

HYACINTH: HYdrogen And Carbon chemistry in the INTerstellar medium in Hydro simulations

Emilio Romano-Díaz

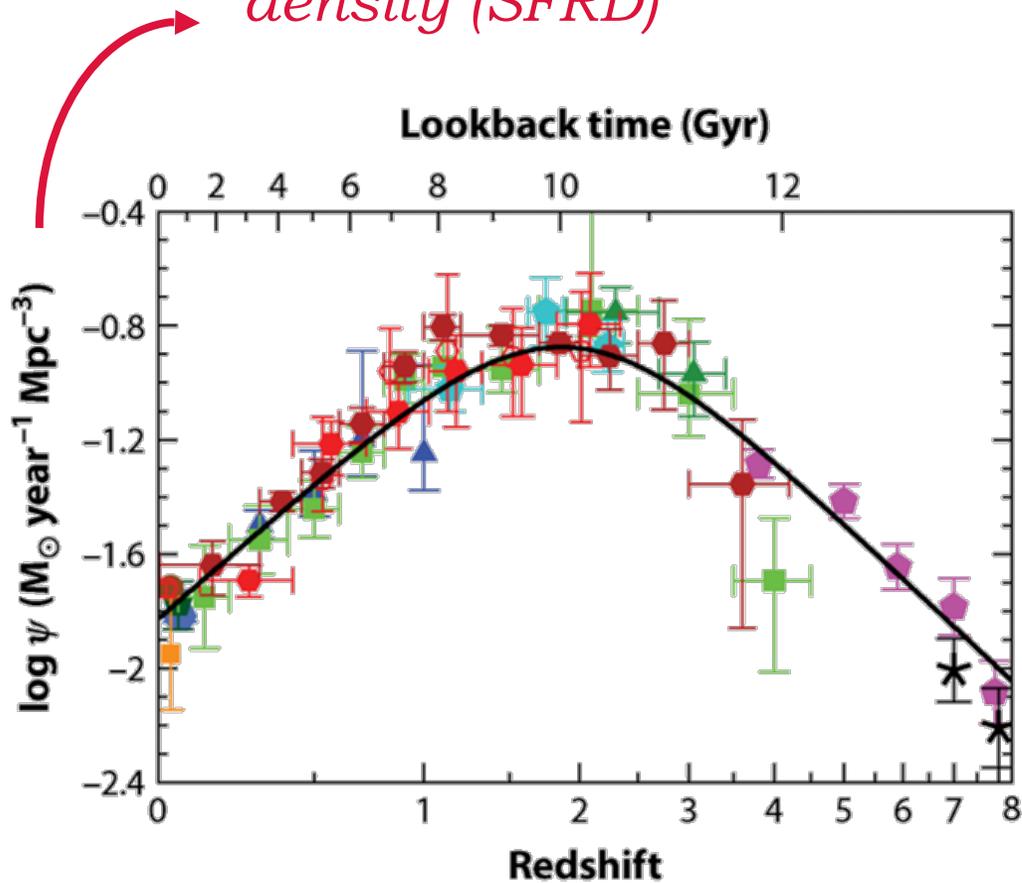
Prachi Khatri & Cristiano Porciani

Khatri, PC, RDE, 2024, A&A, 688, A194

Khatri, RDE, CP, 2025, A&A, 697, A174

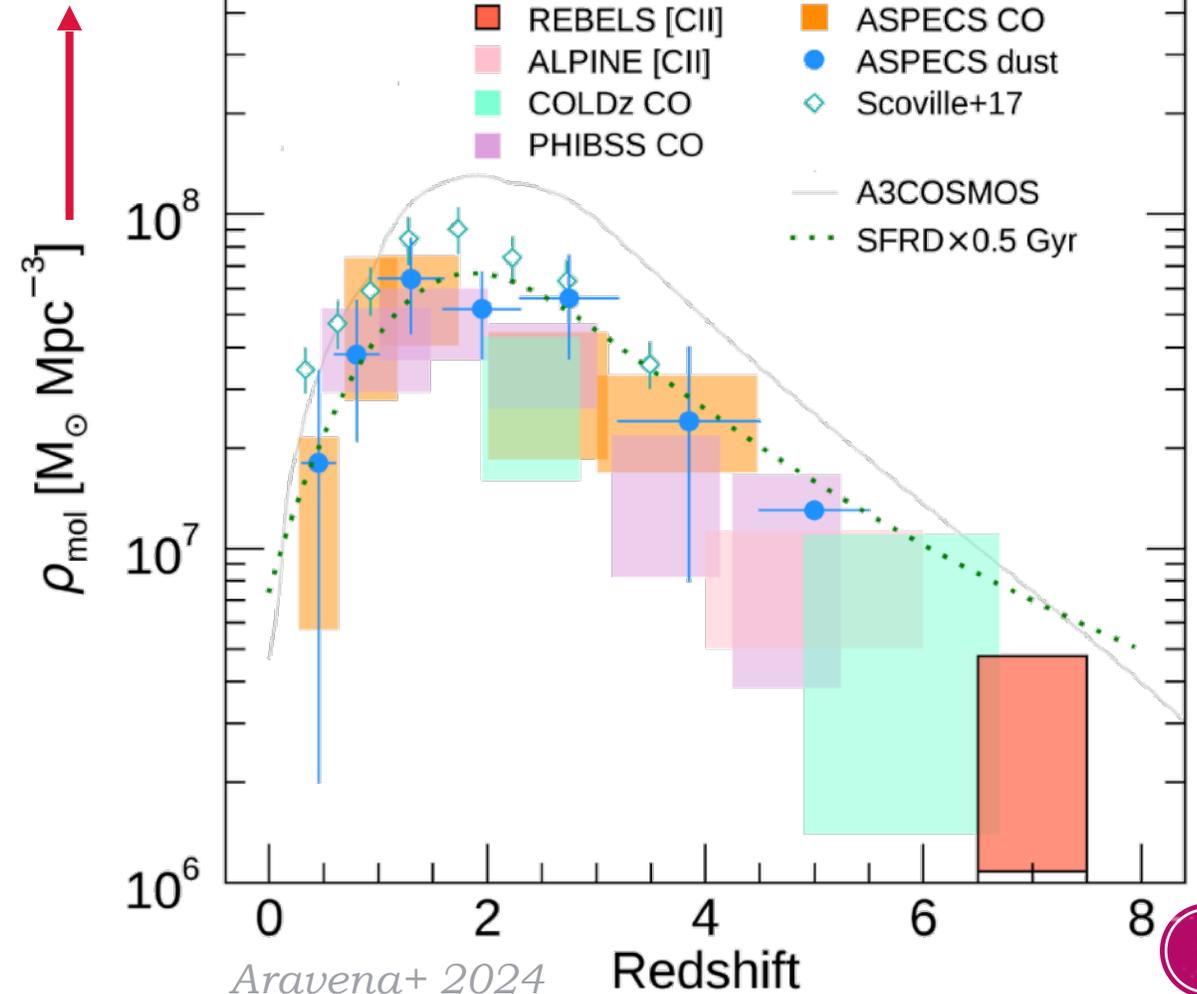
STAR FORMATION ACROSS COSMIC TIME

Star formation rate density (SFRD)



Madau & Dickinson 2014

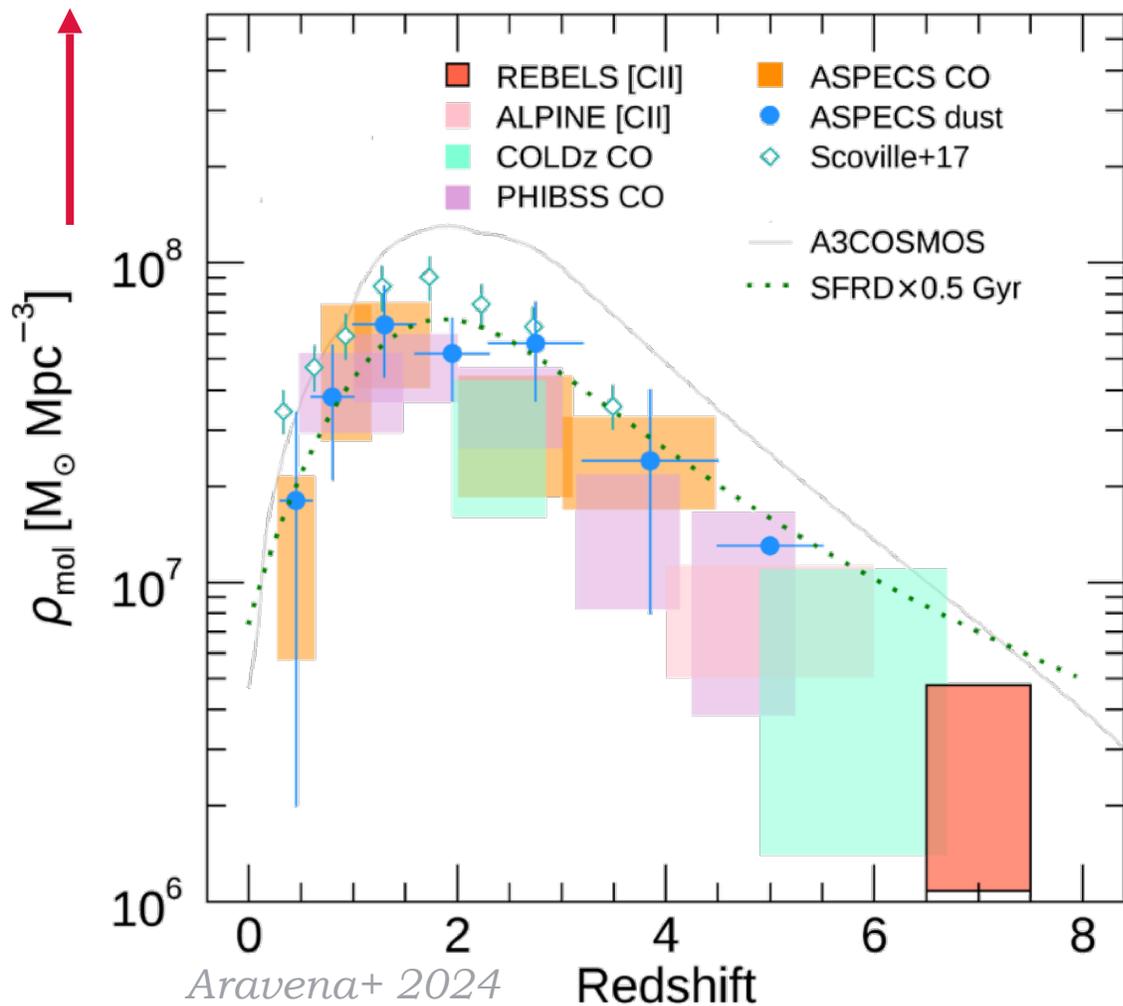
Molecular gas density



Aravena+ 2024

MOLECULAR GAS ACROSS COSMIC TIME

Molecular gas density

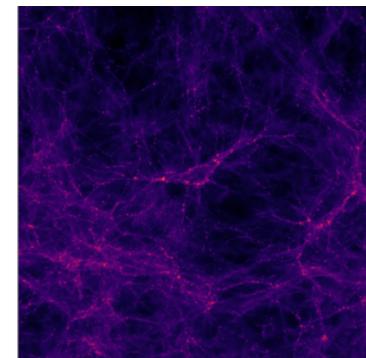


We need **simulations** to complement these observations.

Simulations that model:

- ✓ The formation of galaxies in a **cosmological context**
- ✓ Follow the evolution of **molecular gas** in galaxies.

||
 H_2 and other molecules

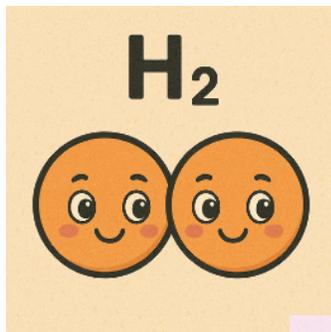


Model chemistry



THE STORY OF H₂

Lacks a permanent dipole moment
⇒ no electric dipolar transitions



Caveat in Using Tracers

Mapping between emission and H₂ abundance sensitive

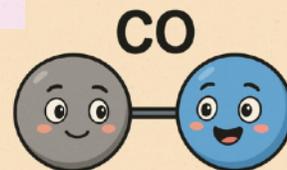
to:

physical conditions like density, metallicity, UV radiation, etc.

Lowest possible transition
(quadrupole rotation)
requires $T \sim 510$ K

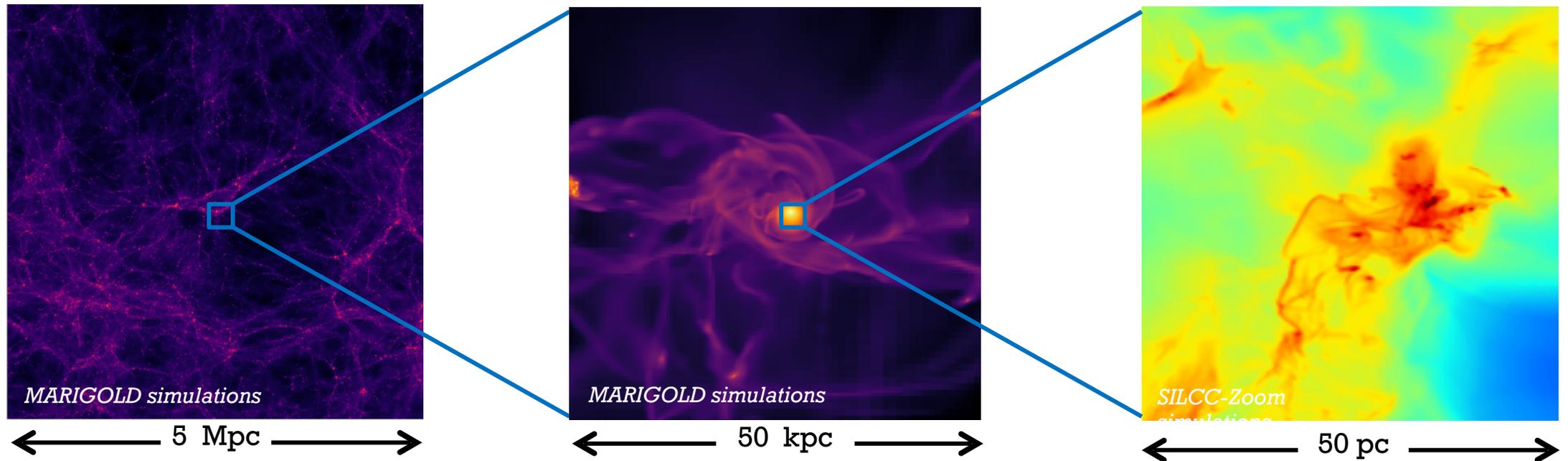


Does not emit under typical conditions of molecular clouds
($T \sim 10$ - 100 K)



CO, C, and C⁺ emission lines serve as indirect tracers of H₂.

