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Searching for heavy resonances via oblique parameters in non-linear effective frameworks

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<u>Sent to PRD [arXiv: 2503.05917]</u> JHEP 01 (**2014**) 157 [arXiv: 1310.3121] PRL 110 (**2013**) 181801 [arXiv: 1212.6769]

OUTLINE

- 1) Motivation
- 2) The effective resonance Lagrangian
- 3) Oblique Electroweak Observables: S and T at NLO
- 4) Phenomenology
- 5) Conclusions

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- Phenomenology 4)
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1. Motivation

- The Standard Model (SM) provides an extremely succesful description of the electroweak and strong interactions.
- A key feature is the particular mechanism adopted to break the electroweak gauge symmetry to the electroweak subgroup, SU(2)_L x U(1)_Y → U(1)_{QED}, so that the W and Z bosons become massive. The LHC discovered a new particle around 125 GeV*.
- Up to now all searches for New Physics have given negative results: Higgs couplings compatible with the SM and no new states. Therefore, we can use EFTs because it seems there is a large mass gap.



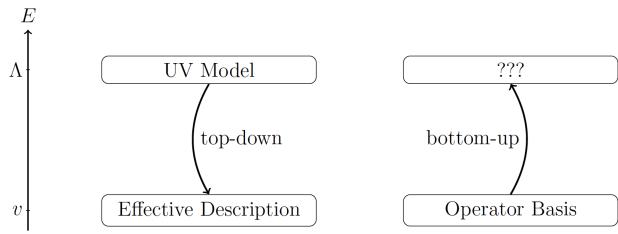


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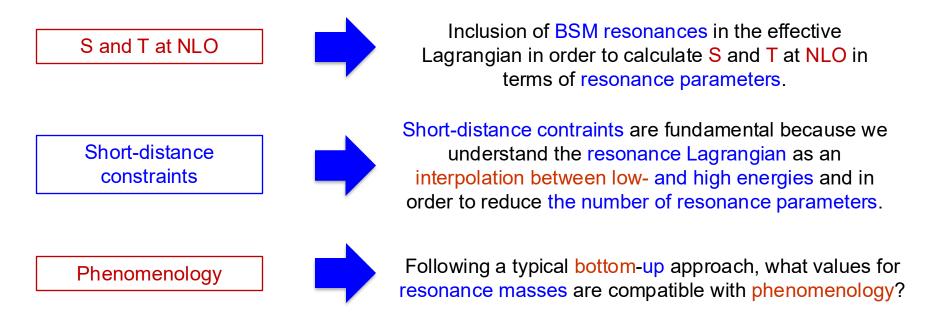
* <u>CMS</u> and <u>ATLAS</u> Collaborations.

Diagram by C. Krause [PhD thesis, 2016]

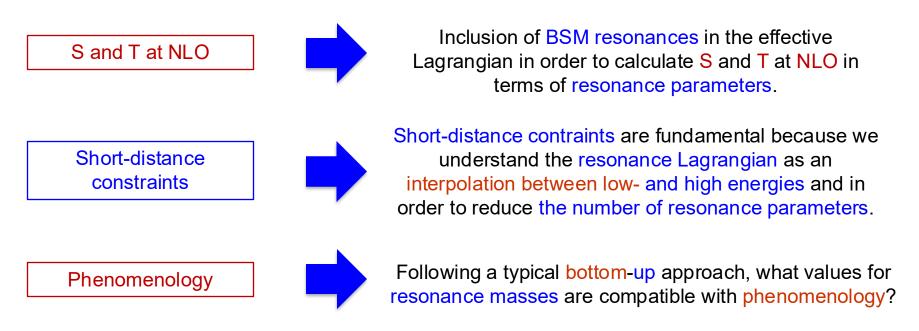
- Depending on the nature of the EWSB we have two possibilities for these EFTs (or something in between):
 - The decoupling (linear) EFT: SMEFT
 - SM-Higgs (forming a doublet with the EW Goldstones, as in the SM)
 - Weakly coupled
 - LO: SM
 - Expansion in canonical dimensions
 - The more general non-decoupling (non-linear) EFT: EWET, HEFT, EWChL
 - Non-SM Higgs (being a scalar singlet)
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 - LO: Higgsless SM + scalar h + 3 GB (chiral Lagrangian)
 - Expansion in loops or chiral dimensions
 - Some composite Higgs models can be described within the EWET.

