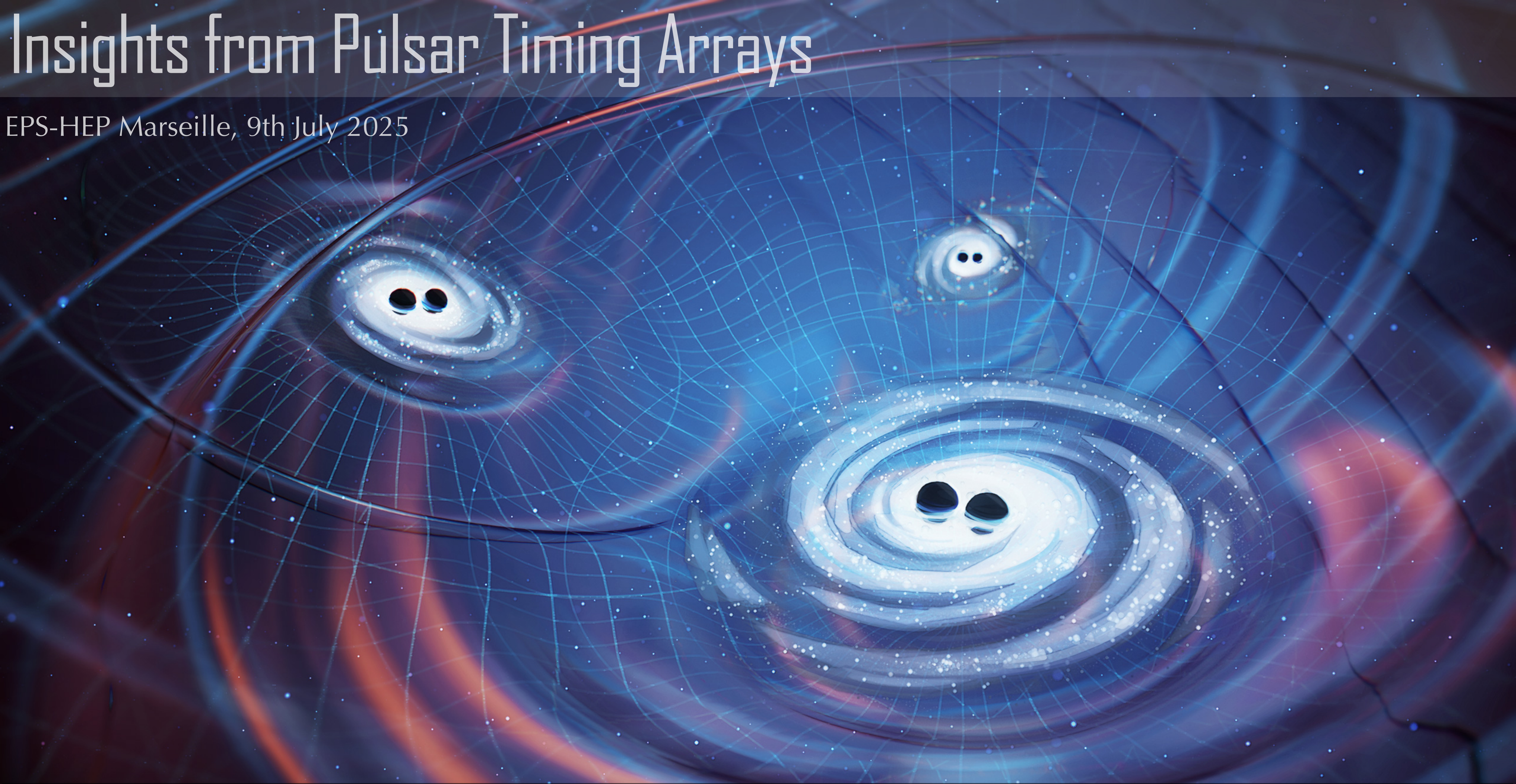


Insights from Pulsar Timing Arrays

EPS-HEP Marseille, 9th July 2025



Sonali Verma [ULB Brussels]

Illustration Credit: Olena Shmahalo for NANOGrav

NANOGrav
Physics Frontiers Center

PULSAR

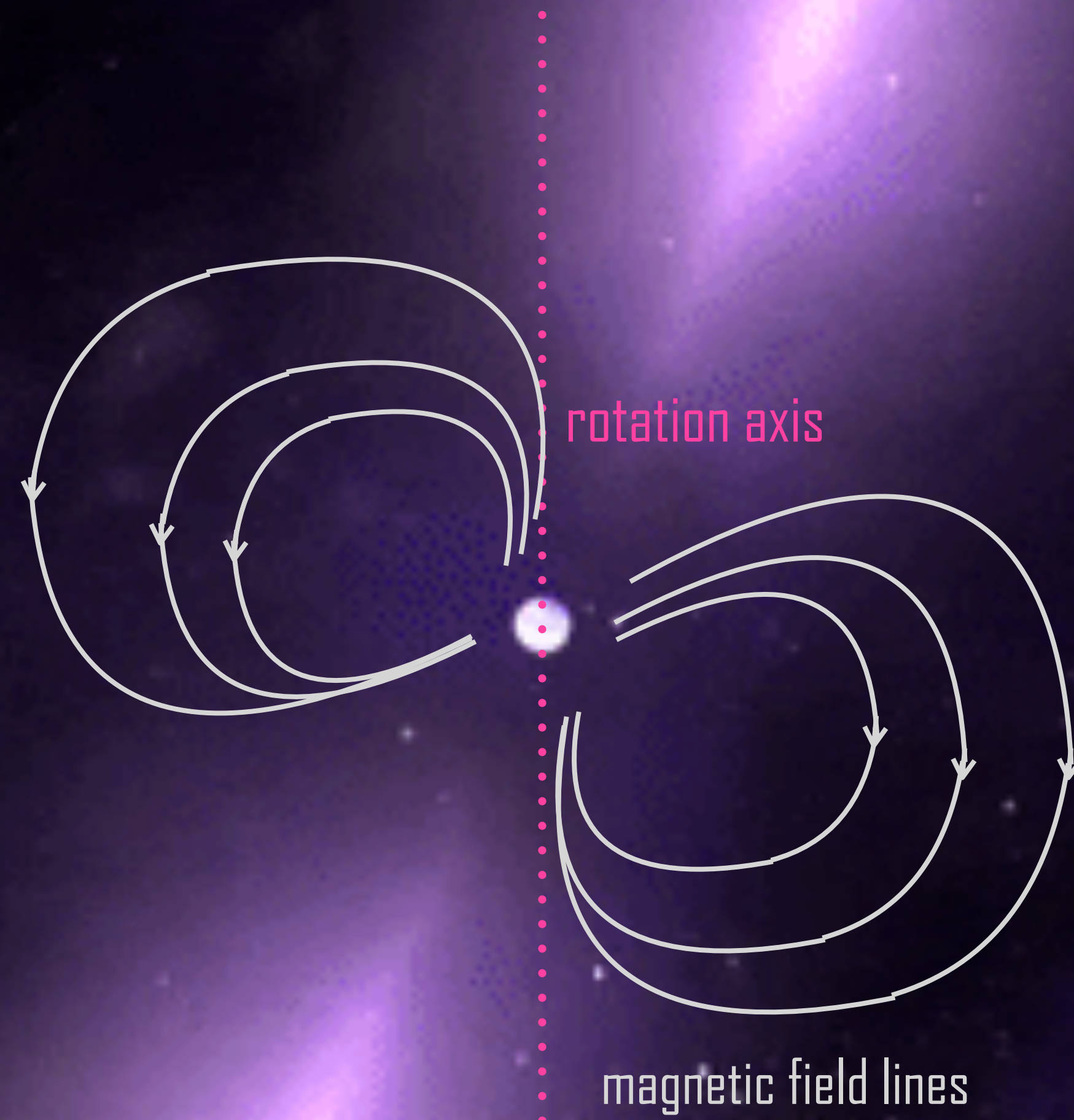
are rotating neutron stars



PULSAR

are rotating neutron stars

radio-beam emitters

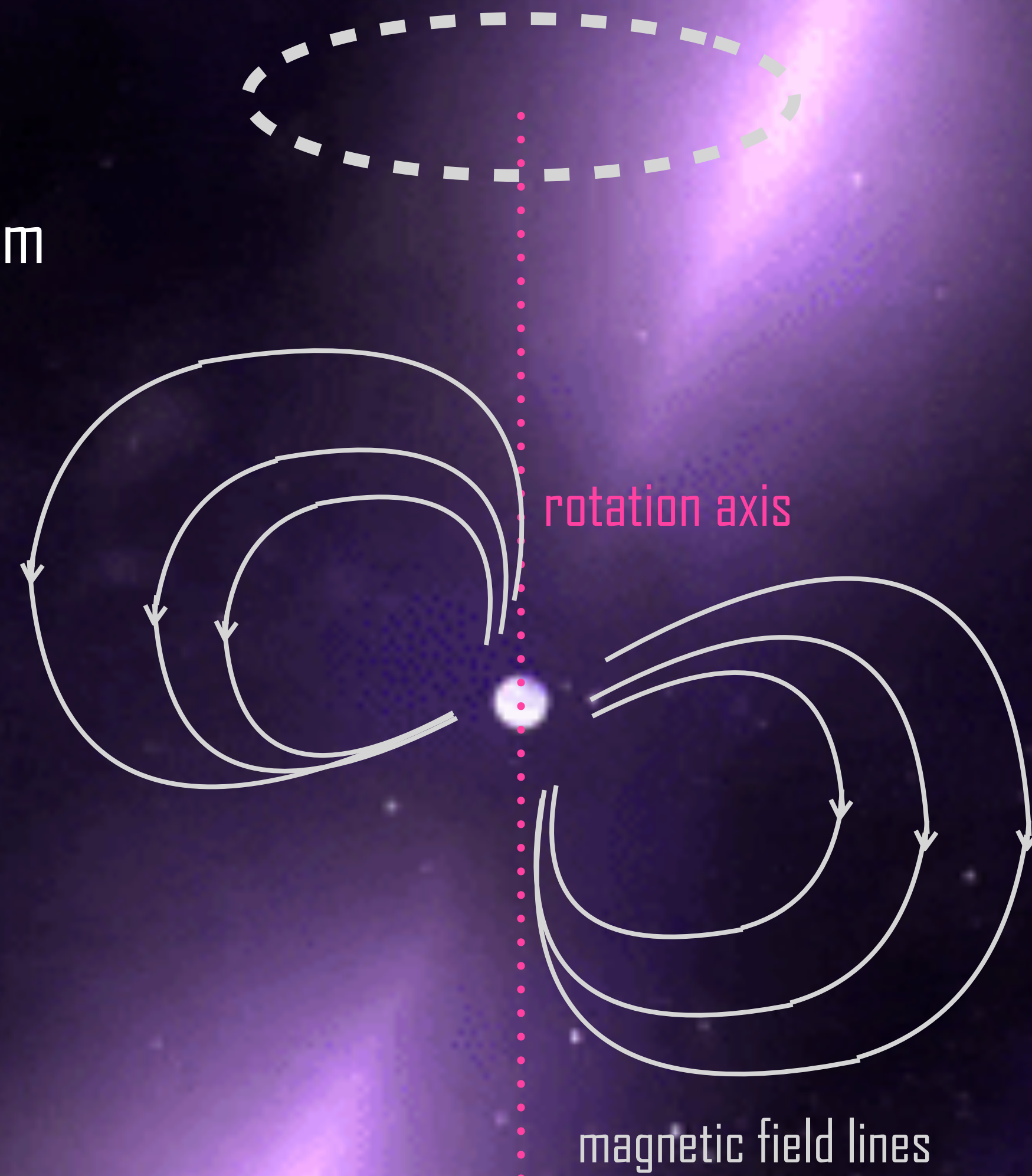


PULSAR

are rotating neutron stars

radio-beam emitters

like a light-house beam

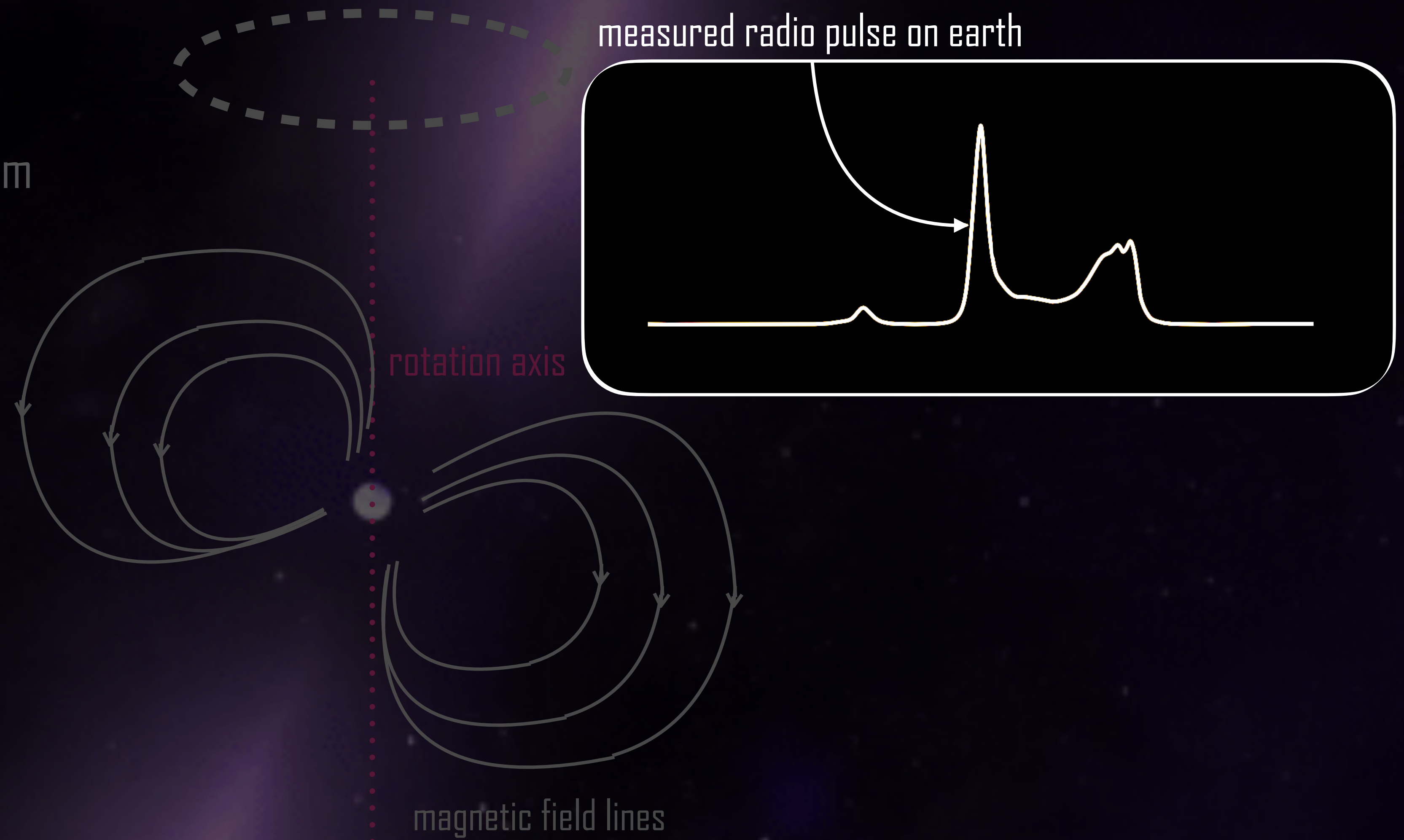


PULSAR

are rotating neutron stars

radio-beam emitters

like a light-house beam

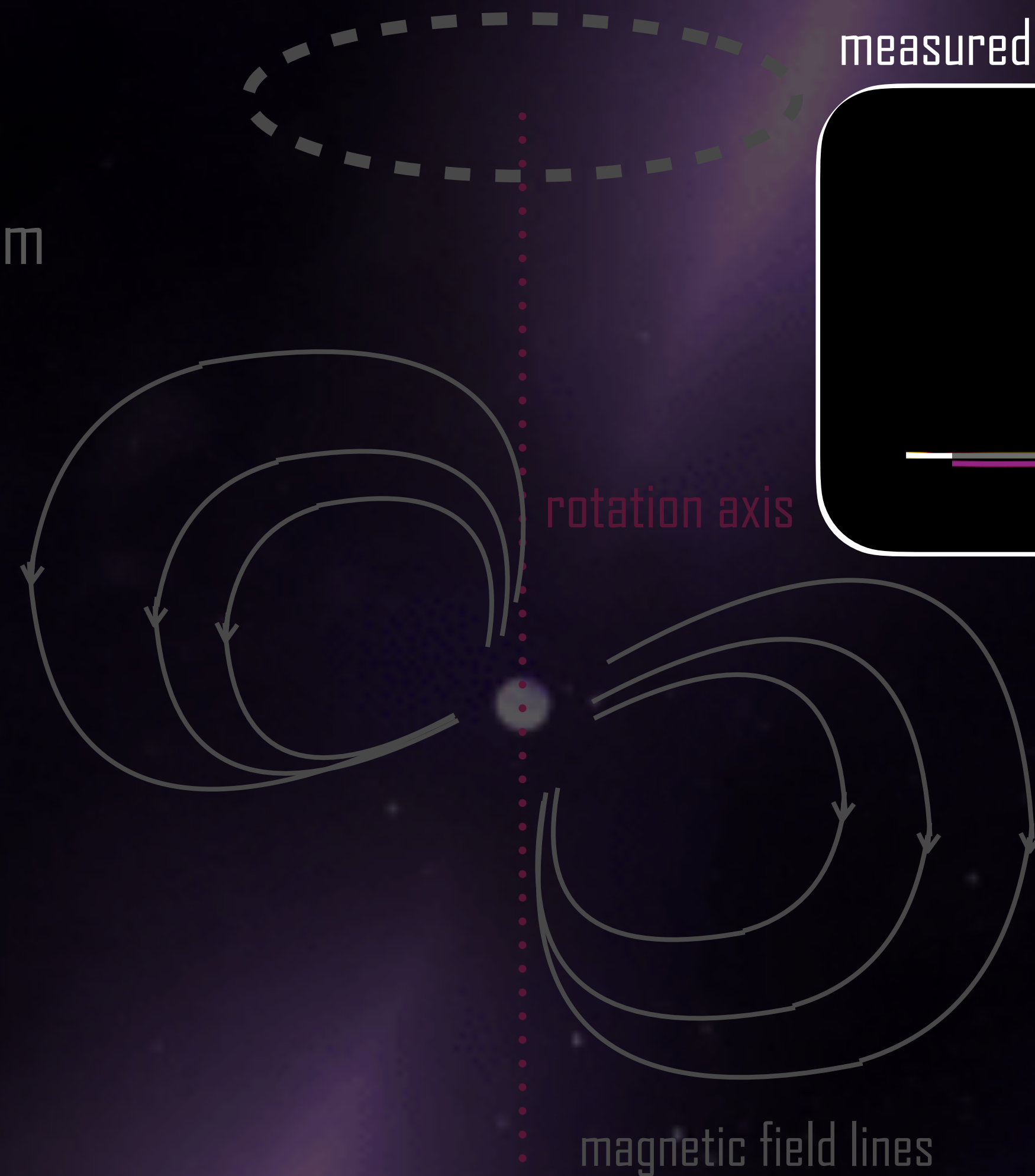


PULSAR

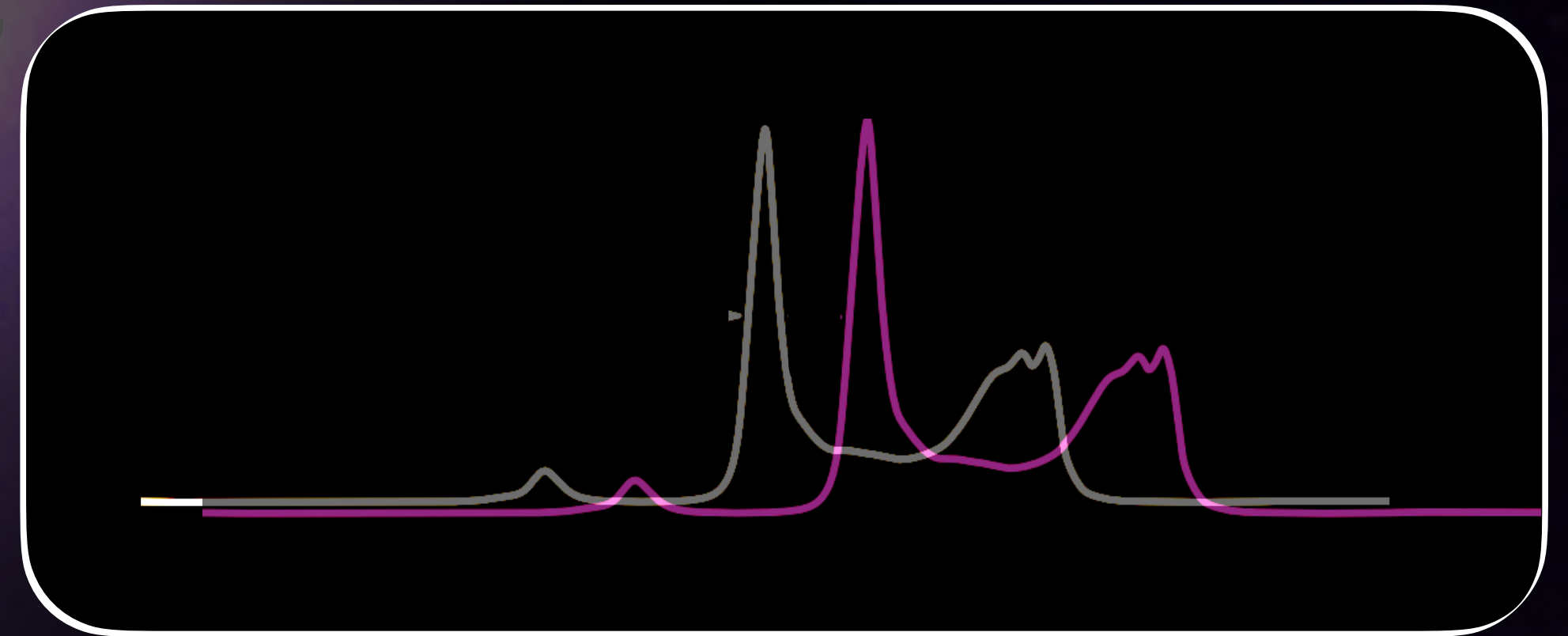
are rotating neutron stars

radio-beam emitters

like a light-house beam



measured radio pulse on earth



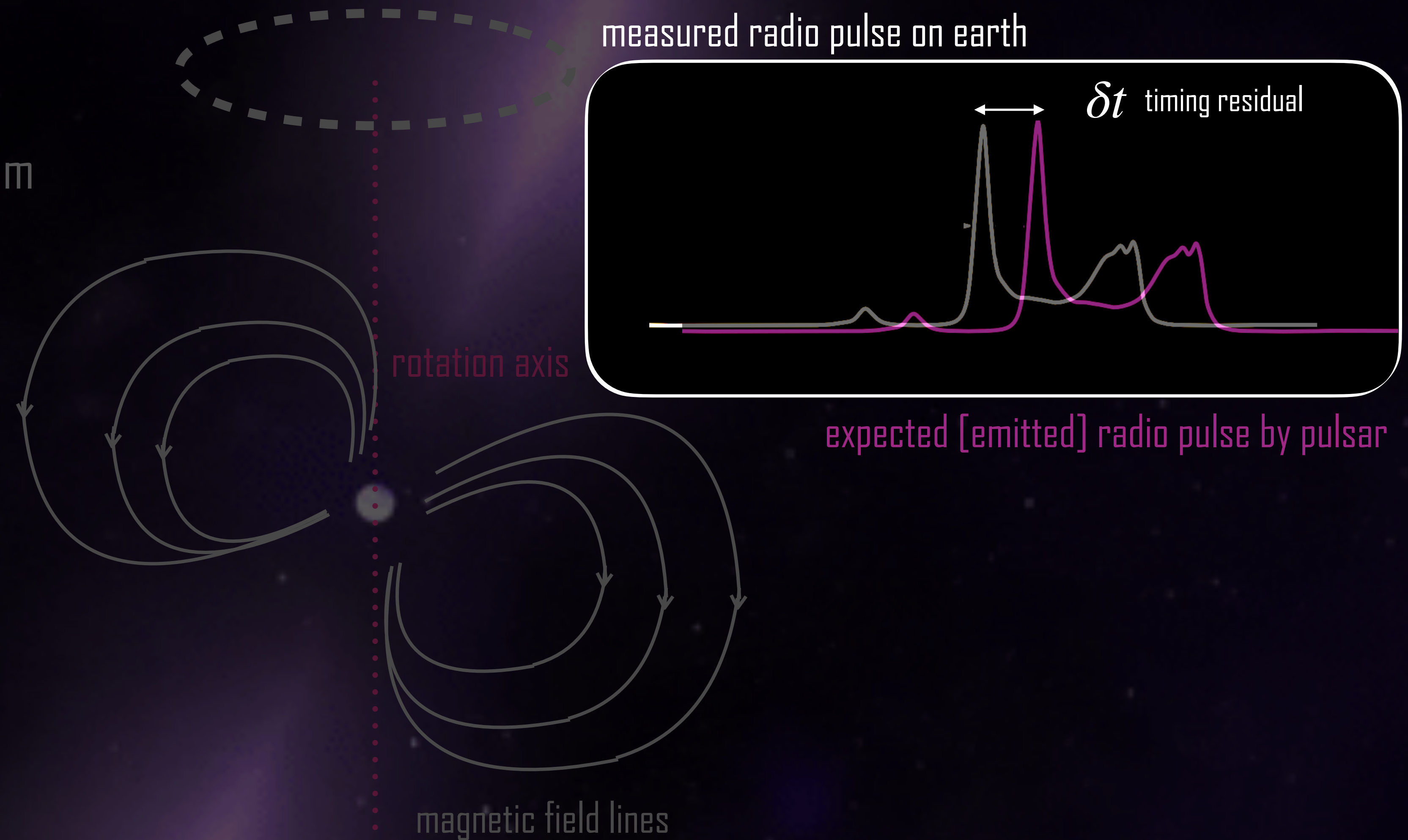
expected [emitted] radio pulse by pulsar

