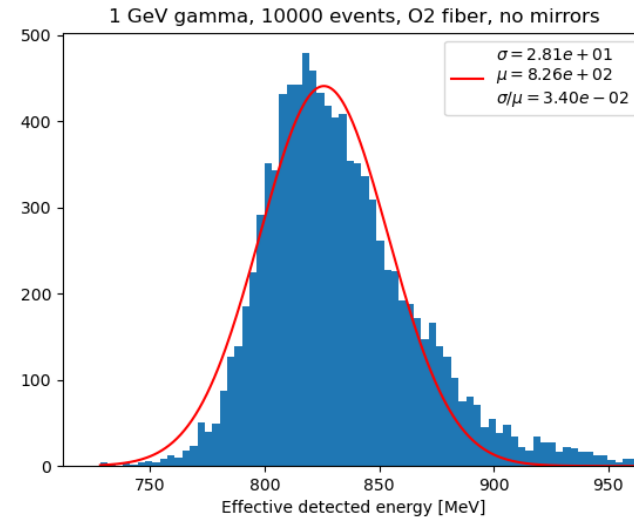


# Event wise weighted deposited E. distribution . 1 GeV, $\gamma$

$$\square E_k = \sum_{i=1}^{400} E_k(z_i) W(z_i)$$

$\square E_k(z_i)$  – energy deposited in the  $i$ -th slice during  $k$ -th

$\square W(z_i)$  - attenuation weight





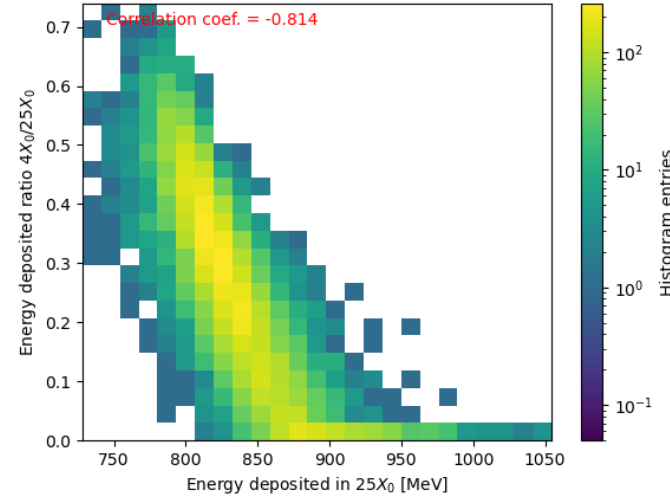
# 4X0/25X0 vs 25X0 weighted correlations. 1 GeV, $\gamma$

Correlation of two variables:

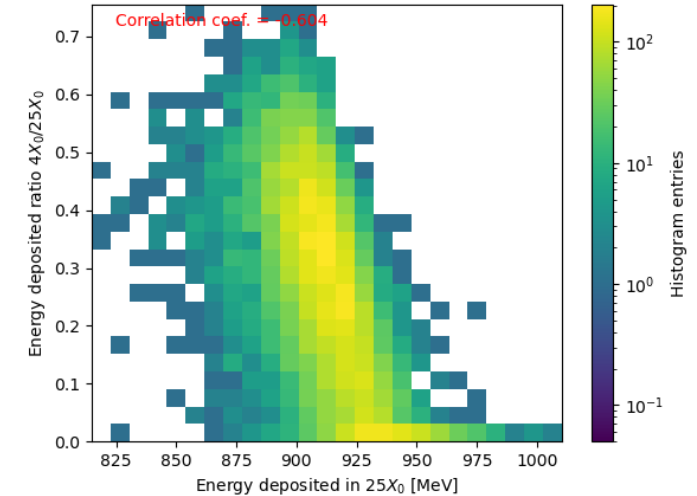
1. energy deposited in the entire detector
2. ratio of energy deposited in the first 64 mm (4X0) to energy deposited in the entire detector

