# Theory status and experimental opportunities of modern $V_{ud}$ determinations



#### Introduction

Theory progress in the last 5 years

Charge radii for CKM unitarity

Experimental opportunities

ASGARD

Summary & Outlook

Three out of four fundamental forces (no gravity):

Standard Model



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18 free parameters



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Great (annoyingly so), consistent with constraints at  $\sim 10^{0-2}~\text{TeV}$ 



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Open questions: dark matter, gravity, neutrino masses, ...



#### Introduction: Weak interaction & CKM matrix

Cabibbo-Kobayashi-Maskawa matrix relates weak and mass eigenstates

$$\left(\begin{array}{c} d\\s\\b\end{array}\right)_{w} = \left(\begin{array}{ccc} V_{ud} & V_{us} & V_{ub}\\V_{cd} & V_{cs} & V_{cb}\\V_{td} & V_{ts} & V_{tb}\end{array}\right) \left(\begin{array}{c} d\\s\\b\end{array}\right)_{m}$$

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(nuclear) eta decay, meson decay ( $\pi$ , K),  $|V_{ub}|^2 \sim 10^{-5}$ 

Violations are sensitive to TeV scale new physics!

#### CKM unitarity: Current status

Signs of non-unitarity at few  $\sigma$  level...

Disagreement between K/2 and K/3  $|V_{us}|$  'Cabibbo angle anomaly'



SM has V-A structure, but more generally

$$\begin{split} \mathcal{L}_{\text{eff}} &= -\frac{G_{\text{F}}\,\tilde{V}_{ud}}{\sqrt{2}} \bigg\{ \bar{e}\gamma_{\mu}\nu_{L}\cdot\bar{u}\gamma^{\mu}[c_{V}-(c_{A}-2\epsilon_{R})\gamma^{5}]d + \epsilon_{\text{S}}\,\bar{e}\nu_{L}\cdot\bar{u}d \\ &-\epsilon_{P}\,\bar{e}\nu_{L}\cdot\bar{u}\gamma^{5}d + \epsilon_{\text{T}}\,\bar{e}\sigma_{\mu\nu}\nu_{L}\cdot\bar{u}\sigma^{\mu\nu}(1-\gamma^{5})d \bigg\} + \text{h.c.}, \end{split}$$

at the quark level

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at the quark level

All  $\epsilon_i$  are proportional to  $(M_W/\Lambda_{BSM})^2$ , change kinematics  $\epsilon_i \lesssim 10^{-4} \rightarrow \Lambda_{BSM} \gtrsim 15$  TeV assuming natural couplings

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Things you need to know

- $G_F$  ( $\mu$  lifetime)
- Radiative corrections
- Hadronic theory
- For each  $\beta$  transition:  $t_{1/2}, Q_{\beta}, BR, (GT/F \text{ mixing})$

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Master formula

$$ft(1+\delta_R')(1+\Delta_R^V)(1+\delta_{NS}-\delta_C) = \frac{K}{G_F^2 V_{ud}^2 M_{\text{tree}}^2}$$

# CKM unitarity: $V_{ud}$ precision

Nuclear sandbox  $\rightarrow$  make hadronic theory easy

- Pion
- Neutron

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$$\pi^+ 
ightarrow \pi^0 e^+ 
u_e$$
 very hard (BR  $\sim 10^{-8}$ )

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Status of  $0^+ \rightarrow 0^+$  ISOL community triumph for 50+ years!

LH, ARNPS 74 (2024) 497

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Separate into tree level & loop level

- $\delta_C$ : Isospin symmetry breaking of  $M_F$
- *f*: phase space factor
- $\delta'_R$ : 'outer' radiative corrections
- $\Delta_R^V$ : single-nucleon 'inner' radiative corrections
- $\delta_{NS}$ : Changes in  $\Delta_R^V$  due to nuclear structure

All except for  $\Delta_R^V$  are **open questions** to this day!

