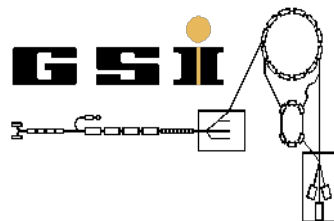


Precision Experiments at Heavy-Ion Storage Rings

Yury A. Litvinov

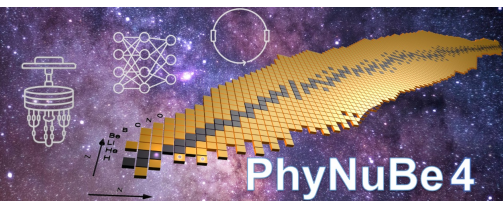
HELMHOLTZ
RESEARCH FOR GRAND CHALLENGES



中国科学院近代物理研究所
Institute of Modern Physics, Chinese Academy of Sciences

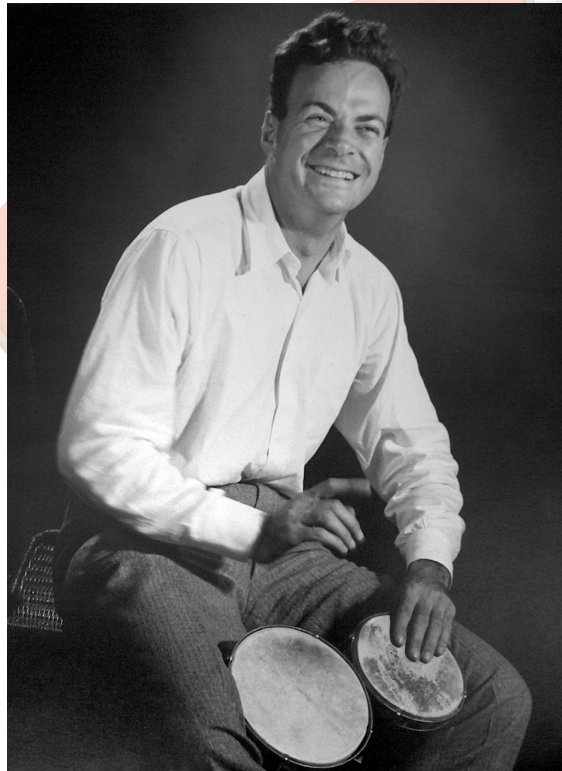


www.gsi.de/astrum



4th PhyNuBe school: Innovative Technologies, Theories, and Methodologies in Nuclear Physics
"Paul Langevin", Haute-Maurienne-Vanoise-Alpen, Aussois, France
17-22 May 2026

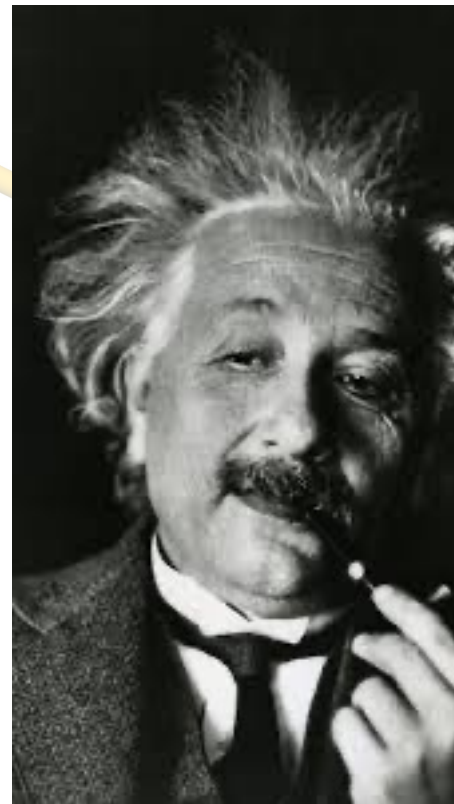
HELMHOLTZ **GSI**



Richard P. Feynman
(Nobel prize 1965)

nobody knows how to teach physics, or to educate people—that's a fact, and if you don't like the way it's being done, that's perfectly natural.

It is nothing short of a miracle that modern methods of instruction have not yet entirely strangled the holy curiosity of inquiry



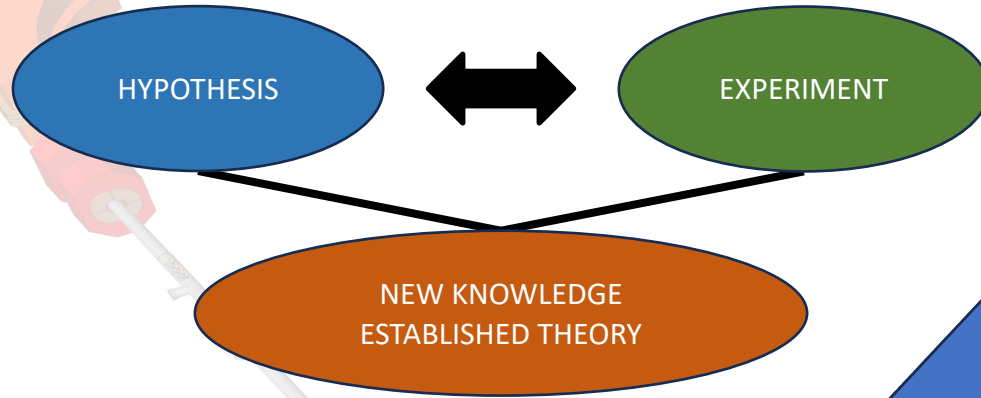
Albert Einstein
(Nobel prize 1921)

Precision Experiments at Heavy-Ion Storage Rings

1. Heavy-ion storage rings: Why? Where? How?
 - a) Introduction to nuclear structure and astrophysics
 - b) Production and separation of radionuclides
 - c) Storage, cooling, and manipulation of beams
2. Mass spectrometry of exotic nuclides
3. Radioactive decays of highly-charged ions
4. Reactions for nuclear astrophysics

How to learn something new?

Only via an experimental confirmation a hypothesis becomes a theory



"The first principle is that you must not fool yourself and you are the easiest person to fool."

R. Feynman

Here should be a picture by M.C. Escher
"Relativity" but it is copyright protected and
cannot be easily displayed

2015 The M.C. Escher Company - Baarn, The Netherlands, bbc.com

M.C. Escher: "Relativity"

Fundamental Interactions

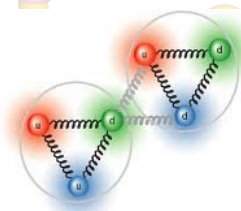
What is so exciting about atomic nuclei?



Electromagnetic



Weak



Strong

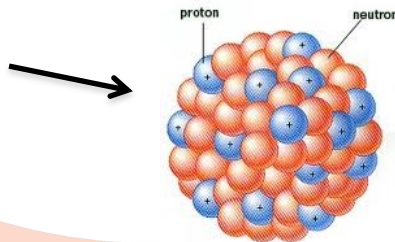


Protons

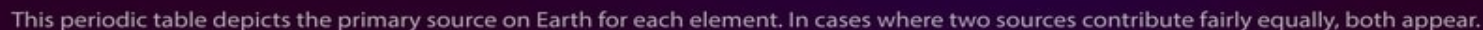


Neutrons

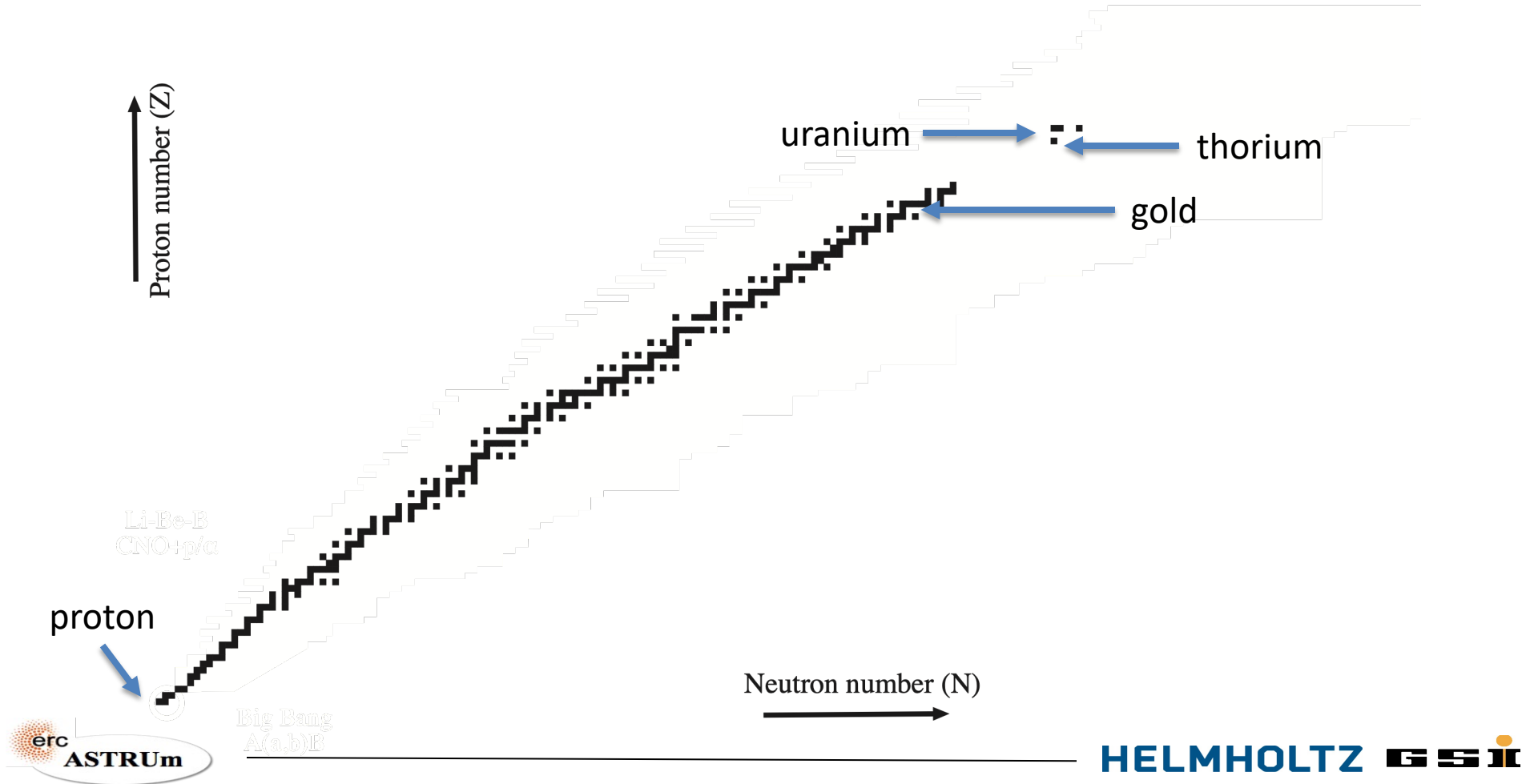
Nucleons
Fermions
($S=1/2$)



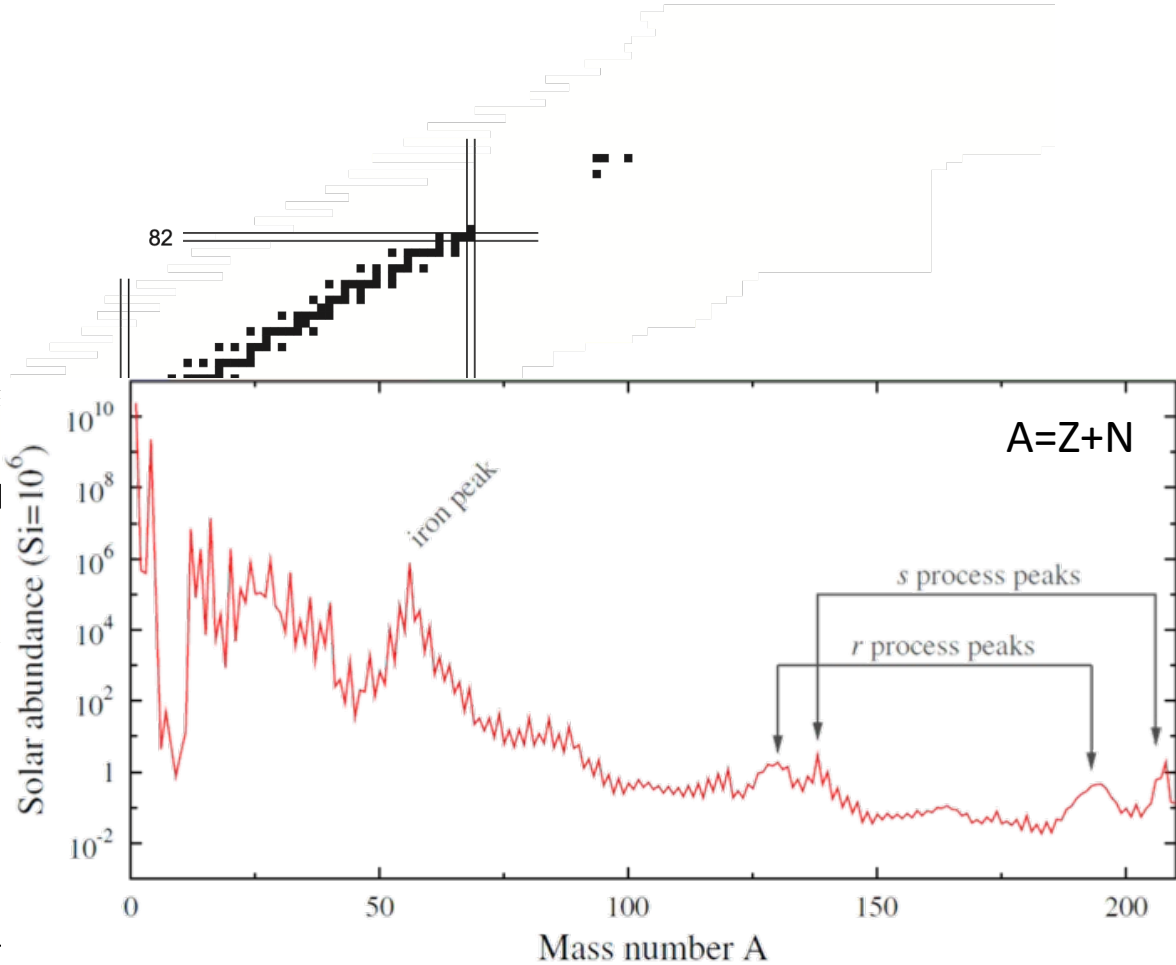
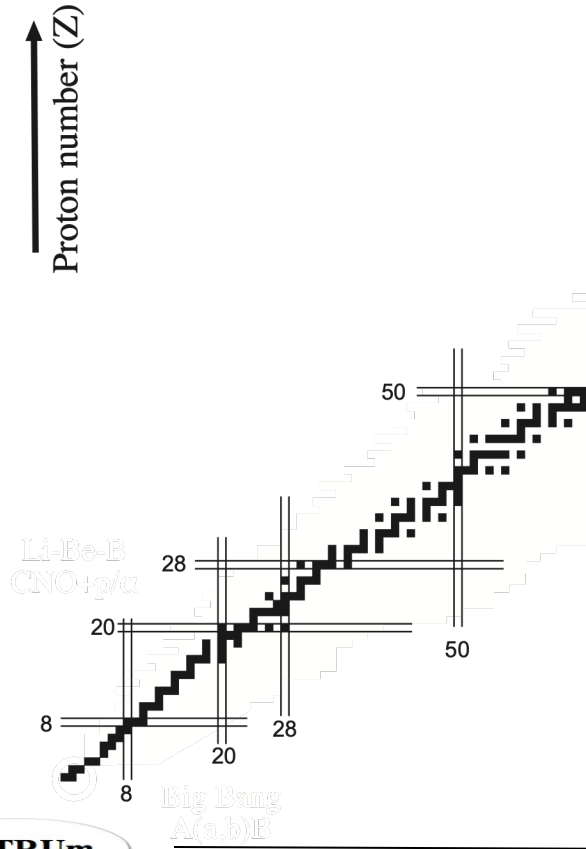
Atomic nuclei – natural results of the complex “game” of complex interactions in a complex quantum many-body system composed of two types of fermions



