

# Non-axion solutions to the strong CP problem and their phenomenology

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*14/11/2024*

Based on  
2303.06156, 2311.00702 [hep-ph] + w.i.p.  
with L. Hall, C. A. Manzari, A. McCune,  
B. Noether & C. Scherb

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(sub- to multi-)  
TeV-scale

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Arises from the following terms of the SM lagrangian :

$$\mathcal{L}_{\text{SM}} \supset \bar{Q}Y_d dH + \bar{Q}Y_u u\tilde{H} + h.c. + \frac{g_s^2 \theta}{32\pi^2} \epsilon^{\mu\nu\rho\sigma} G_{\mu\nu}^a G_{\rho\sigma}^a$$

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In there, two **physical** CP-violating quantities :

- $J_4 = \text{Im Tr} \left[ Y_u Y_u^\dagger, Y_d Y_d^\dagger \right]^3$   
[Jarlskog '85]

- $\bar{\theta} = \theta + \arg \det(Y_u Y_d)$

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Predicts a **neutron electric dipole moment**

[Baluni '79, Crewther/Di Vecchia/Veneziano/Witten '79]

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In there, two physical parameters :

**Strong CP problem :**

- $J_4 = \text{Im Tr} [Y_u Y_d]$

$$\bar{\theta} \lesssim 10^{-10}$$

! Accounts for CP violation (today)

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# The strong CP problem and axions

Leading solution, axions :  $\bar{\theta} = \left\langle \frac{a}{f_a} \right\rangle$  which dynamically  
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[Peccei/Quinn '77,  
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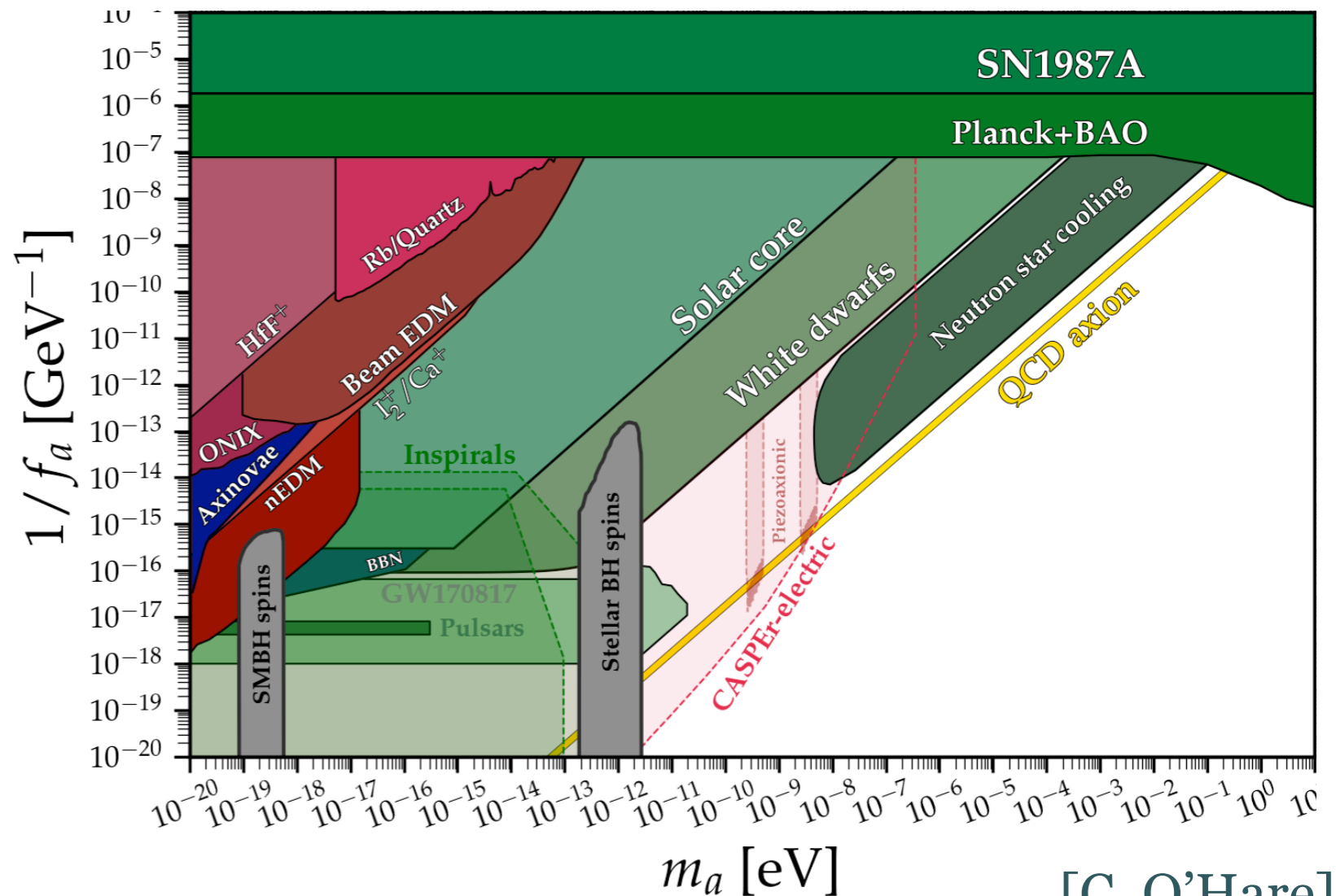
Greatly motivated, let's focus on the pheno : **mostly non-collider BSM signals**

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Dominated by low-energy experiments, astrophysics, late-time cosmology  
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[C. O'Hare]

