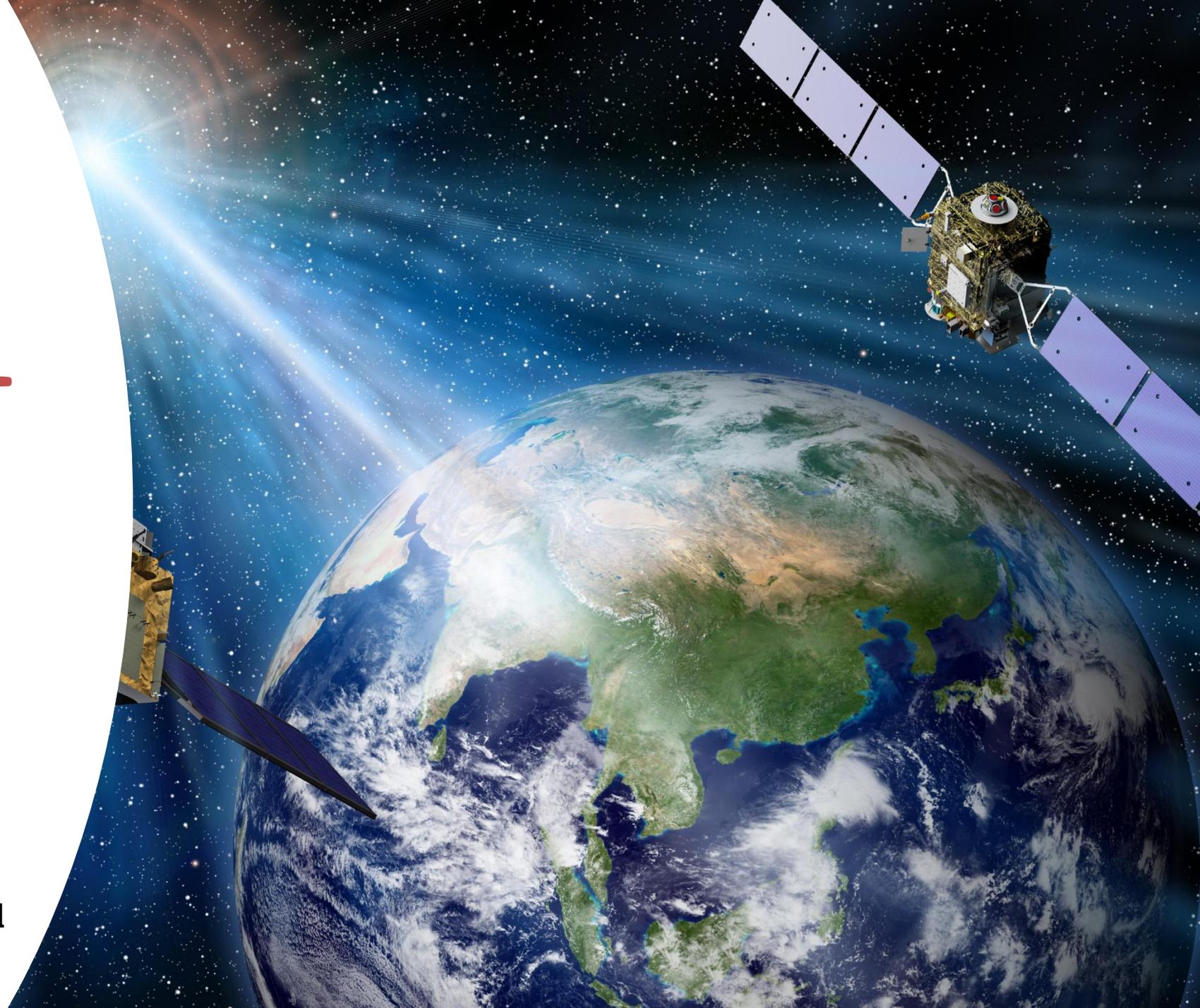


Testing in-vacuo dispersion with GRB neutrinos

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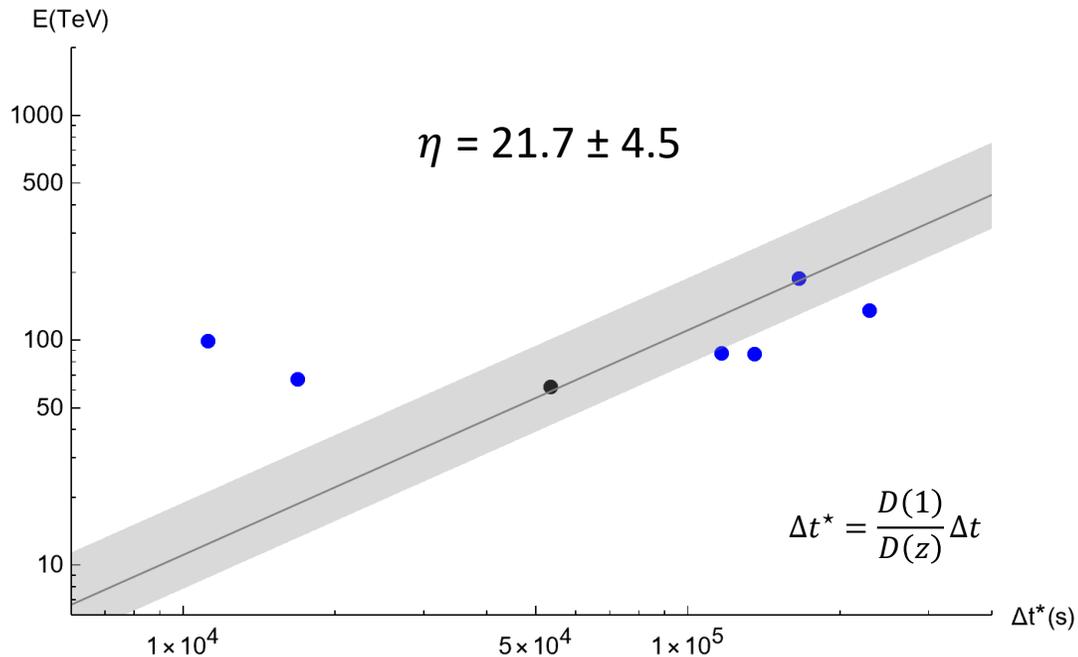


INTRODUCTION

- Theoretical models commonly predict neutrino emission from GRBs, yet after ~ 15 years IceCube (IC) has reported not a single GRB neutrino:
- an intriguing explanation is that in principle our failure to observe GRB neutrinos could be attributed to some quantum properties of spacetime (in-vacuo dispersion):

- $$\Delta t = \eta \frac{E}{M_{Pl}} D(z), \quad \text{where} \quad D(z) = \int_0^z dx \frac{1+x}{H_0 \sqrt{\Omega_\Lambda + (1+x)^3 \Omega_M}}$$

INTRODUCTION (2)



*Amelino-Camelia et al., Nat. Astro (2017),
Amelino-Camelia et al., Nat. Astro (2023)*

- HESE sample (2010-2014)  it is the least contaminated by atmospheric neutrinos.
- Shower events since track events have very poor energy estimates.
- GRBs of known and unknown redshift, roughly estimating the redshift when this is unknown.



IC NEUTRINOS and GRBs OF KNOWN REDSHIFT

- HESE sample (2010-2022).
- We restricted to shower events.
- We restricted to GRBs of known redshift instead of making assumptions to roughly estimate the redshifts as in previous works [*Amelino-Camelia et al., Nat. Astro (2017), Amelino-Camelia et al., Nat. Astro (2023)*].

*Amelino-Camelia, D'Amico, D'Esposito, Fabiano, **DF**, Gubitosi, Guetta, Moia, Rosati, arXiv:2501.13840*



GRB-NEUTRINO CANDIDATES

TEMPORAL COMPATIBILITY

- We take the result of [Amelino-Camelia et al., *Nat. Astro* (2023)], $\eta = 21.7 \pm 4.5$, as a starting point for our analysis:
- any GRB and neutrino times of arrival are regarded as compatible if they satisfy $\Delta t = \eta \frac{E}{M_{Pl}} D(z)$ for some $\eta \in [12.7, 30.7]$ within two standard deviations in the neutrino energy.

