

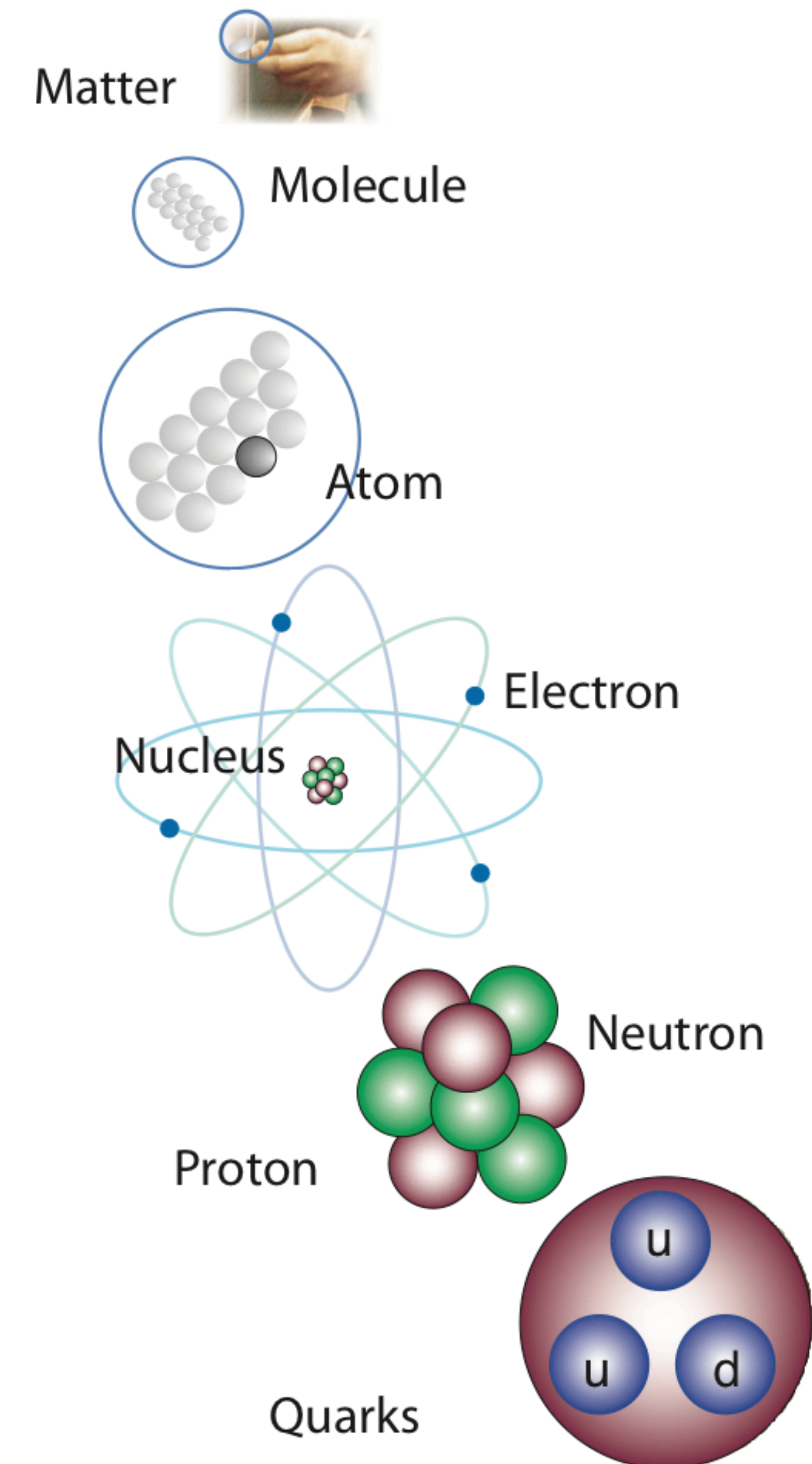
Recent Highlight on light hadrons at BESIII

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(On behalf of the BESIII Collaboration)

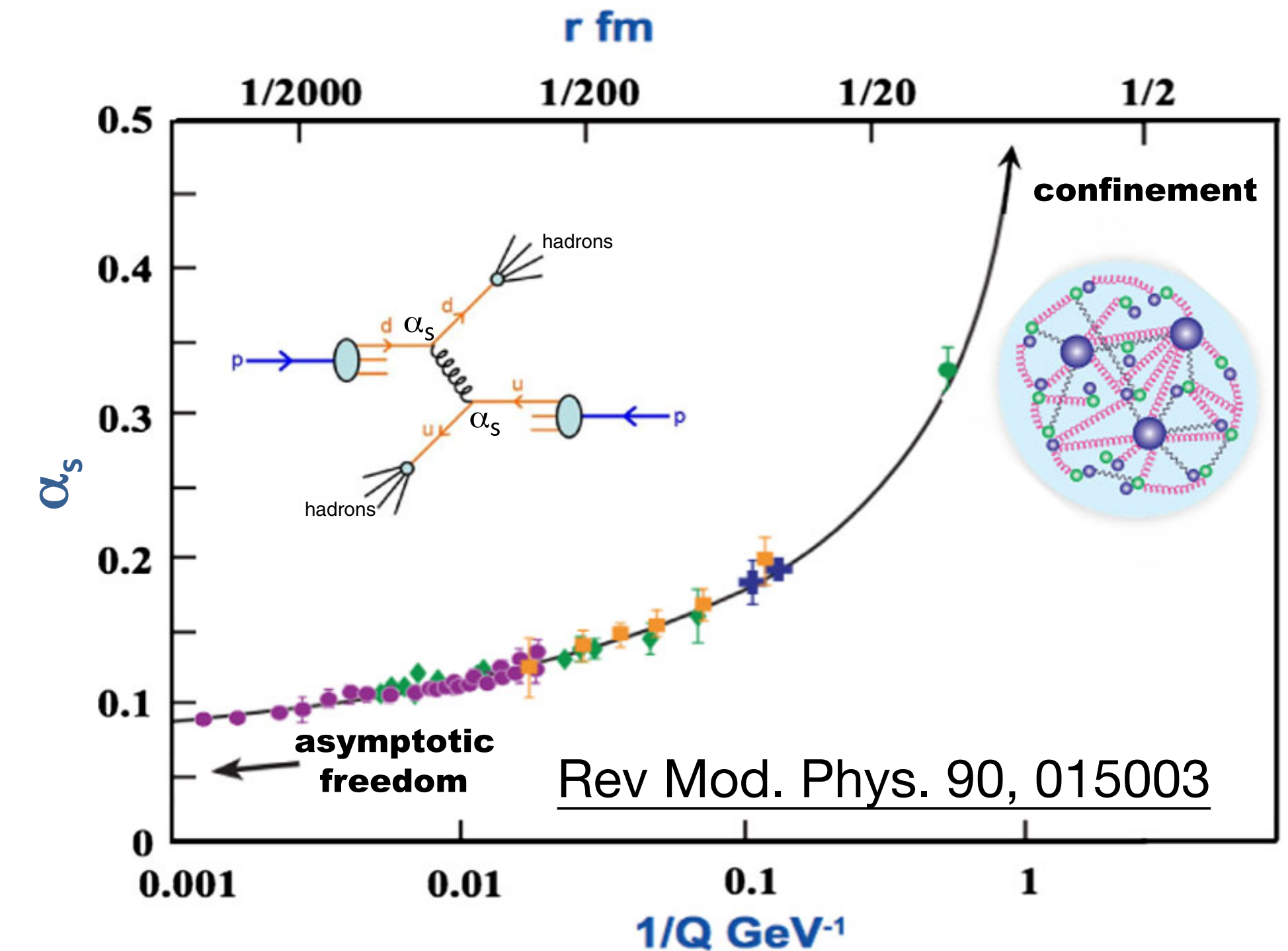
Institute of High Energy Physics, CAS

Fundamental Structure of Matters



Standard Model of Elementary Particles

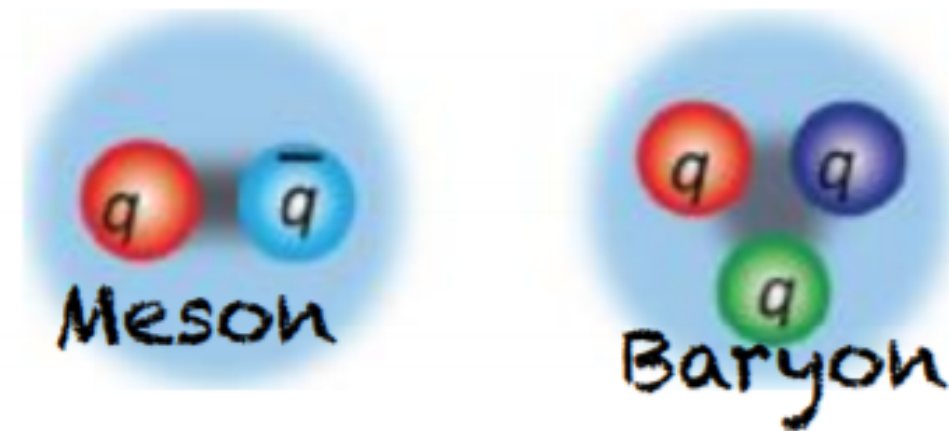
three generations of matter (fermions)			interactions / force carriers (bosons)	
mass charge spin	$\approx 2.2 \text{ MeV}/c^2$ $\frac{2}{3}$ $\frac{1}{2}$	$\approx 1.28 \text{ GeV}/c^2$ $\frac{2}{3}$ $\frac{1}{2}$	$\approx 173.1 \text{ GeV}/c^2$ $\frac{2}{3}$ $\frac{1}{2}$	$\approx 125.11 \text{ GeV}/c^2$ 0 0
QUARKS	u up	c charm	t top	g gluon
	d down	s strange	b bottom	γ photon
LEPTONS	$\approx 0.511 \text{ MeV}/c^2$ -1 $\frac{1}{2}$	$\approx 105.66 \text{ MeV}/c^2$ -1 $\frac{1}{2}$	$\approx 1.7768 \text{ GeV}/c^2$ -1 $\frac{1}{2}$	$\approx 91.19 \text{ GeV}/c^2$ 0 1
	e electron	μ muon	τ tau	Z Z boson
	$< 1.0 \text{ eV}/c^2$ 0 $\frac{1}{2}$	$< 0.17 \text{ MeV}/c^2$ 0 $\frac{1}{2}$	$< 18.2 \text{ MeV}/c^2$ 0 $\frac{1}{2}$	$\approx 80.360 \text{ GeV}/c^2$ ± 1 1
	ν_e electron neutrino	ν_μ muon neutrino	ν_τ tau neutrino	W W boson
				GAUGE BOSONS VECTOR BOSONS
				SCALAR BOSONS



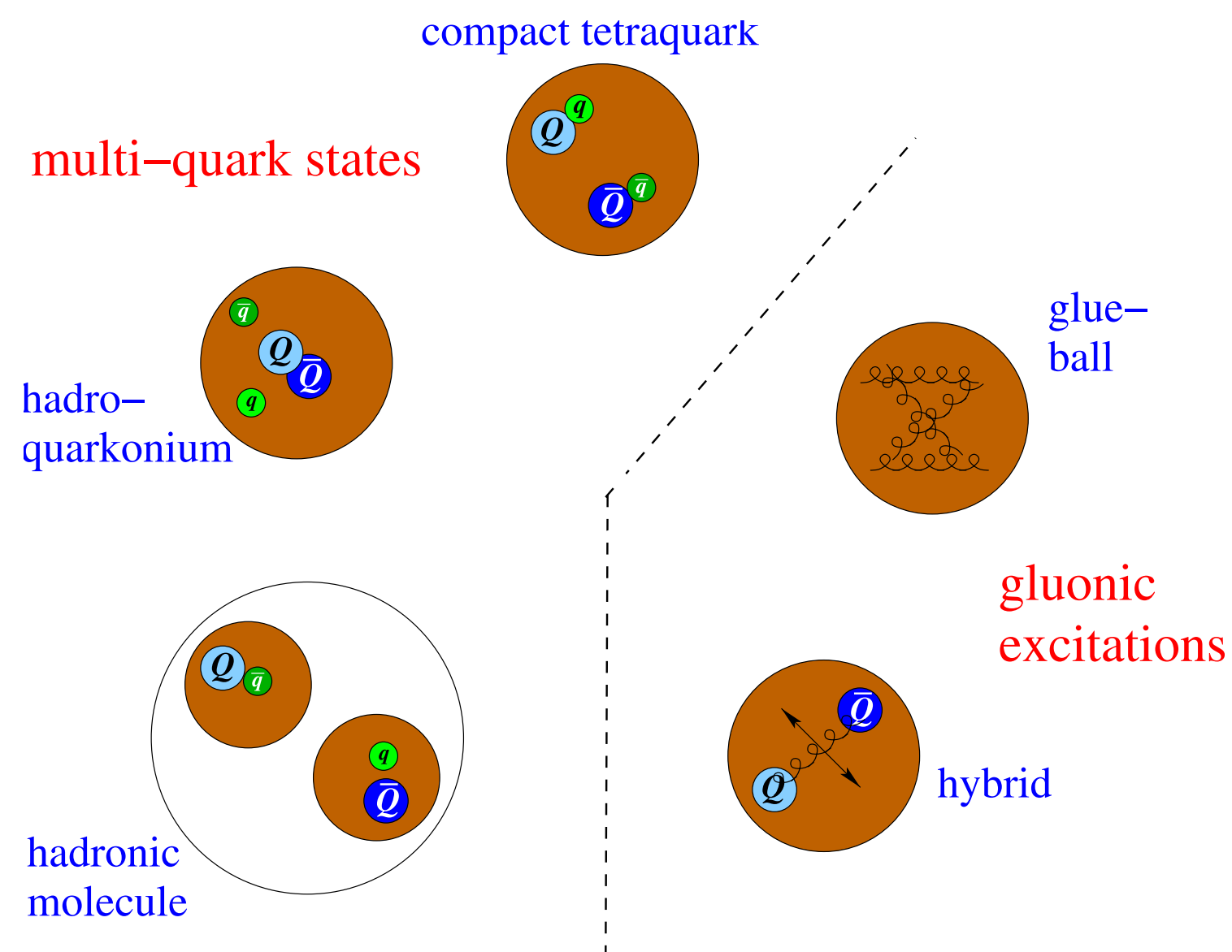
Hadron spectroscopy can provide us clues for the understanding of fundamental structure via the hadron property study

Forms of hadrons

Quark model



New forms of hadrons



Physics report 873 (2020) 1-154

◆ Quark model (QM)

- ◆ Identify hadrons as compound objects consisting of quarks and antiquarks
- ◆ Dynamics description inside hadrons

◆ New form of hadrons:

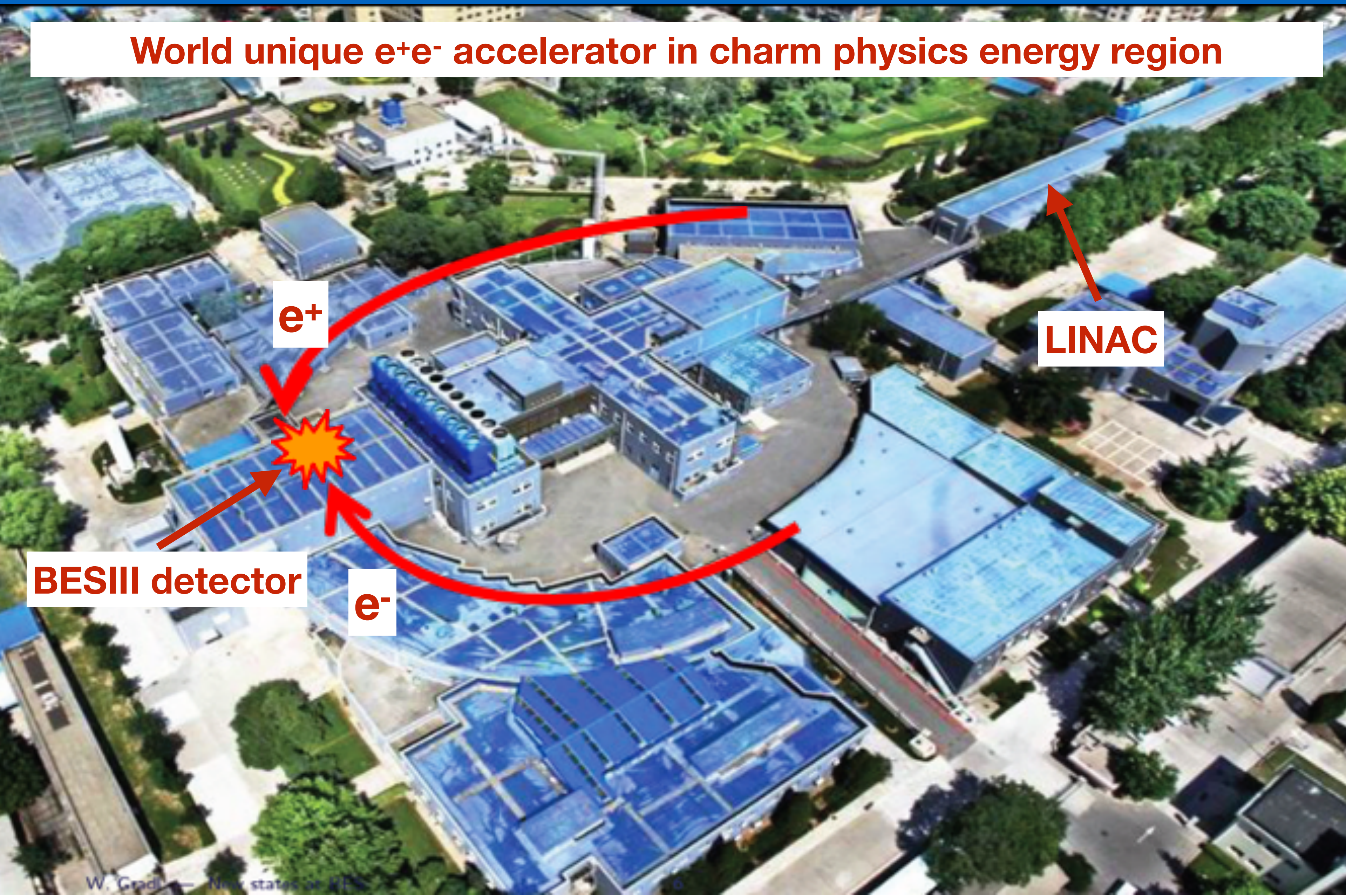
- ◆ **Multi-quark:** quark number ≥ 4
- ◆ **Hybrid state:** the mixture of quark and gluon
- ◆ **Glueball:** composed of gluons

◆ Identification from QM: challenging

- ◆ **Exotic quantum states**
- ◆ **Crypto exotic with particular properties**

Beijing Electron Positron Collider (BEPCII)

