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Tracking Meeting at Lyon - CC October 30, 2024



Tracking_Apollonius in ICEDUST

A New Track/Hit Finding Approach

- Apollonius' problem extended to a **Full Stereo Drift Chamber**
- The method is described in the ArXiv <https://arxiv.org/abs/2401.04576>
- Uses **Julia** programming Language

Given a stereo wire numbered i defined by the stereo angle τ_i , the intersection coordinates $x_i^{\text{Ax.}}, y_i^{\text{Ax.}}$ of the stereo wire in a chosen transverse plane and the wire projection angle ϕ_{si} in this plane, the signed drift distance $d_i^{\text{St.}}$ to this wire i satisfies the equation (2) (see Appendix A) :

$$(x_i^{\text{Ax.}} - x_c)^2 + (y_i^{\text{Ax.}} - y_c)^2 - (R + d_i^{\text{Ax.}})^2 = 0, \quad (2)$$

where the expression of $d_i^{\text{Ax.}}$, function of the stereo wire i and the helix parameters, is given in the equation (A.5b). The absolute value of reconstructed signed drift distance $d_i^{\text{Ax.}}$ can be interpreted as the radius of a circle with the center coordinates $(x_i^{\text{Ax.}}, y_i^{\text{Ax.}})$ in the chosen transverse plane. This circle is tangent to base circle of the helix and therefore can be use in the Apollonius' problem [2].

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arXiv:2401.04576v1 [hep-ex] 9 Jan 2024

GPU-accelerated Interval Arithmetic to solve the Apollonius Problem applied to a Stereo Drift Chamber

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Abstract

We propose a new system of equations which identifies the helix common to all drift distance hits produced by a full stereo drift chamber detector when a charged particle passes through this detector. The equation system is obtained using the Apollonius' problem as guideline which gives it a very simple form and a clear physics interpretability as the case of full axial drift chamber detector. The proposed method is evaluated using drift distance hits constructed from Monte Carlo-generated helix trajectory tracks. The equation system is solved using a robust accelerated GPU brute-force algorithm based on interval arithmetic. All code is written using the Julia programming language.

Keywords: Apollonius' problem, Stereo Drift Chamber, Track Reconstruction, Hit Finding, Interval Arithmetic, Julia Programming Language, GPU.

1. Introduction

The problem studied in this paper is the identification of a helix from a set of drift distance hits given by a Full Stereo Cylindrical Drift Chamber (FSCDC). The search for a helix in a drift chamber with a noisy or non-noisy data set has a long story in particle physics [1].

The idea of applying the Apollonius problem [2] to the search for tracks in an axial drift chamber is not new [3]. This problem is used as guideline to find one equation which satisfy the drift distance hits produced by helix trajectory in a full stereo drift chamber. However, to the best authors' knowledge, this is the first time that the problem of Apollonius is generalised to a FSCDC by taking into account the stereo angle of the wires.

Using a classical root-finding solver in order to recover the helix parameters by solving the system of equations deduced from the Apollonius' problem and applying it to each subset of five hits has some disadvantages like the non-convergence of the calculation without a good initial estimation of the solution and also the total computing time increases exponentially by exhaustively checking all subsets.