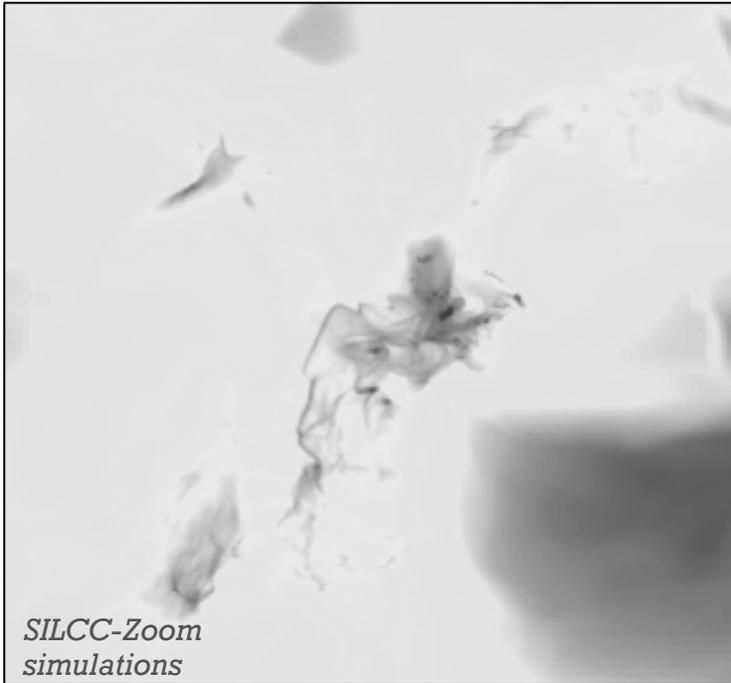
COSMOLOGICAL SIMULATIONS OF GALAXY FORMATION



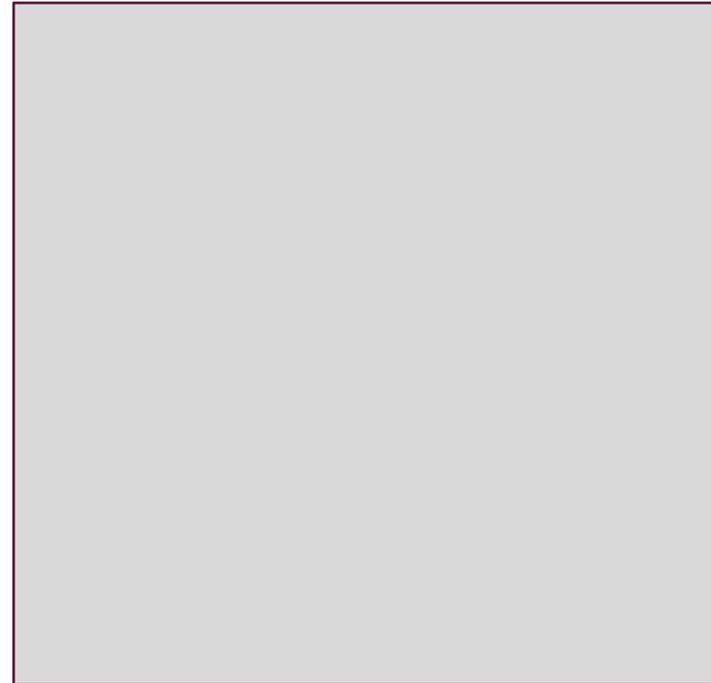
Modelling galaxy formation is a multiscale and multiphysics problem

DENSITY STRUCTURE OF THE ISM

Realistic ISM



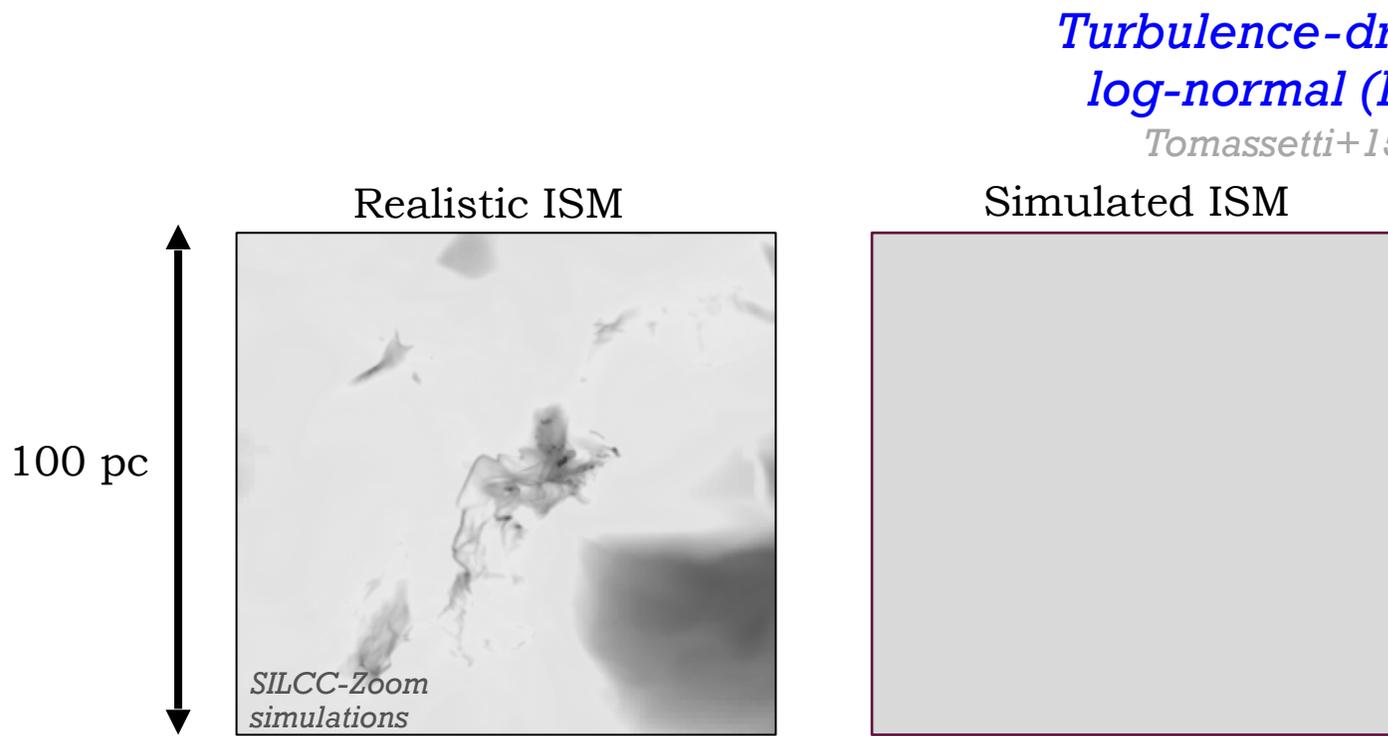
Simulated ISM



100 pc

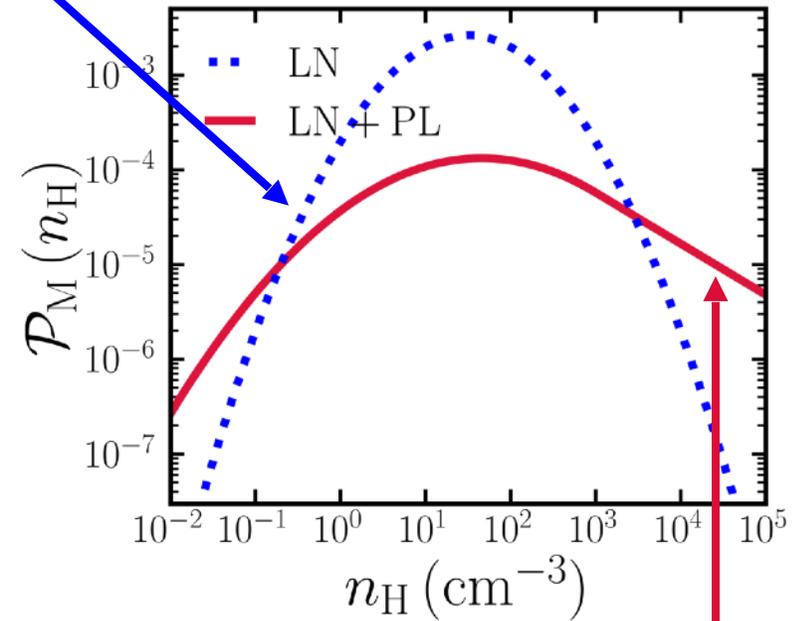
*The finite resolution of simulations misses the **intricate density structure (and other properties)** of the ISM, important for modelling chemical abundances and emission.*

DENSITY STRUCTURE OF THE ISM



*Turbulence-driven
log-normal (LN)
Tomassetti+15*

*A PDF to mimic the
distribution of unresolved
(sub-grid) densities*



*The finite resolution of simulations misses the **intricate density structure** of the ISM, important for modelling chemical abundances and emission.*

*Functional forms of density PDF:
Kainulainen+09,
Kritsuk+11, Federrath+13, Girichidis+14*

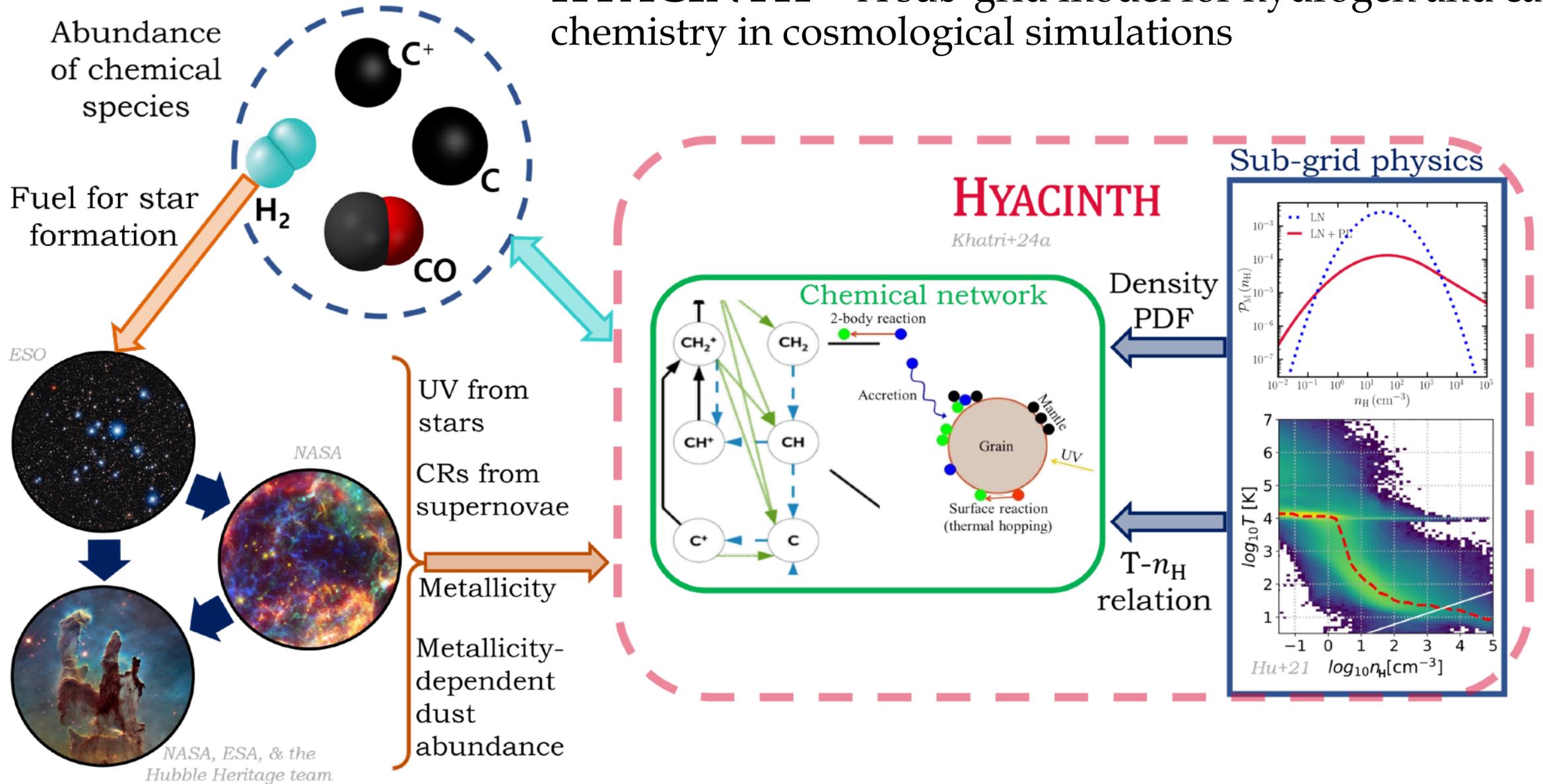
Self-gravity induces a power-law tail

log-normal + power-law (LN+PL)

Sub-grid model HYACINTH

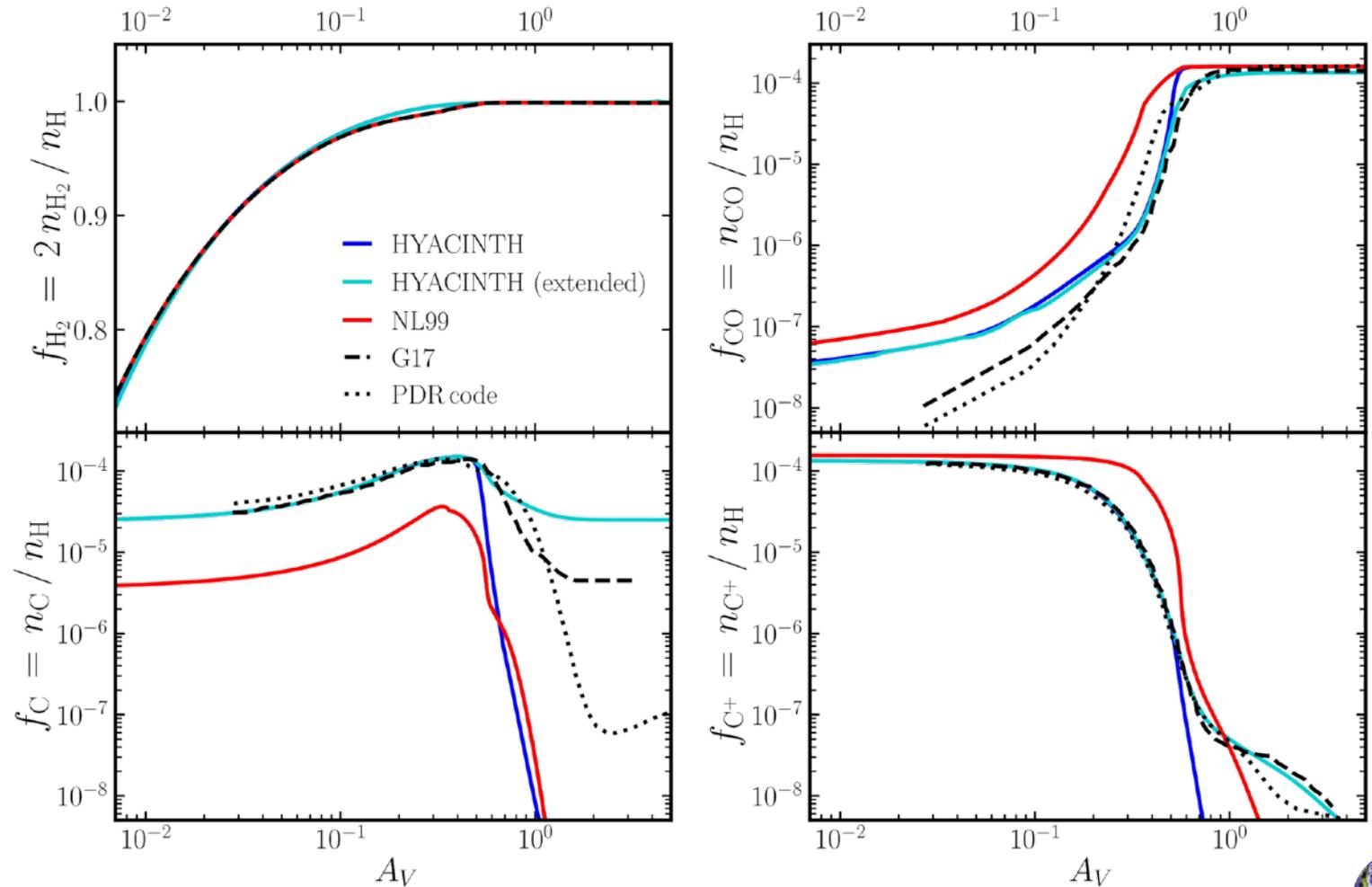


HYACINTH - A sub-grid model for hydrogen and carbon chemistry in cosmological simulations