World unique e^+e^- accelerator in charm physics energy region



2004: Construction

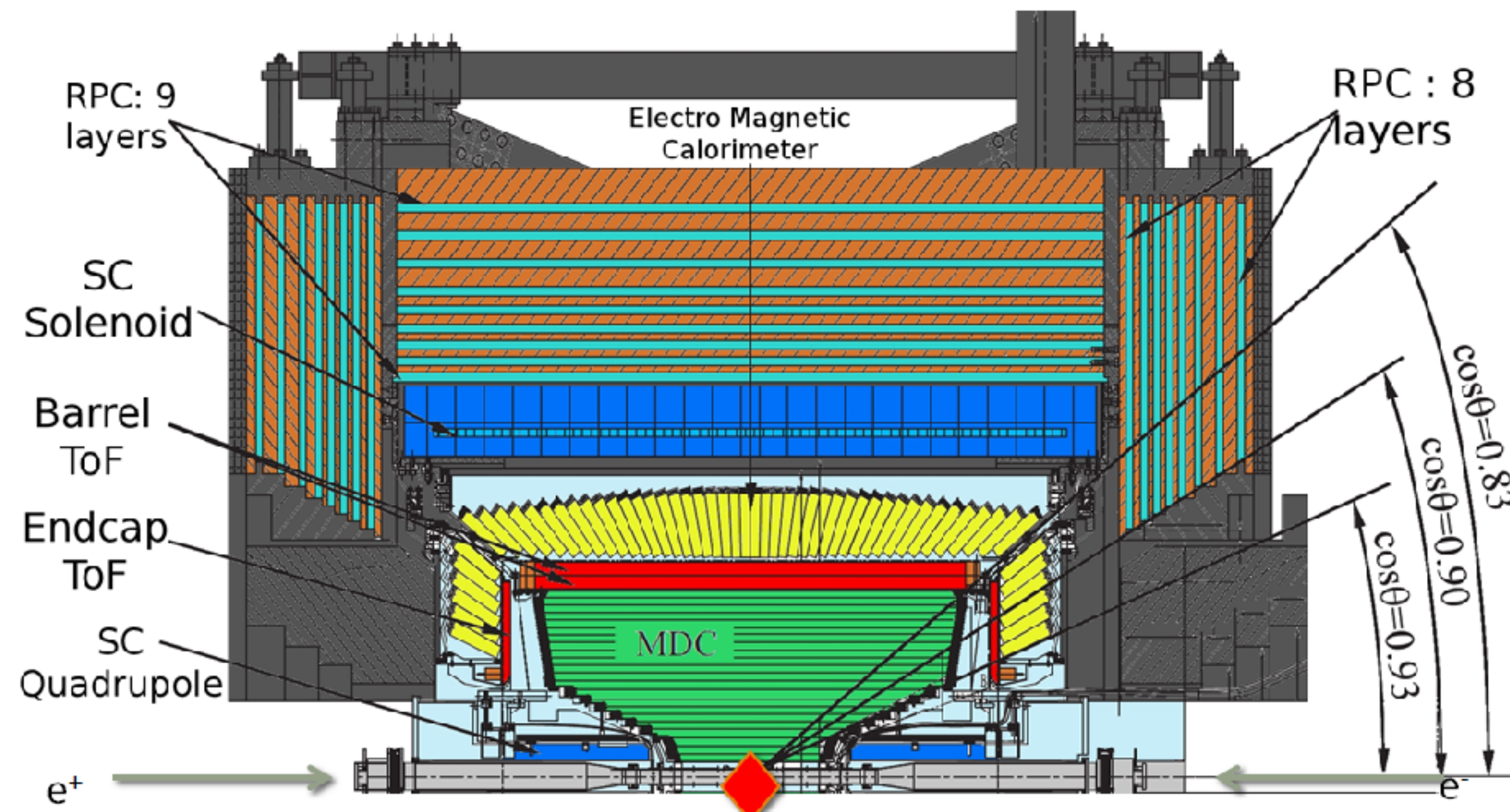
- Double rings
- Beam energy:
1.0 - 2.3 (2.45) GeV
- Designed luminosity:
 $1 \times 10^{33} \text{ cm}^{-2} \text{ s}^{-1}$

2008: test run

2009-now: BESIII physics runs

BESIII detector

Designed for neutral and charged particle with excellent resolution, PID, and large coverage



Total weight 730 ton,
~40,000 readout channel
Data rate: 5kHz, 50Mb/s

- ◆ Magnet: 1T Superconducting
- ◆ MDC: small cell & He gas
 - $\sigma_{xy} = 130 \mu\text{m}$
 - $\sigma_p/p = 0.5\% @ 1\text{GeV}$
 - $dE/dx = 6\%$
- ◆ TOF: plastic scintillator/MRPC
 - $\sigma_T = 80 \text{ ps}$ Barrel
 - $\sigma_T = 110 (60) \text{ ps}$ Endcap
- ◆ EMC: CsI crystals
 - $\Delta E/E = 2.5\% @ 1\text{GeV}$ - Barrel
 - $\Delta E/E = 5\% @ 1\text{GeV}$ - Endcap
- ◆ Muon ID: 9 layer RPC

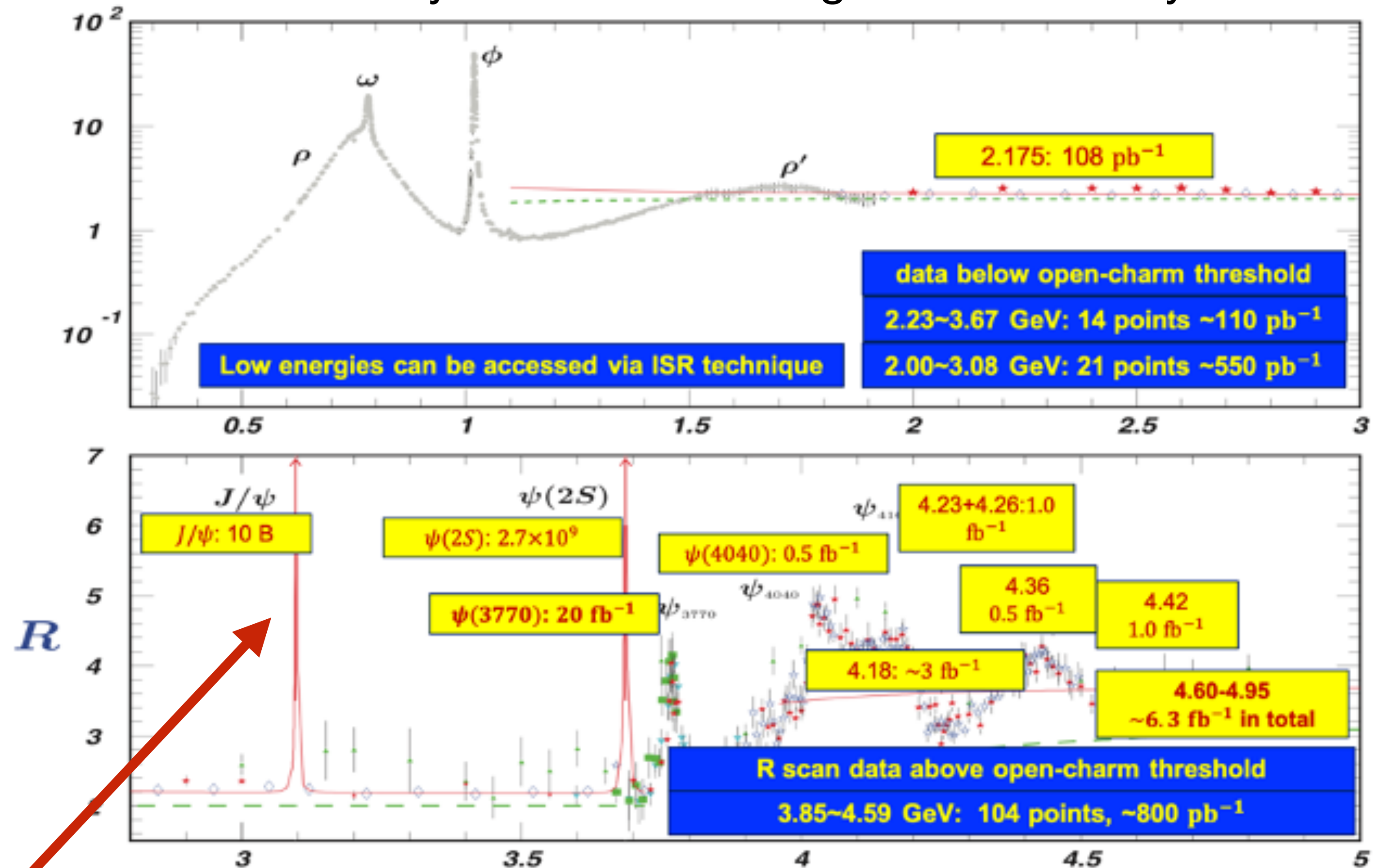
Has been in full operation since 2008, all sub-detectors are in a very good status!

BESIII Data samples

Totally about 50fb⁻¹ integrated luminosity

Data sets collected so far include

- ♦ 10×10⁹ J/ψ events
- ♦ 2.7×10⁹ ψ(2S) events
- ♦ 20 fb⁻¹ ψ(3770)
- ♦ Scan data between 1.8 and 3.08 GeV, and above 3.74GeV
- ♦ Large datasets for XYZ studies:
Scan with >500pb⁻¹ per energy point space 10-20MeV apart

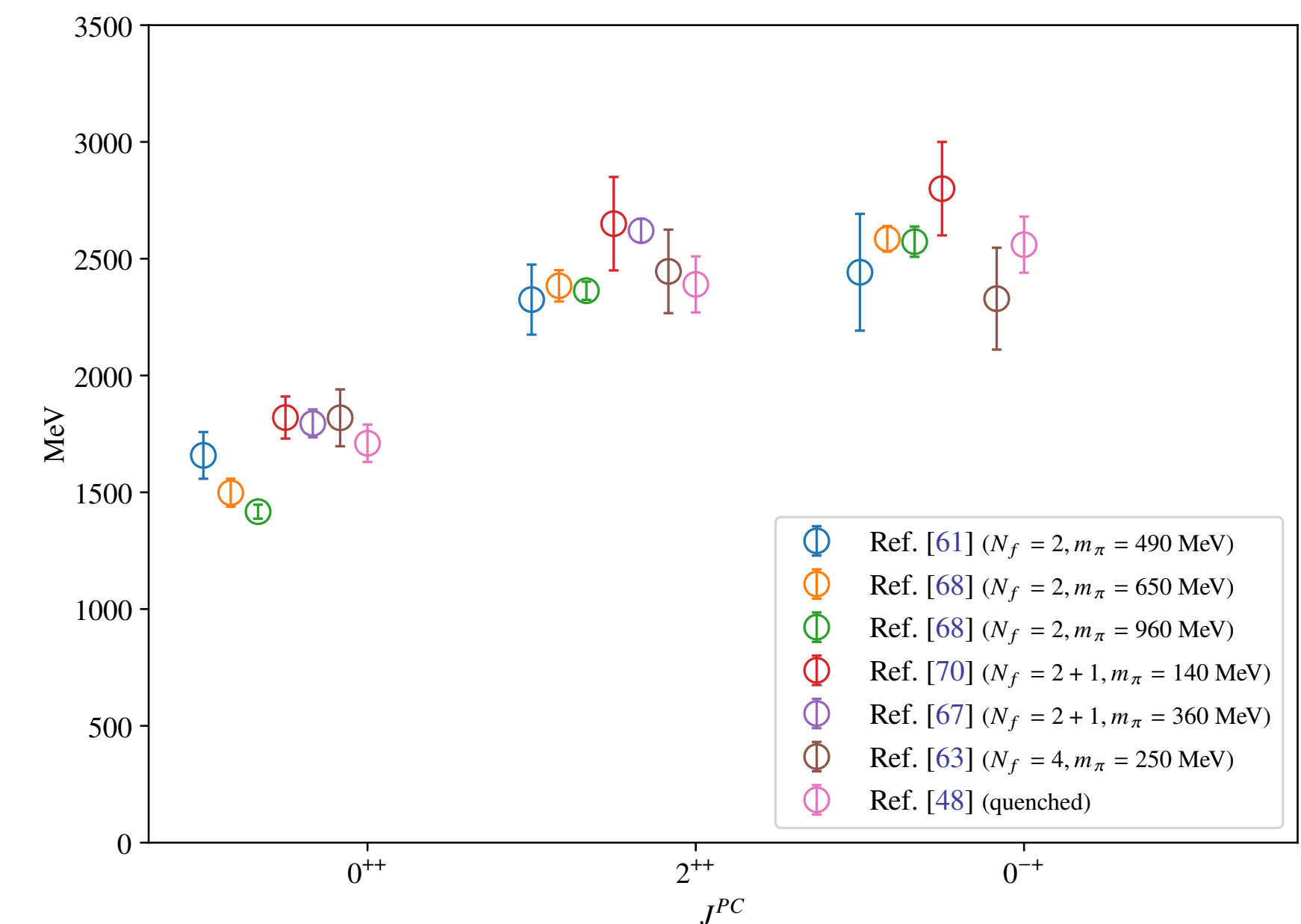


World largest J/ψ data sample : ~10 billion

Glueballs

- ◆ The basic theory for strong interactions is quantum chromodynamics (QCD)
 - ✦ **Gluon self-interaction:** prediction of non-Abelian Gauge SU(3) QCD theory
 - ✦ Glueballs are **unique particles** formed **with force carriers via self-interactions**
 - ✦ **Glueballs to QCD** is just as important as **Higgs Boson to EW**

- ◆ **Lattice QCD** (LQCD) is a non-perturbative method from the first principles in theory.
- ◆ **Different lattice QCD groups** (including lattice simulations with dynamical quarks)
 - ✦ Predictions on **masses and production rates** of pure glueballs
 - ✦ Consistent results and expected to be reliable.
- ◆ Lattice QCD predictions on glueball masses:
 - ✦ **0^{++} ground state:** 1.5 - 1.7 GeV/c²
 - ✦ **2^{++} ground state:** 2.3 - 2.4 GeV/c²
 - ✦ **0^{-+} ground state:** 2.3 - 2.6 GeV/c²



[arxiv:2305.04869](https://arxiv.org/abs/2305.04869)

Historical Glueball Candidates

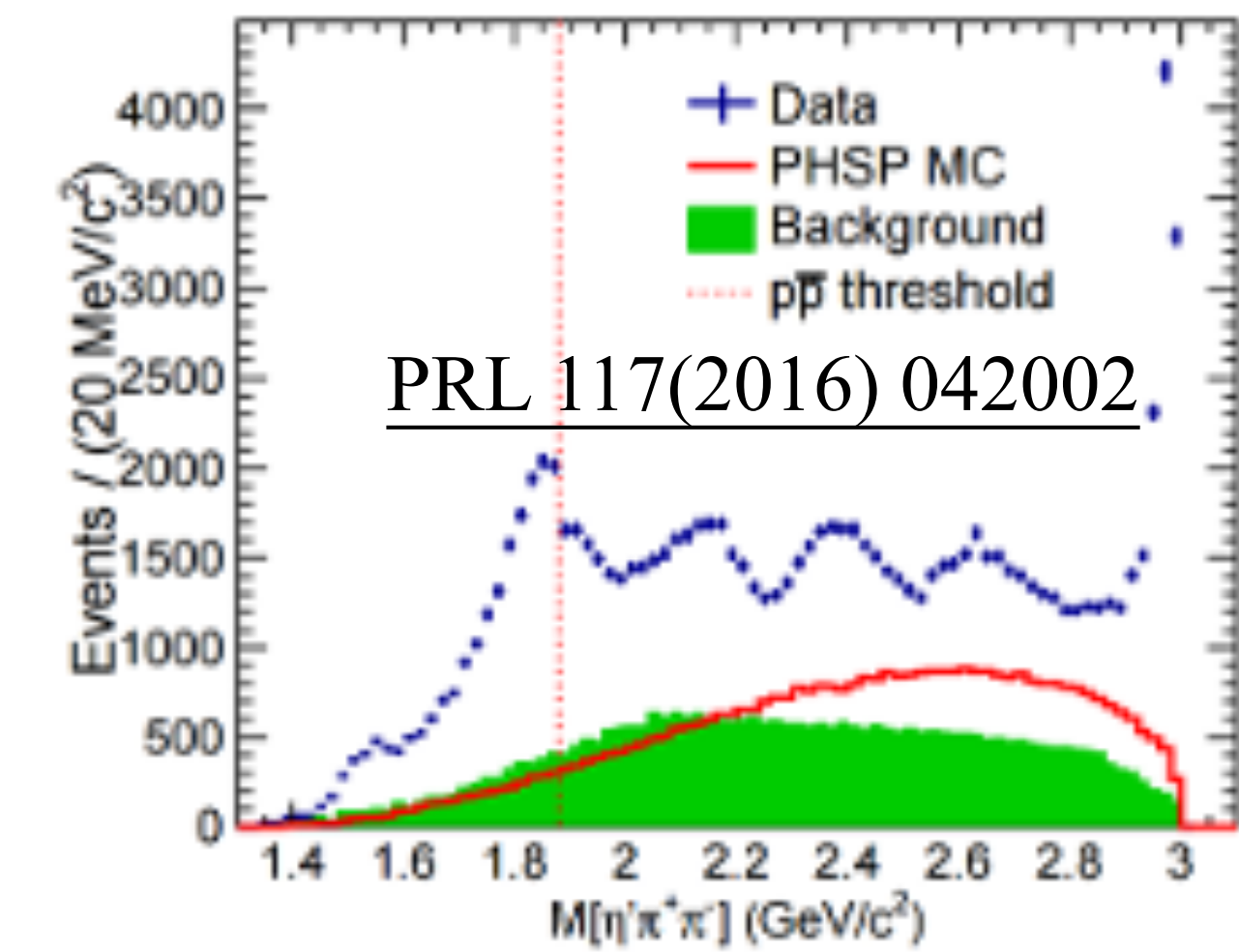
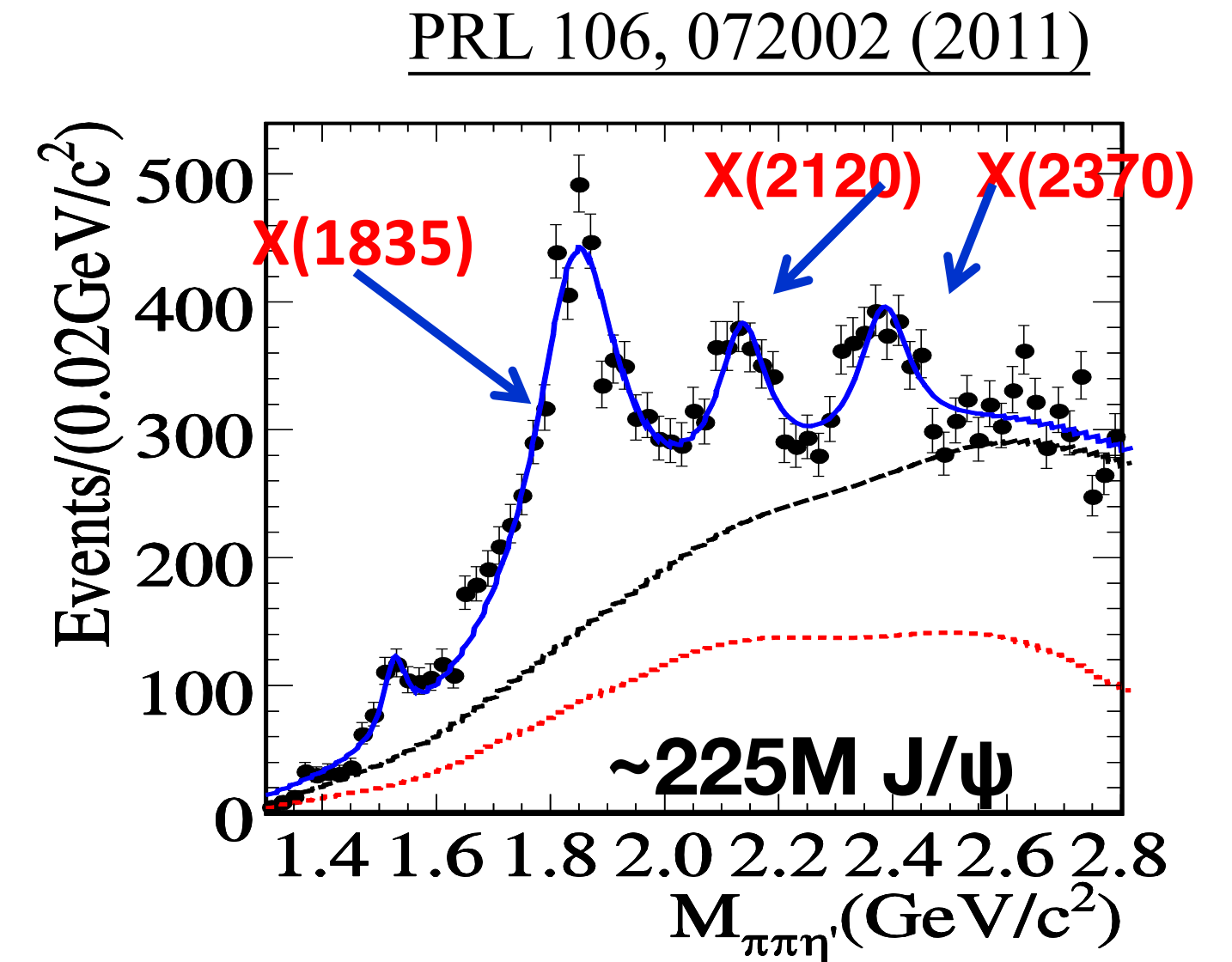
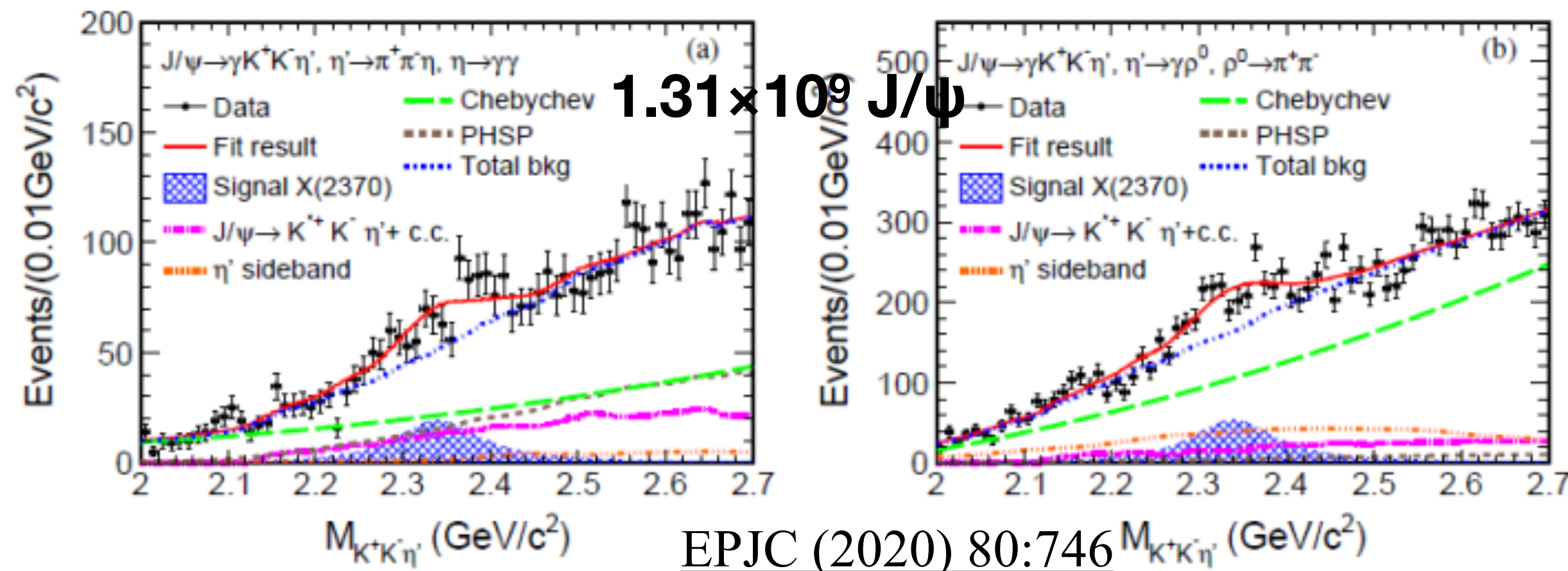
- ◆ Many experiments searched for glueballs over the past 4 decades
- ◆ Many historical glueball candidates, but with some difficulties/controversies.
 - ✦ Scalar Glueball candidate (0^{++}): $f_0(1500)$, $f_0(1710)$
 - ✦ Tensor Glueball candidate (2^{++}): $f_2(2340)$
 - ✦ Pseudoscalar Glueball candidate (0^{-+}): $\eta(1405)$