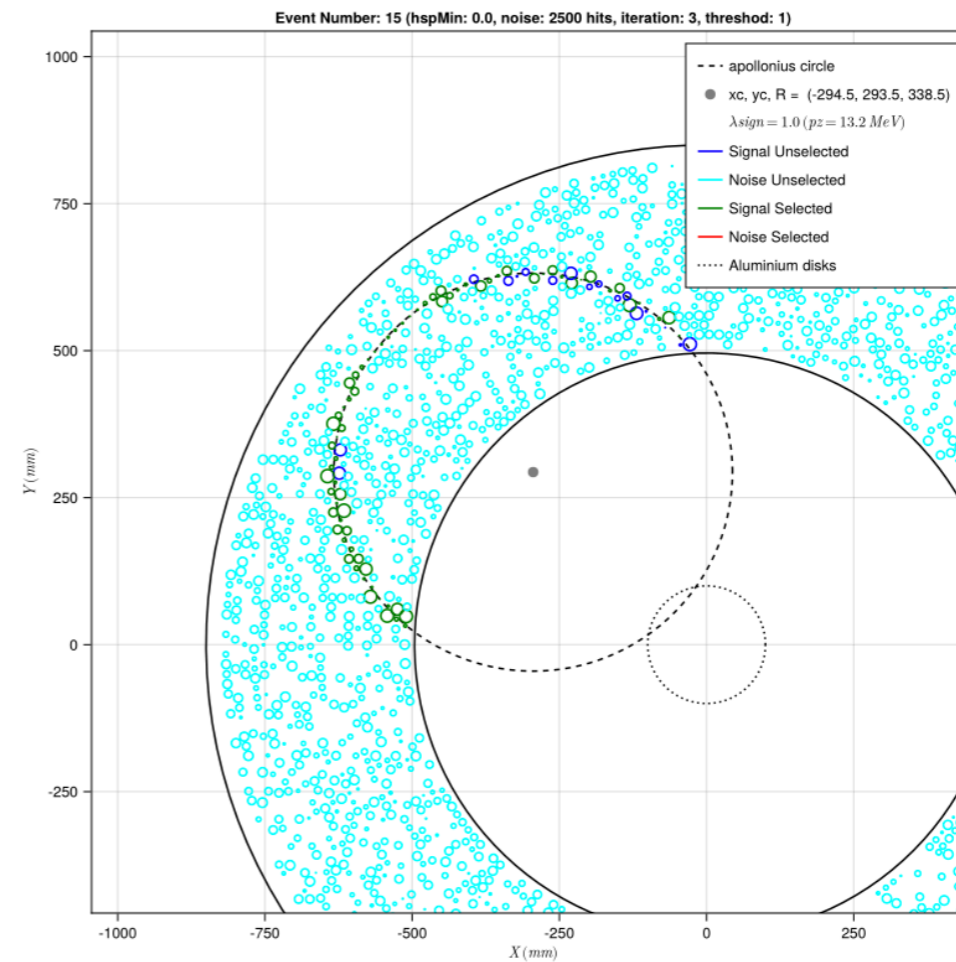
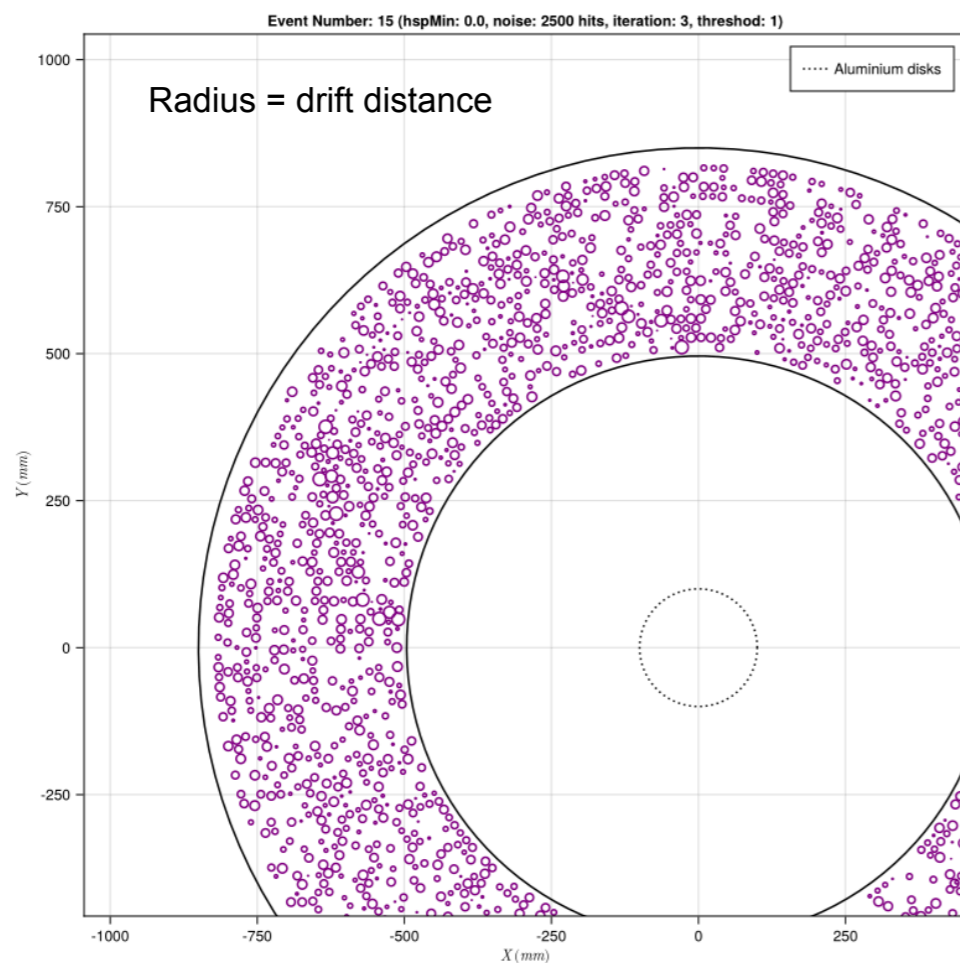
Goal and why Julia

- Find signal hits and tracks in a noisy environment with the **lowest possible processing time** and using **common computer hardware** like GPUs
- Improve efficiency of other methods.

- Julia is a high-level, high-performance dynamic language for scientific and technical computing.
 - Allows an easy use of GPU with available powerful mathematical packages
 - Julia performance is identical to C/C++
 - Main packages for achieving this goal:
 - CUDA.jl (Nvidia)
 - IntervalArithmetic.jl

 - Useful Functionalities:
 - Managing Packages (Pkg) (installation, versioning, compatibilities, ...)
 - Embedding into C/C++
 - Broadcast and vectorization
 - Functions with Full dispatching
 - Garbage Collector (GC)
 - ...

illustration: event with noisy hits



Plot w/ CairoMake.jl package

Processing Time on NVIDIA V100: 2.55 ms/hit

Yao's event

with 2500 hits of noise randomly distributed

- The signal has 89 hits
- 72 hits found (81%)
- 1 hit of noise selected

← Added using Toy_CDC.jl
(our own Julia package
to simulate the CDC)

Development and Testing with Jupyter Notebooks

- Example with a starting part of a Jupyter notebook here is shown the information on packages and type of GPU used.