PULSAR

are rotating neutron stars

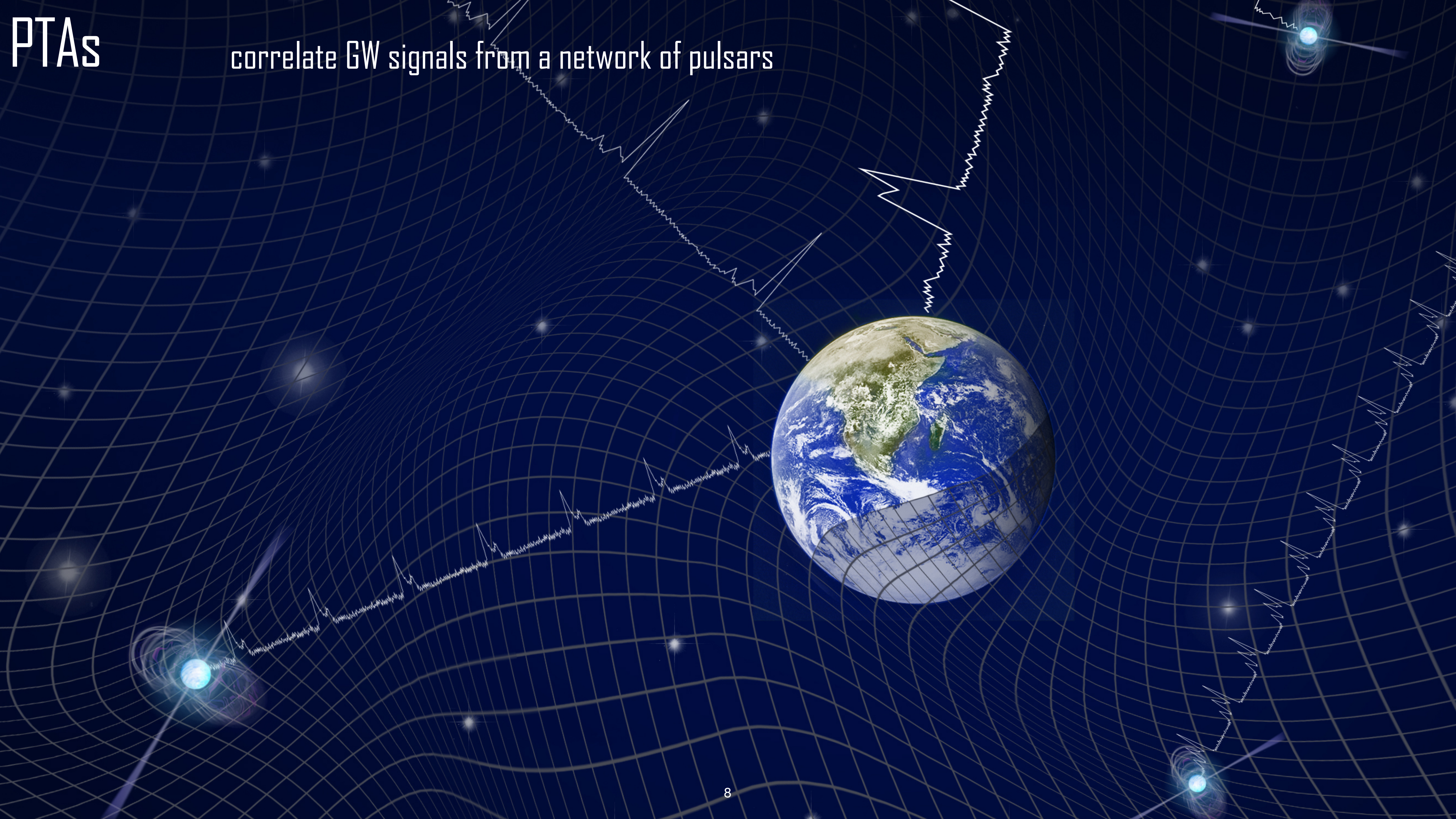
radio-beam emitters

like a light-house beam



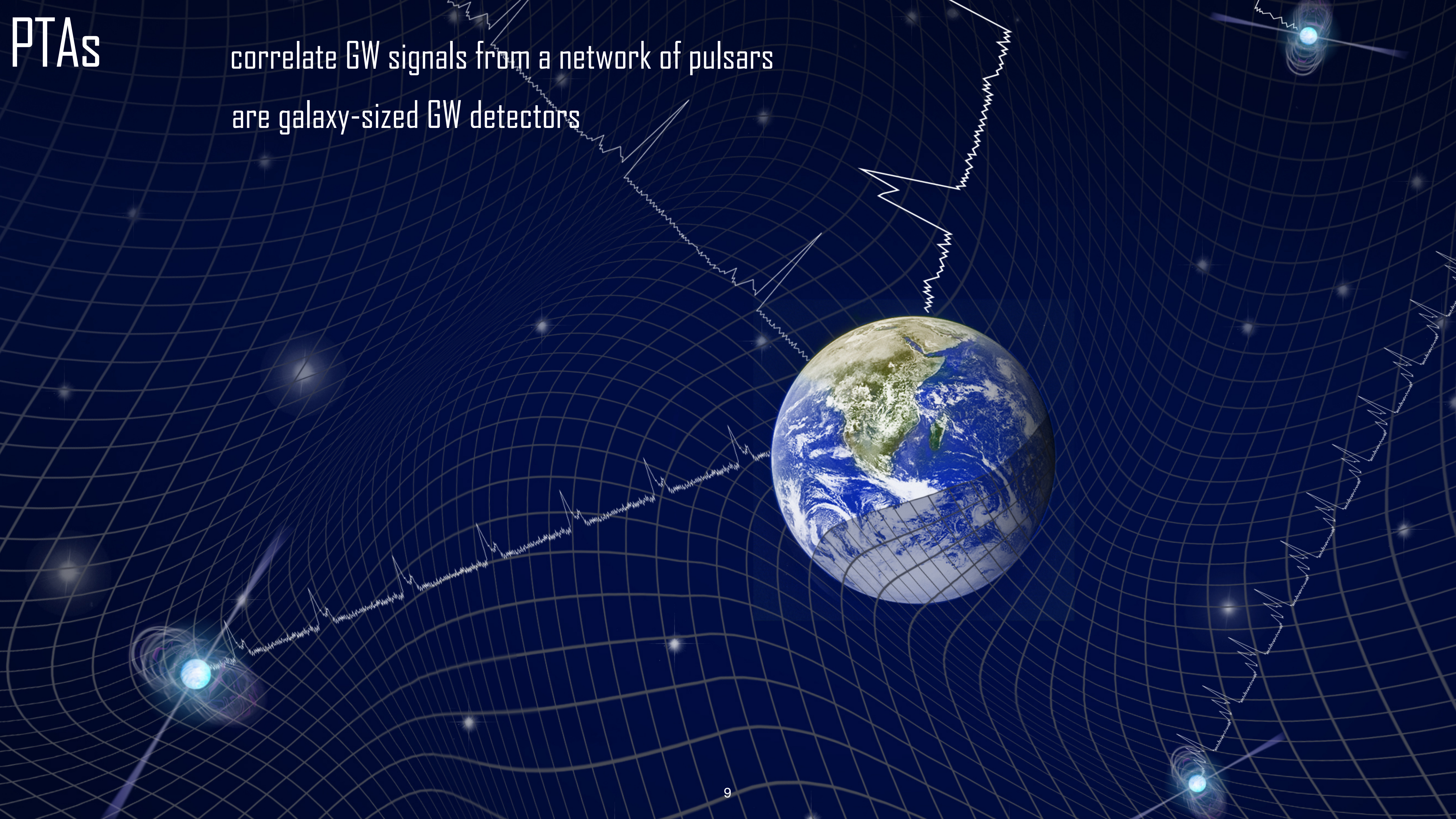
PTAs

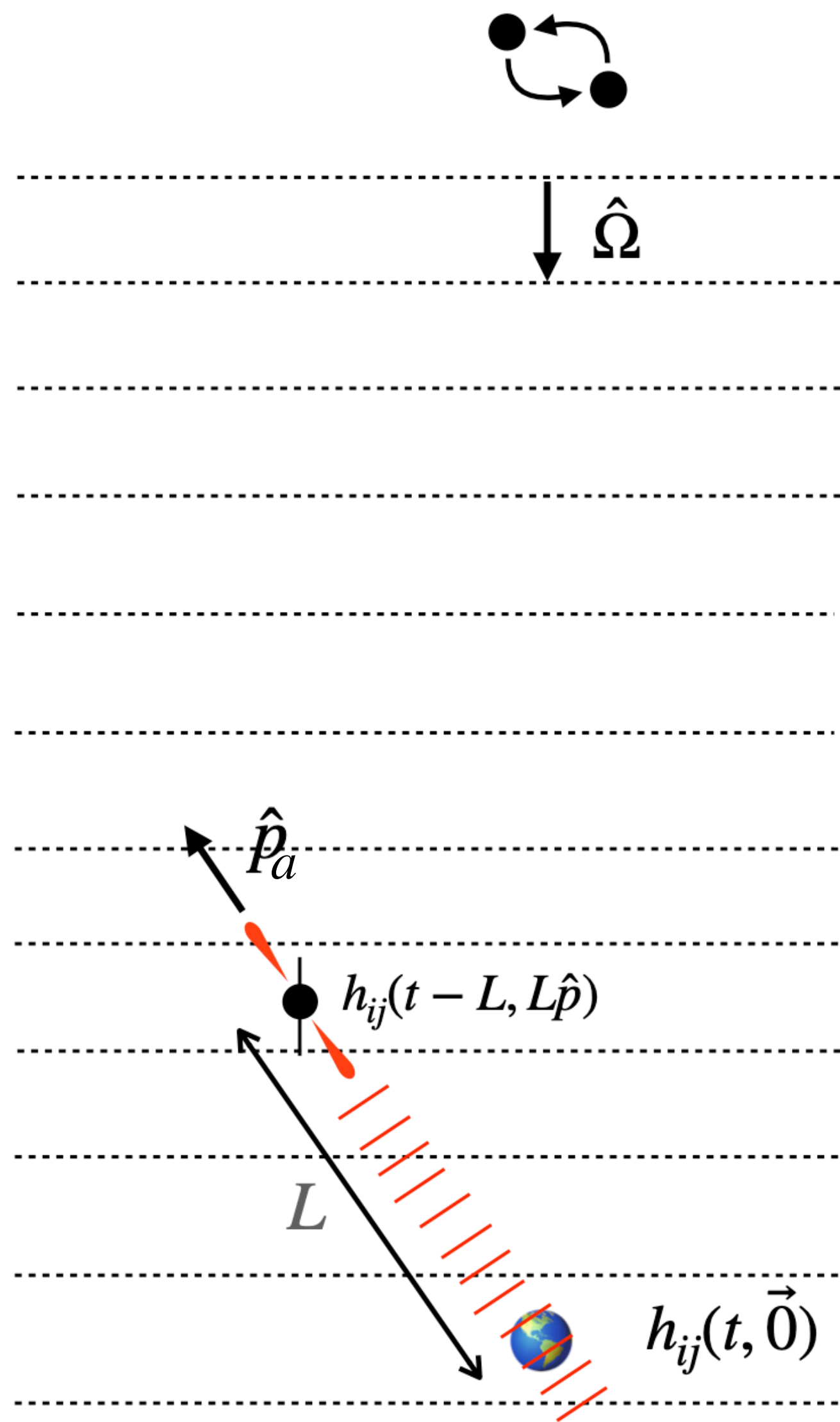
correlate GW signals from a network of pulsars



PTAs

correlate GW signals from a network of pulsars
are galaxy-sized GW detectors

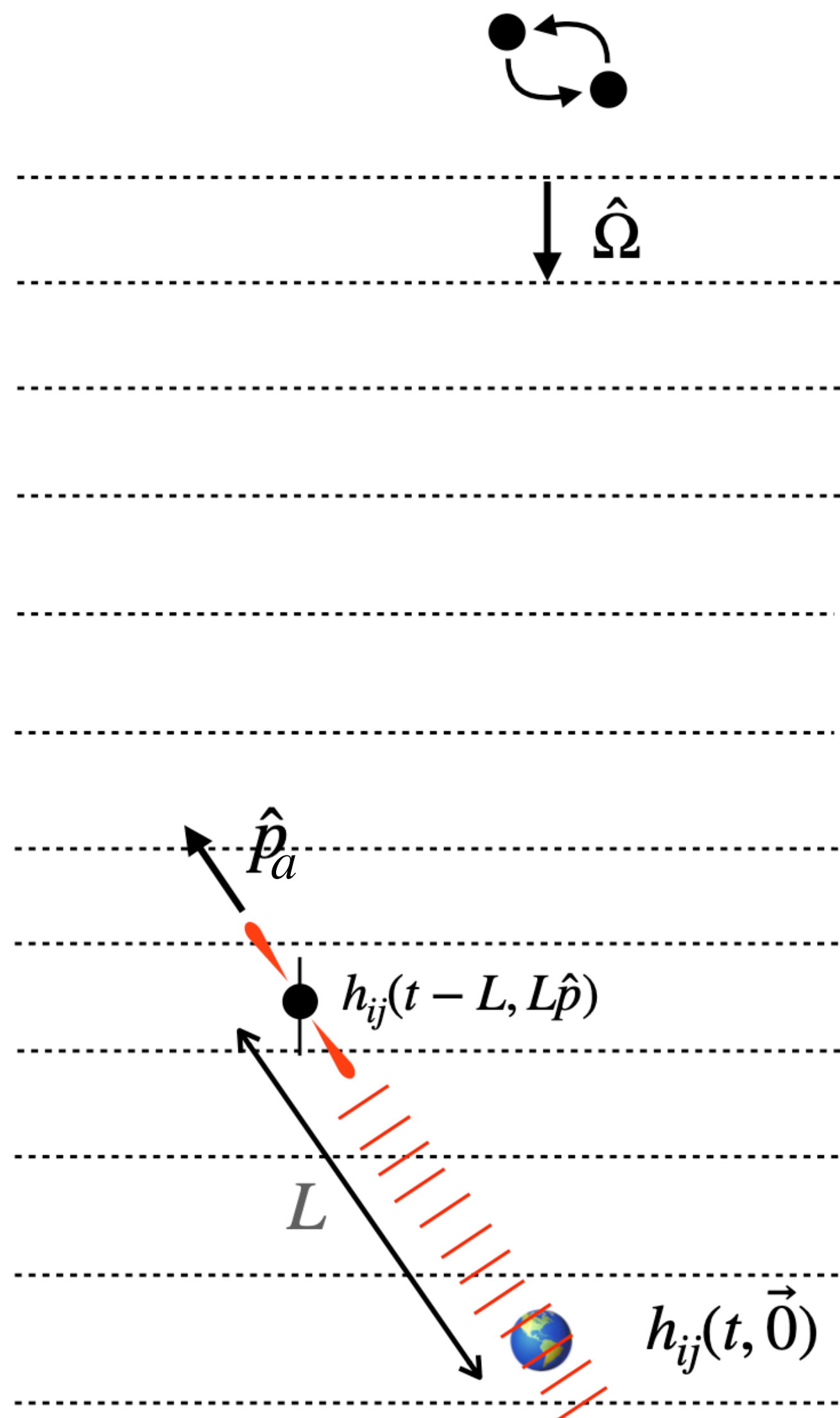




For a distant source of GW

$$z_a(t) \equiv \frac{\Delta\nu_a}{\nu_a} = \frac{1}{2} \frac{\hat{p}_a^i \hat{p}_a^j}{1 + \hat{\Omega} \cdot \hat{p}_a} \left[h_{ij}(t, 0) - h_{ij}(t - L, L\hat{p}_a) \right]$$

Figure from [arxiv: 2308.05847]



For a distant source of GW

$$z_a(t) \equiv \frac{\Delta\nu_a}{\nu_a} = \frac{1}{2} \frac{\hat{p}_a^i \hat{p}_a^j}{1 + \hat{\Omega} \cdot \hat{p}_a} \left[h_{ij}(t, 0) - h_{ij}(t - L, L\hat{p}_a) \right]$$

GW-induced change in pulse frequency

$$\delta t_a = \int_0^t dt' z_a(t')$$

Figure from [arxiv: 2308.05847]

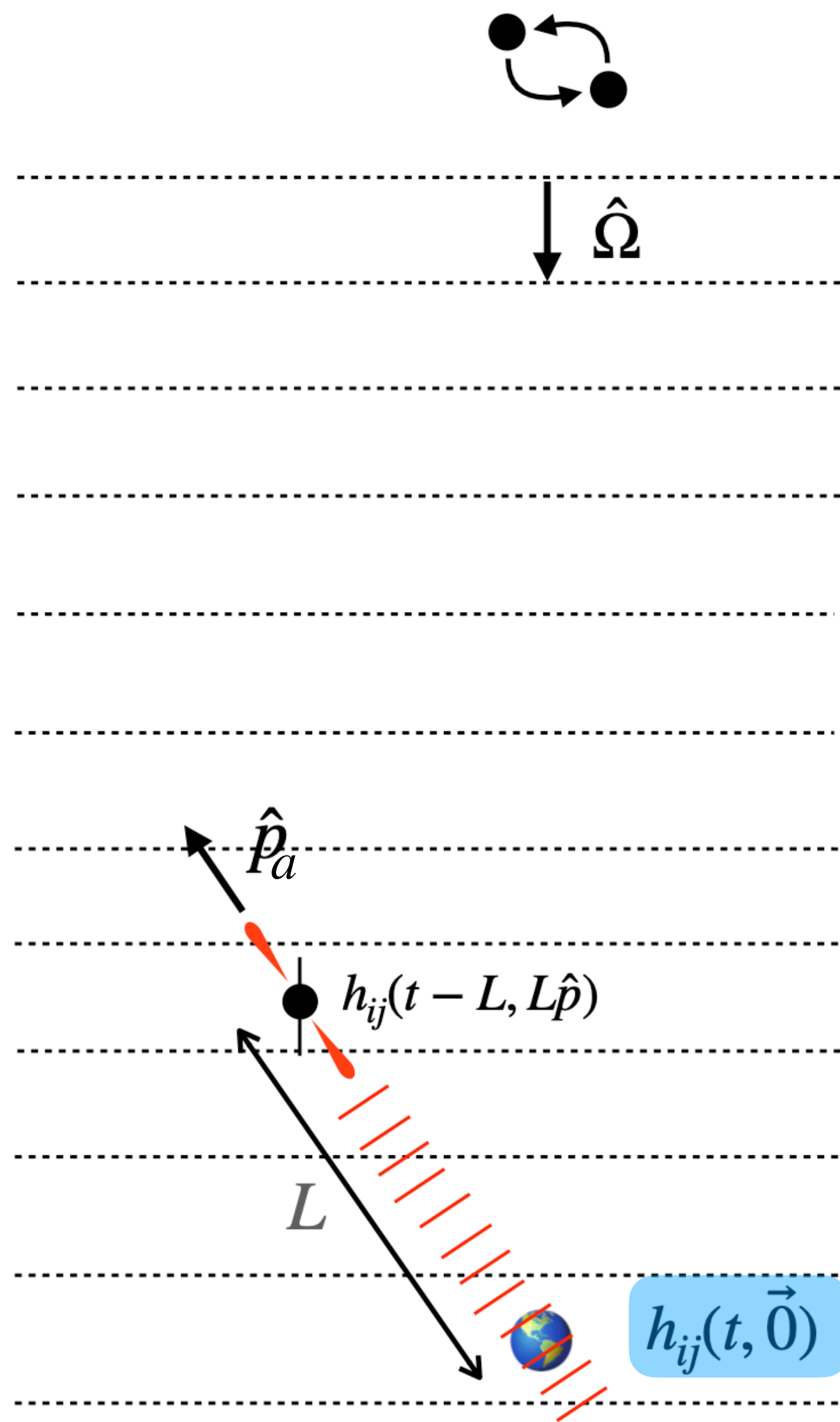


Figure from [arxiv: 2308.05847]

For a distant source of GW

Metric perturbation when pulse is received

$$z_a(t) \equiv \frac{\Delta\nu_a}{\nu_a} = \frac{1}{2} \frac{\hat{p}_a^i \hat{p}_a^j}{1 + \hat{\Omega} \cdot \hat{p}_a} \left[h_{ij}(t, 0) - h_{ij}(t - L, L\hat{p}_a) \right]$$

GW-induced change in pulse frequency

earth term

$$\delta t_a = \int_0^t dt' z_a(t')$$

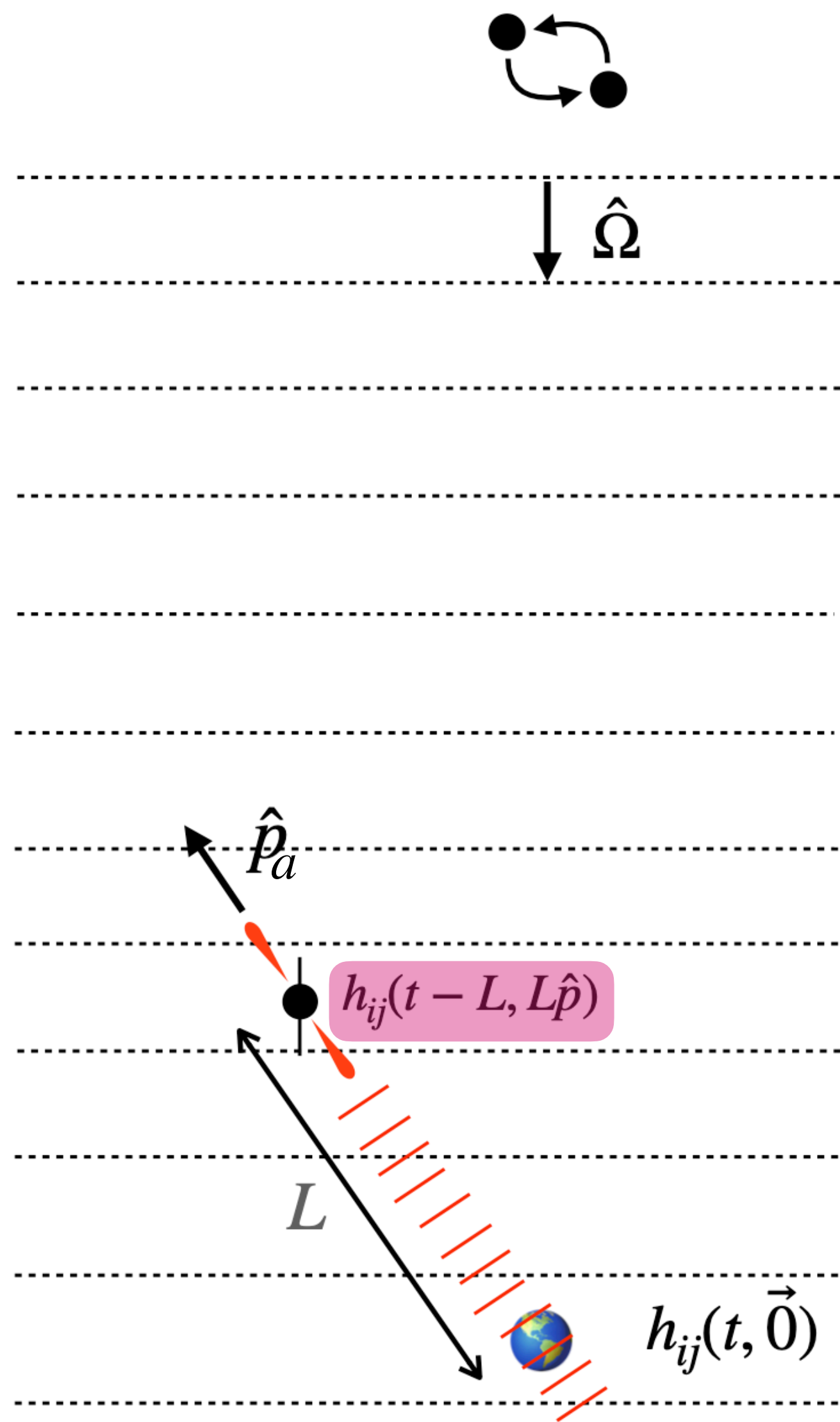


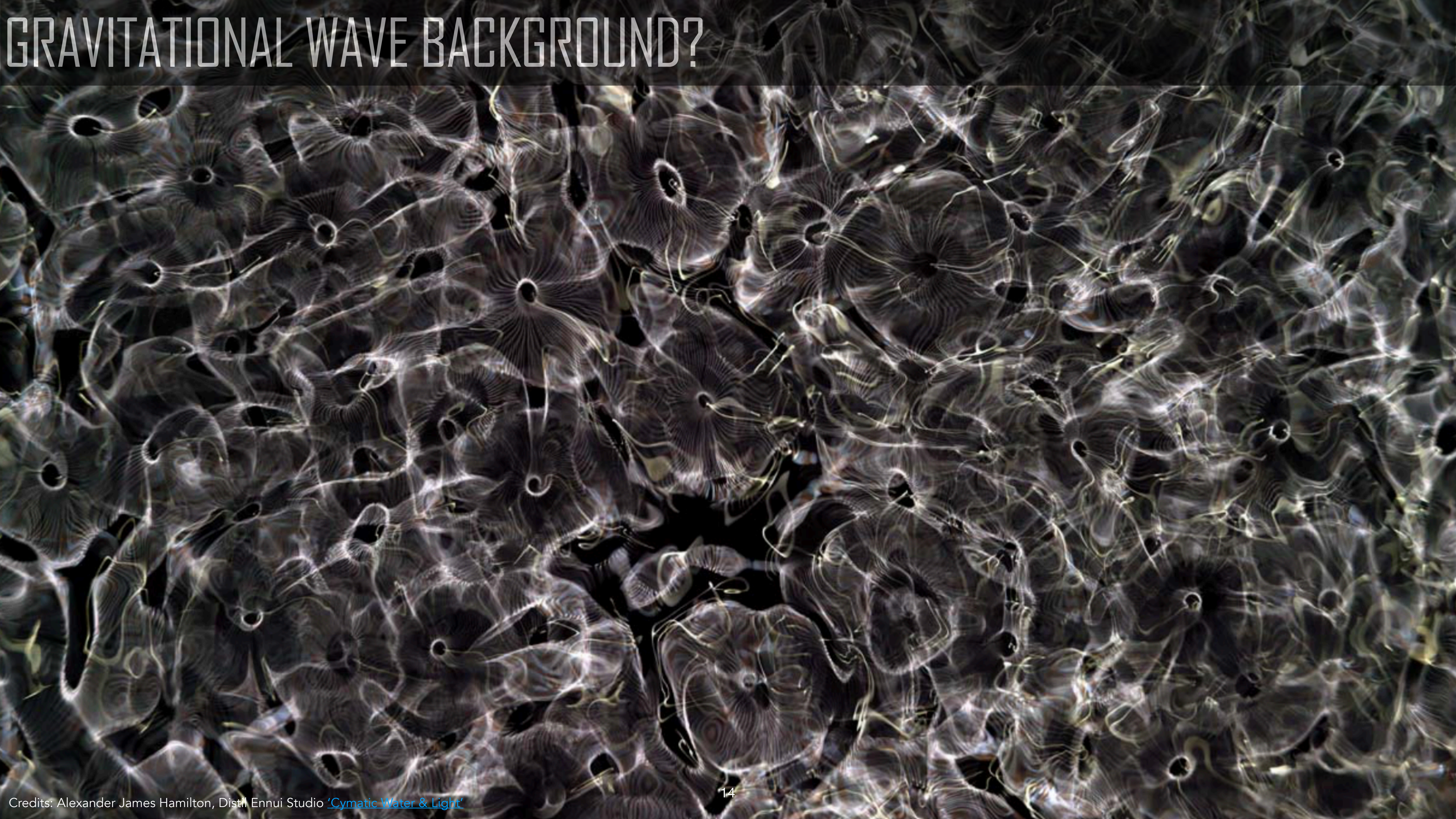
Figure from [arxiv: 2308.05847]

For a distant source of GW

$$z_a(t) \equiv \frac{\Delta\nu_a}{\nu_a} = \frac{1}{2} \frac{\hat{p}_a^i \hat{p}_a^j}{1 + \hat{\Omega} \cdot \hat{p}_a} \left[\overset{\text{Metric perturbation when pulse is emitted}}{h_{ij}(t, 0)} - h_{ij}(t - L, L\hat{p}_a) \right]$$

GW-induced change in pulse frequency
earth term
pulsar term

$$\delta t_a = \int_0^t dt' z_a(t')$$



GRAVITATIONAL WAVE BACKGROUND?