Based on L.H. ARNPS 74 (2024) 497 and Gorchtein, Seng ARNPS 74 (2024) 23

# **Recent changes:** $\Delta_R^V$

Rescaling of coupling constant  $g_V^2 \rightarrow g_V^2 (1 + \Delta_R^V)$ 



Specifically, axial-vector contribution  $\rightarrow$  symmetries don't save you & QCD at intermediate effects

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+50 years of research to improve it

# $\Delta_R^V$ updates

After 2018 jump different calculations performed: convergence



Small differences remain, neutron experimental uncertainty too large to distinguish LH, ARNPS 74 (2024) 497

#### Current status on $\delta_{NS}$

 $V_{ud}$  currently limited by nuclear structure in radiative corrections



More sophisticated picture, first ab initio calculations emerging Gorchtein & Seng ARNPS 74 (2024) 1

#### Progress in nuclear ab initio theory

#### Field is charging full steam ahead on nuclear ab initio



H. Hergert, Frontiers in Physics (2020)

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Schematic description of  $\beta$  decay matrix element

$$M_{fi} \sim \int d^3 x \psi^*_{\nu} \psi^*_{e} \psi^*_{f} \mathcal{O}_{\beta} \psi_{i}$$

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$$F(Z, E_e) \sim |\psi_e(r=R)|^2$$

and weak charge radius

$$\rho_{wc}(r) \sim \psi_f^*(r) O_\beta(r) \psi_i(r)$$

where  $\rho_{wc}(r) = \rho_{ch}(r) + \delta \rho(r)$ , usually nuclear (shell) model

#### Weak charge from charge radii

Isospin symmetry:  $\rho_{wc}$  from 2 out 3 charge radii in T = 1 triplet

$$\rho_{wc}(r) = \rho_{ch,1}(r) + \frac{Z_{-1}}{2}[\rho_{ch,-1}(r) - \rho_{ch,1}(r)]$$



Seng, Gorchtein PRC 109 (2024) 045501

#### Nuclear charge radii: Current data set

#### Experimentalists: pay attention to last column (NA means go)!

A	$\langle r_{\rm ch,-1}^2 \rangle^{1/2}$ (fm) [Ref.]	$\langle r_{\rm ch,0}^2 \rangle^{1/2}$ (fm) [Ref.]	$\langle r_{ch,1}^2 \rangle^{1/2}$ (fm) [Ref.]	$\langle r_{\rm CW}^2 \rangle^{1/2}$ (fm)
10	<sup>10</sup> <sub>6</sub> C	${}_{5}^{10}B$ (ex)	<sup>10</sup> <sub>4</sub> Be: 2.3550(170) [59]	NA
14	<sup>14</sup> <sub>8</sub> O	$^{14}_{7}$ N (ex)	<sup>14</sup> <sub>6</sub> C: 2.5025(87) [59]	NA
18	<sup>18</sup> <sub>10</sub> Ne: 2.9714(76) [59]	${}^{18}_{9}{ m F}$ (ex)	<sup>18</sup> O: 2.7726(56) [59]	3.661(72)
22	<sup>22</sup> / <sub>12</sub> Mg: 3.0691(89) [61]	$^{22}_{11}$ Na (ex)	$^{22}_{10}$ Ne: 2.9525(40) [59]	3.596(99)
26	<sup>26</sup> <sub>14</sub> Si	$^{26m}_{13}$ Al: 3.130(15) [65]	$^{26}_{12}$ Mg: 3.0337(18) [59]	4.11(15)
30	<sup>30</sup> <sub>16</sub> S	$^{30}_{15}P(ex)$	<sup>30</sup> <sub>14</sub> Si: 3.1336(40) [59]	NA
34	<sup>34</sup> <sub>18</sub> Ar: 3.3654(40) [59]	<sup>34</sup> <sub>17</sub> Cl	$^{34}_{16}$ S: 3.2847(21) [59]	3.954(68)
38	<sup>38</sup> <sub>20</sub> Ca: 3.467(1) [62]	<sup>38m</sup> <sub>19</sub> K: 3.437(4) [63]	<sup>38</sup> <sub>18</sub> Ar: 3.4028(19) [59]	3.999(35)
42	<sup>42</sup> <sub>22</sub> Ti	<sup>42</sup> <sub>21</sub> Sc: 3.5702(238) [59]	$^{42}_{20}$ Ca: 3.5081(21) [59]	4.64(39)
46	<sup>46</sup> <sub>24</sub> Cr	46 23 V	<sup>46</sup> <sub>22</sub> Ti: 3.6070(22) [59]	NA
50	<sup>50</sup> <sub>26</sub> Fe	<sup>50</sup> <sub>25</sub> Mn: 3.7120(196) [59]	$^{50}_{24}$ Cr: 3.6588(65) [59]	4.82(39)
54	<sup>54</sup> <sub>28</sub> Ni: 3.738(4) [64]	<sup>54</sup> <sub>27</sub> Co	<sup>54</sup> <sub>26</sub> Fe: 3.6933(19) [59]	4.28(11)
62	<sup>62</sup> <sub>32</sub> Ge	<sup>62</sup> <sub>31</sub> Ga	$^{62}_{30}$ Zn: 3.9031(69) [61]	NA
66	66 34 Se	66 33As	66 32 Ge	NA
70	<sup>70</sup> <sub>36</sub> Kr	<sup>70</sup> <sub>35</sub> Br	<sup>70</sup> <sub>34</sub> Se	NA
74	<sup>74</sup> <sub>38</sub> Sr	<sup>74</sup> <sub>37</sub> Rb: 4.1935(172) [61]	<sup>74</sup> <sub>36</sub> Kr: 4.1870(41) [59]	4.42(62)