X(2370)

◆ Discovered by BESIII in $J/\psi \rightarrow \gamma\pi^+\pi^-\eta'$ in 2011

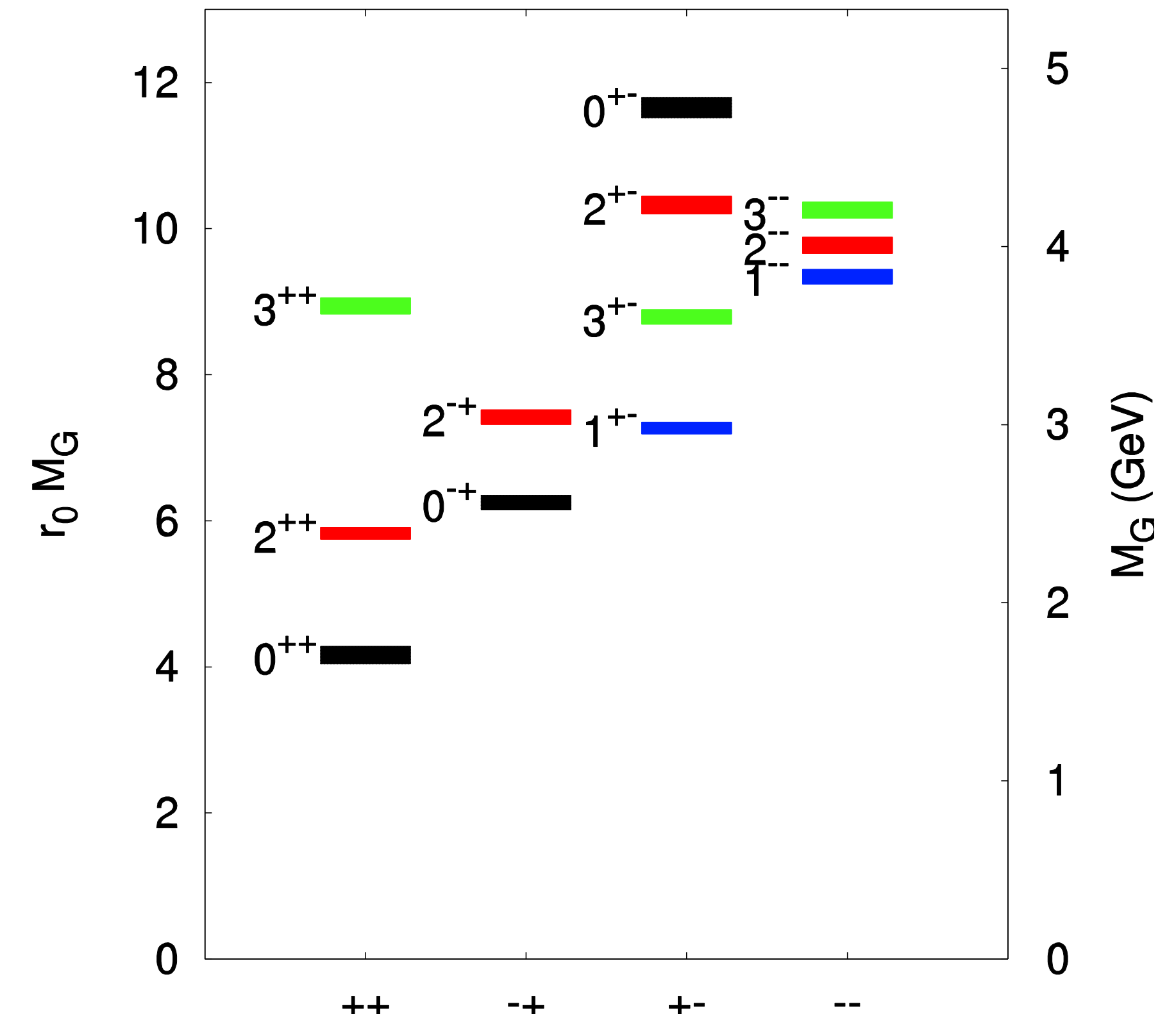
	M(MeV/c ²)	Γ (MeV/c ²)	Sig.
X(1835)	$1836.5 \pm 3.0^{+5.6}_{-2.1}$	$190.1 \pm 9.0^{+38}_{-36}$	$>20\sigma$
X(2120)	$2122.4 \pm 6.7^{+4.7}_{-2.7}$	$83 \pm 16^{+31}_{-11}$	7.2σ
X(2370)	$2376.3 \pm 8.7^{+3.2}_{-4.3}$	$83 \pm 17^{+44}_{-6}$	6.4σ

◆ Confirmed by BESIII in $J/\psi \rightarrow \gamma\pi^+\pi^-\eta'$ and $J/\psi \rightarrow \gamma K\bar{K}\eta'$ (new mode)

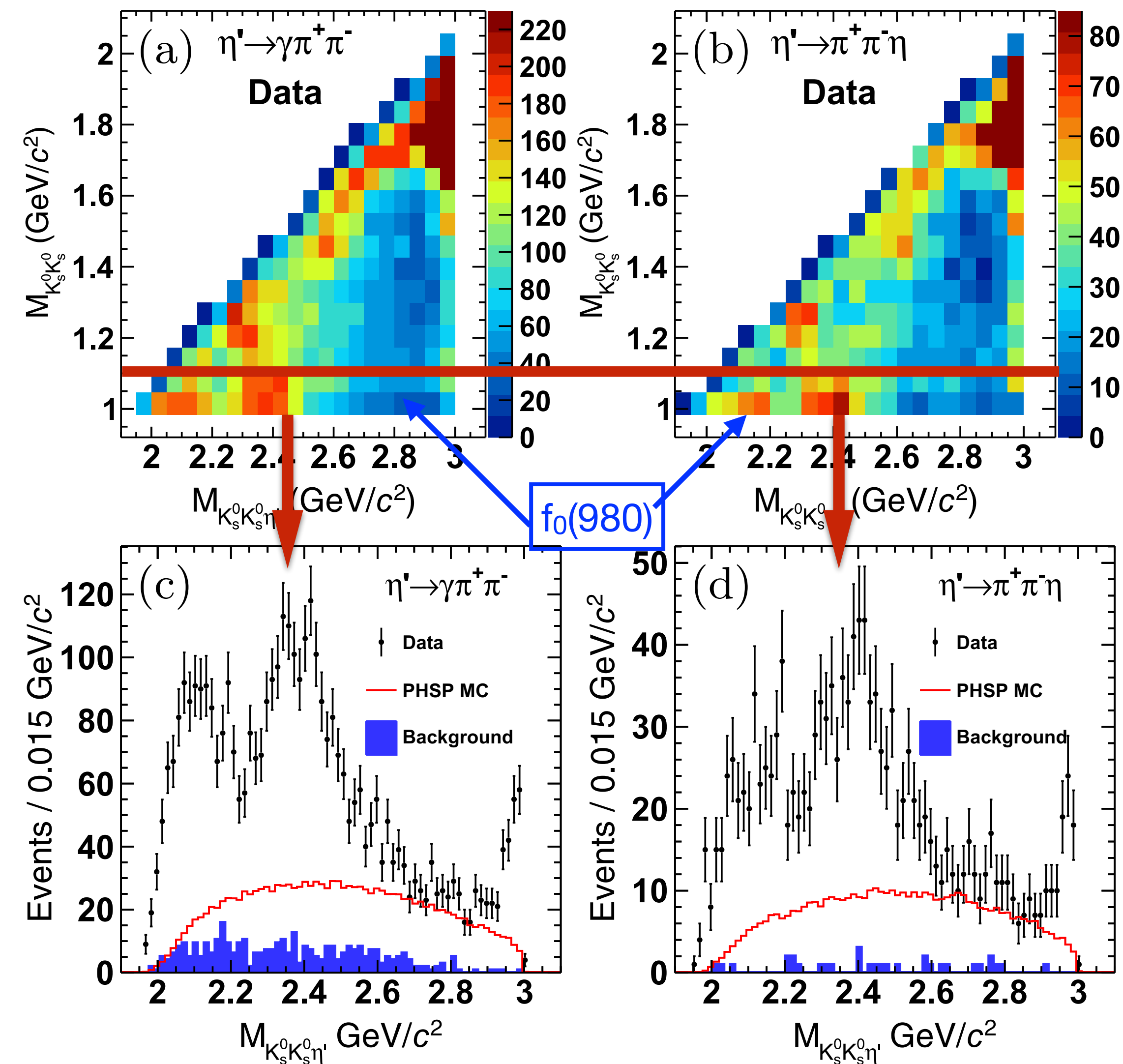


X(2370) - good candidate of 0^{-+} glueball

- ◆ Its mass is consistent with LQCD prediction on the 0^{-+} glueball
- ◆ Produced in the gluon-rich J/ψ radiative decays
- ◆ Observed in flavor symmetric decay modes of $\pi^+\pi^-\eta'$ and $K\bar{K}\eta'$ — favorite decay modes of 0^{-+} glueball
- ◆ Determination of its spin-parity is crucial

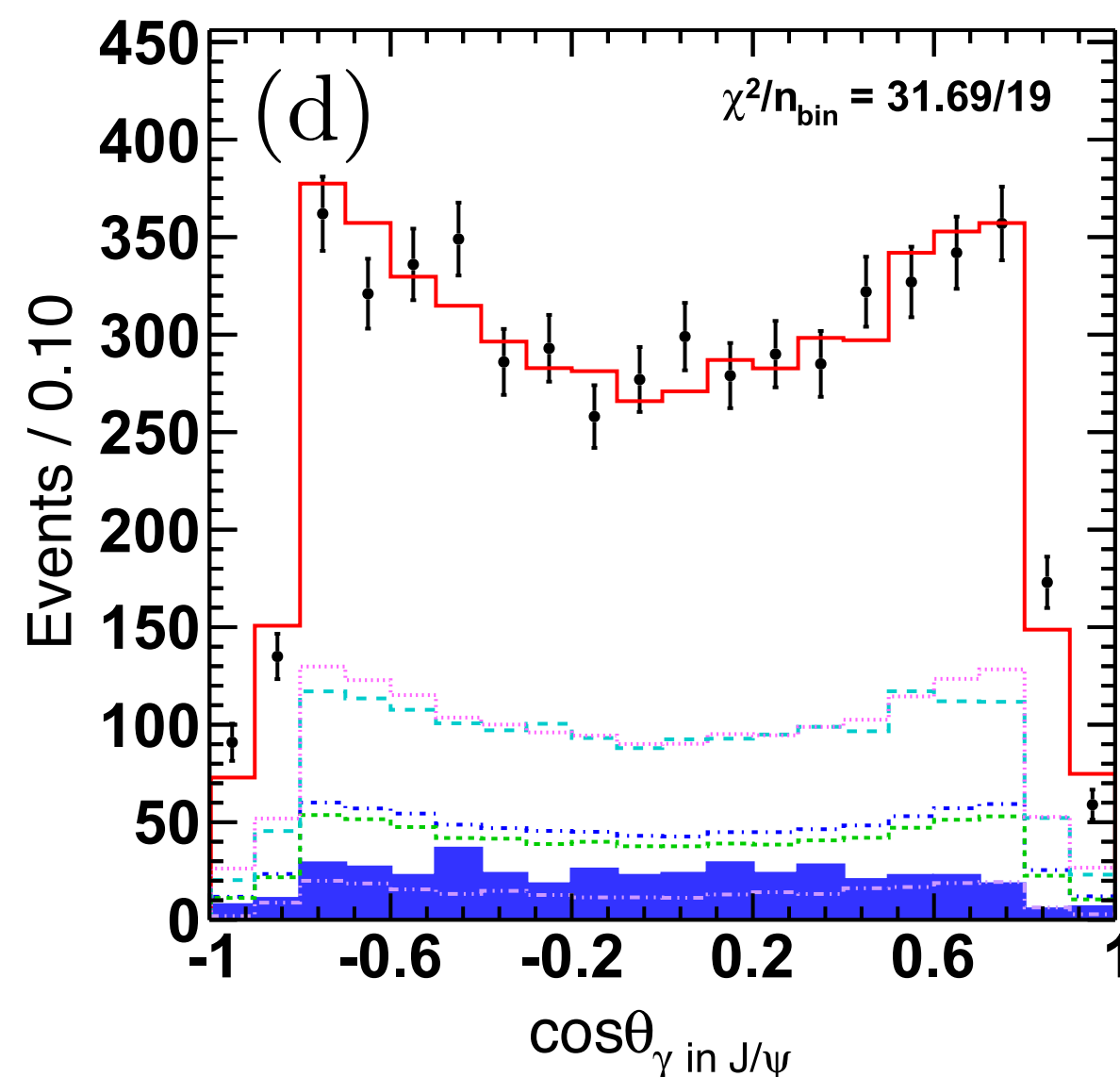
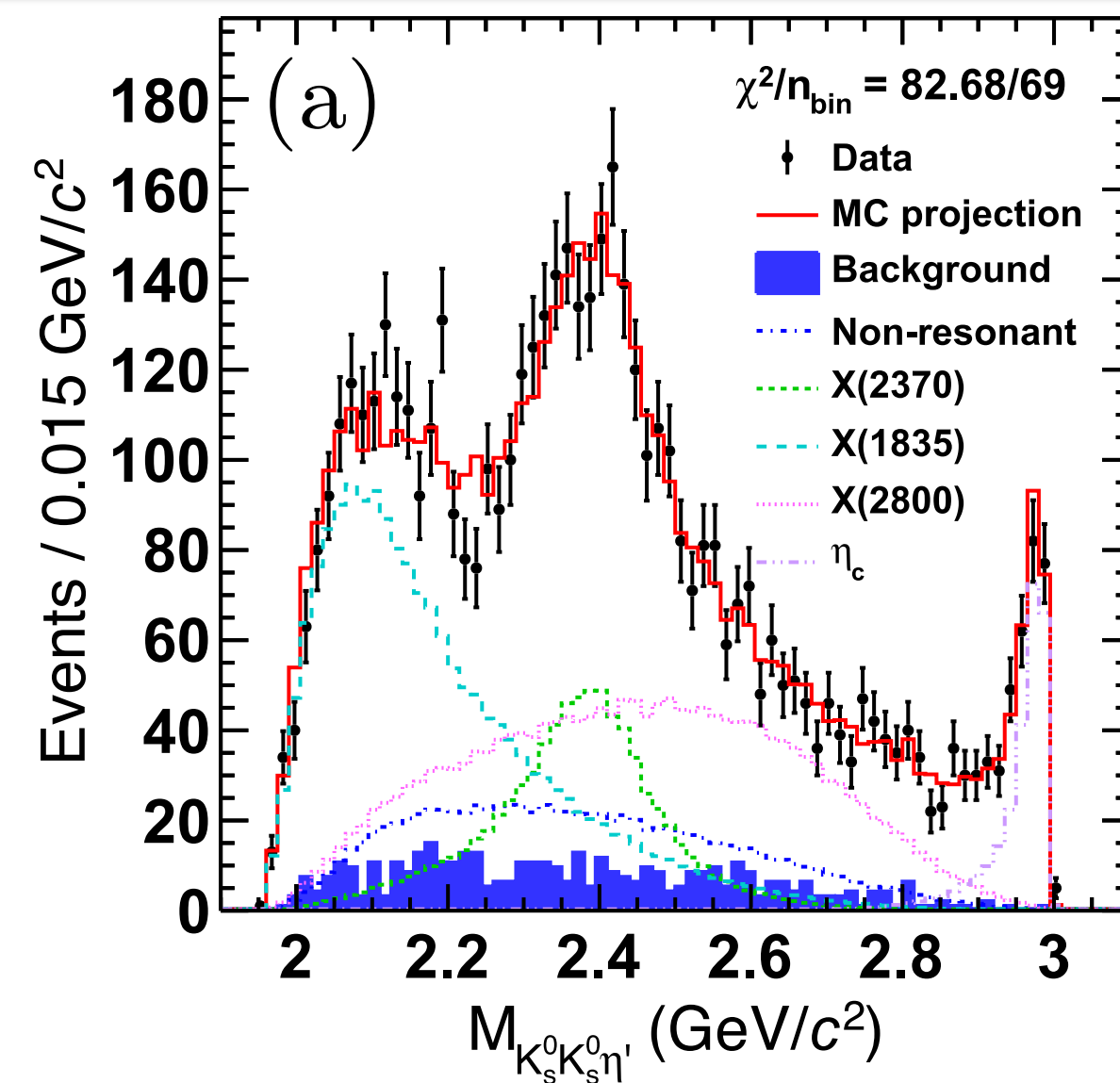


