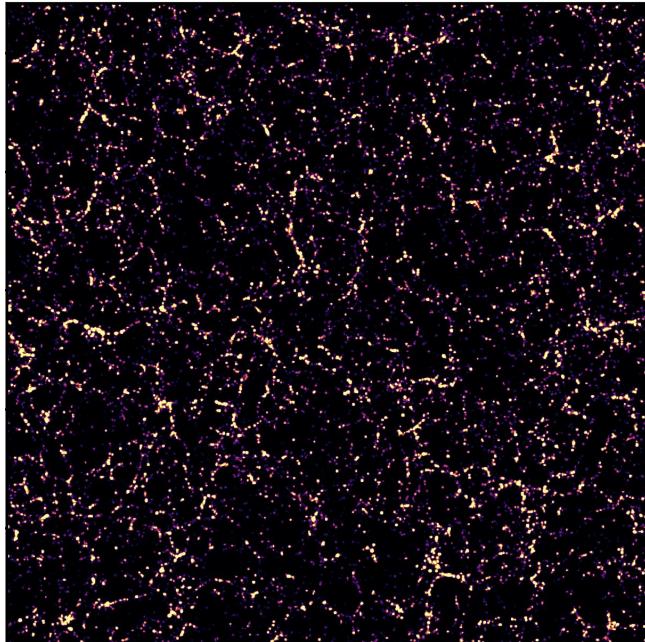




Leon Noble  
Indian Institute of Technology Indore (IIT Indore)

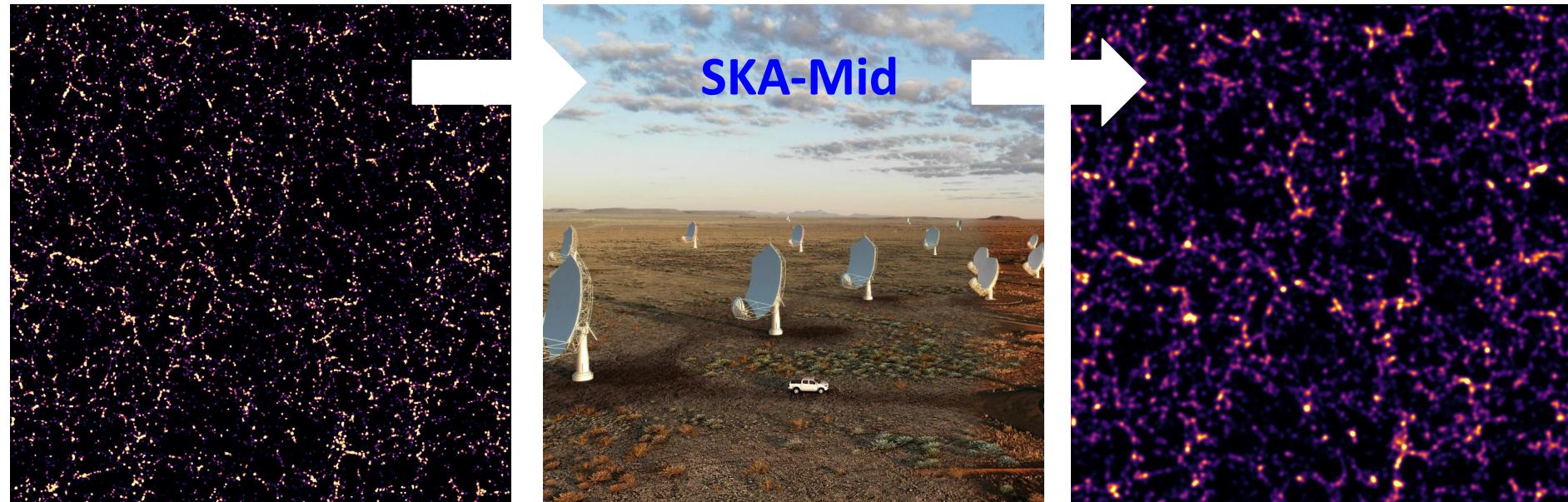
**Collaborators:** Suman Majumdar (IITI), Matteo Viel (SISSA Trieste), Fabio Fontanot (INAF Trieste),  
Gabriella De Lucia (INAF Trieste), Marta Spinelli (Observatoire de la Côte d'Azur Nice)

# Large Scale Structure with HI Intensity Mapping



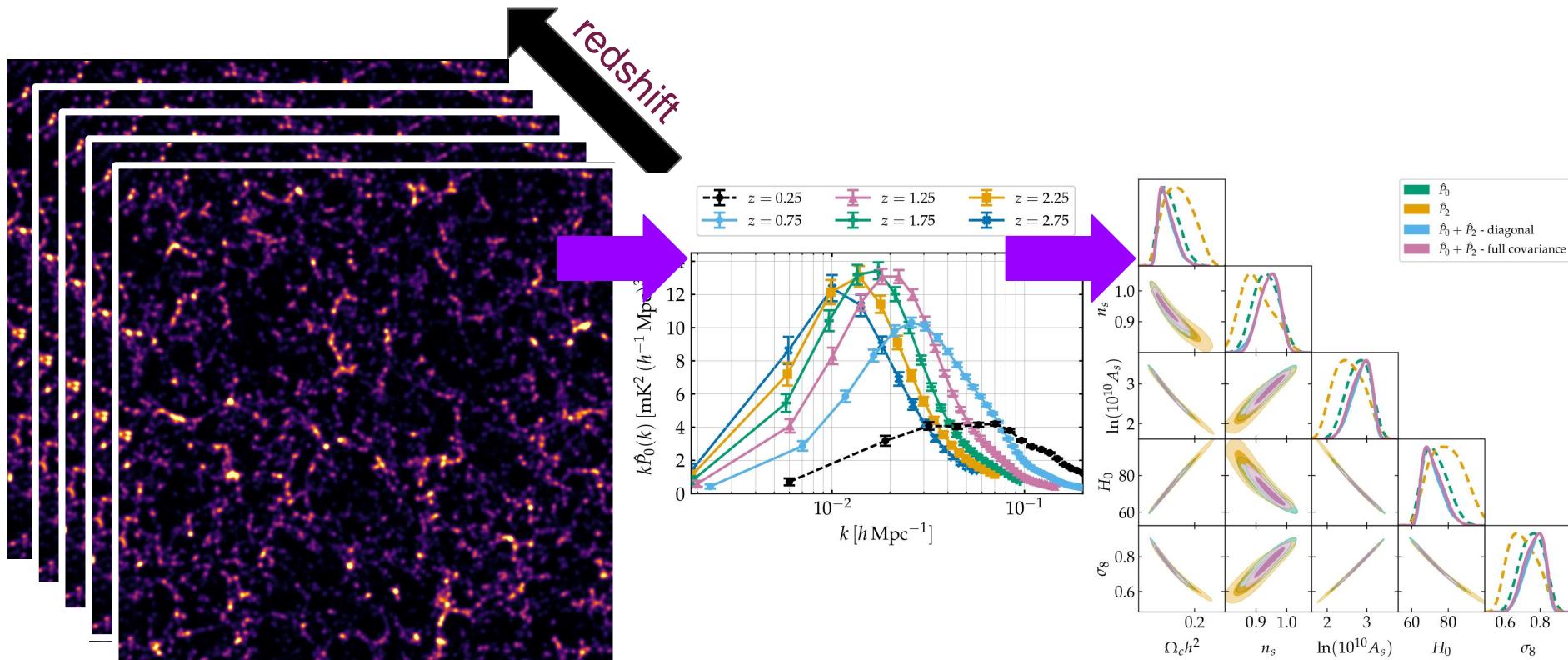
Distribution of **neutral Hydrogen (HI)** is  
biased tracer of **matter clustering**