GRAVITATIONAL WAVE BACKGROUND?

$$\langle \delta t_a(t) \delta t_b(t) \rangle$$

GRAVITATIONAL WAVE BACKGROUND?

Hellings and Downs Correlations

GWB characteristic strain

$$\langle \delta t_a(t) \delta t_b(t) \rangle \simeq \underbrace{\Gamma_{ab}(\zeta_{ab})}_{\text{angular separation } \zeta_{ab} \text{ dependence}} \int df \frac{1}{12\pi^2} f^{-3} \underbrace{h_c(f)^2}_{\text{frequency } f \text{ dependence}}$$

angular separation ζ_{ab} dependence

frequency f dependence

GRAVITATIONAL WAVE BACKGROUND?

$$\langle \delta t_a(t) \delta t_b(t) \rangle \simeq \Gamma_{ab}(\zeta_{ab}) \int df \frac{1}{12\pi^2} \boxed{f^{-3} h_c(f)^2}$$

└
frequency f dependence

GRAVITATIONAL WAVE BACKGROUND?

Hellings and Downs Correlations

GWB characteristic strain

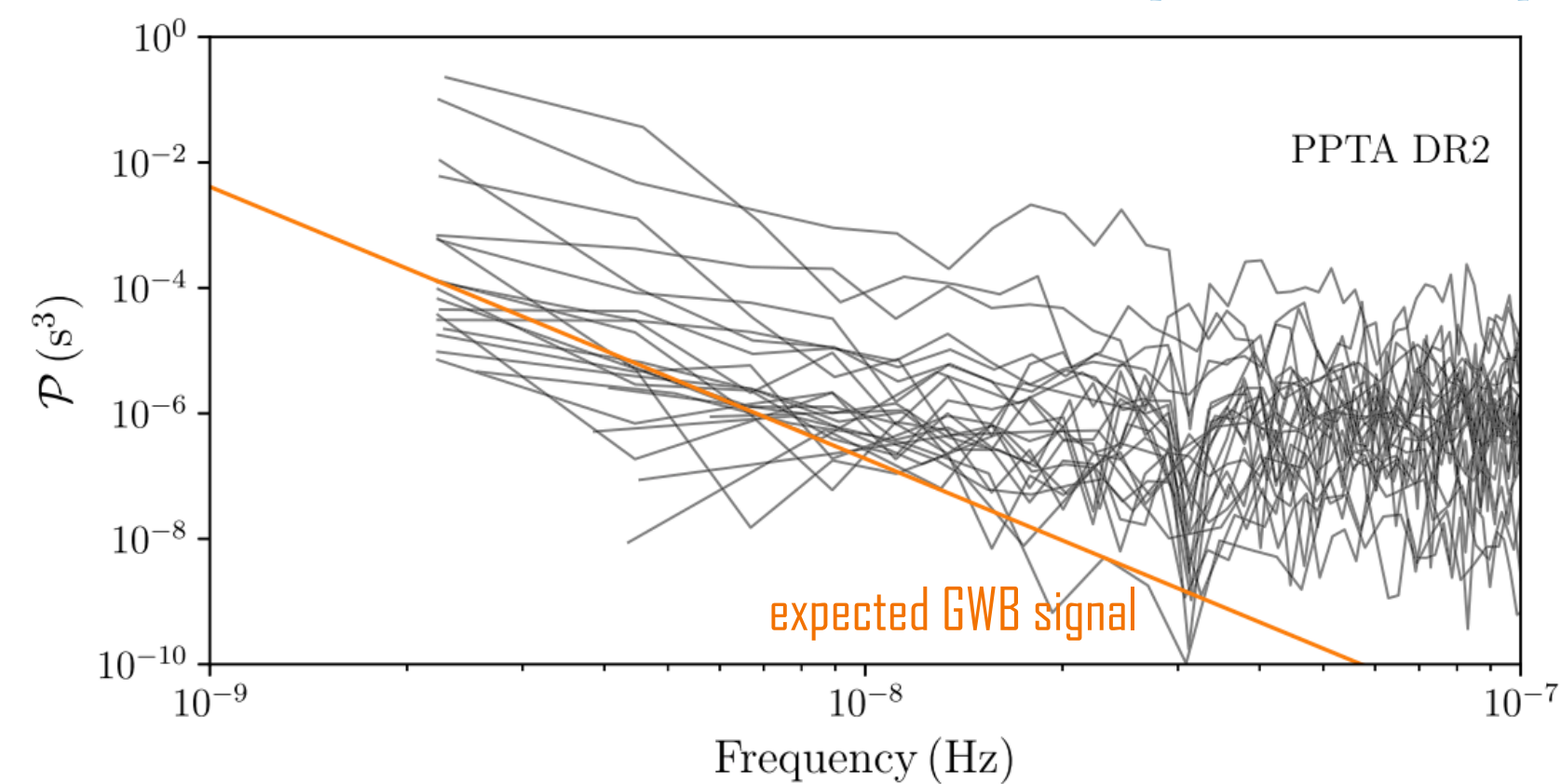
$$\langle \delta t_a(t) \delta t_b(t) \rangle \simeq \underbrace{\Gamma_{ab}(\zeta_{ab})}_{\text{angular separation } \zeta_{ab} \text{ dependence}} \int \underbrace{df}_{\text{frequency } f \text{ dependence}} \frac{1}{12\pi^2} \underbrace{f^{-3} h_c(f)^2}_{\text{GWB characteristic strain}}$$

angular separation ζ_{ab} dependence

frequency f dependence

pulsar noise

[Zic et al. '22]

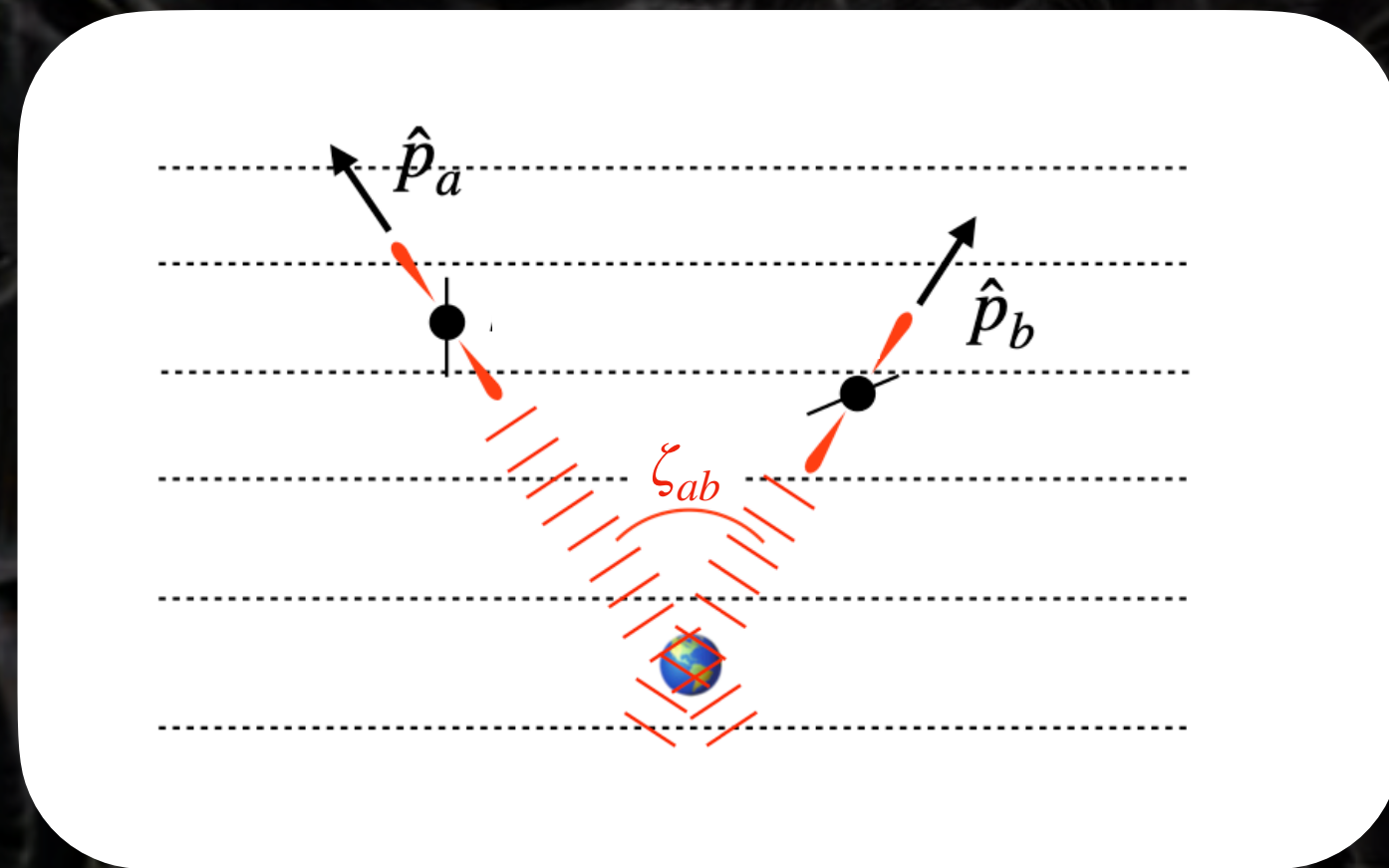


GRAVITATIONAL WAVE BACKGROUND?

Hellings and Downs Correlations

$$\langle \delta t_a(t) \delta t_b(t) \rangle \simeq \boxed{\Gamma_{ab}(\zeta_{ab})} \int df \frac{1}{12\pi^2} f^{-3} h_c(f)^2$$

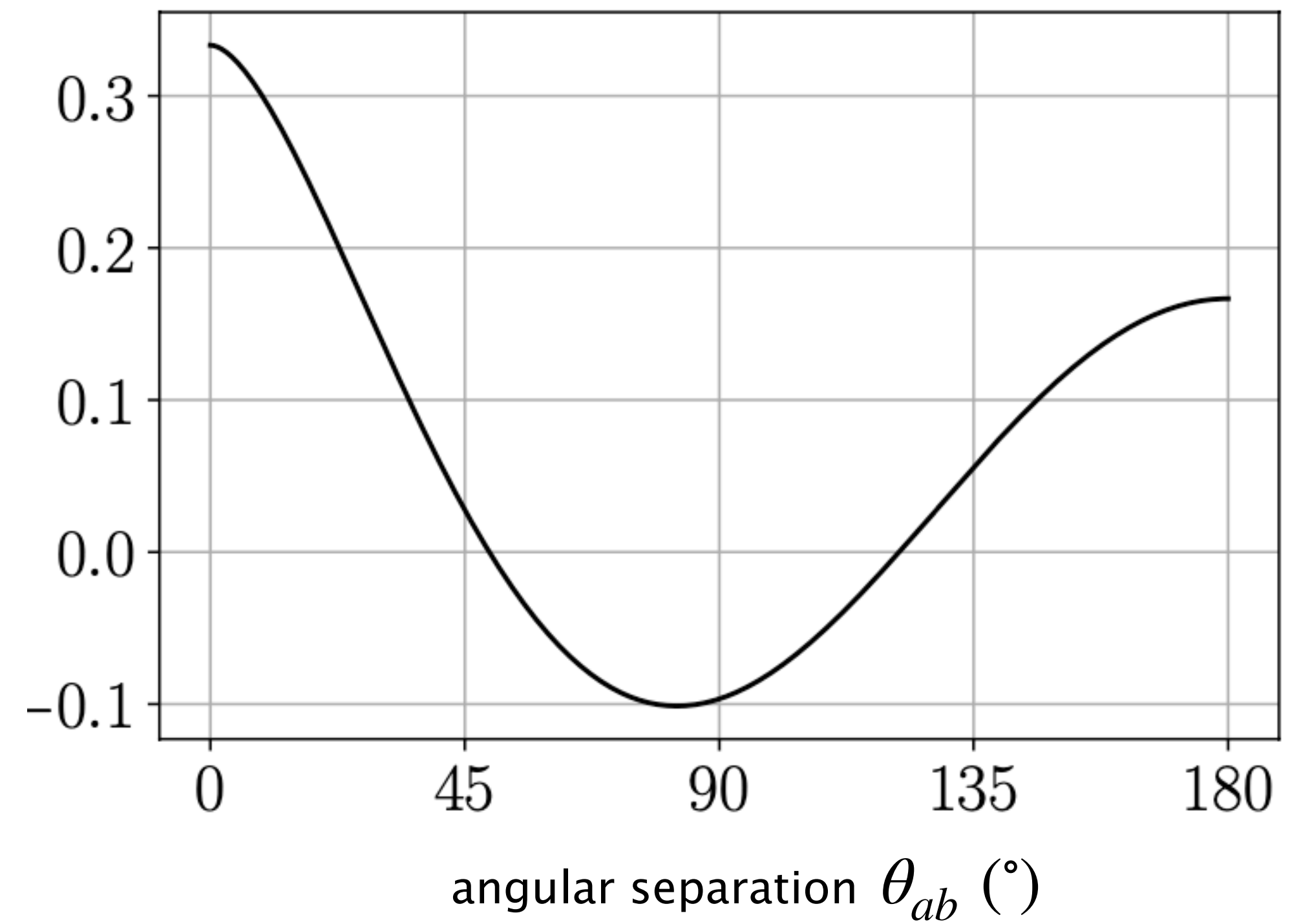
angular separation ζ_{ab} dependence



Expectation at PTAs for an isotropic, unpolarized gravitational wave background

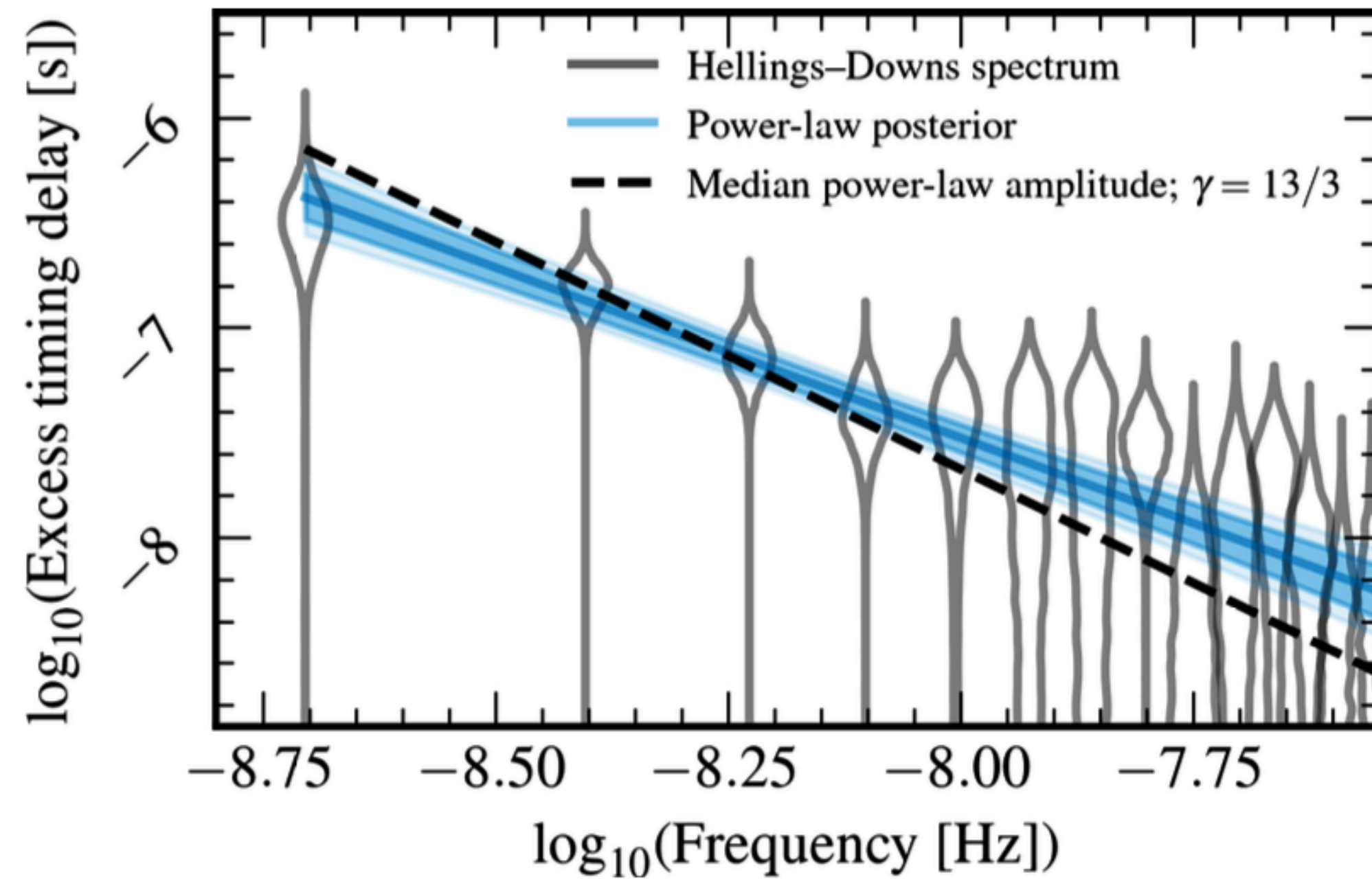
Hellings and Downs Correlations

$$\Gamma_{ab}(\zeta_{ab})$$

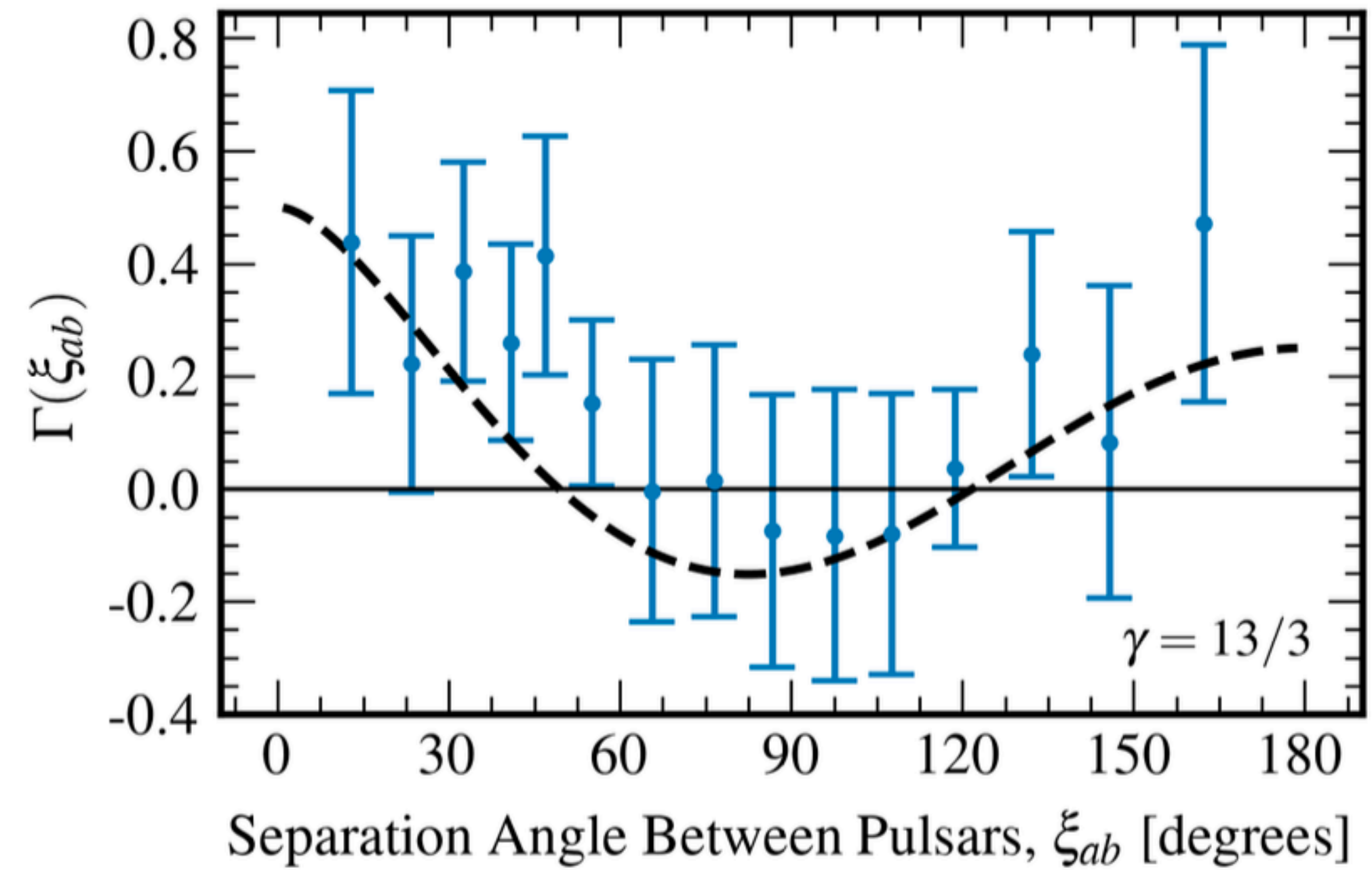


Evidence for GWB?