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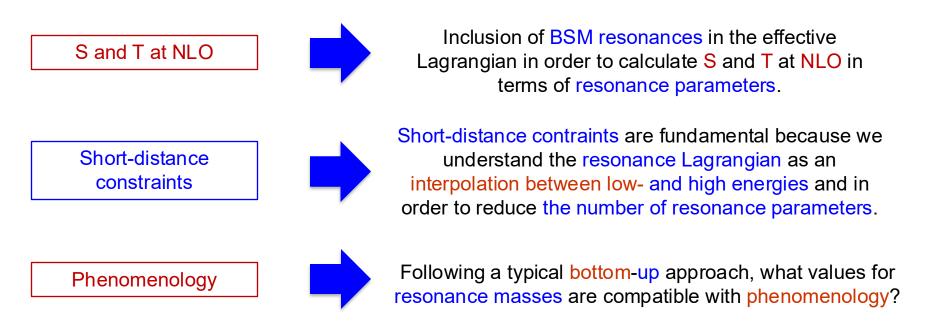
Similarities to Chiral Symmetry Breaking in QCD

i) Custodial symmetry: The Lagrangian is approximately invariant under global SU(2)_L x SU(2)_R transformations. Electroweak Symmetry Breaking (EWSB) turns to be $SU(2)_L x SU(2)_R \rightarrow SU(2)_{L+R}$.

ii) Similar to the Chiral Symmetry Breaking (ChSB) occurring in QCD, *i.e.*, similar to the "pion" Lagrangian of Chiral Perturbation Theory (ChPT)*[^], by replacing f_{π} by v=1/ $\sqrt{(2G_F)}$ =246 GeV. Rescaling naïvely we expect resonances at the TeV scale.

* <u>Weinberg '79</u> * Gasser and Leutwyler <u>'84</u> <u>'85</u> * Bijnens et al. <u>'99</u> <u>'00</u>	** <u>Ecker et al. '89</u> ** <u>Cirigliano et al. '06</u>	^ <u>Dobado, Espriu and Herrero '91</u> ^ <u>Espriu and Herrero '92</u> ^ <u>Herrero and Ruiz-Morales '94</u>
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What do we want to do?



Similarities to Chiral Symmetry Breaking in QCD

$QCD(q_a, G_{\mu u})$	Fundamental EW Theory (??)
\uparrow	\updownarrow
Resonance Chiral Theory	Resonance EW Theory
(σ, ρ, \ldots)	(M_V, M_A, \ldots)
\uparrow	\uparrow
Chiral Perturbation Theory	EW Effective Theory
(f_{π}, π_i)	(v, ϕ_i)

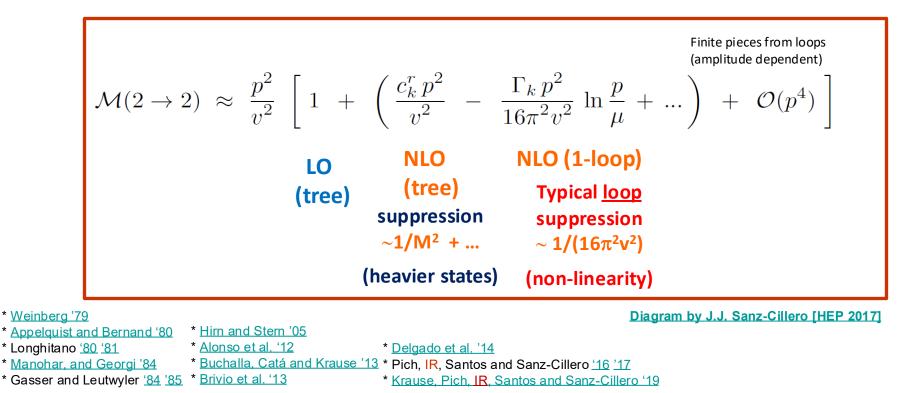
Diagram by J. Santos [VIII CPAN days, 2016]