# HI Line Intensity Mapping

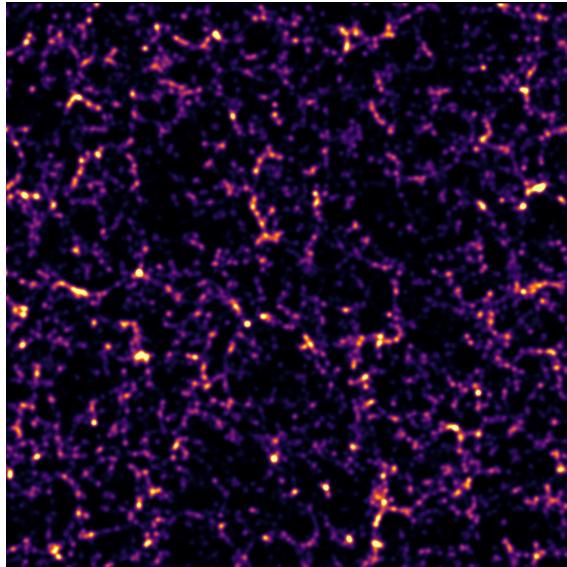


HI LIM with SKA -> key Cosmological probe

# Cosmology with HI LIM



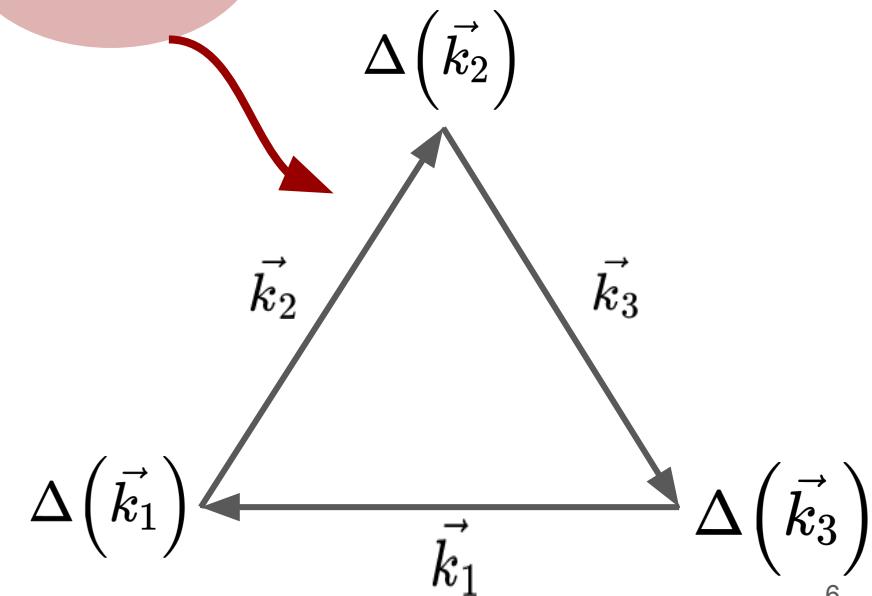
# Late Universe is not Gaussian



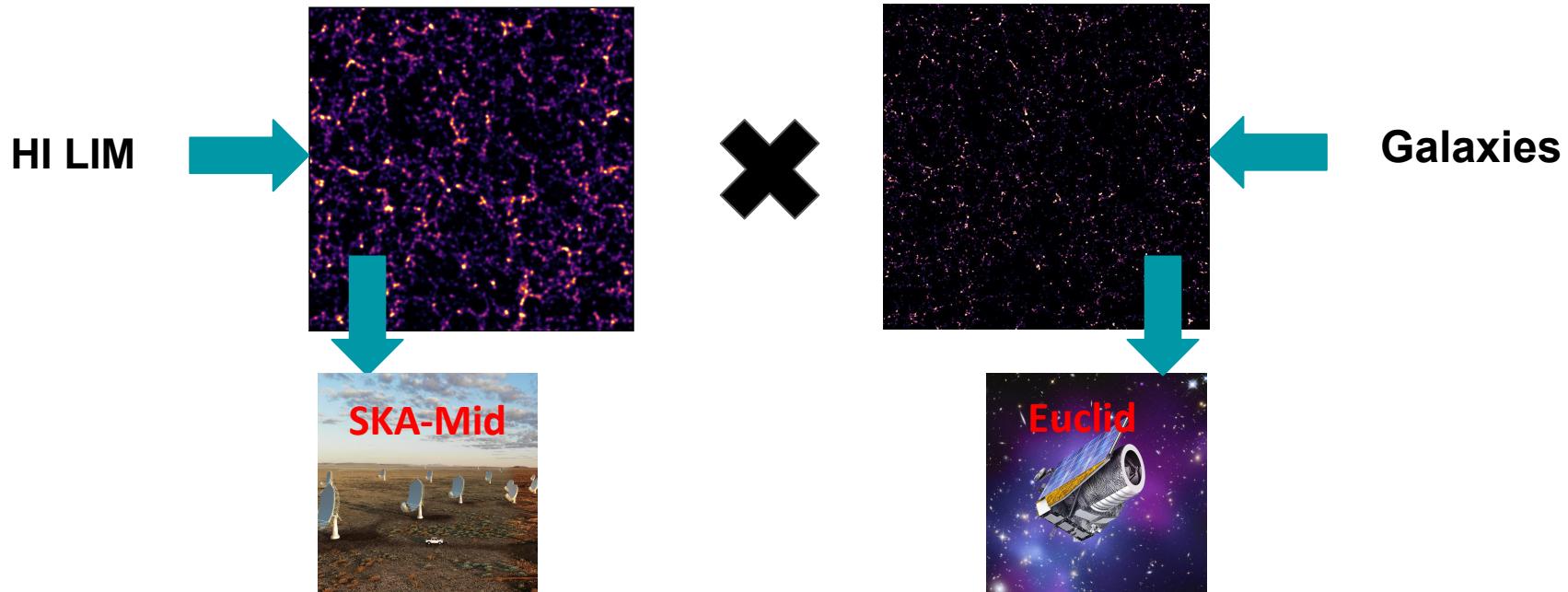
Redshifted **21cm signal** from the post-EoR is **non-Gaussian**  
due to non-linear clustering of matter

# Non-Gaussian Statistics: Bispectrum

$$\langle \Delta(\vec{k}_1) \Delta(\vec{k}_2) \Delta(\vec{k}_3) \rangle = V \delta^K_{\vec{k}_1 + \vec{k}_2 + \vec{k}_3, 0} B(\vec{k}_1, \vec{k}_2, \vec{k}_3)$$



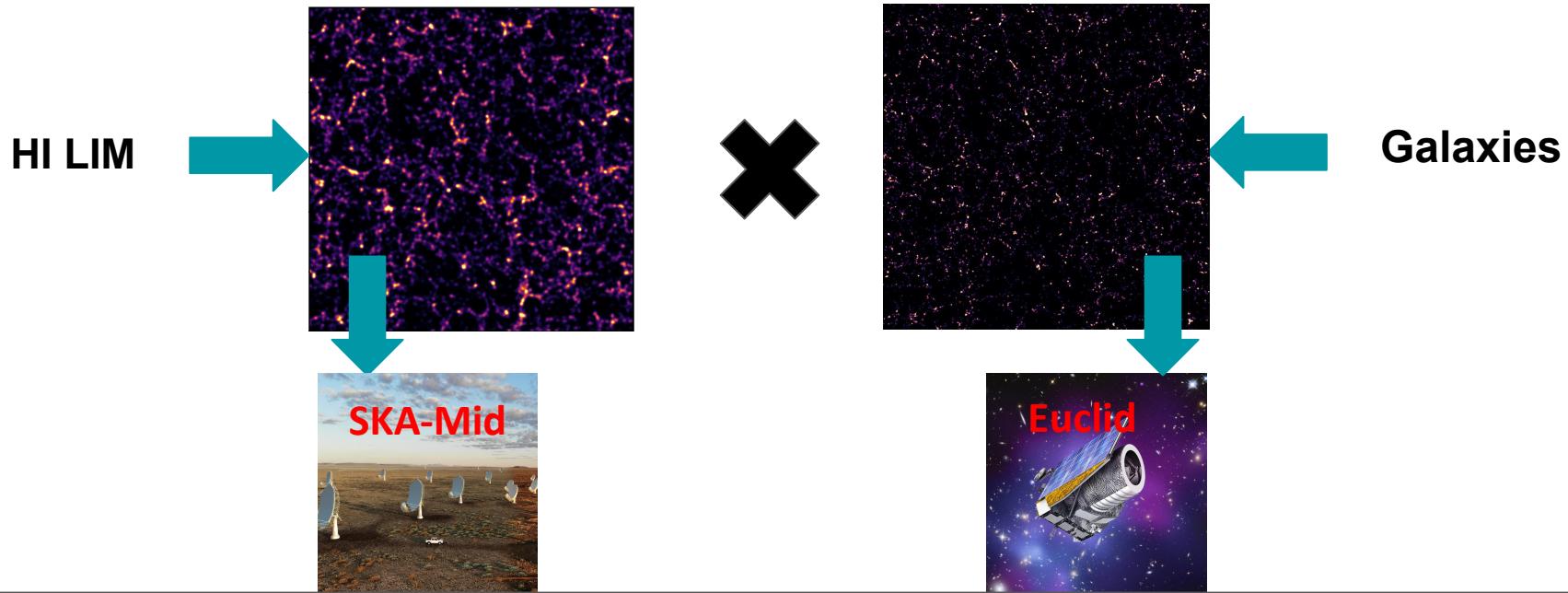
# 21cm-galaxy cross-correlation



Cross-correlation in the redshift range **0.84 - 1.88**

Cross-correlation might allow us to obtain higher SNR  
compared autocorrelation which is severely affected by systematics

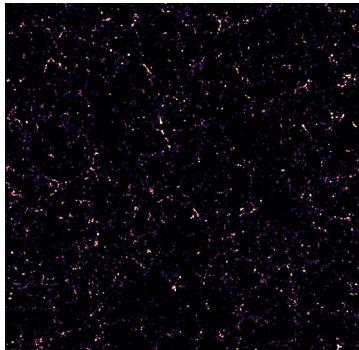
# 21cm-galaxy clustering cross-bispectrum



- Test the **detectability** of 21cm-galaxy cross-bispectrum with SKA-Mid and Euclid.
- Does 21cm-galaxy cross-bispectrum put **tighter constraints** on Cosmological parameters?

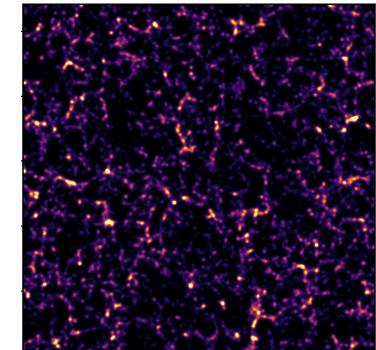
# Simulations

Mock Galaxy  
Catalogue



P-Millennium  
+  
GAEA  
**Semi-analytic galaxy  
formation model**  
(Fontanot et al. 2025)