measured common spectrum



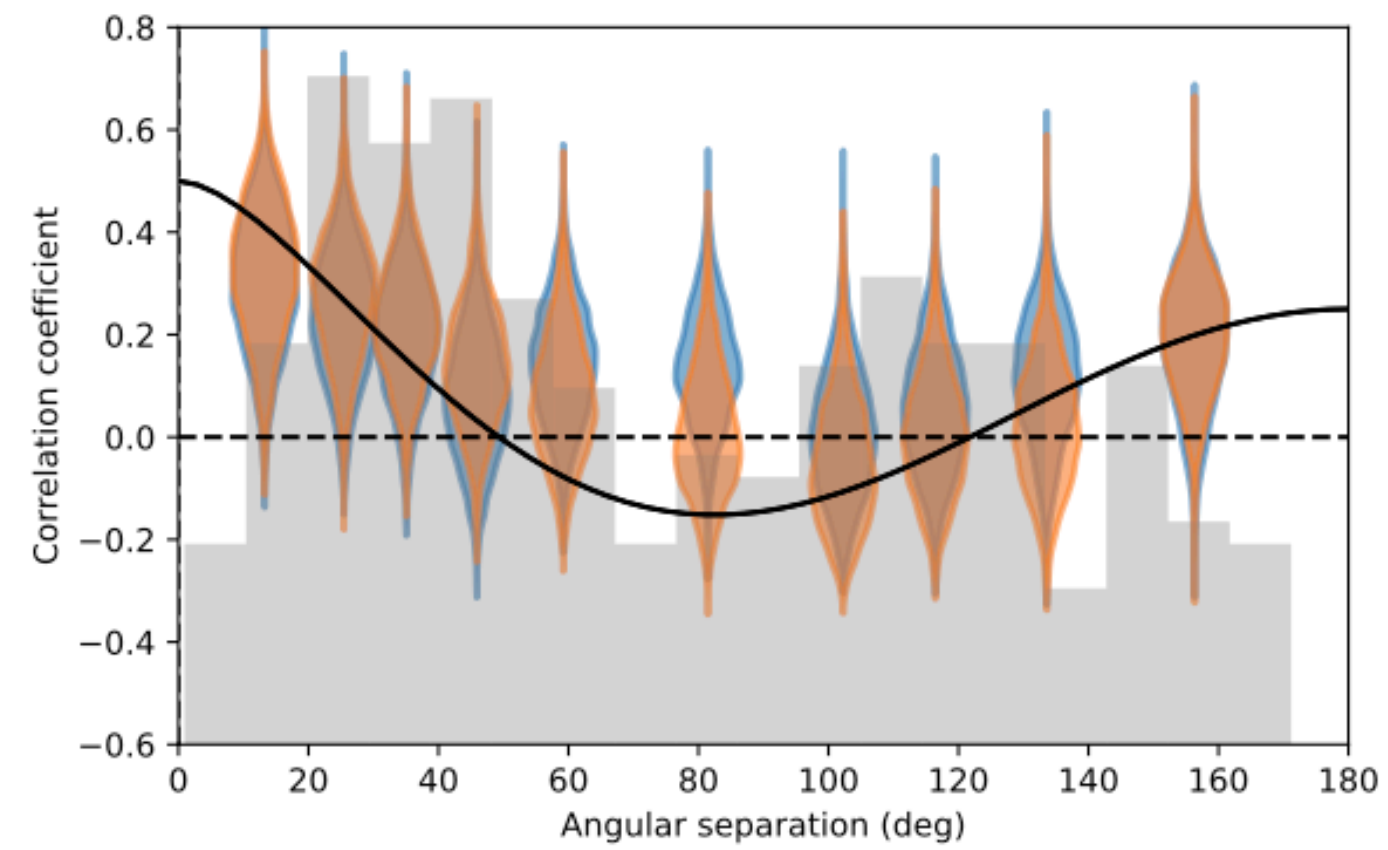
measured angular correlations



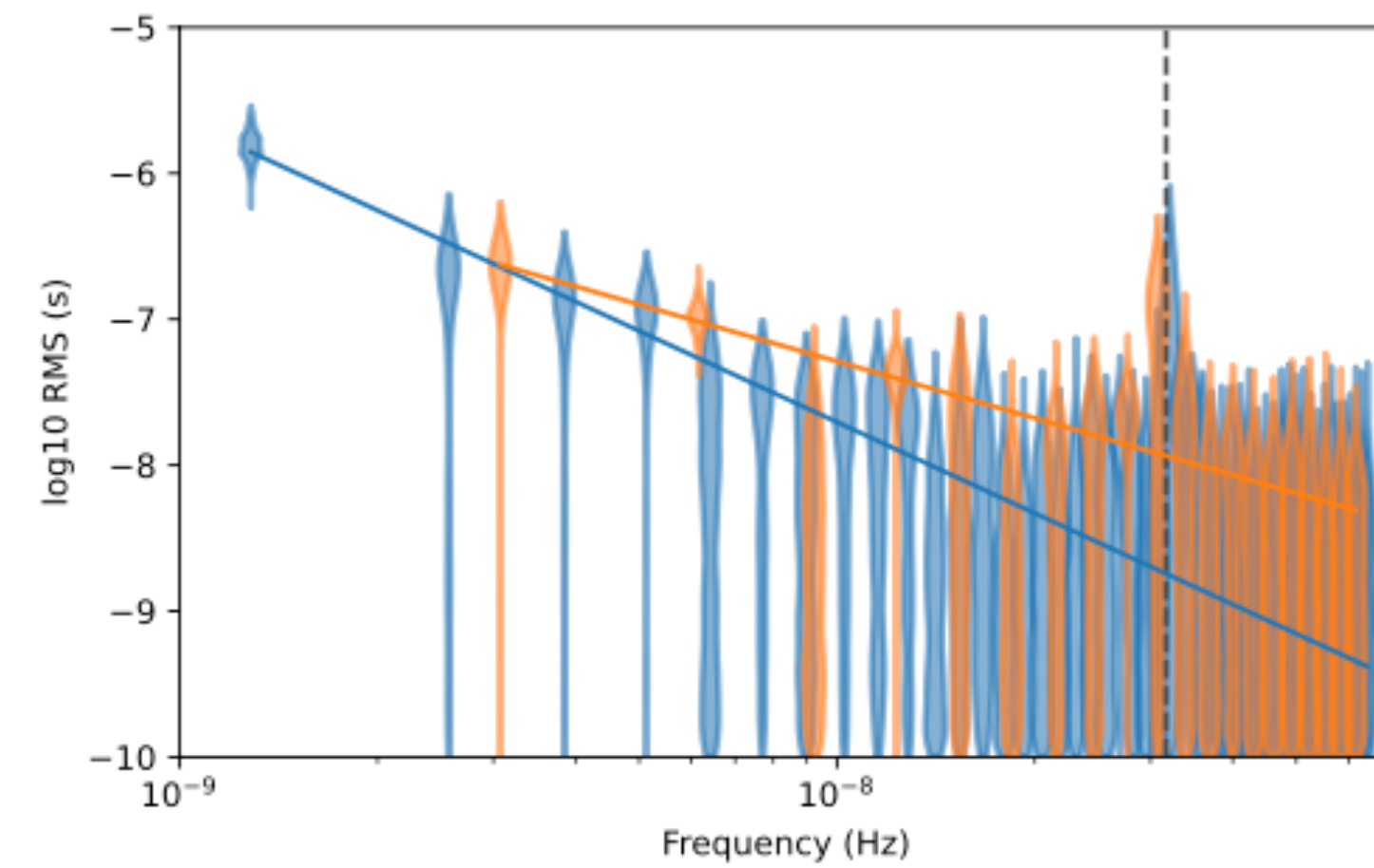
Compelling evidence of Hellings-Downs correlations with false-alarm probability of $p = 10^{-3}$ ($\sim 3 - 4\sigma$)

MORE EVIDENCE?

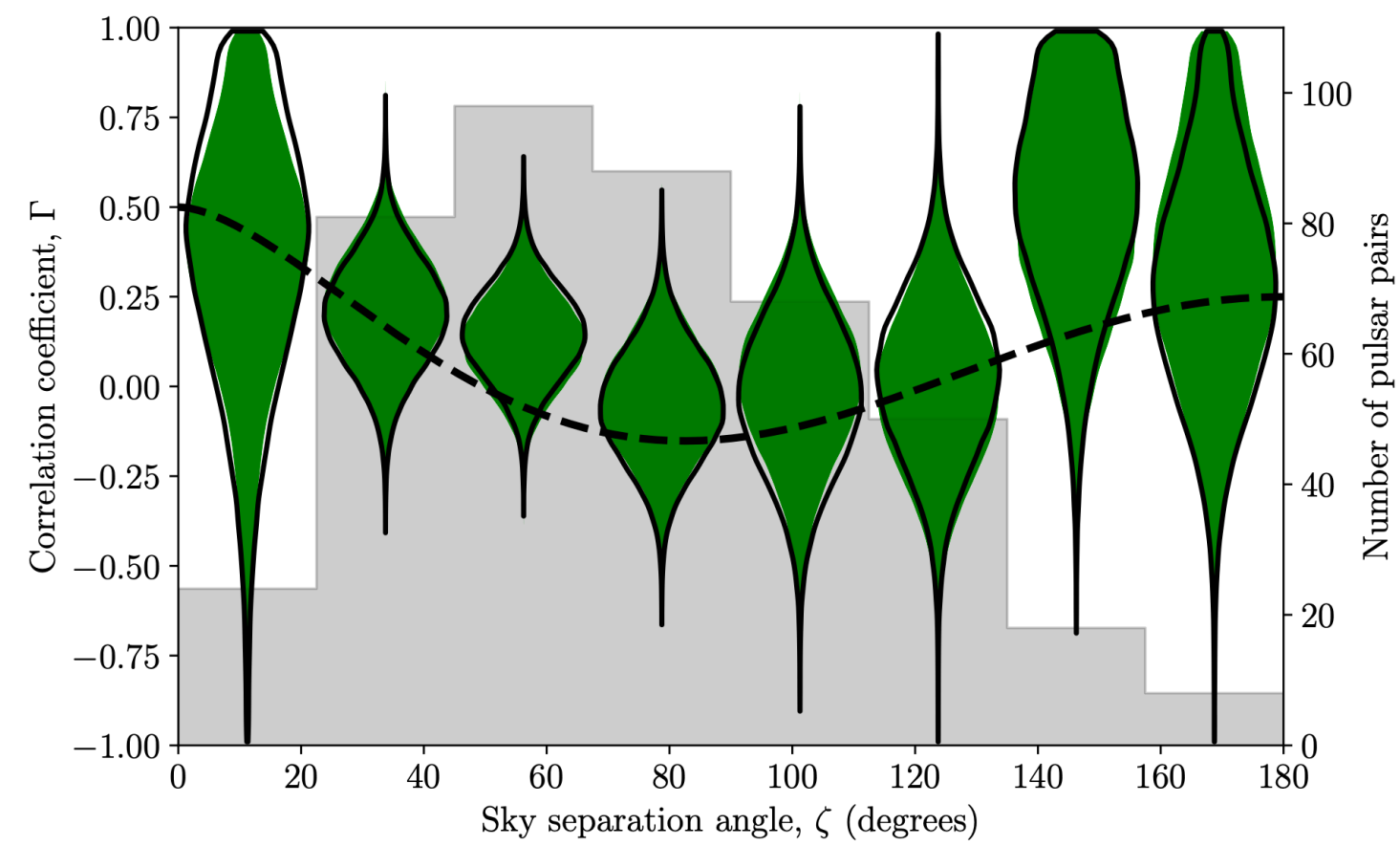
EPTA+InPTA : 25 pulsars, ~ 25 yrs data



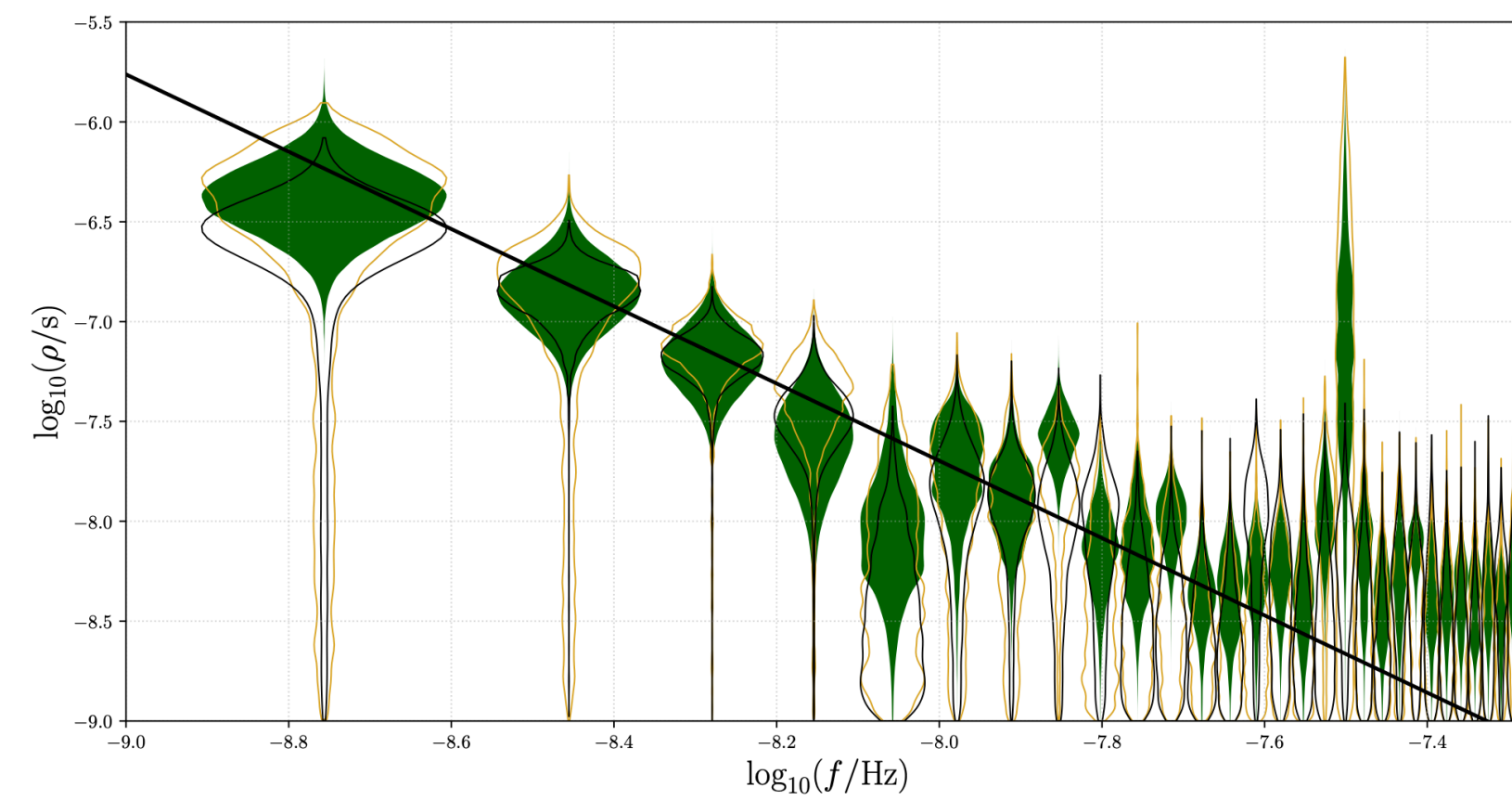
Antoniadis et al. [arxiv:2306.16214]



PPTA : 30 pulsars, ~ 18 yrs data



Reardon et al. [arxiv:2306.16215]



What is the source?

Implication #1

Credits: [Artwork by Lia Halloran](#)



Implication #1

$$h^2\Omega_{\text{GW}} = \frac{2\pi^2}{3H_0^2} A^2 \left(\frac{f}{\text{yr}^{-1}} \right)^{5-\gamma} \text{yr}^{-2}$$

GWB spectrum from inspiralling Supermassive Black Hole Binaries [SMBHB]

Implication #1

$$h^2\Omega_{\text{GW}} = \frac{2\pi^2}{3H_0^2} A^2 \left(\frac{f}{\text{yr}^{-1}} \right)^{5-\gamma} \text{yr}^{-2}$$

GWB spectrum from inspiralling SMBH binaries

Free parameters

Implication #1

$$h^2\Omega_{\text{GW}} = \frac{2\pi^2}{3H_0^2} A^2 \left(\frac{f}{\text{yr}^{-1}} \right)^{5-\gamma} \text{yr}^{-2}$$

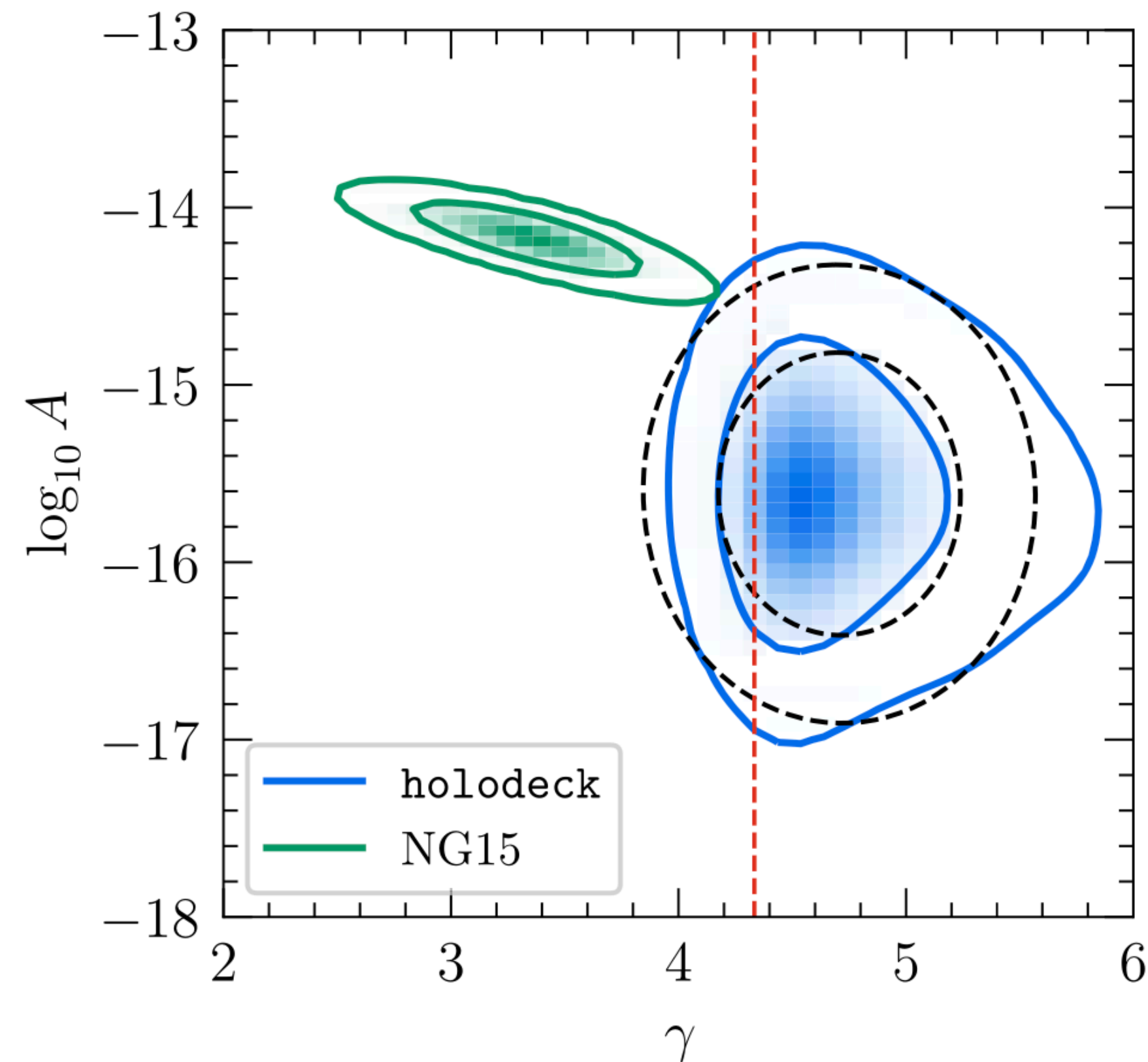
GWB spectrum from inspiralling SMBH binaries

Free parameter

Very standard choice with only GW-driven binaries, $\gamma \rightarrow 13/3$ [Phinney 2001]

Life is not that simple...

[Afzal et. al. (NANOGrav) arxiv:2306.16219]



GWB spectrum from inspir

Implication #2

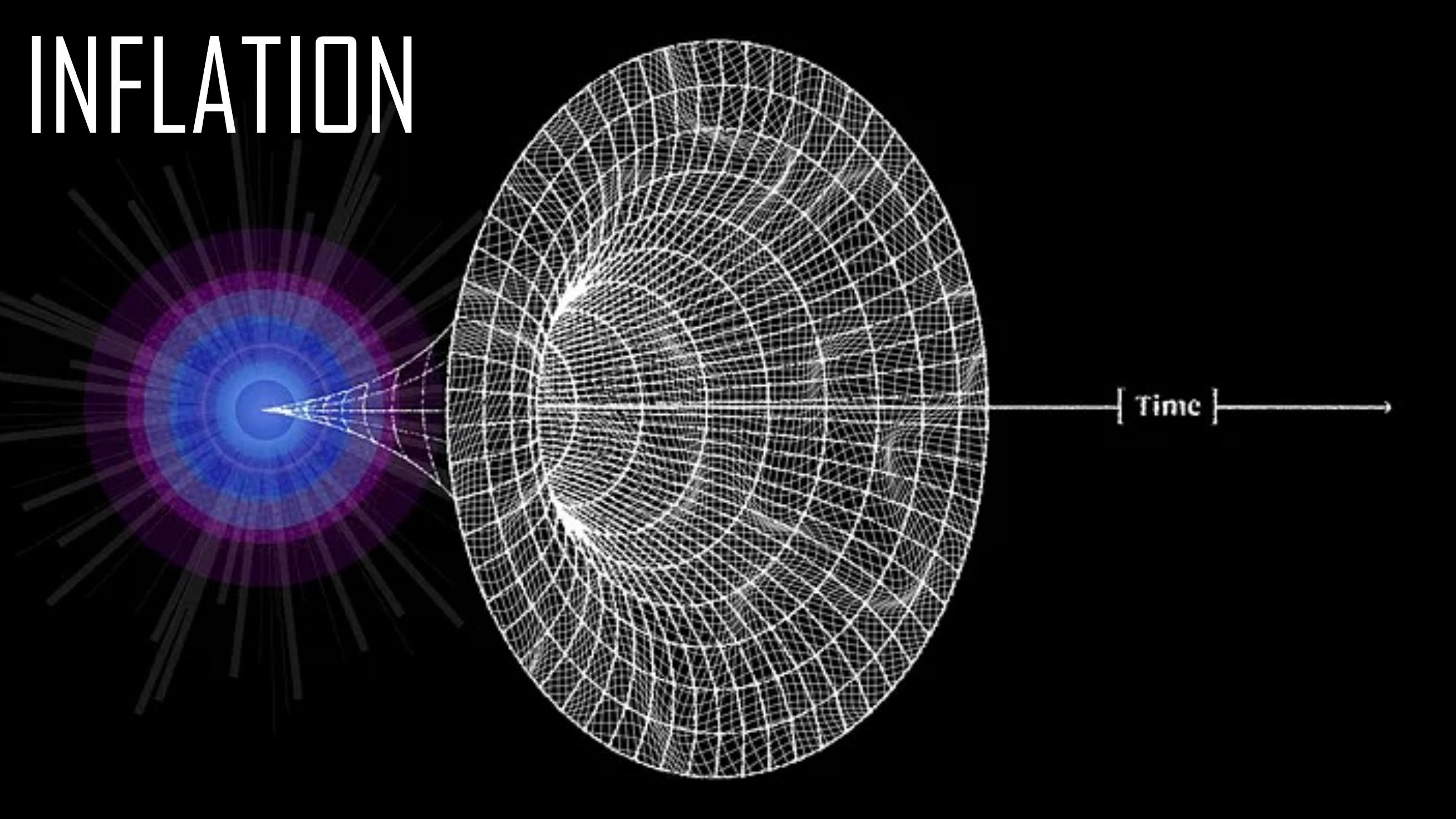
Credits: [Artwork by Lia Halloran](#)



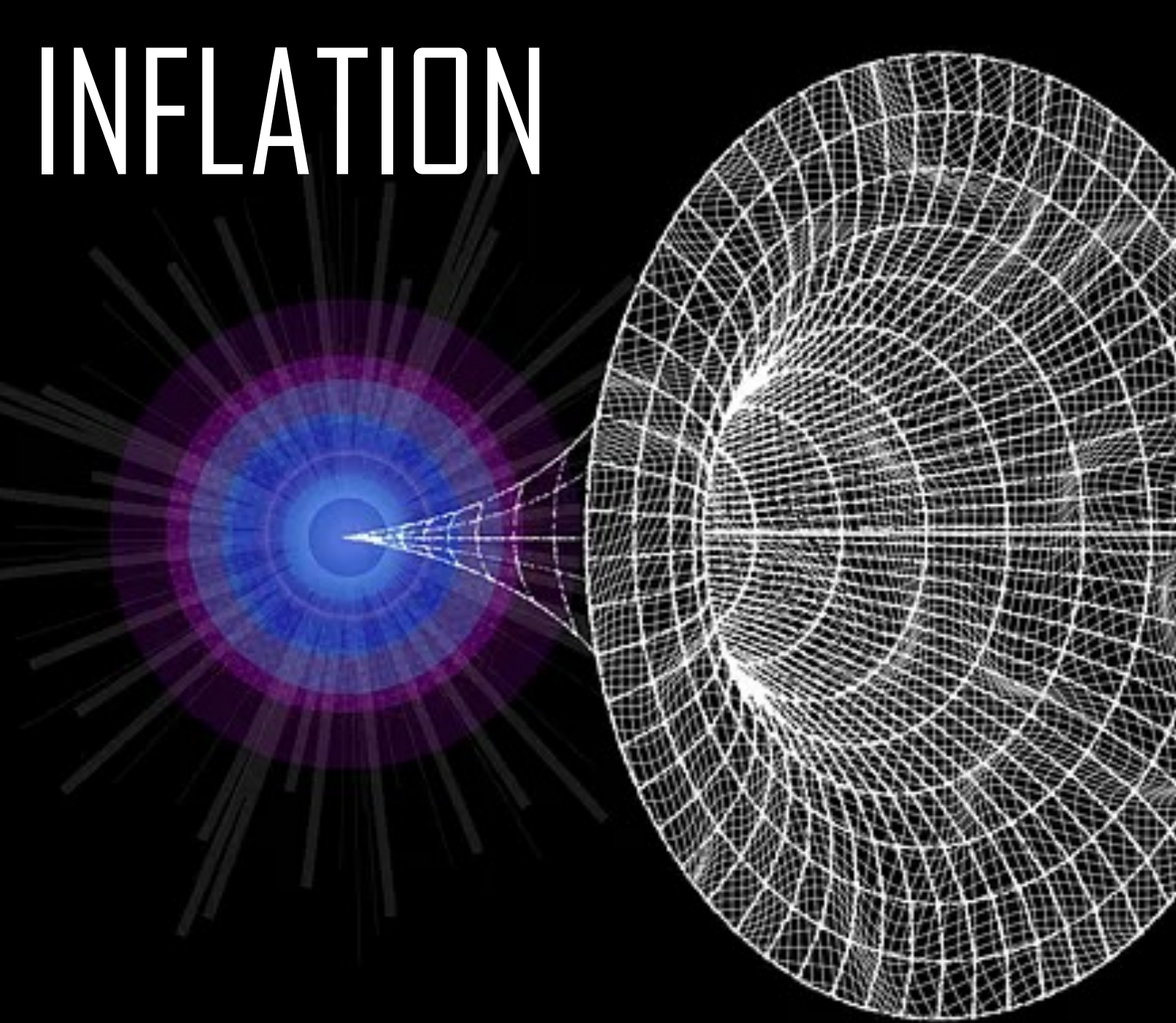
Implications #...