2. The effective resonance Lagrangian

- ✓ Custodial symmetry
- ✓ Degrees of freedom: bosons χ (EW goldstones, gauge bosons, h) + fermions ψ + BSM resonances (V,A).
- ✓ Chiral power counting*

$$rac{\chi}{v} \sim \mathcal{O}\left(p^0
ight) = rac{\psi}{v} \sim \mathcal{O}\left(p
ight) = \partial_\mu, \, m \sim \mathcal{O}(p) = \mathcal{T} \sim \mathcal{O}(p) = g, \, g' \sim \mathcal{O}(p)$$

✓ Inclusion of fermions and odd-parity operators, not considered in our previous works <u>'13</u> <u>'14</u>.



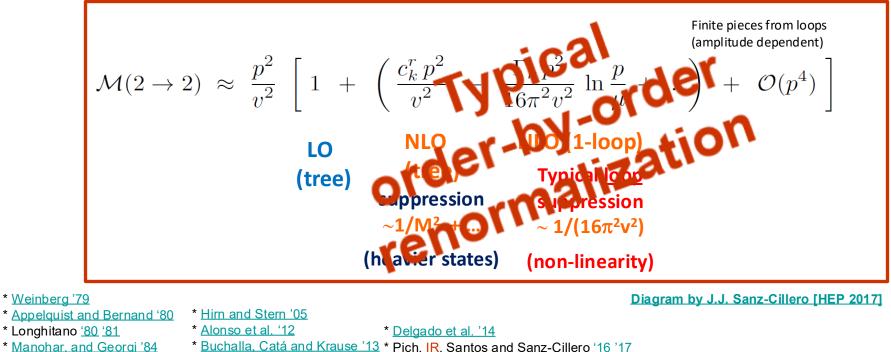
Searching for heavy resonances via oblique parameters in non-linear effective frameworks, I. Rosell

2. The effective resonance Lagrangian

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- * Buchalla, Catá and Krause '13 * Pich, IR, Santos and Sanz-Cillero '16 '17
- * Gasser and Leutwyler '84 '85 * Brivio et al. '13

* Krause, Pich, IR, Santos and Sanz-Cillero '19

✓ The Lagrangian reads:

$$\begin{split} \Delta \mathcal{L}_{\mathrm{RT}} &= -\frac{v^2}{4} \left(1 + \frac{2\kappa_W}{v} h \right) \langle u_{\mu} u^{\mu} \rangle_2 \\ &+ \langle V_{3\,\mu\nu}^1 \left(\frac{F_V}{2\sqrt{2}} f_+^{\mu\nu} + \frac{iG_V}{2\sqrt{2}} [u^{\mu}, u^{\nu}] + \frac{\widetilde{F}_V}{2\sqrt{2}} f_-^{\mu\nu} + \frac{\widetilde{\lambda}_1^{hV}}{\sqrt{2}} \left[(\partial^{\mu} h) u^{\nu} - (\partial^{\nu} h) u^{\mu} \right] + C_0^{V_3^1} J_T^{\mu\nu} \right) \rangle_2 \\ &+ \langle A_{3\,\mu\nu}^1 \left(\frac{F_A}{2\sqrt{2}} f_-^{\mu\nu} + \frac{\lambda_1^{hA}}{\sqrt{2}} \left[(\partial^{\mu} h) u^{\nu} - (\partial^{\nu} h) u^{\mu} \right] + \frac{\widetilde{F}_A}{2\sqrt{2}} f_+^{\mu\nu} + \frac{i\widetilde{G}_A}{2\sqrt{2}} [u^{\mu}, u^{\nu}] + \widetilde{C}_0^{A_3^1} J_T^{\mu\nu} \right) \rangle_2 \,. \end{split}$$

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- Including resonance masses, we have 12 resonance parameters. This number can be reduced by using short-distance information, but contrary to QCD, we ignore the underlying theory (BSM).
 - ✓ Vanishing form factors at high energies allow us to determine $(G_V, \tilde{G}_A, \lambda_1^{hA}, \tilde{\lambda}_1^{hV})$ in terms of the remaining parameters:

$$\frac{G_V}{F_A} = -\frac{\widetilde{G}_A}{\widetilde{F}_V} = \frac{\lambda_1^{hA} v}{\kappa_W F_V} = -\frac{\widetilde{\lambda_1^{hV}} v}{\kappa_W \widetilde{F}_A} = \frac{v^2}{F_V F_A - \widetilde{F}_V \widetilde{F}_A}$$

✓ Weinberg sum rules (WSRs) at LO and at NLO.