ANGULAR COMPATIBILITY

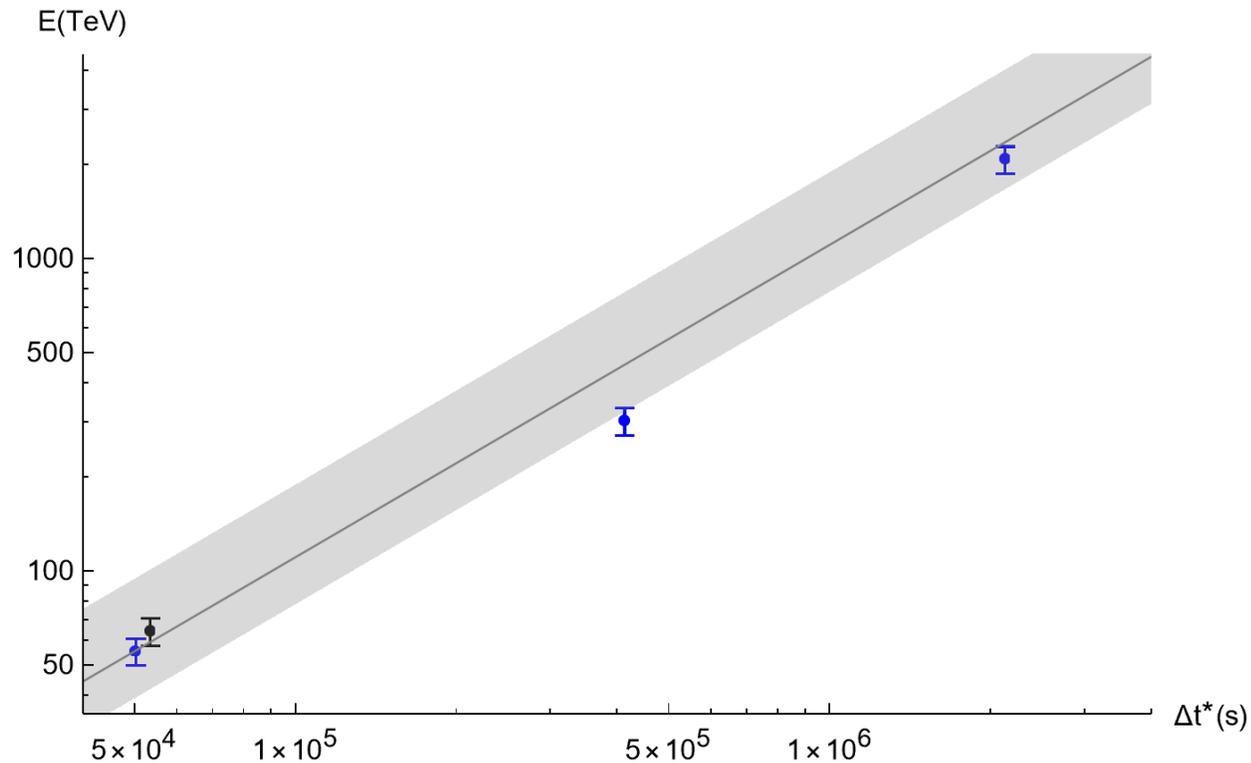
- Neutrino directional information provided by IC in terms of FB8 distributions (not gaussians).
- $S_{dir} = \int P_\nu(\Omega) P_{GRB}(\Omega) d\Omega$, where $P_\nu(\Omega)$ and $P_{GRB}(\Omega)$ are the angular distributions of the neutrino and the GRB.
- The directions of a GRB-neutrino pair as compatible if the corresponding S_{dir} satisfies $S_{dir} \geq S_{dir}^{cut}$



PROPERTIES OF S_{dir}

- S_{dir} can be computed for angular distributions of arbitrary shape.
- Its value increases as the overlap between the two angular distributions increases  it is a good measure of angular compatibility, reflecting how likely it is for two directions to coincide [Abbott et al. *Astrophys. J. Lett.* (2017)] .
- In the main analysis we adopted $S_{dir}^{cut} = \frac{1}{4\pi}$ which is the value taken by S_{dir} whenever one of the distributions is the uniform distribution on the sphere (using simulated data, we checked that this choice for S_{dir}^{cut} entails a 7.8% probability of accidental directional association between a neutrino and a GRB).

MAIN ANALYSIS



- 4 GRB-neutrino candidates with correlation r between Δt^* and E
 $r = 0.9985$
- FAP of finding at least 4 GRB-neutrino candidates with correlation greater than 0.9985 is $P_r = 0.6\%$ (2.8σ).