HI LIM

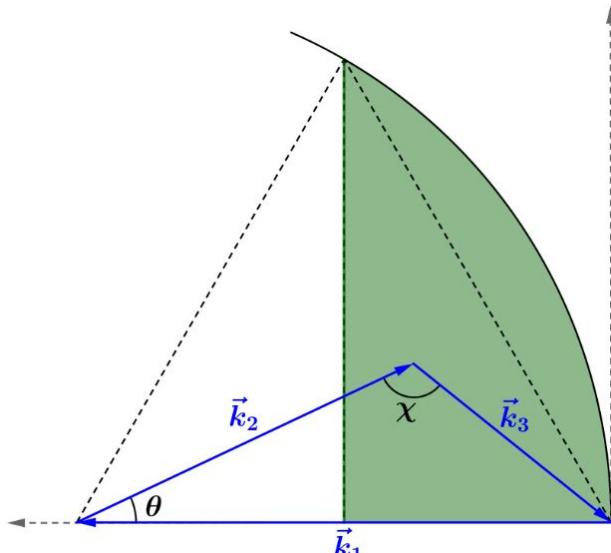


# Unique triangles in the Fourier space

$$k_1 \geq k_2 \geq k_3$$

$$0.5 \leq \cos(\theta) \leq 1$$

$$0.5 \leq k_2/k_1 \leq 1$$



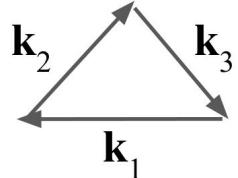
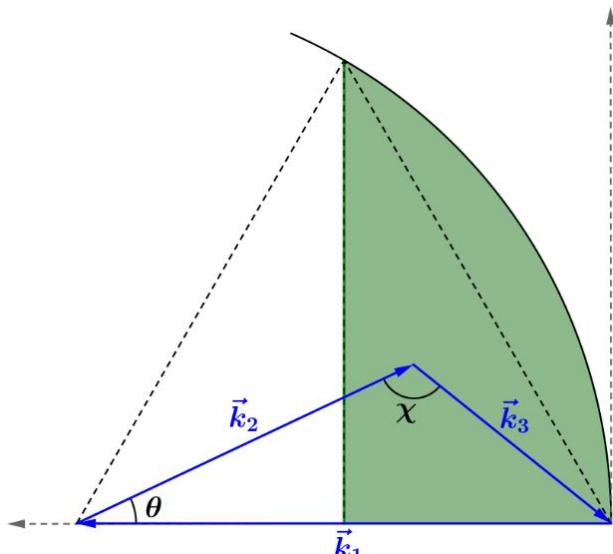
Bharadwaj S. et al. 2020, MNRAS, 493, 594.  
Majumdar S. et al. 2020, MNRAS, 499, 5090.

# Unique triangles in the Fourier space

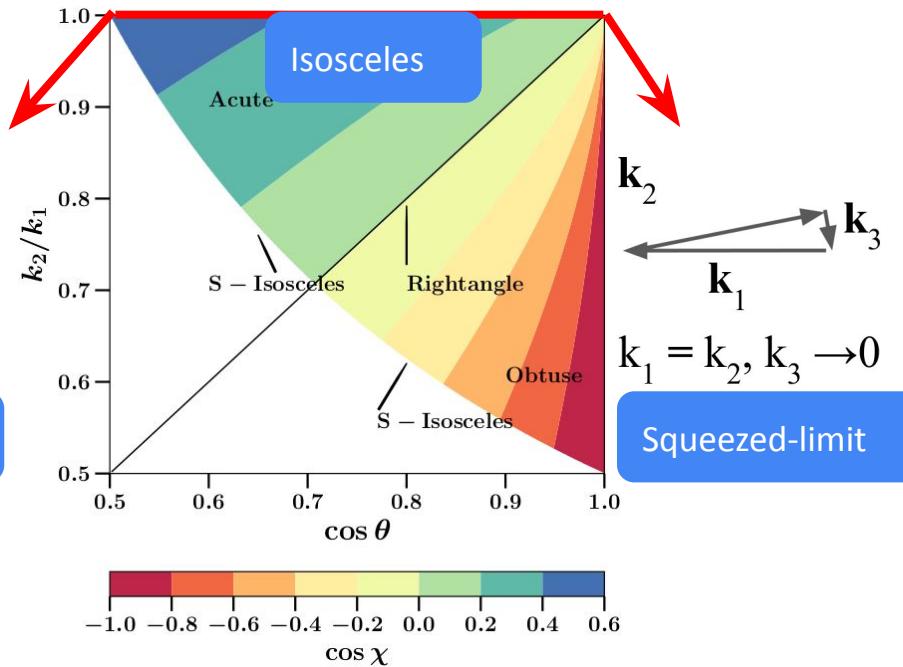
$$k_1 \geq k_2 \geq k_3$$

$$0.5 \leq \cos(\theta) \leq 1$$

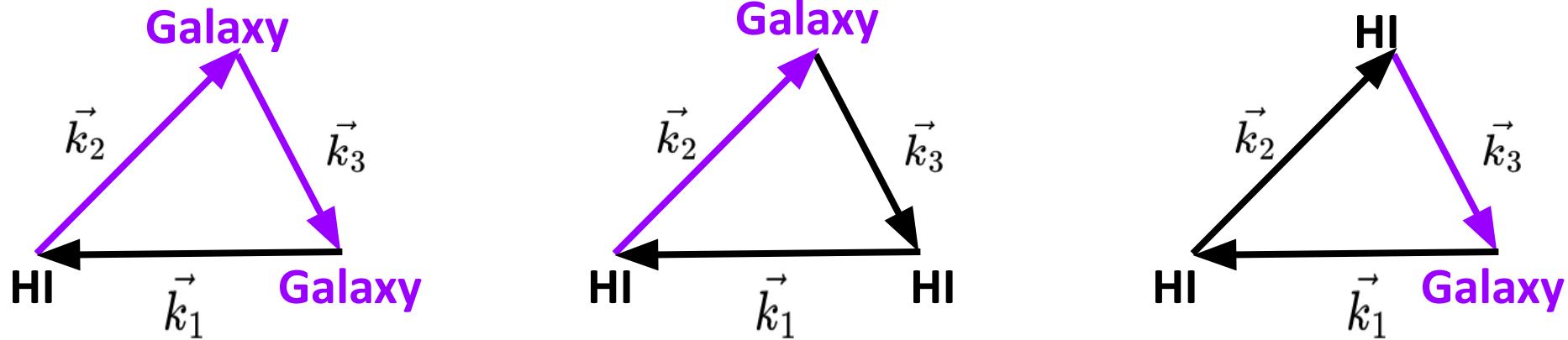
$$0.5 \leq k_2/k_1 \leq 1$$



Equilateral



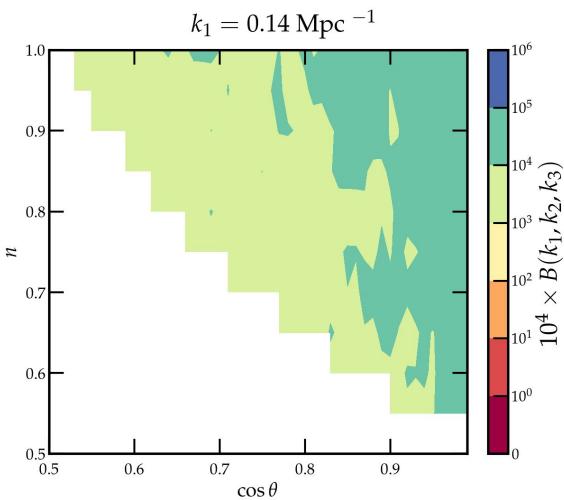
## HI LIM-galaxy cross bispectrum



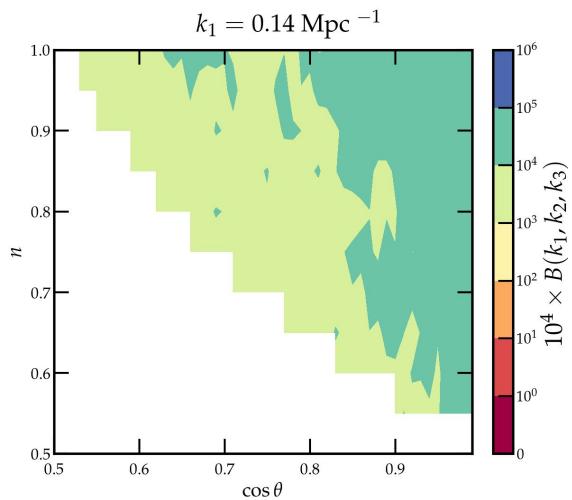
$$\langle \Delta(\vec{k}_1) \Delta(\vec{k}_2) \Delta(\vec{k}_3) \rangle = V \delta^K_{\vec{k}_1 + \vec{k}_2 + \vec{k}_3, 0} B(\vec{k}_1, \vec{k}_2, \vec{k}_3)$$