- ✓ 1st WSR. Vanishing of the 1/s term of $\Pi_{VV}(s) \Pi_{AA}(s)$: $\left(F_V^2 \tilde{F}_V^2\right) \left(F_A^2 \tilde{F}_A^2\right) = v^2$
- ✓ 2nd WSR. Vanishing of the 1/s² term of $\Pi_{VV}(s) \Pi_{AA}(s)$: $\left(F_V^2 \widetilde{F}_V^2\right) M_V^2 \left(F_A^2 \widetilde{F}_A^2\right) M_A^2 = 0$
- ✓ 1st WSR + LHC diboson production imply that contributions from fermionic cuts, terms with $(C_0^{V_3^1}, \tilde{C}_0^{A_3^1})$, are negligible.

3. Oblique Electroweak Observables: S and T at NLO

Universal oblique corrections via the EW boson self-energies (transverse in the Landau gauge)

$$\mathcal{L}_{\rm v.p.} \doteq -\frac{1}{2} W^3_{\mu} \Pi^{\mu\nu}_{33}(q^2) W^3_{\nu} - \frac{1}{2} B_{\mu} \Pi^{\mu\nu}_{00}(q^2) B_{\nu} - W^3_{\mu} \Pi^{\mu\nu}_{30}(q^2) B_{\nu} - W^+_{\mu} \Pi^{\mu\nu}_{WW}(q^2) W^-_{\nu}$$

✓ S parameter*: new physics in the difference between the Z self-energies at $Q^2=M_Z^2$ and $Q^2=0$.

$$e_3 = \frac{g}{g'} \widetilde{\Pi}_{30}(0), \qquad \Pi_{30}(q^2) = q^2 \widetilde{\Pi}_{30}(q^2) + \frac{g^2 \tan \theta_W}{4} v^2, \qquad S = \frac{16\pi}{g^2} \left(e_3 - e_3^{\rm SM} \right).$$

T parameter*: custodial symmetry breaking

$$e_1 = \frac{\Pi_{33}(0) - \Pi_{WW}(0)}{M_W^2} \stackrel{\text{\tiny sm}}{=} \frac{Z^{(+)}}{Z^{(-)}} - 1 \qquad T = \frac{4\pi}{g^{\prime 2} \cos^2 \theta_W} \left(e_1 - e_1^{\rm SM}\right)$$

 We follow the useful dispersive representation introduced by Peskin and Takeuchi* for S and a dispersion relation for T (checked for the lowest cuts):

$$S = \frac{16\pi}{g^2 \tan \theta_W} \int_0^\infty \frac{\mathrm{d}t}{t} \left(\rho_S(t) - \rho_S(t)^{\mathrm{SM}} \right)$$
$$T = \frac{16\pi}{g'^2 \cos^2 \theta_W} \int_0^\infty \frac{\mathrm{d}t}{t^2} \left(\rho_T(t) - \rho_T(t)^{\mathrm{SM}} \right)$$

- ✓ They need to be well-behaved at short-distances to get the convergence of the integral.
- ✓ S and T parameters are defined for a reference value for the SM Higgs mass.
- * <u>Peskin and Takeuchi '92</u>
- ** Barbieri et al. '93