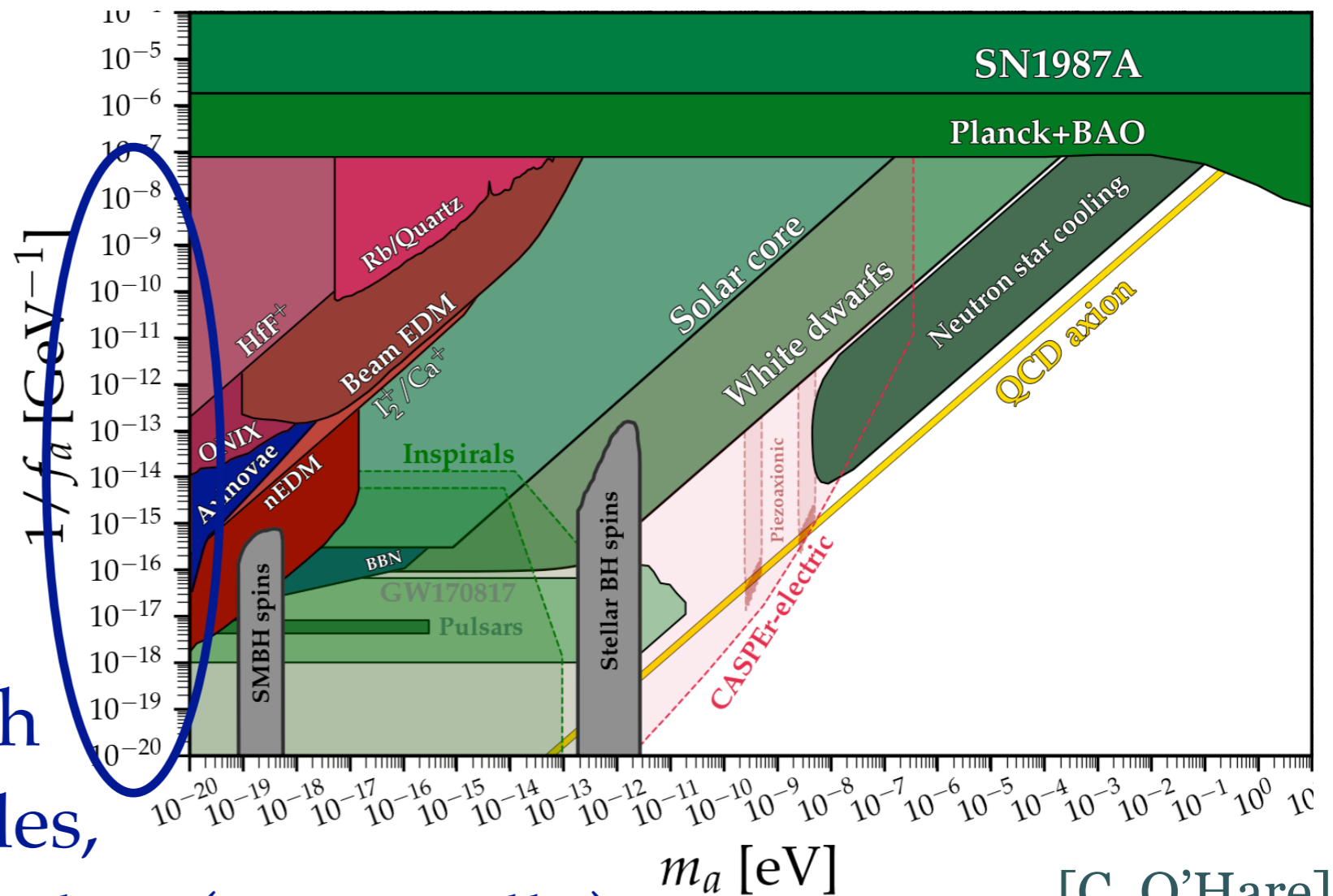
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high scales, colliders (generically)



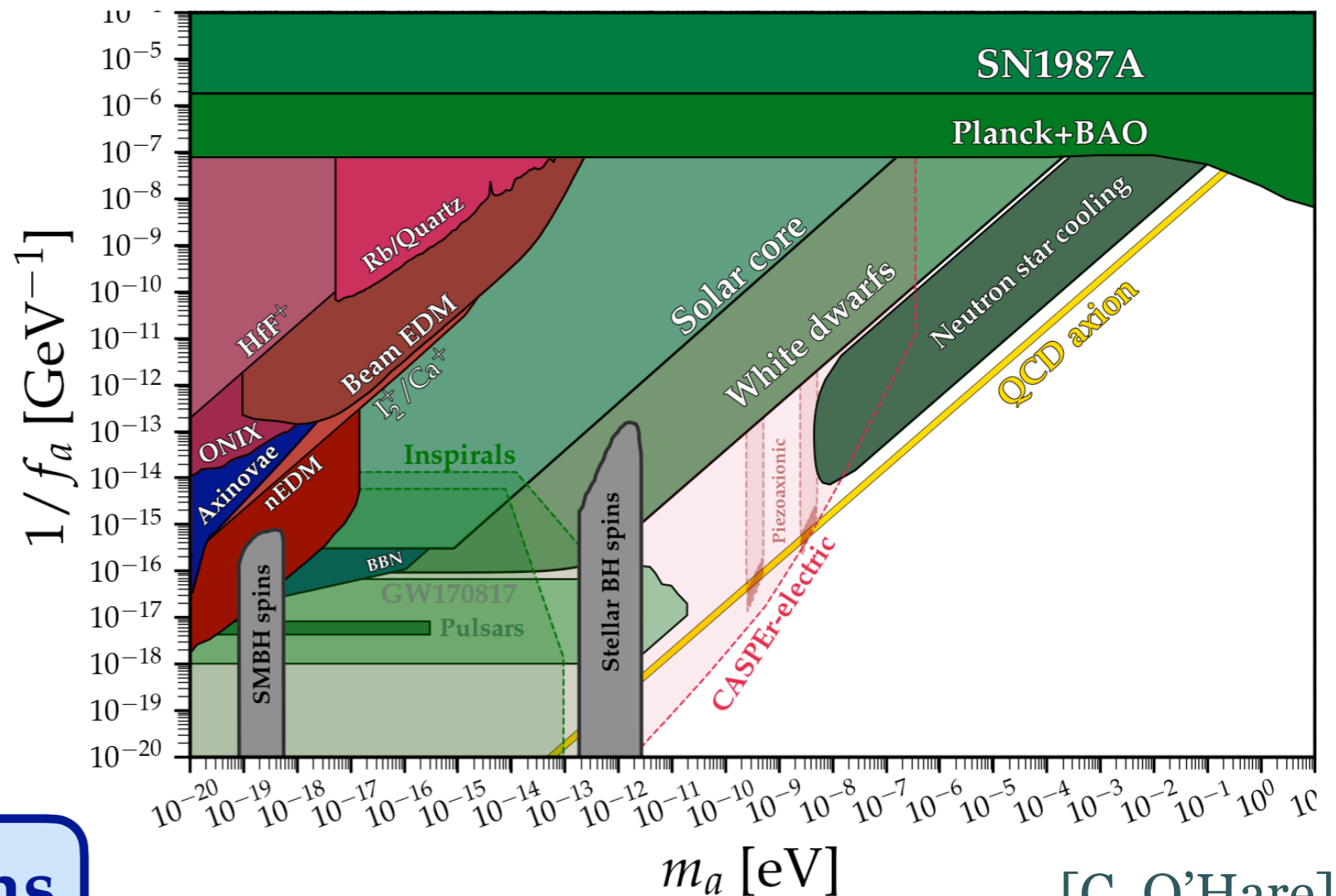
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Today : other paradigms

[C. O'Hare]