A lot to choose from — **triangle shapes, size and cross-combinations....**

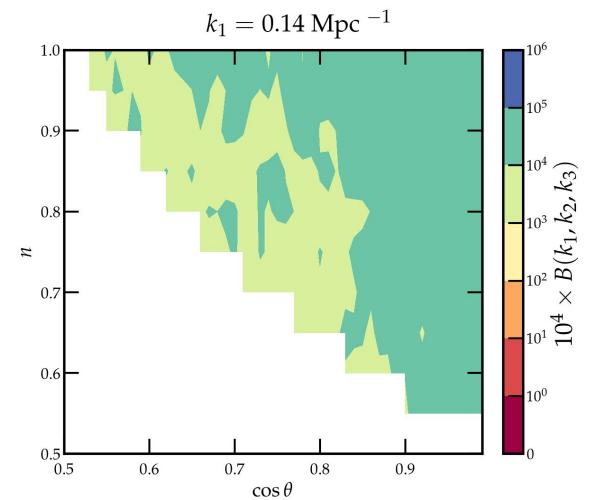
# HI LIM-galaxy cross bispectrum



HI-HI-Gal

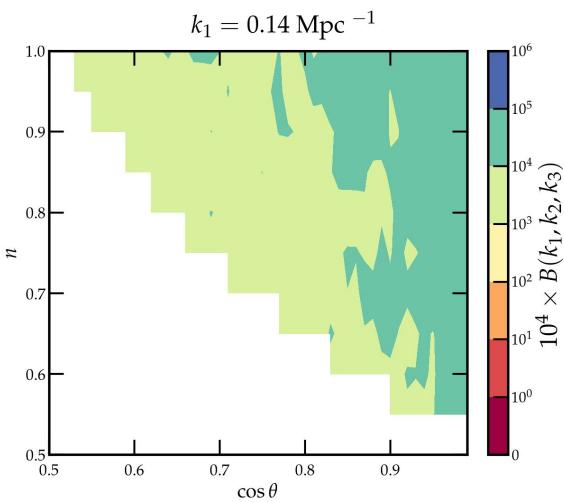


HI- Gal-HI

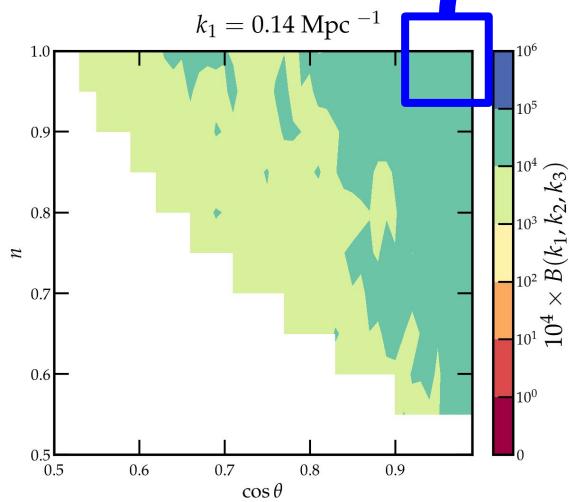


HI-Gal-Gal

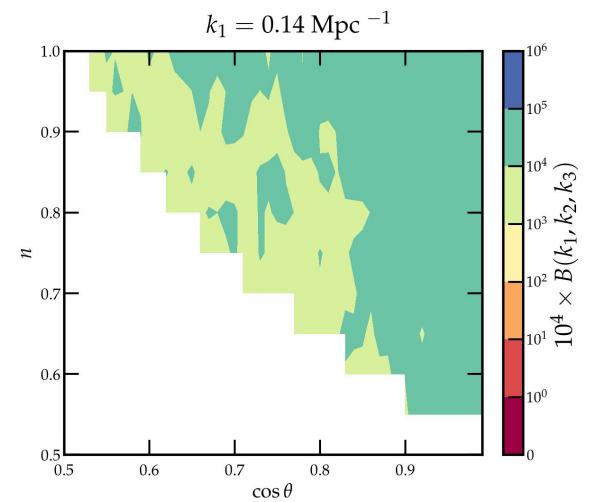
# HI LIM-galaxy cross bispectrum



HI-HI-Gal



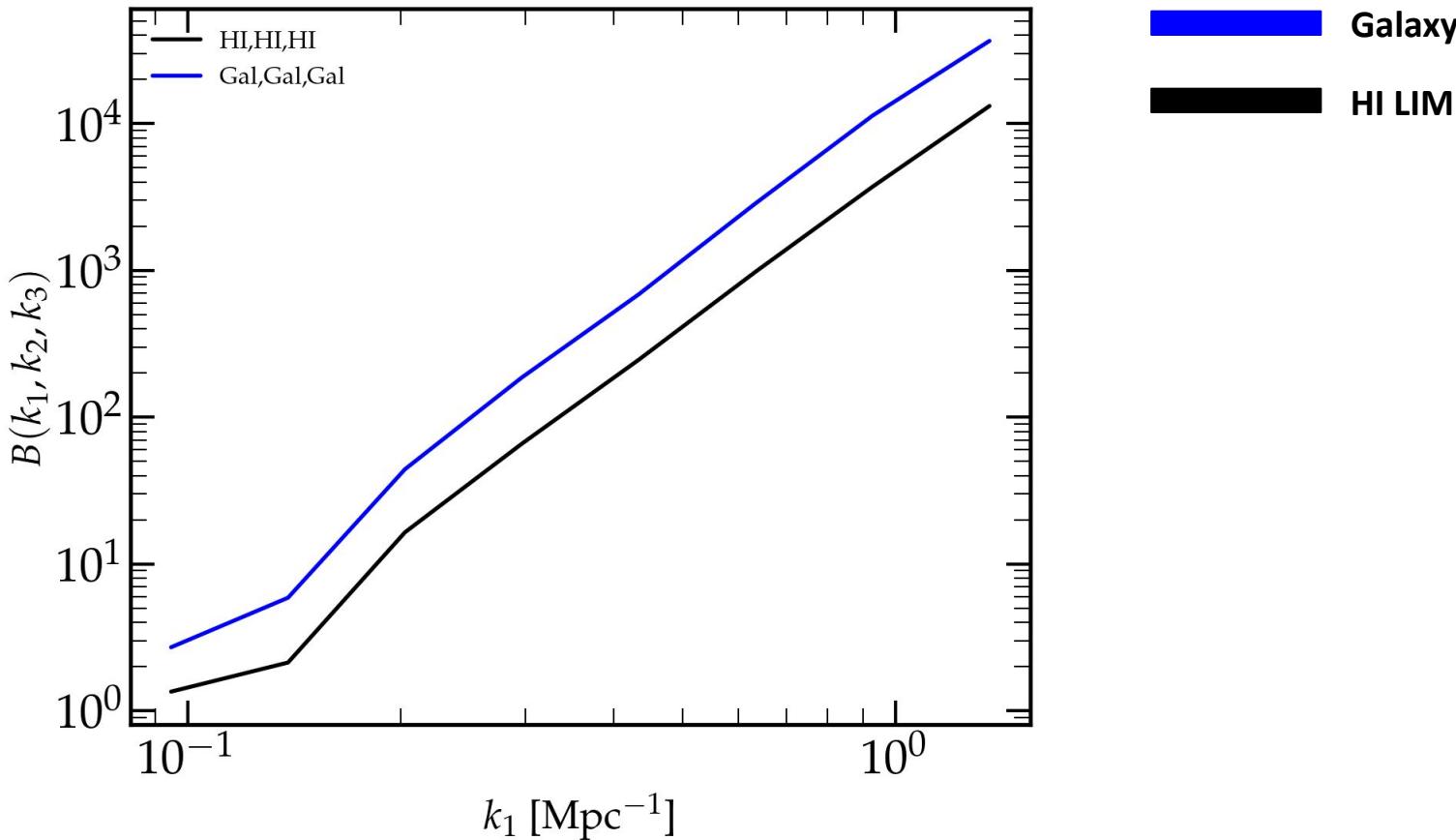
HI- Gal-HI



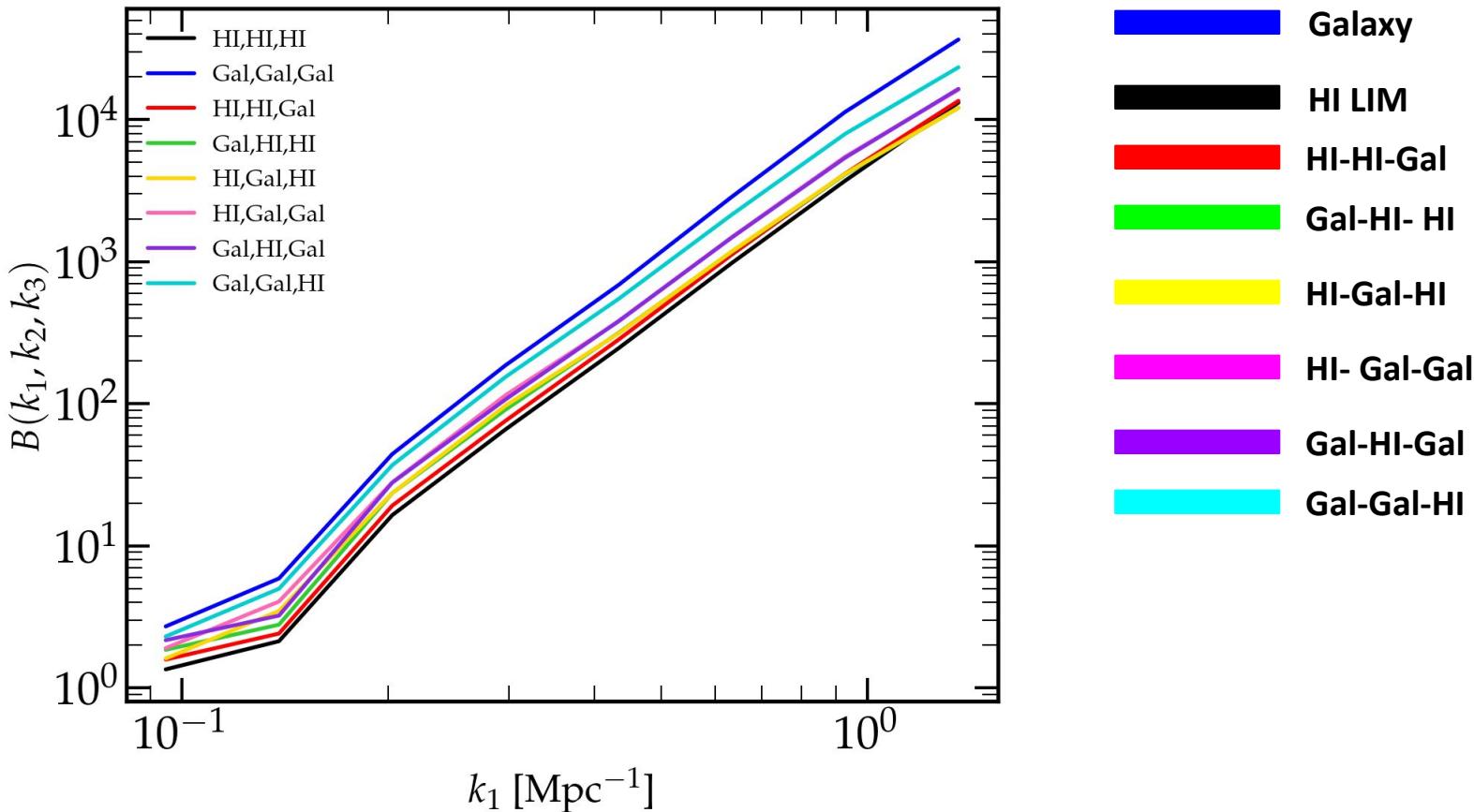
HI-Gal-Gal

$\mathbf{k}_2$   
 $\mathbf{k}_3$   
 $\mathbf{k}_1$   
 $k_1 = k_2, k_3 \rightarrow 0$   
Squeezed