Table 1 Determinations of  $\langle r_{CW}^2 \rangle$  based on available data of nuclear charge radii for isotriplets in measured superallowed decays

Gorchtein, Seng ARNPS 74 (2024) 23-47

#### Phase space updates

Integrating over  $\beta$  spectrum for  $\Gamma$ 

$$f = m_e^{-5} \int_{m_e}^{E_0} dE \ pE(E_0 - E)^2 F(Z, E) C(Z, E) K(Z, E)$$

contains charge radius and weak charge effects.

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PHYSICAL REVIEW LETTERS 131, 222502 (2023)

Editors' Suggestion

Featured in Physics

#### Nuclear Charge Radius of <sup>26m</sup>Al and Its Implication for V<sub>ud</sub> in the Quark Mixing Matrix

P. Platner, <sup>1,2,3,\*</sup> E. Wood,<sup>4</sup> L. Al Ayoubi,<sup>5</sup> O. Beliuskina,<sup>5</sup> M. L. Bissell,<sup>6,1</sup> K. Blaum, <sup>3</sup> P. Campbell,<sup>6</sup> B. Cheal,<sup>6</sup>, R. P. de Groote,<sup>5,4</sup> C. S. Devlin,<sup>6</sup> T. Eronen,<sup>7</sup> L. Filippin,<sup>7</sup> R. F. Garcia Ruiz,<sup>1,8</sup> Z. Ge,<sup>5</sup> S. Geldhof,<sup>7</sup> W. Gins,<sup>5</sup> M. Godefroid,<sup>9</sup> H. Heylen,<sup>1,3</sup> M. Hukkanen,<sup>5</sup> P. Imgram,<sup>9</sup> in A. Jaries,<sup>5</sup> A. Jokinen,<sup>5</sup> A. Kanellakopoulos,<sup>9</sup> A. Kankainen,<sup>5</sup> S. Kaufman,<sup>10</sup> K. Könige,<sup>10</sup> A. Koszorós,<sup>5,4</sup> S. Kujanpää,<sup>3</sup> S. Lechner,<sup>6</sup> S. Malbrunot-Ettenauer,<sup>11,11</sup> P. Müller,<sup>10</sup> R. Mathieson,<sup>4</sup> I. Moore,<sup>5</sup> W. Nörtershäuser,<sup>10</sup> D. Nesterenko,<sup>5</sup> R. Neugart,<sup>31,12</sup> G. Neyens,<sup>1,5</sup> A. Ortiz-Cortes,<sup>5</sup> H. Pentülä,<sup>1</sup> J. Pohjalainen,<sup>5</sup> A. Raggio,<sup>5</sup> M. Reponen,<sup>5</sup> S. Kinta-Antila,<sup>5</sup> L. V. Rodríguez,<sup>31,13</sup> J. Romero,<sup>5</sup> R. Sánchez,<sup>14</sup> F. Sommer,<sup>10</sup> M. Stryjczyk,<sup>6</sup> V. Virtanen,<sup>5</sup> L. Xie,<sup>6</sup> Z. Y. Xu,<sup>9</sup> X. F. Yang,<sup>21,5</sup> and D. T. Yordanov<sup>13</sup>

See also 2502.17070

#### Charge radii for V<sub>ud</sub>

Absolute charge radii are put into question

# The lack of new absolute radii



#### Ongoing efforts with muonic atoms

Slide by Michael Heines; see also Ohayon 2409.08193
Isospin breaking (~Coulomb interaction) means

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with  $\delta_{C} \sim 0.1 - 1\%$  for **nuclei**.