THE NEUTRINO EVENT KM3-230213A

- Track event observed by ARCA on 13 February 2023 at 01:16:47 UTC
- Median energy 220 PeV; 110–790 PeV at 68% confidence; 72 PeV–2.6 EeV at 90% confidence
- J2000 coordinates of 230213A are RA = 94.3° , decl = -7.8° with containment radius $R(68\%) = 1.5^\circ$

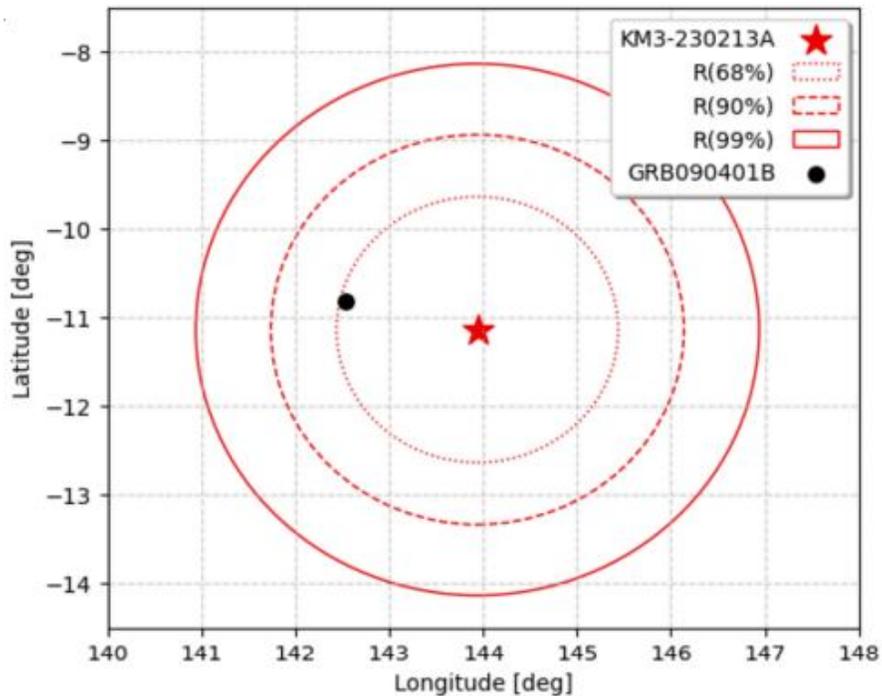
S. Aiello et al. [KM3NeT], Nature 638 (2025)



POSSIBLE ASTROPHYSICAL SOURCES

- Bounds set by IC on the flux of cosmogenic neutrinos  a cosmogenic origin for 230213A is regarded as very unlikely; [*S. Aiello et al. [KM3NeT], Nature 638 (2025)*; *S. W. Li et al. (2025), arXiv:2502.04508*]
- Blazars are not expected to have enough fire power for the observation of such a high-energy neutrino; [*O. Adriani et al. (2025), arXiv:2502.08484*]
- A GRB origin for 230213A would make observational and theoretical sense [*A. Neronov et al. (2025), arXiv:2502.12986*]:
 1. no GRB in good directional and close temporal coincidence with 230213A;
 2. a 220 PeV GRB neutrino could be delayed by several years, even assuming that the QG scale is rather close to the Planck scale  opportunity to test the predictive power of our previous picture.

GRB090401B



*Amelino-Camelia, D'Amico, Fabiano, DF,
Gubitosi, Moia, Rosati, arXiv:2502.13093*

- J2000 coordinates are $RA = 95.088^\circ$, $decl = - 8.972^\circ$ with an angular uncertainty of 0.000065°
- Measured redshift $z = 3.1$
- Long GRB ($T_{90} = 183$ s) observed by Swift on 01 April 2009 at 08:35:25 UTC
- 14-year separation between the two observations !



- unsurprising from an in-vacuo-dispersion standpoint, considering the very high energy of 230213A and the relatively high redshift of 090401B.