TEST OF CHEMICAL ABUNDANCES – Comparison of equilibrium abundances using the slab test

- 19 chemical reactions
- Additional chemical species – He⁺ and HCO⁺ -- important for CO chemistry
- 29 chemical reactions in total
- ≈3.3x computational time



NL99= Nelson & Langer 1999

G17 = Gong et al. 2017

PDR code from Tielens & Hollenbach 1985

Sub-grid model HYACINTH

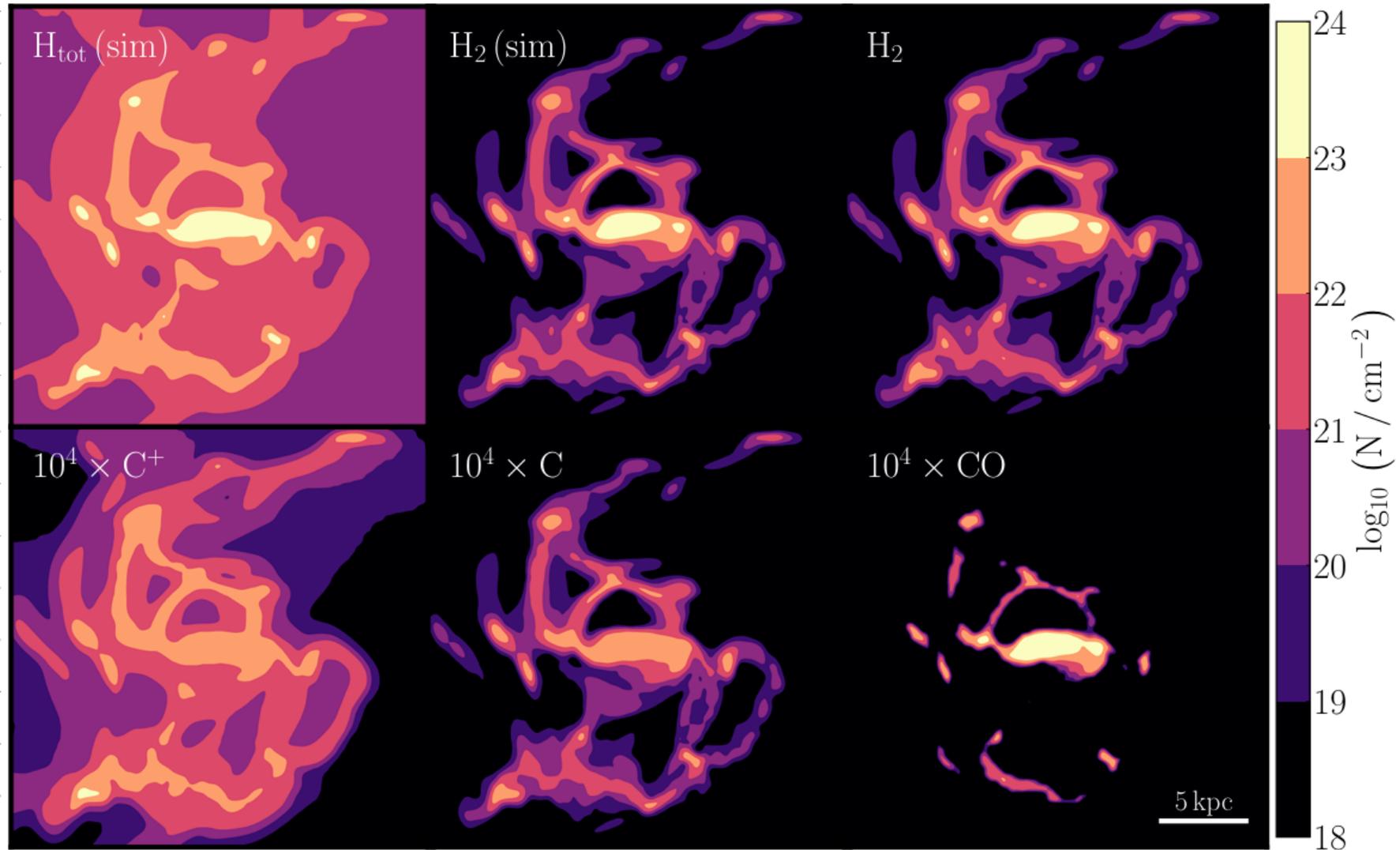


APPLICATION: POST-PROCESSING

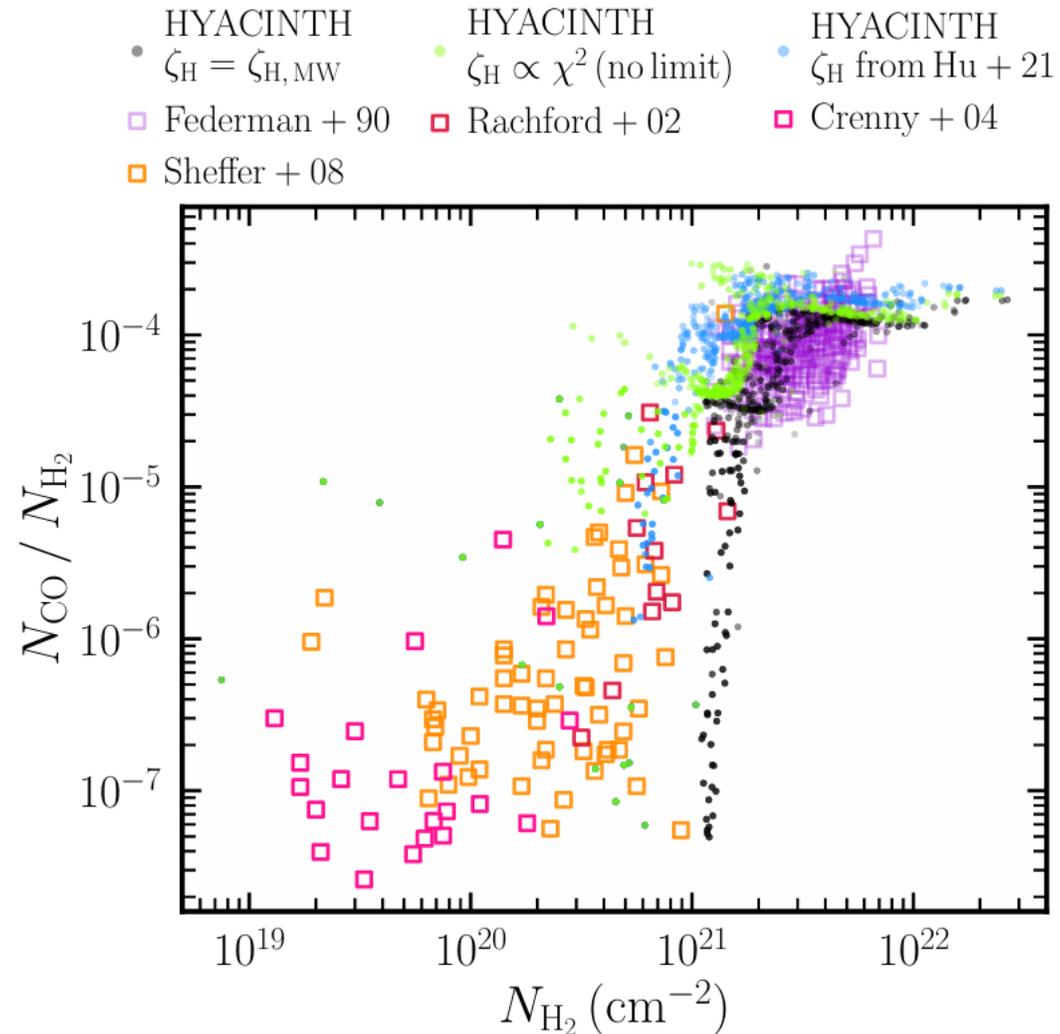
➤ A RAMSES simulated galaxy at $z=2.5$ from Tomassetti+15 including H_2 chemistry and Lyman-Werner RT.

➤ Compute Eq. abundances: H_2 , CO, C, and C^+ using HYACINTH.

- Metallicity – from simulation
- UV flux χ – from simulation
- Different options for the cosmic-ray ionization rate ζ_H
 - constant
 - linear scaling with χ
 - quadratic scaling with χ



COMPARISON WITH OBSERVATIONS



THE MARIGOLD SUITE: COSMOLOGICAL SIMULATIONS USING THE SUB-GRID MODEL HYACINTH

- Follow galaxy formation & evolution in a cosmological context (DM, gas & stars til $z=3$)
- Embed HYACINTH into RAMSES to track the abundances of H_2 , CO, C, and C^+ in addition to the total gas.

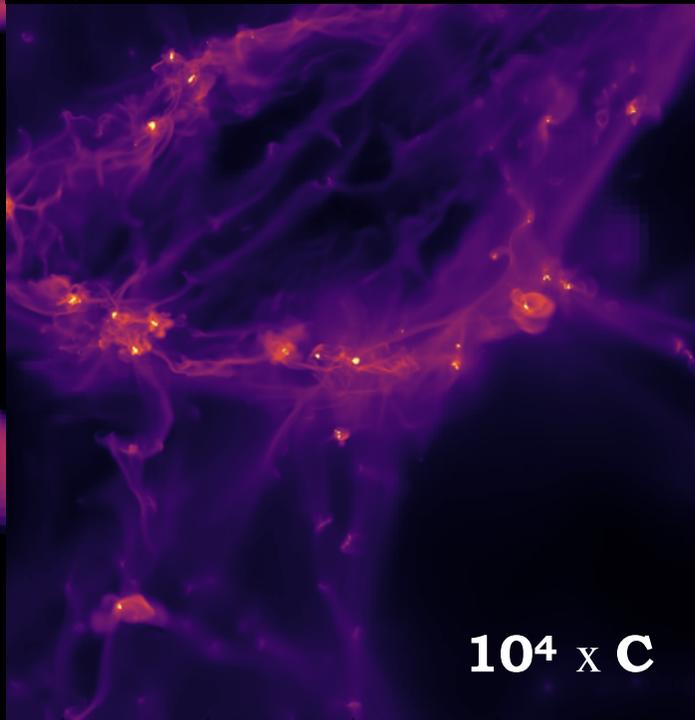
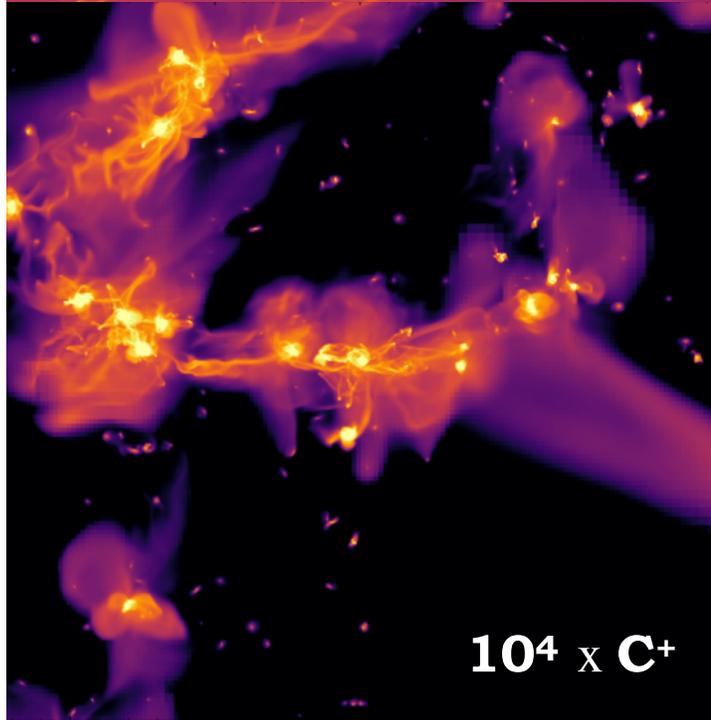
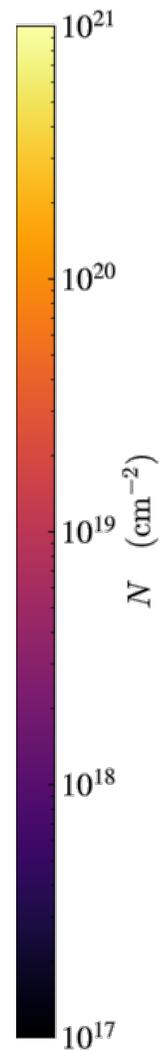
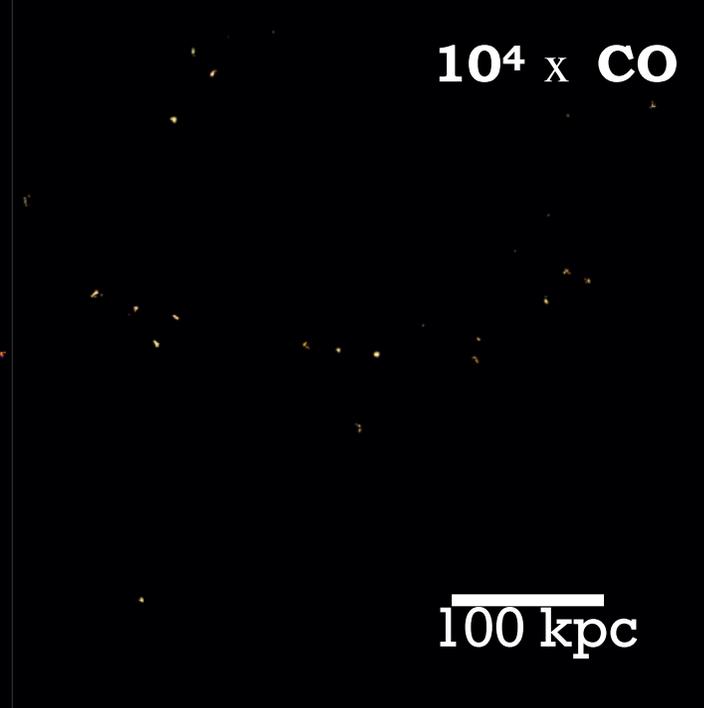
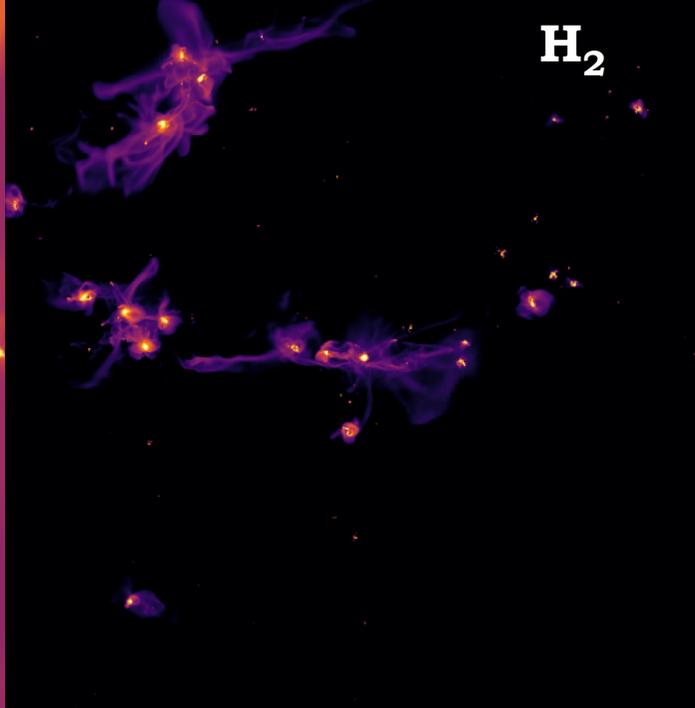
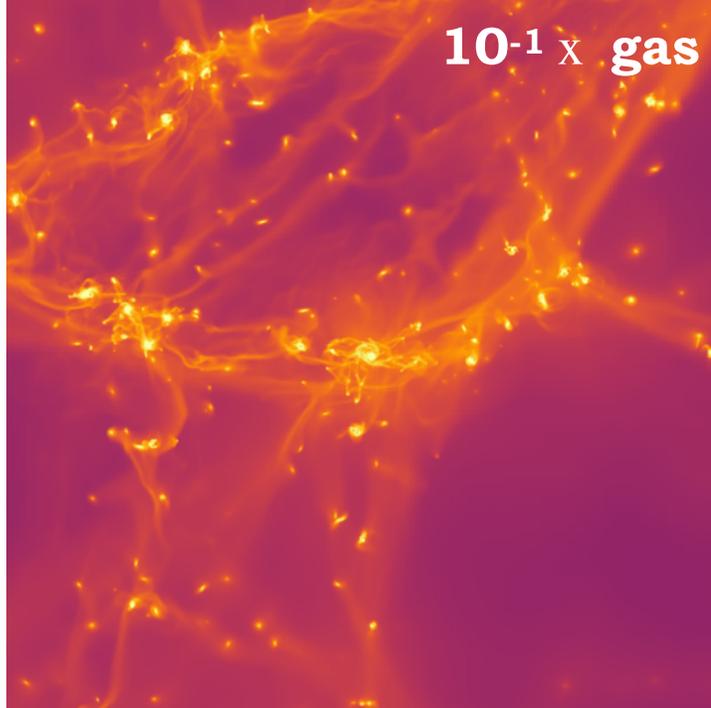
THE MARIGOLD SUITE