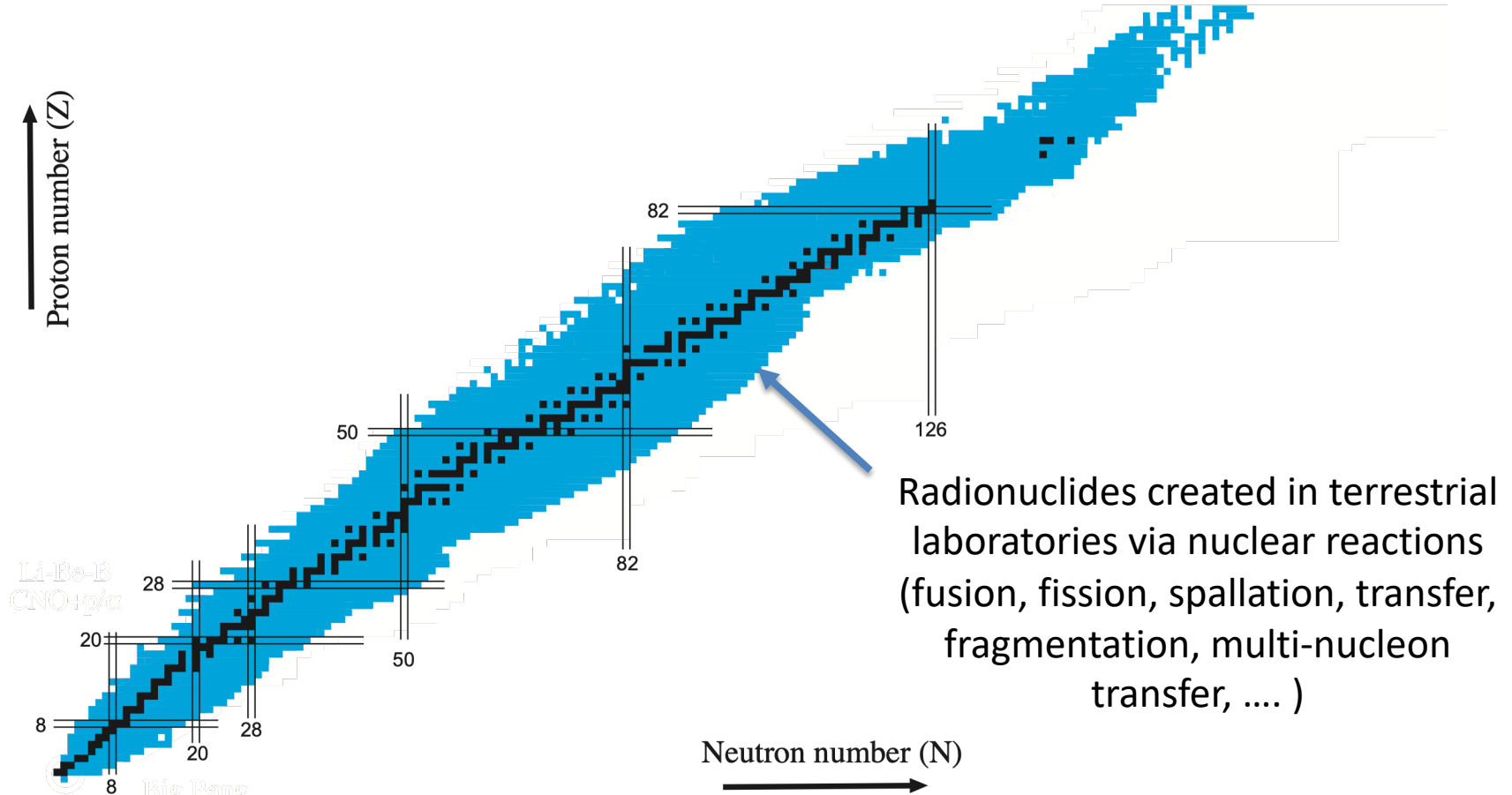
Nuclear Chart: Stable nuclei



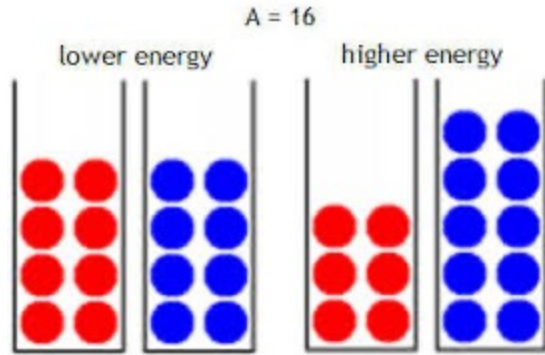
Nuclear Chart: Magic numbers



Nuclear Chart: Known nuclides

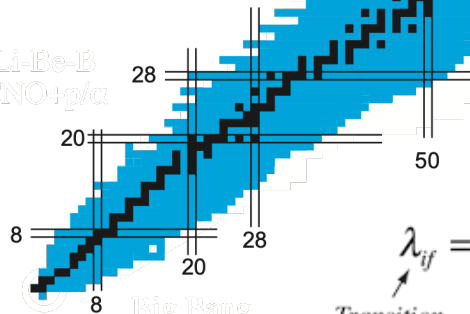


Nuclear Chart: Known nuclides



$$A = Z + N$$

Li-Be-B
CNO+p/a



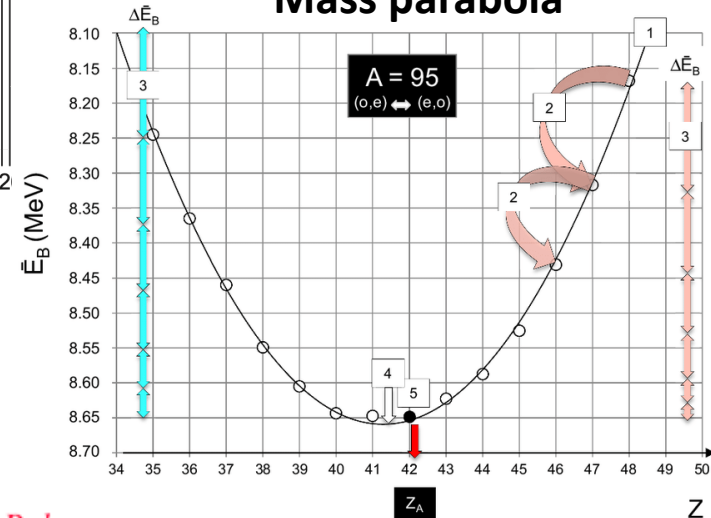
Big Bang
A(a,b)E

$$\lambda_{if} = \frac{2\pi}{\hbar} |M_{if}|^2 \rho_f$$

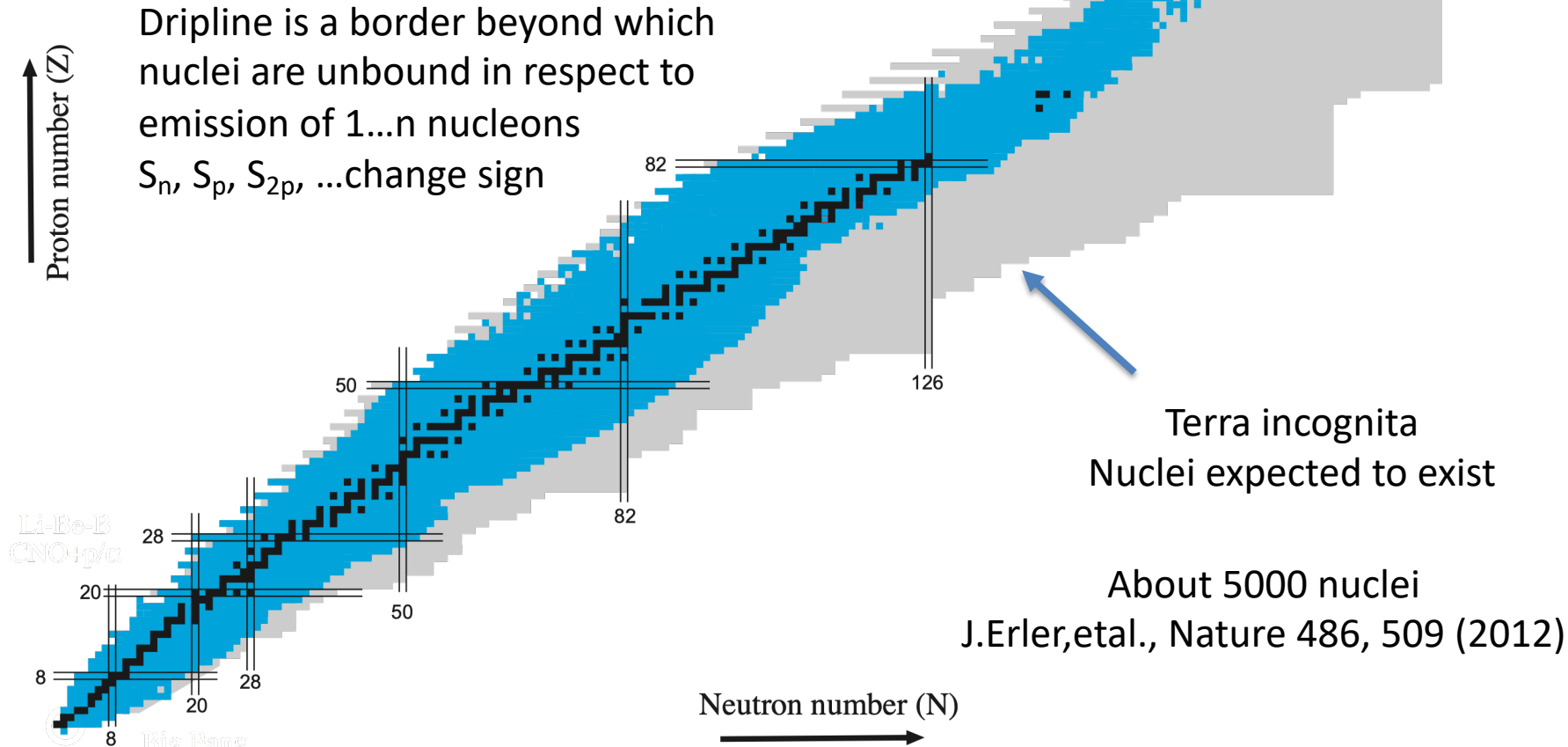
Transition probability Matrix element for the interaction Density of final states

Fermi's Golden Rule

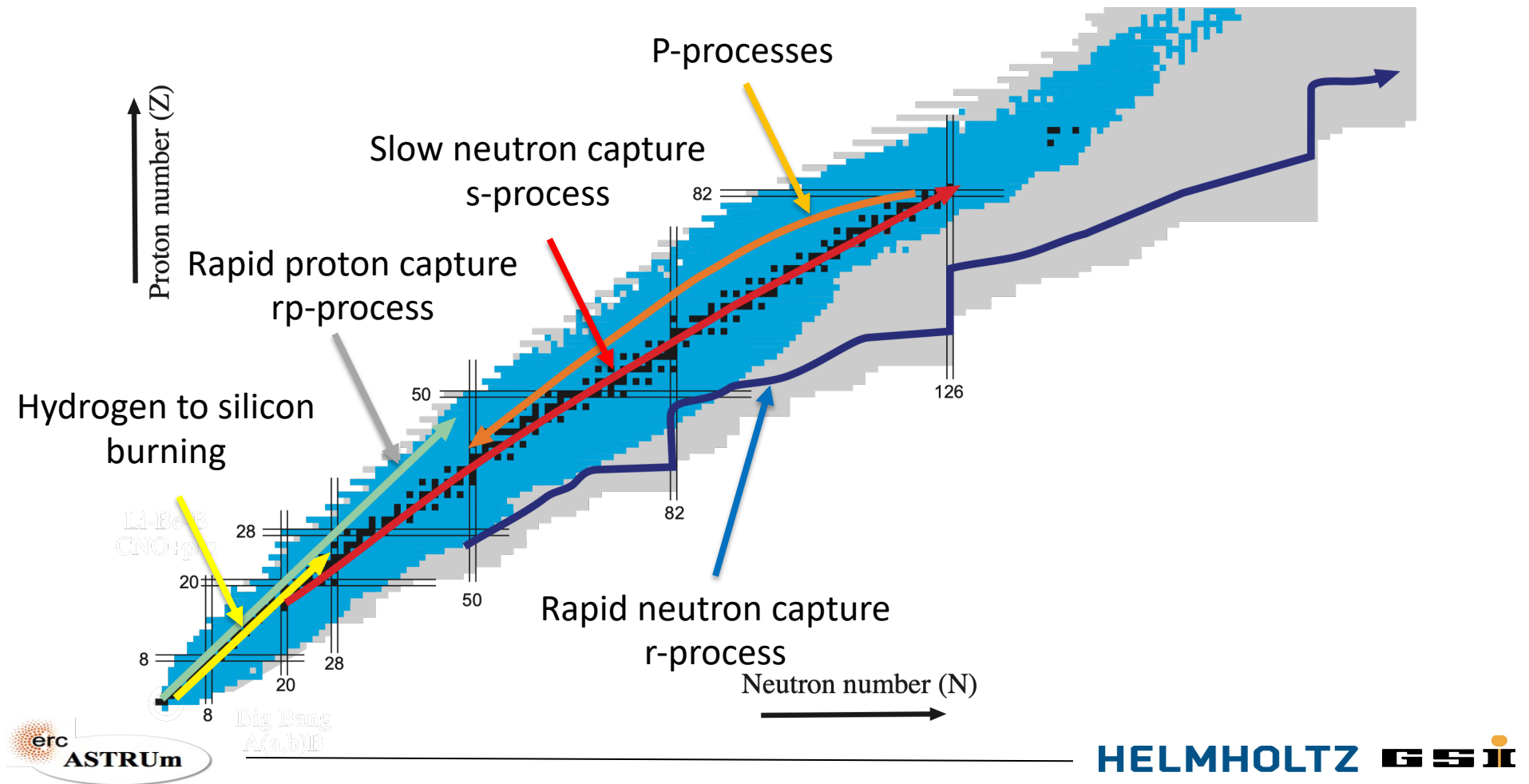
Mass parabola



Nuclear Chart: What is not yet known?



Nucleosynthesis Processes



Nucleosynthesis Processes (best known)