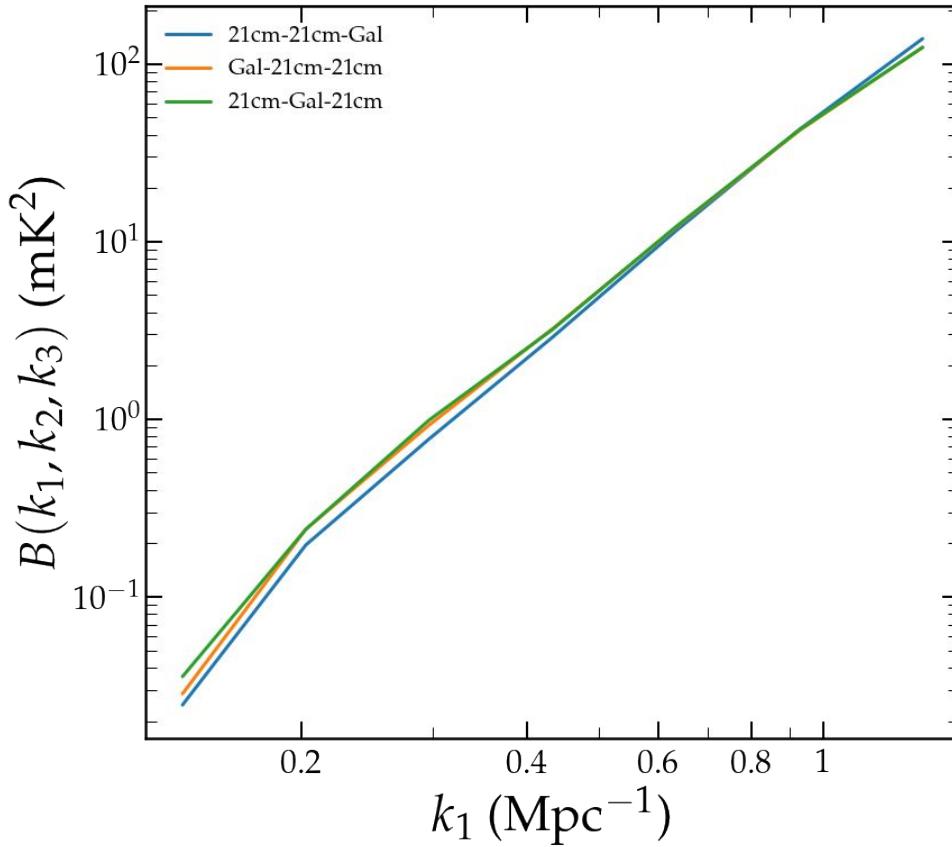
# Squeezed-limit bispectrum



# Squeezed-limit bispectrum



# Squeezed-limit bispectrum

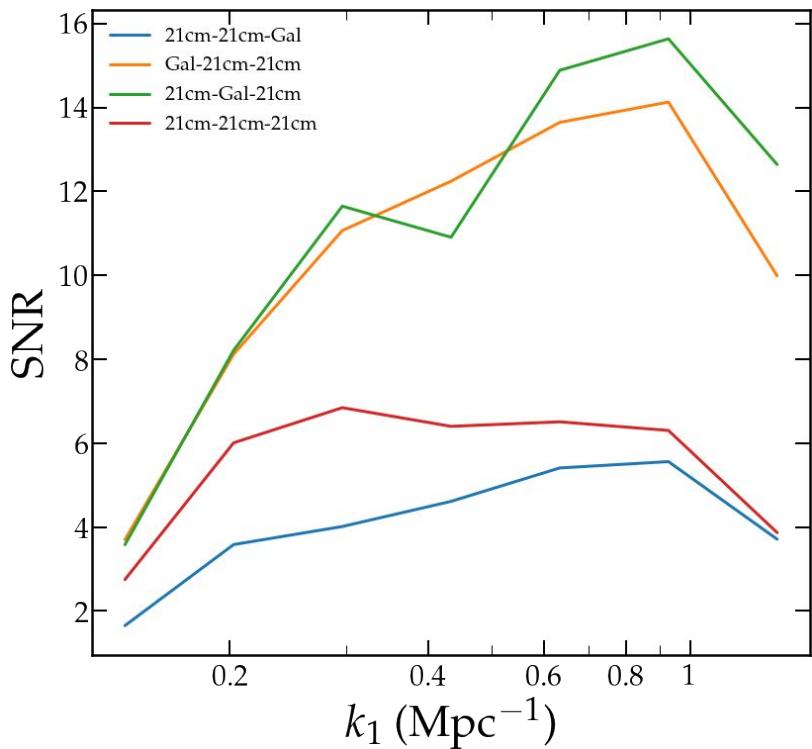


**21cm-21cm-Gal**

**Gal-21cm-21cm**

**21cm-Gal-21cm**

# Detectability of cross-bispectrum: Squeezed-limit

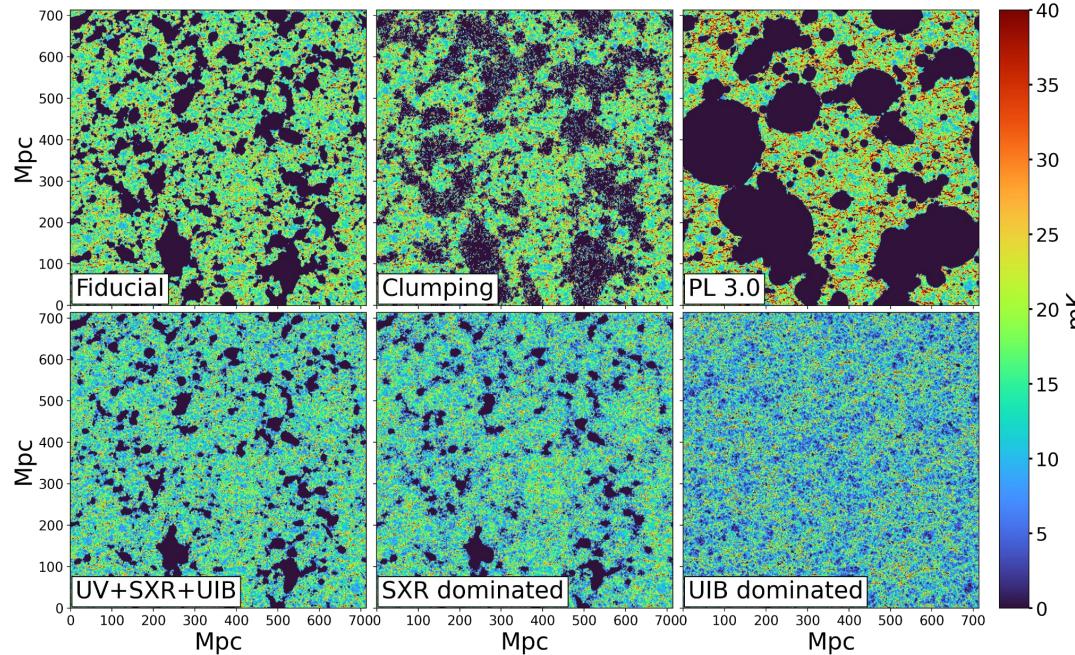


Gal-21cm-Gal  
 21cm-Gal-21cm

1000 hours of SKA-Mid  
observations

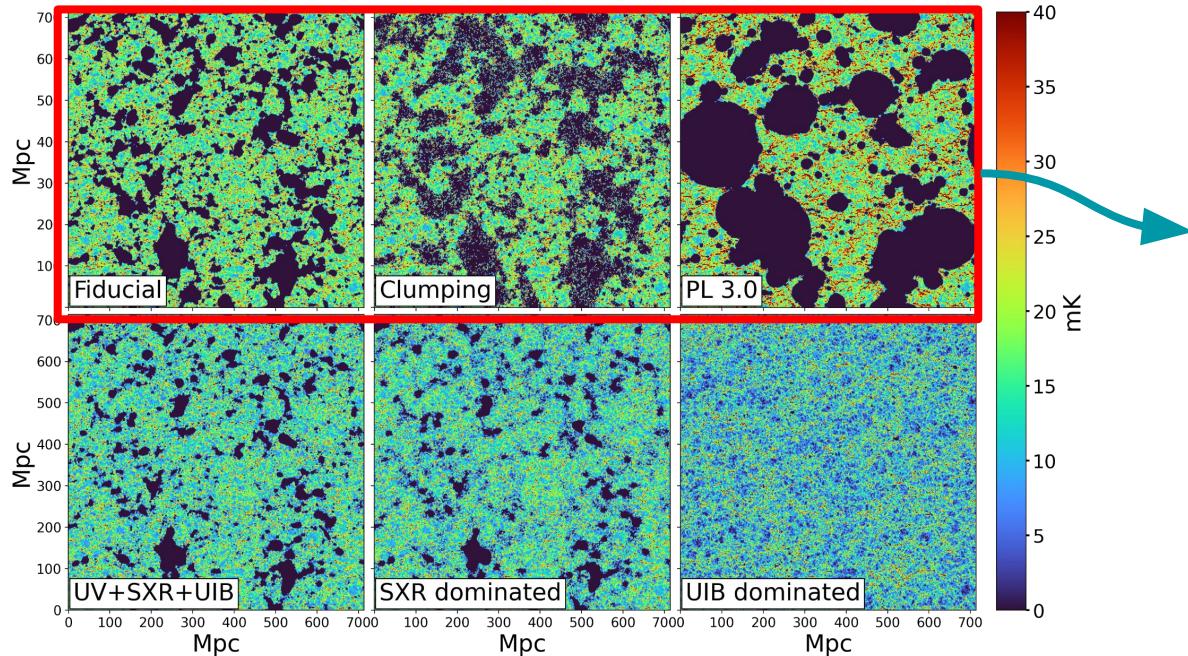
**PRELIMINARY**

# Impact of the sources of reionization on the 21-cm bispectrum



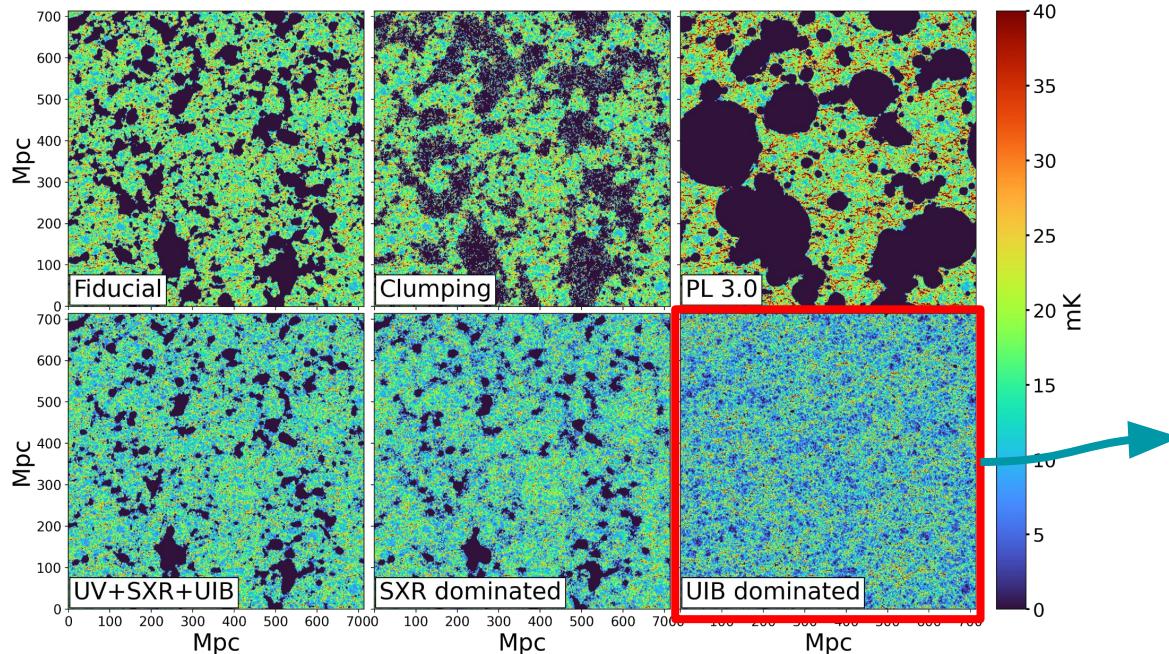
- Impact of various **reionization morphologies** on the **21-cm bispectrum**
- To what extent the **21-cm bispectrum** can distinguish between different reionization morphologies