Simulation	L_{box} (Mpc)	N_{DM}	Δx^{min} (pc)	m_{DM} (M_{\odot})	m_{*} (M_{\odot})
M25	25	1024^3	32	5×10^5	7×10^3
M50	50	1024^3	64	4×10^6	6×10^4

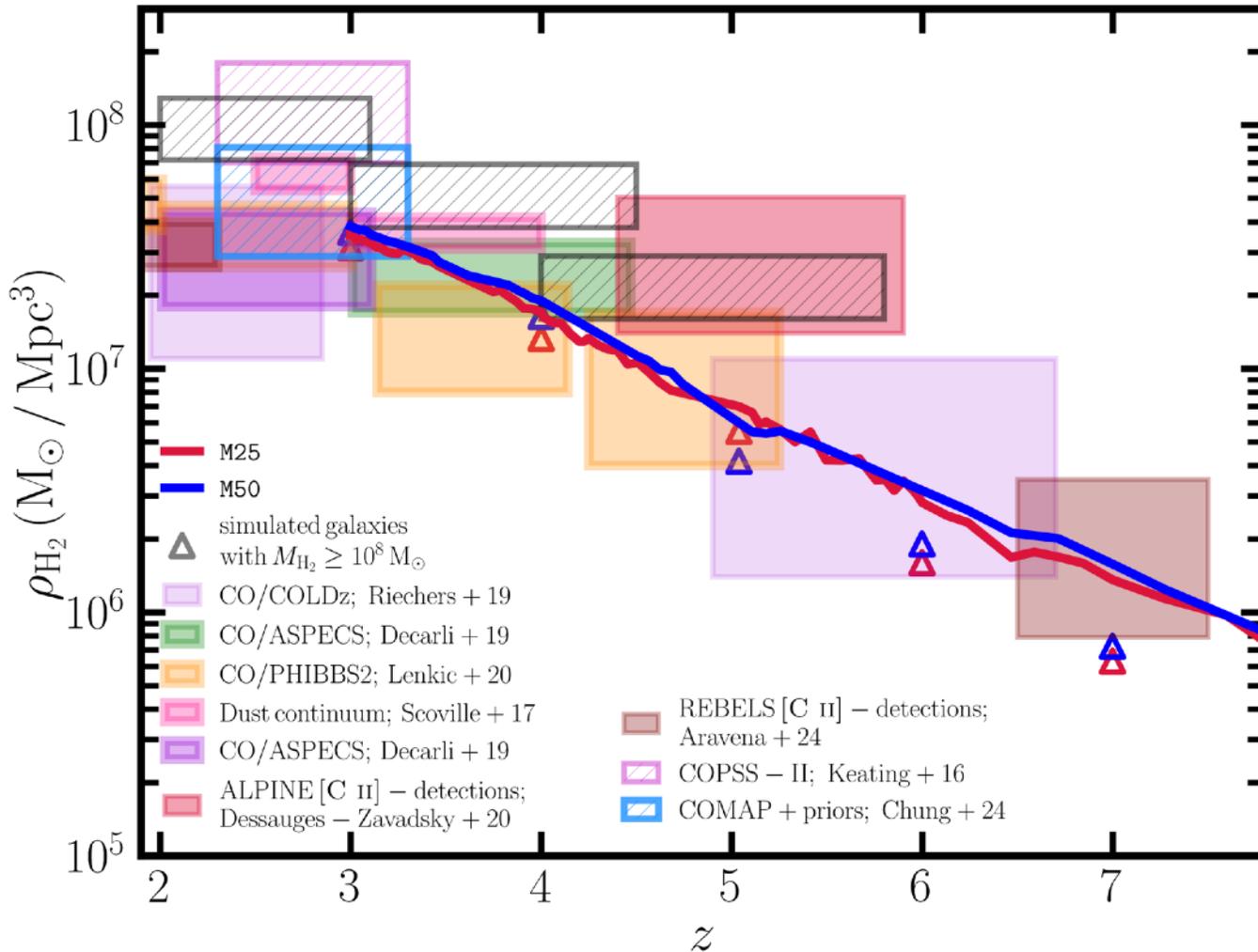
Large enough volume to study statistical properties of galaxies

High spatial resolution to model chemistry and emission properties of galaxies

Sufficiently low particle mass to resolve low-mass galaxies



COSMIC MOLECULAR GAS DENSITY



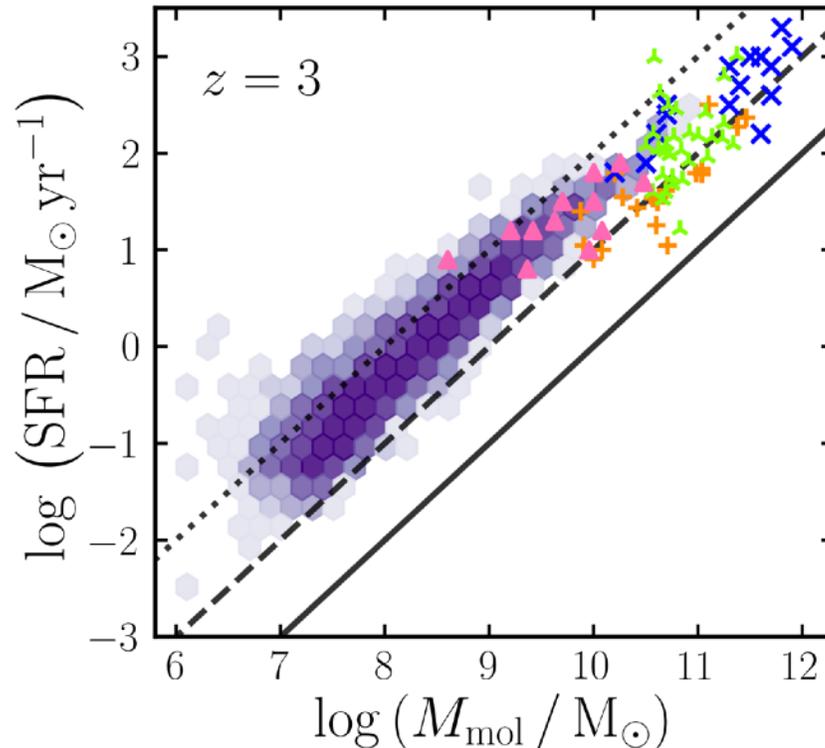
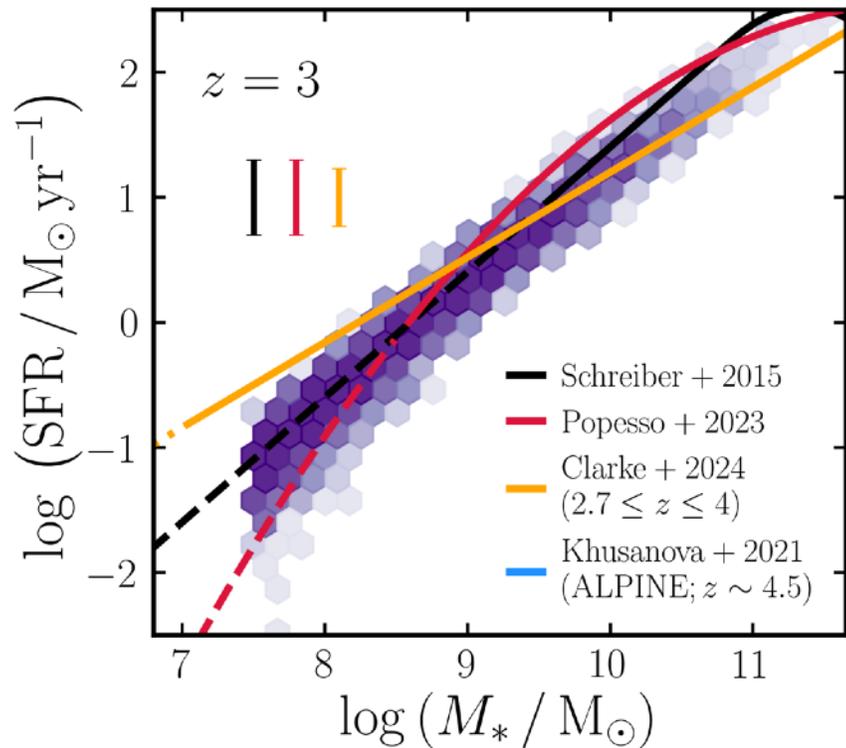
➤ Simulated ρ_{H_2} consistent with observational constraints

➤ Low-mass galaxies dominate the cosmic H_2 budget at $z > 7$

STATISTICAL PROPERTIES OF GALAXIES

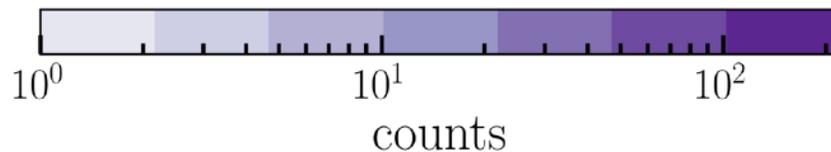
Distribution of simulated galaxies aligns with empirical relations

MARIGOLD



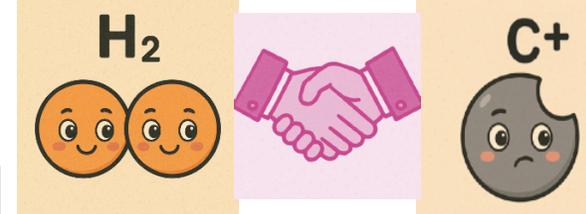
$$\tau_{\text{depl}} = \frac{M_{\text{mol}}}{\text{SFR}}$$