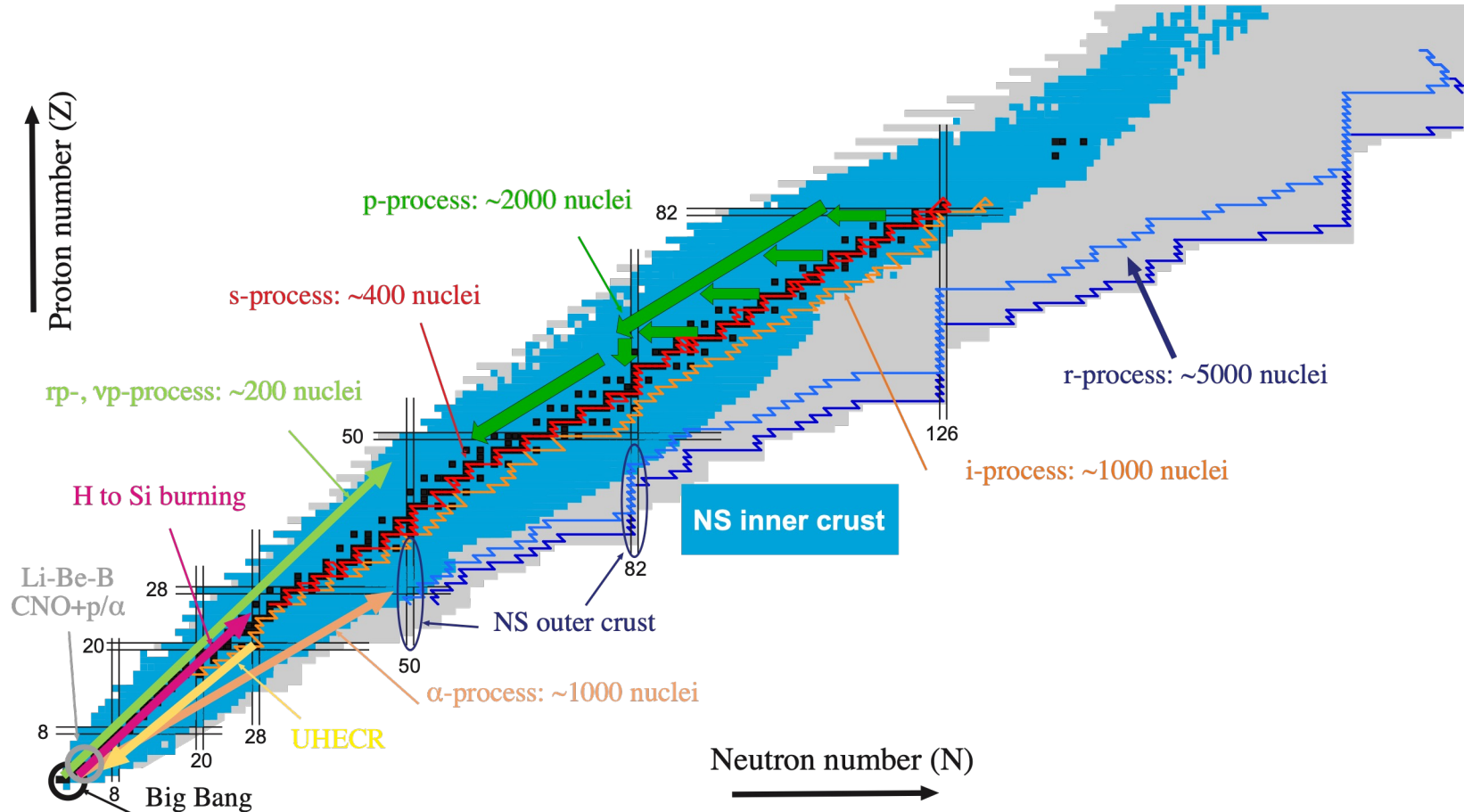
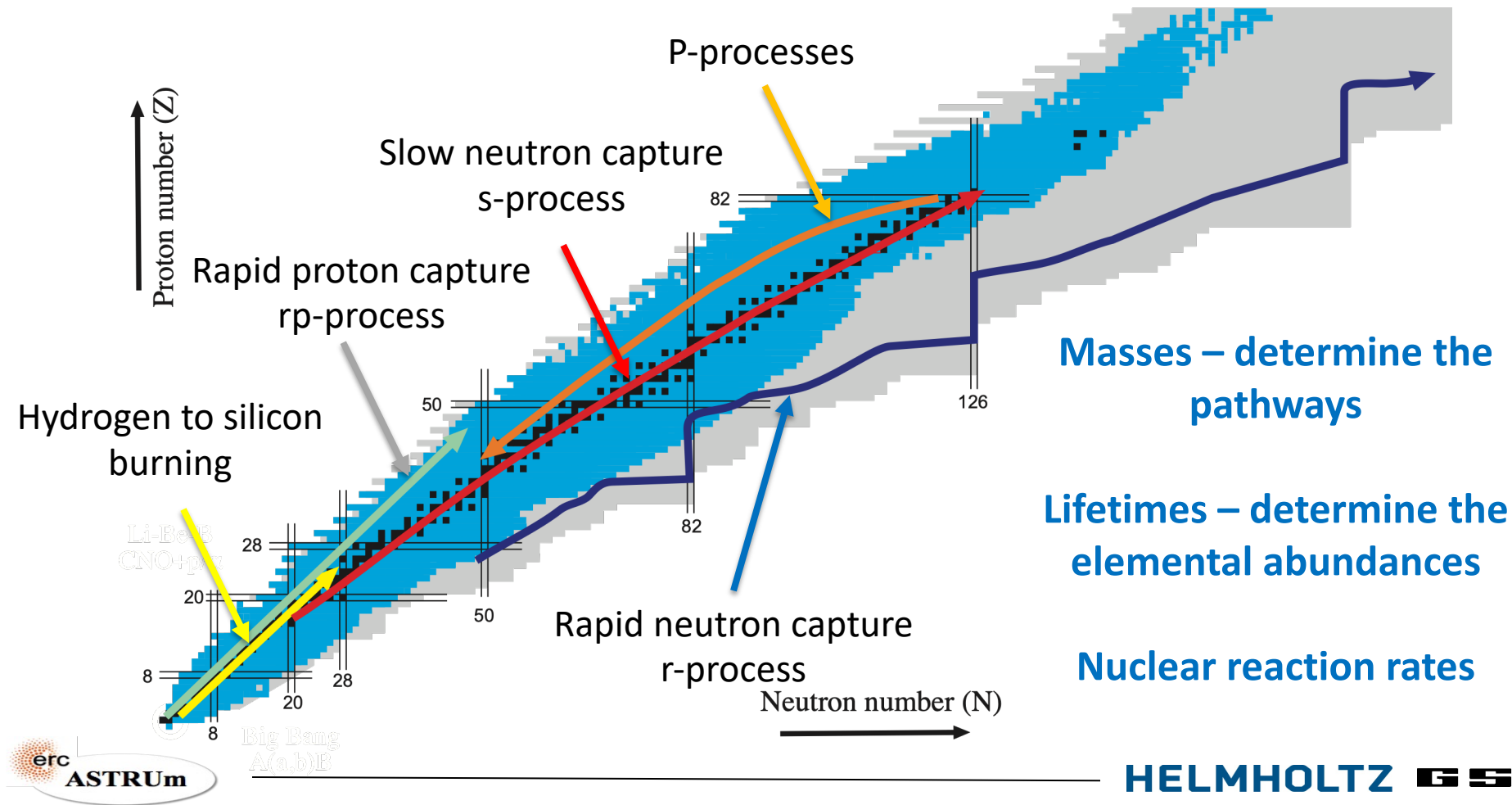


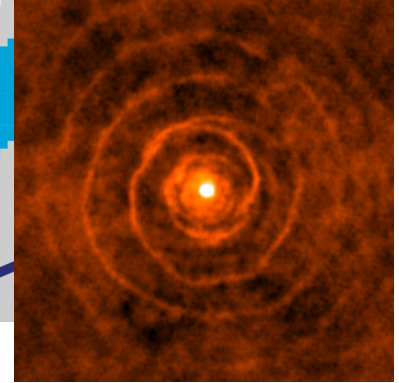
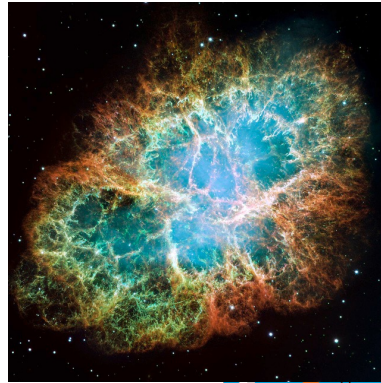
Figure: NuPECC Long Range Plan 2024

Nucleosynthesis Processes

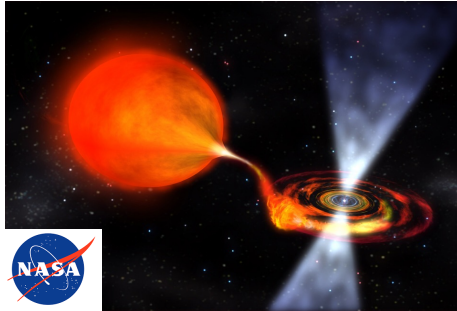


Nucleosynthesis Processes

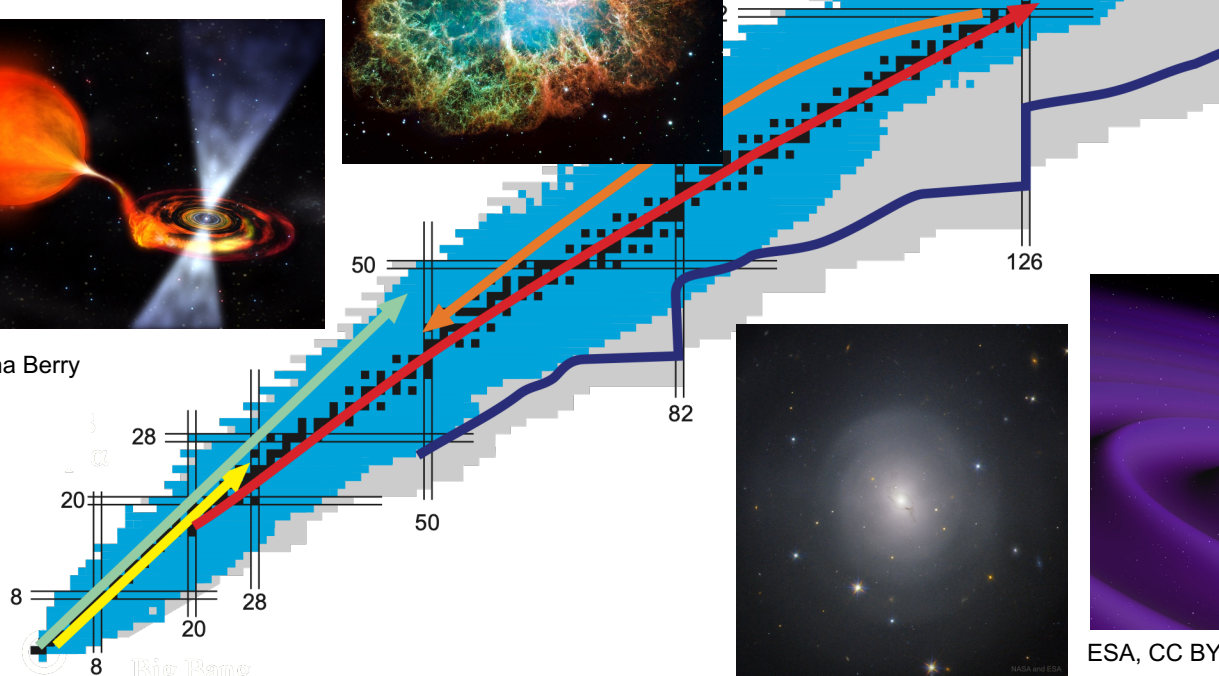
Hubble Gallery
NASA, ESA,
J. Hester, A. Loll



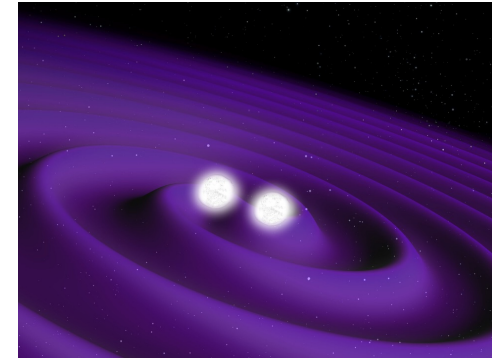
ALMA
(ESO/NAOJ/NRAO)
Hyosun Kim et al.



NASA/Dana Berry



Hubble Gallery, NASA, ESA



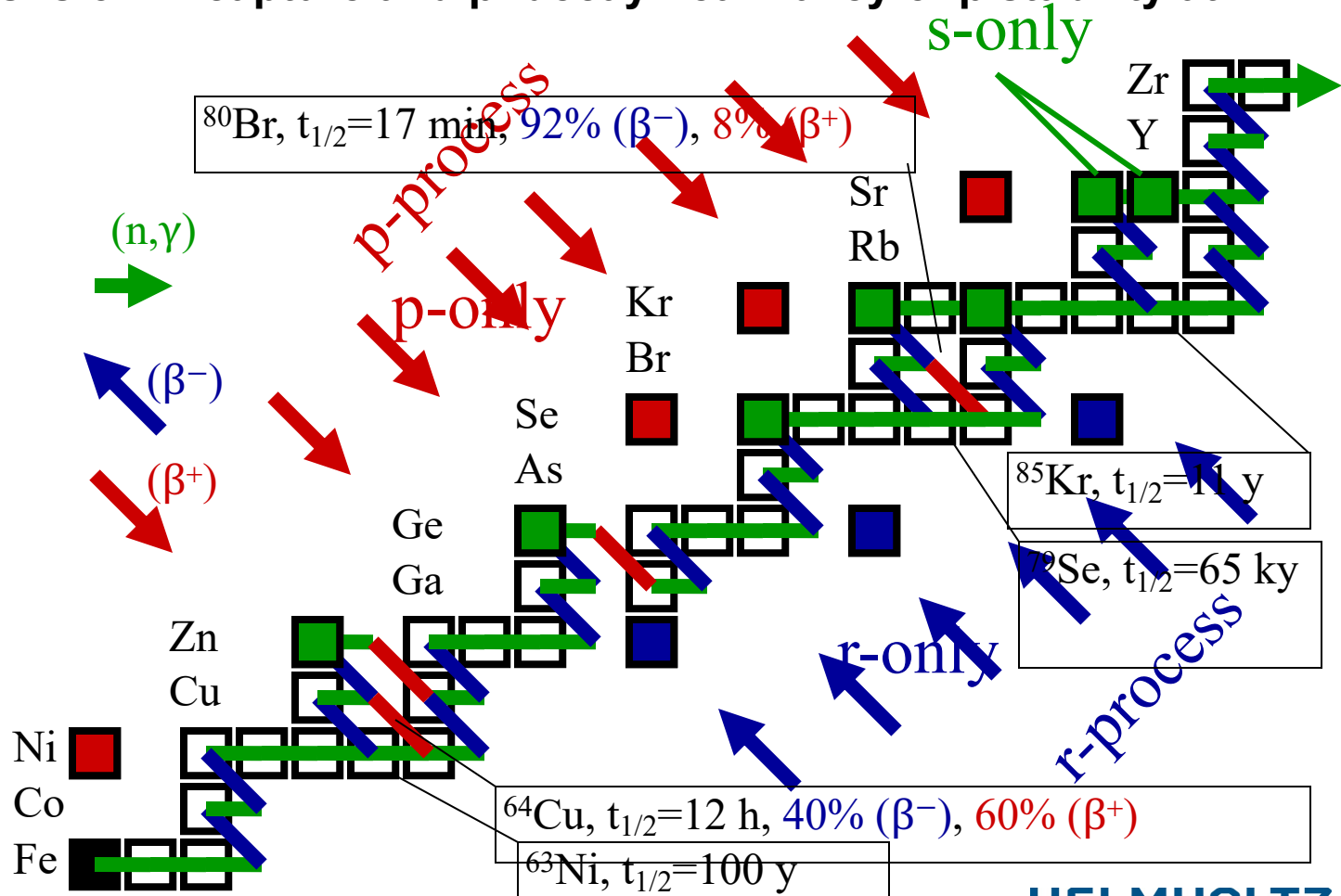
ESA, CC BY-SA 3.0 IGO

Big Bang
Nucleosynthesis

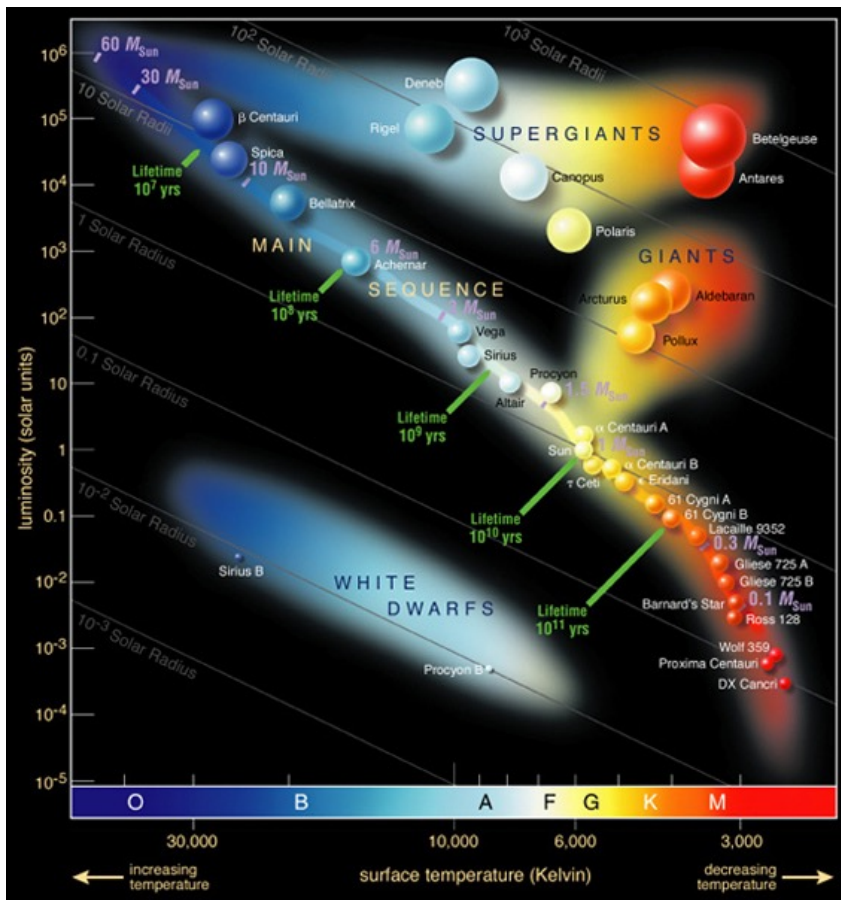
erc
ASTRUM

HELMHOLTZ GSI

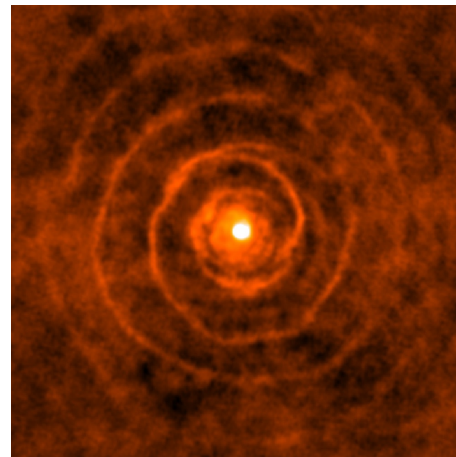
s process: slow n-capture and β^- decay near valley of β stability at $kT = 30$ keV