More about Julia:

- Compilations Just In Time (JIT) based on **LLVM**.
- Very easy to install (and uninstall)
- Open source with a large community (but << Python)
- JuliaHEP community
- Good documentation <https://docs.julialang.org/en/v1/>

```
[2]: import Pkg

[3]: Pkg.activate(".")
Activating project at `~/comet/WilliamProject`
Pkg.add(path="/pbs/home/l/lebrun/comet/dev_julia/Toy_CDC")
Pkg.add(path="/pbs/home/l/lebrun/comet/dev_julia/NewApollonius")

[4]: Pkg.status()
Status `~/comet/WilliamProject/Project.toml`
[b507e648] NewApollonius v1.0.0-DEV `~/pbs/home/l/lebrun/comet/dev_julia/NewApollonius#main`
[7617a686] Toy_CDC v1.0.0 `~/pbs/home/l/lebrun/comet/dev_julia/Toy_CDC#newGeometry`

[5]: Pkg.status(;mode=Pkg.PKGMODE_MANIFEST, outdated=true)
Status `~/comet/WilliamProject/Manifest.toml`
x [79e6a3ab] Adapt v3.7.2 (<v4.0.4): ArrayInterface, CUDA, GPUArrays, GPUArraysCore
x [4fba245c] ArrayInterface v7.5.1 (<v7.10.0): julia
x [ab4f0b2a] BFloat16s v0.2.0 (<v0.5.0): CUDA
x [fa961155] CEnum v0.4.2 (<v0.5.0): CUDA, LLVM
^ [052768ef] CUDA v3.13.1 (<v5.3.4)
^ [6a86dc24] FiniteDiff v2.22.0 (<v2.23.1): julia
x [0c68f7d7] GPUArrays v8.8.1 (<v10.1.1): CUDA
x [46192b85] GPUArraysCore v0.1.5 (<v0.1.6): GPUArrays
x [61eb1bfa] GPUCompiler v0.17.3 (<v0.26.4): CUDA
x [d1acc4aa] IntervalArithmetic v0.20.8 (<v0.22.12): julia
^ [033835bb] JLD2 v0.4.47 (<v0.4.48)
x [929cbde3] LLVM v4.17.1 (<v7.1.0): CUDA, GPUArrays, GPUCompiler
^ [b8f27783] MathOptInterface v1.29.0 (<v1.30.0)
^ [43287f4e] PtrArrays v1.1.0 (<v1.2.0)
^ [91c51154] SentinelArrays v1.4.2 (<v1.4.3)
^ [90137ffa] StaticArrays v1.9.3 (<v1.9.4)
^ [a759f4b9] TimerOutputs v0.5.23 (<v0.5.24)
x [dad2f222] LLVMExtra_jll v0.0.18+0 (<v0.0.29+0): LLVM
^ [f50d1b31] Rmath_jll v0.4.0+0 (<v0.4.2+0)

[5]: import CUDA

[6]: CUDA.versioninfo()
CUDA.devices()
CUDA toolkit 11.7, artifact installation
NVIDIA driver 465.19.1, for CUDA 11.3
CUDA driver 11.3

Libraries:
- CUBLAS: 11.10.1
- CURAND: 10.2.10
- CUFFT: 10.7.2
- CUSOLVER: 11.3.5
- CUSPARSE: 11.7.3
- CUPTI: 17.0.0
- NVML: 11.0.0+465.19.1
- CUDNN: 8.30.2 (for CUDA 11.5.0)
- CUTENSOR: 1.4.0 (for CUDA 11.5.0)

Toolchain:
- Julia: 1.8.5
- LLVM: 13.0.1
- PTX ISA support: 3.2, 4.0, 4.1, 4.2, 4.3, 5.0, 6.0, 6.1, 6.3, 6.4, 6.5, 7.0, 7.1, 7.2
- Device capability support: sm_35, sm_37, sm_50, sm_52, sm_53, sm_60, sm_61, sm_62, sm_70, sm_72, sm_75, sm_80, sm_86

1 device:
0: NVIDIA Tesla K80 (sm_37, 11.170 GiB / 11.173 GiB available)

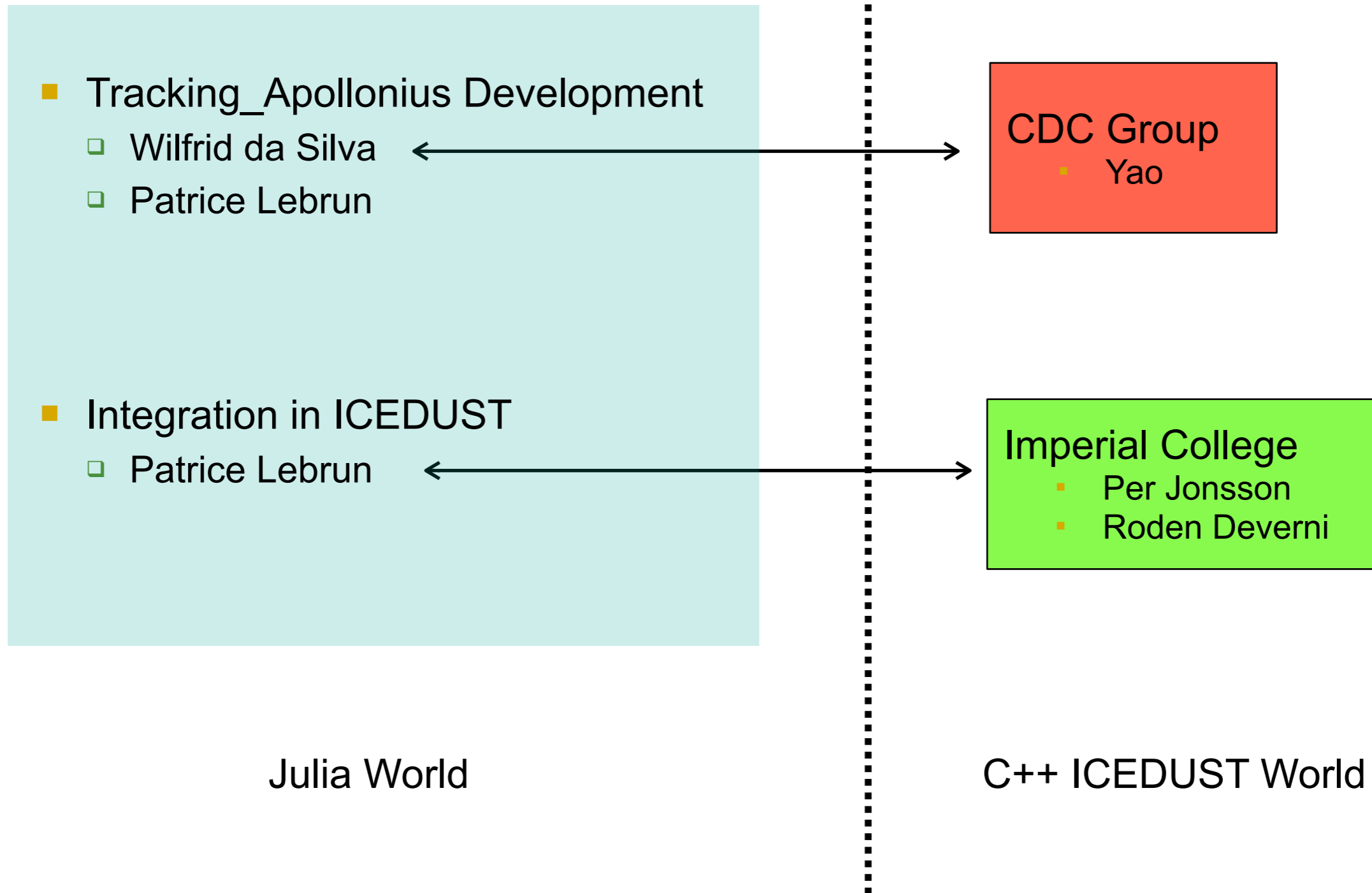
[6]: CUDA.DeviceIterator() for 1 devices:
0. NVIDIA Tesla K80
```