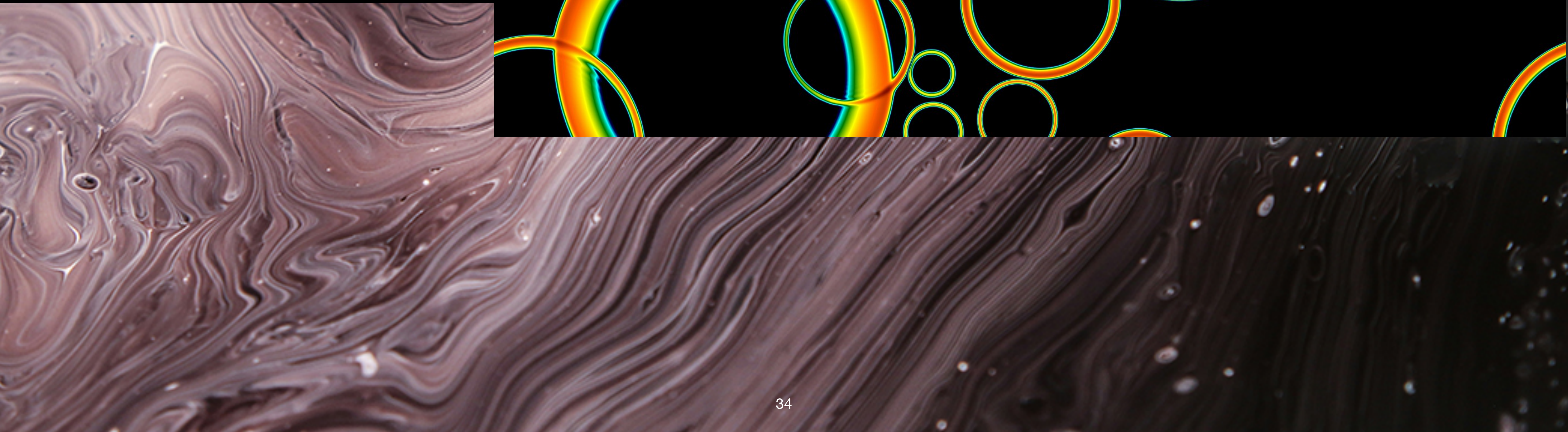
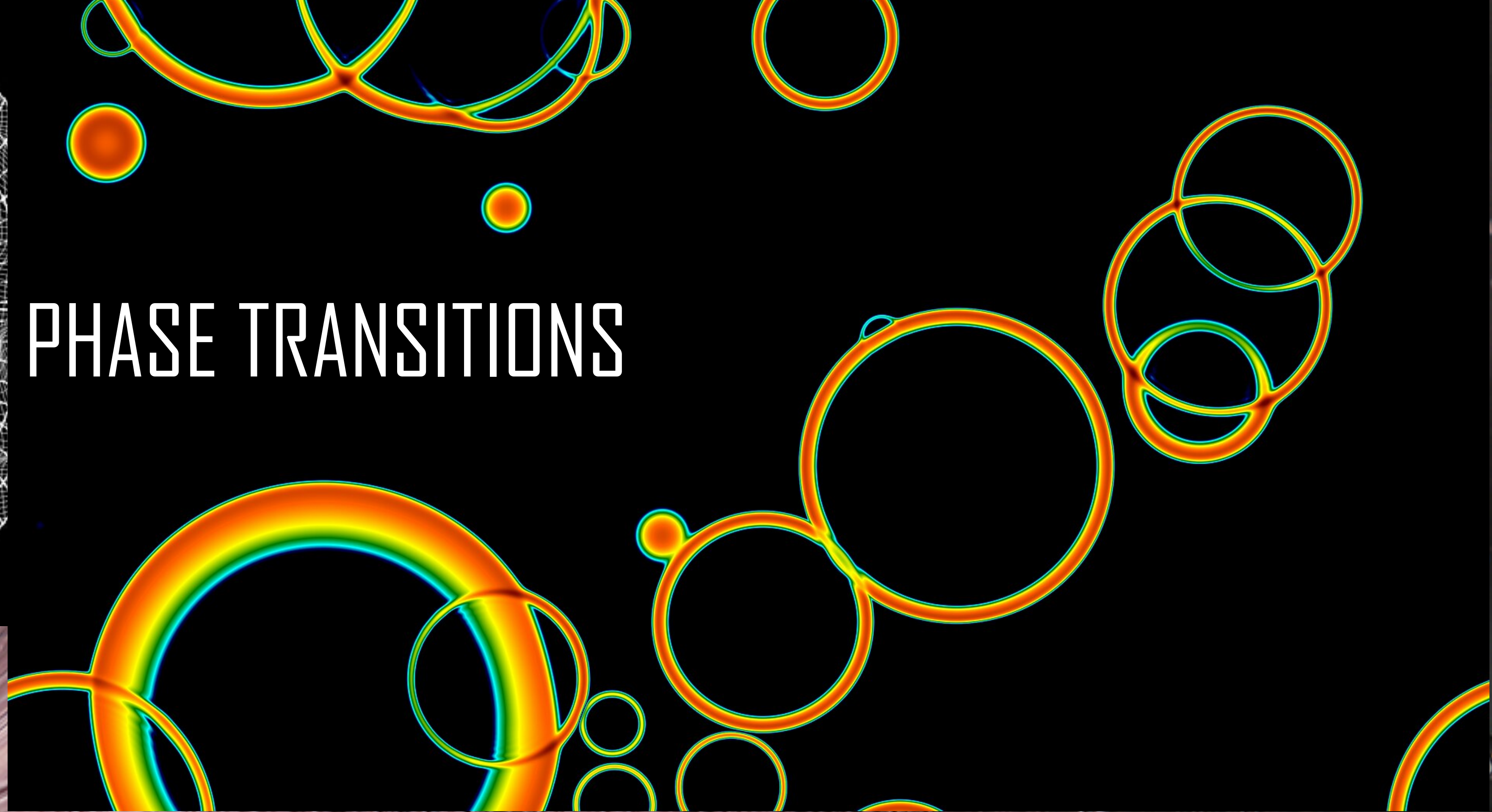
COSMIC STRINGS

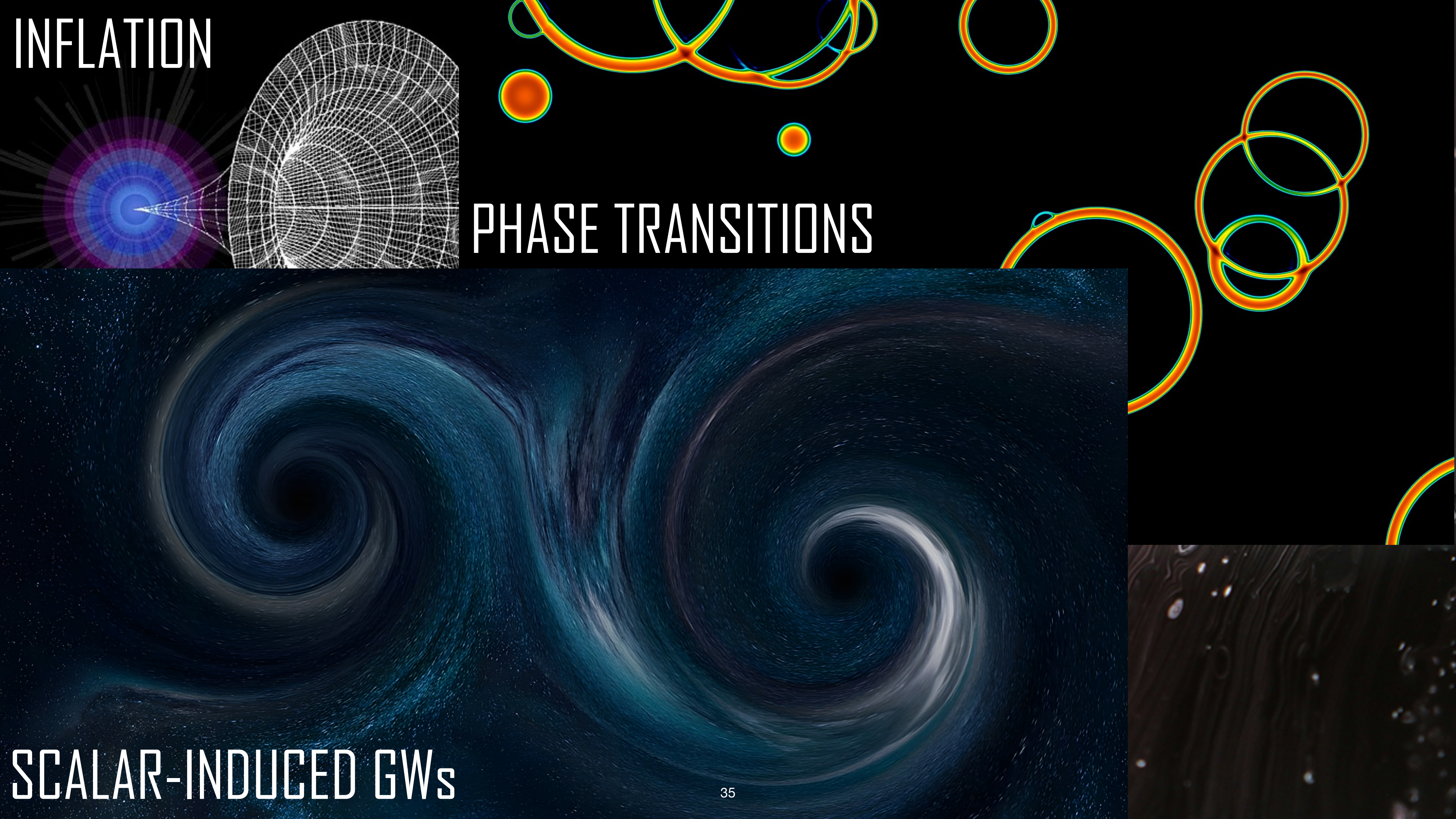


INFLATION



PHASE TRANSITIONS





INFLATION

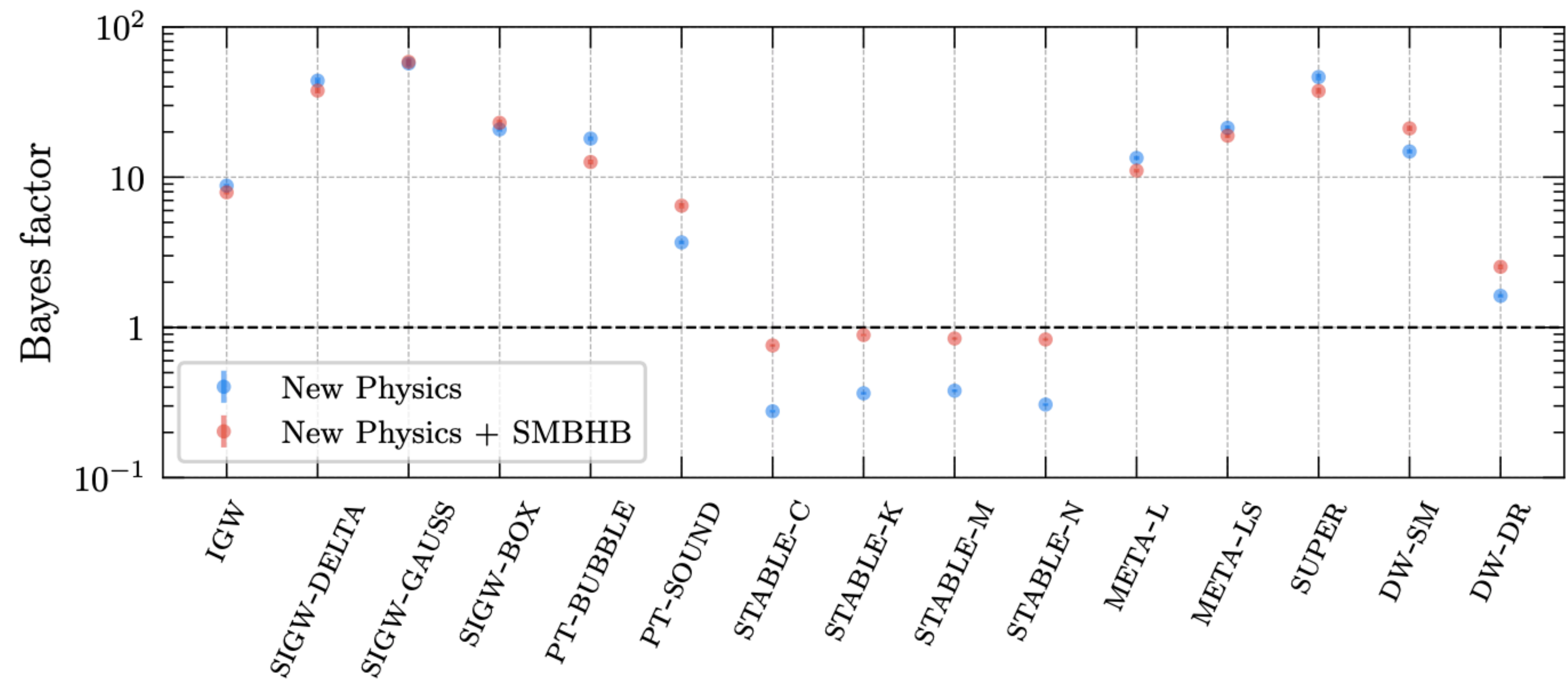
PHASE TRANSITIONS

SCALAR-INDUCED GWs

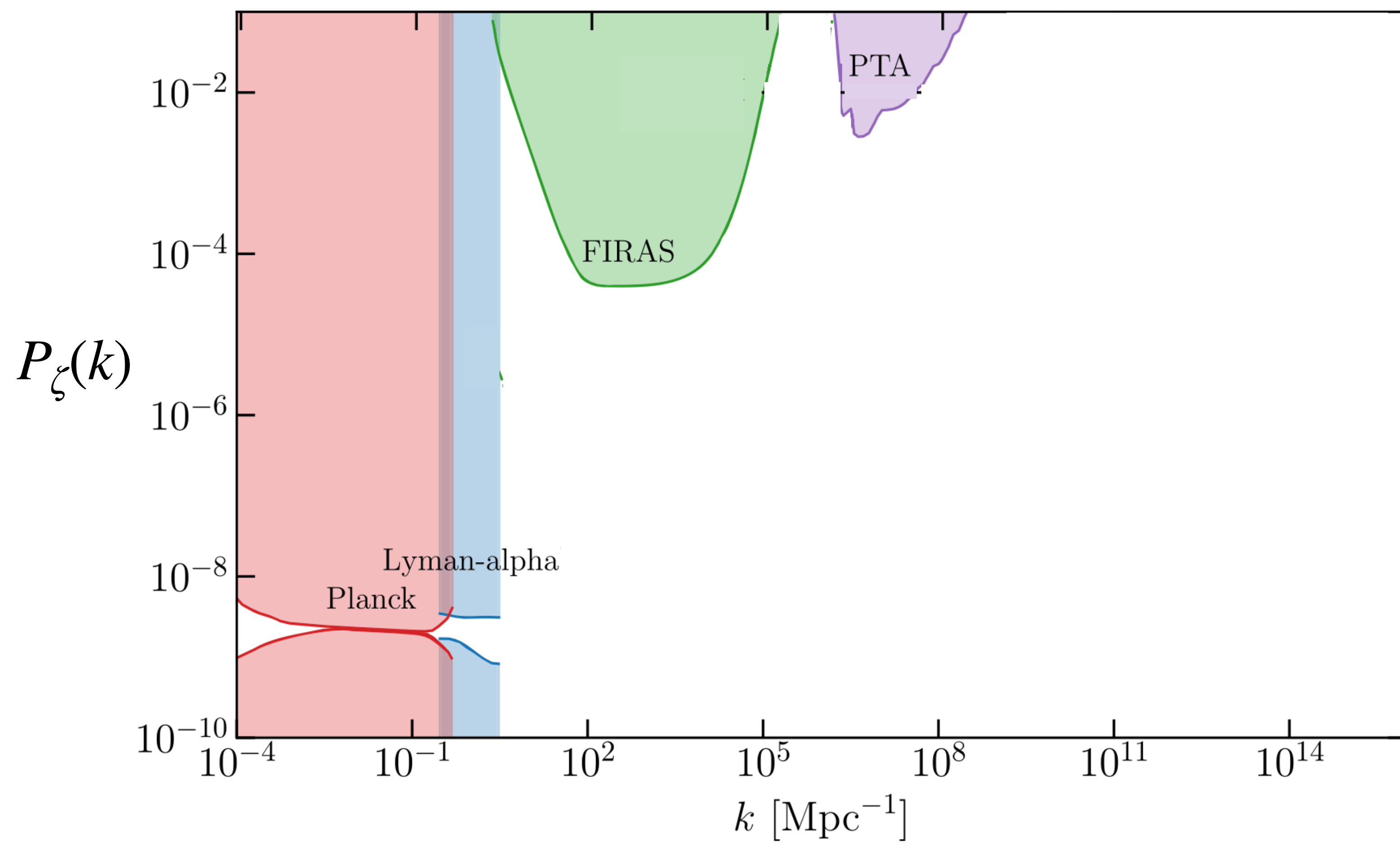
$$h^2\Omega_{\text{GW}}(f; \Theta)$$

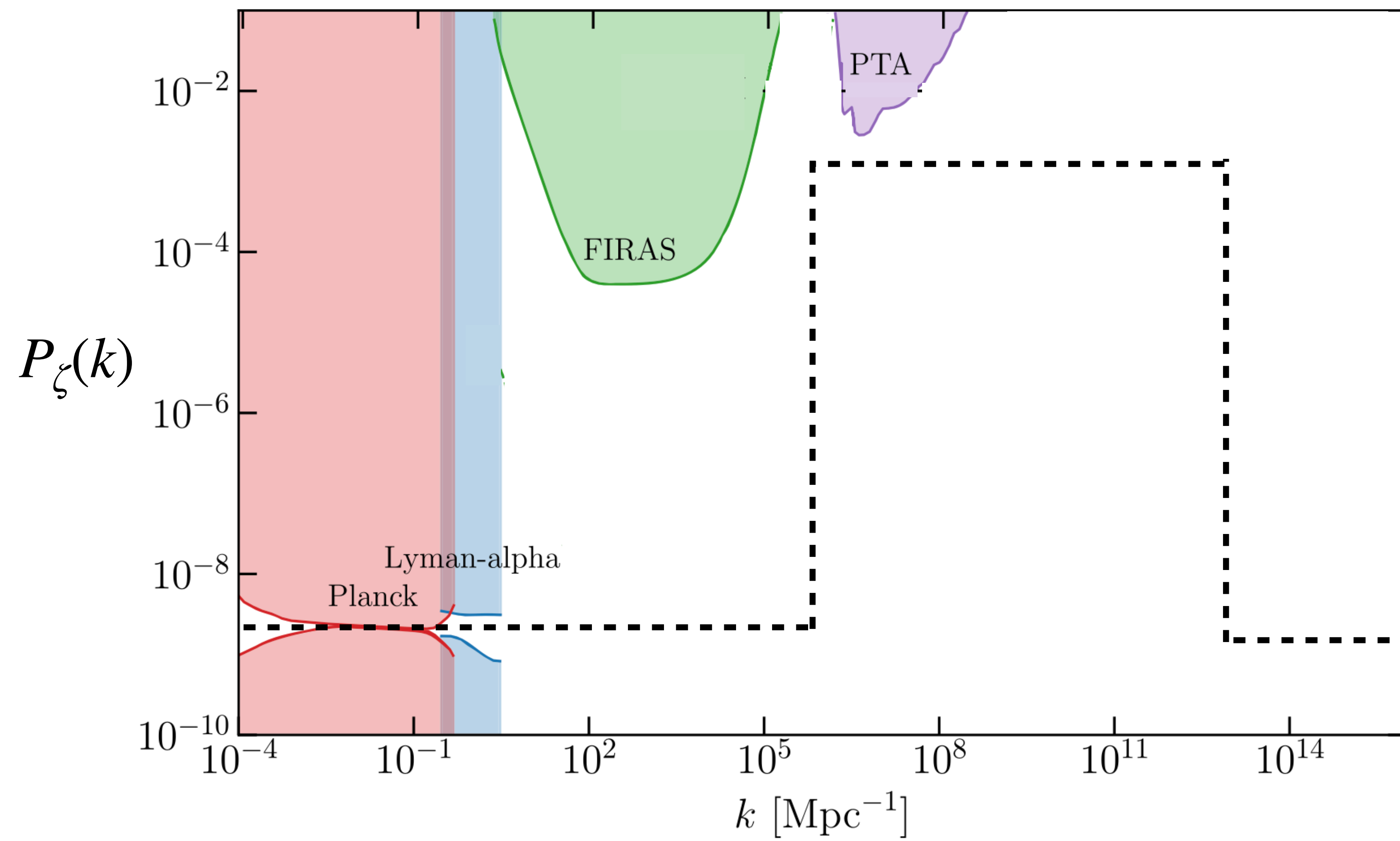
$$h^2\Omega_{\text{GW}}(f; \Theta)$$

Set of free parameters

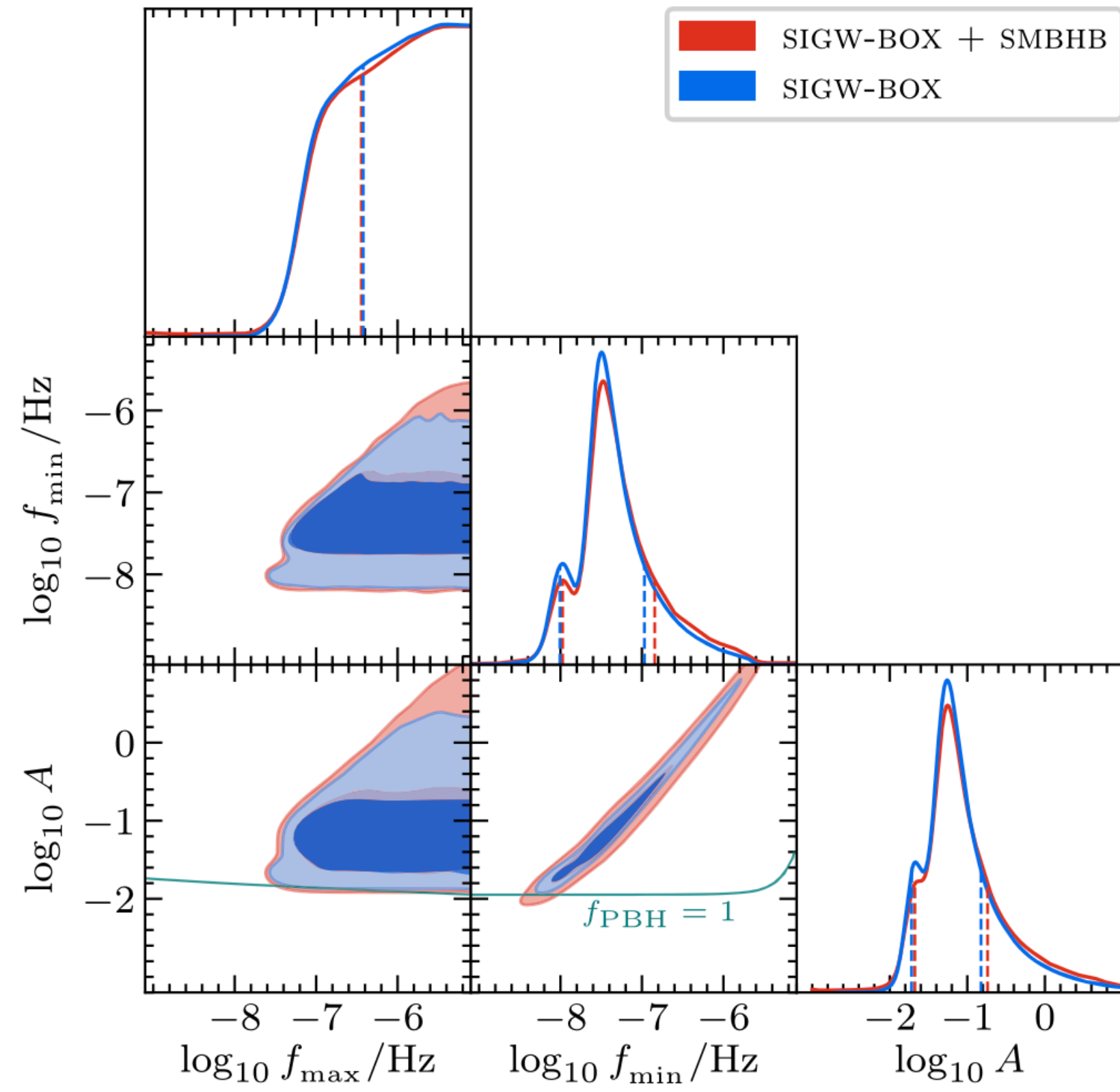


Can we constrain new physics?