Main-sequence relation

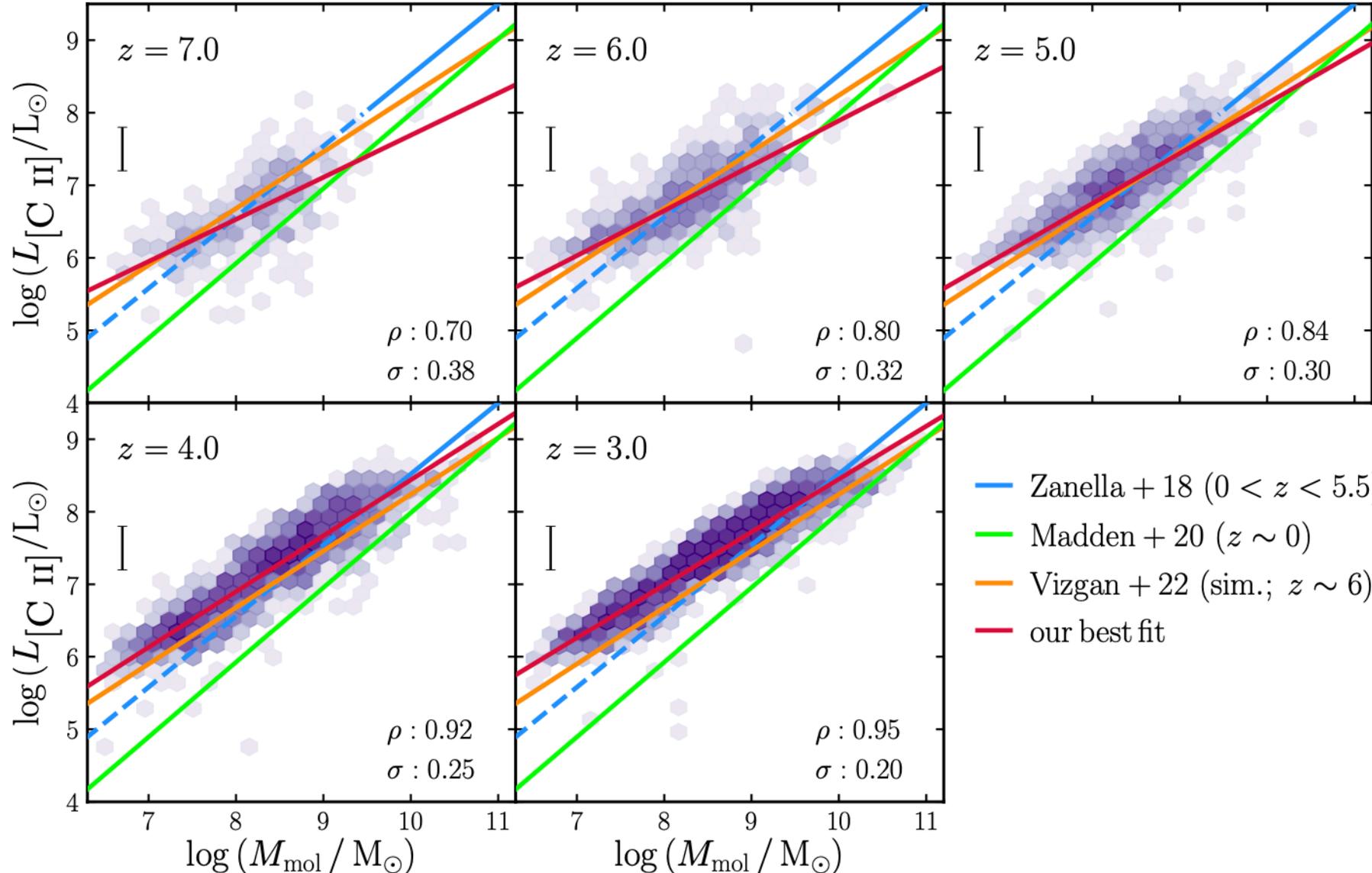


Schmidt-Kennicutt relation

[CII]- M_{mol} RELATION: LINE RADIATIVE TRANSFER



The correlation is weak at high redshifts and strengthens over time

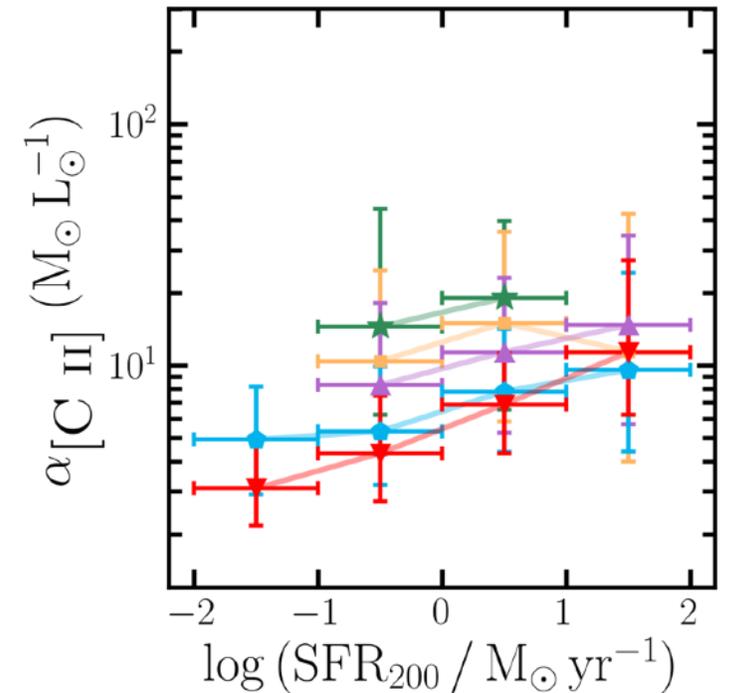
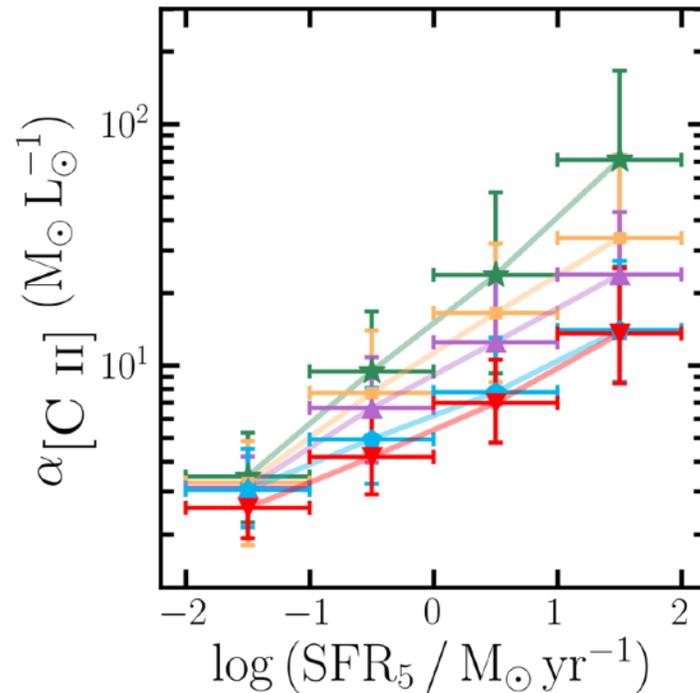
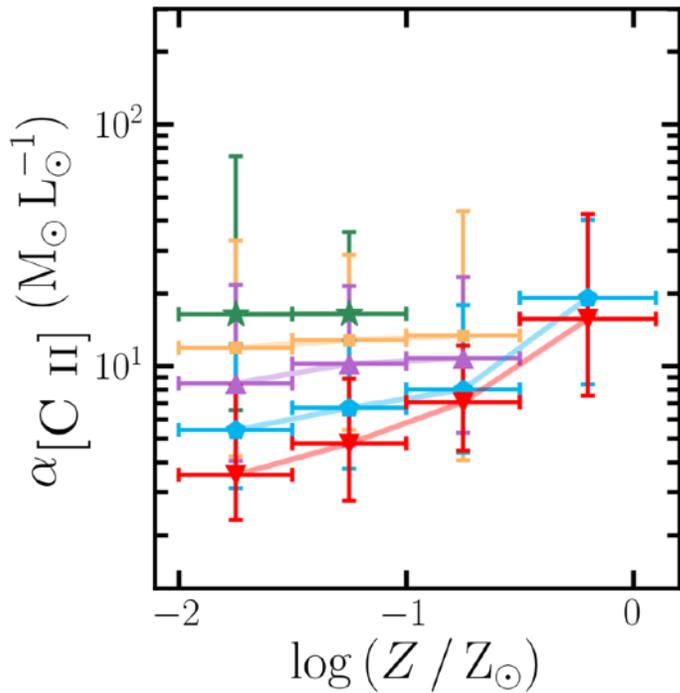


RT: Optically thick

$$\alpha_{[\text{CII}]} = \frac{M_{\text{mol}}}{L_{[\text{CII}]}}$$

The numerical factor used to convert the observed [CII] luminosity to a molecular gas mass

How does $\alpha_{[\text{C II}]}$ change with galaxy properties?



$z = 7$ $z = 6$ $z = 5$ $z = 4$ $z = 3$

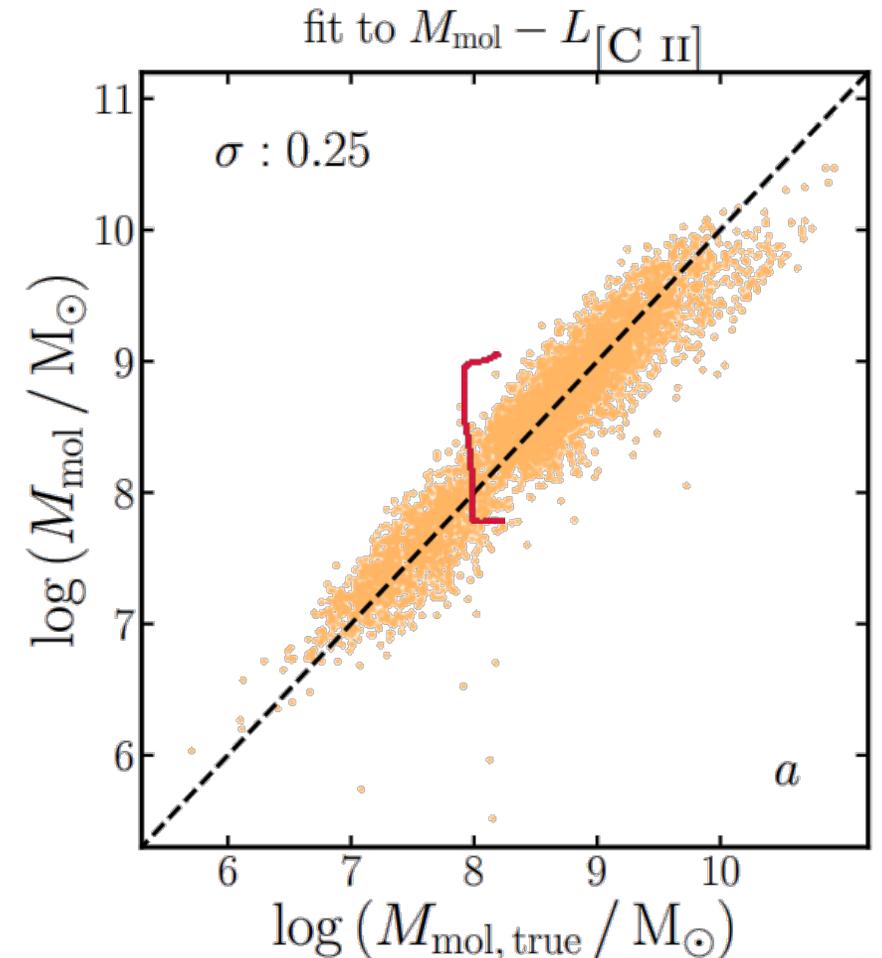
$$\alpha_{[\text{C II}]} = f(Z, \text{SFR}_5, \text{SFR}_{200})$$

If $\alpha_{[\text{CII}]}$ depends on other galaxy properties,
can we do a better job at predicting
 M_{mol} from $L_{[\text{CII}]}$?

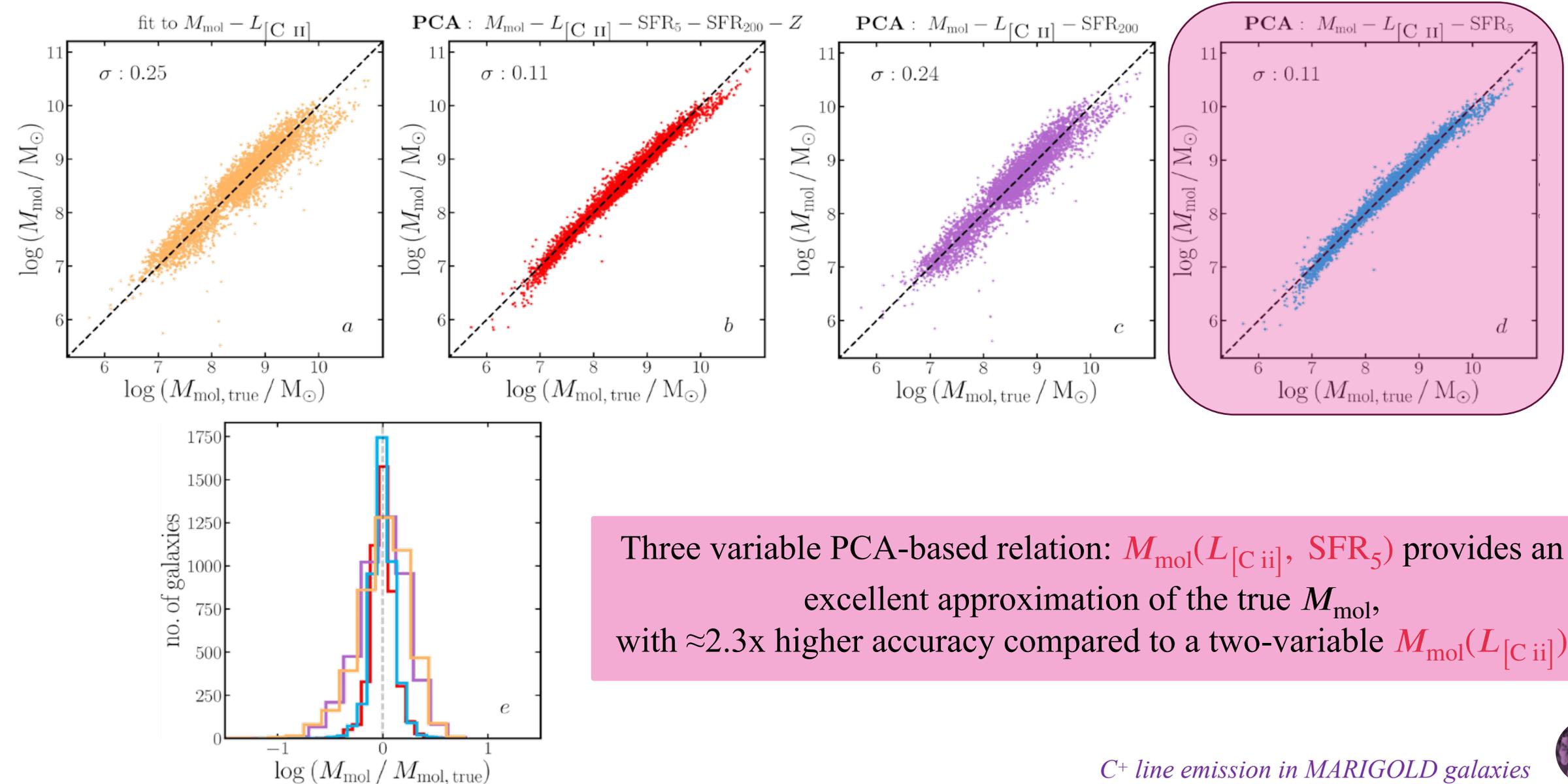
In other words,
can we reduce this **scatter**?