The Hertzsprung–Russell diagram

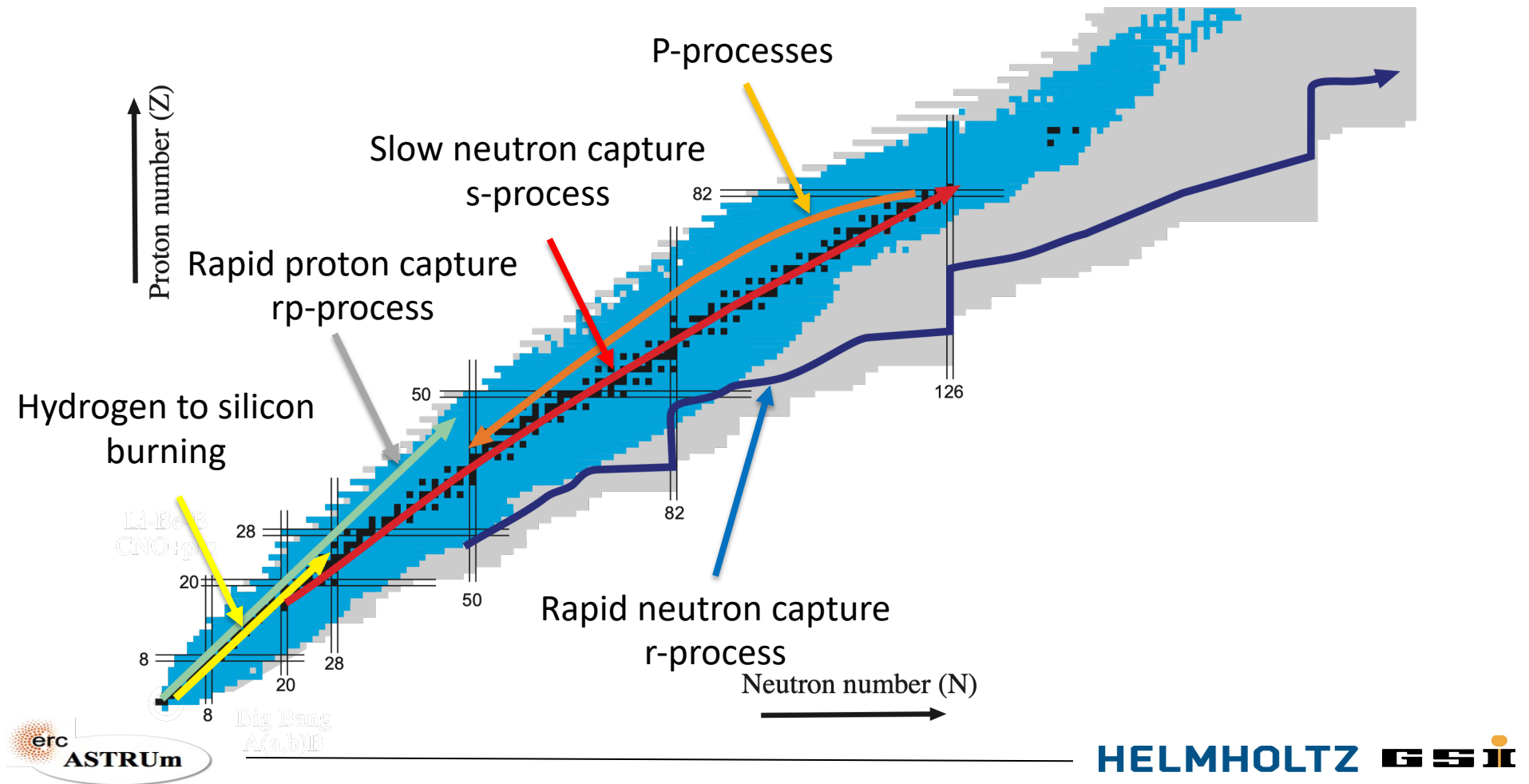


Asymptotic Giant Branch stars

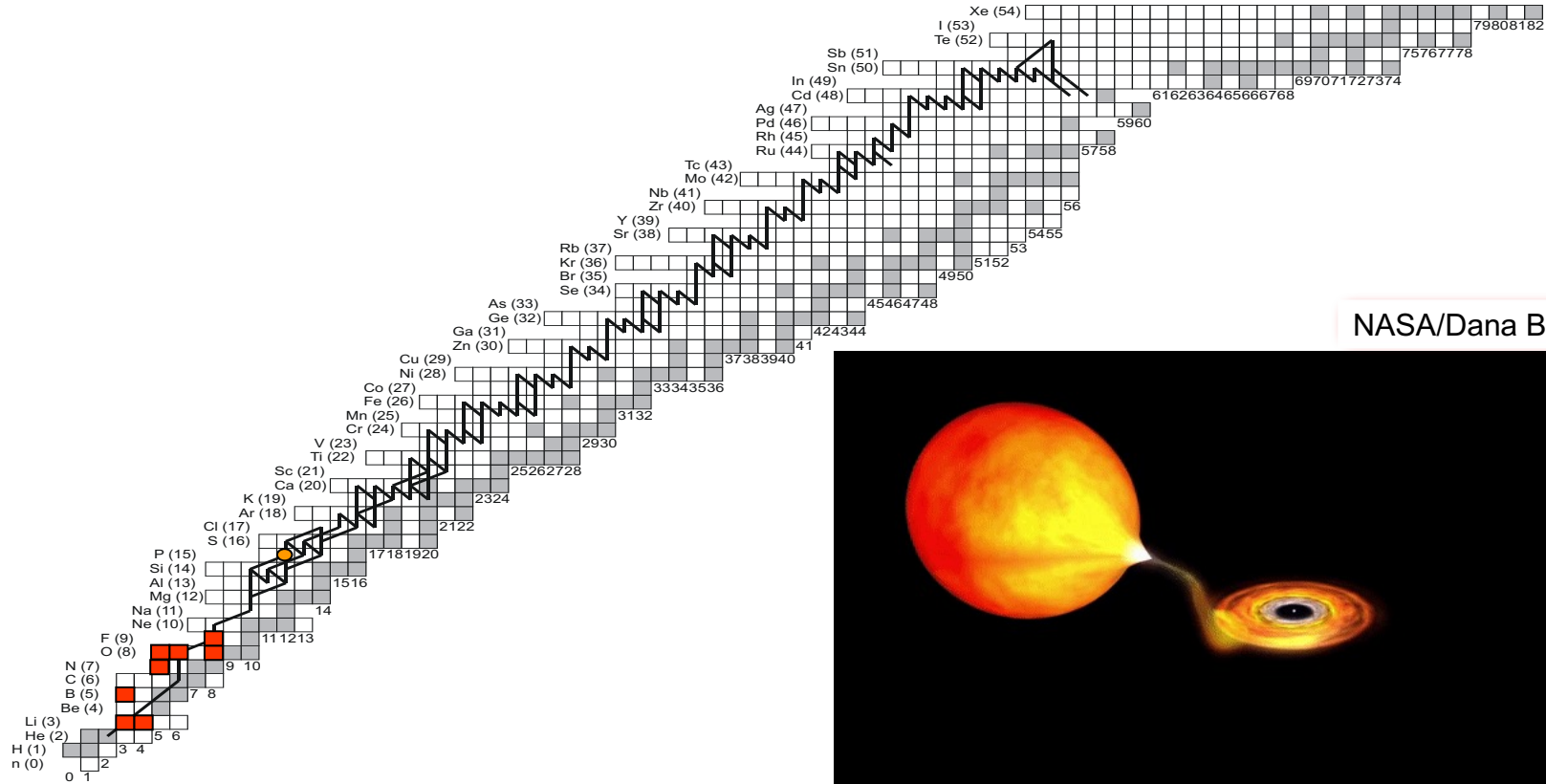


ALMA
(ESO/NAOJ/NRAO)
Hyosun Kim et al.

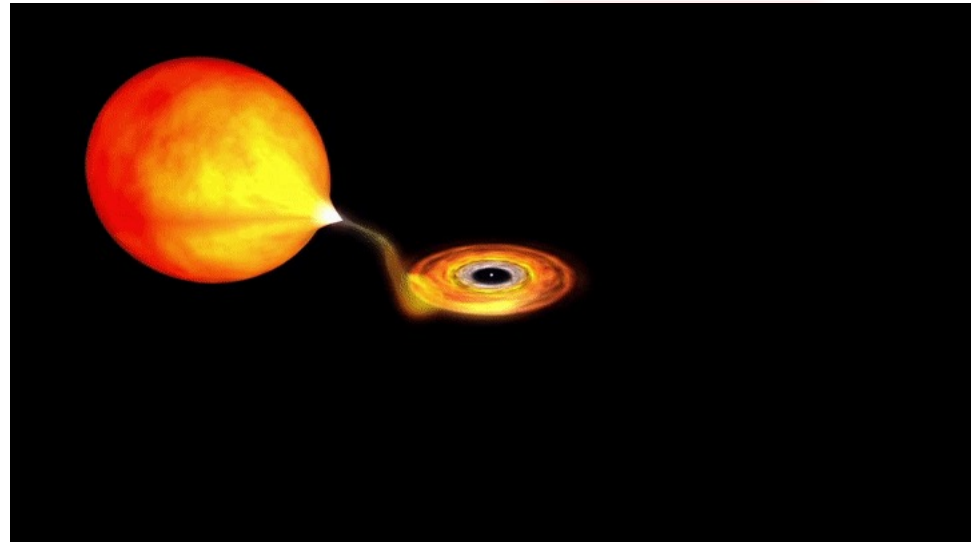
Nucleosynthesis Processes



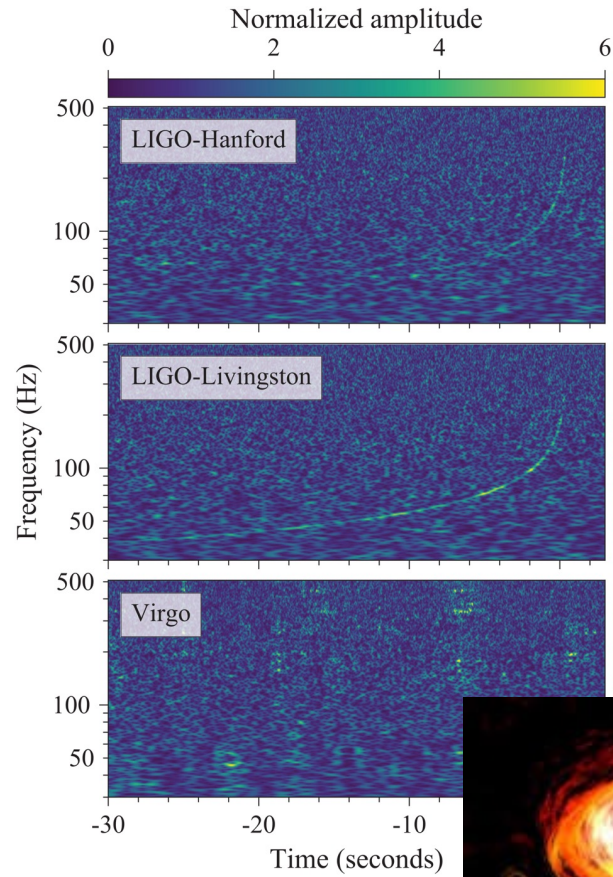
Rapid-proton capture process (rp-process)