[052768ef] CUDA v3.13.1 (<v5.3.4)

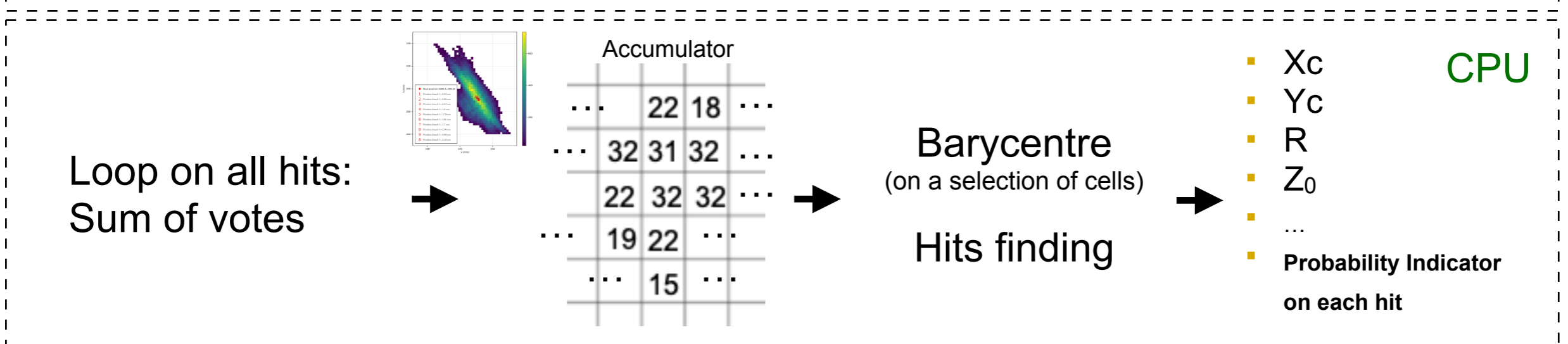
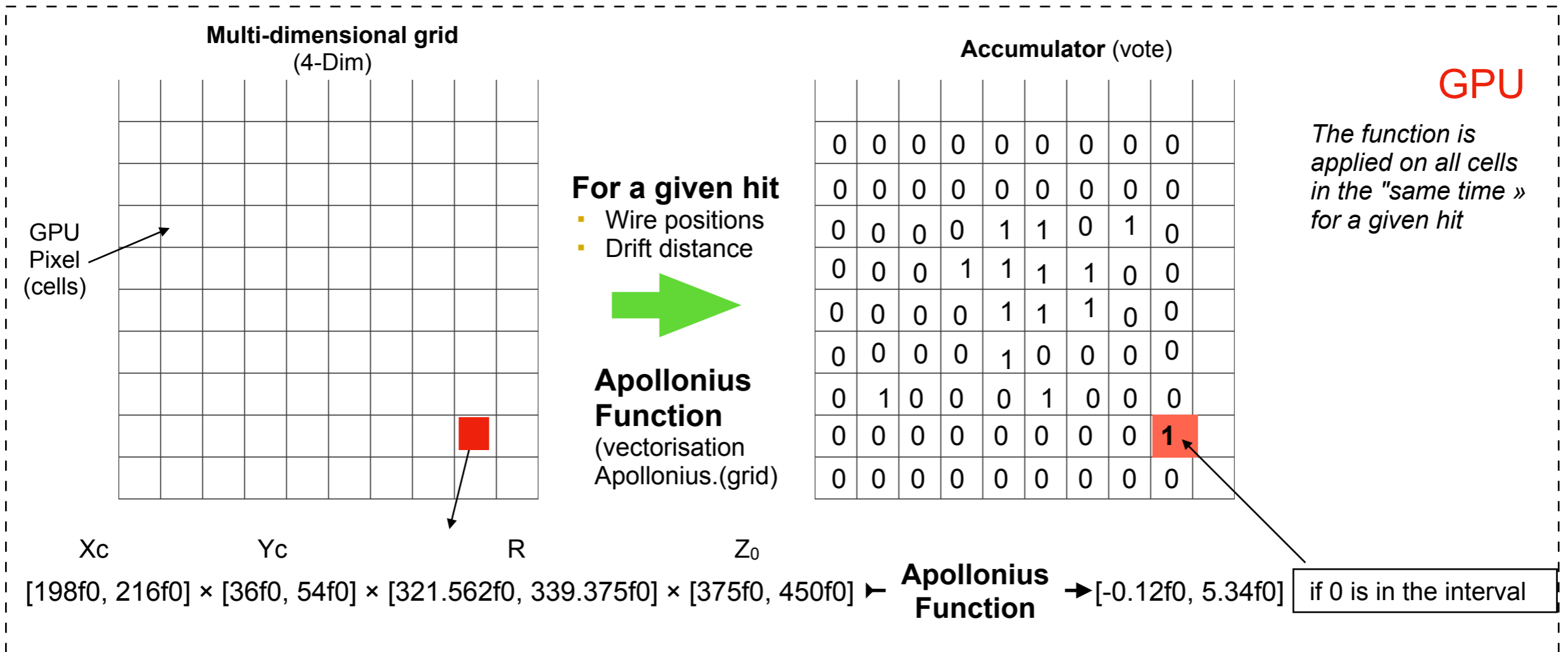
Pinned Version to use old GPU K80, the only one available on jupyterlab
New more powerful GPUs will be available in sept. (last version of CUDA will be used).