Spin-Parity determination of the $X(2370)$ in $J/\psi \rightarrow \gamma K_s^0 K_s^0 \eta'$



- ◆ Analysis advantage of $J/\psi \rightarrow \gamma K_s^0 K_s^0 \eta'$:
 - ◆ Almost background free channel (exchange symmetry and C-parity conservation)
 - ◆ 10 billion J/ψ data
 - ◆ Very good BESIII detector performance
- ◆ Similar structures in $\eta' \rightarrow \pi^+ \pi^- \eta$ / $\gamma \pi^+ \pi^-$ modes:
 - ◆ Evident $f_0(980)$ in $K_s^0 K_s^0$ mass threshold
 - ◆ Clear signal of $X(1835), X(2370), \eta_c$ with $f_0(980)$ selection
- ◆ Best PWA fit can well describe the data:
 - ◆ **Spin-parity of the $X(2370)$ is determined to be 0^- with significance larger than 9.8σ w.r.t. other J^{PC} assumptions**

Spin-Parity determination of the $X(2370)$ in $J/\psi \rightarrow \gamma K_s^0 K_s^0 \eta'$



PRL 132 (2024) 181901

- ◆ Analysis advantage of $J/\psi \rightarrow \gamma K_s^0 K_s^0 \eta'$:
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 - ◆ Evident $f_0(980)$ in $K_s^0 K_s^0$ mass threshold
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 - ◆ **Spin-parity of the $X(2370)$ is determined to be 0^{-+} with significance larger than 9.8σ w.r.t. other J^{PC} assumptions**

Compared with LQCD prediction on Lightest 0^{-+} Glueball

X(2370) measurements:

PRL 132 (2024) 181901

$J^{PC} = 0^{-+}$ with significance $>9.8\sigma$

$M = 2395 \pm 11^{+26}_{-94}$ MeV

$\Gamma = 188^{+18}_{-17}{}^{+124}_{-33}$ MeV

**$B(J/\psi \rightarrow \gamma X(2370))B(X(2370) \rightarrow f_0(980)\eta')B(f_0(980) \rightarrow K^0_s K^0_s)$
 $= (1.31 \pm 0.22^{+2.85}_{-0.84}) \times 10^{-5}$**

LQCD prediction on lightest pseudoscalar glueball:

$J^{PC} = 0^{-+}$

$M = 2395 \pm 14$ MeV

$B(J/\psi \rightarrow \gamma G_{0^{-+}}) = (2.31 \pm 0.80) \times 10^{-4}$

PRD 100 (2019) 054511

- ◆ The measurements are in a good agreement with the predictions on **lightest pseudoscalar glueball**
- ◆ **The spin-parity of the X(2370) is determined to be 0^{-+} for the first time**
- ◆ **Mass is in a good agreement with LQCD predictions**
- ◆ The estimation on $B(J/\psi \rightarrow \gamma X(2370))$ and prediction on $B(J/\psi \rightarrow \gamma G_{0^{-+}})$ are consistent within errors (assuming $\sim 5\%$ decay rate, $B(J/\psi \rightarrow \gamma X(2370)) = (10.7^{+22.8}_{-7}) \times 10^{-4}$)

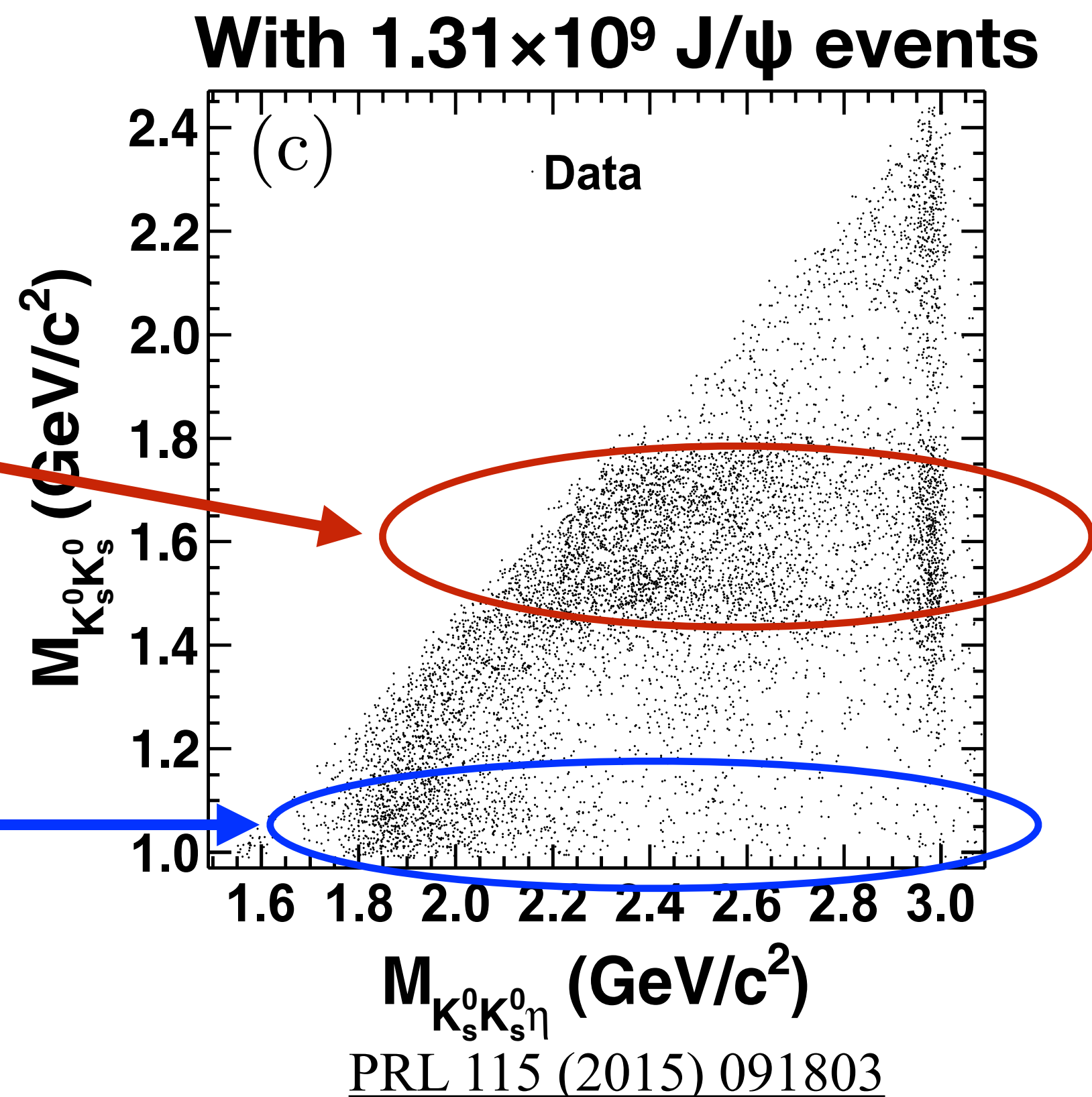
$X(2370)$ in $J/\psi \rightarrow \gamma K_s^0 K_s^0 \eta$

Observation and Spin-Parity Determination of the $X(1835)$ in $J/\psi \rightarrow \gamma K_s^0 K_s^0 \eta$

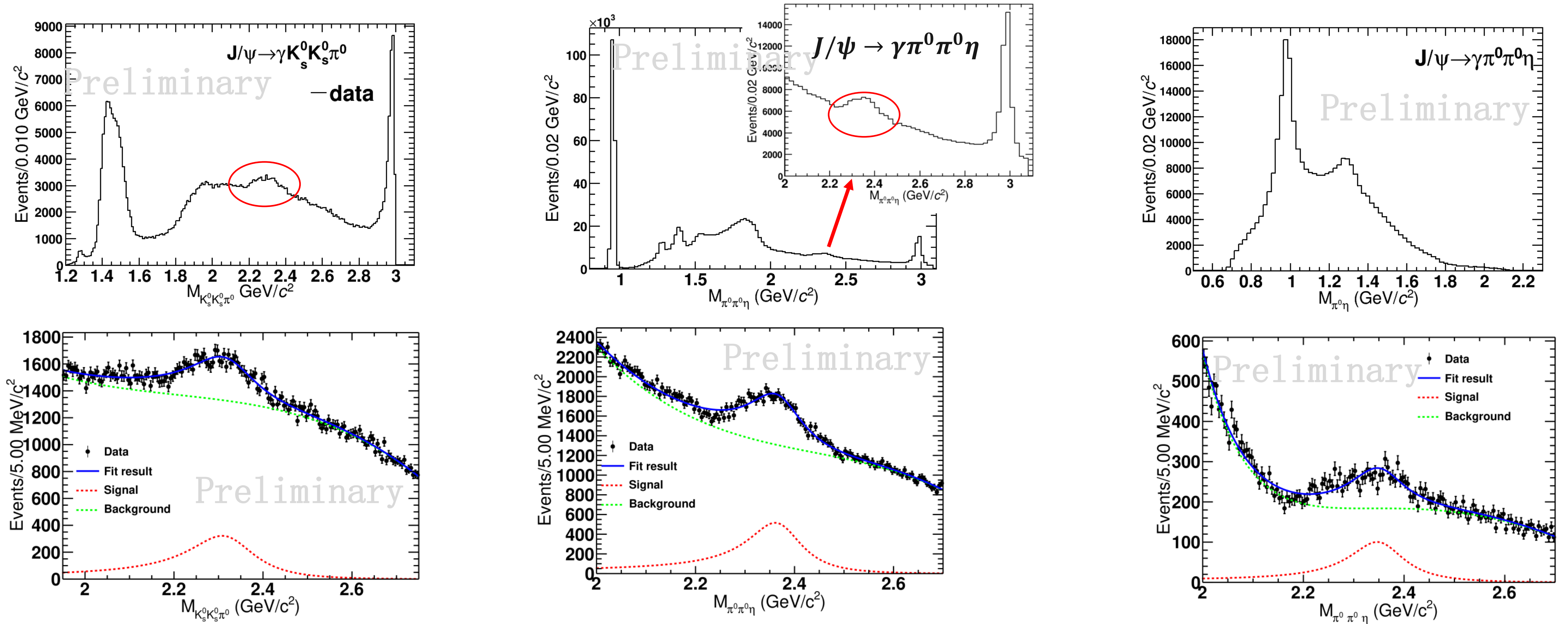
Qualitatively, we can clearly observe: similar decay patterns of the $X(2370)$ and η_c if phase space allows

In the upper KK mass band of 1.5-1.7 GeV range, clear signals of both $X(2370)$ and η_c

In the lower KK mass band of $f_0(980)$, no $X(2370)$, nor η_c



Observation of new decay modes of the X(2370)

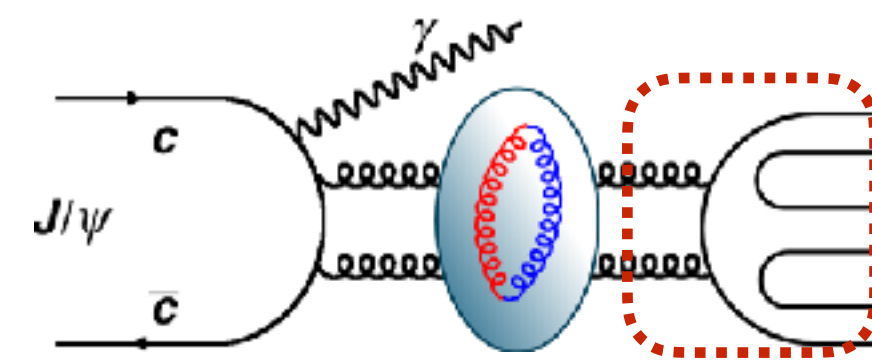
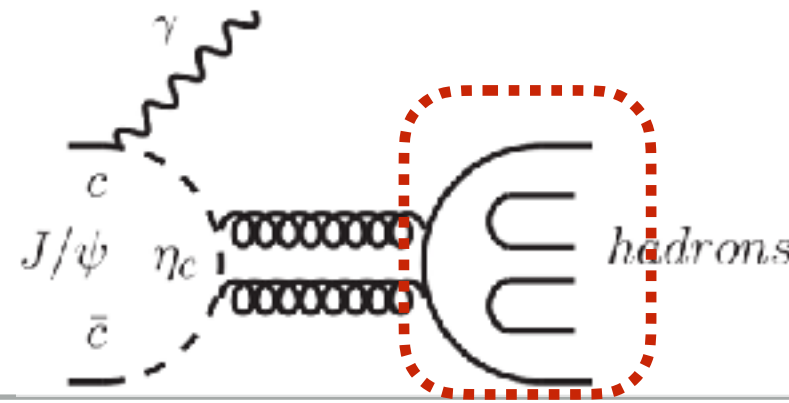


First observation of $X(2370) \rightarrow K_s^0 K_s^0 \pi^0$, $X(2370) \rightarrow \pi^0 \pi^0 \eta$ and $X(2370) \rightarrow a(980) \pi^0$ with **significances $\gg 5\sigma$** and accompanied with η_c

Observation of the X(2370) in the 5 golden decay modes

◆ The glueball decays could be the analogy to Charmonium decays since they all decay via gluons (OZI suppression) [PLB 380 189(1996), Commu. Theor. Phys. 23.373 (1995)]

◆ e.g. the 0^{-+} glueball could have similar decays of η_c



5 major η_c decay modes (from PDG)
— 5 “Golden” modes in 0^{-+} glueball traditional searches

Decays involving hadronic resonances

Γ_1	$\eta'(958) \pi \pi$	$(1.87 \pm 0.26) \%$
Γ_2	$\eta'(958) K \bar{K}$	$(1.61 \pm 0.25) \%$

Decays into stable hadrons

Γ_{34}	$K \bar{K} \pi$	$(7.0 \pm 0.4) \%$
Γ_{35}	$K \bar{K} \eta$	$(1.32 \pm 0.15) \%$
Γ_{36}	$\eta \pi^+ \pi^-$	$(1.7 \pm 0.5) \%$

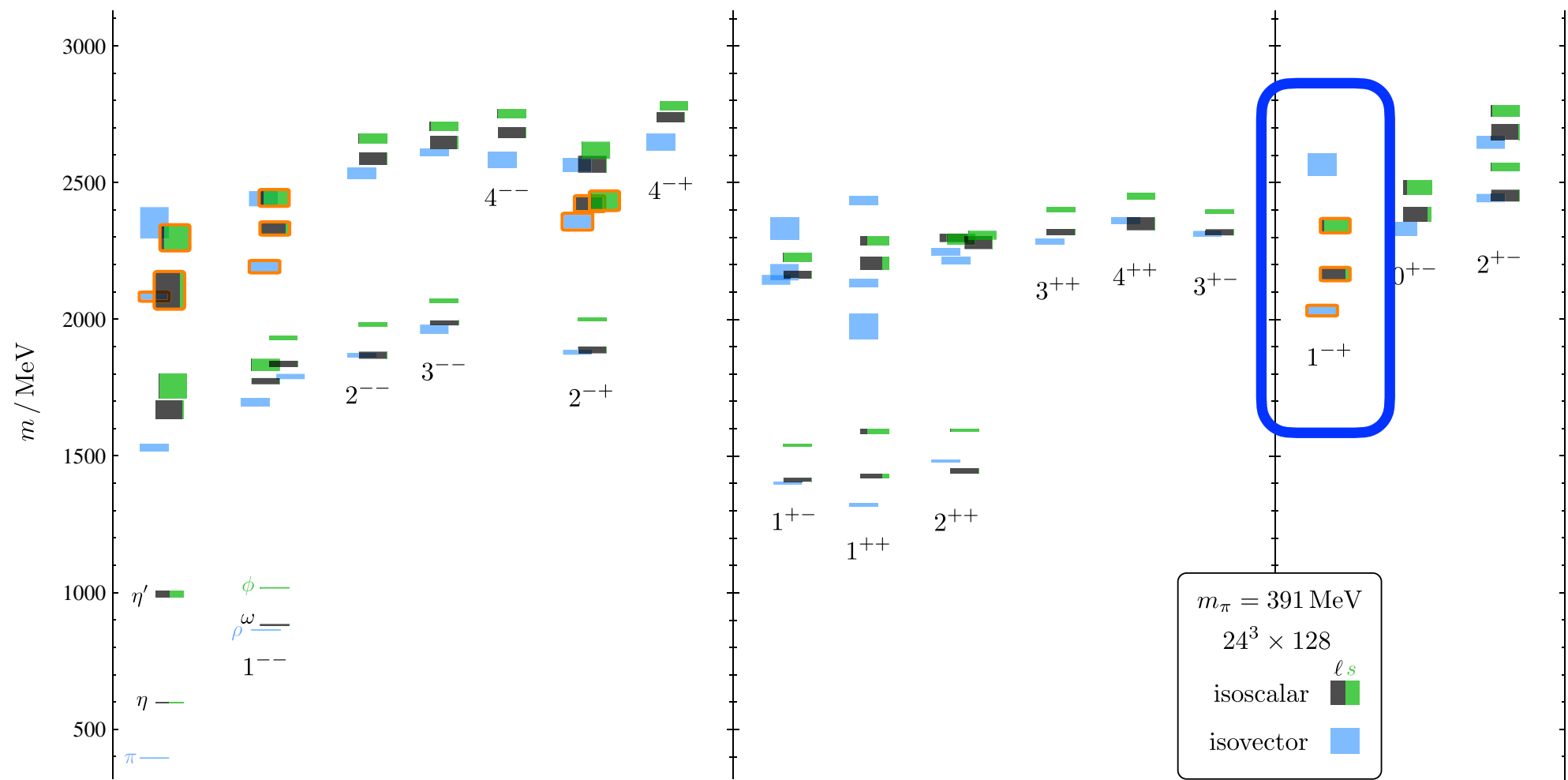
◆ The 0^{-+} glueball decays could be the analogy to η_c decays