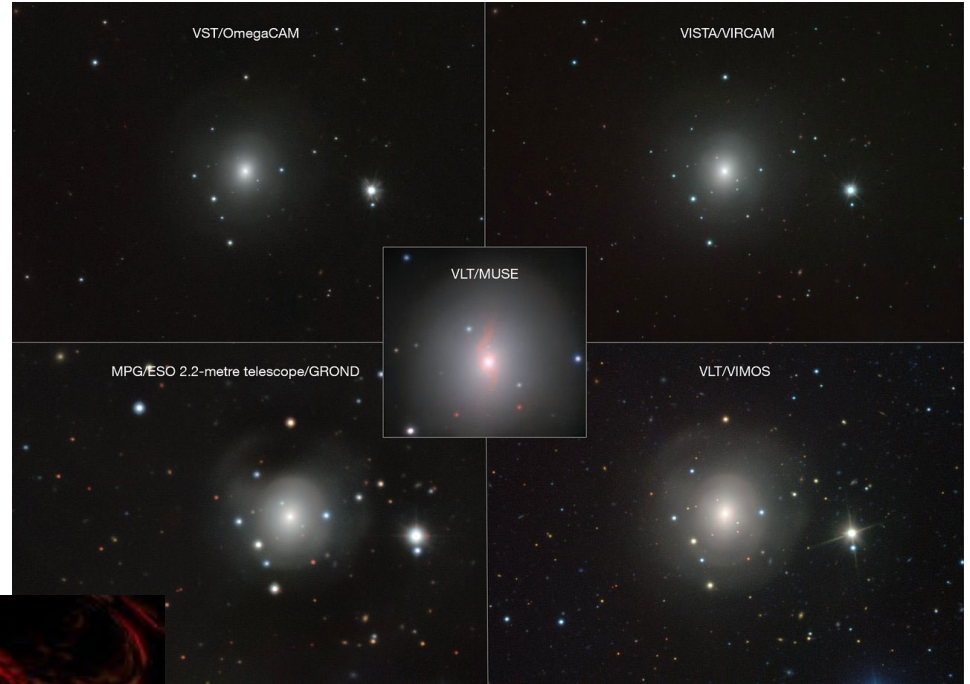
NASA/Dana Berry



Multi-Messenger Astronomy

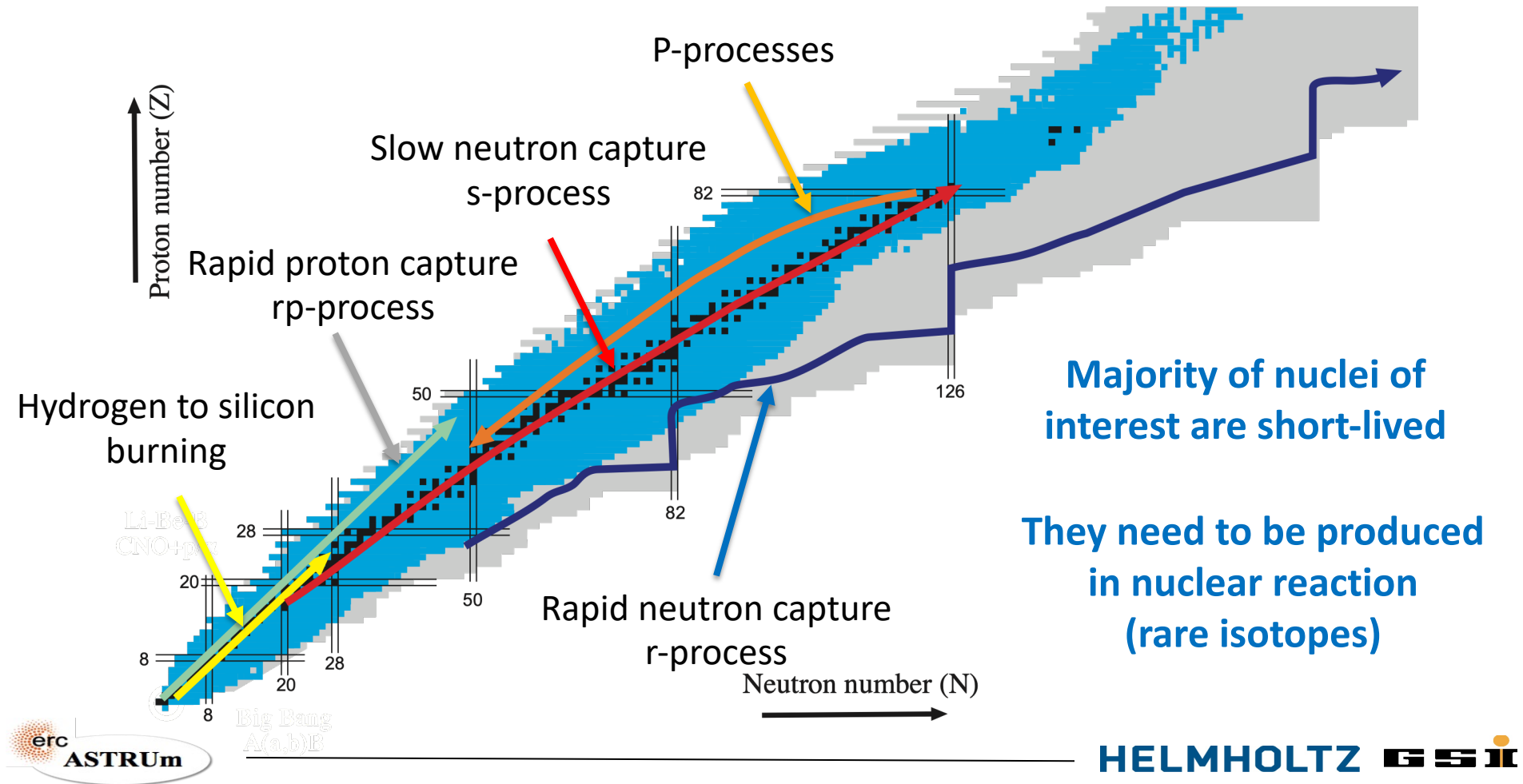


GW170817

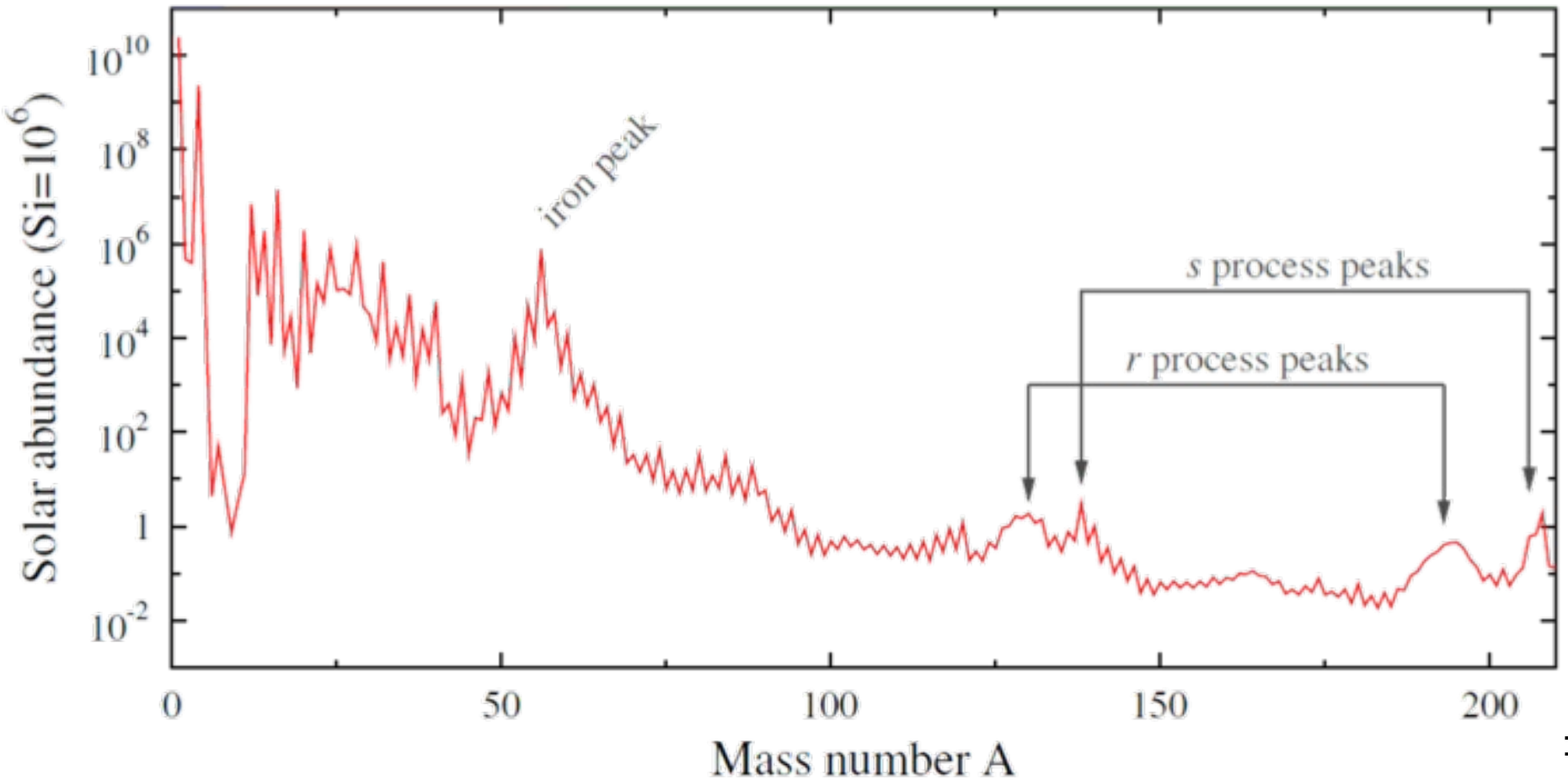


More than 50 other instruments

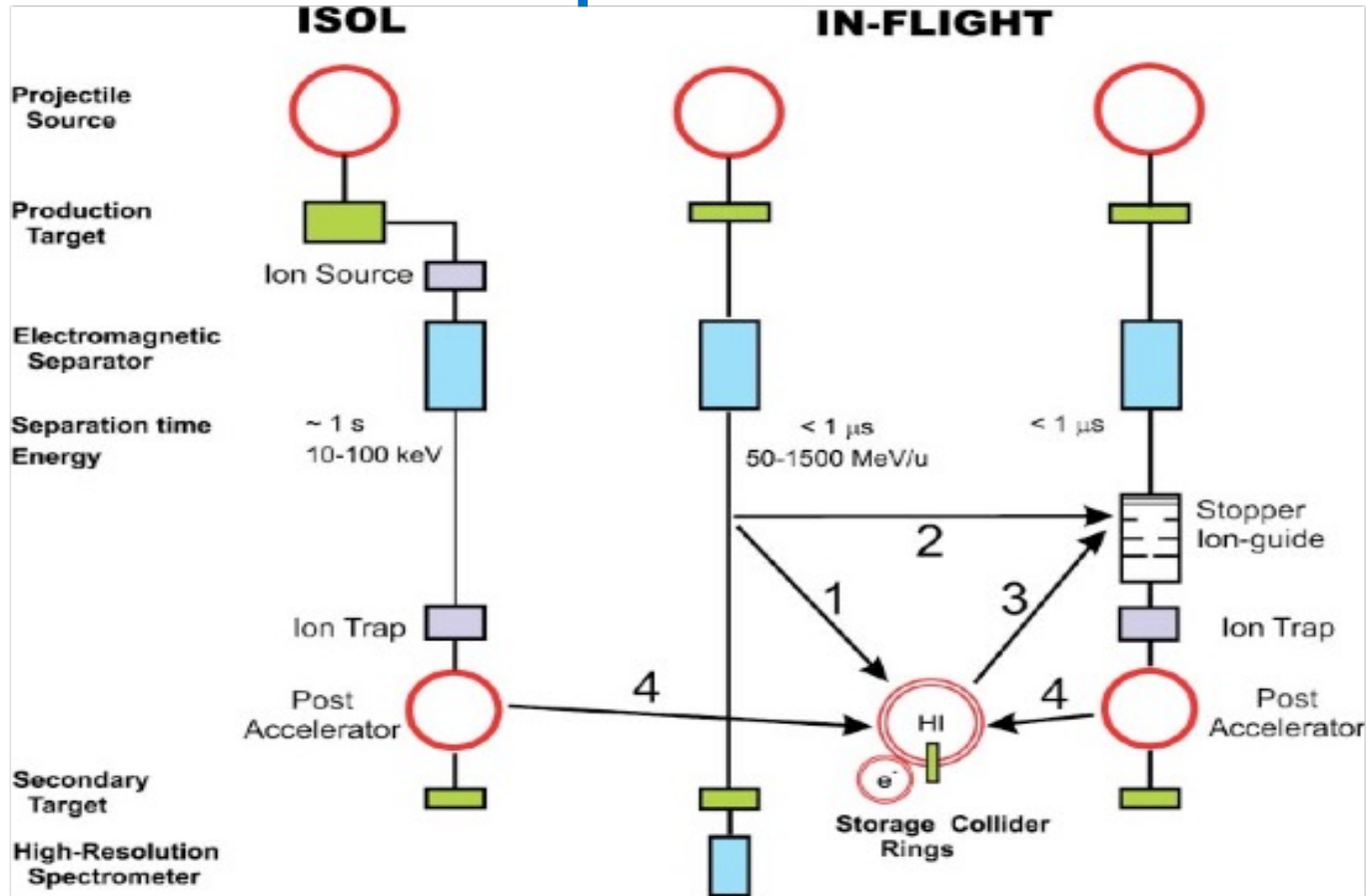
Nucleosynthesis Processes



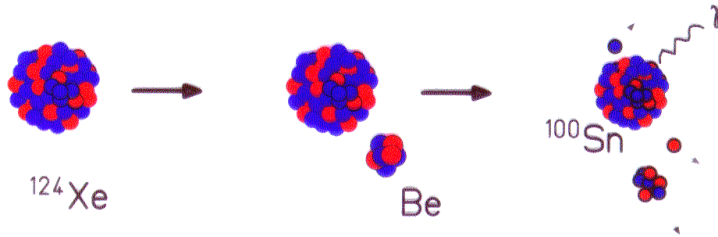
Solar Element Abundances



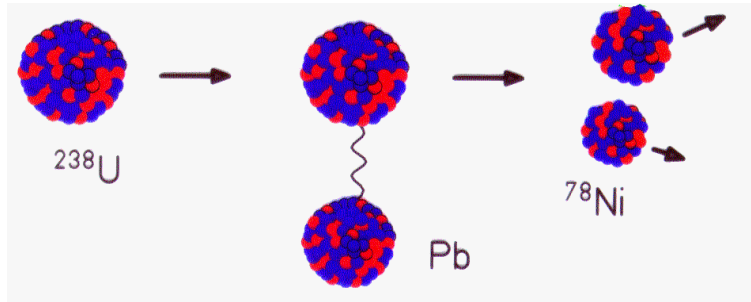
Production and separation of exotic nuclei