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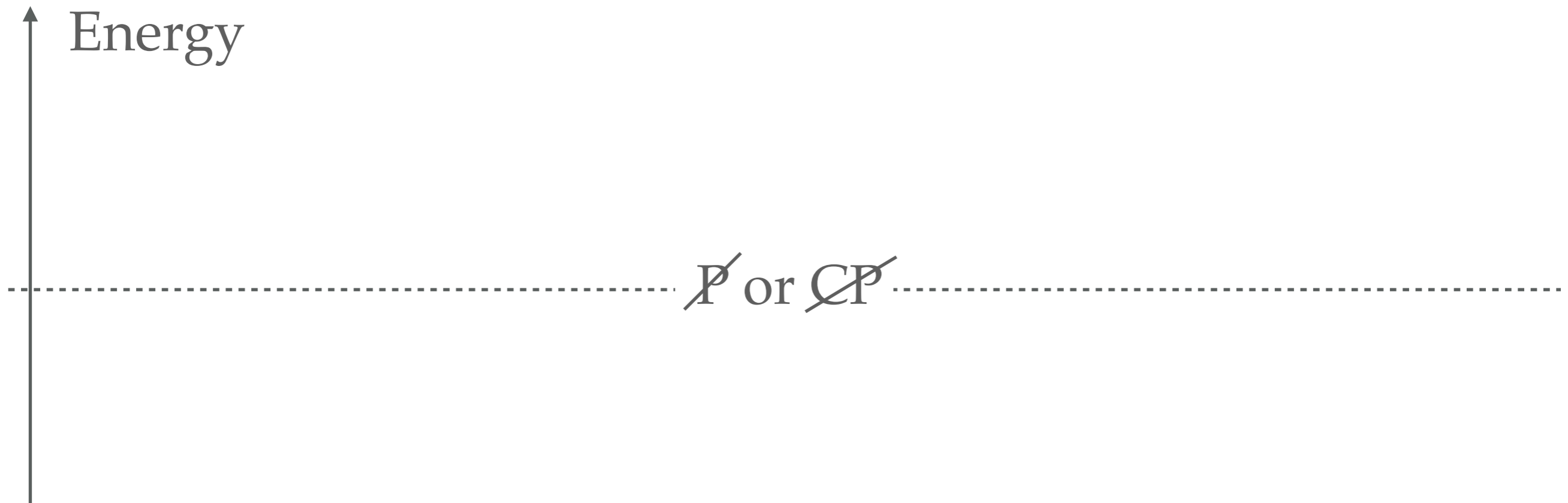
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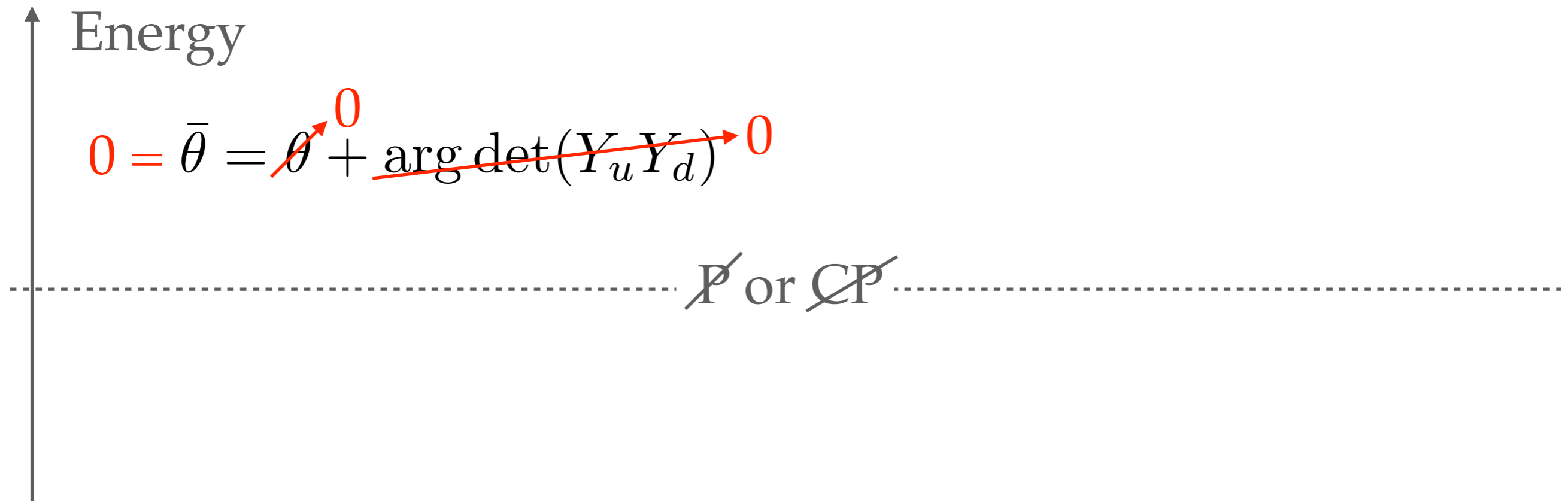


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Energy

**Challenge :**

$$0 = \bar{\theta} = \cancel{\theta} + \cancel{\arg \det(Y_u Y_d)} \rightarrow 0$$

$$0 = J_4 = \text{Im Tr} \left[ Y_u Y_u^\dagger, Y_d Y_d^\dagger \right]^3$$

~~P~~ or ~~CP~~

$$0 \approx \bar{\theta} = \theta + \arg \det(Y_u Y_d)$$

$$0 \neq J_4 = \text{Im Tr} \left[ Y_u Y_u^\dagger, Y_d Y_d^\dagger \right]^3$$

still

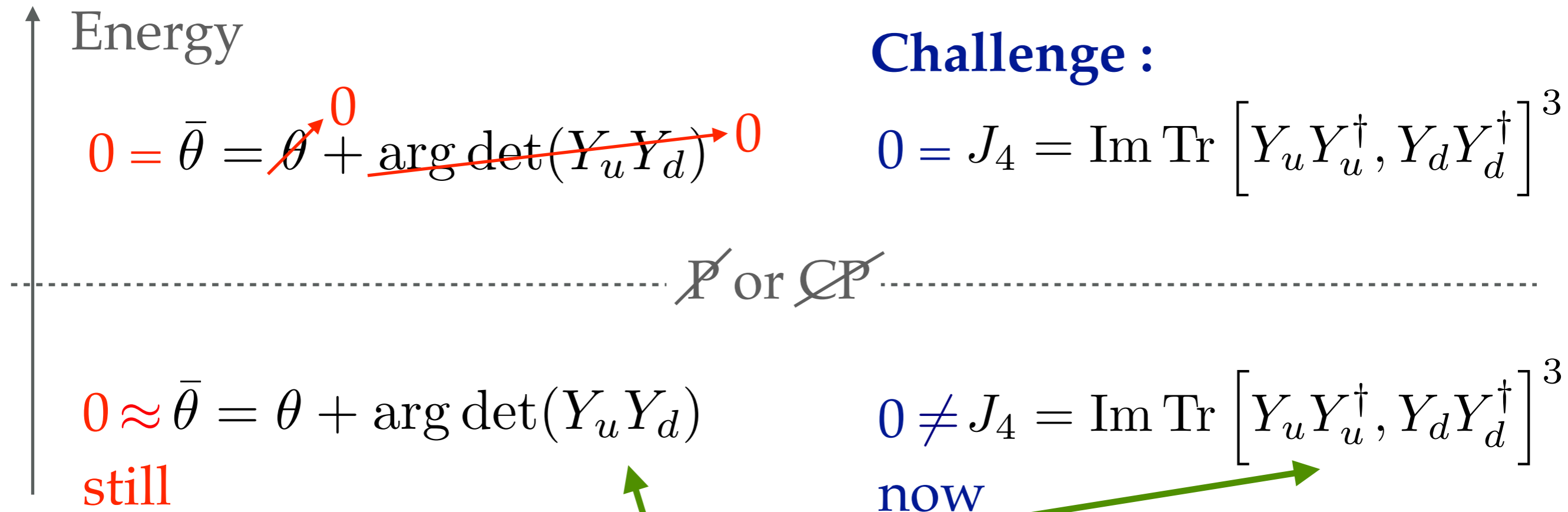
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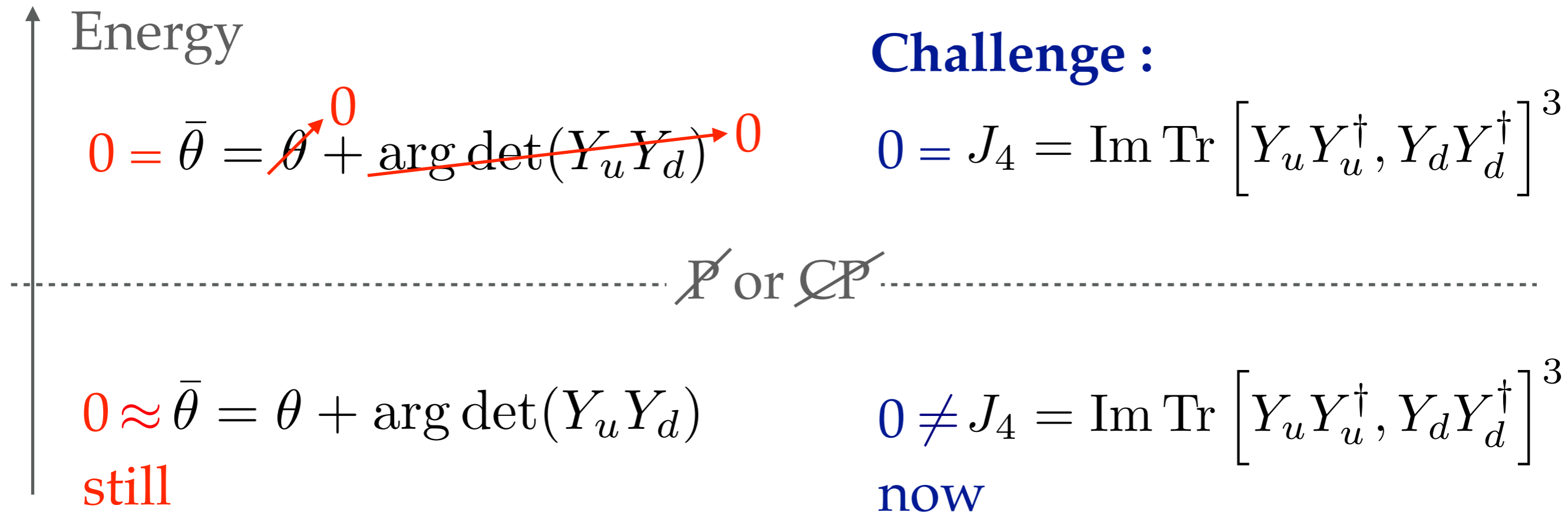
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Natural interplay with flavor physics, **often TeV-scale pheno**