Wikipedia: LLVM is a set of compiler and toolchain technologies[4] that can be used to develop a frontend for any programming language and a backend for any instruction set architecture.

Who



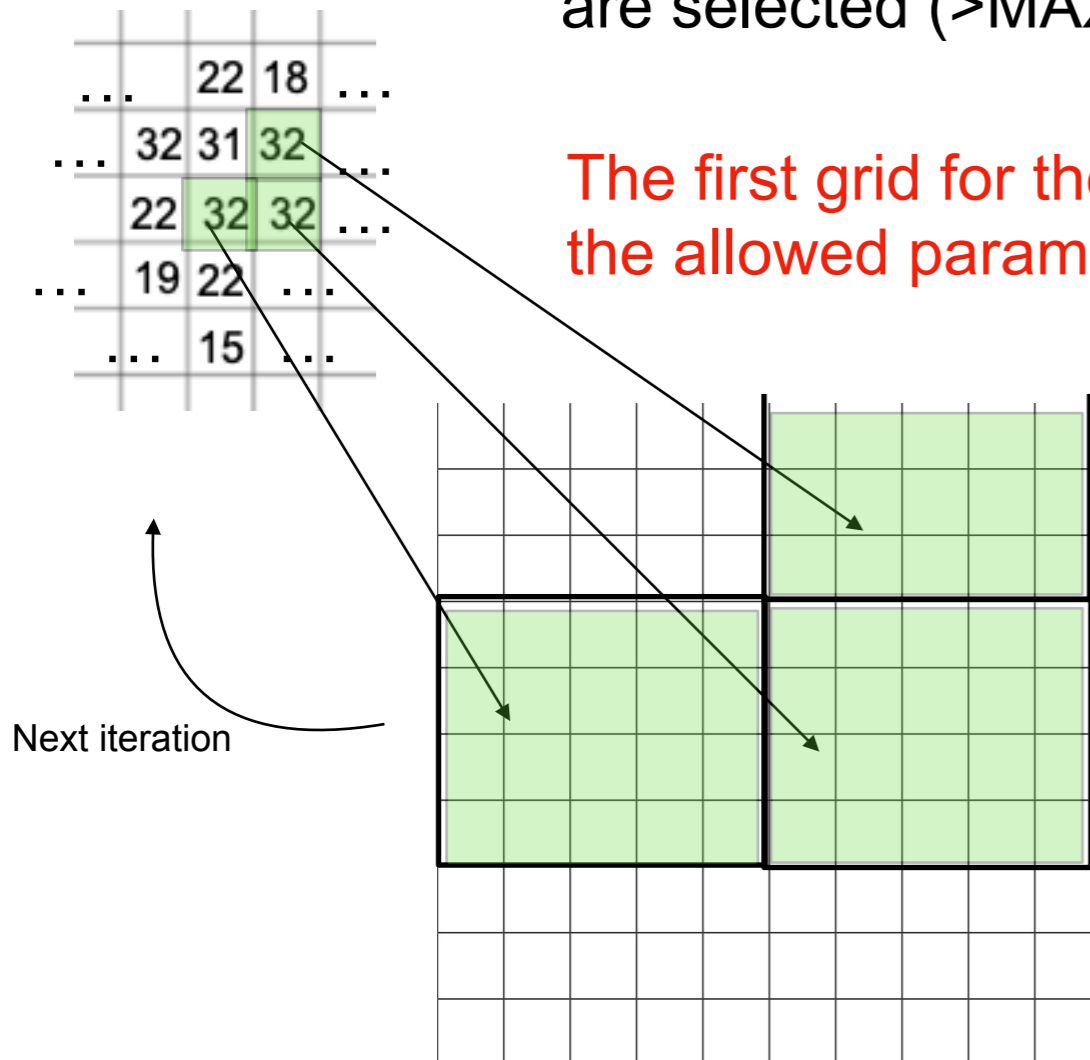
Algorithm Based on Interval Arithmetic with GPU