- ✓ We consider only the lightest two-particle absorptive cuts ($\phi\phi$, $h\phi$, $\psi\bar{\psi}$) and in general we take as working assumptions M_A > M_V and $\tilde{F}_{V,A}^2 < F_{V,A}^2$.
- ✓ LO result (T_{LO} =0):

$$\checkmark \quad \text{With 1st and 2nd WSR:} \quad S_{\text{LO}} = \frac{4\pi v^2}{M_V^2} \left(1 + \frac{M_V^2}{M_A^2} \right) \quad \longrightarrow \quad \frac{4\pi v^2}{M_V^2} < S_{\text{LO}} < \frac{8\pi v^2}{M_V^2}$$
$$\checkmark \quad \text{With only the 1st WSR:} \quad S_{\text{LO}} > \frac{4\pi v^2}{M_V^2}$$

NLO result with 1st and 2nd WSR:

$$S_{\rm NLO} = 4\pi v^2 \left(\frac{1}{M_V^{r\,2}} + \frac{1}{M_A^{r\,2}}\right) + \Delta S_{\rm NLO}^{\rm P-even} + \Delta S_{\rm NLO}^{\rm P-odd}$$

$$\Delta S_{\rm NLO}^{\rm P-even} = \frac{1}{12\pi} \left[\left(1 - \kappa_W^2\right) \left(\log\frac{M_V^2}{m_h^2} - \frac{11}{6}\right) + \kappa_W^2 \left(\frac{M_A^2}{M_V^2} - 1\right) \log\frac{M_A^2}{M_V^2} \right]$$

$$\Delta S_{\rm NLO}^{\rm P-odd} = \frac{1}{12\pi} \left(\frac{\widetilde{F}_V^2}{F_V^2} + 2\kappa_W^2 \frac{\widetilde{F}_V \widetilde{F}_A}{F_V F_A} - \kappa_W^2 \frac{\widetilde{F}_A^2}{F_A^2}\right) \left(\frac{M_A^2}{M_V^2} - 1\right) \log\frac{M_A^2}{M_V^2} + \mathcal{O}\left(\frac{\widetilde{F}_{V,A}^4}{F_{V,A}^4}\right)$$

P-even results correspond to Pich, IR and Sanz-Cillero <u>'13</u> <u>'14</u>

$$T_{\rm NLO} = \Delta T_{\rm NLO}^{\rm P-even} + \Delta T_{\rm NLO}^{\rm P-odd}$$

$$\Delta T_{\rm NLO}^{\rm P-even} = \frac{3}{16\pi\cos^2\theta_W} \left[\left(1 - \kappa_W^2\right) \left(1 - \log\frac{M_V^2}{m_h^2}\right) + \kappa_W^2 \log\frac{M_A^2}{M_V^2} \right]$$

$$\Delta T_{\rm NLO}^{\rm P-odd} = \frac{3}{16\pi\cos^2\theta_W} \left\{ 2\kappa_W^2 \frac{\tilde{F}_A}{F_A} - 2\frac{\tilde{F}_V}{F_V} + \frac{M_V^2}{M_A^2 - M_V^2} \log\frac{M_A^2}{M_V^2} \left(2\frac{\tilde{F}_V}{F_V} - 2\kappa_W^2 \frac{M_A^2}{M_V^2} \frac{\tilde{F}_A}{F_A}\right) + \frac{M_V^2}{M_A^2 - M_V^2} \log\frac{M_A^2}{M_V^2} \left[\left(\kappa_W^2 \frac{\tilde{F}_A^2}{F_A^2} - \frac{\tilde{F}_V^2}{F_V^2}\right) \left(1 + \frac{M_A^2}{M_V^2}\right) + 2\frac{\tilde{F}_V \tilde{F}_A}{F_V F_A} \left(\kappa_W^2 \frac{M_A^2}{M_V^2} - 1\right) + 2\left(\frac{\tilde{F}_V^2}{F_V^2} - \kappa_W^2 \frac{\tilde{F}_A^2}{F_A^2} + \left(1 - \kappa_W^2\right) \frac{\tilde{F}_V \tilde{F}_A}{F_V F_A}\right) \right\} + \mathcal{O}\left(\frac{\tilde{F}_{V,A}^3}{F_{V,A}^3}\right)$$