- Decay modes of $X(2370) \rightarrow \pi \pi \eta', K \bar{K} \eta', K \bar{K} \pi, \pi \pi \eta, K \bar{K} \eta, a(980) \pi$ observed, consistent with 0^{-+} glueball

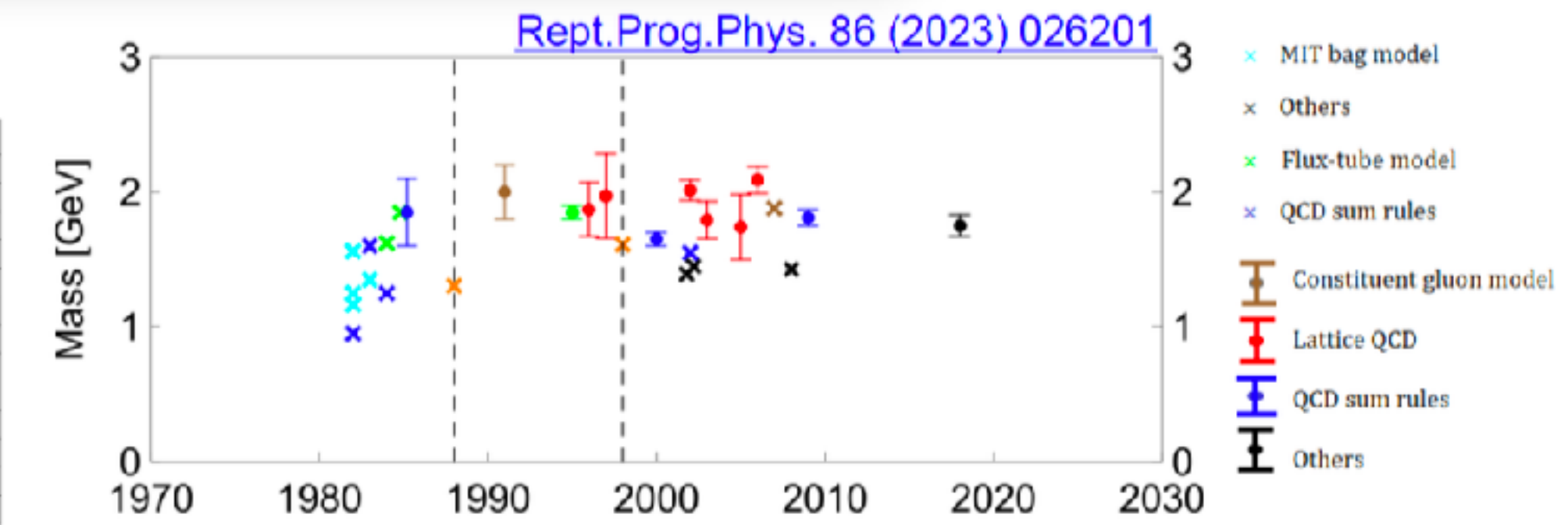
Such high similarity between the X(2370) and η_c decay modes strongly supports the glueball interpretation of the X(2370)

Exotic 1⁻⁺ state

J^{PC}	$q\bar{q}$
0^{++}	yes
0^{+-}	-
0^{-+}	yes
0^{--}	-
1^{++}	yes
1^{+-}	yes
1^{-+}	-
1	yes
2^{++}	yes
2^{+-}	-
2^{-+}	yes
2^{--}	yes
3^{++}	yes
3^{+-}	yes
3^{-+}	-
3^{--}	yes

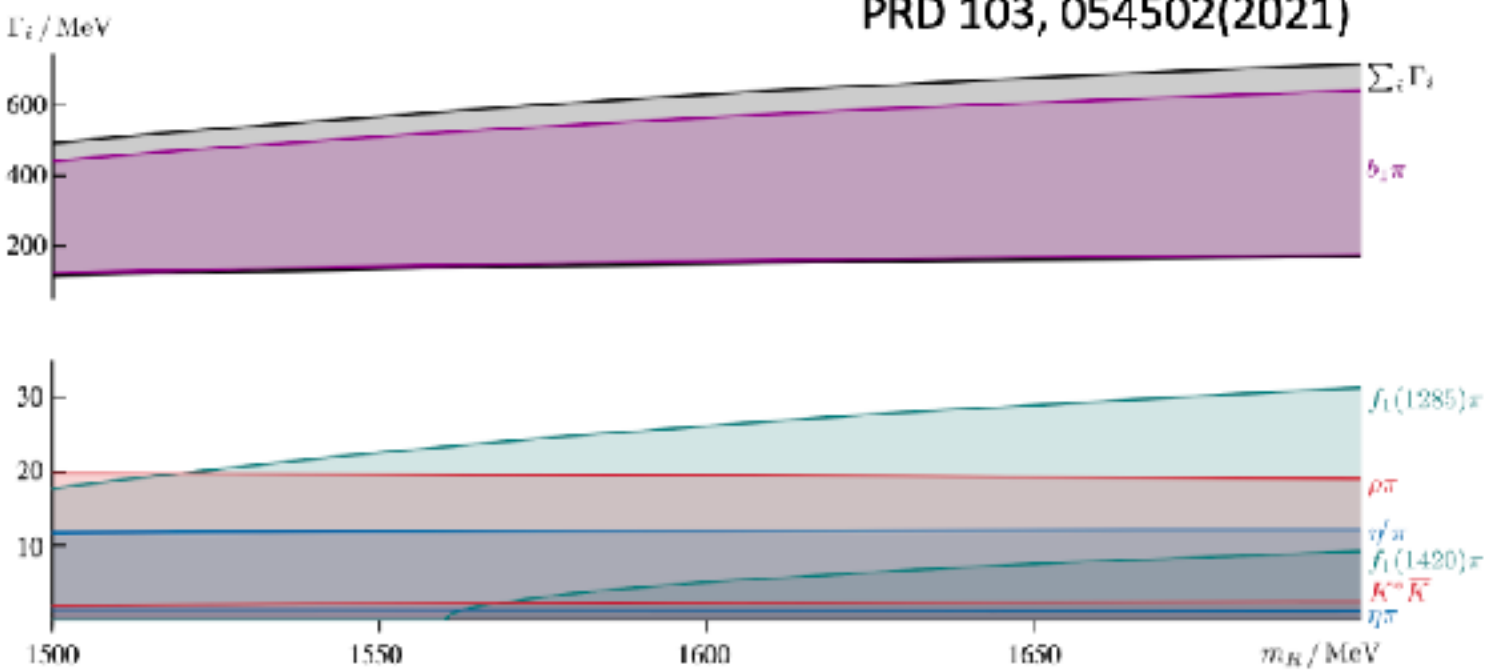


[PRD 88 094505\(2013\)](#)

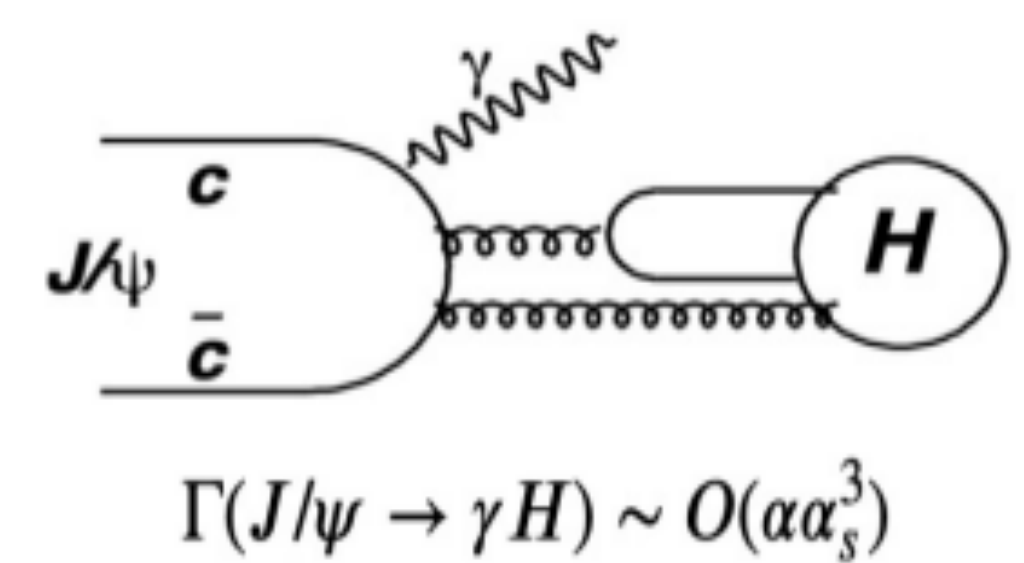


Mass of 1⁻⁺ hybrid

PRD 103, 054502(2021)



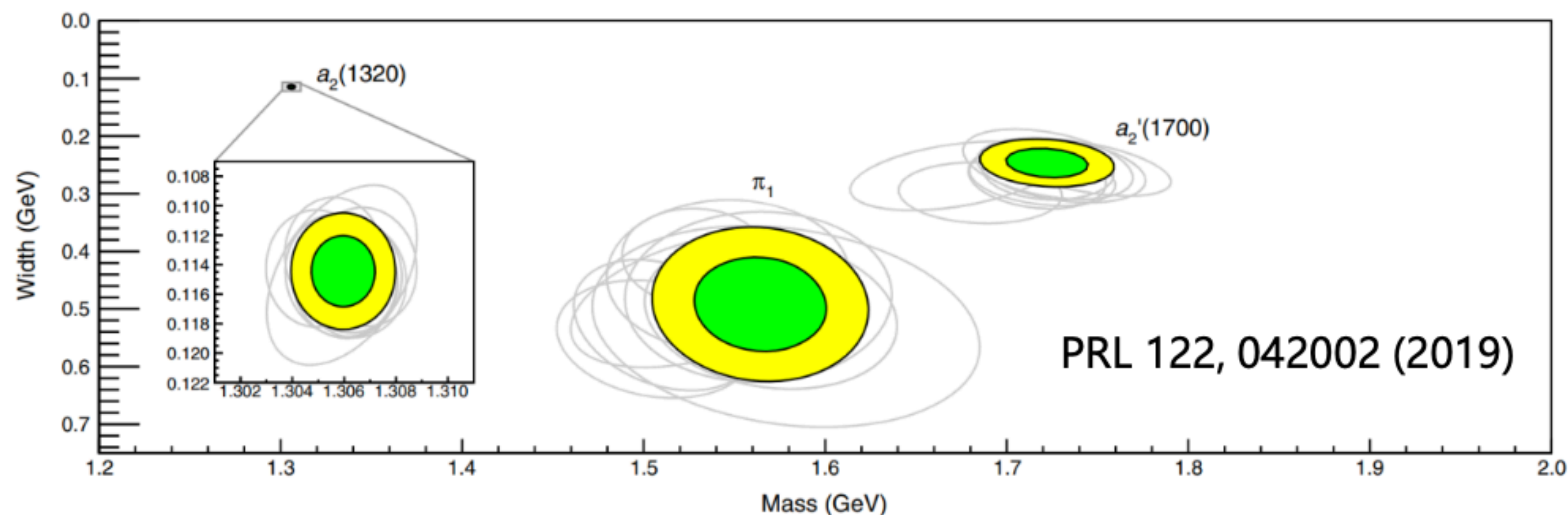
Width of 1⁻⁺ hybrid



- ◆ **Spin-exotic state of 1⁻⁺** : forbidden in conventional quark model
- ◆ Exotic state **1⁻⁺** provide an unique way for hybrid search:
- ◆ LQCD predicts the **lightest nonet of 1⁻⁺ hybrids**: 1.7 - 2.1GeV
- ◆ **Can be produced in the gluon-rich charmonium decays**

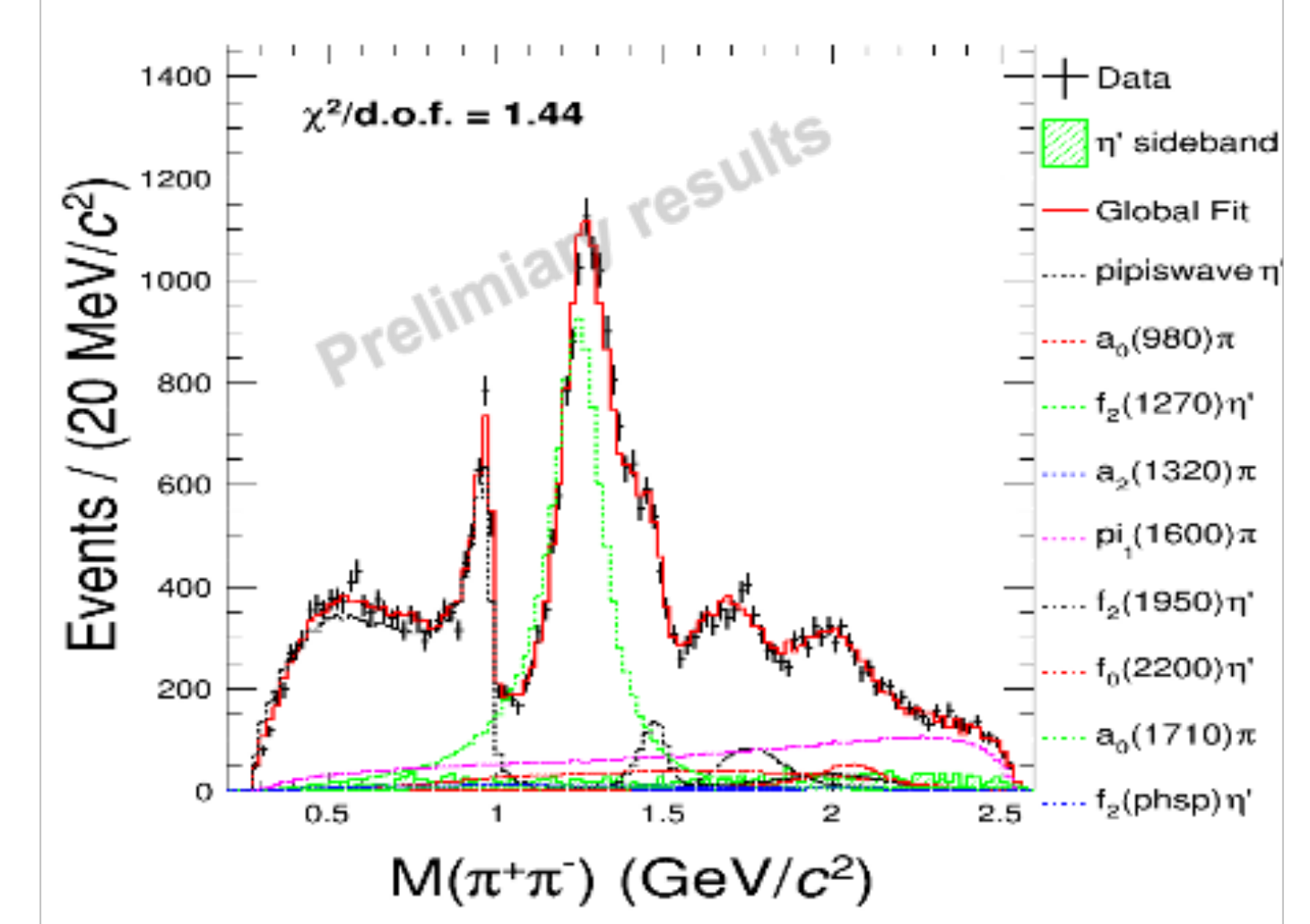
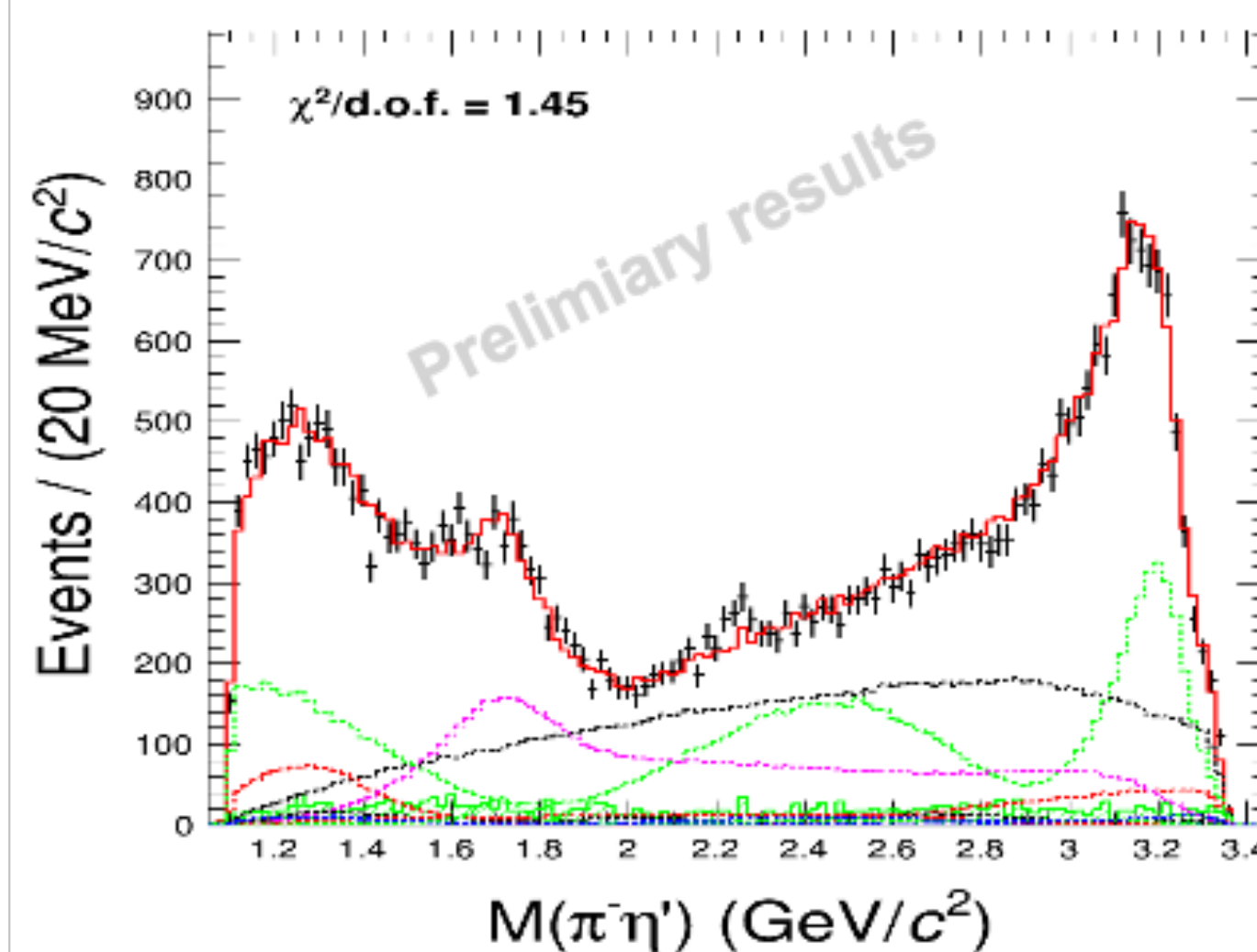
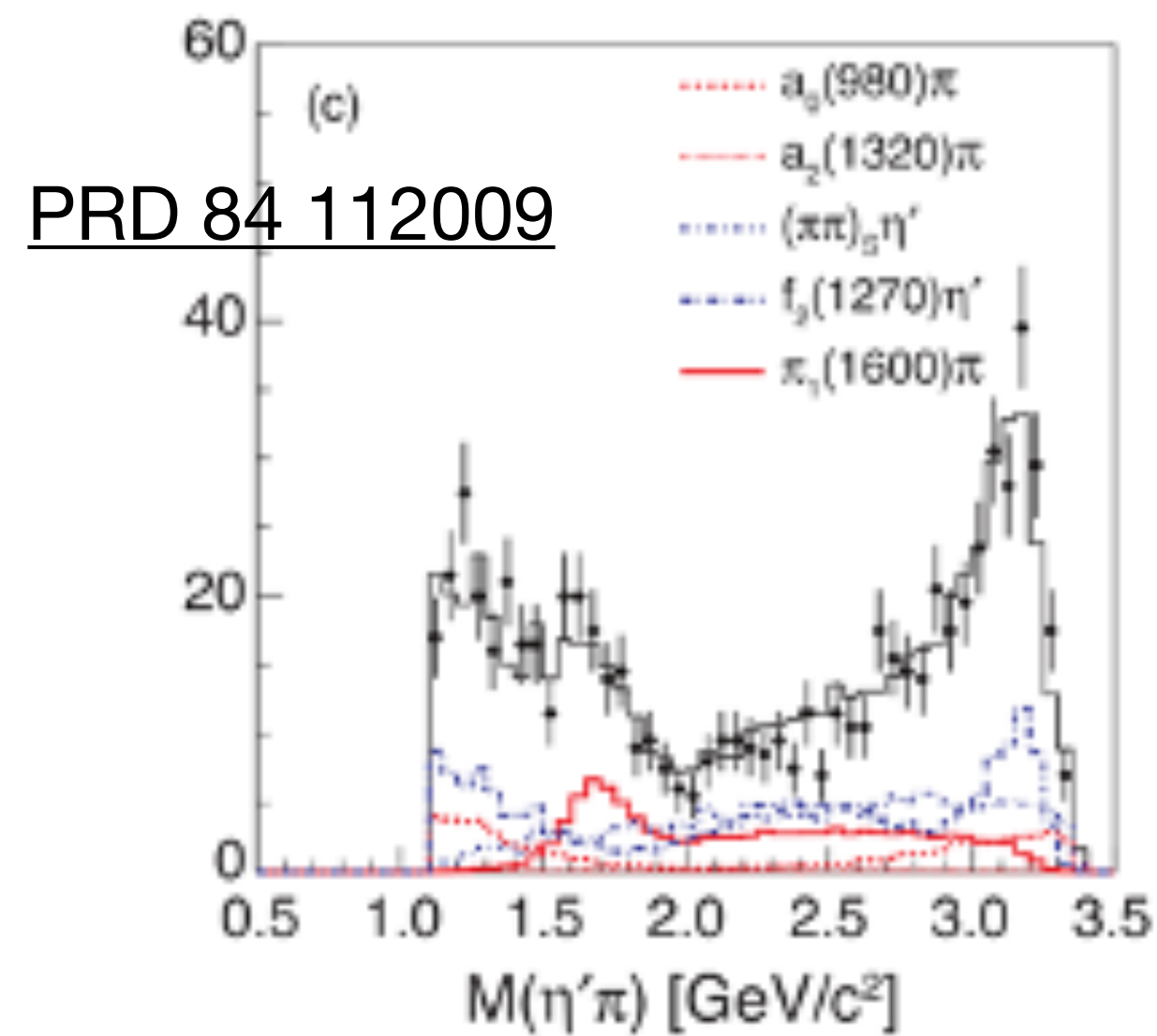
Spin-exotic mesons