Energy deposited for each corresponding slice was weighted

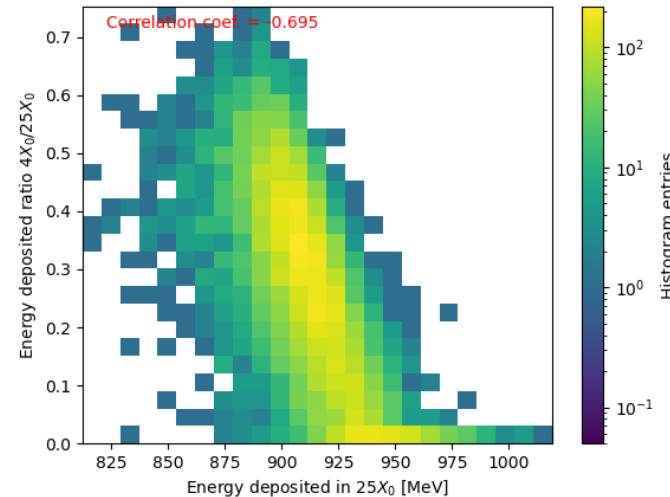
4X0/25X0 vs 25X0 correlations, gamma, 1 GeV, O2 fiber, no mirrors



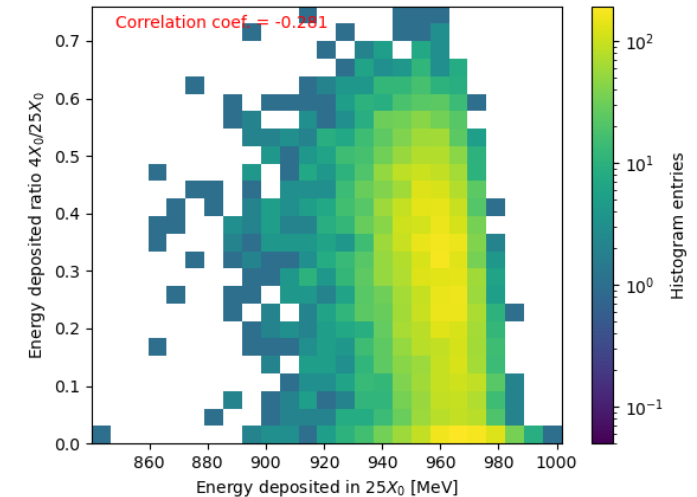
X0/25X0 vs 25X0 correlations, gamma, 1 GeV, O2 fiber, with mirrors