S_{dir} and S_E

- S_{dir} to quantify the directional agreement between the GRB and the neutrino;
- New indicator S_E to quantify the agreement between the experimental information on the energy of the neutrino and the range of energies that in-vacuo dispersion would predict for such a delayed neutrino observation assuming it has been emitted at the GRB redshift:

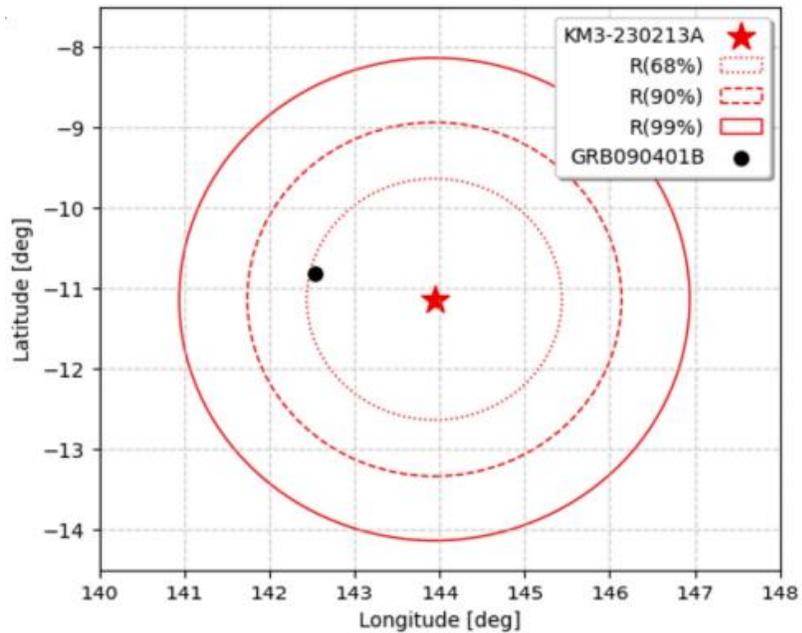
- $$S_E = \int_{E_{min}}^{E_{max}} \frac{\rho_\nu(E)}{E_{max} - E_{min}} dE$$

where:

1. $\rho_\nu(E)$ is the energy distribution of 230213°;
2. Using $\Delta t, z$ we convert the range $\frac{1}{M_{pl}} \cdot [12.7, 30.7]$ into a range $[E_{min}, E_{max}]$ for the inferred energy of 230213°.