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with  $\delta_{\it C} \sim 0.1-1\%$  for <code>nuclei</code>. Traditional approaches separate into

- $\delta_{C1}$ : isospin-mixing meaning  $\langle \pi | a_{p,\alpha} | \phi_i \rangle^* \neq \langle \phi_f | a_{n,\alpha}^{\dagger} | \pi \rangle$
- $\delta_{C2}$ : radial mismatch, i.e. proton and neutron orbits are not the same

but conceptual issues already noted 15 years ago (Miller & Schwenk)

Same problem: strong theory dependence

# On the radar: $\delta_C$

Proton  $\neq$  neutron inside nucleus  $\rightarrow M_F^2 = 2(1 - \delta_C)$ 



It's  $\delta_C$  that brings  $V_{ud}$  from different transitions in line

Grinyer et al., NIMA 622 (2010) 236

Rewrite  $\delta_C$  using standard perturbation theory for  $H = H_0 + V_{ISB}$ 

$$\delta_{C} \simeq \sum_{T=0,1,2} \frac{\langle a; T || V_{\text{ISB}} || g; 1 \rangle^{2}}{(E_{a,T} - E_{g,1})^{2}}$$

over all states a and ground state g, assuming  $V_{\rm ISB}$  is isovector.

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Can charge radii do anything?

PLB 838 (2023) 137654; PLB 846 (2023) 138259

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Can construct object

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which is 0 for perfect isospin symmetry

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if only 1 intermediate state (isovector monopole dominance) contributes,  $\delta_C \sim \Delta M_B^{(1)}$ , but generically a theory discriminator

Transitions	δ <sub>C</sub> (%)						Transitions	$\Delta M_B^{(1)}~({\rm fm}^2)$				
	WS	DFT	HF	RPA	Micro			WS	DFT	HF	RPA	Micro
$^{26m}$ Al $\rightarrow$ $^{26}$ Mg	0.310	0.329	0.30	0.139	0.08		$^{26m}$ Al $\rightarrow$ $^{26}$ Mg	-0.12	-0.12	-0.11	-0.05	-0.03
$^{34}\text{Cl} \rightarrow ^{34}\text{S}$	0.613	0.75	0.57	0.234	0.13		$^{34}\text{Cl} \rightarrow ^{34}\text{S}$	-0.17	-0.21	-0.16	-0.06	-0.04
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What we can measure

$$\Delta M_B^{(1)} \equiv \frac{1}{2} \left( Z_1 R_{p,1}^2 + Z_{-1} R_{p,-1}^2 \right) - Z_0 R_{p,0}^2$$

#### Slide by Ben Ohayon

# Charge radii for ISB

What we want to know						What we can measure						
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The <u>on</u>	ly examp	$\Delta M_B^{(1)}$ le:	$\left  \right\rangle \equiv \frac{1}{2}$	$-\left(Z_1R\right)$	$\frac{2}{p,1} + Z_{-}$	$\frac{1}{1}R_{p,-1}^2 - Z_0$	$R_{p,0}^2 =$	• 0.1 <u>+</u>	1.0 fm	12		
Very high accuracy needed to distinguish models !												

#### ....

Slide by Ben Ohayon

## Takeaways

• Significant reevaluation following CKM non-unitarity, major opportunities/challenges for nuclear ab initio

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Now, let's talk experiment

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Theory progress in the last 5 years

Charge radii for CKM unitarity

Experimental opportunities

ASGARD

Summary & Outlook

# $V_{ud}$ and mirror extraction

If mixing ratio  $\rho$  is known, get  $V_{ud}$ 

 $V_{ud}^2(1+
ho^2)=K imes(1+\delta_{
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ho^2)=K imes(1+\delta_{
m corr})$$

Typically, need to measure angular correlations.

### Either

- Polarized nuclei  $(A_{\beta})$
- measure 2 final states  $(a_{eta
  u})$

but significant experimental difficulties (backscattering, cuts, ...)



LH, ARNPS 74 (2024) 497

## Continuous recoil spectroscopy

#### Can instead recover $\rho$ from recoil spectrum alone!





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..but recoil energies are <keV, and so far only indirect methods (ToF) at percent-level

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..but recoil energies are <keV, and so far only indirect methods (ToF) at percent-level

and interesting isotopes are short-lived

'Conventional' detection technologies become insufficient, need

- Low detection threshold (< 1 keV)
- High ( $\sim$  eV) resolution
- High acceptance

Want to detect athermal phonons  $\rightarrow$  cryogenic systems



# Introducing Superconducting Tunnel Junctions

### Biased Josephson junction



Number of key advantages

- Low threshold energy  $(\sim 1.5 \text{ eV})$
- High energy resolution
- High count rate (up to kHz)

### Combination is unique

Allows for the first time energy spectroscopy of recoiling nuclei from  $\beta$  decay!