4X0/25X0 vs 25X0 correlations, gamma, 1 GeV, Y11 fiber, no mirrors



X0/25X0 vs 25X0 correlations, gamma, 1 GeV, Y11 fiber, with mirrors



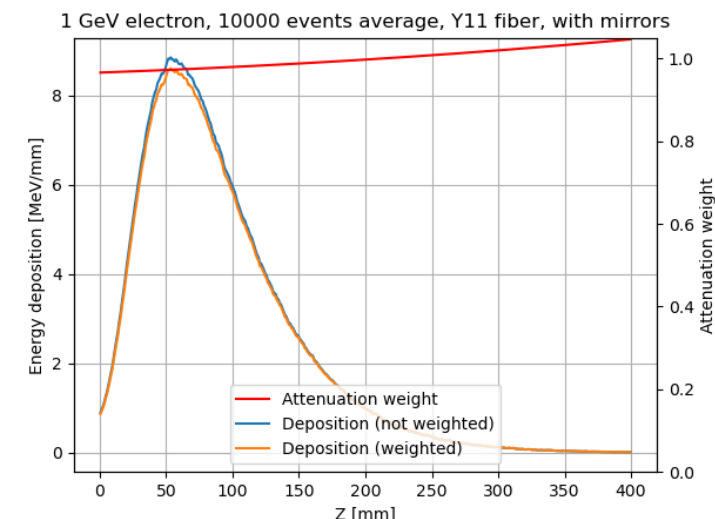
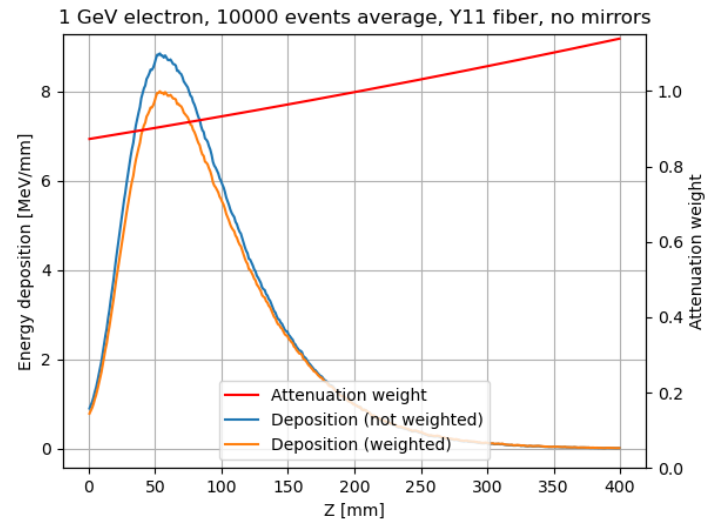
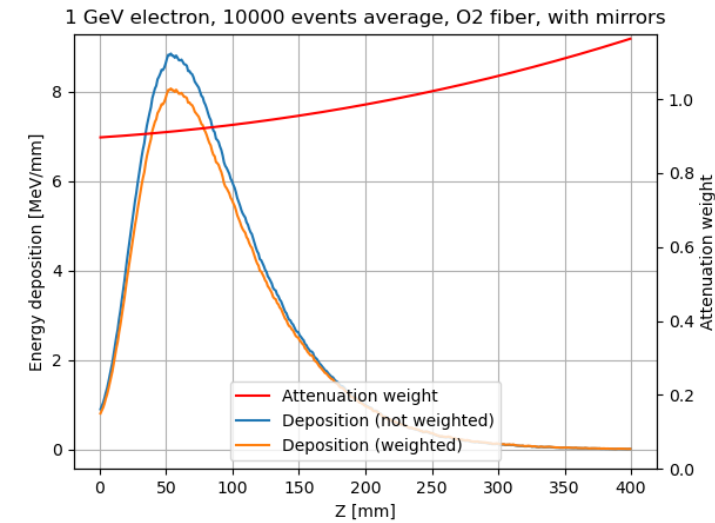
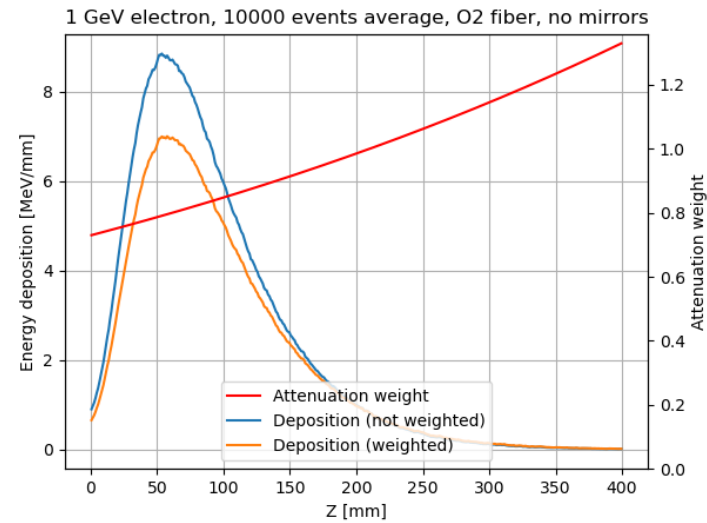
# 1 GeV Electrons

# Average weighted energy deposition shape. 1 GeV, e-

$$\bar{E}(z_i) = \frac{1}{10000} \sum_{k=1}^{10000} E_k(z_i) W(z_i)$$

$E_k(z_i)$  - energy deposited in the i-th slice during k-th event.