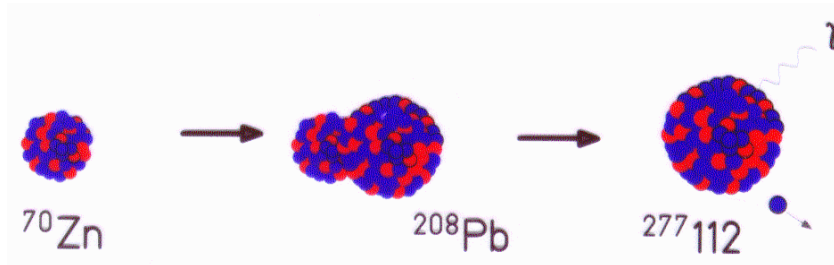
Heavy-Ion Induced Reactions



Fragmentation

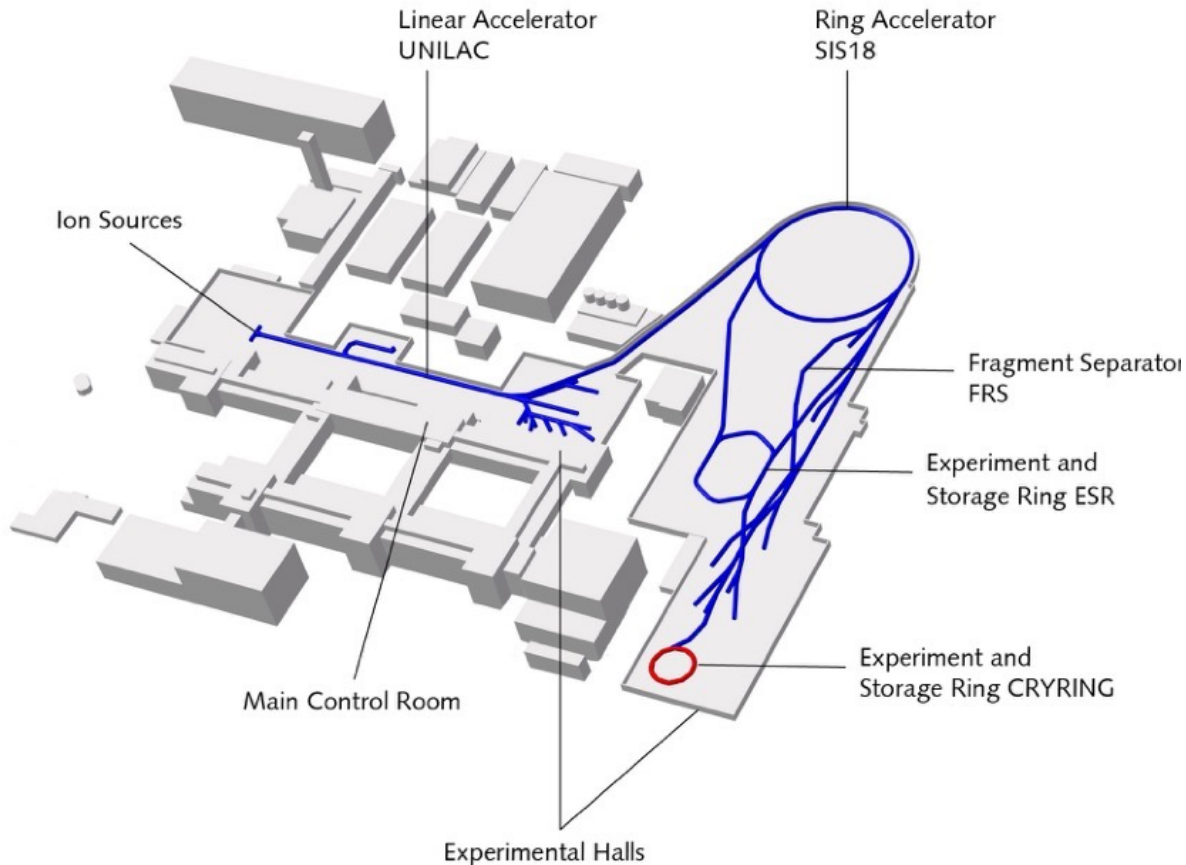


Coulomb dissociation

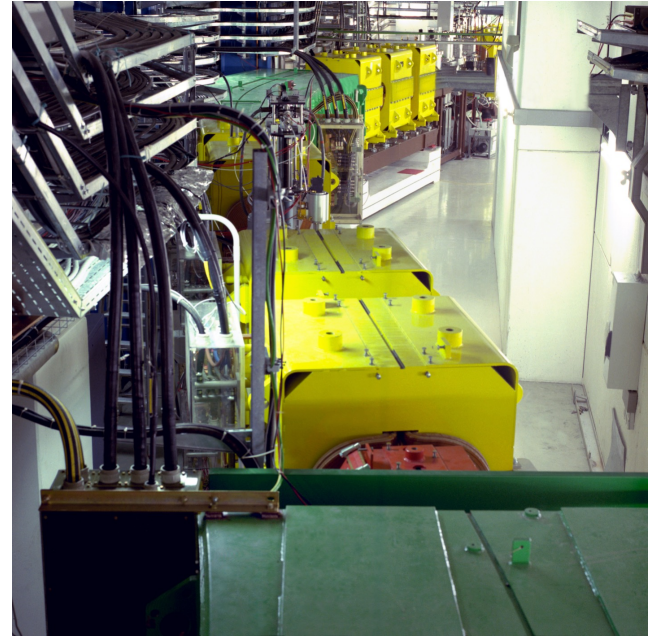


Fusion

Radioactive Ion Beam Facility at GSI



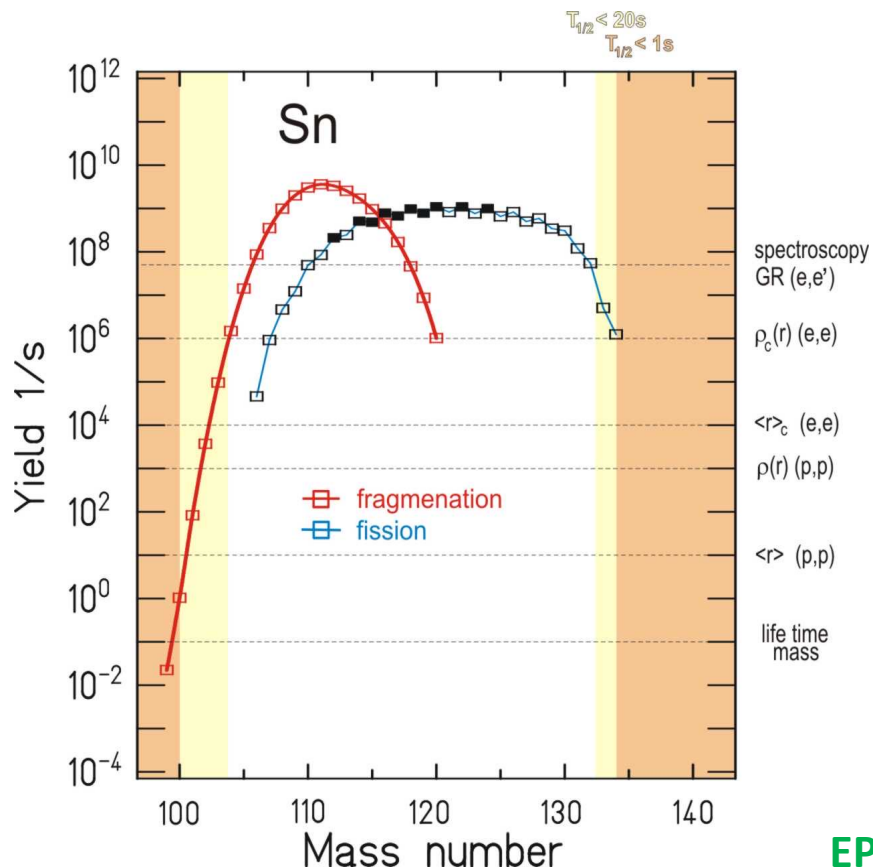
Picture: GSI, Darmstadt



GSI **FAIR**
Phase-0
Research Program

HELMHOLTZ **GSI**

Production Cross-Sections for Tin-Isotopes



nuclides of interest today are

--as a rule--

short-lived

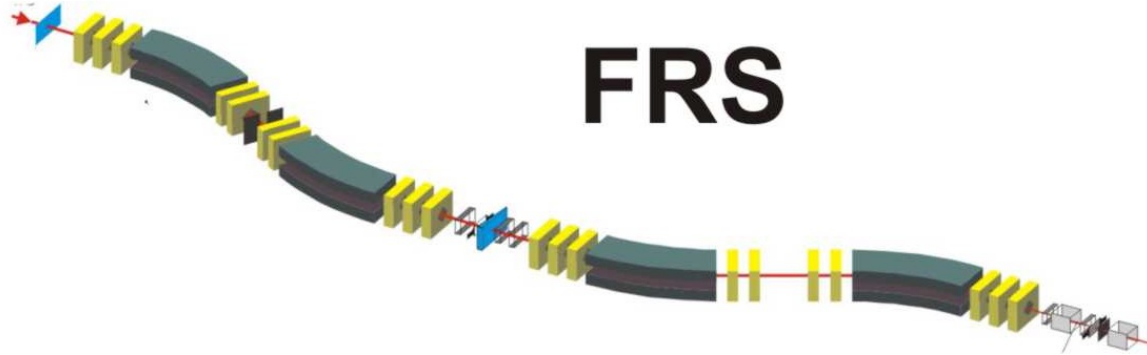
and

have tiny

production cross-sections

EPACS, ABRABLA codes implemented in LISE++

Fragment Separator at GSI



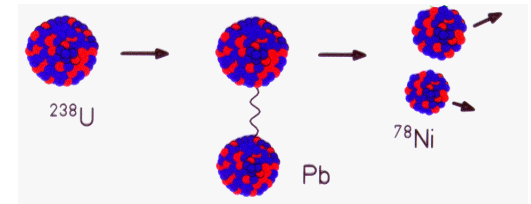
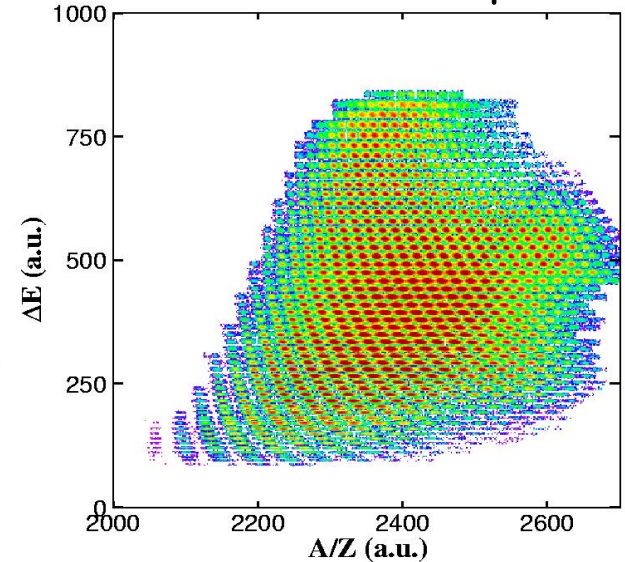
Kinetic energies – hundreds of MeV/u

Tracking provides trajectory – flight path

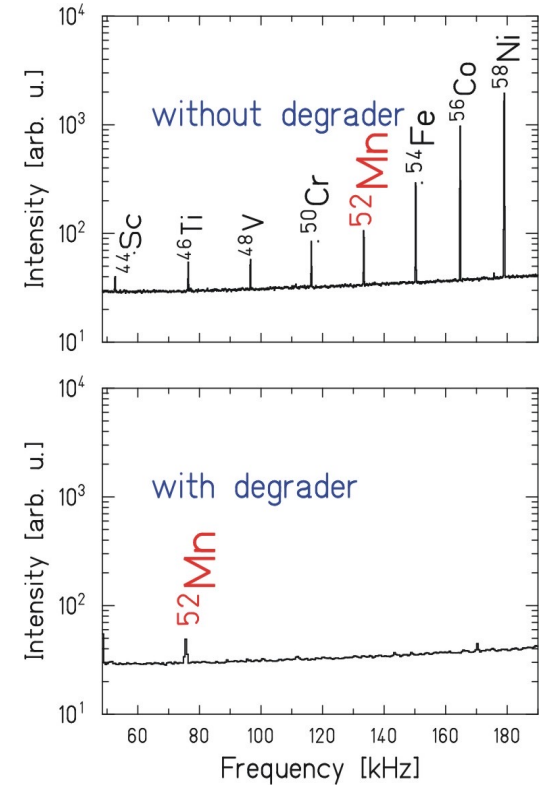
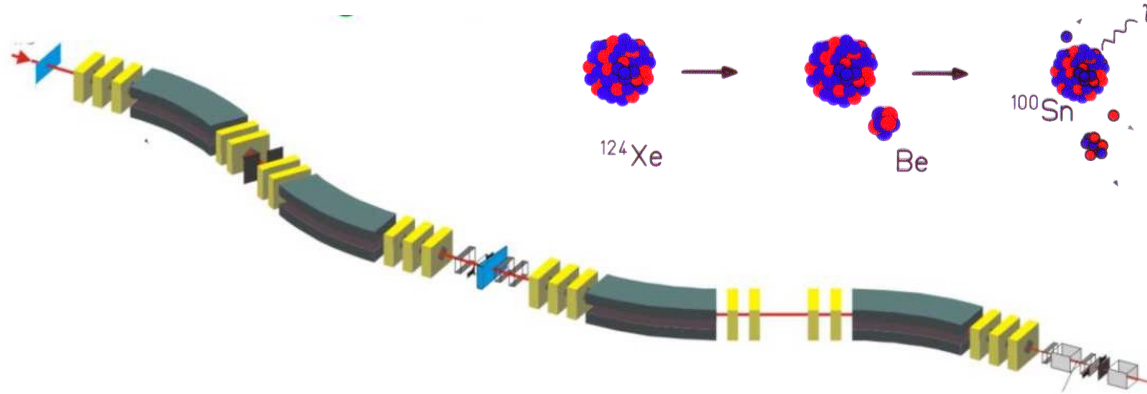
Time-of-flight provides A/Q

Ionization detectors provide Z

About 1000 nuclear species



Fragment Separator at GSI



Tracking provides trajectory – flight path

Time-of-flight provides A/Q

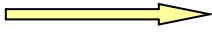
Ionization detectors provide Z

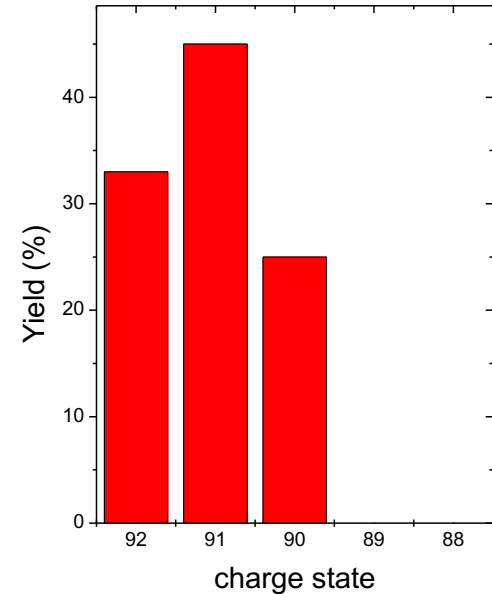
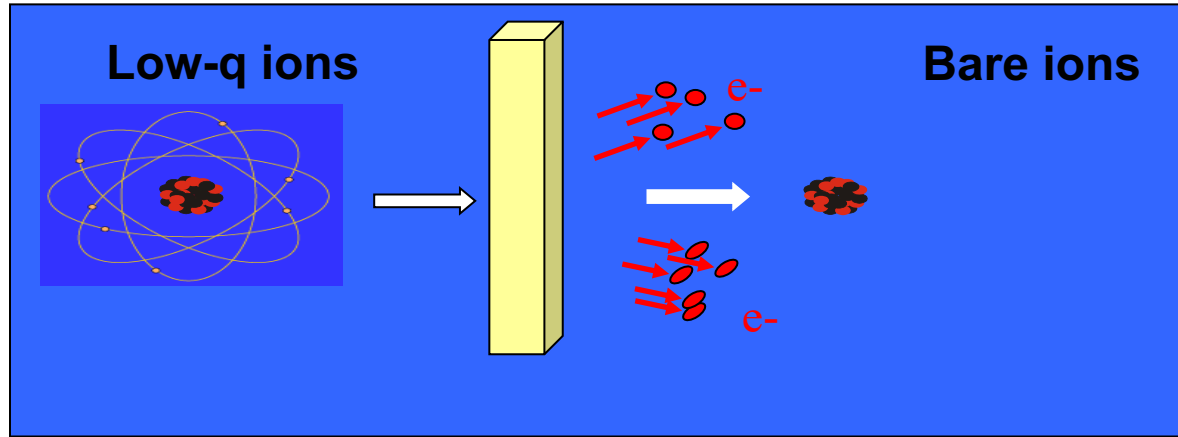
Additional separation criterion – energy loss in specially shaped energy degraders

$$\Delta E \propto Z^2$$

Atomic Charge States at Relativistic Velocities

Bohr criterion: Largest ionization cross section at $v/c \approx v_K/c = \alpha Z$

Uranium $v_K/c \approx 0.67$ $E_{\text{KIN}} \approx 330 \text{ MeV/u}$ 



GLOBAL, CHARGE codes implemented in LISE++

Issue which we have to deal with is velocity!

nuclides of interest today are

--as a rule--

short-lived

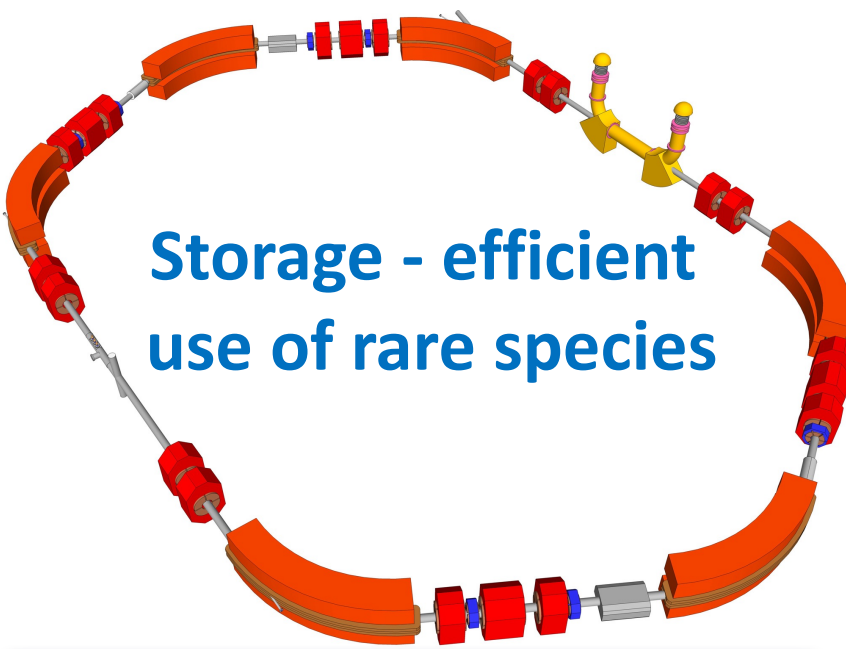
and

have tiny

production cross-sections

Heavy-Ion Storage Rings - Versatile Instruments

Dedicated beam preparation and manipulation techniques



**Storage - efficient
use of rare species**

A huge trap – more than 100 m
circumference, aperture size – 25 cm

**Nuclear reaction inevitably leads to large
momentum spread of the secondary beam**

**Beam cooling - high quality beams
(laser, electrons, stochastic)**

**Small production rates of secondary beams
Accumulation techniques**

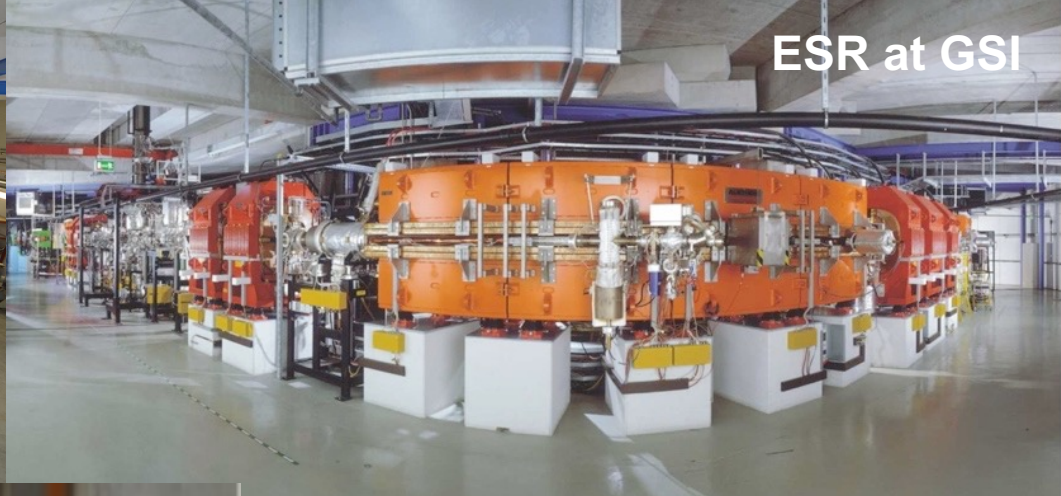
**Nuclear reaction at high energy, whereas
astrophysical reactions are at low energies**

**Adjustment of kinetic energy
(acceleration or deceleration)**

CRYRING at GSI



ESR at GSI



R3 at RIKEN



CSRe at IMP

Photos: M. Lestinsky, A. Zschau, GSI; IMP Lanzhou; RIKEN

CRYRING at GSI



ESR at GSI



- Single-particle sensitivity
- High revolution frequencies
- Broad-band measurements
- High atomic charge states
- High resolving power

R3 at RIKEN



CSR实验环闭环

CSRe at IMP

Charged Particle Motion in Magnetic Field



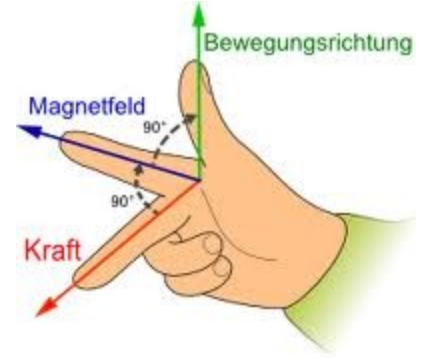
Centripetal Force

$$F_c = \frac{m \cdot v^2}{r}$$

$$F_L = q \cdot v \cdot B$$

$$\frac{m \cdot v}{q} = B \cdot r$$

Velocity!!!