# BeEST@TRIUMF



# <sup>7</sup>Be electron capture

- Responsible for <sup>7</sup>Li creation in stars
- Essential contribution to solar neutrino spectrum

### Measurement campaign

- 1. Implantation at ISAC (TRIUMF)
- 2. Ship to LLNL
- 3. Cool down and measure

# BeEST@TRIUMF

# Most precise $^{7}$ Be L/K capture measurement



PRL 126 (2021) 021803; PRL 125 (2020), 032701

# BeEST neutrino wave packet size limits

### Probe $\nu$ size from $\Delta x \Delta p \ge \hbar/2$ in <sup>7</sup>Li spectrum

#### nature

Article Open access Published: 12 February 2025

# Direct experimental constraints on the spatial extent of a neutrino wavepacket

Joseph Smolsky <sup>CD</sup>, Kvie G. Leach <sup>CD</sup>, Byan Abells, Pedro Amaro, Adrien Andoche, Keith Borbridge, Connor Tray, Robin Cantor, David Diercks, Spencer Fretwell, Stephan Friedrich, Abiaell Ollessie, Mauro Guerra, Ad Hall, Cameron N. Harris, Jackson T. Harris, Leendert M. Hayen, Paul-Antoine Hervieux, Calvin Hinkle, Geen-Bo Kim, Inwook Kim, Amil Lamm, Annika Lennarz, Vincenzo Lordi, ... William K, Warburton + Show authors

Nature 638, 640-644 (2025) Cite this article



First **direct** constraint on neutrino wave packet size!

Open question:  $\sigma_E^{Li} = \sigma_E^{\nu}$  or  $\sigma_p^{Li} = \sigma_p^{\nu}$ ? unresolved!

## BeEST neutrino wave packet size limits

# Probe $\nu$ size from $\Delta x \Delta p \ge \hbar/2$ in <sup>7</sup>Li spectrum



At least 2 orders of magnitude more stringent than global limits! Smolsky et al., Nature 638 (2025) 640

# SALER prototype: First STJ online measurements

#### Use same detector and fridge as BeEST, but online at RIB!



first demonstration, but thermal windows mean difficult and imprecise implantation ultimately limiting precision

# SALER@FRIB: First STJ online measurements

#### Commissioning and first light in April 2024



Hot off the press: FRIB PAC proposal accepted for Fall 25

# Anticipated systematic effects

### Detector measures all deposited energy



Low energy threshold ( $\sim$  eV) means strong overlap with condensed matter physics

# **SALER** limitations

SALER is necessary first step, but can't reach high precision. Even after implantation, substantial systematic effects anticipated



Scattering anticipated to enter at percent-level

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# Introducing ASGARD

### Open STJs up to all ISOL beams, precision spectroscopy



Aluminium Superconducting Grid Assembly for Radiation Detection Installation at DESIR facility in GANIL anticipated 2028

# ASGARD overview



Both  $V_{ud}$  (Type-II) and exotic currents (Type-I)!

### # 1: Windowless dilution fridge allows direct implantation



### Now all ISOL isotopes become available at 100% efficiency

### # 2: Novel, ultra-thin Al-based STJ detectors



30-nm geometry reduces scattering effects by two orders of magnitude

Increased resolution, mitigated material-dependent effects
#### # 3: Precision injection beam line



Custom implantation of all ISOL isotopes

Shallow implantation further reduces scattering by another order of magnitude

## ASGARD: Scattering systematic uncertainty



Uncertainties due to scattering on  $V_{ud} \leq 0.01\%!$ 

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Nuclear charge radii can provide data-driven uncertainties, important theory discriminator

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Mirror isotopes continue to be promising due to large enhancements

Nuclear charge radii can provide data-driven uncertainties, important theory discriminator

Mirror isotopes continue to be promising due to large enhancements

New spectroscopy techniques incoming, recoil spectroscopy with quantum sensors is highly promising!