$W(z_i)$  - attenuation weight

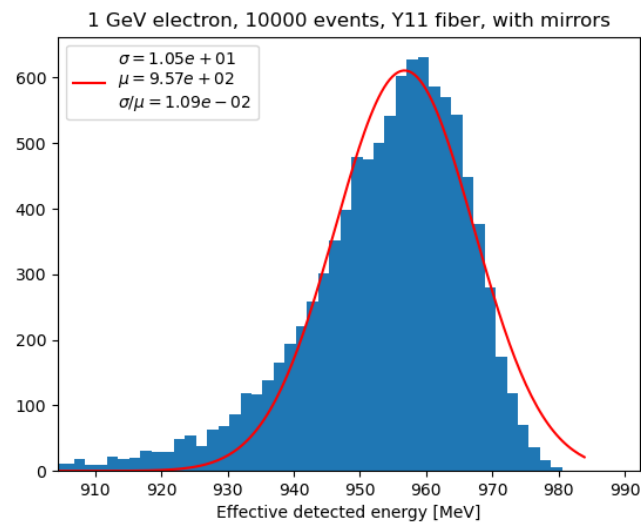
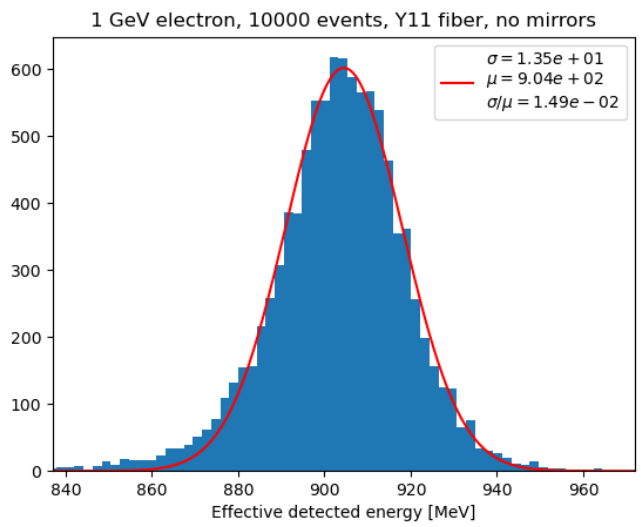
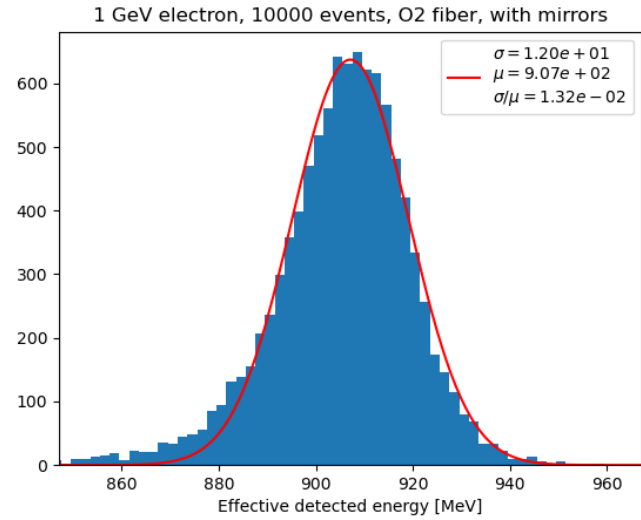
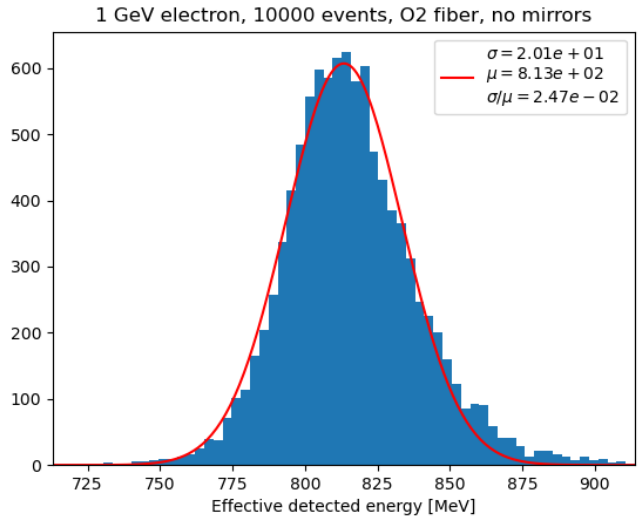


# Event wise weighted deposited E. distribution . 1 GeV, e-

□  $E_k = \sum_{i=1}^{400} E_k(z_i) W(z_i)$

□  $E_k(z_i)$  – energy deposited in the i–th slice during k–th

□  $W(z_i)$  - attenuation weight



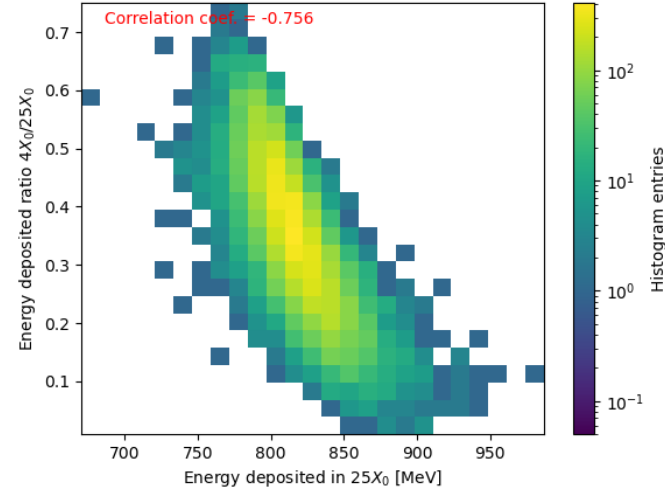
# 4X0/25X0 vs 25X0 weighted correlations. 1 GeV, e-

Correlation of two variables:

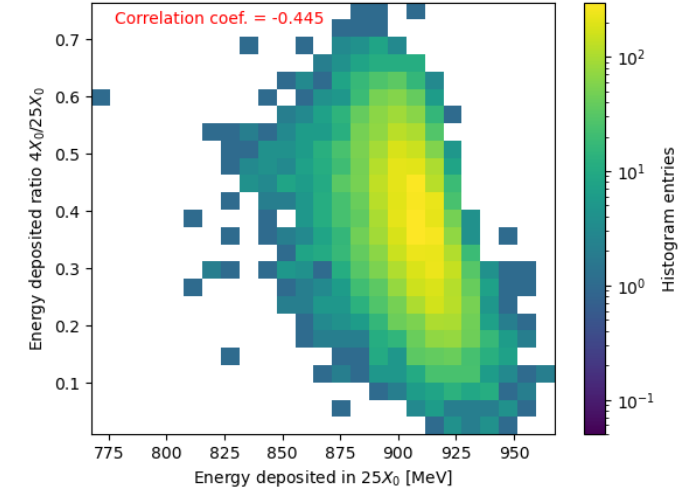
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- ratio of energy deposited in the first 64 mm (4X0) to energy deposited in the entire detector

Energy deposited for each corresponding slice was weighted

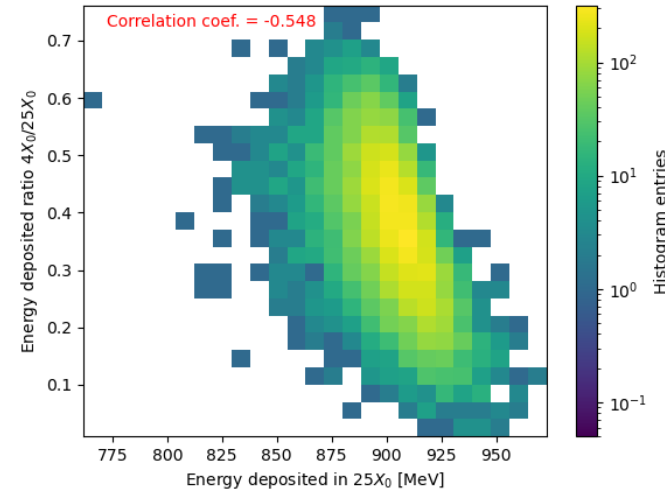
4X0/25X0 vs 25X0 correlations, electron, 1 GeV, O2 fiber, no mirrors



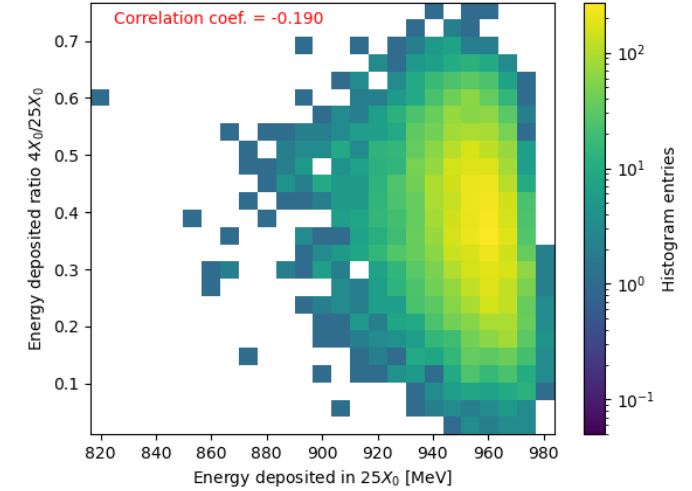
X0/25X0 vs 25X0 correlations, electron, 1 GeV, O2 fiber, with mirrors



X0/25X0 vs 25X0 correlations, electron, 1 GeV, Y11 fiber, no mirrors



X0/25X0 vs 25X0 correlations, electron, 1 GeV, Y11 fiber, with mirrors



# 25 GeV Electrons

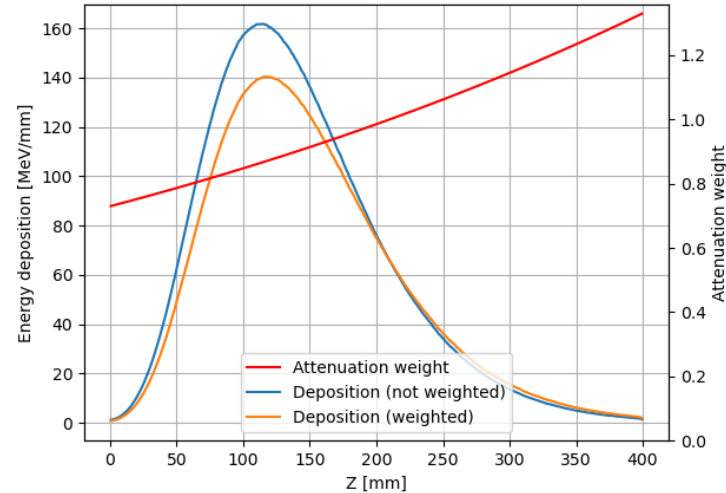
# Average weighted energy deposition shape. 25 GeV, e-