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NLO result with only the 1st WSR:

$$\begin{split} S_{\rm NLO} &> \frac{4\pi v^2}{M_V^{r\,2}} + \Delta \widetilde{S}_{\rm NLO}^{\rm P-even} + \Delta \widetilde{S}_{\rm NLO}^{\rm P-odd} \\ \Delta \widetilde{S}_{\rm NLO}^{\rm P-even} &= \frac{1}{12\pi} \left[\left(1 - \kappa_W^2 \right) \left(\log \frac{M_V^2}{m_h^2} - \frac{11}{6} \right) - \kappa_W^2 \left(\log \frac{M_A^2}{M_V^2} - 1 + \frac{M_A^2}{M_V^2} \right) \right] \,. \\ \Delta \widetilde{S}_{\rm NLO}^{\rm P-odd} &= \frac{1}{12\pi} \left\{ \left(1 - \frac{M_A^2}{M_V^2} \right) \left[\frac{\widetilde{F}_V^2}{F_V^2} + \kappa_W^2 \frac{\widetilde{F}_A}{F_A} \left(2 \frac{\widetilde{F}_V}{F_V} - \frac{\widetilde{F}_A}{F_A} \right) \right] \right. \\ &+ \log \frac{M_A^2}{M_V^2} \left(\frac{\widetilde{F}_V^2}{F_V^2} - \kappa_W^2 \frac{\widetilde{F}_A^2}{F_A^2} - 2 \frac{\widetilde{F}_V \widetilde{F}_A}{F_V F_A} \right) \right\} + \mathcal{O} \left(\frac{\widetilde{F}_{V,A}^4}{F_{V,A}^4} \right) \end{split}$$

$$T_{\rm NLO} = \Delta T_{\rm NLO}^{P-\text{even}} + \Delta T_{\rm NLO}^{P-\text{odd}}$$

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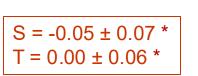
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P-even results correspond to Pich, IR and Sanz-Cillero <u>'13</u> <u>'14</u>



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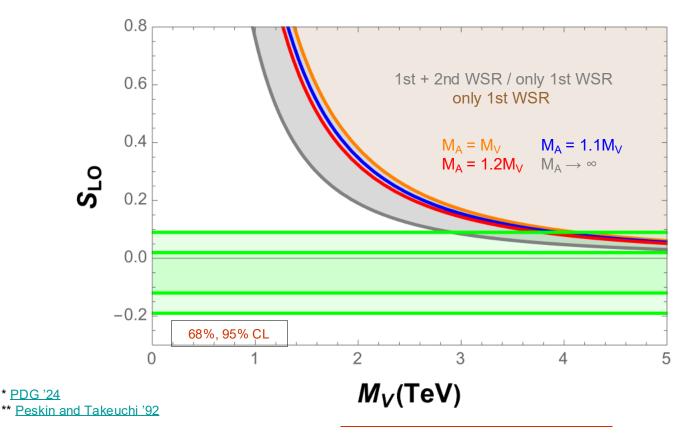
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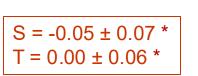
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- Oblique electroweak observables** (S and T).
- Short-distance constraints.
- ✓ Assumptions: lightest two-particle absorptive cuts, $M_A > M_V$ and $\tilde{F}_{V,A}^2 < F_{V,A}^2$.