Iterative Method

The cells having a number of votes greater than a given value are selected ($> \text{MAX-threshold}$) and subdivided to create a new grid.

The first grid for the first iteration has to cover all the allowed parameter space.



Example: 3 iterations (units: mm, MeV)

$E=104.97$

$dE = 1.0e-5$

intervals=[interval(-504.0, 504.0), interval(-504.0, 504.0), interval(87.0, 375.0), interval(0.0, 1500.0), interval(E-dE, E+dE)],

gridSubdivisions=[

(ncellsX = 63, ncellsY = 63, ncellsR = 18, ncellsZ = 30, ncellsE = 1),

(ncellsX=4, ncellsY=4, ncellsR=4, ncellsZ=4, ncellsE=1),

(ncellsX=4, ncellsY=4, ncellsR=4, **ncellsZ=3**, ncellsE=1)]

With this configuration, the first grid has 2143260 cells.

Constraining the trajectory to be in the stopping target, the number of cells is reduced to 661620.

Number of cells in next grids depends on the event.

In the last grid, cell size : $1 \times 1 \times 1 \times 4.2 \text{ mm}^4$.

Equivalent to a single grid
with ~ 32 billion of cells

- Hit finding consists to find hits having a solution in the selected cells (cells with value $>$ threshold).
- **Only hits selected at the previous iteration are used for the next iteration.**
- Time processing is roughly proportional to the number of hits (*more noisy hits less time processing/hit*)

Parameters

- Can only be modified by a Tracking_Apollonius package expert
 - It could be necessary to decide whether some of them can be modified by ICEDUST users.

To use GPU in single or double precision:

```
"precision" => Float32,
```

Value of the uniform Magnetic field used by Apollonius

```
"magneticField" => 1.0f0,
```

If no cells has a number of votes greater or equal to this limit, the accumulator is empty (no track found).

```
"vote_min" => 15,
```

At each iteration, a set of thresholds is defined.

The highest value is used to select cells to create the grid for the next iteration.

A set of hits found correspond to a threshold (each threshold is associated to a probability to be a hit of signal).

A hit is found when it belongs to a cell with a number of votes $> \text{MAX}(\text{votes}) - \text{threshold}$

```
"thresholds_iter" => [[9], [1, 3, 5, 7], [1, 2, 3, 4, 5]],
```

Apollonius circle values are obtained with the cells having a number of votes $> \text{MAX}(\text{votes}) - \text{threshold_results}$.

For instance here, only the cells with the maximum of votes are used.

```
"threshold_results" => 1
```

Possible values domain of the Apollonius helix (X_c , Y_c , R , Z_0 and E)

```
"intervals" => IntervalArithmetic.Interval{Float32}
```

```
[-504f0, 504f0], [-504f0, 504f0], [87f0, 375f0], [0f0, 1500f0], [104.969f0, 104.971f0]],
```

Defines the cells size for each iteration (number of cells in each dimension).

```
"subdivisions" => @NamedTuple{ncellsX::Int64, ncellsY::Int64, ncellsR::Int64, ncellsZ::Int64, ncellsE::Int64}[
```

```
(ncellsX = 63, ncellsY = 63, ncellsR = 18, ncellsZ = 30, ncellsE = 1),
```

```
(ncellsX = 4, ncellsY = 4, ncellsR = 4, ncellsZ = 4, ncellsE = 1),
```

```
(ncellsX = 4, ncellsY = 4, ncellsR = 4, ncellsZ = 3, ncellsE = 1)]
```

Position of the projection plane

```
"zProj" => -791.626,
```

← better to choose 1 (12.5 mm) or 2 (6.25 mm) ?
Is $4.1\bar{6}$ mm not too small ?

Performance

- Yao's events Run001 (no noise added)
 - Number of events: 6754
 - Overall Total Number of Hits: 470710
 - **3.2 ms/hit on 1 device of NVIDIA V100 in single precision (this time per hit decreases when the number of noisy hits increases).**
 - Resolutions [mm] (**assuming a 1 Tesla uniform magnetic field**).