Lorentz Force

r - Radius
 q - Charge
 v - Velocity
 m - Mass
 B - Magnetic induction

Storage ring vocabulary

Reference orbit
Sollbahn ?

A trajectory in the machine of a **reference particle**, that is particle with

$$x = y = s = 0$$

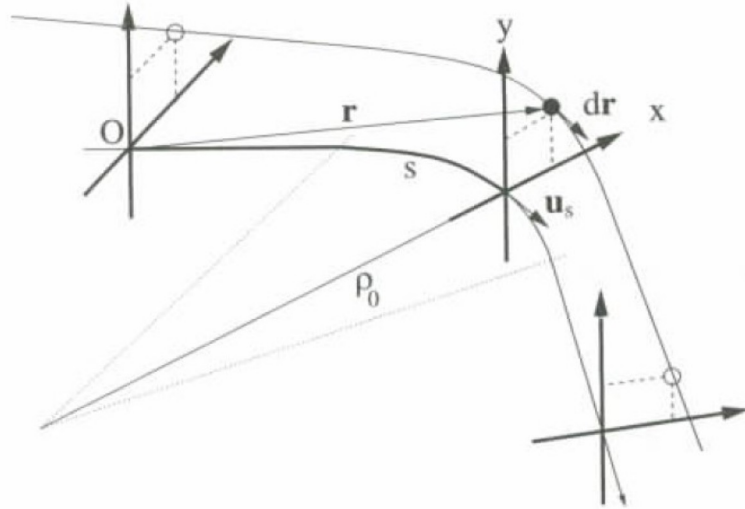


Abb. 4.1. Standardkoordinatensystem (x, y, s)

Curvilinear coordinate system

s – reference orbit / sollbahn

Trajectories of all other particles are treated relative to the reference particle

$$\delta x, \delta p_x, \delta y, \delta p_y, \delta s, \delta p_s$$

Since all deviations are small, momentum can be expressed as angle

$$p_x = x', \delta p_x = \delta x', p_y = y', \delta p_y = \delta y'$$

Storage ring vocabulary

lattice ?

To store ions, a set of magnetic elements such as dipoles, quadrupoles ... is needed which form the **lattice of the ring**



Storage ring vocabulary

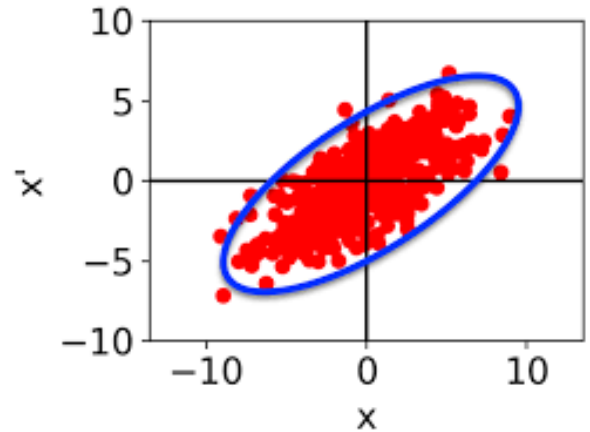
emittance ?

Storage rings have a limited acceptance which can be expressed in terms of the beam **emittance** ϵ and **momentum spread** Δp

$$\epsilon = \pi \cdot \delta x \cdot \delta p = \pi \cdot \delta x \cdot \delta x'$$

6.2 Hill's equations (linear approximation)

$$\left[\begin{array}{l} \frac{d^2 x}{ds^2} + K_x(s)x = \frac{1}{\rho_0(s)} \frac{\Delta p}{p_0} \\ \frac{d^2 y}{ds^2} + K_y(s)y = 0 \end{array} \right] \quad (*)$$



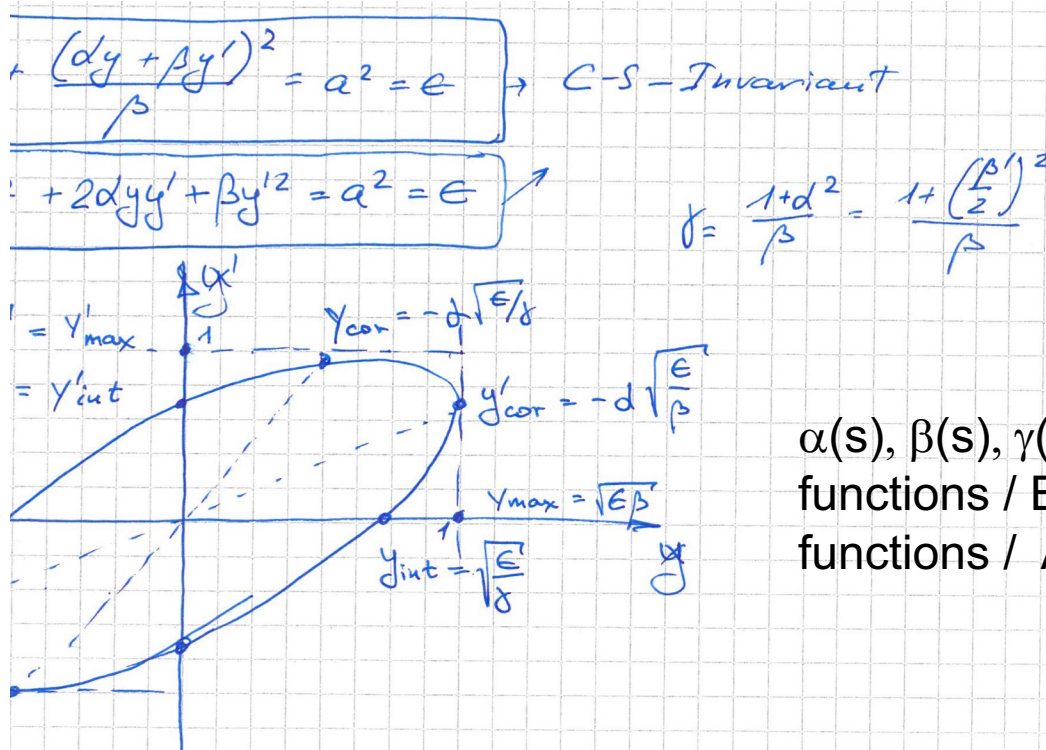
ρ_0 – bending radius of the reference orbit

$K_x(s)$ and $K_y(s)$ are focusing functions which are tabulated for dipoles, quadrupoles etc

Storage ring vocabulary

Courant-Snyder
Invariant?

Liouville's law states that **emittance is strictly conserved** under the action of conservative forces.

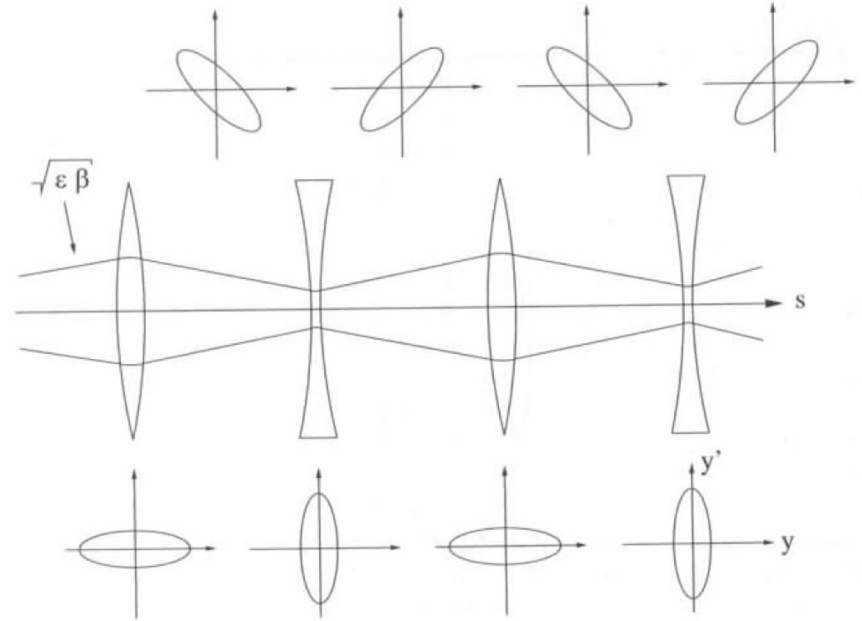
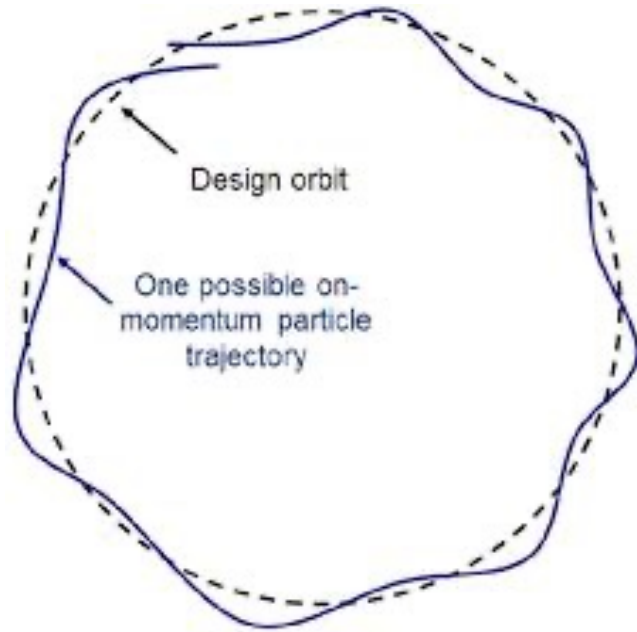


$\alpha(s)$, $\beta(s)$, $\gamma(s)$ – Twiss functions/ Optical functions / Betatron functions / Lattice functions / Amplitude functions

Storage ring vocabulary

Betatron
oscillations
and tune ?

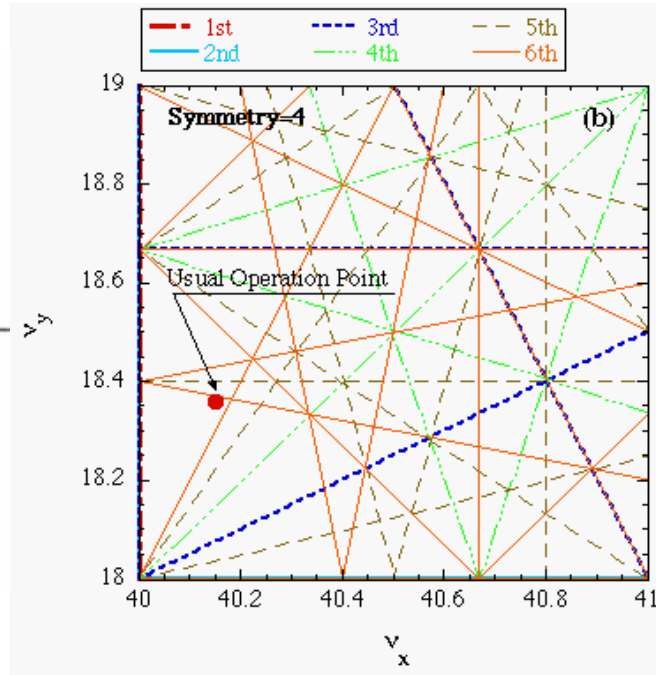
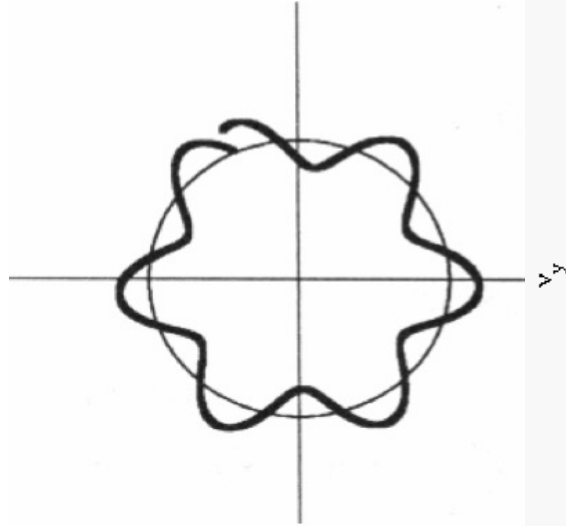
The ions move on periodic orbits around the ideal trajectory 's'
("Sollbahn"), performing **betatron oscillations**. The number of
betatron oscillations per revolution is the **tune Q**.



Storage ring vocabulary

resonance?

Due to imperfections of magnetic fields, misalignments etc., the particles should move on not-repeating trajectories. This implies, that tunes are highly irregular numbers. Tunes like $Q=N$, $N/2$, $N/3$, $N/4$... - cause resonances leading to beam loss.



Tuning does not demand a study of “tunology”, but rather the right feeling and the experience of decades

To save the beam, avoid any crossing of lines

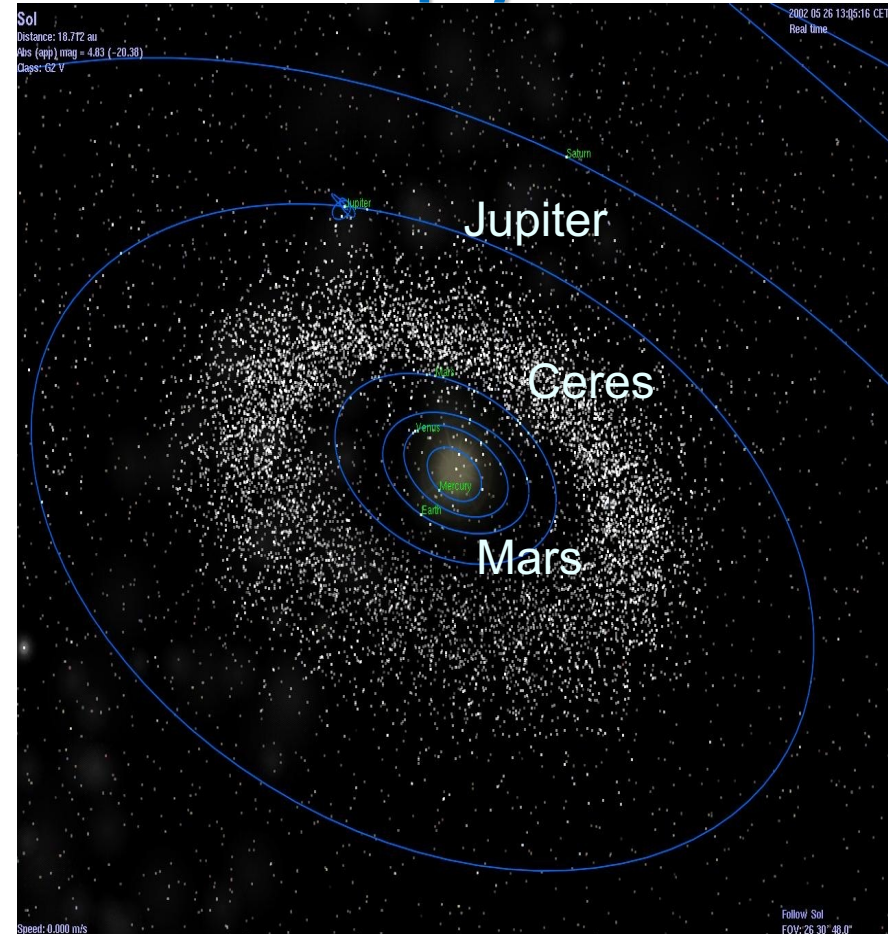
How to do so, if the ions get acc(de)celerated ??

Lost planet or lost beam – all the same physics

Orbit of a former planet Ceres was periodically influenced by Jupiter

3rd Kepler's law: $T^2/a^3 = \text{const.}$

$1 \text{ AU} = 1.5 \cdot 10^8 \text{ km},$	$T_E = 1 \text{ y}$
$a_M = 1.52, a_J = 5.20,$	$R_{MJ} = 0.29$
$a_C = 2.77, \quad "$	$R_{CJ} = 0.53$



Storage ring vocabulary

Synchrotron
principle and
slip factor?