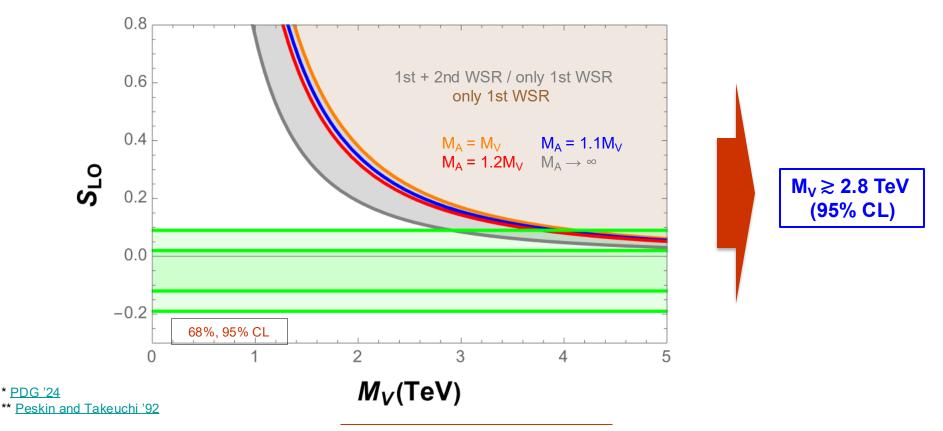
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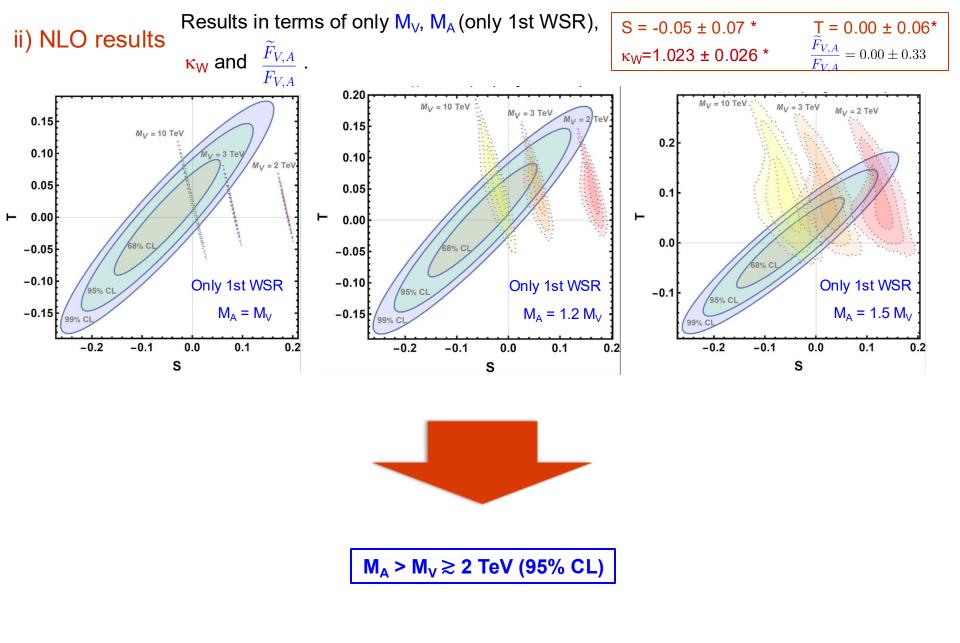