# Example 1 : Higgs-induced CP breaking

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With  $n > 1$  Higgs doublets, one can achieve

[Georgi '78,

Nebot/Botella/Branco '18,

Hall/Manzari/Noether '24,

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Always produces one light second Higgs doublet !

[Miro/Nebot/Queiroz '24]

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Typical 2HDM pheno + additional flavor signals

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[Neboj/Botella/Branco '18]

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$Q_{L,3}$  couplings

$$\Gamma_2 = \begin{pmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \\ \times & \times & \times \end{pmatrix},$$
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2nd Higgs couplings

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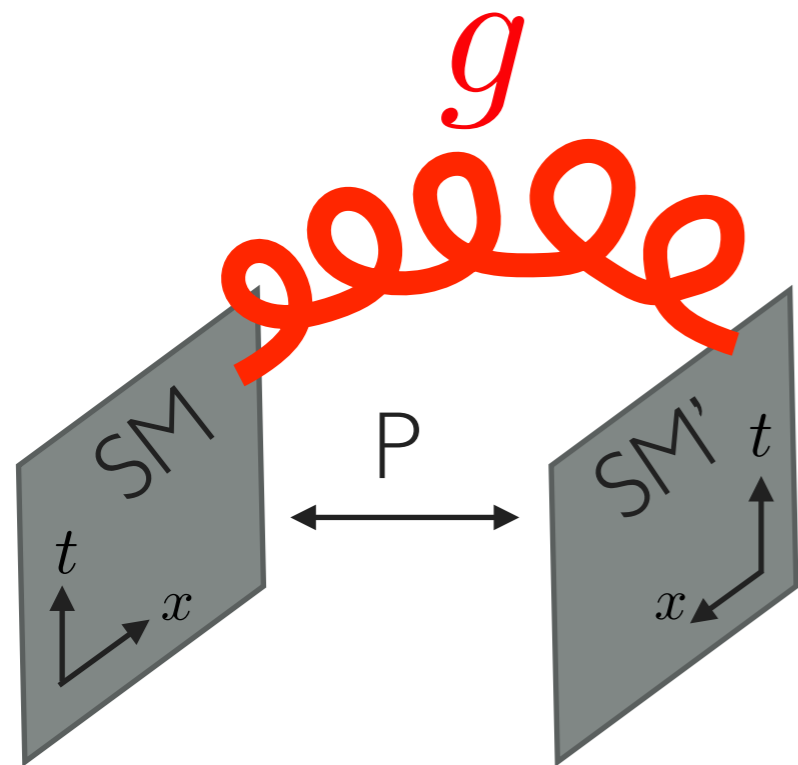
[Nebot/Botella/Branco '18]

More work needed to scan the landscape of models : when do those setups really fulfill the strong constraints from the neutron EDM + flavor physics ? What is the interplay with the flavor puzzle ? Are there still light states in the case of soft breaking of CP ? Etc.

[Ferreira/Lavoura '19, QB/Hall/Manzari/Noether, w.i.p.]

# Example 2 : mirror worlds

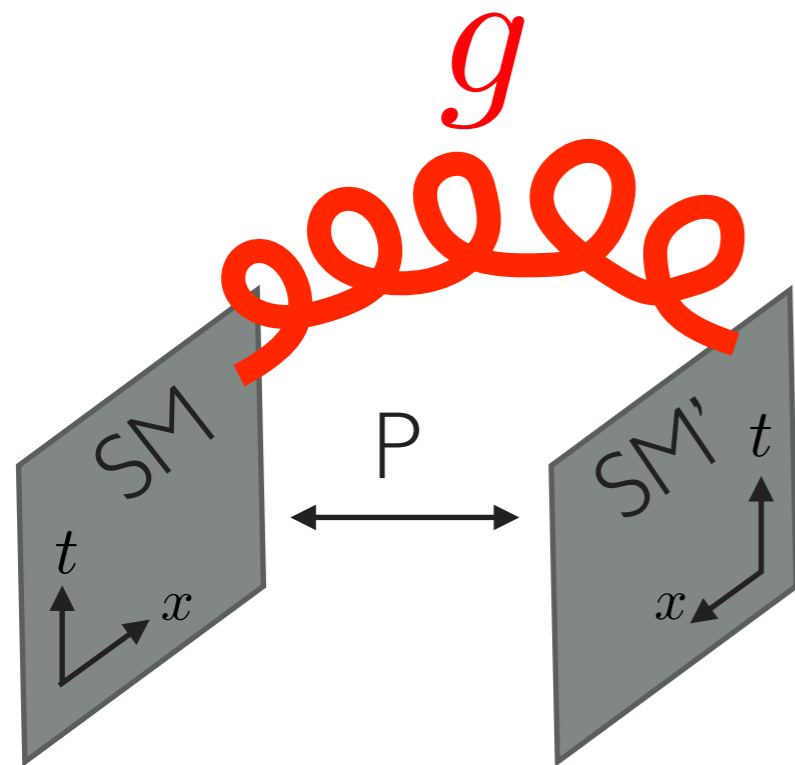
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[Babu/Mohapatra '89, '90, Barr/Chang/Senjanovic '91,  
Hall/Harigaya '18, +Dunsky '18, Craig/Garcia Garcia/  
Koszegi/McCune '20, ... ]