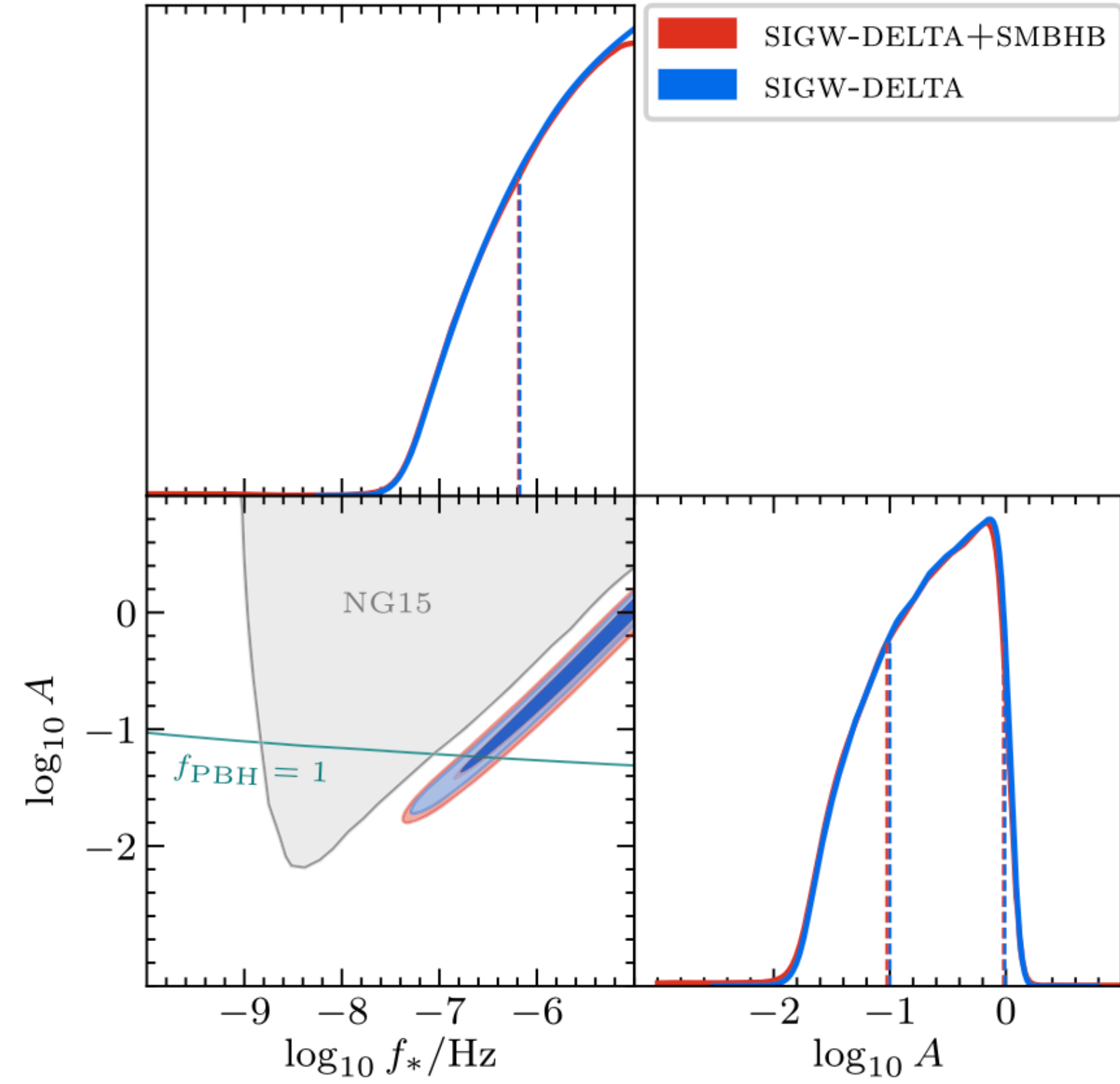




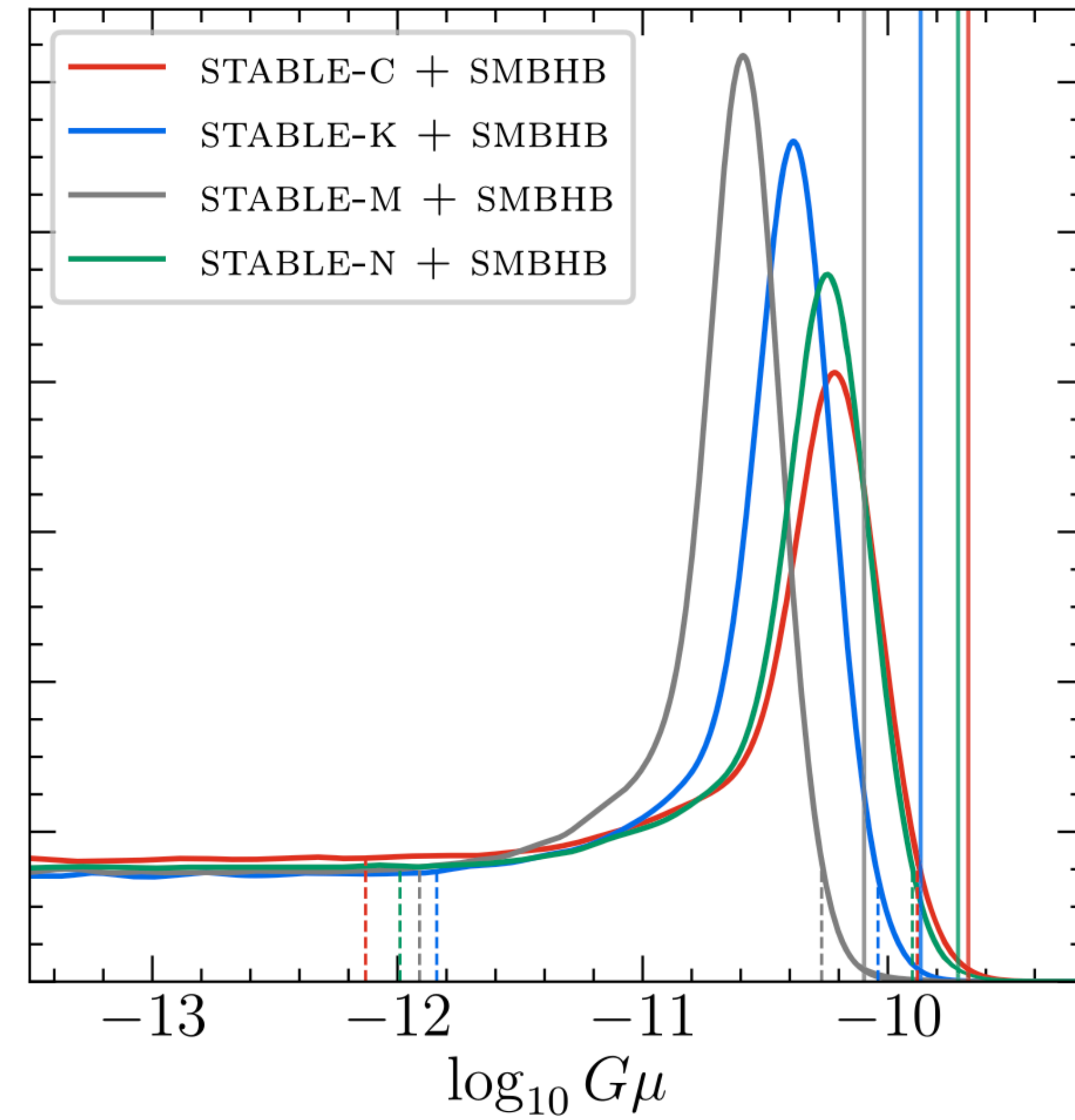
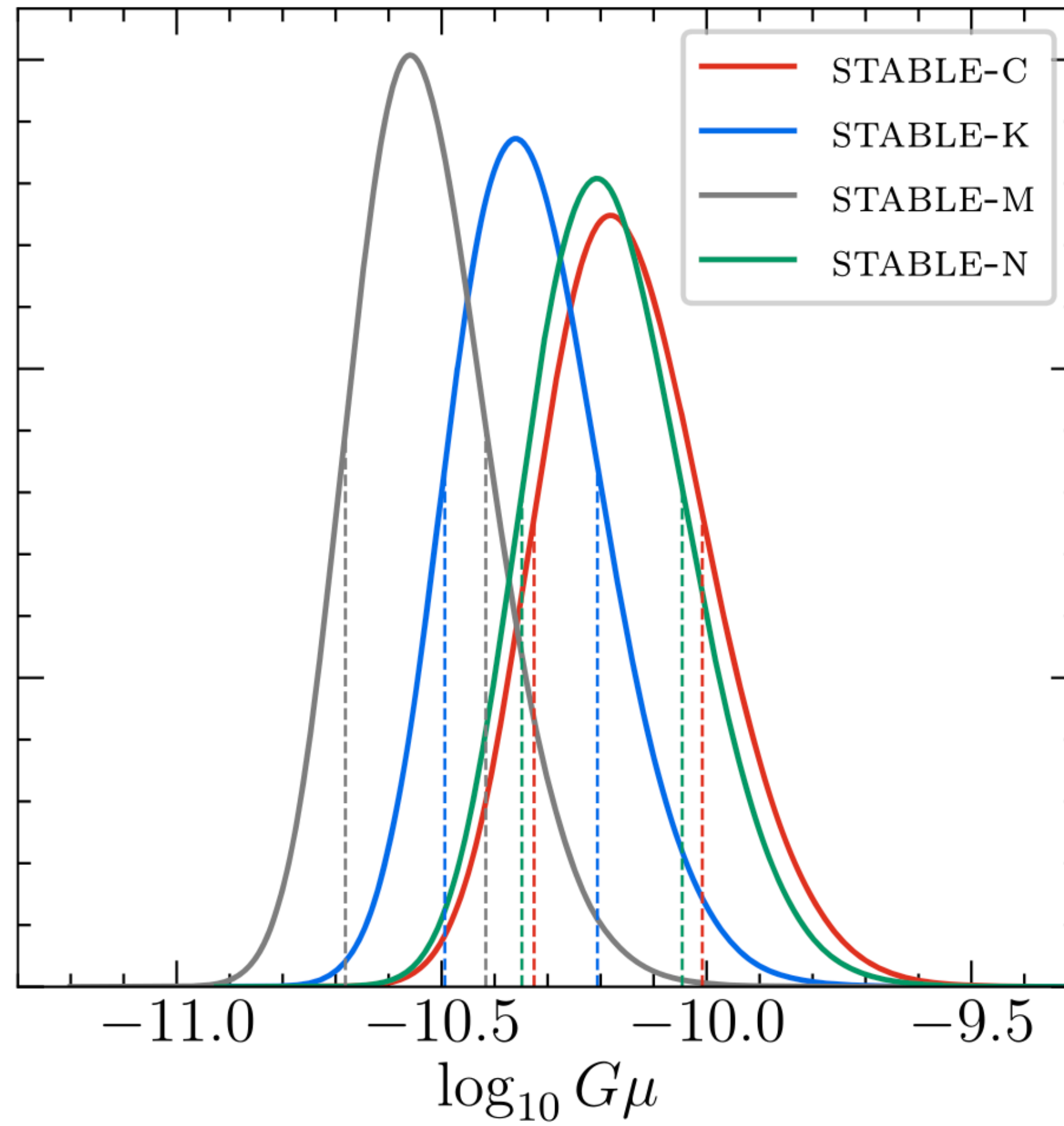
$$\mathcal{P}_R(k) = A \Theta(\ln k_{\max} - \ln k) \Theta(\ln k - \ln k_{\min}).$$



$$\mathcal{P}_R(k) = A \delta(\ln k - \ln k_*).$$



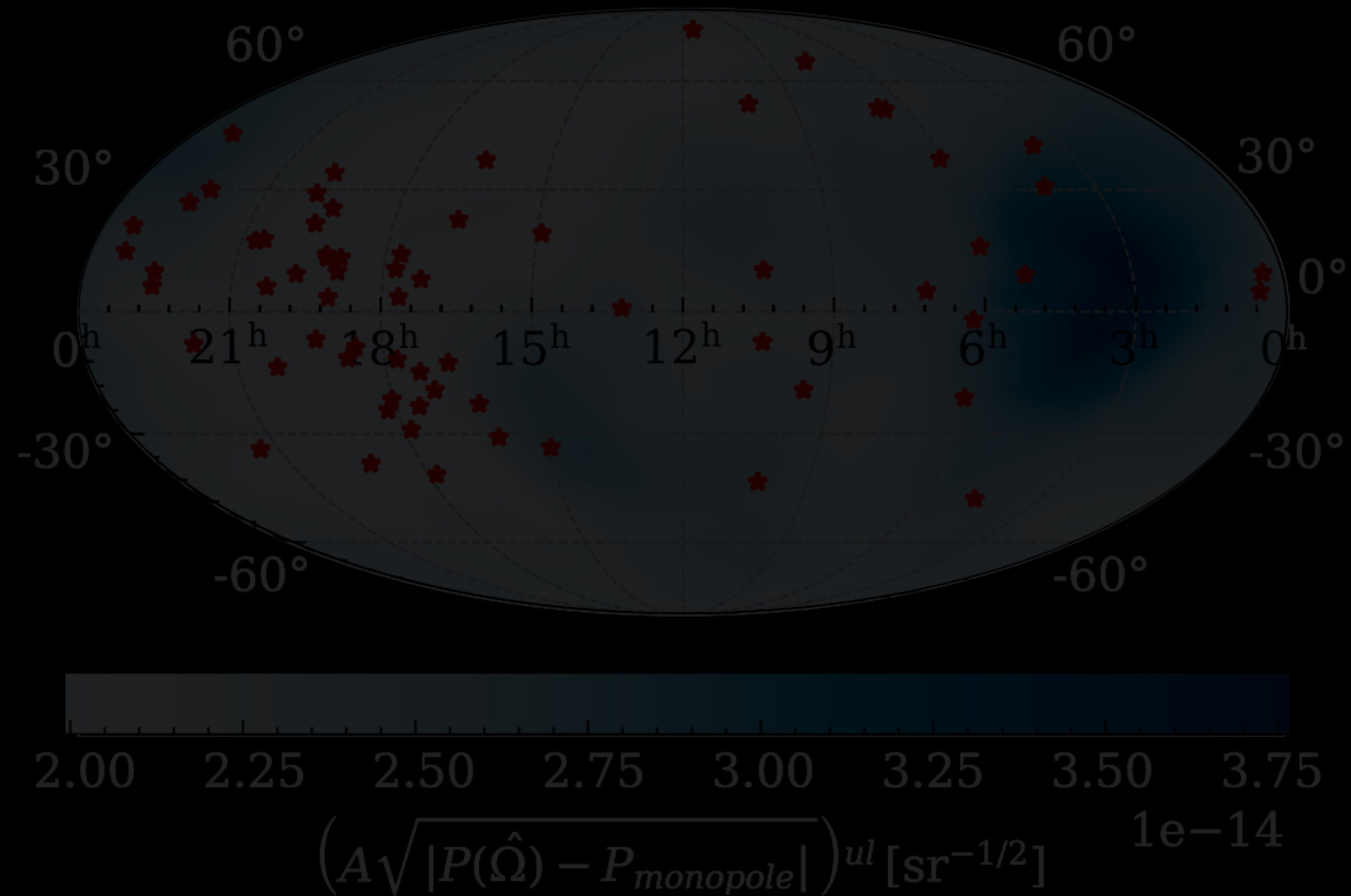
current strongest limits on string tension $G\mu$ come from PTA: $G\mu \lesssim 10^{-10}$



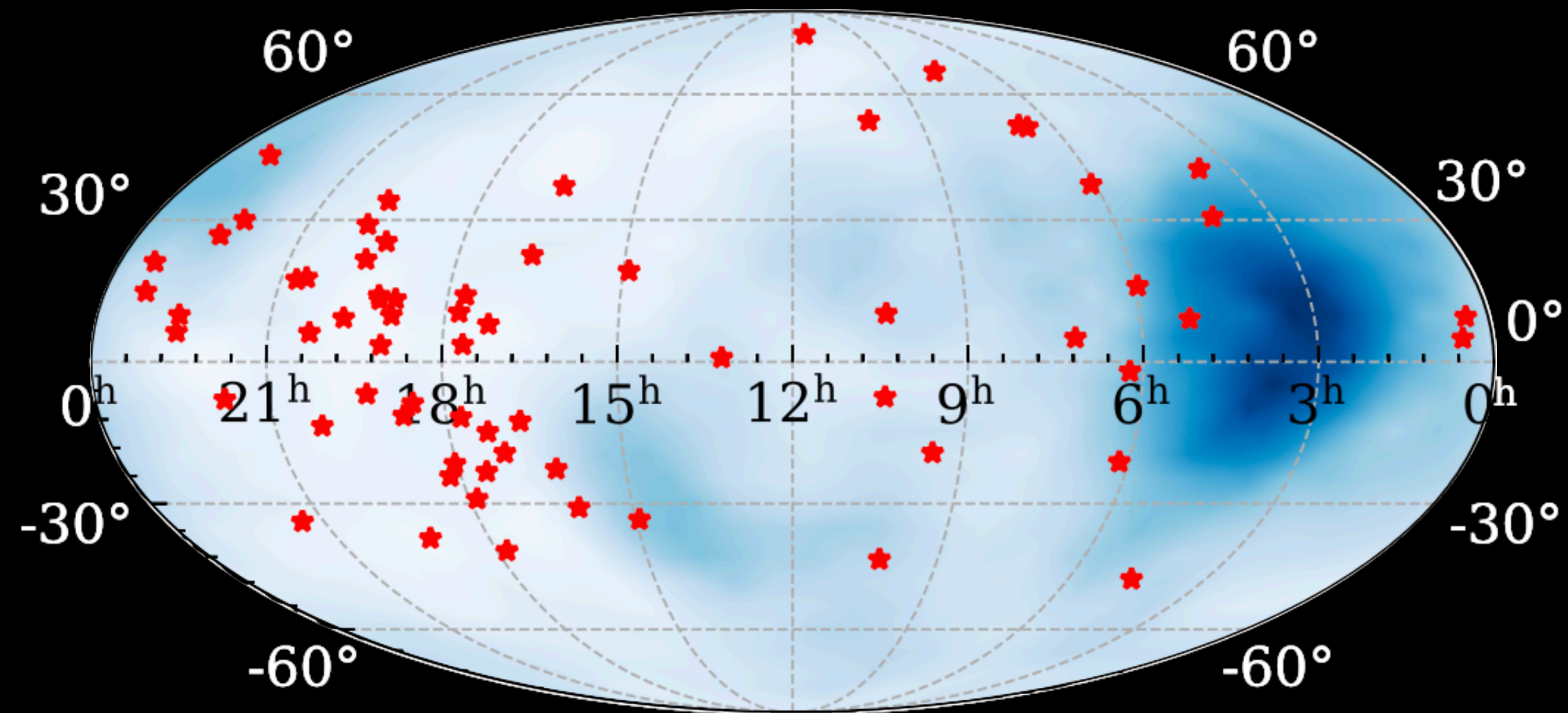
Astro vs Cosmo?

ANISOTROPIES

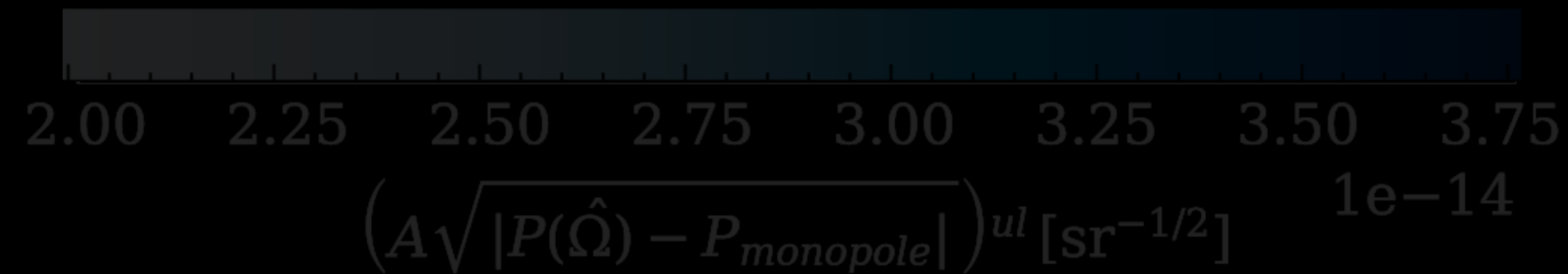
SMBHB-dominated GWB signal will lead to presence of signal anisotropy



SMBHB-dominated GWB signal will lead to presence of signal anisotropy

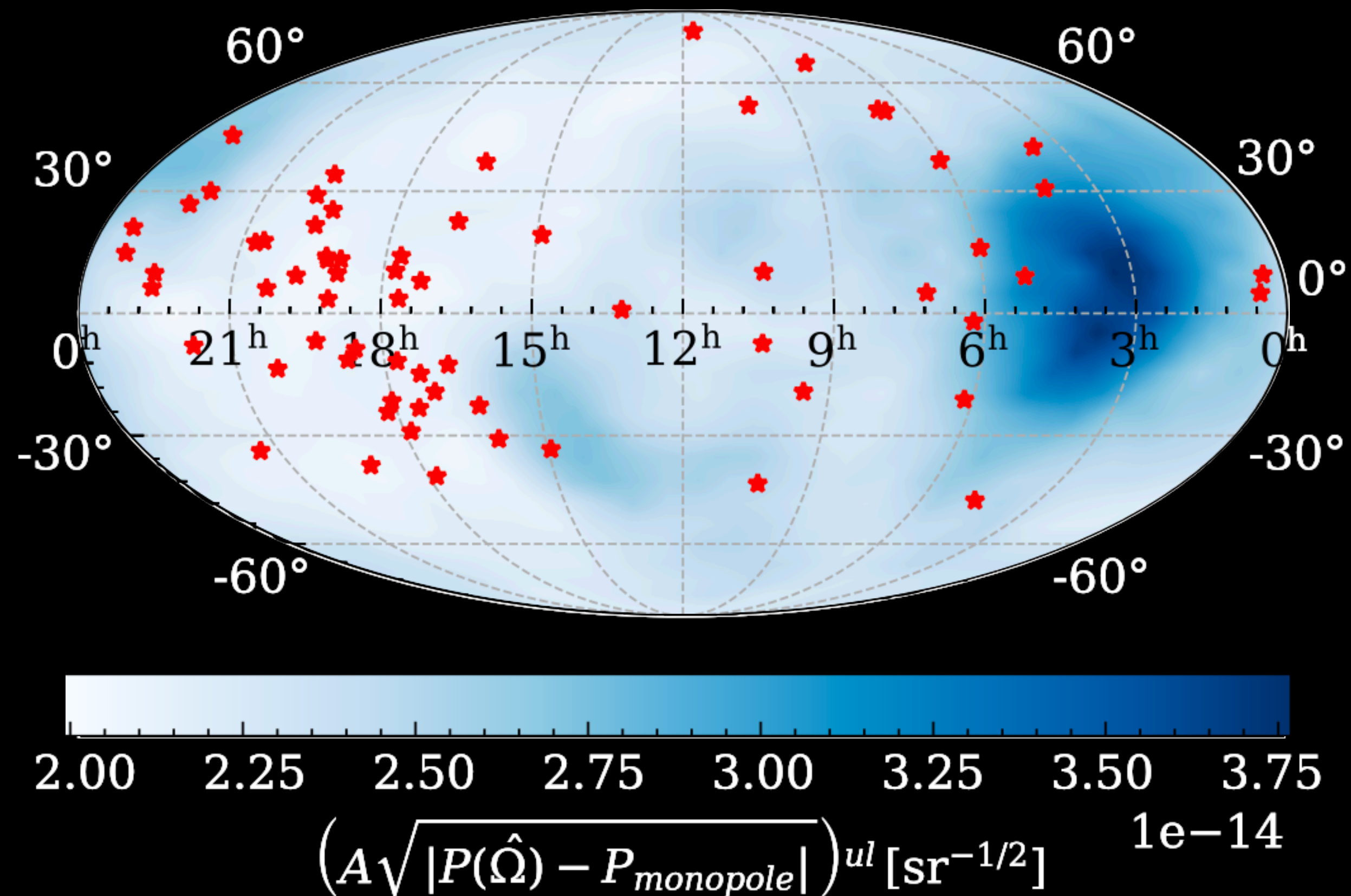


Deviations from isotropic GWB
in terms of characteristic
strain per steradian^{1/2}



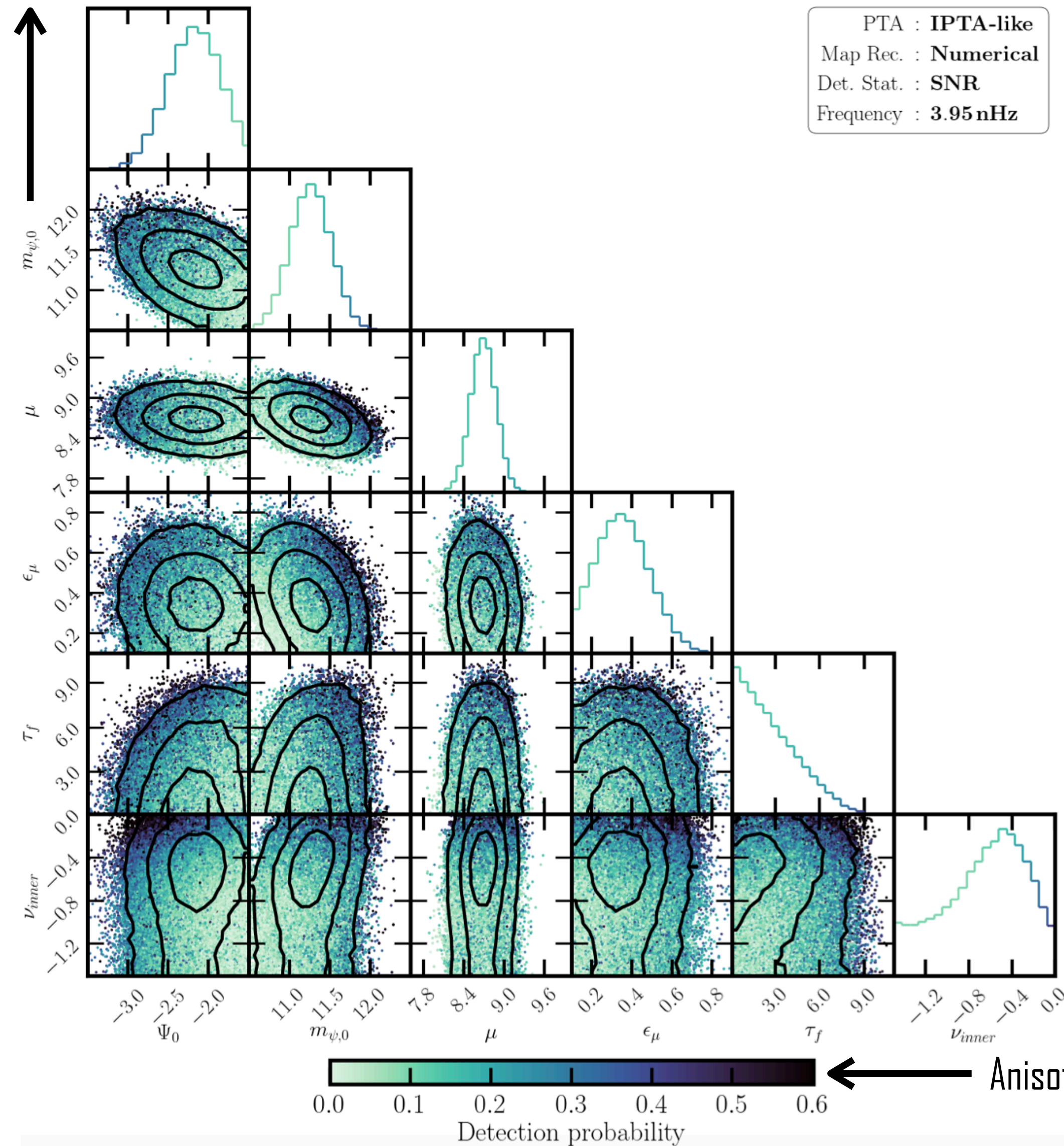
ANISOTROPIES

SMBHB-dominated GWB signal will lead to presence of signal anisotropy



No significant detection of anisotropies in the 15-yr NANOGrav dataset!