=> PCA in the 5D parameter space:

$$M_{\text{mol}} = f(L_{[\text{CII}]}, Z, \text{SFR}_5, \text{SFR}_{200})$$



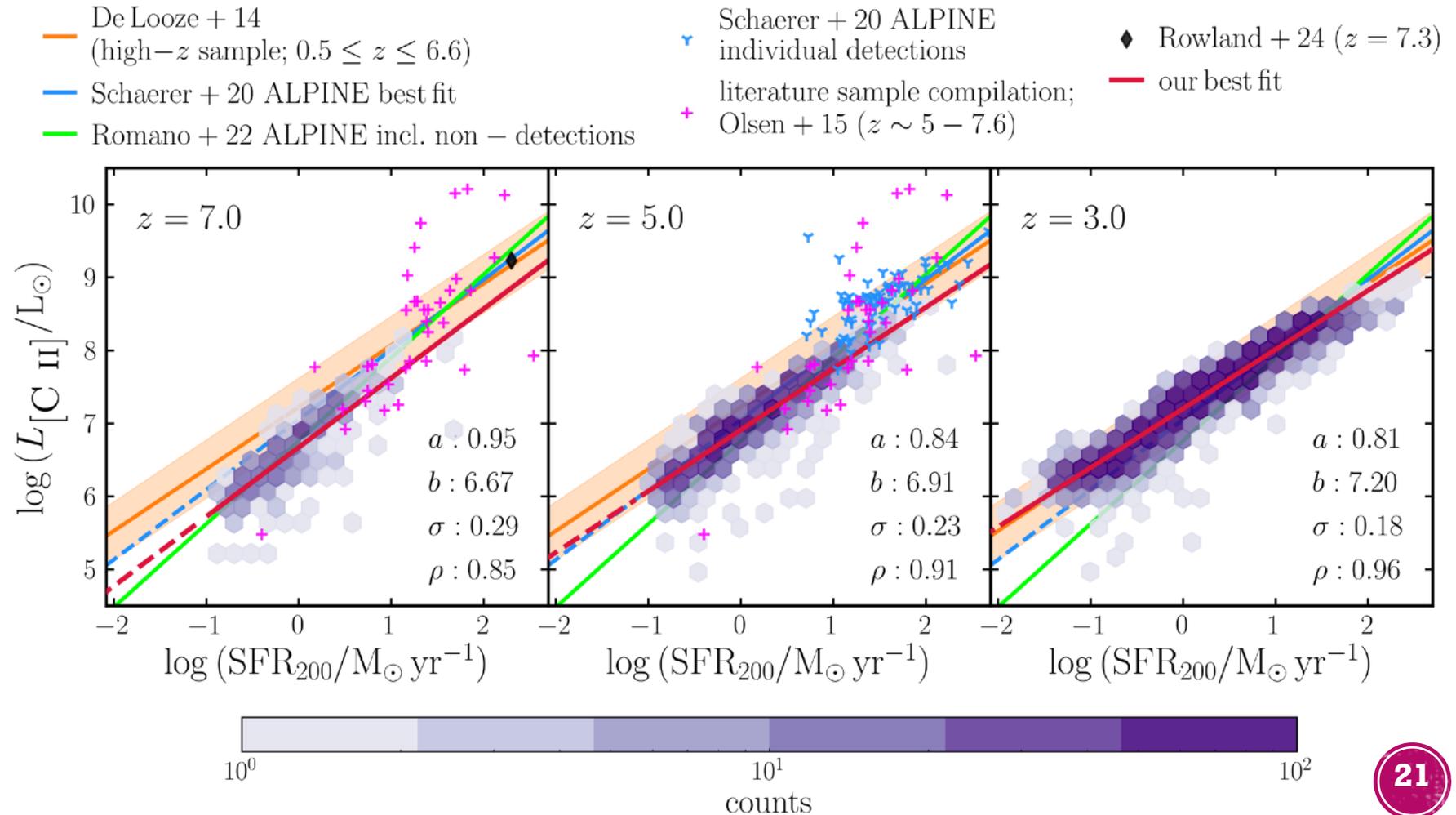
PERFORMANCE OF PCA-BASED RELATIONS



Three variable PCA-based relation: $M_{\text{mol}}(L_{[\text{C II}]}, \text{SFR}_5)$ provides an excellent approximation of the true M_{mol} , with $\approx 2.3x$ higher accuracy compared to a two-variable $M_{\text{mol}}(L_{[\text{C II}]})$

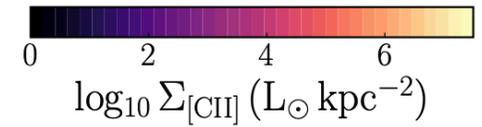
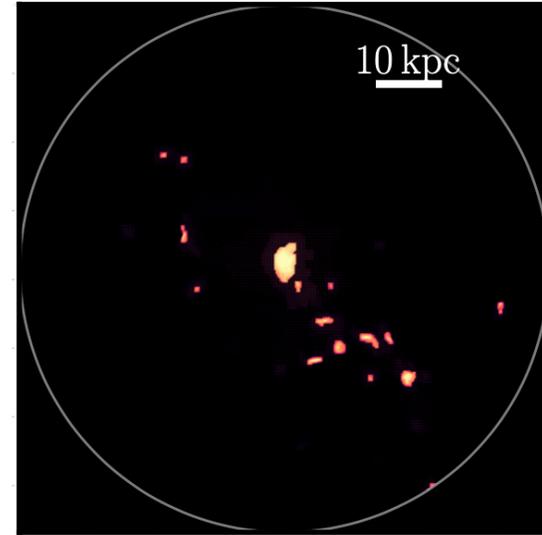
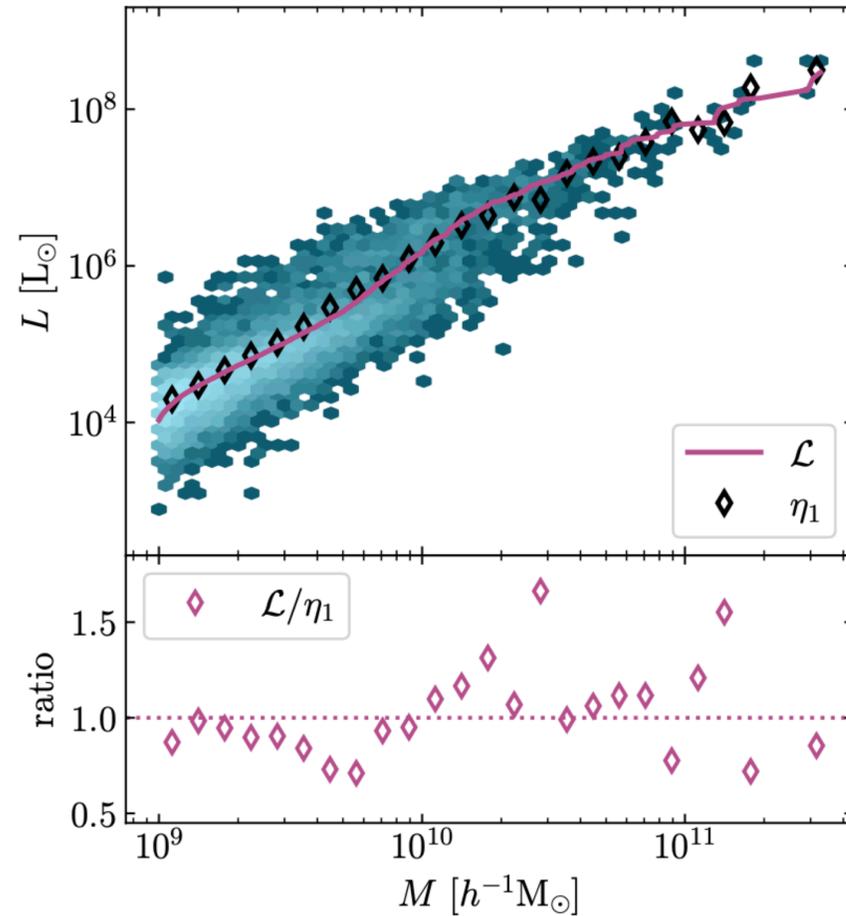
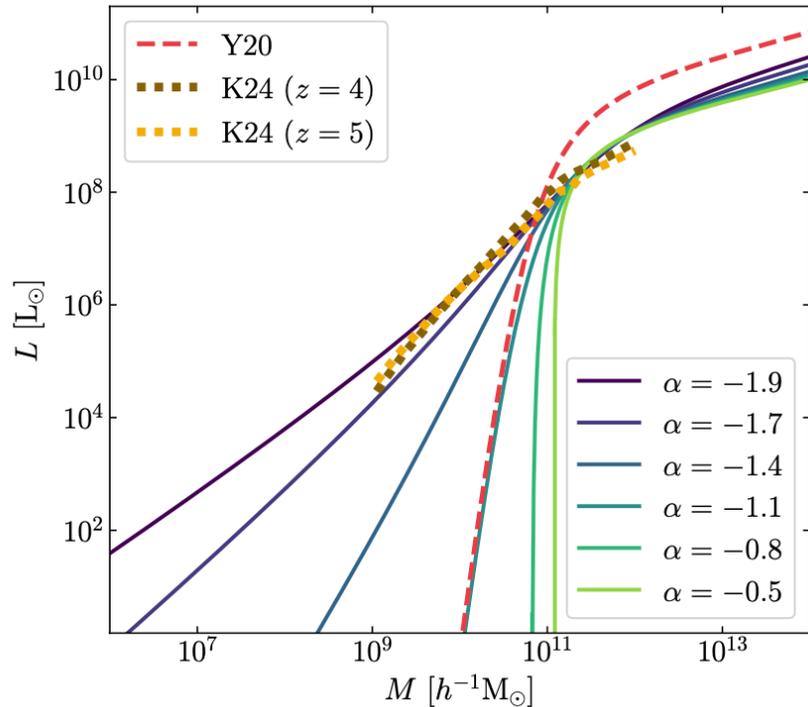
[CII]-SFR RELATION

- The correlation is strong at all redshifts
- Strong evolution in the intercept --- > ~0.5 dex in 1.4 Gyr



MARIGOLD & LIM

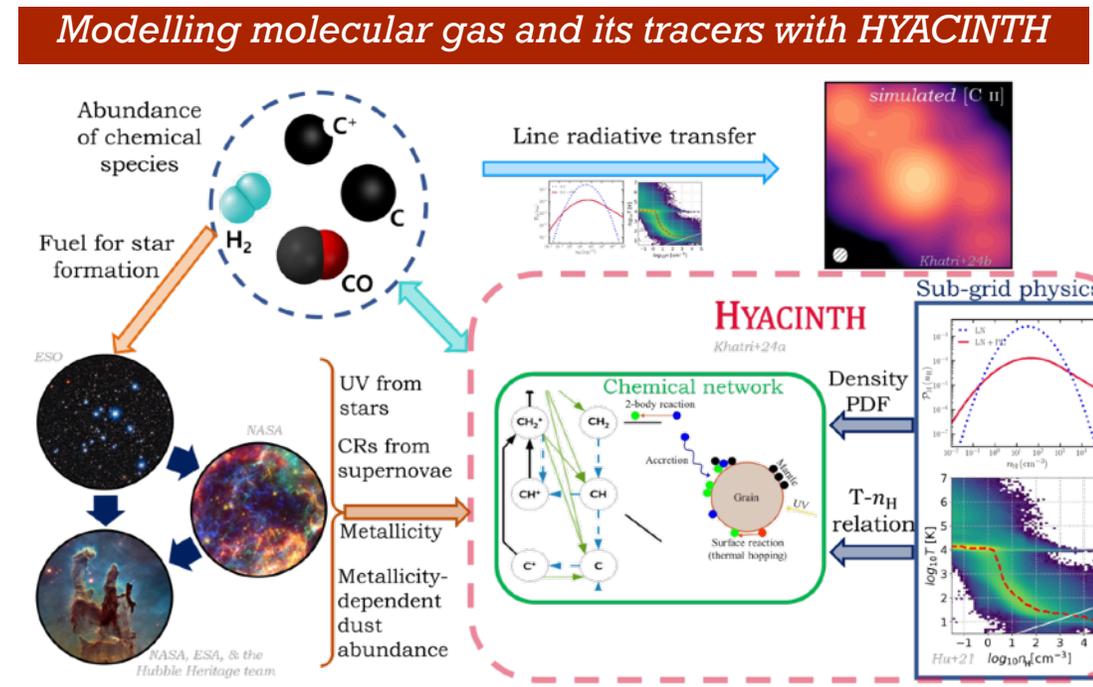
- Our results can be used together with Halo Abundance Matching (HAM) to populate large Nbody simulations for LIM purposes:
- 1 halo - 1 galaxy
- No scatter in $L_{\text{C}+}$ at fixed mass
- CLF: $\phi(L|M,z)$ monotonic function



(Elena Marcuzzo's talk, tomorrow)

CONCLUSIONS

- HYACINTH – a sub-grid model for hydrogen and carbon chemistry in hydro simulations.
- HYACINTH can be used as a post-processing tool
- The MARIGOLD simulations – cosmological simulations for tracing molecular gas & C-related species in galaxies.
- Simulated cosmic H₂ density in agreement with observational estimates.
- [C ii] – M_{mol} correlation
 - Evolves over time
 - Is sensitive to SFR

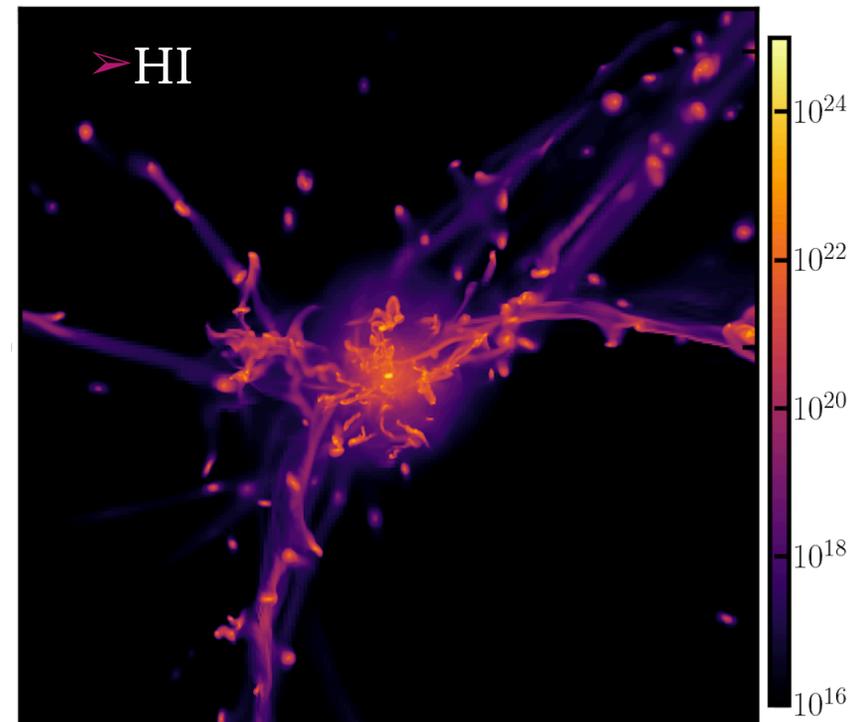
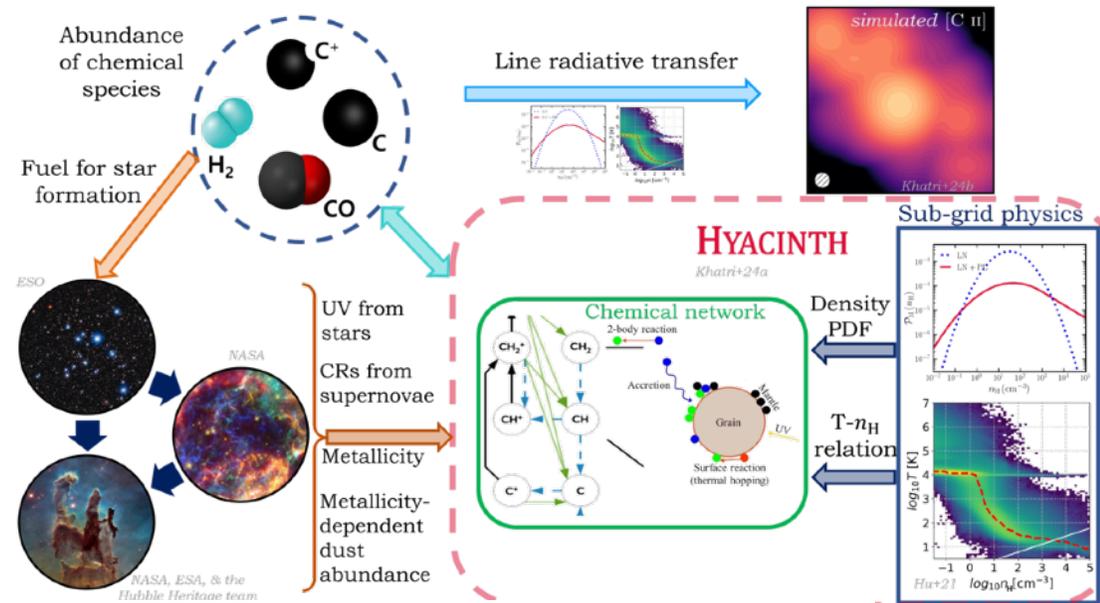


THE FUTURE:

- The future is bright! ☺
- CO analysis: RT -> line emission & LF -> LIM
- Include neutral and ionized hydrogen (HI & HII) within HYACINTH
- Include massive galaxies' contributions -> Constrained Realizations & zoom-ins
- ...