## **BeEST & SALER**





"One should be prepared for further surprises with beta decay"

Niels Bohr, 1933

## **Phonon detection**

Phonons are lattice vibration quanta

Acoustical Mode





Typical energy scale of (tens of) meV  $\rightarrow >$  100 lower than e-h in Si, Ge

# ASGARD Timeline

#### ERC submitted in 2024

Anticipated installation at DESIR@GANIL facility

Currently ongoing systematic effect simulations, theory support & design



# Aside: recent progress on $\Delta_R^A$

First  $\mathcal{O}(\alpha)$  calculation of  $\Delta_R^A$ , follow-up with dispersion relations and lattice QCD

$$\Delta_R^A-\Delta_R^V=0.13(13) imes 10^{-3}$$

# Aside: recent progress on $\Delta_R^A$

First  $\mathcal{O}(\alpha)$  calculation of  $\Delta_R^A$ , follow-up with dispersion relations and lattice QCD

$$\Delta_R^A - \Delta_R^V = 0.13(13) \times 10^{-3}$$

but only first half of the story... also here large ISB effects



First time:  $\delta_{\text{RC}}^{(\lambda)} \in \{1.4, 2.6\} \cdot 10^{-2}$  LH, PRD 103 113001; Seng, Particles 2021, 397; Gorchtein & Seng, JHEP 10 53; PRL 129 121801

Situation is analogues but more complicated than  $0^+ \to 0^+.$  Significant questions on:

- How do energy-dependent terms enter for axial transitions?
- What about nuclear shadowing for spin-dependent transitions?

Mirror decays extract  $\rho = g_A M_{GT}/g_V M_F$  from angular correlations  $(a_{\beta\nu}, A_{\beta})$ , but both effects may mean  $\rho^{\text{corr}} \neq \rho^{\text{Ft}}$ .

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#### Happened before:

double counting was resolved and  $V_{ud}^{\text{mirror}}$  now agrees with  $V_{ud}^{0^+ \rightarrow 0^+}$ 

LH, PRD 103, 113001; LH, ARNPS 74 (2024) 497



## Superconducting tunnel junctions (Slide by Kyle Leach)



- Pulsed 355 nm (3.49965(15) eV) laser at 5 kHz fed through optical fiber to 0.1 K stage
- Illumination of STJ provides a comb of peaks at integer multiples of 3.5 eV
- Intrinsic resolution of our Ta-based devices is between ~1.5 and ~2.5 eV FWHM at ~10 – 200 eV
- Stable response and small quadratic nonlinearity (10<sup>-4</sup> per eV)



## The BeEST experiment (Slide by Kyle Leach)

# **<b>∂**TRIUMF

#### Rare-isotope implantation at TRIUMF-ISAC





A. Samanta et al., Phys. Rev. Mat. (in press) (2022) S. Friedrich et al., Low Temp. Phys. (in press) (2022) C. Bray et al., J. Low Temp. Phys. (in press) (2022) K.G. Leach and S. Friedrich, J. Low Temp. Phys. (in press) (2022) S. Friedrich et al., Phys. Rev. Lett. **125**, 032701 (2021) S. Friedrich et al., Low Temp. Phys. **200**, 2020 (2021)

#### Ta, Al, and Nb-based STJ Sensors









# Introduction: Weak interaction & CKM matrix

Cabibbo-Kobayashi-Maskawa matrix relates weak and mass eigenstates

$$\left(\begin{array}{c} d\\s\\b\end{array}\right)_{w} = \left(\begin{array}{ccc} V_{ud} & V_{us} & V_{ub}\\V_{cd} & V_{cs} & V_{cb}\\V_{td} & V_{ts} & V_{tb}\end{array}\right) \left(\begin{array}{c} d\\s\\b\end{array}\right)_{m}$$

## Introduction: Weak interaction & CKM matrix

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Unitarity requires

$$|V_{ud}|^2 + |V_{us}|^2 + |V_{ub}|^2 = 1$$

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Unitarity requires

$$|V_{ud}|^2 + |V_{us}|^2 + |V_{ub}|^2 = 1$$

(nuclear) eta decay, meson decay ( $\pi$ , K),  $|V_{ub}|^2 \sim 10^{-5}$ 

Violations are sensitive to TeV scale new physics!

## CKM unitarity: Current status

Signs of non-unitarity at few  $\sigma$  level...