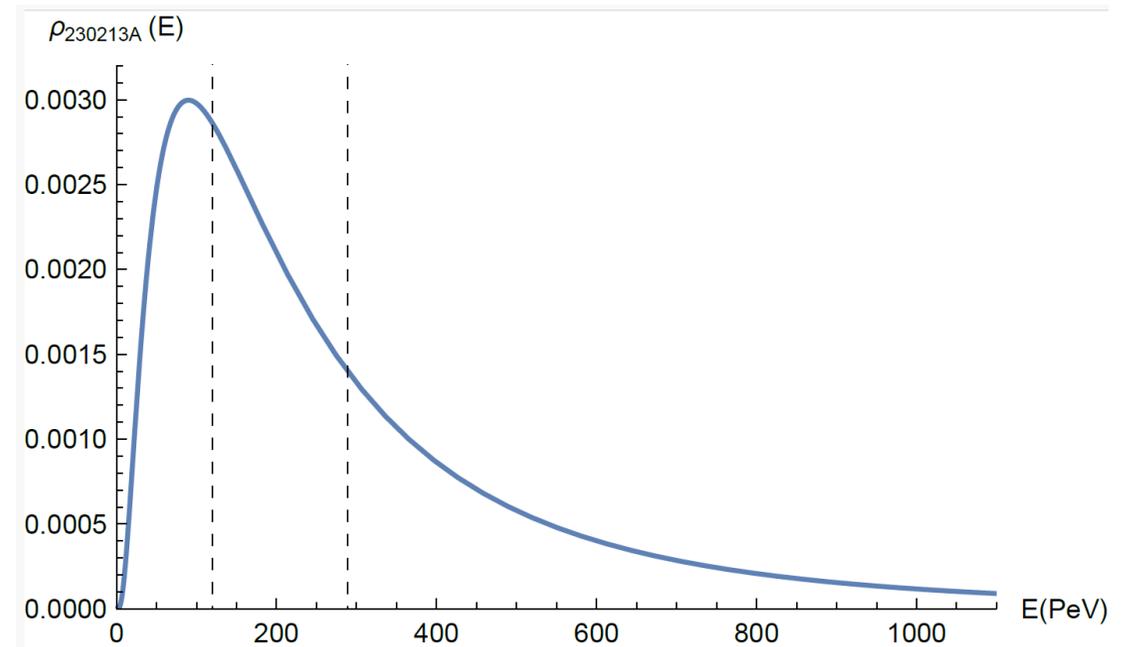
THE 090401B-230213A PAIR

ANGULAR COMPATIBILITY



$$S_{dir} = 194$$

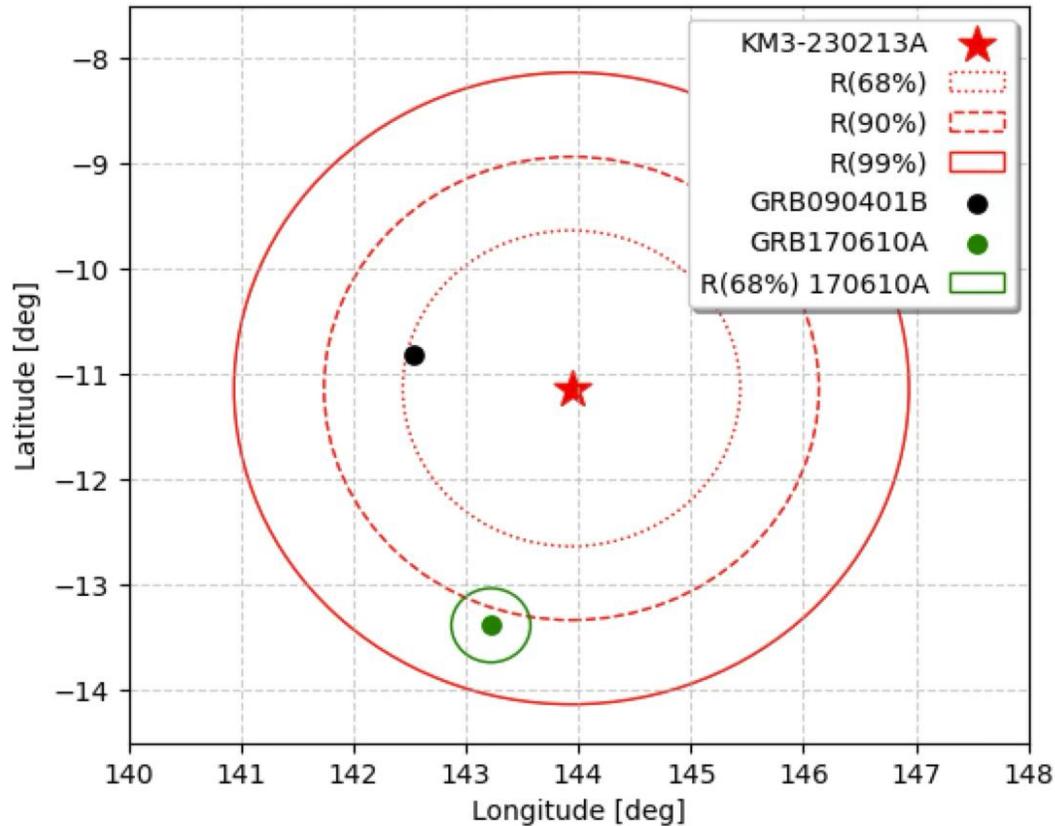
TEMPORAL (ENERGY) COMPATIBILITY



$$S_E = 0.00209 \text{ PeV}^{-1}$$

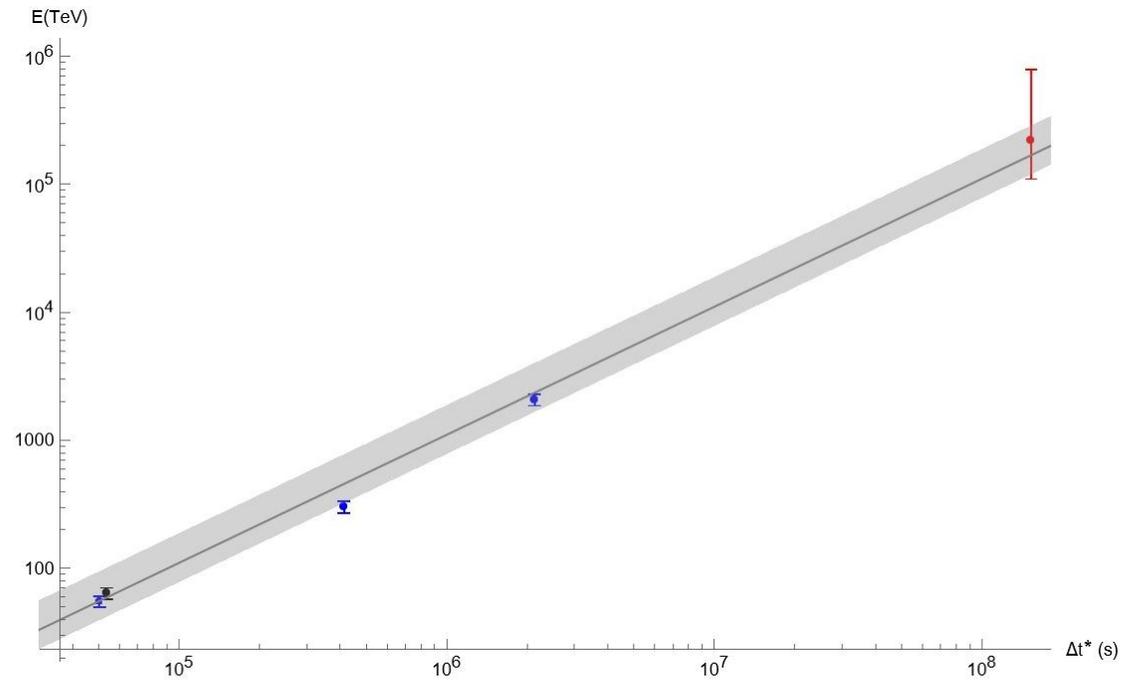
- FAP of finding a GRB that produces $S_{dir} \geq 194$ and $S_E \geq 0.00209 \text{ PeV}^{-1}$, $p = 1.5\%$ (2.4σ).

GRBs OF UNKNOWN REDSHIFT