$$\square \bar{E}(z_i) = \frac{1}{10000} \sum_{k=1}^{10000} E_k(z_i) W(z_i)$$

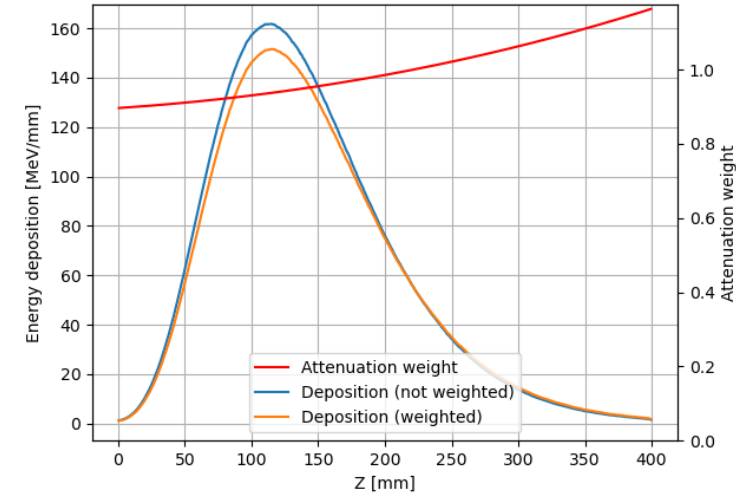
$\square E_k(z_i)$  - energy deposited in the i-th slice during k-th event.

$\square W(z_i)$  - attenuation weight

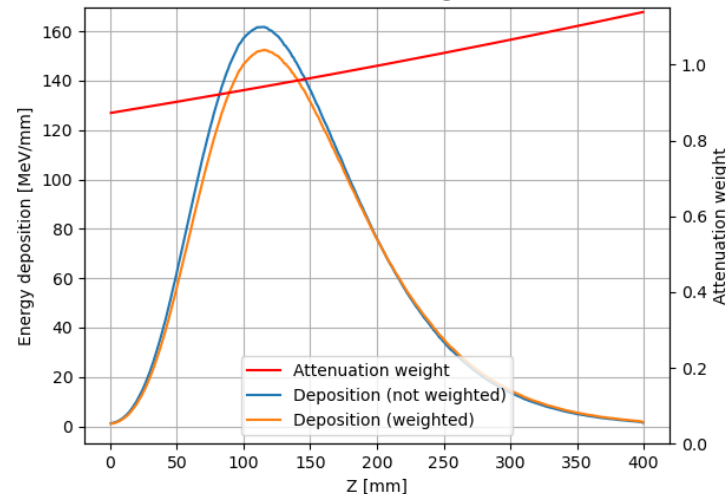
25 GeV electron, 10000 events average, O2 fiber, no mirrors



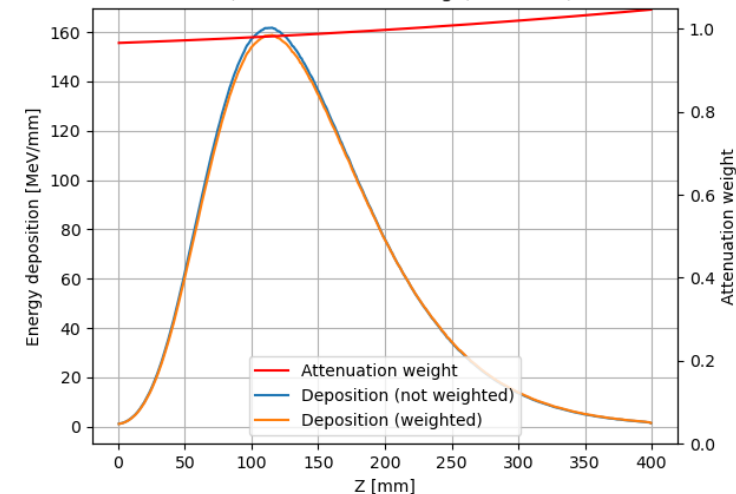
25 GeV electron, 10000 events average, O2 fiber, with mirrors