# Reionization scenarios



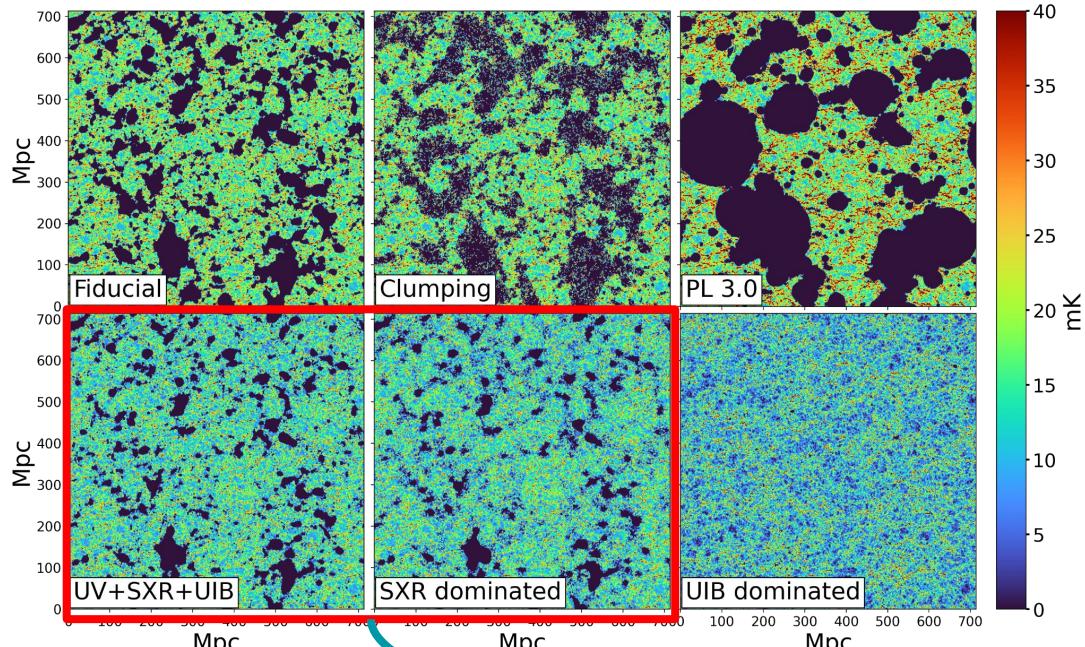
Inside-out reionization  
scenarios

# Reionization scenarios



Outside-in reionization scenario

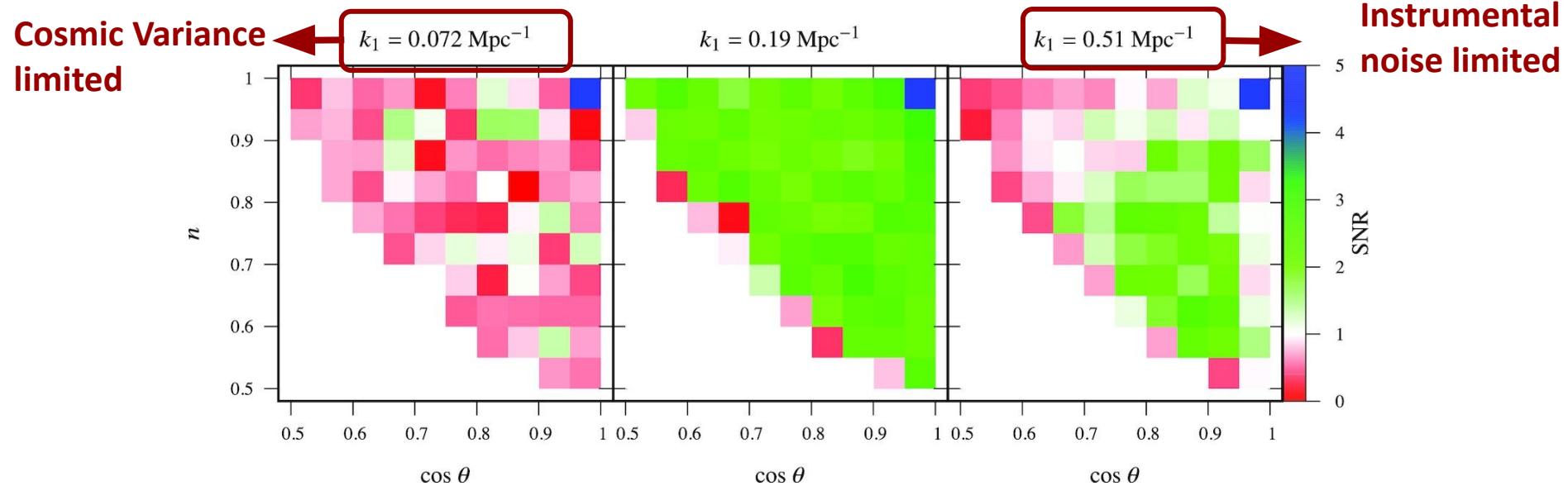
# Reionization scenarios



Combination of **inside-out** and **outside-in**

Noble et al. et al JCAP 10 (2024)003

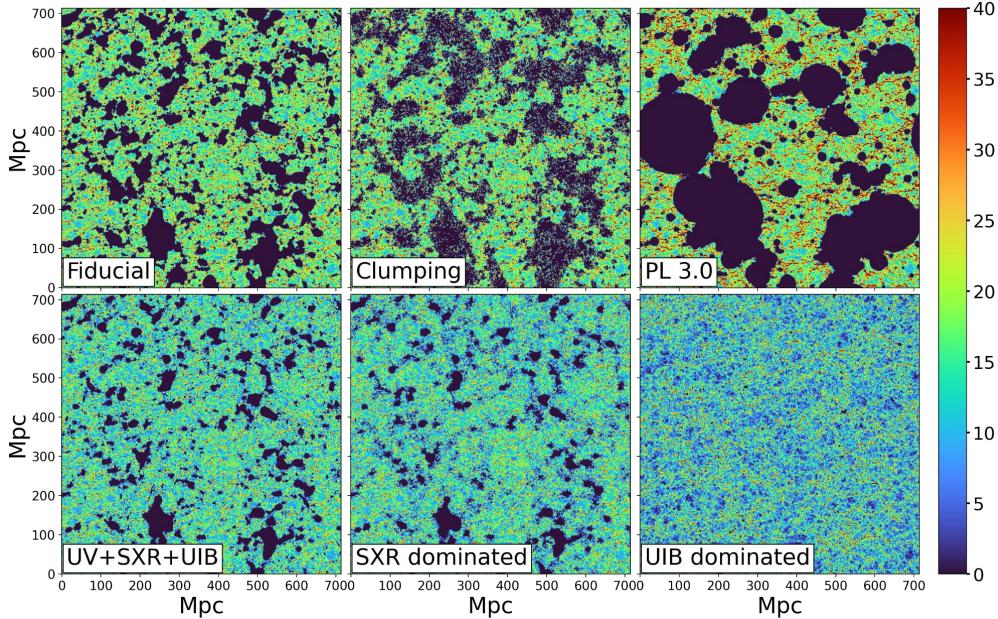
# Squeezed-limit bispectrum



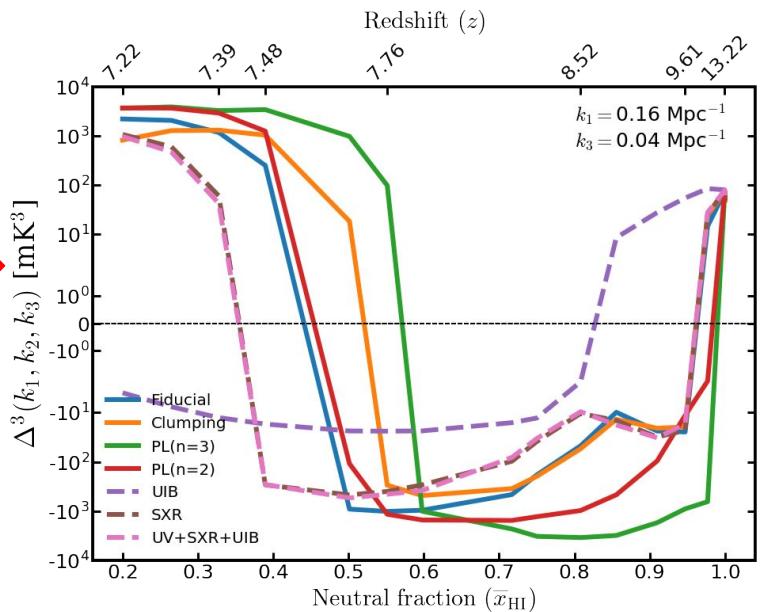
Highest detection probability by SKA (Mondal R. et al., 2021, MNRAS, 508, 3848.)

We will focus on large scale ( $k_1 \sim 0.16 \text{ Mpc}^{-1}$ ) squeezed limit bispectrum