	$SU(3)$	$SU(2)_L$	$U(1)_Y$	$SU(2)'$	$U(1)'$
$Q$	<b>3</b>	<b>2</b>	1/6	<b>1</b>	0
$u^c$	$\bar{\mathbf{3}}$	<b>1</b>	-2/3	<b>1</b>	0
$d^c$	$\bar{\mathbf{3}}$	<b>1</b>	1/3	<b>1</b>	0
$L$	<b>1</b>	<b>2</b>	-1/2	<b>1</b>	0
$e^c$	<b>1</b>	<b>1</b>	-1	<b>1</b>	0
$H$	<b>1</b>	<b>2</b>	1/2	<b>1</b>	0
$Q'$	$\bar{\mathbf{3}}$	<b>1</b>	0	<b>2</b>	-1/6
$u'^c$	<b>3</b>	<b>1</b>	0	<b>1</b>	2/3
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$e'^c$	<b>1</b>	<b>1</b>	0	<b>1</b>	1
$H'$	<b>1</b>	<b>1</b>	0	<b>2</b>	-1/2

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[Babu/Mohapatra '89, '90, Barr/Chang/Senjanovic '91, Hall/Harigaya '18, +Dunsky '18, Craig/Garcia Garcia/Koszegi/McCune '20, ... ]