25 GeV electron, 10000 events average, Y11 fiber, no mirrors



25 GeV electron, 10000 events average, Y11 fiber, with mirrors

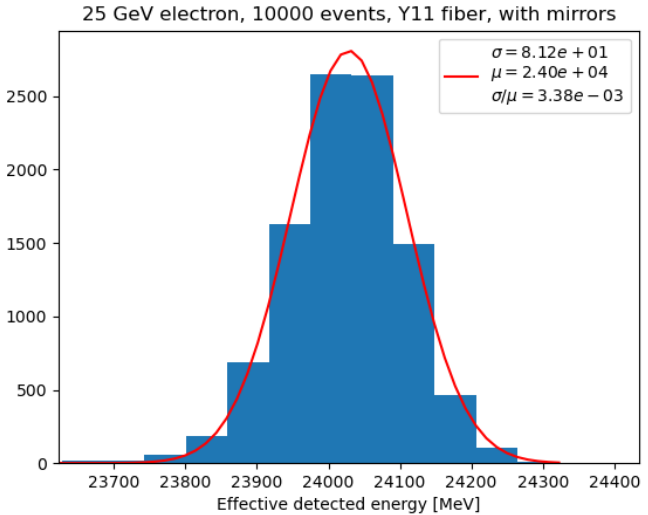
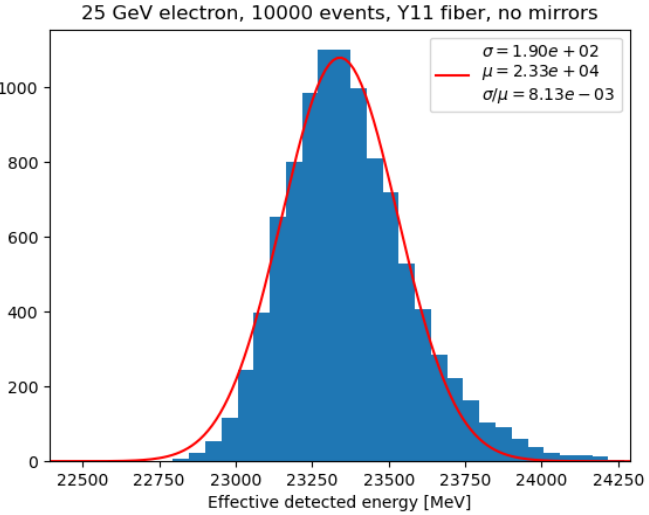
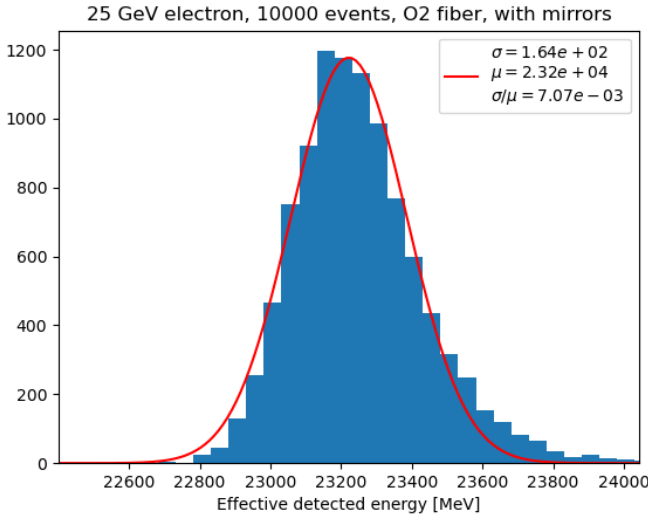
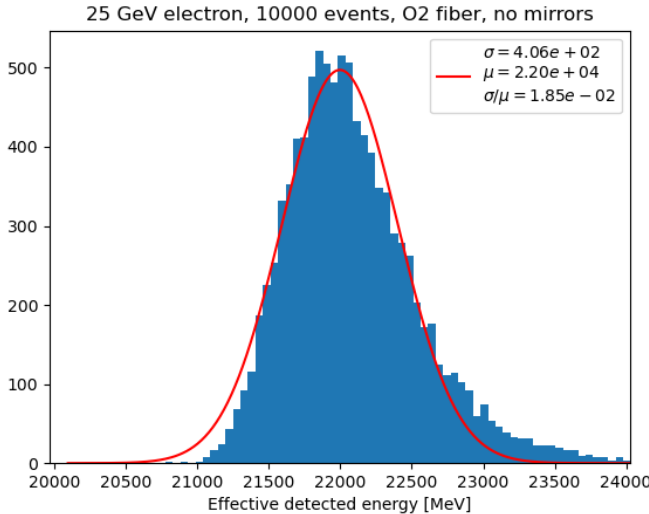