	Mean	RMS
$x_c - x_{c0}$	-0.95	7.71
$y_c - y_{c0}$	-1.55	8.53
$R - R_0$	0.67	10.09

- Resolutions [mm] for differences lower than 20 mm in absolute value

	Mean	RMS	#events
$x_c - x_{c0}$	-0.74	4,89	6629 (98.1 %)
$y_c - y_{c0}$	-1.09	5.73	6552 (97.0 %)
$R - R_0$	0.13	5.33	6478 (95.9 %)

- Efficiencies:
 - Number of hits **not found** (*hit not in the accumulator*):
 - 22401 (4.75 %)
 - Number of hits **found** with the Highest Probability to be a hit of signal (*hit in cells with maximum of votes*):
 - 420068 (89.24 %)

Tracking_Apollonius in ICEDUST (1)

- ICEDUST_externals_source_LFS
 - Official Julia binary Release
 - it's not recommended to use an own build of Julia (CUDA.jl)
 - Currently JULIA/julia-1.10.5-linux-x86_64.tar.gz (64 bits)
 - Other releases are available for many architectures and OS: <https://julialang.org/downloads/>
- ICEDUST_externals_install
 - julia-1.10.5-linux-x86_64 [**bin etc include lib libexec LICENSE.md share**]
- ICEDUST_packages
 - oaJuliaInterface (can be used for other Julia project)
 - Goal: ICEDUST user does not need to know Julia
 - C++ class with members to call some Tracking_Apollonius functions (currently)
 - Tracking_Apollonius is a submodule
 - Tracking_Apollonius **has to be a git repository** to be used by the package manager of Julia
 - Meaning Tracking_Apollonius can be used also in a pure Julia environment (important for development)
- ICEDUST_install
 - **julia_depot** directory where all packages and artefacts are installed (~2.7 Go)
 - Shared library *lib/liboaJuliaInterface.so* and setups and executables for testing are in `oaJuliaInterface/bin`
 - Setup.sh is updated

Tracking_Apollonius in ICEDUST (2)

- Use embedding Julia in C/C++
 - Simple functions are defined in Tracking_Apollonius to be easily called by ICEDUST, avoiding to have very sophisticated C/C++ code to write.
 - Limited to Array and Structure with leaf types (Int, float, double, bool ...)
- Build procedures (new when red)
 - ICEDUST_externals_install

```
git clone git@gitlab.in2p3.fr:Patrice/ICEDUST_external_sources_LFS.git
cd ../; mkdir ext_build; cd ext_build
cmake -DBUILD_JULIA=TRUE -DBUILD_GEANT4_VERSION=4.10.6 ../ICEDUST_external_sources_LFS
make -j4
```

'Patrice' is temporary, it should be comet (hoping so)

- ICEDUST_install
 - build has to be done on machine with GPU (the use of docker is underway).

```
git clone git@gitlab.in2p3.fr:Patrice/ICEDUST_packages.git
cd ICEDUST_packages
git clone git@gitlab.in2p3.fr:Patrice/Tracking_Apollonius
cd ../; mkdir build; cd build
cmake -DBUILD_JULIA=TRUE -DBUILD_GEANT4_VERSION=4.10.6 ../ICEDUST_packages
make -j4
```

Notes:

git clone --recurse-submodules git@gitlab.in2p3.fr:Patrice/ICEDUST_packages.git will replace the two git clone commands when julia will be able to use submodules (a patch is available but not yet applied).

Testing

- Two executables are available in `oaJuliaInterface/bin` for testing and measuring time performance
 - 1st Test (`time TestoaJuliaInterface`)
 - check the result of `Tracking_Apollonius` with a sample of hits
 - Measure the initialisation time
 - 2st Test (`time TestoaJuliaInterfaceLoop <int>`)
 - to measure processing time per hit
 - The sources are in `ICEDUST_packages/oaJuliaInterface/app`
 - Could be used as example to use the interface.

2nd Test Output
(100 loops)

```
ICEDUST_install/oaJuliaInterface/bin$ time TestoaJuliaInterfaceLoop 100
```

```
TestoaJuliaInterfaceLoop:
```

```
Number of loop: 100 ...
```

```
Initialization of Julia (has to be done only once).
```

```
Activate Apollonius project: import Pkg; Pkg.activate("Apollonius"; shared=true); using Tracking_Apollonius
```

```
  Activating project at `~/comet/ICEDUST/ICEDUST_install/julia_depot/environments/Apollonius`
```

```
Module Ptr: 0x14b3f07d1910
```

```
call init_apollonius() ...
```

```
Start init_apollonius
```

```
Precision: Float32
```

```
Magnetic Field: 1.0 Tesla
```

```
Grid Init:
```

```
[-504f0, 504f0] × [-504f0, 504f0] × [87f0, 375f0] × [0f0, 1500f0] × [104.969f0, 104.971f0]
```

```
(ncellsX = 63, ncellsY = 63, ncellsR = 18, ncellsZ = 30, ncellsE = 1)
```

```
cu_array length: 2143260
```

```
cu_array constraint length: 661620
```

```
Dict{String, Any}{"thresholds_iter" => [[9], [1, 3, 5, 7], [1, 2, 3, 4, 5]], "magneticField" => 1.0f0, "iterations" => 3, "zProj" => -791.626, "intervals" => IntervalArithmetic.Interval{Float32}[[-504f0, 504f0], [-504f0, 504f0], [87f0, 375f0], [0f0, 1500f0], [104.969f0, 104.971f0]], "pivot" => Float32[0.0, 0.0], "precision" => Float32, "subdivisions" => @NamedTuple{ncellsX::Int64, ncellsY::Int64, ncellsR::Int64, ncellsZ::Int64, ncellsE::Int64}{(ncellsX = 63, ncellsY = 63, ncellsR = 18, ncellsZ = 30, ncellsE = 1), (ncellsX = 4, ncellsY = 4, ncellsR = 4, ncellsZ = 4, ncellsE = 1), (ncellsX = 4, ncellsY = 4, ncellsR = 4, ncellsZ = 3, ncellsE = 1)}, "vote_min" => 15, "divideandconquer" => true)
```

```
End init_apollonius
```

```
Apollonius is functional: 0
```

```
init_apollonius done
```

```
The status returned by apollonius.init() is: 0
```

```
From get_structure: length of jl_hits_drifts: 146
```

```
From get_structure: length of jl_hits_drifts: 146
```

```
...
```

```
...
```

```
From get_structure: length of jl_hits_drifts: 146
```

```
From get_structure: length of jl_hits_drifts: 146
```

```
From get_structure: length of jl_hits_drifts: 146
```

```
real1m19.585s
```

```
user1m17.655s
```

```
sys 0m2.109s
```