# Evolution of squeezed-limit bispectrum



Noble et al. et al JCAP 10 (2024)003



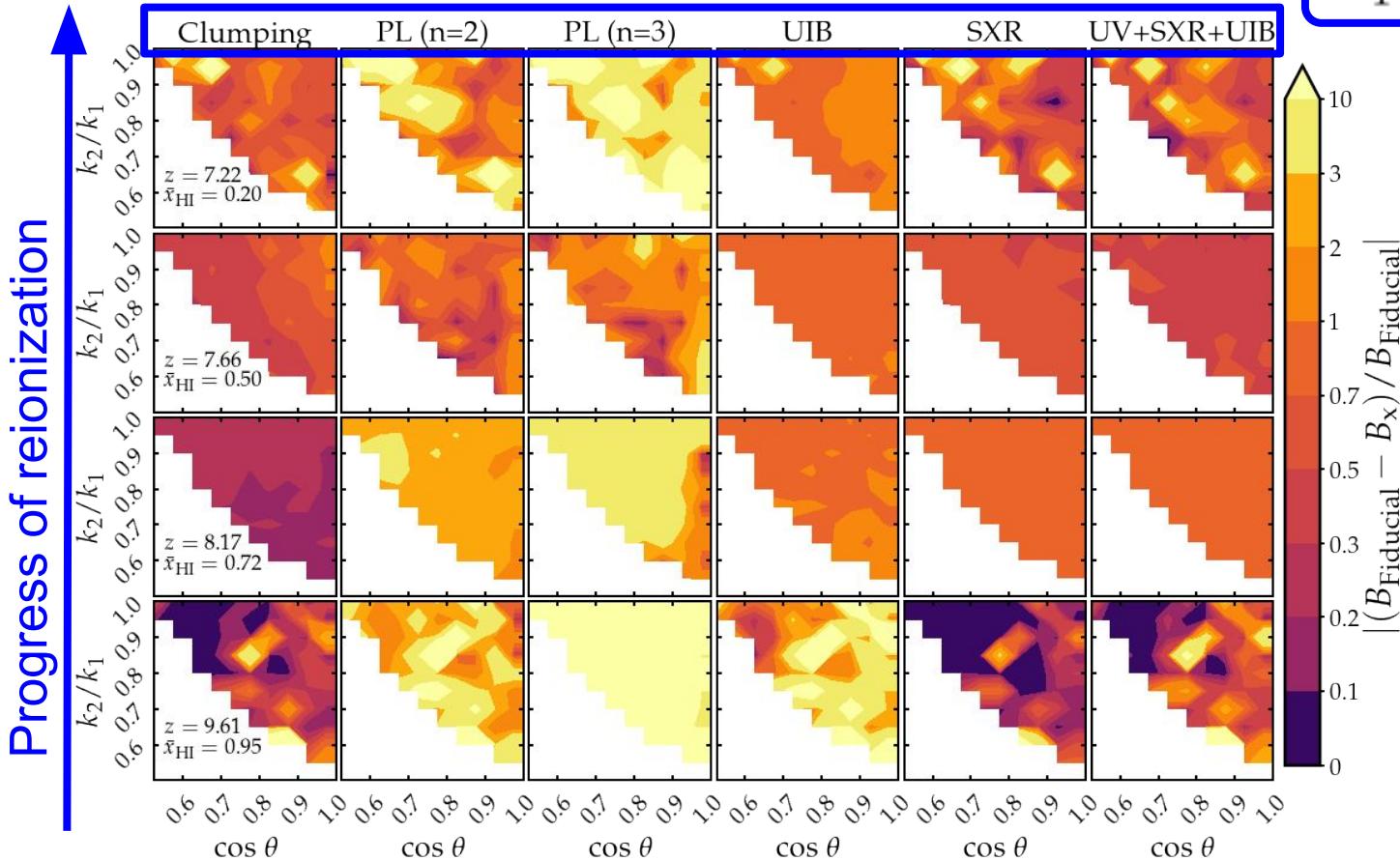
Progress of reionization

## Summary

- We are exploring the clustering of matter using 21cm-galaxy cross-bispectrum.
- Our preliminary analysis show higher detectability (SNR) for the 21cm- galaxy cross-bispectrum for squeezed-limit triangles compared to 21cm auto bispectrum.
- We are estimating the detectability of the cross-bispectrum for other shapes of k-triangles.
- EoR 21cm bispectrum can distinguish reionization morphologies.