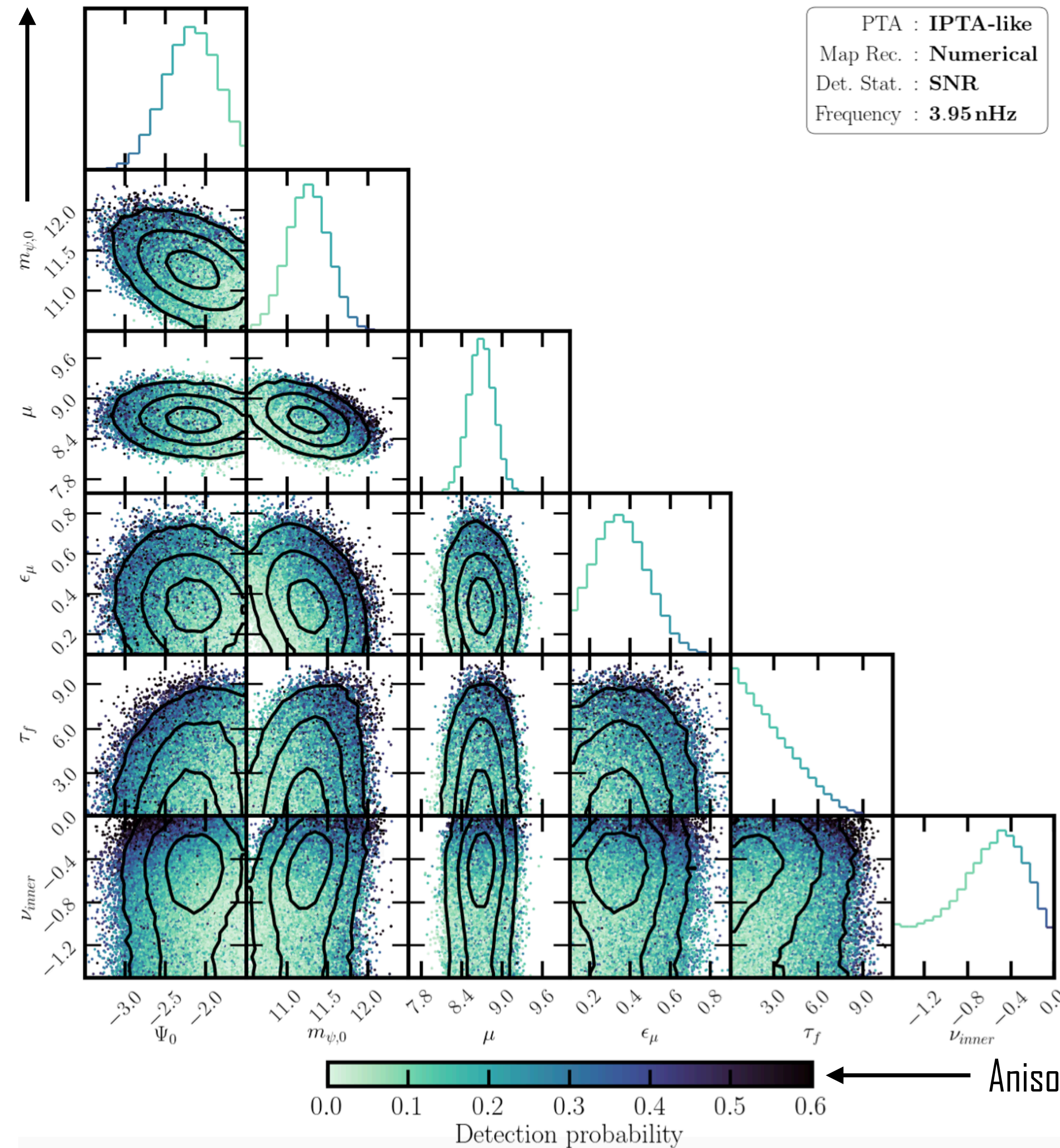
SMBHB population
parameters explaining GWB



$$\text{IPTA} = \text{NANOGrav} + \text{EPTA} + \text{InPTA} + \text{PPTA} + \text{MeerKAT}$$

Will have **improved sensitivity** to anisotropies for SMBH-generated GWB

SMBHB population
parameters explaining GWB



$$\text{IPTA} = \text{NANOGrav} + \text{EPTA} + \text{InPTA} + \text{PPTA} + \text{MeerKAT}$$

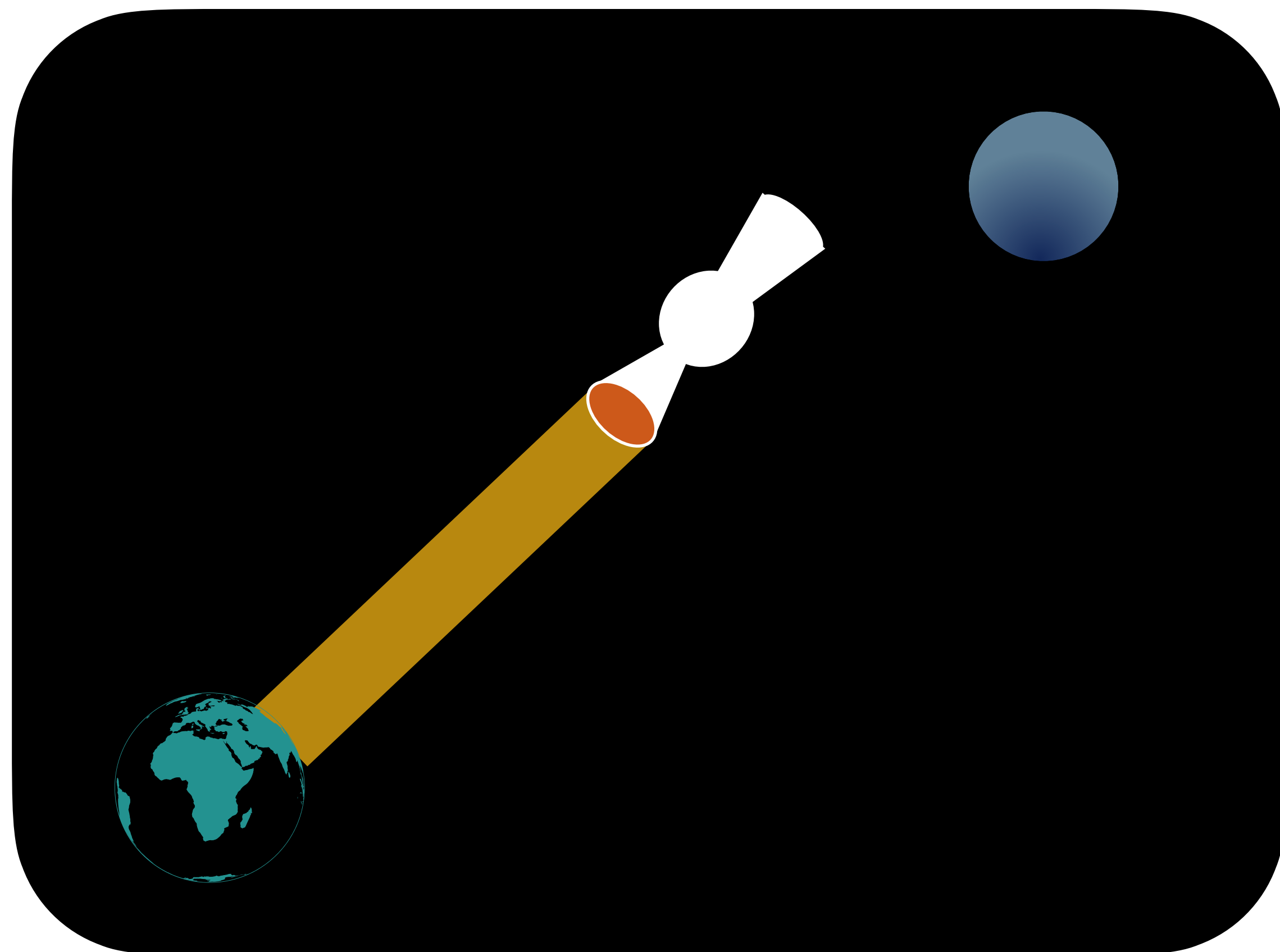
Will have **improved sensitivity** to anisotropies for SMBH-generated GWB

If still no anisotropy? Even with improved sensitivity?

Exclude SMBHB interpretation?

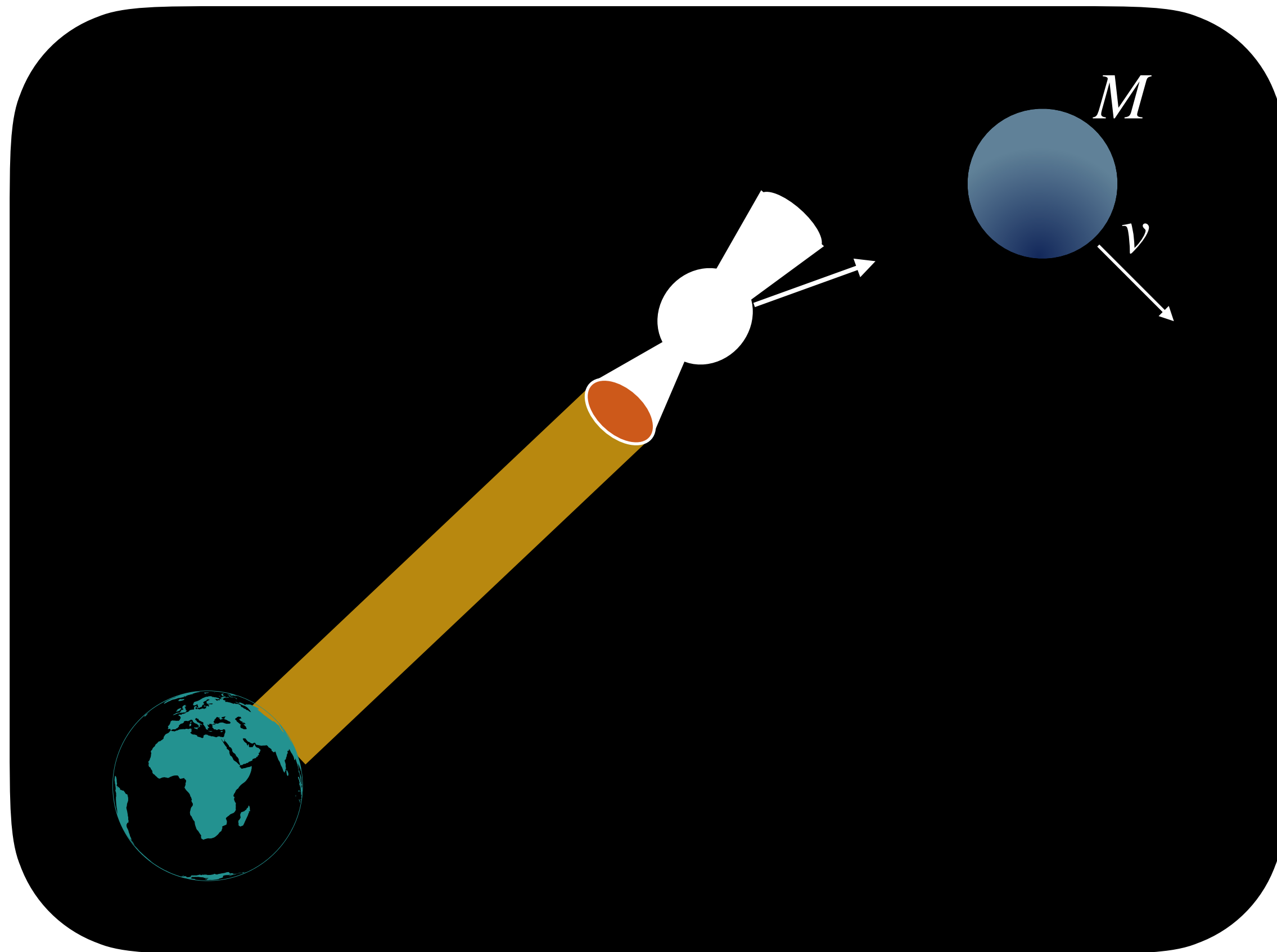
What more with PTAs?

Dark matter searches?



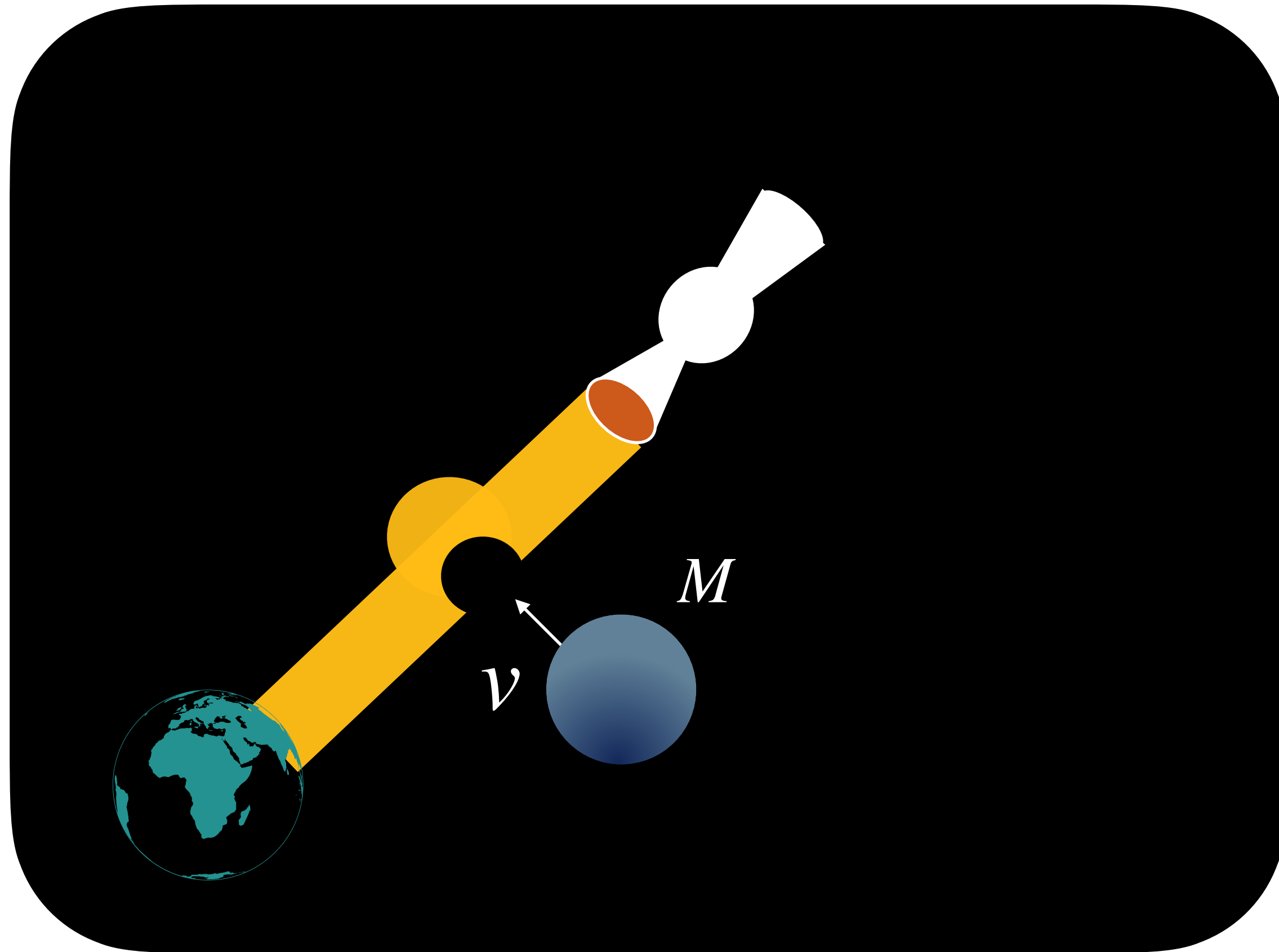
DOPPLER EFFECT

passing Primordial Black hole (PBH) will **pull the pulsar** due to gravitational acceleration, leading to a phase shift in pulse



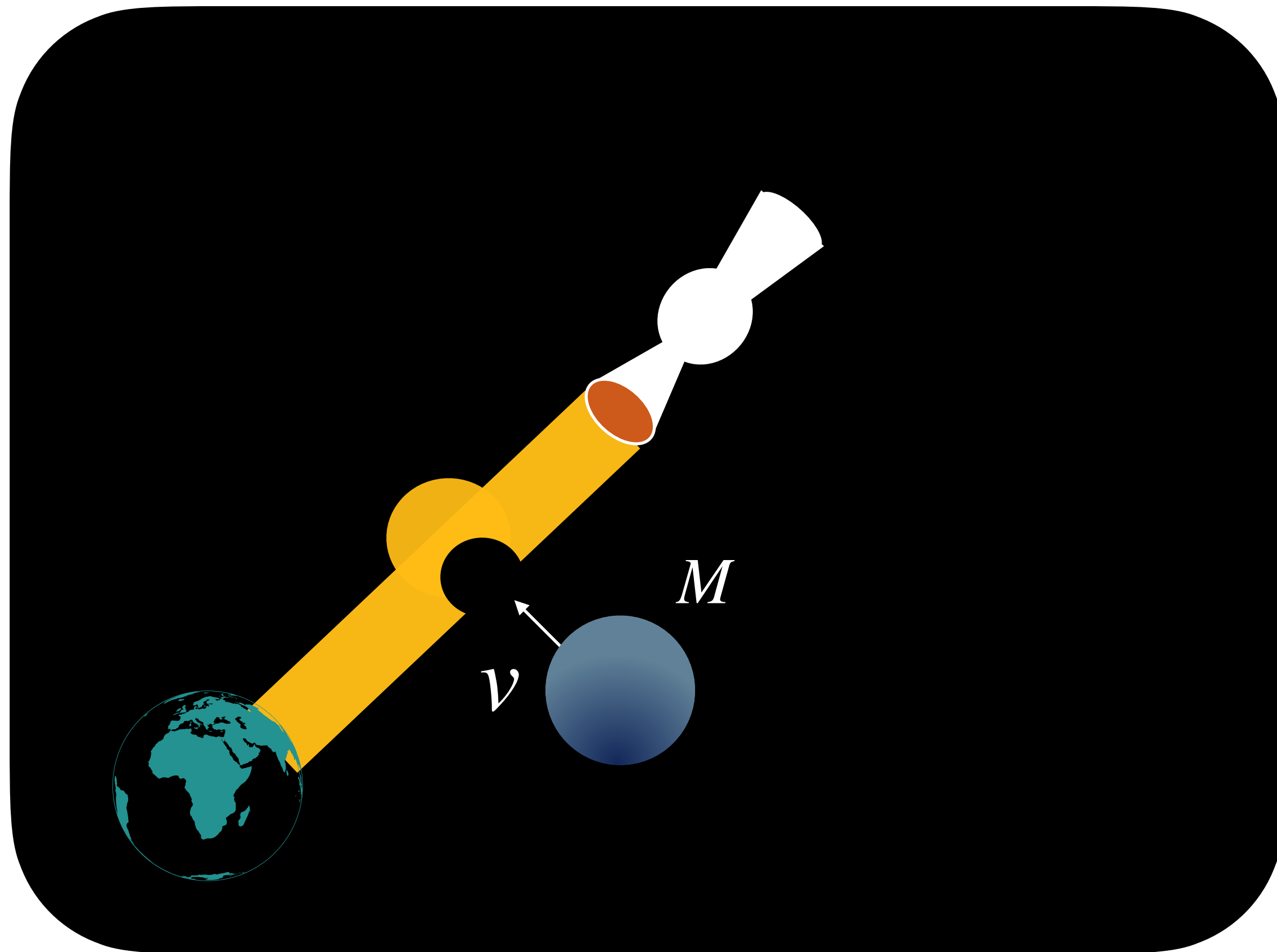
SHAPIRO TIME DELAY

transiting PBH will change light travel time due to its gravitational potential



SHAPIRO TIME DELAY

transiting PBH will change light travel time due to its gravitational potential



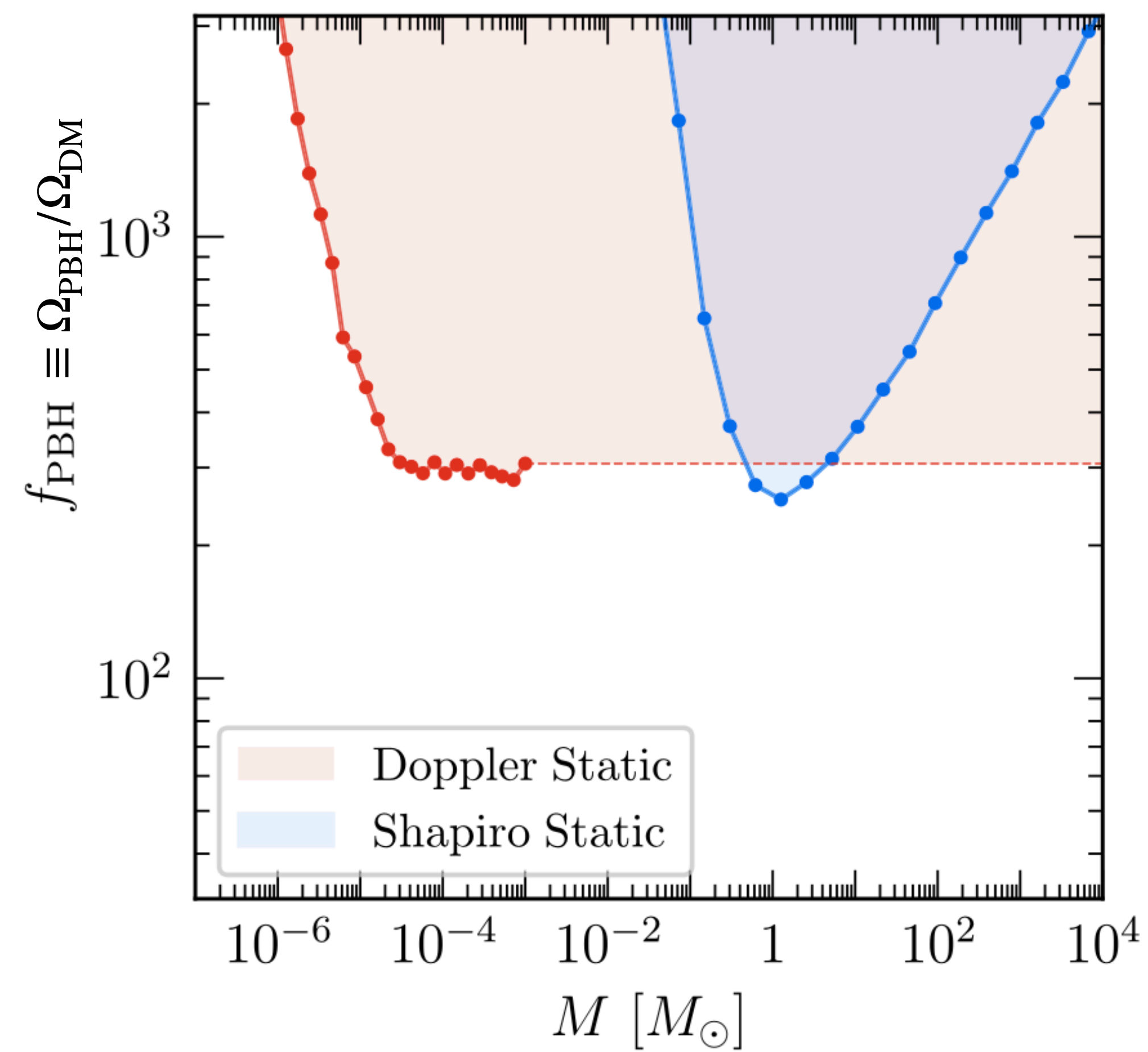
phase shift parameterised as term $\propto t^3$

$$\frac{\delta\phi_S}{\nu} = \frac{A_S}{\text{yr}^2} t^3$$

$$A_S = f(M, v, \tau, \dots)$$

dimensionless amplitude depending on the process kinematic parameters

NANOGrav 15 yr dataset



SUMMARY

- PTAs show compelling evidence for a nHz GWB
- The origin of the GWB is not yet known
- Search for anisotropies in future datasets will help discriminate
- PTAs can be used for local dark matter searches