Trehan+25 in prep

Modelling molecular gas and its tracers with HYACINTH





BACKUP

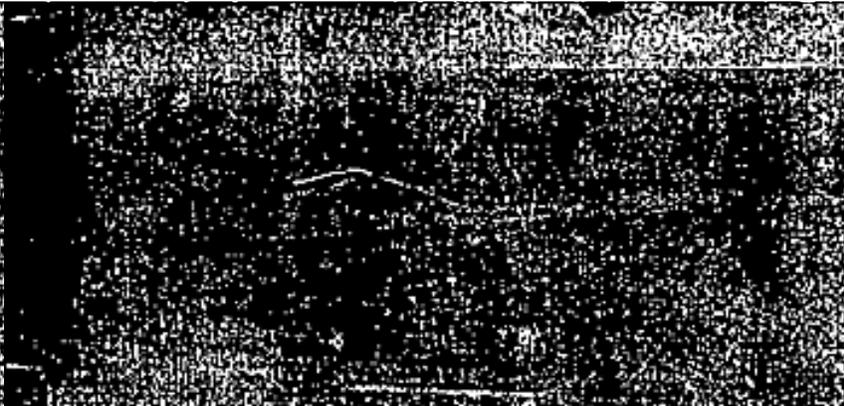
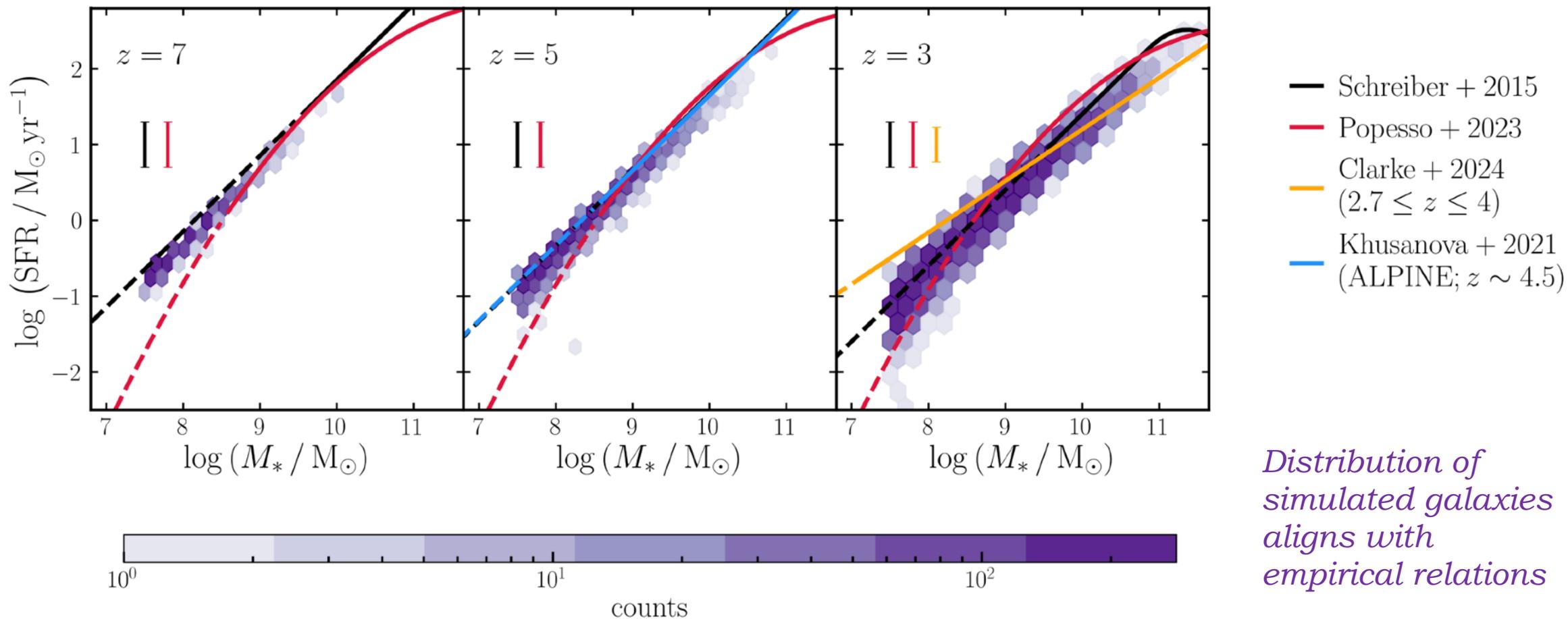


Table 2: Best-fit parameters to the LF for the DPL function given in Eq. (2).

z	$\log(\phi_* / \text{Mpc}^{-3} \text{dex}^{-1})$	$\log(L_* / L_\odot)$	α	β	$\Delta\text{DIC}^{(a)}$	$\Delta\text{DIC}^{(b)}$
7	$-1.84^{+0.15}_{-0.15}$	$6.44^{+0.10}_{-0.11}$	$-1.54^{+0.06}_{-0.05}$	$-2.75^{+0.08}_{-0.09}$	105	107
6	$-1.26^{+0.12}_{-0.12}$	$6.20^{+0.10}_{-0.10}$	$-1.24^{+0.06}_{-0.06}$	$-2.30^{+0.04}_{-0.05}$	222	223
5	$-1.52^{+0.13}_{-0.13}$	$6.72^{+0.11}_{-0.11}$	$-1.42^{+0.03}_{-0.03}$	$-2.31^{+0.05}_{-0.05}$	159	161
4	$-0.91^{+0.08}_{-0.07}$	$7.03^{+0.04}_{-0.04}$	$-1.28^{+0.01}_{-0.01}$	$-2.57^{+0.05}_{-0.05}$	449	451
3	$-1.00^{+0.08}_{-0.08}$	$7.37^{+0.04}_{-0.04}$	$-1.22^{+0.01}_{-0.01}$	$-2.65^{+0.05}_{-0.05}$	174	176

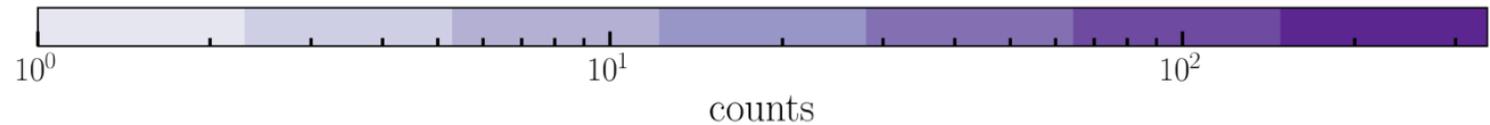
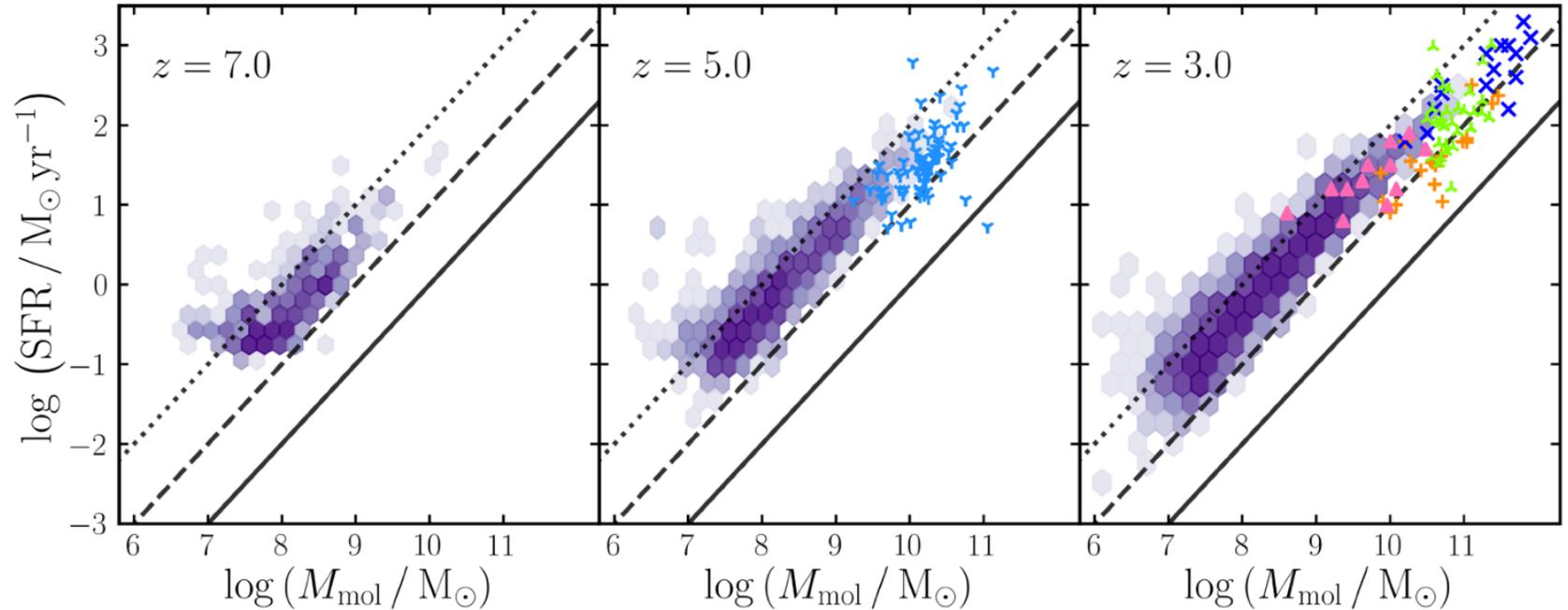
Notes. The last two columns show the values of ΔDIC^a and ΔDIC^b between the Schechter function and the DPL (see text).

MAIN-SEQUENCE OF STAR-FORMING GALAXIES



SFR- M_{MOL} RELATION IN MARIGOLD GALAXIES

- ALPINE ($4.4 \leq z \leq 5.9$)
- ASPECS ($1 \leq z \leq 3.6$)
- PHIBSS ($2.5 \leq z \leq 4$)
- Schinnerer + 2016 ($z \sim 3.2$)
- Catan + 2024 ($2 \leq z \leq 3.6$)
- $\tau_{\text{depl}} = 10 \text{ Gyr}$
- - $\tau_{\text{depl}} = 1 \text{ Gyr}$
- ⋯ $\tau_{\text{depl}} = 0.1 \text{ Gyr}$

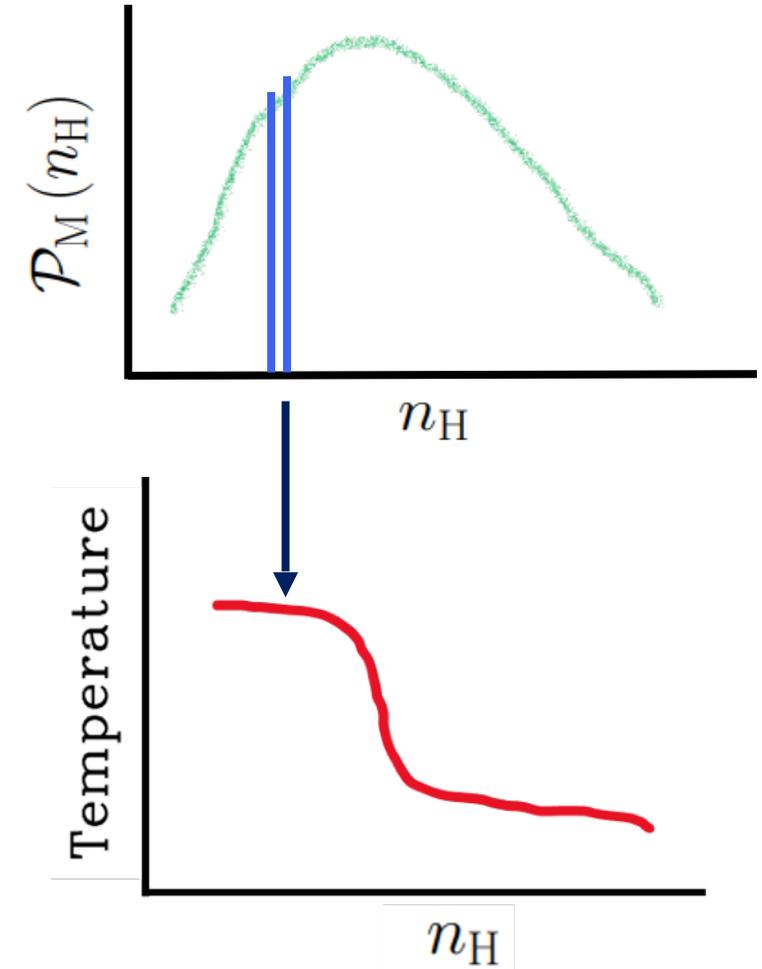


$$\tau_{\text{depl}} = \frac{M_{\text{mol}}}{\text{SFR}}$$

Most simulated galaxies have $\tau_{\text{depl}} = 0.1-1 \text{ Gyr}$ – similar to observed galaxies