- 090401B is the GRB with the best directional agreement with 230213A, even including GRBs of unknown redshift: for all of them, the value of S_{dir} is significantly smaller than 194.
- The directional compatibility between GRB170610A and 230213A corresponds to $S_{dir} = 36$.

OUTLOOK

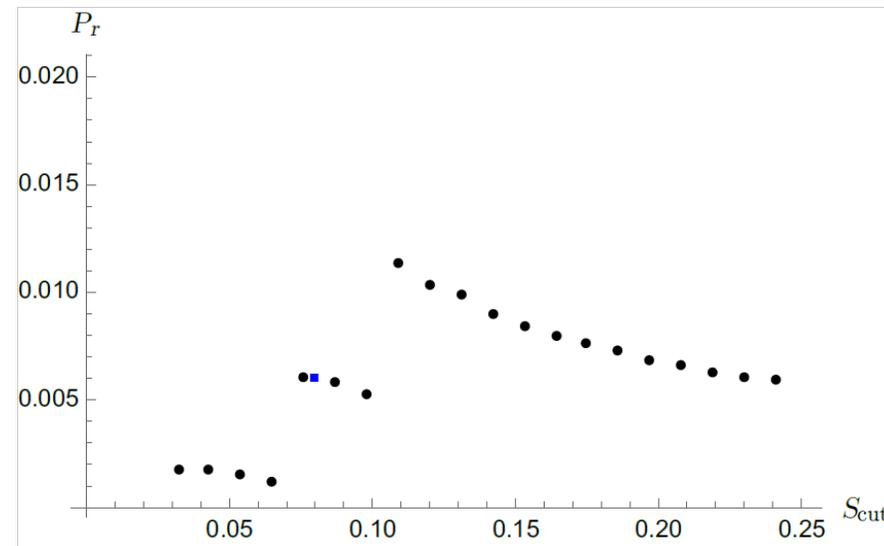


- Combined statistical significance for in-vacuo dispersion of all five GRB-neutrino candidates?
- How to upgrade our statistical approach to include also IC track GRB-neutrino candidates?

Thank you!