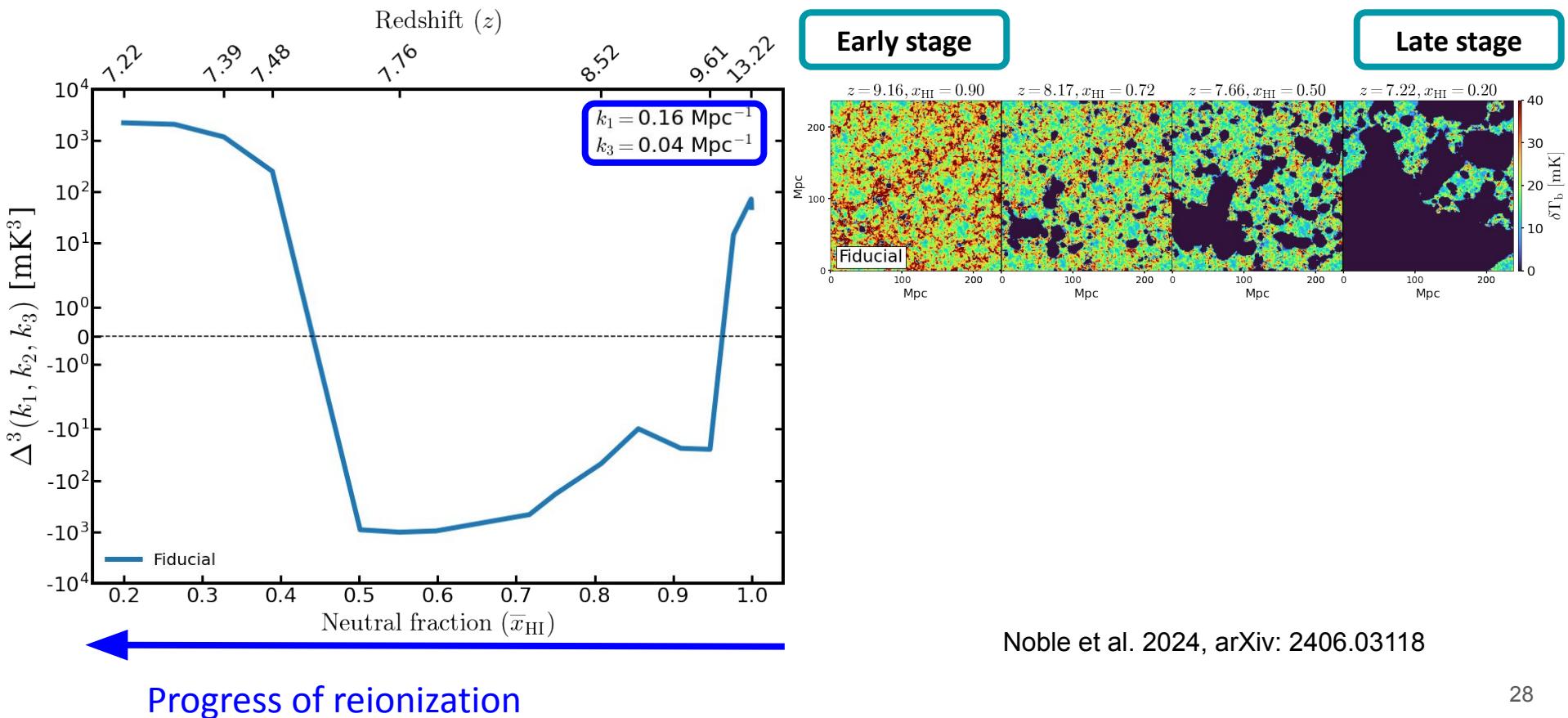


# Magnitude differences in 21-cm bispectrum between different reionization scenarios

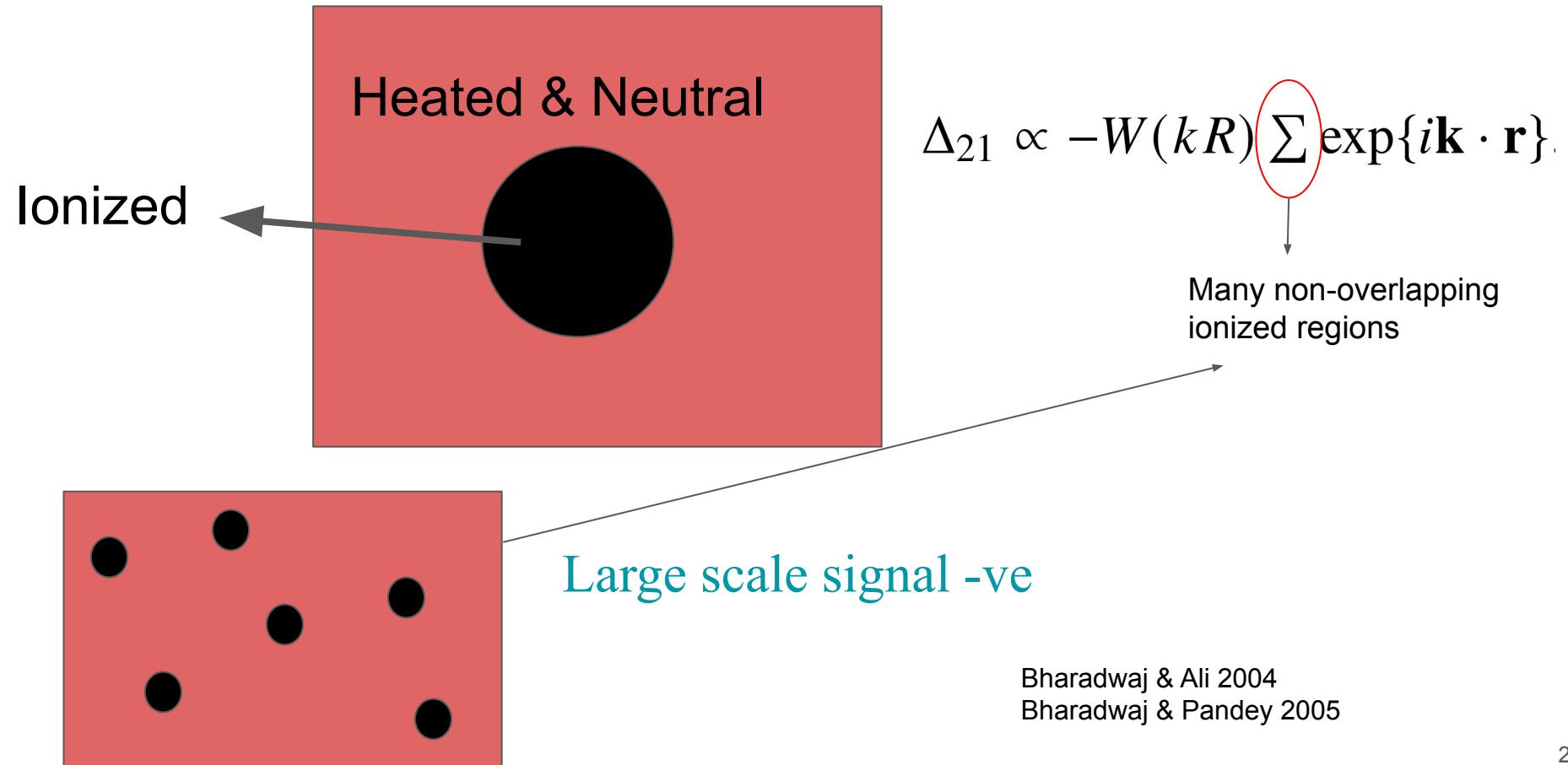


$$k_1 = 0.16 \text{ Mpc}^{-1}$$

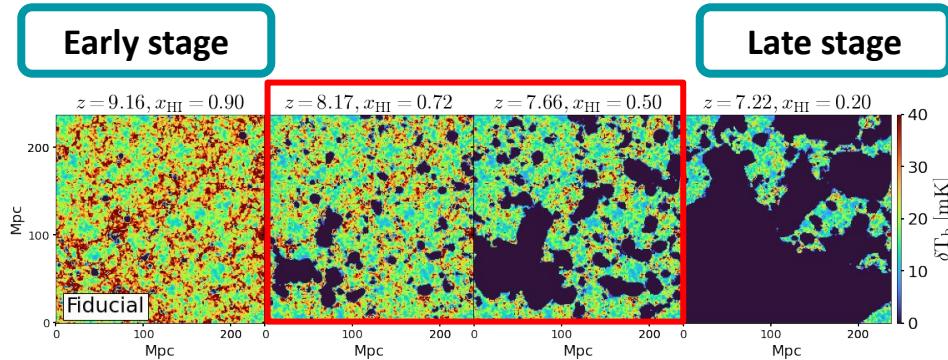
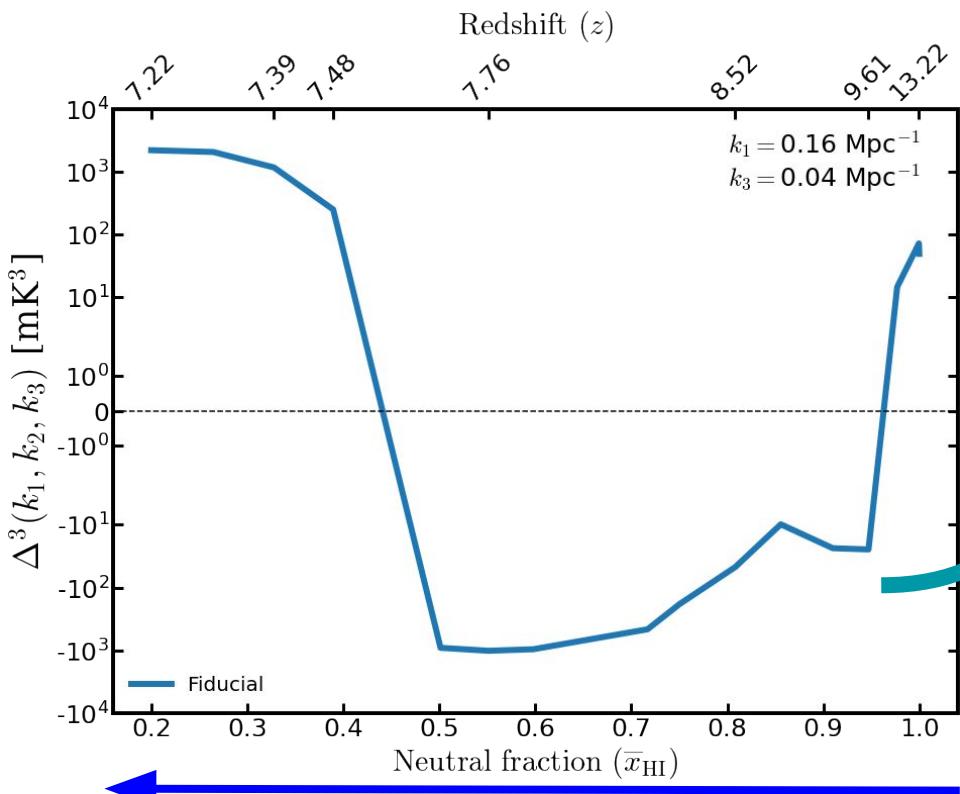
# Evolution of squeezed-limit bispectrum



# Interpretation



# Evolution of squeezed-limit bispectrum

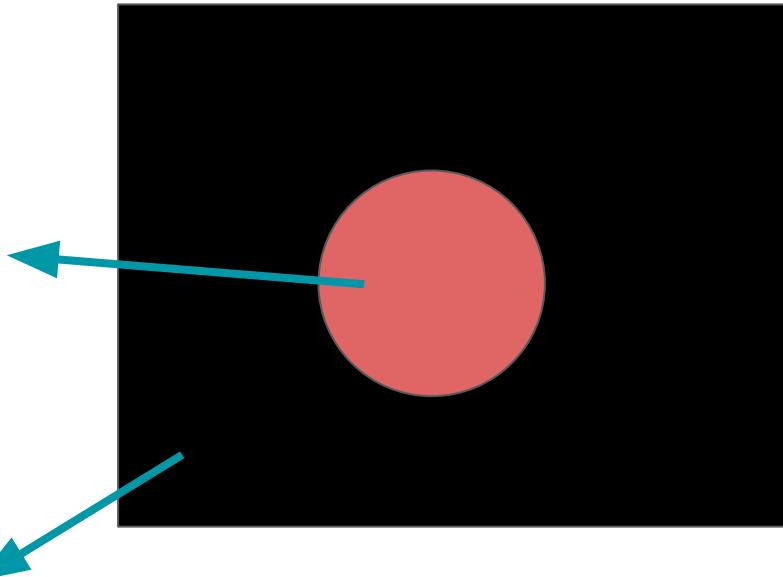


Magnitude of the 21-cm  
bispectrum increases

Noble et al. 2024, arXiv: 2406.03118

# Interpretation

Neutral



Ionized

Large scale signal +ve

$$\Delta_{21} \propto W(kR) \sum \exp\{i\mathbf{k} \cdot \mathbf{r}\}$$

Bharadwaj & Ali 2004  
Bharadwaj & Pandey 2005