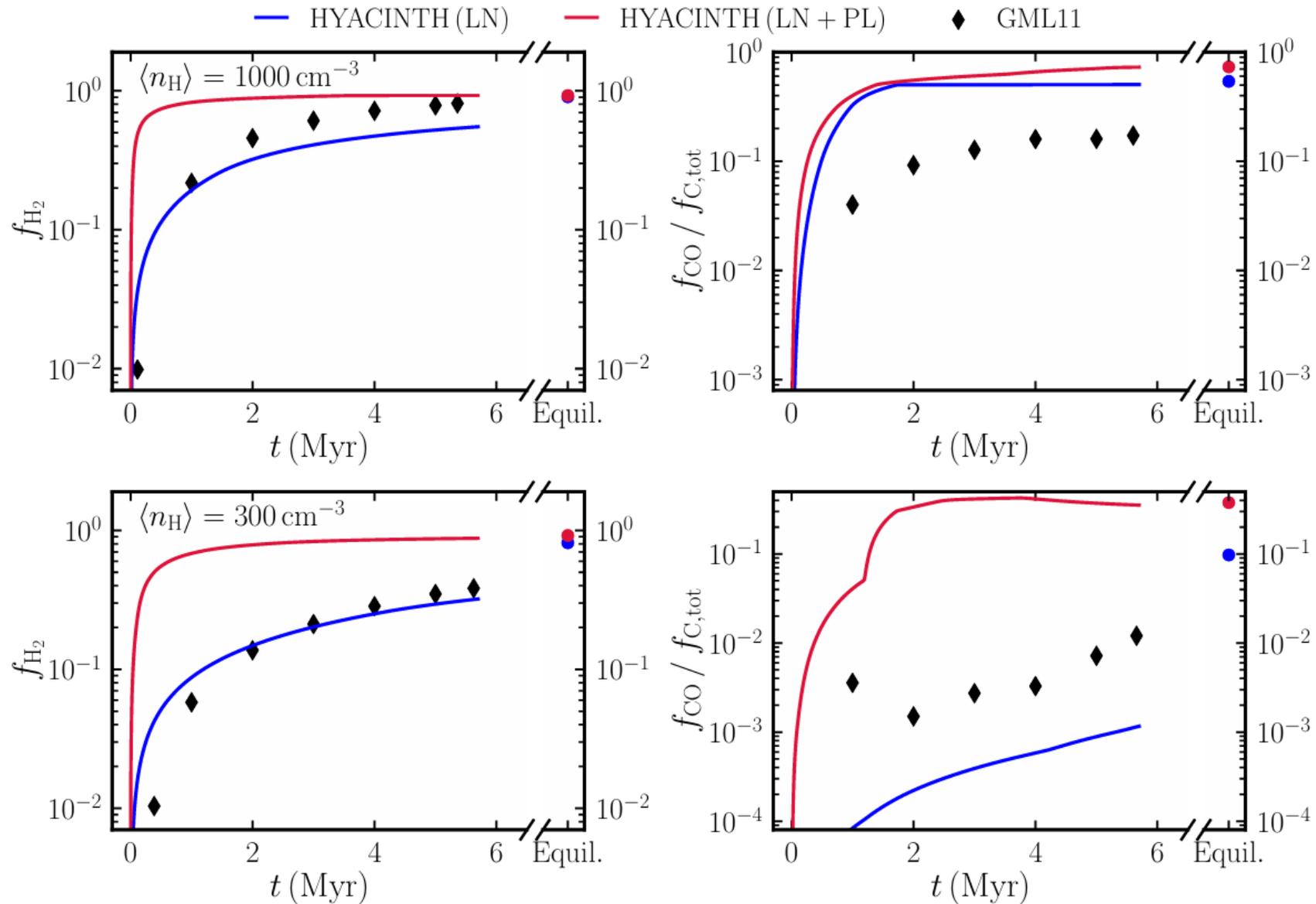
REACTION RATE CALCULATION

- Compute reaction rate at a given n_H
- For temperature-sensitive reactions
 - read out the T corresponding to a given n_H using the **$T - n_H$ relation**
- Integrate over n_H weighing by the **PDF** to obtain the cell-level reaction rate
- Repeat for all reactions in the network

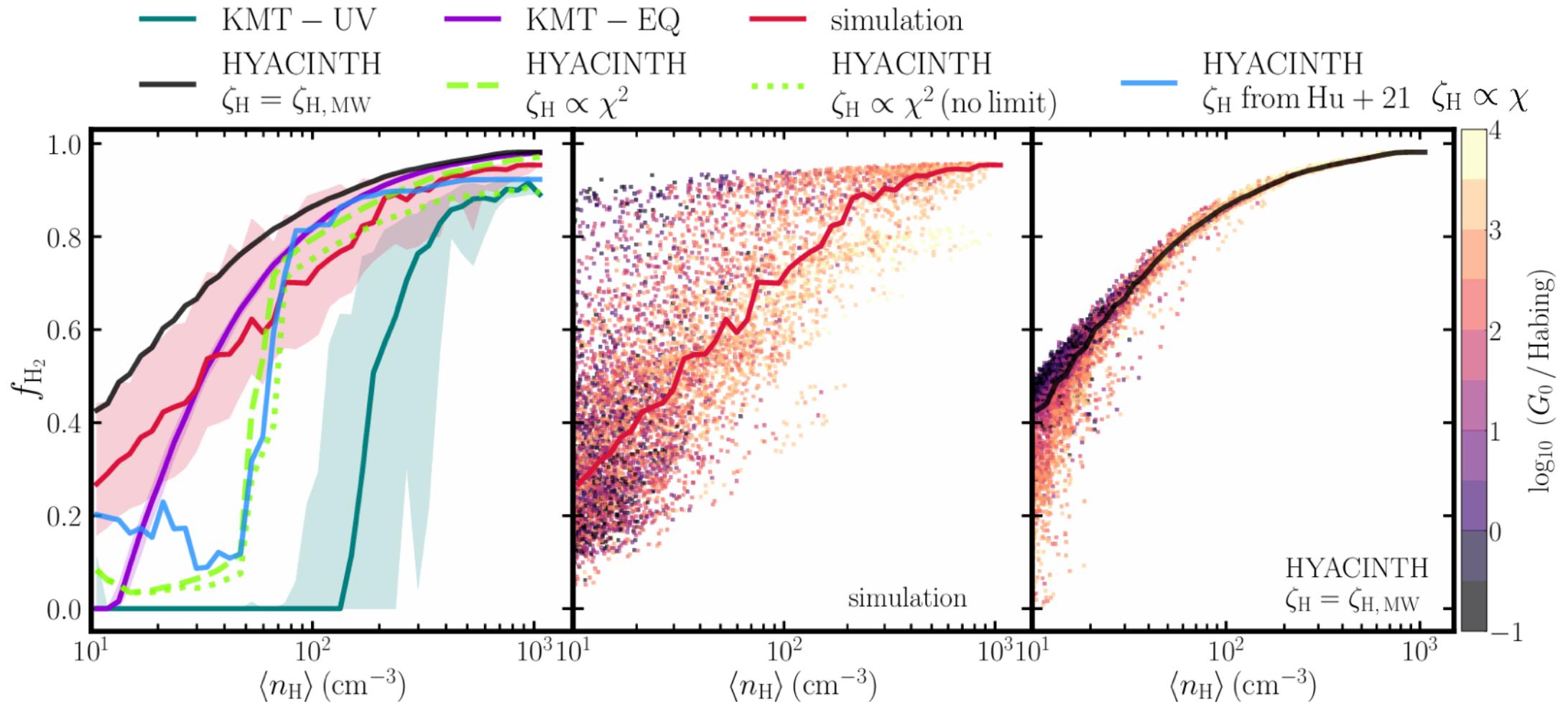


*HYACINTH captures the effect of **microscopic** (i.e., unresolved) density fluctuations on the **macroscopic** (i.e., on resolved scales) chemical abundances.*

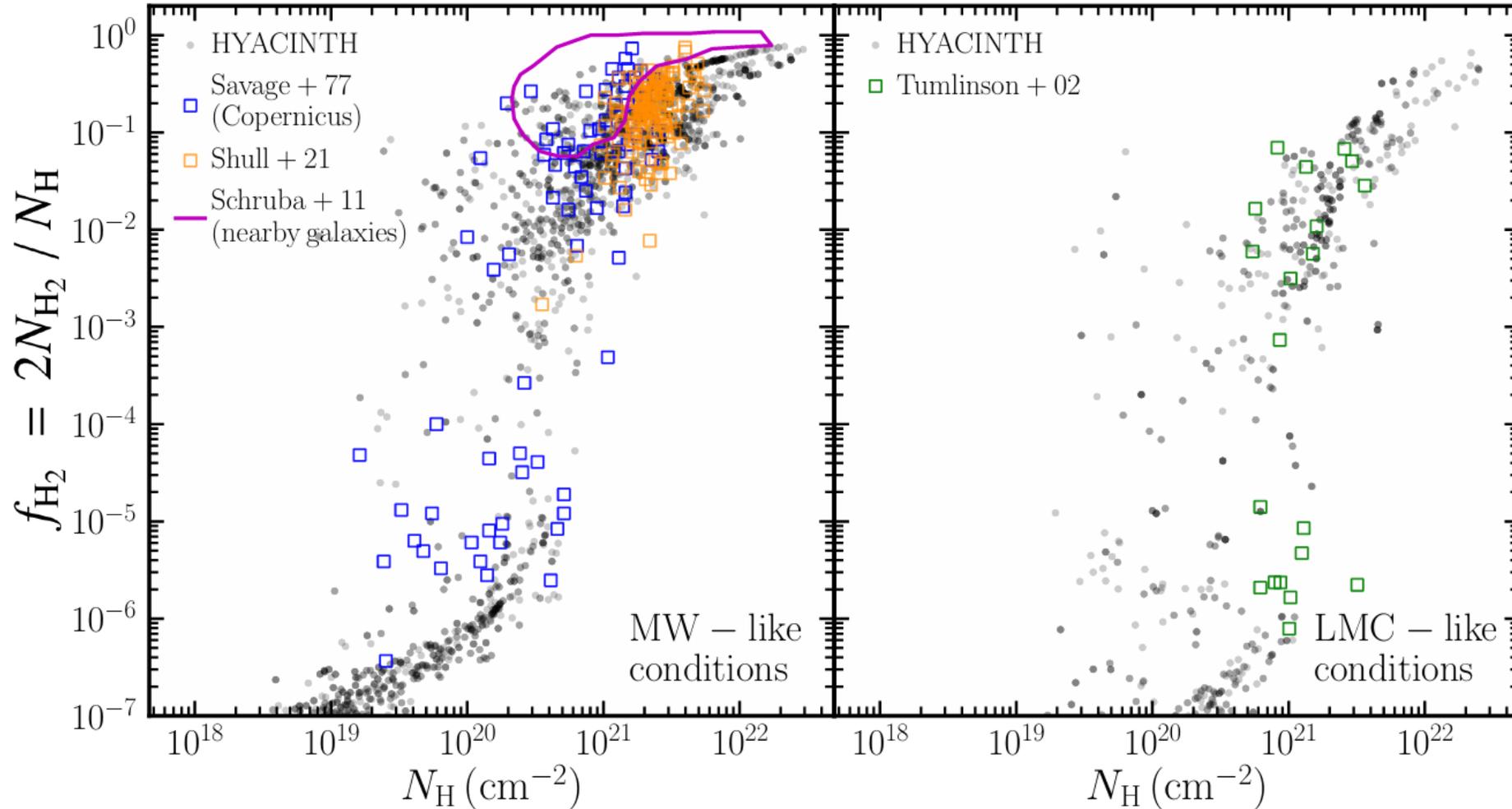
Comparison of dynamically-evolved abundances with Glover & Mac Low 2011



COMPARISON OF APPROACHES

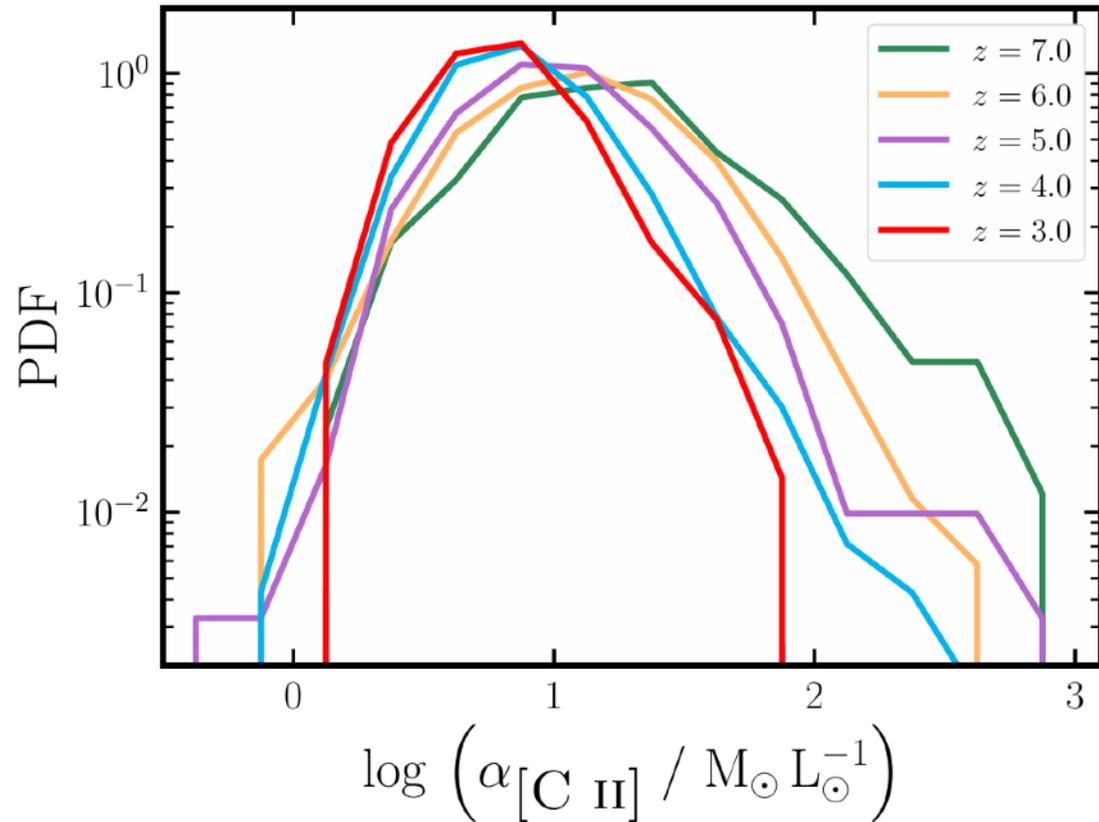


COMPARISON WITH OBSERVATIONS



THE CONVERSION FACTOR $\alpha_{[\text{CII}]}$

Distribution of $\alpha_{[\text{CII}]}$



$$\alpha_{[\text{CII}]} = \frac{M_{\text{mol}}}{L_{[\text{CII}]}}$$

The numerical factor used to convert the observed [CII] luminosity to a molecular gas mass