Disagreement between K/2 and K/3  $|V_{us}|$  'Cabibbo angle anomaly'



## CKM unitarity: Cabibbo Angle Anomaly

#### Signs of non-unitarity at several $\sigma$ (Falkowski CKM2021)



# CKM unitarity: Cabibbo Angle Anomaly

#### Signs of non-unitarity at several $\sigma$ (Falkowski CKM2021)



Takeaways assuming Standard Model physics:

- Most precise  $V_{ud}$  &  $V_{us}$  not consistent with unitarity
- Significant internal inconsistencies within  $V_{us}$
- Taken at face value  $\sim 3\sigma$  for new physics

A more modern way of interpreting BSM physics

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Effective field theory: new physics at scale  $\Lambda_{BSM} \gg LHC$ 

$$\mathcal{L}_{eff} = \mathcal{L}_{SM} + \sum_{i=1} c_i \frac{\mathcal{O}_{4+i}}{\Lambda^i_{BSM}}$$

effective operators O(i). Expansion in parameter  $c_i/\Lambda_{BSM}^i \ll 1$ 

A more modern way of interpreting BSM physics

Effective field theory: new physics at scale  $\Lambda_{BSM} \gg LHC$ 

$$\mathcal{L}_{eff} = \mathcal{L}_{SM} + \sum_{i=1} c_i \frac{\mathcal{O}_{4+i}}{\Lambda_{BSM}^i}$$

effective operators O(i). Expansion in parameter  $c_i/\Lambda_{BSM}^i \ll 1$ 

Phenomenological theories will give different  $\{c_i\}$ ,

but agnostic experimental analysis

SM has V-A structure, but more generally

$$\begin{split} \mathcal{L}_{\text{eff}} &= -\frac{G_{\text{F}}\,\tilde{V}_{ud}}{\sqrt{2}} \bigg\{ \bar{e}\gamma_{\mu}\nu_{L}\cdot\bar{u}\gamma^{\mu}[c_{V}-(c_{A}-2\epsilon_{R})\gamma^{5}]d + \epsilon_{\text{S}}\,\bar{e}\nu_{L}\cdot\bar{u}d \\ &-\epsilon_{P}\,\bar{e}\nu_{L}\cdot\bar{u}\gamma^{5}d + \epsilon_{\text{T}}\,\bar{e}\sigma_{\mu\nu}\nu_{L}\cdot\bar{u}\sigma^{\mu\nu}(1-\gamma^{5})d \bigg\} + \text{h.c.}, \end{split}$$

at the quark level

SM has V-A structure, but more generally

$$\begin{split} \mathcal{L}_{\text{eff}} &= -\frac{G_{\text{F}}\,\tilde{V}_{ud}}{\sqrt{2}} \bigg\{ \bar{e}\gamma_{\mu}\nu_{L}\cdot\bar{u}\gamma^{\mu}[c_{V}-(c_{\text{A}}-2\epsilon_{\text{R}})\gamma^{5}]d + \epsilon_{\text{S}}\,\bar{e}\nu_{L}\cdot\bar{u}d \\ &-\epsilon_{\text{P}}\,\bar{e}\nu_{L}\cdot\bar{u}\gamma^{5}d + \epsilon_{\text{T}}\,\bar{e}\sigma_{\mu\nu}\nu_{L}\cdot\bar{u}\sigma^{\mu\nu}(1-\gamma^{5})d \bigg\} + \text{h.c.}, \end{split}$$

at the quark level

All  $\epsilon_i$  are proportional to  $(M_W/\Lambda_{BSM})^2$ , change kinematics  $\epsilon_i \lesssim 10^{-4} \rightarrow \Lambda_{BSM} \gtrsim 15$  TeV assuming natural couplings

#### Effective field theory tower Slide by V. Cirigliano



#### Effective field theory recipe Slide by V. Cirigliano

- In order to build L<sub>eff</sub>, one needs to specify:
  - \* Relevant low-E degrees of freedom: assume SM field content
    - \* One Higgs doublet, no light VR and no other light fields
  - \* Symmetries: L<sub>eff</sub> must reflect symmetries of underlying theory
    - ★ Assume underlying theory respects SM gauge group SU(3)<sub>c</sub> × SU(2)<sub>W</sub> × U(1)<sub>Y</sub>
    - ★ But not necessarily SM symmetries that result from keeping only terms of dimension  $\leq 4$
  - \* Power counting in E/A,  $v_{EW}/A <<1$  (recall  $v_{EW} = G_F^{-1/2}$ ): organize analysis in terms of operators of increasing dimension (5,6,...)