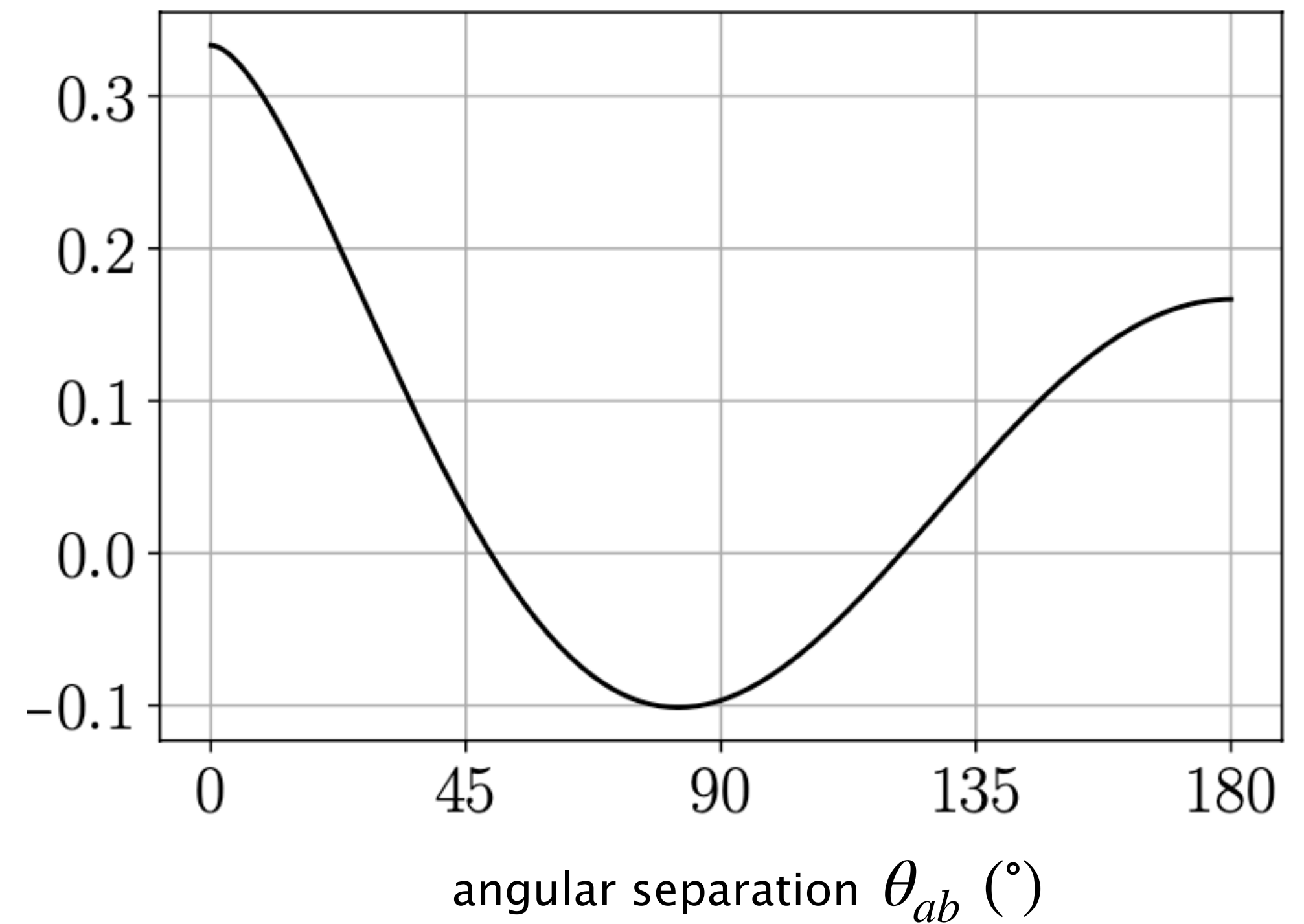
Expectation at PTAs for an isotropic, unpolarized gravitational wave background

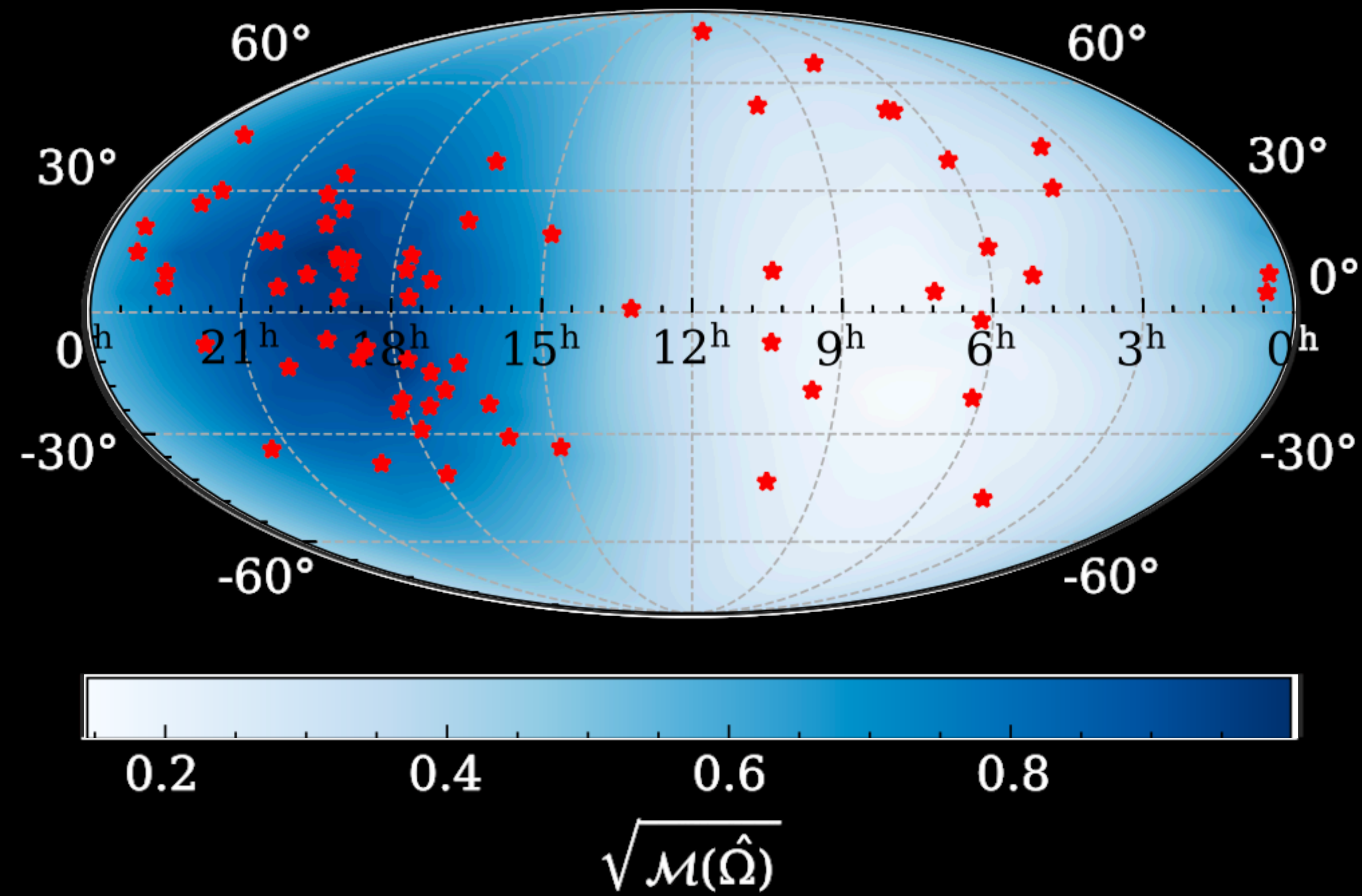
Hellings and Downs Correlations

$$\Gamma_{ab}(\zeta_{ab})$$



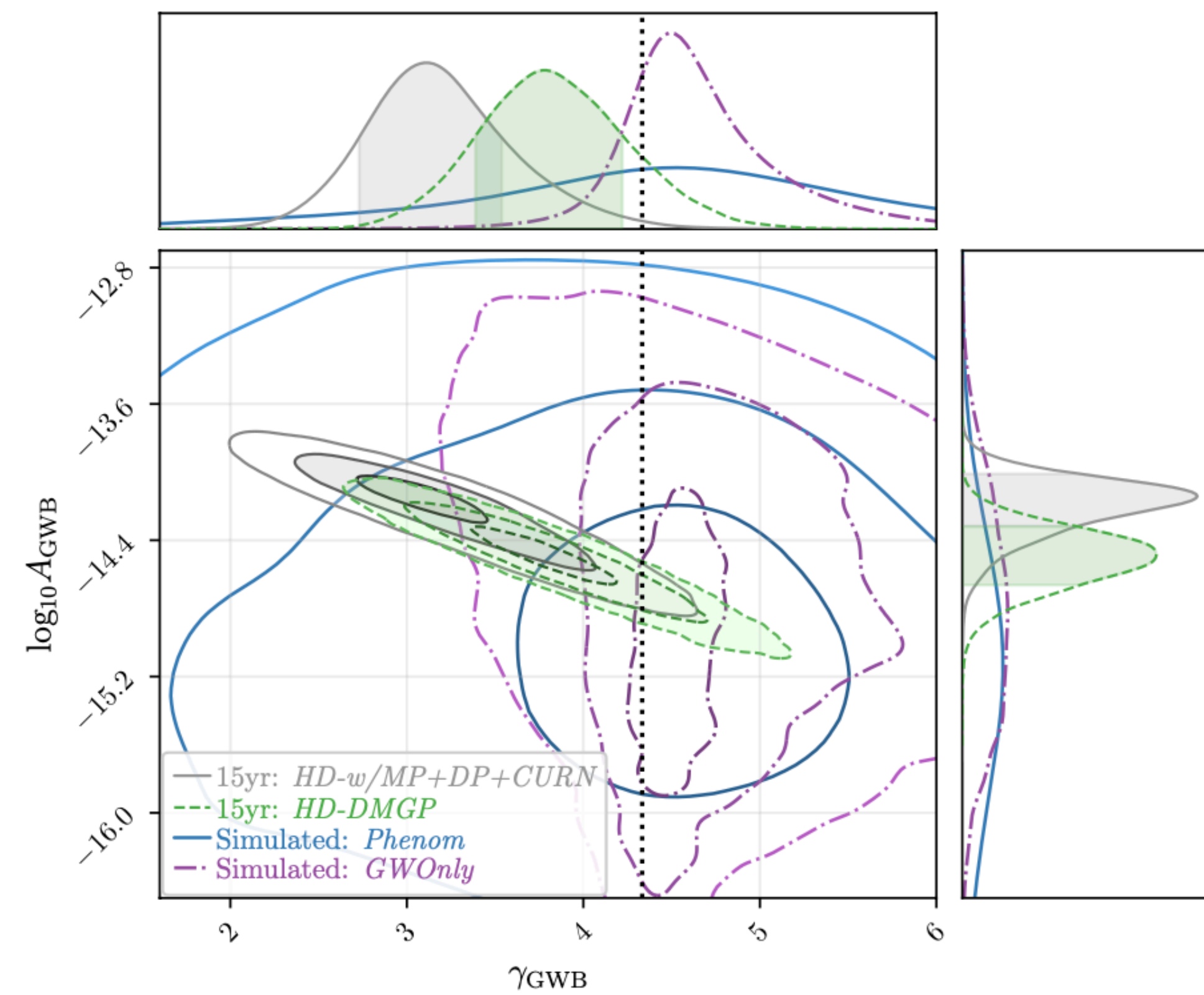
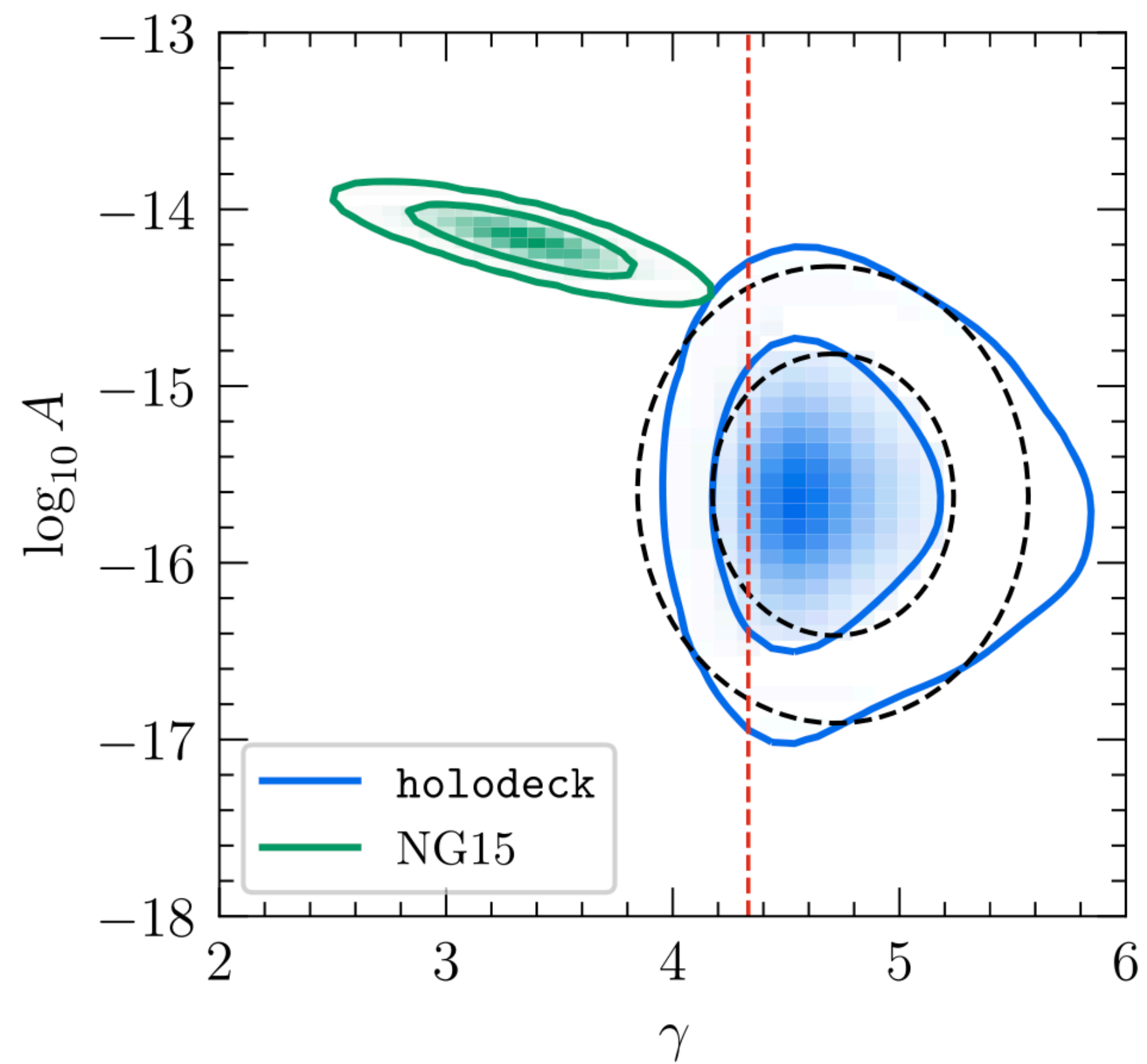
$$\Gamma(\xi_{ab}) = \frac{3}{2}x \ln(x) - \frac{1}{4}x + \frac{1}{2} + \frac{1}{2}\delta_{ab},$$
$$x = \frac{1 - \cos \xi_{ab}}{2}.$$





Current PTA sensitivity to
anisotropies

Life is not that simple...



Useful conversions to understand the plots

$$\sqrt{\Phi_{CURN}} = \sqrt{\frac{1}{12\pi^2 f^3} \frac{1}{T} h_c(f)^2}$$

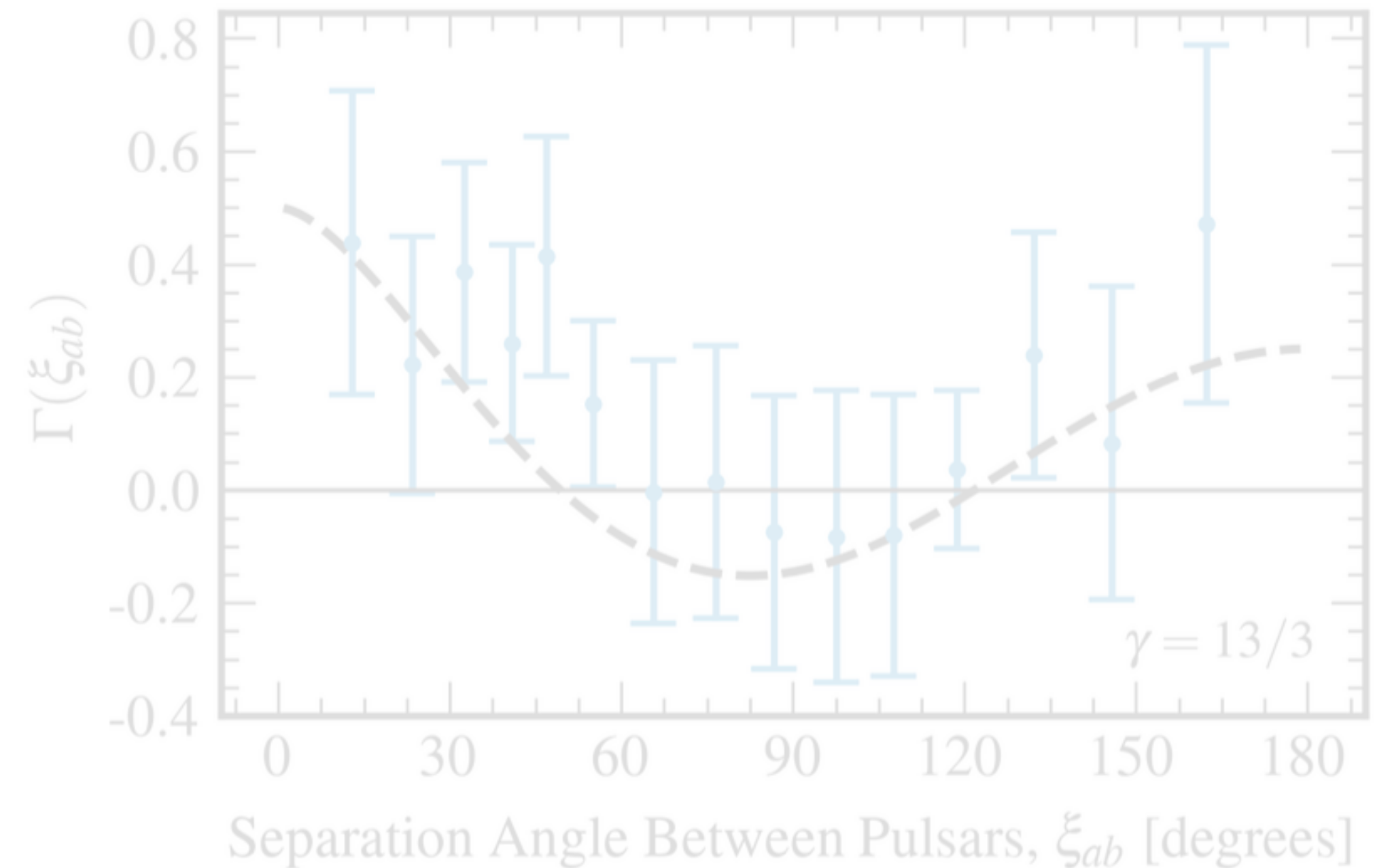
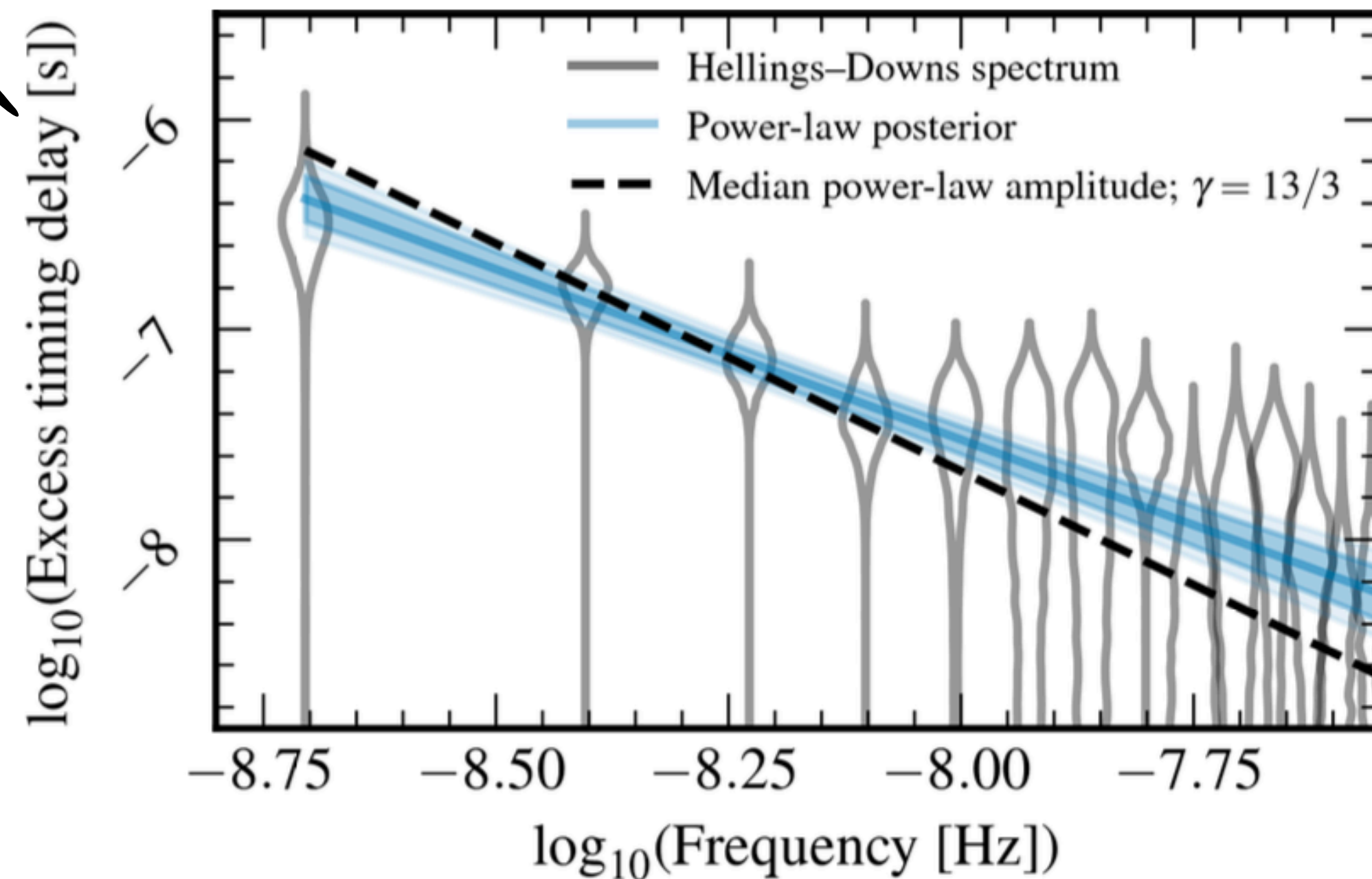
GW characteristic strain!

Parameterise:

$$h_c(f) = A \left(\frac{f}{f_{ref}} \right)^{-\alpha}$$

measured angular correlations

Agazie et al (NG) arxiv:2306.16213



Compelling evidence of Hellings-Downs correlations with false-alarm probability of $p = 10^{-3}$