- ◆ Over 3 decades, experimental evidence for 3 candidates with 1^{-+} state:
 - ◆ All 1^{-+} iso-vectors
 - ◆ $\pi_1(1400)$: seen in $\eta\pi$
 - ◆ $\pi_1(1600)$: seen in $\rho\pi, \eta'\pi, b_1\pi, f_1\pi$
 - ◆ $\pi_1(2015)$: seen in $b_1\pi$ and $f_1\pi$
- ◆ Some claims are controversial
- ◆ $\pi_1(1400)$ and $\pi_1(1600)$ can be one pole



	Decay mode	Reaction	Experiment
$\pi_1(1400)$	$\eta\pi$	$\pi^-p \rightarrow \pi^- \eta p$ $\pi^-p \rightarrow \pi^0 \eta n$ $\pi^-p \rightarrow \pi^- \eta p$ $\pi^-p \rightarrow \pi^0 \eta n$ $\bar{p}n \rightarrow \pi^- \pi^0 \eta$ $\bar{p}p \rightarrow \pi^0 \pi^0 \eta$	GAMS KEK E852 E852 CBAR CBAR
	$\rho\pi$	$\bar{p}p \rightarrow 2\pi^+ 2\pi^-$	Obelix
$\pi_1(1600)$	$\eta'\pi$	$\pi^-Be \rightarrow \eta' \pi^- \pi^0 Be$ $\pi^-p \rightarrow \pi^- \eta' p$	VES E852
	$b_1\pi$	$\pi^-Be \rightarrow \omega \pi^- \pi^0 Be$ $\bar{p}p \rightarrow \omega \pi^+ \pi^- \pi^0$ $\pi^-p \rightarrow \omega \pi^- \pi^0 p$	VES CBAR E852
	$\rho\pi$	$\pi^- Pb \rightarrow \pi^+ \pi^- \pi^- X$ $\pi^-p \rightarrow \pi^+ \pi^- \pi^- p$	COMPASS E852
	$f_1\pi$	$\pi^-p \rightarrow p \eta \pi^+ \pi^- \pi^-$ $\pi^-A \rightarrow \eta \pi^+ \pi^- \pi^- A$	E852 VES
$\pi_1(2015)$	$f_1\pi$	$\pi^-p \rightarrow \omega \pi^- \pi^0 p$	E852
	$b_1\pi$	$\pi^-p \rightarrow p \eta \pi^+ \pi^- \pi^-$	

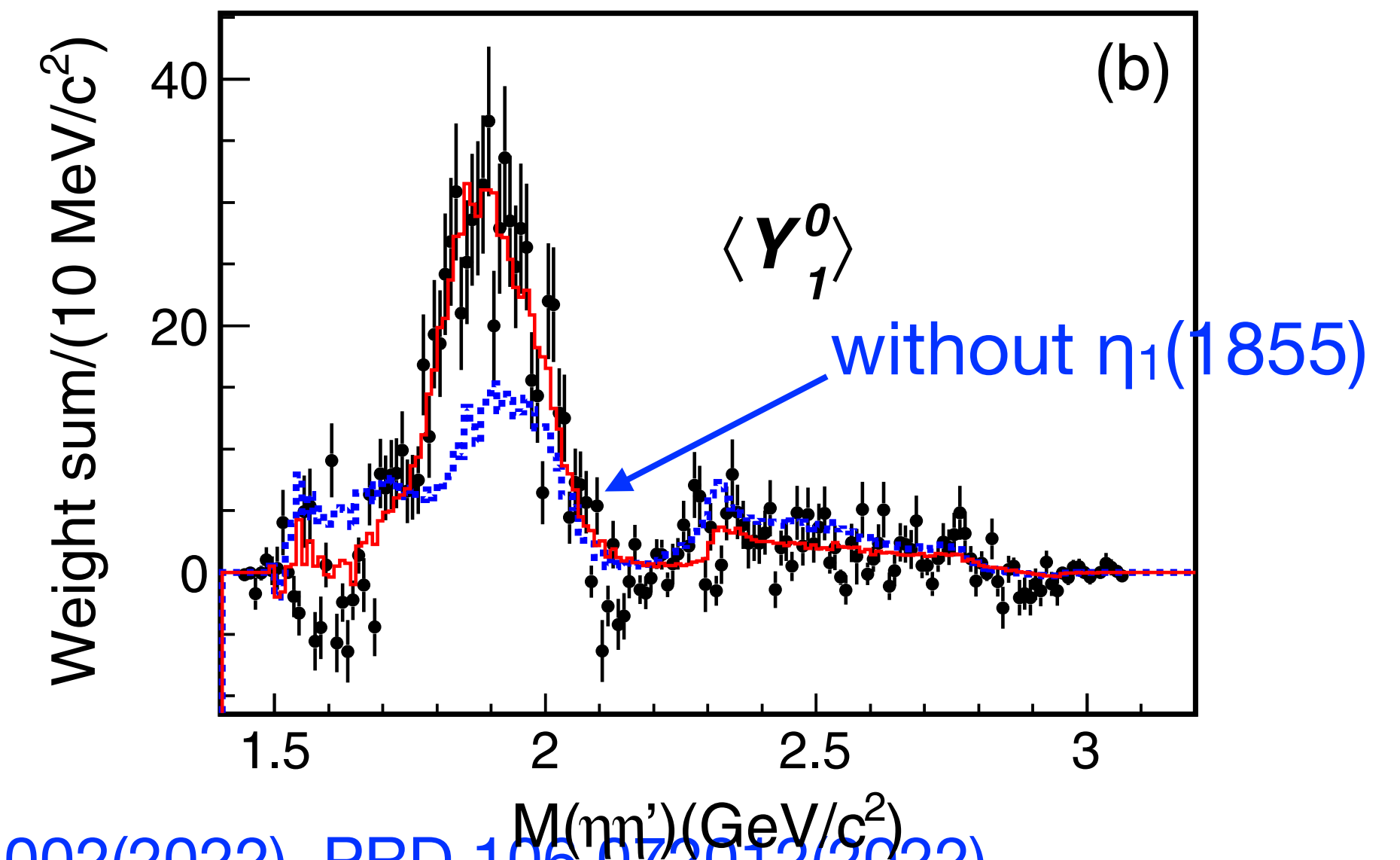
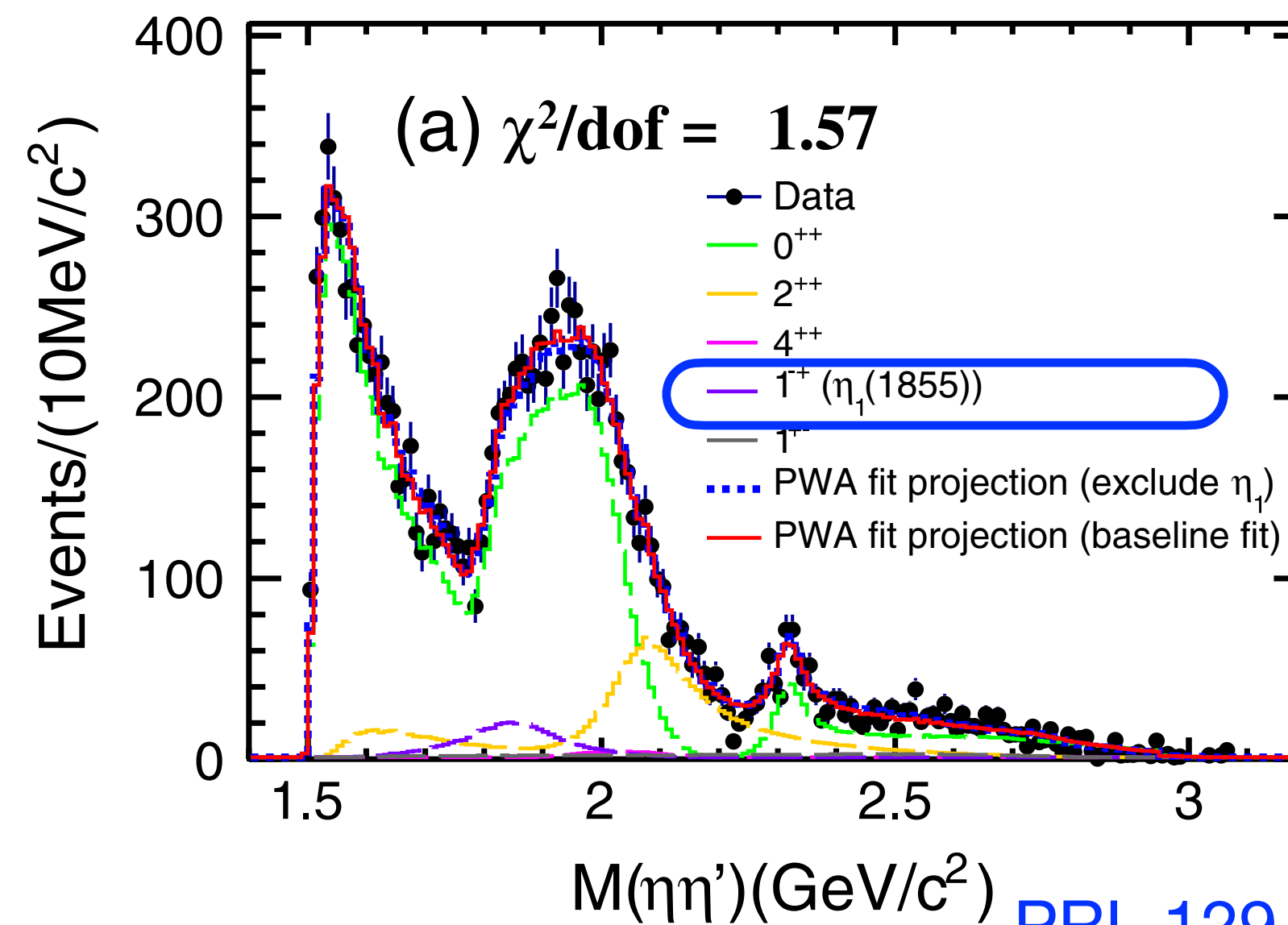
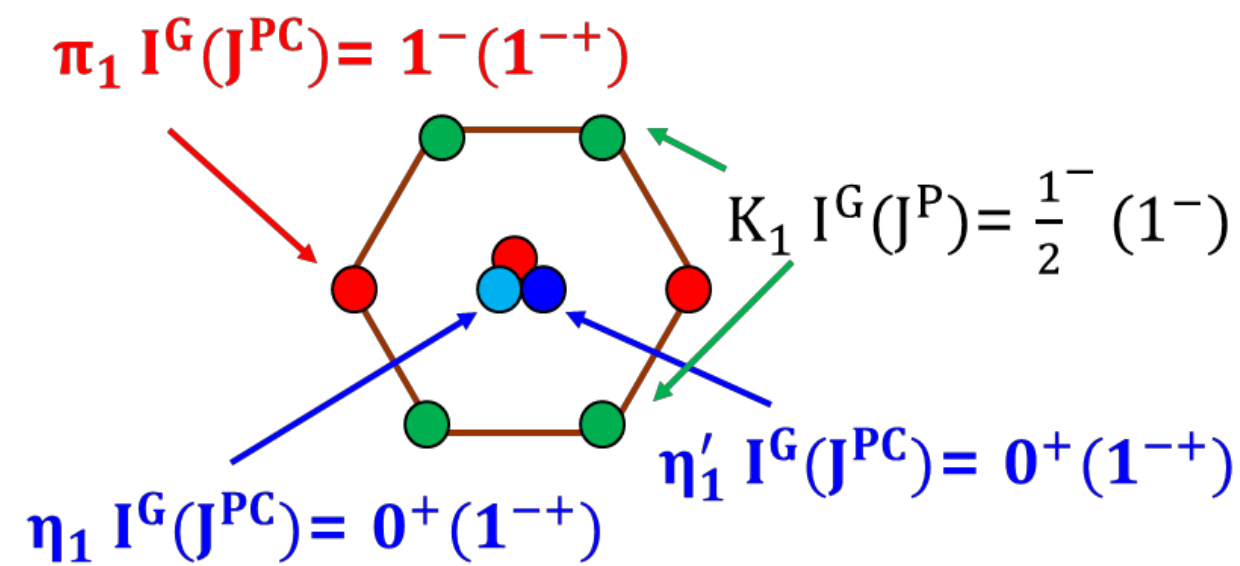
Observation of Exotic 1^{-+} Isovector state $\pi(1600)$



- ◆ CLEO-c results: evidence of an exotic P-wave $\eta'\pi$ amplitude with 4σ and but no significant phase motion
- ◆ PWA in $\psi' \rightarrow \gamma\chi_{c1}(\chi_{c1} \rightarrow \pi^+\pi^-\eta')$ with higher ψ' data sample @ BESIII:
 - ✦ **First observation of Exotic 1^{-+} Isovector state $\pi(1600)$ with a significance $>10\sigma$ better than other J^{PC} assumption**
 - ✦ The significance of phase motion is also greater than 10σ

Observation of An Exotic 1^{-+} Isoscalar $\eta_1(1855)$

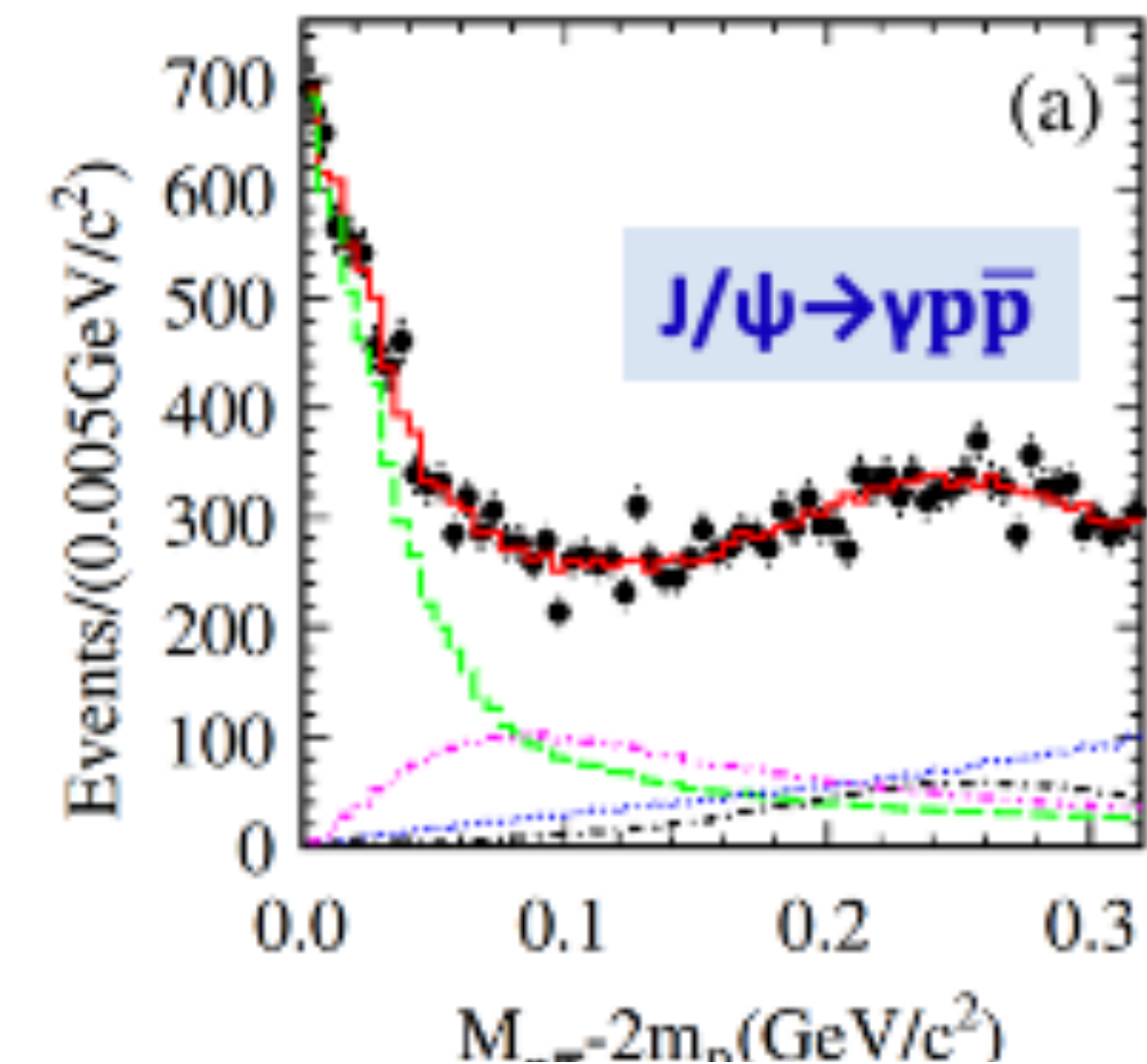
Isoscalar (1^{-+}) is critical to establish the nonet hybrid multiplet: partners for the Isovector (1^{-+})