# **Recent changes:** $\Delta_R^V$

#### Number of new calculations performed



Now good convergence: uncertainty halved but about  $3\sigma$  shift

# Superallowed uncertainties

#### Experimentally, $T_z = -1$ limited by BR (new <sup>10</sup>C welcome)



#### Moving towards mature ab initio theory evaluation

#### Talk by Bertram Blank

Hardy & Towner PRC 102 (2020) 045501

## **Recent changes:** $\delta_{NS}$

Nuclear medium changes nuclear response, but also spectrum





## **Recent changes:** $\delta_{NS}$

Nuclear medium changes nuclear response, but also spectrum



Paradigm shift in analysis, two major effects Quasi-elastic contributions Nuclear polarization

$$\delta^{A}_{NS} = \frac{\alpha}{\pi} [-0.47 \pm 0.14]^{\text{QE}}$$
  $\delta^{A}_{NS}(E) \sim (1.6 \pm 1.6) \times 10^{-4} \left(\frac{E}{\text{MeV}}\right)^{-4}$ 

Estimated using free Fermi gas Current  $0^+ \rightarrow 0^+$  bottleneck

Seng et al., PRD 100 013001

# On the radar: $\delta_C$

Proton eq neutron inside nucleus  $ightarrow M_F^2 = 2(1-\delta_{\mathcal{C}})$ 

- 1. Configuration interaction difference initial  $\leftrightarrow$  final
- 2. Different radial wave function (Coulomb)

$$\delta_C = \delta_{C1} + \delta_{C2}$$

### On the radar: $\delta_C$

Proton  $\neq$  neutron inside nucleus  $\rightarrow M_F^2 = 2(1 - \delta_C)$ 

- 1. Configuration interaction difference initial  $\leftrightarrow$  final
- 2. Different radial wave function (Coulomb)

$$\delta_{C} = \delta_{C1} + \delta_{C2}$$



Grinyer et al., NIMA 622 (2010) 236
### Progress in nuclear ab initio theory



H. Hergert, Frontiers in Physics (2020)

## Monte Carlo methods (Slide by Saori Pastore)

Ab initio is providing bottleneck input for spectral measurements



Dominant terms  $L_{1^{(0)}}$  and  $E_{1^{(0)}}$  have model dependence of ~1% to ~2%

Looking at implementing  $\delta_{NS}$  for <sup>10</sup>C

Standard Model spectrum for <sup>6</sup>He



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### No Core Shell Model (Slide by Michael Gennari)



# Going heavier: IM-SRG type methods (Slide by Heiko Hergert)

- IMSRG for closed and open-shell nuclei: IM-HF and IM-PHFB
  - HH, Phys. Scripta, Phys. Scripta 92, 023002 (2017)
  - HH, S. K. Bogner, T. D. Morris, A. Schwenk, and K. Tuskiyama, Phys. Rept. 621, 165 (2016)

#### • Valence-Space IMSRG (VS-IMSRG)

- S. R. Stroberg, HH, S. K. Bogner, J. D. Holt, Ann. Rev. Nucl. Part. Sci. 69, 165
- In-Medium No Core Shell Model (IM-NCSM)
  - E. Gebrerufael, K. Vobig, HH, R. Roth, PRL 118, 152503
- In-Medium Generator Coordinate Method (IM-GCM)
  - J. M. Yao, J. Engel, L. J. Wang, C. F. Jiao, HH PRC 98, 054311 (2018)
  - J. M. Yao et al., PRL 124, 232501 (2020)

+ Coupled Cluster,  $\ldots$ 

XYZ

Major advances in last decade, EFT come into its own

Quantifiable theory uncertainties are game-changer for precision FS: paradigm shifts are strong driver of progress in the field

Benefit from 'rigorous' theory overlap at low masses (NCSM, GFMC, QMC)

- $0^+ \rightarrow 0^+$  :<sup>10</sup>C & <sup>14</sup>O
- Promising isotopes:  ${}^{6}\text{He}$ ,  ${}^{11}\text{C}$ , ...

to confidently go higher (CC, IM-SRG, IM-GCM, ...)

Path forward for  $0^+ 
ightarrow 0^+ \ V_{ud}$ 

# **BeEST** implantation



## **SALER** implantation



#### 11 MeV <sup>11</sup>C Beam w/ 8µm Al foil

# For a given energy, initial beam from <u>ReA</u> can be +/- a few % in spread

- 1% spread gives ~50 nm width in the depth profile
  - Total <sup>11</sup>C<sup>+</sup> to achieve goal: ~10<sup>7</sup> (< 2 days of beam @ 100 pps)
    - Purity: 1 part in 10<sup>6</sup>

#### 11.1 MeV <sup>11</sup>C Beam



10.9 MeV <sup>11</sup>C Beam