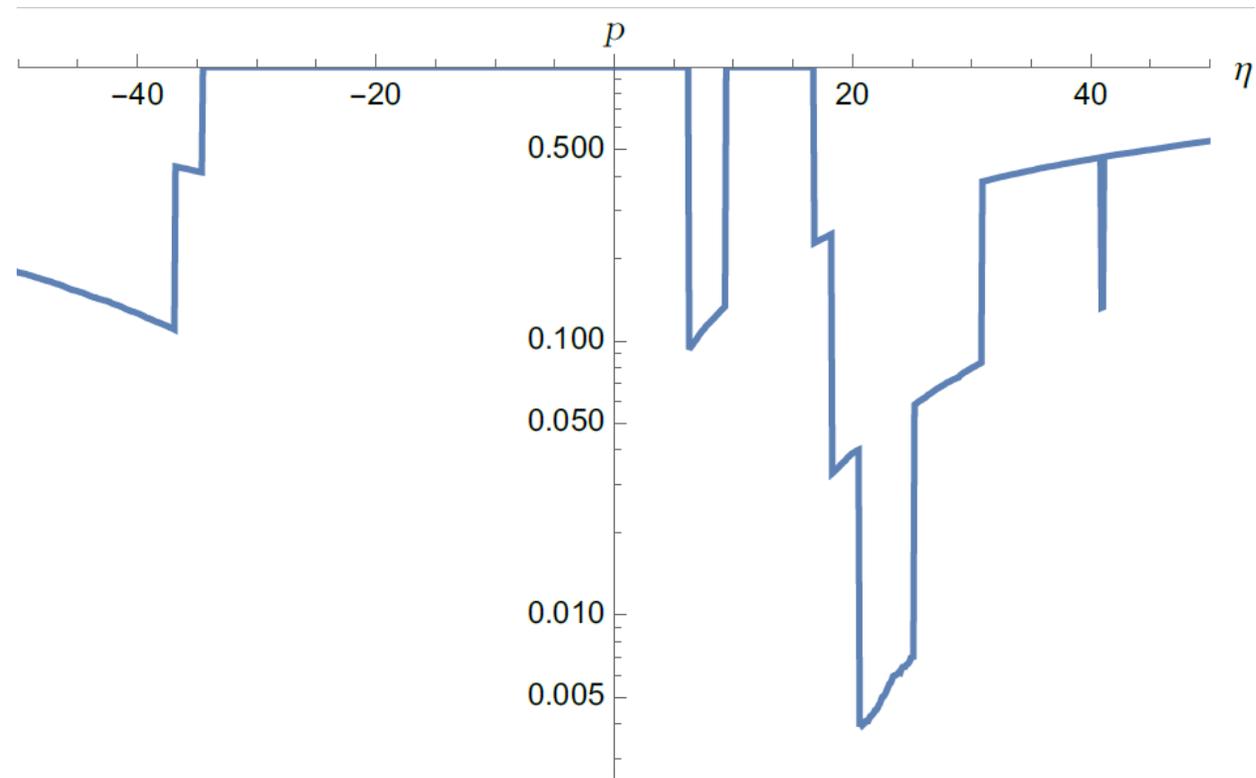
AVENUES FOR REFINING THE STRATEGY OF ANALYSIS

1. Alternative choices of S_{cut} : our main result P_r does not depend strongly on the choice of S_{dir}^{cut} ;



2. Improved correlation r_0 (sensitive to the fact that one should have $\Delta t^* \rightarrow 0$ for $E \rightarrow 0$: $P_{r_0} = 0.4\%$)

p-CURVE FOR $\eta \in [-50, 50]$





FAKE DATA and FAP

- Simulated data obtained from the real data performing the following independent manipulations:
 1. random permutation and a random periodic time translation of neutrino observation times;
 2. random rotation around the Earth's axis of neutrino directions;
 3. random permutation and a random rotation around the Galactic axis of GRB directions.
- FAP of finding at least 4 GRB-neutrino candidates with correlation greater than 0.9985 is $P_r = 0.6\% (2.8\sigma)$.



FAKE DATA and FAP

- Simulated data obtained from true data acting on the GRB directions with a random permutation and a random rotation around the Galactic axis.
- FAP of finding a GRB that produces $S_{dir} \geq 194$ and $S_E \geq 0.00209 \text{ PeV}^{-1}$, $p = 1.5\%$ (2.4σ).