[PRL 129 192002\(2022\), PRD 106 072012\(2022\)](#)

- ◆ $J/\psi \rightarrow \gamma\eta\eta'$ is a good channel for $\eta_1(1^{-+})$ search
- ◆ **Observation of an isoscalar 1^{-+} $\eta_1(1855)$ in $J/\psi \rightarrow \gamma\eta\eta'$ ($>19\sigma$)**
 - ◆ PWA: quasi two-body decay amplitudes in the sequential decay processes with covariant tensor formalism
 - ◆ $M = 1855 \pm 9^{+6}_{-1} \text{ MeV}$, $\Gamma = 188 \pm 18^{+3}_{-8} \text{ MeV}$, $B(J/\psi \rightarrow \gamma\eta_1(1855) \rightarrow \gamma\eta\eta') = (2.70 \pm 0.41^{+0.16}_{-0.35}) \times 10^{-6}$
- ◆ Mass consistent with hybrid on LQCD, and more interpretations (KK Molecule/Tetraquark)

Observation of $X(p\bar{p})$ and $X(1835)$

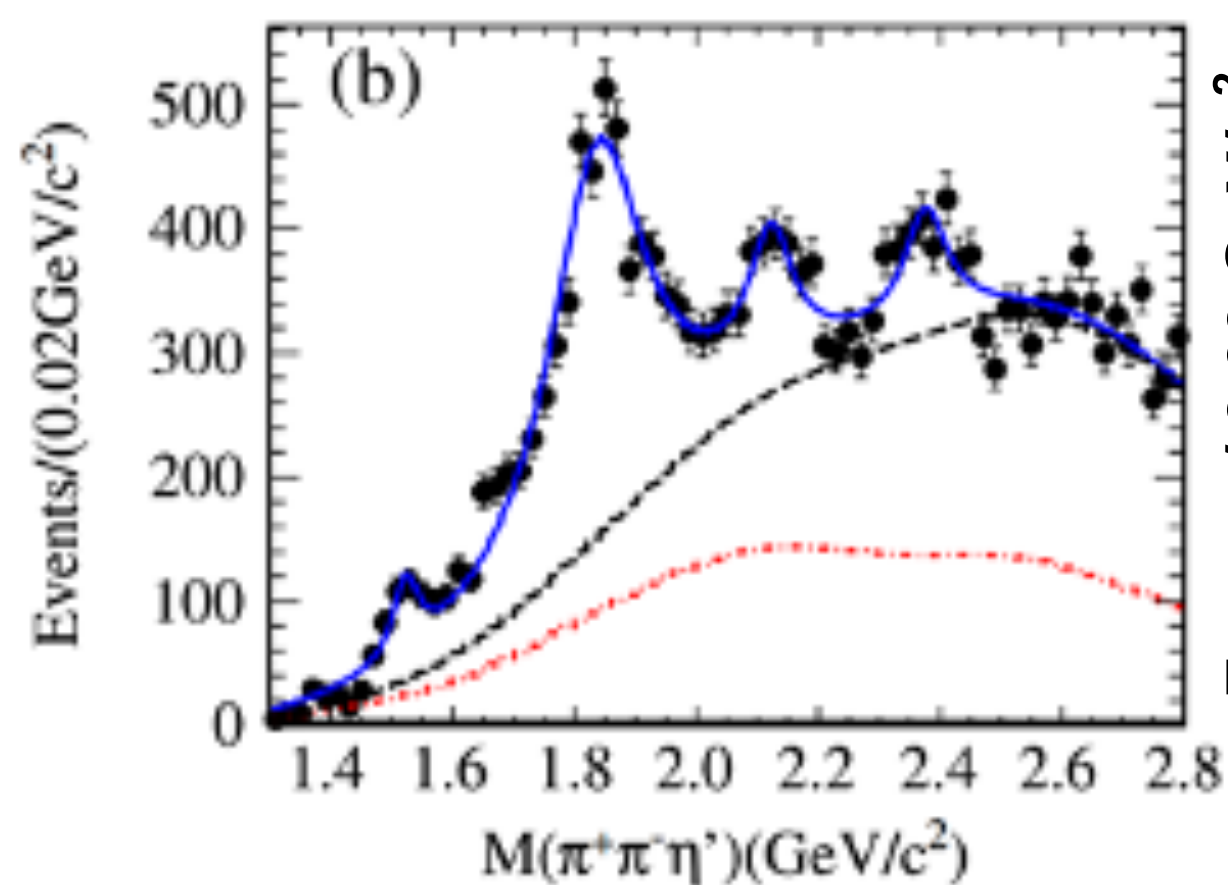


[PRL 108 \(2012\)112003](#)

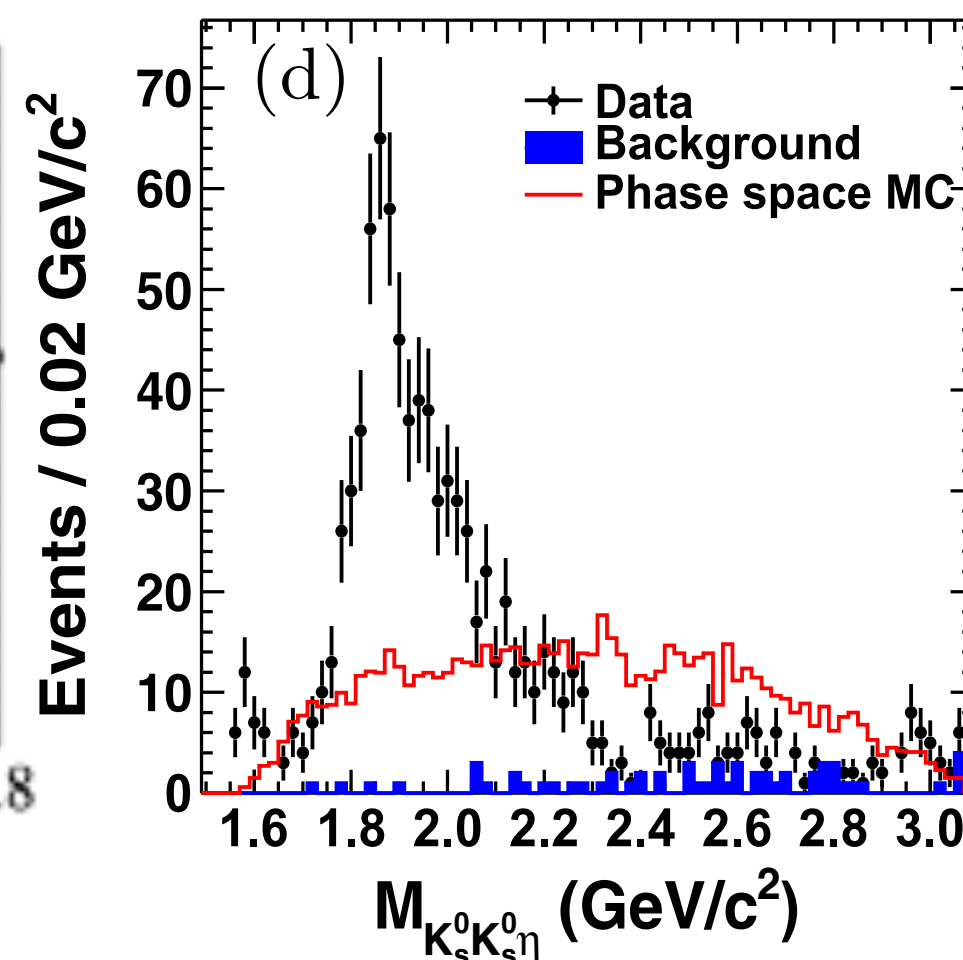
◆ $p\bar{p}$ mass threshold enhancement $X(p\bar{p})$:

- ◆ Discovered in $J/\psi \rightarrow \gamma p\bar{p}$ by BESII in 2003 and confirmed by BESIII and CLEO-c
- ◆ Further determination of Spin-parity to be 0^{-+}
- ◆ No similar threshold structure in other channels → It can not be pure FSI effect

$$M = 1832^{+19}_{-5} +^{+18}_{-17} \pm 19 \text{ MeV}/c^2, \quad \Gamma = 13 \pm 19 \text{ MeV}/c^2 (< 76 \text{ MeV}/c^2 @ 90\% \text{ C.L.})$$



[PRL 106 \(2011\)072002](#)



[PRL 115 091803](#)

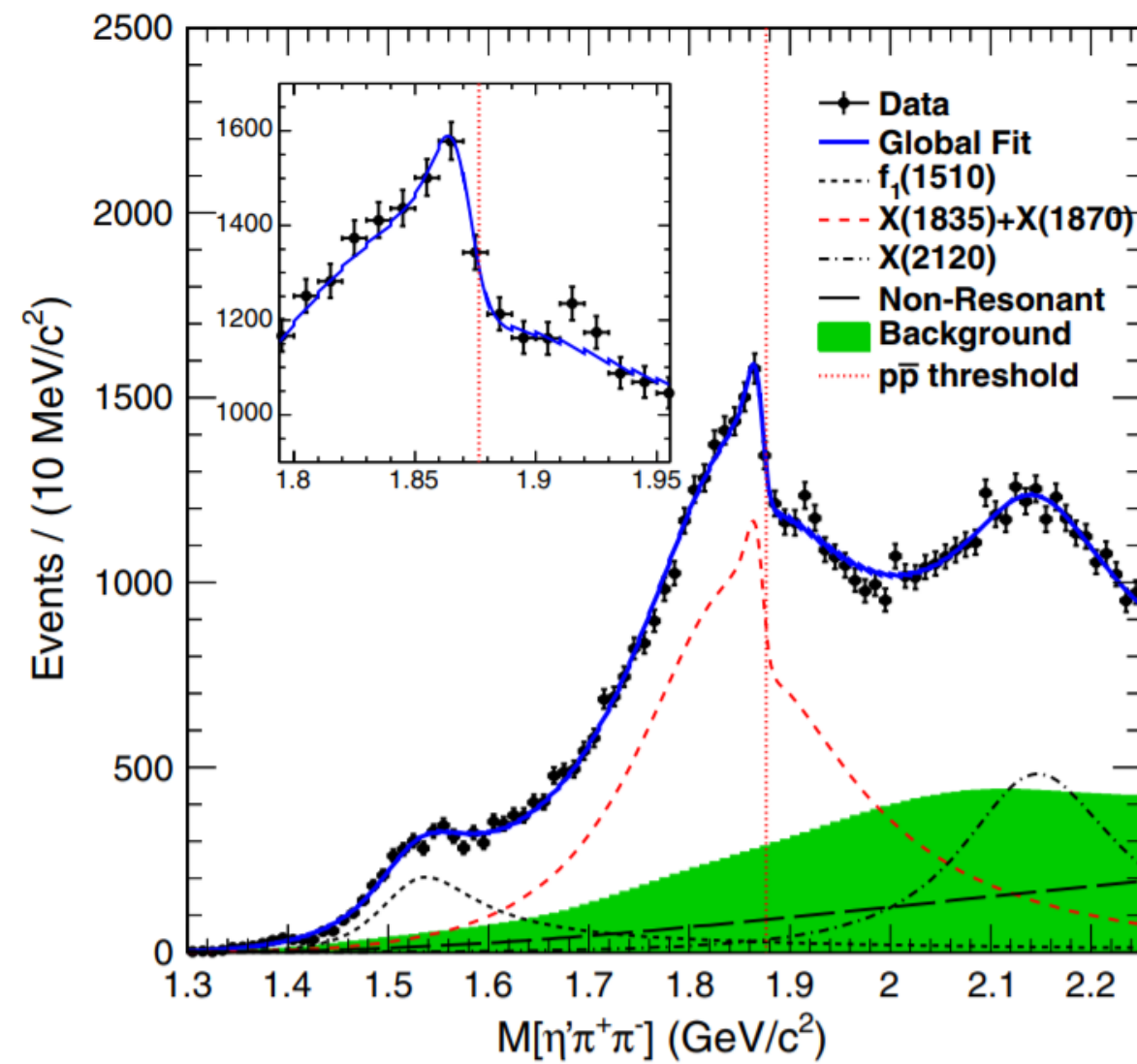
◆ $X(1835)$:

- ◆ Discovered by BESII and confirmed by BESIII in $J/\psi \rightarrow \gamma \pi \pi \eta'$
- ◆ Determination of Spin-parity to be 0^{-+} in $J/\psi \rightarrow \gamma K_s K_s \eta$

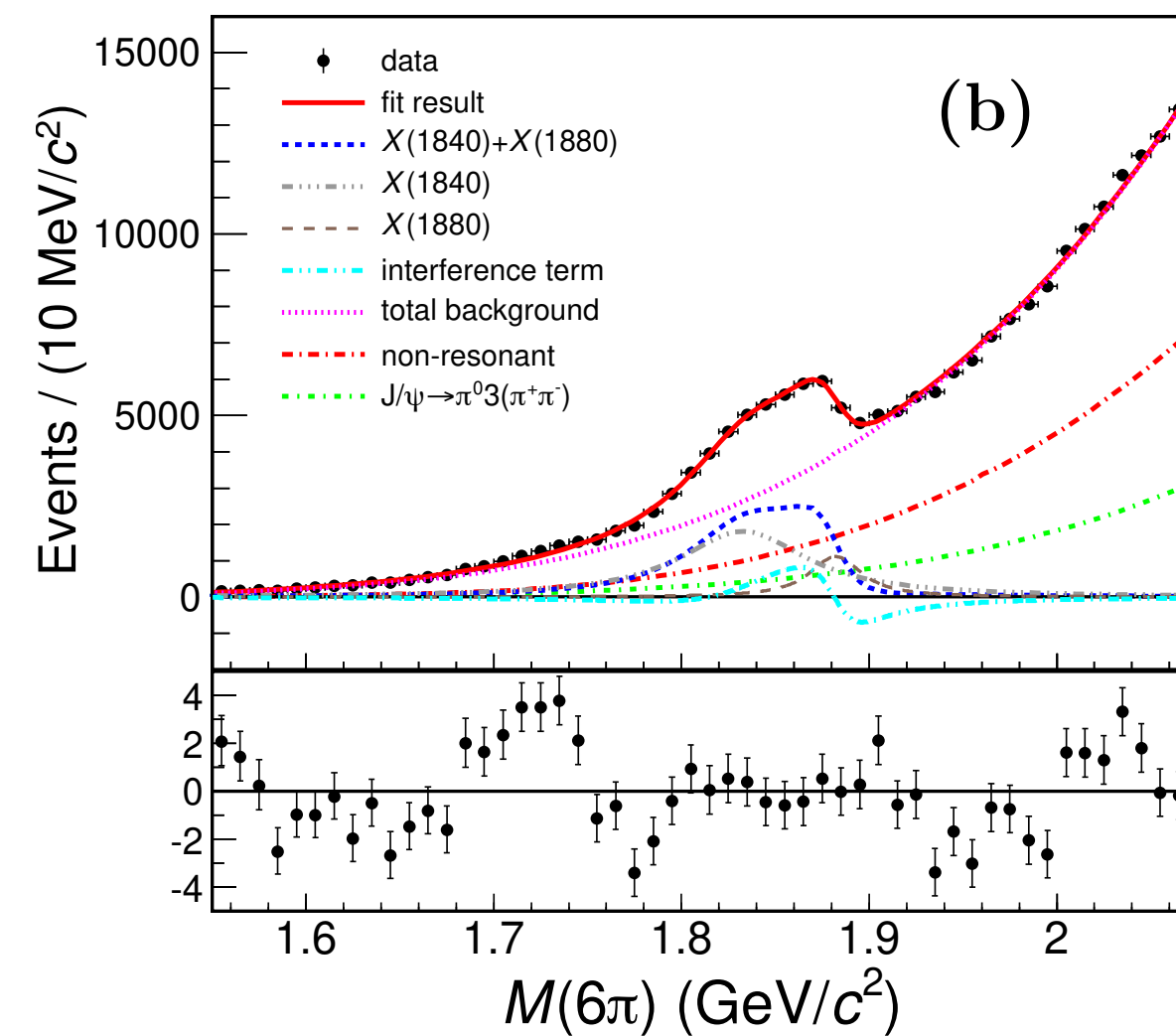
$$M = 1844 \pm 9^{+16}_{-25} \text{ MeV}/c^2$$

$$\Gamma = 192^{+20}_{-17} +^{+62}_{-43} \text{ MeV}/c^2$$

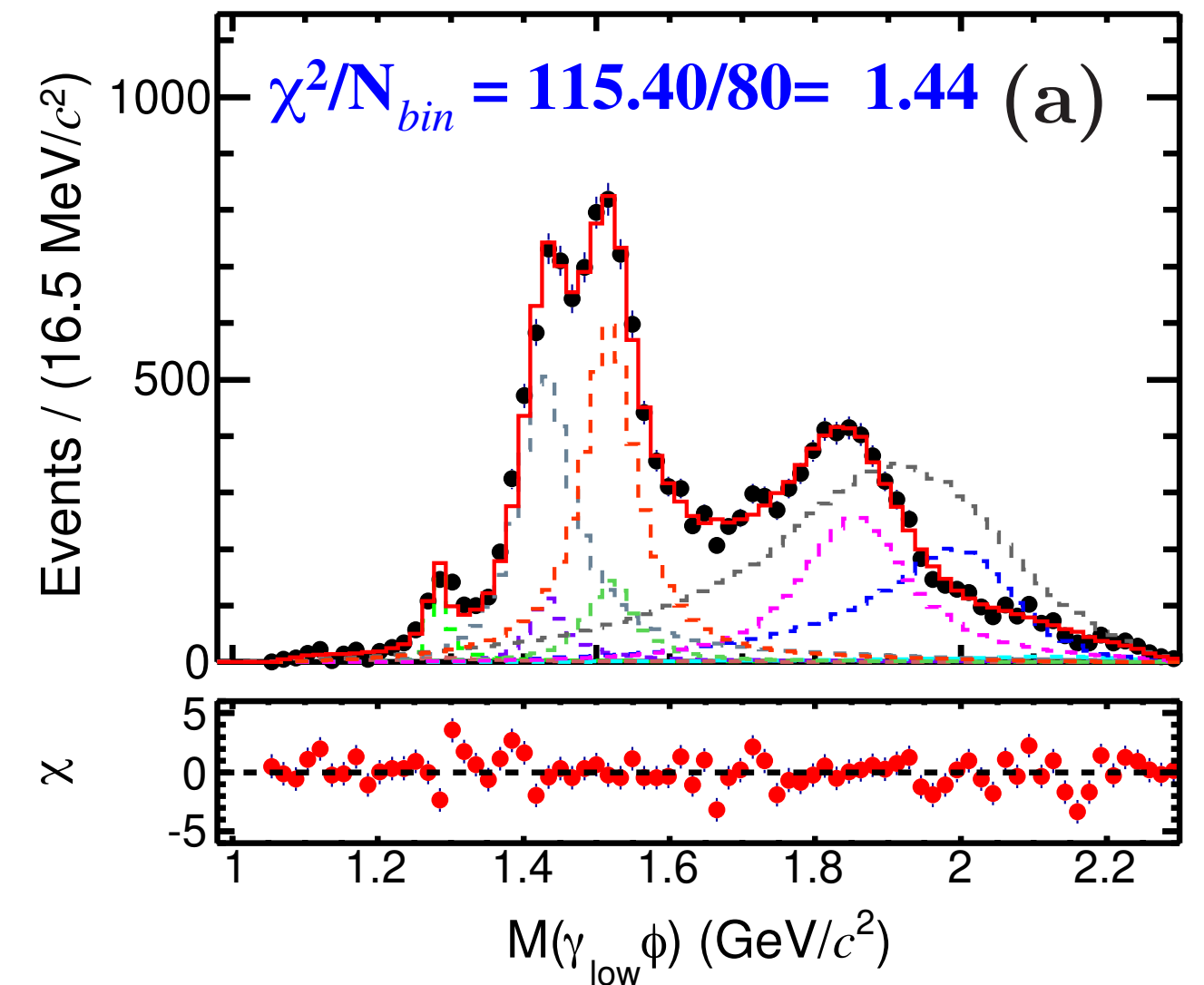
Direct link between the $X(p\bar{p})$ and $X(1835)$