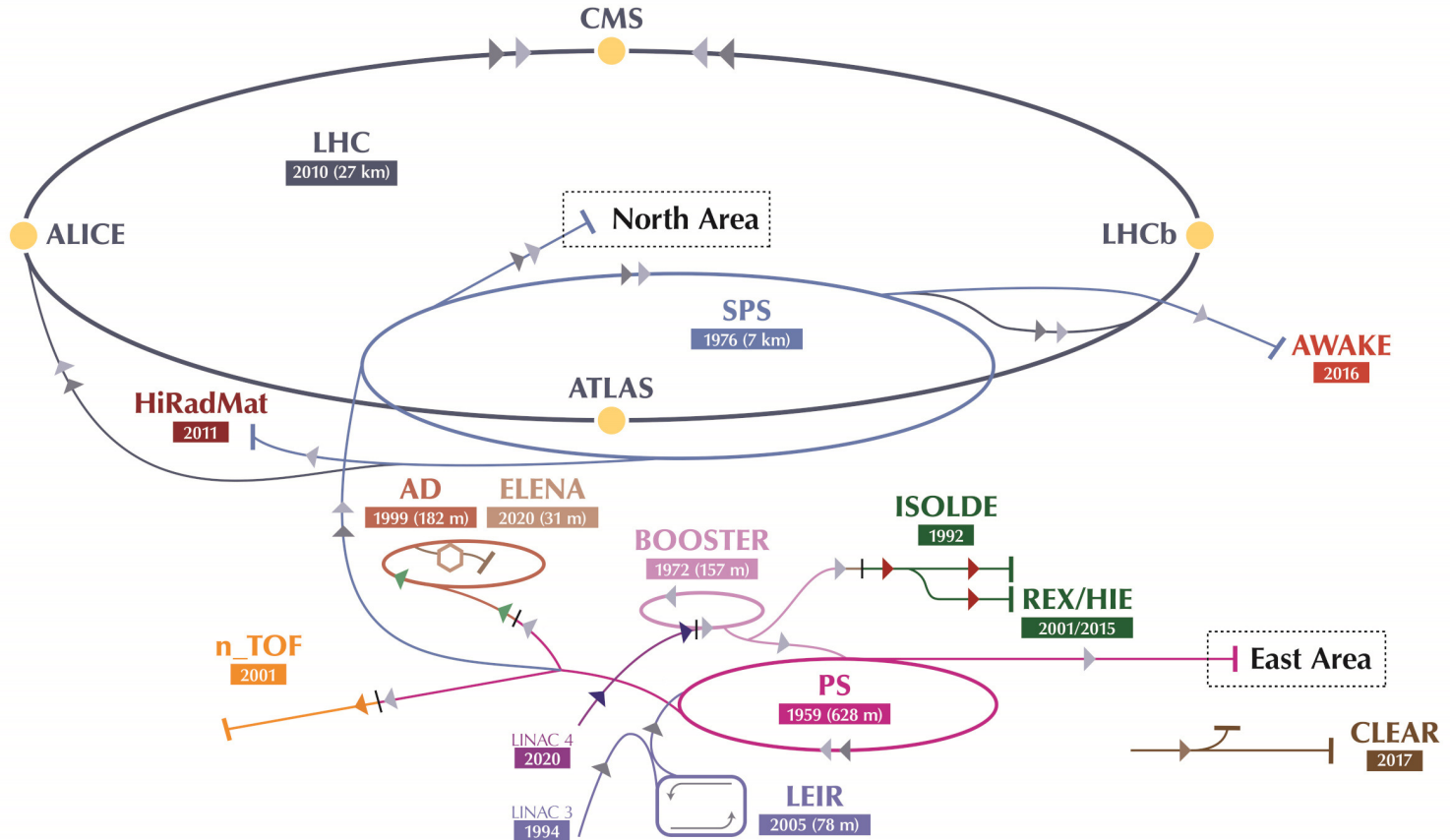
Acceleration/deceleration is only possible if a **change in momentum** transfers into a **change of frequency**.
(Synchronisation)

$$\frac{\Delta \omega}{\omega} = \eta \frac{\Delta p}{p} = \left(\frac{1}{\beta^2} - \frac{1}{\beta_{tr}^2} \right) \frac{\Delta p}{p}$$

↑
dispersion of
particle frequencies

$$\alpha_p = \frac{1}{\beta_{tr}^2} \quad - \text{momentum compaction factor}$$

CERN Facility

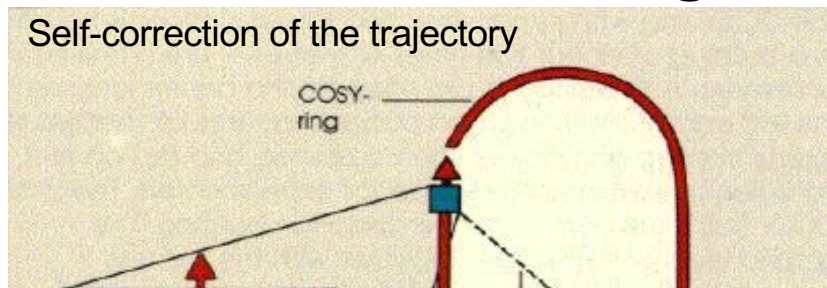


Cooling techniques applied at ion rings

- Lasers = transfer of momentum
- Electrons = mixing of temperatures
- Stochastic = self-correction

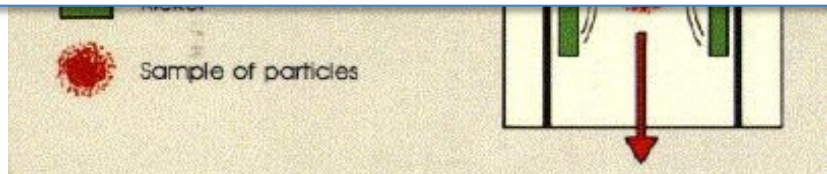


Stochastic Cooling of Secondary Beams



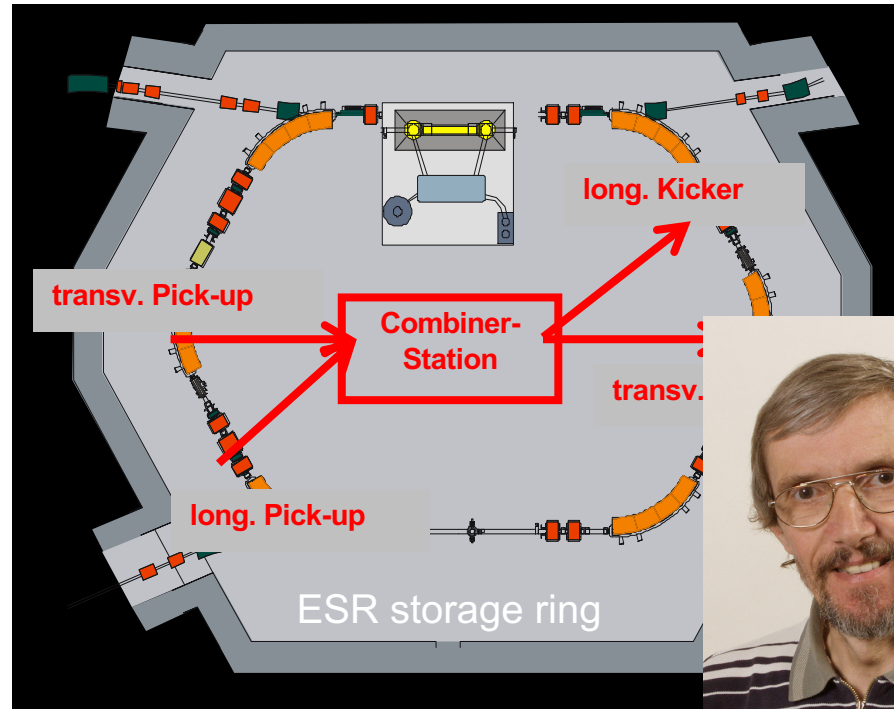
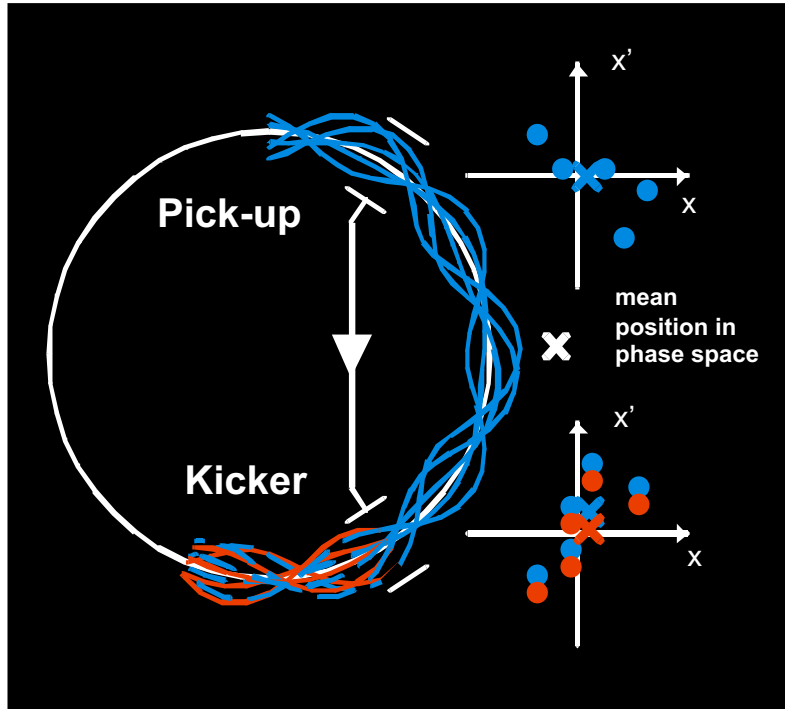
Simon van der Meer
1925 - 2011

Why do you need to send the signal to the opposite side of the ring? Why cannot one simply wait until the beam comes back after full revolution?



Nobel prize 1984: S. van der Meer and C. Rubbia

Stochastic cooling (self-correction of trajectory)

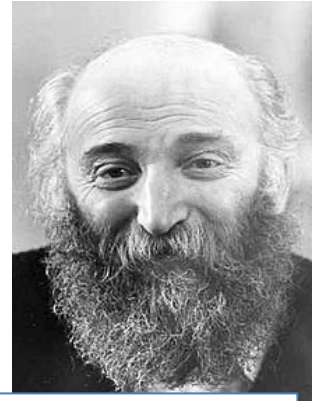
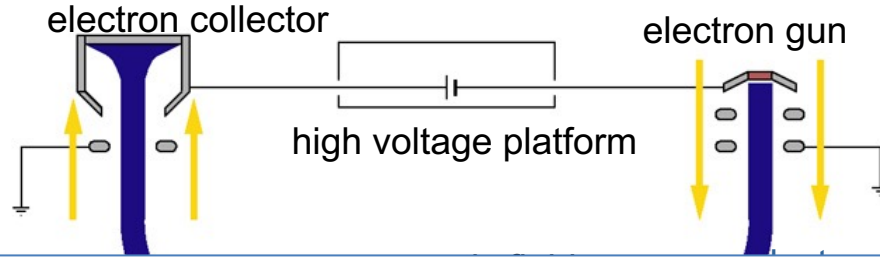


Stochastic cooling is in particular efficient for hot ion beams

Cooling time τ scales as $N_{\text{ion}} / \text{bandwidth}$

Fritz Nolden 2023⁺

Electron Cooling of Secondary Beams



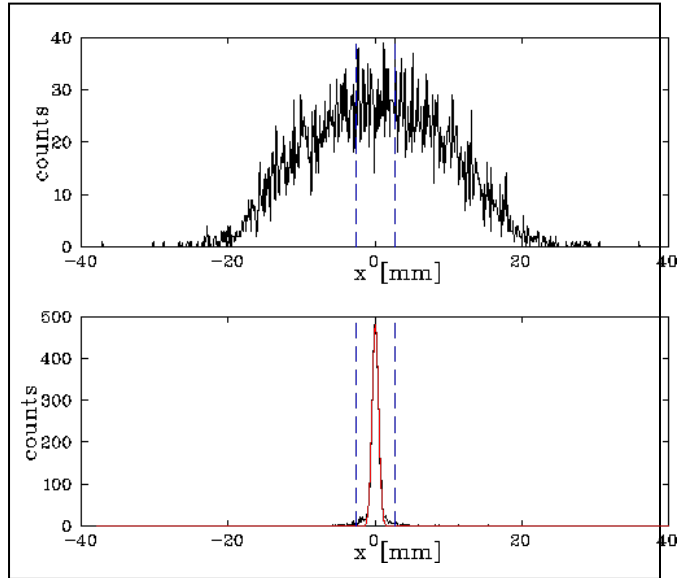
The cross-section for recombination of electrons with highly-charged ions diverges at zero relative velocity. Why stored ions do simply not recombine and get lost from the ring?

Electron cooling (Coulomb cooling)

Cooling by electrons can be treated in analogy to **energy loss** of ions in matter

$$\frac{dE}{dx} \propto \rho \frac{Z^2}{m_e v^2}$$

What acts against cooling ?



- a) ***Intra beam scattering***
Ion-ion scattering
- b) ***Collisions*** (scattering) of ions with the ***residual gas atoms***
- c) ***Charge exchange losses*** of the ions in collisions with the residual gas atoms or cooler electrons
- d) ***Space charge limit***

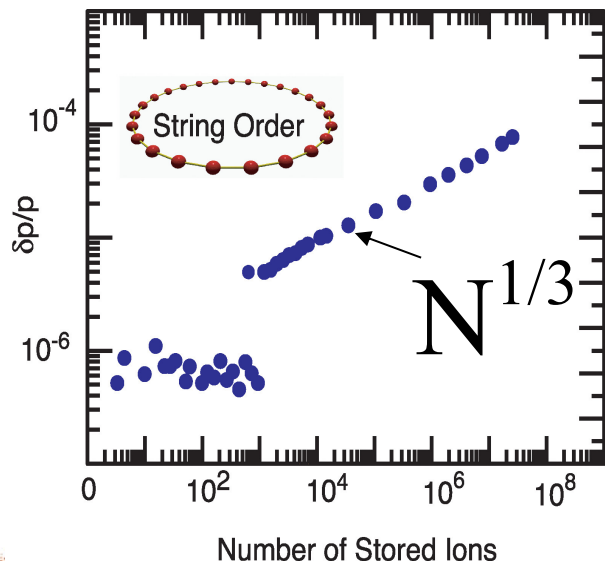
All processes (a - d) scale with Z^2 of the ion

Electron cooling (phase transition)

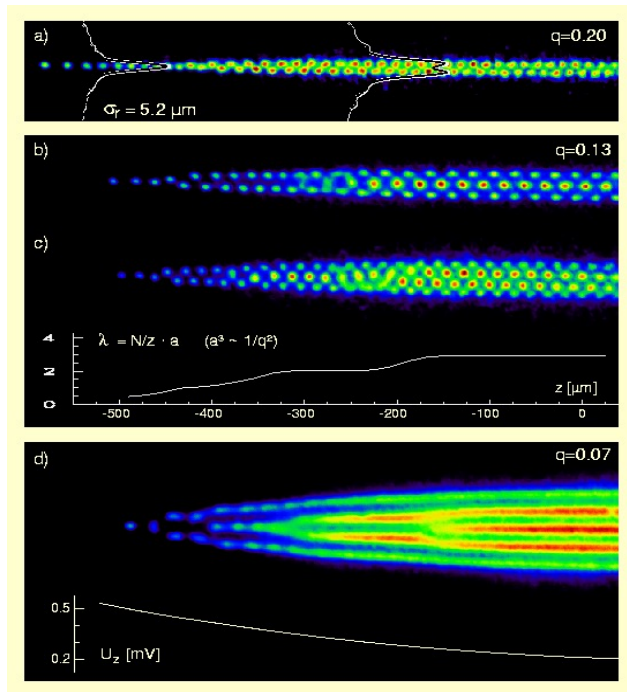
ESR: circumference $\approx 10^4$ cm

For 1000 stored ions, the mean distance amounts to about 10 cm

At mean distances of about 10 cm and larger intra-beam-scattering disappeared



Coulomb
crystals
in PALLAS
ring



T. Schätz, Nature **412** (2001) 442