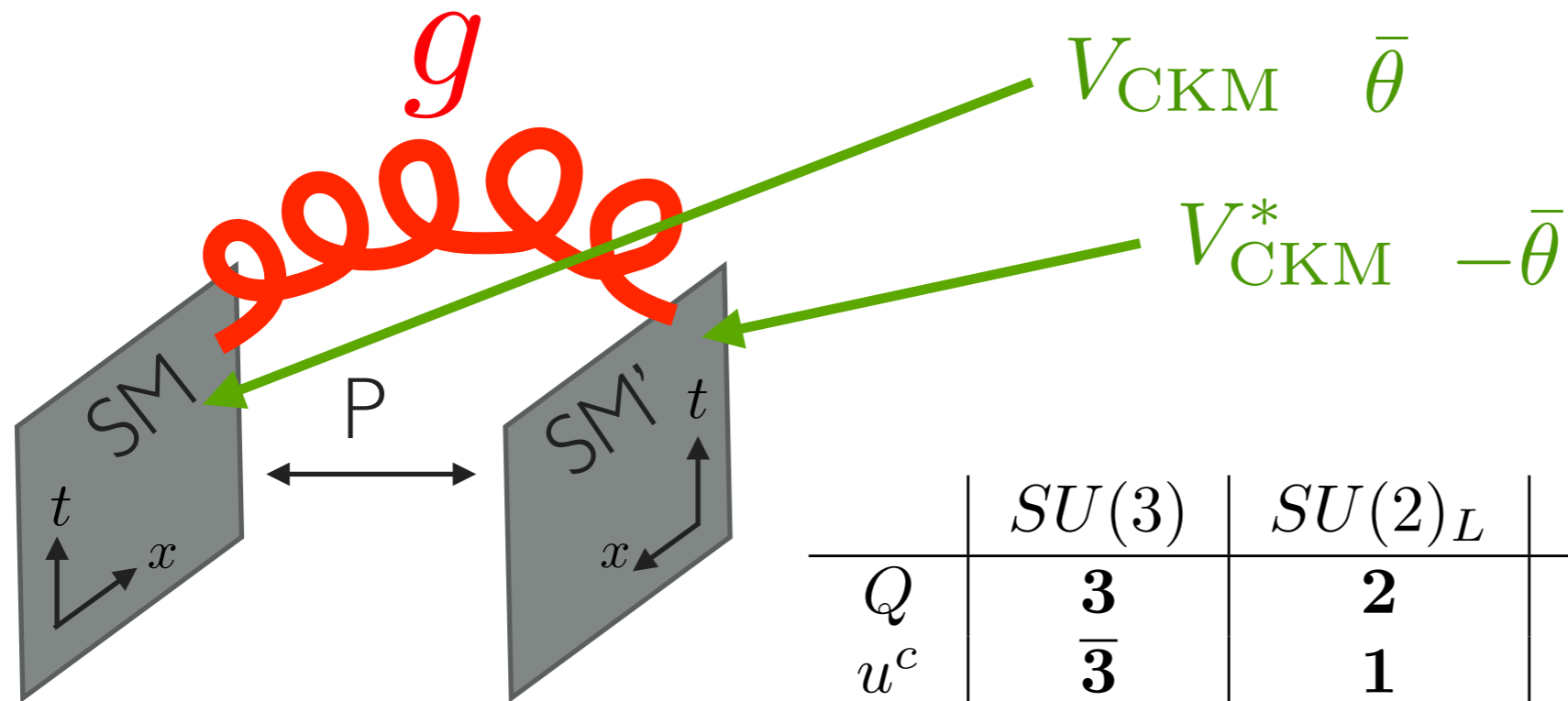
## Mirror forces

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## Mirror particles

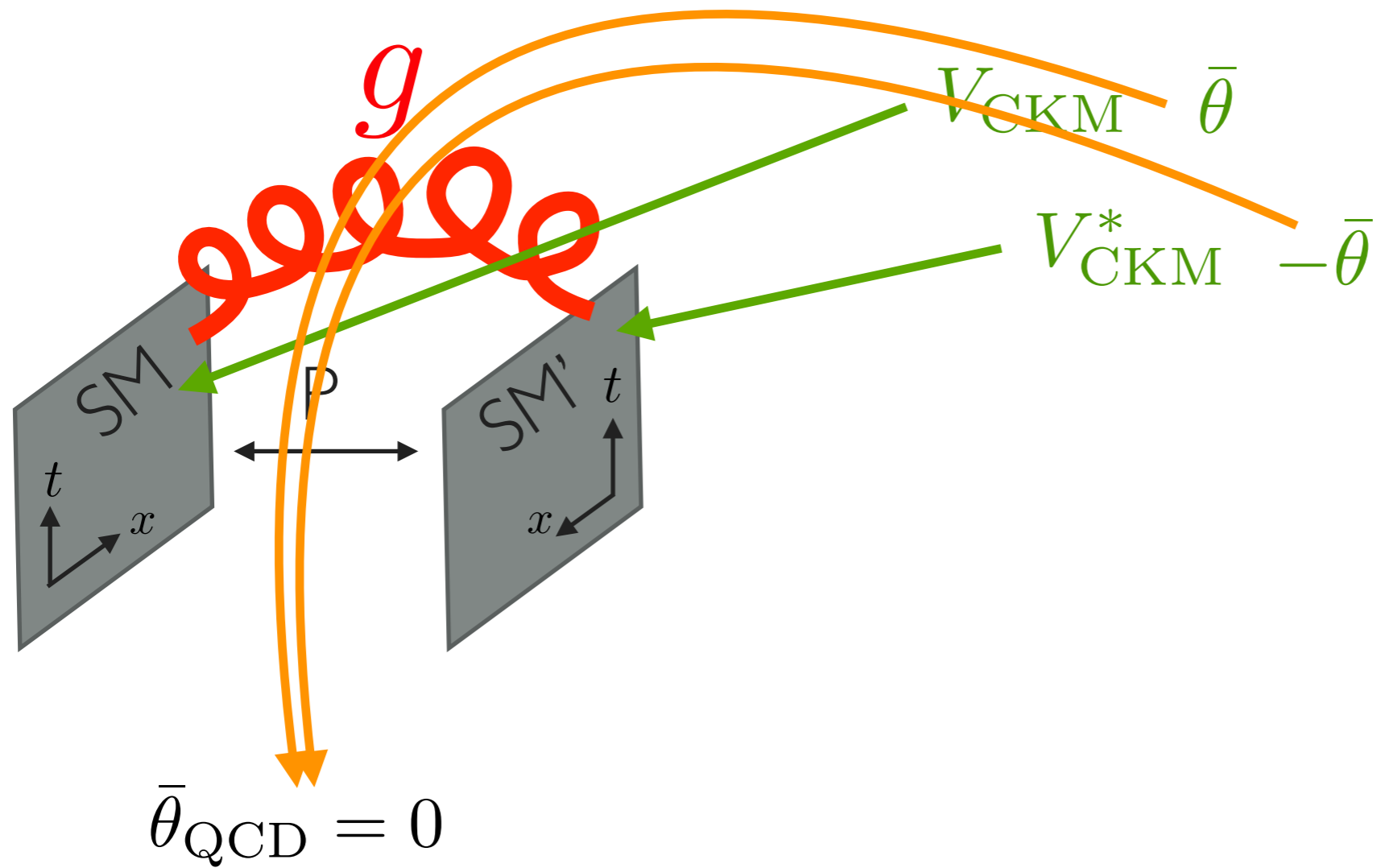


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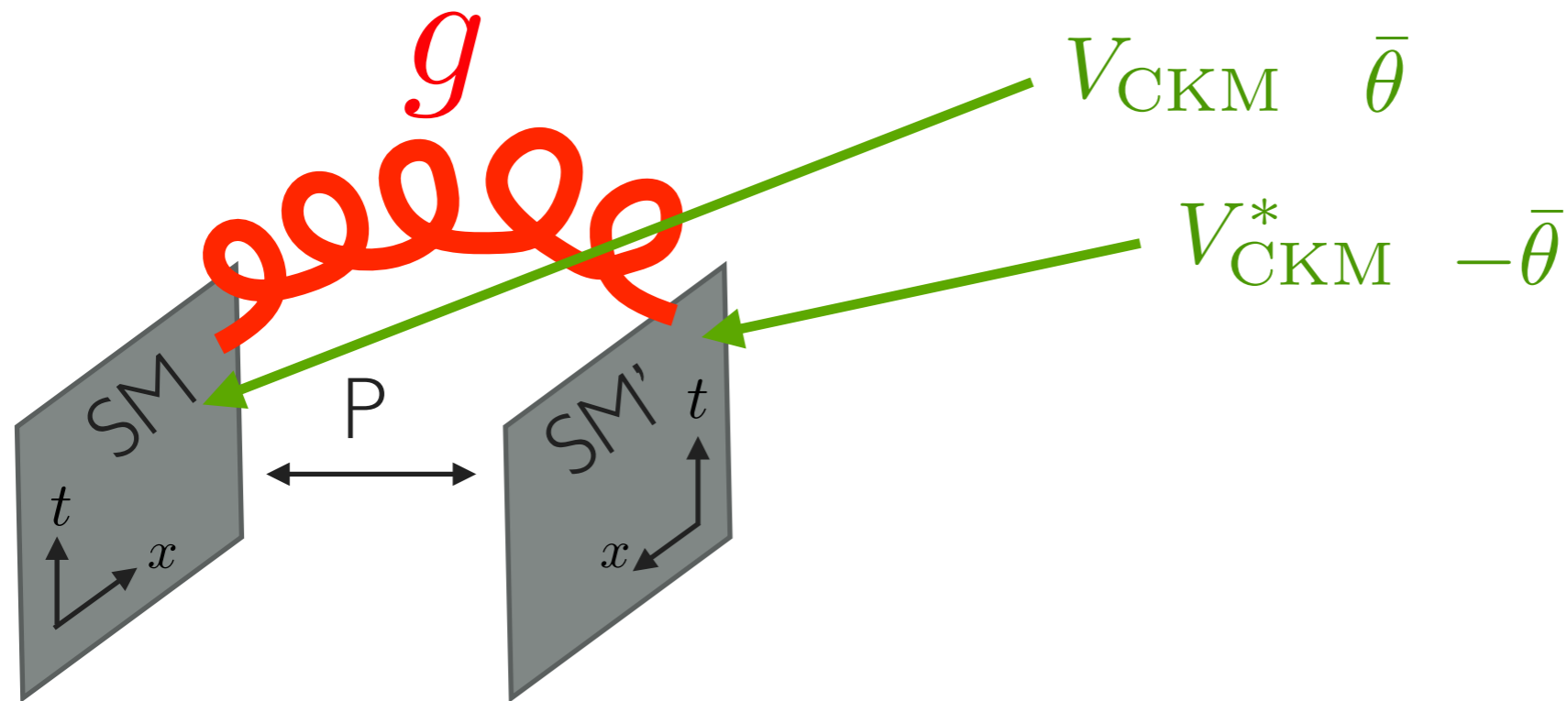


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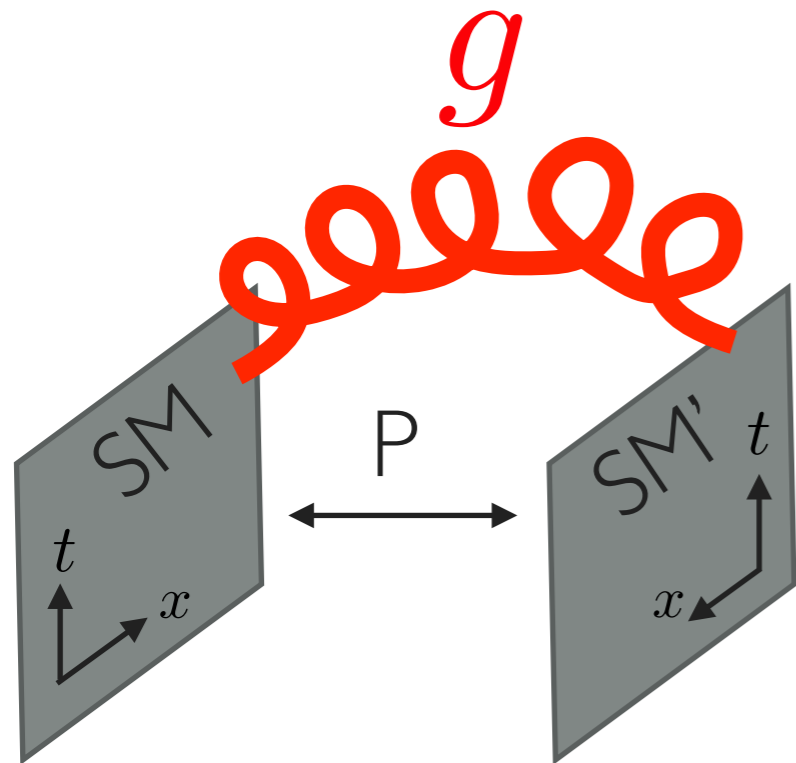
# Example 2 : mirror worlds