[PRL 117, 042002](#)



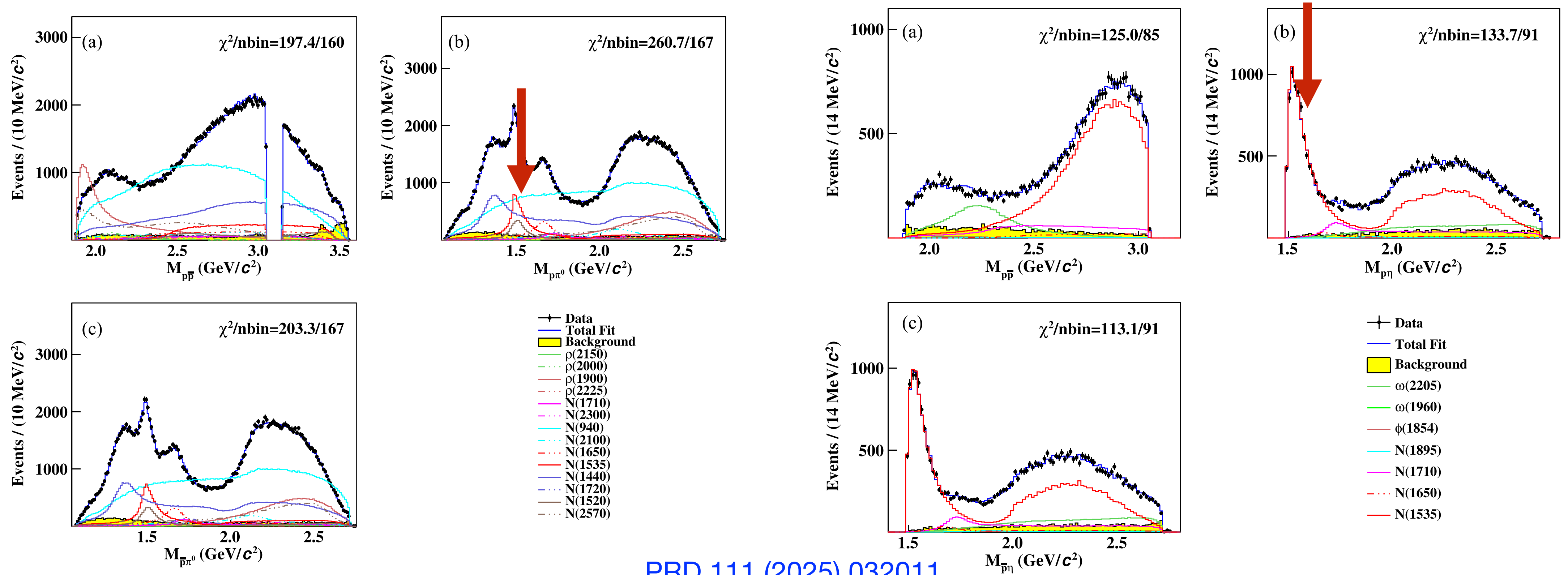
[PRL 132 \(2024\) 151901](#)



[arxiv:2401.00918](#)

- ◆ **Anomalous $\pi\pi\eta'$ line shape near $M_{p\bar{p}}$ threshold: first establish the direct link between the $X(1835)$ and $X(p\bar{p})$**
 - ✦ Two models (Flatte formula/2-resonance) can fit data well: **interpretations of $p\bar{p}$ mass threshold as a molecule state or a bound state**
- ◆ **Anomalous shape observed in $J/\psi \rightarrow \gamma 3(\pi\pi)$ near $M_{p\bar{p}}$ threshold**
 - ✦ **Two structures of $X(1840)$ and $X(1880)$ give a good description on data: interpretation of a bound state**
- ◆ **Mass and width of the $X(1835)$ in $J/\psi \rightarrow \gamma\gamma\phi$ are consistent with those in $J/\psi \rightarrow \gamma K_s K_s \eta$:**
 - ✦ **$X(1835)$ contains a sizable $s\bar{s}$ component**

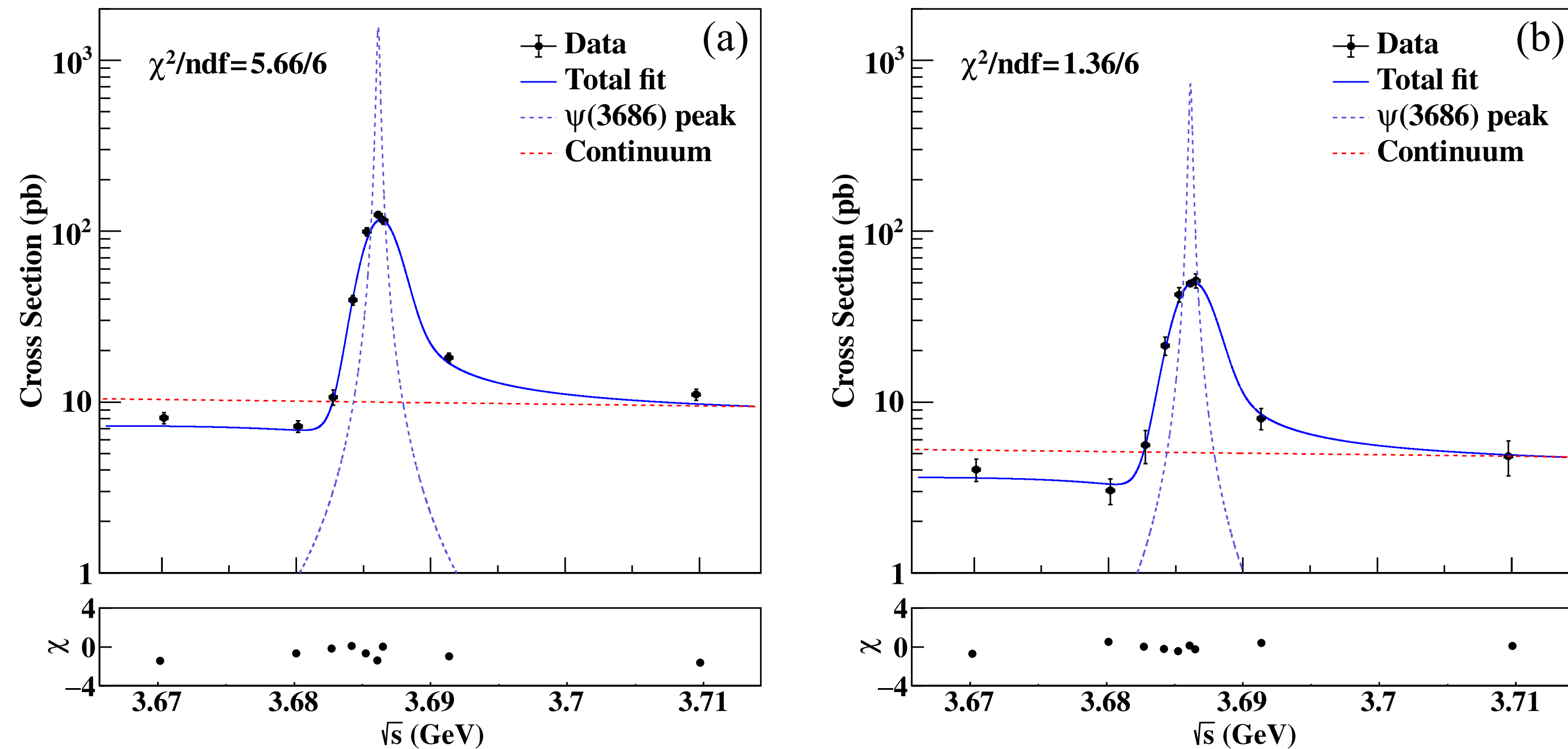
$\psi(3686) \rightarrow p\bar{p}\pi^0$ and $\psi(3686) \rightarrow p\bar{p}\eta$



- ◆ Data can be well described by the well-established N^* states
- ◆ Ratio of the $N(1535)$ decays is measured, which suggests a strong $s\bar{s}$ components

$$\Gamma_{N(1535) \rightarrow N\eta} / \Gamma_{N(1535) \rightarrow N\pi} = 0.99 \pm 0.05 \pm 0.19$$

$\psi(3686) \rightarrow p\bar{p}\pi^0$ and $\psi(3686) \rightarrow p\bar{p}\eta$

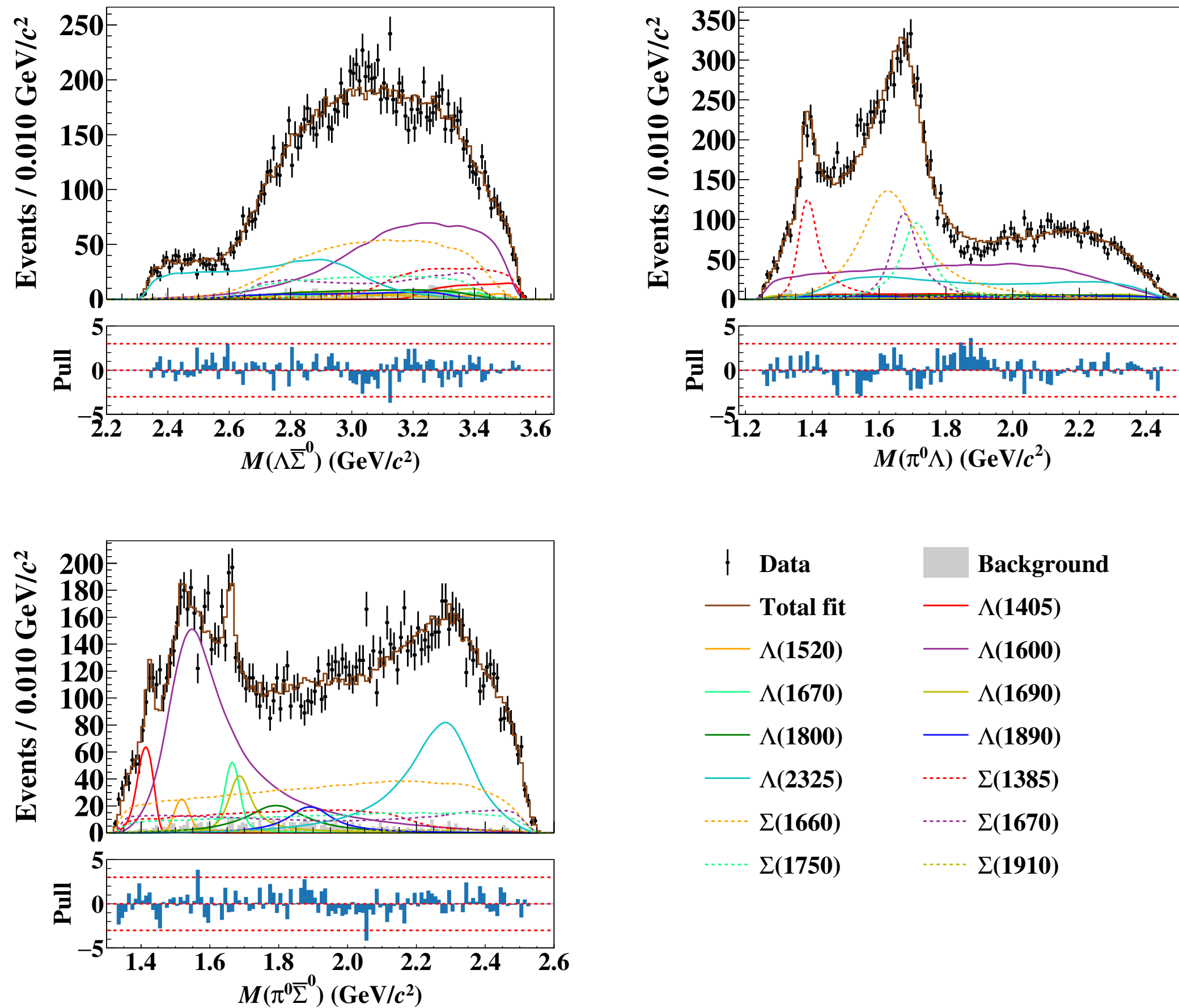


$\psi(3686) \rightarrow p\bar{p}\pi^0$	$\mathcal{B}_f \Gamma_{ee}$ (0.1 eV)	ϕ ($^\circ$)	ΔE (MeV)	\mathcal{B}_f ($\times 10^{-6}$)
Constructive solution	3.12 ± 0.26	65.0 ± 6.7	1.27 ± 0.09	$133.9 \pm 11.2 \pm 2.3$
Destructive solution	4.28 ± 0.32	-68.9 ± 5.7	1.27 ± 0.09	$183.7 \pm 13.7 \pm 3.2$
$\psi(3686) \rightarrow p\bar{p}\eta$	$\mathcal{B}_f \Gamma_{ee}$ (0.1 eV)	ϕ ($^\circ$)	ΔE (MeV)	\mathcal{B}_f ($\times 10^{-6}$)
Constructive solution	1.44 ± 0.15	58.9 ± 14.1	1.39 ± 0.14	$61.5 \pm 6.5 \pm 1.1$
Destructive solution	1.98 ± 0.16	-63.8 ± 12.1	1.39 ± 0.14	$84.4 \pm 6.9 \pm 1.4$

[PRD 111 \(2025\) 032011](#)

- ◆ $B(\psi(3686) \rightarrow p\bar{p}\pi^0)/B(J/\psi \rightarrow p\bar{p}\pi^0)$
 - ◆ $(11.3 \pm 1.2) \%$ (constructive interference)
 - ◆ $(15.4 \pm 1.6) \%$ (destructive interference)
- ◆ $B(\psi(3686) \rightarrow p\bar{p}\eta)/B(J/\psi \rightarrow p\bar{p}\eta)$
 - ◆ $(3.1 \pm 0.4) \%$ (constructive interference)
 - ◆ $(4.2 \pm 0.4) \%$ (destructive interference)
 - ◆ Violated from the “12%” rule

$\psi(3686) \rightarrow \Lambda \bar{\Sigma}^0 \pi^0$



$\Lambda(1405)$ Faltte-like model

$$R(m) = \frac{1}{m_0^2 - m^2 - im_0 \left[\sum_i g_i \frac{q_i}{m} \times \frac{m_0}{|q_{i0}|} \times \frac{|q_i|^{2l_i}}{|q_{i0}|^{2l_i}} B_{l_i}'^2(|q_i|, |q_{i0}|, d) \right]},$$

$$q_i = \begin{cases} \frac{\sqrt{(m^2 - (m_{i,1} + m_{i,2})^2)(m^2 - (m_{i,1} - m_{i,2})^2)}}{2m} & (m^2 - (m_{i,1} + m_{i,2})^2)(m^2 - (m_{i,1} - m_{i,2})^2) \geq 0, \\ \frac{i\sqrt{|(m^2 - (m_{i,1} + m_{i,2})^2)(m^2 - (m_{i,1} - m_{i,2})^2)|}}{2m} & (m^2 - (m_{i,1} + m_{i,2})^2)(m^2 - (m_{i,1} - m_{i,2})^2) < 0. \end{cases}$$

$\Lambda(1405)$ chiral dynamics model (two poles)

$$R(m) = \frac{1}{|I - VG|},$$

$$V_{ij}(m) = -C_{ij} \frac{1}{4f^2} (2m - M_i - M_j) \sqrt{\frac{M_i - E_i}{M_i}} \sqrt{\frac{M_j - E_j}{M_j}},$$

$$G_k(m; \mu) = \frac{1}{(4\pi)^2} \left\{ a_k(\mu) + \ln \frac{M_k^2}{\mu} + \frac{m_k^2 - M_k^2 + m^2}{2m^2} \ln \frac{m_k^2}{M_k^2} \right. \\ \left. + \frac{q_k}{m} [\ln(m^2 - (M_k^2 - m_k^2) + 2q_k m) + \ln(m^2 + (M_k^2 - m_k^2) + 2q_k m) \right. \\ \left. - \ln(-m^2 + (M_k^2 - m_k^2) + 2q_k m) - \ln(-m^2 - (M_k^2 - m_k^2) + 2q_k m) \right\},$$

◆ Due to limited statistics, no separation power for the two $\Lambda(1405)$ models (11σ)

◆ $\Lambda(2325)$ is necessary to better describe data with its spin-parity $J^P = 3/2^-$

Summary

- ◆ A set of interesting and important results from the light hadron spectroscopy achieved:
 - ◆ **Discovery of a glueball-like particle: X(2370)**
 - ◆ Strong correlation between the X(1835) and $M_{p\bar{p}}$ threshold enhancement. A molecule state or a bound state?
 - ◆ Observation of An Exotic 1^{-+} Isoscalar state $\eta_1(1855)$ and Isovector state $\pi(1600)$
 - ◆ ...
- ◆ With the more data, the more extensive and intensive investigation are ongoing, looking forward to new results in the near future.