# Event wise weighted deposited E. distribution . 25 GeV, e-

$E_k = \sum_{i=1}^{400} E_k(z_i) W(z_i)$

$E_k(z_i)$  – energy deposited in the i–th slice during k–th

$W(z_i)$  - attenuation weight





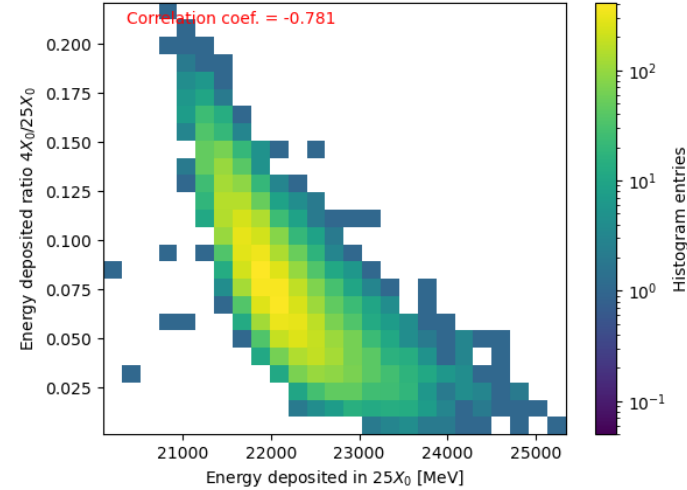
# 4X0/25X0 vs 25X0 weighted correlations. 25 GeV, e-

Correlation of two variables:

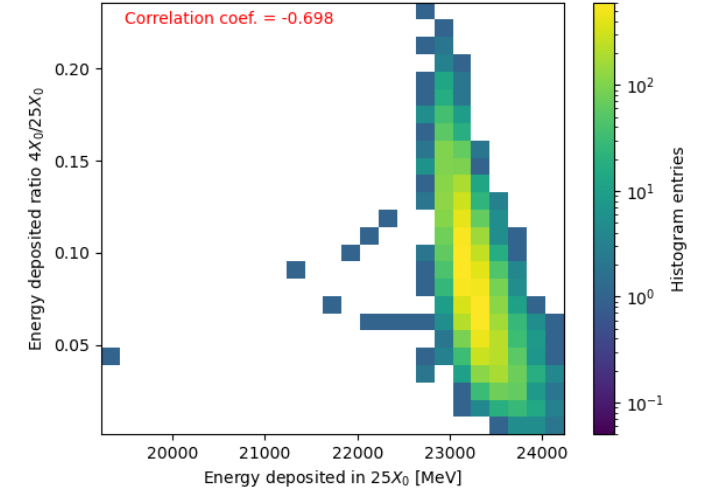
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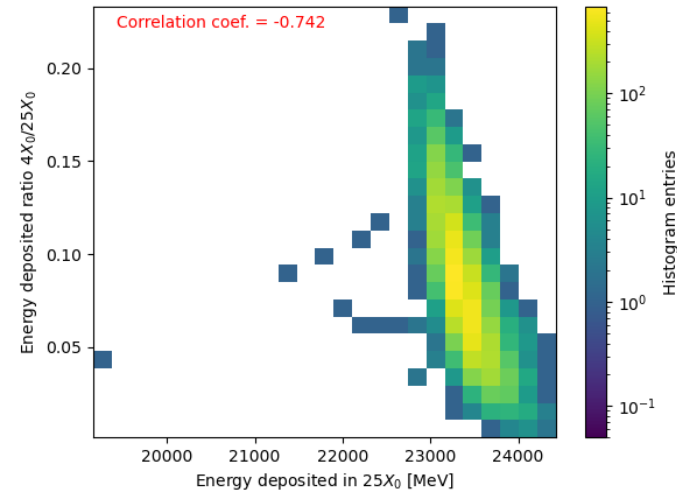
$X_0/25X_0$  vs  $25X_0$  correlations, electron, 25 GeV, O2 fiber, no mirrors



$\bar{X}_0/25X_0$  vs  $25X_0$  correlations, electron, 25 GeV, O2 fiber, with mirrors



$X_0/25X_0$  vs  $25X_0$  correlations, electron, 25 GeV, Y11 fiber, no mirrors



$\bar{X}_0/25X_0$  vs  $25X_0$  correlations, electron, 25 GeV, Y11 fiber, with mirrors