$\langle H \rangle \neq \langle H' \rangle$  : broken parity

$$\bar{\theta}_{\text{QCD}} = 0$$

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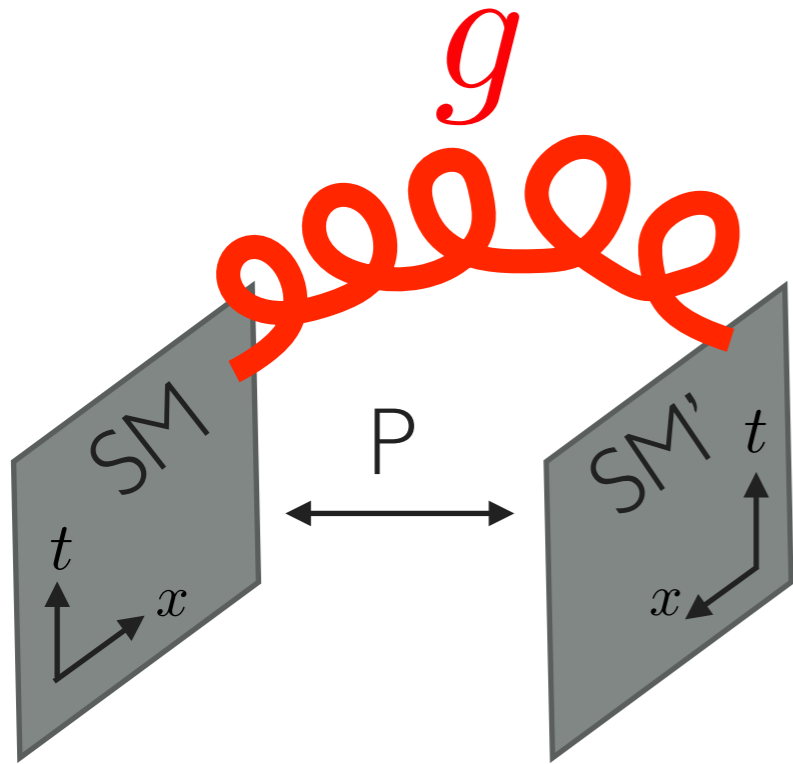
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Can have TeV scale pheno  
(colored vector-like fermions,  
RH-coupled gauge fields, ...)

[D'Agnolo/Hook '15,  
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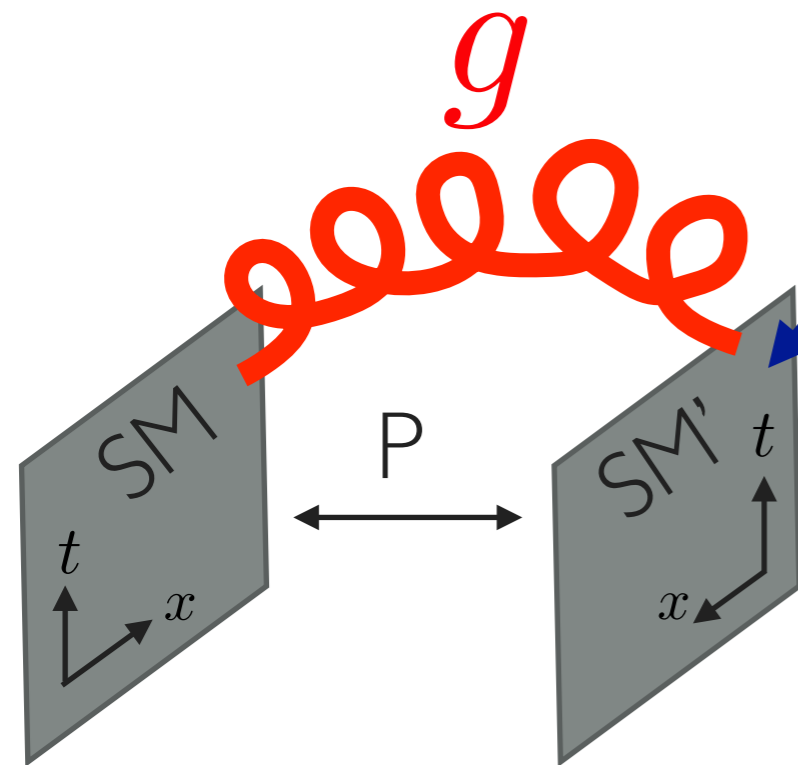
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But the mechanism works even  
when  $\langle H' \rangle$  is quite high ...  
**experimental probes ?**

Generically : only a (computable)  
large-ish neutron EDM.

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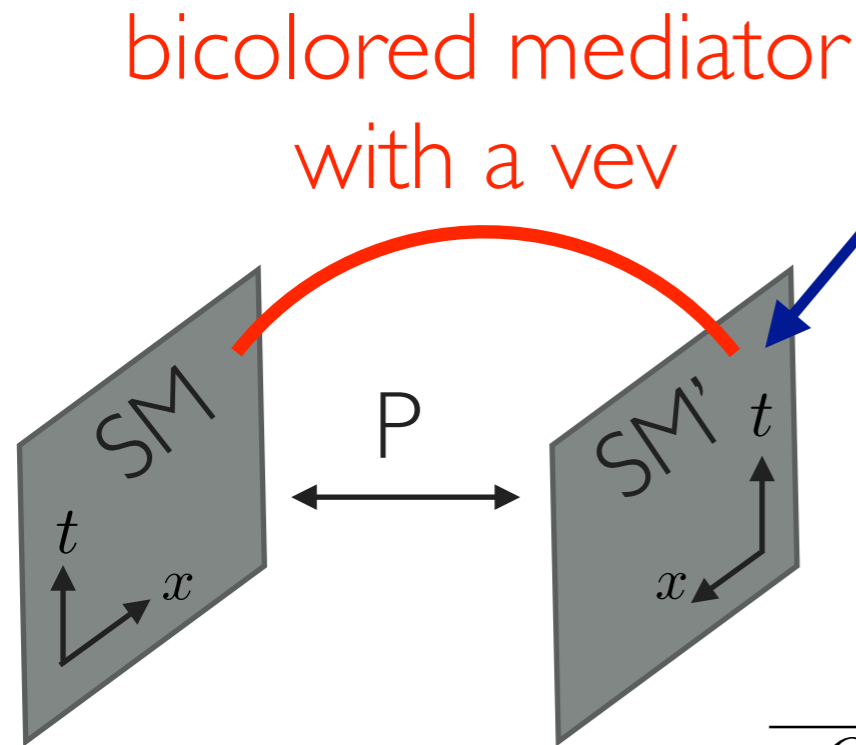
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[Dunsky/Hall/Harigaya '19]