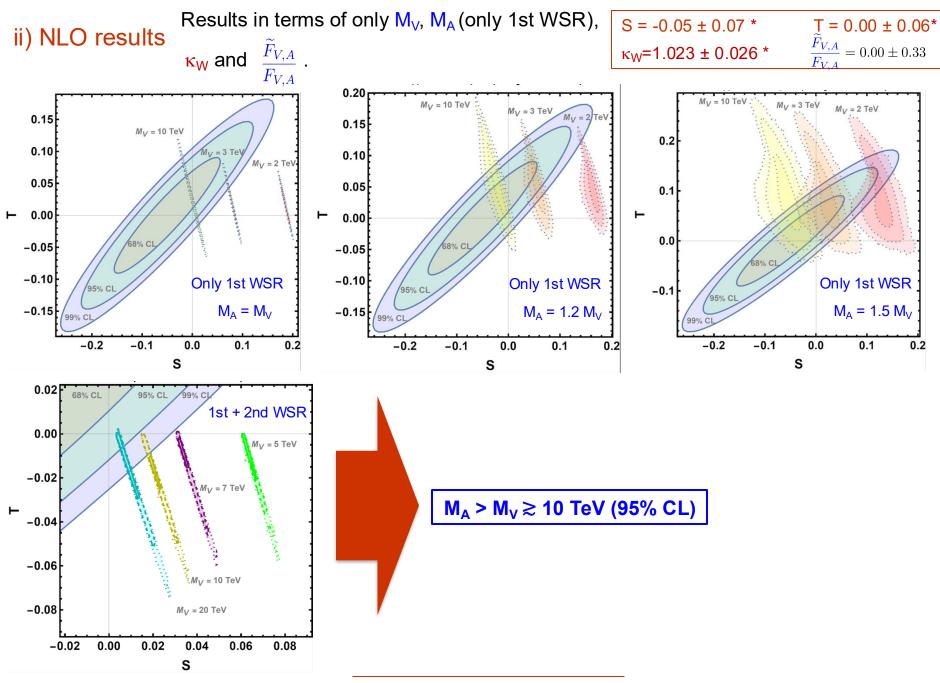
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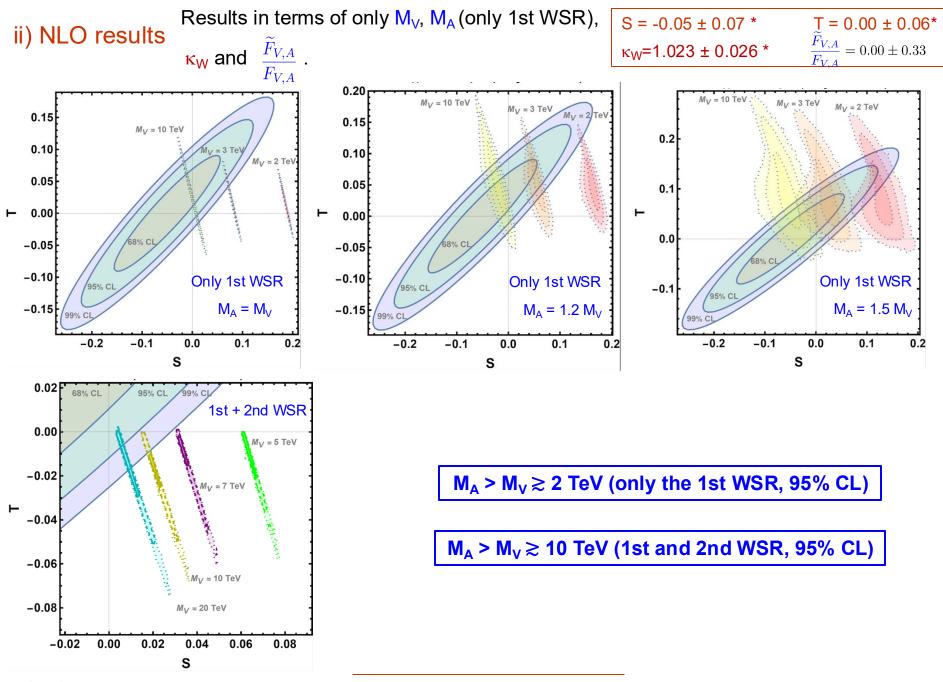
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i) LO results









4. Conclusions

- ✓ Up to now all searches for New Physics have given negative results: Higgs couplings compatible with the SM and no new states. Therefore we can use EFTs because we have a mass gap.
- As a consequence of the mass gap, bottom-up EFTs are appropriate to search for BSM. Depending on the nature of the EWSB we have two possibilities:
 - ✓ Decoupling (linear) EFT: SMEFT
 - ✓ SM-Higgs, weakly coupled and expansion in canonical dimensions
 - ✓ Non-decoupling (non-linear) EFT: EWET (HEFT or EWChL)
 - Non-SM Higgs, strongly coupled and expansion in loops or chiral dimension
- ✓ Phenomenology: S and T at NLO
 - Short-distance constraints: WSRs and well-behaved form factors at high energies.
 - ✓ Assumptions: lightest two-particle absorptive cuts, $M_A \gtrsim M_V$ and $\tilde{F}_{V,A}^2 < F_{V,A}^2$
 - **S**, **T** and κ_W from the PDG.

✓ Results in terms of only M_V, M_A, and $\frac{\tilde{F}_{V,A}}{F_{V,A}}$

Room for these BSM scenarios
(95% CL) $M_A > M_V \gtrsim 2$ TeV (only 1st WSR)
 $M_A > M_V \gtrsim 10$ TeV (1st and 2nd WSR)