Time processing per hit: ~3.1 ms (on V100 GPU type)

CODE

Hits Structure:

Wire positions and drift distances
in the local system of coordinates of the CDC (unit in mm)
Tracking_Apollonius does not know anything about the
geometry

oaJuliaInterface/src/ICDChitsICEDUST.hxx

```
#ifndef OAJULIAINTERFACE_CDChitsICEDUST_HXX
#define OAJULIAINTERFACE_CDChitsICEDUST_HXX

#include <vector>
typedef struct
{
    std::vector<float>* xstarts;
    std::vector<float>* ystarts;
    std::vector<float>* zstarts;
    std::vector<float>* xends;
    std::vector<float>* yends;
    std::vector<float>* zends;
    std::vector<float>* drifts;
}CDChitsICEDUST;
```

```
#include <julia.h>
JULIA_DEFINE_FAST_TLS // only define this once, in an executable (not in a shared library) if you want fast code.

#include <IApollonius.hxx>
#include <ICDChitsICEDUST.hxx>

int main()
{
    IApollonius* apollonius = IApollonius::getInstance(); //singleton because a julia module can be seen as workspace
    // apollonius->CUDA_versioninfo(); //to print information on CUDA and GPU

    int status = apollonius->init();
    if (status != 0) return status; // 0 means everything is ok

    CDChitsICEDUST hits;
    fill_hits(&hits); // A function which fill the hits values

    const std::vector<float>* results = apollonius->apolloniusresults(&hits);
    // work on results (next slide) ...
}
```

Another function to save time processing:

```
const std::vector<float>* results = apollonius->apolloniusresultswithselection(&hits, &selection);
where selection is a vector<bool>
Only hits with a true value are used at the first iteration. All hits are used for hits finding.
```

Results

- `const std::vector<float>* results = apollonius->apolloniusresults(&hits);`

results vector:

```
0: xc
1: yc
2: R
3: Z0
4: RMS xc
5: RMS yc
6: RMS R
7: RMS Z0
8: Vote Max
9: Number of cells in the accumulator
10: Sign of Pz
11: Quality (iteration level)
12: nhits (Number of hits)
13:12+nhits: Probability Indicator for each hit given in input (hit found for a given threshold).
13+nhits:end Sign of each drift distance (-1.0, 0.0 , 1.0 , 99.0 for hit flagged as noise)
```

Quality is related to the iteration number of the given results.

Probability Indicator is a probability for a hit to belong to the track signal.

Results

- Some Function Members are available to get partial informations:
 - the result on the current event is stored in the apollonius object.

```
printf("Xc, Yc, R, Z0 values: %f, %f, %f, %f\n", apollonius->Xc(), apollonius->Yc(), apollonius->R(), apollonius->Z0());  
printf("RMS of Xc, Yc, R, Z0 values: %f, %f, %f, %f\n", apollonius->RMS_Xc(), apollonius->RMS_Yc(), apollonius->RMS_R(),  
apollonius->RMS_Z0());
```

```
printf("Vote max, number of cells values: %d, %d\n", apollonius->vote_max(), apollonius->numberOfCells());  
printf("sign of Pz, Quality values: %f, %f\n", apollonius->PzSign(), apollonius->quality());
```

```
printf("Number of hits: %d\n", apollonius->numberOfHits());
```

```
std::vector<float> hitsProbabilityIndicator = apollonius->hitsProbabilityIndicator();  
printf("Hits Probability Indicator (size=%ld):\n", hitsProbabilityIndicator.size());  
printf("[ ");  
for(size_t i=0; i<hitsProbabilityIndicator.size(); i++)  
    printf("%.2f ", hitsProbabilityIndicator[i]);  
printf("]\n");
```

```
std::vector<float> hitsDriftSigns = apollonius->hitsDriftSigns();  
printf("Hits Drift Signs (size=%ld):\n", hitsDriftSigns.size());  
printf("[ ");  
for(size_t i=0; i<hitsDriftSigns.size(); i++)  
    printf("%.2f ", hitsDriftSigns[i]);  
printf("]\n");
```

Possible Future

- Integrating ICEDUST or a part of it in Julia
 - Why not if Julia has a lot of success
- An example of Integration in high energy physics .
 - Geant4 is used like a package by Julia.
 - Among other conclusion: Geant4.jl can be a very useful add-on to the Geant4 project
 - Tutorials (very easy to setup and portable), interactive development (notebooks), connection to other powerful packages in the Julia ecosystem (visualization, analysis, etc.)

2023 JuliaHEP Workshop

Geant4.jl - New Interface to Simulation Applications

Pere Mato / CERN
9 November 2023

<https://github.com/JuliaHEP/Geant4.jl> *Click on it to get the PDF*

- JuliaHEP is working on ROOT integration
- UnROOT.jl is a packages already available to work with TTree