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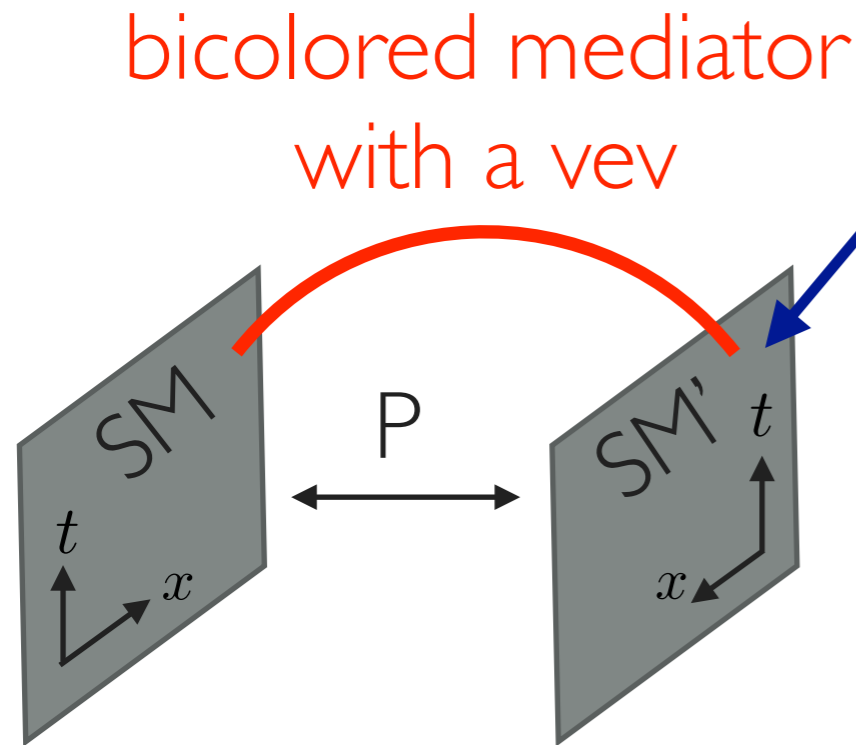


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To produce it thermally, need to embed into

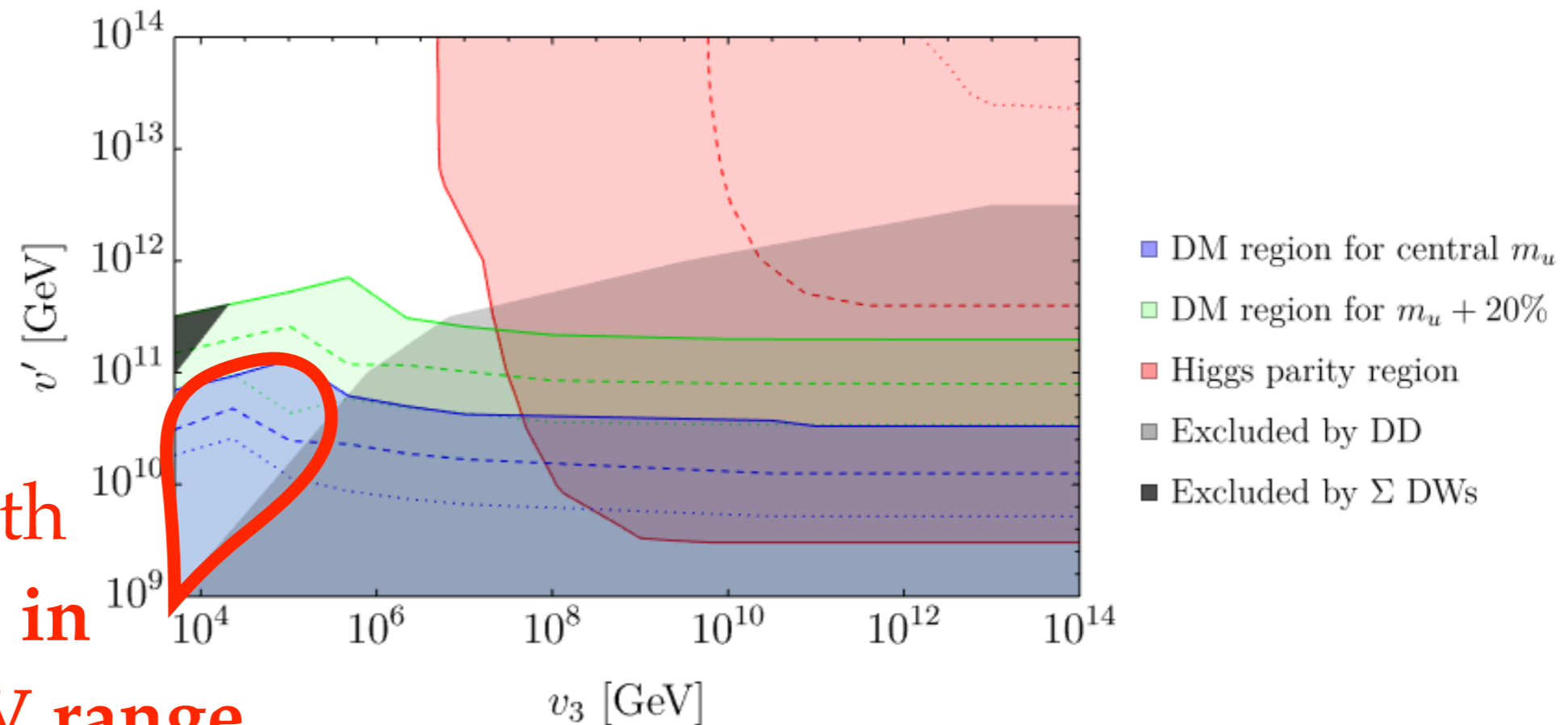
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$u^c$	$\bar{\mathbf{3}}$	<b>1</b>	-2/3	<b>1</b>	<b>1</b>	0
$d^c$	$\bar{\mathbf{3}}$	<b>1</b>	1/3	<b>1</b>	<b>1</b>	0
$L$	<b>1</b>	<b>2</b>	-1/2	<b>1</b>	<b>1</b>	0
$e^c$	<b>1</b>	<b>1</b>	-1	<b>1</b>	<b>1</b>	0
$H$	<b>1</b>	<b>2</b>	1/2	<b>1</b>	<b>1</b>	0
$Q'$	<b>1</b>	<b>1</b>	0	$\bar{\mathbf{3}}$	<b>2</b>	-1/6
$u'^c$	<b>1</b>	<b>1</b>	0	<b>3</b>	<b>1</b>	2/3
$d'^c$	<b>1</b>	<b>1</b>	0	<b>3</b>	<b>1</b>	-1/3
$L'$	<b>1</b>	<b>1</b>	0	<b>1</b>	<b>2</b>	1/2
$e'^c$	<b>1</b>	<b>1</b>	0	<b>1</b>	<b>1</b>	1
$H'$	<b>1</b>	<b>1</b>	0	<b>1</b>	<b>2</b>	-1/2

# Example 2 : mirror worlds



There is a **dark matter candidate** here, the mirror electron

To produce it thermally, now **not all  $\langle H' \rangle$  work !**



Viable region, with  
colored particles in  
the TeV - 100 TeV range



# Outlook

The strong CP problem is usually associated to low-energy probes (or very high-energy ones, usually in cosmology)

Not the case for « **UV** » **solutions to the problem, which may manifest themselves around the TeV**: the strong CP problem can thus be investigated at those scales

A lot of work remains to be done regarding this (old) non-axion paradigm ! Rich interplay with collider and flavor physics, but also cosmology, the hierarchy problem, etc